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THE MEASUREMENT OF THE GROUND WIND STRUCTURE
at Wallops Island
Final Report
NASA Grant NGL 47-004-67
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The Measurement of the Ground Wind Structure at Wallops Island
Final Report

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Department of Engineering Science and Mechanics

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SUMMARY

Detailed measurements of the mean and turbulence characteristics of the surface wind measured near the Atlantic coast at Wallops Island, Virginia, are presented in this comprehensive final report. This final report consists of five articles and a detailed report of the experimental results for the U.S. Department of Energy under contract no. AC 06-79 ET 23007. Earlier reports dealing with the instrumentation, calibration, data handling, data analysis and early results are not included in this final report. Detailed information on these items are available as reports from the National Technical Information Service under NASA-CR-62093, 1973, NASA-CR-137456, 1974, NASA-CR-140586, 1974, and NASA-CR-141422, 1977.

The experimental data were acquired from a 76-meter tall instrumented micrometeorological tower. Mean wind and turbulence measurements were made with two types of instrumentation consisting of cup-vane and temperature probes, primarily used for mean profile measurements of velocity and temperature respectively. The second system, a hot film and thermocouple system, was used for measurement of turbulence variances and covariances and spectra. The cup-vane system was used to acquire data from all wind directions, while the hot-film system was primarily used for turbulence measurements from the two prevailing wind directions, south and north-west.

The micrometeorological tower is a self-standing non-guyed tower with five working platforms at 15.2m (50 ft.) intervals, with cup-vane and aspirated temperature probes mounted at each platform. This instrumentation system is used by N.A.S.A. in conjunction with its sounding rocket launching operations. With this system data could be
acquired without interruption for about eight hours at a rate of one sample each two seconds. A total of 195 digital tapes were generated with this system during the period of July 1974 and December 1978. Approximately 300 data records were analyzed, each varying between 43 and 85 minutes in duration.

Six three-dimensional split-film anemometers (T.S.I.-1080) were used for the turbulence measurements. These instruments were mounted on 1.8m booms at the same levels as the cup-vane instruments and also at the 9m (30 ft.) level. The electronics for this system as well as the data-acquisition and data-handling system were located in an instrumentation trailer parked at the base of the tower. This system was designed to handle outputs from six split-film anemometer systems, sampled at a rate of 200 samples per second for a period of approximately one hour. A total of 32 one-hour data runs were acquired with the hot-film system between July 1976 and December 1978 and analyzed for variances, covariances and spectra.

All data were acquired under predominantly moderately strong wind conditions with an hourly mean wind speed between 10 m/s and 20 m/s at the 76.2 (250 ft.) level. Under these conditions, the atmosphere near the surface cannot be considered neutrally stable, and convective effects must be included in the analysis of the data. For on-shore winds, the surface flow is more complicated as the result of the development of an internal boundary layer. The latter is initiated as the air crossing the beach from the water generally experiences a change in surface roughness and in surface temperature. The internal boundary layer has a height between 15m and 30m at the tower location depending on the development distance from the beach which varies with wind
direction. Also for southerly winds during the day time, the warmer air flows over the cooler water, allowing the formation of a surface-based inversion of variable depth. Under these conditions a low-altitude maximum velocity (surface jet), occasionally below the highest observation level of 76m, has been observed. Under extreme stable conditions at hourly mean velocities in excess of 10 m/s at the highest observation level, the turbulence has been observed to vanish completely. Moreover, low-frequency internal gravity waves have been observed to co-exist with the turbulence.

For continental winds under convective conditions, usually encountered during the day time, the planetary boundary layer (P.B.L.) is usually characterized by a strong upward heat flux and by strong vertical mixing due to the positive buoyancy forces. As the result of this intense mixing process a relative sharp inversion layer separates the mixed layer from the free atmosphere. This inversion delineates the depth of the P.B.L. Under uniform surface conditions the surface flow can be modeled adequately by the Morin-Obukhov (M.O.) similarity theory.

Westerly winds approaching the Wallops site pass in succession over the mainland, the Chesapeake Bay, the "Delmarva" peninsula and the tidal marsh. For the last 100m-300m the air travels over the island before it arrives at the tower location. As the result of the nonuniformity of the surface roughness and the surface temperature encountered by these westerly winds, the applicability of the M.O. theory is questionable. As the air flows over water the upward heat transfer is interrupted and the downward heat flux from the inversion at the edge of the P.B.L. penetrates down to the surface. This downward heat flux is often observed at the tower site under convective conditions, while at the
same time the temperature gradient would suggest an upward heat flux.

More complications of the surface flow may be encountered when clouds are present and condensation of water vapor occurs within the P.B.L. Under these conditions latent heat is released and an inversion layer develops just below the cloud base which is responsible for the suppression of the turbulence below this inversion. Also for westerly winds between $300^\circ$ and $330^\circ$, the instantaneous wind direction experiences frequently large fluctuations toward the north. These direction fluctuations are not normally distributed, providing an explanation for the unusual high lateral turbulence intensities and the non-zero lateral horizontal shear component $\vec{vw}$.

The experimental results of this research program clearly indicate that there is no single and no simple flow model available to describe the mean and turbulent flow near the surface under moderately strong wind conditions at the Wallops Island site. The presence or absence of appreciable low-frequency velocity fluctuations causes the statistical parameters describing the turbulence to vary a great deal. The non-uniform surface conditions and the presence of large-amplitude low-frequency fluctuations, either in the convective boundary layer or in the on-shore winds in the form of interval gravity waves, cause the observed surface flow to be quite different from the M.O. boundary layer flow model.

ACKNOWLEDGEMENTS

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E. Carr and F. Schmidlin as well as the former Director of Wallops Space Flight Center, Mr. R. L. Krieger. In particular the valuable technical assistance of Mr. C. A. Lewis, J. van Overeem, P. H. Randall and R. L. Kelley is acknowledged.
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AN INSTRUMENTATION SYSTEM FOR THE MEASUREMENT OF ATMOSPHERIC TURBULENCE

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Summary

A method is described for the detailed multi-point measurement of the turbulent velocity components and temperature in the atmospheric surface layer. The TSI three-dimensional split-film anemometer system is used as sensor and a special designed data-acquisition and data-handling system is used for the sampling, digitizing and storing of the data on digital magnetic tapes. Further processing of the data is performed in a digital computer and programs are developed to allow efficient calculation of the statistical quantities such as, mean values, covariances, power- and cross-spectral density functions. At the present, six anemometer systems have been mounted on the 30-, 50-, 100-, 150-, 200- and 250-foot levels of the 250-foot Meteorological Tower at NASA, Wallops Flight Center. The tower is located at Wallops Island which is one of the barrier islands protecting the so-called "Delmarva" peninsula from the Atlantic Ocean. The island, which consists of a narrow strip of dunes approximately three meters above sea level, is situated in a northeast—southwest direction and is separated from the mainland by a three-mile wide tidal swamp.

Introduction

The aerodynamic properties of the lower part of the atmospheric boundary layer up to a height of approximately 500 feet, are usually measured with instruments placed on masts, meteorological towers or other tall structures. For measurements at higher altitudes, instruments placed on meteorological balloons or low-flying aircraft can be used. During the last two decades a number of research programs dealing with these measurements and interpretation of the aerodynamic properties of the atmospheric boundary layer have been carried out. A discussion of some of the tower measurements can be found in the literature and a comprehensive review of these studies has been given by Panofsky [1], Busch [2], Haugen [3] and Panofsky [4]. Except for a few cases, most of these research programs have been limited in scope because of the lack of simultaneous and multi-point velocity and temperature measurements over a wide frequency range. For example, in many cases either the

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vertical velocity component or the fluctuating temperature are missing or measurements are made with instruments whose frequency response is limited.

The objective of this NASA-supported research program is to develop a system which will be able to obtain a complete and an extensive set of multi-point measurements of the three velocity components and the temperature in the lower atmosphere. These measurements will allow the accurate determination of mean values and statistical information of the low level atmospheric turbulence.

Instrumentation

The total vector anemometer 1080 system manufactured by Thermo-Systems, Inc, was chosen for this research program since it seems to have the advantage of small physical size, fast response and high sensitivity over a wide range of velocities. In addition, the probe consists of three split-film sensors as shown in Fig.1, which allows the determination of magnitude and direction of the instantaneous velocity vector.

The three sensor rods are mounted mutually perpendicular to form a Cartesian coordinate system from now on referred to as the sensor-oriented coordinate system. The active sensing element consists of a thin platinum film of approximately 1000 ångström thickness and 0.080 inch long, which is placed on a 0.2 inch long and 0.006 inch diameter cylindrical quartz rod. A thin coat of quartz over the film is used to provide protection from the environment. The platinum film on each rod consists of two segments,
separated from each other by two longitudinal splits 180 degrees apart*. The orientation of the splits on each sensor rod is such that it allows the determination of the octant in which the instantaneous velocity vector is located. For minimum support interference, the three sensor rods are mounted at only one end to a thin supporting structure in which the electrical leads are embedded. The active elements on each rod are electrically heated to the same constant temperature by separate anemometer circuits. A copper—constantan thermocouple is mounted close to the sensors and measures the ambient temperature with a maximum frequency response of 25 Hz. The manufacturer's performance specifications list a response up to 1 kHz depending on the cable length used. For tower mounting of the probes, cable lengths of approximately 350 feet and 200 feet were used. The three sensors and the thermocouple are protected, while not in use, by a shield which can be placed over the sensors and retracted pneumatically. An air stream is continuously supplied through the shield, in order to keep the sensors free of contamination and moisture while not in operation.

The data acquisition and data handling system was designed to handle output data from one to thirteen anemometer systems, sampled at a rate of 200 samples per second, for a duration of approximately 45 minutes. All necessary equipment and controls are fixed in an instrumentation trailer placed under the meteorological tower. The system consists of two main parts: (a) the multiplexing and analog recording system, schematically shown in Fig.2 and (b) the demultiplexing, digitizing and digital recording system, shown in Fig.3.

*Patented by Thermo-Systems, Inc.
Fig. 3. Demultiplexing, digitizing and digital recording system.

Each anemometer provides seven analog voltages, one from the thermocouple circuit and six from the anemometer circuits, all in the range of 0–5 volts. All voltages are frequency modulated by voltage-controlled oscillators, each with a different center frequency. For the output of each anemometer there is one set of voltage-controlled oscillators with center frequencies of 8, 12, 16, 20, 24, 28 and 32 kHz, respectively. All voltage-controlled oscillators operate at a deviation from their center frequency of ±1 kHz for a maximum voltage input of ±5 volts. The seven frequency-modulated signals, together with a reference signal of 100 kHz are summed by a summing amplifier to produce one single multiplexed signal of approximately 3 volts peak-to-peak. The multiplexed signals from the six anemometers are simultaneously recorded on six separate channels of a 14-channel analog tape recorder. The time-of-day is recorded on a separate channel of the analog tape recorder and serves as a reference for the recorded data.

At a later time, the analog tape is replayed and the multiplexed signal from the desired channel is demultiplexed to its seven components after passage through seven discriminators. A reference discriminator senses any deviation in the reference frequency of 100 kHz caused by fluctuations in the tape speed of the analog tape recorder and corrects the output of the seven discriminators accordingly. Consequently, the six outputs corresponding to the six anemometer bridge voltages are each passed through a 100 Hz low-pass filter. This is necessary to avoid aliasing (distortion) of the velocity spectra at frequencies below 100 Hz from contributions of frequencies above 100 Hz. Next, the seven analog voltages are passed through the analog-to-digital converter where the analog signals are sampled at a rate of 200 samples per second and each sample is converted to an 16-bit (plus sign) digital word. The total scan, settling and conversion time for the sampling of the seven voltages is 50 microseconds, which is approximately 1% of the time interval between two
scans. The recorded time-of-day is converted to a 32-bit binary coded decimal signal by a serial-to-parallel converter which is interfaced with the controller computer by a custom-designed interface. The computer (DEC Model PDP 11/20) controls the multiplexing, analog-to-digital conversion as well as the digital recording. The computer is programmable in DEC PAL-11 assembly language and has an 8 K memory of 16-bit-words. Access to the computer is obtained through a teletypewriter.

The data conversion starts at a time-of-day prescribed by the operator, and the analog-to-digital converter performs successive scans and conversion of the seven analog voltages into two-byte (16 bit) words at a rate of one scan every 5 milliseconds. These words are stored in one of the four buffers of the computer which in turn dumps the data on a 9-track digital magnetic tape. Each buffer has a capacity of 209 scans which represents 1.05 seconds of data. A total of 2500 records make up a data sample, extending over a time period of approximately 45 minutes.

Operation

The total heat flux for a split-film sensor, where both films are operating at the same temperature is given by

\[ (I_1^2 R_{f1} + I_2^2 R_{f2})/(T_f - T_a) = C + D(\rho U_e)^n, \]

where \( I_1 \) and \( I_2 \) are the heating currents of films 1 and 2, respectively. \( R_{f1} \) and \( R_{f2} \) are the hot film resistances, \( T_f \) is the film operating temperature, \( T_a \) is the ambient temperature, \( \rho \) is the air density, \( U_e \) is the effective cooling velocity which is a function of the velocity magnitude and the sensor yaw angle, \( \phi \), and \( n \) is the exponent in the heat transfer equation. Introducing the relation for the effective cooling velocity as suggested by Hinze [5] and relating the velocity to standard pressure, \( P_s = 29.92 \) inches of mercury and standard temperature \( T_s = 530 \) degrees Rankin, the heat flux equation becomes

\[ (I_1^2 R_{f1} + I_2^2 R_{f2})/(T_f - T_a) = C + DU_e^n (\cos \phi + k^2 \sin^2 \phi)^{n/2}, \]

where \( U_e \) is the velocity related to standard conditions and \( k \) is an experimentally determined coefficient of the order of 0.1.

Introducing the bridge voltages \( E_1 \) and \( E_2 \) for films 1 and 2, respectively, equation (2) can be modified to

\[ Q/\Delta T = (K_1 CF_1 E_1^2 + K_2 CF_2 E_2^2)/(T_f - T_a) = DU_e^n (\cos \phi + k^2 \sin^2 \phi)^{n/2}, \]

where \( Q \) is a measure of the total heat transfer, \( CF_1 \) and \( CF_2 \) are temperature correction factors for films 1 and 2, respectively, to account for cable and ambient temperature changes as discussed and defined by Tieleman and Tavoularis [6]. The constants \( K_1 \) and \( K_2 \) should ideally be the ratio of the film resistance and the square of the corresponding bridge resistance. However, these constants also correct for area and resistance differences of the two films and must be determined experimentally. In addition, for all veloc-
ties of interest in this study, the constant \( C \) may be eliminated by adjustment of the constants \( K_1 \) and \( K_2 \).

Assuming that the three sensors A, B and C are mounted mutually perpendicular, the following trigonometric relation holds for the sensor-yaw angles.

\[
\sin^2 \phi_A + \sin^2 \phi_B + \sin^2 \phi_C = 1. \tag{4}
\]

The standard effective-cooling velocities are related to the magnitude of the standard velocity \( U_s \) and the sensor-yaw angles, \( \phi_\alpha \), by the expression

\[
U_{es_\alpha} = U_s^2 (\cos^2 \phi_\alpha + k_\alpha \sin^2 \phi_\alpha), \tag{5}
\]

where the subscript \( \alpha \) refers to either one of the sensors A, B or C. Assuming that identical values of \( k_\alpha \) exist for all three sensors and using expressions (4) and (5), the magnitude of the standard velocity can be expressed in terms of the effective-cooling velocities of the three sensors as follows,

\[
U_s^2 = \frac{(U_{es_A}^2 + U_{es_B}^2 + U_{es_C}^2)/k_{av}}{k_{av}}. \tag{6}
\]

Here the constant \( k_{av} \) is of the order of 2.1 and needs to be determined through calibration.

The sensor-yaw angles can be obtained from expressions (4) and (5) and be of the following form

\[
|\phi_\alpha| = \arcsin \left( \frac{1 - (C \alpha U_{es_\alpha}/U_s)^2}{1 - k_\alpha} \right)^{1/2}, \tag{7}
\]

where the coefficients \( C_\alpha \) are of the order of unity but due to variations in heat transfer with sensor-pitch angle, \( \phi_\alpha \), these coefficients may deviate a small amount from unity. In reference to Fig.1, it can be seen that the sign of the sensor yaw angles, \( \phi_A \), can be determined by comparing the output voltages of sensor C. In case \( \phi_A \) is zero degrees, the velocity vector is located in a plane formed by the sensors B and C which is similar to the plane formed by the two splits of sensor C. In this case, the ratio of the output voltages of sensor C is defined as

\[
E_{1C}/E_{2C} = R_C. \tag{8}
\]

In general, when the ratio of the film voltages, \( E_{1C}/E_{2C} \) is larger than \( R_C \), the sensor-yaw angle, \( \phi_A \), is considered positive and if the above ratio is less than \( R_C \), \( \phi_A \) is considered to be a negative angle. Similarly, the magnitude of the ratios \( E_{1A}/E_{2A} \) and \( E_{1B}/E_{2B} \) will determine the sign of the sensor-yaw angles \( \phi_B \) and \( \phi_C \), respectively.

The actual velocity components in the sensor-oriented coordinate system can now be calculated since the magnitude of the velocity and its direction with respect to the sensor-oriented coordinate system is known. The actual velocity can be obtained from the standard velocity using the continuity equation and the equation of state for a perfect gas as

\[
U = (P_s/P)(T/T_s)U_s, \tag{9}
\]
where $P$ and $T$ are the ambient pressure and ambient absolute temperature of the air at the time the measurements were made.

The correction factors $CF_1$ and $CF_2$ in expression (3) need to be introduced to account for cable temperature changes as well as ambient temperature changes. According to Tieleman et al. [7], the values for these correction factors for the six different bridge voltages can be calculated as follows:

$$CF_{ai} = \left(1 + \left(\frac{\Delta R_{ca_i}}{R_{fa_i}}\right)\right) \frac{(T_{ta_i}^0 - T_0^0)}{(T_{fa_i} - T_0)}.$$  \hspace{1cm} (10)

Again, the subscript $a$ refers to either sensor A, B or C and the subscript $i = 1,2$ indicates the appropriate film. The zero-superscribed quantities refer to the calibration conditions in the TSI laboratory. $\Delta R_c$ represents the change in cable resistance, $R_f$ represents the hot film resistances. The second factor in (10) represents the correction for ambient temperature and film temperature.

Tieleman et al. [7] tested the accuracy of the three-dimensional split-film anemometer in the low-speed wind tunnel at VPI and SU for a wide range of velocities and angles of attack. In order to improve the accuracy, changes were made in the so-called "improved accuracy" as suggested by Olin and Kiland [8]. In addition, a temperature correction was introduced to correct the output voltages for variations in heat transfer and cable resistance as a result of variations in ambient temperature. These changes were not sufficient since new tests indicated rarely a percentage error of less than 5 percent for the calculation of the velocity components. This high percentage of error was due to a number of problems which were prominent over different ranges of probe-yaw angles. The heat transfer is not constant when the sensor rod is rotated about its axis which results in errors in the evaluation of the cooling velocities, total velocity and sensor-yaw angles. Secondly, large errors are made in estimation of the sensor-yaw angle, $\phi$, when the absolute value of this angle is less than 10 degrees which occurs when the probe-yaw angle, $\beta$, is approximately $\pm 40$ degrees. Errors due to convection of heat from an upstream sensor to a sensor located directly downstream results in a lower estimate for the cooling velocity of the downstream sensor. This occurs when the probe-yaw angle, $\beta$, is $\pm 90$ degrees. For certain probe-pitch angles, the thermocouple senses an ambient temperature which is too high as a result of convection of heat from an upstream sensor. In addition, a different method for the evaluation of the velocity components as suggested by Olin and Kiland [8] was tried with slightly better results. This method was later rejected because the required calibration procedures were too lengthy. From all these tests it was concluded that the TSI three-dimensional split-film probe cannot measure velocity and direction over the full 360° solid angle in three-dimensional flow fields within the accuracy as was claimed by the manufacturer. It was finally concluded that this instrumentation can only be used with the mean velocity closely, parallel to the probe axis if an accuracy of less than 5 percent is required. In order to satisfy this requirement, it was decided to use the three-dimensional split-film probes in conjunction with a
rotating mechanism which allows the probe to be rotated about a vertical axis so that the average probe-yaw angle will be close to zero.

Calibration

Based on the conclusions reached as the result of extensive testing of the probes, new calibration procedures were developed by Tieleman and Tavoularis [6]. The calibration information is obtained from wind tunnel testing of the three-dimensional split-film probe as follows. First, data is taken over a range of velocities between 3.5 and 50 feet per second with each of the three sensors perpendicular to the flow. With the probe-yaw angle, \( \beta \), equal to zero and probe pitch angle, \( \alpha = -35.26 \) degrees, sensor A is perpendicular to the flow. Sensors B and C become perpendicular to the flow when the probe pitch angle, \( \alpha \), equals zero and \( \beta \) is +39.25 degrees and \( \beta \) is -39.25 degrees, respectively. Additional data are taken for \( \alpha = 0 \) degrees and probe-yaw angles in the range of \( \beta = \pm 50 \) degrees in steps of 10 degrees. In addition, measurements have to be made of the cold film resistance and cable resistances in order to determine the correction factors. The various constants that are necessary for the calculation of the velocity components are determined from the above measurements. First, the heat flux from each sensor is calculated when the sensor is perpendicular to the flow according to expression (3), using values for the constants \( K_1 \) and \( K_2 \) those suggested by the manufacturer as a first approximation. These constants for two of the three sensors are then adjusted so that the heat transfer versus cooling velocity curves collapse to one single curve, see Fig.4. The next step is to determine the proper values for coefficients \( D \) and exponent \( n \) in equation (3) with the sensor-yaw angle, \( \phi \), equal to zero. It turns out that no single set of values for \( D \) and \( n \) describes the calibration curve adequately. The calibration curve has to be divided into three ranges with different values for \( D \) and \( n \) in each range. Once the heat flux versus effective cooling velocity relation has been established, the standard cooling velocities, \( U_{eS} \), can now be calculated for the set of data where the probe-yaw angle is varied between \( \pm 50 \) degrees. Assuming that an expression like (6) exists, an average value of the coefficient \( k_{au} \) can be calculated since the magnitude of the standard velocity \( U_{eS} \) is measured independently by a Pitot static tube during the wind tunnel testing. The final step is to determine the calibration constants \( C_\alpha \) and \( k_\alpha \) for expression (7). These constants for sensors B and C are obtained by fitting a curve of the form of expression (7) to the calibration data. The latter are obtained by plotting the velocity ratio \( U_{eS}/U_{eS} \) versus the predetermined sensor-yaw angles, as shown in Fig.5. The yaw angle for sensor A can be obtained by using the trigonometric relation (4) after the values of angles \( \phi_B \) and \( \phi_C \) have been determined.

As an example of the above calibration procedure and the accuracy with which the velocity components can be obtained, the calibration constants for the probe mounted on the 100-foot level of the meteorological tower are given in Table 1.

Figures 6 and 7 show the accuracy with which the velocity components can be obtained as a function of the probe-yaw angle, \( \beta \). For small probe-yaw angles, the velocity components can be determined within 5% with respect to
Fig. 4. Calibration curve for sensor heat flux, $Q/(T_f-T_a)$, versus standard cooling velocity, $U_{es}$ (probe No. 1193).

Fig. 5. Calibration curve for the ratio $U_{es}/U_s$ versus sensor-yaw angle (sensor B of probe No. 1193).
TABLE 1

Calibration constants for the TSI No. 1183 anemometer

<table>
<thead>
<tr>
<th>Sensor</th>
<th>Film</th>
<th>$T_f$</th>
<th>$T_f'$</th>
<th>$T_{f,cold}$</th>
<th>$R_f$</th>
<th>$\alpha_f$</th>
<th>$T_{cold}$</th>
<th>$R_{cold}$</th>
<th>$K$</th>
<th>$k$</th>
<th>$C$</th>
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<td>633</td>
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</tr>
<tr>
<td>B</td>
<td>1</td>
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<td>521</td>
<td>73.5</td>
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<td>7.28</td>
<td>2.1748</td>
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</tr>
</tbody>
</table>

$Q/\Delta T > 0.52$, $D = 0.1299$ and $n = 0.44$

$Q/\Delta T < 0.52$, $D = 0.1723$ and $n = 0.35$

$Q/\Delta T < 0.38$, $D = 0.1761$ and $n = 0.34$

$k_{au} = 2.0665$

$T_{f,cold}$ is the temperature at which the cold-film resistance, $R_{f,cold}$, is measured and $\alpha_f$ is the temperature coefficient of resistivity of the film. $T_{c}$ is the temperature at which the resistance of the cable, $R_{c}$, is measured. $K$ represents the film constants as in equation (3), and $k$ the constant in the expression for the effective cooling velocity (2). $C$ is a constant in the expression for the sensor-yaw angle. $R$ represents the ratio of the two film voltages of each sensor at zero sensor-pitch angle. $D$ and $n$ are a coefficient and exponent in the heat flux expression (3) and $k_{au}$ is a constant in the expression for the determination of the standard velocity.

the magnitude of the velocity vector over a velocity range data are expected to be gathered. For probe-yaw angles of about plus and minus 40 degrees, large errors may occur as a result of the low sensitivity of the ratio $U_{gs}/U_s$ with respect to the sensor-yaw angles $\phi_c$ and $\phi_B$ respectively.

The general calibration procedure which was suggested by TSI proved to be complicated and inaccurate and as a result this new calibration procedure had to be developed. This calibration was based on the recognized fact that the three-dimensional split-film anemometer gives the most accurate results when the probe operates with its axis parallel to the direction of the mean-wind vector and the sensors directed into the wind.

All measurements that are necessary for the calibration are performed at the Quality Verification and Calibration Facility at NASA Wallops Flight Center. The entire procedure is streamlined into a standard form, allowing a reasonably fast and efficient calibration of the large number of anemometers used in this research program. Based on these calibration procedures, a computer program was developed, which converts the output voltages of the anemometers into velocity components and allows the determination of all required calibration constants.
Comparison test

The three-dimensional split-film anemometer was tested in the atmosphere and the results were compared with the results from two Gill propeller anemometers. These propeller anemometers were mounted in such a way that one
was parallel to the TSI probe axis and the other perpendicular to the first one and both in a horizontal plane and located adjacent to the TSI probe. Not only the mean velocity components were compared, but also variances, covariances and power spectra measured with the two different types of instrumentation were compared. The results of these tests are listed in a report by Tieleman and Chen [9], and the results of one set of data are given in Table 2.

**TABLE 2**

<table>
<thead>
<tr>
<th>Mean wind components in the probe oriented coordinate system</th>
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<tbody>
<tr>
<td><strong>TSI No. 1192</strong></td>
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<tr>
<td>$U'$ (ft./sec)</td>
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<tr>
<td>$V'$ (ft./sec)</td>
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<tr>
<td>$\theta$ (degrees)</td>
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<table>
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<tr>
<th>Means, variances and covariances of the velocity components in the mean-wind coordinate system</th>
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<tr>
<td><strong>TSI No. 1192</strong></td>
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<tr>
<td>$U$ (ft./sec)</td>
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<td>$u^2$ (ft./sec)$^2$</td>
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<td>$w^2$ (ft./sec)$^2$</td>
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<tr>
<td>$uw$ (ft./sec)$^2$</td>
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</table>

The velocity components in this table are given in the mean-wind coordinate system, which is determined by the direction of the vertical plane containing the sample mean velocity vector. The 40-minute data run is broken up in 40-second blocks which is necessary for the fast Fourier analysis. The block means of the longitudinal velocity component measured by the Gill anemometer are consistently higher than those measured by the TSI probe; the same is true for the sample mean velocity. This is due to the fact that the propeller anemometer accelerates faster as a result of a sudden velocity increase and decelerates slower as a result of a similar velocity decrease. However, due to the limited response characteristics of the Gill anemometers, the turbulence quantities obtained from the Gill anemometer are consistently lower than those obtained from the TSI anemometer. The same phenomenon is well illustrated in Figs. 8 and 9 where the power spectra of the longitudinal and the lateral velocity components are compared for the two types of anemometers. These results indicate that the Gill anemometer has the proper response capabilities up to 1 Hz. The spectra measured by the Gill anemometers fall off at a faster rate at frequencies higher than 1 Hz while the split-film anemometer
Fig. 8. Power spectrum of the longitudinal velocity component.

Fig. 9. Power spectrum of the lateral velocity component.
spectra show an extensive region where the spectrum function varies as the frequency raised to the $-5/3$ power. Details of the calculation of the statistical quantities and the spectral analysis technique are described in references [6] and [9].

Conclusions

A complete data-acquisition and data handling system was designed to take high frequency (100 Hz maximum) wind and temperature data measured by TSI 1080 three-dimensional split-film anemometers. At the present, six probes are mounted at 50 foot intervals on the 250-foot meteorological tower located at Wallops Island on the Atlantic coast. All probes can be rotated so that their axis can be placed closely parallel to the mean wind direction. The time duration of each data sample is approximately 45 minutes. The output voltages from all six probes are simultaneously recorded on analog magnetic tapes. At a later point in time, the analog tape is played back and the analog signals from each anemometer are digitized, at a rate of 200 samples per second.

The three-dimensional split-film anemometer system provides seven output voltages from which the velocity components in the sensor-oriented coordinate system and the temperature can be calculated. The general calibration procedure as suggested by the manufacturer proved to be complicated and inaccurate, as a result, a new complete calibration procedure has been developed. This calibration procedure is based on the fact that the anemometer gives the most accurate results when the probe operates with its axis parallel to the direction of the mean-wind vector and the sensors directed into the wind. The data measured with these anemometers are compared with the data measured with a set of propellor-type Gill anemometers. Mean values, variances, covariances and spectra of the two horizontal wind components, measured simultaneously with these two types of anemometer systems, are compared. The discrepancies of the measured quantities can be attributed to the varying and limiting response characteristics of the Gill propeller anemometers.

As a result of carefully carried out calibration procedures, accurate statistical estimates of long time series describing the fluctuating wind components can be obtained with the TSI 1080 three-dimensional split-film anemometer system.

Acknowledgements

The research reported in this article is supported by the NASA Grant NGL 47-004-067. Continuous support from the grant monitor, Mr J.F. Spurling of NASA Wallops Flight Center is gratefully acknowledged.
References

A STUDY OF THE MEAN AND TURBULENT FLOW IN THE LOWEST 250-FEET OF AN ON-SHORE WIND

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ABSTRACT

Three-dimensional velocity measurements and temperature measurements were obtained on the 250-foot meteorological tower located near the Atlantic Ocean at Wallops Island, Virginia. The wind approached the tower from the ocean. As the wind passes the shore line at an oblique angle it experiences a change in roughness and possibly a change in surface temperature, resulting in a complex three-dimensional type flow.

Measurements of the mean and turbulent flow quantities were made with a special computer-controlled data-acquisition system. Data analysis includes the following statistical parameters: mean velocity and temperature, variances and covariances including heat fluxes and Reynolds stresses. Nine, one-hour runs were analyzed and the results agreed closely with the suggested model.

INTRODUCTION

The Monin-Obukhov similarity theory is based on the assumptions that the flow in the surface layer can be treated as being steady in the mean and takes place over a horizontal and homogeneous surface. The assumptions that coriolis and pressure-gradient forces are negligible and the flow is parallel to the surface, lead to a one-dimensional treatment of the problem. Real atmospheric flows, where inhomogeneity of the surface is a common occurrence, do not correspond to this ideal situation. Abrupt changes in surface roughness and surface temperature lead to horizontal fluxes of momentum and heat.

An example of this type of flow is the oblique passage of an on-shore wind from the ocean to the land surface. Over the ocean a large part of the radiation is spent on evaporation of the water and much less for heating the water. During a warm summer day, the warmer air blows over the cold water surface and the lower layer of the atmosphere is cooled and an inversion develops. For an on-shore wind this stable layer is heated from below after it crosses the coastline, and in addition the surface roughness changes from
smooth to rough. This leads to development of an unstable internal boundary layer (IBL) with stable air above it. The depth of the IBL increases with increased distance from the shore (Fig. 1). In addition, the overland flow becomes three dimensional if the on-shore wind passes the beach at an oblique angle. After a certain distance inland from the shore, the IBL may reach some degree of equilibrium when the advection of momentum and heat in both the direction of the mean flow as well as in the lateral direction has decreased sufficiently in comparison to the vertical heat flux. At that point the one-dimensional model could describe the flow adequately, and, theoretically, the M-O similarity theory can then be applied to the lower part of the IBL.

An experimental study is currently underway to measure the mean and turbulent flow quantities for such flow. Velocity and temperature measurements are made with fast- and slow-response type instruments mounted at six levels on a 250-foot meteorological tower at NASA-Wallops Flight Center. The tower is located at Wallops Island, Virginia which is bordered by the Atlantic Ocean on the east and a tidal flat on the west. Wind and temperature sensors are located at the 30 and the 50-foot levels and from there at 50-foot intervals along the height of the tower. The island is one of the barrier islands along the coast of the Delmarva peninsula and consists of a narrow strip of dunes 10 feet above sea level and directed approximately along a line from North-East to South-West. The distance from the tower to the shore along the prevailing summer-wind direction (North-South) is approximately 1000 feet (Fig. 2).

A special computer-controlled data-acquisition system is capable of sampling the six fast-response anemometer systems at a rate of 200 samples per second for a period of about one hour. Data analysis includes the determination of the following statistical parameters: mean values, variances, covariances (vertical heat flux and turbulent stress), spectra and cospectra. Nine, one-hour runs with reasonable stationary characteristics have been analyzed, and the results closely agree with the suggested flow model.

MODEL FOR THE ON-SHORE FLOW

The basic governing equations for a thermally-stratified atmospheric boundary layer, where temperature does affect the dynamics of the flow, are the Boussinesq equations. In order to deal with the mean flow and the turbulence separately, Reynolds averaging is introduced. This process leads to the well known Reynolds equations which include the turbulent stresses and the turbulent heat fluxes. It is assumed that humidity variations do not affect the dynamics of the flow and therefore can be considered as a passive part of the air.

In order to facilitate the study of the flow, let us consider the following simplifications:

a. Mean and statistical flow parameters do not vary with time.
b. Mean flow parallel to the surface.
c. Molecular fluxes negligible compared to corresponding turbulent ones.
d. Vertical component of the Coriolis force negligible compared to the gravitational force.
e. Gradients of the pressure field are neglected.

With these imposed conditions, the equations for the mean flow and mean temperature take the following form.

Momentum equation:

x-direction (horizontal and in direction of the surface stress)
\[ U \frac{\partial U}{\partial x} + V \frac{\partial U}{\partial y} = - \frac{\partial p}{\partial x} - \frac{\partial p}{\partial y} - \frac{\partial p}{\partial z} + fV \] (1)

y-direction (horizontal)
\[ U \frac{\partial V}{\partial x} + V \frac{\partial V}{\partial y} = - \frac{\partial p}{\partial x} - \frac{\partial p}{\partial y} - \frac{\partial p}{\partial z} - fU \] (2)

z-direction (vertical)
\[ 0 = - \frac{\partial w}{\partial x} - \frac{\partial w}{\partial y} - \frac{\partial w}{\partial z} + g \frac{T^*}{T_0} \] (3)

Continuity:
\[ \frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} = 0 \] (4)

Thermodynamic energy equation:
\[ U \frac{\partial T^*}{\partial x} + V \frac{\partial T^*}{\partial y} = - \frac{\partial q}{\partial x} - \frac{\partial q}{\partial y} - \frac{\partial q}{\partial z} \] (5)

This is the set of equations that governs the flow in the IBL and the overlying inversion. The Coriolis terms can be neglected in the IBL but not always in the overlying inversion layer. In the absence of large-scale vertical eddies in this layer, no turbulent mixing can occur with the adjacent layers and the effect of Coriolis forces can no longer be ignored.

In the case the flow direction makes an oblique angle with the coast line, the flow becomes three-dimensional in the IBL and horizontal momentum and heat fluxes exist, although these may be small compared to the vertical fluxes. As the flow moves inland the lateral fluxes as well as the longitudinal fluxes will decrease, and the flow in the IBL gradually recovers its one-dimensional character if no other inhomogeneities are encountered.

The question is whether or not experimental data obtained in this three-dimensional flow can be analyzed in the Monin-Obukhov framework, which realistically applies only in the constant flux layer. After the IBL has developed for a certain minimum distance, it can be assumed that the horizontal fluxes become relatively unimportant in comparison to the vertical fluxes. In this case, the local shear velocity, \( U_* = \sqrt{-\frac{\partial w}{\partial z}} \), the local characteristic temperature, \( T_* = \frac{-w}{kU_*} \), the buoyancy parameter, \( g/T_0 \), and the height \( z \) should be the relevant independent variables influencing the
statistical parameters which describe the turbulence. It is assumed that the Coriolis parameter, \( f \), only affects the mean flow and does not affect the turbulence appreciably. With this approach one can define a "local" stability length, \( L = \frac{U_3}{\kappa \frac{g}{\theta_0} \omega} \), which would convert into the surface stability length, \( L_0 \), as the surface layer is approached. Consequently, the dimensionless statistical parameters describing the turbulence should be functions of \( z/L \) only. In order to conclude whether or not the M-O similarity hypothesis can be applied to the IBL and overlying inversion, the experimental results should be compared carefully with the results in the surface layer over uniform terrain. For this purpose the Kansas data will be used as reported by Kaimal et al. [2].

**INSTRUMENTATION, DATA ACQUISITION, DATA HANDLING AND DATA ANALYSIS**

The data are obtained with high frequency three-dimensional split-film anemometers (TSI-1080 D) and a low-frequency system consisting of cup-vane instruments and aspirated platinum-resistance temperature probes. The TSI probes are mounted on the south face of the 250-foot tower at heights of 30, 50, 100, 150, 200 and 250-feet. The cup-vane instruments are mounted on both the South-East and the North-West corner of the tower at 50 foot intervals. The temperature sensors are mounted on the North side of the tower at 50 foot intervals. The data obtained with the low-frequency instruments are recorded on digital tape at a rate of 1 sample every two seconds.

The operation of the three-dimensional anemometers capable of making high-frequency velocity and temperature measurements is discussed in detail by Tieleman and Tavoularis [6]. Each probe is mounted on a rotor which is capable of rotating the probe about a vertical axis so as to align the probes approximately into the mean wind direction. A mini-computer controlled data-acquisition and data-handling system is placed in a trailer located directly beneath the 250-foot meteorological tower.

The output of each anemometer consists of seven voltages, one from the thermocouple and six from the hot films. These signals are low-pass filtered at 100 Hz, and then sampled and digitized at a rate of 200 samples per second. The digital results are analyzed on the IBM-370 computer at VPI and SU. A fast Fourier transform algorithm, developed by Tieleman and Chen [5], is used to calculate the spectra and cospectra. In view of the computer capabilities, the number of data points per block is chosen to be \( N = 2^{13} \) (40.96 seconds in real time). A total of 75 blocks (51.2 minutes in real time) were analyzed per run. Because of this treatment of the data, the turbulence can only be analyzed in a frequency range from 0.0244 Hz to 100 Hz. The high-frequency limit of the thermocouple is approximately 16 Hz although its output is sampled at 200 Hz and analyzed up to 100 Hz. Consequently, variances and covariances as well as spectra and cospectra involving the temperature have to be analyzed differently in order to account for the noise contribution in the frequency range between 16 Hz and 100 Hz.
Four computer programs for the analysis of the data have been developed. The first program converts the voltages to velocity components and temperature, and in addition records those quantities on digital tape. These velocity components are obtained in the TSI-sensor oriented coordinate system [5,6]. The second program calculates block means and block variances of the velocity components and temperature. In addition, the probe-yaw angle, $\beta$, (horizontal angle between mean wind and probe axis) and the total number of reverse arrangements [1] of the means and variances, are calculated at this point. Inspection of the block means and block variances and their total number of reverse arrangements is the test for stationarity of the run. Based on this information a decision is made whether or not to continue the analysis. The third program converts the velocity components in the mean-wind coordinate system (Fig. 2), calculates the block means and removes the block means from the data in each block. Next, all the possible variances and covariances are calculated for each block and averaged to obtain the mean variances and covariances for the entire run. Also the velocity and temperature data with the mean removed are recorded digitally once more. With the fluctuating velocity components available in the mean-wind coordinate system and with the fluctuating temperature, the spectra and cospectra of the following pairs of variables, $u\omega$, $\omega\theta$, and $\omega\theta$ are obtained. The variance of the temperature and $\omega\theta$ covariance were obtained by integration of the $\theta$ spectra and $\omega\theta$ cospectra in the frequency range from $0.0244 \, \text{Hz}$ to $16 \, \text{Hz}$.

DISCUSSION OF RESULTS

Until recently, data were only collected during the summer months. Since the prevailing winds are from the south during the summer, the split-film probes were mounted on the south side of the tower. Originally, thirteen one-hour data runs were taken; however, four of these runs were rejected as being nonstationary. Table 1 shows the results of the mean flow and the turbulence of the nine runs which were analyzed. The values of the direction angle, $\phi$, indicate the direction of the mean-wind vector measured clockwise with respect to north.

The results show clearly the presence of an unstable inner layer and a stable outer layer. For each run, the vertical heat-flux changes direction between 50 and 100 feet. The results (not all listed in Table 1) indicate that the flow is three-dimensional, fluxes of heat and momentum in the horizontal direction are appreciable, but are usually less than the vertical fluxes.

For most of the runs, the velocity profiles when plotted in the usual semi-logarithmic fashion show one or more "kinks." Extrapolation of the velocity from the 50 and 30 foot elevations lead to extremely high roughness lengths, $z_0$, especially for runs 2, 7, 8 and 9 ($z_0 > 1 \, \text{foot}$). These values of $z_0$ are typical for flow over moderately rough terrain, such as wooded areas and suburban areas, but are too high for the terrain at Wallops Island in this case. Consequently, these extremely high roughness lengths indicate the presence of an abnormal boundary layer. The velocities at the higher elevations are much higher than under normal conditions, when large-scale
turbulence provides, as a result of turbulent mixing, a much more uniform velocity profile. In the absence of large-scale eddies, Coriolis forces may become sufficiently important to affect the flow. The results do indicate this, runs 1, 7 and 8 show a maximum clockwise rotation of the mean flow direction of 4 to 10 degrees between the 50 and 250-foot levels.

The mean-temperature profile for the nine runs show some unusual "kinks" mostly between the 100 and 150 foot levels. The most interesting sequence of mean-temperature distributions is from runs 7, 8 and 9 (Fig. 3), which were taken on the afternoon of August 13, 1976 starting at 2:12 P.M., 3:37 P.M. and 5:05 P.M., respectively. The early afternoon runs show a decrease in temperature up to the 100-foot level and an increase in temperature for higher elevations. In the early afternoon the layer above the 100-foot level shows a rather strong positive temperature gradient. As the afternoon progresses this temperature gradient decreases dramatically. The run starting at 5:05 P.M. shows a decrease in surface temperature with a subsequent cooling trend in the lower 50 feet.

Many of the afternoon runs show a decrease in temperature with height up to the 100-foot level, then a slight increase between the 100 and 150 foot levels and decreasing temperatures above the 150-foot level. The temperature profiles obtained outside the IBL are governed by the depth of the inversion layer over the ocean. Apparently, this depth was larger than 250 feet during the early afternoon (Run 7); the second run of the afternoon (Run 8) still shows a positive temperature gradient but of a much smaller magnitude. For the third run (Run 9) the temperature gradient between 100 and 150 feet is slightly positive but above the 150-foot level it is negative. This indicates that during the afternoon the inversion layer is decreasing in depth but also that its degree of stability is decreasing.

No simple relationship exists between the standard deviations of the three velocity components normalized with the local shear velocity and the stability parameter $z/L$ for extreme stable conditions, $z/L > +2.0$ (Figs. 4, 5 and 6). For near neutral conditions the average values of $\sigma_\alpha/U_\alpha$ are 1.75, 1.5 and 1.4 for $\alpha = u, v$ and $w$, respectively. The values of the variances in stable and near-neutral air depend on the frequency response of the instruments with which the velocities are measured and the manner in which the data are analyzed. Low-frequency contributions affect the horizontal variances significantly, and consequently the way in which the means are removed from the original time series can influence the magnitude of these variances a great deal. The results also indicate that the ratios $\sigma_\alpha/U_\alpha$ are very sensitive with stability, and increase drastically for deviations from neutral conditions in both the stable and unstable regime. The standard deviations of the velocity fluctuations, $\sigma_\alpha$, show maximum values in the IBL and decrease rapidly across the interface between this layer and the overlying inversion. In the stable air the vertical variances are usually smaller than the horizontal variances. Inspection of Table 1 reveals that the vertical fluctuations almost disappear for those runs with clockwise rotation of the mean wind with height. This indicates that turbulent mixing in this layer with adjacent air does not exist and Coriolis forces become important.
The ratio, \( \sigma_\theta / |T*| \), shows a great deal of scatter close to neutral thermal stratification as \( T* \) should approach zero (Fig. 7). Values of 2.0 or larger are common in the IBL. In the stable air above this layer, values of this ratio decrease sharply with increased stability to an average of 0.5. Panofsky [4] reports that \( \sigma_\theta / |T*| \) shows an average of 1.8 in stable air and decreases with increasing stability similar to the results obtained at Wallops Island. In this study the temperature ratio, \( \sigma_\theta / |T*| \), was obtained with the local scaling temperature \( T* \) rather than the value of this quantity in the surface layer.

The values of the uw covariances are all negative as expected, except for run 8, 150-foot level. The local shear velocities obtained from these covariances are successfully used as reference velocities for the calculation of the scaling temperature, \( T* \), the stability parameter, \( z/L \), and the flux Richardson number. The uw covariances show maximum values at the 30-foot level except for run 8 and 9. Extremely small values for uw were obtained in the stable air above the IBL. The lowest value was obtained at the 250-foot level for run 7, for which the largest rotation of the mean wind direction was measured. The results in Table 1 indicate that extremely small values of uw not automatically mean absence of large scale eddies. Runs 1 and 8 which show clockwise rotation of the mean-wind direction with height, also show larger uw covariances than those from other runs which do not experience any appreciable rotation of the mean-wind vector. These results seem to indicate that the contribution to the shear for runs 1 and 8 must come from the velocity fluctuations with smaller wave lengths.

The we covariances show positive heat flux in the IBL and negative values in the overlying inversion layer. The values of these covariances are of the same magnitude, indicating that the upward heat flux in the IBL is of the same order as the downward heat flux in the stable layer. Because of the absence of large scale eddies in runs 1, 7 and 8 it can be concluded that heat is more effectively transported by the smaller eddies. Considerable horizontal heat transfer occurs at the interface between the IBL and the overlying stable layer.

The characteristic length-scale of the energy-containing eddies can be obtained from the normalized autocorrelation function using Taylor's hypothesis,

\[
L_x^U = U \int_0^\infty R(\tau) d\tau
\]  \hspace{1cm} (6)

In Table 1 the values of \( L_x^U \) were obtained from the measurements made with the NASA cup-vane instruments. These instruments do not respond to high-frequency velocity fluctuations and consequently, the calculated values for the integral length-scale, \( L_x^U \) may be somewhat high.

An alternate method for obtaining a measure of the scale of the energy containing eddies is the wave length corresponding to the reduced peak frequency of the logarithmic longitudinal velocity spectra:
\[ \lambda_m^u = z/f_m^u \]  

Kaimal [3] gives the following relation for the two length scales

\[ \lambda_m^u = 2\pi L_x^u \]  

According to the results listed in Table 1, there does not seem to exist a simple relation between \( \lambda_m^u \) and \( L_x^u \). For most runs, \( \lambda_m^u > L_x^u \) for the unstable flow in the IBL. This trend is reversed for the stable flow above the IBL; the integral length scale, \( L_x^u \), is in most cases larger than \( \lambda_m^u \) by a factor of 1.5 - 2.0. The length scale, \( \lambda_m^u \), is smaller in the stable air for those runs which show rotation of the mean wind, as is to be expected. The block length used for the analysis of the cup-vane data is about 512 seconds, and removal of the block means results in high-pass filtering at a lower frequency. Consequently, large scale fluctuations are included in the determination of the autocorrelation, resulting in large values of the turbulence integral scale. These low frequency fluctuations which can be identified as gravity waves, are present in run 4 at all levels above the IBL and at the 250-foot level of run 7.

CONCLUSIONS

The results of this experimental study indicate that the stable on-shore flow, modified by changes in surface roughness and surface temperature, does not lead to an ordinary boundary layer with the usual vertical turbulent mixing. The measurements support the physical model which include the development of an unstable internal boundary layer (IBL) with a stable overlying inversion. The magnitudes of the variances of the velocity components and the \( uw \) covariances decrease rapidly across the interface between the two layers. The vertical heat flux is positive in the IBL and negative in the overlying inversion. The roughness lengths, \( z_0 \), are unusually high, indicating that the velocity profile is not the normal profile one would encounter in an atmospheric boundary layer with large-scale turbulent mixing. Under certain conditions these large-scale eddies are absent in the inversion layer and the Coriolis forces gain importance resulting in a noticeable clockwise rotation of the wind direction above the IBL.

The air in the inversion layer and in the IBL are essentially independent, and ordinary boundary-layer models based on turbulent mixing cannot be applied. Consequently, in absence of turbulent momentum exchange with adjacent layers, the wind velocity of the stable layer is larger than the velocity in the adjacent layers. This explains the existence of a low level jet with a maximum velocity at an elevation of approximately 300 feet. It is believed that the presence of the low-level jet depends on the depth and the degree of stability of the inversion layer above the ocean just before it is modified by travelling over land.

The presence of the low-level jet with the corresponding clockwise rotation of the mean wind vector, depends on the existence of large-scale eddies which promote the turbulent mixing between the layers. Large positive values
of the stability parameter, z/L and flux-Richardson number are necessary but not sufficient for the absence of these large-scale eddies. At the present time it is not clear under what conditions this type of flow will occur. In order to shed some light on these questions it will be necessary to study the stable boundary layer over the ocean before it is being modified by the land surface.

REFERENCES


Figure (1) - Model for the temperature profiles for on-shore flow and the internal boundary layer.
Figure (2) - Tower location on Wallops Island and orientation of a general mean-wind coordinate system.

Figure (3) - Temperature distributions for runs 7, 8, 9.

Figure (4) - Ratio of standard deviation of longitudinal velocity and local friction velocity as a function of z/L.
Figure (5) - Ratio of standard deviation of lateral velocity and local friction velocity as a function of $z/L$.

Figure (6) - Ratio of standard deviation of vertical velocity and local friction velocity as a function of $z/L$.

Figure (7) - Ratio of standard deviation of the temperature and local scaling temperature as a function of $z/L$. 
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Atmospheric Turbulence Below 75m in the Convective Boundary Layer (Strong Wind Conditions)

by

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Summary

Mean as well as turbulent velocity and temperature measurements obtained from the 76m micrometeorological tower at Wallops Island, Virginia are discussed. The measurements were obtained with cup-vane instruments and aspirated temperature probes (5 levels) for mean profiles as well as with hot-film probes (6 levels) for turbulence parameters. The wind conditions during data acquisition can be classified as moderately strong (at least 10 m/sec at the 15m level) with winds coming from directions varying between north and west. These conditions are usually encountered following the passage of a cold front. Observations have been compared with strong wind results as listed in several review papers. A new scheme is developed for the normalization of the velocity spectra using a reduced frequency related to the characteristic length scale of the velocity components associated with the inertial subrange.

Introduction

In the field of wind-engineering dealing with wind loads on structures, it is generally assumed that under strong wind conditions the flow in the atmospheric boundary layer is controlled by the mechanically produced turbulence [1,2,3]. In general, the turbulence in the planetary boundary layer (PBL) is either mechanically produced or buoyancy produced. Recent observations throughout the PBL have indicated that significant entrainment of heat and momentum from the free atmosphere is still another source of production of turbulent energy, specifically in the low-frequency range [4,5,6]. Depending on the atmospheric conditions and surface conditions any combination of these three turbulence-producing mechanisms can play an important role in the development of the mean flow and the turbulent structure in the PBL even under moderately strong wind conditions.
Based on observations [4,5] and theoretical considerations [7], the convective boundary layer over uniform terrain has been divided into three different layers:

1. The surface layer (lowest 10% of the PBL or less) where the wind shear plays a dominant role and the momentum and the heat fluxes are reasonably constant with height. Monin-Obukhov similarity applies in this layer to the statistical parameters involving the vertical velocity component, but not to those of the horizontal velocity components. Panofsky [8] has suggested that in the surface layer, proper scaling of the standard deviation, σ, of the horizontal turbulence components is of the following form

\[ \frac{\sigma}{U^*} = f(\frac{z_i}{L}) \]  

where \( U^* \) is the surface friction velocity, \( z_i \) is the height of the PBL delineated by the location of the lowest inversion layer and \( L \) the Monin-Obukhov length.

2. Above the surface layer a free convection layer exists where the convective turbulence dominates the mechanical turbulence (-z/L>1).

3. The remaining part of the PBL is called the mixed layer, where, as a result of strong mixing, the mean flow as well as the turbulence are no longer functions of height and the surface stress.

Overlying this three-layered structure is an inversion layer through which considerable amounts of heat and momentum enters the PBL from the free atmosphere.

Observations made over extremely flat and uniform terrain in northwestern Minnesota [4] show a net downward heat flux in the upper parts of the mixed layer. It was also observed [5] that the entrained warm air descends in the form of discrete plumes and upward heat flux from the surface takes place in the form of distinct thermals in an alternating fashion. Moreover, the spectra of the horizontal velocity components in the surface layer follow two different similarity schemes [6]. The inertial subrange of these spectra follows Monin-Obukhov similarity, whereas the low-frequency range follows mixed-layer similarity with \( z_i \) as the controlling parameter.

How the flow in the convective PBL will be modified as a result of nonuniformities in upstream terrain is difficult to predict. The terrain variations have a more pronounced effect on the flow as it passes several times from land to water
and back to land. In such a case the air will be in a transient state, being affected by variations in the surface fluxes of moisture, heat and momentum. The northwestern flows observed at Wallops Island will have crossed in succession the U.S. mainland, the Chesapeake Bay (20-50 km), the "Delmarva" Peninsula (20-50 km) and for the last 3-5 km the tidal swamp separating Wallops Island from the peninsula. The last 60-100 m, the air travels over the island before it arrives at the tower. During the daytime, the upward heat flux from dryland will be much higher than from water or moist swamp terrain. Consequently, the upstream flow will experience a discontinuity in surface heat flux as it crosses the tidal swamp, and the downward heat flux, which is the result of entrainment of warm air from the free atmosphere, can be expected to penetrate further downward into the PBL.

This paper deals with the discussion of mean flow and turbulence measurements obtained from the 76-meter micrometeorological tower at Wallops Island, Virginia. The data were obtained under strong wind conditions of at least 10 m/sec at the 15-m level and from directions varying between north and west. These conditions are usually encountered following the passage of a cold front. In addition to daytime data, some nighttime observations are reported for comparison. One set of observations was obtained from a direction where a 6.5-m high rocket-fuel storage bunker is approximately 85 m upstream of the tower. The strong wind observations have been compared with the results from the review papers ESDU, 1974 [2] and Counihan [3].

A new scheme is developed for the normalization of the velocity spectra in the high-frequency range using a reduced frequency related to the characteristic length scale of the turbulence associated with the high-frequency range. More stable estimates of the characteristic length scale of the energy-containing eddies can be obtained in this manner as compared to the traditional integral scales obtained from the autocorrelation function.

Experimental Details

The Wallops Island tower is instrumented at six levels with hot-film anemometer probes capable of high-frequency velocity and temperature measurements. A description of these probes, data acquisition and data handling system as well as a
description of the data analysis can be found in detail in a report by Tieleman and Tavoularis [9] and in a shorter version in a paper by the same authors [10]. In addition, cup-vane velocity instruments and aspirated temperature sensing probes used for the measurement of mean quantities are mounted at five levels. The data obtained with the hot-film probes were sampled 200 times per second; the output of the wind- and temperature-profile sensors once every two seconds. A total of six 55-minute periods of observation with the hot-film instruments as well as approximately 25 runs of varying duration (between 48 and 80 minutes) with the cup-vane and aspirated temperature sensors form the data base for this paper. The data from the hot-film probes are analyzed in two frequency ranges, the high-frequency analysis in the range of 0.0244-100 Hz and the low-frequency analysis in the range 0.00153-6.25 Hz. The data from the cup-vane and aspirated temperature sensors are analyzed in the range of 0.00195-0.25 Hz. Computation of spectra followed the procedures as described in a report by Tieleman and Chen [11].

Experimental Results

a. Mean Wind Profile

Mean-wind profiles under strong wind conditions over relatively smooth and uniform terrain follow closely either the logarithmic law

\[ \frac{U}{U_0} = \frac{1}{k} \ln \frac{z}{z_0}, \]

or the power law

\[ \frac{U}{U_1} = \left(\frac{z}{z_1}\right)^\alpha \]

where \( U_0 \) is the profile friction velocity, \( k \) the von Karman constant (\( k = 0.4 \)), \( z_0 \) the roughness length, \( U_1 \) is the mean velocity at some reference height \( z_1 \) and \( \alpha \) the power index.

The height of the layer where these profile laws apply depend on the wind speed, the terrain roughness as well as the surface heat flux and the atmospheric conditions at the upper edge of the PBL. The Wallops velocity profiles show that this height, even under relatively strong wind conditions, may be limited to 50 m or less (Tables I and II). Mean temperature and turbulent heat flux observations show a countergradient downward heat flux to within
a height of 9.1 m above the ground for all runs listed in Table II, including the even-
ing run. These results indicate that warm air is transported downward to the surface, possibly as a result of entrainment of warm air into the PBL from the free atmosphere. Low-frequency components in the measured velocity spectra, for all runs listed in Table II with the exception of run 16, similar to those observed by Kaimal [6], seem to point to the existence of a mixed layer. Such flow will require a transition from the velocity profile in the surface layer to a uniform velocity profile in the mixed layer showing up as a kink in the profile. Changes of this type in the mean velocity profile have been observed for several runs at a height of approximately 50 m. These profile changes are definitely not associated with a change in upstream roughness as is observed for run 186 A with the bunker about 85 m upstream from the tower (Figs. 1 and 2). The variation of the power index with the corresponding roughness length for all Wallops data tend to fall between the relations suggested by ESDU 1972 [12] and Counihan [3] (Fig. 3). This indicates that the Wallops wind profiles below the kink fall in the strong wind category.

b. Turbulence Parameters

1. Turbulent Stress

The measured local shear velocity defined as

$$u^* = [(\overline{uw})^2 + (\overline{vw})^2]^{1/4}$$

obtained from the hot-film probes in the lowest 30 m and analyzed in the high-frequency range \((0.0244 < f < 100 \text{ Hz})\) compared quite well with the profile friction velocity \(U^*_o\). This indicates that the velocity profile up to 30 m is matched with the turbulent stress obtained in the high-frequency range, implying that the foreign low-frequency components do not affect the velocity profile appreciably in this layer and that the mechanical turbulence dominates. Moreover, the results indicate that the profile friction velocity \(U^*_o\) is an accurate measure of the local shear velocity in this layer.

2. Standard Deviations and Turbulence Intensities

Standard deviations of the velocity components were obtained from the cup-vane instruments \((\sigma_u, \sigma_v)\) in the frequency range of 0.00195-0.25 Hz, and from the
hot-film probes \((\sigma_u, \sigma_v \text{ and } \sigma_w)\) in the frequency range of 0.00153-6.25 Hz. Because of the limited frequency response, \(\sigma_u\) from the cup-vane system had to be adjusted by a factor of 1.17 after being compared with \(\sigma_u\) from the hot-film instruments. The results clearly indicate that the ratio \(\sigma_u/U_o\) at the 15 m level is consistently lower for those runs with the convective kink in the velocity profile (table I and II). With a kink the average \(\sigma_u/U_o = 2.5\), and without a kink the average \(\sigma_u/U_o = 2.9\), both measured at the 15 m level, and decreasing to 2.2 and 2.7 respectively at the 76-m level. The variations in \(\sigma_v/U_o\) and \(\sigma_w/U_o\) do not seem to follow any systematical pattern. Average values of \(\sigma_v/U_o\) vary from 2.5 at the 15-m level down to 2.3 at the 76-m level, while the average value of \(\sigma_w/U_o = 1.2\) is uniform over the depth of the layer investigated.

Mixed layer similarity as suggested by Panofsky [3] does not work for the Wallops data, probably as a result of slightly non-homogeneous upstream terrain but more importantly as a result of the variation in upstream surface heat flux. Consequently, for those involved in practical situations when perfectly uniform conditions are rarely encountered, it seems more advantageous to use turbulence intensities. Figures 4, 5 and 6 show the averaged turbulence intensities of all three components compared with the intensities suggested by ESDU, 1974. The comparison is excellent except for the lateral turbulence intensities which are consistently higher than those predicted by ESDU, 1974 [2].

3. Turbulence Scales and Spectra

The characteristic length scales of the energy-containing eddies of the turbulence in the atmospheric surface flow are used quite extensively, especially for geometrically scaled model studies of the flow in wind tunnels. This turbulence length scale is also important in relation to the characteristic size of a structure exposed to a corresponding turbulent flow. Determination of these scales can be achieved by several methods:

a. Integration of the autocorrelation coefficient with respect to the time lag up to the first zero crossing. The autocorrelation coefficient can be obtained either directly from the velocity data or via the Fourier transform of the spectrum function.
b. Determination of the wavelength corresponding to the peak of the logarithmic power spectrum.

c. From the best fit of the measured spectrum function to the corresponding empirical von Karman spectrum functions.

d. By estimation of the velocity spectrum function at zero frequency

$$L_\alpha = \frac{U}{4} \lim_{n \to 0} (S_{\alpha}^2(n)/\sigma^2_\alpha) \text{ for } \alpha = u, v \text{ and } w$$

(4)

e. From theoretical considerations of kinetic energy and dissipation rate. [13]

$$L_\alpha = \sigma^3_\alpha / c \quad \alpha = u, v \text{ and } w$$

(5)

Ideally, these methods should give nearly identical results for a given data set. Most of these methods however have serious shortcomings especially when low-frequency components are present in the data sample. The first method is reasonably accurate for shear generated wind-tunnel turbulence but gives very unstable estimates of the integral length scales of atmospheric turbulence especially in the presence of low-frequency components. The integral length scales do vary considerably with the method the autocorrelation coefficient is obtained. Results show that the scales obtained with the direct method are considerably smaller than those obtained via the spectrum function (Figs. 8, 10). Moreover, length scales obtained from the cup-vane system are on the average smaller than those obtained from the hot-film instruments (Fig. 8). In the case low-frequency components are present, the logarithmic power spectrum does not have a well defined spectral peak and the second method gives unreliable scales. With low-frequency components present, the von Karman spectrum function can only be fitted adequately to the high frequency part of the measured spectra (Figs. 11-13). This requires that the velocity spectra need to be accurately measured in this range up to a frequency of at least 60 Hz for moderately strong wind conditions. Consequently, under these conditions this method can not be used with data obtained from cup or propeller anemometers. Again when low-frequency components are present, estimation of the spectral function at zero frequency gives rise to a great deal of uncertainty making the fourth method useless.
The fifth method requires knowledge of the dissipation rate $\varepsilon$, which can be obtained from the Kolmogorov's spectral law for the inertial subrange

$$S_\alpha(k_1) = K_\alpha \varepsilon^{2/3} k_1^{-5/3}$$

where $k_1$ is the wavenumber in the direction of the mean flow and is usually expressed in terms of frequency by Taylor's hypothesis as $k_1 = 2\pi n/U$. $K_\alpha$ are the Kolmogorov's constants, $K_v = K_w = 4/3 K_u$ assuming isotropy. The universal constant, $K_u$, has been established to be 0.5. In terms of the Eulerian frequency-domain the Kolmogorov's law becomes

$$n S_\alpha(n) = A_\alpha \varepsilon^{2/3} (n/U)^{-2/3}$$

where $A_u = 0.147$ and $A_v = A_w = 0.196$. Whether or not this relation can be applied to the turbulence measured at Wallops Island remains to be seen. The dissipation rate is an impossible quantity to measure independently, without making use of the local-isotropy assumption.

Assuming that the frequency version of the Kolmogorov's law applies, values of the dissipation rate $\varepsilon$ for all three velocity components have been calculated. The results indicate that the dissipation rates, obtained from each individual velocity spectrum for the same data sample, are not identical. The isotropy prediction of 4/3 for the ratios of either one of the lateral spectral values and the corresponding streamwise spectral value is clearly not satisfied in the range where the measured logarithmic spectra functions closely vary as $n^{-2/3}$. These results indicate that the existence of isotropy and the validity of Taylor's hypothesis may not apply to the turbulence encountered at Wallops Island. Until these questions are answered adequately, evaluation of the dissipation rate in the inertial subrange is unreliable, and consequently cannot be used to obtain integral length scales of the turbulence accurately.

The evaluations of these length scales from different instruments and by different methods clearly indicate that in the presence of low-frequency components, the predictions of the integral scale from ESDU [2] are much too low for the moderately strong wind conditions encountered at Wallops Island (Figs. 8-10).
Consequently, an alternate method has to be found to obtain better estimates for the integral length scales of the atmospheric turbulence. Therefore it is proposed that a scheme similar to the one used by Kaimal [14] be adopted in the field of wind engineering. When logarithmic velocity spectra normalized with the total variance are plotted against a modified frequency, $f/f_0$, all spectra for like velocity components collapse in the high-frequency range (Figs. 11-13). Here, $f$ is the reduced frequency $nz/U$ and $f_0$ is the reduced frequency at the intersection of the line of best fit in the range where the logarithmic spectrum is proportional to $n^{-2/3}$, with the line $n S_a(n)/\sigma_a^2 = 1$. For the $v$ and $w$ spectra, obtained from data without low-frequency components, a clearly discernible logarithmic spectral peak is located at $f/f_0 = 3.4$ [15]. If $f_m$ denotes the peak reduced frequency then

$$f_m^\alpha = 3.4 f_0^\alpha \quad \text{for } \alpha = v, w$$

(8)

corresponding to a value of 3.53 obtained from the $v, w$ - von Karman spectrum function. In general no clearly discernible spectral peak can be obtained from the measured $u$ spectra and therefore it is proposed to use a value for the ratio $f_m/f_0$ obtained from the von Karman spectrum function for the $u$ component

$$f_m^u = 3.85 f_0^u$$

(9)

In the case low-frequency components are present, and no clear spectral peak exists a value of $f_0$ can be obtained from the measured spectra and a corresponding value for $f_m$ can be calculated with either (8) or (9). In this case $f_m$ corresponds to a fictitious peak reduced-frequency which would have existed in the case the turbulence was purely shear-generated and low-frequency components would have been absent. A related peak wavelength can then be obtained from

$$\lambda_m = U/n_m = z/f_m$$

(10)

This peak wavelength provides a length scale characteristic of the turbulence in the frequency range corresponding to the range in which the natural frequencies of most structures such as buildings and bridges fall. It is the turbulence in this range, with wavelengths corresponding to the characteristic length of most structures, which is responsible for the dynamic response of structures and is also responsible for the positive and negative local extreme pressures present on the exterior
surface of structures. From the point of view of the engineer dealing with the modelling of the atmospheric surface flow in the wind tunnel in order to conduct wind-load model studies, it is essential that the atmospheric turbulence in this frequency range is modelled accurately. The loading effect of the low-frequency velocity components, corresponding to wavelengths larger than $\lambda_m$, can be considered as being the result of a non-steady mean flow. Consequently, it seems that this new method provides meaningful integral length scales corresponding to that part of the atmospheric turbulence which has a pronounced effect on the dynamic behavior of structures.

Figures 11-13 show the logarithmic spectra of the three turbulence components for run 19, plotted against the modified reduced frequency $f/f_0$ with the corresponding modified von Karman spectrum functions superimposed. Collapse of the spectra in the high-frequency range is of course satisfied, and the presence of low-frequency components in all three spectra is evident. The $v$ spectra show a somewhat different shape between the high- and low-frequency range quite similar to the $v$ spectra obtained at Minnesota [6]. Kaimal [6] explains this odd spectral shape to be a transition between the high-frequency range (inertial subrange) corresponding to the $w$-spectrum and the low-frequency range corresponding to the $u$ spectrum.

The distributions of averaged values of $\lambda_m$ with height for the three velocity components are shown in figure 14. Because of a great deal of variation in atmospheric conditions and of non-uniformity in upstream surface conditions, resulting in appreciable scatter of the data, it is clear that under these circumstances no simple normalization scheme is available. The values of $\lambda_m$ obtained over extremely uniform terrain [5] and under uniform convective conditions show a systematic behavior when plotted in dimensionless form using the height of the boundary layer, $z_i$, as characteristic length scale.

The advantage of the use of peak wavelength over the traditional integral length scale is that uncertainties due to sample rate variations and method of analysis are being eliminated. If the spectral functions and the standard deviations (including the low-frequency components) of the three velocity components
can be determined accurately only then a reliable estimate of the peak wavelength can be obtained. That these peak wave lengths vary a great deal with atmospheric conditions, time of day and variations in upstream surface conditions is a matter that needs further investigation.

Conclusions

The results from this research clearly indicate that under moderately strong wind conditions from directions varying between north and west, the turbulence in the surface flow below 76 m at Wallops Island is not all of mechanical origin. In addition to the shear-generated turbulence, there exist low-frequency velocity fluctuations apparently due to the entrainment of turbulent momentum into the PBL across the lowest inversion.

The flow is certainly not neutrally stratified although bulk-Richardson numbers are relatively small. However, as a result of a stretch of 3-5 km wet tidal swamp just upstream of the tower location, the vertical surface heat flux is being interrupted and warm air which has entered the PBL from the free atmosphere is allowed to penetrate downward against the temperature gradient to within 9 m above the surface.

Consequently, the mean flow and the turbulent flow in this layer cannot be normalized with the usual surface-layer parameters. The flow encountered below 76 m at Wallops Island compares in many aspects quite well with the flow measured at the uniform Minnesota site [4, 5, 6]. However, as the result of the north west wind passing twice from land to water and back to land before reaching the Wallops Island tower, the vertical heat flux is being interrupted giving rise to modifications of the flow. No simple similarity scheme is available at the present time to describe this type of flow, even if the wind conditions can be classified as moderately strong.

The following general conclusions can be made for the daytime flow below 76 m over relatively open terrain with extended areas of water upstream, under moderately strong wind conditions occurring after the passage of a cold front:

1. The height of application of the log-law is limited, transition from this velocity profile to the uniform profile in the mixed layer starts occasionally
below 76 m.

2. The air in this layer is not neutrally stratified. As a result of reduced vertical convective heat flux, warm air from the free atmosphere is transported downward against the temperature gradient.

3. The turbulence in this layer is not all of mechanical origin. Low-frequency velocity fluctuations in all three components are present as a result of entrainment of turbulent momentum from the free atmosphere across the lowest inversion layer.

4. Under these conditions the turbulence intensities except for the lateral component can be estimated quite well from ESDU, 1974 [2]. Measured values of $\sigma_v/U$ are consistently higher than those predicted by ESDU, 1974 [2].

5. In the presence of low-frequency fluctuations, traditional integral length scales of the turbulence are much larger than those predicted by ESDU, 1974 [2].

6. Measured integral scales vary a great deal with instrumentation and type of analysis.

7. Instead of the traditional integral length scale, it is proposed that the peak wavelength, $\lambda_m$, be used as a measure of the characteristic length scale of the energy-containing eddies. The peak wavelength can be obtained from the reduced frequency, $f_o$, at the intersection of a line of best fit through the $n^{-2/3}$-region of the logarithmic spectrum and the line $S_{\alpha}(n)/\sigma_{\alpha}^2 = 1$.

8. With low-frequency fluctuations present the von Karman spectrum function does not fit the spectral data in the low-frequency range.

9. In the case an independent method is used for the determination of the integral length scale, the von Karman spectrum function does not fit the spectral data in the high-frequency range either.

10. Velocity spectra normalized with the reduced frequency, $f_o$, collapse to a single curve in the $n^{-2/3}$ region. The von Karman spectrum functions, modified in the same manner, fit the data well in the high-frequency range.

11. The measured spectra of the v-component show a transition between the high and the low frequency ranges similar to the spectra obtained at Minnesota [6]. This
transition is not predicted by the von Karman spectrum function for this component.

12. In this layer the peak wavelengths, obtained from the reduced frequency \( f_0 \), vary linearly with height.

Acknowledgements

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References


### Table 1: Strong Wind Runs, Cup-Vane Instruments

<table>
<thead>
<tr>
<th>Run</th>
<th>φ (deg)</th>
<th>U (m/sec) at z=15.2m</th>
<th>( \sqrt{\frac{U^2}{U_o^2}} ) at z=15.2m</th>
<th>( \frac{L}{U_o} ) at z=76.2m</th>
<th>U_o (m/sec)</th>
<th>z_o (m)</th>
<th>α</th>
<th>Ri at z=15.2m</th>
<th>Type of Profile</th>
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<td>303</td>
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<td>0.019</td>
<td>0.131</td>
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<td>S</td>
<td>2-25-'77</td>
<td>12:37-13:45</td>
</tr>
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<td>158D</td>
<td>58.0</td>
<td>12.9</td>
<td>3.10</td>
<td>219</td>
<td>0.84</td>
<td>0.020</td>
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<td>14:02-15:02</td>
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<td>158E</td>
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<td>2.84</td>
<td>201</td>
<td>0.77</td>
<td>0.037</td>
<td>0.146</td>
<td>-0.023</td>
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<td>15:02-15:53</td>
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<td>108.3</td>
<td>13.3</td>
<td>2.98</td>
<td>393</td>
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<td>0.031</td>
<td>0.146</td>
<td>-0.027</td>
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<td>12-21-'76</td>
<td>12:22-13:39</td>
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<tr>
<td>153C</td>
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<td>3.15</td>
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<td>0.031</td>
<td>0.146</td>
<td>-0.028</td>
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<td>12-21-'76</td>
<td>14:30-15:38</td>
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<tr>
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<td>0.85</td>
<td>0.031</td>
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<td>12-21-'76</td>
<td>11:14-12:13</td>
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<td>11.4</td>
<td>2.50</td>
<td>342</td>
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<td>0.052</td>
<td>0.157</td>
<td>-0.053</td>
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<tr>
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<td>639</td>
<td>0.73</td>
<td>0.034</td>
<td>0.150</td>
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<td>3-25-'77</td>
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<tr>
<td>128G</td>
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<td>16.8</td>
<td>2.80</td>
<td>191</td>
<td>1.04</td>
<td>0.033</td>
<td>0.136</td>
<td>-0.016</td>
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<td>8-9-'76</td>
<td>17:07-18:07</td>
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<td>128H</td>
<td>136.6</td>
<td>13.9</td>
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<td>9:58-10:58</td>
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<td>0.073</td>
<td>0.173</td>
<td>-0.029</td>
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<td>3-31-'77</td>
<td>13:27-14:27</td>
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<td>209</td>
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<td>0.040</td>
<td>0.160</td>
<td>-0.082</td>
<td>Two</td>
<td>8-9-'76</td>
<td>15:08-16:25</td>
</tr>
</tbody>
</table>

### Table 2: Strong Wind Runs, Hot-Film Anemometers

<table>
<thead>
<tr>
<th>Run</th>
<th>φ (deg)</th>
<th>U (m/sec) at z=15.2m</th>
<th>( \sqrt{\frac{U^2}{U_o^2}} ) at z=15.2m</th>
<th>( \frac{L}{U_o} ) at z=76.2m</th>
<th>U_o (m/sec)</th>
<th>z_o (m)</th>
<th>α</th>
<th>Ri at z=15.2m</th>
<th>Type of Profile</th>
<th>Date</th>
<th>Time EST or EDT</th>
</tr>
</thead>
<tbody>
<tr>
<td>15</td>
<td>114</td>
<td>13.0</td>
<td>2.38</td>
<td>433</td>
<td>0.92</td>
<td>0.082</td>
<td>0.20</td>
<td>-0.039</td>
<td>K</td>
<td>3-23-'77</td>
<td>15:20-16:15</td>
</tr>
<tr>
<td>14</td>
<td>116</td>
<td>12.0</td>
<td>2.79</td>
<td>426</td>
<td>0.85</td>
<td>0.070</td>
<td>0.17</td>
<td>-0.040</td>
<td>K</td>
<td>3-23-'77</td>
<td>13:30-14:25</td>
</tr>
<tr>
<td>19</td>
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<td>11.6</td>
<td>2.57</td>
<td>306</td>
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<td>3-25-'77</td>
<td>14:21-15:16</td>
</tr>
<tr>
<td>17</td>
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<td>12.5</td>
<td>2.61</td>
<td>541</td>
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<td>0.049</td>
<td>0.15</td>
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<td>3-24-'77</td>
<td>12:27-13:22</td>
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<td>3-23-'77</td>
<td>20:30-21:25</td>
</tr>
</tbody>
</table>

Note: Runs 128 taken during passage of hurricane "Belle".
Type of Profile: S-single logarithmic profile, K-kink in profile.
Fig. 1 Typical strong wind velocity profiles, logarithmic representation.

Fig. 2 Typical strong wind velocity profiles, power law representation.
Fig. 3 Variation of power law exponent with roughness length.

Fig. 4 Averaged turbulence intensity, streamwise component.
Fig. 5 Averaged turbulence intensity, lateral component.

Fig. 6 Averaged turbulence intensity, vertical component.
Fig. 7 Records of velocity components.

RECORD OF STREAMWISE VELOCITY COMPONENT,
RUN 19, 250 ft.-LEVEL, $U=13.9$ m/sec, $\sigma_u=1.60$ m/sec,
3-25-'77, 14:21:00, $L_U=306$ m

RECORD OF LATERAL VELOCITY COMPONENT,
RUN 19, 250 ft.-LEVEL, $\sigma_v=1.65$ m/sec, $L_V=479$ m

RECORD OF STREAMWISE VELOCITY COMPONENT,
RUN 16, 250 ft.-LEVEL, $U=11.4$ m/sec, $\sigma_u=0.81$ m/sec,
3-23-'77, 20:30:00, $L_U=77.9$ m

RECORD OF LATERAL VELOCITY COMPONENT,
RUN 16, 250 ft.-LEVEL, $\sigma_v=0.62$ m/sec, $L_V=23.3$ m
Fig. 8 Variation of turbulence integral scale, $L_u^x$, with height.

Fig. 9 Variation of turbulence integral scale, $L_v^x$, with height.
Fig. 10 Variation of turbulence integral scale, $L_w$, with height.

Fig. 11 Normalized logarithmic spectra of $u$. 
Fig. 14 Averaged peak wave lengths for u, v and w.
THE STRUCTURE OF MODERATELY STRONG WINDS AT A MID-ATLANTIC COASTAL SITE (BELOW 75m)

H. W. TIELEMAN and S. E. MULLINS
Virginia Polytechnic Institute and State University, Blacksburg, Virginia, USA

ABSTRACT
Velocity and temperature measurements were obtained from an instrumented 76-meter meteorological tower located near the Atlantic Ocean at Wallops Island, Virginia. The instrumentation consists of a slow-response cup-vane and resistance temperature (profile) system and a hot-film, thermocouple system for turbulence measurements. Results are presented for moderately strong winds from westerly directions (category I) and for on-shore winds from southerly directions (category II).

Results from category I winds indicate the presence of low-frequency velocity fluctuations affecting all turbulence parameters similar to the observations made at Kansas and Minnesota.

Winds of category II experience a change in surface roughness and surface temperature as they cross the coast line, resulting in the development of an internal boundary layer (IBL). The stable ocean air above the IBL shows extremely low turbulence levels, often less than 3%. Because of the lack of turbulent mixing with adjacent layers, Coriolis effects are important and velocity profiles with a maximum velocity (low-level jet) at heights between 60-200 m exist.

INTRODUCTION
Structures and structural elements are usually designed to support the maximum loads that are likely to be imposed upon them within the lifetime of the structure. Under the strongest wind conditions the assumption of a neutrally stable planetary boundary layer (PBL) is probably satisfied. However, problems of fatigue and serviceability of a structure are often overlooked in its design. These problems can become acute under much less severe or under moderate wind conditions. Consequently, in the field of wind loading on structures and their response, one needs to study the flow in the PBL not only under extreme wind conditions but also under more common moderate conditions. Flow characteristics of the PBL under these conditions, mostly corresponding to flow over relatively homogeneous terrain have been summarized in several review papers [1,2,3,4].

These results have formed the basis for empirical models of the wind structure which are also presented in these papers and others [5,6]. Most of the proposed models, with exception of the model proposed by Panofsky [5], are limited to the following conditions: 1. Strong, stationary winds, 2. Neutral thermal stability
3. Level terrain with uniform roughness.

Upon reading of the cited references one does not always get a clear picture when neutral conditions exist. Deaves and Harris [6] do not give any conditions for neutrally stable flow other than the mean velocity has to be strong enough. Counihan [4] considers only those data which specifically indicate adiabatic or near adiabatic conditions, or which have wind speeds in excess of 5 m/s at a height of z=10m. ESDU [2,3] considers neutral stability to exist when the hourly mean wind at a height of 10 m is greater than 10 m/s. Using the gradient Richardson number Ri = (g/8)(dθ/dz)/(dU/dz)^2 as a measure for the degree of thermal stability, near neutral conditions are suggested to exist by Teunissen [1] for |Ri| < 0.03 and by Panofsky [5] for |Ri| < 0.01.

Daytime observations throughout the PBL under moderately strong wind conditions at Minnesota [7,8] indicate that the PBL consists of a surface layer, a mixed layer and an overlying inversion layer delineating the height of the PBL, z., above which the flow is relatively undisturbed by the presence of the earth’s surface (free atmosphere). The height of the PBL increases during the day as the earth surface heats up. The large-scale convective turbulence structure in the PBL interacts with the air in the free atmosphere causing the formation of an inversion through which warmer air of higher velocity and with a clockwise directional shear is entrained into the mixed layer [7,8,9]. Full-scale measurements [8], in, as well as laboratory simulation [10] of the convective PBL seem to suggest the existence of an inverted thermal plume structure throughout the PBL. These large-scale structures contribute significantly to the variances of the turbulence components down in the surface layer [8,11].

Even over the roughest surfaces and under the strongest wind conditions, the wind shear, dU/dz, decreases with height and the convective turbulence gains importance with height. The height above which the convective turbulence cannot be neglected varies with wind speed, surface roughness, time of day, and a variety of atmospheric conditions such as cloud cover, precipitation etc.

Also deviating from the neutrally stable model is an on-shore wind [12]. As the usually stable air passes a coast line, the flow is modified as a result of both a change in surface roughness and surface temperature, giving rise to the development of an internal boundary layer (IBL). Because of the lack of turbulent mixing with adjacent layers, the flow in the inversion layer above the IBL can manifest itself as a surface jet with a maximum mean velocity at a height varying between 60-200 m [12,13].

In this article mean velocity and turbulence measurements which were obtained under moderately strong wind conditions varying in direction from southwest to north (category I) and from southerly directions (category II) are described and compared with empirical relations for the PBL models as listed in the previously mentioned references.

EXPERIMENTAL DETAILS AND DATA HANDLING

Mean wind and turbulence measurements have been obtained with two types of instrumentation from the 76-meter (250 foot) meteorological tower at Wallops Island, Virginia. Wallops Island is one of the barrier islands protecting the so-called “Delmarva” peninsula from the Atlantic Ocean. The island, which consists of a narrow strip of dunes, approximately 3 meters above sea level is situated in a northeast-southwest direction and is separated from the peninsula by a tidal marsh about three kilometers wide (Fig. 1). The island is used by the National Aeronautics and Space Administration as a sounding rocket launch facility.
Profile Instrumentation

Measurements were obtained with cup-vane velocity instruments and aspirated temperature sensing probes at 5 levels mounted at 15 m (50 feet) intervals. This system is primarily used for profile measurements, the outputs are sampled once every two seconds. The data are analyzed in blocks of \(2^8 - 2^56\) samples representing a data record of 512 seconds in duration. Inspection of block means leads to the selection of stationary data samples usually six to ten blocks in length (51 to 85 min). Sample averages of velocity, direction and temperature are obtained as well as variances and covariances of the horizontal components. In addition, a 256-point autocorrelation function of the \(u\) component is calculated from which the turbulence integral scale, \(L_u\), is obtained. Data from this instrumentation system can only be analyzed in the frequency range of 0.00195 - 0.25 Hz.

Turbulence Instrumentation

Six three-dimensional split-film anemometers (TSI-1080 D) are used for turbulence measurements. These instruments are located at the same levels as the cup-vane instruments and also at the 9 m (30 foot) level. The electronics for the split-film anemometers as well as the data-acquisition system are located in an instrument trailer which is parked at the base of the tower. For a detailed description of the calibration procedures and the data-acquisition system consult references 14 and 15. The digitized data (sample rate 200 Hz) are recorded and consequently analyzed on an IBM-370 computer. Four main computer programs have been developed to calculate the following statistical parameters describing the turbulent flow: mean values, variances and covariances, spectra, cross spectra and integral scales [16].

The frequency range in which the data are analyzed is covered in three stages. The highest range (0.0244 - 100 Hz) is obtained by dividing each data record into 80 consecutive blocks of 8192 data points each. For the middle range (0.00153 - 6.25 Hz) and the lowest range (0.00031 - 1.25 Hz), the original data are subjected to a 16-point and an 80-point non-overlapping average respectively. The spectra computed from the averaged data inherently show some scatter in the low-frequency range but the agreement in the overlap regions is excellent.

RESULTS AND DISCUSSION

Terrain Description

Winds corresponding to category I (west-north) are usually encountered following the passage of a cold front and will have crossed in succession the mainland, the Chesapeake Bay (20-50 km), the "Delmarva" peninsula (20-50 km) and the tidal marsh (3 km). Depending on the direction, for the last 200-300 m the air travels over dry land before it arrives at the tower location (Fig. 1). The tidal marsh consists of shallow areas of water interchanged with swamp vegetation, mostly grass of a maximum height of 1 m. Some taller vegetation consisting of bushes and brush of a maximum height of 5 m exists in several upstream directions. For winds in the sector between 20 degrees south of west and west, a 6.5 m high rocket fuel storage bunker is approximately 85 m upstream. An elevated roadway 2 m above the surrounding terrain passes the tower on the west side with 200 m.

Southerly winds (category II) approach the tower from the Atlantic Ocean and cross the beach approximately 300 m upstream of the tower. In the southerly direction a 6 m high rocket assembly building is about 100 m upstream possibly affecting the measurements at the two lower levels. Comparison of the measurements from another meteorological tower (91-m) at Wallops Island shows that the effects on the mean
flow from a 30-m tall rocket launching tower about 300 m upstream in a direction 15 degrees west of south can be considered to be negligible.

Fig. 1. Tower location on Wallops Island and coordinate system orientation

Category I Winds

Mean Wind and Mean Temperature Profiles

For flow over homogeneous terrain under near neutral conditions, the velocity profile should obey the logarithmic law: $U = \frac{U_*}{k} \ln\left(\frac{z}{z_0}\right)$. In practical situations these conditions are seldom met and profile variations usually exist as a result of non-neutral conditions and/or non-uniform upstream terrain.

The logarithmic velocity profiles of category I winds over near-uniform terrain are either linear within the height of observation (76 m) or show two different linear segments (Fig. 2). All upper segments show a tendency towards a uniform profile. The heights of the kinks (intersection of the two linear segments) in the logarithmic velocity profiles seem to vary with the degree of thermal stability in the surface layer. However, values of the profile shear-velocity, $U_*$, obtained from the lower linear segments compare quite well with the shear velocity obtained from turbulence measurements in the surface layer. These observations were made in the stability range $Ri > -0.06$ with $Ri$ evaluated at 15 m and with the shear velocity based on the horizontal shear stress according to $U_* = \sqrt{(\omega u)^2 + (\omega v)^2}$ and analyzed in the high-frequency range (0.0244 - 100 Hz). The implications of these observations are that in this stability range, values of $z_0$ can be obtained which correspond to those obtained under neutral conditions and that the low-frequency velocity fluctuation components do not affect the velocity profile in the surface layer.

Although the scatter of the data is appreciable, profile results indicate that for the stability range $Ri > -0.15$, the average value $z_0 = 0.034$ m corresponds
The Structure of Moderately Strong Winds

Fig. 2. Typical category I logarithmic wind profiles

Fig. 3. The roughness parameter, \( z_0 \), versus \( \text{Ri} \) at \( z = 15.2 \) m for category I winds

quite well with predicted value from ESDU [2] for similar terrain (Fig. 3). For \( \text{Ri} < -0.15 \), \( z_0 \) decreases rapidly as the surface layer becomes more unstable. Figure 4 shows the variation of \( z_0 \) with wind direction, \( \phi \), for category I winds, clearly indicating the location of the bunker at \( \phi = 90^\circ \) and increased roughness for \( \phi > 170^\circ \).

Fig. 4. The roughness parameter, \( z_0 \), versus wind direction for category I winds

For non-neutral conditions the velocity profile is given by \( U = (U*/k)[\ln(z/z_0) - \psi] \), where \( \psi \) is a universal function depending on the stability parameter \( z/L \) which in turn depends on \( \text{Ri} \) [5]. Theoretically, if the velocity, \( U \), is plotted as a function of \( \ln z - \psi \), values of \( z_0 \) corresponding to neutral conditions could be obtained. This technique applied to the category I wind profiles at Wallops Island leads to large corrections resulting in unrealistic estimates of \( z_0 \).
Under moderately strong wind conditions, typical daytime temperature profiles have a maximum negative gradient near the surface and typical nighttime temperature profiles show a maximum positive gradient near the surface both decreasing in magnitude with height. During the evening and night the temperature profiles often show kinks at heights varying between 15 and 45 m. No significant variation in $z$ can be detected for daytime or nighttime data provided they fall in the stability range $-0.15 < R_i < 0.1$ with $R_i$ measured at $z = 15$ m.

Turbulent Stress and Turbulent Heat Flux

The horizontal turbulent shear, $\left[ (u^w)^2 + (v^w)^2 \right]^{1/2}$, is nearly constant throughout the height of the lower linear segment of the logarithmic velocity profile. The magnitude of the individual components vary considerably with height, although $u^w$ is consistently negative, $v^w$ has been observed to be either positive or negative. When analyzed in the middle-frequency range, the magnitude of either shear component is 25% larger in comparison with the high-frequency analysis. The local shear velocity, $U^*$, defined as the square root of the horizontal turbulent stress obtained at the lowest three observation levels and analyzed in the high-frequency range compares well with the profile friction velocity, $U^*_0$.

Daytime observations show negative values for the vertical turbulent heat flux, $w^\theta$, while the horizontal components $(u^\theta$ and $v^\theta$) are either positive or negative. The simultaneous observations of a downward turbulent heat flux and a negative temperature profile lead to the problem that the gradient Richardson numbers ($R_i$) and flux Richardson numbers ($R_f$) have opposite signs. A possible explanation for this phenomena is that category I winds experience a discontinuity in surface heat flux while crossing the Chesapeake Bay and the tidal marsh. Consequently, the downward heat flux as the result of entrainment of warmer air from the free atmosphere can be expected to penetrate deeper into the PBL giving rise to the counter-gradient heat flux.

Variances

Standard deviations of the horizontal velocity components ($\sigma_u, \sigma_v$) were obtained with the cup-vane instruments in the frequency range of 0.00125-0.25 Hz, and of all components from the hot-film probes in the middle frequency range of 0.00153-6.25 Hz. The contributions to the variances outside the middle frequency range are negligible. Because of the limited frequency response of the cup anemometers, $\sigma_v$ from the cup-vane system had to be adjusted by a factor of 1.17, which was based on comparison with $\sigma_v$ obtained from the hot-film instruments. For logarithmic velocity profiles with a kink, the average value $A_v = \sigma_v / U^* \approx 2.5$ and without a kink in the profile, the average value of $A_v = \sigma_v / U^* \approx 2.9$, measured at the 15-m level and decreasing to 2.2 and 2.7 respectively at the 76-m level. Average values of $A_v = \sigma_v / U^*$ vary from 2.5 at the 15-m level to 2.3 at the 76-m level, while the average value of $A_v = \sigma_v / U^* \approx 1.2$ is uniform over the height of observation. These results obtained near the surface are in fair agreement with the average values of these coefficients obtained from several sources [1,4 and 5] of 2.5, 2.0 and 1.2 for $A_u$, $A_v$ and $A_v$ respectively. The variances of the horizontal velocity components show a great deal of variability, and on the average the ratio $A_v$ of the lateral velocity (wind direction) at Wallops Island is larger than at other sites. Inspection of several years of strip-chart recordings of wind speed and direction obtained from a propeller-vane anemometer at Wallops Island indicates that for NW winds, the wind direction shows frequently large fluctuations towards the north, explaining the large values of $A_v$ (Fig. 5).
These recordings indicate that the fluctuations in wind direction are larger than normally encountered and moreover, are not normally distributed which explains the non-zero turbulence stress, $\tau_{vw}$.

The average turbulence intensities are in fair agreement with those suggested by ESDU [3], with the exception of the lateral turbulence intensities, $\sigma_v/U$, whose measured values are consistently higher (Fig. 6).

![Fig. 5. Typical records of wind direction and wind speed for category I winds](image)

**Velocity Spectra**

For frequencies higher than $n = 3U/z$, measured logarithmic velocity spectra vary as $n^{-2/3}$ according to the Kolmogorov's law for the inertial subrange:

$$nS_\alpha(n)/\alpha^2 = (0.27/\alpha^2) \phi c^{2/3} f^{-2/3}$$

and

$$nS_\alpha(n)/\alpha^2 = (0.36/\alpha^2) \phi c^{2/3} f^{-2/3}$$

for $\alpha = v, w$

where $f$ is the dimensionless frequency $f = nz/U$. With $\phi_c = 1$ (assuming near neutral conditions) and with values of $\Lambda_a$ based on either the local shear velocity, $U_a$, or the profile shear velocity, $U_{\text{ref}}$, the Kolmogorov spectrum functions represent the inertial subrange $u, v$ and $w$ spectra quite well for all elevations up to 76m.

For frequencies lower than $n=3U/z$, the observed, $u, v$ and $w$ spectra vary a great deal so that no simple spectrum expression seem to exist for this frequency range. Kaimal et al [17] obtained empirical spectrum formulae based on measurements in the near-neutral surface layer over smooth and homogeneous terrain. These spectrum equations represent the spectra at near-neutral conditions approached from the stable regime ($0^\circ$). The Kansas results [17] show that the near neutral spectra of the horizontal components ($u, v$) approached from the unstable regime ($0^\circ$) have much higher spectral values at low frequencies than predicted by the Kaimal spectrum expressions. The discontinuity observed in the $u, v$ spectra at
near neutral conditions does not exist for the \( w \) component, and consequently the Kaimal spectrum expression should fit all \( w \) spectra at near neutral conditions.

Consequently, for near neutral conditions, \( u, v \) spectra as well as the variances show a great variability depending on the presence of low-frequency components. The latter seem to be the result of a large-scale turbulence structure observed in the mixed layer [8] during the daytime and penetrating down into the surface layer. The near neutral \( u, v \) spectra in the \( 0^- \) category do not follow a single similarity law. In the high-frequency range the Kolmogorov law with the height \( z \) as length scale is appropriate. On the other hand in the low-frequency range the height of the mixed layer, \( z_t \), seems to be the appropriate length scale [11].

All category I daytime \( u, v \) spectra belong to the \( 0^- \) category while only one data run (run 16) taken during the early evening belongs to the \( 0^+ \) category. The difference in the near-neutral \( u \) and \( v \) spectra obtained in the surface layer and belonging to either the \( 0^- \) or the \( 0^+ \) categories is shown in figure 7, which also shows the excellent fit of the Kaimal expressions for the \( u, v \) spectra in the \( 0^+ \) category and for \( w \) spectra from either category. All the measured spectra in the surface layer and up to a height of 76m, follow the Kolmogorov law or the Kaimal expressions in the high-frequency range, although the constants often need to be adjusted. Based on these observations it cannot be automatically assumed that under moderately and possibly strong wind conditions the horizontal turbulence components give rise to spectra belonging to the \( 0^+ \) category.

Integral Scales

The longitudinal scales, \( L_x \) for \( a = u, v, w \), in the direction of the mean flow are often calculated from the normalized autocorrelation function, assuming that Taylor's hypothesis is valid. A second method for obtaining these scales is using the best fit of measured velocity spectra to the corresponding empirical von Karman spectrum functions.

Figure 8 shows the measured scales, \( L_x \), by these two methods for two different data runs. One data run (run 18) with, and a second run (run 16) without low-frequency velocity fluctuations. In the case, low-frequency velocity fluctuations are present, the von Karman spectrum functions represent the data only in the high-frequency range. Consequently, integral scales obtained with the second method are based on the turbulence in the inertial subrange, excluding the contributions of the low-frequency fluctuations which are included when integral scales are obtained from the auto-correlation function. In the case the low-frequency fluctuations are absent the two methods predict almost equal scales (Fig. 9). The ESDU [3] predicted scales for corresponding terrain fall in between the measured scales for the two different data runs.

Probability Density Function

The probability density functions of each of the velocity components are usually considered to be Gaussian in the range of \( \pm 3\sigma \) [3,4]. Careful inspection of many hours of category I wind data show large asymmetrical fluctuations in direction towards the north (Fig. 5). Measured probability density functions indicate that the fluctuations of the velocity magnitude in contrast to the direction fluctuations are usually normally distributed. This was especially observed for daytime data, while for the evening run without low-frequency fluctuations (run 16) both magnitude and direction are almost normally distributed. Several probability density functions of direction fluctuations show a secondary peak or the nucleus of a secondary peak at \(-1.5\sigma \) (Fig. 9). These peaks could be caused by a downward flow of air with a more northerly direction probably as the result of entrainment.
Fig. 7a. U- spectrum, run 16, \( z = 9.1 \) m, \( U = 6.23 \) m/sec \( \sigma_u = 0.91 \) m/sec

Kaimal [17].

Fig. 7b. V- spectrum, run 16, \( z = 9.1 \) m, \( U = 6.23 \) m/sec \( \sigma_v = 0.59 \) m/sec

Kaimal [17].

Fig. 7c. W- spectrum, run 16, \( z = 9.1 \) m, \( U = 6.23 \) m/sec \( \sigma_w = 0.53 \) m/sec

Kaimal [17].

Fig. 7d. U- spectrum, run 18, \( z = 9.1 \), \( U = 10.14 \) m/sec \( \sigma_u = 1.88 \) m/sec

Kaimal [17].
Fig. 7e. $V$-spectrum, run 18, $z=9.1$ m, $U=10.14$ m/sec $\sigma_U=1.42$ m/sec

Fig. 7f. $W$-spectrum, run 18, $z=9.1$ m, $U=10.14$ m/sec $\sigma_W=0.75$ m/sec

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Fig. 8. Integral scales obtained from the autocorrelation function (method 1) and from the von Karman spectrum function (method 2) for two runs, one with low-frequency components (run 18) and one without low-frequency components (run 16).

Fig. 9. Probability density function of the wind direction fluctuations of run 18, 76 m level, $\sigma_\theta=7.97^\circ$. Solid line represents the Gaussian distribution function.
Category II Winds

Mean Wind and Mean Temperature Profiles

The category II velocity profiles when plotted in the usual logarithmic fashion are either straight or curved opposite to the category I logarithmic profiles or show a maximum below the 76-m level (Fig. 10). The roughness lengths obtained from either the straight logarithmic profiles or from the lowest two observations of the curved profiles vary a great deal and are too high for the terrain at Wallops Island. Corrections of these profiles, in order to obtain values of $z_0$ corresponding to the terrain, as suggested by Panofsky [5] are inadequate.

The mean-temperature profiles show some unusual kinks mostly between the 30 and 45 meter levels. The most interesting sequence of mean-temperature distributions is from three runs taken on one summer afternoon (Fig. 11). The early afternoon data show a decrease in temperature up to 30 m with a rather strong positive temperature gradient at higher elevations. As the afternoon progresses this temperature gradient decreases drastically. The majority of observations show a positive temperature gradient above 30 m of varying intensity and below 30 m the temperature gradient is either positive or negative depending on the time of day and the time of year.

Turbulent Stress and Turbulent Heat Flux

The measured turbulent stress $\tau_{uw}$ has a maximum value at the 9 m level, and decreases rapidly with height. The vertical turbulent heat flux $\tau_\theta$ is positive (upward) below 30 m and is negative (downward) at this height and above, corresponding to the observed summer temperature profiles. These results indicate a dual type boundary layer within the height of observation (76 m), with unstable conditions near the surface and an overlying inversion. The unstable layer near the surface corresponds to the internal boundary layer which develops as the onshore wind is heated from below after it crosses the beach. The depth of the IBL increases with distance from the shoreline.

Variances

The standard deviations of the velocity fluctuations, $\sigma_u$, are largest in the IBL and decrease rapidly in the overlying inversion. The ratios, $\sigma_U/U^*$, are quite sensitive to stability and increase for deviations from neutral conditions in both the stable and unstable regime [12]. For near-neutral conditions in the IBL, the average values of $\sigma_u/U^*$ are 1.75, 1.5 and 1.4 for $u = u, v$ and $w$ respectively. Turbulence intensities $\sigma/U$ in the stable air above the IBL (25 m or higher) are about half of the ESDU [3] predicted values with $z_o = 0.001$ m (Fig. 12).

In the IBL with $z_o = 0.01$ m, the ESDU predictions [3] are comparable to the measurements. The hot-film data shown in Figure 12 were acquired during hot and sunny summer afternoons with mean velocities at the 76 m level varying from 6.7 m/sec to 12.7 m/sec. The cup-vane data were obtained during morning and early afternoon in the winter and early spring, with mean velocities at the 76 m level varying from 10.7 m/sec to 20.6 m/sec. For 15 of a total of 38 runs investigated, the streamwise turbulence intensity at the 76 m level is less than 3%. The lateral and vertical turbulence intensities vary in a similar fashion.

Included in Figure 12 are the turbulence intensities for run 7 obtained under extreme stable conditions ($R_f = 425.5$, $U = 10.7$ m/sec at $z=61$ m) during a sunny
Fig. 10. Typical category II logarithmic wind profiles.

Fig. 11. Temperature profiles for runs 7, 8 and 9.

Fig. 12. Variation of turbulence intensity (streamwise component) with height for category II winds.
The Structure of Moderately Strong Winds

warm afternoon in August. Under these conditions the turbulence almost disappears. During a trial run with the hot-film system under similar conditions, the turbulence disappeared completely at the two highest observation levels for at least 20 minutes. For many of the runs, a distinct clockwise rotation of a maximum of 20 degrees of the mean velocity vector with height is observed. With stable air coming from the ocean, maximum velocities at elevations below 200 m have been observed visually from exhaust trails of launched rockets and occasionally measured with the tower instruments below 76 m. (Fig. 10).

Based on these observations it can be concluded that the stable air above the IBL with low turbulence intensities and small turbulence integral scales, loses dynamic contact with the air above and below it. Little mixing and little momentum transfer takes place between the stable air and the adjacent air so that Coriolis forces become important and the stable air encounters little resistance resulting in the low-level jet.

Velocity Spectra

Measured logarithmic velocity spectra of category II winds vary as $n^{-2/3}$ in the inertial subrange and those spectra originating in the IBL belong to the $O^+$ category, varying as $n^{-1}$ in the low frequency range. However, for elevations above the IBL, low-frequency components are present in all three components. Under stable conditions, wave phenomena have been observed near the surface [13, 18] and can be recognized from the turbulence for those flows where the turbulence levels are low. Waves are not random and usually occur at a different frequency band so that a distinct spectral gap exists between the spectral peak due to the turbulence and the spectral peak at lower frequencies due to the waves.

The part of the spectra due to the turbulence in both the IBL and overlying inversion are well represented by the Kaimal expressions, although the constants in these expressions vary with stability [12]. The presence of the low-frequency waves varies a great deal with atmospheric conditions and their effect on the spectra seems to grow with height, as the fluctuations due to turbulence and wave motion fall in similar frequency bands.

Integral Scales

Integral scales obtained from the integration of the normalized autocorrelation functions vary a great deal with the presence of the low-frequency components. Values of the integral scales obtained with this method for the consecutive afternoon runs 7, 8 and 9, measured at the 76-m level, vary from 406, 162 to 56 m respectively. The wavelengths corresponding to the peak of the logarithmic spectra vary substantially with stability and height [12]. For near-neutral conditions in the IBL, the peak-wave length $\lambda^m$ equals $z/0.15$, $z/0.35$ and $z/0.15$ for $u=\nu, v$ and $w$ respectively. Normalized spectral values $n_s(n)/U^2$ evaluated at $f=10$, vary a great deal with stability [12]. Consequently, integral scales obtained from fitting of the von Karmen functions vary with stability as well.

CONCLUDING REMARKS

The wind measurements made at this eastern coastal region under sustained moderately strong wind conditions show marked deviations from observations obtained in purely shear-generated turbulent flow. For near-neutral conditions of category I (west-north) winds, low-frequency velocity and direction fluctuations influence all parameters describing the turbulence. The large direction fluctuations can have a pronounced effect on the response of tall buildings especially in the case the mean wind blows diagonally onto the building [19,20]. In wind tunnel model tests
the non-mechanically produced turbulence cannot be simulated adequately resulting in a discrepancy between model and full-scale tests [20].

For moderately on-shore winds from southerly directions, a surface based inversion is present even with the hourly mean wind speed over 20 m/sec and a maximum velocity (low-level jet) may exist at heights between 60-200 m. The turbulence intensities in the stable layer are often less than 3% and under certain atmospheric conditions the turbulence vanishes completely. Such flow could affect the response of suspension bridges located near coastal areas especially when the bridge decks are at the same height as the almost turbulence-free low-level jet.

Based on the observations made at Wallops Island under moderately strong wind conditions, the turbulence is not of purely mechanical origin. Moreover, as a result of non-homogeneous upstream surface conditions at this site, similarity theories are not applicable.

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REFERENCES


*ORIGINAL PAGE IS OF POOR QUALITY.*
ON THE WIND STRUCTURE NEAR THE SURFACE AT A MID-ATLANTIC COASTAL SITE

by

Henry W. Tieleman*

Introduction

This paper describes the mean flow and turbulence measurements made in the atmospheric surface layer up to a height of 76 m at Wallops Island, Virginia. The observations were made under moderately strong wind conditions with an hourly mean-wind velocity of at least 10 m/s at a height of 76 m. The measurements were made with cup-vane and resistance temperature sensors primarily for profile information and with hot-film and thermocouple instruments primarily for turbulence measurements. [1,2]

Site Description

Wallops Island consists of a narrow strip of dunes, approximately 3 m above sea level, and is situated in a northeast-southwest direction. The island is separated from the "Delmarva" peninsula by a tidal marsh on the west side, and with the Atlantic Ocean on the east. The terrain roughness at this site (Fig. 1) is not nearly as uniform as for other sites usually selected for ground wind experiments.

At the Wallops site, even under the strongest observed wind conditions, neutral thermal stratification has never been observed for any length of time. For most directions the atmospheric winds experience a change in surface roughness and surface temperature before the tower location is reached.

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Discussion of Results

The diabatic wind profile

\[ U = \frac{U_0^*}{K} \left[ \ln \left( \frac{z}{z_0} \right) - \frac{\psi}{L} \right] \]  

(1)
is used to determine the roughness length, \( z_0 \), and the profile friction velocity \( U_0^* \), as outlined by Panofsky [3]. Figure 2 shows the variation of roughness length, \( z_0 \), averaged for each 15° wind sector. An insufficient number of records in the wind sector 75°<\( \phi \)<195°, and upstream buildings made it impossible to get consistent results in this sector. In Figure 3 the profile friction velocity, \( U_0^* \), is compared with the friction velocity, \( U^* \), obtained from the Reynolds stresses either as \( U^* = \sqrt{\overline{w^2}} \) or \( U^* = \left[ \overline{u^2} + \overline{w^2} \right]^{1/4} \). In general the values of \( U_0^* \) are larger than those for \( U^* \). For northwesterly winds \( U_0^* \) compares reasonably well with the friction velocity, \( U^* \), based on the total horizontal Reynolds stress.

Observed values of \( \sigma_\alpha/U^* \) for \( \alpha = u, v \) and \( w \) are consistently lower than the usual near-neutral predictions of \( \sigma_u/U^* = 2.5 \), \( \sigma_v/U^* = 1.9 \) and \( \sigma_w/U^* = 1.3 \). Figure 4 shows the average ratios of standard deviations \( \sigma_v/\sigma_u \) and \( \sigma_w/\sigma_u \) for each 15° wind sector. The observations of \( \sigma_v/\sigma_u \) for wind directions parallel to the island are less than the expected value of 0.8 and for south winds and northwest winds larger than 0.8. Under convective conditions, occurring frequently during daytime for northwest winds, \( \sigma_u \) and \( \sigma_v \) are approximately equal except at the lowest observation level, but the ratios \( \sigma_w/\sigma_u \) are close to the expected value of 0.53 (Table 1). For southwest winds both ratios \( \sigma_v/\sigma_u \) and \( \sigma_w/\sigma_u \) conform closer to their respective expected values of 0.8 and 0.53.

Variations of average turbulence intensities of the horizontal velocity components obtained with the cup-vane system are shown together with their standard deviations and their extreme values for the highest
observation level (z=76.2m) in Figures 5 and 6. In the wind sectors
90°<φ<165° (on-shore winds) and 0°<φ<15° an insufficient number of
records were available and only average turbulence intensities are
shown. Note the low turbulence intensities for southerly winds usually
observed under stable conditions above the internal boundary layer. A
near constant turbulence intensity $\sigma_u / U$ of 14% is observed in the wind
sector 225°<φ<360°, in contrast with $\sigma_v / U$ which reaches a maximum value
of 14% for a wind direction of 300°. This observation is consistent
with the maximum observed value for the ratio $\sigma_v / \sigma_u$ in Figure 4 for the
same wind direction.

For near-neutral stability conditions a universal form for all $u, v$
and $w$ spectra has been proposed by Kaimal [4],

$$\frac{nS_\alpha(n)}{\sigma_\alpha^2} = \frac{0.164 f/f_0}{1+0.164(f/f_0)^{5/3}}$$

for $\alpha = u, v$ and $w$, \hspace{1cm} (2)

where $f = nz/U$ and $f_0$ is the scaling parameter which is the intercept
on the reduced frequency axis of the extrapolated inertial subrange and
the line $nS_\alpha(n)/\sigma_\alpha^2 = 1$. The von Karman spectrum functions, which are
frequently used by wind engineers may also be modified into the Kaimal
format as:

$$\frac{nS_u(n)}{\sigma_u^2} = \frac{0.156 f/f_0}{[1+0.108(f/f_0)^2]^{5/6}}$$

and

$$\frac{nS_\alpha(n)}{\sigma_\alpha^2} = \frac{0.12(f/f_0)}{[1+0.679(f/f_0)^2]^{11/6}}$$

for $\alpha = v, w$. 
The two sets of spectral functions are nearly identical except for the values of the constants, and the Kaimal spectrum is slightly flatter near the spectral peak. In the absence of low-frequency velocity fluctuations, the shape of the observed spectra of the three wind components for southerly (on-shore) winds are remarkably similar and insensitive to stability. Either the Kaimal (2) or the von Karman (3) spectrum functions fit the observed spectra extremely well (Figs. 7,8 and 9). However in the absence of low-frequency components, some of the v and w spectra observed at the lower elevations show that the Kaimal and the von Karman spectrum functions overestimate the spectral densities in the low-frequency range and that the spectral slope is larger than the predicted value of 1.0 (Fig. 10). A secondary spectral peak may develop in the spectra of all three components as the result of low-frequency internal gravity waves (Fig. 11).

For land winds from westerly directions similar observations have been made under generally stable conditions with secondary low-frequency peaks. Also, for some of the v and w spectra, the Kaimal and the von Karman spectral functions overestimate the observed spectral densities in the low frequency range, especially at the lower elevations. Under convective conditions all spectra show varying degrees of increased contribution to the spectral densities in the low-frequency range, specifically for the u and v spectra. In many cases, the w spectra show also an increase in spectral densities at lower frequencies, often increasing with height. In Figures 12 and 13 the u, v and w spectra are shown for z = 9.1 m and z = 76 m respectively in comparison with the Kaimal spectrum function (2). The results also show larger increased spectral densities in the low frequency range for the observations at z=76m than for the observation at z=9.1m.
In the high frequency range all observed logarithmic spectra vary with $n^{-2/3}$, consistent with the Kolmogorov's law for the inertial subrange. In this frequency range, the $v$ and $w$ spectra densities are to be higher than the spectral densities of the $u$ component by a factor of $4/3$ as predicted by isotropy. Nevertheless, for most observed spectra at the Wallops site under either stable or convective conditions, the $u$, $v$ and $w$ spectral densities are the same in the $-2/3$ range, especially for the observations at the lower levels. For some of the spectra observed at the higher elevations either the $v$ or the $w$ spectral values are higher, but the expected spectral ratios

$$\frac{S_v(n)}{S_u(n)} = \frac{S_w(n)}{S_u(n)} = \frac{4}{3}$$

have not been observed for any of the sets of measured spectra including those shown in Figures 12 and 13.

Conclusions

Based on the presented observations, it can be concluded that there is no simple PBL flow model available to describe the mean and turbulent flow at the Wallops site under moderately strong wind conditions. Statistical parameters describing the turbulence vary a great deal with the presence or absence of low-frequency velocity fluctuations. The atmospheric surface flow at this site does not follow the Monin-Obukhov similarity or mixed layer similarity consistently, mainly due to the nonuniformity of the surface roughness and surface temperature. Based on the measurements made at this site under the strongest observed wind conditions, there is no evidence that the PBL flow will approach the neutral boundary-layer model under extreme wind conditions.
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References


TABLE 1: Averages of $\sigma_v/\sigma_u$ and $\sigma_w/\sigma_u$ and their respective standard deviations for north-west winds and south-west winds obtained from hot-film measurements.

<table>
<thead>
<tr>
<th>$z, m$</th>
<th>$\sigma_v/\sigma_u \pm \text{St. Dev.}$</th>
<th>$\sigma_w/\sigma_u \pm \text{St. Dev.}$</th>
<th>$\sigma_v/\sigma_u \pm \text{St. Dev.}$</th>
<th>$\sigma_w/\sigma_u \pm \text{St. Dev.}$</th>
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<td>9.1</td>
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<td>0.48±0.06</td>
<td>0.70±0.06</td>
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<td>15.2</td>
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<td>30.5</td>
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<td>0.64±0.09</td>
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<td>0.62±0.09</td>
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<td>76.2</td>
<td>1.01±0.09</td>
<td>0.61±0.09</td>
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For neutral conditions without low-frequency velocity fluctuation predictions are $\sigma_v/\sigma_u = 0.8$ and $\sigma_w/\sigma_u = 0.53$. 
Fig. 2. Variation of roughness length, $z_0$, with direction.

Fig. 3. Comparison of profile friction velocity, $U^*$, and $U^* = \sqrt{\overline{u'w'}}$ (open symbols) and $U^* = [\overline{u'^2} + \overline{w'^2}]^{1/4}$ (closed symbols) evaluated at $z=15$ m.
Fig. 4. Variation of the ratios $\sigma_v/\sigma_u$ and $\sigma_w/\sigma_u$ with wind direction.

Fig. 5. Variation of turbulence intensity $\sigma_u/U$, with wind direction.
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Fig. 13. Logarithmic u, v and w spectra versus frequency, z=76 m northwest winds.
PLANETARY BOUNDARY LAYER WIND MODEL
EVALUATION AT A MID-ATLANTIC COASTAL SITE

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EXECUTIVE SUMMARY

Detailed measurements of the mean flow and turbulence have been made with the use of a micrometeorological facility consisting of an instrumented 76-m-tall tower located within a 100-m distance from the Atlantic Ocean at Wallops Island, Virginia. An interpretation of the experimental results demonstrates that under moderately strong wind conditions (hourly mean wind speed between 10 m/s and 20 m/s at a height of 10 m), the popular neutral boundary-layer flow model fails to provide an adequate description of the actual flow.

For daytime westerly winds the convective boundary layer, which has been previously observed at sites on the continent, provides an adequate model for the surface flow at the Wallops Island site. However variations from this model have been observed for certain wind directions and under certain atmospheric conditions such as low altitude cloud cover combined with precipitation. The observed low-frequency velocity fluctuations give rise to increased turbulent intensities and larger turbulence integral scales. These low-frequency fluctuations also occur in the surface layer where the observed mean velocity profiles generally fit the logarithmic law quite well.

For on-shore winds the surface flow is complicated as the result of the development of an internal boundary layer (IBL) as the air crossing the beach generally experiences a change in surface roughness and surface temperature. The internal boundary layer has a height between 15 m and 30 m at the tower location depending on wind direction and change in surface conditions. For southerly winds the warmer air
flows over the cooler water allowing the existence of a surface-based inversion of variable depth. Under these conditions a low-altitude maximum velocity (surface jet), occasionally below the highest observation level of 76 m, has been observed. Under extreme stable conditions at hourly mean velocities in excess of 10 m/s the turbulence has been observed to vanish completely. In addition, low-frequency internal gravity waves have been observed to co-exist with the turbulence.

In addition to detailed flow information for all wind directions, averages of the important flow parameters used for design such as vertical distribution of mean velocity, turbulence intensities and turbulence integral scales have been presented for wind-direction sectors with near-uniform upstream terrain. Power spectra of the three velocity components for the prevailing northwesterly and southerly winds are presented and discussed in detail.

The experimental results indicate clearly that the non-uniformity of the upstream surface conditions, the non-neutral thermal stratification and the presence of appreciable low-frequency velocity fluctuations have a pronounced effect on the surface flow. Consequently it is impossible to find a simple and single PBL model to describe the flow at this site even under moderately strong wind conditions. Moreover, there is no evidence that under still stronger wind conditions (hourly mean wind speed at z=10 m over 20 m/s) the surface flow will alter sufficiently as to conform to the neutral boundary-layer model whose turbulence is of purely mechanical origin.
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1. INTRODUCTION

The purpose of this report is to provide information on the local wind climate at a mid-Atlantic coastal site. The acquired information can be used for the design of wind-turbine generators at similar sites. Since wind is a very important design parameter for these generators, information is provided in this report on wind speed, wind direction, wind shear and wind turbulence.

The data presented in this report were collected from an instrumented meteorological tower, 76.2 m (250 feet) tall and located at Wallops Island. This island is one of the barrier islands at the Atlantic coast along the Eastern Shore of Virginia and is used by the National Aeronautics and Space Administration as a sounding rocket launch facility. The results acquired from this facility should be typical for any Atlantic coastal site, although local effects such as upstream buildings and obstacles and changes in surface roughness and surface temperature modify the flow near the surface. At Wallops Island, the surrounding terrain beyond a distance of 100-300 m from the tower can be considered as homogeneous and uniform, so that the flow above a height of approximately 10-30 m should not be affected by local terrain nonuniformities.

The wind and temperature data from this site were acquired under moderately strong wind conditions with an hourly mean velocity of at least 10 m/s at the 76.2 m (250 ft) level. For wind directions between northeast and southwest this requirement had to be reduced to approximately 8 m/s, since strong winds from this sector occur very seldom.
Mean wind and turbulence measurements were made with two types of instrumentation consisting of cup-vanes and resistance temperature probes primarily used for mean profile measurements of velocity and temperature respectively. In addition, the cup-vane instruments were used for turbulence intensities of the two horizontal velocity components and horizontal and vertical turbulence integral scales. The hot-film and thermocouple system was used for measurement of turbulence intensities, turbulence fluxes and velocity spectra in all three directions. The cup-vane system was used to acquire wind data from all directions, while the hot-film system was only used for turbulence measurements from the two prevailing wind directions, south and north-west.

The results of this experimental research are presented in a form suitable for design purposes. Where ever possible the results are also compared with previously published results and with existing empirical models for near-neutrally stratified low-level winds.

2. SITE DESCRIPTION

Wallops Island consists of a narrow strip of dunes, approximately 3 meters above sea level, and is situated in a northeast-southwest direction. The island is separated from the "Delmarva" peninsula by a tidal marsh on the west side, and with the Atlantic Ocean on the east.

Winds with directions varying between west and north are usually encountered following the passage of a cold front. Winds from this sector will have crossed in succession (Fig. 1) the mainland, the Chesapeake Bay (20-50 km), the "Delmarva" peninsula (20-50 km) and the tidal marsh (3-5 km). Depending on the wind direction, for the last
200-300 m the air travels over land before it arrives at the tower location (Fig. 2). The tidal marsh between the island and the peninsula consists of shallow areas of water interchanged with swamp vegetation, mostly grass of a maximum height of 1 m. Some taller vegetation consisting of bushes and brush of a maximum height of 5 m exists in several upstream directions. For wind directions between 255° and 270°, a 6.5 m high rocket fuel storage bunker is approximately 90 m upstream (Fig. 2). An elevated roadway (levee) 2 m above the surrounding terrain passes the tower on the west side within 200 m. Winds with directions varying between north-east and south approach the island from the Atlantic Ocean.

Sectors with approximately the same immediate upstream roughness have been established as shown in Fig. 3. Between 0° (north) and 30° the upstream terrain features two bunkers within a distance of 100 m from the tower. In addition, a few small buildings and intermittent patches of brush are upstream as far as 750 m. Between 30° and 45° (wind direction parallel to the island) many buildings are upstream and winds in this sector should encounter the roughest terrain at this site over a distance of approximately 4 km. For wind directions between 45° and 210° the winds approach the island over water, and cross the beach at varying distances from the tower depending on the direction. For wind directions between 140° and 170° a one-story rocket assembly building is about 100 m upstream of the tower. The prevailing southerly winds vary in direction between 170° and 210°, however in the sector between 195° and 210° the 45-m tall Aerobee tower and associated buildings are about 300 m upstream. For directions between 210° and 230°, the wind direction is approximately parallel to the island.
with part of the Aerobee tower complex approximately 300 m upstream. In this same sector a few other buildings, levees and sand dunes are upstream at greater distances. Between 230° and 330° the upstream terrain is very uniform with no big obstacles other than the aforementioned bunker and roadway. For the sector between 330° and 360°, several patches of brush, 2 levees and one radar building are upstream of the tower within a distance of 500 m with marsh at further upstream distances.

3. INSTRUMENTATION

3.1 Cup-Vane Instruments

The 76 m (250 ft) micrometeorological tower is a self-standing non-guyed tower with working platforms at 15.2 m (50 ft) intervals (Fig. 4). The cup-vane velocity-direction instruments and aspirated temperature probes both primarily used for profile measurements are mounted at 5 levels near each platform. Two sets of cup-vane instruments are mounted at each level on 2m booms on opposite sites of the tower (Fig. 4). An automatic electronic switching circuit ensures that data are taken only with the instruments on the upwind side of the tower. The electronics associated with this instrumentation system, together with a digital readout panel of all instruments from one side of the tower, are located in a small instrumentation building at the base of the tower (Fig. 4). From this location the digitized data are transmitted to the NASA control center at the main base on the peninsula about 13 km to the northwest. Here the data from each level sampled at a rate of 1 sample each 2 seconds are recorded on digital tape. At this sample rate, data can be acquired without interruption for about
8 hours. This instrumentation system is used by NASA in conjunction with its rocket launching operations. Regularly scheduled maintenance and calibration of this system are performed by personnel under NASA's supervision.

3.2 Hot-film Anemometers

Six three-dimensional split-film anemometers (TSI-1080D) are used for turbulence measurements, which include turbulence intensities, turbulence fluxes, spectra and cross spectra of all three turbulence components and temperature. These anemometer systems were chosen for this research program since they have the advantage of small physical size, fast response and high sensitivity over a wide range of velocities. The instruments are mounted on 1.8 m booms at the same levels as the cup-vane instruments and also at the 9 m (30 ft) level. Each hot-film probe is mounted on a rotor, which is capable of rotating the probe about a vertical axis so as to align the probe axis approximately into the mean wind direction. The probe-rotor combination is mounted on a 1.8 m-boom, which in turn is mounted on the railing at each platform. The probes were mounted on the south side of the tower for measurement of the prevailing south winds during the summer and on the north side of the tower for measurement of the prevailing northwest winds during the winter and spring. The electronics as well as the data-acquisition and data-handling system for this instrumentation system are located in an instrumentation trailer parked at the base of the tower (Fig. 4).

Each hot-film probe consists of three split-film sensors used for measurement of wind speed and direction and a copper-constantan thermocouple used for temperature measurements. Each sensor consists of a 0.15 mm diameter quartz rod coated with a platinum film of about
1000 angstrom in thickness. The platinum film on each rod consists of two segments, separated from each other by two longitudinal splits 180° apart. The active elements on each rod are electrically heated to the same constant temperature by separate anemometer circuits. The total sensor length is about 5 mm, and the three sensors are mounted mutually perpendicular to form a Cartesian coordinate system. When the instruments are not used for data acquisition, the three sensors and thermocouple are protected by an aluminum shield which can be moved pneumatically to cover the sensors. As an added precaution, dry filtered air is allowed to blow across the sensors when the shield covers the sensors. This is done to protect the sensors from contamination in the salt-air environment and moisture while not in operation. For a more detailed review of the hot-film anemometer system the reader is advised to consult Reference 1.

Calibration of the hot-film anemometers is carried out in a low-speed wind tunnel located at the main base. In order to obtain data of a desired accuracy from the hot-film instrumentation system, a new calibration and operating procedure was developed. Instead of using the calibration constants supplied by the manufacturer, all constants were obtained from calibration procedures carried out in the low-speed wind tunnel and thermal chamber. This procedure proved to be both time consuming and complicated but necessary. Calibration of each instrument in the wind tunnel was carried out for 11 wind approach angles between plus and minus 50° and for 13 velocities in a range varying between 0.3 and 15 m/s. The best accuracy of the data was obtained for wind
directions parallel to the axes of the instrument, and consequently the tower mounted instruments were rotated in the direction of the mean wind before the data acquisition was started. For details of the calibration procedure and the relations for the conversion from output voltage to velocity components it is suggested that the reader consult References 1 and 2.

4. DATA HANDLING AND DATA ANALYSIS

4.1 Cup-vane Instruments

The output signals from the cup-vane instruments and temperature sensing probes are sampled and digitized at a rate of 1 sample per second. This information is transmitted to the control center of the main base, where every other sample is recorded on digital tape. The data from these tapes, each capable of storing up to 8 hours of data, are then analyzed on the HW-625 computer at NASA, Wallops Flight Center. The data are analyzed in blocks of $2^8$=256 samples, representing a data record of 512 seconds. For each sample the east-west and north-south velocity components are calculated and averaged over 256 samples from which the mean velocity and the mean direction for each block are obtained. Also a block mean for the temperature is calculated. Reasonably stationary sample records of 5 to 10 blocks in length are selected for further analysis. This selection is based on the inspection of the printout of the block means of velocity, direction and temperature for all five levels.

Next the east-west and north-south velocity components and temperature are averaged for the selected sample, from which the sample mean velocity and sample mean direction are calculated. This direction
defines the mean-wind coordinate system with the x-axis parallel to the
direction of the sample mean wind, the y-axis in the horizontal plane
perpendicular to the x-axis and the z-axis vertically upward. For all
the data points in each block the velocity components in the mean-wind
coordinate system are calculated and averaged to obtain the block means.
After the block means were removed from each set of components, variances
and covariances are calculated for each block. Sample variances and
covariances are obtained by averaging of the block variances and covariances
over the total number of blocks. The covariances calculated in this manner
include all the combinations of like velocity components at the different
levels, allowing for the calculation of the vertical turbulence integral
scales of both the u and v components. In addition, the autocorrelation
function, \( R_u(\tau) \) of the streamwise velocity is calculated from which the
turbulence integral scale, \( L_u^x \), is obtained as follows:

\[
\frac{L_u^x}{L_u} = \frac{U}{(\sigma_u)^2} \int_0^{T_1} R_u(\tau) d\tau,
\]

where \( T_1 \) is the time delay for which the first zero-crossing of the
calculated autocorrelation function occurs. The turbulence data
acquired with the cup-vane system are analyzed in a limited frequency
range of 0.00195-0.25 Hz.

A total of 195 digital data tapes were generated during the period
of July 1974 and December 1978. Approximately 300 data samples were
analyzed each varying between 43 and 85 minutes. Initially data were acquired with the cup-vane system only, it was not until February 1976 that the temperature system came on line. However this system is not too reliable and often temperature at one or two levels is missing as the result of the equipment being down or out of calibration. Before a lightning-arrester system was installed on the tower, excessive amount of damage was inflicted on all systems during thunderstorms as a result of line power surges and voltage induction in the cables that connect the instruments on the tower to the electronics at the base of the tower. During the summer of 1976 a thermograph for recording the air temperature at ground level was added to the system.

Occasionally when the equipment on the 76m (250 ft) tower was down, data-acquisition was switched to the 91 m (300 ft) tower located at the north end of the island. This tower is instrumented with cup-vane systems at six levels but has no temperature instruments. Its location from the beach is 280 m as compared to the 76 m (250 ft) tower which is approximately 150 m from the beach. No major buildings or other obstacles exist between the 91 m (300 ft) tower and the beach. However, for ocean winds the overland distance is longer and more modification of the undisturbed ocean winds can be expected at the 91 m (300 ft) tower.

4.2 Hot-film Anemometers

The data-acquisition and data-handling system is designed to handle output from six split-film anemometer systems, sampled at a rate of 200 samples per second for a period of approximately one hour. This system consists of two main parts: (a) the multiplexing and analog recording system and (b) the demultiplexing, digitizing and
digital recording system. The seven output voltages from each anemometer are frequency modulated by voltage-controlled oscillators each with a different center frequency. There is one set of voltage-controlled oscillators for each probe. The seven frequency-modulated signals together with a 100 kHz reference signal are fed into a summing amplifier to produce one single multiplexed signal. The multiplexed signals from each instrument are recorded on separate channels of an analog tape recorder together with time-of-day, which serves as a reference for the recorded data.

At a later time, each of the multiplexed signals is demultiplexed into its seven analog components after passage through seven discriminators. In order to avoid aliasing of the velocity spectra the six output voltages corresponding to the six split films are passed through a 100 Hz low-pass filter. Next the analog voltages are sampled at a rate of 200 Hz, digitized and recorded on digital tape.

A mini-computer (DEC Model PDP 11/20) controls the multiplexing analog-to-digital conversion and the digital recording. Access to the mini-computer is obtained with a teletypewriter. The data conversion starts at a time-of-day prescribed by the operator, and the analog-to-digital converter performs successive scans and conversions of seven analog voltages into 16 bit words at a rate of one scan each 5 milliseconds. These words are stored in one of the buffers of the mini-computer which in turn transfers the data to a 9-track digital magnetic tape. Each buffer has a capacity of 209 scans representing 1.05 seconds of data. A total of 3300 records make up a single sample record over a time period of slightly less than one hour. The tapes with the digitized
data are taken to VPI and SU where the data are analyzed on an IBM-370 computer. Four separate computer programs have been developed to calculate the following major statistical parameters: mean values, variances, covariance spectra and cross spectra.

The first step in the data-analysis procedure is to convert the seven output voltages from each film to three velocity components in the sensor-oriented coordinate system and temperature, using the constants obtained from the calibration data. The converted data are transferred on another magnetic tape to await the next step of the data reduction.

In the second program velocity and temperature data are analyzed in blocks of \( N = 2^{13} = 8192 \) data points, representing nearly 41 seconds of data. For each of these blocks of data mean velocity components, mean velocity and direction, mean temperature and the four standard deviations are calculated. A total of 80 data blocks (almost 55 minutes) are analyzed in this manner. A stationarity trend test is performed on each of the calculated parameters to check for unacceptable nonstationarities. Also inspection of the printout of the block parameters helps in the decision whether or not to continue with the statistical analysis. At this point blocks with unrealistic data can be recognized and omitted from the data sample in future analysis. The sample mean velocity components are obtained by averaging the block means, allowing the calculation of the horizontal angle between the sample mean-wind direction and the probe axis. In the following step this angle is needed to transfer the original velocity components in the sensor-oriented coordinate system into \( u, v \) and \( w \) velocity components of the mean-wind coordinate system as defined previously.
Block means are calculated for the temperature and for the velocity components in the mean-wind coordinates system and removed from the data in each block. The resulting fluctuating components are recorded on magnetic tape for further analysis. Also variances and all covariances for each block are calculated and averaged over 80 blocks to obtain the sample variances and covariances. The statistical parameters, including the spectra to be calculated in the next step, contain only contributions from the fluctuations in the frequency range of 0.0244-100 Hz. In order to include contributions from frequencies below 0.0244 Hz, sixteen consecutive data points are averaged into one data point to form a new data record, which is also recorded on magnetic tape. This averaging is performed after the data are transformed into the mean-wind coordinates and before the block means are removed. In this way only 5 blocks, each 10.92 minutes long, are analyzed allowing for data analysis in the frequency range of 0.00153-6.25 Hz. For these new data records, block variances and covariances and sample variances and covariances are also calculated. For the lowest frequency range the data, after transformation into the mean-wind coordinates, are subjected to an 80-point non-overlapping averaging for analysis in the frequency range between 0.00031-1.25 Hz.

The last step of the data analysis is the spectral analysis of the high, middle and low frequency data in the frequency range of 0.0244-100 Hz, 0.00153-6.25 Hz and 0.00031-1.25 Hz respectively. Spectral estimates are calculated for each block using a specially developed Fast Fourier Transform algorithm [4]. The combined averaging technique is employed, averaging first all the block estimates at a given frequency (ensemble averaging) and then averaging these results
over appropriate frequency intervals (frequency averaging).

In total, 24 one-hour data records were generated with the hot-film system. Nine runs were generated during warm summer afternoons of the year 1976. This set of data was acquired for southerly winds only, and the detailed results are presented in Reference 3. The remaining 15 runs were acquired during the spring of 1977 for winds of northwesterly direction. For some of these data records, data were acquired simultaneously with the cup-vane system.

The hot-film system is extremely delicate. Lightning and powerline fluctuations have often caused difficulties with the operation of the system. It is very seldom that the entire system is fully operational at one particular time. The hot-films also have a tendency to undergo resistance shifts. If an appreciable shift is detected, the probes are recalibrated. Corrections have to be made for changes in cable resistance due to changes in ambient temperature. Similarly, heat transfer corrections have to be made for changes in temperature. Because of the uncertainties in these corrections and other variations, the mean velocity and mean temperature measured with this system are not reliable. Resistance shifts in the active part of the system (films and cables) result in a parallel shift of the heat transfer (voltage)/velocity calibration curve. This shift of course will affect the mean quantities a great deal but should not affect the calculated turbulence quantities as much. As pointed out in Reference 5, the results from these instruments become less accurate for wind directions of +40° and +90° with respect to the probe axis. Consequently, the probes are rotated in the direction of the mean wind prior to data acquisition. For southerly winds this is no problem
since these winds especially at the higher elevations are very steady and have low turbulence levels. For northwest winds, the alignment with the mean wind is more of a problem because of the presence of long-period fluctuations in direction. Precautions were made as much as possible to ensure that data of the highest quality were acquired, and it is believed that the measured turbulence quantities fall within an accuracy level of less than 10%.

5. PLANETARY BOUNDARY LAYER (PBL)

The planetary boundary layer (PBL) may be defined as that part of the atmosphere where the effect of the earth's surface is directly felt. The flow structure of the boundary layer is extremely complex due to the variability of surface roughness changes in terrain, changes in surface temperature, variability of water vapor, presence of clouds and the fact that the flow is turbulent. Consequently, a simple model describing all the variables in the PBL such as velocity, wind direction, temperature and humidity, and covering all possible conditions is still not available.

The unstable or convective PBL is characterized by a strong upward heat flux from the surface and by strong vertical mixing due to positive buoyancy forces. Under these conditions above the surface layer, a well-mixed layer exists with an almost uniform potential temperature and an almost constant wind speed and direction. Due to the convective mixing a relatively sharp inversion is created on top of the mixed layer that delineates the depth of the PBL. Above this inversion the atmosphere is relatively undisturbed by the presence of the earth's surface and only gravity waves are generated. During the course of a sunny day
the convective PBL increases in depth as the land surface heats up and extends up to the inversion layer, which is the result of the convective mixing of unstable air below with warmer stable air above. Under these conditions the convective PBL can be characterized by three different layers, which are, starting from the earth's surface:

1) a surface layer, 2) a mixed layer, and 3) a capping inversion. The existence of this model for the convective PBL is based on theoretical considerations [6], numerical flow modeling [7,8,9,10], laboratory flow modeling [11] and actual observations [12,13,14].

In the case a layer of stable air is present at the surface, and/or one or more stable layers exist at higher altitudes, no capping inversion exists. In stable air, turbulence is suppressed and may vanish completely under extremely stable conditions, and the air in the different layers becomes uncoupled as a result of reduced mechanical mixing. No simple model is available to describe this situation. A surface-based inversion with or without one or more stable layers at higher elevations has been observed over water surfaces, as warm air flows over the cooler water during either day or night [3,18]. Under these conditions a low-level wind maximum (surface jet) is usually observed and the interpretation of the wind fluctuations near the surface is often complicated as a result of the co-existence of turbulence and internal gravity waves. These two phenomena have quite different properties although a non-linear interaction may exist between them.

More complications are introduced in the flow analysis of the PBL when clouds are present and condensation of water vapor occurs within the PBL. As condensation takes place in the layer where the clouds are located, latent heat is released and an inversion layer develops below
the cloud base that is responsible for some degree of suppression of the turbulence. Under these conditions the large-scale plume structure, normally present in the convective PBL, does not develop resulting in a considerable suppression and reduction in low-frequency velocity fluctuations. This phenomenon in turn results in reduced velocity variances and an increased roll-off in the low-frequency range of the spectra of the horizontal velocity components.

Just above the earth’s surface the shear-production of turbulence dominates the buoyant production or suppression of turbulence. However the importance of the shear-produced turbulence diminishes with height as the effect of buoyancy on the turbulence gains importance. In the layer just above the earth’s surface where shear-produced turbulence dominates and the Reynolds stress is nearly constant, the velocity is adequately expressed by the well-known logarithmic law, provided the roughness of the terrain is uniform. As buoyant production or buoyant suppression of turbulence gains importance with height relative to shear production, modification of the logarithmic velocity profile will result.

The buoyant production of turbulence is associated with the upward heat flux of sensible and latent heat, which usually occurs when the atmosphere near the earth’s surface is unstably stratified \( \frac{d\theta}{dz} < 0 \). The buoyant suppression of turbulence is associated with the downward heat flux which usually occurs when the atmosphere is stably stratified \( \frac{d\theta}{dz} > 0 \), where \( \theta \) is the local potential temperature.

Under strong-wind conditions on a sunny day, the layer in which the shear-produced turbulence dominates increases in height, and the logarithmic velocity profile exists to higher elevations before it is eventually
modified as a result of convective activity, even under the strongest wind conditions.

Following this discussion of the PBL, it is unlikely that its flow characteristics are based exclusively on mechanically or shear-produced turbulence. Experimental results describing the mean flow and turbulence in the PBL, under a variety of stability conditions ranging from unstable via near-neutral to stable conditions, clearly indicate that some basic differences exist between the PBL and the typical zero-pressure gradient wind-tunnel boundary layer. The most noticeable differences are observed in the evolving convective PBL on a sunny day with the mixed layer occupying about 90% of the height and the surface layer consisting of the lower 10% of the PBL. In the mixed layer the velocity and wind direction are practically uniform [12,13]. Also, the downward entrainment of heat and momentum at the base of the capping inversion is a phenomenon that makes the assumption of vanishing turbulence at the edge of the boundary layer untenable [12,13,14].

The entrainment of heat and momentum of different magnitude and direction into the mixed layer is mainly responsible for the low-frequency fluctuations observed in the horizontal velocity components down to near ground level [19,20]. These low-frequency fluctuations are not present under stable conditions, although as mentioned before, low-frequency fluctuations associated with gravity waves have been observed under stable conditions [15,18].

An abrupt discontinuity (increase) in low-frequency content has been observed in the spectra of the horizontal velocity components as the thermal stratification changes from stable to unstable [19,20].
Similarly, the variances of the $u$ and $v$ velocity components and the reduced peak frequencies of these spectra increase abruptly as the stratification changes from stable to unstable. These abrupt changes have been observed in the horizontal velocity components $u$ and $v$ only, and do not occur in the vertical velocity component $w$. Experimental evidence of the abrupt increase in variance of the $u$ velocity component and of the total velocity variance as the flow changes from slightly stable to slightly unstable is clearly presented by Busch [21]. For slightly stable stratifications the ratio of the standard deviations of the vertical and longitudinal velocities $\sigma_w/\sigma_u = 0.36$ and for slightly unstable stratifications this ratio is reduced to 0.25.

It has been observed that shortly before sunset the convective boundary layer disintegrates suddenly in a matter of minutes as a surface-based inversion begins to develop [22,23]. During the night (or when there is a heavy cloud cover and water-vapor condensation in the PBL) the large-scale turbulence structure of the convective PBL is suppressed and no low-frequency components are present in the $u$ and $v$ velocity spectra near the earth's surface.

Some of the experimental evidence, used previously in support of the flow description of the PBL, was obtained under relatively strong wind conditions. For example, during the Minnesota experiment [12] two data records (2A1 and 2A2) were acquired each with an hourly mean velocity of approximately 10 m/s at a height of 10 m. For these two data records the mean velocity is practically uniform above 60 m, which is typical for the mixed layer. Also the standard deviations
of the three velocity components do not change appreciably with elevation up to an elevation of 1220 m, indicating that there is little evidence of vanishing turbulence at the edge of the PBL. In addition, the horizontal turbulence stresses $\overline{uw}$ and $\overline{vw}$ exhibit minima near the surface and a considerable upward heat flux is observed up to the top of the mixed layer where the heat flux changes direction due to entrainment of warm air at the base of the capping inversion. The gradient-Richardson numbers for these two records of Reference 12 are approximately $-0.30$ and $-0.46$ respectively, which excludes these records from the near-neutral stability category.

In another example, extremely strong winds with mean velocities up to 28 m/s have been observed at 10 m heights over water [24]. The turbulence intensities of the $u$ and $v$ components show an abrupt increase for mean velocities in excess of 12 m/s ($\sigma_u/U$ from 3% to 15%, $\sigma_v/U$ from 8% to 11.5% and $\sigma_w/U$ remains constant at 5%). There is strong evidence that helical vortices, which form over the ocean under near-neutral conditions, are responsible for this increase in turbulence intensity of the horizontal velocity components. Also nocturnal jets near the earth's surface with a jet velocity of approximately 20 m/s and a gradient Richardson number of +0.5 have been observed in Nebraska [16].

Based on these examples and other experimental evidence presented in the cited references, there is no basis for the assumptions that under strong wind conditions the turbulence in the PBL is purely of mechanical origin and that the PBL flow-structure is similar to that of a zero-pressure gradient wind-tunnel boundary layer with vanishing turbulence at the free stream.
For the benefit of structural engineers and wind engineers who deal with a large number of problems requiring the knowledge of the mean flow and turbulence in the atmosphere, the atmospheric flow characteristics near the earth's surface under strong wind conditions have been reviewed and summarized in several review papers [References 25 through 31]. The input data to most of these review papers were obtained from many different sources and include multi-level tower data and airplane data usually taken over horizontal terrain with near-uniform roughness. The results from these strong-wind experiments have formed the basis for empirical models of the wind structure near the earth's surface and of the atmospheric flows at higher elevations. In many of the review papers it is assumed that under strong wind conditions the turbulence is purely mechanically generated, and that buoyant production and suppression of the turbulence can be neglected. Under these conditions it is then assumed that the atmosphere is neutrally stable and the mean and turbulent flow behave similar to the flow in a zero-pressure gradient turbulent boundary layer developed in a low-speed wind tunnel.

The review papers generally indicate that the PBL under strong wind conditions is neutrally stable but may be modified as the result of thermal effects. However, it is generally assumed that under strong wind conditions there is sufficient mixing that thermal effects can be completely ignored. The neutrally stable PBL-flow model, which is generally assumed in the review papers, has never been experimentally verified at different sites for a large variety of strong wind conditions. Nevertheless, it is widely assumed by many engineers and
scientists in the field on wind engineering that this model provides an adequate description of the flow in the PBL under strong wind conditions.

Upon reading of the review papers one does not always get a clear picture when neutral conditions exist. Deaves and Harris [30] do not give any conditions for the existence of neutrally stable flow in the PBL other than the mean velocity has to be strong enough. Counihan [26] considers only those data which specifically indicate adiabatic or near adiabatic conditions, or which have wind speeds in excess of 5 m/s at a height of z = 10 m. ESDU [27,28,29] considers neutral stability to exist when the hourly mean wind at a height of 10 m is greater than 10 m/s. Using the gradient Richardson number as a measure for the degree of thermal stability in the PBL, near-neutral conditions are suggested to exist by Teunissen [25] for $|\text{Ri}| < 0.03$ and by Panofsky [31] for $|\text{Ri}| < 0.01$ for flow near the surface.

Panofsky [31] also states that wind shear, and therefore mechanical production of turbulence, decreases rapidly with height and that the effect of buoyancy becomes progressively more important. Consequently thermal effects can no longer be neglected even under strong wind conditions for heights above approximately 50 m.

Most of the observations at Wallops Island presented in this report have been made with the mean wind speed at the 76 m (250 ft) level between 10 m/s and 20 m/s and therefore can be considered to belong to the strong-wind category. However the results of these observations will be presented and discussed in the framework of non-neutral PBL-flow.
6. RESULTS AND DISCUSSION

This chapter deals with the discussion of the mean flow and turbulence measurements obtained with the two instrumentation systems mounted on the 76 m (250 ft) meteorological tower at Wallops Island, Virginia.

Data were acquired with the cup-vane and resistance temperature probes during a period of more than 4 years (August 1974 - December 1978). Most of these data records were taken during daytime, although some night records are included. The prevailing wind directions at this site are southerly during the summer and fall, and between west and north during winter and spring. Consequently, for these two direction sectors many data records are available but the data base for on-shore winds in the sector between northwest and south is limited. For this set of data, mean velocity $U$, mean direction $\phi$, mean temperature $T$, the turbulence variances $\sigma_u$ and $\sigma_v^*$, and the turbulence integral scales $L_x$, $L_y$, $L_z$ were obtained for each data record, based on the measurements from 5 levels at 15.3 m (50 ft) intervals on the 76 m (250 ft) tower.

A second set of data was taken with the hot-film instrument system. Nine data records, each one hour long and for southerly wind directions, were acquired during 3 days in July and August of 1976 [3]. In addition 14 data records for winds from northwesterly directions were acquired during several days in March, May and June of 1977 [23].

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*The symbol $\sigma$ refers to the standard deviation, but for simplicity the word variance will be used in the text.*
For these data records the following parameters were obtained: variances and covariances of the three turbulence components and temperature, spectra and cospectra, and longitudinal integral scales $L_u^x$, $L_v^x$ and $L_w^x$, all measured at the same levels as the cup-vane instruments and at 9.1 m (30 ft). For some of these records data were acquired simultaneously with the cup-vane system, allowing direct comparison of the measurements with the two instrument systems.

6.1 Mean Wind and Mean Temperature Profiles

For near-neutral stratification the wind profiles over homogeneous terrain obeys the relation

$$ U = \frac{U_0^*}{K} \ln\left(\frac{z}{z_o}\right) $$

(2)

where $U_0^*$ is the friction or shear velocity, which is ideally equal to $\sqrt{\tau_o/\rho}$, where $\tau_o$ is the surface stress and $\rho$ the air density, $K$ is Von Karman's constant taken at 0.4 and $z_o$ is the roughness length. The height $z$ below which the log-law (2) is valid depends on the stability of the flow or on the relative importance of the buoyant production or suppression of the turbulence with respect to the mechanically produced turbulence. The height where the measured velocity profile starts to deviate from the logarithmic profile varies a great deal and the deviation increases progressively for increasing heights. Under strong convective conditions and under extreme stable conditions the near neutral part of the surface layer is well below 15.2 m (50 ft), the height of the lowest mean-velocity measurement. Consequently under these conditions it is incorrect to fit the log-law (2) to the measured mean-velocity data in order to obtain values of $z_o$ and $U_0^*$. 
The theoretical velocity profile over uniform terrain for the upper part of the surface layer where non-neutral stratification exists, is based on the Monin-Obukhov similarity theory and is given by [32]

\[ U = \frac{U_0^*}{U} \[ \ln\left(\frac{z}{z_0} - \psi\right) \]  

(3)

where \( \psi \) is a universal function of the stability parameter \( z/L \) and \( L \) is the Monin-Obukhov length defined (in the absence of moisture) as [32]

\[ L = \frac{c_p 0 \theta}{K g Q_0} \]  

(4)

where \( T \) is the absolute temperature, \( U^* = \sqrt{\frac{T_0}{\rho}} \) and \( Q_0 \) is the surface heat flux, which can be approximated by \( c_p \rho \bar{w} \theta \) measured in the surface layer. The stability parameter, \( z/L \), depends on the gradient Richardson number [32]

\[ Ri = \frac{g \gamma_a + dT/dz}{T (dU/dz)^2} \]  

(5)

where \( \gamma_a \) is the adiabatic lapse rate (0.01°C/m for dry air and 0.0065°C/m for air saturated with moisture). With the use of the expressions relating \( Ri, z/L \) and \( \psi \) as given by Panofsky [31], the departure from the logarithmic profile due to buoyancy effects in the surface layer can be obtained so that (3) can be used to obtain estimates of \( z_0 \) and \( U^* \).

This approach can be taken for velocity profiles measured in the surface layer, which is loosely defined as that part of the PBL where the horizontal stress and vertical heat flux are nearly constant. The height of the surface layer is frequently estimated as
the lower 10% of the convective PBL depth, \( z_i \), and is limited to a height \( z<L \) [13].

For stable conditions \( L \) varies a great deal and is relatively small [17]. The surface layer is not well defined and often is only a few meters high [33]. Under these conditions the velocity profile for non-neutral conditions cannot be used for estimation of \( z_0 \) and \( U^*_0 \), with velocity measurements taken well above the surface layer.

In general, Monin-Obukhov (M-O) similarity theory can only be applied in the surface layer, when the flow conditions are stationary, when surface conditions are uniform (roughness and temperature), and over level terrain without major topographical features such as mountains etc. If the measured velocity data are linear with \( \ln z \), then this observation does not automatically guarantee that the profile is truly logarithmic. For the majority of sites including the Wallops Island site the above conditions are not met, and application of the M-O similarity concepts such as the empirical flux-profile relationships, which are based on data with the above conditions satisfied, is questionable and should probably be avoided.

For neutral conditions the temperature profile should follow the adiabatic lapse rate of either 0.01 or 0.0065°C/m for dry and saturated air respectively. It is very seldom, even under the strongest wind conditions, that a truly neutral stratification is encountered for any length of time. The usual daytime thermal stratification near the surface is \(- \frac{dT}{dz} > \gamma_a \) (unstable stratification) and \(- \frac{dT}{dz} < \gamma_a \) (stable stratification) for nighttime. There is a short time around sunrise and in the late afternoon before sunset when a neutrally stable stratification is observed near the surface in the first 10 or 20 m. The
stratification of the air at higher elevations varies a great deal with
time of day, cloud cover and season. For southerly flows over the ocean
the air temperature is usually higher than the water temperature and
a surface-based inversion (-dT/dz < \gamma_a) exists day and night.

Changes in temperature and velocity profile occur also as the flow
experiences a sudden change in surface roughness and surface temperature,
and an internal boundary layer (IBL) develops as the flow adjusts itself
to the new surface conditions. On-shore winds at Wallops Island usually
experience an increase in roughness and an increase in surface temperature
in daytime as they cross the beach. For westerly winds the surface
temperature changes as the wind moves from the wet marsh over the warm
land surface during daytime. Within the observation height of 76m at the
Wallops Island site, temperature gradients vary greatly with height and
even change from positive to negative or vice versa. Under these condi-
tions the local Richardson number is not a true indicator of the overall
thermal stratification of the observed flow and M-O similarity does not
apply.

Typical temperature profiles for southerly winds on a summer afternoon
are shown in Figure 5. These temperature profiles clearly indicate the
stable conditions above the IBL in the early afternoon, and the surface
cooling in the late afternoon. Daytime and nighttime temperature profiles
for strong westerly winds are shown in Figure 6. During daytime the
surface temperature is maximum and gradually decreases with height. On
a rainy day with low cloud cover a stable stratification is observed above
40 m. Neutral temperature profiles throughout the tower height are seldom
observed; the second temperature profile shown in Figure 6 is the closest
to an observed neutral temperature profile. Typical nighttime temperature
profiles show a stable stratification near the surface with near neutral
conditions above 15 m.

Ratios of mean velocities at the 15.2 m (50 ft), 30.5 m (100 ft), 45.7 m (150 ft) and 61 m (200 ft) levels with respect to the mean velocity at the 76.2 m (250 ft) level are shown in Figure 7. The plotted data in this figure represent the mean and the plus and minus standard deviation from the mean, as well as the maximum and minimum values of the velocity ratios for the data records acquired in each 15-degree sector. Because the mean velocity at higher elevations is less disturbed by local surface obstacles and is outside the developing IBL, the mean velocity at the 76.2 m (250 ft) level was chosen as the reference velocity. For the one sector between 0° and 15° and the 5 sectors between 90° and 165° (east-southeast) the number of data records available in each sector was four or less, an insufficient number for determination of the standard deviation, and only the average velocity ratios are presented.

Between 230° and 360° (southwest-north) the variation in mean wind speed between the different elevations is relatively minor under moderately strong wind conditions. Conversely, for southerly winds in the sector 160° < φ < 230, large variations in mean wind speeds relative to the mean velocity at the 76.2 m (250 ft) level are observed. For example in the sector between 180° and 195° the mean wind-speed ratio, \( V_{50}/V_{250} \), varies from 0.4 to 0.8, clearly indicating the great variability of mean velocity distribution near the surface. Relatively large variations of the mean velocity ratios are also observed for wind directions approximately parallel to the island for sectors 30°-45° and 210°-225°. For winds from these two sectors a small change in wind direction gives rise to a large variation in upstream terrain roughness. Generally the variations of the mean velocity distribution near the surface for on-shore winds are
much larger than for westerly winds. For on-shore winds, the changing
development length of the IBL, the thermal stratification and other
atmospheric conditions have a great effect on the velocity distribution
near the surface as the data indicate. For southerly winds, a surface-
based inversion exists during the daytime as the result of warmer air flowing
over the colder water [3]. Under these conditions the existence of a sur-
face jet with a maximum mean velocity (jet velocity) within a few hundred
meters from the surface has been observed. The jet velocity has been
observed as low as 45.7 m (150 ft) as shown by the maximum values of
the velocity ratio $V_{150}/V_{250}$ of larger than one for wind directions be-
tween $170^\circ$ and $210^\circ$, and by one of the velocity profiles of Figure 8.

Typical strong-wind velocity profiles for wind directions between
southwest and north are shown in Figure 9. The stronger wind profile
is linear over the entire observation height when presented in
semi-logarithmic coordinates. In the second profile with somewhat lower
velocities, a distinct "kink" is observed. The majority of the measured
velocity profiles for westerly wind directions shows similar "kinks".
The values of $z_0$ obtained from the velocity profiles above the "kink"
are much too small for the upstream terrain. Moreover the two velocity
profiles of Figure 9 are approximately from the same direction. Therefore
the "kinks" in the profiles cannot be the result of an upstream change
in roughness, but must be interpreted as the beginning of the transition
from the surface-layer flow to the uniform mixed-layer flow [13].

6.2 Velocity Profile Parameters $z_0$ and $a$

The roughness length, $z_0$, can be evaluated from fitting of either
the logarithmic law (2) or the non-neutral profile law (3) to the
measured mean velocities in the surface layer. The height of the

surface layer in which (2) and (3) are valid is roughly defined as the layer near the surface which the fluxes $uw$ and $\overline{w\theta}$ are approximately constant and not less than 80% of the surface stress, $\sqrt{\tau_c/\rho}$, and surface heat flux, $Q_o/c_p\rho$, respectively. Measurement of the turbulent fluxes at Wallops Island indicate that the thickness of the surface layer varies a great deal with wind speed, wind direction and thermal stratification.

For on-shore winds the top of the surface layer is generally below the lowest observation level of 9.1 m (30 ft) and for the strongest westerly winds the surface layer extends above the height of the tower. For on-shore winds when an IBL develops as the air crosses the beach, turbulent heat-flux measurements show an upward flux at the lower levels and a downward flux at the higher elevations [3]. Transition usually occurs between the 15.2 m (50 ft) and 30.5 m (100 ft) levels, which should correspond to the height of the IBL at the tower location. The flow above the IBL is still associated with the ocean surface, but is well above the surface layer, which for southerly winds extends only a few meters above the water surface. Consequently no values of the roughness length, $z_o$, for either the land or ocean surface can be obtained from the measured velocity profiles. Despite the fact that two velocity profiles of Figure 8 show a linear variation of velocity with $\ln z$, fitting of the log-law (2) to the velocity data leads to values of $z_o$ of the order of 1m, which are much too high for either the existing upstream terrain or the ocean. The parameters describing the on-shore turbulent flow depend in part on the roughness of the underlying surface (ocean) but also to a great extent on the stability of the flow. Consequently, knowledge of the roughness length, $z_o$, for flows over the ocean is not sufficient for the prediction of the turbulence
parameters for higher elevations as presented by ESDU [28,34].

For westerly winds the local shear velocity \( U^* = \left[ \overline{u^2} + \overline{v^2} \right]^{1/4} \) is approximately constant over most of the observation height, indicating that the surface layer extends well above the lowest observation level of 9.1 m (30 ft). Also the values of the local shear velocity, \( U^* \), compare quite well with the profile friction velocity \( U^*_o \), obtained from mean velocity measurements below the profile "kink". The roughness length, \( z_o \), obtained from fitting of the log-law (2) to the measured mean velocities below the profile "kink", vary with upstream roughness and thermal stability of the flow in the surface layer.

Figure 10 shows the variation of \( z_o \) with wind direction, clearly indicating the effect of the 6.5 m high storage bunker for mean wind directions of 270°. In the sector between 350° and 30° the upstream terrain is much rougher which results in higher values of \( z_o \). For the sectors between 230° and 260° and 280° and 340°, the terrain is reasonably uniform and the average value of the roughness length, \( z_o = 0.034 \) m, corresponds quite well to the predicted values of ESDU [28,29] for similar terrain. In Figure 11 all values for \( z_o \), obtained for wind directions in the before-mentioned sectors, are shown as a function of the gradient Richardson number evaluated at \( z=15.2 \) m (\( R_{i15} \)). The values of \( z_o \) were obtained by fitting of the log-law to the velocity measurements below the profile "kink". The scatter of the data is appreciable for \( R_{i15} > 0.15 \), however the values of \( z_o \) decrease rapidly for \( R_{i15} < 0.15 \). At this point the mean velocity profile in the surface layer can no longer be estimated with the log-law (2), as stability effects start to dominate. An attempt was made to estimate the roughness length by fitting the non-neutral profile (3) to the mean velocity data above the "kink" as outlined by Panofsky [31].
However, this correction technique leads to unrealistic estimates of $z_0$, which seem to indicate that the velocity profile above the "kink" is not part of the surface-layer profile but instead is the transition of the surface layer profile to the mixed layer profile.

In Table I mean profile parameters and turbulence parameters are presented for strong-wind data records with wind directions in the above-mentioned sectors with near-uniform upstream terrain and measured with the cup-vane system and the hot-film anemometers. For the data records with a thermal stratification close to neutral the semilogarithmic velocity profiles (S) are generally linear throughout, and for the records for which the flow is more unstable, kinks (K) start to appear in the profile.

Engineers generally favor the power law as an expression for the velocity profile through the entire PBL over uniform terrain

$$\frac{U}{U_R} = \left(\frac{z}{z_R}\right)^\alpha$$  

(6)

Although under certain conditions this law has fitted observed profiles over uniform terrain quite well, it is now generally accepted that the log-law (2) is preferable over the power law (6) for flow in the surface layer. Also the power law (6) cannot be expected to be a good approximation for wind profiles in the convective PBL. The latter seems to be prevalent over the North American continent even under the strongest wind conditions.

The mean velocity profiles of records 2A1 and 2A2 acquired during the Minnesota 1973 atmospheric boundary layer experiment [12] as well as the velocity profile acquired at the Boulder Atmospheric Observatory (300 m mast [35]) on the morning of the 11th of September 1978 under
extremely strong wind conditions (20-minute average velocity of 18.67 m/s at z=10 m) show clearly that the power law with one constant exponent does not fit the velocity measurements. The measured strong-wind velocity profile at the Boulder site starts to deviate from the log-law (2) at z=22m and becomes more or less uniform above 200 m.

On the other hand mean-velocity measurements made at 3 levels (10m, 80 m and 200 m) of the 213-m mast at Cabauw, the Netherlands, under extremely strong westerly winds (30-minute average velocity of 22.2 m/s at z=10 m) [36] indicate that the power law (6) fits these data quite well. The Cabauw tower is operated by the Royal Netherlands Meteorological Institute and is located about 50 km east from the North Sea coastline. For westerly winds the upstream terrain is flat low-lying pastureland with a very shallow water table. Simultaneous temperature measurements made at 8 levels between 2 m and 200 m indicate a near-neutral thermal stratification with possibly a minimal upward heat flux from the mostly wet upstream terrain that inhibits the formation of a convective PBL, which is typical for the observations of the two North American sites.

As Panofsky [31] has pointed out the power law can be expected to fit the velocity data in the surface layer only over a limited height range. In the near-neutral surface layer where the logarithmic law applies the power-law exponent can be approximated by [31]

\[ \alpha = [\ln(\sqrt{z_1 z_2}/z_o)]^{-1} \]  

(7) clearly showing the variation of \( \alpha \) with roughness, \( z_o \), and geometric mean height, \( \sqrt{z_1 z_2} \) where \( z_1 \) and \( z_2 \) represent the elevation boundaries of the layer over which a near constant \( \alpha \) may be expected. Near the surface \( \alpha \) has a relative large value depending on the value of \( z_o \), but
decreases with height and should approach zero outside the surface layer as transition to the mixed layer takes place.

For westerly winds at the Wallops Island site, power law exponents based on the mean velocities of the three lower levels \(z_1 = 15.2\, \text{m}, \quad z_2 = 45.7\, \text{m}\) are shown in Figure 12 as a function of the roughness length, \(z_0\). Similarly, power law exponents based on the mean velocity measurements under strong-wind conditions (no "kinks") at all five levels and the three highest levels are shown versus roughness length, \(z_0\), in Figures 13 and 14 respectively. Panofsky's relation (7) fits the measurements extremely well except for the results based on the mean velocities of the three highest levels (Figure 14). The reason for this is that on a semi-logarithmic plot of \(U\) vs. \(\ln z\), the results of the higher levels fall close together and may seem to vary in a linear fashion. However in reality the data already deviate from the log-law (2) and all three prediction methods, which are based on known roughness lengths, overestimate the power law exponents obtained from the measured velocity profiles. No attempt was made to obtain power law exponents for the velocity profiles of on-shore winds, because of the variability of the profiles, the presence of an IBL and the absence of values for \(z_0\).

6.3 Turbulence Intensities

Average turbulence intensities of the horizontal velocity components \(u\) and \(v\) measured with the cup-vane instruments at 5 levels, are shown in Figures 15 and 16 for each 15-degree sector. In addition to the average turbulence intensities, the maximum and the minimum observed turbulence intensities for each sector and the mean intensity plus and minus the
standard deviation are shown. In the sector 0°-15° and the 5 sectors between 90° and 165° only average turbulence intensities are shown, because the number of data records available in each of these sectors is four or less. For on-shore winds \( \sigma_{u}/U \) is approximately 10% at \( z=15.2 \) m decreasing to 5% or less at the highest observation level (\( z=76.2 \) m). For westerly winds the \( \sigma_{u}/U \) decreases from about 20% at the lowest level to about 14% at the highest level (Fig. 17). In general the variation of the turbulence intensity, \( \sigma_{u}/U \), in each section is relatively small, except for the two sectors between 195° and 225°.

The turbulence intensity of the v component, \( \sigma_{v}/U \), shows much the same pattern, although some differences can be observed. For on-shore winds the average value of \( \sigma_{v}/U \) at the lowest observation level (in the IBL) is about 8%, decreasing to about 4% at the highest level (above the IBL). For southerly winds in the three sectors between 165° and 210° turbulence intensities for both \( u \) and \( v \) components of less than 2% have been observed at the highest observation levels above the IBL. These observations have been made under stable conditions, and on several occasions the mechanical turbulence has been observed to vanish completely at these elevations at mean velocities of 10 m/s and higher.

The average turbulence intensity \( \sigma_{u}/U \) is nearly constant at each level for wind directions between 240° and 345°. The average turbulence intensity \( \sigma_{v}/U \) at each level increases with wind direction from 240° to about 300° where a maximum is reached and decreases gradually with wind directions from 300° to about 50°. Figure 17 shows the variation of the average turbulence intensities of the \( u \) and \( v \) components with height in the two sectors 240°-255° and 300°-315°. The averaged results are also compared with the estimates of Teunissen [25] and ESDU [28] both
based on the roughness length, $z_o$, whose average is 0.037 m for either one of these sectors [Fig. 10]. Although the upstream terrain for the two sectors is about identical, the values of $\sigma_v/U$ in the sector between 300° and 315° are considerably higher than those for the sector between 240° and 255°. The average values of $\sigma_v/U$ for the latter sector correspond extremely well with the Teunissen estimate, but for the sector between 300° and 315° the average values of $\sigma_v/U$ are about 3 to 4% higher. On the other hand the average values of $\sigma_u/U$ for these two sectors are about identical and fall between the estimates of Teunissen [25] and ESDU [28].

A possible explanation for this unusual behavior of $\sigma_v/U$ can be derived from the visual inspection of several years of strip-chart recordings of wind speed and direction obtained continuously from a propeller-vane anemometer located about 1 km northeast from the tower on Wallops Island. These recordings clearly show that for northwesterly winds the instantaneous wind direction experiences frequently large fluctuations toward the north (Fig. 18). These direction fluctuations are larger than usual and are not normally distributed as shown in (Fig. 19), which explains the large values of both $\sigma_v/U$ and the covariance $\bar{v}w$ measured in this sector.

The turbulence intensity, $\sigma_u/U$, which is constant over near-uniform terrain for westerly wind directions (Fig. 17), instead varies with time of day. Nighttime measurements are systematically 1% higher than the daytime results (Fig. 20). The vertical distribution of the vertical turbulence intensity, $\sigma_w/U$, based on five strong-wind data records obtained with the hot-film system, is shown in comparison with the ESDU [28] and Teunissen estimates in Figure 21.
The vertical distributions of the turbulence intensity of all three components for southerly winds are shown in Figures 22, 23 and 24. For these wind directions an internal boundary layer (IBL) develops as the air crosses the beach. Based on the change in direction of the daytime vertical heat flux \( \overline{w_0} \), which is expected to be positive in the IBL and negative above it [3], the height of the IBL at the tower must be between the 15.2 m (50 ft) level and 30.5 m (100 ft) level. This observation agrees with the relationship given by Elliot [37], which predicts a height of the IBL of approximately 26 m, based on an upwind roughness length over the ocean of \( z_o' = 0.001 \) m and a downwind roughness length of \( z_o'' = 0.01 \) m and a development length of 300 m. The average turbulence intensities of the u and v components from nine data records, obtained with the hot-film instrumentation during summer afternoons, compare surprisingly well with the average turbulence intensities from 29 data records, obtained during winter and early spring under strong wind conditions with the cup-vane system (Figs. 22, 23, 24). The turbulence intensities in the IBL compare reasonably well with the ESDU [28] predictions based on a roughness length of \( z_o = 0.01 \) m. However above the IBL the ESDU [28] predicted values of the turbulence intensities, based on a roughness length \( z_o = 0.001 \) m, overestimate the actual measured values by a factor of two. The turbulence intensities for run 7 [3] obtained under extremely stable conditions \( (R_f = 25.5, U = 10.7 \) m/s at \( z = 61 \) m), which are included in Figures 22 through 24, show lower than average values above the IBL. Under similar conditions it has been observed that the turbulence vanishes completely for some time. The variation of the ratios of average turbulence intensities, \( \sigma_v/\sigma_u \) and \( \sigma_w/\sigma_u \), for all wind directions is shown in Figure 25. The measurements indicate that the values of
these ratios are more or less independent of height, and the data shown in Figure 25 are not only the ratios of the average turbulence intensities of all data records in each sector but are also averaged over all observation levels. For most wind directions the values of \( \sigma_v / \sigma_u \) are between 0.75 and 0.85 in comparison with the predictions of 0.75 and 0.80 by Counihan [26] and Teunissen [25]. The estimates of ESDU [28] are not single valued but are dependent on height and roughness length. Smaller values than 0.75 for \( \sigma_v / \sigma_u \) are observed for wind directions approximately parallel to the island at \( \phi=40^\circ \) and \( \phi=230^\circ \). Values of \( \sigma_v / \sigma_u \) higher than 0.85 are observed for southerly winds for \( \phi=170^\circ \) and for northwesterly winds in the sector \( 280^\circ < \phi < 350^\circ \). That the values of \( \sigma_v / \sigma_u \) are relatively high in this last sector is no big surprise since often large direction fluctuations have been observed in this sector (Fig. 18). Values of \( \sigma_v / \sigma_u \) and \( \sigma_w / \sigma_u \) obtained from the hot-film data records are also shown in Figure 25. The values of \( \sigma_v / \sigma_u \) obtained with this system compare quite well with the cup-vane results. The values of the ratio, \( \sigma_w / \sigma_u \), for winds from the sector between south and southwest and northwesterly winds fall between 0.55 and 0.60 as compared to values of 0.50 and 0.52 as predicted by Counihan [26] and Teunissen [25] respectively.

The results discussed so far in this report show clearly that at the Wallops site large variations in mean as well as turbulent flow occur varying with wind direction. The important observed deviations from the simple neutral boundary-layer models are:

1. The development of an internal boundary layer (IBL) for on-shore winds as they cross the beach.

2. The existence of a surface jet for southerly winds with extremely low turbulence intensities (2% or less and occasionally
vanishing under stable conditions) coexisting with gravity waves.

3. Large direction fluctuations towards the north for north-westerly winds, observed during the daytime, which are responsible for higher than usual lateral turbulence intensities. These observations were made under strong wind conditions and there is no reason to believe that for still stronger wind speeds (maximum observed speeds) these deviations from the neutrally stable boundary-layer model will suddenly vanish.

6.4 Turbulence Integral Scales

6.4.1 Integral Scales, $L_u^X$, $L_u^Z$ and $L_v^Z$ from cup-vane data

In this section the distribution of the turbulence integral scales obtained from measurements with the cup-vane system will be discussed and compared with the estimates from several review papers [25,26,28,29]. The streamwise turbulence integral scale of the $u$ component, $L_u^X$, is calculated from the autocorrelation function (1), $R_u(\tau)$, assuming that Taylor's hypothesis is valid. Averages of all scales, $L_u^X$, obtained from the data records in each 15-degree sector, are plotted along with the maximum and minimum and plus and minus the standard deviation from the average value in Figure 26 for each observation level. Averages only are plotted in the sector $0^\circ-15^\circ$ and between $90^\circ$ and $160^\circ$ because of the limited number of available data records in these sectors. The integral scales, $L_u^X$, increase systematically with height and show a great deal of variability for all wind directions. In general the magnitude of these integral scales is larger for westerly winds than for on-shore winds except for southerly wind directions. At the highest observation level two distinct extremes for the maxima can be observed in the two sectors between $180^\circ$ and $210^\circ$, and between $300^\circ$ and $330^\circ$. For southerly winds between $180^\circ$ and $210^\circ$
the air is frequently stably stratified which under certain conditions may lead to the coexistence of turbulence and low-frequency gravity waves. If gravity waves are present the integral scale obtained from the autocorrelation function can be expected to be high [3], a maximum value of 800 m at the 76.2 m (250 ft) level has been observed. On the other hand, if the low-frequency gravity waves are absent and only turbulence of less than 5% intensity is present (Fig. 15), minimum turbulence integral scales of less than 100 m have been observed for the southerly winds. In the sector between 300° and 330° large variations in $L_u^X$ are also present, which are the result of either the presence or absence of low-frequency velocity fluctuations as can be observed from measured u-spectra.

Vertical integral scales of the horizontal velocity components obtained from the measurements with the cup-vane system can be calculated by integration of the vertical correlation coefficients of either the u or v components.

$$L_i^Z = \int_{0}^{\infty} R_{ii}^Z(z')dz'$$  \hspace{1cm} (8)

where

$$R_{ii}^Z(z') = \frac{1}{\{\sigma_{i}(z)\}^2} \frac{1}{T} \int_{0}^{T} u_i(t,z) u_i(t,z+z')dt$$  \hspace{1cm} (9)

and $i = u$ or $v$

$R_{ii}^Z(z')$ is the vertical correlation coefficient of either the u or v velocity fluctuations measured at two different levels separated by a distance $z'$. For this research program with the Wallops Island tower the separation distance, $z'$, can be either 0, 15.2 m (50 ft),
30.5 m (100 ft), 45.7 m (150 ft) and 61 m (200 ft). The integration (8) should be performed to the point where the correlation coefficient $R_{uu}^Z(z')$ changes for the first time from positive to negative. However only a maximum of five values of the correlation coefficients are available for either upward or downward integration according to expression 8, and often the correlation coefficient has still a large positive value for the maximum separation distance $z'$.

In order to arrive at a reasonable estimate of the vertical scales, it is assumed that the vertical correlation coefficients of the horizontal velocity components $u$ and $v$ decay exponentially in the same manner as has been observed by Dryden et al. [38] for high Reynolds-number grid turbulence, according to

$$R_{ii}^Z(z') = \exp[-z'/L_1^Z]$$

Vertical integral scales of either the $u$ or $v$ velocity components can then be obtained from a least-squares fit of (10) to the available measured correlation coefficients.

Because of the non-symmetric flow in the boundary layer, integral scales obtained from upward and downward integration of the correlation coefficients with the origin at a common point cannot be expected to be the same. Instead a slightly different definition for the vertical integral scale is used as suggested by ESDU [29], where the correlation coefficient is defined as

$$R_{ii}^Z(z') = \frac{1}{\langle \sigma_i(z) \rangle^2} \frac{1}{T} \int_{0}^{T} v_i(t,z+z')v_i(t,z-z')dt$$

(11)

where $i = u$ or $v$. 
With the use of this definition only one vertical integral scale is defined for each height \( z \). However this definition can be used for the evaluation of the integral scales of the \( u \) or \( v \) component at the 45.7 m (150 ft) level only.

The distribution of the vertical turbulence integral scales of the horizontal velocity fluctuations and obtained with the cup-vane system is shown in Figure 27 and 28 respectively. Calculation of these scales is based on expression (10). Integral scales obtained from upward integration of the correlation coefficients are shown as \( LUZ^+ \) or \( LVZ^+ \) on the figures and as \( L_U^+ \) or \( L_V^+ \) in the text. For the integral scales obtained from downward integration the direction of the arrow is reversed. The two-sided integral scales obtained according to the definition (11) are shown as \( LUZ^\downarrow \) or \( LVZ^\downarrow \) on the figures and as \( L_U^\downarrow \) or \( L_V^\downarrow \) in the text. Averages of all the integral scales for each sector as well as the maximum and minimum, and the mean plus and minus the standard deviations for each each sector are shown in these figures. In the sectors 0°-15° and between 90° and 165° not enough data records were available to calculate a standard deviation and only average values are plotted.

The integral scales \( L_U^Z \) for on-shore winds are generally smaller than those for westerly winds by less than a factor of two. The integral scale \( L_U^Z \) measured at the 15.2 m (50 ft) level and the scale \( L_U^Z \) measured at the 76.2 (250 ft) level are of the same magnitude. The smallest observed value of \( L_U^Z \) is about 10 m for southerly winds without the presence of gravity waves. The larger values of \( L_U^Z \) are also observed for southerly winds when gravity waves are present.
Large values of $L_u^z$ are also observed for northwesterly wind directions between $300^\circ$ and $320^\circ$. The upward integrated scales, $L_u^{z+}$, obtained from the lower three levels for wind directions between $0^\circ$ and $100^\circ$ show much less variation than the downward integrated scales, $L_u^{z-}$, from the upper three levels in the same sector. Comparison of the three different scales, $L_u^{z+}$, $L_u^{z-}$ and $L_u^{z}$ of the measurements at the 45.7 m (150 ft) level shows that for winds between $0^\circ$ and $100^\circ$ the upward and downward integrated scales are of the same magnitude (37 m) with the scale $L_u^{z+}$ having an average value of approximately 43 m. For westerly winds between $250^\circ$ and $360^\circ$, $L_u^{z+}$ is about 20 m larger than $L_u^{z-}$.

The vertical integral scale of the v-component, $L_v^z$, behaves in a similar fashion as the scale $L_u^z$, but the latter is generally twice as large. The magnitude of $L_v^z$ for winds from westerly directions is about twice the value of $L_v^z$ for on-shore winds. Minimum values of just a few meters are observed for on-shore winds. Maximum values of these integral scales are associated with winds from northwesterly directions ($\phi=310^\circ$) for which large direction fluctuations have been observed (Fig. 18). For southerly winds ($\phi=180^\circ$) no large maximum values for $L_v^z$ have been observed as for $L_u^z$. For on-shore winds the magnitude of the three different scales at the 45.7 m (150 ft) level are about the same but for westerly winds $L_v^{z+} > L_v^{z-}$ with the value of $L_v^z$ in between.

Figures 29 and 30 show the variation of the relative magnitude of the average turbulence integral scales $L_x/L_u^z$ with wind direction for each observation level. For southerly winds between $135^\circ$ and $225^\circ$, the ratio $L_x/L_u^z$ increases with height from about 3.7 at the lowest
level to values between 10 and 15 at the three highest observation levels. For all wind directions outside this sector the ratio \( \frac{L_x}{L_u} \) is 3.3 and 3.7 at the 15.3 m (50 ft) level and the 76.2 m (250 ft) level respectively. The magnitude of the ratio of average integral scales, \( \frac{L_u}{L_v} \), is 1.9, generally independent of height and wind direction.

6.4.2 Comparison of the Cup-Vane Scales with Predicted Values from References 25, 26 and 29

From the above discussion it is clear that the measured turbulence integral scales \( L_u^x, L_u^y \) and \( L_v^x \) vary significantly with terrain roughness, wind direction, time of day, thermal stability and other atmospheric conditions. In this section the measured integral scales are compared with the predicted scales from either Teunissen [25], Counihan [26] and ESDU [29].

In Figure 31 the averaged turbulence integral scales, \( L_u^x \), obtained from the cup-vane data are shown for two westerly wind-direction sectors over near-identical terrain and are compared with the estimates of References 25, 26 and 29. At the higher elevations the values of \( L_u^x \) in the sector \( 300^\circ < \phi < 315^\circ \) are approximately 100 m larger than those in the sector \( 240^\circ < \phi < 255^\circ \). The Counihan [26] predictions match the measurements below 30 m but for higher elevations all three references under-estimate the measured integral scales. Averaged values of \( L_u^y \) and \( L_v^y \) for the same two wind direction sectors are shown in Figures 32 and 33 and compared with predicted values from Counihan [26] and ESDU [29]. The results show the decrease in magnitude when the change is made from upward to downward integration.
Values of $L^Z_v$ in the sector $300^\circ<\phi<315^\circ$ are about twice as large as those in the sector $240^\circ<\phi<255^\circ$, which is in contrast with the values of $L^Z_u$ which are approximately identical in the two wind-direction sectors. The ESDU [29] predictions of both $L^Z_u$ and $L^Z_v$ match the measured data in the wind sector $240^\circ<\phi<255^\circ$ reasonably well, but underestimate the scales for wind directions between $300^\circ$ and $315^\circ$ for which large wind-direction fluctuations have been observed [Fig. 18].

Figures 34, 35 and 36 show the averaged values of $L^X_u$, $L^Z_u$ and $L^Z_v$ obtained from the cup-vane data, in comparison with the predicted values for southerly winds. Since no measured values of roughness length are available for this wind direction, values of $z_o$ were selected in accordance with the nature of the upstream terrain and Table 1 of Reference 28. Below 20 m, for the flow in the IBL, a roughness length $z_o=0.01$ m is appropriate and for the flow above the IBL a roughness length of $z_o=0.001$ m was selected. The measured longitudinal scales, $L^X_u$, are generally larger than the ESDU [29] predicted values, while the measured vertical scales $L^Z_u$ and $L^Z_v$ are generally smaller than the ESDU [29] predictions. These results support the likelihood that internal gravity waves exist in the surface-based inversion over the ocean. The extent of the waves is much longer in the direction of the flow than in the vertical direction because of the suppression of vertical velocity fluctuations by buoyancy forces in stable air. The results of Figure 30 show clearly the large extent of the streamwise integral scale, $L^X_u$, relative to the vertical scale, $L^Z_u$ for southerly winds only. For these winds the scale ratio $L^X_u/L^Z_u$ above the IBL varies between 10 and 15, for all
other wind directions the magnitude of this ratio is of the order of 4.

Longitudinal integral scales, $L_u^X$, obtained for westerly winds over near-uniform terrain are dependent on time of day (Fig. 37). The scales acquired during nighttime are approximately 50% longer than those obtained from morning records with the scales from afternoon data falling in between. The increase of the scales during daytime can be explained with the increase of the height of the mixed layer (See Fig. 5, Reference 13). However, no definite explanation for the large integral scales observed during nighttime is available.

In Figures 38 and 39 individual values of the turbulence integral scales, $L_u^X$, at the 15.2 m (50 ft) and the 45.7 m (150 ft) levels are plotted versus roughness length, $z_o$. These results are for near-neutral strong wind data records for wind directions varying between $\phi=250^\circ$ and $\phi=30^\circ$. The scatter of the data is appreciable as is to be expected since the previously discussed results also indicate variation of $L_u^X$ with wind direction (Fig. 31) and time of day (Fig. 37). The ESDU [29] and Teunissen [25] predictions are consistently lower than the measurements, while the Counihan predictions [26] fit the measured integral scales reasonably well. Similarly, the corresponding vertical scales $L_u^{Z\downarrow}$ and $L_v^{Z\uparrow}$ are shown versus roughness length, $z_o$, in Figures 40 and 41. The ESDU [29] predictions for $L_v^{Z\downarrow}$ match the measured results quite well, while the predictions for $L_u^{Z\uparrow}$ of the same source fall generally below the measured data except in the range $0.1 \text{ m} < z_o < 1.0 \text{ m}$. 
6.4.3 The Direct and Spectral Methods for Obtaining Turbulence Integral Scales

Integral scales of turbulence are defined for any correlation coefficient as the integral over the entire range of the independent variable, which can be either time or space as previously discussed. In practice the integration process is carried out between the origin and the first zero-crossing. Time scales are related to the length scales in the direction of the flow by assuming the existence of Taylor's frozen turbulence hypothesis. The magnitude of the time scales varies significantly depending on the presence of low-frequency fluctuations and or trends. In order to omit these fluctuations from the time-correlation coefficients, the data should be high-pass filtered at some low frequency. The filtering of the cup-vane data takes place as a result of the block averaging, excluding trends and low-frequency fluctuations below 0.00195 Hz from the sample. Similarly, the hot-film data are high-pass filtered at either 0.0244 Hz or at 0.00153 Hz depending on whether the data are analyzed in the high-frequency range (0.0244-100 Hz) or middle-frequency range (0.00153-6.25 Hz) (See section 4.2). Turbulence integral scales calculated in this way are said to be obtained by the direct method.

An estimate of the size of the energy-containing eddies can also be obtained from the Von Karman interpolation formula for the three-dimensional power spectrum covering the wavenumber-range from the energy containing eddies to the inertial subrange [39].

\[
S(k/k_e) = \frac{C(k/k_e)^4}{[1+(k/k_e)^2]^{17/6}}
\]
where \( k_e \) corresponds to wavenumbers in the range of the energy-containing eddies. With the assumption of isotropic turbulence, expressions for the physical realizable one-dimensional spectrum functions \( S_u(k_1), S_v(k_1) \) and \( S_w(k_1) \) can be obtained (see expressions 3-72 and 3-73, Hinze [40]). The wavenumber of the energy-containing eddies, \( k_e \), can be replaced by the inverse of the turbulence integral scales, \( L_i \), in the appropriate spectrum functions and the constants can be adjusted to fit the measured spectra. The one-dimensional Von Karman spectrum functions obtained in this manner and presented by Teunissen [25] fit the measured spectra of mechanically produced wind tunnel turbulence quite well [41,42]. The spectral expressions for the streamwise and lateral velocity components are given by,

\[
\frac{nS_u(n)}{\sigma_u^2} = \frac{4(nL_i^x/U)}{[1+70.7(nL_i^x/U)^2]^{5/6}}
\]

(13)

and

\[
\frac{nS_i(n)}{\sigma_i^2} = \frac{nL_i^x}{4(-\frac{U}{L_i^x})^{1+188.4(2nL_i^x/U)^2}} \frac{1+188.4(2nL_i^x/U)^2}{(1+70.7(2nL_i^x/U)^2)^{11/6}}
\]

(14)

where \( i = v \) and \( w \).

For the comparison of these wind tunnel spectra with the normalized spectrum functions, the turbulence integral scales, \( L_i \), were determined independently using the previously discussed direct method. The Von Karman spectral equations show the correct \( n^{-5/3} \)-dependence in the inertial subrange. Integration of these expressions over the entire
frequency range leads to unity. At vanishing wavenumbers these spectral equations also predict the proper integral scale $L_i^k = S_i(0)U/4U_i^2$. At low frequencies the logarithmic spectra vary as $n^{-1}$, which also fits the wind tunnel spectra quite well.

However, caution must be taken with the automatic adaption of the Von Karman spectral functions to atmospheric turbulence under near neutral thermal stratification. The work of Kaimal et al [20] clearly points out that under near-neutral conditions the low-frequency content in the spectra of the horizontal velocity components can vary appreciably. In the convective boundary layer spectral data approach a definite shape when near neutral conditions are approached from the stable regime. Under these conditions significant low-frequency velocity fluctuations in the $u$ and $v$ components are absent and the spectral shape of these components is similar to the Von Karman model. On the other hand no unique spectral shape for the $u$ and $v$ component exists for near neutral conditions approached from the unstable regime. Under these conditions, the low-frequency spectral content is much higher and the Von Karman model does not represent the spectral data well.

In order to check the validity of the Von Karman spectral functions, it will be necessary to check these relations against measured spectra, where the frequency is normalized with the local mean velocity and the turbulence integral scale obtained independently via the direct method. In Figures 42 and 43 logarithmic spectra of the $u$-component measured at 5 different elevations for data record 19 (Table 1) are compared with the Von Karman spectral function. The difference in those two illustrations is that variances and integral scales used in Figure 42...
were obtained in the middle-frequency range (0.00153-6.25 Hz) while for Figure 43 the variances and integral scales were obtained in the high-frequency range (0.0244-100 Hz) filtering out the low-frequency fluctuations. In the latter case the Von Karman expression fits the measured spectra quite well in the -2/3 region but in the low-frequency range the measured spectral values are considerably higher than the predicted values. Consequently no distinct spectral peak at the predicted value of the reduced frequency of $nL_x/U=0.146$ is present. Similarly, the measured $v$ spectra follow the Von Karman spectrum in the -2/3 region only if variances and integral scales are used from which the low-frequency components are filtered out. Figures 44 and 45 show the $w$-spectra for run #19 in comparison with the Von Karman spectrum function for variances and integral scales obtained in the middle and high frequency range respectively. In the latter case the measured spectra fit the theoretical Von Karman spectrum function much better especially for the spectra from the higher elevations.

Based on these results the conclusion can be drawn that the theoretical Von Karman spectrum functions do not represent the spectra of atmospheric turbulence in the low-frequency range or in the high-frequency range when turbulence integral scales are used that are obtained via the direct method when low-frequency fluctuations are included. Better fit of the measured spectra in the -2/3 region is achieved when variances and turbulence integral scales are used that are obtained from data records from which the low-frequency fluctuations have been removed. Inversely, if the theoretical Von Karman spectrum functions are used to obtain streamwise turbulence integral scales,
L_i^x, as is suggested in references 25 and 28, then these scales are not equivalent to the integral scales obtained via the direct method. The integral scales obtained via the Von Karman method must be interpreted as integral scales associated with velocity records from which all low-frequency fluctuations with periods longer than approximately 40 seconds have been filtered out.

The expressions for the streamwise turbulence integral scales, L_i^x for i=u,v and w, listed in references 25 and 29 are based on scales obtained via the Von Karman method by either matching of the measured spectra at the peak reduced frequency or by using a best overall fit of the spectra. Consequently the predicted integral scales from these sources must be interpreted as integral scales associated with the high-frequency content of the turbulence components.

6.4.4 Comparison of Integral Scales Obtained Via the Direct and Spectrum Methods With Predicted Values from References 25, 26 and 29.

The turbulence integral scales, L_i^x, obtained from the cup-vane data are obtained via the direct method in the frequency range from 0.00195 Hz to 0.25 Hz. Integral scales obtained from the hot-film data and discussed in this section, are obtained by one of the following three methods:

1. The direct method in the middle-frequency (MF) range (0.00153-6.25 Hz).
2. The Von Karman method, with the spectra and variances obtained from filtered data in the middle-frequency range (VK-MF).
3. The Von Karman method, with the spectra and variances obtained from filtered data in the high-frequency range (0.0244-100 Hz) (VK-HF).
For method 2 and 3 values of $L^x_i$ were obtained by matching the measured logarithmic spectra $(nS_i(n)/\sigma^2_i$ versus $nz/U)$ at $nz/U=10$ to the Von Karman spectrum functions in the $-2/3$ range. Averaged and single-record streamwise integral scales, $L^x_i$, obtained from the cup-vane data or from the hot-film data, the latter derived through one of the above three methods, are shown for the two basic wind directions (south and northwest) in Figures 46 through 57 and are compared with the predicted values of references 25, 26 and 29.

Figures 46, 47 and 48 show the variation of the averaged integral scales, $L^x_i$ with $i= u, v$ and $w$, obtained from the hot-film data (methods 2 and 3) versus height for southerly winds. The predicted values are based on a roughness length, $z_o=0.01 \text{ m}$ in the IBL below 20 m and on a roughness length $z_o=0.001 \text{ m}$ above the IBL. The values of $L^x_i$ from the cup-vane data match the ESDU [29] predictions and the scales obtained from the hot-film data via the Von Karman method in the middle-frequency range match the Teunissen [25] predictions. Values of $L^x_v$ and $L^x_w$ obtained with the use of the Von Karman method in either frequency range fall well below the predictions. Of course, as previously discussed, the ratio of longitudinal scales and lateral scales is much higher for southerly winds than for the other wind directions (Figs. 29, 30).

The effect of buoyancy in the inversion layer tends to suppress the vertical motion and consequently the measured scales $L^x_w$ are much smaller than the predicted scales. It must be assumed that the predicted scales are based on data records taken under conditions where buoyancy had very little effect on the turbulence. The lateral scales, $L^x_v$ and $L^x_w$ obtained via the Von Karman method in the middle-frequency range are about twice as long as the scales obtained from the same data in the high-frequency range.
Figures 49, 50 and 51 show the averaged integral scales, $L^i_i$ for $i=u, v$ and $w$, obtained from the hot-film data and analyzed according to methods 1 and 2 for northwesterly wind directions. In Figure 49 comparison of $L^x_u$ is also made with the cup-vane data. The scales obtained via the direct method from the cup-vane data are generally smaller than the scales from the hot-film data via the direct method in the middle-frequency range. The scales obtained with the Von Karman method in the middle-frequency range are systematically smaller than the scales obtained with the direct method from either the cup-vane or hot-film data in the same frequency range. The Teunissen [25] and ESDU [29] predictions only fit the measured scales obtained via the Von Karman method below a height of 20 m. Above this height the predicted values are systematically lower than the measured values. The Counihan [26] predicted scales of $L^x_u$ fit the observed scales obtained via the direct method below 20 m, however above the height of 20 m the Counihan prediction falls between the measured scales obtained via the direct method and those obtained via the von Karman method.

The measured lateral scales $L^x_w$ and $L^x_v$ obtained via the direct method in the middle-frequency range are three to four times as large as those obtained via the Von Karman method in the same frequency range (Figs. 50, 51). The latter scales match the Teunissen [25] and ESDU [29] predictions very well.

In Figures 52, 53 the integral scales, $L^x_u$, obtained from a single early-evening record are compared with the predicted scales and with the average scales from the daytime records all analyzed in the middle-frequency range. It has been observed [13, 23] that just before sunset the convective boundary layer dissolves abruptly and the low-frequency velocity fluctuations normally associated with the convective
PBL suddenly disappear as can be clearly seen from the comparison of the plotted records of the horizontal velocity components of record 16 (evening run) and record 19 (afternoon run) (Fig. 54). The results indicate much smaller scales if the low-frequency fluctuations of the horizontal components are absent. For record 16 the scales obtained via the direct method are systematically larger than those obtained via the Von Karman method, although the difference is less significant for this early evening run than for the daytime records, which contain low-frequency fluctuations (Figs. 49-51).

Figures 55 through 58 show the averaged integral scales, $L_x^v$ and $L_y^w$, from the daytime records and those for record 16 obtained via the Von Karman method in either the high-frequency range or the middle-frequency range. The Von Karman method for obtaining integral scales provides near-identical results independent of the frequency range if large low-frequency fluctuations are absent (e.g. record 16) or if the low-frequency fluctuations are removed from the data records. If the large low-frequency fluctuations are present (e.g. $u$ and $v$ components of daytime records Fig. 54) and are not removed from the daytime records the Von Karman method leads to much larger integral scales. If no appreciable low-frequency velocity fluctuations are present in the data records, the integral scales obtained via either the direct or the Von Karman method are about the same in magnitude. However, if low-frequency components are present the magnitude of the scales depends on the method by which they were calculated and also depends on the frequency range in which the data are analyzed.
When the integral scales, $L_u^X$, obtained via the two-methods in either one of the frequency ranges, for data records with or without low-frequency content are compared with predicted values (Figs. 49, 52 and 53) one observes appreciable variation. In general, the Teunissen [25] predicted values correspond to scales obtained from data records for which the large low-frequency fluctuations are absent or are filtered out, and obtained via either method. On the other hand the Counihan [26] predicted values correspond more to the scales obtained from data records with low-frequency fluctuations and obtained via the Von Karman method in the middle-frequency range and to the scales obtained from the cup-vane data. The magnitude of the scales obtained from the same data records via the direct method are generally larger than those predicted by Counihan [26]. The ESDU [29] predicted scales fall between the two previously mentioned predictions. The scales obtained from data records of north-west winds with low-frequency fluctuations vary almost linearly with height, while the predicted scales show more a tendency toward independency with height at higher elevations.

Similarly the lateral integral scales, $L_v^X$ (Figs. 50, 55 and 57) also show appreciable variation. The Teunissen [25] and ESDU [29] predictions correspond reasonably well to the scales obtained during daytime via the Von Karman method in the middle-frequency range. The scales obtained from the same daytime records via the direct method are significantly larger than the predictions. On the other hand if low-frequency components are absent or filtered from the data records the measured values for the lateral integral scales, $L_v^X$, fall well below the predicted values.

The integral scales, $L_w^X$, (Figs. 51, 57 and 58) show a similar pattern, the ESDU [29] and Teunissen [25] predictions correspond best
to the scales obtained via the Von Karman method in the middle frequency range. The scales obtained via the direct method in the same frequency range are considerably larger than the predicted values. If low-frequency components are absent or removed from the data records the measured scales are generally lower than the ESDU [29] and Teunissen [25] predictions.

In general it can be concluded that the ESDU [29] and the Teunissen [25] predicted $L_v^X$ and $L_w^X$ scales should be interpreted as scales obtained via the Von Karman method for turbulence with low-frequency fluctuations. On the other hand the Teunissen [25] predicted $L_u^X$ scales should be interpreted as scales obtained from data records from which the large low-frequency fluctuations are absent or are filtered out. In general the horizontal scales $L_u^X$ and $L_v^X$ obtained from the daytime data records via the Von Karman method in the middle-frequency range vary linearly with height, while the predicted scales show a tendency of independence with height at the higher elevations.

6.5 Power Spectra

In this section the power spectra of the three velocity components obtained from the hot-film data are discussed for the two basic wind directions, south and northwest. Ample discussion of the spectra in the previous section has indicated that the spectral shape in the low-frequency range depends greatly on the absence or presence of large low-frequency velocity fluctuations.

The logarithmic spectra obtained from south-wind records generally show very little variation in shape and vary as $f^{-2/3}$ in the high-frequency range and approximately as $f^{+1}$ in the low-frequency range. These two ranges
are separated by a distinct spectral peak. Kaimal (43) suggests that under stable conditions in the absence of appreciable low-frequency fluctuations all spectra can be brought in coincidence and approximated by the empirical relation

\[
\frac{nS_i(n)}{\sigma_i^2} = \frac{0.164(f/f_o)}{1+0.164(f/f_o)^{5/3}}
\]

(15)

with \(i = u, v\) and \(w\),

where \(f = n z / U\) is the reduced frequency and \(f_o\) is the reduced frequency at the point of intersection of the extrapolation of the inertial subrange of the spectra and the line \(nS_i(n)/\sigma_i^2 = 1\). Kaimal's spectra and variances are obtained from data in the frequency range \(0.005 < n < 10\) Hz.

The Von Karman spectrum functions (13, 14) can be modified into similar expressions

\[
\frac{nS_u(n)}{\sigma_u^2} = \frac{0.156f/f_o}{[1+0.108(f/f_o^2)]^{5/6}}
\]

(16)

and

\[
\frac{nS_i(n)}{\sigma_i^2} = 0.12(f/f_o) \left[ \frac{1+0.679(f/f_o^2)}{[1+0.255(f/f_o^2)]^{11/6}} \right]
\]

(17)

with \(i = v\) and \(w\).

In this set of equations the reduced frequency is defined as \(f = n L_x^\lambda / U\). However the parameter \(f/f_o\) for either the Kaimal or the Von Karman expressions represents the wavelength ratio \(\lambda_o / \lambda\), where \(\lambda_o\) is the wavelength associated with the reduced frequency, \(f_o\). In both spectral expressions the parameter \(f/f_o\) is independent of the length scale which is either the elevation or the turbulence integral scale \(L_x^\lambda\).
The Kaimal (15) and the Von Karman (16,17) spectrum functions are nearly identical in the inertial subrange, but the Kaimal spectrum predicts a slightly smaller spectral peak. In the low-frequency range the u-spectra again are about identical, but the Von Karman v and w spectra fall slightly below the Kaimal spectrum.

In Figures 59, 60 and 61 the normalized logarithmic u, v and w spectra \( nS_i(n)/\sigma_i^2 \) are plotted as a function of the modified reduced-frequency \( f/f_o \). The spectra were taken from different data records for winds from southerly directions, which were classified according to the local stability parameter \( z/l \). The spectral data and the variances were obtained from data analyzed in the high-frequency range \( 0.0244 < n < 100 \) Hz. The velocity spectra obtained from stable-air records above the IBL do not differ from those obtained in the unstable air in the IBL and all fit the Von Karman and the Kaimal spectral functions remarkably well.

The empirical spectrum functions (15,16,17) for estimation of the velocity spectra in the case low-frequency fluctuations are absent can be extremely useful if values of \( f_o \) can be predicted. Based on the experimental results it is obvious that \( f_o \) varies with height and with the presence or absence of appreciable low-frequency velocity fluctuations. The results did not indicate any systematic variation of \( f_o \) with stability as suggested by Kaimal [43]. Averaged values of \( f_o = (nz/U)_o \) for each velocity component and obtained from normalized logarithmic spectra in the high-frequency range are shown as a function of height in Figure 62. However, values for \( f_o \) obtained from the same data records but analyzed in the middle-frequency range \( (0.00153 < n < 6.25 \) Hz) depend greatly on the presence of low-frequency velocity fluctuations. If no appreciable low-
frequency fluctuations are present, the values $f_o$ are independent of the frequency range the data are analyzed.

For all $u$-spectra investigated low-frequency fluctuations are present between the low cut-off frequencies for the middle- and high-frequency ranges, 0.00153 Hz and 0.0244 Hz respectively. These spectra do not exhibit a distinct spectral peak but instead values of the logarithmic spectra are approximately the same for $f<0.1$. Values of $f_o$ obtained from the $u$-spectra analyzed in the middle-frequency range are generally smaller than those obtained from the same data records but analyzed in the high-frequency range and seem to converge to a general value in the range $0.02 < f_o < 0.03$, independent of height.

For those records where internal gravity waves affect the spectra above a frequency of $n=0.00153$ Hz, the frequency range for which spectral values are increased varies with elevation. At the lowest elevation ($z=9.1$ m) only the spectral values at the lowest frequencies are affected and an appreciable range where the normalized logarithmic spectrum varies as $f+1$ is still present (Fig. 63). However for spectra from higher elevations the $f+1$-range becomes gradually smaller as the effect of the waves is felt at increasing frequencies until no appreciable frequency range with a $f+1$ spectral distribution is present (Fig. 64).

For those cases values of $f_o$ for the $u$-spectra seem to vary between the lower limit of $f_o=0.02-0.03$ and the values of $f_o$ obtained in the high-frequency range as shown in Figure 62. Similar observations can be made for the $v$ and $w$ spectra. The values of $f_o$ obtained from spectra analyzed in the middle-frequency range are generally lower than those obtained from the same spectra analyzed in the high-frequency range.
Spectra obtained from data records for westerly winds exhibit significant low-frequency content for all elevations and the spectral data fit the Kaimal or the Von Karman spectrum functions (15,16,17) in the inertial subrange (-2/3 region) only (Figs. 65,66,67). The v-spectra (Fig. 66) show a peculiar shape which is typical for spectra of the lateral velocity component in the surface layer of a convective boundary layer [19]. Kaimal's explanation for this shape is based on the fact that in the inertial subrange the spectral values of the v-component are 4/3 times larger than the u-spectra, a requirement for isotropy in this range. (A similar situation exits for the w-spectra.) As the w-spectra reach their peak and start to roll off with lower frequencies, the v-spectra instead continue to increase and start to follow the u-spectra. The result of this is the peculiar shape of the v-spectra in the transition between the -2/3 range and the low-frequency range where the u and v spectra both are independent with elevation but instead vary with the height, z_i, of the convective boundary layer.

In the case the low-frequency fluctuations are absent as is the case just before sunset, as the convective boundary layer disintegrates rapidly, the u, v and w spectra (Figs. 68,69,70) and specifically the v-spectra (Fig. 69) have a completely different character. The v-spectra show a distinct spectral peak and a rapid roll-off at lower frequencies although the spectra values fall above the Von Karman prediction in this range. However in comparison with the spectra of the daytime run 19 [figs. 65, 66,67], the spectra of the evening run 16 show much lower spectra values in the low-frequency range and the peculiar shape of the daytime v-spectra as discussed above has disappeared and the v-spectra resemble the Von Karman
Values of the reduced frequency, $f_0$, defined as the intersection of the extrapolation of the spectra in the inertial subrange and the line $nS_1(n)/\sigma_1^2=1$, were obtained from spectra analyzed in both the high- and middle-frequency range. For the daytime $u$ and $v$-spectra for which appreciable low-frequency velocity fluctuations are present, the values of $f_0$ obtained in the high-frequency range are systematically three times as large as the corresponding values obtained from the spectra analyzed in the middle frequency range, while for the $w$-spectra the ratio $(f_0)_{HF}/(f_0)_{MF}$ is approximately 1.6, indicating that the low-frequency content is larger in the $u$ and $v$ spectra than in the $w$-spectra. For run 16 this ratio for the $u$-spectra is 1.9 and for the $v$ and $w$ spectra 1.25. These results clearly indicate the effect of the low-frequency fluctuations on the location of the inertial subrange when the spectra are presented in the logarithmic form with $nS_1(n)/\sigma_1^2$ and $f=nuz/U$ as coordinates. The distribution of $f_0$ with elevation for daytime spectra and evening spectra analyzed in the middle-frequency range are shown in Figure 71. The results from the daytime spectra show that the values of $f_0$ for each velocity component are approximately independent with height and are $(f_0)_u=0.01$, $(f_0)_v=0.02$ and $(f_0)_w=0.07$. This observation is in agreement with some of the results obtained for southerly winds although the values are somewhat higher because of less low-frequency content. If no low-frequency fluctuations are present in the velocity components, the values of $f_0$ generally increase with height (Figs. 62, 71).

The values of $f_0$ can be used to obtain the wavelengths corresponding to the spectral peaks associated with either the Kaimal or the Von Karman spectral functions. Since for both empirical relations the logarithmic
spectral peak is approximately located at $f/f_0 \approx 3.8$, then $f_m = 3.8f_0$ and

$$(\lambda_m)_i = 0.26z/(f_0)_i \quad \text{for } i=u,v,w.$$  

(18)

Here the wavelength, $\lambda_m = (U/n)_m$, corresponds to the peak of the Kaimal and Von Karman spectrum functions and to the peak of the measured spectra if no appreciable low-frequency fluctuations are present in the data records. The peak wavelengths, $(\lambda_m)_i$, are often used in micrometeorology as measures of the energy containing eddies, or they can be slightly modified to fit the original Von Karman spectrum functions (13,14) from which values of $L^X_i$ can be predicted as proposed by Teunissen [25]

$$L^X_u = 0.146 (\lambda_m)_u$$

and

$$L^X_i = 0.106 (\lambda_m)_i \quad \text{for } i=u,w.$$  

(19)

However it must be realized that these predicted scales associated with the empirical spectrum functions are equivalent to the turbulence integral scale obtained from correlation functions only if no large low-frequency velocity fluctuations are present. In the case large low-frequency velocity fluctuations are present and not filtered from the data records, the scales obtained from correlation functions are generally larger in magnitude (see section 6.4).
7. SUMMARY AND CONCLUSIONS

A rather detailed description has been given of a micrometeorological facility consisting of an instrumented 76 m (250 ft) tower located within a 100 m distance from the shore at Wallops Island, Virginia. The instrumentation system consists of cup-vane and temperature instruments mainly used for profile measurements and a hot-film system for turbulence measurements. The data acquisition and handling system for the hot-film instruments is located in an instrumentation trailer located at the base of the tower. The heart of this system is a PDP 11/20 DEC minicomputer which controls the digitization of the data (200 Hz sample rate) and the data transfer onto digital tape. The digitized data have been analyzed on an IBM-370 computer located on the VPI and SU campus.

Data have been acquired with the cup-vane system under moderately strong wind conditions for all wind directions during a 4 1/2-year period. From this data-base mean velocity and mean temperature profiles and associated parameters (roughness length, z_o, and powerlaw exponent, α) have been derived as well as turbulence intensities, σ_u/U and σ_v/U, and turbulence integral scales, L^x_u, L^z_u and L^y_v. Averages of the calculated flow parameters from all data records in each 15-degree sector have been presented. In addition averaged mean velocity ratios V/V_250, turbulence intensities, σ_u/U, σ_v/U, and turbulence integral scales, L^x_u, have been obtained for 11 sectors each with near-uniform upstream terrain. The results provide information about the microclimate at this site under moderately strong wind conditions. This information is graphically presented in
Figures 72 through 75 from which average wind design data for this coastal site can be established. In addition, data have been acquired with the hot-film system for the southerly and northwesterly prevailing wind directions. With this system turbulence parameters such as turbulence intensities, Reynolds stresses, turbulence heat fluxes, integral scales ($L_u^u$, $L_v^v$ and $L_w^w$) and power spectra of the three velocity components have been obtained.

For all observations made at this site under moderately strong wind conditions, truly neutral thermal stratifications have never been encountered throughout the observation height of 76.2 m for any length of time. For westerly wind direction under sunny daytime conditions the measured velocity and temperature profiles suggest that the surface flow at the Wallops Island site is similar to the surface flow observed during the Minnesota experiment [12]. The observed PBL flow at Minnesota is an example of a typical convective boundary layer, a model of which is described in detail in Reference 13. In addition to mechanical and convective turbulence generated in this atmospheric boundary layer, large-scale turbulence due to the interaction of the mixed layer and the capping inversion (entrainment) affects the mean and turbulent surface flow regardless of the wind velocity. However, appreciable deviations from the convective boundary-layer model may occur depending on atmospheric conditions, time of day and wind direction.

It has been observed that just before sunset the daytime boundary-layer flow is modified drastically as a result of the
disappearance of the large-scale turbulence and appearance of a surface-based inversion. Similarly under conditions of low cloud cover combined with precipitation, an inversion below the cloud cover may develop, impeding the regular development of the day-time convective boundary layer. Under these conditions the influence of the large-scale turbulent motions on the flow below the inversion is reduced, resulting in an appreciable reduction in turbulence intensities and turbulence integral scales. Large negative lateral velocity fluctuations or large wind direction fluctuations towards the north have been observed for northwesterly wind directions specifically between 300° and 315°. For winds in this sector larger values of the lateral turbulence intensity and larger turbulence integral scales have been observed than for winds outside this sector but with the same upstream terrain. In addition, turbulence intensities and turbulence integral scales vary during the daytime as the convective boundary layer develops. The above observations have been made under moderately strong wind conditions with hourly mean-wind speeds between 10 m/s and 20 m/s at z=9.1 m. Based on all the observations made for westerly winds at Wallops Island, there is no evidence that similar flow variations in the surface layer would not exist under extreme and potentially damaging wind conditions with velocities in excess of 20 m/s. Consequently at this point in time it cannot automatically be assumed that for extremely strong winds from westerly directions, the PBL flow at the Wallops Island site is similar to the purely shear-generated,
neutral-stratified boundary-layer flow model, which is so often advocated by wind engineers.

The mean and turbulent flow for southerly winds also differs appreciably from that predicted by the neutral boundary-layer model. During the summertime the warm air blowing over the cooler ocean water gives rise to a surface-based inversion of variable height. Depending on the thermal stability, a low-level jet with a maximum velocity occasionally below the highest observation level has been observed. Under extreme stable conditions the turbulence at the two highest observation levels has been observed to vanish completely and generally internal gravity waves may co-exist with the turbulence. Under these conditions the surface layer is very shallow, well below the lowest observation level. Moreover, the flow near the surface will also undergo a modification as soon as the ocean air crosses the beach and experiences an increase in surface roughness and surface temperature. These modifications of the surface flow manifest themselves in the form of a developing internal boundary layer (IBL) which at the tower location is between 15 m and 30 m in height, depending on the change in surface temperature and the overland development distance which varies with wind direction.

The conclusions of the boundary-layer experiment at Wallops Island can be summarized as follows:

I. Westerly wind directions

1. The observed daytime flow below 76m at Wallops Island is described better by the convective boundary-layer model [13] than by the neutral boundary-layer model.
2. The height at which transition occurs from the logarithmic velocity profile to the mixed-layer velocity profile varies with wind velocity surface roughness and thermal stability.

3. The roughness length, $z_0$, obtained from velocity profiles below the transition are in agreement with predicted values from PBL-flow review papers.

4. The Panofsky relation, $\alpha = z_0 / \ln \sqrt{z_0 z^*}$, is only useful for predicting values of powerlaw exponents for velocity profiles in the surface layer below the elevation where transition to the mixed-layer profile starts.

5. Measured turbulence intensities are generally in agreement with predicted values, except for the lateral turbulence intensities, $\sigma / \bar{U}$, in the northwesterly wind-direction sector $300^\circ < \phi < 315^\circ$. In this sector the turbulence intensities of the horizontal velocity components (u and v) are of the same magnitude.

6. Turbulence intensities of the horizontal components also vary with time of day and atmospheric conditions, or in general with the absence or presence of appreciable low-frequency velocities fluctuating in the frequency range between 0.0015 Hz and 0.02 Hz.

7. The magnitude of the turbulence integral scales depends on the method (direct method or spectral method) by which they are calculated and also on the presence or absence of appreciable low-frequency velocity fluctuations.

8. If appreciable low-frequency content is present and is not filtered from the data records, the turbulence integral scales obtained via the direct method are larger than the predicted values.

9. The turbulence integral scales vary also with time of day, wind direction, surface roughness, and atmospheric conditions such as cloud cover combined with precipitation.

10. The measured vertical integral scales, $L_z^u$ and $L_z^v$ vary with direction of integration but are generally in agreement with predicted values.
11. The ratio $L_x^{x\gamma_{uv}}$ varies generally between 3 and 4 and the ratio $L_u^{x\gamma_{uv}}$ has an approximate value of 2.

12. The daytime turbulence spectra follow the Kaimal model [19] and deviate appreciably from the Von Karman model especially in the low-frequency range.

13. The Von Karman spectral model does not fit the measured spectra if appreciable low-frequency velocity fluctuations are present and are included in the spectral analysis and in the calculation of the variance, $\sigma_1$, and integral scale (direct method).

II. Southerly wind Directions

1. For on-shore winds an IBL develops as the surface air passes the beach and experiences an increase in surface roughness and an increase in surface temperature especially in the summer during daytime.

2. For southerly wind directions warmer air flows over the cooler water creating a surface based inversion which is characterized by a very shallow surface layer, low-level maximum velocity (surface jet), low turbulence intensities, occasional vanishing of the turbulence under extreme stable conditions and co-existence of turbulence and low-frequency internal gravity waves.

3. No simple boundary-layer flow model is available to describe the on-shore flow at the Wallops Island site. Variations in observed velocity and temperature profiles, turbulence intensities and turbulence integral scales are extremely high and can occur within a very short time.

4. Measured velocity spectra (excluding the low-frequency gravity waves) are independent of thermal stability and seem to fit the modified Von Karman spectrum model (16,17) and the Kaimal stable spectrum model (15) extremely well.

As the above conclusions clearly indicate, there is no single and no simple PBL-flow model available to describe the mean and turbulent flow near the surface under moderately strong wind conditions at the Wallops Island site. The presence or absence of appreciable low-frequency velocity fluctuations causes the parameters describing this flow to vary a great deal. The non-uniform surface conditions...
and the presence of the low-frequency fluctuations, either in the convective boundary layer or in the on-shore winds in the form of internal gravity waves, cause the observed surface flow to be quite different from the neutral boundary layer flow model. For the prevailing winds from either the south or westerly directions the experimental results do not show any evidence for the PBL flow to approach the neutral boundary-layer model as the wind speed increases from moderately strong to extreme.

It is assumed that engineers, already aware of uncertainty in modeling the PBL flow, use safety factors in the design of wind turbines to allow for differences in the actual wind environment in comparison with the predictions from the neutral PBL model. The variation of the turbulence intensities and turbulence integral scales, measured under moderately strong wind conditions at the Wallops site, is appreciable. Consequently a great deal of difference may exist between actual measurements and the neutral PBL model. Experimental evidence does not indicate that mean wind and turbulence parameters will conform closer to the neutral PBL-model under higher wind-speed and slightly unstable conditions. The observed differences appear at the lower frequencies which are pertinent to the response characteristics of the larger machines. Therefore, the design of large wind turbines may need an increased safety factor with respect to turbulence at frequencies below about 0.01 Hz.
REFERENCES


34. H. W. Tieleman and S. E. Mullins, "The Structure of Moderately Strong Winds at a Mid-Atlantic Coastal Site (Below 75 m)," Proceedings Fifth International Conference on Wind Engineering, Colorado State University, (1979), II-5, 1-15.


Figure 2: Wallops Island, Immediate Surroundings of the Meteorological Tower.
Marsh, 335m ~ 500m scattered brush

Marsh, 180m ~ 335m scattered brush

Marsh, 180m scattered brush, bunker at 90m

Marsh, 670m ~ 200m scattered brush

Parallel to Wallops Island

Ocean, Aerobee Tower 300m upstream

Ocean, 250m ~ 425m over land

Ocean, 500m ~ 250m over land

In the sector \(140^\circ < \phi < 170^\circ\) two rocket assembly buildings 60m ~ 150m upstream

Ocean, 1100m ~ 500m over land, some small buildings

Parallel to Wallops Island

Marsh, 500m ~ 850m scattered small buildings and brush
Figure 4. The 76.2m (250 ft) Micrometeorological tower at Wallops Island
Figure 5. Afternoon Temperature Profiles for Southerly Winds
Figure 6. Temperature Profiles for Westerly Winds.

- - - Dry adiabatic lapse rate.

- $U_{76.2} = 16.7 \text{ m/s, 12-21-'76, 12:22-13:39}$
- $U_{76.2} = 16.6 \text{ m/s, 1-26-'78, 18:52-19:43}$
- $U_{76.2} = 20.9 \text{ m/s, 8-9-'76, 17:07-18:07}$
- $U_{76.2} = 15.9 \text{ m/s, 1-27-'78, 01:09-02:09}$
- $U_{76.2} = 13.8 \text{ m/s, 1-27-'78, 05:42-06:58}$
Figure 7d. Variation of Mean-Velocity Ratio, V(61.0)/V(76.2) with Wind Direction
Figure 8. Typical Strong-Wind Profiles for Southerly Wind Directions
Figure 9. Typical Strong-Wind Profiles for Westerly Wind Directions
Gradient Richardson Number (5) Evaluated at z=15.2m.
Figure 10. Variation of the Roughness Length, $z_0$, Versus Wind Direction.
Note the larger roughness lengths in the sector $350^\circ-450^\circ$. 
Figure 11. Variation of the Roughness Length, $z_o$, with the Gradient Richardson Number (5) Evaluated at $z=15.2m$
Figure 13. Variation of Power-law Exponent with Roughness Length. Both Based on Velocity Measurements at all Levels,Panofsky's Relation (7) Based on z = 1.5 m and z = 2 m,
Figure 14. Variation of Power-law Exponent with Roughness Length, Both Based on Velocity Measurements Above 45.7m. Panofsky's relation (7) Based on $z_1=45.7m$ and $z_2=76.2m$

--- Panofsky [31] --- Counihan [26] --- ESDU [27]
Figure 15a. Variation of Turbulence Intensity, $\sigma_u/U$, with Direction, $z=15.2m$
Figure 15e. Variation of Turbulence Intensity, $\sigma_u/U$, with Direction, $z=76.2m$
Figure 16a. Variation Turbulence Intensity, σ/UL with Direction z=15.2m
Figure 16d. Variation Turbulence Intensity, $\sigma_u/\bar{u}$, with Direction $z=61.0\text{m}$
Figure 16e. Variation Turbulence Intensity, $\sigma_v/U$, with Direction $z=76.2m$
Figure 17. Variation of Average Turbulence Intensities $\sigma_u/U$ and $\sigma_v/U$ with Height for Two Wind-Direction Sectors.

ESDU [28] ----- Teunissen [25]
Figure 18. Typical Strong-Wind Aerovane Record of Direction and Speed for Northwest Winds, $\phi = 320^\circ$, $U_{10} = 13$ m/s
Figure 19. Probability Density Function of Wind-Direction Fluctuations, $z=76.2\text{m}$, $\sigma_\phi=8^\circ$, $\phi=322^\circ$

--- Gaussian Distribution Function
Figure 20. The Variation of the Vertical Distribution of Turbulence Intensity $\sigma_u / U$, with Time of Day for Westerly Winds
Figure 2.1. Vertical Distribution of Turbulence Intensity, $\sigma_w/U$, for Westerly Winds

Figure 21. Vertical Distribution of Turbulence Intensity, $\sigma_w/U$, for Westerly Winds
Figure 22. Vertical Distribution of the Turbulence Intensity, $\sigma_u/U$, for Southerly Winds
Figure 23. Vertical Distribution of the Turbulence Intensity, $\sigma_v/U$, for Southerly Winds
Figure 25. Variation of Ratios of Average Turbulence Intensity with Wind Direction
Figure 26a. Variation of Turbulence Integral Scale, $L_u^x$, with Wind Direction, $z=15.2m$
Figure 26b. Variation of Turbulence Integral Scale, $L_u^x$, with Wind Direction, $z=30.5m$
Figure 26c. Variation of Turbulence Integral Scale, $L_{u^*}^x$, with Wind Direction, $z=45.7m$
Figure 26d. Variation of Turbulence Integral Scale, $L_x$, with Wind Direction, $z=61.0m$.
Figure 26c. Variation of Turbulence Integral Scale, $L_x$, with Wind Direction, $z=76.2m$
Figure 27a. Variation of Turbulence Integral Scale, \( L_z \), with Wind Direction, \( z = 15.7 \) m.
Figure 27b. Variation of Turbulence Integral Scale, $L_u^+$, with Wind Direction, $z=30.5m$
Figure 27c. Variation of Turbulence Integral Scale, $L_u^z$, with Wind Direction $z=45.7\, m$
Figure 27d. Variation of Turbulence Integral Scale, $l_\text{uf}$, with Wind Direction $\theta$ at 45.7 m

The graph shows the wind direction in degrees on the y-axis, ranging from 0 to 360 degrees, and the integral scale of turbulence, $l_\text{uf}$, in meters on the x-axis, ranging from 0 to 120 m. The data points are represented with various symbols, indicating mean values and maximum and minimum values at different wind directions.
Figure 27f. Variation of Turbulence Integral Scale, $L_u^+$, with Wind Direction $z=61.0m$
Figure 27g. Variation of Turbulence Integral Scale, $L_u^+$, with Wind Direction $z=76.2$ m
Figure 28a. Variation of Turbulence Integral Scale, $L_v^{\uparrow}$, with Wind Direction $z=15.2$ m.
Figure 28b. Variation of Turbulence Integral Scale, $L_{v}^{z}$, with Wind Direction $z=30.5\degree$
Figure 28e. Variation of Turbulence Integral Scale, $L_z$, with Wind Direction $z=45.7$m
Figure 26f. Variation of Turbulence Integral Scale, $L_z^2$, with Wind Direction $z=61.0m$
Figure 29. Variation of the Integral-Scale Ratio $L_x/L_z^2$ for the Three Lowest Observation Levels with Wind Direction. Arrows indicate the direction of integration.
Figure 30. Variation of the Integral-Scale Ratio $\frac{L_u^x}{L_u^z}$ for the Three Highest Observation
Figure 32. Variation of Average Integral Scales, $L_z$ (Cup-Vane) with Height for Two Westerly Wind-Direction Sectors. Arrows on Symbols Indicate the Direction of Integration.
Figure 33. Variation of Average Integral Scales, $L_v^z$ (Cup-Vane) with Height for Two Westerly Wind-Direction Sectors. Arrows on Symbols Indicate the Direction of Integration.
Figure 34. Variation of Average Integral Scales, $L^x$, (Cup-Vane) with Height for Wind-Direction Sector $180^\circ-195^\circ$ (South Winds) $z < 20m + z_0$ and $z > 20m + z_0 = 0.001m$
Figure 35. Variation of Average Integral Scales, $L_u^z$, (Cup-Vane) with Height for Wind-Direction Sector 180°-195° (South Winds).
$z < 20m + z_o = 0.01m$ and $z > 20m + z_o = 0.001m$.

Arrows on Symbols Indicate the Direction of Integration.
Figure 36. Variation of Average Integral Scales, $L_v^z$, (Cup-Vane) with Height for Wind-Direction Sector 180°-195° (South Winds) $z<20m+z=0.01m$ and $z>20m+20m=0.001m$ Arrows on Symbols Indicate the Direction of Integration
Figure 37. Profiles of Average Integral Scales, \( L_u^x \), for Westerly Winds for Different Times of the Day.
Figure 38. Variation of the Integral Scale, $L_u^x$, at $z=15.2$m (50 ft.) with Roughness Length, $z_o$, for all Data Records with a Westerly Wind Direction and $\text{Ri}_{15}>0.1$
Figure 39. Variation of the Interm Scale, \( L_x \), at \( z=45.7m \) (150 ft.) with Roughness Length, \( z_o \), for all data records with a Notherly wind direction and \( R_{15i} > 0.1 \).
Figure 37. Variation of the Integral Scale, $L_z$, at $z=45.7$ m (150 ft.) with Roughness Length, $z_0$, for all Data Records with a Westerly Wind Direction and $\alpha_{15}=0.1$

Figure 40. Variation of the Integral Scale, $L_z$, at $z=45.7$ m (150 ft.) with Roughness Length, $z_0$, for all Data Records with a Westerly Wind Direction and $\alpha_{15}=0.1$
Figure 41. Variation of Integral Scale, $L_v$, at $z=45.7$ m (150 ft.) with Roughness Length, $z_0$, for all Data Records with Westerly Wind Direction and $Ri_{15}>0.1$.
Figure 4. Logarithmic W-spectra for Run 19, a. and b. obtained in the middle-frequency range.}

\[
\log(W_x/u)
\]

- Von Kármán spectrum (14)
Figure 45. Logarithmic w-Spectra for Run 19, $\sigma_w$ and $L_w^X$ Obtained in the High-Frequency Range.
Figure 46. Variation of Average Integral Scales, $L_x$, Obtained with the Hot-Film System (Von Karman Method, High and Middle Frequency Range) and with the Cup-Vane System (Data of the Two Systems Taken Simultaneously), with Height for Southerly Winds.
Figure 47. Variation of Average Integral Scales, $L_x$, obtained with the Hot-Film System (Von Karman Method, High and Middle Frequency Range) with Height for Southerly Winds
Figure 48. Variation of Average Integral Scales, $L_w^x$, Obtained with the Hot-Film System (Von Karman Method, High and Middle Frequency Range), with Height for Southerly Winds.
Figure 49. Variation of Average Integral Scales, $L_u^x$, Obtained with the Hot-Film System (Von Karman and Direct Methods, Middle-Frequency Range) and Cup-Vane System with Height for Northwesterly Winds.
Figure 50. Variation of Average Integral Scales, $L^x_v$, Obtained with the Hot-Film System (Von Karman and Direct Methods, Middle Frequency Range) with Height for Northwesterly Winds
Figure 5.1. Variation of Average Integral Scales, $L_x$, obtained with the Hot-Film System (Von Karman and Direct Methods, Middle Frequency Range) with Height for Northwesterly Winds
Figure 52. Comparison of Integral Scales, $L_u^x$, of Record #16. (Evening Run) (Von Karman and Direct Methods, Middle Frequency Range) Against Average of Daytime Hot-Film Runs (Von Karman, Middle Frequency Range) for Northwesterly Winds
Figure 53. Comparison of Integral Scales, $L_u^x$, Obtained from the Hot-Film System and Analyzed in the Middle- and High-Frequency Range Using the Von Karman Method for Northwesterly Winds.
RECORD OF STREAMWISE VELOCITY COMPONENT,
RUN 19, 250 ft.-LEVEL, $U=13.9$ m/sec, $\sigma_u=1.60$ m/sec,
3-25-77, 14:21:00, $L_x=306$ m

RECORD OF LATERAL VELOCITY COMPONENT,
RUN 19, 250 ft.-LEVEL, $\sigma_v=1.65$ m/sec, $L_x=479$ m

RECORD OF STREAMWISE VELOCITY COMPONENT,
RUN 16, 250 ft.-LEVEL, $U=11.4$ m/sec, $\sigma_u=0.81$ m/sec,
3-23-77, 20:30:00, $L_x=77.9$ m

RECORD OF LATERAL VELOCITY COMPONENT,
RUN 16, 250 ft.-LEVEL, $\sigma_v=0.62$ m/sec, $L_x=23.3$ m

Figure 54. Time Records of Velocity Components. Elapsed Time 55 Minutes
Figure 55. Comparison of Integral Scales, $L_x$, of Record $@16$ (Evening Run) (Von Karman and Direct Methods, Middle Frequency Range) Against Average of Day Time Hot-Film Runs (Von Karman, Middle Frequency Range) for Northwesterly Winds
Figure 56. Comparison of Integral Scales, $L_x$, Obtained from the Hot-Film System and Analyzed in the Middle- and High-Frequency Range Using the Von Karman Method, for Northwesterly Winds
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Figure 59a. Logarithmic u-Spectra Versus Modified Reduced Frequency, $f/f_o$, Analyzed in the High-Frequency Range, South Winds, Unstable Thermal Stratification. $-1.0 < z/L < 0$
Figure 59b. Logarithmic u-Spectra Versus Modified Reduced Frequency, \( f/f_0 \), Analyzed in the High-Frequency Range, South Winds, Stable Thermal Stratification. 
\( 0<z/L<1.0 \)
Figure 59c. Logarithmic $u$-Spectra Versus Modified Reduced Frequency, $f/f_0$. Analyzed in the High-Frequency Range, South Winds, Extremely Stable Thermal Stratification. $z/L>1.0$
Figure 60a. Logarithmic v-Spectra Versus Modified Reduced Frequency, \( f/f_0 \), Analyzed in the High-Frequency Range, South Winds, Unstable Thermal Stratification. 
\(-1.0 < z/L < 0\)
Figure 60b. Logarithmic $v$-Spectra Versus Modified Reduced Frequency, $f/f_0$. Analyzed in the High-Frequency Range, South Winds, Stable Thermal Stratification, $0<z/L<1.0$
Figure 60c. Logarithmic $v$-Spectra Versus Modified Reduced Frequency, $f/f_0$, Analyzed in the High-Frequency Range, South Winds, Extremely Stable Thermal Stratification, $z/L>1.0$
Figure 61a. Logarithmic \( w \)-Spectra Versus Modified Reduced Frequency, \( f/f_0 \), Analyzed in the High-Frequency Range, South Winds, Unstable Thermal Stratification, \(-1.0<z/L<0\)
Figure 61b. Logarithmic $w$-Spectra Versus Modified Reduced Frequency, $f/f_0$, Analyzed in the High-Frequency Range, South Winds, Stable Thermal Stratification, $0<z/L<1.0$
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- Run 19
- $15.2 \text{ m}$
- $30.5 \text{ m}$
- $61.0 \text{ m}$
- $76.2 \text{ m}$

von KARMAN SPECTRUM
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With \( i = u, v, w \) for Westerly Winds. Data Analyzed in  
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Dark Symbols Denote the Data for the Evening Run 16.
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<table>
<thead>
<tr>
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<th>$\phi$ (deg)</th>
<th>$U$ (m/s) at $z$ = 15.2m</th>
<th>$\sqrt{\langle u'^2 \rangle / U_o^2}$</th>
<th>$L^* (m)$ at $z$ = 76.2m</th>
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Note: Type of Profile: S-singie logarithmic profile, K-kink in profile.