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PRINT FIG. 2

NOTICE

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(NASA-Case-NPO-17785-1-CU) ROBUST
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PATENT APPLICATION

ROBUST HIGH-PERFORMANCE CONTROL FOR ROBOTIC MANIPULATORS

BACKGROUND OF THE INVENTION

1. Origin of the Invention

The invention described herein was made in the performance of the work under a NASA Contract and is subject to the provisions of Public Law 96517 (35 USC 202) in which the contractor has elected not to retain title.

2. Field of the Invention

This invention relates to control systems for controlling robotic manipulators.

3. Description of the Prior Art

The next generation of robotic manipulators will perform high-precision tasks in partially unknown and unstructured environments. These tasks require precise motion control of the manipulator under unknown and varying payloads. These requirements are far beyond the capabilities of present-day industrial robot

1 controllers, and demand robust high-performance
2 manipulator control systems. The need for advanced
3 manipulator control systems to accomplish accurate
4 trajectory tracking has therefore been recognized for
5 some time, and two parallel lines of research have been
6 pursued. The primary outcome of such research is the
7 development of two classes of advanced manipulator
8 control schemes, namely model-based and performance-
9 based techniques.

10 Model-based techniques, such as the Computed Torque
11 Method by B. R. Markiewicz: Analysis Of The Computed
12 Torque Drive Method And Comparison With Conventional
13 Position Servo For A Computer-Controlled Manipulator,
14 Technical Memorandum 33-601, Jet Propulsion Laboratory,
15 1973, are based on cancellation of the nonlinear terms
16 in the manipulator dynamic model by the controller.
17 This cancellation is contingent on two assumptions which
18 are not often readily met in practice. First, the
19 values of all parameters appearing in the manipulator
20 dynamic model, such as payload mass and friction
21 coefficients, must be known accurately. Second, the
22 full dynamic model of the manipulator needs to be known
23 and computed on-line in real-time at the servo control
24 rate. Performance-based techniques, such as the direct
25 adaptive control method by S. Dubowsky and D. T.
26 DesForges: The Application Of Model-Referenced Adaptive
27 Control To Robotic Manipulators, ASME Journal of Dynamic
28 Systems, Measurement and Control, Vol. 101, pp. 193-200,
29 1979, attempt to overcome these limitations by adjusting
30 the controller gains on-line in real-time, based on the
31 tracking performance of the manipulator; and, thus,
32 eliminating the need for the manipulator model.
33 Therefore, the identification of the manipulator and
34 payload parameters or the complex manipulator dynamic
35 model is not necessary, and hence a fast adaptation can

1 be achieved. Adaptive control methods, however, may
 2 become unstable for high adaptation rates and treat the
 3 manipulator as a "black-box" by not utilizing any part
 4 of the manipulator dynamics in the control law
 5 formulation.

6 During the past few years, several attempts have
 7 been made to combine the model-based and performance-
 8 based techniques in order to take full advantage of the
 9 merits of both techniques and overcome their
 10 limitations. For instance, the approach of J. J. Craig,
 11 P. Hsu, and S. S. Sastry: Adaptive Control Of
 12 Mechanical Manipulators, Proc. IEEE Intern. Conf. on
 13 Robotics and Automation, Vol. 1, pp. 190-195, San
 14 Francisco, 1986, and R. H. Middleton and G. C. Goodwin:
 15 Adaptive Computed Torque Control For Rigid Link
 16 Manipulators, Proc. IEEE Conf. on Decision and Control,
 17 Vol. 1, pp. 68-73, Athens, 1986, the manipulator
 18 parameters are estimated adaptively first and are then
 19 utilized in a dynamic-based control law.

20 A search was conducted in the following classes and
 21 subclasses.

22	<u>CLASS</u>	<u>SUBCLASS</u>
23	318	561, 567, 568, 569, 599, 600, 601
24		616, 617, and 685, 561, 604, 618 and
25		621
26	364	133, 134, 148, 150, 157, 162, 165,
27		183, 193, 478 and 513
28	901	14, 15 and 19

29 The results of the search include the following
 30 patents:

31	Oswald	4,200,827
32	Penkar et al.	4,773,025
33	Axelby et al.	4,663,703
34	Takahashi et al.	4,639,652
35	Shigemasa	4,719,561

1 Browder 4,341,986
2 Hafner et al. 4,546,426
3 Horak 4,547,858
4 Perzley 4,603,284
5 Perreirra et al. 4,763,276
6 Littman et al. 3,758,762
7 Hiroi et al. 4,563,735
8 Matsumura et al. 4,670,843
9 Shigemasa 4,679,136
10 First attention is directed to Oswald 4,200,827
11 which discloses a control system for a magnetic head
12 including both velocity and position feedback and
13 feedforward signals representing both velocity and
14 acceleration. See Figure 1 and column 3, line 17 to
15 column 6, line 35. Also, see Penkar et al. 4,773,025
16 and Axelby 4,663,703.
17 Next attention is directed to Takahashi et al.
18 4,639,652 which discloses a control system for a robot
19 manipulator including adaptive position and velocity
20 feedback gains. See gain adjuster 14 and gains 5 and 6
21 in Figure 1. Particular attention should be given to
22 the circuit diagram presented in Figure 4 of this
23 reference which differs from Figure 1 only in the use of
24 the transfer function $T(s)$ and operates in accordance
25 with the description beginning at column 4, line 48
26 through column 6, line 29. This reference is of
27 interest only because of the high speed positioning
28 control. It relies upon a prior art technique commonly
29 known as "Identification", in that test runs permit the
30 gains of its control law to be identified.
31 Next attention is directed to Shigemasa 4,719,561
32 which discloses a control system having robust
33 controller 24 in combination with a PID controller 22.
34 See Figure 3 and column 5, line 13.
35 The following references all disclose a control

1 system for a robot manipulator.

2	Browder	4,341,986
3	Hafner	4,546,426
4	Horak	4,547,858
5	Perzley	4,603,284
6	Perreirra et al.	4,763,276

7 The following references are cited as of interest.

8	Littman et al.	3,758,762
9	Hiroi et al.	4,563,735
10	Matsumura et al.	4,670,843
11	Shigemasa	4,679,136

12
13 In contrast to the Computed Torque Method of the
14 prior art, the invention does not rely on an accurate
15 dynamic model in order to control the manipulator.
16 Furthermore, global asymptotic stability of the control
17 system is assured since the feedback adaptation laws are
18 derived from a Lyapunov analysis, and the feedforward
19 controller is outside the servo control loop.

20
21 A new, robust control system using a known part of
22 the manipulator's dynamics in a feedforward control
23 circuit and any unknown dynamics and uncertainties
24 and/or variations in the manipulator/payload parameters
25 is accounted for in an adaptive feedback control loop.

26
27 SUMMARY OF THE INVENTION

28
29 This invention discloses and claims a novel
30 approach of combining model-based and performance-based
31 control techniques. Two distinct and separate design
32 philosophies have been merged into one novel control
33 system. The invention's control law formulation is
34 comprised of two distinct and separate components, each
35 of which yields a respective signal component that is

1 combined into a total command signal for the system.

2 Those two separate system components include a
3 feedforward controller and a feedback controller. The
4 feedforward controller is model-based and contains any
5 known part of the manipulator dynamics that can be used
6 for on-line control to produce a nominal feedforward
7 component of the system's command signal. The feedback
8 controller is performance-based and consists of a simple
9 adaptive PID controller which generates an adaptive
10 control signal to complement the nominal feedforward
11 signal. The feedback adaptation laws are very simple,
12 allowing a fast servo control loop implementation.

13
14 BRIEF SUMMARY OF THE FIGURES OF THE DRAWING

15
16 Figure 1 is a figure depicting a schematic diagram
17 of a typical actuator and link assembly in accordance
18 with the invention;

19 Figure 2 is a figure depicting a
20 feedforward/feedback tracking control scheme in
21 accordance with the invention;

22 Figure 3 is a figure depicting a two-link planar
23 manipulator in a vertical plane in accordance with the
24 invention;

25 Figure 4(i) is a figure depicting the desired
26 [dashed] and actual [solid] trajectories of the joint
27 angle $\theta_1(t)$ in accordance with the invention;

28 Figure 4(ii) is a figure depicting the desired
29 [dashed] and actual [solid] trajectories of the joint
30 angle $\theta_2(t)$ in accordance with the invention;

31 Figure 5(i) is a figure depicting the variation of
32 the tracking - error $e_2(t)$ in accordance with the
33 invention;

34 Figure 5(ii) is a figure depicting the variation of
35 the tracking - error $e_1(t)$ in accordance with the

1 invention;

2 Figure 6(i) is a figure depicting the variation of
3 the control torque $T_1(t)$ in accordance with the
4 invention;

5 Figure 6(ii) is a figure depicting the variation of
6 the control torque $T_2(t)$ in accordance with the
7 invention;

8 Figure 7(i) is a figure depicting the variations of
9 the auxiliary signals $f_1(t)$ [solid] and $f_2(t)$ [dashed]
10 in accordance with the invention;

11 Figure 7(ii) is a figure depicting the variations
12 of the position gains $k_p^1(t)$ [solid] and $k_p^2(t)$ [dashed]
13 in accordance with the invention;

14 Figure 7(iii) is a figure depicting the variations
15 of the velocity gains $k_v^1(t)$ [solid] and $k_v^2(t)$ [dashed]
16 in accordance with the invention;

17 Figure 8 is a figure depicting the functional
18 diagram of the testbed facility in accordance with the
19 invention;

20 Figure 9(i) is a figure depicting the desired
21 [dashed] and actual [solid] PUMA waist angles under
22 adaptive controller in accordance with the invention;

23 Figure 9(ii) is a figure depicting the waist
24 tracking-error under adaptive controller in accordance
25 with the invention;

26 Figure 10(i) is a figure depicting the desired
27 [dashed] and actual [solid] PUMA waist angles under
28 unimation controller in accordance with the invention;

29 Figure 10(ii) is a figure depicting the waist
30 tracking-error under unimation controller in accordance
31 with the invention;

32 Figure 11(i) is a figure depicting the variation of
33 the auxiliary signal $f(t)$ in accordance with the invention;

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1 Figure 11(ii) is a figure depicting the variation
2 of the position gain $k_p(t)$ in accordance with the
3 invention;

4 Figure 11(iii) is a figure depicting the variation
5 of the velocity gain $k_v(t)$ in accordance with the
6 invention;

7 Figure 11(iv) is a figure depicting the variation
8 of the control torque $T(t)$ in accordance with the
9 invention;

10 Figure 12(i) is a figure depicting the desired
11 [dashed] and actual [solid] waist angles with arm
12 configuration change in accordance with the invention;
13 and

14 Figure 12(ii) is a figure depicting the waist
15 tracking-error with arm configuration change in
16 accordance with the invention.

17 18 DESCRIPTION OF THE PREFERRED EMBODIMENT

19 1. SUMMARY OF PRESENTATION.

20 The presentation of the invention is structured as
21 follows. In Section 2, the integrated dynamic model of
22 a manipulator and actuator system is derived. The
23 tracking control scheme is described fully in Section 3.
24 In Section 4, the digital control implementation of the
25 scheme is given. The issue of robustness is discussed
26 in Section 5. The control scheme is applied in Section
27 6 to the model of a two-link arm, and extensive
28 simulation results are given to support the method. In
29 Section 7, the implementation of the proposed control
30 scheme on a PUMA industrial robot is described and
31 experimental results are presented to validate the
32 improved performance of the invention. Section 8
33 discusses the results and concludes the presentation of
34 the description of the invention.

35 2. INTEGRATED DYNAMIC MODEL OF MANIPULATOR-PLUS-

1 ACTUATOR SYSTEM

2 Most papers on manipulator control neglect the
3 dynamics of joint actuators, and treat the joint torques
4 as the driving signals. In this section, I take a
5 realistic approach by including the actuator dynamics
6 and modeling the manipulator and actuators as an
7 integrated system.

8 In many industrial robots such as the Unimation
9 PUMA, the links of the manipulator are driven by
10 electric actuators at the corresponding joints, and the
11 dynamics of the joint actuators must be taken into
12 account. Note that although electric actuators are
13 modeled hereinafter, the results are general since the
14 form of dynamic equations for other types of actuators
15 is essentially the same.

16 Referring to Figure 1, each actuator 100 may be
17 considered as comprising a link 101, driven by a gear
18 110 that meshes with a motor-driven drive gear 125. Many
19 such actuators are generally required for any given
20 robotics application. A single actuator as a general
21 case will be presented in this application for
22 simplicity purposes. It should be understood that
23 several actuators as needed are driven by the command
24 signal as developed by the control system of this
25 invention.

26 Any typical actuator is basically a DC servomotor
27 with a permanent magnet 130 to provide the motor field
28 and the driving signal is a voltage or a current applied
29 to the armature winding. In Figure 1, a driving voltage
30 identified simply as V_j is impressed across a pair of
31 input terminals 140. The resistance and inductance
32 shown in the Figure simply represent the internal
33 parameters typically found in any actuator and such
34 matters are well known in the art and require no further
35 description. Since servomotors are inherently high-speed

low-torque devices, the gear assembly 110,125 is often required to mechanically couple the armature shaft 126 to the robot link 110 in order to obtain speed reduction and torque magnification.

Consider now the j th actuator 100 and suppose that the armature is voltage-driven, as shown in Figure 1. This representation is general because in cases where the armature is current-driven using the current source $i(t)$ with shunt resistance R_c , the driving source can be replaced by the voltage source $v(t) = R_c i(t)$ with series resistance $R_v = \frac{1}{R_c}$. Therefore, without loss of generality, we can assume that the driving source of the j th joint motor is always the voltage source $v_j(t)$ with the internal resistance r_j . This source produces the current $i_j(t)$ in the armature circuit; and the electrical equation for the j th actuator can be written as

$$v_j(t) = r_j i_j(t) + R_j i_j(t) + L_j \frac{d}{dt} [i_j(t)] + K_{b_j} \frac{d}{dt} [\phi_j(t)] \quad (1)$$

where R_j and L_j are the resistance and inductance of the j th armature winding, $\phi_j(t)$ is the angular displacement of the j th armature shaft, and the term $K_{b_j} \frac{d\phi_j(t)}{dt}$ is

due to the back-emf generated in the armature circuit. Let us now consider the mechanical equation of the actuator. Referring to the armature shaft, the "equivalent" moment of inertia and friction coefficient of the total load are given by K. Ogata: Modern Control Engineering, Prentice Hall Inc., N.J., 1970

$$J_j J_{jm} + \left[\frac{N_{jm}}{N_{j\ell}} \right]^2 J_{j\ell} = J_{jm} + (N_j)^2 J_{j\ell} \quad (2)$$

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$$f_j = f_{jm} + \left[\frac{N_{jm}}{N_{jl}} \right] f_{jl} = f_{jm} + (N_j)^2 f_{jl} \quad (3)$$

where $\{J_{jm}, f_{jm}\}$ and $\{J_j, f_{jl}\}$ are the moments of inertia and friction coefficients of the j th motor shaft and the j th robot link respectively, while N_{jm} and N_j are the numbers of gear teeth on the motor side and on the link

side respectively, and $N_j = \frac{N_{jm}}{N_{jl}} < 1$ is the gear ratio.

Although it is assumed that there is one gear mesh between the motor and the link, the result can be extended to multi-mesh gear trains in a trivial manner. See K. Ogata: Modern Control Engineering, Prentice Hall Inc., N.J., 1970. Equations (2) and (3) indicate that, as seen by the motor shaft, the link inertia and friction are reduced by a factor of $(N_j)^2$. Now, the torque $r_j(t)$ generated by the j th servomotor is proportional to the armature current $i_j(t)$; that is,

$r_j(t) = K_{aj} i_j(t)$, and will cause rotation of the armature shaft by $\phi_j(t)$. In addition, the armature will exert an "effective" torque $T_j(t)$ on the j th robot link through the gear train. Thus, the mechanical equation for the j th actuator can be expressed as (refer to K. Ogata, supra)

$$J_j \frac{d^2 \phi_j(t)}{dt^2} + f_j \frac{d\phi_j(t)}{dt} + N_j T_j(t) = r_j(t) \quad (4)$$

Let us now denote the angular displacement of the j th robot joint by $\theta_j(t)$, where

$$\theta_j(t) = N_j \phi_j(t) \quad (5)$$

due to the gear train. Then, (1) and (4) can be written in terms of $\theta_j(t)$ as

$$v_j(t) = (r_j + R_j)i_j(t) + L_j \frac{di_j(t)}{dt} + \frac{1}{N_j} K_{bj} \frac{d\theta_j(t)}{dt} \quad (6)$$

$$r_j(t) = K_{aj} i_j(t) = \frac{J_j}{N_j} \frac{d^2 \theta_j(t)}{dt^2} + \frac{f_j}{N_j} \frac{d\theta_j(t)}{dt} + N_j T_j(t) \quad (7)$$

Eliminating the armature current $i_j(t)$ between (6) and (7), the dynamic model of the j th actuator can be described by the third order differential equation

$$\begin{aligned} \left[\frac{L_j J_j}{K_{aj} N_j} \right] \frac{d^3 \theta_j}{dt^3} + \left[\frac{(r_j + R_j) J_j + L_j f_j}{K_{aj} N_j} \right] \frac{d^2 \theta_j}{dt^2} \\ + \left[\frac{(r_j + R_j) f_j + K_{bj} K_{aj}}{K_{aj} N_j} \right] \frac{d\theta_j}{dt} + \left[\frac{L_j N_j}{K_{aj}} \right] \frac{dT_j}{dt} \\ + \left[\frac{(r_j + R_j) N_j}{K_{aj}} \right] T_j = v_j \end{aligned} \quad (8)$$

Consequently, for an n -jointed robot, the n joint actuators as a whole can be represented by the $(3n)$ th order vector differential equation

$$A\ddot{\theta}(t) + B\dot{\theta}(t) + C\dot{\theta}(t) + D\dot{T}(t) + ET(t) = V(t) \quad (9)$$

where $V(t)$, $\theta(t)$ and $T(t)$ are $n \times 1$ vectors and the $n \times n$ diagonal matrices in (9) are defined by

$$\begin{aligned} A_{jj} &= \left[\frac{L_j J_j}{K_{aj} N_j} \right] ; & B_{jj} &= \left[\frac{(r_j + R_j) J_j + L_j f_j}{K_{aj} N_j} \right] \\ C_{jj} &= \left[\frac{(r_j + R_j) f_j + K_{bj} K_{aj}}{K_{aj} N_j} \right] ; & D_{jj} &= \left[\frac{L_j N_j}{K_{aj}} \right] ; & E_{jj} &= \left[\frac{(r_j + R_j) N_j}{K_{aj}} \right] \end{aligned}$$

In a typical DC servomotor, the inductance of the armature winding is in the order of tenths of millihenries, while its resistance is in the order of a few ohms. Refer to J. Y. S. Luh: Conventional Controller Design For Industrial Robots--A Tutorial,

1 IEEE Trans. Systems, Man and Cybernetics, SMC 13(3), pp.
 2 298-316, 1983. Thus, the inductances L_j can safely be
 3 neglected ($L_j \approx 0$) and in this case the actuator model
 4 (9) reduces (2n)th order model
 5

$$6 \quad G\ddot{\theta}(t) + C\dot{\theta}(t) + ET(t) = V(t) \quad (10)$$

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 8
 9 where $G_{jj} = \left[\frac{(r_j + R_j)J_j}{K_{aj}N_j} \right]$. It is seen that the
 10 approximation $L_j \approx 0$ has resulted in $A = D = 0$, hence a
 11 decrease in the order of the model from $3n$ to $2n$.
 12

13 Now that the joint actuators have been modeled, we
 14 shall consider the manipulator dynamics. In general,
 15 the dynamic model of an n -jointed manipulator which
 16 relates the $n \times 1$ "effective" joint torque vector $T(t)$
 17 to the $n \times 1$ joint angle vector $\theta(t)$ can be written as
 18 (See J. J. Craig: Robotics--Mechanics and Control,
 19 Addison Wesley Publishing Company, Reading, MA, 1986).
 20

$$21 \quad M^*(m, \theta)\ddot{\theta} + N^*(m, \theta, \dot{\theta}) = T \quad (11)$$

22
 23 where m is the payload mass, $M^*(m, \theta)$ is the symmetric
 24 positive-definite $n \times n$ inertia matrix, $N^*(m, \theta, \dot{\theta})$ is the
 25 $n \times 1$ vector representing the total torque due to
 26 Coriolis and centrifugal term, gravity loading term, and
 27 frictional term. The elements of M^* and N^* are highly
 28 complex nonlinear functions which depend on the
 29 manipulator configuration θ , the speed of motion $\dot{\theta}$, and
 30 the payload mass m . On combining (10) and (11), we
 31 obtain the integrated dynamic model of the manipulator-
 32 plus-actuator system as
 33

$$34 \quad M(m, \theta)\ddot{\theta} + N(m, \theta, \dot{\theta}) = V \quad (12)$$

1 where the terms in (12) are defined as

$$2 \quad M(m, \theta) = G + EM^*(m, \theta) \quad ; \quad N(m, \theta, \dot{\theta}) = C\dot{\theta} + EN^*(m, \theta, \dot{\theta})$$

3
4
5 Equation (12) represents a (2n)th order coupled
6 nonlinear system with the $n \times 1$ input vector $V(t)$ of the
7 armature voltages and the $n \times 1$ output vector $\theta(t)$ of
8 the joint angles.

9 Although the manipulator dynamic model (11) and the
10 integrated system model (12) are both of order (2n), it
11 is important to note that the integrated model (12) is a
12 more accurate representation of the system than the
13 manipulator model (11), which does not include the
14 actuator dynamics. This is due to the following
15 considerations:

16 (i) Electrical Parameters: The main contribution from
17 the electrical part of the joint actuators to the
18 integrated system dynamics is the back-emf term $K_b \dot{\theta}(t)$
19 in (6). This term can have a significant effect on the
20 robot performance when the speed of motion $\dot{\theta}(t)$ is high.
21 Note that the back-emf appears as an internal damping
22 term, contributing to the coefficient of $\dot{\theta}(t)$ in (12).
23 The other electrical parameter is the armature
24 resistance R which appears in (6) and converts the
25 applied armature voltage $v(t)$ to the current $i(t)$ and in
26 turn to the driving torque $T(t)$.

27 (ii) Mechanical Parameters. The major contribution from
28 the mechanical part of the joint actuators to the robot
29 performance is due to the gear ratios $N_j [< 1]$ of the gear
30 trains coupling the motor shafts to the robot links. As
31 seen from (4), the "effective" driving torque on the j th
32 link is reduced by a factor of N_j as seen by the j th
33 joint actuator. In addition, from (2) and (3), the
34 moments of inertia and friction coefficients of the j th
35

link are also reduced by a factor of $(N_j)^2$ as seen by the motor shaft. This implies that the mechanical parameters of joint motors, namely the motor shaft inertia and friction, can have a significant effect on the overall system performance; particularly in robots with large gear ratios such as PUMA 560 where N_j is typically 1:100.

3. TRACKING CONTROL SCHEME

Given the integrated dynamic model of the manipulator-plus-actuator system as

$$M(m, \theta) \ddot{\theta} + N(m, \theta, \dot{\theta}) = V \quad (13)$$

The tracking control problem is to devise a control system which generates the appropriate armature voltages $V(t)$ so as to ensure that the joint angles $\theta(t)$ follow any specified reference trajectories $\theta_r(t)$ as closely as possible, where $\theta_r(t)$ is an $n \times 1$ vector.

The intuitive solution to the tracking control problem is to employ the full dynamic model (13) in the control scheme in order to cancel out the nonlinear terms in (13). This approach is commonly known as the Computed Torque Technique (see B. R. Markiewicz, *supra*), and yields the control law

$$V = M(m, \theta) [\ddot{\theta}_r + K_v(\dot{\theta}_r - \dot{\theta}) + K_p(\theta_r - \theta)] + N(m, \theta, \dot{\theta}) \quad (14)$$

where K_p and K_v are constant diagonal $n \times n$ position and velocity feedback gain matrices. This results in the error differential equation

$$\ddot{e}(t) + K_v \dot{e}(t) + K_p e(t) = 0 \quad (15)$$

1 where $e(t) = \theta_r(t) - \theta(t)$ is the $n \times 1$ vector of position
 2 tracking-errors. When the diagonal elements of K_p and
 3 K_v are positive, (15) is stable; implying that
 4 $e(t) \rightarrow 0$ or $\theta(t) \rightarrow \theta_r(t)$ as $t \rightarrow \infty$, i.e. tracking is
 5 achieved. In the control law (14), we have implicitly
 6 made a few assumptions which are rarely true in
 7 practice. The major problem in implementing (14) is
 8 that the values of the parameters in the manipulator
 9 model (13) are often not known accurately. This is
 10 particularly true of the friction term and the payload
 11 mass. Another problem in implementation of (14) is that
 12 the entire dynamic model (13) of the manipulator must be
 13 computed on-line in real time. These computations are
 14 quite involved, and the computer expense may make the
 15 scheme economically unfeasible.

16 In an attempt to overcome the afore-mentioned
 17 limitations of the Computed Torque Technique, a new
 18 tracking control philosophy of the invention is proposed
 19 in this section. The underlying concept in this
 20 invention is that the full dynamic model is not required
 21 in order to achieve trajectory tracking and the lack of
 22 knowledge of full dynamics can readily be compensated
 23 for by the introduction of "adaptive elements" in the
 24 control system. Specifically, the proposed tracking
 25 control system, Figure 2, is composed of two components:
 26 the nominal feedforward controller 220 and the adaptive
 27 feedback controller 250. In Figure 2, the block 235
 28 represents the manipulator plus actuators of the type
 29 generalized earlier herein. The output signals on leads
 30 240 and 245 are the actual velocity and actual position
 31 of the system as sensed in any well known manner. Three
 32 separate input terms are depicted at leads 201, 202, and
 33 203. The signals on these input leads represent,
 34 respectively, desired position (θ_r) on lead 201, desired
 35 velocity ($\dot{\theta}_r$) on lead 202, and desired acceleration ($\ddot{\theta}_r$)

1 on lead 203. The feedforward controller 220 contains
2 computation elements 205 and 210. Computation elements
3 205 and 210 take the known information that is available
4 about the manipulator/system and compute, based upon the
5 input signals at leads 201, 202, or 203 the available
6 partial information that is fed to a summing junction
7 215. The output from summing junction 215 is a signal
8 V_o , which signal is in turn fed into another signal
9 junction 230. The signal V_o from junction 215 is the
10 feedforward component of the total command signal V that
11 is developed by the invention at lead 232 into the
12 manipulator plus actuators 235. Since the feedforward
13 loop 220 is model-based, any known information about the
14 manipulators or the actuator system is input into the
15 control loop. Data on the manipulator dynamics can be
16 used for real-time control at the required sampling
17 rate. Such information can be, for instance, only the
18 gravity loading term or the manipulator full dynamics
19 excluding the payload. The feedforward controller 220
20 is model-based and it acts on the desired joint
21 trajectory $\theta_r(t)$ to produce the actuators driving
22 voltage $V_o(t)$.

23 The role of the feedback controller 250 is to
24 generate the corrective actuator voltage $V_a(t)$, based on
25 the tracking-error $e(t)$, that needs to be added to $V_o(t)$
26 to complement the feedforward controller. The feedback
27 controller 250 is composed of adaptive position and
28 velocity feedback terms and an auxiliary signal $f(t)$.
29 The feedback gains, $K_v(t)$ at element 240 and $K_p(t)$ at
30 element 242 are varied in accordance with an adaptation
31 law that is described in greater detail hereinafter.

32 Suffice it to say at this point that the error
33 terms and the desired terms for position and velocity
34 are adapted to form an adaptation component, V_a , at
35 junction 230 which is then combined with the feedforward

1 component V_0 from loop 220 in order to yield the total
 2 command signal for the control system of this invention.
 3 Thus, the feedback loop 250 employs these stated signals
 4 which are updated continuously in real time to cope
 5 with the nonlinear nature of the system and
 6 uncertainties/variations in the manipulator parameters
 7 or payload. The feedforward and feedback controllers
 8 220, 250 are now discussed separately in Sections 3.1
 9 and 3.2.

10 3.1 NOMINAL FEEDFORWARD CONTROLLER

11 Suppose that some partial knowledge about the
 12 manipulator dynamic model (13) is available in the form
 13 of "approximations" to $\{M(m, \theta), N(m, \theta, \dot{\theta})\}$ denoted by

14 $\{M_0(m_0, \theta_r), N_0(m_0, \theta_r, \dot{\theta}_r)\}$, where m_0 is an estimate of m .

16 Note that $\{M_0, N_0\}$ are functions of the reference
 17 trajectory $\theta_r(t)$ instead of the actual trajectory $\theta(t)$.
 18 The information available in M_0 and N_0 can vary widely
 19 depending on the particular situation. For instance, we
 20 can have $M_0(m_0, \theta_r) = 0$ and $N_0(m_0, \theta_r, \dot{\theta}_r) = G(m, \theta_r)$,

22 where only gravity information is available. Likewise,
 23 it is possible to have $M_0(m_0, \theta_r) = M(0, \theta_r)$ and

24 $N_0(m_0, \theta_r, \dot{\theta}_r) = N(0, \theta_r, \dot{\theta}_r)$,

25 where no information about the payload is available.
 26 Furthermore, the matrices M_0 and N_0 may have either a
 27 "centralized" or a "decentralized" structure. In the
 28 centralized case, each element of M_0 and N_0 can be a
 29 function of all joint variables. In the "decentralized"
 30 case, $[M_0]_{ii}$ and $[N_0]_{ii}$ are functions only of the i th
 31 joint variable and $[M_0]_{ij} = 0$ for all $i \neq j$.

32 The nominal feedforward controller is described by

$$34 \quad V_0(t) = M_0(m_0, \theta_r) \ddot{\theta}_r(t) + N_0(m_0, \theta_r, \dot{\theta}_r) \quad (16)$$

35

1 where V_0 is the $n \times 1$ nominal control voltage vector and
 2 the controller operates on the reference trajectory
 3 $\theta_r(t)$ instead of the actual trajectory $\theta(t)$. It is
 4 important to realize that M_0 and N_0 are based solely on
 5 the information available on the manipulator dynamics
 6 which is used in the real-time control system of this
 7 invention. The controller matrices $\{M_0, N_0\}$ can
 8 therefore be largely different from the model matrices
 9 $\{M, N\}$ due to lack of complete information, or due to
 10 computational constraints. For instance, in some cases
 11 we may wish to discard some elements of M and N in order
 12 to reduce the on-line computational burden, even if the
 13 full knowledge of manipulator dynamics is available.

14 3.2 ADAPTIVE FEEDBACK CONTROLLER

15 In contrast to the feedforward controller 220,
 16 Figure 2, the feedback controller 250 does not assume
 17 any a priori knowledge of the dynamic model or parameter
 18 values of the manipulator plus actuators 235. This
 19 controller 250 operates solely on the basis of the
 20 tracking performance of the manipulator through the
 21 tracking-error $e(t)$. The controller 250 is adaptive and
 22 its gains are adjusted continuously in real-time by
 23 simple adaptation laws to ensure closed-loop stability
 24 and desired tracking performance. The on-line
 25 adaptation compensates for the changing dynamic
 26 characteristics of the manipulator due to variations in
 27 its configuration, speed, and payload.

28 The adaptive feedback controller is described by

$$30 \quad V_a(t) = f(t) + K_p(t)e(t) + K_v(t)\dot{e}(t) \quad (17)$$

31
 32 where $V_a(t)$ is the $n \times 1$ adaptive control voltage vector,
 33 $e(t) = \theta_r(t) - \theta(t)$ is the $n \times 1$ position tracking-error
 34 vector, $f(t)$ is an $n \times 1$ auxiliary signal generated by
 35 the adaptation scheme, and $\{K_p(t), K_v(t)\}$ are the $n \times n$

adjustable PD feedback gain matrices. The feedback control law (17) can be either "centralized" or "decentralized." For the centralized case, the controller adaptation laws are obtained as I have discussed in my paper entitled A New Approach to Adaptive Control of Manipulators, ASME Journal of Dynamic Systems, Measurement, and Control, Vol. 109, No. 3, pp. 193-202, 1987. For the decentralized control case, the gains $\{K_p(t), K_v(t)\}$ are diagonal matrices and their i th diagonal elements are obtained from the adaptation laws (21) - (24) with $e(t)$ replaced by $e_i(t)$. See, for further explanation my paper H. Seraji: Decentralized Adaptive Control of Manipulators: Theory, Simulation, and Experimentation, IEEE Journal of Robotics and Automation, 1988, (to appear). The centralized case yields the controller adaptation laws as

$$f(t) = \gamma_1 \dot{r}(t) + \gamma_2 r(t) \quad (18)$$

$$\dot{K}_p(t) = \alpha_1 \frac{d}{dt}[r(t)e'(t)] + \alpha_2[r(t)e'(t)] \quad (19)$$

$$\dot{K}_v(t) = \beta_1 \frac{d}{dt}[r(t)\dot{e}(t)] + \beta_2[r(t)\dot{e}(t)] \quad (20)$$

where the prime denotes transposition, and $r(t)$ is the $n \times 1$ vector of "weighted" position-velocity error defined as

$$r(t) = W_p e(t) + W_v \dot{e}(t) \quad (21)$$

In (18)-(21), $\{\gamma_1, \alpha_1, \beta_1\}$ are zero or positive proportional adaptation gains, $\{\gamma_2, \alpha_2, \beta_2\}$ are positive integral adaptation gains, and $W_p = \text{diag}_1(w_{pi})$ and $W_v = \text{diag}_1(w_{vi})$ are constant $n \times n$ matrices which contain the position and velocity weighting factors for all joints. Integrating (18) - (20) in the time interval

1 [0,t], one obtains

2 $f(t) - f(0) = \gamma_1 [r(t) - r(0)] + \gamma_2 \int_0^t r(t) dt$

3 $K_p(t) - K_p(0) = \alpha_1 [r(t)e'(t) - r(0)e'(0)] + \alpha_2 \int_0^t r(t)e'(t) dt$

4 $K_v(t) - K_v(0) = \beta_1 [r(t)\dot{e}(t) - r(0)\dot{e}(0)] + \beta_2 \int_0^t r(t)\dot{e}(t) dt$

5
6
7
8 Since the initial values of the reference and actual
9 trajectories are the same, we have $e(0) = \dot{e}(0) = r(0) = 0$.
10 This yields the Proportional + Integral (P+I) adaptation
11 laws
12

13 $f(t) = f(0) + \gamma_1 r(t) + \gamma_2 \int_0^t r(t) dt$ (22)

14 $K_p(t) = K_p(0) + \alpha_1 r(t)e'(t) + \alpha_2 \int_0^t r(t)e'(t) dt$ (23)

15 $K_v(t) = K_v(0) + \beta_1 r(t)\dot{e}(t) + \beta_2 \int_0^t r(t)\dot{e}(t) dt$ (24)

16
17
18 It is noted that the choice of $\{W_p, W_v\}$ affects all
19 adaptation rates in (22) - (24) simultaneously; whereas
20 the adaptation rate for each term $\{f(t), K_p(t), K_v(t)\}$ can be
21 affected individually by the selection of $\{\gamma_1, \alpha_1, \beta_1\}$.
22 independently. The proportional terms in the adaptation
23 laws (22) - (24) act to increase the rate of convergence
24 of the tracking-error $e(t)$ to zero. The use of P+I
25 adaptation laws also yields increased flexibility in the
26 design, in accordance with the features of the
27 invention, by providing a larger family of adaptation
28 schemes than obtained by the conventional I adaptation
29 laws.
30

31 The physical interpretation of the auxiliary signal
32 is obtained by substituting from (21) into (22) to yield
33

34 $f(t) = f(0) + \gamma_1 [W_p e(t) + W_v \dot{e}(t)] + \gamma_2 \int_0^t [W_p e(t) + W_v \dot{e}(t)] dt$ (25)

35 $= f(0) + [\gamma_1 W_p + \gamma_2 W_v]e(t) + [\gamma_2 W_p] \int_0^t e(t) dt + [\gamma_1 W_v] \dot{e}(t)$

Hence, $f(t)$ can be generated by a PID controller with fixed gains acting on the tracking-error $e(t)$. Thus, the feedback controller (17) can be represented by the PID control law

$$V_a(t) = f(0) + K_p^*(t)e(t) + K_v^*(t)\dot{e}(t) + K_I^* \int_0^t e(t) dt \quad (26)$$

where

$$\begin{aligned} K_p^*(t) &= K_p(t) + \gamma_1 W_p + \gamma_2 W_v, & K_v^*(t) &= K_v(t) + \gamma_1 W_v, & (27) \\ & & K_I^* &= \gamma_2 W_p \end{aligned}$$

It is seen that the feedback controller 250 as defined in accordance with equation (26) is composed of three terms which are effective during the initial, intermediate, and final phases of motion:

(i) The initial auxiliary signal $f(0)$ can be chosen to overcome the stiction (static friction) and compensate for the initial gravity loading. This term improves the responses of the joint angles during the initial phase of motion.

(ii) The adaptive-gain PD term $K_p^*(t)e(t) + K_v^*(t)\dot{e}(t)$ is responsible for the tracking performance during gross motion while the manipulator model is highly nonlinear, i.e., the changes of $\theta(t)$ and $\dot{\theta}(t)$ are large. Each gain consists of a fixed part and an adaptive part. The on-line gain adaptation is necessary in order to compensate for the changing dynamics during the intermediate phase of motion.

(iii) The fixed-gain I term $K_I^* \int_0^t e(t) dt$ takes care of the fine motion in the steady-state, while the changes of $\theta(t)$ and $\dot{\theta}(t)$ are small and the manipulator model is

1 approximately linear. Thus the I term contributes
2 during the final phase of motion.

3 3.3 TOTAL CONTROL SYSTEM OF THE INVENTION

4 The total control system is obtained by combining
5 the nominal feedforward controller 220 operating in
6 accordance with equation (16) and the adaptive feedback
7 controller 250 operating in accordance with equation
8 (17) as shown in Figure 2 to yield the control law

$$9 \quad V(t) = V_o(t) + V_a(t) \quad (28)$$

$$10 \quad = [M_o(m_o, \theta_r) \ddot{\theta}_r + N_o(m_o, \theta_r, \dot{\theta}_r)] + [f(t) + K_p(t)e(t) + K_v(t)\dot{e}(t)]$$

11
12 where V is the total voltage applied at the actuators.
13 It is important to note that in this control
14 configuration, closed-loop stability is not affected by
15 the feedforward controller.

16 I shall now discuss two extreme cases:

17 Case i: UNKNOWN MANIPULATOR MODEL

18 When no a priori information is available on the
19 manipulator dynamic model, that is, $M_o = N_o = 0$, the
20 feedforward controller has no contribution, i.e. $V_o(t) =$
21 0. In this case, the control system approach reduces to
22 the adaptive feedback control law

$$23 \quad V(t) = f(t) + K_p(t)e(t) + K_v(t)\dot{e}(t) \quad (29)$$

24 which can be implemented with a high sampling rate.

25 Case ii: FULL MANIPULATOR MODEL

26
27 When the full dynamic model and accurate parameter
28 values of the manipulator, actuators and payload are
29 available for on-line control, that is $M_o = M$ and $N_o =$
30 N , the feedforward controller can generate the required
31 actuator voltage $V_o(t)$. In this case, the adaptation
32 process can be switched off and the feedback controller
33 reduces to a fixed-gain PD controller $\{K_p(0), K_v(0)\}$.
34 The control law is now given by
35

1 $V(t) = M(m, \theta_r) \ddot{\theta}_r + N(m, \theta_r, \dot{\theta}_r) + K_p(0)e(t) + K_v(0)\dot{e}(t)$ (30)
 2 which is the feedforward version of the Computed Torque
 3 Technique. See, for example, P.K.Khosla and T. Kanade:
 4 Experimental Evaluation of Nonlinear Feedback and
 5 Feedforward Control Schemes For Manipulators, Intern.
 6 Journ. of Robotics Research, Vol. 7, No. 1, pp. 18-28,
 7 1988.

8 I have concluded that there is a trade-off between
 9 the availability of a full dynamic model and the
 10 controller adaptation process. In the range of possible
 11 operation, one can go from one extreme of no model
 12 knowledge and fully adaptive controller, to the other
 13 extreme of full model knowledge and non-adaptive
 14 controller.

15 4. DIGITAL CONTROL ALGORITHM

16 In Section 3, it is assumed that the control action
 17 is generated and applied to the manipulator in
 18 continuous time. In practical implementations, however,
 19 manipulators are controlled by means of digital
 20 computers in discrete time. In other words, the
 21 computer receives the measured data (joint positions θ)
 22 and transmits the control signal (actuator voltages V)
 23 ever T_s seconds, where T_s is the sampling period. It is
 24 therefore necessary to reformulate the manipulator
 25 control problem in discrete time from the outset. In
 26 practice, however, the sampling period T_s is often
 27 sufficiently small to allow us to treat the manipulator
 28 as a continuous system and discretize the continuous
 29 control law to obtain a digital control algorithm. This
 30 approach is feasible for the invention, since the on-
 31 line computations involved for real-time control control
 32 are very small; allowing high rate sampling to be
 33 implemented.

34 In order to discretize the control law, let us
 35 consider the adaptation laws (18) - (20) for the

1 feedback controller and integrate them in the time
2 interval $[(N-1)T_s, NT_s]$ to obtain

$$3 \quad f(n) = f(N-1) + \gamma_1 [r(N) - r(N-1)] + \gamma_2 \cdot \frac{T_s}{2} [r(N) + r(N-1)]$$

$$4 \quad K_p(N) = K_p(N-1) + \alpha_1 [r(N)e'(N) - r(N-1)e'(N-1)]$$

$$5 \quad + \alpha_2 \cdot \frac{T_s}{2} [r(N)e'(N) + r(N-1)e'(N-1)]$$

$$6 \quad K_v(N) = K_v(N-1) + \beta_1 [r(N)\ddot{e}(N) - r(N-1)\ddot{e}(N-1)]$$

$$7 \quad + \beta_2 \cdot \frac{T_s}{2} [r(N)\ddot{e}(N) + r(N-1)\ddot{e}(N-1)]$$

8
9 where N and $N-1$ denote the sample instants and refer to
10 $t = NT_s$ and $t = (N-1)T_s$, $e(N) = \theta_r(N) - \theta(N)$ is the
11 discrete position error, and the integrals are evaluated
12 by the trapezoidal rule. The discrete adaptation laws
13 can be written as

$$14 \quad r(N) = W_p e(N) + W_v \dot{e}(N) \quad (31)$$

$$15 \quad f(N) = f(N-1) + \left[\gamma_2 \cdot \frac{T_s}{2} - \gamma_1 \right] r(N-1) + \left[\gamma_2 \cdot \frac{T_s}{2} + \gamma_1 \right] r(N) \quad (32)$$

$$16 \quad K_p(N) = K_p(N-1) + \left[\alpha_2 \cdot \frac{T_s}{2} - \alpha_1 \right] r(N-1)e'(N-1) \quad (33)$$

$$17 \quad + \left[\alpha_2 \cdot \frac{T_s}{2} + \alpha_1 \right] r(N)e'(N)$$

$$18 \quad K_v(N) = K_v(N-1) + \left[\beta_2 \cdot \frac{T_s}{2} - \beta_1 \right] r(N-1)\ddot{e}(N-1) \quad (34)$$

$$19 \quad + \left[\beta_2 \cdot \frac{T_s}{2} + \beta_1 \right] r(N)\ddot{e}(N)$$

20 In the above equations, we have assumed that the
21 discrete velocity error $\dot{e}(N)$ is directly available using
22 a tachometer; otherwise the velocity error must be
23 formed in software as $\dot{e}(N) = \frac{e(N) - e(N-1)}{T_s}$. Equations
24 (31) - (34) constitute the recursive algorithm for
25 updating the feed-back controller.
26
27
28
29
30
31
32
33
34
35

Let us now evaluate the number of on-line mathematical operations that need to be performed in each sampling period T_s to form the discrete feedback control law

$$V_a(N) = f(N) + K_p(N)e(N) + K_v(N)\dot{e}(N) \quad (35)$$

where $e(N)$ and $\dot{e}(N)$ are assumed to be available. For a centralized feedback controller, the total numbers of additions and multiplications in forming $V_a(N)$ are equal to $6n^2 + 3n$ and $6n^2 + 8n$, respectively, where n is the number of manipulator joints. For a decentralized feedback controller, the numbers of operations are reduced to $9n$ additions and $14n$ multiplications. The small number of mathematical operations, particularly in the decentralized case, suggests that we can implement a digital servo loop with a high sampling rate, i.e. very small T_s . This is a very important feature in digital control since slow sampling rates degrade the tracking performance of the manipulator, and may even lead to closed-loop instability.

Let us now turn to the discrete feedforward control law

$$V_o(N) = M_o[m_o, \theta_r(N)]\ddot{\theta}_r(N) + N_o[m_o, \theta_r(N), \dot{\theta}_r(N)] \quad (36)$$

where $\dot{\theta}_r(N)$ and $\ddot{\theta}_r(N)$ are directly available from the trajectory generator. Since the feedforward controller is "outside" the servo loop, it is possible to have a fast servo loop around the feedback controller, and the feedforward voltage $V_o(N)$ is then added at a slower rate. Furthermore, the feedforward control action $V_o(N)$ is computed as a function of the reference trajectory $\theta_r(N)$ only. In applications where the desired path $\theta_r(t)$ is known in advance, the values of the voltage

1 $V_o(N)$ can be computed "off-line" before motion begins
 2 and stored in a look-up table in the computer memory.
 3 At run time, this precomputed voltage history is then
 4 simply read out of the look-up table and used in the
 5 control law. Such an approach can be quite inexpensive
 6 computationally at run time, while allowing
 7 implementation of a high servo rate for feedback
 8 control.

9 The total control law in discrete time is given by
 10 $V(N) = V_o(N) + V_a(N)$
 11
$$= M_o[m_o, \theta_r(N)]\ddot{\theta}_r(N) + N_o[m_o, \theta_r(N), \dot{\theta}_r(N)] \quad (37)$$

 12 $+ f(N) + K_p(N)e(N) + K_v(N)\dot{e}(N)$
 13

14 Equations (31) - (37) constitute the digital control
 15 algorithm that is implemented for on-line computer
 16 control of robotic manipulators.

17 5. ROBUST ADAPTIVE CONTROL

18 The adaptation laws for the feedback controller as
 19 described in Section 3 are derived under the ideal
 20 conditions where unmodeled dynamics is not present and
 21 disturbances do not affect the system. In such
 22 idealistic conditions, the rate of change of a typical
 23 feedback gain $K(t)$ which acts on the signal $s(t)$ is
 24 found to be that set forth below in equation number
 25 (38). In expressing this relationship the auxiliary
 26 signal $f(t)$, is developed by setting $s(t) \equiv 1$.

27
$$\dot{K}(t) = \mu_1 \frac{d}{dt} [r(t)s'(t)] + \mu_2 [r(t)s'(t)] \quad (38)$$

 28
 29

30 where μ_1 and μ_2 are scalar adaptation gains. Extensive
 31 simulation and experimental studies suggest that too low
 32 adaptation gains result in smooth variations in $K(t)$,
 33 but poor tracking performance. On the other hand, too
 34 high adaptation gains lead to oscillatory and noisy
 35 behavior of $K(t)$, but yield perfect trajectory tracking.

(Note that for both low and high adaptation gains, the range of control voltage is more or less the same, since it is primarily dependent on the reference trajectory and manipulator dynamics). This argument suggests that large adaptation gains are necessary to maintain a high speed of controller adaptation in order to ensure rapid convergence of the tracking-error $e(t)$ to zero. In practice, the adaptation gains cannot be selected too large due to a phenomenon known as "fast adaptation instability." When the speed of adaptation, i.e. $\dot{K}(t)$, is too high, the gain $K(t)$ drifts to large values and excites the unmodeled dynamics (parasitic) of the system, which in turn leads to instability of the control system. High speed of adaptation can be either due to large adaptation gains or fast reference trajectory. Another mechanism for instability can be observed in decentralized adaptive control systems. The interconnections among subsystems can cause local controller parameters drift to large values and hence excite the parasitic and lead to instability. For instance, a high amplitude or high frequency reference trajectory of one subsystem can destabilize the local adaptive controller of another subsystem by exciting its parasitic through the interconnections.

We conclude that in an adaptive robot control system, unstable behavior can be observed with large adaptation rates or high degree of interjoint couplings. It is unfortunate that in trying to compensate for the change in the system, the adaptive controller may become sensitive to its own parameters.

I shall now discuss two possible approaches for avoiding the fast adaptation instability:

5.1 TIME-VARYING ADAPTATION GAINS

From equation (38), it is seen that the speed of adaptation $\dot{K}(t)$ depends on the magnitude of the

1 adaptation gains (μ_1, μ_2) and on the weighted tracking-
2 error $r(t)$. Simulation studies with constant adaptation
3 gain algorithms suggest that high gains lead to faster
4 convergence of the tracking-error to zero. However, in
5 the initial phase of adaptation, the weighted tracking-
6 error $r(t)$ is large (e.g. due to static friction) and
7 too high a value of adaptation gain causes instability
8 problems. As the adaptation process goes on, the term
9 $r(t)$ decreases and at this time the adaptation gain is
10 increased in order to achieve faster convergence. With
11 this motivation, the constant adaptation gains μ_1 and
12 μ_2 in (38) are replaced by positive time-varying gains
13 $\mu_1(t)$ and $\mu_2(t)$ without affecting the stability
14 analysis. The time functions $\mu_1(t)$ and $\mu_2(t)$ start with
15 small initial values when the errors are usually large
16 and, as time proceeds, build up to appropriate large
17 final values when the errors are small.

21 5.2 ROBUSTNESS VIA σ -MODIFICATION

22 The P+I adaptation laws discussed so far have no
23 provision for rejecting the destabilizing effect of
24 "noise" introduced through unmodeled dynamics or
25 disturbances. The integral term in the adaptation law
26 acts to integrate a quantity related to the noise term
27 squared. The integration of such a non-negative
28 quantity inevitably creates an undesirable drift in the
29 integral term and ultimately deteriorates the adaptive
30 system performance.

31
32
33 Ioannou and Kokotovic (Instability Analysis and
34 Improvement of Robustness of Adaptive Control,
35 Automatica, Vol. 20, No. 5, pp. 583-594, 1984; Robust

Redesign of Adaptive Control, IEEE Trans. Aut. Control, Vol. AC-29, No. 3, pp. 202-211, 1984) suggest " σ -modification" to the adaptation law in order to eliminate the drift in the integral term and thus counteract instability. The basic idea is to modify the adaptation law (38) by adding a term $-\sigma K(t)$ which removes its purely integral action, that is, instead of (38) we use the σ -modified law

$$\dot{K}(t) = -\sigma K(t) + \mu_1 \frac{d}{dt} [r(t)s'(t)] + \mu_2 [r(t)s'(t)] \quad (39)$$

where σ is a positive scalar design parameter. The size of σ reflects our lack of knowledge about the unmodeled dynamics and disturbances. In equation (39), the leakage or decay term $-\sigma K(t)$ acts to dissipate the integral buildup, and eliminate the drift problem which excites the parasitic and leads to instability. The price paid for the attained robustness is that the tracking-error $\|r(t)\|$ now converges to a bounded non-zero residual set, and hence perfect trajectory tracking is no longer achieved in theory. The size of this residual set depends on the value of σ , but can often be made sufficiently small so that performance degradation is acceptable in practice. The drawback of the σ -modified adaptation law, however, is that in the absence of unmodeled dynamics and disturbances, we can no longer guarantee that $\lim_{t \rightarrow \infty} \|r(t)\| = 0$, unless $\sigma = 0$.

The Proportional + Integral + Sigma (P + I + σ) adaptation laws for the feedback controller in continuous time are now given by

$$f(t) = f(0) + \gamma_1 r(t) + \gamma_2 \int_0^t r(t) dt - \sigma_1 \int_0^t f(t) dt \quad (40)$$

$$K_p(t) = K_p(0) + \alpha_1 r(t)e'(t) + \alpha_2 \int_0^t r(t)e'(t) dt - \sigma_2 \int_0^t K_p(t) dt \quad (41)$$

$$K_v(t) = K_v(0) + \beta_1 r(t) \dot{e}'(t) + \beta_2 \int_0^t r(t) \dot{e}'(t) dt - \sigma_3 \int_0^t K_v(t) dt \quad (42)$$

where $\{\sigma_1, \sigma_2, \sigma_3\}$ are positive scalar design parameters.

For digital control implementation with sampling period T_s , (40) - (42) yield the recursive adaptation laws

$$f(N) = \left[\frac{1 - \sigma_1 \frac{T_s}{2}}{1 + \sigma_1 \frac{T_s}{2}} \right] f(N-1) + \left[\frac{\gamma_2 \frac{T_s}{2} - \gamma_1}{1 + \sigma_1 \frac{T_s}{2}} \right] r(N-1) + \left[\frac{\gamma_2 \frac{T_s}{2} \gamma_1}{1 + \sigma_1 \frac{T_s}{2}} \right] r(N)$$

$$K_p(N) = \left[\frac{1 - \sigma_2 \frac{T_s}{2}}{1 + \sigma_2 \frac{T_s}{2}} \right] K_p(N-1) + \left[\frac{\alpha_2 \frac{T_s}{2} - \alpha_1}{1 + \sigma_2 \frac{T_s}{2}} \right] r(N-1) e'(N-1) \quad (43)$$

$$+ \left[\frac{\alpha_2 \frac{T_s}{2} - \alpha_1}{1 + \sigma_2 \frac{T_s}{2}} \right] r(N) e'(N) \quad (44)$$

$$K_v(N) = \left[\frac{1 - \sigma_3 \frac{T_s}{2}}{1 + \sigma_3 \frac{T_s}{2}} \right] K_v(N-1) + \left[\frac{\beta_2 \frac{T_s}{2} - \beta_1}{1 + \sigma_3 \frac{T_s}{2}} \right] r(N-1) \dot{e}'(N-1) \quad (45)$$

$$+ \left[\frac{\beta_2 \frac{T_s}{2} - \beta_1}{1 + \sigma_3 \frac{T_s}{2}} \right] r(N) \dot{e}'(N)$$

In conclusion, the use of σ -modification is essential in obtaining sufficient conditions for boundedness in the presence of parasitic. However, in the absence of parasitic, σ causes a tracking-error of $O(\sqrt{\sigma})$ to remain. Therefore, there is a trade-off between boundedness of all signals in the presence of parasitic and loss of exact convergence of the tracking-error to zero in the absence of parasitic. In other words, we have sacrificed the performance in an idealistic situation in order to achieve robustness in realistic situations which are more likely to occur in practical applications.

6. SIMULATION RESULTS

1 The tracking control scheme developed in Section 3
2 has been applied to a two-link manipulator for
3 illustration of the benefits of the invention.

4 Consider the planar two-link manipulator in a
5 vertical plane shown in Figure 3, with the end-effector
6 carrying a payload of mass m . The robot links are
7 assumed to be driven directly (without gears) by two
8 servomotors with negligible dynamics. Hence the arm is
9 "direct drive" and we can treat the joint torques as the
10 driving signals. The dynamic equation of motion which

11 relates the joint torque vector $T = \begin{pmatrix} T_1 \\ T_2 \end{pmatrix}$ to the joint

12 angle vector $\theta = \begin{pmatrix} \theta_1 \\ \theta_2 \end{pmatrix}$ is given by H. Seraji, A New
13

14 Approach to Adaptive Control of Manipulators, supra, and
15 H. Seraji, M. Jamshidi, Y. T. Kin, and M. Shahinpoor,
16 Linear Multivariable Control of Two-Link Robots, Journal
17 of Robotic Systems, Vol. 3, No. 4, pp. 349 - 365, 1986.
18
19
20

$$21 \quad T = M(\theta)\ddot{\theta} + N(\theta, \dot{\theta}) + G(\theta) + H(\dot{\theta}) + mJ'(\theta) [J(\theta)\ddot{\theta} + \dot{J}(\theta, \dot{\theta})\dot{\theta} + g] \quad (46)$$

22 where the above terms are:
23

$$24 \quad M(\theta) = \begin{pmatrix} \alpha_1 + \alpha_2 \cos \theta_2 & \alpha_2 + \frac{\alpha_2^2}{2} \cos \theta_2 \\ \alpha_2 + \frac{\alpha_2^2}{2} \cos \theta_2 & \alpha_2 \end{pmatrix}; \quad N(\theta, \dot{\theta}) = \begin{pmatrix} -(\alpha_2 \sin \theta_2)(\dot{\theta}_1 \dot{\theta}_2 + \frac{\dot{\theta}_2^2}{2}) \\ (\alpha_2 \sin \theta_2) \frac{\dot{\theta}_1^2}{2} \end{pmatrix}$$

$$25 \quad G(\theta) = \begin{pmatrix} \alpha_4 \cos \theta_1 + \alpha_5 \cos(\theta_1 + \theta_2) \\ \alpha_5 \cos(\theta_1 + \theta_2) \end{pmatrix}; \quad H(\dot{\theta}) = \begin{pmatrix} v_1 \dot{\theta}_1 + v_2 \operatorname{sgn}(\dot{\theta}_1) \\ v_3 \dot{\theta}_2 + v_4 \operatorname{sgn}(\dot{\theta}_2) \end{pmatrix}$$

$$J(\theta) = \begin{pmatrix} -l_1 \sin \theta_1 - l_2 \sin (\theta_1 + \theta_2) & -l_2 \sin (\theta_1 + \theta_2) \\ l_1 \cos \theta_1 + l_2 \cos (\theta_1 + \theta_2) & l_2 \cos (\theta_1 + \theta_2) \end{pmatrix} ; \quad g \begin{pmatrix} 0 \\ +9.81 \end{pmatrix}$$

In the above expressions, $\alpha_1, \dots, \alpha_5$ are constant parameters obtained from the masses (m_1, m_2) and the lengths (l_1, l_2) of the robot links, and (V_1, V_3) and (V_2, V_4) are coefficients of viscous and Coloumb frictions respectively. For the particular robot under study, the numerical values of the link parameters are $m_1 = 15.91\text{Kg}$; $m_2 = 11.36\text{Kg}$; $l_1 = l_2 = 0.432\text{m}$ so that they represent links 2 and 3 of the Unimation PUMA 560 robot. This yields the following numerical values for the model parameters (H. Seraji, M. Jamshidi, Y. T. Kim, and M. Shaninpoor, *supra*)

$$\alpha_1 = 3.82 \quad ; \quad \alpha_2 = 2.12 \quad ; \quad \alpha_3 = 0.71$$

$$\alpha_4 = 81.82 \quad ; \quad \alpha_5 = 24.06$$

The friction coefficients are chosen as $V_1 = V_3 = 1.0\text{Nt.m/rad.sec}^{-1}$ and $V_2 = V_4 = 0.5\text{NT.m}$ and the payload mass is initially $m = 10.0\text{Kg}$.

The joint angles $\theta_1(t)$ and $\theta_2(t)$ are required to track the cycloidal reference trajectories

$$\theta_{r1}(t) = -\frac{\pi}{2} + \frac{1}{4} \left[\frac{2\pi t}{3} - \sin \frac{2\pi t}{3} \right] \quad 0 \leq t \leq 3$$

$$= 0 \quad 3 < t$$

$$\theta_{r2}(t) = \frac{1}{4} \left[\frac{2\pi t}{3} - \sin \frac{2\pi t}{3} \right] \quad 0 \leq t \leq 3$$

$$= \frac{\pi}{2} \quad 3 < t$$

so that the robot configuration changes smoothly from the initial posture $\{\theta_1 = -\frac{\pi}{2}, \theta_2 = 0\}$ to the final posture $\{\theta_1 = 0, \theta_2 = +\frac{\pi}{2}\}$ in three seconds. The joint angles are controlled by the feedforward and/or feedback tracking control scheme

$$T_1(t) = [M_{11}(\theta_r) \ddot{\theta}_{r1} + M_{12}(\theta_r) \ddot{\theta}_{r2} + G_1(\theta_r)]$$

$$+ [f_1(t) + k_{p1}(t)e_1(t) + k_{v1}(t)\dot{e}_1(t)] \quad (48)$$

$$T_2(t) = [M_{21}(\theta_r)\ddot{\theta}_{r1} + M_{22}(\theta_r)\ddot{\theta}_{r2} + G_2(\theta_r)] \\ + [f_2(t) + k_{p2}(t)e_2(t) + k_{v2}(t)\dot{e}_2(t)]$$

where M and G are defined in (46). It is seen that each tracking control law is composed of feedforward and feedback components. The feedforward component has a centralized structure and is based on the manipulator dynamic model (46). It is a function of the reference trajectory $\theta_r(t)$ and contains the inertial acceleration term $M(\theta_r)\ddot{\theta}_r$ and the gravity loading term $G(\theta_r)$ of the arm itself, without the payload (i.e., $m = 0$). The Coriolis and centrifugal term $N(\theta, \dot{\theta})$, the frictional term $H(\dot{\theta})$, and the payload term are assumed to be unavailable for on-line control and are not incorporated in the feedforward controller. The feedback controller has a decentralized structure and is composed of the auxiliary signal $f(t)$, the position feedback term $k_p(t)e(t)$, and the velocity feedback term $k_v(t)\dot{e}(t)$ where $e(t) = \theta_r(t) - \theta(t)$ is the position tracking-error in radians. The feedback terms are updated as (In this example, the σ -modification was not necessary, and hence $\sigma_1 = \sigma_2 = \sigma_3 = 0$).

$$f_1(t) = f_1(0) + \gamma_1 r_1(t) + \gamma_2 \int_0^t r_1(t) dt - \sigma_1 \int_0^t f_1(t) dt = \int_0^t r_1(t) dt \quad (49)$$

$$k_{p1}(t) = k_{p1}(0) + \alpha_1 r_1(t)e_1(t) + \alpha_2 \int_0^t r_1(t)e_1(t) dt - \sigma_2 \int_0^t k_{p1}(t) dt \\ = r_1(t)e_1(t) + 10 \int_0^t r_1(t)e_1(t) dt \quad (50)$$

$$k_{v1}(t) = k_{v1}(0) + \beta_1 r_1(t)\dot{e}_1(t) + \beta_2 \int_0^t r_1(t)\dot{e}_1(t) dt - \sigma_3 \int_0^t k_{v1}(t) dt \\ = r_1(t)e_1(t) + 10 \int_0^t r_1(t)e_1(t) dt \quad (51)$$

$$r_1(t) = w_{pi} e_1(t) + w_{vi} \dot{e}_1(t) = 3000e_1(t) + 1500\dot{e}_1(t) \quad (52)$$

Note that the initial values of the auxiliary signal and the feedback gains are all chosen arbitrarily as zero. (The numerical values of w_p and w_v in (52) are large since the unit of angle in the control program is "radian." A simple trapezoidal integration rule is used to compute the integrals in the adaptation laws (49) - (51) with $dt = 1$ millisecond.

To evaluate the performance of the proposed control scheme, the nonlinear dynamic model of the manipulator-plus-payload (46) and the tracking control scheme (48) are simulated on a DEC-VAX 11/750 computer with the sampling period of 1 millisecond. In order to illustrate the effectiveness of the proposed control scheme to compensate for sudden gross variation in the payload mass, the mass is suddenly decreased from $m = 10.0$ Kg to zero at $t = 1.5$ seconds (i.e. the payload is dropped) while the manipulator is in motion under the control system operating in accordance with equation (48). The results of the computer simulation are shown in Figure 4(i) - (ii) and indicate that the joint angles $\theta_1(t)$ and $\theta_2(t)$ track their corresponding reference trajectories $\theta_{r1}(t)$ and $\theta_{r2}(t)$ vary closely throughout the motion, despite the sudden payload variation. Figures 5(i) - (ii) and 6(i) - (ii) show the responses of the tracking-errors $e_1(t)$ and $e_2(t)$ and the control torques $T_1(t)$ and $T_2(t)$, and indicate a sudden jump at $t = 1.5$ due to payload change. To show the feedback adaptation process, time variations of the auxiliary signal $f_1(t)$, the position gain $k_{pi}(t)$, and the velocity gain $k_{vi}(t)$ are shown in Figures 7(i) - (iii). It is seen that the feedback terms have adapted rapidly on-line to cope with the sudden payload mass change. The results demonstrate that the invention does not require

1 knowledge of the payload mass m and can adapt itself
2 rapidly to cope with unpredictable gross variations in m
3 and sustain a good tracking performance.

4 7. EXPERIMENTAL RESULTS

5 In this section, the tracking control system
6 described in Section 3.2 is applied to a PUMA industrial
7 robot for test and evaluation purposes.

8 The testbed facility at the JPL Robotics Research
9 Laboratory consists of a Unimation PUMA 560 robot and
10 controller, and a DEC MicroVAX II computer, as shown in
11 the functional diagram of Figure 8. The MicroVAX II
12 hosts the RCCL (Robot Control "C" Library) software,
13 which was originally developed at Purdue University (V .
14 Hayward and R. Paul, Introduction to RCCL: A Robot
15 Control 'C' Library, Proc. IEEE Intern. Conf. on
16 Robotics, pp. 293 - 297, Atlanta, 1984, and subsequently
17 modified and implemented at JPL. During the operation
18 of the arm, a hardware clock constantly interrupts the
19 I/O program resident in the Unimation controller at a
20 preselected sampling period T_s , which can be chosen as
21 7, 14, 28 or 54 milliseconds. At every interrupt, the
22 I/O program gathers information about the state of the
23 arm (such as joint encoder readings), and interrupts the
24 control program in the MicroVAX II to transmit this
25 data. The I/O program then waits for the control
26 program to issue a new set of control signals, and then
27 dispatches these signals to the appropriate joint
28 motors. Therefore, the MICROVAX II acts as a digital
29 controller for the PUMA arm and the Unimation controller
30 is effectively by-passed and is utilized merely as an
31 I/O device to interface the MicroVAX II to the joint
32 motors.

33 To test and evaluate the control system described in
34 Section 3, the tracking controller is implemented on the
35 waist joint θ_1 of the PUMA arm, while the other joints

are held steady using the Unimation controller. The waist control law is coded within the RCCL environment on the MicroVAX II computer. It is assumed that the dynamic model and parameter values of the arm are not available, and hence the feedforward controller is eliminated. The control torque for the waist joint at each sampling instant N is obtained from the adaptive PID feedback control law

$$T(N) = f(N) + k_p(N)e(N) + k_v(N)\dot{e}(N) \quad (53)$$

where $e(N) = \theta_{r_1}(N) - \theta_1(N)$ is the waist position error, $\dot{e}(N) = \frac{e(N) - e(N-1)}{T_s}$ is the waist velocity error formed in the software, and $\theta_{r_1}(t)$ is the reference trajectory for the waist joint. The feedback terms are generated by the following simple recursive adaptation laws (In the experiment, it was not necessary to use σ -modification and hence we set $\sigma=0$).

$$r(N) = 30e(N) + 20\dot{e}(N) \quad (54)$$

$$f(N) = f(N-1) + 0.175[r(N) + r(N-1)] \quad (55)$$

$$k_p(N) = k_p(N-1) + 0.35[r(N)e(N) + r(N-1)e(N-1)] \quad (56)$$

$$k_v(N) = k_v(N-1) + 2.8[r(N)\dot{e}(N) + r(N-1)\dot{e}(N-1)] \quad (57)$$

where the adaptation gains are found after a few trial-and-errors. The sampling period is chosen as the smallest possible value $T_s = 7$ milliseconds (i.e. sampling $f_s = 144\text{Hz}$), since the on-line computations involved in the control law (53) are a few simple arithmetic operations. No information about the PUMA dynamics is used for implementation of the control system, and hence the controller terms are initially zero; i.e. $f(0) = k_p(0) = k_v(0) = 0$.

The PUMA arm is initially at the "zero" position with the upper-arm horizontal and the forearm vertical, forming a right-angle configuration. The waist joint

1 angle $\theta_1(t)$ is commanded to change from the initial
 2 position $\theta_1=0$ to the goal position $\theta_1=\frac{\pi}{2}$ in 2
 3 seconds. The reference trajectory $\theta_{r1}(t)$ is synthesized
 4 by the cycloidal trajectory generator in RCCL as

$$\begin{aligned} 6 \quad \theta_{r1}(t) &= \frac{1}{4} [\pi t - \sin \pi t] & 0 \leq t \leq 2 \\ 7 \quad &= \frac{\pi}{2} & 2 < t \end{aligned}$$

9 While the arm is in motion, the reading of the
 10 waist joint encoder at each sampling instant is recorded
 11 directly from the arm, converted into degrees and stored
 12 in a data file. The values of the auxiliary signal and
 13 feedback gains are also recorded at each sampling and
 14 kept in the same data file. Figure 9(i) shows the
 15 desired and actual trajectories of the waist joint angle
 16 and the tracking-error is shown in Figure 9(ii). It is
 17 seen that the joint angle $\theta_1(t)$ tracks the reference
 18 trajectory $\theta_{r1}(t)$ very closely, and the peak value of the
 19 tracking-error $e(t)$ is 1.40° . The initial lag in the
 20 θ_1 response is due to the large stiction (static
 21 friction) present in the waist joint.

22 Figures 10(i)-(ii) show the tracking performance of
 23 the waist joint for the same motion using the Unimation
 24 controller, which is operating with the sampling period
 25 of 1 millisecond $f_s=1\text{KH}_z$. It is seen that the peak
 26 joint tracking-error in Figure 10(ii) is 5.36° , which
 27 produces 4 centimeters peak position error at the end-
 28 effector. By comparing Figures 9(ii) and 10(ii), it is
 29 evident that the tracking performance of the adaptive
 30 controller is noticeably superior to that of the
 31 Unimation controller, despite the fact that the
 32 Unimation control loop is 7 times faster than the
 33 adaptive control loop. The variations of the auxiliary
 34 signal $f(t)$, the feedback gains $k_p(t)$ and $k_v(t)$, and the
 35 control torque $T(t)$ are also shown in Figures 11(i)-

(iv). It is seen that $f(t)$, $k_p(t)$, $k_v(t)$, and $T(t)$ all start from the initial values of zero and change with time.

I shall now discuss a test relating to the tracking performance of the adaptive controller in a different situation. Suppose that the configuration of the arm is changed smoothly from the initial zero posture to the final vertical posture while the waist joint is in motion. This effectively imposes a dynamic inertial load on the waist motor, as well as introducing torque disturbances in the waist control loop due to inter-joint couplings. We now specify a different desired trajectory for the waist angle whereby θ_1 is commanded to change from 0 to $\frac{\pi}{3}$ in three seconds while tracking a cycloidal trajectory. Using the same adaptive control law (53), the actual recording from the waist joint and the desired trajectory are shown in Figure 12(i) and the tracking-error is plotted in Figure 12(ii). It is seen that the actual trajectory tracks the new desired trajectory very closely, despite the dynamic loading on the waist joint and the inter-joint coupling disturbances. The experimental results demonstrate that the invention's control system is not sensitive to the arm configuration, torque disturbances, or the desired trajectory.

The following observations are made from further experiments on the PUMA robot:

1. Using the Unimation controller, the tracking-error increases for fast motion under heavy payload.

1 For instance, when the arm is fully extended
2 horizontally carrying a five pound payload and the waist
3 joint is moved by 90° in 1.2 seconds, the peak joint
4 tracking-error is about 9° . When transformed to the end-
5 effector, this gives the peak tip error of 16
6 centimeters.
7

8 2. The rate of sampling, T_s , has a central role
9 in the performance of the proposed control scheme. In
10 the adaptive feedback controller, the sampling rate
11 determines the rate at which the feedback gains and the
12 auxiliary signal are updated. Faster sampling rate
13 (smaller T_s) allows higher adaptation rates to be used,
14 which in turn leads to a better tracking performance.
15 When the sampling rate is slow (large T_s), the tracking
16 performance is degraded, and the use of high adaptation
17 gains may lead to closed-loop instability. For
18 instance, for $T_s = 14$ msec, the adaptation gains in (54)-
19 (57) must be reduced to maintain stability, and this
20 degrades the tracking performance. In general, when T_s
21 is large, the effects of sampling and discretization are
22 more pronounced and the control system performance is
23 degraded. Therefore, in practical implementation, it is
24 highly desirable to increase the sampling rate as much
25 as possible by optimizing the real-time control program
26 or using a multi-processor concurrent computing system.
27 In the present experimental setup, for any sampling
28 period T_s , about three msec is taken up by the
29 communication between the Micro VAX II and the Unimation
30 controller; hence for $T_s = 7$ msec only four msec is
31 available for control law computations.
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1 3. The feedback adaptation gains in (54)-(57)
2 should not be chosen unnecessarily high, since too high
3 gains can lead to instability while producing negligible
4 improvement in the tracking performance (e.g., an
5 acceptable peak error of 1° may decrease to 0.1°). For
6 instance, for the adaptation gains given in the above
7 experiment, motion of θ_1 by 90° in 1.2 seconds leads to
8 instability. In this case, it is necessary to decrease
9 the adaptation gains or to introduce σ -modification in
10 order to ensure stability. Therefore, in general, the
11 adaptation gains must be chosen to yield an acceptable
12 tracking performance for the fastest trajectory in the
13 experiment, i.e. "the worst case design".

16 4. For very slow motions of the waist joint
17 (e.g., average speed of $2^\circ/\text{sec}$), the friction present in
18 the waist joint has a dominating effect and therefore
19 the implemented control scheme has a poor performance.
20 This is due to the fact that in this case, the control
21 torque T_c is comparable in magnitude to the stiction T_s
22 of the joint, and hence the net torque $T_c - T_s$ applied to
23 the joint is not sufficiently large. Therefore, for
24 slow motions, it is necessary to introduce a feedforward
25 controller or a friction compensation in order to
26 counteract the effect of stiction. The situation is
27 improved by increasing the sampling rate.

30 8. CONCLUSIONS

31 A new and simple robust control system for accurate
32 trajectory tracking of robotic manipulators has been
33 described. The control system takes full advantage of
34 any known part of the manipulator dynamics in the
35

1 feedforward controller. The adaptive feedback
2 controller then compensates for any unknown dynamics and
3 uncertainties/variations in the manipulator/payload
4 parameters.
5

6 From the tracking point of view, it is desirable to
7 set the feedback adaptation rates as high as possible so
8 that the feedback controller can respond rapidly to
9 variations in the manipulator dynamics or sudden changes
10 in the payload. High rate adaptation, however, can
11 cause instability through the excitation of unmodeled
12 dynamics. The instability is counteracted in the paper
13 by the addition of decay terms to the integral
14 adaptation laws to yield an adaptive controller which is
15 robust in the presence of unmodeled dynamics and
16 disturbances.
17

18 The feedback adaptation laws in Section 3 are
19 derived under the assumption that the robot model is
20 "slowly time-varying" in comparison with the controller
21 terms. In theory, this assumption is necessary in order
22 to derive simple adaptation laws which do not contain
23 any terms from the robot model. In practice, the
24 simulation and experimental studies of Sections 5 and 6
25 justify the assumption, even under gross abrupt change
26 in the payload. This is due to the robust nature of
27 adaptive control schemes, which is discussed briefly in
28 H. Seraji, A New Approach To Adaptive Control of
29 Manipulators, supra. Nevertheless, further simulations
30 and experiments need to be performed using direct-drive
31 arms in fast motions to test the practical limitations
32 of the simplifying assumption of slow time variation.
33
34
35

1 Simulation results for a two-link robot and
2 experimental results of a PUMA industrial robot validate
3 the capability of the invention's control system in
4 accurate trajectory tracking with partial or no
5 information on the manipulator dynamics.
6

7 Finally, the control features presented herein
8 can readily be extended to the direct control of end-
9 effector position and orientation in Cartesian space.
10 In this formulation, the controllers operate on
11 Cartesian variables and the end-effector control forces
12 are then transformed to joint torques using the Jacobean
13 matrix (H. Seraji, An Approach To Multivariable Control
14 Of Manipulators, ASME Journ. Dynamic Systems,
15 Measurement and Control, Vol. 109, No. 2, pp. 146 - 154,
16 1987 and H. Seraji, Direct Adaptive Control Of
17 Manipulators In Cartesian Space, Journal of Robotic
18 Systems, Vol. 4, No. 1, pp. 157 - 178, 1987.
19
20

21 The above description presents the best mode
22 contemplated in carrying out my invention. My invention
23 is, however, susceptible to modifications and alternate
24 constructions from the embodiments shown in the drawings
25 and described above. Consequently, it is not the
26 intention to limit the invention to the particular
27 embodiments disclosed. On the contrary, the invention
28 is intended and shall cover all modifications, sizes and
29 alternate constructions falling within the spirit and
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1 scope of the invention, as expressed in the appended
2 claims when read in light of the description and
3 drawing.
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ROBUST HIGH-PERFORMANCE CONTROL FOR ROBOTIC
MANIPULATORS

ABSTRACT OF THE DISCLOSURE

Model-based and performance-based control techniques are combined for an electrical robotic control system. Thus, two distinct and separate design philosophies have been merged into a single control system having a control law formulation including two distinct and separate components, each of which yields a respective signal component that is combined into a total command signal for the system. Those two separate system components include a feedforward controller and a feedback controller. The feedforward controller is model-based and contains any known part of the manipulator dynamics that can be used for on-line control to produce a nominal feedforward component of the system's control signal. The feedback controller is performance-based and consists of a simple adaptive PID controller which generates an adaptive control signal to complement the nominal feedforward signal.

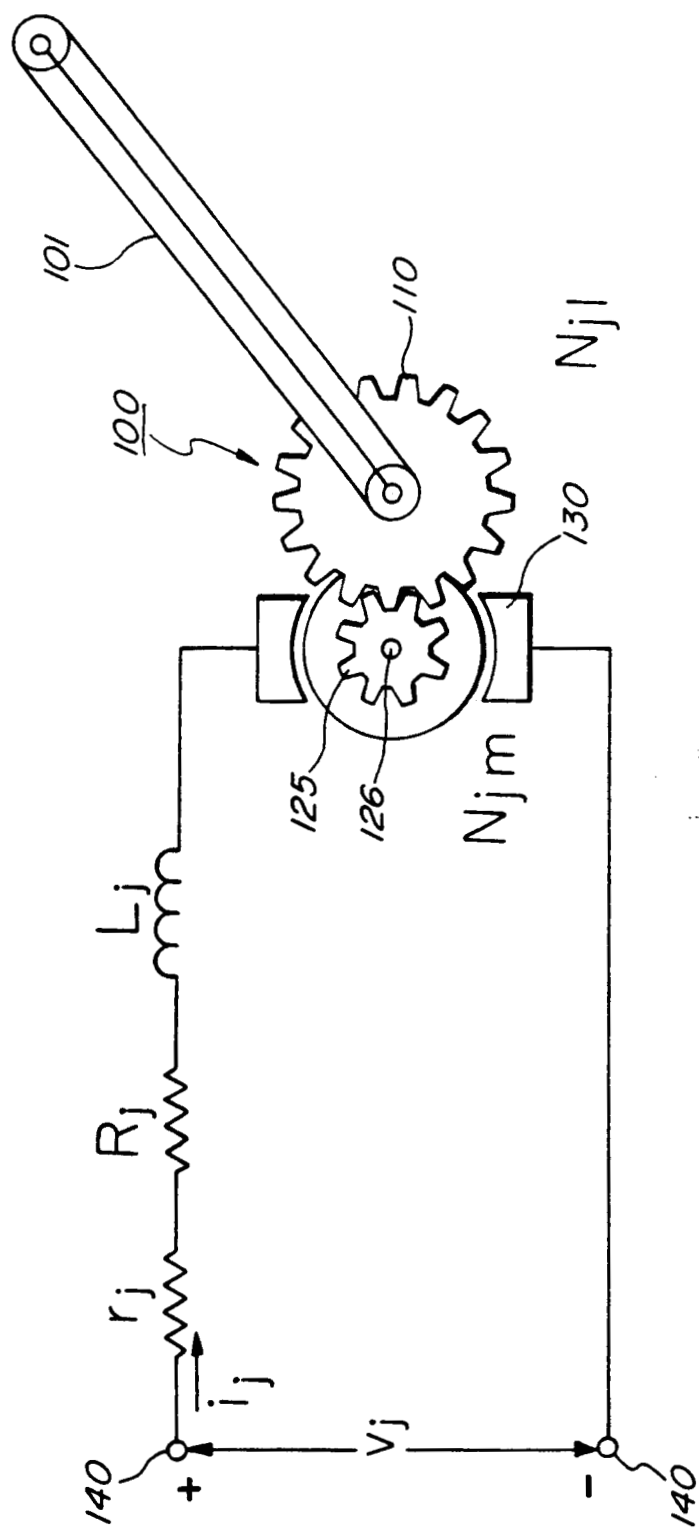


FIG. 1

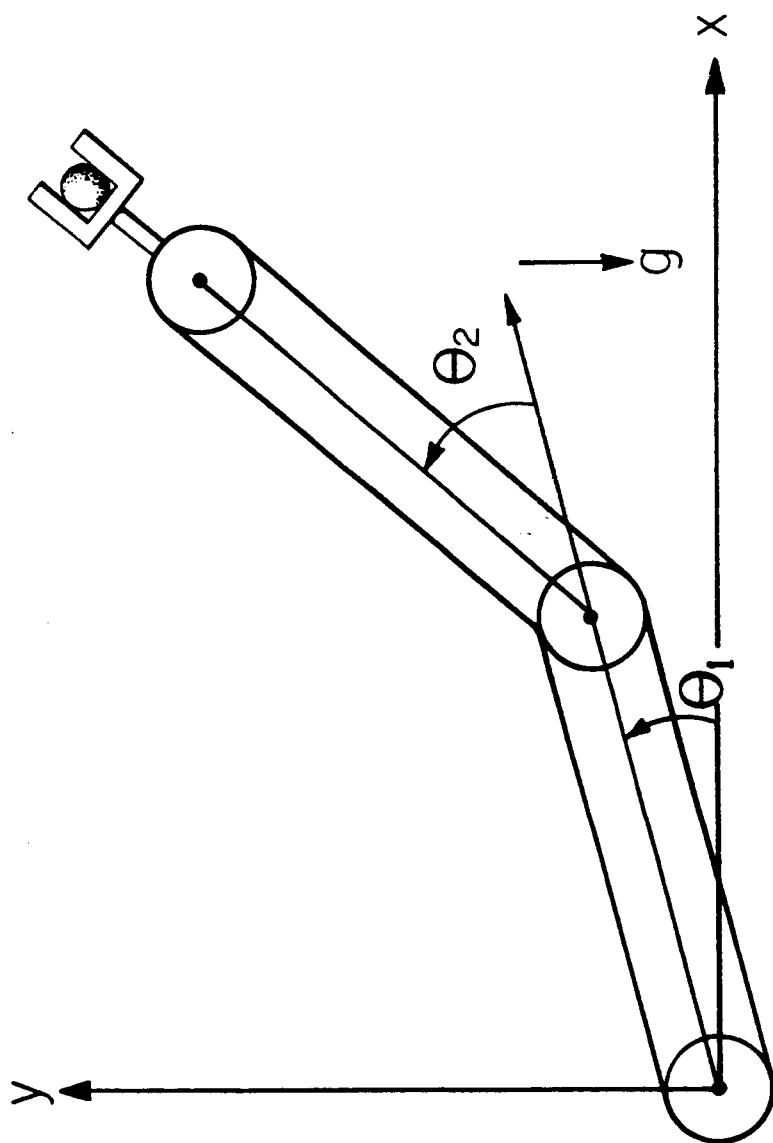


FIG. 3

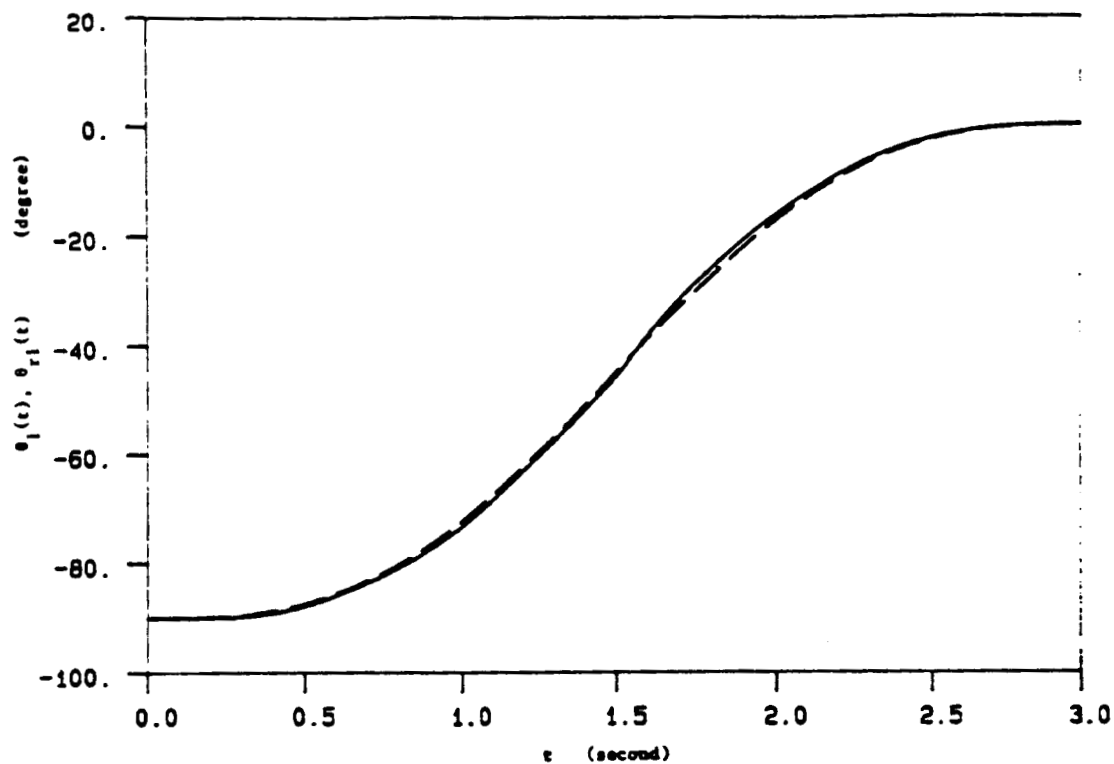


Figure 4(i). Desired [dashed] and Actual [solid] Trajectories of the Joint Angle $\theta_1(t)$

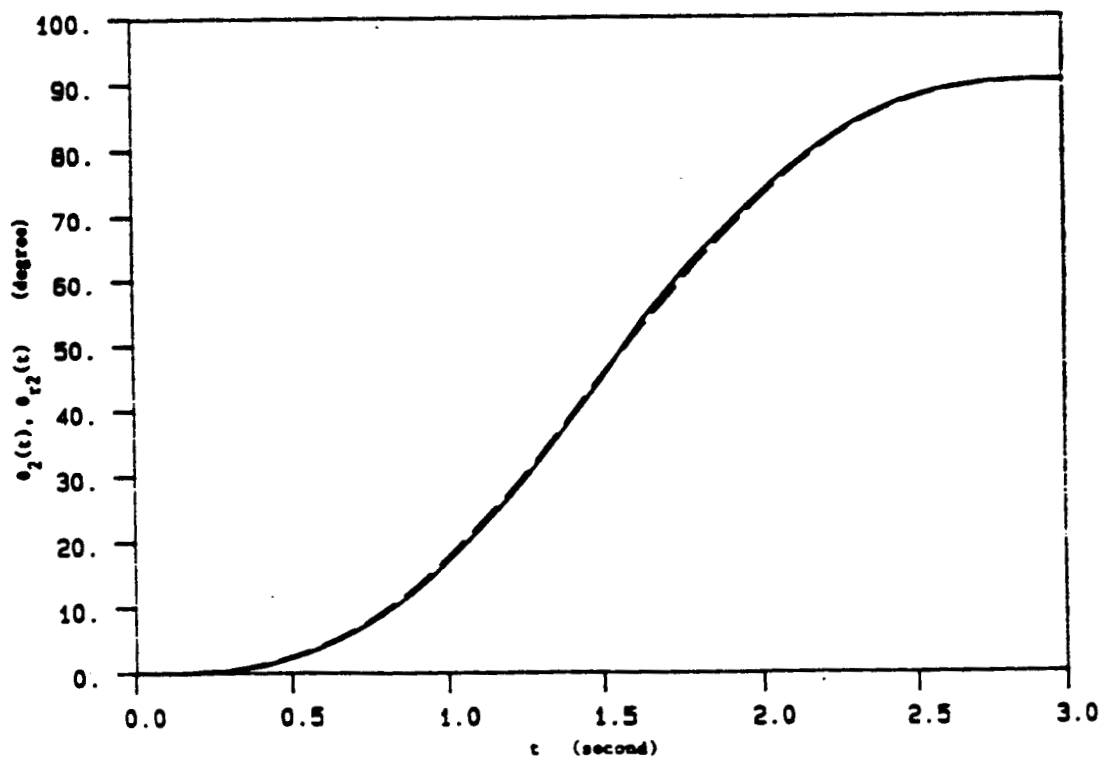


Figure 4(ii). Desired [dashed] and Actual [solid] Trajectories of the Joint Angle $\theta_2(t)$

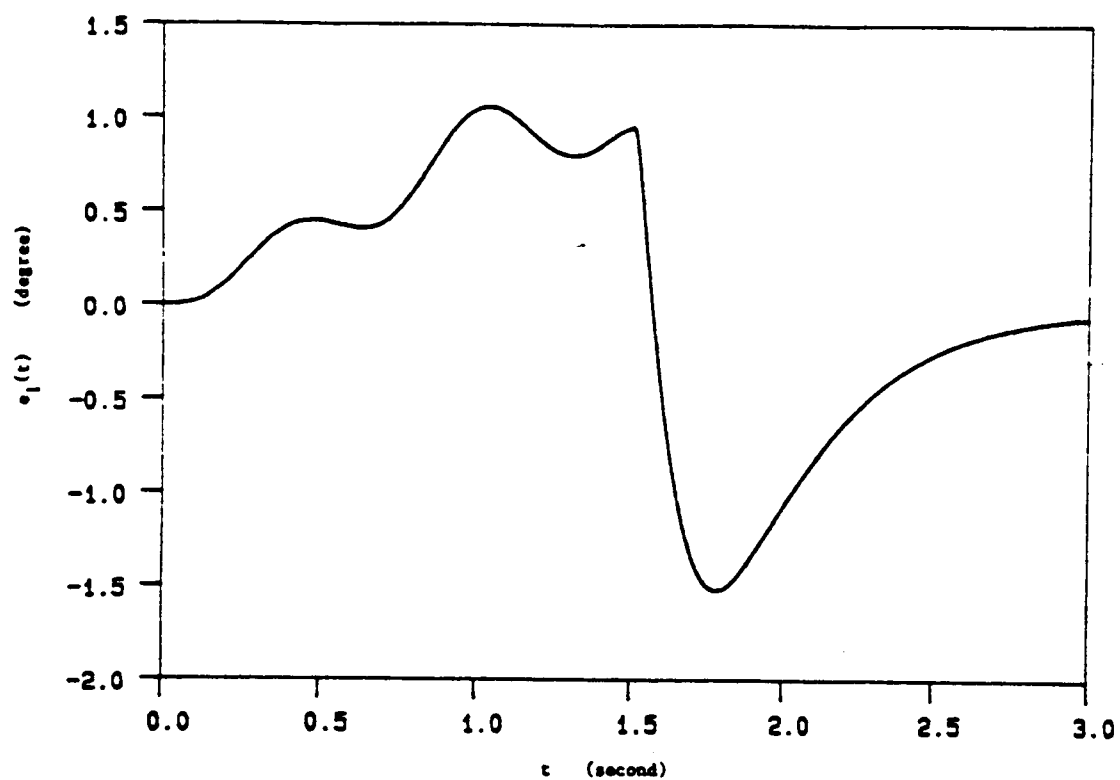


Figure 5(i). Variation of the Tracking - Error $e_1(t)$

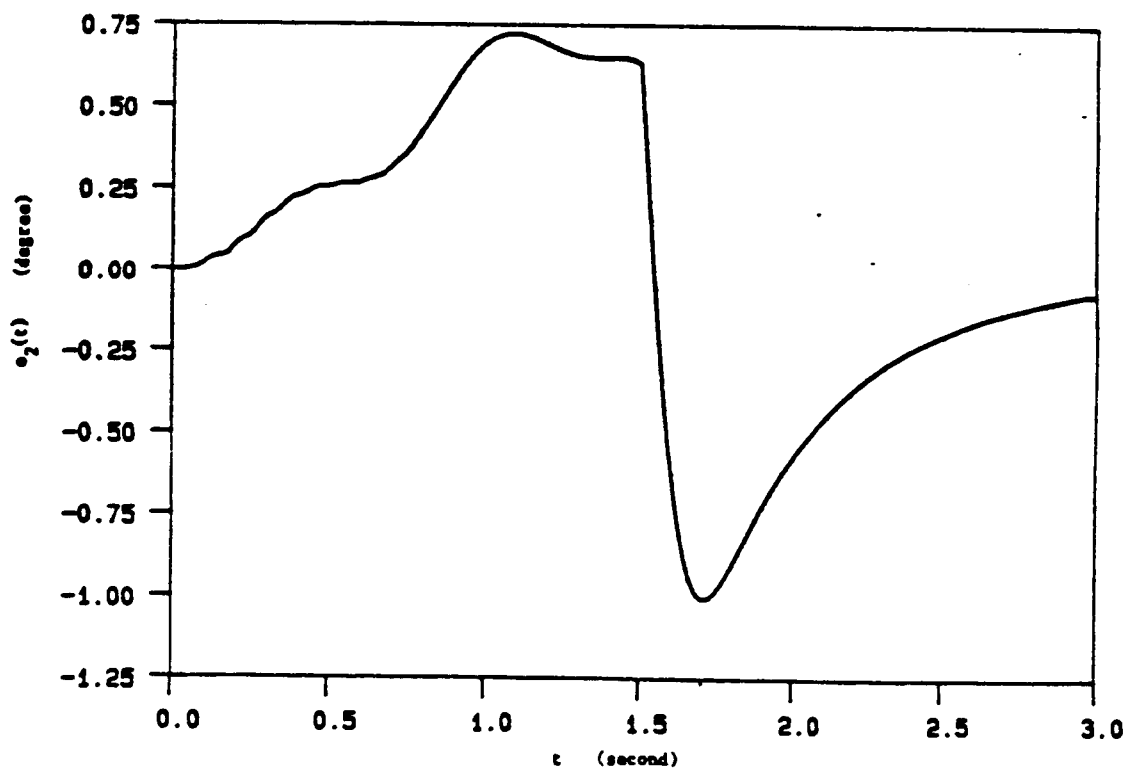


Figure 5(ii). Variation of the Tracking - Error $e_2(t)$

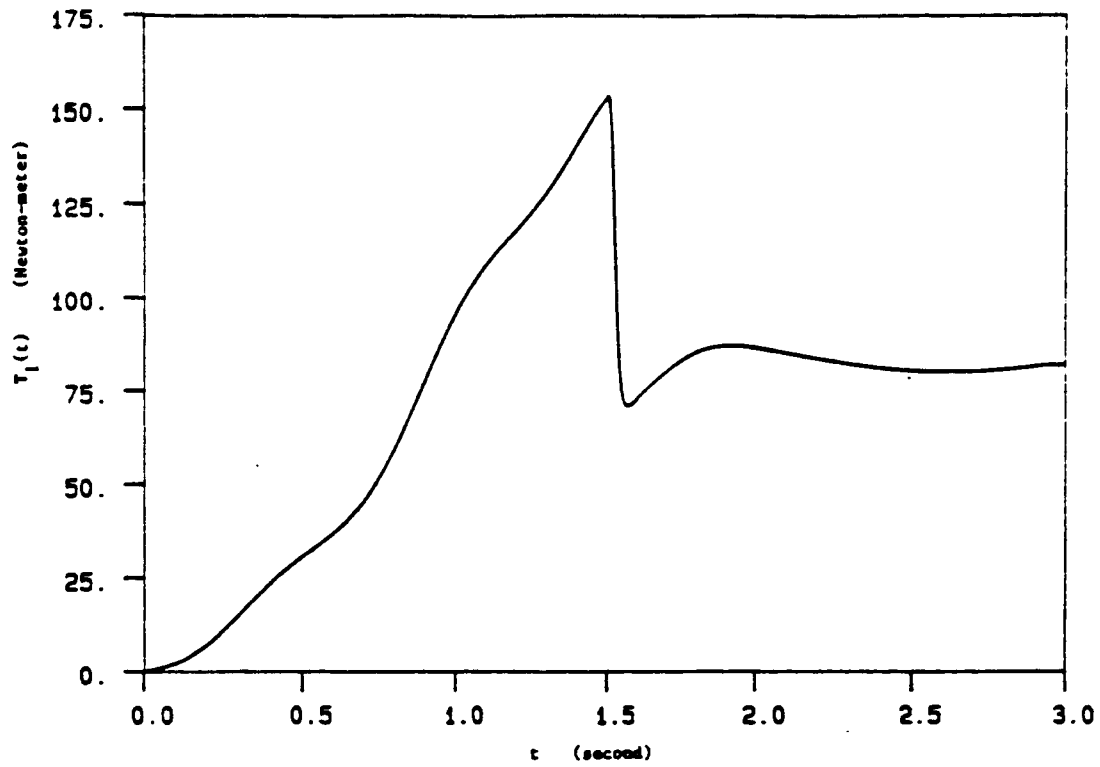


Figure 6(i). Variation of the Control Torque $T_1(t)$

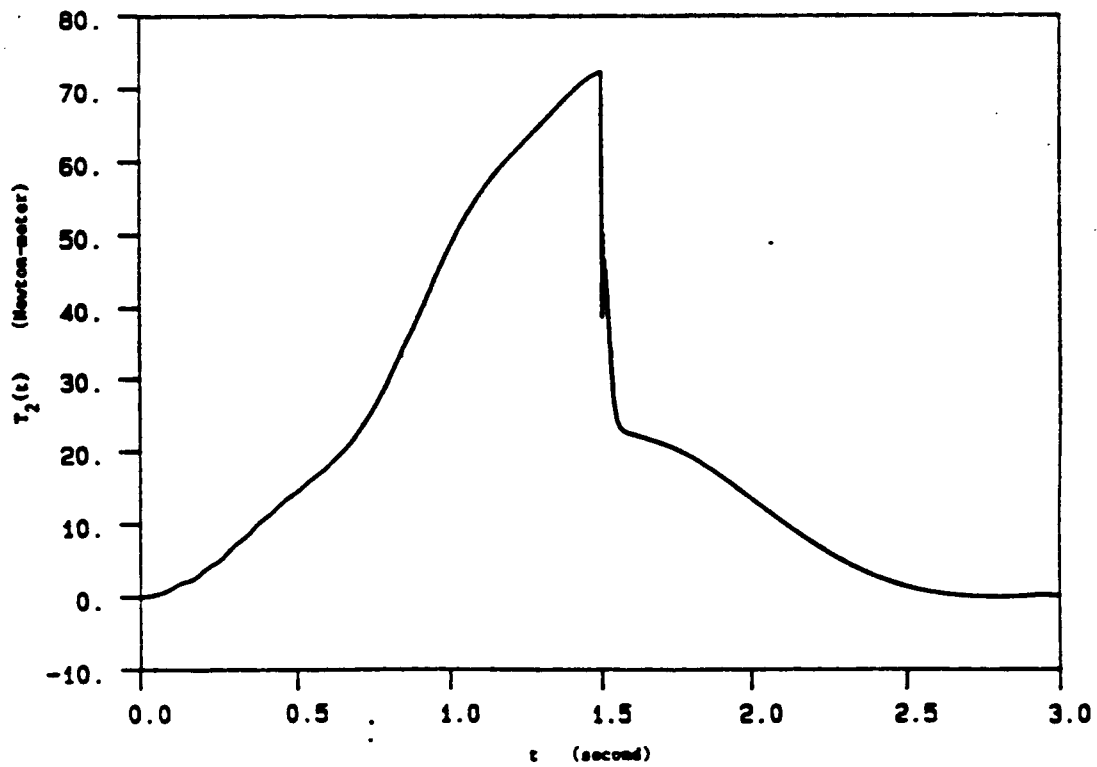


Figure 6(ii). Variation of the Control Torque $T_2(t)$

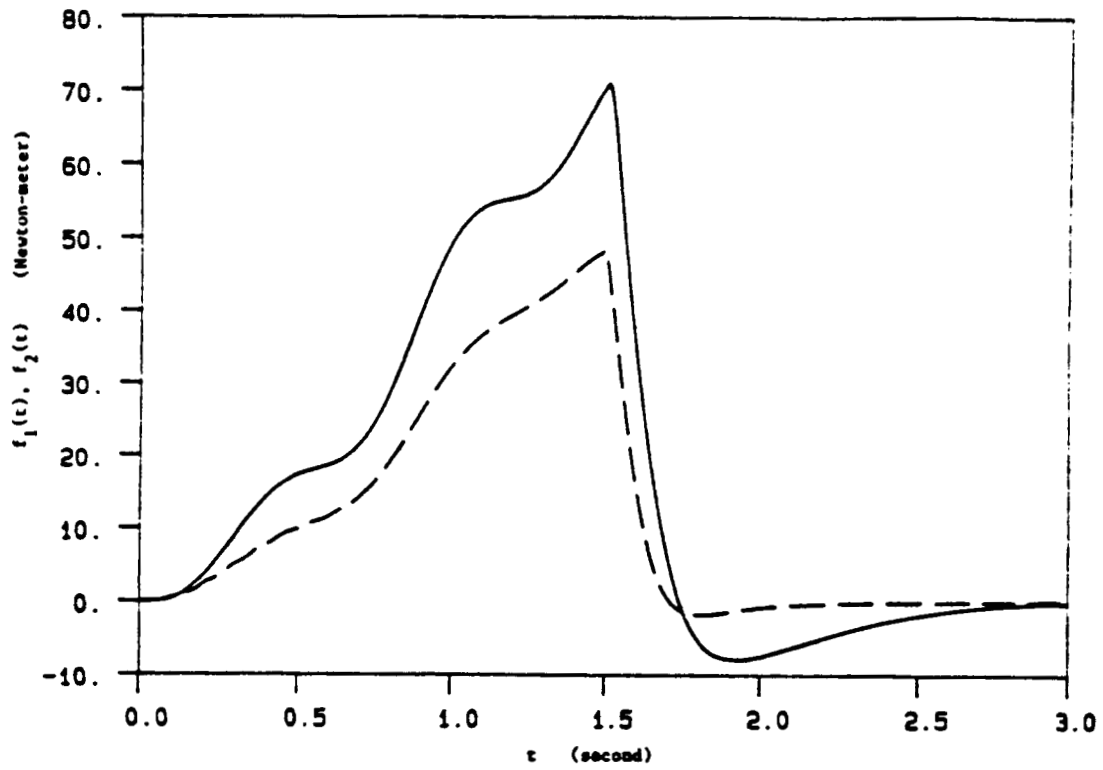


Figure 7(i). Variations of the Auxiliary Signals $f_1(t)$ [solid] and $f_2(t)$ [dashed]

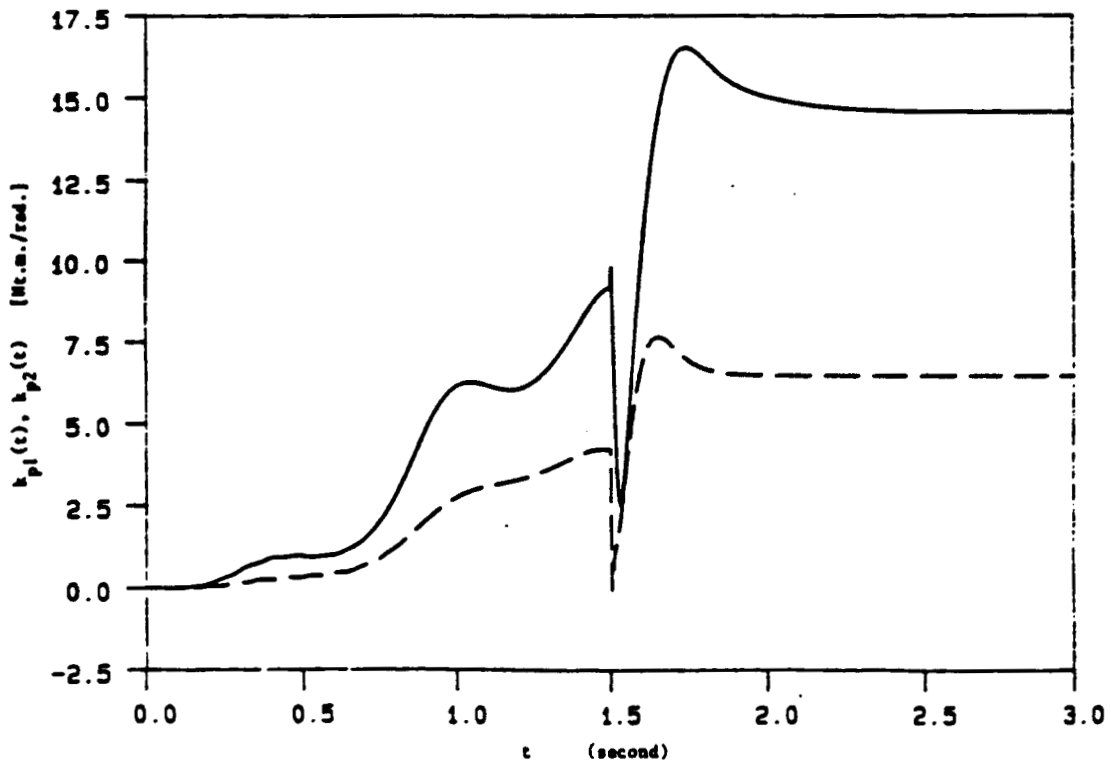


Figure 7(ii). Variations of the Position Gains $k_{p1}(t)$ [solid] and $k_{p2}(t)$ [dashed]

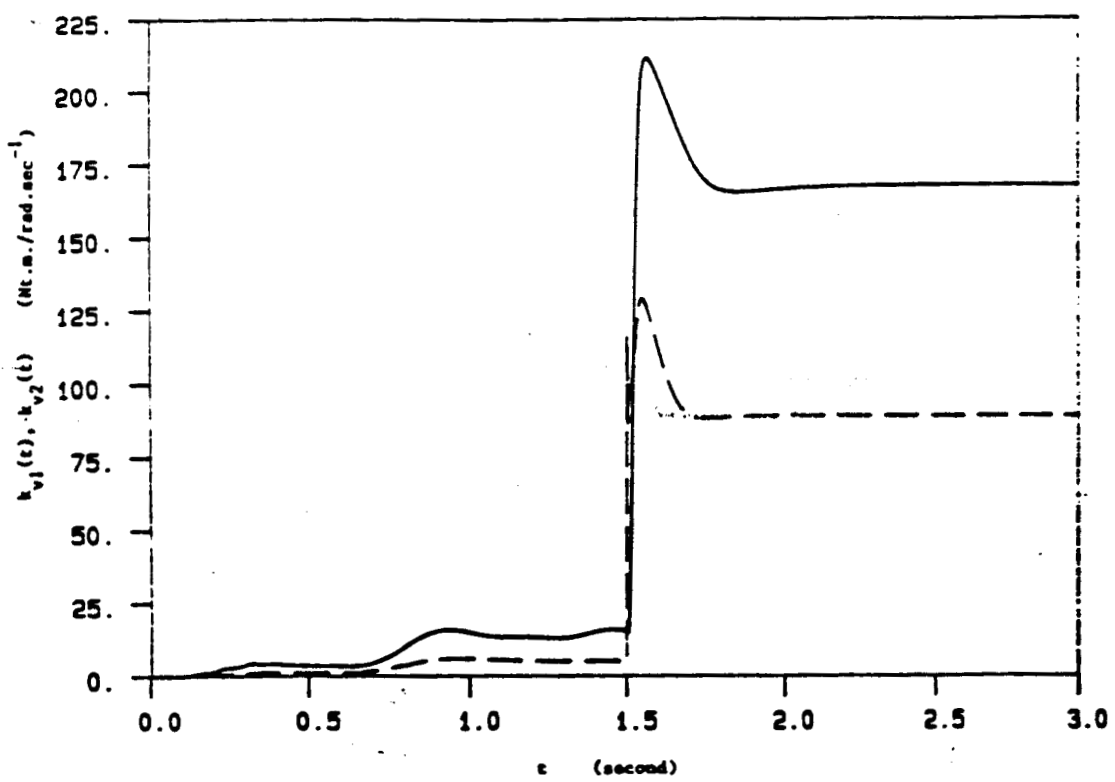


Figure 7(iii). Variations of the Velocity Gains $k_{v1}(t)$ [solid] and $k_{v2}(t)$ [dashed]

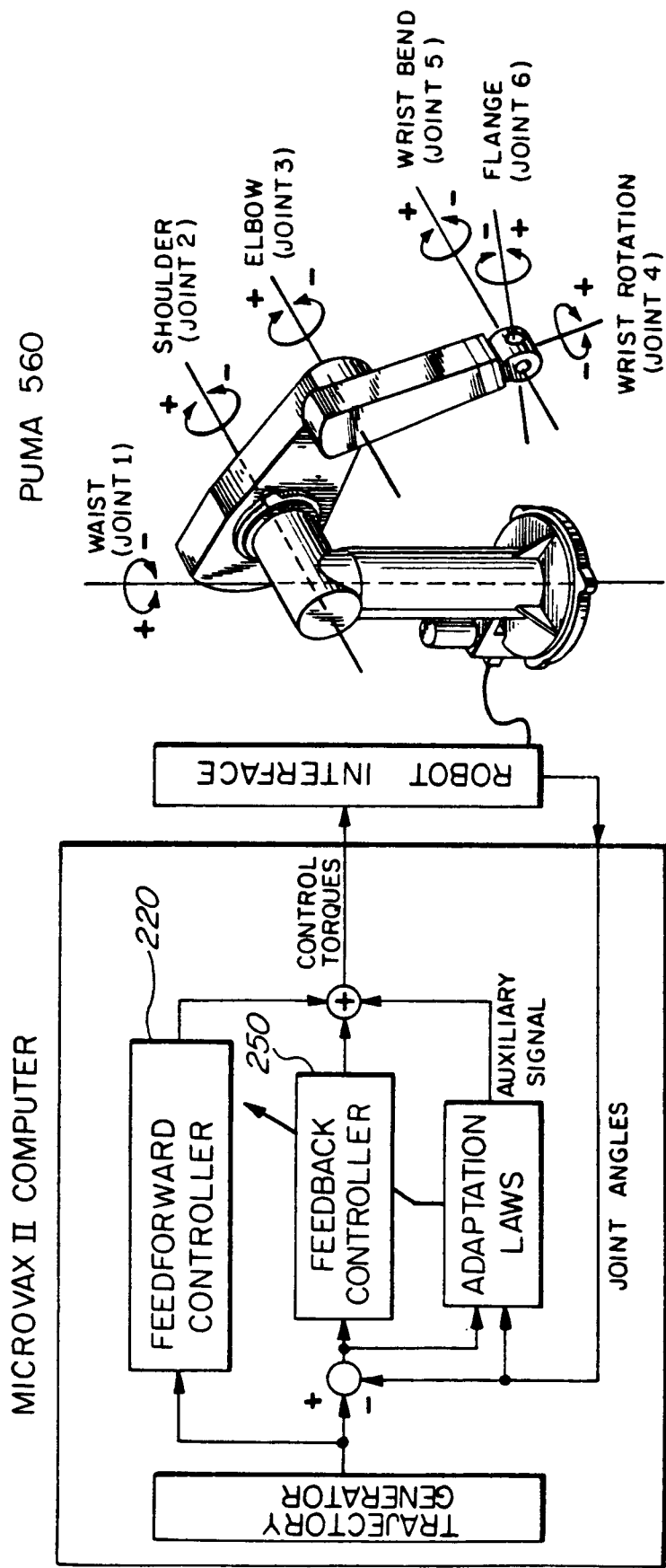


FIG. 8

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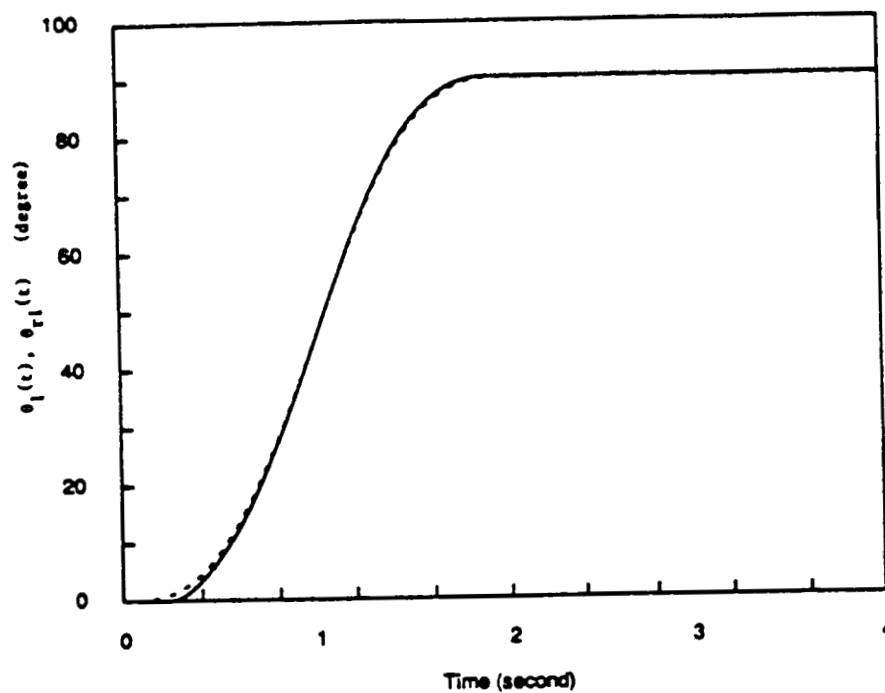


Figure 9(i). Desired [dashed] and Actual [solid] PUMA Waist Angles under Adaptive Controller

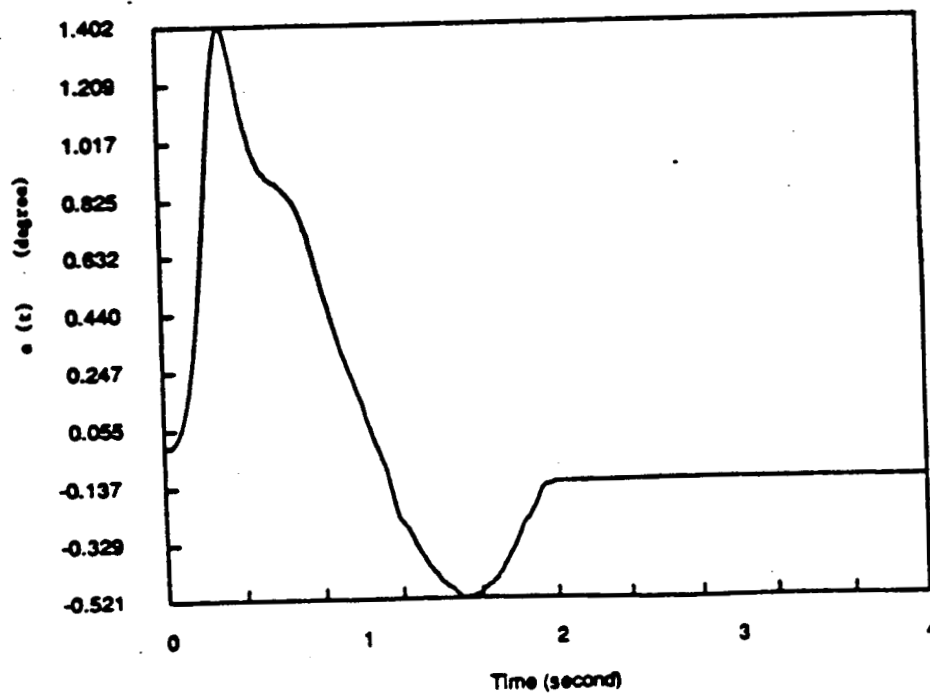


Figure 9(ii). Waist Tracking-Error under Adaptive Controller

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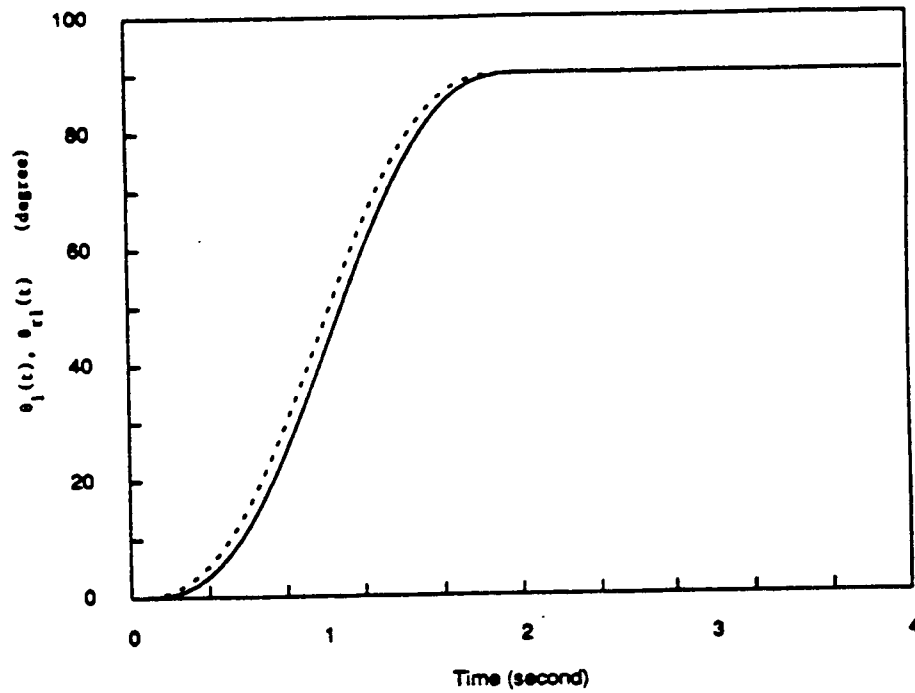


Figure 10(i). Desired [dashed] and Actual [solid] PUMA Waist Angles under Unimation Controller

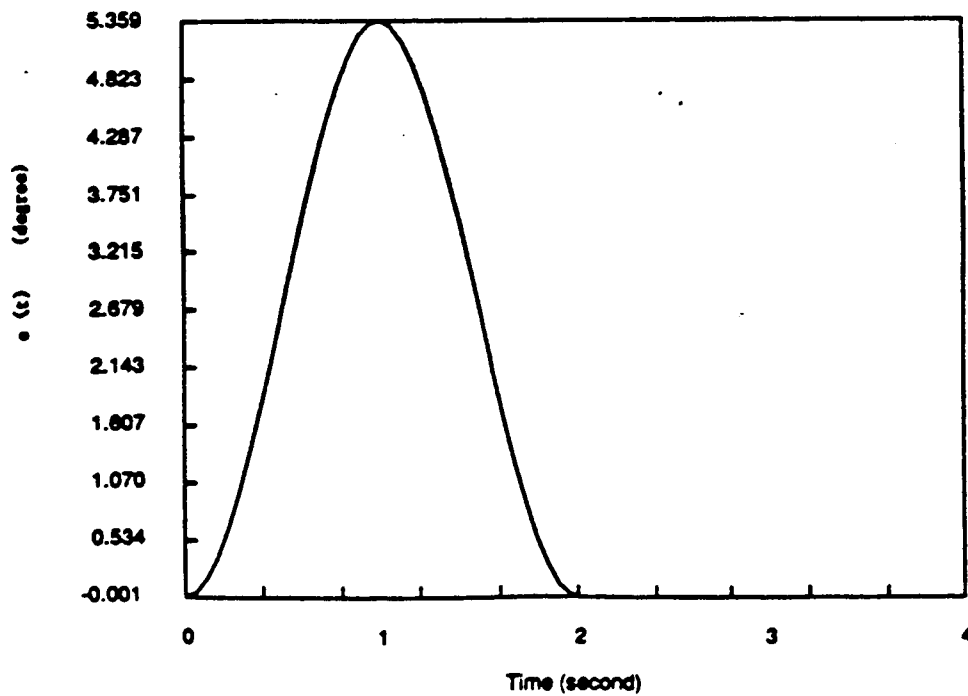


Figure 10(ii). Waist Tracking-Error under Unimation Controller

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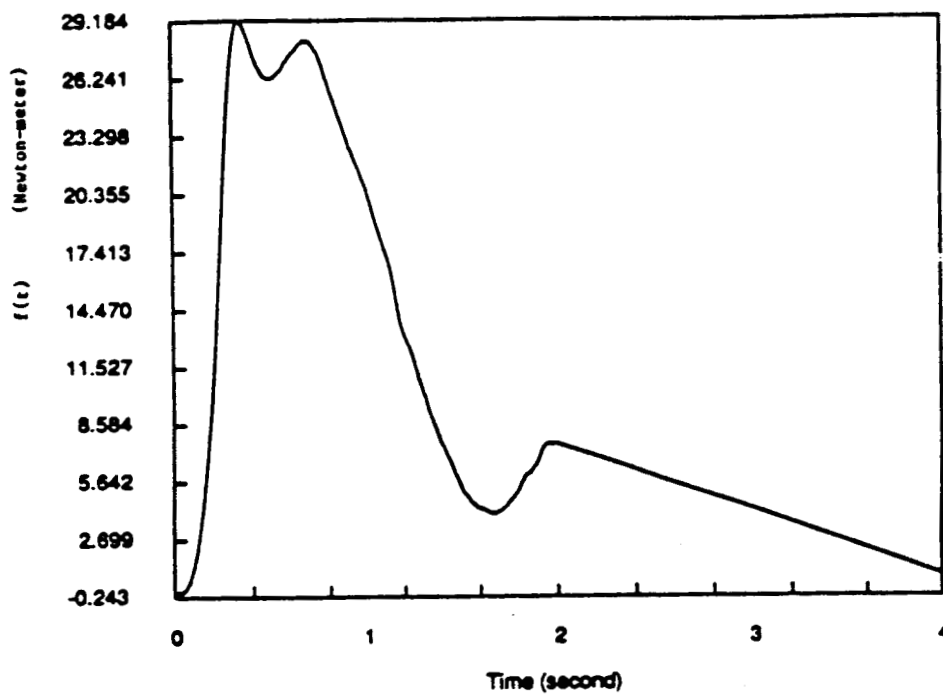


Figure 11(i). Variation of the Auxiliary Signal $f(t)$

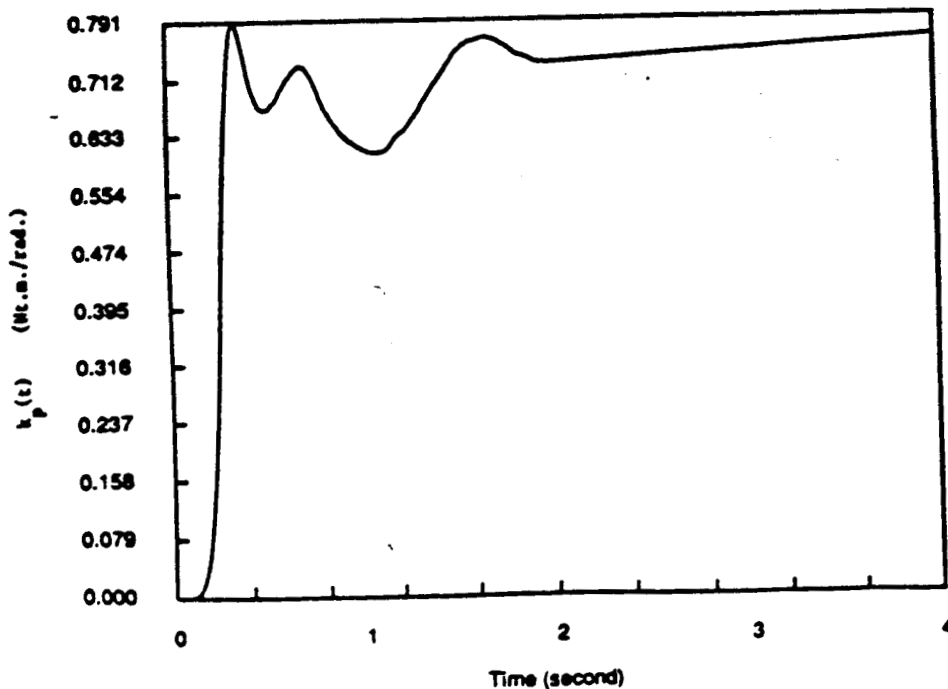


Figure 11(ii). Variation of the Position Gain $k_p(t)$

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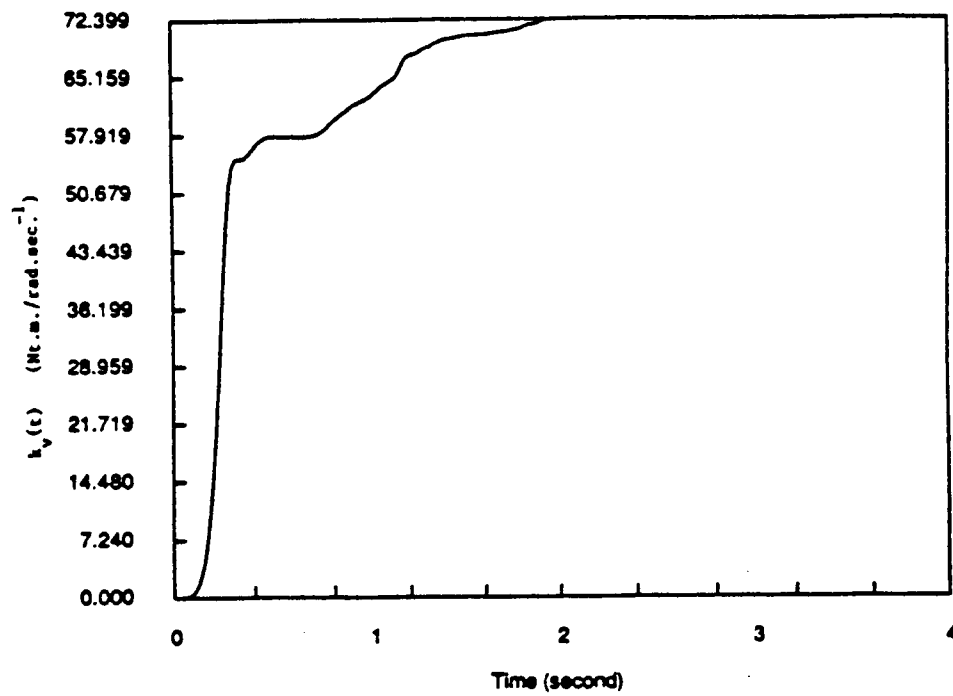


Figure 11(iii). Variation of the Velocity Gain $k_v(t)$

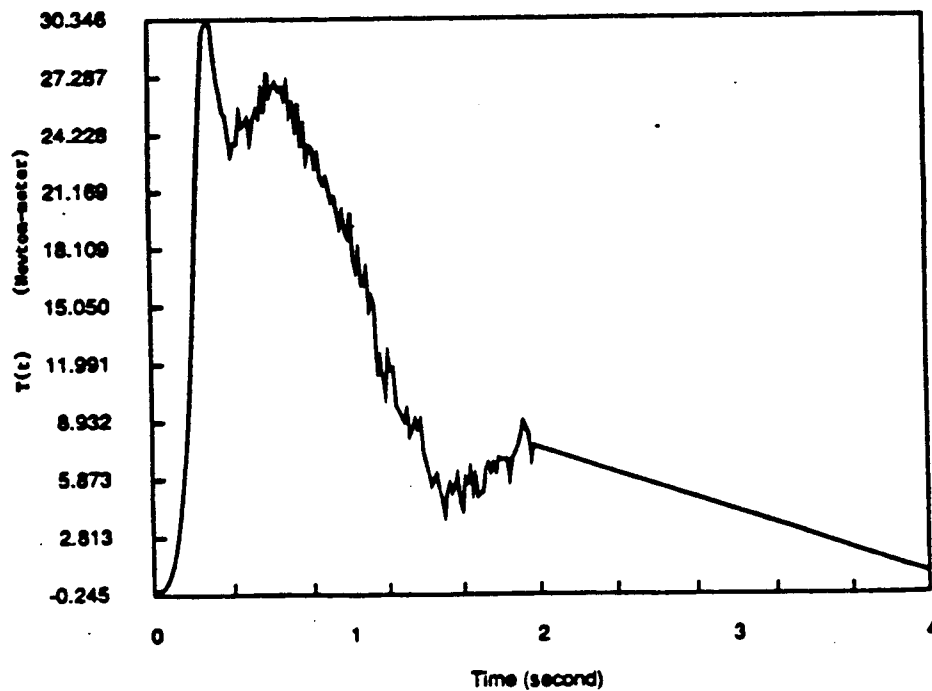


Figure 11(iv). Variation of the Control Torque $T(t)$

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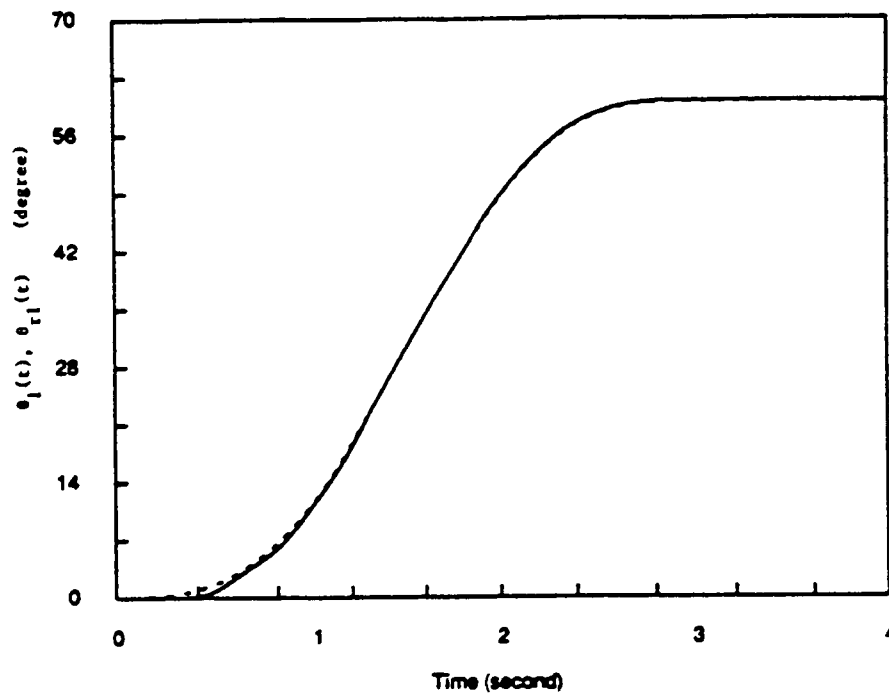


Figure 12(i). Desired [dashed] and Actual [solid] Waist Angles-with Arm Configuration Change

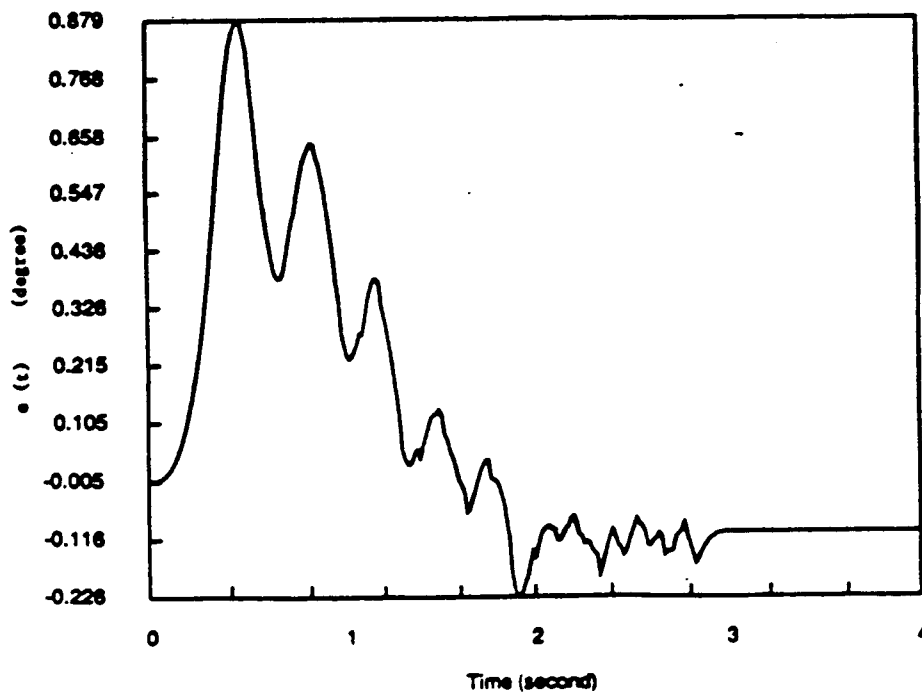


Figure 12(ii). Waist Tracking-Error with Arm Configuration Change