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Technical Memorandum 80608

**Documentation of the
Fourth Order Band Model**

**Eugenia Kalnay-Rivas
David Hoitsma**

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**Goddard Space Flight Center
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November 1979

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TABLE OF CONTENTS

	<u>Page</u>
Preface	i
I. Introduction	I-1
II. Primitive Equations of Motion	II-1
Derivation of the Equations at the Poles	II-3
Computation of the Horizontal Pressure Gradient as suggested by N. A. Phillips	II-7
III. Finite Difference Variables and Grid	III-1
Periodic Filtering of Short Waves	III-3
IV. Boundary Conditions	IV-1
V. Finite Difference Equations	V-1
The Zonal (U) Momentum Equation	V-1
The Meridional (v) Momentum Equation	V-2
The Thermodynamic Energy Equation	V-3
The Moisture Equation	V-4
The Pressure-Tendency Equation	V-5
VI. The Forecast Equations at the Poles	VI-1
Zonal (U) Momentum Equation (Poles)	VI-3
Meridional (V) Momentum Equation (Poles)	VI-3
The Thermodynamics Energy Equation (Poles)	VI-4
The Moisture Balance Equation (Poles)	VI-4
The Pressure Tendency Equation (Poles)	VI-5
The Vertical Velocity Equation (Poles)	VI-5
VII. Diagnostic Equations ($\phi, \dot{\sigma}, p$)	VII-1
VIII. The Time Differencing Scheme	VIII-1
IX. Documentation of the Code (Preliminary)	IX-1
X. Flow Charts	X-1
 Appendix A Reprints of Three Papers	 A-1
A Fourth-Order Forecasting Model	A-1
The 4th Order GISS Model of the Global Atmosphere	A-3
The Effect of Accuracy, Conservation and Filtering on Numerical Weather Forecasting	A-16
 Appendix B Program Listing	 B-1

Preface

We have decided to compile a preliminary documentation of the new GLAS Fourth Order General Circulation Model. The present documentation has not been subjected to a careful editing process; we hope that its possible usefulness will compensate for some of its defects. The model dynamics (COMP0, COMP1 and COMP2) is still undergoing minor improvements, especially in the time differencing scheme which we hope will improve its efficiency. The "physics" routine (COMP3) has not been documented because it is being thoroughly revised. The present version of COMP3, similar to the one used in the GLAS/GISS models (see the documentation by Tsang and Karn), with modifications introduced by Y. Sud (1979) is included in the code. Criticisms and suggestions for improvement will be reatly appreciated, since a final documentation will be prepared in 1980.

We are very grateful to all the people that have helped us generously. In particular, Dr. N. Rushfield had a major impact in the process of making the model operational. W. Connelly, D. Edelmann, D. Han, S. Breining, P. Anolick and M. Almeida were very helpful in the development of the model. The documentation was expertly and cheerfully typed by S. Mathis; D. Edelmann and D. Rosen have also cooperated in its compilation. We want to express our special gratitude toward Dr. Y. Sud, who offered us generously both his advice and his time in the development of the "physics" routine, and most especially to Dr. M. Halem without whose many useful suggestions, constant encouragement, and long patience, this work would not have been finished.

Eugenia Kalnay-Rivas

November 1979

I. Introduction

The band fourth order model is a GCM which uses quadratically conservative, fourth order horizontal space differences on an unstaggered grid and second order vertical space differences with a Matsuno (forward-backward) or a smooth leapfrog time scheme to solve the primitive equations of motion.

This program numerically solves these equations one latitude band at a time which greatly reduces the amount of computer core storage needed to run the program. It also uses the same variable names, order of computations, I/O, post-processing as the standard second order GCM. Appropriate modifications have been made for the fourth order differences and leapfrog scheme. (See the 1978 Goddard Modeling and Simulation Research Review for an overview of the fourth order band model.)

The main feature of this model is that fourth order approximations are used for all the horizontal derivatives. The derivative $\frac{\partial q}{\partial x}$ is approximated by

$$\frac{4}{3} \left(\frac{q(x+\Delta x) - q(x-\Delta x)}{2\Delta x} \right) - \frac{1}{3} \left(\frac{q(x+2\Delta x) - q(x-2\Delta x)}{4\Delta x} \right)$$

and the derivative $\frac{\partial T}{\partial x}$ (qT) by

$$\frac{4}{3} \left[\frac{(T(x)+T(x+\Delta x))(q(x)+q(x+\Delta x)) - (T(x)+T(x-\Delta x))(q(x)+q(x-\Delta x))}{4\Delta x} \right]$$

$$- \frac{1}{3} \left[\frac{(T(x)+T(x+2\Delta x))(q(x)+q(x+2\Delta x)) - (T(x)+T(x-2\Delta x))(q(x)+q(x-2\Delta x))}{8\Delta x} \right]$$

The second approximation is derived by averaging the flux qT to yield a conservative form of the dynamic equations. Note that if T is equal to 1 the second equation reduces to the first.

The primary variables are the horizontal components of the wind velocity, $\mathbf{w}=(u,v)$, the temperature, T , the specific humidity, q , and the shifted surface pressure, π , ($\pi=P_s - P_{top}$, $P_{top}=10$ mb).

The secondary variables are the geopotential, ϕ , the vertical wind velocity, $\dot{\sigma}$, and the pressure, p .

The following pages give the differential equations of motion for the GCM model with the initial and boundary conditions. This is followed by the equations with the corresponding fourth order approximations which use the same notation as the current second order model. A complete description of the primitive equations with the σ coordinate system is found in the Arakawa UCLA notes (1976).

II. Primitive Equations of Motion

1. & 2. Horizontal momentum equations

$$\mathbf{V} \frac{d\pi}{dt} + \pi \frac{d\mathbf{V}}{dt} = \frac{\partial \pi \mathbf{V}}{\partial t} + \nabla \cdot (\pi \mathbf{V} \mathbf{V}) + \frac{\partial}{\partial \sigma} (\pi \dot{\sigma} \mathbf{V}) \\ = -\pi \nabla \phi - \pi \sigma \frac{RT}{p} \quad \nabla \pi - (f + u \frac{\tan \phi}{a}) / kx \pi \mathbf{V} + \pi F$$

3. Continuity equation

$$(3.1) \quad \frac{\partial \pi}{\partial t} + \nabla \cdot (\pi \mathbf{V}) + \frac{\partial}{\partial \sigma} (\pi \dot{\sigma}) = 0, \quad \text{or}$$

$$(3.2) \quad \frac{\partial \pi}{\partial t} = - \int_0^1 \nabla \cdot (\pi \mathbf{V}) d\sigma = - \nabla \cdot \int_0^1 \pi \mathbf{V} d\sigma$$

4. Equation of state

$$\alpha = \frac{RT}{p}$$

5. First law of thermodynamics

$$\frac{\partial \pi T}{\partial t} + \nabla \cdot (\pi V T) + \frac{\partial}{\partial \sigma} (\pi \dot{\sigma} T) = \frac{\pi \omega \alpha}{C_p} + \frac{\pi Q}{C_p} \quad (\omega = \frac{dp}{dt})$$

From $\theta = T/p^k$, $p = p_T + \sigma \pi$, $\omega = \dot{\sigma} \pi + \dot{\pi} \sigma$, $\dot{\pi} = \frac{\partial \pi}{\partial t} + \mathbf{V} \cdot \nabla \pi$, $k = R/C_p$ we get

$$\frac{\partial \pi \dot{\sigma} T}{\partial \sigma} = p^k \frac{\partial \pi \dot{\sigma} \theta}{\partial \sigma} + \pi \frac{\dot{\sigma} \alpha \pi}{C_p} \quad \text{Replacing in 5,}$$

$$\frac{\partial \pi T}{\partial t} + \nabla \cdot (\pi V T) + p^k \frac{\partial \pi \dot{\sigma} \theta}{\partial \sigma} = \frac{\pi \sigma k T}{p} \left(\frac{\partial \pi}{\partial t} + \mathbf{V} \cdot \nabla \pi \right) + \frac{\pi Q}{C_p}$$

6. Humidity equation

$$\frac{\partial \pi q}{\partial t} + \nabla \cdot (\pi V q) = 0$$

7. Hydrostatic equation

$$\frac{\partial \phi}{\partial p} = -C_p \theta \quad (\text{from } \frac{\partial p}{\partial \phi} = -\rho = -\frac{1}{\alpha})$$

Of the variables $\pi, u, v, T, q, \phi, \alpha, \dot{\sigma}$ we update the 5 primary variables π, u, v, T , and q using equations 1, 2, 3.2, 5 and 6. From equations 3.1, 4, and 7 we can obtain ϕ, α , and $\dot{\sigma}$ which are our secondary variables. Note that $p = \sigma\pi + p_{top}$.

Sea level pressure (used only in the smoothing routine SMSHAP)

$$\text{Hydrostatic eq. } \Rightarrow \frac{\partial p}{\partial \phi} = -p = -\frac{1}{\alpha} = -\frac{p}{RT} \therefore \log\left(\frac{SLP}{p}\right) = -\int_{\phi_s}^0 \frac{d\phi}{RT}$$

$$\therefore SLP = p(\sigma=1) \exp\left(-\frac{\phi_s}{RT}\right)$$

DERIVATION OF THE EQUATIONS AT THE POLES

Consider the continuity equation

$$\frac{\partial \pi}{\partial t} + \nabla \cdot (\pi \mathbf{V}) + \frac{\partial \pi \sigma}{\partial \sigma} = 0$$

coupled with a conservation equation $\frac{dT}{dt} = S$ which can be expanded into

$$\frac{\partial \pi T}{\partial t} + \nabla \cdot (\pi V T) + \frac{\partial \pi \sigma T}{\partial \sigma} = \pi S$$

If we integrate this equation over a polar cap of radius $\Delta\phi$

$$\int_0^{2\pi} \int_{\frac{\pi}{2}}^{\frac{\pi}{2}-\Delta\phi} \frac{\partial \pi T}{\partial t} a^2 \cos\phi d\phi d\lambda = - \int_0^{2\pi} \int_{\frac{\pi}{2}}^{\frac{\pi}{2}-\Delta\phi} \nabla \cdot (\pi V T) a^2 \cos\phi d\phi d\lambda$$

$$- \int_0^{2\pi} \int_{\frac{\pi}{2}}^{\frac{\pi}{2}-\Delta\phi} \frac{\partial \pi \sigma T}{\partial \sigma} a^2 \cos\phi d\phi d\lambda - \int_0^{2\pi} \int_{\frac{\pi}{2}}^{\frac{\pi}{2}-\Delta\phi} \pi S a^2 \cos\phi d\phi d\lambda$$

and we assume the value of $\frac{\partial \pi T}{\partial t}$ to be approximately constant over the polar cap

$$\int_0^{2\pi} \int_{\frac{\pi}{2}}^{\frac{\pi}{2}-\Delta\phi} \frac{\partial \pi T}{\partial t} a^2 \cos\phi d\phi d\lambda \approx \left(\frac{\partial \pi T}{\partial t} \right)_{NP} \int_0^{2\pi} \int_{\frac{\pi}{2}}^{\frac{\pi}{2}-\Delta\phi} a^2 \cos\phi d\phi d\lambda$$

$$= 2\pi a^2 (1 - \cos \Delta\phi) \left(\frac{\partial \pi T}{\partial t} \right)_{NP}$$

The first term in the rhs is, using Gauss' theorem

$$- \int_0^{2\pi} \int_{\frac{\pi}{2}}^{\frac{\pi}{2}-\Delta\phi} \nabla \cdot (\pi V T) a^2 \cos\phi d\phi d\lambda = - \int_0^{2\pi} \pi v T a \sin\Delta\phi d\lambda$$

This can be approximated as

$$-\frac{2\pi}{IM} \sum_{i=1}^{IM} \pi_i v_i T_i a \sin \Delta\phi$$

The third term on the rhs is

$$\int_0^{2\pi} \int_{\pi/2}^{\pi/2 - \Delta\phi} \frac{\partial \pi \dot{\sigma} T}{\partial \sigma} a^2 \cos \phi d\phi d\lambda \approx 2\pi a^2 (1 - \cos \Delta\phi) \left(\frac{\partial \pi \dot{\sigma} T}{\partial \sigma} \right)_{NP}$$

and similarly with the source term.

From these equations we obtain

$$\left(\frac{\partial \pi T}{\partial t} \right)_{Pole} = -(-1)^m \frac{\cot \Delta\phi / 2}{a IM} \sum_{i=1}^{IM} (\pi_i v_i T_i) \frac{\pi}{2 - \Delta\phi} - \left(\frac{\partial \pi \dot{\sigma} T}{\partial \sigma} \right)_{Pole} + S$$

$$\text{since } \frac{2\pi a}{IM} \sin \Delta\phi / 2\pi a^2 (1 - \cos \Delta\phi) = \frac{2\sin \Delta\phi / 2 \cos \Delta\phi / 2}{IM a 2 \sin^2 \frac{\Delta\phi}{2}} = \frac{\cot \frac{\Delta\phi}{2}}{a IM}$$

This formulation is used in the continuity, momentum temperature and moisture equations. Note that the first term changes sign in the South Pole ($m=1$). In the momentum equations we make use of the transformation

$$u_i = -\sin \lambda u_i - (-1)^m \cos \lambda v_i$$

$$v_i = (-1)^m \cos \lambda u_i - \sin \lambda v_i$$

where $m=1$ for the South Pole and $m=2$ for the North Pole. u_i, v_i are the "cartesian" velocities at longitude λ_i , and u_i, v_i the corresponding spherical velocities.

The pressure gradient terms are computed making use of Green's

$$\text{Theorem: } \iint \frac{\partial Q}{\partial x} dx dy = \oint Q dy; \iint \frac{\partial P}{\partial g} dx dy = - \oint P dx$$

For example

$$\int_0^{2\pi} \int_{\pi/2}^{\pi/2 - \Delta\phi} \frac{\partial \phi}{\partial x} a^2 \cos \phi d\phi d\lambda = -\phi \Delta\phi (-\cos \lambda d\lambda)$$

$$\phi = \frac{\pi}{2} - \Delta\phi$$

$$\approx + \frac{a\Delta\phi 2\pi}{IM} \sum_{i=1}^{IM} \phi_i \cos \lambda_i$$

In the U-momentum equation we have then the following pressure terms

$$(\frac{\partial \pi U}{\partial t})_P = - \frac{\Delta\phi}{a(1-\cos\phi) IM} \sum_{i=1}^{IM} (\phi_i + (\frac{\sigma RT}{\rho})_P \pi_i) \cos \lambda_i$$

and similarly for πV .

In the model we have approximated $\Delta\phi \approx 2\sin\frac{\Delta\phi}{2}$

Then $\frac{\Delta\phi}{a(1-\cos\phi) IM} \approx \frac{1}{a \sin \frac{\Delta\phi}{2} IM}$

Based on this formulation we construct the fourth order scheme at the Poles by taking $\frac{4}{3}$ of the differences evaluated at $\Delta\phi$ from the Poles (as expanded here), minus $\frac{1}{3}$ of the differences at $2\Delta\phi$ from the Poles.

This formulation is not conservative at the Poles. However we have found that this has had no noticeable effect in the conservation of mass or energy in the model. In our shallow water experiments we studied a set of equations that were quadratically conservative, but inconsistent at the Pole, and another scheme analogous to the GFDL scheme, which is both quadratically conservative and consistent

at the Poles, but suffers from a serious truncation error near the Poles in the pressure gradient term. The scheme that we chose gave better results than the other two (Kalnay-Rivas, 1976).

Computation of the horizontal pressure gradient as suggested by
N. A. Phillips

(1) Let $\theta = \bar{\theta} + \theta'$, $\bar{\theta} = 280^{\circ}\text{K}/1000^k$ i.e. constant

(2) $\phi = \bar{\phi} + \phi'$, $k = R/Cp = .286$

$$\frac{\partial \bar{\phi}}{\partial p^k} = -Cp\bar{\theta} \quad \& \quad \bar{\phi} = \phi_0 - Cp\bar{\theta}p^k \quad \text{with } \phi_0 = Cp\bar{\theta}1000^k$$

(3) $T = \bar{T}(p) + T'$, $\bar{T}(p) = \bar{\theta}p^k$

Thus our new dependent variables are

$$\phi' = \phi + Cp\bar{\theta} (p^k - 1000^k)$$

$$T' = T - \bar{\theta}p^k$$

In this way $\pi(\nabla\phi + \frac{\sigma RT}{p} \nabla\pi)$, the pressure gradient in the momentum equations gets transformed into

$$(4) \quad \pi(\nabla_{\bar{\phi}} + \nabla_{\phi'} + \sigma R \frac{\bar{p}^k}{p} \nabla\pi + \frac{\sigma RT'}{p} \nabla\pi) \\ = \pi(\nabla_{\phi'} + \frac{\sigma RT'}{p} \nabla\pi) + \pi(\nabla_{\bar{\phi}} + \sigma R \frac{\bar{p}^k}{p} \nabla\pi)$$

But the second parenthesis is zero:

$$\nabla_{\bar{\phi}} + \sigma R \frac{\bar{p}^k}{p} \nabla\pi = -Cp\bar{\theta} \nabla p^k + R \frac{\bar{p}^k}{p} \nabla p = 0$$

In regions of steep orography, the second parenthesis in (4) is much larger than the first. When the horizontal pressure gradient terms are computed in their original form, the near cancellation of the two terms introduces large truncation errors. The procedure suggested by Phillips greatly reduces this truncation error. We have chosen a simpler definition of ϕ_0 than the one suggested by Phillips.

III. Finite Difference Variables and Grid

The notation used in fourth band model is the same as the standard GLAS(GISS) second order GCM except that we use a non-staggered horizontal grid. A complete description of the variables can be found in the TSANG-KARN documentation of the GISS 9 level model.

Let u_{ijk} , v_{ijk} , T_{ijk} , q_{ijk} , π_{ij} be the finite difference approximations to the primary variables u, v, T, q , and π at the mesh point $(i\Delta\lambda, j\Delta\phi, (k-\frac{1}{2})\Delta\sigma)$. Also the scaled variables π_u, π_v, \dots are approximated by $\pi u_{ijk}, \pi v_{ijk}, \dots$.

The finite difference equations also use the following geometric arrays:

$$DXP(j) = m_j = a \cos\phi_j \Delta\lambda, \quad DYU(j) = n_j = a \Delta\phi_j,$$

We use a factor of 12 in DXYP to make our scaled fourth order differences simpler.

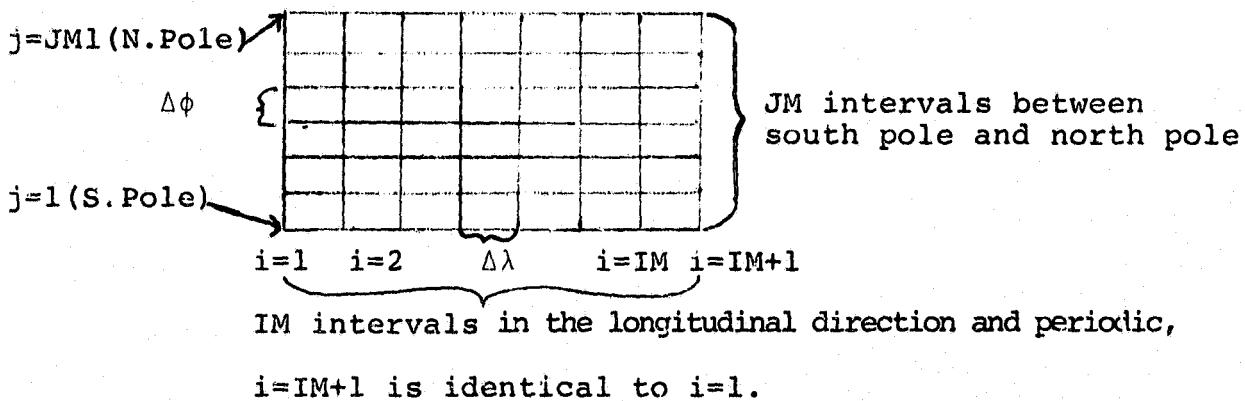
$$DXYP(j) = 12 \cdot m_j \cdot n_j, \quad \pi_{ij} = DXYP(j) \cdot \pi_{ij}, \quad U_{ijk} = n_j \pi_{ij} U_{ijk}$$

$$\dot{s}_{ijk} = \pi_{ij} \cdot \dot{\sigma}_{ijk}, \quad ADLDP = 12 \cdot a^* \Delta\lambda \Delta\phi, \quad V_{ijk}^* = m_j \pi_{ij} V_{ijk}$$

$$F_{ijk} = DXYP(j) f_j + ADLDP \cdot \sin\phi_j U_{ilj}$$

Horizontal Grid

The fourth order band model uses an unstaggered grid in the horizontal direction.



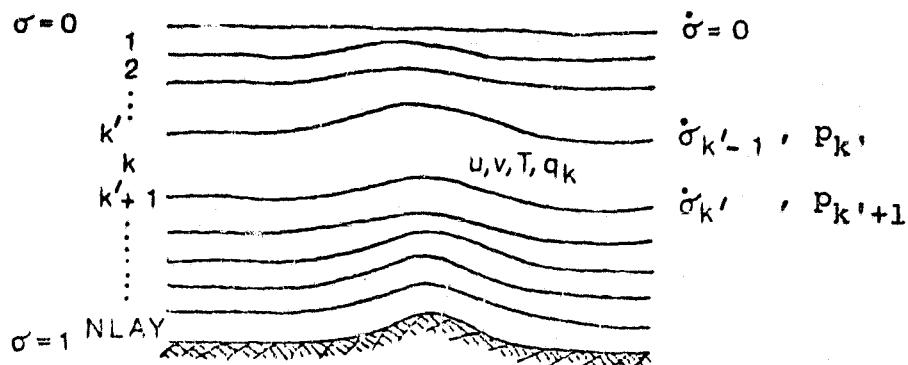
$$\Delta\lambda = \text{DLON} = \frac{2\pi}{IM} \quad \Delta\phi = \text{DLAT} = \frac{\pi}{JM}$$

$$\lambda_i = (i-1)\Delta\lambda - \pi = (i-1)5^\circ - 180^\circ \quad \phi_j = (j-1)\Delta\phi - \frac{\pi}{2} = (j-1)4^\circ - 90^\circ$$

$$JSP = 1 \quad JNP = JM1 = JM+1$$

Vertical Grid

The vertical grid is staggered; the values of all the variables u, v, T, q, π, \dots except $\dot{\sigma}$ are computed at the center of each layer. The values of $\dot{\sigma}$ are computed at the edges of the layers.



In the case of uniform vertical resolution and $NLAY=9$ vertical layers,

$$\sigma_k = \text{SIG}(K) = \frac{k-1}{9}(0, 1/9, \dots, 1)$$

$$\sigma_{k'} = \text{SIGE}(K) = \frac{2k-1}{18} = (\frac{1}{18}, \dots, \frac{17}{18})$$

$$\text{and } \Delta\sigma = 1/9 \dots$$

$\dot{\sigma}_{ijk}$ and its scaled version \dot{s}_{ijk} are defined at the eight interior edges, i.e. for σ_k' with $k=1$ to 8 since $\dot{\sigma}(0)=\dot{\sigma}(1)=0$ from the boundary conditions. The pressure $p_{k'}=\pi\sigma_{k'}+p_{TOP}$ is defined at the same level as $\dot{\sigma}_{k'-1}$. Note for level k we need \dot{s}_{ijk} and \dot{s}_{ijk-1} to form the second order vertical differences:

$$\dot{s}_{ijk} (v_{ijk} + v_{ijk+1}) - \dot{s}_{ijk-1} (v_{ijk} + v_{ijk-1})$$

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III-2 Periodic Filtering of Short Waves

An integral part of the numerical scheme is the periodic application (every ISMTH steps, generally 2 hours) of a 16th order Shapiro filter. This has the effect of removing waves shorter than $4\Delta x$, which are not resolved in the model, while waves longer than $4\Delta x$, which are accurately computed by the difference scheme, are not affected by the filter (Kalnay-Rivas and Hoitsma, 1979).

The filter is applied to an array q_j in the following way:

$$\text{Let } d_+(q_j) = q_{j+1} - q_j, \quad d_-(q_j) = q_j - q_{j-1}$$

Then a Shapiro filter of order $2N$ is given by

$$\bar{q}_j = q_j - (-1)^N (d_+ d_-)^N q_j$$

The response of the filter applied to a wave of the form

$$q_j = Q \exp(i \frac{2\pi}{L} \Delta x j) \text{ is}$$

$$\bar{q}_j = (1 - \sin^2 N \frac{\pi \Delta x}{L}) q_j$$

The 2-dimensional filter is applied as a product of 1-dimensional filters (first in longitude, then in latitude). In latitude we filter the fields on great circles formed by meridians of longitude λ and $\lambda + \pi$, where $0 \leq \lambda < \pi$. We are presently filtering only potential temperature and sea level pressure. These fields were chosen because they are not very affected by orography. Winds are not currently filtered, because the adjustment between mass and velocity fields does not allow the development of short waves in the winds alone. However, in the tropics, where the adjustment of winds to the mass field is minimal, the winds are somewhat noisy, and we may opt to filter them too.

IV. Boundary Conditions

Periodicity in the Zonal (East-West) direction

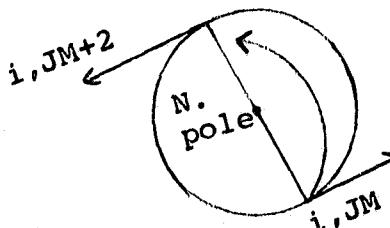
$$\pi_{IM+mj} = \pi_{mj} \quad m=1, 2, 3, \dots, \quad j=2, \dots, JM$$

$$Q_{IM+mjk} = Q_{mjk} \quad m=1, 2, 3, \dots, \quad j=2, \dots, JM, \quad k=1, \dots, NLAY$$

for $Q=u, v, T, q, \phi, \delta, \pi u, \pi v, \dots$

Boundary conditions at the north and south poles. Define the array

INDEX as follows:



$$\text{INDEX}(i) = i + \frac{IM}{2} \quad i=1, 2, \dots, \frac{IM}{2}$$

$$\text{INDEX}(i - \frac{IM}{2}) = i \quad i = \frac{IM}{2} + 1, \dots, IM$$

$$\text{i.e., INDEX: } \frac{IM}{2} + 1, \frac{IM}{2} + 2, \dots, IM, 1, 2, \dots, \frac{IM}{2}$$

Then we can define

$$\pi_{iJM+2} = \pi_{\text{INDEX}(i)JM} \text{ for the points needed "beyond" the North Pole,}$$

$$\text{and } \pi_{i0} = \pi_{\text{INDEX}(i)2} \text{ for the points "beyond" the South Pole}$$

and similarly for T, q, ϕ .

For the horizontal velocity $V=(u, v)$ we have

$$v_{iJM+2k} = -v_{iJMK}$$

$$v_{i0k} = -v_{i2k}$$

V. Finite Difference Equations

THE ZONAL (U) MOMENTUM EQUATION

$$\frac{\partial \pi u}{\partial t} = - \frac{1}{a \cos \phi} \left[\frac{\partial (\pi u \cdot u)}{\partial \lambda} + \frac{\partial (\pi v \cos \phi \cdot u)}{\partial \phi} \right] - \frac{\partial (\pi \dot{u})}{\partial \sigma}$$

$$- \frac{\pi}{a \cos \phi} \left[\frac{\partial \phi}{\partial \lambda} + \frac{\sigma R T}{p} \frac{\partial \pi}{\partial \lambda} \right] + (f + \frac{u \tan \phi}{a}) \pi v + \pi F_x$$

$\frac{\partial \pi U_{ijk}}{\partial t}$ = $\left\{ \begin{array}{l} \text{COMPl: HA: } \underbrace{PU1_{i-1/2j}}_{(U_{ijk}^* + U_{i-1jk}^*) (U_{ijk} + U_{i-1jk})} - \underbrace{PU1_{i+1/2}}_{(U_{ijk}^* + U_{i+1jk}^*) (U_{ijk} + U_{i+1jk})} \\ 4 * [(\underbrace{U_{ijk}^* + U_{i-1jk}^*}_{PU2_{i-1}}) (U_{ijk} + U_{i-2jk}) - (\underbrace{U_{ijk}^* + U_{i+1jk}^*}_{PU2_{i+1}}) (U_{ijk} + U_{i+2jk})] \\ - .5 [(\underbrace{U_{ijk}^* + U_{i-2jk}^*}_{PV1}) (U_{ijk} + U_{i-2jk}) - (\underbrace{U_{ijk}^* + U_{i+2jk}^*}_{PV2}) (U_{ijk} + U_{i+2jk})] \\ + 4 * [(\underbrace{V_{ijk}^* + V_{ij-1k}^*}_{PV1}) (U_{ijk} + U_{ij-1k}) - (V_{ijk}^* + V_{ij+1k}^*) (U_{ijk} + U_{ij+1k})] \\ - .5 * [(\underbrace{V_{ijk}^* + V_{ij-2k}^*}_{PV2}) (U_{ijk} + U_{ij-2k}) - (\underbrace{V_{ijk}^* + V_{ij+2k}^*}_{PV2}) (U_{ijk} + U_{ij+2k})] \\ \text{VA: } + .5 * [\dot{s}_{ijk-1} (U_{ijk} + U_{ijk-1}) - \dot{s}_{ijk} (U_{ijk} + U_{ijk+1})] / \Delta \sigma_k \\ \text{COMP2: PG: } + (\pi_{ij} * n_j * \{ 8 * [\phi_{i-1jk}^* - \phi_{i+1jk}^* + \frac{\sigma_k R T'_{ijk}}{p_k} (\pi_{i-1j} - \pi_{i+1j})] + \\ [\phi_{i+2jk}^* - \phi_{i-2jk}^* + \frac{\sigma_k R T'_{ijk}}{p_k} (\pi_{i+2j} - \pi_{i-2j})] \}) \\ \text{C: COMP3 } + F_{ijk} * \pi_{ij} * V_{ijk} + (\pi F_x) \end{array} \right\}$

Note: COMPl, COMP2, COMP3 are the names of the three subroutines where the different terms are computed. HA: Horizontal advection terms. VA: Vertical advection terms. PG: Pressure gradient terms. C: Coriolis term.

Also note that PV2 is set equal to zero for j=0 and j=JM, i.e., there is no transport of mass across the poles.

THE MERIDIONAL (V) MOMENTUM EQUATION

$$\frac{\partial \pi V}{\partial t} = - \frac{1}{a \cos \phi} \left[\frac{\partial (\pi u \cdot v)}{\partial \lambda} + \frac{\partial (\pi v \cos \phi v)}{\partial \phi} \right] - \frac{\partial \pi \dot{v}}{\partial \sigma}$$

$$- \frac{\pi}{a} \left[\frac{\partial \phi}{\partial \phi} + \frac{\sigma R T}{p} \frac{\partial \pi}{\partial \phi} \right] - \left(f + \frac{u \tan \phi}{a} \right) \pi u + \pi F_y$$

COMP1: HA:

$$\frac{\partial \pi V_{ijk}}{\partial t} = \left\{ 4 \cdot * [(U_{ijk}^* + U_{i-1jk}^*) (V_{ijk} + V_{i-1jk}) - (U_{ijk}^* + U_{i+1jk}^*) (V_{ijk} + V_{i+1jk}) \right.$$

$$- .5 [(U_{ijk}^* + U_{i-2jk}^*) (V_{ijk} + V_{i-2jk}) - (U_{ijk}^* + U_{i+2jk}^*) (V_{ijk} + V_{i+2jk})]$$

$$+ 4 \cdot * [(V_{ijk}^* + V_{ij-1k}^*) (V_{ijk} + V_{ij-1k}) - (V_{ijk}^* + V_{ij+1k}^*) (V_{ijk} + V_{ij+1k})]$$

$$- .5 * [(V_{ijk}^* + V_{ij+2k}^*) (V_{ijk} + V_{ij+2k}) - (V_{ijk}^* + V_{ij+2k}^*) (V_{ijk} + V_{ij+2k})]$$

VA:

$$+.5 * [S_{ijk-1} (V_{ijk} + V_{ijk-1}) - S_{ijk} (V_{ijk} + V_{ijk+1})] / \Delta \sigma_k \}$$

COMP2: P:

$$+(\pi_{ij}^* m_j * \{ 8 \cdot * [\phi_{ij-1k}^* - \phi_{ij+1k}^* + \frac{\sigma_k R T_{ijk}^*}{p_k} (\pi_{ij-1} - \pi_{ij+1})]$$

$$+ [\phi_{ij+2k}^* - \phi_{ij-2k}^* + \frac{\sigma_k R T_{ijk}^*}{p_k} (\pi_{ij+2} - \pi_{ij-2})] \})$$

C: COMP3:
 $-F_{ijk} * \pi_{ij} * U_{ijk} + (\pi F_y)$

THE THERMODYNAMIC ENERGY EQUATION

$$\frac{\partial \pi T}{\partial t} = -\frac{1}{a \cos \phi} \left[\frac{\partial \pi U T}{\partial \lambda} + \frac{\partial \pi V \cos \phi \cdot T}{\partial \phi} \right] - p^k \frac{\partial \pi \dot{\sigma} T / p^k}{\partial \sigma}$$

$$+ \frac{\pi \sigma K T}{p} \left(\frac{\partial \pi}{\partial t} + \frac{U}{a \cos \phi} \frac{\partial \pi}{\partial \lambda} + \frac{V}{a} \frac{\partial \pi}{\partial \phi} \right) + \frac{\pi Q}{C_p}$$

COMP1: HA:

$$\frac{\partial \Pi T_{ijk}}{\partial t} = \{ 4 * [(U_{ijk}^* + U_{i-1jk}^*) (T_{ijk} + T_{i-1jk}) - (U_{ijk}^* + U_{i+1jk}^*) (T_{ijk} + T_{i+1jk})]$$

$$- .5 * [(U_{ijk}^* + U_{i-2jk}^*) (T_{ijk} + T_{i-2jk}) - (U_{ijk}^* + U_{i+2jk}^*) (T_{ijk} + T_{i+2jk})]$$

$$+ 4 * [(V_{ijk}^* + V_{ij-1k}^*) (T_{ijk} + T_{ij-1k}) - (V_{ijk}^* + V_{ij+1k}^*) (T_{ijk} + T_{ij+1k})]$$

$$- .5 * [(V_{ijk}^* + V_{ij-2k}^*) (T_{ijk} + T_{ij-2k}) - (V_{ijk}^* + V_{ij+2k}^*) (T_{ijk} + T_{ij+2k})]$$

VA:

$$+ .5 p_k^k [\dot{s}_{ijk-1} \left(\frac{T_{ijk}}{p_{ijk}^k} + \frac{T_{ijk-1}}{p_{ijk-1}^k} \right) - \dot{s}_{ijk} \left(\frac{T_{ijk}}{p_{ijk}^k} + \frac{T_{ijk+1}}{p_{ijk+1}^k} \right)] / \Delta \sigma_k }$$

COMP2:

$$(+ \frac{\sigma_k K T_{ijk}}{p_{ijk}} [\pi_{ij} \frac{\partial \pi}{\partial t} + U_{ijk}^* \{ 8 * [\pi_{i+1j} - \pi_{i-1j}] + \pi_{i-2j} - \pi_{i+2j} \}]$$

$$+ V_{ijk}^* \{ 8 * [\pi_{ij+1} - \pi_{ij-1}] + \pi_{ij-2} - \pi_{ij+2} \}])$$

COMP3:

$$+ (\frac{\pi Q_{ijk}}{C_p})$$

THE MOISTURE EQUATION

$$\frac{\partial \pi q}{\partial t} = - \frac{1}{a \cos \phi} \left[\frac{\partial \pi U \cdot q}{\partial \lambda} + \frac{\partial \pi V \cos \phi \cdot q}{\partial \phi} \right] - \frac{\partial \pi \delta q}{\pi \sigma} + \pi (E - C)$$

COMP1: HA

$$\begin{aligned} \frac{\partial \Pi q_{ijk}}{\partial t} = & \{ 4.*[(U^*_{ijk} + U^*_{i-1jk}) (q_{ijk} + q_{i-1jk}) - (U^*_{ijk} + U^*_{i+1jk}) (q_{ijk} + q_{i+1jk})] \\ & -.5*[(U^*_{ijk} + U^*_{i+2jk}) (q_{ijk} + q_{i+2jk}) - (U^*_{ijk} + U^*_{i+2jk}) (q_{ijk} + q_{i+2jk})] \\ & +4.*[(V^*_{ijk} + V^*_{ij-1k}) (q_{ijk} + q_{ij-1k}) - (V^*_{ijk} + V^*_{ij+1k}) (q_{ijk} + q_{ij+1k})] \\ & -.5*[(V^*_{ijk} + V^*_{ij-2k}) (q_{ijk} + q_{ij-2k}) - (V^*_{ijk} + V^*_{ij+2k}) (q_{ijk} + q_{ij+2k})] \\ & +.5*[\dot{s}_{ijk-1} (q_{ijk} + q_{ijk-1}) - \dot{s}_{ijk} (q_{ijk} + q_{ijk+1})]/\Delta \sigma_k \} \end{aligned}$$

COMP3:

$$+\Pi(E_{ijk} - C_{ijk})$$

Note: The current transport scheme for the moisture field is being modified.

THE PRESSURE-TENDENCY EQUATION

$$\frac{\partial \pi}{\partial t} = - \sum_{l=1}^L \frac{(\Delta \sigma)_l}{a \cos \phi} \left[\frac{\partial \pi u}{\partial \lambda} + \frac{\partial \pi v \cos \phi}{\partial \phi} \right]$$

COMPL:

$$\begin{aligned} \text{CONV}_{ilj} &= \Delta \sigma_l \{ 8 \cdot * (U_{i-1jl}^* - U_{i+1jl}^*) + U_{i+2jl}^* - U_{i-2jl}^* \\ &\quad + 8 \cdot * (V_{ij-1l}^* - V_{ij+1l}^*) + V_{ij+2l}^* - V_{ij-2l}^* \} \end{aligned}$$

COMPL:

$$\frac{\partial \Pi_{ij}}{\partial t} = \left(\sum_{l=1}^L \text{CONV}_{ilj} \right)$$

THE VERTICAL VELOCITY EQUATION

$$\frac{\partial \pi}{\partial t} = - \frac{1}{a \cos \phi} \left[\frac{\partial \pi u}{\partial \lambda} + \frac{\partial \pi v \cos \phi}{\partial \phi} \right] - \frac{\partial}{\partial \sigma} (\pi \dot{\sigma})$$

Thus

$$\Delta \sigma_k \frac{\partial \Pi}{\partial t} = \text{CONV}_{ikj} - \dot{s}_{ijk}$$

giving:

COMPL:

$$\dot{s}_{ijk} = \{ \dot{s}_{ijk-1} + \text{CONV}_{ikj} - \Delta \sigma_k \frac{\partial \Pi}{\partial T} \}$$

VI. The Forecast Equations at the Poles

The fourth order band model uses a spherical cap at the poles, and the finite difference approximations to the equations of motion must be derived for this spherical region. Stereographic projection is used to give us a well-defined velocity vector at the poles.

From trigonometry, (Fig. VIa) if the vector (U, V) in X-Y coordinates is represented by (U', V') in $X'-Y'$ coordinates where the prime coordinate axes are rotated by an angle λ then,

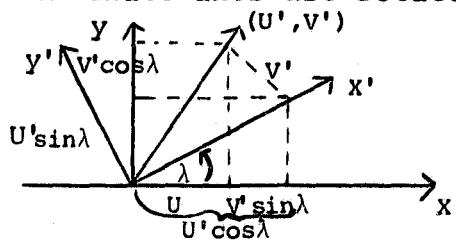


Fig. VIa

$$(1) \quad U = U' \cos \lambda - V' \sin \lambda$$

$$(2) \quad V = U' \sin \lambda + V' \cos \lambda$$

We want to interpret "polar stereographic" velocities (U_{NP}, V_{NP}) also as "spherical" velocities $(U, V)_\lambda$, as we approach the

North Pole along a meridian of longitude λ .

From Fig. VIb, which shows a unit vector in both coordinate systems, we see that, at the North Pole, spherical coordinates are rotated by an angle $(\frac{\pi}{2} + \lambda)$ with respect to the polar stereographic coordinates. Therefore,

$$U_{NP} = U \cos(\lambda + \frac{\pi}{2}) - V \sin(\lambda + \frac{\pi}{2})$$

$$V_{NP} = U \sin(\lambda + \frac{\pi}{2}) + V \cos(\lambda + \frac{\pi}{2})$$

or

$$(3) \quad \boxed{U_{NP} = -U \sin \lambda - V \cos \lambda}$$

$$V_{NP} = U \cos \lambda - V \sin \lambda$$

Similarly, for the South Pole:

$$(4) \quad \boxed{U_{SP} = -U \sin \lambda + V \cos \lambda}$$

$$V_{SP} = -U \cos \lambda - V \sin \lambda$$

also,

$$(5) \quad \boxed{U = -U_{NP} \sin \lambda + V_{NP} \cos \lambda}$$

$$V = -U_{NP} \cos \lambda - V_{NP} \sin \lambda$$

$$(6) \quad \boxed{U = -U_{SP} \sin \lambda - V_{SP} \cos \lambda}$$

$$V = U_{SP} \cos \lambda - V_{SP} \sin \lambda$$

Fig. VIb

The initial values for U_{NPk} , V_{NPk} , U_{SPk} , V_{SPk} are obtained from equations 3 and 4 by averaging in the zonal direction on the line of latitude $j=45$ for the north pole and $j=2$ for the south pole. In the forecast stereographic velocities are advected and transformed back into spherical velocities after each time step by equations 5 and 6.

In the following equation we will denote the polar velocities by $VP_{k,m}$, $VP_{k,m}$ and the temperature and other variables in a similar way, $TP_{k,m}$, $\pi P_{k,m}$, ... where $m=1$ for the south pole and $m=2$ for the north pole. The following constants are used,

$$COEFL=(-1)^m \quad COEF2=-COEFL \quad RADIM=3 \cdot a \cdot IM$$

$$CON1=4COT(.5\Delta\phi)/RADIM$$

$$CON2=-COT(\Delta\phi)/RADIM$$

$$CON3=4DT/(RADIM*SIN(.5\Delta\phi))$$

$$CON4=DT/(RADIM*SIN(\Delta\phi))$$

$$JPOL(K,M)=\begin{pmatrix} 2 & JM \\ 3 & JM-1 \end{pmatrix}$$

$r=JPOL(1,m)$ =first interior value of j (2 for the S. Pole, JM for the N. Pole)

$s=JPOL(2,m)$ =second interior value of j (3 for the S. Pole, JM-1 for the N. Pole).

ZONAL (U) MOMENTUM EQUATION (POLES)

COMP1:

$$\frac{\partial \pi UP_{k,m}}{\partial t} = \{ COEF1 * [CON1 * \sum_{i=1}^{IM} -\pi_{ir} v_{irk} (U_{irk} \sin \lambda_i + COEF1 * v_{irk} \cos \lambda_i) + CON2 * \sum_{i=1}^{IM} -\pi_{is} v_{isk} (U_{isk} \sin \lambda_i + COEF1 * v_{isk} \cos \lambda_i)] + .5 [\dot{SP}_{k-1} (UP_k + UP_{k-1}) - \dot{SP}_k (UP_k + UP_{k+1})] / \Delta \sigma_k \}$$

COMP2:

$$+ \pi P_m [-\frac{CON3}{DT} * \sum_{i=1}^{IM} (\phi'_{irk} + \frac{\sigma_k RTP'_k}{pP_k} \pi_{ir}) \cos \lambda_i + CON4 * \frac{1}{DT} \sum_{i=1}^{IM} (\phi'_{isk} + \frac{\sigma_k RTP'_k}{pP_k} \pi_{is}) \cos \lambda_i]$$

COMP3:

$$+ f_m \pi P_m \cdot VP_{k,m} + (\pi P_m \cdot FP_{k,m})$$

MERIDIONAL (V) MOMENTUM EQUATION (POLES)

COMP1:

$$\frac{\partial \pi VP_{k,m}}{\partial t} = \{ COEF1 * [CON1 * \sum_{i=1}^{IM} -\pi_{ir} v_{irk} (COEF2 * U_{irk} * \cos \lambda_i + v_{irk} \sin \lambda_i) + CON2 * \sum_{i=1}^{IM} -\pi_{is} v_{isk} (COEF2 * U_{isk} * \cos \lambda_i + v_{isk} \sin \lambda_i)] + .5 [\dot{SP}_{k-1} (VP_k + VP_{k-1}) - \dot{SP}_k (VP_k + VP_{k+1})] / \Delta \sigma_k \}$$

COMP2:

$$+ \pi P_m \cdot [-\frac{CON3}{DT} * \sum_{i=1}^{IM} (\phi'_{irk} + \frac{\sigma_k RTP'_k}{pP_k} \pi_{ir}) \sin \lambda_i + \frac{CON4}{DT} * \sum_{i=1}^{IM} (\phi'_{isk} + \frac{\sigma_k RTP'_k}{pP_k} \pi_{is}) \sin \lambda_i]$$

COMP3:

$$- f_m \pi P_m \cdot UP_{k,m} + (\pi P_m \cdot SP_{k,m})$$

THE THERMODYNAMICS ENERGY EQUATION (POLES)

COMP1:

$$\frac{\partial \pi T P_{k,m}}{\partial t} = \{ COEF1 * (CON1 * \sum_{i=1}^{IM} \pi_{ir} V_{irk} T_{irk} + CON2 * \sum_{i=1}^{IM} \pi_{is} V_{isk} T_{isk}) \\ + .5 p P_{k,m}^k * [\dot{S} P_{k-1,m} (\frac{T P_{k,m}}{P P_{k,m}^k} + \frac{T P_{k-1,m}}{P P_{k-1,m}^k}) \\ - \dot{S} P_{k,m} (\frac{T P_{k,m}}{P P_{k,m}^k} + \frac{T P_{k+1,m}}{P P_{k+1,m}^k})] / \Delta \sigma_k \}$$

COMP2:

$$+ (\frac{\pi P_m \sigma_k K T P_{k,m}}{P P_{k,m}} \{ \frac{\partial \pi P_m}{\partial t} + CON5 * \sum_{i=1}^{IM} [(COEF1 * U P_{k,m} \cos \lambda_i + V P_{k,m} \sin \lambda_i) * \\ (8 \pi_{ir} - \pi_{is})] \})$$

COMP3:

$$+ (\frac{\pi P_m}{C_p} Q P_k)$$

THE MOISTURE BALANCE EQUATION (POLES)

COMP1:

$$\frac{\partial \pi q P_{k,m}}{\partial t} = \{ COEF1 * (CON1 * \sum_{i=1}^{IM} \pi_{ir} V_{irk} q_{irk} + CON2 * \sum_{i=1}^{IM} \pi_{is} V_{isk} q_{isk}) \\ + .5 [\dot{S} P_{k-1,m} (q P_{k,m} + q P_{k-1,m}) - \dot{S} P_{k,m} (q P_{k,m} + q P_{k+1,m})] / \Delta \sigma_k \}$$

COMP3:

$$+ (\pi P_m * E P_k)$$

THE PRESSURE TENDENCY EQUATION (POLES)

$$\text{CONVPL}_{k,m} = \text{COEF1} * (\text{CON1} * \sum_{i=1}^{\text{IM}} \pi_{ir} v_{irk} + \text{CON2} * \sum_{i=1}^{\text{IM}} \pi_{is} v_{isk}) \Delta \sigma_k$$

$$\frac{\partial \pi P_m}{\partial t} = \sum_{k=1}^{\text{NLAY}} \text{CONVPL}_{k,m}$$

THE VERTICAL VELOCITY EQUATION (POLES)

$$\dot{s}_p_{k,m} = \dot{s}_p_{k-1,m} + \text{CONVPL}_k - \Delta \sigma_k \frac{\partial \pi P_m}{\partial t}$$

VII. Diagnostic Equations ($\phi, \dot{\sigma}, p$)

Once the updated values of πU , πV , πT , πq are found we unscale:

$$U_{ijk}^{n+1} = \pi U_{ijk}^{n+1} / \pi_{ij}^{n+1} \quad \text{for all } i,j,k.$$

Similarly for V, T, q . We also filter the fields near the poles to prevent linear instability (see subroutine AVRX). $\dot{\sigma}$ is obtained from S by unscaling also.

We determine from π_{ij}^{n+1} and σ_k , p_{ijk}^{n+1}

$$p_{ijk}^{n+1} = \sigma_k \pi_{ij}^{n+1} + p_{TOP} \quad p_{TOP} = \text{constant.}$$

ϕ_s is the surface geopotential (a function only of latitude and longitude)

For the Phillips geopotential we define $(p)^k$ at the center of the layer in the following way:

$$(p)_{ijk}^k = \frac{p_{ijk+1}' - p_{ijk}'}{(k+1)(p_{ijk'+1} - p_{ijk'})} \quad (p^k = \frac{1}{k+1} \frac{\partial p^{k+1}}{\partial p}) \\ k=1, 2, \dots, NLAY$$

where

$$p_{ijk'}^{k+1} = (\text{SIGE}(k) * \pi_{ij} + p_{TOP})^{k+1} \quad (\text{SIGE}(k) = \sigma_k'), \text{ i.e.}$$

p^{k+1} is obtained by exponentiation and $(p)^k$ by differences.

The following equations represent the geopotential calculations used in the old fourth order model.

Let

$$c_{ijk} = \frac{\pi_{ij} \sigma_k R \Delta \sigma_k}{p_{ijk}} - \frac{C_p}{2} \left[\sigma_k \left(\frac{p_{ijk+1}^k}{p_{ijk}^k} - 1 \right) + \sigma_{k-1} \left(1 - \frac{p_{ijk-1}^k}{p_{ijk}^k} \right) \right]$$

for $k=1, \dots, NLAY$

with

$$p_{ij0}^k = p_{ij1}^k \text{ and } p_{ijNLAY+1}^k = p_{ijNLAY}^k$$

An optimized version of c_{ijk} is:

$$c_{ijk} = \frac{\pi_{ij} \sigma_k R \Delta \sigma_k}{p_{ijk}} - \frac{.5 C_p}{p_{ijk}^k} \left\{ \sigma_k (p_{ijk+1}^k - p_{ijk}^k) + \sigma_{k-1} (p_{ijk+1}^k - p_{ijk-1}^k) \right\}$$

Rather than compute ϕ and then subtract $\bar{\phi}$ we do everything at once:

$$(1) \quad \phi'_{ijNLAY} = \phi'_s - CPTH * (PSKAPA - p_{ijNLAY}^k) + \sum_{\ell=1}^{NLAY} c_{ij\ell} T_{ij\ell}$$

$$(2) \quad \phi'_{ij\ell} = \phi'_{ij\ell+1} + \frac{C_p}{2} * (p_{ij\ell+1}^k - p_{ijk}^k) \left(\frac{T_{ijk}}{p_{ijk}^k} + \frac{T_{ijk+1}}{p_{ijk+1}^k} - 2\bar{\phi} \right)$$

where

$$CPTH = C_p \cdot \bar{\phi} \quad PSKAPA = 1000^k = p_s^k.$$

VIII. The Time Differencing Scheme

The fourth order band model has the option of using the Matsuno time scheme or the smooth leapfrog scheme (see MWR-Vol 100 (487-490) R. Asselin).

Let Q^n represent a typical variable that is to be updated to time $n+1$, and let $D(Q^n)$ represent the nonlinear space differences. The Matsuno (Euler-backward) scheme is as follows:

$$\begin{aligned}\tilde{Q} &= Q^n + \Delta t D(Q^n) \\ Q^{n+1} &= Q^n + \Delta t D(\tilde{Q})\end{aligned}$$

The standard leapfrog scheme is given by

$$(1) \quad \frac{Q^{n+1} - Q^{n-1}}{2\Delta t} = D(Q^n)$$

For the smooth leapfrog scheme we replace Q^{n-1} by \bar{Q}^{n-1}

$$(2) \quad Q^{n+1} = \bar{Q}^{n-1} + 2\Delta t D(Q^n)$$

with

$$(3) \quad \bar{Q}^n = (1-\nu)Q^n + .5\nu(\bar{Q}^{n-1} + Q^{n+1})$$

Equation (3) represents a simple time filter except \bar{Q}^{n-1} is used instead of Q^{n-1} in order to save core storage. The above equations (2) and (3) represent the order in which the smooth leapfrog scheme is evaluated. For $n=1$ we define $\bar{Q}^0 = Q^0$ then we update in equation (2) followed by the filtering in equation (3) which is needed for the next time step.

The smoothing step introduces dissipation with respect to time, controlled explicitly by the parameter ν , as compared to the implicit dissipation in the Matsuno scheme. The amplification factor can be found in the paper by Asselin.

A further modification must be made to the smooth leapfrog scheme when source terms are included. Essentially the idea is that we must include the source term effect over two steps rather than one. If we do not do this, then the source effects (COMP3) are included only in every other step which will introduce large discretization errors. (For details see the attached report, Appendix B.)

If the source terms are called every NCOMP3 steps, then for step n=NCOMP3

$$Q_*^n = \bar{Q}^{n-2} + 2\Delta t D(Q^{n-1})$$

$$\bar{Q}_*^{n-1} = (1-\nu) Q^{n-1} + .5\nu(\bar{Q}^{n-2} + Q^n)$$

Then compute the source terms S^n and include in both steps n and n-1,

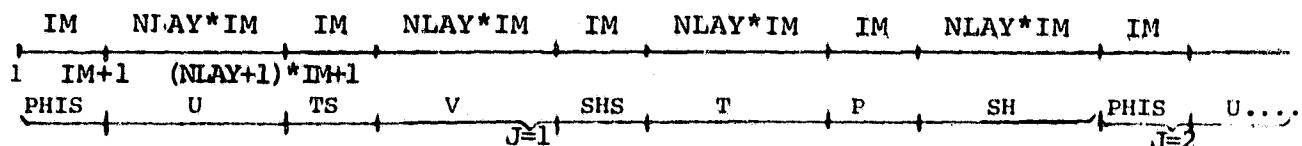
$$Q^n = Q_*^n + NCOMP3 \cdot \Delta t S^n$$

$$\bar{Q}^{n-1} = \bar{Q}_*^{n-1} + NCOMP3 \cdot \Delta t S^n$$

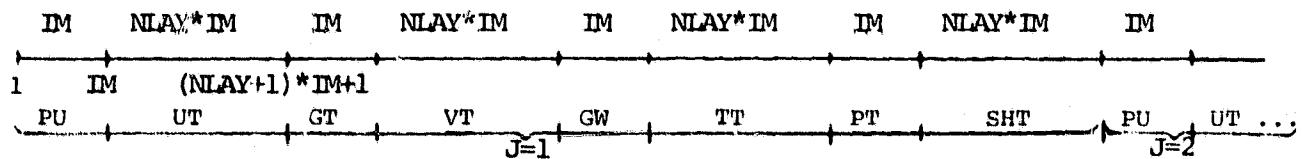
The actual code is complicated by the fact that we actually use scaled and unscaled variables, but the generalization is straightforward.

IX. Documentation of the Code (Preliminary)

The band fourth model uses special equivalences and nonstandard dimensions in order to have the variables P,U,V,T,SH stored in contiguous locations for each line of latitude. Thus, we desire to have the variables stored as follows.



The scaled variables PT, UT, VT, TT, SHT are to be stored as follows:



The above storage designation is accomplished by dimensioning PHIS(4*(NLAY+1)*IM,JNP) instead of PHIS(IM,JNP) (for a fine grid we have PHIS(2880,46), for ultrafine we have PHIS(4800,72)). Then we equivalence NLAY*IM locations of the first line of latitude of U with PHIS(IM+1,1) to PHIS((NLAY+1)*IM,1) (the first IM locations of PHIS are used for the quantity PHIS itself).

Similarly, we equivalence TS(1,1) to TS(IM,1) with PHIS((NLAY+1)*IM+1,1) to PHIS((NLAY+2)*IM,1) and so forth. (See the enclosed computer codes for the exact values in the fine and ultrafine versions.)

In order to have the successive lines of latitude arranged properly in storage we dimension our variables to achieve this purpose. Thus, we have $U(IM, 4*(NLAY+1), 1)$ instead of $U(IM, NLAY, JM)$, similarly for V, T, SH, UT, VT, TT , and SHT . For P we have $P(4*(NLAY+1)*IM, 1)$ instead of $P(IM, JNP)$ and similarly for TS, SHS, GT, GW , and PT . Note that the variables U, UT, \dots are only computed at $IM*NLAY*JNP$ points, the special dimensions are needed to properly align the variables in storage. It is important to recall that we are using two properties of the FORTRAN Compiler:

First, by equivalencing two elements of two different arrays we implicitly equivalence the other elements of the arrays. Second, that last array dimension can be left as 1 as long as it is dimensioned properly in the calling routine or it is equivalence to a properly dimensioned array. Note we could have dimensioned U as $U(IM, 4*(NLAY+1), JNP)$ we would use the same amount of storage. It is crucial to have the $IM*(NLAY+1)$ dimension because it would cause the computations on U for the successive lines of latitude to be shifted $IM*(NLAY+1)$ locations where the next line of latitude of U are stored. For clarity and simplicity in programming we use the standard equivalence of U, V, T, SH with $Q(I, L, N, J)$ with U equivalent to $Q(I, L, 1, J)$ and so forth. Since we want P, U, V, T , and SH in contiguous storage locations and the equivalence of Q with U, V, T , and SH , then we must dimension Q as $Q(IM, NLAY+1, 4, 1)$ instead of $Q(IM, NLAY, 4, 1)$. We fill in the extra locations by including $PHIS, TS, SH$, and P .

COMPØ Description

This subroutine contains the time schemes and controls the calling sequences of the routines COMP1, COMP2, COMP3, and the polar filtering routine AVRX.

The logic of this subroutine involves three considerations. First, it permits one to choose either the Matsuno or the smooth leapfrog time scheme. Second, the latter scheme involves the use of storage arrays PSM and QSM. Third, the unscaling, smoothing of the updated variables QT and the call of subroutine COMP3 occur at the value JS2=J-2 when J is the value of the current line of latitude which is being computed. The routine COMP1 and COMP2 require the values of U,V,... at JS2 in order to compute the updated values at J because fourth order differences are used in the meridional (J) direction. Only after the COMP1 and COMP2 are called for value J can we unscale, smooth, and finish processing the variables at JS2.

The code for the poles is identical in format with the code for the other J values except the variables are scaled by the pressure PPOL only.

The main program contains two calls to COMPØ which cannot be treated independently because of the calling sequence: COMPØ(Q,QT), COMPØ(QT,Q). If the first call is a leapfrog step (LF), the second one must be also LF. If the first call is Matsuno predictor (MP), the second one must be Matsuno corrector (MC). This is represented symbolically by LF \rightarrow LF, or MP \rightarrow MC. The second call can be followed by either MP or LF. Each of these combinations requires different transfers.

Description of the Time Step Sequence Parameters

NSTEP: Counts the time steps. Starts and restarts both begin with $\text{NSTEP}=0$.

NSEQ: The number of steps (combined matsuno and leapfrog) in each (repeated) sequence of time steps.

MLF(I): $\text{MLF}(I)=0$ or 1 according to whether the I^{th} step in the sequence is Leapfrog or Matsuno, respectively. First step is always Matsuno ($\text{MLF}(1)=1$).

ISMTH, } Smoothing routine (SMSHAP) is called $\text{MOD}(\text{NSTEP}-\text{NSM1},$
NSM1: } $\text{ISMTH})$; if $\text{ISMTH}=0$, there is no smoothing.

NCOMP3, } Physics routine (COMP3) is called $\text{MOD}(\text{NSTEP}-\text{NCM1},$
NCM1: } $\text{NCOMP3})$.

Sample Runs

Matsuno only:

$\text{NSEQ}=1$, $\text{MLF}(1)=1$, $\text{MATSUN}=1$, $\text{DT}=750.$, $\text{NSM1}=0$, $\text{NCM1}=0$
 $\text{BCINO3}=4$, $\text{ISMTH}=8$

Leapfrog only:

$\text{NSEQ}=1$, $\text{MLF}(1)=1$, $\text{MATSUN}=0$, $\text{DT}=600.$, $\text{NSM1}=0$, $\text{NCM1}=0$
 $\text{NCOMP3}=5$, $\text{ISMTH}=10$

1 Matsuno, 4 Leap-Frog:

$\text{NSEQ}=5$, $\text{MLF}=(1,0,0,0,0)$, $\text{MATSUN}=\text{not needed}$, $\text{NSM1}=0$,
 $\text{NCM1}=0$, $\text{DT}=600.$, $\text{NCOMP3}=5$, $\text{ISMTH}=10$

COMP1 Description

The COMP1 subroutine contains the horizontal and vertical advection differences. The DO loops over I are arranged to make use of the periodicity of the variables in the zonal (I) direction. For example, suppose we are to compute $D(I)=Q(I+1)-Q(I)$ for $I=1,\dots,IM$. Then the corresponding code is

```
I=IM  
DO 10 IP1=1,IM  
D(I)=Q(IP1)-Q(I)  
I=IP1  
10 CONTINUE
```

Where we used the periodicity $Q(IM+1)=Q(1)$.

In the meridional (J) direction we compute our difference approximations in stages in order to make maximum use of each line of latitude of a typical variable when it is in core. The fourth order difference approximation to $\frac{\partial Q}{\partial \phi}(i,l,j) = D(i,l,j)$

$$(1) \quad \frac{4}{3}(\frac{Q_{ilj+1}-Q_{ilj-1}}{2\Delta\phi}) - \frac{1}{3}(\frac{Q_{ilj+2}-Q_{ilj-2}}{4\Delta\phi})$$

Thus we see that Q_{ilj} will be needed in the difference approximations to $\frac{\partial Q}{\partial \phi}$ for $j-2$, $j-1$, $j+1$, and $j+2$. The corresponding code is

```
DO 20 I = 1,IM  
QFLUX1= 4*(Q(I,L,JP1)+Q(I,L,J))  
QFLUX2=-.5*(Q(I,L,JP2)+Q(I,L,J))  
D(I,L,JP2)= D(I,L,JP2)-QFLUX2  
D(I,L,JP1)= D(I,L,JP1)-QFLUX1  
D(I,L,J) = D(I,L,J)+QFLUX1+QFLUX2  
20 CONTINUE
```

For simplicity the array D is initialized to zero and Q is scaled so that (1) contains no divisions.

At the poles ($j=1$ or $J=JNP=46$) we use the values given in section IV on boundary conditions. We have special code for these cases denoted $J=2$ or $J=JM$ corrections.

COMP2 Description

This routine contains the Coriolis force term, the geopotential calculation (which should be made into a separate subroutine), and the pressure gradient and energy term calculations.

The geopotential PHI is dimensioned PHI(72,9,5) since we only need at most five storage locations for any computation. We use modular arithmetic (MOD5) to compute the indices JMOD, JP1MOD, JP2MOD which correspond to the standard index values of J, J+1, and J+2. Thus PHI(I,L,6) is stored in PHI (I,L,1), and we avoid shifting array values by using the JMOD index as a pointer.

For the south pole calculation we need geopotential values at J=2 and 3, thus, for J=1 we compute PHI for J=1,2, and 3. For successive values of J we need only compute PHI at JP2 which is needed in the pressure gradient calcualtion at J. Therefore, the calculation of PHI and the associated array PK are coded for calculation at JP2. Except for the first J value we are only computing the geopotential at one latitude value for each pressure gradient calculation.

X: Flow Charts

COMPO (Q,QT)

JS1=1
JS2=1

((MAIN LOOP))
DO 10 J=1,JM

((COMPUTE ALL J-PARAMETERS))

IF (JP2>JM) GO TO 25

IF (J>1) GO TO 18

JP2=JP2MOD=2
(SAVE QTPOL(M) IN QSMPOL(M),M=1,2))

18 ((SAVE QJ(JP2) IN QSM(JP2MOD)))

IF (JP2>2) GO TO 25
((INCREMENT JP2,JP2MOD)) GO TO 18

25 CALL COMP1(Q,QT,J)
CALL COMP2(Q,QT,J)

((ELIMINATE NEGATIVE HUMIDITIES))

IF (PT<(400,1100.)) STOP

IF (J<3) GO TO 200

IF (J=3) GO TO 70

29 ((UNSCALE QT(JS2)))
CALL AVRX(QT,JS2)

((LEAP FROG, MATSUNO AS RELATED TO THE
SEQUENCE OF 2 CALLS TO COMPO:
1st CALL \Rightarrow LF \Rightarrow LF or MP \Rightarrow MC,
2nd CALL \Rightarrow LF \Rightarrow LF or LF \Rightarrow MP or MC \Rightarrow MP)

IF (LF \Rightarrow LF) GO TO 45

IF (LF \Rightarrow MP.OR.MC \Rightarrow MP) GO TO 58

((STATUS: MP \Rightarrow MC OR MC \Rightarrow LF))
(P(I,JS2) \leftarrow PSM(I,JS2MOD),Q \leftarrow QSM))

IF (MC \Rightarrow LF) GO TO 63

((STATUS: MP \Rightarrow MC))

(contin.)

COMPJ (Q,QT)

58 ((P(I,JS2)+PT(I,JS2),Q+QT*DXYP*PT)) GO TO 64

45 ((P(I,JS2)+ α^* P(I,JS2)+(PSM+PT),
Q+ β^* DXYP*P*Q+ α^* (QSM+QT*DXYP*PT)))

63 CONTINUE
 ((SOURCE TERM CORRECTION FOR LEAP FROG))

IF (NOT COMP3 CALL) GO TO 67

 ((Q+Q-QT*DXYP*PT))

64 IF (NOT COMP3 CALL) GO TO 67

 IF (MATSUMO PREDICTOR STEP) GO TO 67

 CALL COMP3 (QT,JS2)
 ((COMPLETE SOURCE TERM CORRECTION,
Q+Q+QT*DXYP*PT))

67 IF (J<JM) GO TO 200

 ((INCREMENT JS2,JS2MOD))

 IF (JS2<JM) GO TO 29

70 ((POLES))

200 JS2=JS1
 JS1=J

10 CONTINUE
 ((END OF J LOOP))

RETURN

COMPL (Q,QT,J)

((COMPUTE JP2-JS2MOD))

IF (J>2) GO TO 2150

 JS1=JS2-JS1MOD=JS2MOD=1

(contin.)

COMPL (Q,QT,J)

2150 IF (J=JM) GO TO 2158
 ((COMPUTE PV₁, PV₂ = V_j* + V_{j+2}*))
 IF (J=1) GO TO 2225

2158 ((COMPUTE PU₁, PU₂ = U_i* + U_{i+2}*))
 ((COMPUTE HORIZ.ADVEC.-IN LONG. DIREC.))
 IF (J = JM) GO TO 2237

2225 ((COMPUTE HORIZ.ADV.-IN LAT. DIREC.))
 IF (J>1) GO TO 2290
 ((J=2 CORREC. TO HORIZ. ADVEC & CONV.))
 ((CONV. CALC. FOR CONT. EQ.))

2290 IF (J<JM) GO TO 2405

2237 ((J=JM CORREC. TO HORIZ. ADVEC. & CONV.))
 2405 ((CONV ← CONV * DSIG(L)))
 IF (L<NLAY) GO TO 2150
 IF (J=1) GO TO 2600
 ((COMPUTE SIGDOT,PT))
 ((COMPUTE VERTICAL ADVEC.))

IF (J<JM) RETURN

2600 ((POLES, M=1 or 2))
 ((HORIZ. ADVEC.))
 ((CONT. E.Q.))
 ((SIGDOT PL, PTPOL))
 ((VERT. ADVEC.))
 RETURN

END OF COMPL

Alternative code from ----- to -----

 IF (J.EQ.1) GO TO 2222
 ((COMPUTE PU₁, PU₂))
 ((COMPUTE HA(I))) GO TO 2235

2222 ((J=2 CORREC))
 2235 IF (J<JM) GO TO 2225
 ((J=JM CORREC)) GO TO 2405

2225 ((HORIZ ADVEC(J)))
 ((CONV.CALC.FORCONT.EQ.))

2405 ((CONV CONV*DSIG(L)))

COMP2 (Q, QT, J)

```

((COMPUTE JP2=...))

IF (J>1)                                GO TO 3001
                                         ((JP2=JP2MOD=JPKP2=1))
                                         :3005

3001      ((CORIOLIS))                   GO TO 3032

IF (J>JM)
                                         ((FIRST MAIN LOOP IN L))

3005      ((DO 3030 LX=1,NLAY))
                                         ((COMPUTE ENERGY TERM IN
                                         THERMODYNAMIC EQN))
                                         ((L=NLAY+1-LX))
IF (L<NLAY)                                GO TO 3055

3007      ((COMPUTE PK(I,LL,JPKP2)FORLL=1,NLAY))
                                         ((COMPUTE PHI'(I,NLAY,JP2MOD)) :3065

3055      ((COMPUTE PHI' AT JP2MOD FOR L<NLAY))

3065 IF (JP2=1 or JP2=JNP)                  GO TO 3030
                                         ((COMPUTE W(JP2MOD)))

3030      ((INCREMENT LX))
                                         ((IF J=1 GO TO 3005 AND COMPUTE PHI(2),W(2)))

                                         (( 2nd MAIN LOOP IN L))

3032      IF(J=1)                                GO TO 3111 ( POLES)
                                         ((DO 3031 LX=1, NLAY))

                                         IF (J > 2)                                GO TO 3085
                                         ((J=2: VT,TT CORREC.))

3085      IF (J=2orJM)                            GO TO 3135
                                         (((P) FOR U EQ.))
                                         (((P) FOR V EQ.))

3135      IF (J < JM)                            GO TO 3031
                                         (( CORREC. TO (P) J=JM))
                                         ((POLES))

3111
                                         ((CONTINUE))
                                         ((RETURN))
                                         END

```

A FOURTH-ORDER FORECASTING MODEL*

(E. Kalnay-Rivas, D. Hoitsma, and P. Anolick)

The GISS fourth-order model (Kalnay-Rivas, et al., 1977), which is a fourth-order, energy-conserving GCM on an unstaggered grid, had shown promising capabilities. It produced forecasts that showed an improvement over the second-order GISS forecasts with the same fine grid ($4^\circ \times 5^\circ$) resolution, but that were somewhat inferior to the "ultrafine" forecasts. However, the first version of the model required excessive amounts of computer memory and time for execution.

The model has been reprogrammed into the "fourth-order band model." The new program solves the primitive equations one latitude band at a time. The arrays are stored in an interlaced way, with all arrays being updated at the same latitude stored contiguously, and similarly for all arrays used in the computation of the time derivatives. This design of the program makes effective use of the virtual memory capability of the Modeling and Simulation Facility's IBM 370/165 or Amdahl computers. The virtual memory facility permits the execution of programs whose core size is larger than the one available, by placing the excess on disk and reading in those pages of information needed in the current calculations. The band fourth-order data structure and computations were constructed to optimize this virtual I/O process; a possible improvement may be to interlace also the arrays being updated with those used to compute the time derivatives. The use of the virtual memory facility avoids the explicit I/O used in the current Kern model, and yields a simpler program. (The band structure was suggested by G. Russell.)

The band fourth-order model computations have been optimized so that each time step is computed in the Amdahl in half the time required by the old model. The array structure has also been designed to reduce the amount of overall storage and high-speed memory by a factor of two (see Table 1).

Table 1. Comparison of Fourth-Order Model Computing Requirements.

	Original 4th-Order Model	Band 4th-Order Model
Core (bytes)	3500K	1500K
CPU time per step (COMP1, COMP2)	34 sec	17 sec

*Reprint from Atmospheric and Oceanographic Research Review-1978, G*AS, NASA Technical Memorandum 80253,

The model has been programmed so that it can use both the Matsuno and the leapfrog time schemes, the latter with the Robert time smoother. If Q^n and $D(Q^n)$ denote the fields at time $n\Delta t$ and the corresponding time derivative computed from the space differences, the smoothed leapfrog scheme is

$$Q^{n+1} = \bar{Q}^{n-1} + 2\Delta t D(Q^n)$$

$$\bar{Q}^n = Q^n + .5v(Q^{n-1} + Q^{n+1} - 2Q^n)$$

with $\bar{Q}^0 = Q^0$. The use of a smoothing coefficient requires a slightly smaller time step. For example, with $v = .1$, the model is marginally stable with $\Delta t = 288$ sec., compared to $\Delta t = 300$ sec. for the Matsuno and leapfrog schemes.

The smoothed leapfrog scheme is further modified to include the subgrid "physics" terms, and scaling and spatial smoothing procedures. Since the "physics" is called every few time steps, unless the leapfrog scheme is restarted after every call to the "physics," only one of the two consecutive fields will be affected. The restarting procedure is time-consuming, so it has been replaced by the following algorithm

$$Q^{n-1} = Q^{n-1} - Q^n$$

$$\tilde{Q}^n = Q^n + S^n$$

$$Q^{n+1} = Q^{n-1} + \tilde{Q}^n$$

where S^n corresponds to the "physics" terms. This procedure, which ensures that the physics is applied to two consecutive time steps, has been tested with good results.

The model can be extended into an "ultrafine" version in a straightforward way.

Preliminary Results. The first numerical integrations performed with the new band fourth-order model show dramatic improvements over forecasts made with the GLAS model with the same resolution ("fine grid" or 4° latitude by 5° longitude). The quality of the forecasts is now comparable with those produced with the "ultrafine" (2.5° latitude by 3° longitude) version of the model. Results from a 3-day numerical integration are presented in Figure 1. During an extended 8-day integration of the new fourth-order model, the atmospheric systems remained remarkably smooth, exhibiting a realistic behavior both with respect to position and intensities.

References

Kalnay-Rivas, E., A. Bayliss, and J. Storch, 1977: The fourth-order GISS model of the global atmosphere. Contributions to Atmos. Phys., 20, pp. 299-311.

The 4th Order GISS Model of the Global Atmosphere*

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Abstract: The new GISS 4th order model of the global atmosphere is described. It is based on 4th order quadratically conserving differences with the periodic application of a 16th order filter on the sea level pressure and potential temperature equations, a combination which is approximately enstrophy conserving. Several short range forecasts indicate a significant improvement over 2nd order forecasts with the same resolution (~ 400 km). However the 4th order forecasts are somewhat inferior to 2nd order forecasts with double resolution. This is probably due to the presence of short waves in the range between 1000 km and 2000 km, which are computed more accurately by the 2nd order high resolution model. An operation count of the schemes indicates that with similar code optimization, the 4th order model will require approximately the same amount of computer time as the 2nd order model with the same resolution.

It is estimated that the 4th order model with a grid size of 200 km provides enough accuracy to make horizontal truncation errors negligible over a period of a week for all synoptic scales (waves longer than 1000 km).

1. Introduction

It is generally accepted that the use of 4th order finite differences is more efficient in reducing space truncation errors than the use of higher resolution on a 2nd order model (KREISS and OLIGER, 1972). Linear analyses and shallow water type of experiments give *an upper limit* of the improvement that can be expected from the reduction of errors in the horizontal differences. For example, Table 1 corresponds to a linear wave equation with phase speed $c = 11 \text{ ms}^{-1}$, typical of atmospheric motions. It provides a measure of the "computational predictability period" after which the errors introduced by horizontal truncation alone become very serious. The table suggests that for waves longer than 2000 km a 4th order - 400 km grid model is preferable to a 2nd order - 200 grid model. Waves shorter than 2000 km are forecast more accurately by a 2nd order - 200 km grid model. In order to insure that horizontal truncation errors are small in the 1-3 week period of atmospheric predictability for all synoptic scale waves it is necessary to use either 4th order differences with a grid resolution of the order of 200 km or 2nd order differences with a grid of the order of 100 km. Numerical experiments with simple nonlinear models (WILLIAMSON and BROWNING, 1973; KALNAY-RIVAS 1976a, from now on I) also indicate dramatic reduction of errors by the use of 4th order differences.

All these studies indicate that a considerable improvement in forecasting skill is to be expected from the use of 4th order differences if *a substantial portion of the forecasting errors is due to horizontal truncation errors*. In actual numerical forecasts there are several other important sources of errors: vertical truncation errors, errors in the initial conditions, and poor "physics" (i.e. parameterization of physical processes like radiation, dissipation, subgrid transports, cumulus convection, boundary layers, etc.).

* (Paper presented during the DMG-AMS Meeting, Hamburg 1976; see Preface to Issue 1 - 2/1977)

Table 1. Elapsed time T after which a wave of wavelength L moving with a phase speed $c = 11 \text{ ms}^{-1}$ lags by more than 100 km due to space truncation errors.

	$\Delta x = 400 \text{ km}$	$\Delta x = 200 \text{ km}$
2nd order differences	$L = 2000 \text{ km}, T = 0.4 \text{ days}$	$L = 2000 \text{ km}, T = 1.6 \text{ days}$
	$L = 4000 \text{ km}, T = 1.6 \text{ days}$	$L = 4000 \text{ km}, T = 6.4 \text{ days}$
4th order differences	$L = 2000 \text{ km}, T = 1.5 \text{ days}$	$L = 2000 \text{ km}, T = 21 \text{ days}$
	$L = 4000 \text{ km}, T = 21 \text{ days}$	$L = 4000 \text{ km}, T = 328 \text{ days}$

At the Goddard Institute for Space Studies (GISS), New York, we have developed a 4th order general circulation model (GCM) with the expectation that it will yield more accurate short range forecasts, and probably more realistic climate simulations, but with the improvement limited by the other sources of errors. The model is described in Section 2. The results of several experimental short range forecasts are discussed in Section 3. A sample 36-hour forecast is presented and compared with forecasts by the standard 2nd order GISS model, which has the same resolution as the 4th order model, and by the "ultrafine" 2nd order GISS model, which has twice the horizontal resolution. Section 4 contains the conclusions and a discussion of future work.

2. Description of the model

The 4th order GISS global atmospheric model is a primitive equation model using longitude (λ), latitude (ϕ) and sigma (σ) coordinates. The basic equations and the parameterizations of physical processes are the same as those of the standard 2nd order GISS global model (Somerville et al., 1974). The finite difference scheme is quite different and is described in the following subsections.

2.1. Finite-difference scheme

The horizontal grid is uniform (constant $\Delta\lambda$ and $\Delta\phi$) and non-staggered. There are two ways to define such a grid, depending on whether variables are defined at the poles, as done by WILLIAMSON and BROWNING (1973), or half a grid size away from the poles (HOLLOWAY et al., 1973). We chose the former method because in the absence of smoothing near the poles it allows a time step twice as large as the latter. The singularity that spherical coordinates have at the poles is explicitly avoided by the use of a polar cell where "stereographic" velocities are used.

In the vertical direction we use a staggered grid with σ , the vertical velocity, defined at the boundaries of each layer, and all other variables in the center of the layer. The vertical grid can be non uniform although experiments have been made so far with constant $\Delta\sigma$. Experiments reported in I indicated that no significant improvement in accuracy was obtained when a 4th order staggered conservative scheme was used in the vertical direction. Therefore the model has 2nd order vertical differences. The computation of the geopotential Φ is performed as indicated by ARAKAWA (1972), with a modification suggested by PHILLIPS (1974).

a) Forecast equation away from the poles

Several systems of horizontal difference were tested as reported in I. The scheme chosen for the basis of these experiments consists of the simplest possible quadratically conservative 4th order differences.

We define the finite difference horizontal divergence operator at the vertical level k as

$$D_k(g) = -\frac{1}{a \cos \phi} \left[\frac{4}{3} \delta_\lambda (\Pi u^\lambda g^\lambda) - \frac{1}{3} \delta_{2\lambda} (\Pi u^{2\lambda} g^{2\lambda}) \right. \\ \left. + \frac{4}{3} \delta_\phi (\Pi v \cos \phi \cdot g^\phi) - \frac{1}{3} \delta_{2\phi} (\Pi v \cos \phi \cdot g^{2\phi}) \right]_k \quad (2.1)$$

and the finite difference gradient operator as

$$\nabla g = \frac{i}{a \cos \phi} \left[\frac{4}{3} \delta_\lambda g^\lambda - \frac{1}{3} \delta_{2\lambda} g^{2\lambda} \right] + \frac{\theta}{a} \left[\frac{4}{3} \delta_\phi g^\phi - \frac{1}{3} \delta_{2\phi} g^{2\phi} \right] \quad (2.2)$$

Here $\Pi = p_s - p_t$ is the difference between the pressure at the surface and the constant pressure at the top of the model, a is the radius of the earth, $w = u\hat{i} + v\hat{j}$ is the horizontal velocity vector in spherical coordinates, and we use the finite difference notation

$$\delta_{n\lambda} g = [g(\lambda + n\Delta\lambda/2, \phi, \sigma, t) - g(\lambda - n\Delta\lambda/2, \phi, \sigma, t)]/(n\Delta\lambda), \\ \bar{g}^{n\lambda} = [g(\lambda + n\Delta\lambda/2, \phi, \sigma, t) + g(\lambda - n\Delta\lambda/2, \phi, \sigma, t)]/2, \quad (2.3)$$

and similar formulas for the other independent variables. With this notation, the continuity equation away from the poles is

$$\frac{\partial \Pi}{\partial t} = -D_k(1) - \Pi \delta_\sigma \dot{o}_k \quad (2.4a)$$

or, if we integrate it in the vertical and make use of the boundary condition

$$\dot{o} = 0 \text{ at } \sigma = 0, 1,$$

$$\frac{\partial \Pi}{\partial t} = - \sum_{k=1}^K D_k(1) \Delta o_k \quad (2.4b)$$

where K is the number of vertical layers. Equation (2.4b) is the forecast equation for Π . The momentum equation is

$$\left(\frac{\partial \Pi w}{\partial t} \right)_k = -D_k(w) - \Pi \delta_\sigma (\dot{o} w^\sigma)_k + \left(f + \frac{u_k \tan \phi}{a} \right) \Pi \times (\Pi w)_k \\ - \Pi \left[\nabla \Phi' + \frac{\sigma R T'}{p} \nabla \Pi \right]_k + F_k, \quad (2.5)$$

The first law of thermodynamics is

$$\left(\frac{\partial \Pi T}{\partial t} \right)_k = -D_k(T) - \{ p^k \Pi \delta_\sigma (\dot{o} (T/p^k)^\sigma) \}_k \\ + \left\{ \frac{\Pi \sigma_k T}{p} \left[\frac{\partial \Pi}{\partial t} + w \cdot \nabla \Pi \right] \right\}_k + \frac{\Pi}{C_p} Q, \quad (2.6)$$

Here T is absolute temperature, \mathbf{F} is the frictional force, $\kappa = R/C_p$, Q is the diabatic heating per unit mass, p is the pressure and p^k is computed as indicated in Subsection 2.1c. The moisture equation for the water vapor mixing ratio q is

$$\left(\frac{\partial \Pi q}{\partial t} \right)_k = -D_k(q) - \Pi \delta_g (\partial q^0)_k + \Pi (E - C). \quad (2.7)$$

E and C are the rates of evaporation and condensation.

In the momentum equation (2.5) we follow a device suggested by PHILLIPS (1974) to alleviate the difficulties of the computation of the pressure gradient in σ -coordinates in the vicinity of orography. We define $T' = T - T(p)$, $\Phi' = \Phi - \Phi(p)$, where $T = \theta p^k$, $\theta = 280 \text{ K}/(1000 \text{ mb})^k$, $\Phi = \Phi_0 - C_p \theta p^k$ and $\Phi_0 = [(1000 \text{ mb})^k - p^k]^{-1}$. We have simplified PHILLIPS' expression for Φ_0 since its precise value is not important. With this procedure, in the pressure gradient term there is an exact cancellation of the terms $\nabla \Phi + \frac{\partial R T}{p} \nabla \Pi$, and this implies a significant reduction of truncation errors in regions with steep orography.

b) Forecast equations at the Poles

We have followed the method used by WILLIAMSON and BROWNING (1973) and define a polar cap of radius $a \Delta\phi$ on which we use "stereographic" (or rather "cartesian") velocity components defined by the transformation

$$\begin{aligned} U_{\lambda p} &= -u \sin \lambda + v \cos \lambda \\ V_{\lambda p} &= +u \cos \lambda + v \sin \lambda \end{aligned} \quad (2.8)$$

with inverse

$$\begin{aligned} u &= -U_{\lambda p} \sin \lambda + V_{\lambda p} \cos \lambda \\ v &= +U_{\lambda p} \cos \lambda - V_{\lambda p} \sin \lambda \end{aligned} \quad (2.9)$$

where the top and bottom signs correspond to the north and south poles respectively. The positive x -axis of the cartesian coordinates coincides with the meridian of longitude $\lambda = 0$. The difference in signs at the south pole is due to the choice of a right handed system of coordinates with the vertical unit vector pointing outwards. Formulas (2.8) and (2.9) are used to define "spherical" or "cartesian" velocity components wherever they are required in the finite difference equations.

The finite difference horizontal divergence operator at the poles is defined by an average over all longitudes λ_i :

$$D_{\lambda p, k}(g) = \frac{1+2}{1-3} \left\{ \frac{4}{3} \Lambda_1 (\Pi g)_{\lambda p} + \left(\frac{\pi}{2} - \Delta\phi \right) \right. \\ \left. - \frac{1}{3} \Lambda_2 (\Pi g)_{\lambda p} + \left(\frac{\pi}{2} - 2\Delta\phi \right) \right\}_k \quad (2.10)$$

where $\lambda_i = (i-3) \Delta\lambda$, $\Delta\lambda = 2\pi/1$, and $\Lambda_n = \Delta\lambda \sin(n \Delta\phi) / [2\pi a^2 (1 - \cos(n \Delta\phi))]$. The finite difference gradient operator at the poles is also defined by an average over all longitudes:

$$\nabla_{\lambda p} g = \frac{2}{1a \Delta\phi} \sum_{i=3}^{1+2} \left\{ \frac{4}{3} g_{\lambda p} + \left(\frac{\pi}{2} - \Delta\phi \right) \cdot \frac{1}{6} g_{\lambda p} + \left(\frac{\pi}{2} - 2\Delta\phi \right) \right\} \cdot \{ \cos \lambda_i \pm \sin \lambda_i \} \quad (2.11)$$

Then the continuity equation at the poles is

$$\frac{\partial \Pi_{\pm p}}{\partial t} = + \sum_{k=1}^K D_{\pm p, k}(1) \Delta \sigma_k, \quad (2.12)$$

the momentum equation is

$$\begin{aligned} \left(\frac{\partial \Pi V}{\partial t} \right)_k &= \mp D_{\pm p, k} (V) - \Pi_{\pm p} \delta_\sigma \left(\dot{\sigma}_{\pm p} \bar{V}_{\pm p}^\sigma \right)_k + f_{\pm p} kx (\Pi V)_{\pm p, k} \\ &- \Pi_{\pm p} \left[\nabla_{\pm p} \Phi' + \frac{\sigma RT'}{p} \nabla_{\pm p} \Pi \right]_k + F_{\pm p, k} \end{aligned} \quad (2.13)$$

where $V_{\pm p} = U_{\pm p} i + V_{\pm p} j$. The thermodynamic equation is

$$\begin{aligned} \left(\frac{\partial \Pi T}{\partial t} \right)_{\pm p, k} &= \mp D_{\pm p, k}(T) - \{ p_{\pm p}^k \Pi_{\pm p} \delta_\sigma [\dot{\sigma}_{\pm p} (T_{\pm p} / p_{\pm p}^k)] \}_k \\ &+ \left\{ \frac{\Pi_{\pm p} \sigma \kappa T_{\pm p}}{p_{\pm p}} \left[\frac{\partial \Pi_{\pm p}}{\partial t} + V_{\pm p} \cdot \nabla_{\pm p} \Pi \right] \right\}_k + \frac{\Pi_{\pm p}}{C_p} Q_{\pm p} \end{aligned} \quad (2.14)$$

and the moisture equation is similar.

c) Diagnostic equations

In σ -coordinates, the pressure is defined by $p = \sigma \Pi + p_T$. Following a suggestion by PHILLIPS (1974) we define at the center of a layer $p_k^\kappa = 1/(k+1) \delta_\sigma p_k^{\kappa+1}/\delta_\sigma p_k$, instead of $p_k^\kappa = (\bar{p}_k^\sigma)^\kappa$ as in ARAKAWA (1972). This formula was derived under the assumption that the potential temperature varies in a σ -layer much less than either the temperature or the pressure. PHILLIPS indicated that a more accurate relationship between temperature and geopotential can be expected from this formula.

The geopotential Φ is determined following ARAKAWA (1972): If Φ_S is the surface geopotential, then the geopotential at the center of the lowest layer is

$$\Phi_K = \Phi_S + \sum_{k=1}^K C_k T_k \quad (2.15)$$

and at other levels

$$\Phi_k = \Phi_{k+1} + C_p \Delta \sigma_k + \frac{1}{2} \delta_\sigma (p_k^\kappa + \frac{1}{2}) \left(\frac{T_k + 1/2}{p_k^\kappa + 1/2} \right)^\sigma \quad (2.16)$$

The coefficients C_k are determined from

$$C_k = \frac{\Pi \sigma_k R \Delta \sigma_k}{p_k} - \frac{C_p}{p_k^\kappa} \left(\sigma \Delta \sigma \delta_\sigma p^\kappa \right)_k^\sigma \quad (2.17)$$

The vertical velocity in σ -coordinate is determined from (2.4a) and (2.4b), and the boundary condition $\dot{\sigma} = 0$ at $\sigma = 0, 1$:

$$\delta_\sigma \dot{\sigma}_k = \frac{1}{\Pi} \left\{ \sum_{k=1}^K D_k(1) \Delta \sigma_k - D_k(1) \right\} \quad (2.18)$$

d) **Boundary conditions**

In the east-west direction we use periodicity: $g(\lambda + 2\pi, \phi) = g(\lambda, \phi)$ for all variables. When the value of a variable is needed "beyond" the poles, we define it by continuation along the same meridian:

$$w(\lambda, \pm\left(\frac{\pi}{2} + \Delta\phi\right)) = -w\left(\pi + \lambda \pm\left(\frac{\pi}{2} - \Delta\phi\right)\right); g\left(\lambda, \pm\left(\frac{\pi}{2} + \Delta\phi\right)\right) = g\left(\pi + \lambda, \pm\left(\frac{\pi}{2} - \Delta\phi\right)\right),$$

where g represents all variables other than the two horizontal velocity components. In the vertical the top and bottom are material surfaces through which there is no flux ($\delta = 0$ at $\sigma = 0, 1$) except for subgrid boundary layer fluxes of momentum and heat included in F and Q .

2.2. Filtering near the poles and high order filtering

The CFL computational stability condition requires a very small time step unless linearly unstable short waves are filtered out near the poles. For this purpose several alternative procedures have been tried but so far the method found to give most satisfactory results is the Fourier filtering of the prognostic variables u, v, T and *the indirect smoothing of H through the filtering of the sea level pressure (SLP) field*.

The Fourier filtering is performed polewards of 66° latitude. The amplitudes of the Fourier components of zonal wavenumber n are multiplied by a transfer function which is 1 for $n \leq N$ and decreases linearly to zero between $n = N$ and $n = N + 5$. The number of retained modes is defined by $N(\phi) =$ integer part of $(90 \cos \phi)$. We have tried filtering the stereographic velocities U, V instead of u, v but no improvement was obtained.

Since both the surface geopotential and the surface pressure fields contain large amplitude short wave components due to the presence of orography, an artificial smoothing of these fields represents a distortion of the real geometry of the boundary. On the other hand, the SLP is an intrinsically smooth field, and its high wavenumber components more closely represent atmospheric waves. Therefore in our model *the SLP is filtered near the poles and H is recovered by solving the transcendental equation used to relate them*.

It was found that the 4th order model forecasts were less smooth than those of the 2nd order GISS model, especially in regions with steep orography. Based on the same considerations we have introduced a periodic application of a high (16th) order filter (SHAPIRO, 1970) on the SLP and potential temperature fields, which are not very affected by orography.

The filter is of the form $\bar{g} = \{1 - (F_\phi^2)^8\} \{1 - (F_\lambda^2)^8\} g$, where $F_\lambda^2(g_{ij}) = (g_{i+1j} - 2g_{ij} + g_{i-1j})/4$ and has a response $F_\lambda^2[\exp(ik\lambda)] = -\sin^2(k\Delta\lambda/2) \exp(ik\lambda)$. This filter eliminates waves shorter than $4\Delta\lambda$ and even after hundreds of applications has negligible damping effect on waves longer than $4\Delta\lambda$.

In the meridional direction there are three simple alternative forms for F_ϕ^2 :

$$F_{\phi I}^2(g_{ij}) = (g_{ij+1} - 2g_{ij} + g_{ij-1})/4$$

$$F_{\phi II}^2(g_{ij}) = [(g_{ij+1} - g_{ij}) \cos \phi_{j+1/2} - (g_{ij} - g_{ij-1}) \cos \phi_{j-1/2}] / (4 \cos \phi_j)$$

and

$$F_{\phi III}^2(g_{ij}) = [F_{\phi I}^2(g_{ij} \cos \phi_j)] / \cos \phi_j$$

FRANCIS (1975) used $F_{\phi III}^2$, which is the only one that conserves the area weighted average of g . However, we have found that the three meridional filters produced virtually identical results. This could

be expected because the waves affected by the filter are too short to be strongly influenced by the convergence of the meridians. Since $F_{\phi I}^2$ and $F_{\phi II}^2$ can be programmed as efficiently as F_{λ}^2 we find them preferable. In the model we use $F_{\phi I}^2$, with g continued "beyond" the poles as indicated in Subsection 2.1d. At the poles $\bar{g}_{\pm p}$ is defined as the average over all longitudes λ_i of the filtered values \bar{g}_i . At the present we are applying the high order filter to the SLP and potential temperature fields once every two hours.

2.3. Enstrophy constraint

BAYLISS and ISAACSON (1975) have developed a simple method to make any finite difference scheme conservative with respect to any quantity. The method has been tested in our model by forcing conservation of enstrophy on the dry adiabatic version of the model, although in such a model it is potential enstrophy that is conserved. The procedure is the following: Let the vectors U and V represent the values of the velocity components discretized over the grid and let the functional $G(U, V)$ denote the consistent 4th order approximation of the mean square vorticity. At each time step a correction U' , V' is added to the predicted values \bar{U} , \bar{V} such that $G(\bar{U} + U', \bar{V} + V') = G(U_0, V_0)$ where U_0, V_0 denote the velocities at time $t = 0$. Since this equation cannot be solved explicitly, it is linearized about the predicted values \bar{U} , \bar{V} :

$$\left(\frac{\partial G}{\partial U} \right)_{\bar{U}, \bar{V}} \cdot U' + \left(\frac{\partial G}{\partial V} \right)_{\bar{U}, \bar{V}} \cdot V' = G(U_0, V_0) - G(\bar{U}, \bar{V}) \quad (2.19)$$

If we assume

$$(U', V') = \alpha \left(\frac{\partial G}{\partial U}, \frac{\partial G}{\partial V} \right)_{\bar{U}, \bar{V}} \quad (2.20)$$

then α can be determined from (2.19):

$$\alpha = \frac{G(U_0, V_0) - G(\bar{U}, \bar{V})}{\left| \frac{\partial G}{\partial U} \right|^2 + \left| \frac{\partial G}{\partial V} \right|^2} \quad (2.21)$$

It may be easily shown that the choice (2.20) minimizes $\| U' \| + \| V' \|$, the norm of the correction vector. It has been found that this procedure improves the forecasting skill of the model. However, when it is used in combination with the periodic application of the high order filter the improvement is marginal. Therefore this option is not included in the standard version of our model.

2.4. Summary of the properties of the model

The finite differences of the model have the following properties:

- a) Horizontal differences are performed on a nonstaggered grid and have 4th order truncation errors.
- b) Vertical differences are performed on a staggered grid and have 2:1d order truncation errors.
- c) The differences are conservative in the sense that in the absence of diabatic and dissipation, mass and energy are conserved except for marginal terms at the poles. Non-conservative differences similar to those used by WILLIAMSON and BROWNING (1973), *starting from real data*, proved to be nonlinearly unstable after less than one day of integration.
- d) Unlike the "box method", the horizontal differences remain 4th order near the poles (KALNAY-RIVAS, 1976b)

- e) The model contains *no horizontal diffusion* except for the possible use of a dissipative time scheme and for the periodic application of the high order filter. It has been shown in I that the combination of a 4th order quadratically conservative scheme with the *periodic* application of a high order filter replaces successfully the use of an *enstrophy-conserving scheme*. This is because waves shorter than four times the grid size are the ones subject to aliasing and to large truncation errors, and they are removed by the filter before they attain finite amplitude. Waves longer than four times the grid size are accurately computed by the 4th order scheme and are not affected by the filter.

3. Numerical forecasts

3.1. Analytical initial conditions

The model was tested using 3 dimensional extensions of both the nontrivial steady state solution and the Rossby-Haurwitz wave initial conditions used in I. The forecasts remained smooth during the several days of iteration. Errors in the steady state case were an order of magnitude larger than in I because of the use of single precision arithmetic on the IBM/360-95 computer. However, it was found necessary to use double precision for the longitudinally averaged pressure gradient at the poles in order to avoid excessive local error growth.

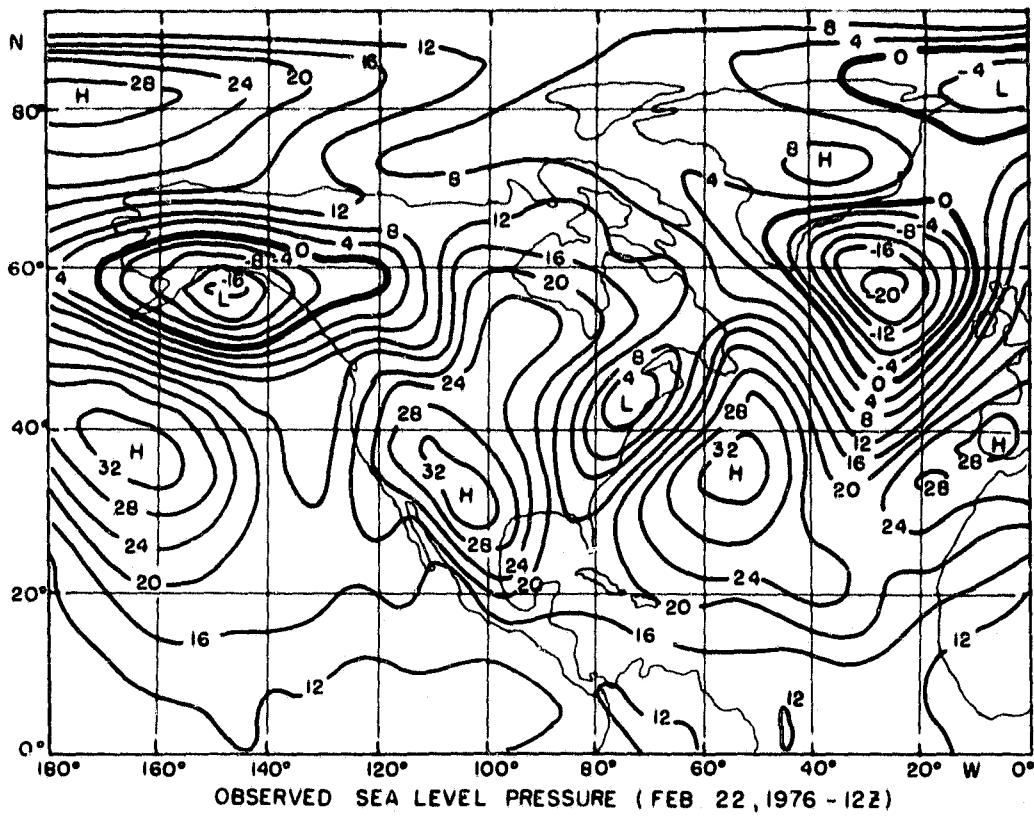
3.1. Forecasts with real initial data

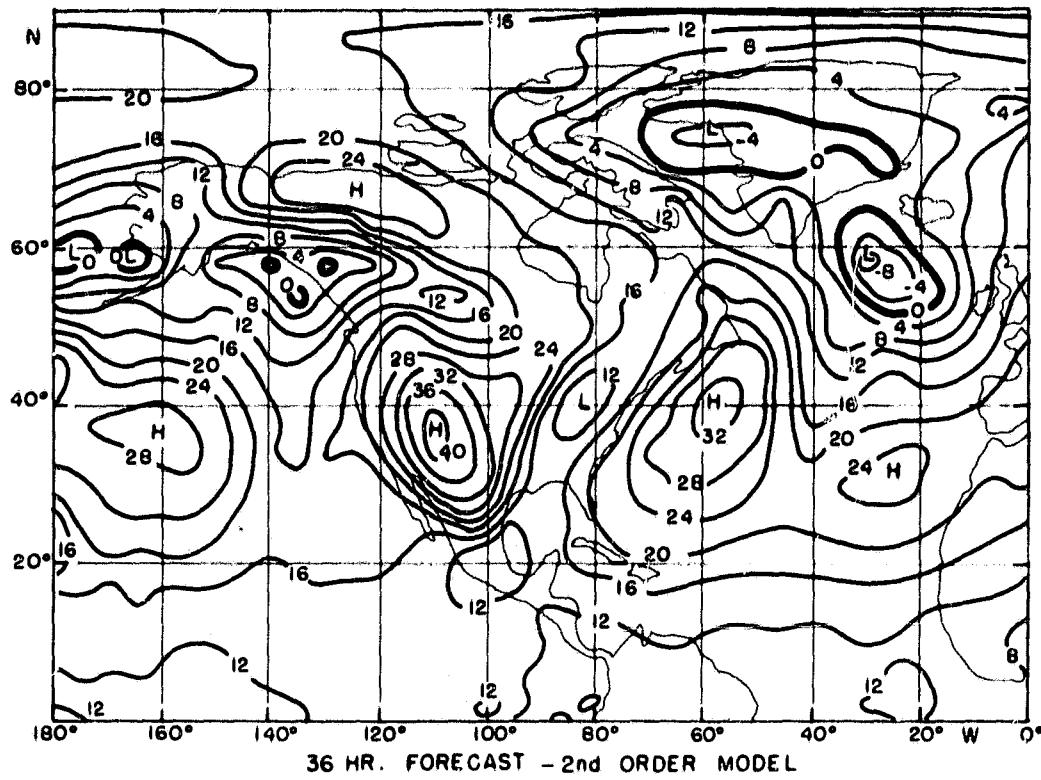
As mentioned before, the parameterization of physical processes included in the terms \mathbf{F} , \mathbf{Q} , \mathbf{C} and \mathbf{E} of Equations (2.5) - (2.7) has been adapted from the standard 2nd order GISS model (SOMERVILLE et al, 1974). The only change that has been introduced is the reduction by a factor of 2 of the surface drag coefficient. This was found to be necessary in order to avoid an excessive damping of the pressure systems after one or two day forecasts. We believe that the fact that in the staggered grid the surface winds are obtained by a horizontal average reduces the relative effect of friction in the standard model. At the present time (November 1976), we have performed 5 experimental short range forecasts. Since they have been made with slightly different versions of the 4th order model, we don't yet have a reliable measure of the model's forecasting skill. The initial data so far has been available in the staggered grid used by the standard model so that winds have been linearly interpolated to the nonstaggered grid. This is a source of error which may have adversely affected the 4th order forecasts.

We have performed a single 4-day forecast which indicated that the model remains very stable and that synoptic systems show no tendency to become unrealistically weak.

All the numerical 4th order forecasts show a significant improvement over the 2nd order forecasts performed with the same resolution. This improvement appears as a better estimation of the changes in position and intensity of several pressure systems. This is an encouraging result, especially in view of the study made by BAUMHEIFNER and DOWNEY (1976) which indicates that the standard 2nd order GISS model forecasts compare favorably with those made by the NMC and NCAR models with similar resolution.

On the other hand, and contrary to our expectations, the forecasts made with the 2nd order GISS model with double horizontal resolution were found to be either similar or superior to the 4th order forecasts. This is more true in the sea level pressure than in the 500 mb forecasts. We consider that there are several possible reasons for this result. One is the extra errors introduced in the 4th order model initial



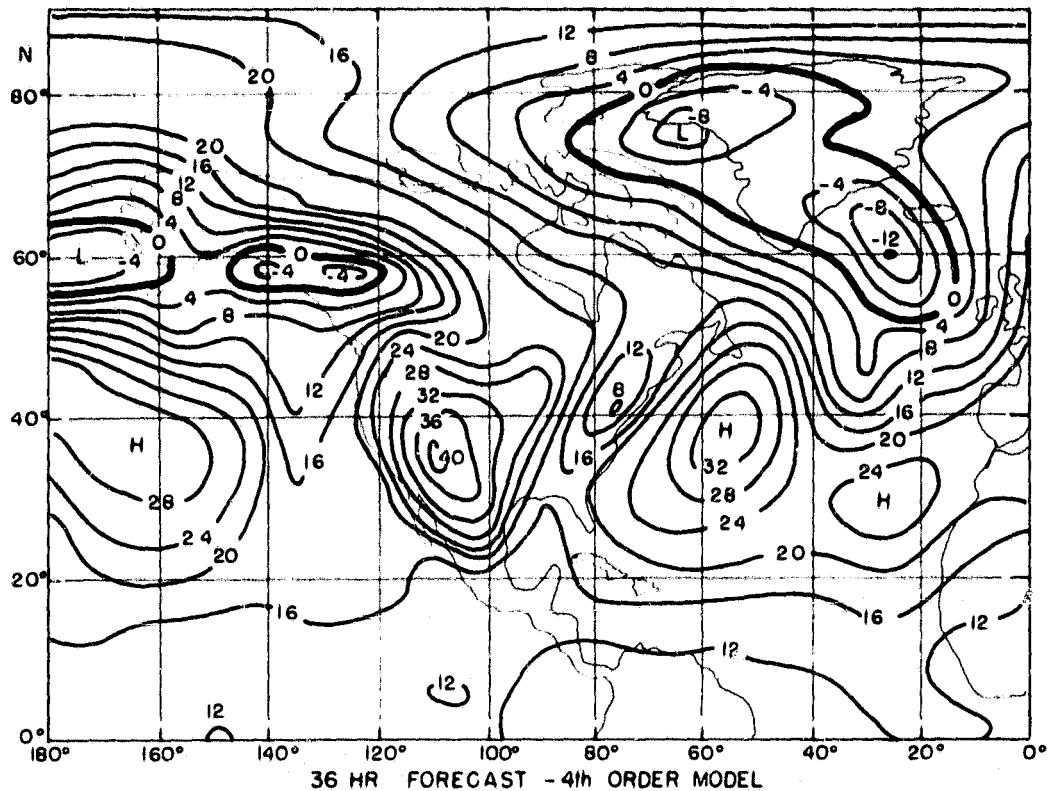


● **Figure 2.** 36 hr. forecast using the standard 2nd order GISS model

type of comparison, the three forecasts share several important deficiencies. For example the intensity of the high over southwest USA has been overpredicted by the three models, probably because of difficulties introduced by the orography. The low south of Alaska has been erroneously split by the three models. This splitting, which is slightly less pronounced in the 4th order forecast, may be due to both errors in the initial data and orographic and coastal problems.

4. Summary and conclusions

We have described the characteristics of the 4th order GISS model of the global atmosphere. It is based on a quadratically conservative scheme with the periodic application of a 16th order filter on the sea level pressure and potential temperature fields. As shown in I this combination is approximately enstrophy-conserving. An operation count of the numerical schemes indicates that with similar code optimization the 4th order model will require approximately the same amount of computer time as the 2nd order enstrophy-conserving GISS model with the same resolution. We also plan to introduce a simplified semi-implicit scheme, and to study the possibility of using the combination of a nonstaggered vertical grid with the Kreiss 4th order method described in I.

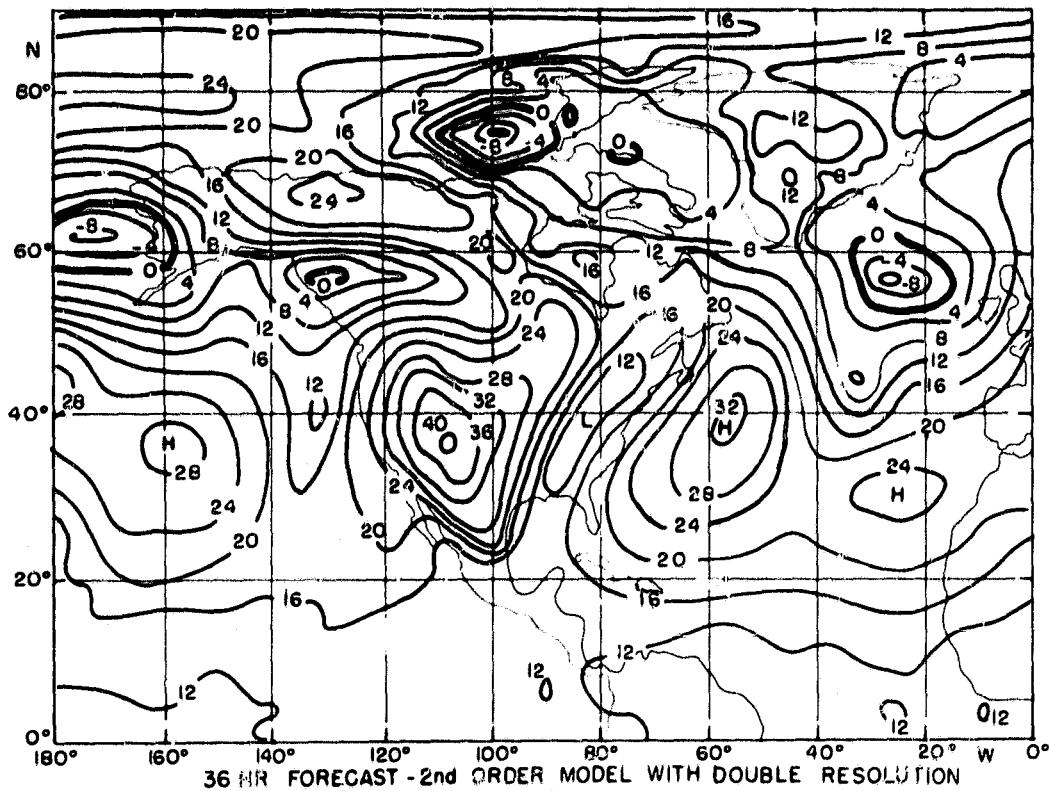


● Figure 3. 36 hr. forecast using the 4th order GISS model with the same resolution as in Figure 2

The results of several short range forecasts indicate a significant improvement over the 2nd order forecast with the same resolution. This improvement is shown in the estimations of changes in position and intensity of several pressure systems. We plan to study the impact that the greater accuracy of 4th order differences has on the forecasting skill of variables of more practical importance, such as temperature and precipitation.

It has been found that the 4th order forecasts are somewhat inferior to the forecasts made with a 2nd order model with double horizontal resolution. We consider that one of the most important reasons for this result are the presence of waves in the range between 1000 km and 2000 km which are computed more accurately by the high resolution 2nd order model than by the 4th order model. Another important reason is that errors introduced by the parameterization of subgrid processes become smaller as the size is reduced.

It is estimated that the 4th order model with a grid size of 200 km provides enough accuracy to make horizontal truncation errors negligible over a period of a week for all synoptic scales (waves longer than 1000 km).



- Figure 4. 36 hr. using the "ultrafine" 2nd order GISS model with double horizontal resolution

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THE EFFECT OF ACCURACY, CONSERVATION AND FILTERING
ON NUMERICAL WEATHER FORECASTING

ORIGINAL PAGE IS
OF FAIR QUALITY

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1. INTRODUCTION

The design of a numerical model for atmospheric simulation is not a straight-forward procedure. Both in the areas of mathematical and numerical analysis, and in the parameterization of physical processes not explicitly resolved, the modeler faces several difficult choices between equally reasonable methods, and sometimes between similarly unsatisfactory methods.

In this paper we discuss the considerations leading to the numerical design of the GLAS Fourth-Order Global Atmospheric Model. This model, which was briefly described in Kalnay-Rivas *et al.*, [1977], has been restructured, and several minor changes were introduced. The computation time and memory requirements for the 4th order model are now similar to those of the present second order GLAS model with the same 4° latitude, 5° longitude and 9 vertical-level resolution [Sommerville *et al.*, 1974]. However, the fourth-order model forecast skill is significantly better than that of the current GLAS model, and after 3 days it is comparable or better than that obtained with the 2.5° by 3° version of the GLAS model.

A discussion of several of the basic characteristics of the model design is contained in section 2. For each of them we present some of the possible alternatives, their advantages and disadvantages, and the reason for our choice. In section 3, we discuss the effect on numerical forecasts of changes in the accuracy, resolution and conservation properties of the models.⁽¹⁾ Section 4 contains some final remarks.

(1) As of this writing, several of the numerical experiments are not complete.

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2. DISCUSSION OF THE DESIGN OF THE MODEL

Different numerical analysts and atmospheric modelers often take different approaches in the design of a numerical model for weather prediction. Sometimes they even have different basic philosophies. For example Arakawa [1966, 1972], has been a pioneer in the development and use of numerical schemes that reproduce as closely as possible the conservation properties of the continuous equations of fluid dynamics that determine the motion of the atmosphere. On the other extreme, Kreiss and Oliger [1972, 1973] have advocated the use of more accurate schemes even when they don't formally satisfy any conservation properties.

The current GLAS model is based on Arakawa's [1972] second order scheme using a staggered grid B. The scheme is energy conserving and approximately enstrophy conserving for non-divergent flow. In this section we isolate the areas in which the Fourth-Order model is different from the GLAS model, discuss some of the alternatives, and the justification of our choice.

2.1 Accuracy

There is a consensus among modelers that for finite difference models with second-order accuracy, horizontal resolution of about 400 km, and about 10 vertical levels, horizontal truncation errors are the most important source of errors. The truncation errors can be reduced by any of the following methods:

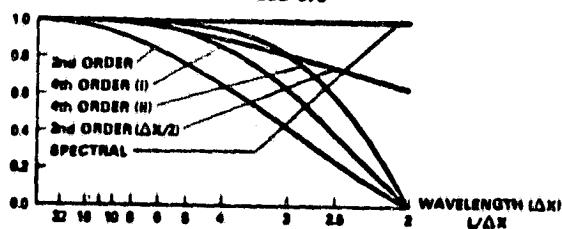
a. Increased horizontal resolution, retaining second-order differences.

Advantages: If the horizontal grid size is reduced by a factor of 2, truncation errors are reduced by a factor of 4. A comparison of the effect of truncation errors on the computational phase speed and group velocity of a linear wave is presented in Fig. 1. Another advantage is that increasing

the resolution allows smaller but possibly important scales to be explicitly included in the model.

Disadvantages: The reduction of error is slow, and the computation time is increased by a factor of 6.

COMPUTATIONAL PHASE SPEED c'/c



COMPUTATIONAL GROUP VELOCITY c'/c

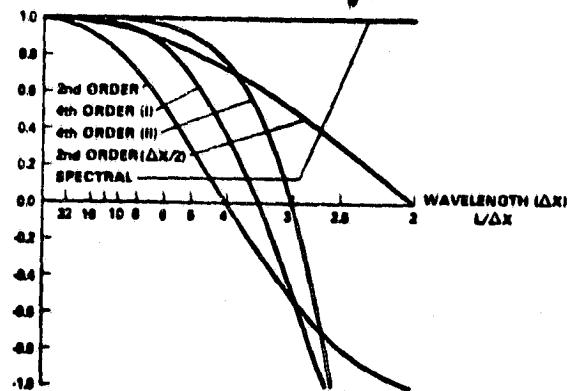


Fig. 1 Computational phase speed and group velocity for a linear wave of constant phase speed c , for different numerical schemes as a function of wavelength L .

b. Fourth order schemes of the first kind. We include in this group the common 5-point explicit fourth order schemes [Kreiss and Oliger, 1972].

Advantages: Phase speed errors are much smaller, especially for long waves (Fig. 1). Waves longer than $5\Delta x$ have smaller errors in their phase speed with fourth order differences than with second order differences with twice the resolution. If we consider the computational group velocity, the crossover occurs at about $7\Delta x$. The computational time is only increased by a factor between 2 and 3. Disadvantages: Waves in the range of $2\Delta x$ to $4\Delta x$ are still grossly misrepresented.

c. Fourth order schemes of the second kind. In this group we include linear finite elements, cubic splines and the "compact" or Pade type 3-point 4th order differences introduced by Kreiss [Orszag & Israeli, 1972], all of which have the same fourth order accuracy.

Advantages: These fourth-order differences are considerably more accurate than the fourth-order differences of the first kind (Fig. 1). The crossover with double-resolution second-order differences in the phase speed error occurs at $3\Delta x$, and in the group velocity error at about $4\Delta x$.

Disadvantages: In the simplest case, Kreiss' fourth order differences require the solution of tri-diagonal matrices. Finite element schemes require the solution of at least block tri-diagonal matrices. Even though there are efficient methods to perform these inversions, they are still computationally expensive. The extra accuracy can be compensated with 4th order differences of the first kind by increasing the resolution, which has other advantages, as we mentioned earlier. These schemes, as well as in higher order finite difference schemes, waves in the range of $2\Delta x$ to $4\Delta x$ are still grossly misrepresented.

d. Spectral schemes.

Advantages: If the basis of the spectral expansion are the eigenfunctions of the wave equation, spectral schemes have no phase speed errors. Because of this they require less resolution than finite difference schemes.

Disadvantages: Because of the large number of computations required for the nonlinear terms, spectral schemes are competitive with finite difference schemes only in combination with the use of less resolution and semi-implicit time schemes.

Our choice: We chose to use fourth order finite differences of the first kind because they are computationally efficient and have small truncation errors except in the range of waves with wavelengths between $2\Delta x$ and $4\Delta x$.

2.2 Type of Grid

Both staggered and unstaggered grids have been widely used by atmospheric modelers.

a. Unstaggered grid: The advantage of this grid is its simplicity. Higher order schemes are easily developed with this grid. Its disadvantage is that all centered differences have to be computed over a distance of $2\Delta x$.

b. Staggered grids: Several staggered grid configurations are possible as reviewed by Arakawa [1972]. The one he called scheme C, which is the most commonly used, has the pressure defined at the center of a grid cell, and the velocity components u and v defined at their corresponding normal walls. This grid has the advantage that the pressure gradient and velocity divergence terms are computed over a distance of only $1\Delta x$, so that inertia gravity waves are computed with double resolution. Therefore, as pointed out by Arakawa, geostrophic adjustment is best represented in this grid. On the other hand, advection terms are computed with no more accuracy than in the unstaggered grid, and in the Coriolis' acceleration term, it is necessary to take horizontal averages of the velocities. The

higher resolution of inertia gravity waves reduces the maximum time step for explicit time schemes by a factor of two. Full fourth order schemes can be developed with staggered schemes but they are very involved [Kainay-Rivas, 1976]. To date, modelers using staggered grids have introduced fourth order differences only in the advection terms.

Our choice: During extended range forecasts, second order errors in the non-advection terms may become important. For this reason we chose to use an unstaggered grid that allows the use of a simple, full fourth-order scheme.

2.3 Conservation Properties and the Use of Horizontal Diffusion

With respect to conservation properties, there are basically 3 types of finite difference schemes for the primitive equations:
a) Nonconservative schemes, the simplest of which is the one based on the advective form of the equations; b) quadratically or energy conserving schemes; and c) enstrophy conserving schemes. Advective and quadratically conservative schemes can be easily developed using staggered or unstaggered grids [Lilly, 1965; Bryan, 1966]. Enstrophy conserving schemes for the primitive equations have been developed on a grid C by Grammeltvedt [1969] and Arakawa and Mintz [1974]. Sadourny [1965a, b] constructed a potential enstrophy conserving scheme on grid C, and Arakawa [1978] has recently developed a potential enstrophy and energy conserving scheme also on grid C.

Nonconservative schemes require a procedure to damp waves shorter than $4\Delta x$, which otherwise grow spuriously causing catastrophic nonlinear instability [Phillips, 1959]. This has usually been done by means of linear or nonlinear horizontal diffusion, or by using dissipative numerical schemes such as the Lax-Wendroff, or schemes that contain explicit horizontal averaging.

Quadratically conservative schemes avoid the unbounded growth of the solutions associated with catastrophic nonlinear instability. However, as Arakawa [1972] and Sadourny [1975a, b] have pointed out, in the course of long integrations, there is still a spurious build up of energy in the shortest waves, which appears as an unbounded growth of the total enstrophy. In the absence of horizontal diffusion, this type of slow nonlinear instability will completely distort the solution. Enstrophy conserving schemes, on the other hand, impose a stronger constraint on the growth of the smallest scales present in the model. For this reason, the UCLA and the GLAS models, which use enstrophy conserving schemes, do not need to include horizontal diffusion.

It should be emphasized that conservation of enstrophy does not necessarily imply a more accurate or realistic simulation. In the real atmosphere, the constraint of quasi-geostrophic motion implies that very little of the energy generated in the baroclinically unstable scales can reach the smallest scales

and be eventually dissipated [Charney, 1972]. In a numerical model, the finite resolution imposes an artificial "wall" at the short end of the spectrum, inducing an excessive accumulation of energy in the shortest waves. This problem is worst in nonconservative schemes, but it appears even in alias-free, energy- and enstrophy-conserving spectral models. This justifies using some parameterization of the unresolved subgrid eddies to withdraw energy from the smallest resolved scales.

For this purpose, Leith [1972] suggested the use of nonlinear horizontal diffusion in which the eddy diffusion coefficient is proportional to the local gradient of vorticity. This formulation is consistent with the transfer of energy to subgrid scales in two-dimensional turbulence. In another widely used formulation, suggested by Smagorinsky [1963] and based on a three-dimensional turbulent cascade theory, the diffusion coefficient is proportional to the deformation tensor. These formulations are better than the use of linear diffusion, but they both share the following problems: a) the diffusion coefficient is computed inaccurately for the shortest waves, and, more importantly, b) when the diffusion coefficient is large enough to avoid the spurious growth of the smallest scales, it produces excessive damping of the larger scales [Merilees, 1975; Williamson, 1978]. Furthermore, at the short end of the spectrum (scales of the order of 100 km), neither quasi-geostrophic nor 3-dimensional isotropic turbulence theories are really justified. Williamson [1978] generalized a higher order diffusion of the form $V^4 k V^2$, suggested by Kreiss and Oliger [1972], still using the deformation type of diffusion coefficient. This formulation has the advantage that, because it is more scale dependent, there is less damping of the longer waves.

In our model, we have taken an approach closer to Fourier filtering the shortest waves, as suggested by Phillips [1959]. Our "subgrid parameterization" is based on the following argument: The 4th order scheme is adequate accurate for waves longer than $4\Delta x$, but grossly inaccurate for waves between $2\Delta x$ and $3\Delta x$. Since the shortest waves cannot provide any useful information in a finite difference scheme, we filter them out of the system while their amplitude is still small. Even though they are filtered out, the shortest waves still play an important role in the model: they act as a buffer or "sponge layer" in the spectrum domain, allowing energy to trickle down from longer waves and avoiding the accumulation of energy that would otherwise occur at the short wave cutoff.

The elimination of the short waves is performed in the model with the periodic use of a 16th order Shapiro [1970] filter, first introduced in GCMs by Francis [1975]. Figure 2 indicates the response of Shapiro filters of order 4, 8 and 16. It can be observed that in the case of a 16th order filter waves longer than 4 are scarcely affected at all

even after 128 applications, which in our model correspond to a 10 day integration. Waves shorter than 4 are virtually eliminated. Lower order filters introduce too much decay at long scales.

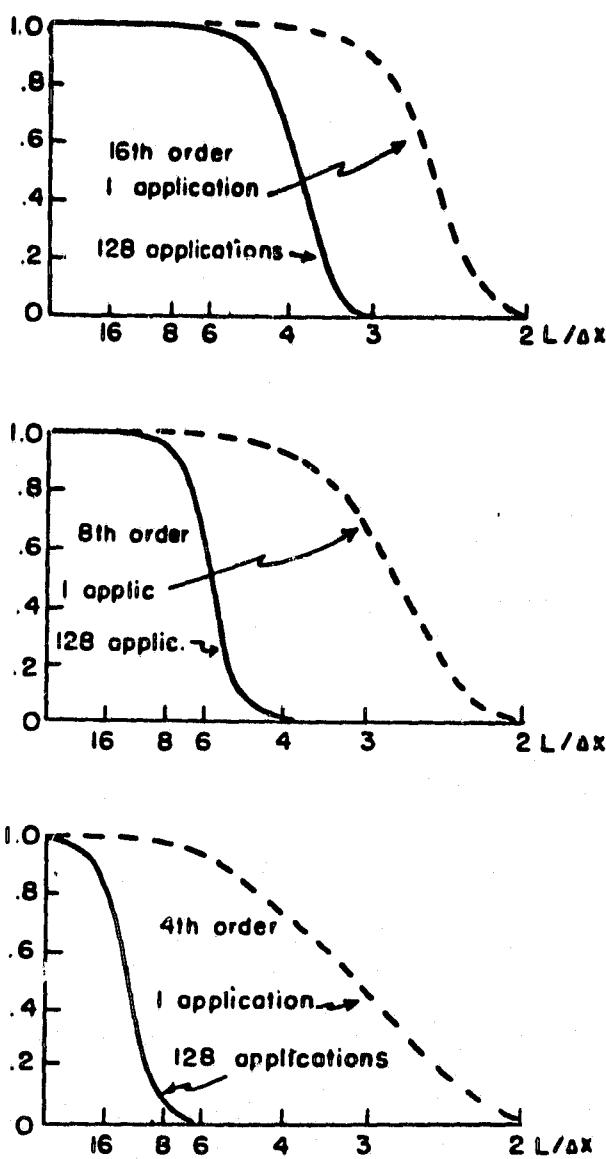


Fig. 2 Response of Shapiro filters after 1 and after 128 applications.

In order to explore the effect of filtering short waves we performed a series of 20 day forecasts with a simple shallow water equation model [Kalnay-Rivas, 1976], using different combinations of schemes, smoothing operators and frequency of application as indicated on Table I.

A1:	4th order, non-conservative, no smoothing.
A2:	" " linear diffusion, $D=10^3 \text{ m}^2/\text{s}$
A3:	" " , 16th order filter/4 hrs.
A4:	" " , " /time step.
B1:	" quadrat. conserv., no smoothing.
B2:	" " , 16th order filter/4 hrs.
B3:	" " , 8th " "
B4:	" " , 4th " "
C:	2nd order, " , no smoothing

TABLE I: Characteristics of the different runs in Fig. 3.

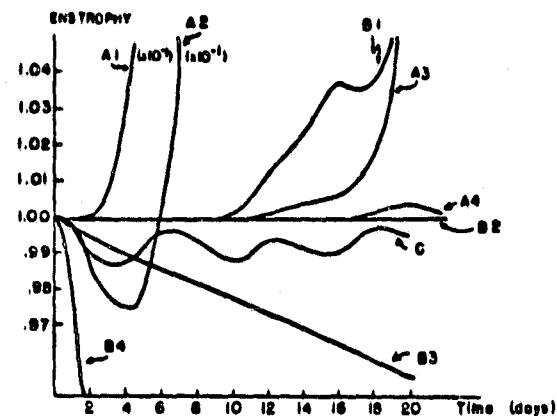
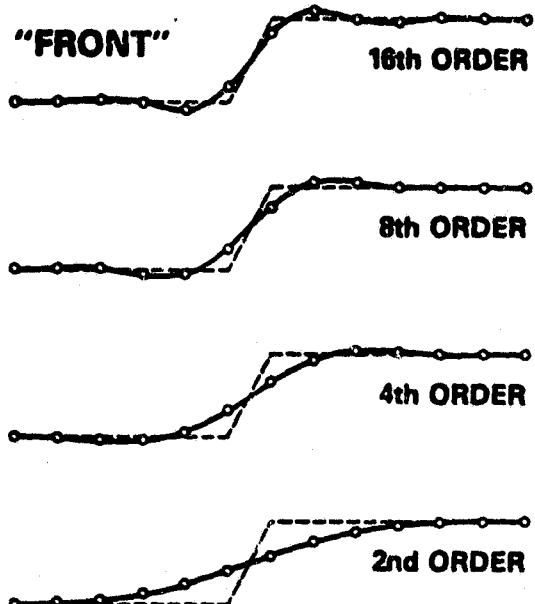


Fig. 3 Variations of total enstrophy during numerical integrations as indicated in Table I. The scale corresponding to experiments A1 and A2 is multiplied by 10^{-3} .

We found that all stable runs conserved total energy with a high degree of accuracy. Fig. 3 shows the variation in time of the total potential enstrophy, which is conserved exactly in the continuous equations. The results indicate that when the 16th order filter is applied every time step (10 minutes) even a formally nonconservative scheme conserves both total energy and total potential enstrophy during a long integration (Run A4). The quadratically conservative scheme controls better the amount of energy going into the smallest scales, so that in Run B2 it was enough to apply the filter every 4 hours to conserve potential enstrophy within 0.05%, even though such conservation is not formally guaranteed in the scheme.

It may be questioned whether the application of a high order filter eliminates small scale features like frontal zones or the effects of orographic or cumulus convection forcing on small scales. Fig. 4 indicates that this is true for lower order filters. However a 16th order filter eliminates only those components which are not resolved anyway, and still allows for the formation of sharp gradient zones and strong local maxima.

10 PASSES (ONE DAY) OF SHAPIRO FILTER



10 PASSES (ONE DAY) OF SHAPIRO FILTER

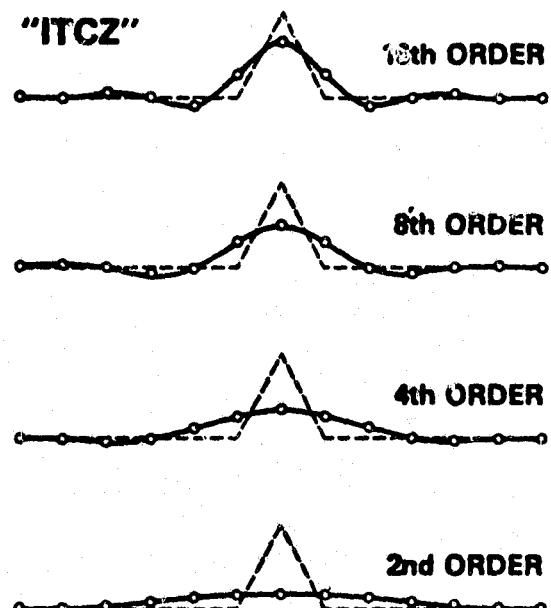


Fig. 4 Effect of 10 applications of a 16th order Shapiro filter on a) a step function b) a spike.

Our choice: We chose to use a quadratically (energy) conserving scheme because it is only slightly less efficient than an advective scheme and it requires the application of a high-order filter only every few hours to avoid the effect of slow nonlinear instability associated with a spurious growth of enstrophy. We apply the filter to the sea level pressure and potential temperature fields in order to compensate for the effect of topography.

3. EXPERIMENTAL FORECASTS: PRELIMINARY RESULTS

We plan to perform an extensive series of forecasts to study the effect of using different schemes and varying resolution on the quality of actual weather forecasts. In this section we present some preliminary results.

We tested the Fourth Order model by making 3-day forecasts from several initial conditions. In every case the model performed much better than the GLAS model with the same 4° by 5° resolution. After 3 days the forecasts were comparable to the 2.5° by 3° version of the GLAS model in the sea level pressure maps, and had slightly less phase errors in the 500 mb maps.

Fig. 5a shows the verification sea level pressure map corresponding to a 3-day forecast with February 19, 1976, 0Z (a case that has been studied in detail by Atlas et al., 1979). Fig. 5b is the 3-day forecast with the Fourth Order 4° by 5° model verifying on the same date. The excessive gradients, especially at high latitudes are due to a faulty computation of the ground temperature by the radiation routine used in that run. Figs. 5c and 5d are the forecasts generated by the GLAS models with 4° by 5° and 2.5° by 3° resolution respectively. Fig. 6 displays the corresponding 500 mb maps.

In Fig. 7a, we present the verification sea level pressure map corresponding to a 3-day forecast with February 1, 1976, 0Z initial conditions. The results of six different 3-day forecasts are shown in Figs. 7b to 7g. The forecast in Fig. 7b was computed with the new full Fourth-Order model, using the same resolution and parameterization of physical processes (except for the long-wave radiation routine) as in the 4° by 5° GLAS model (Fig. 7c). In Fig. 7d, the model was the same as in 7b, but full Second-Order accuracy was used. If we compare these three made with the same resolution, we see that the fourth order model did considerably better, especially in forecasting the development and motion of the cyclone southwest of Greenland. The two second-order forecasts are close to each other.

(3) The idea of filtering these fields is due to Dr. A. Bayliss.

Fig. 7 shows the forecast made with the 2.5° by 3° GLAS model starting from the NASA initial conditions with assimilation of satellite data [Atlas et al., 1979]. All other forecasts were made from NMC's Global Analysis initial conditions. The cyclogenesis forecast was poorer than with the fourth order model, but over continental North America the forecast was better. This may be due to the higher resolution or, possibly, improved initial conditions. Fig. 7f presents the forecast made with NMC's 6-layer, 380 km resolution, which has resolution comparable to our 4° by 5° grid. For these initial conditions, NMC's forecast was better than the GLAS second order forecast, although it shared some of its errors (such as a spurious anticyclogenesis over the Great Lakes).

Fig. 7g shows a forecast made with a slightly different version of the fourth order model. The differences were as follows: In the 7g forecast we used a Matsuno time step, a surface drag that was .75 of that of the standard model, the Shapiro was applied every two hours, and a slightly different scheme for the vertical advection of moisture was used. In the 7b forecast we used a combined Matsuno-leap-frog scheme, the surface drag was the same as in the standard model and the filter was applied every hour. The two forecasts are quite similar, but from other experiments it seems that the positions of the oceanic lows west of Spain and south of Alaska were somewhat affected by the change in frequency of the Shapiro filter.

4. FINAL REMARKS

Although these are preliminary results, the new Fourth-Order model seems to have very good forecasting skill. Similar excellent results with fourth order schemes were reported by Campana [1978, 1979], and by Williamson (1978). Campana found that most of the improvement over the second order model was obtained just by introducing fourth order accuracy on the horizontal averages performed on the Shuman-Hovermale model. Campana also obtained that for 2-day forecasts, fourth order differences were important in the advection terms but not in the pressure and continuity terms. We made shallow water equation experiments that showed some deterioration of the solution after about 8 days when only the advection terms were written with fourth order accuracy. Since baroclinic models are much more unstable than the SWE, Campana's results may not hold during extended forecasts. We are performing experiments to study this possibility in our model. We are also repeating some of the forecasts using a vector invariant form of the momentum equations. The NMC 6-layer PE model used in Fig. 7f is based on such a formulation, and we want to determine if it affects the solution.

We are performing integrations with a 2.5° by 3° version of the Fourth-Order model. From linear theory, this should make horizontal truncation errors negligible for most synoptic scales for periods of a week or longer. Still, narrow atmospheric features like those due to sharp orographic forcing on the ITCZ will remain poorly resolved.

We have found the fourth order model to be extremely sensitive to the parameterization of physical processes. For example, it became unstable through excessive cooling near the surface, apparently due to a flaw in the radiation routine. None of the second order models was sensitive to this problem.

In this paper we have discussed the use of formally nonconservative schemes coupled with periodic filtering of the shortest waves as an alternative to the use of conservative schemes. It is clear from the experimental results that formal enstrophy conservation has had no beneficial impact on the quality of the forecast (Figs. 7c and 7d). Conservation of potential enstrophy [Arakawa, 1978] might have a more positive effect.

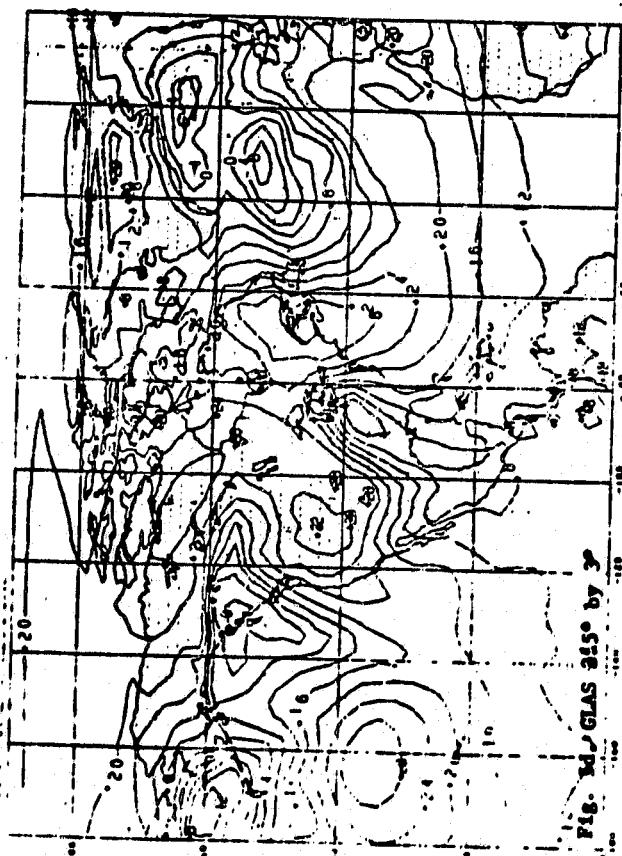
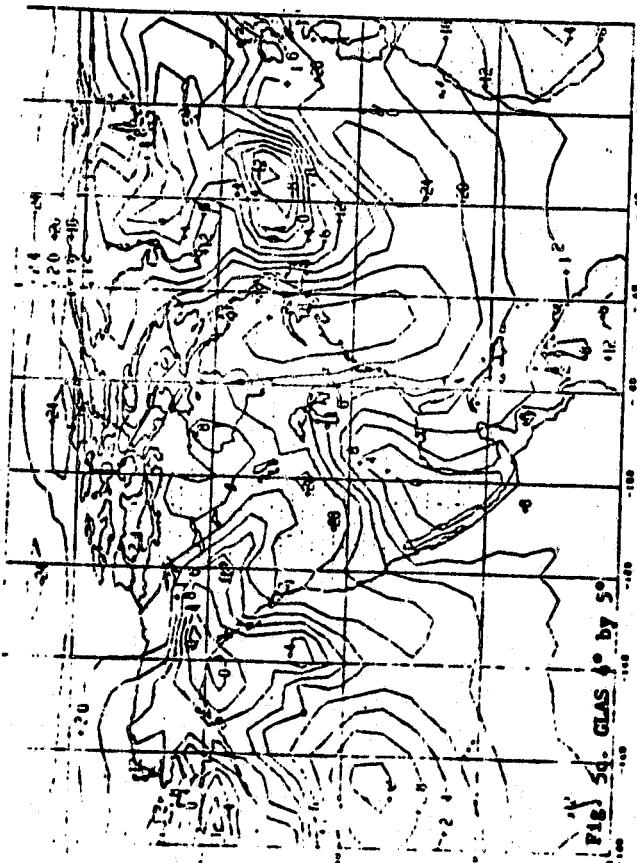
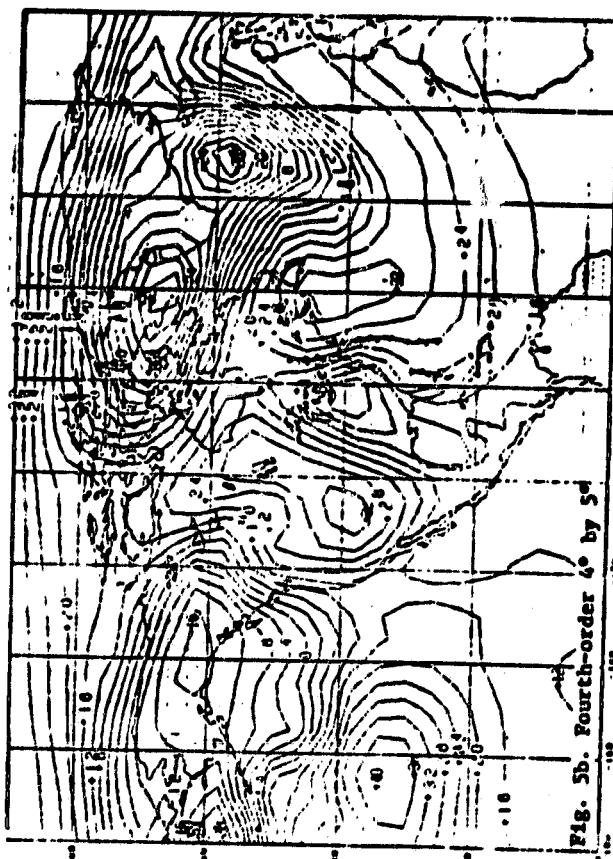
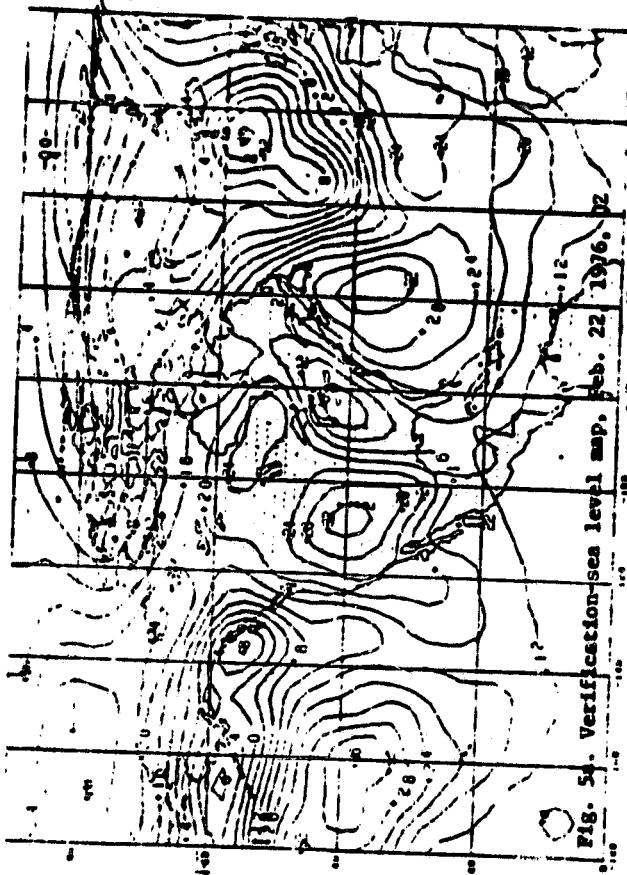
We think that the use of nonconservative schemes with high order periodic filtering is also justified in climate simulations as long as the rates of energy or enstrophy loss due to filtering remain much smaller than the observed rates of generation and dissipation.

Acknowledgements: Dr. A. Bayliss' contribution was crucial in the development of the model. The authors have benefitted from stimulating discussions with Profs. M. Cane, E. Isaacson and D. Randall. The authors are grateful to Dr. M. Halem for his patience, encouragement and many useful suggestions. Dr. N. Rushfield and Mr. W. Connelly were extremely helpful in the development of the program. Dr. M. Wu provided us with her accurate radiation routine.

Fig. 5 Sea level pressure maps corresponding to 3-day forecasts with February 19, 1976, 0Z initial conditions.

Fig. 6 Same as Fig. 5 but 500 mb geopotential heights.

Fig. 7 Same as Fig. 5 but for February 1, 1976, 0Z initial conditions.



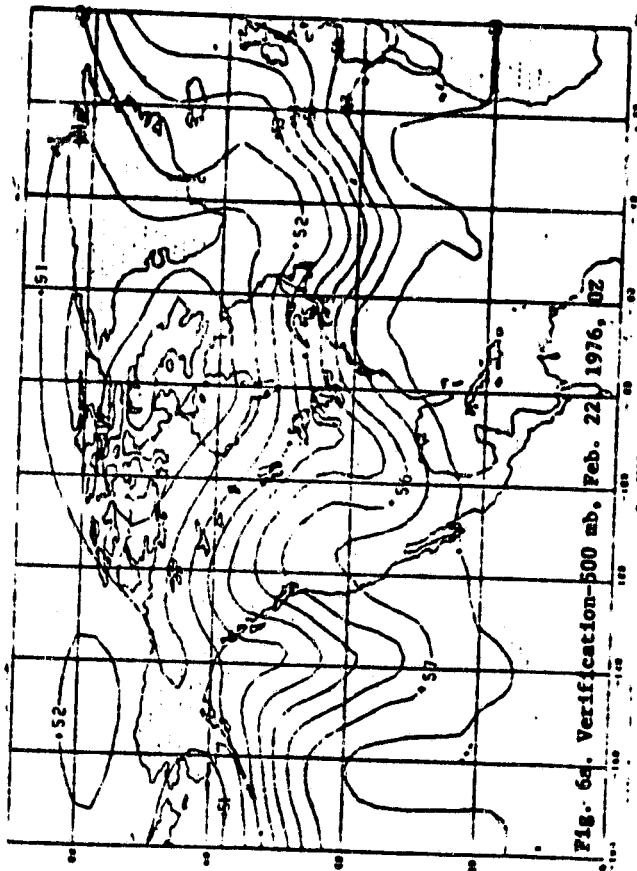


Fig. 6. Verification-500 mb. Feb. 22, 1976.

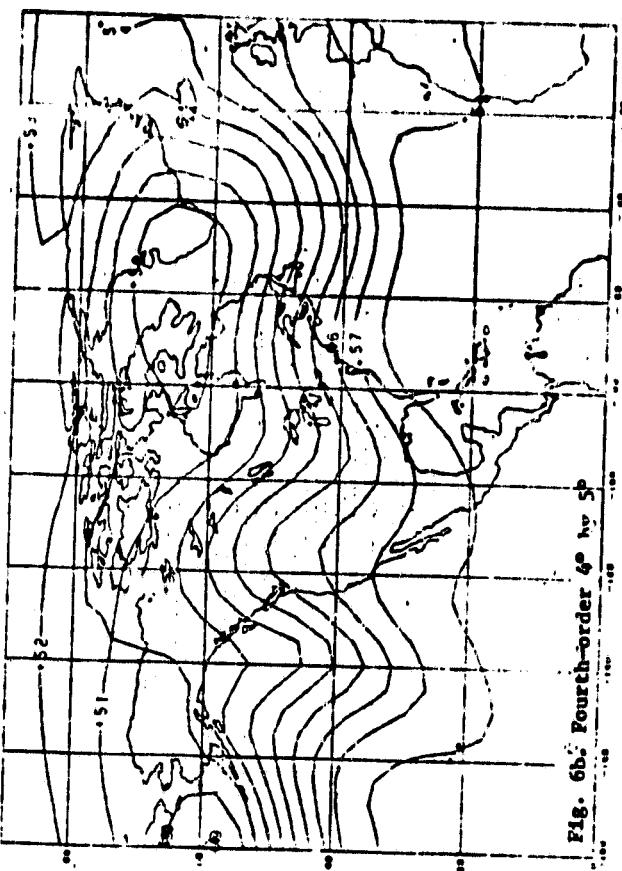
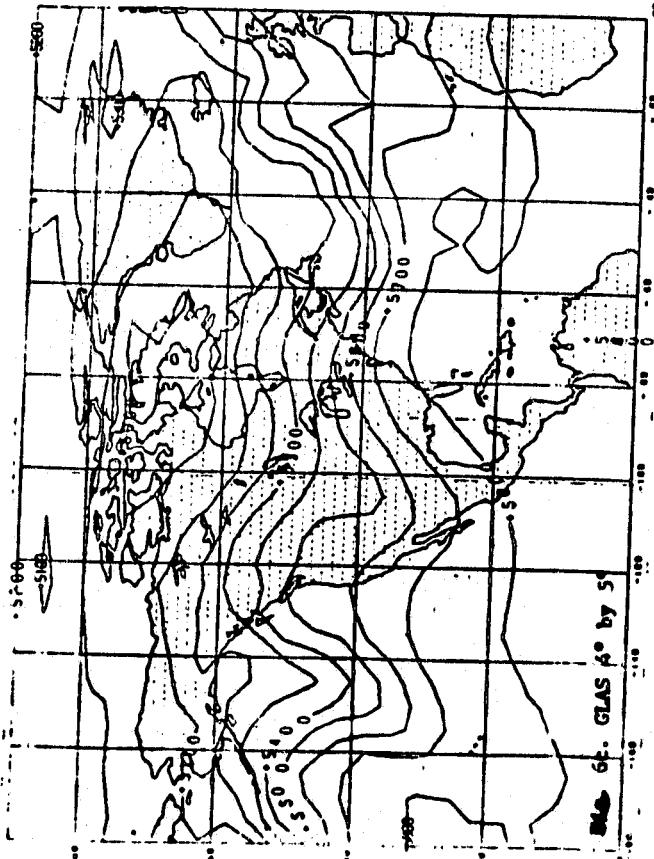


Fig. 6b. Fourth-order 40 by 50



Ms. B. 6. CLAS 60 by S.

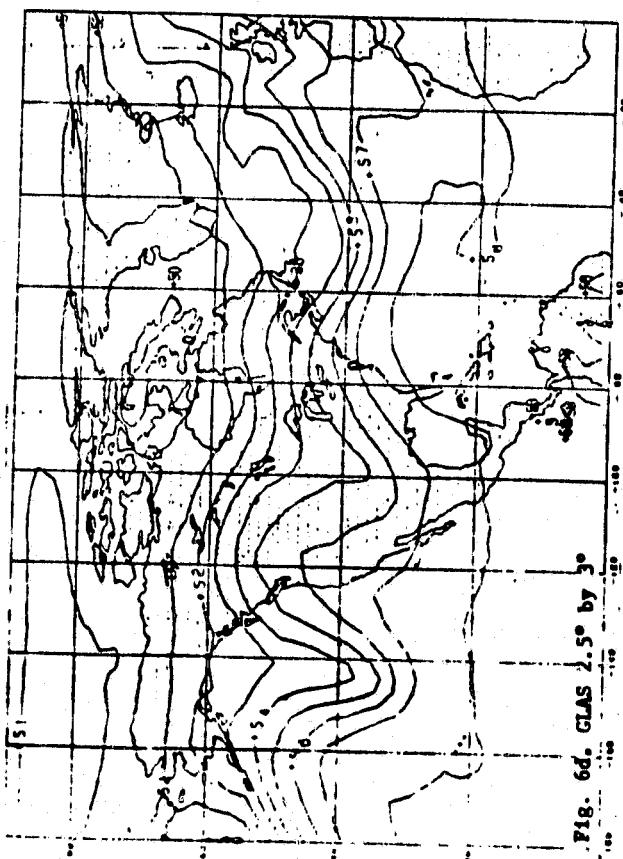


Fig. 6d. CLAS 2.5° by 3°

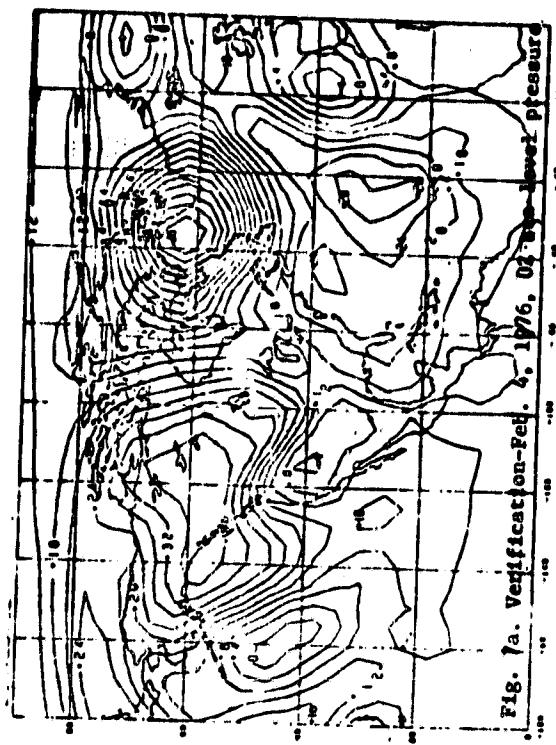


Fig. 7a. Verification- Feb. 1976. 0.2 m. level pressure

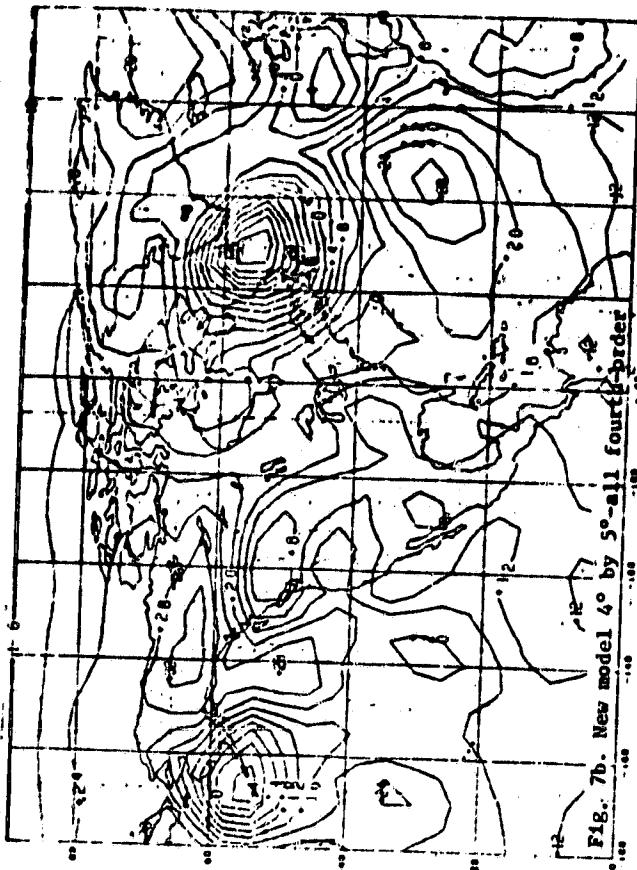


Fig. 7b. New model 4° by 5° all fourth-order

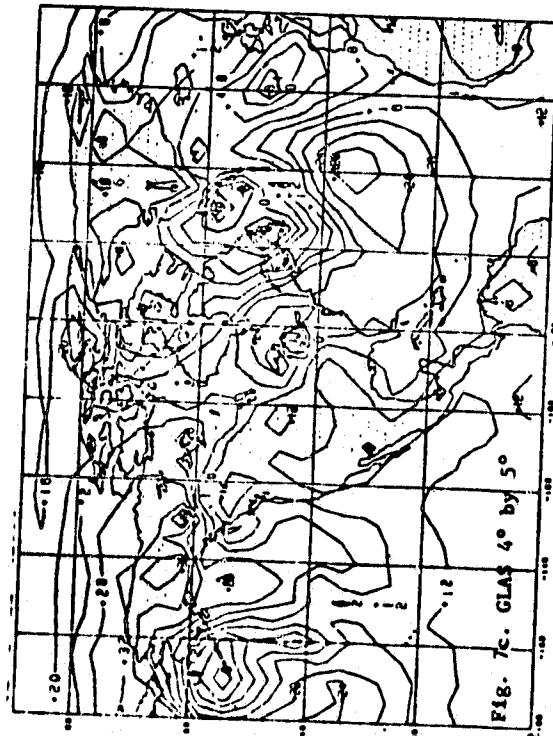


Fig. 7c. GLAS 4° by 5°

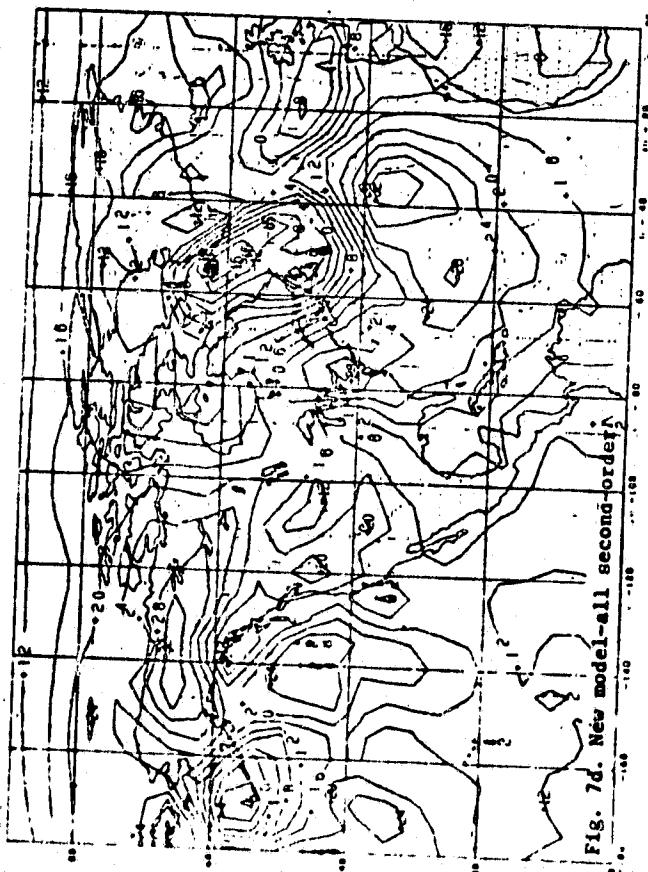
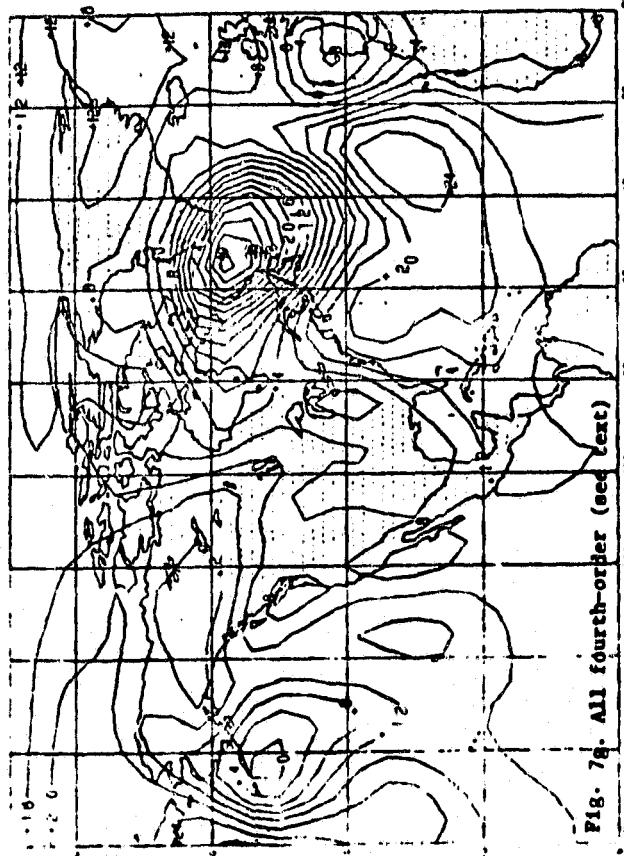
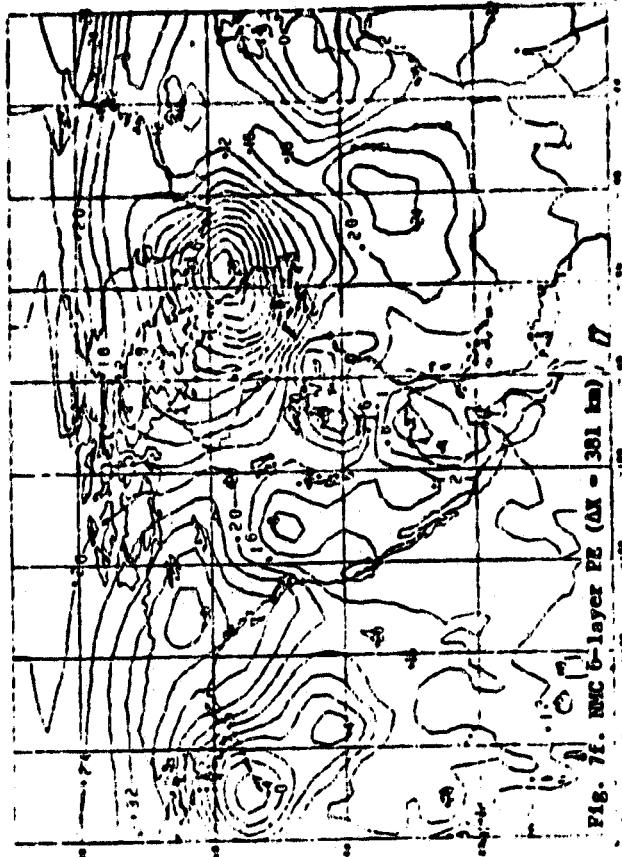
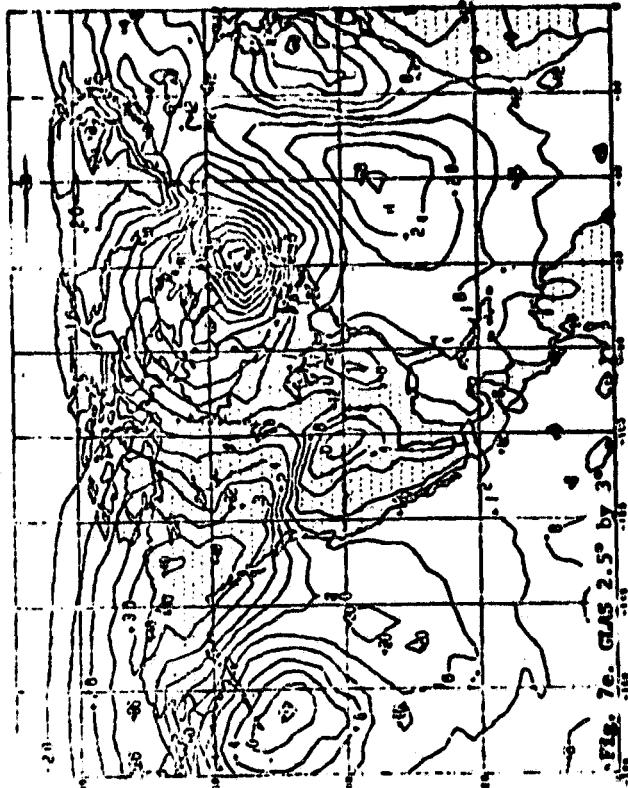


Fig. 7d. New model-all second-order



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EVENT(XTAU)=MOD( ITAU , INTF(XTAU)) .LT. (ITHR
CALL SUPUND
CALL DATE(ADATE)
CALL TIME(ATIME)
CALL CLOCK$;ITM)
NDS=1
ITIME=ITM
LNTM=LTM
CALL INPUT4
DTSAVE = DT
DT$2=*.DT
C
NPCE=1 FOR PREDICTOR STEP
NPCE=1 FOR CORRECTOR STEP
TAU=TAU*12.
TAU=TAU*12.
DTHRD=3600
10THR=INTF(XDTHR)
12.=INTFX;24.
NSTEPC=5*(TAU/DTHR
NSTEPC=5*(TAU-TAU)/DTHR
WRITEL3.26)NSTEPC
26 FORMAT(//30x,'FIRST NSTEP= ',IS//)
NSTEE=0
IF(NSTE=0)EQ.1)MLF(2)=MAISUN
ITAUM=MLF(1)
ITAUM=NSTP*IDTHR
TAU = FLOAT(ITAUM)/XINT
IDA=ITAUM/12.
TDFDAY=FLOAT(ITAU-IDAY*(24)/XINT
CALL DALL
IF(LALTER.GT.0) CALL ALTER
BRITE :3.OUTPUT)
TAUS=TAU
TAPNUM=XLABEL(120)
WRITE (3,901) TAPNUM,TAUST,TAU,TAUT,XLA$R.
NCODE=BLANK
901 E13.26
24 FORMAT(1//50x,'NEXT ORDER //')
IF(ISTART.LE.4) GO TO 45
C*** MAIN LOOP
45 CONTINUE
46 IF(LALTER.GT.0) CALL ALTER2
NSTEPC=NSTEP+NSTEPC
COMG = *FALSE*
IF(NOT EVENT(TAU)) GO TO 50
COMG = *TRUE*,
C
C REPLACE DT WITH MATSUNG TIME-STEP SIZE SINCE
C ANY RESTART NEEDS TO BEGIN WITH A MATSUNG STEP
C
C TEMP = DT
DT = DTSAVE
C
CALL CLOCK$INTM)
C
CODE=ONTAPE
CALL TMRITE
CALL TMRITE
C
INITIALIZE PRECIPITATION ARRAY.
ITAU = TAU + 0.01
IF (MOD(ITAU,12) .NE. 0) GO TO 47
DO 46 J = 1, IN
DO 46 I = 1, IN
SDOTT1, J, 3) = 0.
SDOTT1, J, 4) = 0.
46 CONTINUE
47 CONTINUE
C
C REPLACE DT WITH CURRENT STEP-SIZE
C
C DT = TEMP
C
50 CALL CLOCK$INTM)
TOM=FLOAT(INTM)/100.
LNTM=INTM
LNTM=FLOAT(LNM(4-INTM))/100.
WRITE(3,902)NSTEP, IDAY, TDFDAY, JDATE, JMONTH, STM, TORM, TAU
1 XLABEL(20), NCODE
CALL SSNTCH(4,ISSA)
IF (ISSA.EQ.1) WRITE (3,906)TAU, IDAY, TDFDAY, TAUST, TAU
IF (ISSA.EQ.1) CALL S SCFF
CALL SSNTCH(6,ISS6)
IF (ISS6.EQ.1) WRITE (3,27)NSTEP
27 FORMAT(1//30x,'LAST NSTEP= ',IS//)
IF (ISS6.EQ.1) GOTO 87
IF (TUT+01).GT. TAU) GOTO 88
IF (TUT+01).LT. TAU) GOTO 86
DO 69 J=1,JNP
69 NE=0
60 CALL COM3(U,V,T,S,H,P,U,UPOL,VPOL,TPOL,SPOL,OPOL,JI
60 CALL COM3(U,V,T,S,H,P,U,UPOL,VPOL,TPOL,SPOL,OPOL,JI

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PSM	C	R ₆₄	No.R.	PSL	C	Re4
SAT SFA C	R ₆₄	C	R ₆₄	STH	CE	Re4
SUM	No.R.	C	R ₆₄	SF	CE	Re4
CATA	R ₆₄	C	R ₆₄	BETA	C	Re4
CON4	R ₆₄	C	R ₆₄	C0N4	C	Re4
COSL	C	R ₆₄	No.R.	C0SD	C	Re4
DATE SF	XF	R ₆₄	No.R.	DATA	C	Re4
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FAST	C	L ₆₄	No.R.	DXVP	C	Re4
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JMIN	C	I ₆₄	No.R.	I ₆₄	C	Re4
JIUS	C	I ₆₄	No.R.	JMAX	C	Re4
KSS6 SFA	C	I ₆₄	No.R.	JMS1	C	Re4
NOCS	C	I ₆₄	No.R.	JMS2	C	Re4
PHIS	C	I ₆₄	No.R.	KBS3	C	Re4
RAOT	C	I ₆₄	No.R.	KDUT	C	Re4
SINC	C	I ₆₄	No.R.	KLAY	C	Re4
TAVI F	C	I ₆₄	No.R.	NSTP	SFA	0000C
TEMP SF	C	I ₆₄	No.R.	OPOL	SFA	CE
UPDL SFA CE	C	I ₆₄	No.R.	TOP	S	CE
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DAILY SF	XF	R ₆₄	No.R.	SIM	F	Re4
IDTHR SF	C	I ₆₄	No.R.	SIMP	F	CE
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ITIME S	C	I ₆₄	No.R.	TOTN	SF	CE
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KDOPK	C	I ₆₄	No.R.	XINT FA	C	Re4
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TUST SF	C	I ₆₄	No.R.	DUMMY	C	Re4
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ADPCLD C	C	I ₆₄	No.R.	ITAU	S F	CE
CONVAL	C	I ₆₄	No.R.	NEXT	C	Re4
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ITALTER SF	C	I ₆₄	No.R.	JYEAR	C	Re4
ISTART	C	I ₆₄	No.R.	PULES	CE	CE
MATSUN SF	C	I ₆₄	No.R.	RADIN	C	Re4
MIGCAN SF	C	I ₆₄	No.R.	SEDDFF	SF	CE
NSTEPC SF	C	I ₆₄	No.R.	TOPOL	S A	CE
PHISPL	C	R ₆₄	No.R.	TOPOL	C	Re4
SINLON SF	XF	R ₆₄	No.R.	TOPOG	C	Re4
SUPNDN SF	XF	R ₆₄	No.R.	TOPOL	SF	CE
XLABEL F	C	I ₆₄	No.R.	TOPOL	SF	CE

***** COMMON INFORMATION *****

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CON2	R ₆₄	No.R.	R ₆₄	TMBAR	R ₆₄	ALPHA	R ₆₄	BETA	R ₆₄	TMCP3	I ₆₄	No.R.	I ₆₄	No.R.
IND2P1	I ₆₄	No.R.	R ₆₄	ADL CP	R ₆₄	JMS2	R ₆₄	JMS1	I ₆₄	PSKA	R ₆₄	Y/R	I ₆₄	Y/R
CPTH	R ₆₄	No.R.	R ₆₄	PSKA	R ₆₄	NRSTART	R ₆₄	NRSTART	I ₆₄	INC	R ₆₄	Y/R	I ₆₄	Y/R
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CF	I ₆₄	No.R.	R ₆₄	RADIN	R ₆₄	NRDIST	R ₆₄	NRDIST	I ₆₄	NRDIST	R ₆₄	Y/R	I ₆₄	Y/R
IND2	I ₆₄	No.R.	R ₆₄	NRDIST	R ₆₄	JNEXT	I ₆₄	NRDIST	I ₆₄	NRDIST	R ₆₄	Y/R	I ₆₄	Y/R
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JPOL	I ₆₄	No.R.	R ₆₄	PSIGN	R ₆₄	NRDIST	R ₆₄	NRDIST	I ₆₄	NRDIST	R ₆₄	Y/R	I ₆₄	Y/R
INDEX	I ₆₄	No.R.	R ₆₄	DIFF	R ₆₄	NRDIST	R ₆₄	NRDIST	I ₆₄	NRDIST	R ₆₄	Y/R	I ₆₄	Y/R
PHISPL	R ₆₄	No.R.	R ₆₄	SUM	R ₆₄	NRDIST	R ₆₄	NRDIST	I ₆₄	NRDIST	R ₆₄	Y/R	I ₆₄	Y/R

EQUIVALENED VARIABLES WITHIN THIS COMMON GROUP
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 OPOL 000414
 TPOL 000534
 TPPCL 000654

VARIABLE OFFSETS
 UPOL 000414
 UTPOL 000534
 PPOL 000654

VARIABLE INFORMATION
 005224 HEXADECIMAL BYTES

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 TMP R#4 N.R. SCHAFTA L#4 000014 ADDCLD L#4 000018

NAME OF COMMON BLOCK * S#0T*9E OF BLOCKCOMMON 03B5AB HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 SDOT L#4 000000 OMEGA 1#2 N.R. MMXTS 1#4 N.R.
 COMC 0389AA

EQUIVALENCE OF VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSETS VARIABLE OFFSETS

NAME OF COMMON BLOCK * T#NRE OF BLOCKCOMMON 083C30 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 JSP L#4 000000 JNP 1#4 000004 ISTART 1#4 000008

PTOP R#4	000100	JND 1#4	00014	NLAYP1 1#4	00014	NLAY 1#4	00014
PIN R#4	00030	NLAYM1 1#4	N.R.	NLAYP1 1#4	N.R.	JPI 1#4	N.R.
JN 1#4	00040	K4 1#4	00034	TAUT 1#4	00038	J1 1#4	0003C
WROT 1#4	000440	JTEST 1#4	00044	TEST 1#4	00048	J2 1#4	0004C
JAYS 1#4	00048	INC5 1#4	N.R.	JSB 1#4	0000AC	JNB 1#4	0000BC
DLAT R#4	2000BA	DLMN R#4	0000B6	DT R#4	0000BC	JNA 1#4	0000CC
ITAU L#4	0000C4	XINT R#4	0000C5	IDAY 1#4	0000CC	JDAY 1#4	N.R.
TODAY R#4	0000D8	NCDATE 1#4	0000D6	JDNTH 1#4	0000CC	JYEAR 1#4	N.R.
NSTEP R#4	0000F8	TAUJ 1#4	0000EC	NECOMP3 1#4	0000F4	NMDGAN 1#4	000104
TAUF R#4	000108	TAU 1#4	0000FC	TAUE 1#4	000100	TAUO 1#4	N.R.
DTNUFT R#4	000109	PI R#4	N.R.	GRAV R#4	N.R.	RGAS 1#4	N.R.
KAPA R#4	N.R.	PSL R#4	00011C	ED R#4	000120	FNU 1#4	000124
NFLB L#4	000128	PSF R#4	00012C	MRCH 1#4	N.R.	RSDLIST R#4	N.R.
SIND R#4	N.R.	COSD R#4	N.R.	FHMX R#4	N.R.	CDX 1#4	N.R.
DUNYV R#4	N.R.	TALCT R#4	00013A	DUNYVA R#4	N.R.	XLABEL R#4	N.R.
SIG R#4	000370	DSIG R#4	0003C0	SIGE R#4	N.R.	DSIGO R#4	N.R.
JIPS 1#4	N.R.	JAPS 1#4	N.R.	JIUS 1#4	N.R.	JAMS 1#4	N.R.
KSBS 1#4	N.R.	KNES 1#4	N.R.	LAT 1#4	N.R.	DXU 1#4	N.R.
DXP R#4	N.R.	DYU R#4	N.R.	DYP 1#4	N.R.	DXV 1#4	N.R.
NSKF R#4	N.R.	SIN 1#4	N.R.	V#7 1#4	N.R.	DUMY 1#4	N.R.
PHIS R#4	000D50	ALBEDG 1#2	N.R.	COSL R#4	N.R.	DUMMY 1#4	N.R.

EQUIVALENCE OF VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSETS VARIABLE OFFSETS
 0 000E70 U 000E70
 SMS 0023D0 T 0024FC
 C 000000

NAME OF COMMON BLOCK * T#NRE OF BLOCKCOMMON 081C00 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 WORKX R#4 N.R.

NAME OF COMMON BLOCK * T#NRE OF BLOCKCOMMON 081C00 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 PPU R#4 000003

EQUIVALENCE OF VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSETS VARIABLE OFFSETS
 QT 000120 U 00012C
 GW C01680 T 0017A0

NAME OF COMMON BLOCK * S#56*ME OF BLOCKCOMMON 000000 0 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 ISINTH L#4 000000 NPC 1#4 000004

NAME OF COMMON BLOCK * T#7E OF BLOCKCOMMON 003E00 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 TOPCG R#4 N.R.

NAME OF COMMON BLOCK * DS_7E OF BLOCKCOMMON 0000004 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 ISWTCG L#4 000000

NAME OF COMMON BLOCK * S#1.E OF BLOCKCOMMON 0000000 HEXADECIMAL BYTES

VAR. NAME TYPE REL. ADDR. ME	JIN 1 ⁶⁴	No.R.	VAR. NAME TYPE REL. ADDR. ME	JMAX 1 ⁶⁴	No.R.	VAR. NAME TYPE REL. ADDR. ME	JSUM 1 ⁶⁴	No.R.	VAR. NAME TYPE REL. ADDR. ME	SINTH 1 ⁶⁴	No.R.	VAR. NAME TYPE REL. ADDR. ME	VR. 1 ⁶⁴	No.R.	
NAME OF COMMON BLOCK *	*#31.E	OF BLOCKCOMMON													
VAR. NAME TYPE REL. ADDR. ME	NSEQ 1 ⁶⁴	000009	MLF 1 ⁶⁴	000004	MLF 1 ⁶⁴	000004	MLF 1 ⁶⁴	000004	MLF 1 ⁶⁴	000002C	MLFSNK 1 ⁶⁴	00002C	VAR. NAME TYPE REL. ADDR. ME	NSM1 1 ⁶⁴	000030

OPTIONS IN EFFECT* NAME= MAIN,OPT=02,LINEDIT=55,SIZE=100K.

OPTIONS IN EFFECT* SOURCE,EBCDIC,NOLIST,NODECK,LOAD,MAP,INCEDIT, ID,NOXREF

STATISTICS* SOURCE STATEMENTS = 191 PROGRAM SIZE= 4460

STATISTICS* NO DIAGNOSTICS GENERATED

*** END OF COMPIRATION *****

EVAL 19.6-APR 71

OS/360 FORTRAN H AT GISS 852K BYTES OF CORE NOT USED

DATE

LABEL	ADDR	LABEL	ADDR	LABEL	ADDR	LABEL	ADDR
MAIN	000A44	MAIN	000A62	MAIN	000B7A	MAIN	000BB2
OPT	000B9A	OPT	000D66	OPT	000DB5	OPT	000E44
INCEDIT	000C8A	INCEDIT	000F0A	INCEDIT	000F62	INCEDIT	000FAE
ID	001032	ID	00108E	ID	0010F2	ID	0011C

NAME= MAIN; OPT=02,LINECNT=55,SIZE=100K.

SOURCE,EBCDIC,NOLIST,NODECK,LOAD,MAP,INCEDIT, ID,NOXREF

ROUTINE DAILY NAME= MAIN; OPT=02,LINECNT=55,SIZE=100K.

ROUTINE NINE LAYER GLOBAL CODE BLOCK FOR VM MODEL. FEBRUARY 1976

REAL*8 STINSON,COLSON,SUM

COMMON/FOURTH/CON1,CON2,CON3,CON4,CONS,TBAR,ALPHA,BETA,A,IND2PI.

S IND2,RADIN,END(2),JP1,JP2,MATSN,CNST,INSTARI,CPD2.

S ALBEDO,REAL*4 KAPALLA.

S IND2,JMS1,JMS2,JMS3,CPTK,PSKAP,A,IND2PI.

S JMOD(2,2),JMOD(2,2),SINLON(72),COLSON(72),INDEX(72).

S PSIGN(4),POLES(1,4,81),W(72,9,5),PKL72,9,3,I,DIFF(9).

S CONVPL(9),SDPOL(9,21),PHISPL(21),SUM(2,5).

S EQUIVALENCE (POLE(1,1),POLES(1,1),(QIPOLI(1,1),POLES(1,1)),(TPOL(1,1),POLES(1,1)),(UPOL(1,1),POLES(1,1)),(VPOL(1,1),POLES(1,1)),(UTPOL(1,1),POLES(1,1)),(MTPOL(1,1),POLES(1,1)),(STMPOL(1,1),POLES(1,1)),(PTE(1,1),POLE(1,1)),(PPOL(1,1),POLE(1,1)),(VOL(36,1),VOL(36,1),TPOL(1,1)).

S SHPOL(36,1),APOL(94,21),UTPOL(12),UTPOL(36,1),VTPOL(36,1),UTPOL(36,1),VTPOL(36,1),UTPOL(36,1),VTPOL(36,1).

S SHTPOL(36,1),QIPOL(9,4,2),UT(72,10,4,1).

COMMON /CNTRL/

* JSP,JND,IM,NLAY,PTOP,ISTART,JSFPI,JPNPI,FIN,NLAYM,NLAYPI.

* J1,JH,KH,TAUT,IROT,WROT,JTEST,ITEST.

* NR,JAYS(1,12),NCS(1,1),JSB,JNB,DLAT,DLON.

* DT,TAU,ITAU,XINT,TDAY,JOA,TOFCY,DAE,TAU,DTAU.

* NCYCLE,NCOMP3,NMOLG,ANAGAN,AUTPAUT,LT,TAUE,TALD,DTMUL.

* PI,GRAV,ORGASKAP,PSL,ED,FNU,NFLW,PSF,ORCH,RSDIST,SIND,CSOD.

* RHMAX,CDX,DUNNYC(1,8),IATER,DUNNYA(99).

* XLABEL(20),SIG(20),DSIG(20),SIG(21),DEIGO(19).

* JIPS(1,1),JMS(1,1),JAS(1,1),JMU(1,1),KSE(1,1),KBS(1,1).

* LAT(4,6),DXL(4,6),DXP(4,6),DY(4,6),CY(4,6),LY(4,6),LXP(4,6),SINL(4,6).

* CCSL(4,6),DUNNY(72),PHIS(288,46),ALBEDO(72,46).

DIMENSION UT(2,40,1),V(72,40,1),UT(72,40,1),SM(72,40,1).

SP2880,11,SHS(2880,11),GHS(2880,11),GWS(2880,11),C(3000).

EQUIVALENCE V(1,1),PHIS(1,1),PHIS(1,1),LHS(1,1),PHIS(1,1),PHIS(1,1).

V(1,1,1),PHIS(1,1,1),PHIS(1,1,1),PHIS(1,1,1),PHIS(1,1,1).

S (T1,1,1),PHIS(1,1,1),PHIS(1,1,1),PHIS(1,1,1),PHIS(1,1,1).

S (SH(1,1,1),PHIS(2233,11),UT(1,1,1),PU(1,1,1),GT(1,1,1),GCH(1,1,1).

S PU(1,1,1),C(1,1,1),JSP)

COMMON /WORK2/PU(2880,46)

INTEGER,AMONTH,DAYSPW,DAYSPV

DIMENSION AMONTH(12,12),DAYSPW(12)

DATA AMONTH/ JANU , FEBR , MARCH , APRIL , MAY , JUNE , JULY , AUGUST , SEPT , OCT , NOVEMBER , DECE /.

S *MBER/*

DATA DAYSPW/31,28,31,30,31,30,31,30,31,30,31,30/

DATA IDAYW/30,31,30,31,30,31,30,31,30,31,30,31/

DATA SOLS/ APHEL,ECZN/173**183...0179/

IFIRST=0

C**** CALCULATE GLOBAL MEAN SURFACE PRESSURE

C * * *

ISN 0012 5 SARE=0.

ISN 0013 SMASS=0.

ISN 0014 INC1.

ISN 0015 FINC1.

DO 20 J=2,JM

SPPRESS=0.

DO 10 I=INC1,IM,INC

SPPRESS=SPPRESS+(I,J)

SARE=SAREA+DXPI*(J)*FIN

SMASS=SMAS+(DXPI*(J)*FIN)

DAP = 4 * PI * SIN(S*5*DLAT) ** 2

20 IFIRST=0

```

SAREA = SAREA + 2.0 * DAP
SMSS = SMSS + DAP * (PPDL(11) + PPDL(12))
PBAR=SMSS/SAREA/PPTOP
IFI1IFI2=NE.11 GO TO 20
PBF=PBAR
GO TO 50
DELTAP=PSF-PBAR
DO 40 I=1,1M
DO 40 J=1,JNP
40 PI1,J1=PI,J1+DELTAP
WRITE *,3,9011 DELTAP
CALCULATE CALENDAR
50 JYEAR=11+IDAY/DAY0-11/DAYSPY
DAY=(DAY+IDAY-DAYSPY)*JYEAR-11
J=0
DO 60 MONTH=1,12
J=J+DAYS(MONTH)
IFI1JDAY.LE.J1 GO TO 70
CONTINUE
60 WRITE (3,9021) JDAY
DATE=J-(J-DAYSPY(MONTH))
MONTH(1)=MONTH(1)-MONTH(2)
MONTH(2)=MONTH(2)-MONTH(1)
70 WRITE (3,9021) JDAY
CALCULATE ORBIT POSITION
FDAY=JDAY
SEASON=(FDAY-SOLST)/DAYSPY
DIST=(FDAY-APHEL)/DAYSPY
DECMAX=COS(2*PI*SEASON)
RSDIST=(1.0+ECCN*CD(S(2.0*PI*DST)))*2
SIND=SIN(IDE)
COSD=COS(IDE)
CALL NEWDAY(JDAY)
RETURN

ENTRY DAILY
IFI1ISTARTOLE.4) GO TO 50
IFI1ST=1
50 DO 5
901 FORMAT 10,0 PRESSURE ADDED IN GMP IS.0.F10.0
902 FORMAT 10,0 END

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067C HEX	
E	000120
N	000B40
R	00139C
S	000004
A	000050
M	000130
D	000950
H	000144
T	000438
L	000168
C	000150
I	000534
O	00057C
P	000000
F	000168


```

ISN 0102 WRITE '6.901' IVER
ISN 0103 READ '(5.902)' XLABEL
ISN 0104 C***** WRITE '(3.903)' XLABEL
ISN 0105 COPY INPUT NAMELIST CNTG CORE TAPE AND TITLE PAGE
ISN 0106 20 READ '(5.904)' RECORD
ISN 0107 BRITE '(11.904)' RECORD
ISN 0108 WRITE '(3.905)' RECORD
ISN 0109 IF(IRECORD<1) ONE. ANDEND! GO TO 20
ISN 0110 READ'(11.1' INPUTJ)
ISN 0111 IF(ISTART.EQ.7. AND.PAIZE.NE.0.) WRITE '(11.538)' I START
ISN 0112 IFL(ISTART.EQ.7. AND.PAIZE.NE.0.) WRITE '(11.538)' I START
ISN 0113 READ IN VARIABLE ALBEDO
ISN 0114 C**** READ'(10.1' ALBEDO,J=J1..JNP).I=1..IM)
ISN 0115 READ'(10.1' SURFACE GEOPOTENTIAL
ISN 0116 C**** READ'(17.1' PHIS(J1..J).J=J1..JNP).I=1..IM)
ISN 0117 READ'(17.1' (TOPDG(J1..J).J=J1..JNP).I=1..IM)
ISN 0118 ISN 0119 MELTE 619001.(J..PHIS(J1..J).I=1..IM).J=1..JNP
ISN 0120 1900 FORMAT(1X,46) J=1..JNP. PHIS((J,I)=/9(1X,3E13,6/1/1
ISN 0121 WRITE 619411.(J..(ALBEDO(J,I).I=1..IM).J=1..JNP)
ISN 0122 1941 FORMAT(1X,46).J=1..IM).PAUSE * ALBEDO(J,I)=/2(1X,3.6E13,1/1)
ISN 0123 MNMXTS = TAUT + XINT + *01
ISN 0124 IF(PAUSE.EQ.1*) PAUSE * MOUNT TAPE$:
ISN 0125 CALL LSSTCH ('5. KSSW5')
ISN 0126 ISN 0127 IF(KSSW5.EQ.1) I START=8
ISN 0128 KTR=8
ISN 0129

C * * * ON INITIAL START ENDFILE MODEL OUTPUT TAPE
ISN 0130 IF(ISTART.GE.5. AND.ISTART.LE.7) ENDFILE PTR
ISN 0131 GO TO (30.120,120,40,110,110,40,50,90).I START
ISN 0132 C*** 30 STOP
ISN 0133 C*** SET DEPENDENT QUANTITIES
ISN 0134 40 DLATDPI/JN
FIM=M
ISN 0135 ISN 0136 DLATDPI/JN
KME=4BNLAY+5
ISN 0137 KME=4BNLAY-4
ISN 0138 ISN 0139
ISN 0140 ISN 0141 ISN 0142 ISN 0143 ISN 0144 ISN 0145 ISN 0146 ISN 0147 ISN 0148 ISN 0149
ISN 0150 ISN 0151 ISN 0152 ISN 0153 ISN 0154 ISN 0155 ISN 0156 ISN 0157 ISN 0158 ISN 0159
ISN 0160 ISN 0161 ISN 0162 ISN 0163 ISN 0164 ISN 0165 ISN 0166 ISN 0167 ISN 0168
ISN 0169 ISN 0170 ISN 0171 ISN 0172 ISN 0173 ISN 0174 ISN 0175 ISN 0176 ISN 0177 ISN 0178 ISN 0179
ISN 0180 ISN 0181 ISN 0182 ISN 0183 ISN 0184 ISN 0185 ISN 0186 ISN 0187 ISN 0188 ISN 0189

C * * * IF(DSIG(1)*NE.0.) GO TO 60
DO 50 L=1..NLAY
 50 DSIG(L)=1./NLAY
 60 SIGEL=L
DO 70 L=1..NLAY
 70 DSIG(L)=SIGEL+DSIGEL(L+1)
SIGEL=5*(SIGEL(L)+SIGEL(L+1))
DO 80 L=1..NLAYM
 80 DSIG(L)=SIGEL(L+1)-SIGEL(L)
IF(ISTART.EQ.6.) GO TO 120
IF(ISTART.EQ.7.) GO TO 110
 90 MACHINE CHECK RESTART. ISTART = -6 OR 9
 90 IF(SIGEL(5)NE.1) GO TO 100
 90 WRITE '(15.906)' TAPNUM
 90 READ '(15.907)' TAPNUM
 100 TAUP=TAPU AND(TAPU,TAUT)
 100 WRITE '(3.910)' TAPNUM
 100 READ TAPE ON UNIT KTR
 100 KTR=2
 100 IROT=1
 100 TAU=TAU1
 100 IF(TAU.PT.LT.0.) TAUP=TAU1
 100 TAPNUM=DISK
 100 IF(PAIZE.EQ.0.) GO TO 120
 100 WRITE '(15.909)' TAPNUM
 100 READ '(15.902)' TAPNUM
 100 WRITE '(3.910)' TAPNUM
 100 READ TAPE ON UNIT KTR
 100 KTR=2
 100 IROT=1
 100 TAU=TAU1
 100 IF(TAU.PT.LT.0.) TAUP=TAU1
 100 TAPNUM=DISK
 100 IF(ISTART.LE.4) GO TO 120
 100 IF(TAU.X.LE.TAU.PT.) GO TO 120
 100 IF(TAU.X.LE.TAU.PT.+01) GO TO 120
 100 CONTINUE
 100 WRITE '(6.912)' TAUP

C 120 READ(KTR,ERR=800,END=130)TAUX.C1,(P111..J).J=1..JNP).I=1..IM).
S (ITS1..J).J=1..JNP).I=1..IM).I(SHS1..J).J=1..JNP).I=1..IM).
S CALL RDTAPE(KTR)
S IF(ISTART.LE.4) GO TO 120
S IF(ISTART.LE.4) GO TO 120
S IF(TAU.X.LE.TAU.PT.) GO TO 120
S IF(TAU.X.LE.TAU.PT.+01) GO TO 120
S CONTINUE

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**ORIGINAL PAGE IS
OF POOR QUALITY**

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ISN 0190 CALL EXIT
ISN 0191 C 130 IF(ISTART.EQ.5)GOTO 830
ISN 0192 BACKSPACE KTR
ISN 0193 TAU=TAU
ISN 0194 TAU=TAU
ISN 0195 DO 145 J=J1,JM
ISN 0196 DO 145 J=J1,JM
ISN 0197 BACKSPACE KTR
ISN 0198 BACKSPACE KTR
ISN 0199 BACKSPACE KTR
ISN 0200 IROT=IROT-1
ISN 0201 IF(ISTART.EQ.4)OR(ISTART.EQ.7) GC TO 160
ISN 0202 C*** COPY C ARRAY FROM C1 ARRAY
ISN 0203 C1:6=C1:6
ISN 0204 DO 150 K=1,300
ISN 0205 CTK=CLK1
ISN 0206 IF(ISTART.EQ.2)OR(ISTART.EQ.5) GC TO 160
ISN 0207 REM IND(L1)
ISN 0208 READ(L1,INPUT2)
ISN 0209 C*** IND(L1,INPUT2)
ISN 0210 IF(CTR.EQ.8) XLABEL=C1(116)
ISN 0211 IF(CTR.EQ.8) XLABEL=C1(1220)
ISN 0212 IF(CTR.EQ.12) XLABEL=C1(1220)
ISN 0213 XLABEL=C1(1220)=TAPNU
ISN 0214 CALCULATE DISTANCE PROJECTION ARFA'S
ISN 0215 FJEQ=S(JSP+JNP)
ISN 0216 DO 200 J=1,JNP
ISN 0217 LAT(LJ)=DLAT(LJ-FJEQ)
ISN 0218 DO 210 J=1,JNP
ISN 0219 SIN(LJ)=SINLAT(JJ)
ISN 0220 COS(LJ)=COSLAT(JJ)
ISN 0221 DO 220 J=1,JN
ISN 0222 DOXP(LJ)=RADDLON*COSL(JJ)
ISN 0223 DOXP(LJ)=RADDLON*COSL(JJ)
ISN 0224 DO 230 J=2,JN
ISN 0225 DOXP(LJ)=RAD*DLAT
ISN 0226 DOXP(LJ)=RAD*DLAT
ISN 0227 DVUL(JJ)=RADLAT(LJ)-LAT(JJJ)
ISN 0228 C 230 CONTINUE
ISN 0229 JNPPI=JNP+1
ISN 0230 DO 240 J=2,JNPID2
ISN 0231 DXP(JJ)=120.*DVUL(JJ)*DVUL(JJ)
ISN 0232 DOXP(JNP1-JJ)=DXVP(JJ)
ISN 0233 DXP(JJ)=0.
ISN 0234 WRITE(3,220)(DXVP(JJ),J=1,JNP)
ISN 0235 FORMAT(IX,DXVP=/(IX,SE16.8))
ISN 0236 RETURN
C * * * AUG 23 1977 ADDITIONS HERE TILL RETURN
C
ISN 0237 INC = 1
ISN 0238 BETA = 0. - 2.*ALPHA
ISN 0239 FSD6 = 5. / 6.
ISN 0240 F17 = 17. / 18.
ISN 0241 F98 = .325 / .981.
ISN 0242 R*RGAS
ISN 0243 RADIM = 3.*RAD*IN
ISN 0244 CON1 = 0.*COTAN(.3*DLAT)/RADIM
ISN 0245 CON2 = -(COTAN(DLAT))/RADIM
ISN 0246 CON5 = 1./RADIM*DLAT
ISN 0247 INC = 1.
ISN 0248 JPOL(1,1) = 2
ISN 0249 JPOL(2,1) = 3
ISN 0250 JPOL(1,2) = JM - 1
ISN 0251 JPOL(2,2) = JM
ISN 0252 JPMD(1,1) = 2
ISN 0253 JPMD(2,1) = 3
ISN 0254 JPMD(1,2) = MOD(JM-1,5) + 1
ISN 0255 JPMD(2,2) = MOD(JM-2,5) + 1
ISN 0256 JPDK(1,1) = 2
ISN 0257 JPDK(2,1) = MOD(JM-1,3) + 1
ISN 0258 JPDK(1,2) = MOD(JM-2,3) + 1
ISN 0259 JPDK(2,2) = MOD(JM-2,3) + 1
ISN 0260 JNP=JM+
ISN 0261 JEND(1) = 1
ISN 0262 JEND(2) = JNP
ISN 0263 JNEXT(1) = 2
ISN 0264 JNEXT(2) = JM
ISN 0265 ADLP = 12.*RAD*DLAT*DLON
ISN 0266 IMD2=IM2
ISN 0267 IMU2P1 = 1ND2 + 1
ISN 0268 JMS1 = JM - 1
ISN 0269 JM2 = JM - 2
ISN 0270 JSM2=6
ISN 0271 JMIN = 2 + JSMT
ISN 0272 JMAX = JM - JSMT
ISN 0273 JSUM = JMAX + JMIN
ISN 0274 TWOJM = 2.*JM
ISN 0275 JLM = JMIN - 1
ISN 0276

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ISN 0277      DO 301 I = 1, JLM
ISN 0278      JDH = JMAX + - JMIN
C           IF( J .GE. JMIN )          JDH= JMAX + - JMIN
C           IF( J .LT. JMAX )        JDH= JMAX + - JMIN
C           IF( J .EQ. JMAX )        JDH= JMAX + - JMIN
C           IF( J .EQ. JMIN )        JDH= JMAX + - JMIN
ISN 0279      IMAX=INT(AC*COSL(JDH))
ISN 0280      IMAXL = IMAX - 1
ISN 0281      IMAXP3=IMAX+4
C
ISN 0282      DO 310 I = 1, IMD2
C           IF( I .LE. IMAX )        SINTH(I,J) = -FLOAT(I-IMAXL)/6.
C           IF( I .GT. IMAXP3)      SINTH(I,J) = 0.
C           CONTINUE
C           CONTINUE
ISN 0283      PIKAPA = KAPA + 1
ISN 0284      DO 320 L = 1, NAY
C           DIFF(L) = PIKAPA * DSIG(L)
C           CONTINUE
ISN 0285      PSKAPA = EXPBYK(1000.)
ISN 0286      TMBAR = 280. / PSKAPA
ISN 0287      CP = RGAS / KAPA
ISN 0288      CPD2=5. * CP
ISN 0289      CPTH = CP * TMBAR
ISN 0290      WRITE(6,778)PSKAPATMBAR,RGAS,KAPA,CP,CFTH
ISN 0291      FORMAT(IX,0. PSKAPATMBAR,RGAS,KAPA,CP,CFTH(10,6E15,0)
ISN 0292      PMISPL1 = PHIS(I,1)
ISN 0293      PMISPL2 = PHIS(I,2)
ISN 0294      PMISPL3 = PHIS(I,3)
ISN 0295      INDX1 = IM
ISN 0296      INDX2 = 2*IM
ISN 0297      TWOPI = 2.*PI
ISN 0298      DO 1090 I = 1, IMD2
ISN 0299      ALONG = FLOAT(I-1) * TWOPI / FLOAT(IM)
ISN 0300      C           * * * ALONG = FLOAT(I-1) * TWOPI / FLOAT(IM)
ISN 0301      C           * * * ALONG = FLOAT(I-1) * TWOPI / FLOAT(IM)
ISN 0302      C           * * * ALONG = FLOAT(I-1) * TWOPI / FLOAT(IM)
ISN 0303      C           * * * ALONG = FLOAT(I-1) * TWOPI / FLOAT(IM)
ISN 0304      C           * * * ALONG = FLOAT(I-1) * TWOPI / FLOAT(IM)
ISN 0305      C           * * * ALONG = FLOAT(I-1) * TWOPI / FLOAT(IM)
ISN 0306      C           * * * ALONG = FLOAT(I-1) * TWOPI / FLOAT(IM)
ISN 0307      C           * * * ALONG = FLOAT(I-1) * TWOPI / FLOAT(IM)
ISN 0308      SINLON11 = -DSIN(ALONG)
ISN 0309      COSLON11 = -DCOS(ALONG)
ISN 0310      SINLON1(MD2+1) = -SINLON(1)
ISN 0311      COSLON1(MD2+1) = -COSLON(1)
ISN 0312      INDEK(I,1) = 1 + IMD2
ISN 0313      INDEK(I,MD2+1) = 1
ISN 0314      OHM2=2.*TWOPI/SDAY
ISN 0315      DO 1310 J=1, JM
ISN 0316      F(J,J)=OHM2*SINL(J)
ISN 0317      CONTINUE
ISN 0318      1010  F(JNP1-OHM2,
ISN 0319      DSIGN(1) = -1.
ISN 0320      DSIGN(2) = -1.
ISN 0321      DSIGN(3) = 1.
ISN 0322      DSIGN(4) = 1.
ISN 0323      C           * * * INITIAL VELOCITIES GIVEN ON A STAGGERED GRID.
ISN 0324      C           * * * INTERPOLATION TO UNSTAGGERED GRID IS USED.
ISN 0325      C           * * * MAKE USE OF EQUIVALENCING AND OVERAPPING THE U ARRAY.
ISN 0326      DO 1015 M=1,2
ISN 0327      NM2=N-2
ISN 0328      DO 1018 L=1, NAY
ISN 0329      IF( (ISART,EG,7)GO TO 1017
ISN 0330      Q11,L,NM2,JEND(M)=Q11,L,NM2,JEND(M)
ISN 0331      Q11,L,N,JEND(M)=Q11,L,N,JEND(M)
ISN 0332      CONTINUE
ISN 0333      1017  DO 1015 I=1, IN
ISN 0334      PK1,JEND(M)=PT1,JEND(M)
ISN 0335      CONTINUE
ISN 0336      DO 1020 J = 2, JM
ISN 0337      JP1 = J + 1
ISN 0338      DO 1025 N = 1, 2
ISN 0339      NP2 = N + 2
ISN 0340      DO 1025 L = 1, NAY
ISN 0341      ISL1 = IM
ISN 0342      DO 1025 I = 1, IN
ISN 0343      Q11,LNP2,J=Q11,L,NP2,J
ISN 0344      IF( (ISART,EG,7)GO TO 1026
ISN 0345      Q11,I,N,J)=Q11,I,N,J+Q11,I,L,N,J+Q11,I,L,N,J+ +
ISN 0347      Q11,I,L,N,J=Q11,I,L,N,J+Q11,I,L,N,J
ISN 0348      ISL1 = 1
ISN 0349      GO TO 1025
ISN 0350      Q11,I,N,J=Q11,I,L,N,J
ISN 0351      1026  CONTINUE
ISN 0352      DO 1030 I = 1, IN
ISN 0353      PI1,I,J=PT1,I,J
ISN 0354      1025  CONTINUE
ISN 0355      C           * * * SCALE UT
ISN 0356      C           * * *

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ISN 0355 DO 1020 N = 1.4
ISN 0356 DO 1020 L = 1.4
ISN 0357 DC 1020 I = 1.4
ISN 0358 QTR(L,N,J) = DXP(L,J) * P(I,J) * Q(I,L,N,J)
ISN 0359 1020 C * * * COMPUTATION OF STEREOGRAPHIC POLAR VELOCITIES: UPOL(L,M).
C * * * UPOL(L,M). WHERE M=1 CORRESPONDS TO SOUTH POLE.

ISN 0360 DO 1040 M = 1.2
ISN 0361 COEF1 = -1.0
ISN 0362 DO 1040 L = 1.4
ISN 0363 IF(ISTARTNE,7) GO TO 1052
ISN 0364 S1 = 0.
ISN 0365 S2 = 0.
ISN 0366 DO 1050 I = 1.4M
ISN 0367 S1 = S2 + COEFL*I(L,JNEXT(M)) * SINL(N) - COEF1 * VI(L,JNEXT(M))
ISN 0368 S2 = S1 / FLOAT(I,M) CONTINUE
ISN 0369 1050 UPOL(L,M) = S1 / FLOAT(I,M) * COSL(N) - VI(L,JNEXT(M)) * SINL(N)
ISN 0370 UPOL(L,M) = S2 / FLOAT(I,M)
ISN 0371 ISN 0372 UPOL(L,M) = P(I,JEND(M))
ISN 0373 GO TO 1053
ISN 0374 1052 UPOL(L,M) = -U(I,L,JEND(M)) * SINL(N) - COEF1 * VI(L,JEND(M)) * COSL(N)
ISN 0375 1 VPOL(L,M) = -U(I,L,JEND(M)) * COSL(N) + VI(L,JEND(M)) * SINL(N)
ISN 0376 1053 CONTINUE
TPOL(L,M) = T(I,L,JEND(M))
ISN 0377 SHPOL(L,M) = SH(I,L,JEND(M))
ISN 0378 FPOL(M) = P(I,JEND(M))
ISN 0379 WRITE(6,1968) M,L,PPOL(M),*(OPOL(L,N,M)*N1.4)
ISN 0380 PTPOL(M)=PPOL(M)*OPOL(M)=FPOL(M)
ISN 0381 1968 FORMAT(IX,*,PDL,M)
ISN 0382 PTPOL(M)=PPOL(M)*OPOL(M)=FPOL(M)
ISN 0383 DO 1045 QTPOL(N,M) = OPOL(N,M) * PTPL(N)
ISN 0384 C * * * THE QTPL(N,M) = UPOL(L,M) * SINL(N) * COEF1 * UPOL(L,M) * COSL(N)
C * * * WITH THE PROCEDURE USED IN COMPO AGREES
ISN 0385 DO 1040 I=1,IN
ISN 0386 IF(I,STARTNE,7) GO TO 1054
ISN 0387 VI(L,JEND(M))=--COEF1*UPOL(L,M)*COSL(N)-UPOL(L,M)*SINL(N)
ISN 0388 1044 CONTINUE
ISN 0389 DO 1040 N = 1.4
ISN 0390 1054 QTR(L,N,JEND(M)) = Q(I,L,N,JEND(M)) * PPL(M)
ISN 0391 Ceeee ERROR ENCOUNTERED READING TAUP
ISN 0392 Ceeee CALL EXIT
ISN 0393 Ceeee END-OF-FILE ENCOUNTERED READING LATITUDE RECORD ON UNIT KTR
ISN 0394 Ceeee STOP
ISN 0395 800 WRITE(3,911)
ISN 0396 Ceeee CALL EXIT
ISN 0397 ISN 0398 Ceeee ERROR ENCOUNTERED READING LATITUDE RECORD ON UNIT KTR
ISN 0399 Ceeee WRITE(3,916)
ISN 0400 Ceeee CALL EXIT
ISN 0401 ISN 0402 Ceeee LATER PICKUP TAPE NEEDED
ISN 0403 Ceeee WRITE(3,913)
ISN 0404 Ceeee CALL EXIT
ISN 0405 901 FORMAT(1/40X,0,GISS N LAYER WEATHER MODEL//100X,0,VERSION 10.1)
ISN 0406 SCS FORMAT(1/20A4)
ISN 0407 503 FORMAT(25X,20A4)
ISN 0408 504 FORMAT(10A6)
ISN 0409 505 FORMAT(13X,10A8)
ISN 0410 907 * EGA .4026.2 AS 04.026.20*
ISN 0411 508 FORMAT(1F8.2)
ISN 0412 SCS FORMAT(1/20A4)
ISN 0413 * NUMBER. * ENTER THE NUMBER OF THE NEW OUTPUT TAPE AS A FOUR DIGIT
ISN 0414 S10 FORMAT(1V//)
ISN 0415 * ERROR ENCOUNTERED READING TAUP, C RECORD ON UNIT KTR. *
ISN 0416 S11 FORMAT(1V//)
ISN 0417 S12 FORMAT(1V//)
ISN 0418 910 * OLDER PICKUP TAPE NEEDED. TAUP = F10.2*
ISN 0419 911 FORMAT(1V//)
ISN 0420 912 * REGION SPLIT GRID LIMITS JIP=1115.31X.0
ISN 0421 913 FORMAT(1V//)
ISN 0422 914 * ERROR ENCOUNTERED READING LATITUDE RECORD ON UNIT KTR.
ISN 0423 915 FORMAT(1V//)
ISN 0424 916 FORMAT(1V//)
ISN 0425 917 FORMAT(1V//)
ISN 0426 918 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
ISN 0427 919 FORMAT(1V//)
ISN 0428 920 FORMAT(1V//)
ISN 0429 921 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
ISN 0430 922 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
ISN 0431 923 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
ISN 0432 924 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
ISN 0433 925 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
ISN 0434 926 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
ISN 0435 927 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
ISN 0436 928 FORMAT(1V//)
ISN 0437 929 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
ISN 0438 930 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.
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ISN 0539 1031 * BEING END-OF-FILE ENCOUNTRED READING LATITUDE RECORD ON UNIT KTR.

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NAME		TAG		TYPE		ADD.		NAME		TAG		TYPE		ADD.		NAME		TAG		TYPE		ADD.					
/	INPUT /	SIZE OF PROGRAM		003100		HEXADECIMAL BYTES		/		NAME		TAG		TYPE		ADD.		NAME		TAG		TYPE		ADD.			
NAME	TAG	TYPE	ADD.	R#4	000003	Z	NAME	TAG	TYPE	ADD.	R#4	000001	I	SFA	R#4	00066C	I	SFA	R#4	0000670	N	NAME	TAG	TYPE	ADD.		
C SF	CE	F	S	I#4	000671	L	SF	C E	F	S	I#4	000672	M	SF	R#4	000067C	I	SFA	R#4	000067E	N	SF	C E	F	R#4		
K SF	CE	F	S	I#4	002F10	J	SF	CE	F	S	I#4	00013C	K	SF	R#4	0000680	C	SF	R#4	0000680	CP	SF	CE	F	R#4		
P SF	CE	F	S	I#4	000570	D	SF	CE	F	S	I#4	00008C	O	SF	R#4	0000684	I	SFA	R#4	0000684	JM	SF	CE	F	R#4		
C1 SF	CE	F	S	I#4	00748	I	SF	CE	F	S	I#4	00009C	N	SF	R#4	0000688	M	SF	R#4	0000688	JN	SF	CE	F	R#4		
GW SF	CE	F	S	I#4	001680	K	SF	CE	F	S	I#4	000034	P	SF	R#4	0000692	N	SF	R#4	0000692	PU	SF	CE	F	R#4		
J1 SF	CE	F	S	I#4	00010C	PK	SF	CE	F	S	I#4	00004C	R#4	000120	PT	SF	C	SF	R#4	0000696	SF	SF	CE	F	R#4		
PI SF	CE	F	S	I#4	000120	SH	F	CE	R#4	00303C	R#4	00006AC	S1	SF	R#4	0000698	UT	SF	CE	R#4	0000698	S2	SF	CE	F	R#4	
QT SF	CE	F	S	I#4	001891	TT	CE	R#4	000726	DXP	SF	C	R#4	000728	DXU	S	FIN	S	00006A4	VT	SF	CE	F	R#4			
TS S	C	R#4	001891	DPI	SF	C	R#4	000726	FAC	SF	C	R#4	000728	FIN	S	GSM	S	00006A4	OXU	S	CE	F	R#4				
COX S	C	R#4	001891	PSH	SF	C	R#4	000726	F98	SF	C	R#4	000728	GSM	S	INC	S	00006A4	PI	S	CE	F	R#4				
DYP	S	C	R#4	001891	SHT	S	C	R#4	000726	BETA	S	R#4	000728	INC	S	CON3	S	00006A4	NE	R#4	00006A4	CON4	S	CE	F	R#4	
SM S	CE	R#4	0023D0	TNP	S	C	R#4	000726	COND	S	R#4	000728	CON3	S	CDSL	S	00006A4	NE	R#4	00006A4	CDL2	S	CE	F	R#4		
TAU S	S	C	R#4	0000C0	CGN2	S	C	R#4	000726	DISK	SF	R#4	000728	CDL2	SF	DISK	S	00006A4	NE	R#4	00006A4	DISK	S	CE	F	R#4	
CON1 S	S	C	R#4	0000C0	COSD	S	C	R#4	000726	DXYP	SF	R#4	000728	DISK	SF	DXYP	SF	00006A4	NE	R#4	00006A4	DXYP	SF	CE	F	R#4	
CONS S	S	C	R#4	0000C0	DODF	S	C	R#4	000726	FS6	SF	R#4	000728	DXYP	SF	FS6	SF	00006A4	NE	R#4	00006A4	FS6	SF	CE	F	R#4	
CPTH SF	SF	C	R#4	0000C0	DSIG	SF	C	R#4	000726	IND2	SF	R#4	000728	FS6	SF	IND2	SF	00006A4	NE	R#4	00006A4	IND2	SF	CE	F	R#4	
DLOH SF	SF	C	R#4	0000C0	F7EQ	SF	C	R#4	000726	INCU	S	R#4	000728	IND2	SF	INCU	S	00006A4	NE	R#4	00006A4	INCU	S	CE	F	R#4	
DLON SF	SF	C	R#4	0000C0	FMAX	SF	C	R#4	000726	JAYS	S	R#4	000728	INCU	S	JAYS	S	00006A4	NE	R#4	00006A4	JAYS	S	CE	F	R#4	
FAST S	C	R#4	0000C0	INCS	S	C	R#4	000726	JMAX	SF	R#4	000728	JMAX	SF	JMAX	SF	00006A4	NE	R#4	00006A4	JMAX	SF	CE	F	R#4		
IDAY S	C	R#4	0000C0	IVER	F	C	R#4	000726	JNS2	S	R#4	000728	JNS2	S	JNS2	S	00006A4	NE	R#4	00006A4	JNS2	S	CE	F	R#4		
INCP	S	C	R#4	0000C0	JLIM	SF	C	R#4	000726	JSUM	S	R#4	000728	JSUM	S	JSUM	S	00006A4	NE	R#4	00006A4	JSUM	S	CE	F	R#4	
ITAU	S	C	R#4	0000C0	JSM1	SF	C	R#4	000726	KNN4	S	R#4	000728	KNN4	S	KNN4	S	00006A4	NE	R#4	00006A4	KNN4	S	CE	F	R#4	
JEND SF	SF	C	R#4	0000C0	KAP1	SF	C	R#4	000726	KRDT	S	R#4	000728	KRDT	S	KRDT	S	00006A4	NE	R#4	00006A4	KRDT	S	CE	F	R#4	
JNPS S	SF	C	R#4	0000C0	KRCH	S	C	R#4	000726	KTAU	SF	R#4	000728	KTAU	SF	KTAU	SF	00006A4	NE	R#4	00006A4	KTAU	SF	CE	F	R#4	
JPLS S	SF	C	R#4	0000C0	KTAY	SF	C	R#4	000726	KVOL	S	R#4	000728	KVOL	S	KVOL	S	00006A4	NE	R#4	00006A4	KVOL	S	CE	F	R#4	
JLUS	S	C	R#4	0000C0	KUPL	S	C	R#4	000726	KYAP	S	R#4	000728	KYAP	S	KYAP	S	00006A4	NE	R#4	00006A4	KYAP	S	CE	F	R#4	
KBLS S	S	C	R#4	0000C0	KYCH	S	C	R#4	000726	KYUP	S	R#4	000728	KYUP	S	KYUP	S	00006A4	NE	R#4	00006A4	KYUP	S	CE	F	R#4	
NFLN S	S	C	R#4	000128	KZSU5	S	C	R#4	000726	LADNG	S	R#4	000728	LADNG	S	LADNG	S	00006A4	NE	R#4	00006A4	LADNG	S	CE	F	R#4	
NSMI S	S	C	R#4	000128	PAZSE	S	C	R#4	000726	LSIGO	S	R#4	000728	LSIGO	S	LSIGO	S	00006A4	NE	R#4	00006A4	LSIGO	S	CE	F	R#4	
PTDP S	S	C	R#4	000128	PTDP	S	C	R#4	000726	PTJUL	S	C	R#4	000728	PTJUL	S	PTJUL	S	00006A4	NE	R#4	00006A4	PTJUL	S	CE	F	R#4
SDAV SF	SF	C	R#4	0006DC	ISMP1	S	C	R#4	000726	SPOL	S	C	R#4	000728	SPOL	S	SPOL	S	00006A4	NE	R#4	00006A4	SPOL	S	CE	F	R#4
SINL SF	SF	C	R#4	0006DC	ISNTM	S	C	R#4	000726	SPOL1	S	C	R#4	000728	SPOL1	S	SPOL1	S	00006A4	NE	R#4	00006A4	SPOL1	S	CE	F	R#4
TAUO S	C	R#4	0006F4	JNEXT SF	C	R#4	000726	SPOL2	S	C	R#4	000728	SPOL2	S	SPOL2	S	00006A4	NE	R#4	00006A4	SPOL2	S	CE	F	R#4		
TPDOL S	C	R#4	0006F4	TAUO	S	C	R#4	000726	SPOL3	S	C	R#4	000728	SPOL3	S	SPOL3	S	00006A4	NE	R#4	00006A4	SPOL3	S	CE	F	R#4	
JYEAR	S	C	R#4	0006F4	SPOL4	S	C	R#4	000726	SPOL5	S	C	R#4	000728	SPOL5	S	SPOL5	S	00006A4	NE	R#4	00006A4	SPOL5	S	CE	F	R#4
OMEGA	S	C	R#4	0006F4	SPOL6	S	C	R#4	000726	SPOL7	S	C	R#4	000728	SPOL7	S	SPOL7	S	00006A4	NE	R#4	00006A4	SPOL7	S	CE	F	R#4
PTPOL SF	SF	C	R#4	0006F4	SPOL8	S	C	R#4	000726	SPOL9	S	C	R#4	000728	SPOL9	S	SPOL9	S	00006A4	NE	R#4	00006A4	SPOL9	S	CE	F	R#4
SDPDL	C	R#4	0006F4	SPOL10	S	C	R#4	000726	SPOL11	S	C	R#4	000728	SPOL11	S	SPOL11	S	00006A4	NE	R#4	00006A4	SPOL11	S	CE	F	R#4	
TTPOL CE	CE	R#4	000558	FIXP18	XF	I#4	000726	SPOL12	S	C	I#4	000728	SPOL12	S	SPOL12	S	00006A4	NE	R#4	00006A4	SPOL12	S	CE	F	R#4		
COTAN X	XF	R#4	000000	COND	XF	R#4	000726	SPOL13	S	C	I#4	000728	SPOL13	S	SPOL13	S	00006A4	NE	R#4	00006A4	SPOL13	S	CE	F	R#4		
ALDNO S	CE	R#4	000000	ANDEND	S	C	R#4	000726	SPOL14	S	C	I#4	000728	SPOL14	S	SPOL14	S	00006A4	NE	R#4	00006A4	SPOL14	S	CE	F	R#4	
ABEDO SF	S	C	R#4	000000	DHMYA	S	C	R#4	000726	SPOL15	S	C	I#4	000728	SPOL15	S	SPOL15	S	00006A4	NE	R#4	00006A4	SPOL15	S	CE	F	R#4
DTNLH S	S	C	R#4	000000	DTNLH	S	C	R#4	000726	SPOL16	S	C	I#4	000728	SPOL16	S	SPOL16	S	00006A4	NE	R#4	00006A4	SPOL16	S	CE	F	R#4
FDRNL S	F	C	R#4	000000	DTNLH	S	C	R#4	000726	SPOL17	S	C	I#4	000728	SPOL17	S	SPOL17	S	00006A4	NE	R#4	00006A4	SPOL17	S	CE	F	R#4
I_NAXP3 S	S	C	R#4	000000	I_NAXP3	S	C	R#4	000726	SPOL18	S	C	I#4	000728	SPOL18	S	SPOL18	S	00006A4	NE	R#4	00006A4	SPOL18	S	CE	F	R#4
ISTART SF	S	C	R#4	000000	ISTART SF	S	C	R#4	000726	SPOL19	S	C	I#4	000728	SPOL19	S	SPOL19	S	00006A4	NE	R#4	00006A4	SPOL19	S	CE	F	R#4
MATSYA S	S	C	R#4	000000	MATSYA S	S	C	R#4	000726	SPOL20	S	C	I#4	000728	SPOL20	S	SPOL20	S	00006A4	NE	R#4	00006A4	SPOL20	S	CE	F	R#4
NCYCLE S	S	C	R#4	000000	NCYCLE S	S	C	R#4	000726	SPOL21	S	C	I#4	000728	SPOL21	S	SPOL21	S	00006A4	NE	R#4	00006A4	SPOL21	S	CE	F	R#4
NSTART	S	C	R#4	000000	NSTART	S	C	R#4	000726	SPOL22	S	C	I#4	000728	SPOL22	S	SPOL22	S	00006A4	NE	R#4	00006A4	SPOL22	S	CE	F	R#4
PSMDOL SF	SF	C	R#4	000000	PSMDOL SF	SF	C	R#4	000726	SPOL23	S	C	I#4	000728	SPOL23	S	SPOL23	S	00006A4	NE	R#4	00006A4	SPOL23	S	CE	F	R#4
RECORD SF	CE	R#4	000000	RECORD SF	CE	R#4	000726	SPOL24	S	C	I#4	000728	SPOL24	S	SPOL24	S	00006A4	NE	R#4	00006A4	SPOL24	S	CE	F	R#4		
TAPNUM SF	SF	C	R#4	000000	TAPNUM SF	SF	C	R#4	000726	SPOL25	S	C	I#4	000728	SPOL25	S	SPOL25	S	00006A4	NE	R#4	00006A4	SPOL25	S	CE	F	R#4
***** COMMON INFORMATION *****																											
NAME	COMMON BLOCK *	SIZE OF BLOCKCOMMON	000014	HEXADECIMAL BYTES																							
VAR.	NAME	TYPE	REL.	ADDR.																							

IND2	I ₃₄	000050	RADIN	R ₃₄	000054	JEND	I ₃₄	000058	JPI	I ₃₄	000060
JP2	I ₃₄	N.R.	MATSUM	I ₃₄	000068	JNEXT	I ₃₄	00006C	MDPK	I ₃₄	000074
JMOD	I ₃₄	000084	JPMOD	I ₃₄	000094	SINLON	R ₃₄	0000A4	COSLON	R ₃₄	0001C4
INDEX	I ₃₄	000E4	P SIGN	R ₃₄	000404	POLES	R ₃₄	000414	SDPOL	N.R.	N.R.
PK	R ₃₄	N.R.	DUFF	R ₃₄	000764	CONVL	R ₃₄	N.R.		R ₃₄	N.R.
PHISPL	R ₃₄	0057F4	SUM	R ₃₄							

EQUIVALENCED VARIABLES WITH THIS COMMON GROUP
 VARIABLE OFFSETS
 QPOL 000414
 TPOL 00045C
 TTPOL 00507C

VARIABLE	OFFSET
QPOL	000534
TPOL	000680
TTPOL	0055AC

NAME OF COMMON BLOCK * 11S6.ZE OF BLOCK COMMON

VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
VAR. Q5D6 R ₃₄ 000000	VAR. F17 R ₃₄ 000004	VAR. F98 R ₃₄ 000008

NAME OF COMMON BLOCK * =08SE OF BLOCK COMMON

VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
VAR. PU R ₃₄ 000000	VAR. PU R ₃₄ 000000	VAR. PU R ₃₄ 000000

EQUIVALENCED VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSETS

QT 000120	UT 000120
GW 0017A0	TT

VARIABLE	OFFSET
GT	0J0R40
PT	0021C0

NAME OF COMMON BLOCK * =M.ZE OF BLOCK COMMON

VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
VAR. QSM R ₃₄ N.R.	VAR. PSN R ₃₄ N.R.	VAR. QSMQSL R ₃₄ N.R.

NAME OF COMMON BLOCK * S0T9E OF BLOCK COMMON

VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
VAR. SDOT R ₃₄ 000010	VAR. OMEGA I ₃₂ N.R.	VAR. MINXTS I ₃₄ 0286E0
CONG L ₃₄ 0389A4		

EQUIVALENCED VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSETS
 I5CFO6

VARIABLE	OFFSET
GT	0J0R40
PT	0021C0

NAME OF COMMON BLOCK * -INTRSE OF BLOCK COMMON

VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
VAR. JSP I ₃₄ 000000	VAR. JNP I ₃₄ 000004	VAR. TIM I ₃₄ 000008
PTOP R ₃₄ 000010	PTOP R ₃₄ 000014	JSPPI I ₃₄ 000018
FIM R ₃₄ 000020	FIM R ₃₄ 000024	NLAYI I ₃₄ 000024
JM R ₃₄ 000030	JM R ₃₄ 000034	TAUT I ₃₄ 000028
MRDT R ₃₄ 000040	MRDT R ₃₄ 000044	TEST I ₃₄ 000038
JAYS R ₃₄ 000050	JAYS R ₃₄ 000054	JSB I ₃₄ 000046
DLAT R ₃₄ 000060	DLAT R ₃₄ 000064	JOT R ₃₄ 000048
ITAU R ₃₄ 000070	ITAU R ₃₄ 000074	OTR R ₃₄ 000050
TODAY R ₃₄ 000080	TODAY R ₃₄ 000084	IDAY I ₃₄ 000052
NSTEP R ₃₄ 000090	NSTEP R ₃₄ 000094	JMONTH I ₃₄ 000056
TAUP R ₃₄ 0000F8	TAUP R ₃₄ 0000FC	NCIMP3 I ₃₄ 000060
DTMULT R ₃₄ 000108	DTMULT R ₃₄ 00010C	TAUE R ₃₄ 000100
KAPA R ₃₄ 000118	KAPA R ₃₄ 00011C	GRAV R ₃₄ 000110
NFLY I ₃₄ 000128	NFLY I ₃₄ 00012C	ED R ₃₄ 000120
SIIND R ₃₄ 000130	SIIND R ₃₄ 000134	NRCH I ₃₄ 000124
DUMMYC R ₃₄ 0001370	DUMMYC R ₃₄ 00013C0	RSDIST R ₃₄ 000124
SIG R ₃₄ 0001370	SIG R ₃₄ 00013C0	CDX R ₃₄ 000140
JIPS R ₃₄ 0001370	JIPS R ₃₄ 00013C0	DSIGG R ₃₄ 000140
KSBS R ₃₄ 0001370	KSBS R ₃₄ 00013C0	JMS R ₃₄ 000140
DXP R ₃₄ 0001728	DXP R ₃₄ 0001760	DKU R ₃₄ 000140
F R ₃₄ 0001A08	F R ₃₄ 0001A40	DXP R ₃₄ 000140
PHIS R ₃₄ 00050	PHIS R ₃₄ 00054	DUNAV R ₃₄ 000140

VARIABLE	OFFSET
GT	0J0R40
PT	0021C0

NAME OF COMMON BLOCK * ST.E OF BLOCK COMMON

VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
VAR. JMAX I ₃₄ 000004	VAR. JSUM I ₃₄ 000008	VAR. SMTH R ₃₄ 00000C

VARIABLE	OFFSET
GT	0J0R40
PT	0021C0

VARIABLE	OFFSET
GT	001980
PT	003030

NAME OF COMMON BLOCK * * ST.E OF BLOCK COMMON

VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
VAR. JMAX I ₃₄ 000004	VAR. JSUM I ₃₄ 000008	VAR. SMTH R ₃₄ 00000C

NAME OF COMMON BLOCK * \$N31.E OF BLOCKCOMMON 000C38 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. HE
I¹⁶ 000000 NSEG 000000 VAR. NAME TYPE REL. ADDR. HE
NC1 I¹⁶ 000034 MFL I¹⁶ 000004 VAR. NAME TYPE REL. ADDR. HE
NSM1 I¹⁶ 000030 NSM1 NAME TYPE REL. ADDR. HE

 NAME OF COMMON BLOCK * \$N41.E OF BLOCKCOMMON 000C3C HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. HE
I¹⁶ 000000 C3RT L⁸ 4 VAR. NAME TYPE REL. ADDR. HE
TMC F¹⁶ 000010 000000 NUC3 L⁸ 4 VAR. NAME TYPE REL. ADDR. HE
SMAFTA L⁸ 6 000014 000000 SHSOOD L⁸ 4 VAR. NAME TYPE REL. ADDR. HE
ADPCLD L⁸ 4 000018 000008 FAST L⁸ 4 VAR. NAME TYPE REL. ADDR. HE

 NAME OF COMMON BLOCK * \$DS_2E OF BLOCKCOMMON 000C64 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. HE
I¹⁶ 000000 VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE

 NAME OF COMMON BLOCK * \$IT_1E OF BLOCKCOMMON 000C6E HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. HE
I¹⁶ 000000 GSW I¹⁶ 000004 VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE

 NAME OF COMMON BLOCK * \$S6_1E OF BLOCKCOMMON 000C80 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. HE
I¹⁶ 000000 V46 I¹⁶ 000000 VAR. NAME TYPE REL. ADDR. HE
NPC I¹⁶ 000002 N.R. VAR. NAME TYPE REL. ADDR. HE

 NAME OF COMMON BLOCK * T-7E OF BLOCKCOMMON 0032C0 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE

J#		N.R.		KH	I*4	000030	TAUT	R64	000030	JPUT	I*4	164
MROT	I*4	000040		JTEST	I*4	No.R.	TEST	I*4	No.R.	NA	I*4	No.R.
JAYS	I*4	No.R.		INCS	I*4	No.R.	JSB	I*4	No.R.	JNB	I*4	No.R.
DLAT	R64	No.R.		DLCN	R64	No.R.	DT	R64	No.R.	TAU	R64	00000
ITAU	I*4	No.R.		XINT	R64	No.R.	DAY	I*4	No.R.	JDAY	I*4	No.R.
TODAY	R64	No.R.		JDATE	I*4	No.R.	JMONTH	I*4	No.R.	JYEAR	I*4	No.R.
NSTEP	I*4	No.R.		NCYCLE	I*4	No.R.	NCOMP3	I*4	No.R.	NDGMN	I*4	Yes
TAUP	I*4	No.R.		TAUJ	I*4	No.R.	TAUE	R64	No.R.	TAUQ	R64	No.R.
DMULT	R64	No.R.		PI	R64	No.R.	GRAV	R64	No.R.	RGAS	R64	No.R.
KAPA	I*4	No.R.		PSL	R64	No.R.	ED	No.R.	No.R.	FNU	R64	No.R.
NFLB	I*4	No.R.		PSF	R64	No.R.	NRCH	I*4	No.R.	RDIST	R64	No.R.
SIND	R64	No.R.		COSD	I*4	No.R.	RMAX	R64	No.R.	CDX	R64	Yes
JUNNYC	R64	No.R.		WALTER	I*4	No.R.	DUMYA	R64	No.R.	XLABEL	R64	000320
SIG	R64	No.R.		DSIG	R64	No.R.	SIGE	R64	No.R.	DSIGD	R64	No.R.
JIPS	I*4	No.R.		JNPS	I*4	No.R.	JIUS	I*4	No.R.	JXU	I*4	No.R.
KSBS	I*4	No.R.		DYU	R64	No.R.	LAT	R64	No.R.	DYVP	R64	No.R.
DXP	R64	No.R.		SINL	R64	No.R.	DYP	R64	No.R.	DURMV	R64	No.R.
F	R64	No.R.		ALBEDO	I*2	No.R.	COSL	R64	No.R.			
PHIS	R64	000050										

EQUIVALENTED VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSEE U 000240 00240
 Y 00018C 00018C
 MACHIN

NAME OF COMMON BLOCK * =0\$56-E OF ELOCKCOMMON 081000 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE

VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSEE GT 000084C 00168C
 000084C

NAME OF COMMON BLOCK * =0\$56-E OF ELOCKCOMMON 0388A4 HEXADECIMAL BYTES

VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE
 SDOT R64 000000 COMG L*4 0389A4
 0389A4

EQUIVALENTED VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSEE ISDCT 001500
 001500

NAME OF COMMON BLOCK * =0\$56-E OF ELOCKCOMMON 000000 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE
 0389E0 1*2 019E09

EQUIVALENTED VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSEE

VARIABLE OFFSEE SMS 002300
 C 000000

VARIABLE OFFSEE

VARIABLE OFFSEE

VARIABLE OFFSEE

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C *** (FILEAP AND NEXT STEP IS LEAP)
C *** IF((MATSUN+MATSX)EQ.0)GO TC 45
C *** IF((NEXT CALL IS TO MATS PRED))
C DO 30 (NPC*EQ.1)*AND ((MATSX-EQ.1))EO TO 56
C DO 30 L = INC*INC*INC
C     P1(J,JS2) = PSM(I,J,JS2MOD)
C
C 28 DO 30 N = 1,4
C     DO 30 L = 1,1LAY
C     DO 30 I = INC*INC*INC
C     Q11(L,N,JS2) = QSM(I,L,N,JS2MOD)
C
C 30 IF((NPC*EQ.1))GO TO 63
C     CONTINUE
C
C 31 IF((MATSUN+MATSX)EQ.1)GO TO 63
C     GO TC 67
C
C 32 DO 61 I=INC*INC*INC
C     P11(J,JS2) = P1(J,JS2)
C
C 33 CONTINUE
C
C 34 DO 62 N=1,4
C     DO 62 L=1,1LAY
C     DO 62 I=INC*INC*INC
C     Q11(L,N,JS2) = Q11(L,N,JS2) * ICXP(J,JS2) * PT(J,JS2)
C
C 35 CONTINUE
C     GO TC 64
C
C 36 C *** SMOOTH Q(J,JS2) FOR SMOOTH LEAPFROG TIME SCHEME
C 37 C *** ALPHA = .5 * NU   BETA = 1 - 2. * ALPHA
C
C 38 C 45 DO 48 I = INC*INC*INC
C     P1(I,JS2) = BETA * P1(J,JS2) + ALPHA * (PSM(I,J,JS2) + PT(I,J,JS2))
C
C 39 C 48 DO 50 N = 1,4
C     DO 50 L = 1,1LAY
C     DO 50 I = INC*INC*INC
C     Q11(L,N,JS2) = BETA * DXYP(J,JS2) + Q11(L,N,JS2) * Q11(L,N,JS2)
C
C 40 C 50 $ ALPHA*(QSM(I,L,N,JS2)MOD+Q11(L,N,JS2)+DXYP(J,JS2))
C     CONTINUE
C
C 41 C 51 IF MOD(INSTEPM-NCM1) .NE. 0)GC TO 67
C
C 42 C 52 SOURCE TERM CORRECTION DUE TO LEAPFROG TIME SCHEME
C
C 43 C 53 CONTINUE
C
C 44 C 54 IF MOD(INSTEPM-NCM1) .NE. 0)GC TO 67
C
C 45 C 55 DO 57 N = 1,4
C     DO 57 L = 1,1LAY
C     DO 57 I = INC*INC*INC
C     Q11(L,N,JS2) = Q11(L,N,JS2) - QT(I,L,N,JS2) *
C     IDXP(J,JS2)*PT(I,J,JS2)
C
C 46 C 57 S7 IF MOD(INSTEPM-NCM1) .NE. 0)GC TO 67
C
C 47 C 58 IF((MATSUN*PRED*STEP))
C     IF((MATSUN*E2.1)*AND ((NPC*EQ.0))EO TO 67
C     CALL COMP3(UT,VIT,SHT,PT,QT,UTFOL,VTPOL,SMTPOL,PTPOL,
C
C 48 C 59 S57 QTPOL,J,JS2)
C     CONTINUE
C
C 49 C 60 IF((MATSUN*XN*OR NOT COMP3 STEP))
C     IF((MATSX-EQ.0)*(MOD(INSTEPM-NCM1) .NE. 0))GO TO 67
C
C 50 C 61 DO 65 N=1,4
C     DO 65 L=1,1LAY
C     Q11(L,N,JS2) = Q11(L,N,JS2) + DXYP(J,JS2) * PT(J,JS2)
C
C 51 C 66 CONTINUE
C
C 52 C 67 IF (J .LT. JN)
C     JS2 = JS2 + 1
C     JS2MOD = MOD(JS2-1,5) + 1
C     IF (JS2 .LE. JN) GO TO 29
C
C 53 C *** POLES
C
C 54 C 70 M = 1
C     IF (J .EQ. JN) M = 2
C     COFF1 = (-1.6,0) * M
C
C 55 C *** FILEAP AND NEXT STEP IS LEAP
C     IF((MATSUN+MATSX)EQ.0)GO TC 85
C     IF((MATS PRED*ORIGM'S CORR AND NEXT STEP IS LEAP))
C     IF((MATSUN*EQ.1))AND ((MATSX-EQ.0))GO TC 78
C     P10(M) = PT(POL,M)
C
C 56 C 75 DO 75 L = 1,1LAY
C     QP0(L,N,M) = QT(POL,L,N,M)
C
C 57 C 76 P10(M) = PSNPOL(M)
C     DO 80 N = 1,4
C     DO 80 L = 1,1LAY
C     QP0(L,N,M) = QSMNPOL(L,N,M)
C
C 58 C 80 IF((NPC*EQ.0))GO TO 93
C     CONTINUE
C
C 59 C 81 GO TC 54
C
C 60 C 82

```


NFLW	C	184	Ne.R.	
PHIS	CE	R84	000D50	
RAD	CC	182	Ne.R.	
SIND	CC	R84	Ne.R.	
TAUD	CC	R84	Ne.R.	
UPOL SFA	XR	R84	000000	
ALPHA F	C	R84	000018	
COMP2 SF	XF	R84	000000	
INDEX	C	184	Ne.R.	
JDATE	CC	184	Ne.R.	
JSPP1	C	184	Ne.R.	
NSTEP A	C	184	000008	
PTPOL SFA	XR	R84	000000	
SDPOL C	R84	Ne.R.		
STIN SFA	XR	R84	000000	
DTMULT C	XF	R84	000000	
IBCON F	XF	R84	000003	
JMONTH C	184	184	*R*	
J2M0D SF	C	184	000000	
NCOMP3 A	C	184	0000F0	
NLAYA1	C	184	Ne.R.	
PSKAD A	C	184	Ne.R.	
SHTPOL SFA	XR	R84	000003	

***** COMMON INFORMATION *****

NAME OF COMMON BLOCK * =M..0..Z OF BLOCKCOMMON

VAR. NAME	TYPE	REL.	ADDR.	ME	VAR. NAME	TYPE	REL.	ADDR.	ME
CON1	R84	000000	JNP	C012	CON2	NAME	TYPE	REL.	ADDR.
CDNS	R84	000010	PTOP	R84	CDN3	RE	REL.	ADDR.	ME
IMD2P1	I84	00030	PTC	R84	CON4	RE	000000	000000	C
CPTP	R84	000000	FIM	R84	CON5	RE	000000	000000	C
CP	R84	000000	JM	R84	CON6	RE	000000	000000	C
IMD2	I84	000000	MR0T	R84	CON7	RE	000000	000000	C
JPD2	I84	000000	JAVS	I84	CON8	RE	000000	000000	C
JPOL	I84	000000	DLAT	R84	CON9	RE	000000	000000	C
INDEX PK	R84	000000	LTAU	I84	CON10	RE	000000	000000	C
PHISPL	R84	Ne.R.	TODAY	I84	CON11	RE	000000	000000	C
OSM	R84	000000	NSTEP	I84	CON12	RE	000000	000000	C
			DTAUP	R84	CON13	RE	000000	000000	C
			DTMUL	R84	CON14	RE	000000	000000	C
			KAPA	R84	CON15	RE	000000	000000	C
			NFLW	I84	CON16	RE	000000	000000	C
			SIND	R84	CON17	RE	000000	000000	C
			SIG	R84	CON18	RE	000000	000000	C
			JIPS	I84	CON19	RE	000000	000000	C
			KSBS	I84	CON20	RE	000000	000000	C
			DXP	R84	CON21	RE	000000	000000	C
			F	R84	CON22	RE	000000	000000	C
			PHIS	R84	CON23	RE	000000	000000	C

NAME OF COMMON BLOCK * =M..0..Z OF BLOCKCOMMON
VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME

VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME

NAME OF COMMON BLOCK * =M..0..Z OF BLOCKCOMMON
VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME

NAME OF COMMON BLOCK * =M..0..Z OF BLOCKCOMMON
VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME

VAR. NAME	TYPE	REL.	ADDR.	ME	VAR. NAME	TYPE	REL.	ADDR.	ME
CON1	RE	000000	JNP	R84	CON2	NAME	TYPE	REL.	ADDR.
CDNS	RE	000000	PTOP	R84	CON3	RE	000000	000000	C
CON4	RE	000000	PTC	R84	CON5	RE	000000	000000	C
CON6	RE	000000	FIM	R84	CON7	RE	000000	000000	C
CON8	RE	000000	JM	R84	CON9	RE	000000	000000	C
CON10	RE	000000	MR0T	R84	CON11	RE	000000	000000	C
CON12	RE	000000	JAVS	I84	CON13	RE	000000	000000	C
CON14	RE	000000	DLAT	R84	CON15	RE	000000	000000	C
CON16	RE	000000	LTAU	I84	CON17	RE	000000	000000	C
CON18	RE	000000	TODAY	I84	CON19	RE	000000	000000	C
CON20	RE	000000	NSTEP	I84	CON21	RE	000000	000000	C
CON22	RE	000000	DTAUP	R84	CON23	RE	000000	000000	C
CON24	RE	000000	DTMUL	R84	CON25	RE	000000	000000	C
CON26	RE	000000	KAPA	R84	CON27	RE	000000	000000	C
CON28	RE	000000	NFLW	I84	CON29	RE	000000	000000	C
CON30	RE	000000	SIND	R84	CON31	RE	000000	000000	C
CON32	RE	000000	SIG	R84	CON33	RE	000000	000000	C
CON34	RE	000000	JIPS	I84	CON35	RE	000000	000000	C
CON36	RE	000000	KSBS	I84	CON37	RE	000000	000000	C
CON38	RE	000000	DXP	R84	CON39	RE	000000	000000	C
CON39	RE	000000	F	R84	CON40	RE	000000	000000	C

EQUIVALENCEC VARIABLES WITHIN THIS COMMON GROUP
VARIABLES E OF BLOCKCOMMON
TS 001890 N.R.

VARIABLE OFFSETS
C 000000

NAME OF COMMON BLOCK * =DS..Z E OF BLOCKCOMMON
VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME

VARIABLE OFFSETS
C 000000

NAME OF COMMON BLOCK * \$4079E OF BLOCKCOMMON
VAR. NAME TYPE REL. ADDR. HE
SDOT R4 00000 N.R.
CONG L4 0389A4

EQUIVALENCED VARIABLES WITHIN THIS COMMON GROUP
VARIABLE OFFSET VARIABLE OFFSET

NAME OF COMMON BLOCK * \$5679E OF ELOCKCOMMON
VAR. NAME TYPE REL. ADDR. HE
LSMTH T4 N.R.

038SA2 HEXADECIMAL BYTES
000000 HEXADECIMAL BYTES

NAME OF COMMON BLOCK * \$M31.E OF ELOCKCOMMON
VAR. NAME TYPE REL. ADDR. HE
NSEO T4 N.R.
NCM1 I4 000034

000038 HEXADECIMAL BYTES
0000002C HEXADECIMAL BYTES

NAME OF COMMON BLOCK * \$M31.E OF ELOCKCOMMON
VAR. NAME TYPE REL. ADDR. HE
NLF T4 N.R.
TOPQ R4

000330 HEXADECIMAL BYTES
00000000 HEXADECIMAL BYTES

NAME OF COMMON BLOCK * \$M31.E OF ELOCKCOMMON
VAR. NAME TYPE REL. ADDR. HE
FD R4 N.R.

000330 HEXADECIMAL BYTES
00000000 HEXADECIMAL BYTES

NAME OF COMMON BLOCK * =0F8E OF ELOCKCOMMON
VAR. NAME TYPE REL. ADDR. HE
PU R4 000000

EQUIVALENCE OF VARIABLES WITHIN THIS COMMON GROUP
VARIABLE OFFSET VARIABLE OFFSET

VARIABLE OFFSET

0386A2 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE
MNXTS I4 N.R.
RADT I4 N.R.

VARIABLE OFFSET

VARIABLE OFFSET

VAR. NAME TYPE REL. ADDR. HE
NPC T4 00004

000000 HEXADECIMAL BYTES

VAR. NAME TYPE REL. ADDR. HE
MATSX I4 00002C

000038 HEXADECIMAL BYTES

VAR. NAME TYPE REL. ADDR. HE
N.R.
TOPQ R4

000330 HEXADECIMAL BYTES

VAR. NAME TYPE REL. ADDR. HE
FD R4 N.R.

000330 HEXADECIMAL BYTES

VAR. NAME TYPE REL. ADDR. HE
N.R.
TOPQ R4

000330 HEXADECIMAL BYTES

VARIABLE OFFSET

VARIABLE OFFSET

VAR. NAME TYPE REL. ADDR. HE
NSM1 I4 N.R.

00000000 HEXADECIMAL BYTES

ORIGINAL PAGE IS
OF POOR QUALITY

```

      L = 1
      JP2 = J + 2
      JP1 = J + 1
      JS1 = J - 1
      JS2 = J - 2
      JS1MOD = MOD(JP2-1,5) + 1
      JS2MOD = MOD(JP1-1,5) + 1
      JS1MOD = MOD(J,5) + 1
      JS2MOD = MOD(J,5) + 1
      JS1 = 1
      JS2 = 1
      JS1MOD = 1
      JS2MOD = 1
      C * * BEGIN OF LAYER LOOP
      C * * CALC OF PV
      2150 IF (J .EQ. JM) GO TC 2158
      DO 2154 I = INC, IM, INC
      PV(I,1) = DXP(JI) * PI(L,J) * V(L,L,J) + DXP(JP1) * PI(L,JP1)
      S * V(L,JP1) * P(L,J) * V(L,L,J) + EXP(JP2) * P(L,JP2)
      PV(I,J2) = DXP(JI) * PI(L,J) * V(L,L,J) + EXP(JP2) * P(L,JP2)
      S * V(L,JP2)
      2154 CONTINUE
      C * * PU CALCULATION : OMIT FOR J=1 * SOUTH PQ.EI:
      C
      C IF (J .EQ. 1) GO TC 2225
      2158 IS1 = IM - 1
      I = IM
      PUISI = DVUL(J) * P(IS1,J) * U(IS1,L,J)
      PUI = DVUL(J) * P(IL,J) * UL,L,J
      DO 2160 I = INC, IM, INC
      PUIPI = DVUL(J) * PI(L,J) * U(IP1,L,J)
      PUIPI1 = DVUL(J) * PI(L,J) * U(IP1,L,J)
      PUISI1 = PUISI + PUI
      PUISI2 = PUISI + PUIPI
      PUI = PUIPI
      IS1 = I
      I = IP1
      2160 CONTINUE
      C * * HORIZONTAL ADVECTION OF MOMENTUM, TEMPERATURE, MOISTURE
      C * * COMPUTE FLUXES FIRST IN THE LONGITUDINAL (II) DIRECTION
      C
      IS1 = IM - 1
      I = IM
      00 2223 IP1 = INC, IM, INC
      FLUX1 = FICO * PU(IP1,1)
      FLUX2 = FICO * PU(IP1,2)
      DO 2223 N = 1,4
      OFLUX1 = FLUX1 * (Q(IS1,L,N,J) + Q(IL,N,J))
      OFLUX2 = FLUX2 * (Q(IS1,L,N,J) + Q(IP1,L,J))
      IF(ONE,4,GO TO 100
      OFLUX1 = FLUX1 * (Q(IP1,L,N,J) + Q(IL,N,J))
      OFLUX2 = FLUX2 * (Q(IP1,L,N,J) + Q(IL,N,J))
      IF(QFLUX1.GT.0.0) GO TO 110
      IF(QFLUX2.GT.0.0) GO TO 110
      110 IF((QFLUX1.LT.0.0).AND.(QFLUX2.LT.0.0)) QFLUX2=0.
      110 IF((QFLUX1.LT.0.0).AND.(QFLUX2.LT.0.0)) QFLUX1=0.
      100 CONTINUE
      QIP1,L,N,J = Q(IP1,L,N,J) + CFLUX1
      QIL,N,J = Q(IL,N,J) + CFLUX2
      QIS1,L,N,J = QIS1,L,N,J - CFLUX1 - CFLUX2
      2223 IS1 = I
      I = IP1
      2220 IF (J .EQ. JM)
      CONTINUE
      GO TC 2237
      C * * NO DO FLUX CALCULATION IN THE LATITUDINAL (II) DIRECTION
      C
      2225 DC 2230 I = INC, IM, INC
      FLUX1 = FICO * PV(I,1)
      FLUX2 = FICO * PV(I,2)
      DO 2230 N = 1,4
      QFLUX1 = FLUX1 * (Q(I,L,N,J) + Q(IL,N,J))
      QFLUX2 = FLUX2 * (Q(I,L,N,J) + Q(IL,N,J))
      IF(QFLUX1.GT.0.0) GO TO 120
      IF(QFLUX2.GT.0.0) GO TO 120
      120 IF((QFLUX1.LT.0.0).AND.(QFLUX2.LT.0.0)) QFLUX1=0.
      120 IF((QFLUX1.LT.0.0).AND.(QFLUX2.LT.0.0)) QFLUX2=0.
      115 IF((QFLUX1.LT.0.0).AND.(QFLUX2.LT.0.0)) QFLUX1=0.
      115 IF((QFLUX1.LT.0.0).AND.(QFLUX2.LT.0.0)) QFLUX2=0.
      120 QIP1,L,N,JP2) = QIP1,L,N,JP1) + CFLUX2
      QIS1,L,N,JP2) = QIS1,L,N,JP1) + CFLUX1
      ISN 0029
      ISN 0030
      ISN 0031
      ISN 0032
      ISN 0033
      ISN 0034
      ISN 0035
      ISN 0036
      ISN 0037
      ISN 0038
      ISN 0039
      ISN 0041
      ISN 0042
      ISN 0043
      ISN 0044
      ISN 0045
      ISN 0046
      ISN 0047
      ISN 0048
      ISN 0049
      ISN 0050
      ISN 0051
      ISN 0053
      ISN 0054
      ISN 0055
      ISN 0056
      ISN 0057
      ISN 0058
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      ISN 0060
      ISN 0061
      ISN 0062
      ISN 0063
      ISN 0064
      ISN 0065
      ISN 0066
      ISN 0067
      ISN 0068
      ISN 0069
      ISN 0070
      ISN 0071
      ISN 0072
      ISN 0073
      ISN 0074
      ISN 0076
      ISN CC78
      ISN 0080
      ISN 0082
      ISN 0084
      ISN 0086
      ISN 0087
      ISN 0088
      ISN 0089
      ISN 0090
      ISN 0091
      ISN 0092
      ISN 0093
      ISN 0094
      ISN 0096
      ISN 0097
      ISN 0098
      ISN 0099
      ISN 0100
      ISN 0101
      ISN 0102
      ISN 0104
      ISN 0106
      ISN 0108
      ISN 0110
      ISN 0112
      ISN 0114
      ISN 0115
      ISN 0116
      B4.M1 2690
      B4.M1 2910
      B4.M1 2920
      B4.M1 2940
      B4.M1 2950
      B4.M1 2960
      B4.M1 2970
      B4.M1 2980
      B4.M1 2990
      B4.M1 3000
      B4.M1 3010
      B4.M1 3020
      B4.M1 3030
      B4.M1 3040
      B4.M1 3050
      B4.M1 3060
      B4.M1 3070
      B4.M1 3080
      B4.M1 3090
      B4.M1 3100
      B4.M1 3110
      B4.M1 3120
      B4.M1 3130
      B4.M1 3140
      B4.M1 3150
      B4.M1 3160
      B4.M1 3170
      B4.M1 3180
      B4.M1 3190
      B4.M1 3200
      B4.M1 3210
      B4.M1 3220
      B4.M1 3230
      B4.M1 3240
      B4.M1 3250
      B4.M1 3260
      B4.M1 3270
      B4.M1 3280
      B4.M1 3290
      B4.M1 3300
      B4.M1 3310
      B4.M1 3320
      B4.M1 3330
      B4.M1 3340
      B4.M1 3350
      B4.M1 3360
      B4.M1 3370
      B4.M1 3380
      B4.M1 3390
      B4.M1 3400
      B4.M1 3410
      B4.M1 3420
      B4.M1 3430
      B4.M1 3440
      B4.M1 3450
      B4.M1 3460
      B4.M1 3470
      B4.M1 3480
      B4.M1 3490
      B4.M1 3500
      B4.M1 3510
      B4.M1 3520
      B4.M1 3530
      B4.M1 3540
      B4.M1 3550
      B4.M1 3560
      B4.M1 3570
      B4.M1 3580
      B4.M1 3590
      B4.M1 3600
      B4.M1 3610
      B4.M1 3620
      B4.M1 3630
      B4.M1 3640
      B4.M1 3650
      B4.M1 3660
      B4.M1 3670
      B4.M1 3680
      B4.M1 3690
      B4.M1 3700
      B4.M1 3710
      B4.M1 3720
      B4.M1 3730
      B4.M1 3740
      B4.M1 3750
  
```

ISN 0117

2230 CT(L,N,J) = QT(L,N,J) - QFLUX1 - QFLUX2
CONTINUE

C * * FOLLOWING IS CORRECTION FOR CASE J=2

C * * V(L,N,J) = -V(INDEX(L,N,J))

C * * PV(L,2) FOR J=0 IS EQUAL TO: -CONV(L,N,J) * SEE ABOVE

ISN 0119 IF(J.GT.1) GO TC 2290
DO 2240 L = INC, INC
CONV(L,N,J)=0.
CONTINUE

2240

C * * CONTINUITY EQUATION

C * * DUE TO 1 LINE OF LATITUDE AT A TIME THE DEFINITION OF PV.
C * * AND 0TH ORDER FORM OF CONV. USE COMPUTE IT AS FOLLOWS:

ISN 0124 2290 IS2 = IM - 1
IS1 = IM
DO 2400 L = INC, INC
CONV(L,J,P1) = CONV(L,J,P1) + E0 * PV(L,J)
CONV(L,J) = CONV(L,J) - E0 * PV(L,J)
S = PV(L,J) * (PV(L,1) - PV(L,2)) * (PV(L,2) - PV(L,1))
IS2 = IS1
IS1 = 1
2400 CONTINUE

C * * FOLLOWING IS CORRECTION FOR J=JN.

C * * U(L,L,JM2) = -U(INDEX(L,JM1)) * ETC.

C 2237 IF(L.LT.JM1) GO TC 2405
IS2 = IM - 3
IS1 = IM - 2
IP1 = IM - 1
IP1 = IM - 1
DC 2250 IP2 = INC, INC
PV1JM = JXP(JM1 * P1, JM1) * V(L,L,JM1)

PV2JM = 0.

CONV(L,JM1) = CONV(L,JM1) - E0 * PV1JM
S + PV2JM + DVULAT * (B0 * (P1(S1,JM1) + P1(S2,JM1) * U(LP2,L,JM1))
S - P1(S2,JM1) * U(LP1,L,JM1))

C * * CALCULATION OF THE REMAINDER OF CT(L,L,N,JM1)

C FLUX1 = F1CO * PV1JM
FLUX2 = F2CO * PV1JM
DO 2255 N = 1,4
OPFLUX1 = FLUX1 * ((J.L.N,JM1) + G(L,N,JM1) - NPO)
OPFLUX2 = FLUX2 * ((G(JL,N,JM1) + FSIGNIN) * Q(INDEX(L,L,N,JM1))

IF(J.NE.4) GO TO 126

IF(J.GT.4) GO TO 126

IF(GFLUX1.GT.0) QFLUX1=0.

IF(GFLUX2.GT.0) QFLUX2=0.

IF(P1(SIGNIN(L,N,JM1)) .AND. (QFLUX1.LT.0 .OR. QFLUX2.LT.0))
1.0FLUX2.LT.0 .OR. 1.0FLUX1.LT.0 .OR. 0.0.

1.0FLUX2.LT.0 .OR. 1.0FLUX1.LT.0 .OR. 0.0.
QT(L,N,JM1)=QT(L,N,JM1) - 1.0FLUX1 - QFLUX2
CONTINUE

126 IS2 = IS1
IS1 = L
IP1 = IP2
2255 IP1 = IP2
CONTINUE

C * * END OF LAYER LOOP

C * * COMPUTATION OF SIGN DOT AND NEW SURFACE PRESSURE

C * * SKIP THIS COMPUTATION IF J = ECA(1); SCUTH(2)

C * * P1(T,J) IS EQUIVALENTED TO CONV(L,J)

CONTINUE

1F (J.EQ.1)
DO 2240 L = INC, INC
CONV(L,J) = CONV(L,J)
P1(T,J) = P1(T,J) + CONV(L,J)

2240 IF(J.GT.1) GO TC 2600
P1(T,J) = P1(T,J) + CONV(L,J)

CONTINUE

ISN 0173 IF(J.EQ.1)
DO 2240 L = INC, INC
CONV(L,J) = CONV(L,J)
P1(T,J) = P1(T,J) + CONV(L,J)

2240 IF(J.GT.1) GO TC 2600
P1(T,J) = P1(T,J) + CONV(L,J)

CONTINUE

ISN 0175 IF(J.EQ.1)
DO 2240 L = INC, INC
CONV(L,J) = CONV(L,J)
P1(T,J) = P1(T,J) + CONV(L,J)

2240 IF(J.GT.1) GO TC 2600
P1(T,J) = P1(T,J) + CONV(L,J)

CONTINUE

ISN 0176 IF(J.EQ.1)
DO 2240 L = INC, INC
CONV(L,J) = CONV(L,J)
P1(T,J) = P1(T,J) + CONV(L,J)

2240 IF(J.GT.1) GO TC 2600
P1(T,J) = P1(T,J) + CONV(L,J)

CONTINUE

ISN 0177 IF(J.EQ.1)
DO 2240 L = INC, INC
CONV(L,J) = CONV(L,J)
P1(T,J) = P1(T,J) + CONV(L,J)

2240 IF(J.GT.1) GO TC 2600
P1(T,J) = P1(T,J) + CONV(L,J)

CONTINUE

ISN 0178 IF(J.EQ.1)
DO 2240 L = INC, INC
CONV(L,J) = CONV(L,J)
P1(T,J) = P1(T,J) + CONV(L,J)

2240 IF(J.GT.1) GO TC 2600
P1(T,J) = P1(T,J) + CONV(L,J)

CONTINUE

ISN 0179 IF(J.EQ.1)
DO 2240 L = INC, INC
CONV(L,J) = CONV(L,J)
P1(T,J) = P1(T,J) + CONV(L,J)

2240 IF(J.GT.1) GO TC 2600
P1(T,J) = P1(T,J) + CONV(L,J)

CONTINUE

B4.MI 3760

B4.MI 3770
B4.MI 3790
B4.MI 3800
B4.MI 3810
B4.MI 3820
B4.MI 3830
B4.MI 3840
B4.MI 3850
B4.MI 3860
B4.MI 3870
B4.MI 3880
B4.MI 3890
B4.MI 3900
B4.MI 3910
B4.MI 3920
B4.MI 3930
B4.MI 3940
B4.MI 3950
B4.MI 3960
B4.MI 3970
B4.MI 3980
B4.MI 3990
B4.MI 4000
B4.MI 4010
B4.MI 4020
B4.MI 4030
B4.MI 4040
B4.MI 4050
B4.MI 4060
B4.MI 4070
B4.MI 4080
B4.MI 4090
B4.MI 4100
B4.MI 4110
B4.MI 4120
B4.MI 4130
B4.MI 4140
B4.MI 4150
B4.MI 4160
B4.MI 4170
B4.MI 4180
B4.MI 4190
B4.MI 4200
B4.MI 4210
B4.MI 4220
B4.MI 4230
B4.MI 4240
B4.MI 4250
B4.MI 4260
B4.MI 4270
B4.MI 4280
B4.MI 4290
B4.MI 4300
B4.MI 4310
B4.MI 4320
B4.MI 4330
B4.MI 4340
B4.MI 4350
B4.MI 4360
B4.MI 4370
B4.MI 4380
B4.MI 4390
B4.MI 4400
B4.MI 4410
B4.MI 4420
B4.MI 4430
B4.MI 4440
B4.MI 4450
B4.MI 4460
B4.MI 4470
B4.MI 4480
B4.MI 4490
B4.MI 4500
B4.MI 4510
B4.MI 4520
B4.MI 4530
B4.MI 4540
B4.MI 4550
B4.MI 4560
B4.MI 4570
B4.MI 4580
B4.MI 4590
B4.MI 4600
B4.MI 4610
B4.MI 4620
B4.MI 4630

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      IF (NLAY .EQ. 2) GO TO 2440
      DO 2450 L = 2,NLAYM1
      SD(I,L,J) = SD(I,L-1,J) + CONV(I,L,J) - CSIG(L) * PT(I,L,J)
      IF(OCMG) OMEGAI(I,J,L) = SD(I,L,J)/DXVP(I,J,L)
      CONTINUE
      2430
      2440  GO 2450 I = INC*IM*INC
      DELT = DT * PT(I,J) / DXVP(J)
      11=L-1
      IF(I*EQ.1111=1
      PT(I,J) = PT(I,J) + DT * PT(I,J) / DXVP(J)
      CONTINUE
      2450  IF(I,NOT,CONG) GO TO 2456
      DO 2455 L = 1,NLAYM1
      DC 2455 I = 1,IM
      OMEGAI(J,L) = OMEGAI(J,L) + SIGL*PT(I,J)/DXVP(J)
      2456  CONTINUE
      C * * * VERTICAL ADVECTION OF MOMENTUM AND TEMPERATURE
      C
      C 0203  DO 2490 L = 1,NLAYM1
      ISN 0204  C
      C FIRST DO MOMENTUM
      C
      ISN 0205  C 00 2470 N=1,2
      TSN 0206  C 00 2470 I=INC*IM*INC
      ISN 0207  C SFUX = F2CO*SD(I,L,J)*QQ(I,L,N,J) + Q(I,L,P1,N,J)
      ISN 0208  C Q(I,L,P1,N,J) = Q(I,L,P1,N,J) - SFUX / CSIG(LP1)
      ISN 0209  C Q(I,L,N,J) = Q(I,L,N,J) + SFUX / DSIG(L)
      ISN 0210  C 2470  CONTINUE
      C * * * VERTICAL ADVECTION OF TEMPERATURE
      C * * * TRYING GISS CODE FOR PK CALC. INSTEAD OF 4TH ORDER COE
      C
      ISN 0211  DO 2480 I = INC*IM*INC
      ISN 0212  PL1 = SIG(L) * PT(I,J) + PT(OP
      ISN 0213  PL2 = SIG(LP1) * PT(I,J) + PT(OP
      ISN 0214  PK1 = EXPBYK(P1)
      ISN 0215  PK2 = EXPBYK(P2)
      ISN 0216  SFUX = F2CO * SD(I,L,J) * (T(I,L,J) / P1 + T(I,L,P1) / PK2)
      ISN 0217  T(I,L,P1,J) = T(I,L,P1,J) - PK2 * TFLUX / DSIG(LP1)
      ISN 0218  T(I,L,J) = T(I,L,J) + PK1 * TFLUX / DSIG(L)
      ISN 0219  2480  CONTINUE
      ISN 0220  2490  IF (J .LT. JM)
      ISN 0221  C
      C * * * CALCULATIONS AT THE POLES
      C
      ISN 0223  2600 M = 1
      IF (J .EQ. JM)
      PTDPOL(M) = 0.
      M = 2
      ISN 0224  C * * * WHEN (J=1) OR (J=M) WE DO THE CALCULATIONS AT THE POLES.
      ISN 0225  C * * * MOMENTUM, TEMPERATURE, SPECIFIC HUMIDITY AT SOUTH POLE
      ISN 0226  C * * * CN = 1, AND NORTH POLE CM = 2
      ISN 0227  C * * * JPOL(K,M) = 1,2,3; JM = 1,2
      ISN 0228  C * * * CONI = DXP21 / (3 PI * A * A * SIN(OLAT / 21 * 2)
      ISN 0229  C * * * CON2 = -DXP21 / (3 PI * A * A * SIN(ELAT) * 21)
      ISN 0230  C * * * CORRESPONDS TO THE LATITUDE LINE NEAREST TO THE POLE.
      ISN 0231  C
      ISN 0232  C
      ISN 0233  2505  M = 1
      IF (J .EQ. JM)
      PTDPOL(M) = 0.
      C
      C * * * HORIZ. ADVECT. OF MOMENTUM, TEMPERATURE, SPECIFIC HUMIDITY
      C * * * AT THE NORTH AND SOUTH POLES.
      C * * * 4/4/78 -PIV TO BE CHANGED TO PIV FOR: -PIE LONGCPIE
      C
      ISN 0234  DO 2510 I = INC*IM*INC
      ISN 0235  DO 2510 K = 1,2
      ISN 0236  IF (M*EQ.2) JKP = JNP
      ISN 0237  JK = JPOL(K)
      ISN 0238  PIV = PI(I,JK) * V(I,L,JK)
      ISN 0239  SUMK_1 = SUM(K_1) - PIV * U(I,L,JK) * SIN(LON)
      ISN 0240  $ + COEF1 * V(I,L,JK) * COS(LON)
      ISN 0241  $ + SUM(K_2) - PIV * U(I,L,JK) * COS(LON)
      ISN 0242  $ + V(I,L,JK) * S(INLON)
      ISN 0243
  
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NAME OF COMMON BLOCK & COMMON OF CLOCK COMMON 000000 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE
PIPOL R#4 00000000

NAME OF COMMON BLOCK * *S6* OF CLOCK COMMON 010100 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE
CONV. CONV. R#4 00000000
EQUIVALENTED VARIABLES WITHIN THIS COMMON GROUP
VARIABLE OFFSETS VARIABLE OFFSETS VARIABLE OFFSETS
PIT 000000 SD 000000

NAME OF COMMON BLOCK * =03* OF CLOCK COMMON 081000 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE
PU PU R#4 00000000
EQUIVALENTED VARIABLES WITHIN THIS COMMON GROUP
VARIABLE OFFSETS VARIABLE OFFSETS VARIABLE OFFSETS
GT 000B40 G 0016C

NAME OF COMMON BLOCK * #DS_7E OF CLOCK COMMON 000000 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE
LATCH LATCH R#4 00000000

NAME OF COMMON BLOCK * S*019E OF CLOCK COMMON 038384 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE
SDT SDT R#4 00000000 OMEGA 1*2 019E00 MINIXS 1*4 N.R.
CONG CONG L#4 0389A4
EQUIVALENTED VARIABLES WITHIN THIS COMMON GROUP
VARIABLE OFFSETS VARIABLE OFFSETS VARIABLE OFFSETS
TSD QT 00CF00

NAME OF COMMON BLOCK * *S6-* OF CLOCK COMMON 000000 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE

ORIGINAL PAGE
DUALITY

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ISN 0029 JSI = J - 1
ISN 0030 JS2 = J - 2
ISN 0031 JS2MOD = MOD(JP2-1,5) + 1
ISN 0032 JP1MOD = MOD(JP1-1,5) + 1
ISN 0033 JMD = MOD(J-1,5) + 1
ISN 0034 JS3MOD = MOD(J-4,5) + 1
ISN 0035 JS2MOD = MOD(JS2-1,5) + 1
C * * * JP2P2 = MOD(JP2-1,3) + 1
ISN 0036 JP2P1 = MOD(JP2-1,3) + 1
ISN 0037 JP1K = MOD(J-1,3) + 1
ISN 0038 DTAPA = DT * KAPA
ISN 0039 IF(J>GT+1)
ISN 0040 JP2 = 1
ISN 0041 JP2MOD = 1
ISN 0042 JP2P2 = 1
ISN 0043 GO TO 3001
ISN 0044 GO TO 3005
ISN 0045 C * * * CORIOLIS FORCE FOR 4TH ORDER DOES NOT FOLLOW GISS
C * * * METHOD OF COMPUTATION
C * * * ADLDP = (I2 * RAD * DLAT * DLON = I2. * DRU(J) * DLON)
C * * * ADLDP = (I2 * RAD * DLAT * DLON = I2. * DRU(J) * DLON)
C * * * CONTINUE
C 3001 DO 3000 L = 1,NLAY
DO 3000 I = INC,IN,INC
FX = DT * (F(J) * DXP(J) + ADLDP * SINL(J)) * U(I,L,J)
UT(I,L,J) = UT(I,L,J) + FX * PI(I,J) * VI(I,L,J)
VT(I,L,J) = VT(I,L,J) - FX * PI(I,J) * VI(I,L,J)
CONTINUE
C 3000
C * * * MAIN LOOP
C IF(J>GT+1) GO TO 3032
C DO 3030 LX = 1,NLAY
LPI = L+1
C IF(J>EQ+1.OR.J>EQ+JNP) GO TO 3141
C COMPUTATION OF THE ENERGY TERM FOR THE THERMODYNAMIC
EQUATION FOR J=23.....JM-1,JM
C SET UP CYCLIC I-INDICES
C IS2 = IN - 3
ISI = IN - 2
I = IN - 1
IP1 = IN
C SET UP J-INDICES
C NDXJP2 = JP2
TFTJ,EQ,JNP) NDXJP2 = JM
C NDXJS2 = JS2
TPI,JO,EQ,2) NDXJS2 = 2
C PERFORM CALCULATIONS
C DO 3140 IP2 = INC,IN,INC
SKT = DTAPA*SIGL)*T(I,L,J)/(PTCP+SIGL*PF(I,J))
PIV = DXP(J)*T(I,L,J)
C SET UP PROPER I-INDEX AND PRESSURE TERMS
C NDXI = INDEX(J>EQ,JNP) NDXI = INDEX(I)
G1 = P(NDXI,NDXJP2),
C NDXI = I
IF(J>EQ,JNP) NDXI = INDEX(I)
G2 = P(NDXI,NDXJS2)
C TTI,I,L,J) = TT(I,L,J) + SKT*PI(I,J)*PI(I,J) + DVU(J) *
U(I,L,J)*PI(I,J)*PI(I,J) - PIJP2,J,I,J) + G1 + G2
C P(IJS2,J,I) + PIV*SA*PI(I,J)
C RESET CYCLIC INDICES
C IS2 = ISI
ISI = I
I = IP1
IP1 = IP2
C 3140 CONTINUE
C
ISN 0081
ISN 0082
ISN 0083
ISN 0084
ISN 0085
B4 M1 6670
B4 M1 6680
B4 M1 6690
B4 M1 6700
B4 M1 6710
B4 M1 6720
B4 M1 6730
B4 M1 6740
B4 M1 6750
B4 M1 6760
B4 M1 6770
B4 M1 6780
B4 M1 6790
B4 M1 6800
B4 M1 6810
B4 M1 6820
B4 M1 6830
B4 M1 6840
B4 M1 6850
B4 M1 6860
B4 M1 6870
B4 M1 6880
B4 M1 6890
B4 M1 6900
B4 M1 6910
B4 M1 6920
B4 M1 6930
B4 M1 6940
B4 M1 6950
B4 M1 6960
B4 M1 6970
B4 M1 6980
B4 M1 6990
B4 M1 7000
B4 M1 7010
B4 M1 7020
B4 M1 7030
B4 M1 7040
B4 M1 7050
B4 M1 7060
B4 M1 7070
B4 M1 7080
B4 M1 7090
B4 M1 7100
B4 M1 7110
B4 M1 7120
B4 M1 7130
B4 M1 7140
B4 M1 7150
B4 M1 7160
B4 M1 7170
B4 M1 7180
B4 M1 7190
B4 M1 7200
B4 M1 7210
B4 M1 7220
B4 M1 7230
B4 M1 7240
B4 M1 7250
B4 M1 7260
B4 M1 7270
B4 M1 7280
B4 M1 7290
B4 M1 7300
B4 M1 7310
B4 M1 7320
B4 M1 7330
B4 M1 7340
B4 M1 7350
B4 M1 7360
B4 M1 7370
B4 M1 7380
B4 M1 7390
B4 M1 7400
B4 M1 7410
B4 M1 7420
B4 M1 7430
B4 M1 7440
B4 M1 7450
B4 M1 7460
B4 M1 7470
B4 M1 7480
B4 M1 7490
B4 M1 7500
B4 M1 7510
B4 M1 7520
B4 M1 7530
B4 M1 7540

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ISN 0086      3141  CONTINUE
ISN 0087      C      IF(JEQ0,JMI) GO TO 3036
ISN 0088      C      * * COMPUTE PK AT LATITUDE JP2 USING GISS METHOD
ISN 0089      C      IF(LLLT,NLAY)          GO TC 3055
ISN 0090      C      3007    DO 3010 I = 1,1,N
ISN 0091      C      PL1 = SIGE(I)*P1(I,JP2) + PTOP
ISN 0092      C      PK1 = PL1*EXPBK(PL1)
ISN 0093      C      LL = 1
ISN 0094      C      DO 3010 LLPI1 = 2,NLAYPI
ISN 0095      C      PL2 = SIGE(LLPI1 * P1(I,JP2)) + PTOP
ISN 0096      C      PK2 = PL2*EXPBK(PL2)
ISN 0097      C      PK11 = PL2 - PK2
ISN 0098      C      PK1 = PK2 - PK11
ISN 0099      C      DO 3011 LL = LLPI1
ISN 0100      C      CONTINUE
ISN 0101      C      * * COMPUTATION OF PHI (GEOCENTRAL) AT JF2 FOR L=NLAY.
ISN 0102      C      * * * HERE PHI IS NORMALIZED,I.E.,EQUALS STANDARD PHI(JF2)-PHIBAR.
ISN 0103      C      IF (LL .LT. NLAY)          GO TC 3055
ISN 0104      C      DO 3050 I = INC,IM,INC
ISN 0105      C      PHI(I,L,JP2MOD) = PHIS(I,L,JP2) + CPTM*TPK(I,L,JPKP2) - PSKAPR
ISN 0106      C      LLN1 = 1
ISN 0107      C      DO 3050 LL = 1,NLAY
ISN 0108      C      LP1 = LL+1
ISN 0109      C      IF(LLLE0,NLAY), LP1 = LL
ISN 0110      C      DUM1 = DSIG(I,LL)*TPK(I,LLPI1,JPKP2) - PK(I,LL,JPKP2)
ISN 0111      C      DUM2 = SIGE(LL)*TPK(I,LLPI1,JPKP2) - PK(I,LLN1,JPKP2)
ISN 0112      C      NL = SIG(LL)*P1(I,JP2)
ISN 0113      C      DUM3 = NL * R * DSIG(LL) / (NL + PTOP)
ISN 0114      C      LLM1 = LL
ISN 0115      C      PHI(I,L,JP2MOD) = PHI(I,L,JP2) + (DUM3-DUM2)/LL,JPKP2) / (DUM1+DUM2)/PK(I,LL,JPKP2) * TL(L,JP2)
ISN 0116      C      3050 1 (DUM1+DUM2)/PK(I,LL,JPKP2) * TL(L,JP2),
ISN 0117      C      CONTINUE
ISN 0118      C      * * COMPUTATION OF PHI AT JF2
ISN 0119      C      3055  DO 3060 I = INC,IM,INC
ISN 0120      C      PHIL(I,L,JP2MOD) = PHI(I,L,JP1,JP2MOD) + CRCT2 * (PK(I,L,JP1,JP2MOD) -
ISN 0121      C      S (PK(I,L,JPKP2)), T(I,L,JP2) - T(I,L,JPKP2)) * TL(L,JP2) /
ISN 0122      C      S PK(I,L,JP1,JPKP2) - TIBAR
ISN 0123      C      3060  IF(JF2.EQ.1.OR.JP2.EQ.JNP) GO TO 3030
ISN 0124      C      DO 3070 I = INC,IM,INC
ISN 0125      C      TBAR = TIBAR * PK(I,L,JPKP2)
ISN 0126      C      TPRI1 = T(I,L,JP2) - TBAR
ISN 0127      C      PRES1 = PTOP + SIG(I,L)*P1(I,JP2)
ISN 0128      C      W(I,L,JP2MOD) = SIG(I,L)*P1(I,JP2)
ISN 0129      C      3070  IF(JF2.EQ.1) THEN
ISN 0130      C      CONTINUE
ISN 0131      C      * * IF (J=1) RETURN AND COMPUTE PHI(L,2)
ISN 0132      C      * * FOR SOUTH POLE CALCULATIONS
ISN 0133      C      3030  IF(JEQ0,JMI)
ISN 0134      C      3074  IF(JP2.GE.3)
ISN 0135      C      JP2 = JP2 + 1
ISN 0136      C      JP2MOD = JP2MOD + 1
ISN 0137      C      JPKP2 = JPKP2 + 1
ISN 0138      C      3075  IF(JF2.EQ.1) GO TO 3031
ISN 0139      C      GO TC 3005
ISN 0140      C      * * PRESSURE GRADIENT (V EQUATION) FOR J=2
ISN 0141      C      3032  DO 3031 LX = 1,NLAY
ISN 0142      C      L = NLAYPI - LX
ISN 0143      C      IF(JEQ0,1) GO TO 3031
ISN 0144      C      3080  IF(J.EQ.1) GO TC 3085
ISN 0145      C      DO 3083 I=INC,IM,INC
ISN 0146      C

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C * * * 7/31/78 USING PHILLIPS GEOPOTENTIAL AT PCLES *
C * * PRESSURE GRADIENT AND ENERGY CONVERSION TERMS FOR
C * * MOMENTUM TEMPERATURE EQUATIONS
C * * JPMOD(K,M) = (2,3,4)MOD(JM-1,5)+1 MOD((JM-1)-1,5)+1
C * * MOD(JPK(K,M)) = (2,3,4)MOD(JM-1,3)+1,MOD(JM-2,3)+1
C
C      C PRPOL = SIGIL1 * PPOL(MI + PTOP
C      C SKTPOL = SIGIL1 * KAPL * TPOL(L,M) / PRPL
C      C VPOL = V(L,M,JP2MOD)
C
C COMPUTE SUMMATION FOR TEMPERATURE EQUATION
C
C DO 3211 I=1,IM
C      3211 SUM(1,3) = SUM(1,3) + COEF1 * VPOL(L,M)*CSLDNL(M)
C      1 + VPOL(L,M)*SIN(DNL(M)*B*SP1(L,M)) - PI1(JPOL(2,4)))
C
C MODIFY TEMPERATURE AT POLES
C
C      C TTPO(L,M) = TTPO(L,M) + CT*SKTFOL*PPOL(M)
C      1 (TTPO(L,M) + CONS*SUM(1,3))
C
C DO 3210 I=1,IM
C      3210 K = 1,2
C
C      DO 3220 K = 1,2
C      JK = JPOL(K,M)
C      JKMOD = JPMOD(K,M)
C      MOD3J = MOD(JPK(K,M))
C
C      TERM1 = PHIL(L,JK,MOD) + VPOL(SPI(L,JK)
C      SUM(K,1) = SUM(K,1) + COSLN((L,JK)) * TERM1
C      SUM(K,2) = SUM(K,2) + SINLN((L,JK)) * TERM1
C
C      CONTINUE
C      CNT INUE
C
C      DO 3222 K = 1,2
C      SUM(K,2) = COEF1 * SUM(K,2)
C
C      DO 3222 N = 1,2
C      CHANGED SIGN BELOW TO -
C      C QPOL(L,N,M)=QPOL(L,N,M)-PPOL(M)-(CON3*SUM(1,N)-
C      3220   COH4 * SUM(2,N))
C      CNTINUE
C
C      DO 3222 K = 1,2
C      SUM(K,2) = COEF1 * SUM(K,2)
C
C      DO 3222 N = 1,2
C      CHANGED SIGN BELOW TO -
C      C QPOL(L,N,M)=QPOL(L,N,M)-PPOL(M)-(CON3*SUM(1,N)-
C      3225   COH4 * SUM(2,N))
C      CNTINUE
C
C      DO 3031 CMEGA(1,JKP,L) = OMEGA(1,JKP,L) + (ITPOL(M)+CONS*SUM(1,M))
C
C      3031 CONTINUE
C
C      RETURN
C
C END

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      C * * * 7/31/78 USING PHILLIPS GEOPOTENTIAL AT PCLES *
      C * * PRESSURE GRADIENT AND ENERGY CONVERSION TERMS FOR
      C * * MOMENTUM TEMPERATURE EQUATIONS
      C * * JPMOD(K,M) = (2,3,4)MOD(JM-1,5)+1 MOD((JM-1)-1,5)+1
      C * * MOD(JPK(K,M)) = (2,3,4)MOD(JM-1,3)+1,MOD(JM-2,3)+1
      C
      C      C PRPOL = SIGIL1 * PPOL(MI + PTOP
      C      C SKTPOL = SIGIL1 * KAPL * TPOL(L,M) / PRPL
      C      C VPOL = V(L,M,JP2MOD)
      C
      C COMPUTE SUMMATION FOR TEMPERATURE EQUATION
      C
      C DO 3210 I=1,IM
      C      3210 K = 1,2
      C
      C      DO 3220 K = 1,2
      C      JK = JPOL(K,M)
      C      JKMOD = JPMOD(K,M)
      C      MOD3J = MOD(JPK(K,M))
      C
      C      TERM1 = PHIL(L,JK,MOD) + VPOL(SPI(L,JK)
      C      SUM(K,1) = SUM(K,1) + COSLN((L,JK)) * TERM1
      C      SUM(K,2) = SUM(K,2) + SINLN((L,JK)) * TERM1
      C
      C      CONTINUE
      C      CNT INUE
      C
      C      DO 3222 K = 1,2
      C      SUM(K,2) = COEF1 * SUM(K,2)
      C
      C      DO 3222 N = 1,2
      C      CHANGED SIGN BELOW TO -
      C      C QPOL(L,N,M)=QPOL(L,N,M)-PPOL(M)-(CON3*SUM(1,N)-
      3220   COH4 * SUM(2,N))
      C      CNTINUE
      C
      C      DO 3222 K = 1,2
      C      SUM(K,2) = COEF1 * SUM(K,2)
      C
      C      DO 3222 N = 1,2
      C      CHANGED SIGN BELOW TO -
      C      C QPOL(L,N,M)=QPOL(L,N,M)-PPOL(M)-(CON3*SUM(1,N)-
      3225   COH4 * SUM(2,N))
      C      CNTINUE
      C
      C      DO 3031 CMEGA(1,JKP,L) = OMEGA(1,JKP,L) + (ITPOL(M)+CONS*SUM(1,M))
      C
      C      3031 CONTINUE
      C
      C      RETURN
      C
      C END

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/ COMP2 / SIZE OF PROGRAM 005398 HEXADECIMAL BYTES

NAME	TAG	TYPE	ADD.	NAME	TAG	TYPE	ADD.	NAME	TAG	TYPE	ADD.	
C	R84	000000	X	NAME	000000	X	NAME	000000	X	NAME	000000	
CE	I84	000054	L	SF	I84	000000	M	SF	I84	000000	F	I84
KSF	P84	000000	SF	XR	R84	000000	SF	C	R84	000000	FA	I84
JKP	XR	000000	Q	F	XR	000000	R	SF	R84	000000	N	SF
U	F	000000	D	F	XR	000000	SF	C	R84	000000	T	F
DD	R84	000000	DT	F	C	000000	ED	R84	000000	CP	C	
FX	SF	0000F4	F1	SF	R84	000000	F2	SF	R84	000000	EE	CE
GW	CE	R84	001680	GK	SF	R84	000100	JM	F	G3	SF	CE
IN	F	I84	000008	JL	SF	I84	000100	JM	F	GT	SF	CE
KH	C	I84	000008	JL	SF	I84	000100	LX	SF	C	CE	CE
PI	C	I84	000008	PK	SF	C	003904	PT	XR	CE	CE	CE
QT	XR	R84	000000	SH	SR	R84	000000	RS	CE	R84	000000	CE
UT	SF	R84	000930	VT	SF	SR	000000	WL	SF	R84	000000	CE
CDX	C	R84	000746	DXP	F	C	000118	DXU	C	R84	000118	DVF
DYU	F	C	0007ED	FIM	F	C	000118	FMU	C	R84	000118	INC
I2P1	SF	I84	000120	IP2	SF	I84	000124	ISI	SF	I84	000124	IS2
JKP	SFA	I84	000130	JNB	C	I84	000124	JNP	F	I84	000134	JPS
JS1	SFA	C	000060	JP2	SFA	C	000064	J5B	C	I84	000064	CE
JS2	SFA	I84	000138	JS2	SFA	I84	000138	LAF	SR	I84	000140	LPI
NPC	C	I84	000000	PH1	SF	R84	00013C	PIT	F	R84	000140	PLV
PK1	SF	R84	000100	PK2	SF	R84	000100	PL1	SFA	R84	000140	PL2
PSF	C	R84	000100	PSL	C	R84	000100	PSM	C	R84	000140	SA
RAD	C	R84	000100	SHS	CE	R84	0023DC	SHT	XR	R84	000140	SMG
SKT	SF	I84	000148	SUN	SF	I84	0057FC	TAU	SR	R84	000140	F
CON3	C	I84	008944	CON4	F	C	000000	CON1	SR	R84	000140	BETA
F	C	I84	000008	CON4	F	C	000000	CONS	F	R84	000140	COND
COSL	F	C	000000	CDP2	F	C	000000	COTH	F	R84	000140	COND
DLAT	C	R84	000000	DLDN3	SF	C	000000	DSIG	SR	R84	000140	DIFF
DUM4	SF	I84	000153	DUM3	SF	I84	000154	DYPS	F	R84	000140	DLAT
IDAY	C	I84	000120	IDMD2	C	I84	000154	INCP	F	R84	000140	DLAT
ITAU	C	I84	000120	JAYS	C	I84	000154	INCY	I84	I84	000140	JEND
JHOD	SF	I84	000158	JHPS	F	C	000154	JDAY	I84	I84	000140	JNS2
JNDS	C	I84	000008	KDLS	F	C	000000	JNS1	I84	I84	000140	JIUS
KAPA	F	C	000000	KNBS	C	I84	000084	JIPS	I84	I84	000140	LLMI
LLP1	SF	I84	000160	MRCN	C	I84	000084	KSBS	C	I84	000140	MRDT
NFLN	C	I84	000000	NLA1	F	I84	000000	MRDT	F	I84	000140	PHIS
PPDP	F	C	000010	GPDL	I84	I84	000000	PPOL	F	I84	000140	PPOL
SDOT	C	I84	000000	SIGE	F	C	000000	RGLS	I84	I84	000140	SINL
TERM	C	I84	000000	TAU1	C	I84	000000	TAUP	I84	I84	000140	TAUP
TAUE	C	I84	000000	TAU2	SF	I84	000000	TPOL	F	I84	000140	TPOL

NAME OF COMMON BLOCK * =0\$5E OF BLOCKCOMMON	081C00 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
PU R14 000000	
EQUIVALENCED VARIABLES WITHIN THIS COMMON GROUP	VARIABLE OFFSETS
VARIABLE OFFSETS	VARIABLE OFFSETS
GT 000B40	00168C
NAME OF COMMON BLOCK * =0\$5F_1E OF BLOCKCOMMON	000C00 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
ISUTCH_14 N.R.	
NAME OF COMMON BLOCK * =0\$5F_1E OF BLOCKCOMMON	0385AB HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
SDOT R14 000000	RADT 182
CONG L14 0389A4	019E00
EQUIVALENCED VARIABLES WITHIN THIS COMMON GROUP	VARIABLE OFFSETS
VARIABLE OFFSETS	VARIABLE OFFSETS
ISDOT 00CF00	
NAME OF COMMON BLOCK * =0\$6_1E OF BLOCKCOMMON	000C00 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
ISMTH 18E N.R.	N.R.
NAME OF COMMON BLOCK * =0\$6_1E OF BLOCKCOMMON	000C00 HEXADECIMAL BYTES
VAR. NAME TYPE REL. ADDR. HE VAR. NAME TYPE REL. ADDR. HE	VAR. NAME TYPE REL. ADDR. HE
C:M79 000000	

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ISN 0037          DUMMVII=0.01.L-N-J-Q(I,L,N,J) + ALPHS*(Q(IPINC,L,N,J) - Q(LININC,L,N,J))
      S Q(LI,L,N,J)-Q(I,L,N,J)
      IMINC=1
      10 I=IPNC
          DO 20 L=INC,IM,INC
              20 Q(L,I,N,J)=DUMMVII
                  CONTINUE
              30 IMINC=IM - INC
                  I = IM
                  DO 35 IPINC = INC,IM,INC
                      IF( I .LT. J )=DUMMVII
                      IMINC = I
                      35 I = IPINC
                          DO 40 L = INC,IM,INC
                              P(L,J) = DUMMVII
                          40 CONTINUE
                  GO TO 60

C * * * FOURIER SMOOTHING NEAR POLES
C 1/2*1/2 VERSION 3 SMOOTH ON P AND T
C 1FL(J,OGT,JWIND,AND(J,LT,JMAX))*.JG(JEQ,JNP) RETURN
      ISN 0053          JSUB = JSUM - - - 1
      ISN 0055          IF(JGE.JMAX) JSUB = J-1
      ISN 0056          DO 650 N = 1,4
      ISN 0058          N = 200>NNJ / 2
      ISN 0059          DO 650 L = 1,MLAY
      ISN 0060          DO 650 I = 1,IM
      ISN 0061          DATA(IJ) = Q(I,L,N,J)
                      CONTINUE
      ISN 0063          DO 670 I = 1,INDP1
      ISN 0064          TRAN(I) = SMTH(I,JSUB) * TRAN(I)
                      CONTINUE
      ISN 0065          CALL FOURT2(TRAN,IM,1,+1,-1)
      ISN 0066          DO 680 I = 1,IM
      ISN 0067          0(I,L,N,J) = DATA(IJ) / FLOAT(I)
                      CONTINUE
      ISN 0068          CALL SMSMAP
      ISN 0069          DO 690 I = 1,IM
      ISN 0070          SLPI(J) = P(I,J)
                      CONTINUE
      ISN 0071          100
      ISN 0072          DO 710 I = 1,IM
      ISN 0073          TSURF = T10(SLP(I,J),T(L,NLAY,I,J),T(L,NLAY,J,J),TSURF)
                      CONTINUE
      ISN 0074          110 IF( IM.GT.0IGO TO 781
      ISN 0075          DO 760 I=1,IM
      ISN 0077          DATA(IJ)=SLPI(I,J)
                      CONTINUE
      ISN 0078          CALL FOURT2(TRAN,IM,1,-1,0)
      ISN 0079          DO 770 I=1,INDP1
      ISN 0080          TRAN(I)=SMTH(I,JSUB)*TRAN(I)
                      CONTINUE
      ISN 0081          770 CALL FOURT2(TRAN,IM,1,1,-1)
      ISN 0082          DO 780 I=1,IM
      ISN 0083          SLPI(J)=DATA(IJ)/FLOAT(I)
                      CONTINUE
      ISN 0084          781 CONTINUE
      ISN 0085          782 CONTINUE
      ISN 0086          783 CONTINUE
      ISN 0087          784 CONTINUE
      ISN 0088          785 CONTINUE
      ISN 0089          786 CONTINUE
      ISN 0090          787 CONTINUE
      ISN 0091          788 CONTINUE
      ISN 0092          789 CONTINUE
      ISN 0093          790 CONTINUE

C * * * SMOOTH ALONG LONGITUDE (SEE SMSMAP)
      ISN 0094          NSM = 8
      ISN 0095          IF(I.JELT>8.35.JGT.JM-60) NSM = 4
      ISN 0096          IF(I.JELT<6.0.RJ.GT.JM-4) NSM = 2
      ISN 0097          SIGN = (-1)**NSM
      ISN 0098          CX = 4.88 NSM
      ISN 0099          DO 110 I = 1,IM
      ISN 0100          DATA(IJ) = SLPI(I,J)
                      CONTINUE
      ISN 0101          DO 140 N = 1,NSM
      ISN 0102          I = IM
      ISN 0103          DO 145 IP = 1,IN
      ISN 0104          DATA(IJ) = DATA(IP) - DATA(IJ)
                      CONTINUE
      ISN 0105          145 IS = IM
                          DO 150 I = 1,IN
                              DATA(IJ) = DATA(IJ) - DATA(IS)
                          150 IS = IM
                  CONTINUE
                  DO 160 I = 1,IN

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ISN 0119      160      SLP(I,J) = SLP(I,J) - SGN * DATA(I,J) / CX
ISN 0120      C * * * TRANSFORM BACK TO SURFACE PRESSURE
ISN 0121      MAXIT = 50
ISN 0122      DO 200 I = 1, IN
ISN 0123      PSFC = SLP(I,J) - PTOP
ISN 0124      PHISX = PHIS(I,J)
ISN 0125      DO 210 NITR = 1, MAXIT
ISN 0126      P1 = PSFC - T0*(PSFC/PHISX*TSURF) - PTOP
ISN 0127      PSFC = SUPFC(JI)
ISN 0128      TSURF = T0*(ABS(PSFC-PI)/1000.0*LEL1*SIG10)
ISN 0129      IF (ABS(PSFC-PI)/1000.0*LEL1*SIG10) .GT. 230
ISN 0131      PRINT 220, MAXIT, I,J, NITR, PSFC
ISN 0132      220 FORMAT(IX, MORE THAN ::.15, *ITERATIONS FOR FOF J=.15, * I=.15)
ISN 0133      230 PI(I,J) = PSFC
ISN 0134      CONTINUE
ISN 0135      200 RETURN
ISN 0136      END
ISN 0137

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/ AVR X / SIZE OF PROGRAM 00101A HEXADECIMAL BYTES

NAME	TAG	TYPE	ADD.	NAME	TAG	TYPE	ADD.	NAME	TAG	TYPE	ADD.
C	CE	F	I**4	No.R	I**4	SFA	I**4	No.R	I**4	SFA	I**4
L SF	C	N	I**4	0001A4	P	SF	X*	0001A4	Q	SF	X*
R	C	N	I**4	0000C	XR	X*	0000C	Y	XR	Y	
W	C	N	I**4	0000C	FA	X*	0000C	DT	CU	DT	
ED	C	N	I**4	0004C	CE	R**4	00168	I**4	SFA	I**4	
IP SF	C	I**4	I**4	0001AC	G*	R**4	00168	JM	C	JM	
KN	C	I**4	I**4	0001B4	IS SF	I**4	00030	I**4	C	I**4	
PK	C	I**4	I**4	0001B4	NR	C	164	No.R	PI	C	
TS	CE	R**4	R**4	00000C	PU	CE	R**4	00168	P1 S A	CE	
DXU	C	R**4	R**4	00189	ALP SF	C	R**4	00168	DXP F	C	
FNU	C	R**4	R**4	00189	DYP	C	R**4	0007EC	FIM	C	
INC SF	C	I**4	I**4	000044	FIM SF	C	R**4	0007EC	F98 FA	C	
JP2	C	I**4	I**4	000044	JNB	C	R**4	000054	JP1	C	
NPC	C	I**4	I**4	0001C4	JSB	C	R**4	000050	LAT	C	
RAD	C	I**4	I**4	0001C4	NSM SF	C	R**4	000050	PSL	C	
SFA	C	I**4	I**4	0001CE	SGN SF	C	R**4	0023D9	SIG	C	
ALPH SF	C	I**4	I**4	0004B0	SUM	C	R**4	000000	IND2 S ASF	C	
C0M1	C	R**4	R**4	0001CC	AIRX	C	R**4	0001DC	CATA SF	C	
CONS	C	C	R**4	0001CC	CON2	C	R**4	0001DC	CON2	C	
CPTH	C	C	R**4	0001DC	COSD	C	R**4	0001DC	CDP2	C	
DLN	C	C	R**4	000000	DATA SFA	CE	R**4	000000	DUFF	C	
FSD6	FA	R**4	R**4	000000	DRAT SF	CE	R**4	000000	DSIG	C	
INCS	C	C	I**4	0001E0	GRAY	C	R**4	000000	IDAY	C	
JDAY	C	I**4	I**4	0001E0	IRD	C	R**4	000000	TAU	C	
JAPS	C	I**4	I**4	0001E0	JEND	C	R**4	000000	JMIN	C	
JPJL	C	I**4	I**4	0001E0	JEN0	C	R**4	000000	JMS2	C	
JIUS	C	I**4	I**4	0001E0	JES1	C	I**4	000000	JSUM F	C	
MISS	S	I**4	I**4	0001E0	JSPH	C	R**4	000000	KNBS	C	
NITX SF	SF	I**4	I**4	0001E0	MRC	C	I**4	000000	MIROT	C	
PSFC SFA	SFA	I**4	I**4	0001E0	PTOP FA	C	I**4	000000	PNL	C	
SIGE	C	C	R**4	0001E4	SIND	C	R**4	000000	POPL	C	
TAUT	C	I**4	I**4	0001E4	TANL	C	R**4	000000	RGAS F	C	
VPOL	CE	I**4	I**4	000438	TPOL	CE	R**4	00045C	TAUP	C	
OSIGO	CE	I**4	I**4	000438	XINT	C	R**4	00045C	UPJL	C	
IPINC SF	CE	I**4	I**4	0001EC	UMMY SF	C	R**4	00045C	ALPHA	C	
INEXT	C	I**4	I**4	0001EC	ISM1H	C	I**4	00045C	INDEX	C	
JTEST	C	I**4	I**4	0001EC	JNPI	C	I**4	00045C	JDATE	C	
NSTEP	C	I**4	I**4	0001EC	JYEAR	C	I**4	00045C	JSP1	C	
RADIM	C	I**4	I**4	0001EC	PHISX SFA	C	R**4	0001F4	NDPK	C	
SLEXP S	ASF	I**4	I**4	000000	RHM4X	C	R**4	00045C	PDLSK	C	
FEXP S	XF	I**4	I**4	000000	THBAR	C	R**4	00045C	PSIGN	C	
ALBEDO	C	I**4	I**4	000000	EXP	XF	R**4	000000	SPUL	C	
CMMY	C	I**4	I**4	000000	CONVL	C	R**4	000000	FRXP16	C	
TECON	XF	I**4	I**4	000000	DUNVY	C	R**4	000000	ALOG	C	
NODUTH	C	I**4	I**4	000000	IAD2D	F	I**4	00002C	COSLON	C	
NDGDN	C	I**4	I**4	000000	MLAYN	C	I**4	000024	TEST	C	
PHISPL	C	I**4	I**4	000000	PIPOL	C	R**4	000024	FOURT2 SF	C	
SINLON	C	I**4	I**4	000000	TOFDAY	C	R**4	000000	ISTART	C	
									MAXIT SF	C	
									POLES C	C	
									SDPOL C	C	
									TRAN 3FA CE	C	
									ADLP C	C	
									IMINC SF	C	
									ALOG XF	C	
									TEST C	C	
									JPMD C	C	
									IOPC C	C	
									OPOL C	C	
									SINL C	C	
									TAU	C	
									KNBS	C	
									MIROT	C	
									PNL	C	
									POPL	C	
									RGAS F	C	
									TAUP	C	
									UPJL	C	
									ALPHA	C	
									INDEX	C	
									JDATE	C	
									JSP1	C	
									NDPK	C	
									SPUL	C	
									FRXP16	C	
									CMPY	C	
									CBLG	C	
									DMULT	C	
									ISLTCM	C	
									NCYCLE	C	
									NSTART	C	
									RDIST	C	
									YORE	C	

NAME OF COMMON BLOCK * F16.2E OF BLOCK COMMON

VAR.	NAME	TYPE	REL.	ADDR.	HE	VAR.	NAME	TYPE	REL.	ADDR.	HE	VAR.	NAME	TYPE	REL.	ADDR.
CON1	R**4	N.R	CON2	R**4	N.R	CON3	R**4	N.R	CON4	R**4	N.R	BETA	CON4	N.R	N.R	N.R
CONS	R**4	N.R	THBAR	R**4	N.R	ALPHA	R**4	N.R	BETA	R**4	N.R	RAD	ALPHA	N.R	N.R	N.R
IND2P1	I**4	000020	ADLCP	R**4	N.R	JMS2	I**4	N.R	THBAR	I**4	N.R	CDP2	JMS2	I**4	I**4	I**4
CPTH	R**4	N.R	PSKAPA	R**4	N.R	START	I**4	N.R	ADLCP	I**4	N.R	JP1	START	I**4	I**4	I**4
CF	I**4	I**4	INC	I**4	I**4	JEND	I**4	I**4	PSKAPA	I**4	I**4	MODP2	JEND	I**4	I**4	I**4
IND2	I**4	I**4	RADIN	R**4	N.R	NEXT	I**4	I**4	XLABEL	C	N.R	NEXT	NEXT	I**4	I**4	I**4

NAME OF COMMON BLOCK * F16.2E OF BLOCK COMMON

VAR.	NAME	TYPE	REL.	ADDR.	HE	VAR.	NAME	TYPE	REL.	ADDR.	HE	VAR.	NAME	TYPE	REL.	ADDR.
CON1	R**4	N.R	CON2	R**4	N.R	CON3	R**4	N.R	CON4	R**4	N.R	BETA	CON4	N.R	N.R	N.R
CONS	R**4	N.R	THBAR	R**4	N.R	ALPHA	R**4	N.R	BETA	R**4	N.R	RAD	ALPHA	N.R	N.R	N.R
IND2P1	I**4	000020	ADLCP	R**4	N.R	JMS2	I**4	N.R	THBAR	I**4	N.R	CDP2	JMS2	I**4	I**4	I**4
CPTH	R**4	N.R	PSKAPA	I**4	I**4	START	I**4	I**4	ADLCP	I**4	I**4	JP1	START	I**4	I**4	I**4
CF	I**4	I**4	INC	I**4	I**4	JEND	I**4	I**4	PSKAPA	I**4	I**4	MODP2	JEND	I**4	I**4	I**4
IND2	I**4	I**4	RADIN	R**4	N.R	NEXT	I**4	I**4	XLABEL	C	N.R	NEXT	NEXT	I**4	I**4	I**4

JPOL 164 No.R. JPMCD 164 No.R. S1BLIN 80344 VAR. NAME TYPE REL. ADDR. ME
 INDEX 164 No.R. PSIGN 80344 No.R. POLES 80344 No.R. CUSLJN 80344 VAR. NAME TYPE REL. ADDR. ME
 REC 80344 No.R. DIFF 80344 No.R. CONVL 80344 No.R. SDPOL 80344 VAR. NAME TYPE REL. ADDR. ME
 REC 80344 No.R. SUM 80344 No.R.
EQUIVALENCED VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSETE 00014 00014 00054 SPOL SPOL
 VARIABLE OFFSETE 00014 00014 00054 PCLC PCLC

NAME OF COMMON BLOCK * 1NTR3 OF BLOCKCOMMON 083C30 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 JSP 164 000001 JSP 164 000001 JSP 164 000001
 PTOP 80344 000010 PTOP 80344 000010 PTOP 80344 000010
 F14 80344 000035 F14 80344 000035 F14 80344 000035
 JK 164 000035 JK 164 000035 JK 164 000035
 MROT 164 000035 MROT 164 000035 MROT 164 000035
 JAYS 164 000035 JAYS 164 000035 JAYS 164 000035
 DLAT 164 000035 DLAT 164 000035 DLAT 164 000035
 ITAN 164 000035 ITAN 164 000035 ITAN 164 000035
 TODAY 80344 000035 TODAY 80344 000035 TODAY 80344 000035
 NSTEP 164 000035 NSTEP 164 000035 NSTEP 164 000035
 TAUP 164 000035 TAUP 164 000035 TAUP 164 000035
 DMULT 80344 000035 DMULT 80344 000035 DMULT 80344 000035
 KAPA 164 000035 KAPA 164 000035 KAPA 164 000035
 NFLB 164 000035 NFLB 164 000035 NFLB 164 000035
 SIN 80344 000035 SIN 80344 000035 SIN 80344 000035
 DUMNYC 80344 000035 DUMNYC 80344 000035 DUMNYC 80344 000035
 SIG 80344 000035 SIG 80344 000035 SIG 80344 000035
 JIPS 164 000035 JIPS 164 000035 JIPS 164 000035
 KSBS 164 000035 KSBS 164 000035 KSBS 164 000035
 DKP 80344 000723 DKP 80344 000723 DKP 80344 000723
 PHIS 80344 000050 PHIS 80344 000050 PHIS 80344 000050
 ALBEDO 162 ALBEDO 162 ALBEDO 162
EQUIVALENCED VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSETE 00023DC SHS 00023DC
 VARIABLE OFFSETE C 000000
 VARIABLE OFFSETE C 000000
 NAME OF COMMON BLOCK * 1N56.ZE OF BLOCKCOMMON 00000C HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 F5D6 80344 000000 F5D6 80344 000000 F5D6 80344 000000
 VARIABLE OFFSETE 000000
 NAME OF COMMON BLOCK * 0DS_2E OF BLOCKCOMMON 000004 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 ISOTCP 164 No.R.
 NAME OF COMMON BLOCK * *56-*E OF BLOCKCOMMON 00000E HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 ISMTH 164 No.R. NPC 164 No.R. JMAX 164 No.R.
 NAME OF COMMON BLOCK * * 51E OF BLOCKCOMMON 00000C HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 JMIN 164 000000 JMIN 164 000000 JMIN 164 000000
 NAME OF COMMON BLOCK * =0S55E OF BLOCKCOMMON 001100 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 PU 80344 000000 PU 80344 000000 PU 80344 000000
EQUIVALENCED VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSETE 0001EC G1 000240 GT
 VARIABLE OFFSETE 0001EC G1 000240 GT
 NAME OF COMMON BLOCK * =46.ZE OF BLOCKCOMMON 0033E70 HEXADECIMAL BYTES
 VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME VAR. NAME TYPE REL. ADDR. ME
 DATA 80344 000000 DATA 80344 000000 DATA 80344 000000
EQUIVALENCED VARIABLES WITHIN THIS COMMON GROUP
 VARIABLE OFFSETE 0001EC G1 000240 GT

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*OPTIONS IN EFFECT*
*OPTIONS IN EFFECT*
*STATISTICS* SOURCE STATEMENTS = 136 PROGRAM SIZE= 4122
*STATISTICS* NO DIAGNOSTICS GENERATED
***** END OF COMPILATION *****

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LEVEL 19.6-APR 71

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COMPILER OPTIONS - NAME= MAIN,OPT=02,LINECNT=55,SIZE=1C00K.
SOURCE=BCD(C,NOLIST,NODECK,LOAD,MAP,NOEDIT, ID,NOXREF
COMMON/FOURTH/CON1,CON2,CON3,CON4,CONS,TBAR,ALPHA,BETA,IND2P1,
$ IND2P,IND2,JMS1,CPTM,PPOL,QFOL,QTPL,QTQL,P1,QT,PTPL,QTQL,
$ IND2P,RADIN,IP1,JP2,MATNS,JNE,T12,MODPK(12,2),
$ JPOL(2,2),JPND(2,2),SINLCN(7,2),COSLN(7,2),INDEX(72),
$ PSIGN(4,4),POLES(14,8),T72(9,5),T72(9,3),OFF(9),
$ CONVPL(9,SDPL(9,2),TISPL(2,2),SUM(2,2),
$ DIMENSION PPOL(2),PTPCL(2),TPOL(36,1),QFOL(9,4,2),CT72(10,4,1)
INTEGER 2 ALBEDO
REAL*4 KAPALAT
REAL*8 SINLN,CDSLN,SUM
DIMENSION T(72,4,1),P(12880,1),GT(2880,1),GU(2880,1),CI(300)
COMMON/DMK2/PU(2880,46)
EQUIVALENCE
1(TS(1,1),PHS(172,1,1)),ISHS(1,1),FHS(144,1,1),
2,(GT(1,1),PU(72,1,1)),(GU(1,1),P(144,1,1),(CI(1,1),JSP)
COMMON/JCNTRL,JSP,IM,NLAY,PROPISTART,JSP1,JNP1,FIM,NLAY1,NLAYP1.
* JI,JMK,TAUT,IRUT,MROT,TEST,TEST.
* DT,TAU,ITA,XINT,DAY,TOFDAY,DATE,MONTH(2),JYEAR,INSTEP.
* CYCLE,INCOMP,INHGANT,TAUP,TAU1,TAU2,TALO,DTMULT,
* PI,GRAV,RGAS,KAD,APSL,ED,FNU,NELN,PS,PRCH,RS(1,1),SIND,CQSD,
* RMAX,CX,DUNIV,CX,II,WTER,DUM199,
* XLABEL(20),SIG(20),DSIG(20),SIG(21),LSI(GO(19),
* JIPS(11),JPS(11),IUS(11),JNU(11),KSES(11),BS(11),
* LAT(46),DX(46),DXP(46),DXU(46),CPT(46),CXP(46),F(46),SINL(45),
* COSI(JA(6),DU(6)),PMIS(2880,46),CALBED(72,46),
COMMON/SWTH/DATE(150),CATAI(150),SLP(172,45),
COMMON/NSMH/F5D6,F17,F98
COMMON/DEBUG/ISWTCH
COMMON/SMHD/ISMTN,NPC
COMMON/MFLS/NSEQ,HLF(10),HATSNX,NSML,NCM 1
DATA J2Z/2/

```

```

C * * * DEFINITION OF SURFACE TEMPERATURE AND
C * * * SEA LEVEL PRESSURE FUNCTIONS
C
C SLEXP(HI,T10) = EXP(HI / T10 + F98 * HI / 287) *
T10*PP, T9 = IT8 * ALOG(PP + PTOP) / (F56 * PP + PTOP) /
$ / ALOG((F17 * PP + PTOP) / (F56 * PP + PTOP))
C
C * * FIRST J LOOP
C * * * GET SURFACE PRESSURE AND TEMPERATURE INCLUDING POLES
C
IF(INSTEPole,NSM1)RETURN
N1
D1 200 J = 1,JNP
IF (J .NE. 1 .AND. J .NE. JNP) GO TO 120
DO 130 L = 1,NLAY
C
C POT(J,J1) = TPOL(L,N)
CONTINUE
N=2
130 SLP(1,J) = PPOL(M,

```

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ISN 0013
ISN 0014
ISN 0015
ISN 0016
ISN 0017
ISN 0018
ISN 0019
ISN 0020
ISN 0021
ISN 0022
ISN 0023
ISN 0024
ISN 0025
ISN 0026
ISN 0027
ISN 0028
ISN 0029
ISN 0030
ISN 0031
ISN 0032

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ISN 0191      SLP((I,J)) = SLP(I,J)          CNTINUE
ISN 0192      1360                           CNTINUE
ISN 0193      I310                           CNTINUE
C * * TRANSFORM BACK TO TEMPERATURE
C
ISN 0194      DO 1400 L = 1,NLAY
ISN 0195      DO 1420 L = 1,IM
ISN 0196      PKA = EXP(KISLP((I,J)) * SIG(L) + PTOL)
ISN 0197      POT((L,J,L)) = PG((I,J,L)) * PKAP
ISN 0198      IF ((J.EQ.1 .OR. J.EQ.JNP)) GO TO 1430
ISN 0200      CONTINUE
ISN 0201      GO TO 1400
ISN 0202      1430 DC 1440 I = 2,IM
ISN 0203      POT((I,J,L)) = POT((I,J,L))
ISN 0204      1440                           CNTINUE
ISN 0205      I400                           CNTINUE
C * * RETURN SMOOTHED VALUES
C
ISN 0206      DO 1520 L = 1,NLAY
ISN 0207      DO 1520 I = 1,IM
ISN 0208      T(I,L,J) = POT((I,J,L))
ISN 0209      1520                           CNTINUE
ISN 0210      1525 DC 1530 I = 1,IM
ISN 0211      PI(J,I) = SLP((I,J))
ISN 0212      1530                           CNTINUE
ISN 0213      2000                           CNTINUE
ISN 0214      DO 1550 L = 1,NLAY
ISN 0215      TPOL((L,J)) = POT((I,J,L))
ISN 0216      TPOL((L,J2)) = POT((I,JNP,L))
ISN 0217      1550                           CNTINUE
ISN 0218      *** PPOL((1)) = SLP((1,1))
ISN 0219      PPOL((2)) = SLP((1,JNP))
ISN 0220      IF ((ATNSX(EGO).RETURN))
ISN 0221      12/14 RUN HERE TILL RETURN
ISN 0222      DO 500 J=2,IM
ISN 0223      DO 500 N=1,4
ISN 0224      DO 500 K=1,NLAY
ISN 0225      DO 500 I=1,IM
ISN 0226      QT((I,K,N,J)=P((I,J)*DXY(P,J))*Q((I,K,N,J))
ISN 0227      500                           CNTINUE
ISN 0228      DO 501 J=2,IM
ISN 0229      DC 501 I=1,IM
ISN 0230      PT((I,J))=P((I,J))
ISN 0231      501                           CNTINUE
ISN 0232      DO 502 L=1,NLAY
ISN 0233      DO 502 N=1,6
ISN 0234      DO 502 M=1,2
ISN 0235      QTPOL((N,M))=PPOL((N,M))
ISN 0236      CONTINUE
ISN 0237      PTPOL((1))=PPOL((1))
ISN 0238      PTPOL((2))=PPOL((2))
ISN 0239      599 FORMAT(1X, NEW SMOOTHER ENTERED, TAU=.F12.3,
ISN 0240      RETURN
ISN 0241      END

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