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**A COMPUTER PROGRAM FOR HYDROSTATIC BEARINGS INCLUDING
THE EFFECTS OF NON-UNIFORM FILM THICKNESS AND RELATIVE
VELOCITY FOR VARIOUS METHODS OF LUBRICANT SUPPLY**

by

J. G. Hinkle
V. Castelli
H. C. Rippel
C. D. Zimmerman, Jr.

April, 1964

Prepared for

CALIFORNIA INSTITUTE OF TECHNOLOGY
Jet Propulsion Laboratory

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ABSTRACT

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This is a final report describing the development and use of a computer program for the determination of the load carrying capacity, flow requirements, and righting moments of hydrostatic bearings using an incompressible fluid, including the effects of variable film thickness, relative velocity, and method of lubricant supply. The basic equations, numerical approximations, method of solution, numerical treatment and Fortran Program are presented along with instructions on the use of the program and a sample problem. This work is an extension of that reported in Final Report No. F-B2015 dated January 11, 1963, prepared for California Institute of Technology, Jet Propulsion Laboratory.

Author

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INTRODUCTION

The increasing demands for bearings to support heavy loads have caused the development of hydrostatic lubrication to proceed at an accelerated pace. This was accompanied by a need for more sophisticated analysis of bearing characteristics. For some years hydrostatic bearings have been analyzed by techniques that fell short of a rigorous analysis. This was because of the impossibility of producing by hand an exact analytical solution and, therefore, the necessity for resorting to techniques yielding approximate results, e.g., the electric analog.^{1*}

One of the major shortcomings of the conducting-sheet electric-analog is its inability to treat problems involving non-uniform film thicknesses and relative velocity of bearing members. These problems can often be adequately treated by numerical integration techniques, the utilization of which is only hampered by the extremely lengthy and tedious calculations they require. However, the recent development of high speed digital computers has eliminated this drawback, and numerical integration techniques are at present quite feasible.

In the case at hand, hydrostatic bearings are to be designed for the support of a large radio telescope antenna. A number of rectangular pads will transfer the load of the moving superstructure through the pressurized film of oil to a stationary member on the concrete base. While at first glance the analysis of the bearing (flat slider) appears to offer no problem; in reality, the unit loads are high enough to give rise to non-negligible distortions of the bearing members thus requiring the treatment of variable film thicknesses. While, the particular application involves relatively slow velocity of bearing members, there will be a significant contribution of hydrodynamic effects particularly for favorable film clearance distributions. A previous work² describes in detail the development of a computer program which did not include the effect of relative velocity of bearing members.

*Superscript numerals refer to references at the end of this report.

This report is a complete development of the computer program for the evaluation of pressure distributions, loads, moments, and flows in a hydrostatically-lubricated, rectangular bearing-pad with four or six symmetrically placed rectangular recesses and includes the effect of velocity. The lubricant is to be incompressible, the clearance uniform or non-uniform, and the fluid supply one of the three specified types:

1. Separate pumps feeding each recess
2. Separate pumps feeding opposite pairs of recesses with capillary compensation.
3. Common manifold feeding all recesses with capillary compensation.

This report contains details of the hydrodynamic equations used to analyze the problem, of the numerical technique used for solution, and of the Fortran Program executing the solution complete with block diagrams and flow charts. A guide chart is furnished complete with all the information necessary for using the program and compiling the appropriate input data cards. A sample problem complete with output is also furnished.

BASIC EQUATIONS AND NUMERICAL APPROXIMATIONS

Utilizing the usual lubrication approximations for a continuous film bearing operating with an incompressible lubricant, Reynolds Equation governs the pressure distribution in the clearance space. For bearings with relative motion, Reynolds Equation assumes the following form³

$$\frac{\partial}{\partial x} \left(h^3 \frac{\partial p}{\partial x} \right) + \frac{\partial}{\partial y} \left(h^3 \frac{\partial p}{\partial y} \right) = - 6\mu U \left(\frac{\partial h}{\partial x} \right) \quad [1]$$

For a bearing of rectangular geometry the length of one of the sides can be used as a characteristic length (say L). Then the following dimensionless quantities can be defined in an x-y rectangular coordinate system:

$$X = \frac{x}{L},$$

$$Y = \frac{y}{L},$$

$$H = \frac{h}{c},$$

$$P = \frac{p - p_a}{p_{ref} - p_a}$$

where c is a characteristic film thickness (any value), p_{ref} is a reference pressure (any value), p_a is the ambient pressure (any value), and h and p refer to film thickness and pressure respectively at location (x,y) .

Reynolds equation now assumes the dimensionless form

$$\left(\frac{\partial^2 P}{\partial X^2} + \frac{\partial^2 P}{\partial Y^2} \right) + \frac{3}{H} \left(\frac{\partial H}{\partial X} \frac{\partial P}{\partial X} + \frac{\partial H}{\partial Y} \frac{\partial P}{\partial Y} \right) = - \frac{\Lambda}{H^3} \frac{\partial H}{\partial X} \quad [2]$$

$$\text{where } \Lambda = \frac{6\mu UL}{c^2 (p_{ref} - p_a)}$$

Three types of bearing feed will be used:

- (a) Specified flow to each recess as given by a positive displacement pump feeding the recess.
- (b) Specified total flow to pairs of diametrically opposite recesses as fed by a single constant displacement pump through capillary compensation.
- (c) Single manifold having a specified supply pressure feeding all recesses through capillary compensation.

METHOD OF SOLUTION

The solution of equation [2] can be split into two parts;

- a) a particular solution of the non-homogenous equation.
- b) the solution of the homogeneous equation.

Part (a) is accomplished by solving equation [2] numerically with the conditions that $P = 0$ on the boundaries and all recess areas. This solution shall be called $P_A(X,Y)$. Due to the linearity in P of equation [2], part (b) can be accomplished by the method of superposition. Namely, component solutions, $P_j(X,Y)$, are obtained corresponding to a value of the dimensionless pressure, P , equal to 1 in the j^{th} recess and 0 in all other recesses and at the free boundary. Then the pressure distribution, $P(X,Y)$, corresponding to any operating condition is expressible as the linear combination,

$$P(X,Y) = \sum_j \alpha_j P_j(X,Y) + P_A(X,Y) \quad [3]$$

where α_j is a dimensionless number representing pressure in the j^{th} recess. Defining;

Q_{ij} = flow out of i^{th} recess corresponding to j^{th} component solution.

Q_{iA} = flow out of i^{th} recess corresponding to $P_A(X,Y)$ solution.

The dimensionless flow q_i , out of the i^{th} recess when the pressure distribution $P(X,Y)$ exists is,

$$q_i = \sum_j \alpha_j Q_{ij} + Q_{iA} \quad [4]$$

Integration of the pressure distribution and evaluation of the moments of the pressure distribution with respect to two non-parallel axes (say X and Y) produces the total load (W) and the location of the center of pressure (ξ , η) in the following manner (see Nomenclature):

$$W_j = \iint P_j(X,Y) dXdY \quad j=1, \dots, N, \Lambda \quad [5]$$

$$\xi_j = \iint \frac{P_j(X,Y)X dXdY}{W_j} \quad j=1, \dots, N, \Lambda \quad [6]$$

$$\eta_j = \iint \frac{P_j(X,Y)Y dXdY}{W_j} \quad j=1, \dots, N, \Lambda \quad [7]$$

For the total solution:

$$W = \sum_j \alpha_j W_j + W_\Lambda, \quad [8]$$

$$\xi = \sum_j \frac{\alpha_j \xi_j W_j}{W} + \frac{\xi_\Lambda W_\Lambda}{W}, \quad [9]$$

$$\eta = \sum_j \frac{\alpha_j \eta_j W_j}{W} + \frac{\eta_\Lambda W_\Lambda}{W}, \quad [10]$$

The attractive feature of the method of superposition is that a given set of component solutions can be utilized with any number of feeding methods as long as the bearing geometry is not altered. The computer program is equipped to take advantage of this feature. Specification of the values of the pertinent parameters in the feeding equations leads to the determination of the appropriate values of the coefficients α_j .

In correspondence to the three feeding methods under consideration the determining equations are:

A. Specified Flow to Each Recess:

It is necessary to solve the system

$$q_i = \sum_{j=1}^N \alpha_j Q_{ij} + Q_{i\Lambda} \quad (i = 1, \dots, N) \quad [11]$$

where

q_i = specified quantities (dimensionless)

$Q_{ij}, Q_{i\Lambda}$ = known quantities from component solutions (dimensionless)

Equations (11) form a non-homogeneous system of N algebraic equations in N unknowns (where N is the number of recesses) which can be solved by conventional methods.

B. Specified Flow to Pairs of Recesses With Capillary Compensation.

The following equations hold:

$$QQQ^{(1)} = q_1 + q_2 \quad [12]$$

$$QQQ^{(2)} = q_3 + q_4 \quad [13]$$

$$QQQ^{(3)} = q_5 + q_6 \quad \left. \vphantom{QQQ^{(3)}} \right\} \text{ only for } N = 6 \quad [14]$$

$$q_1 = f_1(p^{(1)} - \alpha_1) \quad [15]$$

$$q_2 = f_2(p^{(1)} - \alpha_2) \quad [16]$$

$$q_3 = f_3(p^{(2)} - \alpha_3) \quad [17]$$

$$q_4 = f_4(p^{(2)} - \alpha_4) \quad [18]$$

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$$\left. \begin{aligned} q_5 &= f_5(p^{(3)} - \alpha_5) \\ q_6 &= f_6(p^{(3)} - \alpha_6) \end{aligned} \right\} \text{only for } N = 6 \quad [19]$$

$$[20]$$

$$q_i = \sum_{j=1}^N \alpha_j Q_{ij} + Q_{iA} \quad (i = 1, \dots, N) \quad [21]$$

The system of $2.5N$ equations [12] through [21] has $2.5N$ unknowns q_i , $\alpha_{j=i}$ ($i = 1 \dots N$), $p^{(K)}$ ($K = 1 \dots N/2$) and can be solved by conventional methods. The quantities $QQQ^{(K)}$ ($K = 1 \dots N/2$) are specified and the f_i 's are known characteristics of the N capillaries.

C. Common Reservoir With Specified Pressure and Capillary Feed to Each Recess.

The following equations hold

$$q_i = f_i(p^{(f)} - \alpha_i) \quad i = 1, \dots, N \quad [22]$$

$$q_i = \sum_{j=1}^N \alpha_j Q_{ij} + Q_{iA} \quad i = 1, \dots, N \quad [23]$$

This system of $2N$ equations in the $2N$ unknowns q_i and α_i ($i = 1, \dots, N$), can be easily solved by conventional methods.

NUMERICAL TREATMENT

Equation [2] is approximated by numerical methods with the adoption of "three point, central difference" formulae. Thus the bearing area is divided in K by M rectangular elements, in the x and y directions respectively. The pressure distribution is represented by these values at the nodal points of the resulting grid.

The coordinates of the nodal points are

$$X_k = (i - 1) \Delta X, \quad [24]$$

$$Y_m = (j - 1) \Delta Y, \quad [25]$$

where i and j designate the location of a particular nodal point in the X and Y directions respectively. (Note that this use of i and j differs from the use of i and j as recess designations.)

For the pressures

$$P_{k,m} = P(X_k, Y_m), \quad [26]$$

$$\left. \frac{\partial P}{\partial X} \right|_{X_k Y_m} = \frac{P_{i+1,j} - P_{i-1,j}}{2 \Delta X}, \quad [27]$$

$$\left. \frac{\partial P}{\partial Y} \right|_{X_k Y_m} = \frac{P_{i,j+1} - P_{i,j-1}}{2 \Delta Y}, \quad [28]$$

$$\left. \frac{\partial^2 P}{\partial X^2} \right|_{X_k Y_m} = \frac{P_{i+1,j} - 2P_{i,j} + P_{i-1,j}}{\Delta X^2} \quad [29]$$

$$\left. \frac{\partial^2 P}{\partial Y^2} \right|_{X_k Y_m} = \frac{P_{i,j+1} - 2P_{i,j} + P_{i,j-1}}{\Delta Y^2}, \quad [30]$$

Equation [2] becomes

$$\begin{aligned} & \frac{P_{i+1,j} + P_{i-1,j}}{\Delta X^2} + \frac{P_{i,j+1} + P_{i,j-1}}{\Delta Y^2} - 2P_{i,j} \left(\frac{1}{\Delta X^2} + \frac{1}{\Delta Y^2} \right) \\ & + \frac{3}{H_{k,m}} \left(\frac{P_{i+1,j} - P_{i-1,j}}{2\Delta X} \left. \frac{\partial H}{\partial X} \right|_{X_k Y_m} + \frac{P_{i,j+1} - P_{i,j-1}}{2\Delta Y} \left. \frac{\partial H}{\partial Y} \right|_{X_k Y_m} \right) \\ & = - \frac{\Lambda}{H^3} \frac{\partial H}{\partial X} \end{aligned} \quad [31]$$

which is solved for $P_{k,m}$.

$$\begin{aligned} P_{k,m} \text{ (evaluated)} &= \frac{1}{2(1+\alpha)} \left[P_{i+1,j} + P_{i-1,j} + \left\{ P_{i+1,j} - P_{i-1,j} \right. \right. \\ & \left. \left. + \frac{2\Lambda\Delta X}{3H_{k,m}^2} \right\} (HX_{i,j}) + \alpha \left\{ P_{i,j+1} + P_{i,j-1} + \left(P_{i,j+1} - P_{i,j-1} \right) (HY_{i,j}) \right\} \right] \\ \alpha &= \left[\frac{\Delta X}{\Delta Y} \right]^2 \end{aligned}$$

where

$$\begin{aligned} HX_{i,j} &= 1.5 \left. \frac{\partial H}{\partial X} \right|_{i,j} \frac{\Delta X}{H_{i,j}} \\ HY_{i,j} &= 1.5 \left. \frac{\partial H}{\partial Y} \right|_{i,j} \frac{\Delta Y}{H_{i,j}} \end{aligned}$$

Starting with an assumed pressure distribution ($P = 1$ in the j^{th} recess and $P = 0$ at the boundaries and in all other recesses for the j^{th} component solution or $P = 0$ at the boundaries and in all recesses for the $N + 1$ component solution), a value of the pressure, $P_{k,m}$, at a grid point is evaluated in terms of the pressure at its four immediately neighboring grid points.

Assuming

$$P'_{k,m} = \gamma P_{k,m}^{(\text{evaluated})} + (1 - \gamma) P_{k,m}^{(\text{old})} \quad [32]$$

to be a new pressure distribution, the process is repeated until negligible changes are obtained from any one iteration. γ is called a "relaxation factor" and its magnitude sets the rate of growth of the pressure distribution. Limiting the value of γ is the well known phenomena of numerical instability.

For excessive values of γ , the rate of growth can be seen to increase steadily in time thereby indicating lack of convergence of the iteration. The occurrence of this phenomenon is internally detected and is automatically eliminated by successive reduction of the value of γ by the factor 0.8. An initial value of $\gamma = 1.5$ was used and was revealed to be overly-optimistic. Hence, an initial value of 1.1 was adopted for this program in order to avoid waste of computer time in unstable iterations.

COMPUTER PROGRAM

The computer program is functionally separated into the following four sub-programs.

(1) Subroutine FORMH

Generation of the bearing geometry gridwork and the clearance distribution either by evaluation of appropriate analytic function or by direct input.

(2) Subroutine TILTH

Tilting by any specifiable amount of the clearance distribution already existing in core storage.

(3) Subroutine REYN

Generation of the component solutions $P_j(X,Y)$ and the corresponding component solution values of the loads W_j , center of pressure coordinates ξ_j , and η_j , and flows $Q_{i,j}$.

(4) Subroutine FLOW

Matching of the component solutions with the proper feeding equations and evaluation of the corresponding pressure distribution $P(X,Y)$, load W , center of pressure coordinates ξ and η , and flows out of each recess, q_j , for any specified feeding conditions.

The program is such that for any given clearance distribution and velocity, the loading and moment results for any of the other feeding methods can be evaluated by repeated, direct entry into Subroutine Flow. It is also possible to make available to the computer the essential results of component solutions W_j , ξ_j , η_j , $Q_{i,j}$ by direct input, so that new feeding conditions can be studied in combination with component solutions obtained during a previous group of runs.

The internal generation of the clearance distribution is executed by a function of the following type.

$$\text{Define } X - X_0 = s \quad \text{where } X_0 = A_{22}$$

$$Y - Y_0 = t \quad Y_0 = A_{23}$$

then

$$\begin{aligned} H_1(X, Y) = & A_1 + A_2 s + A_3 t + A_4 s^2 + A_5 t^2 + A_6 s t + A_7 s^3 \\ & + A_8 t^3 + A_9 s^2 t + A_{10} s t^2 + A_{11} \sqrt{A_{12} + A_{13} s^2 + A_{14} t^2} \\ & + A_{15} \cos(A_{16} s) + A_{17} \cos(A_{18} t) + A_{19} \cos(A_{16} s) \cos(A_{18} t) \\ & - A_{20} \left\{ e^{-A_{21} X} \cos(A_{21} X) + e^{-A_{21}(1-X)} \cos[A_{21}(1-X)] \right. \\ & \left. - 2e^{-\frac{1}{2}A_{21}} \left[\cos\left(\frac{1}{2}A_{21}\right) \right] \right\} \end{aligned} \quad [33]$$

The inclusion of the part of the preceeding expression containing the coefficients A_{20} and A_{21} was motivated by the results of analyses of the deformation of a beam on elastic foundations under a uniformly distributed load over a finite region⁴.

The constants A_{20} and A_{21} are defined as,

$$A_{20} = \frac{\text{load per unit length}}{2kc}$$

$$A_{21} = \Lambda' = \lambda L$$

where

$$\lambda = \sqrt[4]{k/4 E I}$$

It should be noticed that these terms detract from any clearance distribution given by the remainder of the formula an amount equal to the difference between the deflection at the center and the deflection at any point. It is also the task of FORMH to compile an internal tabulation of the derivatives of the clearance distribution necessary for the solution.

Subroutine TILTH acts by the use of the following formula:

$$H(X,Y) = H_1(X,Y) + T_x(X-X_1) + T_y(Y-Y_1) \quad [34]$$

where: $H_1(X,Y)$ represents the distribution of clearance which is to be modified (tilted).

This corresponds to saying that the line,

$$T_x(X - X_1) + T_y(Y - Y_1) = 0$$

is the hinge and that the bearing is tilted in space by an amount,

$$\theta = T_x^2 + T_y^2 \quad [35]$$

This feature is particularly useful in the evaluation of restoring moments corresponding to misalignments. The use of TILTH is optional.

In the use of subroutine REYN, it is important to adopt an appropriate value of the truncation constant (TRUNC). Indeed, a large value of TRUNC will accept component solutions that are only a rough approximation to the asymptotic solution, whereas, exceedingly small values of TRUNC will result in wastefully long computation time.

Originally, TRUNC was evaluated within the computer program as the change in the summation of pressure values at all of the active sill points from one iteration to the next divided by the number of active sill points. This was found to be unrealistic in that for a given value of TRUNC the degree of convergence varied considerably depending upon total grid size ($X + 1$ by $M + 1$) and relative recess sizes (with respect to bearing size). After further study it was found that a more realistic truncation criteria is the change in the summation of pressure values at all of the active sill points from one iteration to the next multiplied by the total number of grid points and divided by the product of γ and the summation of the pressure values at all of the active sill points.

Figure 1 shows the number of iterations required (as a function of TRUNC) to satisfy various assigned values of TRUNC for a typical large-size grid. Figure 2 shows the convergence of the dimensionless recess pressures and dimensionless recess loads. It can be seen that a truncation constant (TRUNC) of approximately 0.3 yields results that agree with the probable asymptotic value within less than one percent and require approximately 230 iterations. This is a reasonable compromise between accuracy and computer time. Several other gridwork sizes and configurations investigated have yielded satisfactory results using 0.3 for the truncation constant.

It was mentioned previously that the value of the relaxation factor γ is internally adjusted to cope with numerical instability. However, if persistent occurrence of this phenomenon forces the adoption of a value of γ lower than 0.16, subroutine REYN abandons the solution, and a note to this effect is introduced in the output tape.

Use of subroutine REYN requires the specification of the quantity LITER. Termination of the iteration is forced whenever a number of iterations equal to LITER have been performed regardless of the truncation criterion. As presently set up, the program will allow a

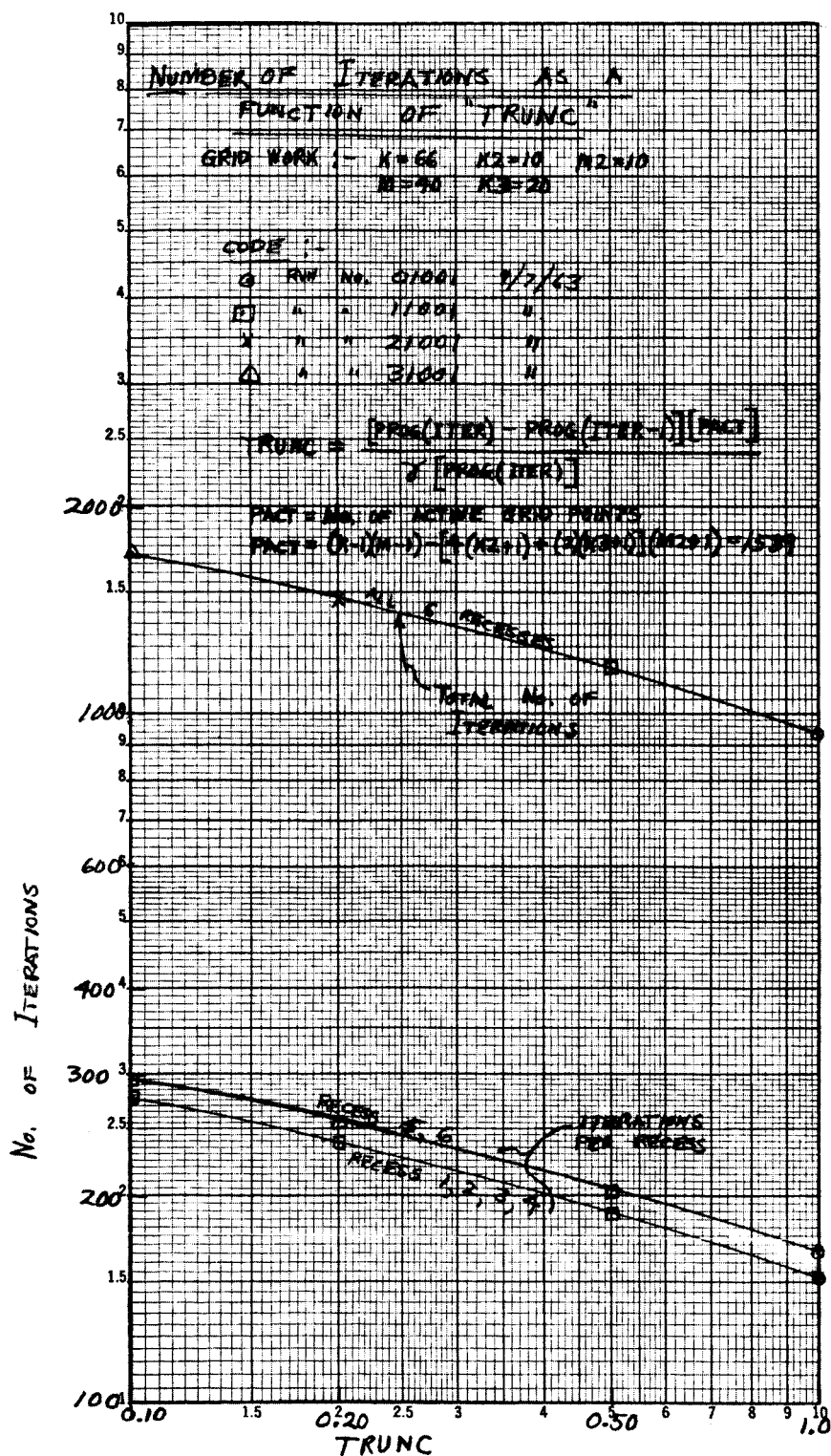


Fig. 1 - NUMBER OF ITERATIONS AS A FUNCTION OF "TRUNC"

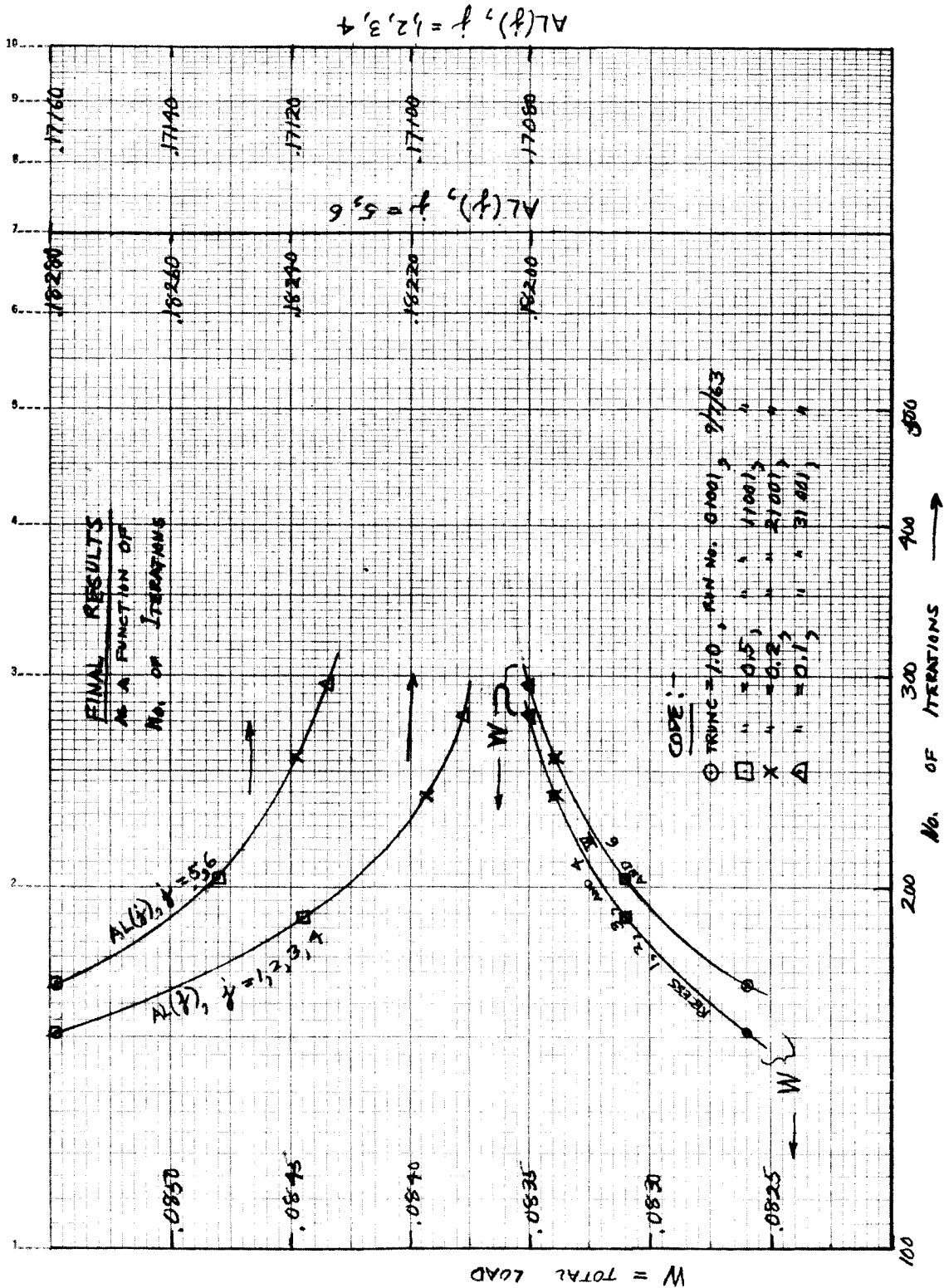


Fig. 2 - FINAL RESULTS AS A FUNCTION OF THE NUMBER OF ITERATIONS

value of LITER up to 1000. If larger values become desirable, the dimension of PROG in Subroutine REYN should be altered to the maximum value of LITER.

The operation of Subroutine FLOW is controlled by the specification of NCASE which, assuming one of the values 1, 2, or 3, indicates the adoption of the first, second, or third feeding method respectively.

The quantity IOUT enables the user to obtain the pressure and clearance profiles on the output tape (IOUT = 1). A value of IOUT = 0 specifies that output of those distributions is not desired. If IOUT = 2, the pressure profile only will appear in the output. If IOUT = 3, the clearance profile only will appear in the output.

The information in Table I will be useful in handling the quantities used in the program.

Subroutine FLOW makes use of a FUNCTION subprogram (FUNCTION DETER) in order to evaluate 4 x 4 or 6 x 6 determinants.

The utilization of the above mentioned sub-programs in the solution of specific problems is coordinated by the MAIN program. Specification of the quantity NSWICH instructs the program to solve one of six possible problems:

NSWICH = 1; CALL EXIT

NSWICH = 2; Solve non-velocity flow problem only with read-in values of W_j , ξ_j , η_j , $Q_{i,j}$.

NSWICH = 3; Solve new flow problem with component solutions already existing in core storage.

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Table I - PROGRAM QUANTITIES

Equation	Fortran Symbol	Output Name
$W_j = \frac{w_j}{L^2(p_{ref} - p_a)}$	W(I)	W(I)
$\xi_j = \frac{x_j}{L}$	CSI(I)	CSI(I)
$\eta_j = \frac{y_j}{L}$	ETA(I)	ETA(I)
$Q_{i,j} = \frac{q_{rc} (12\mu)}{(p_{ref} - p_a)c^3}$	Q(I,J)	Q(I,J)
$q_i = \frac{q_{ri} (12\mu)}{(p_{ref} - p_a)c^3}$	QQ(I)	QQ(I)
$QQQ(K) = \frac{q_{2ri} (12\mu)}{(p_{ref} - p_a)c^3}$	QQQ(K)	Pump Flows
$f_i = 0.2945 \frac{d^4}{lc^3}$	FF(I)	Capillary Factors F(I)
$p^{(f)} = \frac{p_s - p_a}{p_{ref} - p_a}$	PF	Common Constant Pressure
$P_{i,j} = \frac{p_{i,j} - p_a}{p_{ref} - p_a}$	PPPP(I,J)	Pressure Distribution
$\alpha_j = \frac{(p_r)_j - p_a}{p_{ref} - p_a}$	AL(L)	Recess Pressures, AL(j), j=1-N
$W = \frac{w}{L^2(p_{ref} - p_a)}$	WW	Total Load
$\xi = \frac{M_{x=0}}{wL}$	CCSI	CSI
$\eta = \frac{M_{y=0}}{wL}$	EETA	ETA

NSWICH = 4; Entirely new problem with or without velocity.

NSWICH = 5; Tilt clearance distribution existing in core storage and solve resulting problem.

NSWICH = 6; Solve the previous problem considering velocity.

In the event NSWICH = 2, the quantity NIMJ should be specified to inform the computer of the number of recesses in the pad under consideration.

Appendix I contains a block diagram of the entire program, the detailed flow charts, Fortran instruction listings, and IBM 7094 compilation records of the six subprograms (MAIN, FLOW, REYN, TILTH, FORMH, DETER).

Appendix II contains the loading record for use with an IBM 7094. This information is essential if the allowable grid size of 67 x 45 is to be extended.

USE OF THE PROGRAM AND SAMPLE PROBLEMS

A. Input

In order to use the program, the proper input data for the problem to be solved must be put on cards in a prescribed manner. The Input Guide Chart shown in Appendix III indicates the necessary data to be put on cards, its proper format, and the proper sequence of such cards. Figure 3 shows the standard form which is used to facilitate the preparation of punched cards. All of the input data required for solving a single problem is entered in the proper blocks of Figure 3. The number at the upper right-hand corner of each block is for the convenience of the typist to obtain proper word location when right-indexing is used. The following is a detailed explanation of how to specify the numbers to be entered in Figure 3 for proper execution of the particular problem to be solved.

1. Card No. 1 (always required)

The following input data are required in MAIN program

- a. NSWICH: - Any number 1 through 6 may be entered as dictated by the following:
 - 1 = Last problem has been solved. Terminate program.
 - 2 = Solve flow problem only using basic solution results contained on input cards. It should be noted that the input form, Fig. 3, does not allow for these required cards. See the Input Guide Chart in Appendix III for the proper formats and card sequence.
 - 3 = Solve new flow problem with basic solution already in machine (as obtained from previous problem solved).
 - 4 = New problem to be solved.

HYDROSTATIC BEARING PROGRAM INPUT DATA GUIDE
(CROSS OUT CARDS NOT USED)

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CARD NUMBER

① CARD
ARD
NSWICH NIMJ NIGNAL

② 1 CARD
K M INDEX 1 INDEX 2 KI K2 K3 MI M2 AL

③ 5 CARDS (INCLUDE ALL 5)
A(1) A(2) A(3) A(4) A(5)
A(6) A(7) A(8) A(9) A(10)
A(11) A(12) A(13) A(14) A(15)
A(16) A(17) A(18) A(19) A(20)
A(21) A(22) A(23) A(24) A(25)

④ 1 CARD
XI YI TX TY

⑤ 1 CARD
LITER TRUNC PLAM

⑥ 1 CARD
NRVN NCASE IOUT

⑦ 1 CARD
QQ(1) QQ(2) QQ(3) QQ(4) QQ(5) QQ(6)
QQQ(1) QQQ(2) QQQ(3)

⑧ 1 CARD
PF

⑨ 1 CARD
FF(1) FF(2) FF(3) FF(4) FF(5) FF(6)

⑩ 1 CARD
NSWICH

Fig. 3 - HYDROSTATIC BEARING PROGRAM INPUT DATA GUIDE

- 5 = The distribution of clearance already in the machine will be tilted and new basic solutions and final results for the new clearance distribution will be obtained.
 - 6 = The previous zero-velocity problem will be solved considering velocity.
 - b. NIMJ: - If NSWICH = 2 is used, then the value of NIMJ is equal to the total number of recesses. Otherwise NIMJ is left blank.
 - c. NIGNAL: - A 1 is entered here if velocity (PLAM) is to be considered. Otherwise PLAM will not be used by the program.
2. Card No. 2 (Only required when NSWICH = 4)
- The following input data are required in Subroutine FORMH
- a. K: - This is the number of cells in the X-direction formed by the gridwork which simulates the pad. (See Fig. 5). K must be even. The maximum value of K allowed is 66*. (See Section B below.)
 - b. M: - This is the number of cells in the Y-direction formed by the gridwork. (See Fig. 5). M must also be even. The maximum value of M allowed is 44*. (See Section B below.)
 - c. INDEX 1: - If the clearance distribution is to be read in from cards then the value 1 is used for INDEX 1. It should be noted that the standard input form, Fig. 3, does not allow for these required cards. Consult the Input Guide Chart in Appendix III for the proper format and card sequence. If the clearance distribution is to be generated within the machine, INDEX 1 is not equal to 1 (normally left blank).
 - d. INDEX 2: - If the clearance distribution as read in from cards or generated internally (per INDEX 1) is to be tilted, then INDEX 2 = 1. Otherwise, INDEX 2 is not equal to 1.

*The allowable gridwork size $(K + 1) \times (M + 1)$ may be increased by changing all of the subscripted dimension statements from (67,45) to $\left[\begin{matrix} (K+1)_{\max} & (M+1)_{\max} \end{matrix} \right]$.

- e. K1: - This is the number of cells in the X-direction between edges of pad and recesses 1, 2, 3 and 4. (See Section B below.)
 - f. K2: - This is the number of cells representing the length of recesses 1, 2, 3 and 4 in the X-direction. (See Section B below.)
 - g. K3: - This is the number of cells representing the length of recesses 5 and 6 in the X-direction. If only a total of four recesses are to be used, $K3 = 0$. K3 must be an even number (See Section B below.)
 - h. M1: - This is the number of cells in the Y-direction between edges of pad and all of the recesses. (See Section B below.)
 - i. M2: - This is the number of cells representing the width of the recesses in the Y-direction (See Section B below.)
 - j. AL: - This is the ratio of the length of the pad in the Y-direction and the length of the pad in the X-direction (See Fig. 4). $AL = LY/LX$. (See Section B below.)
3. Card Numbers 3 through 7 (Used only if $NSWICH = 4$ and $INDEX \neq 1$)

The following input data are required in Subroutine FORMH.

- a. A(1) thru A(23): - These are the values of the 23 constants used to generate the clearance distribution within the computer. It is important to note that all five cards must be used even if the values contained on any of them are all zeros.
4. Card No. 8 (Used only when; $NSWICH = 4$ and $INDEX\ 2 = 1$, or $NSWICH = 5$)

The following input data are required in Subroutine TILTH.

- a. X1: - The value to be used is the dimensionless distance in the X-direction to the line about which it is desired to rotate the pad. X1 can be any value between 0 and 1. If X1 is 0 then the pad will be rotated about the $I = 1$ gridwork line. If $X1 = 1$, the pad will be rotated about the $I = (K+1)$ gridwork line. If $1X = 0.5$, the pad will be rotated about the center line $I = K/2 + 1$, and so forth.

The value of X1 need not necessarily fall on a gridwork line.

- b. Y_1 : - The value to be used is the dimensionless distance in the Y-direction to the line about which it is desired to rotate the pad. Y_1 can be any value between 0 and AL. If $Y_1 = 0$ then the pad will be rotated about the $J = 1$ gridwork line. If $Y_1 = AL$, the pad will be rotated about the $J = (M+1)$ gridwork line, and so forth. The value of Y_1 need not necessarily fall on a gridwork line.
- c. TX : - The value of TX required to obtain a specific amount of tilt about X_1 may be obtained using the following equation:

$$TX = [H(1, AL/2) - H(0, AL/2)] - [H_1(1, AL/2) - H_1(0, AL/2)] \quad [36]$$

where $H(1, AL/2)$ = desired value of H at $X = 1$, $Y = AL/2$
 $H(0, AL/2)$ = desired value of H at $X = 0$, $Y = AL/2$
 $H_1(1, AL/2)$ = previous value of H at $X = 1$, $Y = AL/2$
 $H_1(0, AL/2)$ = previous value of H at $X = 0$, $Y = AL/2$

- d. TY : - The value of TY required to obtain a specific amount of tilt about Y_1 may be obtained by using the following equation:

$$TY = [H(1/2, AL) - H(1/2, 0)] - [H_1(1/2, AL) - H_1(1/2, 0)] \quad [37]$$

where $H(1/2, AL)$ = desired value of H at $X = 1/2$, $Y = AL$
 $H(1/2, 0)$ = desired value of H at $X = 1/2$, $Y = 0$
 $H_1(1/2, AL)$ = previous value of H at $X = 1/2$, $Y = AL$
 $H_1(1/2, 0)$ = previous value of H at $X = 1/2$, $Y = 0$

5. Card No. 9 (used only if NSWICH = 4, 5 or 6)

The following input data are required in Subroutine REYN.

- a. LITER: - Maximum number of iterations allowable to obtain a component solution. When this number of iterations is reached, the iteration procedure will stop and rest of problem will be solved using component solutions obtained.

- b. TRUNC: - This is the value assigned to the truncation constant. Usually, a value of $TRUNC = 0.30$ yields adequate convergence. However, it is usually good practice to experimentally evaluate a satisfactory value for a particular grid work pattern by varying the assigned value of $TRUNC$ and observing the convergence of the final results.

- c. PLAM: - The number assigned to $PLAM$ is Λ , where

$$\Lambda = \frac{6\mu U L}{(p_{ref} - p_a)c^2}$$

Since $(p_{ref} - p_a)$ is an unknown value prior to solution, $PLAM$ is usually assigned a magnitude of 1.0 although any number may be used.

6. Card No. 10 (always used)

The following input data are required in Subroutine FLOW

- a. NRUN: - The identifying run number is inserted in this block.
- b. NCASE: - The method of feeding code number is inserted in this block per the following:
 - 1 = separate constant displacement pumps feeding each recess.
 - 2 = one constant displacement pump feeding two opposite recesses, i.e., in Fig. 4, one pump feeds recesses 1 and 2, one pump feeds recesses 3 and 4, and the third pump (if used) feeds recesses 5 and 6 with capillary tubes used between pumps and recesses they feed.
 - 3 = common pressure regulated supply manifold feeding each recess through capillary tubes.
- c. IOUT: - The number used here dictates the output desired with regard to clearance and pressure distributions per the following code.
 - 0 = do not print out clearance and pressure distribution.
 - 1 = print out clearance and pressure distribution.
 - 2 = print out pressure distribution only.
 - 3 = print out clearance distribution only.

7. Card No. 11 (Used only if NCASE = 1 or 2)

The following input data are required in Subroutine FLOW.

- a. QQ(1), ... QQ(N): - If NCASE = 1, the values of $q_1 \dots q_N$ are inserted in the first N blocks. N is either 4 recesses or 6 recesses. q_1 is the constant flow to each recess.

- or,
b. QQQ(1), ... QQQ(N/2): - If NCASE = 2, the values of $q_1 \dots q_{N/2}$ to be used are,

$$QQQ(1) = q_1 + q_2$$

$$QQQ(2) = q_3 + q_4$$

$$QQQ(3) = q_5 + q_6 \text{ (if used)}$$

Note: - If NCASE = 3, this card (number 11) is not used.

8. Card No. 12 (Used only if NCASE = 3)

The following input data is required in Subroutine FLOW.

- a. PF: - The number to be used here is the dimensionless manifold pressure, $p^{(f)}$ where

$$p^{(f)} = \frac{(p_s - p_a)}{(p_{ref} - p_a)} = \frac{q_i}{f_i} + \alpha_j \quad [38]$$

Since q_i and α_j are unknown, a value of $p^{(f)} = 1.0$ is usually used although any number may be used.

9. Card No. 13 (Used only if NCASE = 2 or 3)

The following input data is required in Subroutine FLOW.

- a. FF(1), ... FF(N): - Any number may be assigned for FF(I) (the capillary constant, f_i). N is either 4 or 6 recesses. Hence 4 or 6 values of FF(I) are required.

10. Card No. 14 (Used only if previous cards are last problem to be solved).

The following input data is required in the MAIN program.

- a. NSWICH: - The number 1 is used to indicate that last problem has been solved.

B. Selection and Specification of Gridwork Pattern to be Used

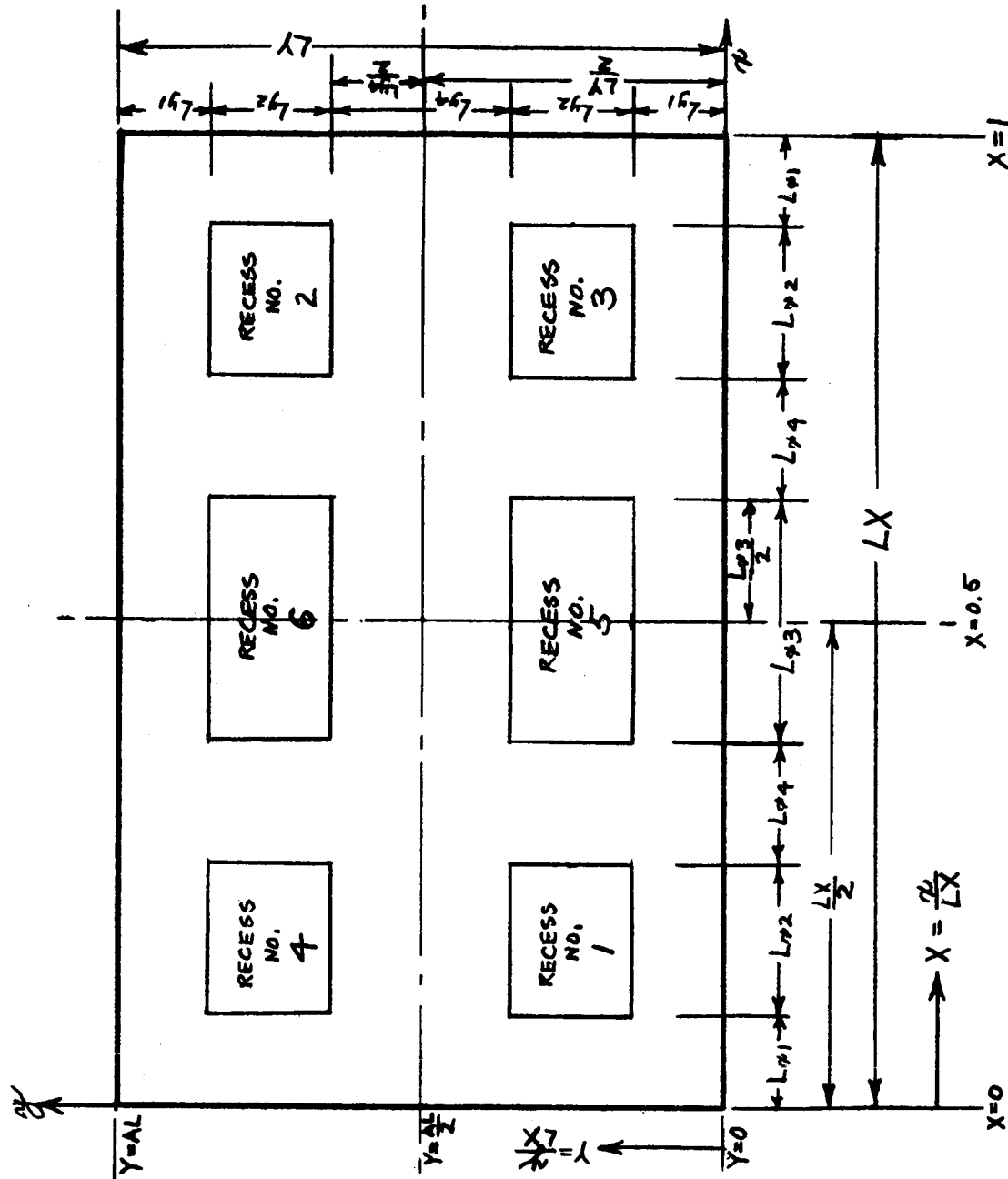
As has been previously indicated it is necessary that a proper balance be achieved between maximum and minimum number of grid points to be used in order to achieve reasonably accurate results without an undue amount of computer time. It should also be evident that there may have to be some compromise between recess size and locating dimensions and computer program gridwork. That is, some of the recess dimensions desired to be used may have to be slightly modified in order to fit into a finite grid point pattern.

Figure 4 shows the required geometry of a 6-recess pad. Note that if a four recess pad is to be considered, the dimension L_{x3} is equal to zero. In order to illustrate how a suitable grid work may be selected and specified, consider the pad of Figure 4 to have the following dimensions:

<u>X-Direction</u>	<u>Y-Direction</u>
$LX = 32.0''$	$LY = 30.0''$
$L_{x1} = 3.0''$	$L_{y1} = 4.5''$
$L_{x2} = 5.0''$	$L_{y2} = 6.0''$
$L_{x3} = 8.0''$	$L_{y4} = 9.0''$
$L_{x4} = 4.0''$	

The first step is to select the smallest sill dimension in the x-direction (L_{x1} or L_{x4} for 6-recesses, L_{x1} or $2L_{x4}$ for 4-recesses) and the y-direction (L_{y1} or L_{y4}). For the above problem we would select,

$$L_{x1} = 3.0'' \text{ and } L_{y1} = 4.5''$$



GEOMETRY OF 6-RECESS PAD
 ($L_{p3} = 0$ FOR 4-RECESS PAD)

Fig. 4 - GEOMETRY OF 6-RECESS PAD

We can write the following equations;

$$\left. \begin{aligned} K_2 &= K_1 \left(\frac{L_{x2}}{L_{x1}} \right) & M_2 &= M_1 \left(\frac{L_{y2}}{L_{y1}} \right) \\ K_3 &= K_1 \left(\frac{L_{x3}}{L_{x1}} \right) & M_4 &= M_1 \left(\frac{L_{y4}}{L_{y1}} \right) \\ K_4 &= K_1 \left(\frac{L_{x4}}{L_{x1}} \right) & M &= M_1 \left(\frac{L_y}{L_{y1}} \right) \\ K &= K_1 \left(\frac{L_x}{L_{x1}} \right) \end{aligned} \right\} \quad [39]$$

Substituting the pad dimensions into equations [39] yields,

$$\left. \begin{aligned} K_2 &= \frac{5}{3}(K_1) & M_2 &= \frac{4}{3}(M_1) \\ K_3 &= \frac{8}{3}(K_1) & M_4 &= 2(M_1) \\ K_4 &= \frac{4}{3}(K_1) & M &= \frac{20}{3}(M_1) \\ K &= \frac{32}{3}(K_1) \end{aligned} \right\} \quad [40]$$

If we now select a number of integer values for K_1 we can evaluate all of the other values of interest. In order to have at least one grid point in the sill, K_1 , and M_1 (or K_4 and M_4 if $L_{x4} < L_{x1}$, and $L_{y4} < L_{y1}$) must be at least 2. The following table summarizes the results obtained when various integer values of K_1 are used in equations [40].

K1	K2	K3 (Even)	K4	K (Even)
2	$3-1/3 = 3$	$5-1/3 = 6$	$2-2/3 = 3$	$21-1/3 = 22$
3	5 = 5	8 = 8	4 = 4	32 = 32
4	$6-2/3 = 7$	$10-2/3 = 10$	$5-1/3 = 5$	$42-2/3 = 42$
5	$8-1/3 = 8$	$13-1/3 = 14$	$6-2/3 = 7$	$53-1/3 = 54$
6	10 = 10	16 = 16	8 = 8	64 = 64
7	$11-2/3 = 12$	$18-2/3 = 18$	$9-1/3 = 9$	$74-2/3 = 74$
8	$13-1/3 = 13$	$21-1/3 = 22$	$10-2/3 = 11$	$85-1/3 = 86$

M1	M2	M4 (Even)	—	M (Even)
2	$2-2/3 = 3$	4	—	$13-1/3 = 14$
3	4 = 4	6	—	20 = 20
4	$5-1/3 = 5$	8	—	$26-2/3 = 26$
5	$6-2/3 = 7$	10	—	$33-1/3 = 34$
6	8 = 8	12	—	40 = 40
7	$9-1/3 = 9$	14	—	$46-2/3 = 46$
8	$10-2/3 = 11$	16	—	$53-1/3 = 54$

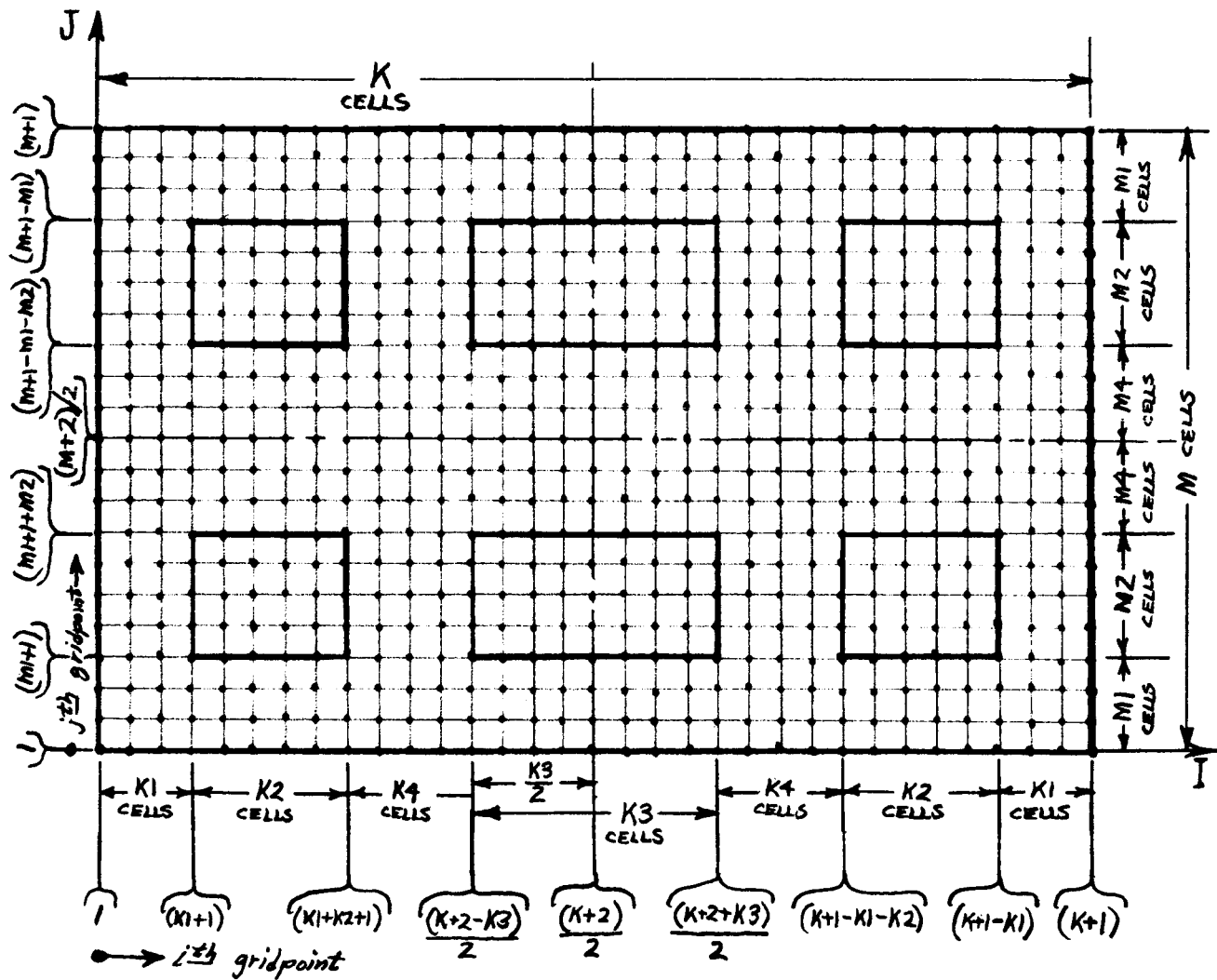
The following items should be noted in the above table.

1. The fractional values when obtained for K₂, K₄ are rounded-off to the nearest odd or even integer.
2. The fractional values when obtained for K₃, K, M₄ and M are rounded-off to the nearest even integer.
3. The values obtained for K₁ = 7 and K₁ = 8 should not be considered since K > 66. (maximum value currently permissible).

While it is permissible to use any combination of the above listed values of K₁ and M₁ (except K₁ = 7 or 8) we can further narrow down the combination to be selected by considering the following:

1. The maximum value of K₁, M₁, K₄ and M₄ should not be greater than 8 in order to yield 7 or less active sill grid points between adjacent recesses or between any recess and the outer periphery of the pad in order to keep computer time within reasonable limits. On this basis we would, therefore, eliminate from consideration K₁ = 7 or 8, M₁ = 5, 6, 7 or 8.
2. While it is permissible to use only one active sill point (K₁ = 2 and M₁ = 2) it is not recommended if other permissible values exist. On this basis we would, therefore, eliminate from consideration K₁ = 2 and M₁ = 2.
3. This leaves us with possible combinations of K₁ = 3, 4, 5 or 6 and M₁ = 3 or 4. Notice that for K₁ = 4 and 5 and for M₁ = 4, that non-integer values were obtained. This means for these values, the resulting grid work will only approximate the actual pad and recess dimensional relationship. On this basis, we therefore eliminate from consideration K₁ = 4 and 5 and M₁ = 4.
4. This leaves us with two possible combinations, K₁ = 3, M₁ = 3 or K₁ = 6, M₁ = 3. Of these two we would select the smaller grid combination (K₁ = 3, M₁ = 3) in order to conserve computer time.

The resulting grid work for K₁ = 3 and M₁ = 3 is shown in Figure 5. The values of K₁ = 3, K₂ = 5, K₃ = 8, K = 32, M₁ = 3, M₂ = 4 and M = 20 are the values that would be entered on input card no. 2 of Fig. 3.



GRIDWORK FOR 6-RECESS PAD
(K3 = 0 FOR 4-RECESS PAD)

Fig. 5 - GRIDWORK FOR A 6-RECESS PAD

C. Output

The output of the program consists of two result pages and a listing of the pressure and clearance distributions over the grid. The first output page contains:

1. Run number
2. Title containing information on bearing type (hybrid includes velocity), number of recesses, and feeding method.
3. Value of Lambda, if used
4. Grid work data
5. Clearance distribution coefficients (for non-zero values)
6. Values of essential results of the component solutions.
7. Final results
8. Recess pressures

The second page contains:

1. Run number
2. Title containing information on bearing type (hybrid includes velocity), number of recesses, and feeding method.
3. A digit array representing configuration of pad with the following code.
 - 0 = external boundary point
 - 1 = recess point
 - 2 = sill point

D. Relationships Among the Dimensionless Variables

A number of dimensionless quantities are defined and evaluated by the computer program. These are:

$$\text{Load Factor} = W = \frac{W}{L^2(p_{\text{ref}} - p_a)} \quad [41]$$

$$\text{Flow Factor} = q_i = \frac{q_{ri} (12\mu)}{c^3(p_{\text{ref}} - p_a)} \quad [42]$$

$$\text{Film Thickness Factor} = H_{i,j} = \frac{h_{i,j}}{c} \quad [43]$$

$$\text{Velocity Factor} = \Lambda = \frac{6\mu UL}{c^2(p_{\text{ref}} - p_a)} \quad [44]$$

$$\text{Recess Pressure Factor} = \alpha_j = \frac{(p_r)_j - p_a}{(p_{\text{ref}} - p_a)} \quad [45]$$

Supply Pressure Factors

Separate pumps feeding each recess (Case 1)

$$\alpha_{js} = \alpha_j \quad [46]$$

One pump feeding two recess thru capillary tubes (Case 2)

$$p_i^{(K)} = \frac{q_i}{f_i} + \alpha_j \quad [47]$$

Each recess fed through capillary tubes from a common supply manifold (Case 3)

$$p^{(f)} = \frac{q_i}{f_i} + \alpha_j = PF \quad [48]$$

Capillary Factors

Case 1; $f_i = \infty$ [49]

Case 2; $f_i = \frac{q_i}{(p_i^{(K)} - \alpha_j)}$ [50]

Case 3; $f_i = \frac{q_i}{(p_i^{(f)} - \alpha_j)}$ [51]

Moment Factors

Component about X = 0

$$\xi = \frac{M_{XO}}{wL} \quad [52]$$

Component about Y = 0

$$\eta = \frac{M_{YO}}{wL} \quad [53]$$

Depending upon the feeding method used, the values of the above mentioned dimensionless quantities are either assigned as input or evaluated within the computer program. The following table indicates whether the quantities are specified as input, (I), appear as output (O), or are able to be evaluated from the output (E).

Dimensionless Factor	FEEDING METHOD		
	Separate Pumps Feeding Each Recess	Separate Pumps Feeding Two Recesses Through Capillaries	Common Manifold at Fixed Pressure Through Capillaries
W	O	O	O
q_i	I	I	O
$H_{i,j}$	I	I	I
Λ	I	I	I
α_j	O	O	O
ξ	O	O	O
η	O	O	O
$p^{(K)}$	—	E	—
$p^{(f)}$	—	—	I
f_i	—	I	I

From the above listed dimensionless factors we can obtain relations useful for evaluating the dimensional quantities of the variables of interest. The following relationships may be derived using the above listed dimensionless factors.

Load-Film Thickness-Flow Coefficient

$$\frac{w(h_{i,j})^3}{L^2 q_{ri} \mu} = \frac{12(W)(H_{i,j})^3}{(q_i)} = (\overline{LHQ_i}) \quad [54]$$

Load-Film Thickness-Velocity Coefficient

$$\frac{L^3 \mu U}{w(h_{i,j})^2} = \frac{(\Lambda)}{6(W)(H_{i,j})^2} = (\overline{LHV}) \quad [55]$$

Film Thickness-Flow-Velocity Coefficient

$$\frac{UL(h_{i,j})}{q_{ri}} = \frac{2(\Lambda)(H_{i,j})}{(q_i)} = (\overline{HQ_i V}) \quad [56]$$

Load-Flow-Velocity Coefficient

$$U \left[\frac{L^5 \mu}{q_{ri}^2 w} \right]^{1/3} = \frac{2(\Lambda)}{[12(W)(q_i)^2]^{1/3}} = (\overline{LQ_i V}) \quad [57]$$

Load-Film Thickness-Flow-Velocity Coefficient

$$\frac{w(h_{i,j})^4 U}{q_{ri}^2 L \mu} = \frac{24(W)(H_{i,j})^4 (\Lambda)}{(q_i)^2} = (\overline{LHQ_i V}) \quad [58]$$

Recess Pressure Coefficient

$$\frac{(p_{rj} - p_a)L^2}{w} = \frac{(\alpha_j)}{(W)} = (\overline{PR_j W}) \quad [59]$$

Supply Pressure Coefficients

Case 1 feed method;

$$\frac{(p_{sj} - p_a)L^2}{w} = \frac{(\alpha_j)}{(W)} = (\overline{PS_j W1}) \quad [60]$$

Case 2 feed method;

$$\frac{(p_{sj} - p_a)L^2}{w} = \frac{(q_i/f_i) + (\alpha_j)}{(W)} = (\overline{PS_j W2}) \quad [61]$$

Case 3 feed method;

$$\frac{(p_{sj} - p_a)L^2}{w} = \frac{(q_i/f_i) + (\alpha_j)}{(W)} = (\overline{PS_j W3}) \quad [62]$$

Pressure Ratio Coefficients

Case I feed method;

$$\frac{(p_{rj} - p_a)}{(p_{sj} - p_a)} = 1.0 = (\overline{\beta_{j1}}) \quad [63]$$

Case 2 feed method;

$$\frac{(p_{rj} - p_a)}{(p_{sj} - p_a)} = \frac{(\alpha_j)}{(q_i/f_i) + (\alpha_j)} = (\overline{\beta_{j2}}) \quad [64]$$

Case 3 feed method;

$$\frac{(p_{rj} - p_a)}{(p_{sj} - p_a)} = \frac{(\alpha_j)}{(p(f))} = (\overline{\beta_{j3}}) \quad [65]$$

Pad Righting Moment-Load Coefficients (about pad center)

Component (about $X = 0.5$)

$$\frac{M_X}{wL} = (0.5 - \xi) = (\overline{MXW}) \quad [66]$$

Component [about $Y = 0.5 (AL)$]

$$\frac{M_Y}{wL} = [0.5(AL) - \eta] = (\overline{MYW}) \quad [67]$$

Total moment coefficient (about pad center)

$$\frac{M}{wL} = \left[(1/2 - \xi)^2 + (AL/2 - \eta)^2 \right]^{\frac{1}{2}} = (\overline{MW}) \quad [68]$$

Direction Angle

$$\phi = \tan^{-1} \left\{ \frac{(AL/2 - \eta)}{(1/2 - \xi)} \right\} = (\overline{MANG}) \quad [69]$$

Pad Righting Moment-Film Thickness-Flow Coefficient

Component about $X = 0.5$

$$\frac{M_X (h_{i,j})^3}{L^3 q_{ri} \mu} = \frac{12(1/2 - \xi)(W)(H_{i,j})^3}{(q_i)} = (\overline{MXHQ_i}) \quad [70]$$

Component about $Y = 0.5(AL)$

$$\frac{M_Y (h_{i,j})^3}{L^3 q_{ri} \mu} = \frac{12(AL/2 - \eta)(W)(H_{i,j})^3}{(q_i)} = (\overline{MYHQ_i}) \quad [71]$$

Total moment

$$\frac{M(h_{i,j})^3}{L^3 q_{ri} \mu} = \frac{12(W)(H_{i,j})^3}{(q_i)} \left[(1/2 - \xi)^2 + (AL/2 - \eta)^2 \right]^{1/2} \quad [72]$$

E. Sample Problems

A flat bearing pad having the dimensions shown in Figure 6 is to be analyzed using the computer program. Each recess is fed from a separate constant displacement pump for the following conditions of clearance distribution and velocity.

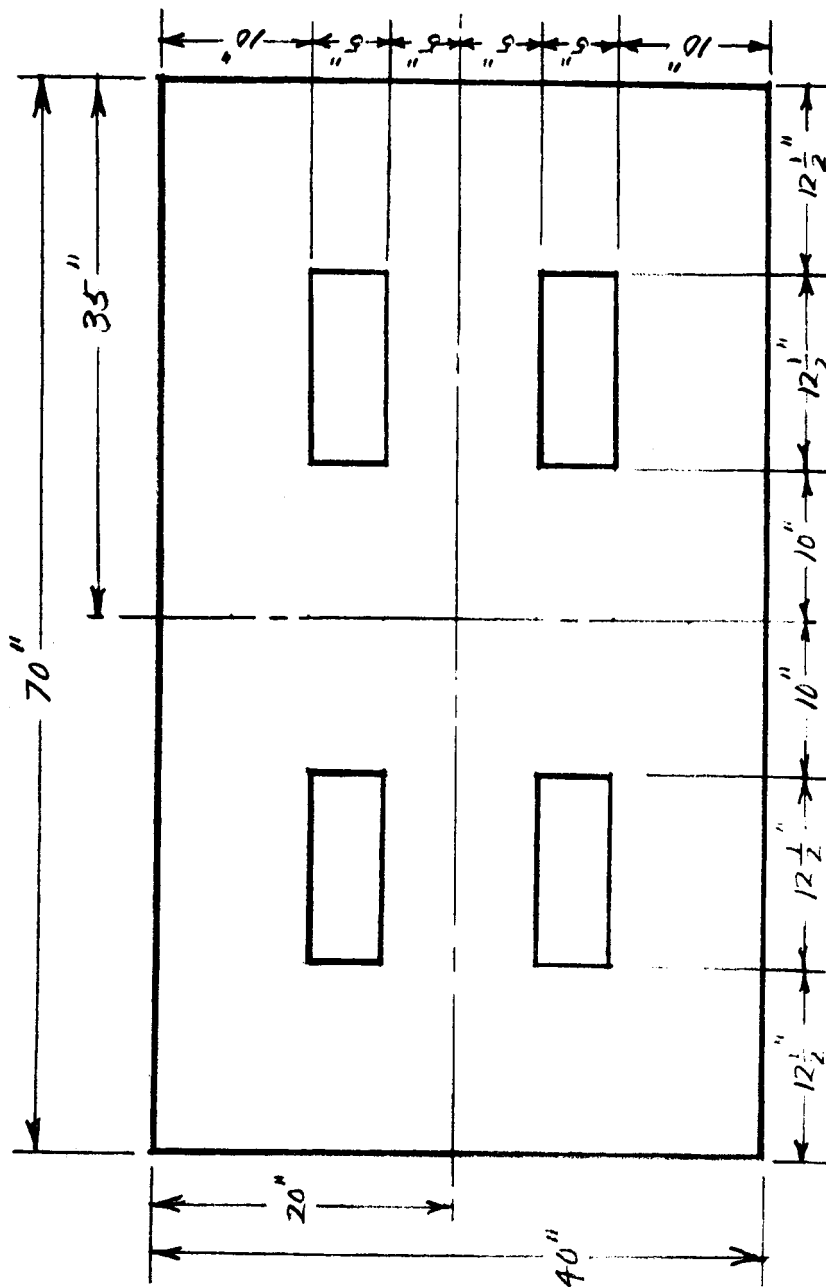
<u>Run Number</u>	<u>Clearance Distribution</u>	<u>Velocity</u>
7701	Uniform clearance all over	0
7702	Tilted about $X = 1/2$, ($H_{1,j} = 0.5$), ($H_{KK,j} = 1.5$)	0
7703	Tilted about $X = 1/2$ ($H_{1,j} = 0.5$), ($H_{KK,j} = 1.5$)	$\Lambda = 1.0$

Copies of the input data sheets for these three runs are shown in Appendix IV.

For convenience, let the dimensionless clearance at the center of the pad be

$$H_c = H \left(\frac{K+2}{2}, \frac{M+2}{2} \right) \quad [73]$$

For all three runs, $H_c = 1.0$



DIMENSIONS OF PAD FOR
SAMPLE PROBLEM

Fig. 6 - DIMENSIONS OF PAD FOR SAMPLE PROBLEM

The dimensionless computer input and output data are summarized below.

Dimensionless Factors	Run Number		
	7701	7702	7703
W	0.0933	0.1187	0.1308
q_1	1.0	1.0	1.0
H_c	1.0	1.0	1.0
ξ	0.5000	0.3708	0.3694
η	0.2857	0.2857	0.2857
α_1	0.30184	0.60023	0.64679
α_2	0.30184	0.17013	0.18384
α_3	0.30184	0.17013	0.18384
α_4	0.30184	0.60023	0.64679
Λ	0	0	1.0

Dimensionless performance coefficients in terms of H_c may be evaluated using equations [54] through [72], yielding the results listed below:

Performance Coefficients	Run Number		
	7701	7702	7703
$\overline{LHQ}_i$	1.1196	1.4244	1.5696
$\overline{LHV}$	0	0	1.275
$\overline{HQ}_i \overline{V}$	0	0	2.0
$\overline{LQ}_i \overline{V}$	0	0	1.72
$\overline{LHQ}_i \overline{V}$	0	0	3.14
$\overline{PR}_j \overline{W}$	3.23	5.07 for 1 & 4 1.44 for 2 & 3	4.95 for 1 & 4 1.40 for 2 & 3
$\overline{PS}_j \overline{W}$	3.23	5.07 for 1 & 4 1.44 for 2 & 3	4.95 for 1 & 4 1.40 for 2 & 3
$\overline{B}_j \overline{1}$	1.0	1.0	1.0
$\overline{MXW}$	0	0.1292	0.1306
$\overline{MYW}$	0	0	0
$\overline{MW}$	0	0.1292	0.1306
$\overline{MANG}$	0	0	0
$\overline{MXHQ}_i$	0	15.48	15.32
$\overline{MYHQ}_i$	0	0	0
$\overline{MHQ}_i$	0	15.48	15.32

Problem 1: - Determine the recess and supply pressure required for a load $w = 1.5 \times 10^6$ pounds, and the given pad length of $L = 70''$.

The equations to be used are,

$$\frac{(p_{rj} - p_a)L^2}{w} = \overline{PR_j W}$$

$$\frac{(p_{sj} - p_a)L^2}{w} = PS_j Wl$$

For the given pad length of $L = 70''$.

$$(p_{rj} - p_a) = (\overline{PR_j W}) \frac{1.5 \times 10^6}{4900} = 306(\overline{PR_j W})$$

Since $\overline{PR_j W} = \overline{PS_j Wl}$,

$$(p_{sj} - p_a) = (p_{rj} - p_a) = 306(\overline{PR_j W})$$

Using the computed values of $\overline{PR_j W}$, The values of recess pressure and supply pressure (pump discharge) in psig are,

Recess No.	Run Number		
	7701	7702	7703
1	988	1550	1515
2	988	441	428
3	988	441	428
4	988	1550	1515

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Problem 2: - Determine the required flow to each recess for a film thickness at the center of the pad of $h_c = 10 \times 10^{-3}$ in, at a load $w = 1.5 \times 10^6$ pounds.

To evaluate the flow, we use the performance coefficient relating load, film thickness and flow.

$$\overline{LHQ}_i = \frac{w(h_c)^3}{L^2 q_{ri} \mu}$$

$$q_{ri} = \frac{w(h_c)^3}{(\overline{LHQ}_i) L^2 \mu}$$

Assuming an SAE 30 oil at an operating temperature of 100°F, $\mu = 15 \times 10^{-6}$ lb-sec/in². Since the same flow is supplied to each recess,

$$q_{ri} = q_r = \frac{1.5 \times 10^6 (10 \times 10^{-3})^3}{(\overline{LHQ}_i) (70)^2 (15 \times 10^{-6})}$$

$$q_r = \frac{20.4}{(\overline{LHQ}_i)}$$

Using the computed values of $\overline{LHQ}_i$ for the three runs gives,

Run No.	$\overline{LHQ}_i$	q_r , (in ³ /sec)	q_r , (GPM)
7701	1.1196	18.23	4.74
7702	1.4244	14.33	3.73
7703	1.5696	13.00	3.38

Problem 3: - What will be the film thickness at the center of the pad if the flow for all recesses in all three cases is $11.53 \text{ in}^3/\text{sec}$ (3 GPM) for a load of $w = 1.5 \times 10^6$ lbs with $\mu = 15 \times 10^{-6} \text{ lb-sec/in}^2$.

Case 7701

$$\frac{w(h_c)^3}{L^2_{q_{ri}}\mu} = (\overline{LHQ}_i) = 1.1196$$

$$h_c = \left[\frac{1.1196 (4900)(11.53)(15 \times 10^{-6})}{1.5 \times 10^6} \right]^{1/3}$$

$$h_c = 0.0086 \text{ in.}$$

Case 7702

$$h_c = (h_c \text{ for } 7701) \left[\frac{\overline{LHQ}_i \text{ for } 7702}{\overline{LHQ}_i \text{ for } 7701} \right]^{1/3} = 0.0086 \left(\frac{1.4244}{1.1196} \right)^{1/3}$$

$$h_c = 0.0093 \text{ in.}$$

Case 7703

$$h_c = (h_c \text{ for } 7701) \left[\frac{\overline{LHQ}_i \text{ for } 7703}{\overline{LHQ}_i \text{ for } 7701} \right]^{1/3} = 0.0086 \left(\frac{1.5696}{1.1196} \right)^{1/3}$$

$$h_c = 0.0096 \text{ in.}$$

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Problem 4: - What velocity of relative motion will yield a film thickness at the center of 0.010 inch for a 13.0 in³/sec flow and a load of 1.5×10^6 pounds for Run No. 7703.

Using the relationship

$$\frac{HQ_i V}{q_{ri}} = \frac{UL(h_c)}{q_{ri}} = 2.0$$

$$U = \frac{2.0(13.0)}{(70)(10 \times 10^{-3})}$$

$$U = 37.2 \text{ in./sec.}$$

Problem 5: - What is the pad righting moment for all three cases when the load is 1.5×10^6 lbs.

To find the pad righting moment,

$$\frac{M}{wL} = (\overline{MW})$$

$$\therefore M = (\overline{MW})wL = (\overline{MW})(1.5 \times 10^6)(70)$$

For the three runs

Run No.	$\overline{MW}$	M(in - lb)
7701	0	0
7702	.1292	13.6×10^6
7703	.1306	13.7×10^6

CLOSURE

In the interim between when the above described computer program was first successfully compiled and the writing of this report, a large number of problems have been run. The operating experience compiled has indicated that the program can readily handle a large variety of hydrostatic bearing design and analysis problems. To date, the computer program results have shown good correlation with the results obtained from the electric analog field plotter technique¹ (uniform clearance, zero velocity). It should be mentioned here that in two similar, previously developed hydrostatic bearing computer programs (which allowed the solution of bearing geometries capable of being solved analytically) the correlation between computer program results and known analytical solutions was extremely good.

An experimental program currently underway at The Franklin Institute (being conducted for the Jet Propulsion Laboratory, Contract No. 950-735) is directed toward establishing the correlation between computer program results and those obtainable experimentally (zero velocity, non-uniform film clearance).

In the course of working with the above described computer program, a number of possible additions, modifications and refinements aimed at making the program more efficient and useful have occurred to Jet Propulsion Laboratory and Franklin Institute personnel. They are enumerated below for the record.

1. Input:- The format of the required input information should be changed in order to make key punching and checking of the same much more convenient.
2. Internal Changes:
 - a. The initial value of gamma should be reduced to 1.0 from 1.1.

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- b. Assign a new FORTRAN name to the ratio of pad y-direction length to x-direction length. Change from "AL" to "YOX". The name AL is confusing since AL (I) is also used as a superscripted variable.
- c. Evaluate the following quantities for subsequent appearance as output.

$$HC = H @ \frac{KK + 1}{2}, \frac{MM + 1}{2}$$

$$ALHCQ(I) = 12(W)(HC)^3/[QQ(I)]$$

$$ALHCV = (\Lambda)/[6(W)(HC)^2]$$

$$HCQV(I) = 2(\Lambda)(HC)/[QQ(I)]$$

$$PRW(I) = [AL(I)]/(W)$$

$$PSW1(I) = [AL(I)]/(W)$$

$$PSW2(I) = \{[QQ(I)]/[FF(I)] + [AL(I)]\}/(W)$$

$$PSW3(I) = (PF)/(W)$$

$$BETA1(I) = [PRW(I)]/[PSW1(I)]$$

$$BETA2(I) = [PRW(I)]/[PSW2(I)]$$

$$BETA3(I) = [PRW(I)]/[PSW3(I)]$$

$$AMXW = (0.50 - CCSI)$$

$$AMYW = [0.50(YOX) - EETA]$$

$$AMW = \{(AMXW)^2 + (AMYW)^2\}^{\frac{1}{2}}$$

$$AMANG = \tan^{-1} \left\{ \frac{(AMYW)}{(AMXW)} \right\}$$

- d. Two recommendations are suggested for reducing the computer time required to obtain the component solutions within subroutine REYN. The first is to initially assign active sill point pressure values other than the currently used value of zero. This would, however, require considerable study before changing. A second possibility is to have

the program recognize beforehand when identical component solutions for the individual recesses will be obtained. For example a symmetrical distribution of clearance in both the x and y-directions yields identical component solutions for recess combinations 1, 2, 3 and 4 and also for 5 and 6. Tilting of such a symmetrical film distribution about only X1 produces identical component solutions for recess combinations 1 and 4, 2 and 3, and 5 and 6. Tilting of a symmetrical film distribution about only Y1 produces identical solutions for recess combinations 1 and 3, and 2 and 4.

3. Output: -

- a. The numerical values of the following quantities should also be written for inclusion in the output:
 YOX, X1, Y1, TX, TY, LITER, TRUNC, PLAM, HC,
 ALHCQ(I), HCQV(I), ALHCV, PRW(I), PSW1(I), PSW2(I),
 PSW3(I), BETA1(I), BETA2(I) BETA3(I), AMXW, AMYW,
 AMW, and AMANG.

Appropriate titles should also be used for these quantities (See equations [54] through [69]).

- b. Eliminate writing out all "progress indicators". Write out only the last two or three values of PROG(ITER). The run number (NRUN) should also be written out in this portion of the output.

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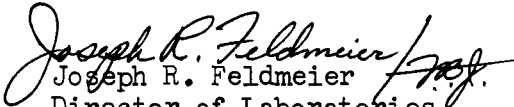
In the judgement of the personnel of The Franklin Institute,
all of the goals set forth in our work proposal have been achieved
during the course of this program.


J. G. Hinkle
Project Engineer


W. W. Shugarts, Jr., Mgr.
Friction & Lubrication Laboratory

Approved by:


N. R. Droulard
Technical Director


Joseph R. Feldmeier
Director of Laboratories

REFERENCES

1. Loeb, A. M., "The Determination of the Characteristics of Hydrostatic Bearings through the use of the Electric Analog Field Plotter," ASLE Transactions, Vol. 1, No. 1, April, 1958.
2. Hinkle, J. G. and V. Castelli, "A Computer Solution for Hydrostatic Bearings with Variable Film Thickness," Franklin Institute Final Report No. F-B2015, January 11, 1963, Prepared for Jet Propulsion Laboratory, Contract No. 950 448.
3. Shaw, M. C. and E. F. Macks, "Analysis and Lubrication of Bearings," McGraw Hill, 1949, N. Y., N. Y.
4. Hetenji, M., "Beams on Elastic Foundation," The University of Michigan Press.

NOMENCLATURE

AL	= ratio of pad y-length/pad x-length
A_n	= dimensionless clearance coefficients
E	= Youngs Modulus (psi)
H	= dimensionless film thickness = h/c
K	= the number of grid cells in the x-direction
L	= length of pad in the x-direction, inches
M	= the number of grid cells in the y-direction
M_x	= moment about $x = \frac{1}{2}$ axis (in-lbs)
M_y	= moment about $y = \frac{AL}{2}$ axis (in-lbs)
N	= total number of recesses
P_{ij}	= dimensionless pressure at grid point i,j
Q_{ij}	= dimensionless flow out of i^{th} recess corresponding to j^{th} component solution
$QQQ^{(k)}$	= dimensionless flow out of k^{th} pair of opposite recesses
T_x	= dimensionless tilt components in x-direction
T_y	= dimensionless tilt components in y-direction
U	= relative velocity of bearing members, in./sec.
W	= dimensionless load
W_j	= dimensionless load of the j^{th} component solution
X	= dimensionless x-coordinate = (x/L)
Y	= dimensionless y-coordinate = (y/L)
c	= a characteristic film thickness, (in.)
d	= capillary diameter (in.)
f_i	= capillary flow factor for i^{th} recess
h	= film thickness, (in.)
i	= grid index
j	= grid index
k	= modulus of the foundation (lb/in^2) as defined in reference 4
l	= capillary length (in.)
p	= pressure, (psia)

NOMENCLATURE (Cont'd)

- p_a = ambient pressure, (psia)
 $p^{(f)}$ = dimensionless supply manifold pressure
 p_r = recess pressure, (psia)
 p_{ref} = reference pressure, (psia)
 p_s = supply manifold pressure, (psia)
 q_i = dimensionless flow out of the i^{th} recess
 q_{ri} = volume flow out of i^{th} recess (in^3/sec)
 q_{rc} = volume flow out of i^{th} recess corresponding to j^{th} component solution (in^3/sec)
 q_{2r} = total volume flow out of one pair of opposite recesses (in^3/sec)
 s = $X - X_o$
 t = $Y - Y_o$
 w = total load, (lbs)
 w_j = load carried by j^{th} recess, (lbs)
 x = cartesian coordinate, (in.)
 x_j = distance in x-direction to center of pressure of component solution (in.)
 y = cartesian coordinate, (in.)
 y_j = distance in y-direction to center of pressure of component solution (in.)
 Λ = velocity factor = $\frac{6\mu UL}{c^2(p_{ref} - p_a)}$
 $\Lambda' = \lambda L$
 $\alpha = \left[\frac{\Delta X}{\Delta Y} \right]^2$
 α_j = dimensionless recess pressure
 β = slope of tilted pad in h, x, y space
 γ = relaxation factor governing pressure distribution growth
 $\Delta X = 1/K$
 $\Delta Y = \frac{AL}{M}$

NOMENCLATURE (Cont'd)

η = dimensionless y coordinate of center of pressure

η_j = dimensionless y coordinate of center of pressure for i^{th} component solution

$$\lambda = \sqrt{\frac{4k}{4El}}$$

μ = absolute viscosity coefficient (reyns)

ξ = dimensionless x coordinate of center of pressure

ξ_j = dimensionless x coordinate center of pressure for i^{th} component solution

APPENDIX I

PROGRAM BLOCK DIAGRAM

MAIN SUBPROGRAM

Fortran Instruction Listings
IBM 7094 Compilation Records
Flow Chart

FLOW SUBPROGRAM

Fortran Instruction Listings
IBM 7094 Compilation Records
Flow Chart

REYN SUBPROGRAM

Fortran Instruction Listings
IBM 7094 Compilation Records
Flow Chart

FORMH SUBPROGRAM

Fortran Instruction Listings
IBM 7094 Compilation Records
Flow Chart

TILTH SUBPROGRAM

Fortran Instruction Listings
IBM 7094 Compilation Records
Flow Chart

FUNCTION DETER SUBPROGRAM

Fortran Instruction Listings
IBM 7094 Compilation Records
Flow Chart

I-2

MAIN PROGRAM FOR HYDROSTATIC BEARINGS WITH VARIABLE FILM THICKNES

STORAGE NOT USED BY PROGRAM

DEC OCT
112 00160
DEC OCT
17379 41743

STORAGE LOCATIONS FOR VARIABLES APPEARING IN COMMON STATEMENTS

DEC OCT	DEC OCT	DEC OCT	DEC OCT	DEC OCT
A 17404 41774	CS1 23456 55640	DX 32559 77457	DY 32558 77456	ETA 23449 55631
H 32557 77455	HX 29542 71546	HY 26527 63637	INDEX1 17381 41745	INDEX2 17380 41744
IPREV 23442 55622	K1 23512 55730	K2 23511 55727	K3 23510 55726	KEY 23441 55621
KK 32561 77461	LIMJ 23464 55650	LITER 20426 47712	M1 23509 55725	M2 23508 55724
MM 32560 77460	NIGNAL 17410 42002	PLAM 17409 42001	P 20425 47711	Q 23506 55722
TRUNC 23507 55723	TX 17406 41776	TY 17405 41775	W 23463 55647	X1 17408 42000
Y1 17407 41777				

STORAGE LOCATIONS FOR VARIABLES NOT APPEARING IN COMMON, DIMENSION, OR EQUIVALENCE STATEMENT

DEC OCT
NIMJ 111 00157
NSWICH 110 00156
DEC OCT
DEC OCT

SYMBOLS AND LOCATIONS FOR SOURCE PROGRAM FORMAT STATEMENTS

EFN LOC
811 1 00154
EFN LOC
812 2 00152
EFN LOC

LOCATIONS FOR OTHER SYMBOLS NOT APPEARING IN SOURCE PROGRAM

DEC OCT
21 94 00136
E12 38 00046
DEC OCT
41 32767 77777
E1E 77 00115
DEC OCT
61 99 00143
E1F 80 00120
DEC OCT
C1G0 109 00155
E1G 85 00125
DEC OCT
D1401 16 00020
E1H 90 00132

LOCATIONS OF NAMES IN TRANSFER VECTOR

DEC OCT
EXIT 4 00004
(FPT) 0 00000
DEC OCT
FLOW 5 00005
(RTN) 3 00003
FORMH 6 00006
(RWT) 1 00001
DEC OCT
FORMH 7 00007
(TSH) 2 00002
DEC OCT
TILTH 8 00010

ENTRY POINTS TO SUBROUTINES NOT OUTPUT FROM LIBRARY

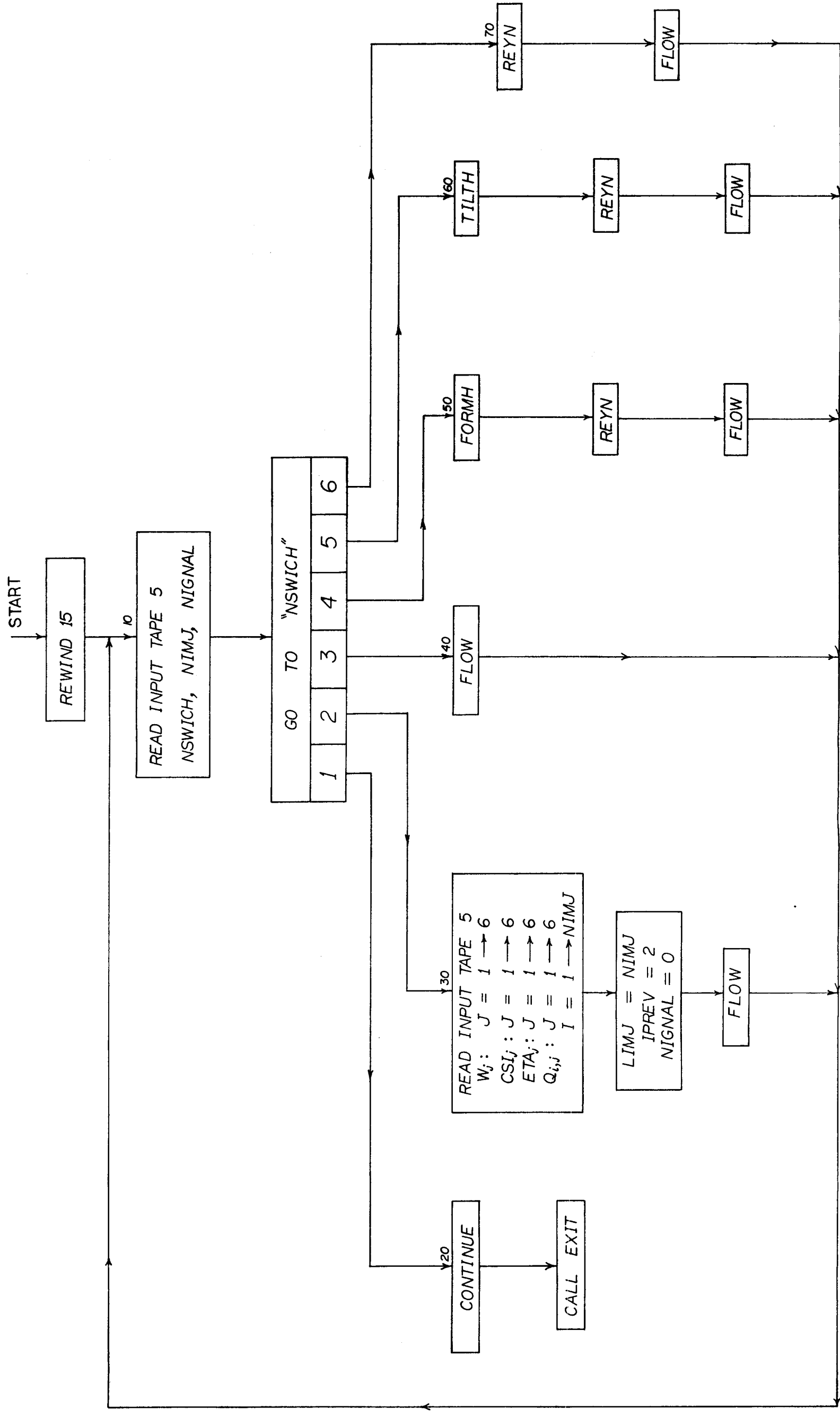
EXIT FLOW FORMH REYN TILTH (FPT) (RWT) (TSH)

EXTERNAL FORMULA NUMBERS WITH CORRESPONDING INTERNAL FORMULA NUMBERS AND OCTAL LOCATIONS

EFN	IFN	LOC	EFN	IFN	LOC	EFN	IFN	LOC
10	7	00021	20	10	00047	30	12	00050
60	39	00126	70	43	00133	40	33	00116
						50	35	00121

JET PROPULSION LABORATORY'S VARIABLE FILM HYDROSTATIC BEARING PROGRAM -- BLOCK DIAGRAM

COMMON : KK, MM, DX, DY, H, HX, HY, K1, K2, K3, M1, M2, TRUNC, Q, LIMJ, W, CSI, ETA, IPREV, KEY, LITER, P, NIGAL, PLAM, XI, Y1, TX, TY, INDEX1, INDEX2



```

SUBROUTINE FLOW
  SUBROUTINE FLOW
    DIMENSION H(67,45), HX(67,45), HY(67,45), Q(6,7), W(7), CSI(7),
    1 ETA(7), AL(7), AAI(6,7), F1(6,6), D1(6), QQ(6), PQ(6),
    1 P(67,45), PPP(67,45), KEY(67,45), MK(10), T(6,6), TT(6), Q(6),
    1 A(23), B(23), LQ(6), NC(23)
    COMMON KK, MM, DX, DY, HX, HY, K1, K2, K3, M1, M2, TRUNC, Q, LIMJ, W, CSI, ETA,
    1 IPREV, KEY, LITER, P, NIGAL, PLAN, X1, Y1, TX, TY, A, INDEX1, INDEX2
    READ INPUT TAPE 5, 1, NKUN, NCASE, IQUT
    1 FORMAT(I5,2I2)
    IF (NIGAL - 1) 111, 1112, 111
    111 LLLL = LIMJ
    GO TO 1115
    1112 LLLL = LIMJ + 1
    AL(LLLL) = 1.0
    1115 GO TO (10, 120, 330), NCASE
    10 READ INPUT TAPE 5, 2, (QQ(III), III=1, LIMJ)
    20 FORMAT (6E12.4)
    DO 80 LK = 1, LIMJ
    DO 40 I = 1, LIMJ
    DO 40 J = 1, LIMJ
    IF (J - LK) 30, 20, 30
    20 IF (NIGAL - 1) 26, 27, 26
    26 AAI(I,J) = QQ(I)
    GO TO 40
    27 AAI(J) = QQ(I) - Q(I, LLLL)
    GO TO 40
    30 AAI(J) = Q(I, J)
    40 CONTINUE
    D(LK) = DETER(AA, LIMJ)
    80 CONTINUE
    DQ = DETER(Q, LIMJ)
    DO 115 LK = 1, LIMJ
    115 AL(LK) = D(LK) / DQ
    GO TO 380
    120 LIMJ2 = LIMJ / 2
    READ INPUT TAPE 5, 2, (QQ(III), III=1, LIMJ2)
    READ INPUT TAPE 5, 2, (FF(III), III=1, LIMJ)
    DO 130 I = 1, LIMJ, 2
    DO 130 J = 1, LIMJ
    TT(I,J) = Q(I,J) + Q(I+1,J)
    130 CONTINUE
    IF (NIGAL - 1) 132, 135, 132
    132 DO 133 I = 1, LIMJ, 2
    II = (I+1)/2
    133 TT(I) = QQ(II)
    GO TO 139
    135 DO 138 I = 1, LIMJ, 2
    II = (I+1)/2
    TT(II) = QQ(II) - Q(II, LIMJ+1) - Q(II+1, LIMJ+1)
    138 CONTINUE
    139 DO 200 I = 2, LIMJ, 2
    IF (NIGAL - 1) 142, 145, 142
    142 TT(II) = 0.0
    GO TO 146
    145 TT(II) = Q(II, LIMJ+1)/FF(II) - Q(II-1, LIMJ+1)/FF(II-1)
    146 DO 200 J = 1, LIMJ

```

SUBROUTINE FLOW

```

140 IF (I-1-J) 140, 150, 140
140 DEL = 0.0
GO TO 160
150 DEL = 1.0
160 IF (I-J) 170, 180, 170
170 DDEL = 0.0
GO TO 190
180 DDEL = 1.0
190 T(I,J) = (Q(I-1,J)+DEL*FF(I-1))/FF(I-1)-(Q(I,J)+DDEL*FF(I))/FF(I)
200 CONTINUE
205 DO 270 LK = 1, LIMJ
DO 230 I = 1, LIMJ
DO 230 J = 1, LIMJ
IF (J-LK) 220, 210, 220
210 AA(I,J) = TT(I)
GO TO 230
220 AA(I,J) = T(I,J)
230 CONTINUE
DILK) = DETER(AA,LIMJ)
270 CONTINUE
DT = DETER(T,LIMJ)
DO 305 LK = 1, LIMJ
305 AL(LK) = O(LK) / DT
DO 310 I = 1, LIMJ
QQ(I) = 0.0
DO 310 J = 1, LLLL
310 QQ(I) = QQ(I) + AL(J) * Q(I,J)
IF (NCASE - 2) 315, 315, 380
315 DO 320 I = 1, LIMJ2
320 PQ(I)=QQ(2*I-1)/FF(2*I-1) +AL(2*I-1)
GO TO 380
330 READ INPUT TAPE 5, 5, PF
5 FORMAT (F10.4)
READ INPUT TAPE 5, 2, (FF(III), III=1,LIMJ)
DO 370 I = 1, LIMJ
IF ( NIGAL - 1) 332, 333, 332
332 TT(I) = PF * FF(I)
GO TO 335
333 TT(I) = PF * FF(I) - Q(I,LIMJ+1)
335 DO 370 J = 1, LIMJ
IF (I-J) 340, 350, 340
340 DDEL = 0.0
GO TO 360
350 DDEL = 1.0
360 T(I,J) = Q(I,J) + DDEL * FF(I)
370 CONTINUE
GO TO 205
380 WW = 0.0
DO 390 I = 1, LLLL
CCSI = CCSI + AL(I) * W(I)
390 WW = WW + AL(I) * W(I)
CCSI = 0.0
EETA = 0.0
DO 400 I = 1, LLLL
CCSI = CCSI + AL(I) * CSI(I)+W(I)/WW
400 EETA = EETA + AL(I) * ETA(I) * W(I) / WW
IF ( NIGAL - 1) 402, 403, 402

```

SUBROUTINE FLOW

```

402 WRITE OUTPUT TAPE 6,6,NRUN,LIMJ
GO TO 410
403 WRITE OUTPUT TAPE 6,32, NRUN, LIMJ
410 GO TO (420, 430, 440),NCASE
420 WRITE OUTPUT TAPE 6,7
7 FORMAT (31X 58HFEEDING = POSITIVE DISPLACEMENT PUMPS FEEDING EACH
  RECESS. /)
GO TO 450
430 WRITE OUTPUT TAPE 6,9
8 FORMAT(14X 92HFEEDING = POSITIVE DISPLACEMENT PUMPS FEEDING PAIRS
  10F RECESSES WITH CAPILLARY COMPENSATION. )
GO TO 450
440 WRITE OUTPUT TAPE 6,9,PF
9 FORMAT (5X 36HFEEDING = COMMON CONSTANT PRESSURE (F7.3,67H ATM.) R
  10F RESERVOIR FEEDING ALL RECESSES WITH CAPILLARY COMPENSATION. /)
450 IF (NCASE - 2) 452, 451, 452
451 WRITE OUTPUT TAPE 6,15,(QQ(I), I=1,LIMJ2)
15 FORMAT ( 11H PUMP FLOWS 3E18.7 )
452 GO TO (460, 480), IPREV
460 K = KK - 1
M = MM - 1
IF ( NIGNAL - 1) 454, 453, 454
453 WRITE OUTPUT TAPE 6,28, PLAM
28 FORMAT ( 10H LAMBOA = F8.4)
29 FORMAT ( 17H GRID POINTS, K = 13,2X 4H M = 13, 5X 5H K1 = 13, 2X
  1 5H K2 = 13, 2X 5H K3 = 13, 3X 5H M1 = 13, 2X 5H M2 = 13 )
454 WRITE OUTPUT TAPE 6,29, K, M, K1, K2, K3, M1, M2
IF ( INDEX1 - 1) 455, 459, 455
455 K1 = 0
DO 458 L = 1, 23
IF ( ABSFIA(L)) - 0.1E-06) 458, 456, 456
456 K1 = K1 + 1
8 (K1) = A(L)
NC(K1) = L
458 CONTINUE
WRITE OUTPUT TAPE 6,4441,(NC(I),B(I), I = 1,K1)
441 FORMAT (24H CLEARANCE COEFFICIENTS /5(4H ,AA 12,3H)= E14.8))
459 IF (INDEX2 - 1) 4460, 461, 4460
4460 IF (NSWICH - 5) 462, 461, 462
461 WRITE OUTPUT TAPE 6,31, X1, Y1, TX, TY
31 FORMAT ( 19H TILTED PAD, X1 = E15.8, 2X 6H Y1 = E15.8, 2X 6H TX =
  1 E15.8, 2X 6H TY = E15.8 )
462 CONTINUE
GO TO 480
C START A NEW PAGE OF OUTPUT
4620 IF (NIGNAL - 1) 463, 464, 463
463 WRITE OUTPUT TAPE 6, 6, NRUN, LIMJ
GO TO 465
464 WRITE OUTPUT TAPE 6,32, NRUN, LIMJ
32 FORMAT (12H1RUN NUMBER 15, 26X 25H HYBRID BEARING PAD WITH 11,
  1 10H RECESSES )
465 GO TO ( 466,467,468),NCASE
466 WRITE OUTPUT TAPE 6,7
GO TO 469
467 WRITE OUTPUT TAPE 6,8
GO TO 469

```

SUBROUTINE FLOW

```

468 WRITE OUTPUT TAPE 6,9, PF
469 WRITE OUTPUT TAPE 6,3, (KEY(I,1), I = 1,KK)
DO 470 J = 2, MM
470 WRITE OUTPUT TAPE 6,4,(KEY(I,J), I=1,KK)
GO TO 549
3 FORMAT(20H PAD CONFIGURATION. 6711 )
4 FORMAT ( 20X 6711 )
480 WRITE OUTPUT TAPE 6,4801
4801 FORMAT ( // 54X 10H OUTPUT )
IF (LIMJ - 4) 490, 490, 500
490 IF (NIGAL - 1) 494, 496, 494
494 WRITE OUTPUT TAPE 6,12,(Q(I,1),I=1,4),(Q(I,1),J=1,4),(W(I,1),I=1,4) ,
1(Q(2,J),J=1,4),(CSI(I,1),I=1,4),(Q(3,J),J=1,4),(ETA(I,1),I=1,4),(Q(4,J
1),J=1,4)
GO TO 510
12 FORMAT ( 8H QQ(I)= 4F9.2,10X10H** Q(I,J)= 4F9.4/8H W(I)= 4F9.4,10
1X2H**8X 4F9.4/8H CSI(I)= 4F9.4,10X 2H** 8X 4F9.4/8H ETA(I)= 4F9.4,
110X 2H** 8X 4F9.4 )
496 WRITE OUTPUT TAPE 6,112,(Q(I,1),I=1,4),(W(I,1),I=1,5),(CSI(I,1),I=1,5),
1(ETA(I,1),I=1,5), 1(Q(I,1),J=1,5),I=1,4)
GO TO 510
112 FORMAT ( 8H QQ(I)= 4F11.4/8H W(I)= 5F9.4/ 8H CSI(I)= 5F9.4/ 8H E
1TA(I)= 5F9.4// 10X 5H J=1, 4X 5H J=2, 4X 5H J=3, 4X 5H J=4, 4X
1 5H J=5, / 8H Q(1,J)= 5F9.4/ 8H Q(2,J)= 5F9.4/ 8H Q(3,J)= 5F9.4/
1 8H Q(4,J)= 5F9.4 )
500 IF (NIGAL - 1) 504, 506, 504
504 WRITE OUTPUT TAPE 6,113,(Q(I,1),I=1,6),(Q(I,1),J=1,6),(W(I,1),I=1,6)
1(Q(2,J),J=1,6),(CSI(I,1),I=1,6),(Q(3,J),J=1,6),(ETA(I,1),I=1,6),(Q(4,
1J),J=1,6),(Q(5,J),J=1,6),(Q(6,J),J=1,6)
GO TO 510
13 FORMAT( 8H QQ(I)= 6F8.2, 2X 10H** Q(I,J)= 6F8.4/8H W(I)= 6F8.4,2X
1 2H** 8X 6F8.4/8H CSI(I)= 6F8.4, 2X 2H** 8X 6F8.4/8H ETA(I)= 6F8.4
1,2X 2H** 8X 6F8.4/58X 2H** 8X 6F8.4/58X 2H** 8X 6F8.4)
506 WRITE OUTPUT TAPE 6,113,(Q(I,1),I=1,6),(W(I,1),I=1,7),(CSI(I,1),I=1,7),
1 (ETA(I,1),I=1,7),(Q(I,1),J=1,7),I=1,6)
113 FORMAT ( 8H QQ(I)= 6F11.4/ 8H W(I)= 7F9.4/ 8H CSI(I)= 7F9.4/ 8H E
1TA(I)= 7F9.4// 10X 5H J=1, 4X 5H J=2, 4X 5H J=3, 4X 5H J=4, 4X
1 5H J=5, 4X 5H J=6, 4X 5H J=7, / 8H Q(1,J)= 7F9.4 / 8H Q(2,J)= 7F
19.4/ 8H Q(3,J)= 7F9.4/ 8H Q(4,J)= 7F9.4/ 8H Q(5,J)= 7F9.4/
1 8H Q(6,J)= 7F9.4 )
510 IF (INCASE - 2) 530, 520, 520
520 WRITE OUTPUT TAPE 6,14,(FF(I), I=1,LIMJ )
14 FORMAT(24H CAPILLARY FACTORS F(I)= 6E16.7 )
530 QQQ = 0.0
DO 540 I=1,LIMJ
540 QQQ = QQQ + QQ(I)
6 FORMAT (12H1RUN NUMBER 15,23X 29HYDROSTATIC BEARING PAD WITH 11,
1 10H RECESSES. )
WRITE OUTPUT TAPE 6,16,MW,CCSI,EETA,QQQ
16 FORMAT (28H FINAL RESULTS = TOTAL LOAD= F8.4, 6H CSI=F7.4 , 6H E
1TA= F7.4, 13H TOTAL FLOW= E15.7 )
DO 543 L = 1, LIMJ
543 LOO(L) = L
WRITE OUTPUT TAPE 6,5432,(LOO(L),AL(L), L = 1,LIMJ)
5432 FORMAT (17H RECESS PRESSURES / 2X 6(6H, AL( 11, 4H) = F8.5))
GO TO (4620,549), IPREV

```

SUBROUTINE FLOW

```

549 IOUT = IOUT + 1
GO TO ( 550, 555, 555, 695), IOUT
550 IPREV=1
WRITE OUTPUT TAPE 6, 8888
8888 FORMAT (1H1)
RETURN
17 FORMAT (8E15.8 )
555 GO TO(560,556), IPREV
556 WRITE OUTPUT TAPE 6, 5555
5555 FORMAT(52HOPRESSURE AND CLEARANCE DISTRIBUTIONS NOT AVAILABLE. )
GO TO 550
560 DO 570 I=1, KK
DO 570 J=1, MM
570 PPPP(I, J) = 0.0
REWIND 15
DO 580 II = 1, LIMJ
READ TAPE 15, P
DO 580 I=1, KK
DO 580 J = 1, MM
580 PPPP(I, J) = PPPP(I, J) + AL(II) * P( I, J)
REWIND 15
KK1 = 0
590 IF (KK - KK1 - 10) 600, 600, 610
600 KK2 = KK
GO TO 620
610 KK2 = KK1 + 10
620 DO 630 L = 1, 10
630 MK(L) = KK1 + L
IF (KK-KK2) 640, 640, 650
640 KK3 = KK2 - KK1
WRITE OUTPUT TAPE 6, 18, NRUN, (MK(L), L = 1, KK3)
GO TO 660
650 WRITE OUTPUT TAPE 6, 18, NRUN, (MK(L), L = 1, 10 )
660 KK11 = KK1 + 1
DO 670 J = 1, MM
670 WRITE OUTPUT TAPE 6, 19, J, (PPPP(I, J), I=KK11, KK2)
19 FORMAT (3H J= 13, 4H, 10F11.4)
IF ( KK - KK2) 690, 690, 680
680 KK1 = KK1 + 10
GO TO 590
18 FORMAT ( 1H1 49X 22H PRESSURE DISTRIBUTION//5H RUN 15, 5X 2H1= 13
1, 918H
I= 13//)
690 CONTINUE
IF (IOUT - 2) 550, 695, 550
695 KK1 = 0
700 IF (KK-KK1 - 10) 710, 710, 720
710 KK2 = KK
GO TO 730
720 KK2 = KK1 + 10
730 DO 740 L = 1, 10
740 MK(L) = KK1 + L
IF (KK - KK2) 750, 750, 760
750 KK3 = KK2 - KK1
WRITE OUTPUT TAPE 6, 21, NRUN, (MK(L), L = 1, KK3)
21 FORMAT ( 1H1 49X 22HCLEARANCE DISTRIBUTION //5H RUN 15, 6H I=
113, 9( 8H I= 13)//)

```

SUBROUTINE FLOW

```

GO TO 770
760 WRITE OUTPUT TAPE 6, 21, NRUN, (MK(I), L=1, 10)
770 KK1 = KK1 + 1
    DO 780 J = 1, MM
780 WRITE OUTPUT TAPE 6, 22, J, (H(I, J), I = KK1, KK2)
    22 FORMAT (3H J= 13, 4H, 10F11.7 )
    IF (KK - KK2) 550, 550, 790
790 KK1 = KK1 + 10
    GO TO 700
END(1, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0)
    
```

SUBROUTINE FLOW

STORAGE NOT USED BY PROGRAM

DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT		
5109	11765	17379	41743								
STORAGE LOCATIONS FOR VARIABLES APPEARING IN COMMON STATEMENTS											
DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT		
A	17404	41774	CS1	23456	55640	DX	32559	77457	ETA	23449	55631
H	32557	77455	HX	29542	71546	HY	26527	63637	INDEX2	17380	41744
IPREV	23442	55622	K1	23512	55730	K2	23511	55727	KEY	23441	55621
KK	32561	77461	LIMJ	23464	55650	LITER	20426	47712	M2	23508	55724
MM	32560	77460	NIGNAL	17410	42002	PLAM	17409	42001	P	20425	47711
TRUNC	23507	55723	TX	17406	41776	TY	17405	41775	W	23463	55647
Y1	17407	41777							X1	17408	42000

STORAGE LOCATIONS FOR VARIABLES APPEARING IN DIMENSION AND EQUIVALENCE STATEMENTS

DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT		
AA	5003	11613	AL	5108	11764	B	5055	11677	D	5101	11755
F	4961	11541	L00	5032	11650	MK	5077	11725	NC	5026	11642
PQ	5083	11733	QQQ	5095	11747	QQ	5061	11705	T	1910	03566

STORAGE LOCATIONS FOR VARIABLES NOT APPEARING IN COMMON, DIMENSION, OR EQUIVALENCE STATEMENT

DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT		
CCSI	1874	03522	DOEL	1873	03521	DEL	1872	03520	DT	1870	03516
EETA	1869	03515	I1	1868	03514	IOUT	1867	03513	I	1866	03512
KI	1864	03510	KK1	1863	03507	KK1	1862	03506	KK2	1861	03505
K	1859	03503	LIMJ2	1858	03502	LK	1857	03501	LLLL	1856	03500
M	1854	03476	NCASE	1853	03475	NRUN	1852	03474	NSWICH	1851	03473
QQQ	1849	03471	NW	1848	03470						

SYMBOLS AND LOCATIONS FOR SOURCE PROGRAM FORMAT STATEMENTS

EFN	LOC	EFN	LOC	EFN	LOC	EFN	LOC	EFN	LOC
811	1 03447	812	2 03445	813	3 03254	814	4 03246	815	5 03443
816	6 03014	817	7 03441	818	8 03425	819	9 03403	81C	12 03235
81D	13 03140	81E	14 03023	81F	15 03356	81G	16 02777	81H	17 02744
81I	18 02723	81J	19 02730	81L	21 02705	81M	22 02667	81S	28 03351
81T	29 03345	81V	31 03310	81W	32 03271	81X	112 03204	81Y	113 03102
814AP	4441 03321	814M1	4801 03242	81590	5432 02757	8150J	5555 02742	818LO	8888 02745

LOCATIONS FOR OTHER SYMBOLS NOT APPEARING IN SOURCE PROGRAM

DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT		
1)	1832	03450	2)	1440	02640	3)	1450	02652	C160	1836	03454
C1G1	1837	03455	C1G3	1838	03456	C1G4	1839	03457	C1G8	1841	03461
C1GA	1842	03462	C1G8	1843	03463	C1100	1844	03464	C1102	1846	03466
C1200	1847	03467	D1108	88	00130	D1114	276	00424	D1127	484	00744
D1130	628	01164	D1238	716	01314	D1270	1324	02454	D1314	275	00423
D1327	483	00743	D1370	1323	02453	D137E	1328	02460	D1420	580	01104
D143T	841	01511	D1714	274	00422	D1727	482	00742	E129	492	00754

F-B2099

SUBROUTINE FLOW

LOCATIONS OF NAMES IN TRANSFER VECTOR

DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT
DETER	2 00002	(FIL)	4 00004	(RLR)	8 00010	(RTN)	1 00001
(SLI)	7 00007	(STH)	3 00003	(TSB)	6 00006	(TSH)	0 00000

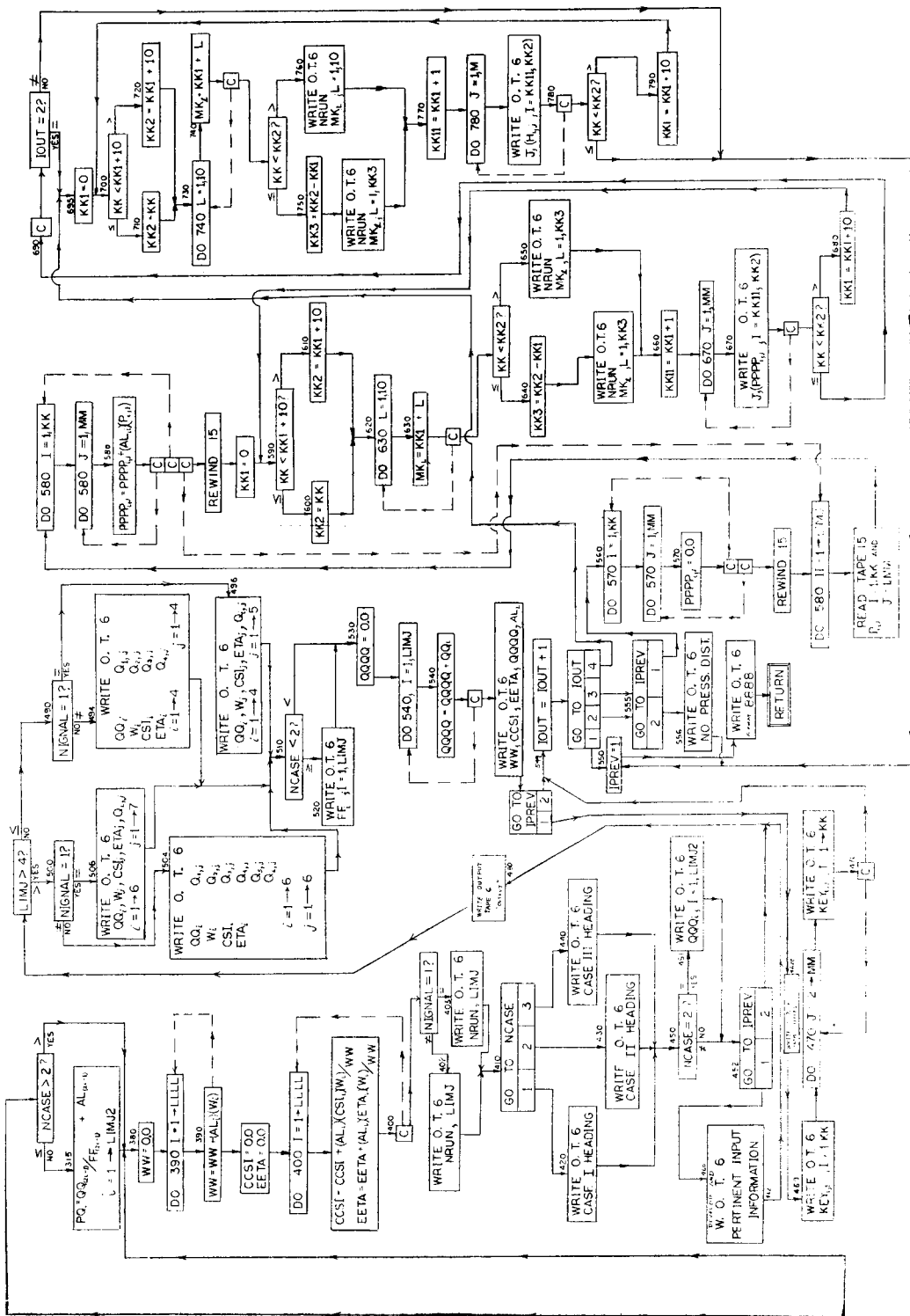
ENTRY POINTS TO SUBROUTINES NOT OUTPUT FROM LIBRARY

DEFER	(FIL)	(RLR)	(RTN)	(RMT)	(SLI)	(STH)	(TSB)	(TSH)
-------	-------	-------	-------	-------	-------	-------	-------	-------

EXTERNAL FORMULA NUMBERS WITH CORRESPONDING INTERNAL FORMULA NUMBERS AND OCTAL LOCATIONS

EFN	IFN	LOC	EFN	IFN	LOC	EFN	IFN	LOC	EFN	IFN	LOC
111	38 00045	1112	40 00052	1115	42 00061	10	43 00064	20	52 00143	80	61 00204
26	53 00146	27	55 00152	30	57 00157	40	58 00163	80	61 00204	80	61 00204
115	65 00217	120	67 00225	130	81 00277	132	83 00307	133	85 00325	133	85 00325
135	87 00333	138	90 00370	139	91 00374	142	93 00430	145	95 00433	145	95 00433
146	96 00443	140	98 00454	150	100 00457	160	101 00461	170	102 00464	170	102 00464
180	104 00467	190	105 00471	200	106 00505	205	107 00522	210	111 00554	210	111 00554
220	113 00557	230	114 00561	270	117 00577	305	121 00612	310	125 00636	310	125 00636
315	127 00656	320	128 00662	330	130 00673	332	139 00750	333	141 00755	333	141 00755
335	142 00761	340	144 00771	350	146 00774	360	147 00776	370	148 01002	370	148 01002
380	150 01020	390	152 01025	400	157 01050	402	159 01063	403	162 01074	403	162 01074
410	164 01105	420	165 01110	430	167 01117	440	169 01126	450	171 01140	450	171 01140
451	172 01145	452	177 01165	460	178 01167	453	181 01202	454	183 01214	454	183 01214
455	186 01245	456	189 01262	458	192 01273	459	198 01315	460	199 01320	460	199 01320
461	200 01325	462	202 01341	4620	204 01342	463	205 01345	464	208 01362	464	208 01362
465	210 01376	466	211 01401	467	213 01410	468	215 01417	469	217 01431	469	217 01431
470	223 01467	480	229 01512	490	231 01524	494	232 01527	496	259 01610	496	259 01610
500	279 01655	504	280 01660	506	313 01753	510	332 02017	520	333 02024	520	333 02024
530	338 02043	540	340 02050	543	344 02102	549	351 02133	550	353 02144	550	353 02144
555	357 02161	556	358 02164	560	360 02173	570	362 02206	580	369 02247	580	369 02247
590	372 02270	600	373 02275	610	375 02300	620	376 02303	630	377 02306	630	377 02306
640	379 02320	650	387 02345	660	393 02364	670	395 02410	680	402 02442	680	402 02442
690	404 02446	695	406 02455	700	407 02462	710	408 02467	720	410 02472	720	410 02472
730	411 02475	740	412 02500	750	414 02512	760	422 02537	770	428 02556	770	428 02556
780	430 02602	790	437 02634								

DIMENSION: H,H,Y,Q,A,L,A, F,D,Q,Q,Q,FF,PQ,W,CS,E,T,A, P,PPPP, KEY,MK,T, TT,Q,Q,HX,AA,B,QQNC
COMMON: KK,MN,DY,D,H, HX, ,HY,K1,K2,K3,M1,M2,TRUNG,CQ, LIN,W,CS,E,T,A,PREV,KEY, LITER, P, SIGNAL, PLAN, X1, Y1, TX, TY, A, INDEX1, INDEX2



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SUBROUTINE REYN
  SUBROUTINE REYN
  DIMENSION HI(67,45), HX(67,45), HY(67,45), QI(6,7), W(7), CSI(7),
  1 ETAI(7), A(23), PPI(67), P(67,45), PROG(1000), KR(6), KRR(6), MR(6),
  1 MRR(6), KEY(67,45)
  COMMON KK,MM,DX,DY,H,HX,HY,K1,K2,K3,M1,M2,TRUNC,Q,LIMJ,M,CSI,ETA,
  1 IPREV,KEY,LITER,P,NIGNAL,PLAM,XI,YI,IX,ITY,A,INDEX1,INDEX2
  READ INPUT TAPE 5,1, LITER, TRUNC, PLAM
  1 FORMAT (I5, 2E16.8)
  ALPHA = (DX * DX) / (DY * DY)
  FACTOR = 1.0 / (2.0 * (1.0 + ALPHA))
  K = KK - 1
  M = MM - 1
  NREL = K + M - K1 - K2 - M1 - M2 - 2
  FK = K
  FM = M
  NACT = (K-1)*(M-1)-(4*(K2+1)+ 2*(K3+1)) *(M2+1)
  PACT = NACT
  IF(K3) 10, 10, 20
  10 LIMJ = 4
  NACT = (K-1)*(M-1) - 4*(K2+1)*(M2+1)
  PACT = NACT
  GO TO 30
  20 LIMJ = 6
  30 KR(1) = 2
  MR(1) = 2
  MR(3) = 2
  KRR(3) = K
  MRR(4) = M
  KR(4) = 2
  KRR(2) = K
  MRR(2) = M
  IF (LIMJ-4) 50,50,40
  40 MR(5) = 2
  MRR(6) = M
  50 MR(4) = M/2+1
  MRR(1) = M/2+1
  MR(6) = M/2+1
  MRR(5) = M/2+1
  MR(2) = M/2+1
  MRR(3) = M/2+1
  REWIND 15
  IF (LIMJ -4) 60,60,70
  60 KRR(1) = K/2+1
  KR(3) = K/2 + 1
  KRR(4) = K/2+1
  KR(2) = K/2+1
  GO TO 71
  70 KKRC = (K-K3+2*K1+2*K2+4)/4
  KRR(1) = KKRC
  KR(4) = KKRC
  KR(6) = KKRC
  KR(5) = KKRC
  KRR(5) = K - KKRC + 2
  KRR(6) = K - KKRC + 2
  KR(2) = K - KKRC + 2
  KR(3) = K - KKRC + 2

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SUBROUTINE REYN

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71 IF (NIGNAL - 1) 72, 74, 72
72 LLLL = LIMJ
  GO TO 75
74 LLLL = LIMJ + 1
75 DO 460 JJJ = 1, LLLL
77 GAMMA = 1.1
78 DO 140 I = 1, KK
  DO 140 J = 1, MM
    IF (JJJ-LIMJ-1) 79, 80, 80
79 KEYIJ = KEY(I,J) + 1
  GO TO ( 80, 90, 80), KEYIJ
80 P(I,J) = 0.0
  GO TO 140
90 IF (I-KR(JJJ)) 80, 100, 100
100 IF (I-KRR(JJJ)) 110, 110, 80
110 IF (J - MR(JJJ)) 80, 120, 120
120 IF (J-MRR(JJJ)) 130, 130, 80
130 P(I,J) = 1.0
140 CONTINUE
  PGAMMA = 1.0 - GAMMA
145 DO 220 ITER = 1, LITER
  PROG(ITER) = 0.0
  DO 146 I = 2, K
    IF (JJJ - LIMJ - 1) 147, 1147, 1147
147 DO 170 J = 2, M
  DO 170 I = 2, K
    KEYIJ = KEY(I,J) + 1
  GO TO (150, 150, 160), KEYIJ
150 PP = P(I,J)
  GO TO 165
160 PPRIME=FACTOR*(P(I+1,J)+P(I-1,J)+P(I+1,J)-P(I-1,J))*HX(I,J)+ALPHA
  1*(P(I,J+1)+P(I,J-1)+P(I,J+1) - P(I,J-1))*HY(I,J))
  PP = GAMMA * PPRIME + PGAMMA * P(I,J)
  PROG(ITER) = PROG(ITER) + PP
165 P(I,J-1) = PPP(I)
  PPP(I) = PP
170 CONTINUE
  GO TO 179
1147 DO 1170 J = 2, M
  DO 1170 I = 2, K
    KEYIJ = KEY(I,J) + 1
  GO TO (1150, 1150, 1160), KEYIJ
1150 PP = P(I,J)
  GO TO 1165
1160 PPRIME=FACTOR*(P(I+1,J)+P(I-1,J)+P(I+1,J)-P(I-1,J))*PLAM(1.5)*DX/
  1*(H(I,J)+H(I,J))*HX(I,J) + ALPHA*(P(I,J+1)+P(I,J-1)+P(I,J+1) -
  1*(I,J-1))*HY(I,J))
  PP = GAMMA * PPRIME + PGAMMA * P(I,J)
  PROG(ITER) = PROG(ITER) + PP
1165 P(I,J-1) = PPP(I)
  PPP(I) = PP
1170 CONTINUE
1179 DO 180 I = 2, K
180 P(I,M) = PPP(I)
  IF ( GAMMA - 0.16) 181, 181, 185

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SUBROUTINE REYN

```

181 WRITE OUTPUT TAPE 6,3333, ITER
3333 FORMAT (25H FORCED OUT AT ITERATION I4, 21H, SOLUTION NOT VALID )
GO TO 235
185 IF (ITER - 6) 220, 220, 190
190 IF (PROG(ITER) - 2.0 * PROG(ITER-1) * PROG(ITER-2)) 210, 210, 200
200 GAMMA = GAMMA * 0.8
WRITE OUTPUT TAPE 6, 1111, JJJ, GAMMA, ITER
1111 FORMAT (7H RECESS I3, 19H, GAMMA CHANGED TO F10.4, 11H, ITERATION
1, I5)
GO TO 78
210 IF (ITER - NREL) 220, 220, 215
215 IF ((PROG(ITER) - PROG(ITER-1)) * PACT / (GAMMA * PROG(ITER))) - TRUNC) 230,
1, 230, 220
220 CONTINUE
ITER = LITER
230 WRITE OUTPUT TAPE 6, 2222, JJJ, ITER, (PROG(LKK), LKK = 1, ITER)
2222 FORMAT (7H RECESS I3, 25H, CONVERGED AT ITERATION I5 / 20H PROGRES
15 INDICATORS / (10F11.6))
235 AAM=0.0
AACSI = 0.0
AAETA = 00.0
J1 = 2
J2 = M
J3 = 2
240 DO 310 J = J1, J2, J3
AW = 0.0
ACSI = 0.0
AETA = 0.0
FJ = J-1
I1 = 2
I2 = K
I3 = 2
250 DO 260 I = I1, I2, I3
FI = I-1
AW = AW + P(I, J)
ACSI = ACSI + FI * P(I, J)
260 AETA = AETA + FJ * P(I, J)
IF (I3 - K) 270, 300, 300
270 AW = 2.0 * AW
ACSI = 2.0 * ACSI
AETA = 2.0 * AETA
IF (I1-2) 280, 280, 290
280 I1 = 3
290 GO TO 250
I1 = 1
I2 = KK
I3 = K
GO TO 250
300 AAM = AAM + AW
AACSI = AACSI + ACSI
310 AAETA = AAETA + AETA
IF (J3 - M) 320, 350, 350
320 AAM = AAM * 2.0
AACSI = AACSI * 2.0
AAETA = AAETA * 2.0
IF (J1-2) 330, 330, 340

```

```

330 J1 = 3
    GO TO 240
340 J1 = 1
    J2 = MM
    J3 = M
    GO TO 240
350 W(JJJ) = AAW * DX * DY / 9.0
    CS(IJJJ) = AACSI * DX * DY / (9.0*W(JJJ))
    ETA(JJJ) = AAETA * DX * DY / (9.0*W(JJJ))
360 DO 440 I1I = 1, LIMJ
    QQ = 0.0
    J = MR(III)
    I1=KR(III)
    I2=KRR(III)
370 DO 380 I = I1, I2
    QQ=QQ+H(I,J)*H(I,J)*H(I,J)*(P(I,J)+1) - P(I,J-1))
    QQ=QQ+0.5*(H(I1,J)*H(I1,J)*H(I1,J)*(P(I1,J+1)-P(I1,J-1))+
    H(I2,J)*H(I2,J)*(P(I2,J+1)-P(I2,J-1)))
    IF (J - MR(III)) 400, 390, 400
390 QQ = -QQ
    J = MR(III)
    GO TO 370
400 TT = 0.0
    I1 = KR(III)
    J1=MR(III)
    J2=MRR(III)
410 IF (JJJ-LIMJ-1) 420, 1420, 1420
420 DO 421 J = J1, J2
421 TT = TT - H(I,J)*H(I,J)*H(I,J)*(P(I+1,J) - P(I-1,J))
    TT = TT + 0.5*(H(I,J1)*H(I,J1)*H(I,J1)*(P(I+1,J1)-P(I-1,J1))+
    H(I,J2)*H(I,J2)*H(I,J2)*(P(I+1,J2) - P(I-1,J2)))
    GO TO 425
420 DO 1421 J = J1, J2
421 TT = TT - H(I,J)*H(I,J)*H(I,J)*(P(I+1,J)-P(I-1,J)) - 2.0*PLAM*DX
    TT * H(I,J)
    TT = TT + 0.5*(H(I,J1)*H(I,J1)*H(I,J1)*(P(I+1,J1) - P(I-1,J1)) +
    H(I,J2)*H(I,J2)*H(I,J2)*(P(I+1,J2)-P(I-1,J2)) + 2.0*DX*PLAM*
    H(I,J2) + H(I,J1)))
425 IF (I - KR(III)) 440, 430, 440
430 TT = -TT
    I = KRR(III)
    GO TO 410
440 Q(II,I,JJJ) = QQ*DX*0.5/DY+TT*DY*0.5/DX
450 WRITE TAPE 15,P
      2 FORMAT (8E15.8)
460 CONTINUE
    END FILE 15
    REWIND 15
    RETURN
    END(1.0,0.0,0.0,0.0,0.0,1.0,0.0,0.0,0)

```

SUBROUTINE REYN

STORAGE NOT USED BY PROGRAM

DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT
2418	04562	17379	41743						
DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT
A 17404	41774	CSI 23456	55640	DX 32559	77457	DY 32558	77456	ETA 23449	55631
H 32557	77455	HX 29542	71546	HY 26527	63637	INDEX1	17381	INDEX2	17380
IPREV 23442	55622	K1 23512	55730	K2 23511	55727	K3 23510	55726	KEY 23441	55621
KK 32561	77461	LIMJ 23464	55650	LITER 20426	47712	M1 23509	55725	M2 23508	55724
MM 32560	77460	NIGNAL 17410	42002	PLAM 17409	42001	P 20425	47711	Q 23506	55722
TRUNC 23507	55723	TX 17406	41776	TY 17405	41775	W 23463	55647	X1 17408	42000
Y1 17407	41777								

STORAGE LOCATIONS FOR VARIABLES APPEARING IN DIMENSION AND EQUIVALENCE STATEMENTS

DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT
KRR 1344	02500	KR 1350	02506	MRR 1332	02464	MR 1338	02472
PROG 2350	04456					PP 2417	04561

STORAGE LOCATIONS FOR VARIABLES NOT APPEARING IN COMMON, DIMENSION, OR EQUIVALENCE STATEMENT

DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT
AACSI 1326	02456	AAETA 1325	02455	AAW 1324	02454	ACSI 1323	02453
ALPHA 1321	02451	AM 1320	02450	FACTOR 1319	02447	FI 1318	02446
FK 1316	02444	FM 1315	02443	GAMMA 1314	02442	I1 1313	02441
I3 1311	02437	I 1310	02436	ITER 1309	02435	J1 1308	02434
J3 1306	02432	JJJ 1305	02431	J 1304	02430	KEYIJ 1303	02427
K 1301	02425	LLLL 1300	02424	M 1299	02423	NACT 1298	02422
PACT 1296	02420	PGAMMA 1295	02417	PPRIME 1294	02416	PP 1293	02415
IT 1291	02413					QQ 1292	02414
						AETA 1322	02452
						FJ 1317	02445
						I2 1312	02440
						J2 1307	02433
						KKRC 1302	02426
						NREL 1297	02421
						QQ 1292	02414

SYMBOLS AND LOCATIONS FOR SOURCE PROGRAM FORMAT STATEMENTS

EFN	LOC	EFN	LOC	EFN	LOC	EFN	LOC
811	1 02365	812	2 02316	8112N	1111 02350	8125E	2222 02335
						81385	3333 02362

LOCATIONS FOR OTHER SYMBOLS NOT APPEARING IN SOURCE PROGRAM

DEC	OCT	DEC	OCT	DEC	OCT	DEC	OCT
11 1270	02366	21 1205	02265	31 1214	02276	61 1223	02307
A1104 1166	02216	A1105 1179	02233	A1106 1192	02250	C1G1 1278	02376
C1G3 1280	02400	C1G6 1281	02401	C1100 1282	02402	C1103 1283	02403
C1105 1285	02405	C1106 1286	02406	C1107 1287	02407	C1204 1288	02410
C1206 1290	02412	D1115 689	01261	D1200 315	00473	D1212 469	00725
D121M 641	01201	D1210 648	01210	D140C 311	00467	D140H 347	00533
E1G 337	00521	E1M 373	00565	E111 435	00663	E113 477	00735
E118 556	01054	E123 775	01407	E110H 349	00535	E120H 349	00535
						A1103 1153	02201
						C1G2 1279	02377
						C1104 1284	02404
						C1205 1289	02411
						D121A 548	01044
						D140Q 395	00613
						E119 506	00772

LOCATIONS OF NAMES IN TRANSFER VECTOR

F-B2099

SUBROUTINE REYN

(LEFT)	DEC	OCT	(FIL)	DEC	OCT	(RTN)	DEC	OCT	(SLO)	DEC	OCT
(STB)	8 00010	5 00005	(STH)	4 00004	3 00003	(TSH)	1 00001	2 00002	7 00007	6 00006	
								(WLR)			

ENTRY POINTS TO SUBROUTINES NOT OUTPUT FROM LIBRARY

(LEFT)	(FIL)	(RTN)	(RWT)	(SLO)	(STB)	(STH)	(TSH)	(WLR)
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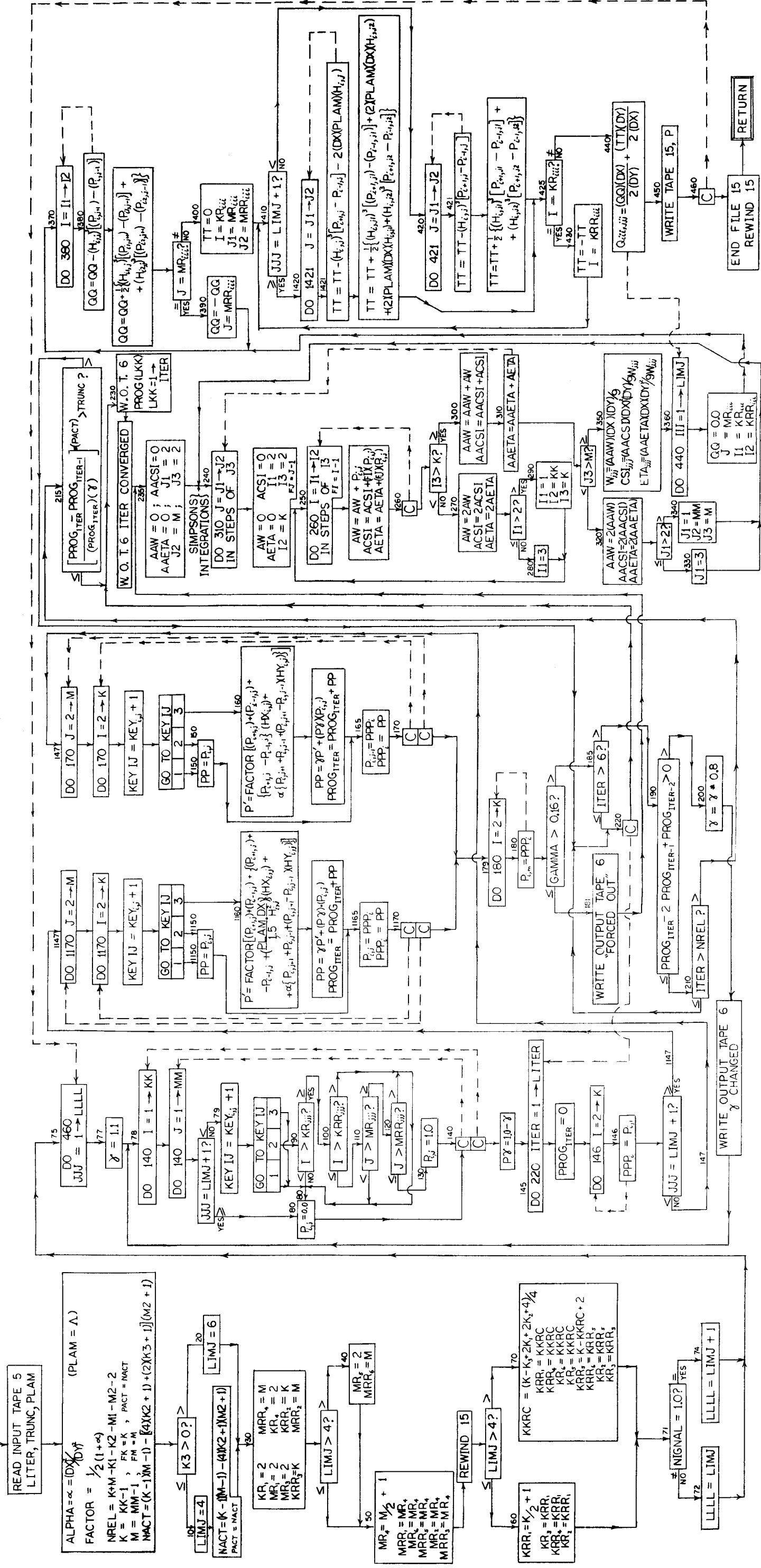
EXTERNAL FORMULA NUMBERS WITH CORRESPONDING INTERNAL FORMULA NUMBERS AND OCTAL LOCATIONS

EFN	IFN	LOC	EFN	IFN	LOC	EFN	IFN	LOC	EFN	IFN	LOC
10	22	00153	20	26	00212	30	27	00214	40	36	00241
60	46	00333	70	51	00374	71	60	00444	72	61	00447
75	64	00455	77	65	00470	78	66	00474	79	69	00523
90	73	00542	100	74	00550	110	75	00554	120	76	00561
140	78	00571	145	80	00605	146	83	00622	147	85	00634
160	91	00665	165	94	00726	170	96	00732	1147	98	00743
1160	104	00774	1165	107	01045	1170	109	01051	179	110	01061
181	113	01106	185	116	01121	190	117	01126	200	118	01137
215	123	01166	220	124	01202	230	126	01211	235	132	01234
250	146	01314	260	150	01353	270	152	01367	280	156	01404
300	162	01417	310	164	01425	320	166	01437	330	170	01454
350	176	01474	360	179	01526	370	184	01562	380	185	01576
400	191	01665	410	195	01707	420	196	01714	421	197	01730
1421	201	02013	425	203	02103	430	204	02111	440	207	02124
460	210	02156									

COMMON: KK, MM, DX, DY, H, HX, HY, KI, K2, K3, MI, M2, TRUNC, Q, LIMJ, W, CSI, ETA, IPREV, KEY, LITER, P, NIGNAL, PLAM, X1, Y1, TX, TY, A, INDEX1, INDEX2

DIMENSION: H, HX, HY, A, PPP, P, PROG, KR, KRR, MR, MRR, Q, W, CSI, ETA, KEY.

COMMON: KK, MM, DX, DY, H, HX, HY, KI, K2, K3, MI, M2, TRUNC, Q, LIMJ, W, CSI, ETA, IPREV, KEY, LITER, P, NIGNAL, PLAM, X1, Y1, TX, TY, A, INDEX1, INDEX2



SUBROUTINE FORMH

```

SUBROUTINE FORMH
  DIMENSION H(67,45), HX(67,45), HY(67,45), A(23), KEY(67,45),
  1 Q(6,7), W(7), CSI(7), ETA(7), PI(67,45)
  COMMON KK,MM,DX,DY,HX,HY,K1,K2,K3,M1,M2,TRUNC,O,LINJ,M,CSI,ETA,
  1 IPREV,KEY,LITER,P,NIGNAL,PLAN,X1,Y1,IX,TY,A,INDEX1,INDEX2
  1 FORMAT(9I3,E16.8)
  READ INPUT TAPE 5, 1,K,M,INDEX1,INDEX2,K1,K2,K3,M1,M2,AL
  KK = K + 1
  MM = M + 1
  FK = K
  FM = M
  DX = 1.0/FK
  DY = AL/FM
  FX = 0.5/DX
  FY = 0.5/DY
  DO 11 J = 2,M
    KEY(1,J) = 0
    KEY(KK,J) = 0
    DO 11 I = 2, K
      11 KEY(I,J) = 1
      DO 21 I = 1, KK
        KEY(1,I) = 0
        21 KEY(I,MM) = 0
        KK1 = K1 + K2 + 2
        KK2 = (K - K3)/2
        DO 31 J = 2, M
          DO 31 I = 2, K1
            11 = K + 2 - I
            KEY(1,J) = 2
            DO 41 I = KK1, KK2
              11 = K + 2 - I
              KEY(I,J) = 2
              41 KEY(11,J) = 2
              IF (K3) 42,42,51
              42 11 = K/2 + 1
              KEY(11,J) = 2
              51 CONTINUE
              MM2 = M - M1 - M2
              MM1 = M1 + M2 + 2
              DO 61 I = 2, K
                DO 61 J = 2, M1
                  JJ = M + 2 - J
                  KEY(I,J) = 2
                  61 KEY(1,JJ) = 2
                  DO 71 J = MM1, MM2
                    71 KEY(1,J) = 2
                    81 CONTINUE
                    IPREV = 1
                    2 FORMAT (6E11.8)
                    IF(INDEX1 - 1) 30, 20, 30
                    20 READ INPUT TAPE 5,2,((H(I,J), I=1,KK), J=1,MM)
                    DO 25 I = 2, K
                      DO 25 J = 2, M
                        HX(I,J) = (H(I+1,J)-H(I-1,J))*75/H(I,J)
                        25 HY(I,J) = (H(I,J+1)-H(I,J-1))*75/H(I,J)

```

SUBROUTINE FORMH

```

3 FORMAT (5E14.8)
GO TO 60
30 READ INPUT TAPE 5,3,(A(1), L = 1,23)
CON = EXPF(-0.5*A(21))*COSF(A(21)*0.5) * 2.0
DO 50 I = 1,KK
  FI = I
  X = (FI - 1.0) * DX
  S = (FI - 1.0) * DX - A(22)
  SS = S * S
  SSS = SS * S
  DO 50 J = 1, MM
    FJ = J
    T = (FJ - 1.0) * DØ - A(23)
    TT = T * T
    TTT = TT * T
    H(I,J) = A(1)+A(2)*S + A(3)*T+A(4)*SS+A(5)*TT+A(6)*S*T+A(7)*SSS+A(8)*
    TTT+A(9)*SS*T+A(10)*S*TT+A(11)*SQRTF(A(12)+A(13)*SS+A(14)*TT)+
    1 A(15)*COSF(A(16)*S)+A(17)*COSF(A(18)*T)+A(19)*COSF(A(16)*S)*COSF(
    1 A(18)*T)-A(20)*((EXPF(-A(21)*X)*COSF(A(21)*X)*EXPF(-A(21)*(1.0-X))*
    1 COSF(A(21)*(1.0-X))-CON)
    HX(I,J) = (A(2)+2.*A(4)*S+A(6)*T+3.*A(7)*SS+2.*A(9)*S*T+A(10)*TT-
    1 A(16)*SINF(A(16)*S)+A(15)+A(19)*COSF(A(18)*T))*1.5*DX/H(I,J)+A(
    120)*A(21)*((EXPF(-A(21)*X)*(COSF(A(21)*X)*SINF(A(21)*X))-EXPF(-A(21
    1)*(1.0-X))*(COSF(A(21)*(1.0-X))+SINF(A(21)*(1.0-X))*1.5*DX/H(I,
    1 J)
    HY(I,J) = (A(3)+2.*A(5)*T+A(6)*S+3.*A(8)*TT+A(9)*SS-A(18)*SINF(A(18)
    1)*T)+A(17)+A(19)*COSF(A(16)*S))*1.5*DY/H(I,J)
    SL = A(12)+A(13)*SS+A(14)*TT
    IF (SL) 50, 50, 40
  40 SLL = A(11)/SQRTF(SL)
    HX(I,J) = HX(I,J)+SLL*A(13)*S*1.5*DX/H(I,J)
    HY(I,J) = HY(I,J) + SLL*A(14)*T*1.5*DY/H(I,J)
50 CONTINUE
60 IF (INDEX2 - 1) 80, 70, 80
70 CALL TILTH
80 RETURN
END(1.0,0.0,0.0,0.0,0.0,1.0,0.0,0.0,0.0)

```

SUBROUTINE FORMH

STORAGE NOT USED BY PROGRAM

DEC OCT
941 01655

DEC OCT
17379 41743

STORAGE LOCATIONS FOR VARIABLES APPEARING IN COMMON STATEMENTS

DEC OCT	DEC OCT	DEC OCT	DEC OCT	DEC OCT
A 17404 41774	CSI 23456 55640	DX 32559 77457	DY 32558 77456	ETA 23449 55631
H 32557 77455	HX 29542 71546	HY 26527 63637	INDEX1 17381 41745	INDEX2 17380 41744
IPREV 23442 55622	K1 23512 55730	K2 23511 55727	K3 23510 55726	KEY 23441 55621
KK 32561 77461	LIMJ 23464 55650	LITER 20426 47712	M1 23509 55725	M2 23508 55724
MM 32560 77460	NIGNAL 17410 42002	PLAN 17409 42001	P 20425 47711	Q 23506 55722
TRUNC 23507 55723	TX 17406 41776	TY 17405 41775	W 23463 55647	X1 17408 42000
Y1 17407 41777				

STORAGE LOCATIONS FOR VARIABLES NOT APPEARING IN COMMON, DIMENSION, OR EQUIVALENCE STATEMENT

DEC OCT	DEC OCT	DEC OCT	DEC OCT	DEC OCT
AL 940 01654	CON 939 01653	FI 938 01652	FJ 937 01651	FK 936 01650
FM 935 01647	FX 934 01646	FY 933 01645	II 932 01644	I 931 01643
JJ 930 01642	J 929 01641	KK1 928 01640	KK2 927 01637	K 926 01636
MM1 925 01635	MM2 924 01634	M 923 01633	SLL 922 01632	SL 921 01631
S 920 01630	SS 919 01627	SSS 918 01626	T 917 01625	TT 916 01624
TTT 915 01623	X 914 01622			

SYMBOLS AND LOCATIONS FOR SOURCE PROGRAM FORMAT STATEMENTS

EFN LOC	EFN LOC	EFN LOC	EFN LOC
811 1 01552	812 2 01550	813 3 01546	

LOCATIONS FOR OTHER SYMBOLS NOT APPEARING IN SOURCE PROGRAM

DEC OCT	DEC OCT	DEC OCT	DEC OCT	DEC OCT
1) 875 01553	2) 850 01522	3) 857 01531	6) 863 01537	A1105 824 01470
A1106 837 01505	C102 903 01607	C1100 904 01610	C1101 905 01611	C1102 906 01612
C1105 907 01613	C1106 908 01614	C1200 909 01615	C1201 910 01616	C1203 911 01617
C1206 912 01620	C1208 913 01621	D120A 194 00302	D130A 193 00301	D1401 318 00476
D1411 436 00664	E7C 215 00327			

LOCATIONS OF NAMES IN TRANSFER VECTOR

DEC OCT	DEC OCT	DEC OCT	DEC OCT
COS 2 00002	EXP 3 00003	SIN 5 00005	SQRT 4 00004
(RTN) 1 00001	(TSH) 0 00000		

ENTRY POINTS TO SUBROUTINES NOT OUTPUT FROM LIBRARY

GUS	EXP	SIN	SQRT	TILTH	(RTN)	(TSH)
-----	-----	-----	------	-------	-------	-------

EXTERNAL FORMULA NUMBERS WITH CORRESPONDING INTERNAL FORMULA NUMBERS AND OCTAL LOCATIONS

DEC OCT	DEC OCT
TILTH 6 00006	

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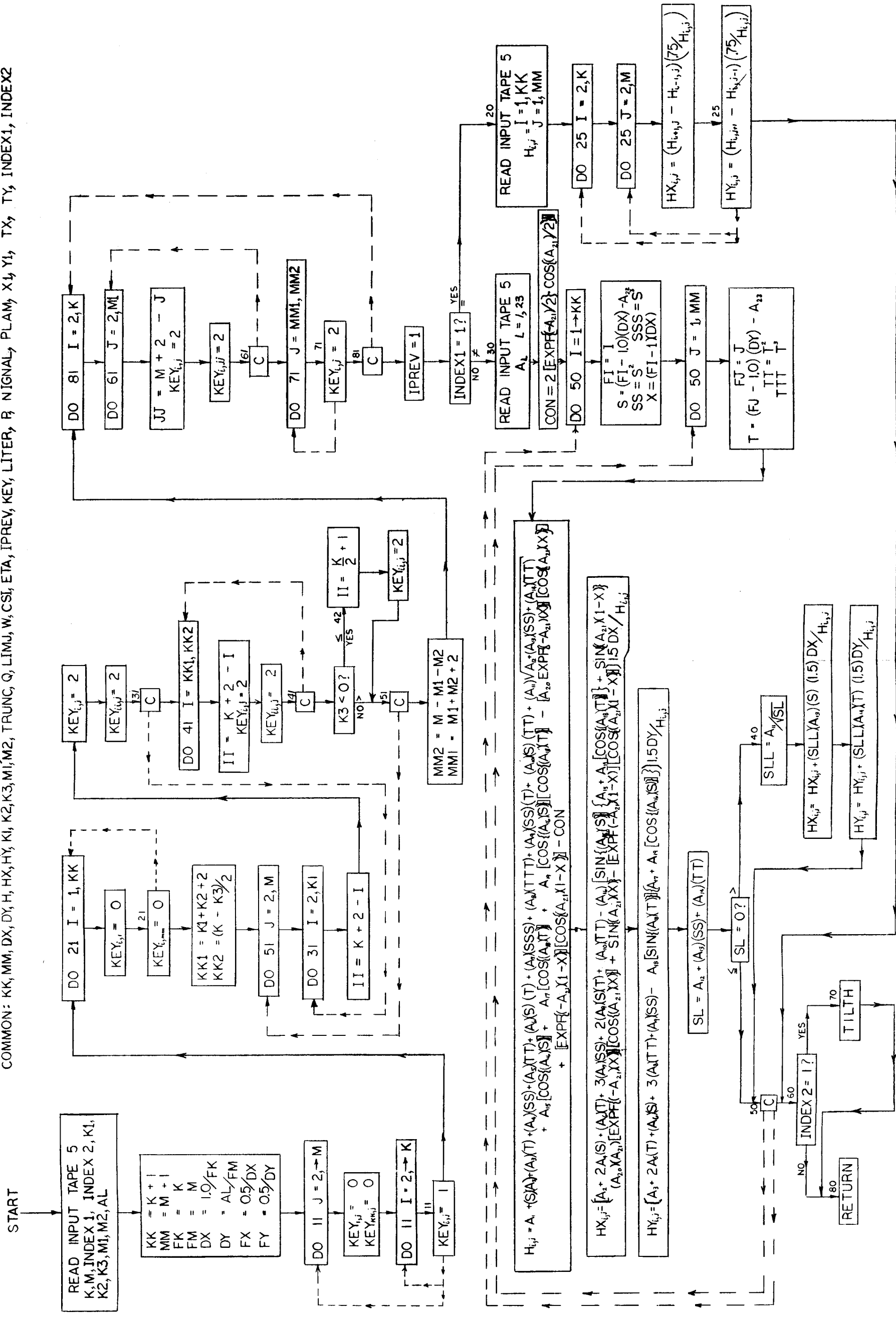
F-B2099

SUBROUTINE FORMH

EFN	IFN	LOC	EFN	IFN	LOC	EFN	IFN	LOC	EFN	IFN	LOC
11	22	00141	21	25	00172	31	32	00263	41	36	00315
51	40	00346	61	47	00467	71	49	00477	81	50	00504
25	63	00606	30	65	00621	40	87	01407	50	90	01443
70	92	01463	80	93	01464						

FORMH

DIMENSION: H, HX, HY, A, KEY, Q, W, CSI, ETA, P
COMMON: KK, MM, DX, DY, H, HX, HY, KI, K2, K3, MI, M2, TRUNC, Q, LIMJ, W, CSI, ETA, IPREV, KEY, LITER, B, NIGAL, PLAM, X4, YI, TX, TY, INDEX1, INDEX2



```

SUBROUTINE TILTH
  SUBROUTINE FILTH
    DIMENSION H(67,45), HX(67,45), HY(67,45), KEY(67,45), Q(6,7), W(7)
    1, CSI(7), ETA(7), A(23), P(67,45)
    COMMON KK,MM,DX,DY,H,HX,HY,K1,K2,K3,M1,M2,TRUNC,Q,LIMJ,W,CSI,ETA,
    1 IPREV,KEY,LITER,P,NIGNAL,PLAM,X1,Y1,TX,TY,A,INDEX1,INDEX2
    READ INPUT TAPE 5, 1, X1, Y1, TX, TY
    1 FORMAT (4E15.8 )
    DO 90 I = 1, KK
      FI = I
      X = (FI - 1.0)* DX - X1
      DO 90 J = 1, MM
        FJ = J
        H(I,J) = H(I,J)*TX*TY*((FJ-1.)*DY-Y1)
        HX(I,J) = HX(I,J) + TX * 1.5 * DX / H(I,J)
        HY(I,J) = HY(I,J) + TY * 1.5 * DY / H(I,J)
      90 CONTINUE
    RETURN
  END(1,0,0,0,0,0,0,0,1,0,0,0,0,0,0)

```

SUBROUTINE IILTH

STORAGE NOT USED BY PROGRAM

DEC OCT
115 00163

DEC OCT
17379 41743

STORAGE LOCATIONS FOR VARIABLES APPEARING IN COMMON STATEMENTS

DEC OCT
A 17404 41774
H 32557 77455
IPREV 23442 55622
KK 32561 77461
MM 32560 77460
TRUNC 23507 55723
YI 17407 41777

DEC OCT
CSI 23456 55640
HX 29542 71546
KI 23512 55730
LIMJ 23464 55650
NIGNAL 17410 42002
TX 17406 41776

DEC OCT
DX 32559 77457
HY 26527 63637
K2 23511 55727
LITER 20426 47712
PLAM 17409 42001
TY 17405 41775

DEC OCT
DY 32558 77456
INDEX1 17381 41745
K3 23510 55726
M1 23509 55725
P 20425 47711
W 23463 55647

DEC OCT
EIA 23449 55631
INDEX2 17380 41744
KEY 23441 55621
M2 23508 55724
Q 23506 55722
X1 17408 42000

STORAGE LOCATIONS FOR VARIABLES NOT APPEARING IN COMMON, DIMENSION, OR EQUIVALENCE STATEMENT

DEC OCT
FI 114 00162

DEC OCT
FJ 113 00161
I 112 00160
J 111 00157
X 110 00156

SYMBOLS AND LOCATIONS FOR SOURCE PROGRAM FORMAT STATEMENTS

EFN LOC
811 1 00151

EFN LOC

LOCATIONS FOR OTHER SYMBOLS NOT APPEARING IN SOURCE PROGRAM

DEC OCT
1) 106 00152

DEC OCT

DEC OCT
(RTN) 1 00001

DEC OCT

(RTN) (TSH)

ENTRY POINTS TO SUBROUTINES NOT OUTPUT FROM LIBRARY

EXTERNAL FORMULA NUMBERS WITH CORRESPONDING INTERNAL FORMULA NUMBERS AND OCTAL LOCATIONS

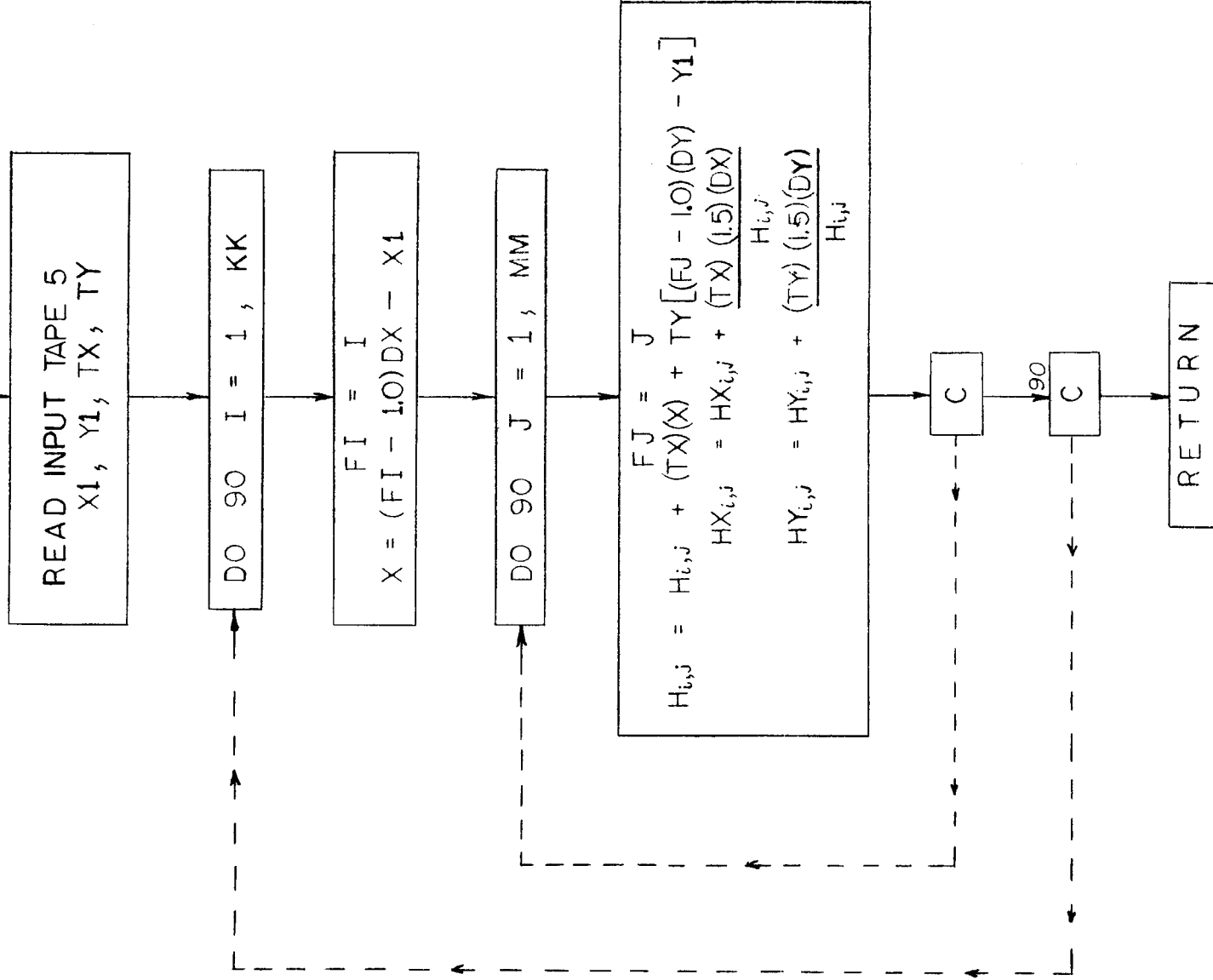
EFN IFN LOC
90 16 00120

EFN IFN LOC

TILTH

JPL VARIABLE FILM HYDROSTATIC BEARING PROGRAM -- BLOCK DIAGRAM

DIMENSION : H, HX, HY, A, KEY, Q, W, CSI, ETA, A, P
 COMMON : KK, MM, DX, DY, H, HX, HY, ..., X1, Y1, TX, TY, A, INDEX1, INDEX2
 START



I-29

FUNCTION DETER(AA,LIMJ).

STORAGE NOT USED BY PROGRAM

DEC OCT
264 00410
32561 77461

STORAGE LOCATIONS FOR VARIABLES NOT APPEARING IN COMMON, DIMENSION, OR EQUIVALENCE STATEMENT

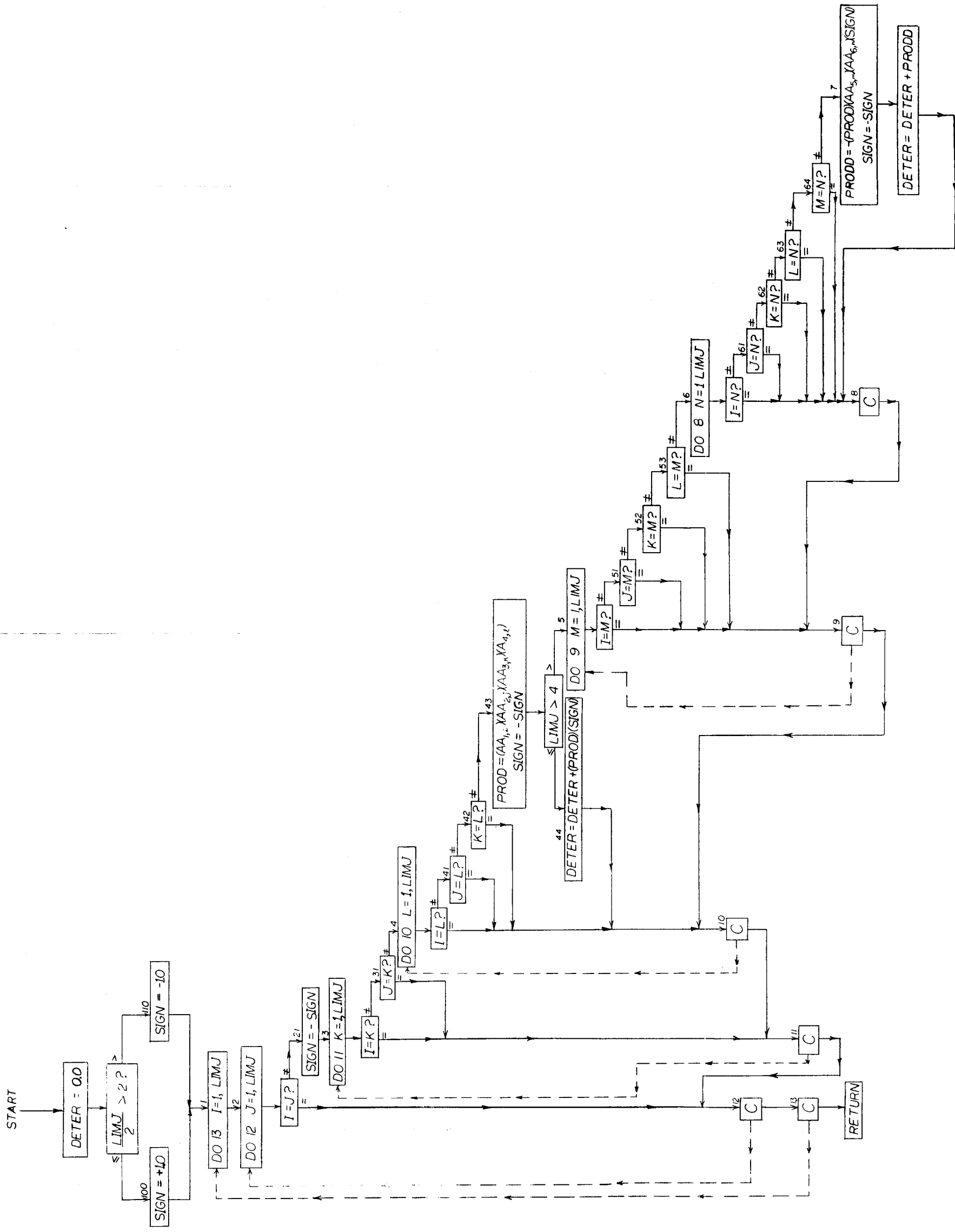
DEC OCT	DEC OCT	DEC OCT	DEC OCT	DEC OCT
263 00407	I 262 00406	J 261 00405	K 260 00404	L 259 00403
M 258 00402	N 257 00401	PRODD 256 00400	PROD 255 00377	SIGN 254 00376

LOCATIONS FOR OTHER SYMBOLS NOT APPEARING IN SOURCE PROGRAM

DEC OCT	DEC OCT	DEC OCT	DEC OCT	DEC OCT
2) 227 00343	3) 230 00346	6) 232 00350	9) 238 00356	C)100 242 00362
C)101 243 00363	C)102 244 00364	C)103 245 00365	C)104 246 00366	C)105 247 00367
C)200 248 00370	C)201 249 00371	C)202 250 00372	C)203 251 00373	C)204 252 00374
C)205 253 00375	D)105 63 00077	D)107 77 00115	D)201 185 00271	D)301 184 00270
D)40V 193 00301	D)60V 192 00300	E)C 96 00140	E)H 131 00203	E)R 176 00260
E)S 183 00267	E)T 187 00273	E)I 199 00307	E)I 199 00307	E)I 187 00273
E)111 199 00307	E)20R 176 00260	E)30T 187 00273		

EXTERNAL FORMULA NUMBERS WITH CORRESPONDING INTERNAL FORMULA NUMBERS AND OCTAL LOCATIONS

EFN	IFN	LOC	EFN	IFN	LOC	EFN	IFN	LOC
100	6	00052	110	8	00055	1	9	00057
3	14	00105	31	16	00121	4	17	00124
43	21	00146	44	24	00165	5	26	00172
53	30	00212	6	31	00215	61	33	00226
64	36	00237	7	37	00242	8	40	00263
11	43	00310	12	44	00316	13	45	00326
						2	10	00067
						41	19	00135
						51	28	00204
						62	34	00231
						9	41	00274
						21	13	00103
						42	20	00143
						52	29	00207
						63	35	00234
						10	42	00302



F-B2099

APPENDIX II

IBM 7094 LOADING RECORD

(Six Subprograms)

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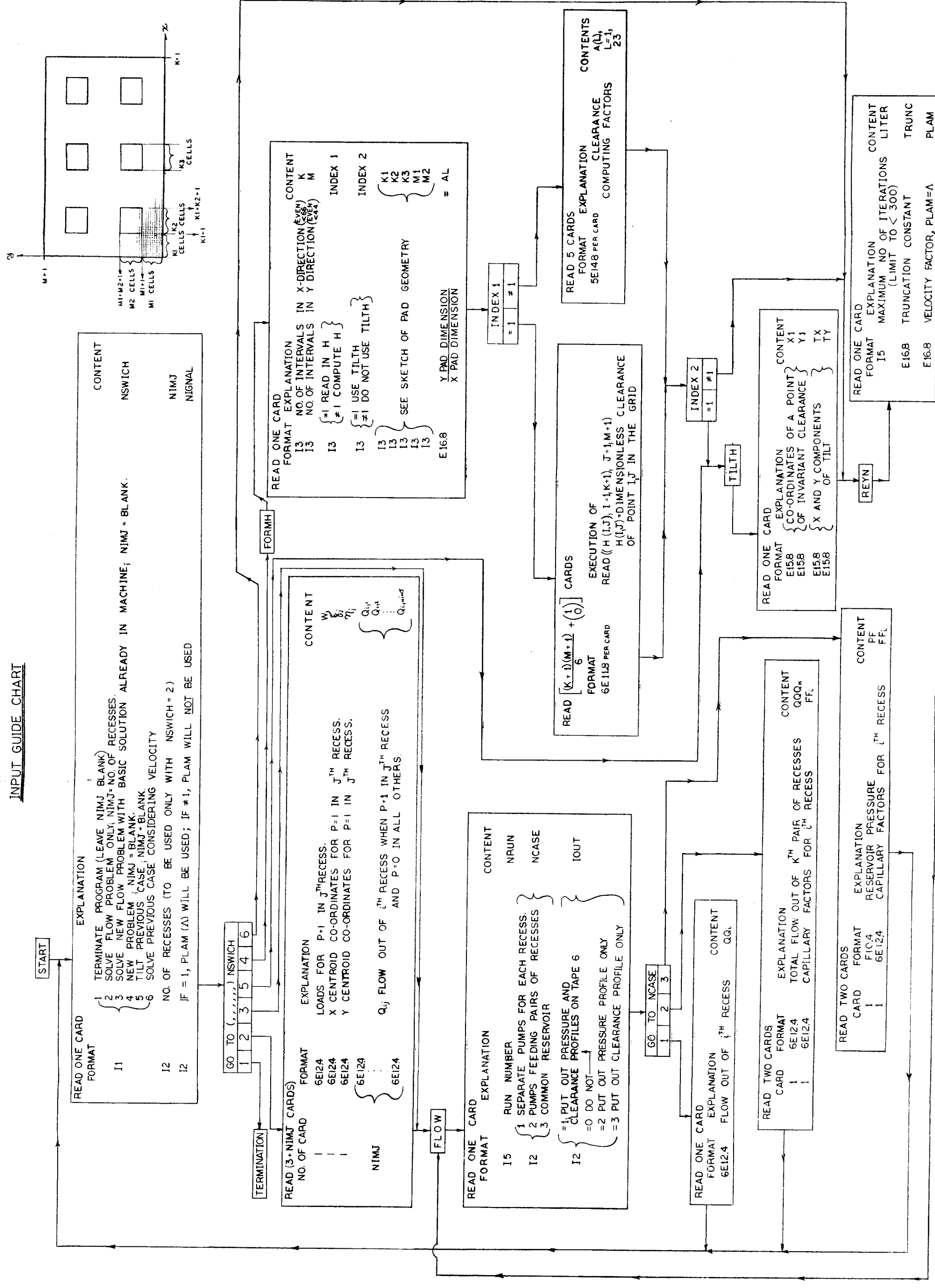
ENTRY POINTS TO SUBROUTINES REQUESTED FROM LIBRARY,											
(FPT) (STB)	(RWT) (SLO)	(TSHM) (WLR)	(RTN) (EFT)	EXIT COS	(STHM) EXP	(FIL) SQRT	(TSB) SIN	(SLI)	(RLR)		
ENTRY NAME	ENTRY ADD.	NO. OF TRANSFERS	LOAD ADD.								
MAIN	00155	00011	00144								
FLOW	00341	00011	00324								
REYN	12326	00011	12311								
TILTH	17101	00002	17073								
FORMH	17271	00007	17256								
DETER	21137	00000	21133								
ERRDMP	21544	00001	21543								
EXIT	21547										
(YES)	21571	00000	21571								
(FPT)	21572	00000	21572								
EXP	21630	00000	21630								
SIN	21710	00000	21707								
COS	21707										
SQRT	22060	00000	22060								
(RLR)	22221	00011	22134								
(TSB)	22145										
(WLR)	22267	00007	22236								
(STB)	22245										
(TSHM)	22334	00006	22323								
(TSH)	22331										
(STHO)	22401	00006	22360								
(STHM)	22371										
(STH)	22366										
(LEFT)	22512	00002	22510								
(RWT)	22521	00002	22517								
(SLI)	22542	00000	22542								
(SLO)	22557	00000	22557								
(RDC)	22625	00007	22574								
(RER)	22603										
(WTC)	22704	00012	22641								
(WER)	22653										
(SET)	23011	00001	22734								
(BUF)	23013										
(EXB)	23016										
(IOB)	22735										
(RTN)	25571	00002	24026								
(FIL)	25560										
(IOH)	24030										
(ICO)	26037	00003	25745								
(TEF)	26036										
(RCH)	26035										
(ETT)	26034										
(REW)	26033										
(WEF)	26032										
(BSR)	26031										
(WRS)	26030										
(RDS)	26027										
(IOS)	25750										
(TRC)	26040										
)PRNT(	26333	00002	26074								
(EXEM)	26076	00000	26704								
(IOU)	26707										
LOGICAL TAPE	MACHINE TAPE	TOTAL WRITES	TOTAL READS	NOISE RECORDS WRITING	RECORDS READING	TOTAL REDUNDANCIES WRITING	READING	POSITIONING ERRORS			
1	A 1	0	493	0	0	0	0	0			
2	B 2	1008	1142	0	0	0	0	0			

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APPENDIX III

INPUT GUIDE CHART

INPUT GUIDE CHART



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APPENDIX IV

SAMPLE PROBLEM INPUT DATA

AND

OUTPUT RESULTS

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HYDROSTATIC BEARING PROGRAM INPUT DATA

CROSS OUT CARDS NOT USED

1. CARD

1	3	5
4		0
NSWICH	NIGNAL	

2. 1 CARD

3	6	9	12	15	18	21	24	27	43
28	16	0	0	5	5	0	4	2	0.57142857
K	M	INDEX1	INDEX2	K1	K2	K3	M1	M2	AL

3.

14	28	42	56	70
1.0	0.0	0.0	0.0	0.0
A(1)	A(2)			

4.

0.0	0.0	0.0	0.0	0.0
-----	-----	-----	-----	-----

5. 5 CARDS
(INCLUDE ALL 5)

0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0
0.0	0.0	0.0	0.0	0.0

7.

0.0	0.0	0.0	0.0	0.0
		A(23)		

8. 1 CARD

15	30	45	60

9. 1 CARD

5	21	37
1000	0.30	0.0
LITER	TRUNC	PLAM

10. 1 CARD

5	7	9
7701	1	1
NRUN	NCASE	IOUT

11. 1 CARD

12	24	36	48	60	72
1.0	1.0	1.0	1.0		
QQ(1)	QQ(2)	QQ(3)	QQ(4)		

12. 1 CARD

10

13. 1 CARD

12	24	36	48	60	72

14. 1 CARD

1

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HYDROSTATIC BEARING PROGRAM INPUT DATA F-B2099
CROSS OUT CARDS NOT USED

1. CARD	1 5	3	5 0										
	NSWICH		NIGNAL										
2. 1 CARD	3	6	9	12	15	18	21	24	27	43			
3.	14	28	42	56	70								
4.													
5. 5 CARDS (INCLUDE ALL 5)													
6.													
7.													
8. 1 CARD	15 0.50	30 0.28571429	45 1.0	60 0.0									
	XI	YI	TX	TY									
9. 1 CARD	5 1000	21 0.30	37 1.0										
	LITER	TRUNC	PLAM										
10. 1 CARD	5 .7702	7 1	9 1										
	NRUN	NCASE	IOUT										
11. 1 CARD	12 1.0	24 1.0	36 1.0	48 1.0	60	72							
	QQ(1)	QQ(2)	QQ(3)	QQ(4)									
12. 1 CARD	10												
13. 1 CARD	12	24	36	48	60	72							
14. 1 CARD	1												

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HYDROSTATIC BEARING PROGRAM INPUT DATA F-B2099

CROSS OUT CARDS NOT USED

1. CARD	1 6 NSWICH	3 	5 1 NIGNAL							
2. 1 CARD	3	6	9	12	15	18	21	24	27	43
3.	14	28	42	56	70					
4.										
5. 5 CARDS (INCLUDE ALL 5)										
6.										
7.										
8. 1 CARD	15	30	45	60						
9. 1 CARD	5 1000 LITER	21 0.30 TRUNC	37 1.0 PLAM							
10. 1 CARD	5 7703 NRUN	7 1 NCASE	9 2 IOUT							
11. 1 CARD	12 1.0 QQ(1)	24 1.0 QQ(2)	36 1.0 QQ(3)	48 1.0 QQ(4)	60	72				
12. 1 CARD	10									
13. 1 CARD	12	24	36	48	60	72				
14. 1 CARD	1 1 NSWICH									

```

RUN NUMBER 7701
HYDROSTATIC BEARING PAD WITH 4 RECESSES.
FEEDING = POSITIVE DISPLACEMENT PUMPS FEEDING EACH RECESS.
K1 = 5 K2 = 5 K3 = 0 M1 = 4 M2 = 2
GRID POINTS, K = 28 M = 16
CLEARANCE COEFFICIENTS
AA 1)= 0.09999999E 01 ,AA
OUTPUT
** Q(I,J)=
1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.00 1.00
0.0773 0.0773 0.0773 0.0773 0.0773 0.0773 0.0773 0.0773 0.0773 0.0773
0.2922 0.2922 0.2922 0.2922 0.2922 0.2922 0.2922 0.2922 0.2922 0.2922
0.1900 0.1900 0.1900 0.1900 0.1900 0.1900 0.1900 0.1900 0.1900 0.1900
0.3815 0.3815 0.3815 0.3815 0.3815 0.3815 0.3815 0.3815 0.3815 0.3815
TOTAL LOAD= 0.0933 CSI= 0.5000 EIA= 0.2857 TOTAL FLOW= 0.4000000E 01
FINAL RESULTS =
RECESS PRESSURES
AL(1) = 0.30184, AL(2) = 0.30184, AL(3) = 0.30184, AL(4) = 0.30184, AL(

```

[illegible]

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PRESSURE DISTRIBUTION

RUN	7701	I= 1	I= 2	I= 3	I= 4	I= 5	I= 6	I= 7	I= 8	I= 9	I= 10
J= 1,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
J= 2,	0.	0.0117	0.0237	0.0362	0.0487	0.0596	0.0665	0.0699	0.0708	0.0708	0.0694
J= 3,	0.	0.0230	0.0470	0.0725	0.0991	0.1232	0.1365	0.1425	0.1438	0.1438	0.1412
J= 4,	0.	0.0334	0.0687	0.1077	0.1519	0.1977	0.2140	0.2198	0.2208	0.2208	0.2180
J= 5,	0.	0.0419	0.0866	0.1379	0.2031	0.3018	0.3018	0.3018	0.3018	0.3018	0.3018
J= 6,	0.	0.0477	0.0980	0.1543	0.2209	0.3018	0.3018	0.3018	0.3018	0.3018	0.3018
J= 7,	0.	0.0508	0.1036	0.1604	0.2243	0.3018	0.3018	0.3018	0.3018	0.3018	0.3018
J= 8,	0.	0.0520	0.1051	0.1596	0.2143	0.2632	0.2835	0.2918	0.2942	0.2942	0.2922
J= 9,	0.	0.0523	0.1052	0.1586	0.2101	0.2534	0.2770	0.2879	0.2912	0.2912	0.2887
J= 10,	0.	0.0520	0.1051	0.1596	0.2143	0.2632	0.2835	0.2918	0.2942	0.2942	0.2922
J= 11,	0.	0.0508	0.1036	0.1604	0.2243	0.3018	0.3018	0.3018	0.3018	0.3018	0.3018
J= 12,	0.	0.0477	0.0980	0.1543	0.2209	0.3018	0.3018	0.3018	0.3018	0.3018	0.3018
J= 13,	0.	0.0419	0.0866	0.1379	0.2031	0.3018	0.3018	0.3018	0.3018	0.3018	0.3018
J= 14,	0.	0.0334	0.0687	0.1077	0.1519	0.1977	0.2140	0.2198	0.2208	0.2208	0.2180
J= 15,	0.	0.0230	0.0470	0.0725	0.0991	0.1232	0.1365	0.1425	0.1438	0.1438	0.1412
J= 16,	0.	0.0117	0.0237	0.0362	0.0487	0.0596	0.0665	0.0699	0.0708	0.0708	0.0694
J= 17,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

PRESSURE DISTRIBUTION

RUN	7701	I= 11	I= 12	I= 13	I= 14	I= 15	I= 16	I= 17	I= 18	I= 19	I= 20
J= 1,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
J= 2,	0.0657	0.0600	0.0545	0.0507	0.0494	0.0507	0.0507	0.0545	0.0600	0.0657	0.0694
J= 3,	0.1337	0.1201	0.1076	0.0995	0.0967	0.0995	0.0995	0.1076	0.1201	0.1337	0.1412
J= 4,	0.2082	0.1797	0.1573	0.1439	0.1396	0.1439	0.1439	0.1573	0.1797	0.2082	0.2180
J= 5,	0.3018	0.2340	0.1989	0.1808	0.1752	0.1808	0.1808	0.1989	0.2340	0.3018	0.3018
J= 6,	0.3018	0.2562	0.2249	0.2071	0.2013	0.2071	0.2071	0.2249	0.2562	0.3018	0.3018
J= 7,	0.3018	0.2649	0.2390	0.2234	0.2182	0.2234	0.2234	0.2390	0.2649	0.3018	0.3018
J= 8,	0.2843	0.2639	0.2447	0.2318	0.2273	0.2318	0.2318	0.2447	0.2639	0.2843	0.2922
J= 9,	0.2798	0.2630	0.2461	0.2343	0.2301	0.2343	0.2343	0.2461	0.2630	0.2798	0.2887
J= 10,	0.2843	0.2639	0.2447	0.2318	0.2273	0.2318	0.2318	0.2447	0.2639	0.2843	0.2922
J= 11,	0.3018	0.2649	0.2390	0.2234	0.2182	0.2234	0.2234	0.2390	0.2649	0.3018	0.3018
J= 12,	0.3018	0.2562	0.2249	0.2071	0.2013	0.2071	0.2071	0.2249	0.2562	0.3018	0.3018
J= 13,	0.3018	0.2340	0.1989	0.1808	0.1752	0.1808	0.1808	0.1989	0.2340	0.3018	0.3018
J= 14,	0.2082	0.1797	0.1573	0.1439	0.1396	0.1439	0.1439	0.1573	0.1797	0.2082	0.2180
J= 15,	0.1337	0.1201	0.1076	0.0995	0.0967	0.0995	0.0995	0.1076	0.1201	0.1337	0.1412
J= 16,	0.0657	0.0600	0.0545	0.0507	0.0494	0.0507	0.0507	0.0545	0.0600	0.0657	0.0694
J= 17,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

PRESSURE DISTRIBUTION									
RUN	7701	I = 21	I = 22	I = 23	I = 24	I = 25	I = 26	I = 27	I = 28
J = 1,		0.	0.	0.	0.	0.	0.	0.	0.
J = 2,		0.0708	0.0699	0.0665	0.0596	0.0487	0.0362	0.0237	0.0117
J = 3,		0.1438	0.1425	0.1365	0.1232	0.0991	0.0725	0.0470	0.0230
J = 4,		0.2208	0.2198	0.2140	0.1977	0.1519	0.1077	0.0687	0.0334
J = 5,		0.3018	0.3018	0.3018	0.3018	0.2031	0.1379	0.0866	0.0419
J = 6,		0.3018	0.3018	0.3018	0.3018	0.2209	0.1543	0.0980	0.0477
J = 7,		0.3018	0.3018	0.3018	0.3018	0.2243	0.1604	0.1036	0.0508
J = 8,		0.2942	0.2918	0.2835	0.2632	0.2143	0.1596	0.1051	0.0520
J = 9,		0.2912	0.2879	0.2770	0.2534	0.2101	0.1586	0.1052	0.0523
J = 10,		0.2942	0.2918	0.2835	0.2632	0.2143	0.1596	0.1051	0.0520
J = 11,		0.3018	0.3018	0.3018	0.3018	0.2243	0.1604	0.1036	0.0508
J = 12,		0.3018	0.3018	0.3018	0.3018	0.2209	0.1543	0.0980	0.0477
J = 13,		0.3018	0.3018	0.3018	0.3018	0.2031	0.1379	0.0866	0.0419
J = 14,		0.2208	0.2198	0.2140	0.1977	0.1519	0.1077	0.0687	0.0334
J = 15,		0.1438	0.1425	0.1365	0.1232	0.0991	0.0725	0.0470	0.0230
J = 16,		0.0708	0.0699	0.0665	0.0596	0.0487	0.0362	0.0237	0.0117
J = 17,		0.	0.	0.	0.	0.	0.	0.	0.

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[illegible]

CLEARANCE DISTRIBUTION										
RUN	7701	I = 21	I = 22	I = 23	I = 24	I = 25	I = 26	I = 27	I = 28	I = 29
J= 1,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 2,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 3,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 4,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 5,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 6,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 7,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 8,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 9,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 10,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 11,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 12,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 13,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 14,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 15,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 16,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
J= 17,	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000

```

RUN NUMBER      7702
HYDROSTATIC BEARING PAD WITH 4 RECESSES.
FEEDING = POSITIVE DISPLACEMENT PUMPS FEEDING EACH RECESS.
      K1 = 5      K2 = 5      K3 = 0      M1 = 4      M2 = 2
GRID POINTS, K = 28      M = 16
CLEARANCE COEFFICIENTS
,AA 1)= 0.09999999E 01 ,AA
      OUTPUT
      ** Q(I,J)=
      1.00      1.00      1.00      2.5957      -0.1453      -0.2683
      -0.8124
      -0.2692
      -0.1379      10.5371      -3.2231
      -0.1379
      -0.2692      -3.2231      10.5371
      -0.1379
      -0.8124      -0.2683      -0.1453
      2.5957
      FINAL RESULTS = TOTAL LOAD= 0.1187      CSI= 0.3708      ETA= 0.2857      TOTAL FLOW= 0.4000000E 01
      RECESS PRESSURES
      , AL(1)= 0.60023,      AL(2)= 0.17013,      AL(3)= 0.17013,      AL(4)= 0.60023,      AL(

```

```

RUN NUMBER 7702
PAD CONFIGURATION. 00000000000000000000000000
HYDROSTATIC BEARING PAD WITH 4 RECESSES.
FEEDING = POSITIVE DISPLACEMENT PUMPS FEEDING EACH RECESS.
02222222222222222222222222222220
02222222222222222222222222222220
02222222222222222222222222222220
02222222222222222222222222222220
02222111112222222111112220
02222111112222222111112220
02222111112222222111112220
02222111112222222111112220
0222222222222222222222222220
0222222222222222222222222220
0222222222222222222222222220
0222222222222222222222222220
0222211111222222211112220
0222211111222222211112220
0222211111222222211112220
0222211111222222211112220
0222222222222222222222222220
0222222222222222222222222220
0222222222222222222222222220
0222222222222222222222222220
000000000000000000000000000000

```

PRESSURE DISTRIBUTION

RUN	7702	I= 1	I= 2	I= 3	I= 4	I= 5	I= 6	I= 7	I= 8	I= 9	I= 10
J= 1,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
J= 2,	0.	0.0337	0.0623	0.0878	0.1100	0.1273	0.1367	0.1398	0.1398	0.1379	0.1310
J= 3,	0.	0.0661	0.1230	0.1746	0.2218	0.2603	0.2788	0.2846	0.2846	0.2816	0.2694
J= 4,	0.	0.0956	0.1788	0.2572	0.3353	0.4088	0.4321	0.4382	0.4356	0.4356	0.4236
J= 5,	0.	0.1196	0.2245	0.3265	0.4408	0.6002	0.6002	0.6002	0.6002	0.6002	0.6002
J= 6,	0.	0.1360	0.2539	0.3649	0.4784	0.6002	0.6002	0.6002	0.6002	0.6002	0.6002
J= 7,	0.	0.1453	0.2691	0.3810	0.4883	0.6002	0.6002	0.6002	0.6002	0.6002	0.6002
J= 8,	0.	0.1494	0.2746	0.3827	0.4757	0.5482	0.5745	0.5819	0.5782	0.5782	0.5627
J= 9,	0.	0.1505	0.2757	0.3820	0.4701	0.5347	0.5653	0.5746	0.5696	0.5696	0.5495
J= 10,	0.	0.1494	0.2746	0.3827	0.4757	0.5482	0.5745	0.5819	0.5782	0.5782	0.5627
J= 11,	0.	0.1453	0.2691	0.3810	0.4883	0.6002	0.6002	0.6002	0.6002	0.6002	0.6002
J= 12,	0.	0.1360	0.2539	0.3649	0.4784	0.6002	0.6002	0.6002	0.6002	0.6002	0.6002
J= 13,	0.	0.1196	0.2245	0.3265	0.4408	0.6002	0.6002	0.6002	0.6002	0.6002	0.6002
J= 14,	0.	0.0956	0.1788	0.2572	0.3353	0.4088	0.4321	0.4382	0.4356	0.4356	0.4236
J= 15,	0.	0.0661	0.1230	0.1746	0.2218	0.2603	0.2788	0.2846	0.2846	0.2816	0.2694
J= 16,	0.	0.0337	0.0623	0.0878	0.1100	0.1273	0.1367	0.1398	0.1398	0.1379	0.1310
J= 17,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

PRESSURE DISTRIBUTION

RUN	7702	I= 11	I= 12	I= 13	I= 14	I= 15	I= 16	I= 17	I= 18	I= 19	I= 20
J= 1,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
J= 2,	0.1182	0.0997	0.0811	0.0658	0.0546	0.0473	0.0433	0.0416	0.0416	0.0413	0.0412
J= 3,	0.2443	0.2020	0.1615	0.1297	0.1071	0.0926	0.0849	0.0823	0.0823	0.0828	0.0830
J= 4,	0.3922	0.3084	0.2387	0.1885	0.1546	0.1335	0.1228	0.1206	0.1206	0.1248	0.1258
J= 5,	0.6002	0.4111	0.3048	0.2377	0.1942	0.1674	0.1540	0.1532	0.1532	0.1701	0.1701
J= 6,	0.6002	0.4496	0.3439	0.2716	0.2231	0.1921	0.1747	0.1683	0.1683	0.1701	0.1701
J= 7,	0.6002	0.4601	0.3620	0.2914	0.2416	0.2081	0.1875	0.1763	0.1763	0.1701	0.1701
J= 8,	0.5267	0.4444	0.3650	0.3001	0.2512	0.2170	0.1947	0.1813	0.1813	0.1739	0.1705
J= 9,	0.5081	0.4377	0.3648	0.3024	0.2542	0.2197	0.1969	0.1830	0.1830	0.1750	0.1705
J= 10,	0.5267	0.4444	0.3650	0.3001	0.2512	0.2170	0.1947	0.1813	0.1813	0.1739	0.1705
J= 11,	0.6002	0.4601	0.3620	0.2914	0.2416	0.2081	0.1875	0.1763	0.1763	0.1701	0.1701
J= 12,	0.6002	0.4496	0.3439	0.2716	0.2231	0.1921	0.1747	0.1683	0.1683	0.1701	0.1701
J= 13,	0.6002	0.4111	0.3048	0.2377	0.1942	0.1674	0.1540	0.1532	0.1532	0.1701	0.1701
J= 14,	0.3922	0.3084	0.2387	0.1885	0.1546	0.1335	0.1228	0.1206	0.1206	0.1248	0.1258
J= 15,	0.2443	0.2020	0.1615	0.1297	0.1071	0.0926	0.0849	0.0823	0.0823	0.0828	0.0830
J= 16,	0.1182	0.0997	0.0811	0.0658	0.0546	0.0473	0.0433	0.0416	0.0416	0.0413	0.0412
J= 17,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

RUN	7702	PRESSURE DISTRIBUTION									
		I= 21	I= 22	I= 23	I= 24	I= 25	I= 26	I= 27	I= 28	I= 29	I=
J= 1,		0.	0.	0.	0.	0.	0.	0.	0.	0.	
J= 2,		0.0407	0.0394	0.0368	0.0323	0.0256	0.0185	0.0117	0.0055	0.	
J= 3,		0.0823	0.0802	0.0758	0.0671	0.0524	0.0371	0.0232	0.0109	0.	
J= 4,		0.1255	0.1238	0.1195	0.1091	0.0810	0.0554	0.0340	0.0159	0.	
J= 5,		0.1701	0.1701	0.1701	0.1701	0.1094	0.0712	0.0430	0.0200	0.	
J= 6,		0.1701	0.1701	0.1701	0.1701	0.1190	0.0797	0.0487	0.0228	0.	
J= 7,		0.1701	0.1701	0.1701	0.1701	0.1206	0.0827	0.0513	0.0242	0.	
J= 8,		0.1679	0.1644	0.1580	0.1446	0.1139	0.0818	0.0519	0.0248	0.	
J= 9,		0.1670	0.1623	0.1538	0.1381	0.1112	0.0811	0.0519	0.0249	0.	
J= 10,		0.1679	0.1644	0.1580	0.1446	0.1139	0.0818	0.0519	0.0248	0.	
J= 11,		0.1701	0.1701	0.1701	0.1701	0.1206	0.0827	0.0513	0.0242	0.	
J= 12,		0.1701	0.1701	0.1701	0.1701	0.1190	0.0797	0.0487	0.0228	0.	
J= 13,		0.1701	0.1701	0.1701	0.1701	0.1094	0.0712	0.0430	0.0200	0.	
J= 14,		0.1255	0.1238	0.1195	0.1091	0.0810	0.0554	0.0340	0.0159	0.	
J= 15,		0.0823	0.0802	0.0758	0.0671	0.0524	0.0371	0.0232	0.0109	0.	
J= 16,		0.0407	0.0394	0.0368	0.0323	0.0256	0.0185	0.0117	0.0055	0.	
J= 17,		0.	0.	0.	0.	0.	0.	0.	0.	0.	

CLEARANCE DISTRIBUTION											
RUN	7702	I = 21	I = 22	I = 23	I = 24	I = 25	I = 26	I = 27	I = 28	I = 29	I =
J= 1,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 2,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 3,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 4,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 5,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 6,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 7,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 8,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 9,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 10,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 11,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 12,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 13,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 14,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 15,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 16,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	
J= 17,		1.2142857	1.2500000	1.2857143	1.3214286	1.3571429	1.3928571	1.4285714	1.4642857	1.5000000	

```

RUN NUMBER      7703
HYBRID BEARING PAD WITH 4 RECESSES
FEEDING = POSITIVE DISPLACEMENT PUMPS FEEDING EACH RECESS.

LAMBDA = 1.0000
GRID POINTS, K = 28      M = 16
CLEARANCE COEFFICIENTS
AA 11= 0.099999999E 01 ,AA      M1 = 4      M2 = 2

```

	OUTPUT				
Q(1,I) =	1.0000	1.0000	1.0000	1.0000	
W(1,I) =	0.0762	0.0800	0.0762	0.0028	
CS1(I) =	0.2746	0.6943	0.2746	0.2974	
ETA(I) =	0.1889	0.3802	0.1913	0.3826	0.2857
	J=1,	J=2,	J=3,	J=4,	J=5,
Q(1,J) =	2.5957	-0.1453	-0.2683	-0.8124	-0.0774
Q(2,J) =	-0.1379	10.5371	-3.2231	-0.2692	-0.0813
Q(3,J) =	-0.2692	-3.2231	10.5371	-0.1379	-0.0813
Q(4,J) =	-0.8124	-0.2683	-0.1453	2.5957	-0.0774
FINAL RESULTS =	TOTAL LOAD= 0.1308 CSI = 0.3694 ETA= 0.2857 TOTAL FLOW= 0.4000000E 01				
RECESS PRESSURES					
AL(1) =	0.64679,	AL(2) =	0.18384,	AL(3) =	0.18384,
AL(4) =	0.64679,	AL(5) =	0.64679,	AL(6) =	0.64679,

[illegible]

F-B2099

PRESSURE DISTRIBUTION

RUN 7703	I= 1	I= 2	I= 3	I= 4	I= 5	I= 6	I= 7	I= 8	I= 9	I= 10
J= 1,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
J= 2,	0.	0.0363	0.0672	0.0946	0.1185	0.1371	0.1473	0.1507	0.1486	0.1412
J= 3,	0.	0.0712	0.1325	0.1881	0.2390	0.2805	0.3005	0.3067	0.3034	0.2903
J= 4,	0.	0.1030	0.1927	0.2771	0.3613	0.4406	0.4656	0.4722	0.4694	0.4565
J= 5,	0.	0.1289	0.2419	0.3519	0.4750	0.5468	0.6468	0.6468	0.6468	0.6468
J= 6,	0.	0.1466	0.2736	0.3932	0.5155	0.6468	0.6468	0.6468	0.6468	0.6468
J= 7,	0.	0.1566	0.2900	0.4106	0.5262	0.6468	0.6468	0.6468	0.6468	0.6468
J= 8,	0.	0.1610	0.2959	0.4123	0.5126	0.5907	0.6190	0.6230	0.6230	0.6063
J= 9,	0.	0.1621	0.2971	0.4116	0.5066	0.5762	0.6091	0.6192	0.6138	0.5922
J= 10,	0.	0.1610	0.2959	0.4123	0.5126	0.5907	0.6190	0.6270	0.6230	0.6063
J= 11,	0.	0.1566	0.2900	0.4106	0.5262	0.6468	0.6468	0.6468	0.6468	0.6468
J= 12,	0.	0.1466	0.2736	0.3932	0.5155	0.6468	0.6468	0.6468	0.6468	0.6468
J= 13,	0.	0.1289	0.2419	0.3519	0.4750	0.5468	0.6468	0.6468	0.6468	0.6468
J= 14,	0.	0.1030	0.1927	0.2771	0.3613	0.4406	0.4656	0.4722	0.4694	0.4565
J= 15,	0.	0.0712	0.1325	0.1881	0.2390	0.2805	0.3005	0.3067	0.3034	0.2903
J= 16,	0.	0.0363	0.0672	0.0946	0.1185	0.1371	0.1473	0.1507	0.1486	0.1412
J= 17,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

PRESSURE DISTRIBUTION

RUN 7703	I= 11	I= 12	I= 13	I= 14	I= 15	I= 16	I= 17	I= 18	I= 19	I= 20
J= 1,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
J= 2,	0.1273	0.1074	0.0874	0.0710	0.0589	0.0511	0.0467	0.0449	0.0447	0.0445
J= 3,	0.2632	0.2177	0.1741	0.1398	0.1155	0.0999	0.0916	0.0889	0.0894	0.0896
J= 4,	0.4226	0.3324	0.2573	0.2033	0.1668	0.1441	0.1325	0.1303	0.1348	0.1359
J= 5,	0.6468	0.4430	0.3286	0.2562	0.2094	0.1806	0.1662	0.1655	0.1838	0.1838
J= 6,	0.6468	0.4846	0.3707	0.2929	0.2406	0.2073	0.1886	0.1818	0.1838	0.1838
J= 7,	0.6468	0.4959	0.3902	0.3141	0.2605	0.2246	0.2024	0.1904	0.1879	0.1842
J= 8,	0.5676	0.4790	0.3935	0.3235	0.2710	0.2341	0.2101	0.1958	0.1890	0.1842
J= 9,	0.5475	0.4718	0.3933	0.3260	0.2741	0.2371	0.2126	0.1976	0.1890	0.1842
J= 10,	0.5676	0.4790	0.3935	0.3235	0.2710	0.2341	0.2101	0.1958	0.1879	0.1842
J= 11,	0.6468	0.4959	0.3902	0.3141	0.2605	0.2246	0.2024	0.1904	0.1838	0.1838
J= 12,	0.6468	0.4846	0.3707	0.2929	0.2406	0.2073	0.1886	0.1818	0.1838	0.1838
J= 13,	0.6468	0.4430	0.3286	0.2562	0.2094	0.1806	0.1662	0.1655	0.1838	0.1838
J= 14,	0.4226	0.3324	0.2573	0.2033	0.1668	0.1441	0.1325	0.1303	0.1348	0.1359
J= 15,	0.2632	0.2177	0.1741	0.1398	0.1155	0.0999	0.0916	0.0889	0.0894	0.0896
J= 16,	0.1273	0.1074	0.0874	0.0710	0.0589	0.0511	0.0467	0.0449	0.0447	0.0445
J= 17,	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

RUN	7703	PRESSURE DISTRIBUTION									
		I= 21	I= 22	I= 23	I= 24	I= 25	I= 26	I= 27	I= 28	I= 29	I=
J= 1,		0.	0.	0.	0.	0.	0.	0.	0.	0.	
J= 2,		0.0440	0.0425	0.0397	0.0349	0.0277	0.0199	0.0126	0.0060	0.	
J= 3,		0.0889	0.0867	0.0819	0.0725	0.0566	0.0401	0.0250	0.0118	0.	
J= 4,		0.1356	0.1337	0.1291	0.1178	0.0875	0.0598	0.0367	0.0172	0.	
J= 5,		0.1838	0.1838	0.1838	0.1838	0.1182	0.0770	0.0464	0.0216	0.	
J= 6,		0.1838	0.1838	0.1838	0.1838	0.1286	0.0861	0.0526	0.0246	0.	
J= 7,		0.1838	0.1838	0.1838	0.1838	0.1303	0.0893	0.0554	0.0262	0.	
J= 8,		0.1814	0.1777	0.1708	0.1562	0.1231	0.0884	0.0561	0.0268	0.	
J= 9,		0.1804	0.1753	0.1662	0.1492	0.1201	0.0876	0.0561	0.0269	0.	
J= 10,		0.1814	0.1777	0.1708	0.1562	0.1231	0.0884	0.0561	0.0268	0.	
J= 11,		0.1838	0.1838	0.1838	0.1838	0.1303	0.0893	0.0554	0.0262	0.	
J= 12,		0.1838	0.1838	0.1838	0.1838	0.1286	0.0861	0.0526	0.0246	0.	
J= 13,		0.1838	0.1838	0.1838	0.1838	0.1182	0.0770	0.0464	0.0216	0.	
J= 14,		0.1356	0.1337	0.1291	0.1178	0.0875	0.0598	0.0367	0.0172	0.	
J= 15,		0.0889	0.0867	0.0819	0.0725	0.0566	0.0401	0.0250	0.0118	0.	
J= 16,		0.0440	0.0425	0.0397	0.0349	0.0277	0.0199	0.0126	0.0060	0.	
J= 17,		0.	0.	0.	0.	0.	0.	0.	0.	0.	