Entry Dynamics of Space Shuttle Orbiter With Longitudinal Stability and Control Uncertainties at Supersonic and Hypersonic Speeds

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SUMMARY

A six-degree-of-freedom simulation analysis was conducted to examine the effects of longitudinal static aerodynamic stability and control uncertainties on the performance of the space shuttle orbiter automatic (no manual inputs) entry guidance and control systems. To establish the acceptable boundaries, the static aerodynamic characteristics were varied either by applying a multiplier to the aerodynamic parameter or by adding an increment. The vehicle stability and control was found to be most critical from Mach 4 to 5 for the range of the entry trajectory studied. The boundaries were established as those which provided satisfactory flight in this Mach range and satisfactory trajectory targeting with either of two previously identified control system modifications included in the system.

INTRODUCTION

A reusable Earth-to-orbit transportation system known as the space shuttle is being developed by the National Aeronautics and Space Administration. The space shuttle will be capable of inserting payloads of up to 29,500 kg (65,000 lb) into a near-Earth orbit, retrieving payloads already in orbit, and landing with a payload of up to 14,500 kg (32,000 lb). The space shuttle consists of an orbiter, an external fuel tank, and two solid rocket boosters (SRB). The SRB's will be recovered after each launch for reuse. The external tank is designed for one use and is not recovered.

The orbiter will have the capability to enter the Earth's atmosphere, fly up to 2040 km (1100 n. mi.) cross range, and land horizontally. A closed-loop guidance system is being developed to provide the necessary roll-angle and angle-of-attack commands for either the automatic flight control system (primary mode) or a pilot-operated, augmented flight control system. A general description of the configuration and mission is given in reference 1.

The orbiter aerodynamic configuration has evolved through several design iterations, and wind-tunnel test data have been obtained at various conditions throughout the design evolution. There are data uncertainties due to variations in wind-tunnel conditions, instrumentation uncertainties, extrapolation of previous configuration data to the latest configuration, extrapolation of wind-tunnel data to flight, and evolutionary configuration changes from the present design to the flight hardware. Thus, to establish confidence in the overall system design, it is necessary to determine the range of uncertainties in the aerodynamic parameters with which the guidance and control systems can cope.

With the aid of a six-degree-of-freedom simulation, an analysis was undertaken to establish the ability of the system to cope with uncertainties in the aerodynamic characteristics during entry. This report presents results of the longitudinal stability and control portion of this analysis. The results of the
lateral-directional stability and control portion of the analysis are presented in reference 2.

The shuttle orbiter longitudinal stability and control characteristics have been varied during a 600-sec period of the entry during which the Mach number decreases from 13 to 1.5 and the altitude decreases from 56.4 km (185 000 ft) to 21.3 km (70 000 ft). These 600 seconds represent the period during which the orbiter performs its most extreme maneuvers and where the aerodynamic parameters are undergoing significant changes as the vehicle decelerates from hypersonic to low-supersonic velocities and the angle of attack is lowered from its deorbit value of 34.25° to 10°. These results have been obtained without considering external disturbance sources such as winds. This simulation study considered the orbiter center of gravity to be located at the most forward entry operational center of gravity (65 percent of the fuselage reference length) and offset laterally by 0.0381 m (1.5 in.), the maximum expected lateral offset.

**SYMBOLS**

Values are given in SI Units and U.S. Customary Units. Calculations were made in U.S. Customary Units. All coefficients and vehicle rates are in the body axis system. A G before any aerodynamic coefficient indicates a multiplication gain.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
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<tbody>
<tr>
<td>( \bar{c} )</td>
<td>mean aerodynamic chord, m (ft)</td>
</tr>
<tr>
<td>( C_m )</td>
<td>pitching-moment coefficient, ( \frac{\text{Pitching moment}}{q \alpha S} )</td>
</tr>
<tr>
<td>( C_{m\alpha} )</td>
<td>( \frac{\partial C_m}{\partial \alpha} ), deg⁻¹</td>
</tr>
<tr>
<td>( \Delta C_m )</td>
<td>pitching-moment increment</td>
</tr>
<tr>
<td>( \Delta C_m, \delta_{BF} )</td>
<td>pitching-moment increment due to body flap deflection</td>
</tr>
<tr>
<td>( \Delta C_m, \delta_e )</td>
<td>pitching-moment increment due to elevon deflection</td>
</tr>
<tr>
<td>( \Delta C_m, \delta_{SB} )</td>
<td>pitching-moment increment due to speed brake deflection</td>
</tr>
<tr>
<td>( I_{sp} )</td>
<td>specific impulse, sec</td>
</tr>
<tr>
<td>( I_x )</td>
<td>moment of inertia about body roll axis, kg-m² (slug-ft²)</td>
</tr>
<tr>
<td>( I_y )</td>
<td>moment of inertia about body pitch axis, kg-m² (slug-ft²)</td>
</tr>
<tr>
<td>( I_z )</td>
<td>moment of inertia about body yaw axis, kg-m² (slug-ft²)</td>
</tr>
<tr>
<td>( I_{xz} )</td>
<td>cross product of inertia about body roll and yaw axes, kg-m² (slug-ft²)</td>
</tr>
<tr>
<td>L/D</td>
<td>lift-drag ratio</td>
</tr>
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</table>
Mach number

body roll rate, deg/sec

body pitch rate, deg/sec

free-stream dynamic pressure, Pa \((\text{lb}/\text{ft}^2)\)

reference area, \(m^2 (\text{ft}^2)\)

Earth relative velocity, \(m/\text{sec.(ft/sec)}\)

angle of attack, deg

change in angle of attack, deg

change in commanded angle of attack, deg

sideslip angle, deg

aileron deflection angle, \((\delta_e,\text{left} - \delta_e,\text{right})/2\), deg

body flap deflection angle (positive down), deg

elevon deflection angle, \((\delta_e,\text{left} + \delta_e,\text{right})/2\), deg

rudder deflection angle (positive trailing edge, left), deg

speed brake deflection angle (positive open), deg

body roll angle, deg

Subscripts:

\(i\) initial condition

\(c\) command

**SPACE SHUTTLE ORBITER DESCRIPTION**

The physical characteristics of the space shuttle orbiter used in this study are summarized in table I. A sketch of the orbiter is shown in figure 1. The mission used was a once-around return from a \(104^\circ\) inclined orbit launched from the Western Test Range. Figure 2 depicts this entry on a world map and figure 3 shows some of the trajectory parameters.

**Guidance System**

A guidance system has been designed to provide the necessary roll-angle and angle-of-attack commands for either the automatic flight control system or for
pilot displays for an augmented manual flight control system. The entry guidance is designed to direct the orbiter from 121.9 km (400 000 ft), the atmospheric interface, down to 21.3 km (70 000 ft), the beginning of the landing phase. The entry down range and cross range are controlled through roll-angle modulation, whereas the angle of attack follows a preselected schedule. The guidance system is described in more detail in appendix A of reference 3.

Automatic Flight Control System

This control system compares the vehicle attitude with the guidance commands and directs aerodynamic control-surface deflections and the reaction control system (RCS) jet firings. The aerodynamic control surfaces depicted in figure 1 include elevons (which are used as ailerons and elevators), a rudder with speed brake capability, and a body flap for longitudinal trim. RCS jets are used to supplement control about the roll, pitch, and yaw axes. The roll and pitch jets are used only during the early part of the entry at low dynamic pressures. The jets have a nominal vacuum thrust of 3870 N (870 lb). To approximate the effects of thrust buildup with time and thrust loss due to back pressure increases with decreasing altitude, an average thrust level of 3336 N (750 lb) and an Isp of 242 seconds for each jet were used in this study.

The longitudinal part of the control system uses the elevons to achieve the commanded angle of attack and provide pitch rate damping. The body flap deflection is based on the longitudinal center-of-gravity location and in the study was at the upward deflection limit of -11.7°. The speed brake follows the deflection schedule shown in figure 4 which provides a nose-up increment in pitch and allows the elevons to have a more downward deflection.

The lateral-directional part of the control system operates in two basic modes. In the spacecraft mode (α > 18° or M > 5), the roll-angle command from the guidance system is directed to the yaw RCS channel, which produces a yawing rate and a small β, and allows the effective dihedral of the orbiter to generate a rolling moment. The ailerons are used for turn coordination. In the spacecraft mode the rudder is not engaged. The control system switches to the aircraft mode when α ≤ 18° and M ≤ 5. In this mode the ailerons are used for roll control and the rudder, now activated, with yaw jet augmentation is used for turn coordination. The control system is described in more detail in appendix B of reference 3.

SIMULATION DESCRIPTION

The automatic reentry flight dynamics simulator (ARFDS) used for this study is an automatic (unmanned), nonlinear, six-degree-of-freedom, interactive, digital computer program developed at the Langley Research Center that utilizes hardware developed for real-time simulations (ref. 3). ARFDS is controlled from a console where changes can be made between and during runs; such changes include multiplying aerodynamic parameters by constants or adding increments, modifying initial conditions, and altering system gains. This capability has been used to start at different points in the trajectory when flying with the guidance system or to bypass the guidance system and put in step commands to the control system.
at various conditions. The vehicle response is observed on time-history strip charts.

The nominal entry trajectory used in this study was for a once-around southerly launch from the Western Test Range requiring approximately 1852 km (1000 n. mi.) cross range.

The nominal aerodynamic characteristics used in this study are from the data base available as of June 1974. These data include longitudinal and lateral-directional static aerodynamic characteristics and damping derivatives. The nominal values of the longitudinal stability and control derivatives are shown in figures 5 to 8. Interference and cross-coupling effects from reaction control system (RCS) jets were also accounted for throughout the speed range as described in reference 3. The actuators for the elevens and rudder were approximated by first-order lag filters with rate and position limiting.

AERODYNAMIC PARAMETER VARIATION

Four longitudinal stability and control parameters were varied both independently and in combination to determine how uncertainties in these parameters would affect vehicle controllability and the vehicle capability to meet the guidance performance requirements. The longitudinal parameters were: the pitching moment for undeflected controls (Cm), the pitching-moment increment for elevon control effectiveness (ΔCm, δe), the pitching-moment increment for body flap control effectiveness (ΔCm, δBF), and the pitching-moment increment for speed brake control effectiveness (ΔCm, δSB). The nominal data at Mach numbers 1.5, 3.0, 4.0, and 5.0 are shown in figures 5 to 8. The pitching moment for undeflected controls was varied both by an increment and/or a multiplier. The increment of Cm (ΔCm) varied the level of the pitching moment only, whereas the multiplier also varied the stability (Cm|).

CRITERIA FOR SATISFACTORY FLIGHT

There are several criteria by which the simulation results can be judged and those used in this study are shown in table II. The normal acceleration limit was never exceeded in this study unless control was lost completely. Varying the longitudinal characteristics generally resulted in changing the elevon angle at a given Mach number and angle-of-attack combination. Since the elevens were also used for roll control and the yaw due to aileron changed with elevon angle (see ref. 2), the lateral-directional dynamics were directly affected by varying the longitudinal characteristics. Thus, the ϕ oscillation and the RCS fuel consumption were appropriate criteria in this study.

CRITICAL COMBINATIONS

Vehicle response to step commands and guidance system directed entry simulations were performed with the multipliers or increments on the aerodynamic parameters held constant during a simulation. The simulation results were compared with these criteria to determine when the system exhibited satisfactory perform-
The aerodynamic parameters in these simulations were varied first independently, since the four longitudinal parameters were considered to be independent of one another, and then in combination to establish critical combinations. A critical combination is a set of off-nominal parameters in which a criteria violation will occur if the variation from the nominal of any one of the parameters is increased. In some instances the variation of a parameter was reduced to allow larger variation in other parameters to obtain more reasonable parameter variation bounds. These critical combinations determined the boundary values for each parameter.

DISCUSSION OF RESULTS

During the entry phase under study (see fig. 3), the nominal pitching moment of the orbiter with undeflected controls was negative (nose down). Some nose-up moment (positive $C_m$) is provided by deflecting the speed brake through the deflection schedule shown in figure 4. The resulting nominal elevon deflection angle and the angle-of-attack trends with Mach number are shown in figure 9. The elevon history results from changing pitching-moment characteristics with Mach number and angle of attack, the pitch down motion, cross coupling from roll reversal maneuvers, and the speed brake schedule. From Mach 4.5 to Mach 4, the speed brake closes down from 85° to 55°. Thus, the elevon deflection goes from its least negative value to about Mach 4.6 to nearly its most negative value just below Mach 4 as is seen in figure 9.

Entry simulations, in which guidance commands are fed to the control system, revealed that the major impact of varying the longitudinal stability and control parameters was to change the elevon deflection required to follow the commanded angle-of-attack schedule. Thus, the elevon angles and vehicle response at Mach 5 and Mach 4 are used hereafter as key indicators of the effects of uncertainties in the presentation of the simulation results.

Variation of $C_m$

The pitching moment for undeflected controls was varied both by applying increments (which result in a shift of the pitching-moment curves) and by multipliers (which also change the stability level). The results are presented in figures 10 to 12.

Increments from $-0.014$ to $0.014$ were applied to the pitching-moment coefficient and the resulting elevon angles that occurred at Mach 4 and 5 in the entry simulations are shown in figure 10. There was substantial change in the elevon angle at both Mach numbers but no significant effect was noted in the entry simulations. A further test of the effect of this change on the system is shown in figure 11. The vehicle response to a step roll-angle command and a constant angle-of-attack command is presented for nominal aerodynamics and with a pitching-moment increment of $0.014$. These results are for $M_s = 4$ which is just after the switchover to the aircraft mode. At this point in the trajectory, the lateral-directional control system is weak (see ref. 2) and is therefore very sensitive to the elevon angle. In these simulations the vehicle is untrimmed directionally (the center of gravity is offset laterally $0.0381$ m (1.5 in.)) so
the control activity during the first 10 seconds is to establish the trim. At 10 seconds the control system receives a 60° roll-angle step command. Figure 11(a) shows that the vehicle responds by producing a maximum roll rate of about 5°/sec with little sideslip (B). The roll angle reaches the command value at about 25 seconds and experiences a slight overshoot which is quickly nulled. There is a very small pitch rate and α is constant. With a pitch increment of 0.014, figure 11(b) shows that the vehicle has some difficulty accomplishing the maneuver. The maximum roll rate (p) is about 4°/sec and there is about 5° overshoot in roll angle followed by a convergent oscillation. This type of response will be discussed in more detail later in this paper. The vehicle response was also examined for a pitching-moment increment of -0.014 at both Mach 4 and 5 and both of these cases had less overshoot than the one shown in figure 11. In these simulations there was no longitudinal stability or control problem and the vehicle was able to target properly in closed loop simulations.

The elevon deflection angles that occurred at Mach 4 and 5 in entry simulations with a multiplier on Cm are shown in figure 12. Decreasing the multiplier results in a more downward deflection of the elevons to provide a nose-down increment to counter the loss of the nose-down increment in Cm. Increasing the multiplier or the nose-down increment drives the elevon in the negative direction to provide a nose-up increment. Between GCm values of 0.2 to 1.6, the vehicle remains controlled and achieves the guidance targeting requirements. For a value of 1.8, the vehicle followed the control commands well but was unable to meet the targeting requirements at 457 m/sec (1500 ft/sec). The degraded L/D due to negative elevon was apparently insufficient for the guidance algorithm.

A GCm value of zero drove the elevon sufficiently positive so that the adverse yaw due to aileron resulted in a buildup in β when the aileron tried to control the roll angle and control was lost. In these simulations there still was no indication of a longitudinal stability or control problem due to these variations in GCm.

Variation of Control Effectiveness

The effect of multiplier variation GΔCm,δe on elevon deflection at M = 4 and 5 during entry simulation is shown in figure 13. As the control authority of the elevon is increased, the elevon angle (δe) is driven toward zero. As the effectiveness is decreased, a more negative deflection is required to produce the positive (nose-up) increment. For a GΔCm,δe value of 0.3, δe reached the limit of -35° (data point not shown). With GΔCm,δe = 0.4, the vehicle was unable to meet the guidance targeting requirements because of the degraded L/D.

The effects of applying multipliers to the nose-up increments due to the fixed body flap and scheduled speed brake in entry simulations are shown in figure 14. Multipliers from 0.2 to 1.6 on each of these parameters separately did not significantly affect the elevon deflection angle or the ability of the vehicle to remain controlled.

Although the elevon angle at Mach 5 is one of the more positive elevon angles in the trajectory, it does not seem to be a significant point in the trajectory in this study. The control problems have been shown to develop after
switchover to the rudder-aileron system. The ranges of the multipliers used in this study have not been found to affect the system prior to switchover except when $\delta_e$ in the entry simulations went to $-35^\circ$. Therefore, in the ensuing discussion, only the $\delta_e$ that occurs in the entry simulations at Mach 4 is presented in the results.

Combined Variation of $C_m$ and $\Delta C_m, \delta_e$

The effects of multiplier variation on $C_m$ for degraded elevon effectiveness on the entry simulation-elevon deflection at Mach 4 are shown in figure 15. The decreased control effectiveness had a marked effect upon the variation of $\delta_e$ with $G_C m$ as the figure shows. At Mach 4, the combination of increased stability and decreased control effectiveness required elevon deflections near the upper limit. For $G_A C_m, \delta_e = 0.6$ and $G_C m = 1.4$, vehicle response simulation results after switchover showed that control was lost because of insufficient aileron remaining for roll control. For $G_C m = 1.3$, the vehicle failed to meet the guidance algorithm targeting requirements as roll control after switchover was loose and L/D was degraded. For $G_A C_m, \delta_e = 0.7$ and $G_C m = 1.4$ the vehicle also failed to achieve the targeting requirements for the aforementioned reasons. A series of plots depicting the vehicle response to a step roll-angle command at $M_1 = 4$ is presented in figure 16 for $G_A C_m, \delta_e = 0.7$ and $G_C m = 1.4$. Since $\delta_e$ was less than $-30^\circ$ and the elevon position limit is $-35^\circ$, there was insufficient aileron control to arrest the reversal and control was lost. For $G_A C_m, \delta_e = 0.7$ with $G_C m = 1.3$ and $G_A C_m, \delta_e = 0.6$ with $G_C m = 1.2$, the vehicle achieved the targeting requirements even though the roll angle was difficult to maintain.

For $G_C m = 0.2$ and $G_A C_m, \delta_e = 0.6$, control was lost when the vehicle was unable to control $\beta$ and the roll angle after switchover. For $G_C m = 0.3$ and $G_A C_m, \delta_e = 0.6$, the vehicle recovered from a $\beta$ of 1.7° and a roll-angle error oscillation of 33° after switchover to fly the guidance system roll-angle limits and achieve the targeting requirements. Also 86 kg (190 lb) of yaw RCS fuel was expended to augment the rudder after switchover. For $G_C m = 0.4$ and $G_A C_m, \delta_e = 0.6$ and 0.7, the vehicle recovered from roll-angle errors of 11° and 10°, respectively, and achieved the targeting requirements.

Figure 17 presents the vehicle response to a step roll-angle command at $M_1 = 4$ for both $G_C m = 0.3$ and 0.4 and $G_A C_m, \delta_e = 0.6$. For $G_C m = 0.3$ (fig. 17(a)) the roll oscillation following the roll-angle change was rather severe with large sideslip angles. The rudder along with significant yaw jet firing (the steps in the $\delta_r$ curve indicate when the yaw jets fire) was eventually able to control the sideslip angle satisfactorily. For $G_C m = 0.4$, the rudder was able to control the sideslip angle without yaw jet augmentation, and roll-angle control was improved.

Increased elevon effectiveness ($G_A C_m, \delta_e > 1$) reduced the effect of $G_C m$ variation as is shown in figure 18 where the $\delta_e$ occurring at Mach 4 in entry simulations is plotted. The vehicle handled properly and achieved the guidance targeting requirements for all the data points shown.
The elevon effectiveness was varied for several values of $GC_m$ and the $\delta_e$ values occurring at Mach 4 in entry simulations are shown in figure 19. As $GAC_m, \delta_e$ was decreased, $\delta_e$ goes toward the extremes depending upon the value of $GC_m$. For $GC_m = 0.4$ and $GAC_m, \delta_e = 0.4$, the vehicle was barely able to achieve the targeting requirements after recovering from a roll-angle control problem after switchover. The guidance targeting requirements were achieved for $GC_m = 0.6$ for the values of $GAC_m, \delta_e$ shown ($GAC_m, \delta_e > 0.6$). Also the targeting requirements were met for $GC_m = 1.2$ and the values of $GAC_m, \delta_e$ shown. For $GC_m = 1.3$, $GAC_m, \delta_e$ must be equal to or greater than 0.7 to generate sufficient L/D to achieve the targeting requirements. Thus, some critical values of $GC_m$ and $GAC_m, \delta_e$ are identifiable, namely $GAC_m, \delta_e = 0.7$, $GC_m = 0.4$, and $GC_m = 1.3$. A $GAC_m, \delta_e$ value of 1.8 is a boundary value because simulation tests were not conducted at larger values.

Combined Variation of $C_m$, $\Delta C_m, \delta_e$, $\Delta C_m, \delta_{BF}$, and $\Delta C_m, \delta_{SB}$

Both the body flap and speed brake provide positive (nose-up) pitching-moment increments (figs. 7 and 8) and variations in these coefficients have been shown to have little effect on the vehicle with otherwise nominal aerodynamics. The positive pitch increment of these devices will result in more positive elevon deflections for multipliers greater than one. (See fig. 14.) Thus, whenever $GC_m$ and $GAC_m, \delta_e$ are near boundary values for positive elevon deflections, multipliers on body flap and/or speed brake pitching moment will affect controllability and targeting capability.

For $GAC_m, \delta_e = 1.8$ and $GC_m$ between 0.4 and 1.3, body-flap multiplier variations from 0.6 and 1.4 have little effect on the elevon deflection (fig. 20(a)) and the controllability. For $GC_m = 0.4$, $GAC_m, \delta_e = 0.7$, and $GAC_m, \delta_{BF} = 1.4$ (fig. 20(b)), $\delta_e$ was increased to the point where the adverse yaw due to aileron made roll-angle control poor after switchover and the vehicle barely missed achieving the targeting requirements. For $GC_m = 0.6$ and the values of $GAC_m, \delta_{BF}$ shown, targeting requirements were met. The vehicle response to a step roll-angle command at M_i = 4 for $GC_m = 0.4$ and 0.6 with $GAC_m, \delta_e = 0.7$ and $GAC_m, \delta_{BF} = 1.4$ is shown in figure 21. The difficulty with roll angle ($\theta$) and sideslip ($\beta$) for $GC_m = 0.4$ is apparent and the improvement in going to $GC_m = 0.6$ is evident as $\delta_e$ was decreased from about 3° to -1° which decreases the adverse yaw due to aileron. Reducing $GAC_m, \delta_{BF}$ to 1.3 for $GC_m = 0.4$ and $GAC_m, \delta_e = 0.7$ had negligible effect on the system performance.

For $GAC_m, \delta_e = 0.7$ and $GC_m = 1.3$ (fig. 20(b)), the vehicle tended to roll off after switchover but it was able to meet the targeting requirements for the values of $GAC_m, \delta_{BF}$ shown. For $GC_m = 1.2$, the vehicle did not experience the roll-off tendency.

The effects of variations of the speed brake effectiveness in the presence of increased and/or decreased $C_m$ and elevon effectiveness are presented in figure 22. For $GAC_m, \delta_e = 1.8$, there is little effect for both increased and decreased $C_m$. (See fig. 22(a).) For decreased elevon effectiveness, $GAC_m, \delta_e = 0.7$, and for decreased $C_m$, $GC_m = 0.4$ (fig. 22(b)), the vehicle barely met the targeting requirements for $GAC_m, \delta_{SB} = 1.4$. The sideslip angle $\beta$ reached 1.35° after switchover and roll-angle control was very poor. For
increased stability, $G C_m = 1.2$, roll angle tended to be poor but the vehicle was able to meet the targeting requirements for the values of $G A C_m, \delta_{SB}$. For $G C_m = 1.3$ and $G A C_m, \delta_{SB} < 0.7$ the vehicle was unable to meet the targeting requirements because of the degraded $L/D$.

The preceding discussion has shown that degraded elevon effectiveness, when combined with variations in $C_m$ and either body-flap or speed-brake effectiveness variations, resulted in marginal performance for several combinations. This performance was poorest when all four parameters were varied. For example, although $G C_m = 0.4$, $G A C_m, \delta_e = 0.7$, and $G A C_m, \delta_{BF} = 1.4$ barely met the targeting requirements, adding in $G A C_m, \delta_{BF} = 1.4$ resulted in control loss. For $G A C_m, \delta_{SB} = G A C_m, \delta_{BF} = 1.3$, $G C_m = 0.4$, and $G A C_m, \delta_e = 0.7$, roll-angle control was very poor and the targeting requirements were not met. A further decrease in the multipliers for speed brake and body flap effectiveness provided satisfactory performance; however, it was decided to retain some tolerance in both the speed brake and body flap effectiveness and decrease the tolerance in $C_m$, that is, make $G C_m = 0.6$ a boundary value instead of $G C_m = 0.4$. Similarly, it was decided to change the upper $G C_m$ boundary from $1.3$ to $1.2$, since when $G C_m = 1.3$, $G A C_m, \delta_e = 0.7$, and $G A C_m, \delta_{SB} = 0.7$, the vehicle failed to meet targeting requirements. The multiplier $G A C_m, \delta_e$ could have been changed to 0.8 from 0.7 and achieved the same result; however, to obtain a more symmetrical tolerance band for $G C_m$ it was decided to change the boundary value for $G C_m$ in lieu of $G A C_m, \delta_e$. With these boundary values for $G C_m$ established, the effects of varying $G A C_m, \delta_{SB}$ and $G A C_m, \delta_{BF}$ together are shown in figures 23 to 25.

For $G A C_m, \delta_e = 1.8$ (fig. 23), there was little effect on $\delta_e$ at Mach 4 in the entry simulations over the range of variations shown. With $G C_m = 0.6$ and $G A C_m, \delta_{BF} = G A C_m, \delta_{SB} = 1.4$, the vehicle met the targeting requirements and controlled satisfactorily. The vehicle response to a step roll-angle command at $M_i = 4$ for these multiplier values is shown in figure 24. There was some roll-angle overshoot and an oscillation which damps out.

The elevon deflection angles occurring at Mach 4 in entry simulations for $G A C_m, \delta_e = 0.7$ are shown in figure 25. For $G C_m = 0.6$ and the values of $G A C_m, \delta_{BF} < 1.0$ (shown in fig. 25(a)), the vehicle roll-angle errors were minimal and targeting requirements were met. For $G A C_m, \delta_{BF} = 1.4$ and the values of $G A C_m, \delta_{BF}$ shown, the vehicle also performed satisfactorily. For $G A C_m, \delta_{BF} = 1.6$ and $G A C_m, \delta_{SB} = 1.6$, however, the vehicle was unable to meet targeting requirements, and roll-angle excursions were greater than $20^\circ$ after switchover. $G A C_m, \delta_{SB} = 1.4$ resulted in some improvement over $G A C_m, \delta_{SB} = 1.6$. The vehicle response at $M_i = 4$ for $G A C_m, \delta_{BF} = 1.6$ and $G A C_m, \delta_{SB} = 1.4$ is shown in figure 26. The oscillation following the reversal does not appear to be damping out readily; thus, this combination was not considered to be satisfactory.

The results for $G C_m = 1.2$ are shown in figure 25(b). For $G A C_m, \delta_{BF} = 1.4$, the vehicle performed satisfactorily for all values of $G A C_m, \delta_{SB}$ shown. For $G A C_m, \delta_{BF} = 0.8$, the vehicle also performed satisfactorily for the points shown. For $G A C_m, \delta_{BF} = 0.7$ and $G A C_m, \delta_{SB} = 1.0$, the vehicle was required to fly the guidance minimum roll-angle limits to meet the targeting requirements. Nevertheless, the targeting capability was adequate for $G A C_m, \delta_{SB} = 0.8$ and 0.7 whereas the vehicle was unable to meet targeting requirements for $G A C_m, \delta_{SB} = 0.6$. 
Parameter Boundary Values

At this point some apparent boundary values for each of the four parameters have emerged, based on controllability and the targeting ability. The boundary values of the multipliers are as follows: the pitching moment $G_{Cm}$ can be varied between 0.6 and 1.2; the elevon effectiveness in pitch $GAC_{m,\delta e}$ can be varied from 0.7 to 1.8; the body flap effectiveness in pitch $GAC_{m,\delta BF}$ can be varied from 0.7 to 1.4; and the speed brake effectiveness in pitch $GAC_{m,\delta SB}$ can be varied from 0.7 to 1.4. The ranges for each of these coefficients assume that each of the other coefficients is within its respective boundaries and the lateral-directional aerodynamics are nominal. Also, it was shown initially that an increment in pitching moment from -0.014 to 0.014 can be tolerated by the system.

Discussion of Roll-Off Tendency

In the previous discussion, it was shown that when the elevon deflection was positive at switchover, there tended to be a build-up of the sideslip angle $\beta$ accompanied by poor roll-angle control which sometimes resulted in loss of control. A detailed analysis of this tendency discussed in reference 2 showed that the rolling moment due to sideslip angle can be sufficient to overpower the aileron. This was particularly true when the yaw due to aileron deflection was adverse which means that as the aileron was deflected to counter the induced rolling moment, a yawing moment was generated which increased the sideslip angle and induced more adverse rolling moment. The rudder is designed to control this yawing tendency but at switchover at $\alpha = 18^\circ$, the rudder is weak. Increasing the yaw jet augmentation of the rudder after switchover, as proposed in reference 2, has been found to improve the sideslip control and reduce the tendency to roll off. For $G_{Cm} = 0.6$, $GAC_{m,\delta e} = 0.7$, $GAC_{m,\delta BF} = 1.4$, and $GAC_{m,\delta SB} = 1.4$, increased yaw jet augmentation of the rudder reduced $\beta$ from 0.64° to 0.28° and reduced roll-angle error from about 11° to less than 3° in the entry simulations. The system consumed 23 kg (51 lb) more RCS fuel with increased augmentation and the targeting capability was improved slightly. Other combinations of boundary values of the multipliers also showed improved roll-angle control and required less than the increment of 23 kg (51 lb) of RCS fuel. Figure 27 shows the vehicle response to a roll-angle reversal at $M_1 = 4$ with and without increased rudder augmentation by the yaw jets for $G_{Cm} = 0.6$, $GAC_{m,\delta e} = 0.7$, and $GAC_{m,\delta BF} = GAC_{m,\delta SB} = 1.4$. With the increased augmentation the oscillation following the roll reversal is virtually eliminated. Notice the sawtooth appearance of the rudder curve with increased augmentation that indicated the firing of the yaw jet. Delaying the switchover to an angle of attack of 15°, as discussed in reference 2, for the condition $G_{Cm} = 0.6$, $GAC_{m,\delta e} = 0.7$, $GAC_{m,\delta BF} = 1.4$, and $GAC_{m,\delta SB} = 1.4$ also resulted in smaller sideslip angles and bank angle errors after the switchover since the rudder is more effective at the lower angle of attack and lower Mach number. Again the targeting was slightly improved and about 18 kg (39 lb) more RCS fuel was consumed as the entry controller, using the yaw RCS jets for roll-angle control, was used for a longer period of time.
System Response Analysis

The control system was commanded to respond to both 2° angle-of-attack step commands and 30° roll-angle step commands (as defined in the procurement specification) separately at 3048 m/sec (10 000 ft/sec), 1524 m/sec (5000 ft/sec), 1067 m/sec (3500 ft/sec), and 610 m/sec (2000 ft/sec). Generally, the system performed well even with the boundary values for the coefficients. The procurement specification response envelope was not met in all cases as is shown in figure 28. For $G_{C_m} = 1.2$, $G_{AC_m,SE} = 0.7$, $G_{AC_m,BF} = 0.7$, and $G_{AC_m,SB} = 0.7$, the elevon was deflected up and when the system was commanded to pitch up 2°, the elevon moved to very near the up deflection limit at 1067 m/sec (3500 ft/sec) and 610 m/sec (2000 ft/sec). This was the worst response of the combinations and conditions tested. Thus, the boundary values herein established do not necessarily meet the procurement specification but they are not far from the response of the nominal system. With nominal lateral-directional aerodynamics and these boundary values, the system did respond satisfactorily to 30° roll-angle step commands with increased rudder augmentation.

CONCLUSIONS

A six-degree-of-freedom simulation analysis was conducted to examine the effects of longitudinal static aerodynamic stability and control uncertainties on the performance of the space shuttle orbiter automatic (no manual inputs) entry guidance and control systems. To establish the acceptable boundaries, the static aerodynamic characteristics were varied either by applying a multiplier to the aerodynamic parameter or by adding an increment. The vehicle stability and control was found to be most critical from Mach 4 to 5 for the range of the entry trajectory studied and the vehicle was found to fly satisfactorily in this Mach range on or within the following boundaries:

1. The pitching-moment coefficient can be decreased to 0.6 or increased to 1.2 times its nominal value.

2. The elevon effectiveness in pitch can be from 0.7 to 1.8 times its nominal value.

3. The body flap effectiveness in pitch can be from 0.7 to 1.4 times the nominal value.

4. The speed brake effectiveness in pitch can be from 0.7 to 1.4 times the nominal value.

5. If an increment in the pitching moment is allowed to cover all these off-nominal values, the increment can be from -0.014 to 0.014.

Basically, the system appeared sound in longitudinal stability and controllability. However, lateral-directional stability and control weaknesses were affected...
by pitching-moment variations and two system modifications were found to help establish satisfactory performance in the boundaries listed.

Langley Research Center
National Aeronautics and Space Administration
Hampton, VA 23665
August 17, 1977

REFERENCES


TABLE I.- PHYSICAL CHARACTERISTICS OF SPACE SHUTTLE ORBITER

Mass properties:

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
<th>Conversion</th>
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<tbody>
<tr>
<td>Mass, kg (lb)</td>
<td>83 001 (182 986)</td>
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<tr>
<td>$I_x$, kg-m² (slug-ft²)</td>
<td>1 029 052 (759 000)</td>
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<tr>
<td>$I_y$, kg-m² (slug-ft²)</td>
<td>7 816 187 (5 765 000)</td>
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</tr>
<tr>
<td>$I_z$, kg-m² (slug-ft²)</td>
<td>8 015 489 (5 912 000)</td>
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<tr>
<td>$I_{xz}$, kg-m² (slug-ft²)</td>
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Wing:

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<th>Conversion</th>
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<td>Reference area, m² (ft²)</td>
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<td>$c$, m (ft)</td>
<td>12.06 (39.57)</td>
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<td>Span, m (ft)</td>
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Elevon:

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<th>Conversion</th>
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<td>Reference area, m² (ft²)</td>
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<td>Chord, m (ft)</td>
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Rudder:

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<td>Chord, m (ft)</td>
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Body flap:

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<td>Reference area, m² (ft²)</td>
<td>12.54 (135.0)</td>
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<tr>
<td>Chord, m (ft)</td>
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TABLE II.- SYSTEM PERFORMANCE CRITERIA

<table>
<thead>
<tr>
<th>Criterion</th>
<th>Requirement</th>
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<tbody>
<tr>
<td>Entry guidance target requirements</td>
<td>Altitude error ≤+0.3 km (+1000 ft); range error ≤+9.3 km (+5 n. mi.); flight-path angle error ≤±1°</td>
</tr>
<tr>
<td>Normal acceleration</td>
<td>≤2.5g</td>
</tr>
<tr>
<td>Amplitude of $\phi$ oscillation</td>
<td>≤±10°</td>
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<tr>
<td>Increase in RCS fuel consumption due to</td>
<td>≤135 kg (300 lb)</td>
</tr>
<tr>
<td>off-nominal aerodynamics</td>
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</table>
Figure 1 - Space shuttle orbiter.
Figure 2.- Space shuttle orbiter entry.
Figure 3.- Space shuttle orbiter entry trajectory parameters.
Figure 3.— Concluded.
Body flap schedule

Forward center of gravity, $\delta_{BF} = -11.7^\circ$

Aft center of gravity, $\delta_{BF} = 16.3^\circ$

Speed brake schedule

Figure 4.- Body flap and speed brake schedules.
Figure 5. - Pitching moment for undeflected controls.
Figure 6.- Elevon effectiveness.

(a) $M = 1.5$. 

$\delta_e, \text{deg}$

$\alpha, \text{deg}$
Figure 6.- Continued.

(b) $M = 3.0$

$\delta_e, \text{deg}$

$\Delta c_m, c_a$

$a, \text{deg}$
Figure 6. - Continued.

(c) $M = 4.0$.

$\delta_\alpha$, deg

$\Delta C$, $\delta e$

$\alpha$, deg
(d) $M = 5.0$.

Figure 6.- Concluded.
Figure 7.- Body flap effectiveness. \( \delta_{BF} = -11.7^\circ \).
Figure 8.- Speed brake effectiveness.
Figure 10. Effect of pitching-moment increment on elevon deflection.
Figure 11.- Vehicle response simulations at $M_i = 4$ with various levels of $\Delta C_m$ ($\alpha_c = 17.6^\circ$, $\phi_c = -30^\circ$ for time $<10$ sec and $\phi = 30^\circ$ for time $\geq 10$ sec).
Figure 11.- Continued.

(a) Concluded.
(b) $\Delta C_m = 0.014$.

Figure 11.-- Continued.
Figure 11.— Concluded.
Figure 12.- Effect of pitch stability variation on elevon deflection.
Figure 13.- Effect of elevon effectiveness variation on elevon deflection.
Figure 14.- Effect of body-flap and speed-brake effectiveness variation on elevon deflection.
Figure 15. Effects of pitch stability variation on elevon deflection with degraded elevon effectiveness. M = 4.
Figure 16.- Vehicle response simulations at $M_1 = 4$ for $GC_m = 1.4$ and $G\Delta C_m,\delta e = 0.7$ ($\alpha_c = 17.6^\circ$, $\phi_c = -30^\circ$ for time $<10$ sec and $\phi_c = 30^\circ$ for time $\geq 10$ sec).
Figure 16.— Concluded.
Figure 17.- Vehicle response simulations at $M_1 = 4$ with $G\Delta C_m, \delta_e = 0.6$ with varying $G C_m$ ($\alpha_c = 17.6^\circ$, $\phi_c = -30^\circ$ for time <10 sec and $\phi_c = 30^\circ$ for time $\geq 10$ sec).
(a) Concluded.

Figure 17.- Continued.
Figure 17.- Continued.

\[ GC_m = 0.4. \]
(b) Concluded.

Figure 17.— Concluded.
Figure 18.- Effects of pitch stability variations on elevon deflection with increased elevon effectiveness. \( M = 4 \).
Figure 19.- Effects of elevon effectiveness variation on elevon deflection with increased and decreased pitch stability.  $M = 4$. 
Figure 20.- Effects of body-flap effectiveness variation on elevon deflection with increased and decreased pitch stability and elevon effectiveness. $M = 4$.
Figure 20.- Concluded.

(b) $G\Delta C_m, \delta e = 0.7$.

$G\Delta C_m, \delta e$
Figure 21.- Vehicle response simulations at $M_i = 4$ with $G\Delta C_m \delta e = 0.7$ and $G\Delta C_m \delta BF = 1.4$ with varying $G C_m$ ($\alpha_c = 17.6^\circ$, $\phi_c = -30^\circ$ for time <10 sec and $\phi_c = 30^\circ$ for time $\geq$10 sec).
(a) Concluded.

Figure 21.- Continued.
Figure 21.- Continued.

(b) $G_{C_m} = 0.6$. 

Figure 21.- Continued.
(b) Concluded.

Figure 21.- Concluded.
Figure 22.- Effects of speed-brake effectiveness variation on elevon deflection with increased and decreased pitch and elevon effectiveness. $M = 4$. 

(a) $\Delta C_m, \delta e = 1.8$. 

$\delta e$, deg

$G C_m$

- $0.4$
- $0.6$
- $1.2$
- $1.3$

$G \Delta C_m, \delta SB$

$0.6$ $1.0$ $1.4$
Figure 22.- Concluded.

(b) $GAC_m, \delta e = 0.7$. 

Figure 22.- Concluded.
Figure 23.— Effects of speed-brake effectiveness variation on elevon deflection with increased and decreased pitch stability and body flap effectiveness and increased elevon effectiveness. $G\Delta C_{m,\delta e} = 1.8$; $M = 4$. 

$G_{C_m}$ $G\Delta C_{m,\delta BF}$

- ○ 0.6 0.7
- □ 0.6 1.4
- ◊ 1.2 0.7
- △ 1.2 1.4
Figure 24.- Vehicle response simulations at $M_i = 4$ with $GC_m = 0.6$, $GAC_m, \delta_e = 1.8$, $GAC_m, \delta_{BF} = 1.4$, and $GAC_m, \delta_{SB} = 1.4$ ($\alpha_c = 17.6^\circ$, $\phi_c = -30^\circ$ for time <10 sec and $\phi_c = 30^\circ$ for time $\geq 10$ sec).
Figure 24.—Concluded.
Figure 25.- Effects of speed-brake effectiveness variation on elevon deflection with increased and decreased body flap effectiveness and pitch stability and decreased elevon effectiveness. $G_{A C_m, \delta e} = 0.7$; $M = 4$. 

(a) $G_{C_m} = 0.6$. 
Figure 25.- Concluded.

(b) \( GC_m = 1.2 \).

Figure 25.- Concluded.
Figure 26.— Vehicle response simulations at $M_\perp = 4$ with $GC_m = 0.6$, $G\Delta C_m, \delta_e = 0.7$, $G\Delta C_m, \delta_{BF} = 1.6$, and $G\Delta C_m, \delta_{SB} = 1.4$ ($\alpha_c = 17.6^\circ$, $\phi_c = -30^\circ$ for time $< 10$ sec and $\phi_c = 30^\circ$ for time $\geq 10$ sec).
Figure 26.- Concluded.
Figure 27.- Vehicle response simulations at $M_i = 4$ with $GC_m = 0.6$, $GAC_m, \delta e = 0.7$, $GAC_m, \delta BF$ and $GAC_m, \delta SB = 1.4$ without and with increased rudder augmentation ($\alpha_c = 17.6^\circ$, $\phi_c = -30^\circ$ for time <10 sec and $\phi_c = 30^\circ$ for time $\geq 10$ sec).
(a) Concluded.

Figure 27.- Continued.
(b) With increased rudder augmentation.

Figure 27.- Continued.
(b) Concluded.

Figure 27.- Concluded.
Desired response envelope

Nominal

Desired response envelope

$G_{C_m} = 0.6; \quad G_{AC_m, \delta e} = 1.8; \\
G_{AC_m, \delta_{BP}} = 1.4; \quad G_{AC_m, \delta_{SB}} = 1.4$

Desired response envelope

$G_{C_m} = 1.2; \quad G_{AC_m, \delta e} = 0.7; \\
G_{AC_m, \delta_{BP}} = 0.7; \quad G_{AC_m, \delta_{SB}} = 0.7$

Figure 28.- Pitch response as a function of stability and control effectiveness. 
$V_R = 0.61 \text{ km/sec (2000 ft/sec)}$. 

65
A six-degree-of-freedom simulation analysis was conducted to examine the effects of longitudinal static aerodynamic stability and control uncertainties on the performance of the space shuttle orbiter automatic (no manual inputs) entry guidance and control systems. To establish the acceptable boundaries, the static aerodynamic characteristics were varied either by applying a multiplier to the aerodynamic parameter or by adding an increment. With either of two previously identified control system modifications included, the acceptable longitudinal aerodynamic boundaries were determined.