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EIGENSYSTEM SYNTHESIS FOR ACTIVE FLUTTER SUPPRESSION ON AN OBLIQUE-WING AIRCRAFT

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Abstract

The application of the eigensystem synthesis technique to place the closed-loop eigenvalues and shape the closed-loop eigenvectors has not been practical for active flutter suppression, primarily because of the availability of only one control surface (aileron) for flutter suppression. The oblique-wing aircraft, because of its configuration, provides two independent surfaces (left and right ailerons), making the application of eigensystem synthesis practical. This paper presents the application of eigensystem synthesis using output feedback for the design of an active flutter suppression system for an oblique-wing aircraft. The results obtained are compared with those obtained by linear quadratic Gaussian techniques.

Symbols

A	plant matrix
B	control matrix
C	output matrix
I	identity matrix
K	eigensystem gain matrix
L	partitioned matrix of specified components of $(\lambda_i I - A)^{-1} B$
\bar{L}	complex conjugate transpose of L
M	partitioned matrix of unspecified components of $(\lambda_i I - A)^{-1} B$
u	input vector
V	eigenvector matrix
v_i	closed-loop eigenvector
v_i^a, v_i^d	achievable and desired eigenvectors, respectively
v_i^*	complex conjugate of v_i
x	state vector

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y

output vector

λ_i, λ_i^*

closed-loop eigenvalue and its conjugate

σ

minimum singular value of the return difference matrix

Introduction

The U.S. Navy and NASA are currently involved in the design and development of an unsymmetric-skew-wing aircraft capable of 65° wing sweep and flight at Mach 1.6. Such a unique configuration exhibits aeroelastic behavior distinctly different than that of straight, swept-back, or swept-forward wings and has a potential for poor modal response characteristics. The most serious result of such characteristics can be flutter, an unstable motion caused by an interaction between structural vibrations and aerodynamic forces.¹ Active suppression of aerodynamic wing flutter can result in substantial weight savings and increases in performance compared with passive methods such as increased structural stiffness and mass balancing.

The synthesis of modal control systems for unsymmetric aircraft requires considerably more states than are necessary for symmetric configurations because all degrees of freedom must be adequately represented in a single formulation. The model representing the aircraft must include rigid-body modes, flexible modes, unsteady aerodynamics, actuators, and gust states. Control laws have been formulated for active flutter control using the standard linear quadratic Gaussian (LQG) procedure;²⁻⁴ the synthesized optimal feedback control laws are of the same order as the aircraft plant. Practicalizing the control law requires order reduction by techniques such as transfer function matching, modal truncation, and residualization.⁵⁻⁷

To investigate modal control synthesis strategies for an oblique-wing configuration, a generic skew-wing aircraft model was developed for 45° wing skew at a flight condition of Mach 0.70 at 10,000 ft altitude. At this flight condition the aircraft has an unstable flutter mode. An active implementable flutter control law was developed⁸ using the LQG design technique and modal residualization to reduce the order of the controller. However, this method increased the order of response of the closed-loop system as compared with that of the open-loop system and degraded modal control characteristics.

Eigensystem synthesis procedures are suitable for flight control system design because they do not increase the order of the system. Also, the difficulty in incorporating specifications such as damping, frequency, and decoupling within a quadratic performance index makes the eigensystem synthesis procedure a promising design alternative. The performance specifications can be interpreted in terms of desired closed-loop eigenvalues and eigenvectors. Moore⁹ and others have shown how feedback can be used to place closed-loop eigenvalues and shape closed-loop eigenvectors. References 10 to 12 successfully demonstrate the use of an eigenstructure assignment procedure for aircraft control system design.

The eigensystem synthesis technique using output feedback to place closed-loop eigenvalues and shape closed-loop eigenvectors has not been used for active flutter suppression, primarily because of the availability of only one control surface for flutter suppression, making eigenvector shaping impractical. The oblique-wing aircraft, because of its configuration, provides two independent control surfaces (left and right ailerons) and makes the application of eigensystem synthesis practical.

This paper presents the application of eigensystem synthesis to the design of an active flutter suppression system for a generic model of an oblique-wing aircraft. The results obtained are compared with those obtained by LQG techniques.

Flutter Suppression Using Eigenstructure

The generic oblique-wing aircraft aerodynamic model used in the system synthesis process is a simple beam representation of the fuselage and wing. The aerodynamic model was developed by superimposing aero panels over the beams, as shown in Fig. 1. The aircraft modal characteristics were developed using NASTRAN analysis. At the sweep configuration (45°) and flight condition (Mach 0.70, 10,000 ft) selected, the unaugmented aircraft has a flutter mode characterized as primarily wing bending. Because the intent of this paper is to demonstrate a design synthesis process, the model order was reduced considerably; the final model contained a rigid-body (primarily pitch) mode along with three elastic modes. The model reduction process did not significantly affect the flutter mode characteristics. Details of the aircraft model formulation are given in Ref. 8.

The aircraft design model includes the linearized form of the unsteady aerodynamics, actuators, and gust model dynamics and can be represented as

$$\dot{x} = Ax + Bu \quad (1)$$

$$y = Cx \quad (2)$$

where x is a 24×1 state vector, y is a 5×1 output vector, u is a 2×1 input vector, and A , B , and C are the plant, control, and output matrices, respectively, of suitable dimensions. The 24 states include the rigid-body mode, flexible mode deflections, flexible mode rates, unsteady

aerodynamic states, actuator deflection and rate states, and wind gust states. Eight states result from the retained structural modes, eight from the two-lag-term set of approximated unsteady aerodynamics, six from the two actuators, and two from the gust model. The five outputs consist of pitch angle, pitch rate, and three accelerations: center of gravity and right and left wingtips. The two inputs are right and left aileron deflections.

For the system under consideration, the following conditions hold:¹¹

1. A maximum of five closed-loop eigenvalues can be assigned arbitrarily with the stipulation that if λ_i is a complex closed-loop eigenvalue, its complex conjugate λ_i^* must also be a closed-loop eigenvalue.
2. A maximum of five eigenvectors can be altered. If the shape of a complex eigenvector v_i is altered, its complex conjugate v_i^* must be altered in the same way.
3. For each eigenvector whose shape is altered, a maximum of two eigenvector elements can be chosen arbitrarily.

4. Achievable eigenvectors must lie in the subspace spanned by the columns of $(\lambda_i I - A)^{-1}B$ of dimension two, which is the number of independent control variables. A desired eigenvector v_i^d will in general not reside in the prescribed subspace and cannot be achieved. The optimal achievable eigenvector v_i^a is obtained by the orthogonal projection of v_i^d onto the subspace spanned by $(\lambda_i I - A)^{-1}B$.

Given the system of equations (1) and (2) and assuming an output feedback, the control input u is given by

$$u = Ky \quad (3)$$

where K is the gain matrix of dimension 2×5 . For the closed-loop system, the following relationship holds:

$$(A - BKC)v_i = \lambda_i v_i \quad (4)$$

where v_i is a closed-loop eigenvector and λ_i a closed-loop eigenvalue; or

$$(\lambda_i I - A)v_i = -BKCv_i = Bm_i \quad (5)$$

where

$$m_i = -KCv_i \quad (6)$$

In general, the desired eigenvector v_i^d does not reside in the achievable subspace, and an approxi-

mate solution by methods of orthogonal projection can be obtained.¹³

If

$$L_i = (\lambda_i I - A)^{-1} B \quad (7)$$

then the achievable eigenvector v_i^a is given by

$$v_i^a = L_i (\bar{L}_i^* L_i)^{-1} \bar{L}_i^* d \quad (8)$$

and the gain K is given by

$$K = -M(CV)^{\dagger} \quad (9)$$

where the superscript \dagger denotes pseudoinverse, \bar{L}_i^* is the complex conjugate transpose of L_i , and

$$M = [M_1 \ M_2 \ \dots \ M_n] \quad (10)$$

$$V = [v_1^a \ v_2^a \ \dots \ v_n^a] \quad (11)$$

Results

The control law synthesized by the method outlined was applied to the design of an active flutter suppression controller for an oblique-wing aircraft. A generic 45° wing-skew structural model was developed to simulate flutter at a subsonic flight condition of Mach 0.70 and an altitude of 10,000 ft.

Table 1 gives the eigenvalues of the open-loop aircraft model. The unstable eigenvalue pair at this flight condition ($0.5 \pm 14.37i$) represents primarily wing bending.

The design objective was to stabilize the aircraft without exceeding the specified root-mean-square (rms) control activity so that saturation would not occur. Based on actuator limitations, the rms deflection of the aileron was limited to 5° and the deflection rate to 30 deg/sec. In addition to stabilizing the aircraft with low surface activity, it is required that the controller be robust. The controller considered here is multi-input, multi-output: the right and left wing control surfaces are independent of each other because of the unsymmetric nature of the aircraft. Robustness of the multi-loop control system is evaluated by using the singular values of the return difference matrix.¹⁴

The process of selecting desired closed-loop eigenvalues and eigenvectors for the case under consideration presents a problem. The selection of desired eigenvalues and eigenvectors normally is based on engineering judgment and requires a clear insight into physical aspects of the plant being controlled. Most of the physical insight for the flutter problem is lost in the process of model reduction from the original large dimensions to the 24th-order model developed for the control system synthesis process.

A time-consuming and arbitrary method for the selection of eigenvectors did lead to stabilization of the aircraft. Another method, using closed-loop eigenvalues and eigenvectors obtained through LQG design assuming full-state feedback, was used to obtain a stable closed-loop system. The closed-loop eigenvalues and eigenvectors obtained by this method were selected as the desired eigenvalues and eigenvectors for the eigensystem synthesis process.

Table 2 gives the desired locations of the five closed-loop eigenvalues as well as the desired eigenvectors. Five eigenvalues were located, including the unstable flutter mode, at the desired location. The achieved eigenvectors are given in Table 2. The feedback gain K was evaluated based on the achieved eigenvalues and eigenvectors. The values of K and the closed-loop eigenvalues of the aircraft are also indicated in Table 2.

Table 3 gives the comparative description of the rms values of response to gust input for both the LQG design⁸ (seventh-order controller) and the controller designed using eigensystem synthesis. The eigensystem synthesis rms values for the surface deflections and rates are within the prescribed range and compare favorably with those obtained by the other method.

The controller developed by this method (K is a 2×5 matrix) is extremely simple to implement. In comparison, the LQG design technique uses a full-order controller (the order being the same as that of the plant). Even a reduced-order controller is difficult to implement and increases the order of the system.

However, this eigensystem synthesis approach compromises robustness. Stability robustness of multi-input, multi-output feedback control systems is characterized by the minimum singular value of the return difference matrix of the plant input or output.¹⁴ Figure 2 shows the plots of the minimum singular values σ for the controller developed in this paper and the full-state feedback controller developed using the LQG technique.⁸ A degradation in robustness is evident from the plot. However, the reduced-order controller is not as robust as the one designed using the eigensystem procedure, as is evident from Fig. 2.

Conclusions

An implementable flutter controller for a 45°-skew oblique-wing aircraft mathematical model was designed using the eigensystem synthesis technique. The controller does not increase the order of the system and is extremely simple to implement, whereas the LQG design technique uses a full-order controller, is difficult to implement, and increases the order of the system. Work is in progress to improve stability margins by using constrained optimization techniques to shape the singular value spectrum.¹⁵ A standard performance index is minimized while trying to satisfy minimum singular value constraints at the plant input or output, or both.

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Table 1 Open-loop
eigenvalues

0.0000 + 0.0000i
-0.4187 + 0.0000i
-0.4229 + 0.0000i
-4.2075 + 0.0000i
-0.1612 + 5.0036i
-0.1612 - 5.0036i
-1.9397 + 14.0551i
-1.9397 - 14.0551i
0.5011 + 14.3649i
0.5011 - 14.3649i
-20.0000 + 0.0000i
-20.0000 + 0.0000i
-30.8526 + 0.0000i
-35.1822 + 0.5223i
-35.1822 - 0.5223i
-37.1170 + 3.5647i
-37.1170 - 3.5647i
-39.6927 + 0.6080i
-39.6927 - 0.6080i
-41.3346 + 0.0000i
-36.4000 + 37.1354i
-36.4000 - 37.1354i
-36.4000 + 37.1354i
-36.4000 - 37.1354i

Table 2 Eigensystem variables

Desired eigenvectors (from LQG method)						Desired eigenvalues
3.9999	0.0438 + 0.0049i	0.0438 - 0.0049i	0.0015 + 0.0007i	0.0015 - 0.0007i		-0.0003 + 0.0000i
0.0000	-0.0317 + 0.0018i	-0.0317 - 0.0018i	-0.0245 + 0.0089i	-0.0245 - 0.0089i		-0.2355 - 5.0020i
0.0000	0.0011 + 0.0001i	0.0011 - 0.0001i	0.0023 + 0.0004i	0.0023 - 0.0004i		-0.2355 + 5.0020i
0.0000	0.0047 + 0.0001i	0.0047 - 0.0001i	-0.0004 + 0.0004i	-0.0004 - 0.0004i		-0.5041 - 14.3657i
-0.0010	-0.0349 + 0.2177i	-0.0349 - 0.2177i	-0.0104 + 0.0216i	-0.0104 - 0.0216i		-0.5041 + 14.3657i
0.0000	-0.0017 - 0.1588i	-0.0017 + 0.1588i	-0.1154 - 0.3565i	-0.1154 + 0.3565i		
0.0000	-0.0009 + 0.0057i	-0.0009 - 0.0057i	-0.0075 + 0.0330i	-0.0075 - 0.0330i		
0.0000	-0.0014 + 0.0236i	-0.0014 - 0.0236i	-0.0054 - 0.0065i	-0.0054 + 0.0065i		
0.0746	2.8445 + 16.2616i	2.8445 - 16.2616i	-6.5976 - 0.9621i	-6.5976 + 0.9621i		
0.0612	1.9139 + 5.3855i	1.9139 - 5.3855i	2.4618 + 6.5556i	2.4618 - 6.5556i		
-0.0247	-7.3179 - 74.9682i	-7.3179 + 74.9682i	2.4855 - 3.2472i	2.4855 + 3.2472i		
0.0829	0.9809 - 29.5832i	0.9809 + 29.5832i	10.8184 - 32.7421i	10.8184 + 32.7421i		
-0.0699	-2.6257 - 15.7088i	-2.6257 + 15.7088i	7.1162 + 3.8695i	7.1162 - 3.8695i		
-0.0578	-1.6892 - 3.9659i	-1.6892 + 3.9659i	-2.0765 - 5.6525i	-2.0765 + 5.6525i		
0.0015	6.1769 + 73.0802i	6.1769 - 73.0802i	-2.6786 - 0.0123i	-2.6786 + 0.0123i		
-0.1024	-1.9195 + 26.9120i	-1.9195 - 26.9120i	-12.8369 + 31.1018i	-12.8369 - 31.1018i		
0.0000	0.0000 + 0.0001i	0.0000 - 0.0001i	0.0004 + 0.0003i	0.0004 - 0.0003i		
0.0000	-0.0003 + 0.0001i	-0.0003 - 0.0001i	-0.0050 + 0.0055i	-0.0050 - 0.0055i		
0.0000	-0.0006 - 0.0016i	-0.0006 + 0.0016i	-0.0766 - 0.0740i	-0.0766 + 0.0740i		
0.0000	0.0000 + 0.0000i	0.0000 - 0.0000i	0.0009 + 0.0001i	0.0009 - 0.0001i		
0.0000	0.0000 + 0.0000i	0.0000 - 0.0000i	0.0016 + 0.0130i	0.0016 - 0.0130i		
0.0000	-0.0001 + 0.0001i	-0.0001 - 0.0001i	-0.1878 + 0.0159i	-0.1878 - 0.0159i		
0.0000	0.0000 + 0.0000i	0.0000 - 0.0000i	0.0000 - 0.0000i	0.0000 + 0.0000i		
0.0000	0.0000 + 0.0000i	0.0000 - 0.0000i	0.0000 - 0.0000i	0.0000 + 0.0000i		
Achieved eigenvectors						Achieved closed-loop eigenvalues
3.9999	0.0438 + 0.0049i	0.0438 - 0.0049i	0.0015 + 0.0007i	0.0015 - 0.0007i		-0.0003 + 0.0000i ^a
0.0000	-0.0317 + 0.0018i	-0.0317 - 0.0018i	-0.0245 + 0.0089i	-0.0245 - 0.0089i		-0.4187 + 0.0000i
0.0000	0.0011 + 0.0001i	0.0011 - 0.0001i	0.0023 + 0.0004i	0.0023 - 0.0004i		-0.4229 + 0.0000i
0.0000	0.0047 + 0.0001i	0.0047 - 0.0001i	-0.0004 + 0.0004i	-0.0004 - 0.0004i		-3.6775 + 0.0000i
-0.0010	-0.0349 + 0.2177i	-0.0349 - 0.2177i	-0.0104 + 0.0216i	-0.0104 - 0.0216i		-0.2355 + 5.0020i ^a
0.0000	-0.0017 - 0.1588i	-0.0017 + 0.1588i	-0.1154 - 0.3565i	-0.1154 + 0.3565i		-0.2355 - 5.0020i ^a
0.0000	-0.0009 + 0.0057i	-0.0009 - 0.0057i	-0.0075 + 0.0330i	-0.0075 - 0.0330i		-1.3818 + 12.9445i
0.0000	-0.0014 + 0.0236i	-0.0014 - 0.0236i	-0.0054 - 0.0065i	-0.0054 + 0.0065i		-1.3818 - 12.9445i
0.0746	2.8445 + 16.2616i	2.8445 - 16.2616i	-6.5976 - 0.9621i	-6.5976 + 0.9621i		-0.5041 + 14.3657i ^a
0.0612	1.9139 + 5.3855i	1.9139 - 5.3855i	2.4618 + 6.5556i	2.4618 - 6.5556i		-0.5041 - 14.3657i ^a
-0.0247	-7.3179 - 74.9682i	-7.3179 + 74.9682i	2.4855 - 3.2472i	2.4855 + 3.2472i		-23.1705 + 0.0000i
0.0829	0.9809 - 29.5832i	0.9809 + 29.5832i	10.8184 - 32.7421i	10.8184 + 32.7421i		-21.2819 + 13.9913i
-0.0699	-2.6257 - 15.7088i	-2.6257 + 15.7088i	7.1162 + 3.8695i	7.1162 - 3.8695i		-21.2819 - 13.9913i
-0.0578	-1.6892 - 3.9659i	-1.6892 + 3.9659i	-2.0765 - 5.6525i	-2.0765 + 5.6525i		-34.5807 + 1.0410i
0.0015	6.1769 + 73.0802i	6.1769 - 73.0802i	-2.6786 - 0.0123i	-2.6786 + 0.0123i		-34.5807 - 1.0410i
-0.1024	-1.9195 + 26.9120i	-1.9195 - 26.9120i	-12.8369 + 31.1018i	-12.8369 - 31.1018i		-39.5120 + 1.8798i
0.0000	0.0000 + 0.0001i	0.0000 - 0.0001i	0.0004 + 0.0003i	0.0004 - 0.0003i		-39.5120 - 1.8798i
0.0000	-0.0003 + 0.0001i	-0.0003 - 0.0001i	-0.0050 + 0.0055i	-0.0050 - 0.0055i		-39.9263 + 0.0000i
0.0000	-0.0006 - 0.0016i	-0.0006 + 0.0016i	-0.0766 - 0.0740i	-0.0766 + 0.0740i		-30.2236 + 29.6354i
0.0000	0.0000 + 0.0000i	0.0000 - 0.0000i	0.0009 + 0.0001i	0.0009 - 0.0001i		-30.2236 - 29.6354i
0.0000	0.0000 + 0.0000i	0.0000 - 0.0000i	0.0016 + 0.0130i	0.0016 - 0.0130i		-49.9016 + 16.2655i
0.0000	-0.0001 + 0.0001i	-0.0001 - 0.0001i	-0.1878 + 0.0159i	-0.1878 - 0.0159i		-49.9016 - 16.2655i
0.0000	0.0000 + 0.0000i	0.0000 - 0.0000i	0.0000 - 0.0000i	0.0000 + 0.0000i		-33.5655 + 41.6373i
0.0000	0.0000 + 0.0000i	0.0000 - 0.0000i	0.0000 - 0.0000i	0.0000 + 0.0000i		-33.5655 - 41.6373i
Eigensystem feedback gain matrix, K						
0.0000	0.0004	-0.0006	-0.0001	0.0002		
0.0000	0.0009	-0.0010	-0.0001	-0.0001		

^aSee desired eigenvalues.

Table 3 Root-mean-square responses at flutter conditions

	Right wing		Left wing	
	δ , deg	$\dot{\delta}$, deg/sec	δ , deg	$\dot{\delta}$, deg/sec
Full-state feedback	1.58	7.91	0.28	3.58
Full-order controller with Kalman estimator	1.58	12.58	0.41	5.64
Full-order controller with robust Kalman estimator	2.06	11.21	0.41	5.02
Reduced-order controller	1.51	10.04	0.41	4.90
Eigensystem synthesis	0.62	4.81	0.69	8.46

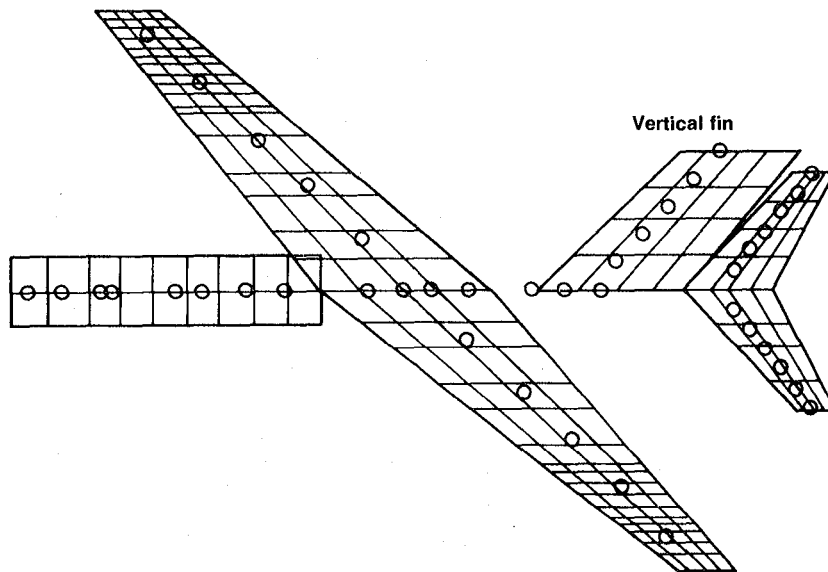


Fig. 1 Generic model (aero panels and node points). Vertical fin shown in X-Y plane.

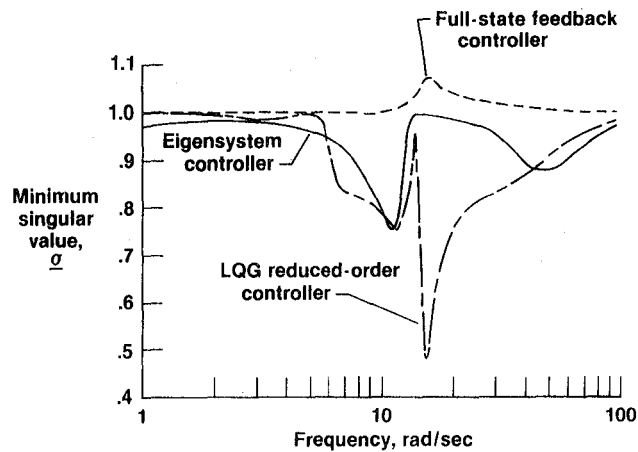


Fig. 2 Minimum singular values of the return difference matrix.

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