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IMPROVEMENTS AND NEW FEATURES IN THE PDF MODULE

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**Overview**

- Modeling: What models are used in this package and what are their advantages and disadvantages.
- Numerics: Describe how the PDF model is implemented and what are the features of the program.
- Future Developments: What can be expected in the future from the NASA Lewis PDF code.

## PDF Modeled Equations.

- Exact scalar PDF transport equation is:

$$\begin{aligned}
 \frac{\partial}{\partial t}(\bar{\rho}P) + \frac{\partial}{\partial x_i}(\bar{\rho}\bar{U}_iP) + \frac{\partial}{\partial \phi_\alpha}(\bar{\rho}S_\alpha(\underline{\psi}, p, \eta)P) \\
 = \frac{\partial}{\partial x_i}(\langle \bar{\rho}\bar{u}_i | \underline{\psi}, \eta \rangle P) + \frac{\partial}{\partial \phi_\alpha}(\langle \frac{\partial J_i^\alpha}{\partial x_i} | \underline{\psi}, \eta \rangle P) \\
 + \frac{\partial}{\partial \eta}(\langle \frac{\partial q_i^\alpha}{\partial x_i} | \underline{\psi}, \eta \rangle P) + \frac{\partial}{\partial \eta}(\langle \frac{Dp}{Dt} | \underline{\psi}, \eta \rangle P)
 \end{aligned} \tag{1}$$

- Terms on the LHS exact - need to model the four terms on RHS, corresponding to turbulent convection, molecular mixing and the pressure term.

### Turbulent Convection

- This term is modeled as a simple gradient diffusion process.

$$\langle \bar{\rho}\bar{u}_i | \underline{\psi}, \eta \rangle P \approx D_t \frac{\partial P}{\partial \psi_\alpha} \tag{2}$$

- $D_t$  is the turbulent diffusion coefficient, equal to the eddy viscosity. (Assume unity Schmidt)
- Disadvantage: Counter-gradient diffusion known to occur in some pre-mixed flames.

### Molecular Mixing.

- Molecular mixing can be viewed as process which changes the shape of the scalar PDF without affecting the mean.
- Molecular mixing is modeled by two models: A coalescence/dispersion model (Hsu and Chen) and a relax-to-mean model (Dopazo).
- Advantages of both models is that they are simple and readily adaptable to any number of scalars.
- Disadvantages are the relative lack of physics in the models.

### Pressure Term.

- Pressure term model is based on second order closure models for compressible flows (eg. Sarkar).

$$\left\langle \frac{Dp}{Dt} | \underline{\psi}, \eta \right\rangle \approx \frac{\partial \langle p \rangle}{\partial t} + \langle U_i \rangle \frac{\partial p}{\partial x_i} + 0.8 \rho \langle k \rangle \frac{\partial \langle U_i \rangle}{\partial x_i} \quad (3)$$
$$+ 0.15 \rho P_r M_t - 0.2 \rho \epsilon M_t^2$$

- Advantages are that model is tried and tested in finite volume codes. Disadvantage is that only the mean pressure can be used for model. Ideally we would like a stochastic process for two state variables.

## Numerics

- Solution of scalar PDF transport equation achieved by a particle based Monte Carlo scheme.
- PDF represented by an ensemble of particles, each with a composition and enthalpy.
- PDF evolves by the motion of these particles in physical, scalar and enthalpy space, by exact and modeled processes. eg. Convection, reaction, mixing.
- Statistics (eg. means) obtained by averaging over ensemble of particles.

### Numerical Details - Monte Carlo Scheme

- Module based on cell-centered quantities.
- PDF method is a nodal one. ie. All particles reside at the center of the cell, and can move only to neighboring cells.
- Number of particles at each node is the same and the number remains fixed.
- Statistics obtained by averaging over particles at each node, and also by time-averaging.

## Numerics - Convection

- Upwind scheme used for mean convection, and central difference for turbulent convection.
- Evolution achieved by moving particles in from adjacent nodes. Particles are selected at random.
- Fractions of particles are treated by random convection.

$$\text{if } 6.3 \text{ particles then } \begin{cases} 6.0 & 70\% \text{ of the time} \\ 7.0 & 30\% \text{ of the time} \end{cases} \quad (4)$$

## Numerics - Reaction

- Although reaction source term treated exactly, several different numerical schemes are needed. Timing figures are for % of time spent in the PDF part of the code on SPARC II workstation.
- No reaction: For scalar mixing calculations.  
(Timing: 17.2 %)
- Equilibrium reaction: Assume reaction proceeds at infinite speed. Table of equilibrium composition as a function of mixture fraction obtained from separate CHEMKIN routine.  
(Timing: 24.4 %)

## Numerics - Reaction Cont.

- One-step global reaction schemes. Westbrook and Dryer global reactions integrated for each time-step.  
(Timing: 51.1 %)
- Tabulated reaction increments. Users create their own table of composition increments as a function of scalars using the adaptive tabulation scheme provided, plus the users favourite reduced mechanism.  
(Timing: 58.9 %)
- Chemkin full mechanism integration. Very slow and not recommended except for parallel applications.  
(Timing: 97.8 %)

## Numerics - Averaging

- To reduce statistical error in the evaluation of the mean scalar quantities (without increasing the number of particles per node), time averaging is employed.
- A weighted time average is used to give more weight to recent values and less to those in the far past.

$$\langle\langle\phi\rangle\rangle_t = \frac{1}{w_t + 1}(\langle\phi\rangle_t + w_t\langle\langle\phi\rangle\rangle_{n-1}) \quad (5)$$

$$w_t = c_t(w_{t-1} + 1) \quad (6)$$

### **Numerics: Misc.**

- A portable random number generator is now included in the module, set up for 32 bit machines.
- A time step check is now performed to ensure boundedness of the PDF solution. ie. no negative numbers of particles.
- Rplus/PDF release ported to workstation environment. K-epsilon now standard turbulence model.

### **Future Work.**

- Release of 3D version with new improvements.
- Implementation of parallel processing for distributed cluster environment. (PVM based)
- Include model for another state variable to close PDF modeling.





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