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# HEAT TRANSFER IN PIPES Th. Burbach

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#### HEAT TRANSFER IN PIPES

#### Th. Burbach

#### Introduction

"Heat transfer" is the heat exchange which takes place between a fluid and a solid when they have different temperatures. Heat transfer occurs through two different processes: through conduction and through convection of heat. While a heat transfer through unordered movement of molecules occurs in heat conductance, heat transfer by convection takes place through movement of many larger aggregates, which change location and carry their heat with them. In this latter process, one differentiates between "free" and "forced" convection. flow condition results solely from gravity of unequal densities occurring from temperature differences, then one speaks of "free convection". If, on the other hand, the velocity field is determined by pressure differences under diminishing density differences, then we are dealing with "forced convection". this study we shall investigate only heat transfer with forced The great interest in technology for heat transfer explains the large number of investigations carried out in this Records of experiments on heat transfer with heated gases and steam have been made by Groeber [1], Josse [2], Jordan [3], Poensgen [4], Tietschel [5] and Nusselt [6]. There are fewer investigations on heat exchange with fluids flowing through /48\* In this direction, the works of Stanton [7]. Soennecken [8] and Stender [9] should be mentioned. While test results gained by various experimenters on gases agree fairly well, this is not the case for measurements on fluids. explained only through theoretical treatment of heat

<sup>\*</sup>Numbers in the margin indicate pagination in the foreign text.

transfer using similarity observations. Such an investigation shows that heat transfer is independent of Reynolds number  $\frac{\pi d}{\sqrt{}}$  (U = mean velocity in the pipe, d = pipe diameter, v = kinematic viscosity), of the relative test length z/d (z = distance of measuring point from intake), of the relative roughness 🕇 (c approximately = height of roughness element), and of a substance value  $\sigma = \frac{\lambda}{2}$  (# = heat conduction, c = specific heat,  $\mu$  = viscosity). It has a value of almost 1 in gases, but varies greatly with temperature in fluids. Thus, a variable plays a smaller role with gases, a fact which has simplified relationships and theory. In 1910, Prandtl [10] already formulated such a theory for the situation  $\sigma \neq 1$ . He succeeded in deriving a formula for heat transfer in gases. An expansion of this equation also for the situation  $\sigma$  1, i.e., for any fluid, is given in Chapter 2 of this study using a concept from Prof. Schiller based on similarity observations. experiments, discussed in Chapter 3, were needed to test this formula for longer test lengths and to answer the question: "What is the influence of substance value o and, further, of relative test length on heat transfer?"

Chapter One

#### Theoretical Observation

It is customary, for all practical questions of heat transfer to assume a heat transfer number a which is defined by:

$$Q = a \left( \overline{\partial} - \theta_{-} \right) \tag{1}$$

(Q = transferred amount of heat per unit of time and surface,  $\theta$  = mean fluid temperature,  $\theta_w$  = wall temperature). In this formula, amount of heat Q is further determined by the equation:

$$Q = \lambda_w \left( \frac{\partial \theta}{\partial y} \right)_w \tag{2}$$

in which w means that the value of the temperature gradient is

set for  $\frac{\partial \Theta}{\partial y}$  and that pipe wall temperature and/or the temperature of the fluid which is in contact with it and equal to it is set for heat conductivity  $\lambda$ . Since the mean fluid and pipe wall temperature can be measured so that  $\overline{\Theta} -- \Theta_w$  may be considered as known, using (1) and (2) and eliminating Q, one arrives at a suitable formula for heat transfer a, when an easily measurable dimension can be assumed for the value of in equation (2).

Since differential equations of impulse conduction and convection and of temperature conduction and convection are similar in fluids,  $\frac{\partial \Theta}{\partial y}$  can be determined. Reynolds first ascertained the similarity of these two processes, and, based on this, he succeeded in deriving an equation for heat transfer. We shall use such similarity observations here to investigate more generally the question: "When is a temperature field similar to a velocity field?" Prandtl found this to be the case in a system1 where  $\sigma = 1$ . In this way, however, we obtain only an /50 equation for a when  $\sigma = 1$ . If, in the same way, seeking a velocity field similar to the temperature field, we wish to obtain an equation for any o, this will not be possible without additional assumptions, and then only approximately. Below we shall see that experiences with velocity distribution of turbulent atom flow permit us to make such assumptions [11, 12]. First, we must formulate the requirement that temperature dispersion and velocity dispersion at the wall are similar and/or that the dimensionless gradients are equal at the wall. condition is written as:

Since the velocity field is only a function of the Reynolds number, another system could be used instead of this one for the velocity field.

$$\frac{\left(\frac{\partial u_{1}}{\partial y}\right)_{w} \cdot r_{1}}{\overline{u}_{1}} = \frac{\left(\frac{\partial \Theta}{\partial y}\right)_{w} \cdot r_{1}}{\overline{\Theta} - \Theta_{w}}$$
(3)

If the relationship between pressure drop and velocity gradient at the wall is introduced into equation 30:

$$-\operatorname{grad}_{x} p = \frac{2 \mu_{w}}{r_{i}} \left( \frac{\partial u_{i}}{\partial y} \right)_{w}$$
 (4)

then the following is obtained, taking (2) into consideration:

$$\frac{-\operatorname{grad}_{\mathbf{z}'\mathbf{p}\cdot\mathbf{r}_{1}^{2}}}{2\,\mu_{\mathbf{w}}\cdot\mathbf{\bar{u}}_{1}} = \frac{\mathbf{Q}\cdot\mathbf{r}_{s}}{\lambda_{\mathbf{w}}\left(\overline{\boldsymbol{\theta}}-\boldsymbol{\theta}_{\mathbf{w}}\right)}.\tag{5}$$

This equation states that a very definite relationship must exist between pressure decrease and amount of heat per unit of time and surface. In a stationary situation mean velocity maintains its value along the pipe while mean temperature of the fluid eventually nears the wall temperature as the result of the heat released outwardly during flow. According to Prandtl, as much new heat has to be created by heat sources inside the fluid section as the pipe loses, for the temperature field also to attain inertia condition along the pipe, that is, for it to attain a complete pattern with regard to the stationary condition. If we call the yield of these heat sources per volume q, we obtain the following relationship between Q and q:

$$2 r_2 \pi Q = r_2^2 \pi q \text{ oder } : Q = \frac{r_2}{2} q.$$
 (6)

Using (6) one can now write equation (5) in the following form:

$$\frac{-\operatorname{grad}_{x}p}{q} = \frac{r_{z}^{2}\overline{u}_{1}\mu_{w}}{r_{1}^{2}(\overline{\Theta} - \Theta_{w})\lambda_{w}} \tag{7}$$

Equation 7 represents the relationship which must be satisfied between pressure gradient and heat yield inside the fluid and/or converted amounts of heat, so that gradients on the wall are "similar."

This relationship can be obtained from differential equations of impulse conduction and convection and of temperature conduction and convection formulated in dimensionless variables u\*. x\*, etc. They are given here:

$$\frac{\varrho_{1}\overline{u}_{1}^{2}}{r_{1}}\left(u_{1}^{*}\frac{\partial u_{1}^{*}}{\partial x_{1}^{*}}+v_{1}^{*}\frac{\partial u_{1}^{*}}{\partial y_{1}^{*}}+\ldots\right) = -\operatorname{grad}_{x} p + \frac{\mu\overline{u}_{1}}{r_{1}^{2}}\left(\frac{\partial^{2} u_{1}^{*}}{\partial x_{1}^{*2}}+\ldots\right)$$

$$\frac{c}{r_{2}}\frac{\varrho_{2}\overline{u}_{2}}{r_{2}}\frac{(\overline{\theta}-\theta_{w})}{cx_{2}^{*}}\left(u_{2}^{*}\frac{\partial\theta^{*}}{\partial x_{2}^{*}}+v_{2}^{*}\frac{\partial\theta^{*}}{\partial y_{2}^{*}}+\ldots\right) = q + \frac{\lambda(\overline{\theta}-\theta_{w})}{r_{2}^{*}}\left(\frac{\partial^{2}\theta^{*}}{\partial x_{2}^{*2}}+\ldots\right)$$
(8)

The first equation is true for the velocity field of a flow, the second for the temperature field of a second flow which is similar to the first field.

With equation (7) a comparison of the right side of both differential equations, which contains the viscosity and/or heat conduction component and relate primarily to the processes near the wall apparently because of the laminarity there, shows immediately that one obtains the relationship originating there between grad<sub>x</sub> p and q for both components of the right side through the similarity statement.

All the differential equations show, further, that condition (7) can be satisfied only when the following ratio is simultaneously true:

$$\frac{-\operatorname{grad}_{x} p}{q} = \frac{\varrho_{1} \overline{u}_{1}^{2} \cdot r_{z}}{r_{1} c \varrho_{z} \overline{u}_{z} (\theta - \theta_{w})}.$$
 (7a)

This statement is acceptable only under the condition that the velocity fields of both flows are similar, that is, that at corresponding points, u\*1 = u\*2, etc., everywhere. Then and only then can the convective components act everywhere like the expressions in front of the parentheses. The condition mentioned above simply means that the Reynolds number in both cases are must be the same. This does not give us answer to our question. As a result, we make the obvious assumption that we may limit the aforementioned requirement of similarity of both velocity fields

to the turbulent atom, since the inertia components involved here are the most essential item. The requirement that the velocity profile be similar in the turbulent atom, independent of the Reynolds number, is actually satisfied to great extents for the Reynolds number. It suffices to point to the reliability of the Prandtl-Karman 1/7 exponent law of velocity distribution. It justifies the similarity statement of equation (7a).

Since (7) and (7a) must be satisfied simultaneously, if velocity and temperature fields are to be entirely similar, the following condition must be observed:

$$\frac{r_{2}^{2}\overline{u}_{1}\mu_{w}}{r_{1}^{2}(\overline{\Theta}-\Theta_{w})\lambda_{w}} = \frac{\varrho_{1}\overline{u}_{1}^{2}r_{2}}{r_{1}c\varrho_{2}\overline{u}_{2}(\overline{\Theta}-\Theta_{w})} \qquad \text{or}$$

$$\left(\frac{\varrho\overline{u}r}{\mu_{w}}\right)_{1} = \left(\frac{c_{1}\varepsilon\overline{u}r}{\lambda_{w}}\right)_{2}$$

$$\text{Reynolds}_{1} = \text{Peclet}_{2} \qquad (9)$$

or

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That is: the velocity field of a flow (system 1) is similar to the temperature field of another flow (system 2) if the Reynolds number for system 1 is equal to the Peclet number for system 2. Using this similarity law: "Reynolds = Peclet" makes it easy to establish a formula for heat transfer which is true for all fluids. The foregoing considerations showed that the per-unit volume and -time heat produced, q, must stand in a definite ratio to pressure gradients to guarantee similarity of both profiles. According to equation 7a:

$$q = -\operatorname{grad}_{x} p \frac{r_{1} c \varrho_{2} \overline{u}_{2} (\partial - \theta_{x})}{\varrho_{1} u_{1}^{2} \cdot r_{2}}$$
(10)

Considering equations (1) and (6) we obtain the following equation from (10) for a:

$$\alpha = -\operatorname{grad}_{x} \operatorname{p} \frac{\operatorname{c} \varrho_{z} \overline{\operatorname{u}}_{z} \operatorname{r}_{1}}{2 \varrho_{z} \overline{\operatorname{u}}_{z}^{2}} \tag{11}$$

so that for the dimensionless heat transfer number  $\frac{ad}{\lambda}$  there results:

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$$\frac{a \, d}{\lambda} = \frac{\gamma}{4} (Pe') \frac{c \, \varrho_1 \, \overline{u}_1 \cdot d}{\lambda}$$

$$\frac{a \, d}{\lambda} = \frac{\gamma}{4} (Pe) \cdot Pe. \tag{12}$$

in which  $\psi$  represents the resistance coefficients. Using Blasius' value for  $v = \frac{0.1582}{\sqrt{P^2}}$ , we obtain:

$$\frac{a \, \mathrm{d}}{\lambda_{\infty}} = 0.03955 \, \left( \frac{\overline{\mathrm{u}} \, \mathrm{d} \, \overline{\varrho} \, \overline{c}}{\lambda_{\infty}} \right)^{\frac{3}{4}} \tag{12a}$$

The indices in this formula should indicate for which temperatures with great temperature differences the separate material values are to be inserted--according to the meaning they take on from heat transfer.

Equations (12) and (12a) represent the heat transfer law for fluids which we are seeking. Special equation (12a) is, of course, only valid when the conditions underlying the derivation are satisfied. The distance from the test length to the measuring point is primarily long enough here to guarantee the validity of Blasius' law. An experimental proof of this theoretical formula can be expected only from heat transfer numbers, which are measured far enough from the intake.

#### Chapter 2: Experimental Investigations

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## a) Description of the Experiment Apparatus

The test apparatus depicted in Figure 1 has proven after lengthy preliminary tests to be very suited to answer the questions posed in our introduction and to test the heat transfer laws which we have just derived. The test apparatus permits heat transfer numbers to be measured in very different distances from the intake.

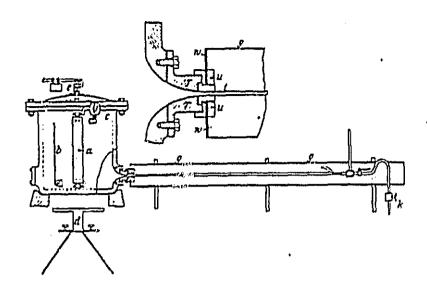
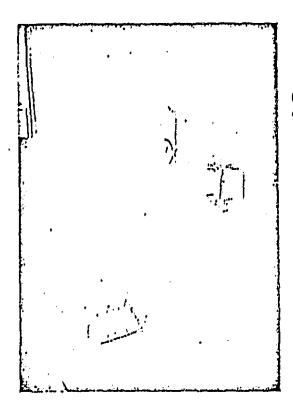


Fig. 1 and la: Test apparatus

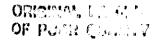
A large test length makes it possible to test the theoretical formula from the previous chapter. By gradually changing the distance from the intake, the influence of the test length could by investigated. By changing the initial temperature in the vessel and the flow speed in the test pipe, tests could be carried out on the influence of the dimensions "Reynolds" and "Peclet" and  $\sigma = \frac{\lambda}{cM}$  on heat transfer numbers. The heat flow always traveled water-to-wall, since hot water flows through a cold /55 pipe in the test apparatus. To calculate heat transfer number, the following dimensions had to be measured in accordance with the definitions given in the previous chapter: transfered amount of heat along a given measuring section, temperature inside the pipe wall, mean fluid temperature, and mean flow velocity of the water in the pipe. The transfered amount of heat could be calculated from the variation of the mean fluid temperature for the involved measuring section.



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Fig. 2: Test apparatus

A gas burner in a steel cast vessel with an inner diameter of 50 cm heated water to the desired temperature. The vessel was cast by the Leipzig firm Max Jahn and possessed, as can be seen from Fig. 1 and the photographic depiction in Fig. 2, various /56 control instruments, such as: water stand glass a, manometer c, and safety valve e. A mercury thermometer b, bent at a right angle, determined water temperature in the vessel. After its installation in the vessel, the thermometer was calibrated with a normal thermometer. The large heat capacity of the vessel and a sensitive setting on the gas burner d made it possible to regulate the water temperature to 1/10th of a degree. The vessel was connected to the Institute's compressed air line (Fig. 2f) to attain starting temperatures over 100 degrees and also to obtain a large velocity range in the test pipe. The highest attainable flow-through velocity 5 m/sec was established by a high pressure of 6 atmospheres.



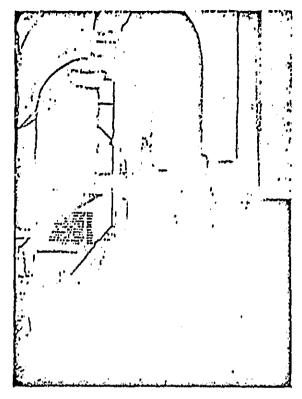


Fig. 3: Test apparatus

An electric heating device was erected to shorten the 157 heating time, which amounted to several hours when using gas and a full vessel. Tests to heat the vessel water directly using a nickel wire resistance were unsuccessful. On the other hand, an electric circulating heater from Loki-Works in Offenbach worked Kettle water traveled through a hot water pump a in very well. Fig. 3 (produced by Schwada, Erfuhrt) to the cirulating heater (7 kW) and then flowed back to the vessel. When the desired vessel temperature was nearly reached, the heater and pump were shut The starting temperature was regulated by the sensitivity settings on the gas burner. The regulator on gas burner d is indicated in Fig. 1. The electric heating device is not shown, to avoid confusion in the drawing. In the photograph of the entire device in Fig. 3 the pipe lines of the circulating heater can be seen.

In connection with the description of the vessel, the heavy rust formation in the vessel should be mentioned here, since it can cause disturbances when the device is put on line. A lead or chrome coating of the vessel would have made it too heavy to take out of the test structure. The only solution was to paint all of the parts coming in contact with water with a rust protector on location. After a number of unsuccessful attempts with minium, lacquer paint and other rust proofers on the market, Krusta Nera enamel lacquer from the firm Heyn & Manthe, Berlin, proved to be effective as a long-term rust proofer for the vessel.

A precision brass pipe, 2 m long and with 5.0 mm l.W. and l.O mm wall thickness, was used for test pipe. A small intake converter (t in Fig. 1) was welded to one end. Using a clamping nut u, it was bolted to a larger intake converter T fastened securely onto the vessel. The two funnels were screwed into each other smoothly. The test pipe, as seen in Fig. 1, was placed in a long zinc trough g, which was filled with ice water during the test. It guaranteed a well-defined outside temperature for the trough g in Fig. la was screwed onto the vessel at the afortmentioned intake converter T. Good heat insulation at w was of particular importance. Further, it was necessary that the /58 thermic effect of the ice water begin exactly at the beginning of the pipe to permit a clear determination of the test length. Details of the apparatus, which satisfied all requirements, can be seen in Fig. la.

The test pipe had to be straightened very precisely during measuring, since, as tests had shown, even a small sag in the pipe had a substantial effect on heat transfer. A silver-constantan thermoelement determined pipe wall temperature. Its thermal power was measured with a sensitivity of 10<sup>-4</sup> Volts by a so-called tower instrument from the firm Siemens & Halske. Installation in the pipe wall required great care, so that heat was not drawn from the measuring place by the element itself, and

the geometry of the pipe wall was not altered. A short description of the construction with references to Fig. 4 is in order here, since the apparatus is thermally efficient and has

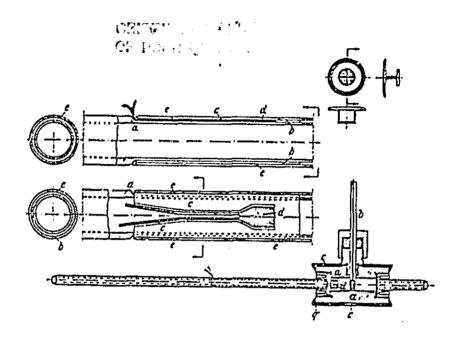


Fig. 4 (center), 4a (above), 4b (below): Measuring points.

proven itself quite well in every aspect. The two silver constantan wires, each 3/10 mm thick, were soldered to each other and the soldering bead was hammered out to a thickness of 4/10 The soldering spot was cut to fit installation (d in Fig. 4, 4a, 4b). To bring this thermoelement as close as /59 possible to the inside of the pipe wall, this wire was stripped from point a to the end of the test pipe in a length of 6.5 cm with a wall thickness of 3/10 mm. A further reduction proved impossible because of strength limitations. A 4/10 mm thick, notched casing b was clamped on the tapered pipe piece. electrically insulated thermoelement c-d fit into the notch. clamping on another casing e the original wall thickness of 1 mm was restored throughout and the thermoelement simultaneously closed completely to the outside. This installation permitted the thermoelement wires to go 2 cm into the pipe wall so that the measuring point would not lose heat to the element itself.

A mercury thermometer measured fluid temperature in the pipe. Its scale was calibrated against a normal thermometer, so that the correct temperature was indicated when the mercury container was rinsed with water. A device, depicted in Fig. 4b, was constructed so that this thermometer indicated the mean temperature of a precisely given cross section which was necessary to determine the test length. This device should be described here briefly. A thick-walled measuring body, which also secures the thermometer b, is wrapped with insulation band c and protects the test pipe from the cross section q on up against heat losses, so that a drop in the mean temperature can no longer take place. A twisting, brass water mixer d is located in the insulated pipe piece in front of the fluid thermometer. Its form can be seen in Fig. 4a. It causes good mixing of the water so that the thermometer actually indi ates the mean temperature, Two regulator valves established the desired flow-through speed. A rough setting was produced by the simple metal ball faucet shown to the right of the fluid thermometer in Fig. 1. A finely turned screw (k in Fig. l) permitted a more exact regulating by continuously changing the flow-through resistance. flow-through resistance. The mean flow-through temperature u in the test pipe could be determined by timing the flow-through mass M obtained in t sec according to the equation:

$$r^t \pi \varrho \overline{u} = \frac{M}{t}$$

The Helmhotz Society provided the funds for the equipment /60 and apparatus described here. Without their generous assistance this project would not have been possible, and we thank them for it.

b) Execution of the Tests: Measuring Accuracy and Test Results

Before we present the results of the measurements, we shall describe the tests for determining heat transfer numbers briefly.

The actual measurements could begin after regulating the starting temperature in the vessel and filling the ice water trough. First, the stretching device with 20 kg tractive force was activated to straighten the test pipe. Then, the compressed air pressure in the vessel was set to produce approximately the desired flow-through velocity. The exact setting was regulated by the fine setting device at the end of the test pipe. constant discharge of the safety valve, even during the test, permitted a very good constant of the mean flow-through velocity, which was of great importance to measuring accuracy. Heat exchange stabilized about 20 to 30 seconds after the measurements This could be recognized from the constant setting on the fluid thermometer. The water mass emerging in about 50 seconds was timed to determine the mean flow-through velocity. indicator instrument for pipe wall temperature and the fluid thermometer were read a number of times during the timing period. The timed water mass had to be weighed on a platform scale immediately following the test, since the hot water evaporated very rapidly.

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The mercury thermometer settings could be read with a precision of 1/10 degree, if the flow-through velocity in the test pipe was beyond the critical range. Such an exact determination of pipe wall temperature was not possible because of the limited sensitivity of the indicator galvanometer. Reading errors during measuring amounted to ± 3/10 degree, but multiple readings reduced this error factor by 1/10 degree. After each measurement the ice water mixture in the trough was replenished, and the melted water was removed from time to time. The length of one measurement, including all preparations, amounted to about 1/4 hour; an average of 20 tests could be made per day.

The sequence of measurements was already prescribed by the test apparatus. As can be seen in Fig. 1, the apparatus had only

one measuring point for fluid velocity at a certain distance from the vessel, since installation of additional fluid temperature measuring points would have disturbed the construction. <u>/61</u> To measure the temperature change along the pipe for calculating the transferred amount of heat, it was necessary to move the fluid temperature measuring place along the pipe, that is, to move it to another distance from the vessel. The easiest way to achieve this was to disconnect the pipe from the vessel. this procedure only provided a shortened distance from the vessel, the measurements proceeded in the following fashion: First, the fluid and pipe wall temperature independence of the mean flow due to velocity was determined at a constant initial temperature in the vessel and with the largest test length having 400 diameters. When this independence was ascertained at about 40 test points in the velocity range of 5-500 cm/sec, the same tests were carried out at three other vessel temperatures to increase the measuring range. Thus, the influence of initial temperature on heat transfer could be ascertained. change the relative test length, a piece of pipe was cut from the vessel, and the same measurements were carried out at the same four initial temperatures. In this way the test length was varied seven times. Each time the pipe was cut, it was thoroughly cleaned inside and outside to avoid any obstructions. Two sets of curves were obtained for each of the four initial temperatures in the vessel: the fluid and the pipe wall temperature independences of the mean flow-through velocity at seven different test lengths. In all sets of curves the abscissa indicates the flow-through velocity, the ordinate indicates the temperature of the measuring points. The parameter was the relative test length. The curves may be used to obtain the decrease in fluid and pipe wall temperature along the pipe independently of the flow-through velocity at four different initial temperatures in the vessel.

At the beginning of the tests, the pipe length up to the reference point for the fluid temperature (cross section q in Fig. 4b) amounted to 200 cm. At a pipe diameter of 0.5 cm the fluid temperature measuring point was 400 diameters away from the intake. The corresponding test length for pipe wall temperature, however, amounted to only 390 diameters, since the soldering bead of the thermoelement lay exactly 10 diameters in front of the fluid temperature measuring point. The test lengths for the other two temperature measuring points are given in Table 1.

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TABLE I.

RELATIVE TEST : LENGTH FOR

Pipe Wall	Temperature	Fluid Temp	Fluid Temperature	
Measuring	Point	Measuring	Point	
	390		400	
	290		300	
	210		220	
	140		150	
	90		100	
	50		60	
	20		30	

The course of the fluid and pipe wall temperature for turbulent flow condition was determined along the pipe at five different flow-through velocities for each of the four initial temperatures and recorded in the graphs in Figures 5 - 9. (Kettle temperatures 69.2 degrees, 85.5 degrees, 101.8 degrees, 118.0 degrees; velocities 100 cm/sec; 104 cm/sec, 200 cm/sec, 300 cm/sec, 500 cm/sec.) A numerical record of these results is to be found in Table II, in which test results for laminar and unsteady flow condition are given.



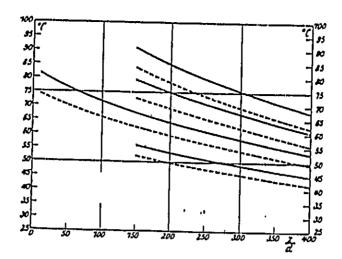


Fig. 5: Course of fluid and pipe wall temperature along pipe at 100 cm/sec mean flow-through velocity.

Solid line = fluid temperature; dotted line = pipe wall temperature; parameter: vessel water tempterature.

Since the per-second heat loss of the fluid flow in any pipe element of length dz must equal the amount of heat released outwardly at the same time, the following equation results:

$$r^2 \pi \overline{u} \overline{\varrho} \overline{c} d\theta = a 2 r \pi d z (\overline{\theta} - \theta_w).$$



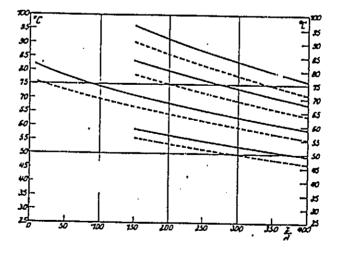


Fig. 6: Course of the fluid and pipe wall temperature along pipe at 140 cm/sec mean flow-through velocity.

Solid line = fluid temperature; dotted line = pipe wall temperature; parameter: vessel water tempterature.

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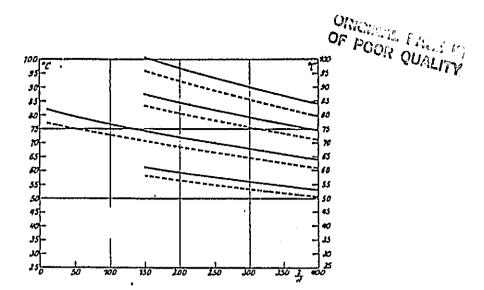


Fig. 7: Course of the fluid and pipe wall temperature along pipe at 200 cm/sec mean flow-through velocity.

Solid line = fluid temperature; dotted line = pipe wall temperature; parameter: vessel water tempterature.

One obtains the following relationship for a:

$$\alpha = \frac{1}{2} r \overline{u} \frac{\overline{e} c}{\overline{e} c} \frac{d \overline{\theta}}{dz} \cdot \frac{1}{(\overline{\theta} - \theta_w)}$$

The heat transfer numbers given in Table II are calculated according to this formula. The value of  $\theta$  --  $\theta_w$  can be taken directly from the curves for individual test lengths. (64) By placing a tangent on the fluid temperature curve we obtain the value  $\frac{d\,\overline{\theta}}{d\,z}$  for a certain test length. The curves had to be drawn in very large scale for this purpose to obtain enough precision. Since this curve gives the change of the fluid temperature with the pipe length, the tangent of the slope angle of the tangent is the value  $\frac{d\,\overline{\theta}}{d\,z}$  we are looking for. Of course, the scale ratio has to be taken into consideration for it.

The given a values in strict accordance with the form of their calculation are valid only for an infinitely small pipe length. A differential a is given which is valid for only a very definite test length on which the calculation is based. This is contrary to the heat transfer numbers related to data in literature where mean values are represented by a finite pipe

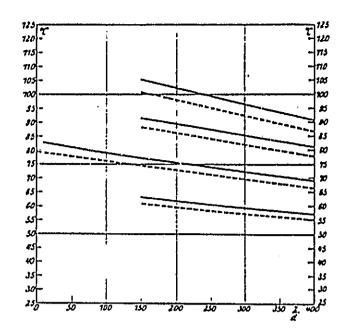
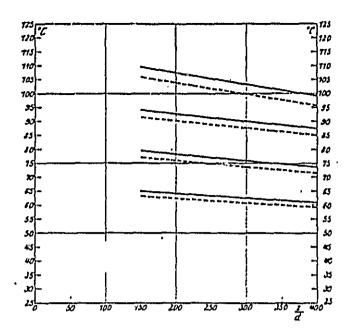


Fig. 8: Course of the fluid and pipe wall temperature along pipe at 300 cm/sec mean flow-through velocity.

Solid line = fluid temperature; dotted line = pipe wall temperature; parameter: vessel water tempterature.

length. For this reason, the procedure described here enables us to calculate heat transfer numbers for any test length and is particularly useful when the influence of the test length /65 is determined by heat transfer number. The influence of radiation was not taken into consideration in my test material, since evaluation showed this influence was smaller than 1/10%, even in the maximum situation.



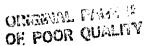
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Fig. 9: Course of the fluid and pipe wall temperature along pipe at 500 cm/sec mean flow-through velocity. Solid line = fluid temperature; dotted line = pipe wall temperature; parameter: vessel water tempterature.

# c) Discussion of Measurements and Comparison to Theory

An exact theory of heat transfer for laminar flow condition was formulated by Nusselt [13] in 1910, and handled in detail in the book by Groeber [14]. Nusselt's investigation found that, for large test lengths, the dimensionless formulated heat transfer number  $\frac{a\cdot d}{2}$  assumes the value 3.65 independent of flow velocity.

If one plots the dimensioneless Peclet number  $\frac{u \log c}{v \log c}$  as abscissa  $\frac{66}{66}$  essentially being a measure of velocity, and the dimensionless heat transfer number  $\frac{a \log c}{2}$  as ordinate, a line parallel to the abscissa is obtained as the theoretical curve for laminar flow condition. Using the equation  $\frac{a \log c}{2} = 0.0395$ . Possible for the turbulent condition likewise to be given a theoretical curve for large test lengths.



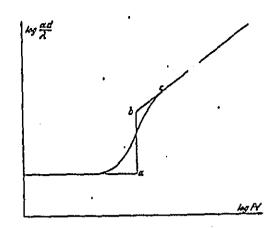


Fig. 10: Theoretic course of heat transfer numbers.

In a logarithmic coordinate system with Peclet as abscissa and  $\frac{ad}{2}$ as ordinate, this curve is a straight one. Its slope angle arphi is tangent  $\varphi = 3/4$ . If both straight lines are entered in a logarithmic coordinate system, the following theoretical picture, given in Fig. 10, is obtained for heat transfer with laminar and turbulent flow. For small Peclet values left of point a in Fig. 10 laminar flow prevails and, for this reason, and is constant here. For large Peclet numbers right of point b the turbulent flow is completely developed and  $\frac{a \cdot \alpha}{3}$  is proportional to 3/4 of the Peclet exponent. For the boundary situation of very great test lengths, the transfer from laminar to turbulent values must occur very acutely, as represented in Fig. 10 by the straight line a--b. A totally, correspondingly abrupt transfer is obtained in a resistance coefficient-Reynolds number diagram for the increase of resistance coefficients resulting from laminar t turbulent values for large test lengths [15]. For smaller test lengths the transfer does not occur so suddenly, but is rather more or lessed blurred. For even with laminar flow intake disturbances will not yet be completely faded, and these cause the heat transfer number to move above the theoretical

horizontal at an earlier point. On the other hand, turbulence is not yet fully developed in small Reynolds numbers, also as the

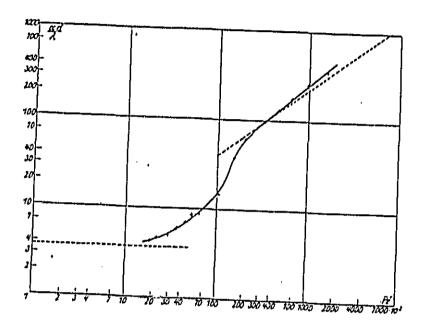


Fig. 11: Experimental values for z/d = 400 with both theoretical straight lines.

result of the short intake. Therefore, the theoretical straight line is attained only at higher values of  $Pe = \frac{Rey}{\sigma}$ . This causes the heat transfer numbers left of point c to have to curve down from the turbulent straight line to come closer to the laminar straight line. This consideration necessarily leads to a curve with a turning point for the transfer range. This /68 curve is drawn into Fig. 10. An experimental confirmation of this theoretical concept should be expected only from measurements which are made at a large distance from the input. For this reason, Fig. 11 contains my measuring results for the greatest test length of 400 diameters together with both theoretical straight lines.

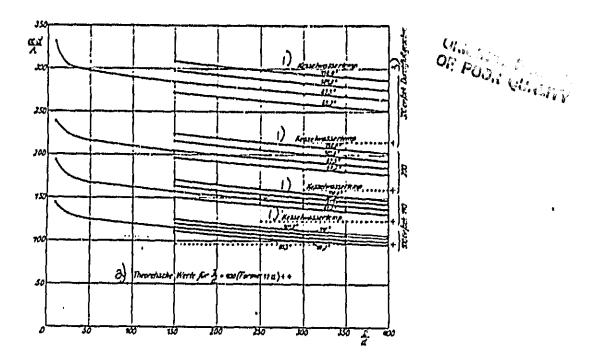


Fig. 12: Experimental course of dimensionless heat transfer number along pipe at four velocities and four vessel temperatures. Key: 1) Kettle water temperature

- 2) Theoretical value for z/d = 400 (formula 12 a) + +
- 3) Flow-through velocity

One recognizes immediately that the test results confirm theoretical considerations. In laminar range the heat transfer numbers do not reach the theoretical value completely, however, a gradual approximation to the straight line seems sure. complete correspondence with the previous considerations, the test values lie on a curve with a turning point in the transfer The fact that the test points for the turbulent flow condition do not agree completely with the theoretical straight line probably has to do with severe thermic disturbances coming from the vessel and not faded completely at these test lengths and for that reason causing an increase in heat /69 transfer numbers. The correctness of this interpretation is verified by Fig. 12, which reproduces the experimentally determined cause of the heat transfer number with the pipe length at four vessel temperatures. It can be seen clearly that the heat transfer numbers at high vessel temperatures, that is, with greater thermic disturbances, assume higher values as test length increases and come closer and closer to the theoretical

The course of these curves, therefore, allows us toexpect that the calculated and the measured test values also agree for higher vessel temperatures with correspondingly larger The values calculated here lose their meaning with test lengths. smaller test lengths, since, as corresponding measurements showed, the Blasius law is no longer valid for them. in these cases are given only to emphasize the approximation of test values to theoretical values. For test lengths which are not too short, measured deviations from Blasius' law are so small that they do not suffice to explain the large number of heat transfer numbers observed as deviations from theoretical law. is quite apparent that the development of the final temperature profile still must be influenced substantially by the dimensionless  $\sigma_{2}\frac{\lambda}{u}$ . It is easy to overlook the fact that, ceteris paribus, greater specific heat requires a higher test length for the temperature profile. This probably explains the fact that measurements for gases ( $\sigma = 1$ ) are substantially less able to show this effect than are our measurements for liquids, for which the value of o is substantially smaller than 1.

Before we consider my measurements on short test lengths, we shall compare a quite recently proposed theory of Prandtl's [16] on heat transfer for turbulent pipe flow and my tests at 400 diameters test length. As already pointed out in the anticipation to this study, this new theory from Prandtl compliments his earlier work, in which the relationship of velocity on the inside of the boundary level to the middle velocity in the pipe still remained undetermined. In his new theory Prandtl now finds the following formula for the dimensionless heat transfer number:

$$\frac{a \cdot d}{\lambda} = 0.0395 \frac{(2 \text{Rey})^{\frac{2}{3}}}{\sigma + 1.6 (1 - \sigma) \text{Rey}^{-\frac{1}{3}}}$$

According to Prandtl's own words, the number factor 1.6 in the comminator is very uncertain in this equation and most likely may be determined from heat transfer observations. If one

follows this suggestion and ascertains this number factor from my test material with 400-diameter test length, then a value of 0.4 is obtained. In Fig. 13 the Prandtl equation with this number factor is given for the  $\sigma$  values 1/4, 1/2, and 1. Furthermore, my test value for  $\sigma$  = 1/4 is included. As one sees, the measuring points correspond quite well to the Prandtl curve for  $\sigma$ 

= 1/4.

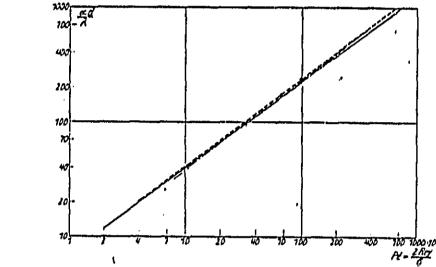


Fig. 13: Formula from Prandtl.

Number factor 0.40; for  $\sigma = 1/4$  -- . --;  $\sigma = 1/2$  -- -- ; for  $\sigma = 1$  ---- identical with Schiller.

Experimental values for  $\sigma = 1/4$  + + +

Further, it is also very noteworthy that, for nearly all possible  $\sigma$  values from 1/4 to 1 with this number factor, the Prandtl curves hardly differ from the theoretical straight lines developed here. Both theoretical curves for every number factor for  $\sigma$  = 1 agree, as can be seen immediately from Prandtl's formula. As seen, as well, from Fig. 13, the maximum deviation of the Prandtl curves amounts to 8% for the remaining  $\sigma$  values in the large Peclet range of 6000 to 600,000. This small deviation is present, however, only for the number factor 0.4. Figures 14 and 15 show clearly how inserting other number values into the Prandtl equation moves this deviation up or down.

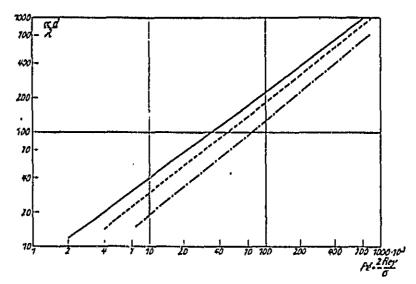


Fig. 14: Formula from Prandtl.

Number factor 1.50; for  $\sigma = 1/4$  -- . --;  $\sigma = 1/2$  - - - 
for  $\sigma = 1$  ----- identical with Schiller.

Experimental values for  $\sigma = 1/4$  + + +

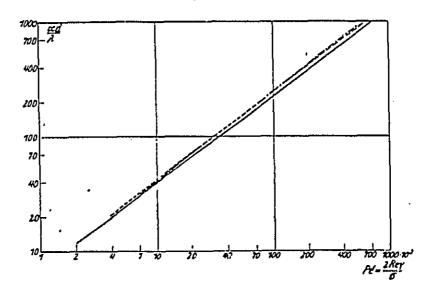


Fig. 15: Formula from Prandtl.

Number factor 0.30; for  $\sigma = 1/4$  -- . --;  $\sigma = 1/2$  - - - - :

for  $\sigma = 1$  ----- identical with Schiller.

Experimental values for  $\sigma = 1/4$  + + +

In Fig. 14 the theoretically resulting number value 1.6 is  $\frac{72}{1}$  inserted, in Fig. 15 the value 0.3. From these curves we see, as

well, that the influence of  $\sigma$  on heat transfer with the Prandtl curves is very much dependent on the dimension of the number factor. This is contrary to the formula given here, in which  $\sigma$  occurs only in the combination  $\frac{Rey}{\sigma}$ . One advantage of our theory, it seems to me, is that there is no uncertain factor in it, as is the case with Prandtl's theory. Only new tests with large test lengths can ascertain which of the two formulas better represents the truth. These tests also must measure the pressure drop to determine the valid resistance law and must demonstrate increased measuring precision.

My results, also for smaller test lengths, are reproduced in Fig. 16 (Table). Not only the two theoretical straight lines are given, but also partial comparisons of test results from Stender and Stanton. I cannot explain why Stender and Stanton's test results are substantially lower than my measurements. Substantially closer to our results are Nusselt's test results for compressed air and other gases which practically agree with our measurements for  $\frac{Z}{d} = 400$ . This might seem surprising since the mean test lengths in Nusselt's tests amounted to only about 50 diameters. Nusselt's values are lower than ours relative to the same test lengths. The reason for this may lie in the extension of the starting stretch by reducing the  $\sigma$  value in our experiment.

Establishing a heat transfer law also for small test lengths would advance technology greatly, since, in practice, primarily heat transfer with small test lengths occurs. This is very difficult, however, since the number of independent dimensions influencing the heat transfer multiplies with the transfer. Besides the relative test length, another variable is the dimension of the intake disturbances governed by free convection. For a numerical determination of these disturbances the velocity field with free convection must be known. Nusselt [17] has shown that this velocity field is dependent on the following two \(\frac{73}{2}\) dimensionless factors:

on  $\sigma = \frac{\lambda}{c\,\mu}$  and Grashof  $Gr = \frac{n^3\,g\,(T_W - T_H)\,\beta}{r^2}$  (a for us = about vessel radius, g = earth's acceleration,  $T_W - T_H = t_H =$ 

To simplify matters, only the large "Grashof" will be considered for calculating the intake disturbances in the vessel. Since the heat transfer formula must be converted into the law derived in Chapter 1 before it can be established for the boundary case of infinitely large test lengths, it is written here in the following form:

$$\frac{a\,d}{\lambda} = 0.0395 \left(\frac{\overline{u}\,d\,\overline{\varrho}\,\overline{c}}{\lambda}\right)^{\frac{1}{4}} \cdot e^{0.02275 \cdot 10^{-6} \frac{G\,r \cdot d}{k}} \tag{13}$$

The values of "Grashof" at the four vessel temperatures were determined by measurements of the temperature difference between vessel wall and fluid and are given in Table 3 with the number material needed for calculation. The number factor in the exponent of equation (13) was determined empirically. Using this equation, it was possible to represent the test results for 200-to 400-diameter test lengths for all four vessel temperatures with sufficient precision. The values of  $\frac{\alpha d}{\lambda}$  calculated using formula (13) are given in the last column of Table 2. Due to the complexities of the relationships in the starting area, the equation imparted here, in spite of its dimensionlessness, serves only for orientation and, as such, has no universal validity.

### Summary of the Results

1. In this study, the heat transfer from hot water to a cold copper pipe in laminar and turbulent flow condition was determined. The mean flow-through velocity in the pipe, the relative test length and the initial temperature in the vessel were varied extensively during the tests. The measurements confirm Nusselt's theory for large test lengths in laminar range.

- 2. By establishing a similarity law for a temperature and velocity field for turbulent flow condition, a new equation was derived for heat transfer for large test lengths. This equation agrees satisfactorily with the measurements for large test lengths.
- 3. The test results also were compared with the new Prandtl formula for heat transfer. The value of the number factor, still uncertain in that equation, resulted from measurements at 0.4. Measured values and those calculated with this number agreed very well.
- 4. The influence of intake disturbances could be determined by the dimensionless "Grashof". Using an equation, it was possible to represent the test material for 200- to 400-diameter test length at four different vessel temperatures.

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Tables.
Table II.\*

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ū	$\overline{\boldsymbol{v}}$	θ₩	$\ddot{\theta} - \theta_{\kappa}$	ij . ē	d z	u	c	
em	0.0	O !!	20	CA)	Co	CAL	CAL	
iec	C"		Cu	cm1 Co	em	еш³ н-с Со	E Co	
Har townstan			z/d	= 400	/. Carrie			
5,0	6,6	4,2	2,4	1,0022	0.014	0,0115	1,0025	
6,0	9,2	6,0	3,2	1,0012	0,053	0.0125	1,0016	
8,0	12,9	8,7	4,2	0,9998	0,057	0,0136	1,0005	
30,0	16,4	11,1	5,3	0,9985	0,069	0,0162	0,9997	
12,5	20,0	13,7	6,3	0,9972	0,077	0,0191	0,9990	
15,0	23,2	16,2	7,0	0,8960	0,088	0,0235	0,9985	
18,0	26,7	18,4	8,3	0,9947	0,091	0,0245	0,9981	
30,0	30,2	21,4	8,8	0,9934	0,098	0,0415	0,9978	
45,0	34,0	28,9	5,1	0,9919	0,096	0,1072	0,9976	
60,0	38,0	34,1	3,9	0,9904	0,092	0,1750	0,9975	
	•	•	z/d =	350			, ,	
5,0	7.9	5,5	2,4	1.0017	0,054	0,0141	1,0020	
6,0	10,5	7,4	3,1	1,0007	0,064	0,0155	1,0012	
8,0	14,5	10,3	4,2	0,9992	0,070	0,0166	1,0001	
10,0	18,2	12,8	5,4	0,0978	0,083	0,0192	0,9993	
12,5	22,0	15,6	6,4	0,9965	0,089	0,0216	0,9986	
15,0	25,5	17,8	7,7	0,9952	0,100	0,0242	0,9982	
18,0	29,1	19,8	9,3	0.9938	0,099	0,0238	0,9979	
30,0	32,6	23,8	8,8	0,9925	0,100	0,0448	0.9976	
45,0	36,5	31,3	5,2	0,9910	0,105	0,1127	0,9975	
60,0	40,3	36,2	4,1	0,9895	0,099	0,1790	0,9975	
, ,	•	·	z/d	= 300	•	'		
5,0	9,5	7,1	2,4	1,0011	0,069	0,0180	1,0015	
6,0	12,3	9,2	3,1	1,0000	0,079	0,0191	1,0007	
8,0	16,3	12,1	1,2	0,9985	0,086	0,0204	0,9997	
10,0	20,5,	14,8	5,7	0,9970	0,097	0,0212	0,9989	
12,5	24,3	17,6	6,7	0,9956	0,097	0,0225	0,9983	
15,0	28,0	19,7	8,3	0,9942	0,106	0,0238	0,9980	
18,0	31,6	21,6	10,0	0,9928	0,102	0,0227	0,9977	
30,0	35,3	26,5	8,8	0,9914	0,113	0,0478	0,9975	
45,0	39,1	34,0	5,1	0,9900	0,110	0,1200	0,9975	
60,0	42,8	38,0	4,2	0,9885	0,104	0,1836	0,9975	
x/d == 250								
5,0	11,4	9,0	2,4	1,0004	0,086	0,0224	1,0010	
6,0	14,4	11,1	3,3	0,9992	0,098	0,0223	1,0001	
8,0	18,6	14,1	4,5	0,9977	0,109	0,0242	0.9992	
10,0	23,0	16,9	6,1	0,9961	0,111	0,0226	0,9985	
12,5	26,8	19,7	7,3	0,9947	0,113	0,0247	0,9981	
15,0	30,6	21,9	8,7	0,9932	0,110	0,0236	0,9978	
18,0	34,0	23,8	10,2	0,9919	0,112	0,0245	0,9976	

<sup>\*</sup> T.N.: Commas in numerical entries represent decimal points.

Tables.
Table II

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i.	ų.	F	Pé-udec	2Rey = ud	n = 1 = 0	A = a · d	
Ø	<u>t</u>	cm²				exp.	
cm rec C	cm*	M-C	-	-	_	<u> </u>	
<del> </del>			r/d = 400	<u></u>		***************************************	
0.001840	Lacona			l teno i		1	
0,001342	0,9999	0,01446	1667	173,0	0,0926	4,28	
0,001349	0,9998	0,01340	2228	224,0	0,1005	4,62	
0,001359	0,9994	0,01207	2942	331,0	0,1127	5,00	
0,001368	0,9989	0,01100	3650	455	0,1245	5,93	
0,001379	0,9982	0,01007	4520	620	0,1373	6,92	
0,001388	0,9975	0,00036	5380	801	0,1489	8,45	
0,001397	0,9966	0,00865	6410	1040	0,1625	8,78	
0,001403	0,9956	0,00803	10570	1870	0,1766	14,72	
0,001439	0,0944	0,00742	15500	3032	0,1955	37,2	
0,001460	0,0929	0,00687	20360	4370	0,2140	60,0	
			/d == 350				
0,001347	0,8998	0,01390	1660	179,8	0,0968	5,23	
0,001354	0,9996	0,01290	2217	232,5	0,1050	5,73	
0,001365	0,9992	0,01156	2927	346,0	0,1181	6,10	
0,001375	0,9986	0,01052	3630	475,0	0,1310	6,97	
0,001356	0,9978	0,00960	4492	0.51,0	0,1449	7,61	
0,001395	0,9909	0,00888	5350	845,0	0,1579	8,70	
0,001403	0,8959	0,00820	6370	1097	0,1722	8,48	
0,001419	0,9948	0,00764	10485	1964	0,1872	15,8	
0,001449	0,9935	0,00706	15390	3190	0,2071	38,9	
0,001468	0,9921	0,00658	20200	4560	0,2255	61,0	
		1	/d == 300		_		
0,001353	0,9997	0,01328	1859	188,2	0,1017	6,65	
0,001301	0,9995	0,01228	2204	244,0	0,1108	7,02	
0,001372	0,9989	0,01103	2910	362,5	0,1246	7,45	
0,001383	0.9981	0,00096	3600	502,0	0,1393	7,07	
0,001394	0,9972	0,00912	4460	686,0	0,1535	8,08	
0,001402	0,9962	0,00840	5320	893,0	0,1680	8,48	
0,001410	0,8952	0,00780	6340	1153	0,1820	8,08	
0,001429	0,9939	0,00724	10400	2071	0,1990	16,70	
0,001459	0,9925	0,00672	15270	2350	0,2193	41,20	
0,001477	0,8911	0,00029	20085.	4770	0,2377	62,10	
z/d = 250							
0,001360	0,9996	0,01257	1638	199	0,1032	8,24	
0,001368	0,9992	0,01160	2190	259	0,1178	8,14	
0,001381	0,9985	0,01040	2890	385	0,1331	8,75	
0,001391	0,9975	0,00910	3580	532	0,1485	8,14	
0,001402	0,9966	0,00863	4438	724	0,1633	8,82	
0,001411	0,9955	0,00797	5280	941	0,1784	8,35	
0,001419	0,9944	0,00743	6290	1210	0,1925	8,64	

Tables. Table II

u	ë	Θ,,	<u></u> <del>0</del> − 0 <sub>w</sub>	ψ · c	d $\overline{\theta}$	Œ	c			
cm	Co	C u	C u	CAL	Co	CA)	cal			
Hrc .	U			cm) Ca	cm .	em <sup>2</sup> see Co	g Co			
z/d == 250										
30,0	38,1	29,4	8,7	0,9904	0,125	0,0534	0,9975			
45,0	42,0	36,7	5,3	0.9889	0,122	0,128	0,9975			
60,0	45,5	41,0	1,5	0,9875	0,114	0,188	0,9975			
			z/d	= 200		•	,			
5,0	13,6	11,2	2,4	0,9996	0,103	0,0268	1,0003			
0,0	16,8	13,4	3,4	0,9984	0,111	0,0244	0,9990			
8,0	21,4	10,6	4,8	0.9967	0,126	0,0262	0,9988			
10,0	25,8	19,3	6,5	0,9951	0,122	0,0234	0,9982			
12,5	29,7	22,2	7,5	0,9936	0,135	0,0280	0,9979			
15,0	33,5	24,4	0,1	0,9921	0,132	0,0270	0,9976			
18,0	36,9	26,3	10,6	0,9908	0,135	0,0284	0,8975			
30,0	43,4	32,4	9,0	0,9891	0,143	0,0589	0,9975			
45,0	45,1	39,7	5,4	0,9876	0,134	0,138	0,9975			
60,0	48,3	43,7	4,0	0,9864	0,122	0,196	0,9976			
z/d == 150										
5,0	16,6	14,2	2,4	0,9965	0,134	0,0348	0,9996			
6,0	20,0	16,6	3,4	0,9972	0,163	0,0359	0,9990			
8,0	24,8	19,8	5,0	0,9954	0,176	0,0350	0,9983			
10,0	29,3	22,5	6,8	0,9937	0,187	0,0342	0,9979			
12,5	33,3	25,2	8,1	0,9922	0,180	0,0345	0,9976			
15,0	36,9	27,2	9,7	0,9908	0,177	0,0339	0,9975			
18,0	40,7	28,9	11,8	0,9894	0,180	0,0339	0,9975			
30,0	45,5	35,7	9,8	0,9875	0,180	0,0680	0,9975			
45,0	48,8	42,6	6,0	0,9802	0,160	0,148	0,9977			
60,0	51,5	46,5	5,0	0,9852	0,137	0,203	0,9979			
			z/d	<del></del> 100						
100	71,8	66,0	5,8	0,9769	0,181	0,381	1,0003			
140	74,3	69,7	4,6	0,9759	0,140	0,520	1,0007			
200	76,8	73,0	3,8	0,9748	0,100	0,660	1,0011			
300	78,9	76,1	2,8	0,9739	0,072	0,939	1,0015			
	·		*/d	l = 50		•				
100	76,8	70,0	6,8	0,9748	0,224	0,402	1,0011			
140	78,1	72,8	5,3	0,9742	0,168	0,540	1,0014			
200	79,6	75,2	4,4	0,9736	0,127	0,703	1,0016			
300	80,8	77,8	3,0	0,9730	0,080	0,974	1,0018			
			<b>z/</b> c	i == 25	•	·				
100	79,6	72,5	7,1	0,9736	0,217	0,424	1,0016			
140	80,4	74,6	5,8	0,9732	0,194	0,570	1,0018			
200	81,1	-76,4	4,7	0,9729	0,141	0,730	1,0019			
300	81,9	. 78,6	3,3	0,9725	0,090	0,995	1,0020			
	•					•				

Tables. (continued)

i.		ינ	Pe = udoc	2 Rey = ud	0 = 7 ×	Y = 1 4 4
	<u>н</u>	cm <sup>2</sup>		_		exp.
Tem Acc O	cm)	PCC		-		
CHI MC O	- 121		d = 250			
			•	1 4145		18,5
0,001441	( 0,0020	0,00085	10300	2190	0,2124	1
0.001470	0,6614	0,00038	15140	3530	0,2330	43,5
0.001487	0'(RKK)	0,00600	19920	5000	0,2510	) 63,2
·	•		t,'d == 200		•	
0,001369	0.56863	0,01184	1825	211	0,1157	9,79
0,001378	0,54188	0,01090	2173	275	0,1266	8,87
0,001378	0,181711	0,00375	2670	410	0,1431	9,41
0,001401	0,11104	0,00882	3550	567	0,1597	B,34
	0,0057	0,00510	4395	772	0,1755	8,80
0,001412 0,001421	0,1846	0,00750	5240	1000	0,1910	9,50
,	0,0003	0,00702	6240	1260	0,2055	8,84
0,001429	0,9117	0,00045	10200	2325	0,2279	20,3
0,001453	0,000	0,00001	15000	3725	0,2464	40,6
0,001481	0,9888	0.00573	19760	5240	0,2650	65,5
0,001497	0,,,,,,,,,	•	z/d = 150	-	•	
	t amount	1 0,01034	1 1807	1 229	0,1264	1 126
0,001381	0,0888	0,01006	2150	298	0,1386	12,9
0,001390	0,0082	0,00902	2837	444	0.1503	12,5
0,001403	0,9971	0,00518	3510	611	0,1740	12,1
0,001414	0,0059	0,00753	4355	830	0.1907	12,1
0,001424	0,000	0,00701	5190	1070	0,2061	11,8
0,001432	0,9933	0,00701	6165	1378	0,2228	11,8
0.001439	0,0019	0,00600	10100	2500	0,2475	23,2
0,001460	0,6860	0,00568	14850	3960	0.2668	49,5
0,001494	0,0880	0,00545	19600	5500	0,2810	67,3
0,001508	0,0873	1 0,00-710	r/d == 100			• .
					1 0.200	1 120,0
0,001580	0,9707	0,00107	30500	13250	0,399	162,4
0,001601	0,0752		12700	17720	0,415	210,5
0,001614	0,9737	0,00382	60100	26200	0,434	289,0
0,001626	0,0725	0,00373	89900	40200	0,448	1 203,0
	•		z/d = 50			
0,001602	1 0,9737	0,00382	30100	13090	0,430	125,3
0,001613	0,0730	0,00376	42300	18610	0,441	167,4
0,001622	0,9720		60000	27100	0,452	216,5
0.001633	0,9713	0,00364	89500	41200	0,461	298,0
	•	•	r/d == 25			
0.001018	0,9720	1 0.00369	1 30200	13550	0,449	131,4
0,001612			42000	19170	0,457	175,8
0,001620	ومستا	1		27600	0,462	224,2
0,001627			89200	41800	0,469	301,0
0,001636	1 0,000	- 1 -1	,	•	•	

Tables. Table II

							<u> </u>				
u	Ō	G <sub>*</sub>	$\overline{\theta} - \theta_{\pi}$	₩ · ē	d <del>0</del>	α	Į.				
em	Cº	Ø	o	cm³ C <sup>II</sup>	cm.	cm <sup>2</sup> Noc Co	g O"				
	z/d = 10										
100	1 81,5	74,2	7,3	0,9727	0,260	0.467	1,0019				
140	81,9	75,8	6,1	0.3725	0,226	0,630	1,0020				
200	82,2	77,2	5,0	0,9724	0,160	0,778	1,0020				
300	82,6	79,1	3,5	0,9722	0,104	1,085	1,0021				
r/d == 400											
100	45,1	41,8	] 3,2	0,9876	0,074	0,286	0,9975				
100	53,2	19,2	4,0	0,9645	0,098	0,302	0,9980				
100	60,7	66,0	4,7	0,9816	0,123	0,321	0,9987				
100	67,9	62,4	5,5	0,9766	0,150	0,334	0,9997				
			z/d	<b>= 350</b>							
100	47,0	43,7	3,3	0,9869	0,078	0,292	0,9976				
100	65,8	51,7	4,1	0,9835	0,104	0,312	0,0982				
100	64,1	59,1	5,0	0,9802	0,136	0,333	0,9992				
100	71,6	68,0	5,6	0,9770	0,157	0,343	1,0002				
			z/d	<b>= 300</b>							
100	49,1	45,7	3,4	0,9861	0,083	0,301	0,9977				
100	68,5	64,3	4,2	0,9824	0,110	0,322	0,9985				
100	67,6	62.4	5,2	0,9787	0,144	0,339	0,9996				
100	75,6	69,7	5,9	0 9753	0,173	0,358	1,0009				
			r/d	= 250							
100	51.3	17,7	3,0	0,9853	0,092	0,315	0,9979				
100	61,2	50,9	4,3	0,9814	0,116	0,331	0,9988				
100	71,2	65,8	5,4	0,9772	0,157	0,355	1,0002				
100	80,1	73,9	6,2	0,9733	0,192	0,377	1,0017				
				<b>⇒</b> 200							
100	53,6	49,9	3,7	0,9844	390,0	0,326	0,9980				
100	64,3	59,7	4,6	0,9801	0,131	0,349	0,9992				
100	75,1	69,5	0,6	0,8755	0,171	0,373	1,0008				
100	85,2	78,6	6,6	0,9710	0,215	0,396	1,0026				
				<b>=</b> 150							
100	56,1	52,2	3,9	0,9834	0,109	0,343	0,9982				
100	67,9	62,7	5,2	0,9768	0,155	0,365	0,0397				
100	79,5	72,9	6,6	0,9736	0,190	0,350	1,0017				
100	8,09	83.9	6,9	0,9684	0,237	0,416	1,0037				
			2/d	<del>=</del> 400 ,							
140	49,2	46,4	2,8	0,9860	0,063	0,388	0,9977				
140	58,9	55,4	3,5	0,9823	0,086	. 0,423	0,9985				
140	67,9	63.8	4,1	0,9786	0,108	0,451	0,9997				
140	76,1	71,2	4,9	0,9751	0,136	0,473	1,0010				

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Tables.

	,	9.3				· · · · · · · · · · · · · · · · · · ·		
ž w	- u	 ''	pa udec	2 Rey = vd	0 to 1/4	۸ = "d	A	
* #r	l c	1"	A W	x v c). 四点	- <del>σ</del> μ	7 TW	calculated	
cal	- F	em <sup>‡</sup>					Formula	
cm sec Q	cm,	960	<del></del>	-	_	erp.	12a 13	
	·		<del>'</del>	ويحديث	<u>'====</u>			
- 001010	14			:/d ⇒ 10				
0,001016	0,9705		30100	13890	0,462	144,1		
0,001025	0,0700		41900	19500	0,165	194,0		
0,001630	0,8701		89700	27900	0,468	239,0		
0,001638   0,9701   0,00356   89100   42200   0,473   331,0								
z/d == 400								
0,001490	10,0002	1000004	33160	8280	0,250	l 90,0	97,2   105,0	
0.001519	0.9805		32400	9435	0,291	99,2	95,5 108,1	
0,001540	0.9628		31720	10590	0,334	103,6	94,0 113,7	
0,001572	0.9769		31100	11660	0,376	103,1	92,0 121,4	
••	, .,	.,	•	/d ≈ 350	11		2-1-   4-11.	
0.001497	10.0894	0,00565	1 32860	8550	0,259	97,4	96,8   105,8	
0,001529	0.0853		32150	9825	0,305	102.0	95,0 109,6	
0.001559	0,9810		31400	11110	0,354	102,6	03,3 115,8	
0.001550	0,9768		30770	12280	0,399	108,0	91,9 125,2	
*,******	1 4,0 , 50	, -,,,,,,,		/d == 300	( 0,000	1 100,0	1 0110   12015	
0,001505	0.9884	0.00366	32750	8840	0,209	100,0	90,3   106,8	
0.001839	0,0830		31900	10245	0,203	104,6	94,4 111,6	
0.001572	0.9791		31100	11050	0,375	107,7	92,6 119,3	
0.001601	0,9745		30430	12885	0,424	111,7	91,1 130,8	
0,001001	1010110	0100000		/d == 250	0,121	222,7	2111   10010	
0,601513	0,0874	0,00545	32550	9175	0,282	103,9	95,8   108,5	
0.001550	0,0825		31650	10055	0,202	100,9	93,9 114,7	
0.001585	0,9770		30500	12100	0,396	112.0	92,0 124,7	
0.001017	0,9717		30050	13055	0,455	116,6	90,3 139,2	
•,•••••	1 -1-1-1		,	/d == 200	( 0,100	110,0	1 2010 1 10012	
0,001522	10,9863	0.00526	1 32350	/u == 200 1 9510	0.294	107,0	95,4 ]	
0,001501	0.9809		31360	11155	0,356	111.8	93,2	
0,001600	0.9745	, ,	30470	12820	0,421	116,3	91,2	
0,001636	0,9085		29630	14450	0,488	120,8	89,3	
0,0000	1 012000	0,000.0		/d = 150	0,100	14010	0010	
0,001531	0,9851	0,00506	32100 <sup>2</sup>	/u == 180   9885	0,308	1100	0401	
0,001573	0,9760		31100	11660	0,308	112,0 115.9	94,9 92,6	
0,001613	0,972)	0.00370	30150	13510	0,376	115,9	90,5	
0.001657	0.9018		29200	15380	0,527	125,4	88,4	
-1001-001	1 -110	2,000,000		•	0,021	11997	00,2 }	
			_	/d = 400		•		
0,001508	0,9884		45800	12380	0,270	128,6	123,8 133,8	
0,001544	0,9837		44500	14430	0,324	136,8	121,2 137,3	
0,001577	0,9789		43400	16350	0,377	143,1	118,9 143,9	
0,001606	0,9741	0,00385	42450	18180	0,428	147,3	117,0 153,4	
							A	

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OF FOLD CHARLEY

Tables.
Table II

	บ็	G	θ*	<u></u> <del>0</del> − 0,	₽ · C	<u>d</u> <del>d</del> ℓ	a	i c
	em Fee	C*	C*	C.	cm' C	C.	emi He Ci	E Cr.
t/d *: 350								
	140	51,0	48,1	2,9	0,0854	0,070	0,416	0,9376
	140	61,0	57,4	3,6	0,9814	0,032	0,435	0,9378
	140	70,7	60,3	4,3	0,9774	0,120	0,466	1,0001
	140	70,0	74,6	5,0	0,9735	0,144	0,490	1,0016
		,	,	r/d	<b>≈</b> 300		-,	*,****
	140	52,9	49,9	( )	0,9840	0,075	0,430	0,0980
	140	63,3	59,6	74.5	0,9805	0,095	0,454	0,9990
	140	73,6	69,1	4,5	0,9762	0,125	0,475	1,0000
	140	63,2	76,2	5,0	0,8719	0,150	0,510	1,0023
		•	,	r/d	<b>⊷</b> 250	•		
	140	54,6	51,8	3,0	0,9639	0,077	0,441	0,9961
	140	65,B	62,0	3,8	0,9795	0,103	0,465	0,9394
	140	76,7	72,0	4,7	0,9748	0,135	0,490	1,0011
	140	87,1	62,0	5,1	0,9701 .	0,162	0,536	1,0030
				±/d	<b>= 200</b>		•	
	140	56,6	53,6	3,2	0,9831	0,083	0,446	0,9983
	140	68,4	64,5	3,9	0,9784	0,110	0,483	0,9998
	140	60,0	75,2	4,8	0,9734	0,143	0,508	1,0017
	140	9),ភ	65,9	5,6	0,9080	0,184	0,657	1,0038
					150			
	340	\$66	55,5	3,4	0,0823	0,090	0,455	0,9965
	140	71,1	67,0	41	0,9772	0,120	0,501	1,0002
	140	83,6	78,6	5,0	0,9717	0,157	0,634	1,0023
	140	96,2	90,2	6,0	0,9057	0,200	0,503	1,0018
				-12	<b>=</b> 400			
	200	1 53,3 1	50,8	2,5	0,9645	0,055	0,541	0,9960
	2(10	64.1	61.1	3,0	0,9802	0,071	0,560	0,0992
	200	74,7	71,2	3,5	0,9757	0,089	0,620	1,0008
	200	64,0	79,6	4.4	0,9715	0,120	0,663	1,0024
		•	•	z/d .	= 350	• • • • •	,	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
	200	1 54,7	52,1	2,6	0,6439	0,059	0,558	0,9981
	200	66,0	62,8	3,2	0,9794	0,078	0,596	0,9994
	200	77,0	/3,3	3,7	0,9747	0,097	0.638	1,0012
	200	87,0	82,6	4,4	0,9702	0,124	0,684	1,0030
				z/d	<b>300</b>		•	
	200	56,3	53,5	2,8	0,9833	0,064	0,563	0,9963
	200	68,0	64,7	3,3	0,9785	0,082	0,606	0,9997
	200	79,4	75,7	3,7	0,9736	0,100	0,657	1,0016
	200	90,2	85,6	4,6	0,9686	0,133	0,700	1,0036

Chile in

Tables.

Andrew State Committee

ž,		F P	Pe-udec	21tey - 10 d	n = 1/4	A in a cd	A			
~#	l'		λw	1	C //	A W	Cuicolurad			
[A2	E	cm <sup>2</sup>		(		exp.	Formula			
CIII ME C	cmi	M'C	_	-	_	i – i	12n 13			
		<u> </u>	1	/d = 350			- Tari			
0.001515	0.9876	0.00546	45500	12770	0,280	137,2	123,2   134,7			
0,001552	0.0826	0.00170	44250	14885	0,336	141,1	120,7   139,3			
0,001557	0.0773	0.00112	43100	16980	0.301	146,9	116,3 147,1			
0.001020	0,9720		42000	16970	0.451	151,2	110,0 158,2			
		, ,	, Ł	/d ⊫ 300	, ,,,,,		, , , , ,			
0,001522	0.08671	0.00533	45260	13130	0,200	141,2	122,8   136,3			
0,001561	0.9814	0.00154	13920	15415	0,351	145,3	120.0 141.9			
0,001598	0.9756	0.00398	42700	17585	0.411	148,7	117,5 151,5			
0,001034	0,9698	0.00354	41600	19770	0,475	150,0	115,2 165,5			
•	•	•	Z.	/d == 250	,		, , , , .			
0.001530	0.9857	0,00517	45000	13530	0.301	144,0	122,2   138,5			
0,001570	(030,0	0.00130	43050	15940	0.305	148,0	119,4 146,0			
0,001010	0,9738	0.00382	42320	16320	0.433	152,2	116,7 158,3			
0,001049	0,9872	0,00338	41150	20700	0,503	163,3	114,3 176,5			
z/d = 200										
0,001537	0,9647	0,00501	44760	13970	0,312	145,1	121.7   142.3			
0,001580	0,0766	0,00125	43300	16470	0,380	153,0	118,7 152,5			
0,001622	0,9716	0,00307	42000	10070	0,455	110,0	116,0 169,7			
0,001065	0,0043	0.00322	40700	21730	0,535	167,1	113,2 194,7			
•	•	,	2	.'d ⊨ 150	•		•			
0,001544	0,0837	0,00185	44500	14430 [	0,324	147,3	121,2			
0,001690	0,8771	0,00110	43000	17070	0,397	157,5	118,1			
0,001636	0,9095	0,00352	41520	19860	0,478	163,1	115,0			
0,001682	0,9010	0,0X1307	40150	22800	0,508	167,6	112,2			
							•			
0.000 000 1		0.66400	_	'd == 400						
0,001526	0,0803	0,00529	64500	16900	0,203	177,3	160,1 173,1			
0,001500 0,001606	0,0810 0,0750	0,00450	02600 60700	22220 25500	0,355	185,0	150,5 177,4			
0,001000	0.9693	0,00350	59200	26560	0,420 0,4825	193,0	163,0   165,1			
0,001010	0,2003]	0,000.00			0,4020 }	202,0	150,1   196,8			
0,001531	0.98581	0.00518	64250 I	/d == 350 19300 - f	0.200	1001	180 6 . 154 5			
0,001531	0,8600	0.00438	62200	22820	0,300 0,307	162,1 189,3	159,6   174,5 155,8   179,8			
0,001615	0.9736	0.00381	60300	20230	0,307	197,6	152,2   189,3			
	0,9673	0.00338	68650	29580	0,504	207,0	149,1 203,3			
-1	-,,	-1		/d == 300	Almai	-0110 1	ranta I moto			
0.001530	0.9850!	0.00505 [	64000	19790 I	0,309	183,1	159,1   176,6			
0,001531	0,8550	0,00427	61850	23400	0,378	192,3	155,1 183,3			
	0,9721	0,00370	59900	27000	0,451	202,2	151,4 195,2			
-1.	0,9652	0,00327	58150	30580	0,525	210,2	148,1 212,7			
,	,= = -1	,	1		-,		6*			
							Ð-			

Tables.
Table II

ū	ंड	Θ <sub>w</sub>	<i>\overline \overline \text{\text{\overline \text{\overline \text{\overl</i>	ş. <del>c</del>	d <del>U</del>	п	<u> </u>			
em	<del></del>	<del></del>		(A)	C"	ca)	ce.l			
sec	C*	C.	G.	em³ C	em	em³ ме C°	ų C•			
r/d = 250										
200	57,8	55,0	1 2.8	0.0827	0,060	0.550	1389,0			
200	70.1	66,7	3,4	0,9777	0,087	0,625	1,000			
200	62,0	78,2	3,8	0.0725	0,106	0.678	1,0020			
200	93,5	8,83	4,7	0,9671	0,140	0,721	1,0043			
#00	1 1.010	1 00,0	•	= 200	, -,					
200	59.4	50,6	2.8	0.9821	0,008	0.596	0.9986			
200	72,2	08,6	3,4	0,9767	0,089	0,640	1,0003			
200	84.7	80,7	4,0	0,0712	0,114	0,692	1,0025			
200	07,0	92,2	4,8	0,9653	0,148	0.744	1,0050			
200	טווע	1 2010		= 150 == 150	, 0,,,0	1	] 2,444			
200	61,2	58,3	2,9	0.0813	0.072	0.610	0,9988			
200	74,4	70,8	3,6	0,0755	0,090	0,052	1,0007			
200	67,6	63,4	4,2	0,9099	0,124	0,715	1,0030			
200	100,8	95,9	4,9	0.9033	0,155	0,760	1,0058			
200	1 1040	5010	1 210	i oleann	, 0,,,,,	, 0,	, ,,,,,,,,			
			z/d	<b>= 400</b>						
300	57,2	55,2	2,0	0,9630	0,012	0,774	0,9984			
300	69,3	66,7	2,6	0,9780	0,059	0,633	0,9999			
300	81,3	78,1	3,2	0,9728	0,079	0,900	1,0019			
300	90,9	\$6,8	4,1	0,9083	0,108	0,956	1,0037			
	•		2/6	i≕ 350	•	•	•			
300	58,3	56,2	2,1	0,9825	0,045	0,789	0,9985			
300	70,8	68,2	2,6	0,9774	0,061	0,859	1,0010			
300	63,0	80,1	3,2	0,9719	0,081	0,922	1,0023			
300	93,7	89,5	4,2	0,9670	0,113	0,976	1,0043			
		•	1/0	300	•	•	•			
300	59,4	57,2	2,2	0,9820	0,048	103,0	0,0986			
300	72.4	09,7	2.7	0,0767	0,004	0,868	1,0004			
300	85,3	82,1	3,2	0,9709	0,082	0,933	1,0026			
300	90,5	92,3	4,2	0,9656	0,115	0,992	1,0049			
,	•		z/6	= 250	•	•	•			
300	60,6	58,4	2.2	0,9816	0,049	0,820	0,9987			
300	74,0	71,3	2,7	0,9760	0,066	0,693	1,0000			
300	87,4	84,2	3,2	0,9700	0,081	0,955	1,0030			
300	99,4	95,2	4,2	11,9640	0,118	1,017	1,0055			
		•	r/c	1 == <b>2</b> 00	•					
300	61,9	59,6	2,3	0,9811	0,052	0,831	0,0982			
300	75,6	72,9	2,7	0,9753	0,067	0,907	1,0003			
300	89,4	86,2	3,2	0,9690	0,066	0,976	1,0034			
300	102,3	98,1	4,2	0,9625	0,121	1,040	1,0001			
	•	- '	•	•	•	*	•			

Tables.

2		F	Pé = udice	2 Rey≡ ud	n ==	$A = \frac{n  d}{k \pi}$	Acalculated
cal	<u></u>	cm.					Formula
cm sec Ce	cm1	F(1C	•-			exp,	124 13
	<u>'</u>			'd = 250			
0.001540	100000	l a ssant i		í		1 1555	
0,001542	0,0843	, ,	63700	20230	0,316	188,0	158,6   179,7
0,001634	0,9777	0,00415	61500	24085	0,392	190,7	154,5 188,0
0,001033	0,9629	•	59450 57600	27910	0,470	207,3	150,6 204,3
0,001010	i otuarni	0,00310		31040	0,548	215,1	147,1 227,0
0,001549	0.9535	0,00181	63400 i	/d == 200	0.000	. 100.0	
0,001597	0,9535	0,00101	61100	20780	0,328	192,3	156,0   164,7
0,001044	0,9088	0,00347	59000	24050 28800	0,403	200,4	153,7 197,4
0,001000	0,9601	, ,	57050	i i	0,488	210,5 220,0	149,7   219,0   146,0   251,1
0,001010	LOTROPI	ן טיזנטטנט ן	,	32780	0,575	220,0	146,0   251,1
0,001556	0,0825	L COLLEGE		,'d ≈= 150	0.000	ممدا	
0,001605	0,9752	0,00108 0,00391	03000	21360	0,339	196,0	157,3
0,001055	0,9670	0,00334	00750 58550	25370 26750	0,417	203,2	153,0
0.001705	0,9577		56400	34000	0,608 0,602	216,0 223,0.	148,9
0,001100	10,000,1	0,00204	20400	31000	0,002	, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,	1 144'9
			,	/d ⊷ 400			
0,001543	10,9846	0.00498	95600	30120	0,315	251,0	215,0   232,5
0,001589	0.0781	0,00120	92300	35720	0,387	262,0	209,4 237,3
0,001034	0,9710	0,00361	£9300	41550	0,465	275,2	201,3 247,2
0,001608	0,9617		87050	1630	0,532	256,5	200,4 202,8
'	,	,	Z	/d == 350	•	• '	•
0.001547	0.9840	0,00490	95300	30020	0,321	255,0	214,5   234,5
0,001595	0,9772	0,00411	91850	36500	0,397	269,0	208,7 240,8
0,001042	0,9697	0,00354	88750	42370	0,477	280,5	203,4 253,0
0,001679	0,9628]	0,(4:3)5	86400	47020	0,552	290,7	199,3 271,7
,	•		2.	′d == 300	•	,	•
0,001551	0,9835)	0,00481	95000	31200 [	0,328	259,0	214,0   237,5
0,001601	0,9763	0,00403	91500	37220	0,407	271,0	208,1 246,0
0,001650	0,9684	0,00315	88250	43450	0,492	283,0	202,5 261,0
0,001090	0,9608	0,00306	85650	46030	0,573	294,0	195,0 284,5
	-	•	Z	'd = 250			
0,001550	0,9526	0,00472	91650	31760	0,330	263,5	213,4 241,9
0,001607	0,9754	0,00396	91100	37880	0,416	278,0	207,4 253,6
0,001658	0,9671	0,00337	67700	44500	0,507	288,0	201,6 273,4
0,001702	0,9587	0,00208	84950	50330	0,593	298,5	196,8   303,7
		•	Z,	/d = 200			
0,001561	0,9821	0,00464	94250	32330	0,343	266,0	212,7 248,7
0,001613	0,9745	0,00387	90700	38760	0,427	281,0	206,7 265,4
0,001668	0,9057	0,00330	87200	48450	0,520	#93,2-	200,7 293,7
0,001713	0,9567	0,00269	84250	51900	0,617	303,5	195,6 336,5

Tables. Table II

				<u> </u>						
ົນ	ij	θ,,	<u></u> <del>0</del> −0,,	<u>6. c</u>	d <del>Ø</del>	a	c			
em see	C.	C•	C.	cal em³ Cº	C <sub>0</sub>	cm1 rec C	cal g C°			
<u> </u>	<del></del>	—		/d == 150						
300	63.1	60,8	2,3	0,9806	0,053	0,852	0.9990			
300	77,2	74,5	2,7	0,9746	0,008	0,920	1,0012			
300	91,5	88,3	3,2	0,9650	0,088	0,998	1,0030			
300	105,3	101,0	4,3	0,9008	0,127	1,065	1,0068			
z/d == 400										
500	61,1	59,5	) ),6	0,9814	0,029	1,112	0,9988			
500	73,6	71,7	2,1	0,9760	0,042	1,220	1,0006			
500	87,6	85,3	2,3	0,9099	0,050	1,317	1,0031			
500	99,2	05,7	3,5	0,9642	0,083	1,428	1,0054			
			z	/d == 350						
500	61.8	00.2	1,6	0,6811	0,030	1,149	0,9989			
500	74,9	72,7	2,2	0,9756	0.045	1,247	1,0008			
500	88,8	80,4	2,4	0,9093	0,053	1,338	1,0033			
500	101,3	97,8	3,5	0,9630	0,084	1,444	1,0059			
			Z.	/d == 300						
500	62,6	60,9	1,7	0,9808	0,032	1,155	0,9990			
500	76,0	73,7	2,3	0,9751	0,047	1,246	1,0010			
500	90,1	87,7	2,4	0,9687	0,053	1,337	1,0036			
500	103,3	89,8	3,5	0,9619	0,085	1,460	1.0033			
			Z,	d = 250						
500	63,5	61,7	1,8	0,9804	0,033	1,124	0,9991			
600	77,2	74,9	2,3	0,9746	0,048	1,271	1,0012			
500	91,4	89,0	2,4	0,8080	0,054	1,361	1,0038			
600	105,4	101,9	3,5	0,9607	0,086	1,476	1,0068			
				d = 200						
500	61.3	62,5	1,8	0,9801	0,035	1,110	0,9992			
500	78,4	76,0	2,4	0,9740	0,050	1,270	1,0014			
500	92,7	90,3	2,4	0,9675	0,056	1,410	1,0041			
500	107,5	104,0	3,5	0,9595	0,068	1,509	1,0073			
F00				d = 150						
600	65,1	63,3	1,3	0,9798	0,030	1,224	0,9992			
500	79,6	77,2	2,4	0,9736	0,051	1,294	1,0016			
500 500	94,2	91,6	2,6	0,9657	0,061	1,418	1,0044			
500	109,6	106,0	3,6	0,9583	0,092	1,530	1,0078			

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Tables.

				·					
, <del>**</del>	ē	ŗ	Pe = udec	$2\operatorname{Rey} = \frac{\overline{u}}{\overline{v}} \frac{d}{\overline{v}}$	$a = \frac{1}{C \mu}$	$\Lambda = \frac{ad}{\lambda_w}$	calcu	ulnte	
CA)	E	cm					For	muln	
em sec Co	cm,	HEC				exp.	12a	13	
	<u> </u>		<del></del>	<u> </u>	<u> </u>	<u>'</u>			
				z/d = 10		i		_	
0,001566	0,9815	•	93900	32900	0,350	272,3	212,2		
0,001620	0,9735	0,00380	90250	39180	0,438	254,0	205,8	ŀ	
0,001675	0,9643	0,00322	86700	40600	0,538	298,0	199,8	İ	
0,001725	C,9545	0,00280	83500	53600	0,642	308,5	194,3	İ	
r/d == 400									
0,001560	0,9826	0,00470	157300	53200	0,338	356,5	312,4	337,8	
0,001609	0,9755	0,00396	151600	63150	0,416	379,0	303,9	3/4,4	
0,001662	0,9670	0,00336	145900	74400	0,510	396,0	295,3	357,3	
0,001704	0,9589	0,00298	141400	83900	0,594	418,5	288,4	378,1	
			•	z/d == 35		•	,	,	
0,001563	0,9822		156950	53800	0,342	367,5	311,9	341,0	
0,001612	0,9749	0,00391	151300	63900	0,423	380,5	303,4	350,2	
0,001667	0,9661	0,00333	145300	75300	0,518	401,0	294,3	366,0	
0.001712	0,9574	0,00292	140600	85650	0,610	421,5	287,2	391,5	
			,	z/d = 30				•	
0,001566	0,9818	,	156500	54500	0,346	368,5	311,2	345,5	
0,001617	0,9742	•	150700	64800	0,430	385,5	302,5	357,6	
0,001672	0,9053		144750	76450	0,528	399,5	293,5	378,3	
0,001720	0,9560	0,00286	139750	87450	0,626	424,5	265,9	410,7	
			•	z/d = 2t	50				
0,001569	0,9813	0,00454	156200	55100	0,352	358,0	310,8	352,2	
0,001621	0,9735	0,00380	150300	65800	0,438	392,0	301,9	369,0	
0,001677	0,9644	0,00322	144300	77050	0,538	400,0	292,8	397,0	
0,001728	0,9544	0,00260	139000	. 80300 ±	0,043	427,0	284.7	439,2	
				z/d == 20	00 .			•	
0,001572	0,9809	0,00449	155600	55700	0,357	376,2	310,2	362,6	
0,001626	0,9728	0,00374	149700	66850	0,445	390,5	301,0	386,6	
0,001683	0,9635	0,00318	143600	78650	0,548	419,0	291,8	427,0	
0,001736	0,8527	0,00275	138100	90920	0,658	434,5	283,3	487,2	
			•	z/d == 18	50				
0,001575	0,9805	0,00144	155500	50300	0,362	389,0	309,7	ſ	
0.001630	0,9720	0,00370	149300	67600	0,452	397,0	300,4		
0,001688	0,9624	0,00314	143150	79000	0,556	420,0	291,1	'	
0,001744	0,9510	0,00269	137300	92950	0,677	438,5	282,1	ļ	

## TABLES.

EQUILITER TAX

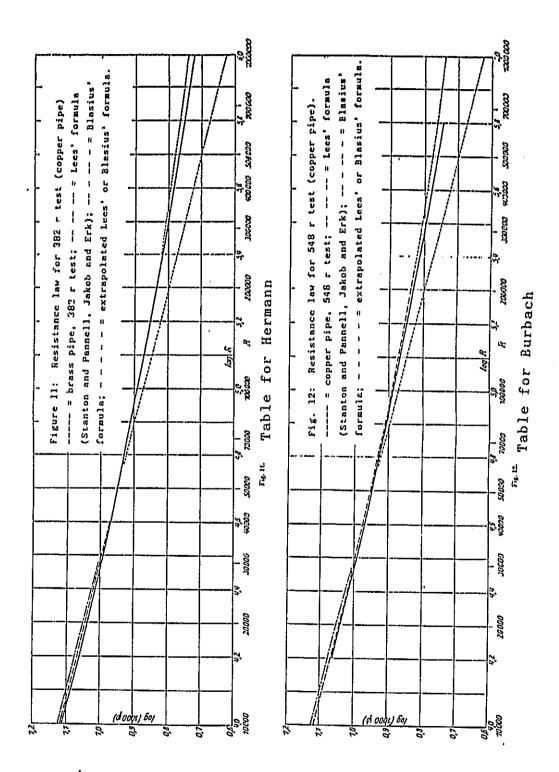
TABLE III
CALCULATION OF "GRASHOF" AND "G" FOR FOUR VESSEL TEMPERATURES

 $\beta = 0,00018$  °C-1; g = 961  $\frac{\text{cm}}{\text{sec}^2}$ ; a = 25 cm

at vessel temperature 
$$T_0 = 69.2^{\circ}$$
  $T_w - T_D = 9.5^{\circ}$  at vessel temperature  $T_D = 85.5^{\circ}$   $T_m - 10.8^{\circ}$  at vessel temperature  $T_D = 10.8^{\circ}$  at vessel temperature at vessel temperature

$$\begin{array}{lll} \nu_{03,1}{}^{\circ} & = & 0,00420 & \frac{cm^{\circ}}{acc} \\ \nu_{03,1}{}^{\circ} & = & 0,00345 & \frac{cm^{\circ}}{acc} \\ \nu_{191,1}{}^{\circ} & = & 0,00290 & \frac{cm^{\circ}}{acc} \\ \nu_{1313,0}{}^{\circ} & = & 0,00250 & \frac{cm^{\circ}}{acc} \\ & & & & & & & & & & & & \\ Gr_{49,1}{}^{\circ} & = & 1,376 \cdot 10^{\circ} \\ & & & & & & & & & & & \\ Gr_{311,0}{}^{\circ} & = & 2,202 \cdot 10^{\circ} \\ & & & & & & & & & & & \\ Gr_{131,0}{}^{\circ} & = & 3,346 \cdot 10^{\circ} \\ & & & & & & & & & & & \\ Gr_{1313,0}{}^{\circ} & = & 4,768 \cdot 10^{\circ} \end{array}$$

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