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No. 689

TANDEM AIR PROPELLERS

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TANDEM AIR PROPELLERS

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## SUMMARY

Tests of 2-blade, adjustable-pitch, counterrotating tandem model propellers, adjusted to absorb equal power at maximum efficiency, were made at Stanford University.

The characteristics, for  $15^{\circ}$ ,  $25^{\circ}$ ,  $35^{\circ}$ , and  $45^{\circ}$  pitch settings at 0.75 R of the forward propeller and for 8-1/2 percent, 15 percent, and 30 percent diameter spacings, were compared with those of 2-blade and 4-blade propellers of the same blade form.

The tests showed that the efficiency of the tandem propellers was from 0.5 percent to 4 percent greater than that of a 4-blade propeller and, at the high blade-angle settings, not appreciably inferior to that of a 2-blade propeller.

It was found that the rear tandem propeller should be set at a blade angle slightly less than that of the forward propeller to realize the condition of equal power at maximum efficiency. Under this condition the total power absorbed by the tandem propellers was from 3 percent to 9 percent more than that absorbed by the 4-blade propeller and about twice that absorbed by a 2-blade propeller.

### INTRODUCTION

Tandem air propellers have been the subject of both experimental and theoretical investigations (references 1 to 5). The experimental studies for which data are available relate for the most part to tandem propellers separated by considerable distance, about one diameter, and with a body representing an engine nacelle between. The forward propeller was thus a tractor with interference in the rear, and rear propeller a pusher with interference forward of it.

At the request and with the financial assistance of the National Advisory Committee for Aeronautics, the present experimental study was carried out. The purpose was to determine the characteristics of tandem propellers under the condition of close spacing such as would be practicable with an engine having two concentric shafts geared together and with opposite directions of rotation.

While, in this case, the characteristics of the individual propellers of the tandem combination as well as the effect of each propeller upon the other might be of interest, the important consideration is the relation of the characteristics of the tandem combination as a whole to those of a single propeller designed to absorb the same power at the same angular velocity and speed of advance.

It is obvious that, for tandem propellers of the same form, size, and angular velocity, the division of power absorbed between them would depend primarily on the relation of blade angle. It seemed that an equal division of power under the usual conditions of operation might constitute an incidental advantage, since there would be no rolling moment due to propeller torque acting on the plane and the slipstream would be without twist. The condition that equal power should be absorbed by the two propellers at maximum efficiency of the combination was therefore arbitrarily chosen for determining the relation of pitch settings used for test.

## APPARATUS AND TESTS

Wind tunnel.- The experiments of this investigation were carried on in the wind tunnel of the Daniel Guggenheim Aeronautical Laboratory of Stanford University. This tunnel is of the Eiffel type with open throat 7-1/2 feet in diameter. The maximum wind velocity is 90 miles per hour.

<u>Dynamometer.</u> The propeller dynamometer is shown schematically in figure 1. It consists essentially of a long electric motor which is provided with a direct connected, right-hand rotation shaft  $S_1$  and a geared, left-hand rotation shaft  $S_2$ . The whole assembly is mounted on knife edges below the shaft axis and is restrained from rolling by the torque arm A. The spider that carries the pinions of the bevel gear train is restrained from turning about the shaft axis by a second torque arm B.

The right-hand propeller  $P_1$  is keyed to shaft  $S_1$ and the left-hand propeller  $P_2$ , to shaft  $S_2$ . Any desired spacing of the propellers is obtained by moving  $P_1$ along its shaft.

The right- and left-hand shafts are restrained from relative axial movement by thrust bearings, but the whole shaft assembly is free from longitudinal constraint. The total thrust is measured by a weighing device connected to a thrust bearing carried on shaft  $S_1$ .

The dynamometer is shielded by a sheet-metal cover from wind forces other than those acting upon the propellers.

For this arrangement it can be shown that

$$Q_{A} = Q_{P_{1}} + Q_{P_{2}} + Q_{F}$$
(1)

and

$$Q_{\rm B} = 2Q_{\rm P} + Q_{\rm F} \tag{2}$$

- where  $Q_A$  is restraining torque acting through torque arm A.
  - $Q_{P_1}$ , torque due to air forces acting on propeller  $P_1$ .
  - $R_{P_3}$ , torque due to air forces acting on propeller  $P_2$ .
    - Q<sub>F</sub>, torque required to turn shafts against a combination of frictional resistances in the dynamometer bearings.
    - $Q_B$ , restraining torque acting through torque arm B.

From (1) and (2)

 $q_{P_1} - q_{P_2} = q_A - q_B \tag{3}$ 

and

$$Q_{P_1} + Q_{P_2} = Q_A - Q_F \tag{4}$$

If the left-hand propeller, P2, alone is on the shaft

$$Q_A = Q_{P_2} + Q_F$$
  
 $Q_B = 2Q_{P_2} + Q_F$ 

hence for this case

$$Q_{\rm F} = 2Q_{\rm A} - Q_{\rm B} \tag{5}$$

Figure 2 shows the appearance of the forward end of the dynamometer. It may be seen that the model propellers are well forward, actually one and one-half diameters, of any considerable slipstream obstruction.

Model propellers. - The propellers used in these tests were all 3-foot diameter metal models of standard U.S. Navy plan form and blade section. One was right-hand, 2-blade; another, left-hand, 2-blade; and the third, right-hand, 4blade. Blades of all were adjustable in pitch. The geometrical pitch-diameter ratio, for a setting of 16.6° at 0.75 R, was 0.7 from 0.6 R outward to the tip. It gradually decreased from 0.6 R toward the hub to a value of 0.42 at 0.15 R. The plan form, the sections, and the pitch distribution were those of propeller E in reference 6.

<u>Tests.</u> Tests of the right- and left-hand 2-blade propellers and the 4-blade propeller were made at bladeangle settings for 0.75 R of  $15^{\circ}$ ,  $25^{\circ}$ ,  $35^{\circ}$ , and  $45^{\circ}$ .

In the tests of single propellers the torque arm B (fig. 1) and the pinions of the bevel gear train were removed. The two shafts were then locked together. The balance connected to torque arm A thus indicated the air-force torque on the propeller alone, the friction torque  $Q_{\rm p}$  being eliminated.

Tests of the tandem propellers were made with the right-hand propeller in the forward position and set at blade angles for 0.75 R of  $15^{\circ}$ ,  $25^{\circ}$ ,  $35^{\circ}$ , and  $45^{\circ}$ . The left-hand propeller was set at a blade angle such that the two propellers absorbed equal power at maximum efficiency for the combination. The method of realizing this condition is shown in figure 3. With the forward propeller set at  $25^{\circ}$  and the rear propeller set first at  $25^{\circ}$  and later at

24°, the differences in power coefficient of the forward and rear propellers were determined and plotted as functions of V/nD. At V/nD = 0.9, maximum efficiency of the 25° 2-blade propeller alone, the value of  $C_p$ (RH-LH) is seen to be -0.0023 for the 25° setting of the rear propeller and 0.0045 for the 24° setting. By interpolation the setting of the rear propeller that would give equal power at V/nD = 0.9 was estimated to be 24.7°.  $C_p$  (RH-LH) for the 24.7° setting of the rear propeller is also shown in figure 3. It is seen to be zero at V/nD = 0.9.

In the foregoing tost it was assumed that V/nD for maximum efficiency of the tandem combination would be the same as for a single propeller having a pitch setting equal to that of the forward propeller of the tandem pair. This assumption was later justified. (See figs. 4 and 7.)

Three spacings of the tandem propellers were used; 8-1/2 percent, 15 percent, and 30 percent of propeller diameter, center to center of blade shanks. Originally it was planned that a closer spacing of 7-1/2 percent diameter would be employed, but propeller hubs and necessary bearings between them limited the minimum spacing to the 8-1/2 percent diameter.

For the tests of the tandem propellers, it was necessary to determine the friction torque  $Q_F$  in order to measure the total wind force torque  $Q_{P_1} + Q_{P_2}$ . Preliminary tests showed that friction torque was independent of torque load in the form of a couple with its center at the shaft axis but that it depended primarily on rotational speed and oil viscosity; the oil viscosity was a function of the temperature.

The tandem propeller tests therefore consisted of alternate runs of the left-hand rear propeller alone and of the two propellers in tandem. From the observations of  $Q_A$  and  $Q_B$  for the single propeller runs,  $Q_F$  was computed by equation (5) and plotted against time. Values of  $Q_F$  for the intermediate runs with tandem propellers were then taken from a fair curve drawn through the plotted points. Uniform time intervals were used in corresponding operations of consecutive observations.

Following the Stanford laboratory practice, a constant

angular velocity was used for each test. Variation in the parameter V/nD was secured through change of the wind velocity. Because of limitations imposed by wind speed and by power and rotational speed available in the dynamometer, the rotational speeds employed were 2,000, 1,800, 1,500; and 1,100 revolutions per minute for the 15°, 25°, 35°, and 45° blade-angle settings, respectively. Assuming that the full-scale propeller would be 9 feet in diameter and would operate at 2,000 r.p.m., the Reynolds Number of the tests was thus from 0.11 to 0.05 full scale.

The observations of the tests were reduced to the usual coefficients

$$C_{T} = \frac{T}{\rho n^{2} D^{4}}$$

$$C_{P} = \frac{P}{\rho n^{3} D^{5}}$$

$$\Omega = \frac{T \times V}{P} = \frac{C_{T}}{C_{D}} \times \frac{V}{nD}$$

$$\sigma = \frac{5}{\rho T^{5}} = \frac{V}{nD} \sqrt{\frac{5}{C_{P}}}$$

where T is propeller thrust.

- ρ, mass density of the air.
  - η, revolutions per unit time.
  - D, propeller diameter.
  - P, power absorbed.
  - V, velocity.

# RESULTS AND DISCUSSION

The propeller coefficients derived from the observa-

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tions of these tests are given in table I. For the tandem propellers,  $C_P$  and  $C_s$  are coefficients computed for the total power of the tandem pair as  $C_T$  is a coefficient computed for the total thrust.  $C_P$  (RH-LH) is the difference between the power coefficient of the forward (right-hand) and rear (left-hand) propellers. The coefficients  $C_T$ ,  $C_P$ , and  $\gamma$  are shown graphically as functions of V/nD in figures 4 to 8. In addition, working charts for design selection of 2-blade, 4-blade, and tandem propellers are included in figures 9 to 11. The method of using these charts is described in reference 7, and a curve of  $C_P$  has been included for convenience in calculation of the thrust of automatic propellers at low air speeds. The final figure 12 compares a selected tandem-propeller combination with the 4-blade propeller.

From figures 4 and 5 it may be seen that the results of tests of the right-hand and left-hand 2-blade propellers at the same blade-angle settings are not identical. The right-hand propellers appear to absorb slightly smaller power and to have somewhat greater peak efficiency, particularly for the lower blade-angle settings. Micrometer measurements revealed that the right-hand blades were appreciably thinner than the left-hand, possibly enough to account for the difference in power coefficients found. The results for right-hand and left-hand propellers are, however, probably as nearly the same as could be expected from blades produced by the best commercial practice. For all practical purposes, the right- and the left-hand propellers may be regarded as identical.

In order to realize the condition of equal power at maximum efficiency in tandem propellers, it was found in all cases except that of the  $15^{\circ}$  setting the rear propeller should be set at the smaller blade angle. Eiffel's tests (reference 5) gave similar results. These present tests show that the difference in blade-angle setting required is a function of blade angle itself. For the  $15^{\circ}$ setting no difference was found, while for  $25^{\circ}$ ,  $35^{\circ}$ , and  $45^{\circ}$ , the differences were  $0.3^{\circ}$ ,  $0.6^{\circ}$ , and  $1.1^{\circ}$ , respectively. In some cases it was found impracticable to realize, exactly, the condition of equal power at maximum efficiency. It was attained, however, within the limitations imposed by minimum observable change in blade angles, about  $0.1^{\circ}$ , and by probable error in difference of torque, about 0.02 lb. ft.

The data of figure 8 show that the spacing of tandem propellers has little effect upon the characteristics of the combination. With respect to efficiency the 15-percent diameter spacing appears somewhat better than the closer spacing of 8-1/2 percent diameter. The 30-percent spacing is but little, if any, better than 15 percent. It may be noted that thrust developed and power absorbed by the tandem propellers increase slightly with the spacing. This result may be accounted for by the increase in blade-angle setting of the rear propeller required to maintain the condition of equal power at maximum efficiency as spacing is increased.

Effects of spacing, practically identical to the foregoing, were observed for the tandem propellers at  $35^{\circ}$  bladeangle setting of the forward propeller. Since the 15-percent diameter spacing appeared definitely better than 8-1/2percent and not appreciably worse than 30 percent for these two cases, only the 15-percent spacing was investigated for the forward propeller at  $15^{\circ}$  and  $45^{\circ}$ .

One incidental effect of close spacing was observed. At 8-1/2 percent the tandem propellers were extremely noisy. At 15 percent the sound was noticeably more than that produced by a 4-blade propeller of the same pitch, whereas, at 30 percent, it was but little louder to the ear than for a 4-blade propeller.

For corresponding blade-angle settings of 2-blade propellers and the forward blades of the tandem propellers, (compare, for example, figs. 4 and 7, and figs. 9 and 11) tandem propellers are generally less efficient than 2-blade propellers. The difference in maximum efficiency varies inversely with the blade-angle setting. It is about 4 percent at  $15^{\circ}$  and 0.5 percent at  $35^{\circ}$ . For  $45^{\circ}$  the tandem propellers appear to have a maximum efficiency about 0.5 percent greater than the 2-blade propeller. In the climbing range, taken arbitrarily at 0.75 V/nD for maximum efficiency, the tandem propellers show about 5 percent less efficiency than the 2-blade propellers for the  $15^{\circ}$  setting but about 2.5 percent greater efficiency than the 2-blade propellers for the  $45^{\circ}$  setting.

At maximum efficiency, the power absorbed by the tandem propellers is from 1.87 to 1.97 times that absorbed by a 2-blade propeller. In the climbing range, the ratios are from 1.97 to 2.09. In each case the smaller ratio applies to the lower setting.

Comparison of the efficiency curves of the tandem and 4-blade propellers (fig. 12) shows that, under practically all conditions of operation, the tandem propellers are somewhat more efficient. At maximum efficiency, the difference in favor of the tandem propellers is from 0.5 to 1.5 percent. In the climbing condition it becomes 2.5 percent for the 45° blade-angle setting.

At maximum efficiency the tandem propellers absorb from 3 to 5 percent more power than the 4-blade propellers. In the climbing condition the difference is from 4 to 9 percent. In both cases the high blade-angle propellers show the greater difference.

The preceding comparisons of power and efficiency are made at equal values of V/nD. Since the tandem propellers absorb greater power than 4-blade propellers, however, a more significant basis for comparison of efficiency is at equal values of the speed-power coefficient  $C_g$ . Figure 12 shows the efficiencies of the  $45^{\circ}$  4-blade and  $45^{\circ}$  to  $43.9^{\circ}$  tandem propellers as functions of the speed-power coefficiency of  $C_g$  throughout the working range, the efficiency of the tandem propellers is appreciably greater. The maximum difference is about 4 percent. The gain in efficiency for this case is the largest found. For smaller blade-angle settings it becomes progressively less and is negligible, about 0.5 percent, at  $15^{\circ}$ .

## CONCLUSIONS

These tests have shown that identical, counterrotating, 2-blade, close-spaced, tandem propellers, adjusted in pitch to absorb equal power at maximum efficiency have from 0.5 percent to 4 percent greater efficiency than that of 4blade propellers of the same blade form and designed to absorb the same total power.

Tandem propellers are inferior in efficiency to single 2-blade propellers for blade-angle settings at 0.75 R of less than 35°. For higher blade-angle settings, the tandem propellers have an appreciable advantage.

Tandem propellers absorb from 3 percent to 9 percent more power than 4-blade propellers and about twice the power of 2-blade propellers of equal diameter.

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Daniel Guggenheim Aeronautical Laboratory, Stanford University, July 14, 1937.

# Table 1. Continued on following pages.

## TABLE I PROPELLER COEFFICIENTS

2 -Blade Right-Hand Propeller 15° at 0.75 B

	1	10 40 0.10	n				20° at 0.75 R		
V/nD	CT	ç ş	Cs	η	V/nD	CT	CP	Cs	η
0.740	0.0040	0.0103	1.848	0.291	1.181	0.0033	0.0160	2.700	0.240
.716	.0085	.0126	1.717	.482	1.140	.0110	.0218	2.451	.577
.681	.0153	.0160	1.557	.653	1.086	.0192	.0289	2.207	.720
.646	.0206	.0186	1.433	.718	1.040	.0275	.0361	2.022	.792
.626	.0248	.0204	1.364	.760	.994	.0350	.0418	1.877	.832
.600	.0290	.0226	1.280	.771	.944	.0409	.0464	1.745	.830
.568	.0334	.0241	1.197	.787	.898	.0479	.0515	1.626	.836
.529	.0395	.0265	1.094	.789	.854	.0536	0548	1.527	.835
.509	.0423	.0276	1.043	.780	.803	.0604	.0586	1.417	.828
.478	.0463	.0285	.974	.775	.767	.0641	.0609	1.342	.807
.449	.0499	.0294	.909	.761	.718	.0699	.0632	1.248	.794
.420	.0537	.0305	.845	.740	.667	.0776	.0662	1.148	,782
.390	.0571	.0312	.780	.713	.612	.0823	.0673	1.050	.748
.348	.0622	.0323	.692	.672	.540	.0898	.0684	.924	.709
.302	.0673	.0329	.598	.617	.500	.0927	.0682	.855	.680
.222	.0754	.0330	.439	.507	.430	.0962	.0705	.731	.586
					.328	.0966	.0718	.556	.442
			Section 1	13	.233	.0947	.0751	.391	.294

TABLE I - Continued

2 -Blade Right-Hand Propeller

#### TABLE I - Continued

## 2 -Blade Right-Hand Propeller

		35° at 0.75 R	in the second				45° at 0.75	R	
V/nD	CT	°P	Cs	η	V/nD	°T	CP	Cs	η
1.620	0.0219	0.0555	2.889	0.639	2.254	0.0286	0.1034	3.550	0.623
1.571	.0275	.0616	2.744	.700	2.170	.0375	.1170	3.335	.696
1.518	.0352	.0705	2.580	.758	2.103	.0448	.1282	3.173	.735
1.454	.0439	.0799	2.411	.794	2.040	.0521	.1387	3.027	.759
1.395	.0514	.0879	2.268	.816	1.959	.0596	.1493	2.867	.782
1.335	.0589	.0950	2.137	.826	1.888	.0662	.1574	2.732	.794
1.255	.0666	.1018	1.984	.822	1.813	.0737	.1665	2.595	.802
1.205	.0726	.1070	1.884	.817	1.740	.0804	.1745	2.469	.802
1.141	.0805	.1124	1.767	.814	1.656	.0864	.1818	2.329	.787
1.067	.0851	.1163	1.641	.780	1.577	.0888	.1858	2.210	.754
1.009	.0894	.1191	1.544	.757	1.492	.0910	.1863	2.089	.729
.940	.0910	.1209	1.435	.708	1.408	.0891	.1840	1.977	.682
.874	.0932	.1210	1.333	.674	1.321	.0899	.1835	1.855	.648
.817	.0930	.1220	1.244	.623	1.227	.0914.	.1837	1.723	.611
.739	.0939	.1225	1.126	.566	1.136	.0928	.1846	1.593	.571
.675	.0952	.1246	1.024	.516	1.044	.0933	.1856	1.462	.525
.600	.0962	.1272	.907	.454	.923	.0941	.1906	1.285	.456
.529	.0984	.1299	.796	.401	.824	.0944	.1934	1,145	.403
.440	.0991	.1345	.657	.324	.713	.0944	.1970	.987	.342
.314	.1025	.1395	.466	.230	.559	.0984	.2075	.766	.265

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TABLE I - Continued

2 -Blade Right-Hand Propeller

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#### H.A.O.A.

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Table 1. Continued.

### TABLE I - Continued

### 2 -Blade Left-Hand Propeller

# TABLE I - Continued

2 -Blade Left-Hand Propeller

	and the second	15° at 0.75	R	A ANTARY			25° at 0.75	R	
V/nD	CT	CP	Cs	η	V/nD	CT	CP	Cs	η
0.757	0.0007	0.0080	1.988	0.071	1.178	0.0042	0.0182	2.624	0.272
.717	.0089	.0126	1.719	.507	1.129	.0143	.0271	2.323	.595
.674	.0165	.0167	1.528	666	1.081	.0232	.0350	2.113	.714
.630	.0239	.0204	1.372	.737	1.027	.0317	.0416	1.940	.786
.599	.0294	.0230	1.274	.766	.974	.0390	.0466	1.798	.816
.565	.0347	.0253	1.178	.774	.914	.0470	.0519	1.653	.827
.544	.0376	.0263	1.126	.776	.858	.0545	.0562	1.527	.832
.510	.0429	.0280	1.043	.781	.796	.0621	.0605	1.394	.817
.478	.0479	.0297	.967	.770	.732	.0696	.0637	1.269	.799
.444	.0531	.0313	.888	.752	.674	.0776	.0674	1.156	.776
.416	.0561	.0322	.827	.724	.592	.0861	.0688	1.012	.741
.368	.0617	.0332	.727	.684	.519	.0932	.0693	.886	.698
.326	.0668	.0336	.643	.648	.457	.0946	.0706	.776	.614
.282	.0707	.0341	.554	.584	.405	.0922	.0740	.682	.505
.224	.0757	.0342	.440	.497	.329	.0928	.0753	.552	.404
.129	.0844	.0330	.255	.331	.238	.0948	.0774	.397	.293

#### TABLE I - Continued

2 -Blade Left-Hand Propeller

#### TABLE I - Continued

2 -Blade Left-Hand Propeller 45° at 0.75 R

		35° at 0.75	R						
V/nD	CT	CP	Cs	η	V/nD	CT	CP	Cs	η
1.601	0.0252	0.0597	2.813	0.675	2.205	0.0340	0.1114	3.422	0.674
1.550	.0323	.0681	2.654	.735	2.156	.0400	.1215	3.287	.710
1.503	.0390	.0747	2.526	.784	2.060	.0499	.1381	3.061	.744
1.431	.0476	.0847	2.345	.805	1.984	.0576	.1496	2.900	.765
1.380	.0535	.0904	2.230	.816	1.912	.0644	.1570	2.769	.784
1.322	.0614	.0980	2.105	.829	1.819	.0732	.1664	2.605	.800
1.265	.0664	.1023	1.996	.822	1.713	.0820	.1756	2.427	.799
1.198	.0739	.1077	1.871	.822	1.642	.0869	.1810	2.312	.789
1.121	.0819	.1123	1.735	.817	1.546	.0885	.1837	2.170	.745
1.046	.0878	.1156	1.610	.795	1.467	.0887	.1817	2.063	.721
.993	.0898	.1187	1.523	.751	1.442	.0890	.1813	2.028	.708
.912	.0882	.1202	1.393	.669	1.357	.0885	.1820	1.908	.660
.818	.0900	.1216	1.247	.605	1.265	.0900	.1818	1.778	.626
.713	.0924	.1230	1.085	.536	1.178	.0913	.1811	1.657	.594
.681	.0936	.1240	1.033	.515	1.087	.0920	.1811	1.530	.552
.604	.0962	.1200	.914	.461	.973	.0936	.1835	1.365	.496
.491	.0996	.1306	.737	.374	.841	.0976	.1881	1.175	.436
.412	.1016	.1341	.616	.312	.709	.1002	.1940	.984	.366
					.551	.1022	.2003	.760	.281

В

С

V/nD 0.744 .713 .679 .646 .627 .595 .553 .525 .493 .467 .445 .406 .381 .335 .300 .263 .227

#### TABLE I - Continued

4-Blade Propeller

	15° at 0.75	R				25° at 0.75	R	
CT	CP	Cs	η	V/nD	CT	CP	Cs	n
0.0020	0.0155	1.713	0.095	1.171	0.0062	0.0327	2.320	0.222
.0137	.0220	1.532	.445	1.128	.0209	.0458	2.090	.515
.0244	.0278	1.391	.597	1.078	.0381	.0594	1.897	.692
.0353	.0334	1.275	.684	1.046	.0488	.0685	1.788	.745
.0405	.0359	1.221	.708	.998	.0613	.0785	1.661	.779
.0494	.0403	1.132	.730	.960	.0719	.0864	1.567	.799
.0600	.0449	1.029	.741	.906	.0824	.0936	1.455	.798
.0680	.0480	.964	.743	.883	.0888	.0979	1.405	.801
.0758	.0512	.893	.731	.853	.0978	.1038	1.342	.803
.0825	.0535	.839	.720	.823	.1041	.1084	1.283	.791
.0861	.0548	.796	.698	.786	.1126	.1130	1.216	.783
.0958	.0576	.719	.677	.735	.1221	.1174	1.128	.765
.1004	.0594	.670	.646	.687	.1331	.1226	1.045	.748
.1086	.0610	.586	.596	.640	.1429	.1265	.968	.722
.1148	.0624	.523	.552	.583	.1545	.1300	.877	.693
.1206	.0632	.457	.502	.523	.1633	.1313	.785	.650
.1258	.0634	.394	.451	.465	.1736	.1341	.695	.603
		1		.409	.1780	.1368	.609	.532
				.333	.1753	.1411	. 493	.406

.267

.1771

TABLE I - Continued

#### 4-Blade Propeller

#### 4-Blade Propeller

TABLE I - Continued

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.331

		35° at 0.75	R				45° at 0.75	R	
V/nD	C <sub>T</sub>	CP	Cs	η	V/nD	CT	CP	Cs	η
1.597	0.0409	0.1032	2.515	0.632	2.184	0.0661	0.2135	2.978	0.676
1.544	.0545	.1189	2.364	.708	2.085	.0865	.2418	2.772	.746
1.484	.0684	.1347	2.217	.754	2.020	.0990	.2619	2.640	.764
1.440	.0796	.1476	2.112	.776	1.930	.1160	.2856	2.480	.784
1.406	.0873	.1550	2.042	.790	1.848	.1289	.3022	2.350	.790
1.374	.0956	.1641	1.972	.801	1.807	.1364	.3100	2.283	.796
1.336	.1031	.1704	1.905	.808	1.710	.1522	.3290	2.136	.791
1.274	.1153	.1816	1.792	.808	1.626	.1635	.3447	2.013	.772
1.206	.1312	.1954	1.672	.810	1.542	.1679	.3502	1.902	.739
1.138	.1451	.2065	1.561	.799	1.448	.1704	.3500	1.786	.706
1.078	.1565	.2146	1.467	.786	1.349	.1716	.3505	1.664	.661
1.006	.1661	.2213	1.362	.757	1.258	.1722	.3502	1.552	.619
.938	.1669	.2268	1.263	.691	1.134	.1756	.3510	1.398	.567
.877	.1695	.2275	1.179	.653	1.052	.1779	.3530	1.295	.530
.820	.1700	.2265	1.104	.616	.958	.1815	.3571	1.177	.487
.750	.1724	.2298	1.006	.563	.821	.1830	.3614	1.007	.415
.670	.1757	:2352	.895	.501	.660	.1876	.3725	.804	.332
.584	.1812	.2410	.776	.439	.532	.1910	.3828	.644	.265
.482	.1843	.2440	.638	.364					
.352	.1884	.2534	.463	.262					

# TABLE I - Continued

4-Blade Propeller

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#### TABLE I. - Continued

# Tandem Propellers

Right-Hand (Forward) 15° at 0.75 R Left-Hand (Rear) 15° at 0.75 R

15 Percent Diameter Spacing

#### TABLE I - Continued

Right-Hand (Forward) 25° at 0.75 R Left-Hand (Rear) 24.7° at 0.75 R

15 Percent Diameter Spacing

V/nD	CT	Cp	C <sub>P</sub> (RH-LH)	Cs	η	V/nD	CT	CP	C <sub>P</sub> (RH-LH)	Cs	η
0.749	0.0023	0.0166	0.0009	1.700	0.102	1.185	0.0038	0.0288	0.0042	2.410	0.157
.715	.0143	.0232	.0006	1.518	.440	1.125	.0258	.0484	.0028	2.064	.600
.675	.0271	.0297	.0007	1.363	.625	1.051	.0493	.0683	.0016	1.798	.759
.639	.0382	.0353	.0006	1.247	.690	.969	.0731	.0871	.0006	1.578	.813
.602	.0494	.0408	.0005	1.142	.729	.912	.0878	.0982	.0001	1.450	.815
.568	.0595	.0452	.0003	1.056	.747	.830	.1084	.1123	0005	1.286	.801
.550	.0636	.0468	.0002	1.015	.748	.732	.1309	.1251	0013	1.110	.766
.520	.0718	.0495	0003	.949	.754	.668	.1455	.1320	0021	1.002	.736
.491	.0795	.0528	0004	.885	.739	.600	.1600	.1372	0027	.893	.700
.441	.0920	.0573	0006	.781	.708	.519	.1755	.1408	0042	.768	.647
.408	.0990	.0601	0004	.716	.672	.437	.1889	.1455	0060	.643	.567
.362	.1078	.0619	0011	.632	.631	.333	.1955	.1515	0088	.486	.428
.308	.1203	.0654	0011	.532	.567	.247	.1987	.1566	0110	.358	.313
.242	.1318	.0663	0019	.416	.480				1	1	

TABLE 1 - Continued

Tandem Propellers Right-Hand (Forward) 35° at 0.75 R Left-Hand (Rear) 34.4° at 0.75 R

#### TABLE I - Continued

# Tandem Propellers

# Right-Hand (Forward) 45° at 0.75 R Left-Hand (Rear) 43.9° at 0.75 R

	15	Percent	Diameter Space	cing		15 Percent Diameter Spacing							
V/nD	CT	Cp	C <sub>P</sub> (RH-LH)	Cs	η	V/nD	CT	CP	C <sub>P</sub> (RH-LH)	Cs	η		
1.611	0.0385	0.1019	0.0060	2.543	0.610	2.250	0.0557	0.2011	0.0123	3.100	0.623		
1.547	.0576	.1238	.0045	2.350	.720	2.150	.0744	.2270	.0099	2.892	.705		
1.489	.0728	.1405	.0019	2.207	.766	2.074	.0923	.2533	.0068	2.730	.755		
1.442	.0837	.1530	.0016	2.100	.789	1.995	.1082	.2757	.0048	2.582	.784		
1.377	.1003	.1710	.0005	1.960	.808	1.919	.1253	.2968	.0014	2.447	.810		
1.310	.1161	.1870	0005	1.830	.813	1.849	.1390	.3176	.0009	2.327	.809		
1.244	.1297	.1986	0011	1.722	.812	1.762	.1546	.3357	0014	2.192	.811		
1.182	.1447	.2110	0023	1.614	.810	1.682	.1680	.3517	0021	2.072	.803		
1.105	.1606	.2220	0036	1.494	.800	1.598	.1804	.3653	0023	1.954	.790		
1.042	.1718	.2310	0041	1.397	.784	1.506	.1895	.3762	0074	1.832	.759		
.969	.1851	.2386	0055	1.294	.751	1.410	.1933	.3822	0134	1.698	.713		
.889	.1925	.2476	0066	1.178	.691	1.314	.1949	.3830	0197	1.592	.668		
.816	.1975	.2554	0074	1.075	.631	1.230	.1976	.3843	0194	1.488	.632		
.732	.1988	.2570	0093	.962	.566	1.132	.2011	.3845	0184	1.370	.592		
.662	.2016	.2590	0104	.868	.515	1.016	.2047	.3867	0178	1.229	.538		
.597	.2056	.2635	0115	.779	.466	.883	.2084	.3930	0185	1.064	.460		
.493	.2112	.2705	0121	.639	.385	.756	.2115	. 4028	0195	.907	.397		
.349	.2196	.2840	0135	.449	.269	.613	.2136	.4125	0216	.731	.317		

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#### TABLE 1 - Continued

#### Tandem Propellers

Right-Hand (Forward) 25° at 0.75 R Left-Hand (Rear) 24.5° at 0.75 R 8-1/2 Percent Diameter Spacing

TABLE I - Conti	nued
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### Tandem Propellers

Right-Hand (Forward) 25° at 0.75 R Left-Hand (Rear) 24.8° at 0.75 R

30	Percent	Diameter	Spac	Ing
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V/nD	CT	с <sub>р</sub>	C <sub>P</sub> (RH-LH)	Cs	η	V/nD	CT	CP	C <sub>P</sub> (RH-LH)	Cs	η
1.177	0.0055	0.0307	0,0058	2.363	0.211	1.187	0.0059	0.0318	0.0007	2.365	0.222
1.127	.0230	.0475	.0049	2.072	.546	1.140	.0234	.0474	.0005	2.100	.563
1.080	.0391	.0605	.0038	1.891	.698	1.096	.0385	.0602	.0004	1.923	.697
1.029	.0549	.0742	.0023	1.733	.762	1.045	.0551	.0744	.0001	1.758	.774
.970	.0720	.0870	.0010	1.581	.803	.990	.0695	.0858	0	1.619	.802
.918	.0854	.0970	.0004	1.465	.808	.944	.0811	.0941	0	1.514	.812
.858	.0997	.1070	0001	1.343	.799	.896	.0944	.1036	0002	1.410	.816
.790	.1151	.1159	0007	1.216	.784	.855	.1055	.1107	0005	1.328	.815
.728	.1295	.1238	0013	1.107	.760	.784	.1230	.1216	0010	1.195	.793
.666	.1445	.1306	0020	1.001	.737	.756	.1290	.1253	0014	1.145	.778
.598	.1585	.1360	0031	.892	.697	.704	.1406	.1302	0016	1.060	.760
.521	.1735	.1400	0039	.772	.646	.655	.1511	.1347	0018	.978	.734
.449	.1852	.1410	0043	.664	.589	.607	.1626	.1390	0026	.901	.710
.352	.1961	.1469	0060	.517	.470	.540	.1755	.1416	0035	.798	.669
.245	.2000	.1535	0080	.356	.319	.469	.1871	.1445	0058	.691	.607
			2			.415	.1939	.1493	0070	.607	.539
						.346	.1970	.1544	0098	.503	.441
						.240	.1976	.1595	0120	.346	.297



Figure 2.- Forward end of propeller dynamometer with tandem propellers at 15 percent diameter spacing.

Table 1. Concluded. Figure 3

E



Figure 1.- Schematic section of propeller dynamometer.

N.A.C.A.





N.A.C.A.



Figure 4. - Power, thrust, and efficiency. 2-blade right-hand propeller.

N.A.C.A.



Figure 5. - Power, thrust, and efficiency. 2-blade left-hand propeller.







and L.H. (rear) propellers with 15% diameter spacing.

N.A.C.A.





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Cp

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Figure 9.- Working chart. 2-blade right-hand propeller

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Figure 10.- Working chart. 4-blade right-hand propeller.



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Figure 11.- Working chart. 2 - blade R.H. (front) and L.H. (rear) propeller with 15 percent diameter spacing



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Figure 12.- Comparison of efficiency for  $45^{\circ}$  4-blade propellers and  $45^{\circ}$  - 43.9° tandem propellers at same values of C<sub>s</sub>.