

COMBUSTION ANOMALIES IN STOP-RESTART

FIRING OF HYBRID ROCKET ENGINES

Aerospace and Mechanical Sciences Report No. 945

by

M. A. Saraniero, L. H. Caveny, M. Summerfield

NASA Grant NGR 31-001-109

September 1970

Transmitted by:

Martin Summerfield Principal Investigator

1. Distribution of this document is unlimited.

Qualified requestors may obtain additional copies from the Defense Documentation Center. All others should apply to the Clearinghouse for Federal Scientific and Technical information.

Guggenheim Laboratories for the Aerospace Propulsion Sciences Department of Aerospace and Mechanical Sciences PRINCETON UNIVERSITY Princeton, New Jersey

ACKNOWLEDGEMENTS

This research was sponsored by the Office of Advanced Research and Technology, National Aeronautics and Space Administration under Research Grant NGR 31-001-109. The Program Manager for this program was Mr. Robert W. Ziem, Chief, Solid Propellant Technology, Office of Advanced Research and Technology. The Technical Manager for this program was Mr. Earl E. Van Landingham, Head, Applied Rocket Research Section, Propulsion Branch, NASA, Langley Research Center. The Contracting Officer for the program was Mr. John McDonald, Code DHC-5, Office of Grants and Research Contracts.

Mr. P. L. Stang initiated the design of the experimental apparatus. Prof. H. Isoda, while on leave from the University of Tokyo, provided advice and assistance during the development of the thermocouple techniques.

The experimental apparatus was built with the assistance of the technician group under the guidance of Mr. C. R. Felsheim. Mr. S. O. Morris instrumented the system, Mr. J. H. Semler fabricated many of the motor components, and Mr. E. R. Crosby provided the photographic coverage. Mr. J. Slade, an undergraduate, and Mr. J. Lamendola, a summer employee, assisted in the experimental firings and data reduction

Conditions of Reproduction

Reproduction, translation, publication, use and disposal in whole or in part by or for the United States Government is permitted.

An experimental investigation of the restart process of an oxygen-Plexiglas hybrid rocket demonstrated that preheating the fuel (as a consequence of a previous ignition and a temporary extinguishment) significantly increases the rate of chamber pressurization and produces regression rate overshoots during reignition. Higher rates of chamber pressurization measured during the restart transient imply faster instantaneous regression rates of the fuel during restart. Transient periods following the initial ignition and the restart after a two-second shutdown were observed for four experimental tests which were conducted at two oxidizer flow rates, 0.078 lbm/sec and 0.039 lbm/sec, and two chamber pressures, 80 psig and 320 Thermocouples made from 0.001 inch diameter chromel- · psig. alumel wire were embedded in the fuel to record subsurface temperature histories.

A mathematical model of the thermal processes in the fuel and the events that occur during an experimental firing was developed to calculate the regression rate transients. Quantitative agreement with experimental results was obtained by making nominal corrections to the calculated convective and radiative heating rates. A parametric study investigated the influence of the fuel's thermal characteristics (thermal conductivity, surface temperature, and heat of gasification) and the shut-down duration on the transient responses. The calculated results showed that instantaneous regression rate overshoots were as high as 29% when high energy fuels are reignited.

The results of this study indicate that the transient behaviors of pressure and regression rate during reignition after shut-down (the duration of which has been varied over a range of 0.9 to 4.0 sec) can be anticipated and predicted once the regression characteristics of individual fuel/oxidizer combinations have been established. Thus, extensive experimental firings of full scale rocket motors will not be required to adequately predict pressure-time histories and fuel consumption following reignition if proper attention is given to understanding the thermal distributions during shut-down periods.

TABLE OF CONTENTS

			Page
	Title Page Acknowled Abstract Table of C List of T List of F Nomenclat	gments Contents ables igures	ii iii iv vi vii x
	Chapter		
	Ι.	INTRODUCTION TO THE CONCEPT OF THE HYBRID COM- BUSTION MOTOR A. Preliminary Remarks B. Problems in Connection with Ignition, Shut-down and Restart	1
	II.	LITERATURE SURVEY A. Hybrid Combustion Models B. Time Dependent Operation	4
,	III.	THE EFFECTS OF THE THERMAL ASPECTS OF THE HYBRID FUEL ON THE SHUT-DOWN DURATION AND RESTART PROCESS A. Influence of a Preheated Fuel B. Thermal Aspects of the Shut-down Period C. Thermal Aspects to be Considered in For- mulating a Reignition Model	10
	IV.	EXPERIMENTAL APPARATUS A. Overall Gas System B. Description of the Hybrid Motor C. Timing System D. Hybrid Ignition System E. Description of the Hybrid Rocket Fuel F. Components of the Aft Housing G. Instrumentation	14
	ν.	EXPERIMENTAL RESULTS AND DISCUSSION A. Thermocouple Measurements B. Chamber Pressure Measurements C. Regression Rate Measurements D. Photographic Observations	18
	VI.	 A PARAMETRIC INVESTIGATION OF THE TRANSIENT RE- GRESSION RATE BEHAVIOR FOLLOWING A SHUT-DOWN A. Formulation and Solution of the Mathemat- ical Model Heat Conduction Equation for the Fuel The Thermal Driving Force to the Sur- face of the Fuel Solution to the Heat Conduction Equation B. Simulation of a Hybrid Motor Test Firing 	22

TABLE OF CONTENTS - cont'd.

Chapter		
VII	SUMMARY AND CONCLUSIONS WITH SUGGESTIONS FOR FUTURE WORK A. Summary and Conclusions B. Suggestions for Future Work	32
Reference Tables Figures Appendix Appendix	s A - Thermocouple Technique B - Commercially Available Experimental Apparatus and Equipment	34 37 40 83 86

DD 1473

Page

LIST OF TABLES

PageTable ICompendium of Hybrid Motor Firings37Table IIDatum Case Properties Used in the Calculations38for the 02-Plexiglas System

Table III Calculated Parameters for the Ignition and Re- 39 ignition Processes

· .

List of Figures

Figure No.	Caption	
1	Conceptual Representations of a Conventional and Inverse Hybrid Rocket Motor	
2	Simplified Hybrid Combustion Model for Flow over a Flat Plate	
3	Turbulent Boundary Layer Combustion Model	
4	Variation of Regression Rate with MP for Plexiglas	
5	Steady-State Thermal Profile in a Hybrid Rocket Fuel	
6	Transient Regression Rate Behavior during the Establishment of a Thermal Profile in a Hybrid Fuel	
7	Model of the Nonuniform Heat Distribution during Shut-down	
8	Changes in the Steady-State Thermal Profile as a Result of Shut-down and Reignition	
9	Schematic Drawing of Hybrid Motor Assembly	
10	Gas System Schematic Drawing	
11	Exploded View of the Hybrid Motor	
12	Photograph of Hybrid Motor Mounted in Test Cell	
13	Photograph of Steady-State Hybrid Motor Operation	
14	Electrical Schematic Drawing	
15	Temperature-Time Responses of Thermocouples Located 4.0 to 6.0 inches from Injector (Experimental Results for Run 17)	
16	Temperature-Time Responses of Thermocouples Located 4.0 to 6.0 inches from Injector (Experimental Results for Run 18)	
17 .	Temperature-Time Responses of Thermocouples Located 4.0 to 6.0 inches from Injector (Experimental Results for Run 22)	
18	Temperature-Time Responses of Thermocouples Located 4.0 to 6.0 inches from Injector (Experimental Results for Run 23)	

Figure No.	Caption
19	Nonsteady and Nonuniform Heat Distribution to the Fuel during the Shut-down Duration
20	Examples of the Change in Thermocouple Output as the Bead enters the Gas Phase
21	Log T_X vs. Time for Run 17 with Measured Surface Temperatures Indicated
22	Log T_X vs. Time for Run 18 with Measured Surface Temperatures Indicated
23	Log T_X vs. Time for Run 22 with Measured Surface Temperatures Indicated
24	Log T_X vs. Time for Run 23 with Measured Surface Temperatures Indicated
25	The Thermal Profiles Measured by Four Thermocouples during Run 18
26	Log T_X vs Time for Run 22 to Compare the Time to Establish Thermal Equilibrium with the Time to Establish 90% of the Equilibrium Chamber Pressure
27	Effect of a 2.0 sec Shut-down on the Pressure Transient Following Reignition (Experimental Results for Run 17)
28	Effect of a 2.0 sec Shut-down on the Pressure Transient Following Reignition (Experimental Results for Run 18)
29	Effect of a 2.0 sec Shut-down on the Pressure Transient Following Reignition (Experimental Results for Run 22)
30	Effect of a 2.0 sec Shut-down on the Pressure Transient Following Reignition (Experimental Results for Run 23)
31	Pressure-Time Histories of the Ignition and Reignition Process (Experimental Results for Run 17)
32	Pressure-Time Histories of the Ignition and Reignition Process (Experimental Results for Run 18)
33	Pressure-Time Histories of the Ignition and Reignition Process (Experimental Results for Run 22)

Figure No.	Caption
34	Pressure-Time Histories of the Ignition and Reignition Process (Experimental Results for Run 23)
35	Effects of Pressure on the Total Regression and Its Axial Dependence along the Grain
36	Flame Spreading during Hybrid Ignition
37	Flame Distribution during Steady Burning of the Hybrid Rocket
38	Schematic of the Nodal Point Array with the Hollow Cylinder
39	Effects of Shut-down and Reignition on the Calculated Steady-State Thermal Profile for the Nonradiative and Radiative Cases
40	Calculated Thermal Profiles Shown at their Respective Instantaneous Surface Locations
41	Measured and Calculated Temperature-Time Responses for Two Thermocouples
42	Effect of Shut-down Duration on the Transient Regression Rate Behavior following Reignition (Nondimensional Form)
43	Effect of Shut-down Duration on the Transient Regression Rate Behavior following Reignition
44	Calculated Transient Regression Rate Behaviors for High Energy Fuels
45	Effect of Shut-down on the Calculated Transient Regression Rate Behaviors for High Energy Fuels
46	Plexiglas Fuel Instrumented with Four Thermocouples

NOMENCLATURE

a	coefficient in burning rate law, r=apn	
A	area of the motor port	(in^2) (cm^2)
, B	linear pyrolysis law pre-exponential factor (when used in Chapter VI)	(cm/sec)
В	mass transfer number	
с _н	Stanton number	
с _н о	Stanton number in the absence of blowing	
CH/CHO	blowing coefficient	
с _р	specific heat of gas (Btu/lbmF)	(cal/gC)
Cs	heat capacity of the solid fuel	(cal/gC)
đ.	diameter	(in)
Е	activation energy	(cal/g-mole)
G	total mass flux per unit area	(lbm/in ² sec)
G _{O2}	oxygen mass flux per unit area based on initial diameter of the motor port	(lbm/in ² sec)
^h conv	convective heat transfer coefficient (Btu/ft ² sec F)	(cal/cm ² sec K)
h	enthalpy	(cal/g)
∆h	sensible enthalpy difference be- tween the flame and the wall	(cal/g)
∆h s	heat required to gasify condensed phase after vaporization temperature is achieved	(cal/g)
ΔH	effective heat of gasification of solid fuel, latent heat (Btu/lbm	n) (cal/g)
К	constant	
k	thermal conductivity	(cal/cm sec K)
Le	Lewis number	
Μ.	Mach number	
n	pressure exponent of simple burning rat	e law

Nu	Nusselt number	
P	pressure	(psi) (atm)
Pc	steady-state chamber pressure	(psi) (atm)
Pr	Prandtl number	
Q	net heat flux to the surface	(Btu/sec)
đ	heat transfer rate	(Btu/ft ² sec)
q _s	rate of energy released associated wit chemical reactions and phase changes at the gas-solid interface.	h (cal/cm ² sec)
r	radius	(cm) (in)
ŕ	regression rate (in/sec)	(cm/sec)
R	universal gas constant, 1.9867	(cal/g mole K)
Re	Reynolds number	
Rez	Reynolds number based on z	
Red	Reynolds number based on diameter	
ΔR	total regression	(in)
t	time	(sec)
t _{ign} .	igniter duration	(sec)
trun	initial firing duration	(sec)
trei	firing duration following reignition	(sec)
tshd	shut-down duration	(sec)
Т	temperature,	(C)
T s	surface temperature	(C)
Τ _f	temperature in the flame or in com- bustion zone at the fully reacted state	(C) .
u	axial velocity component	(ft/sec)
v	free stream gas velocity	(ft/sec)
Z	longitudinal coordinate in stream direction	(in)
Z	pre-exponential factor	(cal/cm ² sec)

مهاورتها والمحمد الأفاطيري المحافظ وتتعاول

05.5753.5

- xi -

2-92-23

n en nie nie the diele neurolasie windsze in diele beerde de standard die die die die die die die de der daard

Greek Symbols

			•
α_{g}	absorptivity of gas		
B	coefficient in Beer's Law		(cm ⁻¹)
S	depth in significant heating		(in)
E	emissivity		
х	thermal diffusivity		(in ² /sec)
μ	viscosity coefficient		(g/cm sec)
S	mass density	$(1bm/ft^3)$	(g/cm ³)
0	Stefan-Boltzman constant	(cal/sec c	$m^2 C^4$)
Subscript	<u>s</u>		
b	bulk		
с	solid (i.e. condensed) phase		
е	edge of boundary layer		
f'	fuel		
g	gas		
r	radiation		
s	gas-solid interface		
t	instantaneous .		
W	wall		
x	distance from initial surface of surface regression	in directi	on (in) (cm)
T.	steady-state		
0	ambient conditions deep in fue	1	
Superscripts			
*	evaluated at reference tempera by Eq. VI-9	ture defin	ed ·

- xii -

1.1

والمراجع المراجع والمتحد والمتحد والمتحد والمحتج والمتحد والمحتج والمحتج والمحتج والمحتج والمحتج والمحتج والمح

CHAPTER I

INTRODUCTION TO THE CONCEPT OF THE

HYBRID COMBUSTION MOTOR

I-A: Preliminary Remarks

Research and development programs have advanced the hybrid rocket motor state-of-the-art to the point that it is at times competitive and, in several applications, superior to either conventional liquid or solid propellant rocket motors. The application of hybrid rocket motors in advanced propulsion systems is imminent. The hybrid rocket features the advantages of a high specific impulse in a storable system, a wide range of thrust modulation, stopstart capabilities, and the safety of separate fuel and oxidizer storage. A hybrid rocket consists of a gaseous or vaporized oxidizer passing over a solid fuel. The high specific impulse is obtained through the use of special high energy ingredients in the solid fuel and by using high energy fluid oxidizers. The inverse of this configuration has been demonstrated; the inverse hybrid consists of a solid oxidizer and liquid or gaseous fuel. Conceptual representations of both the conventional and inverse hybrids are shown in Fig. 1.

The combustion processes of a hybrid rocket may be considered to consist of a reacting boundary layer with heat and mass transfer as well as chemical reactions occuring simultaneously. The combustion model for an oxidizer flowing over a flat plate of fuel is shown in Fig. 2. After ignition is achieved, the injected gaseous oxidizer and the fuel vapor (vaporized from the solid fuel by the heat feedback from the flame zone) are mixed in the boundary layer and form a turbulent diffusion flame zone.

The combustion rate of the hybrid rocket motor ingredients depends on a complex interplay of the following: (1) total mass flux of the oxidizer, (2) total mass flux of the fuel, (3) convective and diffusive mass transfer of the reactants and products in the turbulent boundary layer, (4) convective and radiative heat transfer from the flame to the surface and (5) motor and chamber configurations that may promote or retard the combustion processes. The resulting interactions that exist between fuel regression rate and fuel geometry, wherein the point regression rate is a function of the upstream regression rates and the flow conditions, posed serious problems to the development of hybrid motors. No simple regression rate expression, such as $\dot{r} = a \dot{r}^n$ as applied to conventional solid propellants, could be prescribed by previous hybrid researchers; rather, a complex combustion model is needed to predict the rate of regression of the solid phase as a function of the geometry of the motor, the flow rate of the oxidizer, the operating pressure, and the characteristics of the fuel. Because of the complexities of the combustion process, considerable difficulty is being experienced in the development of rocket motor configurations that produce uniform regression of the solid fuel.

A large portion of the hybrid rocket research has focused on the following two aspects of this surface regression problem: (a) a physical model describing the reaction in the boundary layer as a function of the physical properties of the propellant ingredients to yield a thermal driving force and (b) a mathematical model of the regression rate that encompasses the thermodynamic properties of the propellant and the fluid dynamics of the flow.¹ The development of these regression rate models has coincided with advances made in the fundamental investigations of the hybrid combustion mechanism. The results of more recent studies are reviewed in Chapter II.

I-B: Problems in Connection with Ignition, Shut-down and Restart

While researchers have made significant advances in fundamental investigations of the combustion mechanism 2,3, the development of more sophisticated, high energy propellant combinations with additives and high metal loading in polymer fuels has produced new developmental problems. Of particular interest to practical hybrid configurations are the problems that might occur during ignition, shut-down, and restart periods. They may arise as a result of one or more of the following factors:

- A high loading of metal powder used in some hybrid fuels imparts a high thermal conductivity to the fuel. Thus, more heat must be transferred to the subsurface regions to achieve ignition. As a result, pronounced delays in achieving steadystate operation are encountered.
- 2. When partially oxidized fuel charges are employed for enhancement of specific impulse or for enhancement of regression rate, the exothermic reactions induced by the burning process during the normal thrust period continue rather vigorously after oxidizer shut-off, and so sharp thrust termination becomes uncertain.

- 3. The slow regression rate characteristic of most hybrid fuels produces a thick heated layer that remains on the fuel surface after shut-off of the oxidizer at thrust termination, and this residual heat can produce continued charring, surface reaction, and/or hot fuel vapor evolution for some time afterward.
- 4. If the state of the surface is altered considerably as a result of a continued reaction and residual heating after combustion termination, the restart process may be adversely affected. For example, if a deep heated region is produced in the fuel, significant overpressures may result during the reignition transient.⁴

A complete understanding of these factors and the ability to predict their influence on the ignition and restart processes is a prerequisite to the design of a high performance, rapidly responding hybrid rocket. Overpressurization and excessive rates of pressurization during the reignition transient period may lead to increases in the weight of structural components and erratic thrust versus time histories.

In particular, the restart or reignition process requires additional considerations as a result of the thermochemical processes and thermophysical changes that may occur in the fuel binder during the shut-down period. Because both the total redistribution of heat (by convection, conduction, and radiation) throughout the motor and the degree of preheatedness of the fuel are functions of time during the shut-down duration, a formidable problem evolves in predicting the pressure transients during the restart process.

Out of this description emerge the problems that require both theoretical and experimental considerations that are essential to gain an understanding of the ignition and restart processes. Also, because of the continuing trend toward larger, more sophisticated, and more costly hybrid motors, experimental results that can be applied to practical hybrid rockets must be achieved using laboratory scale rocket motors. Therefore, a study has been conducted to determine the effects of the following factors on the restart process: (1) temperature profiles in the fuel, (2) heat redistribution to the fuel from the motor following oxidizer termination and (3) the duration of the shut-down interval.

CHAPTER II

LITERATURE SURVEY

No simple regression rate law is available to the hybrid rocket designer and analyst. Instead, previous researchers have formulated difficult to use, qualitative expressions that describe the processes occurring in the reacting boundary layer adjacent to the regressing fuel. Numerous studies in which both simple and complex approaches to the reacting boundary layer have provided various regression rate expressions. The purpose of the following discussion is not to give a complete account of all the previous hybrid regression rate studies (this has been expertly done in Ref. 1) but rather, to indicate to the reader the general direction and scope of previous research on regression rate models for hybrid rockets. In Chapter III, a discussion of the factors influencing the problems connected with shut-down and restart will be treated.

II-A: Hybrid Combustion Models

The nature of combustion within a hybrid rocket, wherein combustion is controlled by convective and radiative heat transfer, rather than a direct reaction between the oxidizer and the fuel, suggests that a combustion model could be similar to that of a turbulent diffusion flame within the boundary layer with mass addition. As a result of this similarity, the sought after regression rate law describing such a combustion model would naturally contain terms coupling it to the aerothermodynamics of the boundary layer. Attention has therefore been focused on the chemically reacting boundary layer. Lees⁵ presented a comprehensive study of convective heat transfer from reacting boundary layers by considering the influence of fuel mass addition from the wall.

Marxman and Gilbert⁶ applied Lees' generalized category of a reacting boundary layer to the combustion process in a hybrid rocket. They found that if Le=1 when the boundary layer is laminar, and if Reynold's analogy is valid when the boundary layer is turbulent, the regression rate is proportional to heat flux reaching the surface from the turbulent boundary layer adjacent to the fuel. The result was a regression rate equation based on an ideal turbulent boundary layer. The combustion model, as shown in Fig. 3, assumes a thin flame combustion layer above the solid fuel. Marxman and Gilbert's regression rate law illustrates the coupling between the fluid dynamics of the flow and the aerodynamics of the boundary layer. The complete equation is given below:*

$$i = \frac{KGR_{aa}}{f} \frac{C_{H}}{C_{H_{o}}} \frac{u_{e}}{u_{g}} \frac{sh}{sH} + \frac{\sigma \varepsilon_{w}(\varepsilon_{a}T_{e}^{+} - \alpha_{g}T_{w}^{+})}{g} SH$$
(1)

Three important parameters are included in the The first parameter is the blowing coefficient equation. ratio, CH / CHO , relating the coupling between regression rate and boundary layer flow by accounting for the partial blockage of heat transfer to the fuel surface as a result of mass addition from the fuel surface. The second parameter is the independent variable, $\Delta h/\Delta H$, coupling the regression rate equation to a thermodynamic parameter dependent on only the fuel-oxidizer combination and its gasification process. The third parameter is the velocity ratio, Ue/Ua , leading to a solution locating the flame position relative to the boundary layer thickness. Marxman and Gilbert have also included a radiation term to include any additional heat transfer as a result of radiative energy. However, during normal operating conditions, the radiative addition is likely to be small in comparison to the convective heat transfer. Applying Eq. 1, less the radiation term, to an oxygen-Plexiglas system, Marxman and Gilbert have correlated regression rates over a wide range of oxidizer mass fluxes and Reynolds numbers and obtained agreement with experimental values within a factor of two. However, as noted by Marxman and Gilbert, experimental and theoretical work is still needed to clarify the influences of the parameters in the equation.

It is convenient at this time to introduce and define the mass transfer number $B=(u_e/u_g)(\Delta h/\Delta H)$. This parameter plays a dual role in hybrid combustion. Initially, **B** may be considered as a thermodynamic constant characterized by the physical properties of the solid and the gas phase of the particular propellants. Further, it has also been shown that $B=P_{-}^{-\alpha-H}B$ is the similarity parameter of a boundary layer with mass injection. Thus, if **B** is constant along the wall, the velocity, species concentration, and enthalpy profiles are similar in the boundary layer. Since the Prandtl number of the gas is near unity, E' and B are not only similar, but also approximately equal.

*All symbols are defined in the nomenclature.

- 5 -

Thus, \boldsymbol{B} serves to couple the regression rate equation to a particular propellant combination and the fluid dynamics of the flow.¹

An empirical analysis of the regression rate equation was performed by Anderson.⁷ Anderson⁷ applied the Dittus-Boelter heat transfer equation to turbulent flow over a fuel sample in a blast tube. Using the Dittus-Boelter equation

$$Nu = \frac{h_{conv} d}{k} = K Re_{d}^{0.8} Pr^{0.4}$$
⁽²⁾

and a constant Prandtl number of unity

$$P_{\rm r} = \frac{c_{\rm P} \, \mu}{k} = 1 \tag{3}$$

the heat transfer coefficient becomes

$$h_{conv} = K R_{ed}^{\circ.8} = K \left(\frac{gdV}{V}\right)^{0.8}$$
(4)

Anderson then applies the ideal gas law to express \mathcal{J} , \mathcal{V} , and \mathcal{W} (and thus R_{ed}) in terms of temperature, T, pressure, P, and Mach Number, M. The heat transfer rate is equal to the convective heat transfer coefficient multiplied by the temperature difference, $T_f - T_w$.

$$q = h_{\text{CONV}} \left(T_{f} - T_{w} \right) = K \left(M \cdot P \right)^{0.8} \left[\frac{T_{f} - T_{w}}{T_{f}} \right]$$
(5)

The regression rate will be directly proportional to the amount of heat reaching the surface and inversely proportional to the heat required to vaporize the solid. Hence, a simplified regression rate equation is given:

$$\dot{r} = \frac{K(MP)}{\beta_{f} \Delta H} \begin{bmatrix} \frac{T_{f} - T_{w}}{T_{f} \alpha B} \end{bmatrix}$$
(6)

In summary, Anderson related the regression rate equation to Mach number, pressure, and the heat of ablation of the solid fuel. The equation is independent of the oxidizer choice, and his results for the regression rate of Plexiglas as a function of the Mach numberpressure produce, M.P, is shown in Fig. 4. Anderson believes that this practical expression, in terms of easily obtained parameters, is a good approximation over a wide range of the oxidizers and is therefore a useful engineering tool for the design of hybrid motors.

In an extension of Anderson's work, Hurt and Anderson⁸ arrived at Eq. 6 by an approach that included experimental and theoretical examination of the convective heat transfer through the laminar sublayer protion of the turbulent boundary layer. The laminar sublayer normally offers the greatest resistance to heat flow. Hurt and Anderson⁸ postulated that the ablation of the solid fuel is controlled by the thickness of the viscous sublayer and that a heat transfer coefficient with zero fuel mass addition could be chosen and multiplied by a correction factor to account for the effect of fuel mass addition at the wall.

The pressure dependence of both metalized and nonmetalized hybrid fuels has received considerable attention.9,10,11 Smoot and Price concluded9,10 that in regions of lower oxidizer flow rates the regression rates were independent of pressure and increased as the 0.8 power of specific total flow rate. However, at high flow rates, the regression rate was nearly independent of flow, but increased markedly with pressure. Thus, their expperimental results are in good agreement with those predicted by the turbulent heat transfer model for only the lower flow rates. It was therefore postulated by Smoot and Price^{9,10} that rate limiting chemical kinetic processes were the cause of the observed pressure dependence.

It is important to mention that the approaches to modeling a regression rate law, whether it is the turbulent boundary layer combustion model or the M.P correlation, have primarily been directed at the steady-state condition. That is, the regression rate is directly proportional to the heat reaching the surface. Therefore, neither approach has been extended to consider a transient period when the instantaneous regression rate is changing to approach its steady-state value. A transient regression rate may arise as a result of any of the following: (1) after ignition, the burning conditions approach the steadystate value, (2) a throttling maneuver when a rapid change in oxidizer flow is followed by an increasing or decreasing regression rate and (3) termination of the oxidizer flow when the regression rate approaches zero.

II-B: Time Dependent Operation

An analytical investigation of the time dependent transient period has been performed by Marxman, Wooldridge and Muzzy.¹² Their results are directed at only the transient period following initiation of heat to the surface (ignition). This transient period is related to the time required to achieve a steady-state thermal profile in the fuel. During this period, the regression rate is not proportional to the heat flux received at the surface since the thermal profile is developing to the steady-state conditions. During ignition transients the ratio of the heat conducted into the solid to the heat that gasifies the fuel is higher than for the steady-state conditions. As a result, regression rate equations based on steady-state thermal balances at the gas-solid interface do not apply during transient conditions. Thus, it is necessary to account for the developing thermal profiles in the fuel in order to predict the instantaneous regression rate.

Marxman, et al. continued their analysis to predict the depth of the thermal profile as a function of time. The steady-state penetration depth, S_{∞} , which the protile will reach is proportional to the thermal diffusivity and inversely proportional to the steady-state regression rate as approximated by Eq. 7.

$$S_{\infty} = 3 \frac{\chi}{\dot{r}_{\infty}}$$

The nomenclature associated with the steady-state thermal profile is shown in Fig. 5.

As a result of their analysis the transient behavior of the regression rate can be expressed as a function of the parameter $C_s(T_s-T_o)/\Delta H$ (assuming r_o/A is constant) as shown in Fig. 6. Consequently, the transient periods are greater for fuels with a low ΔH or a high vaporization temperature. However, the possibility of decreasing the transient period arises as a result of increasing T_0 , the initial fuel temperature. This is not considered by Marxman, Wooldridge and Muzzy. Although T_0 is considered the constant temperature deep in the fuel, T_0 may be increased as a result of a previous firing.

In conclusion then, the relationship established between the transient regression rate and the time to establish a thermal profile can be extended one step further.

(7)

cussed in more detail in the next chapter.

Contraction on the second

THE EFFECTS OF THE THERMAL ASPECTS OF A HYBRID FUEL ON THE SHUT-DOWN DURATION AND RESTART PROCESSES

III-A: Influence of a Preheated Fuel

The purpose of this discussion is to examine the problems that may arise in predicting the reignition process as a result of a nonuniform, nonsteady thermal profile in the fuel. A search of previous efforts revealed that insufficient emphasis has been placed on the factors influencing the reignition process.¹³ Therefore, an experimental program was undertaken to determine the influence of a preheated fuel on the reignition process by comparing the pressure-time histories and subsurface temperature measurements of the ignition and reignition transients leading to steady-state operation.

As mentioned previously, problems connected with shutdown and reignition may arise as a result of many factors. By way of review, a few of the factors are: (1) charring of the fuel as a result of residual heat in the fuel, (2) continued exothermic surface reactions after termination of oxidizer flow and (3) heated subsurface layers causing significant overpressurizations during the reignition transients. Furthermore, the ignition criteria applied to the initial ignition model may become invalid for reignition as a result of nonuniform heat transfer to the fuel during shut-down.

Therefore, for the design of advanced maneuvering missiles to include accurate, predictable, stop-start operation, emphasis must be placed on the thermal aspects influencing the shut-down period and the reignition process.

III-B: Thermal Aspects of the Shut-down Period

The following sequence of events provides a model for considering the thermal aspects that influence the shutdown period:

- 1. A hybrid rocket motor is operating at steadystate conditions.
- The flow of oxidizer into the motor ports is terminated, causing chamber pressure to decrease. As a result of this, heat transfer to the propellant surface is reduced. The net effect is extinguishment.

- 3. Heat contained in the fuel at the surface is conducted into the interior of the fuel.
- 4. The fuel may continue to receive conductive heat energy from continued exothermic reactions in a metal loaded fuel even after the cessation of oxidizer flow. Also, the flow of the hot premixed combustion gases remaining in the chamber will contribute to the convective heat transfer to the fuel.
- 5. The fuel may also receive heat in the form of radiant energy.

Since the propellant surface is cool in comparison to motor components, such as the nozzle, the redistribution of the total heat energy will proceed toward an equilibrium value. However, this redistribution of heat is both nonuniform and nonsteady. A model for the nonuniform distribution of heat transfer to the fuel is shown in Fig. 7. As a result of this redistribution, if excessive heat is conducted into the subsurface layers, a thick layer of the fuel is effected. For example, in a 70-percent lithium-fluorine hybrid system, melt layer depths of greater than 0.125 inches have been measured.¹⁴ Reignition of this type of surface allows for much of the fuel to be stripped away from the surface and not vaporized before it is ejected from the motor. This can greatly reduce combustion efficiency and may hinder or even prevent reignition.

In conclusion, the degree of heating of the fuel at a given location is dependent upon motor geometry, temperature distribution throughout the motor, characteristics of the propellant, and duration of the shut-down period.

III-C: Thermal Aspects to be Considered in Formulating A Reignition Model

There is presently no model that can be used to predict the prerequisite igniter energy or delivery rate for the reignition of a preheated hybrid fuel. The purpose of the following discussion is not to develop such a model, but rather to incorporate the results gained from a thermal study of the shut-down period into a descriptive model that can be used to predict a satisfactory reignition process in practical hybrid rockets.

As the combined convective and radiant heat transfer to the fuel during shut-down is conducted into the fuel and away from the surface (as described in the previous section), a thermal wave travels through the fuel. Since the fuel is no longer burning, i.e. surface is no longer regressing, the heating penetrates deeper into the fuel than for steady-state conditions.

The temperatures in the layers near the surface will decrease as the deeper sublayers are preheated. An example of the thermal profile established during the shutdown interval is compared to a steady-state profile in Fig. 8, curves 1 and 2 respectively. The slope and depth of curve 2 is particularly significant in the reignition model as they determine the amount of igniter energy needed to reignite the motor and also determine the transient regression rate behavior prior to the steady-state conditions.

It seems evident that if the same igniter energy as applied on the initial ignition is applied to the preheated fuel, the following sequence should occur:

- 1. Ignition delay will decrease because less energy is absorbed by the fuel before it reaches ignition conditions. The time between the onset of the ignition stimulus and the actual reignition event must be predictable to control accurate thrusting maneuvers.
- 2. As a result of the already preheated sublayers, a thermal profile (curve 3) is established which penetrates deeper into the fuel than the steadystate profile (curve 2). The preheated fuel requires less heat flux to the surface to bring the fuel to its vaporization point. Thus a greater fraction of the heat flux can be used for vaporizing the fuel. As a result, instantaneous regression rates will be higher. The transient behavior of the regression rate following reignition will rise more rapidly. If a sufficiently deep layer of fuel has been preheated, the regression rate may overshoot its steady-state value. Due to the nonuniformity of the thermal profile along the fuel, the regression rates along the fuel grain will not be uniform. The overall effect is to complicate the axial dependence of regression rate and to enhance the possibility of a local burn-out of the fuel, thereby prematurely exposing the motor case to the hot combustion gases.
- 3. If higher instantaneous regression rates are encountered, higher chamber pressures following the reignition stimulus will occur. These will result from higher rates of fuel mass addition to the combustion process. The reignition model

must, therefore, consider the degree of preheatedness of the fuel to account for the increased fuel mass addition in order to anticipate the chamber pressure within structural limits of the motor.

In summary, if the same ignition stimulus is applied to a preheated fuel, the degree of preheatedness influences the reignition process as follows: ignition will occur sooner, instantaneous regression rates will be higher, and chamber pressures will be greater. An experimental program must first determine to what extent a preheated fuel influences the restart of a hybrid motor and then investigate the effects of propellant properties, shut-down duration and igniter stimulus. An oxygen-Plexiglas hybrid motor was designed for this program and is described in Chapter IV.

and an a firm a firm and a state of the state

CHAPTER IV

EXPERIMENTAL APPARATUS

IV-A: Overall Gas System

A hybrid rocket motor was designed and constructed for experimental investigations of the ignition and restart processes. Figs. 9 and 10 show schematic drawings of the hybrid motor and overall gas system respectively. The system consists of oxygen, methane and nitrogen sources and their associated regulators and gauges. Oxygen is stored in type 1A bottles containing 244 cu. ft. at 2200 psig, and its flow is regulated from the test cell by a nitrogen dome regulator. Immediately upstream of the solenoid and flow metering orifice, an oxygen reservoir holds 15 in.³ at the system stagnation pressure. The pressure in this reservoir is registered on the oxygen reservoir gauge (0-2000 psig) in the test cell. The oxygen reservoir pressure and the orifice size are matched to achieve the desired oxidizer mass flows.

Methane is stored in type 1A bottles at 2200 psig and fed through a two stage regulator to the solenoid in the methane line. The pressure set on the second stage of the regulator and the orifice downstream of the solenoid were matched to achieve stoichiometry between the ignition gases, methane and oxygen.

The orifices used as flow metering devices were calibrated using a gas-water displacement apparatus. All the orifices tested were found to be $\pm 3\%$ of theoretically predicted flows.

Nitrogen, stored at 375 psig, was used to purge any residual burning and remove combustion gases from the system. The motor is shown in an exploded view in Fig. 11 with its components labeled.

IV-B: Description of the Hybrid Motor

The fuel consisted of a hollow cylinder of Plexiglas 10.0 inches in length and 3.0 inches in outer diameter. The initial port diameter was 1.0 inch for all experimental firings. Final port diameters were always less than 1.2 inches. Gaseous oxygen was used as the oxidizer. Experiments were conducted at two oxygen flow rates, 0.0785 lbm/sec and 0.0392 lbm/sec. Experiments were conducted over a range of steadystate chamber pressures between 60 and 700 psig. Ignition was achieved by a methane-oxygen torch igniter mounted on the forward housing. Igniter durations were varied between 50 msec and 500 msec. A plenum, or mixing chamber, located aft of the grain, was designed to receive the hot combustion products and eject them out the nozzle. The motor in Fig.12 is shown assembled and mounted for firing in the test cell.

ar eo Nordhiadachtar i middaith Bhallaichtar a Normhra bhailtean comraite an bhaile ann chadainn <u>Comra ann an</u>

A normal test firing consisted of one or two 5 to 10 sec successive firings with a predetermined shut-down duration. A photograph of the hybrid rocket in steady-state operation is shown in Figure 13.

IV-C: <u>Timing System</u>

Four automatically resetting timers were integrated on the firing console. Two, 0-30 sec, ATC timers (series 305D) provided selection of the firing duration and shut-down duration. The hybrid firing duration timer controlled power to the solenoid in the oxygen line. At the end of the firing duration, the timer would signal the solenoid to close and initiate the shut-down timer. The firing duration timer would reset automatically for a duplicate second firing duration.

Two other timers were available for setting the igniter durations. For single firing runs the #2 cam of the firing sequencer could provide the desired igniter duration. However, accurate positioning of the cam proved to be time consuming and not reproducible. For two successive firings, an initial igniter duration could be set on the sequence cam, while the restart igniter duration could be set on the igniter duration timer mounted on the console. This timer had a 0-1000 msec range. Single firing igniter durations sould also be set on the igniter duration timer. The timer controlled the opening and closing of the solenoid valve in the methane line. Figure 14 shows the electrical schematic drawing for the entire system.

IV-D: Hybrid Ignition System

The ignition of polymethylmethacrylate (commonly referred to as Plexiglas or PMM) was achieved with a methaneoxygen gas torch. The igniter system allowed both igniter mass flow rates and igniter durations to vary as a controlled experimental parameter. Methane was metered through a flow metering orifice in approximate stoichiometric proportion to the experimental oxygen flow rate. The igniter gases were then mixed and ignited in the forward housing and then injected into the motor port.

The actual ignition sequence occurred as follows: (1) two spark plugs were actuated for 500-700 msec, (2) methane valve was opened, (3) oxygen valve was opened, (4) hot igniter gases entered the motor, (5) ignition was achieved, (6) methane flow was terminated, and (7) constant oxygen flow was supplied for the duration of the firing.

IV-E: Description of the Hybrid Fuel

Plexiglas has been used extensively by other researchers, 15, 10, 17, 18, 19 before experimenting with high energy fuels. As a fuel, PMM provides a safe, practical, inexpensive laboratory model. Results obtained from this model can be used as a guide for the development of analytical models for the prediction of ignition and restart transients of other hybrid engines.

وأواله يراد أألية المتصاد والمتحافظة المتصلة فتسوك

A cylindrical shape was chosen for the motor configuration, rather than a normal flat slab model, because a cylindrical grain provides a realistic simulation to practical hybrid combustion motors. However, there are definite disadvantages inherent to the cylindrical configuration. They are: (1) photography of the burning mechanism is hampered by focusing through a burning surface and (2) measured regression rates on curved surfaces are inaccurate.*

IV-F: Components of the Aft Housing

The aft housing receives the hot combustion products from the oxidizer and Plexiglas reaction. In order to prevent high heat transfer rates to the pressure transducer housing, a high density graphite insert was inserted in the mixing chamber. The graphite insert was made in three sections. The first section, adjacent to the grain, had a slight taper to provide a gradual change from the port diameter to the mixing chamber diameter. Without this insert, complex flow patterns and undesired heating eddies would occur immediately aft of the grain.

Motor nozzles were fabricated from copper to prevent any measurable erosion in the throat section. Nozzles were designed with a slight convergent section leading to a precise throat diameter. Required pressure seals were maintained with rubber 0-rings.

IV-G: Instrumentation

n - N. CONTRACTORISTING CONTRACTORISTICS AND CONTRACTOR CONTRACTORISTICS - CONTRACTORISTICS - CONTRACTORISTICS

Chamber pressure measurements were recorded during all experimental firings. A Dynisco pressure transducer, Model PT-76, was mounted over the mixing chamber forward of the nozzle blocks. A 1/4 inch thick disk of General Electric RTV 580 rubber was bonded to the diaphram to protect the sensitive diaphragm from contact with the hot combustion gases.

The same model transducers were also placed downstream of the solenoid values in the oxygen and methane flow lines for initial tests. These pressure recordings were used to determine flow rates and opening/closing times of the solenoid values. The oxygen solenoid value fully opened and closed in 25 msec. The methane solenoid value opened to the full position in 40 msec and closed in 25 msec. The times measured for firing duration and igniter duration were measured from the time the oxygen and methane value received

* The total regression, ΔR , was measured with an accuracy of ± 0.0005 inches which gave reliable regression rate measurements to -1%.

their respective electrical signals to open. The signals to open and close the valves were recorded by the visicorder.

The RTV shielded pressure transducer had a natural frequency of 22000 cps. 20 twas reliable to a frequency-amplitude response to 8000 cps. The transducers were driven with B & F Transducer Conditioning Modules. The pressure transducers were initially calibrated using the Amthor 0-2000 type 472 Deadweight Tester. Each experimental firing was accompanied by a pressure calibration of the motor with a regulated nitrogen supply.

Some experimental firings were instrumented with fine bare wire thermocouples embedded in the fuel. These thermocouples were made from chromel-alumel wire 0.001 inches in diameter. A detailed explanation of the technique developed to embed these thermocouples will be given in Appendix I.

Both pressure signals and thermocouple outputs were fed to Dana Model 3520 D. C. Amplifiers. At the Honeywell Model 1508 Visicorder, these signals were matched with Honeywell galvonometers (Model 1650) and were recorded at a visicorder speed of 12 in/sec with timing marks every 10 msec.

Thermocouple outputs were calibrated prior to the firing by using a potentiometer to input a desired voltage to the galvonometers. Amplifiers could then be adjusted to match the desired deflection per millivolt. Most thermocouple outputs were calibrated for 1/2 inch deflection per 3 millivolts.

High speed photography, using a 16mm Wollensak Fastex camera, provided observations of the ignition and restart phenomena. High speed films can locate the point of ignition, direction of flame spreading, and the rate of flame propagation over the surface.

Films taken at 1500 and 2000 frames per second were electronically sequenced to be at operational speeds at the time of ignition. Two neon marking lights were used to coordinate recorded data and filmed observations. One mark recorded simultaneously on both the film and visicorder served as a reference mark. The second mark was an oscillating timing light set at 100 H_{m} .

CHAPTER V

EXPERIMENTAL RESULTS AND DISCUSSION

V-A: Thermocouple Measurements

Thermocouples were embedded in the Plexiglas fuel for five experimental firings. At each experimental oxidizer flow rate, 0.078 lbm/sec and 0.039 lbm/sec, we attempted to investigate two operating pressures of approximately 80 and 360 psig. Four firings, Runs 17, 18, 22, and 23, were instrumented with four thermocouples per firing, each at a different depth in the fuel (see Table I). A fifth firing, Run 19, was conducted with five thermocouples spaced axially along the grain all at the same subsurface depth. All five firings were conducted with the same firing sequence, $t_{run}=5.0$ sec, $t_{shd}=2.0$ sec, and $t_{rei}=5.0$ sec.

The temperatures recorded during Runs 17, 18, 22, and 23, were plotted versus time, in Figs. 15-18. Focusing our attention on the shut-down duration (5-7 sec), it is evident that the temperatures in the subsurface layers continued to rise after termination of the oxidizer flow. This temperature rise is caused by continued heat conduction from higher temperature regions near the surface and radiation from the hot motor components.

However, as mentioned previously, this redistribution of heat during the shut-down period may not be uniform. The results obtained from Run 19, shown in Fig. 19, give supporting evidence to the nonuniformity of the heat distribution. More clearly, Fig. 19 shows the temperatures recorded at 1.75, 6.0 and 7.5 inches from the injector face increased 5, 3 and 6 degrees C respectively during the shut-down interval, while temperatures at 4.5 inches from the injector face decreased 3 degrees C during the first second of shut-down and increased 2 degrees C during the last second of shut-down. In conclusion, the results shown in Figs. 15-19 exhibit the nonsteady and nonuniform temperatures of the subsurface layers and confirm our earlier notions of the nonsteady, nonuniform heat distribution during the shut-down interval.

Thermocouple data was also used to measure the growth of the thermal profile following ignition and reignition stimuli and during the shut-down interval. In order to experimentally model a thermal profile, three factors were considered: (1) instantaneous regression rate, \dot{r}_{t} , (2) instantaneous location of the surface and (3) accurate knowledge of the thermocouple location.

The instant that the ablating surface passes each thermocouple bead can be approximated in two ways. First, an examination of voltage output from the thermocouple reveals a smooth voltage output while in the solid region, but as the temperature sensing bead enters the molten liquid or gas phase region, the voltage output becomes wavy or rippled. Two examples taken from different firings are shown in Fig. 20. Second, plots of recorded temperature data on a log T_x vs. time scale yield a straight line in the solid region during steady-state. However, a noticeable change in the slope, normally in the form of a departure from the straight line steady-state approximation, occurs when the thermocouple records the surface temperature, T_s. Temperature measurements and the times the thermocouple beads reach the surface are shown in Figs. 21 to 24.

By combining the two previous observations an empirical regression rate can be attained and applied to determine the location of the burning surface during the entire firing. An example of several experimental thermal profiles measured during initial steady-state operation, shut-down and reignition steady-state operation are shown in Fig. 25 for Run 18. It should be noted here that the maximum error in the thermocouple placement was 0.005 cm which represents the sum of the maximum errors of each individual measurement taken. For further analysis, the profiles will be represented as smooth curves to facilitate any comparisons.

The profiles shown in Fig. 25 particularly show the overheating of the subsurface layers deeper in the fuel as the shut-down duration proceeds. The entire heat capacity of the thermal wave is free to "cook" the deeper layers of fuel as little or no heat is used for ablation. It also appears that almost immediately after the reignition stimulus is applied at t = 7.00 sec, the thermal profile established at t = 7.12 sec is deeper than the steady-state profile at t = 4. This would imply faster instantaneous regression rates because a smaller fraction of the heat is transferred to the subsurface regions of the fuel and consequently more heat is available to vaporize more fuel. The results would imply higher transient regression rates as the preheated regions are consumed.

Further comparison of the measured penetration depth of the thermal profile during initial steady-state operation with the steady-state penetration depth predicted by Marxman, Wooldridge and Muzzy¹² in Eq. 7 show close agreement. However, the measured thermal profiles following the reignition stimulus penetrate deeper into the fuel with temperatures generally exceeding corresponding steadystate profiles (Fig. 25). Furthermore, comparisons of the times to reach steadystate chamber pressure (as tabulated in Table 1) with the times to establish a steady-state thermal profile agree · very closely. The time to establish a steady-state thermal profile may be estimated graphically from a plot of log T vs. time. When the temperature-time response from a thermocouple becomes linear, a steady-state thermal profile has been established as shown in Fig. 26.

V-B: Chamber Pressure Measurements

The major purpose of the experimental investigation was to determine the influence of a preheated thermal profile on the reignition transient by comparing the pressure-time histories of the ignition and reignition transients, respectively. These comparisons of pressure-time histories were made following a two second shut-down. The pressures during reignition transients were always greater than the respective initial pressures during the ignition transient, as shown in Figs. 27-30. However, both the ignition and reignition processes approached similar steady-state pressures in the chamber as shown in Figs. 31-34.

Reignition delays were up to 15% less than ignition delays. Furthermore, the times to reach 90% of steady-state pressures following reignition were one-fourth of the initial ignition times. Both ignition delays and the times to reach 90% of steady-state chamber pressure, t the compendium given in Table 1.

V-C: Regression Rate Measurements

Average regression rates were measured on each experimental firing by measuring the change in web thickness per firing duration. Weight loss measurements were also recorded and compared with previous runs of the same durations. Regression rates were measured at nine stations, space at one inch intervals beginning from the injector face of the fuel. Only the regression rates measured at the 5th station, 5 inches from the injector face, are recorded in Table 1.

Experimental conditions precluded the measurement of instantaneous regression rates during the firing duration. From the results of the pressure measurements, we can infer that the instantaneous regression rates following reignition of a preheated fuel were faster than their respective regression rates following ignition of an ambient fuel. However, the results obtained from measuring average regression rates do provide meaningful information helpful in understanding other problems of hybrid combustion. For example, total regression, ΔR , rather than regression rate $\dot{\mathbf{r}}$, was plotted versus the distance from the injector face for three firings of the same duration, but at different operating pressures, 600, 325 and 80 psig respectively. The results in Fig. 35 show a definite xdependence on regression rate with minimum burning occurring at midstream. Referring to the same figure, (Fig. 35) the pressure effect on regression rate is also noticeable. Runs 10 and 13 at higher pressures, 600 and 325 psig respectively, have similar total regressions; Run 15 at a lower pressure, 76 psig, has a smaller total regression. These results concur with the earlier mention of the pressure dependence and the chemical kinetics.

V-D: Photographic Observation

Extensive photographic observations of the ignition and reignition processes and the flame propagation during the pressure transients were made. Although no significant difference could be detected between the ignition event and reignition event, both processes were characterized by long flame spreading durations (usually 350 msec) very similar to the long chamber filling intervals. A flame spreading interval during hybrid ignition is shown in Fig. 36.

. The most peculiar result of the photographic observation was the unusual distribution of flame intensity throughout the motor core. The high speed films show a nonsteady, almost pulsating, nonuniform flame distribution during steady-state operation. A sequence of photos in Fig. 37 show the flame. Similar pulsating flames were reported by Courtney²¹ in a double-slab 0_2 -Plexiglas system. The nonuniform intensity seen in both Figs. 36 and 37 raises the question of complete combustion along the surface of the fuel. What appears to be a region of "spotty" higher intensity burning upstream indicates that upstream burning exhausts the oxygen supply. Accordingly, the oxygen concentration in the downstream boundary layer is not sufficiently high to burn the Plexiglas at the grain surface. One hypothesis is that hot combustion products passing over the downstream regions of the grain melts the Plexiglas and carries the melt to the plenum chamber where it is burned.

CHAPTER VI

A PARAMETRIC INVESTIGATION OF THE TRANSIENT REGRESSION RATE BEHAVIOR FOLLOWING A SHUT-DOWN

In order to gain a better understanding of the transient regression rate behavior on the restart process of a hybrid rocket motor, a mathematical model was developed to calculate the instantaneous regression rates of the fuel and the temperature profiles in the fuel. The model, in the form of an extension and modification to an existing computer program²², calculates the temperature-time responses at locations corresponding to the thermocouples at subsurface depths. A discussion of the computer solution to the heat conduction equation used to compute regression rates is given in the following section. Subsequent to that section, the approach used in the parametric study will be treated, and the results presented.

VI-A: Formulation and Solution of the Mathematical Model

The mathematical model of the regressing fuel may be considered in two parts: 1) the thermal driving force to the fuel surface that gasifies, decomposes and transports the fuel into contact with the oxidizing species in the chamber and 2) the transient moving boundary heat conduction within the fuel.

VI-A.1: Heat Conduction Equation for the Fuel

The equation governing transient heat conduction within a nonstationary medium (in cylindrical coordinates) is

The terms in Eq. (VI-1) have the following physical significance:

- I Time rate of energy accumulation and temperature rise at a particular point
- II Rate of energy convection due to motion of the coordinate system

- III Energy transfer by thermal conduction in the solid
 - IV Term which accounts for effects of varying crosssectional geometry in the cylinder on energy transfer by thermal conduction
 - V Rate of radiative heat transfer to the subsurface regions

The boundary condition at the gas-solid interface for the fuel is

$$\ddot{q}_{s} + \ddot{q}_{g}(T_{s}, T_{r}, P) = k \left(\frac{\partial T}{\partial z}\right)_{c,s}$$
 (VI-2)

Where **G** is the convective heat flux from the combustion products flowing over the fuel. The quantity **G** is the rate of heat release at the gas-solid interface due to gasification of the fuel. For conventional fuels the gasification at the gas-solid interface is generally considered to be endothermic. The quantity **G** is usually expressed in one of two ways, in terms of an Arrhenius relation

$$\dot{g}_{s} = Z_{s} \exp\left(\frac{-E_{s}}{RT_{s}}\right)$$

(VI-3)

or in terms of a net energy release per unit mass converted from the condensed phase to the gas phase

$$\dot{q}_{s} = \dot{s}_{f} \Delta h_{s}$$
 (VI-4)

The regression rate at the surface is controlled by both a linear pyrolysis law,

$$\dot{r}_{b} = B_{s} \exp\left(\frac{-E_{s}}{RT_{s}}\right)$$
 (VI-5)

and a heat balance at the surface,

$$\dot{r}_{b} = \frac{\left[\lambda_{c} \left(\frac{\partial T}{\partial \chi} \right)_{c,s} - \lambda_{g} \left(\frac{\partial I}{\partial \chi} \right)_{g,s} + \beta_{r} \right]}{g_{c} \Delta h_{s}} \qquad (VI-6)$$

When the pyrolysis law (Eq. VI-5) describes the regression rate, the temperature at the gas-solid interface, T_s , increases as the heat flux to the solid-phase surface increases. As T_s increases, by Eq. (VI-5), a corresponding increase in f_b occurs. However, we chose to adopt a simpler description of the pyrolysis process, namely

$$T_s = T_s' = constant$$
 (VI-5)

The value of **b** will now be controlled by the other equations of the problem, but it will also increase as the heat flux increases.

The boundary condition for $x \rightarrow \infty$ is

$$\frac{\partial \mathbf{x}}{\partial \mathbf{x}} = \mathbf{0} \tag{VI-7}$$

the initial condition is

$$\Gamma(x,t) = T_{i} \qquad (VI-8)$$

Because of the low thermal conductivity of the fuel and the rapid surface regression, the conditions of Eq. (VI-7) is reached just 0.01 cm below the gas-solid interface.

Ignition is assumed to occur when either the surface or the interface reaches a prescribed ignition temperature.

VI-A.2: The Thermal Driving Force to the Surface of the Fuel

The reactions and transport phenomena within the boundary layer adjacent to the fuel surface, if treated analytically, would be a most formidable aerothermochemical exercise. Several investigators have attempted such analyses with only limited success.¹, 6, ¹² An examination of the bulk processes indicate that it may be both attractive and meaningful to consider the convective heat transfer from the reacting gases to the fuel using the same functional relationships as those developed for nonreacting turbulent boundary layers. There are two justifications for this: 1) the work of Anderson and Hurt⁷, ⁸ demonstrated that the surface gasification rates of hybrid fuels can be correlated in terms of emperical turbulent boundary layer parameters and 2) the analytical relationships for the thermal driving force developed by Marxman and coworkers¹, ⁶, ¹²have similar functional dependencies on free stream pressure and velocity as those dependencies on turbulent convective heating.

Accordingly, the thermal driving force used in the model was based on the empirical relationships for high speed turbulent forced convection as presented by Eckert.²³

* It should be pointed out that we understood why the simple convective boundary does not fully account for the diffusion blowing, and kinetic processes within the boundary layer. Rather it is used as a systematic means of correlating measured results within the budget limitations of the study. แล้วประวัติมีของที่ประเพณีตรีแต่ (25 จะมีแขนขร้างไทยสายประวัติมีประวัติประวัติประวัติประวัติประวัติประวัติประวัต

The following general conditions were considered to prevail: 1) the boundary layer is steady and completely turbulent, 2) an inviscid flow field, external to the boundary layer, is imposed by the internal ballistic relationships of the chamber 3) the conditions at the fuel surface and in the inviscid flow field are quasisteady and 4) the heat conduction within the fuel is unsteady. In an effort to account for the effects of temperature on the physical properties of the gases, they are evaluated at the following reference temperature

$$T^* = T_{f} + 0.5 (T_{f} - T_{s})$$

(VI-9)

(VI-10)

The convective heat transfer coefficient based on the temperature difference, $T_{\!\!f}$ - $T_{\!\!S}$, is

$$h_x = 0.0296 C_c c_p g^* V P_r^{-2/3} R_e^{*-1}$$

The factor C_c is adapted to make the calculated steadystate regression rates agree with the measured steadystate regression rates.

VI-A.3: Solution to the Heat Conduction Equation

The method of explicit finite differences and relaxation were used to solve the differential equations, Eq. (VI-1). The several terms in the solid-phase energy equation are considered by writing the derivatives in terms of the corresponding finite differences. For example,

$$\frac{\partial T}{\partial x} = \frac{T(t+\Delta t) - T(t)}{\Delta t} = \frac{\Delta T}{\Delta t} \qquad (VI-11)$$

and

$$\frac{\partial T}{\partial x} = \frac{T_{n+1} - T_{n-1}}{2 \Delta x} \qquad (VI-12)$$

or

$$\frac{\partial T}{\partial x} = \frac{\Delta T}{\Delta x}$$
(VI-13)

The differential temperature over the time interval,
$$\Delta t$$
, is

$$\Delta T = \dot{r} \left(\frac{T_{n+1} - T_{n-1}}{2 \Delta \chi} \right) \Delta t + k \left[\frac{\begin{pmatrix} \partial T \\ \partial \overline{\chi} \end{pmatrix}_{\chi + \Delta \chi / 2}}{\Delta \chi} - \begin{pmatrix} \partial T \\ \partial \overline{\chi} \end{pmatrix}_{\chi - \Delta \chi / 2} \right] \frac{\Delta t}{gC_s}$$
(VI-14)

$$+ \left[\frac{k}{r} \left(\frac{T_{n+1} - T_{n-1}}{2 \Delta \chi} \right) \right] \frac{\Delta t}{gC_s} + \frac{\Delta t}{gC_s} \beta \theta_n \exp \left(-\beta \chi \right)$$

Applying the techniques of explicit finite differences, the materials are treated as a series of elemental volumes through the cylinder. The mass of each volume is considered to be concentrated at a point referred to as a nodal point. Fig. 38 illustrates an elemental volume and its nodal point, n. The area at $x - \Delta x/2$ is A_{in} , the area at $x + \Delta x/2$ is A_{out} , and the area at x is \overline{A} . The heat transferred into the left side of the elemental volume is

$$Q_{n} = A_{n} q_{n} = -A_{n} k \left(T_{n} - T_{n-1} \right) / \Delta \chi \qquad (VI-15)$$

The heat transferred out of the right side is

The temperature T_n is the bulk temperature of the nodal volume whose heat capacity is $c_5 \mathscr{G} \bigtriangleup x$ $(A_{in} + A_{out})/2$. The heat flux at the center of the elemental volume; i.e., at the position x, is approximated as the mean heat flux

$$g(\pi) = \frac{(g_{IN} + g_{out})}{Z}$$
(VI-17)

Substituting Eqs. (VI-15) and (VI-16) into Term III of Eq. (VI-14) yields

$$\begin{bmatrix} -\frac{Q_{out}}{A_{out}} + \frac{Q_{III}}{A_{IN}} \end{bmatrix} \frac{\Delta t}{\Delta \chi_{fG}}$$
(VI-18)

where f and C_S are evaluated at T_n .

$$-\left[\frac{k}{r}\left(\frac{\frac{Pout}{Aout}-\frac{PiN}{AiN}}{2}\right)\right]\frac{\Delta t}{gS}$$

(VI-19)

Term II accounts for motion with respect to some fixed reference point. In this analysis the solid-phase material is maintained at a fixed position in space and the burning surface moves at the calculated burning rate relative to that fixed position in space. As the solid-phase layers are consumed, the nodal points within a material are repositioned so that the incremental distances between the nodal points, Δx , are equal. As the thickness of the solid phase is decreased, the number of nodal points in solid phase is decreased so as to maintain the stability of the numerical solution. Two factors control the increment and Δx : 1) the desired accuracy of the sizes ∆t solution; and, 2) the stability criterion for the finite difference equations. By decreasing the increment size Δx , the solution can be made more accurate, but the time required for the calculations increases disproportionately since the time increment **\Delta**t must also be decreased to maintain the stability of the solution. A sufficient condition for stability is to insure that the sum of all the factors multiplying the temperature at a particular nodal point is greater than or equal to zero. In the method presented here, the time increment does not vary as different materials are considered. Thus, it is sufficient to consider the stability of the critical nodal point. The numerical solution is set up so that the critical nodal point for stability is the nodal point at the surface of the fuel. Accordingly, stability is insured when

$$1 - \frac{2\Delta t}{c_s \rho \Delta k^2} \left(k + h_{conv} \Delta \chi \right) \ge 0 \qquad (VI-20)$$

Numerous check calculations were performed on all portions of the numerical solution. In several instances it was possible to compare the values calculated by the numerical solution with the values from closed-form solutions and series solutions.

VI-B: Simulation of a Hybrid Motor Test Firing

The purpose of the parametric study was threefold (1) to compare the thermal profiles in the solid fuel established during steady-state operations to those established during shut-down and reignition, (2) to compare computed

- 27 -

regression rate behaviors during restarts following different shut-down durations with the regression rate behaviors following initial ignition and (3) to evaluate and compare the thermal response of several hypothetical high energy fuels.

The initial task was to prescribe sufficient input conditions to the computer program to simulate an experimental firing. Run 18 was chosen as the datum case for comparison purposes, and the sequence that follows outlines the approach used to simulate the 0_Plexiglas system.

- 1. The physical properties of the Plexiglas fuel, the properties of the chamber gases and the grain dimensions were input to the program. No parameter was input to the initial datum case to consider the heating of subsurface layers by radiation. However, as further discussed in Appendix I, our experiments showed that radiant heating to the subsurface layers of the Plexiglas fuel was significant and must be accounted for in future investigations.
- 2. The gas-torch igniter was simulated by applying a heat flux to the surface of the fuel in a step function initiated at t = 0.0. After 100 m sec, the step function was followed by a decreasing ramp function to zero at 300 mrec. The magnitude of the igniter heat flux was fixed at a value that produced ignition delays that agreed approximately with the experimental results.
- 3. The pressure-time history recorded during Run 18 was also an input to the program. From the pressure-time history, the program calculated an effective convective heat transfer coefficient, h, and then a heat flux to the surface, Q. The heat flux to the surface determined the regression rate. Small corrections were made to computed convection coefficients to make the regression rates agree with experimental results. This sequence summarizes the inputs to the datum case; a complete list of input parameters is given in Table II.

VI-C: Calculated Results for a Plexiglas Fuel

The calculated results of the datum case partially simulated the experimental results of Run 18. The computed steady-state regression rates were within 1% of the measured average regression rate. Ignition delays of 0.077 sec were computed and were approximately equal to those recorded and photographed during the experiments. However, as was indicated by a comparison of measured and calculated thermocouple responses, radiant heating to the subsurface regions should be included in the solution to the heat conduction equation.

An important advantage of the computer simulation was that thermal responses can be compared for a range of fuel properties. The thermal profiles for the nonradiative datum case are presented in two forms, Figs. 39a and 40a. In Fig. 39a, the results of the passage of a thermal wave penetrating through the fuel during shut-down to preheat the sublayers above their respective steady-state temperatures is clearly illustrated. Curve 1 represents the steady-state profile at t = 4.0 sec. Superimposed on the same axis, curve 2 is the thermal profile 2.0 seconds after shut-down just prior to restart. The temperatures in the layers adjacent to the surface have diminished slightly; however, the thermal wave has preheated the subsurface layers considerably. Curve 3 is the thermal profile at t = 9.0 sec, less than two seconds after reignition. This thermal profile is slowly approaching its original steadystate condition. In Fig. 40a, the same profiles are shown at their instantaneous surface locations. At t = 5.0sec, the reaction stops and the surface ceases to ablate. Therefore, the profiles at t = 6.0 and t = 7.0 sec are shown at the same surface.

The results obtained from the temperature-time histories at the thermocouple locations did not agree with the experimental results of Run 18. The computed temperature-time histories lagged in response to ignition and were below the experimental values recorded. It was concluded that the poor agreement resulted from considering only convective heating in the computed temperatures, while the experimental results were obtained by sensing convective and radiative heat to the subsurface layers.

Therefore, two additional heating relationships were considered to account for the subsurface radiant heating. They were

(1) a radiative heat flux to the fuel

$$g_r = A_{fs} - (T_f^4 - T_w^4)$$

and

(2) subsurface heating by radiation using Beer's Law^{24}

 $g_x = g_r \exp(-\beta x)$

This introduced two additional parameters to the study, the overall radiation interchange factor, A_{fs} , and the Beers' Law parameter, β .

With these two appropriate values added, Case I becomes the modified datum case considering a radiative system. The temperature-time responses of the locations corresponding to the thermocouples were in reasonable agreement. A comparison of the measured and computed temperature-time responses for two thermocouples is shown in Fig. 41. The lack of better agreement between the two temperature-time responses was probably due to the uncertainty of the true location of each thermocouple and unknowns associated with radiation effects. Further considerations of the thermocouple technique is given in Appendix I.

A comparison of the thermal profiles for the nonradiative datum case and the radiative Case I is shown in Figs. 39 and 40. As already described, Figs. 39a and 40a are for the nonradiative datum case, while Figs. 39b and 40b show the effects of radiation on the system. A faster regression rate is noticeable by the more advanced positions of the instantaneous surfaces in Fig. 40b. Also, the chemical reaction in the system does not stop at t = 5.0 sec. Instead, a slow continuous surface reaction occurs causing a low regression rate during the shut-down period. As a result, additional heat is transferred to the fuel during shut-down, and, as compared with the thermal profiles in Fig. 40a, profiles now have less of a slope and more heat stored in the fuel.

The results of Case I were considered an accurate representation of the experimental firing. The major purpose of the parametric study could now be accomplished: to compare the calculated instantaneous regression rate behaviors on restarts following varied shut-down durations. Three shut-down durations were considered: Case I with a 2.0 sec shut-down, Case II with a 0.9 sec shut-down and Case III with a 4.0 sec shut-down. The instantaneous regression rate behaviors are presented in two graphical forms.

First, in Fig. 42, a nondimensional form similar to that used by Marxman, Wooldridge and Muzzy in Ref. 12, the transient regression rate behaviors for Cases I, II and III are compared. Results indicate that increasing shut-down duration (up to an undetermined time) increases the degree of overshoot. Second, in Fig. 43, if the results are presented in the dimensions of regression rate and time, the results are more obvious. The steady-state regression rates for the radiative and nonradiative systems are shown in dashed and solid lines respectively. The regression rate tail-off associated with the drop in chamber pressure should lead to extinction. However, slow burning is continued during the shut-down. The restart pressurizations were initiated at 5.9, 7.0 and 9.0 sec for Cases I, II, and III respectively. The computed transient regression rates are plotted for comparisons. The regression rate overshoots are now obvious and are clearly increasing with increased shut-down durations. The restart of the nonradiative datum case is also plotted for comparison. Results such as ignition delay and the time to reach 90% of initial steady-state regression rate on restart are tabulated for comparison in Table III. It should be noted that the time to reach 90% of the initial regression rate on restart following any shut-down duration is nearly one-fifth of the time to reach 90% of the steady-state regression rate on ignition. That is, steadystate regression rates on reignition are achieved five times as fast as on initial ignition.

VI-D: Hypothetical High Energy Fuel

The physical properties of a hypothetical fuel, whose physical ingredients were similar to a fuel consisting of 50% Boron, 20% ammonium perchlorate, AP, and 30% binder, were substituted for the Plexiglas properties for a series of calculations to determine the regression rate overshoots that may occur in a practical high energy fuel. The fuel was assumed to be opaque to thermal radiation. Surface temperature and latent heat were varied for three cases, and the values for each case is listed in Table III (Case IV, V and VI). The transient regression rates are plotted in Fig. 44. The regression rate overshoots are increased as the latent heats are decreased and the surface temperatures increased.

An additional case, similar to Case V, was considered with a 4.0 sec shut-down duration. As all the other initial parameters were equal, the regression rate transients following ignition were similar. However, the regression rate behavior following the 2.0 sec and 4.0 sec shut-downs were different and are compared in Fig. 45. The overshoot following the 2.0 sec shut-down was 18% greater than steadystate, whereas the overshoot following a 4.0 sec shut-down was 20% greater.

CHAPTER VII

SUMMARY AND CONCLUSIONS WITH SUGGESTIONS FOR FUTURE WORK

VII-A: Summary and Conclusions

From an analytical study of the shut-down and restart processes, it was concluded that if proper attention is focused on the inter-relationships between: (1) the nonsteady thermal state of the fuel during shut-down, (2) the instantaneous regression rate behaviors following a shutdown duration and (3) the pressure transients following reignition, the pressure-time histories and fuel consumption following reignition may be anticipated. Experimental results have provided conclusive evidence that such relations between the thermal state of the fuel, the instantaneous regression rate, and the transient chamber pressure do exist.

The thermocouple probes, especially fabricated for this study, provided accurate subsurface temperature histories and consistent surface temperature measurements. Thermocouple studies showed that a nonsteady, nonuniform thermal state exists in the fuel during shut-down and a deeper thermal profile develops. Chamber pressures measured during the transient and chamber filling interval following reignition of a preheated fuel have everywhere exceeded their respective initial ignition transient pressures. From these experimental results, we can infer that the higher chamber pressures are a result of the higher rates of fuel mass addition, and therefore faster instantaneous regression rates, caused by the preheating of the fuel.

However, experimental conditions have precluded any measurement of the instantaneous regression rates to verify our inference. Therefore, an additional parametric study, using a computer to simulate an experimental firing of the O2-Plexiglas hybrid rocket motor, was performed to determine the effects of preheating and shut-down on instantaneous regression rate behavior. The computer results were conclusive and as expected; the calculated restart regression rate transients had overshoots as large as 21% above steady-state values. The times to reach 90% of equilibrium chamber conditions following reignition were one-fourth as long as the times on initial ignition. The regression rate overshoots increased as the shut-down duration was increased for the shut-down intervals investigated (0.9 sec to 4.0 sec.). The same computer simulation was applied to three hypothetical high energy fuels to determine the influence of the shut-down duration on reignition regression rate transients in a practical hybrid fuel. The results were similar to those obtained from the PMM study.

The combined results from the parametric computer study and the experimental O₂-Plexiglas motor study proved that radiant heating to the subsurface layers is not negligible and cannot be ignored as previous researchers have assumed. Radiant heating to the subsurface layers of the fuel must be considered in the heat conduction equation in order for experimental results to agree with calculated predictions. The effects of radiation in the PMM system increased the instantaneous regression rates and increased the depths of the thermal profiles in the fuel.

In conclusion, the effects of a preheated fuel (as a consequence of a previous ignition and a temporary shutdown) will greatly influence the chamber filling interval and the instantaneous regression rates following reignition. Therefore, attention must be focused on the overall thermal distribution during shut-down in order to predict satisfactory pressure-time histories and design the reliable structural components capable of withstanding the excessive rates of pressurization following reignition.

VII-B: Suggestions for Future Work

Future experimental work should be directed at:

- determining the upper limit of the shut-down duration needed to eliminate the influence of the preheated fuel,
- 2. extending the computer simulation to predict the time when the preheated fuel no longer contributes to an overshoot on reignition,
- investigating the minimum time for steady chamber conditions to be regained following step changes in the oxidizer flow and chamber pressure, thereby simulating throttling maneuvers,
- 4. incorporating the experimental results from a simple polymeric fuel (Plexiglas) and the computer predictions for a metal loaded fuel (for example, 40% Al, 60% Plexiglas) to predict the restart process for a metal loaded hybrid rocket motor.

REFERENCES

- 1. Marxman, G. A. and Wooldridge, C. E., "Research on the Combustion Mechanism of Hybrid Rockets," <u>Advances in</u> <u>Tactical Rocket Propulsion</u>, AGARD CP No. 1, Aug. 1968, pp. 421-478.
- Barrère, M. and Moutet, A., "Résultats Récents Obtenus sur les Systèmes Hybrides ou à Lithergols," ONERA, Chatillon, France, Oct. 1966.
- Moutet, A. and Barrère, M., "Contribution a l'Étude de la Combustion dans les Fusées à Lithergol on Hybrides," <u>Advances in Aeronautical Sciences</u>, Pergamon Press, New York, 1961, p. 465.
- Summerfield, Martin, <u>Design Principles for Predicting</u> <u>Start-Stop Performance of Solid and Hybrid Rocket Mot-</u> <u>ors</u>, (NASA Grant NGR 31-001-109), Princeton University, Department of Aerospace and Mechanical Sciences, May 1970, pp. 15-20, (a proposal for research, unpublished).
- 5. Lees, L., "Combustion and Propulsion," <u>Third AGARD</u> <u>Colloquium</u>, Pergamon Press, New York, 1958, p. 451.
- 6. Marxman, G. and Gilbert, M., "Turbulent Boundary Layer Combustion in the Hybrid Rocket, "<u>Ninth Symposium on</u> Combustion, Academic Press, New York, 1963, p.371.
- 7. Anderson, Stanley E., "A Discussion of the Parameters Affecting the Burning Rate of Hybrid Fuels," Rohm and Haas, Huntsville, Ala., Second ARPA Hybrid Meeting, Jan., 1963.
- 8. Hurt, L. J. and Anderson, S. E., "Hydrodynamic Factors Influencing the Combustion of Hybrid Propulsion System," <u>Chemical Engineering Progress Symposium Series</u> No. 61, Vol. 62.
- 9. Smoot, L. D. and Price, C. F., "Regression Rates of Nonmetalized Hybrid Fuel Systems," <u>AIAA Journal</u>, Vol. 3, No. 8, Aug. 1965, pp. 1408-1413.
- Smoot, L. D. and Price, C. F., "Regression Rates of Metalized Hybrid Fuel Systems," <u>AIAA Journal</u>, Vol. 4, No. 5, May 1966, pp. 910-915.
- 11. Kosdon, F. A. and Williams, F. A., "Pressure Dependence of Nonmetalized Hybrid Fuel Regression Rates," <u>AIAA</u> Journal, Vol. 5, No. 4, April 1967, pp. 774-778.
- 12. Marxman, G. A., Wooldridge, C. E. and Muzzy, R. J., "Fundamentals of Hybrid Boundary-Layer Combustion," <u>Heterogeneous Combustion, Progress in Astronautics and</u> <u>Aeronautics</u>, Vol. 15, Academic Press, New York 1964, p. 485.

- 34 -

- 13. Connaughton, J. W., Wilson, B. F. and Wharton, W. W., "An Experimental Study of Hypergolic Ignition and Restart in a Unique Hybrid Window Motor," AIAA Paper, No. 66-69, Jan. 1966.
- 14. Drew, Walter B., "An Analytical Method for Determining the Melt Layer Thickness and Regression Rates for a Hybrid or Tribrid Rocket Motor," NASA TN-D-5699, Langley Research Center, Hampton, Va., May 1970.
- 15. McAlevy, R. F. and Lee, S. L., "The Linear Pyrolysis of PMM," Technical Report ME-RT66006, Stevens Institute of Technology, Hoboken, N. J., July 1966.
- 16. Zabelka, R. J. and Brink, D. F., "Studies in Hybrid Combustion," (NOTS TP 3550, NAWWEPS 8541), Naval Ordnance Test Station, April 24, 1968, pp. 19-29, 92, 202, 207-208.
- Rabinovitch, B., "Regression Rates and the Kinetics of Polymer Degradation," <u>Tenth Symposium (International)</u> on Combustion, Cambridge, England, 1965, pp. 1395-1402.
- 18. Fineman, Stephen, "Some Analytical Considerations of the Hybrid Rocket Combustion Problem," Princeton University, Department of Aerospace and Mechanical Sciences, MSE Thesis, 1962.
- 19. Houser, T. J. and Peck, M. V., "Research in Hybrid Combustion," <u>Heterogeneous Combustion, Progress in</u> <u>Astronautics and Aeronautics</u>, Vol. 15, Academic Press, New York, 1964, p. 559.
- 20. Most, William J., "Ignition Transient Prediction and Control of Solid Propellant Rocket Motors," Princeton University, Department of Aerospace and Mechanical Sciences, Ph.D. Thesis, June 1969, p. 43.
- 21. Courtney, W. G., Kineyko, W. R. and Dawson, B. E., "Combustion During Perpendicular Flow," <u>Heterogeneous</u> <u>Combustion, Progress in Astronautics and Aeronautics</u>, Vol. 15, Academic Press, New York, 1964, p. 523.
- 22. Caveny, L. H., "Generalized Moving Boundary Heat Conduction Solution - A Fortran IV Program", Princeton University, Department of Aerospace and Mechanical Science, in preparation.
- 23. Eckert, E. R. C., "Survey on Heat Transfer at High Speeds", University of Minnesota, December 1961.

Benkenhalder Sellana hande anderschelse Belleville ander die bester die die Bester aus die bester Bester die Bester die

- 24. Hottel, H. C. and Sarofim, A. F., <u>Radiative Transfer</u>, McGraw-Hill, New York, 1967, pp. 199-235.
- 25. Brewer, W. D., "Effect of Thermocouple Wire Size and Configuration on Interval Temperature Measurements in a Charring Ablator", <u>NASA TN-D-3812</u>, Langley Research Center, Va., March 1967.
- 26. Strittmater, R. C., and Holmaes, H. E., and Watermeier, L. A., "Lead Loss Problem for a Thermocouple Imbedded in a Burning Propellant", Journal of Spacecraft and Rockets, Vol. 3, No. 8, August 1966, pp. 1302-1303.

		- 37 -		
	Thermocouple Depths (in) (+ 0.002 inches)	0.025/0.035/0.060/0.075 0.040/0.070/0.100/0.130 all at 0.125		0.018/0.035/0.065/0.090 0.020/0.030/0.040/0.055
	r ₅ x1 0 ² (in∕sec)	1.19 1.21 2.37 1.39 1.20 1.090 0.828	0。946 0.687	
auc	Ignition Delay (sec)	0.075 0.070 0.075 0.070 0.0750 0.0750 0.0750 0.0750 0.0750000000000	0.085 0.080	0,085 0,070) 0,050) (0,050)
	t_9p_c (sec)	1.470 1.150 1.150 1.150 1.3200 1.3200 1.3000 1.32000 1.32000 1.32000 1.32000000000000000000000000000000000000	2.71 3.36	(1250) 285 (0.72)
	P _C psig	600 645 650 675 620 670 670 670 600 77 77 77 70 70 70 (3350) (310) Flux = 0	640 600	(385) (70) (70)
~2 F ± 40	t _{rei} (sec)	0 2 0 0 2		5°0 5
	t shđ (sec)	2.0 2.0 2.0 were at	•	2.0
1	t (sec)	20 v v v v v v v v v v v v v v v v v v v	5.0	5.0
	t _{ign} (sec)	0.500 0.100 0.100 0.050 0.100 0.250 0.250 0.100 0.100 0.100 0.050 0.050 0.050 0.050 0.050 0.050 0.050 0.050 0.050	0.100 0.050	0.100 0.050
	Run #		20 21	22 23

Table I

Table II

Datum Case Properties Used in the Calculations for the O2-Plexiglas System

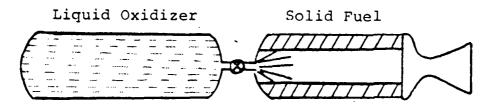
Thermal Conductivity, 🍌 cal/cm K sec	0.001213
Specific Heat of gas, c, cal/g-c	0.35
Density, f_{f} , g/cm^3	1.683
Thermal Diffusivity, X , cm ² /sec	0.002325
Ratio of Specific Heats, 🖌 ,	1.2
Average Molecular Weight, combustion gases g/g -mole	28.0
Initial Temperature, T _O , C	21.1
Throat Diameter of Nozzle, d _t , cm	0.434
Diameter of Motor Port d, cm	2.54
Maximum Chamber Pressure, P _c , atmos	24.80
Surface, Temperature, T _s , C	372.0
Latent Heat, Δ H, cal/g	-351.0
Igniter Heat Flux, Q, cal/cm ² sec	13.65
Flame Temperature, T _f , C	2732.0

Table III

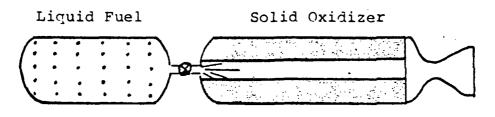
Calculated Parameters for the Ignition and Reignition Processes

	Datum	Case I	Case II	Case III		Case V	Case VI	Case VII
Fuel	PMM	PMM	PMM	PMM		B o ron	Boron	B <mark>o</mark> ron
Surface Temperature, T _S , C	372	372	372 ·	372		372	500	372
Latent Heat, AH, cal/g	351	351	351	351	351	100	100	100
Radiation Considered YES/NO	NO	YES	YES	YES	NO	N0	N0	N0
Shut-down Duration, t _s hd, sec	2.0	2.0	0.9	4.0	2.0	2.0	2.0	4.0
Ignition Delay sec,	0.078	0.075	0.075	0.075		0.516	0.864	0.516
t at t = 4.95 sec cm/sec	0.0271	0.0306	0.0315	0.0306		0.044	0.0311	0.044
Time to 90% t (lst IGN) t ₂ , sec	1.75	1.55	2.05	1.55		2.0	1.9	2.0
Reignition Delay (sec) Maximum r _t on Restart cm/sec	0.0313	0.0343	0.0358	0.0372		0.2 0.052	0.3 0.0401	0.2 0.0539
Regression Rate Overshoot, %	15.0	12.0	14.0	21.6		18.1	29 . 0	20.0
Time to 90% of Initial t (Restart) t ₂ , sec	0.50	0.45	0.45	0.40		0.4	0.45	0.38
Decrease in Ignition Interval t_2/t_1	0.286	0 . 29	0.22	0.258		0.20	0.236	0.19

- 39 -



Conventional Hybrid Rocket Motor



- Inverse Hybrid Rocket Motor
- Fig. 1 Conceptual Representation of a Conventional and an Inverse Hybrid Rocket Motor

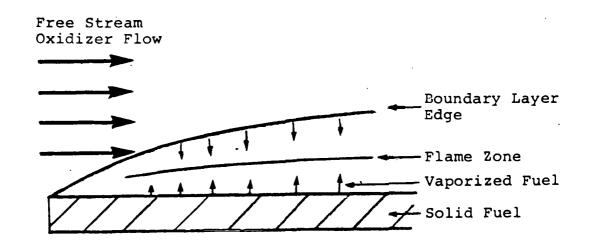


Fig. 2 Simplified Hybrid Combustion Model for Flow over a Flat Plate

R ool

6092

iko yang dikakeran kenda Pederanan di Kenderan di Kenderan.

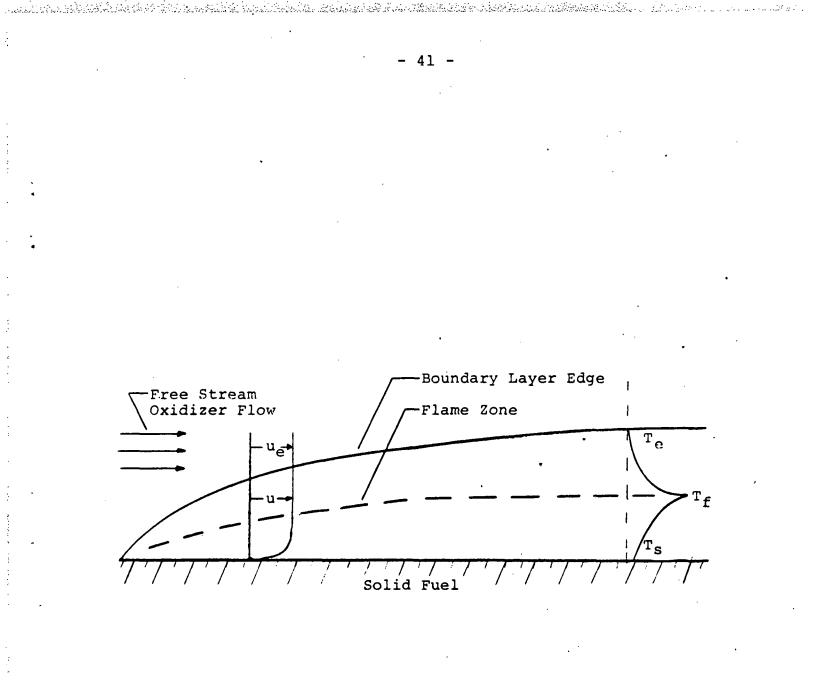
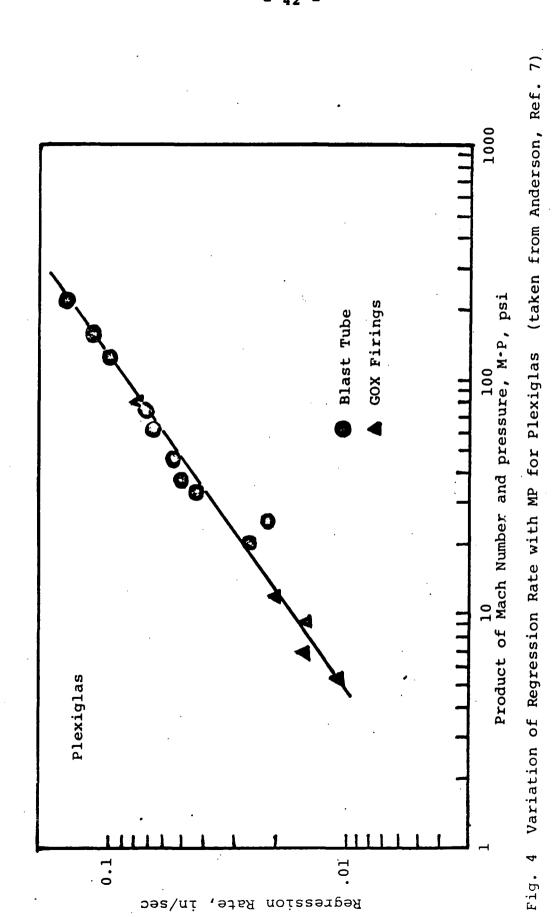
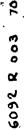


Fig. 3 Turbulent Boundary Layer Combustion Model (taken from Marxman and Gilbert, Ref. 6)



42 -



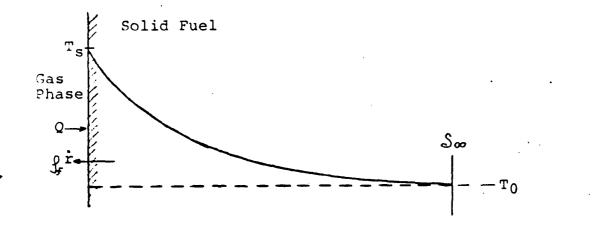


Fig. 5 Steady-State Thermal Profile in a Hybrid Rocket Fuel

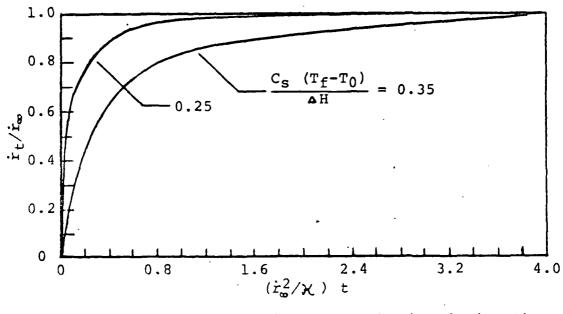


Fig. 6 Transient Regression Rate Behavior during the Establishment of a Thermal Profile in a Hybrid Fuel (taken from Marxman et al., Ref. 12)

- 43 -

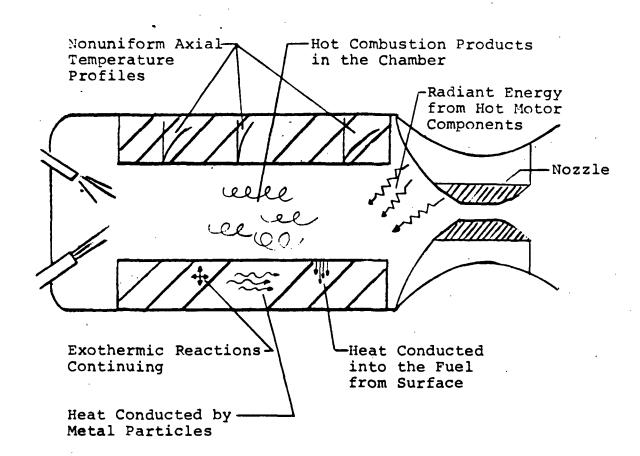
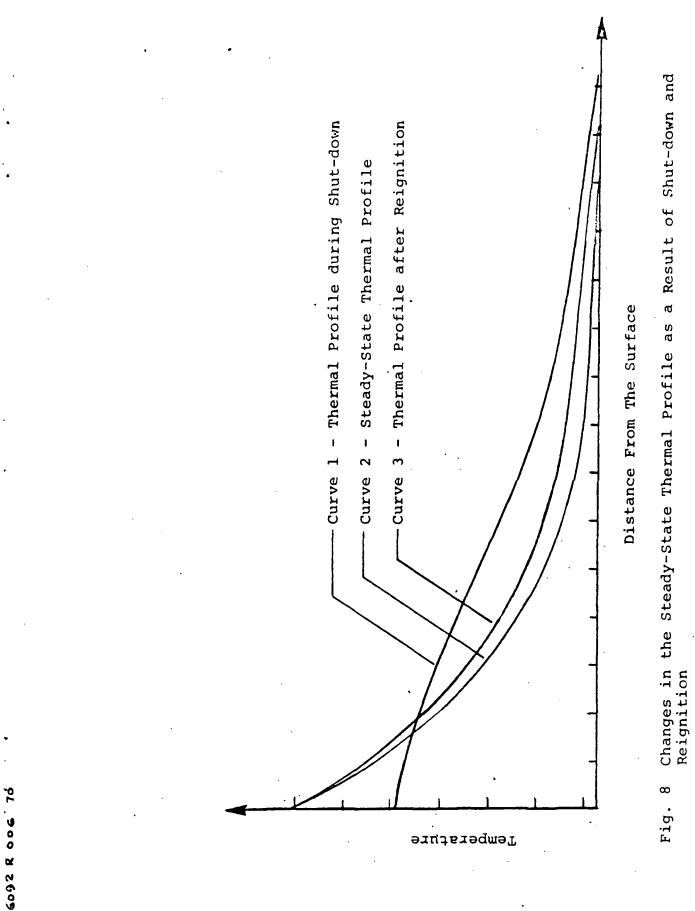


Fig. 7 Model of the Nonuniform Heat Distribution during Shut-down

10

- 44 -

CONTRACTOR STATES



- 45 -

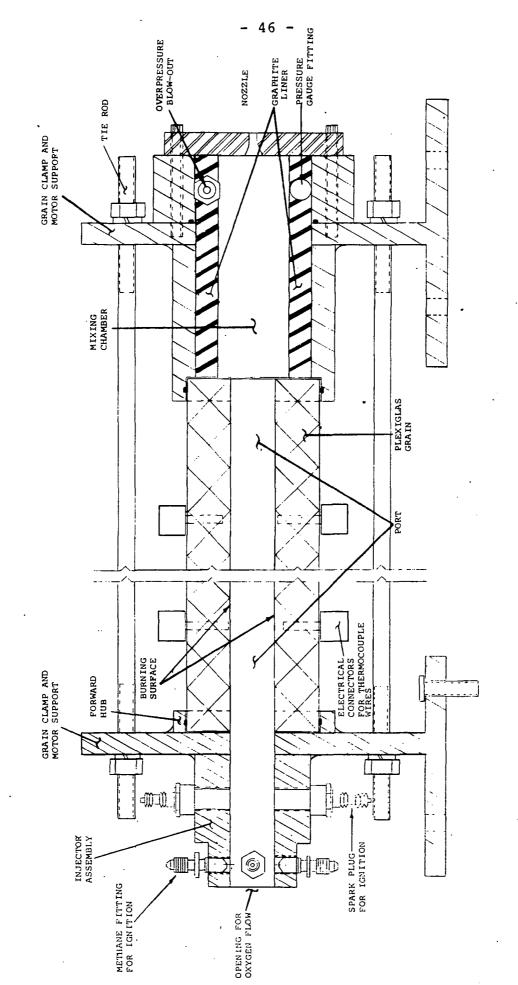
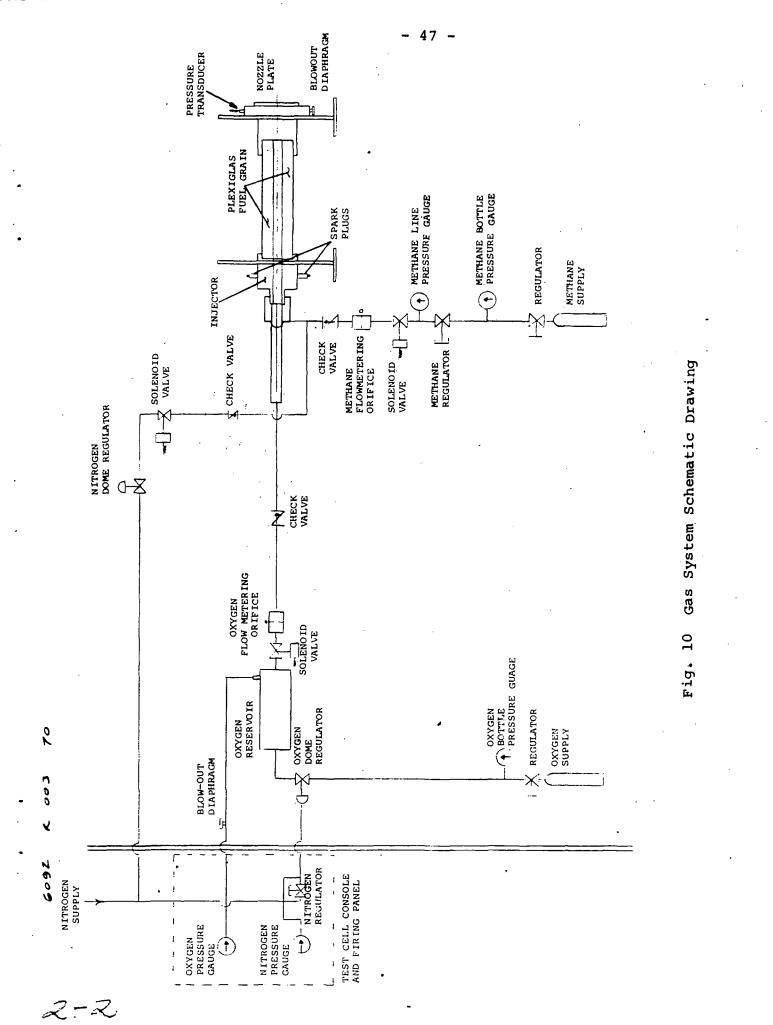
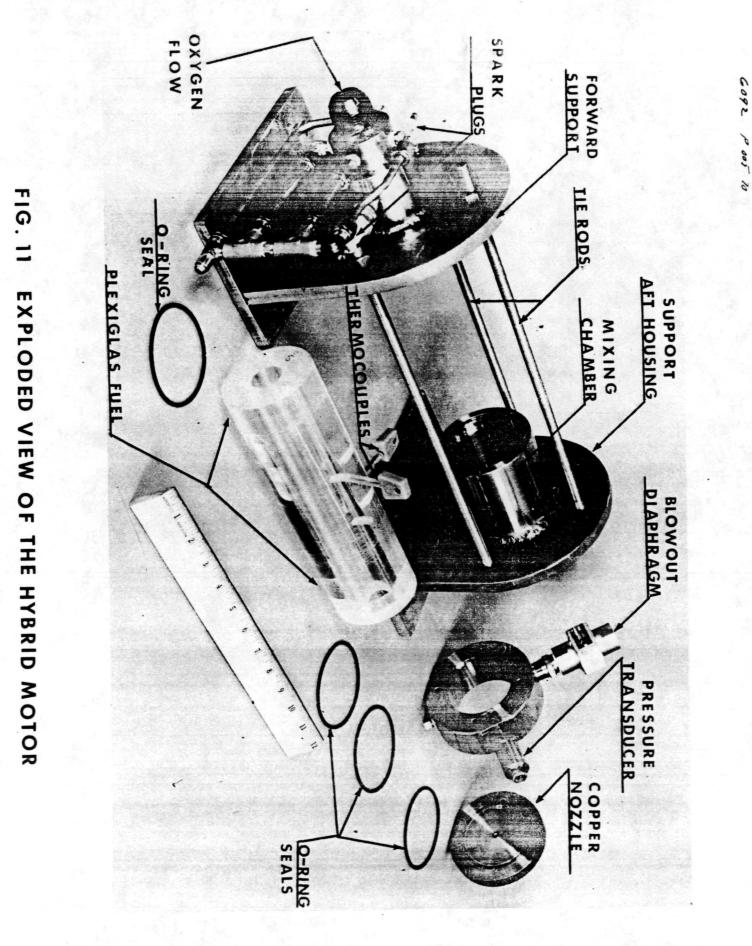


Fig. 9 Schematic Drawing of Hybrid Motor Assembly

2002 R 002

10





- 87

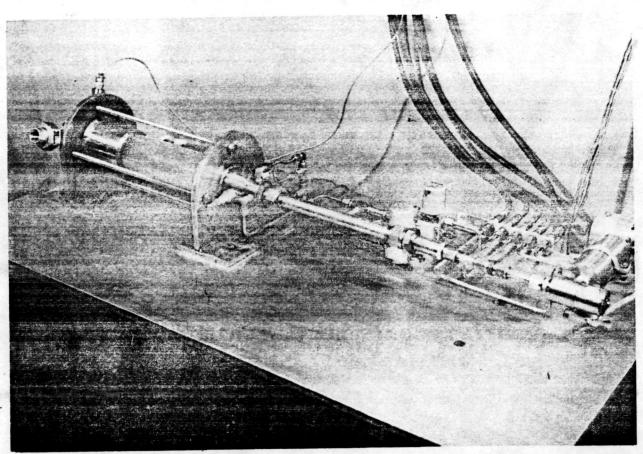


Fig.12 Photograph of hybrid motor mounted in test bay

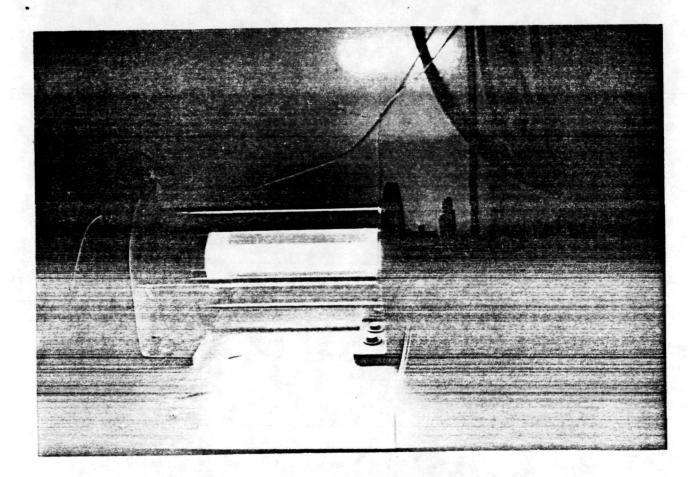


Fig.13 Photograph of steady state hybrid motor operation

49

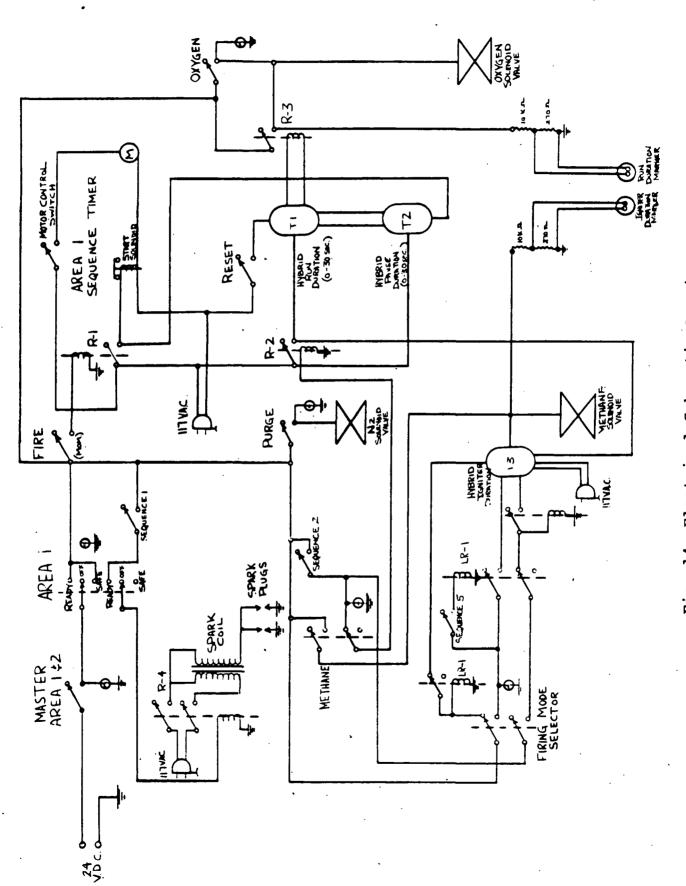
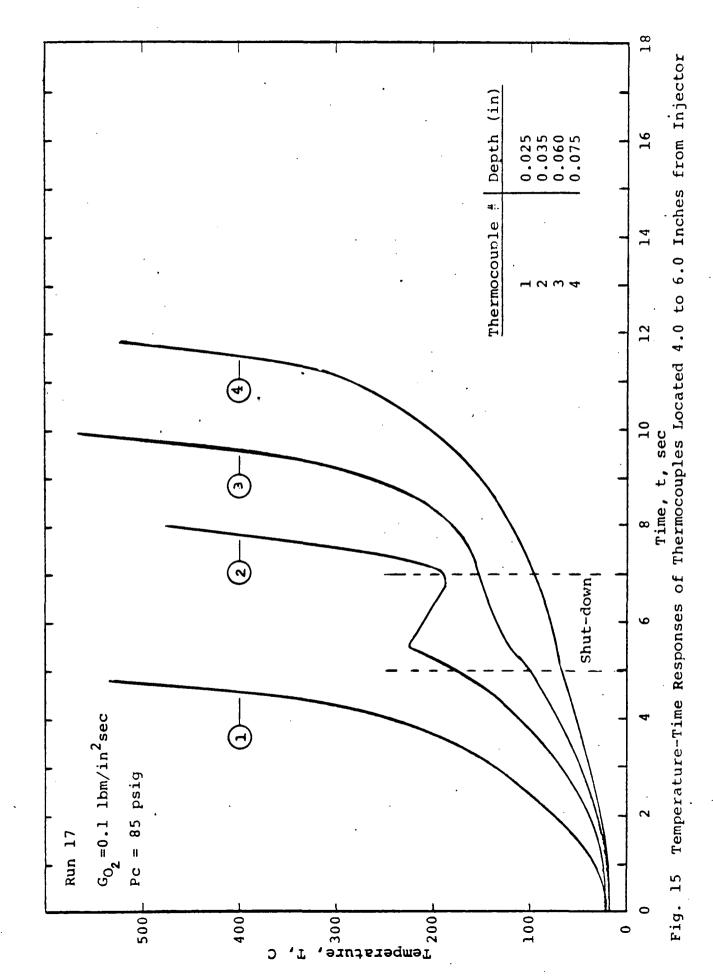


Fig. 14 Electrical Schematic Drawing

- 50 -

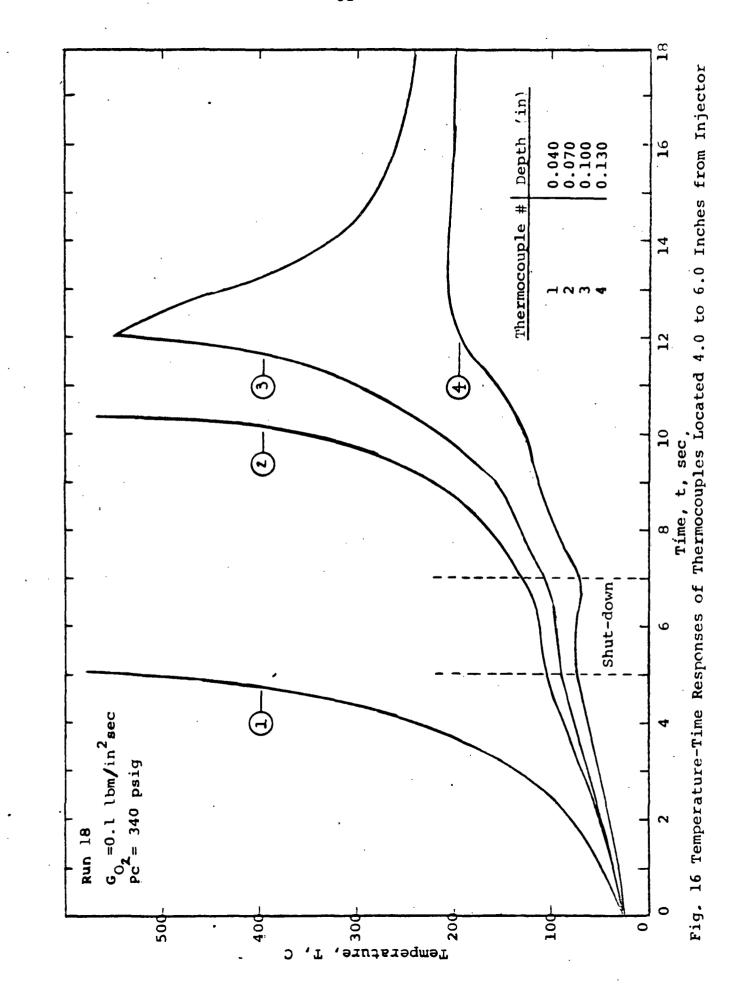
ないないとないで、 ないない いいてい しょう

. . .

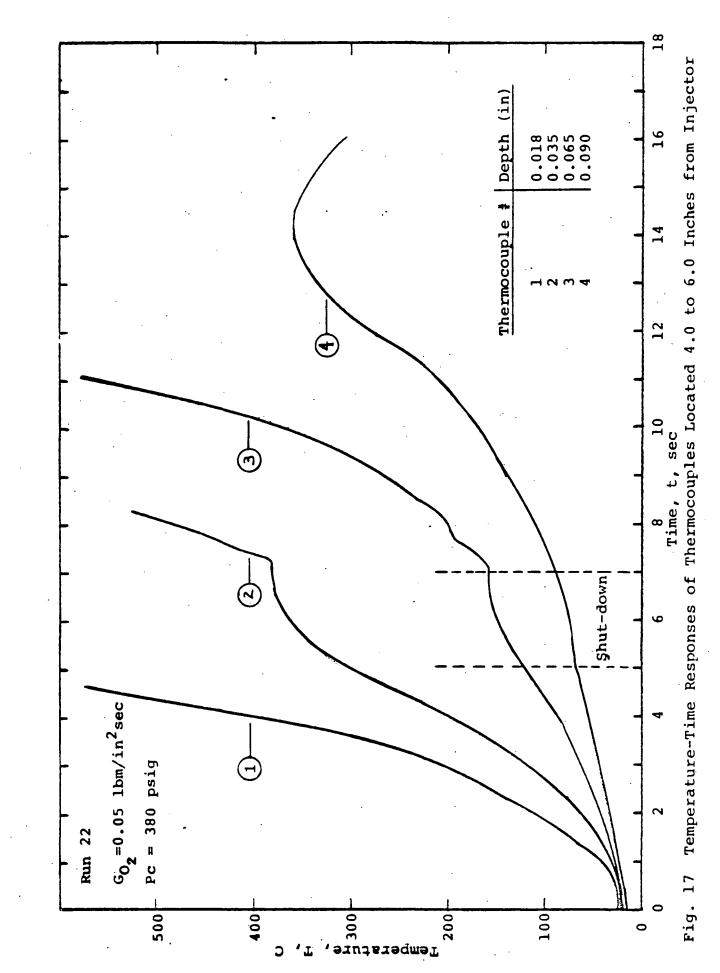


- 51 -

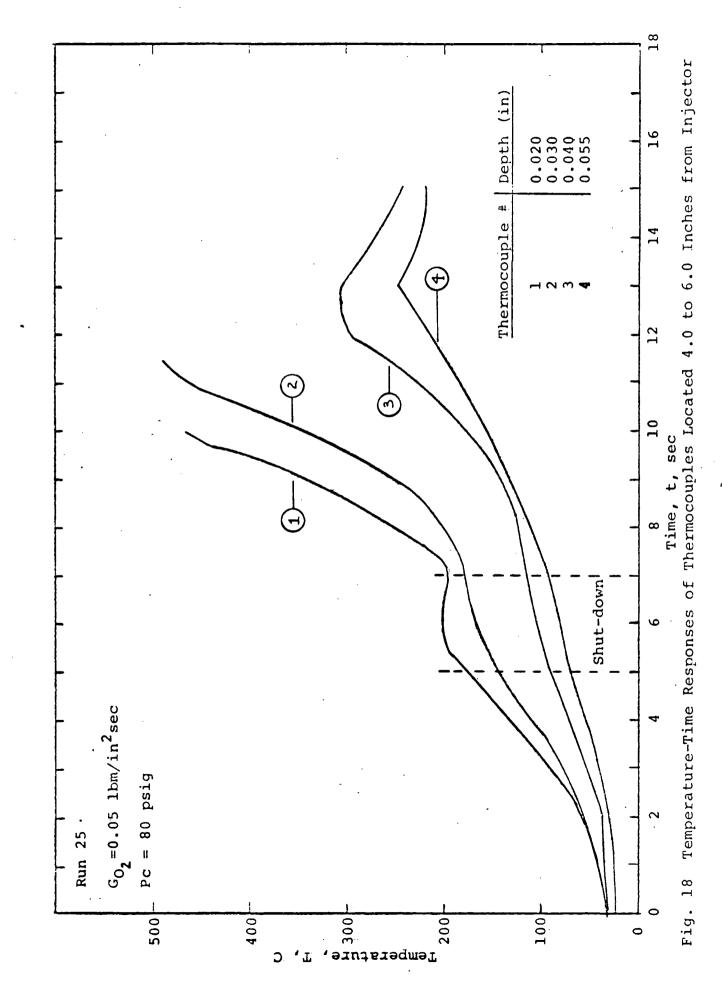
.



- 52 -



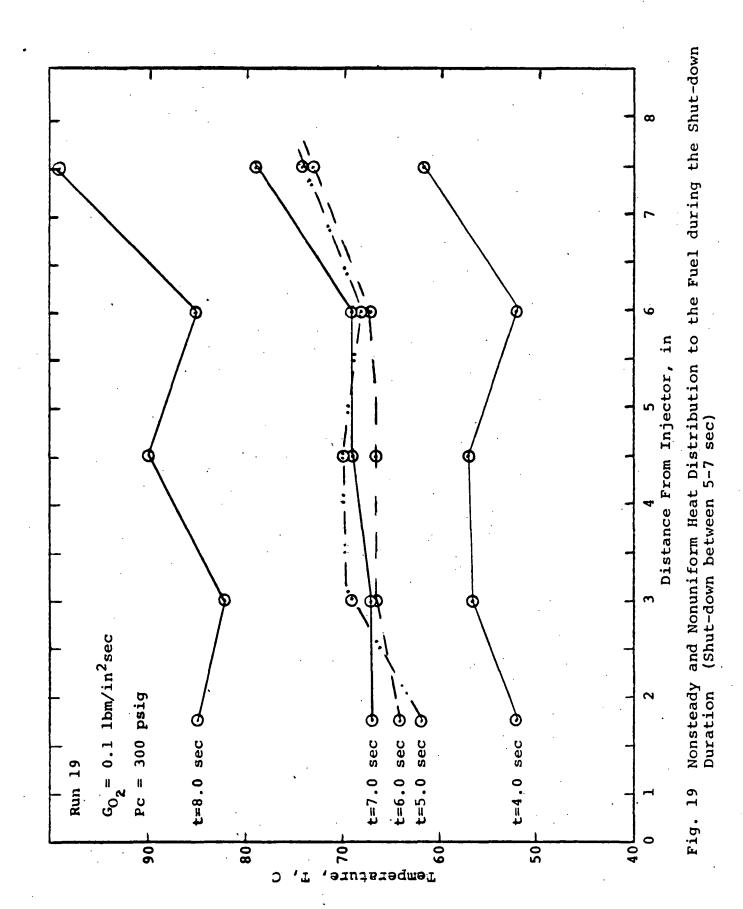
- 53 -



R 011

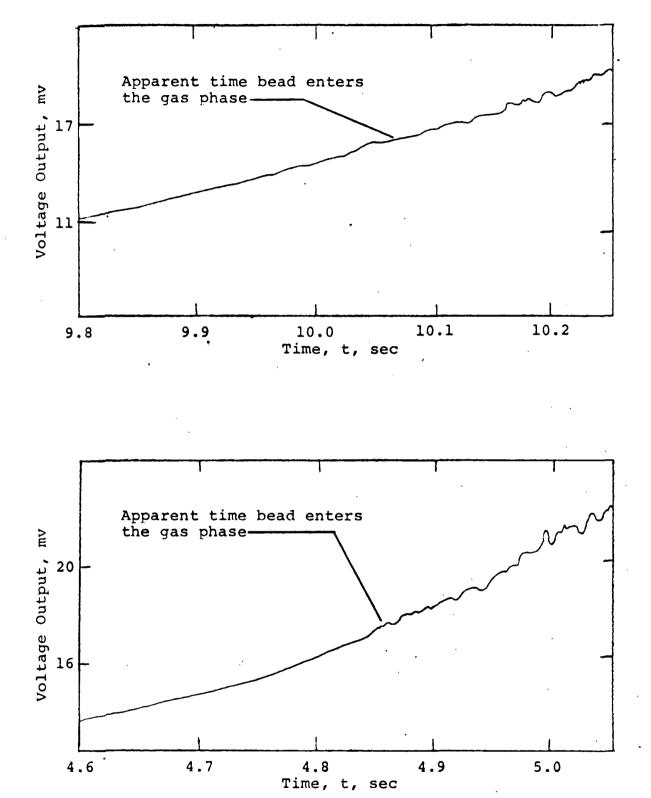
5092

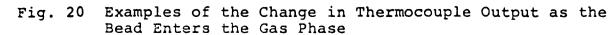
- 54 -



- 55 -

6032 X 012 '70





- 56 -

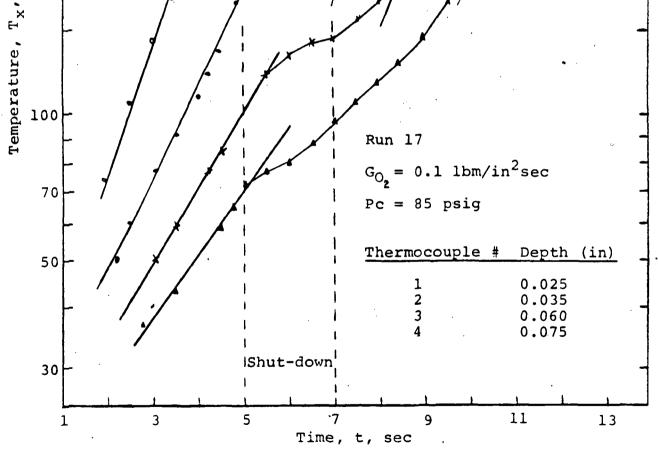
υ

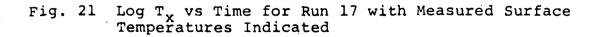
20

40

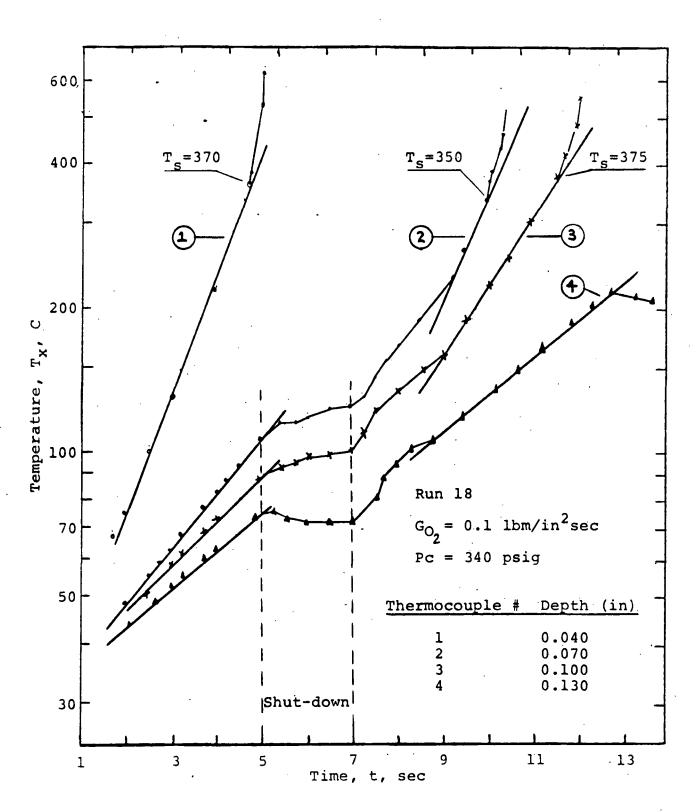
α

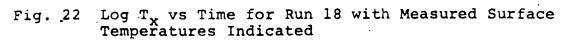
6092





- 57 -

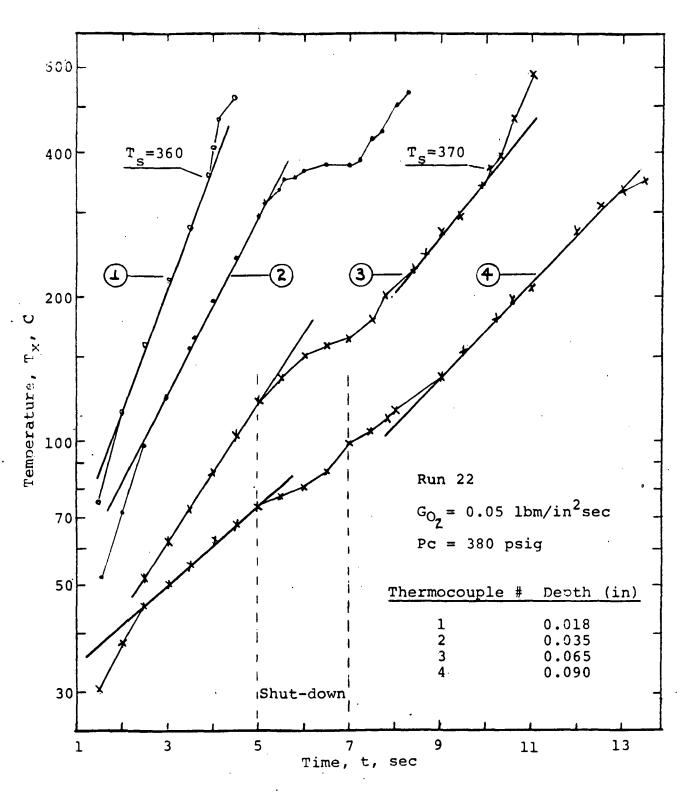


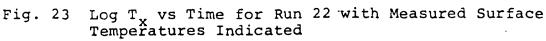


R ols

6032

- 58 -

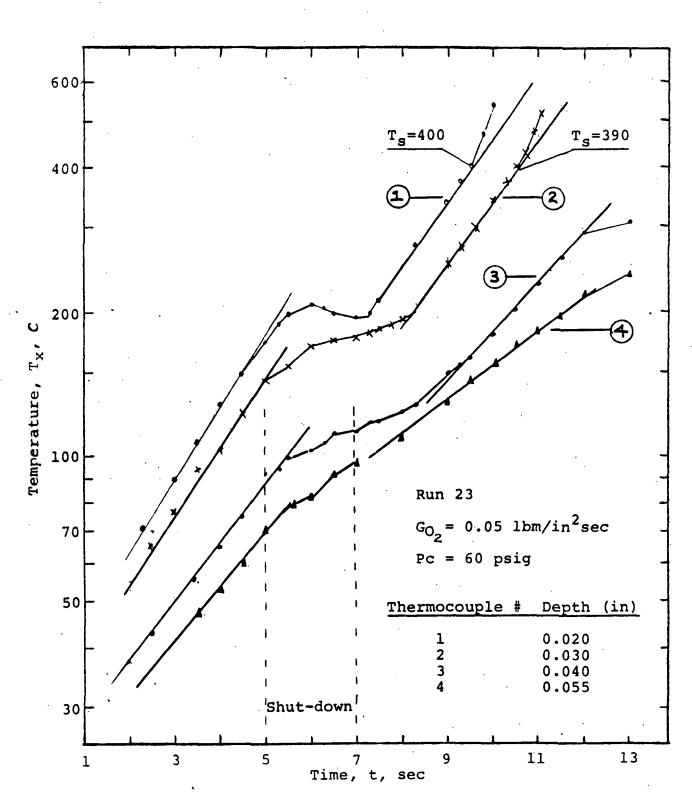


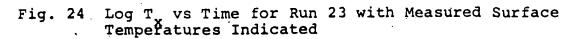


R o S

6092

- 59 -





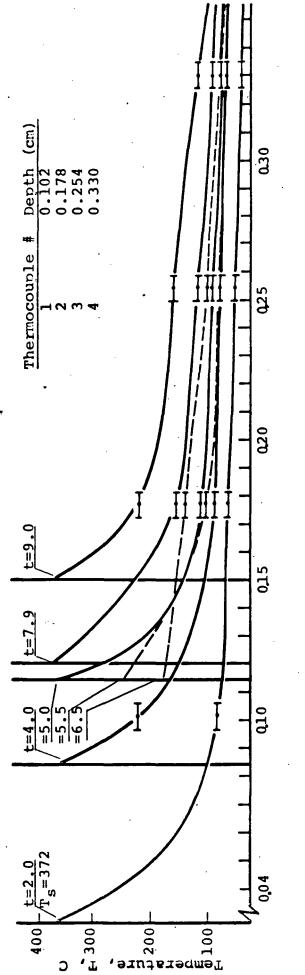
E I O

N

5032

- 60 -

t



Initial Distance From The Surface, x, cm.

61

Surface Temperature, T_S, during Firing Intervals Was Assumed to be Constant. The Thermal Profiles Measured by Four Thermocouples during Run 18. Fig. 25

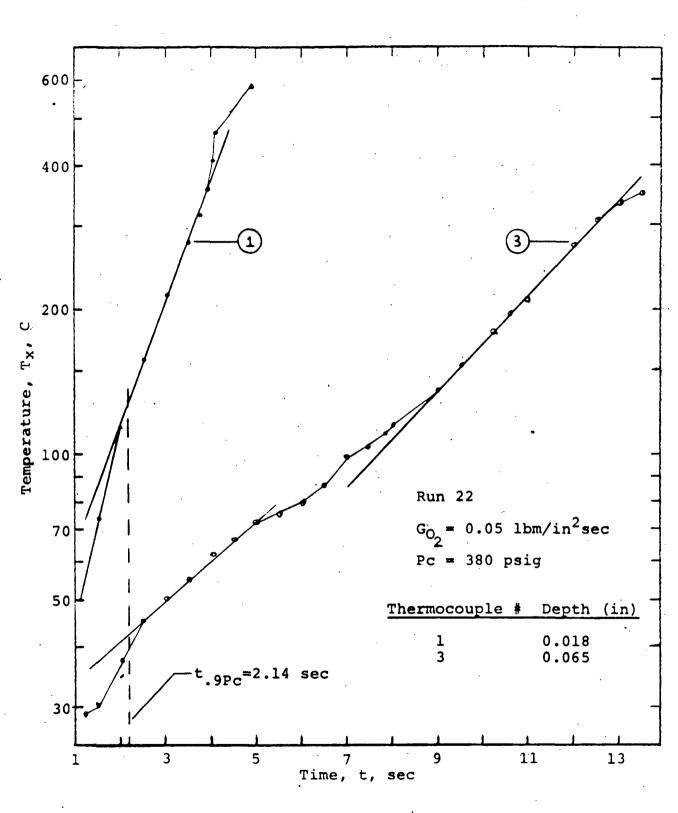
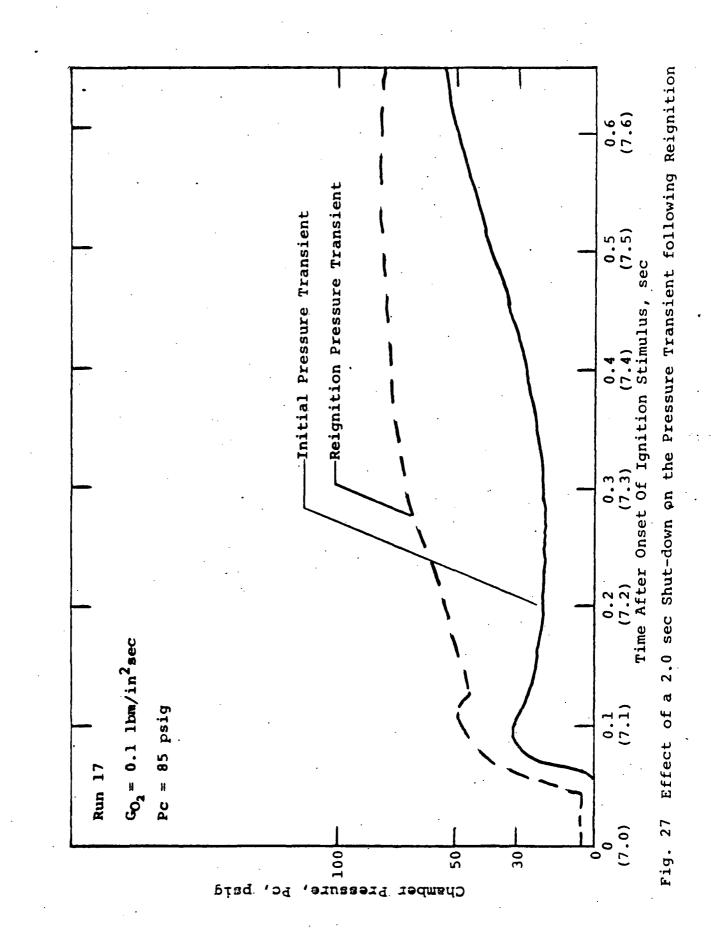


Fig. 26 Log T, vs Time for Run 22 to Compare the Time to Establish Thermal Equilibrium, as Indicated by the Straight Line Approximation, with Time to Establish 90% of the Steady-State Chamber Pressure, t.9Pc

ō

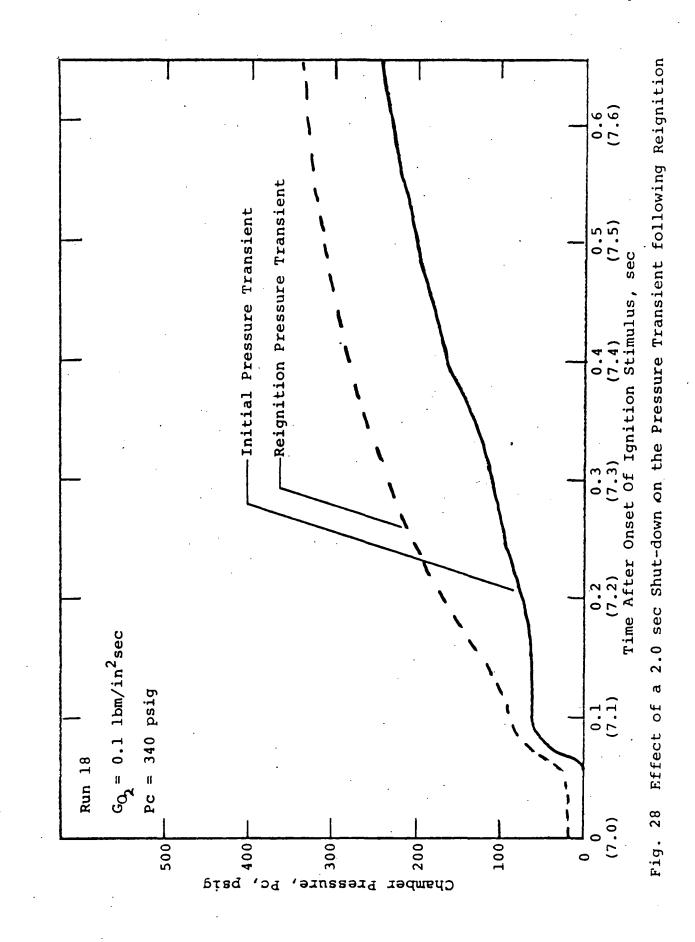
A 1000

- 62 -

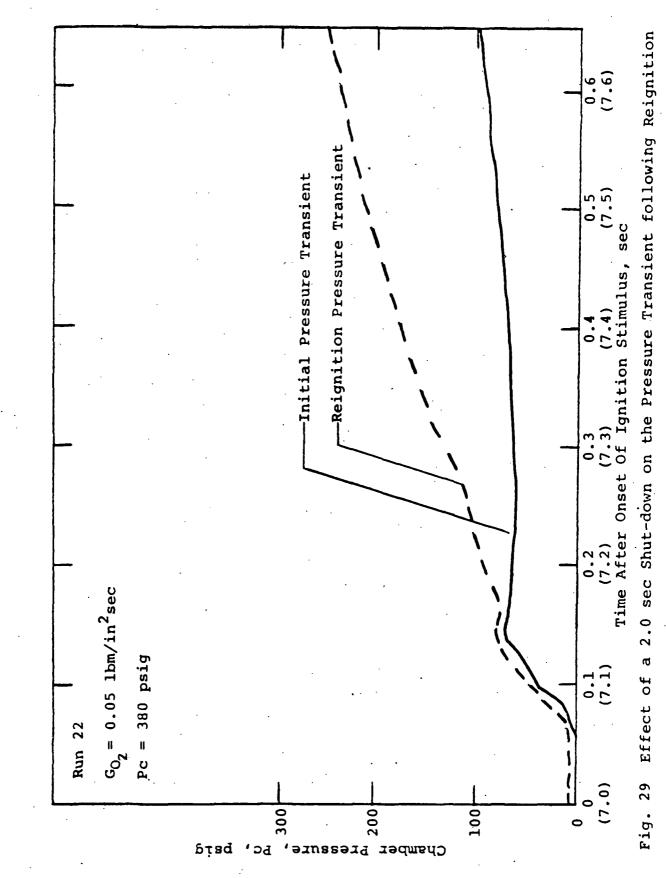


63 -

6092 R 020 ' 70

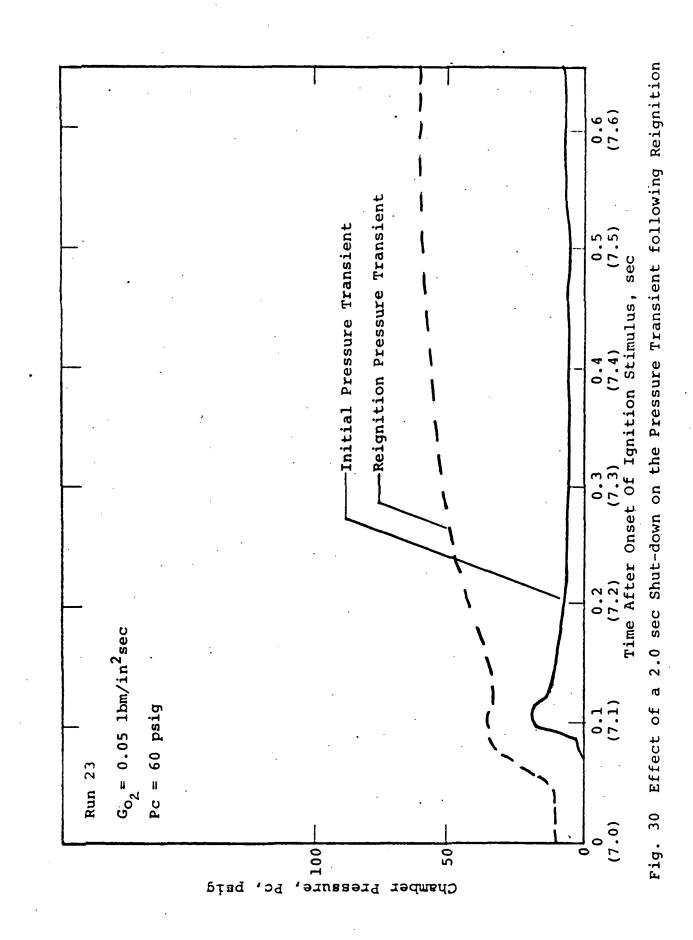


64 -



- 65 -

.

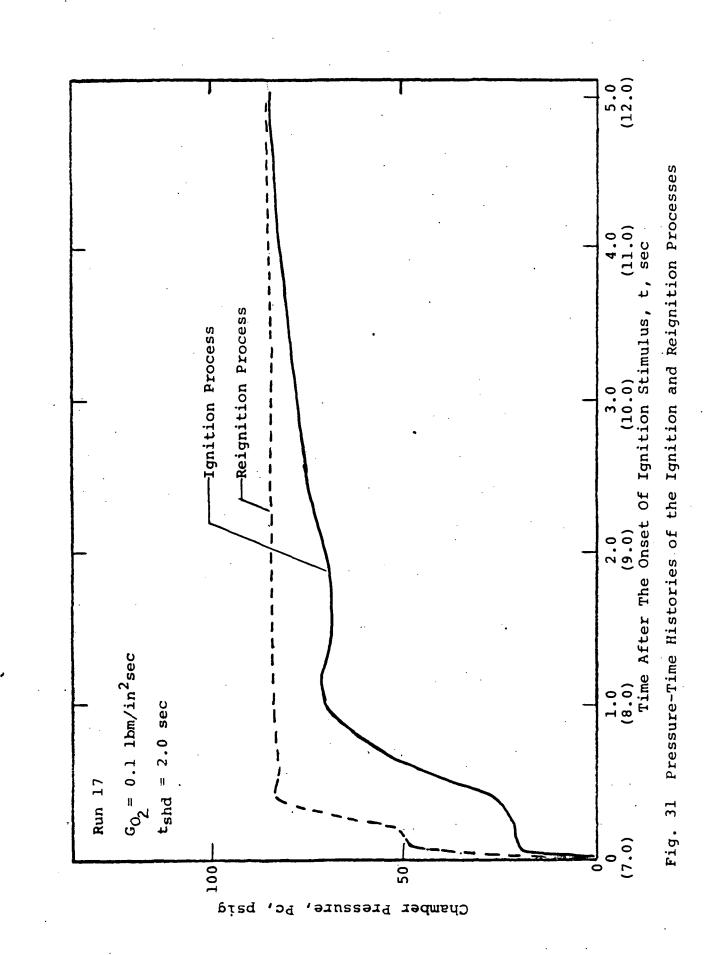


023

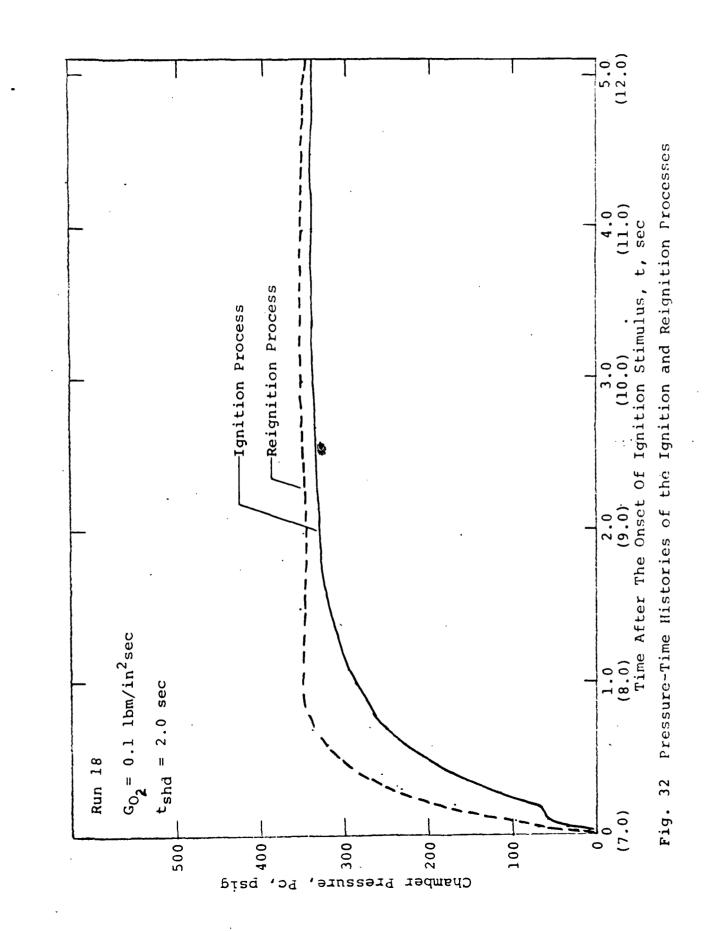
α

6092

- 66 -

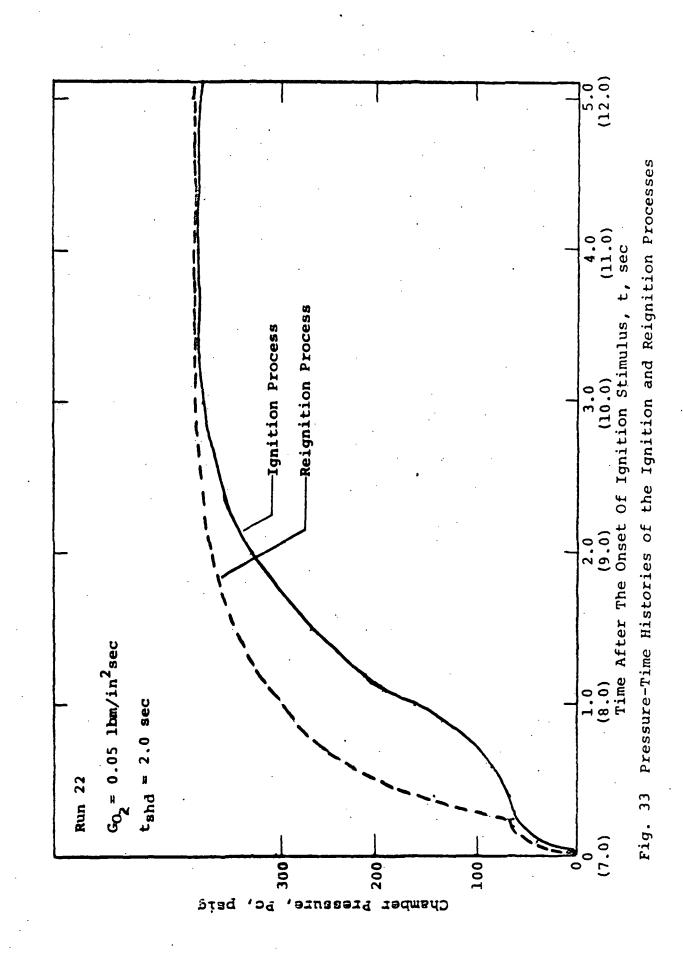


- 67 -

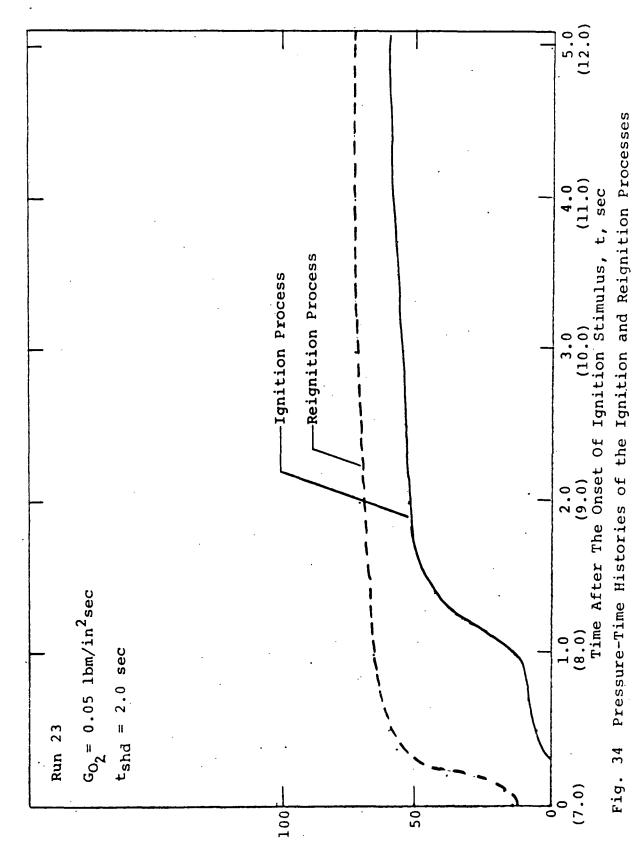


- 68 -

6097 R 025, 70



- 69



Cramber Pressure, Pc, psig

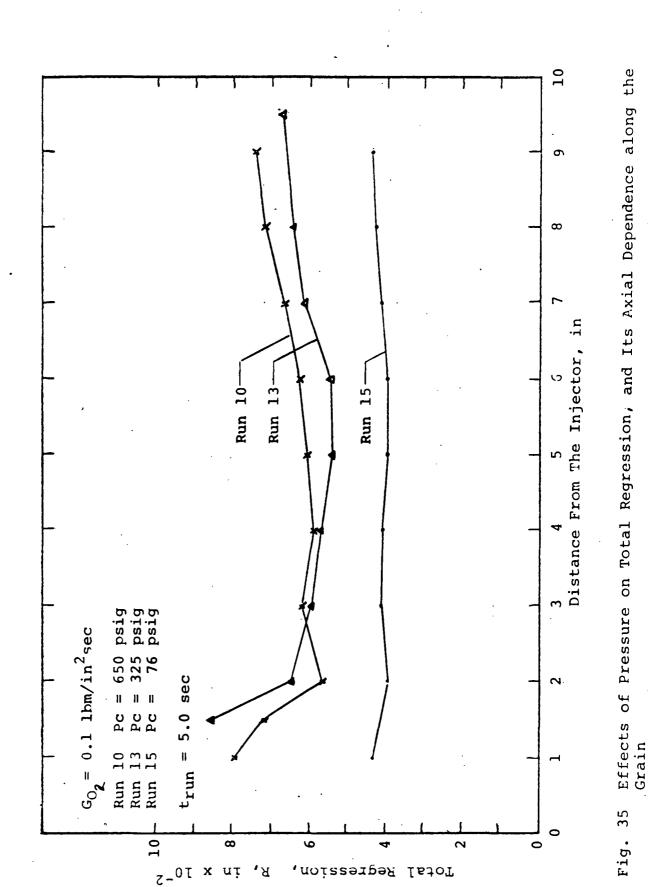
0

021

OL,

6092

-70 -



02.8

۷

6092

- 71 -

FLAME SPREADING DURING HYBRID IGNITION

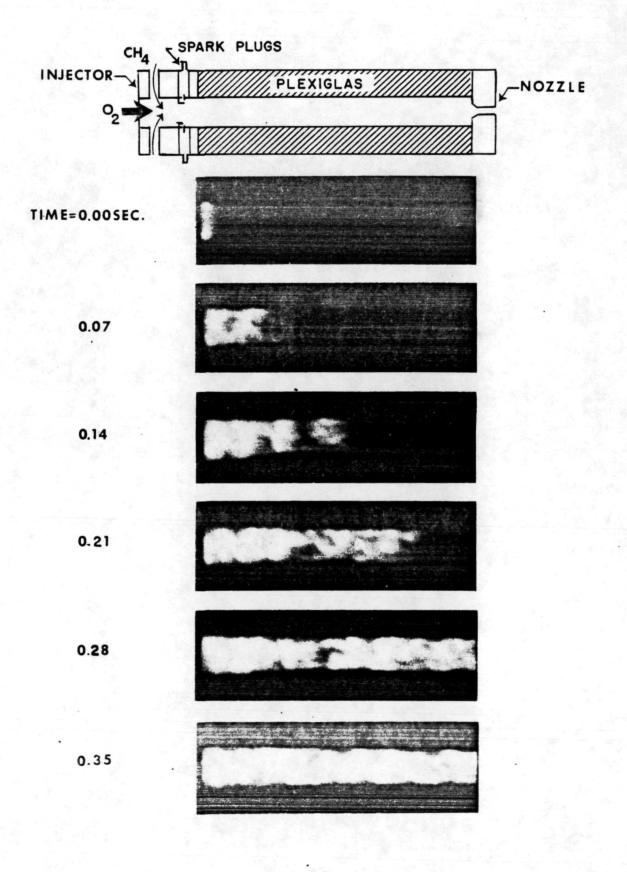
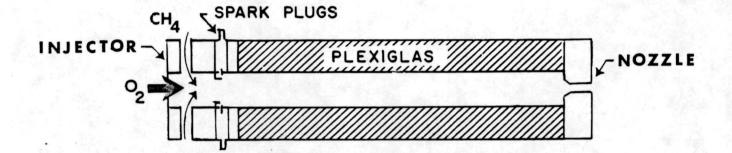


FIGURE 36



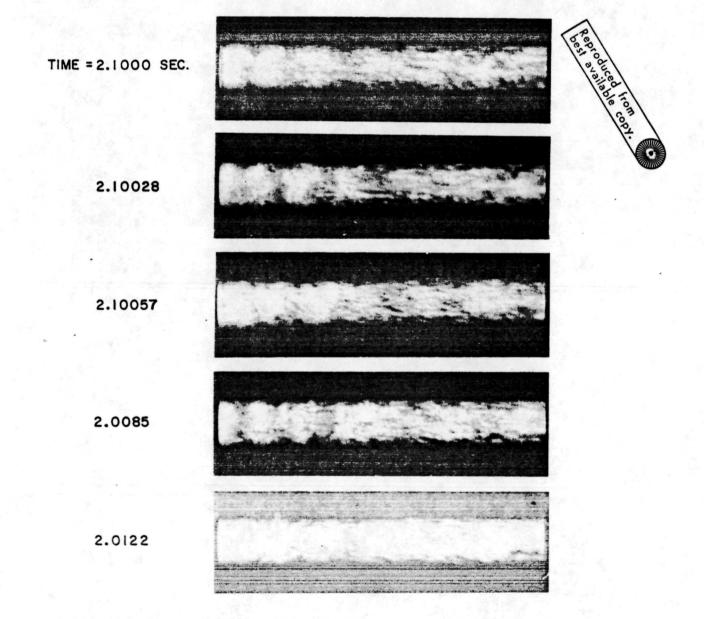


Fig. 37 Flame Distribution During Steady Burning of Hybrid Rocket

6092 P'003 70

73

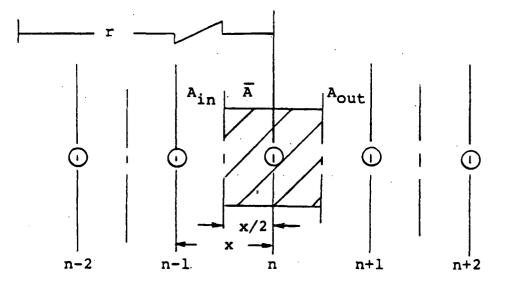
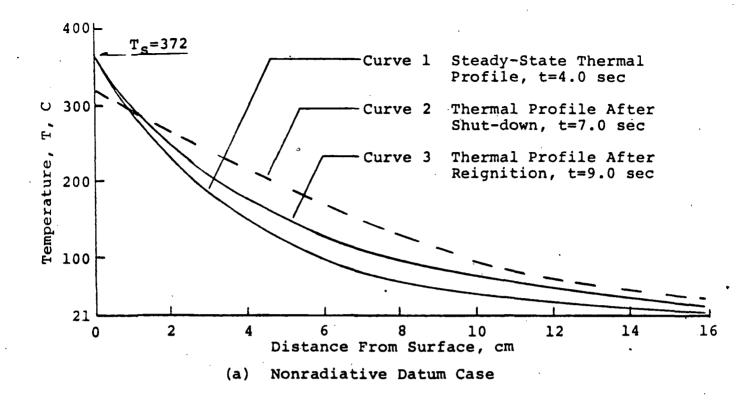


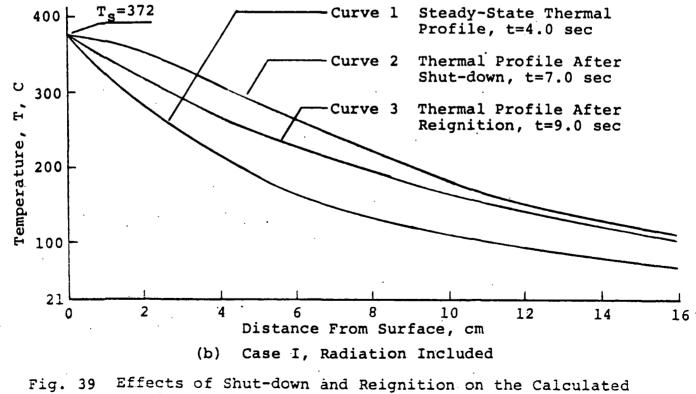
Fig. 38 Schematic of the Nodal Point Array within the Hollow Cylinder

029

ď

2609





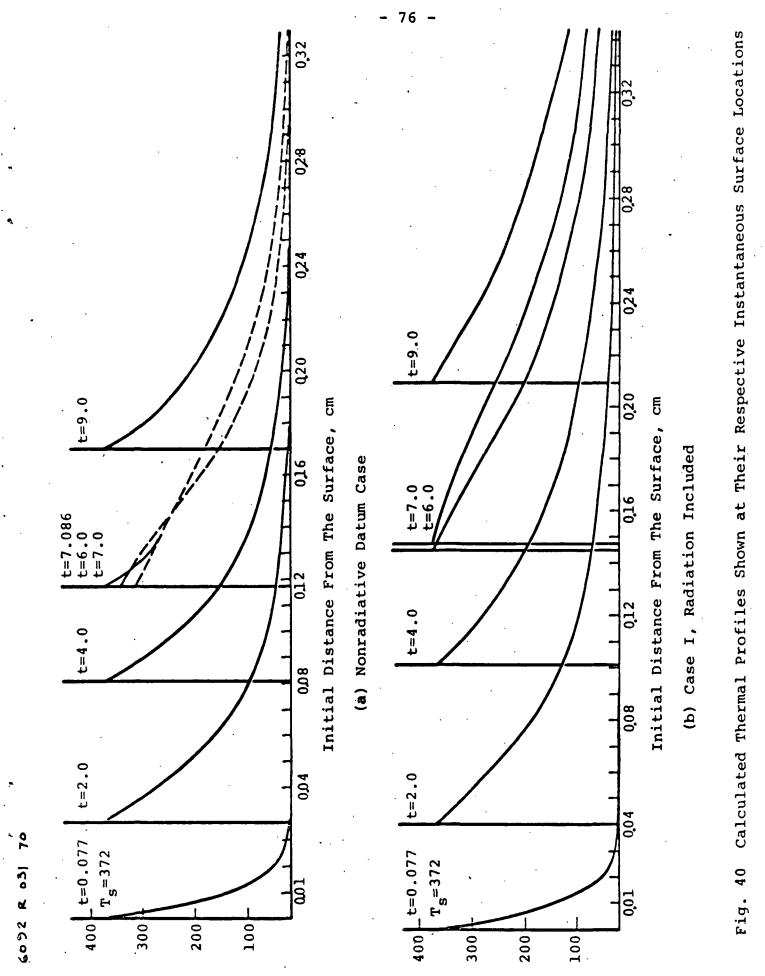
030

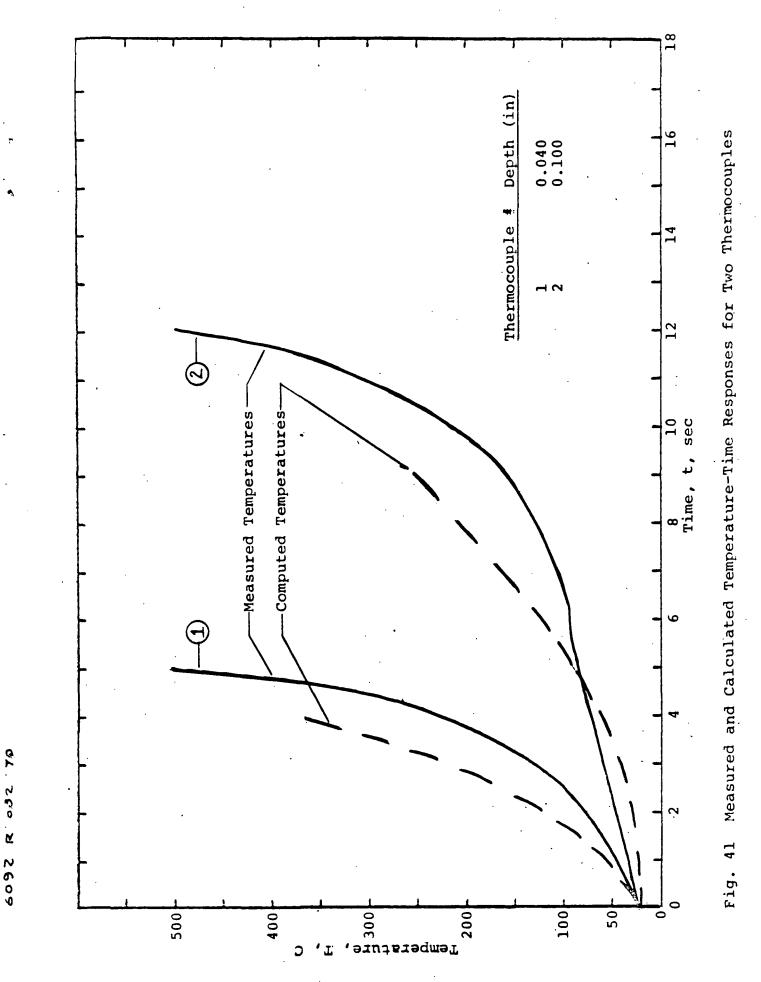
2

6092

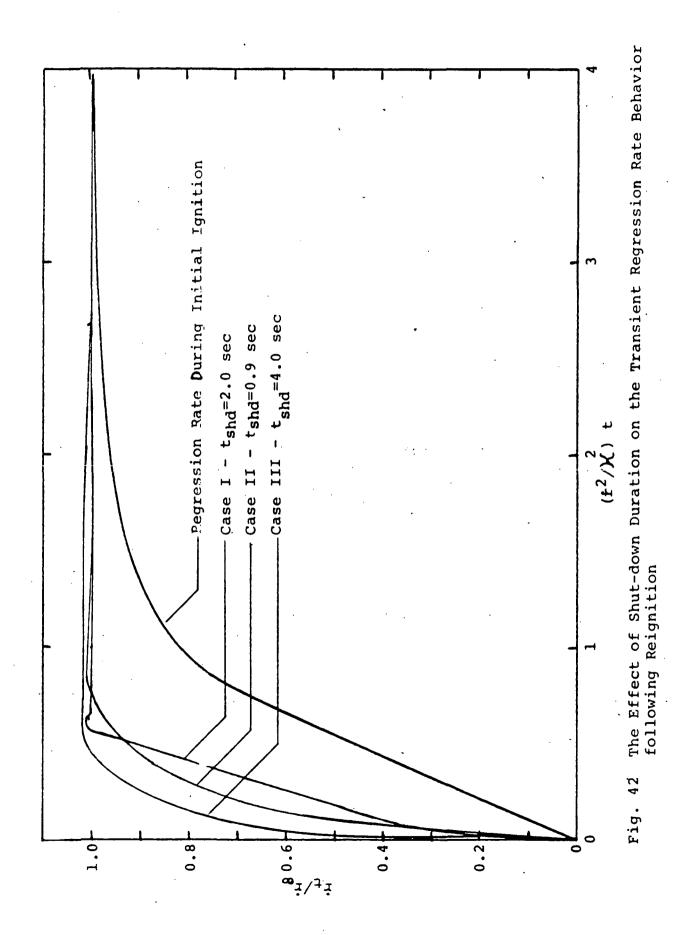
g. 39 Effects of Shut-down and Reignition on the Calculated Steady-State Thermal Profile for the Nonradiative and Radiative Cases

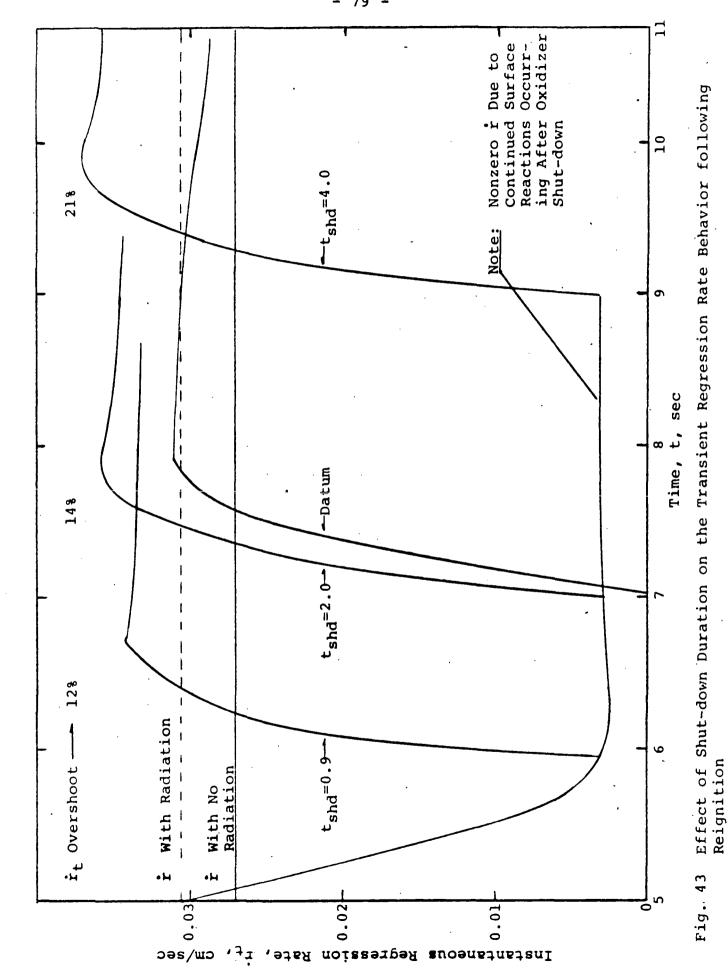
- 75 -





- 77 -





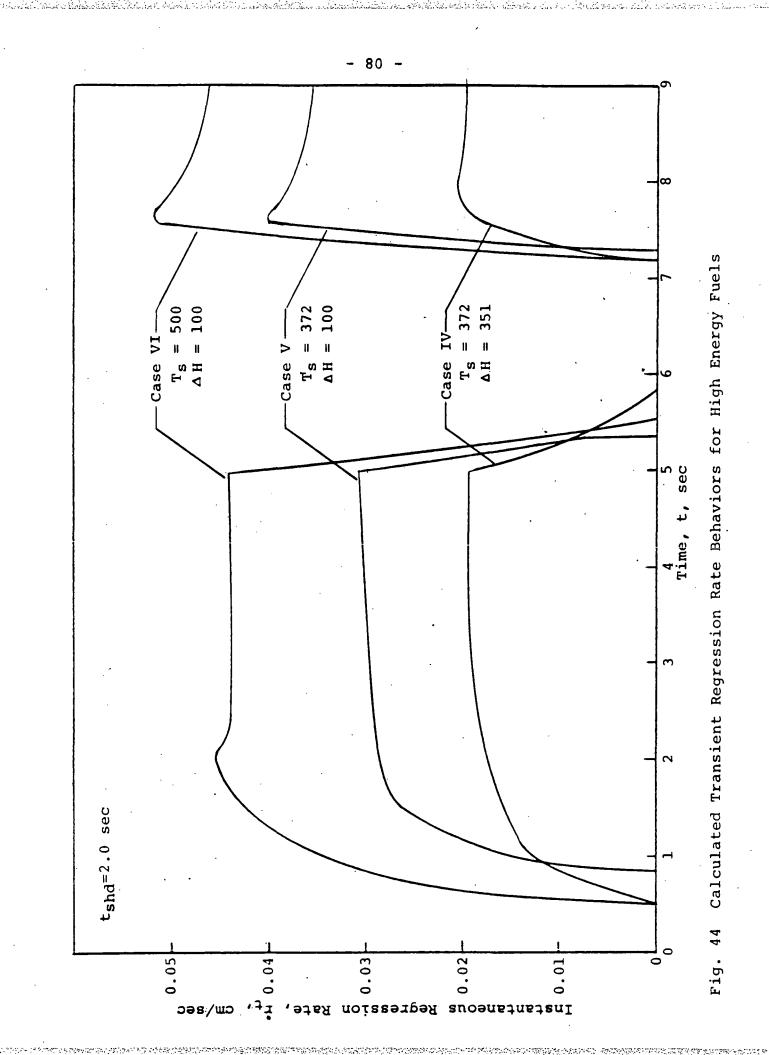
- 79 -

a de la composition d

4

R 034 070

6092



۶.

đ

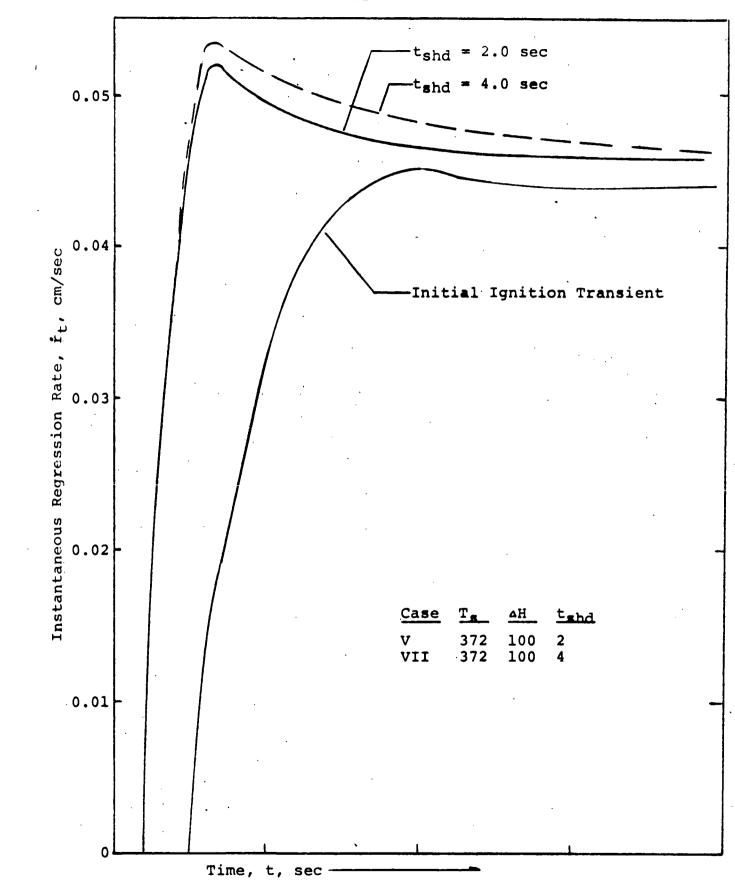


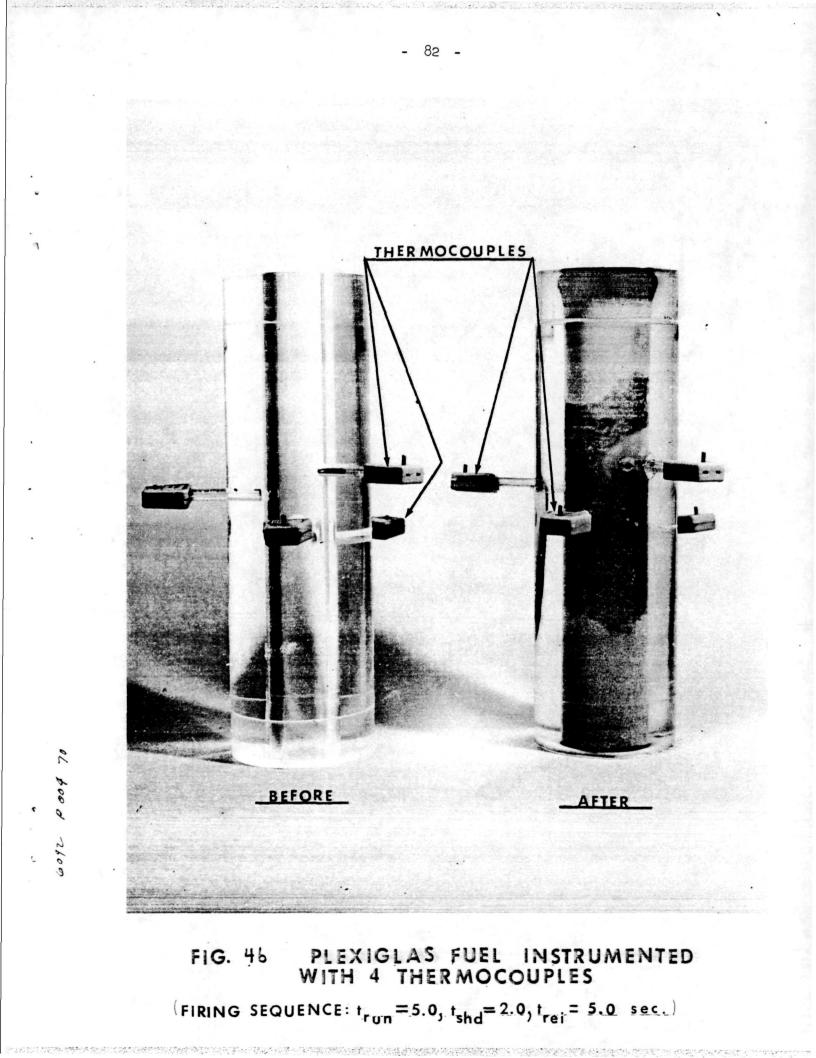
Fig. 45 Effect of Shut-down on the Calculated Transient Regression Rate Behaviors for High Energy Fuels

036 70

ď

5092

- 81 -



APPENDIX A

THERMOCOUPLE TECHNIQUE

App. A-1: Considerations of the Possible Errors in Thermocouple Data

The 1-mil chromel-alumel thermocouples used in this study were purchased from Omega Engineering Inc, Stamford, Connecticut. These thermocouples provided accurate responses over the temperature range of interest and small enough wire diameter to enable temperatures to be measured without greatly disturbing the surrounding material. Yet, they were strong enough to withstand positioning on Plexiglas rods and embedding in the fuel. A Plexiglas grain instrumented with four thermocouples embedded in the fuel is shown before and after firing in Fig. 46.

Certain errors are inherent to every temperature study. A brief listing follows to describe some of these.

The major problem associated with any procedure (1)is the uncertainty in location of the point at which the temperature is being measured. The uncertainty arises from two factors. The first uncertainty is locating the actual position of the thermocouple at a prescribed depth from the surface. Each successive measured dimension used to locate the bead compounds the tolerance errors given on the previous dimension. The second uncertainty is the error in locating the effective junction of the thermocouple. The effective junction, as defined by Brewer²⁵ is the point in the material whose temperature corresponds to the measured temperature output of the thermocouple. For example, the recorded temperature may be assumed to be the temperature on the surface of the bead when in fact it is the temperatures at the center of the bead.

(2) Considerable errors in temperature measurements may result from the disturbance in the material caused by the presence of the temperature probe itself. In particular, lead wires can cause considerable heat to be conducted away from the point of measurement. Studies of this conduction error made by $Brewer^{25}$ show that the errors are significant if the thermocouple lead wires near the bead are parallel to the direction of heat flow. Strittmater, et al.²⁶ agree that it is attractive to consider directing the leads along an isotherm to prevent heat losses through them. However, as the authors²⁵ indicate, an isotherm could be difficult to locate due to nonuniform burning surfaces resulting from propellant roughness. Also, as the entire surface is seldom ignited all at once, placement of the lead wires parallel to the initial grain surface involves the risk that the burning surface will reach the lead wire before the bead and preheat it by conduction.

A compromise between the two considerations mentioned above was made for this study. Lead wires in the vicinity of the bead were oriented perpendicular to the heat flow to minimize the conduction error. At a sufficient distance away from the bead, the lead wires were directed away from the surface plane to avoid their heating before the bead.

(3) The temperature recorded by a sensing probe is dependent on its surrounding environment. The influence of radiative heating can produce large increases in temperature responses because the radiation effect is proportional to the temperature of the source raised to the fourth power minus the temperature of the sink raised to the fourth power. However, it was initially assumed for these experiments that the radiation effect on the thermocouple outputs would be insignificant and could be ignored. This assumption was based on two factors: 1) the emissivities of PM in the temperature range of interest is close to unity and 2) the temperature sensing probes were made from materials that would reflect most of the radiant energy reaching Therefore, as previous workers have assumed^{6,15,18}, the bead. the radiation effects would be negligible. However, as discovered from the results of the thermocouple data, radiation to the subsurface regions of the fuel is significant. Thus, a solution to the heat conduction equation considering only convective heating would yield poor results when compared to experimental data, but when two radiation parameters are considered, the solution produced favorable results. Therefore, it has been an incorrect assumption by previous researchers to disregard the radiative influence on temperature measurements in Plexiglas systems.

App. A-2: Thermocouple Mounting Procedure

A mounting procedure was devised to minimize all the errors. The thermocouples were positioned and maneuvered with the aid of a micromanipulator and a Stereo-zoom microscope. The procedure used for mounting and installing are discussed in the following.

(1) The thermocouple was placed on a 1/4 inch diameter rod in a machined groove 0.005 inches in depth across the diameter of the face. Plexiglas rods 1/4 x 2 inches were used so as not to effect the properties of the fuel. The thermocouple was positioned in the groove with the bead as close to center as possible. A drop of PS-18, a plexiglas cement, was used to fasten the thermocouple bead to the rod. This cement was used since it hardens to the same material as the surrounding fuel. Therefore, it should not effect ablation in the areas of the bead or the fuel surrounding the bead.

(2) The lead wires were also cemented across the face of the 1/4 inch rod. When embedded in the fuel, the lead wires will be perpendicular to the heat flow in the vicinity of the bead and thereby minimize the conduction error described earlier. The remaining lengths of lead wire were drawn along the sides of the rod and cemented into 0.132 inch groove. An Omega, 1/4 inch Chromel-Alumel, adapter was fitted to the end of the rod and the lead wires were connected to their respective terminals. The rod, complete with thermocouple, was ready for installation in the fuel.

(3) Radial holes with flat bottoms to assure positive depth locations were drilled into the Plexiglas fuel grains. Normally each hole was measured to locate each thermocouple at a different depth. The holes were half filled with the same Plexiglas cement, PS-18, and the rods were carefully inserted, forcing some of the cement and most of the air bubbles to the surface. This procedure assured a gas-tight seal near the bead. The rods were secured with tape and at least 24 hours was allowed for drying before firing the instrumented grain.

The mounting procedure, although an arduous task requiring enduring patience, produced a reliable thermocouple probe. One hundred percent of the thermocouples installed in the fuel functioned property.

		뇌					86 -					
	AND EQUIPMENT	Manufacturer or Distributor	Commercial Plastics & Supply Trenton, N. J.	. Omega Engineering, Inc. Stamford, Conn.	The Matheson Co., Inc. East Rutherford, N. J.	Dynisco, Division of Amer- ican Brake Shoe Company Cambridge, Mass.	Marotta Valve Corp. Boonton, N. J.	DuPont Photo Products Wilmington, Del.	Commercial Plastics & Supply Trenton, N. J.	Wollensak • Rochester, N. Y.		
APPENDIX B	VAILABLE EXPERIMENTAL APPARATUS AND EQUIPMENT	Use	Hybrid Rocket Fuel	Subsurface temperature histories	Regulate flow of igni- tion gas	Measure chamber pressure	Electrically operated on-off valves	16 MM High Speed Re- versal Films	Embedding thermocouples	High Speed Movies	·	•
	COMMERCIALLY AVAILABLE	<u>Item</u>	Plexiglas (PMM)	Thermocouples (CHAL-001)	<pre>Methane regulator (Two-stage) (MOD-3:Ser.3050)</pre>	Pressure Transducer (PT-76-2M)	Solenoid Valves (MV-74)	High Speed Film (931-A)	Plexiglas Cement (PS-18)	Wollensak Model WF-16 Fastex Camera		

5.267.575

265

2. 2.

¢

07855836 * CROST

A hard barren

Security Classification						
	CONTROL DATA -	-				
(Security classification of title, body of abstract and in 1. ORIGINATING ACTIVITY (Corporate author)	ndexing annotation must		SECURITY CLASSIFICATION			
Princeton University		Unc	lassified			
Department of Aerospace and M	lechanical Sciences	2b. GROUP				
REPORT TITLE			- 			
Combustion Anomalies In Stop-	Restart Firi	ng Of Hyb	orid Rocket Engines			
4. DESCRIPTIVE NOTES (Type of report and inclusive dates)						
Scientific Interim NASA GRA	NT NGR 31-00	1-109				
Michael A. Saraniero, Leonard	H. Caveny.	Martin Su	mmerfield			
Machael III Baraniero, Econard						
REPORT DATE	78. TOTAL NO	-	76. NO. OF REFS			
September, 1970		O				
E. CONTRACT OR GRANT NO.	94. ORIGINAT	JR'S REPORT NO	JMBER(3)			
b. PROJECT NO.	AMS Re	AMS Report No. 945				
c .		PORT NOIS /A-	, other numbers that may be seed to t			
с.	95. OTHER RE this report)	- 0 K I NO(3) (AN)	r other numbers that may be assigned			
1.						
0. DISTRIBUTION STATEMENT						
1. Distribution of this docu	ment is unli	mited.				
1. SUPPLEMENTARY NOTES	12. SPONSORI	IG MILITARY AC	TIVITY			
	•		ced Research And			
Tech; Other	Techno		utics & Space Admin			
3. ABSTRACT	Nacion		Autics & Space Admin			
An experimental investig						
Plexiglas hybrid rocket demon						
consequence of a previous ign significantly increases the r						
duces regression rate oversho	ots during r	eignition	. Transient			
periods following the initial	. ignition an	d the res	tart after a two-			
second shutdown were observed conducted at two oxidizer flo	I IOT IOUT EX	perimenta 78 and 0	1 tests which were 039 lbm/sec and			
two chamber pressures, 80 and			ples (0.001 inch			
dia. wire) were embedded in t	he fuel to re	ecord sub	surface temperature			
histories. A mathematical mo	del of the th	hermal pr	ocesses in the fuel			
was developed to correlate th	e data and to	o calcula	te the regression			
rate transients. A parametri fuel's thermal characteristic	c study inve	stigated	the influence of the			
			that regression rate			
overshoots can be as high as	29% when high	h energy	fuels are reignited			
	transient b	ehavior a	fter shut-down can			
The results indicate that the		teristics	of individual fuel,			
The results indicate that the be anticipated once the regre						
The results indicate that the be anticipated once the regre oxidizer combinations have be	en establish	ed. Thus	, extensive experi-			
The results indicate that the be anticipated once the regre oxidizer combinations have be mental firings of full scale	en establish rocket motor:	ed. Thus s should	, extensive experi- not be required to			
The results indicate that the be anticipated once the regre oxidizer combinations have be mental firings of full scale adequately predict pressure t proper attention is given to	en establish rocket motor: ime historie:	ed. Thus s should s followi	, extensive experi- not be required to ng reignition if			
The results indicate that the be anticipated once the regre oxidizer combinations have be mental firings of full scale adequately predict pressure t	en establish rocket motor: ime historie:	ed. Thus s should s followi	, extensive experi- not be required to ng reignition if			

Security Classification

Unclassified Security Classification

KEY WORDS	LIN	LINKA		LINK B		LINK C	
	ROLE	₩Т	ROLE	WT	ROLE	wт	
Hybrid Rocket Motor Hybrid Rocket Motor Combustion							
Ignition					1		
Re-ignition							
Surface Temperature		· ·					
Thermocouple measurements and temperatur	e						
profiles						l .	
Heat conduction in regressing solid Oxygen/Plexiglas (PMM) combustion							
oxygen/ Prexigias (PMM) combustion							
•							
						1	
			· ·				
					·		
		!			•		
		1]		
·		1	1				
		ŀ					
					•		
			1				
			[[.]				
			1				
	· · ·		1				
						•	
						•	
	1.	1					
·							
		<u> </u>	!		l		

Unclassified Security Classification