

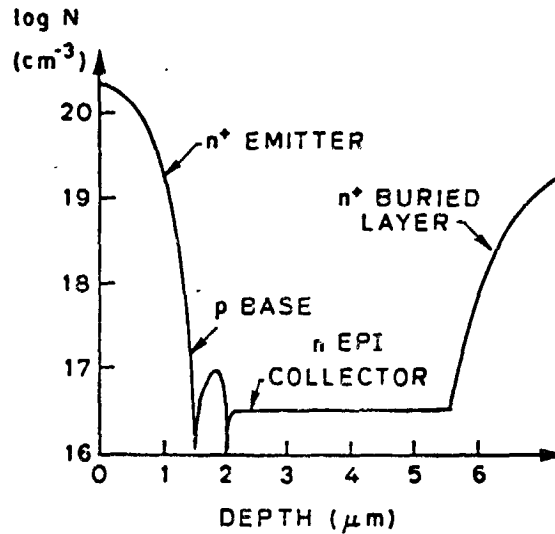
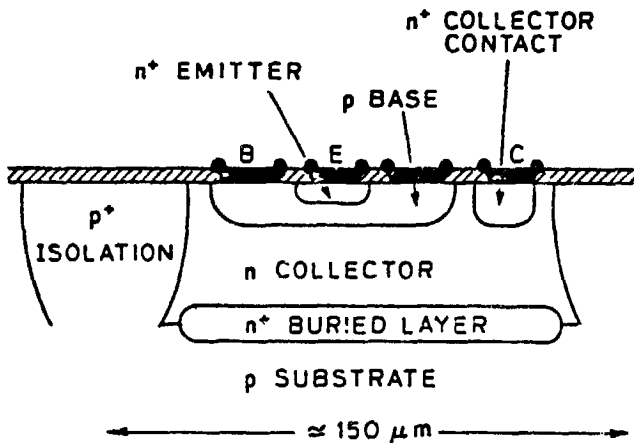
MEASUREMENT OF MINORITY CARRIER TRANSPORT
PARAMETERS IN HEAVILY DOPED n-TYPE SILICON

STANFORD UNIVERSITY

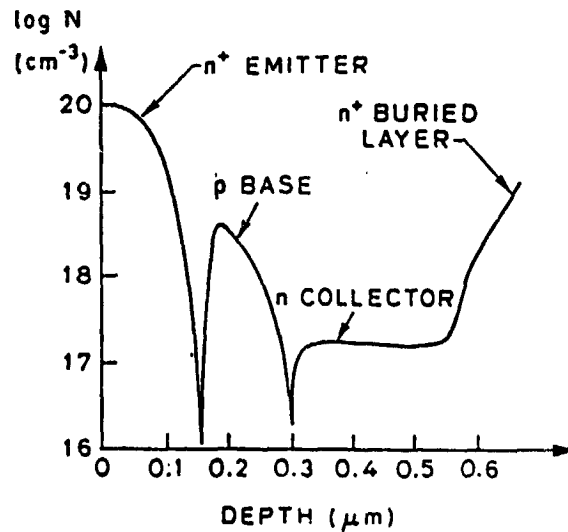
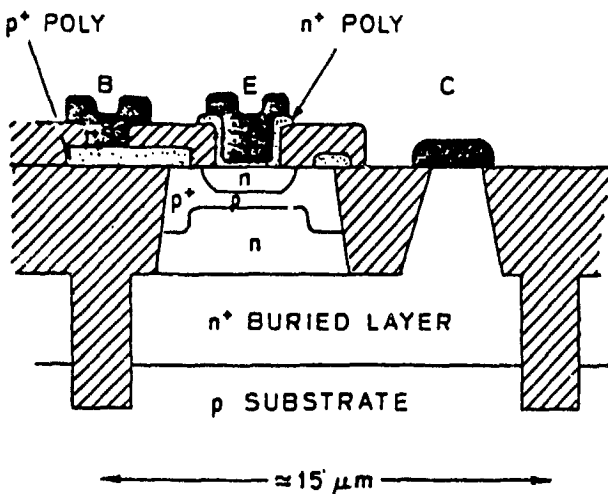
J. del Alamo
R.M. Swanson

Scaled Bipolar Devices

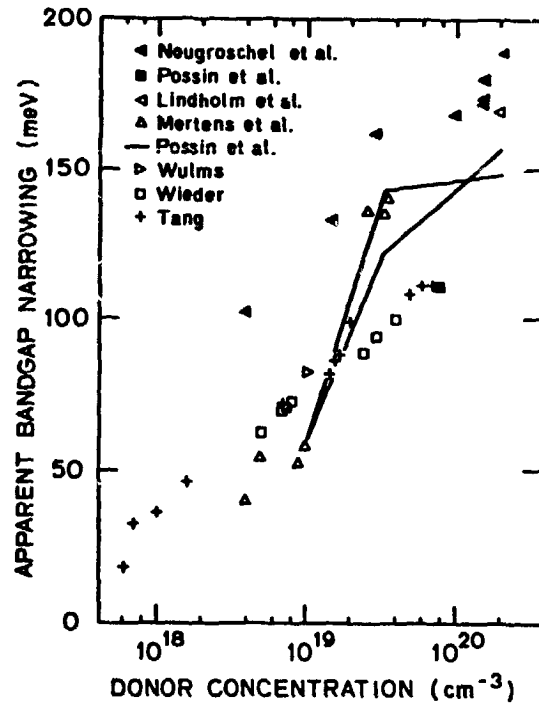
1970's



1980's



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Basic Transport Equations

Assumptions:

- n-type silicon
- steady state
- quasi-neutrality
- low injection
- 1-D

1. Hole current equation:

$$J_p = p\mu_p \frac{dF_{fp}}{dx}$$

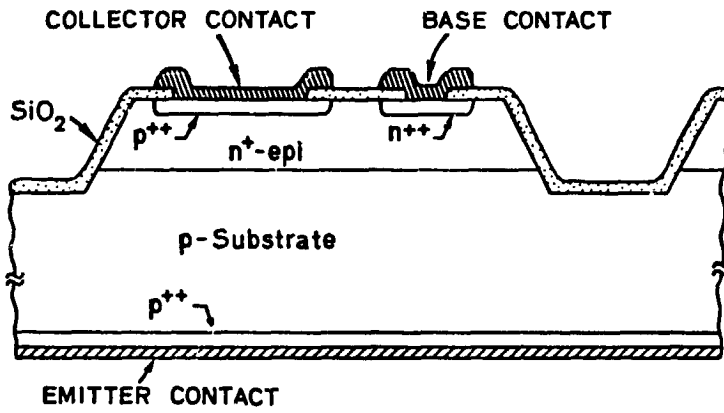
2. Hole continuity equation:

$$\frac{1}{q} \frac{dJ_p}{dx} = -R = -\frac{p - p_0}{\tau_p}$$

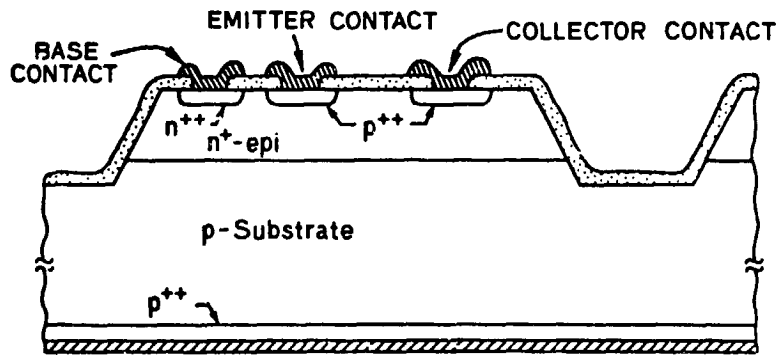
3. Hole density equation:

$$p = \int_{-\infty}^{\infty} \rho_v(E) [1 - f(E)] dE = p_0 \exp \frac{E_F - E_{fp}}{kT}$$

Vertical Transistor



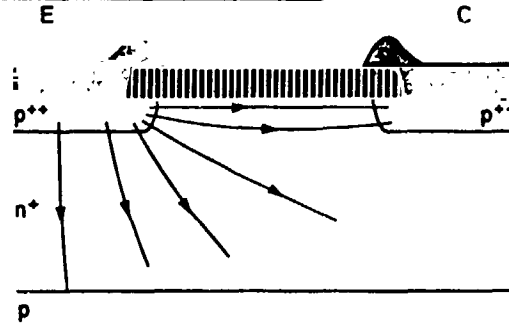
Lateral Transistor



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Lateral Transistors

Extraction of diffusion length



Collector current:

$$I_{oci} = qAF_L(p_o D_p) \left(\frac{1}{L_p} \right) \frac{1}{\sinh\left(\frac{W_{Bi}}{L_p}\right)}$$

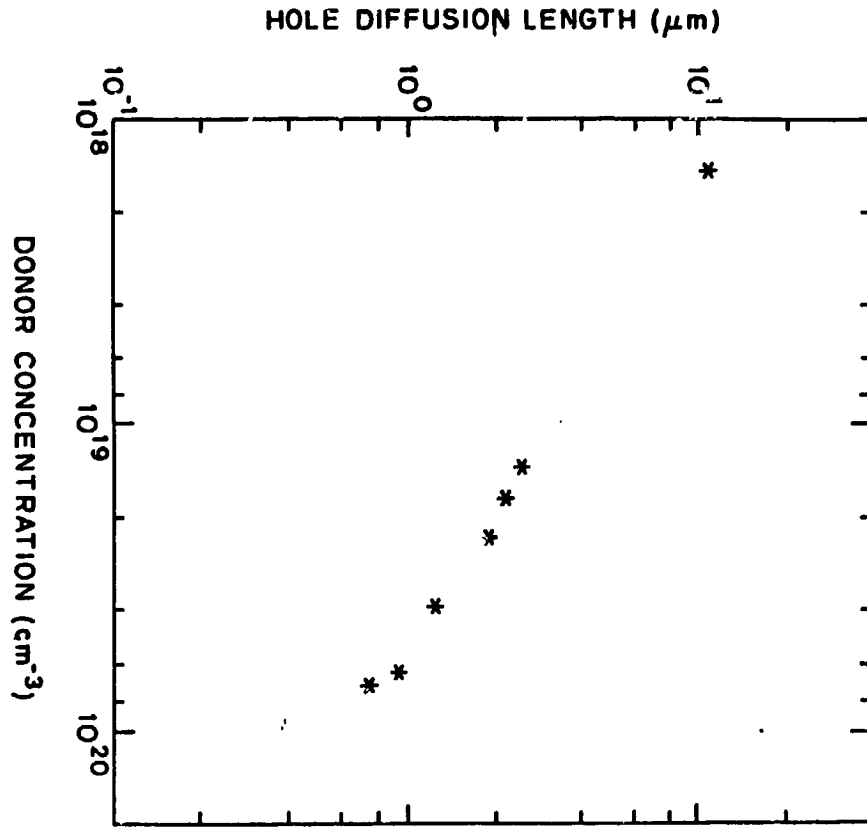
If $W_{Bi} \gg L_p$

$$I_{oci} = qAF_L(p_o D_p) \left(\frac{2}{L_p} \right) \exp - \left(\frac{W_{Bi}}{L_p} \right)$$

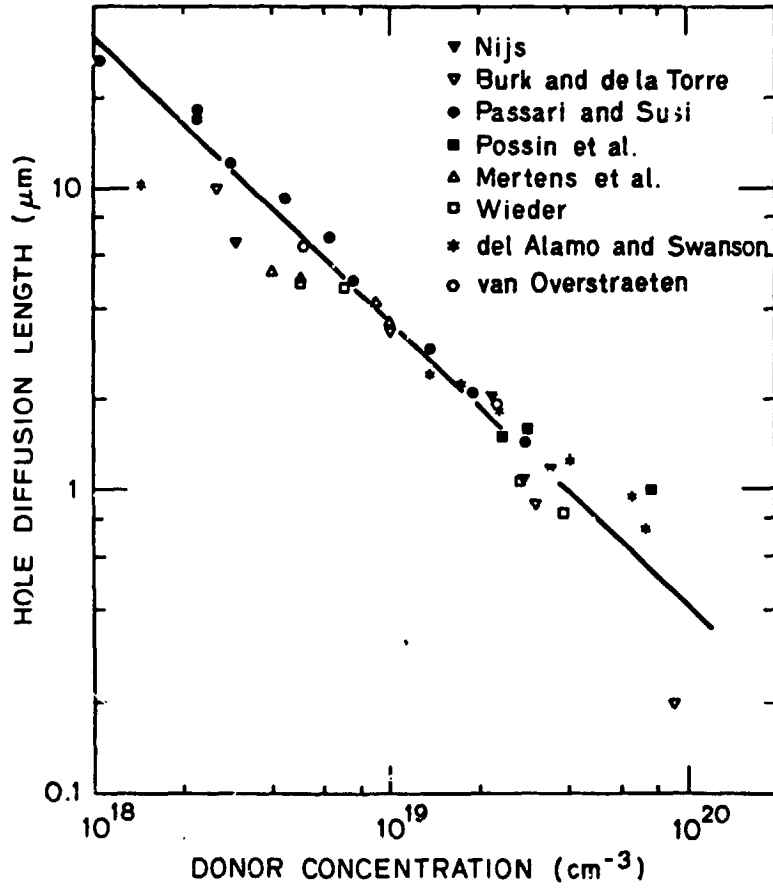
Then

$$\frac{I_{oci}}{I_{oc1}} = \exp - \left(\frac{W_{Bi} - W_{B1}}{L_p} \right)$$

HIGH-EFFICIENCY DEVICE RESEARCH

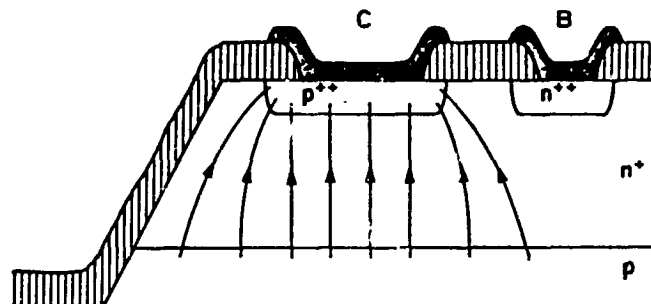


HIGH-EFFICIENCY DEVICE RESEARCH



Vertical Transistors

Measurement of $p_0 D_p$



Collector current:

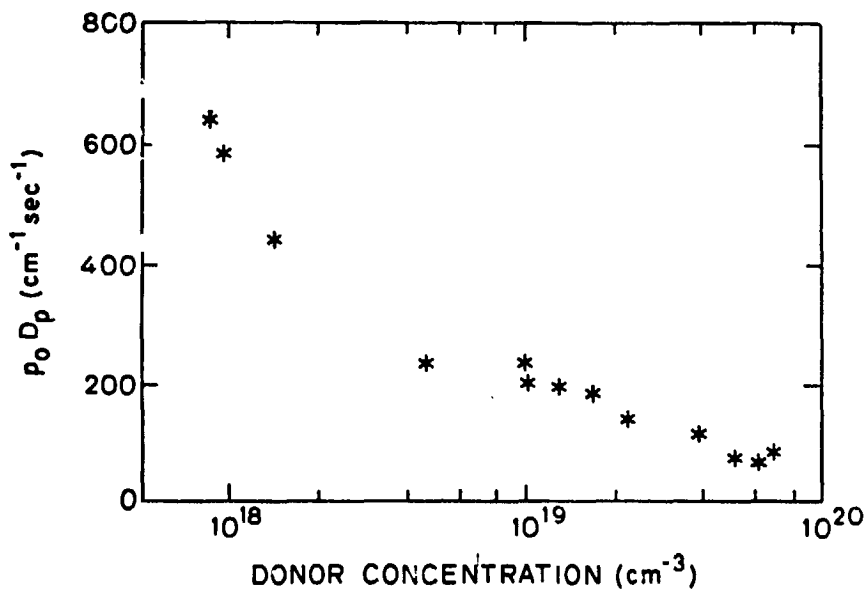
$$J_{oc} = p_0 D_p \left(\frac{1}{L_p} \right) \frac{1}{\sinh\left(\frac{W_B}{L_p}\right)}$$

If $W_B \ll L_p$

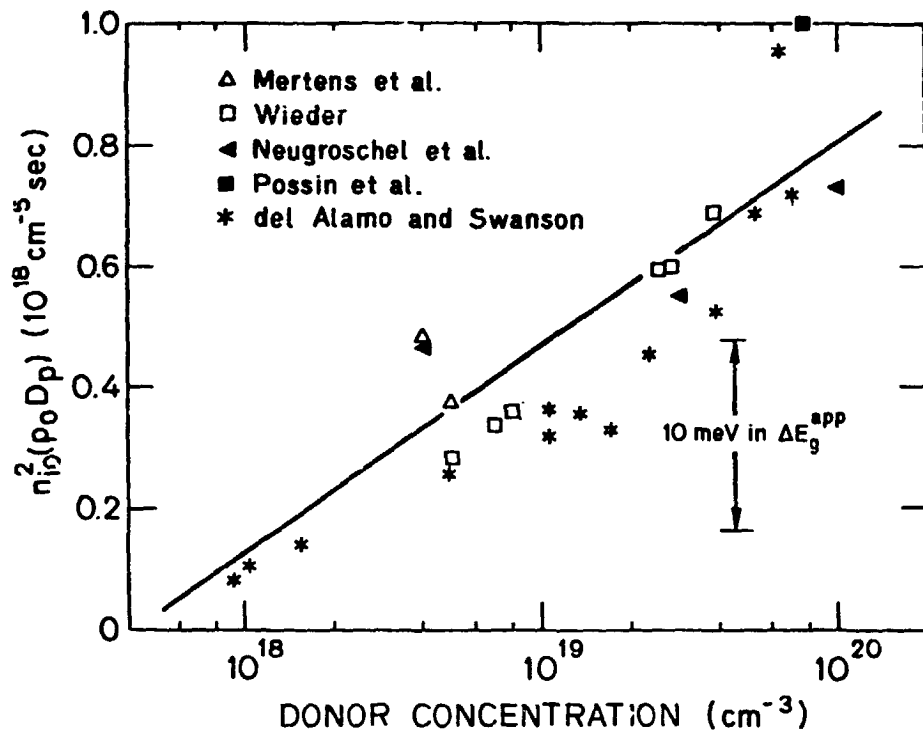
$$J_{oc} \approx p_0 D_p \frac{1}{W_B}$$

If $W_B \gg L_p$

$$J_{oc} \approx p_0 D_p \frac{2}{L_p} e^{-p - \frac{W_B}{L_p}}$$



HIGH-EFFICIENCY DEVICE RESEARCH



Authors	$N_d (cm^{-3})$	$x_j (\mu m)$	$J_o (A/cm^2)$	
			measured	calculated
Kwark and Swanson	3.3×10^{19}	1.0	8.3×10^{-13}	1.1×10^{-12}
Kwark and Swanson	4.6×10^{19}	0.66	1.1×10^{-12}	1.5×10^{-12}
Ning and Isaac	1.2×10^{20}	0.20	2.8×10^{-12}	2.8×10^{-12}
Patton and Plummer	2.1×10^{19}	0.20	3.2×10^{-12}	3.6×10^{-12}
Patton and Plummer	4.4×10^{19}	0.23	2.6×10^{-12}	2.6×10^{-12}

Conclusions

1. There are only two independent parameters that control minority carrier transport and recombination in heavily doped silicon: $p_0 D_p$ and L_p .
2. These parameters have been measured in heavily phosphorus doped silicon.
3. With the use of these measured parameters, accurate prediction of the emitter saturation current of bipolar transistors has been demonstrated.

