

NASA TECHNICAL NOTE



NASA TN D-7893

NASA TN D-7893

(NASA-TN-D-7893) ROLE OF ELECTRON
CONCENTRATION IN SOFTENING AND HARDENING OF
TERNARY MOLYBDENUM ALLOYS (NASA) 23 p HC
\$3.25

N75-14888

CSSL 11F

H1/26

Unclas
08631

ROLE OF ELECTRON CONCENTRATION IN SOFTENING AND HARDENING OF TERNARY MOLYBDENUM ALLOYS

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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION • WASHINGTON, D. C. • JANUARY 1975

1. Report No. NASA TN D-7893		2. Government Accession No.		3. Recipient's Catalog No.	
4. Title and Subtitle ROLE OF ELECTRON CONCENTRATION IN SOFTENING AND HARDENING OF TERNARY MOLYBDENUM ALLOYS				5. Report Date January 1975	
				6. Performing Organization Code	
7. Author(s) Joseph R. Stephens and Walter R. Witzke				8. Performing Organization Report No. E-8101	
9. Performing Organization Name and Address Lewis Research Center National Aeronautics and Space Administration Cleveland, Ohio 44135				10. Work Unit No. 501-16	
				11. Contract or Grant No.	
12. Sponsoring Agency Name and Address National Aeronautics and Space Administration Washington, D.C. 20546				13. Type of Report and Period Covered Technical Note	
				14. Sponsoring Agency Code	
15. Supplementary Notes					
16. Abstract <p>An investigation was conducted to determine the effects of various combinations of hafnium, tantalum, rhenium, osmium, iridium, and platinum in ternary molybdenum alloys on alloy softening and hardening. Hardness tests were conducted at four test temperatures over the temperature range 77 to 411 K. Results showed that hardness data for ternary molybdenum alloys could be correlated with anticipated results from binary data based upon expressions involving the number of s and d electrons contributed by the solute elements. The correlation indicated that electron concentration plays a dominant role in controlling the hardness of ternary molybdenum alloys.</p>					
17. Key Words (Suggested by Author(s)) Hardness; Alloy softening; Alloy hardening; Electron concentration; Molybdenum alloys			18. Distribution Statement Unclassified - unlimited STAR Category 26 (rev.)		
19. Security Classif. (of this report) Unclassified		20. Security Classif. (of this page) Unclassified		21. No. of Pages 21	22. Price* \$3.00

* For sale by the National Technical Information Service, Springfield, Virginia 22151

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ROLE OF ELECTRON CONCENTRATION IN SOFTENING AND HARDENING OF TERNARY MOLYBDENUM ALLOYS

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SUMMARY

An investigation was conducted to determine softening and hardening behavior in ternary Mo alloys and to correlate these effects with electron concentration in the alloys. Solute additions to molybdenum (Mo) involved combinations of hafnium, tantalum, rhenium, osmium, iridium, and platinum. Alloys were prepared by arc-melting high-purity electron-beam-melted Mo and high-purity alloying elements. Hardnesses were determined by means of a modified microhardness test unit over the temperature range 77 to 411 K, which corresponds to the temperature range investigated in a previous study by the authors on binary Mo alloys and where alloy softening is normally observed for body-centered-cubic metals. A total of 66 ternary Mo alloys were studied at four test temperatures in order to characterize their hardness behavior and to permit a comparison with anticipated results based on binary Mo alloy data.

Results showed that hardness behavior of ternary Mo alloys could be correlated with results anticipated from binary data based upon expressions involving the number of s and d electrons contributed by the solute elements. It was further shown that combining alloying elements at concentrations that produce the maximum amount of softening in Mo does not result in additive softening in ternary Mo alloys. Once a critical electron concentration is exceeded, only alloy hardening is observed. A comparison of hardness behavior with literature data on Hall coefficient and magnetic susceptibility for tungsten-rhenium alloys showed that the hardness minimums occur at the same rhenium concentrations where minimums are observed for the physical-property measurements. These observations and the correlation of hardness with electron concentration further support the hypothesis that alloy softening in group VI metals is an intrinsic characteristic of these metals and that electron concentration plays the dominant role in controlling hardness.

INTRODUCTION

A previous investigation by the authors demonstrated that electron concentration plays the major role in determining the hardness of binary molybdenum alloys (ref. 1). Results showed that alloy hardening produced by additions of hafnium (Hf) and tantalum (Ta) to molybdenum (Mo) and alloy softening and hardening produced by additions of rhenium (Re), osmium (Os), iridium (Ir), and platinum (Pt) to Mo could be correlated with the difference in the number of s and d electrons of the solute element and Mo. These findings suggest that an intrinsic property of the alloys controls the hardness behavior of the Mo-base alloys investigated. If this argument is valid, it should be possible to predict the hardness behavior of ternary alloys on the basis of previously determined hardness data for binary alloys.

An alternative explanation of alloy softening is that solute elements can reduce the hardening effects associated with interstitial impurities by some form of substitutional-interstitial association and thus soften the alloy. This hypothesis has grown out of the work on the group V metals Ta (refs. 2 and 3) and niobium (Nb) (refs. 4 and 5), where interstitial solubilities are very high relative to their solubilities in the group VI metals chromium (Cr), Mo, and tungsten (W). If solute-interstitial association is important in softening of group VI metals, prediction of hardness for ternary alloys from binary data might not be possible because of variations in interstitial content from alloy to alloy.

The primary purpose of this investigation was to characterize the hardness behavior of ternary Mo alloys and compare these results with those expected on the basis of binary hardness data. A secondary purpose of this investigation was to determine if softening observed in binary alloys was additive in ternary alloys when the solutes were combined at concentration levels producing maximum softening in binary alloys.

Alloy additions to Mo included various combinations of Hf, Ta, Re, Os, Ir, and Pt. Hardness, the primary experimental measurement for this study, was determined for each alloy at four test temperatures over a homologous temperature range of 0.02 to 0.15 T_m (where T_m is the absolute melting temperature of unalloyed Mo), the temperature range where alloy softening was observed for binary Mo alloys.

SYMBOLS

- C solute content, at. %
- H hardness
- R Hall coefficient
- T_m absolute melting temperature of unalloyed Mo

ΔV difference in number of s and d electrons between solute and solvent

$$\Delta V_{av} = \frac{C_1 \Delta V_1 + C_2 \Delta V_2}{C_1 + C_2}$$

X_R residual paramagnetism

Ω electron concentration parameter

EXPERIMENT

Materials

Materials for this investigation included high-purity electron-beam-melted Mo, Ta, and Re; commercial-purity Hf turnings and Pt foil; and hydrogen-annealed Os and Ir powders. Ingots were prepared by nonconsumable triple arc-melting of 70-gram charges in a water-cooled copper mold followed by drop casting into a square-cross-section mold.

Table I presents analyzed compositions in atomic percent of the Mo alloys. Interstitial analyses of several alloys from each alloy series in ppm by weight are also listed in table I.

Slices approximately 3 millimeters thick and 15 millimeters on a side were cut from the cast ingots for hardness testing. One face of each specimen that was to be used for hardness testing was given a metallographic polish. Specimens were then annealed in a vacuum of 1×10^{-4} newton per square meter or better for 1 hour at 0.7 to 0.8 T_m in order to reduce segregation and produce single-phase, equiaxed, strain-free specimens.

Apparatus

The modified microhardness test unit used in this study has been described previously (ref. 6). The test unit permitted hardness testing over the temperature range 77 to 411 K.

Procedure

Molybdenum alloy compositions were selected to determine if softening observed in binary Mo alloys is additive when concentrations of the solutes producing maximum softening in binary alloys are combined to form ternary alloys. Solute combinations of this

type included Re-Os, Re-Ir, Re-Pt, and Ir-Pt. Alloying elements that produce only hardening in binary Mo alloys also were combined with those elements that cause softening in Mo. These alloy combinations included Ir-Hf, Ta-Pt, Re-Hf, and Re-Ta. A third combination of solute elements consisted of those elements that were shown in the previous study to produce only hardening in Mo, namely, Hf and Ta. A total of 66 ternary alloys were investigated.

Test temperatures for ternary Mo alloys were selected to cover the temperature range where alloy softening was observed for the binary Mo alloys, that is, less than $0.17 T_m$ (ref. 1). Test temperatures in equivalent increments included 77, 188, 300, and 411 K or 0.027 , 0.065 , 0.104 , and $0.143 T_m$, respectively. At least 10 diamond pyramid hardness impressions were made on each alloy at each test temperature. A load of 1 kilogram and a dwell time of 15 seconds were used for the impressions. The relative standard deviation was 5 percent.

RESULTS

Solute Effects

In order to determine if alloy softening observed in binary Mo alloys is additive, solute additions of Os, Ir, and Pt corresponding to those concentrations producing the maximum amount of softening at 77 K in the binary alloys were combined with Re, which ranged in concentration from 2 to 23 atomic percent. Hardnesses for the ternary Mo alloys are summarized in table I.

Figure 1 shows the effect of Re on the hardnesses of the ternary alloys. Binary data for Mo-Re alloys are shown in figure 1 for comparison. The minimum hardnesses for Mo-Os, Mo-Ir, and Mo-Pt binary alloys at 77 K are also plotted on the ordinate in figure 1 to illustrate the softening achieved in binary alloys. It should be noted that the hardness increases with increasing Re content for three of the ternary systems investigated, which demonstrates that alloy softening is not additive.

Also shown in figure 1 are hardness data for a series of alloys containing Mo-6.5-Ta-Re. (Concentrations are given in at. %.) The hardness for another binary Mo alloy, Mo-7.9Ta, plotted on the ordinate, is near that obtained for the same Ta content in the ternary alloys. While Ta increases the hardness of Mo in binary alloys, combining a Mo-Ta alloy with Re produces softening in the ternary alloy system. It should be observed that the Mo-Ta-Re curve parallels the Mo-Re curve, the hardness minimum occurring at a Re content of approximately 8 atomic percent for both alloy series.

A second comparison of hardening in binary and ternary alloys is shown in figure 2 for the Mo-Hf and Mo-8.5Re-Hf alloy series. The Re content is near the amount of Re producing the maximum amount of softening in the binary Mo-Re system. Only hardening

is observed in this ternary system, and the two curves converge at higher Hf contents, which indicates that the hardening effect of Re is negligible in systems with high Hf contents.

A final form of hardness behavior in the ternary alloys is illustrated in figure 3 for Mo-3.5Ta-Pt alloys and Mo-6.8Ta-Pt alloys compared with the binary Mo-Pt alloys. The curve is drawn through the binary data, and it can be seen that the ternary data, which are for alloys containing 2 to 5.5 atomic percent Pt, lie along the hardening portion of the curve independent of Ta content up to 6.8 Ta.

Temperature Effects

The variation of hardness with temperature for the ternary Mo alloys is shown in figures 4 to 6. In figure 4(a) the changes in hardness with temperature for unalloyed Mo and a binary Mo-1.1Os alloy containing an amount of Os similar to that in the ternary alloys are compared with changes in hardness in the ternary Mo-0.96Os-Re alloys. The temperature dependency of hardness for Mo is reduced upon alloying with Os. The ternary alloy curves are parallel to the binary alloy curves, and both have a much lower temperature dependency of hardness than unalloyed Mo. This behavior is also observed for the other two elements that produce softening in Mo combined with Re (Ir and Pt), as shown in figures 4(b) and (c). In contrast, Ta added to Mo does not reduce the temperature dependence of hardness for a Mo-7.9Ta alloy, as shown in figure 4(d). The ternary alloy Mo-6.5Ta-2.6Re exhibits a similar temperature dependency of hardness. However, when the Re content exceeds the Ta content as in the ternary Mo-6.5Ta-7.8Re alloy, the variation of hardness with temperature is reduced substantially. The remaining ternary alloys in this series, with Re contents of 13.5, 18.5, and 22.8 atomic percent, also exhibit a reduced temperature dependency of hardness paralleling that of the Mo-6.5-Ta-7.8Re alloy.

Figure 5 shows the variation of hardness with temperature of unalloyed Mo, a binary Mo-8.2Re alloy, and a series of ternary Mo-8.5Re-Hf alloys. Adding Re to Mo reduces the temperature dependency of hardness, and further additions of Hf result in a similar reduced temperature dependency of hardness for Hf contents ranging from 1.9 to 8.7 atomic percent.

In figure 6 ternary Mo-Ta-Pt alloys are compared with unalloyed Mo and two binary alloys, Mo-4.9Ta and Mo-4.8Pt. Unalloyed Mo and the Mo-4.9Ta alloy exhibit a similar variation of hardness with temperature, while the Mo-4.8Pt alloy and the ternary alloys exhibit slightly reduced temperature dependencies of hardness.

Electron Concentration Effects

In a previous study by the authors (ref. 1) on hardness behavior of binary Mo alloys, it was shown that hardness could be correlated with an electron concentration parameter Ω , expressed by

$$\Omega_{\text{binary}} = C^{1/2} \Delta V \quad (1)$$

where C is the concentration of solute in atomic percent and ΔV is the difference in number of s and d electrons between the solute element and Mo.

A schematic representation of the hardness behavior of binary Mo alloys at 77 K is shown in figure 7 as a function of Ω . The figure is divided into the following three regions: A, characterized by hardening as a result of Ta or Hf additions; B, characterized by softening as a result of Re, Os, Ir, or Pt additions; and C, characterized by hardening as a result of larger additions of Re, Os, Ir, or Pt. The division between regions B and C corresponds to the hardness minimum and is temperature dependent. Values of the electron concentration parameter at the hardness minimum Ω_{min} and the corresponding amounts of solute content in the binary Mo alloys (fig. 11 of ref. 1) for the four temperatures used in this study are as follows:

Test temperature, K	Electron concentration parameter at hardness minimum, Ω_{min}	Solute content at Ω_{min} , at. %			
		Re	Os	Ir	Pt
77	2.7	7.1	1.8	0.8	0.5
186	2.0	3.8	1.0	.4	.2
300	1.2	1.5	.4	.2	.1
411	.5	.2	.1	.03	.02

Thus, binary alloy combinations that fall in region B at lower temperatures may fall in region C at higher temperatures because of the shift of region B to lower values of Ω with increasing temperature.

To correlate the hardness of ternary alloys due to solute additions from the same region or from adjacent regions, the following expression was used:

$$\Omega_{\text{ternary}} = (C_1 + C_2)^{1/2} \Delta V_{\text{av}} \quad (2)$$

where

$$\Delta V_{av} = \frac{C_1 \Delta V_1 + C_2 \Delta V_2}{C_1 + C_2}$$

There are a total of 11 possible combinations of A, B, and C to form ternary alloys (see fig. 7(b)). Of these combinations, eight have been related to equation (2). The remaining three possible combinations of ternary alloys, which involve solute additions from each of the hardening regions A and C, could not be correlated by equation (2), but could be described by equation (1), as is shown in this section.

Table I also summarizes the values of the difference in s and d electrons ΔV_{av} , the electron concentration parameter Ω , and the types of solute combinations for the ternary Mo alloys. Figure 8 shows the correlation of hardness with the square root of total solute content and the average electron concentration for the first group of eight types of solute combinations in the ternary Mo alloy systems, as described schematically in figure 7(a). The lines drawn are least-squares lines for the binary Mo alloys (ref. 1), so that a comparison can be made with the ternary-alloy data points. The ternary data are in good agreement with the hardness that would be anticipated from results for the binary alloys at each of the four test temperatures.

The remaining ternary alloys involve combinations of solutes from regions A and C in figure 7(a). Since these two areas represent hardening regions, softening would not be expected to occur in $A + C = B$ type combinations. This was found to be true, and it was further observed that equation (2) also did not adequately describe the $A + C = A$ or $A + C = C$ combinations. Examination of figures 2 and 3 suggests that the contributions to hardness by Re in the Mo-Re-Hf system and the contributions by Ta in the Mo-Ta-Pt alloys which involve only $A + C$ combinations are essentially nil. This suggests that the ternary data can be correlated with Ω for Hf and Pt for these two series of ternary alloys. The remaining alloy system, Mo-Ta-Re, involving $A + C$ combinations followed a similar pattern.

Figure 9 shows the correlation of hardness with Ω at the four test temperatures for the $A + C$ alloys. The figure further shows that $A + C = A$ combinations can be correlated with Ω for Hf or Ta while $A + C = B$ or $A + C = C$ combinations can be correlated with Ω for Pt or Re. The only exception to the previous correlations were the $A + C = A$ alloys in the Mo-Ta-Pt system, which were better correlated with Ω for Pt but deviated from the least-squares line, as indicated by the solid data points in figure 9. This deviation above the least-squares line is probably due to some hardening contributed by Ta, which ranged in content from 8 to 36 atomic percent.

Observation of figures 8 and 9 suggests that the value of Ω at the hardness minimum (Ω_{\min}) decreases with increasing test temperature in a manner that is similar to the results observed previously for binary Mo alloys (fig. 12 of ref. 1).

DISCUSSION

Correlation of Hardness With Electron Concentration

Hardness results for the ternary Mo alloys have further confirmed the importance of electron concentration in controlling the hardness of Mo alloys. This was particularly borne out by the combination of solute elements that produced softening in the binary Mo alloys. The results showed that for $B + B = B$ combinations, behavior is additive and further softening is produced. However, if the critical electron concentration corresponding to the hardness minimum for binary alloy systems is exceeded in the ternary alloys, $B + B = C$, no further softening will occur and hardening begins. Therefore, no additive softening effects were observed upon combining Re at a concentration which produced the maximum amount of softening in Mo with concentrations of Os, Ir, or Pt corresponding to solute contents at the hardness minimum.

The results further showed that there was good agreement between the measured hardnesses for ternary alloys and the hardnesses that would be expected from binary data. Electron concentration was shown to play a dominant role in controlling the hardness of the ternary Mo alloys by using equation (2), which averages the electron concentration contributed by each solute, and by taking into consideration the hardening and softening regions shown schematically in figure 7. Solutes from the same or adjacent regions in figure 7 could be adequately described by equation (2), and the data were in good agreement with least-squares lines for the binary data.

In contrast, hardening produced by solutes from each of the two hardening regions could not be correlated by using equation (2). This was anticipated since equation (2) would predict ternary alloys formed by solutes from the two hardening regions falling in the softening region. However, only hardening would be expected in this type of ternary alloy. The hardness results could be correlated by using equation (1), which avoids the problem of placing the ternary alloys in the softening region. It is not understood why just one solute controls the hardness in these alloys; however, this behavior was observed in Mo-Ta-Re, Mo-Hf-Re, and Mo-Ta-Pt alloys. The correlation of hardness with electron concentration points to an intrinsic property controlling hardness in binary and ternary Mo alloys. This finding is in contrast with previous results obtained by the authors on Nb alloys (ref. 5), where atom size misfit was observed to control hardness.

Most theories of solid solution strengthening contain an expression involving shear modulus and an atom size misfit parameter (ref. 7). More recently, attempts have been

made to correlate hardening and softening with electron concentration. Stern (ref. 8) showed that solution hardening occurs in titanium (Ti) alloys predominantly by an electronic mechanism. In general, high hardening rates were produced in Ti alloys for which columns of the solute and solvents are far apart in the periodic table, that is, for which the difference in s and d electrons is great.

In addition, the results of reference 5 suggested a similar trend of increased hardening rates in Nb alloys with increase in periodic table group number of the solute element. However, atom size misfit played the major role in controlling the hardness of Nb alloys.

In previous studies on binary Mo alloys (ref. 1) electron concentration played the major role in controlling both alloy softening and alloy hardening. Again a trend of increased hardening rate with increasing difference in s and d electrons between solvent and solute was observed.

Finally, attempts were made by Leslie and coworkers to correlate iron (Fe) alloy toughness (ref. 9) and modulus (ref. 10) with number of s and d electrons. In general, an improvement in toughness was observed with increasing difference in the number of valence electrons between solute and solvent. Similarly, the modulus increased with the increase in difference of valence electrons between solute and Fe.

Correlation of Physical Properties With Electron Concentration

The results discussed in the last section suggest that electron concentration plays an important part in determining the mechanical properties of various metals and alloys, with possibly the most dominant role being found in alloys of the group VI metals. Of particular interest, of course, is the initial softening observed in Cr-Re and W-Re (ref. 6); in Mo-Re, Mo-Os, Mo-Ir, and Mo-Pt (ref. 1); and in the ternary Mo alloys of this study, which is followed by alloy hardening once a critical electron concentration has been reached. Some insight into the reason for this behavior may be gained by consideration of the work by Budagovskiy, Bykov, Gavriluk, and Podyachev (ref. 11). These researchers studied the W-Re system (up to 25 at. % Re) by means of electrical resistivity, Hall effect, angular distribution of the annihilation of photons, and magnetic susceptibility.

Figure 10(a) is a comparison of hardness (ref. 6) and Hall coefficient (ref. 11) of W-Re alloys at 77 K. It should be noted that the minimum in hardness and maximum in Hall coefficient occur at a Re content of approximately 8 atomic percent. Figure 10(b) is a similar comparison of hardness and magnetic susceptibility (residual paramagnetism) measurements at 300 K on W-Re alloys. The hardness minimum and magnetic susceptibility maximum occur at approximately 5 atomic percent Re at this temperature. In contrast to the W-Re alloys, Nb-Mo alloys exhibit only alloy hardening (ref. 5), and

as shown in figure 10(c), from the work of Jones, Pessall, and McQuillan (ref. 12), magnetic susceptibility decreases monotonically with increasing Re content.

The comparisons in figures 10(a) and (b) strongly suggest a direct correlation between mechanical properties (hardness) and electron structure, as indicated by the Hall coefficient and magnetic susceptibility. The abrupt change from softening to hardening in W-Re alloys is reflected by a similar change in physical properties, which suggests a change in electronic structure occurs at a critical composition in the W-Re system. These correlations further support the contention that alloy softening and hardening of body-centered-cubic group VI metals are intrinsic properties of these metals and are controlled primarily by electronic structure.

In contrast, alloy hardening of body-centered-cubic group V metals is controlled by atomic size misfit, as shown by previous work by the authors on Nb-base alloys (ref. 5). Alloy softening in these metals is apparently an extrinsic effect and, as suggested by others (refs. 2 to 4), is due to some type of solute-interstitial association.

CONCLUSIONS

Based on a hardness study of ternary alloys of molybdenum (Mo) with various combinations of hafnium (Hf), tantalum (Ta), rhenium (Re), osmium (Os), iridium (Ir), and platinum (Pt), the following conclusions are drawn:

1. Alloy softening observed in ternary Mo alloys (studied in this investigation) and in binary Mo alloys (studied previously by the authors) is a real characteristic of these alloys, as well as other group VI metals.

2. Alloy softening and hardening in ternary Mo alloys can, in general, be predicted from binary data by using expressions involving the number of s and d electrons contributed by the solute elements.

3. There is a critical electron concentration corresponding to the hardness minimum for all binary and ternary Mo alloys, which decreases with increasing test temperature. Combining solute elements Re, Os, Ir, and Pt at concentrations that produce the maximum amount of softening in Mo does not result in additive softening in ternary Mo alloys.

4. A direct correlation exists between hardness and electron structure for group VI metals. A comparison of hardness with literature data on Hall coefficient and magnetic susceptibility for W-Re alloys shows that the hardness minimums occur at the same Re concentrations where maximums are observed for Hall coefficient and magnetic susceptibility.

5. The ability to predict the hardness of ternary Mo alloys from binary data and to correlate the data with the number of s and d electrons suggests that extrinsic effects such as solute-interstitial interactions do not substantially affect the hardness of the Mo-base alloys.

Lewis Research Center,
National Aeronautics and Space Administration,
Cleveland, Ohio, October 29, 1974,
506-16.

REFERENCES

1. Stephens, Joseph R.; and Witzke, Walter R.: Alloy Hardening and Softening in Binary Molybdenum Alloys as Related to Electron Concentration. *J. Less Common Metals*, vol. 29, 1972, pp. 371-388.
2. Hasson, D. F.; and Arsenault, R. J.: Substitutional-Interstitial Interactions in BCC Alloys. *Treatise in Materials Science and Technology*, volume 1. H. Herman, ed., Academic Press, 1972, pp. 179-246.
3. Smialek, R. L.; Webb, G. L.; and Mitchell, T. E.: Solid Solution Softening in BCC Metal Alloys. *Scripta Met.*, vol. 4, 1970, pp. 33-38.
4. Ravi, K. V.; and Gibala, R.: The Strength of Niobium-Oxygen Solid Solutions. *Acta Met.*, vol. 18, no. 6, June 1970, pp. 623-634.
5. Stephens, Joseph R., and Witzke, Walter R.: Hardness Behavior of Binary and Ternary Niobium Alloys at 77 and 300 K. NASA TN D-7847, 1974.
6. Stephens, J. R.; and Witzke, W. R.: Alloy Softening in Group VIA Metals Alloyed With Rhenium. *J. Less-Common Metals*, vol. 23, 1971, pp. 325-342.
7. Leslie, W. C.: Iron and Its Dilute Substitutional Solid Solutions. *Met. Trans.*, vol. 3, no. 1, Jan. 1972, pp. 5-26.
8. Stern, E. A.: Application of Alloy Physics to Solution Strengthening. Presented at Materials Engineering Congress, Am. Soc. Metals, Oct. 1973.
9. Leslie, W. C.; Sober, R. J.; Babcock, S. G.; and Green, S. J.: Plastic Flow in Binary Substitutional Alloys of BCC Iron-Effects of Strain Rate, Temperature and Alloy Content. *ASM Trans.*, vol. 62, no. 3, Sept. 1969, pp. 690-710.

10. Speich, G. R. ; Schwoeble, A. J. ; and Leslie, W. C. : Elastic Constants of Binary Iron-Base Alloys. Met. Trans., vol. 3, no. 8, Aug. 1972, pp. 2031-2037.
11. Budagovskiy, S. S. ; Bykov, V. N. ; Gavriluk, M. I. ; and Podyachev, V. N. : Some Electron Structure Characteristics of W-Re Solid Solutions. Metallofiz., no. 44, 1973, pp. 57-67.
12. Jones, D. W. ; Pessall, N. ; and McQuillan, A. D. : Correlation Between Magnetic Susceptibility and Hydrogen Solubility in Alloys of Early Transition Elements. Phil. Mag., vol. 6, no. 63, Mar. 1961, pp. 455-459.

TABLE I. - SUMMARY OF HARDNESS DATA AND ELECTRON CONCENTRATION RELATIONS FOR TERNARY MOLYBDENUM ALLOYS

Analyzed solute content				Analyzed interstitial content, ppm by wt.			Temperature, K				Difference in electron concentration, $\Delta V_{av} = \frac{C_1 \Delta V_1 + C_2 \Delta V_2}{C_1 + C_2}$	Electron concentration parameter, $\Omega_{ternary} = (C_1 + C_2)^{1/2} \Delta V_{av}$ (a)	Temperature, K			
at. %	Solute	at. %	Solute	Car-bon	Oxy-gen	Nitro-gen	Vickers hardness number						77	188	300	411
							Type of ternary combination									
0.44	Re	0.23	Os	32	26	2	371	238	143	99	1.34	1.10	B+B=B	B+B=B	B+B=B	C+C=C
.43		.52		---	---	---	342	225	150	135	1.48	1.48	B+B=B	B+B=B	B+B=B	C+C=C
.96		.25		30	26	2	352	229	138	113	1.21	1.33	B+B=B	B+B=B	B+B=B	C+C=C
2.23		.96		---	---	---	341	249	188	173	1.30	2.32	B+B=B	B+B=B	C+C=C	C+C=C
4.02		.92		130	9	5	356	257	206	182	1.18	2.64	B+B=B	C+B=C	C+C=C	C+C=C
8.01		.95		---	---	---	368	288	232	211	1.11	3.31	C+B=C	C+B=C	C+C=C	C+C=C
12.19		.96		---	---	---	378	315	250	228	1.07	3.89	C+B=C	C+B=C	C+C=C	C+C=C
16.06		1.82		---	---	---	429	358	309	267	1.08	4.59	C+B=C	C+C=C	C+C=C	C+C=C
2.23	Re	0.54	Ir	---	---	---	362	268	212	186	1.39	2.31	B+B=B	B+C=C	C+C=C	C+C=C
4.31		.56		77	6	13	357	293	223	201	1.23	2.71	B+B=B	C+C=C	C+C=C	C+C=C
8.11		.58		---	---	---	366	304	232	230	1.13	3.34	C+B=C	C+C=C	C+C=C	C+C=C
11.72		.60		---	---	---	411	344	265	237	1.10	3.85	C+B=C	C+C=C	C+C=C	C+C=C
15.79		1.63		---	---	---	480	432	361	327	1.19	4.95	C+C=C	C+C=C	C+C=C	C+C=C
0.37	Re	0.35	Pt	11	28	---	367	317	221	180	2.46	2.09	B+B=B	B+C=C	B+C=C	B+C=C
2.21		.47		---	---	---	385	280	234	201	1.53	2.50	B+B=B	C+C=C	C+C=C	C+C=C
3.45		.57		---	---	5	384	336	272	235	1.43	2.86	B+C=C	C+C=C	C+C=C	C+C=C
3.37		1.08		---	150	---	431	382	327	295	1.73	3.65	B+C=C	C+C=C	C+C=C	C+C=C
3.88		.45		118	13	3	365	290	248	212	1.31	2.73	B+B=B	C+C=C	C+C=C	C+C=C
7.37		2.15		4	23	---	592	550	456	421	1.68	5.18	C+C=C	C+C=C	C+C=C	C+C=C
7.97		.46		---	---	---	371	314	258	228	1.16	3.38	C+C=C	C+C=C	C+C=C	C+C=C
7.10		1.21		17	23	5	479	424	389	333	1.44	4.14	B+C=C	C+C=C	C+C=C	C+C=C
11.83		.41		---	---	---	411	405	270	241	1.10	3.85	C+B=C	C+C=C	C+C=C	C+C=C
22.96		.43		10	35	6	444	381	311	284	1.06	5.10	C+B=C	C+C=C	C+C=C	C+C=C
0.45	Ir	0.51	Hf	---	---	---	355	269	220	188	0.34	0.34	B+A=B	C+A=B	C+A=B	C+A=B
0.10	Ir	0.15	Pt	96	---	---	348	248	185	182	3.60	1.80	B+B=B	B+B=B	B+C=C	C+C=C
.16		.77		---	32	---	396	367	287	257	3.83	3.69	B+C=C	B+C=C	B+C=C	C+C=C
.29		1.83		---	---	1	508	507	466	419	3.86	5.62	B+C=C	B+C=C	C+C=C	C+C=C
.48		3.85		37	---	---	782	727	636	593	3.89	8.09	B+C=C	C+C=C	C+C=C	C+C=C
.19		.29		---	25	---	366	281	236	196	3.60	2.50	B+B=B	B+C=C	C+C=C	C+C=C
.66		.42		105	13	7	418	349	286	265	3.39	3.52	B+B=B	C+C=C	C+C=C	C+C=C
.60		.11		30	26	2	373	287	235	203	3.15	2.66	B+B=B	C+B=C	C+C=C	C+C=C
1.20		.08		18	24	2	458	349	288	260	3.06	3.46	C+B=C	C+B=C	C+C=C	C+C=C
1.83		1.05		---	---	---	596	534	481	444	3.36	5.71	C+C=C	C+C=C	C+C=C	C+C=C
0.54	Ta	0.50	Pt	---	---	---	377	284	236	174	1.40	1.43	A+C=B	A+C=B	A+C=C	A+C=C
1.84		.79		21	25	4	440	351	295	263	.50	.81	A+C=B	A+C=B	A+C=B	A+C=B
1.87		.74		21	32	---	434	400	303	283	.42	.87	A+C=B	A+C=B	A+C=B	A+C=B
3.37		2.04		---	6	---	561	473	415	376	.89	2.06	A+C=B	A+C=B	A+C=B	A+C=B
3.61		3.14		---	77	1	686	643	542	475	1.33	3.44	A+C=B	A+C=B	A+C=B	A+C=B
5.47		4.15		21	---	---	776	675	620	551	1.72	4.76	A+C=B	A+C=B	A+C=C	A+C=C
8.02		1.63		---	6	---	587	495	432	383	.16	-.48	A+C=A	A+C=A	A+C=A	A+C=A
6.87		2.85		---	18	---	645	559	529	458	.50	1.57	A+C=B	A+C=B	A+C=B	A+C=B
6.73		3.86		---	---	1	779	683	649	577	.82	2.68	A+C=B	A+C=B	A+C=B	A+C=C
6.78		5.38		11	---	---	832	808	710	675	1.21	4.23	A+C=B	A+C=B	A+C=B	A+C=C
9.35		1.70		---	---	1	579	492	422	384	.23	-.77	A+C=A	A+C=A	A+C=A	A+C=C
12.25		2.95		---	14	---	748	688	596	545	.20	-.75	A+C=A	A+C=A	A+C=A	A+C=C
15.04		.92		12	18	4	573	489	422	371	.71	-2.84	A+C=A	A+C=A	A+C=A	A+C=A
16.06		1.15		11	---	---	559	470	405	358	.67	-2.76	A+C=A	A+C=A	A+C=A	A+C=A
20.70		2.35		---	---	1	719	668	606	555	.38	-1.83	A+C=A	A+C=A	A+C=A	A+C=A
36.86		2.91		17	---	---	701	655	600	545	.65	-4.07	A+C=A	A+C=A	A+C=A	A+C=A
0.56	Ta	0.46	Hf	---	449	---	421	268	175	135	-1.45	-1.47	A+A=A	A+A=A	A+A=A	A+A=A
1.04		1.14		18	26	4	447	283	194	175	-1.52	-2.25				
1.00		6.30		33	26	8	533	444	359	335	-1.86	-5.03				
10.80		10.99		49	---	---	650	559	498	461	-1.50	-7.02				
0.46	Re	4.68	Hf	44	---	---	476	373	293	299	-1.73	-3.83	B+A=A	B+A=A	B+A=A	C+A=A
1.00		9.47		---	---	---	583	494	435	426	-1.71	-5.54	B+A=A	B+A=A	C+A=A	C+A=A
1.91		.12		---	---	2	366	248	145	118	.82	1.17	B+A=B	C+A=B	C+A=B	C+A=C
4.18		.28		---	---	---	343	234	161	145	.81	1.71	B+A=B	C+A=B	C+A=C	C+A=C
8.58		1.93		---	---	---	386	308	266	235	.45	1.46	C+B=B	C+A=B	C+A=C	C+A=C
8.50		3.72		92	23	2	443	357	299	272	-.09	-.30	C+A=A	C+A=A	C+A=A	C+A=A
8.64		6.33		16	19	---	524	430	401	354	-.27	-1.04	C+A=A	C+A=A	C+A=A	C+A=A
8.43		8.73		---	---	---	583	500	436	403	-.53	-2.18	C+A=A	C+A=A	C+A=A	C+A=A
2.64	Re	6.18	Ta	14	27	---	424	308	203	187	-0.40	-1.19	B+A=A	C+A=A	C+A=B	C+A=B
7.81		7.02		12	133	---	385	313	246	228	.05	.21	C+A=B	C+A=B	C+A=B	C+A=B
13.46		6.42		---	---	---	413	344	306	269	.35	1.58	C+A=B	C+A=B	C+A=C	C+A=C
18.47		6.35		52	23	---	450	363	329	291	.49	2.43	C+A=B	C+A=C	C+A=C	C+A=C
22.82		6.70		---	---	---	462	409	348	307	.55	2.97	C+A=C	C+A=C	C+A=C	C+A=C

^aFor all A+C combinations Ω_{binary} was used rather than $\Omega_{ternary}$.

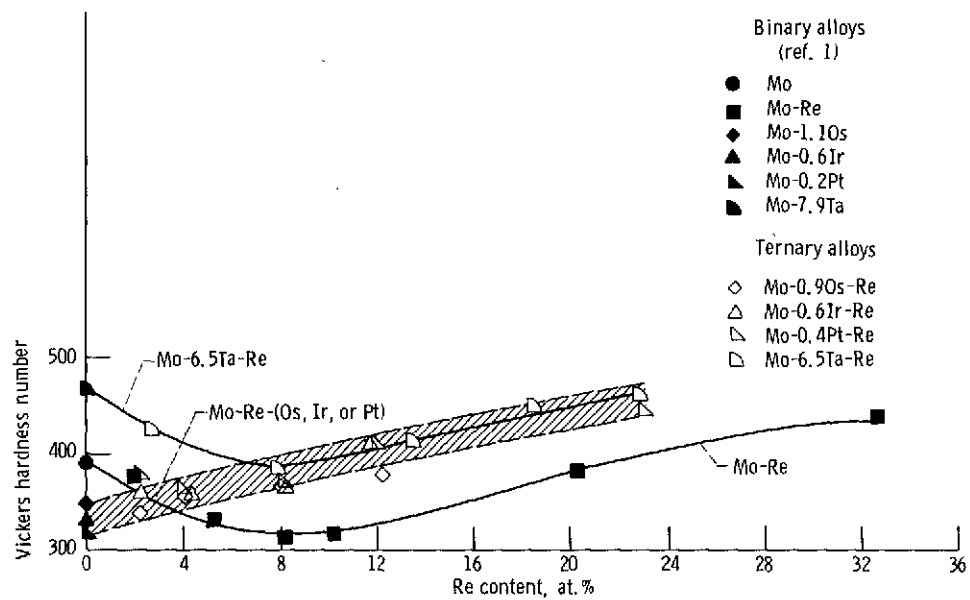


Figure 1. - Effect of Re on hardness in ternary Mo-base alloys at 77 K.

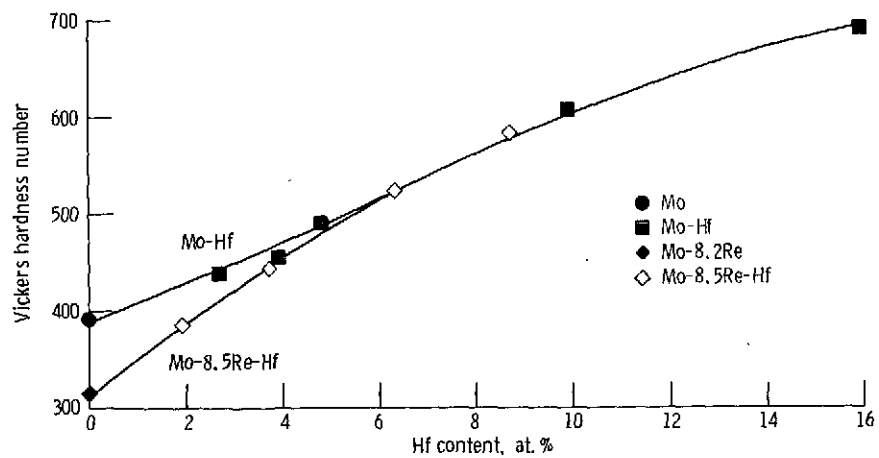


Figure 2. - Effect of Hf on hardness at 77 K in binary Mo-Hf alloys and ternary Mo-8.5Re-Hf alloys.

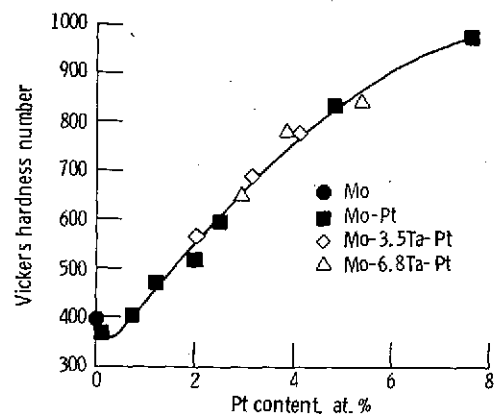


Figure 3. - Effect of Pt on hardness at 77 K in binary Mo-Pt alloys and in ternary Mo-3.5 Ta-Pt and Mo-6.8Ta-Pt alloys.

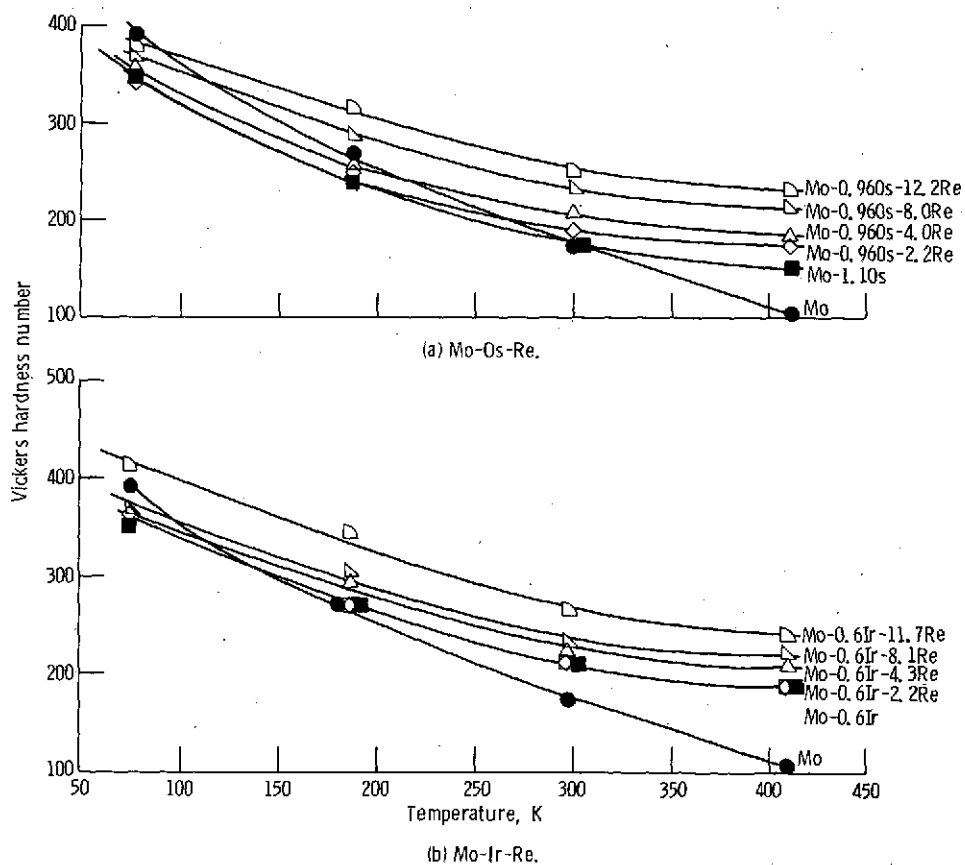


Figure 4. - Effect of temperature on hardness of ternary Mo-Os-Re, Mo-Ir-Re, Mo-Pt-Re, and Mo-Ta-Re alloys.

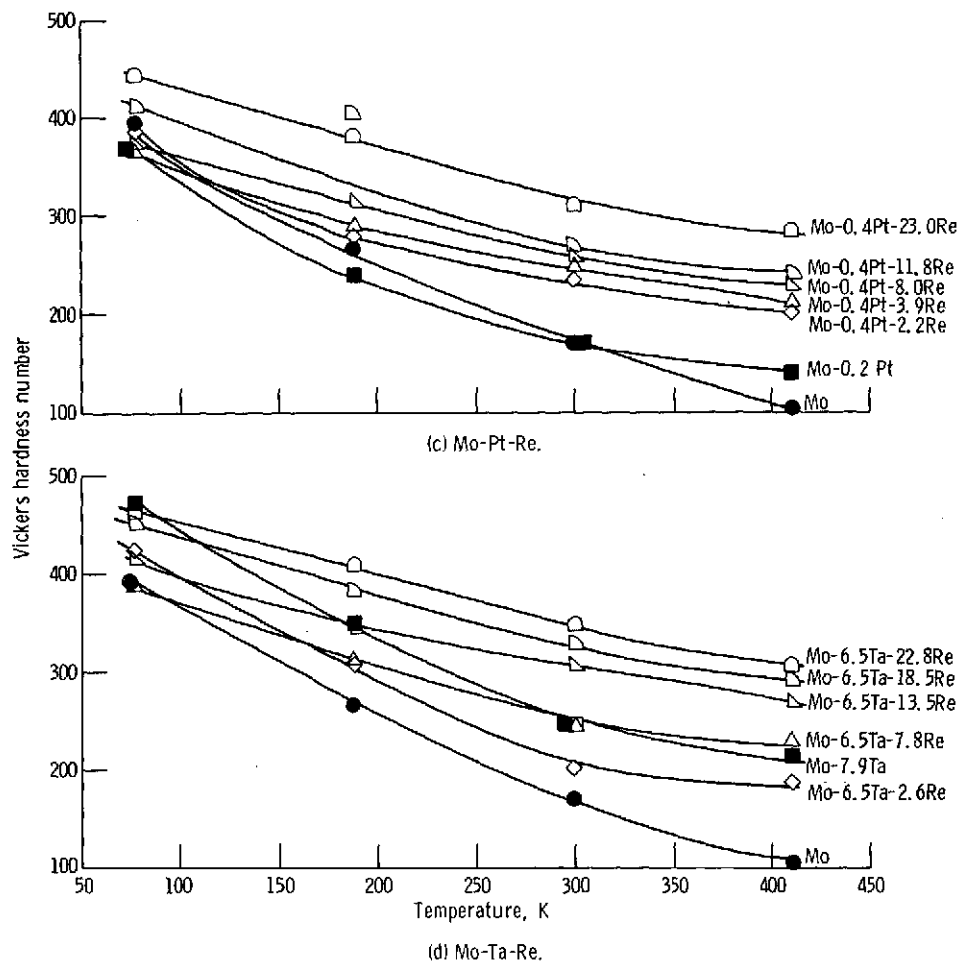


Figure 4. - Concluded.

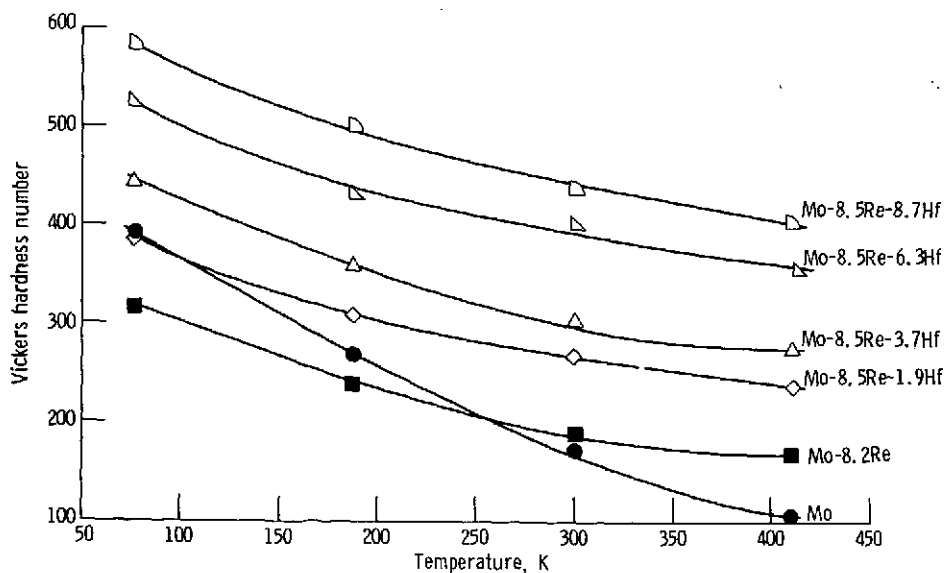


Figure 5. - Effect of temperature on hardness of ternary Mo-Re-Hf alloys.

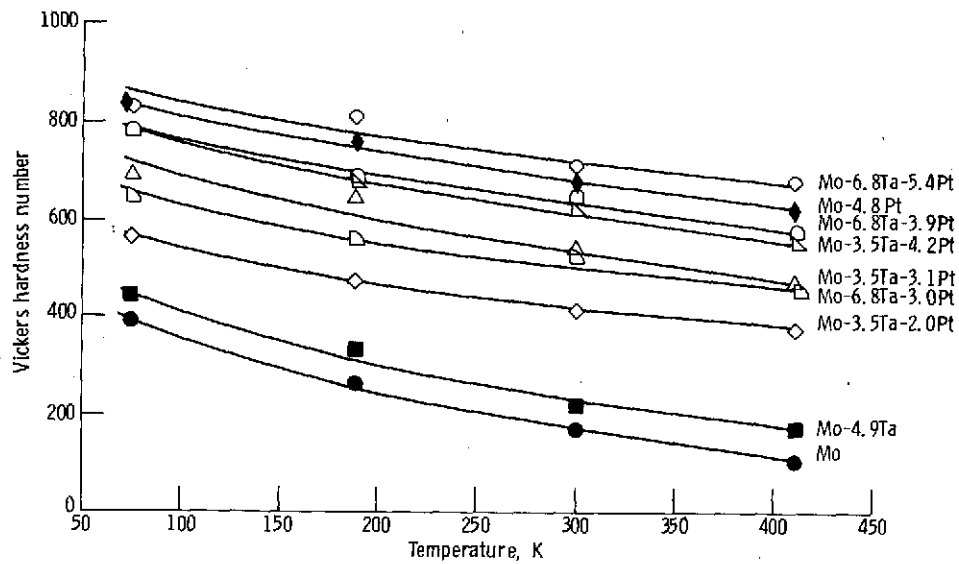
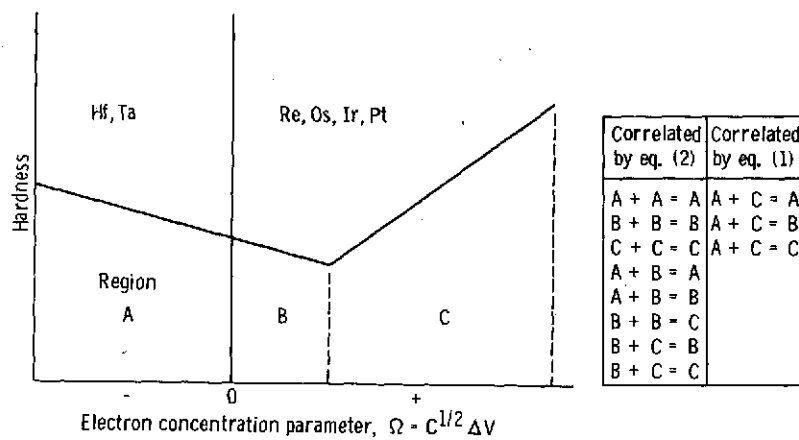


Figure 6. - Effect of temperature on hardness of ternary Mo-Ta-Pt alloys.



(a) Schematic of binary data.

(b) Possible ternary alloy combinations.

Figure 7. - Schematic representation of binary Mo data and possible ternary alloy combinations.

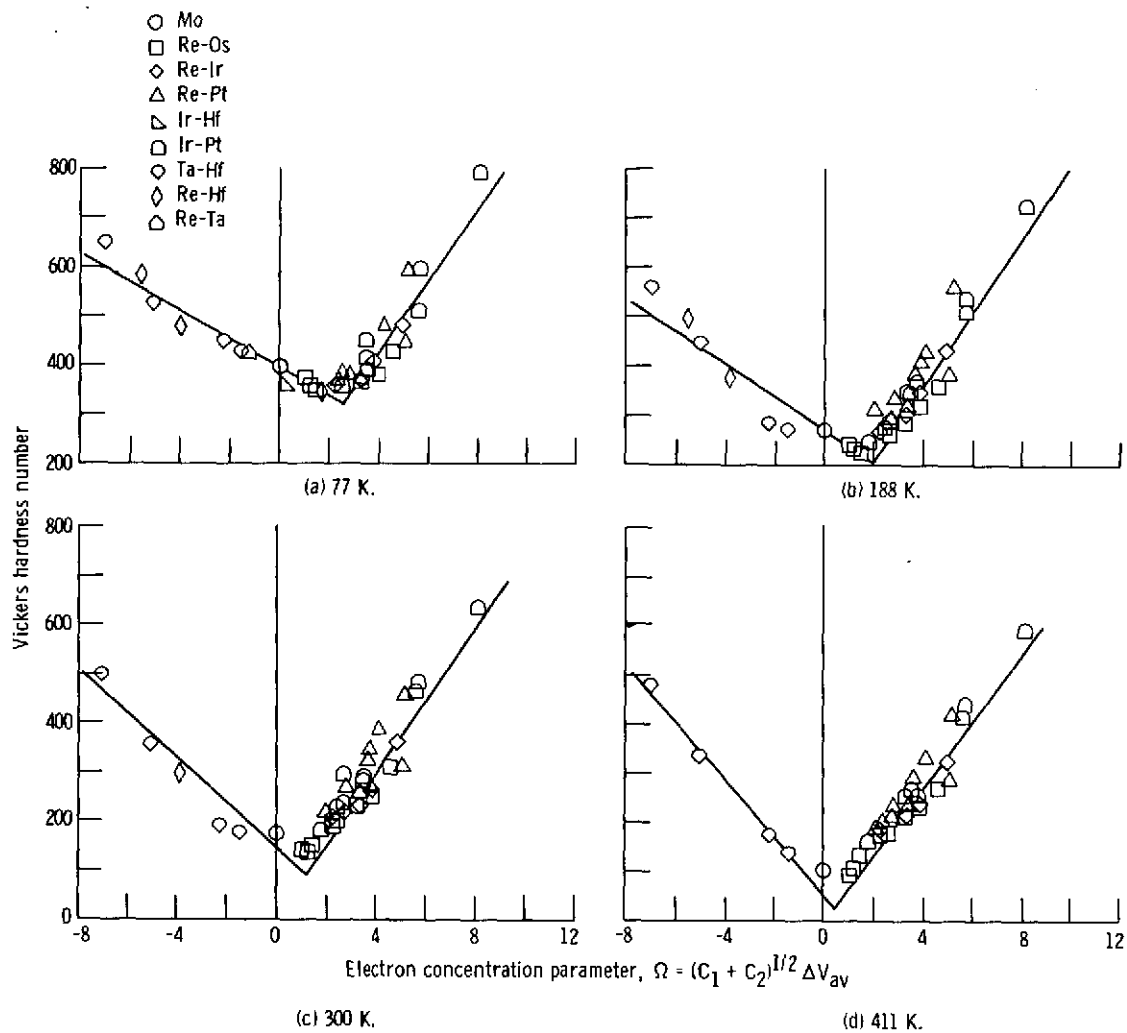


Figure 8. ~ Correlation of hardness of ternary Mo alloys with square root of total solute content and average difference in number of s and d electrons.

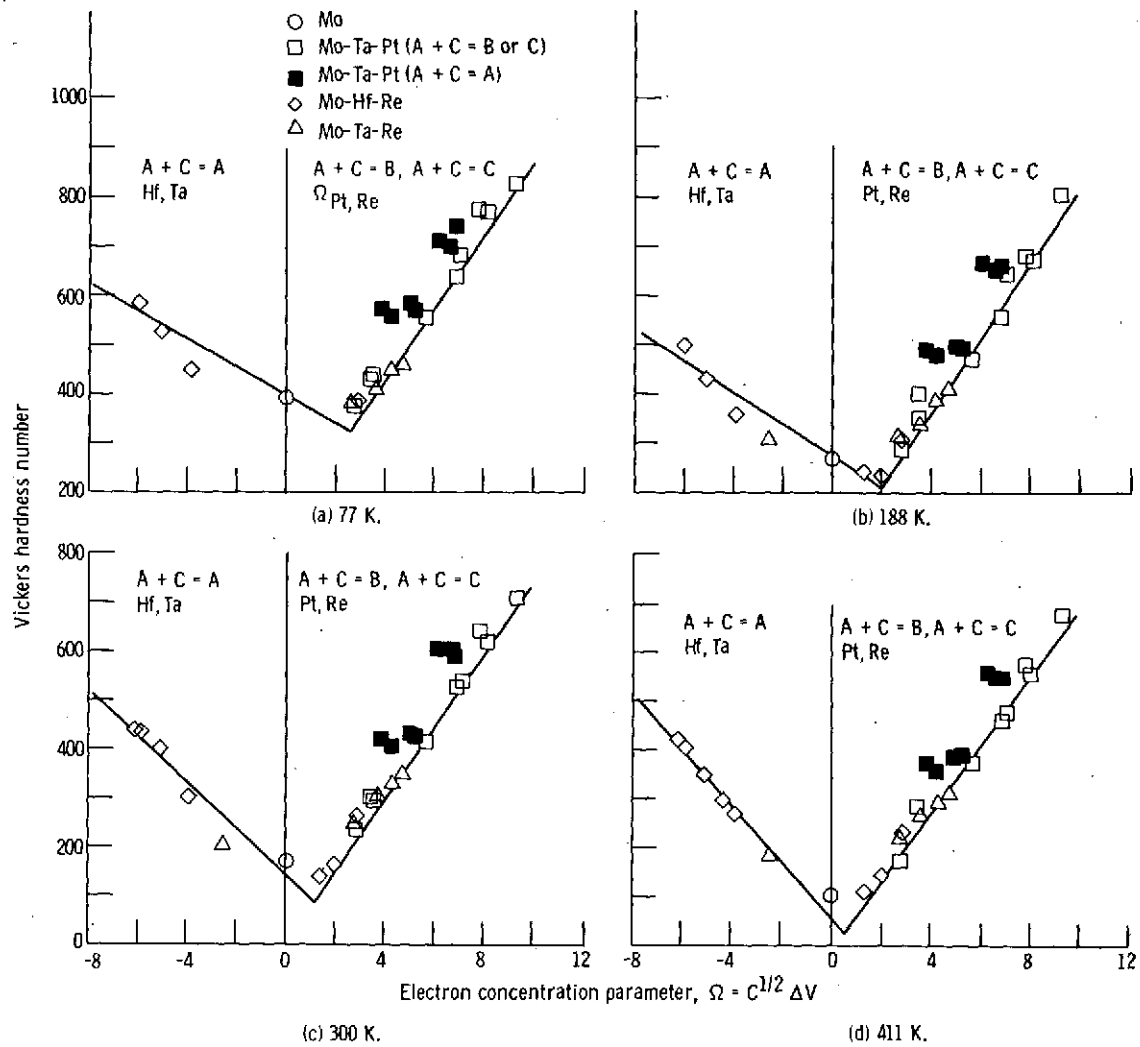


Figure 9. - Correlation of hardness of ternary Mo alloys, $A + C$ combinations, with square root of individual solute content and difference in number of s and d electrons.

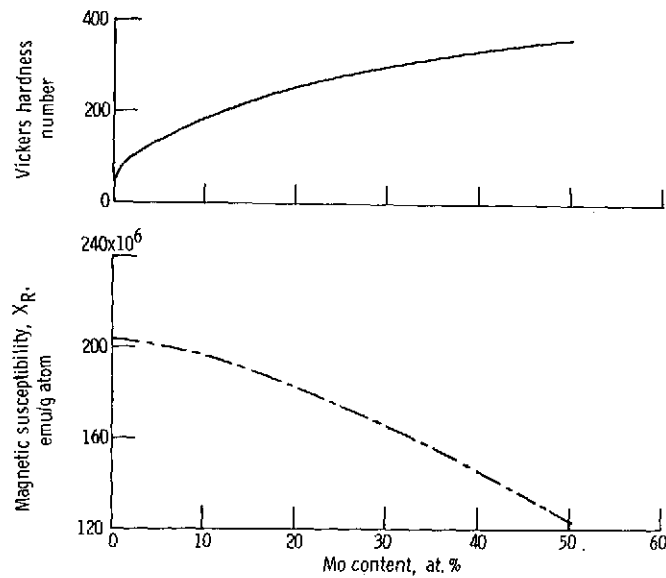
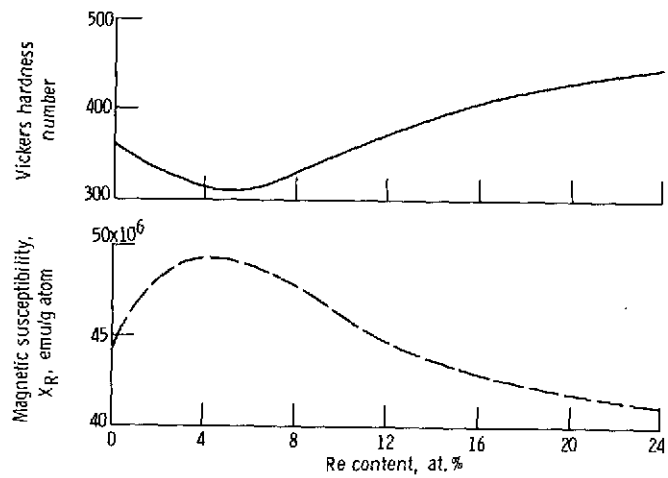
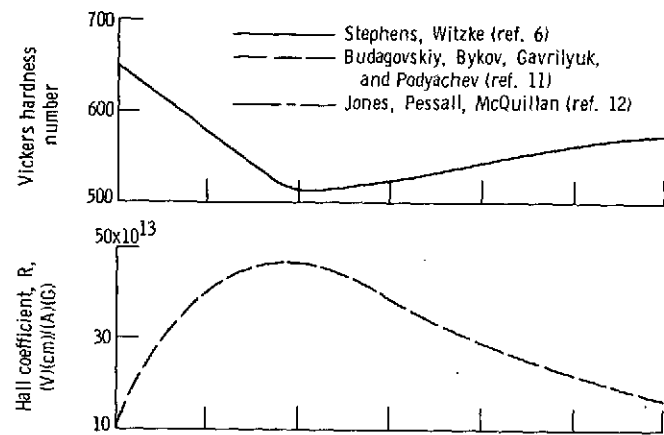


Figure 10. - Correlation of hardness of W-Re and Nb-Mo alloys with Hall coefficient and magnetic susceptibility measurements.