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**A MODEL EQUATORIAL ELECTROJET**

BY  
**MASAHISA SUGIURA**  
**JOSEPH C. CAIN**

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Masahisa Sugiura

and

Joseph C. Cain

NASA-Goddard Space Flight Center

Greenbelt, Md.

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## Abstract

The cross-sectional profile of the equatorial electrojet is determined for various longitudes along the dip equator, using a set of 48 Gauss coefficients for the earth's magnetic field. The electrojet profile is found to vary appreciably with longitude due to the asymmetry of the magnetic field. To demonstrate the longitudinal variation of the electrojet the profiles for longitudes  $80^{\circ}$  E (for India) and  $280^{\circ}$  E (for Peru) are shown. The maximum current density in the electrojet for the latter longitude is found to be much greater than that for the former longitude. Also the width of the electrojet is greater at  $280^{\circ}$  E than at  $80^{\circ}$  E. The magnetic field produced by the electrojet is computed for various longitudes along the dip equator and also for the locations of six magnetic observatories near the dip equator. The theoretically expected field changes are qualitatively in agreement with the observed values for these observatories. The average electron drift velocity in the electrojet is estimated; over Peru this velocity reaches a few km/sec during a sunspot maximum period at the height of the peak of the electrojet. This value is considerably higher than earlier estimates and is well above the critical electron velocity, i.e., the ion thermal velocity, above which the two-stream instability can occur.

## Introduction

The recent rocket explorations of the equatorial electrojet in India (Maynard and Cahill, 1965a) and off the coast of Peru (Davis et al., 1965; Maynard and Cahill, 1965b) have stimulated general interest in this subject, and it seems timely to present a model electrojet with which the new measurements may be compared. The magnetic observations made in the equatorial regions at ground level have been discussed extensively (Onwumechilli, 1959a, 1959b; Osborne, 1962a, 1962b, 1963; Forbush and Casaverde, 1961). The model presented here is based on a model atmosphere described below and on the magnetic field configuration determined with the 48 Gauss coefficients given by Jensen and Cain (1962). These coefficients were chosen as being the most accurate available at the time this work was begun. A recalculation made with a more recent model (Hendricks and Cain, 1966) has shown that changes in the final results are sufficiently small that the conclusions drawn in this paper are not altered.

Assuming that the physical quantities of the ionosphere are the same everywhere along the dip equator except for the differences arising from the asymmetry of the earth's permanent magnetic field, the cross-sectional profile of the electrojet is determined for different longitudes. In particular, two such profiles, one for longitude  $80^{\circ}\text{E}$  for India and another for longitude  $280^{\circ}\text{E}$  for Peru, are presented. Using such profiles the magnitude of the magnetic field due to the electrojet as observed at ground level is computed as a function of longitude. The longitude variation so obtained is shown to be in fair agreement with the observations at several equatorial observatories.

The average electron drift velocity in the electrojet is estimated, and is shown to be well above the threshold velocity for the two-stream instability discussed by Farley (1963a, 1963b) and Buneman (1963).

### Conductivity profile

We take a rectangular coordinate system ( $x, y, z$ ) such that: the  $x$ - $y$  plane coincides with the ground with the positive  $z$  axis pointing upward; the  $y$  axis is along the dip equator its positive direction being eastward; the  $x$  axis is directed south. The primary electric field is assumed to be static and parallel to the  $y$  axis; we denote this field by  $E_y$ . If we further assume that the vertical Hall current is entirely inhibited by the (vertical) polarization of the medium, this polarization field  $E_z$  is given by

$$E_z = [\sigma_2 / (\sigma_0 \tan^2 I + \sigma_1)] E_y$$

where  $\sigma_0$ ,  $\sigma_1$ , and  $\sigma_2$  are the direct, the Pedersen, and the Hall conductivity, respectively, and where  $I$  is the magnetic dip (Hirono, 1952; Baker and Martyn, 1953). Thus at the dip equator, where  $I = 0$ , the vertical polarization field is  $\sigma_2/\sigma_1$  times the original horizontal field. In Figure 1 the ratio  $\sigma_2/\sigma_1$  is plotted against height. (The ionospheric parameters used for the calculation of the conductivity elements are given in the Appendix.) In the region near 100 km level  $\sigma_2/\sigma_1$  is extremely large, being 20 to 30. It is essentially this large vertical polarization field that drives the electrojet. The sum of the Pedersen current  $\sigma_1 E_y$  and the Hall current  $\sigma_2 E_z$  is the total electrojet current. At the dip equator this is  $\sigma_3 E_y$ , where  $\sigma_3 = \sigma_1 + \sigma_2^2/\sigma_1$ ;  $\sigma_3$  is called the Cowling conductivity.

We denote the effective conductivity in the y direction by  $\sigma_{yy}$ , where

$$\sigma_{yy} = \sigma_1 + \sigma_2^2 / (\sigma_0 \tan^2 I + \sigma_1)$$

Since the electric field  $E_y$  is assumed to be uniform, the cross-sectional profile of  $\sigma_{yy}$  in the x-z plane gives the corresponding profile of the relative current density. The ionospheric parameters are taken to be functions of z alone; while the magnetic field as determined from the 48 Gauss coefficients varies with longitude along the dip equator. It is only the latter that generates the longitudinal variation of the electrojet profile. The electron density distribution at noon is not likely to be the same everywhere along the dip equator, but what we intend to show here is the effect of the nonuniformity of the magnetic field along the dip equator, separating this from other possible effects. We make an idealization that the primary electrostatic field is assumed to be uniform and parallel to the dip equator. The exact electric field distribution can be determined only if the wind pattern and the distributions of the electron density and other ionospheric quantities are completely known all over the world. Without a complete knowledge of these factors we have to rely on known properties of the magnetic variation Sq and of the associated electric field theoretically deduced. The general direction of the electric field in midday in the equatorial region as inferred by the dynamo theory is approximately eastward (Maeda, 1955). The characteristics of Sq are known to be similar along the lines of equal dip, and near noon the Sq current in low latitudes appears to flow nearly parallel to the dip equator (Price and Wilkins, 1963). Thus

for an idealized model the assumption that the primary electric field is parallel to the dip equator seems to be appropriate.

Figures 2 and 3 show contours of equal values of the effective conductivity  $\sigma_{yy}$  in the vertical plane normal to the dip equator for longitude  $80^\circ\text{E}$  (for India) and for longitude  $280^\circ\text{E}$  (for Peru). The numbers indicated along the contours are in units of  $10^{-15}$  e.m.u., or  $10^{-4}$  mho/meter in m.k.s. units. With the assumption that  $E_y$  is uniform the electric current density is proportional to  $\sigma_{yy}$ , hence the profiles can be thought of as the current density profiles. It should be noted that the horizontal scale is 20-fold contracted; therefore, the actual profiles are much more oblong horizontally than is seen in these figures.

#### Electrojet over Peru ( $280^\circ\text{E}$ )

The peak of  $\sigma_{yy}$  is at 103.5 km altitude directly above the dip equator, and its value is 118 in the units used in Figure 3, i.e.,  $1.18 \times 10^{-13}$  e.m.u. ( $1.18 \times 10^{-2}$  mho/meter). The altitudes at which  $\sigma_{yy}$  is reduced to one-half the peak are 97 km and 110.5 km directly above the dip equator. The contour for this half-peak value extends horizontally from 50 km north to 80 km south of the dip equator. It is noted that the electrojet profile is not symmetric with respect to the dip equator; this feature is solely due to the asymmetry of the magnetic field with respect to the dip equator.

#### Electrojet over India ( $80^\circ\text{E}$ )

The  $\sigma_{yy}$  peak is at 102.0 km altitude above the dip equator, and its value is 71 in the same units as in Figure 2, i.e.,  $0.71 \times 10^{-13}$  e.m.u.

( $0.71 \times 10^{-2}$  mho/meter). Thus over India the peak altitude is about 1.5 km lower than over Peru and the peak value over India is only 60% of that over Peru. The altitudes at which  $\sigma_{yy}$  is one-half the peak are 95.5 km and 110 km. Thus the thickness of the electrojet measured by these altitudes is nearly the same in India as in Peru; the thickness so defined is about 14 km. However, the steepness of the conductivity variation with height is much more pronounced over Peru than over India. Horizontally the contour for the half-peak value extends from 55 km north to 40 km south of the dip equator over India. There is a tendency that the electrojet stretches more to the south than to the north in Peru, while in India the tendency is opposite. It is noted that not only is the peak current density smaller over India than over Peru the width of the electrojet is much narrower over India. To illustrate the large differences between the profiles the contours for these longitudes are superimposed upon each other in Figure 4.

It is interesting to note that the altitude of the major part of the electrojet is a little lower than the altitude at which the normal Sq current flows at latitudes slightly off the dip equator as if the electrojet hangs below the Sq current sheet.

#### At other longitudes

As has been shown above for two representative longitudes the peak value of  $\sigma_{yy}$  over the dip equator varies considerably with longitude. The maximum of this  $\sigma_{yy}$  peak occurs near longitude  $310^{\circ}\text{E}$  where its value is  $1.33 \times 10^{-13}$  e.m.u. and the minimum near  $90^{\circ}\text{E}$  where the peak value of  $\sigma_{yy}$  is  $0.68 \times 10^{-13}$  e.m.u. Thus with regard to the  $\sigma_{yy}$  peak India is



close to the minimum and Peru to the maximum, making this pair well suited for further experimental studies of longitudinal inequality of the electrojet.

Having constructed conductivity profiles for different longitudes it is possible to calculate the longitudinal variation of the magnetic field produced by the model electrojet. The horizontal magnetic field  $\Delta H_0$  at the dip equator due to the electrojet is shown in Figure 5 as a function of longitude; values are normalized in the manner explained below to make them comparable with the observational data. The scale can be adjusted, however, by multiplying a constant. It is noted that the value of  $\Delta H_0$  at  $280^\circ\text{E}$  is almost twice that at  $80^\circ\text{E}$ .

To compare the computed field with the observations at the six magnetic observatories listed in Table 1 the horizontal component of the electrojet field at the actual locations of these observatories was computed. There will be an induction effect from the conducting earth, and this effect may be different at different observatories. However, for the sake of simplicity we assume that the horizontal component of the magnetic field due to the electrojet is increased by the induction at the same rate everywhere. Then this factor can be absorbed in the normalization constant in the computed field. For the observational data we take the peak amplitude in  $H$  measured from the midnight value for the annual average  $H$  variation for the five international quiet days for 1958. Denoting these values by the observed  $\Delta H$ , the normalization constant for the calculated  $\Delta H$  is determined so that the average of the latter over the six observatories becomes equal to the corresponding

average of the observed  $\Delta H$ . The observed and the calculated  $\Delta H$  so defined are plotted in Figure 6.

The agreement between the computed and the observed values of  $\Delta H$  is only qualitative. The computed  $\Delta H$  for Huancayo is too large and those of Trivandrum and Ibadan too small compared with the corresponding observed values. The longitudinal variation of  $\Delta H$  calculated here seems to be much larger in amplitude than is observed. Without quantitative arguments we point out that the change in the conductivity with longitude will reduce the longitudinal variation of the electrojet intensity because of the electrostatic field set up by the electrojet itself; in particular, at longitudes near the conductivity maximum at  $310^\circ\text{E}$  longitude the electrojet may be appreciably suppressed by this effect. It is also pointed out that the observed values used in this paper are the annual averages of the amplitude in  $H$  and are only crude measures. The primary purpose of the present paper is to present a model profile of the electrojet, and not to discuss the longitudinal variation in the intensity of the electrojet in precise terms. Also the observed average amplitude  $\Delta H$  (measured from the midnight level) has large seasonal variations. The amplitude is largest in equinox for all the stations except for Jarvis Island where it is a maximum in December solstice; while the amplitude is smallest in December solstice for Ibadan, Addis Ababa, and Trivandrum, but for Jarvis Island, Koror, and Huancayo the minimum is in June solstice. Thus it appears that factors other than the longitudinal inequality in the permanent magnetic field play an important

part in producing the longitudinal variation in the electrojet.

As to the width of the electrojet there is little observational data to compare with the present result. However, Onwumechilli (1959b) estimated the width of the electrojet in Nigeria to be about 440 km; while Forbush and Casaverde (1961) took the electrojet width to be about 660 km in Peru. Since these figures are based on different models, they cannot be compared directly. Nevertheless the tendency that the electrojet is of greater width in South America than in Africa is in complete agreement with our present results.

#### Magnetic field distribution through the electrojet

To provide theoretical values to be compared with the recent rocket measurements the magnetic field was computed as a function of height directly above the dip equator both for longitudes  $80^{\circ}\text{E}$  and  $280^{\circ}\text{E}$ ; the results are shown in Figure 7. In the calculation the value of  $E_y$  was adjusted so as to give values of  $\Delta H$  at ground level comparable with the typical observed values in India and in Peru during the periods the rocket firings were made. For  $80^{\circ}\text{E}$ , i.e., for India, the electrojet field at ground level on the dip equator is  $24\gamma$ ; if the induction effect is taken to be one-half of this value, the total field will be  $36\gamma$ . For  $280^{\circ}\text{E}$ , i.e., for Peru, the electrojet field at the ground is taken to be  $53\gamma$  so that with the same rate for the induction effect as above the total field would be about  $80\gamma$ . These values are very much lower than those observed in 1958 because the solar activity is near a minimum during the period we are concerned here. In Figure 7 the magnetic

field directly due to the electrojet alone is shown without the induced field. When the induction effect is included the magnetic field gradient below 90 km would tend to become smaller than is shown in these figures.

With the present model there is a sudden reversal in the vertical gradient of the magnetic field at about 90 km altitude, above which the field change is very nearly linear to about 115 km. There is a second turning point at about 125 km to 130 km altitude, and the change becomes nearly linear again above this level.

#### Discussions

1. Rastogi (1962) compared the observed electrojet effects in the American, African, and Indian zones and showed that the effect is most pronounced in the American zone, less so in Africa and least in India. This is in agreement with the present result shown in Figure 5. By an approximate calculation Rastogi argued that  $\sigma_3$  at 100 km level varies very little with longitude, and suggested that the observed large longitudinal variation is probably due to a longitudinal variation in the electric field. However, the present calculation shows that  $\sigma_3$  varies appreciably with longitude, the ratio of  $\sigma_3$  at 80°E to that at 280°E being 0.61 at 102.5 km altitude. The errors introduced by the approximations in Rastogi's argument contribute enough to mask the dependence of  $\sigma_2^2/\sigma_1$  on the magnetic field. The wind pattern and the electron density distribution are not likely to be exactly the same along the equator, but we point out that the asymmetry of the magnetic field alone

could give rise to a considerable longitudinal variation in the electrojet intensity.

2. In the dynamo theory the conductivity is usually integrated over the thickness of the ionosphere. The integrated value of our  $\sigma_3$  from 90 km to 160 km altitude is compared in Table 2 with the height-integrated  $\sigma_3$  given by other workers. Although these values are in agreement in magnitude, it seems that for detailed studies of the global Sq current system the variation in the conductivity with longitude (as well as with latitude), in addition to the variations with season and solar cycle, should be taken into account. A new calculation is under way to construct an electrojet model based on the actual rocket measurement of electron density recently made over the dip equator off the coast of Peru.

3. Since the Hall current due to the vertical polarization field is the main constituent of the electrojet, the average electron velocity,  $v_e$ , can be approximately represented by

$$v_e = (E_z/B)/(1 + v_e^2/\omega_e^2)$$

where  $v_e$  and  $\omega_e$  are the electron collision and cyclotron frequencies respectively. The direction of the electron stream is westward. At the electrojet height  $v_e \ll \omega_e$ , and hence the average electron velocity is very nearly  $E_z/B$ . Therefore, if  $E_y$  is uniform,  $v_e$  varies with height proportionately with the ratio  $\sigma_2/\sigma_1$ . Thus when  $E_y/B$  is multiplied to the abscissa in Figure 1, it approximately gives the average drift velocity of the electrons in the electrojet as a function of height. Throughout the height range 90 km to 130 km over Peru  $v_e$  is given, to a

good approximation, by  $3.8 \times 10^4 (\sigma_2/\sigma_1) E_y$  m/sec when  $E_y$  is expressed in volts/m. When  $E_y = 2.4 \times 10^{-3}$  volts/m,  $\Delta H$  at Huancayo due directly to the electrojet is 100 $\gamma$ ; if the induction effect is taken to be one-half of this external field, the total variation observed will be about 150 $\gamma$ . With this value of  $E_y$ , the average electron drift velocity at the height of the peak current is 2.7 km/sec. The average ion velocity is little affected by the presence of the large polarization field in the electrojet, and is only of the order of a few meters per second at the most in the 100 km to 110 km region. During sunspot minimum years the average electron streaming velocity at the electrojet peak would be about one-half of the above estimate.

Farley (1963a, 1963b) and Buneman (1963) have shown that if the streaming electron velocity relative to the corresponding ion velocity exceeds the ion thermal velocity a two-stream plasma instability can occur and they attributed a certain type of E region irregularities observed at the dip equator (and in the auroral zone) to longitudinal ion waves generated by this instability. The observational aspect of this interesting phenomenon has been discussed in detail by Bowles, Balsley, and Cohen (1963) and Cohen and Bowles (1963). The ion thermal velocity in the electrojet region is about 400 m/sec. If we take this value as the minimum critical electron drift velocity for the instability, the present model over Peru shows that if  $E_y$  is taken to be  $2.4 \times 10^{-3}$  volts/m, the average electron drift velocity in the electrojet region is well above this critical value.

Zmuda (1960) estimated the electron drift velocity at 310 m/sec. This value is based on a current density of  $1 \times 10^{-5}$  amp/m<sup>2</sup> with an electron density of  $2 \times 10^5$  electrons/cm<sup>3</sup>. His estimate of the average electron velocity is considerably lower than our estimate. At the height of the peak current density in the present model the electron density is  $8.0 \times 10^4$  electrons/cm<sup>3</sup>, and the current density is  $2.8 \times 10^{-5}$  amp/m<sup>2</sup>. As was pointed out by himself the high electron density Zmuda used corresponds to the density in a sporadic E layer; while the present electron density may be thought to be a value under a normal condition. In Zmuda's model the electric current density is averaged over the thickness of the electrojet; therefore, the current density quoted above must be considerably lower than that at the peak of the electrojet. As to the estimate of the electric field, Zmuda's estimate,  $4 \times 10^{-4}$  volts/m, is lower than the value adopted here, namely,  $2.4 \times 10^{-3}$  volts/m. This is because Zmuda took  $\sigma_3$  to be constant through the electrojet region; moreover his value of  $\sigma_3$ , i.e.,  $2.5 \times 10^{-2}$  mho/m, is higher than the present estimate at the electrojet peak, i.e.,  $1.18 \times 10^{-2}$  mho/m; his  $\sigma_3$  is high because of the high electron density in his model. Matsushita (1962) estimated the horizontal electric field to be  $1.6 \times 10^{-3}$  volts/m, and obtained an estimate of the average electron drift velocity of 500 m/sec by averaging the current over the thickness of the electrojet. Since these authors assumed the current to be uniform over a thickness of a few tens km, the current density is greatly reduced compared with the present current density estimate for the peak electrojet altitude.

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## APPENDIX

The conductivity elements  $\sigma_0$ ,  $\sigma_1$ , and  $\sigma_2$  (in e.m.u.) are calculated by the following formulas:

$$\begin{aligned}\sigma_0 &= N_e e^2 [(m_e \nu_e)^{-1} + (m_i \nu_i)^{-1}] \\ \sigma_1 &= N_e e^2 [(m_e \nu_e)^{-1} \nu_e^2 (\nu_e^2 + \omega_e^2)^{-1} + (m_i \nu_i)^{-1} \nu_i^2 (\nu_i^2 + \omega_i^2)^{-1}] \\ \sigma_2 &= N_e e^2 [(m_e \nu_e)^{-1} \nu_e \omega_e (\nu_e^2 + \omega_e^2)^{-1} - (m_i \nu_i)^{-1} \nu_i \omega_i (\nu_i^2 + \omega_i^2)^{-1}]\end{aligned}$$

where

$N_e$  = electron density, electrons/cm<sup>3</sup>

$e$  = magnitude of the electronic charge

$m_{e,i}$  = electron, or ion, mass

$\nu_{e,i}$  = electron, or ion, collision frequency

$\omega_{e,i}$  = electron, or ion, cyclotron frequency, taken to be positive regardless of the sign of charge

It is assumed that there is only one type of singly ionized ions.

Because of the polarization of the medium the electron density is not exactly the same as the ion density. However, the deviation ( $\Delta N_e$ ) from the neutrality is extremely small. Assuming that all the quantities concerned vary with  $z$  alone, we can estimate the charge density from Poisson's equation:  $dE_z/dz = 4\pi e \Delta N_e$ .

Thus

$$\Delta N_e = (4\pi e)^{-1} E_y d(\sigma_2/\sigma_1)/dz$$

Taking  $E_y = 2.4 \times 10^3$  e.m.u.,  $\Delta N_e$  is of the order of  $10^{-4}$  cm<sup>-3</sup> in the electrojet region. Thus the assumption of neutrality in the computation of the conductivity elements is justified.

Following Chapman (1956) the collision frequencies are computed by the following formulas:

$$\nu_e = \nu_{ei} + \nu_{en}$$

where

$$\nu_{ei} = [34 + 4.18 \log (T^3 N_e^{-1})] N_e T^{-3/2}$$

$$\nu_{en} = 5.4 \times 10^{-10} N_n T^{1/2}$$

and

$$\nu_i = \nu_{in} = 2.6 \times 10^{-9} (N_e + N_n) W^{-1/2}$$

where  $N_n$ ,  $T$ , and  $W$  are the neutral particle density, the temperature, and the mean molecular weight of the ions (which is assumed to be equal to that of the neutral particles).

The atmospheric model given by Champion and Minzner (1963) was used for  $N_n$ ,  $T$ , and  $W$ . These data together with the computed collision frequencies are given in Table 3 in an abbreviated form. The profile of the electron density  $N_e$  used is shown by the heavy curve in Figure 8; this curve is a smoothed average of the two dotted curves that represent the rocket data obtained at Wallops Island by Bauer and Jackson (1963) with the CW propagation technique. The electron density profile adopted here is meant only to serve as a model. In a new model to be presented in a later publication the electron density determined by the actual rocket measurements in the electrojet region and a more recently determined spherical harmonic representation of the main field will be used.

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Table 1. Six equatorial observatories used in this paper.

Observatory	Longitude	Latitude	Dip*	Distance from dip
				equator to station**
Ibadan	3. <sup>o</sup> 90E	7. <sup>o</sup> 43N	-5. <sup>o</sup> 29	233 <sup>km</sup>
Addis Ababa	38.77E	9.03N	-1.42	56
Trivandrum	76.95E	8.50N	-1.94	83
Koror	134.50E	7.33N	-0.22	21
Jarvis Island	160.03W	0.38S	1.77	-80
Huancayo	75.33W	12.05S	0.70	-48

\* Computed values based on the spherical harmonic representation of the main field, and not observed values.

\*\* The distance between the computed dip equator and the station; positive when the station is south of the dip equator.

Table 2. Comparison of estimates of the height-integrated  $\sigma_3$  by several workers.

Present paper	80°E	1.21 x 10 <sup>-7</sup> e.m.u.
	280°E	1.97
H. Maeda (1953)		0.775
Baker and Martyn (1953)		1.64
Fejer (1953)		1.80
Chapman (1956) hot ionosphere		2.08
	cold ionosphere	1.93
Hirano and Kitamura (1956)		1.52

Table 3. The atmospheric model used in this paper.

Height	$N_n$	$W$	$T$	$v_e$	$v_i$
	$\text{cm}^{-3}$		$^{\circ}\text{K}$	$\text{sec}^{-1}$	$\text{sec}^{-1}$
90 km	$6.584 \times 10^{13}$	29.00	180	$4.77 \times 10^5$	$3.18 \times 10^4$
100	$1.036 \times 10^{13}$	28.88	210	$7.61 \times 10^4$	$5.02 \times 10^3$
110	$2.073 \times 10^{12}$	28.56	257	$1.63 \times 10^4$	$1.01 \times 10^3$
120	$5.235 \times 10^{11}$	28.07	349	$4.72 \times 10^3$	$2.57 \times 10^2$
130	$1.650 \times 10^{11}$	27.70	515	$1.85 \times 10^3$	$8.15 \times 10^1$
140	$7.476 \times 10^{10}$	27.31	715	$1.03 \times 10^3$	$3.72 \times 10^1$
150	$4.115 \times 10^{10}$	26.93	893	$7.22 \times 10^2$	$2.06 \times 10^1$
160	$2.622 \times 10^{10}$	26.65	1022	$5.89 \times 10^2$	$1.32 \times 10^1$



## Figures

Figure 1. The ratio  $\sigma_2/\sigma_1$  (for  $280^\circ\text{E}$  longitude) as a function of height.

Figure 2. The conductivity ( $\sigma_{yy}$ ) profile for longitude  $80^\circ\text{E}$  for India in the vertical plane perpendicular to the dip equator; contours of equal  $\sigma_{yy}$  are drawn in units of  $10^{-15}$  e.m.u., or  $10^{-4}$  mho/meter; north to the right. Note that the horizontal scale is 20-fold contracted in comparison with the vertical scale.

Figure 3. The conductivity ( $\sigma_{yy}$ ) profile for longitude  $280^\circ\text{E}$  for Peru, units are the same as in Figure 2.

Figure 4. A comparison of the conductivity profiles for longitudes  $80^\circ\text{E}$  and  $280^\circ\text{E}$ ; units are the same as in Figures 2 and 3.

Figure 5. The computed electrojet field at the dip equator as a function of longitude.

Figure 6. Comparison of the observed values of  $\Delta H$  with those computed, for six equatorial observatories.

Figure 7. The magnetic field produced by the electrojet as a function of height, for longitudes  $80^\circ\text{E}$  and  $280^\circ\text{E}$ .

Figure 8. The electron density profile used in this paper. Two curves drawn with broken lines represent profiles obtained by rockets over Wallops Island (Bauer and Jackson, 1963).

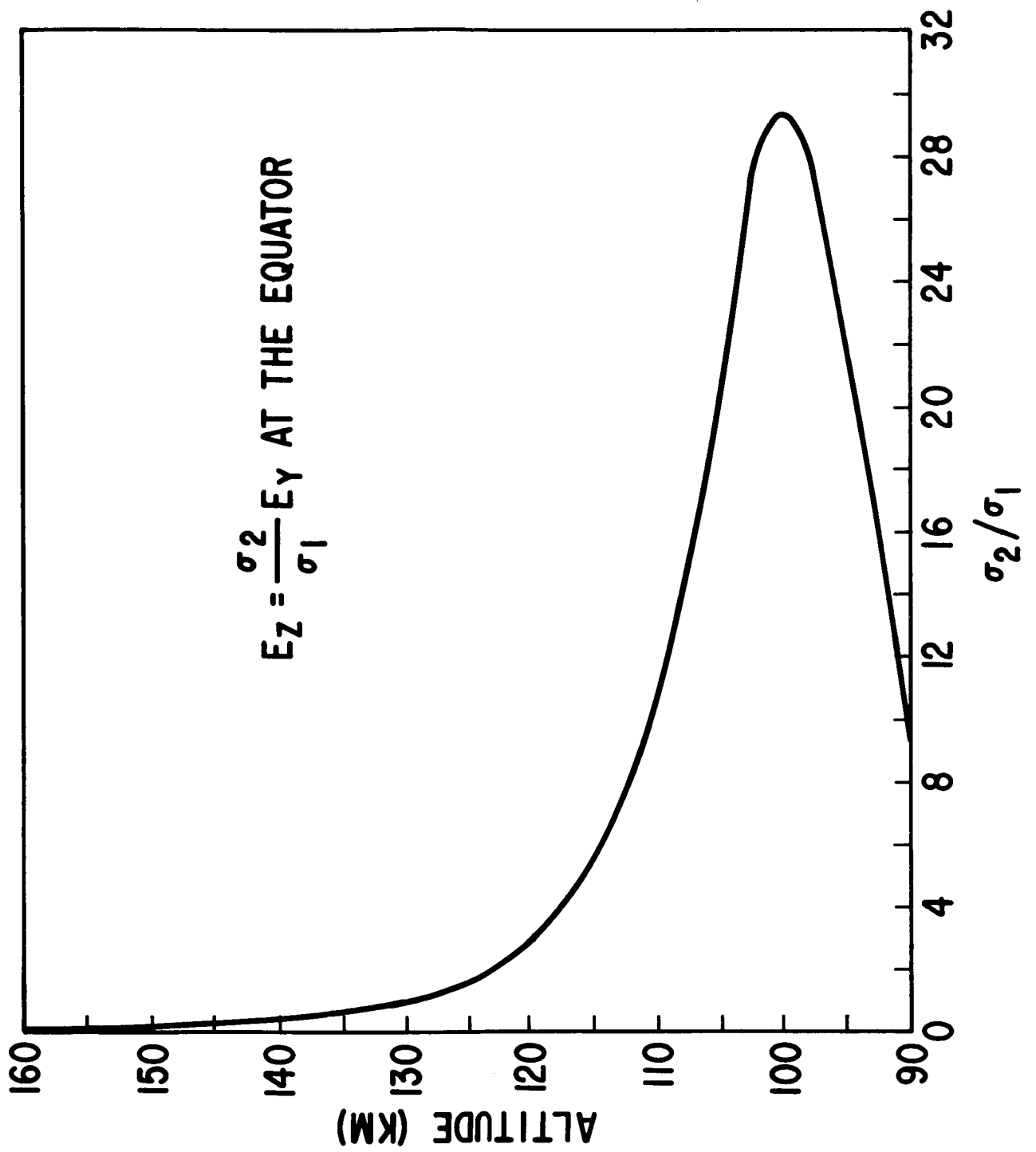


Figure 1

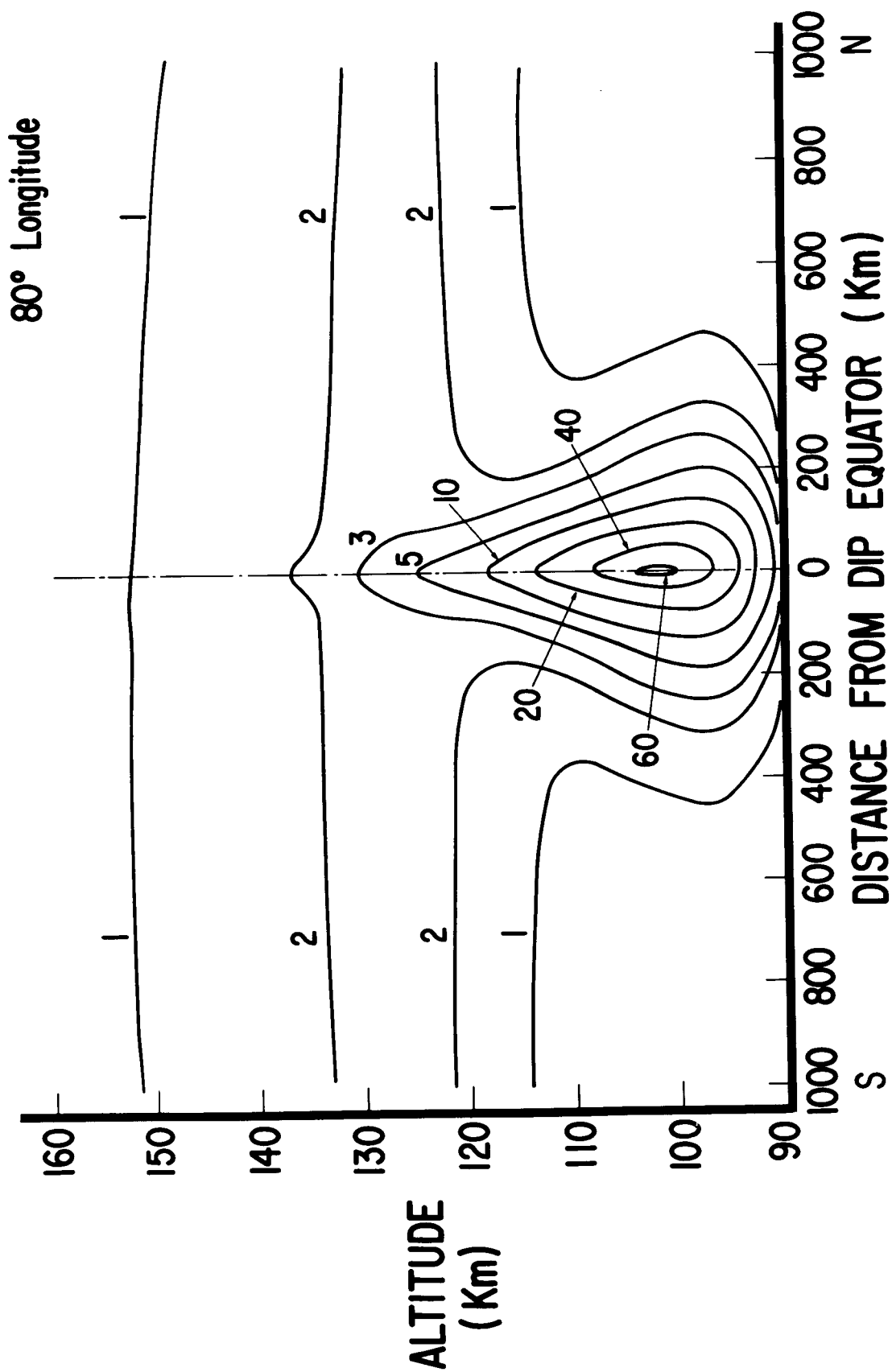


Figure 2

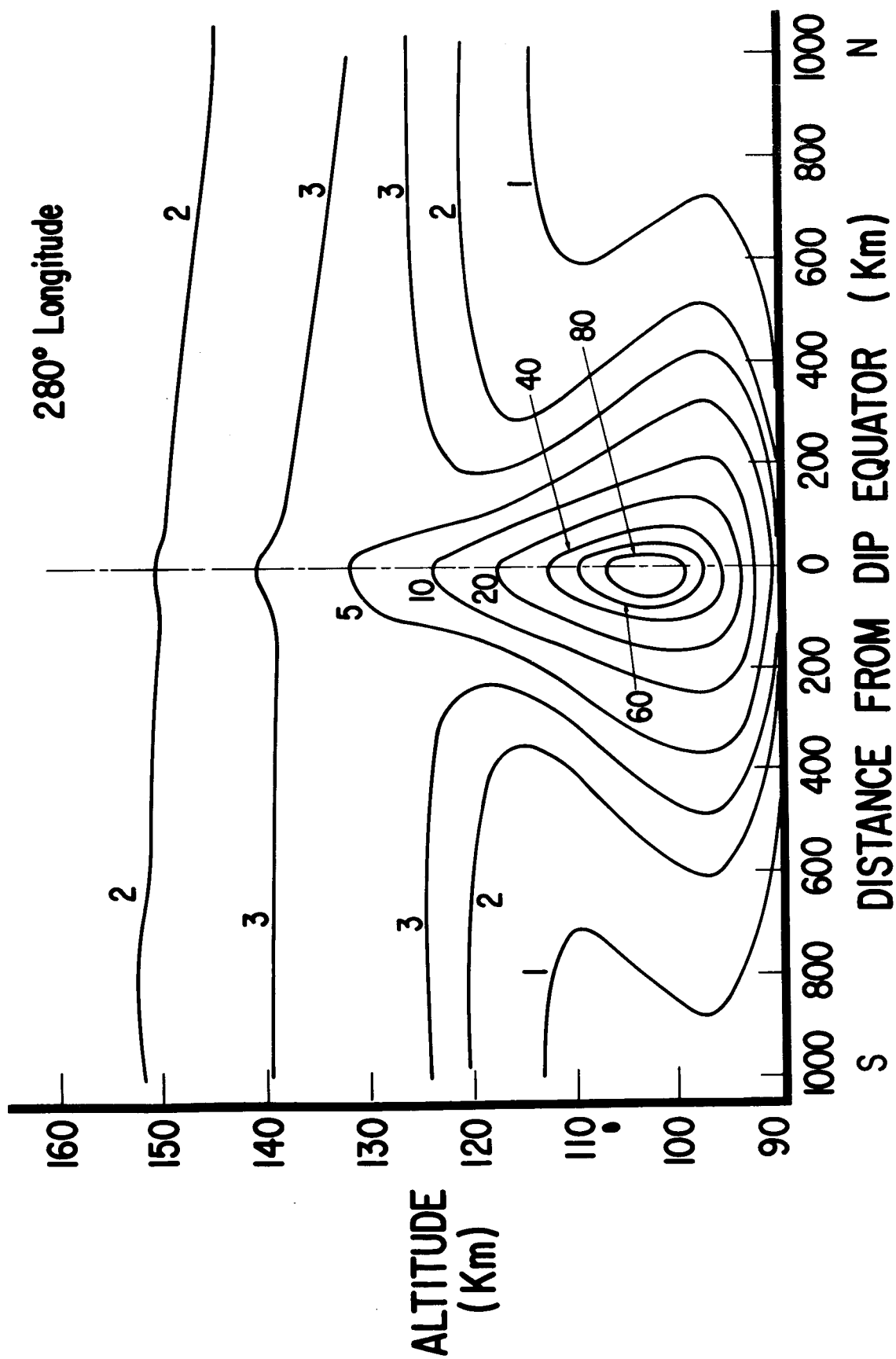


Figure 3

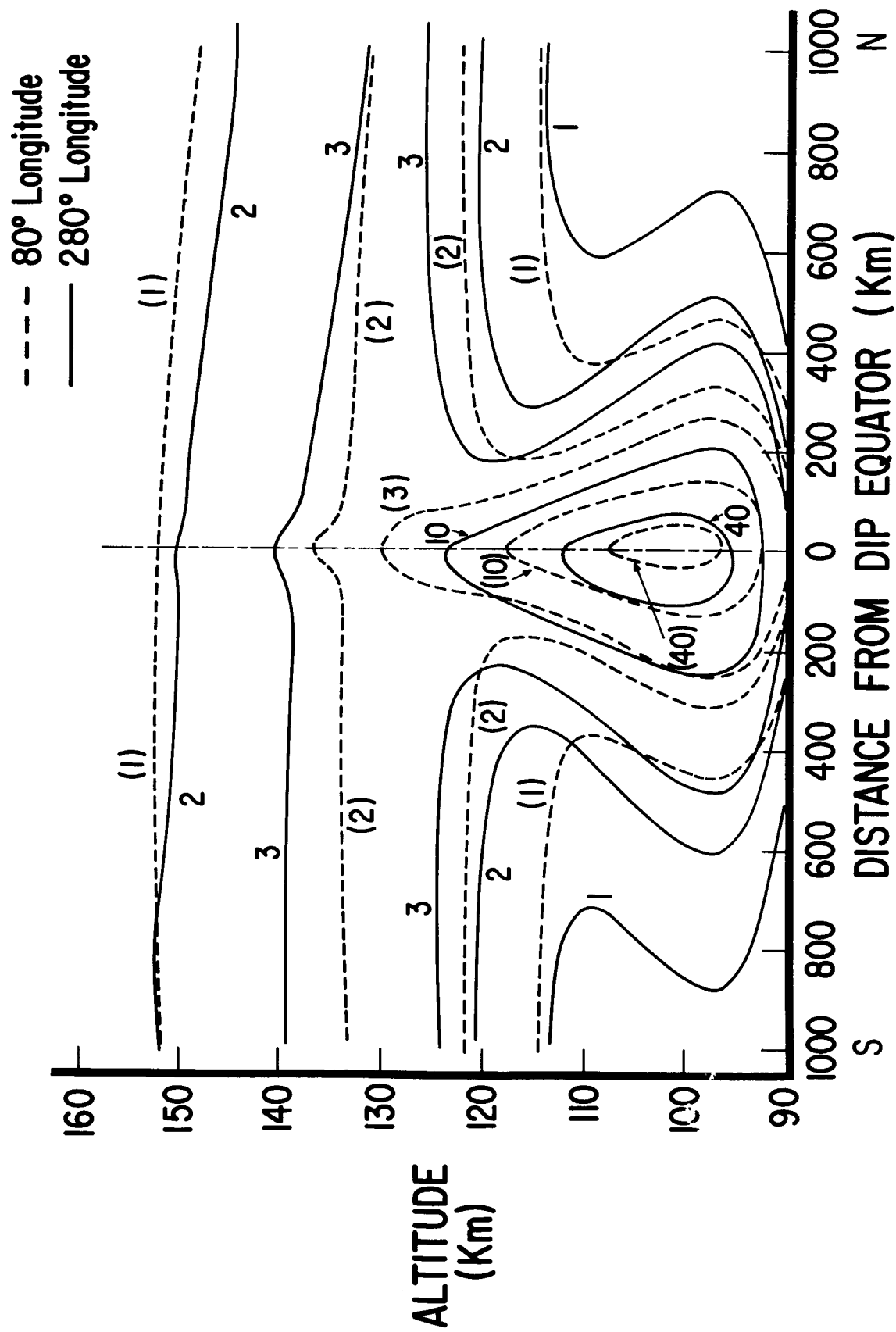


Figure 4

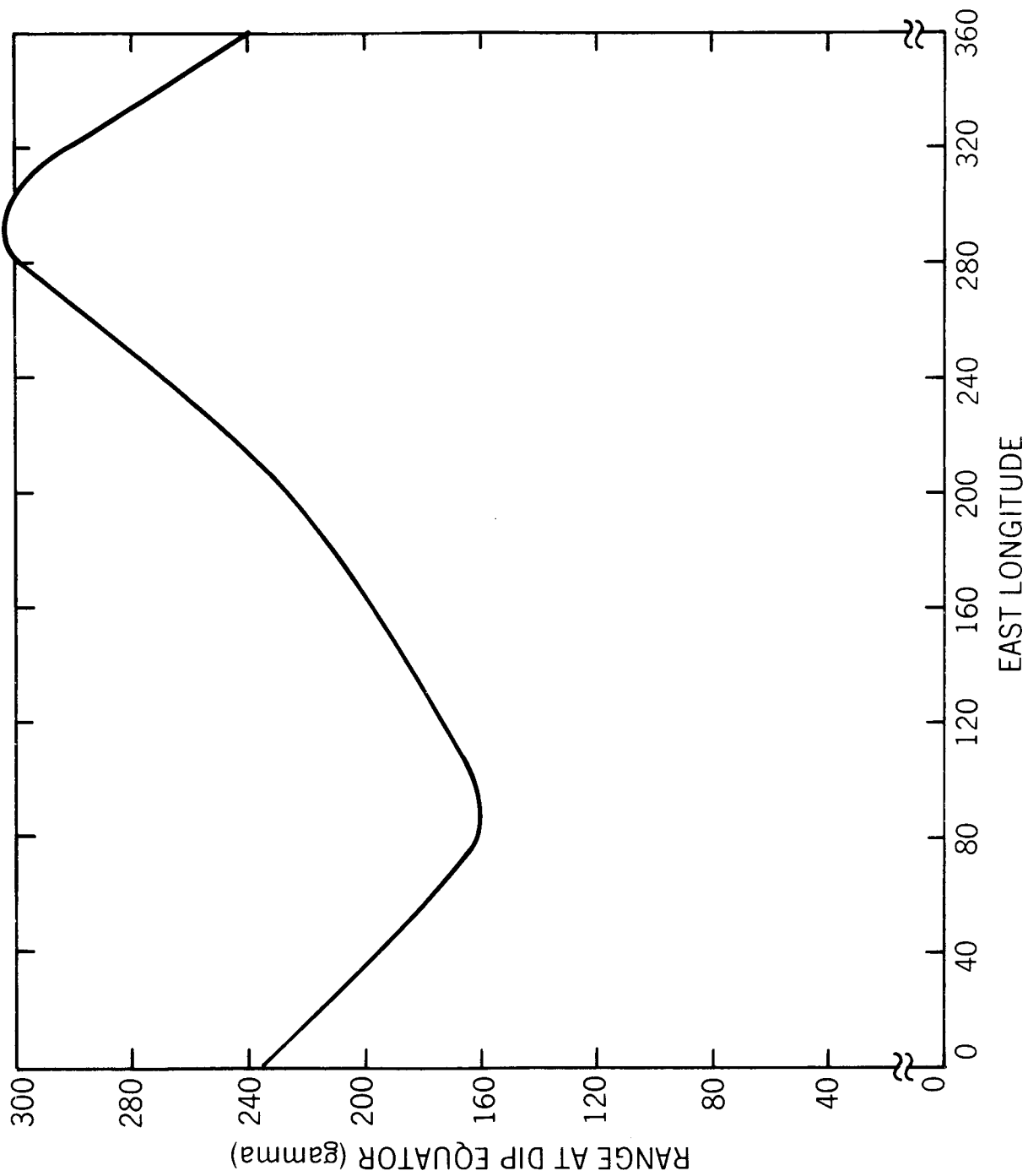


Figure 5

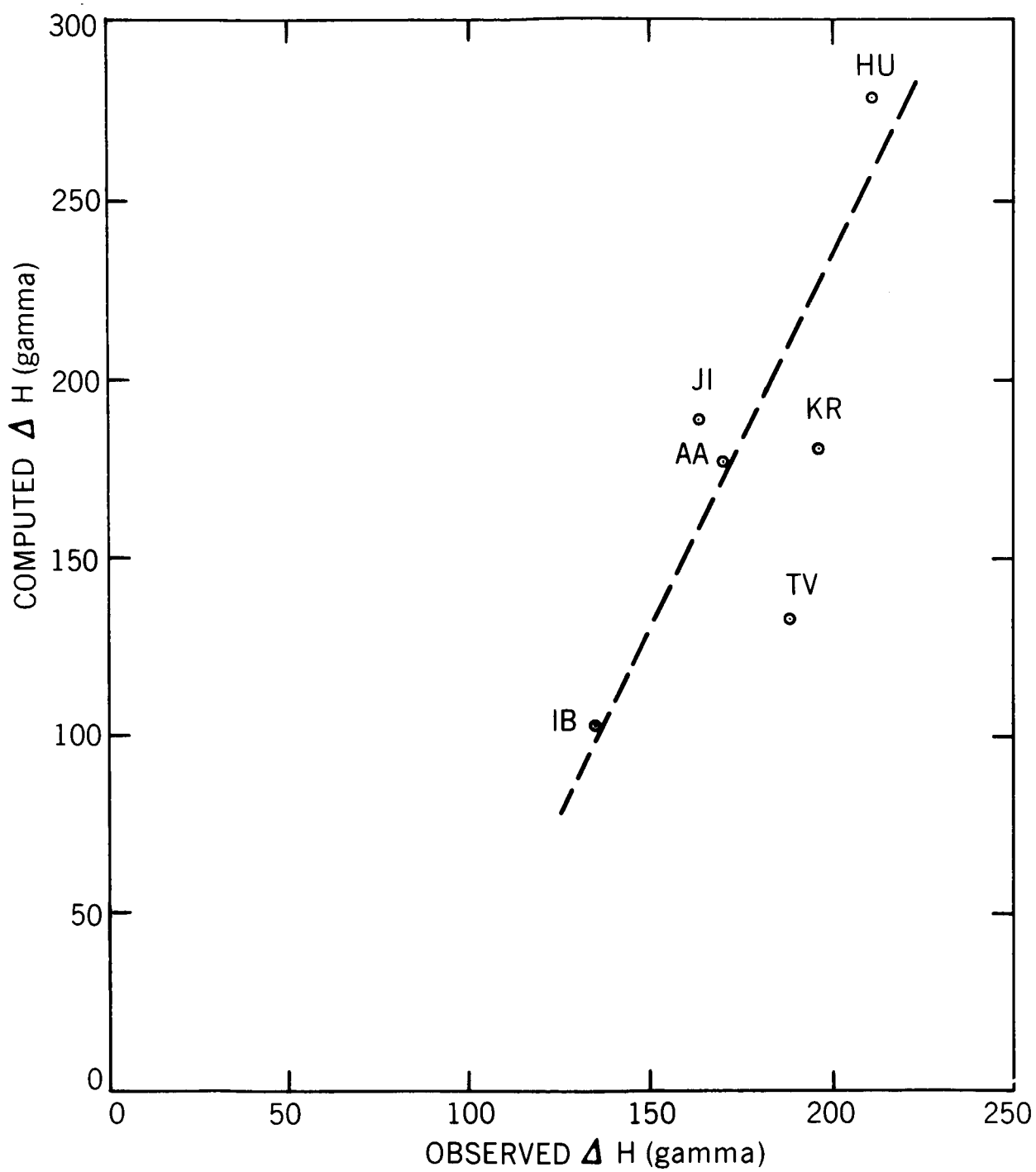


Figure 6

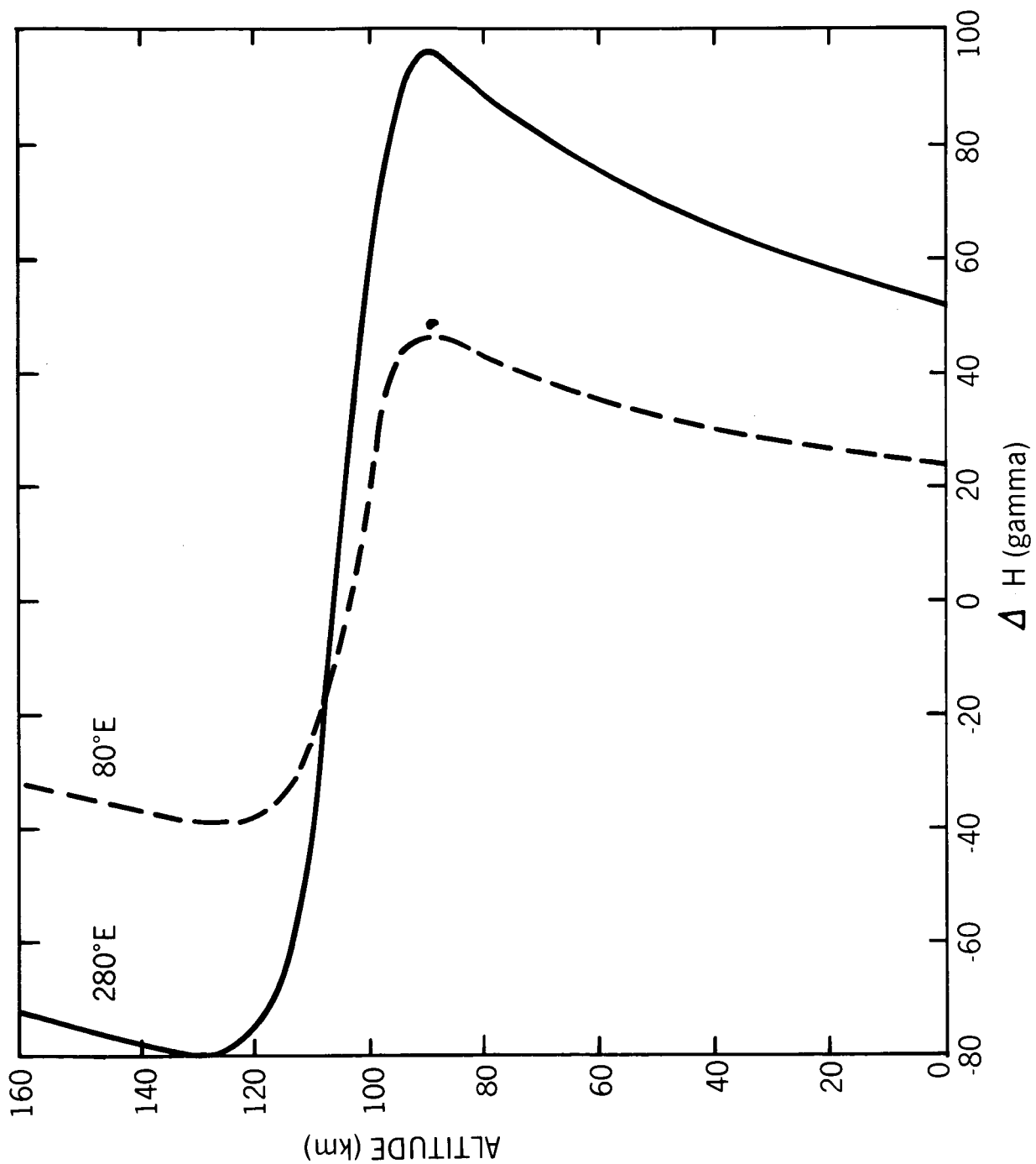


Figure 7



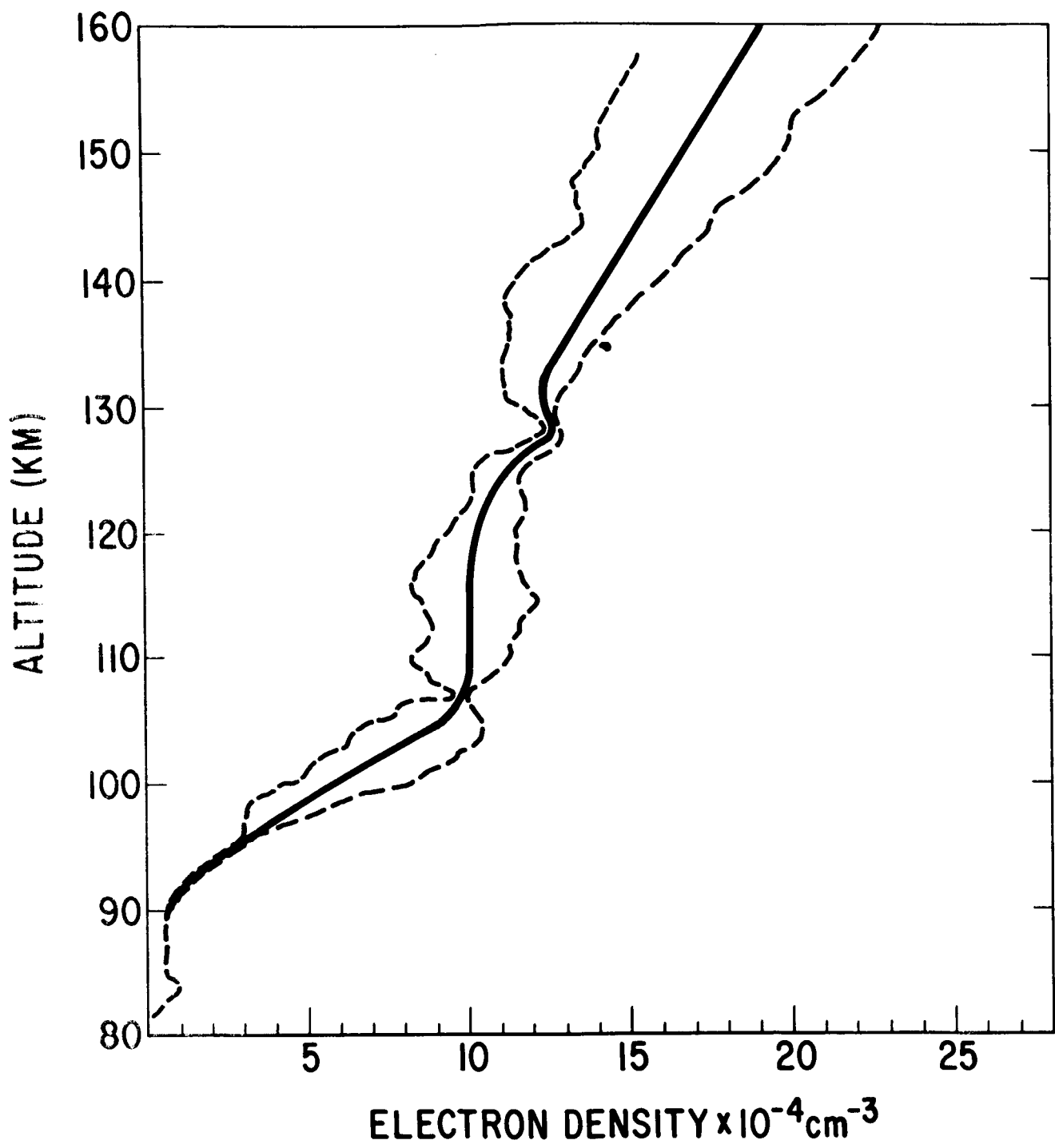


Figure 8