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## NASA TECHNICAL MEMORANDUM

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ON LANDSAT IMAGERY (NASA) 28 p HC AO3/MF Unclas
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NEAREST NEIGHBOR, BILINEAR INTER POLATION AND BICUBIC INTERPOLATION GEOGRAPHIC CORRECTION EFFECTS ON LANDSAT IMAGERY
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By Robert N. Jayroe, Jr.
Data Systems Laboratory

September 1976


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George C. Marshall Space Flight Center Marshall Space Flight Center, Alabama

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## TABLE OF CONTENTS

Page
I. INTRODUCTION ..... 1
II. BRIEF DESCRIPTION OF THE IMAGE DATA . ..... 2
II. RESULTS ..... 3
IV. SUMMARY OF OBSERVATIONS ..... 20

## LIST OF ILLUSTRATIONS

Figure Title Page

1. Grey scale determination for $N N, B L$, and $B C$ at location X ..... 2
2. Joint histogram of chamels 2 and 3 for the original data ..... 11
3. Joint histogram of channels 2 and 3 lor NN corrected data ..... 12
4. Joint histogram of chamels 2 and 3 for BL corrected data. ..... 13
5. Joint histogram of chamels 2 and 3 for BC corrected data ..... 14
6. Density slice image of channel 1 for the original data ..... 15
7. Density slice image of channel 1 lor the BC corrected data ..... 16
8. Absolute value image difference of BL and BC for channcl 3 ..... 19

## LIST OF TABLES

Table Title Page

1. Channel 1 Histograms and Deviations for TSPO Data Set. . . ..... 4
2. Channel 2 Histograms and Deviations for TSPO Data Set. . . ..... 5
3. Channe1 3 Llistograms and Deviations for TSPO Data Set. . . ..... $u$
4. Chamel 4 Histomrams and Deviations Eor TSPO Data Set. . . ..... 7
5. Histogram Statisties for TSPO Data Set ..... 8
G. Histogram Deviation Statistics for TSPO Data Set ..... 9
6. Absolute Value Dilference Ilistogram for NN, BL, and BC Overlays ..... 17
7. Accumulative Percentages for Absolute Value Differences of NN, BL, and BC Overlays ..... 18

# NEAREST NEIGHBOR, BILINEAR INTERPOLATION AND BICUBIC INTER POLATION GEOGRAPHIC CORRECTION EFFECTS ON LANDSAT IMAGERY 

## I. INTRODUCTION

There are basically two steps involved in geographically correcting image clata. The first step is utilization of a transformation, which tells where to obtain grey scale information from the original data for a particular pixel location on a geographically correct coordinate system imas, e. In a majority of cases, the location for obtaining grey scale information irom the original image occurs in between pixcls, and this requires that the grey scale value be estimated. The second step, therefore, involves deciding how to assign or estimate the grey scale value. There are three techmiques commonly used for determining the proper grey scale valuc: Nearest Neighbor (NN), Bilincar Interpolation (BL), and Bicubic Interpolation (BC). Figure 1 illustrates how the grey scale values are determined for a location ( X ) in between pixels (represented by a dot) for the three techniques. For NN there is a direct assignment (indicated by an arrow) of a grey scale value of the pixel that is closest to the location X . For the interpolation techniques, the lines connceting pixels show the pixels used in interpolating to determine a grey scale value at the location represented by deltas. The lines connecting the deltas show arother interpolation process required to determine the grey scale value at the desired location $X$. The $B L$ requires a pair of pixel grey scale values, while the $B C$ requires a set of four pixcl grey scale values.

The objectives of the effort are to determine what effects are observed when image data are geographically corrected using the three techniques and to be aware of potential impacts these effects may have on image compression and classification. Effects imply that there will be a deviation between what is observed and what is expected or at least a change will be noticed as a result of the registration (geographic correction) process. In this case, there are only three basic questions that can be asked: what has changed, how much change is there, and where co these changes occur?


Figure i. Grey scale determination for NN, BL, and $B C$ at location $X$.

## II. BRIEF DESCRIPTION OF THE IMAGE DATA

The data set consisted of Landsat digital imagery, April 4, 1973, ID Number 1265~15444. The test site extracted from that imarory was 255 pixels wide and 200 scans long, and corresponded to the Bald Knols, Tonossee Guadrangle. The data were geographically corrected to correspond to a digital ground truth map (GTM), supplied by the Temessee State Plaming Orlice (TSPO) of Nashville, Tennessee, that was 565 pixels wide and 500 scans long. This particular data set has been extensively described, literally and pictorially, as well as extensively classified with various classification techniques that are discussed in a NASA Report. ${ }^{1}$ According to the ground truth information, the test site is 0.83 percent urban, 2.53 percent transportation/ communication, 28.68 percent agriculture, 65.93 percent forest, and 2.03 percent water.

[^0]
## 1II. RESULTS

To determine what had changed and how much change was observed, histograms were computed for the original four bands of data and for the four bands of data that were geographically corrected using NN, BL, and BC. The histograms of the original image had to be normalized so that all of the histograms contain the same number of pixels, because the original image was approximately four times smaller than the geographically correct image. Tables 1 through 4 show this information for the four bands as well as histogram deviations between the original data and the geographically corrected data. Maxima and minima of the histograms are indicated by X and N , respectively, and the mode of the histogram is indicated by XX. The lines scparating grey scale values show where each band was density sliced to produce grey scale imares. In the columns of deviations, a plua siem indieates that more pixels of a particular grey scale value wore requeseed to be transferred from the original image to the corrected image than wore present in the original image. A minus sign indicates that not all of the pixels of a particular grey scale value were requested to be transfored from the original to the corrected image.

One possible interpretation is that the number of pixels with grey scale values that were left over on the original image (indieated by a minus sign) had their grey scale values changed to accommodate a request for more pixels of another grey scale value (indicated by a plus sign). In this sense, the number of grey scale value changes that occurred is shown as absolute value sums under the deviation columns. This number divided by two is the number of pixels which had their grey scale values changed. The numbers under the four columns to the left of the deviation columns show that all of the histograms for the test site contain $2110: 5$ pixels.

Examination of the maxima and minima of the histograms shows that NN most nearly preserves the histogram structure of the original data, while the interpolation methods act as a filter smoothing away most of the structure. This tends to make the procedure of choosing density slices more difficult because all of the natural indications in the data are no longer there. Also, the least amount of grey scale charges occur for NN. Table 5 shows the statistics calculated from the histograms, and indicates that, although the mode of the histogram may change, the moan value appears to be changed very little. However, the variance is reduced quite considerably in some cases. Table 6 is a summary of the number of pixels that had their grey scale values changed and the resulting percent changes in the histograms.

TABLE 1. CHANNEL 1 HISTOGRAMS AND DEVIATIONS FOR TSPO DATA SET

| Grey Scale Value | Oripinal Data | NN | LBL | LC | Devintuots |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | NN-O | BL-O | S3C-O | IUL-NN | me-nN | 10C-13L |
| 21 | 12 X | 11 X | 0 | 10 | - 1 | - 12 | - 2 | - 11 | - 1 | + 10 |
| 22 | 4 N | 3 N | 8 | 41 | - 1 | + 4 | + ${ }^{3}$ | + 6 | + ${ }^{4}$ | + 析 |
| 23 | 2048 | 25:3 | 72 | 280 | - 11 | - 102 | $\pm 16$ | - 161 | + 27 | + 208 |
| 24 | 2380 | 1842 | 598 | 1.440 | -38 | -762 | - 06 | - 744 | $+109$ | + 848 |
| 25 | 1562 | 4 54za | 4111 | 5.400 | - 20 | -1451 | + 848 | -1 431 | + 565 | +2885 |
| 26 | 1343 | 12345 | 11338 | 13 278 | + 7 | -2004 | - 62 | -2018 | - 69 | +1944 |
| 27 | 25486 | 252822 | 201 189 | 225728 | -184 | -2 257 | -1748 | -2103 | -1 064 | + 5029 |
| 28 | 343858 | 35394 X | $0450 \pm \mathrm{xX}$ | 41.1528 | $-564$ | + 145 | -2 670 | + \% ${ }^{\text {¢ }}$ - | -2 312 | -2 824 |
| 29 | 18566 N | 18413 N | 27859 | 250604 N | -15is | +9 43\% | +7008 | +5) 580 | +7 ${ }^{2} 51$ | -2 295 |
| 30 | 344678 XX | 91470 XX | ${ }^{27} 2009$ | 2 t 0.44 X | -207 | -7259 | -4 468 | -690 | -8999 | -1 104 |
| 31 | 129206 N | 12367 N | 18006 | 17803 | +101 | +5843 | *5497 | +5880 | +5 356 | - 2138 |
| 32 | 15469 X | 15712 X | 10002 | 15932 | +244 | + 595 | - 1.47 | + 360 | - 80 | - 740 |
| 33 | 14654 | 14752 | 15043 | 14.222 | +168 | + 439 | - 308 | + 291 | - 530 | - 821 |
| 84 | 14256 | 14876 | 12606 | 1255 | +120 | -1 490 | -1401 | -1 7110 | -2081 | - 311 |
| 35 | 7880 | 7965 | 8085 | 8146 | +139 | + 239 | + 5 | + 100 | + 1121 | + 81 |
| 36 | 2860 N | 2908 N | 4854 | 5193 | +58 | +20134 | 4243 | +1976 | +2 265 | + 309 |
| 37 | 5350 X | 54858 | 3465 | 5385 | +83 | -1836 | -1 511 | -1 068 | -1594 | + 8774 |
| 35 | 1843 | 1876 | 1814 | 2885 | +39 | - 29 | + 540 | - 61 | + 514 | + 575 |
| 39 | 1583 | 1622 | 1082 | 1488 | $+29$ | - 501 | - 95 | - 540 | - 184 | + 400 |
| 40 | G.10 N | 0655 | 630 | 916 | + 16 | - 10 | + 269 | - 45 | $+253$ | + 286 |
| 41 | 9368 X | 350 X | 313 | 817 | $+1$ | - 550 | - 329 | - 515 | - 303 | + 224 |
| 42 | $\pm 70$ | 1 CL | 229 | 51.4 | $+10$ | - ${ }^{\text {¢ }}$ | + 171 | + 42 | + 161 | + 110 |
| 4 | 130 ${ }^{3}$ | 134 N | 157 | 2088 | + 4 | + 27 | + 33 | + 24 | $+91$ | + 71 |
| 44 | 20\% X | 205 X | 111 | 169 | + 2 | - 92 | - 34 | - 9 9 | - 36 | + 59 |
| 45 | 170 | 168 | 87 | 136 | - $\quad$ - | - 83 | - 34 | - 76 | - 27 | + 49 |
| 40 | 81 | 77 | 66 | 89 | - 4 | - 15 | + 8 | - 11 | $+12$ | + 25 |
| 47 | 208 | 19 N | 48 | 76 | - 1 | + 28 | $\pm 50$ | + 29 | + 57 | + 28 |
| 48 | 110 X | 102 X | 34 | 51 | -8 | - 76 | - 59 | - 08 | - E1 | + 17 |
| 49 | 23 | 27 | 3 | 48 | - 1 | + 6 | $+20$ | + 7 | $+21$ | + 14 |
| 50 | 20 N | 18 N | 48 | 356 | - 2 | + 8 | + 15 | + 10 | + 17 | + 7 |
| b1 | 45 X | 41 | 24 | 37 X | - 4 | - 21 | - 8 | - 17 | - 4 | -13 |
| 52 | 41 | 448 | 0 | 28 | $+3$ | - 32 | - 14 | - $\quad 35$ | - 16 | + 19 |
| 54 | 88 | 30 | 9 N | 20 | + 2 | - 40 | - $y$ | - 81 | - 10 | + 11 |
| 5.1 | 0 | 0 | 10 X | 14 | 0 | + 10 | $+14$ | + 10 | + 1-4 | + 4 |
| 55 | 0 N | 0 N | 5 | 9 | 0 | + 5 | $+\quad 4$ | * 5 | + 0 | + 4 |
| 50 | 248 | 26 x | 5 | 7 | + 2 | - 19 | - 17 | - 21 | - 19 | + 2 |
| 57 | 4 | 4 | $\stackrel{A}{4}$ | 5 | 0 | 0 | + 1 | 0 | + 1 | + 1 |
| 58 | 0 N | 0 | 1 | 4 N | 0 | + 1 | $+4$ | + 1 | + 4 | + 3 |
| 59 | 12 X | $15 \times$ | 1 | 9 X | +3 | - 11 | - 3 | - 14 | $\cdots$ | + 8 |
| 60 | 0 | 0 | 0 | 4 | 0 | 0 | + 4 | 0 | $+4$ | + 4 |
| 61 | 0 | 0 | 0 | 2 | 0 | 0 | + 2 | 0 | + 2 | + 2 |
|  | 211075 | 211075 | 211075 | 211075 | 121921 | 141 8891 | 1248641 | 1375461 | 144 486\| | 1171761 |



TABLE 2. CHANNEL 2 HISTOGRAMS AND DEVIATIONS FOR TSPO DATA SET

| Orey scale <br> Value | Orighoal Datn | NN | BL. | 13C | Desfuts:\% |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | NNO | HL-O | nc-0 | HLINNN | LSC-NN |  |
| 12 | 0 | 0 | 0 | 4 | 0 | 0 | + 8 | 0 | $+3$ | + ${ }^{4}$ |
| 13 | 0 | 0 | 0 | 10 | 0 | 0 | + 16 | 4 | $+16$ | - 16 |
| 1.4 | 4.4 | 28 | 4 | H1 | $+4$ | - 20 | + 57 | + 24 | + 5 | + 77 |
| 10 | 204 | 271 | 45 | 274 | $+7$ | - 215 | + 10 | - 2283 | + 3 | + 2293 |
| 15 | 025 | 315 | 240 | 556 | - 10 | - 376 | - 09 | - 2080 | - 83 | + 307 |
| 17 | 718 | 720) | 677 | 930 | + 11 | - 141 | + 268 | 158 | + 2551 | + 604 |
| ${ }^{4}$ | 2488 X | 2 290 8 | 1184 | 1787 | + 6 | -1 104 | - 751 | -1 | - 766 | + 585 |
| 15 | 609 N | G6a N | 1855 | 2805 | + 15 | +1210 | +1014 | +1 195 | +1 499 | $+704$ |
| 20 | 4997 | $501 \%$ | 5469 | 4870 | + 16 | -1 5 | - 127 | -1 544 | - 14, ${ }^{2}$ | +1 4101 |
| 21 | 7875 | 7415 | 0685 | 8061 | + 41 | - 6852 | + 7400 | - 704 | + 665 | +18385 |
| 22 | $14 \% 808$ | 14898 | 1156 | 125404 | +154 | - 2000 | -2 260 | - 5 \% 3 \% | -4 | + 440 |
| 23 | 15308 | 15488 | 15985 | 15.514 | +136 | + 682 | + 211 | + 547 | + 75 | - 571 |
| 24 | 20528 X | 205100 X | 13898 | 18105 | + 28 | - 050 | -242a | - $00{ }^{\text {cter }}$ | -2 4E5 | -1 4033 |
| 8 | 1.4849 N | 14251 N | 81178 | 191878 | -8 | +6 033 | $+5440$ | +6 447 | +5 448 | -1 499 |
| 20 | 21644 | 21005 | 84820 | 21810 | - 11 | +2 585 | + 10 | +2546 | + 177 | -2 415 |
| 24 | 27059 xX | $27015 \times \mathrm{x}$ | 20.2988 | \% - 74 XX | - 44 | - 887 | -29 485 | -783 | -22 4.12 | -28 458 |
| 28 | 224887 | 23517 | 22797 |  | -170 | - 690 | -1498 | - 520 | -1 3 24 | - 802 |
| 29 | 18973 | 18 B39 | $15 \mathrm{cg6}$ | 45080 | - ${ }^{5}$ | -4878 | -3003 | -2 44.4 | -2 720 | + 184 |
| 30 | \% 424 | 3400 N | 100052 | 9082 | - 24 | +64 630 | +62560 | +6652 | +6\% | - 70 |
| 31 | 11605 x | 11) 505 | 83410 | 8177 | - 68 | -3865 | -5 4ins | - ${ }^{-157}$ | -3 360 | - 16\% |
| 36 | 503 | 5407 | 5407 | $6 \mathrm{B4}{ }^{\text {c }}$ | + 69 | + 69 | $+504$ | 0 | + 435 | + 455 |
| 980 | 2 ctan N | ${ }^{41198}$ | 5 \%\% | 3389 | + 80 | + 605 | + 922 | + 613 | + Sto | + 257 |
| \% | $3759 \times$ | \% 702 x | 2960 | 3047 | + 4 | - 733 | - 712 | - ys | - 7.45 | + ${ }^{+1}$ |
| 36 | 2426 | 2427 | 1898 | 2258 | + 4 | - 5 | - 170 | - 5 505 | - 17\% | + 304 |
| 40 | 13.50 N | 1094 N | 1483 | 1574 | + 14 | + ${ }^{\text {difig }}$ | + 4304 | + 3\$3 | +460 | + 14: |
| 37 | 1 670 2 | 1691 X | 1104 | 1540 | $+15$ | -. 572 | - 306 | - 367 | - 10.1 | + 204 |
| \% | 710 | 738 | 820 | 1011 | + 23 | +110 | + 201 | + 980 | + 278 | + 182 |
| 313 | 013 N | $622{ }^{2}$ | 718 | 806 | + 3 | + 164 | + 298 | + 90 | + 184 | + 88 |
| 40 | B. 44 X | 450 X | 559 | 68\% | + 12 | $\sim 285$ | - 150 | - 2897 | - 168 | + 123 |
| 41 | 301 N | 3809 N | 4 CF | 587 | + 2 | $+\quad 98$ | + 2206 | + 56 | + 204 | + 128 |
| 42 | 601 X | 611 X | 314 | 447 | +10 | - 267 | - 158 | - 267 | - 16d | $+105$ |
| 43 | 2515 | 2365 | 423 | 38\% | + 5 | + 92 | + 152 | + 87 | $+117$ | + 60 |
| 4 | 204 | 25. | 276 | 312 | - 20 | + 12 | + 48\% | + 22 | + | + 26 |
| 40 | 44: X | 455 X | 250 | 258 | + 12 | - 107 | - 189 | - 208 | - 200 | + ${ }^{\text {y }}$ |
| 40 | 363 | 335 | 165 | 258 | $+0$ | - 164 | -71 | - 170 | - 77 | + 93 |
| 47 | 101 N | 107 N | 133 N | 181 | + 0 | + 2 | + 80 | + 26 | + 74 | + 48 |
| 48 | 207 \% | 210゙5 X | 138 X | 175 | + ${ }^{\text {c }}$ | - 615 | - 72 | - 76 | - | + |
| 45 | 77 | 80 | TE N | 111 | $+3$ | + 1 | + 24 | - 2 | + 61 | + 23 |
| 54 | 69 N | 68 N | 87 X | 15 | - 1 | 4 18 | + 60 | + 19 | + 64 | + 45 |
| 51 | 106 X | 109 X | 79 | 90 | + 3 | - 27 | - 16 | - 30 | - 19 | + 11 |
| 5 | 77 | $72 . \mathrm{N}$ | 57 N | 84 | - 5 | - 20 | + 0 | - 15 | + 14. | + 29 |
| \% | 77 | B1 X | 58 X | B. 1 | + 4 | - 19 | + 7 | - 20 | + 3 | + 26 |
| $5:$ | 17 N | 35 N | 28 N | 5 | - 2 | - 9 | $+17$ | - 7 | + 13 | + 26 |
| 55 | 101 X | 100 X | 28 | 5 | - 1 | - 76 | - 51 | - 72 | - 30 | + 24 |
| 54 | 28 N | 25 | 26 X | 47 | - 3 | + B | + 19 | + 11 | + 22 | + 11 |
| 57 | 3 d | 3 | $2 \%$ | 41 | - 1 | - 5 | + 9 | - 4 | + 10 | + 1.4 |
| 58 | 32 | ata | 28 | \% 5 | - 1 | - 10 | + 7 | - 11 | + 0 | + 17 |
| 59 | 88 | 31 | 18 | 31 | $-1$ | - 14 | - 1 | - 13 | 0 | + 18 |
| 60 | 24 N | 27 N | 16 N | - 2 | + 8 | - 8 | - 1 | - 11 | - 4 | + 7 |
| 61 | 42 | 11 | 27 X | 47 | - 1 | - 5 | - 5 | - 4 | - 4 | 0 |
| 02 | 49 X | 48 x | 10 | 23 | - 1 | - 54 | - 208 | - 32 | - 25 | + 7 |
| 6.5 | 16 N | 27 N | 12 | 19 | + 1 | - 4 | + 3 | - 5 | + 2 | + 7 |
| 6.9 | 41 X | $42 \times$ | 11 | 20 | + 1 | - 30 | - 21 | - 31 | - 22 | + 9 |
| $\mathrm{B}_{5}$ | 0 | 0 | 1 N | 15 | 0 | + 1 | + 18 | + 1 | + 15 | + 17 |
| 66 | 0 N | 0 N | 4 | ${ }^{5}$ | 0 | + 4 | + 9 | $+\quad 4$ | + 9 | - 5 |
| 67 | 16 X | 17 X | 4 x | 14 | + 1 | - 12 | - 2 | - 15 | - 3 | + 10 |
| 68 | 4 | 4 | 0 | 4 | 0 | - 4 | 0 | - 4 | 0 | 4 |
| 69 | 4 | 4 N | 1 | 7 | 0 | - 8 | + | - 3 | + | $+0$ |
| 70 | 4 | 5 X | 0 | 2 | $+1$ | - 4 | - 2 | - 5 | 4 | + 2 |
| 71 | 0 | 0 | 0 | 7 | 0 | 0 | - 7 | 0 | + 7 | + 7 |
| 72 | 0 | 0 | 0 | 1 | 4 | 0 | $\cdots \quad 1$ | 0 | + 1 | + 1 |
| 7 | 0 | 0 | 0 | 3 | 0 | 0 | + 3 | 13 | + 3 | + ${ }^{\text {j }}$ |
| 74 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | (1) |
| 75 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 76 | 0 | 0 | 0 | 4 | 0 | 0 | 0 | 0 | 0 | 0 |
| 7 | 0 | 0 | 0 | 1 | 0 | 0 | + 1 | 1 | + | + |
|  | 211085 | 211075 | 211075 | 211475 | 113561 | 130 24al | 1265461 |  | 1262321 | $117950 \\|$ |

TABLE 3．CHANNEL 3 HISTOGRAMS AND DEVIATIONS FOR TSPO DATA SET

| Guw stimles Valla | $\begin{aligned} & \text { Ordganal } \\ & \text { Lheta } \end{aligned}$ | W＊ | 13. | IE | Devtaticar |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | SiN－O | 131，0 | 10－0 | 21，－8N | 11CMN | HEW $\mathrm{HL}_{4}$ |
| 7 | $\checkmark$ | 0 | $\stackrel{1}{ }$ | $\pm$ | 0 | ${ }^{3}$ | $\pm 8$ | 4 | $+2$ | ＋ 2 |
| 自 | 0 | 0 | 4 | 4 | 0 | 0 | 43 | 0 | ＋ 6 | ＋ |
| 3 | 4 x | 4 x | 0 | 15 | 0 | － 1 | ＊18 | － 4 | $+11$ | ＋ 18 |
| 16 | 0 N | 0 \％ | 0 | 92 | 0 | 9 | － 4 | is | ＋ 32 | － 92 |
| 11 | 13 | 47 | 1 | 74 | 42 | － 44 | ＋ | － 46 | ＋ 27 | ＋74 |
| 12 | 64i | E4t | 8 | 43 | －1 | － 3 | －30 | － 60 | －${ }^{2}$ | －姓 |
| 15 | 2243 $\times$ | $221 \times$ | 29 | 183 | － 2 | － 191 | －กี้ | －198 | －68 | －181 |
| 14 | 176 | 174 | 76 | 171 | － 1 | － 04 | $\cdots \quad 4$ | －in | － 3 | ＋ 92 |
| 14 | 160 | 1783 X | 108 | 169 | － 10 | － 88 | ＋ 9 | － 08 | － | － 011 |
| 16 | $6_{65} 8$ | 44 N | 146 | 2st | ＋8 | ＋ 51 | ＋ 92 | ＋ 46 | ＋ 4 | ＋ 0 |
| 17 | 2078 | 2015 | 1608 | 157 | －心 | － 27 | － 70 | － 51 | － 48 | － 40 |
| 15 | 145 | 19\％ | 154 | 156 | $\cdots 1$ | － 15 | － 53 | － 14 | $\cdots$－ 3 | － 24 |
| 10 | 174 | 185\％ | 162 N | 160 | $+0$ | － 27 | － 4 | － | － 20 | ＋ 4 |
| 8 | 170 | 10n $\%$ | 172 | 2 | ＋ 86 | ＋${ }^{2}$ | － 13 | － 14 | － 2 | ＋ 10 |
| 21 | 142 Ev | 146\％ | 218 | 1994 | $+5$ | － 56 | ＋ 81 | ＋ 73 | ＋ 78 | ＋ 8 |
| 22 | 2040 | 24.4 | 224 | 254 | － 2 | 06 | － 8 | －54 | ＋17 | ＋© |
| ＊${ }_{\text {d }}$ | 402 | ใ d $^{3}$ | twi | 44 | －1 | － 802 | － 48 | － 108 | ＋ 00 | ＋ 104 |
| 它 9 | 6is | 067 | 453 | 759 | ＋ 24 | － 88 | － 245 | －${ }^{-9}$ | ＋ 240 | －2\％4 |
| 25 | 1514 | 1835 | 913 | 1 1 | $+10$ | －\＄39 | － 111 | － 818 | － 20 | ＋ 118 |
| 㕱 | 1806 | 1 13： | 1 149 | 2148 | $+34$ | － 172 | ＋505 | － $20 \pm$ | ＋ 808 | － 700 |
| 4 | 4 4 4 | ＋111 | 28980 | 3 CLS | ＋28 | －1 155 | －465 | －1 221 | －453 | － 2 2ts |
| 128 | 4251 | ＋155 | 4 465 |  | － 26 | － 609 | $+1454$ | ＋ $47 \pi$ | ＋1．4E0 | ＋803 |
| 2 | 4265 | 4845y | 4043 | ¢ 770 | － 8 | － 4.5 | ＋ 414 | －2e6 | $+80^{7}$ | ＋ 700 |
| 150 |  | 14.615 | 12 cose |  | － 84 | －1 ¢ $_{\text {¢ }}$ | －1 \％${ }^{2}$ | －1 6315 | －1907 | ＋ 208 |
| 31 | 14， 800 | 1.40 ded | 14 ${ }^{\text {ma }}$ | 14 35 | －19\％ | 4 ㄴ4 | －大ud | ＋ | －8834 | －Etr |
| 超 | 17170 x | 170003 x | 185748 |  | － 71 | －1．815 | －2847\％ | －1 3 \％${ }^{\text {¢ }}$ | －5408 | －1 06 |
| 3 | 853 | 日 $\mathrm{O}_{5}$ |  | 1364\％${ }^{\text {¢ }}$ | －的 | ＋6．610 | ＋6．905 | ＋6 6 W0 | ＋6： 294 | －1 182 |
| W | 20785 x | 202548 | 14 \＄15\％ | 120 60 x | －376 | －61 174 | －7036 | －4，6id | －4 | －צ゙上1 |
| 䢕 | 4 SE 5 5 | 4 7 7 枵 | 11978 | 11.485 | －1205 | ＋71120 | ＋15 548 | 47\％95 | 4675 | －5xt |
| ： 4 | 17 15\％ x | 17 5¢5 | 118 | 1002\％ | － | －6 615 | －15 4043 | －6 1489 |  | － 4 － 4 |
| T | 40808 | 40418 | 5485 | 816 | － 18 | ＋ 1514 | 4 dotil | ＋1723 | ＋1415 | 155 |
| 5 | 0963 X | 9590 X | 6950 |  | － 14 |  | －3 198 | －34 |  | ＋ 224 |
| （19） | 1400 N | 1415 y | 4077 | 4601 | $+1$ | ＋2160 | ＋+1 18＊ | ＋13164 | ＋3 ${ }^{\text {1 }}$ | ＊14 |
| 49 |  | （6） 3.1 x | 395 |  | ＋ 61 | － tho | －2040 | －2\％ | －2 59\％ | －${ }^{4}$ |
| 41 | 40925 | 465 |  | せ150 | ＋Iu | ＋25cy |  | ＋28 5EM $^{\text {a }}$ | ＋2 ciul | ＋ 77 |
| 4 | 4.458 | 4 20x X | $2 \mathrm{LS4} \mathrm{X}$ | a 920 | ＋ 42 | －1 478 | －8 801 | －1．49 | －1 ट－5 | －\％ |
| 4in | 2904 | 2 ctc | 3 Wosk | 2 CH | $+68$ | ＋ 209 | ＋244 | ＋\＄32 | $+181$ | － 155 |
| 4. | 20\％ | 2055 |  | 2607 N | $+1$ | －日16 | －${ }^{\text {a }}$ | ＋ 618 | ＋ 758 | －603 |
| 45 | ＋ 8518 | 488 | Stase | 2 s 973 | ＋ 2 | －1 669 | －1051 | －1 641 | －1976 | －565 |
| 46 | 1242 N | 12 ta | 3088 | 28045 | ＋ 21 | 418.56 | 41 638 | 41812 | ＋1614 | －119 |
| ． 84 | 3 smbx | \％ 4 dis $\mathbf{x}$ | 38 | $4091 \%$ | ＋77 | － 504 | －${ }^{\text {a }}$ | －如 6 | －864 | －162 |
| $4{ }^{4}$ | 2164 | aty | 9309 | 30475 N | ＋ 57 | －1 245 | ＋ 211 | ＋1 04s | ＋ 504 | －234 |
| 415 | 4 tan \％ | 4 \％81 X |  | 3 msi | ＋ 55 | － 1874 | －1 025 | － 742 | －1 u5－4 | － 2154 |
| col | ＊\％\％0\％${ }^{\text {N }}$ | 2 yata | $3{ }^{3}$ | 41404 | ＋ 20 | ＋ 757 | ＋ 539 | ＋727 | ＋ 5 त̈ld | － 108 |
| 51 | 3053 | －\％ay | a 6 6tic | 5 顽 | ＋ 43 | ＋ 518 | － 79 | ＋ 158 | －134 | － 2882 |
| 8 | 4 3 \％x | 44778 | 3）${ }^{\text {\％}}$ | a 8 tri | 4195 | －403 | －ExS | － 407 | －${ }^{2} 376$ | －10\％ |
| 54 | a Fate N | 4 BET | 4004 | 3 yc | ＋ 01 | 4 3 3 相 | －121 | ＋ 413 | 4 | －2\％iz |
| \％ |  | 38568 | 410 L E | 3 EcI X | ＋\＃3 | － 172 | － 6 | －115 | －1บธ | － 585 |
| 5 | 26500 N | 21010 dit | 3 yc | 37514 | ＋ 69 | ＋1 14 | ＋ 4104 | 410 | ＋ 1356 | － 2.48 |
| 56 | ＋¢ba X | $4{ }^{4}$ | ts bist | 4605 | ＋ 40 | － 988 | －1 080 | －1040 | －1 068 | － 40 |
| 57 | 2 at | ¢ \％8 |  | 5 21235 | $+46$ | ＋tides | ＋654 | ＋ 6.87 | ＋ | － 4 |
| 53 | 1265 y | 2 HIP | $2 \pm 22$ | 5 | ＋ 62 | ＋ 21.5 | ＋1 685 | ＋811 | ＋1 482 | ＋ 141 |
| 5 | 4． 128 \％ | $4 \mathrm{tac} x$ | 2080 | 515 | ＋ 48 | －1888 | －1 1314 | －1 546 | －1 408 | ＋176 |
| 68 |  | 4 min N | 2 tal | 2\％304 | － 82 | － $20 \%$ | ＋\＄989 | ＋ 1.8 | － 217 | ＋105 |
| 41 | $2246 \times$ | 2995 | 1905 | 2107 | ＋ 30 | － 687 | － | －\＄0\％ | －${ }^{2} 8$ | ＋34y |
| 920 | 120 | 18150 | 1 บธ | 15 | 4 c | －185 | ＋ 2 2tit | －\％ 47 | ＋ 173 | ＋4226 |
| 9.3 | E4，M | Eat N | 750 | 1 1－40 | ＋ 6 | ＋ 211 | ＋4ibis | ＋ 2043 | ＋Evo | + tivt |
| 6 | 1 bite X | 1040 X | 69 | तᄌty | ＋ | － 8.47 | －－ | －4te | － 268 | ＋105 |
| 45 | 535 | 191 | 36\％ | 578 | ＋ 6 | － 208 | － 7 | － 209 | － 12 | $+105$ |
| 04 | 200 N | 290 ＊ |  | S3x | ＋ 10 | － 26 | － 103 | － | ＋${ }^{\text {a }}$ | ＋ 134 |
| 57 | บブロ | 37\％ 8 | 854 | 56． | ＋ 1 | － 215 | － 70 | －2\％9 | － 71 | $+145$ |
| 6 | H1 N | 75 | 40 | 158 | － 0 | ＋ | ＋ 107 | ＋ 11 | $+113$ | ＋102 |
| 839 | 13） X | 14 H | \％ | 118 | － | －！ 0 | － 10 | － 98 | － 14 | $+50$ |
| 76 | 67 | ${ }^{12}$ | 31 | 76 | ＋ 5 | $\cdots 26$ | ＋131 | － 31 | $+8$ | ＋98 |
| 71 | 20 N | 21 N | 24 | $5{ }_{5}$ | ＋ 1 | ＋ 4 | 4 | ＋${ }^{4}$ | ＋ 87 | ＋${ }^{4}$ |
| 72 | 888 | 318 | 11 | 84 | ＋${ }^{1}$ | － 17 | ＋B | － 20 | ＋ 5 | ＋ 65 |
| 7 | 发 | 28 | 6 | 15 | 0 | － 28 | －401 | － 22 | － 10 | ＋1ta |
| 74 | 0 | ${ }^{6}$ | 4 | 16 | 4 | ＋है | $+16$ | ＋ 6 | $+16$ | ＋ 10 |
| 76 | 0 | $\checkmark$ | 2 N | 7 | $v$ | ＋ | $+7$ | ＋ 2 | 4 | $\pm 5$ |
| \％${ }^{\text {a }}$ | 2118 | \％ 18 | 6 X | 0 | ＋ 1 | － 11 | － 17 | － 16 | － 18 | － 3 |
| 74 | 0 | 0 | T | 4 | $\checkmark$ | ＋ 3 | ＋ 2 | ＋${ }^{3}$ | ＋ 2 | － 1 |
| 78 | 4 | 0 | 0 | 3 | 18 | 0 | $+3$ | 0 | ＋${ }^{+}$ | $4 \times 8$ |
| 78 | 4 | 4 | 1 | $6 \%$ | 0 | －${ }^{2}$ | ＋ 2 | － 3 | $4{ }^{4}$ | ＊ 5 |
| So | 0 | 0 | 2 | ${ }_{2}$ | 0 | ＋ 2 | ＋ 2 | ＋ 2 | 42 | U |
| 81 | 41 | ${ }^{3}$ | 0 | 2 | 0 | 0 | $+2$ | 0 | $\pm$ \＃ | ＋ 2 |
| \＄t | 4 | 5 | 0 | 1 | ＋ 1 | － 4 | －䊽 | － 5 | 4 | ＋ 1 |
|  | 211076 | 211075 | 211075 | 2011475 | 123661 | 1960．301 | 11640 besel | 4458741 | ［ 455000 | 1158401 |

TABLE 4. CHANNEL 4 HISTOGRAMS AND DEVIATIONS FOR TSPO DATA SET

| Gray Scalo Value | Orfabial Dals | NN | 11. | 5 C | Deviations |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | NNOO | H2L-O | BC-O | HSL-NN | $\mathrm{BC}-\mathrm{NN}$ | BC-BL |
| 1 | 0 | 0 | 0 | 8 | 1 | 0 | * $\quad y$ | 0 | + 6 | + $\quad \mathrm{y}$ |
| 2 | 4 | $\checkmark$ | 9 | 58 | +1 | - 4 | + ${ }^{1}$ | - $\quad$ B | + 6: | * \$5 |
| \$ | 76 | \% 2 | 4 | 115 | - 1 | - 95 | + 42 | - 64 | + 28 | + 108 |
| 4 | 82 | 203t | 3 | 207 | + 2 | - 145 | - 24 | - 197 | -26 | + 171 |
| 5 | 204.4 | 207 X | 125 | 202 | + ${ }^{\text {d }}$ | - 104 | - 10 | - 142 | - 68 | + 77 |
| 0 | 222: | 2926 | 177 | 184 | + 3 | - 40 | - 34 | - ${ }^{-14}$ | - $4 \pm$ | + ${ }^{\text {a }}$ |
| 7 | 207 N | 209 N | 219 | 210 | + 2 | + 12 | + | + 19 | + 1 | - |
| 8 | 248 : | 2400 X | 240 | 200 | $+12$ | - 8 | + 12 | - 20 | 0 | + 3 29 |
| 0 | 211 N | $218 \times$ | 840 | 267 | + 7 | + 19 | + 56 | + 12 | 44 y | + ${ }^{+}$ |
| 10 | 420 | 320 | 291 | 270 | -13 | - 42 | - 54 | - 280 | - 41 | - 12 |
| 11 | 3781 | 836 | 241 | 400 | $+10$ | - 2 | + 20\% | - $12^{\text {ch}}$ | $+17$ | + ${ }^{\text {div }}$ |
| 12 | 407 | 482 | 455 | 6 6.2 | +15 | - 12 | $+105$ | - 27 | +150 | + 177 |
| 13 | 1031 | 1447 | $80 \pm$ | 1188 | $+15$ | - 28.80 | + 104 | - 242 | $4 *-91$ | + 384 |
| 14 | 2529 |  | 1900 | 2797 | + $\mathrm{bib}^{\text {d }}$ | - ${ }^{3}$ | + 466 | - 286 | +612 | + 7989 |
| 10 | ¢ Oab | 5 0.91 | 4572 | 5064 | -17 | - 186 | + 900 | - 169 | 45323 | +1 092 |
| 16 | 12574 | 12620 | 11 W3 | 12246 | $+47$ | -1 244 | + ${ }^{4} \mathrm{H}$ | -1 296 | - 980 | + 010 |
| 17 | 14*** | 18205 | 18.548 | 18920 | - 51 | + $\quad 2$ | - 104 | + $\mathrm{Ba}^{3}$ | - 5 | - 1 ats |
| 13 | 9n 70\% | " " - | 2030407 | 22025 | - 48 | + 653\% | - 705 | + 878 | - 400 | -1 3 36 |
| 13 | 942012 X | " $\quad$ " 0 | 245085 | 228774 | - | + 884 | - 127 | +1 189 | -12\% | -1 311 |
| 20 | 24126 | 二a | 21854 | 21024 | -490 | - 2.29 | -1102 | + 185 | -676 | - 800 |
| 21 | 17808 | 1 C 710 | 16 Urc | 16275 | -296 | - 402 | - Gat | - 104 | -x\% | - 2031 |
| 22 | 10 dye | 10674 | 10)30̆9 | \$0 \%it | - 13 | - 32 | + ${ }^{\circ} \mathrm{i}$ | - \% \%1d | * 6 | - 378 |
| 23 | 5991 | 0 015 | 6600 | 6748 | +229 | + 609 | + 757 | + 587 | +735 | + 148 |
| 24 | 5853 | 5055 | 5402 | 5388 | +102 | - 3ti | - 471 | - $40 \pm$ | -574 | - 110 |
| 25 | d 470 N | 4540 N | 5129 | 4875 | + 68 | + 05 | + 208 | + 5Gy | +35 | - 24d |
| 20 | 4598 X | 4654 X | 5205 | 4785 | + ${ }^{\text {a }}$ | $\because 606$ | + 284 | + 5 ¢81 | 4149 | - 422 |
| 27 | $4{ }^{4} 780$ | 4) 6546 N | -130 | 4813 | + 67 | + 551 | $+240$ | + 484 | +173 | - 311 |
| 4 4 | 5115 | 52.15 | 5295 | 5050 | +128 | + 140 | - 6 C | + 52 | -190 | - 245 |
| 29 | 5261 | 5348 | 5008 | 5200 | $+87$ | $+40^{\prime \prime}$ | - 61 | +320 | -148 | - 108 |
| 291 | $5380 \times$ | 5489 X | 5561 | 5148 | + 95 | + 2015 | -182 | + 152 | -281 | - 415 |
| \% 1 | 4611 is | - "He N | 5393 | 515 | + 00 | $+786$ | + 518 | +080 | +408 | - 268 |
| H2 | $5 \$ 06$ | \% 451 X | 5324 | 4991 | +85 | - 42 | - 375 | - 127 | -460 | - - \% |
| a | 4 44.5 | 4505 | 4512 | 4565 | $+64$ | + 67 | + 140 | + 3 | $+70$ | + 78 |
| 34 | 3 357 | 3708 | 3 3 5\% | 5888 | $+51$ | - 94 | + 231 | - 145 | $\checkmark 290$ | 1 - |
| 3ts | 2971 | d01\% | 2804 | 3095 | + 48 | - 103 | 4. 124 | - 1\%1 | $+76$ | + $22 \%$ |
| $\pm 6$ | 2565 | 2642 | 2296 | 2484 | 47 | - 275 | - 81 | - 302 | -1c8 | + 198 |
| 37 | 1957 | 2027 | 1 8440 | 1968 | +701 | - 117 | + 11 | - 187 | - 59 | + 128 |
| 㾂 | 1310 | 158 Cd | 1350 | $16{ }^{161}$ | $+14$ | - 160 | +121 | - 174 | +107 | + 281 |
| 10 | 1165 | 1103 | 10.84 | 1206 | + | - 1211 | +101 | - 145 | + 76 | + 28x |
| 40 | 1015 | 1050 | 738 | 965 | + 41 | - 277 | - 54 | - 313 | - 91 | + $22 \pi$ |
| 41 | 67\% | 593 | 49.1 | 071 | +21 | - 76 | + 99 | - 99 | -76 | + 177 |
| 12 | 406 | 397 | 291 | 421 | -9 | - 115 | + 15 | - 100 | +21 | $+150$ |
| 48 | 244 | . 34 | 217 | 279 | $+20$ | - 27 | + 35 | - 7 | + 15 | + 62 |
| 44 | 22: | 22. | 136 | 215 | $+6$ | - $\mathrm{gr}^{7}$ | - 7 | - 43 | - 15 | + 80 |
| 45 | 150 | 127 | 68 | 140 | - 3 | - 68 | $+10$ | - 50 | + 13 | + ${ }^{\text {a }}$ |
| . 6 | 45 | 48 | 12 | 81 | - i | - 87 | + 32 | - 33 | + 3 \% | + 69 |
| 47 | 12 | 12 | 4 | 40 | ${ }_{0}$ | - 8 | + 24 | - 8 | + 28 | + 32 |
| 48 | 4 | 4 | 0 | 18 | 0 | - 4 | + 14 | - 4 | $+14$ | + 18 |
| 49 | 0 | 0 | 0 | 5 | 0 | 4 | + 5 | 0 | + 5 | - 0 |
|  | 212075 | 2211075 | 211075 | 211075 | \|2824| | 111 ${ }^{\text {\% }} 78$ \% | 106141 | 1115401 | 460561 | \|13446| |

TABLE 5. HISTOGRAM STATISTICS FOR TSPO DATA SET

|  | Channel 1 |  |  |  | Channel 2 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Original | NN | BL | BC | Original | NN | BL | BC |
| Mode | 30.00 | 30.00 | 28.00 | 28.00 | 27.00 | 27.00 | 27.00 | 27.00 |
| Mean | 30.24 | 30.27 | 30.27 | 30.27 | 26.80 | 26.80 | 26.80 | 26.79 |
| Mean Square | 926.15 | 924.33 | 922.4? | 924.38 | 738.67 | 737.25 | 733.53 | 737.68 |
| Variance | 11.70 | 8.21 | 6.46 | 8.31 | 20.49 | 19.24 | 15.52 | 19.82 |
| rms | 3.42 | 2.86 | 2.54 | 2.88 | 4.53 | 4.37 | 3.94 | 4.45 |
|  | Channel 3 |  |  |  |  | Chan | 14 |  |
|  | Original | NN | BL | BC | Original | NN | BL | BC |
| Mode | 34.00 | 34.00 | 32.00 | 32.00 | 19.00 | 19.00 | 19.00 | 19.00 |
| Mean | 39.14 | 39.24 | 39.24 | 39.24 | 22.37 | 22.43 | 22.43 | 22.42 |
| Mean Square | 1637.11 | 1611.92 | 1603.90 | 1612.01 | 541.83 | 541.89 | 538.47 | 542.27 |
| Variance | 105.49 | 72.08 | 63.99 | 72.50 | 41.54 | 38.84 | 35.52 | 39.53 |
| rms | 10.27 | 8.49 | 8.00 | 8.52 | 6.44 | 6.24 | 5.96 | 6.29 |

TABLE 6. HISTOGRAM DEVIATION STATSTICS FOR TSPO DATA SET

| Channel 1 | \# Changes <br> $\%$ Change | NN-O | BL-O | BC-O | BL-NN | $\mathrm{BC}-\mathrm{NN}$ | BC-BL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1096 | 18940 | 17432 | 18673 | 17243 | 8585 |
|  |  | 0.52 | 8.97 | 8.26 | 8.85 | 8.17 | 4.07 |
| Channel 2 | \# Changes | 693 | 19621 | 18473 | 19347 | 18136 | 8975 |
|  | \% Change | 0.33 | 9.30 | 8.75 | 9.17 | 8.59 | 4.25 |
| Channel 3 | \# Changes | 1393 | 33243 | 33004 | 32937 | 32780 | 7740 |
|  | Cot Change | 0.66 | 15.75 | 15.64 | 15.60 | 15.53 | 3.67 |
| Channel 4 | \# Changes | 1412 | 5639 | 4807 | 5770 | 4178 | 6723 |
|  | \% Chang | 0.67 | 2.67 | 2.28 | 2.73 | 1.98 | 3.19 |

[^1]Figures 2 through 5 present black and white representations of color coded joint histograms between channels 2 and 3 for the original data and for the three geugraphically corrected sets of data. In the figures white represents ro simultaneous occurrence of pixel values in channels 2 and 3 except for the por... . that appears in all the figures near the bottom of the joint histograms. In this case, white shows where a majority of the data occur and these data belong mostly to the forest category. Again, NN preserves most of the structure of the original joint histogram and the filtering or smoothing effect of the interpolation techniques is visible in Figures 4 and 5.

Figures 6 and 7 show the result of density slicing the original data and the BC corrected data, respectively, for channel 1 using the slices indicated in Table 1. In Tigures 6 and 7, the lighter areas represent forest and the darker areas represent agrisulture. The curvilinear feature at the left (west) center edge of the image is a portion of a river, which continues across the center of the image. The curvilinear feature starting at the middle of the bottom (suruth) edge of the image and continuing towards the top left corner is a highway. If Figure 6 is viewed from an east-west direction, the linear pattern of banding is evident. Howəver, if Figure 7 is viewed from an east-west direction the banding is considerably less evident. BL and BC tend to reduce the banding problem, whereas NN does not.

To determine where the deviations occur, absolute value difference histograms and innges were computed for the three geographic correction techniques. The images obtained from using NN, bL, and BC can only be compared with themselves and not with the original image, which has a different coordinate system. The first column in Table 7 is the absolute value grey scale differences that can occur when the geographically corrected images are absolute value differenced. The next four columns are the number of pixels in each channel that have a particular absolute value grey scale difference for comparing NN and BL . The remaining eight columns are interpreted in a similar manner. Table 8 shows the accumulative percentages for the absolute value differences. For example, when NN is being compared with BL using chennel $1,55.02$ percent of both images are identical, 89.3 percent differ by $\pm 1$ or less, and 96.28 percent of both images differ by $\pm 2$ or less. Figure 8 shows an absolute value image difference of $B L$ and $B C$ for channel 3. The areas where the is no disagreement occur where there is no symbol, and the larger and darker symbols indicate larger absolute value differences. The largest differences appear to occur at transitions between features, such as agriculture and forest, because these features are rather clearly outlined.


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Figure 3. Joint histogram of channels 2 and 3 for NN corrected data.


Figure 5. Joint histogram of channels 2 and 3 for BC corrected data.

Figure 6. Density slice image of channel 1 for the original data.


Figure 7. Density slice image of channel 1
for the BC corrected data.
TABLE 7．ABSOLUTE VALUE DIFFERENCE HISTOGRAM FOR NN，BL，AND BC OVERZAYS

|  | 范 | 惑记利 ${ }^{\circ}$ |
| :---: | :---: | :---: |
| $\begin{gathered} \text { 品 } \\ p \end{gathered}$ | \％ |  <br>  |
|  | 管 |  |
|  | 병 |  |
| ${ }_{\mid c}^{0}$ | 管 |  <br>  |
|  | 505 |  <br>  |
|  | 영 |  <br>  |
|  | 픙 |  <br>  |
| $\begin{aligned} & 9 \\ & \frac{2}{2} \\ & \vdots \end{aligned}$ | 式 | 了忍品 0 水 |
|  | \％ |  <br>  |
|  | 器 |  <br>  |
|  | 풉 |  <br>  |
|  |  |  |

TABLE 8．ACCUMULATTYE PERCENTAGES FOR ABSOLUTE VALUE DIFTERENCES

|  | 宮 | 管 | 笭 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | \％ | \％ | \％ | 号 |  |
|  | N゙ㄲ | $\begin{aligned} & 3 \\ & \text { Wi } \\ & \text { 品 } \end{aligned}$ | $\begin{aligned} & \text { ザ } \\ & \text { ஷí } \end{aligned}$ |  |  |
|  | 동 |  | $\begin{aligned} & \stackrel{\bullet 0}{-1} \\ & \stackrel{6}{6} \end{aligned}$ |  |  |
| $\begin{gathered} \text { u} \\ \underset{\sim}{4} \\ \underset{y}{2} \end{gathered}$ | 志 | $\begin{aligned} & \infty \\ & \infty \\ & \infty \\ & \dot{f} \end{aligned}$ | $\begin{aligned} & \stackrel{9}{i} \\ & -i \end{aligned}$ | $\begin{aligned} & 0 \\ & \dot{8} \\ & \dot{8} \end{aligned}$ | $\begin{aligned} & 8 \\ & 8 \\ & \dot{8} \end{aligned}$ |
|  | 垫 | $\begin{aligned} & \text { E. } \\ & \text { M } \end{aligned}$ |  | $\begin{array}{r} \dot{+} \\ \text { - } \end{array}$ | No |
|  | 逆 | $\begin{aligned} & \stackrel{\circ}{\circ} \\ & \dot{ஜ} \end{aligned}$ | $\begin{aligned} & \mathrm{N} \\ & \mathrm{E} \end{aligned}$ | $\begin{aligned} & \text { 잉 } \\ & \dot{8} \end{aligned}$ | $8$ |
|  | $\sqrt[6]{0}$ | $\begin{aligned} & \text { ஸi } \\ & \stackrel{y}{\circ} \end{aligned}$ | $\begin{aligned} & \stackrel{9}{\stackrel{1}{7}} \\ & \stackrel{\rightharpoonup}{\infty} \end{aligned}$ | $\begin{aligned} & \text { H } \\ & \dot{8} \\ & \dot{8} \end{aligned}$ |  |
| $\begin{aligned} & \text { H } \\ & \text { 分 } \\ & \text { 臬 } \end{aligned}$ | 荌 |  | $\begin{aligned} & \mathbb{Z} \\ & \infty \\ & \infty \end{aligned}$ | $\begin{aligned} & \text { 以 } \\ & \text { ì } \\ & \text { in } \end{aligned}$ |  |
|  | \％ | $\begin{aligned} & \text { 品 } \\ & \text { + } \end{aligned}$ | $\begin{aligned} & 8 \\ & \stackrel{8}{8} \end{aligned}$ | $\stackrel{セ}{5}$ | \％ \％ － |
|  | 묄 |  |  | $\begin{aligned} & \text { 중 } \\ & \text { © } \end{aligned}$ |  |
|  | 둥 | $\begin{aligned} & \text { 잉 } \\ & \text { is } \end{aligned}$ | $\begin{aligned} & \stackrel{0}{0} \\ & \dot{\infty} \end{aligned}$ | $\begin{aligned} & \text { か } \\ & \stackrel{\circ}{\circ} \end{aligned}$ |  |
| $\bigcirc$ |  |  | $\rightarrow$ | ～ | $\infty$ |



A linear pattern of agreements and disagreements can be seen in the direction from the lower left corner to the upper right cormer of Figure 8. The light linear pattems correspond to data talken from locations very close to pixels on the original image, and the dark linear patterns correspond to data taken from locations in between pixels on the original image. This linear pattern occurs in all the image differences with each pair of geographic correction techniques and, therefore, must be present to some degree in all of the geographically corrected data.

## IV. SUMMARY OF OBSERVATIONS

Based upon the results obtained from comparing the original image data and the geographically corrected image clata and from comparing the corrected data using $N N, B L$, and $B C$, the following observations were made:
a) The histograms provided information on whether or not the same number of pixels were selected from each grey scale category and transferred from the original to the geographically correct image. The histograms provide no information on where the pixel grey scale values are placed in the geographically correct image.
b) The absolute value image differences provide information on where the disagreement occurs between the correction techniques and on the consistency of the techniques, but do not indicate which technique is best.
c) In all channels, the NN histogram is most like the original data histogram in that it preserves the maxima/minima structure of the original histogram and does not create any new grey scale values.
d) The interpolation methods act as a filter smoothing out most of the original histogram maxima/minima structure and may create new great scale values that were not present in the original histogram data.
e) The following is a ranking for channels 1,2 , and 3 according to histogram similarities:

1) NN is most like $O$
2) BC is most like BL
3) BC is most like NN
4) BC is most like $O$
5) $B L$ is most like $N N$
6) BL is most like O .

There was very little difference observed between categories 4) and 5) in channels 1 and 2, but were switched in channel 3 .
f) The ranking for channel 4 was:

1) NN is most like O
2) BC is most like NN
3) BC is most like O
4) BL is most like O
5) BL is most like NN
6) BC is most like BL .

Comparing with the original histogram only, NN, BC, and BL, respectively, were most like $O$ for all channels.
g) The correction techniques appear to have little effect on the image mean value, although the mode may change, but the variance of the image was reduced. In all chamels, BC reduced the variance the least, then NN and BL, respectively.
h) Very little difference could be seen between the original and the geographically corrected images when density slicing was used. However, the interpolation methods appeared to partially remove some of the banding.
i) Comparisons of the geographically corrected images indicate that 30 to 65 percent of the pixels were in exact agreement, and that 65 to $9^{\prime \prime} 7$ prent of the pixels differed by $\pm 1$ or less.
j) In comparing the registration methods, the most agreements occurred in channel 1, then 4 , 2 and .
k) The greatest disagreements appeared it transitions between two or more features, and the majority oi disagreements the image difference. The greatest disagreements appeared to show up more readily in the infrared channels than in the visible channels.

1) A regular linear pattern of agreement and disagreement appears in all of the geographically corrected image differences, which is a direct result of the geographic transformation.
n) The CPU time for the NN, BL, and BC was $34.8,59.6$, and 135.5 s , respectively.

As a result of these observations, there are some potential problems that are worth exploration and commentary. First, if the image contained a few large homogeneous areas, then it prow hbly would not matter which geographic correction technique was used to correct the image, at least in the large homogeneous areas. The problem areas aje the transitions between two or more features. The results presented in the reference (footnote) also show that the majority of misclassifications occur at transitions between two or more features. Thus, there is a question of whether the image data should be registered (geographically corrected) and then classified or classified and then registered. If the image data are classified first, then the choice of registration techniques is limited : ' he NN. This procedure needs to be explored to determine the order and combination of registration and classification techniques that minimize classification errors.

Secondly, preliminary results using transform compression techniques indicate that the greatest deviations between the compressed/reconstructed image and the original image also occur at transition regions. Hence, the order of importance of compression and registration need to be explored as well as their combined impact on various classification techniques.

Thirdy, the transform compression techniques and the interpolation geographic correction methods act as filters on the image data, smoothing out most of the natural cliscrimination presint in the uriginal image data. These two effects, plus the fact that the transformation injects linear patterns into the image data, need to be explored for impact on change detection and multitemporal classizication.

## APPROVAL

# NEAREST NEIGHBOR, BILINEAR INTER POLATION AND BICUBIC INTER POLATION GEOGRAPHIC CORRECTION EFFECTS ON LANDSAT IMAGERY 

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The information in this report has been reviewed for security classifiction. Review of any information concerning Department of Defense or Atomic Energy Commission programs has been made by the MSFC Security Classification Officer. This report, in its entirety, has been determined to be unclassified.

This document has also been reviewed and approved for technical accuracy.


[^0]:    1. Jayroe, R., Atkinson, R., Dasarathv, B., Lybanon, M., Ramrapriyan, H.: Classification Software Technique Assessment. NASA Technical Note, NASA TN D-8240, May 1976.
[^1]:    \#Changes is the number of pixels that had to have their grey scale values reassigned. The transformation/
    registration algorithm either:

    1. Did not select all the pixels from a particular grey scale, some were left over; or
    2. Selected more pixils than were available from a particular grey, hence the pixels that were left over had to be relabeled.
