

## LIDAR MEASUREMENTS OF SLANT VISUAL RANGE

Yu.S.Balin, S.I.Kavkyanov, G.M.Krekov,  
I.A.Razenzov  
The Institute of Atmospheric Optics, Siberian  
Branch, USSR Academy of Sciences, Tomsk, 634055  
U S S R

When converting the lidar equation

$$P_z = A_z z^{-2} \beta_z T_{oz}^2 = A_z z^{-2} \beta_z \exp \left\{ -2 \int_0^z \sigma_z' dz' \right\} \quad (1)$$

relative to the extinction coefficient  $\sigma_z$  and, correspondingly, the visual range, one encounters the instability of solution at the increase of the optical density of the sounding path ( $P$  is the lidar signal from the distance  $z$ ,  $T_{oz}$  is the transmittance of the layer  $[0, z]$ ,  $\beta_z$  is the backscattering coefficient,  $A_z$  is the calibration function). The search for a stable solution has resulted in the appearance of a set of inversion algorithms differing mainly in the manner of assigning the a priori information on the profile sought [1]. The paper suggests a stable algorithm of inversion and gives a comparative analysis and experimental verification of some methods of processing the signals at sounding the optically dense atmospheric formations.

The solution of Eq.(1), relative to  $\sigma_z$ , has, as known, the form

$$\sigma_z = \Psi_z \left( \frac{\Psi_{z_k}}{\sigma_{z_k}} - 2 \int_{z_k}^z \Psi_z' dz' \right)^{-1} \quad \Psi_z = \frac{P_z z^2}{A_z g_z T_{oz}^2} \quad (2)$$

$g_z = \beta_z / \sigma_z$  is the lidar ratio,  $z_k$  is the reference (calibration) point, which can be chosen randomly along the sounding path  $[z_s, z_m]$ . The theoretical analysis and model calculations showed that the choice of a reference point  $z_k$  determines, in many respects, the stability of the solutions obtained. That is, the stability is the higher, the farther  $z_k$  is from the lidar. For  $z_k = z_m$  the solution of the form

$$\sigma_z = \Psi_z \left( \frac{\Psi_{z_m}}{\sigma_{z_m}} - 2 \int_{z_m}^z \Psi_z' dz' \right)^{-1} = \Psi_z \left( \frac{\Psi_{z_m}}{\sigma_{z_m}} + 2 \int_z^{z_m} \Psi_z' dz' \right)^{-1} \quad (3)$$

is most stable [1]. The similar conclusion has been arrived at by Klett [2]. His algorithm does not in fact differ from (3).

The main difficulty encountered when utilizing Eq.(3) is the necessity of measuring  $\sigma_{z_m}$  by an independent technique. The use, in this case, of logarithmic derivative (determination of  $\sigma_{z_m}$  based on the lidar-signal logarithm slope in the vicinity of  $z_m$ ) is problematical due to the instability of the method to random variations of the signal. The most admissible is the processing of li-

dar signals with the use of integral calibration when transmittance of a sufficiently large segment  $[\tau_0, \tau_m]$  is considered to be known. When  $\tau = \tau_m$  the solution has the form

$$\sigma_z = \frac{\psi_z}{2} \left( \varepsilon \int_{\tau_0}^{\tau_m} \psi_{z'} d\tau' + \int_{\tau}^{\tau_m} \psi_{z'} d\tau' \right)^{-1} \quad \varepsilon = (T_{\tau_0 \tau_m}^{-2} - 1)^{-1} \quad (4)$$

and is absolutely stable [1].

For approximately evaluating the parameter  $\varepsilon$ , one should use in Eq. (4) the lidar data together with different qualitative assumptions on the optical properties of the atmosphere along the path [1]. The simplest estimate  $T_{\tau_0 \tau_m}^2$  can be obtained by using the least-square method assuming the statistical homogeneity along the path

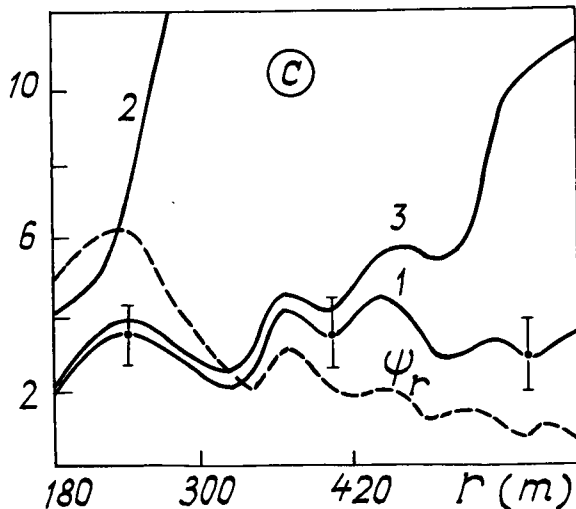
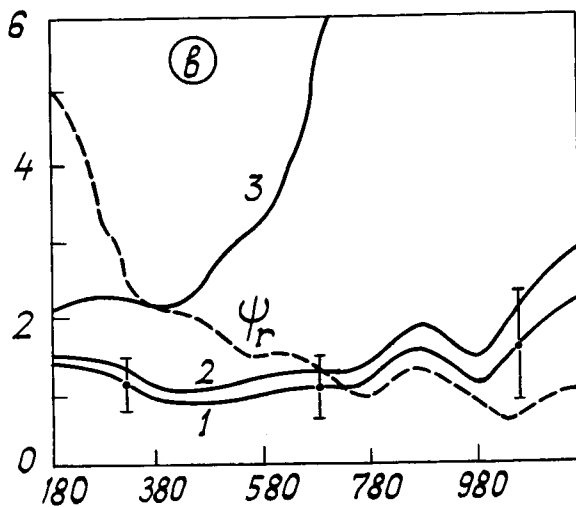
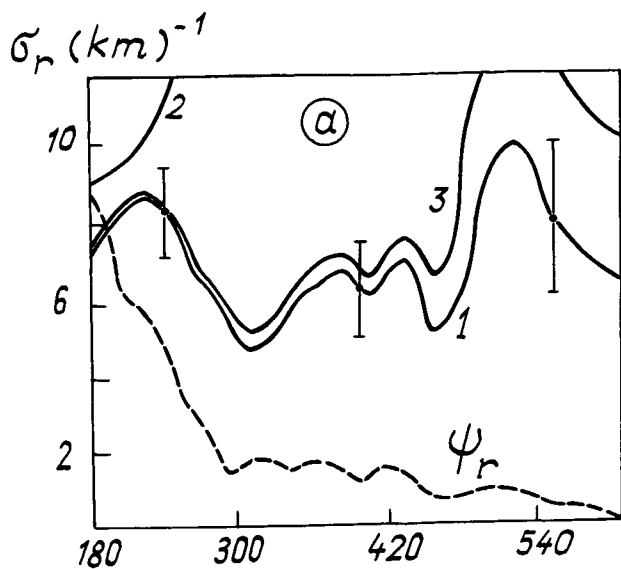
$$T_{\tau_0 \tau_m}^2 = \exp \left\{ -\frac{3}{(\tau_m - \tau_0)^2} \int_{\tau_0}^{\tau_m} (\tau - \tau_0) \ln \frac{\psi_{\tau_0}}{\psi_{\tau}} d\tau \right\} \quad (5)$$

Such an approximation is sufficient for the sounding paths close to horizontal.

The data on sounding fogs obtained with the use of lidar "LOZA-3" developed at the Institute of Atmospheric Optics was used to experimentally verify the algorithms (4,5). The sounding at  $\lambda = 0.53 \mu\text{m}$  was carried out in the horizontal direction with simultaneous monitoring for the optical state of the atmosphere with the photometer placed at the beginning of the path. Some results of these measurements are given in figures where the signals  $\psi_z$  and the profiles  $\sigma_z$  restituted with the use of the algorithm described (curves 1) are shown in relative units. The profiles  $\sigma_z$  restituted using Eq.(2) with the photometer calibration at the beginning of the path (curves 2) and using Eq.(3) in which  $\sigma_{\tau_m}$  value is determined using the method of logarithmic derivative (curves 3) are presented for comparison

$$\sigma_{\tau_m} = \frac{1}{2(\tau^* - \tau_m)} \ln \frac{\psi_{\tau_m}}{\psi_{\tau^*}} \quad (6)$$

In many cases the use of photometer calibration at the beginning of the path resulted, as it should be expected, in the solution divergence (Figs. a-c). The use of the value  $\sigma_{\tau_m}$  from (6) for calibration does not allow one to carry out stable processing, since in this case  $\sigma_{\tau_m}$  strongly depends on choice of the point  $\tau^*$  corresponding to the assumption on homogeneity  $\sigma_z$  at the segment  $[\tau^*, \tau_m]$ . If in Figs. a, c the value  $\sigma_{\tau_m}$  obtained from (6) can be considered valid, then the inhomogeneity at the end of the path for the case b leads to a negative value  $\sigma_{\tau_m}$  and divergence of the profile  $\sigma_z$ . The necessity in choosing a homogeneous segment of the path makes the automated processing of the results difficult. It should be noted that the use of some model value  $\sigma_{\tau_m}$  for calibration, as the calibrations showed, gives sufficient accuracy for large optical depths of the path  $\tau \approx 2$  only. In the range  $0.5 \leq \tau \leq 2$ , the most probable



at sounding fogs, the solution is quite critical to the accuracy of evaluation  $\sigma_r$ . The algorithms (4,5) gave stable results for all signal  $\psi_r$  realizations. Thus, the use of functional limitations to the type of the solution sought (in this case, the assumption on statistical homogeneity of the path) allows one to construct stable algorithms for processing the results. The use of the more detailed information on solution and noises [1] gives the possibility of obtaining optimal algorithms with wider application limits than those of algorithms (4,5).

#### References

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