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Experimental and Analytical Study of the Longitudinal Aerodynamic Characteristics of Analytically and Empirically Designed Strake-Wing Configurations at Subcritical Speeds

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SUMMARY

Sixteen analytically and empirically designed strakes have been tested experimentally on a wing-body at three subcritical speeds in such a way as to isolate the strake-forebody loads from the wing-afterbody loads. Analytical estimates for these longitudinal results have been made using the suction analogy and the augmented vortex lift concepts. The comparisons show that the pitch data, both total and components, are bracketed well by the high- and lowangle-of-attack modelings of the vortex lift theories. The lift data are generally better estimated by the high-angle-of-attack vortex lift theory and then only until maximum lift or strake-vortex breakdown occurs over the wing. The compressibility effects noted in the data for the strake-forebody lift are explained theoretically by a reduction in the wing upwash associated with increasing Mach number which leads to smaller potential and vortex lifts on the forward lifting surfaces.

Aerodynamic synergism was investigated experimentally; as expected, there was an additional lift benefit for all configurations as a result of the interaction. Furthermore, there was a delay in pitch-up associated with the synergism.

Mach number has a small effect on the "additional lifting surface efficiency factor" whereas changes in the strake geometry have larger effects. Geometry changes such as increasing area or slenderness ratio generally produce a more efficient strake. However, it is possible to obtain the larger values of this factor with approximately half the area of the original, also the largest, gothic strake by using a suitable analytical design for the gothic leading edge. These results correlate well with strake-vortex-breakdown observations in the water tunnel.

Strake geometry is also important in determining the maximum lift that a configuration will develop, with gothic leading-edge shaping being preferred for ratios of strake area to wing reference area of less than 0.25 based on the strakes considered herein.

INTRODUCTION

Strake-wing aerodynamics are becoming of increasing interest due to the mutual benefits derived from the combination. (See ref. 1.) For the wing, these benefits include: (1) minimal interference at or below the cruise¹ angle of attack, (2) upper-surface boundary-layer control at moderate to high angle

¹In particular, at cruise it is possible that the small impact of the strake may only be attainable by the use of camber or dihedral so as to "unload" the strake under this condition. Neither one of these is addressed in this paper, as only planar strakes are considered.

of attack due to the strake vortex, (3) load redistribution due to effective use of the upper surface, and (4) reduced area required for maneuver loads. For the strake, these benefits are: (1) strake vortex strengthened by upwash from the main wing and (2) the need for only a small area - hence, wetted area and comparatively lightweight structure - to generate its significant contribution to the total lift because the strake provides large amounts of vortex lift.

In view of these strake benefits, it is appropriate to consider how best to maximize them by proper shaping of the strake. One way would be to use an empirical approach based on previous knowledge, a second would be cut-and-try, a third would be analytical, and a fourth would be a combination of the preceding three. At the time of development of the lightweight fighters F-16 and YF-17, only the first two procedures were available. After these airplanes were developed, reports were written, references 2 and 3, which summarized the wind-tunnel test results of about 100 different strakes for each airplane, along with an analysis to help guide future strake-wing integrations. However, these reports still do not give the aerodynamicist an analytical method for shaping the strake leading edge. One possible approach would be to isolate some critical parameter, such as leading-edge suction, and then design the strake in the presence of the wing while monitoring this parameter.

As a step in this direction, a simpler approach with the emphasis on delaying strake-vortex breakdown has been developed and reported in reference 4. There the shape of the isolated strake is determined uniquely in a flow which is simpler but related to the three-dimensional potential by specifying primarily the leading-edge suction distribution. Reference 4 reports the first design application of this method in which the resulting shape was area scaled until the three-dimensional suction distribution over both the strake and the wing was considered to be acceptable. The windtunnel test of the strake-wing combination showed it to perform well. However, to determine if this method could be used to develop better strakes, it was applied to the development of over 200 configurations. Only 24 were considered suitable, or interesting enough, for further evaluation. These, along with 19 empirically designed strakes mounted on the same wing-body, were tested, in a cooperative program with the authors, in the Northrop 16- by 24-Inch Diagnostic Water Tunnel. From the results reported in references 5 and 6, only 16 strake-wing configurations, 7 analytically designed and 9 empirically designed, were considered of sufficient interest to be tested on a similar wing-body in a wind tunnel. These tests, like those in water, were to be done at zero sideslip because of the large test matrix involved. It is recognized that the effects of sideslip and leading- and trailing-edge flaps are important with regard to vortex breakdown and the resulting amount of useful lift attainable; however, these effects are beyond the scope of the present study. This report documents the wind-tunnel results and presents the analytical estimates for both the complete configurations and the components using the method described in references 1, 4, and 7.

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SYMBOLS AND ABBREVIATIONS

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Dimensional quantities are given in both SI Units and U.S. Customary Units. Measurements and calculations were made in U.S. Customary Units.

AD	analytically designed
Ъ	span ($b_w = 50.8 \text{ cm} (20 \text{ in.})$)
с	constant pressure specification in strake design
c _D	drag coefficient, $\frac{\text{Drag}}{q_{\omega} s_{\text{ref}}}$
C _{D,0}	experimental value of drag coefficient at $C_{L} = 0$
cL	lift coefficient, $\frac{\text{Lift}}{q_{\omega}s_{\text{ref}}}$
C _{L,max}	maximum value of $C_{L,tot}$
c _m	pitching-moment coefficient about 56.99 percent body length station, $\frac{\text{Pitching moment}}{q_{\infty}s_{\text{ref}}c_{\text{ref}}}$
۵cp	lifting pressure coefficient
c _s	leading-edge suction-force coefficient, $K_{v,le} \sin^2 \alpha$
CT	leading-edge thrust-force coefficient,
с	chord, cm (in.)
ĉ	characteristic length used in determination of $K_{v,se}$, cm (in.)
c _{ref}	reference chord, 23.33 cm (9.185 in.)
cs	section suction-force coefficient, $\frac{\text{Section suction force}}{q_{\infty}c}$
dFs	differential leading-edge suction force (see sketch D)
đĩ	differential leading-edge length
ED	empirically designed

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 $\frac{(C_{L,tot})_{swb}}{(C_{L,tot})_{wb}} \left(\frac{S_{ref}}{S_{ref} + S_s} \right)$ additional lifting surface efficiency factor, f ∂(Normal force/q_∞S_{ref}) (KP in table IV) Kp potential lift factor, ∂ (sin α cos α) vortex lift factor (KV in table IV) Κv Kv,le (KV LE in table IV) d sin² a q_S_{ref} side-edge vortex lift factor, K_{v,se} $\frac{1}{q_{\infty}s_{\text{ref}}} \frac{\partial (|s.F.|_{se,left} + |s.F.|_{se,right})}{\partial \sin^2 \alpha}$ (KV SE in table IV) augmented vortex lift factor, $(K_{v,le}/l)\tilde{c}$ (see appendix A) K_v, se l distance along leading edge from apex, cm (in.) free-stream Mach number М polynomial pressure specification in strake design \mathbf{P} free-stream dynamic pressure, N/m^2 (lb/ft²) d^{∞} ratio of exposed strake area to wing reference area, S_S/S_{ref} Ra exposed semispan ratio, $[(b/2)_{s}/(b/2)_{w}]_{exp}$ Rb strake slenderness ratio, (Length/Semispan) exp Rs radius of curvature, cm (in.) r S area reference wing area, 0.1032 m^2 (1.1109 ft²) Sref potential-flow suction force S.F. $= \frac{c_s c}{\alpha^2 (b/2)}$ s free-stream velocity, m/sec (ft/sec) U

Wnet	sum of induced downwash and U α at α = 1 rad, m/sec (ft/sec)
- Wnet	average value of w _{net} , m/sec (ft/sec)
x,y	local coordinates defining strake planform, cm (in.) (see table III)
x _c	location of centroid of particular loading, cm (in.)
×ref	location of reference point from nose of model, 54.832 cm (21.587 in.) (X SUB REF in table IV)
x	= $x_{ref} - x_{c,i}$, cm (in.) (i stands for subscripts p, le, se, and \overline{se})
α	angle of attack, deg (ALPHA in table IV)
Γ(1)	equivalent circulation associated with leading-edge suction, m ² /sec (ft ² /sec)
Γ(1)	average value of $\Gamma(l)$, m^2/sec (ft ² /sec)
η	fraction of exposed strake semispan
Λ	leading-edge sweep angle, deg
ρ	density of fluid, kg/m^3 (slugs/ft ³)
3-D	three-dimensional
Subscripts	3:
BD-TE	strake vortex breakdown at wing trailing edge in water tunnel
exp	exposed
inb'd	inboard -
le	leading edge
max	maximum
outb'd	outboard
р	potential
r	root
S	strake
se	side edge
se	augmented side edge

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swb strake-wing-body configuration

tot total configuration

vle vortex effect due to leading edge

vse vortex effect due to side edge

vse vortex effect due to augmented term

w wing

wb wing body

MODEL DESCRIPTION AND TEST CONDITIONS

The model was composed of a basic wing-fuselage onto which were mounted any of 16 pairs of strakes; the resulting configuration was tested in the Langley High-Speed 7- by 10-Foot Tunnel. Individual descriptions of the various model components follow.

Basic Wing-Body

The basic wing-body used in this test is shown in figure 1. The model features forebody and afterbody components separated by a metric break for multiple component aerodynamic testing. Total loads were measured by the main balance located in the aft fuselage while strake-forebody loads were measured by the forebody balance attached to, but ahead of, the metric break. Because a few strakes were very long, wings had to be mounted on the aft fuselage in an aft position for those runs. (See tables I and II for appropriate wing position and parametric descriptions of the strakes.) The aft wing position was 4.39 cm (1.73 in.) rearward of the more commonly used forward wing position which is shown in figure 1.

The wing has an untwisted, 44° swept trapezoidal planform with reference aspect ratio, taper ratio, and area of 2.5, 0.2, and 0.1032 m² (1.1109 ft²), respectively. Its airfoil sections are symmetrical, uncambered, and biconvex and vary linearly in maximum thickness from 6 percent of chord at the wingfuselage juncture to 4 percent at the tip. The preceding features are based on the reference wing which includes area between the leading and trailing edges projected to the model center line. The moment reference point is defined as the longitudinal position of the quarter-chord point of the wing at the wing-fuselage juncture when the wing is mounted in the forward position and corresponds to 56.99 percent of the body length.

Body and strake wipers were installed to prevent flow through the metric break between the two parts of the fuselage and the strake and wing. These wipers consisted of thin-gage steel tack welded to the lower surface of the strake and Mylar² glued around the forebody so as to transmit essentially no load from one component to the other. (See ref. 7.) Figure 2 shows a photograph of a typical model with wipers on.

No. 120 carborundum grit was applied to the forebody in a ring 2.54 cm (1 in.) aft of the nose. This same size grit was also applied 2.54 cm (1 in.) aft of the leading edges of the strake and wing on both the top and bottom surfaces.

Strakes

Figure 3 shows the strake planforms initially tested in the water tunnel (ref. 5), along with the prescribed suction distributions used to generate their shapes and whether constant pressure specification C or polynomial pressure specification P was employed. The 16 strakes selected for the present wind-tunnel tests are delineated by shading in figure 3. In table III, the planform perimeters of the 16 strakes are defined. The groups identified refer to either the basic shapes that resulted from the analytical studies - reflexive and gothic - or those strakes which were variations of the AD 24 strake and were therefore designated "empirically designed."

All strakes were constructed of 0.318 cm (0.125 in.) flat plate steel with the edges nominally beveled to a sharp edge. The strakes were attached to the forebody ahead of the metric break through the use of small body slots and minimal external brackets. (It should be mentioned that the strake-body was tested alone with no wing to aid in the assessment of lift and pitching-moment synergistic effects.) Figure 4 shows a photograph of some of the strakes.

Analytically Designed Strakes

There are seven strakes in the analytically designed group, and they are designated by an AD prefix. One (AD 24) is the original strake, two others (AD 22 and AD 23) are different area scalings of the AD 24 strake, and the remainder are composed of three gothic strakes (AD 14, AD 17, and AD 19) and one reflexive strake (AD 9). Note that the reflexive stake AD 9 (fig. 3(a)) has the same prescribed $s-\eta$ distribution as does the gothic strake AD 19 (fig. 3(b)); the primary difference in their design is due to the differing pressure specification. For additional details of these analytically designed strakes, see table I and reference 5.

Empirically Designed Strakes

The nine strakes in the empically designed group are designated by an ED prefix and are categorized by either being scaled (ED 12 and ED 13) or cut (ED 2, ED 4, ED 5, ED 6, ED 9, ED 10, and ED 11). The scaled strakes have their chords scaled to either 70 or 30 percent of the AD 24 strake. The cut series

²Mylar: Registered trademark of E. I. duPont de Nemours & Co., Inc.

are trimmed versions of the AD 24 strake having area removed along the apex, trailing-edge, or inboard-edge regions. However the strake is altered, it always abuts the fuselage and wing simultaneously. See table II and reference 5 for additional details.

Test Conditions and Corrections

The tests were conducted in the Langley High-Speed 7- by 10-Foot Tunnel at Mach numbers of 0.2, 0.5, and 0.7 and atmospheric conditions. These Mach numbers correspond to Reynolds numbers, based on c_{ref} , of 1.08 × 10⁶, 2.39 × 10⁶, and 2.87 × 10⁶, respectively. The model was mounted on the high-angle-of-attack sting support system shown in figure 5 and was tested only at zero sideslip. The angle of attack varied from approximately -2^o to approximately 53^o.

Blockage and jet-boundary corrections have been applied to the data, and the angle of attack used herein has been corrected for sting deflection. All drag measurements have been corrected to a condition of free-stream static pressure in the balance chambers and on the forebody base. For the main balance, this correction was applied to the chamber only since the model base was feathered.

RESULTS AND DISCUSSION

Results from the wind-tunnel tests at the three test Mach numbers are presented herein with an analysis of the various geometrical effects; the test results are compared with theoretical estimates, where appropriate. The theoretical method used is detailed to show how the different aerodynamic components are treated in each angle-of-attack range. Aerodynamic synergism is discussed for both lift and pitching moment, along with the effects of Mach number and strake geometry on the "additional lifting surface efficiency factor." The latter is a measure of how efficient the strake-wing-body synergism is in relation to simply increasing the wing area by an amount equal to that of the strake.

Basic Data Presentation

The basic longitudinal data are presented in figures 6 to 8. In these figures the effects of Mach number on the aerodynamic loads are given for the complete configuration (fig. 6) and for the wing-afterbody and strake-forebody components (figs. 7 and 8, respectively).

Effect of Mach Number on Total Longitudinal Characteristics

Figures 6(a) to 6(p) present the total-model longitudinal aerodynamic characteristics at Mach numbers of 0.2, 0.5, and 0.7. For each of these three Mach numbers, the difference in maximum angle of attack was due to the model

reaching the support system or balance limits, or encountering severe buffeting at different values in the pitch run. Increasing Mach number has the expected effect of increasing $C_{L,tot}$, although by a small amount, at the lower values of α , as well as providing a slight increase in the longitudinal stability below C_{L,max}. For shorthand notation, all strake-wing configurations will henceforth be denoted by the strake designation. Some of the strake-wing configurations, AD 9, AD 14, AD 17, AD 22, AD 23, AD 24, ED 9, and ED 11, exhibit a slight increase in the value of $C_{L,max}$ with increasing Mach number. A discussion of $C_{L,max}$ is presented in more detail in the section "Synergistic Effects." All but the smallest configurations ($R_a \approx 0.1$), AD 22, ED 4, ED 6, and ED 13, develop pitch-up at the higher values of $C_{L,tot}$ and M = 0.2because the strakes generate a significant portion of the total lift once the strake-vortex breakdown has progressed ahead of the wing-strake juncture. For the test Mach number range, the drag-coefficient results show no strong effect of compressibility on $C_{D,O}$; thus, there is little difference in C_D with changing Mach number up to near CL, max. The data themselves vary as $C_{D,O} + C_{L} \tan \alpha$.

Effect of Mach Number on Component Longitudinal Characteristics

Figures 7(a) to 7(p) and 8(a) to 8(p) show the effects of Mach number on the wing-afterbody and the strake-forebody longitudinal aerodynamic characteristics, respectively. There, C_D and C_m are plotted against $C_{L,tot}$ so that the contributions to the total model, shown in figure 6, can be isolated and presented in a similar format. In the discussion of figure 6 it was noted that C_L for the total configuration increased with M at a fixed angle of attack. From figure 7 the wing-afterbody is seen to behave in the same manner as the total configuration; whereas, from figure 8 the strake-forebody shows a reduction in lift with increasing Mach number. It is somewhat surprising that the strake-forebody lift coefficient should fall off with increasing Mach number since these 16 strake components are low-aspect-ratio lifting surfaces and hence should exhibit very little sensitivity to changes in Mach number. Evidently the cause for the reduction in $\,C_{\rm L}\,$ is the decrease in wing upwash associated with the increasing subsonic Mach number, as reported in reference 1. This is discussed in more detail later. However, it is not surprising that the increase in CL, max, which occurs for some strake-wing-body configurations at M = 0.5, shows up on the wing-afterbody graphs since the wing is a moderate-aspect-ratio lifting surface and therefore Mach number sensitive. Due to model and/or balance limitations, $C_{L,max}$ was not reached at M = 0.7. Lastly, the pitch-up reported previously for certain configurations results from the pitch-down tendency of the wing-afterbody at higher values of α or being exceeded by the pitch-up tendency of the strake-forebody. This C_{L.tot} has been alluded to already. Configurations of this type with vortex breakdown on the lee side would need to employ a low tail for stability and control.

The analytical estimation of the Mach effect on the longitudinal aerodynamic characteristics is taken up later for both a complete configuration and its components.

Theoretical Results

This section contains a description of the manner in which the strakeforebody and the wing-afterbody were theoretically modeled using the suction analogy. Also, comparisons are made between analytical estimates and data results for both total and component aerodynamic loads.

Modeling Method

The suction analogy has been used successfully to estimate the vortexflow contributions to lift, drag, and pitching moment associated with the potential-flow edge force (i.e., unaugmented terms) for delta and rectangular wings. However, for configurations in which forward-shed vorticity passes over the aft part of the configuration, another contribution to vortex lift can arise (ref. 8). It is designated "augmented vortex lift" in reference 9, and its basic derivation is repeated in appendix A of the present paper for completeness. These two separate types of vortex lift (ref. 7) are illustrated in sketch A for a strake-wing configuration.



Sketch A.- Basic theoretical approach.

References 4 and 7 point out that, depending on the range of α , there are two different flow-field models which are appropriate for a strake-wing

configuration. These two models (ref. 7), shown in sketch B, are determined from oil-flow and water-vapor photographs in the Langley wind tunnel and from dye studies in the Northrop water tunnel. Sketch B shows that at low angles



Sketch B.- Theoretical vortex lift model for strake wing.

of attack the strake and wing leading-edge vortices were individually distinguishable over the wing. However, at high angles of attack the wing surface flow pattern evidenced one region of spanwise vortex flow. Although the highangle-of-attack flow patterns might be interpreted as strake- and wing-vortex coalescence, additional observations revealed the presence of the unburst wing leading-edge vortex core in addition to the strake core at the high values of α . These observations suggest that the wing vortex had not coalesced with the strake vortex but merely had been displaced away from the wing upper surface by the strake vortex, thus allowing the strake vortex to dominate the surface flow patterns. Accordingly, the vortex lift effects due to the wing leadingedge and side-edge vortices may be decreased at high angles of attack because of their vertical displacement.

Putting all the preceding concepts together leads to the generalized forms of the equations for $C_{\rm L}$, $C_{\rm D}$, and $C_{\rm m}$ associated with the following suction analogy. These equations contain the direct and augmented vortex lift terms and are explicitly

$$C_{I} = K_{D} \sin \alpha \cos^{2} \alpha + (K_{V,le} + K_{V,se} + K_{V,se}) \sin \alpha |\sin \alpha \cos \alpha$$
 (1a)

$$C_D = C_{D,O} + C_L \tan \alpha = C_{D,O} + K_p \sin^2 \alpha \cos \alpha + (K_{v,le} + K_{v,se} + K_{v,se}) \sin^3 \alpha$$

(1b)

$$C_{m} = K_{p} \frac{\bar{x}_{p}}{c_{ref}} \sin \alpha \cos \alpha + \left(K_{v,le} \frac{\bar{x}_{le}}{c_{ref}} + K_{v,se} \frac{\bar{x}_{se}}{c_{ref}} + K_{v,se} \frac{\bar{x}_{se}}{c_{ref}} \right) |\sin \alpha| \sin \alpha$$
(1c)

where the particular x-terms equal $x_{ref} - x_{C,i}$ with i standing for p, le, se, or se. It is realized that each of the terms in equations (1) may be for a single planform or be representative of combinational terms of the same type for the strake-wing configuration. The values of $K_{v,le}$ and $K_{v,se}$ are easily obtainable for each planform by appropriate use of computer codes, such as the vortex-lattice method described in reference 10. However, the $K_{v,se}$ terms require attention as to their computation (appendix A), origin, and angleof-attack range of validity.

From sketch C it can be seen that at low angles of attack where the vortex is small, the negative augmentation factor associated with the swept-back



Sketch C .- Theoretical vortex lift parameters for strake wing.

trailing edge of the strake (ref. 9) will be negligible and is therefore taken to be zero in the computation. Augmented effects will occur on the wing due to both the wing and strake vortices and may be expressed as

$$\left(K_{\mathbf{v}, \mathbf{se}} \right)_{\mathbf{W}} = \frac{(K_{\mathbf{v}, le})_{\mathbf{W}}}{l_{\mathbf{W}}} \tilde{c}_{\text{outb'd}, \mathbf{W}} + \frac{(K_{\mathbf{v}, le})_{\mathbf{s}} + (K_{\mathbf{v}, \mathbf{se}})_{\mathbf{s}}}{l_{\mathbf{s}}} \tilde{c}_{\text{inb'd}, \mathbf{W}}$$
(2)

where l_W is the length of the exposed wing leading edge, $\tilde{c}_{outb'd,W}$ is the tip chord, and $\tilde{c}_{inb'd,W}$ is the wing chord at the strake-wing juncture. (See sketch C.) At high angles of attack, vortex lift will be lost by the strake due to the trailing-edge notch as would occur for an isolated strake. However, this vortex lift will not be lost to the configuration; it will be recovered by the wing as part of the augmented-vortex-lift effect due to the strake vortex. To approximate the length which the strake vortex persists over the wing, the chord at the wing-fuselage juncture was chosen. The augmented effects at high angles of attack may be expressed as

$$(K_{v,se})_{s} = \frac{(K_{v,le})_{s} + (K_{v,se})_{s}}{l_{s}} \tilde{c}_{s}$$
(3)

and

$$(K_{v,se})_{w} = \frac{(K_{v,le})_{s} + (K_{v,se})_{s}}{l_{s}} \tilde{c}_{w}$$
(4)

Because vortex lift associated with the wing leading-edge and side-edge vortices may be decreased due to the aforementioned vertical displacement effects, it may be assumed that

$$(K_{v,le})_{w} = (K_{v,se})_{w} = 0$$
(5)

as a limiting case for high angle of attack.

In the computation of C_m , the value of $x_{C,se}$ associated with each individual piece of augmented vortex lift is taken to be coincident with the centroid of the affected geometrical area. For example, at low angles of attack along the wing tip, the term $\frac{(K_{v,le})_{w}}{l_{w}} \sim c_{outb'd,w}$ acts at the center of the tip chord.

The preceding then is the method used to make the theoretical estimates of C_L , C_D , and C_m for the strake-forebody, the wing-afterbody, and the total configuration. For reference, the values of K_p , K_v , and \bar{x} are summarized for both high-angle-of-attack and low-angle-of-attack solutions in table IV for all configurations at M = 0.2, in table V for the AD 19 configuration at M = 0.2, 0.5, and 0.7, and in table VI for the basic wing-body (both forward and aft wing positions) at M = 0.2, 0.5, and 0.7.

Comparison With Data at M = 0.2

Complete configuration. - Figures 9(a) to 9(p) present high-angle-of-attack and low-angle-of-attack vortex lift estimates, along with data for the longitudinal aerodynamic characteristics of complete configurations at M = 0.2. A comparison for C_D shows that up to $C_{L,max}$ or vortex breakdown, the high angle-of-attack vortex lift theory (including $C_{D,O}$) yields the better agreement with the C_L and C_D data. Within this range of α , the C_L data in some cases exceeds the high-angle-of-attack theory. This indicates that the wing may be contributing some vortex lift to the total, and, therefore, all of the assumptions for the high-angle-of-attack theory are not realized. Above this range of α neither theory appropriately models the flow. It is also seen that the two theories generally bracket the C_m data, again up to $C_{L,max}$ or vortex breakdown. The ability of the theories to do this is encouraging in that they are able to estimate collectively the general nonlinear C_m versus $C_{L,tot}$ characteristics for this class of configuration. It can be noted that the lowangle-of-attack vortex lift theory may, in general, estimate better the Cm results than those obtained with the high-angle-of-attack theory (fig. 9(m), for example). This occurs because the low-angle-of-attack theory produces a load center farther aft at a particular value of $C_{L,tot}$ even though this value is larger than the data at the same angle of attack.

The potential-flow curve is added to the $C_{L,tot}$ versus α plots for reference. It is interesting to note that for the configurations with the smaller values of R_a , in particular AD 22, ED 4, and ED 13, the $C_{L,tot}$ data at the higher angles of attack tend to follow the $C_{L,p}$ curve even though the flow there is nothing like potential.

Components.- The wing-afterbody and strake-forebody longitudinal aerodynamic data and the high-angle-of-attack and low-angle-of-attack estimates at M = 0.2 are given in figures 10(a) to 10(p). Just as for the complete configuration, the individual data components are generally well estimated by the high-angle-of-attack theory or a collective combination of theories up to $C_{L,max}$ or large-scale vortex breakdown. What is particularly useful is that the individual C_m components are tightly bracketed by the high-angle-of-attack and low-angle-of-attack vortex lift theories. The C_L data for the strakeforebody are, in general, reasonably well estimated by the two closely spaced theories until the strake vortex begins to break down on the strake at the higher values of α . The spacing between the two theories is larger for the wing-afterbody, with the data tending to be generally on or above the estimates from the high-angle-of-attack theory. This continues until the strake vortex begins to break down ahead of the wing trailing edge. From these figures it is seen that, in general, those configurations which have the higher values of Rb, i.e., AD 24, ED 4, ED 5, ED 6, ED 12, and ED 13, have their aerodynamic components better estimated by the high-angle-of-attack theory than do the others. A reason could be that the larger strake span is better modeled by this theory since it may provide proportionately more area for a given length, which in turn enables the strake vortex to act more completely on the strake and not on the fuselage. (See ref. 7.) Lastly, note that at the higher angles of attack the wing-afterbody lift variations follow the potential curves even though the flow is closer to a Helmhotz type.

Effect of Mach Number on the AD 19 Configuration

Figures 11(a) and 11(b) present for the AD 19 strake-wing-body a comparison of the effect of increasing Mach number on the total and component lift and pitching-moment characteristics for the high-angle-of-attack vortex lift theory and data as taken from figures 6(d), 7(d), and 8(d). Only one configuration was chosen with which to perform this study since, for the limited Mach range, no large differences in compressibility effects were expected to exist for these models. A comparison of the theory with data (fig. 11(a)) indicates at low angle of attack that both have the same trends and C_m , though a different magnitude of change with increasing Mach for C_{T.} number. For $\alpha > 16^{\circ}$, the C_L estimates have an opposite trend with increasing Mach number than do data because the vortex lift contributions are decreasing faster than the potential lift terms increase. (See table V and the K_{p} and K_{v} usage in equation (la).) These two trends are delineated in the component characteristics shown in figure 11(b). There the falloff in strakeforebody $C_{T_{i}}$ is seen to be larger than the increase in wing-afterbody $C_{T_{i}}$ with Mach number over the upper range of α . The comparison does confirm that the wing upwash is decreasing its effect on the strake as postulated previously because the changes that take place in the wing interference are automatically accounted for by the theory using the Prandtl-Glauert rule for compressibility, i.e., the equivalent wing in incompressible flow being stretched longitudinally.

Effect of Mach Number on Basic Wing-Body Configuration

Figures 12(a) and 12(b) show the effect of Mach number on the longitudinal data for the basic wing-body configuration with the wing in the fore and aft positions, respectively. Because of early vortex breakdown on the wing-body, the data will not likely demonstrate vortex lift and, therefore, may be approximated by potential theory though the flow is not potential. Even this approximation is seen not to be especially good for $\alpha > 17^{\circ}$. These data certainly point up the need for a flow control device, such as a strake, which is able to organize the wing flow field from $\alpha \approx 8^{\circ}$ up to $\alpha \approx 30^{\circ}$. Figure 12 also shows that the compressibility effects are of the same magnitude for the wing in either position, as would be expected. These wing-body data and theoretical estimates are used in the subsequent section "Strake Efficiency."

Synergistic Effects

The favorable interference often produced by placement of two (or more) lifting surfaces in close proximity so that the aerodynamic results measured exceed the sum of the individual components tested separately is oft-times referred to as a synergistic effect. Plots of lift synergism are often used (see, for example, ref. 1) since they provide a convenient way of displaying one of the principal benefits of strake-wing aerodynamics. Figures 13(a) to 13(p) present the lift synergism for the configurations reported herein. Lift synergism is determined using the lift-coefficient results obtained from three sources. (These three sources are indicated, for example, by the three curves of fig. 13(a).) The first is the total lift coefficient of the wing and body (short-dash curve). The second is the lift coefficient for the wing-afterbody obtained in the presence of the forebody and then added to the strake-forebody lift coefficient measured in the presence of the afterbody (long-dash curve). The third is the total lift coefficient for the strake-wing-body configuration (solid curve). A comparison of the first and second sources yields the direct area effect of adding the strake, while comparing the second and third sources provides the effect of aerodynamic synergism. (See fig. 13(a).)

Since lift-synergism plots have proven to be valuable, figures 14(a) to 14(p) have been prepared in order to determine the useful information that may be discerned from pitching-moment synergism. (Their construction is similar to the lift synergism.) Both kinds of synergism plots were generated by data interpolation, and they are discussed in this section.

Lift

From figures 13(a) to 13(p) it is clear for all the strakes tested in combination with a wing-body that favorable interference was experienced for $\alpha > 13^{\circ}$. The extent of the maximum synergistic effect, defined as the difference between the upper two curves divided by the middle curve times 100 percent, varied between configurations from a high of 53 percent for the ED 5 strake to a low of 21 percent for the AD 22 strake. The average value for these maximum effects is around 42 percent; and for a fixed strake shape, AD 22 through AD 24, the effect increases with increasing R_a . The maximum synergism effect generally occurs quite close to the value of α associated with $C_{L,max}$ for the complete configuration. This value of α is less than that for $C_{L,max}$ of the components added together and, hence, points up another useful feature of the aerodynamic synergism, i.e., a larger $C_{L,max}$ and that occurring at a lower α .

After $C_{L,max}$ has been reached for the upper and middle curves of figures 13(a) to 13(p), the lift coefficient C_L tends to fall off more rapidly for the synergistic combination (upper curve) than when the component lift coefficients are added together (middle curve). This falloff trend for the middle curve is most likely associated with its wing-afterbody component in that this component never has available to it the benefit of the strake forward-shed vorticity. Hence, when the strake-vortex effect is curtailed at the higher angles of attack on the synergistic combination, the reduction in wing-afterbody lift coefficient is much more severe.

Pitching Moment

By studying the pitching-moment synergistic plots, the data from figures 14(a) to 14(p) show that, apart from the expected lift-coefficient range extension, there are two general conclusions regarding longitudinal stability which result. They are discussed in order of their occurrence with increasing synergistic C_L . First, from low to moderate C_L , the stability is unchanged or slightly reduced by synergism; second, from moderate C_L to $C_{L,max}$, synergism causes a delay in pitch-up onset. The preceding conclusions are a result of the interference effects keeping the total load centroid in about the same location during most of the C_L range and then permitting the load center to move forward as $C_{L,max}$ is approached. This forward movement is associated with the wing upwash on the strake vortex causing the strake to generate a larger fraction of the total lift at the higher angles of attack as the synergistic sum decreases. (See figs. 10 (a) and 13 (a) as examples.) The $C_{L,max}$ occurs when the strake vortex breaks down in the vicinity of the strake-wing juncture (ref. 11). (See appendix B for additional discussion.) Thereafter, depending on the strake shape, the vortex breakdown point moves forward on the strake at a rate which may keep C_L near $C_{L,max}$ and thereby accentuate the positive moment generation tendency of the configuration.

Strake Efficiency

One way to assess strake efficiency with regard to maneuver capability is to compare the increase in lift obtained with the strake in place with what would have been expected by enlarging the wing area by an equal amount. In equation form, this can be quantified by the parameter f

 $f \equiv \frac{(C_{L,tot})_{swb}}{(C_{L,tot})_{wb}} \left(\frac{S_{ref}}{S_{ref} + S_s} \right) = \frac{(C_{L,tot})_{swb}}{(C_{L,tot})_{wb}(1 + R_a)}$

Total
$$C_{L}$$
 including aerodynamic synergism

$$\equiv \frac{1}{Scaled C_{L}}$$
 with increased area (6)

which is given the name "additional lifting surface efficiency factor" in reference 7 where it was first presented. The condition of f > 1 will exist when the incremented increase in C_L associated with adding the area in the form of a strake exceeds the direct effect of that produced by increasing the basic wing area. The satisfaction of this condition means that, from a lift production standpoint, adding strake area is more efficient than just increasing wing area. Furthermore, with respect to weight, the low-aspect-ratio shape of the strake leads to a lighter weight structure (with lower gust response) than for the simply enlarged wing. Although this additional wing area would lead to an increase in span and therefore cruise lift-drag ratio, it cannot be done without an inherent weight penalty.

Figure 15 shows the manner in which f is presented and compares representative data (AD 19) with theory. The theory uses the high-angle-of-attack vortex lift theory for the strake-wing configuration (fig. 9(d)) and potential theory for the wing-body (fig. 12(a)) since each best approximates its respective data. Figure 15 shows that above $\alpha \approx 14^{\circ}$ the theoretical and experimental values of f exceed unity because of the synergistic vortex lift being generated on the configuration. This figure also shows that for $17^{\circ} \leq \alpha < 40^{\circ}$ the experimental results produce values of f greater than predicted by the theory. This increase is due to the loss of lift effectiveness on the wing associated with its own leading-edge vortex breakdown and large-scale stall. If the usual leading-edge flow control devices were applied to the wing, the difference between the two f curves would be expected to diminish

considerably. This experimental increase in f can be traced to figure 12(a) where, in particular for M = 0.2, $(C_{L,tot})_{wb}$ departs from the potential theory at $\alpha \approx 17^{\circ}$. As a further note, it can be seen by comparing figure 15 with figure 9(d) that the maximum or peak value of f occurs at the same angle of attack as the maximum $(C_{L,tot})_{swb}$, as would be anticipated. The second peak in f versus α , which occurs at $\alpha \approx 44^{\circ}$, results from the sudden post-stall loss of measurable lift on the wing-body, $(C_{L,tot})_{wb}$, at M = 0.2. (See figs. 12(a) and 12(b).)

Mach number effects on f for each strake-wing combination are discussed next, followed by a comparison of f for various combinations at M = 0.2 which highlight the various geometrical effects over the range of α tested. For the complete configuration, $C_{\rm L, Max}$ is discussed more fully at the end of this section.

Effect of Mach Number

Though the range of α is not as extensive for M = 0.5 and M = 0.7 as at M = 0.2 in figures 16(a) to 16(p), there is enough range to establish two general consequences of increasing Mach number on the plots of f versus α : (1) f increases near the largest test value of α and (2) f decreases near $\alpha = 6^{\circ}$. Thus, at the higher angles of attack, the effect of compressibility is to produce larger lifts on the strake-wing-body, and, conversely, at lower angles of attack the effect is larger on the wing-body.

An explanation may be that at lower angles of attack with the wing-body being more Mach number dependent than the more slender strake-wing-body, and with vortex flow not yet dominating the aerodynamic characteristics, the denominator of f, given in equation (6),

 $(C_{L,tot})_{wb}(1 + R_a)$

increasingly exceeds its numerator

(C_{L,tot})_{swb}

thereby producing these smaller values with increasing Mach number. However, at the higher angles of attack the vortex flows dominate, with their effects being larger on the strake-wing-body (the more slender configuration) than on the wing-body. The $(C_{L,tot})_{swb}$ data indicate that near $\alpha \approx 16^{\circ}$ the effect of Mach number is small, due in part to the configuration slenderness but also due to the unchanging type of flow field since, for the latter, the vortex systems do not generally break down over the wing until a larger angle of attack is reached. Although true of the strake-wing-body, this is not true for the wing-body in that $(C_{L,tot})_{wb}$ falls off with increasing Mach number at $\alpha \approx 16^{\circ}$ because the leading-edge vortex has already undergone breakdown at a lower value of α . The post breakdown $(C_{L,tot})_{wb}$ characteristics indicate a reversing

influence of increasing M and α to the extent that at $\alpha \approx 16^{\circ}$ an inverse Mach number effect is seen. (See figs. 12(a) and 12(b).)

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Effect of Strake Geometry

This section examines the effect of strake geometry on f versus α by concentrating on the various geometrical features that can be totally or partially isolated. Among them are (1) area effect for a fixed leading-edge shape, (2) area and slenderness combination associated with simple chordwise scaling, (3) fixed area but with differing shapes, (4) shape effect for a fixed semispan, and (5) others which include the empirically designed series and the indirect effect of pressure specification, i.e., special strake shapes. For additional insight into these effects, corresponding strake-vortex breakdown angle data from the Northrop water tunnel is also discussed.

Area effect.- Figure 17 shows the effect of area scaling for a fixed strake shape, and therefore slenderness $R_s = 7.00$, by using the AD 22, AD 23, and AD 24 strake series. Three effects of increasing area are noted from this figure: (1) increasing f_{max} with R_a , (2) increasing α required to reach f = 1 with increasing R_a , and (3) the α at which the first f "hump" occurs increases with R_a . The first effect is simply associated with the larger strake developing the higher values of $(C_{L,tot})_{swb}$. The second effect is associated with the increasing downwash being imposed on the wing by the strakes of larger area, hence semispan, thereby requiring the configuration to reach a higher value of α before f becomes larger than unity. The third effect is due to the larger values of $(C_{L,tot})_{swb}$ occurring at larger values of α , with both being proportional to the R_a increase. Additional pertinent information has already been given in the section on lift synergism and the general discussion of strake efficiency. Both pertain to the third effect, hence it will not be discussed further for any of the other geometrical variations.

The α_{BD-TE} results from the water tunnel (ref. 6) follow the same trend with R_a as does $f_{max}.$

<u>Chordwise scaling</u>.- Figure 18 shows the AD 24, ED 12, and ED 13 configurations, all with the same value of $R_b = 0.297$ but each having a different fraction of the AD 24 chord variation. There are two major geometrical variations here: increasing area and slenderness ratio. Together they yield (1) increasing f_{max} and (2) increasing α required to reach f = 1. The impact of these geometrical features has been noted previously, particularly for the first item. The second item is caused by the larger area producing an additionally imposed downwash on the wing.

These α_{BD-TE} results also follow the same trend with R_a as does f_{max} (ref. 6).

<u>Fixed area.</u> Figures 19(a) to 19(d) show the variation of f with α for a set of strakes having values of $R_a \approx 0.119$, $R_a \approx 0.169$, $R_a \approx 0.185$, and $R_a \approx 0.263$, respectively. For the empirically designed strakes, the effect of slenderness is slight on the first f "hump" at $R_a \approx 0.119$, but not so at

 $R_a \approx 0.263$. The ED 9 strake (fig. 19(d)) is seen to have a larger value of f_{max} . This is apparently associated with the more stable vortex system arising from the more slender strake and its smoother leading-edge shape variation (ref. 5).

The analytically designed strakes in figure 19(b), $R_a \approx 0.169$, have the same value of R_s and R_b and differ only slightly in their shape. The one with a slightly higher value of R_a (less than 4 percent larger), lower initial sweep, and higher α_{BD-TE} (from ref. 6) has a higher value of f_{max} .

Figure 19(c) shows two analytically designed strakes and one empirically designed strake for $R_a \approx 0.185$. These results also show that, although there is less than 3 percent difference in R_a between the three strakes, the ED 5 (which has the larger value of R_a) has the largest value of f_{max} . The ED 5 has the largest value of R_b and produces f = 1 at the smallest value of α . This is different from what was noted for the area effect, which means that not only is area important but also its distribution – associated with the leading-edge shape – in producing relatively large values of $(C_{L,tot})_{swb}$ at lower angles of attack.

Fixed semispan.- Figure 20 shows results for four analytically designed strakes with R_b fixed at 0.212. The AD 14, AD 17, and AD 19 have values of f_{max} which, though approximately the same, vary in order of increasing R_a . (Note that these three strakes have more than 18 percent differences in R_a .) Reference 6 also shows the values of α_{BD-TE} to have that same order; and although all are of approximately the same value, there is a difference in maximum magnitude of about 2°. The AD 23 strake has a somewhat smaller value of f_{max} than do the other three, although its value of R_a is not that different from the value for the AD 14. They all have about the same value of α at which f = 1.

In figure 21 the AD 14, AD 17, and AD 19 configurations have curves of f versus α compared with those of the AD 24. The comparison shows f_{max} of all four to be similar, though the value of f_{max} for the AD 24 is slightly higher. What is particularly interesting is that the AD 14, AD 17, and AD 19 strakes have areas which range from 53 to 63 percent of the AD 24 strake and still produce these high values of f_{max} . This means that these smaller area strakes have efficiencies equivalent to the larger AD 24, up to fmax and may, therefore, be classified as "better" strakes. Two other features of figure 21, apart from the increased angle of attack required to reach f = 1 for the AD 24 (larger R_b), are that (1) f_{max} occurs at a slightly higher angle of attack for the AD 24 and that (2) the curve of f versus α beyond f_{max} is significantly higher for the AD 24 than for the other configurations. Both features are associated with the value of R_a for the AD 24 strake being larger; the first feature is attributed to the larger lift deficiency, in terms of f, which must be initially overcome, and the second feature results from the (CL, tot) swb retaining a higher value beyond f_{max} , which is associated with the larger area that the flow from the strake vortex can act upon.

<u>Other parameters</u>.- Figures 22(a) to 22(c) show the variations of f and α for the apex, trailing-edge, and inboard-edge cut series, respectively. Taking the cut series as a group, the ED 5 strake and ED 9 strake are as effective up to f_{max} as the AD 24 strake, while having areas of 58 percent and 80 percent less, respectively. Therefore, it can be seen that selected empirical alterations of an analytically designed strake are possible which have only a small impact on the value of f_{max} . The preferred methods of empiricalstrake-shape altering appear to be those of removing small amounts of area along the inboard or trailing edges. Reference 5 also shows these methods leading to improvements in strake-vortex stability, i.e., larger values of $\alpha_{\rm BD-TE}$.

Figure 23 has been prepared to examine indirectly the effect of pressure specification on f versus α . The comparison is indirect because the different pressure specifications, constant and polynomial, taken in conjunction with the same suction prescription yield two different strake shapes. Figure 23 shows the value of f_{max} to be larger for the gothic strake (AD 19) - designed using the constant type - than for the reflexive strake (AD 9). The AD 19 strake does however have larger values of R_a and R_b than the AD 9, due in part to the AD 9 strake being very long (i.e., more slender) for the same value of R_b . Hence, on the surface one could conclude that the effect of Ra was the major cause for the difference. However, it can be seen from figure 21 that there are analytically designed strakes, of the same or smaller area and larger values of R_b than for the AD 9, which have values of f_{max} comparable to those of the AD 19. The strakes in figure 21 are all gothic and were generated with the constant pressure specification. Thus the area distribution/leading-edge shape are important. Also, since reference 5 determined that the polynomial pressure specification leads to strakes which tend to reflex toward the tip and have, as a group, lower values of α_{BD-TE} , it can be concluded that the constant pressure specification yields preferable strake shapes and characteristics of f versus α .

Generation of CL.max

The maximum lift coefficients that the configurations generate are examined with the aid of figure 24. It is seen that for all analytically designed strakes using the constant pressure specification and for all those designed empirically and employed herein, the variations of $C_{L,max}$ with R_a follow the same curve. Though this curve has a markedly different gradient on either side of $R_a \approx 0.20$, the values of the curve are all well above those for the reference curve $(C_{L,max})_{wb}(1 + R_a)$. This is another way of seeing that addition of area in the form of a strake - some ranges of strake R_a are better than others - is a more efficient producer of $C_{L,max}$ than just enlarging the wing while keeping the reference area constant. The reason for the rapid reduction in $C_{L,max}$ with R_a for the gothic strakes having $R_a > 0.2$ is unclear. Further efforts in strake design may enable $C_{L,max}$ to be increased in such a way as to lie along the extrapolated curve.

Similar data for three empirically designed ogee (reflexive) strakes tested on the same wing-body were obtained from reference 12 and have been plotted in figure 24. A faired curve of these data passes very close to the data point for the analytically designed reflexive strake (AD 9) and has a different variation than the other data curve for R_a greater than approximately 0.20. In particular, for values of R_a below 0.25 the gothic or more gothic-like strakes generate a larger value of $C_{L,max}$ than do the empirically designed ogee strakes from reference 12 or the analytically designed reflexive strake reported herein.

Better Strakes

A criterion is sought by which the strakes may be more rigorously delineated into categories so that the "better" ones may be exposed. From the study of f versus α (figs. 17 to 23) and $C_{L,max}$ versus R_a (fig. 24) better performing strakes have been discussed; however, a concise statement as to what qualifies a strake to be a better one has not yet been established. This will now be attempted.

Since f is a function of R_a , $(C_{L,tot})_{swb}$, and $(C_{L,tot})_{wb}$ and since $(C_{L,tot})_{swb}$ is also a function of R_a , α , and M, it is clear that R_a is a prime variable. Therefore, one should seek, at an appropriate angle of attack, not only the maximum value of $(C_{L,tot})_{swb}$ and f but a way to maximize the variation of the aerodynamic synergistic effect with area change R_a , i.e., $(\partial f/\partial R_a)_{max}$. This can be formulated as

$$\frac{\partial f}{\partial R_{a}} = \frac{1}{1 + R_{a}} \left[\frac{1}{(C_{L, tot})_{wb}} \frac{\partial (C_{L, tot})_{swb}}{\partial R_{a}} - f \right]$$
(7)

where

$$f = \frac{(C_{L, tot})_{swb}}{(C_{L, tot})_{wb}(1 + R_a)}$$

One could solve directly for the value of R_a at which $\partial f/\partial R_a$ is maximized by examining $\partial^2 f/\partial R_a^2 = 0$. However, the determination of $\partial f/\partial R_a$ at a fixed α is difficult enough to accomplish from the data; hence the second partial derivative is even more subject to question. Thus, those strakes that <u>maximize</u> $\partial f/\partial R_a$ belong to a family which should produce better strakes; hence, this maximization may be used as one possible criterion.

Table VII presents the $\partial f/\partial R_a$ results for the gothic-like strakes at the value of α required for $(C_{L,max})_{swb}$. (Note that strakes having essentially the same value of α are used in the determination of $\partial (C_{L,tot})_{swb}/\partial R_a$ from figure 24 for use in eq. (7).) From the table it can be seen that those strakes which generally show up as the better ones all have values of $\partial f/\partial R_a > 3.0$, and furthermore these values are the largest obtained. By maximizing $\partial f/\partial R_a$ it is clear that the intention is to determine those strakes for which a given change in R_a produces the most benefit in f for a fixed value of α . This does not say whether $C_{L,max}$ or f_{max} is among the highest or not, only that for a value of α increasing R_a , for those strake shapes which have high values of $\partial f/\partial R_a$, should produce a rapid increase in f.

The preceding, therefore, provides another criterion for better strake shape determination, the criterion being that strakes from any source which have a value of $\partial f/\partial R_a > 3.0$ should be considered good shape candidates.

As a point of interest, if a strake could be designed so as to yield $(C_{L,max})_{swb} = 2.0$ at $R_a = 0.245$ (the end point of the extrapolated lower part of the curve as given by

$$\frac{\partial (C_{L,tot})_{swb}}{\partial R_{a}} \approx 5.0$$

for gothic-like configurations in fig. 24), it would produce $f(\text{at } C_{L,max}) \approx 2.0$ with $\partial f/\partial R_a \approx 3.0$ at $\alpha \approx 28^{\circ}$. Hence, this configuration would have all the good features previously identified, i.e., large values of $C_{L,max}$, f_{max} (also, f at $C_{L,max}$), and $\partial f/\partial R_a$, and therefore be theoretically able to generate even larger values of f and $C_{L,max}$ if its shape were scaled up. (It should be noted that even without area scaling this value of f at $C_{L,max}$ is larger than any obtained to date.)

CONCLUSIONS

An experimental and analytical study has been presented for 16 analytically and empirically designed strake-wing-body configurations at Mach numbers of 0.2, 0.5, and 0.7. From the basic data, both total and component, synergism studies, comparisons with theoretical estimates, and the strake lift effectiveness study, the following conclusions have been made:

1. Pitch-up appears fundamental for many of the configurations and would therefore require a low tail for stability and control.

2. High-angle-of-attack vortex lift theory reasonably estimates the lift and the lift dependent drag up to strake-vortex breakdown.

3. High-angle-of-attack and low-angle-of-attack vortex lift theories bracket both the total and component pitching-moment data up to maximum lift or strake-vortex breakdown.

4. Overall compressibility effects are slight on the total components, due primarily to a falloff in lift and upwash on the strake-forebody compensated by an increase in lift on the wing-afterbody associated with the increasing sub-critical Mach number.

5. Synergistic lift effect is usually accompanied by a delay in pitch-up.

6. It is possible to generate essentially the same level of f, the additional lifting surface efficiency factor, with gothic strakes having areas from about one-half to two-thirds the size of the original gothic analytically designed strake (AD 24).

7. Based on the strakes studied herein, those having $\partial f/\partial (\text{Strake area/Reference wing area}) > 3.0$ belong to a family of strakes that are better performers.

Langley Research Center National Aeronautics and Space Administration Hampton, VA 23665 February 24, 1981

APPENDIX A

AUGMENTED VORTEX LIFT

The concept of an augmented vortex lift term arises from the wellestablished fact that for many delta wings the leading-edge vortex generated on the wing persists for a considerable distance downstream and, therefore, can act on other surfaces such as the aft part of more generalized planforms or aircraft horizontal tails. Upon examining experimental results for the more generalized planforms, one concludes that the augmentation effect just introduced is not accounted for by the suction analogy although for simple deltas it is. The primary problem appears to be the interaction, or lack of it, when both leading-edge and side-edge vortex flows are involved. This situation as well as when the trailing edge of a simple delta is notched positively or negatively appear not to be modeled by the suction analogy. Sketch D shows examples of two systems employed that account for vortex lift





Sketch D.- Concept of augmented vortex lift.

on delta and cropped-delta wings; the first system is a theoretical one developed from a planar potential theory and utilizing the suction analogy along the leading edge and side edge, and the second system is an extension that accounts for the action of the leading-edge shed vortex in the vicinity of the side edge of cropped-delta wings. The following important points are made from sketch D: (1) The leading-edge suction distribution has a peak value somewhere along the leading edge away from the extremities and goes to zero at the tip because no-edge forces are present beyond the point of maximum

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span, and (2) for the cropped-delta wing, the aft part of the wing can generate additional (augmented) vortex lift (above that associated with the direct side-edge effect) because of the presence of the leading-edge vortex (as discussed in ref. 8).

In order to estimate the augmented vortex lift, it is first necessary to quantify the circulation of the shed vortex along the wing leading edge. This can be done as indicated by the lower sketch in sketch D. The Kutta-Joukowski law has been employed to relate the differential suction force along the leading edge to an unknown circulation $\Gamma(l)$ by $dF_S = -\rho w_{net}(l)\Gamma(l) dl$. Using a coordinate transformation, it can also be related to the leading-edge suction distribution along the span as

$$\frac{c_{s}c}{\alpha^{2}} = -2 \sec \Lambda \frac{\Gamma(l)w_{net,le}}{\alpha^{2}u^{2}}$$

Sketch E shows an idealized distribution of the product $\frac{-\Gamma(l)w_{net,le}}{\alpha^2 u^2}$; note

that it is basically linear, along with a fairly reasonable $\frac{-w_{net,le}}{w_{net,le}}$ (upwash)



Sketch E.- Variables used in augmented-vortex-lift determination for cropped delta wings, delta part idealized. (Note: b = Wing span, $c_t = Tip$ chord, $\Delta x = Distance along side edge, and <math>y = Distance along semispan.$)

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distribution for a cropped-delta wing, also basically linear. As a consequence, $\frac{\Gamma(l)}{\alpha^2 U}$ can be estimated as shown. Because the actual circulation does not go to zero (hence the vortex persists downstream), the distribution of circulation, essentially constant, cannot be used. Instead, an average value is employed. With an average value used for $\frac{\Gamma(l)}{\alpha^2 U}$, it is consistent to utilize an average value for $\frac{-W_{\text{net},le}}{U}$ as well. This result can be expressed in terms of the leading-edge vortex lift factor by

$$\int_{0}^{b/2} \frac{c_{s}c \, dy}{\alpha^{2}} = \frac{K_{v,le}}{2} S_{ref} = -2 \sec \Lambda \frac{\Gamma(l)\overline{w}_{net,le}}{\alpha^{2} u^{2}} \frac{b}{2}$$

Hence,

$$\frac{\overline{\Gamma}(l)}{\alpha^{2}U} = \frac{-K_{v,le}S_{ref}}{2b \sec \Lambda} \frac{\overline{w_{net,le}}}{U}$$

Employing this result in the Kutta-Joukowski law, this time along the side edge, permits the estimation of the augmented vortex lift. The details yield

Augmented vortex lift along one edge =
$$-\rho \bar{w}_{net,se} = \frac{\Gamma(l)}{\alpha^2} \tilde{c}$$

where the distribution $\frac{-w_{net,se}}{U}$ and its average are again reasonably depicted at the bottom right of sketch E, and \tilde{c} is a characteristic streamwise length. By inspection of sketch E,

Then, defining the augmented vortex lift along one edge divided by α^2 as $\frac{K_{v,se}}{2} q_{\infty} S_{ref}$ leads to

$$\frac{K_{v,se}}{2} q_{\infty} S_{ref} = q_{\infty} \frac{K_{v,le}}{b sec \Lambda} S_{ref} \tilde{c}$$

or

$$K_{v,se} = \left[\frac{K_{v,le}}{(b/2) \text{ sec } \Lambda}\right]\tilde{c}$$

The term in brackets results from the use of average values and amounts to assuming that the leading-edge vortex lift factor is developed at a constant rate along the leading-edge length (b/2) sec Λ . For cropped-delta wings the value of \tilde{c} is taken to be the length of the tip chord.

From the preceding discussion, the contributions of the augmented term to vortex-flow aerodynamics are determined to be

$$C_{L,vse} = K_{v,se} |\sin \alpha| \sin \alpha \cos \alpha$$

 $C_{D,vse} = K_{v,se} \sin^3 \alpha$

and

$$C_{m,vse} = K_{v,se} | \sin \alpha | \sin \alpha \frac{\bar{x}_{se}}{c_{ref}}$$

where $\overline{x_{se}}$ is taken from the reference point to the centroid of the augmented vortex lift. This location is generally taken to occur at the centroid of the affected area.

APPENDIX B

STRAKE-VORTEX BREAKDOWN IN AIR AND WATER

From previous sections in this paper, a qualitative correlation has been pointed out to exist between the f_{max} variation, determined from wind-tunnel data, and the angle for strake-vortex breakdown at the trailing edge, observed in the water tunnel (ref. 5). Based on that correlation, it is interesting to consider how well the quantitative values of α_{BD-TE} in air would agree with those observed in water. For delta wings the agreement was determined in reference 3 to be good; however, not as much is known about the agreement for configurations like that of the strake-wing-body. During the wind-tunnel test reported in this paper, the atmospheric water vapor and tunnel temperature were such as to cause the strake vortex, and sometimes the wing vortex, to be visible for the AD 24 configuration. Because of the vortex visibility a video tape was made for the range of α from 16° to >35° at M = 0.3. From the tape, still photographs have been prepared and are presented in figure 25. Since the AD 24 was also a configuration tested in the water tunnel, photographs from that test (ref. 5) are available over a similar range of α and are also presented in figure 25 for comparison. (The angles of attack for the water-tunnel data are corrected for wall effects using the wind-tunnel lift-coefficient data.)

From these two sets of flow-field data it can be seen that there are at least three items which deserve comment. The first is that the strake vortex is better able to persist in the wing pressure field while in air than in water. This is most likely associated with the Reynolds number $(1.76 \times 10^4 \text{ in water})$ and 1.51×10^6 in air) and its effect on the upper-surface pressure field associated with the different characteristics of the boundary layers. The second item is the very rapid progression in air with small increase in α over the wing for the strake-vortex breakdown position once the trailing edge has been reached.

The different rates of vortex breakdown progression for configurations tested in the water and wind tunnel can also be seen for the delta wings of Wentz (ref. 13) tested in air and the water-tunnel results published by Headley (ref. 3). They are compared in figure 26 and even though the values of $\alpha_{\rm BD-TE}$ agree, the higher swept deltas are seen to exhibit a much more rapid forward progression of vortex breakdown position in air than in water. The third item is that α for strake-vortex breakdown at the strake-wing junction is about 32° in both air and water. This signifies that once the wing pressure field is traversed, the strake-vortex breakdown progression commences from the same position at about the same α .

Based on the second item, one should expect some differences in the force data in the α range from approximately 22° to approximately 32°. Wind-tunnel data at the same Mach number (0.3) as that for the strake-vortex photographs are available and are presented in figure 27. Force data for the water-tunnel model is not available for comparison; however, it is interesting to examine the wind-tunnel data for C_L versus α in light of both sets of strake-vortex photographs. From these data it can be seen that $C_{L,max}$ occurs in the α range from 30° to 35°. It is in this range that the strake vortex begins to

APPENDIX B

break down in air ahead of the wing trailing edge. This breakdown occurs at α values some 10^o to 13^o larger in air than in water, and so one might speculate that water-tunnel force tests would show $C_{L,max}$ occurring at a lower value of α .

Figure 9(g) presented the $C_{\rm L}$ versus α data for the AD 24 strakewing-body configuration at M = 0.2 in comparison with theory and, thereby, demonstrates that the falloff in lift-curve slope is a part of an <u>expected</u> <u>theoretical trend</u> for $\alpha > 20^{\circ}$. This fact, coupled with the wind-tunnel strakevortex-breakdown photographs for the model, should encourage the reader to employ caution in inferring from water-tunnel photographs quantitative information about the force data, as suggested in reference 11 for fighter-type configurations.

The use of water-tunnel photographs has been shown in reference 5 to be useful in sorting out the quantitative effects of different configurations. This appendix points out that further study is needed in order to more fully appreciate and account for the impact of Reynolds number on strake-vortex breakdown.

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TABLE I.- PERTINENT GEOMETRIC PROPERTIES OF ANALYTICALLY

DESIGNED STRAKES

[From ref. 5]

Strake designation	$\Lambda(n = 0),$ deg	Rs	Rb	Ra	Wing position
AD]	76.76	4.92	0.212	0.100	Forward
AD 2	83.55	6.51	.212	.100	
AD 3	77.14	5.33	.212	.110	
AD 4	83.75	7.04	.212	.112	
AD 5	72.06	3.94	.212	.079	
AD 6	71.29	3.55	.212	.070	
AD 7	69.01	4.99	.212	.126	
AD 8	80.70	5.76	.212	.108	
AD 9a	75.10	10.65	.197	.183	Aft
AD 10	79.41	5.91	.212	.112	Forward
AD 11	73.29	3.56	.212	.066	
AD 12	73.43	3.01	.212	.038	
AD 13	77.19	8.69	.212	.199	
AD 14 ^a	46.18	6.99	.212	.172	
AD 15	63.65	5.92	.212	.140	
AD 16	65.52	5.29	.212	.123	
AD 17 ^a	70.78	7.77	.212	.185	
AD 18	74.54	4.98	.212	.103	
AD 19 ^a	56.80	8.50	.212	.205	
AD 20	66.14	5.07	.212	.127	
AD 21	69.97	4.65	.212	.092	
AD 22 ^a	60.65	7.00	.144	.077	
AD 23 ^a	60.65	7.00	.212	.166	↓
AD 24 ^a	60.65	7.00	.297	.325	Aft

^aStrakes reported on in this paper.

TABLE II.- PERTINENT GEOMETRIC PROPERTIES OF EMPIRICALLY

DESIGNED STRAKES

[From ref. 5]

Strake designation	$ \Lambda(\eta = 0), \\ deg $	R _S	Rb	Ra	Chord modification	Wing position
AD 24 ^a	60.65	7.00	0.297	0.325	(b)	Aft
ED 1 ED 2 ^a ED 3 ED 4 ^a	60.00 60.00 60.00 60.00	6.10 5.19 3.98 2.77	0.297 .297 .297 .297	0.305 .266 .195 .114	Removal of apex region	Forward
ED 5 ^a ED 6 ^a ED 7 ED 8	60.65 60.65 60.65 60.65	5.83 5.22 4.53 3.65	0.262 .226 .181 .119	0.188 .124 .065 .021	Removal of trailing-edge region	
ED 9 ^a ED 10 ^a ED 11 ^a	73.32 77.57 80.12	7.79 8.62 9.59	0.253 .208 .163	0.259 .192 .131	Removal of inboard- edge region	Aft Forward
ED 12 ^a ED 13 ^a	56.89 50.42	5.18 2.78	0.297	0.227	Chordwise scaling	
ED 14 ED 15	50.42 50.42	2.78 2.78	0.297 .297	0.078 .076	Chordwise extension (snag) on ED 13 strake	
ED 16 ED 17 ED 18	50.42 50.42 50.42	5.63 4.64 3.63	0.297 .297 .297	0.325 .246 .166	Addition of side- edge/trailing- edge area to ED 13 strake	

5-1-1-T

No.

^aStrakes reported on in this paper. ^bAnalytically designed strake from which empirical variations are made.

AD 9					
x			У		
cm	in.	cm	in.		
0.000 0.919 2.169 3.665 5.367 7.242 9.268 13.724 18.626 23.891 29.385 34.557 39.119 42.606	0.000 0.362 0.854 1.443 2.113 2.851 3.649 5.403 7.333 9.406 11.569 13.605 15.401 16.774	0.000 0.201 0.401 0.599 0.800 1.001 1.201 1.600 2.002 2.400 2.802 3.200 3.602 4.001	0.000 0.079 0.158 0.236 0.315 0.394 0.473 0.630 0.788 0.945 1.103 1.260 1.418 1.575		

AD 14					
2	¢		У		
cm	in.	cm	in.		
0.000 0.325 0.818 1.433 2.154 2.974 3.886 5.982 8.440 11.298 14.623 18.590 23.589 31.991	0.000 0.128 0.322 0.564 0.848 1.171 1.530 2.355 3.323 4.448 5.757 7.319 9.287 12.595	0.000 0.229 0.457 0.686 0.914 1.143 1.374 1.831 2.289 2.746 3.203 3.660 4.120 4.577	0.000 0.090 0.180 0.270 0.360 0.450 0.541 0.721 0.901 1.081 1.261 1.441 1.622 1.802		

TABLE III STRAK	PLANFORM	PERIMETER	POINTS
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. . . .

AD 17					
x	5		У		
cm	in.	cm	in.		
0.000 0.693 1.473 2.334 3.274 4.290 5.385 7.813 10.577 13.721 17.328 21.560 26.817 35.550	0.000 0.273 0.580 0.919 1.289 1.689 2.120 3.076 4.164 5.402 6.822 8.488 10.558 13.996	0.000 0.229 0.457 0.686 0.914 1.143 1.374 1.831 2.289 2.746 3.203 3.660 4.120 4.577	0.000 0.090 0.180 0.270 0.360 0.450 0.541 0.721 0.901 1.081 1.261 1.441 1.622 1.802		

AD 19					
2	ς		У		
em	in.	cm	in.		
0.000 0.455 1.115 1.935 2.893 3.980 5.189 7.968 11.247 15.085 19.558 24.491 30.170 38.892	0.000 0.179 0.439 0.762 1.139 1.567 2.043 3.137 4.428 5.939 7.700 9.642 1.878 15.312	0.000 0.229 0.457 0.686 0.914 1.143 1.374 1.831 2.289 2.746 3.203 3.660 4.120 4.577	0.000 0.090 0.180 0.270 0.360 0.450 0.541 0.721 0.901 1.081 1.261 1.441 1.622 1.802		
AD 22					
--	--	--	---		
x	<u>.</u>		у		
cm	in.	cm	in.		
0.000 0.318 0.721 1.201 1.748 2.357 3.028 4.552 6.327 8.387 10.777 13.477 16.693 21.836	0.000 0.125 0.284 0.473 0.688 0.928 1.192 1.792 2.491 3.302 4.243 5.306 6.572 8.597	0.000 0.155 0.312 0.467 0.622 0.780 0.935 1.247 1.557 1.869 2.182 2.492 2.804 3.117	0.000 0.061 0.123 0.184 0.245 0.307 0.368 0.491 0.613 0.736 0.859 0.981 1.104		

AD 23				
х			У	
cm	in.	cm	in.	
0.000 0.465 1.062 1.763 2.565 3.459 4.445 6.683 9.291 12.319 15.827 19.792 24.514 32.070	0.000 0.183 0.418 0.694 1.010 1.362 1.750 2.631 3.658 4.850 6.231 7.792 9.651 12.626	0.000 0.229 0.457 0.686 0.914 1.143 1.374 1.831 2.289 2.746 3.203 3.660 4.120 4.577	0.000 0.090 0.180 0.270 0.360 0.450 0.541 0.721 0.901 1.081 1.261 1.261 1.441 1.622 1.802	

AD 24			
x		У	
em	in.	cm	in.
0.000 0.653 1.486 2.471 3.597 4.849 6.231 9.365 13.023 17.262 22.179 27.739 34.356 44.943	0.000 0.257 0.585 0.973 1.416 1.909 2.453 3.687 5.127 6.796 8.732 10.921 13.526 17.694	0.000 0.320 0.643 0.963 1.283 1.603 1.925 2.565 3.208 3.848 4.491 5.131 5.773 6.414	0.000 0.126 0.253 0.379 0.505 0.631 0.758 1.010 1.263 1.515 1.768 2.020 2.273 2.525

A REAL PROPERTY.

ED 2				
х у				
cm	in.	em	in.	
0.000 6.985 7.041 8.270 16.114 22.730 25.977 33.320	0.000 2.750 2.772 3.256 6.344 8.949 10.227 13.118	0.000 4.034 4.041 4.491 5.131 5.773 6.030 6.414	0.000 1.588 1.591 1.768 2.020 2.273 2.374 2.525	

TABLE	III	Continued
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ED 4 x			
х у			у.
cm	in.	cm	in.
0.000 10.437 10.478 17.821	0.000 4.109 4.125 7.016	0.000 6.025 6.030 6.414	0.000 2.372 2.374 2.525

.

ED 5 X			
x			У
cm	in.	cm	in.
0.000 0.653 1.486 2.471 3.597 4.849 6.231 9.365 13.023 17.262 22.179 25.425 28.953 33.142	0.000 0.257 0.585 0.973 1.416 1.909 2.453 3.687 5.127 6.796 8.732 10.010 11.399 13.048	$\begin{array}{c} 0.000\\ 0.320\\ 0.643\\ 0.963\\ 1.283\\ 1.603\\ 1.925\\ 2.565\\ 3.208\\ 3.848\\ 4.491\\ 4.874\\ 5.260\\ 5.667\end{array}$	0.000 0.126 0.253 0.379 0.505 0.631 0.758 1.010 1.263 1.515 1.768 1.919 2.071 2.231

ED 6 X			
x		У	
cm	in.	cm in.	
0.000 0.653 1.486 2.471 3.597 4.849 6.231 9.365 13.023 17.262 22.179 25.425	0.000 0.257 0.585 0.973 1.416 1.909 2.453 3.687 5.127 6.796 8.732 10.010	0.000 0.320 0.643 0.963 1.287 1.603 1.925 2.565 3.208 3.848 4.491 4.874	0.000 0.126 0.253 0.379 0.505 0.631 0.758 1.010 1.263 1.515 1.768 1.919

TABLE III Continued

y ED 9				
x			У	
em	in.	cm in.		
0.000 1.124 2.378 3.758 6.894 10.551 14.791 19.709 25.267 31.884 42.472	0.000 0.442 0.936 1.479 2.714 4.154 5.823 7.759 9.948 12.553 16.721	0.000 0.321 0.641 0.962 1.603 2.245 2.886 3.527 4.169 4.810 5.451	0.000 0.126 0.253 0.379 0.631 0.884 1.136 1.389 1.641 1.894 2.146	

ED 10			
x			У
em	in.	cm	in.
0.000 1.505 3.136 6.793 11.033 15.951 21.509 28.126 38.714	0.000 0.592 1.235 2.674 4.344 6.280 8.468 11.073 15.242	0.000 0.321 0.641 1.283 1.924 2.565 3.207 3.848 4.489	0.000 0.126 0.253 0.505 0.758 1.010 1.263 1.515 1.768

ED 11						
x			У.			
cm	in.	cm	in.			
0.000 1.896 6.137 11.054 16.613 23.230 33.817	0.000 0.747 2.416 4.352 6.540 9.146 13.314	0.000 0.321 0.962 1.603 2.245 2.886 3.527	0.000 0.126 0.379 0.631 0.884 1.136 1.389			

TABLE III (Conclude	d
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ED 12					
x			У		
cm	in.	cm	in.		
0.000 0.549 1.224 2.007 2.885 3.856 4.912 7.290 10.033 13.183 16.805 20.876 25.687 33.271	0.000 0.216 0.482 0.790 1.136 1.518 1.934 2.870 3.950 5.190 6.616 8.219 10.113 13.099	0.000 0.320 0.643 1.283 1.283 1.603 1.925 2.565 3.208 3.848 4.491 5.131 5.773 6.414	0.000 0.126 0.253 0.379 0.505 0.631 0.758 1.010 1.263 1.515 1.768 2.020 2.273 2.525		

ED 13					
x			У		
cm	in.	cm	in.		
0.000 0.411 0.879 1.392 1.946 2.540 3.170 4.544 6.076 7.780 9.690 11.791 14.209 17.818	0.000 0.162 0.346 0.548 0.766 1.000 1.248 1.789 2.392 3.063 3.815 4.642 5.594 7.015	0.000 0.320 0.643 1.283 1.283 1.603 1.925 2.565 3.208 3.848 4.491 5.131 5.773 6.414	0.000 0.126 0.253 0.379 0.505 0.631 0.758 1.010 1.263 1.515 1.768 2.020 2.273 2.525		

TABLE IV.- THEORETICAL LOADING FACTORS AND THEIR CENTROIDS FOR HIGH~

ANGLE-OF-ATTACK AND LOW-ANGLE-OF-ATTACK SOLUTIONS AT M = 0.2

CONFIGURATION NO. AD 9

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
STI	RAKE			
	КР=	•41229	27.58463	10.86009
ΚV	Lē=	1.57299	18.77365	7.39120
WI	NG			
	K₽ ≠	2.57992	-10.68390	-4.20626
ΚV	LÉ=	2.20256	-8.61060	-3.39000
Kγ	SE=	•48510	-21.12574	-9.31722

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER DF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE					
WING	ΚV	WS=	•94005	-13.34557	-5.25416
	ΚV	WT=	.60981	-20.95048	-8.24822
HIGH ALPHA					
STRAKE		K V =	14224	.70822	.27883
WING	ΚV	WR=	1.09716	-12.08363	-4.75734

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

LOW ALPHA	HIGH ALPHA
1.57299	1.43075
4.23752	1.09716
5.81051	2.52791
	LOW ALPHA 1.57299 4.23752 5.81051

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

CONFIGURATION NO. AD 14

AERODYNAMIC PARAMETEPS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
ST	RAKE			
	KP≖	•51482	27.26040	10.73244
ΚV	LE=	1.18831	20.79823	8.18828
WI	1G			
	KP=	2.47838	-6.95109	-2.73665
КV	LE=	1.86479	-5.54965	-2.18490
ΚV	S E =	•47626	-16.91000	-6.65748

1

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER DF (CM.)	PRESSURE (IN.)
LOW ALPHA					
WING	κv	WS=	.91187	-9.42461	-3.71047
	ΚV	WT=	•53377	-16,78056	-6.60652
HIGH ALPHA					
STRAKE		KV=	16172	4.50743	1.77458
WING	κv	WR=	1.09051	-8.04471	-3.16721

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	1.18831	1.02659
WING	3.78669	1.09051
TOTAL	4.97500	2.11709

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTRULDS POSITIVE AHEAD OF X SUB REF.

ALL MANAGER

CONFIGURATION NO. AD 17

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM•)	(IN.)
STR	RAKE			
	K P =	•51754	27.97658	11.01440
κv	LE=	1.39443	23.46973	9.24005
WIN	NG			
	KP=	2.47649	-6.95990	-2.74012
κV	LE=	1.86658	-5.54805	-2.18427
ĸ٧	SE=	.47651	-16.90997	-6.65747

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSURE
LOW ALPHA					
STRAKE			****		~~~~~~
WING	ΚV	WS=	.96713	-9.42461	-3.71047
	КV	WT =	•53426	-16.78056	-6.60652
HIGH ALPHA					
STRAKE		KV=	17153	4.50743	1.77458
WING	κV	WR=	1.15659	-8.04471	-3.16721

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

. .

	LOW ALPHA	HIGH ALPHA
STRAKE	1.39443	1.22290
WING	3.84450	1.15659
TOTAL	5.23893	2.37950

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING RODT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

CONFIGURATION NO. AD 19

AERUDYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

		CENTER OF	P RE SSUR E
		(CM.)	(TN•)
RAKE			
K P =	.51920	29.09821	11.45599
LE=	1.52509	24.71550	9,73051
١G			
КР≖	2.47571	-6.96455	-2.74195
LE=	1.86943	-5.54314	-2.18234
SE=	•47676	-16.90992	-6.65745
	RAKE KP= LE≠ NG KP= LE= SE=	RAKE KP= •51920 LE= 1•52509 NG KP= 2•47571 LE= 1•86943 SE= •47676	CENTER JF (CM.) RAKE KP= .51920 29.09821 LE= 1.52509 24.71550 NG KP= 2.47571 -6.96455 LE= 1.86943 -5.54314 SE= .47676 -16.90992

- 1

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE				******	
WING	κv	WS=	•96788	-9.42461	-3.71047
	кv	WT=	•53509	-16.78056	-6.60652
HIGH ALPH	4				
STRAKË		KV=	17166	4.50743	1.77458
WING	κv	WR=	1.15749	-8.04471	-3.16721

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	1.52509	1.35343
WING	3.84917	1.15749
TOTAL	5.37426	2.51092

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF.

Colored States and

43

CONFIGURATION NO. AD 22

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

		CENTER OF	PRESSURE
		(CM.)	(IN•)
STRAK	E		
KP	 .36314 	25.62949	10.09035
KV LE	•84897	15.40152	6.06359
WING			
КР	 2.61135 	, -7 •77578	-3.06133
KV LE	= 1.92669	-6.56003	-2.58269
KV SE	• 46973	-18.16844	-7.15293

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER DI	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE					
WING	ĸν	₩S=	1.01560	-8.79326	-3.46191
	κv	WT=	•50789	-16.78056	-6.6065?
HIGH ALPHA					
STRAKE		K V =	11543	5.44753	2.14470
WING	κv	WR=	1.14311	-7.86382	-3.09599

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	.84897	•73354
WING	3.91992	1.14311
TUTAL	4.76889	1.87664

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

CONFIGURATION NU. AD 23

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

		CENTER OF	PRESSURE
		(CM.)	(IN.)
STRAKE			
K₽=	•51110	25.71595	10.12439
KV LE≠	1.23796	19.06619	7.50637
WING			
K P =	2.45116	-8.19130	-3.22492
KV LŁ≖	1.86461	-6.80517	-2.67920
KV \$E=	• 47797	-18.16710	-7.15240

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER DF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE					
WING	ΚV	WS=	•94890	-9.42461	-3.71047
	κV	WT=	•53371	-16.78056	-6.60652
HIGH ALPHA					
STRAKE		KV≖	16829	4.50743	1.77458
WING	κV	WP=	1.13479	-8.04471	-3.16721

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	1.023796	1.06967
WING	3.82520	1.13479
TOTAL	5.06316	2.20446

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

CONFIGURATION NO. AD 24

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROTOS FOR RESPECTIVE COMPUNENTS

				CENTER	() F	PRESSURE
				(CM.)		(TN.)
STE	XAKE					
	K P=	•71047		26.0795	8	10.26755
κV	LE=	2.58358		20.7994	3	8.18875
WIN	IG					
	K₽≢	2.29250	*	-11.4550	4	-4.50986
κv	Lê=	2.12844	-	-9.2186	3	-3.62938
κv	SE=	• 49145		-21.0591	4	-8.29100

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSUPF
LUW ALPHA				(CM.)	(IN.)
STRAKE					
WING	КV	WS=	1.30214	-14.39884	-5.66490
	ΚV	WT=	.68298	-20.95048	-3.24922
HIGH ALPHA					
STPAKE		K V =	35128	84525	33278
WING	ΚV	WR=	1.69015	-12.32460	-4.85220

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS.

	LOW ALPHA	HIGH ALPHA
STRAKE	2.58358	2.23230
WING	4.60502	1.69015
TOTAL	7.18860	3.92245

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD DE X SUB REE

CONFIGURATION NG. ED 2

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE CUMPONENTS

		CENTER	OF PRESSURE
		(CM.)	(IN.)
STRAK	E		
KP	• 72502	26.3606	54 10 . 38608
KV LE	= 2.05003	3 21.6430	01 3.52087
WING			
KP	2.27735	5 -7.478	24 -2.94419
KV LE	= 2.1308	5 -5.0553	16 -1.99022
KV SE	.4844	7 -16.9108	-6.65783

*

-- - --

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSURE
				(CM+)	(IN•)
LOW ALPHA					
STRAKE					
WING	ΚV	₩S=	1.40750	-10.2189?	-4.02320
	ΚV	WT=	.68376	-16.78056	-6.60652
HIGH ALPHA					
STRAKE		K V =	37970	3.32467	1.30892
WING	К٧	WR=	1.62690	-8.25705	-3.25081

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	2.05003	1.67033
WING	4.70657	1.82690
TOTAL	6.75660	3.49723

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

- States

.

CONFIGURATION NO. ED 4

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

		CENTER OF	PRESSURE
		(CM.)	(IN.)
STRAKE			
К Р=	•63951	19.13682	7.53418
KV LE≖	.81712	13.03442	5.13166
WING			
K P=	2.36253	-7.16318	-2.82015
KV LE=	2.07982	-5.13568	-2.02192
KV SE=	•48295	-16.90952	-6.65729

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE					
WING	ΚV	WS=	1.05164	-10.21892	-4.02320
	κV	WT=	•66738	-16.78056	-6.60652
HIGH ALPHA					
STRAKE		K V =	28370	3.32467	1.30892
WING	κV	WR=	1.36501	-8.25705	-3.25081

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	.81712	• 53342
WING	4.28179	1.36501
TOTAL	5.09891	1.89843

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF.

CONFIGURATION NO. ED 5

AEPODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
STR	RAKE			
	KP=	•61122	25.27465	9.95065
кV	LE≠	1.81488	17.78000	7.00000
WIN	٩G			
	K₽≡	2.39163	-7.17987	-2.82672
KV	LE≖	2.14088	-4.92785	-1.94010
κV	S∈≡	• 48 347	-16.91074	-6.65777

*

AUGMENTED KV AND RESPECTIVE CENTRAID

				CENTEP OF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE					
WING	ΚV	WS=	1.27772	-9.89605	-3.89608
	κv	WT=	•65476	-16.78056	-6.60652
HIGH ALPHA					
STRAKE		K V =	29434	3.80543	1.49820
WING	ΚV	WR=	1.60284	-8.17290	-3.21768

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	1.81488	1.52054
WING	4.55683	1.60284
TOTAL	6.37171	3.12338

* WS - WING-STRAKE JUNCTURE> WT - WING TIP+ WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF.

CONFIGURATION NO. ED 6

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPUNENTS

			CENTER DF	PRESSURE
			(CM.)	(JN.)
STR	RAKE			
	K₽=	•51109	23.90473	7.41131
ĸν	LE=	1.28527	15.71219	6.18590
WIN	16			
	K P=	2.47902	-6.92226	-2.72530
ΚV	LE=	2.24632	-4.38198	-1.72519
κV	SE∗	•47872	-16.91109	-6.65791

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER DF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE					
WING	ΚV	₩S=	1.21764	-9.55342	-3.76119
	ΚV	WT=	•65443	-16.73055	-6.60652
HIGH ALPHA					
STRAKE		KV=	23299	4.31562	1.69906
WING	κv	WR=	1.47499	-8.08034	-3.18124

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STPAKE	1.28527	1.05228
WING	4.59711	1.47499
TOTAL	5.88238	2.52727

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTRUIDS POSITIVE AHEAD OF X SUP REF

CONFIGURATION ND. ED 9

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	('IN•)
STR	AKE			
	K d =	•58661	26.20599	10.31732
ΚV	LE=	2.17464	19.57205	7.70553
WIN	G			
	K P =	2.42399	-11.11763	-4.37702
κV	LE=	1.76518	-10.23904	-4.03112
ΚV	SE=	•49116	-21.12429	-9.31665

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE			**-		
WING	ĸν	WS =	1.21596	-13.97296	-5.50116
	ΚV	WT=	•53266	-20.95048	-8.24822
HIGH ALPHA					
STRAKE		KV=	26690	22599	08897
WING	κv	₩R≖	1.51077	-12.23265	-4.81601

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	2.17464	1.90774
WING	4.00496	1.51077
TOTAL	6.17960	3.41851

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BUDY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

CONFIGURATION ND. ED 10

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FUR RESPECTIVE COMPUNENTS

		CENTER OF	PRESSURE
		(CM.)	(TN.)
STRAKE			
KP≠	● 50 54 8	28.50904	11.22403
KV LE≖	1.77967	22.76328	9.96192
WING			
K P=	2.48890	-6.92711	-?.727?1
KV Ld=	1.80450	-5.75122	-2.26426
KV SE≖	•47589	-16.91475	-6.65935

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER DF	PRESSURF
				(CM.)	(IN.)
LOW ALPHA					
STRAKE	-				
WING	ĸν	¥5=	1.14091	-9.38705	-3.69569
	ΚV	w T =	•51389	-16.79056	-6.60652
HIGH ALPHA	4				
STRAKE		K V =	19777	4.56336	1.79660
WING	кν	WR=	1.35936	-8.03424	-3.16309

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
S TRAKE	1.77967	1.58190
WING	3.93519	1.35936
TOTAL	5.71486	2.94126

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS PISITIVE AHEAD OF X SUB REF.

1

CONFIGURATION ND. ED 11

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
ST	RAKE			
	KP=	•40680	28.47213	11.20950
κv	LE=	1.44936	21.37585	8.41569
WI	١G			
	K₽≡	2.57467	-6.64505	-2.61616
ΚV	LE=	2.00681	-4.90713	-1.93194
κv	SÉ≖	.47403	-16.91361	-6.65890

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE					
WING	κv	WS=	1.10913	-8.97117	-3.53196
	κv	WT=	•54106	-16.78056	-6.60652
HIGH ALPHA					
STRAKE		KV=	14511	5.18262	2.04040
WING	К٧	WR=	1.26942	-7.91582	-3.11646

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	1.44936	1.30425
WING	4.13104	1.26942
TOTAL	5.58040	2.57367

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING RUDT AT BUDY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

CONFIGURATION NO. ED 12

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(TN.)
ST	RAKE			
	K P=	.70071	24.62352	9.69430
ΚV	LE=	1.85714	17.32354	6.82029
WT	NG			
	KP=	2.31505	-7.40247	-2.91436
κV	LE=	2.12297	-5.09212	-2.00477
κV	SE=	•48518	-16.91343	-6.65883

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE					
WING	КV	¥S=	1.25039	-10.21892	-4.02320
	ΚV	WT=	.68123	-16.78056	-6.60652
HIGH ALPHA	4				
STRAKE		KV≃	33732	3.32467	1.30892
WING	ΚV	WR=	1.62298	-8.25705	-3.25081

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ΑLPHA	HIGH ALPHA
STRAKE	1.85714	1.51982
WING	4.53976	1.62298
TOTAL	6.39690	3.14280

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING POOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF.

TABLE IV.- Concluded

CONFIGURATION NO. ED 13

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

.

			CENTER OF	PRESSURE
			(CM.)	(<u>t</u> n •)
ST	RAKE			
	K₽=	•60003	19.20697	7.56180
κV	t,£≖	1.29273	10.49254	4 •1 30 92
WIN	NG			
	KP=	2.39464	-7.08858	-2.79078
KV	LE=	2.04864	-5.18236	-2.04030
κV	S E =	•47730	-16.91452	-6.65926

-

AUGMENTED KV AND RESPECTIVE CENTROID

			CENTER DE	PRESSURE
			(CM.)	(IN.)
ĸν	√ S≖	1.55413	-10.21892	-4.02320
KV	WT=	65738	-16.79056	-6.60652
	KV=	41926	3.32467	1.30892
ĸν	W R =	2.01723	-8.25705	-3.25081
	к v кv	KV 4S= KV 4T= KV= KV=	KV √S= 1.55413 KV WT= .65738 KV=41926 KV WR= 2.01723	CENTER 1F (CM.) KV dS= 1.55413 -10.21892 KV WT= .65738 -16.78056 KV=41926 3.32467 KV WR= 2.01723 -8.25705

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	НІСН АЦРЧА
STRAKE	1.29273	. 97347
WING	4.73744	2.01723
TOTAL	6.03017	2.89070

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING RUDT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

TABLE V.- THEORETICAL LOADING FACTORS AND THEIR CENTROIDS FOR HIGH-ANGLE-

OF-ATTACK AND LOW-ANGLE-OF-ATTACK SOLUTIONS FOR AD 19 CONFIGURATION

AT M = 0.2, 0.5, AND 0.7

CONFIGURATION NO. AD19, M=0.2

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

		CENTER OF	PRESSURE
		(CM.)	(IN.)
STRAKE			
K P =	•51920	29.09821	11.45599
KV LE=	1.52509	24.71550	9.73051
WING			
K P =	2.47571	-6.96455	-2.74195
KV LE=	1.86943	-5.54314	-2.18234
KV SE=	• 47676	-16.90992	-6.65745

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSURE
				(CM.)	(IN.)
LOW ALPHA					
STRAKE					
WING	κv	WS=	96788	-9.42461	-3.71047
	ΚV	WT=	•53509	-16.78056	-6.60652
HIGH ALPHA					
STRAKE		KV=	17166	4.50743	1.77458
WING	κv	WR=	1.15749	-8.04471	-3.16721

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	1.52509	1.35343
WING	3.84917	1.15749
TOTAL	5.37426	2.51092

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

CONFIGURATION NO. AD19, M=0.5

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
STI	RAKE			
	K P =	•51203	29.20243	11.49702
ΚV	LE=	1.28436	24.71052	9.72855
WI	NG			
	K P =	2.60191	-6.94693	-2.73501
ĸν	LE=	1.91991	-5.70278	-2.24519
ĸν	SE=	•52424	-16.90406	-6.65514

*

AUGMENTED KV AND RESPECTIVE CENTROID

			CENTER DF (CM.)	PRESSURE (IN.)
κv	WS=	. 81510	-9.42461	-3.71047
ĸν	WT=	•54954	-16.78056	-6.60652
	KV=	14456	4.50743	1.77458
κV	WR=	•97478	-8.04471	-3.16721
	к v к v к v	KV WS= KV WT= KV= KV WR=	KV WS= .81510 KV WT= .54954 KV=14456 KV WR= .97478	CENTER DF (CM.) KV WS= .81510 -9.42461 KV WT= .54954 -16.78056 KV WR= .97478 -6.04471

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	1.28436	1.13980
TOTAL	5.09316	2.11458

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

TABLE V.- Concluded

CONFIGURATION NO. AD19, M=0.7

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
STRA	IK E			
k	(P=	• 49980	29.42991	11.58658
KV L	.E= :	1.00813	24.90026	9.80325
WING	5			
ĸ	(P= 2	2.78608	-6.93080	-2.72866
KV L	.E= :	1.98825	-5.94225	-2.33947
KV S	E=	• 59649	-16.89273	-6.65068

*

AUGMENTED KV AND RESPECTIVE CENTROID

				CENTER OF	PRESSURE
				(CM+)	(IN.)
LOW ALPHA					
STRAKE					
WING	ΚV	WS=	•63980	-9.42461	-3.71047
	ΚV	WT=	•56910	-16.78056	-6.60652
HIGH ALPHA					
STRAKE		KV=	11347	4.50743	1.77458
WING	κv	WR=	•76514	-8.04471	-3.16721

TOTAL KV TERMS FOR RESPECTIVE COMPONENTS

	LOW ALPHA	HIGH ALPHA
STRAKE	1.00813	●89466
WING	3.79364	•76514
TOTAL	4.80177	1.65979

* WS - WING-STRAKE JUNCTURE, WT - WING TIP, WR - WING ROOT AT BODY

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

TABLE VI.- THEORETICAL LOADING FACTORS FOR BASIC WING-BODY CONFIGURATION,

FORWARD AND AFT WING POSITIONS, AT M = 0.2, 0.5, AND 0.7

CONFIGURATION NO. WB (FORWARD), M=0.2

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
FUR	EBODY			
	KP=	14528	40.60881	15.98772
ΚV	LE=	•79525	25.53876	10.05463
WIN	łG			
	KP=	2.82136	-5.86677	-2.30975
ΚV	LE=	2.08937	-4.50195	-1.77242
KV	SE=	•47270	-16.89933	-6.65328

CONFIGURATION NO. WB (AFT), M=0.2

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
FOR	REBODY			
	KP≈	•12428	44.15490	17.38382
ΚV	LE=	•71655	26.26426	10.34026
WIN	IG			
	KP=	2.68387	-12.27110	-4.83114
ΚV	LE=	1.88166	-10.26772	-4.04241
ĸν	SE=	•44007	-21.12594	-8,31730

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

CONFIGURATION NO. WB (FORWARD), M=0.5

÷

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
FOR	EBODY			
	KP=	•14084	41.23959	16.23606
КV	LE=	•77081	25.69708	10.11696
WIN	G			
	KP=	2.95294	-5.87690	-2.31374
ĸν	LE#	2.13494	-4.74203	-1.86694
ĸν	SE=	•52153	-16.89377	-6.65109

CONFIGURATION NO. WB (AFT), M=0.5

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
FOR	EBODY			
	K P =	.12237	44.55653	17.54194
ΚV	LE=	•70601	26.33711	10.36894
WIN	G			
	KP=	2.82370	-12.27750	-4.83366
ΚV	LE=	1.92481	-10.46036	-4.11825
KV	SE=	.48500	-21.12427	-8.31664

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF.

TABLE VI.- Concluded

CONFIGURATION NO. WB (FORWARD), M=0.7

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
FOF	REBODY			
	K-₽ =:	•13443	42.25679	16.63653
кV	LE=	•73947	25.93050	10.20886
WIN	١G			
	KP=	3.14255	-5.90174	-2.32352
KV	LE=	2.19310	-5.10675	-2.01053
KV	SE=	•59623	-16.88247	-6.64664

CONFIGURATION NO. WB (AFT), M=0.7

AERODYNAMIC PARAMETERS

INPUT KP, KV, AND CENTROIDS FOR RESPECTIVE COMPONENTS

			CENTER OF	PRESSURE
			(CM.)	(IN.)
FOR	EBODY			
	KP=	•11987	45.10319	17.75716
ĸν	LE=	•69273	26.43553	10.40769
WIN	١G			
	KP=	3.02807	-12.28616	-4.83707
ĸν	LE=	1.97715	-10.77852	-4.24351
КV	SE=	• 55497	-21.11832	-8.31430

NOTE: CENTROIDS POSITIVE AHEAD OF X SUB REF

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TABLE VII.- $\partial f / \partial R_a$ RESULTS AT M = 0.2

Strake designation	Ra	Rb	α*, deg	(C _{L,tot}) _{wb} at α*	$\frac{\frac{\partial (C_{L, tot})_{swb}}{\partial R_{a}}}{\alpha \star}$	f at α*	$\frac{\partial f}{\partial R_a}$
AD 9	0.183	0.197	26.8	0.87	Not available	1.50	
AD 14	.172	.212	27.3	.86	≈5.0	1.62	3.58
AD 17	.185	.212	28.4	.88	≈5.0	1.63	3.42
AD 19	.205	.212	29.3	.90	≈5.0	1.64	3.25
AD 22	.077	.144	36.0	.97	≈3.5	1.19	2.25
AD 23	.166	.212	34.2	.96	≈4.0	1.44	2.34
AD 24	.325	.297	31.9	.92	≈3.0	1.63	1.23
ED 2	.266	.297	36.9	.96	≈3.5	1.55	1.66
ED 4	.114	.297	30.3	.91	≈3.5	1.34	2.25
ED 5	.188	.262	28.3	.88	≈5.0	1.65	3.39
ED 6	.124	.226	33.2	.95	≈3.0	1.32	1.64
ED 9	.259	.253	30.6	.91	≈3.5	1.63	1.76
ED 10	.192	.208	28.4	.88	≈5.0	1.59	3.43
ED 11	.131	.163	38.4	.95	≈3.5	1.31	2.10
ED 12	.227	.297	33.4	.95	≈3.0	1.53	1.33
ED 13	.098	.297	34.2	.96	~4.0	1.26	2.65

Note: $\alpha^* = \alpha$ for $(C_{L,max})_{swb}$.

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Figure 1.- Three-view drawing of typical wind-tunnel model. Shaded area is associated with forebody balance; linear dimensions are in centimeters (inches).



Figure 2.- Three-quarter rear view of typical configuration.



Figure 3.- Analytically and empirically designed strakes. strakes tested in wind tunnel.)

(Shading indicates those



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ALC: NO

Figure 3.- Continued.





(c) Empirical group.



Figure 4.- Typical strakes.



Figure 5.- Three-quarter front view of model mounted on high-angle-of-attack sting support in Langley High-Speed 7- by 10-Foot Tunnel.


(a) AD 9.

Figure 6.- Effect of Mach number on basic longitudinal characteristics for complete configuration.

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(b) AD 14.

Figure 6.- Continued.



(c) AD 17.

Figure 6.- Continued.



(d) AD 19.

Figure 6.- Continued.

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(e) AD 22.

Figure 6.- Continued.



(f) AD 23.

Figure 6.- Continued.



(g) AD 24.

Figure 6.- Continued.

Carden Married Street of S



(h) ED 2.

Figure 6.- Continued.

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Figure 6.- Continued.





Figure 6.- Continued.





Figure 6.- Continued.



(l) ED 9.

Figure 6.- Continued.



(m) ED 10.

Figure 6.- Continued.



(n) ED 11.

Figure 6.- Continued.



(O) ED 12.

Figure 6.- Continued.





Figure 6.- Concluded.



(a) AD 9.

Figure 7.- Effect of Mach number on basic longitudinal characteristics for wing-afterbody.

87



(b) AD 14.

Figure 7.- Continued.



(c) AD 17.

Figure 7.- Continued.



(d) AD 19.

Figure 7.- Continued.



(e) AD 22.

Figure 7.- Continued.





Figure 7.- Continued.



(g) AD 24.

Figure 7.- Continued.







I

Figure 7.- Continued.



(j) ED 5.

Figure 7.- Continued.





(k) ED 6.

Figure 7.- Continued.



(1) ED 9.

Figure 7.- Continued.



(m) ED 10.

Figure 7.- Continued.



(n) ED 11.

Figure 7.- Continued.







Figure 7.- Continued.







Figure 7.- Concluded.



Figure 8.- Effect of Mach number on basic longitudinal characteristics for strake-forebody.

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r = 1



(b) AD 14.

Figure 8.- Continued.



Figure 8.- Continued.



(d) AD 19.

Figure 8.- Continued.




(e) AD 22.

Figure 8.- Continued.







Figure 8.- Continued.



(g) AD 24.

Figure 8.- Continued.





Figure 8.- Continued.





(i) ED 4.

Figure 8.- Continued.



(j) ED 5.

Figure 8.- Continued.





(k) ED 6.

Figure 8.- Continued.



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(1) ED 9.

Figure 8.- Continued.



(m) ED 10.

Figure 8.- Continued.







Figure 8.- Continued.



Figure 8.- Continued.







Figure 8.- Concluded.





Figure 9.- Complete-configuration longitudinal aerodynamic characteristics at M = 0.2; data and theoretical estimates.

119



(b) AD 14.

Figure 9.- Continued.



(c) AD 17.

Figure 9.- Continued.





Figure 9.- Continued.



(e) AD 22.

Figure 9.- Continued.





Figure 9.- Continued.



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(g) AD 24.

Figure 9.- Continued.

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(h) ED 2.

Figure 9.- Continued.



(i) ED 4.

Figure 9.- Continued.

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(j) ED 5.

Figure 9.- Continued.



(k) ED 6.

Figure 9.- Continued.



(1) ED 9.

Figure 9.- Continued.





Figure 9.- Continued.

131



(n) ED 11.

Figure 9.- Continued.



Figure 9.- Continued.





Figure 9.- Concluded.



Figure 10.- Component longitudinal aerodynamic characteristics at M = 0.2; data and theoretical estimates.



(b) AD 14.

Figure 10.- Continued.



(c) AD 17.

Figure 10.- Continued.





Figure 10.- Continued.



Figure 10.- Continued.





Figure 10.- Continued.



(g) AD 24.

Figure 10.- Continued.





Figure 10.- Continued.


(i) ED 4.

Figure 10.- Continued.



(j) ED 5.

Figure 10.- Continued.



(k) ED 6.

Figure 10.- Continued.





Figure 10.- Continued.



(m) ED 10.

Figure 10.- Continued.



(n) ED 11.

Figure 10.- Continued.



(O) ED 12.

Figure 10.- Continued.



(p) ED 13.

Figure 10.- Concluded.



(a) Complete configuration.

Figure 11.- Effect of Mach number on lift and pitching-moment characteristics for AD 19 configuration; data and theoretical estimates.





Figure 11.- Concluded.



(a) Forward wing position.

Figure 12.- Effect of Mach number on longitudinal aerodynamic characteristics for basic wing-body configuration; data and theoretical estimates.



(b) Aft wing position.Figure 12.- Concluded.



Figure 13.- Aerodynamic synergism effect on configuration lift at M = 0.2.



(b) AD 14.

Figure 13.- Continued.



(c) AD 17.

Figure 13.- Continued.

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Figure 13.- Continued.



(e) AD 22.

Figure 13.- Continued.

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(f) AD 23.

Figure 13.- Continued.



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(g) AD 24.

Figure 13.- Continued.



Figure 13.- Continued.



(i) ED 4.

Figure 13.- Continued.

Γ



(j) ED 5.

Figure 13.- Continued.



(k) ED 6.

Figure 13.- Continued.



(1) ED 9.

Figure 13.- Continued.



(m) ED 10.

Figure 13.- Continued.

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(o) ED 12.

Figure 13.- Continued.

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Figure 13.- Concluded.



i,

(a) AD 9.

Figure 14.- Aerodynamic synergistic effect on configuration pitching moment at M = 0.2.





Figure 14.- Continued.





Figure 14.- Continued.

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(d) AD 19.

Figure 14.- Continued.



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(e) AD 22.

Figure 14.- Continued.



(f) AD 23.

Figure 14.- Continued.



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(g) AD 24.

Figure 14.- Continued.

177

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(h) ED 2.






Figure 14.- Continued.

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(j) ED 5.

Figure 14.- Continued.



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(k) ED 6.

Figure 14.- Continued.





(1) ED 9.

Figure 14.- Continued.



(m) ED 10.

Figure 14.- Continued.

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(n) ED 11.

Figure 14.- Continued.



(o) ED 12.





(p) ED 13.

Figure 14.- Concluded.



Figure 15.- Theoretical and experimental variation of f with α for AD 19 at M = 0.2.



(a) AD 9.

Figure 16.- Effect of Mach number on additional lifting surface efficiency factor f.



(b) AD 14.

Figure 16.- Continued.





Figure 16.- Continued.



(d) AD 19.

Figure 16.- Continued.



(e) AD 22.

Figure 16.- Continued.



(f) AD 23.

Figure 16.- Continued.







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(h) ED 2.

Figure 16.- Continued.



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Figure 16.- Continued.



Ι.

(j) ED 5.

Figure 16.- Continued.



(k) ED 6.

Figure 16.- Continued.



Figure 16.- Continued.

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Figure 16.- Continued.



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Figure 16.- Continued.

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(o) ED 12.

Figure 16.- Continued.



Figure 16.- Concluded.



Figure 17.- Effect of R_a on f for a fixed gothic-strake shape at M = 0.2 and $R_s = 7.00$.



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Figure 18.- Effect of chordwise scaling on f for AD 24 strake at M = 0.2 and $R_b = 0.297$.



Figure 19.- Effect of strake shape, R_s , and R_b on f at fixed R_a and M = 0.2.



h 4 ____

Figure 19.- Continued.



Figure 19.- Continued.



Ser. 18. - 1

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(d) $R_a \approx 0.263$.

Figure 19.- Concluded.



Figure 20.- Effect of strake shape on f at $R_b = 0.212$ and M = 0.2.



Figure 21.- Effect of R_a , R_b , and R_s on f for the "better" gothic strakes at M = 0.2.



Figure 22.- Effect of removing area from AD 24 stake on f at M = 0.2.



(b) Trailing-edge cut.





(c) Inboard-edge cut.

Figure 22.- Concluded.


Figure 23.- Effect of strake-design pressure specification (for a fixed prescribed suction distribution) on f at M = 0.2.





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(a) 16⁰ ≤ α ≤ 21.7⁰.















WATER





M = 0.3AIR





Figure 25.- Continued.



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M = 0.3AIR

α = 30°

α 🖬 32.5°

WATER

(c) $30^{\circ} \leq \alpha \leq 32.6^{\circ}$.







WATER

(d) α < 35.4⁰.

Figure 25.- Continued.



AIR

Real And







WATER

Figure 25.- Concluded.

(e) α ≧ 35.4⁰.

α = 37.6°



Figure 26.- Vortex breakdown progression on delta wings in air and water.



Figure 27.- Effect of strake vortex on lift data. AD 24; M = 0.3.

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16. Abstract Sixteen analytically and empirically designed strakes have been tested experimentally on a wing-body at three subcritical speeds in such a way as to isolate the strake-forebody loads from the wing-afterbody loads. Analytical estimates for these longitudinal results have been made using the suction analogy and the augmented vortex lift concepts. The synergistic data are reasonably well estimated or bracketed by the high- and low-angle-of-attack vortex lift theories over the Mach number range and up to maximum lift or strake-vortex breakdown over the wing. Also, the strake geometry is very important in the maximum lift value generated and the lift efficiency of a given additional area. Increasing size and slenderness ratios are important in generating lift efficiently, but similar efficiency can also be achieved by designing a strake with approximately half the area of the largest gothic strake tested. These results correlate well with strake-vortex-breakdown observations in the water tunnel.					
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