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PHYSICS OF HEAVILY DOPED SILICON AND  
SOLAR-CELL PARAMETER MEASUREMENT

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CONTRACT: PHYSICS OF HEAVILY  
DOPED SILICON AND SOLAR-CELL  
PARAMETER MEASUREMENT

CONTRACTOR: UNIVERSITY OF  
FLORIDA, FRED A. LINDHOLM

GOALS: THEORY & EXPERIMENT ON  
 $\Delta E_G$  ENERGY GAP,  $\tau$  LIFETIME,  $S$  RECOMB.  
 $D$  VELOCITY, DIFFUSIVITY, MOBILITY  
IF N AND/OR P IS HIGH.

ALSO

ACCURATE DETERMINATION OF  $\tau, S,$   
IN QUASINEUTRAL REGIONS

REPORT DATE: 10/2/84 (3 MOS.)

Colored & Presented by  
C. Tang Sah

# HIGH-EFFICIENCY SILICON SOLAR CELL RESEARCH

Status (Briefly)

3 Parameters:  $\Delta E_G$ ,  $\tau_B$ ,  $S_{BSF}$

1

1. ENERGY-GAP MODEL DEVELOPED,  
COMPARED WITH  
PHOTOLUMINESCENT  
AND TRANSPORT DATA.

$\Delta E_G$

2

2. ELECTRICAL SHORT-CIRCUIT  
CURRENT DECAY (ESSCD)  
DEVELOPED AND IMPROVED

3. ESSCD AUGMENTED BY ADMITTANCE  
VS.  $\omega$  AND  $V$  (FORWARD)

4. ESSCD+ADMITTANCE APPLIED TO  
MEASURE  $S$  AND  $\tau$  FOR BASE OF  
MANY BSF SOLAR CELLS

$\tau_B, S_{BSF}$

## Publications

2 [ ESSCD IN TRANS ED. Y - ESSCD  
BEING WRITTEN,  $\tau_B, S_{BSF}$

1 [ ENERGY GAP MODEL IN  
PHOTOVOLTAICS CONF.,  $\Delta E_G$   
ALSO DETAILED VERSION UNDER  
REVIEW, PHYS. REV.

CO-WORKERS: A. NEUGROSCHER, ALL  
WORK: P.T. LANDSBERG, C.T. SAH,  
AND NEUGROSCHER ON ENERGY GAP.

# HIGH-EFFICIENCY SILICON SOLAR CELL RESEARCH

## Remarks on Energy Gap Model

- ENERGY GAP = KEY PARAMETER
- SIMPLE USEFUL FORMULA
- REPRESENTS EXPERIMENTAL FACTS
  - 5K (OPTICAL = PL)
  - 300K (TRANSPORT DATA)
- HEAVILY DOPED (LARGE N OR P)
- HIGHLY EXCITED (LARGE N AND P)
  - STRONG IRRADIATION
  - P/N TRANSITION REGION
- T DEPENDENCE
  - SOLAR CELLS AT 300K
  - EXPERIMENTS, OTHER T

- ~~Handwritten scribbles~~
- Simple understandable Theory :-
    - Debye (Carrier) Screening ← Electrostatic Coulombic
    - SAH (1966), chapter 6
    - SAH, McNutt, Chan, TR28 (June 1974)
    - SAH, et al, SOLAR CELL (1978)
    - LANDSBERG, N.L.S. (1984)

# HIGH-EFFICIENCY SILICON SOLAR CELL RESEARCH

TEMPERATURE DEPENDENCES OF

$\sqrt{n_i p_i}/n_i$ ,  $E_G$ ,  $n_i$  and  $L_D$   
OF SILICON

C. T. Sah, N. J. McMurtt and C. H. Chan

Technical Report No. 28

June 27, 1974

Solid State Electronics Laboratory

Technical Report No. 28

June 27, 1974

Electrical Engineering Research Laboratories

University of Illinois

Urbana, Illinois

The actual energy gap also includes the electron-hole, electron-electron and hole-hole electrostatic interaction energies which reduces the energy gap at high carrier concentrations. This effect is represented by  $\Delta E_G$ ,

$$\Delta E_G = -e/4\pi\epsilon_0(\lambda_D+a) \quad (4)$$

$$= -1.23 \times 10^{-4} / (L_D+a) \text{ Volts} \quad (5)$$

# HIGH-EFFICIENCY SILICON SOLAR CELL RESEARCH

## 1984 Landsberg Version

### EXPRESSION FOR GAP SHRINKAGE

$$(1): E_G(N, P) = W + \frac{e^2}{\epsilon a} e^{-k_D(N, P) a}$$

$$(2): E_G = W + \frac{e^2}{\epsilon a}, \text{ for } N = P = 0$$

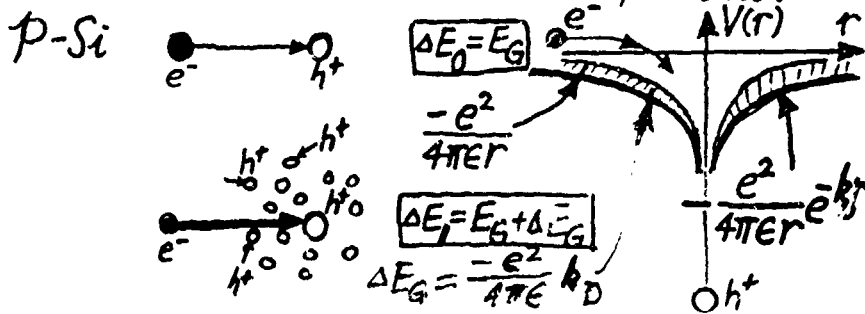
$$(3): \Delta E_G = \frac{e^2}{\epsilon a} [1 - e^{-k_D(N, P) a}]$$

$$= \frac{e^2}{\epsilon} k_D(N, P)$$

$$\lambda_D = \frac{1}{k_D} = \text{Debye Screening Length}$$

### 1966 Sah Version: Screening by Majority

★ carriers on minority carrier  $\Delta E_G$   
 NOTE:  $\Delta E_G$  data is from minority carrier experiments!



Screening Wave Number  $k_D$

$$k_D^2 = \frac{4\pi e^2}{\epsilon_0 \epsilon_r} \left[ \frac{N_D}{C} F_{-1/2}(\eta_D) + \frac{N_A}{C} F_{-1/2}(\eta_A) + \dots \right]$$

FOR GENERAL N AND P.

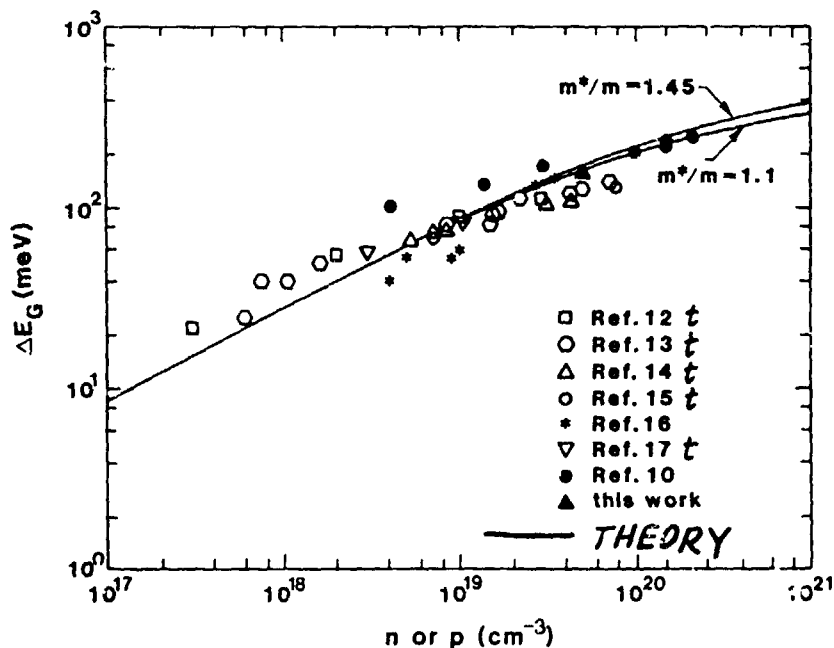
FOR LOW CONCENTRATIONS, FERMI INTEGRALS BECOME EXPONENTIALS:

$$k_D^2 = \frac{4\pi e^2}{\epsilon_0 \epsilon_r} (N_D + N_A) / kT$$

OR, FOR DEGENERATE DENSITY N,

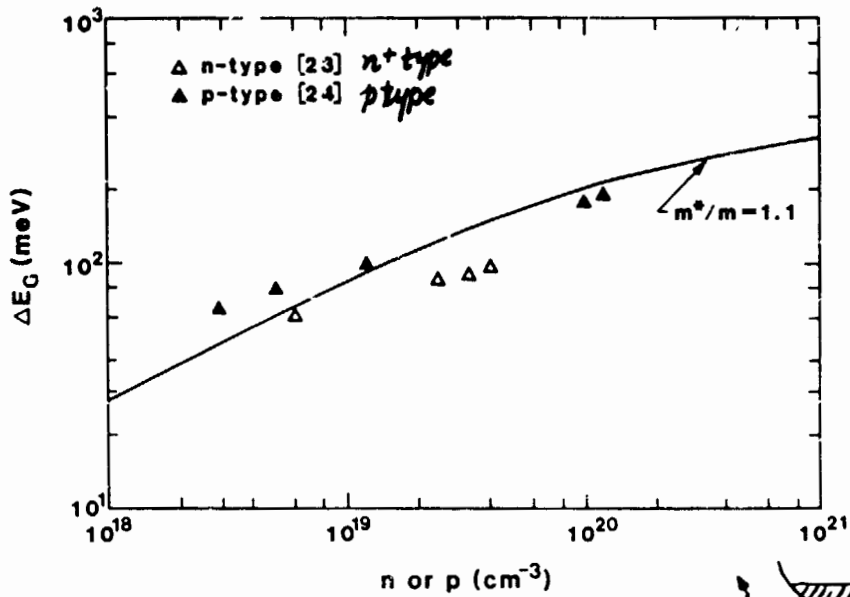
$$k_D^2 = \left( \frac{3}{\pi} \right)^{1/3} \left( \frac{2m^*}{\hbar^2} \right)^{2/3} \left( \frac{2}{\pi} \right)^{1/3} N^{1/3}$$

MKS unit  
( $4\pi$  of CGS taken out.)

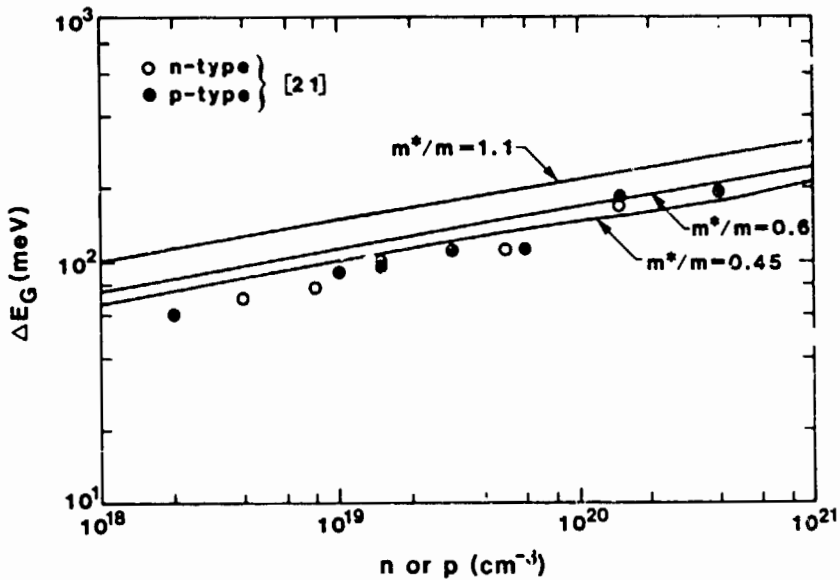
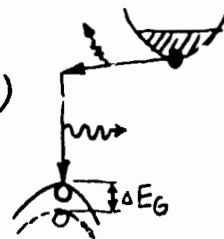


Comparison with minority carrier transport or 'pn' product measurements in bipolar devices: diodes, transistors.

# HIGH-EFFICIENCY SILICON SOLAR CELL RESEARCH



Luminescence data (Dumke)  
 at 300K  
 23. Dumke, APL 42, 196, (1983)  
 24. Dumke, JAP 54, 3200 (1983)



5K photoluminescence and excitation data  
 Wagner PR B29, 2002 (1984)

HIGH-EFFICIENCY SILICON SOLAR CELL RESEARCH

2. MEASUREMENT OF  $S_{BSF}$  AND  $\tau_B$  IN QUASINEUTRAL BASE OF BSF CELLS

ESSCD  $\leftrightarrow$  slope & intercept

1. REPORT IMPROVED ESSCD: ELECTRICAL SHORT-CIRCUIT CURRENT DECAY BY USE OF FAST MOS TRANSISTOR SWITCH (10 ns.).
2. ADVANTAGE OF ESSCD VS OPEN-CIRCUIT VOLTAGE DECAY, REVERSE STEP RECOVERY, ETC. IT AVOIDS INFLUENCE OF HOLES & ELECTRONS IN P/N SCR BY FORCING DENSITIES TO EQUILIBRIUM VALUES IN 10 ps.
3. TO MEASURE  $S$  AND  $\tau$  IN BASE YOU NEED SLOPE OF  $\log v(t)$  AND ONE OTHER PIECE OF DATA. THIS IS BEST PROVIDED BY  $Y(j\omega, V) =$  ADMITTANCE MEASURED ON BRIDGE.  $Y$  PROVIDES TWO THINGS:
- (A) SEPARATION OF  $Q_{NB}$  FROM  $Q_{NB}$  I BY CHANGING  $\omega$ .
  - (B) CONFINEMENT OF  $Y$  RESPONSE TO VOLUME (NOT SURFACE) FOR LARGE  $\omega$ ; THUS CAN GET  $\tau$  EVEN IF  $DIFF. LENGTH > BASE THICKNESS.$

ESSCD

$G_{QN}$  VS  $\omega$

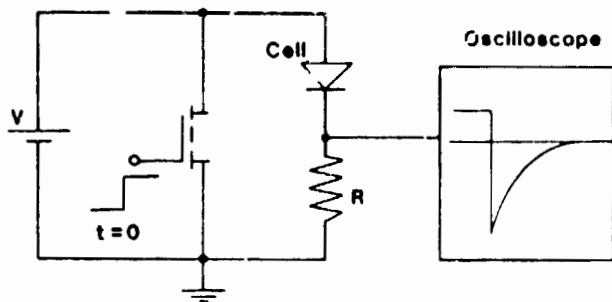
$C_{HF} - C_{LF} \rightarrow \tau_B$

$Y(\omega)$  actually  $-C_{HF} + C_{LF} = G_{QN}$  VS  $\omega$

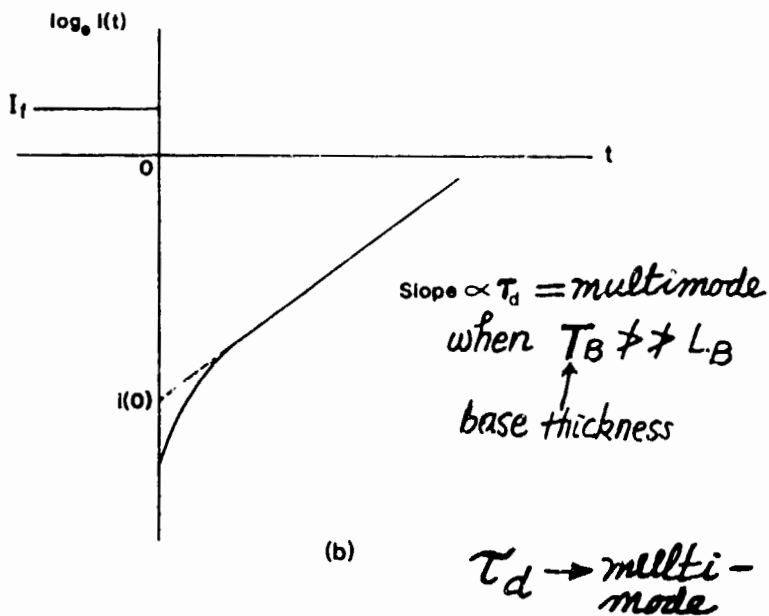
$G_{QN}$  VS  $\omega$



# HIGH-EFFICIENCY SILICON SOLAR CELL RESEARCH

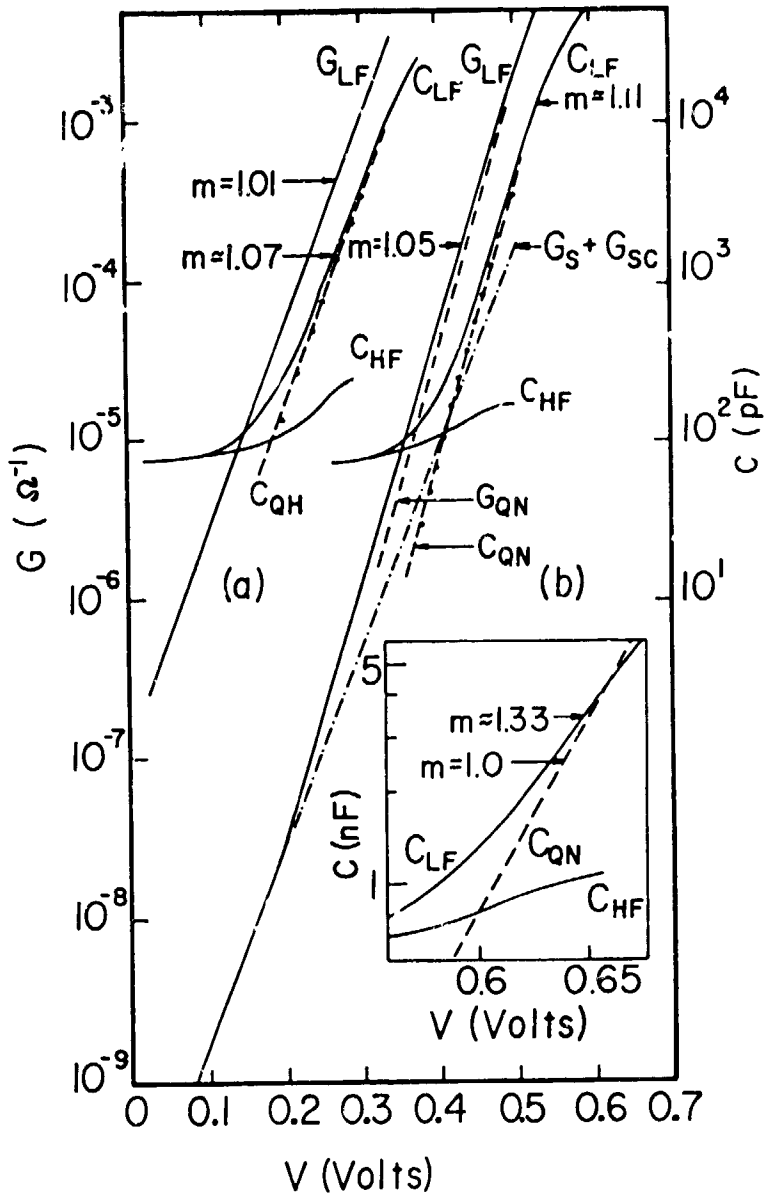


(a)

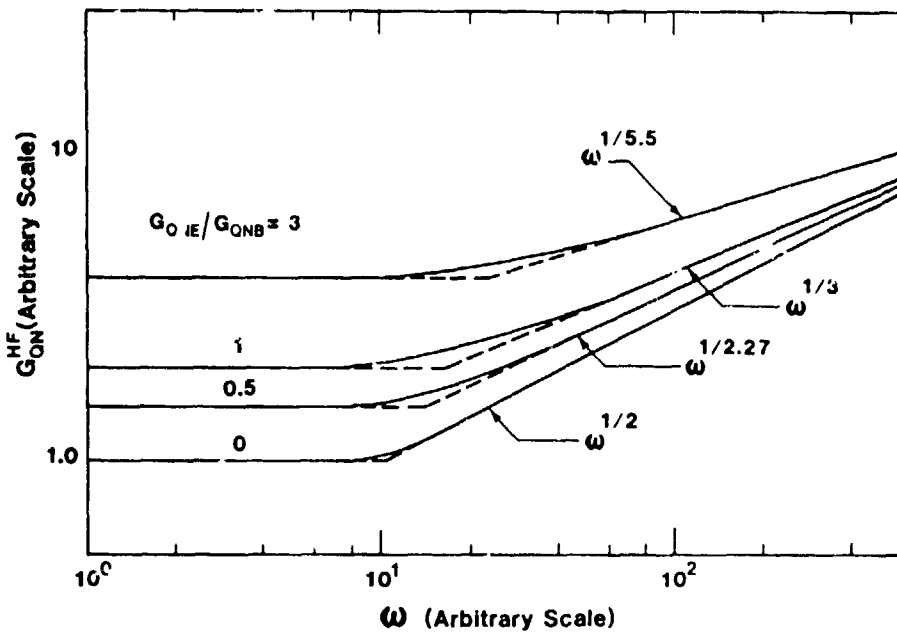


(b)

# HIGH-EFFICIENCY SILICON SOLAR CELL RESEARCH



# HIGH-EFFICIENCY SILICON SOLAR CELL RESEARCH



## Recommendations

- 1. USE ~~NEW~~ <sup>OLD-RENEWED</sup> ENERGY GAP MODEL IN COMPUTER SIMULATION.  $\Delta E_G$
  - 2. USE ESSCD +  $Y(j\omega, V)$  FOR  $\tau_B$  AND  $S_{BSF}$
- NEAR TERM EFFORTS:
- 1. NEW EXPERIMENTS TO EXPLORE ENERGY GAP MODEL FURTHER.  $\Delta E_G$
  - 2. ADAPT  $S_E$  AND  $\tau_E$  MEASUREMENTS TO EMITTER, USING  $Y(j\omega)$ .
  - 3. THEORY TO ACCOUNT FOR  $\Delta E_D$  &  $\Delta E_A$  IMPURITY BAND INFLUENCE FOR MODERATELY HIGH DENSITIES:  $10^{18}$
  - 4. ACCOUNT FOR HOLES AND ELECTRONS IN SCR TO IMPROVE ACCURACY OF OPEN-CIRCUIT VOLTAGE DECAY  $C_{SCR}$   $G_{SCR}$
- 1.  $\Delta E_G, \oplus \Delta E_D + \Delta E_A$
  - 2.  $S_{BSF}, \tau_B, \oplus S_E, \tau_E$