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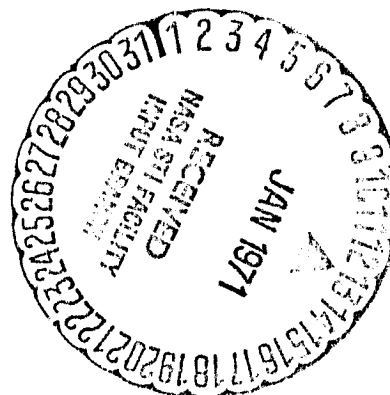
QUADRUPOLE SEGMENTED
ROD STUDY

October 1970

Contract NAS5-11185
SPO Number 30001

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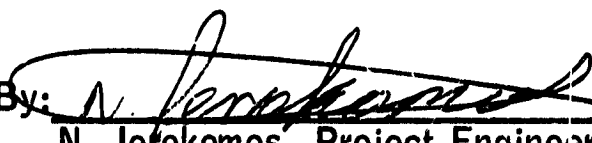
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Greenbelt, Maryland

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**QUADRUPOLE SEGMENTED
ROD STUDY**

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INTRODUCTION

Introduction of ions into a quadrupole mass filter system under normal conditions inherently introduces affects which are detrimental to the probability of a stable ion traversing the length of the quadrupole without striking the rods. These detrimental conditions are determined by the characteristics of the scan line of the system, fringing fields, phase, initial amplitude and entry angle as well as several other parameters. Designing and operating a quadrupole in such a manner as to minimize one or several of the above detrimental characteristics is possible, for example, quad bias to slow the ions down after they are accelerated to get the maximum intensity from the source and masking, to eliminate small values of amplitude which cause unstable particles to be very penetrating, etc. In this report the use of segmented rods is discussed in the application of reducing the affects of the fringe fields and the instabilities of the scan line.

SCAN LINE EFFECT

A quadrupole is normally scanned by varying the magnitude of the ac and dc potentials along a scan line whose slope is determined by the resolution at which the system is to be operated. Figure 1 shows the typical a, q plot of the stability characteristics of a quadrupole with a scan line (SL) superimposed on this plot.

In Figure 1, two stability regions are shown to illustrate the point of one scan line being able to scan different masses (M and $\bar{M}$). The scan line, as it develops from the origin to maximum transmission ((a_1, q_0) or (a_1', q_0')), passes first through an unstable region until it crosses the stability boundary for a given mass. As the ion passes through the unstable region its y-axis amplitude increases continually until the ion enters the stable region. The amplitude increases by an almost exponential growth, as shown in Figure 2. The rate of growth versus time spent in the unstable region is of course also determined by initial conditions, such as phase at which the ion enters with respect to the RF field, initial amplitude and angle, etc. The time an ion spends in the unstable region is largely dependent on the fringe fields which the ions must pass through before they reach the position of full strength of the ac and dc fields.

The fringe fields are defined by the scan line and their relative affect can thus be calculated.

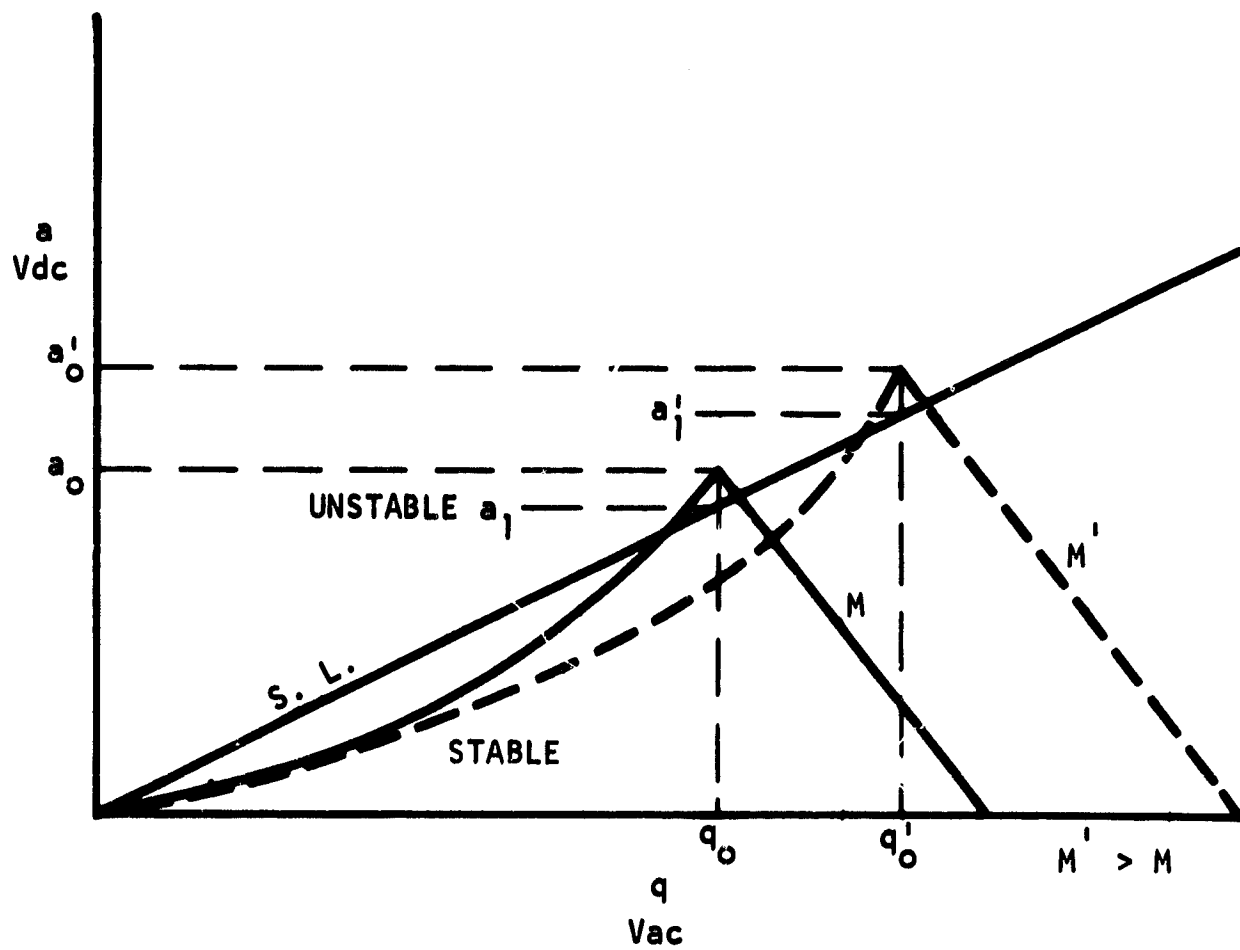


FIGURE 1. Typical Scan Line

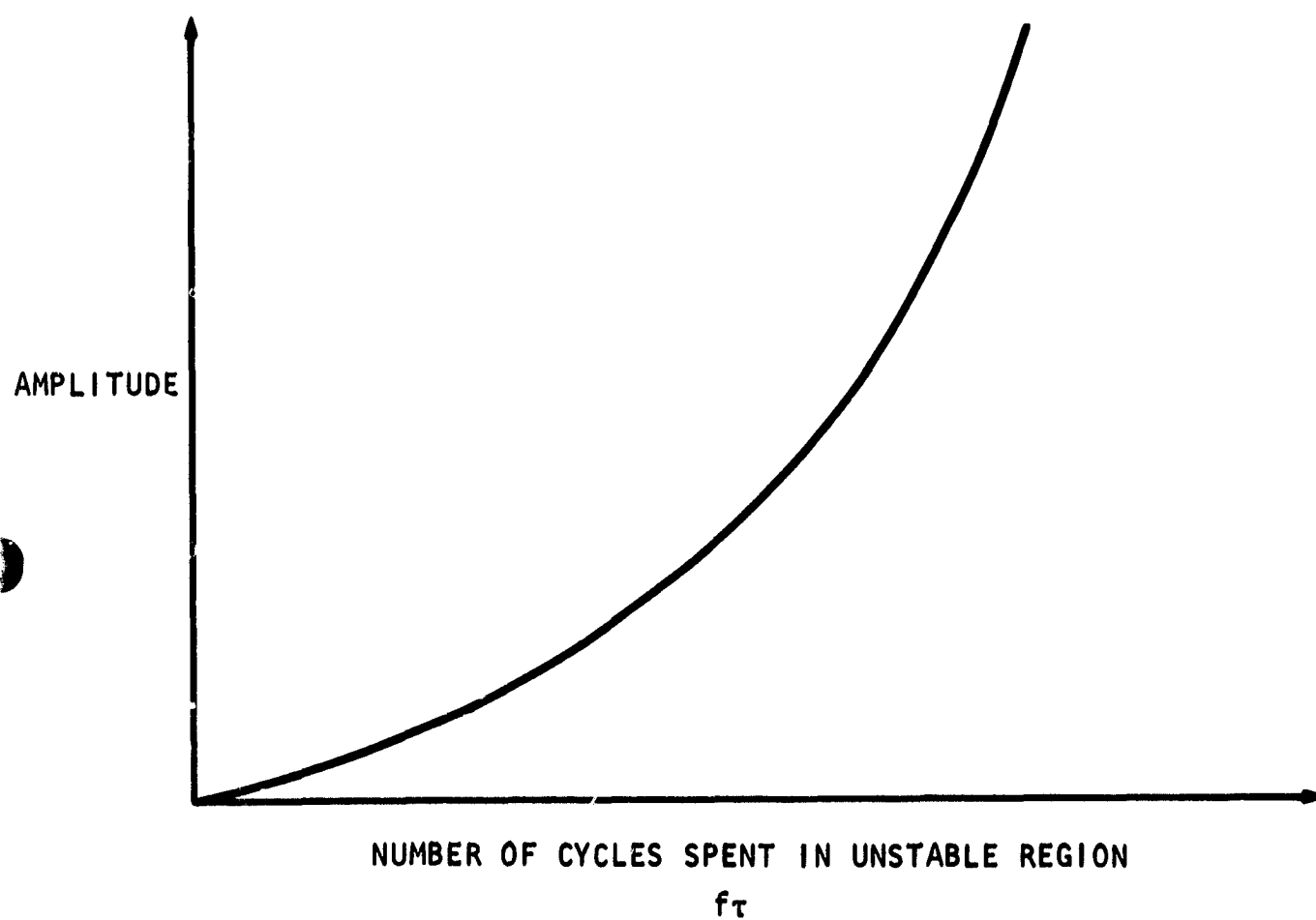


FIGURE 2. Amplitude Growth Vs. Time Spent by Ion in Unstable Region

The acceleration of an ion by the field can be expressed

$$\ddot{\bar{y}} = 0.25 (a - 0.4755q^2) \omega^2 \bar{y} \quad (1)$$

where

$\ddot{\bar{y}}$ = acceleration averaged over several cycles

a and q are the dimensionless coordinates

ω = angle of oscillation

$\bar{y}$ = mean displacement

Equation 1 can be rewritten as

$$\ddot{\bar{y}} = 0.25 \Delta a \omega^2 \bar{y} \quad (2)$$

The quantity $0.25 \Delta a \omega^2$ can be considered as a spring constant for an undamped system.

If Δa is negative there is a restoring force. If Δa is positive the amplitude of an ion will continue to grow.

Since an ion found in the fringe field will most likely be found in the unstable region of Figure 1, the maximum radial acceleration (growing amplitude) can be compared with the restoring force of the stable region once the particle enters that region

Since an ion must "travel" along the scan line whether or not it is found in the stable region, then any

$$\frac{a_1}{q_1} = \frac{a_2}{q_2} \quad (3a)$$

or

$$a_1 = \frac{a_2}{q_2} q_1 \quad (3b)$$

Since " a " can also be approximated by

$$a_1 = \frac{1}{2} q_1^2 \quad (4)$$

then

$$\frac{a_2}{q_2} q_1 - \frac{1}{2} q_1^2 = \Delta a_1 \quad (5)$$

by differentiating Δa_1 with respect to q_1

$$\frac{d(\Delta a_1)}{dq_1} = \frac{a_2}{q_2} - q_1 = 0 \quad (6a)$$

or

$$q_1 = \frac{a_2}{q_2} \quad (6b)$$

substituting 6b into 5

$$\left(\frac{a_2}{q_2}\right)^2 - \frac{1}{2} \left(\frac{a_2}{q_2}\right)^2 = \Delta a_1 = \frac{1}{2} \left(\frac{a_2}{q_2}\right)^2 \quad (7a)$$

or

$$\Delta a_1 = \frac{1}{2} \frac{a_2^2}{2a_2} = \frac{1}{4} a_2 \quad (7b)$$

Since the scan line passes very close to the apex for all resolving powers, Equation 7b can be approximated as

$$\Delta a = \frac{1}{4} a_o = 0.059 \quad (8)$$

Since this value is positive, it will cause the ion amplitude to grow continually. When this is compared to the restoring force note that it is of much higher magnitude for resolving powers higher than 4, since

$$\frac{\Delta a}{a_o} = \frac{\Delta M}{M} \quad (9a)$$

or

$$\Delta a = a_o \frac{\Delta M}{M} = \frac{1}{4} a_o \quad (9b)$$

then

$$\frac{\Delta M}{M} = \frac{1}{4} \quad (9c)$$

From the above analysis, the fringe fields appear to cause an ion to acquire a large amplitude proportional to the time it spends in this fringe region, as shown in Figure 2.

As an ion enters the quadrupole it will experience a side energy impulse which will be approximately proportional to the field strength for the first few cycles of the field before the ion can be "normalized" with the field. Since this impulse is proportional to the field strength over the first few cycles, a fringe field is desirable to minimize the impulse.

Figure 3 shows the relationship of impulse magnitude versus time length (or cycles) of the fringe field.

Showing the impulse dependence on the length of the fringe field in a quadrupole system mathematically is extremely difficult. However, analyzing a fringe field in a parallel plate configuration, which will give a result that approximates the results of a quadrupole field, is possible.

In a parallel plate geometry only ions with $n\pi$ phase to the field are stable while all other phases exhibit a constant drift term in their amplitude. In a quadrupole ac field all phases are stable but of different amplitude. In any event, parallel plate analysis will, in fact, give the relative magnitude of the drift rate of an ion in a varying field (fringe). Thus, if the drift rate is smaller in a long ramp field, it will indicate that long fringe fields impart a smaller impulse to the ions, which means improved operation of a quadrupole.

Let the field be defined by

$$E = (1 - e^{-at}) E_0 \sin (\omega t + \phi) \quad (10)$$

where

a = growth rate

t = time

E_0 = field strength

ϕ = phase of ion entry

The differential equations of motion are

$$\ddot{y} = \frac{q}{M} E_0 (1 - e^{-at}) \sin (\omega t + \phi) \quad (11)$$

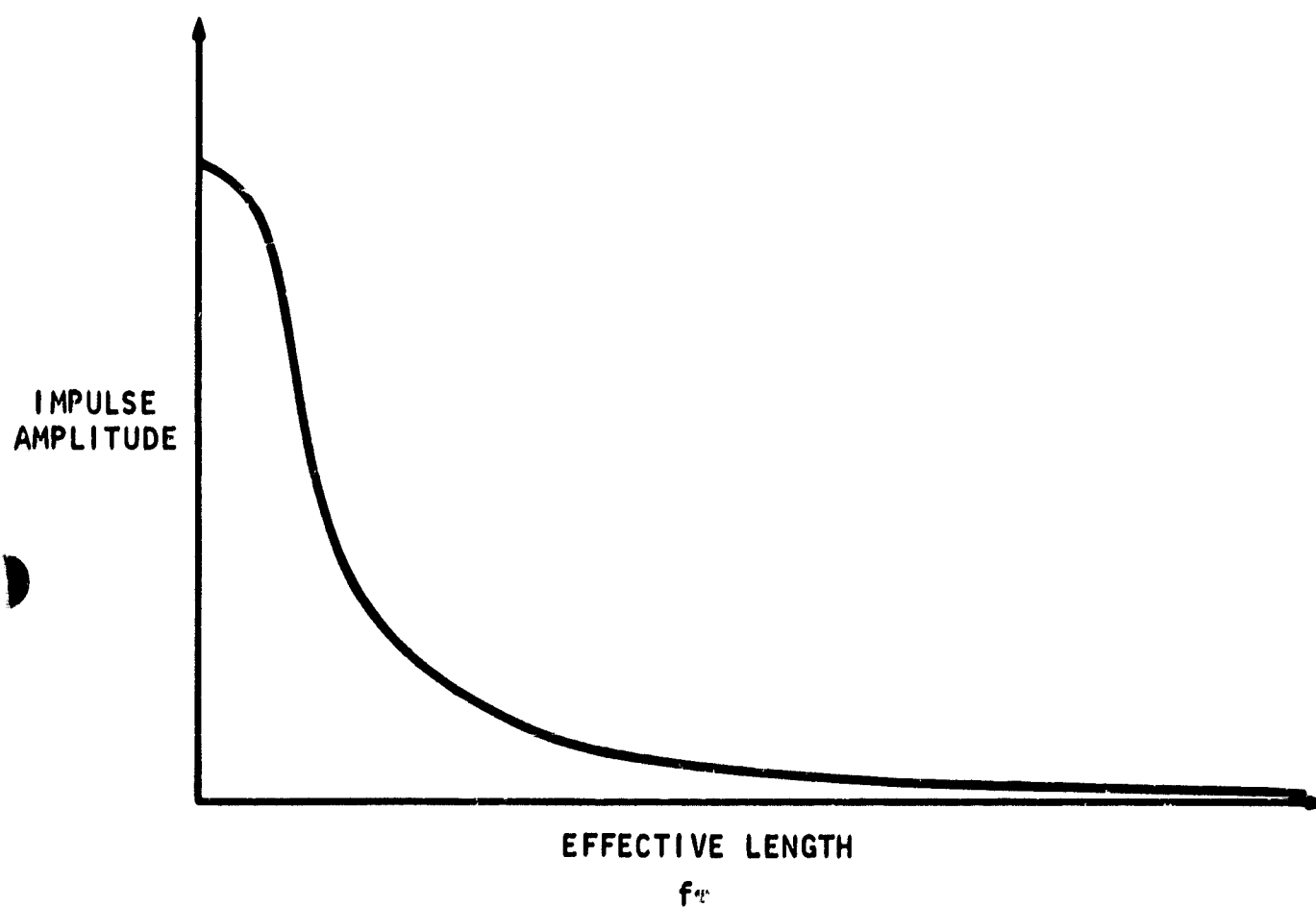


FIGURE 3. Ion Impulse Vs. Length of Fringe Field

integrating:

$$\dot{y} = \frac{q}{M} E_0 \left[-\frac{1}{\omega} \cos (\omega t + \phi) - \frac{e^{-at}}{a^2 + \omega^2} \left\{ -a \sin (\omega t + \phi) - \omega \cos (\omega t + \phi) \right\} \right] + C \quad (12)$$

solving for C at $t = 0$; $\dot{y} = \dot{y}_0$

$$C = \dot{y}_0 - \frac{q}{M} E_0 \left\{ -\frac{1}{\omega} \cos \phi + \frac{1}{a^2 + \omega^2} (a \sin \phi + \omega \cos \phi) \right\} \quad (13)$$

giving

$$\begin{aligned} \dot{y} = \frac{q}{M} E_0 \left[-\frac{1}{\omega} \cos (\omega t + \phi) + \frac{e^{-at}}{a^2 + \omega^2} \left\{ a \sin (\omega t + \phi) + \omega \cos (\omega t + \phi) \right\} \right] + \dot{y}_0 - \frac{q}{M} E_0 \left\{ -\frac{1}{\omega} \cos \phi + \frac{1}{a^2 + \omega^2} (a \sin \phi + \omega \cos \phi) \right\} \end{aligned} \quad (14)$$

Integrating again to obtain the amplitude and solving for the second constant of integration:

$$\begin{aligned} y = & \left[\dot{y}_0 - \frac{q}{M} E_0 \left\{ \frac{a \sin \phi + \omega \cos \phi}{a^2 + \omega^2} - \frac{\cos \phi}{\omega} \right\} \right] t \\ & + \frac{q}{M} E_0 \left[-\frac{\sin (\omega t + \phi)}{\omega^2} - \frac{ae^{-at}}{(a^2 + \omega^2)^2} (a \sin (\omega t + \phi) + \omega \cos (\omega t + \phi)) + \frac{\omega e^{-at}}{(a^2 + \omega^2)^2} (-a \cos (\omega t + \phi) + \omega \sin (\omega t + \phi)) \right] \\ & + y_0 - \frac{q}{M} E_0 \left[-\frac{\sin \phi}{\omega^2} - \frac{1}{(a^2 + \omega^2)^2} \right. \\ & \left. (-a^2 \sin \phi - 2a\omega \cos \phi + \omega^2 \sin \phi) \right] \end{aligned} \quad (15)$$

For the condition where $a \gg \omega$ (short ramp)

$$y = y_0 + \dot{y}_0 t - \frac{q}{M} \frac{E_0}{\omega^2} \left[\sin(\omega t + \phi) - \sin \phi \right] - \frac{q}{M} \frac{E_0}{a} \left(\sin \phi + 2 \frac{\omega}{a} \cos \phi \right) - \frac{q}{M} \frac{E_0}{\omega} \left(\frac{\omega}{a} \sin \phi - \cos \phi \right) t \quad (16)$$

The terms which have a growth rate are

$$\dot{y}_0 t - \frac{q}{M} \frac{E_0}{\omega} \left(\frac{\omega}{a} \sin \phi - \cos \phi \right) t \quad a \gg \omega \quad (17)$$

This has to be compared with the growth term with conditions of $a \ll \omega$ (long ramp)

$$y = y_0 + \dot{y}_0 t - \frac{q}{M} \frac{E_0}{\omega^2} \left[\sin(\omega t - \phi) - \sin \phi \right] + \frac{q}{M} \frac{E_0}{\omega^2} \left(\sin \phi - 2 \frac{a}{\omega} \cos \phi \right) - \frac{q}{M} \frac{E_0}{\omega^2} \text{ at } \sin \phi \quad (18)$$

The growth terms from Equation 18 are

$$\dot{y}_0 t - \left(\frac{q}{M} \frac{E_0}{\omega^2} a \sin \phi \right) t \quad a \ll \omega \quad (19)$$

In order for the impulse to be small with long ramps

$$\frac{\text{Equation 17}}{\text{Equation 19}} > 1$$

or

$$\frac{\dot{y}_0 t - \frac{q}{M} E_0 \left(\frac{1}{a} \sin \phi - \cos \phi \right) t}{\dot{y}_0 t - \frac{q}{M} E_0 \left(\frac{a}{\omega^2} \sin \phi \right) t} > |1| \quad (20)$$

Let

$$\dot{y}_0 t - \frac{q}{M} E_0 = K_1 - K_2 \quad (21)$$

then

$$\frac{k_1 - k_2 \left(\frac{1}{a} \sin \phi - \cos \phi \right) t}{k_1 - k_2 \left(\frac{a}{\omega^2} \sin \phi \right) t} \quad \begin{matrix} a \gg \omega \\ a \ll \omega \end{matrix} > |1| \quad (22a)$$

or

$$\frac{\frac{1}{a} \sin \phi - \cos \phi}{\frac{a}{\omega^2} \sin \phi} > |1| \quad (22b)$$

when $\phi \rightarrow n\pi$; $\frac{1}{a} \sin \phi - \cos \phi \rightarrow \pm 1$

and $\frac{a}{\omega^2} \sin \phi \rightarrow 0$

thus; Equation 22b $\rightarrow \pm \infty$

when $\phi \rightarrow \frac{n\pi}{2}$; $\frac{1}{a} \sin \phi - \cos \phi \rightarrow \pm \frac{1}{a}$

and $\frac{a}{\omega^2} \sin \phi \rightarrow \pm \frac{a}{\omega^2} < \frac{1}{a}$

Thus, the amplitude growth is shown to experience a smaller change due to the impulse from a long ramp field than a short one. This is the desired end result in normal quadrupole operation where the initial entrance amplitude and side energy of an ion are small. If the initial amplitude and side energy are large, then under some phases the short ramp is more beneficial than a long ramp.

Considerable effort can be spent to determine the best ramp conditions for a quadrupole with known distribution of amplitudes and entrance side energies if operating a quadrupole at maximum efficiency is desired.

For a given set of entrance conditions there apparently will be only one ramp geometry that will provide optimum results. Shortening or lengthening the fringe field ramp will deteriorate the operation of the system.

Figures 2 and 3 can be normalized and combined to determine the general shape of the ion amplitude with respect to the length of the fringe field or the field ramp shown in Figure 4 with the results shown in Figure 5.

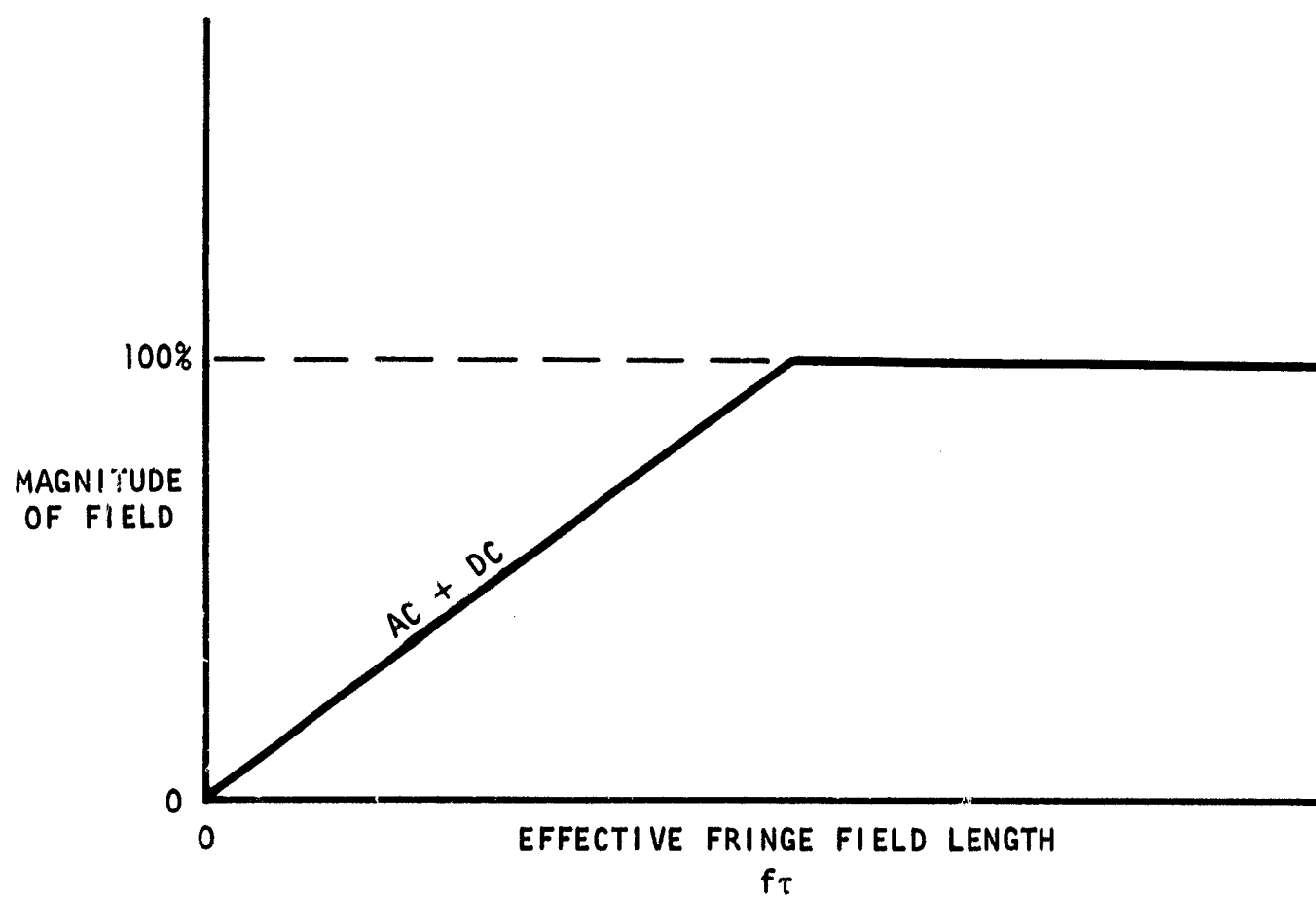


FIGURE 4. Fringe Field Ramp

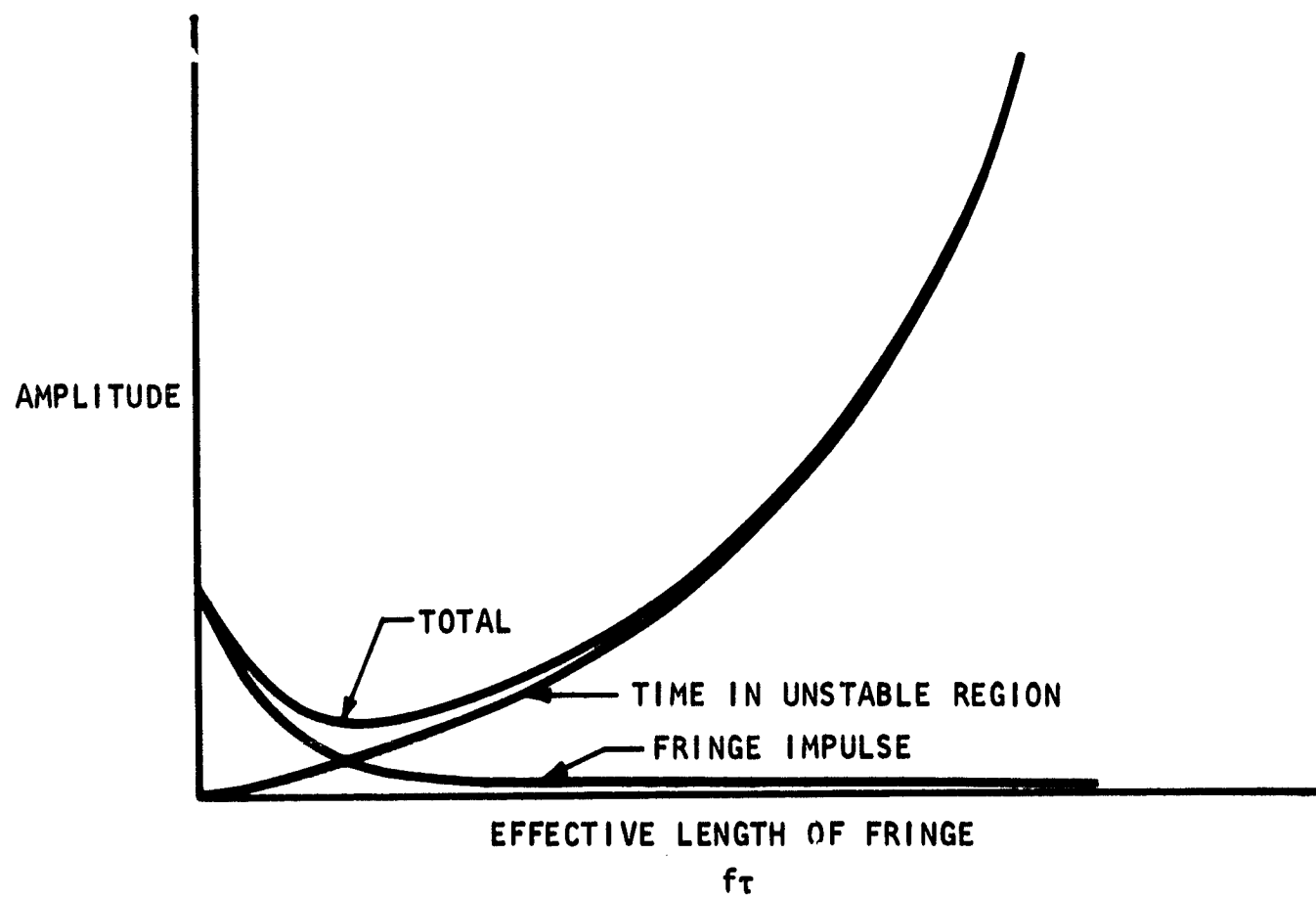


FIGURE 5. Ion Amplitude for a Given Fringe Field Length

From Figure 5 note that with a normal scan line, which passes through the unstable region, fringe fields of about one to three cycles possess minimum amplitude. Fringe fields of longer duration exhibit a fast increase of amplitude due to the exponential growth of the term which is determined by the time the ion spends in the unstable region. A large amplitude is of course detrimental to the operation of the quadrupole because ions with such large amplitudes will hit the rods and be eliminated.

Figure 5 indicates that the greater part of the ion amplitude is attributed to the time an ion spends within the unstable region. This time can be characterized by the field ramp (see Figure 4) of varying length. W. M. Brubaker¹ has shown by use of computer data that a ramp of two cycles gives a lower amplitude to ions than no ramp at all and several hundred times lower than a ramp of 10 cycles. These data confirm the general shape of Figure 5.

Examining Figure 5, the question can be asked; how can the contribution of the unstable region to the amplitude of an ion in a quadrupole be reduced? The answer appears to be very simple; the ion amplitudes will be greatly reduced if the scan line of the quadrupole can be altered so that it is found entirely within the stability region. Figure 6 shows a typical scan line versus a desired scan line of operation.

A scan line, as shown in Figure 6 (desired), is difficult to achieve and still scan many masses, but similar effect can be obtained by making the fringe fields mostly ac, delaying the dc fringe. In this way, obtaining a long ac ramp which will impart a small initial impulse to an ion as it enters the field is possible while the absence of the dc fringe field will allow all ions to be stable until the ions adjust to the field. The application of the delayed dc will not begin to filter the ions of different mass until these ions are adjusted with respect to the RF field.

This effect can be easily obtained, as Brubaker has shown, by use of segmented rods, where essentially there are two quadrupoles in tandem and the first four rods have only ac applied to them.

By use of this method, Brubaker has shown that the amplitude of ions in an ac delayed dc ramp can be reduced to about one-third the magnitude of the best ac plus dc ramp (of about two cycles).

Such a large reduction of amplitude of course means higher sensitivity of the quadrupole at a given resolution.

Use of segmented rod geometry, however makes the quadrupole excessively long for the type of applications in which ASD is involved.

¹"A Study of the Introduction of Ions into the Region of Strong Fields Within a Quadrupole Mass Spectrometer", W.M. Brubaker, 1967 Final Report, Contract NASW-1298.

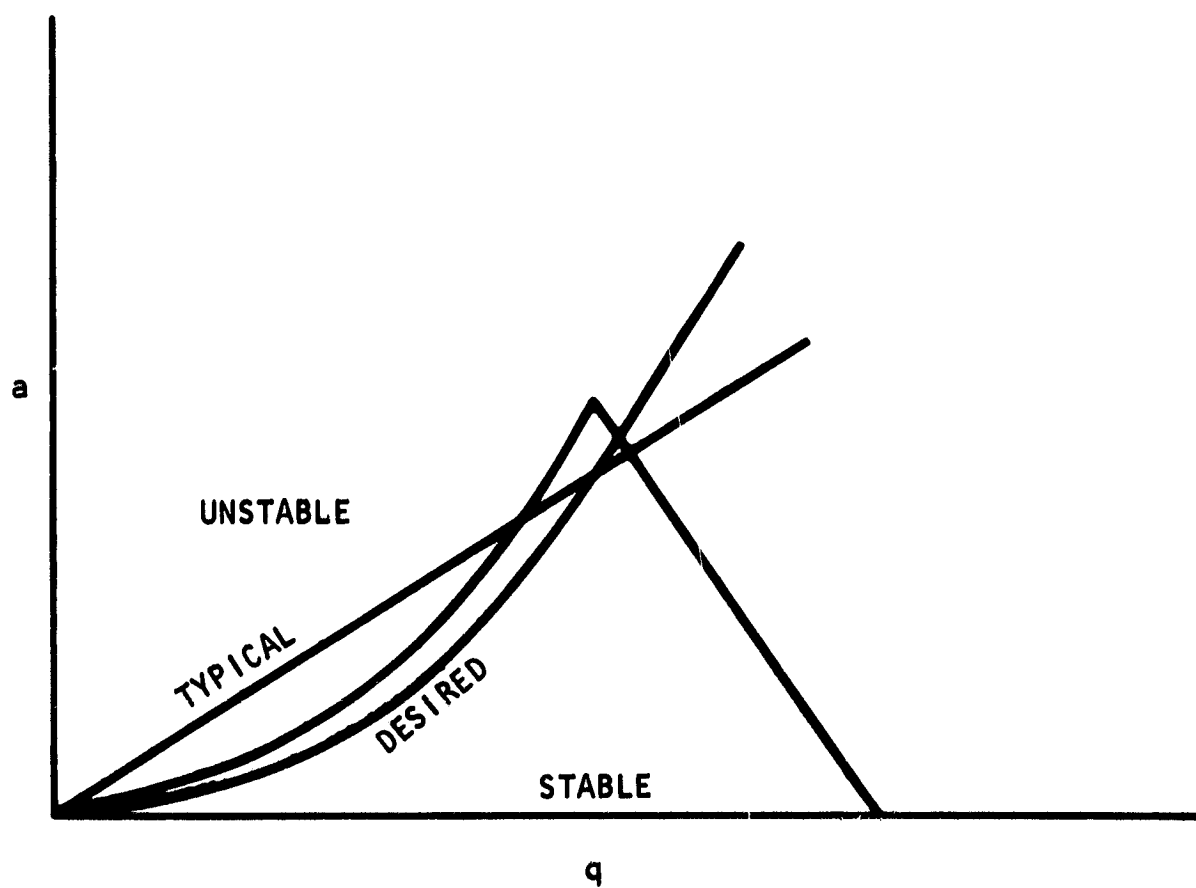


FIGURE 6. Typical Vs. Desired Scan Line

ASD also utilizes high energy ions and quadrupole bias. An ion with high energy quickly passes through the fringe field; thus, remaining in the unstable region for a very short time. The application of quadrupole bias then slow the ions down so that these ions will spend sufficient time within the quadrupole to be adequately filtered.

The end result of high energy ions with quadrupole bias is to achieve a minimum amplitude of ions with minimum length and weight of the quadrupole. The amplitude of the ions in the ASD method is not considered much higher than a factor of two to three higher than that obtained with segmented rods, since the operating point is in the valley of the curve in Figure 5. Thus, the sensitivities of the two approaches may be considered comparable in light of the length and weight considerations.

COMPUTER ANALYSIS

All of the mathematical analysis of the fringe field ramps was done with fields of parallel plates and then the assumption was made that the results could be applied to quadrupole fields. Brubaker has done considerable computer work of ion trajectories in segmented quadrupole fields, but it was felt that additional data was required to determine the optimum ramp characteristics for any ASD applications which could utilize segmented rod geometry.

The first approach undertaken was to determine the mathematics for a hyperbolic ramp and write a computer program to analyze ion trajectories in such fields. The results were of such complexity that it would have required considerable time and effort to obtain a final amplitude of the ions.

The most reasonable approach appeared to be one of utilizing our existing computer programs for ion trajectories in quadrupoles modified to contain a fringe field ramp, then use the identical initial conditions which Brubaker used and compare the end results with those of Brubaker.

To accomplish this, it was necessary to break the program into two subroutines. The first part was the ramp section, where the computer determined the trajectory of the ion in a continually varying a and q parameters according to the field variations of the ramp. The computer would then determine the exit conditions of the ramp, such as amplitude, angle and phase, and use these conditions as the entry conditions for the second subroutine where the fields were constant.

The resultant amplitudes were compared with those given in Reference 1 at approximately the same number of cycles down the z -axis and were found to be, in all cases, larger than those obtained by Brubaker. This was true for both y and x axes.

As a further check, several phases were run and also a comparison was made with a no ramp condition. Again, the amplitude obtained with a ramp was higher than with no ramp. The data for both ramp and no ramp conditions is shown in Appendix A.

The results of this computer analysis indicated that there is perhaps some subtle error in the approach, taken here, in manipulating the ramp of the fields. Examining the computer program and method did not appear to shed any light on the matter. Therefore, ASD felt that no additional runs could provide reliable conclusions, unless considerable time and effort were spent on this problem.

SUMMARY

Theoretical analysis indicates that correct manipulation of the entrance fringe fields could be very beneficial in the operation of a quadrupole mass spectrometer. This manipulation can take the form of an ac delayed dc ramp as in the segmented rod approach, or an ac plus dc ramp as in the biasing of the quadrupole approach taken by ASD. Segmented rod geometry appears to give higher intensity for a given set of conditions, but quadrupole bias has an edge on length and weight conditions. The computer data obtained by ASD can only be termed inconclusive with considerable more effort required to correct and complete.

APPENDIX A

Computer data for various conditions.

1. Different Ramps
2. Different a and q Values
3. Different Phases
4. No Ramp

Figure 7 shows the relative maximum amplitudes of the ion trajectories computed herein.

ANALYSIS I

a = .2346200; q = .7048200
 .2330000 .7060000
 ac ramp 0° to 4320°

dc ramp 2160° to 4320°

$\gamma = 0$

$\eta = 0.010$

$\phi = 0^\circ$

Also compared with no ramp condition

X - RODS RAMP #1

Segmented rod transmission analysis. Enter a and q, dc and ac ramp entrances, and exits. ? .23462, .70432, 2160, , 4320, 4320, . Enter initial phase

?

A = .23462000 Q = .70482000

DC Ramp

Entrance = 2160 Exit = 4320

AC Ramp

Entrance = 0 Exit = 4320

X-Axis Analysis

Enter ETA and GAMMA

? .01,

X-ETA = .0100 X-GAMMA = .00000

Initial Phase = 0

PHASE	AMP
134	.0100
358	.0104
530	.0100
715	.0107
900	.0097
1070	.0107
1271	.0090
1422	.0099
1649	.0075
1768	.0079
2897	-.0053
3068	-.0040
3209	-.0048
3949	.0053

Phase Distance = 4320 Phase Angle = 360
 X-ETAF = -.0019 X-GAMMAF = -.00230

Ramp exit conditions

Y-RODS RAMP #2

Y-Axis Analysis

Enter ETA and GAMMA

7.01,

Y-ETA = .0100 Y-GAMMA = .00000

Initial Phase = 0

A = .2346200

Q = .7048200

PHASE	AMF
-------	-----

134	.0100
362	.0096
525	.0100
726	.0091
886	.0097
1093	.0084
1241	.0090
1467	.0071
1589	.0075
1867	.0048
1912	.0048
2769	-.0040
2802	-.0040
3084	-.0083
3204	-.0074
3438	-.0140
3568	-.0119
3798	-.0236
3925	-.0199
4159	-.0429
4282	-.0362

Phase Distance = 4320 Phase Angle = 360

Y-ETAF = -.0382 Y-GAMMAF = -.02092

Ramp exit conditions

X-RODS Second Segment #1A

Quadrupole Trajectory Maxima

Enter A, Q, ETA, GAMA, I PHASE, X and or Y
?.23462,.70482,-.0019,-.0023,0,X

A = .23462000 Q = .70482000 GAMMA = -.00230

X-Axis Analysis

PHASE	AMP	PHASE	AMP	
0	-.0019	10077	-.0230	
51	-.0022	10438	.0268	
154	-.0019	10798	-.0302	
331	-.0034	11159	.0329	
709	.0084	11519	-.0351	
1073	-.0133	11879	.0366	
1435	.0180	12240	-.0373	
1797	-.0223	12600	.0374	
2157	.0262	12960	-.0368	
2518	-.0296	13321	.0355	
2879	.0325	13681	-.0335	
3239	-.0348	14042	.0309	
3599	.0364	14402	-.0277	
3960	-.0373	14763	.0239	
4320	.0375	15124	-.0198	
4680	-.0370	15486	.0152	
5041	.0358	15849	-.0104	
5401	-.0339	16001	-.0028	.0101 final
5762	.0314	16001	-.0028	.0101 conditions
6122	-.0282			
6483	.0246			
6844	-.0205			
7205	.0160			
7568	-.0112			
7935	.0063			
8617	-.0042			
8990	.0092			
9354	-.0141			
9716	.0187			

1600° = 44.4 Cycles = Length of Quadrupole
(for mass 50 with 10 ev energy)

Y-RODS Second Segment 2A

Quadrupole Trajectory Maxima

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y

?.23462,.70482,-.0382,-.02092,,Y

A = .23462000 Q = .70482000 GAMA = -.02092

Y-AXIS Analysis

PHASE	AMP	PHASE	AMP	PHASE	AMP
0	-.0382	6871	-.0290	14216	.1297
186	-.0973	7004	-.0398	14416	.0541
346	-.0584	7753	.0486	14573	.0887
544	-.1378	7894	.0336	14787	.0324
710	-.0784	8107	.0911	14926	.0461
903	-.1756	8265	.0553	15675	-.0422
1073	-.0967	8464	.1320	15811	-.0303
1262	-.2098	8630	.0755	16001	-.0824 -.0373
1435	-.1130	8823	.1702	16001	-.0824 -.0373
1622	-.2399	8992	.0941		
1796	-.1270	9182	.2050		
1981	-.2651	9354	.1108		
2157	-.1385	9542	.2357		
2341	-.2850	9716	.1251		
2518	-.1471	9901	.2617		
2701	-.2992	10077	.1370		
2879	-.1528	10261	.2825		
3060	-.3074	10438	.1460		
3240	-.1553	10621	.2975		
3420	-.3095	10799	.1521		
3601	-.1548	10980	.3066		
3780	-.3052	11160	.1552		
3961	-.1511	11340	.3095		
4139	-.2949	11520	.1551		
4322	-.1444	11700	.3063		
4499	-.2787	11881	.1519		
4683	-.1348	12059	.2968		
4859	-.2568	12242	.1456		
5044	-.1224	12419	.2814		
5218	-.2298	12603	.1364		
5406	-.1075	12779	.2604		
5578	-.1982	12964	.1244		
5768	-.0905	13138	.2341		
5937	-.1626	13326	.1099		
6131	-.0715	13498	.2031		
6295	-.1238	13688	.0931		
6497	-.0510	13857	.1681		
6653	-.0825	14051	.0744		

Final conditions

X-RODS RAMP #3

Segmented Rod Transmission Analysis

A = .2330000 Q = .70600000
DC RAMP
Entrance = 2160 Exit = 4320
AC RAMP
Entrance = 0 Exit = 4320

X_AXIS Analysis

Enter ETA and GAMMA

?.01,,

X-ETA = .0100 X-GAMMA = .00000

Initial Phase = 0

PHASE	AMP
134	.0100
358	.0104
530	.0100
715	.0107
900	.0097
1070	.0107
1272	.0090
1422	.0099
1649	.0075
1768	.0079
2897	-.0053
3068	-.0040
3209	-.0048
3949	.0053

Phase Distance = 4320 Phase Angle = 360

Ramp exit conditions

X-ETAF = -.0019 X-GAMMAF = -.00230

Y-RODS RAMP #4

Y-AXIS Analysis

A = .2330000

Enter ETA and GAMMA

Q = .7060000

? .01,

Y-ETA = .0100 Y-GAMMA = .00000

Initial Phase = 0

PHASE	AMP
-------	-----

134	.0100
362	.0096
525	.0100
726	.0091
886	.0097
1093	.0084
1241	.0090
1467	.0070
1589	.0075
1868	.0048
1912	.0048
2767	-.0040
2804	-.0040
3084	-.0083
3204	-.0074
3438	-.0139
3568	-.0118
3797	-.0233
3926	-.0196
4158	-.0420
4283	-.0353

Phase Distance = 4320 Phase Angle - 360

Ramp exit conditions

Y-ETAF = -.0371 Y-GAMMAF = -.02001

To enter quadrupole without ramp type GO

?GO

Enter quadrupole length.

Enter Inputs?

?16000,YES

X-RODS Second Segment 3A

Quadrupole Trajectory Maxima

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y

? .233, .706, -.0019, -.0023, X+, X

A = .23300000 Q = .70600000 GAMMA = -.00230

X-AXIS Analysis

PHASE	AMP	PHASE	AMP	
0	-.0019	8629	-.0082	
51	-.0022	8993	.0131	
154	-.0019	9355	-.0178	
331	-.0034	9717	.0221	
709	.0084	10077	-.0260	
1073	-.0134	10438	.0293	
1435	.0180	10799	-.0321	
1797	-.0223	11159	.0342	
2157	.0261	11519	-.0356	
2518	-.0295	11880	.0363	
2879	.0322	12240	-.0362	
3239	-.0343	12601	.0355	
3599	.0356	12961	-.0340	
3960	-.0363	13321	.0318	
4320	.0362	13682	-.0290	
4681	-.0354	14043	.0256	
5041	.0339	14404	-.0216	
5401	-.0317	14765	.0173	
5762	.0288	15127	-.0126	
6123	-.0254	15492	.0076	
6484	.0214	15879	-.0027	
6845	-.0170	16001	-.0019	.0005
7207	.0123	16001	-.0019	.0005
7573	-.0074			
7964	.0024			
8085	.0019			
8248	.0032			

Final conditions

Y-RODS Second Segment 4A

Quadrupole Trajectory Maxima

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y

?.233,.706,-.0371,-.02001,,Y

A = .23300000 Q = .70600000 GAMMA = -.02001

Y-AXIS Analysis

PHASE	AMP	PHASE	AMP	PHASE	AMP
0	-.0371	5751	.0712	11517	-.0932
186	-.0941	5942	.1570	11701	-.1923
347	-.0558	6115	.0847	11879	-.0982
544	-.1301	6301	.1796	12060	-.1974
712	-.0727	6477	.0939	12241	-.0983
902	-.1596	6661	.1932	12419	-.1927
1075	-.0858	6839	.0984	12603	-.0935
1261	-.1813	7020	.1974	12779	-.1785
1437	-.0946	7201	.0980	12966	-.0840
1621	-.1941	7379	.1917	13138	-.1555
1799	-.0986	7563	.0928	13329	-.0703
1980	-.1972	7738	.1766	13496	-.1248
2161	-.0977	7926	.0828	13694	-.0529
2339	-.1906	8097	.1528	13854	-.0880
2524	-.0920	8289	.0687	14066	-.0325
2698	-.1746	8456	.1214	14207	-.0470
2886	-.0816	8655	.0510	14955	.0410
3057	-.1500	8813	.0841	15091	.0295
3250	-.0671	9028	.0304	15307	.0825
3416	-.1180	9166	.0428	15465	.0502
3616	-.0491	9914	-.0452	15664	.1200
3773	-.0802	10053	-.0316	15831	.0680
3991	-.0282	10267	-.0864	16001	.1485
4124	-.0386	10425	-.0521	16001	.1485
4862	.0494	10624	-.1234		
5015	.0338	10791	-.0696		
5226	.0903	10983	-.1544		
5386	.0540	11154	-.0835		
5584	.1268	11342	-.1777		

Final conditions

NO RAMP #5 (See #1 and 1A)

Quadrupole Trajectory Maxima

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y
?.23462,.70482,.01,,0,XY

A = .23462000 Q = .70482000 GAMMA = .00000

X AXIS Analysis

PHASE	AMP	PHASE	AMP
0	.0100	10082	-.0076
360	-.0099	10443	.0066
721	.0096	10704	-.0055
1081	-.0092	11165	.0043
1442	.0085	11528	-.0031
1802	-.0077	11895	.0017
2163	.0068	12325	-.0005
2524	-.0057	12354	-.0005
2885	.0045	12575	-.0011
3247	-.0033	12950	.0024
3613	.0020	13314	-.0037
4005	-.0006	13676	.0049
4124	-.0005	14037	-.0061
4288	-.0009	14397	.0071
4669	.0022	14758	-.0080
5033	-.0035	15119	.0088
5395	.0047	15479	-.0093
5757	-.0059	15839	.0097
6117	.0070	16200	-.0100
6478	-.0079	16560	.0100
6839	.0086	16920	-.0098
7199	-.0093	17281	.0095
7559	.0097	17641	-.0090
7920	-.0099	18002	.0083
8280	.0100	18362	-.0074
8640	-.0099	18723	.0064
9001	.0096	19084	-.0053
9361	-.0091	19446	.0041
9722	.0084	19809	-.0028
		20177	.0015
		20321	.0006

Max here ~ .01

Second Seg. Max (above) ~ .03 Amplitude

NO RAMP # 6 (See 2 and 2A)

A = .23462000 Q = .70482000 GAMMA = .00000

Y-AXIS Analysis

PHASE	AMP	PHASE	AMP	PHASE	AMP
0	.0100	6837	-.0090	13673	.0063
180	.0199	7021	-.0185	13862	.0136
361	.0099	7198	-.0095	14035	.0073
540	.0195	7380	-.0194	14222	.0155
722	.0096	7559	-.0099	14396	.0082
899	.0187	7740	-.0198	14581	.0171
1083	.0091	7920	-.0100	14757	.0089
1259	.0175	8100	-.0199	14941	.0184
1444	.0084	8281	-.0099	15118	.0095
1618	.0160	8460	-.0195	15301	.0193
1805	.0076	8642	-.0097	15479	.0098
1978	.0142	8819	-.0188	15660	.0198
2167	.0066	9002	-.0092	15840	.0100
2337	.0120	9179	-.0177	16020	.0199
2529	.0054	9363	-.0085	16201	.0100
2696	.0097	9539	-.0162	16380	.0196
2892	.0042	9725	-.0077	16561	.0097
3055	.0071	9898	-.0144	16739	.0189
3260	.0028	10086	-.0067	16922	.0093
3411	.0044	10257	-.0124	17099	.0179
3643	.0014	10448	-.0056	17283	.0086
3755	.0017	10617	-.0100	17459	.0165
4175	-.0013	10812	-.0044	17645	.0078
4266	-.0011	10975	-.0075	17818	.0147
4510	-.0040	11178	-.0030	18006	.0069
4659	-.0026	11332	-.0048	18178	.0127
4866	-.0067	11557	-.0016	18368	.0058
5027	-.0040	11680	-.0021	18537	.0104
5224	-.0093	12120	.0009	18731	.0046
5391	-.0053	12161	.0009	18895	.0079
5583	-.0117	12431	.0036	19097	.0032
5753	-.0064	12577	.0024	19253	.0052
5942	-.0139	12786	.0063	19472	.0018
6115	-.0074	12946	.0038	19603	.0025
6302	-.0157	13144	.0089	20321	-.0031
6476	-.0083	13310	.0051		
6661	-.0173	13503	.0114		

2nd Seg.
 Max ~ .1

Max ~ .3 with 2nd segment

X-RODS NO RAMP #7 (See 3 and 3A)

Quadrupole Trajectory Maxima

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y

A = .23300000 Q = .70600000 GAMMA = .00000

X-AXIS Analysis

PHASE	AMP	PHASE	AMP
0	.0100	10806	-.0043
360	-.0099	11169	.0029
721	.0096	11537	-.0016
1081	-.0091	12220	.0013
1442	.0084	12591	-.0027
1802	-.0076	12954	.0041
2163	.0066	13316	-.0053
2524	-.0054	13677	.0065
2886	.0042	14038	-.0075
3249	-.0029	14398	.0083
3618	.0015	14759	-.0090
4301	-.0014	15119	.0096
4671	.0028	15480	-.0099
5034	-.0041	15840	.0100
5396	.0054	16200	-.0099
5757	-.0065	16561	.0096
6118	.0075	16921	-.0092
6478	-.0084	17282	.0085
6839	.0091	17642	-.0077
7199	-.0096	18003	.0067
7560	.0099	18364	-.0056
7920	-.0100	18725	.0043
8280	.0099	19088	-.0030
8641	-.0096	19456	.0016
9001	.0091	20139	-.0013
9362	-.0085	20321	.0003
9722	.0076		
10083	-.0066		
10444	.0055		

End of Ramp Above ~ .002

Second Rod Max ~ .035

.0022

Y-RODS NO RAMP #8 (See 4 and 4A)

A = .23300000 Q = .70600000 GAMMA = .00000

Y-AXIS Analysis

PHASE	AMP	PHASE	AMP	PHASE	AMP
0	.0100	7358	-.0029	14941	-.0197
180	.0198	7783	.0017	15119	-.0100
362	.0098	7857	.0016	15300	-.0199
539	.0189	8110	.0060	15481	-.0099
724	.0090	8259	.0039	15659	-.0192
898	.0169	8465	.0100	15844	-.0093
1087	.0078	8628	.0059	16018	-.0176
1257	.0142	8823	.0136	16206	-.0082
1451	.0062	8992	.0075	16377	-.0151
1615	.0108	9182	.0165	16570	-.0067
1819	.0043	9355	.0088	16736	-.0188
1971	.0068	9541	.0186	16936	-.0049
2204	.0021	9718	.0096	17093	-.0080
2314	.0025	9900	.0197	17312	-.0028
2733	-.0021	10080	.0100	17443	-.0038
2829	-.0018	10260	.0199	18192	.0051
3069	-.0064	10442	.0098	18335	.0035
3220	-.0041	10619	.0191	18546	.0092
3425	-.0104	10804	.0092	18706	.0055
3588	-.0061	10978	.0174	18904	.0129
3783	-.0139	11167	.0081	19071	.0072
3952	-.0077	1137	.0148	19262	.0160
4142	-.0167	11530	.0066	19435	.0086
4315	-.0089	11695	.0115	19621	.0182
4501	-.0187	11897	.0047	19797	.0095
4678	-.0097	12052	.0076	19981	.0196
4860	-.0198	12275	.0026	20159	.0100
5040	-.0100	12401	.0034	20321	.0196
5220	-.0199	12853	-.0013		.0064
5402	-.0098	12868	-.0013		
5579	-.0190	13151	-.0055		
5764	-.0091	13297	-.0037		
5938	-.0172	13506	-.0096		
6127	-.0080	13667	-.0057		
6297	-.0145	13864	-.0132		
6491	-.0064	14032	-.0074		
6655	-.0111	14222	-.0162		
6858	-.0045	14395	-.0087		
7012	-.0072	14581	-.0184		
7239	-.0023	14757	-.0096		

ANALYSIS II

a = .233000; q = .70600

ac ramp 0° to 4320°

γ = .01

η .01

ϕ 0°

Also compared with no ramp condition.

X-RAMP #1

Segmented Rod Transmission Analysis

Enter A and Q, DC and AC Ramp Entrances, and Exits

?.233,.706,2160,,4320,4320,

Enter Initial Phase

?0,

A = .23300000 Q = .70600000

DC RAMP

Entrance = 2160 Exit = 4320 (Delayed

AC RAMP

Entrance = 0 Exit = 4320

X-AXIS Analysis 1

Enter ETA and GAMMA

?.01,.01,

X-ETA = .0100 X-GAMMA = .01000 (Initial)

Initial Phase = 0

PHASE	AMP
-------	-----

1111	.0688
------	-------

1228	.0661
------	-------

1449	.0832
------	-------

1613	.0729
------	-------

1795	.0880
------	-------

1995	.0675
------	-------

2139	.0766
------	-------

3241	-.0605
------	--------

3974	.0525
------	-------

Phase Distance = 4320 Phase Angle = 360 ϕ

X-ETAF = η .0226 X-GAMMAF = -.02557 γ

Y-AXIS Analysis 1A

Enter ETA and GAMMA

A = 233000

? .01, .01,

Q = 706000

Y-ETA = .0100 Y-GAMMA = .01000

Initial Phase = 0

PHASE	AMP
-------	-----

953	.0589
1026	.0584
1278	.0753
1422	.0693
1621	.0855
1803	.0706
1967	.0830
2191	.0575
2308	.0621
3452	-.0573
3553	-.0529
3801	-.1161
3922	-.1004
4159	-.2221
4282	-.1883

Phase Distance = 4320 Phase Angle = 360 ϕ

Y-ETA η = -.1987 Y-GAMMA γ = -.10983

SHORT X-ROD #2

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y

A = .23300000 Q = .70600000 GAMMA = -.02557 Derived η and γ

X-AXIS Analysis

PHASE	AMP	
4320	.0226	
4667	-.0805	
5033	.1356	
5395	-.1881	
5756	.2369	
6117	-.2809	
6478	.3193	
6839	-.3512	
7199	.3761	
7559	-.3932	
7920	.4025	
8280	-.4036	
8641	.3965	
9001	-.3814	
9361	.3586	
9722	-.3285	
10083	.2918	
10443	-.2492	
10805	.2015	
11167	-.1499	
11531	.0954	
11908	-.0397	
12092	-.0206	
12184	-.0231	
12586	.0776	
12952	-.1327	
13315	.1854	
13676	-.2345	
14037	.2788	
14398	-.3175	
14758	.3497	
15119	-.3749	
15479	.3925	
15840	-.4022	
16001	-.0470	.4881
16001	-.0470	.4881

LONG X-ROD #3

Quadrupole Trajectory Maxima

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y
?.233,.706,.0226,-.02557,X<-<+,X

A = .23300000 Q = .70600000 GAMMA = -.02557

X-AXIS Analysis

PHASE	AMP	PHASE	AMP
0	.0226	8266	.0776
347	-.0805	8632	-.1327
713	.1356	8995	.1854
1075	-.1881	9356	-.2345
1436	.2369	9717	.2788
1797	-.2809	10078	-.3175
2158	.3193	10438	.3497
2519	-.3512	10799	-.3749
2879	.3761	11159	.3925
3239	-.3932	11520	-.4022
3600	.4025	11880	.4037
3960	-.4036	12240	-.3971
4321	.3965	12601	.3824
4681	-.3814	12961	-.3599
5041	.3586	13322	.3303
5402	-.3285	13682	-.2939
5763	.2918	14043	.2515
6123	-.2492	14404	-.2041
6485	.2015	14766	.1527
6847	-.1499	15131	-.0983
7211	.0954	15506	.0426
7588	-.0397	15707	.0199
7772	-.0206	15772	.0207
7864	-.0231	16001	-.0164
		16001	-.0164

←End of short rod

-.0478
-.0478

Quadrupole Trajectory Maxima #4

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y
?.233,.706,.0226,-.02557,4320,X

A = .23300000 Q = .70600000 GAMMA = -.02557

X-AXIS Analysis

PHASE	AMP	PHASE	AMP
4320	.0226	12586	.0776
4667	-.0805	12952	-.1327
5033	.1356	13315	.1854
5395	-.1881	13676	-.2345
5756	.2369	14037	.2788
6117	-.2809	14398	-.3175
6478	.3193	14758	.3497
6839	-.3512	15119	-.3749
7199	.3761	15479	.3925
7559	-.3932 See	15840	-.4022
7920	.4025 Long	16200	.4037
8280	-.4036 X-Rod	16560	-.3971
8641	.3965 Above	16921	.3824
9001	-.3814	17281	-.3599
9361	.3586	17642	.3303
9722	.3285	18002	-.2939
10083	.2918 -.0021	18363	.2515
10443	-.2492	18724	-.2041
10805	.2015	19086	.1527
11167	-.1499	19451	-.0983
11531	.0954	19826	.0426
11908	-.0397	20027	.0199
12092	-.0206	20092	.0207
12184	-.0231	20321	-.0164
		20321	-.0164

(Off-set of phase on long rod)

-.0478
-.0478

NO RAMP COMPARISON #5

Quadrupole Trajectory Maxima

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y
?.233,.706,.01,.01,0,XY

A = .23300000 Q = .70600000 GAMMA = .01000

X-AXIS Analysis

PHASE	AMP	PHASE	AMP
0	.0100	10438	-.1264
42	.0111	10799	.1386
170	.0084	11159	-.1480
327	.0134	11519	.1544
708	-.0351	11880	-.1577
1073	.0565	12240	.1577
1435	-.0768	12601	-.1546
1797	.0956	12961	.1484
2157	-.1125	13321	-.1391
2518	.1271	13682	.1271
2879	-.1392	14043	-.1124
3239	.1484	14403	.0955
3599	-.1547	14765	-.0767
3960	.1578	15127	.0563
4320	-.1577	15492	-.0349
4681	.1544	15874	.0132
5041	-.1480	16029	.0084
5401	.1386	16159	.0112
5762	-.1264	16547	-.0328
6123	.1116	16913	.0543
6484	-.0946	17275	-.0747
6845	.0757	17636	.0937
7207	-.0552	17997	-.1109
7572	.0311	18358	.1257
7957	-.0121	18719	-.1381
8099	-.0084	19079	.1476
8243	-.0123	19439	-.1542
8628	.0339	19800	.1576
8993	-.0554	20160	-.1578
9355	.0758	20321	-.0196
9716	-.0947		
10077	.1117		

Max here is ~1/3
max of second
segment

.1898

Quadrupole Trajectory Maxima

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y
?.233,.706,-.1987,-.10983,4320,Y

A = .23300000 Q = .70600000 GAMMA = -.10983

Y-AXIS Analysis #2A

PHASE	AMP	
4320	-.1987	
4506	-.5067	
4667	-.3016	See Y-Rod Above
4864	-.7046	
5032	-.3944	
5222	-.8678	
5395	-.4669	
5581	-.9883	
5757	-.5159	
5941	-1.0599	
20321	-1.0599	-.0478
23021	-1.0599	-.0478

Y-ROD (LONG) Calculated Values From Above

Quadrupole Trajectory Maxima

Enter A,Q,ETA,GAMA,I PHASE, X and/or Y
?.233,.706,-.1987,-.10983,0,Y

A = .23300000 Q = .70600000 GAMMA = -.10983

Y-AXIS Analysis #3A

PHASE	AMP	
0	-.1987	
186	-.5067	
347	-.3016	
544	-.7046	
712	-.3944	
902	-.8678	
1075	-.4669	
1261	-.9883	
1437	-.5159	
1621	-1.0599	
16001	-1.0599	-.0478
16001	-1.0599	-.0478

Y-ROD NO RAMP #5A

A = .23300000 Q = .70600000 GAMMA = .01000

Y-AXIS Analysis

PHASE	AMP	PHASE	AMP	PHASE	AMP
0	.0100	6838	-.0452	14213	.0372
189	.0301	7020	-.0925	14432	.0129
340	.0194	7200	-.0468	14563	.0175
545	.0489	7380	-.0934	15312	-.0243
708	.0285	7562	-.0461	15456	-.0164
903	.0653	7739	-.0896	15666	-.0436
1073	.0361	7924	-.0430	15826	-.0260
1262	.0785	8098	-.0814	16024	-.0608
1435	.0419	8287	-.0378	16191	-.0340
1621	.0878	8457	-.0692	16382	-.0750
1798	.0455	8650	-.0307	16555	-.0404
1980	.0928	8815	-.0536	16741	-.0855
2160	.0469	9017	-.0220	16917	-.0447
2340	.0932	9172	-.0353	17101	-.0918
2522	.0459	9396	-.0118	17279	-.0467
2699	.0890	9521	-.0155	17460	-.0936
2884	.0426	9964	.0063	17641	-.0464
3058	.0804	9997	.0063	17819	-.0907
3247	.0372	10271	.0262	18003	-.0438
3417	.0678	10417	.0174	18178	-.0834
3611	.0299	10626	.0454	18366	-.0390
3775	.0519	10787	.0268	18537	-.0719
3978	.0210	10984	.0623	18730	-.0323
4132	.0334	11152	.0347	18896	-.0569
End of above ramp.		11342	.0762	19095	-.0238
Max ~0.22 with ramp		11515	.0409	19252	-.0391
(hits rods with ramp)		11701	.0863	19469	-.0140
4360	.0108	11877	.0450	19605	-.0194
4477	.0135	12061	.0922	20321	.0213
4901	-.0081	12239	.0468		.0120
4979	-.0076	12420	.0935		
5230	-.0282	12601	.0463		
5379	-.0184	12779	.0902		
5585	-.0472	12964	.0434		
5748	-.0277	13138	.0824		
5943	-.0638	13326	.0384		
6112	-.0354	13497	.0706		
6302	-.0774	13690	.0315		
6475	-.0414	13856	.0552		
6661	-.0871	14056	.0229		

ANALYSIS III

a = .2346200; q = .7048200

ac ramp 0° to 4320°

dc ramp 2160° to 4320° and 2160° to 6480°

γ = 0; .01

η = .01

ϕ = 0°; 90°

Compare with Analysis I

Segmented Rod Transmission Analysis

Enter A and Q, DC and AC Ramp Entrances, and Exits

?.23462,.70482,2160,4320←←←,4320,4320,

Enter Initial Phase

?0,

A = .23462000 Q = .70482000

DC RAMP

Entrance = 2160 Exit = 4320

AC RAMP

Entrance = 0 Exit = 4320

X-AXIS ANALYSIS - DC DELAYED #1

Enter ETA and GAMMA

?.01,,

X-ETA = .0100 X-GAMMA = .00000 Initial

Initial Phase = 0

PHASE	AMP
134	.0100
358	.0104
530	.0100
715	.0107
900	.0097
1070	.0107
1271	.0090
1422	.0099
1649	.0075
1768	.0079
2897	-.0053
3068	-.0040
3209	-.0048
3949	.0053

Phase Distance = 4320 Phase Angle = 360

X-ETAF = -.0019 X-GAMMAF = -.00230

Y-AXIS ANALYSIS #1A

Enter ETA and GAMMA

?.01,,

Y-ETA = .0100 Y-GAMMA = .00000

Initial Phase = 0

PHASE	AMP
134	.0100
362	.0096
525	.0100
726	.0091
886	.0097
1093	.0084
1241	.0090
1467	.0071
1589	.0075
1867	.0048
1912	.0048
2769	-.0040
2802	-.0040
3084	-.0083
3204	-.0074
3438	-.0140
3568	-.0119
3798	-.0236
3925	-.0199
4159	-.0429
4282	-.0362

Phase Distance = 4320 Phase Angle = 360

Y-ETAF = -.0382 Y-GAMMAF = .02092

SEGMENTED ROD TRANSMISSION ANALYSIS

Enter A and Q, DC and AC Ramp Entrances, and Exits

? .23462, .70482, 2160, , 4320, 4320,

Enter Initial Phase

? 0,

A = .23462000 Q = .70482000

DC RAMP

Entrance = 2160 Exit = 4320

AC RAMP

Entrance = 0 Exit = 4320

X-AXIS ANALYSIS #2

Enter ETA and GAMMA

? .01, .01,

X-ETA = .0100 X-GAMMA = .01000 Initial

Initial Phase = 0

PHASE	AMP
-------	-----

1111	.0688
------	-------

1228	.0660
------	-------

1449	.0831
------	-------

1613	.0729
------	-------

1795	.0880
------	-------

1995	.0676
------	-------

2139	.0767
------	-------

3241	-.0605
------	--------

3974	.0525
------	-------

Phase Distance = 4320 Phase Angle = 360

X-ETAF = .0224 X-GAMMAF = -.02565

Y-AXIS ANALYSIS #2A

Enter ETA and GAMMA

? .01, .01,

Y-ETA = .0100 Y-GAMMA = .01000

Initial Phase = 0

PHASE	AMP
953	.0589
1026	.0584
1278	.0752
1422	.0693
1621	.0855
1803	.0706
1968	.0831
2191	.0576
2308	.0623
3453	-.0562
3552	-.0521
3802	-.1150
3921	-.0999
4160	-.2221
4281	-.1891

Phase Distance = 4320 Phase Angle = 360

Y-ETAF = -.1998 Y-GAMMAF = -.11207

SEGMENTED ROD TRANSMISSION ANALYSIS

Enter A and Q, DC and AC Ramp Entrances, and Exits

? .23462, .70482, 2160, , 4320, 4320,

Enter Initial Phase

? 90,

A = .23462000 Q = .70482000

DC RAMP

Entrance = 2160 Exit = 4320

AC RAMP

Entrance = 0 Exit = 4320

X-AXIS ANALYSIS #3

Enter ETA and GAMMA

? .01, ,

X-ETA = .0100 X-GAMMA = .00000 Initial ϕ = 90°

Initial Phase = 90

PHASE	AMP
257	.0102
445	.0098
621	.0104
812	.0095
978	.0102
1182	.0088
1332	.0095
1558	.0073
1679	.0078
1973	.0048
1987	.0048
2817	-.0045
2960	-.0038
3130	-.0050
3869	.0052

Phase Distance = 4320 Phase Angle = 360

X-ETAF = -.0010 X-GAMMAF = -.00194

Y-AXIS ANALYSIS #3A

Enter ETA and GAMMA

? .01,,

Y-ETA = .0100 Y-GAMMA = .00000

Initial Phase = 90

PHASE	AMP
-------	-----

258	.0098
441	.0102
629	.0095
800	.0102
997	.0091
1156	.0099
1368	.0081
1507	.0087
1752	.0061
1847	.0064
3001	-.0071
3108	-.0065
3349	-.0126
3477	-.0109
3708	-.0213
3836	-.0180
4068	-.0380
4193	-.0321

Phase Distance = 4320 Phase Angle = 360

Y-ETAF = -.0525 Y-GAMMAF = -.05665

SEGMENTED ROD TRANSMISSION ANALYSIS

Enter A and Q, DC and AC Ramp Entrances, and Exits

? .23462, .70482, 2160, , 4320, 4320,

Enter Initial Phase

? 90,

A = .23462000 Q = .70482000

DC RAMP

Entrance = 2160 Exit = 4320

AC RAMP

Entrance = 0 Exit = 4320

X-AXIS ANALYSIS #4

Enter ETA and GAMMA

? .01, .01,

X-ETA = .0100 X-GAMMA = .01000

Initial Phase = 90

PHASE	AMP
1030	.0636
1129	.0621
1363	.0790
1518	.0711
1708	.0868
1899	.0693
2054	.0801
2295	.0516
2381	.0534
3163	-.0557
3356	-.0375
3465	-.0413
3906	.0396
4042	.0322
4200	.0436

Phase Distance = 4320 Phase Angle = 360

X-ETAF = .0224 X-GAMMAF = -.05492

Y-AXIS ANALYSIS #4A

Enter ETA and GAMMA

? .01, .01,

Y-ETA = .0100 Y-GAMMA = .01000

Initial Phase = 90

PHASE	AMP
-------	-----

1194	.0725
------	-------

1325	.0683
------	-------

1535	.0851
------	-------

1708	.0726
------	-------

1881	.0866
------	-------

2092	.0635
------	-------

2224	.0704
------	-------

2506	.0382
------	-------

2540	.0383
------	-------

2371	-.0460
------	--------

3454	-.0440
------	--------

3713	-.0993
------	--------

3830	-.0871
------	--------

4070	-.1916
------	--------

4191	-.1636
------	--------

Phase Distance = 4320 Phase Angle = 360

Y-ETAF = -.2699 Y-GAMMAF = -.29306

SEGMENTED ROD TRANSMISSION ANALYSIS

Enter A and Q, DC and AC Ramp Entrances, and Exits
 ? .23462, .70482, 2160, 4320, 6480, 4320,
 Enter Initial Phase
 ? 0,

A = .23462000 Q = .70482000

DC RAMP

Entrance = 2160 Exit = 6480

AC RAMP

Entrance = 0 Exit = 4320

X-AXIS Analysis #5
 Enter ETA and GAMMA
 ? .01,,

X-ETA = .0100 X-GAMMA = .00000
 Initial Phase = 0

PHASE	AMP
134	.0100
358	.0104
530	.0100
715	.0107
900	.0097
1070	.0107
1271	.0090
1422	.0099
1649	.0075
1768	.0079
2903	-.0054
3049	-.0045
3226	-.0061
3973	.0055
4163	.0034
4282	.0039
4705	-.0046
4863	-.0034
5011	-.0045
5428	.0044
5584	.0032
5728	.0042
6141	-.0049
6336	-.0029
6422	-.0031

Phase Distance = 6480 Phase Angle = 360

X-ETAF = -.0028 X-GAMMAF = .00240

Y-AXIS ANALYSIS #5A

Enter ETA and GAMMA

?.01,,

Y-ETA = .0100 Y-GAMMA = .00000

Initial Phase = 0

PHASE	AMP
134	.0100
362	.0096
525	.0100
726	.0100
886	.0097
1093	.0084
1241	.0090
1467	.0071
1589	.0075
1867	.0048
1912	.0048
2757	-.0039
2818	-.0039
3075	-.0074
3223	-.0060
3422	-.0094
3601	-.0065
3774	-.0093
3979	-.0053
4124	-.0068
4906	.0034
4982	.0033
5236	.0083
5373	.0066
5592	.0137
5736	.0106
5954	.0216
6091	.0171
6317	.0368
6445	.0305

Phase Distance = 6480 Phase Angle = 360

Y-ETAF = .0319 Y-GAMMAF = .01651

SEGMENTED ROD TRANSMISSION ANALYSIS

Enter A and Q, DC and AC Ramp Entrances, and Exits

?.23462.,70482,2160,,6480,4320,

Enter Initial Phase

?0,

A = .23462000 Q = .70482000

DC RAMP

Entrance = 2160 Exit = 6480

AC RAMP

Entrance = 0 Exit = 4320

X-AXIS ANALYSIS #6

Enter ETA and GAMMA

?.01,.01,

X-ETA = .0100 X-GAMMA = .01000

Initial Phase = 0

PHASE	AMP
1111	.0688
1228	.0660
1449	.0831
1613	.0729
1795	.0880
1995	.0676
2139	.0767
2411	.0446
2446	.0447
3251	-.0600
3435	-.0413
3569	-.0492
4313	.0602
5037	-.0603
5755	.0589
6468	-.0545

Phase Distance = 6480 Phase Angle = 360

X-ETAF = -.0541 X-GAMMAF = .01076

Y-AXIS ANALYSIS #6A

Enter ETA and GAMMA

? .01, .01,

Y-ETA = .0100 Y-GAMMA = .01000

Initial Phase = 0

PHASE	AMP
953	.0589
1026	.0584
1278	.0752
1422	.0693
1621	.0855
1803	.0706
1968	.0831
2191	.0576
2307	.0622
3438	-.0670
3578	-.0550
3784	-.0949
3957	-.0649
4136	-.0996
4336	-.0556
4487	-.0749
4735	-.0305
4816	-.0321
5602	.0682
5724	.0578
5957	.1307
6088	.1069
6318	.2379
6444	.1985

Phase Distance = 6480 Phase Angle = 360

Y-ETAF = .2085 Y-GAMMAF = .11096

SEGMENTED ROD TRANSMISSION ANALYSIS

Enter A and Q, DC and AC Ramp Entrances, and Exits
?.23462,.70482,2160,,6480,4320,

Enter Initial Phase
?90,

A = .23462000 Q = .70482000

DC RAMP

Entrance = 2160 Exit = 6480

AC RAMP

Entrance = 0 Exit = 4320

X-AXIS ANALYSIS #7

Enter ETA and GAMMA

? .01,,

X-ETA = .0100 X-GAMMA = .00000

Initial Phase = 90

PHASE	AMP
257	.0102
445	.0098
621	.0104
812	.0095
978	.0102
1182	.0088
1332	.0095
1558	.0073
1679	.0078
1973	.0048
1987	.0048
2822	-.0046
2946	-.0041
3142	-.0060
3895	.0044
4045	.0034
4208	.0047
4639	-.0032
4735	-.0029
4935	-.0051
5371	.0028
5445	.0027
5654	.0049
6073	-.0033
6192	-.0028
6364	-.0042

Phase Distance = 6480 Phase Angle = 360

X-ETAF = -.0023 X-GAMMAF = .00520

Y-AXIS ANALYSIS #7A

Enter ETA and GAMMA

? .01,,

Y-ETA = .0100 Y-GAMMA = .00000

Initial Phase = 90

PHASE	AMP
258	.0098
441	.0102
629	.0095
800	.0102
997	.0091
1156	.0099
1368	.0081
1507	.0087
1752	.0061
1847	.0064
2993	-.0066
3124	-.0057
3336	-.0095
3505	-.0069
3687	-.0103
3881	-.0063
4038	-.0086
4272	-.0039
4376	-.0044
5151	.0071
5278	.0059
5503	.0128
5645	.0099
5863	.0203
6002	.0160
6226	.0340
6357	.0279

Phase Distance = 6480 Phase Angle = 360

Y-ETAF = .0449 Y-GAMMAF = .04813

SEGMENTED ROD TRANSMISSION ANALYSIS

Enter A and Q, DC and AC Ramp Entrances, and Exits

? .23462, .70482, 2160, , 6480, 4320,

Enter Initial Phase

? 90,

A = .23462000 Q = .70482000

DC RAMP

Entrance = 2160 Exit = 6480

AC RAMP

Entrance = 0 Exit = 4320

X-AXIS ANALYSIS #8

Enter ETA and GAMMA

? .01, .01,

X-ETA = .0100 X-GAMMA = .01000

Initial Phase = 90

PHASE	AMP
1030	.0636
1129	.0621
1363	.0790
1518	.0711
1708	.0868
1899	.0693
2054	.0801
2294	.0517
2383	.0537
3173	-.0521
3322	-.0419
3493	-.0575
4233	.0596
4958	-.0562
5678	.0557
6391	-.0568

Phase Distance = 6480 Phase Angle = 360

X-ETAF = -.0418 X-GAMMAF = .05201

Y-AXIS ANALYSIS #8A

Enter ETA and GAMMA

? .01, .01,

Y-ETA = .0100 Y-GAMMA = .01000

Initial Phase = 90

PHASE	AMP
1194	.0725
1325	.0683
1535	.0851
1708	.0726
1881	.0866
2092	.0635
2224	.0704
3355	-.0585
3480	-.0507
3697	-.0912
3863	-.0652
4048	-.1027
4241	-.0608
4400	-.0854
4632	-.0382
4739	-.0429
5515	.0609
5631	.0526
5867	.1212
5998	.0989
6227	.2185
6355	.1809

Phase Distance = 6480 Phase Angle = 360

Y-ETAF = .2941 Y-GAMMA = .31753

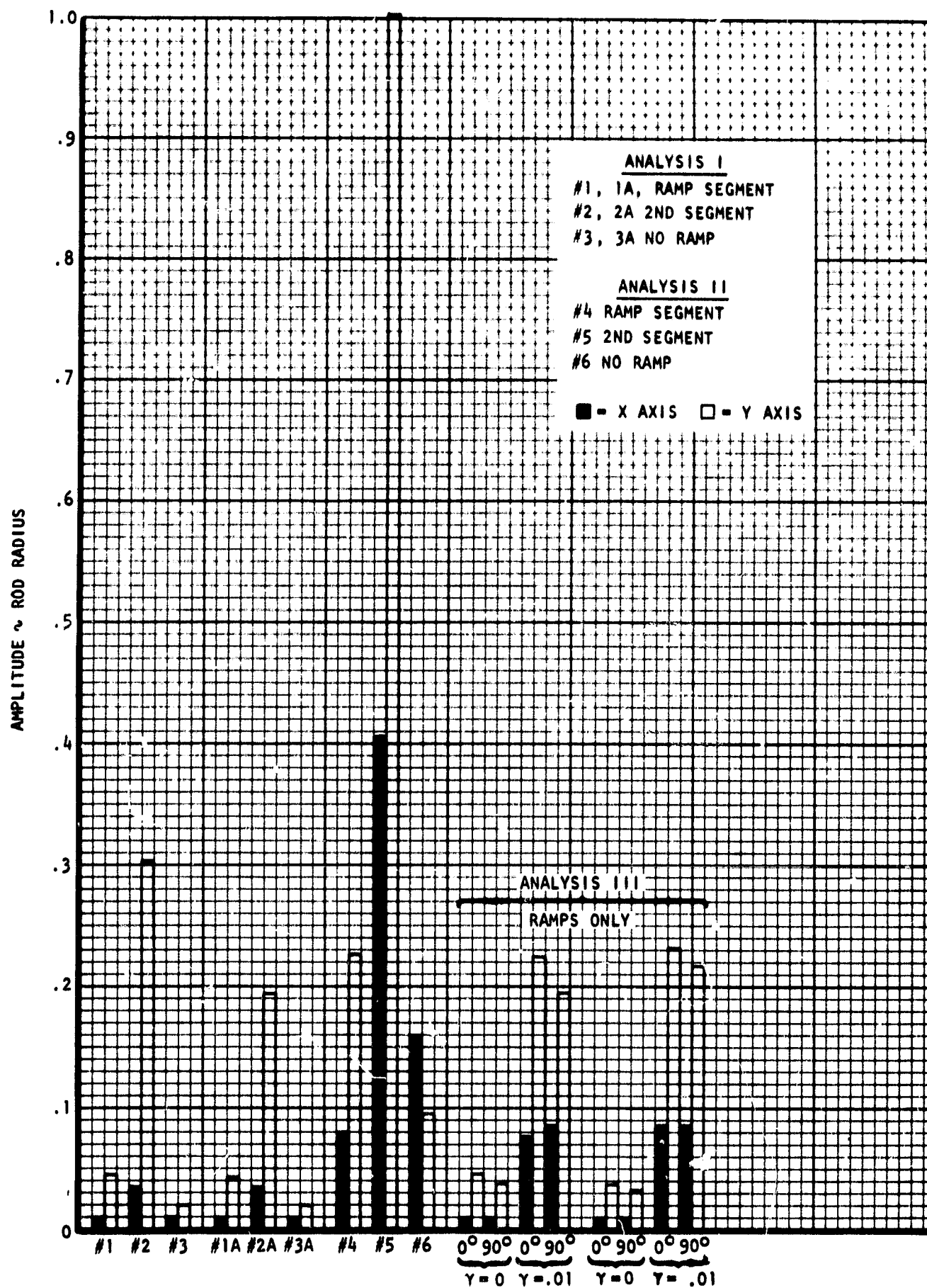


FIGURE 7. Summary of Appendix 1 Amplitude