



# Analysis of Random Segment Errors on Coronagraph Performance

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## Agenda

Introduction

Review and Update of 2015 SPIE O&P presented “Preliminary  
Analysis of Random Segment Errors on Coronagraph  
Performance”

New results for Mamadou N'Diaye's Coronagraph



## Introduction

Purpose is to determine how to specific telescope tolerances.

Exoplanet Science is so difficult that we must study performance of Telescope and Coronagraph as a system.

Developed MATLAB tool of contrast leakage as a function of random telescope wavefront error instability:

Primary Mirror Motion:	Secondary Mirror Motion
– Segment Piston	– Coma – lateral shear
– Segment Tip/Tilt	– Power - despace
– Segment Astigmatism	– Spherical – despace
– Segment Trefoil	
– Backplane Bending	

Only concerned with random motion. Assume that ‘signature’ of a fixed repetitive motion can be subtracted.

Don't need 10 pm Tip/Tilt – need Tip/Tilt that is stable to 10 pm.

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## Preliminary analysis of effect of random segment errors on coronagraph performance

Mark T. Stahl, H. Philip Stahl,  
NASA Marshall Space Flight Ctr.

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Jet Propulsion Laboratory  
California Institute of Technology



## Summary

At 2015 SPIE O&P we presented “Preliminary Analysis of Random Segment Errors on Coronagraph Performance”

### Key Findings:

- Contrast Leakage for 4<sup>th</sup> order  $\text{Sinc}^2(X)$  coronagraph is 10X more sensitive to random segment piston than random tip/tilt.
- Fewer segments (i.e. 1 ring) or very many segments (> 16 rings) has less contrast leakage as a function of piston or tip/tilt than an aperture with 2 to 4 rings of segments.

### Revised Findings:

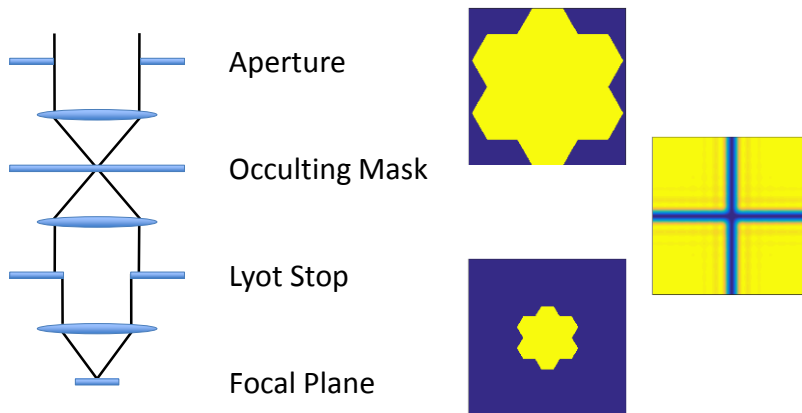
- Piston is only 2.5X more sensitive than Tip/Tilt

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## Integrated Model

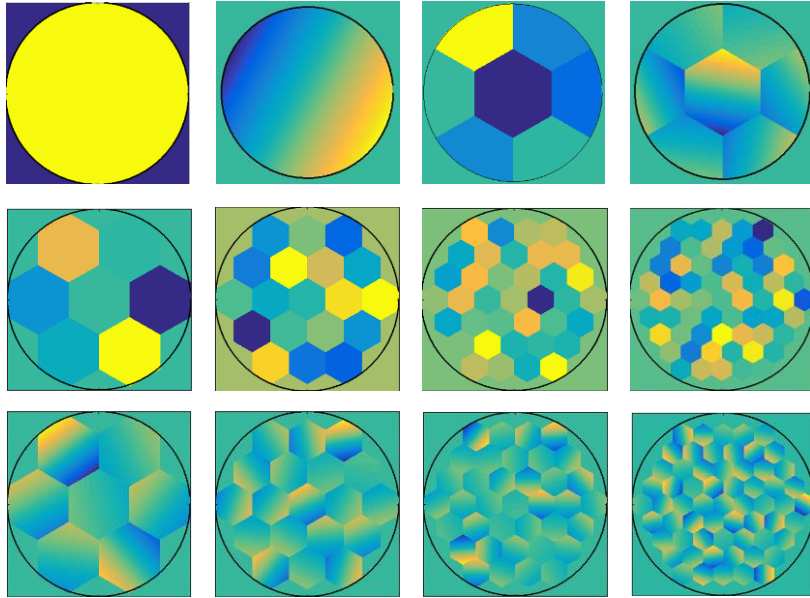
Using Matlab, we created an integrated model of a segmented aperture telescope and a single stage internal linear band-limited coronagraph:  $\{1 - \text{sinc}^2(x) \times \text{sinc}^2(y)\}$ .



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### Input Pupil Functions



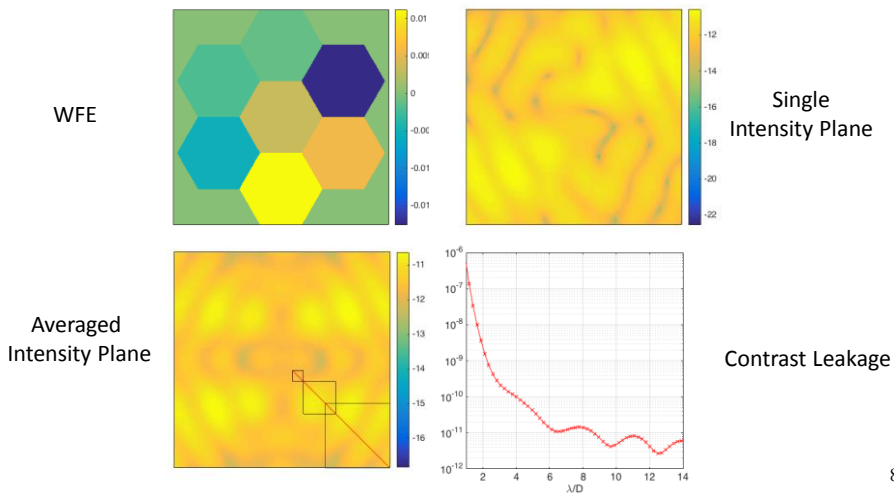
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### Integrated Model – Output

Output is Contrast (single realization & N average)

- Average inside ROI from 1-2  $\lambda/D$ , 2-5  $\lambda/D$  & 4-10  $\lambda/D$
- 10 pm rms piston, N = 16

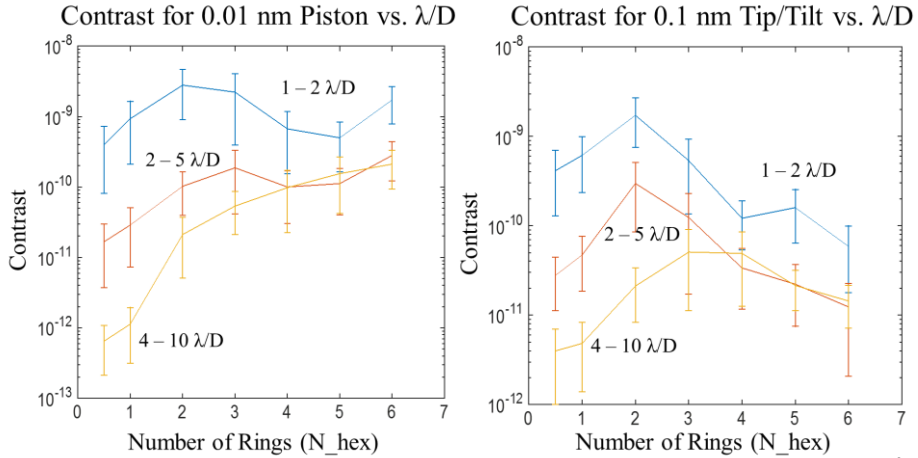


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### WFE Sensitivity vs Number of Segments - OLD

- Contrast Leakage is 10X more sensitive to Piston than Tilt.
- Contrast Leakage is less for fewer segments

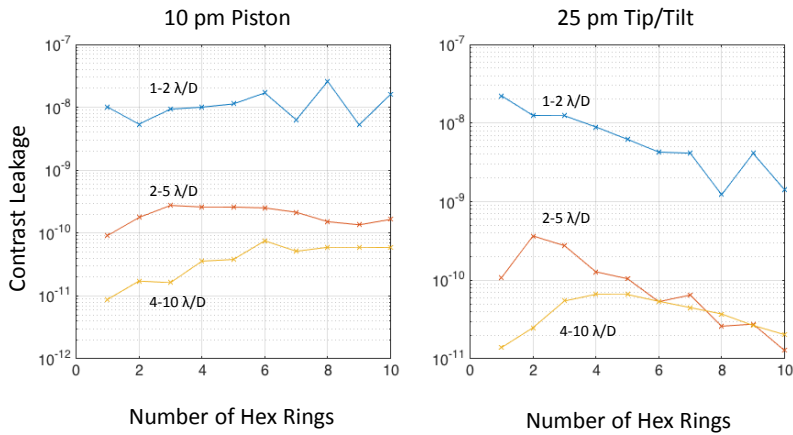


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### WFE Sensitivity vs Number of Segments

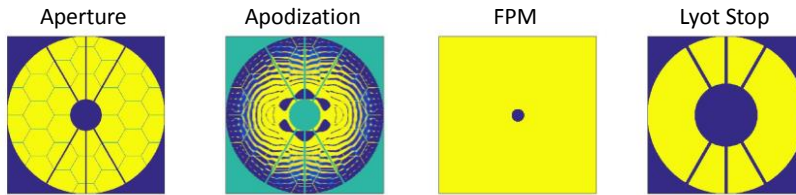
- Contrast Leakage is 2.5X more sensitive to Piston than Tilt.
- Contrast Leakage is less for fewer segments



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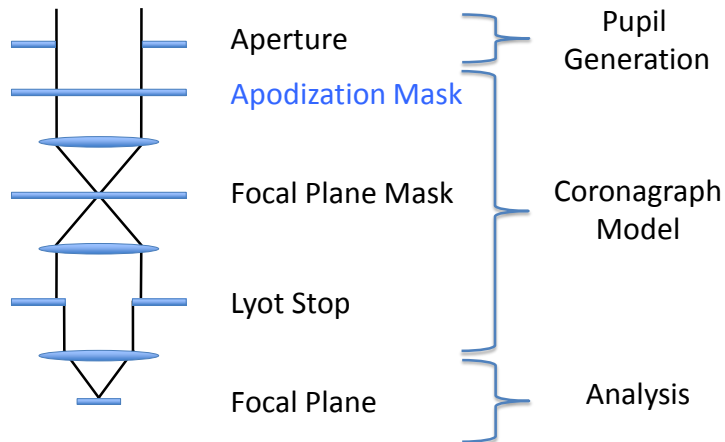
## Analysis of Random Segment Errors on Performance of Mamadou N'Diaye's Coronagraph



N'Diaye et al.. "Apodized pupil Lyot coronagraphs for arbitrary apertures v hybrid shaped pupil designs for imaging Earth-like planets with future space observatories", ApJ (2016).



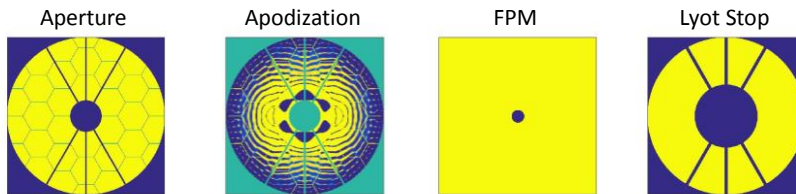
## Integrated Model





## STScI Coronagraph Model

- APLC/SP design for an ATLAST-like aperture
  - Model supplied by Mamadou N'Diaye
  - Segment gaps applied using grey scale edge blending
  - Apodization mask is grey scale (not fully binary)
  - Uses a  $4 \lambda/D$  radius Focal Plan Mask (FPM)

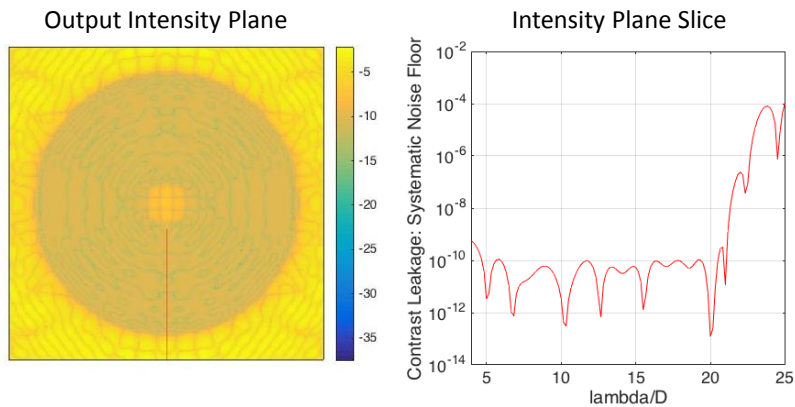


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## Ideal Performance – $4 \lambda/D$ IWA

- Aberration free input

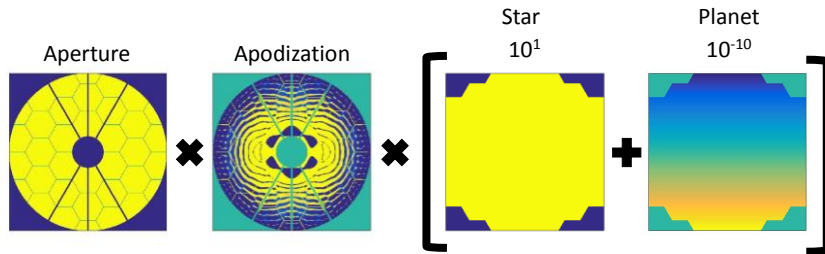


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## Pupil Function – No WFE

- Pupil Function models the telescope
- $\text{Pupil}(x,y) = \text{Aperture}(x,y) * \text{Phase}(x,y) = A(x,y)e^{-i\Phi(x,y)}$
- Aperture Mask
  - Defines segments, secondary obscuration, spiders
  - Apodization mask application
- Phase defines telescope WFE
  - Global tilt used to simulate a planet
  - Planet flux set to  $10^{-10}$

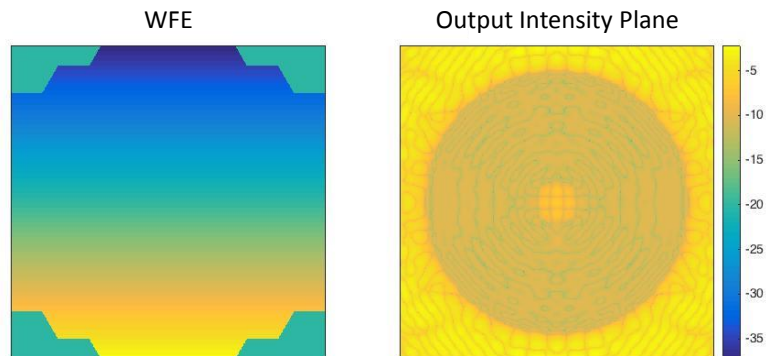


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## Exoplanet

- $10^{-10}$  flux exoplanet added using global tilt at  $6 \lambda/D$



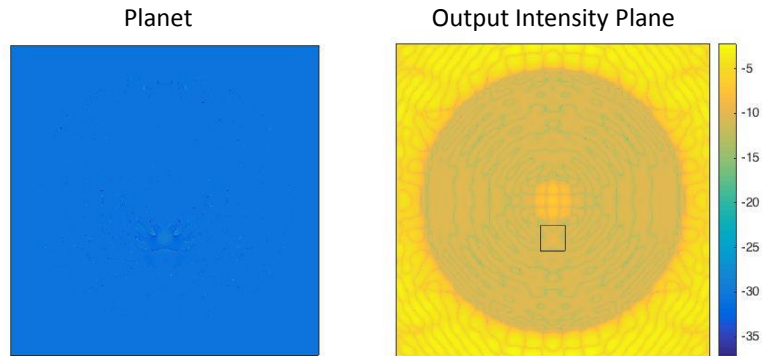
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## Exoplanet @ $6 \lambda/D$

- PSF subtraction use to view planet
- 4 x 4 mas ROI box

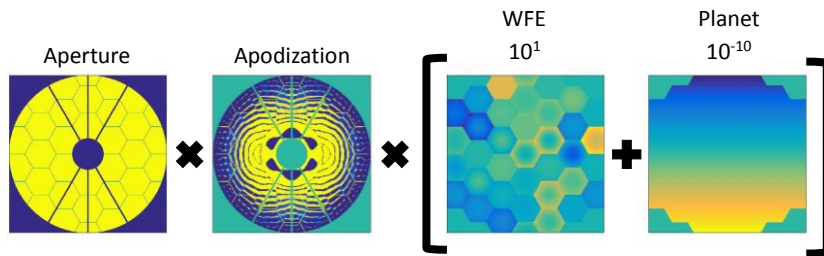


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## Pupil Function – with WFE

- Pupil Function models the telescope
- $\text{Pupil}(x,y) = \text{Aperture}(x,y) * \text{Phase}(x,y) = A(x,y)e^{-i\Phi(x,y)}$
- Aperture Mask
  - Defines segments, secondary obscuration, spiders
  - Apodization mask application
- Phase defines telescope WFE
  - Global and segment aberration application (starlight)

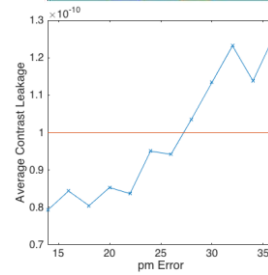
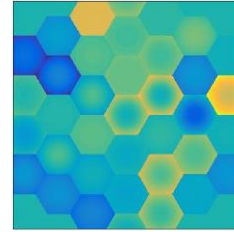
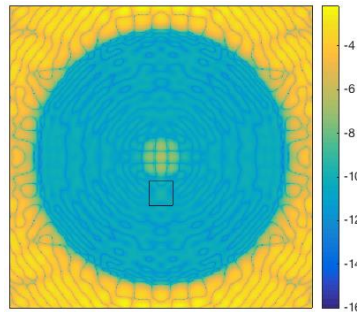


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## Sensitivity Analysis

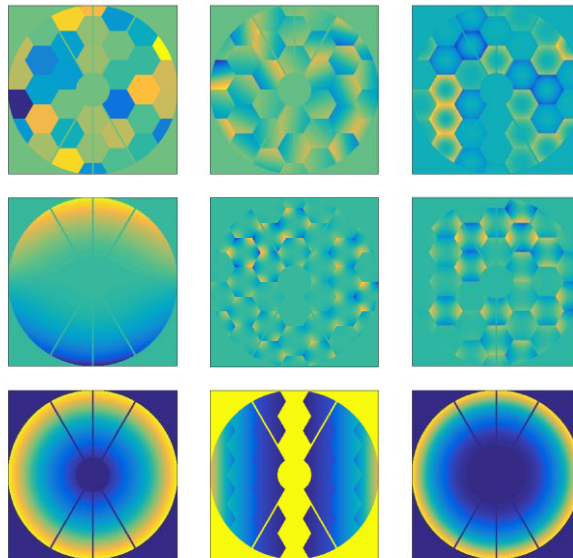
- Average 50 realizations of pupil WFE
- Quantify contrast over 4x4 mas 'planet' ROI
- Plot Average Contrast Leakage vs. Aberration Amplitude



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## Aberrations Studied

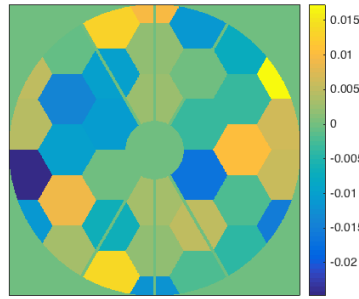


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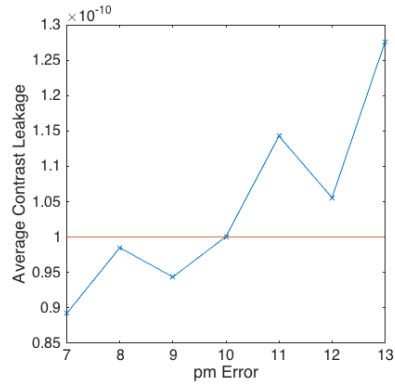


## Segment Piston – 10 pm rms

Single Random WFE



Average Contrast Leakage of 50 WFEs

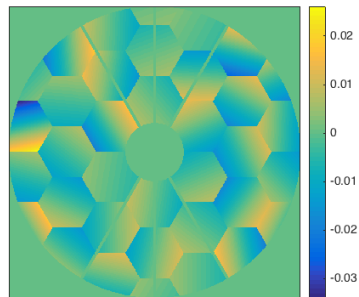


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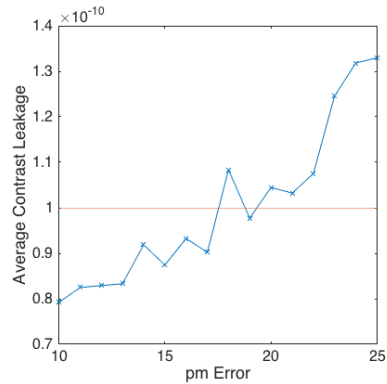


## Segment Tip / Tilt – 20 pm

Single Random WFE



Average Contrast Leakage of 50 WFEs

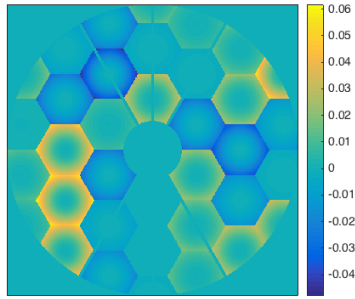


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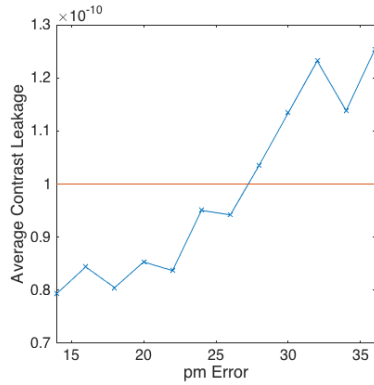


## Segment Power – 30 pm

Single Random WFE



Average Contrast Leakage of 50 WFEs

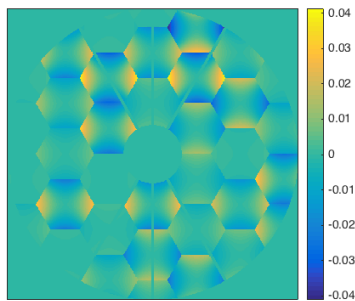


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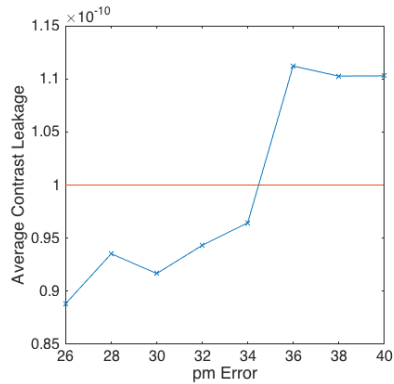


## Segment Astigmatism – 35 pm

Single Random WFE



Average Contrast Leakage of 50 WFEs

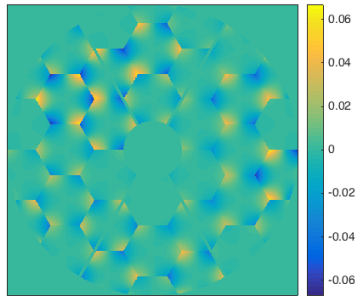


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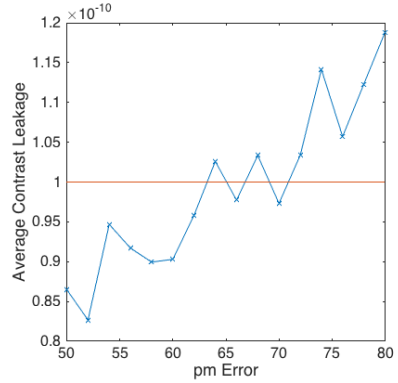


## Segment Trefoil – 65 pm

Single Random WFE



Average Contrast Leakage of 50 WFEs

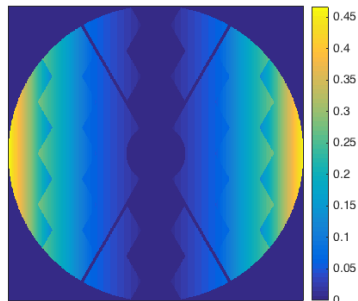


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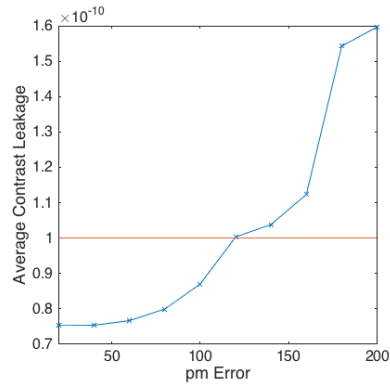


## Back Plane Bend About Y – 120 pm

Single Random WFE



Average Contrast Leakage of 50 WFEs

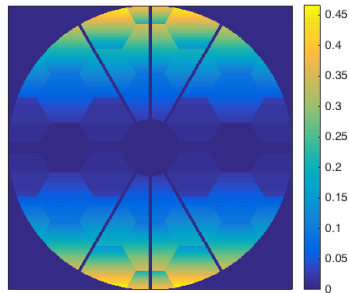


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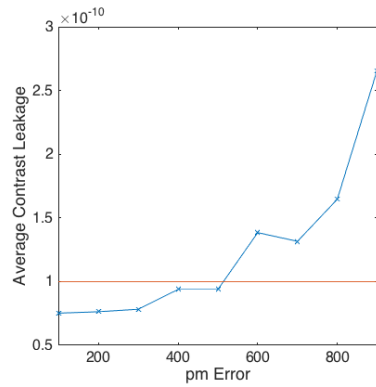


## Back Plane Bend About X – 500 pm

Single Random WFE



Average Contrast Leakage of 50 WFEs

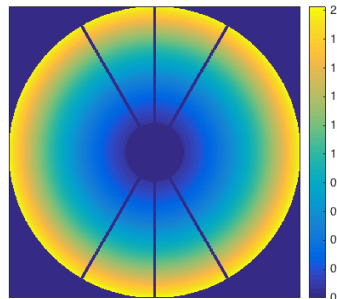


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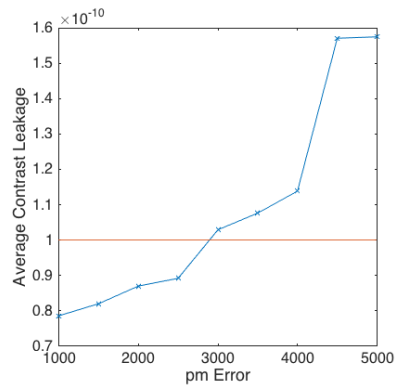


## Global Power – 3000 pm

Single Random WFE



Average Contrast Leakage of 50 WFEs

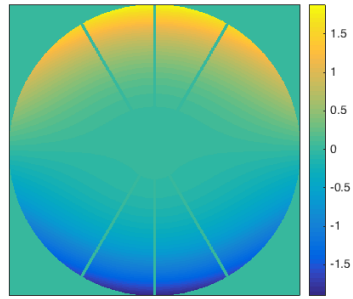


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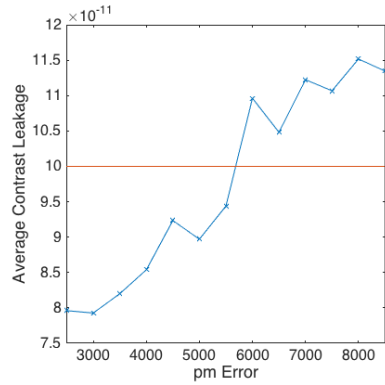


## Global Coma – 5800 pm

Single Random WFE



Average Contrast Leakage of 50 WFEs

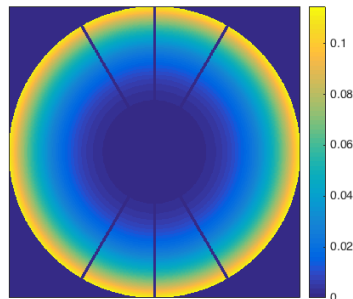


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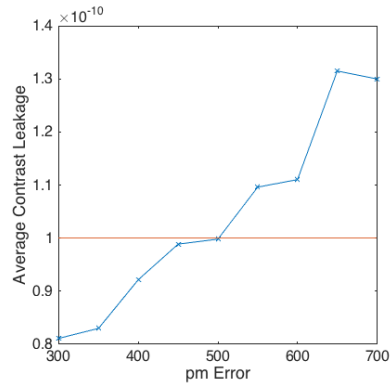


## Global Spherical – 500 pm

Single Random WFE



Average Contrast Leakage of 50 WFEs

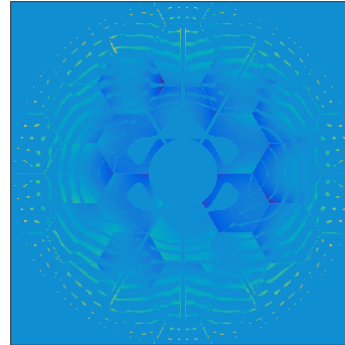


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## Summary

Segments		WFE (pm)
	Piston	10
	Tip / Tilt	20
	Power	30
	Astigmatism	35
	Trefoil	65
Global		
	Power	3000
	Coma	5800
	Spherical	500
Back Plane		
	Bend About X	500
	Bend About Y	120



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## Conclusion

Have developed a tool and methodology to investigate the effect of telescope dynamic modes on coronagraph contrast leakage.

If you give us a coronagraph model, we will use it in this tool.

Future enhancements:

- Look at contrast leakage over smaller ROI at different  $\lambda/D$
- Spectral bandwidth

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