



OPTIMIZATION OF ORBITAL ASSIGNMENT AND SPECIFICATION

OF SERVICE AREAS IN SATELLITE COMMUNICATIONS

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CHAPTER I

INTRODUCTION

Since the launch of the first commercial communications satellite, the INTELSAT I, in April 1965, satellite communications have become more and more popular internationally [1,2,3]. Not only does the number of satellites continue to increase, but the demand for future satellite services is growing rapidly [3,4]. This situation creates a problem of how to provide enough satellite communications capacity to satisfy all the potential users. The study of this report is devoted to contributions toward solving this problem by developing methods that can efficiently utilize the spectrum and orbit resources.

The most popular satellite orbit for the civil communications services is the geostationary orbit [5,6]. The idea of using this orbit was proposed by Arthur C. Clarke [1]. However, the geostationary orbit can accommodate only a limited number of satellites for a given frequency channel because satellites that have the same frequency channel must be properly separated from one another in space for acceptable interference protection [6]. When the geostationary orbit is considered "crowded" with satellites, it is crowded in terms of electromagnetic compatibility. This requirement greatly limits the satellite capacity of the geostationary orbit.

A method of increasing the communications capacity is to increase the spectral band available for satellite communications use. The

spectral region of interest lies between the maximum usable frequency (MUF) for reflection by the ionosphere and the first oxygen absorption line (about 60 GHz) [7]. By international agreement, this spectral region is divided into many bands for various services, e.g., the broadcasting-satellite service (BSS), the fixed-satellite service (FSS), the military service, navigation, weather detection, etc [2,8]. As a result, only a limited number of spectral bands are available for the civil communications services.

As an example of the large demand for satellite communications, when the 11 to 12 GHz spectral band for civil satellite service was opened for use on an international basis, every administration requested some frequency channels [4]. Even those administrations that do not need, or cannot afford, a satellite at the present time requested channel assignments for future use. Therefore, lack of enough spectrum and orbit resources becomes a serious problem with regard to planning for future communications satellite traffic, i.e., orbital and frequency allocations.

The goal of the orbital and frequency planning task is to use the limited amount of resources to provide enough communications capacity to satisfy every potential user. The main concern of the planning task is to ensure that mutual interference between different satellite systems is acceptable; a poorly planned scenario would be likely to result in unacceptable carrier-to-interference ratios (C/I), and hence unacceptable signal quality, for at least some users. To avoid this, the satellite orbital locations and frequency channel allocations should

be carefully planned. This planning task becomes very difficult when the number of satellites and channels to be assigned becomes large.

Moreover, since the demand for present and future communications satellites is large, it is important to use the available spectrum and orbit resources efficiently. In other words, the objective is to achieve the maximum information-transfer capacity for the resources allocated.

In 1977, the spectral band 11.7 to 12.5 GHz was assigned to Region 1 and the band 11.7 to 12.2 GHz to regions 2 and 3 for the planning of the BSS. The administrations in Regions 1 and 3 completed the planning in the 1977 World Administrative Radio Conference (WARC-77) [9]. The plan was based generally on spacing the satellites uniformly at 6 degrees, when they are assigned the same frequency channel [10]. The administrations in Region 2 delayed the planning process in WARC-77, with the intention of making the most efficient use of the geostationary orbit and the spectral band [11,12]; then proposed a plan at the Regional Administrative Radio Conference in 1983 (RARC-83) [13,14]. Planning for the fixed-satellite communications service (FSS) has been deferred to conferences in 1988 or beyond. Therefore, a method is needed to solve the assignment problem in as near an optimal way with regard to this objective as possible.

Much work has been done on this problem. Several studies discuss some important factors that should be considered in the assignment problem. A study by D. J. Withers identifies three areas that should be exercised in order to achieve effective resource utilization [15]. The

first area is engineering for an interference-limited environment by properly using the antenna characteristics, signal modulation, and multiple-access techniques to minimize the interference power. The second area is effective inter-system coordination. It includes: 1) proper pairing of the up- and down-link bands, 2) a standard frequency translation between up- and down-link bands, 3) an agreed scale of permissible single-entry interference noise allocation, 4) maximization of the satellite service arc by easing the satellite elevation angle constraint. The third area is the reduction of inhomogeneity in orbit-spectrum sharing. Also in the Final Acts of the WARC-77, the importance of placing satellites as close as possible for efficient orbit utilization is expressed [16]: the satellite spacing should be small, while still keeping the mutual interference acceptable.

Some studies deal with the orbital assignment problem alone. A Japanese study tackles the problem of orbit utilization through a non-linear programming optimization procedure with the objective of minimizing the total orbital arc used for a scenario [17]. The basic approach is to relate the satellite geocentric angular separation to the interference power; the problem is formulated as a non-linear programming problem and the sequential unconstrained minimization technique is applied to solve it numerically. Another Japanese study modified the above program so that it can find the optimal orbital assignment for a new satellite when it is inserted into an existing scenario [18]. The result is optimal in the sense of finding the best location for the new satellite, while making some modification to the

existing scenario, such that the satellite separations or, equivalently, the interference powers still meet the requirements. The best location for inserting the new satellite is chosen so that the total orbital arc occupied by the final result is minimized. To carry out rigid planning of many satellites, an evolutional model is used by repeatedly using the modified program to assign satellite locations one by one, and the ordering of insertion must first be chosen. It is not obvious, and appears unlikely, that the quality of the result is independent of this ordering.

Some studies deal with the frequency assignment problem alone. The methods of map-coloring and dot-linkage have been proposed to achieve the most conservational use of the spectrum resource [19,20,21,22]. A Japanese study tackles this problem by rearranging the frequency assignment of a given scenario that has an initial optimal orbital assignment [23]; e.g., orbital assignment is obtained from [17] with the frequency assignments assumed the same for all satellites. Therefore, in this Japanese study the frequency assignment, identified as a permutation problem, is handled independently of the orbital assignment; it is formulated as an integer program and the optimal permutation is obtained via the branch-and-bound method. When the new frequency assignments are made, the required satellite orbital separations may be reduced. The objective is the minimization of the total orbital arc occupied by the final scenario. Note that the combination of the two Japanese studies [17,23] becomes a complete package that solves the orbital and frequency assignments in two steps.

Some studies deal with both the orbital and frequency assignments. Some of these are aimed more at obtaining a better understanding of the problem than at actually solving it [24,25]. An application-oriented research group in Canada developed a software package for planning synthesis in connection with RARC-83 [26,27,28]. It is a multiple-stage process, and one of the objectives spelled out in the report is the minimization of the total orbital arc occupied by the scenario. First the minimum required orbital separations that meet the single-entry protection ratio are calculated for all pairs of satellites. These data are calculated in the following four cases: co-polarization and co-channel, co-polarization and adjacent channel, cross-polarization and co-channel, cross-polarization and adjacent channel. The initial scenario is an equal-spaced orbital assignment with co-channel, co-polarization frequency assignment. Then, the computer program can let the planner make changes both manually and automatically in the channel and/or polarization assignments, and manually in the orbital assignments. The program always produces a scenario, even if it turns out not to meet the required protection ratios. The result is a local. optimum and not necessarily a global optimum.

Two methods have been proposed by a research group at the Ohio State University. The first method uses an extended gradient search technique to improve an existing scenario [29]. A sum of negative exponentials of the aggregate effective C/I ratios is used as the objective function to be minimized; therefore the procedure seeks to maximize the smallest of all such C/I ratios. The gradient direction of the objective function at the point representing the existing scenario

is calculated; then the objective function values at some discrete points along the negative of this direction are found. The point yielding the most favorable (minimum) objective function value is chosen as a new scenario to start another search process. The iterative process stops when a better scenario can not be found. The second method is called the cyclic coordinate search method [30]. In this method each orbital and frequency variable is varied in turn. Each time a set of points is examined, the point yielding the most favorable objective function value is selected as the new coordinate value for that variable. A cycle is completed when all the orbital and frequency variables have been varied once. The cyclic process is repeated with suitably adjusted step sizes until it reaches a solution where the improvement of C/I results halts. The detailed description of the two methods is given in Chapter III.

Transmission of a signal from the Earth terminal and its reception at a satellite constitutes an up-link; and transmission of a signal from a satellite and its reception at the Earth terminal constitutes a down-link. By international agreement, the up-link signals and the down-link signals are not in the same spectral band, so that the signals will not interfere with each other [31]. In this study only the regulation of the down-link traffic is considered. The up-link problem can be implemented similarly in another spectral band. Note that the above studies [17,26,27,28,29,30] also deal only with the down-link communications traffic regulation.

In Chapter II, some of the important factors and parameters involved in the carrier and interference power calculations are

discussed. Note that in this study an effective carrier-to-interference power ratio is used to evaluate the feasibility of a scenario; in Section II.F it will be shown that this is equivalent to the more usual margin calculation.

In Chapter III, the objective function to be minimized in the extended-gradient and cyclic-coordinate search techniques to improve a given scenario is analyzed [29]. It is shown that this function has large values when two (or more) orbital or frequency assignments are collocated; this indicates that both the signal quality requirement and the permutation of the orbital/frequency assignments need to be looked into in order to find the globally optimal scenario. Furthermore, some arguments are given which indicate that the objective function is likely to be a function with only one local minimum for a fixed permutation of orbital and frequency assignments; even though a definitive proof has eluded us, a set of numerical examples are presented which support these arguments. This suggests that a sufficient condition for obtaining the globally optimal solution by the extended-gradient search method is that it should terminate as an ordinary gradient search with the optimal permutation in orbital and frequency assignments.

In Chapter IV, a different approach, the ΔS concept, is presented. It is shown that the single-entry C/I protection requirement is equivalent to a required minimum satellite separation; hence the highly non-linear C/I requirement can be viewed as constraints on the satellite locations. With this approach the orbital assignment can be formulated as a mixed-integer program and solved by the branch-and-bound method; or

it can be formulated as a linear program with non-linear side constraints and solved by a version of the simplex method for linear programming with restricted basis entry.

Chapter V intends to show that an important body of information for choosing FSS service areas is the communications-demand density. It is proposed that the service areas of an FSS system should be specified according to the communications-demand density in conjunction with the concept of small-beam design; the frequency re-use scheme can be implemented through small beams and well-separated service areas. A case study demonstrates that the communications supply for the United States could be significantly increased if the service areas are specified according to these principles. The ΔS concept presented in Chapter IV is used in this case study.

CHAPTER II

DESCRIPTION OF PARAMETERS AND FACTORS IN C/I CALCULATIONS

A. INTRODUCTION

The feasibility of a scenario is evaluated according to the signal quality [32], which is usually expressed in terms of the signal-to-noise ratio (S/N) [33]. For instance, the unweighted signal quality requirement for 625-line, color-television signal is suggested to be a S/N ratio of 33 dB for 99% of the worst month [34]. The signal power (S) is measured in the baseband channel after modulation improvement and baseband processing [35,36]. For the purpose of planning the broadcasting-satellite service (BSS), the requirement is that the pre-detection carrier-to-noise ratio (C/N) at the receiver input should equal or exceed 14 dB for 99% of the worst month or 10 dB for 99.9% of the worst month [37,38].

The noise power includes the receiver thermal noise (N_t) and all the interference powers from other communications systems [39]. In order that the interference powers from other communications systems will not further degrade the C/N level, the total (or aggregate) interference power level should be weak enough so that its contribution to the total noise power is negligible.

There are several criteria how weak the total interference power should be [40,41]; two which are commonly used are the interference-to-thermal noise ratio (I/N_t) and the carrier-to-interference power ratio (C/I) [40]. In this study the C/I criterion is used to evaluate the feasibility of a scenario, with a minor modification. Account must be taken of the fact that a given interference level at the same frequency as the desired carrier is more damaging than the same level of interference at a far removed frequency. This can be done by multiplying each interference power at a non-carrier frequency by a relative protection factor (less than unity) before adding the interference powers to obtain an effective ratio (C/I_e). This is discussed in more detail in Section II.F, where it is also shown that this formulation is fully equivalent to the more usual, but less convenient, representation in terms of margins.

In the following sections some of the important factors and parameters involved in the C/I_e calculation are discussed.

B. SATELLITE

A satellite is a relay terminal, its basic function is to receive signals from some Earth stations and to re-transmit them to other Earth stations. It has receiving and transmitting antennas, and a frequency translator [42,43] or, in some cases, more sophisticated signalprocessing circuits which include frequency shifting.

A satellite may use any orbit to travel [2], but the geostationary orbit is the most popular orbit for civil communications. In this orbit

the satellite position is almost stationary with respect to any place on Earth; thus complicated satellite tracking systems at the Earth terminals may be avoided. This orbit is directly above the equator at a height of 37,165 kilometers above the Earth surface [2]. By international agreement this will be the main orbit for civil communications services [5,6]. Therefore, in this study only this orbit is considered.

Because the satellite is away from the Earth, it is possible to control its position and attitude only to a certain precision. A satellite drifts away from its designated orbital location and its position needs to be adjusted from time to time [44,45]. With present technology, a satellite orbital location may be maintained within 0.1 degree in the north-south and east-west directions, resulting in 0.14 degree of maximum excursion [44]. As for attitude control, the transmitting antenna pointing error may be kept within 0.1 degree, and the tolerance in the rotation about the beam axis is typically two degrees [44,45]. For the calculations of this report, the pointing error may be taken into account through the minimum elliptical beam calculation to be discussed in Section II.D, or through the antenna discrimination function to be discussed in Section II.E. The satellite rotational error may be taken into account through the minimum elliptical beam calculation to be discussed in Section II.D.

C. SERVICE AREA

A service area is a designated area on the Earth surface to which a corresponding satellite directs its signals. Actually an antenna transmits its signal in all directions according to its pattern function, even though its target area is of limited size. By international agreement, a service area should be illuminated by its satellite main beam within the -3 dB contour of that beam [46,47]. This means that the received power density at any point in the service area should be within 3 dB of the power density at the antenna aim point.

For simplicity, a service area is represented by a set of test points at its boundary. To evaluate the C/I_e results of a scenario, one calculates the C/I_e values at all the test points of all the service areas, and compares them with the C/I_e requirement level. Because the interference is likely to be the worst on the service area boundaries, a scenario with satisfactory C/I_e values at all the test points should guarantee that the C/I_e values will be good at all the places inside all the service areas. The test points are also used to generate the minimum elliptical beam parameters to be discussed in Section II.D.

In this study a satellite and its corresponding service area(s) are viewed as a communications system. A service area may have several satellites, but all of these satellites are treated independently of one another.

D. MINIMUM ELLIPTICAL BEAM

The antenna main beam (-3 dB contour) of a satellite to its designated service area should be shaped, using available antenna technology, to fit the shape of the service area as suitably as possible [48]. However, a reference antenna pattern for shaped beams is still unavailable, i.e., there exists no internationally agreed method for predicting, for regulatory purposes, the discrimination to be expected from shaped beams outside their respective service areas. In order to analyze a scenario in terms of C/I_e results, the interference powers are therefore calculated by assuming that a service area is illuminated by a minimum elliptical beam from the satellite position that covers all the test points of that service area [47].

This minimum ellipse is specified by five parameters: the longitude and latitude of the beam aim point, the orientation angle, and the major- and minor-axis beam widths. In Figure 2.1, the aim point, which is on the Earth surface, is denoted as A. The antenna beam plane is a plane perpendicular to the satellite beam axis, SA, and passing through the aim point A. The vectors AM and AN denote the major and minor axes. The beam widths in the directions of these two axes, viewed from the satellite, are ψ_{max} and ψ_{min} , respectively. The orientation angle, which is not shown, is the angle measured anti-clockwise in the antenna beam plane from a line parallel to the equatorial plane to the major axis of the ellipse. The more detailed descriptions of these parameters can be found in a National Telecommunication and Information Administration (NTIA) document [49].



Figure 2.1. Minimum ellipse configuration.

To generate the ellipse data, one needs to specify the nominal satellite location and the locations of a set of test points; other parameters that can be specified are the minimum beam width, minimum elevation angle, satellite pointing error and rotational error. The resulting elliptical cone covers all the test points that are used to generate this ellipse; in a worst-case calculation that includes the specified satellite pointing error and rotational error. A computer program developed by Akima was used to generate the five ellipse parameters for the calculations of this report [49].

With these parameters, the half-power beam width (HPBW), ψ_{to} , with respect to any test point, T, on the Earth surface can be calculated by means of a somewhat involved procedure. First the vector AP of Figure 2.1 is calculated, where P is the intersection of the line ST and the antenna beam plane. Then, the angle σ between the vector AP and the major axis AM is calculated. The length of AR is calculated from

$$AR = AM \cdot [\cos^{2}(\sigma) + A_{r}^{2} \cdot \sin^{2}(\sigma)]^{-1/2}, \qquad (2.1)$$

where A_r , called the axial ratio of the elliptical beam, is the ratio between AM and AN. Then it is assumed that the ratios between the angles ψ_{max} , ψ_{min} , ψ_{to} and their corresponding arcs AM, AN, AR are the same; this is a very good approximation when the angles are not large. With this approximation, the angle ψ_{to} is calculated from

$$\Psi_{to} = \Psi_{max} \cdot [\cos^2(\sigma) + A_r^2 \cdot \sin^2(\sigma)]^{-1/2}$$
, (2.2)

where A can be seen as the ratio between ψ_{max} and ψ_{min} .

The off-axis angle, $\psi_{\mbox{t}}$, toward the point T is calculated by the cosine law

$$\cos(\psi_t) = (ST^2 + SA^2 - AT^2)/(2 \cdot ST \cdot SA),$$
 (2.3)

where ST, SA, AT denote distances in Figure 2.1.

The off-axis angle ψ_t and the corresponding HPBW ψ_{to} will be used to calculate the directivity of the antenna toward the specific point, T. The antenna pattern envelopes used to calculate the directivity will be described in Section II.E.

The detailed description of all the parameters and the formulations of all the calculations can be found in the Spectrum Orbit Utilization Program (SOUP) manual [50]. A streamlined SOUP code is listed in Appendix A. It is much less complicated than the original SOUP code. The basic calculation is exactly the same, but with fewer options. For instance, the streamlined version does not consider propagation loss.

E. ANTENNA REFERENCE PATTERNS AND PROTECTION RATIO

Two sets of antenna reference patterns are used in the study. They are representations, adopted by the International Radio Consultative Committee (CCIR), of the envelopes of real antenna patterns. Their use therefore should result in a near worst-case interference power calculation. The first set includes the satellite transmitting antenna reference patterns and the ground receiving antenna reference patterns suggested in the International Radio Consultative Committee Conference

Preparatory Meeting in 1982 (CCIR-CPM-82) for the Regional Administration Radio Conference for Region 2 in 1983 (RARC-83) [10,51,52]. These are the BSS patterns. The gain, G, of the transmitting antenna is calculated from [53,54]

$$G = e \cdot [(\pi/\psi_{max})/(180/223)]^2 \cdot A_r , \qquad (2.4)$$

where the symbols mean

e : the beam efficiency, taken as 0.6 in this study, ψ_{max} : the beam width of the major axis, in radians, A_r : the axial ratio of the elliptical beam.

The ground receiving antenna gain in the BSS calculations is taken as 40.2 dB, corresponding to a circular-beam antenna of 1-meter diameter, 12 GHz carrier frequency and 0.6 beam efficiency. The reference patterns are shown in Figures 2.2 and 2.3, and are used in the calculation of the objective function values in Chapter III.

In Figures 2.2 and 2.3, both the transmitting and receiving antennas have two reference patterns with mutually orthogonal polarizations. The transmitting antenna transmits signals of the designated polarization according to the co-polarization pattern, at the same time it also transmits orthogonally polarized signals according to the cross-polarization pattern. The receiving antenna receives the wanted signals according to the co-polarization pattern by aligning its polarization parallel to that of the wanted signal. Any signal that is co-polarized with the wanted signal is received according to the



A: co-polar component (dB)

$-12(\psi/\psi_0)^2$	for	0	<	ψ/ψο	<	1.58
$17 = 25 \cdot 10 \cdot (1 + 1)$	TOP	1.58	<u> </u>	Ψ/Ψο	<	3.16
$-17.5-25 \log(\psi/\psi_0)$	tor	3.16	<	ψ/ψ_0		
after intersection with curve	C: a	s curv	/e	C		

B: cross-polar component (dB)

C: minus the on-axis gain (dB), (G=42.5 dB in this illustration) ψ : off-axis angle ψ_0 : half-power beam width

Figure 2.2. BSS satellite transmitting reference patterns.



A: co-polar component without side-lobe suppression (dB)

0	for	ψ/ψ_{0}	<	0.25
$-12(\psi/\psi_{0})^{2}$	for 0.25	$\langle \psi/\psi_0$	<	0.94
$-11.3-25 \cdot \log(\psi/\psi_0)$	for 0.94	$\langle \psi/\psi_0$	<	18.88
-43.2dB (-3dBi)	for 18.88	$\langle \psi/\psi_0$		

B: cross-polar component (dB)

```
-25
                                           for
                                                     0 < \psi/\psi_0 < 0.25
 -30-40 \cdot \log[1-\log(\psi/\psi_0)]
                                                \begin{array}{rrrr} 0.25 < \psi/\psi_{0} < 0.44 \\ 0.44 < \psi/\psi_{0} < 1.28 \end{array}
                                           for
 -20
                                           for
 -17.3-25 \cdot \log(\psi/\psi_0)
                                                1.28 < \psi/\psi_0 < 3.22
                                           for
         until intersection with co-polar component curve;
 -30
         then as for co-polar component
\psi: off-axis angle,
\psi_0: half-power beam width
Half-power beam width = 1.8 degrees
Nominal on axis gain = 40.2 \text{ dB}
Flat portion for \psi/\psi_0 less than 0.25 takes account the antenna
```

pointing error

Figure 2.3. BSS ground receiving reference patterns.

co-polarization pattern, and any signal that is cross-polarized with the wanted signal is received according to the cross-polarization pattern. These unwanted signals constitute the interference power at the receiver input.

In the second set of reference antenna patterns, intended for the fixed-satellite service (FSS) calculations, the satellite transmitting antenna reference pattern given in Figure 2.4 is a modified version of the fast fall-off reference pattern from CCIR-CPM-82/RARC-83 [55]. This modified reference pattern had been suggested as useful for the FSS systems [56,57]. The transmitting antenna gain is again calculated from Equation (2.4). The ground receiving antenna reference pattern, shown in Figure 2.5, is a modified version of the reference pattern from the International Radio Consultative Committee (CCIR-82) Report 391-4 [58]. The modification is suggested in a CCIR-82 Recommendation and in the CCIR-CPM-82/RARC-83 Report [59,60], and should become the standard in the year 1987. The receiving antenna gain is 43.2 dB, corresponding to a circular-beam antenna of 4.5-meter diameter, 4 GHz carrier frequency and 0.6 beam efficiency. Note that there is no cross-polarization pattern in Figure 2.4 because such a pattern has not been adopted by the international committee.

The relative protection ratio, $PR(dB)-PR_0(dB)$, used in Chapter III is taken from a CCIR-CPM-82 Report [61] and is shown in Figure 2.6. The value of PR_0 is the co-channel protection ratio; the value of the actual protection ratio $PR(dR)-PR_0(dB)$ depends on the carrier frequency offset between the wanted and unwanted signals as well as on the modulation



relative gain below on-axis gain (dB)

 $\begin{array}{ccccccc} -12(\psi/\psi_0)^2 & \mbox{for} & 0 & <\psi/\psi_0 < 0.5 \\ -18.75^{\circ}\psi_0^{2} \cdot [(\psi/\psi_0) - \alpha]^2 & \mbox{for} & (0.4/\psi_0) + \alpha & <\psi/\psi_0 & <(1.265/\psi_0) + \alpha \\ -30 & \mbox{for} & (1.265/\psi_0) + \alpha & <\psi/\psi_0 & <1.585 \\ -24-30^{\circ}\log(\psi/\psi_0) & \mbox{for} & 1.585 & <\psi/\psi_0 \\ & \mbox{after intersection with } -G: \mbox{ as } -G \end{array}$

 $\begin{array}{l} \psi : \text{ off-axis angle} \\ \psi_o: \text{ half-power beam width} \\ \alpha : \text{ by definition: } \alpha = 0.5[1-(0.8/\psi_o)] \\ \text{G}: \text{ on-axis gain} \\ \text{In the figure, G} = 38.8 \ \text{dB}, \ \psi_o = 2 \ \text{degrees.} \end{array}$





relative gain below on axis gain (dB)

 ψ : off-axis angle ψ_0 : half-power beam width G : on-axis gain Half-power beam width = 1.17 degrees G : 43.2 dB





0	for		B	<	0.274
$-35.6(\beta -0.274)$	for 0.274	<	B	<	0.92
-23-71(β -0.92)	for 0.92	<	ß		

PR₀: co-channel protection ratio
 β : normalized frequency offset unit
 = (f_{unwanted} - f_{wanted})/(Carson's bandwidth)

Figure 2.6. BSS frequency protection ratio.
method of the signals [62]. The Carson bandwidth will be taken as 25.2 MHz, which is appropriate for the BSS TV/FM case.

F. RECEIVED-POWER CALCULATION

Refer to Figure 2.7 for the geometry, but note that the radius of the Earth relative to that of the geostationary orbit is exaggerated greatly for clarity. In this figure, the satellites assigned to service areas A, B are designated S_A , S_B , respectively. The aim points of S_A , S_B are the points a, b. The point d is one of the test points in A. The test points are normally chosen on the boundary of their service areas because interference is likely to be the worst there. The minimum ellipses of A, B from S_A , S_B are labeled E(A), E(B). For the test point d, the off-axis angle of the $S_{\mbox{\scriptsize A}}$ signal and the corresponding HPBW in the direction toward d are $\psi_{\texttt{tc}},\,\psi_{\texttt{tco}};\,\texttt{the subscript}$ c is meant as a mnemonic for carrier. The distance from S_A to d is x. These values are used to calculate the carrier power received from S_A at d. Also, for test point d, the off-axis angle of the S_R signal and the corresponding HPBW are designated ψ_{ti} , ψ_{tio} , respectively. Since the receiving antenna at the test point d is pointed at S_A , its off-axis angle toward S_B is ψ_{ri} . The distance from S_B to d is y. These values are used to calculate the interference power received from S_B at d.

Referring to Figure 2.7, the carrier power, C, at d is calculated by means of the Friis transmission equation [63,64]:



Figure 2.7. Configuration of received-power calculation.

$$C = \frac{P_{A} \cdot G_{A} \cdot D_{A}(\psi_{tc}) \cdot G_{d} \cdot c^{2}}{f_{A}^{2} \cdot (4\pi)^{2} \cdot x^{2}} , \qquad (2.5)$$

where the symbols mean

- P_A : the transmitting power of S_A ,
- $G_{\mbox{\scriptsize A}}$: the transmitting antenna gain of $S_{\mbox{\scriptsize A}}$,
- D_A : the co-polarization transmitting antenna discrimination from S_A in the direction toward d,
- G_d : the receiving antenna gain at d,
- c : the velocity of light,
- f_A : the carrier frequency.

In Chapter III, the effective isotropic radiated powers are assumed constant for all the satellites. In Chapters IV and V, it is assumed that the carrier power densities at the aim points are equal for all the service areas [65]; therefore, all the satellite transmitting powers are adjusted to meet this requirement.

The interference power received at d must be calculated with care because there may be a polarization mismatch between the wanted and unwanted signals. Both of the orthogonally polarized signals transmitted from S_B must be decomposed into two components, one that is parallel to the wanted signal of the receiver and the other that is orthogonal. With the proper choice of the antenna reference patterns, the received interference power from each component is calculated from

$$I = \frac{P_{B} \cdot G_{B} \cdot D_{B}(\psi_{ti}) \cdot G_{d} \cdot D_{d}(\psi_{ri}) \cdot c^{2}}{f_{B}^{2} \cdot (4\pi)^{2} \cdot y^{2}}$$
(2.6)

where the symbols mean

 P_B : the transmitting power of S_B ,

 G_B : the transmitting antenna gain of S_B ,

- D_B : the transmitting discrimination from S_B to d,
- G_d : the receiving antenna gain at d,
- D_d : the receiving antenna discrimination from d in the direction toward S_B when the antenna is pointed at S_A , f_B : the interference frequency.

The total interference power is the summation of all the components. For instance when the signals of S_A and S_B are co-polarized, the received interference power at d from S_B is calculated from [64,66]

$$I_{cp} = I_{tc,rc} + I_{tx,rx} + (I_{tc,rx} + I_{tx,rc}) \cdot D_{x}$$
, (2.7a)

when they are cross-polarized, the received interference power is calculated from

$$I_{xp} = I_{tc,rx} + I_{tx,rc} + (I_{tc,rc} + I_{tx,rx}) \cdot D_{x}$$
 (2.7b)

Here the subscripts mean

- cp : wanted and unwanted signals are co-polarized,
- xp : wanted and unwanted signals are cross-polarized,
- tc : signal transmitted according to the co-polarized reference
 pattern,
- tx : signal transmitted according to the cross-polarized
- rc : signal received according to the co-polarized reference
 pattern,

rx : signal received according to the cross-polarized reference pattern.

The term D_X is the rain depolarization factor [66,67]. Since the propagation effect is not considered in this report, the term D_X is taken to be zero. Also, Equation (2.7a) is further simplified as

$$I_{cp} = I_{tc,rc} , \qquad (2.7c)$$

because the cross-polarization component, which arises from the crosspolarized patterns of both the transmitting and receiving antennas, is negligible compared to the co-polarization component. Finally it should be noted that Equation (2.7b) is an approximation. In an actual case, these terms should add as phasors, not in a power sense; but to perform that calculation the relative phases of the tc, tx patterns and that of the rc, rx patterns would have to be known. So, without the term n_x , a worst-case formula would be

$$I_{xp} = (\sqrt{I_{tc,rx}} + \sqrt{I_{tx,rc}})^2$$
 (2.7d)

When the carrier frequencies of the wanted and unwanted signals are different, a frequency filtering factor must be included in the effective interference power calculation. The proper expression for such a filtering factor can be easily obtained as follows. When evaluating the effect of the unwanted signal, the usual procedure is to calculate a term called the protection margin M_i from

$$M_{i}(dB) = (C/I_{i})(dB) - PR_{i}(dB),$$
 (2.8)

where the symbols mean

i : index of frequency channel of the wanted signal,

I₁ : total interference power in channel i,

PR_i : protection ratio against interference power in channel
 i.

The interference power is acceptable when the value of $M_i(dB)$ is positive. (When there are several interference signals of the same carrier frequency, their total interference power is obtained by decomposing every polarized signal into parallel and orthogonal components with respect to the wanted signal, then calculating each interference power and summing them, as discussed above.) When there are several unwanted signals of different carrier frequencies, the equivalent protection margin, M, that evaluates the over-all effect of the interference power is calculated from [68,69]

$$M(dB) = -10 \cdot \log \left[\sum_{i} 10^{-M_{i}(dB)/10} \right], \qquad (2.9)$$

where each term M_i is the protection margin in one frequency channel, and the summation is over all frequency channels. Equation (2.9) can be re-written as

$$M(dB) = -10 \cdot \log(\sum_{i} 10^{-\{(C/I_{i})(dB) - PR_{i}(dB)\}/10})$$

$$= -10 \cdot \log(\sum_{i} 10^{-\{(C/I_{i})(dB) - [PR_{i}(dB) - PR_{0}(dB)]\}/10} \cdot 10^{PR_{0}(dB)/10})$$

$$= -10 \cdot \log(\sum_{i} 10^{-\{(C/I_{i})(dB) - [PR_{i}(dB) - PR_{0}(dB)]\}/10}) - PR_{0}(dB)$$

$$= C(dB) - 10 \cdot \log(\sum_{i} 10^{\{I_{i}(dB) + [PR_{i}(dB) - PR_{0}(dB)\}/10}) - PR_{0}(dB)$$

If the equivalent total, or aggregate effective interference power, I_e , is defined from the expression of the equivalent protection margin, M, as

$$M(dB) = (C/I_e)(dB) - PR_O(dB)$$

= C(dB) - I_e(dB) - PR_O(dB) , (2.11)

(2.10)

then the equivalent aggregate interference power can be expressed as

$$I_{e}(dB) = 10 \cdot \log(\sum_{i} 10^{\{I_{i}(dB) + [PR_{i}(dB) - PR_{0}(dB)]\}/10})$$
(2.12)

Therefore, the quantity $[PR_i(dB)-PR_o(dB)]$, which is the relative protection ratio in Figure 2.6, can be interpreted as a filtering factor operating on the interference power when the carrier frequencies of the wanted and unwanted signals are different, and denoted as $F(f_{wanted}, f_{unwanted})(dB)$. This approach will be taken throughout Chapter III. For a scenario of many satellites and where each satellite has many frequency channels, the aggregate effective interference power, I_{knj}^{e} , received in channel n at test point j in service area k is calculated from a power summation of terms of the type given in Equation (2.12),

$$I_{knj}^{e}(dB) = 10 \cdot \log\{ \sum_{i \in K/k} \sum_{m \in N_{i}} 10^{[Iim,knj(dB)+F(f_{n},f_{m})(dB)]/10} + I_{i \in K/k} \sum_{m \in N_{i}} 10^{[Iim,knj(dB)+F(f_{n},f_{m})(dB)+F(f_{n},f_{m})(dB)]/10}$$

$$\Sigma = 10^{[I_{km,knj}(dB) + F(f_n,f_m)(dB)]/10}$$

$$\sum_{m \in N_k/n} \{2.13a\}$$

or

$$I_{knj}^{e} = \sum_{i \in K/k} \sum_{m \in N_{i}} I_{im,knj} F(f_{n},f_{m}) + \sum_{m \in N_{k}/n} I_{km,knj} F(f_{n},f_{m})$$
(2.13b)

where the symbols mean

- K/k : the index set of all the satellites, excluding satellite Sk,
- N_i : the index set of all the channels assigned to satellite i,
- Iim,knj : the single-entry interference power from channel m of S_i, received at channel n of test point j in service area k,
- $F(f_n,f_m)$: the relative protection ratio between the carrier frequency f_n and interference frequency f_m , as shown in Figure 2.6.

The aggregate (C/I_e) value in a channel at test point d is obtained by calculating the values of C using Equation (2.5) and I_e using Equation (2.13b) and dividing.

G. SIGNAL QUALITY REOUIREMENT

When the signal quality requirement is stated as "S/N be no less than 30 dB for 99% of the worst month" [38], the main concern is to obtain satisfactory performance except during rare, large attenuation of signals due to heavy rains [70]. The prediction of statistical rain rate distributions as a function of geography will not be adressed in this study. In this study the carrier and interference powers are calculated without considering atmospheric absorption and rain attenuation. As for the assumption that the carrier power densities are the same at all satellite antenna aim points, the satellite transmitting powers can be adjusted to allow for these propagation effects so that the power density requirements are still satisfied; but this has not been done in the calculations which will be presented.

Most satellites function as a repeater [71]: they receive a signal, change the signal carrier frequency, and transmit it back to Earth. In such a design, any interference power generated on the up-link remains in the signal when re-transmitted in the down-link [72]. In this study, only the interference power generated in the down-link is considered; any interference power from the up-link is not included in the calculation. For BSS, it has been proposed in international telecommunication meetings that the C/I_e requirement value in the up-link be 10 dB higher (better) than that of the down-link [73,74,75]. Therefore for the BSS the interference power in the up-link should make an insignificant contribution to the overall interference power, and can be neglected. For FSS, the C/I_e requirement values for the up- and down-links may not differ much [76,77]. Therefore for the FSS case the

 C/I_e requirement value for each half link must be specified with care so that the total interference power does not degrade the signal quality excessively.

In evaluating the feasibility of a scenario, first one calculates the C/I_e values at all the test points; then compares them with the pre-determined C/Ie requirement value. A scenario is said to be good when all the resulting C/I $_{\rm e}$ values exceed the requirement value [78,79]. In Chapter III, a C/Ie requirement value of 30 dB will be used to evaluate the quality of the extended gradient search results; the precise required value depends on the modulations, but 30 dB is typical [78]. In Chapter IV, the requirement value is arbitrarily set at 25 dB in the numerical calculation; the precise value is relatively unimportant because the main goal of the numerical calculations in Chapter IV is to demonstrate the feasibility of the method. In Chapter V, the requirement value is set at 20 dB in the numerical calculation, where the U.S. is used as a case study, for the following reason. For the U.S. domestic satellite systems in the 6/4 GHz band, four-degree spacing between two satellites was used initially to regulate the orbital assignments. However, in order to better utilize the orbit resource, the Federal Communication Commission (FCC) has decided to adopt two-degree spacing in the satellite planning task in the 6/4 GHz band, to be effective beginning in 1987 [80]. Since the method proposed in Chapter V is not meant only for the U.S., the C/I_e requirement is set at 20 dB in the numerical calculations so that it could appear more reasonable on the international basis, and would be compatible with the assumed antenna parameters, as discussed in Section V.E.1.

CHAPTER III

THE OBJECTIVE FUNCTION OF THE EXTENDED-GRADIENT AND CYCLIC-COORDINATE SEARCH METHODS

A. INTRODUCTION

The main purpose of the study in this chapter is to explore the mathematical nature of the orbital/frequency assignment problem by investigating an objective function used in the extended-gradient and cyclic-coordinate search methods to solve the satellite planning problem. It is shown that in order to find the global optimum solution one must deal with both the permutation of the orbital/frequency assignments and the signal quality requirement, e.g., the C/I ratio, in the optimization process. It is also shown that for a given set of scenarios with fixed orbital permutation (frequencies fixed) the function defined by the smallest single-entry C/I value has at most one local maximum. This strongly suggests that the objective function has only one local minimum for a given orbital permutation, as supported by some numerical evidence; this indicates that the extended gradient search process is highly likely to find the global optimal solution if it terminates as an ordinary gradient search with optimal orbital/frequency permutation.

B. GENERAL DISCUSSION OF THE GRADIENT AND CYCLIC-COORDINATE SEARCH METHODS AND THEIR OBJECTIVE FUNCTIONS

1. Introduction

The purpose of including this section is to introduce the basic principles of the gradient and cyclic-coordinate search methods, and to demonstrate how they perform for a particular objective function. Using the gradient search method for the assignment problem was proposed by Professor Clarence H. Martin of the Department of Industrial and Systems Engineering [29]; using the cyclic coordinate search method was proposed by Professor Clark A. Mount-Campbell of the Department of Industrial and Systems Engineering [30]; the objective function used in both methods was formulated by Professor Curt A. Levis of the Department of Electrical Engineering and Professor Clarence H. Martin of the Department of Industrial and Systems Engineering [29]; the numerical calculations discussed in Section III.B were performed by Professor Charles H. Reilly and Mr. David J. Gonsalvez of the Department of Industrial and Systems Engineering [30].

2. The Gradient and Cyclic-Coordinate Search Methods

The gradient and cyclic-coordinate search methods are two techniques commonly used by systems engineers to find an optimal condition for system performance [81,82]. In applying either method, an objective function, which is a function of a set of decision variables, is constructed in order to rank candidate solutions. The decision

variables represent the controllable operating conditions of the system; in the present application, they are the satellite orbital location and frequency channel assignments. The objective function should be a measure of the performance of the system under the conditions specified by the values of the decision variables. For instance, one solution, or specification of values for the decision variables, should represent more attractive operating conditions than a second solution if the former solution yields a greater (smaller) value when evaluated in an objective function which is to be maximized (minimized). The optimal solution (operating conditions) should be that solution which provides the greatest (smallest) objective-function value, when the objective function is to be maximized (minimized).

With such an objective function, the gradient search is performed in the following way [29,81]. Assume that the function is concave (convex) and is to be maximized (minimized). First a point that represents an initial operating condition is located, and the gradient components of the objective function at that point are calculated. Then a proper step size is chosen in the gradient (negative-gradient) direction so as to reach another point representing another operating condition. Because the objective-function value predicts the system performance, a sufficiently small step in the gradient (negativegradient) direction should always lead to a new condition that is better than the initial condition, at least according to the chosen objective function. Then, the same procedure is repeated with the improved operating condition as the new initial point and the search step size

properly adjusted according to the magnitude of the gradient: the smaller the gradient, the smaller the step size. This procedure should be repeated until a point is reached at which the gradient search does not yield improvement in system performance. This final solution will correspond to the optimal operating condition.

When the objective function is not concave (convex), global optimality of the solution is not guaranteed; instead the solution may converge to a local optimum, with the choice of the initial starting point influencing strongly which local optimum is selected. To reduce this influence and enhance the likelihood of finding a global or nearglobal optimum, a modified gradient search procedure, called an extended gradient serach, was used in the present application [86]. Consider the objective function as one to be minimized. First, the gradient direction at the initial point is calculated. Then from this point a search line is extended in the negative-gradient direction to the boundary of the feasible region; the objective function is calculated at a set of ten equally-spaced points along that search line. The point with the most favorable objective-function value is chosen as the new starting point to do another calculation. If the starting solution is the most favorable solution, another ten equally-spaced points between the starting solution and the first tested point are examined, the point yielding the most favorable objective-function value is chosen as the new starting solution. The procedure stops when no solution can be found that yields a more favorable objective-function value.

Since the search line is extended, the method may allow the search process to go from a region with one local minimum to another region; this reduces the likelihood of the search being "trapped" at an undesirable minimum, i.e., one much greater than the global minimum.

The cyclic coordinate search method, with a given objective function, proceeds as follows [30,82]. First, an initial operating condition is assumed. Then the decision variables are varied in turn, one at a time. Each time a set of points, where the corresponding variable is varied along its feasible coordinate range, is examined; the point yielding the most favorable objective-function value is identified, and the search continues from this new solution with another decision variable and the same search process. A cycle is completed when every decision variable has been allowed to vary; once a cycle is completed, another cycle can begin. When there is no more improvement in the objective-function value, the process is repeated within a smaller region and with smaller step-sizes. The whole search process terminates when no more improvement is obtained with a step size commensurate with the accuracy to be obtained.

3. An Objective Function for Satellite Orbital/Frequency Assignments

For the satellite planning problem, a suitable objective function is formulated as [29]

$$Z = \Sigma \Sigma \Sigma \Sigma Z_{knj}$$

keK neN_k jeJ_k

$$= \sum \sum \sum \exp \{a - [C_{knj}(dB) - I_{knj}^{e}(dB)]\}, \quad (3.1)$$

keK neN_k jeJ_k

where the symbols mean

- K : the index set of all satellites,
- N_k : the index set of all frequency channels assigned to satellite k,
- J_k : the index set of test points of service area k,
- a : arbitrary parameter used to avoid overflow in computer
 calculation,

$$I_{knj}$$
: the effective interference power at channel n of test point j in service area k, in dB.

It is assumed that each satellite is associated with one service area; thus the index k that represents a satellite also represents its corresponding service area. Note that it is the satellites that are counted in the index set K; one service area may be served by several satellites and each satellite is treated as an individual unit. The value of C_{knj} is calculated from Equation (2.5). The value of I_{knj}^{e} is calculated from Equation (2.13a), reproduced here

$$I_{knj}^{e}(dB) = 10 \cdot \log_{10} \{ \sum_{i \in K/k} \sum_{m \in N_{i}} 10^{[Iim,knj(dB)+F(f_{n},f_{m})(dB)]/10} + \frac{10^{[Ikm,knj(dB)+F(f_{n},f_{m})(dB)]/10}}{m \in N_{k}/n} \}, \qquad (3.2)$$

where I_{im,knj}, calculated from Equation (2.6), is the interference from channel m of satellite i into channel n of test point j in a service area served by satellite k. In Equation (3.1) the exponentially weighted summation is over all the frequency channels, at all the test points, in all the service areas. In Equation (3.2), the doublesummation adds the interference from all other satellites, and the single-summation adds the interference from other channels of the same satellite.

The satellite locations, denoted by o_1 for satellite 1, and the carrier frequencies, denoted by f_{1h} for channel h of satellite 1, are the decision variables. The limits of the orbital variables are usually determined by elevation angle constraints [83]; sometimes an eclipse-protection requirement may impose additional restrictions [84]. The limits of the frequency variables are determined by the limits of the available spectral band [4].

It is clear that the orbital variables are continuous variables; however, this is not necessarily true for the frequency variables. In past international conferences, generally the available spectral bands were each divided into channels of equal bandwidth, with each channel specified by its center frequency [85]. This is likely to be true for future conferences also; then the frequency variables will be discrete.

In the gradient search method, the derivatives with respect to all the decision variables need to be calculated; since it is impossible to differentiate with respect to a discrete variable, it is assumed here that in the frequency assignment the center frequencies of all the channels are allowed to vary continuously while each channel still has the same, fixed bandwidth. With this assumption, differentiation with respect to the frequency variables is allowed, and the frequency protection ratio of Figure 2.6 can be used. It is hoped, but cannot be guaranteed, that the optimization of the continuous-varying channel problem will lead to at least a near-optimum of the discrete channel problem.

Note in Figure 2.6 that there is a plateau in the frequency protection ratio. When two satellites are assigned frequencies with the frequency offset in this range, the gradient search method would find variation of these frequency assignments not useful because it would not change the objective-function value. This is definitely not the result the system planner wants, because separating the frequency assignments sufficiently could produce better C/I_e results. To avoid this problem, the plateau is deformed to form an isosceles triangle with small slopes $(\pm 0.05 \text{ dB/unit }\beta)$; this modification allows the frequency assignments to be separated if the frequency offset is located in the plateau region.

From Equation (3.1) it is clear that the value of Z_{knj} is small for large $(C/I_e)_{knj}(dB)$ values. Since a good scenario should have large C/I_e at all test points, the global minimum of the objective function is likely to be a good solution for the assignment problem.

The gradient components of Z are

$$\nabla Z = \left(\frac{\partial}{\partial o_1} Z, \frac{\partial}{\partial o_2} Z, \dots, \frac{\partial}{\partial f_{11}} Z, \dots\right)$$
 (3.3)

where the partial derivatives have been taken for all the decision variables; also

$$\frac{\partial}{\partial o_{1}} Z = k \varepsilon K n \varepsilon N_{k} j \varepsilon J_{k} Z_{knj} \frac{-\partial (C/I_{e})_{knj} (dB)}{\partial o_{1}} , \qquad (3.4)$$

$$\frac{\partial}{\partial f} Z = k \varepsilon K n \varepsilon N_k j \varepsilon J_k Z_{knj} \frac{-\partial (C/I_e)_{knj} (dB)}{\partial f_{1h}} , \qquad (3.5)$$

Referring to Figure 2.5 and Equations (2.5), (2.6), moving S_A clearly changes ψ_{tc} , ψ_{ri} , and x, moving S_B changes also parameters ψ_{ti} , ψ_{ri} , and y. Every satellite acts both as a desired and interfering source, so it affects the parameters associated with S_A in some terms, and those with S_B in others, and both in a few terms. As one moves S_A and S_B , the effective isotropic radiated powers, i.e., the products $P_A \cdot G_A$, $P_B \cdot G_B$ of satellites S_A and S_B respectively, are kept constant; but the carrier powers calculated from Equation (2.5) change somewhat at the test points, causing some contribution to $\partial Z/\partial o_1$. Also, the minimum ellipses must be recomputed for new satellite locations; the change in ellipse changes ψ_{tco} , ψ_{tio} and therefore D_A (ψ_{tc}), D_B (ψ_{ti}) since D_A depends on ψ_{tc}/ψ_{tco} and similarly for D_B .

Here one sees that in Equation (3.4) or (3.5), Z_{knj} is the weighting factor for the terms $\partial/\partial o_1[(C/I_e)_{knj}(dB)]$ and $\partial/\partial f_{lh}[(C/I_e)_{knj}(dB)]$. Since the term Z_{knj} is a negative exponential function of $(C/I_e)_{knj}(dB)$, it will be largest for the values k, n, and j

for which $(C/I_e)_{knj}(dB)$ is smallest; so the weight serves to emphasize the contribution from those test points and channels which need improvement most urgently. With such an objective function, the gradient search method tends to relocate most strongly the orbital/frequency assignments that are responsible for the worst C/I_e terms, and the result is an increase of these C/I_e values. This, of course, was the rationale for choosing the exponential function. A numerical example, below, will illustrate this point.

4. Numerical Exercise Using the Extended Gradient Search Method

A numerical exercise will now be given to show that the properties associated with the objective function are indeed as discussed, and that the performance of the extended gradient search method with respect to this objective function is as predicted.

In this exercise seven administrations are under consideration; they are Argentina, Bolivia, Brazil, Chile, Paraguay, Peru and Uruguay (denoted as ARG, BOL, BRZ, CHL, PRG, PRU, and URG respectively) with the geographic relation shown in Figure 3.1 and the test points listed in Table 3.1. It is assumed that every administration has requested one orbital location and three contiguous frequency channels, with cross polarizations for adjacent channels, for its satellite; the orbital locations and the carrier frequencies of the leading (lowest) channels are the decision variables, and these leading channels all have the same polarization. The feasible orbital arc was taken from 90 to 110 degrees west, and the spectral band from 12,200 to 12,300 MHz, for all satellites; the bandwidth of each channel is assumed to be 12 MHz, with



Figure 3.1. Geographic relation of the seven South American administrations.

Table 3.1

ARGENTINA Lon. Lat.		PARAGUAY Lon. Lat.	
-66.2 -62.8 -53.8 -56.7 -63.8 -73.2 -73.2 -71.4 -70.5 -68.6	-21.8 -22.0 -27.2 -36.9 -54.7 -54.8 -50.9 -39.0 -31.4 -24.8	-57.6 -58.6 -56.2 -54.7 -54.2 -58.1 -59.1 -62.2 -62.7 -58.7	-25.3 -27.3 -27.2 -25.5 -24.1 -20.2 -19.3 -20.5 -22.2 -27.2
BOLIVIA		PERU	
-65.Ø -65.5 -69.Ø -6Ø.Ø -57.5 -67.5 BRAZIL	-12.2 -9.8 -11.2 -16.1 -18.Ø -22.7	-7Ø.4 -69.Ø -7Ø.5 -74.Ø -7Ø.Ø -75.2 -8Ø.3 -81.3 -81.2	-18.3 -12.3 -9.4 -7.6 -2.7 $-\emptyset.0$ -3.4 -4.4 -6.1
-6Ø.5 -52.Ø -46.Ø	4.5 3.0 -1.5	URUGUAN	-13.4
-35.Ø -42.Ø -53.Ø -56.3 -7Ø.8 -73.Ø -69.Ø	-7.5 -22.5 -32.5 -29.5 -10.5 -7.0 1.0	-56.2 -54.9 -53.5 -53.2 -55.6 -56.9 -57.6	-34.9 -35.0 -34.0 -32.7 -30.8 -30.1 -30.2
CHILE		-58.2 -58.4 -57.9	-31.9
-69.5 -67.1 -7Ø.Ø -71.7 -68.4 -72.8 -75.7 -74.Ø -7Ø.4	-17.5 -23.Ø -34.2 -43.2 -52.3 -51.3 -46.8 -28.9 -18.3		-34.3

Test Points of Seven Administrations

a 2.58 MHz guardband between two channels. The carrier and interference powers are calculated from Equations (2.5), (2.6) and (2.13a); the antenna reference patterns are from Figures 2.2 and 2.3; the frequency protection ratio is from Figure 2.6; the ellipse data are calculated from [49].

In this calculation the initial scenario is that all satellites are collocated at 110 degrees west, and the initial frequency assignments extend from 12,235 to 12,265 MHz in 5 MHz intervals. The intermediate solutions at all the search steps and the final solution after ten search processes are shown in Figure 3.2 to demonstrate how the search process proceeds. In Figure 3.2(c), only the worst aggregate C/I_e values for these administrations are shown. In these figures the administrations are denoted by numbers according to alphabetic order: 1 for Argentina, 2 for Bolivia, 3 for Brazil, 4 for Chile, 5 for Paraguay, 6 for Peru and 7 for Uruguay. The improvement of the C/I_e results is clearly seen as the iteration process proceeds. The orbital assignments are almost steady after iteration 7, and the frequency assignments are almost steady after iteration 5; this indicates that the search process may have reached the vicinity of a local minimum.

The improvement mechanism of the extended-gradient search method can be observed as follows. Note that the C/I_e results of administrations 3, 4, 6 and 7 are the worst after iteration 1; then at iteration 2, the orbital and frequency assignments of these four satellites make a very significant change, while that of the other three satellites are almost unchanged. This is exactly the purpose of the











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Figure 3.2. Continued.

exponentiation in the objective function as discussed in Section III.B.3.

The purpose of modifying the ordinary gradient search method can be seen as follows. It is known that the objective function takes on large values when some of the orbital and/or frequency assignments are identical (for reason to be explained in Section III.C); hence exchanging the position of two satellites means jumping over such a region. In Figure 3.2(a) the orbital order established in iteration 1 is disturbed by the extended search process: the order of satellites 2 and 5 is changed at iteration 7. Thus the extended gradient search method can move from a region with one local minimum to another region.

5. Numerical Exercise Using the Cyclic Coordinate Search Method

The performance of the cyclic coordinate search method is demonstrated here; the same objective function is used to solve the same assignment problem. The initial scenario is changed as follows: all satellites are at 110 degrees west and 12,250 MHz. The results are shown in Figure 3.3. The improvement in the C/I_e results is obvious.

C. EMPIRICAL EXAMINATION OF THE OBJECTIVE-FUNCTION TOPOGRAPHY

1. The Importance of the Objective-Function Surface Topography to the Gradient and Cyclic-Coordinate Search Methods

The topography of the objective function greatly influences the outcome of the search methods. An objective function has only one



Figure 3.3. Numerical example of the cyclic coordinate search method.







Figure 3.3. Continued.

local maximum (minimum) if it is strictly concave (convex) or pseudo-concave (pseudo-convex). (See Appendix B for the definitions and properties of concave, strictly-concave and pseudo-concave functions.) The gradient and cyclic-coordinate search methods should lead one to a point very close to this maximum (minimum), if not directly locate it. If the objective function is not strictly concave, strictly convex, pseudo-concave, or pseudo-convex, it may have several local maxima or The greatest maximum (least minimum) is called the global minima. maximum (minimum), or simply maximum (minimum). The best operating conditions correspond to the global maximum (minimum), when the objective function is to be maximized (minimized). For such a function. both the gradient and the cyclic-coordinate search procedures will almost certainly give improvement to an initial operating conditions. However, both procedures may eventually be trapped at a local optimum instead of reaching the global optimum.

Therefore, knowledge of the mathematical properties of the objective function is important in determining whether the gradient and cyclic-coordinate search methods are to succeed. For instance, when the objective function has only one local maximum (minimum), or if the local maxima (minima) all correspond to nearly equal objective-function values, then it will be relatively easy to obtain a near-optimal solution by either method. If, on the other hand, there exist many local maxima (minima) at which the objective-function value is much smaller (greater) than its global maximum (minimum) value, then there is a greater likelihood of arriving at a solution which is much poorer than the true optimum.

Therefore, the topography of the objective function used for the satellite orbital and frequency assignment synthesis, i.e., Equation (3.1), will be examined next.

2. Relation Between Variations of Orbital/Frequency Separations and Single-Entry C/I_e Value

A very important concept should be pointed out first: for two satellites and their corresponding service areas, the single-entry C/I_e values at all the test points increase as the satellite orbital/ frequency separations increase.

In the C/I_e calculation several terms are relatively invariant when satellite locations change. The received carrier powers are calculated from Equation (2.5), and the interference powers are calculated from Equations (2.6) and (2.13a). The satellite effective isotropic radiated powers (EIRP), defined as the product of the transmitting power and the transmitting antenna gain, are assumed the same for both satellites, regardless of orbital locations. Because the service areas are covered by the main beams within the -3 dB contour, the carrier transmitting discrimination factor at the test point is always larger than, and close to -3 dB. Because the geostationary orbit radius is 6.6 times the Earth radius, the propagation distances from the satellites to all the test points vary little when satellite locations are changed.

One factor that dominates the variations of the single-entry $\ensuremath{\text{C/I}}_e$ values is the receiving discrimination term $D_d(\psi_{ri})$ in the interference power, and that variation depends chiefly on the satellite spacing. Any relative change of the two satellite locations will change the ground antenna off-axis angles toward the interfering satellite. Through the reference pattern in Figure 2.3, this angular change induces a substantial change in the interference power. The further the two satellites are separated, the lower the discrimination factors, and thus the lower the interference. Another factor, the interference transmit discrimination term $D_B(\psi_{ti})$, also varies when the satellite locations are changed; however, the change of $D_{B}(\psi_{tj})$ is much less than the change of $D_d(\psi_{ri})$ because ψ_{ti} (seen from the geostationary satellite toward the Earth) changes much less than ψ_{ri} (seen from the ground upward to the sky) when the location of the interfering satellite is changed. The single-entry C/I_{e} values increase when the corresponding satellite spacing increases until the discrimination factor $D_d(\psi_{ri})$ is in the far side-lobe of the reference pattern; then the C/I_e values become almost constant as the spacing keeps on increasing. This will be called "quasi-monotonic" variation: C/I_e values decrease (increase) continuously or remain constant when satellite spacing decreases (increases) continuously.

For a given service-area pair, the single-entry C/I_e value depends mainly on the magnitude of the satellite spacing, and slightly on the mean satellite orbital location. (It will be shown in Chapter IV that it varies only slightly for a large range of this mean satellite

location.) Therefore, for the purpose of the discussion in this section, an approximation is made by assuming that, for a given service-area pair, the single-entry C/I_e values at all the test points depend only on the magnitude of the satellite spacing and are independent of the mean satellite location.

Another factor that dominates the variation of the single-entry C/I_e values is the frequency offset in the frequency assignments. As explained in Section II.F, the frequency filtering factor of Figure 2.6 must be included in the effective interference calculation when the carrier frequencies of the wanted and unwanted signals are different. The larger the frequency offset, the lower the filtering factor, and the lower the interference. Therefore, the variations of the single-entry C/I_e values also depend strongly on the separation of the frequency assignments: for given orbital assignments, the further the frequency assignments are separated, the higher the single-entry C/I_e values.

3. Topographic features of the objective function

a) Objective-function topography of three-satellite example, orbital variables only

For simplicity a three-satellite system will be used to demonstrate some key points. The three satellites are S_1 , S_2 , S_3 , and these symbols will also be used to designate their orbital locations. A single channel will be considered so that no frequency variables are involved; in this case I and I_e are identical. The configuration space for this example is described here. First one draws the three orbital variable axes and indicates the feasible region, as in Figure 3.4. The line segment HB measures the feasible range for S_1 , HD for S_2 , HF for S_3 . In this figure the three satellites are assumed to have the same feasible orbital range, i.e., HB = HD = HF; therefore the feasible region is a cube. Any point in this cube represents an assignment scenario; its coordinates S_1 , S_2 , S_3 are the satellite orbital locations of this assignment. For example, the point H represents the assignment in which all three satellites are collocated at one end of the orbital arc; the point A is for three satellites collocated at the other end; the point B is for S_1 located at one end while S_2 and S_3 are collocated at the other. Note that associated with every point in the configuration space there is an objective-function value which can be calculated by Equation (3.1).

Several important features need to be mentioned. First, any point on the line AH indicates a three-satellite collocation. Then, all the points in the shaded plane ABHE correspond to S₂, S₃ collocation; those in the plane ACHF to S₁, S₂ collocation; those in the plane ADHG to S₁, S₃ collocation. Points within any one of the six sub-regions separated by the three collocation planes have the same satellite permutation. For example within the sub-region bounded by the planes AHB, AHC, ABC and HBC, all the points have the satellite permutation S₁>S₂>S₃; this is indicated by the notation 1-2-3 in Figure 3.4. Since the objectivefunction value is large when the C/I values are small, the objective function should have the highest values along the line AH because the






C/I values are the smallest for collocated satellites. Near the pairwise collocation planes ABHE, ACHF, ADHG the objective function should be moderately high, while between these planes the objective function falls off to form valleys because all the satellites are spread out. Thus we can visualize the objective-function topography as dominated by a system of ridges corresponding to satellite collocations; these ridges are connected to each other at the line AH where three satellites are collocated. Of course, the ridges will be high if the service areas are close together and hence the transmitting discrimination factor DB in Equation (2.6) is large; they will be small when the service areas are well separated.

An arbitrary plane in this cube may be chosen to show the objective-function values corresponding to points on this plane. The plane chosen here is the plane CJKLFMNP shown in Figure 3.5(a). The objective function might have the shape shown in Figure 3.5(b). The base plane is divided into six sub-regions by its intersection with the shaded planes in Figure 3.4. Each intersection line represents the collocation of two satellites, and each sub-region represents one permutation of the three satellites. The objective-function topography sketch shows these sub-regions separated by the ridges representing two-satellite collocation.

The objective-function values of a real set of scenarios will now be calculated here to confirm the above arguments. The three administrations are: S₁ for Peru, S₂ for Bolivia, S₃ for Paraguay. The orbital locations chosen for the calculation constitute the shaded plane



(a) an arbitrary plane.



(b) its objective-function surface.

Figure 3.5. Typical shape of objective function.

RSTU shown in Figure 3.6; it is inside the region of permutation $S_1>S_2>S_3$, and is a plane for which the value of S_2 is constant at $60^{\circ}W$. The value of S_1 ranges from 60 to 64 degrees west, while the value of S_3 ranges from 57 to 60 degrees west. The objective-function value is calculated from Equation (3.1), the values of C and I are calculated from Equations (2.5), (2.6) and (2.13a), the antenna reference patterns are taken from Figures 2.2 and 2.3, the ellipse data are calculated from [49]; the test points are those given in Table 3.1 for these administrations. The results are listed in Table 3.2, and the topography is plotted in Figure 3.7. As predicted, the maximum of the objective function in this plane occurs at R, the three-satellite collocation, the objective function rises to apparent ridges above the lines RS and RU which lie in the planes ABH and ADH of two-satellite collocations, and away from the lines of satellite collocation the objective function falls off and forms a valley.

The typical topography of the objective-function surface for points lying on a plane inside any region of fixed permutation is shown in Figure 3.8. The point R' will be on the line AH, the lines R'S' and R'U' will be in the planes of two-satellite collocation, the points T' will be chosen in the R'S'U' plane. This figure illustrates the type cal shape and locations of the tip, ridges and valley.





Table 3.2

$z = \sum_{K} Z$	Σ exp[a-(C ^J k	2/I) _{kj} (ab)],	a = 5,
$S_2(BOL) = 60$ degrees,				
S ₁ (PRU)	S ₃ (PRG)	z		ln(z)
60.	60.	0.2625 1	3+4	7.873
	59.5	0.8918 1	E+3	6.793
	59.	0.7644 1	E+3	6.639
	58.	0.7606 1	E+3	6.634
	57.	0.7601 1	E+3	6.633
60.5	60.	0.1529 H	E+4	7.333
	59.5	0.1084 1	E +3	4.685
	59.	0.4488 1	E+2	3.804
	58.	0.4460 1	E+2	3.798
	57.	0.4455 1	2+2	3.797
61.	60.	0.1010 1	S+4	6.918
	59.5	0.5477]	E+2	4.003
	59.	0.2781 1	E-1	-3.582
	58.	0.1111 1	E-1	-4.500
	57.	0.1104 1	E-1	-4.506
62.	60.	0.9673 1	E+3	6.874
	59.5	0.5322 1	E+2	3.974
	59.	0.1490 1	E-1	-4.206
	58.	0.1498 1	E-4	-11.109
	57.	0.6218 1	E 5	-11.989
63.	60.	0.9613 1	E+3	6.868
	59.5	0.5289 1	E+2	3.968
	59.	0.1454 1	E-1	-4.231
	58.	0.8250 1	E 5	-11.705
	57.	0.1852 1	E-6	-15.502
64.	60.	0.9596 1	E+3	6.867
	59.5	0.5277 1	E+2	3.966
	59.	0.1440	E-1	-4.241
	58.	0.7938 1	E-5	-11.744
	57.	0.1058	E-6	-16.062



Figure 3.7. Topography of objective function.





A point made in Section III.B.3 can also be illustrated by referring to Figure 3.7. The gradient direction at the point x is almost perpendicular to the line RS. This means that when this gradient direction is followed, the orbital location of S_1 is almost unchanged while S_3 is placed further away from S_2 . Note that points close to the line RS correspond to nearly collocating the satellites S_2 and S_3 ; when these satellites are close to each other, the test points of their service areas have low C/I values. This means that the corresponding weighting factors in Equation (3.4) are high, and the gradient search process will push the two responsible satellites S_2 and S_3 apart.

b) Objective-function topography of n-satellite case

The general shape of the objective-function topography for an n-satellite case will now be addressed. Note that the orbital and frequency variables are two different classes of decision variables so that their effects on the objective-function topography should be discussed separately.

In the first step only the orbital variables are discussed; it is assumed that the frequency assignments are the same for all the satellites. For a case of n satellites to be assigned orbital locations, the n orbital variables constitute an n-dimensional configuration space, and it is divided into n! regions of different orbital permutations (i.e., satellite orderings) by n(n-1)/2 (n-1)dimensional hyperplanes of two-satellite collocation. Each region of a fixed orbital permutation is surrounded by (n-1) hyperplanes of two-

satellite collocation and two (n-1)-dimensional boundary hyperplanes, each corresponding to one satellite at the boundary of its feasible orbital arc. The objective function has large values when satellites whose service areas are not well separated are collocated. For two neighbouring regions of different permutations, the corresponding permutations differ only in exchanging the relative positions of two satellites. Therefore the hyperplane between these two regions corresponds to the collocation of these two satellites, and the objective function may have large values in this hyperplane. All of these hyperplanes will connect at the line where all satellites are collocated; as a result the objective function has many local minima within the complete feasible region, and they can be characterized by their specific orbital permutations.

In general a satellite is associated with an orbital location and a set of frequency allocations. Basically, the effect of the frequency variables on the topography depends on the frequency protection ratio pattern shown in Figure 2.6. There is one important similarity between this pattern and the co-polarization antenna patterns: the relative protection ratio value is non-increasing as the frequency offset increases. So the spreading of the frequency assignments has the same effect on the objective-function value as the spreading of the orbital assignments: the further the frequency assignments are separated, the less the interference, and the smaller the objective-function value. Hence the objective function may have large values when the frequency assignments are collocated (or nearly collocated since the plateau in

Figure 2.6 has a certain bandwidth), and local minima may occur where frequency assignments are spread out.

The total number of local minima of the objective function in a case of n orbital and n frequency variables can be deduced as follows. Theoretically, the n orbital variables create n! regions with at least one local minimum in each region, then in each region the n frequency variables further create n! sub-regions with at least one local minimum in each sub-region. Therefore, there might be at least (n!)² local minima in this case. However, in reality the number of local minima is likely to be smaller, e.g., the collocation of two satellites may not result in bad C/I values to produce a hyperridge of large objective-function values when the service areas are well separated.

Also, another important conclusion can be deduced from the above discussion: the local minima of the objective function may be characterized by the permutations of their orbital/frequency assignments.

c) Possibility of one local minimum for a fixed permutation of orbital/frequency assignments

(1) Introduction

Figures 3.6 and 3.7 also show that the objective function as a convex (or pseudo-convex) function with only one local minimum within a region of fixed orbital permutation. In this case this result should be obvious because, for a three-satellite example with only orbital variables, the objective function can be minimized by spreading the outside satellites as far as allowed by the feasible arc, i.e., until they reach the boundaries. It is interesting to speculate whether, for a general case of n satellites, there is only one local minimum in a region of fixed orbital/frequency permutation. If this conjecture could be shown to be true, or approximately true in the sense that all the minima for a fixed permutation have approximately equal objectivefunction values, then an ordinary (not extended) gradient search procedure would be sure to find an optimal, or at least near-optimal solution for a given orbital/frequency permutation. However, a definitive proof of the conjecture has eluded us. The remainder of this chapter presents evidence that it is likely to be true for the orbital variables. Therefore, in this section it is assumed that every satellite has been assigned the same frequency channel, and the discussion is confined to a region of fixed orbital permutation.

(2) Locations of Global Maximum and Local Minima of Objective Function

First, it is shown that the global maximum of the objective function corresponds to a scenario of all-satellite collocation by showing that the objective-function value decreases quasi-monotonically along any linear trajectory starting from all-satellite collocation.

Definition 1

For two scenarios x, y in the n-dimensional configuration space, the linear trajectory between them is specified by the set of scenarios z such that

z = ax + (1-a)y, (3.6) where a is a parameter with value $0 \le a \le 1$.

Lemma 1

Assume that all the satellites have continuous feasible orbital arcs. Then given any two scenarios x, y, there exists a linear trajectory between them which is completely inside the feasible region; i.e., the feasible region is a convex set.

Proof

A scenario z in the n-dimensional configuration space is expressed by a 1*n row matrix $z=(z_1, z_2, \dots, z_n)$, where the components are the satellite locations of satellites 1, 2, ... n respectively.

Along a linear trajectory of starting scenario x and final scenario y, a scenario z satisfies

$$z = ax + (1-a)y$$
, (3.7a)

where 0<a<1, or

$$(z_1, z_2, \dots, z_n) = a(x_1, x_2, \dots, x_n) +$$

 $(1-a)(y_1, y_2, \dots, y_n),$ (3.7b)

or

Since all the satellites have continuous feasible orbital arcs, one has $z_i \in F_i$ if x_i , $y_i \in F_i$ for $1 \le i \le n$, where F_i is the feasible arc for satellite i. Hence any scenario z along this linear trajectory is well defined, and the linear trajectory is completely inside the feasible region. So the feasible region is a convex set.

Lemma 2

Within a region of fixed orbital permutation in the n-dimensional configuration space all the pairwise satellite separations vary linearly along a linear trajectory.

Proof

From Lemma 1, for scenario z the pairwise satellite separation between satellites i, j is $|z_i-z_j|$. From Equation (3.7c) one has

$$(z_i - z_j) = a(x_i - x_j) + (1 - a)(y_i - y_j),$$
 (3.8a)

where $0 \le 1$. Since all the scenarios are of the same orbital permutation, $(x_i - x_j)$ and $(y_j - y_j)$ must have the same sign. Then, since

both a and (1-a) are positive, (z_i-z_j) will also have this same sign. Therefore, Equation (3.8a) can be rewritten as

$$|z_{j}-z_{j}| = a|x_{j}-x_{j}| + (1-a)|y_{j}-y_{j}|$$
, (3.8b)

i.e., all the pairwise satellite separations vary linearly when a scenario is varied along a linear trajectory.

Theorem 1

The global maximum of the objective function is on the line of all-satellite collocation.

Proof

A linear trajectory that starts with all-satellite collocation is illustrated in Figure 3.9, note that the ordering of the satellites remains the same. Since the initial pairwise spacings are all zero, from Lemma 2 all the satellite spacings increase linearly in the trajectory. As discussed in Section III.C.2, all the single-entry C/I values increase quasi-monotonically when the corresponding pairwise satellite spacings increase linearly. As a result, all the aggregate C/I values, which involve the summation of all their contributing single-entry interference powers, must also increase quasi-monotonically in the process. Thus the objective-function value, which is the summation of the exponential of the negative of the aggregate C/I values, must decrease quasi-monotonically. Hence, the global maximum of the objective function is on the line of all-satellite collocation.





Theorem 2

Local minima of the objective function occur at boundaries of the feasible region such that all of the pairwise most widely separated satellites are at opposite limits of their respective feasible arcs.

Proof

Let the satellites be numbered according to their orbital positions, so that $x_1 < x_2 < \dots x_n$. Let the lower limits of their feasible arcs be denoted e_i (i=1,2,...,n) and the upper limits ω_i (i=1,2,...,n).

Assume $x_1 \neq e_1$, i.e., satellite 1 is not at the lower limit of its feasible arc. Then

$$z = a(e_1, x_2, x_3, \dots, x_n) + (1-a)x$$
, $0 \le a \le 1$ (3.9)

defines a linear trajectory for which all the $|z_1-z_j|$ (j=2,3,...,n) must increase continuously away from the other satellites. All other spacings remain unchanged on the trajectory. As discussed in Section III.C.2, this increases the single-entry C/I values involving satellite 1 quasi-monotonically while all other single-entry C/I values remain unchanged; therefore the objective-function value will decrease quasi-monotonically along the trajectory. Therefore it can not be a local minimum for the scenario x with $x_1 \neq e_1$. This proves the theorem.

(3) Topography of the worst single-entry C/I value

In the following section the topography of an auxiliary function A, defined as the the worst (smallest) single-entry C/I value, will be investigated. Although it is not the objective function Z, it is hoped that these two functions may have sufficient resemblance that some of the properties about Z can be extrapolated from A. First the function is defined as

$$A = Min [(C/I)_{i,kj}], \qquad (3.10)$$

i \varepsilon K, k \varepsilon K, j \varepsilon J_k

where the symbols mean

- (C/I)i,kj : the single-entry C/I value at test point j of service area k and the single-entry interference power is from satellite i,
- J_k : index set of test points of service area k,

K : index set of satellites in a scenario.

The value of A for a given scenario is obtained as follows. First all the single-entry interference from any one satellite to all the test points of other satellite systems are calculated using Equation (2.6), and these values are denoted as $I_{i,kj}$ when i is the interfering satellite and j is the test point in service area k. The carrier power at any test point is calculated using Equation (2.5), and is denoted C_{kj} when j is the test point in service area k. The value of $(C/I)_{i,kj}$ is calculated by taking the ratio of C_{kj} and $I_{i,kj}$. The value of A is obtained from choosing the smallest of all the $(C/I)_{i,kj}$ terms for that scenario (note that a scenario is a point in the configuration space).

Note that, if this function is used as the objective function for the extended-gradient or cyclic-coordinate search method, then the most favorable assignment is that for which the objective function is the global maximum.

Considering only the orbital variables, we wish to show that this function has at most one local maximum (hence a global maximum when it exists) for each ordering (permutation) of the satellites, and that such a maximum must lie on a boundary of the feasible region. Some lemmas and definitions will be useful in the proof of this theorem.

Lemma 3

Within a region of fixed permutation in the feasible region, all the $(C/I)_{i,jk}$ terms are quasi-monotonic functions along any linear trajectory (orbital variables only).

Proof

As discussed in Section III.C.2, for a service-area pair, the single-entry C/I values at all the test points vary quasi-monotonically as the satellite spacing varies. According to Lemma 2 all the pairwise satellite spacings either increase or decrease linearly, or remain constant along a linear trajectory within a region of fixed permutation. Therefore all the single-entry (C/I)_{i,kj} functions along that trajectory vary quasi-monotonically.

Definition 2

For two curves that have a countable number of common points, a vertex of the two curves is a common point of the two curves.

Let a function Y(x) be defined from a set of quasi-monotonic functions $Y_i(x)$, is I in a finite range as

$$Y(x) = Min [Y_i(x)].$$
 (3.11)
i \varepsilon I

Lemma 4

If the local maximum of Y(x) exists, it must occur at a vertex or at the boundary of the allowed range.

Proof

Assume that $Y(x_0)$ is a local maximum (minimum) of Y(x), and it is not a vertex of $Y_i(x)$, is I, nor is it at the boundary. Then Y(x) is equal to one of the $Y_i(x)$ in the vicinity of x_0 ; hence Y(x) is monotonic in the vicinity of x_0 . Being a local maximum (minimum) means that $Y(x) \langle Y(x_0) (Y(x) \rangle Y(x_0))$ for x in the vicinity of x_0 , which contradicts the fact that Y(x) is monotonic in the vicinity of x_0 . Hence the local maxima (minima) of Y(x) occur at the vertices or at the boundary.

Lemma 5

Y(x) can not have more than one local maximum.

Proof

Suppose that, as shown in Figure 3.10, the function Y(x) has two separated local maxima at x_1 and x_3 , then there must exist a local minimum at some point x_2 between x_1 and x_3 . By lemma 4, this local minimum must be at the vertex of two $Y_1(x)$, say $Y_1(x)$ and $Y_2(x)$. The point x_2 being a local minimum of Y(x) requires, in the vicinity of x_2 ,



Figure 3.10. Hypothetical case where two maxima occur in a linear trajectory. (Proved impossible by contradiction)

$$Y(x) > Y(x_2) \qquad \text{for } x > x_2 \quad \text{and } x < x_2 \tag{3.12}$$

Let $Y_1(x)$ be the function which coincides with Y(x) for $x < x_2$ (i.e., the curve 1_1) and $Y_2(x)$ the function which coincides with Y(x) for $x > x_2$ (i.e., the curve 1_2) in the vicinity of x_2 , then one has

$$Y_1(x) > Y(x_2)$$
 for $x < x_2$. (3.13)

 $Y_1(x)$ being quasi-monotonic means that, from Equation (3.13),

$$Y_1(x) < Y(x_2)$$
 for $x > x_2$ (3.14)

in the vicinity of x_2 . The same reasoning that led to these two equations, when applied to $Y_2(x)$, gives in the vicinity of x_2 ,

$$Y_2(x) > Y(x_2) \qquad \text{for } x > x_2 , \qquad (3.15)$$

$$Y_2(x) \le Y(x_2)$$
 for $x \le x_2$. (3.16)

Remembering that Y(x) coincides with $Y_2(x)$ (by definition of $Y_2(x)$ above) for x>x₂, Equation (3.15) can be rewritten

$$Y(x) > Y(x_2) \qquad \text{for } x > x_2 , \qquad (3.17)$$

and together with Equation (3.14) this gives

$$Y_1(x) < Y(x) \qquad \text{for } x > x_2 \qquad (3.18)$$

in the vicinity of x_2 . This contradicts the definition of Y(x) in Equation (3.11). Thus Y(x) can have at most one local maximum.

Theorem 3

Along any linear trajectory within a region of fixed permutation in the feasible region, the auxiliary function A has at most one local maximum (orbital variables only).

Proof

The discussion here is confined to a linear trajectory within a region of fixed permutation. From Lemma 3, all the single-entry C/I terms are quasi-monotonic functions on such a trajectory. The function A is defined as the minimum of all these C/I terms; thus the function A may be identified with Y(x) in Lemma 5 if the trajectory parameter a is identified with x in that lemma. Therefore, from Lemma 5, the function A has at most one local maximum (hence a global maximum when it exists) along a linear trajectory.

Theorem 4

The auxiliary function A has at most one local maximum within a region of fixed permutation in the configuration space (orbital variables only).

Proof

The discussion here is still confined to a region of fixed permutation. It will be shown that Theorem 3 is contradicted if the function A has two local maxima within such a region. Suppose that the function A has two local maxima at x_1 and x_2 , then the linear trajectory that passes through both x_1 and x_2 will have two local maxima at x_1 and x_2 ; however, this is a clear contradiction of Theorem 3. Hence within

this region the function A has at most one local maximum; hence any maximum must be global in the region. Because the C/I variations are only quasi-monotonic, there may be sub-regions in which the value of A is constant; if this value is not exceeded elsewhere in this region, A will not have a distinct maximum in this region.

Theorem 5

The local maxima of the auxiliary function A are located at the boundary of the feasible region in the configuration space (orbital variables only).

Proof

By the same argument as in Theorem 2, a scenario located in the interior of a feasible region cannot be a local maximum because it is always possible to find a scenario located at the boundary that has better or equal single-entry C/I values. Thus any maximum of A has to be at the boundary.

(4) Numerical test

As discussed in Section III.B.3, the objective function Z is formulated to emphasize the worst aggregate C/I_e terms by exponentiating the negative of the aggregate C/I_e value; thus it is reasonable to say that there is a direct relationship between the function Z and the negative of the worst aggregate C/I_e term, or several such terms if they are of approximately equal value. In view of Theorem 4, this suggests that the function Z is likely to have only one local minimum within a region of fixed permutation. Since a rigorous proof has eluded us, a

numerical example of a four-administration model was calculated to investigate this feature: the four administrations are Argentina, Bolivia, Paraguay, and Peru; the feasible orbital range is from 62 to 68 degrees west. The objective-function value was calculated from Equation (3.1), the values of C and I were calculated from Equations (2.5), (2.6), and (2.13a); the antenna reference patterns are from Figures 2.2 and 2.3; the ellipse data were calculated from [49]. Since it is known from Theorem 2 that the local minima must be located at the boundaries of the feasible region in the configuration space, the objective function values at all the 24 boundary planes of this numerical example were calculated; the equal-height contour plots are shown in Appendix C, where Argentina, Bolivia, Paraguay and Peru are denoted as ARG, BOL, PRG, and PRU respectively. In each figure, two satellites are located at opposite ends of the feasible arc, and the (varying) orbital locations of the other two are indicated by the coordinates. The upper triangle represents one permutation and the lower triangle another permutation. Clearly there is only one local minimum for each permutation. The results suggests that for a general case (n satellites) it is likely that there is only one local minimum within a region of fixed orbital permutation.

D. DISCUSSION AND CONCLUSION

Even though the objective function in Equation (3.1) is not the only one that might be formulated to solve the orbital/frequency assignment problem, it still should be representative of objective functions designed to maximize low C/I_e ratios. Therefore many of the

mathematical features of the assignment problem can be inferred from this function.

Referring to Figures 3.4 and 3.5 and the discussions in Section III.C, the objective function of Equation (3.1) often has large values at points of either orbital or frequency assignment collocation, and the local minima can be characterized by the permutations of their orbital/ frequency assignments. This feature indicates that there might be on the order of $(n!)^2$ local optimum solutions for a n-satellite case of n orbital variables and n frequency variables; in reality the number of local optima is likely to be smaller because the collocation of two satellites may not result in bad C/I_e ratios when the service areas or their frequencies are well separated. Still, one thing is clear: permutation of the orbital/frequency assignments is an important part of the problem. Therefore a technique for finding the globally optimal (or a near-optimal) scenario must be able to choose the proper permutation of the orbital/frequency assignments, as an important step toward satisfying the C/I_e requirement.

Also, the discussion in Section III.C.3.c, which shows that the objective function is likely to have only one local minimum within a given orbital permutation, suggests that in order for an extended gradient search method to obtain the globally optimal solution, it should terminate as an ordinary gradient search with the optimal permutation in orbital/frequency assignments.

CHAPTER IV

OPTIMAL ORBITAL ASSIGNMENTS BY MEANS OF THE AS CONCEPT

A. INTRODUCTION

In this chapter a direct correspondence between the single-entry C/I_e protection requirements and the necessary satellite spacings is exhibited. This relationship is used to formulate linear constraints to enforce single-entry C/I_e protection requirements between all pairs of satellites. Two new formulations are then developed under the assumption that frequency assignments are the same for all the service areas. One is a mixed integer linear program, solved by a branch-and-bound procedure. The other is a linear program with both linear and nonlinear side constraints, the simplex method with restricted basis entry can be used to find an approximate solution when this formulation is used. As a consequence, the cumbersome nonlinear C/I_e expression used for the synthesis formulation in Chapter III is avoided.

The 1977 World Administrative Radio Conference (WARC-77) suggested that for maximum orbit utilization, space stations should be placed as close to each other as is consistent with keeping the mutual interference to acceptable levels [16]. This concept was explored by a Canadian study group by relating the single-entry C/I protection requirement to the satellite spacing [26,27,28]; they formulated a

orbital/frequency assignment program, for use at the 1983 Regional Administrative Radio Conference (RARC-83), based on the satellite spacing requirement. The concept of using this relationship in conjunction with linear optimization is original, to our best knowledge. The author is indebted to Professor Charles H. Reilly of the Department of Industrial and Systems Engineering for the mixed-integer and linear programming formulations and to Mr. David J. Gonsalvez for the actual programs.

The organization of the chapter is as follows. First the relationship between the single-entry C/I_e protection requirement and pairwise satellite spacing will be formulated, and the relative importance of system parameters will be discussed. Next, exact and approximate methods of calculating the required spacing will be presented. This will be followed by a heuristic discussion of the relationship between single-entry and total acceptable protection requirements, in order to establish single-entry requirements which are highly likely to lead to satisfaction of the total acceptable C/I_{o} protection requirement. Next the principle of the methods will be elucidated with a very simple hypothetical four-service area example to show how satellite ordering (permutation) enters into the linear optimization process. Finally the results of both the mixed integer program (MIP) and restricted-basis entry linear program (RBLP) formulations will be presented for a scenario of six South American administrations.

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B. RELATION BETWEEN SINGLE-ENTRY C/I_e PROTECTION REQUIREMENT AND REQUIRED SATELLITE SPACING

The relationship between a single-entry C/I_e requirement and the required satellite spacing will now be derived. The general configuration of two service areas A, B and the locations of their satellites S_A , S_B is shown in Figure 4.1 which is identical to Figure 2.7. Refer to Section II.F for detailed description of all the parameters. It is assumed that frequency assignments are the same for both satellites. The received carrier power, C, in channel n (carrier frequency f_n) at test point d is given in Equation (2.5) as

$$C = \frac{{}^{P}_{A} \cdot {}^{G}_{A} \cdot {}^{D}_{A}(\psi_{tc}) \cdot {}^{G}_{d} \cdot {}^{c}}{f_{n}^{2} \cdot (4\pi)^{2} \cdot {}_{x}^{2}}; \qquad (4.1)$$

the effective single-entry interference power, I_n^e , from S_B to channel n of test point d can be inferred from Equation (2.6) as

$$I_{n}^{e} = \sum_{m} \frac{{}^{P}_{B} \cdot {}^{G}_{B} \cdot {}^{D}_{B} ({}^{\Psi}_{ti}) \cdot {}^{G}_{d} \cdot {}^{D}_{d} ({}^{\psi}_{ri}) \cdot {}^{c^{2}} \cdot F(f_{n}, f_{m})}{f_{m}^{2} \cdot (4\pi)^{2} \cdot y^{2}}$$
$$= \frac{{}^{P}_{B} \cdot {}^{G}_{B} \cdot {}^{D}_{B} ({}^{\psi}_{ti}) \cdot {}^{G}_{d} \cdot {}^{D}_{d} ({}^{\psi}_{ri}) \cdot {}^{c^{2}}}{(4\pi)^{2} \cdot y^{2}} \cdot \sum_{m} \frac{F(f_{n}, f_{m})}{f_{m}^{2}}, \qquad (4.2)$$

where the summation is over all frequency channels assigned to S_B . The term "single-entry" is defined as the aggregate of emissions from any





one satellite entering any receiver in the wanted service within the channel to be protected [87]. The single-entry I_n^e values are different for different channels, and the worst one is in the channel at the center of the assigned band; it is denoted as I_e , and is used to evaluate the interference effect in this chapter.

The exact single-entry C/I_e ratio (in center channel n) at test point d is therefore

$$\frac{C}{I_{e}} = \frac{P_{A} \cdot G_{A} / x^{2}}{P_{B} \cdot G_{B} / y^{2}} \cdot \frac{D_{A} (\psi_{tc})}{D_{B} (\psi_{ti}) \cdot D_{d} (\psi_{ri})} \cdot \frac{1}{f_{n}^{2} \cdot [\sum_{m} (f_{n}, f_{m}) / f_{m}^{2}]} .$$
(4.3)

Even though the only independent variables in Equation (4.3) are the satellite orbital locations, there are many hidden parameters and relationships. The minimum ellipse (its size, orientation, and aim point) for S_A is a function of satellite location. It is assumed in this chapter that the carrier power flux densities at the aim points are equal for all the satellite systems. For any ellipse size there is a corresponding G_A value, and the value of P_A must be adjusted to give the required power density at the aim point. As for D_A(ψ_{tc}), the value of ψ_{tc} depends on the satellite location, and there is also an implicit parameter ψ_{tco} which is a function of the ellipse (refer to Figure 2.1). The same considerations apply to satellite S_B, and G_B, P_B, D_B. Strictly speaking, the values of G_d, and thus D_d, are different for different channels because they are functions of carrier frequencies; in this chapter the values of G_d for all channels are assumed the same, which is reasonable for a narrow band frequency assignment.

The exact calculation of Equation (4.3) is complicated, it is therefore worthwhile to seek an approximation to Equation (4.3). Because the geostationary orbit radius is 6.6 times the Earth radius, the propagation distances x and y are approximately equal. Then, since the power densities at the respective aim points are assumed equal [65], it follows that

$$\frac{P_A \cdot G_A}{x^2} \approx \frac{P_B \cdot G_B}{y^2} \qquad (4.4)$$

When the service-area shape can be fitted reasonably with an ellipse, the test point d should be located on or near the -3 dB contour [46,47], giving

$$D_{A}(\psi_{tc}) \approx 1/2 \quad . \tag{4.5}$$

Equation (4.3) can therefore be approximated as

$$\frac{C}{I_{e}} \approx \frac{1}{2 \cdot D_{B}(\psi_{ti}) \cdot D_{d}(\psi_{ri})} \cdot \frac{1}{f_{n}^{2} \cdot [\sum_{m} F(f_{n}, f_{m})/f_{m}^{2}]}$$
(4.6)

The factor $1/\{f_n^2 \cdot [\Sigma F(f_n, f_m)/f_m^2]\}$ is a constant since it is assumed that the frequency assignments are the same for all satellites (note that f_n is at the center channel). An internationally agreed $F(f_n, f_m)$ reference function exists only for the BSS, but not for the FSS which is the subject of the study in this chapter. However, it is known that numerous U.S. FSS satellites have 24 transponders in the 6/4 GHz band occupying the whole 500 MHz bandwidth, each transponder channel is 36 MHz wide and the guard band between two channels is 4 MHz (crosspolarization discrimination allows frequency re-use in a satellite). In this chapter only the co-channel interference will be considered. Thus the value of $1/{\{f_n^2 \cdot [\Sigma F(f_n, f_m)/f_m^2]\}}$ is taken to be one. Then Equation (4.6) can be approximated as

$$\frac{C}{I_e} \approx \frac{1}{2 \cdot D_B(\psi_{ti}) \cdot D_d(\psi_{ri})}$$
 (4.7)

The variation of the C/I_e values with respect to the satellite orbital locations will now be discussed. Because the service areas are stationary and the satellite orbit radius is 6.6 times the earth radius, the value of ψ_{ti} , and hence the value of $D_B(\psi_{ti})$, changes little when the location of S_B, the interfering satellite, is changed by a small arc length. When the service-area pair and system parameters are given, the term ψ_{ri} , and thus $D_d(\psi_{ri})$, becomes the only factor that can significantly affect the C/I_e values; this is done by changing the satellite spacing to vary ψ_{ri} , and thus the $D_d(\psi_{ri})$ value. To have an acceptable single-entry C/I_e ratio, the main contributions are seen to come from the terms $D_B(\psi_{ti})$ and $D_d(\psi_{ri})$. The term $D_B(\psi_{ti})$ comes from the separation between the two service areas; the further they are separated, the less the value $D_B(\psi_{ti})$. The very fact that it comes from the geographic separation of the service areas makes it a valuable resource for the system planner. The term $D_d(\psi_{ri})$ comes from the satellite spacing; the larger the spacing, the larger the value ψ_{ri} , and the smaller the value $D_d(\psi_{ri})$. The most important feature about the satellite spacing is that this quantity can be controlled by the system planner.

For a given single-entry C/I_e protection requirement, the system planner should first look for the term $D_B(\psi_{ti})$ for its contribution to the margin between C and I_e ; when this is not enough, he then has to look for the term $D_d(\psi_{ri})$ to make up the difference. For satellite S_A located at 1 and S_B located to the east of S_A , the threshold satellite spacing that lets the resulting worst single-entry C/I_e value equal the protection requirement is the local required spacing for the satellite pair, and is designated as $\Delta s_A(1), B(1+)$; here the sign + means east of 1. For S_B to the west of S_A it would be $\Delta s_A(1), B(1-)$. With any less spacing at least one of the test points would have an unacceptable single-entry C/I_e ratio, while with any more spacing all the singleentry C/I_e ratios would be better than the requirement. Thus, the $\Delta s(1)$ function can be viewed as the reflection of the single-entry protection requirement, eg., $|S_A-S_B| > \Delta s_{AB}$ would guarantee satisfactory single-entry C/I_e ratios at all the test points in service areas A and B.

Since a satellite spacing requirement given by $\Delta s(1)$ is equivalent to the equivalent single-entry protection requirement, it can be taken as a constraint on the relative locations of the corresponding satellites. So, instead of thinking about a scenario having satisfactory single-entry C/I_e values, one may think about the scenario satisfying all the $\Delta s(1)$ constraints. One important feature about the $\Delta s(1)$ value is that, in producing the margin between C and I_{e} , it fully utilizes the service-area separation to minimize the necessary satellite spacing. This approach corresponds directly to the idea proposed in WARC-77: for maximum orbit utilization satellites should be placed as close to each other as is consistent with keeping the mutual interference to acceptable levels [16]; hence the set of $\Delta s(1)$ values is exactly what the system planner should use in order to achieve this goal. Using the $\Delta s(1)$ value in the orbit planning task has a great advantage in terms of numerical calculations. While the C/I_e expression involves many geometric equations and is highly nonlinear with respect to the orbital variables, the $\Delta s(1)$ set can be calculated once and for all for each service-area pair and then used as constraints. This greatly changes the aspect of the orbital assignment task, and the methods to solve it; this will be apparent in Section IV.F.

It is suggested in WARC-77 that single-entry protection requirements can be used as a guide for determining sharing criteria [87]; still the total interference from all sources must be calculated to evaluate the scenario definitively. In this chapter, satellite orbit planning methods are developed based on single-entry protection

requirements; it will be shown in Section IV.D that this is likely to lead to adequate aggregate protection when the single-entry C/I_e protection requirement is larger than the total acceptable protection requirement by 5 dB. First, one needs to turn one's attention to algorithms for calculating the Δ s values just defined.

C. CALCULATION OF AS VALUES

1. Exact Method

An exact determination of the required satellite spacings requires solution of Equation (4.3) for ψ_{ri} for various locations of S_A. An explicit solution has not been found; still, a numerical value can be obtained by evaluating the right side of Equation (4.3) (or equivalently Equations (4.1) and (4.2)) for increasing separations until the required C/I_e value results. Specifically, the rigorous calculation of the threshold satellite spacing for two service areas A, B may be done by the following algorithm. (Refer to Figure 4.2 for the geometric relations.)

- (1) Set the location of satellite S_A at orbital location 1.
- (2) Move the location of satellite S_B incrementally from 1 toward the east. After each move, use the streamlined Spectrum/Orbit Utilization Program (SOUP) code in Appendix A to calculate the C/I_e values at all the test points of the two service areas.



Figure 4.2. Configuration of $\Delta s(1)$ value calculation.
- (3) There exists a satellite spacing beyond which all the C/I $_{\rm e}$ values exceed the single-entry protection requirement, and below which at least one C/I value is worse than the protection requirement. This is the satellite spacing for the two service areas at the prescribed locations and is denoted as $\Delta s_{A(1),B(1+)}$, where the sign + means east of 1.
- (4) Repeat procedures (1)-(3) for S_B west of S_A ; the resulting spacing is denoted as $\Delta s_A(1), B(1-)$, where the sign means west of 1.
- (5) Repeat (1)-(4) with a set of new locations for satellite S_A until its feasible arc has been covered.

The above calculation is rather time consuming. For each test position, the minimum ellipse data of the service area has to be generated.

2. Approximate Method

To ease the computational burden, an approximate method was adopted. This method is based on the assumption that the power densities at the ground receiver locations do not change when the location of either satellite is moved away from 1 by a small arc length. The procedure is:

(1) Collocate the two satellites at 1. Use the streamlined SOUP code in Appendix A to calculate all the ground receiver C/I_e values.

- (2) Pick out the test point with the worst C/I_e value, calculate the margin between this C/I_e value and the single-entry protection requirement. At this point the service-area separation factor has been accounted for, so this margin should be made up by separating the two satellites from collocation to produce the receiving discrimination loss $D_d(\psi_{ri})$ toward the interfering satellite.
- (3) Use the receiving antenne reference pattern in Figure 2.5 to calculate the necessary off-axis angle that provides this margin; this is the topocentric angular separation (viewed from the test point with the worst C/I_e value) the two satellites should have.
- (4) Spread the satellites symmetrically apart from 1 step by step until the separation gives this necessary topocentric angle at this test point. The final geocentric separation is the approximate $\Delta s(1)$ value when S_A and S_B are in the vicinity of orbital location 1.

The computer code for this calculation is listed in Appendix D.

An example of the Δ s(1) calculation is shown in Table 4.1 with the two administrations being Bolivia (BOL) and Paraguay (PRG). The satellite transmitting and ground receiving reference patterns are given in Figures 2.4 and 2.5. Initially the satellites are located at 90 degrees west. The interference calculation is carried out, and the test point with the worst C/I_e value, -0.66 dB, is at 62.2 degrees west

Table 4.1

COUNTRY	SATELLITE	(LON.)	FREQUENCY	(MHz)	
EOL	-90.01	Ø	4650.00	r	
PRG	-90.01	Ø	4000.00	r	
TEST COUNTR	Y : BOL	SATELLITE	-95.05		
TEST Lon.	POINT LAT.	INT. SAT.	C/I (dB)	MARGIN	(dB)
-65.ØØ	-12.2Ø	PRG	28.86	-1.14	
-65.5Ø	-9.8Ø	PRG	27.51	-2.49	
-69.ØØ	-11.20	PRG	27.78	-2.22	
-60.ØØ	-16.1Ø	PRG	8.02	-21.98	
-57.5Ø	-18.00	PRG	2.58	-27.42	
-67.5Ø	-22.7Ø	PRG	14.88	-15.12	
TEST COUNTR	Y: PRG	SATELLITE	: -9C.ØØ		
TEST	POINT	INT. SAT.	C/I (dB)	MARGIN	(dB)
-57.6Ø	-25.3Ø	BOL	7.75	-22.25	
-58.6Ø	-27.3Ø	BOL	10.58	-19.42	
-56.2Ø	-27.20	BOL	14.54	-15.46	
-54.7Ø	-25.50	BOL	13.22	-16.78	
-54.2Ø	-24.10	BOL	11.2Ø	-18.80	
-58.1Ø	-20.20	BOL	1.15	-28.85	
-59.1Ø	-19.3Ø	BOL	C.58	-29.92	
-62.20	-20.50	BOL	-Ø.66	-3Ø.66	
-62.7Ø	-22.20	EOL	-£.35	-30.25	
-58.7£	-27.20	EOL	10.15	-19.25	

Example of $\Delta s(1)$ Calculation Procedure

WORST MARGIN IS -30.66 dB AT PRG (-62.20, -20.50) REQUIRED SATELLITE SPACING : 4.00 AT -90.00 FOR C/I 30.0 dB

longitude, 20.5 degrees south latitude in Paraguay. The single-entry C/Ie protection requirement is chosen to be 30 dB, hence it requires 30.66 dB attenuation from the ground receiving discrimination to provide the necessary margin between C and Ie. Then the receiving reference pattern is used to calculate the required off-axis angle, i.e., the topocentric angle, of the two satellites as seen from the test point with the worst C/I_e value. The satellite geocentric spacing is obtained from step (4) of the approximate method, the result is shown in Table 4.1 which shows that, in the vicinity of 90 degrees west, the necessary satellite spacing for these two service areas is four degrees. This spacing should result in at least 30 dB single-entry C/I_e values at all test points, with the worst one at 30 dB. This result can not be guaranteed precisely, since the test point which was the worst for the original satellite locations may not be the worst for the new locations, and since new ellipses were not generated for the new satellite locations.

Using the same antenna parameters and 30 dB protection requirement, some of the $\Delta s(1)$ values for several service-area pairs at different mean satellite locations are listed in Table 4.2. The calculation is made in 10- or 20-degree increments.

An example of the curve $\Delta s(1)$ vs. mean satellite location 1 is shown in Figure 4.3, the two administrations are Paraguay and Uruguay. The $\Delta s(1)$ value is fairly constant within a large range of satellite locations, and starts to increase when the satellite elevation angle is small.

Tab	le	4.	2
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country pair	longitude	۵s	country pair	longitude	Δs
ARG BOL	-78	4.00	CHL PRG	-2Ø	3.Ø5
	-80	4.82		-30	2.45
	-98	4.05		-49	1 69
	-100	4 12		-50	1.05
	-100	4.12		- 510	1.35
	-118	4.1/		-6.0	1.14
				7Ø	1.23
ARG CHL	-7Ø	4.18		-8Ø	1.14
	-8Ø	4.Ø5		-9Ø	1.25
	-90	4.00		-107	1 46
	-199	A 92		-11%	2 00
	-110	4.02		-110	2.00
	-110	4.13		-120	3.32
ARG PRG	-78	4.24	CHL PRU	-70	3.84
	-80	4.28		-8ø	3.83
	-9 <i>Ø</i>	4.32		-9Ø	3.85
	-1ØØ	4.28		-100	3.83
	-11Ø	4.32		-11Ø	3.94
ARG PRU	-78	Ø.94	CHL URG	-29	2.52
	_ <u>9</u> <i>a</i>	1 94		- 20	1 44
	-00	1 15		- 3.0	<i>x</i> • • •
	- 30	1.10		- 4,0	10.33
	-199	1.25		-50	0.80
	-110	1.41		-60	Ø.43
				-7Ø	Ø.42
ARG URG	-7Ø	4.18		-8Ø	Ø.41
	-80	4.14		-90	1.03
	-98	A 96		-199	1 28
	~199	4 96		-119	1 50
	-1.00	4.00		-110	1.35
	110	3.94		-120	2.10
BOL CHI	-7Ø	4.13	PRG PRU	-20	Й.45
	-99	A 20		- 19	Q 47
	- 0.0	4.20			2.47
	- 30	4.28		-6.0	10.48
	-100	4.39		- / 10	Ø.49
	-11Ø	4.57		-80	£.49
				-9Ø	Ø.5Ø
BOL PRG	-7ø	4.09		-120	Ø.85
	-80	3.99		-110	1.10
	- 9 0	A 00		-120	1 75
	-100	4 02		120	1.70
	-100	4.03			
	-110	4.104	PKG URG	- 210	2.35
				-410	2.20
BOL PRU	-7Ø	3.87		-6Ø	2.13
	-8Ø	3.95		-7ø	2.16
	-90	3.99		-80	2.19
	-199	A 10		-90	2 20
	- 1 1 0	4 26		-100	2.20
	-110	4.20		- 100	2.34
				-110	2.46
BOL URG	-2Ø	Ø.43		-12Ø	2.64
	-4Ø	Ø.42			
	-6Ø	Ø.4Ø	PRU UP.G	-28	Ø.45
	- 7 Ø	0.39		- 10	Ø 43
	_0 <i>a</i>	a 29		- C a	<i>a</i> 11
	- 00	0.00		- UU _ 7 M	Q 47
	- 30	10.30		- / 10	10.410
	-188	10.84		-80	2.37
	-11Ø	Ø.94		-9Ø	Ø.37
	-12Ø	1.Ø9		-188	Ø.33
				-110	Ø.32
				-128	Ø.36

$\Delta s(1)$ Values of Six South American Administrations







Although the $\Delta s(1)$ values are calculated up to two decimal fractions, in practical situations only the first decimal fraction is meaningful because the typical satellite station keeping inaccuracy is 0.1 degree [44]. The reason for keeping two decimal fractions is only to show their variations more precisely.

3. Validity of Approximate Method

The approximate method gives the correct result if the power densities at all the test points do not change when the satellites are moved by a small arc length. Strictly speaking, the power-density invariance assumption is not correct because the carrier power densities are designed to be constant only at the beam centers [65]. However, in practise, it is a highly acceptable assumption. To demonstrate this point more clearly, Equation (4.3) is written as

$$C/I_{e} = K(1_{A}, 1_{B})/D_{d}(\psi_{ri})$$
, (4.8)

where

$$K(1_{A},1_{B}) = \frac{P_{A} \cdot G_{A}/x^{2}}{P_{B} \cdot G_{B}/y^{2}} \cdot \frac{D_{A}(\psi_{tc})}{D_{B}(\psi_{ti})} \cdot \frac{1}{f_{n}^{2} \cdot [\sum_{m} F(f_{n},f_{m})/f_{m}^{2}]}, \quad (4.9)$$

and l_A and l_B denote the orbital locations of S_A and S_B . The approximate method consists of calculating K for collocation, i.e., K(l,l), then assuming that this value remains constant as satellite locations are shifted a few degrees from l. The discussion in Section

IV.B (specifically, the paragraphs covering Equations (4.4) to (4.7) and the one immediately following Equation (4.7)) does indicate that this is a very good approximation.

Some examples support these arguments and show that the C/I_e values at the ground receivers do not change by more than 1 dB when the satellites are moved by two degrees; an example will now be given to demonstrate this point. In this example the Bolivia and Paraguay satellites are located at 92 and 88 degrees west, respectively, a four-degree separation as suggested from the result in Table 4.1. The C/I_e results from the streamlined SOUP calculation are given in Table 4.3. Note that the worst C/I_e value is very close to the 30 dB single-entry protection requirement, which indicates that the $\Delta s(1)$ value of the approximate method is very close to that of the exact method.

4. Relation Between Service-Area Adjacency and △s(1) Value

For any adjacent service-area pairs the $\Delta s(1)$ values for a given protection requirement are approximately independent of the sizes and shapes of the service areas. This can be seen best from Equation (4.7); for adjacent service areas A and B, the test point d in service area A with the worst C/I_e is on or near the common border with B, and its $D_B(\Psi_{ti})$ will be approximately 1/2 (-3dB). This determines the required $D_d(\Psi_{ri})$, and Ψ_{ri} , and hence $\Delta s(1)$. As another way of looking at it, the carrier and interference power densities along the common border are nearly equal because they are designed to be approximately 3 dB below the respective beam-center power densities, which are designed to be

Table 4.3

 $\ensuremath{\mathsf{C/I}_{e}}$ Results to Show Validity of Approximate Method

COUNTRY	SATELLI	TE (LON.)	FREQUENCY	(MHz)	
EOL	-92	.øø	4 <i>EI</i> C.Ø	Ø	
PRG	-88	.00	4056.0	Ø	
TEST COUNTRY	: EOL	SATELLITE	: -92.00		
TËST P Lon.	OINT LAT.	INT. SAT.	C/I (dB)	MARGIN	(권명)
-65.Ø£	-12.20	PRG	59.67	29.67	
-65.5Ø	-9.8Ø	PRG	58.32	28.32	
-69.ØØ	-11.20	PRG	58.71	28.71	
-6 <i>D</i> .ØØ	-16.1Ø	PRG	38.82	8.82	
-57.5Ø	-18.00	PRG	33.23	3.23	
-67.5Ø	-22.7Ø	PRG	46.83	16.33	
TEST COUNTRY	: PRG	SATELLITE	: -88.ØØ		
TEST P LON.	OINT LAT.	INT. SAT.	C/I (dB)	MARGIN	(dB)
-57.6Ø	-25.3Ø	BOL	38.33	8.33	
-58.6Ø	-27.3Ø	BOL	41.27	11.27	
-56.20	-27.2Ø	BOL	44.88	14.88	
-54.7Ø	-25.5Ø	BOL	43.33	13.33	
-54.2Ø	-24.10	ĐOL	41.26	11.26	
-58.1Ø	-20.20	BOL	31.79	1.79	
-59.1Ø	-19.3Ø	BOL	30.75	Ø.75	
+62.2Ø	-20.5%	BOL	3Ø.£6	Ø.06	
-62.7Ø	-22.20	BOL	30.39	Ø.39	
-58.7Ø	-27.2Ø	BOL	40.86	1Ø.86	

equal. Therefore, the required margin between C and I_e is provided only by the satellite spacing. Since this is true for all adjacent servicearea pairs, the required satellite spacings are nearly the same. For the receiving reference pattern in Figure 2.5 and a 30 dB single-entry C/I_e protection requirement, these $\Delta s(1)$ values are approximately four degrees, as can be seen from several cases in Table 4.2.

The $\Delta s(1)$ values for two non-adjacent service areas are likely to be smaller, and depend on their shapes, sizes and the separation between them. This is evident from Equation (4.7) since $D_B(\psi_{ti})$ is likely to be smaller numerically (also in dB) in this case compared to the adjacent case. Heuristically, because of the service-area separation, the interference power densities in these two service areas are likely to have a deeper transmitting antenna discrimination loss relative to the carrier power densities. Therefore, the system needs less receiving antenna discrimination loss, $D_d(\psi_{ri})$, to achieve the required C/I_e ratio. This means that less satellite spacing, or a smaller $\Delta s(1)$ value, is needed. This is shown in several cases in Table 4.2.

D. RELATION BETWEEN SINGLE-ENTRY AND TOTAL ACCEPTABLE C/Ie PROTECTION REQUIREMENTS

In satellite communications, a scenario is evaluated by computing an equivalent margin (see Equations (2.8) and (2.9)), which takes into account all the interference, at all the test points. In Chapter II this was shown to be equivalent to comparing the aggregate C/I_e values with the total acceptable protection requirement. It is therefore essential that an assignment algorithm is based ultimately on the total acceptable protection requirement. However, it was also suggested in WARC-77 that the single-entry protection requirement can be used as a guide for determining sharing criteria; of course the total interference from all sources still must be calculated to evaluate the scenario fully [87]. The extended-gradient and cyclic-coordinate search methods discussed in Chapter III are based on the aggregate C/I_e values. In contrast, the methods in this chapter, using the Δ s concept, are based on single-entry C/I_e protection requirements. Clearly such an approach will be acceptable only if there exists some relationship between the single-entry and aggregate C/I_e values.

Although so far no such relationship has been established rigorously, it is generally felt that the single-entry C/I_e protection requirement does not need to exceed the total acceptable requirement hy more than a few decibels. In order to ensure that a scenario made on the basis of single-entry C/I_e protection requirement would result in acceptable aggregate C/I_e values, WARC-77 suggested that the single-entry C/I_e protection requirement be higher by 5 dB than the total acceptable protection requirement [78]. Note that numerically 5 dB is equal to 3; this suggestion is therefore based on the assumption that at the test point which has the worst aggregate C/I_e value the aggregate interference will not exceed three times the strongest single-entry interference. This assumption is supported by the characteristics of the satellite transmitting and ground receiving antenna reference patterns. Referring to Figures 2.4, 2.5 and Equation

(2.6), because these two reference patterns are highly directional, among all the received single-entry interference powers only the few that come from the main or near side-lobe of the transmitting reference patterns and are received in the main or near side-lobe of the receiving reference pattern are relatively strong; the others are generally weak enough to be negligible. However, it is difficult to prove rigorously that 5 dB extra protection requirement is absolutely enough to cover the difference between the single-entry and aggregate C/I_e values; hence the aggregate C/I_e results must be calculated to evaluate the feasibility of a scenario. In the numerical examples in this chapter, 5 dB extra protection was used for all service areas.

In any case, the methods to be described below do not depend on the validity of 5 dB, or any universal number. If the final analysis by the streamlined SOUP program shows more than 5 dB extra protection is needed for some service areas, then a more appropriate value may be chosen to compute the $\Delta s(1)$ values for an improved synthesis.

E. PERMUTATIONAL ASPECT OF THE ORBITAL-ASSIGNMENT PROBLEM

With a data base of $\Delta s(1)$ values for all the service area pairs, conceptually the planning problem could be solved by choosing a proper ordering or permutation of the satellites and completing the scenario by locating every satellite in its feasible orbital range while making

sure that the $\Delta s(1)$ constraints are satisfied. As an example, consider a four-service area case with the geographic relation as shown in Figure 4.4 with the objective of finding a scenario that uses the least orbit resource. The satellites are denoted as SA, SB, SC and SD. Assume that the values of $\Delta s_{BC}(1)$ and $\Delta s_{BD}(1)$, the required satellite spacings for the non-adjacent service areas, are constant and are two degrees; similarly assume that the $\Delta s(1)$ for all the adjacent service areas are constant and are four degrees. A scenario that meets this objective would be the ordering $S_D-S_B-S_C-S_A$ with minimum required satellite spacing because it requires only eight degrees of orbital arc. Arrangements that do not include both the s_B-s_C and s_B-s_D satellite adjacencies would have to require at least a ten-degree arc. In this example, with the objective of conserving orbit resource, the basic concept is to have adjacent satellites serve non-adjacent service areas; here it utilizes the service-area separation to reduce the need for satellite spacing, and achieves the maximum orbit utilization suggested in reference [16].







In such a brute-force procedure, it is likely that a feasible solution can not be found for a particular ordering. It could be that the available orbital arc for the task is used up before the allocation of all the satellites has been completed. Then, another ordering has to be tried.

Note that there are m! possible permutations for m satellites. This number becomes astronomical when m is large. If the goal is to find a scenario which is optimal by some criterion, in principle all the m! permutations have to be tested. Even if each test is simple and fast, the overall workload is still enormous.

F. ORBITAL ASSIGNMENT OPTIMIZATION FORMULATIONS

1. $\triangle s(1)$ Constraint and Objective Function

The orbital assignment problem can now be formulated as the optimization of a yet unspecified objective function, subject to the $\Delta s(1)$ constraints on pairwise satellite spacings. The protection requirements will be satisfied because of the constraints. Also, it is highly desirable if the $\Delta s(1)$ values are linear functions of the orbital variables so that a simple optimization technique, e.g., linear programming, can be used. This is apparently not true from Table 4.2 and Figure 4.3. Still, the $\Delta s(1)$ values can be approximated by piecewise linear functions, or the maximum value of $\Delta s(1)$ within a given orbital range, denoted as ΔS , can be used as a constant parameter in the optimization formulation. The objective function is, in principle, entirely arbitrary, but we shall restrict it to a linear function of the

orbital locations since the whole purpose of this approach was to avoid the computational complexity of nonlinear optimization.

The objective function used in the numerical examples below is the sum of the absolute deviations of the assigned satellite positions from an arbitrary prescribed set of such positions, an "ideal" set. Such an "ideal" set might arise from requests of the user administrations. Alternatively, it may be specified as a tool for the synthesis, e.g., if the westernmost end of the available orbital arc is selected as the "ideal" location for all satellites, the resulting scenario is likely to allow the insertion of additional satellites at the eastern end at a later time with a minimum of readjustment.

Other objective functions which have been proposed for minimization are the length of the occupied orbital arc and the constant zero. The latter simply seeks to find a solution which satisfies the Δ s(l) constraints.

2. Mixed-Integer and Restricted-Basis Linear Programming Formulations

With the single-entry C/I_e protection requirement enforced by the $\Delta s(1)$ constraints and a linear objective function, the problem can be formulated as a mixed integer program (MIP) [88]. Either the piecewise linear Δs functions or the constant ΔS parameters might be used to formulate this program; in this chapter the constant ΔS parameters will be used. The set of satellite locations which satisfy the ΔS constraints and the feasible orbital range constraints constitutes the

feasible region. When the problem is solved via the branch-and-bound algorithm, the globally optimal solution is guaranteed [88]. However, the computational effort required to find this solution can be prohibitively long when the problem size, i.e., the number of satellites, is large.

To ease the burden on computational effort, the same problem can be formulated as a linear program (LP) with a set of nonlinear side constraints; only the constant ΔS parameters can be used to formulate this program. A linear program is much more readily solvable than a nonlinear program or an integer program, and is most often solved by the simplex method [81]. However, in this problem, the nonlinear side constraints prevent one from using the simplex method in its most common form. The method can be modified to handle these nonlinear side constraints through the use of restricted basis entry. In doing so, one is certain to find a local, but not necessarily a global, optimum. The computational effort required by the LP technique should be acceptable when the problem size is large.

The MIP and the restricted-basis entry LP (RBLP) formulations are given in Appendix E as formulated by Professor Charles H. Reilly of the Department of Industrial and Systems Engineering for both of the non-trivial objective functions discussed above.

G. NUMERICAL EXAMPLES

1. Definition of the Problem

In this example, a model of six administrations in South America, as shown in Figure 4.5, is used; they are Argentina (ARG), Bolivia 113





(BOL), Chile (CHL), Paraguay (PRG), Peru (PRU), and Uruguay (URG). The feasible orbital ranges for all the administrations are taken to be from 80 to 110 degrees west. It is assumed that all satellites have the same frequency assignments. The antenna reference patterns are from Figures 2.4 and 2.5. The optimization requirement is to minimize the sum of the deviations of the actually assigned positions from the satellite preferred locations. Three sets of satellite preferred locations are considered, as listed in Table 4.4: in case 1, all the preferred satellite locations are at the center of the feasible range; in case 2, all the preferred satellite locations are at the western boundary; in case 3, every administration has its preferred satellite location at a longitude for which the azimuth angle of the satellite from the administration center is close to zero.

First, all the $\Delta s(1)$ values must be calculated. They were calculated using a 30 dB single-entry protection requirement; the results are listed in Table 4.2. The ΔS values of the six-administration problem, obtained from Table 4.2 by choosing the maximum $\Delta s(1)$ values over the feasible range 80 to 110 degrees, are listed in Table 4.5. They are denoted as ΔS_{ij} for satellite i and j in Appendix E. Using the ΔS parameters instead of the approximate piecewise linear Δs functions results in a conservative design (C/I_e will tend to be larger), at the expense of possibly not using the orbit resource with maximum efficiency; but the alternative, i.e., using the Δs functions instead of the ΔS parameters as constraints, would complicate the MIP formulations; note that the piecewise linear constraints can not be used in the RBLP formulation.

1able 4.4	Ta	b1	е	4.	4
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Satellite preferred locations of six

administrations

preferred	ARG	BOL	CHL	PRG	PRU	URG
case 1	95	95	95	95	95	95
case 2	110	110	110	110	110	110
case 3	87.5	92.5	97.5	87.5	102.5	82.5

Table 4.5

 ΔS parameters of six administrations

۵S	ARG	BOL	CHL	PRG	PRU	URG
ARG	*	4.17	4.19	4.32	1.41	4.14
BOL		*	4.57	4.04	4.26	0.94
CHL			*	2.00	3.94	1.59
PRG				*	1.10	2.46
PRU					*	0.37
URG						*

2. MIP and RBLP Results

The solutions of the MIP and RBLP fomulations for this objective function, i.e., Formulations III and IV in Appendix E, are listed in Table 4.6 together with the values of the total deviations, the occupied orbital arcs and the computer run times in seconds. These data were provided by Professor C. Reilly and Mr. D. Gonsalvez of the Department of Industrial and Systems Engineering.

Because of the ΔS constraints, the solution is guaranteed to satisfy the single-entry C/I_e protection requirements; still the aggregate C/I $_{\rm e}$ values need to be checked. By assuming that the term $1/{f_n^2 \cdot \sum_m [F(f_n, f_m)/f_m^2]}$ equals one in Equation (4.3), this becomes a co-channel interference calculation. The aggregate C/I_e results of the MIP solution of case 1 (which happens to be the most densely packed solution), calculated from the streamlined SOUP code in Appendix A, are listed in Appendix F. The results show that of the total 54 test points, only three places in Chile, three places in Paraguay and one place in Peru have aggregate C/I_e values between 27 to 30 dB while all the rest of the C/I $_{\rm e}$ values are above 30 dB. Note that the ${\rm \Delta S}$ values (Table 4.5) were calculated from single-entry C/I_e protection requirement of 30 dB, with the objective of guaranteeing that the aggregate C/I $_{\rm e}$ values be no less than 25 dB (see the discussion in Section IV.D). Clearly this objective has been achieved; in fact, the aggregate C/I_e results are better than expected.

A likely reason for the aggregate C/I_e values to be better than expected is the following. First note that in this example every

Table 4.6

Mixed integer and linear program results

	cas	e 1	cas	e 2	cas	e 3
satellite	MIP	LP	MIP	LP	MIP	LP
ARG	88.68	105.74	101.35	110.00	88.76	101.26
BOL	99.57	101.57	97.18	104.33	92.93	92.50
CHL	95.00	97.00	105.54	99.76	97.50	97.07
PRG	93.00	95.00	107.54	97.76	84.44	87.50
PRU	91.06	93.06	109.63	108.59	102.50	102.67
URG	96.59	92.54	110.00	105.86	81.98	82.50
deviation	18.42	23.71	28.76	33.69	5.27	14.36
arc	10.89	13.20	12.82	12.24	20.52	20.17
cpu(sec)*	25.23	1.31	13.39	1.30	2.86	1.25

* IBM-3081 computer

administration requires only one satellite. For a satellite and its corresponding service area, usually only the first adjacent satellites on both sides are close enough to produce significant interference, and these satellites do not usually influence the same test point; interference from far-away satellites are in general negligible because the actual satellite spacings are much larger than the required minimal spacings. This can be seen from the C/I_e results in Appendix F: among the seven test points with C/I_e less than 30 dB, only two receive two strong and almost equal signal, i.e., the two in Chile with C/I_e of 27.52 dB and 28.37 dB, and none receive more than two. Therefore the 5 dB margin between single-entry and total acceptable protection requirements is adequate for these sample problems; this confirms the argument made in Section IV.D.

3. Comparison Between MIP and RBLP Techniques

Referring to Table 4.6, note that the total deviations in the MIP solutions are smaller than those of the RBLP solutions. This is not unexpected since the MIP solution guarantees a global optimum with respect to the objective function while the RBLP formulation does not. On the other hand, the computer run times for the MIP formulation are significantly longer, and they are known to increase more rapidly with problem size than is the case with the RBLP formulation. As stated in Section IV.F.2, the computer run time could be prohibitively long for the MIP formulation when the problem size, i.e., the number of satellites, is large. Therefore, the RBLP formulation becomes more

attractive as a practical method of solving a real-world problem. The MIP formulation is useful primarily for evaluating the performance of the RBLP formulation on small problems.

4. Suggestions for Further Improvement

The C/I_e ratios in Appendix F suggest that a uniform 5 dB margin between the single-entry and total acceptable C/I_e protection requirements may result in over-protection. This raises the concern that, for a limited orbit resource and a large number of requests, a satisfactory scenario might never be found if the orbit resource barely allows every service area to have only the threshold aggregate C/I_e value.

When a feasible solution of the MIP or RBLP formulation does not exist for a given set of ΔS constraints, the reason could be either that the ΔS constraints are too high, or that there exists no solution that could satisfy the total acceptable C/I_e protection requirement. To find out which, a progressive testing process could be used by gradually decreasing the C/I_e requirement level in the $\Delta S(1)$ calculation, and using these values in the MIP or RBLP calculation. Note that as the single-entry C/I_e requirement is gradually decreased, the first point at which a feasible solution (feasible in terms of the ΔS requirements) exists may be such that the total acceptable C/I_e requirement is not satisfied at some test points. However, this does not mean that a feasible solution (feasible in terms of total acceptable C/I_e requirement) does not exist; this is because the margins between the

single-entry and total acceptable C/I_e protection requirements may not have to be the same for all satellite pairs. When this is the case it is proposed that the gradient search method be used to fine-tune the solution and improve those unacceptable aggregate C/I_e values; this approach is discussed below. If no solution is obtainable when the $\Delta s(1)$ values are calculated using the total acceptable C/I_e protection requirement and the ΔS parameters are the minimum (over 1) of the $\Delta s(1)$ values, a feasible scenario definitely does not exist.

To demonstrate how the gradient search method can fix the worst C/I_e terms, the resulting satellite locations of the MIP solution of case 1 are laid out as shown in Figure 4.6; here B is for satellite of Bolivia, U of Uruguay, C of Chile, P of Paraguay, E of Peru, and A of Argentina. Indicated in the figure are the actual spacings (above the arrows) and the ΔS values (below the arrows) between a satellite and its first and second adjacent satellites. The star (*) sign means that the actual spacing is larger than the corresponding ΔS value. First note that there is no star sign for the Chile satellite, while other satellites have at least one star. This means that the spacings between the Chile satellite and its first and second adjacent satellites are all at their minimal required values. This may explain why the C/I_e results for Chile are worse than the others. Then note that this scenario may be modified by moving the Peru satellite to the right (eastward) and moving the Uruguay satellite to the left (westward) by a small amount. Although this modification increases the sum of the absolute deviations from the "ideal" locations, it also improves the $\ensuremath{\mathsf{C/I}_{e}}$ results for Chile





(igstarrow : Actual separation larger than required separation.

by increasing the satellite spacings for the Chile satellite; note that the Peru and Uruguay satellites are its east and west adjacent satellites. This demonstrates that the gradient search technique can be used on the MIP or RBLP solution to improve the aggregate C/I_e results.

5. Possible Extensions of the Method

The ΔS concept has many flexibilities. It was demonstrated here for elliptical satellite antenna beams, but it can also be applied to shaped beams if the shaped beam reference pattern is given. At present, such a pattern is not available. Also, to use the Δs approach the antenna reference patterns and the C/I_e protection requirement need not be the same for all administrations. Such non-uniformity merely changes the interference calculations, margin calculations, and the resulting $\Delta s(1)$ values, but the same optimization procedures are still applicable.

The formulations may be useful when new satellites need to be added into an existing scenario in which the locations of existing satellites can not be changed. The computational burden of either technique depends greatly on the number of decision variables. For a task of adding more satellites, all the information about the existing scenario constitutes fixed parameters, and the only decision variables correspond to the new satellites. Therefore, the problem size is small, and the computational burden is reasonable.

This chapter has dealt only with the orbital assignment, not the frequency assignment. This is useful for the case that every satellite uses the full complement of the available spectral band. Still, the

same procedure should work if there is an a priori frequency assignment scenario; a considerable body of literature exists on such frequency assignments [19,20,21,22]. The only modification is to use the proper protection requirement value (by referring to the frequency assignments and protection ratio) in the Δ s(l) calculation; the planning process will be exactly the same.

H. CONCLUSION AND RECOMMENDATION

In this chapter, two techniques are presented to solve the orbital assignment problem. The MIP technique guarantees to find the globally optimal solution, but may require prohibitively long computing time when the problem size is large. Still it is very useful for testing other methods on small problems and may be applicable when a few satellites are added into an existing scenario. The RBLP technique guarantees to find a locally, but not necessarily a globally optimal solution, but is more practical in terms of the computational effort.

Two approximations are used in these methods. The first one appears in the $\Delta s(1)$ calculation; however, it is shown to be acceptable. The second one is to use maximum $\Delta s(1)$ values, ΔS , in the MIP and RBLP formulations; this decreases the efficiency of orbit use, but probably not seriously.

It is recommended that these methods be tried on larger scenarios, and that the extensions given in Section IV.G.5 be investigated.

CHAPTER V

A SERVICE-AREA SPECIFICATION PROCEDURE

A. INTRODUCTION

In the previous chapters the optimization of orbital and frequency assignments was considered for communications satellites serving a given set of service areas defined by political boundaries. Now, procedures for choosing such service areas will be discussed in the fixed-satellite service (FSS) context, with the objective of increasing the communications capacity for all users. The need to study ways in which the concept of service areas should be defined was brought up in CCIR report 453-3 [89], and the study in this chapter is intended to give insight to that concept. By means of an illustrative example it will be shown that the considerations of traffic-demand density and of minimum allowable spacing (Δ S, see Chapter IV) can serve as a basis for designing service areas for this objective.

B. HISTORICAL PERSPECTIVE

1. Service Area Assignment

In the broadcasting-satellite service (BSS) planning, a satellite service area is usually specified by the territories of an administration, a subdivision of an administration, or (in some cases) a

grouping of administrations [9,13]. Thus there appeared to be no need for a procedure for defining service areas for the WARC-77 and RARC-83 deliberations.

The situation is quite different with respect to FSS. The FSS satellites were initially used primarily for inter-administration communications. International consortia operated such satellites, with service areas chosen on the basis of demand (or market), technological considerations, and the composition of the consortium. The Intelsat satellites are examples of this type of operation. More recently, satellites have also been employed for intra-administration (Domsat) communications, e.g., satellite communications in U.S., Canada and the U.S.S.R. (if the latter is considered as a single entity; technically the International Telecommunication Union (ITU) regards each separate Soviet Republic as an administration) [90]. The simplest technology leads to large service areas; e.g., the whole contiguous continental U.S. (CONUS). While an experimental FSS satellite using regional and switched spot beams is at the heart of the NASA Advanced Communications Technology Satellite (ACTS) program [91], most civilian U.S. operational and planned systems are based on CONUS coverage. In current approaches to the orbital and frequency assignments for the FSS, the idea of specifying service areas by the territories of the administrations seems to be still prevalent.

2. Insufficiency of Communications Supply from Limited Spectrum and Orbit Resources

As FSS planning proceeds, it has become clear that the communications demand is very large [92,93]. As an example, the U.S. fixed-service communications supply appears to be in great mismatch with the demand [80,94]. The projected U.S. domestic FSS communications demand in the year 2000, as estimated in a COMSAT Laboratory report, is shown in Table 5.1, and is also shown as a "pie chart" in Figure 5.1 [94]; the total communications demand is equivalent to 2,474 transponders.

By international agreement the total bandwidth of the 6/4 GHz spectral band assigned to the FSS is 480 MHz [94,95] (note that at present this is the only band in the planning stage). This band is divided into 12 slots, each consisting of a frequency channel 36 MHz wide followed by a guard band of 4 MHz. Therefore, including the cross-polarization channels, there are 24 frequency channels in this band [94,95]; this is shown in Figure 5.2. A typical U.S. FSS satellite has 24 transponders transmitting the signals in these 24 channels. Therefore the total estimated demand of 2,474 transponders implies a need for 103 satellites to fulfill the demand with the 6/4 GHz band.

Because of interference between satellite systems, satellites must be separated from each other to have proper protection [16,96,97]. For the antenna technology available up to the year 1982, satellites with CONUS beams for systems proposed at that time needed to be separated by more than three degrees [98]. However, the amount of communications capacity so provided in the 6/4 GHz band is far from enough to satisfy

35x 10 ³ Channels60 Channels111625038Mbitts/s1.5Mbitts/MHz4774770.68 Channels0.68 Channels/MHz174770.68 Channels0.66 Channels/MHz92vIDE0233Channels0.069 Channels/MHz9250Channels0.028 Channels/MHz92		6816 x 10 ³ Channels 120 Channels/MH _z 1578 3348 Mbits/s 2.0 Mbits/MH _z 41 7814 Channels 1.1 Channels/MH _z 203	IRAFFIC BM EFFICIENCY TRANSPONDERS (3	TRAFFIC FORECAST SUMMARY - YEAR 2000 TRAFFIC FORECAST SUMMARY - YEAR 2000	s/MHz 1578 11 ₂ 1578 s/MHz 203 s/MHz 16 HZ 477 s/MHz 477	2.0 MDIUS/MUZ 1.1 Channels/F 60 Channels/H 1.5 Mbits/MHZ 0.68 Channels/M	6816 x 10 ³ Channels 3343 Mbits/s 7814 Channels 35 x 10 ³ Channels 411 Channels
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Table 5.1

TRANSPONDER ALLOCATIONS

(US Domestic Traffic)



TRUNKING (1822)

Figure 5.1. Projected U.S. Domestic FSS coommunications demand for the year 2000. CPS stands for Customer Premises Service. The number in parentheses indicates number of transponders.

Downlink Channelization CFD1

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$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	N		- 4.120
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		50	- 4.100
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			- 4.080
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			- 4.060
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	12		- 4.040
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	15		- 4.000
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m = -3.760 -3.740 -3.720			- 3,789
	~		
- 3.720			- 3.760
- 3.720		ري ا	- 3.740
			- 3.720

Figure 5.2. Allocation of frequency channels in 6/4 GHz band.

the FSS demand [99]. In order to increase the communications supply, the Federal Communication Commission (FCC) decided that the orbit resource should be more efficiently utilized and announced in the year 1984 that future antenna technology should allow two-degree spacing for U.S. FSS satellites, and satellite orbital planning should be based on two-degree spacing after the year 1987 (This also applies to the 14/12 GHz band) [80]. This will enable the U.S. to have about 25 geostationary satellites in the 6/4 GHz band. Clearly this still falls far short of the projected demand of 103 satellites!

Other spectral bands, e.g., the 14/12 GHz band, have been allocated to the FSS [31]. This should help increase the U.S. FSS communications supply. Still, it is apparent that the spectrum resource is limited, and that the orbit resource should be more efficiently utilized in order to maximally re-use the spectrum resource.

3. Relation Between Frequency Re-Use and Service-Area Specification

The advantage of using narrow antenna beams to achieve frequency re-use has been recognized for some time [89,100]. Thus it was noted in CCIR report 453-3 that it is necessary to study ways in which the concept of coverage area should be defined [89]. Specifically, It was brought up in this report that under certain circumstances a satellite may transmit separate information on the same frequencies twice, or even a greater number of times, using antennas serving different parts of the world. This general idea has already found practical application with

the Intelsat series of satellites; while Intelsat IV satellites used global-coverage beams, Intelsat IV-A and V satellites employ hemispherically restricted beams to allow frequency re-use [101,102].

In view of the scarcity of the spectrum/orbit resources relative to demand, it becomes necessary to develop a method of specifying service areas such that the advantages of the narrow-beam concept can be fully utilized for efficient spectrum/orbit management.

C. SERVICE-AREA SPECIFICATION BY △S CONCEPT AND COMMUNICATIONS-DEMAND DENSITY

1. Role of **AS** Concept in Service-Area Specification

In order to provide more traffic supply, the Δ S concept discussed in Chapter IV suggests that the Δ S values between satellite pairs should be as small as possible so that more satellites can be allocated in the orbit. As discussed in detail in Section IV.C, the margin between the carrier power, C, and the single-entry interference, I, comes mainly from the transmitting and receiving antenna discrimination factors in the interference power; the former comes from the separation between the two service areas, the latter from the separation between the two satellites. Also, as discussed in Section IV.C, for a given single-entry C/I protection requirement, the larger the transmitting discrimination loss, the less the receiving discrimination loss and thus the less satellite separation is needed. For the special case when the transmitting discrimination loss is enough for the protection
requirement to be met, the satellites can be collocated, or equivalently a satellite can have two beams serving two service areas simultaneously; this is exactly what CCIR report 453-3 means by using the same frequency band twice at one satellite [89].

Referring to Figure 2.4, the transmitting discrimination value depends on two factors: the half-power beam width (HPBW) and the off-axis angle. The value of HPBW depends on the size of the service area: the smaller the service area, the smaller the value of HPBW, and the narrower the beam; this is the narrow-beam idea stated in references [89,100]. The off-axis angle depends on the service-area separation. The combination of these two factors should be the key to the subject of service-area definition. If the system planner can control these two factors to reduce the Δ S values between satellite pairs, more satellites can be assigned in the orbit and a larger communications supply; i.e., more circuits, can be provided. To achieve this purpose, basically the service areas should be as large as possible.

2. Role of Communications-Demand in Service-Area Specification

The simple demand/supply concept implies that the supply should be used where the demand is; hence the communications-demand density must also be consulted in specifying service areas. There is precedent for using communications traffic-demand density quantitatively in the technical design of satellite systems. In time-division multiple access

(TDMA) system design, a simple rule is: the areas with heavy communications demand should be given more access to the communications system [103]. Similarly, service areas should specify regions with enough traffic demand to justify having satellite access as an area. Hence information about the communications traffic-demand density is an essential prerequisite to a reasonable choice of service areas.

3. General Consideration

Hence, the ΔS concept and the communications traffic-demand density should both be considered when specifying service areas. It is apparent that small and separated service areas allow the geostationary orbit to be used more efficiently; on the other hand, potential demand increases with the service-area size: a satellite which serves one metropolitan area (e.g., Boston) has less potential demand than one which serves a corresponding region (e.g., the Eastern U.S.) or the entire administration or a grouping of administrations. There has to be a compromise between these two factors. The overall rule is that the selected service areas must have enough communications demand to justify their own satellite beams.

There are, of course, other factors which need to be taken into account in a practical plan. For example, multiple-beam satellites, which may also be beam-switching, require more advanced technology and are likely to be more expensive than single-beam ones. Such economic and perhaps other operational matters will not be considered here; only the communications capacity will be addressed.

D. APPLICATION OF SERVICE-AREA SPECIFICATION CONCEPT TO A LARGE ADMINISTRATION OR GROUP OF ADMINISTRATIONS

1. General Description

The idea of service-area specification by the ΔS concept and traffic-demand density may greatly benefit an administration, or a group of administrations, that has a large territory, when most of the traffic demand is between several small regions. When this idea is applied to such a situation, it is proposed to serve such administration(s) with a mixture of administration-coverage beams and intra-administration regional beams. The administration-coverage beams are intended to serve primarily areas of relatively low demand, while the majority of traffic demand from high-demand regions would be carried on the regional beams. The necessary separations between regional-beam satellites are usually smaller than those of the administration-coverage satellites. Thus if, instead of assigning the entire available orbital arc to administration-coverage satellites, a part is used to accommodate regional-beam satellites, then more satellites can be allocated in this arc and more communications supply can be provided.

Recall the scenario which has 25 CONUS beam satellites in the 6/4 GHz band with every satellite using the full spectral band (Section V.B.2). At first look it seems that this scheme uses the spectrum and orbit resources to their full extent for Earth station antenna technology which requires two-degree satellite spacing. However, if some of the service areas are changed from CONUS to smaller, separated

regions, the ΔS values for their satellites will be smaller than two degrees, hence some orbit resource becomes available to allocate more satellites in the orbit.

2. Procedure of Service-Area Specification and Satellite Assignment

When regional service areas are to be specified, first the traffic-demand density should be considered. Because of the population distribution or the commercial activities, usually there will exist some regions of relatively small size and large traffic demand. Often such regions include several large cities relatively close to each other. Such regions are good candidates for regional service areas within the administration(s). In selecting these service areas, three things should be considered simultaneously: the areas should be of small size, they should have large traffic demand, and the separations between these service areas should be large.

After the regional service areas have been selected tentatively, the Δ S values between these service area pairs should be calculated by the method described in Chapter IV. Note that service areas for which the Δ S values are zero can be served by a single satellite; this is the multiple-beam design described in CCIR report 453-3. Different from the multiple-beam TDMA design, in this case the two beams can be active simultaneously [104]. Also note that multiple-beam satellites can carry both inter- and intra-regional communications.

A traffic-demand matrix can be formulated for these tentative service areas. The elements in this matrix are traffic demand between

the regions that can be carried by the regional-beam satellites: the diagonal elements are the intra-regional taffic demand, the off-diagonal elements are the inter-regional traffic demand. The latter are non-zero only when the corresponding service areas can be served by multiple-beam satellites. A complete demand matrix consists of the above-described matrix plus one additional element: the traffic demand which cannot be carried by regional satellites and must be carried by administration-coverage satellites.

Examination of the ΔS and demand matrices may suggest a revision of the regional service areas. For example, if many of the ΔS values for a particular region are large (e.g., approaching the ΔS value for administration-coverage satellites), this may indicate the region is too large, or too close to other regions, or both. On the other hand if many of the demand matrix elements corresponding to a region are very small, this may indicate the region is too small, or it is not a good candidate to be a regional service area. Thus a good choice of regional service areas becomes a compromise between achieving satisfactory ΔS values and a satisfactory demand matrix, as will be evident from the example below.

A scenario including both regional and administration-coverage beams may, in principle, be constructed by any suitable method, e.g., by extensions of the methods of Chapters III and IV. Here a scenario will be generated by deassigning some of a series of equally spaced administration-coverage satellites and then allocating regional-beam satellites in this vacated orbital arc, consistent with the ΔS

requirement. The number of administration-coverage satellites to be deassigned and the number of regional beams to be assigned are determined by consulting the traffic-demand matrix. This procedure has the advantage of being compatible with a network of uniformly spaced administration-coverage satellites; the new scenario might even evolve out of such a system. It also has the advantage of demonstrating the important concepts without the computational complexity of optimization.

3. Traffic Distribution Between Narrow- and Wide-Beam Systems

The traffic-demand problem is completely solved when the amount of traffic-supply is enough, or more than enough, to meet the demand. However, as stated earlier, the demand usually far exceeds the supply, and usually the adoption of the regional-service area idea can only improve, but not completely solve the demand/supply problem. Therefore, an important task of the procedure is to make sure all the demands have their proper share of the supply.

It will be assumed that the satellites serving the regional service areas are dedicated satellites which are not designed to provide administration-wide service. Therefore some satellites need to be preserved to provide administration-wide communications service, even though the traffic demand which can not be served on a regional basis may be small. Many criteria could be used to decide the distribution of satellite beams. It is known that, compared to a scenario with only administration-coverage beams, there will be a larger communications supply when the narrow-beam idea is implemented. Therefore, one

criterion might be that all the demands have an equal percentage of supply-increase, another criterion might be that the total communications supply has the maximum amount of increase and no one suffers any supply decrease. The latter is used to develop the scenario in Section V.E.

E. NUMERICAL EXAMPLE

1. Description of Parameters

Since the only available detailed traffic-demand density data available to the authors is the projected long-distance telephone traffic among major cities in the U.S., it will be used in an example to numerically explore the advantage of the service area specification concept. Because only the 6/4 GHz band is in the planning stage, this example considers the communications capacity only for this band. Also, only the down-link communications traffic regulation problem will be considered; the up-link problem can be implemented similarly in the up-link spectral band.

Of the total projected FSS communications demand shown in Table 5.1, more than 63% consists of long-distance telephone voice traffic [94]. The telephone voice demand will be taken as indicative of total demand. This assumption is justified in part because only telephone voice data is available to us, in part because it seems likely that the geographical distribution of other communications will be similar to that of telephone voice traffic, and in part because the objective here

is only to demonstrate a method, not to design a system. More detailed examination shows that a large portion of the voice long-distance telephone demand comes from major cities (or metropolitan areas), and there are 28 cities that share more than 75% of the voice long distance telephone demand. The list of these 28 cities, and the projected long distance voice telephone demand between them are shown in Table 5.2 [94]. The U.S. map in Figure 5.3 shows the locations of these 28 cities with their communications rankings: the cities indicated by triple circles are in the top 5 rankings, double circles are for rankings from 6 to 10, single circles for rankings from 11 to 15, and solid dots for rankings from 15 and up.

In order to arrive at Δ S values and C/I ratios consistent with the antenna patterns shown in Figures 2.4 and 2.5, the C/I results of two CONUS beam satellites with 2.5-degree spacing were calculated and are listed in Table 5.3, and the worst single-entry C/I value is 25 dB. This value will be used as the single-entry C/I protection requirement for the U.S.; the total acceptable C/I protection requirement will then be 20 dB if 5 dB extra protection is needed to compensate for multiple interference. It is not implied here that 2.5-degree spacing or a 20 dB aggregate protection ratio is recommended. The purpose here is only to arrive at a consistent set of parameters for demonstrating a regional-coverage assignment procedure.

The calculations in this section are on a co-channel basis. Since adjacent channels in the scheme of Figure 5.2 are cross-polarized, it is assumed that there is enough polarization and frequency discrimination that this is a satisfactory approximation.

Long Distance Voice Telephone Demand Between Top 28 Cities in U.S. in the Year 2000

US DOWESTIC VOICE IRAFFIC

TRAFFIC MATRIX EARTH STATION TO EARTH STATION IN 2000 IS 68146 CHANNELS.

TOTAL TRAFFIC FOR US

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ES HAME INEW-YORK INEW-YORK INEW-YORK INEW-YORK INEW-YORK INEW-YORK INEW-YORK INEW-YORK INEW-COS SAN-FRAH BOSJOH BOSJOH BOSJOH BOSJOH BOSJOH BOSJOH BOSJOH BOSJOH DALLAS ALAHIA ATLAHI

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Table 5.2 (Continued)

US DOWESTIC VOICE TRAFFIC

TRAFFIC MATRIX EARTH STATION TO EARTH STATION

TOTAL TRAFFIC FOR US

IN 2000 IS 68146 CHANNELS.

	2	63	- 15	72	60	65	65	65	57	57	46	† 2	38	34	30	30	27	27	23	0	23	61	- 61	15		-	=	8		1
M1111EA	2	_			_	_	_	_			_		_						_						_				12	
TAMPA 19	228	107	95	76	12	68	68	68	91	61	64	42	96	54	30	30	J 0	27	0	23	23	23	19	15	Ξ	=	Ξ	8	1328	
RALE1GH 18	251	118	101	84	80	76	76	72	68	65	53	49	42	38	34	11	34	0	27	27	27	23	23	15	15	=	Ξ	8	1468	
21_101_12	262	126	011	87	8/	80	80	76	12	68	51	61	46	42	38	1 +0	0	140	30	27	27	23	23	151	15	15	15	8	1546	+
11 AMI 16	274	129	811	15	16	84	8	80	76	72	19	53	64	42	30	0	34	34	30	30	30	27	23	61	15	15	15	8	1622	
SYRACUSE 15	289	1 2 2 1	122	95	92	87	87	84	80	76	919	53	61	46	0	38	38		30	30	30	27	27	19	15	15	15	=	1690	
14 14	312	148	1551	103	103	95	95	16	84	80	68	61	53	0	46	42	42	38		40	10	30	27	19	61	15	15	=	1832	
ATLAHTA 13	346	164	148	114	11	101	103	103	95	16	76	68	0	53	64	64	46	42	38	38	38	5	30	23	61	61	19	=	2033	
ANAHE IM 12	384	183	164	129	126	1	*=	11	101	66	84	0	69	19	53	53	61	6+	42	42	42	38	10	27	23	19	19	15	2252	
041145	1	205	183	145	141	129	129	126	118	1	0	84	76	69	61	61	57	53	1 9	46	46	42	38	27	27	23	23	15	2520	
02	=		5	4	\$	9	7	80	6	0	Ξ	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28		
ES. HAME	NUUT WITH	I TOS_ANGL	CHICAGO	SAH_FRAN	BOSTON	DE TROLI	WASHINGT	CINCINNA	PHILADEL	CLEVELIE	DALLAS	ANANE IM	ATLANIA	HOISDON	SYRACUSE	M MI	SI_LOUIS	RALEICH	TANPA	MINNEAPL	SEATTLE	KANSAS_C	DENVER	MILWAUKE	SAN ANTO	PHOFMIX	NEW ORLE	SALT_LAK	TOTAL	

Table 5.2 (Continued)

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US DOWESTIC VOICE TRAFFIC

TRAFFIC MATRIX EARTH STATION TO EARTH STATION

IOIAL TRAFFIC FOR US

IN 2000 IS 68146 CHANNELS.

Ī	Ī								++
S. HAME	10.	SEATTLE 21 21	KANSAS_C	DENVER 23	MILWAUKE	SAN_AHIO 25	PHOENTX 26	NEW_ORI E 27	SALT_LAK
UW_YORK	-	217	194	183	133	122		114	76
S_ANGL	2	103	16	84	65	57	53	53	•
IICACO	5	16	84	76	57	53	46	46	30
UL_FRAN	*	72	65	19	46	42	38	90	27
DSTON	S	68	61	57	42	36	1	5	23
TROIT	9	65	57	53	38	38	34	34	23
VSHINGT	7	65	57	53	38	3.8	5	J.	23
INCINNA	8	65	57	53	38	34	30	30	23
IILADEL	6	57	53	64	38	5	30	30	61
EVELND	101	57	49	46	5	30	27	27	19
VELAS	=	46	42	38	27	27	23	23	15
IAHE IM	12	42	38	1	27	23	19	61	15
LAHIA	1.1	38	34	30	23	61	61	61	=
USTON	-	5	30	27	61	19	15	15	Ξ
RACUSE	15	30	27	27 1	61	15	15 1	15	Ξ
Inv	16	30	27	23	61	15	15	15	8
_LOUIS	12	27	23	23	15	15	15	15	8
I E I CH	18	27	23	23	15	15	Ξ	Ξ	8
רוי ⊳ ע	61	23	23	61	15	Ξ	=	=	8
HILEAPL	20	23	19	19	15	=	=	=	B
ATTLE	21	0	19	61	15	=	=	=	80
NSAS_C	22	19	0	15	1	Ξ	8	8	8
IVER	23	61	15	0	=	=	8	8	•
LWAUKE	24	15	Ξ	Ξ	3	8	8	8	*
1 OINV 1	25	=	=	=	ß	0	*	4	-
JENIX	26	=	80	8	B	•	0	-	-
V_ORLE	27	Ξ	8	8	83	4	-	0	4
LI_LAK	28	8	8	•	•	*	4	•	0
I J VI OI	 	1274	1134	1054	788	1 602	641	6414	1 36
•	•	-				- · · ·	,	-:;	-)))



Figure 5.3. Locations of top 28 cities in U.S. with largest long-distance telephone demand in the year 2000. Î

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C/I Results of Two CONUS-beam satellites with

2.5-degree spacing

COUNTRY	SATELLITE	(LON.)	FREQUENCY (MHz)
USA	-100.00)	4000.00
USA	-102.50)	4000.00
TEST COUNT	RY : USA	SATELLITE	: -100.00
TEST Lon.	POINT LAT.	INT. SAT.	C/I (dB)
-69.20	47.40	USA	-108.35
-66.90	44.80	USA	-108.29
-69.90	41.50	USA	-107.71
-81.80	24.40	USA	-108.44
-97.20	26.00	USA	-107.61
-117.10	32.30	USA	-108.47
-124.20	40.40	USA	-108.50
-122.80	49.00	USA	-108.39
-95.10	49.40	USA	-107.22
TEST COUNTR	RY : USA	SATELLITE	: -102.50
TEST Lon.	POINT LAT.	INT. SAT.	C/I (dB)
-69.20	47.40	USA	-108.35
-66.90	44.80	USA	-108.30
-69.90	41.50	USA	-107.72
-81.80	24.40	USA	-108.41
-97.20	26.00	USA	-107.60
-117.10	32.30	USA	-108.51
-124.20	40.40	USA	-108.54
-122.80	49.00	USA	-108.41
-95.10	49.40	USA	-107.19

2. Specifying Four Service Areas According to AS Consideration and Traffic-Demand Density

Referring to Figure 5.3 about the communications traffic-demand density, four service areas that cover most of the top 28 cities may be specified as shown in Figure 5.4. The first service area, called the East region, covers the cities New York (1), Boston (5), Washington D.C. (7), Philadelphia (9), and Raleigh (18). The second service area, called North Central, covers Chicago (3), Detroit (6), Cincinnati (8) and Cleveland (10). The third service area, called West, covers Los Angeles (2), San Francisco (4) and Anaheim (12). The fourth service area, called South Central, covers Dallas (11), Houston (14), San Antonio (25) and New Orleans (27). These regional service areas were obtained by trial and error as reasonable compromises between the ΔS matrix and demand matrix requirements. For example, the traffic demand for the North Central region could be increased by including Syracuse (15), St. Louis (17), Minneapolis (20), Kansas City (22), and Milwaukee (24); however, this would increase its size and reduce the separation between regions, thus it would increase $\Delta S_{E,NC}$ and $\Delta S_{NC,SC}$ sufficiently to prohibit sufficient frequency re-use. Even as it is, $\Delta S_{E,NC}$ turns out too large to use a multiple-beam design. Its size could be reduced by eliminating Chicago (3) and Detroit (6) from this region, but then the traffic-demand might be too low to justify having its own satellite beams. This illustrates the compromise between ΔS and traffic demand which must be the basis in specifying regional service areas.



Four selected regions with proper service-area separation and large communications demand. Figure 5.4.

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The Δ S matrix of the four service areas is shown in Table 5.4: the Δ S values between any two of the four service areas, except between East and North Central, are zero. To demonstrate that a multiple-beam scheme is feasible, the C/I ratio of a three-beam satellite serving East, West and South Central is shown in Table 5.5, and the C/I ratio of a three-beam satellite serving North Central, West and South Central is shown in Table 5.6; in both cases, the worst aggregate C/I values are larger than 25 dB. The Δ S value between East and North Central is 1.24 degrees, as indicated in Table 5.7; however, for numerical convenience 1.25-degree spacing will be used for the East and North Central satellites.

With this ΔS matrix, there can be two classes of regional-beam designs for satellites serving these four regions. In the first one the service areas East, West and South Central, or any combination of these, can use one multiple-beam satellite. In the second, the service areas North Central, West, and South Central, or any combination of them, can use one multiple-beam satellite. There are two overall restrictions: satellites serving the East and North Central regions respectively need to be separated by at least 1.25 degrees, and any two satellites that serve the same service area must be separated by no less than 2.5 degrees. Aside from these restrictions, a scenario can have any combination of the two regional-beam designs. For example, two adjacent satellites that serve the regions East and North Central, respectively, can also serve the service areas West and/or South Central.

Table 5.4	
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	۵S	East	N. Central	West	S. Central
	East	2.50	1.25	0	0
N.	Central		2.50	0	0
	West			2.50	0
s.	Central				2.50

 ΔS matrix of four regions

~C/I Results of collocating satellites serving

East, West and South Central regions

REGION EAS WES SCR	SATELLITE -105.00 -105.00 -100.00	(LON.)	FREQUENCY (MHz) 4000.00 4000.00 4000.00	
TEST REGION	: EAS	SATELLITE	: -105.00	
TEST LON. -74.Ø2 -74.Ø2 -74.Ø2	POINT LAT. 4Ø.72 4Ø.72 4Ø.72	INT. SAT WES SCR TOTAL	. C/I (dB) 44.30 34.35 33.93	MARGIN (dB)
-71.Ø7	42.35	WES	42.57	8.86
-71.Ø7	42.35	SCR	34.43	
-71.Ø7	42.35	TOTAL	33.86	
-77.Ø2	38.9Ø	WES	44.29	7.21
-77.Ø2	38.9Ø	SCR	32.49	
-77.Ø2	38.9Ø	TOTAL	32.21	
-75.12	39.95	WES	44.54	8.54
-75.12	39.95	SCR	33.9Ø	
-75.12	39.95	TOTAL	33.54	
-78.65	35.78	WES	43.28	3.76
-78.65	35.78	SCR	28.91	
-78.65	35.78	TOTAL	28.76	
TEST REGION	: WES	SATELLITE	: -100.00	
TEST P -118.25 -118.25 -118.25	OINT 34.Ø5 34.Ø5 34.Ø5	INT. SAT EAS SCR TOTAL	. C/I (dB) 44.13 32.33 32.05	MARGIN (dB) 7.ø5
-122.4Ø	37.8Ø	EAS	43.56	8.37
-122.4Ø	37.8Ø	SCR	33.8Ø	
-122.4Ø	37.8Ø	TOTAL	33.37	
-117.95	33.85	EAS	43.97	6.75
-117.95	33.85	SCR	32.Ø2	
-117.95	33.85	TOTAL	31.75	
TEST REGION	: SCR	SATELLITE	: -1 <i>EE</i> . <i>BØ</i>	
-96.80 -96.80 -95.80	32.78 32.78 32.78 32.78	INT. SAT EAS WES TOTAL	. C/1 (dB) 34.30 37.52 32.82	MARGIN (dB) 7.82
-98.52	29.47	EAS	35.71	7.45
-98.52	29.47	WES	35.22	
-98.52	29.47	TOTAL	32.45	
-9£.12	29.97	EAS	28.14	2.85
-9£.12	29.97	WES	39.74	
-9£.12	29.97	TOTAL	27.85	

C/I results of collocating satellites serving

North Central, West and South Central regions

PEGION WES NCR SCR	SATELLIT -100. -100. -100.	E (LON.) ØØ ØØ	FREQUENCY (M 4000.00 4000.00 4000.00	Hz)	
TEST REGION :	: WES	SATELLITE :	-101.05		
TEST_PO1 LON. -118.25 -118.25	LAT. 34.05 34.05	INT. SAT. MCR SCR	C/I (dB) 43.46 32.33	MARGIN	(dB)
-118.25	34.05	TOTAL	32.00	7.ØØ	
-122.4Ø -122.4Ø -122.4Ø	37.8Ø 37.8Ø 37.8Ø	NCR SCR TOTAL	43.47 33.2Ø 33.36	8.36	
-117.95 -117.95 -117.95	33.85 33.85 33.85	NCR SCR TOTAL	43.23 32.02 31.70	6.7Ø	
TEST REGION :	NCR	SATELLITE :	-1ØC.CØ		
TEST PC -87.63 -87.63	DINT 41.28 41.88	INT. SAT. WES SCR	C/I (dB) 42.72 3ø.48	MARGIN	(dB)
-87.63	41.88	TOTAL	30.23	5.23	
-81.68 -81.68 -81.68	41.5Ø 41.5Ø 41.5Ø	WES SCR TOTAL	43.22 31.6Ø 31.5Ø	6.5Ø	
-83.Ø5 -83.Ø5 -83.Ø5	42.33 42.33 42.33	WES SCR TOTAL	43.97 32.84 32.52	7.52	
-84.52 -84.52 -84.52	39.1Ø 29.1Ø 39.1Ø	WES SCR TOTAL	43.73 29.55 29.39	4.39	
TEST REGION :	SCR	SATELLITE :	-106.00		
TEST PC -96.80 -95.80 -95.80	01NT 32.78 32.78	INT. SAT. WES NCR	C/I (dB) 37.Ø2 31.Ø8	MARGIN	(dB)
-96.80	32.78	TUTAL	30.09	5.09	
-95.37 -95.37 -95.37	29.77 29.77 29.77	NCR TOTAL	38.87 34.Ø2 32.79	7.79	
-98.52 -90.52 -90.52	29.47 29.47 29.47	WES NCR TOTAL	35.22 34.37 31.77	6.77	
-90.12 -90.12 -90.12	29.97 29.97 29.97	WES NCR TOTAL	39.74 29.5Ø 29.11	4.11	

 Δs calculation for East and North Central regions

REGION	SATELLITE	(LON.) FR	EQUENCY (MI	Hz)	
NCR	-7Ø.ØØ		4005.00		
EST	-7Ø.ØØ		4000.00		
TEST REGION	: NCR	SATELLITE :	-70.00		
TEST Lon.	POINT LAT.	INT. SAT.	C/I (dB)	MARGIN (dB)
-87.63	41.88	EST	28.66	3.66	
-83.Ø5	42.33	EST	14.71	-1Ø.29	
-84.52	39.1Ø	EST	17.1Ø	-7.9Ø	
-81.68	4 1.5Ø	EST	8.59	-16.41	
TEST REGION	I : EST	SATELLITE :	-70.00		
TEST	POINT	INT. SAT.	C/I (dB)	MARGIN (dB)
-71.Ø7	42.35	NCR	29.£Ø	4. <i>S</i> Ø	
-75.12	39.95	NCR	22.11	-2.89	
-78.65	35.78	NCR	12.64	-12.36	
-74.Ø2	4Ø.72	NCR	29.5Ø	4. 5Ø	
-74.Ø2	40.72	NCR	29.5Ø	4.50	

WORST MARGIN IS -16.41 dB AT NCR (-81.68, 41.50) REQUIRED SATELLITE SPACING : 1.24 AT -70.00 FOR C/I 25.0 dB

The projected long-distance telephone demand matrix between the major cities in these four areas is given in Table 5.8(a). When traffic demand for a region or between regions is computed below, we shall simply add matrix elements from Table 5.2. For instance, internal demand for the West region would be the demand from L.A. to San Francisco (2)-(4), San Francisco to L.A. (4)-(2), L.A. to Anaheim (2)-(12), Anaheim to L.A. (12)-(2), San Francisco to Anaheim (4)-(12), Anaheim to San Francisco (12)-(4). For demand from the West region to the North Central region, one would add the matrix elements corresponding to transmission from each of (2), (4), (12) to each of (3), (6), (8), (10). To make these numbers more applicable to the satellite planning task, they are converted to a corresponding number of satellite beams in the following way. From Figure 5.2, there are 24 frequency channels in the 6/4 GHz spectral band, and each channel is 36 MHz wide. Assuming that a high quality telephone channel occupies 8 KHz bandwidth, one MHz bandwidth can carry 120 telephone channels, and hence a full spectral band can carry 103,680 telephone channels. The number of satellite beams is therefore obtained from the number of telephone channels by dividing by 103,680. Table 5.8(a) is re-stated as satellite beam requirements in Table 5.8(b).

A complete requirement matrix, R, for the U.S. is shown in beam units in Table 5.9. In this matrix, the inter- and intra-regional communications demand of the four regions that can use the two regional-beam designs are listed individually, the rest of the demand, i.e., 73.15 beams, that must go through the CONUS-beam satellites is listed in one category. Note that the inter-regional demand between

Telephone communications demand between major

cities in four regions

(a) In channel units

	channels	East	N. Central	West	S. Central
	East	558400	514000	400200	198700
N.	Central	514000	240400	253300	124300
	West	400200	253300	124800	97800
s.	Central	198700	124300	97800	31200

(b) In beam units

	beams	East	N. Central	West	S. Central
	East	5.38	4.95	3.85	1.91
N.	Central	4.95	2.31	2.44	1.19
	West	3.85	2.44	1.20	0.94
s.	Central	1.91	1.19	0.94	0.30

Complete	requirement	matrix

	beams	East	N. Central	West	S. Central	CONUS
	East	5.38	*	3.85	1.91	
N.	Central	*	2.31	2.44	1.19	73.15
	West	3.85	2.44	1.20	0.94	
s.	Central	1.91	1.19	0.94	0.30	

East and North Central is included in the CONUS beam category because it can not use any of the two regional-beam designs.

3. Improvement of traffic-supply matrix with service-area specification

A supply matrix is used to express the traffic-supply arrangement; each element in this matrix is the amount of traffic supply from one region to another offered from a scenario, up to the maximum amount of demand from the corresponding regions.

If the communications demand is supported by 25 CONUS-beam satellites, the average percentage of satisfaction, s, is

s = 25/103

= 24.27%

Assuming that each user in the continental U.S. has equal probability of accessing all satellites, then each user will have the same percentage of satisfaction and the corresponding supply matrix in beam numbers is given by

$$S = S \cdot R , \qquad (5.1)$$

which is shown in Table 5.10. This represents the total supply expected from the all-CONUS system. While the origin and destination of traffic by regions East, N. Central, S. Central and West are not particularly meaningful with the all CONUS-beam design, the same partitioning as in Table 5.9 has been retained in Table 5.10; this will prove convenient when this scheme is compared to the multiple-beam designs to be discussed.

Supply matrix without regional-beam

satellites

	beams	East	N. Central	West	s.	Central	CONUS
	East	1.305	*	0.934		0.463	
N.	Central	*	0.560	0.592		0.289	17.753
	West	0.934	0.592	0.291		0.228	
s.	Central	0.463	0.289	0.228		0.073	

When implementing the two regional-beam designs, some of the 25 CONUS beam satellites must be preserved; the criterion here is to have the maximum total increase of traffic supply and no loss for any individual. The projected total demand is 103 beams. The requirement matrix that can use the two regional-beam designs, which is simply the regionally served part of Table 5.9, is shown in Table 5.11; the regional sub-total requirement is found to be 29.85 beams. Suppose there are m CONUS satellites being replaced by the regional-beam designs. If the taffic which can be carried only by the CONUS beams does not suffer any loss after implementing the regional-beam designs, the number m must satisfy the requirement

 $(25-m)/(103-29.85) \ge (25/103).$

The maximum value of m, denoted by M, is 7. Replacing M consecutive CONUS satellites with regional-beam satellites will lead to the maximum total increase of traffic supply. For a general case, the value of M is calculated from

 $M = IFIX[n-(n/t) \cdot (t-r)], \qquad (5.2)$

where the symbols are

IFIX : a function whose value is the largest integer equal to or less than the argument,

n : number of satellites in a scenario before implementing regional-beam designs,

t : total communications demand,

r : communications demand that is to be satisfied by the regional-beam designs.

Tal	b1	е	5	•	1	1
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	beams	East	N. Central	West	S. Central	sub-total
	East	5.38	*	3.85	1.91	11.14
N.	Central	*	2.31	2.44	1.19	5.94
	West	3.85	2.44	1.20	0.94	8.43
s.	Central	1.91	1.19	0.94	0.30	4.34

Requirement matrix of four regions

total 29.85

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Reference to the ΔS matrix in Table 5.4 shows the orbital arc that accommodates seven CONUS-beam satellites can support thirteen satellites with 1.25-degree spacing. Of these thirteen satellites, there could be maximally seven beams illuminating the region East since satellites serving the same service area must be separated by no less than 2.5 degrees. Then, because of the ΔS restriction which does not allow collocation of East and North Central beams, there can be at most six beams illuminating North Central. (The reason that East has been allotted more beams than North Central is that it has more demand.) The maximum numbers of beams for West and South Central are both six. They can not be seven because the beam arrangement should allow inter-regional communications from East or North Central to West and South Central; the choice of seven West beams would result in beam-collocation of the East and West beams and no communications between West and North Central. (If these statements do not seem clear, the reader is encouraged to refer to Figure 5.5, which shows the sequence of the thirteen regional-beam satellites, and to experiment with other arrangements, keeping in mind both restrictions and regional-beam designs discussed in Section V.E.2.) With these beam assignments, the supply of regional beams to these four regions is listed in Table 5.12.

The corresponding percentages of satisfaction for the four regions are listed in Table 5.13; the corresponding supply matrix, obtained by multiplying elements of each row with the respective percentage of satisfaction, is shown in Table 5.14(a). It is assumed that the

Supply of regional beams to four regions

	region	beams
	East	7
N.	Central	6
	West	6
s.	Central	6
	total	25

Percentage of satisfaction of demand by

means of regional beams

region	p. o. s.
East	7/11.14 = 0.6283
N. Central	1
West	6/8.43 = 0.7117
S. Central	1

satellite traffic is likely to be symmetrical, hence this matrix needs to be symmetrized. The adjustment should be dominated by the first row because the demand from/to East is the largest and the rate of successful connection depends therefore most strongly on the availability of the channels to the East. The first step is to symmetrize the first column and row, and the matrix should become as shown in Table 5.14(b). Next, the adjustment should be dominated by the third row because the communications from/to West is the second largest. Note that since the value of its first element has been decreased in step one, the available communications supply to the other three elements will increase. The total demand represented by the last three elements in row three can be seen from Table 5.9 to be 4.58 beam units. The beam supply corresponding to these elements are the six beams allotted to the West region (see Table 5.12) minus the 2.419 beam units assigned to the first element of row three in Table 5.14(b), or 3.581beams. The percentage of satisfaction is therefore 2.419/3.581, or 0.7818, which means the matrix is adjusted as shown in Table 5.14(c). This adjustment procedure continues, but is less complicated for the remaining two rows because the amount of beam supply for North Central and South Central is larger than the demand. The adjustment is completed by satisfying the demand, i.e., inserting the corresponding elements from Table 5.11, and the final result is shown in Table 5.14(d). At this point it should be recalled that the design began by converting seven of 25 satellites to regional-beam use, see discussion above Equation (5.2); thus 18 remain for CONUS coverage. For a clear

Supply matrix adjustment

(a) Step one

I	beams	East I	N. Central	West	S. Central
	East	3.380	*	2.419	1.200
N.	Central	*	2.310	2.440	1.190
	West	2.740	1.736	0.854	0.669
s.	Central	1.910	1.190	0.940	0.300

(b) Step two

	beams	East	N.	Central	We	est	s.	Central
	East	3.380		*	2.4	19		1.200
N.	Central	*						
	West	2.419						

S. Central 1.200

Table 5.14 (Continued)

(c) Step three

	beams	East	N. Central	West	S.	Central
	East	3.380	*	2.419		1.200
N.	Central	*		1.908		
	West	2.419	1.908	0.938		0.735
s.	Central	1.200		0.735		

(d) Final step

	beams	East	N. Central	West	S. Central	sub-total
	East	3.380	*	2.419	1,200	7
N.	Central	*	2.310	1.908	1.190	5.408
	West	2.419	1.908	0.938	0.735	6
s.	Central	1.200	1.190	0.735	0.300	3.425

comparison of how the regional-beam designs increase the communications supply, the supply matrix without these regional-beam designs (as shown in Table 5.10) is re-listed in Table 5.15, and the supply matrix with regional-beam designs is given in Table 5.16. It is obvious that the design has accomplished its objective: increasing the communications supply (i.e., satellite availability) to the four regions while decreasing it for no user.

One possible beam arrangement that could provide the number of beams listed in Table 5.12 is shown in Figure 5.5. One possible communications traffic distribution that could provide the supply matrix as shown in Table 5.14(d) is shown in Figure 5.6, and is derived as follows. First, one should saturate the capacity of the one-beam satellites with intra-regional traffic supply, as in satellites S2, S7, and S_{12} . Then one should try to saturate the capacity of the two-beam satellites with inter-regional traffic supply, as in S₃, S₄, S₅, S₆, S₈, Sg, S_{10} , and S_{11} ; because of the limited supply given in Table 5.14(d), S5, S6, and S8 are not fully used by inter-regional traffic, and the remaining capacity in each is assigned to intra-regional traffic. The traffic of the three-beam satellites are then distributed to fulfill the remaining traffic supply quota in Table 5.14(d). Also note that as shown in Figure 5.6, additional intra-regional beams are available for North Central and South Central. Comparison of the supply matrix in Table 5.16, which is implemented by Figure 5.6, with the requirements in Table 5.9 show that this situation can be viewed as more than 100% satisfaction of the demand for these regions.

	beams	East	N. Central	West	S. Central	CONUS
	East	1.305	*	0.934	0.463	
N.	Central	*	0.560	0.592	0.289	17.753
	West	0.934	0.592	0.291	0.228	
s.	Central	0.463	0.289	0.228	0.073	

Supply matrix without regional beams

Table 5.16

Supply matrix with regional beams

	beams	East	N. Central	West	S. Central	rest
	East	3.380	*	2.419	1.200	
N.	Central	*	2.310	1.908	1.190	18
	West	2.419	1.908	0.938	0.735	
s.	Central	1.200	1.190	0.735	0.300	



Figure 5.5. Possible beam arrangement for four regions.

168
ŝ		2	က	4	Ŋ	0	2	ω	ດ	9	,	12	<u>ម</u>
Serving	ш≥∾	z	шS	z≥	шS	z≩	ш	zυ	ш≥	zυ	ш≥	z	ш≶∾
Traffic	0.735 0.755 0.755	- Z	– ш о	- Z }	<u>о</u> 0.3 0.3 0.3 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5		Ξ	Z 31 2 31 0 31 0 31 0 31	– Ⅲ }	- Z 0	- μ ≥	- Z	0.159 С. 846 С. 846 С. 846 С. 846
Additional available beams	0.265 S				0.5 S	0.092 N		0.5 0.81 0.81					<u>- 0</u>
Notation :	[°z≯]	 - Z		ection ea (s)	of be serve	d d d							·

Figure 5.6. Possible communications distribution for four regions.

4. Discussion of Numerical Example

The above example was formulated by observing the communicationsdemand density on a map and selecting service areas intuitively according to the following criteria: the communications demand within and between the service areas should be high, the service areas should be small, and the distance between these service areas should be large. To some extent these criteria conflict, and a compromise was necessary. Although the service areas were specified intuitively, there should be ways to automate this process. The ultimate criterion for the choice of service area specification is that it should result in the maximum communications supply. Intermediate criteria in terms of the ΔS and demand matrix elements would be useful if they can be developed.

It was fortunate that the required spacing between the East and North Central satellites turned out slightly less than half the value for CONUS-beam satellites; this made the satellite "conversion" from CONUS to regional-beam particularly simple and straightforward. For other choices of service areas, the Δ S matrix will be different, so will the beam arrangement and the resulting communications supply. Still the principle is the same: smaller Δ S values means more satellites. It is hoped that this example will provide insight for generating more general and automated procedures.

The concept of replacing administration-coverage satellites with regional-beam ones may have great practical merit. At present, satellite planning work may take place many years before the actual satellite implantation. It is very difficult to make a plan that can

cope with the technologies available twenty years later; therefore, a good plan should be flexible so that the administrations will not be tied to old technologies. For example, if CONUS-beam designs are used in the U.S. planning process with the option of "converting" some to multiple-beam designs later, higher information capacity can be obtained within the framework of an existing scenario, i.e., without changes in the remaining satellites. Therefore, from the viewpoint of flexibility, the multiple-beam replacement option should be attractive as a component of the U.S. planning.

F. DISCUSSION AND CONCLUSION

It was suggested that service areas of the FSS system should be specified according to the communications traffic-demand density in conjunction with the Δ S concept, because this could enable the system planner to specify more satellites and provide more communications supply. When applying this concept to specify satellites for an administration which has heavy traffic between several small and separated regions, it was shown that a mixture of administration coverage and intra-administration regional coverage can increase the communications capacity compared with only administration coverage. A numerical example was used to illustrate the design procedure for replacing several of a series of uniformly spaced administrationcoverage satellites with regional-beam ones. It was shown that a substantial communications capacity increase could be obtained for many users without decreasing the capacity for any user. The procedure was

intuitive in part, and it is recommended that techniques for formalizing and automating it be investigated.

The regional service-area concept in this chapter is closely related to the ΔS concept in Chapter IV. In Chapter IV, the specification of service areas is given and fixed and the focus of the study is allocating satellite locations in the orbit. The focus in Chapter V is the specification of service areas. It is found that consideration of ΔS and traffic demand leads to useful techniques for this specification.

An important advantage in specifying smaller (i.e., regional as opposed to administration-coverage) service areas in the case of geographically large administrations is the reduction of interference to other communications systems. A smaller service area means a smaller beam, and hence a faster drop of the field strength away from the service area. Thus, the use of regional service areas can give better interference protection to other service areas, not only within but also outside the same administration.

In this chapter, the inter-satellite service (ISS) was not considered. The adoption of the ISS might affect this study significantly.

CHAPTER VI

CONCLUSION

The purpose of this study has been to explore orbit and frequency assignment methods with which the spectrum/orbit resources can be efficiently utilized for satellite communications.

In Chapter III, the mathematical nature of the orbital/frequency assignment problem is investigated by analyzing an objective function used by the extended-gradient and cyclic-coordinate search techniques. It is shown that the permutation of the orbital/frequency assignments is an important part of the problem. This indicates that a necessary condition for a technique to be able to find the globally optimal scenario is that it should to be able to deal with both the continuous aspects of satisfying the signal quality requirement and with the permutation problem. It is also shown that, at least when the frequency variables are fixed, for a given orbital permutation this objective function is likely to have only one local minimum. This suggests that a sufficient condition to obtain the globally optimal solution by a extended gradient search method is that it should terminate as the ordinary gradient search procedure with the optimal permutation in orbital and frequency assignments.

In Chapter IV, a technique for obtaining the optimal orbital assignments is presented. The idea is to convert the signal quality requirement to minimum satellite spacing requirements and use them as constraints on the relative satellite locations. With a set of these

constraints, the assignment problem can be formulated as a mixed integer program (integer programming is often used to solve a permutation problem) and solved by the branch-and-bound method. The globally optimal solution is guaranteed; however, the required computational time may be prohibitively long when the problem size (number of satellites to be assigned) is large. To overcome this difficulty, the same problem is formulated as a linear program and solved by a version of the simplex method with restricted basis entry; only a locally optimal solution is guaranteed, but the method is more practical in terms of computational effort. The solutions of both programs are guaranteed to have satisfactory single-entry C/I_e (carrier-to-effective interference ratio) results.

In Chapter V, a basis of specifying service areas for the FSS system is proposed. It is suggested that while some satellites should cover large territories, some satellites should cover smaller regions where the communications demands are high. Smaller and separated service areas require smaller necessary satellite spacings, thus more satellites can be allocated in the orbit and higher communications supply can be obtained. The method involves simultaneous consideration of a requirement matrix and the Δ S matrix for the proposed regions. A numerical example, in which projected voice telephone demand is used for the requirement matrix, demonstrates the validity of this approach.

APPENDIX A

STREAMLINED SOUP CODE

C*** > C T C*****	>> MAIN PROGRA	M << SOUP PROGRAM ************************************	
C I	MPLICIT INTEGE	R*4(I-N), REAL*8(A-H, O-Z)	
c c	HARACTER*6 NAM	ESA	
	COMMON / CONSTS/	E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP, PFD, ALOGE, ALN10, COIMIN, COISING	
ີ່ເ	COMMON / PARAMS/	NUMSAR, NAMESA(10,2), NTPSA(10), CPH IO(10)	
C C	COMMON /VECTOR/	DSLON(10),RSLON(10),XO(10),YO(10), ROAIKJ, XOAC(10),YOAC(10),ZOAC(10),ROAC(10)	
c c l	COMMON /VARBLS/	<pre>FREQ(10), IPOLAR(10), GAINR(10), GAINT(10), EIRP(10), IPTNST(10), IPTNER(10)</pre>	
	COMMON /MINELL/	BCLAT(10),BCLON(10),DBCLAT(10),DBCLON(10), REFLAT(10),REFLON(10),AXR(10), ORIENT(10),AXMAJ(10)	
	COMMON /TPOINT/	RELON(10,20), RELAT(10,20), DELON(10,20), DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)	
c c	COMMON /ANGLES/	YPH IT, YPH IR, PH ITK, YPH IO	
	COMMON /REAL/	PIKJ, PKKJ, FW FQM, FW DRCK, YFW DRC, YFW DRX, XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ	
C C*****	***********	***************************************	
с о)PEN (UNIT=20,F))PEN (UNIT=6,FII	LLE='INPUTO.DAT',TYPE='OLD') LE='NASAP.DAT',TYPE='NEW')	
	CALL ICONST CALL INPUTO		
Č A	ASSUME POWER DENSITIES AT ALL BEAM AIM POINTS ARE CONSTANT		
2 C	O 2 K = 1,NUMS CALL GAINER(I EIRP(K) = PFI CONTINUE	SAR K) D+10.*DLOG10(4.*PI*ROAC(K)*ROAC(K))-ERDB	
ç c	CALL ZFUNCT		
C S E	STOP IND		
c s	SUBROUTINE ZFUNG	CT	
C*** > C*** > C	> THIS ROUTING > STEP IN THE	E IS THE OVERALL CONTROL ROUTINE AT EACH << LINE SEARCH PROCEDURE <<	
C****** C	************	***************************************	
I	MPLICIT INTEGE	R*4(I-N),REAL*8(A-H,O-Z)	

```
С
      CHARACTER*6 NAMESA
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
      COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPHI0(10)
С
      COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10),
                       ROAIKJ,
     1
                       XOAC(10), YOAC(10), ZOAC(10), ROAC(10).
     2
C
      COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
     1
                       EIRP(10), IPTNST(10), IPTNER(10)
С
      COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
                       REFLAT(10), REFLON(10), AXR(10),
     1
                       ORIENT(10), AXMAJ(10)
     1
C
      COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),
     1
                       DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)
С
      COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
С
                       PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
      COMMON / REAL/
                       XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
     1
С
C**
                                         *******************************
С
C***
          INITIALIZE PARAMETER
      >>
С
      DO 10 I=1,NUMSAR
      CALL REFCAL(I)
      CONTINUE
  10
С
      >> OUTER SUMMATION (OVER K) FOR ALL SERVICE AREAS <<
C***
С
      DO 1000 K = 1, NUMSAR
          JNTP = NTPSA(K)
          WRITE(6,705) NAMESA(K,1), DSLON(K)
С
C***
      >> MIDDLE SUMMATION (OVER J) FOR ALL TEST POINTS IN AREA K <<
C
          DO 900 J = 1, JNTP
            CALL KPHI (K, J)
            CALL XPHIO (K, K, J)
            CALL KPWDRC (K, J)
            CALL XPWFQ (FREQ(K), FREQ(K))
            CALL XPOWER (K, K, J)
C***
     >>
            CALCULATE INTERFERENCE POWER
            SUMP=0.
            DO 500 I = 1,NUMSAR
                IF (I.EQ.K) GO TO 500
                CALL ZPHI (I,K,J)
                CALL XPHIO (I,K,J)
                IF (IPOLAR(I).EQ. IPOLAR(K)) THEN
                   CALL ZPWDRC (I,K,J)
                   ELSE
```

```
CALL ZPWDRX (I,K,J)
               END IF
               CALL XPWFQ (FREQ(K), FREQ(I))
               CALL XPOWER (I, K, J)
               COI = PKKJ-PIKJ
               DMGN = COI - COISING
С
         WRITE (6,706) DELON (K, J), DELAT (K, J), NAMESA (I, 1), PIKJ, COI, DMGN
С
             IF (PIKJ .LT. -700.) PIKJ = -700.
С
                     TEN1 = 10. ** (PIKJ/10.)
                     SUMP = SUMP + TEN1
 500
             CONTINUE
С
         IF(NUMSAR.NE.2) THEN
         SUMPDB = 10.*DLOG10(SUMP)
         COIT = PKKJ-SUMPDB
         TDMGN = COIT-COIMIN
         WRITE (6,708) DELON (K, J), DELAT (K, J), SUMPDB, COIT, TDMGN
         END IF
С
 900
         CONTINUE
 1000 CONTINUE
С
 705 FORMAT(//,12X,'TEST COUNTRY :',A6,5X,'SATELLITE :',F8.2,//,15X,
1'TEST POINT',10X,'INT. SAT.',2X,'INT. FWR',3X,'C/I (dB)',
     25X, 'MARGIN')
 706 FORMAT (15X, F7.2, 2X, F7.2, 5X, A6, 4X, F8.2, 4X, F6.2, 6X, F6.2)
     FORMAT (13X, 2(2X, F7.2), 6X, 'TOTAL', 4X, F8.2, 4X, F6.2, 6X, F6.2,/)
 708
      RETURN
      END
С
      SUBROUTINE ICONST
С
C***
      >> THIS ROUTINE INPUTS CONSTANTS THAT ARE USED IN THE PROGRAM <<
С
    C**
С
      IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
      COMMON /CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
                      PFD, ALOGE, ALN10, COIMIN, COISING
     1
С
          C*
С
      E = 2.7182818285
      PI = 3.1415926536
      RADIAN = PI / 180.0
      DEGREE = 180.0 / PI
      GCR = 6.6134
      ER = 6.371E+06
      ALOGE = 0.4342944819
      ALN10 = 2.3025850930
      ERDB = -20.0 * DLOG10(ER)
      PFD = -90.
      EAP = 0.6
С
      RETURN
      END
```

```
С
       SUBROUTINE INPUTO
С
C***
       >>
           THIS ROUTINE INPUTS
                                                                     <<
C***
       >>
                           SERVICE AREA DATA
                                                                     <<
                        -
C***
       >>
                           INITIAL SATELLITE LOCATIONS
                        _
                                                                     <<
C***
       >>
                           INITIAL FREQUENCY ASSIGNMENTS
                        -
                                                                     <<
C***
       >>
                        -
                           INITIAL POLARISATIONS
                                                                     <<
C***
                           ANTENNA PATTERN TYPE
       >>
С
C*
                     -----
                                                             **********
Ç
       IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
       CHARACTER*6 NAMESA
С
       COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
       COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPH IO(10)
С
       COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10),
     1
                       ROAIKJ,
                       XOAC(10), YOAC(10), ZOAC(10), ROAC(10)
     2
С
      COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
     1
                       EIRP(10), IPTNST(10), IPTNER(10)
С
      COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
     1
                       REFLAT(10), REFLON(10), AXR(10),
     1
                       ORIENT(10), AXMAJ(10)
С
      COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),
     1
                       DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)
С
C*
С
C***
         INPUT DATA FOR SATELLITE, BEAM, EARTH STATION CHARACTERISTICS
      >>
С
      READ(20,*) COISING
        COIMIN = COISING - 5.
      READ(20,*) NUMSAR
      DO 10 N = 1, NUMSAR
           READ(20,801) (NAMESA(N,I),I=1,2)
           READ(20,*)DSLON(N), FREQ(N), IPOLAR(N), IPTNST(N), IPTNER(N)
           READ(20,*) DBCLON(N), DBCLAT(N), ORIENT(N), AXMAJ(N), AXMIN
           READ(20,*) NTP
        DO 12 N1=1,NTP
           READ(20,*)DELON(N,N1),DELAT(N,N1)
С
           RELON(N, N1) = DELON(N, N1) * RADIAN
           RELAT(N, N1) = DELAT(N, N1) * RADIAN
        CONTINUE
  12
С
           NTPSA(N) = NTP
           FREQ(N) = FREQ(N) * 1000.
           RSLON(N) = DSLON(N) * RADIAN
           AXR(N) = AXMAJ(N) / AXMIN
           ORIENT(N) = ORIENT(N) *RADIAN
           AXMAJ(N) = AXMAJ(N)*RADIAN
```

BCLON(N) = DBCLON(N) * RADIANBCLAT(N) = DBCLAT(N) * RADIANС 10 CONTINUE C C*** >> REFLECT INPUT DATA << С WRITE(6,901) DO 20 N = 1, NUMSAR WRITE(6,902) NAMESA(N,1), DSLON(N), \$ FREQ(N), IPOLAR(N), IPTNST(N), IPTNER(N) CONTINUE 20 С 801 FORMAT (2A6) FORMAT (//12X, 'COUNTRY', 5X, 'SATELLITE', 5X, 'FREQUENCY', 3X, 901 'POLAR.', 3X, 'PTN(ST)', 3X, 'PTN(ER)',/) S 902 FORMAT (13X, A6, 5X, F9.2, 5X, F9.2, 5X, 12, 7X, 12, 8X, 12) С C*** >> SET UP THE VECTORS FOR THE TEST POINTS << С DO 30 K = 1, NUMSAR С XOI = DCOS(RSLON(K))YOI = DSIN(RSLON(K)) XO(K) = XOIYO(K) = YOIС BCLT = BCLAT(K)BCLN = BCLON(K)COSBLT = DCOS(BCLT)CXE = COSBLT*DCOS(BCLN) CYE = COSBLT*DSIN(BCLN) CZE = DSIN(BCLT)С XOACI = CXE-GCR*XOI YOACI = CYE-GCR*YOI ZOAC(K) = CZEROACI = DSQRT(XOACI * XOACI + YOACI * YOACI + CZE*CZE)С XOAC(K) = XOACIYOAC(K) = YOACIROAC(K) = ROACIС DO 30 J = 1, NTPSA(K) COSLAT = DCOS(RELAT(K, J)) ZE(K, J) = DSIN(RELAT(K, J))30 CONTINUE С RETURN END С SUBROUTINE GAINER(K) С С THIS IS TO CALCULATE EARTH RECEIVER GAIN FROM ANTENNA С DIAMETER, AND TRANSMITTER GAIN FROM HPBW. С IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z) С

```
CHARACTER*6 NAMESA
С
       COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
      COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
                       EIRP(10), IPTNST(10), IPTNER(10)
     1
С
      COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPH IO(10)
С
      COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
                       REFLAT(10), REFLON(10), AXR(10),
     1
     ī
                        ORIENT(10), AXMAJ(10)
С
        X0 = 223./180.
         GO TO (10,20,30,40,50), IPTNER(K)
C
C
         FSS, DIAMETER 3 METERS
С
 10
        D = 3.
        WAVEL = 300. / FREQ(K)
        X1 = D/WAVEL
        GAINR(K) = 10.*DLOG10(PI*PI*X1*X1*EAP)
        CPHIO(K) = XO/X1
         GO TO 60
C
C
        FSS, DIAMETER 3 METERS
С
        D = 3.
 20
        WAVEL = 300. / FREQ(K)
        X1 = D/WAVEL
        GAINR(K) = 10.*DLOG10(PI*PI*X1*X1*EAP)
        CPHiu(K) = X0/X1
         GO TO 60
C
C
C
        FSS, DIAMETER 4.5 METERS
        D = 4.5
 30
        WAVEL = 300. / FREQ(K)
        X1 = D/WAVEL
        GAINR(K) = 10.*DLOG10(PI*PI*X1*X1*EAP)
        CPHIO(K) = XO/X1
        GO TO 60
C
C
C
        FSS, DIAMETER 4.5 METERS
 40
        D = 4.5
        WAVEL = 300. / FREQ(K)
        X1 = D/WAVEL
        GAINR(K) = 10.*DLOG10(PI*PI*X1*X1*EAP)
        CPHIO(K) = XO/X1
        GO TO 60
C
C
        BSS, DIAMETER 1 METER
С
        D = 1.
 50
        WAVEL = 300. / FREQ(K)
        X1 = D/WAVEL
        GAINR(K) = 10.*DLOG10(PI*PI*X1*X1*EAP)
        CPHIO(K) = XO/X1
```

```
с
с
        CALCULATE TRANSMIT GAIN FROM HPBW
С
 60
        GAINT(K) = 10.*DLOG10(EAP*AXR(K)*(PI*X0/AXMAJ(K))**2)
С
        RETURN
        END
С
      SUBROUTINE KPHI (K, J)
С
C***
          THIS ROUTINE COMPUTES THE VECTOR COMPONENTS OF THE LINK <<
      >>
C***
            K-K-J, AND THE CORRESPONDING TRANSMITTING PHI ANGLE <<
      >>
С
          C**
С
      IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
      CHARACTER*6 NAMESA
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                      PFD, ALOGE, ALN10, COIMIN, COISING
С
      COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPH IO(10)
С
      COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10),
     1
                      ROAIKJ,
     2
                      XOAC(10), YOAC(10), ZOAC(10), ROAC(10)
С
      COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
                      EIRP(10), IPTNST(10), IPTNER(10)
     1
С
      COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
                      REFLAT(10), REFLON(10), AXR(10),
     1
     1
                      ORIENT(10), AXMAJ(10)
С
      COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),
     1
                      DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)
С
      COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
С
                      PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
      COMMON / REAL/
     1
                      XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
С
          *************************************
C
С
      XOAKKJ = XE(K, J) - GCR * XO(K)
      YOAKKJ = YE(K, J) - GCR * YO(K)
      ZOAKKJ = ZE(K, J)
      ROAKKJ = DSQRT (XOAKKJ *XOAKKJ + YOAKKJ *YOAKKJ + ZOAKKJ *ZOAKKJ)
С
      COSPHI = (XOAC(K) * XOAKKJ + YOAC(K) * YOAKKJ + ZOAC(K) * ZOAKKJ)
               / (ROAC(K) * ROAKKJ)
     $
      PHITK = DARCOS(COSPHI)
С
      RETURN
      END
С
      SUBROUTINE ZPHI (I, K, J)
С
C***
      >> THIS ROUTINE COMPUTES THE PHI ANGLES <<
```

```
...
```

```
C***
       >> (FOR I INTERFERING WITH K TEST POINT J) <<
C
C۱
С
       IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
       CHARACTER*6 NAMESA
С
       COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
       COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPHI0(10)
С
       COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10),
                        ROAIKJ,
     2
                       XOAC(10), YOAC(10), ZOAC(10), ROAC(10)
С
      COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
     1
                        EIRP(10), IPTNST(10), IPTNER(10)
С
      COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
                       REFLAT(10), REFLON(10), AXR(10),
     1
     1
                       ORIENT(10), AXMAJ(10)
C
      COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),
     1
                       DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)
С
      COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
С
      COMMON / REAL/
                       PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
     1
                       XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
С
C*
                            ********
С
C***
      >> CALCULATE OFF AXIS VECTOR COMPONENTS (____IKJ) <<
С
      XOAIKJ = XE(K, J) - GCR * XO(I)
      YOAIKJ = YE(K, J) - GCR * YO(I)
      ZOAIKJ = ZE(K, J)
      ROAIKJ = DSQRT (XOAIKJ *XOAIKJ + YOAIKJ *YOAIKJ + ZOAIKJ *ZOAIKJ)
С
C***
          COMPUTE DISCRIMINATION ANGLES
      >>
                                           <<
C***
      >> FOR THE TRANSMITTING ANTENNA
                                           <<
С
      TNUMER = XOAC(I) * XOAIKJ + YOAC(I) * YOAIKJ + ZOAC(I) * ZOAIKJ
      TDENOM = ROAC(I) * ROAIKJ
      TEMPU = TNUMER / TDENOM
С
      YPHIT = 0.0
      IF (DABS(TEMPU) .LT. 1.0) YPHIT = DARCOS(TEMPU)
С
C***
      >>
          COMPUTE DISCRIMINATION ANGLES
                                           <<
C***
      >>
            FOR THE RECEIVING ANTENNA
                                           <<
С
      TNUMER = XOAKKJ * XOAIKJ + YOAKKJ * YOAIKJ + ZOAKKJ * ZOAIKJ
      TDENOM = ROAKKJ * ROAIKJ
      TEMPU = TNUMER / TDENOM
С
      YPHIR = 0.0
      IF (DABS(TEMPU) .LT. 1.0) YPHIR = DARCOS(TEMPU)
```

```
С
      RETURN
       END
С
       SUBROUTINE XPHIO (I,K,J)
С
C***
      >> THIS ROUTINE COMPUTES THE ELLIPTICAL BEAM HALF POWER
      >> BEAM WIDTH USING THE METHOD GIVEN IN THE SOUP-3 MANUAL
C***
Ĉ
               C*
С
      IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
      CHARACTER*6 NAMESA
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
      COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPH I0(10)
С
      COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10),
     1
                       ROAIKJ,
     2
                       XOAC(10), YOAC(10), ZOAC(10), ROAC(10)
С
      COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
     1
                       EIRP(10), IPTNST(10), IPTNER(10)
С
      COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
     1
                       REFLAT(10), REFLON(10), AXR(10),
     1
                       ORIENT(10), AXMAJ(10)
С
      COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),
     1
                      DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)
С
      COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
С
                      PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
      COMMON / REAL/
     1
                      XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
С
       C*
С
      PHIS = RSLON(I)
      PHIC = BCLON(I)
      THETAC = BCLAT(I)
С
      SINPHS = DSIN(PHIS)
      COSPHS = DCOS(PHIS)
      COSTC = DCOS(THETAC)
С
      COSW = COSTC * DCOS(PHIS-PHIC)
      SINW = DSIN(DARCOS(COSW))
С
      RSLAT = 0.
      IF ( BCLON(I).EQ.RSLON(I) ) GO TO 1
      IF ( BCLAT(I).EQ.RSLAT ) GO TO 2
      ARG = COSTC * DSIN(DABS(BCLON(I)-RSLON(I))) / SINW
      A = DASIN(ARG)
      IF (BCLON(I).GT.RSLON(I) .AND. BCLAT(I).GT.RSLAT) A=2.*PI-A
      IF (BCLON(I).LT.RSLON(I) .AND. BCLAT(I).LT.RSLAT) A=PI-A
IF (BCLON(I).GT.RSLON(I) .AND. BCLAT(I).LT.RSLAT) A=PI+A
```

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COSA = DCOS(A)SINA = DSIN(A) GO TO 3 1 CONTINUE $\cos A = -1$. SINA = 0. A = PIIF (BCLAT(I).LT.RSLAT) GO TO 3 COSA = 1.A = 0.GO TO 3 2 CONTINUE $\cos A = 0$. SINA = 1. A = PI/2.IF (BCLON(I).LT.RSLON(I)) GO TO 3 SINA = -1.A = 1.5*PICONTINUE 3 С TANT = SINW / (GCR - COSW) TRAD = DATAN (TANT) SINT = DSIN(TRAD) COST = DCOS(TRAD) С $A21 = - \cos A + \sin PHS$ A22 = COSA * COSPHS SINA A23 = С A31 = SINT * COSPHS + COST * SINA * SINPHS A32 = SINT * SINPHS - COST * SINA * COSPHS A33 = COST * COSAС FLAT = REFLAT(I)FLON = REFLON(I)CSFLAT = DCOS(FLAT)VR1 = CSFLAT * DCOS(FLON) VR2 = CSFLAT * DSIN(FLON) VR3 = DSIN(FLAT) С BLAT = BCLAT(I) BLON = BCLON(I)CSBLAT = DCOS(BLAT) VC1 = CSBLAT * DCOS(BLON) VC2 = CSBLAT * DSIN(BLON) VC3 = DSIN(BLAT)С PHIE = RELON(K, J)THETAE = RELAT(K, J)COSTE = DCOS(THETAE) VE1 = COSTE * DCOS(PHIE) VE2 = COSTE * DSIN(PHIE) VE3 = DSIN(THETAE) С VS1 = GCR * COSPHS VS2 = GCR * SINPHS VS3 = 0.0С VRMVCl = VRl - VCl VRMVC2 = VR2 - VC2

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 C^{-3}

VRMVC3 = VR3 - VC3С VEMVS1 = VE1 - VS1 VEMVS2 = VE2 - VS2VEMVS3 = VE3С SINUMR = A31*VRMVC1 + A32*VRMVC2 + A33*VRMVC3 SIDENR = A21*VRMVC1 + A22*VRMVC2 + A23*VRMVC3 С S2NUMR = A31*VEMVS1 + A32*VEMVS2 + A33*VEMVS3 S2DENR = A21*VEMVS1 + A22*VEMVS2 + A23*VEMVS3 С IF (SIDENR. NE .0.0) GO TO 10 S1 = PI / 2.0GO TO 15 10 S1 = DATAN(S1NUMR/S1DENR)С IF (S2DENR. NE .0.0) GO TO 20 15 S2 = PI / 2.0GO TO 25 20 S2 = DATAN (S2 NUMR / S2 DEN R)С 25 SIGMA = S2 - S1CS = DCOS(SIGMA)SS = DSIN(SIGMA) AR = AXR(I)P0 = AXMAJ(I) / DSQRT(CS*CS + AR*AR * SS*SS) С YPHIO = PORETURN END С SUBROUTINE REFCAL(N) С C*** >> THIS ROUTINE CALCULATES THE REFERENCE POINT LAT. & LON. << C*** >> BASED ON THE ALGORITHM IN SOUP MANUAL 3.4, MAY 1983 << С C**** С IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z) С CHARACTER*6 NAMESA С COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP, 1 PFD, ALOGE, ALN10, COIMIN, COISING С COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPH I0(10) С COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10), 1 ROAIKJ, 2 XOAC(10), YOAC(10), ZOAC(10), ROAC(10) С COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10), 1 EIRP(10), IPTNST(10), IPTNER(10) С COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10), 1 REFLAT(10), REFLON(10), AXR(10), 1 ORIENT(10), AXMAJ(10) С COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),

```
1
                      DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)
С
      COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
С
                      PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
      COMMON / REAL/
     1
                      XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
С
C*
                   C
      PGMPS = BCLON(N) - RSLON(N)
      COSTG = DCOS(BCLAT(N))
      COSPP = DCOS (PGMPS)
      Q1 = COSTG * DSIN(PGMPS)
      Q2 = GCR - COSTG * COSPP
      Q3 = DSQRT(Q1**2+Q2**2)
С
      SX = DATAN2(Q1,Q2)
      SY = DATAN2(DSIN(BCLAT(N)), Q3)
С
      AMAJ2 = AXMAJ(N) * 0.5
      SX2 = AMAJ2 * DCOS(ORIENT(N))
      SY2 = AMAJ2 * DSIN(ORIENT(N))
С
      X1 = SX + SX2
      Y1 = SY + SY2
С
      Q4 = DARCOS(DCOS(X1) + DCOS(Y1))
      Q5 = DSIN(Q4)
      T = GCR + Q5
      IF (T.LE. 1.0) GO TO 10
С
      X1 = SX - SX2
      Y1 = SY - SY2
      Q4 = DARCOS(DCOS(X1) * DCOS(Y1))
      Q5 = DSIN(Q4)
      T = GCR + Q5
      IF (T.LE. 1.0 .AND. T.GE. -1.0) GO TO 10
      IF (T.GT. 0.) T = 1.0
      IF (T .LT. 0.) T = -1.0
С
      WRITE(6,901) T
 901 FORMAT (/10X, '****** POSSIBLE ERROR IN ELLIPSE SELECTION ',
     Ś
             F5.1)
С
  10 PX = DARSIN(DSIN(Y1)/Q5)
      IF (X1 .LT. 0.0) PX = PI - PX
      D = DARSIN(T)
      BLAM = D - Q4
REFLAT(N) = DARSIN(DSIN(BLAM) * DSIN(PX))
      AL = DAR COS (DCOS (BLAM) /DCOS (REFLAT (N)))
      IF (DABS(PX) .GT. PI/2.) AL = -AL
      REFLON(N) = RSLON(N) + AL
С
      RETURN
      END
С
С
      FUNCTION DARSIN(X)
С
        IMPLICIT REAL*8(A-H, O-Z)
```

DARSIN = DASIN(X)RETURN END С FUNCTION DARCOS(X) С IMPLICIT REAL*8(A-H, O-Z) DARCOS = DACOS(X)RETURN END С SUBROUTINE KPWDRC (K, J) С C*** >> THIS ROUTINE COMPUTES THE CARRIER SIGNAL DISCRIMINATING << >> FACTOR (DESIRED POWER - CO-POLARISED ONLY - PHIR=0) C*** << С C*** С IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z) С CHARACTER*6 NAMESA С COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP, 1 PFD, ALOGE, ALN10, COIMIN, COISING С COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPH I0(10) С COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10), ROAIKJ, 1 XOAC(10), YOAC(10), ZOAC(10), ROAC(10) 2 С COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10), 1 EIRP(10), IPTNST(10), IPTNER(10) С COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10), 1 REFLAT(10), REFLON(10), AXR(10), 1 ORIENT(10), AXMAJ(10) С COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20), 1 DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20) С COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHI0 С COMMON / REAL/ PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX, 1 XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ С C ************** ******** С PT = PHITKP0 = YPHI0С GO TO(10,20,30,40,50), IPTNST(K) С 10 CALL PTNST1 (PT, PO, GAINT(K), DISC) GOTO 60 С 20 CALL PTNST2 (PT, P0, GAINT(K), DISC) GOTO 60 С 30 CALL PTNST3 (PT, P0, GAINT(K), DISC)

```
GOTO 60
С
  40
      CALL PINST4 (PT, PO, GAINT(K), DISC)
       GOTO 60
С
      CALL PTNST5 (PT, P0, GAINT(K), DISC)
  50
С
      YDSCT = DISC
  60
C
C
       PREVENTING INPERFECT MINIMUM ELLIPSE NOT COVERING ALL POINTS
С
C
        IF (YDSCT.LT.-3.) YDSCT=-3.
С
      >> COMPONENT OF DESIRED POWER DEPENDENT ON ORBIT LOCATION
C*
                                                                       <<
С
      PWDRCK = EIRP(K) + YDSCT + GAINR(K) - 20.0 * DLOG10(ROAKKJ)
      RETURN
С
      END
С
      SUBROUTINE ZPWDRC (I,K,J)
С
C***
           THIS ROUTINE COMPUTES THE INTERFERENCE SIGNAL
      >>
                                                                   <٢
C***
      >>
           TRANSMITTING AND RECEIVING DISCRIMINATIONS FOR
                                                                   <<
C***
                                                                   <<
           THE CO-POLARISED CASE
      >>
С
          *********************
C*
С
      IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
      CHARACTER*6 NAMESA
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
      COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPHI0(10)
С
      COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10),
     1
                        ROAIKJ,
     2
                        XOAC(10), YOAC(10), ZOAC(10), ROAC(10)
С
      COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
     1
                        EIRP(10), IPTNST(10), IPTNER(10)
С
      COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
                        REFLAT(10), REFLON(10), AXR(10),
     1
     1
                        ORIENT(10), AXMAJ(10)
С
      COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),
     1
                       DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)
С
      COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
C
      COMMON / REAL/
                       PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
     1
                       XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
С
C*
0
C***
          TRANSMITTING DISCRIMINATION <<
      >>
```

PT = YPHIT P0 = YPHIOGO TO(10,20,30,40,50), IPTNST(I) С CALL PTNST1(PT, P0, GAINT(I), DISC) 10 GOTO 60 С 20 CALL PTNST2(PT, P0, GAINT(I), DISC) GOTO 60 С CALL PTNST3(PT, P0, GAINT(I), DISC) 30 GO TO 60 С 40 CALL PTNST4(PT, PO, GAINT(I), DISC) GO TO 60 С CALL PTNST5(PT, P0, GAINT(I), DISC) 50 С 60 YDSCT = DISCС C*** >> RECEIVING DISCRIMINATION << С PR = YPHIR PO = CPHIO(K)С GO TO(110,120,130,140,150), IPTNER(K) С 110 CALL PINER1 (PR, PO, FREQ(I), GAINR(K), DISC) GOTO 160 С 120 CALL PTNER2(PR, P0, FREQ(I), GAINR(K), DISC) GOTO 160 С 130 CALL PTNER3(PR, P0, FREQ(I), GAINR(K), DISC) GO TO 160 С 140 CALL PINER4 (PR, P0, FREQ(I), GAINR(K), DISC) GO TO 160 С 150 CALL PINER5 (PR, P0, FREQ(I), GAINR(K), DISC) С 160 YDSCR = DISC С C*** >> COMPONENT OF POWER DEPENDENT ON THE ORBIT LOCATION << C*** >> CO-POLARISED CASE << С YPWDRC = EIRP(I) + YDSCT + YDSCRŚ - 20. * DLOG10(ROAIKJ) С RETURN END С SUBROUTINE ZPWDRX (I,K,J) С C*** >> THIS ROUTINE COMPUTES THE INTERFERENCE POWER << C*** TRANSMITTING AND RECEIVING DISCRIMINATIONS FOR >> << C*** >> THE CROSS-POLARISED CASE << С C** *** С

```
IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
 С
       CHARACTER*6 NAMESA
 С
       COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
      1
                        PFD, ALOGE, ALN10, COIMIN, COISING
 С
       COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPH IO(10)
С
       COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10),
                        ROAIKJ,
      1
      2
                        XOAC(10), YOAC(10), ZOAC(10), ROAC(10)
С
       COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
                        EIRP(10), IPTNST(10), IPTNER(10)
      1
С
       COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
                        REFLAT(10), REFLON(10), AXR(10),
      1
      1
                        ORIENT(10), AXMAJ(10)
С
       COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),
      1
                        DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)
С
       COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
С
       COMMON / REAL/
                        PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
     1
                        XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
С
C*
                             ************************
                                                                   *******
С
C***
           TRANSMITTING DISCRIMINATION <<
       >>
С
       PT = YPHIT
       P0 = YPHIO
С
      GO TO (10,12,14,16,18), IPTNST(I)
С
  10
      CALL PINSTI (PT, PO, GAINT(I), DISC)
      GO TO 20
С
      CALL PINST2(PT, PO, GAINT(I), DISC)
  12
      GO TO 20
С
  14
      CALL PINST3(PT, P0, GAINT(I), DISC)
      GO TO 20
С
  16
      CALL PTNST4(PT, P0, GAINT(I), DISC)
      GO TO 20
С
  18
      CALL PINST5(PT, PO, GAINT(I), DISC)
С
  20
      YDSCT = DISC
С
C***
      >> RECEIVING DIRECTIVITY <<
С
      PR = YPHIR
      PO = CPHIO(K)
С
      CALL XPTNER1 (PR, PO, GAINR(K), DISC)
      YDSXR = DISC
```

```
C
C***
           COMPONENT OF POWER DEPENDENT ON THE ORBIT LOCATION
      >>
                                                                 <<
C***
      >>
                          CROSS-POLARISED CASE
                                                                 <<
С
 100
      YPWDRX = EIRP(I) + YDSCT + YDSXR
                    - 20.0 * DLOG10(ROAIKJ)
      Ś
С
      RETURN
      END
C
      SUBROUTINE XPWFQ (FQD, FQI)
С
C***
          THIS ROUTINE COMPUTES THE FREQUENCY DEPENDENT PORTION
      >>
                                                                   <<
C***
      >> IN THE POWER EQUATION
                                                                   <<
С
C**
          ***********************
                                             *****
С
      IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
      CHARACTER*6 NAMESA
С
      COMMON /CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                      PFD, ALOGE, ALN10, COIMIN, COISING
С
      COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPH I0(10)
С
      COMMON /VECTOR/ DSLON(10),RSLON(10),XO(10),YO(10),
     1
                       ROAIKJ,
     2
                       XOAC(10), YOAC(10), ZOAC(10), ROAC(10)
С
      COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
     1
                      EIRP(10), IPTNST(10), IPTNER(10)
С
      COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
     1
                       REFLAT(10), REFLON(10), AXR(10),
     1
                      ORIENT(10), AXMAJ(10)
С
      COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),
     1
                      DELAT(10,20), XE(10,20), YE(10,20), ZE(10,20)
С
      COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
С
      COMMON / REAL/
                      PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
     1
                      XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
С
C*
                С
Č***
      >>
         POWER BEING CALCULATED IS INTERFERING POWER <<
С
      X = (FQI - FQD)
      ABSX = DABS(X)
      IF (ABSX. LE. 15.) THEN
        FF = 0.
        ELSE
        FF = -(ABSX-15.)*1.6
      END IF
С
      PWFQM = FF - 20.0 * DLOG10(FQI)
С
```

```
RETURN
       END
С
       SUBROUTINE XPOWER (I,K,J)
С
C***
          THIS ROUTINE CALCULATES ALL THE POWERS AFTER THE
                                                                  <<
       >>
C***
           DIRECTIVITY AND FREQUENCY PORTIONS ARE COMPUTED
       >>
                                                                  <<
С
C*
С
       IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
       CHARACTER*6 NAMESA
С
       COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
       COMMON / PARAMS/ NUMSAR, NAMESA(10,2), NTPSA(10), CPHI0(10)
С
      COMMON /VECTOR/ DSLON(10), RSLON(10), XO(10), YO(10),
                       ROAIKJ,
     1
                       XOAC(10), YOAC(10), ZOAC(10), ROAC(10)
     2
С
      COMMON /VARBLS/ FREQ(10), IPOLAR(10), GAINR(10), GAINT(10),
     1
                       EIRP(10), IPTNST(10), IPTNER(10)
С
      COMMON /MINELL/ BCLAT(10), BCLON(10), DBCLAT(10), DBCLON(10),
                       REFLAT(10), REFLON(10), AXR(10),
     1
     1
                       ORIENT(10), AXMAJ(10)
С
      COMMON /TPOINT/ RELON(10,20), RELAT(10,20), DELON(10,20),
                       DELAT (10,20), XE (10,20), YE (10,20), ZE (10,20)
     1
C
      COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
С
      COMMON / REAL/
                       PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
     1
                       XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
С
                            **********************
C1
                  ******
С
                      GO TO 100
      IF (K. EQ . I)
С
C***
         POWER BEING CALCULATED IS AN INTERFERING POWER <<
      >>
С
      IF (IPOLAR(I). EQ . IPOLAR(K)) GO TO 50
С
Č***
      >> CROSS-POLARIZED <<
С
      PIKJ = YPWDRX + PWFQM + ERDB + 27.56
      RETURN
С
      >> CO-POLARIZED <<
C***
С
  50
      PIKJ = YPWDRC + PWFQM + ERDB + 27.56
      RETURN
С
C***
      >> POWER BEING CALCULATED IS A DESIRED POWER <<
С
 100
      PKKJ = PWDRCK + PWFQM + ERDB + 27.56
      RETURN
```

```
С
       END
С
         SUBROUTINE PTNST1 (PT, P0, G, DISC)
С
С
       FSS SATELLITE TX PATTERN FROM CCIR REPORT 558-2
С
       IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                        PFD, ALOGE, ALN10, COIMIN, COISING
С
       X=PT/P0
      IF (X .LE. 1.3) GO TO 10
       IF (X .LE. 3.15) GO TO 20
С
      DISC = -(7.5 + 25.0 * DLOG10(X))
      IF (DISC.LE.(-G-10.)) DISC = -G-10.
      GO TO 40
С
 10
      DISC = -12.0 * X * X
      GO TO 40
С
      DISC = -20.0
  20
С
  40
      RETURN
      END
С
         SUBROUTINE PTNST2 (PT, P0, G, DISC)
С
      FSS SATELLITE TX PATTERN FROM RARC 83 $ 5.1.10.1
С
С
      IMPLICIT INTEGER*4(1-N), REAL*8(A-H, O-Z)
С
      COMMON /CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                        PFD, ALOGE, ALN10, COIMIN, COISING
С
      DP0 = P0*DEGREE
      X1 = PT/P0
      X2 = DP0/0.8
      X3 =.5*(1.-1./X2)
С
      P1 = .4/DP0 + X3
      P2 =1.155/DP0 +X3
      P3 =1.60/DP0+X3
      P4 = 4.0/DP0+X3
      P5 = 6.968/DP0 + X3
      P6 = 10.**((G-11.5)/25.)/X2 + X3
С
      IF (X1 .LE. 0.5)
                         GO TO 10
      IF (X1 .LE. P2)
                         GO TO 12
      IF (X1 .LE. P3)
                         GO TO 14
      IF (X1 .LE. P4)
IF (X1 .LE. P5)
                         GO TO 16
                         GO TO 18
      IF (X1 .LE. P6)
                         GO TO 20
С
      DISC = -G
      GO TO 40
С
 10
      DISC = -12.0 * X1 * X1
```

```
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```

```
GO TO 40
С
 12
      DISC = -18.75*DP0*DP0*(X1-X3)*(X1-X3)
      GO TO 40
С
 14
      DISC = -25
      GO TO 40
С
      DISC = -17.5 - 25.*DLOG10((X1-X3)*X2)
 16
      GO TO 40
С
 18
      DISC = -35.
      GO TO 40
С
 20
      DISC = -11.5 - 25.* DLOG10((X1-X3)*X2)
С
      RETURN
  40
      END
С
        SUBROUTINE PTN ST3 (PT, P0, G, DISC)
С
      FSS SATELLITE TX PATTERN FROM RARC 83 $ 5.1.10.1
С
Ĉ
      WITH MODIFICATION
С
      IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
      DP0 = P0 *DEGREE
      X1 = PT/P0
      X2 = DP0/0.8
      X3 = .5*(1.-1./X2)
С
      IF (X1 .LE. 0.5) GO TO 10
      P2 = 1.265/DP0 + X3
      IF (X1 .LE. P2) GO TO 12
      P3 = 10.**((30.-24.)/30.)
      IF (X1 .LE. P3) GO TO 14
      P4 = 10.**((G-24.)/30.)
      IF (X1 .LE. P4) GO TO 16
С
      DISC = -G
      GO TO 40
С
 10
      DISC = -12.0 * X1 * X1
      GO TO 40
С
 12
      DISC = -18.75*DP0*DP0*(X1-X3)*(X1-X3)
      GO TO 40
С
 14
      DISC = -30.
      GO TO 40
С
 16
      DISC = -24.-30.*DLOG10(X1)
С
  40
      RETURN
      END
С
        SUBROUTINE PTN ST4 (PT, P0, G, DISC)
```

С Ċ FSS SATELLITE TX PATTERN FROM RARC 83 \$5.10.1 С WITH MODIFICATION С IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z) С COMMON /CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP, 1 PFD, ALOGE, ALN10, COIMIN, COISING С DP0 = P0 * DEGREEX1 = PT/P0X2 = DP0/0.8X3 = .5*(1.-1./X2) С IF (X1 .LE. 0.5) GO TO 10 P2 = 1.265/DP0 + X3IF (X1 .LE. P2) GO TO 12 P3 = 10.**((30.-24.)/30.)IF (X1 .LE. P3) GO TO 14 P4 = 10.**((G-24.)/30.)IF (X1 .LE. P4) GO TO 16 С DISC = -GGO TO 40 С 10 DISC = -12.0 * X1 * X1GO TO 40 С 12 DISC = -18.75*DP0*DP0*(X1-X3)*(X1-X3)GO TO 40 С 14 DISC = -30. GO TO 40 С 16 DISC = -24.-30.*DLOG10(X1)С 40 RETURN END С SUBROUTINE PTNST5 (PT, P0, G, DISC) С С SATELLITE TX PATTERN FROM RARC 83 P.111, С **BSS PATTERN** С IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z) С COMMON /CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP, 1 PFD, ALOGE, ALN10, COIMIN, COISING С X1 = PT/P0С IF (X1 .LE. 1.58) GO TO 10 IF (X1 .LE. 3.16) GO TO 12 IF (X1 .LE. 10.) GO TO 14 С DISC = -42.5GO TO 40 С 10 DISC = -12.0 * X1 * X1GO TO 40

```
С
 12
      DISC = -30.
      GO TO 40
С
      DISC = -17.5-25.*DLOG10(X1)
 14
       GO TO 40
С
  40
      RETURN
      END
С
         SUBROUTINE PTNER1 (PR, P0, F, G, DISC)
С
č
      FSS EARTH REVEIVER PATTERN FROM CCIR REPORT 391-4
      ANTENNA DIAMETER 3 METERS, MAIN LOBE NOT GAUSSIAN
с
с
      IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
                        PFD, ALOGE, ALNIO, COIMIN, COISING
     1
С
      DPR = PR*DEGREE
      DP0 = P0 * DEGREE
      D = 3.
      WAVEL = 300./F
      X1 = D/WAVEL
      G1 = 2. + 15.* DLOG10(X1)
      PM = 20./X1* DSQRT(G-G1)
      PS = 15.85 / X1**0.6
С
      IF (DPR .LE. PM) GO TO 50
      IF (DPR .LE. PS) GO TO 60
      IF (DPR .LE. 48.) GO TO 70
С
      DISC = -10.
      GO TO 80
С
      DISC = G- 2.5E-3 * X1*X1*DPR*DPR
  50
      GO TO 80
С
  60 \text{ DISC} = \text{Gl}
      GO TO 80
С
  70 DISC = 32.-25.*DLOG10(DPR)
С
  80
      RETURN
      END
С
         SUBROUTINE PTNER2 (PR, P0, F, G, DISC)
С
      FSS EARTH REVEIVER PATTERN FROM CCIR REPORT 391-4
č
      MAIN LOBE GAUSSIAN, ANTENNA DIAMETER 3 METERS,
MODIFIED FOR NON US COUNTRIES
С
č
С
      IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                        PFD, ALOGE, ALN10, COIMIN, COISING
С
      DPR = PR*DEGREE
      X = PR/PO
```

P2 = 10.**((32.+10.)/25.)С IF (X.LE.0.5) THEN DISC = G - 12.*X*XGO TO 80 ELSE IF (DPR .GE. P2) THEN DISC = -10. GO TO 80 END IF С DISC = G - 12.*X*XD1 = 32. - 25.*DLOG10(DPR)IF (D1 .GE. DISC) DISC = D1 С 80 RETURN END С SUBROUTINE PTNER3 (PR, P0, F, G, DISC) С C C FSS EARTH REVEIVER PATTERN FROM CCIR REPORT 391-4 MAIN LOBE GAUSSIAN, ANTENNA DIAMETER 4.5 METERS, Ĉ MODIFIED FOR US ONLY С IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z) С COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP, 1 PFD, ALOGE, ALN10, COIMIN, COISING С DPR = PR * DEGREEX = PR/P0P2 = 10.**((29.+10.)/25.)С IF (X.LE.1.) THEN DISC = G - 12.*X*XGO TO 80 ELSE IF (DPR .GE. P2) THEN DISC = -10. GO TO 80 END IF С DISC = G - 12.*X*XD1 = 29. - 25.*DLOG10(DPR) IF (D1 .GE. DISC) DISC = D1 С 80 RETURN END С SUBROUTINE PTNER4 (PR, P0, F, G, DISC) С Ċ C FSS EARTH REVEIVER PATTERN FROM CCIR REPORT 391-4 MAIN LOBE GAUSSIAN, ANTENNA DIAMETER 4.5 METERS, С MODIFIED FOR US ONLY Ĉ IMPLICIT INTEGER *4(I-N), REAL *8(A-H, O-Z) С COMMON /CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP, 1 PFD, ALOGE, ALNIO, COIMIN, COISING С DPR = PR*DEGREE X = PR/P0

```
P2 = 10.**((29.+10.)/25.)
С
       IF (X.LE.1.) THEN
       DISC = G - 12.*X*X
       GO TO 80
       ELSE IF (DPR .GE. P2) THEN
DISC = -10.
       GO TO 80
       END IF
С
       DISC = G - 12.*X*X
D1 = 29. - 25.*DLOG10(DPR)
       IF (D1 .GE. DISC) DISC = D1
С
  80
       RETURN
       END
С
       SUBROUTINE PTNER5 (PR, P0, F, G, DISC)
С
       EARTH REVEIVER PATTERN FROM RARC-83 P.115 CURVE B
С
С
       BSS PATTERN
Ĉ
       IMPLICIT INTEGER*4(I-N), REAL*8(A-H, O-Z)
С
       COMMON /CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
                         PFD, ALOGE, ALN10, COIMIN, COISING
      1
С
       X = PR/PO
С
       IF (X .LE. 0.25) GOTO 10
       IF (X .LE. 0.94) GOTO 12
IF (X .LE. 18.88) GOTO 14
С
       DISC = G - 43.2
       RETURN
С
  10 DISC = G
       RETURN
С
  12 DISC = G - 12. * X * X
       RETURN
С
       DISC = G - 11.3 - 25. * DLOG10(X)
  14
       RETURN
С
  .
       END
С
       SUBROUTINE XPTNER1 (PR. PO.G. DISC)
С
С
       CROSS POLARIZATION RECEIVER PATTERN, BSS
С
       IMPLICIT REAL*8(A-H, O-Z)
С
       X = PR/P0
       IF (X.LE.0.25) GO TO 40
       IF (X.LE.0.44) GO TO 50
       IF (X.LE.1.28) GO TO 60
       IF (X.LE.3.22) GO TO 70
       IF (X.LE.5.60) GO TO 80
IF (X.LE.18.88) GO TO 90
```

С	
	DISC = G-43.2
	GO TO 100
С	
40	DISC = G-25.
	GO TO 100
С	
50	DISC = G-(30.+40.*DLOG10(1.0-X))
	GO TO 100
С	
60	DISC = G-20.
	GO TO 100
C	
70	DISC = G - (17.3 + 25.* DLOG10(X))
	GO TO 100
С	
80	DISC = G-30.
	GO TO 100
С	
90	DISC = G-(11.3+25.*DLOG10(X))
С	
100	RETURN
	END

APPENDIX B

CONCAVE, QUASI-CONCAVE AND PSEUDO-CONCAVE FUNCTIONS

The content in this appendix is from the book "Nonlinear Programming" written by Olvi L. Mangasarian [105]. All the page numbers appearing in the content are referred to this book. Here only the concave functions are discussed; the same discussions apply to convex functions with obvious substitution.

Definition of convex set (p. 39)

A set IcR^n is a convex set if, for x,y εI , $a \varepsilon R$, 0 < a < 1, one has (1-a)x+ay εI , (B.1)

here R^{n} is the set of n-dimensional vector space, R is the set of real numbers.

Definition of concave function (p. 56)

A numerical function f defined on a set ICR^n is said to be concave at xel if, for yel, $0 \le 1$, (1-a)x+ayel, one has

(1-a)f(x)+af(y) < f[(1-a)x+ay]; (B.2)

f is said to be concave on I if it is concave at each $x \in I$.

Definition of strictly concave function (p. 57)

A numerical function f defined on a set ICR^n is said to be strictly concave at xeI if, for yeI, x=y, 0<a<1, (1-a)x+ayeI, one has

$$(1-a)f(x)+af(y) < f[(1-a)x+ay]$$
; (B.3)

f is said to be strictly concave on I if it is strictly concave at each $x \in I$.

Definition of quasi-concave function (p. 132)

A numerical function f defined on a set ICR^n is said to be quasi-concave at xeI if, for yeI, f(x) < f(y), $0 \le a \le 1$, $(1-a)x + ay \in I$, one has

f(x) < f[(1-a)x+ay]; (B.4) f is said to be quasi-concave on I if it is quasi-concave at each xeI.

Definition of strictly quasi-concave function (p. 137)

A numerical function f defined on a set ICR^{n} is said to be strictly quasi-concave at xeI if, for yeI, f(x) < f(y), 0 < a < 1, (1-a)x+ayeI, one has

$$f(x) < f[(1-a)x+ay]$$
; (B.5)

f is said to be strictly quasi-concave on I if it is strictly quasi-concave at each $x \in I$.

Theorem 1 (p. 139)

Let f be a numerical function defined on the convex set I in R'', and let xeI be a local maximum. If f is strictly quasi-concave at x, then f(x) is a global maximum of f on I.

Definition of pseudo-concave function (p. 141)

Let f be a numerical function defined on some open set in \mathbb{R}^n containing the set I. f is said to be pseudo-concave at xeI if it is differentiable at x, and for yeI, $\nabla f(x)(y-x) < 0$, one has

 $f(y) < f(x) \qquad ; \qquad (B.6)$

f is said to be pseudo-concave on I if it is pseudo-concave at each $x \in I$.

Theorem 2 (p. 143)

Let I be a convex set in R^n , and let f be a numerical function defined on some open set containing I. If f is pseudo-concave on I, then f is strictly quasi-concave on I and hence also quasi-concave on I. The converse is not true.

Theorem 3 (p. 144)

Let f be a numerical function defined on some open set I in R^n , let $x \in I$, and let f be differentiable at x. If f is concave at x, then f is pseudo-concave at x, but not conversely.

Theorem 4 (p. 145)

Let I be a convex set in R^n , and let f be a numerical function defined on some open set containing I. If f is pseudo-concave on I, then each local maximum of f on I is also a global maximum of f on I.

A final note: a function that is strictly concave is also concave, a function that is concave is also pseudo-concave, a function that is pseudo-concave is also strictly quasi-concave, a function that is strictly quasi-concave is also quasi-concave; the converse is not true.

APPENDIX C



ARG=62. BØL=68.










BØL=62.

PRG=68.







PRG=62.

BØL=68.





PRU=62. ARG=68.



B0L=68.

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APPENDIX D

AS CALCULATION CODE

C*** C C C C C C C	>> MAIN PROGRAM THIS IS TO CALCU FOR TWO SERVICE IN IT IAL SATELLIT SUBROUTINES SAME SERVICE AREA IS	4 << ULATE THE NECESSARY SATELLITE SPACING 2 AREAS. 7E LOCATIONS SHOULD BE THE SAME. 8 AS MINI-SOUP PROGRAM, EXCEPT DIMENSION OF 5 TWO
č	IMPLICIT REAL*8((A-H, O-2)
c	CHARACTER*6 NAME	25A
С	COMMON / CONSTS/	E, PI, RADIAN. DEGREE, GCR, ER, ERDB, EAP, PFD, ALOGE, ALN10, COIMIN, COISING
c	COMMON / PARAMS/	NUMSAR.NAMESA(2.2),NTPSA(2),CPHI0(2)
C	COMMON / VECTOR/	DSLON(2),RSLON(2),XO(2),YO(2), ROAIKJ,
с	2	XOAC(2), YOAC(2), ZOAC(2), ROAC(2)
c	COMMON /VARBLS/	<pre>FREQ(2), IFOLAR(2), GAINR(2), GAINT(2), EIRP(2), IFTNST(2), IFTNER(2)</pre>
	COMMON /MINELL/ 1 1	BCLAT(2),BCLON(2),DBCLAT(2),DBCLON(2), REFLAT(2),REFLON(2),AXR(2), ORIENT(2),AXMAJ(2)
	COMMON /TPOINT/ 1	RELON(2.20), RELAT(2.20), DELON(2.20), DELAT(2.20), XE(2.20), YE(2.20), ZE(2.20)
с с	COMMON /ANGLES/	YPH IT, YPH IR, PH ITK, YPH 10
	COMMON / REAL/	PIKJ, PKKJ, FWFQM, FWDRCK, YPWDRC, YPWDRX, XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
C****	COMMON / SRCH/	DMGN (2 , 20)
с	OPEN (UNIT=20,FI	LE='INPUT0.DAT', TYPE='OLD')
с	OPEN (UNIT=6,FIL	.E='DSOUT.DAT',TYPE='NEW')
с	CALL INPUTO	
•	DO 2 K = 1, NUMS CALL GAINER(K	SAR ()
<mark>2</mark>	CONTINUE	+10. *DLOG10(4. *PI *ROAC(K) *ROAC(K)) - ERDB
c	CALL 2FUNCT CALL SEPAR	
	STOP END	
c	SUBROUTINE ZFUNC	I
č***	>> THIS ROUTINE	IS THE OVERALL CONTROL ROUTINE FOR <<

********** C*1 С IMPLICIT REAL*8(A-H,O-Z) С CHARACTER*6 NAMESA С COMMON / CONSTS/ E, PI, RADIAN. DEGREE, GCR, ER, ERDB, EAP, 1 PFD, ALOGE, ALN10, COIMIN, COISING С COMMON / PARAMS/ NUMSAR, NAMESA(2.2), NTPSA(2), CPH I0(2) С COMMON /VECTOR/ DSLON(2), RSLON(2), XO(2), YO(2), 1 ROAIKJ, 2 XOAC(2), YOAC(2), ZOAC(2), ROAC(2)С COMMON /VARBLS/ FREQ(2), IPOLAR(2), GAINR(2), GAINT(2), 1 EIRP(2), IPTN ST(2), IPTNER(2) С COMMON /MINELL/ BCLAT(2), BCLON(2), DBCLAT(2), DBCLON(2), 1 REFLAT(2), REFLON(2), AXR(2), 1 ORIENT(2), AXMAJ(2) С COMMON /TPOINT/ RELON(2.20), RELAT(2.20), DELON(2.20), 1 DELAT(2,20), XE(2,20), YE(2,20), ZE(2,20) С COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO С COMMON / REAL/ PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX, 1 XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ С COMMON / SRCH/ DMGN(2,20) C**** *************** **************************** С C*** >> INITIALIZE PARAMETER С DO 10 I=1,NUMSAR CALL REFCAL(I) 10 CONTINUE С C*** >> OUTER SUMMATION (OVER K) FOR ALL SERVICE AREAS << С DO 1000 K = 1, NUMSAR JNTP = NTPSA(K)WRITE(6,705) NAMESA(K,1), DSLON(K) C C*** >> MIDDLE SUMMATION (OVER J) FOR ALL TEST POINTS IN AREA K << C DO 900 J = 1.JNTPCALL KPHI (K, J) CALL XPHIO (K,K,J) CALL KPWDRC (K, J) CALL XPWFQ (FREQ(K), FREQ(K)) CALL XPOWER (K, K, J) Č*** >> CALCULATE INTERFERENCE POWER SUMP=0. DO 500 I = 1,NUMSAR IF (I.EQ.K) GO TO 500 CALL ZPHI (I,K,J)

```
CALL XPHIO (I,K,J)
                IF (IPOLAR(I).EQ.IPOLAR(K)) THEN
                   CALL ZFWDRC (I,K,J)
                   ELSE
                   CALL ZPWDRX (I,K,J)
                END IF
                CALL XPWFQ (FREQ(K), FREQ(I))
                CALL XPOWER (I,K,J)
                COI = PKKJ-PIKJ
                DMGN(K,J) = COI - COISING
С
       WRITE(6,706)DELON(K, J), DELAT(K, J), NAMESA(I, 1), PIKJ, COI, DMGN(K, J)
 500
              CONTINUE
С
 900
      CONT INUE
 1000 CONTINUE
С
 705
     FORMAT(//,12X,'TEST COUNTRY :',A6,5X,'SATELLITE :',F8.2,//,15X,
     1'TEST POINT', 10X, 'INT. SAT.', 2X, 'INT. FWR', 3X, 'C/I (dB)',
     25X, 'MARGIN')
 706
      FORMAT(/,15X,F7.2,2X,F7.2,5X,A6,4X,F8.2,4X,F6.2,6X,F6.2)
      RETURN
      END
С
С
        SUBROUTINE SEPAR
С
С
      THIS IS TO FIND THE MINIMAL REQUIRED SATELLITE SPACING FOR TWO
С
       SERVICE AREAS
С
С
       ********************************
С
      IMPLICIT REAL*8(A-H, O-Z)
С
      CHARACTER*6 NAMESA
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN. COISING
С
      COMMON / PARAMS/ NUMSAR, NAMESA(2.2), NTPSA(2), CPH10(2)
С
      COMMON /VECTOR/ DSLON(2), RSLON(2), XO(2), YO(2),
     1
                       ROAIKJ,
     2
                       XOAC(2), YOAC(2), ZOAC(2), ROAC(2)
С
      COMMON /VARBLS/ FREQ(2), IPOLAR(2), GAINR(2), GAINT(2),
     1
                       EIRP(2), IPTNST(2), IPTNER(2)
С
      COMMON /MINELL/ BCLAT(2), BCLON(2), DBCLAT(2), DBCLON(2),
     1
                       REFLAT(2), REFLON(2), AXR(2),
                       ORIENT(2), AXMAJ(2)
     1
С
      COMMON /TPOINT/ RELON(2,20), RELAT(2,20), DELON(2,20),
     1
                       DELAT(2,20), XE(2,20), YE(2,20), ZE(2,20)
С
      COMMON /ANGLES/ YPHIT, YPHIR, PHITK, YPHIO
С
      COMMON / REAL/
                       PIKJ, PKKJ, PWFQM, PWDRCK, YPWDRC, YPWDRX,
     1
                       XOAKKJ, YOAKKJ, ZOAKKJ, ROAKKJ
С
```

```
COMMON / SRCH/
                       DMGN(2,20)
С
      ************
C
C
                        ************
        NTP1 = NTPSA(1)
        NTP2 = NTPSA(2)
С
С
      SELECT WORST MARGIN AMONG ALL C/I VALUES AT ALL TEST POINTS
C
        RMIN1 = DMGN(1,1)
        DO J=2,NTP1
         RMIN1 = DMIN1(RMIN1,DMGN(1,J))
        END DO
        RMIN2 = DMGN(2,1)
        DO J=2,NTP2
         RMIN2 = DMIN1(RMIN2, DMGN(2, J))
        END DO
С
С
       NO SATELLITE SPACING REQQUIRED
С
        IF (RMIN1.GE.0..AND.RMIN2.GE.0.) THEN
          WRITE(6,1)
 1
          FORMAT (//,11X,' **** SATELLITE SEPARATION NOT NEEDED ****')
          RETURN
        END IF
С
С
       CALCULATE TOPOCENTRIC AND GEOCENTRIC ANGLE (SATELLITE SPACING)
С
         FROM WORST TEST POINT
С
       PRECAUSION MADE IF TWO SYSTEMS USE DIFFERENT RECEIVING PATTERNS
С
        IF(IPTNER(1).EQ.IPTNER(2))THEN
          IF (RMIN1.LE.RMIN2) THEN
           CALL MINMGN(1.J1,RMIN1)
           WRITE (6,2) RMIN1, NAMESA(1,2), DELON(1,J1), DELAT(1,J1)
           CALL PTNANG(1, RMIN1, TOPOANG)
           CALL GEOANG(2,1,J1, TOPOANG, DELTAS)
          ELSE
           CALL MINMGN(2, J2, RMIN2)
           WRITE (6,2) RMIN2, NAMESA(2,2), DELON(2,J2), DELAT(2,J2)
           CALL PTNANG(2, RMIN2, TOPOANG)
           CALL GEOANG(1.2, J2, TOPOANG, DELTAS)
          END IF
        ELSE
          CALL MINMGN(1, J1, RMIN1)
          WRITE (6,2) RMIN1, NAMESA(1,2), DELON(1, J1), DELAT(1, J1)
          CALL PTNANG(1, RMIN1, TOPOANG1)
          CALL GEOANG(2,1,J1,TOPOANG1,DELTAS1)
          CALL MINMGN(2, J2, RMIN2)
          WRITE (6,2) RMIN2, NAMESA(2,2), DELON(2, J2), DELAT(2, J2)
          CALL PTNANG(2, RMIN2, TOPOANG2)
          CALL GEOANG(1,2,J2,TOPOANG2,DELTAS2)
          DELTAS = DMAX1(DELTAS1, DELTAS2)
        END IF
С
        WRITE(6,100) DELTAS.DSLON(1), COISING
 2
        FORMAT (//,11X,'WORST MARGIN IS ',F6.2,' AT',A6,'(',
     1 F7.2,',',F7.2,')')
        FORMAT(/,11X,'SATELLITE SEPARATION : ',F5.2,' AT ',
 100
     1 F7.2,' FOR C/I ',F4.1,' dB')
С
```

```
RETURN
         END
С
         SUBROUTINE MINMGN(K1, J1, RMIN)
C
C
         THIS IS TO FIND THE MINIMUM MARGIN AMONG THE TEST POINTS
С
      IMPLICIT REAL*8(A-H, O-Z)
С
      CHARACTER*6 NAMESA
С
      COMMON / CONSTS/ E, PI, RADIAN. DEGREE, GCR, ER, ERDB, EAP,
     1
                        PFD, ALOGE, ALN10, COIMIN, COISING
С
      COMMON / PARAMS/ NUMSAR, NAMESA(2,2), NTPSA(2), CPHI0(2)
С
      COMMON / SRCH/
                        DMGN(2,20)
С
         DO J=1,NTPSA(K1)
          IF(DMGN(K1,J).LE.RMIN) THEN
           JI = J
            RETURN
          END IF
         END DO
        RETURN
         END
С
         SUBROUTINE PTNANG(K1, RMIN. TO POANG)
C
C
         THIS IS TO CALCULATE THE TOPOCENTRIC ANGLE (FROM GROUND
Ċ
          RECEIVING REFERENCE PATTERN) NECESSARY TO PROVIDE
С
          THE DISCRIMINATION
Ċ
      IMPLICIT REAL*8(A-H,O-Z)
С
      CHARACTER*6 NAMESA
С
      COMMON / CONSTS/ E, PI, RADIAN. DEGREE, GCR, ER, ERDB, EAP,
     1
                        PFD, ALOGE, ALN10, COIMIN, COISING
С
      COMMON / PARAMS/ NUMSAR, NAMESA(2,2), NTPSA(2), CPHI0(2)
С
      COMMON /VARBLS/ FREQ(2), IPOLAR(2), GAINR(2), GAINT(2),
     1
                        EIRP(2), IPTNST(2), IPTNER(2)
С
      COMMON / SRCH/
                        DMGN(2,20)
С
         IF (IPOLAR(1).NE.IPOLAR(2)) THEN
         CALL XRPTNER1 (PR, CPH 10 (K1), GAINR(K1), RMIN)
         GO TO 60
         END IF
С
         GO TO (51,53,55,57,59), IPTNER(K1)
С
 51
         CALL RPTNER1 (PR, CPHIO(K1), FREQ(K1), GAINR(K1), RMIN)
         GO TO 60
 53
         CALL RPINER2 (PR. CPHIO(K1), FREQ(K1), GAINR(K1), RMIN)
         GO TO 60
 55
         CALL RPINER3 (PR. CPHIO(K1), FREQ(K1), GAINR(K1), RMIN)
         GO TO 60
```

```
57
        CALL RPINER4 (PR, CPHIO(K1), FREO(K1), GAINR(K1), RMIN)
         GO TO 60
 59
         CALL RPTNER5(PR, CPHI0(K1), FREQ(K1), GAINR(K1), RMIN)
С
 60
        TOPOANG = PR * DEGREE
        RETURN
        END
С
        SUBROUTINE GEOANG(1, K, J, TO POANG, DELTAS)
С
С
        THIS IS TO ITERATE TO CALCULATE THE NECESSARY GEOCENTRIC
С
          ANGLE FOR THE REQUIRED DISCRIMINATION
Ĉ
      IMPLICIT REAL*8(A-H, O-Z)
С
      CHARACTER*6 NAMESA
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                        PFD, ALOGE, ALN10, COIMIN, COISING
С
      COMMON / PARAMS/ NUMSAR, NAMESA(2,2), NTPSA(2), CPHI0(2)
С
      COMMON /VECTOR/ DSLON(2), RSLON(2), XO(2), YO(2),
     1
                        ROAIKJ,
     2
                        XOAC(2), YOAC(2), ZOAC(2), ROAC(2)
С
      COMMON /MINELL/ BCLAT(2), BCLON(2), DBCLAT(2), DBCLON(2),
     1
                        REFLAT(2), REFLON(2), AXR(2),
                        ORIENT(2), AXMAJ(2)
     1
С
      COMMON /TPOINT/ RELON(2,20), RELAT(2,20), DELON(2,20),
     1
                        DELAT(2,20), XE(2,20), YE(2,20), ZE(2,20)
С
      COMMON / SRCH/
                        DMGN(2.20)
С
        DSLONG = DSLON(I)
С
        IF (DB CLON (K).GE. DB CLON (I)) THEN
           DELTA = 0.01
           DSK = DSLONG+TOPOANG/2.
           DSI = DSLONG-TOPOANG/2.
         ELSE
           DELTA = -0.01
          DSK = DSLONG-TOPOANG/2.
           DSI = DSLONG+TOPOANG/2.
        END IF
С
 20
        DSK = DSK-DELTA
DSI = DSI+DELTA
        RSK = DSK*RADIAN
         RSI = DSI*RADIAN
        XOAK = XE(K, J) - GCR * DCOS(RSK)
        YOAK = YE(K, J) - GCR * DSIN(RSK)
         ZOAK = ZE(K, J)
        ROAK = DSQRT (XOAK*XOAK+YOAK*YOAK+ZOAK*ZOAK)
        XOAI = XE(K, J)-GCR*DCOS(RSI)
        YOAI = YE(K, J) -GCR *DSIN(RSI)
         ZOAI = ZE(K, J)
        ROAI = DSQRT(XOAI*XOAI+YOAI*YOAI+ZOAI*ZOAI)
        ARG = (XOAK*XOAI+YOAK*YOAI+ZOAK*2OAI)/(ROAK*ROAI)
```

```
TOPO = DACOS(ARG) * DEGREE
         IF (TOPO. GT. TOPOANG) GOTO 20
        DELTAS = DABS(DSK-DSI)+0.02
         RETURN
         END
С
        SUBROUTINE RPINERI (PR, P0, F, G, DISC)
С
С
      FSS EARTH RECEIVER REFERENCE PATTERN FROM CCIR REPORT 391-4
        ANTENNA DIAMETER 3 METERS, MAIN LOBE NOT GAUSSIAN
С
С
      IMPLICIT REAL*8(A-H,O-Z)
С
      COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                        PFD, ALOGE, ALN10, COIMIN. COISING
С
      D = 3.
      WAVEL = 300./F
      X1 = D/WAVEL
      G1 = 2. + 15.* DLOG10(X1)
С
      IF (DISC.GE. (G1-G)) GO TO 50
      IF (DISC.GE. (-G-10.)) GO TO 60
С
      PR = PI
      GO TO 80
С
  50
      PR = RADIAN * DSQRT(-DISC*400./(X1*X1))
      GO TO 80
С
  60
      PR = RADIAN*10.**(-(DISC+G-32.)/25.)
С
  80
      RETURN
      END
С
         SUBROUTINE RPTNER2 (PR, P0, F, G, DISC)
С
Ĉ
      FSS EARTH RECEIVER PATTERN FROM CCIR REPORT 391-4
        MAIN LOBE GAUSSIAN, ANTENNA DIAMETER 3 METERS,
MODIFIED FOR NON US COUNTRIES
c
c
С
      IMPLICIT REAL*8(A-H,O-Z)
С
      COMMON / CONSTS/ E, PI, RADIAN. DEGREE, GCR, ER, ERDB, EAP,
     1
                        PFD, ALOGE, ALN10, COIMIN, COISING
С
      IF (DISC.GE.-3.) THEN
      PR = P0 * DSQRT(-DISC/12.)
       GO TO 80
      ELSE IF (DISC.LE.-(G+10.)) THEN
      PR = PI
      GO TO 80
      END IF
С
      PR1 = P0 * DSQRT(-DISC/12.)
      PR2 = RADIAN * 10.**(-(G+DISC-32.)/25.)
      PR = DMAX1(PR1, PR2)
С
  80
      RETURN
       END
```

```
С
      SUBROUTINE RPINER3 (PR, P0, F, G, DISC)
С
С
      FSS EARTH RECEIVER PATTERN FROM CCIR REPORT 391-4
        MAIN LOBE GAUSSIAN, ANTENNA DIAMETER 4.5 METERS,
С
С
        MODIFIED FOR US ONLY
С
      IMPLICIT REAL*8(A-H, O-Z)
С
      COMMON / CONSTS/ E, PI, RADIAN. DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
      IF (DISC.GE.-12.) THEN
      PR = PO * DSQRT(-DISC/12.)
      GO TO 80
      ELSE IF (DISC.LE.-(G+10.)) THEN
      PR = PI
      GO TO 80
      END IF
С
      PR1 = P0 * DSQRT(-DISC/12.)
      PR2 = RADIAN * 10.**(-(G+DISC-29.)/25.)
      PR = DMAX1(PR1, PR2)
С
  80
      RETURN
      END
С
      SUBROUTINE RPINER4 (PR, P0, F, G, DISC)
C
C
      FSS EARTH RECEIVER PATTERN FROM CCIR REPORT 391-4
С
        MAIN LOBE GAUSSIAN, ANTENNA DIAMETER 4.5 METERS,
С
        MODIFIED FOR US ONLY
С
      IMPLICIT REAL*8(A-H, O-Z)
С
      COMMON / CONSTS/ E, PI, RADIAN. DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
      IF (DISC.GE.-12.) THEN
      PR = P0 * DSQRT(-DISC/12.)
      GO TO 80
      ELSE IF (DISC.LE.-(G+10.)) THEN
      PR = PI
      GO TO 80
      END IF
С
      PR1 = P0 * DSQRT(-DISC/12.)
      PR2 = RADIAN * 10.**(-(G+DISC-29.)/25.)
      PR = DMAX1(PR1,PR2)
С
  80
      RETURN
      END
С
      SUBROUTINE RPINER5 (PR, P0, F, G, DISC)
С
С
      BSS PATTERN, RARC-83.CPM, P.115 CURVE-B,
С
        ANTENNA DIAMETER 1 METER
С
      IMPLICIT REAL*8(A-H, O-Z)
С
```

```
....
```

```
COMMON / CONSTS/ E, PI, RADIAN, DEGREE, GCR, ER, ERDB, EAP,
     1
                       PFD, ALOGE, ALN10, COIMIN, COISING
С
      IF (DISC.GE.-10.6032) THEN
      PR = P0 * DSQRT(-DISC/12.)
      GO TO 80
      ELSE IF (DISC.LE.-43.2) THEN
      PR = PI
      GO TO 80
      END IF
С
      PR = P0 * 10.**(-(DISC+11.3)/25.)
С
 80
      RETURN
      END
С
      SUBROUTINE XRPTNER1 (PR, P0.G, DISC)
с
с
      CROSS POLARIZATION RECEIVER PATTERN
С
      IMPLICIT REAL*8(A-H,O-Z)
С
      X = PR/P0
      IF (DISC.GE.-20.) GO TO 60
      IF (DISC.GE.-30.) GO TO 70
      IF (DISC.GE.-43.2) GO TO 80
С
      PR = PI
      GO TO 100
С
 60
      PR = 0.
      GO TO 100
С
 70
      PR = 10.**(-(17.3+DISC)/25.) * P0
      GO TO 100
С
 80
      PR = 10.**(-(11.3+DISC)/25.) * P0
С
 100
      RETURN
      END
```

APPENDIX E

FORMULATIONS OF MIXED-INTEGER AND LINEAR PROGRAMS

A. ALGORITHMS

A mixed integer program (MIP) can be solved by a branch-and-bound algorithm [88]. In such an algorithm, a linear objective function is to be optimized; the constraints of the problem are expressed as linear equalities or inequalities. Some, but not necessarily all, of the decision variables are integers. The set of feasible solutions that satisfy the constraints constitutes the feasible region. For our purpose, we can assume that the integer variables are bounded. Because the integer variables have a finite number of feasible values, the number of feasible solutions is finite; therefore an enumerative approach can be used to theoretically test all the feasible solutions in order to find the globally optimal solution(s).

To perform the enumeration by the branch-and-bound algorithm, the set of feasible solutions can be structured as a tree, and every branch represents one possible value of a particular integer variable. For the branch-and-bound concept, "branching" means testing a path that leads to a subset of feasible solutions, "bounding" means calculating the upper and lower bounds of the objective function value associated with the tested path. In the enumerative process, the upper and lower bounds of the objective function value are updated whenever more favorable values

are found in the branch-and-bound process. In the branch-and-bound process a path is tested against the updated upper and lower bounds: it finds a more favorable upper or lower bound of the objective function value and updates it, or it terminates testing that path and all its associated feasible solutions once it determines that this path can not yield a more favorable upper or lower bound of the objective function value. The process terminates when the updated upper and lower bounds are equal, or when it determines that an optimal solution does not exist. All the feasible solutions will have been considered implicitly, but hopefully very few will have been examined explicitly. A globally optimal solution is guaranteed, if one exists, by this process.

The linear program (LP) is commonly solved by the simplex method [81]. In this program a linear objective function is to be optimized; the constraints of the problem are expressed as linear equalities or inequalities. All the decision variables are continuous variables, and they must have nonnegative values. The set of feasible solutions constitutes a feasible region that is a convex set; its boundaries are the hyperplanes representing the linear constraints and nonnegativity restrictions. Because the objective function and the constraints are all linear equations, a locally optimal solution is always at a vertex which is the intersection of the bounding hyperplanes. The simplex method examines a sequence of locally optimal feasible solutions of the linear program. Each solution examined shares at least one boundary with the previous one, and has an objective function value no less

favorable than that of the previous solution. The process terminates when it is determined that no improved solution can be found.

The simplex method can be modified to handle nonlinear complementarity constraints through the use of restricted basis entry: when a complementary variable enters the basis at a non-zero value, its complement is forced to be non-basic and cannot enter the basis (except when the variable leaves). The effect of this modification is that the continuous feasible region is divided into many distinct subregions. Although the simplex method can still work, it only guarantees a local, but not necessarily a global, optimum, provided a feasible solution is found.

As the number of satellites increases, the computational time needed to find a solution typically increases exponentially for the MIP technique, but only polynomially for the restricted basis LP (RBLP) technique. Therefore, the MIP technique may take a prohibitively long time to solve a large problem; and the RBLP technique becomes an acceptable alternative, even though sub-optimal, rather than globallyoptimal, solutions may be found.

B. PARAMETERS AND VARIABLES

The coordinate system here is in the reverse longitude direction of the common global system, hence the longitude values increase as one moves in the westerly direction. Or simply speaking, the new coordinate system uses the magnitude of west longitude; in this way, there are only non-negative variables in both of the new formulations.

The parameters in the formulations are:

W_j(E_j) : westernmost(easternmost) feasible location for satellite j in degrees west, d_j : preferred location for satellite j relative to E_j, ΔS_{ij} : required satellite separation between satellites i and j, X_{ij} = { 1, if satellite i is west of j, X_{ij} = { 1, if satellite i is west of j, x_{ij} = { 0, otherwise, m : number of satellites. E = min {E_j}, W = max {W_j}.

The decision variables are:

 x_j : relative location of satellite j with respect to E_j , $p_{ij}(n_{ij})$: degrees west(east) of satellite i that satellite j is located,

 $x_j^{+}(x_j^{-})$: degrees west(east) of its preferred location that satellite j is located,

Y : length of the occupied orbital arc.

Note that the nonnegative variable p_{ij} alone can not represent the separation between satellites i and j, and another nonnegative variable, n_{ij} , is needed when i is east of j. Therefore when satellite i is west of j, the value of p_{ij} is positive, and n_{ij} should be set equal to zero; when satellite i is east of j, n_{ij} is positive and p_{ij} should be zero. Also note from the definition of x_j , the coordinate system for every satellite is re-originated at the eastern-most bound, E_j .

C. FORMULATION I

If the optimal criterion is to minimize the total amount of orbital arc occupied by the satellites to be synthesized, the MIP formulation is

subject to

$x_{i} - x_{j} - p_{ij} + n_{ij} = 0,$	for i < j	(E.2)
p _{ij} + n _{ij} > ΔS _{ij} ,	for i < j	(E.3)
× _j < ₩ _j - E _j ,	for all j	(E.4)
p _{ij} + n _{ij} - Y < 0,	for i < j	(E.5)
$x_j > 0,$	for all j	(E.6)
p _{ij} , n _{ij} ≥ 0,	for i < j	(E.7)
Y > 0,		(E.8)
$(E - W) \cdot x_{ij} + p_{ij} < 0,$	for i < j	(E.9)
$(W - E) \cdot x_{ij} + n_{ij} < (W - E),$	for i < j	(E.10)
× _{ij} ε {0,1},	for i < j	(E.11)

Equations (E.9) and (E.10) guarantee that

$$p_{ij} < 0, \text{ or } n_{ij} < 0.$$
 (E.12)

Together with Equation (E.7), one has

$$p_{ij} = 0, \text{ or } n_{ij} = 0.$$
 (E.13)

If the optimal solution can be found, the optimal values of the variables x_j 's specify the optimal orbital locations for the satellites. Otherwise, the code will tell the user that a feasible solution does not exist.

It is possible that the objective is only to have a feasible solution that satisfies the C/I protection requirements, as described in Chapter IV. Then one could reformulate the objective function of Equation (E.1) and ignore the variable Y, Equations (E.5) and (E.8). The calculation process will either stop when it finds a feasible solution, or determines that none exists.

Also, the same formulation (Equations (E.1) through (E.11)) is still applicable if the system requirement is to have the maximum C/I results for all the service areas, and there is no interest in the conservation of the orbit resource. One could progressively adjust the C/I protection requirement and repeat the ΔS and MIP calculations until the resulting scenario uses up the whole feasible arc. This result is the scenario that offers the maximum C/I.

D. FORMULATION II

For the same objective as stated above, the LP formulation with the nonlinear side constraints is

subject to

$x_{i} - x_{j} - p_{ij} + n_{ij} = 0,$	for i < j	(E.15)
p _{ij} + n _{ij} > ∆S _{ij} ,	for i < j	(E.16)
$x_j < W_j - E_j$,	for all j	(E.17)
p _{ij} + n _{ij} - Y ≤ 0,	for i < j	(E.18)
x _j > 0,	for all j	(E.19)
p _{ij} , n _{ij} ≥ 0,	for i < j	(E.20)
Y > 0,		(E.21)
p _{ij} .n _{ij} = 0,	for i < j	(E.22)

The solution to this problem is an orbital assignment.

In this formulation, Equation (E.22) is not a linear equation, thus the simplex method needs to be modified through the use of restricted basis entry: the variable p_{ij} can not be a basic variable if n_{ij} is a basic variable, and vice versa. Although the simplex method can still work, it only guarantees a locally optimal solution, provided a feasible solution is found.

E. FORMULATION III

It is possible that every administration has a preferred satellite location and hopes the actual assigned location will be near the preferred location. Solutions become less and less attractive as the actual location becomes further and further removed from the preferred location. A suitable objective is to minimize the sum of the absolute deviations of the satellites' actual locations from their preferred locations, i.e., to minimize the total deviation. The MIP formulation is

Minimize $f = \sum_{j} (x_j^+ + x_j^-)$ (E.23)

subject to

$x_{j} - x_{j}^{+} + x_{j}^{-} = d_{j},$	for all j	(E.24)
x _i - x _j - p _{ij} + n _{ij} = 0,	for i < j	(E.25)
p _{ij} + n _{ij} ≥ ∆S _{ij} ,	for i < j	(E.26)
х _ј < W _j - E _j ,	for all j	(E.27)
$x_{j}, x_{j}^{+}, x_{j}^{-} > 0,$	for all j	(E.28)
p _{ij} , n _{ij} ≥ 0,	for i < j	(E.29)
$(E - W) \cdot x_{ij} + p_{ij} < 0,$	for i < j	(E.30)
$(W - E) \cdot x_{ij} + n_{ij} < (W - E),$	for i < j	(E.31)
x _{ij} ε {0,1},	for i < j	(E.32)

The optimal values of the variables x_j prescribe optimal locations for the satellites which minimize the total deviation of the prescribed locations from the preferred locations. Equations (E.9) and (E.10) guarantee that

$$p_{ij} < 0, \text{ or } n_{ij} < 0.$$
 (E.12)

Together with Equation (E.7), one has

$$p_{ij} = 0, \text{ or } n_{ij} = 0.$$
 (E.13)

If the optimal solution can be found, the optimal values of the variables x_j specify the optimal orbital locations for the satellites. Otherwise, the code will tell the user that a feasible solution does not exist.

It is possible that the objective is only to have a feasible solution that satisfies the C/I protection requirements, as described in Chapter IV. Then one could reformulate the objective function of Equation (E.1) and ignore the variable Y, Equations (E.5) and (E.8). The calculation process will either stop when it finds a feasible solution, or determines that none exists.

Also, the same formulation (Equations (E.1) through (E.11)) is still applicable if the system requirement is to have the maximum C/I results for all the service areas, and there is no interest in the conservation of the orbit resource. One could progressively adjust the C/I protection requirement and repeat the ΔS and MIP calculations until the resulting scenario uses up the whole feasible arc. This result is the scenario that offers the maximum C/I.

Table E.1

Satellite preferred locations of six

administrations

URG	PRU	PRG	CHL	BOL	ARG	country
95	95	95	95	95	95	case 1
110	110	110	110	110	110	case 2
82.5	102.5	87.5	97.5	92.5	87.5	case 3

Table E.2

ΔS parameters of six administrations

ΔS	ARG	BOL	CHL	PRG	PRU	URG
ARG	*	4.17	4.19	4.32	1.41	4.14
BOL		*	4.57	4.04	4.26	0.94
CHL			*	2.00	3.04	1.59
PRG				*	1.10	2.46
PRU					*	0.37
URG						*

The ΔS matrix for these six countries is in Table E.2. The resulting assignments, together with the total occupied arc Y, the total deviation Z of the prescribed locations from the preferred locations, and the C.P.U. times in seconds are listed in Table E.3.

It is clear that the solutions obtained by solving the MIP formulation are better than those found by solving the LP formulation. The MIP solutions can never be worse than the corresponding LP solutions, but more computer time is required to solve the MIP formulation.

Table E.3

Mixed-integer and linear program results

	case 1		cas	case 2		case 3	
satellite	MIP	LP	MIP	LP	MIP	LP	
ARG	88.68	105.74	101.35	110.00	88.76	101.26	
BOL	99.57	101.57	97.18	104.33	92.93	92.50	
CHL	95.00	97.00	105.54	99.76	97.50	97.07	
PRG	93.00	95.00	107.54	97.76	84.44	87.50	
PRU	91.06	93.06	109.63	108.59	102.50	102.67	
URG	96.59	92.54	110.00	105.86	81.98	82.50	
deviation	18.42	23.71	28.76	33.69	5.27	14.36	
arc	10.89	13.20	12.82	12.24	20.52	20.17	
cpu(sec)*	25.23	1.31	13.39	1.30	2.86	1.25	

* IBM-3081 computer

APPENDIX F

C/I CALCULATION OF MIXED INTEGER PROGRAM RESULT

COUNTRY	SATELLITE	(LON.) 1	FREQUENCY (M	lHz)
ARG BOL CHL FRG FRU URG	-88.61 -99.5 -95.80 -93.80 -93.80 -91.91	8 7 Ø 6 9	4888.88 4823.89 4223.88 4823.88 4823.88 4823.88 4823.88	
TEST COUNTR	Y: ARG	SATELLITE	-38.68	
TEST	POINT	INT. SAT.	C/I (dB)	MARGIN (dB)
-63.20 -63.20 -63.20 -63.20 -65.20 -65.20 -65.20	-21.80 -21.80 -21.80 -21.80 -21.80 -21.80	BOLØ99 CHLØ95 PRGØ93 PRUØ91 URGØ96 TOTAL	4Ø.83 37.25 39.39 41.47 68.Ø2 33.39	10.83 7.25 9.39 11.47 38.02 8.39
-62.80 -62.80 -62.80 -62.80 -62.80 -62.80 -62.80	-22.88 -22.88 -22.88 -22.88 -22.88 -22.58 -22.58	BOLØ99 CHLØ95 PRGØ93 PRUØ91 URGØ96 TOTAL	41.37 51.35 32.Ø3 53.86 67.24 31.48	11.37 21.35 2.Ø3 23.86 37.24 6.48
-53.80 -53.80 -53.80 -53.80 -53.80 -53.80 -53.80	-27.20 -27.20 -27.20 -27.20 -27.20 -27.20 -27.20	BOL Ø99 CH: Ø95 Prgø93 Pruø91 Urgø96 Total	53.05 63.14 31.53 52.74 49.37 31.39	23.25 33.14 1.53 22.74 19.37 6.39
-56.7Ø -53.7Ø -56.7Ø -56.7Ø -56.7Ø -56.7Ø	-36.90 -36.90 -36.90 -36.90 -36.90 -36.90 -36.90	BOL Ø99 CHL Ø95 PR GØ93 PR UØ91 UR GØ96 TOTAL	69.73 55.57 59.61 53.45 41.77 41.25	39.73 25.57 29.61 23.45 11.77 16.25
-63.80 -63.80 -63.80 -63.80 -63.80 -63.80	-54.78 -54.78 -54.78 -54.78 -54.78 -54.78	BOL #99 CHL #95 PRG#93 PRU#91 URG#96 TOTAL	72.73 42.01 67.29 52.85 74.65 41.65	42.73 12.Ø1 37.29 22.85 44.65 16.65
-68.3Ø -63.3Ø -63.3Ø -63.3Ø -63.3Ø -63.3Ø	-54.80 -54.80 -54.80 -54.80 -54.80 -54.80 -54.80	BOL Ø99 CHL Ø95 PRGØ93 PRUØ91 URGØ96 TOTAL	73.38 39.26 68.21 53.16 75.74 39.Ø8	43.38 9.26 38.21 23.16 45.74 14.Ø8
-73.2Ø -73.2Ø -73.2Ø -73.2Ø -73.2Ø	-50.90 -50.90 -50.90 -50.90 -50.90 -50.90	BOLØ99 CHLØ95 PRGØ93 PRUØ91 URGØ96	73.25 35.44 68.41 52.91 75.82	43.25 5.44 38.41 22.91 45.82

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-73.20	-50.90	TOTAL	35.36	10.36
$ \begin{array}{c} -71.40 \\ -71.$	-39.00 -39.00 -39.00 -39.00 -39.00 -39.00 -39.00	BOLØ39 CHU395 PRGØ93 PRUØ91 URGØ96 TOTAL	70.45 35.45 65.26 54.18 71.36 35.28	4Ø.45 5.45 35.76 24.13 41.26 1Ø.38
- 7.21.50 - 7.21.50 - 7.21.50 - 7.21.50 - 7.21.50 - 7.21.50 - 7.21.50	-31.40 -31.43 -31.43 -31.43 -31.43 -31.40 -31.40	BOLØ39 CHLØ95 PRGØ93 PRUØ91 URGØ96 TOTAL	7Ø.35 35.1Ø 61.53 54.78 63.29 35.33	4Ø.35 5.1Ø 31.63 24.78 38.29 1Ø.Ø3
- 63.60 - 63.60 - 63.60 - 63.60 - 63.60 - 63.60	-24.80 -24.80 -24.80 -24.80 -24.80 -24.80 -24.80	BOL Ø99 CHL Ø95 PR GØ93 PR UØ91 UR GØ96 TOTAL	49.00 35.23 59.37 53.21 67.38 34.96	19.00 5.23 29.37 23.21 37.38 9.96
TEST COUNTR	Y : BOL	SATELLITE :	-99.57	
TEST -65.80 -65.80 -65.90 -65.90 -65.90 -65.90	POINT -12.20 -12.20 -12.20 -12.20 -12.20 -12.20 -12.20	INT. SAT. ARGØ88 CHLØ95 Prgø93 Pruø91 URGØ96 Total	C/I (dB) 7Ø.32 61.Ø1 64.35 45.32 66.Ø8 45.11	MARGIN (dB) 40.32 31.01 34.85 15.32 36.08 20.11
-65.50 -65.50 -63.50 -65.50 -63.50 -63.50 -63.50	-9.80 -9.80 -9.80 -9.80 -9.80 -9.80 -9.80	ARGØ88 CHLØ95 PRGØ93 PRUØ91 URGØ96 TOTAL	69.00 59.68 63.52 42.75 66.37 42.60	39.00 29.68 33.52 12.75 36.37 17.60
-69.88 -63.88 -69.88 -69.88 -69.88 -69.88 -69.88	-11.20 -11.20 -11.20 -11.20 -11.20 -11.20	AR GØ88 CHLØ95 PRGØ93 PRUØ91 URGØ96 TOTAL	69.81 60.49 64.34 38.97 66.93 38.92	39.81 30.49 34.34 8.97 36.93 13.92
-63.80 -63.80 -63.80 -53.80 -53.80 -53.80 -63.80	-16.10 -16.10 -16.10 -16.10 -16.10 -16.10	AR GØ88 CHLØ95 PR GØ93 PR UØ91 UR GØ96 TOTAL	47.93 60.57 43.69 67.54 62.26 42.18	17.93 30.57 13.69 37.54 32.26 17.18
-57.50 -57.50 -57.50 -57.50 -57.50 -57.50 -57.50	-18.00 -18.00 -18.00 -18.00 -18.00 -18.00 -18.00	ARGØ88 CHLØ95 PRGØ93 PRUØ91 URGØ96 TOTAL	41.71 59.57 38.56 66.53 59.66 36.80	11.71 29.57 8.56 36.53 29.66 11.8Ø

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-67.50 -22. -67.50 -22. -67.50 -22. -67.50 -22. -67.50 -22. -67.50 -22. -67.50 -22.	7Ø ARGØ88 7J CHLØ95 7J PRGØ93 7J PRCØ93 7J URGØ96 7J URGØ96 7J TOTAL	41.44 31.31 49.35 54.71 57.30 31.35	11.44 1.91 19.85 24.71 29.20 6.35
TEST COUNTRY : CH	L SATELLITE	: -95. <i>30</i>	
TEST POINT -60.50 -17. -60.50 -17. -60.50 -17. -60.50 -17. -60.50 -17. -60.50 -17. -60.50 -17.	INT. SAT 5Ø ARGØ83 5Ø BOLØ99 5Ø PRGØ93 5Ø PRUØ91 5Ø URGØ96 5Ø TOTAL	 C/I (dB) 62.92 3J.58 5Ø.44 3Ø.53 55.17 27.52 	MARGIN (dB) 32.92 Ø.58 20.44 Ø.33 25.17 2.52
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	ØØ ARGØ88 ØØ BOLØ99 ØØ PRGØ93 ØØ PRUØ91 ØØ URGØ96 ØØ TOTAL	35.33 32.18 35.49 48.86 49.75 29.19	5.33 2.18 5.49 18.86 19.75 4.19
-73.88 -34. -75.88 -34. -75.88 -34. -75.88 -34. -75.88 -34. -78.88 -34. -78.88 -34.	227 ARGØ88 28 BOLØ99 28 PRGØ93 28 PRUØ91 28 URGØ96 28 TOTAL	35.39 61.16 54.61 59.79 51.30 35.20	5.39 31.16 24.61 29.79 21.30 10.20
-71.70 -43. -71.70 -43. -71.70 -43. -71.70 -43. -71.70 -43. -71.70 -43. -71.70 -43.	28 ARGØ88 29 BOLØ99 20 PRGØ93 28 PRUØ91 28 URGØ96 28 TOTAL	35.24 62.26 58.53 59.09 56.00 35.15	5.24 32.26 28.53 29.Ø9 26.ØØ 1Ø.15
-72.80 -51.3 -72.80 -51.3 -72.80 -51.3 -72.80 -51.3 -72.80 -51.3 -72.80 -51.3	ARGØ88 BØ BOLØ99 BØ PRGØ93 BØ PRUØ91 BØ URGØ96 BØ TOTAL	34.91 63.54 59.73 58.11 58.12 34.85	4.91 33.54 29.73 28.11 28.10 9.85
-75.70/ -46.8 -75.70/ -46.8 -75.70/ -46.8 -75.70/ -46.8 -75.70/ -46.8 -75.70/ -46.8	8 ARGØ88 8 BOLØ99 8 PRGØ93 8 PRUØ91 8 URGØ96 8 TOTAL	36.11 63.76 6Ø.28 58.44 58.5Ø 36.Ø4	6.11 33.76 30.28 28.44 28.50 11.04
-74.00 -28.9 -74.00 -28.9 -74.00 -28.9 -74.00 -28.9 -74.00 -28.9 -74.00 -28.9 -74.00 -28.9	8 ARGØ88 8 BOLØ99 8 PRGØ93 8 PRUØ91 8 URGØ96 8 TOTAL	41.43 62.06 55.97 60.69 55.35 41.03	11.43 32.06 25.97 30.69 25.35 16.03
-7Ø.4Ø -18.3 -7Ø.4Ø -18.3	Ø ARGØ88 Ø Bolø99	63.43 31.3Ø	33.43 1.8Ø

-73.40 $-18.35-73.40$ $-18.30-73.40$ $-18.30-73.40$ $-18.30-73.40$ -18.30	PRGØ93 Pruø91 Urgø96	50.94 31.17 55.51 28 37	2Ø.94 1.Ø7 25.51	
-75.40 10.50		20.37	5.57	
TEST COUNTRY : PRG	SATELLITE :	-93. <i>30</i>		
TEST POINT -57.60 -25.30 -57.60 -25.30 -57.60 -25.30 -57.60 -25.30 -57.60 -25.30 -57.60 -25.30 -57.60 -25.30	INT. SAT. Argø88 Bolø99 Chlø95 Pruø91 Urgø96 Total	C/1 (dB) 32.1Ø 4Ø.41 52.58 52.47 46.66 31.31	MARGIN (dB) 2.1Ø 1Ø.41 22.38 22.47 16.66 6.31	
-58.60 -27.30 -53.60 -27.30 -53.60 -27.30 -56.60 -27.30 -58.60 -27.30 -58.60 -27.30 -58.60 -27.30	ARGØ88 BOLØ99 CHLØ95 PRUØ91 URGØ96 TOTAL	30.07 43.33 50.95 50.84 35.20 28.70	Ø.Ø7 13.33 2Ø.95 2Ø.84 5.2Ø 3.7Ø	
-56.20 -27.20 -56.20 -27.20 -56.20 -27.20 -56.20 -27.20 -56.20 -27.20 -56.20 -27.20 -56.20 -27.20	ARGØ88 BOLØ99 CHLØ95 PRUØ91 URGØ96 TOTAL	31.10 45.13 51.31 51.20 37.50 30.00	1.10 15.13 21.31 21.20 7.50 5.00	
-54.70 -25.50 -54.70 -25.50 -54.70 -25.50 -54.70 -25.50 -54.70 -25.50 -54.70 -25.50 -54.70 -25.50	ARGØ88 BOLØ99 CHLØ95 PRUØ91 URGØ96 TOTAL	31.86 43.23 51.46 51.34 49.Ø9 31.39	1.86 13.23 21.46 21.34 19.Ø9 6.39	
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	ARGØ88 BOLØ99 CHLØ95 PRUØ91 URGØ96 TOTAL	31.72 41.6Ø 51.Ø3 5Ø.91 57.11 31.19	1.72 11.60 21.03 20.91 27.11 6.19	
-53.10 -20.20 -53.10 -20.20 -58.10 -20.20 -58.10 -20.20 -58.10 -20.20 -58.10 -20.20 -58.10 -20.20	ARGØ88 BOLØ99 CHLØ95 PRUØ91 URGØ96 TOTAL	32.21 36.69 51.87 51.75 6Ø.6Ø 3Ø.81	2.21 6.69 21.87 21.75 3Ø.6Ø 5.81	
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	AR GØ88 BOLØ99 CHLØ95 PR UØ91 UR GØ96 TOTAL	31.99 35.81 51.46 51.35 61.11 38.41	1.99 5.81 21.46 21.35 31.11 5.41	
-62.20 -20.50 -62.20 -20.50 -62.20 -20.50 -62.20 -20.50 -62.20 -20.50	AR GØ88 BOLØ99 Chlø95 PR UØ91	31.81 35.22 45.9 <i>8</i> 51.45	1.81 5.22 15.90 21.45	
-62.20 -62.20	-20.50 -20.50	URG ø96 To tal	6Ø.Ø7 3Ø.Ø2	3Ø.Ø7 5.Ø2
--	---	--	--	--
-62.70 -62.70 -62.70 -52.70 -52.70 -62.70 -62.70	-22.20 -22.20 -22.20 -22.20 -22.20 -22.20 -22.20	ARGØ88 BOLØ99 CHLØ95 PRUØ91 URGØ96 TOTAL	31.Ø3 35.5Ø 38.46 51.18 57.93 29.13	1.Ø3 5.5Ø 8.45 21.18 27.93 4.13
-53.70 -53.70 -53.70 -53.70 -53.70 -53.70 -58.70	-27.20 -27.20 -27.20 -27.20 -27.20 -27.20 -27.20	ARGØ88 BOLØ99 CHLØ95 PRUØ91 URGØ96 TOTAL	3Ø.12 43.Ø1 51.Ø2 5Ø.9Ø 35.62 28.82	Ø.12 13.Ø1 21.Ø2 2Ø.9Ø 5.62 3.82
TEST COUNTR	RY : PRU	SATELLITE :	-91.Ø6	
TEST -7Ø.4Ø -7Ø.4Ø -7Ø.4Ø -7Ø.4Ø -7Ø.4Ø	POINT -18.30 -18.30 -18.30 -18.30 -18.30 -18.30 -18.30	INT. SAT. Argø88 Bolø99 Chlø95 Prgø93 Urgø96 Total	C/I (dB) 52.44 38.18 30.25 50.24 68.67 29.54	MARGIN (dB) 22.44 8.18 Ø.25 2Ø.25 38.67 4.54
-69.00 -69.00 -69.00 -69.00 -69.00 -69.00	-12.30 -12.30 -12.30 -12.30 -12.30 -12.30 -12.30	ARGØ88 BOLØ99 CHLØ95 PRGØ93 URGØ96 TOTAL	53.36 38.54 48.79 51.15 73.04 37.81	23.36 8.54 18.79 21.15 43.04 12.81
-78.58 -78.58 -78.58 -78.58 -78.58 -78.58 -78.58	-9.40 -9.40 -9.40 -9.40 -9.40 -9.40	ARGØ88 BOLØ99 Chlø95 PRGØ93 URGØ96 TOTAL	54.10 41.74 59.68 53.03 75.81 41.14	24.10 11.74 29.68 23.03 45.81 16.14
-74.00 -74.00 -74.00 -74.00 -74.00 -74.00	-7.68 -7.68 -7.68 -7.68 -7.68 -7.68	ARGØ88 BOLØ99 CHLØ95 PRGØ93 URGØ96 TOTAL	54.91 57.52 6Ø.49 56.79 78.36 5Ø.97	24.91 27.52 3Ø.49 26.79 48.36 25.97
-78.88 -78.88 -78.88 -78.88 -78.88 -78.88	-2.78 -2.78 -2.78 -2.78 -2.78 -2.78 -2.78	ARGØ88 BOLØ99 CHLØ95 PRGØ93 URGØ96 TOTAL	52.37 66.3Ø 57.95 54.98 77.12 49.65	22.37 36.3Ø 27.95 24.98 47.12 24.65
-75.20 -75.20 -75.20 -75.20 -75.20 -75.20 -75.20	8.88 8.88 8.88 8.88 8.88 8.88 8.88 8.8	ARGØ88 BOLØ99 CHLØ95 PRGØ93 URGØ96 TOTAL	54.94 66.68 58.34 58.41 77.5Ø 51.97	24.94 36.68 28.34 28.41 47.5Ø 26.97

-80.30	-3.4Ø	AR GØ88	55.04	25.84
-ea.3ø	-3.4Ø	BOLØ99	66.33	36.83
-S.J.3Ø	-3.4.3	CH6Ø95	58.49	28.49
- ` *.3ø	-3.4Ø	PRGØ93	59.5Ø	29.5Ø
- 30	-3.41	URGØ96	77.35	47.65
-E.J.3Ø	-3.4Ø	TOTAL	52.70	27.7Ø
-81.30	-4.40	ARGØ88	55.54	25.54
-51.30	-4.40	BOLØ99	66.47	36.47
-61.30	-4.40	CHLØ95	58.13	28.13
-81.30	-4.40	PRGØ93	59.34	29.34
-81 30	- 4 . 4 0	URGØ96	77.29	47.29
-81.3Ø	-4.4Ø	TOTAL	52.41	27.41
-81 20	-6.10	ARGØ88	55.26	25.26
-61 20	-6.10	BOLØ99	66.79	36.79
-81 20	-6.10	CHL Ø95	58.45	28.45
-81 20	-6.10	PRGØ93	59.17	29.17
-81 20	-6 10	IRGROG	77.61	47.61
-81.20	-6.1Ø	TOTAL	52.33	27.33
-76 10	-13.49	ARGØ88	54.34	24.34
-76 10	-13.49	BOLAGO	52.75	22.75
-76 10	+13 40	CHI 095	36 94	6 94
-76 10	-13.40	PRGM93	55.68	25.68
-76 10	-13 40	URCOSS	75 66	45 66
-76 10	-13 40		36 69	11 20
/0.10	13.40	IVIAL	30.05	11.05

TEST COUNTRY : URG

SATELLITE : -96.59

TEST	POINT	INT. SAT.	C/I (dB)	MARGIN	(dB)
-56.20	-34.90	ARGØ88	38.13	8.13	
-56.20	-34.90	BOLØ99	55.95	25.95	
-56.20	-34.90	CHLØ95	49.15	19.15	
-56.20	-34.90	PRGØ93	57.89	27.89	
-56.20	-34.90	PRIIMAI	62.90	32.90	
-56 20	-34 90	TOTAL	37 68	12 68	
00.20	04.2%	10142	07.00	12.00	
-54.90	-35.00	ARGØ88	38.7Ø	8.7Ø	
-54.90	-35.00	BOLØ99	56.02	26.02	
-54.90	-35.00	CHLØ95	49.21	19.21	
-54.90	-35.00	PRGØ93	57.96	27.96	
-54.90	-35.00	PRUØ91	62.96	32.96	
-54.90	-35.00	TOTAL	38.19	13.19	
-53.50	-34.00	ARGØ88	39.49	9.49	
-53.50	-34.00	BOLØ99	56.28	26.28	
-53.5Ø	-34.00	CHLØ95	49.47	19.47	
-53.50	-34.00	PRGØ93	51.23	21.23	
-53.50	-34.00	PRUØ91	63.22	33.22	
-53.50	-34.00	TOTAL	38.73	13.73	
-53.2Ø	-32.7Ø	ARGØ88	39.27	9.27	
-53.2Ø	-32.7Ø	BOLØ99	55.99	25.99	
-53.2Ø	-32.7Ø	CHLØ95	49.18	19.18	
-53.20	-32.7Ø	PRGØ93	44.41	14.41	
-53.20	-32.7Ø	PRUØ91	62.93	32.93	
-53.20	-32.7Ø	TOTAL	37.71	12.71	
-55.60	-3Ø.8Ø	AR GØ88	38.43	8.43	

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-55.6Ø	-3Ø.8Ø	BOLØ99	FC 21	n <i>c</i>
-55.6ø	-3Ø.8Ø	CHLØ95	40 41	26.21
-55.60	-30.80	PRCMAR	47.41	19.41
-55.6Ø	-30.80	PPURO1	37.26	7.26
-55.60	-30 80	TOTAL	63.16	33.16
		TOTAL	34.61	9.61
-55.90	- 3 67 1 67	ABCOOD		
	-30 10		37.58	7.58
-56.90	-30.10	BULMAA	47.88	17.88
-56 90	-20.10	CHLØ95	49. Ø2	19.02
-56 90	-30.10	PRG/093	35.1Ø	5.10
-56 90	-30.10	PRUØ91	62.77	32.77
-38.90	-30.10	TOTAL	32.9Ø	7.90
-57 .6Ø	-30.20	ARGØ88	27 54	
-57.6Ø	-3Ø.2Ø	BOLAGO	40 40	7.54
-57.6Ø	-30.20		40.42	18.42
-57.6Ø	-30.20	PRCMAD	49.19	19.19
-57.6Ø	-38.28	PPII/201	36.30	6. 3Ø
-57.60	-30 20		62.94	32.94
	00.20	IUTAL	33.59	8.59
-58.20	-31.9Ø	ARGØ88	38 30	9 2 7
-58.20	-31.9Ø	BOLØ99	56 91	0.30
-53.2Ø	-31.9Ø	CHLØ95	A1 25	26.91
-53.2Ø	-31.90	PRGØ93	41.33	11.35
-58.2Ø	-31.90	PRUMAI	4J.02 62 oc	15.82
-53.2Ø	-31.9Ø	TOTAL	26 02	33.86
		· · · · · ·	30.03	11.Ø3
-58.40	-33.9Ø	ARGØ88	37 24	7
-58.40	-33.9Ø	BOLØ99	55 92	1.24
-58.4Ø	-33.90	CHLØ95	37 27	25.83
-58.4Ø	-33.9Ø	PRGM93	57.27	/.2/
-58.4Ø	-33.9Ø	PRUMPI	62 77	27.77
-58.4Ø	-33.90	TOTAL	02.77	32.77
_		IVIAL	34.19	9.19
-57.90	-34.50	ARGØ88	37.13	7 1 2
-5/.90	-34.5Ø	BOLØ99	55.54	7.13 25 EA
-57.90	-34.5Ø	CHLØ95	38.25	20.04
-57.9Ø	-34.50	PRGØ93	57 48	0.25
-57.9Ø	-34.50	PRUØ91	57 49	27.48
-57.9Ø	-34.50	TOTAL	24 50	32.48
			34.30	9.58

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