# SILICON SHEET N85-32442 ANALYSIS OF INCLINED GROWTH OF SILICON SHEET

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**Program Goals** 

- DEVELOP A GENERAL-PURPOSE FINITE ELEMENT PROGRAM FOR ANALYSIS OF SILICON SHEET GROWTH IN INCLINED CONFIGURATIONS. VERIFY ANALYSIS WITH EXPERIMENTAL DATA OF OTHERS.
- USE PROGRAM TO STUDY PARAMETRIC SENSITIVITY OF VARIOUS GROWTH GEOMETRIES WITH RESPECT TO:
  - THERMAL CONTROL AND GROWTH RATE
  - DOPANT SEGREGATION
  - THERMAL STRESS

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- INTERFACE MORPHOLOGY AND INSTABILITY
- UNDETERSTAND TRANSITIONS IN INTERFACE MORPHOLOGY AND RELATIONSHIP TO DOPANT SEGREGATION.

#### Outline

- 1. THERMAI-CAPILLARY MODELING OF MENISCUS-DEFINED RIBBON-GROWTH
- 2. PREVIOUS RESULTS FOR EDGE-DEFINED FILM-FED GROWTH
- 3. PROTOTYPE MODEL FOR INCLINED RIBBON GROWTH
- 4. CALCULATIONS OF NONLINEAR MORPHOLOGICAL STRUCTURE

# SILICON SHEET

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## Prototype of Inclined Ribbon Growth



SOLUTION INVOLVES DETERMINING

- 1. TEMPERATURE FIELD IN MELT
- 2. MELT/CRYSTAL INTERFACE SHAPE
- 3. MELT/GAS INTERFACE SHAPE
- 4. CRYSTAL THICKNESS

## Complete Analysis of Meniscus-Defined Growth System Required

- Solution of energy equations in all phases (melt, crystal, die) and accurate account of radiative heat transport fo surroundings
- 2. DETERMINATION OF MELT/SOLID INTERFACE SHAPE
- CALCULATION OF MELT/GAS INTERFACE SHAPE TO SATISFY EQUATION OF HYDROSTATICS.
- 4. CALCULATION OF SHEET THICKNESS TO SATISFY EQUILIBRIUM GROWTH ANGLE.
- DEFINES A VERY COMPLEX NONLINEAR FREE-BOUNDARY PROBLEM. ALGORITHM FOR SOLUTION HAS ALREADY BEEN DEVELOPED.

### Strategy for Development of Analysis

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- COMPUTER-AIDED CALCULATIONS ARE BASED ON FINITE ELEMENT METHODS DEVELOPED FOR EFG SYSTEM IN COLLABORATION WITH RESEARCHERS AT MOBIL SOLAR ENERGY COMPANY.
- THERMAL STRESS ANALYSIS ALSO BASED ON FINITE ELEMENT SOLUTION OF NONLINEAR EQUATIONS FOR ELASTOPLASTIC DEFORMATION COUPLED WITH THERMAL-CAPILLARY HEAT TRANSFER ANALYSIS.
- COMPARISON WITH EXPERIMENTS WILL INTEGRATE HEAT TRANSFER BOUNDARY CONDITIONS APPROPRIATE FOR PARTICULAR GROWTH CONFIGURATION DIRECTLY INTO THE FINITE ELEMENT ANALYSIS.