General Disclaimer

One or more of the Following Statements may affect this Document

- This document has been reproduced from the best copy furnished by the organizational source. It is being released in the interest of making available as much information as possible.

- This document may contain data, which exceeds the sheet parameters. It was furnished in this condition by the organizational source and is the best copy available.

- This document may contain tone-on-tone or color graphs, charts and/or pictures, which have been reproduced in black and white.

- This document is paginated as submitted by the original source.

- Portions of this document are not fully legible due to the historical nature of some of the material. However, it is the best reproduction available from the original submission.

THERMAL AND MECHANICAL STRUCTURE OF THE

UPPER MANTLE: A COMPARISON BETWEEN

CONTINENTAL AND OCEANIC MODELS

C. Froidevaux

Laboratoire de Physique des Solides*
Université Paris-Sud
Orsay, France 91405

G. Schubert and D. A. Yuen
Department of Geophysics and Space Physics
University of California
Los Angeles, California 90024

ABSTRACT

Temperature, velocity and viscosity profiles for coupled
thermal and mechanical models of the upper mantle beneath
continental shields and old ocean basins show that under
the continents, both tectonic plates and the asthenosphere,
are thicker than they are beneath the oceans. The minimum
value of viscosity in the continental asthenosphere is
about an order of magnitude larger than in the shear zone
beneath oceans. The shear stress or drag underneath con-
tinental plates is also approximately an order of magnitude
larger than the drag on oceanic plates. Effects of shear
heating may account for flattening of ocean floor topography
and heat flux in old ocean basins.

INTRODUCTION

Plate tectonics has stressed the importance of the con-
cepts of lithosphere, the rigid surface layer of the Earth
which is divided into a mosaic of moving plates, and of
asthenosphere, a softer layer under the plates facilitating
the mechanical decoupling with the lower mantle. The con-
cept of an asthenosphere was derived long ago from the study
of isostasy. On the other hand, the physical structure of
the upper mantle has been discussed either on the basis of
seismic velocity distributions derived from observations
(Press, 1972; Knopoff, 1972; Jordan, 1975), or on the basis
of purely thermal models (McKenzie, 1967; Sclater and Franche-
teau, 1970; Turcotte and Oxburgh, 1972). Both of these latter
approaches have led to the conclusion that the physical
structure is different under oceans and under continents.
It is, however, difficult to make quantitative comparisons
between seismological data and theoretical thermal profiles,
since this involves a precise description of the petrologi-
cal state of the mantle. For oceanic plates alone other
geophysical data like topography have been used to test
theoretical thermal models (Sorokhtin, 1973; Davis and Lister,
1974; Parsons and Sclater, 1975; Oldenburg, 1976). Convec-
tive models have not focused on the distinction between
oceanic and continental regions.

Here we present models of the upper mantle wherein
both the thermal and flow velocity profiles are calculated
on the basis of coupled thermal and mechanical equations
satisfying simple geophysical boundary conditions (Froidevaux
and Schubert, 1975; Schubert et al., 1976). This is illus-
trated in Figure 1 which shows the oceanic model on the
left, and the continental one on the right. The boundary
conditions indicated in the figure, are that the temper-
ature and horizontal velocity at the surface be T_o and u_o,
and that the horizontal velocity at great depth be zero.
In the continental case the heat flows at the surface q_o
and at great depth q_∞ are also imposed, whereas in the
oceanic case, the temperature at great depth T_∞ and the
vanishing of the vertical velocity at the surface are
specified. The physical quantities to be calculated are
also listed in the figure; they are temperature T, hori-
zontal velocity u, shear stress τ and viscosity, and, for
the oceanic case only, vertical velocity v. Except for
τ, these quantities vary with depth y. In the oceanic
case they all vary with horizontal distance from the ridge
x, i.e. with age x/u_o. Given a petrologic model of the
mantle, seismic velocity profiles can also be computed.

All models are based on the law of deformation of
olivine (Post, 1973; Kohlstedt et al., 1975)

$$\dot{\varepsilon} = \frac{B_3 \tau^3}{T} \exp\left(-\frac{E^* + pV^*}{RT}\right)$$ (1)

where T is the absolute temperature, p is the pressure,
$\dot{\varepsilon} \equiv \frac{1}{2} du/dy$ is the strain rate, and R is the gas constant.
The proportionality constant B_3 and the activation energy
E^* have been measured in the laboratory, whereas the acti-
vation volume V^* has to be estimated. The justification
for a model based on olivine is that this mineral is the
most abundant in the mantle and it deforms more readily
than other minerals in most mantle-derived peridotite
samples (Boullier and Nicolas, 1973). The coupling between
velocity and temperature comes about through the T-dependence
of (1) and through the viscous heating term $2\tau\dot{\varepsilon}$ in the
temperature equation. In the continental case the temper-
ature equation also contains a radioactive heating term Q_m
and a vertical conduction term. The continental mantle
is overlain by a crust divided in 2 layers. Radioactive
heat generation Q_1 in the upper 8 km is a given quantity,
whereas the volumetric heat production Q_2 for the 32 km
thick lower crust has to be calculated to satisfy the boun-
dary conditions. In the oceanic case the temperature equa-
tion contains both horizontal and vertical advection of
heat, vertical conduction of heat and viscous dissipation.
Since horizontal advection of heat is a dominant effect,
radioactive heating has been neglected in this presentation.
The vertical velocity in the oceanic model requires consider-
ation of another mechanical equation, the continuity equation.

These models imply a mechanical decoupling between the surface, moving at velocity u_o, and deeper regions. They do not fix, a priori, the depth of the shear zone nor the magnitude of τ. Since no return flow is assumed at shallow depth, the momentum equation simply states that τ is independent of y; in the oceanic case it will however vary with x, the horizontal coordinate or age.

The system of equations just described contains no time dependence. The models should thus apply in regions where steady state might exist. We assume this to be the case for oceans and for old shields (Polyak and Smirnov, 1968). The quasi-equality of heat flow for old continental shields and old ocean basins has been considered a paradox. Our models should tell us something about this problem. They should also lead to an interesting comparison of the lithosphere-asthenosphere structures of both regions. Such comparisons will be presented in section 3, after the most striking characteristics of the models have been reviewed for continents in section 1 and for oceans in section 2. Further details and mathematical formulations are given in Froidevaux and Schubert (1975) and Schubert et al. (1976).

1. TEMPERATURE AND VELOCITY UNDER OLD CONTINENTAL SHIELDS

The values of the rheological parameters in (1) depend
on the amount of volatiles, particularly water, present in
the mantle (Carter and Avé Lallemant, 1970; Stocker and Ashby,
1973). It is therefore useful to test the behavior of our
thermo-mechanical model when B_3, E^* and V^* have values ap-
propriate to wet or dry olivine. This is illustrated in Figure
2, where solutions are drawn for extreme values of V^* (11 and
30 cm^3/mole) for a continental system with mantle radioactivity
but without heat flow from great depth. The hatched areas in
Figure 2 indicate the range of solutions for intermediate val-
ues of V^*. Other parameter values are listed in the figure
caption. The temperature rises monotonically to a final value
depending mainly upon V^*. This dependence reflects the con-
tribution of shear heating to the thermal state. The velocity
drops from its surface value, 5 cm/yr, to zero in a shear
zone or asthenosphere beneath the rigid plate or lithosphere.
The depth of the shear zone is shallow or the lithosphere is
thin when the pressure dependence in (1) is strong, i.e. when
V^* is large. A larger activation volume also yields a thinner
asthenosphere. These characteristics are shown by the dotted
bands representing the shear zones for the various solutions.
The temperature and velocity profiles are relatively insensi-
tive to whether the mantle is wet or dry. One remarkable
property of all these solutions, is that the viscosity reaches

about the same minimum value of 10^{21} poise in the shear zone, or asthenosphere. Thermo-mechanical coupling leads to self-adjustment of the temperature and of the depth of the asthenosphere, so that the values of the rheological parameters do not influence the value of the viscosity minimum.

What variables in our continental models have a major influence on the viscosity value in the asthenosphere? There are two: the amount of radioactive heat sources in the mantle and the plate velocity. The effects of radiogenic heating in the mantle Q_m are seen in Figure 3 which presents continental solutions for u_o = 2 cm/yr with Q_m = 0 HGU and Q_m = 0.06 HGU (1 HGU = 10^{-13} cal/cm^3 sec). The addition of radioactivity raises the temperature at all depths, moves the asthenosphere upward and reduces the value of the minimum viscosity by an order of magnitude. By comparing solutions in Figures 2 and 3 for V^* = 11 cm^3/mole and Q_m = 0.06 HGU one finds that an increase in plate velocity from 2 to 5 cm/yr lowers the viscosity by another factor of 4. The viscosity profile for V^* = 11 cm^3/mole, Q_m = 0.06 HGU and u_o = 5 cm/yr is shown as the dashed curve in Figure 3. The computed shear stress τ, i.e. the drag under the continental plate, also decreases with increases in mantle radioactivity and plate velocity. For the cases in Figure 3 with u_o = 2 cm/yr, the τ values are 114 bars for Q_m = 0 HGU and 27.2 bars for Q_m = 0.06 HGU; in the latter case τ drops to 17.1 bars when u_o is increased to 5 cm/yr. This decrease of τ with u_o is not as

strong as that found by Froidevaux and Schubert (1975) in situations where viscous heating was the dominant effect in the mantle and τu_o was almost constant in the velocity range investigated.

Comparisons with the Earth have been attempted and the results are shown in Figure 4. Since the activation volume is not known we imposed an additional constraint on the model, namely that the geotherm is required to pass through the data points (shaded areas in Figure 4) derived from phase equilibria in kimberlite nodules from the South-African shield (Boyd, 1973; MacGregor and Basu, 1974). Only the unperturbed branch (Green and Guéguen, 1974) of this experimentally determined geotherm is used. Solutions for wet (Post, 1973) and dry (Kohlstedt and Goetze, 1974) olivine rheological parameters are obtained with $q_\infty = 0.1$ HFU, the imposed heat flow from the deep mantle. This value of q_∞ corresponds to an estimate of the adiabatic temperature gradient. The temperature solutions in Figure 4, which approximately satisfy the nodule data, are relatively insensitive to the value of the activation volume. Thus the model geotherms alone do not provide much of a constraint on the value of V^*. However, since the sheared nodules in kimberlites are thought to originate at depths of about 180 km or somewhat deeper (Boullier and Nicolas, 1973), one can use the depth of the shear zone in the model solutions as an additional constraint on acceptable models and appropriate values of V^*.

For wet olivine, a V^* between 20 and 28 cm^3/mole would give models with acceptable temperatures and shear zones starting at depths between about 225 km and 180 km, respectively. For dry olivine, no solutions could be found which simultaneously satisfied the constraints in both temperature and depth to the top of the shear zone (depth at which $u/u_o = 0.95$). In the case of dry olivine V^* values of 16 and 20 cm^3/mole yield models with shear zones starting at depths of about 305 km and 260 km, respectively.

The viscosity minima for both the wet and dry solutions have values of about 10^{21} poise. The shear stresses for these solutions are abo _ 80 bars, in agreement with values proposed by Goetze and Kohlstedt (1973) on the basis of dislocation studies in mantle derived peridotite nodules. The heat generation values Q_2 in the lower crust range from 0.75 to 0.8 HGU, about 40% to 35% lower than averaged values for gabbro. In these solutions, the granitic upper crustal layer had $Q_1 = 5$ HGU and $Q_m = 0.06$ HGU was specified for the mantle down to 500 km depth.

In conclusion, if a steady state regime is assumed to exist under old continental shields, our coupled thermomechanical model is capable of satisfactorily predicting the physical structure of the upper mantle. The finite thickness asthenosphere underlying the rigid lithosphere is a consequence of the strong T and p dependences of the mechanical constitutive equation (1). Under old continents the

depth of the asthenosphere is determined mainly by V^*, whereas its 'softness' is essentially governed by Q_m and u_o. Shear wave velocity profiles computed on the basis of solid state data for pure olivine and our model geotherms are flat. This agrees with seismological data and emphasizes that the seismological low velocity zone, which does not exist under old continental shields, is not equivalent to the shear zone or asthenosphere.

2.   TEMPERATURE AND VELOCITY UNDER OLD OCEANIC BASINS

For oceanic plate models, the two-dimensional flow field
u and v and temperature profile depend not only upon depth but
also upon distance from the ridge as pictured in Figure 1.
The boundary conditions do not include the surface heat flow,
since this quantity is not well known. Instead we have im-
posed the temperature T_∞ at great depth. This quantity is
not known either, so that several values between $1200^\circ C$ and $1600^\circ C$ have
been used. This boundary condition has the advantage of
making a comparison with purely thermal models simple. All
models in this and the remaining parts of the paper are based
upon a dry olivine rheology.

The temperature profiles are dominated by heat advection,
i.e. by lithospheric and asthenospheric cooling. This is
particularly true for high T_∞ values and slow plates. For a
rather cool asymptotic temperature $T_\infty = 1200^\circ C$ and a high
plate velocity $u_0 = 10$ cm/yr, Figure 5 shows solutions for 2
ages, 10 and 150 My. For 10 My the T profile is almost ident-
ical to the purely thermal solution calculated for the same
variable thermal conductivity (dotted curve). The velocity
profiles u (y) and v (y) are seen to depend on the value of
V^*; the shear zone is shallower when V^* is large, as was
found in the continental models. In Figure 5 the hatched
areas indicate again the range of solutions for intermediate

values of V^*. The viscosity minimum is less than 10^{21} poise, for $T_\infty = 1600^\circ C$ it drops below 10^{20} poise. The vertical velocity v increases from zero to an asymptotic value in the region where the horizontal velocity drops to zero, i.e. in the asthenosphere. The finite value of v at great depth provides a mass flow necessary for the accretion of the thickening lithosphere. For an age of 150 My Figure 5 shows that the temperature profile departs strongly from the purely thermal cooling solution (dotted curve). This is due to shear heating, an effect which is stronger for larger values of V^*. The viscosity in the asthenosphere is somewhat higher beneath old oceans. At 150 My the upward velocities are an order of magnitude smaller than at 10 My.

Shear heating generates marked departures from a simple $\sqrt{age}$ dependence for derived quantities like lithosphere thickness, topography and heat flow. This is illustrated in Figure 6 for the first two of these geophysical quantities. The lithosphere thickness, defined as the depth at which u falls to 95% of the surface value u_o, increases with age, but not as fast as a $\sqrt{age}$ law which would yield a straight line on this plot. As mentioned earlier the thickness is smaller for larger V^* values. For each value of V^* the upper and lower curves correspond to u_o values of 10 cm/yr and 2 cm/yr, respectively. Shear heating is stronger for larger u_o values; consequently the lithospheric plate is somewhat thinner. The

topography of the ocean floor represented in Figure 6
by the water-depth also departs from a $\sqrt{age}$ law indicated
by the dashed straight line. The departure is very
pronounced for $V^* = 30$ cm^3/mole. The experimental
points redrawn from Parsons and Sclater (1975) could be
fitted for a V^* value just above 11 cm^3/mole. This
topography model reflects the gradual cooling of the lith-
osphere and asthenosphere; it was computed for a thermal
expansion coefficient $\alpha = 4\times10^{-5}$ K^{-1}. No data is avail-
able for the lithospheric thickness as defined here. The
depth of origin of sheared peridotite nodules might in
the future give some constraints. For now we can only
say that the depth to the seismic low velocity zone infer-
red from surface and body wave data increases monotonically
up to ages as old as 150 My (Leeds, 1975; Sipkin and
Jordan, 1976). The ocean floor heat flow data, on the
other hand are too controversial to warrant a detailed
comparison. Our models of q_0 for $T_\infty = 1200^\circ$C also show
a certain amount of flattening, i.e., a departure from
an (age)$^{-1/2}$ proportionality for heat flow. Viscous
dissipation provides additional heat to the old ocean floor.
Stress values increase by factors of 2 to 5 for the cases
shown above as age increases. They are less than 80 bars
for solutions based on the rheology of dry olivine. For a
wet olivine rheology, stresses and shear heating effects
are reduced by factors of 2 to 3. They are also reduced for
larger T_∞ values, $T_\infty = 1200^\circ$C being the value applicable to

Figures 5 and 6.

In summary, for young ages thermo-mechanical coupling
beneath oceans is negligible and the T profiles are close
to the solutions for simple boundary layer cooling. Note
however that although the isotherms for such purely thermal
solutions are parabolic, they would not yield a parabolic
lithosphere because of the pressure depend nce of the vis-
cosity implied by equation (1). A second point to emphasize
is that departures from $\sqrt{age}$ laws at old ages are a result
of distortion of the geotherms by shear heating. This ex-
planation of known geophysical behavior (see topography) is
more satisfactory than that based on the ad hoc representa-
tion of the lithosphere by a slab of constant thickness
(Parsons and Sclater, 1975). The stage is now set for a
comparison of continents and oceans.

3. A DIRECT COMPARISON OF CONTINENTAL AND OCEANIC MODELS
   BASED ON A DRY OLIVINE RHEOLOGY.

So far we have shown that the one-dimensional flow field
under old continental shields, as well as the two-dimensional
flow field under oceanic plates, and their associated temper-
ature fields can be modelled on the basis of simple geophysical
boundary conditions and physical properties corresponding to
the thermal conductivity and rheology of olivine as measured
in the laboratory.

A comparison of the situations under old continents and
under old oceanic basins can be undertaken. This requires
an appropriate matching of boundary conditions. We shall pro-
ceed in the following way. First we take $T_o = 0^o C$, $q_o = 1.05$
HFU (1HFU = 10^{-6} cal/cm^2 sec) for continental shields and
compute solutions corresponding to $q_\infty = 0$ HFU. This yields
a computed temperature T_∞ at great depth under old continents.
We then compute oceanic solutions for the same T_o and T_∞
values, and of course for the same surface velocity u_o. All
this is carried out under the assumption that mantle rheo-
logical properties are identical to those of dry olivine
and are the same under ocean basins and under continental
shields. Since the activation volume V^* has not been measured
in the laboratory, we present solutions for $11 \leq V^* \leq 30$ cm^3/mole.

In the oceanic models, where horizontal and vertical ad-

vection of heat dominates, we shall neglect the thin basaltic crust as well as mantle radioactivity. However the continental models not only include a radioactive crust with $Q_1 = 5$ HGU and a lower crust with a Q_2 value which has to be computed, but also a radioactive upper mantle with $Q_m = 0.06$ HGU, a reasonable average value. We realize that the true value of Q_m is not well determined; for example Sorokhtin (1974) has argued that its value could be zero. In any case, although the specific comparison discussed here is based on a continental model with nonzero Q_m we can use the results of Figure 3 to infer the effect of a smaller or zero value of Q_m beneath continents. Shear heating is, of course, included in both oceanic and continental models.

Figure 7 gives continental and oceanic solutions for $u_o = 2$ cm/yr. For $V^* = 11$ cm^3/mole and 30 cm^3/mole, the continental solutions have $T_\infty = 1392$ $^\circ$C, $Q_2 = 1.04$ HGU and $T_\infty = 1665$ $^\circ$C, $Q_2 = 0.59$ HGU, respectively. The corresponding oceanic geotherms for an age of 150 My have surface heat flow values of 0.82 and 0.98 HGU, respectively. Both the surface heat flows in the oceanic cases and the lower continental crustal radioactivity have reasonable values when compared with geophysical and geochemical data.

What are the most striking points emerging from a comparison of the solutions in Figure 7? Firstly, we see that the oceanic geotherm is everywhere higher than the corres-

ponding continental one and thus has a much steeper grad-
ient at shallow depths. This is basically due to the exist-
ence of a thick radioactive crust for the continents. As
a consequence the lithospheric thickness is larger under
continental shields than under old oceanic basins. This is
pictured by the position of the top boundary of the dotted
bands representing the depth range of the asthenosphere
(defined by $0.05 \leq u/u_o \leq 0.95$). The asthenosphere beneath
continents is thicker than that under oceans. The value of
the viscosity minimum in the continental asthenosphere is
essentially an order of magnitude larger than that in the
oceanic shear zone. Similarly the drag under the continental
plate is about an order of magnitude larger than that beneath
the oceanic plate. The drag is given by the computed value
of shear stress τ which is 4.9 and 27.2 bars for the oceanic
and continental cases, respectively, when $V^* = 11$ cm^3/mole;
corresponding τ values for $V^* = 30$ cm^3/mole are 10.7 and
124 bars. These results compare favorably with those of
Forsyth and Uyeda (1975) and Solomon et al. (1975) who
suggest a larger drag under continental plates on the basis
of analyses of plate motions.

To discuss the relative importance of the various heat
sources beneath the oceans and continents we have constructed
Table 1 from the solutions of Figure 7. In order to make
vertical heat advection into the oceanic lithosphere negligible

we now define the base of the oceanic lithosphere as the depth for which $u = 0.995\ u_o$. For consistency we apply the same definition of lithospheric base to the continental case, even though there is no advection in the continental models. Given this definition we can read the entries in Table 1 for lithospheric thickness and sublithospheric temperature directly from Figure 7. The heat flux into the base of the lithosphere, q_L, is computed as the product of thermal conductivity and temperature gradient at the appropriate depth from the detailed solutions. The difference between surface heat flow q_o and q_L is either the contribution of lithosphere radioactivity to q_o in the continental case or the contribution of horizontal advection to q_o in the oceanic case.

Table 1 shows that a substantial fraction (1/3 to 2/3) of the surface heat flow in the old ocean floor comes from the cooling of the lithosphere as it thickens and moves away from the ridge. The remainder of the surface heat flow derives from asthenospheric cooling, vertical advection, and viscous dissipation τu_o. The source of the continental surface heat flux is radiogenic heating in the crust (55 to 70%) and in the mantle (26%), and viscous dissipation (19 to 4%).

Sclater and Francheteau's (1970) purely conductive model of the oceanic lithosphere does not include advection of heat. Our results show that this is still important even for an age of 150 My and must be included when the "equality"

of heat flow between continental shields and oceanic basins
is discussed. One should notice finally that the sub-astheno-
spheric temperature is considerably higher (200-400°C) than
the temperature just under the plates. In the literature
these 2 quantities are often indiscriminately equated, just
as the constant thickness slab introduced by McKenzie (1967)
for mathematical convenience is often presented as the lith-
osphere.

CONCLUDING REMARKS

This paper has shown that it is possible to construct satisfactory models of the upper mantle beneath both continents and oceans. Under the oceans, the plates are found to be thinner, the asthenosphere softer and hence the drag smaller than under the continents. The comparison of continental and oceanic models with each other and with the real earth would be improved by including radioactivity under the oceans and by accounting for a nonzero heat flux from great depth. Further improvement would require additional data on possible lateral heterogeneities in the distribution of radioactive heat sources and in the rheological properties of the mantle.

ACKNOWLEDGMENT

REFERENCES

Boyd, F. R., A pyroxene geotherm, Geochim. et Cosmochim. Acta, 37, 2533-2546, 1973.

Boullier, A. M., and A. Nicolas, Texture and fabric of peridotite nodules from kimberlites, in Lesotho Kimberlites, edited by P. H. Nixon, pp. 57-66, Lesotho National Dev. Corp., Maseru, 1973.

Carter, N. L., and H. G. Avé Lallemant, High temperature flow of dunite and peridotite, Geol. Soc. of America Bulletin, 81, 2181-2202, 1970.

Davis, E. E. and C. R. B. Lister, Fundamentals of ridge crest topography, Earth Planet. Sci. Lett., 21, 405-413, 1974.

Forsyth, D. and S. Uyeda, On the relative importance of the driving forces of plate motion, Geophys. J. Roy. Astron. Soc., 43, 163-200, 1975.

Froidevaux, C. and G. Schubert, Plate motion and structure of the continental asthenosphere: A realistic model of the upper mantle, J. Geophys. Res., 80, 2553-2564, 1975.

Goetze, C., and D. L. Kohlstedt, Laboratory study of dislocation climb and diffusion in olivine, J. Geophys. Res., 78, 5961-5971, 1973.

Green, H. W. II., and Y. Gueguen, Origin of kimberlite pipes by diapiric upwelling in the upper mantle, Nature, 249, 617-620, 1974.

Jordan, T. H., The continental tectosphere, Rev. Geophys. Space Phys., 13, 1-12, 1975.

Knopoff, L., Observation and inversion of surface wave
dispersion, Tectonophysics, 13, 497-519, 1972.

Kohlstedt, D. L. and C. Goetze, Low Stress, High Temperature
Creep in Olivine Single Crystals, J. Geophys. Res., 79,
2045-2051, 1974.

Kohlstedt, D. L., C. Goetze and W. B. Durham, Experimental
deformation of single crystal olivine with application
to flow in the mantle, Proc. 1974 NATO Conf. on Petrophysics,
Newcastle-upon Tyne, in press, 1975.

Leeds, A. R., Lithospheric thickness in the western Pacific,
Phys. Earth Planet. Interiors, 11, 61-64,
1975.

MacGregor, I. D., and A. R. Basu, Thermal structure of the
lithosphere; a petrologic contribution, Science, 185,
1007-1011, 1974.

McKenzie, D. P., Some remarks on heat flow and gravity
anomalies, J. Geophys. Res., 72, 6261-6273, 1967.

Oldenburg, D. W., A Physical Model for the Creation of the
Lithosphere, in press, Geophys. J. Roy. Astr. Soc.,
1976.

Parsons, B. and J. G. Sclater, An analysis of the variation
of ocean floor heat flow and bathymetry with age, sub-
mitted to Geophys. J. Roy. Astron. Soc., 1975.

Polyak, B. G. and Y. B. Smirnov, Relationship between heat
flow and the tectonics of continents, Geotectonics, 4,
205-213, 1968.

Post, R. L., The flow laws of Mount Burnett dunite, Ph.D. thesis, Univ. of Calif., Los Angeles, 1973.

Press, F., The earth's interior as inferred from a family of models, in The Nature of the Solid Earth, edited by E. C. Robertson, pp. 147-171, McGraw-Hill, New York, 1972.

Schatz, J. F. and G. Simmons, Thermal conductivity of earth materials at high temperatures, J. Geophys. Res., 77, 6966-6983, 1972.

Schubert, G., C. Froidevaux and D. A. Yuen, Oceanic lithosphere and asthenosphere: thermal and mechanical structure, submitted to J. Geophys. Res., 1976.

Sclater, J. G. and J. Francheteau, The implication of terrestrial heat flow observations on current tectonic and geochemical models of the crust and upper mantle of the earth, Geophys. J. Roy. Astro. Soc., 20, 509-537, 1970.

Sclater, J. G., New perspectives in terrestrial heat flow, Tectonophysics, 13, 257-291, 1972.

Sipkin, S. A. and T. H. Jordan, Lateral heterogeneity of the upper mantle determined from travel times of multiple ScS, submitted to J. Geophys. Res., 1976.

Solomon, S. C., N. H. Sleep and R. M. Richardson, On the forces driving plate tectonics: Inferences from absolute plate velocities and intraplate stress, Geophys. J. Roy. Astr. Soc., 42, 769-803, 1975.

Sorokhtin, O. G., Global Evolution of the Earth (in Russian), "Science" edition, Moscow, 1974.

Stocker, R. L., and M. F. Ashby, on the rheology of the upper mantle, Reviews of Geophys. and Space Phys., 11, 391-426, 1973.

Turcotte, D. L. and E. R. Oxburgh, Mantle convection and the new global tectonics, Ann. Rev. Fluid Mech., 4, 33-68, 1972.

	$V^* = 11$ cm^3/mole		$V^* = 20$ cm^3/mole	
	Ocean (150 My)	Continent	Ocean (150 My)	Continent
Lithospheric thickness L (km)	140	245	95	185
Sublithospheric temperature T_L (°C)	1225	1185	1190	1260
Temperature below the asthenosphere T_∞ (°C)	1392	1392	1665	1665
Heat Flux into the lithosphere q_L (HFU)	0.28	0.19	0.63	0.37
Contribution of lithosphere radio-activity to q_o (HFU)	-	0.86	-	0.68
Contribution of advection to q_o (HFU)	0.54	-	0.35	-
Surface heat flow q_o (HFU)	0.82	1.05	0.98	1.05
Contribution of shear heating τu_o to q_L (HFU)	0.0074	0.041	0.016	0.19

Table 1. Comparison of thermal states under old oceans and continental shields.

FIGURE CAPTIONS

Figure 1. Oceanic (left) and continental (right) models.
The boundary between lithosphere and astheno-
sphere appears to be sharp for artistic reasons
only; its depth is not a specified parameter.
For the oceanic case the temperature T_o, hori-
zontal and vertical velocities u_o and v_o at
the surface, as well as the temperature T_∞
and the zero horizontal velocity $u = o$ at
great depth are given as boundary conditions.
For the continental case the boundary conditions
are the temperature T_o, the velocity u_o and the
heat flow q_o at the surface, as well as the
heat flow q_∞ and zero velocity $u = o$ at great
depth. The continental mantle has a volumetric
radiogenic heat-source Q_m. It is overlain by
a crust with thermal conductivity k_c. The
crust has an 8 km upper layer with radiogenic
heat sources Q_1 and a 32 km lower layer with
unspecified radiogenic heat sources Q_2. The
quantities listed on the right hand side of
both the oceanic and continental diagrams are
those to be computed.

Figure 2. Temperature and velocity profiles for a wet and a dry olivine continental mantle containing radioactive heat sources. The parameter values for the wet case are $B_3 = 5.41 \times 10^{-15}$ cm$^3\frac{sec^5K}{gm^3}$, $E^* = 95$ kilocal/mole (Post, 1973), and for the dry case $B_3 = 6.45 \times 10^{-13}$ cm$^3\frac{sec^5K}{gm^3}$, $E^* = 125$ kilocal/mole (Kohlstedt and Goetze, 1974). The activation volume V^* was 11 or 30 cm^3/mole and the corresponding solutions are labelled accordingly. The hatched area indicates the range of solutions for intermediate values of V^*. In all of these figures, the mantle thermal conductivity model $k_m(T,z)$ of Schatz and Simmons (1972) is used. The continental crust has a top layer of 8 km with $Q_1 = 5$ HGU and a bottom layer of 32 km with the computed Q_2 value quoted in the text. The mantle radioactivity content $Q_m = 0.05$ HGU is specified down to 500 km depth. Boundary conditions are $T_o = 0$ ^oC, $q_o = 1.05$ HFU, $u_o = 5$ cm/yr, $q_\infty = 0$ HFU. The computed shear stress τ is 9.3 bars ($V^* = 11$ cm^3/mole) or 50.9 bars ($V^* = 30$ cm^3/mole) for the wet case, and 17.1 bars ($V^* = 11$ cm^3/mole) or 63.2 bars ($V^* = 30$ cm^3/mole) for the dry case. The dotted bands indicate the depth range of the asthenosphere for a particular value of V^* in cm^3/mole.

The asthenosphere is defined as the depth range between $u = 0.95\ u_o$ and $u = 0.05\ u_o$.

Figure 3.   Temperature, velocity, and viscosity profiles for a dry olivine, continental mantle. $Q_m = 0.0$ HGU or 0.06 HGU, $V^* = 11\ cm^3\ mole^{-1}$, $u_o = 2\ cm\ yr^{-1}$, and $q_\infty = 0.0$ HFU. For the models with mantle radio-activity, the heat sources extend down to 500 km depth. The computed shear stresses are 27.2 bars ($Q_m = 0.06$ HGU) and 114 bars ($Q_m = 0.0$ HGU). The dashed curve is the viscosity profile for $V^* = 11\ cm^3/mole$, $Q_m = 0.06$ HGU and $u_o = 5\ cm/yr$ ($\tau = 17.1$ bars).

Figure 4.   'Realistic' models of the upper mantle beneath continental shields. The shaded region delineates the approximate range of the pyroxene geotherms (MacGregor and Basu, 1974). Computed models of the thermal and mechanical structures are shown for a range of activation volumes for wet and dry olivine. Geotherms satisfying the paleotemper-atures are relatively insensitive to the value of activation volume. An additional mechanical constraint based on the interpretation of sheared nodules (Boullier and Nicolas, 1973) is imposed on the depth of the top of the shear zone. For

wet olivine and q_∞ = 0.1 HFU, the activation

volumes for the solutions which best satisfy

<u>both</u> the thermal and mechanical constraints

lie between 20 and 28 cm^3 $mole^{-1}$. For dry

olivine acceptable solutions could not be

found. The computed shear stresses are 88.8

bars (V^* = 28 cm^3/mole), 71.9 bars (V^* = 20

cm^3/mole), 62.5 bars (V^* = 6 cm^3/mole) for

wet olivine, and 88.1 bars (V^* = 20 cm^3/mole)

and 62.4 bars (V^* = 4 cm^3/mole) for dry olivine.

Figure 5. Temperature, viscosity, horizontal and vertical

velocity fields of an oceanic lithosphere and

asthenosphere model for a dry olivine rheology.

T_∞ = 1200°C and u_o = 10 cm yr^{-1}. Solutions

are shown for two extreme values of V^*, 11 and

30 cm^3 $mole^{-1}$, and for two ages, 10 and 150 My.

They are indicated in the figure by the numbers

adjacent to the curves. For an age of 10 My,

temperature profiles are insensitive, at the

accuracy of our graph, to the value of V^*.

This is not so for the velocity curves. The

shaded area between two such curves represents

the range of solutions for intermediate values

of V^*. For an age of 150 My the temperature

profiles depend on V^*. The upper curve is for

$v^* = 30$ cm^3 mole^{-1} and the lower one is for
$v^* = 11$ cm^3 mole^{-1}. The dotted curves denote
the temperature profiles for simple boundary
layer cooling with variable thermal conduct-
ivity. The conduction solution for 10 My is
similar to the $v^* = 11$ cm^3 mole^{-1} and $v^* = 30$
cm^3 mole^{-1} curves. The stresses developed in
these oceanic models are 11.8 bars ($v^* = 11$ cm^3/mole),
34.0 bars ($v^* = 30$ cm^3/mole) for 10 My and 25.8
bars ($v^* = 11$ cm^3/mole), 75.5 bars ($v^* = 30$ cm^3/mole)
for 150 My.

Figure 6. Bathymetry of the ocean floor and lithospheric
thickness (depth at which $u/u_0 = 0.95$) as a
function of (age)$^{1/2}$ for a dry olivine rheology
with $T_\infty = 1200^\circ$C, and $v^* = 11$ and 30 cm^3 mole^{-1}.
For the depth of water plot, $u_0 = 10$ cm yr^{-1}
and $\alpha = 4 \times 10^{-5}$ K^{-1}. The shaded region represents
the bathymetry solutions for intermediate values
of v^*. The dashed lines are the ocean floor
depths for simple boundary layer cooling. The
data points are taken from Parsons and Sclater
(1975). For the thickness of the lithosphere
curves, the value of u_0 distinguishes the solid
curves with the same value of v^*; the thicker
lithosphere is for $u_0 = 2$ cm yr^{-1}, the thinner

one is for $u_o = 10$ cm yr^{-1}.

Figure 7.   A comparison of the thermal and mechanical

structures between old oceanic basins (150 My)

and continental shields. Dry olivine rheology,

$u_o = 2$ cm yr^{-1}, $q_\infty = 0.0$ HFU and equal asymptotic

temperatures, T_∞, are required for both tectonic

models. $Q_m = 0.06$ HGU is specified for the

continental mantles down to 500 km depth. The

effect of an increase in V^* is greater on con-

tinental models, which decouple at a greater

depth than the oceanic ones. The viscosity

minima for the oceanic cases are an order of

magnitude lower than the continental values.

The stresses in the continental cases (124.0

bars, $V^* = 30$ cm^3 $mole^{-1}$; 27.2 bars, $V^* = 11$

cm^3 $mole^{-1}$) are an order of magnitude greater

than those found for the oceanic solutions

(10.7 bars, $V^* = 30$ cm^3 $mole^{-1}$; 4.9 bars,

$V^* = 11$ cm^3 $mole^{-1}$).

Fig. 1

Fig. 2
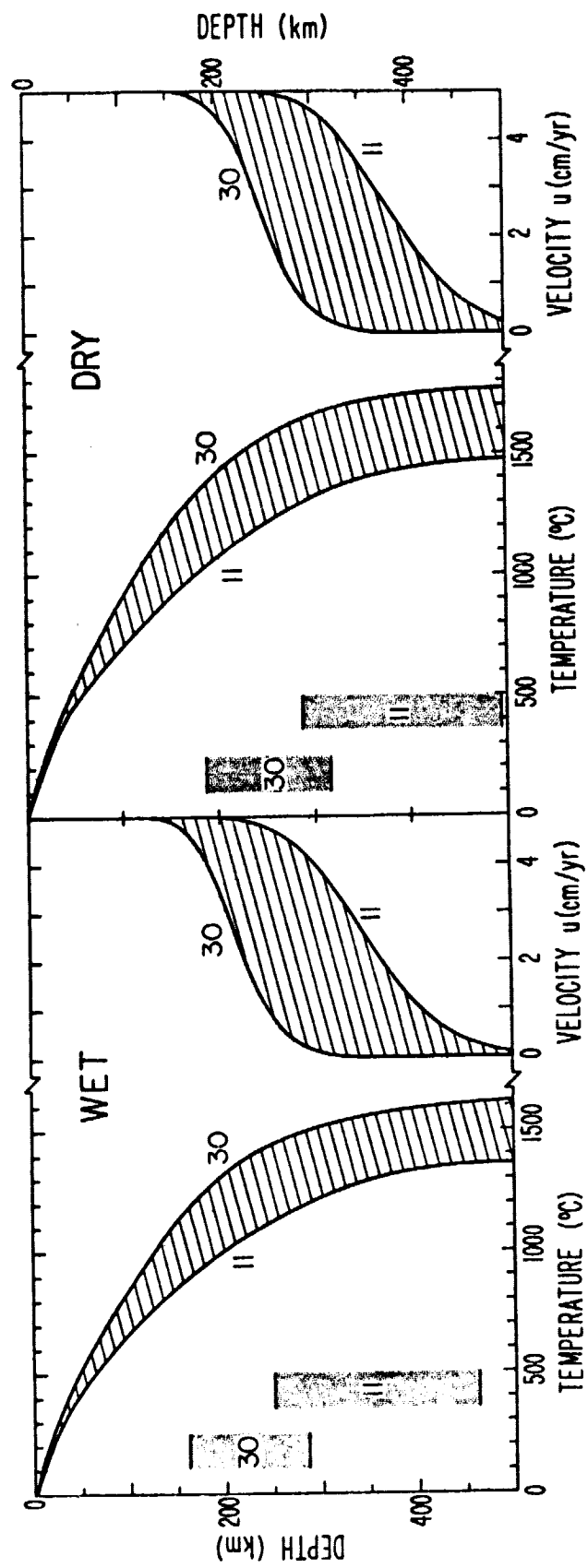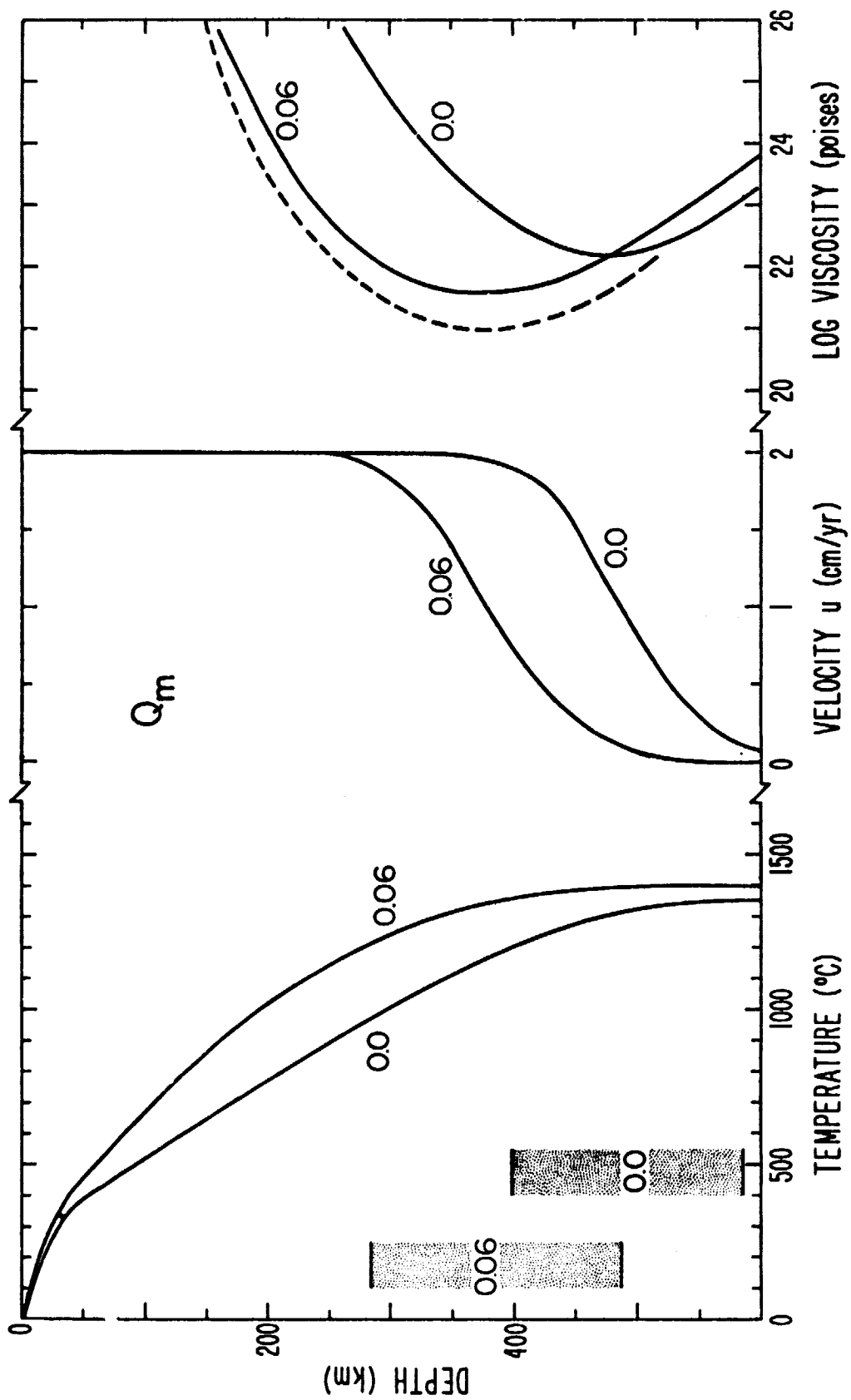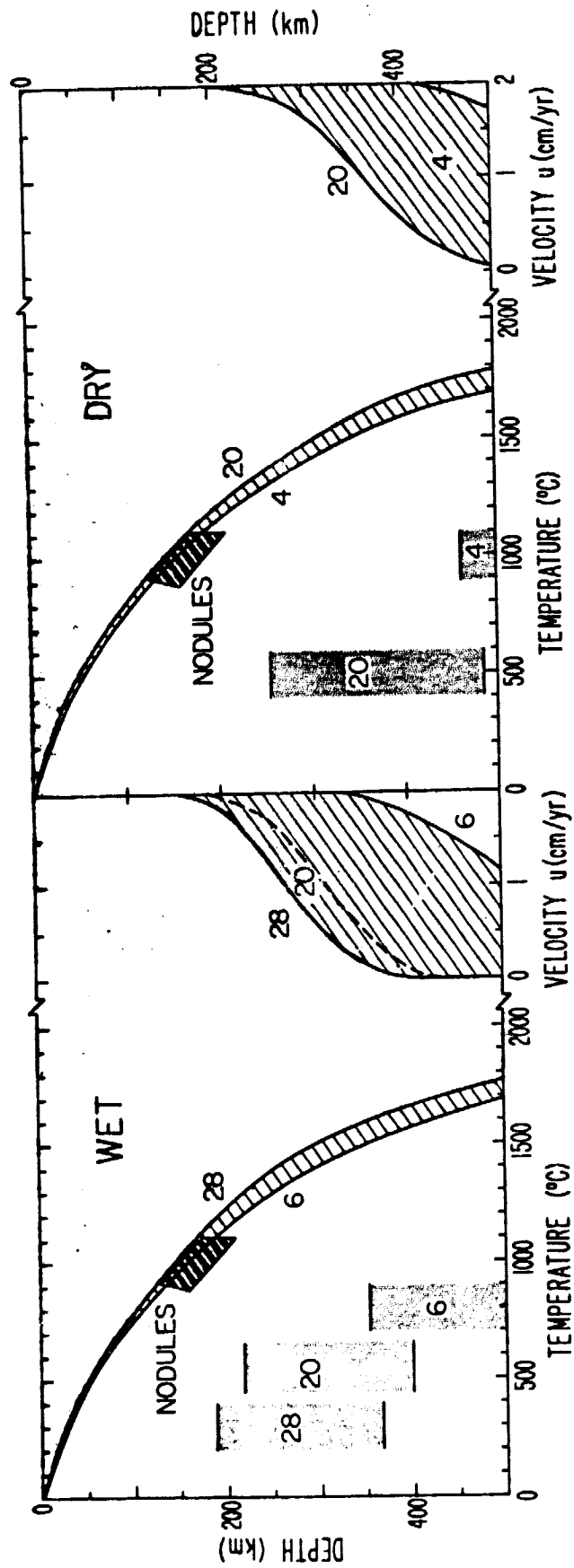
Fig. 3

Q_m

TEMPERATURE (°C)

VELOCITY u (cm/yr)

LOG VISCOSITY (poises)

DEPTH (km)

Fig. 4

Fig. 5

Fig. 6

Fig. 7