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#### A STIRLING ENGINE COMPUTER MODEL FOR

# PERFORMANCE CALCULATIONS

### by Roy Tew, Kent Jefferies, and David Miao

Lewis Research Center

#### SUMMARY

To support the development of the Stirling engine as a possible alternative to the automobile spark-ignition engine, the thermodynamic characteristics of the Stirling engine were analyzed and modeled on a computer. The modeling techniques used are presented. The performance of an existing rhombic-drive Stirling engine was simulated by use of this computer program, and some typical results are presented. Engine tests are planned in order to evaluate this theoretical model.

# INTRODUCTION

The Department of Energy (DOE) has established programs whose purpose is to reduce fuel consumption and emissions of highway vehicles. The Stirling Engine Highway Vehicle Systems Program is one such program. Its purpose is to develop the Stirling engine as a possible alternative to the spark-ignition engine. It will be implemented through government participation with industry. NASA Lewis Research Center has project management responsibility for the program.

At NASA Lewis a Stirling-engine digital-computer model is being developed for predicting engine performance. This report documents the present modeling techniques and shows some preliminary predictions of one version of the model, which is configured to represent a particular single-cylinder rhombic-drive engine.

Analysis of the ideal Stirling cycle is straightforward (ref. 1), but this analysis is useful only as a reference against which to compare real cycles. Schmidt developed a somewhat more realistic analysis that considers the effect of dead volume and assumes sinusoidal piston motion (ref. 1). The basic power and efficiency (the Carnot efficiency) calculated by the Schmidt analysis can be multiplied by experience factors to estimate performance in the initial stages of engine sizing. (Ranges of experience factors are discussed in refs. 2 and 3.) Rios (ref. 4), Qvale (ref. 5), and Martini (ref. 2) have each developed models that first calculate a basic power and efficiency and then correct these basic values with separate, independent loss calculations. The most detailed performance models so far reported simulate real-time variations in gas temperatures, pressures, and flow rates at various control volumes within the working space. Some or all of the loss calculations are an integral part of the model and can thus interact with the basic thermodynamic calculations and with each other. Detailed models that have been reported in the open literature are those of Urieli (refs. 6 and 7), Finkelstein (ref. 8), and Finegold and Vanderbrug (ref. 3). A listing of Urieli's computer model is given in reference 8 and a listing of the Finegold-Vanderbrug model, in reference 3. Allan Shock of Fairchild Industries is also developing a detailed model (ref. 9). The more detailed models should be of value in studying the effects on performance of engine details not considered in the simpler models, in refining the loss calculations of the simpler models, and in investigating the significance of physical effects such as gas inertia and pressure dynamics on engine performance. However, these models appear to require too much computer time for use in a design optimization program: One run with such an optimization program might investigate hundreds of designs, or even several thousand. Since the less detailed models such as those of Qvale, Rios, and Martini require much less computer time, they would seem to be more appropriate for use in a design optimization program. Unfortunately, the models that have been published in the open literature have not been adequately validated.

N. V. Philips and its licensees have both a design-optimization program and detailed performance prediction models, which have been developed over the years with the aid of extensive test data. However, these programs and the test data are proprietary and are presently available only under license.

The model being developed by NASA Lewis differs from the Urieli and Finegold models essentially in that the Lewis model assumes that gas inertia and pressure-wave dynamics can be neglected in predicting Stirling engine performance. The Lewis model also uses an integration technique that avoids instability caused by excessive heat transfer between gas and metal when large time increments are used. Thus, the Lewis type model should be inherently more efficient in terms of computing time, than the more general Urieli and Finegold models.

The Lowis model differs from the Rios and Martini models essentially in that it more closely represents the distributed-parameter nature of the working space by dividing each heat exchanger into several control volumes and, also, by making the heat-exchanger inefficiencies an integral part of the cycle calculations. The Lewis model is thus more general in nature but less efficient in terms of computing time than the models of Rios ...d Martini.

Two versions of the computer performance model have been developed. One version is configured to model a rhombic-drive ground power unit (GPU) designed and built for the U.S. Army by General Motors. This unit was designed to produce 3 kilowatts of electric power (or about 6 kW of brake power). The other version is configured to model a free-piston engine. This document contains a description and program listing of the GPU version of the model. The GPU engine parameters are given in reference 2. The model is also briefly described in reference 2, along with some performance prediction comparisons between it and the Martini model.

The GPU-3 engine has been run through initial checkout tests at NASA Lewis; engine accessories were powered by the engine and instrumentation

was minimal (ref. 10). Testing with accessories run independently of the engine and with more instrumentation is now getting under way; these tests will provide basic engine data for evaluation and refinement of the computer model.

#### **GENERAL DESCRIPTION OF MODEL**

The GPU engine, for which this model predicts performance, is shown schematically in figure 1. There are actually <u>cight</u> separate flowpaths through each of eight regenerators and coolers with five heater tubes serving each regenerator. In the model, however, it is assumed that the same flow conditions exist in each of the eight flowpaths so that it is necessary to model only one path. The model represents the working space by a series of subdivisions called contrc' volumes; this type of model is sometimes called a nodal model.

The model calculates indicated power and efficiency for given engine speed, mean pressure, and fixed heater and cooler metal temperatures. The indicated efficiency is based on heat into the gas plus conduction losses. The model also simulates temperature, pressure, and flow variations over the cycle at various stations in the working space. The working space consists of the expansion space, the heater, the regenerator, the cooler, and the compression space.

The engine working space is represented by 13 control volumes, as shown in figure 2; the adjacent metal walls are represented by 13 corresponding control volumes. The metal temperatures, <u>except</u> for those in the regenerator, are assumed to be constant. This is a reasonable assumption for any given run since the heater and cooler metal temperatures are essentially boundary temperatures that are controlled by the combustor and the cooling water flow, respectively; these temperatures vary little over a cycle because the metal heat capacity is much greater than that of the gas.

The calculation procedure used in the model is outlined in figure 3; the equations used in the calculations are discussed in the section EQUA-TIONS AND ASSUMPTIONS USED IN DEVELOPING THE MODEL. Each set of calculations shown in figure 3 within the inner loop is made at each integration time step during each engine cycle except that it is necessary to use the pressure-drop equations only during the last cycle. Also, the conduction and shuttle heat-transfer losses are calculated just once, during the last engine cycle. (Shuttle heat transfer is heat transfer by heat ing of the displacer at the hot end of the stroke and cooling of the displacer at the cold end (ref. 2).) Between cycles, corrections to the regenerator metal temperatures are made to speed up convergence to steady operation. Typically it takes about 10 cycles with regenerator temperature correction to adjust the regenerator metal temperatures to their steady operating values. (The model predicts that these temperatures vary with an amplitude of about  $6^{\circ}$  C or less over a cycle.) In addition, a number of cycles are required for the leakage between the working and buffer spaces to adjust the mass distribution. The smaller the leakage rate, the longer the time required for the mass distribution to reach steady state. For the range of leakage rates considered thus far, it takes longer for the mass distribution to steady out than for the regenerator metal temperatures to settle out. Current procedure is to turn the metal temperature convergence scheme on at the fifth cycle and off at the 15th cycle. The model is then allowed to run for 15 to 25 more cycles to allow the mass distribution to settle out. When a sufficient number of cycles have been completed for steady-state operation to be achieved, the run is terminated.

Current computing time is about 5 minutes for 50 cycles on a UNIVAC 1100, or 0.1 minute per cycle. This is based on 1000 iterations per cycle, or a time increment of  $2\times10^{-5}$  second when the engine frequency is 50 hertz.

The computing time can be decreased by decreasing the number of iterations per cycle; the corresponding effect on predicted indicated power and efficiency is shown in figures 4 and 5 for one series of runs. These figures show that some error is in oduced by reducing from 1000 to 500 iterations per cycle and that the error becomes more significant if only 200 iterations per cycle are used.

The conjuter program is written in FORTRAN V and, in card format, is about 1300 cards long (including plotting subroutines). The program was designed to be an engineering tool for use in establishing the validity of the modeling techniques. It could be used rather easily by others but has not been designed or extensively documented for that purpose. A listing, not including the plotting subroutines, is presented in appendix E.

#### EQUATIONS AND ASSUMPTIONS USED

#### IN DEVELOPING THE MODEL

First, the basic equations and assumptions used in making the thermodynamic calculations in the working space are stated. Then a relatively complete presentation of the equations used in the model is made that corresponds very closely to the steps shown in the outline of calculation procedure (fig. 3).

# WORKING-SPACE THERMODYNAMIC CALCULATIONS

Each of the 13 gas control volumes shown in figure 2 is a special case of the generalized control volume shown in figure 6. The generalized control volume includes flow across two surfaces, heat transfer across a surface, and work interchange between the gas and a piston. Each of the three heater, five regenerator, and three cooler control volumes has flow across two surfaces and heat transfer across one surface but is of fixed volume; therefore, no work is done by the gas in these volumes. The expansionand compression-space control volumes each have flow across one surface and heat transfer across one surface and are of variable volume; therefore, the gas in these two volumes is responsible for the work output of the engine. The three basic equations used to model the thermodynamics of the gas in each control volume are conservation of energy, conservation of mass, and equation of state. These equations are used to determine the temperature and mass distributions and the pressure level within the working space at a particular time. A fourth basic equation, the momentum equation, in steady-state form, is used to calculate pressure drop across each control volume in order to evaluate its effect on indicated power and efficiency. However, this pressure-drop calculation is decoupled from the thermodynamic calculations; it has no effect on the temperature and mass distributions. This assumption simplifies the model and should be reasonable when the pressure drop is sufficiently small in relation to the pressure level.

The energy, mass, and state equations, as written for the generalized control volume shown in figure 6, are as follows, where three formulations of the equation of state are shown:

Conservation of energy (for negligible change in kinetic energy across the control volume):

$$\frac{d}{dt}(MC_vT) = hA(T_w - T) + C_p(w_iT_i - w_oT_o) - P\frac{dV}{dt}$$
(1)

Rate of changeRate ofof internal energyheat transferof control volumeacross boundsof control volumeof control vol

Rate ofRate of enthalpyheat transferflov acrossacross boundaryboundary ofof control volumecontrol volume

Rate of work done by gas in control volume

**Conservation of mass:** 

$$\frac{\mathrm{d}M}{\mathrm{d}t} = \mathbf{w}_{i} - \mathbf{w}_{0} \tag{2}$$

Equation of state:

$$PV = MRT \quad \text{for ideal gas}$$

$$PV = MR \left[ T + \left( 0, 02358 \frac{O_R}{\text{psi}} \right) P \right] \quad \text{for hydroge: - real gas}$$

$$PV = MR \left[ T + \left( 0, 01613 \frac{O_R}{\text{psi}} \right) P \right] \quad \text{for helium - real gas}$$
(8)

## where

A	heat-transfer area of control volume			
C <sub>D</sub> ,C <sub>V</sub>	heat capacities at constant pressure and volume			
h	heat-transfer coefficient			
М	mass of gas in volume			
P	pressure			
R	gas constant			
Т	bulk or average temperature of gas in volume			
т <sub>і</sub> ,т <sub>о</sub>	temperatures of gas flowing across surfaces i and o, respectively (in fig. 6)			
т <sub>w</sub>	temperature of metal wall adjacent to heat-transfer area A			
t	time			
v	volume			
w <sub>i</sub> ,w <sub>o</sub>	flow rate across surfaces i and o, respectively			
(The real	l-gas equations of state were developed from data in ref. 11.)			

Several assumptions are inherent in the use of these equations:

(1) Flow is one dimensional.

(2) Heat conduction through the gas and the regenerator matrix along the flow axis is neglected. The thermal conductivity of the regenerator matrix is assumed to be infinite in calculating the overall gas-to-matrix heat-transfer coefficient.

(3) Kinetic energy can be neglected in the energy equation.

(4) The pressure-drop calculation (based on the conservation-ofmomentum equation) can be decoupled from the other three basic equations. This implies use of a uniform pressure level throughout the working space at a given time in applying these equations.

(5) The time derivative term in the momentum equation is neglected (see appendix D).

(The last three assumptions are not made in the generalized models of Urieli (refs. 6 and 7) and Shock (ref. 9).) Thus these two models provide a means of checking the validity of these assumptions.)

In appendix A it is shown that equations (1) and (2) and the ideal-gas equation of state can be used to derive the following differential equation:

$$MC_{p} \frac{dT}{dt} = hA(T_{w} - T) + C_{p}w_{i}(T_{i} - T) - C_{p}w_{o}(T_{o} - T) + V \frac{dP}{dt}$$
(4)

The same result is obtained if either of the real-gas equations of state are used in the derivation. This equation says that the bulk or average gas temperature of a control volume is a function of the following three processes:

(1) Heat transfer across the boundary from the wall

- (2) Gas flow across the boundary
- (3) Pressure level

One approach to numerically integrating equation (4) is to solve for the temperature derivative

$$\frac{\mathrm{d}\mathbf{T}}{\mathrm{d}t} = \frac{\mathrm{h}\mathbf{A}}{\mathrm{M}\mathbf{C}_{\mathbf{p}}} \left(\mathbf{T}_{\mathbf{w}} - \mathbf{T}\right) + \frac{\mathbf{w}_{\mathbf{i}}}{\mathrm{M}} \left(\mathbf{T}_{\mathbf{i}} - \mathbf{T}\right) - \frac{\mathbf{w}_{\mathbf{0}}}{\mathrm{M}} \left(\mathbf{T}_{\mathbf{0}} = \mathbf{T}\right) + \frac{\mathrm{V}}{\mathrm{M}\mathbf{C}_{\mathbf{p}}} \frac{\mathrm{d}\mathbf{P}}{\mathrm{d}t}$$
(5)

and then set

$$\mathbf{T}^{\mathbf{t}+\Delta \mathbf{t}} = \mathbf{T}^{\mathbf{t}} \div \frac{\mathbf{d}\mathbf{T}}{\mathbf{d}\mathbf{t}} \Delta \mathbf{t}$$

where

This is a first-order numerical integration. A similar but higher order technique (Runge-Kutta fourth order, for example) could also be used on equation (5). This type of approach was not used.

The approach used (which helps to avoid numerical instability problems) was to decouple the three processes that contribute to the temperature change and solve for the temperature change due to each process separately. This second approach allows a trade-off between computing time and accuracy of solution (as indicated in figs. 4 and 5) with much less concern for numerical instabilities. The approach is suggested by representation of equation (5) in the following form:

$$\frac{dT}{dt} = \frac{dT}{dt} + \frac{d$$

where

$$\frac{dT}{dt}\Big|_{due to change} = \frac{V}{MC_p} \frac{dP}{dt}$$
(5a)  
in pressure

$$\frac{dT}{dt}\Big|_{due to} = \frac{\frac{w_i(T_i - T) - w_o(T_o - T)}{M}}{M}$$
(5b)  
mixing  
$$\frac{dT}{dt}\Big|_{due to} = \frac{hA}{MC_p} (T_w - T)$$
(5c)  
heat transfer

In appendix B it is shown that equations (5a) and (5c) can be integrated in closed form and that equation (5b) can be numerically integrated. When the results of appendix B are modified slightly to show just how they are used in the model, the resulting expressions are

$$T_{\mathbf{p}}^{t+\Delta t} = T^{t} \left(\frac{\mathbf{p}^{t+\Delta t}}{\mathbf{p}^{t}}\right)^{(\gamma-1)/\gamma}$$
(ja')

$$T_{PM}^{t+\Delta t} = \frac{M^{t}T_{P}^{t+\Delta t} + \left(w_{i}^{t+\Delta t}T_{i}^{t+\Delta t} - w_{o}^{t+\Delta t}T_{o}^{t+\Delta t}\right)\Delta t}{M^{t+\Delta t}}$$
(5b')

$$T^{t+\Delta t} = T^{t+\Delta t}_{PM} + \left(T^{t}_{W} - T^{t+\Delta t}_{PM}\right) \left(1 - e^{-(n^{t+\Delta t}A/M^{t+\Delta t}C_{p})\Delta t}\right)$$
(5c')

where the superscripts t and  $t+\Delta t$  denote values of the variables at times t and  $t + \Delta t$ . The subscript P denotes the value of the temperature after it has been updated for the effect of change in pressure. The subscript PM denotes the value of the temperature after it has been updated for the effects of change in pressure and mixing. No subscript (as on the left side of equation (5c') denotes the value of the temperature after it has been updated for all three effects - change in pressure, mixing, and heat transfer to or from the metal.

# PRESENTATION OF EQUATIONS IN ORDER

# OF CALCULATION PROCEDURE

The equations considered so far have been derived and discussed with reference to the generalized control volume of figure 6. In the computer model these equations are applied to each of the 13 control volumes shown in figure 2. Thus temperatures, masses, heat-transfer coefficients, flow rates, etc., are all subscripted with an index. The index varies from 1 to 13 for variables that are averages of the control volumes and from 1 to 13 for values at the interfaces between control volumes. The numbering procedure used for control volume and interface indexes is defined in figure 2. The equations discussed in this section include these indexes. The presentation of the equations follows the steps shown in the outline of calculation procedure in figure 3.

Pressure (step 2 in fig. 3), - The pressure P is calculated by

$$p^{t+\Delta t} = R \frac{\int_{-1}^{13} M_1^t r_1^t}{\int_{-1}^{13} V_1^t}$$
(6)

where

P pressure

R gas constant

Equation (6) is obtained by summing the ideal-gas equation

$$PV_I = M_I RT_I \qquad I = 1,13$$

over each of the 13 control volumes (remembering that pressure is assumed to be the same in all control volumes) and then solving for P. If the real-gas equation of state for hydrogen is used then and the same procedure is followed, the result is

$$P^{t+\Delta t} = R \frac{\sum_{I=1}^{13} M_{I}^{t} T_{I}^{t}}{\sum_{I=1}^{13} V_{I}^{t} - 0.02358 R \sum_{I=1}^{13} M_{I}^{t}}$$
(7)

Equations (6) and (7) are both included in the program. Also an equivalent real-gas equation for helium is included. An index in the input data specifies whether a real or ideal equation is to be used.

Update temperatures for effect of change in pressure (step 3 in fig. 3). - It was not necessary to use the subscripts P and PM of equations (5a'), (5b'), and (5c') in the computer model. Applying the three equations in sequence without the subscripts produced the same effect as if the subscripts had been used. Therefore, if the subscript P is dropped from equation (5a') and the control volume index I is introduced, the result is

$$T_{I}^{t+\Delta t} = T_{I}^{t} \left(\frac{\mathbf{p}^{t+\Delta t}}{\mathbf{p}^{t}}\right)^{(\gamma-1)/\gamma}$$
(8)

This equation is commonly used to relate temperature and pressure for an adiabatic fixed-mass process.

<u>Mass distribution (step 4 in fig. 3)</u>. - The equations for mass distribution are derived by assuming that the mass redistributes itself in accordance with the new volumes and temperatures in such a way that pressure is uniform throughout the working space. This assumption, of course, introduces inaccuracies in the solution, but the inaccuracies are relatively small because the pressure drop in Stirling engines is usually a small portion of the total pressure of the fluid. The pressure P throughout the working space is derived from the perfect-gas law as follows: The perfectgas law for the  $I^{th}$  control volume can be written

$$M_{I} = \frac{PV_{I}}{RT_{I}}$$

Summing over the 13 control volumes

$$\sum M_{I} = M_{total} = \frac{P}{R} \sum_{i=1}^{13} \frac{V_{I}}{T_{I}}$$

and solving for P/R gives

$$\frac{P}{R} = \frac{M_{total}}{\underbrace{\frac{13}{1-1}} V_{I}}$$

. .

Now substituting for P/R into the perfect-gas equation for the I<sup>th</sup> control volume gives

$$M_{I} = \frac{M_{total}}{\sum_{i=1}^{13} \frac{V_{I}}{T_{I}}} \frac{V_{I}}{T_{I}}$$

The form of this equation used in the model is

$$M_{I}^{t+\Delta t} = M_{total} \frac{\frac{V_{I}^{t}}{T_{I,P}^{t+\Delta t}}}{\left| \frac{13}{1 + \Delta t} \right|} \qquad I = 1, 13$$
(9)

(where  $T_{I,P}^{t+\Delta t}$  represents  $T_{I}$  updated for pressure but not for mixing and heat transfer).

The preceding equation calculates the new mass distribution for the case of a perfect gas. The following equation, which can be derived in the same manner, is used to approximate the real properties of hydrogen:

$$M_{I}^{t-\Delta t} = M_{total} \frac{V_{I}^{t}}{\left(T_{I,P}^{t+\Delta t} + 0.02358 \text{ p}^{t+\Delta t}\right)} \qquad I = 1,13 \quad (10)$$

$$\frac{13}{I=1} \left[ \frac{V_{I}^{t}}{\left(T_{I,P}^{t+\Delta t} + 0.02358 \text{ p}^{t+\Delta t}\right)} \right]$$

A similar equation that approximates the real properties of helium is included in the model.

Flow rates (step 5 in fig. 3). - Once the new mass distribution is known, the new flow rates are calculated from the old and new mass distributions according to

where w<sub>I</sub> is the flow rate at the I<sup>th</sup> interface between control volumes. Update temperatures in each control volume for effect of gas flow

and

between control volumes (step 6 in fig. 3). - The following equations (modifications of equation (5b') in the section WORKING-SPACE THERMO-DYNAMIC CALCULATIONS) were used to update temperature for the mixing effect following gas flow between control volumes:

$$T_{1, PM}^{t+\Delta t} = \frac{M_{1}^{t}T_{1, P}^{t+\Delta t} + \left(-w_{1}^{t+\Delta t}\theta_{1}^{t+\Delta t}\right)\Delta t}{M_{1}^{t+\Delta t}}$$

$$T_{I, PM}^{t+\Delta t} = \frac{M_{1}^{t-t+\Delta t} + \left(w_{I-1}^{t+\Delta t}\theta_{I-1}^{t+\Delta t} - w_{I}^{t+\Delta t}\theta_{I}^{t+\Delta t}\right)\Delta t}{M_{1}^{t+\Delta t}} \quad \text{for } I = 2, 12 \quad (12)$$

$$T_{13, PM}^{t+\Delta t} = \frac{M_{13}^{t}T_{13, P}^{t+\Delta t} + \left(w_{12}^{t+\Delta t}\theta_{12}^{t+\Delta t}\right)\Delta t}{M_{13}^{t+\Delta t}}$$

(where the subscript PM indicates the temperature has been updated for pressure change and mixing).

The equations for the first and thirteenth control volumes (expansion and compression spaces, respectively) are simpler in form than those for the other control volumes because there is flow across only one surface in each of these volumes. (The leakage flow between compression and buffer spaces is handled independently; it does not appear in eq. (12).) The temperature of the fluid flowing across the interface has been given a new variable name  $\theta$  to better distinguish it from the average control volume temperature T and to keep the subscripts as simple as possible. The procedure used to update the temperature  $\theta$  for each interface is now defined.

The temperature of the fluid flowing across a control volume boundary is just the bulk temperature of the control volume from which the fluid came - for flow from the expansion-space, heater, cooler, or compression-space control volumes. This is a reasonable assumption for these volumes since the actual temperature gradient across each is expected to be relatively small. In the five-control-volume regenerator, however, the temperature gradient is not small. One option would be to increase the number of control volumes in the regenerator. However, to save computing time, an alternative approach was used. It was assumed that a temperature gradient existed across each volume in the regenerator. The magnitude of the gradient was assumed to be equal to the corresponding regenerator metal gradient.

A schematic of a regenerator control volume is shown in figure 7(a). Flow across both interfaces is, for now, assumed to be in the direction shown (which is defined to be the positive flow direction). The crosshatched area represents the portion of the fluid that will flow across interface I during the time increment  $\Delta t$ . The assumed temperature profile of the control volume is characterized in figure 7(b). The vertical dashed line in figure 7(b) defines the temperature at the left boundary of the fluid that will flow across interface I during  $\Delta t$ . If  $T_I$  is defined as the average temperature of control volume I and  $\Delta T_I$  equals one-half the change in temperature across the control volume, then  $T_I - \Delta T_I$  is the temperature of the fluid at interface I and

$$T_{I} - \Delta T_{I} + \frac{W_{I} \Delta t}{M_{I}} 2 \Delta T_{I}$$

is the temperature of fluid at the vertical dashed line. (Figure 3 shows the numbering schemes used for the control volumes and the interfaces between control volumes.)

Now the temperature of the fluid that flows across an interface during  $\Delta t$  is assumed to be equal to the average temperature of that fluid before it crosses the interface. The average temperature of the fluid in the crosshatched area of figure 7(a) is then

$$\frac{1}{2}\left[\left(T_{I} - \Delta T_{I} + \frac{w_{I} \Delta t}{M_{I}} 2 \Delta T_{I}\right) + \left(T_{I} - \Delta T_{I}\right)\right] = T_{I} - \Delta T_{I} + \frac{w_{I} \Delta t}{M_{I}} \Delta T_{I}$$

Therefore, for the flow directions shown in figure 7(a), the updated temperatures of the fluid that crosses the interfaces during  $\Delta t$  are

$$\theta_{I}^{t+\Delta t} = T_{I,P}^{t+\Delta t} - \Delta T_{I} + \frac{w_{I}^{t+\Delta t} \Delta t}{M_{I}^{t}} \Delta T_{I} \qquad w_{I}^{t+\Delta t} > 0$$

$$\theta_{I-1}^{t+\Delta t} = T_{I-1,P}^{t+\Delta t} - \Delta T_{I-1} + \frac{w_{I-1}^{t+\Delta t} \Delta t}{M_{I-1}^{t}} \Delta T_{I-1} \qquad w_{I-1}^{t+\Delta t} > 0$$
(13)

If the flow direction is reversed at both interfaces, then

$$\theta_{I}^{t+\Delta t} = T_{I+1}^{t+\Delta t} + \Delta T_{I+1} + \frac{w_{I}^{t+\Delta t} \Delta t}{M_{I+1}^{t}} \Delta T_{I+1} \qquad w_{I}^{t+\Delta t} < 0$$

$$\theta_{I-1}^{t+\Delta t} = T_{I}^{t+\Delta t} + \Delta T_{I} + \frac{w_{I-1}^{t+\Delta t} \Delta t}{M_{I}^{t}} \Delta T_{I} \qquad w_{I-1}^{t+\Delta t} < 0$$

$$(14)$$

<u>Heat-transfer coefficients (step 7 in fig. 3)</u>. - The assumptions and equations used in calculating heat-transfer coefficients are discussed in appendix C. The heater and cooler equations are based on wellestablished, steady-flow correlations for tubes. The regenerator equation is based on an extrapolation of a steady-flow correlation. There is a need for additional steady-flow heat-transfer data for Stirling engine heat-exchanger components, especially regenerators. In addition, data are needed to determine how to modify steady-flow correlations for the periodic-flow conditions that exist in Stirling engines.

Update temperature in each gas control volume for effect of heat transfer between gas and metal (and determine heat transfer between gas and metal) (step 8 in fig. 3). - This temperature update is accomplished by using the following equation (a modification of eq. (5c'):

$$T_{I}^{t+\Delta t} = T_{I,PM}^{t+\Delta t} \left( T_{w,I}^{t} - T_{I,PM}^{t+\Delta t} \right) \left[ 1 - e^{\left( -h_{I}^{t+\Delta t}A_{I}/M_{I}^{t+\Delta t}C_{p} \right)\Delta t} \right] I = 1,13$$

where  $T_{w,I}$  is the wall temperature of  $I^{th}$  control volume. Note that, no matter how large the heat-transfer coefficient, the gas temperature cannot change more than the  $\Delta T$  between the wall and the gas. Thus this calculation cannot cause the solution to become unstable, but it can lead to significant inaccuracies if the time increment  $\Delta t$  is made too large.

The heat transferred between gas and metal is then calculated from

$$Q_{I}^{t+\Delta t} = -\left(T_{I}^{t+\Delta t} - T_{I,PM}^{t+\Delta t}\right) M_{I}^{t+\Delta t} C_{p} \qquad I = 1,13$$
(15)

so that heat transfer from gas to metal is defined to be positive.

Regenerator metal temperature (step 9 in fig. 3). - The equation used to update the metal temperatures in the five regenerator control volumes is

$$M_{IC} \frac{dT_{W,I}}{dt} = Q_{I} \qquad I = 5,9 \qquad (16)$$

where  $Q_{I}$  is the rate of heat transfer between gas and metal. This is integrated numerically by setting

$$\mathbf{T}_{\mathbf{w},\mathbf{I}}^{\mathbf{t}+\Delta\mathbf{t}} = \mathbf{T}_{\mathbf{w},\mathbf{I}}^{\mathbf{t}} + \frac{\mathbf{Q}_{\mathbf{I}}^{\mathbf{t}+\Delta\mathbf{t}}}{\mathbf{M}_{\mathbf{I}}\mathbf{C}} \Delta \mathbf{t}$$
(17)

where

 $M_T$  mass of metal in  $I^{th}$  volume

C thermal capacitance of metal

**Δt** time increment

For most regenerators the thermal capacitance of the metal is so much larger than the thermal capacitance of the adjacent gas volume that an excessive number of engines cycles (from the point of view of computing time) are required for the metal temperatures to reach steady state. Therefore, it is necessary to apply a correction to the metal temperatures after each cycle to speed up convergence. The method used is discussed in the section <u>Convergence scheme for regenerator metal temperatures (step 19 in</u> fig. 3). <u>Pressure-drop calculations (step 10 in fig. 3)</u>. - Since the pressuredrop calculations have been decoupled from the heat- and mass-transfer calculations, pressure drop needs to be calculated only over the last cycle. The indicated work calculation can then be corrected for pressure-drop loss.

A general form of the conservation of momentum equation for onedimensional flow is

<del>2</del> (pv)	$= -\frac{\partial}{\partial \mathbf{x}} (\rho \mathbf{v}^2)$	$- \frac{f}{D_h} \frac{1}{2} \rho v^2$	- <u>8</u> - <u>8</u>	(18)
Rate of accumulation of momentum per unit volume	Rate of momentum gain by convection per unit volume	Rate of momentum gain by viscous transport (fric- tional forces) per unit volume	Rate of momentum gain due to pressure force per unit volume	

# where

ρ density

v velocity of flow

f friction factor

D<sub>h</sub> hydraulic diameter

P pressure

t time

x distance

In appendix D it is shown that by combining the continuity and momentum equations and then neglecting the time derivative term in the resulting equation, the following equation results:

$$\mathbf{v} \, \mathrm{d}\mathbf{v} + \frac{\hbar v^2}{2D_h} \, \mathrm{d}\mathbf{x} + \frac{\mathrm{d}P}{\rho} = 0 \tag{19}$$

This equation can be integrated over a length L for the special cases of adiabatic or isothermal flow processes (the two extremes). When the resulting adiabatic and isothermal expressions are applied to the GPU regenerator, the contribution of the v dv term is negligible for the two extremes. Since the effect of the term is more significant in the regenerator than in the heater and cooler, the expression for pressure drop can be reduced to

$$\frac{f}{2}\frac{v^2}{D_h}dx + \frac{dP}{\rho} = 0$$
(20)

or applying the differential equation (20) over a finite length L

$$\Delta P = \frac{f}{D_h} \frac{1}{2} \rho v^2 L \qquad (21)$$

where  $\Delta P$  is the pressure drop over length L.

A modification of this equation can also be used to ccount for the effect of expansions and contractions in flow area. The form of the modified equation is

$$\Delta \mathbf{P} = \mathbf{K} \frac{1}{2} \rho \mathbf{v}^2 \tag{22}$$

It is applied at each area change in the flowpath between the expansion and compression spaces. At a particular point where an area change occurs, K is a function of the two areas and the direction of flow (since an expansion for one flow direction is a contraction when the flow reverses). The term K is calculated in accordance with the procedure given in references 12 and 13.

For the heater and cooler control volumes the friction factor f is determired from

$$\begin{cases} \mathbf{f}_{I} = \frac{16}{N_{Re_{I}}} & N_{Re_{I}} < 1500 \\ \\ \mathbf{f}_{I} = \frac{0.046}{N_{Re_{I}}^{0.2}} & N_{Re_{I}} \ge 1500 \\ \end{cases}$$
(23)

where  $N_{Re_{I}}$  is the Reynolds number (based on plots of smooth-tube friction factors in ref. 14).

For the regenerator control volumes

$$-0.0190N_{Re_{I}} + 0.54 \qquad I = 5,9 \qquad (24)$$

which is a fit of the curve shown in figure 8. This curve was derived from the experimental steady-flow air data taken on the regenerator cooler unit of the GPU-3 engine and was extrapolated to the low Reynolds number range (below 50). Since the sample runs for this report were made, this curve has been compared with other wire-screen data from Kays and London (ref. 13). This comparison suggests that the curve should be somewhat higher in the below-50 Reynolds number range. (This range is important in the regenerator.)

There is a need for additional pressure drop data for Stirling engine heat-exchanger components, especially for regenerators. Also additional data are needed to determine how to modify the steady-flow pressure drop correlations for periodic-flow conditions. With the pressure level P known (which is now assumed to be the pressure at the center of the regenerator) and the  $\Delta P$ 's across each of the control volumes in the heater, regenerator, and cooler known, the pressures needed in the work calculations,  $P_{e}$  and  $P_{c}$ , can be calculated as follows:



<u>Heat conduction from hot end to cold end of engine and shuttle loss</u> (step 11 in fig. 3). - Three separate paths were considered in the calculation of heat-conduction losses from the hot end to the cold end of the engine:

- (1) Through each of the eight regenerators
- (2) Through the cylinder walls
- (3) Through the walls of the displacer from the hot space to the cold space

The effect of temperature on conductivity was considered. A calculation of the conduction loss through the gas inside the displace suggested that the loss along this path was small enough to be neglected. The dimensions used in calculating these conduction losses and the locations where the temperature measurements will be made are shown in figure 9.

The displacer picks up heat from the cylinder at the hot end of its stroke and loses heat to the cylinder at the cold end of its stroke. This shuttle loss is calculated  $L_{\downarrow}$  using the following equation from reference 2:

$$Q_{\text{shuttle}} = \frac{K_{\pi} DS^2 \Delta T}{8CL}$$
(26)

#### where

- K thermal conductivity of gas
- D displacer diameter
- S stroke
- $\Delta T$  temperature difference across displacer length
- C clearance between displacer and cylinder
- L displacer length

Conduction ar shuttle calculations are made just once after steady operation has been achieved.

Sum up heat transfers between gas and metal for each component (step 12 in fig. 3). - The basic heat into the working space per cycle is the sum of the net heat transfer from metal to gas in the heater and expansion-space control volumes over the cycle. The basic heat out of the working space per cycle is the sum of the net heat transfer from the gas to the metal in cooler and compression-space control volumes per cycle. Since it is assumed that there are no losses from the regenerator matrix, the net heat transferred between gas and metal in the regenerator over ... cycle should be zero. This net heat transfer in the regenerator over the cycle appears to be the most convenient single criterion for judging when convergence of regenerator metal temperatures has been achieved. However, for small leakage rates, using this criterion to judge convergence to steady operation can lead to significant errors. That is, even though the regenerator metal temperatures have converged so that the net heat transfer in the regenerator per cycle is small, small changes in the mass distribution between working and buffer spaces from one cycle to the next can cause a significant change in performance over many cycles.

Leakage flow between working and buffer spaces (step 13 in fig. 3). -A leakage flow between working and buffer spaces can be calculated according to

$$\mathbf{w} = \mathbf{C} \sqrt{\left| \mathbf{P}_{\mathbf{c}} - \mathbf{P}_{\text{buff}} \right|} \tag{27}$$

where

C constant (0.0001 was assumed for sample run)

P<sub>c</sub>, P<sub>buff</sub> compression - and buffer -space pressures

where flow is from compression space to buffer space if  $P_c > P_{buff}$ , and the reverse if  $P_{buff} > P_c$ . This equation was used to investigate the sensitivity of performance to leakage. This procedure for calculating loss due to leakage will have to be updated when more information about leakage flow becomes available. Relatively small leakage flows will increase the number of cycles required for the mass distribution between the working and buffer spaces to reach steady operating values.

<u>Compression-, expansion-, and buffer-space volumes (step 14 in fig. 3).</u> - The crankshaft angle is defined in the schematic shown in figure 10. Compression-, expansion-, and buffer-space volumes are calculated from the crankshaft angle by the following set of equations (as derived from fig. 10):

$$L_{y} = \sqrt{L^{2} - (e - r \cos x)^{2}} \equiv \text{Projection of rod length } L \text{ on vertical axis.}$$

$$Y_{1} = r \sin x + L_{y} \equiv \text{Position of displacer yoke}$$

$$Y_{2} = r \sin x - L_{y} \equiv \text{Position of power-piston yoke}$$

$$Y_{1, \min} = \sqrt{(L - r)^{2} - e^{2}}$$

$$L_{y, \max} = \sqrt{L^{2} - (e - r)^{2}}$$

$$V_{e} = A_{d}(Y_{1} - Y_{1, \min}) + V_{e, \text{clearance}} \equiv \text{Expansion-space volume}$$

$$V_{e} = 2(A_{d} - A_{rod})(L_{y, \max} - L_{y}) + V_{c, \text{clearance}} \equiv \text{Compression-space volume}$$

$$V_{buff} = A_{pr}(-Y_{2} - Y_{1, \min}) + V_{buff, \text{clearance}} \equiv \text{Buffer-space volume}$$
(28)

where

e eccentricity

r crank radius

x crank angle

A<sub>d</sub> displacer cross-sectional area

A<sub>pr</sub> piston cross-sectional area minus piston rod cross-sectional area

A<sub>rod</sub> displacer rod cross-sectional area

and  $V_e$  and  $V_c$  are the two volumes needed to calculate the indicated power.

Work, power, and efficiency calculations (step 16 in fig. 3). - The indicated work is calculated according to

$$W = \oint P(dV_e + dV_c)$$
 (29)

over all but the last cycle. Since heat-exchanger ineffectivenesses, dead volumes, and leakage from working space to buffer space are all an integral part of the calculations, the work calculated in equation (29) includes the effect of these losses. Over the last cycle, after steady operation has been achieved, pressure-drop losses are calculated. To include this loss, till indicated work calculation was revised to

$$W = \oint \left[ P_e \, dV_e + P_c \, dV_c \right] \tag{30}$$

The indicated power is just the indicated work per cycle times the engine frequency.

The conduction and shuttle transfer losses are calculated only once after steady operation has been achieved. These losses increase the heat input and heat output by the same amount. Since it is assumed that they do not interact with the working space, they affect the efficiency but not the power calculations.

The net heat into the engine per cycle is defined to be the basic heat input (from step 12) plus conduction and shuttle losses minus one-half the total windage (pressure drop) loss. (It would probably be more accurate to use the heater windage loss plus one-half the regenerator windage loss for windage credit in calculating the net heat input (as in ref. 2). However, if the regenerator loss is considerably larger than the heater and cooler losses, it is a reasonable assumption to use one-half the total loss for windage credit.)

Indicated efficiency is defined to be the indicated work per cycle divided by the net heat into the engine per cycle (as defined in the previous paragraph).

<u>Convergence scheme for regenerator metal temperatures (step 19</u> <u>in fig. 3).</u> - The scheme used to correct regenerator metal temperatures between cycles was arrived at through trial and error. The correction is made as follows:

$$\Delta T_{I} = \frac{\frac{Time=N}{Time=0} \Delta t}{\frac{Time=0}{Time=N} \frac{(T_{w,I} - T_{I}) \left[1 - e^{\left(-h_{I}A_{I}/M_{I}C_{p}\right)\Delta t}\right] M_{I}}{\prod_{Time=0}{Time=0} \left[1 - e^{\left(-h_{I}A_{I}/M_{I}C_{p}\right)\Delta t}\right] M_{I}} \qquad I = 5,9 \quad (31)$$

where

N number of iterations per cycle

 $\Delta T_{I}$  weighted average change in gas temperature over cycle for  $I^{th}$  regenerator control volume

T<sub>I</sub> I<sup>th</sup> average gas temperature

Tw.I Ith wall temperature

Then let

$$\Delta T_{I} = \Delta T_{I, \text{old}} \times F_{1} + \Delta T_{I} \times F_{2} \qquad I = 5,9 \qquad (3.),$$

where  $F_1 = 0.4$  and  $F_2 = 10.0$  are the factors that seem to work best. The final step in the correction is

$$T_{w,5,new} = T_{w,5,old} - \left(\frac{5 \Delta T_5 + 4 \Delta T_6 + 3 \Delta T_7 + 2 \Delta T_8 + \Delta T_9}{3}\right)$$

$$T_{w,6,new} = T_{w,6,old} - \left(\frac{4 \Delta T_5 + 8 \Delta T_6 - 6 \Delta T_7 + 4 \Delta T_8 + 2 \Delta T_9}{3}\right)$$

$$T_{w,7,new} = T_{w,7,old} - \left(\frac{\Delta T_5 + 2 \Delta T_6 + 3 \Delta T_7 + 2 \Delta T_8 + \Delta T_9}{1}\right)$$

$$T_{w,8,new} = T_{w,8,old} - \left(\frac{2 \Delta T_5 + 4 \Delta T_6 + 6 \Delta T_7 + 8 \Delta T_8 + 4 \Delta T_9}{3}\right)$$

$$T_{w,9,new} = T_{w,9,old} - \left(\frac{\Delta T_5 + 2 \Delta T_6 + 3 \Delta T_7 + 4 \Delta T_8 + 5 \Delta T_9}{3}\right)$$
(33)

In an attempt to improve upon the rate of convergence, the scheme used by Urieli (ref. 7) was tried. This is a correction of the form

$$\mathbf{T}_{\mathbf{w},\mathbf{I},\mathbf{new}} = \mathbf{T}_{\mathbf{w},\mathbf{I},\mathbf{old}} = \mathbf{F}_{\mathbf{I}} \times \mathbf{Q}_{\mathbf{I}} \qquad \mathbf{I} = 5,9 \qquad (34)$$

where  $Q_{I}$  is the net heat transferred from the  $I^{th}$  metal node to the  $I^{th}$  gas node over the previous cycle. An attempt was made, by trial and error, to pick the optimum combination of factors  $F_{I}$  (I = 5,9) to speed

up convergence. This procedure worked in the Lewis model but not as well as the previously described approach.

#### **RESULTS GENERATED WITH MODEL**

Some sample performance predictions and plots of engine variables over a cycle are shown for the GPU simulation run characterized in table I. The assumed metal boundary temperatures are shown in figure 11. Performance predictions for this run are shown in table II.

The ratio of "dead volume" to the change in total working-space volume over the cycle is a very important factor in Stirling engine performance. Dead volume is the volume of the heat-exchanger components plus clearances in the expansion and compression spaces. It decreases the ratio of maximum to minimum pressure that can be achieved over the cycle. Better definitions of GPU engine dead volume by refined calculations and gas displacement measurements, since these sample runs were made, indicate a larger dead volume than used in the model for the sample runs. Using the larger dead volume would result in lower predicted power than shown here.

Expansion - and compression - space volumes are shown in figure 12 as a function of time. Zero time corresponds to minimum compression space volume. The cycle is complete at 0.02 second. One and one-half cycles are shown on this and the following plots. These volumes, together with the plot of total volume in figure 13, are keys to the behavior of the engine variables shown in later figures.

Expansion - and compression - space pressures are plotted in figure 14. These plots correlate closely with the plot of total volume in figure 13: Minimum pressure corresponds closely to maximum total volume. The pressure drop between expansion and compression spaces is a small percentage of the pressure level (<3 percent).

A plot of this pressure drop as a function of time in figure 15 shows that the maximum positive  $\Delta P$  (where  $\Delta P = P_{\rho} - P_{c}$ ) occurs a little before 0.008 second. The corresponding flow rates into and out of the heat exchangers are shown in figures 16 to 18. (Additional flow rates calculated at the control-volume interfaces within the heat exchangers are not shown here). The maximum positive flow rates just before 0.008 second correspond to the region of the volume plots in figure 12, where the compressionspace volume is increasing at its maximum rate and the expansion-space volume is decreasing at its maximum rate (to give the maximum rate of volume displacement from the hot to the cold space). Similarly, the maximum negative flow rates and pressure drop occur just before 0.016 second, where the maximum rate of volume displacement from the cold to the hot space occurs. Pressure drop is greater for positive than for negative flow primarily because of the lower average pressures and, therefore, higher velocities when flow is from the hot toward the cold space. Pressure is lower because positive flow occurs when working-space volume is at and near its maximum.

The differences in inlet and outlet flows for each of the heat-exchanger components divide each cycle into two regions - a region where net mass is removed from the component, and a region where net mass is stored in the component. These regions are labeled in the plots of flow rates for the heater in figure 16. Similar flow-rate plots for the regenerator and cooler are shown in figures 17 and 18.

Pressure-volume diagrams for the expansion and compression spaces are shown in figures 19 and 20. Since the expansion-space work is positive and the compression-space work is negative, the net indicated work per cycle is the difference of the areas within these two diagrams (219 joules (162 ft-lbf) in this case). The area within the pressure-volume diagram of figure 21 represents net indicated work uncorrected for pressure-drop loss (231 joules, or 170 ft-lbf).

Expansion- and compression-space temperatures are shown in figures 22 and 23. The temperature variations correlate well with the pressure variations of figure 14. In both the expansion and compression spaces the temperature variations are about 23 percent of the peak temperature in the space. Plots of indicated power and efficiency are shown in figures 24 and 25 as a function of engine speed for three average working-space pressures. Other run conditions are as specified in table I, except that for the runs at the two lower pressure levels the cooler temperature was 5.6 K ( $10^{\circ}$  R) lower than specified in table I.

A number of runs were made to compare predicted performance for hydrogen and helium. Indicated power for both fluids is shown as a function of frequency in figure 26. The power was larger for hydrogen except for frequencies below about 17 hertz. (For a series of runs made with no leakage, power was greater for hydrogen for all frequencies above 5 Hz.)

Indicated efficiency for both fluids is shown as a function of frequency in figure 27. The efficiency for hydrogen was greater than that for helium above about 13.5 herts, at which point the curves cross over. (For the series of runs made with no leakage, there was no crossover; however, the curves did get closer together as the frequency was decreased to 5 herts. At 5 herts, the efficiencies were 35.7 percent for hydrogen and 34.8 percent for helium.)

The data from figures 26 and 27 are replotted in figure 28 in a form used by several other authors. The hydrogen and helium curves cross over so that below about 12 hertz the model predicts higher efficiencies for helium than for hydrogen at a given pressure level. When the runs were repeated with no leakage calculation, the curves did not cross over but became quite close at 5 hertz, the lowest frequency considered. Similar curves predicted by Urieli's model indicated a crossover of the helium and hydrogen curves in the 30-to 40-hertz range (ref. 7) for no leakage and a significantly different engine. In the same reference, Urieli also shows curves for a Philips engine (a heat-pipe-operated swashplate type) which indicate that, in an efficiency-versus-power plot, the helium and hydrogen curves would cross over in the 40- to 45-hertz range. (It is not known whether or not the Philips' curves include the effect of a leakage calculation). In figure 28, in the low-frequency range, the efficiency drops off rapidly due to the increasing significance of static conduction and shuttle heat-transfer losses as the power level drops.

# CONCLUDING REMARKS

As shown above, the Stirling engine performance model discussed herein tracks engine cyclical performance. Testing of the ground-powerunit engine now under way at NASA Lewis will provide the basic engine performance data necessary for a quantitative evaluation of the modeling process for mechanically linked engines. The data resulting from these tests and comparisons of the model predictions with the data are subjects for future reports.

There is little information in the literature applicable to the periodicflow processes occurring in Stirling engines. An expanded base on both periodic-flow and steady-flow heat-transfer and pressure-drop data for Stirling engine heat-exchanger components is needed to improve the level of confidence in predicting engine heat-transfer and pressure-drop characteristics.

It is expected that better definition of the actual engine dead volumes, modifications to the presently incorporated heat-transfer and pressuredrop correlations, and, perhaps, tightening of some of the simplifying assumptions may be required before the model predicts real-engine performance with a high degree of quantitative accuracy. However, the model's qualitative ability to predict variations in the state of the working gas over a cycle and to predict performance trends has already been useful in helping to understand operation of the engine, to plan the experimental program, and to study sensitivity to various engine and workinggas parameters.


# APPENDIX A

# DERIVATION OF GAS TEMPERATURE DIFFERENTIAL EQUATION

The basic gas-volume equations are used in the derivation. For convenience they are listed again here:

$$\frac{d}{dt} (MC_vT) = hA(T_w - T) + C_p(w_iT_i - w_oT_o) - P\frac{dV}{dt}$$
(1)

$$\frac{\mathrm{d}\mathbf{M}}{\mathrm{d}\mathbf{t}} = \mathbf{w}_{\mathbf{i}} - \mathbf{w}_{\mathbf{o}} \tag{2}$$

$$PV = MRT$$
(3)

Expanding the first term of equation (1) gives

$$MC_{v} \frac{dT}{dt} + C_{v}T \frac{dM}{dt} = hA(T_{w} - T) + C_{p}(w_{i}T_{i} - w_{o}T_{o}) - P \frac{dV}{dt}$$
(A1)

Differentiating equation (3) gives

$$MR \frac{dT}{dt} + RT \frac{dM}{dt} = P \frac{dV}{dt} + V \frac{dP}{dt}$$
(A2)

Letting  $R = C_p - C_v$  in the first and second terms of equation (A2) and solving for

$$C_v T \frac{dM}{dt}$$

yields

$$C_{v}T \frac{dM}{dt} = M(C_{p} - C_{v}) \frac{dT}{dt} + C_{p}T \frac{dM}{dt} - P \frac{dV}{dt} - V \frac{dP}{dt}$$
(A3)

.

Substituting the right side of equation (A3) for the second term of equation (A1) yields

$$\mathbf{M} \bigvee_{\mathbf{t}} \frac{d\mathbf{T}}{d\mathbf{t}} + \mathbf{M} (\mathbf{C}_{\mathbf{p}} - \bigvee_{\mathbf{t}}) \frac{d\mathbf{T}}{d\mathbf{t}} + \mathbf{C}_{\mathbf{p}} \underbrace{\mathbf{T}}_{\mathbf{t}} \frac{d\mathbf{M}}{d\mathbf{t}} - \mathbf{P} \frac{\mathbf{W}}{\mathbf{t}} - \mathbf{V} \frac{d\mathbf{P}}{d\mathbf{t}}$$
$$= \mathbf{h} \mathbf{A} (\mathbf{T}_{\mathbf{W}} - \mathbf{T}) + \mathbf{C}_{\mathbf{p}} (\mathbf{w}_{\mathbf{i}} \mathbf{T}_{\mathbf{i}} - \mathbf{w}_{\mathbf{0}} \mathbf{T}_{\mathbf{0}}) - \mathbf{P} \frac{\mathbf{W}}{\mathbf{t}}$$

or

$$MC_{p}\frac{dT}{dt} + C_{p}T\frac{dM}{dt} - V\frac{dP}{dt} = hA(T_{w} - T) + C_{p}(w_{i}T_{i} - w_{o}T_{o})$$
(A4)

Using equation (2) to substitute for dM/dt in equation (A4) gives

$$MC_{p} \frac{dT}{dt} = hA(T_{w} - T) + C_{p}(w_{i}T_{i} - w_{o}T_{o}) - C_{p}T(w_{i} - w_{o}) + V \frac{dP}{dt}$$

 $\mathbf{or}$ 

$$MC_{p} \frac{dT}{dt} = hA(T_{w} - T) + C_{p}w_{i}(T_{i} - T) - C_{p}w_{o}(T_{o} - T) + V \frac{dP}{dt}$$
(4)

which is the equation used in the model to solve for gas temperature.

# APPENDIX B

# INTEGRATION OF DECOUPLED TEMPERATURE EQUATIONS

The equation

$$\frac{dT}{dt} |_{due to} = \frac{V}{MC_p} \frac{dP}{dt}$$
(5a)  
change in  
pressure

can be integrated in closed form by solving the equation of state for V/M and substituting in equation (5a).

$$PV = MRT \rightarrow \frac{V}{M} = \frac{RT}{P}$$

Substituting

$$\frac{dT}{dt} = \frac{RT}{PC_p} \frac{dP}{dt}$$

$$\frac{dT}{T} = \frac{R}{C_p} \frac{dP}{P} = \frac{C_p - C_v}{C_p} \frac{dP}{P} = \frac{\gamma - 1}{\gamma} \frac{dP}{P}$$

$$\therefore \ln T \bigg|_{t}^{t+\Delta t} = \frac{\gamma - 1}{\gamma} \ln P \bigg|_{t}^{t+\Delta t}$$

$$\frac{T^{t+\lambda t}}{T^t} = \left(\frac{p^{t+\Delta t}}{p^t}\right)^{(\gamma-1)/\gamma}$$

$$\frac{dT}{dt} \Big|_{\substack{t=\frac{w_i(T_i - T) - w_o(T_o - T)}{M}}} = \frac{\frac{w_i(T_i - T) - w_o(T_o - T)}{M}}{M}$$
(5b)

By using numerical integration let

$$\mathbf{T}^{t+\Delta t} = \mathbf{T}^{t} + \frac{\mathbf{d}\mathbf{T}}{\mathbf{d}t} \Delta t$$

$$= \mathbf{T}^{t} + \frac{\mathbf{w}_{i}^{t+\Delta t} \left(\mathbf{T}_{i}^{t+\Delta t} - \mathbf{T}^{t}\right) - \mathbf{w}_{o}^{t+\Delta t} \left(\mathbf{T}_{o}^{t+\Delta t} - \mathbf{T}^{t}\right)}{\mathbf{M}^{t+\Delta t}} \Delta t$$

$$= \mathbf{T}^{t} + \frac{\left(\mathbf{w}_{o}^{t+\Delta t} - \mathbf{w}_{i}^{t+\Delta t}\right)\mathbf{T}^{t}}{\mathbf{M}^{t+\Delta t}} \Delta t + \frac{\mathbf{w}_{i}^{t+\Delta t}\mathbf{T}_{i}^{t+\Delta t} - \mathbf{w}_{o}^{t+\Delta t}\mathbf{T}_{o}^{t+\Delta t}}{\mathbf{M}^{t+\Delta t}} \Delta t$$

Since

$$\mathbf{w}_{i} = \frac{\mathbf{M}^{t+\Delta t} - \mathbf{M}^{t}}{\Delta t} + \mathbf{w}_{o}^{t+\Delta t} \rightarrow \left(\mathbf{w}_{i}^{t+\Delta t} - \mathbf{w}_{o}^{t+\Delta t}\right) \Delta t = \mathbf{M}^{t+\Delta t} - \mathbf{M}^{t}$$

have

$$\mathbf{T}^{t+\Delta t} = \mathbf{X} + \frac{(\mathbf{M}^{t} - \mathbf{M}^{t+\Delta t})}{\mathbf{M}^{t+\Delta t}} \mathbf{T}^{t} + \frac{\left(\mathbf{w}_{i}^{t+\Delta t}\mathbf{T}_{i}^{t+\Delta t} - \mathbf{w}_{o}^{t+\Delta t}\mathbf{T}_{o}^{t+\Delta t}\right)}{\mathbf{M}^{t+\Delta t}} \Delta t$$

$$T^{t+\Delta t} = \frac{M^{t}T^{t}}{M^{t+\Delta t}} + \frac{\left(w_{1}^{t+\Delta t}T_{1}^{t+\Delta t} - w_{0}^{t+\Delta t}T_{0}^{t+\Delta t}\right)\Delta t}{M^{t+\Delta t}}$$

$$\frac{dT}{dt}\Big|_{due to} = \frac{hA}{MC_{p}}(T_{w} - T) - \frac{dT}{T_{w} - T} = \frac{hA}{MC_{p}}dt \qquad (5c)$$
heat transfer

Assume  $T_w$  is constant over the time increment for the purpose of integrating the left side with respect to time. This is a reasonable assumption since  $T_w$  changes much more slowly than T due to the relatively large heat capacity of the metal. It was a so assumed that h and M were constant over the time increment to allow integration of the right side of the equation.

$$(T_{\mathbf{w}} - T)_{t}^{it + \Delta t} = \frac{hA}{MC_{p}} t_{t}^{it + \Delta t}$$

$$\ln \frac{(T_{\mathbf{w}} - T)^{t + \Delta t}}{(T_{\mathbf{w}} - T)^{t}} = -\frac{hA}{MC_{p}} \Delta t$$

$$(T_{\mathbf{w}} - T)^{t} = (T_{\mathbf{w}} - T)^{t} e^{-(hA - MC_{p})\Delta t}$$

$$(T_{\mathbf{w}} - T)^{t + \Delta t} = (T_{\mathbf{w}} - T)^{t} e^{-(hA - MC_{p})\Delta t}$$

or

$$\mathbf{T}^{t+\Delta t} = \mathbf{T}^{t} + (\mathbf{T}_{\mathbf{w}} - \mathbf{T}^{t}) \begin{pmatrix} -(hA/MC_{p})\Delta t \\ 1 - e \end{pmatrix}$$

This equation says that, as the time increment is made larger, the gas temperature approaches the wall temperature asymptotically. Thus using large time increments cannot cause instabilities because of excessiv change in gas temperature.

# APPENDIX C

# HEAT-TRANSFER-COEFFICIENT EQUATIONS

# HEATER AND COOLER

The heat-transfer equation used in the heater and cooler is

.

$$\mathbf{h}_{\mathbf{I}} = \frac{\mathbf{k}_{\mathbf{I}}}{\mathbf{D}_{\mathbf{I}}} \left( 0.\ 001871 \ \frac{\mathbf{D}_{\mathbf{I}} \overline{\mathbf{w}}_{\mathbf{I}}}{\mu_{\mathbf{I}} \mathbf{A}_{\mathbf{CS},\mathbf{I}}} + 15 \right)$$
(C1)

which was derived by linearizing

$$\frac{hD}{k} = 0.023 \left(\frac{Dw}{\mu A_{cs}}\right)^{0.8} \times \left(\frac{C_p \mu}{k}\right)^{0.4}$$
Nusselt Reynolds Prandtl
number number number

where

- h heat-transfer coefficient
- D hydraulic diameter
- k thermal conductivity
- w flow rate

u viscosity

A<sub>cs</sub> cross-sectional flow area

This equation is reportedly valid (ref. 14) for turbulent flow of gases when  $0.7 < Prandtl number < 120, 10\,000 < Reynolds number <math>\lesssim 120\,000$ , and  $\Delta T$  is moderate. The Prandtl number was essentially constant over the temperature range of interest at 0.68 to 0.69. With the assumption that

$$\left(\frac{C_{p}\mu}{k}\right)^{0.4} = (0.688)^{0.4} = 0.861$$

equation (C2) reduces to

$$\frac{hD}{k} = 0.0198 \left(\frac{Dw}{\mu A_{cs}}\right)^{0.8}$$
(C3)

Heater and cooler Reynolds numbers were calculated in the model range from 0 to 25 000 but are mostly above 10 000. When equation (C3) was linearized, the result was

$$\frac{hD}{k} = 2.001871 \left( \frac{Dw}{\mu A_{cs}} \right) + 15$$
 (C4)

which is equivalent to equation (C1). Plots of equations (C3) to (C4) are compared in figure 29.

### REGENERATOR

In reference 15, heat-transfer data for a  $79 \times 79$ -wire/cm (200  $\times$  200-wire/in, ), 0.051-cm- (0.002-in, -) diameter wire screen are given. The data were extrapolated to 400 layers with the result shown as a solid curve in figure 12.

A linear approximation to this curve

$$\frac{hD}{k} = 0.06071 \left( \frac{Dw}{\mu A_{cs}} \right) + 3.7$$
 (C5)

is also shown in figure 30. This equation was used to calculate heattransfer coefficients in the regenerator.

### EXPANSION SPACE

This analysis assumes perfect insulation between the combustion gas and the expansion-space wall. Heat transfer between metal and gas is a combination of radiation and convection. For radiation

$$\frac{\mathbf{Q}}{\mathbf{A}} = \sigma \mathbf{F} \left( \mathbf{T}_{\mathbf{W}}^{\mathbf{4}} - \mathbf{T}^{\mathbf{4}} \right)$$

and

$$h_{rad} = \frac{Q}{A}$$
  
 $T_w - T$ 

where

 $\sigma$  Boltzmann constant

F emissivity times view factor

Tw wall temperature

T gas temperature

- Q rate of heat flow
- A heat-transfer area

h<sub>rad</sub> radiation heat-transfer coefficient

The overall F is assumed to be 0.7.

The convection heat-transfer coefficient is

$$h_{conv} = 0.023 (Re)^{0.8} (Pr)^{0.4} \frac{k}{D_h}$$
 Re > 10 000 (C7a)

(C6)

$$h_{conv} = 0.023 (Re)^{0.8} (Pr)^{0.4} \frac{k}{D_h} \left[ 1 + \left( \frac{D_h}{L} \right)^{0.07} \right] = 2100 < Re \le 10\ 000$$

43

where L is the maximum distance from the cylinder head to the displacer, and

$$h_{conv} = 1.86 (Graetz number)^{0.333} \frac{k}{D_h}$$
 Graetz number > 10; Re  $\leq 2100$  (C7b)

or

 $h_{conv} = 5.0 \text{ Btu/hr-ft}^2 \cdot R$  Graetz number  $\leq 10$ ; Re  $\leq 2100$  (C7c)

where Graetz number =  $\text{Re} \times \text{Pr} \times D_h/L$ . The value in equation (C7c) is an assumed cutoff point (close to the natural convection coefficient). For the combined heat-transfer coefficient the values obtained from equations (C6) and (C7) are added.

The volume of the insulated part of the heater tubes adjacent to the expansion space is lumped with the expansion space. (It is treated as an expansion-space clearance volume.) However, the heat-transfer rates between the insulated tubes and the gas are calculated separately before they are combined with the rate for the expansion space. The same equations, (C6) and (C7), are used, but in this case the convection strongly dominates the combined value.

#### COMPRESSION SPACE

Since the radiation effect is small in the compression space, only convection heat transfer is considered. Equation (C7) is used for the calculation. It is assumed that the wall temperature is known. Without detailed analysis or test data to identify this wall temperature, it seems reasonable to assume that it is about equal to the average compressionspace gas temperature over the cycle. The net result is that very little heat transfer takes place in the compression space and the compressionspace process is essentially adiabatic.

# APPENDIX D

# MOMENTUM EQUATION

A general form of the conservation-of-momentum equation for onedimensional flow is

$$\frac{\partial}{\partial t} (\rho v) + \frac{\partial}{\partial x} (\rho v^2) + \frac{f}{2D_h} \rho v^2 + \frac{\partial P}{\partial x} = 0 \quad (D1)$$
Rate of Rate of Rate of Rate of accumulation momentum momentum momentum of momentum gain by gain by gain by gain by per unit volume convection viscous pressure force per unit transport per unit volume volume volume

Expanding the first and second terms of equation (D1) yields

$$\rho \frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \frac{\partial \rho}{\partial t} + \mathbf{v} \frac{\partial (\rho \mathbf{v})}{\partial \mathbf{x}} + \rho \mathbf{v} \frac{\partial \mathbf{v}}{\partial \mathbf{x}} + \frac{\mathbf{f}}{2\mathbf{D}_{\mathbf{h}}} \rho \mathbf{v}^2 + \frac{\partial \mathbf{P}}{\partial \mathbf{x}} = 0$$
(D2)

By the continuity equation

•

$$\mathbf{0} = (\mathbf{v}_{0}) \frac{\mathbf{6}}{\mathbf{x}_{0}} + \frac{\mathbf{q}_{0}}{\mathbf{x}_{0}}$$

and second and third terms of equation (D2) can be eliminated to yield

$$\rho \frac{\partial \mathbf{v}}{\partial t} + \rho \mathbf{v} \frac{\partial \mathbf{v}}{\partial \mathbf{x}} + \frac{\mathbf{f}}{2\mathbf{D}_{h}} \rho \mathbf{v}^{2} + \frac{\partial \mathbf{P}}{\partial \mathbf{x}} = 0$$
 (D3)

The first term in equation (D3) is neglected in the model. Neglecting this term and multiply the resulting equation by  $\partial x/\rho$  yields

$$\mathbf{v} \partial \mathbf{v} + \frac{\mathbf{f}}{\mathbf{D}_{\mathbf{h}}} \mathbf{v}^2 \partial \mathbf{x} + \frac{\partial \mathbf{P}}{\rho} = \mathbf{0}$$
 (D4)

Note that at zero flow and second and third terms of equation (D3) are zero, so that it reduces to

$$\rho \, \frac{\partial \mathbf{v}}{\partial \mathbf{t}} + \frac{\partial \mathbf{P}}{\partial \mathbf{x}} = \mathbf{0}$$

in which case the time derivative term is responsible for any pressure drop. The significance of this time derivative term could be investigated by the use of a comprehensive model such as that of Urieli (ref. 7),

### APPENDIX E

# **PROGRAM LISTING AND DEFINITION OF VARIABLES**

This appendix includes

(1) A listing of the computer program with the short form of the printed output for a sample run. (The Calcomp plotting subroutines are not included in the listing.)

(2) Definitions of the variables that are read into the main program using a NAMELIST format

(3) Definitions of the variables shown in the printed output Other key variables used in the program are defined with comment statements that are used throughout the program.

The program consists of a main program and four subroutines. It is programmed in FORTRAN V and has been run on a UNIVAC 1110. All input data are either contained within the program or are read into the main program via the 20 NAMELIST parameters. Values of the NAMELIST parameters used in the sample run were printed out and are shown as part of the output.

#### LISTING OF COMPUTER PROGRAM

#### Main Program

C MAIN PROBRAM C DOES INITIALIZATION. UPDATES PISTON POSITIONS--EXPANSION, COMPRESSION C AND BUFFER SPACE VOLUMES. INTEGRATES PODELTAIVE TO DETERMINE WORK. C DETERMINES WHEN CYCLES IS COMPLETE. DIMENSION X(2),V(13),REYNO(13), OR(5),TMAX(12) DIMENSION TG(12),TGA(13),TM(13),TMAVG(13),DTM(13) COMMON DTIME,F(12),WB(13),DELP(13),P,PE,PC CONHON /CVC/ QEXP, QHEATR, QREEEN, QCOOL R, OCOMP, ENFRTH, ENFHTR, IENFCIR, ENFRTC, URNEP, URNEXP, 24R4CMP, URNEEX, URNEEN, URNEP, URNEN, SUNNUM(13), SUNDEN(13), ENTM. SWDISP, WPIST, WTPIST, GEXPN, GEXPP, GHEATN, GHEATP, GCODLN, GCOOLP, GCOMPN, GCCOMPP, GREGN, GREGP, WDISPP, WDISPN, WPISTP, SWPISTN, GCNDRI, GCNDRO, GCNOCL, GCNDD, GCNDCN, GSHTL, TGEXPA, TGCMPA COMMON /DELTAP/AD, AP, COMMON /TAVCYC/TGCYC(12), TGACYC(13), THCYC(13) CONMON/CTIT/NCURV,ISET1.ISET2.ISET3 CONHON /JNDEX/JIP,NOCVC VAMELIST /STRLNG/P.REALGS.FIPCVC.IPRINT.ITMPS.COEFF.TJ.P3.ONEGA. •FACT1.FACT2.NOCYC.NSTRT.NOEND.HWGAS.TG.TGA.TH.RHCFAC.JIP AD , AP , AR , APISTR / 6.0,6.0,0.11,0.60/ DATA 1 DATA RCRANN, E, RODL, V 3CL, DIAMD, DIAMP, DIAMDR, DIAMPR/ 13.543, 0.82, 1.91, 24.84, 2.75, 2.75, 0.375, 0.875/ DATA VA ¥/J.D.2+1.5948..933.5+J.624.3+D.243.0.J/ C READ IN INITIAL PRESSURES, TENPERATURES AND OTHER PARAMETERS WHICH C DEFINE THE NATURE OF THE RUN TO BE MADE READ (S,STRLNG,END=1))) DTIME=1./ (OHEGA+FIPCYC) WRITE (6,STRLNG) INITIALIZATION C FHULT=1. ITER=3 TINE=D.D PSI=0.0 PSIDEG=0.0 SAVET=0.3 I PLOT=0 PRSUM:0.0 NOITPC=0 DO 11 1=1+13 1f(1-EQ+13) GO TO 12 TGCVC(1)=TG(1) 12 TGACYC(I)=TGA(1) 11 THCVC(I)=TH(1) CPCVC=1./(OHEGA+DTIME) C R. CP. CV IN UNITS OF IN-LBF/ LBM-DEG. R GARHA=1.394 R=9197. CP=32557. CA:5339D\* 8=.32758 IT LANCASINELAL GO TO 15 8=.01613

-----424935\* CP211580. CV28948. 15 CONTINUE [PEIPHINT IPANTZELPRINT/25 ADRIAD-AR APRIAP-APISTR 11414150811(RODL-RCRAWK)++2-E++2) 15001HH1196714000L042-11-RCRAMK14021 100744156RT (800L002-1E+RCRANA1002) STRONVIZ. + (RODYME-RODYMM) 1#7007:7008 # 1 1 1 3 4 0 0 V H X 14712-RODVH1 ¥11124041211-218181+3.945 ¥113122.+408+(RODYH#-80071+0.353 ¥324PR+1-1121-11MIN1+¥3CL V3STARIV3 VOV#1=3.3 D0 33 1=1.13 30 VOVRT=VOVRT+V111/(T64(T)+B+P+REAL63) #3=#3+#3\$1.4/ (R+113+8+#3+REAL65)) ALPHA = UJOR / VOVAT SI&JZALPHA/IP+ALPHA) H=W3/5183 PESP PCIP 00 50 121.13 50 46(1)2Pev(1)/(Re(T84(1)+8+P+REAL85)) 1START:1 J=1 100 CONTINUE 100 CONTINUE 17 (J.LT. 15TART) 60 TO 100 175 (F (J)P.6T.0) 60 TO 100 17 (J.LT.(NOCYC-1)) WRITE (6,133) 130 FORMAT (\*2 TIME ANGLE R(1) T(2) TO\*,7R.\*TD\*,9R.\*T2\*,9R.\*T2 15, SL.\* PE PC PRIM PROUT \*,3R.\*F(0)\*,5R.\*F(0)\*) 17 (J.EE.(NOCYC-1)) WRITE (6,132) 17 FORMAT (\* TIME ANGLE RF1 RE2 RE3 RE4 RE5\* 1\* RE6 RE7 RE6 RE9 RE10 RE11 RE12 2\*RE13\*) 15 (J.FD.WACYCL WRITE (6,133) 15 (1.60.4000405 WRITE (6.133) 133 FORMET (\* 11ME ANGLE ) 15 FB FT FB 11 F2 F3 F4 F5 F10 F11 F12\*1 F\$\* ..... BEBINNING OF LOOP C 140 11ER:17ER+1 IF4J.6E.(NOCVC-41) 1PRINT=1PRN12 (\* ((TIME+SAVET).6T.5.0) 60 10 700 10=10+1 V101L=0.0 00 142 1JR=1,13 142 1707L=201 00 142 VIOIL:VIOIL:VIIJM) IF (JP.61.0) 60 10 170 IF (JP.61.0) 60 10 170 IF (JP.11. IPRINT) 60 10 170 IF (J.11.(NOCYC-1)) WRITE (6.160) VINE.PSIDL6.X.(6(0).V6(0). IT64(1).T64(1)).PE.PC.PRIN.PROUT.F(0).F6.0.1X.0F0.2.2F0.5) IF (J.E0.(NOCYC-1)) WRITE (6.162) VINE.PSIDE6.REVNO 162 FORMAT (1X.FT.0.F6.1.13F6.0) IF (J.E0.NOCYC) WRITE (6.163) VINE.PSIDE6.F 163 FORMAT (1X.FT.0.F6.1.12F0.5) IF (JT67.0.F6.1.12F0.5) IF (JT67.0.F6.1.1000) VE.V60.70 1F (117495.60.1) WITE (6,660) 16,784,78 660 FORMAT (\* 162\*,68,12F6.3/,\* 1642\*,13F6.0/,\* 182\*,13F6.0/)

170 1920 180 TIME=DTIME+FLOATLITERS I FUTTELEDIANE OF LOATUTENT IFUTTER.EQ.IFIX(.3/DTIME) .AND. J.L7.6) BD TO TOD C CALL HEAT EXCHANGER SUBROUTINE TO UPDATE BAS LUMP MASSES, FLOW RATES. C TEMPERATURES, PRESSURE + REGENERATOR METAL TEMPERATURES. CALL HEATX (TIME, TG, TGA, TM, REYNO, QR, X, RODY, J, DIAMD, X1MIN, LODYNX, V, SIB3, W, HUBAS, RHCFAC, REALBS, CONDID, NOCYCI PRSUN=PRSUN+P NOITPC=NOITPC+1 C UPDATE EXPANSION AND COMPRESSION SPACE PRESSURES. ILBE/IN21 PEOLDEPE PCOLDEPC POLDEP 1F (J.LT. (NOCVC+5)) 80 TO 243 PRINCIDELPISS+DELPIGS+D.S+DELPI7SS+FHULT+P PROUT=P-10.S+DELP171+DELP181+DELP1911+FHULT PE:IDELP(2) +DELP(3) +DELP(4)) +FRULT+PRIN PC=PROUT-10ELP113)+DELP1111+DELP11211+FHULT 80 TO 245 240 PE=P PC=P PRIN=P PROUT :P 245 CONTINUE AE: IPE +PEOLD3/2. AC=(PC+PCOLD)/2. A:(P+POLD)/2. DELPRS=PRIN-PROUT DELPHT=PE-PRIN DELPCL=PROUT-PC C CALCULATE INTERNAL ENERGY OF WORKING SPACE GAS. (FT-LRF) UTOTAL=0.0 DO 250 1=1,13 250 UTDTAL=UG(I)+CV+TGA(I)/12.+UTOTAL 260 CONTINUE C BUFFER SPACE BLEED FLOW,FLOTOB (LBN/SEC) IF (1PC-P3) .6E. 0.) 60 to 270 SIB3P=-C0EFF+(P3-PC)++.5/W \$0 10 260 270 \$183P=C0EFF+(PC-P3)++.5/# 300 CONTINUE FLOTOB=\$163P+W IF (FLOTOB.GE.O) ENTHUB=CP+T6A(13)+FLOTOB+DTIME/12. IF (FLOTOB.LT.D) ENTHUB=CP+T3+FLOTOB+DTINE/12. ENTHLENTH+ENTHUR \$163=\$163+\$163P+DTIME 46(13)=46(13)-FLOTOR+DTINE 1F (FLOTOB.LT.D.D) TBA(13)=T64(13)-FLOTOB+DTIME+ 1113-16A(13))/NG(13) \$20 P30L0=P3 P3=13/(V3/15163+x+#1-8+#EAL65) AJ=IP30LD+P31/2. C UPDATE CRANK ANGLE, PSIIRADIANS), PSIDEGIDEBREES) PSIOLDEPSI PS1=PS1+ONEGA+DTINE+6.28318 IF (PSI.6E.6.28318) PSI=PSI-6.28318 PSIDE6=PS1+360./6.28318 C UPDATE PISTON POSITIONS (IN)

RODY=SQR1(RODL++2-(E-RCRANK+COS(PS1))++2)

C UPDATE EXPANSION, CONPRESSION, AND BUFFER SPACE VOLUMES. (183)

#10LD=#411

¥10LD:¥(1) ¥130LD:¥(13)

X(1)=RCRANK+SIN(PSI)+RODY X(2)=RCRANK+SIN(PSI)-RODY

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V(1):AD0(1(1)-1)MIN)+0.965 ¥1131=2, +ADR+ (RODYNX-RODY) +0.353 ¥3=AP441-X121-X1M1N1+¥3CL C CALCULATE WORK (FT-LBF)--EXPANSION SPACE WORK, WRNEXP; COMPRESSION C SPACE WORN, WRNCHP; TOTAL WORN, WRNH; DISPLACER WORN, WDISP; POWER PISTON C dorn, wpist; pressure drop worn loss in Expansion and compression C SPACES, WANLEY AND WANLCH WANPIWARP ACTIVITY - VISOLD 1/12. DWERP=AE+(V(1)-V10LD)/12. WRREXP=WRREXP+DWEXP IF (DWEXP.6T.0.0) WEXPP=WEXPP+DWEXP IF (DWEXP.LT.0.0) WEXPN=WEXPN+DWEXP OWCMP=AG06V(13)-V130L0)/12. WRECHE - WRECHP + DWCHP IF (DUCHP.6T.D.D) UCHPPEUCHPPODUCHP IF (DUCHP.LT.D.D) UCHPREUCHPNODUCHP WRRLEX=WRRLEX+(A-AE ++(V(1)-V10LB)/12. URAL CHEWRAL CH+ (A-AC )+ (V (13)-V130LD)/12. WRKLPIWRKLP+(A-AC)+(4(13)-V130L0)/12. #R4H=#R#H+14E+1#11-#10LD1+AC+1#131-#130LD11/12. DUDISP=1AE+AD-AC+ADR)+1111-110LD1/12. #DISP:WDISP+DWDISP IF IDUDISP.87.0.01 UDISPP=NDISPP+DUDISP IF IDUDISP.L1.0.01 UDISPN=NDISPN+DUDISP DUPIST: AC+ADR+1x(2)-120LD1/12. #PIST=#PIST+D#PIST IF (DWP1ST.6T.0.0) WP1STP=WP1STP+DWP1ST IF (DWP1ST.LT.0.3) WP1STN=WP1STN+DWP1ST WTP1ST=WTP1ST+AC+ADR+(X{2}-X2QLD)/12. 00 533 1=1,13 17(1.70.13) 60 10 531 TGCYC(1)=T6CYC(1)+T6(1) 531 76ACYC(I)=76ACYC(I)+78A(1) 530 THEVELID=THEVELID+THLID .AND. PSI.LT.3.14159 1 60 TO 650 IF (PSIOLO.GT.3.14159 50 TO 140 END OF LOOP £ 650 CONTINUE C CALCULATE AVERAGE GAS TEMPERATURES OVER THE CYCLE FOR EACH CONTROL VOLUME 00 533 1=1.13 IF(I.FG.13) 60 70 530 T6CYC(1)=76CYC(1)/CPCVC 535 76ACYC(1)=76ACYC(1)/CPCYC 533 THEYELLISTHEVELTSJEPEYS TOEXPASTBACYC (1) TOCHPASTBACYC1131 DO 667 11=1,6 JJ=11+6 THAT ( 11) =0.0 667 THAXEJJ1=5000. IF (JIP\_GT.O.AND.J.NE.(NOCYC-1)) 60 TO 668 IF (J.LT.(NOCYC-1)) WRITE (6,163) TIME,PSIDEG,K.P.P3,T64(1), ITGALISI, PE, PC, PRIN, PROUT, VILI, VILI IF LJIP-EQ.D3 WRITE 16,6633 T6,764,TH IFIJ.LT.NSTRT .GR. J.GT.NGENDI 60 TO 675 C CONVERSENCE SCHEHE FOR REBENERATOR HETAL TEMPERATURES. D0 670 J1=5.9 570 NTMAINSTRT 570 DTHEJIJ=FACTI+DTHEJIJ+FACTZ+SUNNUNEJIJ/SUNDENEJIJ TH(\$)=TH(\$)-(\$,\*DTH(\$)\*\*,\*DTH(6)\*3,\*DTH(7)\*2,\*DTH(8)\*DTH(9)1/3, TH(6)=TH(6)-(\*,\*DTH(5)\*8,\*DTH(6)\*6,\*DTH(7)\*\*,\*DTH(8)\*2,\*DTH(9)1/3, TH(7)=TH(7)-(1.+DTH(6)+2.+DTH(6)+3.+DTH(7)+2.+DTH(6)+DTH(9)) TH(\$)=TH(\$)-(2.\*DTH(5)+4.\*DTH(6)+6.\*DTH(7)+8.\*DTH(8)+4.\*DTH(9))/3. TH(9)=TH(9)-(0TH(5)+2.+DTH(6)+3.+DTH(7)+4.+DTH(8)+5.+DTH(9))/3. 60 10 675 675 CONTINUE

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```
DO 673 1=1.5
673 3R111=0.0
     AVENSP:PRSUM/FLOAT (NOITPE)
     CALL CYCL (TINE, UTOTAL, STROKV, AVENSP)
     00 532 1=1+13
     IF (1.E0.13) GO 10 535
16CVC(1)=0.0
535 TGACYCIII=0.0
532 THEVEILI=3.0
     PRSUN=0.0
     . OL TPC= 3
      7=7+7
     1f(J.NE.(NOCYC-1)) 60 TO 680
1PL0T=0
      ITER=0
      SAVET=TINE
      T14E=D.
 SED I 'J.LE.NOCYCH 60 TO 125
TOG CONTINUE
50 T. 10
1000 CONTINUE
570P
      END
```

#### Subroutine HEATEX

```
C THIS SUBROUTINE CALCULATES HEAT TRANSFER AND UPDATES TEMPERATURES AND
C PRESSURE
       SUBROUTINE HEATX ITINE, TE, TEA, THA, REVNO, QR, X, RODY, JCYCLE, DIAND,
      1 X 1 N N ROD YN X, V, SIG 3, W , MWG A S, RHCFAC , RE ALGS, CONDIO, NOCYC )
COMMON DTIME, F(12), WG (13), DELP(13), P, PE, PC
        CONHON /CYC/ QEXP, ONEATR, QREGEN, QCOOLR, QCOMP, ENFRTH, ENFHTR,
      1ENFCTR, ENFATC, URNP, WRKERP,
2WR4CMP, WRKEX, WRKER, WRKEP, WRKEN, SUMNUM(13), SUMDEN(13), ENTH,
      JUDISP, WPIST, WTPIST, QEXPN, QEXPP, QNEATN, QHEAT, ,
42COOLN, QCOOLP, QCONPN, QCONPP, QREGN, QREGP, WDISPP, WDISPN, WPISTP,
5WPISTN, QCNDRI, QCNDRO, QCNDCL, QCNDD, QCNDCN, QSNTL, TGEXPA, TGCNPA
        CONMON /DELTAP/AD, AP.
                                                              HAL131
        DIVENSION COEFX(40), DPX(40)
DIVENSION TGA(13), TH
                                       THA(13), TGAD(13), THAG(13), X(2)
G(13), THIX(13), TG(12), DH(13), AC5(13),
        DIMENSION CPH(13).
      1ANT(13), COND(13), VIS(13), REVNO(13), OR(5)
DIMENSION V(13), WGOLD(13), XL(13), FAVG(13), DNSTV(13), FRICT(13)
        DATA DH/1.437, 3+0.1190, 5+0.003800, 3+3.0439.1.487/.
             AC5/3.250,3+0.05561.5+0.4380,3+0.05124,3.150/,
              AH1/3.3,245.727...922.5482.56,342.288.0.0/.
                                                             4+10.0/,
               CPN/4+10.0.5+.011.
               xL/0.0,2+3.06,2.098,5+0.178,3+0.187,0.0/,
      1
       1 IDEX/1/
C SHILLENYORAULIC DIAMETER, IN.; ACSILLEFLOW AREA, IN2; ANT=HEAT TRANSFER, IN2;
C CPHELISHETAL HEAT CAPACITY, BTU/LBN-DEG.R; XLIIJELENGTHS FOR CALCULATING
C PRESSURE DROP, IN
C CP,CV ARE IN BTU/LBM-DEG.R:GAS CONSTANT, R, IS
C IN IN-LBF/ILBM-DEG R)
        8=.02358
        CP=3.484
        GA4MA=1.394
```

```
9=9197.
        LF (MWGAS.NE.4) GO TO 5
        8=.01613
        CP=1.239
        9=4632.
        GANNA=1.657
     5 CONTINUE
        CV=CP/GANNA
DO 13 I=1.13
IF (MWGAS.EQ.4) GO TO 6
C CONDUCTIVITY, CONDIT! HAS UNITS BTU/IN-SEC-DEG.R
C VISCOSITY,VIS(1) HAS UNITS LBM/IN-SEC
COVD(1)=2.401E-9+76A(1)+1.263E-6
        VIS(1)=4.683E-10+T6A(1)+2.619E-7
     60 TO 8
6 C07D(1)=1.962E-9+T6A(1)+1.115E-6
        VISII)=1.058E-9+T6A111+5.9197-7
     8 THADIIISTNAII)
    10 TEADEIN=TEAEIN
POLD=P
C CALCULATE PRESSURE.LBF/IN2
        SUNWI=J.J
        SU#V=0.0
        DO 10 1=1,13
        SUNWT=SUNWT+NG(1)+TGA(1)
    14 SU4V=SUMV+V(I)
       P=ReSUMNT/(SUMY-BeRewe(1.-SIG3)#REALGS)
FGAMMA=(P/POLD)##((GAMMA-1.)/GANMA)
       DO 23 J=1+13
TGAD(J)=TGAD(J)+FGANMA
    20 THIXEJETGADEJE
C CALCULATE MASSES, NGIII, IN EACH GAS LUMP. .LBM
        504:3.0
        DO 200 1=1,13
  200 SUNSSUN-POV(I)/(RO(THIX(I)+BOP REALGS))
       DO 220 I=1,13
  220 WGOLD(T)=WG(I)
       00 240 1=1,13
  240 #GILI=Well.-SIG3JOPOVIEJ/IROSUNOITHEXIEJOBOPOREALGSIE
  IF (NDEX.EQ.2) GO TO 243
DO 242 I=1,13
242 NGOLD(I)=WG(I)
C CALCULATE FLOW RATES, FIII TELOHISEC, BETWEEN GAS LUMP
  243 40EX=2
       F(1)=(WGOLD(1)-WG(1))/DTIME
  00 300 1=2,12
300 F(1)=(WG0LD(1)-WG(1))/DTIME+F(1-1)
       DD 24 1=1.12
IF(FII).LT.0.) 60 TD 22
        16(1)=16A0(1)
      IF(1)6T.4 .AND. 1.LT.10) TG(1)=TGAO(1)-(TMA(5)-TMA(9))/8.+
IF(1)0DTIME+(TMA(5)-TMA(9))/8./WGOLD(1)
    60 TO 24
"2 T6(1)=T6A0(1+1)
       IF(1.GT.3 .AND. I.LT.9) TG(1)=TGAD(1+1)+(THA(5)-THA(9))/8.+
       IFILIODTINE+(THA15)-THA(9))/8./WGOLD(I+1)
    24 CONTINUE
C CALCULATE AVERAGE FLOW RATES FOR EACH GAS LUMP.
FAVG(1)=F(1)
DO 30 1=2,12
30 FAVG(1)=(F(1-1)+F(1))/2.
       FAVG(13)=F(13)
C REVISE GAS TEMPERATURES TO ACCOUNT FOR MIXING.
IF (F(1)).LT.0.0) TMIX(1)=(WGOLD(1)+TMIX(1)-F(1)+DTTME+
      176(1))/w6(1)
        00 100 1=2.12
```

OF POOR QUALITY

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100 THIX(I)=(#60L0())+THIX(I)+(F(I-1)+T6(I-1)-F())+T6(I)+
      IDTIME H/WG(I)
       1F (F(12).ST.D.D) THIX(13)=(WSOLD(13)+THIX(13)+F(12)+
      1011HE+16(12))/86(13)
  110 CONTINUE
C CALCULATE REVNOLDS NO S. REVNOID; HEAT TRANSFER AREAS, ANTII;
C HEAT TRANSFER COEFFICIENTS, NAILI BETWEEN GAS + HETAL LUMPS.
C HAIIJ HAS UNITS BTU/SEC-DEG.R
       REVNO(1)=DH(1)+ABS(F(1))/(VIS(1)+ACS(1))+.3331
       AHT(1)=3.1416+DTAMD+(X(1)-X1MIN)+16.6
       441'1=COND(1)/DH(1)+(1.071E-3+DH(1)+ABS(F(1))/(VIS(1)+
* 1))+15.1+AHT(1)
C TO N- : EXPANSION SPACE PROCESS ADIABATIC SET HA 1 =0.0
       HAL11: 3.3
£
C
C
  QUENCHING IN EXP. SPACE--RADIATION .70 EFFECTIVE--HCONV=5/3600/144 HI
       1:1
       xL(1)=x(1)-x1010+.01
       KL(13)=V(13)/AP+.01
       F0A=D.7
       IF(ABS(THIX(1)-THA(1)).LE.1.3) 50 TO 42
       3RAD=0.1730F0A01(TWIK(1)/100.1000-17HA(1)/100.1000)
HRAD=QRAD/(TWIK(1)-TMA(1))/3633./100.
       50 TO 43
   42 HRAD=0.0
   N3 CONTINUE
       PR=CP+VIS(I)/COND(I)
       4CONV=0.0234 REVNO(1)++0.8+PR++0.++COND(1)/DH(1)
       IFIREVND(1).G1.2100.0.AND.REVND(1).LT.10000.) HCONV=HCONV+(1.+(DH)
      11)/XL(1))++0.7)
       BRAETZ=REYNO(1)+PR+DH(1)/XL(1)
       IFIRE YND(I).LE.2103.3.AND.GRAETZ.GT.10.) HCDNV=1.06+GRAETZ++3.333+
      1CONDETS/DHETS
       IFIRE YND( I).LE.2100.0.AND.GRAETZ.LE.10.1 HCONV=5.0/3600./144.
EFILEO.13) GO TO NO
C ACCOUNT FOR HEAT TRANSFER TO INSULATED PORTION OF HEATER TUBES
C (ADJACENT TO EXPANSION SPACE) ALONG WITH HEAT TRANSFER TO EXPANSION
C SPACE WALL
       #L1=1-371
       REYNO1=DH121+ABS4F1111/8.D/(VIS111+ACS121)+.0001
       AHT1=14.955+XL1
       4C3NV1=0.023+RE4N01++0.8+PR++D.++C0ND111/DH121
       HAI= CHRAD+HCONVIJ+AHTI
       HAELD=EHRAD+HCONVJOAHTELD+HAL
C
       00 43 1=2,12
       REVNO(1)=DH(1)+ABS(F(1-1)+F(1))/2./8./(VIS(1)+ACS(1))+.0001
      [F ([.LT.5.0R.1.6T.9) HA(1)=COND(1)/DH(1)+(1.87)E-3+
1DH(')+ABS((F(1-1)+F(1))/2.1/8./
      21 VISII)+ACS(I))+15.)+AHT(I)+8.
       IF (1.6E.5.AND.I.LE.9) HA(I)=COND(I)/DH(I)+(0.06)71+
      10H(1)+ABS((F(1-1)+F(1))/2.)/8./
      26 VISCI) #ACSCI11 #3.71#AHTCI1#8.
   NO CONTINUE
       HAL43=0.3
       DO 41 1=5.9
    41 HATIS=RHCFAC+HATIS
       REVNO(13)=DH(13)+ABS(F(12))/(VIS(13)+ACS(13))+.D331
       AHT(13)=6.2832+DIAMD+(RODYMX-RODY)+5.5
     HA(13)=COND(13)/DH(13)+(1.871E-3+DH(13)+ABS(F(12))/
1(VIS(13)+ACS(13))+15.0+AHT(13)
C TO MAKE COMPRESSION SPACE PROCESS ADIABATIC SET HA 13 =3.0
C 44(13)= 0.0
       1=13
       IFIF-EQ-131 60 TO 42
   44 HACISITHCONVEANT(13)
C
```

```
53
```

```
C CALCULATE RATES OF HEAT TRANSFER RETUEEN GAS AND METAL AND REVISE
C BAS TENPERATURES TO ACCOUNT FOR HEAT TRANSFER TO OR FROM METAL.
      00 120 N=1,13
      HANCE-DTIMEONAINI/INBINIOCPI
      FCTR=1.-EXPINAUC)
      DIGA: (THAOIN) -THIXIN) SOFCTR
      3441=-DIGAOUBINIOCP/DTINE
      NFCTR:FCTRONG(N)
      HOTSA: OTSAONS (N)
      SUMMUMANT:SUMMUMANT+#0164
      SUADENINS=SUNDENINS+#FCTR
  120 TEACHISTHINCHIOTGA
      LF IJCVCLE.LT. INOCVC-511 60 10 64
C CALCULATE DEWSITY, FRICTION FACTORS, AND DELTA PRESSURES
C FOR EACH LUMP.
  D0 130 1=1.13
130 DNSTV(11=P/(R+(164(1)+B+P+R[4[65))
      00 100 1=2,12
If (REVNO(1).L1.1503.AND.1.L1.5.3R.I.6T.9) FRICT(1)=16./REVNO(1)
      192790111000.2
      IF 11.6E.5.AND.1.LE.01 FRICT(1):3.96+EXP(-0.0190+#EVN0(1))+0.54
  140 DELPIII=FRICTIII+FAVEII+ABSIFAVEII++XLII+
     1132.20DH1110DNSTV11104CS11100206.060.1
C PRESSURE CROP CALCULATIONS
      00 141 1=1.40
  141 DPX111=54444
      ACSEXP=V(1)/AD+3.1416+2.75/8.
      ACSCO4=V1131/AP+3.141642.75/8.
      1:1
      [FIFI]).LE.0.0) J=2
      ZEP
      F01=F(1)
      F32=F121
      F04=F141
      F30:F101
      F12:F4121
      CALL NDELPIJ, ACSENP, AC31021, DH1321, NL 1021, DNS141321, VIS1321, FD1
     #,2,COEFX(01),DPX(01),1)
C
      CALL #DELP(3,ACS102),ACS102),DH(32),HL(02),DHSTV(02),VIS(02),F01
     N. 2. COEFX(02), DPX(02), 2)
      CALL XDELPIN, ACSID21, ACSID21, DHIJ21, RL (D21, DNSTV(031, V15103), FO?
     #,2,COEF#1031,OP#1031,31
C
      OPFR1C=0.0
      XF5=XF15)
      00 142 1:2,12
      17(1.E0.2) XL(2)=XL2+1.321
17(1.LT.5.OR.1.5T.9) NTVPE=10
17(1.GE.5.AND.1.LE.9) NTVPE=11
      CALL NDELPINTYPE, ACSIII, ACSIII, DHIII, NLIII, ONSTVIII, VISIII, FAVGII
     X, 2, COEFR(1+2), DPX(1+2), (1+2))
      #L121=XL2
      DELPITITOPHIL+21
DFFRICTOPFRIC+DELPITI
UTTRICID
192 CONTINUE
C
      1717101.67.0.0) 60 TO 61
CALL XGELP(1.4CS(001.622000.0H130).XL(00).DNSTV(001.VIS(04).FO
     x, 2, COEFX(15), JPX(15), 15)
      60 10 62
   61 CONTINUE
      CALL NOELPII, .62.000, ACSILOF, DHILOF, NLILOF, DWSTVIIOF, VISILOF, FOP
     X, Z, COEFR(16), DPX(10), 16)
   62 CONTINUE
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. ... is oscie is

CALL XDELP15, ACS1121, .043370, JH1121, AL1121, DNSTV1121, VIS1121, F12 #. Z. COFF#1171. DP#1173.171 J=2 17171121.LE.3.31 7=1 CALL NDELP(J, ACS(12), ACSCON, DH(12), XL(12), DNSTV(12), V15(12), F12 x.2.COEFX(18).DFX(18).18) DPSUN:0.0 D0 63 1=1.17 DPSU4=DPSU4+DPX(]) ORIGINAL PAGE IS OF POOR QUALITY 63 CONTINUE DELPHIN=OPFRIC DELPHISHOPSUR C DELP4C21:DELP4021+DPK4011+DPX4021 361P1031=061P1031+0PX1031 GELP(34)=DELP(34)+0PX(15) DELP4101=0ELP4101+0PX4161 DELP(12)=DELP(12)+DPX(17)+OPX(18) 17% CONTINUE C CALCULATE HEAT CONDUCTION ICALL HEAT CONDUCTION SUBROUTINES IF INCOND.NE.3) CALL CNDCT ITMA.QCREG .QCVL.QCONDD.QCAN.QSHTTL. 1446431 NCOND:3 64 CONTINUE C REVISE REBEWERATOR METAL TEMPERATURES. DO 177 J=5.9 177 THALJI=THALJI=GLJI=DT [HE/CPHLJ] C CONVERT 01,1'S TO FT-LBF & SUN UP FOR EACH COMPONENT. QTOT=0.0 9EX:3.0 SHEAT: 0.0 QHETN:0.0 DHETP:0.3 SREGE:0.0 0#6P=0.0 BREN:C.J 30001:0.0 QCOL P=0.0 BCOLN:D.J 2034=0.0 00 179 J=1.13 BADD=01 JI+DTIME+777.3 IF IJ.EO.IF GEX:GEX+GADD IF IJ.GE.2.AND.J.LE.+) QHEAT=QHEAT+QADD IF (J.6E.2.AND.J.LE.N.AND.VADD.LT.D.D) QHETN=QHETN+GADD IF (J.6E.?.AND.J.LE.N.AND.QADD.6T.D.J) QHETP=JHETP+QADD IF (J.GE.S.AND.J.LE.9) ORE&E:ORE&E +0ADD IF (J.GE.S.AND.J.LE.9.AND.QADD.GT.D.)) OREP:046P-0ADD IF (J.GE.S.AND.J.LE.9.AND.GADD.LT.D.J) GREN: QPEN+GADD IF ( 1.GE. 10.AND. J.LE. 121 0COOL = 0COOL + 0ADD IF (J.GF.13.4ND.J.LE.12.AND.GADD.LT.3.0) GCOLN-GCOLN+GADD IF (J.GE.10.AND.J.LE.12.AND.GADD.GT.3.0) GCOLP=GCOLP+OADD IF (J.EG.13) GCOM=GCOM+GADD 179 3701=0101+0ADD 00 185 J=1.5 185 OR(J)=QR(J)+Q(J)+DTINE/CPH(J) JEXP=QEXP+QEX IF COEX .LT.J.D. OF XPN: OF XPN.OF.X IF IGEN .GT.D.DF QEMPPEGEMPP+GEM ONEATR:ONEATR+ONEAT THEATH CHEATH + CHETN QHEATP = QHEATP + QHETP OREGEN=ORFGEN+OREGE OREGN=OREGN+ORGN ORESP=ORESP+ORSP AC0014:000014+00001

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3C30LFIGC00LF+QC0LF

QC30FIGC0NF+QC0N

QC30FIGC0NF+QC0M

IF 4QC4.6T.J.D) QC0NFFIQC0NF+QC0N

IF 4QC4.5T.J.D) QC0NFFIQC0NF+QC0N

3C4D7IGC40FI+QCRE6 4071MC+777.3

QC4DR0IGC40FI+QCRE6 4071MC+777.3

QC4DR0IGC40FI+QCRE6 4071MC+777.3

QC4DC40C4+QC4N+071ME+777.3

QC4DC40C4+QCAN+071ME+777.3

QC4DC40C4+QCAN+071ME+777.3

QC4DC40C4+QCAN+071ME+777.3

QC4T14UC

ENFR1HICUFFTH-AMIN1FF1+0+CF,J.J1+761+0+071ME

ENFR1HICUFFTH-AMIN1FF1+0+CF,J.J1+761+0+071ME

CMFC1RICUFFTC+AMIN1FF1+0+CF,J.J1+761+0+071ME

CMFC1RICUFFTC+AMIN1FF1+0+CF,J.J1+761+0+071ME

CMFC1C2C4FR1C+AMAX14F1+0+CF,J.J1+761+0+071ME

CMFUNM
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Subroutine CYCL

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C THIS SUBROUTING IS CALLED JUST ONCE PER CVCLE--WHEN THE CVCLE IS COMPLETE.
C IT CALCULATES--NET HEAT IN AND OUT, NET WORN PER CVCLE, INDICATED POWERS
C AND EFFICIENCY, ETC. HEAT AND WORN BUANTITIES ARE STORED FOR CALCULATION
C OF AVERAGES DVER S CVCLES. AFTER STORING, INTEGRATED HEAT AND WORN
C BUANTITIES ARE RESET TO ZERO IN PREPARATION FOR WEAT CVCLE.
SUBROUTINE CVCL ITINE, UTOTAL, STROKY, AVGUSPI
          DISCUSION VARIADAS, STORE (11,66)
          CO9404 DII4E, Fill, #5(13), DELP(13), P.P., PC
          DATA J.N.STORE.OLDIIN/203. 40703./
DATA JIP1/0/
         COMMON /CVC/ QEIP, GHEATH, GREAFN, GCOOL R, GCONP, ENFRTH, ENFHTH,
IENFCIA, ENFRTC, WRAP, WRAEIP,
JURACAP, WRALER, WRALCA, WRALP, WRAH, SUMMUN(13), SUNDEN(13), ENTH,
         JOLLSP, UPIST, UTPIST, OC KPN, OCKPP, ONE ATV. ONE ATP.
         NECOOL W, BCOOL P, BCORPH, OCCXFF, BREEN, BREEP, HDISPP, HDISPN, HPINTP,
        SUPISIN, OCNORI, OCNORO, OCNOCL, OCNOD, OCNOCH, OSNIL, TECHPA, TECHPA
          CONNON /TAVEYC/16CVC(12), TBACVC(13), THEVC(13)
          DAJON ATFITION NONA
          EQUIVALENCE (VARILI, OCAP)
          J:J+}
          424+1
          J191:J191+1
          IFIOLOTIN.BI.TIME > OLDTIN:D.
DELTIN:TIME-OLDTIN
          OLDTIN:TIME
          DIN: -OEXP-OHEATR+OCNDRI+OENDCL+OCNDD+OCNDCN+OSHTL-WARLT/2.
          814349-4439-28418
          BOUT = BCOOL R + BCOMP + BCNDRO + BCNDCL + BCNDO + BCNDCH + BSNTL
          WRETOTEWRKE HP + WRECHP
          WRALTIWRALER+WRALCH
          WRRRASSWRN TOT + WRNLT
          EFFTOT=WANTOT/QIN
          EFFP:WRNP/QIN
          REFFLIENFRIMZENFHIR
          REFF2:ENFCTR/ENFRIC
          PURNP:URNH/ (553.+DELTIN)
```

PARKA=PARHP4.7457 FREQ=1./DELTIN ENSPH=STROKV+FREQ+63. C STORE VARIABLES FOR CALCE' ATION OF AVERAGES OVER 5 EVELES. STORE(K,1)=QIN STORE (#,2)=QOUT STOREIN, 31:WRKEXP STOREIK, 4) = WRKCMP STOREIK, 5) = WRKTOT STORE (K, 6) = EFFTOT STOREIN,7)=REFF1 STOREIN, BISREFF2 STOREIN, DISORESEN STOREEK, 131=PWRHP STORE (#,11)=FREQ STOREIN, 121 =WRKLT STORETR,131=ENTH STORE (K, 14) -UTOTAL STORE(K,15)=EN3PH STORE (K, 16) =AVGWSP STORE (K, 17) = UDISP STORE (K, 16) = UPIST ORIGINAL PAGE IS STORE (K, 19)=UTPIST STOREIK, 201 = WRKLP OF POOR QUALITY STORE IN , 211=BEXPN STOREIN, 221 =QEXPP STOREIN, 231 =QNEATN STORE (N. 24) = QHEATP STORE (N. 25) = QCOOLN STORE IN . 261=0COOLP STORE IN . 271=0COMPN STORE (K, 28)=QCOMPP STORE (K, 29) = OREGN STORE IN, 301=QRE 6P STORE (K, 31) = NOISPP STORE (K, 32)=NDISPN STORE (K, 33)=NPISTP STORE (K, 34)=UPISTN STORE (K, 35) =QCNDR1 STORE (K, 36)=QCNDRO STORE (K, 37)=QCNDCL STORE (K, 38)=OCNOD STORE (N, 39) =QCNDCN STORE IN, NOISTGE XPA STORE(K, 41)=TGCPPA STORE (K, 42)=QSHTL STORE (K, 43) =QIND STORE IN . 44 JEURHBAS DO 93 L=1.13 IF(I.EQ.13) 60 TO 91 H=L+48 STORE (K, N)= T6CYC(L) 91 M=L+60 STORE(R,M)=TGACVC(L) #=L+73 90 STOREIR, HI=THCYC(L) 100 CONTINUE ISU CONTINCE IF (JIP-6T-D-AND-JIPI-NE-NGCVC) 50 TO 301 IF (JIP-6T-D) WRITE (6,202) 202 FORMAT (\* LAST CYCLE\*) WRITE (6,200) GIN.GOUT.WRKEXP.WRACMP.WRRTOT.EFFTOT.REFF1.REFF2. •RESEN, PURHP, FREQ, URNLT, ENTH, UTOTAL, •ENJPN, AVGNSP, UDISP, WPIST, UTPIST, NRNLP, •QENJPN, QEXPP, QHEATN, QHEATP, QCOQLN, QCOQLP, QCONPN, QCONPP, •QREGY, QREGP, WDISPP, WDISPN, WPISTP, WPISTN, QCNDRI, QCNDRO, +OCNDCL, QCNDD, QCNDCN, TGE XPA, TGCNPA, QSHTL, QINB, WRKBAS

230 FORMAT (/\* Q1w2\*,F8.3,1X,\*QOUT2\*,F8.3,1X,\*WRMEXP2\*,F8.3,1X, 1'WR4(PP2\*,F8.3,1X,\*WRNTOT2\*,F8.3,1X, 2\*(FF10T2\*,F8.3,1X,\*REFF12\*,F8.3,1X,\*REFF22\*,F8.3,1X/ 3\* OREGEW2\*,F8.3,\* PWRHP2\*,F8.3,\* FREG2\*,F8.3, UTOTAL2\*, 5\*13.3/\* (M3PM2\*,F10.3,\* AVGWSP2\*,F8.3,\* UTOTAL2\*, 6\* J01SP2\*,F8.3,\* UPIST2\*,F8.3,\* UTPIST2\*,F8.3,\* URMLP2\*,F8.3/, 7\* 0C1PW2\*,F8.3,\* 0C1PP2\*,F8.3,\* 0HEATM2\*,F8.3,\* 0HEATP2\*,F8.3/, 0\* 0C00LM2\*,F8.3,\* 0C1PP2\*,F8.3,\* 0HEATM2\*,F8.3,\* 0HEATP2\*,F8.3/, 0\* 0FEGW2\*,F8.3,\* 0C00LP2\*,F8.3,\* 0C0MPW2\*,F8.3,\* 0HEATP2\*,F8.3/, 0\* 0FEGW2\*,F8.3,\* 0C00LP2\*,F8.3,\* 0C0MPW2\*,F8.3,\* 0C1SPW2\*,F8.3/, 1\* UPISTP2\*,F8.3,\* 0C00LP2\*,F8.3,\* 0CMDR12\*,F8.3,\* 0CMDR02\*,F7.3,\*/ 2\* 0CVDCL2\*,F8.3,\* 0SWTL2\*,F8.3/,\* 01WB 2\*,F8.3,\* URK8AS 2\*,F8.3} 301 COWTINUE JUN CONTINUE DO 300 1=1.66 370 VAR11)=3.3 1FtJ.EQ.5) 60 TO 400 RETURN 100 1:0 J=3 DO 450 ##=1,86 STORET11, NRJ=STORET1, NR7/5. 00 450 14:2,5 SSD STORE(11, MAJESTORE(11, MAJ+STORE(EM.MAJ/S. S75 CONTINUE IF (JIP.ST. C. AND. JIPI.NE. NOCYC) SO TO 601 URITE (6,600) URITE (6,200) (STORE(11,8%),8%=1,44) IF (JIP.6T.D) WRITE (6.234) 204 FORMAT (\* AVERAGE TEMPERATURES OVER LAST CVCLE\*) WRITEIS, 2011 TECVC, TEACYC, THCVC 16CYC: ', 4x, 12F8.0/, ' TEACYC: ', 13F8.0/, ' THCYC: ', 13F8.0 201 FORMAT 1\* 1/) SOO FORMAT LIND, "AVERAGE VALUES OF LAST & CYCLES" SOL RETURN END

#### Subroutine CNDCT

```
SUBROUTINE CNDCT (THA.OCRE6 .OCVL.OCONDD.OCAN.OSHTTL.HUGAS)
DIMENSION THAILSI. Trv1831. Trv1831.TCA
                                                                                 TCVL131, TCAN(3).
        ACANIZI, DCANIZI
CONNON /CVC/ QEXP, ONEATR, DREGEN, GCOOL R, GCOMP, ENFRTH, ENFNTR,
       1
       IENFCTR.ENFRTC.URNP.URNEXP.
       ZWR4CHP, WRMLEX, WRMLCH, WRMLP, WRMH, SUMNUM(13), SUMDEN(13), ENTH,
       JUDISP, WPIST, WTPIST, QE IPN, QENPP, QHEATN, QHEATP,
QCOLN, QCOOLP, QCONPN, QCOMPP, QREGN, QREGP, WDISPP, WDISPN, WPISTP,
       SUPISTN, GCNDRI, GCNDRO, GCNDCL, GCNDD, GCNDCN, QSHTL, TGEXPA, TGCMPA
        DATA TRD, TR1, TR2, TCVL/1760., 1172., 585., 1760., 1255., 975./,
e12, R2, R3, R4, RL3, KL4/1.38, 1.62, 1.56, 1.53, 1.126, 0.400/.
       ۱
                R11.R0.R1.XL1.XL2./0.454.0.521.0.495.0.400.0.470/.
                   ACONDD. DCONDD/D. 5875.1.716/.
                   TCAN/1400.,1203.,1103./.
                   ACAN, DCAN/1.154,1.196.3.5.0.75/.
        1
1 CLEAR, DISPD, STRONE/.010, 2.75, 1.23/
C ACONDR, ACVL, ACONDD, ACAN---AREA S IN IN2
C DCONDR, DCVL, DCONDD, DCAN---DISTANCE IN IN
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ORIGINAL PAGE IS OF POOR QUALITY

C TCVL.TCAN--- TENPERATURES IN DEGREES R C CLEAR--CLEARANCE BETWEEN DISPLACER AND CVLINDER, IN. C DISPD---DISPLACER DIAMETER, IN C STROKE---DISPLACER STROKE. IN. C CALCULATE MEAT CONDUCTED THROUGH CYLINDER, BTU/SEC TCAV61=(TCVL(1)+TCVL(2))/2. TCAV62=(TCVL(2)+TCVL(3))/2. THEND1=(.00387+TEAV61+6.793)/(3630.+12.) IF (TEAV61.6T.1063.) THEND1=(.30%67+TEAV61+5.932)/(3600.+12.) THEND2=(.00387+TEAV62+6.793)/(3600.+12.) IF (TCAV62-67,1060.) THCN02:(.)0467+TCAV62+5.932)/(3600.+12.) QCVL1:6.283+THCN01+R12+(R3-R2)+(TCVL(1)-TCVL(2))/(RL3+AL06(((R3-18121+182+812))/(483+812)+(82-812))) 3CVL2=6.2030THCND20R120(R4-R3)0(TCVL(2)-TCVL(3))/(XL40ALOG(((R4-1R12)+(R3+R12))/((R4+R12)+(R3-R12)))) BCVL:10CVL:00CVL21/2. C CALCULATE MEAT CONDUCTED THROUGH DISPLACER,BTU/SEC TEAVE=(TECXPA+TECHPA)/2. THCOND=1.00387+T64V5+6.7931/13600.+12.1 IF (164V6.67.1060.) THCOND=(.)3467+764V6+5.9321/(3633.+12.) gcondo=4condo=Thcond+(765xP4-75cnP4)/Dcondd C CALCULATE MEAT CONDUCTED THROUGH EXTERNAL CAN, BTU/SEC QCAN=0.0 DO 300 I=1,2 TCAV6=+TCAN11 >+TCAN11+1)>/2. THEOND=(.00387+TEAV6+6.793)/(3603.+12.) IF (TEAV6.6T.1060.) THEOND=(.00467+TEAV6+5.932)/(3600.+12.) 300 BCAN=QCAN+ACANIII+THCOND+ITCANIII-TCANII+1)}/(DCANII)+2.) C CALCULATE HEAT CONDUCTION THROUGH REGENERATOR, BTU/SEC TRAV61=(TRO+TR1)/2. TRAV82=(191+182)/2. THEND1=(.03387+TRAV61+6.7931/(3630.+12.1 IF (TRAV61.6T.1060.) THCND1=4.00%67+TRAV61+5.9321/(3600.+12.) THCND2=4.00387+TRAV62+6.7931/(3630.+12.) IF (IRAV62.6T.1060.) THCHD2=1.006.5T4TRAV62.5.9321/(3600.412.) OCRIN=3.1424(R0442-R1)44214THCHD1 4(TRO-TR1)/XL1 3CROUT = 6.283 THCND2+R11+IR1-R01+ITR0-TR11/IXL2+ALOGIIIR1-R111+ 1(R0+R11))/((R1+R11)+(R0-R11)))) SCREG=OCTIN+OCROUT1/2.+0. C CALCULATE SMUTTLE MEAT TRANSFER, BTU/SEC IF (HW6A5.E0.4) THCND6=1.962E-D941 TCVL(1)+TCVL(3))/2.+1.115E-6 QSHTTL=THCND6+3.1416+DISPD+STRONE++2+ITCVL(1)-TCVL(3))/18.D+CLEAR+ 14 XL 3+ XL 9 ... RETURN END

59

Subroutine XDELP

SUBRJUTINE XDELP(K, AREAIN, AREAOT, DNX, XLGTH, ROX, VISX, FLOWIN, PYIN, XCDEF, DP, N) C IDEVIFICATION OF TYPE OF LOSSES C RTYPE:I CONTRACTION--RTYPE:2 EXPANSION--RTYPE:3 9D-TURN --RTYPE:A 1 C RTYPE:5 OTHER TURN --RTYPE:2 EXPANSION-TUBE--RTYPE:3 PD-TURN --RTYPE:A 1 C RTYPE:5 OTHER TURN --RTYPE:4 FRICTION-TUBE--RTYPE:3 PD-TURN --RTYPE:A 1 C RTYPE:5 OTHER TURN -OR TUBE--ISOTHERMAL C RTYPE:9 FRICTION+MOMENTUM FOR REBENERATOR--ISOTHERMAL

```
DIAENSION COEFECADI.DPECADI
DATA BRAV/32.2/, #51/0.006945/
        6444A:0P
        IF (ABSIFLOWIN).LE.D.D) RETURN
PREJ.
Pouted.
Demoneo.
        ATYPESK
        AINZAREAIN/144.
        ADUT: AREADT/144.
        DE=DHX/12.
        #L6=#L8TH/12.
        R0=R01+144.+12.
        ¥15C=¥15#+12.
        FLOW=ABS4FLOWIN1/8.3
        PINEPHIN
        RONEANERO
        1FIAIN-ABUTI 30, 30, 31
    30 ANINEAIN
AEAIN/AOUT
        30 10 32
    31 ANIN=AQUT
        A=ADUT/AIN
    30 CONTINUE
        IFIA.LT.D.DDI) A=D.D
VEL=FLOW/AHIN/RO
        VELHD=R0+VEL++2/(2.0+6RAV)
RE=R0+VEL+DE/VISC
        80 10 11.2.3.4.5.6.7.6.7.6.7.KTYPE
C
     1 CONTINUE
    * C-VIINUE
* RTVPE:1 CONTRACTION
IF(RC-3000.01 12.12.11
11 COEF:-0.444+0.5
%0 TO 100
12 COEF:-0.444+1.0
complements
C
        60 TO 100
C
     2 CONTINUE
    #TYPE:2 EXPANSION
IF(RE-3000.0) 21.21.22
21 COEF=(1.3-2.6+A+1.335+A++2)+(-1.3)
C
    60 T0 100
22 COEF=11.0-2.0928+A+0.996+A+=21+(-1.0)
         80 10 100
C
      3 CONTENUE
        COEF=0.22
80 TD 102
C
      . CONTINUE
        COEF=3.0+0.22
30 TO 102
C
      S CONTINUE
        COEF =0.11
60 TO 102
C
      6 CONTENUE
       RTYPE:6 FRICTION-TUBE
C
        IFIRE.LT.1500.) COEF-16.0/RE+14L6/4DE/4.0))
IFIRE.GE.1500.) COEF=3.346/RE+43.244X6/4DE/4.0))
         60 TO 102
C
      7 CONTINUE
        ATVPETT FRICTION-REGENERATOR
C
```

```
COEF=0.96+EXP1-0.0190+RE1+0.54
         COEF=COEF+(#LG/IDE/4.D))
   60 10 102
130 COEF=3.3-A++2+COEF
102 DP=COEF+VELH0+PSI
       Z UF=COEF=VELHDOPSI

IFI NTVPE.LT.BJ 60 TO 101

«TVPE=8 FRICTION+NOMENTUM --TUBE NTVPE=9 SAME FOR REGENERATO

NTVPE=13 --TUBE MON.+FRIC. NTVPE=11--FOR REGERATOR ADI

IFINTVPE.BE.10) GAMMA1=BARMA

UMA1=VEL/SQRT(GAMMA+PIN+1++.0/0/006RAV)

UMA2=1.D/SQRT(1.D/XMA1++Z-BAMMA+COEF)

FMA2=1.D/SQRT(1.D/XMA1++Z-BAMMA+COEF)
C
C
         PHA21=1.0
         IFLABSIINMAZ-XMALI/XMALI.LE.J.JJI 60 TO 52
     51 XHAD=1XHA1+XHA21+0.5
         FMA21=((BANNA-1.0)+XNA3++2+2.3)/((BANNA-1.3)+XNA1++2+2.0)
         FINTVPE.LT.10) FNA2121.0
IFINTVPE.LT.10) SANNA121.0
RHAZ=1.0/SQRT11.G/XHA1002-GANMA0COEF.GANMA01GANMA1.1.0)/2.0/GANMA1
        10AL0611X441/X44010020FH42111
         IFEABSERMAZ-RMADI.67.0.0011 60 'J 51
    52 TR=1.3/FHA21
         VR:XMA2/XMA1+5QRI(1.0/FMA21)
PR:XMA1/XMA2+5QRI(1.0/FMA21)
POUT:PR=PIN
         DP=PIN-POUT
   101 CONTINUE
         IFIFLOWIN-LE.O.O. DP=1-1.J+OP
         COEFAIN)=COEF
         DPX(N):DP
         RETURN
                                                                                   ORIGINAL PAGE IS
         END
                                                                                   OF FOOR QUALITY
```

# Printed Output of Sample Run

STRLMS					
•	:	· # \$08000 + 03			
PEAL 65	:	-133333903E+31			
FIPCTC	x	-10093990E+34			
104141	2	+530			
THPL	2	• 3			
CDE ##		.1000300001-93			
13	:	. 70003860f +03			
P3	2	.873339936+33			
842 54	I	- 500020001 +32			
FACTI	-	- 10000001 -00			
FACTZ	-	.1933339936+32			
	-	45.8			
ISTOT	-	- 50			
	÷.				
	:				
74	:				
	•		· 100000000 • 04 •	- 100 700 700 404 .	. 1000000000000000000000000000000000000
				. 1334333000 +34.	. 10 / 4035 8 + 04 ,
	-			- 240000001 -0 3 -	
104	-	- 1 v0a30001 •34,	· 106000000 • 04 .	. 186088306+84 .	.16508008E+04,
		.165030030+34,	· 147400082 • 34,	.133438306+34,	.137423336+84,
		- / /5030002 +03,	• 2 • 00000000 • 0 3 •	• \$40708308 +03 •	•\$ <b>\000000E</b> •03.
		-243238836+33			
1.	÷	- 176838036+34,	- 19 300 <b>0</b> 000 + 64 ,	. 19308838E +B4 .	.162500990(+0%,
		-165837832+34,	.149403036+34,	.133437336+34,	.13743330E+04,
		.775030036+03,	.346000000000000.	- 5400000E +0 3 ,	.5+0000002+73,
		-2400000000 +03			
RHEFAC	I	- 100030002 + 31			
110	Ξ	•1			

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#### SEND LAST EVELE

AT A THE TAXENESS AND TE 179.851 WHATER IDS.077 WHATER -161.296 WHATET 100.181 EFFIDT: .036 HTF1: .097 HTF2: .090 AFGEN: .137 PWHMP: 13.137 FFTD: 50.323 WHATE 17.515 (HTM: -1.033 UTDIAL: 1760.093 EN3PP: 3566.009 AVEWSP: 790.200 WDISP: -10.219 WPIST: 150.000 WTP1ST: 150.000 WHATE: 6.003 EN3PP: 3566.009 AVEWSP: 790.200 WDISP: -10.219 WPIST: 150.000 WTP1ST: 150.000 WHATE: 6.003 EN3PP: 3566.009 AVEWSP: 70.200 WDISP: -10.219 WPIST: 150.000 WTP1ST: 150.000 WHATE: 6.003 EN3PP: 3566.009 AVEWSP: 70.200 WDISP: -10.219 WPIST: 150.000 WTP1ST: 150.000 WHATE: 6.003 EN3PP: 3566.009 AVEWSP: 70.200 WDISP: 0.710 WDISP: -10.020 WTST: 150.000 WHATE: .007 EN3PP: 3566.009 AVEWSP: 70.200 WDISP: 0.710 WDISP: -10.020 WTST: .007 EN3PP: 3566.009 AVEWSP: 0.2018 WHATE: .000 EN3PP: 3566.009 AVEWSP: 0.2018 WHATE: .000 EN3PP: 310.257 WHATE: .000 EN3PP: 310.267 WHATE: .000 EN3PP: 310.267 WHATE: .000 EN3PP: 310.267 WHATE: .000 EN3PP: .000 EN3PP:

AVERAGE VALUES OF LAST & CYCLES

 014::329.057 00015:170.202 WMR(MP: 300.600 WMR(MP:-160.079 WMRT01: 103.610 EFF101: .436 MTFF1: .997 MEFF2: .995

 0416::329.057 00015:170.202 WMR(MP: 30.600 WMR(T: 17.601 ENTH: -1.550 WT01AL: 1773.604

 CM350H: .162 PMR4P: 15.076 F002: 50.000 WMR(T: 17.601 ENTH: -1.550 WT01AL: 1773.604

 CM350H: .162 PMR4P: 15.076 F002: 50.000 WMR(T: 17.601 ENTH: -1.550 WT01AL: 1773.604

 CM350H: .162 PMR4P: 1773.607 WD150: -10.203 WD151: 154.022 WT0151: 154.022 WMRLP: 6.427

 QETEMI: -870.03 BEEBP: 02.021 OWEATE: 30.060 WEATP: 30.603 GCOLM: .200 GCOOLP: 156.709 GCOMPM: -.0353 GCOMPP: 2.208

 QETEMI: -870.03 BEEBP: 02.021 OWEATE: 0.465 WD15PE: -16.080 WD151F: 540.070 WD151M:-105.000 COMPM: -.0353 GCOMPP: 2.208

 QETEMI: -870.03 BEEBP: 02.021 OWEATE: 0.465 WD15PE: -16.080 WD151F: 540.070 WD151M:-105.000 COMPM: -.0353 GCOMPP: 2.208

 QETEMI: -870.03 BEEBP: 02.021 OWEATE: 0.203 WD151F: 540.070 WD15M:-105.000 COMPM: -.0353 GCM0RD: P.003

 BECHBCL: -8157 GCMDD: 1.233 GCWDCW: 1.231 TBEEPA:1720.276 TGEMPA: 635.850 GSH11: 0.907

 AVERAGE TEMPERATURES OVER LAST CVCLC

 AVERAGE TEMPERATURES OVER LAST CVCLC

 TBECVC: 1700. 1740. 1655. 1548. 1397. 1209. 1022. 817. 641. 639. 638. 640.

 TAGETC: 1720. 1700. 1703. 1625. 1007. 1332. 1115. 929. 705. 633. 679. 632. 636.

 TAGETC: 1760. 1930. 1828. 1992. 1303. 1115. 929. 705. 540. 540. 540. 540.

# DEFINITIONS OF NAMELIST INPUT VARIABLES

COEFF	leakage coefficient for flow between buffer and compression spaces
FACT1, FACT2	convergence constants used in regenerator metal temperature convergence scheme
FIPCYC	number of iterations per cycle
IPRINT	number of iterations between printouts (if JIP=0)
IT MPS	<ol> <li>printout gas and metal control volume temper- ature at every iteration</li> <li>do not do the above</li> </ol>
JIP	>0, short-form printout =0, long-form printout
MWGAS	4, use helium working gas ≠4, use hydrogen working gas
NOCYC	number of engine cycles to be run
NOEND	number of cycle at which convergence scheme is turned off
NSTRT	number of cycle at which regenerator metal temper- ature convergence scheme is turned on
OMEGA	drive speed, Hz
P	initial pressure, lbf/in. <sup>2</sup> (N/m <sup>2</sup> ) (approximately equal to mean pressure for GPU)
P3	initial buffer space pressure, $lbf/in$ , (N/m <sup>2</sup> )
REALGS	1, use real-gas equation of state 0, use ideal-gas equation of state

<sup>&</sup>lt;sup>1</sup>Although both U.S. customary and SI units are given here, U.S. customary units are used in the program.

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RHCFAC	regenerator heat-transfer coefficient multiplication factor
TG	12 control volume interface gas temperatures, <sup>O</sup> R (K)
TGA	13 control volume gas temperatures, <sup>O</sup> R (K)
TM	13 metal boundary temperatures, <sup>O</sup> R (K)
T3	buffer space temperature (assumed constant), <sup>O</sup> R (K)

**Definitions of Output Variables** 

AVGWSP mean working-space pressure,  $lbf/in.^2$  (N/m<sup>2</sup>)

. .

EFFTOT efficiency, WRKTOT/QIN

-----

- ENTH net enthalpy flow from working space to buffer space over one cycle, ft-lbf (J)
- EN3PM rate of displacement of working-space gas, in. <sup>3</sup>/min (cm<sup>3</sup>/min)
- FREQ rotational frequency of crankshaft, Hz
- **PWRHP** indicated power WRKTOT/cycle period, hp (kW)
- QCNDCL heat conduction through cylinder, ft-lbf/cycle (J/cycle)
- QCNDCN heat conduction through insulation container, ft-lbf/cycle (J/cycle)
- **QCNDD** heat conduction through displacer, ft-lbf/cycle (J/cycle)
- **QCNDRI** heat conduction through regenerator casing, ft-lbf/cycle (J/cycle)
- QCNDRO heat conduction through regenerator casing, ft-lbf/cycle (J/cycle)
- QCOMPN heat from compression-space wall to gas, ft-lbf/cycle (J/cycle)
- QCOMPP heat from gas to compression-space wall, ft-lbf/cycle (J/cycle)

QCOOLN	heat from c	cooler to	gas,	ft-lbf/cycle	(J/cycle)
--------	-------------	-----------	------	--------------	-----------

- QCOOLP heat from gas to cooler, ft-lbf/cycle (J/cycle)
- QEXPN heat from metal wall to gas in expansion space, ft-lbf/cycle (J/cycle)
- QEXPP heat from gas to metal wall in expansion space, ft-lbf/cycle (J/cycle)
- QHEATN heat from heater to gas, ft-lbf/cycle (J/cycle)
- QHEATP heat from gas to heater, ft-lbf/cycle (J/cycle)
- QIN heat into gas in expansion space and heater tubes over one cycle, ft-lbf (J)
- QOUT heat out of gas in cooler tubes and compression space over one cycle, ft-lbf (J)
- QREGEN net heat flow from gas to regenerator metal over one cycle, ft-lbf (J)
- QREGN heat from regenerator metal to gas, ft-lbf/cycle (J/cycle)
- QREGP heat from gas to regenerator metal, ft-lbf/cycle (J/cycle)
- QSHTL shuttle heat loss, ft-lbf/cycle (J/cycle)
- REFF1 a measure of regreserator effectiveness
- **REFF2** another measure of regenerator effectiveness
- TG gas temperature at interface of two adjacent control volumes, <sup>O</sup>R (K)
- TGA working bulk gas temperature of a control volume,  ${}^{O}R$  (K)
- TGACYC cycle-time average temperature of TGA,  ${}^{O}R$  (K)
- TGCMPA as TGACYC in compression space
- TGCYC cycle-time average temperature of TG,  $^{O}R$  (K)
- **TGEXPA** as **TGCYC** in expansion space
- TM metal temperature of a metal control volume,  ${}^{O}R$  (K)

- TMCYC cycle-time average temperature of TM,  $^{O}R$  (K)
- UTOTAL internal energy content of working-space gas, ft-lbf (J)
- WL\_SP net work done on displacer piston by working-space gas, ft-lbf (J)
- WDISPN work done on gas by displacer, ft-lbf/cycle (J/cycle)
- WDISPP work done on displacer by gas, ft-lbf/cycle (J/cycle)
- WPISTP work done on piston by gas, ft-lbf/cycle (J/cycle)
- WPIST work done on power piston by working-space gas, ft-lbf (J)
- WPISTN work done on gas by piston, ft-lbf/cycle (J/cycle)
- WRKCMP work done by the gas in compression space over one cycle, ft-lbf (J)
- WRKEXP work done by the gas in expansion space over one cycle, ft-lbf (J)
- WRKLP power-piston work lost due to pressure drop from regenerator to compression space, ft-lbf/cycle (J/cycle)
- WRKLT \_\_\_work lost due to pressure drop over one cycle, ft-lbf (J)
- WRKTOT net work done by gas in working space over one cycle, WRKEXP + WRKCMP, ft-lbf (J)

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# TABLE I. - CHARACTERISTICS OF STIRLING ENGINE

# GROUND-POWER-UNIT SIMULATION RUN

Working fluid
Frequency, Hz
Average working-space pressure, N/m <sup>2</sup> (psi) 5.50×10 <sup>6</sup> (800)
Heater temperature (average gas temperature for
control volume 2, fig. 2), K ( <sup>O</sup> R)
Cooler temperature (cooler metal-wall temperature),
K ( <sup>0</sup> R)
Leakage flow coefficient (used in eq. (27)) 0.0001

# TABLE II. - PERFORMANCE PREDICTIONS FOR STIRLING ENGINE

#### **GROUND-POWER-UNIT SIMULATION RUN** ----

-----

Indicated power, kW (hp)
Indicated officiency
Indicated work per cycle, J (ft-lbf)
Work loss per cycle, due to pressure drop, J (ft-lbf) 11.7 (8.6)
Conduction heat loss per cycle, J (ft-lbf)
Shuttle heat loss per cycle, J (ft-lbf)


Figure 1. - Schematic of a single-cylinder Stirling engine with rhombic drive.



Figure 2. - Heat- and mass-transfer control volumes.



Figure 3. - Outline of calculation procedure.

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Figure 6. - Generalized control volume.



Figure 7. - Sample regenerator control volume and temperature profile.





Figure 9. - Schematic showing dimensions needed for calculating heat conduction. (Regenerator, housing, cylinder, and displacer are 310 stainless steel. Dimensions are in cm (in.).)



Figure 10. - Schematic showing geometric relations between piston positions and crankshaft angle.



Figure 11. - Assumed metal boundary temperatize of for sample run.







Figure 14. - Expansion- and compression-space pressures as functions of time.











🗧 🗤 re 19. - Expansion-space pressure-volume diagram.

















Figure 24. - Indicated power as a function of engine frequency for several average working-space pressures.







Figure 26. - Indicated power as a function of engine frequency for hydrogen and helium.

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Figure 27. - Indicated efficiency as a function of engine frequency for hydrogen and helium.



Figure 28. - Indicated efficiency as a function of indicated power (with engine frequency shown on curves).





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7. Authorist Roy Tew, Kent Jefferies, and	Devid Miao		8 Performing Organi E-9613	zation Report No
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15 Suplementery Notes Final report. Presared under	Interagency Age		-1011	
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