

OPTIMUM DIMENSIONS OF POWER SOLENOIDS FOR MAGNETIC SUSPENSION

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# OPTIMUM DIMENSIONS OF POWER SOLENOIDS FOR MAGNETIC SUSPENSION

B. A. Kaznacheyev

Electromagnetic systems based on compensating the forces acting on an object (model) with controlled magnetic fields are widely used in many areas of technology. A power magnetic suspension designed to work in conjunction with wind tunnels is an example of this type of system [1]. Figure 1 shows the block diagram of a device which makes it possible to stabilize the position of ferromagnetic model 4 in the direction of axis  $O_z$  by varying the current in power solenoid 3. Here the control signal is produced by model position sensor 1 and transformed by power amplifier 2. In these suspensions, the model is placed at a significant distance from the solenoid, and this distance is many times greater than the model's dimensions [2]. Power  $P$  consumed by the solenoid is great; it reaches tens and hundreds of kilowatts [2]. Under these conditions, it is necessary to determine solenoid dimensions  $l$ ,  $R_1$ , and  $R_2$  so that the value of power  $P$  is smallest at given distance  $c$  and external force  $G$ .

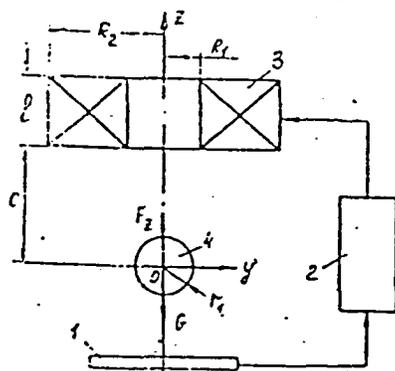


Figure 1. Block diagram of a single-component magnetic suspension.

When optimizing solenoid dimensions, we assume that the model

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\*Numbers in the margin indicate pagination in the foreign text.

is a solid ferromagnetic sphere with a small radius  $r_1 < c$  and constant magnetic permeability  $\mu$ . The magnitude of electromagnetic force  $F_z$  is found using the method given in [3]:

$$F_z = - \frac{VK_m}{1 + NK_m} H_z(0; 0) \frac{\partial B_z(0; 0)}{\partial c},$$

where  $K_m = \mu - 1$  is the magnetic susceptibility of model material;  $V = 4/3\pi r_1^3$  is model volume;  $N = 1/3$  is the solid sphere's demagnetizing factor; and  $H_z(0; 0)$  and  $\frac{\partial B_z(0; 0)}{\partial c} = \mu_0 \frac{\partial H_z(0; 0)}{\partial c}$  are the intensity of the solenoid's magnetic field and its derivative in the center of the model, respectively. Component  $H_z(0; 0)$  on the axis is determined by double integration along the solenoid's copper section:

$$H_z(0; 0) = \frac{w_0 JK_3}{2} \int_c^{l+c} \int_{R_1}^{R_2} \frac{y^2 dy dz}{R_1^2 + y^2 + z^2 R_1^2} \quad /95$$

where  $w_0$  is the number of solenoid loops in a unit of area;  $t$  is solenoid current, and  $K_3$  is the solenoid charge coefficient.

As the result of integration, we obtain:

$$\begin{aligned} H_z(0; 0) &= \frac{w_0 JK_3}{2} \left\{ (l+c) \ln \frac{U_2}{U_1} - c \ln \frac{u_2}{u_1} \right\}, \\ \text{where} \quad u_1 &= R_1 + \sqrt{c^2 + R_1^2}; \quad U_1 = R_1 + \sqrt{(l+c)^2 + R_1^2}; \\ u_2 &= R_2 + \sqrt{c^2 + R_2^2}; \quad U_2 = R_2 + \sqrt{(l+c)^2 + R_2^2}. \end{aligned}$$

After several transformations, we find the derivative:

$$\frac{\partial B_z(0; 0)}{\partial c} = \frac{\mu_0 w_0 JK_3}{2} f,$$

$$\text{where} \quad f = \ln \frac{u_1 U_2}{u_2 U_1} - \frac{c^2(R_1 u_1 - R_2 u_2)}{u_1 u_2 (u_1 - R_1)(u_2 - R_2)} + \frac{(l+c)^2 (R_1 U_1 - R_2 U_2)}{U_1 U_2 (U_1 - R_1)(U_2 - R_2)}$$

(1)

Thus, electromagnetic force is

$$F_z = - \frac{K_M V I^2 \mu_0 K_s^2}{4(1 + NK_M)} \left\{ (c + l) \ln \frac{U_2}{U_1} - c \ln \frac{u_2}{u_1} \right\} f. \quad (2)$$

The power consumed by the solenoid can be determined using the solenoid's geometric dimensions:

$$P = \rho \omega^2 \mu_0 K_s (R_2^2 - R_1^2) l, \quad (3)$$

where  $\rho$  is the conductor's specific electrical resistance.

We find current magnitude from (2) and enter it in (3). Finally:

$$\rho = \frac{4 \mu_0 F_z (1 + NK_M) c^2}{\mu_0 K_M V K_s} \frac{\bar{l} (\bar{R}_2^2 - \bar{R}_1^2)}{\left\{ (\bar{l} + 1) \ln \frac{U_2}{U_1} + \ln \frac{u_2}{u_1} \right\} f} \quad (4)$$

where  $\bar{l} = l/c$ ;  $\bar{R}_1 = R_1/c$ , and  $\bar{R}_2 = R_2/c$  are relative solenoid dimensions.

It is evident that at a given  $c$  and  $F_z$ , the solenoid consumes minimum power if the function entered in (4)

$$F(\bar{l}; \bar{R}_1; \bar{R}_2) = \frac{\bar{l} (\bar{R}_2^2 - \bar{R}_1^2)}{\left\{ (\bar{l} + 1) \ln \frac{U_2}{U_1} + \ln \frac{u_2}{u_1} \right\} f} \quad (5)$$

has its minimum value at selected parameters  $l$ ,  $R_1$  and  $R_2$ . Optimum solenoid parameters thus determined do not depend on the magnitude of (the conductor's) specific resistance, which varies as the result of heating.

Figure 2 shows function (5) as a function of solenoid length  $l$  for different outside radii  $\bar{R}_2$  and fixed inside radius  $\bar{R}_1 = 0.3$ . As can be seen from this graph, for each  $\bar{R}_2$  there is a solenoid length  $l_{opt}$ , at which minimum power is consumed by the solenoid. The increase in power when  $\bar{l} > \bar{l}_{opt}$  is due to the fact

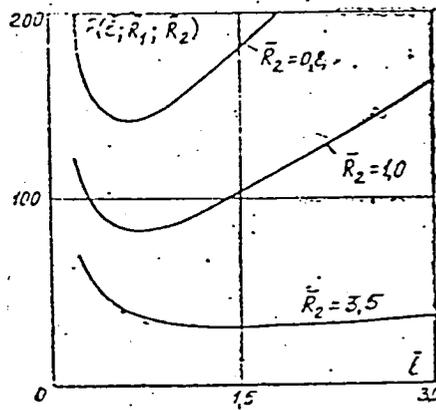


Figure 2. Graphs of function  $F(\bar{l}; \bar{R}_1; \bar{R}_2)$  as a function of relative length  $\bar{l}$  when  $\bar{R}_1 = 0.3$ .

that the loops distant from the model contribute very little to electromagnetic force. The increase in power when  $\bar{l} > \bar{l}_{opt}$  is due to the sharp increase in solenoid current necessary to create the given electromagnetic force. From Figure 2 it follows that solenoid length must be more carefully selected when  $\bar{R}_2$  is smaller since, when  $\bar{R}_2$  increases, the minimum value of function  $F(\bar{l}; \bar{R}_1; \bar{R}_2)$  becomes ambiguous.

Figure 3 shows graphs of function  $F(\bar{l}; \bar{R}_1; \bar{R}_2)$  as a function of  $\bar{l}$  for different inside radii  $\bar{R}_1$  and fixed outside radius  $\bar{R}_2 = 1.1$ . Minimum power (whose magnitude depends on the value of  $\bar{R}_1$ ) consumed by the solenoid can be seen on the curves. As opposed to the curves shown in Figure 2, curves in Figure 3 in the  $\bar{l}_{opt}$  area are virtually independent of  $\bar{R}_1$ . This means that solenoid lengths must be more carefully selected for a variable inside radius than for a variable outside radius, especially when  $\bar{R}_2$  is large.

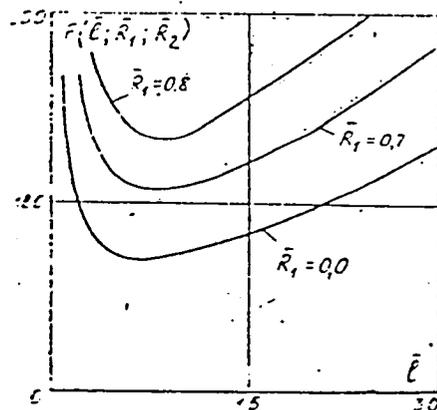


Figure 3. Graphs of function  $F(\bar{l}; \bar{R}_1; \bar{R}_2)$  as a function of relative length  $\bar{l}$  when  $\bar{R}_2 = 1.1$ .

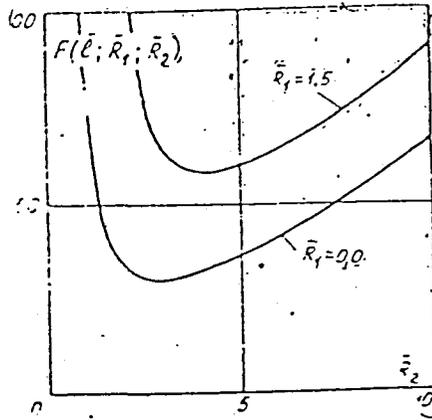


Figure 4. Graphs of minimum values of function  $F(\bar{l}; \bar{R}_1; \bar{R}_2)$  as a function of  $\bar{R}_2$ .

Figure 4 shows graphs of the minimum values of function  $F(\bar{l}; \bar{R}_1; \bar{R}_2)$  corresponding to  $\bar{l}_{opt}$  as a function of outside radius  $\bar{R}_2$  for different inside radii  $\bar{R}_1$ . The absolute minimum value of three-variable function  $F(\bar{l}, \bar{R}_1, \bar{R}_2)$  and the optimum solenoid geometric dimensions corresponding to this minimum can be found by using a computer. Calculations give the following values:  $\bar{l} = 1.35$ ;  $\bar{R}_1 = 0.10$ ,  $\bar{R}_2 = 2.9$ . The minimum value of function  $F_{min}$  is 29.994.

Power consumed by the solenoid can be further reduced either by profiling the solenoid [4], or by using superconductive electromagnets [2].

## REFERENCES

1. Katsnel'son, O. G., Edel'shteyn, A. O., Avtomaticheskiye izmeritel'nyye pribory s magnitnym podveshivaniyem [Automatic Measuring Devices with Magnetic Suspension], Moscow, "Energiya" Press, 1970, pp. 163-175.
2. Magnitnaya podveska modeley v aerodinamicheskikh trubakh. Obzory, perevody, referaty. [Magnetic Suspension of Models in Wind Tunnels. Surveys, Translations, Abstracts.], Scientific-Technical Information Department of the N. E. Zhukovskiy Central Aerodynamic Institute, No. 557, 1979, pp. 3-35.
3. Ioffe, B. A., Kalinin', R. K., Orientirovaniye detaley elektromagnitnym polem [Orienting Components with a Magnetic Field], Riga, "Znaniye" Press, 1972, pp. 25-30.
4. Montgomery, D. B., Polucheneye sil'nykh magnitnykh poley s pomoshch'yu solenoidov [Obtaining Strong Magnetic Fields with Solenoids], Moscow, "Mir" Press, 1971, pp. 37-40.

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