



pFUnit 3.0 Tutorial Advanced

Tom Clune

Advanced Software Technology Group
Computational and Information Sciences and Technology Office
NASA Goddard Space Flight Center

April 10, 2014

Outline



- 1 Introduction
 - Overview
- 2 API - Advanced
- 3 Test-driven development

Outline



- 1 Introduction
 - Overview
- 2 API - Advanced
- 3 Test-driven development

Class Overview



Primary Goals:

- Learn how to use pFUnit 3.0 to create and run unit-tests
- Learn how to apply test-driven development methodology

Prerequisites:

- Access to Fortran compiler supported by pFUnit 3.0
- Familiarity with F95 syntax
- Familiarity with MPI¹

Beneficial skills:

- Exposure to F2003 syntax - esp. OO features
- Exposure to OO programming in general

¹MPI-specific sections can be skipped without impact to other topics.

Syllabus



- **Thursday PM - Introduction to pFUnit**
 - ▶ Overview of pFUnit and unit testing
 - ▶ Build and install pFUnit
 - ▶ Simple use cases and exercises
 - ▶ Detailed look at framework API
- **Friday AM - Advanced topics (including TDD)**
 - ▶ User-defined test subclasses
 - ▶ Parameterized tests
 - ▶ Introduction to TDD
 - ▶ Advanced exercises using TDD
- **Friday PM - Bring-your-own-code**
 - ▶ Incorporate pFUnit within the build process of your projects
 - ▶ Apply pFUnit/TDD in your own code
 - ▶ Supplementray exercises will be available

Materials



- ① You will need access to one of the following Fortran compilers to do the hands-on portions
 - ▶ gfortran 4.9.0 (possibly available from cloud)
 - ▶ Intel 13.1, 14.0.2 (available on jellystone)
 - ▶ NAG 5.3.2
- ② Last resort - use AWS
 - ▶ ssh keys are at <ftp://tartaja.com>
 - ▶ user name: `pfunit@tartaja.com` passwd: `iuse.PYTHON.1969`
 - ▶ login: `ssh -i user1 user1@54.209.194.237`
- ③ You will need a copy of the exercises in your work environment
 - ▶ Browser: <https://modelingguru.nasa.gov/docs/DOC-2529>
 - ▶ Jellystone:
`/picnic/u/home/cacruz/pFUnit.tutorial/Exercises.tar`
- ④ These slides can be downloaded at
<https://modelingguru.nasa.gov/docs/DOC-2528>

Outline



- 1 Introduction
- 2 API - Advanced
 - API: pFUnit test Hierarchy
 - API: Misc
 - Parser: Advanced
- 3 Test-driven development

Peeking under the hood - what is inside pFUnit?



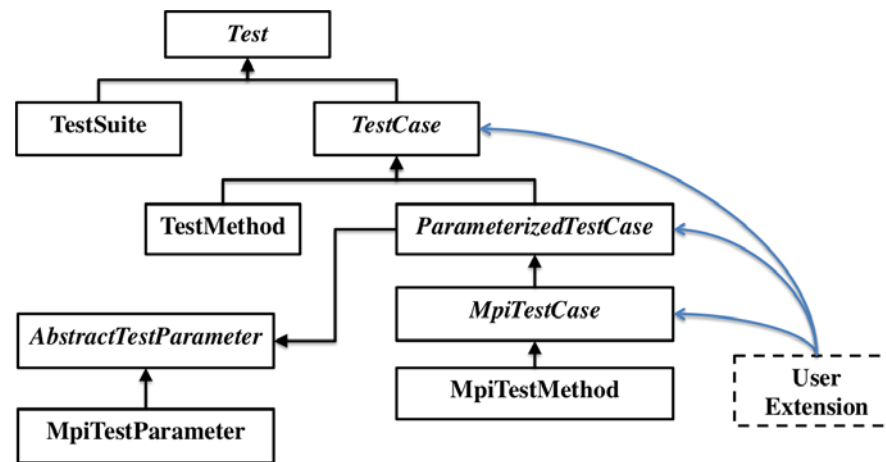
www.shescribes.com

Outline



- 1 Introduction
- 2 API - Advanced
 - API: pFUnit test Hierarchy
 - API: Misc
 - Parser: Advanced
- 3 Test-driven development

Hierarchy of Test Classes



Test



Role: Abstract base class for all test objects.

Implementation: Framework provides various subclasses for common/generic cases. Users can define custom subclasses for specific purposes. Provided subclasses include:

- *TestCase*
- `TestMethod`
- *MpiTestCase*
- `MpiTestMethod`
- `TestSuite`

TestSuite



Role: Aggregates collection of tests into single entity.

Implementation: TestSuite objects are simultaneously Test objects *and* collections of tests. Run() method applies run() to each contained test.

TestCase class



Role: *Abstract* Test subclass that provides some services that are common to most Test subclasses.

Implementation:

TestMethod class



Role: Simple concrete Test subclass that supports the common case where test procedure receives no arguments.

Implementation: Constructor stores a procedure pointer to vanilla Fortran subroutine with no arguments. A restricted form of test fixture is permitted by specifying `setUp()` and `tearDown()` methods that also have no arguments. (I.e. fixture is not encapsulated.)

TestMethod API



Constructor:

```
function TestMethod(name, method[, setUp, tearDown])  
  character(len=*), intent(in) :: name  
  procedure(empty) :: method  
  procedure(empty) :: setUp  
  procedure(empty) :: tearDown
```

Methods:

ParameterizedTestCase class



Role: Allows a single test procedure to be executed multiple times with different input values.

Implementation: *ParameterizedTestCase* objects contain an *AbstractTestParameter* object that encapsulates input. Subclasses of *ParameterizedTestCase* must generally also subclass *AbstractTestParameter*.

MpiTestCase class



Role: (*Abstract*) Extends *ParameterizedTestCase* with support for MPI.

Implementation: *MpiTestCase* modifies the `runBare()` launch mechanism to create an appropriately sized MPI group and corresponding subcommunicator. Processes within that group then call the user's test procedure, while any remaining processes wait at a barrier.

MPI based tests *must not* use `MPI_COMM_WORLD`, and must instead obtain MPI context from the passed test object.

The following convenient type-bound procedures are provided:

```
getProcessRank() ! returns rank within group  
getNumProcesses() ! returns size of group  
getMpiCommunicator() ! returns the bare MPI com.
```

MpiTestMethod class



Role: Simple concrete Test subclass that supports common MPI cases that just need basic MPI context.

Implementation: Analogous to the vanilla TestMethod, except that user test procedures are now passed an object which must be queried for any MPI context that the test needs.

MpiTestMethod API



Constructor:

```
function MpiTestMethod(name, method, numProcesses, [, setUp]
  character(len=*) , intent(in) :: name
  procedure(empty) :: method
  integer :: numProcesses ! requested
  procedure(empty) :: setUp
  procedure(empty) :: tearDown
```

Outline



- 1 Introduction
- 2 API - Advanced
 - API: pFUnit test Hierarchy
 - API: Misc
 - Parser: Advanced
- 3 Test-driven development

TestResult class



Role: “Scorecard” – accumulates information about tests as they run.

Implementation: Each `run()` method for `Test` objects has a mandatory `TestResult` argument. The *Visitor* pattern is used to allow the `TestResult` object to manage and monitor the test as it progresses.

Note: *Visitor* is a somewhat advanced pattern and uses OO capabilities in a nontrivial manner. Users should not need to be aware of this, but developers of framework extensions likely will.

Abstract BaseTestRunner class



Role: Runs a test (usually a TestSuite).

Implementation: Run() method constructs and configures a TestResult object, then runs the passed Test object.

TestRunner class



Role: Default Runner for pFUnit.

RobustRunner class



Role: Runner subclass that executes tests within a separate process.

Implementation: Collaborates with SubsetRunner. RobustRunner restarts SubsetRunner if it detects a hang or a crash. Currently a bit unreliable.
(Irony)

Outline



- 1 Introduction
- 2 API - Advanced
 - API: pFUnit test Hierarchy
 - API: Misc
 - Parser: Advanced
- 3 Test-driven development

Annotations: @testCase



```
@testCase  
@testCase(<options>)
```

- Indicates next line defines a new derived type which extends TestCase.
- All test procedures in file must accept a single argument of that extended type.
- Accepts the following options:
 - ▶ `constructor=<name>` Specifies the name of the function to construct corresponding test object. Default is a constructor with same name as derived type²
 - ▶ `npes=[<list-of-integers>]` Indicates that extension is a subclass of `MpiTestCase`, and provides a default set of values for NPES for all test procedures in the file. Individual tests can override.
 - ▶ `esParameters={expr}` Indicates that extension is a subclass of `ParameterizedTestCase`, and provides a default set of parameters for all tests in the file. Can be overridden by each test.
 - ▶ `cases=[<list-of-integers>]` Alternative mechanism for specifying default test parameters where a single integer is passed to the test constructor.

²This Fortran feature is somewhat unreliable, even prior to 14.0.2

Annotations: @testParameter



Encapsulated test fixture



```
. module SomeTests_mod
.   use pFUnit_mod
.   implicit none
.   @testCase
.   type, extends( TestCase ) :: MyTestCase
.     real, allocatable :: xInitial(:)
.   contains
.     procedure :: setUp
.     procedure :: tearDown
.   end type MyTestCase
contains
.
.
.   subroutine setUp(this)
.     class (MyTestCase), intent(inout) :: this
.     xInitial = [1.,3.,5.,3.,1.]
.   end subroutine setUp
.
.   subroutine tearDown(this)
.     class (MyTestCase), intent(inout) :: this
.     deallocate(this%xInitial)
.   end subroutine tearDown
.
```

...

Encapsulated test fixture (cont'd)



```
...
:
: @test
: subroutine anotherTest(this)
:   class (MyTestCase), intent(inout) :: this
:
:   real, allocatable :: x(:)
:
:   x = oneStep(this%xInitial)
:   @assertEqual(...)
:
:   end subroutine anotherTest
:
: end module MyTests_mod
```

Encapsulated test fixture (cont'd)



What you need to know:

- Declare derived type that EXTEND's `TestCase`
- Annotate TestCase extension with `@testCase`
- Declare TYPE-BOUND procedures: `setUp` and `tearDown`
- Annotate test procedure in usual way with `@test`
- Declare single test procedure argument as

```
class (<your type>), intent(inout) :: <dummy>
```

MPI test fixture



```
module SomeMpiTests_mod
:   use pFUnit_mod
:   implicit none
:
:   @testCase(npes=[1,3,5])
:   type, extends(MpiTestCase) :: MyTestCase
:       integer :: rank, npes
:       integer :: peEast, peWest
:   contains
:       procedure :: setUp
:       procedure :: tearDown
:   end type MyTestCase
:
: contains
:
:   subroutine setUp(this)
:       class (MyTestCase), intent(inout) :: this
:       integer :: rank, npes
:       this%rank = this%getProcessRank()
:       this%npes = this%getNumProcesses()
:       this%peWest = mod(this%rank + this%npes - 1, this%npes)
:       this%peEast = mod(this%rank + 1, this%npes)
:   end subroutine setUp
:
: ...
```

MPI test fixture (cont'd)



```
...
:
: @test
: subroutine anotherTest(this)
:   class (MyTestCase), intent(inout) :: this
:
:   integer :: comm
:   real :: x(0:2)
:
:   comm = this%getMpiCommunicator()
:
:   call someMpiProcedure(comm,x)
:
:   @mpiAssertEqual(this%peWest, x(0))
:   @mpiAssertEqual(this%rank, x(1))
:   @mpiAssertEqual(this%peEast, x(2))
:
:   end subroutine anotherTest
: end module MyTests_mod
```


MPI test fixture (cont'd)



What you need to know:

- Declare derived type that EXTEND's `MpiTestCase`
- Annotate TestCase extension with `@testCase`
 - ▶ Optionally specify default npes list: `(npes=[...])`
- Declare TYPE-BOUND procedures: `setUp` and `tearDown`
- Annotate test procedure in usual way with `@test`
- Declare single test procedure argument as

```
class (<your type>), intent(inout) :: <dummy>
```

- Use `@mpiAssert*` to synchronize returns

Parameterized tests



Suppose you want to test an interface using variant input data:

Parameterized tests



Suppose you want to test an interface using variant input data:
E.g. sorting a list ...

```
list = sort([1,2,3,4])  
list = sort([4,3,2,1])  
list = sort([1,4,2,3])  
list = sort([1,2,3,1])
```

Parameterized tests



Suppose you want to test an interface using variant input data:
E.g. sorting a list ...

```
list = sort([1,2,3,4])  
list = sort([4,3,2,1])  
list = sort([1,4,2,3])  
list = sort([1,2,3,1])
```

or varying boundary conditions...

```
call solve(x, BC='dirichlet')  
call solve(x, BC='neumann')
```

Parameterized tests (cont'd)



One simple strategy is to just duplicate tests:

```
@test
subroutine test1()
  @assertEquals([1,2,3,4], sort([1,2,3,4]))
end subroutine test1

@test
subroutine test2()
  @assertEquals([1,2,3,4], sort([4,3,2,1]))
end subroutine test2
...
```

Parameterized tests (cont'd)



One simple strategy is to just duplicate tests:

```
@test
subroutine test1()
  @assertEquals([1,2,3,4], sort([1,2,3,4]))
end subroutine test1

@test
subroutine test2()
  @assertEquals([1,2,3,4], sort([4,3,2,1]))
end subroutine test2
...
```

This can be quite tedious if there are many cases and/or the tests are more complex.

Parameterized tests (cont'd)



Another approach is to loop within a test

```
@test
subroutine test()
  real, allocatable :: x(:)

  call checkDeriv(x, x**0)
  call checkDeriv(x**2, 2*x)
  call checkDeriv(x**3, 3*x**2)
  ...

contains

  subroutine checkDeriv(fx, dfx)
    real, intent(in) :: fx
    real, intent(in) :: dfx
    @assertEqual(dfx, deriv(fx))
  end subroutine checkDeriv
end subroutine test1
```

Parameterized tests (cont'd)



Another approach is to loop within a test

```
@test
subroutine test()
  real, allocatable :: x(:)

  call checkDeriv(x, x**0)
  call checkDeriv(x**2, 2*x)
  call checkDeriv(x**3, 3*x**2)
  ...

contains

  subroutine checkDeriv(fx, dfx)
    real, intent(in) :: fx
    real, intent(in) :: dfx
    @assertEqual(dfx, deriv(fx))
  end subroutine checkDeriv
end subroutine test1
```

Here we lose information about which case(s) failed.

Parameterized tests (cont'd)



pJUnit provides custom support for parameterized tests:

- Exercise tests across list of user-defined parameters
- User EXTEND's two classes:
 - ▶ `ParameterizedTestCase` (analog of `TestCase`)
 - ▶ `AbstractTestParameter`
- Annotation argument: `testParameters={<expr>}`
 - ▶ Specifies default parameter list for `@testCase`
 - ▶ Override with argument to `@test`
- Failures indicate parameter caused failing assert.
 - ▶ Provided through type-bound interface `toString()` on `AbstractTestParameter`

Example: Parameterized test



...

```
7  @testParameter
8  type, extends(AbstractTestParameter) :: StringTestParameter
9      character(:), allocatable :: string
10     character(:), allocatable :: lowerCase
11     character(:), allocatable :: upperCase
12     contains
13     procedure :: toString
14 end type StringTestParameter
```

...

```
66 function toString(this) result(string)
67     class (StringTestParameter), intent(in) :: this
68     character(:), allocatable :: string
69
70     string = '{' // this%string // ',' // this%lowerCase //
71             ',' // this%upperCase // '}'
72 end function toString
```

Example: Parameterized test (cont'd)



```
...
16  @testCase(testParameters = {getParams()}, constructor=
    newTest_StringUtilities)
17  type, extends(ParameterizedTestCase) :: Test_StringUtilities
18  character(:), allocatable :: string
19  character(:), allocatable :: lowerCase
20  character(:), allocatable :: upperCase
21  end type Test_StringUtilities

24
25  function getParams() result(params)
26  type (StringTestParameter), allocatable :: params(:)
27
28  params = [ &
29  StringTestParameter('a', 'a', 'A'), &
30  StringTestParameter('b', 'b', 'B'), &
31  StringTestParameter('A', 'a', 'A'), &
32  StringTestParameter('1', '1', '1'), &
33  StringTestParameter('+', '+', '+'), &
34  StringTestParameter('a1B2c3D4', 'a1b2c3d4', 'A1B2C3D4')
    &
35  ]
36
37  end function getParams
```

Example: Parameterized test (cont'd)



```
...
48  @test
49  subroutine test_toLowerCase(this)
50      class (Test_StringUtilities), intent(inout) :: this
51
52      @assertEqual(this%lowerCase, toLowerCase(this%string))
53
54  end subroutine test_toLowerCase
55
56
57  @test
58  subroutine test_toUpperCase(this)
59      class (Test_StringUtilities), intent(inout) :: this
60
61      @assertEqual(this%upperCase, toUpperCase(this%string))
62
63  end subroutine test_toUpperCase
```

Example: Parameterized test (cont'd)



To specify a variant list of parameters:

```
.. @test (testParameters={getOtherParams()})  
.. subroutine test_toUpperCase(this)  
..   class (Test_StringUtilities), intent(inout) :: this  
..  
..   @assertEqual(this%upperCase, toUpperCase(this%string))  
..  
.. end subroutine test_toUpperCase
```

Combining MPI and Parameterized Test



Combining MPI and Parameterized Test



Good news:

`MpiTestCase` is a **subclass** of `ParameterizedTest`

Combining MPI and Parameterized Test



Good news:

`MpiTestCase` is a **subclass** of `ParameterizedTest`

- Extend `MpiTestCase`

Combining MPI and Parameterized Test



Good news:

`MpiTestCase` is a **subclass** of `ParameterizedTest`

- Extend `MpiTestCase`
- Extend `MpiTestParameter` (invisible with simple MPI)

Combining MPI and Parameterized Test



Good news:

`MpiTestCase` is a **subclass** of `ParameterizedTest`

- Extend `MpiTestCase`
- Extend `MpiTestParameter` (invisible with simple MPI)
- Framework augments `toString()` to ensure that rank/npes is always included in failure messages

Outline



- 1 Introduction
- 2 API - Advanced
- 3 Test-driven development

TDD





Old paradigm:

- Tests written by separate team (black box testing)
- Tests written *after* implementation



Old paradigm:

- Tests written by separate team (black box testing)
- Tests written *after* implementation

Consequences:

- Testing schedule compressed for release
- Defects detected late in development (\$\$)



Old paradigm:

- Tests written by separate team (black box testing)
- Tests written *after* implementation

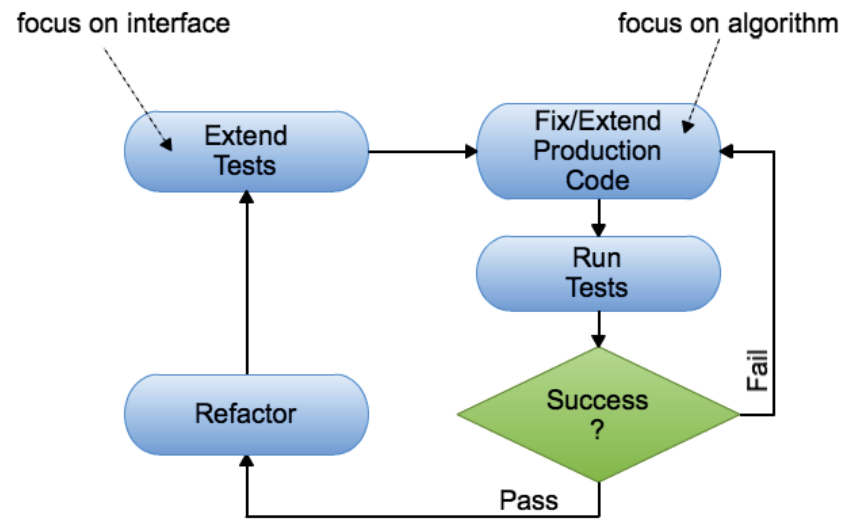
Consequences:

- Testing schedule compressed for release
- Defects detected late in development (\$\$)

New paradigm - Test-driven development (TDD)

- Developers write the tests (white box testing)
- Tests written *before* production code
- *Enabled by emergence of strong unit testing frameworks*

The TDD cycle



Anecdotal Testimony



- Many professional SEs are initially skeptical
 - ▶ High percentage refuse to go back to the old way after only a few days of exposure.
- Some projects drop bug tracking as unnecessary
- Often difficult to sell to management
 - ▶ “What? More lines of code?”

Not a panacea



Not a panacea



- Requires training, practice, and discipline

Not a panacea



- Requires training, practice, and discipline
- Need strong tools (framework + refactoring)

Not a panacea



- Requires training, practice, and discipline
- Need strong tools (framework + refactoring)
- Does not invent new algorithms (e.g. FFT)
 - ▶ No such thing as magic

Not a panacea



- Requires training, practice, and discipline
- Need strong tools (framework + refactoring)
- Does not invent new algorithms (e.g. FFT)
 - ▶ No such thing as magic
- Maintaining tests difficult during a major re-engineering effort.

Not a panacea



- Requires training, practice, and discipline
- Need strong tools (framework + refactoring)
- Does not invent new algorithms (e.g. FFT)
 - ▶ No such thing as magic
- Maintaining tests difficult during a major re-engineering effort.
 - ▶ But isnt the alternative is even worse?!!

Experience to date



TDD has been used heavily within several projects at NASA

- Mostly for “infrastructure” portions - relatively little numerical
- pFUnit itself
- Snowfake - virtual snowflakes; Multi-lattice Snowfake
- DYNAMO - spectral MHD code on spherical shell
- GTRAJ - offline trajectory integration (C++)
- SpF - OO parallel spectral framework

Observations:

- \sim 1:1 ratio of test code to source code
- Works very well for *infrastructure*
- Learning curve
 - ▶ 1-2 days for technique
 - ▶ Weeks-months to wean old habits

TDD - Talking Points

- How large of a step at each cycle?



TDD - Talking Points



- How large of a step at each cycle?
 - ▶ Gauge by time
 - ▶ If steps are going quickly try larger changes
 - ▶ If iteration > 10 min, start iteration over (repository is your friend)

TDD - Talking Points



- How large of a step at each cycle?
 - ▶ Gauge by time
 - ▶ If steps are going quickly try larger changes
 - ▶ If iteration > 10 min, start iteration over (repository is your friend)
- Triangulation
 - ▶ Start with simple tests
 - ▶ Add tests that probe weaknesses in existing implementation
 - ▶ Stop when it is apparent that new tests will all pass
- Don't test constructors and accessors

TDD - Talking Points



- How large of a step at each cycle?
 - ▶ Gauge by time
 - ▶ If steps are going quickly try larger changes
 - ▶ If iteration > 10 min, start iteration over (repository is your friend)
- Triangulation
 - ▶ Start with simple tests
 - ▶ Add tests that probe weaknesses in existing implementation
 - ▶ Stop when it is apparent that new tests will all pass
- Don't test constructors and accessors
- Commit/backup *frequently*

TDD - Talking Points



- How large of a step at each cycle?
 - ▶ Gauge by time
 - ▶ If steps are going quickly try larger changes
 - ▶ If iteration > 10 min, start iteration over (repository is your friend)
- Triangulation
 - ▶ Start with simple tests
 - ▶ Add tests that probe weaknesses in existing implementation
 - ▶ Stop when it is apparent that new tests will all pass
- Don't test constructors and accessors
- Commit/backup *frequently*
- Use synthetic data to make results *obvious*

TDD - Talking Points



- How large of a step at each cycle?
 - ▶ Gauge by time
 - ▶ If steps are going quickly try larger changes
 - ▶ If iteration > 10 min, start iteration over (repository is your friend)
- Triangulation
 - ▶ Start with simple tests
 - ▶ Add tests that probe weaknesses in existing implementation
 - ▶ Stop when it is apparent that new tests will all pass
- Don't test constructors and accessors
- Commit/backup *frequently*
- Use synthetic data to make results *obvious*
- Private vs testable

TDD - Talking Points



- How large of a step at each cycle?
 - ▶ Gauge by time
 - ▶ If steps are going quickly try larger changes
 - ▶ If iteration > 10 min, start iteration over (repository is your friend)
- Triangulation
 - ▶ Start with simple tests
 - ▶ Add tests that probe weaknesses in existing implementation
 - ▶ Stop when it is apparent that new tests will all pass
- Don't test constructors and accessors
- Commit/backup *frequently*
- Use synthetic data to make results *obvious*
- Private vs testable
 - ▶ One module has everything PUBLIC
 - ▶ 2nd module is default private - just export the things you want PUBLIC
 - ▶ Tests use first module; application uses 2nd.

TDD - Talking Points



- How large of a step at each cycle?
 - ▶ Gauge by time
 - ▶ If steps are going quickly try larger changes
 - ▶ If iteration > 10 min, start iteration over (repository is your friend)
- Triangulation
 - ▶ Start with simple tests
 - ▶ Add tests that probe weaknesses in existing implementation
 - ▶ Stop when it is apparent that new tests will all pass
- Don't test constructors and accessors
- Commit/backup *frequently*
- Use synthetic data to make results *obvious*
- Private vs testable
 - ▶ One module has everything PUBLIC
 - ▶ 2nd module is default private - just export the things you want PUBLIC
 - ▶ Tests use first module; application uses 2nd.
- *Think* when writing tests; *autopilot* when writing implementation

TDD - process reminder



- 1 Extend test (new test procedure, new assert, etc)
- 2 *Verify test fails* **Red Light**
- 3 Alter implementation to pass test
- 4 Refactor to eliminate redundancy **Green Light**
- 5 Repeat

TDD Demonstration: Factorial



Instructions:

Use TDD to implement factorial function

To make it interesting, we'll add tests to guard against illegal inputs and overflow.



- Change into the directory `./Exercises/TDD_Warmup`
- Set PFUNIT for a serial build
- `% make tests` (ensure that make is working for you)

TDD Demonstration: Dynamical System



Instructions:

We are going to build a set of classes that will integrate a simple dynamical system:

- State of system is specified by a scalar, t , and 2 vectors: x and v
- Denote timestep with h
- Force (F) on system is any function of x, v, t
- Initial integration will be via forward Euler: $Y_{n+1} = Y_n + hF(Y_n, t)$
- Then we will “upgrade” to RK4

Possible unit tests for Dynamical System



Forward Euler integration

- $F(t) = 0, v(t = 0) = 0$ leaves $x_{n+1} = x_0$
- $F(t) = 0, v(t = 0) = v_0$ has $x_{n+1} = nhv_0$
- $F(t) = 0, v(t = 0) = v_0$ has $v_{n+1} = v_n$
- $F(t) = F(t = 0) = a, v(t = 0) = x(t = 0) = 0$ has $v_{n+1} = v_n + ha$
- $v_{n+1} = v_n + hF(t_n)$
- $x_{n+1} = x_n + hv_n$
- If $h = 0, x_n = x_0$ and $v_n = v_0$ for any F
- Vary number of dimensions



- Change into the directory `./Exercises/TDD_DynamicalSystem`
- Set PFUNIT for a serial build
- `% make tests` (ensure that make is working for you)

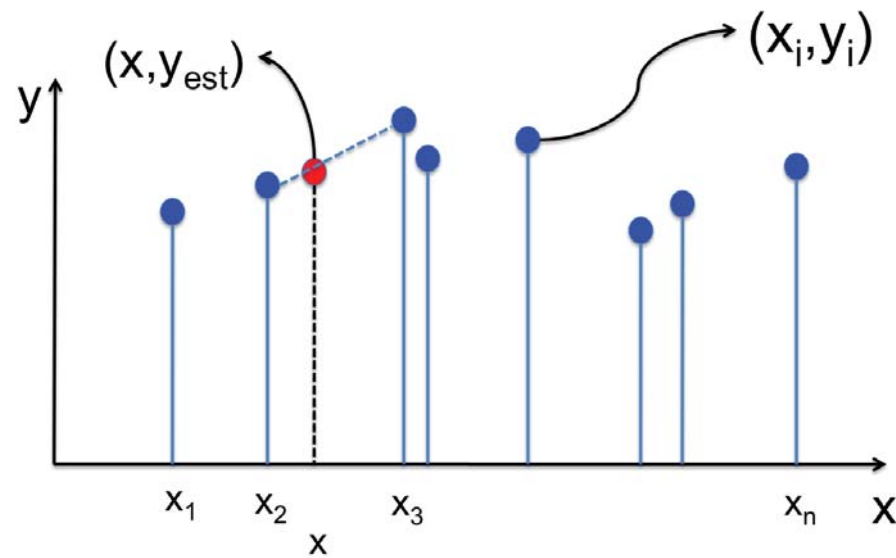
Runge-Kutta (RK4)



$$y_{n+1} = y_n + \frac{1}{6}h(k_1 + 2k_2 + 2k_3 + k_4)$$
$$t_{n+1} = t_n + h$$

$$k_1 = f(t_n, y_n)$$
$$k_2 = f\left(t_n + \frac{1}{2}h, y_n + \frac{h}{2}k_1\right)$$
$$k_3 = f\left(t_n + \frac{1}{2}h, y_n + \frac{h}{2}k_2\right)$$
$$k_4 = f(t_n + h, y_n + hk_3)$$

Demo: Build a Linear 1D Interpolator



Interpolation ...



What are some potential tests?

Interpolation ...



What are some potential tests?

- Bracket: Find i such that $x_i \leq x < x_{i+1}$

Interpolation ...



What are some potential tests?

- Bracket: Find i such that $x_i \leq x < x_{i+1}$
- Computing weights:

$$w_a = \frac{x_{i+1} - x}{x_{i+1} - x_i}$$
$$w_b = 1 - w_a$$

Interpolation ...



What are some potential tests?

- Bracket: Find i such that $x_i \leq x < x_{i+1}$
- Computing weights:

$$w_a = \frac{x_{i+1} - x}{x_{i+1} - x_i}$$
$$w_b = 1 - w_a$$

- Combining weighted sum: $y = w_a y_i + w_b y_{i+1}$

Tests for finding enclosing bracket



$\{x_1, x_2, x_3\}$	x	Expect	Comment
{1.,2.,3.}	1.5	$i = 1$	vanilla
{1.,2.,3.}	2.5	$i = 2$	vary x
{1.,2.,4.}	3.0	$i = 2$	irregular spacing
{1.,2.,4.,5.}	2.5	$i = 2$	vary # of nodes
{1.,2.,3.}	2.0	$i = 2$	edge case
{1.,2.,3.}	1.0	$i = 1?$	edge case
{1.,2.,3.}	3.0	$i = 2?$	edge case
{1.,2.,3.}	0.5	exception?	out-of-bounds
{3.,2.,1.}	1.5	exception?	support inverted order?

Tests for compute weights



x_i	x_{i+1}	x	expected	Comment
1.	2.	1.0	$w_a = 1.0$	left end
1.	2.	2.0	$w_a = 0.0$	right end
1.	2.	1.5	$w_a = 0.5$	middle
1.	3.	1.5	$w_a = 0.75$	vary interval
1.	2.	0.0	$w_a = ?$	out-of-bounds
1.	1.	1.0	?	duplicate node

Tests for combine weights



w_a	y_a	y_b	expected	Comment
1.	1.	2.	$y = 1.0$	left end
0.	1.	2.	$y = 2.0$	right end
0.5	1.	2.	$y = 1.5$	middle
0.5	3.	2.	$y = 2.5$	vary data



Live Demo: Cross Fingers

References



- pFUnit: <http://sourceforge.net/projects/pfunit/>
- Tutorial materials
 - ▶ <https://modelingguru.nasa.gov/docs/DOC-1982>
 - ▶ <https://modelingguru.nasa.gov/docs/DOC-1983>
 - ▶ <https://modelingguru.nasa.gov/docs/DOC-1984>
- TDD Blog
<https://modelingguru.nasa.gov/blogs/modelingwithtdd>
- *Test-Driven Development: By Example* - Kent Beck
- Mller and Padberg," About the Return on Investment of Test-Driven Development," <http://www.ipd.uka.de/mitarbeiter/muellerm/publications/edser03.pdf>
- *Refactoring: Improving the Design of Existing Code* - Martin Fowler
- JUnit <http://junit.sourceforge.net/>

Acknowledgements



- This work has been supported by NASA's High End Computing (HEC) program and Modeling, Analysis, and Prediction Program.
- Many thanks to team members Carlos Cruz and Mike Rilee for helping with implementation, regression testing and documentation.
- Special thanks to members of the user community that have made contributions.
 - ▶ Sean Patrick Santos
 - ▶ Matthew Hambley
 - ▶ Evan Lezar