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NAVIGATION STUDY FOR LOW-ALTITUDE EARTH SATELLITES

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NAVIGATION STULY FOR LOW-ALTITUDE EARTH SATELLITES

Prepared for

GODDARD SPACE FLIGHT CENTER

Вy

COMPUTER SCIENCES CORPORATION

Under

Contract NAS 5-27888 Task Assignment 44500

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ABSTRACT

This document describes several navigation studies for lowaltitude Earth satellites. The use of Global Positioning System Navigation Package data for Landsat-5 orbit determination is evaluated. In addition, a navigation analysis for the proposed Tracking and Data Acquisition System is presented. This analysis, based on simulations employing oneway Doppler data, is used to determine the agreement between the Research and Development Goddard Trajectory Determination System and the Sequential Error Analysis Program results. Properties of several geopotential error models are studied as they apply to orbit navigation error anlaysis, and an exploratory study of orbit smoother process noise is presented.

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SECTION 1 - INTRODUCTION

This document describes several studies performed for the National Aeronautics and Space Administration/Goddard Space Flight Center (NASA/GSFC) relating to low-altitude Earth satellite navigation analysis. The first two studies analyzed the accuracy of satellite orbit determination using advanced navigation systems: the Global Positioning System (GPS), currently under development, and the Tracking and Data Acquisition System (TDAS), under study as a successor to the Tracking and Data Relay Satellite System (TDRSS). The latter two studies analyzed lumped geopotential modeling and orbit smoother process noise, two major components associated with orbit determination error analysis.

The GPS navigation study analyzed the orbit determination capabilities of the Landsat-5 (705-kilometer (km) altitude, 98-degree (deg) inclination) satellite. Landsat-5 uses navigation messages from GPS satellites that are extracted by an onboard Global Positioning System Navigation Package (GPSPAC). This study extended the effort of a previous analysis¹ that considered Landsat-4 GPSPAC data. The results of the Landsat-5 study and its comparison with the Landsat-4 study are presented in Section 2.

The TDAS navigation study, presented in Section 3, analyzed the performance of a 600-km, 28-deg inclination satellite using simulated TDAS one-way Doppler data. The study used a

¹B. T. Fang and E. Seifert, "An Evaluation of Global Positioning System Data for Landsat-4 Orbit Determination," paper delivered at AIAA 23rd Aerospace Science Meeting, January 1985; also Computer Sciences Corporation, CSC/TM-84/6077, <u>Tracking and Data Acquisition System/</u> <u>Global Positioning System (TDAS/GPS) Navigation Analysis</u>, September 1984.

number of TDAS enhancements that have been made to the Research and Development Goddard Trajectory Determination System (R&D GTDS). It served as a verification of a previous study that considered the same satellite scenario but used the TDAS enhanced Sequential Error Analysis (SEA) program.

The analysis of lumped geopotential modeling, presented in Section 4, studied several error models. All models use spherical-harmonic representations but with different sets of coefficients representing the errors. Global gravity error maps and orbit propagation errors corresponding to different error models are presented.

The orbit_smoother process noise study investigated the new smoother capacity to the SEA program. Limited investigations using this capacity have been performed to further explore orbit smoothers and also to validate the fading memory process noise option of the SEA smoother capability. The results of this study are presented in Section 5.

Appendix A describes the validation of the SEA program smoother/TDAS capability used in the orbit smoother process noise study. Appendix B describes utilities used in conjunction with the lumped geopotential error model study.

SECTION 2 - LANDSAT-5 ORBIT DETERMINATION USING GPSPAC DATA

This section discusses the accuracies of GPSPAC data for computing Landsat-5 orbits. The GPSPAC data were extracted from telemetry and processed by a large, sophisticated, batch orbit determination program (R&D GTDS) to produce 16-hour arc orbit solutions. The accuracies of the GPSPAC data and the orbit solutions were inferred from the following:

- Observation residuals
- Overlap ephemeris comparisons
- Comparisons with independent solutions derived from ground tracking data

As with the Landsat-4 GPSPAC data, it was found that pseudorange data appear inferior to delta pseudorange (Doppler) data. Efforts were made to determine whether pseudorange data are corrupted by several possible preprocessing sources of errors or whether data from individual GPS satellites may be defective. The latter effort involved computing Landsat-5 orbits from data from a single GPS satellite and was also a subject of interest by itself.

Section 2.1 presents an overview of the data studied and the orbit determination scenarios used. Section 2.2 describes Landsat-5 orbit solutions computed from GPSPAC data; Section 2.3, solutions based on data originating from single GPS satellites; and Section 2.4, solutions obtained from ground tracking data and inquiries into their accuracy degradation in comparison with Landsat-4 solutions. Section 2.5 investigates several possible sources of preprocessing errors and Section 2.6 summarizes the conclusions of the study.

2.1 OVERVIEW OF STUDY DATA

The Landsat-4 spacecraft (705-km altitude, 98-deg inclination orbit), launched in July 1982, carried an experimental NAVSTAR (Reference 2-1) GPSPAC and was the first satellite to use the GPS. The GPSPAC has a receiver/processor assembly that receives and decodes GPS tracking measurements and estimates the Landsat-4 position and velocity by using an onboard Kalman filter. The tracking measurements provideo by GPSPAC are called pseudoranges and delta-pseudo ranges. The former are decoded from pseudorandom noise ranging code and represent measured signal transit times from the GPS satellites to Landsat-4. The latter are computed from Doppler shifts of carrier signals, integrated over a nominal interval of 0.6 second. The term "pseudo" is used because these measurements were derived from the Landsat clock, which was not synchronized with the GPS clocks. The quoted precisions of these data are 1.5 meters (m) for the pseudorange and 2 centimeters (cm) for the delta pseudorange.

Landsat-5, launched in July 1984, is a replacement for the disabled Landsat-4 spacecraft. It has similar mission objectives and orbit characteristics. It also carries a GPSPAC with minor software modifications to avoid some known anomalies (Reference 2-2) that occurred in the Landsat-4 GPSPAC.

During the previous task assignment (42100), an investigation of the Landsat-4 GPSPAC data quality (Reference 2-3) was undertaken. The present study extended that effort to Landsat-5 GPSPAC data. As in the Landsat-4 study, the R&D GTDS batch orbit determination differential correction (DC) program was used to process both the GPSPAC telemetry to the ground and Ground Spaceflight Tracking and Data Network

(GSTDN) data. R&D GTDS allows extensive force modeling that is unavailable in the onboard GPSPAC Kalman filter.

The data in this study were obtained over four separate time periods: in April and August of 1984, and in May and July of 1985. The baseline force model and the orbit determination scenario used for the GSTDN and GPSPAC data solutions are as follows:

GPSPAC data solutions

21-by-21 Goddard Earth Model (GEM)-9 geopotential model Jacchia-Roberts atmospheric density model Cowell integrator 16-hour data arc length Solve for orbital elements, drag parameter, clock bias, clock drift Select every 10th pair of

observations

Use observation standard deviations = 1000 m (pseudorange) and 0.8 cm (delta pseudorange) GSTDN data solutions

21-by-21 GEM-9 geopotential model Jacchia-Roberts atmospheric density model Cowell integrator 30-hour data arc length Solve for orbital elements, drag parameter Select all observations

Use range-rate observations only for orbit solution

2.2 ANALYSIS OF LANDSAT-5 GPSPAC DATA ORBITS

Eight 16-hour data arcs using the NAVSTAR system's GPS data, as received by Landsat-5 GPSPAC, were processed with the R&D GTDS DC program and the same baseline force model employed in analyzing the Landsat-4 GPSPAC orbits. (These orbits will henceforth be referred to as the baseline set of GPSPAC data orbits.) As will be discussed in Section 2.4, the Landsat-5 GSTDN solutions displayed ephemeris overlap differences consistently larger than those observed for Landsat-4. In comparison, the Landsat-4 GSTDN solutions displayed enough accuracy to be used as definitive solutions. Because of this degradation, the Landsat-5 GSTDN orbits could not be used as definitive solutions for comparison with corresponding GPSPAC solutions. Therefore, the present Landsat-5 analysis used the comparison among overlapping GPSPAC data orbit ephemerides and observation residuals to provide an idea of the GPSPAC accuracies.

The maximum ephemeris position differences for the four Landsat-5 GPSPAC data overlap periods vary from 64 to 19 m, compared to maxima with an average $\supset f 2$ m, and a standard deviation of 14 m for six Landsat-4 GPSPAC overlap periods. As shown in Table 2-1, the 1984 GPSPAC overlap comparisons of 61 and 64 m are larger than the 1985 GPSPAC overlap comparisons of 19 and 32 m. (It is interesting to note that studied GPSPAC data solutions in 1985 involve six GPS satellites whereas those in 1984 involve five; nonetheless, reference to GPSPAC data solutions by the year of observation is for convenience only.) The improvement in the overlap comparisons for the 1985 GPSPAC data solutions, but no improvement in the corresponding 1985 GSTDN data (which is summarized in Section 2.4), appears to rule out the possibility that some unexplained dynamic errors common to GSTDN and GPSPAC data solutions are responsible for poor 1984 GPSPAC comparisons.

An examination of data residuals of the Landsat-5 GPSPAC orbit solutions shows that large pseudorange measurement residuals exist and vary substantially from GPS satellite to GPS satellite. These characteristics are in agreement with those observed in the Landsat-4 GPSPAC data solutions. Figure 2-1, which is a partial listing of a typical Landsat-5 GPSPAC observation residual report illustrating the large pseudorange residuals, displays no correlation between pseudorange residuals and delta-pseudorange measurements. This rules out systematic time tag errors as possible sources for the systematic GPSPAC range errors observed.

RUN	ARC START TIME	ARC LENGTH	NO OF OBSERVA	SOLVE FOR PARAMETERS				RESIDUAL MAXIMUM POSITION DIFFERENCES STATISTICS OVER 4 HOUR OVERLAP OF ADJACENT DEVIATIONS ARCS (meters)						IUM POSIT M GSTDN (REMARKS			
	(date hour)	(hours)	TIONS	£1	B (10 ⁻³ sec)	B (10 ⁻⁸ sec/ sec)	RANGE (meters)	DELTA RANGE {cm}	RADIAL	с	ALONG TRACK	RSS	RADIAL	с	ALONG TRACK	RSS		
G4A	840413	16	1297	1 592	- 3 127	- 3 262	100 1	2 39					13 4	30 6	45 1	54 3		1
	2 h								5 69	14 4	61 0	61 3						Ļ
G48	840413 14 h	16	1192	2 900	- 4 772	- 3 257	71 50	2 27					10 6	35 2	70 3	77 1	ONLY EVERY 10TH PAIR OF OBSERVATION DATA PROCESSED	
G8A	840807	16	1103	2 125	1 036	- 2 283	84 25	2 25					14 0	16 9	49 1	50 4	•	
	3 h								16 6	76	63 8	63 9	1					ſ
G8B	840807	16	1110	3 011	- 0 197	- 2 278	83 02	2 38					24 3	7 89	68 0	68 3		
	15 h																	+
G5A	850524	16	1190	4 913	- 2 228	- 0 6494	76 44	2 21					13 5	11 9	52 2	53 3		ļ
ł	19 h]							4 94	7 67	17 9	19 4			ł		1	I
G5B	850525	16	1146	- 6 119	- 2 508	- 0 6467	66 33	2 19					18 9	3 12	77 2	77 3		
	7 h																1	
G7A	850726	16	1142	2 493	- 0 6720	- 0 3611	84 39	2 18					-	_	- 1	-	l .	
	Oh								5 08	19 4	29 5	32 1						85
G7B	850726	16	1000	- 2 259	- 0 8280	- 0 3571	53 93	2 18					_	-	-	-		76a*)
L	12 h						l											0112

Table 2-1. Landsat-5 GPSPAC Data Orbit Solution Characteristics and Comparisons With GSTDN Solutions

NOTES SATELLITE AND TIME PERIOD LANDSAT 5 APRIL 1984 - JULY 1985

DATA GPS RANGE AND DELTA RANGE WITH RANGE WEIGHTED LIGHTLY

FORCE MODEL BASELINE

1

SOLVE FOR PARAMETERS DRAG SCALE FACTOR $e_1 = \Delta C_D / C_D$, CLOCK BIAS B AND DRIFT B AT EPOCH

C L AND RSS ARE THE ACROSS TRACK ALONG TRACK AND ROOT SUM SQUARED COMPARE DIFFERENCES RESPECTIVELY

1

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GIDS OBSERVATION RESIDUAL REPORT

							END	OF	ITERATION	NUMBER	5								
TIME OF OBS	i		GPS	NO	EDIT	OBS	0		0-0	2	R A T	10	с		ELV	10	T A	0	BS
YYMMDD HHMM	55	5555				TYPE					10 S	IGMA			GPS	5		N	0
840414 0335	31	3291		3		RGPS	20555	996	6 57	7255	0	0577	20555	9389	26	47	0 0	1099	
840414 0335	31	3291		3		DELA	0	193	60	4729	0	5911	0	1936	26	47	0 0	1100	
840414 0336	50	6492		3		AGPS	20608	793	9 56	0749	0	0561	20608	7379	25	89	00	1101	
840414 0336	50	6492		3		DELR	0	607	3 0	5600	0	7000	0	6073	25	88	0 0	1102	
840414 0337	56	6295		3		RGPS	20694	035	2 56	7501	0	0568	20693	9784	24	99	0 0	1103	
840414 0337	56	6295		3		DELR	0	944	6 - 0	8825	1	1031	0	9447	24	98	0 0	1104	
840414 0339	11	4100		3		RGPS	20834	787	5 54	9823	0	0550	20834	7325	23	54	0 0	1105	
840414 0339	11	4100		Э		DELR	1	314	4 2	2863	2	8579	1	3144	23	53	0 0	1106	J
840414 0340	45	4795		2		RGPS	23799	309	5 47	8019	Ö	0478	23799	2617	- 1	31	0 0	1107	
840414 0340	45	4795		2		DELR	4	386	0 -1	3533	1	6916	4	3860	- 1	34	0 0	1108	
840414 0342	32	4520		3		RGPS	21428	875	5 53	5017	Ó	0535	21428	8220	17	76	0 0	1109	J
840414 0342	32	4520		3		DELR	2	205	3 - 4	5615	5	7018	2	2053	17	74	0 0	1110	,
840414 0344	02	3532		3		RGPS	21784	789	6 50	3040	õ	0503	21784	7393	14	48	0 0	1111	
840414 0344	02	3532		3		DELR	2	540	4 - 2	4399	3	0499	2	5404	14	45	0 0	1112	
840414 0345	24	4544		3		RGPS	22150	929	8 48	9816	õ	0490	22150	8808	11	21	0 0	1113	
840414 0345	24	4544		3		DELR	2	806	6 -1	5124	ī	8906	2 2	8066	11	18	ōō	1114	
840414 0347	27	2582		4		AGES	23359	556	ล้ คว่	6347	ò	0836	23359	4731	2	07	ōō	1115	
840414 0347	27	2582		à		DELR	- 3	090	5 3	0651	ž	8314	- 3	0906	2	10	ōŏ	1116	
840414 0348	47	4369		à		RCPS	22950	227	g 85	5167	ō	0855	22950	1884	š	46	ōŏ	1117	
840414 0148	47	4369		Å			- 1	631	5 -0	6679	ŏ	8149	- 1	0315	5	48	ñ ñ	1119	
840414 0350	n a	2165		4		PCPS	22547	004	0 86	9179	ň	0045	22547	0081	ă	86	ňň		
840414 0350	0 Q	2155		4			- 2	054	1 4	6284	š	7855	- 2	9542	8	89	ňň	1120	
840414 0351	27	1200		7		DCDS	24000	200	50	5010	2	0506	24000	2296	- 4	00	ňň	1121	
840414 0351	57	7209		1			1 1	403	a 50	1222	ň	0216	1 1	4070	- 5	01	ňň	1122	
	£ 7	0026		3		BCBS	24604	1340		4054	2	0614	24604	1000		åa	ňň	1122	
B40414 0352	53	5620		2		DELO	24004	610	4 51	4004	~	2050	24004	5300		99	~ ~	1123	
940414 0352	22	2716		3		DCDS	21244	010		0376	6	2938	21244	5390		65	~ ~	1124	
B40414 0354	27	2715		7		0610	21344	510	9 90 0 6	3494	č	5606	- 2	5020		69	~ ~	1125	
840414 0354	22	2/15		4			21067	047	0 5 3 1/5	2404	0	1053	21052	742.	19	22		1120	,
840414 0355	33	2100		2		0510	21007	457	3 105	0770	ž	4777	41007	1 = 7 3	22	34	~ ~	1127	
840414 0355	33	2100		2		DELK	20750	40/	4 107	9770	6	1000	20750	1072	26	34	~ ~	1120	
840414 0356	51	0495		2		NGP3	20/39	371	1 107	9902	Ň	0707	20/35	2034	20	35	000	1129	
840414 0358	51	0495		7		DCDC	20510	234		1462	~	0703	20510	2544	20	~ 1		1130	
840414 0357	26	3687		4		NGP5	20510	3/0	2 108	1404	Ě	0620	20510	20/4	24	97	00	1131	
840414 0357	28	308/		4		DCDC	20202	140	6 4 E 111	0304	5	0029	20202	7407	20	39		1132	
840414 0359	24	3080		4		NGPS	20283	819	5 111	1303		2242	20283	/103	30	39		1133	
840414 0339		3080		4		DELK	20078	9/8	9 -0	1/94	×	1120	20075	5/69	30	41		1134	
840414 0400	10	24/3		4		HUPS OFLO	20075	041	0 II3	8094	2	1139	20075	3212	32	22	00	1135	
840414 0400	10	2473		4		DELR	10006	800	· · · ·	8112	É	2040	10000	1664	34	20	00	1130	, ,
840414 0401	10	2000		4		RUPS	19880	800		9890	Ŷ	1130	13000	7334	34	0.0		1137	
840414 0401	16	2066		4		DELK	10001	524	5 -1	4928		8660	10607	6245	34	90	00	1138	
840414 0402	35	4460		4		RGPS	19681	305	1 114	0285	, v	1140	19687	1911	34	20	00	1139	
840414 0402	32	4460		4		DELR		393	9 1	/330	4	1662	105.1	7979	37	28	00	1140	
840414 0403	11	4255		4		HGPS	19544	882	1 114	2552	, v	1143	19244	/6/9	39	03	00	1141	
840414 0403	41	4255		4		DELK		137	3 0	3029	, v	3/8/		1977	79	05	00	1142	
840414 0404	4/	3621		4		HGPS	19424	964	5 119	1068	0	1192	19424	8453	40	5/	0 0	1143	1
840414 0404	4/	3651		4		DELR	- 0	986	2 1	3532	1	6915	- 0	9862	40	58	0 0	1144	
840414 0405	53	J248		4		RGPS	19328	087	9 113	9587	0	1140	19327	9/40	41	84	0 0	1145	1
840414 0405	53	3248		4		DELR	-0	773	5 -0	7324	0	9154	- 0	7735	41	85	0 0	1146	1
840414 0407	12	6445		4		RGPS	19242	919	1 114	6570	0	1147	19242	8044	42	99	0 0	1147	
840414 0407	12	6445		4		DELR	- 0	512	2 1	3105		6381	- 0	5122	43	00	0 0	1148	
840414 0408	18	6243		4		RGPS	19198	568	0 114	0210	0	1140	19198	4540	43	61	0 0	1149	j.
840414 0408	18	6243		4		DELR	- 0	292	1 0	6002	0	7503	- 0	2921	43	61	0 0	1150	J.
840414 0409	24	5443		4		RGPS	19178	513	z 114	8783	0	1149	19178	3984	43	89	00	1151	
840414 0409	24	5443		4		DELR	- 0	071	0 - 1	7220	2	1525	- 0	0709	43	89	0 0	1152	
840414 0410	30	4643		4		RGPS	19182	747	3 115	0050	0	1150	19182	6323	43	84	0 0	1153	,
840414 0410	30	4643		4		DELR	0	149	8 - 3	2074	4	0092	0	1499	43	84	0 0	1154	
840414 0411	44	4827		5	* * *	RGPS	24689	352	4 135	7784	0	1358	24689	2167	43	84	0 0	1155	r i i i
840414 0411	41	4827		5	• • •	DELR	- 3	845	7 1	5200	1	9000	- 3	8457	43	84	0 0	1156	i
840414 0413	50	2200		5		RGPS	23878	572	9 137	8933	0	1379	23878	4350	0	37	0 0	1157	
840414 0413	50	2200		5		DELA	- 3	883	6 0	7933	0	9917	- 3	8836	0	40	0 0	1158	j.
840414 0415	43	0254		4		RGPS	19525	721	1 109	6832	0	1097	19525	6115	39	35	0 0	1159	J.

OBSERVATIONS AND COMPUTED OBS	UNITS FOR INFORMATION RESIDUALS	EDII FLAG
RANGES ARF IN KM RATES AND RANGE DIFFERENCES ARE IN KM/SEC ANGLES ARE IN DEGREES DIR COSINES SCALED BY 1000 DTIC ARE IN MICROSECONDS	RANGES ARE IN METERS RATES AND RANGE DIFFRN ARE IN ANGLES ARE IN SECONDS OF ARC DIR COSINES SCALED BY 1000 DTIC ARE IN MICROSECONDS	 =COMPUTE(O-C) (NOT IN NORMAL MATRIX) I CM/SEC++ =EDIT BY ELEVATION ANGLE +++ =EDIT BY 3 SIGMA CRITERIA +++= EDIT FROM SCOPE * = EDIT BY ATMOSPHERIC INTERFERENCE

Figure 2-1. Partial Observation Residual Report for GPSPAC Data Orbit Solution (Run G4B)

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Studies (discussed more fully in Section 2.5) that examine the effects of correcting assumed GPSPAC time tag errors give results that support this conclusion about no time tag errors. GPSPAC data observation residuals will be discussed further in Section 2.3.

In keeping with the methods employed in the Landsat-4 GPSPAC analysis, the baseline GPSPAC data orbit determination scenario was repeated with two different a priori observation weight specifications. When the weights were set to 10 m for pseudorange observations and 1000 cm for deltapseudorange observations (effectively producing a range-only solution), the orbit comparison with the independent GSTDN data orbit produced larger differences than those seen in the baseline delta-range-only solutions in Table 2-1. When the weights were set to 1.5 m and 0.2 cm, respectively (in accordance with quoted data precision), the orbit solutions resulted in larger overlap differences than the baseline delta-range-only solutions but were typically smaller than the corresponding range-only solution. These trends in the variously weighted Landsat-5 GPSPAC solutions are in agreement with the trends observed in the Landsat-4 data. Table 2-2 summarizes the Landsat-5 results.

2.3 ORBIT SOLUTIONS USING DATA FROM SINGLE GPS SATELLITES

As discussed in Section 2.2, the observed large pseudorange residuals present in the GPSPAC data solutions do not appear to be specific to any single GPS satellite. Nevertheless, there was interest in whether intercomparisons of GPSPAC solutions, each using data from only a single GPS NAVSTAR satellite, would divulge erratic data associated with a GPS or would provide insight into the cause of the observed large pseudorange residuals. It was uncertain whether single GPS relay solutions would even converge because of the lack of

RUN	RUN ARC START ARC NO OF		SOLVE FOR PARAMETERS			RESI STATI STAN DEVIA	DUAL STICS, IDARD TIONS	MAXIMUM POSITION DIFFERENCES OVER 4 HOUR OVERLAP OF ADJACENT ARCS (meters)				MAXIN FRO	IUM POSIT M GSTDN (REMARKS			
	(date, hour)	(hours)	TIONS	e1	B (10 ⁻³ sec)	8 (10 ⁻⁸ sec/ sec)	RANGE (meters)	DELTA RANGE (cm)	RADIAL	с	ALONG TRACK	RSS	RADIAL	С	ALONG TRACK	RSS	
R4A	840413	16	1295	-0 209	-3 128	-3 261	41 85	2 66					25	25	70	73	
1	2 h								72	18	48	51					RANGE SOLUTION
R48	840413	16	1191	1 316	-4 772	- 3 256	50 35	2 80					30	13	112	113	
	14 h																
R8A	840807	16	1102	19 757	1 036	- 2 283	64 52	3 23					43	15	133	134	
1	3.1								45	23		1/2					PAIR OF OBSERVATION
R8B	840807	16	1109	15 56	-0 197	-2 278	68 52	3 12					31	16	99	101	DATA PROCESSED
	15 h								,								
P4A	840413	16	1278	0 867	- 3 128	-3 261	36 79	2 62					24	28	64	68	
	2 հ								29	14	36	39				1	
P4B	840413	16	1183	0 969	- 4 772	3 256	48 01	2 62					26	18	101	103	
	14 h																EVENLY WEIGHTED
P8A	840807	16	665	67 56	1 035	-2 283	55 26	3 08					49	33	188	191	300011014
	3 h								48	24	177	178					ONLY EVERY 10TH
P8B	840807	16	1103	36 79	-0 197	-2 277	63 93	3 13					32	21	122	122 125 DATA PRO	DATA PROCESSED
L	15 h	l															

Table 2-2. Landsat-5 GPSPAC Data Range-Rate and Evenly Weighted Orbit Solution Characteristics and Comparisons With GSTDN Solutions

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NOTES SATELLITE AND TIME PERIOD LANDSAT 5 APRIL-AUGUST 1984

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FORCE MODEL BASELINE

SOLVE FOR PARAMETERS DRAG SCALE FACTOR $e_1 = \Delta C_D / C_D$ CLOCK BIAS B AND DRIFT B AT EPOCH C L AND RSS ARE THE ACROSS TRACK ALONG TRACK AND ROOT SUM SQUARED COMPARE DIFFERENCES RESPECTIVELY

sufficient geometry. First, all observations, except for those associated with the requested GPS satellite, were edited from the GPSPAC data. Next, the resulting single GPS satellite data were input into an unmodified R&D GTDS run to process GPSPAC data. These single relay orbit solutions-except as otherwise specified--used the same dynamics, modeling, etc., employed in the corresponding composite relay solutions.

Contrary to geometrical considerations, the single GPS satellite solutions displayed robustness in their ability to recover the clock parameters and to converge using very short observation arcs. The single GPS solutions can converge in as little as two Landsat orbital periods provided that the observation timespan's placement is chosen so as to minimize GPS-Landsat nonvisibility periods. Also, the single GPS satellite solutions, even those of short duration, can recover the clock parameters (clock bias and drift) when no a priori information is provided. Table 2-3 summarizes the characteristics of several single GPS satellite GPSPAC data solutions.

Recovery of the clock parameters to a high degree of agreement, together with the single relay solution's ability to converge even with no a priori clock information, indicates that the clocks in the GPSPAC data are highly observable. This high clock observability provides the ability to resolve small variations in the clock parameters. This clock variability is evident, in Table 2-3, between range and delta-range solutions over the same observation timespan. The clock parameters can be expressed in terms of their resulting corrections to pseudorange measurements to yield an effective range offset. Using this technique, the variability of the observed clock for the ensemble of single GPS satellite solutions over the same observation timespan is presented in Table 2-4.

RUN ^a	OBSERVATIONS FROM GPS		NO OF	RESII STATI STAN DEVIA	DUAL STICS, DARD TIONS	SOLVE	FOR PARAM	ETERS	
1D	SATELLITE NO	(hours)	TIONS	RANGE (meters)	DELTA RANGE (cm)	ę1	B (10 ⁻³ sec)	B (10 ⁻⁸ sec/ sec)	
G42A	2	3	577	2 35	2 01	- 0 290	,- 3 1277	- 3 2631	COMBINED SOLUTION
G42B	2	3	577	2 35	2 01	- 0 290	-3 1277	- 3 2631	COMBINED SOLUTION, ZERO A PRIORI CLOCK PARAMETERS
G43A	3	2 5	430	41 86	2 01	0 001	- 3 1276	- 3 2640	DELTA-RANGE SOLUTION
G43B	3	2 5	423	1 53	2 02	-0 145	-3 1280	3 2606	COMBINED SOLUTION
G43C	3	3	592	12 91	2 80	0 007	- 3 1269	- 3 2668	RANGE SOLUTION
G43D	3	3	592	24 34	2 09	- 0 003	-3 1279	- 3 2615	DELTA-RANGE SOLUTION
G43E	3	3	585	2 12	2 11	0 557	-3 1276	- 3 2631	COMBINED SOLUTION
G43F	3	3	585	2 12	2 11	0 557	- 3 1276	- 3 2631	COMBINED SOLUTION, ZERO A PRIORI CLOCK PARAMETERS

Table 2-3.	Characteristics	of	GPSPAC	Data	Solutions	Usinq	Observations	From	Single
	GPS Satellites					2			2

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NOTES SATELLITE AND TIME PERIOD LANDSAT-5, APRIL 1984

DATA ALL AVAILABLE PAIRS OF OBSERVATIONS PROCESSED

FORCE MODEL BASELINE

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SOLVE-FOR PARAMETERS DRAG SCALE FACTOR $\rho_1 = \Delta C_D/C_D$, CLOCK BIAS B, AND DRIFT B AT EPOCH

^aALL SOLUTION ARC TIMES START ON 840413, 2 HOURS

^bALL SOLUTIONS INVOLVE PAIRS OF GPS RANGE AND DELTA-RANGE OBSERVATIONS IN COMBINED SOLUTIONS, BOTH DATA TYPES HAVE COMPARABLE WEIGHTINGS IN DELTA-RANGE SOLUTIONS, RANGE IS WEIGHTED LIGHTLY, IN RANGE SOLUTIONS, DELTA-RANGE IS WEIGHTED LIGHTLY

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RUN ^a ID	OBSERVATIONS FROM GPS	NO OF	RESIDUAL STATISTICS, STANDARD DEVIATIONS		SOLVE	-FOR PARAM	RANGE EQUIVALENT CLOCK DIFFERENCE	
	SATELLITE NO	TIONS ^b	RANGE (meters)	DELTA RANGE (cm)	۴ı	B (10 ⁻³ sec)	B (10 ⁻⁸ sec/ sec)	FROM COMPOSITE ^C (meters)
G4A	ALL GPSs-COMPOSITE	1297	100 1	2 39	1 591	-3 12752	- 3 26234	_
G41	1	2650	67 0	2 20 ·	- 3 280	- 3 12855	- 3 25963	76
G42	2	2446	152 6	2 20	0 487	- 3 12708	- 3 26375	- 10
G43	3	2581	185 3	2 27	1 621	- 3 12681	- 3 26434	- 38
G44	4	3000	180 4	2 49	9 872	- 3 12924	- 3 25785	130
G45	5	2080	55 4	2 29	-0 331	- 3 12828	- 3 26020	45

Table 2-4. Intercomparisons of GPSPAC Data Solutions Using Single and Composite GPS Observation Sets

NOTES SATELLITE AND TIME PERIOD LANDSAT-5, APRIL 1984

DATA GPS RANGE AND DELTA-RANGE, WITH RANGE WEIGHTED LIGHTLY

FORCE MODEL BASELINE

SOLVE-FOR PARAMETERS DRAG SCALE FACTOR $\rho_1 = \Delta C_D/C_D$, CLOCK BIAS B, AND DRIFT B AT EPOCH

^aALL SOLUTIONS HAVE DATA ARC LENGTHS OF 16 HOURS STARTING ON 840413, 2 HOURS

^bFOR COMPOSITE SOLUTION, ONLY EVERY 10TH PAIR OF OBSERVATION DATA IS PROCESSED, FOR SINGLE GPS SATELLITE SOLUTIONS, ALL PAIRS OF OBSERVATION DATA ARE PROCESSED

^CTHIS VALUE IS THE DIFFERENCE BETWEEN THE RANGE EQUIVALENT CLOCK ERROR FOR RUN ID G4A AND THE RANGE EQUIVALENT CLOCK ERROR FOR THE GPS SATELLITE SOLUTION CORRESPONDING TO THE TABLE ENTRY THE RANGE EQUIVALENT OF CLOCK ERROR IS CALCULATED AS $\delta R = (B + B \Delta t) C$, WHERE Δt IS CHOSEN AS HALF THE SOLUTION ARC LENGTH, OR 8 HOURS, AND C IS THE SPEED OF LIGHT

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Possibly related to the observed clock variations are characteristic gross structure signatures of the pseudorange residual in the GPSPAC solution plots. The typical pseudorange residual plots can be fit fairly well with a linear, nonzero slope function. This is most pronounced in single GPS satellite solutions but is also present in composite GPS solutions. Representative pseudorange residual plots for both single GPS satellite and composite GPS solutions are shown in Figure 2-2. One possible interpretation of the nonzero slope structure in the pseudorange residuals is that an inconsistency occurs in the observed clock drift rate between the pseudorange and delta-pseudorange GPSPAC data measurements.

In the search for information pertaining to the anomalous large pseudorange residuals, the inconsistency between pseudorange and delta-pseudorange measurements was rediscovered. This was previously discussed in connection with comparisons of GPSPAC data delta-range solutions to range solutions. In those instances, the inconsistency was most notable in the Landsat-4 analysis, when the delta-range solutions gave better comparison with GSTDN solutions than the corresponding range or evenly weighted solutions. In its present manifestation, the inconsistency can be interpreted as a mismatch between the observed clock parameters for delta pseudorange and pseudorange data. Alternately, the inconsistencies could be attributed to uncorrected signal propagation errors or difficulties with electronics.

Finally, intercomparisons between single GPS satellite solutions and between single satellite and composite solutions did not reveal any highly erratic single GPS satellite. All single satellite solutions agree within a maximum of \sim 80 m, and typically less than \sim 40 m. When observations corresponding to that GPS satellite for which single GPS satellite solution intercomparisons show the largest deviations

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Figure 2-2. Representative Observation Residual Plots for GPSPAC Data Solutions Employing Composite and Single GPS Satellite Observation Sets

- (a) Range residuals for a solution that employs observations from all available GPS NAVSTAR satellites a composite solution (Run G7B).
- (b) Composite solution's corresponding delta-range residuals. Delta-range residual plots for single GPS satellite solutions display similar signature and residuals.
- (c) Range residuals for a GPSPAC data solution using observations from a single GPS satellite (Run G-43).

were edited from a composite solution, the large pseudorange residuals are still seen.

2.4 ASSESSMENT OF LANDSAT-5 ORBITS COMPUTED FROM GSTDN DATA

2.4.1 COMPARISON OF LARGE OVERLAP DIFFERENCES 10 LANDSAT-4 GSTDN SOLUTIONS

GSTDN data for this task were processed in 30-hour overlapping arcs, with overlap periods of 6 hours each. The difference between two adjacent orbital solutions in the overlap period serves as a measure of the GSTDN datadetermined orbital accuracy. In this study, Landsat-5 GSTDN data from two different calendar years were processed. Overlapping arcs, sets of two runs each, were processed for April and August 1984 and for May 1985. The first two sets correspond to available GPSPAC data sets. The May 1985 GSTDN data were chosen, based on optimal GSTDN and GPSPAC data availability, from 13 timespans in 1985.

The maximum ephemeris position differences for the three overlapping periods were 106, 59, and 110 m. The rootmean-square (rms) ephemeris position differences for the two overlap periods were 64, 33, and 83 m. These differences are considerably greater than those in the Landsat-4 study. For Landsat-4, the maximum ephemeris position differences of seven overlap comparison periods averaged 29 m, with a standard deviation of 13 m. The rms ephemeris position differences for the Landsat-4 overlap periods averaged 18 m, with a standard deviation of 7 m. Tables 2-5 and 2-6 summarize the results of Landsat-5 GSTDN characteristics.

Although this study processed only a limited number of GSTDN tracking intervals, independent results indicate that 1984 and 1985 Landsat-5 solutions give consistently larger overlap differences when compared to the previous Landsat-4

RUN	ARC START TIME (date, hour)	ARC LENGTH	NO OF TRACKING	NO OF OBSERVA-	COMPUTED DRAG SCALE FACTOR	RESIDUAL STATISTICS, RANGE-RATE	MAXIN OVER 6-I	AUM POSIT HOUR OVEF ARCS (ON DIFFERI ILAP OF AD meters)	REMARKS	
		(hours)	INVOLVED	TIONS	$\varrho_1 = \Delta C_D / C_D$	DEVIATIONS (cm/sec)	RADIAL	CROSS- TRACK	ALONG- TRACK	RSS TOTAL	
GDA	840413 0 h	30	3	507	-1 472	3 048	10 6	13 8	105 7	105 8	BASELINE MODEL JACCHIA ROBERTS ATMOSPHERIC DENSITY MODEL A PRIORI
GDB	840414 0 h	30	5	702	-0 919	4 114					DRAG COEFFICIENT $C_D =$ 20, A DRAG SCALE FAC- TOR SOLVED FOR, 21 × 21
GDM	840807 0 h	30	3	399	-8 833	3 478	81	87	58 4	59 2	GEM 9 GEOPOTENTIAL MODEL
GDN	840808 0 h	30	4	444	-7 493	2 956					
S4A	840413 0 h	30	3	507	— 1 96 5	3 035	10 2	13 8	101 1	101 3	HARRIS-PRIESTER F100 ATMOSPHERIC DENSITY MODEL, A PRIORI DRAG
S4B	840414 0 h	30	5	702	-0 674	4 100					COEFFICIENT $C_D = 20$, A DRAG SCALE FACTOR SOLVED FOR, 21 × 21 GEM
S8A	840807 0 h	30	3	399	-3 858	3 454	77	81	69 8	70 3	9 GEOPOTENTIAL MODEL
S8B	840808 0 h	30	4	444	-4 348	2 960					
GMA	840413 0 h	30	3	507	1 549	3 238	10 7	13 6	101 2	101 7	BASELINE ATMOSPHERE MODEL, WITH 36 × 36 GEM 10B GEOPOTENTIAL MODEL
GMB	840414 0 h	30	5	702	1 092	3 860					
GMC	840413 0 h	30	3	507	-1 136	2 775	95	98	83 9	84 2	BASELINE MODEL WITH 36 × 36 GEM 10B GEOPOTEN- TIAL MODEL, MARSH STA-
GMD	840414 0 h	30	5	703	0 959	2 822					TION COORDINATES

Table 2-5. 1984 GSTDN Data Orbit Solution Characteristics

NOTES SATELLITE AND TIME PERIOD LANDSAT-5, APRIL-AUGUST 1984

DATA GSTDN RANGE-RATE DATA

RSS, ROOT-SUM-SQUARED

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RUN	ARC START TIME	ARC LENGTH (hours)	NO OF TRACKING STATIONS INVOLVED	NO OF OBSERVA- TIONS	COMPUTED DRAG SCALE	RESIDUAL STATISTICS, STANDARD DEVIATIONS		MAXIMU OVE AD	JM POSITI R 6-HOUR JACENT A	ON DIFFEI OVERLAP RCS (mete	REMARKS		
	(date, hour)				$\varrho 1 = \Delta C_D / C_D$	RANGE (meters)	DELTA RANGE (cm)	RADIAL	CROSS- TRACK	ALONG- TRACK	RSS TOTAL		
GS1	850524	30	3	239	- 11 07	-	1 319	11 1	26.4	107.3	110.2	BASELINE MODEL	
GS2	850525 6 h	30	5	270	4 40	_	1 396		204	107 3		RANGE-RATE DATA ONLY	
GSA	850524	30	4	400	8 97	10 47	5 361	16.2	19.7	69.0	69.1	NO OBSERVATION PROCESS- ING PERFORMED, BOTH	
GSB	850525 6 h	30	6	387	5 73	4 322	5 775	5 775			0.5 1	RANGE AND RANGE-RATE DATA INCLUDED	

Table 2-6. 1985 GSTDN Data Orbit Solution Characteristics

NOTES SATELLITE AND TIME PERIOD LANDSAT-5, MAY 1985 DATA GSTDN RANGE-RATE DATA

RSS IS ROOT-SUM-SQUARED

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GSTDN solutions. Tracking statistics do indicate an increasing amount of TDRS-East tracking data available for Landsat-5 in 1985. Overlap differences of TDRS-only solutions, associated with the single-TDRS S-band certification results, report 82, 71, 35, and 74 m (Reference 2-4). In addition, private conversations with investigators (Yuri Nakai, Computer Sciences Corporation) who are analyzing 1985 Landsat-5 orbit solution overlap differences using combinations of GSTDN, TDRSS, and Bilateration Ranging Transponder System (BRTS) data indicate ephemeris overlap differences consistently larger than the average 29 m observed for Landsat-4.

2.4.2 ANALYSIS OF LANDSAT-5 LARGER-THAN-EXPECTED OVERLAP EPHEMERIS DIFFERENCES

It was originally thought that these larger-than-expected overlap ephemeris differences could be attributed to inadequacies in atmospheric density modeling. Modeling error was suspected because the overlap comparison plot of the alongtrack difference, as shown in Figure 2-3, displays sinusoidally increasing differences that are generally typical of force modeling mismatch between the orbit solutions involved. No significant improvement was seen, however, when a different atmospheric model (Harris-Priester) was used.

In an attempt to reduce these ephemeris differences, the April 1984 GSTDN data arcs were again processed using the standard orbit determination scenario, but with two variations. First, orbits were obtained by using the 36-by-36 GEM-10B geopotential model. Second, a second set of orbits was obtained by using the Marsh tracking station position coordinates in addition to the GEM-10B model. As was also true in the Landsat-4 study, using these improved models did not result in substantial improvement in orbit determination performance. The results of the 1984 GSTDN orbit determination runs are summarized in Table 2-5.



Figure 2-3. Landsat-5 GSTDN Orbit Solution Overlap Ephemerus Comparison

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Although the previous Landsat-4 experience with unified S-band (USB) tracking data revealed systematic errors in the range observations, the May 1985 GSTDN data arcs were reprocessed using both range and range-rate observations. This was done to determine if range errors were caused by redundant observation correction preprocessing in R&D GTDS. When the preprocessing was deleted, the resulting orbit solutions still displayed large range and range-rate residual statistics. Probably because of the greater observability afforded by the range observations, the maximum position difference was decreased from 110 to 69 m--still large in comparison with the Landsat-4 accuracies. The results of the 1985 GSTDN orbit determination runs are summarized in Table 2-6.

2.4.3 LANDSAT-5 SOLUTIONS INVOLVING FEWER TRACKING STATIONS

In comparison to previous Landsat-4 GSTDN data, the Landsat-5 solutions involved fewer ground tracking stations. In the typical Landsat-4 GSTDN 30-hour arc solutions, between 6 and 10 ground stations were involved in tracking. For the six baseline Landsat-5 GSTDN solutions in Tables 2-5 and 2-6, between three and five tracking stations were involved.

Irregularity of the Landsat-5 tracking passes may also contribute to the larger-than-expected overlap ephemeris differences. Figure 2-4 displays a plot of the ground tracking passes for Landsat-5 GSTDN data, beginning on April 13, 1984. This plot shows the 30-hour intervals for baseline run IDs GDA and GDB and their corresponding overlap interval extending from 0 hours to 6 hours on April 14 (840414).

Because it was suspected that the sparse tracking over the GDA-GDB 6-hour overlap contributed to its poor ephemeris overlap comparison (from Table 2-5, a maximum position difference rss of 106 m), alternate 30-hour arcs were chosen.



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LEGEND	
A – GDS8	NOTES CAPITAL LETTERS INDICATE THE CORRESPONDENCE BETWEEN TRACKING
B — ULA3	PASSES (WITH A TYPICAL DURATION OF 10 MINUTES) AND THE TRACKING
C – MAD3	STATION FROM WHICH THE MEASUREMENT SIGNAL ORIGINATED
D – AG03	THE TRACKING PASSES ABOVE THE TIME AXIS CONTRIBUTE TO THE OR- BIT SOLUTION OVER THE DATA ARC
E - GWM3	THE TRACKING PASSES BELOW THE TIME AXIS ARE PRESENT IN THE
F – GDS3	GSTDN DATA BASE

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Figure 2-4. Plot of Ground Tracking Passes and Orbit Solution Arcs Involving April 1984 Landsat-5 GSTDN Data

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These alternate arcs, labeled GDC and GDD, begin at 840413 18 hours and 840414 18 hours, respectively, and have a 6-hour overlap beginning at 840414 18 hours. As seen from the plot in Figure 2-4, this alternate overlap time includes more uniform tracking. This is reflected in the GDC-GDD overlap ephemeris comparison RSS of 44 m (from Table 2-7), which is a significant improvement over the GDA-GDB overlap (although it is still inferior to the Landsat-4 GSTDN overlap maxima, which have an RSS average of 28.8 m). Part of this improvement may also result because the alternate GDC and GDD arcs involve more tracking stations, four and six, respectively, compared to three and five for GDA and GDB.

A second set of GSTDN data orbit solutions were performed, using 39-hour arcs. These two arcs, labeled GDE and GDF, also have a 6-hour overlap, beginning at 840414 9 hours. The maximum position difference rss of this overlap is 72 m (Table 2-7). Although the number of tracking stations involved remained the same as in the GDC-GDD solutions, the larger orbit arcs resulted in a poorer overlap comparison. This suggests that the relatively small number of stations involved in Landsat-5 GSTDN data cannot be compensated for by extending orbit solutions over arcs of greater duration, thereby increasing the number of observations and possibly the number of tracking stations. Instead, the GDE-GDF overlap, when compared to GDC-GDD errors, indicates that the force modeling errors begin to increase at a greater rate than the observational benefits.

2.4.4 ANALYSIS OF LANDSAT-4 GSTDN SOLUTIONS WITH REDUCED NUMBER OF TRACKING STATIONS

To determine if poor Landsat-5 GSTDN solutions result from the small number of tracking stations involved, Landsat-4 GSTDN solutions with a reduced number of tracking stations were generated. The results of these solutions are summarized in Table 2-8. The first entry in the table, the

RUN	ARC START TIME	ARC	NO OF TRACKING	NO OF OBSERVA-	$\begin{array}{l} \text{COMPUTED} \\ \text{DRAG SCALE} \\ \text{FACTOR} \\ e_1 = \Delta C_D / C_D \end{array}$	RESIDUAL STATISTICS, RANGE-RATE	MAXIN OVER 6-1	IUM POSITI IOUR OVER ARCS (ON DIFFERE LAP OF AD meters)	NCES JACENT	REMARKS
	(date, hour)	(hours)	INVOLVED	TIONS		DEVIATIONS (cm/sec)	RADIAL	CROSS- TRACK	ALONG- TRACK	RSS TOTAL	
GDC	840413 18 h	30	4	703	2 045	3 84	84	10 4	44 2	44 3	BASELINE MODEL
GDD	840414 18 h	30	6	723	0 065	3 54					
GDE	840413 0 h	39	4	767	-0 424	4 44	14 5	13 5	71 4	71 6	
GDF	840414 9 h	39	6	829	-0 390	4 31					

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Table 2-7. Additional Landsat-5 GSTDN Data Orbit Solution Characteristics

NOTES SATELLITE AND TIME PERIOD LANDSAT-5, APRIL 1984

DATA GSTDN RANGE-RATE DATA

RSS IS ROOT SUM SQUARED

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SEE FIGURE 2-4 FOR TRACKING PASSES AND ORBIT SOLUTION ARCS

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RUN	ARC START TIME	NO OF TRACKING	NO OF TRACKING	NO OF OBSERVA-	$\begin{array}{c} \text{COMPUTED} \\ \text{DRAG SCALE} \\ \text{FACTOR} \\ e_1 = \Delta C_D/C_D \end{array}$	RESIDUAL STATISTICS, RANGE-RATE	MAXIN OVER 6-1	IUM POSITI IOUR OVER ARCS (ENCES JACENT	REMARKS	
(d	(date, hour)	ACCEPTED	ACCEPTED	TIONS		DEVIATIONS (cm/sec)	RADIAL	CROSS- TRACK	ALONG- TRACK	RSS TOTAL	
GL4	821001 0 h	10	16	145	- 0 236	2 62	2 4	15 2	62	15 5	LANDSAT-4 BASELINE SOLUTION (PRESENTED FOR COMPARISON)
GL5	821002 0 h	6	16	116	0 294	3 45					
GL41	821001 0 h	3	4	207	- 0 779	3 17	10 3	23 1	155 2	155 4	LANDSAT-4 SOLUTIONS WITH REDUCED NO OF TRACKING STATIONS
GL51	821002 0 h	4	9	468	- 0 347	2 94	65	8 2	25 6	25 7	
GL42	821001 0 h	4	9	453	-0 251	2 89					·
GL43	821001 0 h	4	6	304	- 0 286	2 99	11 7	13 7	30 5	33 3	
GL52	821002 0 h	2	7	367	- 0 349	2 87	70	54	28 7	28 7	
GL44	821001 0 h	6	11	661	- 0 268	2 60					

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Table 2-8. Summary of Landsat-4 GSTDN Solutions With Peduced Number of Tracking Stations

NOTES SATELLITE AND TIME PERIOD LANDSAT-4, OCTOBER 1982

DATA GSTDN RANGE-RATE DATA

RSS IS ROOT SUM SQUARED

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ALL SOLUTIONS HAVE DATA ARC LENGTHS OF 30 HOURS

SEE FIGURE 2-5 FOR TRACKING PASSES AND ORBIT SOLUTION ARCS

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overlap comparison between the nonreduced Landsat-4 arcs GL4 and GL5, is presented as the standard for comparison. The remaining entries in the table present comparative ephemeris overlap differences for orbits generated over the same timespans as GL4 and GL5 but using different reduced sets of tracking stations.

The Landsat-4 GL4-GL5 set was chosen because it displays the smallest ephemeris overlap difference of all the Landsat-4 GSTDN comparisons. It was reasoned that the GL4-GL5 set would therefore produce the greatest range of sensitivity to reduced tracking station scenarios. In addition, because of the large number of stations involved, it was hoped that appropriate subsets of the GL4-GL5 tracking stations could be found to approximately reproduce the tracking geometries available in the Landsat-5 GSTDN solutions. Unfortunately, the latter purpose was frustrated by the absence of valid Landsat-4 observations corresponding to tracking stations in the Landsat-5 station set and the geometrical complications introduced in choosing substitution stations.

The reduced station results in Table 2-8 do produce poorer overlap comparisons. Specifically, as seen in set GL41-GL51 in comparison to set GL42-GL51, overlap comparisons deteriorate rapidly after some cutoff number of tracking station. As shown in the table, below this cutoff number the number of tracking passes involved begins to play an increasing importance in the overlap differences. As shown in Figure 2-5, which displays the tracking schedules for those runs summarized in Table 2-8, the number and duration of nontracking intervals also appears to affect the ephemeris differences.

Because of these complications introduced by station geometry, the number of tracking passes, and the amount and

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LEGEND			
		NOTES	CAPITAL LETTERS INDICATE THE CORESPONDENCE BETWEEN TRACKING
A – GDS8	F – GDS3		PASSES (WITH A TYPICAL DURATION OF 10 MINUTES) AND THE TRACK-
B – ULA3	G — BLTA		ING STATION FROM WHICH THE MEASUREMENT SIGNAL ORIGINATED
C – MAD3	H – MAD8		THE TRACKING PASSES ABOVE THE TIME AXIS CONTRIBUTE TO THE OR- BIT SOLUTION OVER THE DATA ARC
D — AGO3	I – ORR3		THE TRACKING PASSES BELOW THE TIME AXIS ARE PRESENT IN THE

J – BDA3

E – MIL3

ING STATION FROM WHICH THE MEASUREMENT SIGNAL ORIGINATED THE TRACKING PASSES ABOVE THE TIME AXIS CONTRIBUTE TO THE OR-BIT SOLUTION OVER THE DATA ARC THE TRACKING PASSES BELOW THE TIME AXIS ARE PRESENT IN THE **GSTDN DATA BASE**

Plot of Ground Tracking Passes and Orbit Solution Arcs Involving Figure 2-5. October 1982 Landsat-4 GSTDN Data

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duration of nontracking intervals, the reduced station results were inconclusive in determining the extent to which poor Landsat-5 GSTDN orbit solutions result solely from the small number of tracking stations. One very interesting statistic is that, for the Landsat-4 GSTDN tracking intervals (Figure 2-5), an average of 88 percent of the available stations and only 50 percent of the available tracking passes were accepted and thus contributed to the solution.¹ In contrast, for the Landsat-5 GSTDN tracking intervals (Figure 2-4), all the available stations and all the available tracking passes were accepted and thus contribute to the solution. This may indicate that the Landsat-5 solutions, because of the lower density of data, incorporated observations that would otherwise be edited out.

The present results and the previous Landsat-4 experiences lead to the conclusion that more stations, although each contains random errors and possibly even systematic errors, result not only in better observation geometry but also in a larger number of observations. A large amount of data is needed because many observations will be edited out because of validity, elevation, or 3σ editing. After this editing, if a sufficient amount of data remains, the remaining error sources can be averaged out in the orbit determination process to produce small ephemeris overlap differences. In short, more stations provide more measurements, more observability, and better statistics in dealing with existing observation error sources.

¹Available refers to observations--associated with a particular tracking pass or station--that are both present in the input data and not deleted by user observation accept/ reject criteria; accepted data must meet the previous available criteria and must also not be edited out of the orbit solution due to either validity editing, elevation editing, or 3^o editing.

2.5 ANALYSIS OF POSSIBLE MISMATCHES BETWEEN GLI AND R&D GTDS

This section presents the results of an analysis to determine if possible inconsistencies or inaccuracies introduced in the R&D GTDS.orbit determination processing cause the large pseudorange measurement residuals seen in both Landsat-4 and Landsat-5 GPSPAC data orbits (as described in Section 2.2). In the course of this analysis, the R&D GTDS code, which processes GPSPAC data, was investigated for correctness and consistency with the mathematical specifications of the GPSPAC/Landsat-D Interface System (GLI) (Reference 2-5). As noted in Section 2.1, the GPSPAC extracts GPS data from telemetry that is in turn preprocessed to transform it from Earth-fixed to inertial coordinates. In addition to other functions, GLI performs this preprocessing of the Landsat GPSPAC data for use in R&D GTDS.

This investigation verified the correctness of the R&D GTDS code that processes the GPSPAC data. However, a coordinate . frame mismatch can occur when the coordinate reference frame of the R&D GTDS orbit integrator does not match the inertial frame of the GPSPAC data's internal state, which is included with the observations. For instance, in run ID G4A of Table 2-1, the Landsat-5 GPS orbit solution is integrated in a true-of-reference-date (TOR) coordinate frame (Reference 2-6) referenced to April 13, 1984. However, the observations' GPS inertial position and velocities are expressed in a coordinate frame referenced to April 8, 1984, the date EPOCH of the GPSPAC data observation file. Because the R&D GTDS does not check for reference frame inconsistency between the GPSPAC observations and the integration reference frame, it fails to take into account the Earth's precession and nutation effects (Reference 2-7) occurring in the 5 days between April 8 and April 13.

To correct this reference frame inconsistency, each GPS observation's position and velocity (the S and SDOT) vector (expressed in the GPSPAC EPDATE TOR frame) is rotated by a stand-alone routine to the reference date to be used by the R&D GTDS orbit integrator. For the G4A run, this rotation was from the April 8, 1984, to the April 13, 1984, TOR coordinate frame. This rotated GPSPAC data were then processed in an R&D GTDS DC run. The resultant Landsat-5 GPSPAC orbit solution still displays the same large pseudorange residuals previously observed. In fact, the converged orbit solution results in a state vector of the same magnitude as that generated in the nonrotated G4A run, except that it was rotated through a small angle. This result was to be expected because the reference frame rotation does not affect the individual GPSPAC pseudorange and delta-pseudorange measurements. Instead, it rotates the entire NAVSTAR GPS multisatellite constellation through a fixed angle, which in this case corrects for the precession and nutation effects occurring between April 8 and April 13.

The comparison plot between the nonrotated G4A orbit and the G4A orbit with no reference frame inconsistency is shown in Figure 2-6. The comparison displays a constant difference in the spacecraft along-track direction. Because Landsat has a 98-deg-inclination orbit, this offset is due primarily to nutation effects. The difference in the cross-track direction, due primarily to precession effects, displays a sinusoidally varying function of period roughly equal to Landsat's own 98-minute period. The zeros in the difference function occur approximately over the poles while the extremes occur near the equatorial crossings.

Table 2-9 summarizes the characteristics of comparisons between nonrotated and reference rotated GPSPAC solutions for Landsat-4 and -5. The solutions were performed for Landsat-4 arcs to determine if reference rotation would



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Figure 2-6. Ephemeris Comparison Between GPS Orbit (Run G4A) Solutions With and Without Reference Frame Mismatch Correction (1 of 3)

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Figure 2-6. Ephemeris Comparison Between GPS Orbit (Run G4A) Solutions With and Without Reference Frame Mismatch Correction (2 of 3)

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Figure 2-6. Ephemerus Comparison Between GPS Orbit (Run G4A) Solutions With and Without Reference Frame Mismatch Correction (3 of 3)

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RUN ARC START ARC NO OF		SOLVE FOR PARAMETERS		RESIDUAL STATISTICS, STANDARD DEVIATIONS		MAXIMUM POSITION DIFFERENCES OVER 4 HOUR OVERLAP OF ADJACENT ARCS (meters)				MAXIMUM POSITION DIFFERENCES FROM GSTDN ORBITS (meters)				REMARKS					
	(date hour)	(hours)	TIONS	e1	B (10 ⁻³ sec)	B (10 ⁸ sec/ sec)	RANGE (meters)	DELTA RANGE (cm)	RADIAL	с	ALONG TRACK	RSS	RSS ^a	RADIAL	с	ALONG TRACK	RSS	RSSª	
GP1R	820910	16	705	- 0 305	- 0 369	- 0 786	132 5	2 53		_				11.1	44 4	31 7	49 7	46 5	SATELLITE LANDSAT 4
	18 h								25	15 8	13 0	18 5	20 5					1	
GP2R	820911	16	682	- 1 107	- 0 708	- 0 785	246 9	2 79						11.7	41 7	55 1	637	63 6	
	6 h																		
GP4R	821001	16	738	- 0 230	- 0 571	- 0 704	312.8	3 59						12.2	61 9	32 1	64.9	48 1	
	19 h								10 2	34 4	473	540	53 8			•= ·			
GP5B	821002	16	592	-0.610	-0.875	_ 0 702	204.2	2 43						6.2	55.2	37.2	65.4	62.2	
	7 h		552	-0010	-00/5	-0702									55 2	372	0.54	033	
			700		4 000				}										
GP6H	821112	16	/90	-02//	-1027	-0546	1312.0	2 40	7.4		40.7		41.0	10 0	59 3	33 9	626	415	
	19 N					Ì			1	14.5	407	41 1	410	ľ					
GP7R	821113	16	795	- 0 693	- 1 264	- 0 545	145 1	2 62						76	72 7	39 6	80 2	53 1	!
	7 h							1											
				1 504	0.407														
I G4AH	840413	16	1297	1 594	-3 127	- 3 262	100 0	2 39]					13.4	541	575	790	54 3	SATELLITE LANDSAT 5
	2 n																		

Table 2-9. Reference Rotated GPSPAC Data Orbit Solution Characteristics and Comparisons With Nonrotated Solutions

NOTES FORCE MODEL BASELINE ONLY EVERY 10TH PAIR OF OBSERVATION DATA IS PROCESSED

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SOLVE FOR PARAMETERS DRAG SCALE FACTOR $\rho_1 = \Delta C_D/C_D$ CLOCK BIAS B AND DRIFT B AT EPOCH

C L AND RSS ARE THE ACROSS TRACK ALONG TRACK AND ROOT SUM SQUARED COMPARE DIFFERENCES RESPECTIVELY

^aFOR COMPARISON PURPOSES RSS CORRESPONDING TO PREVIOUSLY REPORTED NONROTATED GPSPAC DATA SOLUTIONS (FOR LANDSAT 4 FROM REFERENCE 2 3) ALL OTHER TABLE ENTRIES ARE FROM ROTATED SOLUTIONS

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improve the GPSPAC-GSTDN ephemeris overlap compares. In most cases, very little difference is seen. Contrary to what was expected, in four instances, the reference frame rotation gives larger GPSPAC-GSTDN differences; although this may be caused by some geometric effect, these results are not fully understood and should be studied further. In any case, the rotation of the reference frame does not appear to cause, or affect, the large pseudorange residuals seen in any of the GPSPAC delta-range solutions.

A possible processing mismatch occurs if the GLI and R&D GTDS programs use different Greenwich hour angle (GHA) constants. To account for error on the order of 100 m, the GHA correction is estimated to be a rotation of roughly the same order of magnitude as that used to correct the coordinate reference frame inconsistency, that is, approximately 2 x 10^{-4} deg. As was expected, the correction of possible GHA errors resulted in comparison plots analogous to the reference frame rotation correction.

This study also considered other conceivable errors that can produce range error signatures on the order of 100 m and appear GPSPAC range-dependent, but are delta-range insensitive--in short, the range error signatures match the trend of the pseudorange residual errors seen in both the Landsat-4 and -5 GPSPAC solutions. Two possible error sources, which under certain scenarios meet this error signature and can be corrected for in the R&D GTDS processing, are time tag errors associated with a measurement or with the transformation from Earth-fixed to inertial coordinates. When these postulated errors were fixed, in isolation or in combination, the characteristic pseudorange residual errors in the R&D GTDS orbit solutions were increased or were only mildly affected, but they were still present.

2.6 CONCLUSIONS

The major conclusions concerning the accuracies of GPSPAC data for computing Landsat-5 orbits can be summarized as follows:

1. Landsat-5 orbit determination using GPSPAC data Landsat-5 orbit solutions computed from GPSPAC deltapseudorange (Doppler) data are good. Maximum differences between GPSPAC and GSTDN solution are generally under 70 m. Maximum differences between partially overlapping GPSPAC solutions are even smaller. There is a good possibility that the GPSPAC solutions are superior to the GSTDN solutions in accuracy.

2. For orbit determination instead of real-time navigation, simultaneous data from four GPS satellites are not necessary. The results indicate that approximately 3 hours of data from a single GPS satellite are sufficient to resolve the Landsat-5 orbit and clock. A study of a randomly selected sample shows that the Landsat-5 orbit solutions based on individual GPS satellites agree to within 80 m, and typically less than 40 m.

3. As with the case of Landsat-4 GPSPAC data, there exist some inconsistencies between the Landsat-5 GPSPAC pseudorange and delta-pseudorange data. Landsat-5 solutions derived from pseudorange data generally differ from the GSTDN solutions by maximas over 100 m. Furthermore, large, GPS-independent, range observation residuals of over 100 m are seen in delta-pseudorange Landsat-5 GPSPAC data solutions. Based on these, it may be concluded that the pseudoranges have systematic errors on the order of 100 m in addition to the expected clock errors. The cause of these systematic errors has not been determined, although bad data

from an individual GPS satellite and several easily committed preprocessing errors have been eliminated as possible reasons.

4. In connection with the GPSPAC study, the computation of Landsat-5 orbits from GSTDN data was undertaken. Unfortunately, there are not as many ground tracking stations for Landsat-5 as for Landsat-4, and the accuracy of the resulting Landsat-5 orbit solutions is not as good as that of the corresponding Landsat-4 solutions. Investigation shows that this degradation cannot be attributed solely to dynamic modeling errors accentuated by the sparsity of tracking coverage.

2.7 REFERENCES

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SECTION 3 - LOW-ALTITUDE SATELLITE NAVIGATION USING SIMULATED TDAS ONE-WAY DOPPLER DATA

This study investigated the extent of agreement between orbit determination results using simulated TDAS one-way Doppler data and linear error analysis results from a previous study. The simulation and orbit determination results were obtained using the R&D GTDS TDAS enhancements described in Reference 3-1. These simulation/orbit determination results were compared, for an analogous satellite navigation scenario, with error analysis results presented in Reference 3-2 and produced using the TDAS-enhanced SEA program.

The scenario used to generate the R&D GTDS simulated data is presented in Section 3.1, and the corresponding orbit determination scenario, in Section 3.2. From the previous SEA error analysis results, the dominant orbit error sources for the satellite considered in this study were geopotential uncertainty, clock acceleration, and TDAS ephemeris errors. The contributions from these error sources, found using the R&D GTDS simulation/orbit determination results, and their comparison with the error analysis results are discussed in Section 3.3. Conclusions are presented in Section 3.4.

3.1 SIMULATION SCENARIO

3.1.1 TDAS CONFIGURATION

The present study considered a TDAS configuration identical to that used in the SEA error analysis study in Reference 3-2. The configuration consists of three geosynchronous satellites located at longitude 73 deg, 188 deg, and 318 deg east. These satellites are located relative to the continental United States as shown in Figure 3-1. Relay tracking of the user satellite occurs through either of the two frontside TDAS relays. In addition, tracking signals from the ground may be relayed through the 73-deg backside



Figure 3-1. TDAS Configuration

TDAS via one of the frontside TDAS, when the target is not observable to the frontside TDASs.

3.1.2 USER SATELLITE

One user satellite at a 28.8-deg inclination and 600-km altitude was considered. The satellite is considered to have an area-to-mass ratio of 0.0027 meters² per kilogram (m^2/kg) . This spacecraft orbit scenario is similar to that planned for the Space Telescope mission. A nominal drag coefficient of $C_p = 2.0$ is assumed.

3.1.3 TRACKING DATA

The R&D GTDS one-way TDAS tracking data simulate tracking signals originating from the ground and relayed through the TDAS satellites to be received and decoded for range and Doppler information by the user satellite. In this simulation, range-rate Doppler data are modeled as the range difference between two consecutive integrated ranges, spaced 10 seconds (sec) apart. To reproduce the errors present in the previous error analysis study, the data simulated are corrupted by various systematic and random errors. The baseline truth model used in simulating the one-way TDAS data is as follows:

Description	Model						
Geopotential	21-by-21 GEM-9						
Solar flux/atmospheric density	Harris-Priester F150, C _D = 2.0						
Random measurement error Range Range-rate equivalent of Doppler noise	5 m 5 millimeters (mm)/sec						
Measurement biases Range Range-rate equivalent of Doppler bias	l0 m l mm/sec						
User clock error B	10 ⁻¹⁰ (sec/sec)/day						

TDAS ephemeris	error		
Height		25	m
Crosstrack		23	m
Alongtrack		40	m

Two alternate tracking schedules, similar to those used in Reference 3-3, were considered: the broadcast or beacon mode, in which continuous tracking is available, and the scheduled mode, in which tracking is scheduled for 30 minutes (min) every orbit, cycled through the three TDAS satellites with a 20- to 25-min data gap in between. For convenience, these will be referred to as the forward-link beacon tracking (FLBT) and forward-link scheduled tracking (FLST).

During the tracking periods, observations were simulated at a rate of one pair of range and range-rate measurements every 20-sec (although, in the orbit solutions, the observation weights were adjusted to result in a range-rate solution). The user satellite is sometimes visible to two TDAS satellites simultaneously. To be consistent with the error analysis study, it was assumed that the user satellite is tracked through one TDAS satellite and then switched to the next TDAS satellite when the first one leaves the user's field of view. In contrast with previous studies (References 3-1 and 3-4), no attempt was made to minimize tracking through the backside TDAS. The FLBT and FLST tracking schedules used are shown in Table 3-1; it is identical to that used in the error analysis study in Reference 3-2.

3.2 ORBIT DETERMINATION SCENARIO

An extended Kalman filter (EKF) orbit determination solution was used to reduce the simulated data discussed above. In this solution, the variables estimated were the position and velocity vectors, an effective atmospheric drag coefficient (ρ_1) , and the bias and drift of the onboard clock (B and B).

Table 3-1.	Tracking Schedules for 600-Kilometer-Altıtude, 28-Degree-Inclinatıon User Satellite

FORWARD	D-LINK BEACON	TRACKING	FORWARD-L	INK SCHEDULE	D TRACKING	
TDAS1	TDAS2	TDAS3	TDAS1	TDAS2	TDAS3]
0-3	64—95	3-64	100-110	65-75	5—15]
95—132	166-200	132—166	205-215	170 - 180	135—145	
200-236	269 - 305	236 269	305-315	270-280	240-250	
305-340	372-408	340—372	410-420	375-385	340-350	
408-444	475-510	444—475	510-520	480-490	445455	
510—547	580-612	547-580	615—625	580 590	550-560	
612—650	684-715	650—684	720 - 730	685-695	655-665	
715—753	788-819	753—788	820-830	790800	755—765	
819—856	890924	856-890	925-935	895—905	860-870	
924—960	993—1028	960—993	1030 1040	995—1005	960 970	
1028—1064	1096-1131	1064—1096	1135-1145	1100-1110	1065—1075	
1131 1168	1200-1234	1168-1200	1235 - 1245	1200 - 1210	11701180	
1234—1271	1304 1336	1271 — 1304	1340 1350	1305-1315	1275—1285	5
1336—1375	1409—1439	1375—1409		1410-1420	1375 - 1385	111/8
1439-1440						0112 (

The following state process noises were introduced: between measurements, the variances of the velocity components increase at a rate of 10^{-10} square meters per second cubed $(m^2/sec^2)/sec$; similarly, the clock drift rate variance increases at a rate of 10^{-6} nanoseconds (nsec) per second cubed $(msec/sec)^2/sec$ between measurements. The complete baseline offset force model is summarized as follows:

Description	Model					
Geopotential	21-by-21 GEM-7					
Solar flux/atmospheric density	Harris-Priester F200, C _D = 2.2					
User clock error B (clock bias) B (clock drift)	10 ⁻² sec 10 ⁻⁶ sec/sec					
A priorı offset in user satellite state (from truth model state)	300 m in x, y, z; (positions) 30 cm/sec in x, y, z (velocities)					

The baseline a prior1 statistics are as follows:

Description	Standard Deviation
A priori state uncertainty User H, C, L Orbit H, C, L	500 m 1 m/sec
User Bias Clock Drıft	l msec 200 nsec/sec
Drag parameter	1
Gravitational constant, GM	0.25 parts per million (ppm)
Process noise Velocity variance growth rate Clock drift rate variance	10 ⁻¹⁰ (m ² /sec ²)/sec 10 ⁻⁶ (nsec/sec) ² /sec

3.3 SIMULATION/ORBIT DETERMINATION ERROR RESULTS

3.3.1 GEOPOTENTIAL ERROR

To compare the simulation results of this study with the error analysis results of the previous study, a common geopotential error model was chosen. The common error model, which can be accommodated using R&D GTDS, is the difference between the 8-by-8 GEM-1 and the GEM-9 truncated to 15 by 15. In R&D GTDS, the contribution from the GEM-9/GEM-1 difference model was determined using the following method.

First, data were simulated using the baseline version of the truth model except that the geopotential model employed was the GEM-9 truncated to 15 by 15. These data were next reduced using two variations of the baseline force model. The first variation employed the same GEM-9 15-by-15 geopotential model used in simulating the data. In effect, this run incorporated no geopotential model mismatch. The second orbit determination run employed the 8-by-8 GEM-1, so that the run incorporated the GEM-9/GEM-1 model mismatch. Finally, the reduced ephemeris files of the two orbit solutions were compared, with statistics generated on the user's state vector differences over time. To the extent that nonlinear effects can be ignored, the differences in the ephemeris comparisons should arise solely from the GEM-9/GEM-1 model mismatch.

Very close agreement was seen between the R&D GTDS simulation and the previous SEA error analysis results for geopotential errors arising from the GEM-9/GEM-1 difference In the error analysis study, an FLBT maximum posimodel. tion error for the GEM-9/GEM-1 difference was reported as 38 m; in this study, 42 m was found using the simulation/ orbit determination method discussed previously. As shown in Figure 3-2, the geopotential errors display the characteristic signature that the projections along the spacecraft h, C, and L directions are approximately the same, with the H projection being the smallest. In addition, the rss total geopotential error contribution is observed to be fairly constant in time. These observations are in agreement with the error signatures for the GEM-1/GEM-9 errors found from the SEA error analysis results.



Figure 3-2. Geopotential (GEM-9/GEM-1 Difference Model) Error Projections in the User Orbit Plane as Determined From R&D GTDS FLBT Simulation (1 of 3)

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Figure 3-2. Geopotential (GEM-9/GEM-1 Difference Model) Error Projections in the User Orbit Plane as Determined From P&D GTDS FLBT Simulation (2 of 3)

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Figure 3-2. Geopotential (GEM-9/GEM-1 Difference Model) Error Projections in the User Orbit Plane as Determined From R&D GTDS FLBT Simulation (3 of 3)

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3.3.2 CLOCK ACCELERATION ERROR

The clock acceleration error was determined using the following method. Data were first simulated using the baseline truth model and reduced with the baseline force model; a converged user ephemeris file was then generated. Next, data were again simulated, using the same tracking schedule, but the baseline truth model was modified to exclude user clock acceleration offset. These simulated data were then reduced, using the same baseline force model as before, and a converged ephemeris file was generated. As the final step in determining the user clock acceleration error, the differences between these two user ephemeris files was calculated.

Very good agreement was found for the errors due to clock acceleration between R&D simulation and the SEA error analysis results of the previous study. In this study, a maximum clock acceleration error for FLBT tracking was 26 m; in the previous study, the maximum observed was 30 m. In the error analysis study, it was observed that the clock acceleration error contribution to the range-rate measurement error increases with elapsed time and is generally linear and in the spacecraft alongtrack direction. This study's simulation runs, which are range-rate solutions, are in agreement with those observations.

It should be noted that the present study's R&D solution used an EKF, whereas the previous study used a Kalman Filter (KF).¹ Even with this difference, the simulation and error analysis results show agreement in the interaction

¹The EKF, a variation to the KF, differs in that the solvefor state vector is corrected at each observation instead of waiting until the last observation. Descriptions of the EKF and KF in terms of their implementation in R&D GTDS are provided in Reference 3-5.

between clock process noise and clock acceleration error observed. The R&D GTDS FLBT results are 26 m compared with SEA's 30 m for clock acceleration error. Figure 3-3 displays ephemeris comparison plots of the contribution of acceleration error resulting from the R&D GTDS FLBT mode.

In addition, simulation and error analysis runs display consistent results if clock drift process noise is not used to compensate for clock errors in the filter. In SEA, when clock drift process noise is absent, clock acceleration causes an error reaching 200 m in an FLBT range-rate orbit solution after 24 hours. In R&D GTDS, simulations under the same scenario give a similarly inflated clock acceleration error of 132 m.

3.3.3 TDAS EPHEMERIS ERROR

R&D GTDS and SEA use slightly different TDAS ephemeris error modeling initialization. As described in Reference 3-1, the satellite ephemeris error model present in SEA is used in R&D GTDS for TDAS satellites. A description of this ephemeris error model and its input is presented in Reference 3-5. In the R&D GTDS implementation, to allow the greatest flexibility possible, the input phase angles θ and ϕ are specified separately for each TDAS relay. In contrast, in SEA, only a single seed--input into a random number generator -- is used to specify the phase input initialization for the up to 18 GPS satellites possible. The output of the SEA random number generator has been determined, but because these numbers are real and the input phases into R&D GTDS are integers, an error of up to 0.5 deg can occur. This input mismatch can result in small inconsistencies between R&D GTDS and SEA ephemeris error contributions. In the case of small phase angles, this mismatch is enlarged because of the trigonometric functions involved. Nevertheless, close agreement is seen between the



Figure 3-3. User Clock Acceleration Error Projections in the User Orbit Plane as Determined From R&D GTDS FLBT Simulation (1 of 3)

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Figure 3-3. User Clock Acceleration Error Projections in the User Orbit Plane as Determined From R&D GTDS FLBT Simulation (2 of 3)

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Figure 3-3. User Clock Acceleration Error Projections in the User Orbit Plane as Determined From R&D GTDS FLBT Simulation (3 of 3)

simulation and error analysis results for the contribution of TDAS ephemeris error.

In R&D GTDS, the method of determining the contribution to TDAS ephemeris error is similar to that used in determining clock acceleration error. Specifically, instead of using the baseline truth model without clock acceleration, data are simulated without TDAS ephemeris error. The data are reduced using the baseline force model, and the converged ephemeris is then compared with an ephemeris generated using the baseline truth and force models.

From SEA, the contribution from TDAS ephemeris error is 23 m; from R&D GTDS simulation results for the FLBT mode, this error is 19 m. The ephemeris error, as shown in Figure 3-4, has its largest contribution in the alongtrack direction where it increases rapidly at first but then appears to saturate or display very slow growth. Similar signatures are seen in the SEA error analysis results.

3.3.4 ERROR RESULTS WITH LESS FREQUENTLY SAMPLED DATA

Previous error analysis results show that systematic error is the dominant error source. Little performance degradation would therefore be expected if the tracking data are reduced by sampling. Error analysis results also indicate that there is very little difference in navigation performance if tracking data are sampled and processed at 3-min intervals instead of the 20-sec intervals used in the baseline scenario. This observation is similarly verified in this study's simulation results. In varying the sample rate, the observation weights must, however, be properly scaled to offset the increase in the navigation error covariance resulting from the rarefied tracking data. Alternately, as employed in the SEA error analysis study, the change in sample rate may be compensated for through scaling the process noise.



Determined From R&D GTDS FLBT Simulation (1 of 3)

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Determined From R&D GTDS FLBT Simulation (3 of 3)

3.3.5 COMPARISON BETWEEN FLBT AND FLST TRACKING MODES

In agreement with the SEA error analysis results, this study's FLST simulation results displayed navigation performance inferior to that in the FLBT mode. Table 3-2 contrasts the error contributions in the two modes and their comparison with the results obtained from the SEA error analysis. The error analysis and simulation results display the same increasing trend in geopotential error contribution from FLBT to FLST mode. R&D and SEA results also show that clock acceleration error is reduced in the FLST mode.

As discussed in the error analysis study, caution must be exercised in comparing FLST and FLBT results directly because the two modes have different amounts of tracking but nonetheless use the same baseline process noise. In addition, in comparing R&D GTDS simulation results with the previous SEA error analysis results, a certain amount of caution must be exercised because R&D GTDS employs an EKF whereas SEA uses a KF. The difference in processing between the two types of filters may cause some of the differences between the error analysis and simulation results, specifically the errors seen for TDAS ephemeris.

3.4 CONCLUSIONS

Surprising agreement is seen between R&D GTDS simulation results and SEA error analysis results for a 600-km altitude and 28-deg-inclination spacecraft for both the FLST and FLBT modes. The agreement is a confirmation of the error analysis results and provides confidence in the methods used in the SEA error analysis program and the meaningfulness of its results. Because it directly parallels the actual orbit determination process, there is no direct substitution for the method of simulation and orbit determination used in this study. In comparison to SEA, simulation systems such as R&D GTDS are much larger and more environmentally

Table 3-2. Navigation Error Comparison Between R&D GTDS Simulation and Previous SEA Error Analysis Results

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	MAXIMUM POSITION ERROR (m) DURING 24 HOURS OF NAVIGATION FOR TWO TRACKING MODES							
EBBOB SOURCE		FLST		FLBT			1	
	SEA ^a R&D GTDS			SEA ^a R&D GTDS				
	20 SEC	180 SEC	20 SEC	20 SEC	180 SEC	20 SEC		
GEOPOTENTIAL (GEM-9/GEM-1 DIFFERENCE MODEL)	63	87 2	93 5	38	42 2	Ь		
CLOCK ACCELERATION	17	14 8	14 8	30	24 3	25 6	101	
TDAS EPHEMERIS	23	20 8	21 4	23	15 5	18 6		

^aSEA RESULTS WERE REPORTED FOR ONLY THE 20-SEC OBSERVATION SAMPLING FREQUENCY ^bRUN WAS NOT PERFORMED

dependent, and so they are inherently more difficult to use and are computationally more expensive. The consistency of this study's simulation results with previous error analysis would therefore suggest that, after suitable calibration between simulation and error analysis has been ensured, efficiency of effort may be obtained in performing the majority of the navigation analysis with an error analysis program such as SEA.

3.5 REFERENCES

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The following spherical harmonic representation of the geopotential is generally recognized as the most convenient for orbital analysis:

$$V = \frac{GM}{r} \left[1 + \sum_{l=2}^{\infty} \sum_{m=0}^{l} \frac{a_e}{r} P_{lm} (\sin \phi) (C_{lm} \cos m\lambda) + S_{lm} \sin m\lambda \right]$$

$$(4-1)$$

where

GM = geocentric gravitational constant
 a_e = mean equatorial radius of the Earth
 P_{lm} = normalized associated Legendre function of
 degree l and order m

r, ϕ , λ = distance to the center of the Earth, latitude, and longitude

 C_{lm} , S_{lm} = normalized spherical harmonic coefficients

The quantity GM provides a scale for the whole field; a provides a scale for the altitude dependence, r; and C_{ℓ_m} and S_{ℓ_m} characterize the geographic, or nonspherical, variations. A geopotential model is defined by these parameters. Of necessity, the field is truncated at some finite degree and order. Over the years, NASA/GSFC has developed a series of progressively more accurate GEMs based on satellite tracking data, satellite-borne altimetry, and surface gravimetry. GEM-10B (Reference 4-1), complete to degree and order 36 by 36, is currently the most accurate model. The Goddard Trajectory Determination System (Reference 4-2), which is used for operational orbit determination at GSFC, has provisions for GEM-9 (Reference 4-3) further truncated to degree and order 21 by 21.
Even with accurate geopotential models such as GEM-9 and GEM-10B, the uncertainty in these models remains a major error source for low-altitude Earth satellite orbit determination. Geopotential error arises because of truncation (omission error) and because of errors in the spherical harmonic coefficients (commission error). Generally, with the derivation of a GEM, an error covariance matrix describing the uncertainties and correlations of the spherical harmonic coefficients is a standard byproduct. In principle, it would be straightforward to use this covariance matrix in linear error analysis to compute the effect of commission error on satellite orbit determination accuracy. However, the size of the covariance matrix makes this approach prohibitively expensive in computations.

As a simpler alternative, a so-called lumped geopotential error model was suggested (Reference 4-4) and implemented in orbit determination error analysis programs. Briefly, this approach takes the weighted differences of the geopotential coefficients of two independent geopotential models and computes the orbit determination error resulting from the lumped effect of these differences. Subsequently, standard deviations, which are the scaled-up formal uncertainties of GEM spherical harmonic coefficients, were used in place of the coefficient differences. The theoretical objection to the use of standard deviations was first raised in Reference 4-5. Its practical inadequacy was brought out in vivid graphical displays in Reference 4-6.

Section 4.1 describes the rationale of the lumped geopotential error model. Section 4.2 discusses the global distribution of gravity error for different geopotential error models. Section 4.3 discusses navigation and orbit prediction errors introduced by geopotential uncertainty. Section 4.4 compares results obtained using TDRS data with

those from the lumped geopotential error model for GEM-9. Section 4.5 presents conclusions.

4.1 THE LUMPED ERROR MODEL

The derivation of each GEM is always accompanied by a careful error analysis to assess its accuracy. Reference 4-7 on GEM-7 and GEM-8 is an outstanding example of the conscientiousness and thoroughness associated with such assessments. Analyses of GEM-9 and GEM-10 accuracies are available in References 4-3 and 4-1, respectively. Reference 4-8 contains a discussion of gravity model improvement and its implications for operational orbit determination.

As discussed before, each GEM is accompanied by an error covariance matrix associated with the geopotential coefficients. The covariance matrix is computed based on assumed precisions of tracking and other data from which the geopotential is derived. Because not all error sources in tracking data and in spherical harmonic coefficient estimation methods can be accounted for, the computed error covariance is not a true indication of the accuracy of the spherical harmonic coefficients. Part of the objective of geopotential model accuracy analysis is to derive a calibration factor, which is used to scale up the standard deviations from the error covariances to more realistic levels. The calibration factor is typically around 3.3.

One of the obvious methods of assessing a geopotential model is to compare it with other independently derived geopotential models. The lumped geopotential error model, first proposed by Martin and Roy (Reference 4-4), takes one-half the differences of two uncorrelated models of comparable accuracy as a measure of the accuracies of the individual models. The rationale can be explained as follows. Let $\begin{pmatrix} C_{\ell m} \end{pmatrix}_{model A}$ be the geopotential coefficients of the two models. If the two models are uncorrelated

but of comparable accuracy, their average is closer to the truth, i.e.,

$$\left(C_{\ell m} \right)_{\text{truth}} \approx \frac{1}{2} \left[\left(C_{\ell m} \right)_{\text{model A}} + \left(C_{\ell m} \right)_{\text{model B}} \right] \cdot (4-2)$$

and an estimate of the individual errors can be obtained as

$$\begin{pmatrix} \Delta C_{\ell m} \end{pmatrix}_{model A} = \begin{pmatrix} C_{\ell m} \end{pmatrix}_{model A} - \begin{pmatrix} C_{\ell m} \end{pmatrix}_{truth}$$

$$\approx \frac{1}{2} \begin{bmatrix} \begin{pmatrix} C_{\ell m} \end{pmatrix}_{model A} - \begin{pmatrix} C_{\ell m} \end{pmatrix}_{model B} \end{bmatrix}$$

$$(4-3)$$

Of course, an estimate using the sample mean based on only two samples, as in Equation (4-3), is not very reliable. The lumped model introduces additional samples or statistics by considering not a single C_{lm} but the whole set of C_{lm} 's and S_{lm} 's in the geopotential model. In other words, it is not saying that ΔC_{lm} as given in Equation (4-3) is a good indicator of the accuracy of individual coefficients, but that the aggregate effect of all ΔC_{lm} 's on the computed orbit is a reasonable representation of the effect of the geopotential uncertainty on orbit determination.

The key assumption of the lumped model is the requirement that the two models be uncorrelated. This generally means that the models be derived by two different organizations based on different data sets. It also implies that this lumped model does not adequately represent omission errors. The assumption that the two models are of equal accuracy is not essential, as the simple average in Equation (4-3) can be replaced by a weighted average. In the spirit of minimum variance estimators, the weights can be chosen to be inversely proportional to the variances of the individual models. In practice, an educated guess or external calibration can be used to assign the weights.

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The lumped model has been used in many orbit determination error analysis studies, perhaps not so much because it is a good model but because nothing better is available. Part of the difficulty of this approach is the availability of independent models. In a study (Reference 4-9) of onboard orbit determination using GEM-9 truncated to various degrees, it was suggested that the lumped model be used to represent the uncertainty in the truncated GEM-9 as follows: GEM-9 standard deviations would be used to represent the uncertainties of those spherical harmonic coefficients retained in the truncated model, and truncation errors would be represented by the truncated high degree and order GEM-9 spherical harmonic coefficients themselves. There are two theoretical objections (Reference 4-5) to the use of standard deviations instead of coefficient differences in the lumped model:

- The errors in the geopotential coefficients are likely to have both positive and negative signs, whereas the standard deviations are all positive.
- The standard deviations do not contain information about correlations among the coefficients.

It may be argued that, because the primary interest is in orbit determination errors, rather than in the errors in the geopotential coefficients, the use of the positive standard deviations may not be objectionable if the orbit error sensitivities to these coefficients are randomly distributed to serve to randomize their aggregate effect. Elrod, however, showed that this is not the case (Reference 4-6). Figure 4-1, reproduced from Reference 4-6, shows that the use of GEM-9 standard deviations results in a nonuniform global distribution of gravitational acceleration errors that is greater in the Northern Hemisphere with a singularity near



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on the map represent gravitational acceleration uncertainties in mgals $(10^{-5} \text{ meter per second}^2)$ rounded to the nearest

integer.)

0 deg longitude and 60 deg latitude. Such anomalous distribution is not supported by other evidence. Furthermore, Elrod showed that the anomaly does not occur if the rss result is obtained rather than the algebraic sum of the lumped error model. There is no question that the use of GEM-9 standard deviations in the lumped error model is faulty. The effect of false singularity is perhaps not serious for error analysis of the batch orbit determination method, but it can exaggerate local navigation errors in sequential navigation methods.

Because the standard deviations do not convey information about correlations, an obvious alternative is to assume that all errors in the spherical harmonic coefficients of a geopotential are uncorrelated. The total error of the geopotential model can thus be obtained as the rss of the error contribution of individual coefficients. Although it is known that certain geopotential coefficients are highly correlated, this model is perhaps as reasonable as any, short of having to consider the actual correlations. The major drawback of this model is the excessive amount of computation required to compute separately the error contributions of individual error coefficients, versus the spirit of the lumped error model. At best, only the level of orbit determination error resulting from geopotential uncertainty can be expected; therefore, the computationally expensive rss approach may not be justifiable, and simpler alternatives would be desirable. The following alternatives are proposed as candidates for study:

 Random-Sign Method--The lumped model will use the GEM-9 standard deviations, with positive and negative signs randomly assigned to them.

 Random-Phase Method--The terms involving the spherical harmonic coefficients in the geopotential representation, Equation (4-1), may be written as

$$C_{lm} \cos m\lambda + S_{lm} \sin m\lambda = \sqrt{C_{lm}^2 + S_{lm}^2} \cos (m\lambda - \phi_m)$$
 (4-4)

In this method, the amplitudes

$$\sqrt{c_{\ell m}^2 + s_{\ell m}^2}$$

are computed from GEM-9 standard deviations, but the phase angles, ϕ_m , are selected from a uniform random distribution between 0 and 2π (for zonals, the phase is randomly chosen as 0 or π , i.e., random sign).

In addition to these models dependent on internal accuracy estimates, two geopotential models uncorrelated with GEM-9 are used in conjunction with GEM-9 to form geopotential difference error models. One of these is the 1969 Smithsonian Astrophysical Observatory (SAO) Standard Earth (Reference 4-10), referred to as the SAO model below. The other will be referred to as the MDl model. One-half of the difference of this model and GEM-5 has been considered representative of the accuracy of GEM-5 (Reference 4-11). Both the SAO and MDl models are inferior to GEM-9 in accuracy.

4.2 <u>GLOBAL DISTRIBUTION OF GRAVITY ERROR FOR DIFFERENT GEO-</u> POTENTIAL ERROR MODELS

The gravitational acceleration as specified by a geopotential model will have errors that vary with the geographical location (longitude and latitude) and decrease with the altitude. A gravity error map such as that illustrated in Figure 4-1 shows the magnitude (but not the direction) of

the gravitational acceleration error at a given altitude as a function of longitude and latitude, as predicted by a geopotential error model. Different error models give rise to different error characteristics. Of interest are orders of magnitude and geographical fluctuations of the errors. Figures 4-2 through 4-22 are gravity error maps at 200-, 400-, and 600-km altitudes for the following geopotential error models:

- GEM-9/MDl one-half difference model
- GEM-9/SAO one-half difference model
- GEM-9/GEM-5 difference model
- GEM-5/MD-1 one-half difference model
- GEM-9 standard deviation model
- GEM-9 random sign model
- GEM-9 random-phase model
- GEM-9 uncorrelated model

The difference models, discussed in Section 4.1, are selfexplanatory. The GEM-9 standard deviation model uses positive GEM-9 standard deviations as spherical harmonic error coefficients. The gravity error map for this model at 200-km altitude is shown in Figure 4-1, so only the maps at 400- and 600-km altitudes are shown here. The random-sign and random-phase models are also explained in Section 4.1. A number of variants of these models were also considered, but they did not show significant difference from those described here. The uncorrelated model is based on the rss of the contributions of individual coefficients; computing these errors is expensive, and the gravity error maps were taken from Reference 4-6. To provide a reference for gauging the magnitudes of gravity errors, Figure 4-23 shows a map representing the gravitational acceleration (not the error) resulting from the nonaxisymmetric (i.e., the nonzonal) portion

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Figure 4-2. GEM-9/MD1 One-Half Difference Model, 200-Kilometer Altitude

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Figure 4-3. GEM-9/MDl One-Half Difference Model, 400-Kilometer Altitude

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65	+	1	1	2	3	3	2	1	1	1	2	2	1	1	2	2	2	1	1	1	1	2	2	2	2	1	0	1	2	3	2	1	1	2	2	1	1	1
70	+	2	1	2	2	3	з	з	2	2	2	2	1	0	t	1	1	1	1	1	1	1	2	2	1	1	1	2	2	2	t	1	1	2	2	1	1	2
75	+	1	1	2	3	3	3	3	3	2	1	1	1	1	t	1	1	1	0	1	1	1	1	1	1	1	2	2	2	1	t	1	1	1	1	1	1	1
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Figure 4-4. GEM-9/MD1 One-Half Difference Model, 600-Kilometer Altitude

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Figure 4-5. GEM-9/SAO One-Half Difference Model, 200-Kilometer Altitude

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Figure 4-6. GEM-9/SAO One-Half Difference Model, 400-Kilometer Altitude

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30	+	3	2	2	3	2	2	2	2	3	2	1	1	2	2	3	2	1	3	2	1	1	1	2	1	1	1	1	1	1	2	1	з	2	2	2	2	3
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-80	4	7	2	2	2	2	2	2	5	2	2	2	-	-	5	5	5	2	5	2	2	2	2	2	2	2	2	2	7	7	2	2	2	2	2	2	3	2
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Figure 4-7. GEM-9/SAO One-Half Difference Model, 600-Kilometer Altitude

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Figure 4-8. GEM-9/GEM-5 Difference Model, 200-Kilometer Altıtude

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70 65	+	23	33	23	22	22	23	23	23	23	23	23	13	23	23	3	34	3	4	47	4	4	58	5	4	4	5	5	5	5	6	7 7 5	6	6 5	44	33	23	23
55		3	2	1	2	6	7	67	4	2	4	4 5 5	4	4	6	7	9	8	2	8 7 5	5	5	8	8	6	4	3	5	4	2	2	3	4	67	3 4 5	2	2	3
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Figure 4-9. GEM-9/GEM-5 Different Model, 400-Kilometer Altitude

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85	+	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0
80	+	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	t	2	2	1	1	• •	1	1	1	1	1	1	0
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70	+	2	2	2	1	2	1	1	1	1	1	1	t	1	1	2	2	2	з	3	3	3	3	3	3	3	3	3	3	3	4	4	4	4	3	2	2	2
65	٠	2	2	2	1	2	2	2	2	2	2	2	2	2	2	3	3	з	4	4	4	4	5	5	4	3	3	4	4	з	4	4	4	3	3	2	2	2
60	+	2	2	1	1	2	3	3	2	2	2	2	2	2	3	3	- 4	5	5	5	5	5	6	6	4	3	3	4	3	2	3	4	3	з	2	1	2	2
55	+	2	2	1	1	4	4	4	3	1	3	3	2	3	4	5	6	5	6	5	4	3	5	5	4	3	2	з	3	1	1	2	3	4	2	1	1	2
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Figure 4-10. GEM-9/GEM-5 Difference Model, 600-Kilometer Altitude

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Figure 4-11. GEM-5/MD1 One-Half Difference Model, 200-Kilometer Altitude

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Figure 4-12. GEM-5/MDl One-Half Difference Model, 400-Kilometer Altitude

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Figure 4-13. GEM-5/MDl One-Half Difference Model, 600-Kilometer Altitude

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Figure 4-15. GEM-9 Standard Deviation Model, 600-Kilometer Altitude

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Figure 4-16. GEM-9 Formal Uncertainties With Random Signs, 200-Kilometer Altitude

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Figure 4-19. GEM-9 Formal Uncertainties With Random Phase, 200-Kilometer Altitude

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Figure 4-20. GEM-9 Formal Uncertainties With Random Phase, 400-Kilometer Altitude

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Figure 4-21. GEM-9 Formal Uncertainties With Random Phase, 600-Kilometer Altitude

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-40 -45 -50 -55 -60 -65	* * * * * *	•	357856	10 10 11 12 10 11	14 12 14 16 12	14 16 16 13 9	25 25 24 22 17 19	29 30 29 26 21 22	23 24 23 20 19 23	21 19 20 23 24 26	22 24 25 25 25 25	23 24 23 21 20 23	27 22 17 17 19 22	30 23 16 16 19 22	26 21 18 18 19 21	28 21 17 17 18 21	26 18 10 12 16 20	20 17 15 14 15 18	20 18 19 19 19 20	24 20 24 24 23	25 26 29 33 31 27	21 21 26 31 31 28	14 14 14 18 22 25	7 10 12 10 14 22	8 10 10 8 12 21	9 11 10 5 9 19	7 8 9 7 8 16	6 4 5 8 11 15	6 9 11 13	10 12 14 14 14	14 15 14 13 15 17	16 14 10 12 18 20	14 11 9 15 20 22	16 16 15 17 21 22	14 17 18 19 22 20	13 15 14 13 14 13	15 15 12 11 86	10 10 11 14 11 6	3 5 7 8 5 6
-70 -75 -80 -85 -90		•	13 18 19 19 20	18 23 23 21 21	22 27 26 22 21	26 31 28 24 21	28 33 30 25 21	30 34 31 26 22	30 33 32 26 22	30 33 32 27 22	29 32 31 27 22	27 30 31 27 22	26 30 31 28 22	26 30 31 28 22	26 31 31 28 22	27 32 31 27 22	27 32 32 27 22	27 32 32 27 22	26 32 31 26 22	26 31 30 26 22	28 30 29 25 22	29 30 28 24 21	29 29 27 23 21	28 29 26 22 21	28 28 24 21 21	26 26 23 20 20	23 24 21 19 20	20 21 19 18 20	19 19 17 17 20	18 18 15 16 20	18 17 14 15 20	19 16 13 14 20	20 15 12 14 19	18 13 11 14 20	15 11 11 15 20	10 10 12 16 20	7 10 14 17 20	9 13 16 18 20	13 18 19 19 20
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Figure 4-23. Gravity Map at a 200-Kilometer Altitude for the Nonaxisymmetric Portion of GEM-9

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of the GEM-9 spherical harmonic coefficients. The maps depict the following:

• As expected, gravity errors for every model decrease with altitude.

• In addition to the anomalous distribution of gravity errors discussed for the GEM-9 standard deviation model, difference models involving the MDl and a GEM model show a band of large differences at latitudes near the Equator.

• The GEM-9 uncorrelated model predicts a very uniform distribution of errors with a magnitude around 4 milligals (mgals) $(10^{-5} \text{ m/sec}^2)$ at 200 km. The GEM-9 standard deviation model predicts errors, apart from the anomalous region, at a level considerably smaller than those given by the other models. The other models generally give rise to errors from 1 to 10 mgals and show much greater fluctuations from one location to another.

4.3 <u>NAVIGATION AND ORBIT PREDICTION ERRORS INTRODUCED BY</u> GEOPOTENTIAL UNCERTAINTY

The interest in geopotential error models is not so much in the gravity errors themselves but in their effect on satellite navigation accuracy. Satellite navigation error analyses were thus conducted using the SEA program to evaluate, under postulated navigation scenarios, the expected orbit determination and prediction errors resulting from the geopotential errors given by different error models. The baseline scenario considered was for low-altitude Earth satellite navigation based on a sequential filter using continuous TDAS range and Doppler tracking data sampled at 3-min intervals for 1 day, followed by 5 days of propagation without tracking. Navigation at 200 and 600 km and at 28and 57-deg inclinations was considered. No process noise was introduced in the filter; thus, the 5-day propagation results should agree with those based on a batch orbit

determination process. The expected navigation errors resulting from geopotential uncertainties are summarized in Table 4-1 for the different geopotential error models.

4.4 COMPARISON WITH LANDSAT-5 ORBIT DETERMINATION RESULTS

Some results on Landsat-5 orbit determination using GSTDN and single-TDRS tracking data are presented in Reference 4-12. Measures of orbit accuracies are provided by

- Overlap ephemeris comparisons of definitive orbit solutions (34-hour data arcs with 10 hours of overlap)
- Ephemeris comparisons of definitive and predictive orbit solutions (1- or 2-day predictions based on 34-hour data arcs)

The overlap comparisons of definitive solutions derived from TDRS data have maximum differences of 82, 71, 35, 74, and 35 m. One-day predictions have maximum differences of 186, 131, 40, 172, and 79 m from definitive solutions. Two-day predictions have maximum differences of 412 and 172 m. Although these differences, or errors, result from a combination of geopotential and atmospheric uncertainties and tracking errors, it is expected that geopotential uncertainties play a major role. These numbers can thus serve as bases for the calibration of geopotential error models. For this purpose, error analyses were set up to evaluate, under the same tracking and batch orbit determination scenario, orbit errors resulting from the GEM-9/SAO one-half difference error model and the GEM-9/MDl one-half difference model. The GEM-9/SAO error model predicts a maximum position error of 57 m during the tracking period and maximum errors of 184 and 236 m during 1-day and 2-day propaga-These numbers appear quite reasonable compared with tions. actual orbit determination results quoted above. The GEM-9/ MD1 error model predicts a maximum position error of 77 m

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Table 4-1.	Navigation	Errors	Resulting	From	Geopotential
	Uncertaint	ies			

000/7		ORBIT POSI (me	TION ERROR ters)
CHARACTERISTICS	MODEL	MAXIMUM DURING 24 HOURS OF TRACKING	MAXIMUM DURING 5-DAY PREDICTION
200-km ALTITUDE,	GEM-9 STANDARD DEVIATION	21	205
28-deg INCLINATION	½ GEM-9/SAO DIFFERENCE	149	481
	½ GEM-9/MD-1 DIFFERENCE	168	3209
	½ GEM-5/MD-1 DIFFERENCE	186	3495
	RANDOM SIGN	148	496
	RANDOM PHASE	108	575
200-km ALTITUDE,	GEM-9 STANDARD DEVIATION	56	1171
57-deg INCLINATION	½ GEM-9/SAO DIFFERENCE	126	1271
	½ GEM-9/MD-1 DIFFERENCE	253	44886
	½ GEM-5/MD-1 DIFFERENCE	227	42745
	RANDOM SIGN	105	4562
	RANDOM PHASE	238	2511
600-km ALTITUDE,	GEM-9 STANDARD DEVIATION	9	71
28-deg INCLINATION	½ GEM-9/SAO DIFFERENCE	60	246
	½ GEM-9/MD-1 DIFFERENCE	73	597
	½ GEM-5/MD-1 DIFFERENCE	71	576
	RANDOM SIGN	68	154
	RANDOM PHASE	44	118
600-km ALTITUDE,	GEM-9 STANDARD DEVIATIONS	14	235
57-deg INCLINATION	½ GEM-9/SAO DIFFERENCE	58	686
	½ GEM-9/MD-1 DIFFERENCE	81	1537
	½ GEM-5/MD-1 DIFFERENCE	77	2330
	RANDOM SIGN	35	395
	RANDOM PHASE	44	118

during the tracking period but unrealistic, smaller maximum errors of 58 and 64 m during propagations.

4.5 CONCLUSIONS

The results described in the preceding sections show that the choice of an appropriate model is very difficult. The models studied may be classified into two categories: those dependent on internal accuracy estimates and those dependent on comparisons with other models.

Error models based on internal accuracy estimates run the risk of being unduly optimistic. This weakness can, however, be remedied by a calibration scale factor. The real difficulty is the need to consider correlations between errors in the geopotential coefficients. This is impractical because of the large computational requirements.

Short of actually considering the correlations, the GEM-9 uncorrelated standard deviation model seems to be the most appropriate, although correlations do exist. However, even this model is computationally prohibitive. Comparison of the error map of this model with those of the geopotential difference models shows that the geographical fluctuation of the error as predicted by this model may be too mild. On the other hand, based on the same comparisons, it seems that the predicted gravity error magnitude for GEM-9, approximately 5 mgals at a 200-km altitude, is reasonable.

The random-sign and random-phase models, which are simple to implement, give rise to gravity error maps that seem reasonable, with local error fluctuations possibly somewhat excessive. The orbit determination errors based on these models also appear reasonable, although the error growths during prediction do not clearly exhibit the distinct characteristic of a sinusoidal variation superimposed on a linear growth. The main objection to these models is that they are empirical models without sound theoretical justifications.

The GEM-9 standard deviation model, when compared with other models, shows gravitational errors that are too low in the Southern Hemisphere and near the Equator. Therefore, its prediction of orbit errors for low-inclination satellites is too optimistic. On the other hand, this model has an unrealistic concentration of large errors near 0-deg longitude and 65-deg latitude that may give rise to anomalous orbit error spikes near these regions. This model is definitely faulty and should not be used.

A comparison between different geopotential models provides information about the accuracies of the individual models. The geopotential difference error models use the weighted differences of the spherical harmonic coefficients of two geopotential models as error coefficients. If one of the geopotential models is considerably more accurate than the other, the straight difference of the two models can be considered, with good confidence, as representative of the errors of the less-accurate model. If the two models are derived from independent sources, there is some justification in using their weighted differences as characterizing the accuracies of individual models, although the justification is weak and cannot be rigorously proven.

SAO and MD1 are models independent of GEM-9. GEM-9 was derived several years after SAO and MD1, and there should be no disagreement that GEM-9 is a considerably improved model. Thus, the GEM-9/SAO and GEM-9/MD1 difference models serve as good error models for the SAO and MD1 geopotential models. Doubling the numbers shown in Figure 4-5, which are for one-half the model differences, implies that the gravitational errors for the SAO model at a 200-km altitude vary from 2 to 26 mgals. The error map shows local fluctuations but not any particularly recognizable features. Similarly, it might be said that Figure 4-2, with the errors doubled, describes the accuracy of the MD1 model. It should be noted that, in Figure 4-2, there is a band of large errors at equatorial latitudes reaching, at a 200-km altitude, as large as 60 mgals (in accuracy), which is comparable in magnitude to the total contribution of the nonaxisymmetric portion of GEM-9. This band and its large magnitude is bothersome, because no ready explanations exist. Away from this band, the error distribution appears reasonable.

Of course, it is not the errors for these older models but the accuracy of GEM-9 that is of interest here. Since, at best, only the level of orbit determination error resulting from geopotential uncertainty can be expected, it may not be unreasonable to take the scaled difference of GEM-9 and a less accurate model as an error model for GEM-9, with the scale factor determined from some means of calibration. For instance, it might be speculated that GEM-9 is twice as accurate as MD1 and that therefore one-half of the GEM-9/MD1 difference would serve as an error model for GEM-9. This is, of course, not completely satisfactory because gravity errors are expected to become more uniformly distributed for higher order and more accurate models. The band of large errors, shown in Figure 4-2, is probably reflective of the nonuniform inaccuracies of MD1, and a simple scaling of the error model that preserves this feature of concentrated error would not be a good error model for GEM-9. The same consideration also applies to the GEM-9/SAO difference model. However, as shown in Figure 4-5, this difference model has a more random error distribution devoid of particular unexplainable features. Thus the GEM-9/SAO difference model, with a proper scaling factor, appears to be a reasonable error model for GEM-9.

The primary interest is not in the global gravity error distribution itself but in the effect of geopotential errors on orbit determination accuracies. Table 4-1 shows the orbit determination and prediction errors according to the
different geopotential error models. The following may be observed from the results presented in the table:

• With the exception of the GEM-9 standard deviation model, the orbit determination errors predicted by the different models do not differ by a factor greater than two during the tracking period. The error of the GEM-9 standard deviation model is too low. Greater differences occur for orbit propagation beyond the tracking period.

• The GEM-9/MDl and GEM-5/MDl one-half difference models are similar. Perhaps as a result of the large band of anomalous errors discussed earlier, the orbit determination errors predicted by these models are erratic (The excessive errors for the 200-km-altitude, 57-deg-inclination orbit and the small propagation errors for Landsat-5 as discussed in Section 4.4.)

It may be concluded from this study that the GEM-9 standard deviation model and GEM-9/MDl and GEM-5/MDl difference models are all faulty and should not be used. The random-sign and random-phase models are difficult to justify theoretically and do not seem to offer any advantage over the GEM-9/SAO difference model. Although the GEM-9 uncorrelated model has not been extensively studied, it is not expected to be much more accurate than the GEM-9/SAO difference model, yet the computational burden is much greater. It appears, from this limited study, that the scaled GEM-9/SAO difference model is the best error model for GEM-9. A scaling factor of onehalf is tentatively suggested before the availability of additional calibration.

4.6 REFERENCES

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SECTION 5 - ORBIT SMOOTHER PROCESS NOISE STUDY

Because the batch method of orbit determination is a subset of an orbit smoother, an improved orbit determination accuracy would be expected with a smoother. As discussed in Appendix A, the SEA program now has the capability of evaluating the performance of orbit smoothers. Limited investigations using this new capability have been performed as an exploratory study of orbit smoothers and also to validate the fading memory process noise option of the SEA smoother capability. Two different orbit determination scenarios are considered:

- The baseline TDAS navigation scenario for a 600-kmaltitude, 28-deg inclination satellite considered in Section 3
- The 34-hour arc Landsat-5 orbit determination scenario referred to in Section 4.4 (This investigation is undertaken in part to determine if the degradation of Landsat-5 orbit accuracy discussed in Section 2 results from geopotential errors compounded by the reduction in tracking coverage.)

The TDAS navigation smoother results are summarized in Table 5-1. Two process noise options are considered: the linear growth option and the fading memory option. The linear growth option assumes that, in addition to the modeled evolution of the covariance matrix, there is an additive increase (noise) in the variances of the Cartesian velocity components proportional to the time elapsed since the last measurement. The fading memory option assumes a multiplicative increase of the whole covariance matrix. The orbit smoother does indeed improve the performance over that of a batch orbit determination process for this particular TDAS scenario. The major error sources are geopotential errors and clock acceleration; the TDAS ephemeris errors are secondary, and other error sources are negligible. Although the fading memory option has not been investigated in as much detail as the linear growth option, the former does not appear to offer any advantage over the latter.

Table 5-1.	Orbit	Smoother	Performance	for	the	TDAS
	Navig	ation Scei	nario			

	Orbit Po	osition Errors (m)
Process Noise Option	Maxima	Root Mean Square
Linear Growth Rate		
10 ⁻¹⁶ (m/sec) ² /sec	104	46
10 ⁻¹⁴ (m/sec) ² /sec	78	41
10^{-12} (m/sec) ² /sec	67	33
10^{-10} (m/sec) ² /sec	40	24
10 ⁻⁸ (m/sec) ² /sec	42	23
Facing Memory Multi- plicative Factor		
1.1	61	24
1.25	63	36
1.5	98	38

The Landsat-5 results are presented in Table 5-2. Tracking oata consist of single TDRS and ground station data. The only error source considered is the one-half the GEM-9/SAO geopotential difference discussed in Section 4. Generally, increasing the process noise tends to decrease dynamic error at the expense of measurement error. Although measurement noise is excluded, Table 5-2 shows that an optimum noise level exists above which the dynamic error also increases. Another interesting result shown in Table 5-2 is that, with the addition of ground tracking data, orbit errors actually increase if process noise is not introduced. This is not a generally valid conclusion but shows that the behavior of

dynamic error is difficult to predict. On the other hand, Table 5-2 shows that, with the use of process noise, orbit errors are decreased when more tracking data are available.

Table 5-2. Landsat-5 Orbit Smoother Error Caused by One-Half GEM-9/SAO Differences

	Process Noise Linear Growth Bate	Orbit Po	Orbit Position Error (m)				
Tracking Data	(m/sec) ² /sec	Maximum	<u>Root Mean Square</u>				
Single TDRS and Lanasat-5 ground tracking stations	10-8 10-10 10-12 0	69 56 47 57	24 20 24 28				
As above with ad- dition of several Landsat-4 ground tracking stations	10-12 0	42 69	17 30				

Other results not shown in Tables 5-1 and 5-2 include the following:

- Maximum errors generally occur near two ends of the data arc where smoothing has smaller effects.
- Orbit solutions propagated beyond the data arc are generally less accurate for smoothed solutions than for batch solutions. This is not unexpected because the process noise introduced in an orbit smoother is artificial rather than physical.

SECTION 6 - CONCLUSIONS

Several topics related to low-altitude satellite orbit determination have been investigated. The topics studied and major conclusions reached are summarized below.

• Landsat-5 Orbit Determination using GPSPAC data--Landsat-5 orbit solutions computed from GPSPAC deltapseudorange (Doppler) data are good. Maximum differences between GPSPAC and GSTDN solutions are generally under 70 m. Maximum differences between partially overlapping GPSPAC solutions are even smaller. There is a good possibility that the GPSPAC solutions are superior to the GSTDN solutions in accuracy.

For orbit determination instead of real-time navigation, simultaneous data from four GPS satellites are not necessary. The study results indicate that approximately 3 hours of data from a single GPS satellite are sufficient to resolve Landsat-5 orbit and clock. A study of a randomly selected sample shows that the Landsat-5 orbit solutions based on individual GPS satellites agree to within 80 m, and typically less than 40 m.

As with Landsat-4 GPSPAC data, some inconsistencies exist between the Landsat-5 GPSPAC pseudorange and deltapseudorange data. Landsat-5 solutions derived from pseudorange data generally differ from the GSTDN solutions by maximas over 100 m. Furthermore, large, GPS-independent range observation residuals of over 100 m are seen in delta-pseudorange Landsat-5 GPSPAC data solutions. Based on these, it may be concluded that the pseudoranges have systematic errors on the order of 100 m in addition to the expected clock errors. The causes of these systematic errors

have not been determined, although bad data from an individual GPS satellite and several easily committed preprocessing errors have been eliminated as possible reasons.

In connection with the GPSPAC study, the computation of Landsat-5 orbits from GSTDN data was undertaken. Unfortunately, there are not as many ground tracking stations for Landsat-5 as for Landsat-4, and the accuracy of the resulting Landsat-5 orbit solutions is not as good as the corresponding Landsat-4 solutions. Investigations show that this degradation cannot be attributed solely to dynamic modeling errors accentuated by the sparsity of tracking coverage.

• TDAS Simulation--Simulated TDAS one-way Doppler data were generated. The data, with errors added, were input to an extended Kalman filter in R&D GTDS for the navigation of low-altitude Earth satellites. Comparisons with truth models yielded information about the navigation performance. The results showed very good agreement with those obtained earlier from error analysis using the SEA program. The agreement provides confidence in the TDAS capabilities of both programs and indicates that TDAS navigation performance can be studied economically using SEA instead of the computationally expensive simulations.

• Error Model for GEM-9--Several candidate error models for GEM-9 were studied. Although the specification of an appropriate model was difficult, the use of the GEM-9/SAO difference model with a proper scaling factor is recommended. A scaling factor of one-half is tentatively suggested before the availability of additional calibration.

• Orbit Smoothers--Some exploratory study of orbit smoothers was conducted using SEA. The fading memory process noise option of SEA was validated. However, this option does not seem to offer particular advantages over the linear growth option. This limited study showed that an orbit

smoother can indeed outperform a batch orbit determination
process in accuracy. The following two observations may be
made concerning orbit smoothers: (1) If accuracy is of primary concern, a smoothed orbit near the ends of the data arc
can be discarded because smoothing action is less at the
ends and orbit errors are generally greater. (2) Because
process noises are generally artificial rather than physical,
orbit propagation beyond the data arc from a smoothed orbit
' is generally not as accurate as the propagation from a batch
solution.

• Validation of the SEA Smoother/TDAS Capability--The SEA Smoother/TDAS capability was fully validated by testing. An inconvenience of the SEA smoother is that it will not output smoother error analysis results at times not coincident with a measurement. It is possible to trick the program into outputting results by introducing dummy measurements with negligible data weights, i.e., large measurement variances.

APPENDIX A - VALIDATION AND VERIFICATION OF THE SEA SMOOTHER/ TDAS CAPABILITY

The Sequential Orbit Determination Error Analysis (SEA) Program has been enhanced to incorporate error analysis capabilities for the following orbit determination scenarios:

- Orbit determination using the smoother method
- Orbit determination using the proposed Tracking and Data Acquisition System (TDAS) data

These enhancements to SEA were designed and implemented in 1984 under Task 42100.

This appendix outlines the results of the validation and verification testing of these enhancements. For the convenience of discussion, the enhanced SEA program will be referred to as SEA Version 4.1 to distinguish it from the unenhanced SEA Version 3.1.

The testing to validate and verify the SEA enhancements was divided into three phases:

• Phase 1 tests ensured that the enhancements have not corrupted the integrity of the original capabilities of SEA Version 3.1.

• Phase 2 tests compared the SEA Version 4.1 error analysis results with those of the independent Orbit Analysis (ORAN) Program. (ORAN is an error analysis program for the batch orbit determination method, which can be considered a subset of an orbit smoother. Thus, ORAN can be used to verify some, but not all, of the SEA smoother capabilities.)

• Phase 3 tests focused on the smoother algorithm's numerical stability and expected behavior under controlled operating conditions.

These three test phases and their results are described in more detail in Sections A.1, A.2, and A.3, respectively. During the course of testing several software modifications or corrections were required. After they were implemented, the testing sequence was reinitialized. These modifications or corrections are described in the sections describing the testing phases during which they occurred.

Finally, all keyword deck setups and associated job control language (JCL) used in testing have been archived so that they may be used as prototype benchmarks for future modifications to SEA. For reference, the listings of all deck setups are reproduced in Section A.5. References to setups are made in Sections A.1, A.2, and A.3. The convention for labeling a particular setup is as follows: PiSjRk, where i, j, and k are integers associated with the phase, a given scenario, and a given run number, respectively, for which the test was performed. For brevity, the corresponding SEA Version 3.1 control runs used in Phase 1 of the testing are not listed.

A.1 PARALLEL FUNCTIONAL VERIFICATION

A.1.1 TESTING DESCRIPTION

This phase of testing verified the functional integrity between SEA Version 3.1 and SEA Version 4.1 for nonsmoother options. It was undertaken to ensure that the smoother and TDAS enhancements had not corrupted the existing SEA options and processing. Parallel functional verification was performed under four different tracking scenarios:

1. Direct tracking of a low-altitude satellite from 10 ground stations--The satellite orbit is at a 200-km altitude and 28-deg inclination. An effective drag coefficient is alternately a solve-for or a consider parameter in the orbit determination process. Tracking data are available

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whenever the satellite is visible to a station (deck setup PlSlT1).

2. Tracking of a user satellite by six Global Positioning System (GPS) satellites. The user orbit is at a 400-km altitude and 57-deg inclination. Tracking data are available during periods of visibility. Several different geopotential error models are considered (deck setup PlS2T1).

3. Scheduled relay tracking of a user satellite through two Tracking and Data Relay Satellite System (TDRSS) relays. The user satellite is at a 600-km altitude and a 98-deg inclination (deck setup PIS3T1).

4. Continuous beacon tracking of a user satellite through three TDAS satellites (one backside, two frontside)--The user satellite is at a 600-km altitude and a 28-deg inclination (deck setup PIS4T1).

Each of these four tracking scenarios constituted more than one test run. In the test runs performed for this phase, most nonsmoother options were tested, although not in all possible combinations.

SEA Version 3.1 does not include either the smoothing or TDAS options; thus, the basis for comparison in this phase of testing was the forward-filtered results and those reports that are smoother/TDAS independent. In testing associated with the TDAS scenario, this comparison was slightly modified: the forward-filtered results of SEA Version 4.1 were compared with a TDAS-only modification of SEA Version 3.1. This was to test for any interference that might be present when the TDAS and smoother updates were combined in SEA Version 4.1. In addition, the SEA Version 4.1 tests were run with and without requesting the smoother option to test for any smoother-introduced inconsistency in the forward-filtered results.

A.1.2 TESTING RESULTS

All tests performed using SEA Version 3.1 agreed with their corresponding SEA Version 4.1 runs. It may be concluded that the smoother/TDAS updates have not corrupted any of the many options preexisting in SEA.

This agreement is demonstrated by the output listings shown in Figures A-1 and A-2, both of which are associated with the GPS tracking scenario. Figure A-1 displays the forwardfiltered error budget at 1440 min past epoch resulting from the nonupdated SEA Version 3.1. Figure A-2 displays the corresponding output resulting from SEA Version 4.1 (run PlS3T1). Although only three decimal places of accuracy are output, the length of propagation is long enough (1 day) so that any divergence would be displayed.

A.2 INDEPENDENT VERIFICATION

A.2.1 TESTING DESCRIPTION

For the independent verification phase, the smoother error analysis results of SEA Version 4.1 were compared and contrasted with corresponding results from the batch orbit determination error analysis program ORAN. SEA and ORAN are two independent programs with different capabilities; comparisons were thus made under restricted conditions in which correspondence or near correspondence between the two programs exists. In particular, this means that no TDAS tracking and no process noise were introduced into this phase of testing. Also, clock errors in SEA Version 4.1 were emulated by measurement biases in ORAN.

Under these restrictions, the same geopotential error models, measurement errors, and tracking systems were considered. However, the atmospheric drag models for the two programs are somewhat different. SEA uses the Harris-Priester model, and ORAN uses the Jacchia model.

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			ERROR	BUDGE	ſ			
SOLRAD I	SAT-01H 	SAT-01C 	SAT-01L - METERS 124D-01 105	RSS-POS - METERS .130D-01 .717	SAT-01HD HET/SEC 207D-05 .530D-04	SAT-01CD MET/SEC - 311D-05 - 253D-03	SAT-01LD HET/SEC .337D-05 .493D-03	RSS-VEL MEI/SEC .503D-05 .557D-03
ACCEL I MEASBI I MEASBI 2 MEASBI 4	*•534 1.95 <u>-•5820</u> =06_ •0 •0			4.98 16.0 .133D-05 .0 .0			422D-02 162D-02 603D-09 .0 .0	
RSS	2.15	.980	16.5	16.8	.2260-01	.714D-02	•454D-02	.241D-01
SOLRAD I GRAVCDEF LJNPED Accel 1 Measbi 1 Measbi 2 Measbi 4 Measbi 5 RSS	SAT-02H 4ETERS 0 553 224 0 .0 .0 .161D-01 .0 .597	SAT-02C HETERS 0 285D-01 -3.02 0 0 -0 -424 0 3.05	SAT-02L METERS 0 140D-01 64.5 0 -0 -0 108 .0 64.5	RSS-POS METERS 0 554 64.6 0 0 0 0 437 .0 64.6	SAT-02HD MET/SEC 0 310D-05 105 0 0 .0 .0 .0 .120D-03 .0 .105	SAT-02CD MET/SEC 0 583D-04 166D-01 0 0 854D-03 .0 .166D-01	SAT-02LD MET/SEC 0 649D-03 313D-03 0 0 178D-04 721D-03	RSS-VEL MET/SEC 0 .052D-03 .106 0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0
	USERDRAG	CLKUT I	DRIFT 1	MEASBI 3				
SOLRAD I GRAVCJEF LUMPEJ ACCEL I HEASBI I MEASBI 2 MEASBI 4 MEASBI 5 RESS	.3130-05 .7440-04 -2580-02 -8440-03 .1270-09 .0 .0 .0 .0 .0	•225D-01 •428 2•97 51•1 •162D-04 •0 •0 •0 •0	380D-06 .446D-05 411D-05 362D-01 .852D-11 .0 .0 .0 .0 .362D-01	• 0 • 0 • 0 • 0 • 0 • 0 • 0				
			-					10

Figure A-1. SEA Version 3.1 Forward-Filtered Error Budget at 1440 Minutes. User Tracking Through Six GPS Satellites

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			ERROR	BUDGEI			_	•
SJLRAD 1 Gravcdef	SAT-01H - 4ETERS	SAT-01C HETERS -106D-03 -217D-01	SAT-01L 	RSS-POS METERS •130D-01 •717	SAT-01HD MET/SEC 207D-05 .530D-04	SAT-01CD HET/SEC .311D-05 253D-03	SAT-01LD -MET/SEC -337D-05 -493D-03	RSS-VEL MET/SEC .503D-05 .557D-03
ACCEL I ACCEL I ALASBI I	534 1.95 .582D-06	309 .930 271D-06	-15.9 -1170-05	4.98 16.0 	•5240-02 •220D-01 •914D-09	7130-02 214D-04 394D-10	+ 162D-02 - 603D-09	•9800-02 •2200-01 •1100-08
HEASBI 4 - HEASBI-5 RSS	• 0 • 0 • 0 2 • 15	.980	.0	•0 •••••••••••••••••••••••••••••••••••	.0 .226D-01	•0 •0 •714D-02	•0 0_ •454D-02	•0 •0 •241D-01
SJLRAJ 1 GRAVCJEF LUMPEJ ACCLL 1 MEASBI 1 MEASBI 2 MEASBI 2 MEASBI 5 RSS	SAT-02H METERS 0 553 - 224 0 0 0 - 161D-01 0 597	SAT-02C 4ETERS 0 285D-01 -3.02 0 0 0 -424 3.05	SAT-02L METERS 0 -0140D-01 64.5 0 0 0 -0 -0 -108 0 64.5	RSS-POS METERS 00 554 64.6 0 0 0 0 437 0 64.6	SAT-02HD HET/SEC - 0 - 0 - 105 - 0 - 0 - 120D-03 - 0 - 105	SAT-02CD MET/SEC - 583D-04 - 166D-01 - 0 - 0 - 854D-03 - 166D-01	SAT-02LD MET/SEC .0 .649D-03 .313D-03 .0 .0 .0 .0 .178D-04 .0 .721D-03	RSS-VEL MET/SEC 0 0652D-03 106 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
SJLRAD 1 GRAVCDEF LJMPED ACCEL 1 MEASBI 1 MEASBI 2 MEASBI 4 MEASBI 5	USERDRAG .313D-35 .744D-04 -258D-02 -344D-03 .127D-09 .0 .0	CLKd1 1 • 225D-01 428 2.97 51.1 • 162D-04 • 0 • 0	DRIFT 1 350D-06 .446D-05 411D-05 362D-01 .652D-11 .0 .0	MEASBI 3 • 0 • 0 • 0 • 0 • 0 • 0 • 0 • 0				•
RSS	.2710-02	51.2	. 3620-01	•0				ኇ

Figure A-2. SEA Version 4.1 Forward-Filtered Error Budget at 1440 Minutes. User Tracking Trhough Six GPS Satellites

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Because the two programs use different error analysis algorithms, some differences in the results produced were expected even if the initial conditions and input values were the same. Special attention was therefore accorded the degree of disagreement between SEA and ORAN results to ensure that discrepancies were not larger than bounds established by physical considerations.

Independent verification was performed under two different tracking scenarios using corresponding SEA and ORAN setups:

1. Direct tracking of two TDRS-type spacecraft through a single ground tracking station--Dynamic errors considered are lumped geopotential modeling errors (GEM-9 15x15 - GEM-1 8x8) and gravitational constant. Measurement bias errors are considered on both range and range-rate data (deck setups P2S1T1 and P2S1T10 (the 0 indicates the ORAN run)).

2. Relay tracking of a user satellite through two TDRSS-type satellites--The user satellite is at a 400-km altitude and a 28-deg inclination. Dynamic and measurement errors are of the same type as those in the previous scenario. In addition, an effective drag uncertainty is considered (deck setups P2S2T1 through P2S2T20).

In this phase of testing, the smoother results of SEA Version 4.1 were compared with the batch results from ORAN. In addition, corresponding observation measurements and propagated ephemerides between SEA Version 4.1 and ORAN served as additional bases for comparison.

A.2.2 TESTING RESULTS

In the course of testing, it was found that the two programs usually agree quite well: two to three decimal digits were quite common for most numeric results. Close comparison between the two programs was achieved in the direct tracking scenario. Figures A-3 and A-4 display the error budget

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TINE FRONT EPOCH IN MINUTES = 1080.

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FRROR RUNGET

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GRAVCOFF LUMPFD MEASHIII MEASHIII MEASFII MEASFII MEASFII MEASFII	527-0111 11ETFRS 3.43 278 607D-01 7.21 7.99	SAT-01C VFTFRS 21P .272 159 .0 -31.1 .0 31.1	SAT-01L "ETFRS -28.3 2.11 -20.4 -40.4 -40.4 -33.4	RSS-POS MFTERS 24.5 20.15 20.4 51.4 .0 62.3	SAT-01Hn MFT/SEC 2070-02 -1610-03 1490-02 0 2960-02 0 -3910-02	SAT-01CD MET/SFC .1247-03 .1550-04 .9250-04 .0 .6540-03 .0 .6730-03	SAT-01LD HFT/SEC 2620-03 1360-04 4270-05 0 3870-03 .0 .4680-03	RSS-VEL MET/SEC 2090-02 1620-03 1500-02 0 3050-02 0 4000-02
GRAVOOFF LUMPFJ MFASSIJ VEASSIJ VEASSIJ RSS	SAT-02H METERS 3.54 635 0 17°P-01 -3.43 4.97	SAT = A2C SFTF RS . R21 3.31 .0 .595 .7 1.59 3.71	SAT - 02L MFTFRS 28-5 6-94 -015 -03-7 42-9	RSS-PDS 4FTERS 28.7 7.71 .0 - .20.5 .0 .24.0 43.3	SAT-02HN MET/SEC - 2080-02 - 5150-03 0 - 1500-02 0 - 1880-02 - 3220-02	SAT-02CD MET/SEC. -120D-03 -435D-04 -901D-04 -192D-02 -192D-02	SAT-021 D MET/SEC .254D-03 .159D-04 .0 .166D-05 .0 .782D-04 .266D-03	RSS-VEL MET/SEC .210n-02 .5180-03 0 .150n-02 .269n-02 .376n-02

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Figure A-3. SEA Version 4.1 Smoothed Error Budget at 1080 Minutes. Direct Tracking on Two TDRS-Type Spacecraft

		ESTIMATED HO	FRROR FOR	ARC NO. 1 DUE	TO UNNODELED PAR	AMETERS		
DELTA H (METERS)	NFLTA C (VFTFRS)	NELTA L (VETERS)	RSS POS (METERS)	DELTA HDOT (CM/SEC)	CFLTA CONT (CM/SFC)	DELTA LDOT (CM/SFC)	RSS VFL (CM/SFC)	UNAD.JUSTED PARAMETER
		TIMF = 108n_0r	MTNUTF	S YYHNOD SATELITE	ННИМ 55.5 = 8nn3n [.] 1	1800 0.0	-	
3,4244 27861 -626160-01	165A8 27295 12875	-28,324 2.1153 -20,376	28.531 2.1539 20.376	20736_ - 161390_01 14918	.13071470-01 .20 .14905120-02 .1 10004510-01 4	4242980-01 8646602-02 8569790-03	.20948_ .162650_01 .14951	GRAVCO MD1_MD2 GRAV RNGRIASI
7 ,1973	-30,992	-40,267	51.320	29491	6523936n-01 - 3	866051 <u>n</u> -01	0 30451	RNGBIAS2 RDOTRIAS1 RDOTRIAS1
3.5321 .63369	91497 3,3604	28,476 6.9516	28.709 7.7472	SATELI TTE : 20853_ 516390_01	2	544630 <u>5</u> -01 5628140-02	.21050 .51859n-01	GRAVCO MD1-MD2 GRAV
.14625n_01 _14625n_01	-0 -65650 -0 2-2164	20.486 -23.475	20.497 23.830	.0 150n2 14548	-196660680-02 -11 0 -1860768 8	353914ñ-03 181564ñ-02	.15033 .0 .26300	RNGRIASI RNGRIAS2 RDOTBIAS1 RDOTBIAS2

Figure A-4. ORAN Batch Error Budget at 1080 Minutes. Direct Tracking on Two TDRS-Type Spacecraft

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output from SEA Version 4.1 and ORAN (setups P2SIT1 and P2SIT10) at 1080 min after epoch.

In the relay tracking scenario, a limitation in ORAN complicated the process of comparison between the two programs. ORAN does not model the TDRSs directly as relay satellites with given orbits; an artifice has to be used to make ORAN simulate the relay role of the TDRSs.¹ Naturally, greater disparities should be expected between the results.

An example of the relay tracking scenario results is shown in Figures A-5 and A-6, in which the error budget outputs for 180 min past epoch are shown for SEA and ORAN, respectively (deck setups P2S2T1 and P2S2T10). All error budgets agree quite well except for the errors caused by the gravity coefficient uncertainty and the drag uncertainty. The ORAN result shows considerably greater effect for the gravity coefficient uncertainty. This was expected because, in the artifice of ORAN simulation, this uncertainty also accounts for part of the TDRSS ephemeris errors. In other words, the ORAN result includes both the dynamic effect of gravity coefficient uncertainty and the geometric effect of TDRSS ephemeris error that can be attributed to gravity coefficient uncertainty in deriving the TDRS orbits. The drag uncertainty effects from the two programs are different because, as discussed above, two different atmospheric drag models were used.

A comparison between SEA and ORAN was also performed for the scenario in which all three satellite orbits are solved for simultaneously. Figures A-7 and A-8 demonstrate the results of setups in which both relay and direct tracking of the

¹EG&G Wasnington Analytical Services Center, Inc., <u>TDRSS</u> <u>Era Orbit Determination System Review Study</u>, B. T. Fang and B. P. Gibbs, December 1975.

TIME FROM EPOCH IN MINUTES = 1A0.0

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FRROR BUDGET

	SAT-01H	SAT+01C	SAT-01L	RSS-POS	SAT-01HD	SAT-01CD	SAT-01LD	RSS-VEL
USERDRAG	•17A	2.40	-9.55	9.85	9670-02	- 273D-02	- 204h-03	100n-01
GRAVFOFF	•420	_378D_01	107	.660	-527N-04	900D-03	. 545n+03	105n-02 ·
LJAPED	+14.4	65.6	_3 <u>0_</u> 4	73.7	.360n÷01	.3490-01	•50eu=01	.5420-01
TEASEL 1	-2.33	-3.31	1-59	4,35	9150-03	.3720-02	. 2610-02	•464D-02
	•735 •100D 05	2.27	3,18	* 99 * 700 00	15/0-02	• 6870 - 02		• <u>/100-02</u>
MEASAL 4	-2930-03	3660-02	9430-03	.3790-02	-1430-05	. 444D_05	-3130-06	-4720-05
PSS	14.6	65.8	32 n	74 6	.373n_01	-35AD-01	2080-01	5580-01

Figure A-5. SEA Version 4.1 Smoothed Error Budget at 180 Minutes. Relay Tracking of 400-Kilometer-Altitude Spacecraft Through Two TDRSs

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	EDDOD	F 20				-			
EXTRACT HOL	Енкілн	F JH	VAC.	NO.	1	DUF	тп	UNMODELED	PARAMETERS

METERS)	NELTA C (METERS)	METERS)	RSS POS (METERS)	NFLT∆ HDNT (C ^M /SFC)	DELTA (DAT (CM/SEC)	DELTA LDOT (CM/SEC)	BSS VFL (rti/sfc)	UNAN IUSTED PARAMETER
-1.3109	5,8107	TTME = 180.000 5.5197	•TNUTF: 8.1207	S YYWMOD HHM SATELITTE 1 - 23791 - 4	M 55.5 = 80031 337399	01 300 D.O.	56707	C B A U C O
-14,257 -853640_01 -2,3331 -7,3335	68,339 1,1265 -3,3104 2,2714	_97,309 _4,3585 1,5947 3,1859	74,987 4,5050 4,3526 3,9806	3,3766 3, 44027 1 -915920-01 3 -15715 6	460653 2 274946 - 723932	. 040667_ 39893755-02 2614493_ 6155615_01	5.2415 .45900 .46414	MD1-MD2 GRAV DRAG RNGRIAS1
- 2929/ ri-n3	40912D_02 -36599D_02	- 396460-02 - 947980-03	549701_02 379090_02	422000-03 - 6 143360-03 - 4 SATELI TTE 2	0693410_03 4818790_03	57745995_05 51264975_04	.7392555-03 .471605-03	RDOTRIAS2 RDOTRIAS1 RDOTRIAS2
- 13116 - 817240_06 - 299880_05	- 188297_01 _131930_04 _348370_04	-20.675 1.0003 -25390D-05 -576720-06	24,930 1,0091 ,134720-04 ,349620-04	.20872 - 8 .729920_02 - 2 .923900_08 - 9 .501850_08 - 5	2832790-02 4961790-02 5063680-07	24690330-01 94132755-03 50029395-08	.21034 .777050-02 .957000-07	GRAVCO MD1_MD2 GRAV DRAG DNCDIACI
	.301680_04 _691630_08 193790_07	195610_05 _444P50_0P 570480_08	303190_04 755150_09 203320_07	365523_08 7	5319273_07 653Pn50_10 0732900_09 _ 1	16774213_07 62764649_11 15134579_10	772515-07 •904990-10 •113880-09	RNGPTAS2 RDOTBIAS1 RDOTBIAS2
1.9010 205850_r5 205850_r5 205850_r5 201440_r5	-1.9311 -2.7022 158930-04 221570-04 -289200-04	20.95x 14.599 -,533490-05 .118240-05 -,134950-05	24.227 14.95A .168910.04 .293020.04 .293027.04	SATFLITTE 3 -21065 - 1 -10712 - 1 -361840_07 5 -469770_08 60 121800_07 2	6337450-02 4775740-01 72644000-07 69644020-98 1 2345770-07	26381210-01 76468733-02 13226000-07 18767193-07 19927375-07	.21233 10841_ .690180_07 .204430_07	GRAVCO MD1-MD2 GRAV DRAG RNGPIAS1
249350_03 .220643_03	_123930_07 145760_07	13n230_n7 842720_n8	141490_07 169910_07	886745_10 80 -696465_10 _2	6358590_10 7294761_101	4421253_10 13233935_10	.124410-09 .67809^-10	RDOTRIAS1 RDOTRIAS2 RDOTRIAS2

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Figure A-6. ORAN Batch Error Budget at 180 Minutes. Relay Tracking of 400-Kilometer-Altitude Spacecraft Through Two TDRSs

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			E R R O R	8 U D G E 1	, -			e et
MEASBI 1 Measbi 2 Measbi 3	SAT-01H HETERS -1.47 1.19 414D-02	SAT-01C HETERS 2.04 2.86 130D-01	SAT-01L METERS -1.03 -1.86 861D-01	RSS-POS METERS 2.72 3.61 ,8720-01	SAT-01HD MET/SEC 	SAT-01CD MET/SEC .844D-02 .948D-02 441D-04	SAT-01LD MET/SEC -159D-02 143D-02 .597D-05	RSS-VEL MET/SEC .876D-02 .998D-02 .683D-04
RSS RSS	889D-02 1.90	432D-02 3.51	•423D-01 2•12	•435D-01 4•52	184D-05 .328D-02	•245D-04 •127D-01	•952D-05 •214D-02	•2640-04 •1330-01
MEASBI 1 MEASBI 2	SAT-02H METERS -1.42 -230	SAT-02C METERS 23+4 12-6	SAT-02L METERS -3.62 -4.74	RSS-POS METERS 23.7	SAT-02HD MET/SEC .794D-04 .187D-03	SAT-02CD MET/SEC .183D-02	SAT-02LD MET/SEC .104D-03 .290D+04	RSS-VEL MET/SEC 183D-02
MEASBI 3 NEASBI 4 RSS	381D-01 . 542D-01 1.44		•112 •9270-01 5•97	• 278 • 495 27• 3	5920-05 .5860-05 .2030-03	298D-04 .170D-04 .244D-02	• 2460 - 05 - • 3610 - 05 • 1090 - 03	• 3050-04 • 1830-04 • 2460-02
	SAT-03H Meters	SAT-03C Meters	SAT-03L Meters	RSS-POS Meters	SAT-OJHD HET/SEC	SAT-03CD Met/sec	SAT-03LD Met/sec	RSS-VEL NET/SEC
MEASBI 1	-1.52	_ 19.9	_ 5.92 _	20.8	500D-03	+134D-02	•128D-03	-144D-02
MEASBI Z	-1.95	18.3	368	10.4	- 3370+04	+100D=02	•144D=03 •346D=06	-10/0-02
MEASBE 4	+482D=02	.170	•236	.291 _	-1590-04	9010-05	•206D=06	-1830-04
RSS	2.47	27.1	5.95	27.8	-508D-03	-213D-02	.1920-03	-2200-02

Figure A-7. SEA Version 4.1 Smoothed Error Budget at Epoch. Relay Tracking Scenarios in Which User and Relay Orbits Are Solved for Simultaneously

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TIME FROM EPOCH-IN MINUTES = .0

ESTIMATED HOL FPROR FOR ARC NO. 1 DHE TO HINMODELED PARAMETERS

(PETERS)	I TETERS	(VETERS)	(HETERS)	ΠΕΕΤΔ ΗΠΟΙ (Γ4/SFC)	976174 CD97 (CM/SFC)	DELTA LDOT (CM/SFC)	RSS VEL (rm/sfc)	UNAD, JUSTED PARAMETER
		TJMF = 10	MINUTI	S YYMMOD H	HMM 55.5 = 806	รถา ก อ.ก		
-1,4754 1,1995 -,416415,62 -,316415,62	-0.0414 2.1575 104105-61 434555-62	-1.(274 -1.6556 96177D_01 -42394D_01	2.7202 3.60°3 .372430_01 .435190_01	5475L1775 1 17206 27921 519120-02 - 190510-03	_A440144 _9475101 _44042810_02 _24481620_02	.1592187 .1427880 .59897243.03 .94836767.03	.87597 .99906_ .683410-02 .263230-02	RNGRIAS1 RNGRIAS2 RDOTRIAS1 RDOTRIAS3
-1.4210 22819 191226-11 541636-01	21.40X 12.634 25175 - 43251	-3.6353 -4.7454 _11019 _32449D_01	2×.726 13.502 .27824 .49426	SATELITE 2 .903230-02 .187370-01 591710+03 - .584610-03	.1831492 .1623463 .29873610-02 .17008260-02 -	.10431140-01 28903380+02 24571670-03 .36090940-03	.18362 .16345 .305535-02 .183430-02	RNGRIASI RNGRIAS2 RJOTRIAS1 RDOTRIAS2
-1. 200 -1.9479 - 419320-02 - 425820-02	16.009 1.533 29668 1676		?C.822 18.439 _46498 -29047	SATFLITTE 3 498770-01 842360-02 .231890-02 159150-02 -	.1336306 .1656153 .25061160-02 - .90320930-03	.12779080-01 .14358780+01 .34412230-04 .20249220-04	.14301 .16645 .341450-02 .183009-02	R VGRIAS1 RNGRIAS2 RDOTRIAS1 RDOTRIAS2

Figure A-8. ORAN Batch Error Budget at Epoch. Relay Tracking Scenarios in Which User and Relay Orbits Are Solved for Simultaneously

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relays are present (deck setups P2S2T2 and P2S2T2O). These figures display the error budgets for all three satellites at the epoch or starting time and show very good agreement.

A.3 FUNCTIONAL PERFORMANCE VALIDATION

A.3.1 TESTING DESCRIPTION

As mentioned in Section A.2.1, the SEA smoother capability cannot be verified in the presence of process noise by examining the agreements between SEA and ORAN. Thus, the final phase of testing concentrated on the effects of process noise on the smoother behavior. (See Section 5 for a related study.)

If the smoother was implemented correctly, the following results should be observed in the tests:

• The smoothed state variances should be smaller than the corresponding filtered state variances. This should be true irrespective of the magnitude of the process noise.

• The smoothed state variances should increase with the increase of the process noise.

• The process noise should introduce a fading memory feature into an estimator. Thus, the effect of dynamic errors is attenuated with the use of process noise whereas the effect of measurement noise is amplified. Furthermore, the filter is a one-sided fading memory estimator whereas the smoother is a two-sided fading memory filter. The fluctuation of errors with time is thus considerably smaller for a smoother than for a filter.

This phase of testing was performed using the following tracking scenarios with controlled process noise parameters:

 Scheduled relay tracking of a user satellite through two TDRSs--The user satellite was at a 600-km altitude and a 28-deg inclination. A nominal velocity variance process

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noise of $1 \times 10^{-9} \text{ m}^2/\text{sec}^3$ and several variations were used (deck setup P3S1T1).

2. Continuous tracking of a user satellite through three TDAS satellites (one backside, two frontside)--The user satellite is at a 600-km altitude and a 28-deg inclination. A nominal velocity variance process noise of 1 x 10^{-9} m²/ sec³ and several variations were used (deck setup P3S2TL).

A.3.2 TESTING RESULTS

During the course of this phase of testing, the following errors relating to the process noise in backward filtering/ smoothing were uncovered and corrected:

- The process noise variance had an incorrect sign because the elapsed time was computed based on backward time differences.
- The process noise variance was not propagated using the backward transition matrix. This was a subtle error that was intimately related to the method chosen to model the process noise in forward filtering.
- The backward filter/smoother executive did not include the backward process noise added since the last measurement, when it computed the smoothed error results.

After these corrections were made, tests performed confirmed that all process noise effects listed in Section A.3.1 were indeed observed, thus providing confidence that the SEA smoother capability was working correctly. Figures A-9 through A-12 show some sample error analysis results at 1140 min of a 1440-min TDAS tracking arc (run corresponding to Scenario 2 of Section A.3.1). The reduction of error from filtering (Figure A-9) to smoothing (Figure A-10) and the decrease in dynamic error (lumped geopotential) and

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ERROR BUDGET

. .	SAT-01H	-jAT-01C	- 5+T-01L		5AT-01HD			- ASS-VEL
	METERS	METERS	METERS	METERS	HET/SEC	HET/SEC	MET/SEC	HET/SEC
SOLRAD 1	4190-02	2880-03	.2210-02	•475D-02	4390-05	-,106D-05	• 5250-05	•693D-05
GRAVCIEF	.557	•681	5150-01	.881	9450-04	3350-03	•581D-03 ⁻	•6770-03
LUMPED	-4.47	-16.4	10.2	19.8	5520-02	1860-01	•428D-02	.198D-01
ACCEL 1	1-13		==13.7	17.2	122D-01	8010-02	-•5000-05	-147D-01
MEASBI 1	+.432D-01	.103	.674D-01	•130	531D-04	• 56 3D-04	•3400-04	•845D-04
NEASBE 2	.407	4290-01	881	.971	.7980-03	785D-03	368D-03	-118D-02
NEASBE 3 -	515D-01							
MEASBI 4	336	1.08	541	1.25	.185D-03	2590-03	.2150-03	•384D-03
MEASBI 5	6310-02	.646D-01	121	+138	•488D-04	1470-03	142D-05	-155D-03
MEASBI 6	.6100-01	.183D-01 - ·	.363	- 369	2500-04	.2210-03	5620-04	•229D-03
EPHEMERR	.865	3.89	14.0	14.5	105D-01	• 621D-02	103D-02	122D-01
RSS	4.75 _	19.8.			1700-01	.2120-01	.491D-02	•276D-01
.	USERDRAG	- 	-DA1#1					
SOLRAD 1	.3400-05	-6470-02	2600-06	•				
GRAVCOEF	.7370-04	5.62	7290-04					
LUNPED	686D-04	-45.6	-7410-03					
ACCEL	4520-03	24.7						
NEASBI I	.1020-03	-14.3	282D-03					
HEASBE 2	2470-04	2.48	2000-04					
MEASB1-3								
MEASOI 4	-124D-03	1.69	6120-04					
HEASHI 5	-211D-04	-15.9	.2310-03					
MEASBI 6		6.32	- 9200-04					
EPHENERA	.518D-03	-71.2	339D-03					
RSS		92.3						
	STAND	ARD DEV	ATION	- CORREL	ATION H	ATRIX		
	SAT-01X	SAT-01	¥	SAT-012	5AT-01X0	SAT-01V	D SA	T-012D
SAT-OLX	- 975	. 431		- 133	377	-414		.331
SAT-OLY	431			404	202	-887		.615
SAT-012	.133	404		.916	255	-640		494
SAT-01X0	377	- 202		- 255	-5520-03	.156	-	-114
SAT-OLYD	414	. 887		- 640	.156	126D	-02	.487
SAT-017D	. 331	-615		494	114	487		-116D-02
USERDRAG	- 3120-02		0-02	-351D-02	2470-02		-02	-3530-02
CLEBII	-1370-01	513	0-02	-3820-01	- 4 4 6 D - 0 4	-230D	-01 -	-122D-01
DRIFT 1	640D-01	320		146	123	288		-194
	USERDRAG	CLK81	1	DRIFT I	•			
SAT-OLK	3120-02	.137	0-01	6400-01				
SAT-OLY	.3320-02	513	D-02	326				â
SAT-OLZ	.3510-02	. 382	D-01	146				90
SAT-OLXD	2470-02	- 446	D-04	123				1 50
SAT-OLYD	.3910-32	.230	D-01	288				
SAT-01ZD	.3530-02	122	D-01	194				7 😥
USERDRAG	.2500-01	. 352	D-02	3510-02				0 57
CLKBI 1	.3520-02	4.39	. –	579				O 🐔
DRIFT 1	3510-02	579		.1100-03				20

Figure A-9. SEA Version 4.1 Forward-Filtered Error Budget at 1140 Minutes. Nominal Velocity Variance Rate Process Noise of 1 x 10⁻⁹ Meter²/ Second³ F POOR QUALITY

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ERROR BUDGET

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SOLRAJ I GRAVCOEF LUMPED ACCEL I MEASBI 1 MEASBI 2 MEASBI 3 MEASBI 4 MEASBI 5 MEASBI 5 MEASBI 6 EPHEMERR RSS	SAT-01H HETERS - 241D-04 - 689 -5.59 1.40 - 206D-01 - 198 - 211D-01 - 141 - 428D-03 - 568D-01 1.21 5.93	-5AT-01C METERS .087D-05 .736 -13.2 14.0 .589D-02 .591 807D-01 .57 .749D-01 .340D-01 .917 19.3	5AT-01L HETERS 812D-04 .396D-01 5.99 -7.80 .361D-01 512 489D-01 442 442 850D-01 .333 13.8 16.9	R55-P05- METERS .851D-04 I.01 I5.5 I6.1 .420D-01 .806 967D-01 .725 .113 .340 I3.8 26.3	MET/SEC 472D-06 570D-05 285D-02 .911D-02 254D-04 .496D-03 425D-04 .416D-03 .679D-04 186D-03 105D-01 .142D-01	6AT-01CD MET/SEC 144D-05 374D-03 645D-02 236D-04 168D-03 .137D-04 .410D-04 .991D-05 705D-03 .256D-02 .120D-01	SAT-OILD RSS-VEL MET/SEC MET/SEC .381D-06 .156D-05 .520D-03 .641D-03 .415D-02 .819D-02 -128D-02 .134D-01 .194D-04 .398D-04 192D-03 .557D-03 .432D-05 .687D-04 .432D-05 .687D-04 .432D-04 .733D-03 .160D-02 .108D-01 .454D-02 .191D-01
	USERDRAG	-CLK811	DR1FF1				
SULRAD 1 GRAVCDEF LUMPED ACCEL 1 MEASBI 1 MEASBI 2 MEASBI 2 MEASBI 3 MEASBI 4 MEASBI 5 MEASBI 5 MEASBI 6 EPHEMERR RSS	• 413D-05 • 576D-04 - 101D-02 - 197D-03 • 102D-03 - 489D-04 - 115D-03 • 606D-04 • 123D-04 • 672D-03 • 125D-02 S T A N D	.634D-02 5.97 -45.6 37.5 -14.3 2.64 -3.15 -2.14 -15.9 6.37 -70.8 95:2	932D-07 739D-04 .665D-03 403D-01 279D-03 393D-04 463D-04 458D-04 231D-03 939D-04 266D-03 .403D-01 A I I O N	- CORREL			
_	SAT-01X	SAT-01Y		SAT-012	SAT-01XD	SAF-01YD-	
SAT-018	. 720	- 500		. 202	617	. 644	<u> </u>
SAT-OLY	.509	- 449*		-1859D-01	100 -	607	310
SAT-012	202	- 0800	- 01		• I U V	• OU /	DLLA
		-•0340	-01	.543	.130	.310	•251
SAT-OIXD	637	.109		•543 •130	•130 •4610-03	• 310 - • 133	•251
SAT-DIXD SAT-DIYD	637	8590 - 109 - 607		•543 •130 •310	•130 •461D-03 -•133	•310 •133 •511D-0	•251 •263 •3 •9100-01
SAT-01XD SAT-01YD SAT-01ZD	637 .644 .486	8550 -109 .607 .338		•543 •130 •310 •251	• 1 30 • 4610-03 • 1 33 • 283	.007 -310 133 .5110-0 .9100-0	-251 -263 -3 -9100-01 -1 -6960-03
SAT-OIXD SAT-OIYD SAT-OIZD USERDRAG -	637 .644 .486 	6590 .109 .607 .338	-01	•543 •130 •310 •251 •7212D=03	.130 .461D-03 133 283 		- 251 - 263 - 263 - 263 - 263
SAT-OIXD SAT-OIYD SAT-OIZD USERDRAG - CLKBI I	637 .644 .486 .1740-03 .1070-01			•543 •130 •310 •251 •7212D=03 •528D=01	.130 .461D-03 133 283 		-251 -263 -263 -3 -9100-01 -1 -6960-03 -32470-03
SAT-OIXD SAT-OIXD SAT-OIXD Userdrag Clkbi i Drift i	637 .644 .486 	039U .109 .607 .338 	-03 -01 -02	•543 •130 •310 •251 •7212D-03 •528D-01 •176D-03	.100 .130 .461D-03 133 283 		-251 -263 -263 -3 -9100-01 -1 -6960-03 -32470-03 -1 -1740-01 -27020-03
SAT-OIXD SAT-OIYD SAT-OIYD USERDRAG USERDRAG CLKBI I DRIFT I	637 .644 .486 .174D-03 .107D-01 119D-02 USERDRAG		-01 -03	•543 •130 •251 •72120-03 •5280-01 •1760-03	.100 .130 .461D-03 133 283 		-251 -263 -263 -3 -9100-01 -6960-03
SAT-OIXD SAT-OIYD SAT-OIZD USERDRAG - CLKBI I DRIFT I SAT-OIX	637 .644 .486 		-01 -03	•543 •130 •251 •251 •528D-01 •176D-03 DRIFT 1	.100 .130 .461D-03 133 283 		• 250 • 251 - 283 • 9100-01 • 6960-03 • • - • 1740-01 • - • 1740-01 • - • 7020-03
SAT-OIXD SAT-OIZD USERDRAG - CLKBI I DRIFT I SAT-OIX SAT-OIX	637 .644 .486 		-01 -03 -00 -02 -02 -01 -01 -01	•543 •130 •251 •251 •5280-01 •5280-01 •1760-03 DRIFT 1	.130 .4610-03 133 283 		-251 -263 -263 -3 -9100-01 -1 -6960-03 -32470-03
SAT-OIXD SAT-OIZD USERDRAG - CLKDI I DRIFT I SAT-OIX SAT-OIX SAT-OIZ	637 .644 .486 1740-03 .107D-01 119D-02 USERDRAG 174D-03 .158D-03 .212D-03		-01 -03 -00 -02 -01 -01 -01 -01	-543 -130 -310 -251 -2120-03 -528D-01 -1760-03 DRIFT 1 119D-02 1404D-02 1760-03	.130 .4610-03 133 283 		- 251 - 263 - 263 - 263 - 263 - 260-01 - 6960-03
SAT-OIXD SAT-OIZD USERDRAG - CLKBI I DRIFT 1 SAT-OIX SAT-OIX SAT-OIXD	637 .644 .486 .174D-03 .107D-01 119D-02 USERDRAG 174D-03 .158D-03 .212D-03 .514D-03		-01 -03 -01 -02 -02 -01 -01 -01 -01 -02	•543 •130 •251 •251 •528D-01 •176D-03 DRIFT 1 119D-02 176D-03 176D-03 176D-03	.100 .130 .461D-03 133 283 		- 251 - 263 - 263 - 263 263
SAT-01XD SAT-01YD SAT-01ZD USERDRAG - CLKB1 1 DRIFT 1 SAT-01X SAT-01X SAT-01X SAT-01XD SAT-01XD	637 .644 .486 		-01 -03 -001 -02 -01 -01 -01 -02 -01	•543 •130 •251 •251 •528D-01 •176D-03 DRIFT 1 -1190-02 -1760-03 -154D-02 -154D-02 -280D-02	.100 .130 .4610-03 133 283 		-251 -263 -263 -3 -910D-01 -696D-03 -3247D-03
SAT-01XD SAT-01YD SAT-01ZD USERDRAG - CLKDI I DRIFT I SAT-01X SAT-01X SAT-01Y SAT-01ZD SAT-01ZD	637 .644 .486 .1740-03 .107D-01 119D-02 USERDRAG 174D-03 .1580-03 .212D-03 .514D-03 .170-03 .247D-03		-01 -03 -00 -02 -01 -01 -01 -01 -01 -02 -01 -01 -01 -01 -01 -01 -01	.543 .130 .310 .251 .528D-03 .528D-01 .176D-03 DRIFT 1 .119D-02 .176D-03 .154D-02 .280D-02 .280D-02 .280D-02 .702D-03	.100 .130 .4610-03 133 283 	- 010 - 133 - 133 - 5110-(- 9100-0 1700-0 - 4210-(- 2800-0	-251 -263 -263 -3 -910D-01 -1 -696D-03 -3247D-03 174D-01 -2702D-03
SAT-OIXD SAT-OIZD USERDRAG - CLKDI I DRIFT I SAT-OIX SAT-OIX SAT-OIY SAT-OIYD SAT-OIZD USERDRAG	637 .644 .486 174D-03 .107D-01 119D-02 USERDRAG 174D-03 .158D-03 .212D-03 .14D-03 .170D-03 .250D-01		-01 -03 -01 -02 -01 -01 -01 -01 -01 -02 -01 -02 -01 -02 -01 -02	-543 -130 -251 -251 -7212D-03 -528D-01 -176D-03 -176D-03 -119D-02 -176D-03 -154D-02 -280D-02 -202D-03 -550D-04	.10 .130 .4610-03 133 283 	- 01/ - 0133 - 0133 - 0133 - 010-0 - 010-0	- 251 - 263 - 263 - 263 - 263 - 263 - 265 - 263 - 265 - 265
SAT-01XD SAT-01YD SAT-01ZD USERDRAG - CLK01 I DRIFT I SAT-01X SAT-01X SAT-01Z SAT-01ZD SAT-01ZD SAT-01ZD SAT-01ZD SAT-01ZD USERDRAG CLK01 I	637 .644 .486 		-01 -03 -01 -02 -01 -02 -01 -02 -01 -02 -01 -02 -01 -02 -01 -02	.543 .130 .310 .251 .528D-03 .528D-01 176D-03 DRIFT 1 119D-02 	.100 .130 .4610-03 133 283 	- 00 / - 0133 - 0133 - 010-0 - 0133 - 010-0 - 0133 - 010-0 - 010-0	-251 -263 -263 -3 -910D-01 -696D-03 -3247D-03 -174D-01 -702D-03
SAT-01XD SAT-01YD SAT-01ZD USERDRAG - CLKB1 1 DRIFT 1 SAT-01X SAT-01Y SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD SAT-01YD	637 644 666 		-01 -03 -01 -02 -01 -01 -01 -01 -01 -01 -01 -01 -01 -01	.543 .130 .310 .251 .528D-01 .528D-01 .528D-01 .176D-03 DRIFY 1 1190-02 .176D-02 .176D-02 176D-02 .280D-02 .280D-02 .280D-02 .550D-04 .151D-01 .422D-02	.100 .130 .4610-03 133 283 	- 00 / - 0133 - 0133 - 0100-0 -	-251 -263 -263 -3 -910D-01 -1 -696D-03 -3247D-03

Figure A-10. SEA Version 4.1 Smoothed Error Budget at 1140 Minutes. Nominal Velocity Variance Rate Process Noise of 1 x 10-9 Meter2/ Second³

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	-		ERROR	8 BUDGET				
	SAT-01H VETERS	SAT-OLC METERS	SAT-01L METERS	RSS-PUS METERS	SAT-01HD HET/SEC	SAT-01CD MET/SEC	SAT-01LD MET/SEC	RSS-VEL MET/SEC 736D-06
GRAVCJEF	•557	.019	219	.862	7870-04	299D-03	.6430-03	•713D-03
LUMPED	-3.63	-7.24	-1.02	8.17	• 268D-02	•454D-02 811D-02	.4750-03 .394D-02	• 52 90-02 • 116D-01
MEASBI 1	-1-08	3600-01	6550-01	.101	2520-04	.1640-03	7570-04	.1820-03
MEASBE 2	.6700-01	.271	481	•555	+412D-03	134D-02 214D-03	-1930-03	-1410-02
MEASOI J Measol 4	107	109	-1.33	1.75	• 50 60 -0 3	.135D-02	-250D-03	-146D-02
MEASBI 5	3470-01	.205	113	.237	.108D-03	• 504D-04	.614D-04	-134D-03
MEASHI 6 Fohenedd	506D-01 350	d53 -5.18	•274 15•8	.898	1110-01	- 285D-02	7770-03	.115D-01
RS3	3.95	11.2	24.6	27.3	•136D-01	• 994D-02	•411D-02	.1730-01
	USERDRAG	CLKƏT I	DRIFT 1					
SULRAD 1	-5090-00 -	•275D-0J	4230-08					
GRAVCUEF	2930-06	1.56	107D-04 .359D-04					
ACCEL I	2970-05	16.7	3990-01					
MEASUE 1	1750-06	-15.2	2600-03					
MEASUL 2	8570-07	1.12	1550-04					
MEASUL +	1000-06	1.73	4520-04					
MEASBLO	2030-06	5.60	6750-04					
EPHEMER ?	1190-05	-90.5	•715D-04 •399D-01					
	S T A N D			- CORREL			· 0	AT-012D
	SAL-UIX	341-01	•	SAT-012		JAT-011	· .	
SAT-ULX	13.7	. 360		+ 9230-02	267		-01	.412
-SAL-012			10=0			612D	-01	.485D-01
SAT-OLKO	267	•120	0-01	. 345	•174D=01	•568 •6060	-02	390D-01
541-0175	412			.489D-01	340D-01		- uz	2890-01
USERDRAG	1500-04	-118	0-04	9240-05	.1070-04	•114D	-04	·2850-05
- <u>CLK31 1</u> -DRIFT 1			J-J2	-720D-02	2460-01	-1050	+02	
					-			
	JSE RD RAG	CLKBI	1 .	DRIFT I				
5A[-01X		.227	D-01		-			-
SAT-012	3240-05	. 623	0-02	.7200-02				
SAF-UIX) SAF-OIX)	.1070-04	415	D-02	2460-01				O A
SAT-ULZS	-28-D-15	1.38	D-02	3290-01		***		Ť ă
USENDAAU	-2570-31	•152	D-04	357D-05				T 5
DRIFT 1	3570-05	103		427D-02				d S
								OR IS
								Ø TI
	Figure A.	-11. SEA V	Version 4	1 Smoothed	Error Buda	et at		n li
	rigure A				JILOL Dudy	to Drogona		r 2
		1140	minutes.	verocity	variance Ra	Le Process		3
		Noise	e of l x l	.0 ^{-o} Meter2,	/Second 3			₹ 3

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TIME FRUM EPOCH IN MINUTES = 1140.

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RSS-VEL NET/SEC 0520-03 0520-03 12620-01 12620-01 12620-01 12620-03 12640-03 126600-03 126600-03 126000000000000000000000000000000000000		T-012D -526 -329 -329 -329 -329 -329-03 -159 -159 -159-03 -4520-03 -4520-03	
SAT-01LD MET/551 87123054 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-04 5870-04 5870-04 5870-04 5870-04 5870-04 5870-04 5870-04 5870-04 5870-03 58700-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 5870-03 58700-03 59700-03 59700-03 59700-03 59700-03 59700-03 59700-03 59700-03 59700-03 59700-03 59700-03 59700-03 597000000000000000000000000000000000000		S A 2 2 2 2 2 4 2 2 4 2 2 4 2 2 2 2 2 2 2	
SAT-01CD MET/SECD 		A T R T X SAT-01 C 4630 C 46300 C 4630 C 4630 C 46300 C 4630 C 46300 C 463000 C 46300 C 463000 C 463000 C 46300 C 463000 C 463000 C 463000 C 46300 C	:
SATT-01HD HEAT-01HD -1560 -1560 -1560 -1560 -1560 -1560 -1560 -1560 -1560 -1560 -1560 -1560 -160 -160 -160 -160 -160 -160 -160 -1		A T I D N M SAF-01XD - 24550-01 - 24550-01 - 2220-03 - 445 - 6240-02 - 5760-03	
RSS-POS HETERS -1300-01 -1300-01 -1300 -1300 -197 -197 -197 -197 -197 -197 -197 -197		- C G R H E L 5AT-012 5AT-012 -291 -1291 -1291 -1270-02 -1270-02 -1270-02	
SAT-01L METERS 	DRIFT 1 	017 017 446 446 446 446 446 446 446 446 446 44	10-05 10-02 10-02 10-05 10-05 10-05 10-05 10-04 000
JAT-01C METERS +2450-03 +2450-03 +12450 -150 +1340 +1340 +1340 -1340-01 -3540-01 -3540-01 -3540-01 -3540-01	CLKHI 1 6780-01 6780-01 		
SAT-01H SAT-01H -11105-01 -11105-01 -3430 -3430-02 -4230-02 -7710-01 -7710-01 -247 -247 -247 -247 -247 -2110-01 -247 -247 -91	USERDAAG .2830-02 .1430-02 .47890-02 .4460-02 .1440-02 .1440-02 .1440-02 .1440-02 .3210-03 .3210-03 .3210-01	S T A N D S AT - 01X - 421 - 421 - 731 - 731 - 526 - 15540 - 15540 - 1290-02	
506.440 444VCJEF 444VCJEF 400000 40000 464301 464301 464301 464301 464300 464300 464300 464300 464300 464300 464300 464300 464300 464300 464300 464300 464300 464300 464300 46430000000000	501 443 1 544 435 1 544 401 5 104 7 104 7 104 7 104 7 10 104 7 10 10 10 10 10 10 10 10 10 10 10 10 10	SAT-01X SAT-01X SAT-01X SAT-01X SAT-01X SAT-01X CVKRU20 CVKV CVKVCVKU20 CVKVCVX CVKVCVX CVKVCVX CVKVX CVX CVX CVX CVX CVX CVX CVX CVX CVX C	541-01X 541-01X 541-01X 541-01X 541-01X 541-01X 541-01X 541-01X 541-11 11 11

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SEA Version 4.1 Smoothed Error Budget at 1140 Minutes. Velocity Variance Rate Process Noise of 1 x 10^{-12} Meter²/Second³

Figure A-12.

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increase in measurement error (TDAS ephemeris error and others) as the process noise increases (Figure A-10, A-11, and A-12), should be noted.

A.4 CONCLUSIONS

The following conclusions can be drawn from the series of tests performed:

• The SEA smoother/TDAS enhancements were implemented successfully. The only major errors uncovered were those process noise errors described in Section A.3.2.

• The SEA smoother/TDAS capabilility is now fully validated and ready for use.

• The close agreement between the process-noise-free SEA smoother results and the batch ORAN results verifies that SEA now also has the error analysis capability for a batch orbit determination process. Because SEA is a wellstructured, well-documented, and easily enhanced program, it can be easily modified to analyze new tracking systems and data types, whether these are used in a sequential or batch orbit determination mode.

One of the limitations of a smoother (or a smoother error analysis program) is that, for discrete time measurements, smoothed states (or smoother errors) are only available at those measurement times peculiar to the tracking scenario. This means that the smoother results will not be output during data gaps between tracking passes. Smoother output from SEA during data gaps can be obtained by entering fictitious measurements at the desired output times. These artificially introduced, fictitious measurements are given large standard deviations so that they do not affect the error analysis accuracy.

A.5 LISTING OF TEST DECK SETUPS

The following pages contain listings of representative deck setups used in the validation and verification of the SEA smoother/TDAS capabilities.

//ZBPAP1T1 JOB (GC002,311H,FFF), 'SEA P1S1T1', MSGLEVEL=(1,1), MSGCLASS=A, TIME=30, CLASS=C, NOTIFY=ZBPAP 11 /*JOBPARM LINES=30 /*ROUTE PRINT PRTSS //*MEMBER P1S1T1 DATA IN TESTPAN LIBRARY //*DIRECT TRACKING OF A 200-KM 28 DEG INC S/C, W/DRAG A SOLVE-FOR //*RANGE AND RANGE RATE MEASUREMENTS EVERY 180 0 SECONDS //*DETERMIN TRACKING SCHEDULE, FOR 13 TRACKING STATIONS, FOR 24 HRS //*USING SMTHDU5M SEA SMOOTHER/TDAS UPDATES, SEA VER 4 1 KEYWORDS //*WITH SMOOTHING //STEP1 EXEC PGM=PAN#1, REGION=300K, COND=(1, LE) //PANDD1 DD DSN=GCDEV.MVT SEA.PANLIB DATA, UNIT=DISK, DISP=SHR DD DSN=&&SEAUPD, UNIT=VID, SPACE=(CYL, (2, 1), RLSE), //PANDD2 DISP=(NEW, PASS), DCB=(RECFM=FB, LRECL=80, BLKSIZE=3600) 11 //SYSPRINT DD SYSOUT=* //SYSPUNCH DD DUMMY //SYSIN DD DSN=ZBPAP SMTHDU5M DATA, UNIT=DISK, DISP=SHR EXEC FORTRANH, PARM='XREF' //SYSLIN DD SPACE=(CYL.(2.1)) //SOURCE.SYSTERM DD DUMMY //SOURCE.SYSPRINT DD DUMMY //SYSIN DD DSN=&&SEAUPD, UNIT=VIO, DISP=(OLD, DELETE) EXEC LINK, PARM= 'LET, LIST, MAP, SIZE=(200K, 20K) ', REGION=250K //SYSLIB DD DSN=SYS2 FORTLIB, DISP=SHR DD DSN=GCDEV SEAMVS LOAD, DISP=SHR 11 //SYSPRINT DD SYSOUT=* //SYSUT1 DD SPACE=(TRK, (55, 1, 1)) //SYSLIN DD DD * 1 INCLUDE SYSLIB(SEA) ENTRY MAIN //GD EXEC PGM=GSFC, REGION=400K //STEPLIB DD DSN=&&LODMOD, DISP=(OLD, DELETE) //FT01F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404) SPACE=(CYL, (5, 1)) SORTING FOR TRACKING DATA SCHEDULE 11 //FT02F001 DD UNIT=DISK.DCB=(RÉCFM=VBS,LRECL=44,BLKSIZE=4404), // SPACE=(CYL,(1,1)) MERGING FOR TRACKING DATA SCHEDULE //FT03F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404, BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1)) 11 DSN=&&SORTRK SORTED TRACKING DATA SCHEDULE 11 //FTOSFOO1 DD DDNAME=DATAS TRACKING SCHEDULE CARD INPUT //*FT06F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=3990), //FTO6F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=141), SPACE=(CYL, (3, 1), RLSE), 11 SEA PRINTER OUTPUT DSN=&&PRTOUT 11 //*FT08F001 DD DDNAME=INPCRD SEA KEYWORD CARD INPUT //*INPCRD DD * //FT08F001 DD * SEA KEYWORD CARD INPUT EPOCHTIM O 99 861101 00000 0000 USERSATO 6578140. 1 11 1 0 0001 28.8 USERSATO 1 12 1 0 n 0 SATELITE 2 11 42166750. 0.0004 50 0 SATELITE 2 12 0 358 0 0 3 11 SATELITE 42163592 42 0 0004 5.0 0 228 SATELITE 3 12 0 0 0 STATIONS 323003.857 1 0 0 2532329 162 1441 37 2430737 214 STATIONS 2 0 0 352029.642 0 913310D+03 2430735 042 STATIONS 3 0 0 352029 642 0 918710D+03 283029.905 STATIONS 5 0 0 2791826.183 -0 558200D+02 STATIONS 6 0 0 -075717.371 3454022.570 0 528370D+03 2952031 937 -0 337500D+02 STATIONS 8 0 0 322105 001 STATIONS 11 0 0 220734.461 2002005 439 0 113975D+04 2791823 853 2430735 561 STATIONS 12 0 0 283029.774 -0 544500D+02 STATIONS 13 0 0 352031.937 0 912710D+03 STATIONS 4 0 0 402719.656 3554953.596 0 8089900+03 -330903.596 0 706610D+03 7 STATIONS 0 0 2892001 065 STATIONS 0 385954 656 2830926 161 -0 250000D+01 9 0 131838.265 1444412 524 0 115950D+03 STATIONS 10 0 0 EARTH 15 15 150 0 SPCPARAM 0 0 0.00272 20 1 EBOUTPUT -99 30 0 30 0 2 1440 0 CLKBIAS 1000000 1 1 CLKDRIFT 200 0 0 000001 1 1

USERDRAG 1 1 0 1 -1 0.25 GRAVCOEF /* DD UNIT=DISK, DSN=ZBBTF ZBEXS.GEM DATA(RECOEF2), DISP=SHR 11 DD * 11 SATSOLPR 1 -1 MEASBIAS 200000010002. 10.0 2 -1 1300000010013. MEASBIAS 3 -1 001 MEASBIAS -1 1000000010000. 10 0 2 .001 MEASBIAS 3 -1 1000000010000 MEASBIAS -1 500000010000. 10 0 2 MEASBIAS - 1 1200000010000 .001 3 EPHEMERR 1 25.0 23 0 40 0 EPHERROR 99 . 11574 CLKACCEL 1 -1 COVARANC 1 2.5D+05 2.5D+05 2 5D+05 1.0D+00 1 0D+00 1 0D+00 NOISECOV 0 1 1 Ο. 0 1 00000D-10 1.00000D-10 1 00000D-10 0 /* //*FT09F001 DD SYSOUT=*.DCB=(RECFM=VBA.LRECL=137.BLKSIZE=3990). //FT09F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141), 11 SPACE=(CYL, (2, 1), RLSE); 11 DSN=&&NOMOUT SATELLITE NOMINAL TRAJECTORY OUTPUT //*FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=3990), //FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141). 11 SPACE=(CYL, (2, 1), RLSE), 11 DSN=&&MEASOUT PROCESSED MEASUREMENTS PRINTER OUTPUT //FT20F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1,1)), 11 DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK, 11 SEQUENTIAL ERROR BUDGET SUMMARY DSN=&&FESUM //FT21F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1, 1)) DCB=(RECFM=VBS,LRECL=144,BLKSIZE=2884),UNIT=DISK, DSN=&&SESUM BACKWARD SMOOTHER ERROR BUDGET SUMMARY 11 11 //FT27F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=196,BLKSIZE=1964, BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1,1)) 11 VISIBLE TRACKING DATA SCHEDULE 11 DSN=&&AKKHIN //FT40F001 DD UNIT=DISK, DCB=(RECFM=FB, LRECL=1688, BLKSIZE=18568), DISP=(NEW, DELETE), SPACE=(CYL, (2, 1), RLSE), 11 DSN=&&SMSTOR SMOOTHER INFORMATION STORAGE FILE 11 //GO SYSUDUMP DD DUMMY //*SYSUDUMP DD SYSOUT=*, SPACE=(TRK, 1), DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922) //* //GO DATA5 DD * 86110100000 0000 3 - 1 100020001 3 1800.0 10000.0 1440.0 0 00 100030001 1800.0 3 10000 0 1440.0 0 00 10000002 1800.0 2 1.5 1440 0 0 00 20000001 2 20 0 1 5 640 O 732.0 638 0 733 0 20000001 3 20 0 0 002 640 O 638 0 732 0 733.0 30000001 2 20.0 1.5 732.0 638 0 640 O 733 0 300000001 20 0 0 002 3 638.0 640 0 732 0 733 0 50000001 2 20 0 1.5 459.0 365 0 369 0 463 0 556 0 646.0 649 0 552.0 0 002 500000001 3 20.0 459 0 365 0 369.0 463 0 552 0 556 0 646 0 649 0 60000001 2 20 0 1 5 668 O 665 0

600000001	3	20 0	0 002	
665 0	668 0			
70000001	2	600 0	15	
1200 0	1440.0			
70000001	3	600 0	0.002	
0.00	240 0			
80000001	2	20.0	15	
369 0	373.0		462 0	466 0
556 0	559 0			
80000001	3	20.0	0 002	
369 0	373.0		462.0	466 0
556 0	559 0			
1100000001	2	20 0	1.5	
627 0	631.0		721.0	724 0
815.0	817 0			
1100000001	3	20 0	0 002	
627.0	631 0		721 0	724 0
815 0	817 O			
1200000001	2	20 0	15	
365 0	369 0		459 0	463 O
552 0	556 O		646 0	649 0
1200000001	3	20 0	0 002	
365 0	369 0		459 0	463 0
552.0	556 O		646 0	649 O
1300000001	2	20 0	1.5	
638.0	640 0		732 0	733 0
_				
1300000001	3	20 0	0 002	
638 Q	640 0		732 0	733 0

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/* //NTSO EXEC PGM=NOTIFY,COND=EVEN //

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.//ZBPAP2T1 JOB (GCOO2,311H,FFF), 'SEA P1S2T1', TIME=30,
            MSGCLASS=X, MSGLEVEL=(1,1), NOTIFY=ZBPAP, CLASS=C
11
/*JOBPARM LINES=30
//*ROUTE PRINT RMT6
//*MEMBER P1S2T1.DATA IN TESTPAN LIBRARY
//*6 GPS'S TRACKING A 400-KM 57 DEG INC S/C,
//*RANGE AND RANGE RATE MEASUREMENTS EVERY 300 0 SECONDS
 //*USING SMTHDU5M SEA SMOOTHER/TDAS UPDATES, SEA VER 4 1 KEYWORDS
//*WITH SMOOTHING
//STEP1 EXEC PGM=PAN#1, REGION=300K, COND=(1, LE)
//PANDD1 DD DSN=GCDEV.MVT.SEA PANLIB DATA, UNIT=DISK, DISP=SHR
            DD DSN=&&SEAUPD, UNIT=VIO, SPACE=(CYL, (2, 1), RLSE),
 //PANDD2
               DISP=(NEW, PASS), DCB=(RECFM=FB, LRECL=80, BLKSIZE=3600)
//SYSPRINT DD SYSOUT=*
//SYSPUNCH DD DUMMY
//SYSIN DD DSN=ZBPAP.SMTHDU5M DATA,UNIT=DISK,DISP=SHR
       EXEC FORTRANH, PARM= 'XREF'
//SYSLIN DD SPACE=(CYL,(2,1))
//SOURCE.SYSTERM DD DUMMY
//SOURCE.SYSPRINT DD DUMMY
//SYSIN DD DSN=&&SEAUPD.UNIT=VIO.DISP=(OLD.DELETE)
       EXEC LINK, PARM= 'LET, LIST, MAP, SIZE= (200K, 20K) ', REGION=250K
11
//SYSLIB DD DSN=SYS2.FORTLIB, DISP=SHR
          DD DSN=GCDEV.SEAMVS.LOAD,DISP=SHR
11
//SYSPRINT DD DUMMY
//SYSUT1 DD SPACE=(TRK, (55, 1, 1))
//SYSLIN DD
         DD *
11
 INCLUDE SYSLIB(SEA)
 ENTRY MAIN
 //GO EXEC PGM=GSFC, REGION=400K
//STEPLIB DD DSN=&&LODMOD, DISP=(OLD, DELETE)
//FTO1FO01 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404)
               SPACE=(CYL, (5, 1)) SORTING FOR TRACKING DATA SCHEDULE
//FT02F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404),
               SPACE=(CYL, (1, 1)) MERGING FOR TRACKING DATA SCHEDULE
 //
//FT03F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404,
               BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1))
11
               DSN=&&SORTRK
                                   SORTED TRACKING DATA SCHEDULE
11
//FT05F001 DD DDNAME=DATA5
                                   TRACKING SCHEDULE CARD INPUT
//*FT06F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=3990),
//FT06F001 DD SYSOUT **, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141),
               SPACE=(CYL, (3, 1), RLSE),
//
                                   SEA PRINTER OUTPUT
               DSN=&&PRTOUT
11
//*FT08F001 DD DDNAME=INPCRD
                                    SEA KEYWORD CARD INPUT
//*INPCRD DD *
 //FT08F001 DD *
                                   SEA KEYWORD CARD INPUT
                                           000000.0000
EPOCHTIM 2 1 -9
                     860101.
USERSATO 1 11 1
                     6978140.
                                           0.0005
                                                                57.0
USERSATO
           1 12
                 1
                     0.
                                           0.
                                                                0
SATELITE 2 11
                     26560123.0
                                           .001
                                                                63.0
SATELITE 2 12
                      120.0
                                           0.0
                                                                100 0
SATELITE 3 11
SATELITE 3 12
                     26580123.0
                                           .001
                                                                63.0
                      120.0
                                           0 0
                                                                140.0
                                           .001
SATELITE
          4 11
                     26560123.0
                                                                63.0
SATELITE
          4 12
                      120.0
                                           00
                                                                180 0
SATELITE
          5 11
                     26560123.0
                                           .001
                                                                63 0
SATELITE
          5 12
                     240.0
                                           0 0
                                                                60 0
SATELITE
          6 11
                     26560123 0
                                            001
                                                                63.0
SATELITE
          6 12
                     240.0
                                           00
                                                                100 0
          7 11
SATELITE
                     26560123.0
                                            001
                                                                63 0
SATELITE 7 12
                     240.0
                                                                140.0
                                           0.0
EARTH
              4
                 0
           4
                      .0
SPCPARAM 1
              0
                 0
                      .0117618
                                           .0
                                                                2 0
GRAVCOEF O 0 -1
                      1.0
                                                                 0
                                           . 0
/*
    DD DSN=ZBBTF.ZBEXS.GEM.DATA(RECDEF4),DISP=SHR,UNIT=DISK
11
    DD *
//
                     0.25
USERDRAG
              0 -1
         1
CLKBIAS
              0
                      10000
           1
                1
CLKDRIFT
              0
                      10000
           1
                 1
CLKACCEL
              0 -1
                      .0001
           1
MEASBIAS 2
                -1
                     200010000.
                                           5.0
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MEASBIAS
                      300010000.
                                            50
          2
                -1
                -1
MEASBIAS
          2
                      400010000
                                            5 0
MEASBIAS
                      500010000
                                            50
          2
                -1
          2
                      600010000
MEASBIAS
                                            5.0
                - 1
MEASBIAS
           2
                -1
                      700010000
                                            50
                      200010000 0
MEASBIAS
          3
                - 1
                                            .001
MEASBIAS
          З
                -1
                      300010000 0
                                            .001
MEASBIAS
          3
                      400010000 0
                -1
                                             001
MEASBIAS
          3
                -1
                      500010000.0
                                            .001
                -1
MEASBIAS
          3
                      600010000.0
                                             001
                -1
                      700010000.0
MEASBIAS
          3
                                            .001
EPHEMERR
           1
              0
                 0
                      10 0
                                            10.0
                                                                  20 0
EPHERROR
                 0
                                                                   0
          0
              0
                      99.0
                                            . 0
EBOUTPUT
          0 99
                 2
                      1440.0
                                            30 0
                                                                  30 0
COVARANC
              0
                 0
           1
100000.0
             100000 0
                          100000 0
                                         1.0
                                                      1 0
                                                                   1 0
NOISECOV
           1
                 0
              1
                                         1 00000D-10 1.00000D-10 1.00000D-10
      0
                   0.
                                 0
/*
/*
//*FT09F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=3990),
//FTO9F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141),
11
               SPACE=(CYL,(2,1),RLSE),
                                    SATELLITE NOMINAL TRAJECTORY OUTPUT
11
               DSN=&&NOMOUT
//*FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=3990),
//FT10F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=141),
               SPACE=(CYL, (2, 1), RLSE)
17
               DSN=&&MEASOUT
                                    PROCESSED MEASUREMENTS PRINTER OUTPUT
11
//FT20F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1, 1)),
               DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK,
11
                                    SEQUENTIAL ERROR BUDGET SUMMARY
11
               DSN=&&FESUM
//FT21F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1, 1)),
               DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK,
11
                                    BACKWARD SMOOTHER ERROR BUDGET SUMMARY
11
               DSN=&&SESUM
//FT27F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=196, BLKSIZE=1964,
               BUFNO=1),DISP=(NEW,PASS),SPACE=(CYL,(1,1)),
DSN=&&AKKHIN VISIBLE TRACKING DATA SCHEDULE
11
11
//FT40F001 DD UNIT=DISK, DCB=(RECFM=FB, LRECL=1688, BLKSIZE=18568),
               DISP=(NEW, DELETE), SPACE=(CYL, (2, 1), RLSE)
11
               DSN=&&SMSTOR
                                    SMOOTHER INFORMATION STORAGE FILE
11
//GO SYSUDUMP DD DUMMY
//*SYSUDUMP DD SYSOUT=*, SPACE=(TRK, 1),
                DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922)
//*
//GO.DATA5 DD *
                      85010100000.0000
                                                                           -1
          3
       20001
                     2
                        300.0
                                      1.0
0 00
                 1440.0
       20001
                        300 0
                                      0.001
                     3
0.00
                 1440 0
       30001
                     2
                        300.0
                                      1.0
0.00
                 1440.0
       30001
                     3
                        300.0
                                      0.001
0.00
                 1440.0
       40001
                        300.0
                                      1.0
                    2
0.00
                 1440.0
        40001
                        300 0
                                      0.001
                     3
                 1440 0
0.00
       50001
                    2
                        300.0
                                      1 0
                1440.0
0.00
       50001
                     3
                        300.0
                                      0.001
0.00
                 1440.0
                        300 0
       60001
                     2
                                      1 0
0.00
                 1440.0
                                      0 001
       60001
                        300.0
                    3
0 00
                 1440.0
       70001
                       300.0
                                       1.0
                    2
0 00
                 1440 0
       70001
                    3 300.0
                                      0.001
                1440.0
0.00
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//NTSO EXEC PGM=NOTIFY, COND=EVEN //

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//ZBPAP3T1 JOB (GC002 311H, FFF), 'SEA P1S3T1', MSGLEVEL=(1,1), MSGCLASS=X, TIME=30, CLASS=C, NOTIFY=ZBPAP 11 /*JOBPARM LINES=40 //*ROUTE PRINT PRTSS //*MEMBER P1S3T1.DATA IN TESTPAN LIBRARY //*TDRSS TRACKING OF A 600-KM 98 DEG INC S/C //*RANGE AND RANGE RATE MEASUREMENTS EVERY 180 0 SECONDS //*USING SMTHDU5M SEA SMOOTHER/TDAS UPDATES, SEA VER 4.1 KEYWORDS //*WITH SMOOTHING //STEP1 EXEC PGM=PAN#1, REGION=300K, COND=(1, LE) //PANDD1 DD DSN=GCDEV MVT SEA PANLIB DATA, UNIT=DISK, DISP=SHR //PANDD2 DD DSN=&&SEAUPD, UNIT=VIO, SPACE=(CYL, (2, 1), RLSE), DISP=(NEW, PASS), DCB=(RECFM=FB, LRECL=80, BLKSIZE=3600) 11 //SYSPRINT DD SYSOUT=* //SYSPUNCH DD DUMMY //SYSIN DD DSN=ZBPAP SMTHDU5M DATA, UNIT=DISK, DISP=SHR EXEC FORTRANH, PARM='XREF' 11 //SYSLIN DD SPACE=(CYL,(2,1)) //SOURCE.SYSTERM DD DUMMY //SOURCE.SYSPRINT DD DUMMY //SYSIN DD DSN=&&SEAUPD, UNIT=VID, DISP=(OLD, DELETE) EXEC LINK, PARM= 'LET, LIST, MAP, SIZE= (200K, 20K) ', REGION=250K 11 //SYSLIB DD DSN=SYS2 FORTLIB, DISP=SHR DD DSN=GCDEV.SEAMVS.LOAD,DISP=SHR 11 //SYSPRINT DD SYSOUT=* //SYSUT1 DD SPACE=(TRK, (55,1,1)) //SYSLIN DD 11 DD * INCLUDE SYSLIB(SEA) ENTRY MAIN //GO EXEC PGM=GSFC, REGION=400K //STEPLIB DD DSN=&&LODMOD,DISP=(OLD,DELETE) //FT01F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=44,BLKSIZE=4404) SPACE=(CYL, (5, 1)) SORTING FOR TRACKING DATA SCHEDULE 11 //FT02F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44; BLKSIZE=4404) // SPACE=(CYL,(1,1)) MERGING FOR TRACKING DATA SCHEDULE //FT03F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=44,BLKSIZE=4404, BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1)) 11 SORTED TRACKING DATA SCHEDULE DSN=&&SORTRK 11 //FTO5FOO1 DD DDNAME=DATA5 TRACKING SCHEDULE CARD INPUT //*FT06F001 DD SYSOUT=*.DCB=(RECFM=VBA.LRECL=137.BLKSIZE=3990). //FTO6FO01 DD SYSOUT==, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141), SPACE=(CYL,(3,1),RLSE), DSN=&&PRTOUT SEA PRINTER OUTPUT 11 11 //*FT08F001 DD DDNAME=INPCRD SEA KEYWORD CARD INPUT //*INPCRD DD * //FT08F001 DD * SEA KEYWORD CARD INPUT EPOCHTIM 99 851101. 00000.0000 1 USERSATO 1 11 6978140. 0.0001 98 8 1 USERSATO 1 12 0 0 0 1 6778140. SATELITE 2 11 0.0017 28 1 SATELITE 160 0 2 12 1 0 ٥ SATELITE 3 11 42166750. 0004 5.0 0 0 3 12 358 SATELITE 0 0 0 SATELITE 4 11 0 42163592.42 0 0004 50 SATELITE 4 12 0 228 0 0 42163592 42 0 0004 5 0 SATELITE 5 11 Ω SATELITE 5 12 0 113 0. 0 STATIONS 323003 857 2532329.162 1441 37 0 0 1 STATIONS 0 0 385953.936 2830929 141 0 40000D+01 3 STATIONS 0 402719 656 3554953.596 0 8089900+03 4 0 STATIONS -075717 371 6 0 0 3454022.570 0 528370D+03 0 -330903.596 0 706610D+03 STATIONS 7 0 2892001.065 -0.337500D+02 STATIONS 0 0 322105 001 8 2952031 937 STATIONS 10 0 0 131838 265 1444412 524 0 115950D+03 STATIONS 11 0 0 220734 461 2002005 439 0 113975D+04 -0 544500D+02 STATIONS 12 0 0 283029.774 2791823 853 STATIONS 13 0 0 352031 937 2430735 561 0.912710D+03 150 0 EARTH SPCPARAM 0 1 0 0 0011765 2 0 2.0 -99 1020 0 30 0 30.0 EBOUTPUT 2 MEASRMNT 1020 CLKBIAS 1000000 1 1

200 0 0 000001 CLKDRIFT 1 1 USERDRAG 0 1 1 1 GRAVCOEF -1 0 25 /* 11 DD UNIT=DISK.DSN=ZBBTF.ZBEXS.GEM DATA(RECOEF2).DISP=SHR // SATSOLPR 1 - 1 . 1 MEASBIAS 1000300010000. 0 00001 2 -1 MEASBIAS 600000010000 10.0 2 - 1 MEASBIAS 3 1000000010000. 001 1 MEASBIAS 2 700000020000. 10 0 - 1 -1 MEASBIAS 3 300000020000. 001 EPHEMERR 25.0 23.0 40.0 1 EPHERROR 99. CLKACCEL .11574 1 -1 COVARANC 1 1.0D+05 1 0D+05 1.0D+05 1 0D+00 1 0D+00 1 0D + 00COVARANC 2 1 1 0D+06 1 OD-06 0 0 0. 0 Ο. 1 0D+06 Ο. 0. 5 0D-01 1 0D-06 ٥. 0 1.0D+06 1.0D-06 0 1 OD-06 0 0 1 0D-06 5.0D+00 0 5 OD-09 0. 5 0D-01 5 0D+00 5 OD-09 Ο. Ο. 1 OD-06 1 0D-06 1 0D-06 5 OD-09 5 OD-09 5 0D+00 NOISECOV 1 0 1 0 0 0 1 00000D-10 1 00000D-10 1.00000D-10 NOISECOV 2 0 1 1 00000D-12 1.00000D-12 1.00000D-12 0 0 0 /* //*FT09F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=3990), //FT09F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141), SPACE=(CYL, (2, 1), RLSE) 11 - DSN=&&NOMOUT SATELLITE NOMINAL TRAJECTORY OUTPUT 11 //*FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=3990), //FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141), SPACE=(CYL, (2, 1), RLSE) 11 11 DSN=&&MEASOUT PROCESSED MEASUREMENTS PRINTER OUTPUT //FT20F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1, 1)), DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK 11 11 DSN=&&FESUM SEQUENTIAL ERROR BUDGET SUMMARY //FT21F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1,1)), // DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK, 11 DSN=&&SESUM BACKWARD SMOOTHER ERROR BUDGET SUMMARY //FT27F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=196, BLKSIZE=1964, 11 BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1)) 11 DSN=&&AKKHIN VISIBLE TRACKING DATA SCHEDULE //FT40F001 DD UNIT=DISK, DCB=(RECFM=FB, LRECL=1688, BLKSIZE=18568), 11 DISP*(NEW, DELETE), SPACE=(CYL, (2, 1), RLSE) 11 DSN=&&SMSTOR SMOOTHER INFORMATION STORAGE FILE //GO SYSUDUMP DD DUMMY //*SYSUDUMP DD SYSOUT=*.SPACE=(TRK.1). DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922) 1/* //GO.DATA5 DD * 86110100000.0000 3 - 1 100030001 2 180.0 30.0 1440 0 0 00 100030001 3 180 0 0.01 0 00 1440 0 100040001 2 180 0 30 0 1440 0 0.00 3 100040001 180 0 0.01 0 00 1440 0 1000400050002 2 180.0 30 0 120.0 0.00 10000002 2 60.0 1.5 30 0 39.0 1122.0 1128 0 1218.0 1227.0 1317 0 1323 0 3 0 002 10000002 60.0 30 0 39.0 1122 0 1128 0 1317 0 1323 0 1218 0 1227 0 30000002 2 60 O 1 5

1128 0	1134.0		1032.0	1038 0
300000002 1032.0	3 1038.0	60 0	0 002 1128.0	1134 0
40000002 852.0	2 861.0	60 0	1.5	
40000002	3	60.0	0 002	
600000002 354.0 552.0 1344.0	2 363.0 558 0 1350 0	60 0	1 5 453 0 1245 0	462 O 1254.0
600000002 354 0 552 0 1344 0	3 363 0 558.0 1350.0	60.0	0 002 453.0 1245 0	462 0 1254 0
70000002 237.0 435.0	2 255 0 447 0	60.0	1.5 339 0 534 0	348.0 543 0
70000002 237.0 435.0	3 255 0 447 0	60 0	0 002 339 0 534 0	348 O 543 O
800000002 936.0 1131 0	2 942 0 1140.0	60 0	1 5 1032 0 1230 0	1041 0 1236 0
80000002 936 0 1131.0	3 942 0 1140.0	60.0	0.002 1032 0 1230 0	1041 0 1236 0
90000002 50 0	2 30,0	180.0	15	
1000000002 3 00 201 0 399.0 594 0	2 12 0 207 0 405 0 503.0	60.0	1.5 102 0 300.0 495.0 1389 0	111 0 306 0 504 0 1395 0
100000002 3.00 201.0 399 0 594.0	3 12 0 207.0 405.0 503.0	60.0	0 002 102 0 300.0 495 0 1389 0	111 0 306.0 504 0 1395.0
100000002 18 0 213 0 1206.0 1401 0	2 27.0 225.0 1212.0 1410 0	60.0	1.5 114 0 312 0 1305 0	126 0 321 0 1311 0
1100000002 18.0 213 0 1206 0 1401 0	3 27 0 225 0 1212 0 1410.0	60.0	0.002 114 0 312 0 1305 0	126 0 321 0 1311 0
1200000002 933 0 1028.0 1323 0	939 0 1034.0 1329 0	60.0	1 5 1029 0 1224 0	1038 0 1233 0
1200000002 933 0 1028.0 1323 0	3 939.0 1034.0 1329.0	60.0	0.002 1029.0 1224 0	1038 0 1233 0
1300000002 27 0 1314 0	2 36 0 1320.0	60 0	1 5 1218.0 1413 0	1224 O 1419 O
1300000002 27 0 1314 0	3 360 1320.0	60 0	0 002 1218 0 1413 0	1224 O 1419 O

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/* //NTSO EXEC PGM=NOTIFY,COND=EVEN //

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//ZBPAP4T1 JOB (GCO02,311H,FFF), 'SEA P1S4T1',
            MSGCLASS=X, TIME=30, MSGLEVEL=(1,1), NOTIFY=ZBPAP, CLASS=C
11
/*JOBPARM LINES=30
//*ROUTE PRINT RMT6
//*MEMBER P1S4T1 DATA IN TESTPAN LIBRARY
//*USING SMTHDU5M SMOOTHER/TDAS UPDATES, SEA VER 4 1 KEYWORDS
//*TDAS TRACKING SCENARID, CONTINUOUS BEACON TRACKING
//STEP1 EXEC PGM=PAN#1,REGION=300K,COND=(1,LE)
//PANDD1 DD DSN=GCDEV MVT SEA PANLIB DATA, UNIT=DISK, DISP=SHR
//PANDD2
           DD DSN=&&SEAUPD, UNIT=VIO, SPACE=(CYL, (2, 1), RLSE),
               DISP=(NEW, PASS), DCB=(RECFM=FB, LRECL=80, BLKSIZE=3600)
11
//SYSPRINT DD SYSOUT=*
//SYSPUNCH DD DUMMY
//SYSIN DD DSN=ZBPAP SMTHDU5M DATA, UNIT=DISK, DISP=SHR
      EXEC FORTRANH, PARM='XREF'
11
//SYSLIN DD SPACE=(CYL,(2,1))
//SOURCE SYSTERM DD DUMMY
//SOURCE SYSPRINT DD DUMMY
//SYSIN DD DSN=&&SEAUPD, UNIT=VIO, DISP=(OLD, DELETE)
// EXEC LINK, PARM='LET, LIST, MAP, SIZE=(200K, 20K)', REGION=250K
//SYSLIB DD DSN=SYS2 FORTLIB, DISP=SHR
         DD DSN=GCDEV SEAMVS LOAD, DISP=SHR
11
//SYSPRINT DD SYSOUT=*
//SYSUT1 DD SPACE=(TRK, (55, 1, 1))
//SYSLIN DD
         DD *
11
 INCLUDE SYSLIB(SEA)
 ENTRY MAIN
//GO EXEC PGM=GSFC, REGION=400K
//STEPLIB DD DSN=&&LODMOD, DISP=(OLD, DELETE)
//FT01F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=44,BLKSIZE=4404)
               SPACE=(CYL, (5, 1)) SORTING FOR TRACKING DATA SCHEDULE
11
//FT02F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=44,BLKSIZE=4404),
               SPACE=(CYL,(1,1)) MERGING FOR TRACKING DATA SCHEDULE
11
//FT03F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404,
               BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1)),
11
11
               DSN=&&SORTRK
                                   SORTED TRACKING DATA SCHEDULE
//FTOSFOO1 DD DDNAME=DATA5
                                   TRACKING SCHEDULE CARD INPUT
//*FT06F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=3990),
//FT06F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=141),
               SPACE=(CYL, (3, 1), RLSE),
11
                                   SEA PRINTER OUTPUT
11
               DSN=&&PRTOUT
//*FT08F001 DD DDNAME=INPCRD
                                    SEA KEYWORD CARD INPUT
//*INPCRD DD *
//FT08F001 DD *
                                   SEA KEYWORD CARD INPUT
EPOCHTIM 3
                     840805
                                           120000 0000
                 1
USERSATO
          1 11
                 1
                     6681144
                                           0 00078765
                                                               57 01940796
USERSATO
          1 12
                      96 4218
                                           360
                 1
                                                                0
SATELITE
                     42166750
                                         0 0004
                                                               50
          2 11
                 0
SATELITE
          2 12
                 0
                     360
                                         160
                                                               292
SATELITE
          3 11
                 0
                     42163592 42
                                         0 0004
                                                                5 0
          3 12
SATELITE
                                                               22
                 0
                     240
                                         60
SATELITE
          4 11
                     42163592 42
                                         0 0004
                                                               50
                 0
SATELITE
         4 12
                 0
                                         60
                                                                292
                     240
EARTH
          15 15
                                                                150 0
SPCPARAM
                          0 00214
             0
                 0
                                                                22
         1
                     323003 857
STATIONS
          1
             0 0
                                           2532329 162
                                                                 1441 37
GRAVCOEF
                -1
     DD UNIT=DISK, DSN=ZBBTF ZBEXS GEM DATA(RECOEF), DISP=SHR
11
     DD *
USERDRAG
          1
                 1
                        1.
                       1000
CLKDRIFT
          1
                 1
CLKACCEL
                - 1
                      0 12
SATSOLPR
                - 1
                       1.
          1
EPHEMERR
           1
                          10 0
                                              20 0
                                                                     50 0
EPHERROR
                  99
EBOUTPUT
              1 2
                        1320
                                          10
                                                                10
COVARANC
          1
     1 0D+06
                  1 0D+06
                                            1 0D+00
                                                         1 OD+00
                               1 0D+06
                                                                      1 00+00
NOISECOV
          1
              1
                 0
                   0
                                0
                                       1 00000D-10 1 00000D-10 1 00000D-10
      0
/*
//*FT09F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=3990),
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//FT09F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141). 11 SPACE=(CYL, (2, 1), RLSE), DSN=&&NOMOUT SATELLITE NOMINAL TRAJECTORY OUTPUT 11 //*FT10F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=3990), //FT10F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=141), SPACE=(CYL, (2, 1), RLSE), 11 11 DSN=&&MEASOUT PROCESSED MEASUREMENTS PRINTER OUTPUT //FT20F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1, 1)), 11 DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK, DSN=&&FESUM SEQUENTIAL ERROR BUDGET SUMMARY 11 //FT21F001 DD DISP=(NEW,PASS),SPACE=(CYL,(1,1)), // DCB=(RECFM=VBS,LRECL=144,BLKSIZE=2884),UNIT=DISK. 11 DSN=&&SESUM BACKWARD SMOOTHER ERROR BUDGET SUMMARY //FT27F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=196,BLKSIZE=1964, BUFND=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1)), DSN=&&AKKHIN VISIBLE TRACKING DATA SCHEDULE 11 11 //FT40F001 DD UNIT=DISK, DCB=(RECFM=FB, LRECL=1688, BLKSIZE=18568), DISP=(NEW, DELETE), SPACE=(CYL, (2, 1), RLSE), DSN=&&SMSTOR SMOOTHER INFORMATION STORAGE FILE 11 11 //GO SYSUDUMP DD DUMMY //*SYSUDUMP DD SYSOUT=*,SPACE=(TRK,1), //* DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922) //GO DATA5 DD * 3 840805120000 0000 - 1 000100020001 3 180 0 01 25 0 80 120 185 215 310 285 415 380 475 515 570 610. 665. 700 760 795 860. 890 960 985 1055 1090 1160 1265. 1190 1285 000100030001 3 180 0 01 30 80 130 185 230 285. 335. 380 430. 475 525 565. 625. 755 660 720. 820 860 925 960 1030 1055 1125. 1150 1225 1245. 0001000300040001 3 180 0 01 120. 25 130 30 215 230 310 335 415. 430. 515. 525 610 625 705 720 805 820 900 925 995 1030 1090 1120 1190 1220. 1300 1320

/*

EXEC PGM=NOTIFY, COND=EVEN //NTSO

11

ORIGINAL PAGE IS OF POOR OUALITY //ZBPAPSOR JOB (GC002,311H,FFF),'SEA P2S1T1',MSGLEVEL=(1,1), // MSGCLASS=A, TIME=30, CLASS=C, NOTIFY=ZBPAP /*JOBPARM LINES=30 /*ROUTE PRINT RMT6 //* MEMBER P2S1T1 IN TESTPAN //* SOLVE FOR ONLY TWO SATELLITES, PROPOGATE FOR 1 DAY //* WITH 15X15 GEM9 - 8X8 GEM1 MISMATCH, GM (DATA CUT-OFF AT 1440MIN) //* USE ZBPAP SMTHDU5M.DATA TO UPDATE THE SEA SOURCE //STEP1 EXEC PGM=PAN#1, REGION=300K, COND=(1, LE) //PANDD1 DD DSN=GCDEV.MVT.SEA.PANLIB.DATA,UNIT=DISK,DISP=SHR DD DSN=&&SEAUPD, UNIT=VIO, SPACE=(CYL, (2, 1), RLSE), //PANDD2 DISP=(NEW, PASS), DCB=(RECFM=FB, LRECL=80, BLKSIZE=3600) 1 //SYSPRINT DD SYSOUT=* //SYSPUNCH DD DUMMY //SYSIN DD DSN=ZBPAP.SMTHDU5M.DATA,UNIT=DISK,DISP=SHR EXEC FORTRANH, PARM= 'XREF', TERM= '*' 11 //SYSLIN DD SPACE=(CYL, (2, 1)) //SYSPRINT DD DUMMY //SYSIN DD DSN=&&SEAUPD, UNIT=VIO, DISP=(OLD, DELETE) EXEC LINK, PARM= 'LET, LIST, MAP, SIZE= (200K, 20K) ', REGION=250K, 11 NBLK=100 11 //SYSLIB DD DSN=SYS2.FORTLIB,DISP=SHR DD DSN=GCDEV.SEAMVS.LOAD.DISP=SHR 11 //SYSPRINT DD SYSOUT=* //SYSUT1 DD SPACE=(TRK, (55, 1, 1)) //SYSLIN DD DD * 11 INCLUDE SYSLIB(SEA) ENTRY MAIN //GD EXEC PGM=GSFC.REGION=500K //GO.STEPLIB DD DSN=&&LODMOD, DISP=(OLD, DELETE) //FT01F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=44,BLKSIZE=4404) SPACE=(CYL, (5, 1)) SORTING FOR TRACKING DATA SCHEDULE 11 //FT02F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404) SPACE=(CYL, (1, 1)) MERGING FOR TRACKING DATA SCHEDULE 11 //FT03F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=44,BLKSIZE=4404, // BUFN0=1),DISP=(NEW,PASS),SPACE=(CYL,(1,1)), SORTED TRACKING DATA SCHEDULE 11 DSN=88SORTRK //FTO5FOO1 DD DDNAME=DATA5 TRACKING SCHEDULE CARD INPUT //*FTO6F001 DD SYSOUT **, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922), //FTOBFOO1 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141), SPACE=(CYL,(1,1),RLSE), DSN=&&PRTOUT SEA PRINTER OUTPUT 11 11 //*INPCRD DD * //*FT08F001 DD DDNAME=INPCRD SEA KEYWORD CARD INPUT //FT08F001 DD * SEA KEYWORD CARD INPUT EPOCHTIM 1 1 800301. 00000 0000 42166663.0 USERSATO 1 11 0.2499 D-7 7.0 1 USERSATO 1 12 319. ٥. 158.92521261 1 42166663.0 0.17865865 D-7 7. SATELITE 2 11 1 158.9521261 SATELITE 2 12 1 189. Ο. EARTH 8 8 40.0 GRAVCOEF -1 0.25 /* 11 DD UNIT=DISK, DSN=ZBBTF.ZBEXS.GEM.DATA(RECOEF), DISP=SHR DD * 11 SPCPARAM 0 0 0.036 1 5 1 SPCPARAM 2 0 0 0.036 1.5 MEASBIAS 000100010000001. 2 -1 5.0 MEASBIAS 2 -1 0001000200000001 50 -1 MEASBIAS 3 000100010000001. 0.0005 MEASBIAS 3 -1 000100020000001 0.0005 STATIONS 0 0 323003.857 2532329.162 1441 37 1 EBOUTPUT 2 1440. 180. 30.0 1 COVARANC 1 1.0D+06 1.0D+06 1 0D+00 1.0D+06 1.0D+00 1.0D+00 //*FT09F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=1922), //FTO9FOO1 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141), SPACE=(CYL,(1,1),RLSE), 11 DSN=&&NOMOUT 11 SATELLITE NOMINAL TRAJECTORY OUTPUT //*FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922), //FT10F001 DD SYSOUT=*.DCB=(RECFM=VBA.LRECL=137.BLKSIZE=141),

			DI CE)					
11	SPALE = (GIL, (I, I)	, KLGE), DDOCESCED ME	ACUDEMENTE DETNITED OUT				
//	DD DICD=00M		PRUCESSED ME	ASUREMENTS PRINTER UUT	PUI			
//F120F001		5W, PA33/,: Cem-VBC //	SPACE-(CIL,(I,I DECL-144 DIVET7	(), E = 0.004 (DIT=DICK				
11		DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK,						
//	USN=&&F		SEQUENTIAL E	KKUK BUUGEI SUMMART				
//F121F001		EW, PASS),: Cenevoc	SPACE=(CTL,(1,1	(),				
11		CFM=VB5,L	RECL=144, BLKS12	E=2884),UNI(=UISK,				
//	USN=885	ESUM Ski dod-(d)	BACKWARD SMU	UTHER ERRUR BUDGET SUM	MAKT			
//FT27F001	DD UNITEDI	SK,DCB=(R	ECFM=VBS,LRECL=	196, BLKSIZE= 1964,				
11	BUENU=1),DISP=(N	EW, PASS), SPACE=	(CYL, (1, 1)),				
//	USN=&&A	KKHIN	VISIBLE TRAC	KING DATA SCHEDULE				
//FT40F001	DD UNITEDI	SK, DCB=(R	ECHMERE, LRECLET	688, BLKSIZE=18568),				
11	DISP=(N	EW, DELETE), SPACE=(CYL, (2	, 1), RLSE),				
//	DSN=&&S	MSTOR	SMOOTHER INF	URMATION STURAGE FILE				
//GO SYSUDU	IMP DD DUMM	Y	(
//*SYSUDUMF	DD SYSOUT	= * , SPACE =	(TRK, 1),					
//*	DCB=(R	ECFM=VBA,	LRECL=137,BLKSI	ZE=1922)				
//GO DATAS	DD *				-			
3	8	003010000	00.0000		0			
00010001	0001 2	10	30.0					
0 0	10		120 0	121.0				
240.0	241.0		360.0	361.0				
480.0	481 0		600 0	601.0				
720.0	721.0		840.0	841.0				
960.0	961.0		1080	1081.				
1200.	1201		1320.	1321				
1440.	1440.							
00010001	0001 3	10.	0.003					
0.0	1.0		120 0	121.0				
240 0	241.0		360 0	361.0				
480.0	481.0		600.0	601.0				
720.0	721 0		840.0	841.0				
960.0	961 0		1080.	1081.				
1200	1201.		1320.	1321.				
1440	1440.							
00010002	0001 2	10.	30.0					
1.0	2.0		121.0	122.0				
241 0	242 0		361.0	362.0				
481.0	482.0		601.0	602.0				
721.0	722.0		841.0	842.0				
961 0	962.0		1081.	1082.				
1201.	1202		1321.	1322.				
00010002	0001 3	10	0.003					
10	2.0		121.0	122.0				
241.0	242.0		361.0	362.0				
481.0	482.0		601 0	602.0				
721.0	722.0		841.0	842.0				
961.0	962.0		1081.	1082.				
1201.	1202.		1321.	1322				

-

/* //NTSO EXEC PGM=NOTIFY,COND=EVEN //

•

.

```
//ZBPAP2S2 JOB (GC002,311H,FFF), 'SEA P2S2T1', MSGLEVEL=(1,1),
// MSGCLASS=X, TIME=30, CLASS=C, NOTIFY=ZBPAP
/*JOBPARM LINES=30
/*ROUTE PRINT RMT6
//* MEMBER P2S2T1 IN TESTPAN
//* SOLVE FOR ONLY ONE OF 3 SATELLITES, PROPOGATE FOR 1 DAY
//* USE ZBPAP.SMTHDU5M.DATA TO UPDATE THE SEA SOURCE
//STEP1 EXEC PGM=PAN#1, REGION=300K, COND=(1, LE)
//PANDD1 DD DSN=GCDEV MVT.SEA.PANLIB.DATA,UNIT=DISK,DISP=SHR
           DD DSN=&&SEAUPD, UNIT=VIO, SPACE=(CYL, (2, 1), RLSE),
//PANDD2
               DISP=(NEW, PASS), DCB=(RECFM=FB, LRECL=80, BLKSIZE=3800)
//SYSPRINT DD SYSOUT=*
//SYSPUNCH DD DUMMY
//SYSIN DD DSN=ZBPAP.SMTHDU5M.DATA.UNIT=DISK.DISP=SHR
      EXEC FORTRANH, PARM='XREF', TERM='*'
//SYSLIN DD SPACE=(CYL, (2,1))
//SYSPRINT DD DUMMY
//SYSIN DD DSN=&&SEAUPD, UNIT=VIO, DISP=(OLD, DELETE)
      EXEC LINK, PARM='LET, LIST, MAP, SIZE=(200K, 20K)', REGION=250K,
11
         NBLK=100
11
//SYSLIB DD DSN=SYS2.FORTLIB, DISP=SHR
         DD DSN=GCDEV.SEAMVS.LOAD.DISP=SHR
11
//SYSPRINT DD SYSOUT=*
//SYSUT1 DD SPACE=(TRK, (55, 1, 1))
//SYSLIN DD
         DD *
11
 INCLUDE SYSLIB(SEA)
 ENTRY MAIN
//GO EXEC PGM=GSFC.REGION=500K
//GO.STEPLIB DD DSN=&&LODMOD,DISP=(OLD,DELETE)
//FT01F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404)
// SPACE=(CYL,(5,1)) SORTING FOR TRACKING DATA SCHEDULE
//FT02F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=44,BLKSIZE=4404),
               SPACE=(CYL, (1, 1)) MERGING FOR TRACKING DATA SCHEDULE
11
//FT03F001 DD UNIT=DISK.DCB=(RÉCFM=VBS,LRECL=44,BLKSIZE=4404,
// BUFN0=1),DISP=(NEW.PASS),SPACE=(CYL,(1,1)),
11
                                  SORTED TRACKING DATA SCHEDULE
               DSN=&&SORTRK
11
//FTOSFOO1 DD DDNAME=DATAS
                                   TRACKING SCHEDULE CARD INPUT
//*FT06F001 DD SYSOUT=*.DCB=(RECFM=VBA,LRECL=137.BLKSIZE=1922).
//FTO6F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141),
               SPACE=(CYL,(1,1),RLSE),
11
                                   SEA PRINTER OUTPUT
              DSN=&&PRTOUT
11
//*FT08F001 DD DDNAME*INPCRD
                                   SEA KEYWORD CARD INPUT
//*INPCRD DD *
//FT08F001 DD *
                                   SEA KEYWORD CARD INPUT
EPOCHTIM
                 1 800301.
                                        000000.0000
          1
                                          0.0017
                                                              28.
USERSATO
          1 11
                     6778140.
                 1
USERSATO
          1 12
                 1
                      0.
                                          ο.
                                                               0
SATELITE
          2 11
                     42168663.0
                                        0.2499
                                                           D-7 7.0
          2 12
SATELITE
                     319
                                        0.
                                                              158.92521261
SATELITE
          3 11
                     42166663.0
                                        0.17885865
                                                           D-7 7.
                                                              158 9521261
SATELITE
          3 12
                     189.
                                        ٥.
EARTH
          8
             8
SPCPARAM
                         0.0011765
             0
                0
                                                              2 0
                                         1.5
          1
                                         SPCPARAM
          2
             0
                0
                         0.036
SPCPARAM
          3
             0
                0
                         0.036
                                         STATIONS
                     323003.857
             0
                                         2532329.162
                                                              1441.37
          1
               0
USERDRAG
               -1
                         0.25
GRAVCOEF
                -1
                         0.25
/*
11
     DD UNIT=DISK, DSN=ZBBTF.ZBEXS.GEM.DATA(RECOEF), DISP=SHR
11
     DD ¥
MEASBIAS
                    0001000200010000.
                -1
                                         5 0
          - 2
MEASBIAS
               -1
                    0001000300010000.
                                         5.0
          2
                    0001000200010000.
                                         0.0005
MEASBIAS
          3
               -1
                    0001000300010000.
MEASBIAS
          3
                -1
                                         0.0005
                                                              30 0
EBOUTPUT
                       1440.0
              1
                2
                                          180.0
COVARANC
          1
     1.0D+05
                  1.0D+05
                              1.0D+05
                                           1.0D+00
                                                        1.00+00
                                                                    1.0D+00
/*
//*FT09F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922),
//FT09F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=141),
              SPACE=(CYL,(1,1),RLSE),
11
```

DSN=&&NOMOUT SATELLITE NOMINAL TRAJECTORY OUTPUT 11 //*FT10F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=1922), //FT10F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=141), SPACE=(CYL, (1, 1), RLSE), 11 PROCESSED MEASUREMENTS PRINTER OUTPUT DSN=&&MEASOUT 11 //FT2OF001 DD DISP=(NEW,PASS),SPACE=(CYL,(1,1)), // DCB=(RECFM=VBS,LRECL=144,BLKSIZE=2884),UNIT=DISK, 11 DSN=&&FESUM SEQUENTIAL ERROR BUDGET SUMMARY //FT21F001 DD DISP=(NEW,PASS),SPACE=(CYL,(1,1)), // DCB=(RECFM=VBS,LRECL=144,BLKSIZE=2884),UNIT=DISK, 11 BACKWARD SMOOTHER ERROR BUDGET SUMMARY DSN=&&SESUM 11 //FT27F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=196, BLKSIZE=1964, BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1)), DSN=&&AKKHIN VISIBLE TRACKING DATA SCHEDULE $^{\prime\prime}$ 11 //FT40F001 DD UNIT=DISK, DCB=(RECFM=FB, LRECL=1688, BLKSIZE=18568), DISP=(NEW, DELETE), SPACE=(CYL, (2, 1), RLSE), 11 11 DSN=&&SMSTOR SMOOTHER INFORMATION STORAGE FILE //GO.SYSUDUMP DD DUMMY //*SYSUDUMP DD SYSOUT=*, SPACE=(TRK, 1), DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922) //* //GO.DATA5 DD * 800301000000.0000 З 0 000100020001 2 600. 30. 10. 360. 000100020001 600. 3 0.3 10 360. 000100030001 2 600. 30. 10. 360. 000100030001 600. 3 0.3 10. 360.

```
/*
//NTSO EXEC PGM=NOTIFY,COND=EVEN
//
```

.

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```
//ZBCPYSOT JOB (GJ002,311H,FFF), 'SEA P2S2T2', MSGLEVEL=(1,1),
// MSGCLASS=X, TIME=30, CLASS=C, NOTIFY=ZBCPY
/*JOBPARM LINES=30
/*ROUTE PRINT PRTSS
//* MEMBER P2S2T2 IN TESTPAN
//* Solve for all three satellites, propogate for 1 day
//* **** USING EQUAL WEITHTS FOR A DATA TYPE- REGARDLESS OF S/C
//* USE ZBCPY.SMTHDU5M DATA TO UPDATE THE SEA SOURCE
//STEP1 EXEC PGM=PAN#1, REGION=300K, COND=(1, LE)
//PANDD1 DD DSN=GCDEV.MVT.SEA.PANLIB.DATA,UNIT=DISK,DISP=SHR
//PANDD2
           DD DSN=&&SEAUPD, UNIT=VIO, SPACE=(CYL, (2, 1), RLSE),
              DISP=(NEW, PASS), DCB=(RECFM=FB, LRECL=80, BLKSIZE=3600)
11
//SYSPRINT DD SYSOUT=*
//SYSPUNCH DD DUMMY
//SYSIN DD DSN=ZBCPY SMTHDU5M.DATA,UNIT=DISK,DISP=SHR
      EXEC FORTRANH, PARM='XREF', TERM='*'
//
//SYSLIN DD SPACE=(CYL, (2,1))
//SYSPRINT DD SYSOUT=*
//SYSIN DD DSN=&&SEAUPD, UNIT=VIO, DISP=(OLD, DELETE)
11
      EXEC LINK.PARM='LET.LIST.MAP.SIZE=(200K,20K)'.REGION=250K.
         NBLK=100
11
//SYSLIB DD DSN=SYS2.FORTLIB, DISP=SHR
         DD DSN=GCDEV.SEAMVS.LOAD.DISP=SHR
11
//SYSPRINT DD SYSOUT=*
//SYSUT1 DD SPACE=(TRK, (55, 1, 1))
//SYSLIN DD
         DD *
INCLUDE SYSLIB(SEA)
 ENTRY MAIN
//GO EXEC PGM=GSFC.REGION=500K
//GO.STEPLIB DD DSN=&&LODMOD, DISP=(OLD, DELETE)
//FT01F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404)
              SPACE=(CYL, (5, 1)) SORTING FOR TRACKING DATA SCHEDULE
11
//FT02F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404)
              SPACE=(CYL, (1, 1)) MERGING FOR TRACKING DATA SCHEDULE
11
//FTO3FOO1 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404,
              BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1))
11
11
              DSN=&&SORTRK
                                  SORTED TRACKING DATA SCHEDULE
//FTO5FOO1 DD DDNAME=DATA5
                                  TRACKING SCHEDULE CARD INPUT
//*FT06F001 DD SYSOUT=*.DCB=(RECFM=VBA.LRECL=137.BLKSIZE=1922).
//FTOGFOO1 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141),
              SPACE=(CYL,(1,1),RLSE),
11
                                  SEA PRINTER OUTPUT
11
              DSN=&&PRTOUT
//FTO8FOO1 DD DDNAME=INPCRD
                                   SEA KEYWORD CARD INPUT
//*FT09F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922),
//FT09F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=141),
               SPACE=(CYL, (1, 1), RLSE)
11
11
              DSN=&&NOMOUT
                                   SATELLITE NOMINAL TRAJECTORY OUTPUT
//*FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922),
//FT10F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=141),
              SPACE=(CYL,(1,1),RLSE)
11
                                  PROCESSED MEASUREMENTS PRINTER OUTPUT
11
              DSN=&&MEASOUT
//FT20F001 DD DISP=(NEW,PASS),SPACE=(CYL,(1,1)),
              DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK,
11
11
              DSN=&&FESUM
                                   SEQUENTIAL ERROR BUDGET SUMMARY
//FT21F001 DD DISP=(NEW,PASS),SPACE=(CYL,(1,1)),
              DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK,
11
                                  BACKWARD SMOOTHER ERROR BUDGET SUMMARY
11
              DSN=&&SESUM
//FT27F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=196, BLKSIZE=1964,
              BUFND=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1))
//
                                   VISIBLE TRACKING DATA SCHEDULE
              DSN=&&AKKHIN
11
//FT40F001 DD UNIT=DISK, DCB=(RECFM=FB, LRECL=1688, BLKSIZE=18568),
              DISP=(NEW, DELETE), SPACE=(CYL, (2, 1), RLSE)
//
11
                                  SMOOTHER INFORMATION STORAGE FILE
              DSN=&&SMSTOR
//GO.SYSUDUMP DD DUMMY
//*SYSUDUMP DD SYSOUT=*,SPACE=(TRK,1),
1/*
               DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922)
//INPCRD DD *
EPOCHTIM 1
                 1 800301.
                                        000000.0000
USERSATO
                                                              28.
                                          0.0017
         1 11
                - 1
                     6778140.
USERSATO
          1 12
                1
                      0
                                          0
                                                               ο.
         2 11
                     42166663.0
SATELITE
                                        0 2499
                                                           D-770
                1
                                                              158.92521261
SATELITE 2 12
                1
                     319.
                                        Ο.
```

SATELITE 3 SATELITE 3	3 11 3 12	1 1	4: 1:	2166663.0 89.		- 0	17865865		D-77 158	9521261
EARTH 8	8 8								40	0
SPCPARAM 1	i 0	0		0.00117	765		2.0		2.	0
SPCPARAM 2	2 0	0		0.036			1.5			
SPCPARAM 3	3 0	0		0.035			1.5			
STATIONS 1	10	0	3	23003 857		2	2532329.16	2	144	1 37
MEASBIAS 2	2	-1	00	010002000	10000	D. 5	5.0			
MEASBIAS 2	2	-1	00	010003000	10000	D. 5	50			
MEASBIAS 3	3	-1	00	010002000	10000	0 0	0.005			
MEASBIAS 3	3	-1	00	010003000	10000	b (0.005			-
EBOUTPUT	0	2		1440.		•	180.		30.	0
COVARANC 1							4 00 00		1 00.00	4 00.00
1.0D+C)5	1	. 00	+05 1.	. OD+(05	1 00+00		1.00+00	1 00+00
/*										
//GU.DATA5	DD	¥								
3			. 8	0030100000	0.00	200				1
10010002000	11	260	2	800		30				
10.		300	•	600		0.2				
10		260	3	800.		03				
10.	•	300	• •	800		30				
10		360	4	000.		JU.				
00010003000	11	500	3	600		0.3				
10		360				•••				
00010002	00	01	2	10.		30.0				
0.0		1.0	-		120	0	121	0		
240.0		241	. 0		360	. ŏ	361	Õ		
480.0		481	.0		600	.0	601	.0		
720.0		721	.0		840	.0	841	.0		
960.0		961	0		1080	0.	108	1.		
1200.		120	1.		1320	ο.	132	1.		
1440.		144	0.							
00010002	00	01	3	10.		0.3				
0.0		1.0			120	.0	121	.0		
240.0		241	.0		360	.0	361	.0		
480.0		481	.0		600	.0	601	.0		
720.0		721	.0		840	.0	841	.0		
960 0		961	.0		1080	0.	108			
1200.		120	1.		132	υ.	132	.1.		
1440.	00	144	U.	10		20 0				
1 0	00	2 0	4	10.	121	0.0	122	0		
241.0		242	0		361	.0	362	0		
481.0		482	ō		601	.0	602	0		
721.0		722	Ō		841	.0	842	ō		
961.0		962	. 0		108	1.	108	2.		
1201.		120	2.		132	1.	132	2.		
		• •	_							
00010003	00	01	3	10.		0.3				
1.0		2.0	~		121	.0	122			
241.U		242	.0		301	.0	362			
721 0		402	.0		844		842			
961 0		962			102		109	2		
1201		120	2ັ		132	1.	132	2.		

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,

/* //NTSO EXEC PGM=NOTIFY,COND=EVEN //

```
//ZBPAPSWN JOB (GCOO2,311H,FFF), 'SEA P3S1T1', MSGLEVEL=(1,1),
// MSGCLASS=A, TIME=30, CLASS=C, NOTIFY=ZBPAP
/*JOBPARM LINES=30
/*ROUTE PRINT PRTSS
//* MEMBER P3S1T1 IN TESTPAN
//* SOLVE FOR ONLY ONE OF 3 SATELLITES, PROPOGATE FOR 1 DAY
//* WITH VELOCITY PROCESS NOISE OF 1 OD-09 ON STATE VELOCITIES
//* USE ZBPAP.SMTHDU5M.DATA TO UPDATE THE SEA SOURCE
//* SMTHDUP3 MODIFIED TO SET VAR DELTAT WITH THE OPPOSITE SIGN
//STEP1 EXEC PGM=PAN#1, REGION=300K, COND=(1, LE)
//PANDD1 DD DSN=GCDEV.MVT.SEA.PANLIB.DATA,UNIT=DISK,DISP=SHR
//PANDD2
            DD DSN=&&SEAUPD, UNIT=VIO, SPACE=(CYL, (2, 1), RLSE)
               DISP=(NEW, PASS), DCB=(RECFM=FB, LRECL=80, BLKSIZE=3600)
11
//SYSPRINT DD SYSOUT=*
//SYSPUNCH DD DUMMY
//SYSIN DD DSN=ZBPAP.SMTHDU5M DATA,UNIT=DISK,DISP=SHR
      EXEC FORTRANH, PARM='XREF', TERM='*'
11
//SYSLIN DD SPACE=(CYL,(2,1))
//SYSPRINT DD DUMMY
//SYSIN DD DSN=&&SEAUPD, UNIT=VIO, DISP=(OLD, DELETE)
      EXEC LINK, PARM='LET, LIST, MAP, SIZE=(200K, 20K)', REGION=250K.
11
         NBLK=100
11
//SYSLIB DD DSN=SYS2.FORTLIB, DISP=SHR
          DD DSN=GCDEV.SEAMVS.LOAD,DISP=SHR
11
//SYSPRINT DD SYSOUT =*
//SYSUT1 DD SPACE=(TRK, (55, 1, 1))
//SYSLIN DD
         DD *
 INCLUDE SYSLIB(SEA)
 ENTRY MAIN
//GO EXEC PGM=GSFC, REGION=500K
//GO.STEPLIB DD DSN=&&LODMOD, DISP=(OLD, DELETE)
//FT01F001 DD UNIT=DISK.DCB=(RECFM=VBS.LRECL=44.BLKSIZE=4404)
               SPACE=(CYL, (5, 1)) SORTING FOR TRACKING DATA SCHEDULE
//FT02F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404)
// SPACE=(CYL,(1,1)) MERGING FOR TRACKING DATA SCHEDULE
//FTO3F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=44,BLKSIZE=4404,
               BUFND=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1))
11
               DSN=&&SORTRK
                                   SORTED TRACKING DATA SCHEDULE
11
//FT05F001 DD DDNAME=DATA5
                                   TRACKING SCHEDULE CARD INPUT
//*FT06F001 DD SYSOUT=*,DCB=(RECFM=VBA,LRECL=137,BLKSIZE=1922),
//FTOBFOO1 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141),
               SPACE=(CYL, (1, 1), RLSE),
11
                                   SEA PRINTER OUTPUT
11
               DSN=&&PRTOUT
//*FT08F001 DD DDNAME=INPCRD
                                     SEA KEYWORD CARD INPUT
//*INPCRD DD *
//FT08F001 DD *
                                    SEA KEYWORD CARD INPUT
EPOCHTIM
                 1 800301.
                                         000000.0000
USERSATO
           1 11
                     6778140.
                                           0.0017
                                                                28
                 1
USERSATO
             12
                 1
                      0.
                                                                0
           1
                                           0
                      42186663.0
SATELITE
          2 11
                                         0.2499
                                                            D-7 7 0
SATELITE
                     319.
          2 12
                                         0.
                                                                158.92521261
SATELITE
                      42166663.0
                                         0.17865865
                                                            D-77
          3 11
SATELITE
          3 12
                      189
                                         o
                                                                158 9521261
EARTH
             8
           8
SPCPARAM
              0
                 0
                          0 0011765
                                                                0 0000000001
           1
SPCPARAM
          2
                          0.036
                                           1 5
              0
                 0
SPCPARAM
          3
              0
                 0
                          0.036
                                           1.5
STATIONS
          1 0 0
                     323003.857
                                          2532329 162
                                                                1441 37
GRAVCOEF
                          0.25
                -1
/*
11
     DD UNIT=DISK, DSN=ZBBTF.ZBEXS.GEM.DATA(RECOEF), DISP=SHR
     DD *
11
MEASBIAS
                    0001000200010000.
                                          5.0
          2
                -1
                                          5.0
MEASBIAS
          2
                -1
                    0001000300010000.
                                          0.0005
MEASBIAS
          3
                -1
                    0001000200010000.
MEASBIAS
          3
                -1
                    0001000300010000.
                                          0.0005
EBOUTPUT
              1
                 2
                        360
                                           30.
                                                                30.0
COVARANC
          1
     1 0D+05
                  1.0D+05
                               1 0D+05
                                                         1 0D+00
                                            1.0D+00
                                                                      1.0D+00
NOISECOV 1 1 0
     0.0D+00
                  0.0D+00
                               0.0D+00
                                            1.0D-09
                                                         1 OD-09
                                                                      1 OD-09
/*
```

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```

```
//*FT09F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922),
//FT09F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141),
11
               SPACE=(CYL,(1,1),RLSE),
               DSN=&&NOMOUT
                                    SATELLITE NOMINAL TRAJECTORY OUTPUT
11
//*FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922),
//FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141),
               SPACE=(CYL, (1, 1), RLSE),
11
               DSN=&&MEASOUT
                                    PROCESSED MEASUREMENTS PRINTER OUTPUT
11
//FT20F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1,1)),
11
               DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK,
               DSN=&&FESUM
                                    SEQUENTIAL ERROR BUDGET SUMMARY
11
//FT21F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1,1)),
               DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK,
11
                                    BACKWARD SMOOTHER ERROR BUDGET SUMMARY
               DSN=&&SESUM
11
//FT27F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=196,BLKSIZE=1964,
// BUFND=1),DISP=(NEW,PASS),SPACE=(CYL,(1,1)),
                                    VISIBLE TRACKING DATA SCHEDULE
11
               DSN=&&AKKHIN
//FT40F001 DD UNIT=DISK, DCB=(RECFM=FB, LRECL=1688, BLKSIZE=18568),
               DISP=(NEW, DELETE), SPACE=(CYL, (2, 1), RLSE)
11
11
                                    SMOOTHER INFORMATION STORAGE FILE
               DSN=&&SMSTOR
//GO.SYSUDUMP DD DUMMY
//*SYSUDUMP DD SYSOUT=*, SPACE=(TRK, 1),
//*
                DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922)
//GO.DATA5 DD *
                      800301000000.0000
                                                                            0
          3
000100020001
                    2 600
                                      30.
                360
10.
000100020001
                        600
                                      0.3
                     3
                360
10.
000100030001
                    2
                        600.
                                      30
                360
10
000100030001
                     3
                        600.
                                      0.3
10
                360
```

```
/*
//NTSO EXEC PGM=NOTIFY,COND=EVEN
//
```

```
//ZBCPYSTS JOB (GJ002,311H,FFF), 'SEA P3S2T1', TIME=30,
           MSGCLASS=X, MSGLEVEL=(1,1), NOTIFY=ZBCPY, CLASS=C
11
/*JOBPARM LINES=100
/*ROUTE PRINT PRTSS
//*MEMBER P3S2T1 IN TESTPAN
//*BEAKON TRACKING (FLBT) FOR A SPACE TELESCOPE MISSION MODEL
//*RANGE AND RANGE RATE MEASUREMENTS EVERY 180 0 SECONDS
//*USING SMTHDU5M SEA SMOOTHER/TDAS UPDATES, SEA VER 4 1 KEYWORDS
//*WITH SMOOTHING
//*WITH LOW ACCCURACY TRACKING EVERY 30 MINUTES TO INCREASE THE
//*NUMBER OF SMOOTHED ERROR BUDGETS
//STEP1 EXEC PGM=PAN#1, REGION=300K, COND=(1, LE)
//PANDD1 DD DSN=GCDEV.MVT.SEA.PANLIB.DATA,UNIT=DISK.DISP=SHR
           DD DSN=&&SEAUPD, UNIT=VIO, SPACE=(CYL, (2, 1), RLSE),
//PANDD2
               DISP=(NEW, PASS), DCB=(RECFM=FB, LRECL=80, BLKSIZE=3800)
11
//SYSPRINT DD SYSOUT=*
//SYSPUNCH DD DUMMY
//SYSIN DD DSN=ZBCPY.SMTHDU5M.DATA,UNIT=DISK,DISP=SHR
      EXEC FORTRANH, PARM='XREF', TERM='*', OUT='*'
//SYSLIN DD SPACE=(CYL, (2, 1))
//SOURCE.SYSTERM DD SYSOUT=*
//SOURCE.SYSPRINT DD DUMMY
//SYSIN DD DSN=&&SEAUPD, UNIT=VIO, DISP=(OLD, DELETE)
      EXEC LINK, PARM= 'LET, LIST, MAP, SIZE= (200K, 20K) ', REGION=250K
//SYSLIB DD DSN=SYS2.FORTLIB,DISP=SHR
         DD DSN=GCDEV.SEAMVS LOAD, DISP=SHR
//SYSPRINT DD SYSOUT=*
//SYSUT1 DD SPACE=(TRK, (55, 1, 1))
//SYSLIN DD
         DD 4
11
 INCLUDE SYSLIB(SEA)
 ENTRY MAIN
// EXEC PGM=GSFC, REGION=400K
//STEPLIB DD DSN=&&LODMOD, DISP=(OLD, DELETE)
//FT01F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404)
               SPACE=(CYL, (5, 1)) SORTING FOR TRACKING DATA SCHEDULE
//FT02F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=44, BLKSIZE=4404)
               SPACE=(CYL, (1,1)) MERGING FOR TRACKING DATA SCHEDULE
//
//FT03F001 DD UNIT=DISK,DCB=(RECFM=VBS,LRECL=44,BLKSIZE=4404,
11
               BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1))
11
                                   SORTED TRACKING DATA SCHEDULE
               DSN=&&SORTRK
//FT05F001 DD DDNAME=DATA5
                                   TRACKING SCHEDULE CARD INPUT
//*FTO6F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=3990),
                DSN=8&PRTOUT
                                    SEA PRINTER OUTPUT
//*
//FTO6FOO1 DD SYSOUT=*
               DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141),
11
               SPACE=(CYL, (3, 1), RLSE)
11
//*FTO8FOO1 DD DDNAME=INPCRD
                                    SEA KEYWORD CARD INPUT
//*INPCRD DD *
//FT08F001 DD *
                                   SEA KEYWORD CARD INPUT
                     861101.
EPOCHTIM 3
                - 1
                                          000000.0000
USERSATO
                     6978140.
                                          0.0001
                                                               28 8
          1 11
                 1
USERSATO
          1 12
                                                               0.
                      0.
                                          0.
                1
SATELITE
                     42166750
                                        0.0004
                                                               5.0
          2 11
                0
SATELITE
          2 12
                0
                     358
                                                                 0
                                          0
                     42163592.42
                                        0 0004
                                                               5 0
SATELITE
          3 11
                0
SATELITE
          3 12
                0
                     228.
                                          0
                                                                 Ο.
                     42163592 42
                                        0.0004
                                                               5 0
SATELITE
          4 11
                0
SATELITE
          4 12
                0
                     113.
                                          0.
                                                                0.
                     323002.867
                                          2532329.163
                                                                1441 37
STATIONS 1 0
                0
EARTH
         15 15
                                                               150.0
SPCPARAM
          1 0
                0
                         0.00272
                                                               2.0
                                          30.0
EBOUTPUT
                         1440.0
                                                               30.0
             -1
                2
CLKBIAS
          1
                 1
                      1000000.
CLKDRIFT
                                          0.000001
                 1
                      200.0
          1
USERDRAG
                 1
                      .025
          1
GRAVCOEF
                - 1
                         0.25
/*
     DD UNIT=DISK, DSN=ZBBTF.ZBEXS.GEM.DATA(RECOEF2), DISP=SHR
11
     DD *
11
SATSOLPR
                -1
MEASBIAS 2
MEASBIAS 3
                      1000200010000.
                -1
                                        10.0
                -1
                      1000200010000.
                                        .001
```

MEASBIAS 2 1000300010000 10 0 -1 -1 MEASBIAS 1000300010000. .001 3 MEASBIAS 2 1000200040001. 10.0 -1 MEASBIAS 1000200040001. .001 3 - 1 EPHEMERR 1 25.0 23 0 40.0 EPHERROR 99 CLKACCEL 1 -1 . 11574 COVARANC 1 1 0D+00 2.5D+05 2.5D+05 2.5D+05 1 0D+00 1 0D+00 NOISECOV 1 0 1 0 0. 1 00000D-10 1.00000D-10 1.00000D-10 0 /* //*FT09F001 DD SYSOUT=*.DCB=(RECFM=VBA.LRECL=137.BLKSIZE=3990) //* DSN=&&NOMOUT SATELLITE NOMINAL TRAJECTORY OUTPUT //FT09F001 DD SYSOUT=* DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141), 11 SPACE=(CYL,(2,1),RLSE) 11 //*FT10F001 DD SYSOUT=*, DCB=(RECFM=VBA, LRECL=137, BLKSIZE=3990) 11* DSN=&&MEASOUT PROCESSED MEASUREMENTS PRINTER OUTPUT //FT10F001 DD SYSOUT=* DCB=(RECFM=VBA, LRECL=137, BLKSIZE=141), 11 SPACE=(CYL,(2,1),RLSE) 11 //FT20F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1, 1)), DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK, 11 DSN=&&FESUM SEQUENTIAL ERROR BUDGET SUMMARY 11 //FT21F001 DD DISP=(NEW, PASS), SPACE=(CYL, (1, 1)), DCB=(RECFM=VBS, LRECL=144, BLKSIZE=2884), UNIT=DISK 11 BACKWARD SMOOTHER ERROR BUDGET SUMMARY 11 DSN=&&SESUM //FT27F001 DD UNIT=DISK, DCB=(RECFM=VBS, LRECL=196, BLKSIZE=1964, BUFNO=1), DISP=(NEW, PASS), SPACE=(CYL, (1, 1)) 11 DSN=&&AKKHIN VISIBLE TRACKING DATA SCHEDULE 11 //FT40F001 DD UNIT=DISK, DCB=(RECFM=FB, LRECL=1688, BLKSIZE=18568), DISP=(NEW, DELETE), SPACE=(CYL, (2, 1), RLSE) 11 SMOOTHER INFORMATION STORAGE FILE 11 DSN=&&SMSTOR //GO.SYSUDUMP DD DUMMY //*SYSUDUMP DD SYSOUT=*,SPACE=(TRK,1), DCB=(RECFM=VBA, LRECL=137, BLKSIZE=1922) 1/* //GO.DATA5 DD * 3 861101000000.0000 -1 100020001 1.66667 2 180.0 0.00 2.7 95.3333 132.0 200.3333 235.7 339 7 304.6666 407.6666 443.7 510.0 547.0 753 0 612.3333 650.0 715.3333 819.6666 856.0 924.3333 959 7 1028.3333 1064.0 1131.3333 1167.7 1233.6666 1271.0 1336.3333 1374.4 1439 6666 1440.0 3 100020001 180.0 0.00186667 2.7 0.00 95.3333 132.0 200.3333 235.7 304.6666 339 7 443.7 510.0 407 6666 547 0 650.0 715.3333 612.3333 753 0 819.6666 · 856.0 924.3333 959 7 1064.0 1131 3333 1028.3333 1167 7 1233.6666 1271 0 1336 3333 1374 4 1439.6666 1440 0 100030001 2 180.0 1 66667 63.6666 95.0 166.3333 200 0 407 4 268.6566 304.4 371.6666 509.7 475 3333 580.0 612.0 684.3333 787 6666 715.0 819.4 890.3333 924.0 992.6866 1028.0 1095.6666 1131 0 1199.6666 1233.4 1408.6866 1304.0 1336.0 1439.4 0.00166667 3 180 0 100030001 63 6668 95.0 166.3333 200 0 268.6666 304.4 371.6666 407 4 509.7 475.3333 612.0 580.0 787 6666 684.3333 715.0 819 4 890.3333 924.0 992.6666 1028.0 1199.6666 1233.4 1095.6666 1131.0

1304.0	1336.0		1408 6666	1439.4
10002000400	01 2	180.0	1 66667	
3 00	63.4		132 3333	166.0
236.0	268.4		340.0	371.4
444 0	475.0		547.3333	579.7
650.3333	684.0		753 3333	787.4
856.3333	890.0		960 O	992 4
1064.3333	1095.4		1168.0	1199.4
1271.3333	1303.7		1374.6666	1408.4
10002000400	01 3	180 0	0.00166667	
3.00	63.4		132.3333	166.0
236.0	268.4		340 0	371 4
444.0	475 0		547 3333	579.7
650.3333	684 O		753.3333	787.4
856.3333	890.0		960.0	992.4
1064.3333	1095.4		1168 0	1199.4
1271.3333	1303.7		1374.6666	1408 4
100020001	3	1800.0	10000.0	
0.00	1440.0			
100030001	3	1800.0	10000 0	
0.00	1440 0			
10002000400	01 3	1800.0	10000.0	
0.00	1440.0			

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/* //NTSO EXEC PGM=NOTIFY,COND=EVEN //

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APPENDIX B - UTILITIES FOR GEOPOTENTIAL ERROR MODEL STUDIES

This appendix describes two utilities adapted from the Sequential Error Analysis (SEA) program for geopotential error model studies. Both utilities compute the gravitational acceleration errors that result from a given geopotential error model. The first utility outputs the magnitudes of the acceleration errors as a function of geocentric latitude and longitude at a fixed altitude. The second utility outputs the magnitudes as well as the acceleration components in the radial, alongtrack, and crosstrack directions as the satellite travels in its orbit. These two utilities are described in more detail in Sections B.1 and B.2.

B.1 GEOPOTENTIAL ACCELERATION ERROR WORLD-MAP UTILITY

This SEA utility computes the uncertainty in the gravitational acceleration due to nonspherical effects of the Earth at a specified altitude for a given geopotential error model. The utility computes and prints out the global distribution of gravitational acceleration uncertainties in meters per second squared for latitudes between -89 deg and +89 deg¹ with 5-deg increments and longitudes varying between 0 deg and 360 deg with 10-deg increments.

The utility also generates a global distribution plot of the gravitational acceleration uncertainties in milligals (10^{-5}m/sec^2) rounded to the nearest integer, with longitude as abscissa and latitude as ordinate.

¹The geopotential computation subroutine is adapted from the corresponding GTDS subroutine, which has a singularity at the poles (<u>+90</u> deg). The use of <u>+89</u> deg avoids this program deficiency.

B.1.1 INPUT DATA SETUP

This utility can be executed using the SEA keyword cards setup, and no special keyword cards are required. The geopotential error model is provided by the LUMPGEOP keyword card followed by the corresponding set of RECOEF cards if other than the default model--GEM-9 formal uncertainties--is desired. The coefficients of any geopotential error model, except the default model, can be scaled using the first real field of the LUMPGEOP keyword card. The altitude for which geopotential acceleration uncertainties are computed is based on the orbital elements provided on the USERSATO card.

B.1.2 MODIFICATIONS TO SEA PROGRAM

Modifications are made in subroutines RDKEYS and SPART to adapt SEA to function as described in Section B.l. In subroutine RDKEYS, which reads in keyword cards, modifications are made so that the first real field (Rl) on the LUMPGEOP keyword card can be used as a scaling factor (multiplication factor) to the sine and cosine coefficients uncertainties of an input geopotential error model. This provides a convenient means to scale down or scale up the coefficients to study the effects of an error model.

Subroutine SPART, which normally computes the gravitational accelerations due to a geopotential model, is modified to compute the acceleration uncertainties resulting from a geopotential error model instead. A nested DO-loop for latitudes and longitudes is added so that the subroutine computes and outputs the global distribution of gravitational acceleration uncertainties. These uncertainties are calculated based on the orbital radius of the user satellite as provided by the orbital elements in the USERSATO card. The subroutine also converts the acceleration uncertainties from meters per second squared to milligals (rounded to the nearest integer) and generates a global distribution plot of

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gravitational acceleration uncertainties. After printing out the above results, the program execution is allowed to terminate instead of executing the rest of the normal SEA program.

B.1.3 REQUIRED CODING UPDATES TO SEA PROGRAM

· -

The following is the listing of Panvalet updates to the Panvalet SEA source program stored in the data set GCDEV.MVT.SEA.PANLIB.DATA. To create an updated SEA program load module, the updates that follow must be compiled and linked to the existing SEA load module GCDEV.SEAMVS.LOAD.

```
++UPDATE RDKEYS, 1, TEMP
++C 229.229
       DPMAP(ILUMP) = 1 ODO
       IF ( R1 NE. 0.0D0 ) DPMAP(ILUMP) = R1
++C 251,252
       CSIG(I1, I2+1 ) = R1 * DPMAP(ILUMP)
       CSIG(31-I1, 33-I2 ) = R2 * DPMAP(ILUMP)
++WRITE WORK, RDKEYS
++UPDATE SPART, 1, TEMP
++C 69,69
       COMMON/CONST / AE, GM, DUM(3), THETG, DTR
++C 73,73
      COMMON/FMODEL/CSIG(30,33),C(30,33),MAXDEG,MAXORD,NMAX,MMAX
++C 76
       LOGICAL*1 HORZ(115), VERT, SLASH
       INTEGER*2 PLOT(40,40),A1(40),A2(40)
       DATA DLAT/5 DO/, DLON/10 DO/, FACTOR/1.D5/
DATA HORZ/115*'-'/, VERT/'+'/, SLASH/'I'/
С
       DO 50 ICOL = 1, 112, 3
       HORZ(ICOL) = SLASH
   50 CONTINUE
++D 93,94
       WRITE(6, 10)R
    10 FORMAT('1' ///.' *** ENTER SPART TO GENERATE WORLD MAP '.
      * '- USE GEOP UNCER''S TO CALC ACCELERATIONS ***',///,
* ' THE SIZE OF THE GEOPOTENTIAL UNCERTAINTY IS SPECIFIED BY '.
      * 'THE "EARTH" KEYWORD'.//.
* ' THE ORBITAL RADIUS FOR WHICH THIS WORLD MAP IS BEING ',
      * 'CALCULATED IS R =' D25 15,/////,
                THE C ARRAY CONTAINING THE GEOPOTENTIAL UNCER''S IS. ()
      * /
C
       PRINT OUT THE C ARRAY CONTAINING THE GEOPOTENTIAL UNCER'S
C
C
       CALL OUTCOF(C, MAXDEG, MAXORD, 1)
С
       INDO = 180 DO/DLAT + 1
       IND1 = 360.DO/DLON + 1
С
       ENTER LATITUDE LOOP
С
С
       WRITE(6,390)
  390 FORMAT( 1
                           NON-SPHERICAL ACCELERATION AS A FUNCTION',
      * ' OF LATITUDE AND LONGITUDE')
С
       ALAT = (DLAT + 90 D0)
       DO 1000 I=1, INDO
       IF ( MOD(I,2) .NE O AND. I GT 1 ) WRITE(6,401)
  401 FORMAT('1')
       WRITE(6,400)
  400 FORMAT(/)
          ALAT = ALAT - DLAT
          A_{11}I) = ALAT
          ALAT1 = ALAT
          IF ( ALAT GE. 90.D0 ) ALAT1 = ALAT - 1 O
IF ( ALAT LE -90 D0 ) ALAT1 = ALAT + 1 O
          SINP = DSIN(DTR*ALAT1)
          COSP = DCOS(DTR*ALAT1)
++C 112,112
С
      ENTER LONGITUDE LOOP
С
С
      ALON = -(DLON + O DO)
      DO 2000 J = 1, IND1
          ALON = ALON + DLON
          A2(J) = ALON
          ALAM = DTR*ALON
-+C 205
      PLAMDA = PLAMDA / ( R * COSP)
++C 209
      PPSI = PPSI/R
С
      COMPUTE ACCELERATION
C
```

~

.

```
С
       ACC = DSQRT(PS*PS + PLAMDA*PLAMDA + PPSI*PPSI)
С
       WRITE(6,500) ALAT1, ALON, ACC
  500 FORMAT(' ALAT=', G14 8, ' ALON=', G14 8, ' ACC=', G14 8)
С
С
       LOAD PLOT ARRAY
С
       PLOT(I,J) = ACC*FACTOR + 0.5
С
 2000 CONTINUE
С
 1000 CONTINUE
С
С
   ******** GENERATE PLOT *******
                                                                  -
Ĉ
       WRITE(6,700)
  700 FORMAT('1',//,T36,' UNCERTAINTY IN NONSPHERICAL GRAVITATIONAL',
* ' ACCELERATION (MGAL)',/,2X,'<LAT>' 3X,/)
C
       DO 800 I=1, INDO
          WRITE(6,750) A1(I), VERT, (PLOT(I, J), J=1, IND1)
  750
          FORMAT(3X, 13, 3X, A1, 4013)
  800 CONTINUE
С
  WRITE(6,770) HORZ,(A2(I).I=1,IND1,2)
770 FORMAT(/,T10,115A1,//,2X,'<LONG>',2X,I3,19I6)
                             *******
С
  *********
IF ( 5 NE O )STOP
++WRITE WORK, SPART
```

.

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B.2 UTILITY FOR COMPUTING GRAVITATIONAL ACCELERATION UNCER-TAINTIES ALONG THE TRAJECTORY OF A USER SATELLITE

This SEA utility computes the gravitational acceleration uncertainties that result from a given geopotential error model as a user satellite travels in its orbit. The utility computes and prints out a table of radial, crosstrack, and alongtrack components; the magnitudes of the gravitational acceleration uncertainties; and the latitude and longitude of the ground trace of the satellite, for each error budget time requested.

The data are then presented in five separate plots. The first four plots show the radial (height), crosstrack, and alongtrack components and the magnitudes of the gravitational acceleration uncertainties, respectively, as a function of time from epoch. The last plot shows the magnitudes of the gravitational acceleration uncertainties as the satellite moves in its orbit as a function of latitude and . longitude.

B.2.1 INPUT DATA SETUP

This utility can be executed using the SEA keyword cards setup, and no special keyword cards are required. The geopotential error model can be set up the same way as described in Section B.1.1.

B.2.2 MODIFICATIONS TO SEA PROGRAM

In subroutine RDKEYS, which reads in keyword cards, modifications are made so that the first real field (Rl) on the LUMPGEOP keyword card can be used as a scaling factor (multiplication factor) to the sine and cosine coefficients uncertainties of an input geopotential error model. This provides a convenient means to scale down or scale up the coefficients to study the effect of an error model.

In subroutine FORCE, which calculates force per unit mass acting on the satellite for the integration of the nominal trajectory, additional codings are added to print out a table of time from epoch; latitude; longitude; radial, crosstrack, and alongtrack components; and the magnitudes of the gravitational acceleration uncertainties whenever current time equals error budget time. This subroutine is modified so that, for each error budget time, SPART is called twice: the first time for computing the geopotential acceleration uncertainties due to the geopotential error model; the second time to help in computing the nominal trajectory of the user satellite. The acceleration uncertainties computed are stored in separate arrays for later plotting purpose. To be able to recognize the error-budget time, the calling sequence of FORCE is also modified to include the input of the variable EBTIME.

Subroutine FORCE is called from subroutine INTAG for each of the integration steps for the propagation of the satellite trajectory. Coding modification is therefore required in INTAG whenever FORCE is invoked using the modified calling sequence. The calling sequence (argument list) of INTAG is also modified with the addition of the variable EBTIME, to be able to transfer the error-budget time to FORCE.

Subroutine SEQUEN, which controls the forward sequential filter computation, specifies the variable EBTIME, which is passed to subroutine INTAG through its calling sequence.

Modifications are made to suppress the error-budget and standard deviation correlation output reports. In addition, a new subroutine, GTPLOT, is added at the end of the filter computation to generate five separate plots (Section B.2). GTPLOT uses the arrays previously loaded in subroutine FORCE to generate the required plots.

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Minor modifications are also made in subroutine SEAOl to suppress the error summary reports and error plots. In addition to the nonspherical gravitational accelerations or acceleration uncertainties, the calling sequence of subroutime SPART is modified to pass the latitude and longitude of the user satellite to the calling subroutine, FORCE.

Subroutine THCL is also modified to output the 3 by 3 transformation matrix for transforming the gravitational acceleration uncertainties from inertial coordinates to height, crosstrack, and alongtrack coordinates.

B.2.3 REQUIRED CODING UPDATES TO SEA PROGRAM

The following is the listing of Panvalet updates to the Panvalet SEA source program stored in the data set GCDEV.MVT.SEA.PANLIB.DATA. To create an updated SEA program load module, the updates that follow must be compiled and linked to the existing SEA load module GCDEV.SEAMVS.LOAD.

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```
-+UPDATE FORCE, 1, TEMP
++C 1,1
       SUBROUTINE FORCE ( T , ISAT , D2Y , ACCEL , EBTIME)
++C 40
       LOGICAL*1 LTOOUT
++C 45.45
       COMMON/CONST / AE, GM, DUMMY(5), RTD
       COMMON/FMODEL/C(30,33),CSIG(30,33)
      COMMON/GTRACK/GTMIN(96), GALAT(96), GALAM(96), GGRAV(96,3), GG(96),
     * IGCNT
      DIMENSION CTEMP(30,33)
       DATA DEBTIM / -1 ODO /
++C 50
      DIMENSION GRAV(3), TR(3,3)
С
       LTOOUT - TRACKING ORIENTED OUTPUT FLAG
      LTOOUT = .FALSE
       IS EBTIME A NEW ERROR BUDGET TIME
С
       IF ( EBTIME NE. CEBTIM ) LTOOUT = TRUE
++D 72
С
С
       GENERATE THE TRACKING ORIENTED OUTPUT ONLY DURING ERROR
С
       BUDGET REQUEST TIMES
С
       IF ( T .NE EBTIME ) GO TO 550
       IF ( NOT. LTOOUT ) GO TO 550
С
      FIND THE ACCELERATION DUE TO GEM UNCERTAINTIES CONTAINES IN CSIG
С
С
       - BUT FIRST STORE THEM IN ARRAY C BECAUSE THIS IS THE ARRAY ACTED
С
         UPON BY SUBROUTINE SPART
С
      DO 510 IROW = 1,30
          DO 515 ICOL =1,33
             CTEMP(IROW, ICOL) = C(IROW, ICOL)
             C(IROW, ICOL) = CSIG(IROW, ICOL)
  515
          CONTINUE
 . 510 CONTINUE
       CALL SPART(X, XDD, ALAT, ALAM)
      DO 530 IROW = 1,30
          DO 535 ICOL =1,33
             C(IROW, ICOL) = CTEMP(IROW, ICOL)
          CONTINUE
  535
  530 CONTINUE
       CALL THCL1(STATE(1, ISAT), TR)
       CALL MATMUL(TR, XDD, GRAV, 3, 3, 1)
       G = DSQRT(GRAV(1)*GRAV(1)+GRAV(2)*GRAV(2)+GRAV(3)*GRAV(3))
       ALAT = RTD * ALAT
       ALAM = RTD * ALAM
       IF ( ALAM GE O ODO ) GO TO 537
       IMULT = 1.0DO + DABS(ALAM / 360 DO)
       ALAM = ALAM + DFLOAT(IMULT) * 360 ODO
  537 TMIN = T / 60 0D0
С
С
       LOAD ARRAYS USED LATER FOR PLOTTING
С
      IGCNT = IGCNT + 1
       GTMIN(IGCNT) = TMIN
      GALAT(IGCNT) = ALAT
      GALAM(IGCNT) = ALAM
      GGRAV(IGCNT,1) = GRAV(1)
GGRAV(IGCNT,2) = GRAV(2)
      GGRAV(IGCNT, 3) = GRAV(3)
      GG(IGCNT) = G
С
  WRITE(6,500) TMIN,ALAT,ALAM,GRAV,G
500 FORMAT(' TMIN=',G17 10,' ALAT=',G14 8,' ALAM=',G14 8,
+ ' GRAV= ',3(G14 8,1X),' G=',G14 8)
      OEBTIM = EBTIME
  550 CALL SPART(X, XDD, ALAT, ALAM)
++WRITE WORK, FORCE
++UPDATE INTAG, 1, TEMP
++C 1,1
      SUBROUTINE INTAG(T1, T2, PXX, TXU, PXZ, D2Y, YDY, YDY1, RK, ACCEL, EBTIME)
++C 244,244
```

```
CALL FORCE (T, ISAT, D2Y, ACCEL, EBTIME)
++C 295 295
      CALL FORCE(T, ISAT, D2Y, ACCEL, EBTIME)
++WRITE WORK, INTAG
++UPDATE RDKEYS, 1, TEMP
++C 229,229
      DPMAP(ILUMP) = 1 ODO
      IF ( R1 NE O ODO ) DPMAP(ILUMP) = R1
++C 251,252
      CSIG(I1, I2+1 ) = R1 * DPMAP(ILUMP)
      CSIG(31-I1, 33-I2 ) = R2 * DPMAP(ILUMP)
++WRITE WORK, RDKEYS
++UPDATE SEQUEN, 1, TEMP
++C 167
      COMMON/GTRACK/GTMIN(96), GALAT(96), GALAM(96), GGRAV(96, 3), GG(96),
      * IGCNT
++C 176,177
++C 207
      IGCNT = 0
++C 292,292
   95 CALL INTAG(TIME, TTO, PXX, TXU, PXZ, D2Y, YDY, YDY1, RK, ACCEL, EBTIME)
++D 343,346
++D 412,413
++C 458,459
С
С
      GENERATE GEOPOTENTIAL TRACK ERROR PLOTS
С
  800 CALL GTPLOT(EBSTOP)
++WRITE WORK, SEQUEN
++UPDATE SEA01, 1, TEMP
++C 216,216
      SUPPRESS ERROR SUMMARY REPORT AND PLOT, BECAUSE THIER EXECUTION
С
С
          IN COMBINATION WITH THESE UPDATED, RESULTS IN A SOC1 ABEND
С
      CALL OUTRSS
С
++C 220,220
С
      CALL PLTHLC
++WRITE WORK, SEA01
++UPDATE SPART, 1, TEMP
++C 1,1
      SUBROUTINE SPART ( X, XDD, ALAT, ALAM )
++C 93
      ALAT = DARSIN(SINP)
++WRITE WORK, SPART
++UPDATE THCL, 1, TEMP
++C 4,4
      SUBROUTINE THCL1 ( X, T )
++R 17,,/6,6/3,3/
++D 35,37
++D 55,61
++WRITE WORK, THCL
++INSERT WORK
      SUBROUTINE GTPLOT(EBSTOP)
С
      IMPLICIT REAL*8(A-H.O-Z)
С
      COMMON/GTRACK/GTMIN(96), GALAT(96), GALAM(96), GGRAV(96,3), GG(96).
     * IGCNT
С
      DIMENSION TPLOT(53, 103), XLINE(101), YLINE(53)
      DIMENSION XLAB(11), SYM(4)
      DIMENSION PLOT(40,111), DIGITS(36)
      LOGICAL*1 HORZ(113), VERT, SLASH
      INTEGER*2 A1(40), A2(40)
      DATA DLAT/5 DO/, DLON/10 DO/, FACTOR/1 D5/
DATA HORZ/113*'-'/, VERT/'I'/, SLASH/' '/
С
      DATA SYM /'H',
                    Ϋ́ĊΫ́.
Ϋ́LΎ.
     *
     *
                    'R'/
     *
              DOT /' '/,
      DATA
             DASH /'-'/,
     ×
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ANILET /'I /,
      *
             BLANK / ' ' ,
      ×
            OVERFL / ' * '/
      *
      * OVERFL / '*'/
DATA DIGITS/'0', '1', '2', '3', '4',
* '5', '6', '7', '8', '9',
* 'A', 'B', 'C', 'D', 'E',
* 'F', 'G', 'H', 'I', 'J',
* 'K', 'L', 'M', 'N', 'D',
* 'P', 'Q', 'R', 'S', 'T',
* 'U', 'V', 'W', 'X', 'Y',
* 'Z'/
      *
      *
      *
      *
      ×
С
       D0 5 ICOL = 4, 112, 6
       HORZ(ICOL) = SLASH
     5 CONTINUE
       HORZ(1) = VERT
       HORZ(113) = VERT
С
       DO 7 I=1,40
           DO 8 J=1,111
              PLOT(I,J) = BLANK
     8
           CONTINUE
     7 CONTINUE
С
c
       BUILD XLINE AND YLINE
       DO 10 I=1,101
    10 XLINE(I) = DASH
       DO 20 I=1,101,10
    20 \text{ XLINE(I)} = D0T
       DO 30 I=1,53
    30 YLINE(I) = ANILET
       DO 40 I=2,52,5
  - 40 YLINE(I) = DOT
С
c
       INITIALIZE ARRAY TPLOT AND LOAD AXIES
       DO 50 ICOL=2,102
           DO 60 IROW=2,52
               TPLOT(IROW, ICOL) = BLANK
    60
           CONTINUE
    50 CONTINUE
       DO 80 I=2,102
           TPLOT(1,I) = XLINE(I-1)
TPLOT(53,I) = XLINE(I-1)
    80 CONTINUE
        DO 90 I=1.53
           TPLOT(I,1 ) = YLINE(I)
           TPLOT(I, 103) = YLINE(I)
    90 CONTINUE
¢
С
       FIND MAX AND MIN OF THE GEOPOTENTIAL ACCELERATIONS
С
       AMAX = -1 \text{ OD} - 50
       AMIN = 1 0D+50
       DO 200 I=1, IGCNT
           IF ( GG(I) GT. AMAX ) AMAX = GG(I)
           DO 210 ISET=1,3
               IF ( GGRAV(I, ISET) LT AMIN ) AMIN = GGRAV(I, ISET)
  210
           CONTINUE
  200 CONTINUE
       WRITE(6,4000)AMAX,AMIN
 4000 FORMAT('0**** AMAX = ',D25 15,' AMIM = ',D25 15,/)
С
cc
       FIND SCALING FOR THE X AXIES
       IEBED = EBSTOP/60 ODO + 5DO
       IEBST = 0 0
       IXSCAL = ( ( DFLOAT(IEBED) - DFLOAT(IEBST))/100 ODO ) + 99999DO
       XSCAL = IXSCAL
       IXMIN = IEBST
 WRITE(6,4010)EBSTOP,IEBED,IEBST,XSCAL,IXMIN
4010 FORMAT('0***** EBSTOP =',D14 7,' IEBED = ',I6,' IEBST =',I6,
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*' XSCAL =',D14 7,' IXMIN =',I6,/) -
C
С
      FIND SCALING FOR THE Y AXIES
С
      YRANGE = ( AMAX - AMIN ) * 1 OD5
      YSCAL = YRANGE / 50 ODO
      YTEMP = YSCAL * 5 ODO
C ROUND YTEMP UP TO NEAREST
                               1 MG
      IYTEMP = ( YTEMP * 10 ODO ) +
                                       99999DO
      YTEMP = DFLOAT(IYTEMP) / 10 DO
      YSCAL = YTEMP / 5 ODO
      YMIN = ( ( AMIN * 1.0D5 ) / YRANGE ) * ( YSCAL * 50 0D0 )
C ROUND YMIN DOWN TO NEAREST . 1 MG
      IYTEMP = YMIN * 10 DO
      IF ( YMIN LT 0 ODO ) IYTEMP = ( YMIN * 10 DO ) - 99999DO
      YMIN = DFLOAT(IYTEMP) / 10 DO
      YMAX = YMIN + 50 ODO * YSCAL
      WRITE(6,4020) YRANGE, YSCAL, YMIN, YMAX
 4020 FORMAT('0**** YRANGE =', D14 7,' YSCAL =', D14 7,' YMIN =', D14 7,
     *' YMAX =', D14 7,/)
С
С
      LOOP OVER ALL FOUR PLOTS
С
        WHERE. ISET = 1, HEIGHT PLOT (H)
                        2, CROSS TRACK PLOT (C)
3, ALONG TRACK PLOT (L)
С
C
С
                        4, RSS PLOT (R)
C
      DO 500 ISET = 1.4
С
С
        LOAD INDIVIDUAL POINTS IN TO ARRAY TPLOT
C
         YCOR = YMIN / YSCAL
 WRITE(6,4040) ISET,YCOR
4040 FORMAT('0**** ISET =',I3,' YCOR =',D14 7,/)
         DO 600 I = 1, IGCNT
             IXCOL = ( GTMIN(I) / XSCAL ) + 5DO
IF ( ISET LT 4 )
                IYROW = ( (GGRAV(I, ISET) * 1 OD5 ) / YSCAL ) - YCOR + 5
             IF ( ISET EQ. 4 )
      * IYROW = ( (GG(I) * 1 OD5) / YSCAL ) - YCOR + 5
WRITE(6,4050)IYROW,IXCOL,SYM(ISET)
 4050 FORMAT(' **** IYROW =', I5, ' IXCOL =', I5, '
                                                       USING SYMBOL->', A1)
             TPLOT(52-IYROW, IXCOL+2) = SYM(ISET)
  600
         CONTINUE
С
С
        PRINT OUT ARRAY TPLOT ONE ROW AT A TIME
С
         WRITE(6,2000)
 2000 FORMAT('1', T10, 'PLOT OF TRACK ACCELERATIONS FROM THE ',
     *'GEOPOTENTIAL UNCERTAINTY, IN MGAL',//)
         YVAL = YMAX + 5.0 * YSCAL
         DO 700 IROW = 1,53
             WRITE(6,2010) (TPLOT(IROW, ICOL), ICOL=1,103)
 2010 FORMAT(' ', T14, 103A1)
             IF ( MOD(IROW-2,5) NE 0 ) GO TO 800
             YVAL = YVAL - 5 0 * YSCAL
             WRITE(6,2050)YVAL
 2050 FORMAT( '+', T3, F10.2)
         CONTINUE
  800
      LATER ON ONE MAY WISH PLACE HERE THE CODE TO GIVE
С
С
      Y-AXIS LABELS
  700
         CONTINUE
         IXVAL = IXMIN - 10 * IXSCAL
         DO 900 I=1,11
             IXVAL = IXVAL + 10 * IXSCAL
             XLAB(I) = IXVAL
         CONTINUE
  900
 WRITE(6,2100)XLAB
2100 FORMAT(' ',T8,11F10 2,//,T47
     * 'TIMES FROM EPOCH IN MINUTES')
С
      BEFORE PRINTING NEXT PLOT, BLANK OUT TPLOT ARRAY
С
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IF ( ISET EQ 4 ) GO TO 500
          D0 1006 ICDL=2,102
             DO 1010 IROW=2,52
                 TPLOT(IROW, ICOL) = BLANK
 1010
             CONTINUE
 1000
          CONTINUE
  500 CONTINUE
С
С
      LOAD PLOT ARRAY TO GENERATE LONGITUDE LATITUDE PLOT
С
      DO 1020 II=1, IGCNT
      I = 19 5D0 - ( GALAT(II) / DLAT )
      ALAMT = GALAM(II)
      JCOL = ( ALAMT / 3 3333D0 ) + 3.5D0
      AMGAL = GG(II) * FACTOR + 0 5
      IMGAL = AMGAL
      IF ( IMGAL LE 36 ) GD TO 1018
      PLOT(I, JCOL) = OVERFL
      GO TO 1020
 1018 CONTINUE
      WRITE(6,4060)II,GTMIN(II),II,GALAT(II),ALAMT,AMGAL,I,JCOL
 4060 FORMAT(' **** GTMIN(',12,')=',F7.2,' GALAT(',12,')=',
* D14.7,' ALAMT=',D14 7,' AMGAL=',F6 2,' I=',I3,' JCDL=',I3)
С
      PLOT(I, JCOL) = DIGITS ( IMGAL + 1 )
С
 1020 CONTINUE
С
C
      GENERATE LATITUDE/LONGITUDE PLOT
С
      INDO = 180 ODO / DLAT + 1
      IND1 = 360 OD0 / DLON + 1
      ILONGV = 0
      ILATV = 90
      DO 1025 I=1,40
      A1(I) = ILATV
ILATV = ILATV - 5
      A2(I) = ILONGV
      ILONGV = ILONGV + 20
 1025 CONTINUE
      WRITE(6, 1030) HORZ
 1030 FORMAT('1',//,T36,' UNCERTAINTY IN NONSPHERICAL GRAVITATIONAL',
                           ' ACCELERATION (MGAL)',/,2X,'<LAT>',3X,/,
     *
                            9X, 115A1)
     *
С
      DO 1040 I=1,INDO
          WRITE(6, 1050) A1(I), VERT, (PLOT(I, J), J=1, 111), VERT
         FORMAT(3X, I3, 3X, A1, 111A1, A1)
 1050
 1040 CONTINUE
С
 WRITE(6,1060) HORZ,(A2(I),I=1,19)
1060 FORMAT(' ',T10,113A1,//,10X,I3,18I6,//,60X,
     * '<LONG>')
      RETURN
      END
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