## NASA Technical Paper 2969

1990

# NASA Supercritical Airfoils

A Matrix of Family-Related Airfoils

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National Aeronautics and Space Administration

Office of Management

Scientific and Technical Information Division

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#### Summary

A concerted effort within the National Aeronautics and Space Administration (NASA) during the 1960's and 1970's was directed toward developing practical two-dimensional turbulent airfoils with good transonic behavior while retaining acceptable low-speed characteristics and focused on a concept referred to as the supercritical airfoil. This distinctive airfoil shape, based on the concept of local supersonic flow with isentropic recompression, was characterized by a large leading-edge radius, reduced curvature over the middle region of the upper surface, and substantial aft camber.

This report summarizes the supercritical airfoil development program in a chronological fashion, discusses some of the design guidelines, and presents coordinates of a matrix of family-related supercritical airfoils with thicknesses from 2 to 18 percent and design lift coefficients from 0 to 1.0.

#### Introduction

A concerted effort within the National Aeronautics and Space Administration (NASA) during the 1960's and 1970's was directed toward developing practical airfoils with two-dimensional transonic turbulent flow and improved drag divergence Mach numbers while retaining acceptable low-speed maximum lift and stall characteristics and focused on a concept referred to as the supercritical airfoil. This distinctive airfoil shape, based on the concept of local supersonic flow with isentropic recompression, was characterized by a large leading-edge radius, reduced curvature over the middle region of the upper surface, and substantial aft camber.

The early phase of this effort was successful in significantly extending drag-rise Mach numbers beyond those of conventional airfoils such as the National Advisory Committee for Aeronautics (NACA) 6-series airfoils. These early supercritical airfoils (denoted by the SC(phase 1) prefix), however, experienced a gradual increase in drag at Mach numbers just preceding drag divergence (referred to as drag creep). This gradual buildup of drag was largely associated with an intermediate off-design second velocity peak (an acceleration of the flow over the rear upper-surface portion of the airfoil just before the final recompression at the trailing edge) and relatively weak shock waves above the upper surface.

Improvements to these early, phase 1 airfoils resulted in airfoils with significantly reduced drag creep characteristics. These early, phase 1 airfoils and the improved phase 1 airfoils were developed before adequate theoretical analysis codes were available and resulted from iterative contour modifications during wind-tunnel testing. The process consisted of evaluating experimental pressure distributions at design and off-design conditions and physically altering the airfoil profiles to yield the best drag characteristics over a range of experimental test conditions.

The insight gained and the design guidelines that were recognized during these early phase 1 investigations, together with transonic, viscous, airfoil analysis codes developed during the same time period, resulted in the design of a matrix of family-related supercritical airfoils (denoted by the SC(phase 2) prefix).

The purpose of this report is to summarize the background of the NASA supercritical airfoil development, to discuss some of the airfoil design guidelines, and to present coordinates of a matrix of family-related supercritical airfoils with thicknesses from 2 to 18 percent and design lift coefficients from 0 to 1.0. Much of the discussion pertaining to the fundamental design concepts is taken from reference 1 and unpublished lectures on supercritical technology presented by Richard T. Whitcomb in 1970. Information on the development of supercritical airfoils and earlier publications were originally classified confidential but have since been declassified. Reference 2 discusses potential benefits of applying supercritical airfoil technology to various types of aircraft and flight programs to demonstrate such applications. Table I indicates some of the major milestones in the development of supercritical airfoils.

The high maximum lift and docile stall behavior observed on thick supercritical airfoils generated an interest in developing advanced airfoils for low-speed general aviation application. Starting in the early 1970's, several such airfoils were developed. Emphasis was placed on designing turbulent airfoils with low cruise drag, high climb lift-to-drag ratios, high maximum lift, and predictable, docile stall characteristics.

During the mid 1970's, several medium-speed airfoils were developed that were intended to fill the gap between the low-speed airfoils and the supercritical airfoils for application on light executive-type airplanes. These airfoils provided higher cruise Mach numbers than the low-speed airfoils while retaining good high-lift, low-speed characteristics.

References 3 to 12 document the research effort on NASA low- and medium-speed airfoils.

#### Symbols

 $C_p$  pressure coefficient,  $\frac{p-p_{\infty}}{q_{\infty}}$ 

 $C_{p,\text{sonic}}$  pressure coefficient corresponding to local Mach number of 1.0

С	airfoil chord, distance along refer- ence line from leading edge to trail- ing edge
$c_d$	section drag coefficient
$c_l$	section lift coefficient
$c_m$	section pitching-moment coefficient about the quarter chord
$c_n$	section normal-force coefficient
K	curvature of airfoil surfaces, $d^2y/dx^2$
M	free-stream Mach number
m	slope of airfoil surface, $dy/dx$
p	pressure, psf
q	dynamic pressure, psf
$R_c$	Reynolds number based on free- stream conditions and airfoil chord
$\mathbf{SC}$	supercritical
TE	trailing edge
t/c	thickness-to-chord ratio
x	distance along airfoil reference line measured from leading edge
y	distance normal to airfoil reference line
lpha	angle of attack
Subscripts:	
DD	drag divergence
1	lower surface

- u upper surface
- $\infty$  free-stream conditions

#### Airfoil designation:

The airfoil designation is in the form SC(2)-0710, where SC(2) indicates supercritical (phase 2). The next two digits designate the airfoil design lift coefficient in tenths (0.7), and the last two digits designate the airfoil maximum thickness in percent chord (10 percent).

SC(1)-0710	supercritical (phase 1) $-0.7$ design lift coefficient, 10 percent thick
SC(2)-0710	supercritical (phase 2)—0.7 design lift coefficient, 10 percent thick

SC(3)-0710	supercritical (phase $3$ )— $0.7$ design
	lift coefficient, 10 percent thick

#### **Development of Supercritical Airfoils**

#### **Slotted Supercritical Airfoil**

In the early 1960's, Richard T. Whitcomb of the Langley Research Center proposed, on the basis of intuitive reasoning and substantiating experimentation, an airfoil shape (fig. 1) with supersonic flow over a major portion of the upper surface and subsonic drag rise well beyond the critical Mach number (ref. 13). The airfoil had a slot between the upper and lower surfaces near the three-quarter chord to energize the boundary layer and delay separation on both surfaces. It incorporated negative camber ahead of the slot with substantial positive camber rearward of the slot. Wind-tunnel results obtained for two-dimensional models of a 13.5-percent-thick airfoil of the slotted shape and a NACA 64A-series airfoil of the same thickness ratio indicated that for a design-section normal-force coefficient of 0.65 the slotted airfoil had a drag-rise Mach number of 0.79 compared with a drag-rise Mach number of 0.67 for the 64A-series airfoil. The drag at a Mach number just less than that of drag rise for the slotted airfoil was due almost entirely to skin friction losses and was approximately 10 percent greater than that for the 64A-series airfoil. The slotted airfoil shape also significantly increased the stall normal-force coefficient at high subsonic speeds. The pitchingmoment coefficients for the slotted shape were substantially more negative than those for more conventional airfoils. The rationale leading to the slotted shape was discussed in reference 13. Because the slotted airfoil was designed to operate efficiently at Mach numbers above the "critical" Mach number (the freestream Mach number at which local sonic velocities develop) with an extensive region of supersonic flow on the upper surface, it was referred to as the "supercritical airfoil." Reference 14 indicated that the gains obtained for this two-dimensional slotted airfoil shape were also realized for a threedimensional swept wing configuration that incorporated the airfoil shape.

#### **Integral Supercritical Airfoil**

It was recognized that the presence of a slot increased skin friction drag and structural complications. Furthermore, both two-dimensional and threedimensional investigations of the slotted airfoil indicated that the shape of the lower surface just ahead of the slot itself was extremely critical and required very close dimensional tolerances.

Because of these disadvantages, an unslotted or integral supercritical airfoil (fig. 1) was developed in the mid 1960's. The results of the first work on the integral airfoil were given limited distribution in 1967 in a confidential Langley working paper. This paper was later declassified and formed the basis for much of the review of NASA supercritical airfoils presented in reference 1. Except for the elimination of the slot, the general shape of this integral airfoil was similar to that of the slotted airfoil. Proper shaping of the pressure distributions was utilized to control boundarylayer separation rather than a transfer of stream energy from the lower to upper surface through a slot. The maximum thickness-to-chord ratio for the integral supercritical airfoil was 0.11 rather than 0.135 as used for the slotted airfoil. Theoretical boundarylayer calculations indicated that the flow on the lower surface of an integral airfoil with the greater thickness ratio of the slotted airfoil would have separated because of the relatively high adverse pressure gradients at the point of curvature reversal.

The experimental results shown in figure 2 indicated that for a normal-force coefficient of 0.65 the drag-rise Mach number for the integral airfoil was slightly higher than that for the slotted airfoil of reference 13. However, a simplified analysis indicated that the drag rise for a slotted airfoil with the same thickness ratio of the integral airfoil would be roughly 0.81. A rule of thumb is that, all else being equal, there is approximately 0.01 change in dragrise Mach number for every 0.01 change in thickness ratio. Thus, the integral airfoil was somewhat less effective than the slotted airfoil in delaying drag rise.

For reference, the drag-rise characteristics for a NACA 64<sub>1</sub>-212 airfoil, obtained from reference 15, are also presented in figure 2. A comparison of the thickness distribution for this 6-series airfoil with that for the supercritical airfoil suggested that the 11-percent-thick supercritical airfoil was approximately structurally equivalent to the 12-percent-thick 6-series airfoil. Compared with this 6-series airfoil, the integral supercritical airfoil delayed the drag-rise Mach number by an increment somewhat greater than 0.1.

Note the dip in drag coefficient at M = 0.79 for the slotted airfoil. There has been much discussion over the years as to whether it is possible to isentropically decelerate a supersonic flow to a subsonic flow without creating a shock wave. At this particular point, the shock wave almost disappeared. There was only a very small glimmer of a wave in schlieren pictures and there did not appear to be much wave energy loss in the wake drag measurements behind the model. It was, for all practical purposes, a shockfree condition. Even though the ideal of a shockfree flow had been accomplished, it was decided that since aircraft must be efficient over a range of operating conditions, a shock-free point-design flow was impractical. It was believed that it was more important to design airfoils that had the lowest possible level of drag up to the cruise point without the shock-free drag dip. The low-speed drag for the integral airfoil was about the same level as for the more conventional 6-series airfoil because the added skin friction of the second component of the slotted airfoil had been eliminated. There was a gradual rise in drag due to wave losses and finally an abrupt rise when the flow finally separated, but no attempt was made to achieve a shock-free condition.

The integral supercritical airfoil also provided a substantial increase in the Mach number and normalforce coefficient at which boundary-layer separation occurred compared with that for the conventional NACA 6-series airfoil of similar thickness (fig. 3). The separation boundary in figure 3 is sometimes called a buffet boundary. In this case, it represents a force boundary, that is, the boundary where the flow over the whole airfoil deteriorated rapidly. Beyond this line, the airfoil experienced large drag increases. The boundary for the 6-series airfoil, indicating a gradual decrease with increasing Mach number, is typical of conventional airfoils. For the supercritical airfoil, the boundary is pushed well out in both Mach number and normal force. This is extremely important for maneuvering aircraft.

In addition, pitching-moment coefficients for the integral supercritical airfoil were reduced compared with the slotted airfoil (fig. 4). It should be noted, however, that the relatively large pitching moments on supercritical airfoils are not as penalizing in their application to swept wings as commonly thought. Tests of three-dimensional aircraft configurations incorporating the supercritical airfoil (ref. 16) have indicated that the optimum twist for supercritical wings designed for higher speeds is greater than for lower speed designs. As the design Mach number approaches 1.0, the magnitude of the optimum twist increases. This large amount of twist substantially reduces or eliminates the trim penalty associated with the greater negative pitching moment for the supercritical airfoil.

A more recent comparison (ref. 17) of the trim drag measurements for a wide-body transonic model with conventional and supercritical wings at a Mach number of 0.82 indicated that the trim drag for the supercritical wing configuration was not significantly higher than that for the conventional widebody configuration.

The contours of the integral airfoil were such that it could be defined by several equations empirically fitted to various regions of the airfoil. Since the supercritical airfoil concepts were still in the development stage, however, these equations were never published.

#### **General Design Philosophy**

This section discusses the concepts and reasoning at this point in the development of supercritical airfoils that were incorporated into the integral supercritical airfoil.

A comparison of supercritical flow phenomena for a conventional airfoil and the NASA supercritical airfoil is shown in figure 5. As an airfoil approaches the speed of sound, the velocities on the upper surface become supersonic because of the accelerated flow over the upper surface, and there is a local field of supersonic flow extending vertically from the airfoil and immersed in the general subsonic field. On conventional airfoils this pocket of accelerating supersonic flow is terminated near midchord by a more or less pronounced shock wave with attendant wave losses. This shock wave is followed immediately by a decelerating flow to the trailing edge. The pressure rise through the shock wave may, when superimposed on the adverse pressure gradient at the trailing edge, cause separation of the boundary layer with further increases in drag as well as buffeting and stability problems.

The surface pressure distribution and flow field shown at the bottom of figure 5 are representative of those obtained for NASA supercritical airfoils. The upper-surface pressure and related velocity distributions are characterized by a shock location significantly aft of the midchord, an approximately uniform supersonic velocity from about 5 percent chord to the shock, a plateau in the pressure distribution downstream of the shock, a relatively steep pressure recovery on the extreme rearward region, and a trailing-edge pressure slightly more positive than ambient pressure. The lower surface has roughly constant negative pressure coefficients corresponding to subcritical velocities over the forward region and a rapid increase in pressure rearward of the midchord to a substantially positive pressure forward of the trailing edge.

The elimination of the flow acceleration on the upper surface ahead of the shock wave results primarily from reduced curvature over the midchord region of the supercritical airfoil and provides a reduction of the Mach number ahead of the shock for a given lift coefficient with a resulting decrease of the shock strength. The strength and extent of the shock at the design condition could be reduced below that of the pressure distribution shown by shaping the airfoil to provide a gradual deceleration of the supersonic flow from near the leading edge to the shock wave. The extensive experiments up to this point indicated that the shape associated with the design point pressure distribution shown in figure 5 provided acceptable drag values over a wide Mach number and lift coefficient range.

Figure 6 shows a schematic of what happens in the supersonic flow field above the upper surface of the supercritical airfoil to yield a very weak shock wave and in some cases to eliminate the shock. As mentioned earlier, the local supersonic field is immersed in a subsonic field, and the division between the two fields is called the sonic line. The airfoil produces expansion waves, or waves that tend to reduce pressure and increase velocity starting near the leading edge. If the flow field were a purely supersonic flow, there would be a continual expansion or acceleration of the flow from leading edge to trailing edge. There is actually an infinite series of expansions that move out of this supersonic field, but the effect is illustrated schematically for a single expansion shown as a dashed line. These lines are called characteristic lines. When the flow is mixed, the expansion waves that emanate from the leading edge are reflected back from the sonic line as compression waves that propagate back through the supersonic field to the airfoil surface. Up to this point of contact, all the expansion waves have been accelerating the flow, but as soon as the compression waves get back to the surface, they start to decelerate the flow. These compression waves are then reflected off the solid airfoil surface as more compression waves. So, there are sets of competing waves or disturbances working in the flow that are the key to obtaining good transonic characteristics for airfoils. The idea is to design the shape of the airfoil just right so that these compression or decelerating disturbances tend to balance out the accelerating ones to get an airfoil that has a flat top pressure distribution even though there is continuous curvature over the upper surface. Two primary factors influence the balancing of these expansion and compression waves: the leading edge and the surface over the forward and midchord regions. First, there need to be strong expansions from the leading-edge region so they can be reflected back as compression waves—thus the large leading radius characteristic of supercritical airfoils. The leading edge is substantially larger than for previous airfoils and is more than twice that for a 6-series airfoil of the same thickness-to-chord ratio. Second, the curvature over the midchord region must be kept fairly small so that there is not a very large amount of accelerations being emanated that must be overcome by the reflected compression waves-thus the flattened upper-surface characteristic of supercritical airfoils.

Isentropic recompression is thus encouraged and at design conditions an extensive chordwise region of generally constant supersonic flow is maintained over the upper surface and terminated with a very weak shock wave. As noted in reference 18, these two concepts are consistent with the work done by Pearcey (ref. 19) when he demonstrated that the essential geometric feature of sections designed to exploit the isentropic compression due to waves reflected from the sonic line is an abrupt change on the upper surface from the relatively high curvature of the leading edge to a relatively low curvature downstream and that this can be provided with a large leading-edge radius.

Pressure distributions measured on the 11-percent-thick integral airfoil provide a general indication of the flow phenomena associated with NASA supercritical airfoils at design, subcritical, intermediate off-design, and high-lift conditions (fig. 7).

Figure 7(a) shows the nearest experimental pressure distribution to design conditions at a Mach number slightly above the design value. The shock wave location is rearward of that for the design condition with a small acceleration ahead of the shock. This causes a slight increase in shock losses but does not result in boundary-layer separation. Separation would occur when the shock wave moves farther rearward and the pressure plateau is eliminated.

The flow is a little more complex over the aft part of the airfoil. One of the important features of the supercritical airfoil is to keep the flow just behind the shock wave moving at close to the speed of sound (fig. 5). The plateau in the pressure distribution tends to control the forward movement of disturbances associated with the decelerating flow near the trailing edge of the airfoil. This prevents the disturbances from moving forward near the surface and causing the flow to converge into the usual shock wave. However, since the flow at a moderate distance above the surface is subsonic, the disturbances can move forward and downward into the supersonic region to decelerate the flow leading into the shock wave. The combination of these effects significantly reduces the extent and strength of the shock wave. In fact it was a key factor in obtaining the shockfree design condition described in reference 13 for the slotted airfoil.

The pressure plateau behind the shock wave is also necessary to stabilize the boundary layer. When the boundary layer moves through the pressure drop at the shock, it decelerates more than the stream flow because it does not have as much momentum as the stream. If the pressure gradient behind the shock wave is too great, the boundary-layer flow will reverse and result in separated flow. The problem is how to keep the boundary-layer flow from reversing. If the boundary layer has to go through a continuous adverse pressure gradient from ahead of the shock to the trailing edge, boundary-layer theory indicates that it will separate. However, the plateau in the pressure distribution rearward of the shock wave allows a reenergization of the boundary layer by mixing between the shock and the final pressure rise at the trailing edge. As a result, the boundary layer can move through a greater total pressure rise without separating.

Considering another part of the boundary-layer story, the pressure coefficient at the trailing edge on a conventional airfoil is fairly positive. Theoretically it recovers to stagnation pressure, but in reality, because it is impossible for the boundary layer to reach stagnation conditions, it separates locally and the pressure rise is less. On the supercritical airfoil, the intent was to keep the boundary layer attached while it underwent the total pressure rise through the shock wave and the trailing-edge recovery. If the pressures had to rise from the level ahead of the shock to the usual positive pressures at the trailing edge, boundary-layer theory indicates that it would separate even though there is a plateau. Therefore, the supercritical airfoil was designed so that the pressure coefficient at the trailing edge was only slightly positive by making the slope of the lower surface equal to that of the upper surface at the trailing edge. This results in the airfoil having a very sharp and thin trailing edge. The importance of this effect is shown by the experimental data in figure 7(a). The nearambient pressure at the trailing edge, which results from the small included angle of the trailing edge, reduces to a minimum the total pressure rise the upper-surface boundary layer must traverse and thus minimizes the tendency toward separation.

Turning now to the lower surface, it has been mentioned before that lift is produced by the aft lower-surface cusp, resulting in the type of aft-loaded pressure distribution shown in figure 7(a). There is a severe pressure rise near two-thirds chord to substantially positive pressures in the cusp region. Again referring to boundary-layer theory, boundary layers going into such positive pressures tend to separate much more readily than when going into a pressure rise from less than stream pressure to stream pressure, so that a pressure rise on the lower surface greater than that on the upper surface cannot be tolerated. Therefore, it is important that the velocities on the forward region of the lower surface do not go supersonic. As soon as the flow there goes supersonic, a shock wave pressure rise is superimposed on the pronounced pressure rise leading into the cusp, which increases the tendency for the boundary layer to

separate. In fact, experiments were conducted where the flow on the lower surface went supersonic, and for such cases, the flow did separate.

Attention was also paid to the shape of the pressure rise into the lower-surface cusp as defined by the Stratford criteria of reference 20. There is initially an abrupt rise or steep positive gradient followed by a gradually decreasing gradient into the cusp. This in effect forces the boundary layer right up to the point of separation and then eases off by reducing the rate of pressure rise. In theory, at this point there is zero shear or skin friction, although no decrease in drag that would be associated with this supposedly zero shear was ever measured during supercritical airfoil testing.

In figure 7(b), a subcritical pressure distribution is shown for the same angle of attack. The pressure distribution has a negative peak near the leading edge, followed by a gradual increase in pressure. It is important to keep this peak from becoming so high that the flow will separate. By keeping the velocities down in the middle region (region of low surface curvature) while accelerating the flow over the rear region (region of high surface curvature), the pressure distribution over the mid upper surface is quite flat and has a low level. The lower surface is the same as at supercritical speeds because the lower surface even for the supercritical case is still subcritical.

In figure 7(c), a pressure distribution is shown for an intermediate condition between the design and subcritical points at a Mach number just below the design value. Notice that the front part of the pressure distribution looks quite similar to that of the design point, fairly flat, but the shock location is significantly farther forward than for the design condition. Behind the shock wave the flow experiences a reacceleration because of the increased curvature of the rear part of the airfoil resulting in a second supersonic peak near three-quarter chord. When attempting to design for a minimum shock strength condition, the rearward curvature had to be increased and, as a result, the reacceleration velocity at the intermediate conditions could be sufficiently great to cause a second shock wave. The total pressure rise through this second shock and the immediately following trailing-edge pressure recovery may cause significant boundary-layer separation near the trailing edge.

The pressure distribution shown in figure 7(d) is that measured at the high-lift corner of the variation of normal force with Mach number for separation onset, shown previously in figure 3. The shock wave, associated with a local upstream Mach number of 1.4, causes a very large adverse pressure gradient. However, the trailing-edge pressure recovery and a surface oil flow visualization study indicated that the boundary layer did not completely separate. The bulge in the pressure distribution aft of the shock wave and the surface oil study indicated a very large separation bubble under the shock with flow reattachment near three-quarter chord. For conventional airfoil shapes, the presence of a shock wave associated with an upstream Mach number of 1.4 would cause very severe boundary-layer separation. The key to the greater stability of the boundary layer for the supercritical airfoil was the plateau in the pressure distribution aft of the shock described above. For conventional airfoils, the pressure immediately downstream of the shock wave continues to increase and the higher pressure behind the bubble tends to force the bubble away from the surface. With the plateau on the supercritical airfoil, this adverse effect is eliminated.

#### **Effects of Trailing-Edge Thickness**

The design philosophy of the supercritical airfoil required that the trailing-edge slopes of the upper and lower surfaces be equal. This requirement served to retard flow separation by reducing the pressurerecovery gradient on the upper surface so that the pressure coefficients recovered to only slightly positive values at the trailing edge. For an airfoil with a sharp trailing edge, as was the case for early supercritical airfoils, such restrictions resulted in the airfoil being structurally thin over the aft region.

Because of structural problems associated with sharp trailing edges and the potential aerodynamic advantages of thickened trailing edges for transonic airfoils (discussed, for example, in ref. 18), an exploratory investigation was made during the early development phases of the supercritical airfoil to determine the effects on the aerodynamic characteristics of thickening the trailing edge (fig. 8). Figure 9 shows that increasing the trailing-edge thickness of an interim 11-percent-thick supercritical airfoil from 0 to 1.0 percent of the chord resulted in a significant decrease in wave drag at transonic Mach numbers; however, this decrease was achieved at the expense of higher drag at subcritical Mach numbers. Various numbering systems were used during the development of the supercritical airfoils. The 11-percentthick airfoil with 0-percent-thick trailing edge was referred to as airfoil 4, and the 11-percent-thick airfoil with the 1-percent-thick blunt trailing edge was referred to as airfoil 5. These airfoil numbers had no special meaning with respect to airfoil characteristics but were simply configuration numbers used for identification purposes. Figure 1 summarizes the progression of supercritical airfoil shapes to this point.

Advantages of thick trailing edges at transonic Mach numbers were real and significant, but practical application appeared to depend on whether the drag penalty at subcritical Mach numbers could be reduced or eliminated. Two questions naturally arose: what would the optimum trailing-edge thickness be for supercritical airfoils, and could the drag penalty at the subcritical Mach numbers due to the thickened trailing edge be reduced by proper shaping of the trailing edge?

In order to investigate more comprehensively the effects of trailing-edge geometry, a refined 10-percent-thick supercritical airfoil was modified (circa 1970) to permit variations in trailing-edge thickness from 0 to 1.5 percent of the chord and inclusion of a cavity in the trailing edge (fig. 10). The refined 10-percent-thick airfoil with the 1-percentthick blunt trailing edge was identified as airfoil 9, the 1-percent-thick trailing edge with cavity as airfoil 9a, the 1.5-percent-thick trailing edge with cavity as airfoil 10, and the 0.7-percent-thick trailing edge with cavity as airfoil 11. The results. discussed in reference 21 and summarized in figures 11 and 12, suggested several general conclusions: (1) increasing trailing-edge thickness yielded reductions in transonic drag levels with no apparent penalty at subcritical Mach numbers up to a trailingedge thickness of about 0.7 percent, (2) increases in both subsonic and transonic drag levels appeared with increases in trailing-edge thickness beyond approximately 0.7 percent, (3) small drag reductions through the Mach number range resulted when the 1.0-percent-thick trailing edge was modified to include a cavity in the trailing edge, (4) there appeared to exist some relationship between the optimum airfoil trailing-edge thickness and the boundary-layer displacement thickness over the upper surface of the airfoil (reversal of the favorable effect of increasing trailing-edge thickness appeared to occur when the airfoil trailing-edge thickness exceeded the displacement thickness of the upper-surface boundary layer at the trailing edge), and (5) the general design criterion to realize the full aerodynamic advantage of trailing-edge thickness appeared to be such that the pressure coefficients over the upper surface of the airfoil recover to approximately zero at the trailing edge with the trailing-edge thickness equal to or slightly less than the local upper-surface boundary-layer displacement thickness. The experimental results for airfoil 9a were included in the AGARD experimental data base of reference 22 for computer program assessment.

As a consequence of this investigation, most subsequent experimental development of supercritical airfoils was carried out with cusped trailing edges about 0.7 percent thick. Much later in the supercritical airfoil development program, when the availability of analytical codes (discussed in later sections) made it easier to explore variations in trailing-edge geometry, the optimum trailing-edge thickness was found to vary with the maximum thickness of the airfoil and to be somewhat less than 0.7 percent.

#### **Effects of Maximum Thickness**

In order to provide a source of systematic experimental data for the early supercritical airfoils, the 11-percent-thick airfoil 5 and the 10-percent-thick airfoil 9 were reported in more detail in reference 23 to compare the aerodynamic characteristics of two airfoils of different maximum thicknesses. As noted above, the trailing edges of both airfoils were blunt and 1 percent thick. Although maximum thickness was the primary variable, dissimilarities between the two airfoils prevented a comparison based on pure thickness. However, general observations concerning the results were made. For the thinner airfoil, the onset of trailing-edge separation began at an approximately 0.1 higher normal-force coefficient at the higher test Mach numbers, and the drag divergence Mach number at a normal-force coefficient of 0.7 was 0.01 higher. Both effects were associated with lower induced velocities over the thinner airfoil.

#### Effects of Aft Upper-Surface Curvature

The dissimilarities between the 11-percent-thick airfoil 5 and the 10-percent-thick airfoil 9 were in the contours of the rear upper surface. As discussed earlier, the rear upper surface of the supercritical airfoil is shaped to accelerate the flow following the shock wave in order to produce a near-sonic plateau at design conditions. Near the design normal-force coefficient, at intermediate supercritical conditions between the onset of supersonic flow and the design point, the upper-surface shock wave is forward and the rear upper-surface contour necessary to produce the near-sonic plateau at design conditions causes the flow to expand into a second region of supercritical flow in the vicinity of three-quarter chord. Care must be exercised that this second region of supercritical flow is not permitted to expand to such an extent that a second shock wave is formed, which would tend to separate the flow over the rear portion of the airfoil. As part of the systematic wind-tunnel development of the supercritical airfoil, modifications over the rear upper surface of supercritical airfoil 5 were made to evaluate the effect of the magnitude of the off-design second velocity peak on the design point. Surface slopes over the rear upper surface of airfoil 5 were modified as shown in figure 13, and the resultant airfoil was designated as airfoil 6. The modification was accomplished by removing material

over approximately the rear 60 percent of the upper surface without changing the trailing-edge thickness and resulted in an increase in surface curvature around midchord and a decrease in surface curvature over approximately the rearmost 30 percent of the airfoil. (For small values of slope, curvature may be approximated by dm/dx, which is the second derivative of the surface contour  $d^2y/dx^2$ .) The evaluation is documented in reference 24.

The results indicated that attempts to reduce the magnitude of the second velocity peak at intermediate off-design conditions in that particular manner had an adverse effect on drag at design conditions. The results suggested, however, that in order to avoid drag penalties associated with the development of the second velocity peak into a second shock system on the upper surface at intermediate off-design conditions, the magnitude of the second peak should be less than that of the leading-edge peak.

Wave losses are approximately proportional to the local Mach number entering the shock and can be minimized by maintaining a region of low curvature and thereby reducing local velocities ahead of the shock. The broad region of relatively low, nearly uniform, upper-surface curvature on the supercritical airfoil extends from slightly rearward of the leading edge to about 70 or 75 percent chord. Reference 25 describes the results of extending this region of low curvature nearer to the trailing edge in an attempt to achieve a more rearward location of the upper-surface shock wave without rapid increases in wave losses and associated separation, thus delaying the drag divergence Mach number at a particular normal-force coefficient or delaying the drag break for a particular Mach number to a higher normal-force coefficient. Extending this low curvature region too near the trailing edge, however, forces a region of relatively high curvature in the vicinity of the trailing edge with increased trailing-edge slope. This high curvature would be expected to produce a more adverse pressure gradient at the trailing edge, where the boundary layer is most sensitive, and would result in a greater tendency toward trailing-edge separation. The degree and chordwise extent of low curvature therefore strongly influences both the strength of the shock wave and the onset of trailing-edge separation, the two principal causes of drag divergence. The results indicated that although simply extending the region of low curvature farther than on earlier supercritical airfoils provided a modest improvement in drag divergence Mach number, it had an unacceptably adverse effect on drag at lower Mach numbers.

#### An Improved Supercritical Airfoil

During the early development of the twodimensional supercritical airfoil, emphasis was placed upon developing an airfoil with the highest dragdivergence Mach number attainable at a normal-force coefficient of about 0.7. The normal-force coefficient of 0.7 was chosen as the design goal since, when account was taken of the effects of sweep, it was representative of lift coefficients at which advanced technology near-sonic transports utilizing the supercritical airfoil concept were then expected to cruise.

The resultant airfoil, identified as supercritical airfoil 11, with a ratio of maximum thickness to chord of 0.10 and a ratio of trailing-edge thickness to chord of 0.007, had a drag divergence Mach number of about 0.79 and was reported in reference 21. This airfoil experienced, however, a "creep" or gradual increase in the drag coefficient of about 14 counts  $(c_d \text{ increment of } 0.0014)$  between the subcritical Mach number of 0.60 and the drag divergence Mach number at the design normal-force coefficient. This gradual buildup of drag was largely associated with an intermediate off-design second velocity peak and relatively weak shock waves above the upper surface at these speeds. It was believed that with proper shape refinements, the drag creep could be reduced or eliminated.

Following the development of airfoil 11, design studies of advanced technology transport configurations suggested that cruise Mach number requirements would be somewhat lower than originally anticipated, thereby reducing wing sweep and lift coefficient. Consequently, the design lift coefficient at which the supercritical airfoil was being developed was lowered to about 0.55. The wind-tunnel tests (circa 1972) required for airfoil optimization at the lower normal-force coefficient also provided the opportunity to explore the drag creep problem, thus drag creep was included as a goal and an important factor in the wind-tunnel program. The result (ref. 26) was an airfoil, identified as airfoil 26a, with a slightly smaller leading-edge radius, reduced curvature over the forward and rear upper sufface, reduced aft camber, and minor changes over the lower surface. Until this point in the supercritical airfoil development program, the airfoils could more or less still be defined by several empirical equations. In the process of developing airfoil 26a, attempts were made to retain the capability of being able to describe the airfoils with geometric functions, but such efforts were not successful. Airfoil 26a and subsequent airfoils were not, therefore, mathematically described.

Such refinements in the airfoil shape produced improvements in the overall drag characteristics at normal-force coefficients from about 0.30 to 0.65 compared with earlier supercritical airfoils developed for a normal-force coefficient of 0.70. The drag divergence Mach number of the improved supercritical airfoil 26a varied from approximately 0.82 at a normal-force coefficient of 0.30 to 0.78 at a normal-force coefficient of 0.80 with no drag creep evident up to normal-force coefficients of about 0.65. As discussed in reference 26, these improved drag creep characteristics were largely attributed to a more favorable flow recompression over the forward upper surface and the elimination of a region of overexpansion near three-quarter chord.

#### **Effects of Aft Camber**

During the development of the improved 10-percent-thick airfoil 26a, a number of systematic contour modifications were evaluated. These individual modifications were intermediate steps toward a definite design goal but may be organized into small groups of related contour variations. One such grouping showed the effects of variations in surface slope and curvature distributions over the rear portion of the airfoil. Although not approached from the standpoint of camber effects per se, the variations of surface slope and curvature distributions resulted in airfoils with different aft camber and, for convenience, were referred to in this manner. Reference 27 documents the aerodynamic characteristics of these airfoils with different aft camber.

#### **Supercritical Airfoil 31**

Emphasis on fuel economy during the early 1970's generated considerable interest in fuel-conserving aircraft envisioned to cruise at Mach numbers near those of then current transports. Such an aircraft could utilize supercritical airfoil technology to achieve weight and drag reductions by permitting the use of thicker wings with higher aspect ratios and less sweep. Because wings with higher aspect ratios would require airfoils with design lift coefficients higher than 0.55, airfoil improvements again centered around developing an airfoil with a design normal-force coefficient of about 0.70 without incurring the troublesome drag creep problem of the earlier airfoil 11.

In order to apply the drag creep improvements incorporated into airfoil 26a, it was used as the starting point in extending the design normal-force coefficient to 0.70. Initially, the location of maximum uppersurface thickness above the reference line was moved forward from 0.40c to 0.38c, and the rear of the airfoil (both upper and lower surfaces) was displaced downward by an amount that varied from 0.0c at the new position of maximum thickness to 0.01c at the trailing edge, thereby increasing the aft camber. Moving the position of upper-surface maximum thickness forward by 0.02c simply compressed the forward upper surface longitudinally and maintained the same general family resemblance to airfoil 26a.

In addition to the aforementioned changes, several experimental modifications were necessary before arriving at the final configuration: airfoil 31 (circa 1974). These modifications consisted of small curvature variations near the upper-surface leading edge to better control the development of supersonic flow in this region and over the forward lower surface to flatten the forward lower-surface pressure distribution. Geometric characteristics of airfoil 31 are shown in figure 14 and compared with those of airfoil 12. Airfoil 12 differs very little from airfoil 11 (ref. 26) and was selected as a basis of comparison because data were available over a wider range of off-design conditions than for airfoil 11.

The results presented in reference 28 and summarized in figure 15 show that airfoil 31 produced significant improvements in the drag characteristics compared with the earlier supercritical airfoil 12 designed for the same normal-force coefficient  $(c_n = 0.7)$ . Drag creep was practically eliminated at normalforce coefficients between 0.4 and 0.7 and greatly reduced at other normal-force coefficients. Substantial reductions in the drag levels preceding drag divergence were also achieved at all normal-force coefficients. The Mach numbers at which drag diverged were delayed for airfoil 31 at normal-force coefficients up to about 0.6 (by approximately 0.01 and 0.02 at normal-force coefficients of 0.4 and 0.6, respectively) but were slightly lower at higher normal-force coefficients. The trade-off between reduced drag levels preceding drag divergence through the range of normal-force coefficients and reduced drag divergence Mach numbers at the higher normal-force coefficients called attention to the compromises that are sometimes necessary in the design of airfoils for practical applications over a wide range of operating conditions.

Supercritical airfoils through number 31 were developed through intuitive contour modifications in the wind tunnel before adequate theoretical design or analysis codes were available and are referred to as phase 1 airfoils. They resulted from an experimentally iterative process of evaluating experimental pressure distributions at design and off-design conditions and physically altering the airfoil profile to yield the best drag characteristics over a range of test conditions. The models were constructed to provide the capability of on-site (mounted in test section) modifications. They consisted of a metal core with metal leading and trailing edges that were removable to provide leading- and trailing-edge modifications. The upper and lower surfaces between the steel leading and trailing edges were formed with plastic filler material that could be easily reshaped. Changes to the surface contours could be made by adding or removing fill material. Control and measurement of the contours were provided by templates that rode spanwise on the metal leading and trailing edges. When time permitted and contour variations were known ahead of time, sweep templates were constructed to aid in model changes. When experimental data suggested changes during a tunnel entry, short spanwise strips of the model were first modified and smoothed by hand and then a template cast to that shape was made to aid in getting a uniform contour across the remainder of the span. Using such techniques, it was believed that coordinates could be maintained to an experimental accuracy of about y/c = 0.0001(y = 0.0025 in. for a 25-in.-chord model). It was not realistic or practical to believe that the models could be modified and measured on site much better than this.

#### **Theoretically Designed Supercritical Airfoil**

The successes in achieving virtually shock-free flow in wind-tunnel tests of two-dimensional airfoils. combined with the evolution of advanced technology aircraft, gave impetus to the development of a practical approach to the theoretical design of transonic lifting airfoils with minimum wave losses. One approach was the complex hodograph method for the design of shockless supercritical airfoils reported in reference 29. This mathematical approach was used by P. R. Garabedian of New York University to design an airfoil to be shock free (isentropic recompression) at a Mach number of 0.78, a lift coefficient of 0.59, and with a maximum thickness-to-chord ratio of about 0.10. The aerodynamic characteristics of this airfoil were then measured in the Langley 8-Foot Transonic Pressure Tunnel to evaluate experimentally the validity of the design technique. Reference 30 presents the results of the experiment and compares them with the aerodynamic characteristics of the improved supercritical airfoil 26a, which was experimentally designed for similar design conditions.

Three major conclusions were reached: (1) except for slight degradation at off-design conditions (drag creep and reduced drag divergence Mach numbers at low  $c_n$ ), the experimental aerodynamic characteristics of the theoretical airfoil compared well with those of the experimentally designed airfoil; (2) undue emphasis on a single-point shockless design goal would more than likely compromise off-

design characteristics—a more realistic design goal would be a minimum wave loss design point that would also provide acceptable off-design characteristics; and (3) the complex hodograph design method could be a valuable design tool if used in conjunction with an adequate analysis program to evaluate off-design characteristics.

Theoretical and experimental results of several other airfoils designed by use of the complex hodograph method of reference 29 are reported in references 31 and 32.

#### **Theoretical Drag Calculations**

The airfoil analysis code described in reference 29 gained wide acceptance for the prediction of twodimensional pressure distributions but was based on a nonconservative form (NCF) of the equation for the velocity potential describing transonic flow. As discussed by Garabedian (refs. 33 and 34), however, the NCF method fell short of giving an adequate prediction of drag-rise Mach numbers because of erroneous positive terms in the artificial viscosity. The shock jumps defined by the NCF method created mass instead of conserving it (see, also, ref. 35), resulting in overprediction of the wave drag, especially in the case of large supersonic zones. A correction was made to this "old" analysis code to account for the mass generated by the NCF method, leading to a more satisfactory evaluation of the wave drag. In addition to the corrected wave drag formulation, an accelerated iteration scheme developed by Jameson (ref. 36) was incorporated to reduce computation time. A comparison between experimental drag characteristics and theoretical drag characteristics derived from the improved "new" analysis code for the interim supercritical airfoil 27 is presented in reference 37. Results (representative results shown in fig. 16) indicate that the "new" version of the analysis code provides more accurate predictions of drag rise and suggest a good cookbook method of applying the new code.

#### **General Design Guidelines**

During the experimental development of these phase 1 airfoils, design guidelines were recognized that yielded the best compromises in drag characteristics over a range of test conditions.

The first guideline, referred to as the sonic plateau, is that at some incremental normal-force coefficient and Mach number below the design conditions the pressure distribution on the upper and lower surfaces be flat with the upper-surface pressures just below the sonic value. A generalized off-design sonic-plateau pressure distribution on a representative supercritical airfoil is presented in figure 17. The increment in normal-force coefficient was a function of the design normal-force coefficient and appeared to be about -0.25 to -0.30 for  $c_n = 0.70$ . The increment in Mach number was just enough to reduce the upper-surface pressures to below sonic velocity. This "sonic plateau" was an off-design condition that was observed to be consistent with the best compromise between design and off-design drag characteristics over a wide range of conditions. Whenever off-design drag characteristics were sacrificed in order to enhance the design drag characteristics, deviation from a flat, sonic plateau was observed. Toward the end of the experimental phase 1 airfoil development effort, judgments as to the suitability of various model modifications were generally made on the basis of two experimental data points—the design condition and the off-design sonic-plateau condition.

On the upper surface the sonic plateau extends from near the leading edge to the start of the aft pressure recovery and on the lower surface from near the leading edge to the recompression region entering into the cusp. The rearward extent of the upper-surface plateau is determined by a second design guideline that requires the gradient of the aft pressure recovery be gradual enough to avoid local separation problems near the trailing edge for lift coefficients and Mach numbers up to the design point. Consequently, the rearward extent of the upper-surface plateau would depend on thickness ratio since the thicker the airfoil, the higher the induced velocities from which the flow must recover and, therefore, the farther forward the aft pressure recovery must begin.

A third design guideline requires that the airfoil have sufficient aft camber so that at design conditions the angle of attack be about zero. This prevents the location of the upper-surface crest (position of zero slope) from being too far forward with the negative pressure coefficients over the midchord acting over a rearward-facing surface. Both experiments and theoretical analyses have indicated that an increase in angle of attack to positive values results in an abrupt increase in wave drag. A generalized design pressure distribution on a representative supercritical airfoil is presented in figure 18.

The aft camber results in a concave region near the trailing edge on the lower surface with positive pressures, producing negative pitching moments and increased hinge moments, while the physical concavity reduces the structural depth of the flap or aileron. As noted in reference 38, however, both experimental and calculated results have indicated that these positive pressures are important in achieving a high drag-rise Mach number. The depth of the concavity must, therefore, be a compromise based on a number of considerations. A fourth design guideline specifies a gradually decreasing velocity in the supercritical flow region over the upper surface. This usually results in the highest drag-rise Mach number for a given design lift coefficient. Also, the highest usable drag rise or lift coefficient is generally obtained with a weak shock wave at the end of the supercritical region (ref. 38). Permitting a weak shock rather than trying to design for a shock-free design point also reduces the off-design penalties usually associated with "point design" airfoils.

#### Analytically Designed Supercritical Airfoils

Based on the general design guidelines discussed above, two supercritical airfoils (fig. 19) were designed (circa 1975)—the 10-percent-thick airfoil 33 reported in reference 39 and the 14-percent-thick airfoil reported in reference 40. The design normalforce coefficient was 0.7 for both airfoils. An iterative computational design process was used that consisted of altering the airfoil coordinates until the viscous airfoil analysis program of reference 29 indicated that the aforementioned design criteria had been satisfied. Until this point in the development of supercritical airfoils, design had been totally dependent on experimental methods and was extremely tedious, time consuming, and expensive. The design of these two airfoils by using the numerical code and the experimental verification of the results was intended to demonstrate that airfoils could be reliably designed by computational methods, thus reducing the cost and wind-tunnel time of developing supercritical airfoils.

Figure 20 presents sketches of the experimentally developed airfoil 31 and the analytically designed airfoil 33, and figures 21 and 22 compare the experimental pressure distributions nearest to the off-design sonic-plateau and design conditions for the two airfoils. To obtain airfoil 33, the ordinates of airfoil 31 were modified over the forward upper and lower surfaces, decreased over the rear upper surfaces, and increased in the vicinity of 80 percent chord on the lower surface. Referring to the experimental pressure distributions that approach the off-design sonicplateau criterion (fig. 21), the alterations over the upper surface and forward lower surface were necessary to obtain the desired plateau pressure distribution and to reduce the upper-surface aft pressure recovery gradient. The ordinates on the rear lower surface were increased, with the maximum increase at 80 percent, to provide increased depth for control surface and flap structural requirements. Subtracting from the upper surface and adding to the lower surface over the aft portion of the airfoil in this manner reduced the aft camber and, therefore, increased the

angle of attack required to achieve a given normalforce coefficient. The modifications also had to assure that the angle-of-attack design guideline had been met, that is, that the angle of attack required for the design normal-force coefficient of 0.7 remain near  $0^{\circ}$ .

Since the best drag-rise characteristics are often obtained on airfoils with a small amount of uppersurface trailing-edge separation and since theoretical treatments of the flow at trailing-edge regions are generally unreliable, theoretically predicted flow separation at 98 percent chord was accepted during the design process. Attempts to achieve a more rearward location of theoretical separation by reducing the aft pressure recovery gradient would have forced the rear terminus of the sonic plateau forward, resulting in higher induced velocities in the plateau region and a probable reduction in drag-rise Mach number. Relaxing the separation requirements in this manner during the design process proved to be reasonable since the computational results generally overpredicted separation and separation was not observed in the experimental data. The upper-surface sonic plateau extended from approximately 3 to 80 percent chord on the 10-percent-thick airfoil and from approximately 5 to 66 percent chord on the 14-percentthick airfoil.

The experimental results (refs. 39 and 40) showed that the 10-percent-thick airfoil 33 and the 14-percent-thick airfoil had good drag-rise characteristics over a wide range of normal-force coefficients with no measurable shock losses up to the Mach numbers at which drag divergence occurred for normal-force coefficients up to 0.7. The dragrise characteristics of the computationally designed, 10-percent-thick airfoil 33 are compared with those of the earlier experimentally designed airfoil 31 in figure 23 and with those of the analytically designed 14-percent-thick airfoil in figure 24.

Reference 41 documents the low-speed characteristics of the 14-percent-thick airfoil obtained in the Langley Low-Turbulence Pressure Tunnel. This airfoil demonstrated excellent low-speed qualities and achieved unflapped  $c_{l,\max} = 2.22$  at  $R_c = 12 \times 10^6$ . Reference 42, which discusses the status of

Reference 42, which discusses the status of NASA's airfoil research program in 1975, includes information on the status of supercritical airfoils during that time period.

#### Matrix of Phase 2 Supercritical Airfoils

The experimental verification of the design guidelines or "target pressure distributions" and the success with which two airfoils were designed using computational methods prompted the design of a matrix of family-related airfoils, all based on the guidelines described above and referred to as the supercritical phase 2 airfoils.

Figures 25 and 26 show the matrix of the airfoils that were designed and indicate the various applications to which they may be applied. The solid symbols indicate the airfoils that have been tested. The 10- and 14-percent-thick airfoils, as discussed above, were tested in the Langley 8-Foot Transonic Pressure Tunnel and reported in references 39 and 40. The three 6-percent-thick airfoils were tested in the Langley 6- by 28-Inch Transonic Tunnel. The results of the 6-percent-thick airfoils also verified the analytical design process but are unpublished. Airfoil coordinates, along with sketches of the airfoils, are presented in tables II through XXII. Even though the codes would have permitted definition of coordinates to more decimal places than shown in these tables, it was felt that the development program was still essentially an experimental process, and, except for the thinner airfoils, no attempt was made to define the vertical coordinates to less than y/c = 0.0001. Attention is called to the fact that the coordinates are not presented relative to conventional chord lines. To simplify comparisons between supercritical airfoils, it was the custom to present coordinates relative to a common reference line rather than the standard method of defining airfoils relative to a reference chordline connecting the leading and trailing edges.

Design conditions for each airfoil were established by specifying maximum thickness and lift coefficient and letting the Mach number "float" to assume whatever value was required to achieve the generalized design and off-design pressure distributions shown in figures 17 and 18. Figures 27 and 28 show representative off-design sonic-plateau pressure distributions for some of the airfoils and indicate the design lift coefficient and the Mach numbers at which the sonic plateaus occurred. Figure 29 shows the analytical drag divergence Mach numbers and includes the measured drag divergence Mach numbers for the 10- and 14-percent-thick airfoils designed for  $c_1 =$ 0.70 discussed above. Drag divergence Mach number was defined as the point where the slope-of the curve of section drag coefficient as a function of Mach number equals 0.1,  $dc_d/dM = 0.1$ . Figure 30 shows how the leading-edge radius of the airfoils varies with maximum thickness and indicates the variation to be parabolic in nature.

All airfoils were assumed to be fully turbulent during the design process with transition at 3 percent chord. For airfoils less than 6 percent thick, chord Reynolds number was specified to be  $10 \times 10^6$ . For airfoils 6 percent thick or more, chord Reynolds number was specified to be  $30 \times 10^6$ . These Reynolds numbers were felt to be representative of the probable applications for the airfoils.

If airfoils with thickness ratios intermediate to those presented in tables II to XXII are desired, and changes in thickness ratios are not more than 1 or 2 percent, the ordinates can be linearly scaled or interpolated from these tables without seriously altering the gradients of the theoretical pressure distributions. The two symmetrical airfoils shown in the matrix were developed by wrapping the thickness distribution of the least-cambered airfoil of each thickness ratio around the reference line, filling in the resultant upper and lower rear cusped surfaces so that the surfaces were straight lines from about 65 percent chord to the trailing edge, and making small modifications to the coordinates to make sure that both surfaces satisfied the upper-surface sonic-plateau guideline at zero angle of attack. The 12-percent-thick symmetrical airfoil, SC(2)-0012, was tested at high Reynolds numbers in the Langley 0.3-Meter Transonic Cryogenic Tunnel, and the results were reported in reference 43. The 14-percentthick airfoil cambered for 0.7 lift coefficient was also tested at high Reynolds numbers and reported in references 44 and 45.

#### **Phase 3 Supercritical Airfoils**

There appeared to be some concern that the leading-edge radii of the supercritical airfoils were too large to be compatible with good low-speed characteristics, that the airfoils had nose down pitching moments that were too large, and that there was not enough structural depth over the rear cusp region where flaps would normally be located. After the design of the matrix of phase 2 airfoils was completed, an attempt was made to address these concerns during the late 1970's. The airfoils studied during these investigations were referred to as supercritical phase 3 airfoils.

Studies (using the same iterative computation techniques as used in the design of the phase 2 airfoils) indicated that reductions in pitching moments could be achieved by thickening the airfoil in the vicinity of the rear lower surface and undercutting the forward lower surface without significantly degrading the airfoil performance at design conditions. Undercutting the forward lower surface also resulted in an effectively smaller leading-edge radius.

Figure 31 compares sketches of the original 12-percent-thick phase 2 supercritical airfoil designed for 0.7 lift coefficient and the same airfoil with the forward lower surface undercut. Figure 32 indicates that the upper surface was relatively unaffected at design conditions by this modification. The curvatures over the lower surface where the undercut sur-

face fairs back into the original airfoil are increased, resulting in higher velocities in the midchord region and slightly reduced pitching moments at a more negative angle of attack. Removing material in this manner increases curvature at the ends of the removal area and decreases curvature in the middle of the area and has a "water bed" effect on the velocities: velocities go up in one place but go down somewhere else.

Thickening the aft region of the airfoil by about 9 percent of the original thickness at 80 percent chord (fig. 33) to approximately the same thickness as a NACA 65-series airfoil by filling in the lower-surface cusp also resulted in a small decrease in pitching moment (fig. 34) but required a slightly higher angle of attack to achieve the same lift coefficient. More recent studies (ref. 46, for example) have indicated that substantial thickening of supercritical-type airfoils in the vicinity of 80 percent chord would be possible without sacrificing transonic performance.

In order to evaluate such modifications experimentally, the existing 14-percent-thick model used in the low-speed evaluation of SC(2)-0714 was modified and tested at low speeds in the Langley Low-Turbulence Pressure Tunnel. Figure 35 shows sketches of the two airfoils and figures 36 and 37 compare the theoretical pressure distributions at the design and sonic-plateau conditions. The experimental results (unpublished) indicated that small reductions in leading-edge pressure peaks were achieved with the smaller leading-edge radius but that low-speed stall occurred a couple of degrees earlier and the maximum lift attained decreased from about 2.2 to 2.1. Subsequent tests of the NASA SC(3)-0714 in the Langley 0.3-Meter Transonic Cryogenic Tunnel are reported in references 47 and 48.

The effort to incorporate these phase 3 modifications into the entire matrix of phase 2 supercritical airfoils was abandoned, however, when on the thinner 6-percent-thick airfoils the increased curvature on the lower surfaces caused the lower-surface velocities to become supersonic and depart from the design guidelines that had been established.

#### **Concluding Remarks**

A concerted effort within the National Aeronautics and Space Administration (NASA) during the 1960's and 1970's was directed toward developing practical two-dimensional turbulent airfoils with good transonic behavior while retaining acceptable low-speed characteristics and focused on a concept referred to as the supercritical airfoil. This distinctive airfoil shape, based on local supersonic flow with isentropic recompression, was characterized by a large leading-edge radius, reduced curvature over the middle region of the upper surface, and substantial aft camber.

This report has summarized the NASA supercritical airfoil development program in a chronological fashion, discussed some of the airfoil design guidelines, and presented coordinates of a matrix of family-related supercritical airfoils with thicknesses of 2 to 18 percent and design lift coefficients from 0 to 1.0.

NASA Langley Research Center Hampton, VA 23665-5225 January 16, 1990

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Milestone	Date	Reference
Experimentally designed slotted SC airfoil	1964	13 (TM X-1109)
Experimentally designed integral SC airfoil	1966	
Thickened-trailing-edge experiments	1970	21 (TM X-2336)
Improved SC airfoil 26a	1972	26 (TM X-2978)
Theoretically designed SC airfoil	1973	30 (TM X-3082)
Experimentally designed SC airfoil 31	1974	28 (TM X-3203)
Analytically designed 10-percent-thick SC airfoil 33	1975	39 (TM X-72711)
Analytically designed 14-percent-thick SC airfoil	1975	40 (TM X-72712)
Matrix of phase 2 SC airfoils	1976 - 1978	
Phase 3 SC airfoils	1979	

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Table I. Major Milestones in the Development of NASA Supercritical Airfoils

	<u> </u>		 		
x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>	x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
x/c 0.000 .002 .005 .010 .020 .030 .040 .050 .060 .070 .080 .090 .100 .110 .120 .130 .140 .150 .160 .170 .180 .190 .200 .210 .220 .230 .240 .250 .260 .270 .280	(y/c) <sub>u</sub> 0.00000 .00135 .00205 .00280 .00375 .00445 .00500 .00550 .00590 .00625 .00660 .00690 .00720 .00745 .00770 .00770 .00770 .00790 .00810 .00845 .00860 .00845 .00890 .00910 .00910 .00920 .00920 .00950 .00965 .00970	0.00000 00135 00205 00280 00375 00445 00500 00550 00590 00625 00660 00690 00720 00745 00770 00745 00790 00810 00845 00845 00845 00845 00890 00900 00910 00920 00940 00950 00965	.500 .510 .520 .530 .540 .550 .560 .570 .580 .590 .600 .610 .620 .630 .640 .620 .630 .640 .650 .640 .650 .660 .700 .710 .720 .720 .720 .720 .720 .720 .720 .72	.00970 .00965 .00960 .00955 .00950 .00940 .00930 .00920 .00910 .00900 .00890 .00890 .00880 .00870 .00860 .00845 .00830 .00815 .00800 .00755 .00770 .00755 .00740 .00755 .00740 .00720 .00700 .00680 .00660 .00620 .00600 .00580	$\begin{array}{c}00915\\00900\\00885\\00870\\00855\\00840\\00820\\00800\\00780\\00780\\00760\\00735\\00710\\00685\\00660\\00635\\00610\\00585\\00610\\00585\\00510\\00585\\00510\\00435\\00410\\00435\\00410\\00385\\00360\\00335\\00310\\00285\\00260\\ \end{array}$
.280 .290 .300 .310 .320 .330 .350 .360 .370 .380 .390 .400 .410 .420 .420 .420 .440 .450 .460 .450 .460 .470 .480 .490	.00970 .00975 .00980 .00995 .00990 .00995 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .01000 .00995 .00985 .00980 .00975	00970 00975 00980 00995 00995 00995 00995 00995 00995 00995 00995 00995 00995 00985 00985 00985 00975 00955 00955 00925	.800 .810 .820 .830 .840 .850 .860 .870 .880 .900 .910 .920 .920 .930 .940 .950 .950 .960 .970 .980 .990 1.000	.00555 .00530 .00505 .00480 .00455 .00395 .00365 .00330 .00295 .00255 .00215 .00170 .00120 .00015 00045 00110 00180 00265 00360	00240 00220 00200 00180 00155 00145 00140 00140 00140 00150 00150 00160 00175 00195 00220 00250 00250 00290 00340 00470 00550

Table II. Coordinates of 2-Percent-Thick Supercritical Airfoil SC(2)-0402 Designed for 0.4 Lift Coefficient

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x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	0.00000	0.00000		.500	.01465	01330
.002	.00210	00210		.510	.01460	01310
.005	.00320	00320		.520	.01450	01280
.010	.00440	00440		.530	.01440	01250
.020	.00590	00590		.540	.01430	01220
.030	.00700	00700		.550	.01420	01190
.040	.00780 .00850	00780		.560	.01410	01160
.050 .060	.00910	00850		.570	.01400	01130
.080	.00960	00910 00960	· .	.580	.01390 .01380	01100 01060
.070	.01010	01010		.600	.01365	01020
.090	.01050	01050		.610	.01355	00980
.100	.01090	01090		.620	.01335	00940
.110	.01130	01130		.630	.01320	00900
.120	.01160	01170		.640	.01305	00860
.130	.01190	01200		.650	.01290	00820
.140	.01220	01230		.660	.01275	00780
.150	.01250	01260		.670	.01260	00740
.160	.01270	01290		.680	.01240	00700
.170	.01290	01310		.690	.01220	00660
.180	.01310	01330		.700	.01200	00620
.190	.01330	01350		.710	.01180	00580
.200	.01350	01370		.720	.01160	00540
.210	.01365	01390		.730	.01140	00500
.220	.01380 .01395	01410		.740	.01120 .01100	00460
.230	.01395	01430		.750 .760	.01100	00420 00380
.240	.01410	01440 01450		.770	.01050	00340
.250	.01430	01460		.780	.01025	00300
.270	.01440	01470		.790	.01000	00260
.280	.01450	01480		.800	.00975	00220
.290	.01460	01490		.810	.00950	00180
.300	.01470	01500		.820	.00920	00150
.310	.01475	01500		.830	.00890	00120
.320	.01480	01500		.840	.00860	00090
.330	.01485	01500		.850	.00830	00060
.340	.01490	01500		.860	.00790	00040
.350	.01495	01500		.870	.00750	00020
.360	.01500	01500		.880	.00710	.00000
.370	.01500	01500		.890	.00620	.00010 .00020
.380	.01500	01500			.00570	
.390	.01500 .01500	01490 01480		.910	.00510	.00020
.400	.01500	01470		.930	.00450	.00000
.410	.01500	01460		.940	.00380	00020
.430	.01500	01450		.950	.00310	00050
.440	.01495	01440		.960	.00230	00090
.450	.01490	01430		.970	.00150	00140
.460	.01485	01410		.980	.00060	00200
.470	.01480	01390		.990	00030	00280
.480	.01475	01370		1.000	00130	00370
.490	.01470	01350				

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Table III. Coordinates of 3-Percent-Thick Supercritical Airfoil SC(2)-0403Designed for 0.4 Lift Coefficient

<b>r</b>			_			
x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	0.00000	0.00000	1	.500	.01430	- 01280
.002	.00210	00210		.510		01380
.005	.00320	00320	ĺ	.520	.01420 .01410	01360
.010	.00430	00430		.520		01340
.020	.00570	00570			.01400	01320
.030	.00680			.540	.01390	01300
.040	.00760	00680		.550	.01375	01270
.050	.00830	00760		.560	.01360	01240
.060	.00890	00830		.570	.01345	01210
.070	.00950	00890		.580	.01330	01180
.080		00950		.590	.01315	01150
.090	.01000	01000		.600	.01300	01120
.100	.01050	01050		.610	.01280	01090
.110	.01090	01090		.620	.01260	01060
.110	.01130	01130		.630	.01240	01030
	.01170	01170		.640	.01220	00990
.130	.01200	01200		.650	.01200	00950
.140	.01230	01230		.660	.01180	00910
.150	.01260	01260		.670	.01160	00870
.160	.01285	01290		.680	.01140	00830
.170	.01310	01310		.690	.01115	00790
.180	.01330	01330		.700	.01090	00750
.190	.01350	01350		.710	.01065	00710
.200	.01370	01370		.720	.01040	00670
.210	.01390	01390		.730	.01015	00630
.220	.01405	01410		.740	.00990	00590
.230	.01420	01430		.750	.00960	00550
.240	.01435	01440		.760	.00930	00510
.250	.01450	01450		.770	.00900	00480
.260	.01460	01460		.780	.00870	00450
.270	.01470	01470		.790	.00840	00420
.280	.01480	01480		.800	.00810	00390
.290	.01485	01490		.810	.00770	00360
.300	.01490	01500		.820	.00730	00330
.310	.01495	01510		.830	.00690	00310
.320	.01500	01510		.840	.00650	00290
.330	.01500	01510		.850	.00610	00270
.340	.01500	01510		.860	.00560	00260
.350	.01500	01510		.870	.00510	00250
.360	.01500	01510		.880	.00460	00250
.370	.01500	01510		.890	.00400	00250
.380	.01500	01510		.900	.00400	
.390	.01500	01510		.910	.00340	00260 00280
.400	.01495	01510	1	.920	.00200	
.410	.01490	01500		.920	.00120	00300
.420	.01485	01490		.940	.000120	00330 00370
.430	.01480	01480		.940	00040	
.440	.01475	01470		.960	00150	00420
.450	.01470	01460		.900	00150	00480
.460	.01465	01450		.970		
.470	.01460	01440		.980	00360	00630
.480	.01450	01420		1.000	00470	00720
.490	.01440	01400		1.000	00590	00830
	.01440	.01400	L			

### Table IV. Coordinates of 3-Percent-Thick Supercritical Airfoil SC(2)-0503 Designed for 0.5 Lift Coefficient

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x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>
0.000	0.00000	0.00000		.500	.01970	01790
.002	.00280	00280		.510	.01960	01760
.005	.00430	00430		.520	.01950	01730
.010	.00590	00590		.530	.01940	01695
.020	.00800	00800		.540	.01930	01655
.030	.00950 .01060	00950		.550	.01920	01615
.040	.01155	01060 01155		.560	.01905 .01890	01575 01530
.060	.01235	01155		.570	.01875	01485
.070	.01305	01305		.590	.01860	01440
.080	.01365	01365		.600	.01845	01390
.090	.01425	01425		.610	.01830	01340
.100	.01475	01475		.620	.01810	01290
.110	.01520	01525		.630	.01790	01240
.120	.01560	01570		.640	.01770	01185
.130	.01600	01610		.650	.01750	01130
.140	.01635	01650		.660	.01730	01075
.150	.01670	01690		.670	.01705	01020
.160	.01700	01720		.680	.01680	00965
.170	.01730	01750		.690	.01655	00910
.180	.01755 .01780	01780		.700	.01630	00855 00800
.200	.01805	01810 01840		.720	.01570	00745
.210	.01825	01840		.730	.01540	00690
.220	.01845	01880		.740	.01505	00635
.230	.01865	01900		.750	.01470	00580
.240	.01885	01920		.760	.01435	00525
.250	.01900	01940		.770	.01395	00470
.260	.01915	01950		.780	.01355	00420
.270	.01930	01960		.790	.01315	00370
.280	.01945	01970		.800	.01270	00325
.290	.01955	01980		.810	.01225	00280
.300	.01965	01990		.820	.01175	00240
.310	.01975	02000		.830 .840	.01125	00200
.320	.01985 .01990	02000 02000		.840	.01070 .01015	00165 00135
.340	.01995	02000		.860	.00955	00110
.350	.02000	02000		.870	.00895	00085
.360	.02005	02000		.880	.00830	00065
.370	.02010	02000		.890	.00765	00050
.380	.02010	02000		.900	•00695 <sup>·</sup>	00040
.390	.02010	01990		.910	.00625	00040
.400	.02010	01980		.920	.00550	00045
.410	.02010	01970		.930	.00475	00055
.420	.02010	01960		.940	.00395	00075
.430	.02010	01950		.950	.00310	00105
.440 .450	.02005 .02000	01930 01910		.960 .970	.00225 .00135	00145 00200
.450	.01995	01910		.970	.00135	00265
.470	.01990	01870		.990	00050	00345
.480	.01985	01850		1.000	00150	00435
.490	.01980	01820				
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Table V. Coordinates of 4-Percent-Thick Supercritical Airfoil SC(2)-0404Designed for 0.4 Lift Coefficient

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	••••••••••••••••••••••••••••••••••••••				
x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>	x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	0.0000	0.0000	.500	.0290	0271
.002	.0043	0043	.510	.0288	0267
.005	.0064	0064	.520	.0286	0263
.010	.0089 .0122	0089	.530	.0284	0258
.030	.0122	0122 0144	.540	.0282	0253
.040	.0161	0144	.550	.0279	0248
.050	.0175	0175	.560	.0276	0243
.060	.0187	0187	.580	.0273	0237 0231
.070	.0198	0197	.590	.0267	0225
.080	.0207	0206	.600	.0263	0219
.090	.0215	0215	.610	.0259	0213
.100	.0223	0223	.620	.0255	0207
.110	.0230	0230	.630	.0251	0201
.120	.0236 .0242	0237	.640	.0247	0195
.140	.0242	0243	.650	.0242	0188
.150	.0253	0249 0254	.660	.0237	0181
.160	.0258	0259	.680	.0232	0174
.170	.0262	0264	.690	.0222	0167 0160
.180	.0266	0268	.700	.0217	0153
.190	.0270	0272	.710	.0211	0146
.200	.0273	0276	.720	.0205	0139
.210	.0276	0279	.730	.0199	0132
.220	.0279	0282	.740	.0193	0125
.230 .240	.0282	0285	.750	.0187	0118
.240	.0285	0288	.760	.0181	0111
.260	.0289	0290 0292	.770	.0174	0104
.270	.0291	0294	.790	.0167	0097
.280	.0293	0296	.800	.0160 .0153	0090 0084
.290	.0295	0297	.810	.0146	0078
.300	.0296	0298	.820	.0139	0072
.310	.0297	0299	.830	.0132	0066
.320	.0298	0300	.840	.0124	0060
.330	.0299	0301	.850	.0116	0055
.340	.0300	0301	.860	.0108	0050
.360	.0301 .0301	0301 0301	.870	.0100	0045
.370	.0301	0301	.880	.0092	0041
.380	.0301	0300	.900	.0084	0037 0034
.390	.0301	0299	.910	.0068	0031
.400	.0301	0298	.920	.0059	0029
.410	.0301	0297	.930	.0050	0028
.420	.0300	0295	.940	.0041	0028
.430	.0299	0293	.950	.0032	0029
.440	.0298	0291	.960	.0023	0031
.450 .460	.0297 .0296	0288 0285	.970	.0014	0034
.480	.0295	0285	.980 .990	.0004	0039
.480	.0294	0279	1.000	0006 0016	0046 0055
.490	.0292	0275			0055

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Table VI. Coordinates of 6-Percent-Thick Supercritical Airfoil SC(2)-0406 Designed for 0.4 Lift Coefficient

			_			
x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>
0.000	0.0000	0.0000	ľ	.500	.0288	0270
.002	.0043	0043		.510	.0286	0266
.005	.0065	0065		.520	.0284	0262
.010	.0088	0088		.530	.0282	0257
.020	.0119	0119		.540	.0280	0252
.030	.0140	0140		.550	.0277	0247
.040	.0157	0157	1	.560	.0274	0241
.050	.0171	0171		.570	.0271	0235
.060	.0183	0183	- 1	.580	.0268	0229
.070	.0194 .0204	0194 0204		.590 .600	.0265	0223 0217
.080	.0213	0213	1	.610	.0259	0211
.100	.0221	0221		.620	.0255	0205
.110	.0228	0229		.630	.0251	0199
.120	.0235	0236		.640	.0247	0192
.130	.0241	0242		.650	.0243	0185
.140	.0247	0248		.660	.0239	0178
.150	.0252	0253		.670	.0234	0171
.160	.0257	0258		.680	.0229	0164
.170	.0262	0263		.690	.0224	0157
.180	.0266	0267		.700	.0219	0150
.190	.0270	0271		.710	.0213	0143
.200	.0274	0275		.720	.0207	0136
.210	.0277	0278		.730	.0201	0129
.220	.0280	0281		.740	.0195	0122
.230	.0283	0284		.750	.0189	0115
.240	.0286	0287		.760	.0182	0108
.250	.0288	0289		.770	.0175	0101
.260	.0290	0291 0293		.780	.0168 .0161	0094
.270	.0292 .0294	0295		.790 .800	.0153	0088 0082
.280	.0294	0295		.810	.0155	0076
.300	.0295	0297		.820	.0137	0071
.310	.0297	0298		.830	.0128	0066
.320	.0298	0299		.840	.0119	0061
.330	.0299	0300		.850	.0110	0057
.340	.0300	0300		.860	.0100	0053
.350	.0300	0300		.870	.0090	0050
.360	.0300	0300		.880	.0079	0048
.370	.0300	0300		.890	.0068	0047
.380	.0300	0299		.900	.0056	0047
.390	.0300	0298		.910	.0044	0048
.400	.0300	0297		.920	.0031	0050
.410 .420	.0300	0296 0294		.930 .940	.0018 .0004	0054 0059
.420	.0299 .0298	0294		.940	0010	0066
.430	.0298	0292		.950	0025	0076
.450	.0296	0287		.970	0041	0088
.460	.0295	0284		.980	0059	0103
.470	.0294	0281		.990	0078	0120
.480	.0292	0278		1.000	0098	0139
.490	.0290	0274				

Table VII. Coordinates of 6-Percent-Thick Supercritical Airfoil SC(2)-0606 Designed for 0.6 Lift Coefficient

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(y/c)<sub>u</sub> x/c (y/c)<sub>1</sub> (y/c)<sub>u</sub> x/c  $(y/c)_1$ 0.000 0.0000 0.0000 .500 .0287 -.0270 .002 .0043 -.0043 .510 .0285 -.0266 .005 .0065 -.0065 .520 .0283 -.0261 .010 .0088 -.0088 .530 .0281 -.0256 .0117 -.0117 .020 .540 .0278 -.0251 .0138 .030 .550 .0275 -.0246 -.0155 .040 .0155 .0272 .560 -.0240 .050 .0169 -.0169 .570 -.0234 .060 .0181 -.0181 .580 .0266 -.0228 .070 .0192 -.0192 .590 .0263 -.0222 .0202 .080 -.0202 .600 .0260 -.0216 .090 .0211 -.0211 .610 .0256 -.0210 .100 .0219 -.0219 .620 .0252 -.0204 .110 .0227 -.0227 .630 .0248 -.0197 .120 .0234 -.0234 .640 -.0190 .0244 .130 .0240 -.0240 .650 .0240 -.0183 .0246 .140 -.0246 .660 .0236 -.0176 .150 .0252 -.0251 .670 .0231 -.0169 .160 .0257 -.0256 .680 .0226 -.0162 .170 .0262 -.0261 .690 .0221 -.0155 .180 .0266 -.0265 .700 .0216 -.0148 .190 .0270 -.0269 .710 -.0141 .0211 .0274 .200 -.0273 .720 .0206 -.0134 .210 .0277 -.0277 .730 .0200 -.0127 .220 .0280 -.0280 .0194 .0188 .740 -.0120 .230 .0283 -.0283 .750 -.0113 .0286 .240 .760 -.0286 .0182 -.0106 .250 .0288 -.0288 .770 .0175 ~.0099 .0290 .260 -.0290 .780 .0168 -.0093 -.0292 .270 .0292 .790 .0161 -.0087 .280 .0294 .800 .0154 -.0081 .290 .0295 -.0296 .810 .0146 -.0075 .0296 .300 -.0297 .820 .0138 -.0070 .0297 .310 -.0298 .830 -.0065 .0129 .0298 .320 -.0299 .840 .0120 -.0061 .0299 .330 -.0300 .850 .0110 -.0057 .340 .0300 -.0300 -.0054 .860 .0100 .350 .0300 -.0300 .870 .0089 -.0052 .0300 .360 -.0300 .880 .0077 -.0051 .0300 .370 -.0300 .890 .0064 -.0051 .0300 .380 -.0299 .900 .0051 -.0052 .390 .0300 -.0298 .910 .0037 -.0054 .400 .0300 -.0297 .920 -.0058 .0022 .410 .0299 -.0296 .930 .0006 -.0064 .420 .0298 -.0294 .940 -.0072 -.0011 .430 .0297 -.0292 .950 -.0029 -.0082 .440 .0296 -.0290 .960 -.0048 -.0095 .0295 .450 -.0287 .970 -.0068 -.0111 .0294 .460 -.0089 -.0284 .980 -.0130 .470 .0293 -.0281 .990 -.0112 -.0152

.480

.490

.0291

.0289

-.0278

-.0274

1.000

-.0138

-.0177

Table VIII. Coordinates of 6-Percent-Thick Supercritical Airfoil SC(2)-0706Designed for 0.7 Lift Coefficient

	~					-
x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	Ó.0000	0.0000	Ī	.500	.0254	0281
.002	.0042	0042		.510	.0249	0279
.005	.0064	0064		.520	.0244	0277
.010	.0087	0087		.530	.0239	0275 0273
.020	.0117	0117		.540	.0234 .0229	0273
.030	.0140 .0158	0140 0158		.560	.0223	0269
.040	.0174	0174		.570	.0217	0267
.050	.0188	0187		.580	.0211	0265
.070	.0200	0199		.590	.0205	0263
.080	.0211	0209		.600	.0198	0261
.090	.0221	0218		.610	.0191	0259
.100	.0230	0226		.620	.0184	0257
.110	.0238	0234		.630	.0177	0255 0253
.120	.0245	0241		.640 .650	.0169 .0161	0251
.130	.0252	0247		.660	.0153	0249
.140	.0258 .0264	0253 0259		.670	.0144	0247
.150	.0269	0264		.680	.0135	0245
.160	.0274	0269		.690	.0126	0243
.180	.0278	0273		.700	.0117	0241
.190	.0282	0277		.710	.0107	0239
.200	.0285	0281		.720	.0097	0237
.210	.0288	0284		.730	.0087	0236
.220	.0291	0287		.740	.0076	0235
.230	.0293	0290		.750	.0065	0234
.240	.0295	0292		.760	.0053 .0041	0233 0233
.250	.0297	0294		.770 .780	.0041	0233
.260	.0298	0296 0297		.780	.0015	0233
.270	.0300	0298		.800	.0001	0234
.280	.0300	0299		.810	0014	0235
.300	.0300	0300		.820	0030	0237
.310	.0300	0300		.830	0046	0239
.320	.0300	0300		.840	0063	0242
.330	.0299	0300		.850	0081	0246
.340	.0298	0300		.860	0100	0251
.350	.0297	0300		.870	0120 0141	0257
.360	.0296	0299		.880	0162	0272
.370	.0294	0298 0297	1	.900	0184	0281
.380	.0292	0296		.910	0206	0292
.400	.0288	0295		.920	0229	0305
.400	.0286	0294	1	.930	0253	0320
.420	.0283	0293	1	.940	0277	0337
.430	.0280	0292		.950	0302	0356
.440	.0277	0291	1	.960	0328	0377
.450	.0274	0290	1	.970	0355	0400
.460	.0270	0289		.980	0383 0412	0425
.470	.0266	0287	1	.990 1.000	0412	0452
.480	.0262	0285 0283	1	1.000		.0402
.490	.0256		1	L	<u>l</u>	<u> </u>

Table IX. Coordinates of 6-Percent-Thick Supercritical Airfoil SC(2)-1006 Designed for 1.0 Lift Coefficient

		-			
0					
	<u></u>				
<b></b>	l		<b></b>	1	
x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>	x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>
0.000	0.00000	0.00000	.500	.04840	04840
.002	.00760 .01160	00760 01160	.510	.04810	04810
.010	.01550	01550	.520	.04780	04780 04740
.020	.02070	02070	.540	.04700	04700
.030	.02430	02430	.550	.04650	04650
.040	.02700	02700	.560	.04600	04600
.050	.02920	02920	.570	.04550	04550
.000	.03110 .03280	03110 03280	.580	.04490	04490
.080	.03430	03430	.590	.04430	04430
.090	.03570	03570	.610	.04360 .04280	04360 04280
.100	.03690	03690	.620	.04200	04200
.110	.03800	03800	.630	.04110	04110
.120	.03900	03900	.640	.04020	04020
.130	.04000 .04090	04000 04090	.650	.03920	03920
.150	.04170	04090	.660	.03820	03820
.160	.04250	04250	.680	.03715 .03610	03715 03610
.170	.04320	04320	.690	.03505	03505
.180	.04390	04390	.700	.03400	03400
.190	.04450	04450	.710	.03295	03295
.200	.04510 .04560	04510	.720	.03190	03190
.220	.04580	04560 04610	.730	.03085	03085
.230	.04660	04660	.740	.02980	02980 02875
.240	.04700	04700	.760	.02770	02770
.250	.04740	04740	.770	.02665	02665
.260	.04780	04780	.780	.02560	02560
.270	.04810 .04840	04810	.790	.02455	02455
.280	.04840	04840 04870	.800	.02350	02350
.300	.04900	04900	.810	.02245	02245 02140
.310	.04920	04920	.830	.02035	02035
.320	.04940	04940	.840	.01930	01930
.330	.04960	04960	.850	.01825	01825
.340 .350	.04970 .04980	04970 04980	.860	.01720	01720
.350	.04990	04980	.870	.01615	01615 01510
.370	.05000	05000	.890	.01510	01510
.380	.05000	05000	.900	.01300	01300
.390	.05000	05000	.910	.01195	01195
.400	.05000 .05000	05000	.920	.01090	01090
.410	.04990	05000 04990	.930	.00985	00985
.430	.04980	04980	.940	.00880	00880 00775
.440	.04970	04970	.960	.00670	00670
.450	.04960	04960	.970	.00565	00565
.460	.04940	04940	.980	.00460	00460
.470	.04920 .04900	04920 04900	.990	.00355	00355
.480	.04900	04900	1.000	.00250	00250
• 7 90		.04070	L		

Table X. Coordinates of 10-Percent-Thick Symmetrical Supercritical Airfoil SC(2)-0010

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Table XI. Coordinates of 10-Percent-Thick Supercritical Airfoil SC(2)-0410 Designed for 0.4 Lift Coefficient

			_			
x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	0.0000	0.0000		.500	.0490	0465
.002	.0076	0076		.510	.0488	0460
.005	.0116	0116		.520	.0485	0454
.010	.0155	0155		.530	.0482	0447
.020	.0207	0207		.540	.0479	0440
.030	.0242	0242		.550	.0476	0432
.040	.0269 .0291	0269		.560	.0472	0423
.050 .060	.0310	0291 0310		.570	.0468	0413 0402
.080	.0327	0310		.580	.0459	0390
.080	.0342	0342		.600	.0454	0378
.090	.0356	0356		.610	.0449	0365
.100	.0368	0369		.620	.0443	0352
.110	.0379	0381		.630	.0437	0338
.120	.0389	0392		.640	.0431	0324
.130	.0399	0402		.650	.0425	0309
.140	.0408	0411		.660	.0418	0294
.150	.0416	0420		.670	.0411	0278
.160	.0424	0428		.680	.0404	0262
.170	.0431	0435		.690	.0396	0246
.180	.0438	0442		.700	.0388	0230
.190	.0444	0449		.710	.0380	0214
.200	.0450	0455		.720	.0372 .0363	0198
.210	.0456	0460		.740	.0353	0182
.220	.0461 .0466	0465		.740	.0345	0166 0150
.230	.0400	0470 0474		.760	.0336	0134
.240	.0474	0478		.770	.0326	0118
.260	.0478	0481		.780	.0316	0102
.270	.0481	0484		.790	.0306	0087
.280	.0484	0487		.800	.0296	0072
.290	.0487	0489		.810	.0285	0058
.300	.0489	0491		.820	.0274	0044
.310	.0491	0493		.830	.0263	0031
.320	.0493	0494		.840	.0252	0018
.330	.0495	0495		.850	.0241	0006
.340	.0496	0496		.860	.0229	.0005
.350	.0497 .0498	0497		.870 .880	.0217 .0205	.0015
.360 .370	.0498	0497 0497		.890	.0193	.0024 .0031
.370	.0500	0497		.900	.0180	
.380	.0500	0496		.910	.0167	.0037 .0041
.400	.0500	0495		.920	.0154	.0041
.410	.0500	0494		.930	.0141	.0043
.420	.0500	0492		.940	.0127	.0041
.430	.0500	0490		.950	.0113	.0037
.440	.0499	0488		.960	.0098	.0031
.450	.0498	0485		.970	.0083	.0023
.460	.0497	0482		.980	.0067	.0012
.470	.0496	0478		.990	.0050	0001
.480	.0494	0474		1.000	.0032	0017
.490	.0492	0470				

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x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>	
0.000	0.0000	0.0000		.500	.0488	0465	
.002	.0076	0076		.510	.0486	0459	
.005	.0116 .0155	0116 0155		.520	.0483	0453	
.020	.0206	0206		.530	.0480	0446	
.030	.0241	0241		.540 .550	.0474	0439 0431	
.040	.0268	0268		.560	.0470	0422	
.050	.0290	0290		.570	.0466	0412	
.060	.0309	0309		.580	.0462	0401	
.070	.0326	0326		.590	.0458	0390	
.080	.0341	0341		.600	.0453	0378	
.090	.0355	0355		.610	.0448	0366	
.100	.0367	0367 0379		.620	.0443	0353	
.120	.0389	0390		.630	.0438	0340 0327	
.130	.0399	0400		.650	.0426	0313	
.140	.0408	0409		.660	.0419	0299	
.150	.0417	0418		.670	.0412	0284	
.160	.0425	0426		.680	.0405	0269	
.170	.0432	0433		.690	.0397	0254	
.180	.0439	0440		.700	.0389	0238	
.190 .200	.0445	0446 0452		.710	.0381	0222	
.200	.0451 .0456	0452		.720	.0372	0206	
.220	.0461	0463		.740	.0353	0190	
.230	.0466	0468		.750	.0343	0158	
.240	.0470	0472		.760	.0332	0142	
.250	.0474	0476		.770	.0321	0126	
.260	.0478	0480		.780	.0309	0111	
.270	.0481	0483		.790	.0297	0096	
.280	.0484	0486		.800	.0285	0081	
.290 .300	.0487 .0489	0489 0491		.810	.0272	0068	
.310	.0489	0491		.820 .830	.0259	0056	
.320	.0493	0495		.840	.0245	0045 0035	
.330	.0495	0496		.850	.0216	0026	
.340	.0496	0497		.860	.0201	0018	
.350	.0497	0498		.870	.0185	0012	
.360	.0498	0498		.880	.0169	0007	
.370	.0499	0498		.890	.0153	0004	
.380	.0500	0498 0497		.900	.0136	0003	
.390	.0500	0497		.910 .920	.0119 .0101	0004	
.410	.0500	0495		.920	.0083	0007	
.420	.0500	0493		.940	.0064	0012	
.430	.0499	0491		.950	.0045	0030	
.440	.0498	0489		.960	.0025	0042	
.450	.0497	0486		.970	.0004	0056	
.460	.0496	0483		.980	0018	0073	
.470	.0494	0479		.990	0042	0093	
.480 .490	.0492 .0490	0475 0470		1.000	0067	0116	
.490	.0490	04/0	L				

Table XII. Coordinates of 10-Percent-Thick Supercritical Airfoil SC(2)-0610Designed for 0.6 Lift Coefficient

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		····	 		
x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>	x/c	(y/c) <sub>11</sub>	(y/c) <sub>1</sub>
	· · · · u	·-· · T		· · · u	1.1. T
0.000	0.0000	0.0000	.500	.0487	0465
.002	.0076	0076	.510	.0484	0459
.005	.0116	0116	.520	.0481	0453
.010	.0155	0155	.530	.0478	0446
.020	.0206	0206	.540	.0475	0438
.030	.0240	0240	.550	.0471	0430
.040	.0267	0267	.560	.0467	0421
.050	.0289	0289	.570	.0463	0411
.060	.0308	0308	.580	.0459	0401
.070	.0325	0325	.590	.0454	0390
.080	.0340	0340	.600	.0449	0379
.090	.0354	0354	.610	.0444	0367
.100	.0366	0366	.620	.0439	0355
.110	.0378	0378	.630	.0433	0342
.120	.0389	0389	.640	.0427	0329
.130	.0399	0399	.650	.0421	0315
.140	.0408	0408	.670	.0414	0301
.150	.0417	0417	.680	.0407	0287
.160	.0425	0425	.690	.0393	0272
.170	.0432	0432	.700	.0385	0257
.180 .190	.0439 .0445	0439	.710	.0377	0242 0226
.200	.0445	0446	.720	.0368	0210
.210	.0457	0452	.730	.0359	0194
.220	.0462	0458	.740	.0349	0178
.230	.0467	0468	.750	.0339	0162
.240	.0471	0472	.760	.0328	0147
.250	.0475	0476	.770	.0317	0132
.260	.0479	0480	.780	.0305	0117
.270	.0482	0483	.790	.0292	0103
.280	.0485	0486	.800	.0279	0089
.290	.0488	0489	.810	.0265	0076
.300	.0490	0491	.820	.0250	0064
.310	.0492	0493	.830	.0235	0053
.320	.0494	0495	.840	.0219	0044
.330	.0496	0496	.850	.0203	0036
.340	.0497	0497	.860	.0186	0030
.350	.0498	0498	.870	.0169	0026
.360	.0499	0498	.880	.0151	0023
.370	.0500	0498	.890 .900	.0133	0022
.380	.0500	0498	.900	.0114	0023
.390	.0500	0497	.910	.0095	0026
.400	.0500	0496	.930	.0075	0032 0040
.410	.0500	0495	.940	.0033	
.420	.0499	0493	.950	.0033	0050 0063
.430	.0498	0491 0489	.960	0012	0078
.440	.0497	0489	.970	0036	0078
.450	.0495	0488	.980	0062	0117
.400	.0493	0479	.990	0090	0141
.480	.0491	0475	1.000	0119	0168
.490	.0489	0470			
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Table XIII. Coordinates of 10-Percent-Thick Supercritical Airfoil SC(2)-0710Designed for 0.7 Lift Coefficient

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F		· · · · · · · · · · · · · · · · · · ·				
						$\leq$
			1		T	T
x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	0.0000	0.0000		.500	.0455	0454
.002	.0076 .0116	0076		.510	.0449	0449
.010	.0116	0116		.520	.0443	0444
.020	.0207	0156 0207		.530	.0437	0439
.030	.0242	0242		.540	.0430	0434 0428
.040	.0270	0270		.560	.0416	0428
.050	.0294	0294		.570	.0408	0416
.060	.0315	0314		.580	.0400	0410
.070	.0333	0332		.590	.0391	0404
.090	.0349 .0364	0348		.600	.0382	0398
.100	.0378	0362 0375		.610	.0373	0392
.110	.0390	0375		.620 .630	.0363	0386 0380
.120	.0401	0398		.640	.0342	0374
.130	.0412	0408	1	.650	.0330	0367
.140	.0422	0418		.660	.0318	0360
.150	.0431	0427		.670	.0305	0353
.160 .170	.0439	0435		.680	.0292	0346
.170	.0447	0443		.690	.0278	0339
.190	.0460	0450 0457		.700 .710	.0264	0332
.200	.0466	0463		.720	.0233	0325 0319
.210	.0471	0468		.730	.0217	0313
.220	.0476	0473		.740	.0200	0307
.230	.0480	0478		.750	.0183	0301
.240	.0484	0482		.760	.0165	0295
.250 .260	.0487	0486		.770	.0147	0290
.200	.0490	0489 0492		.780	.0128	0285
.280	.0495	0492		.790 .800	.0109	0280
.290	.0497	0496		.810	.0089	0276 0272
.300	.0498	0498		.820	.0048	0269
.310	.0499	0499		.830	.0027	0266
.320	.0500	0500		.840	.0005	0264
.330	.0500 .0500	0500		.850	0017	0263
.340	.0500	0500 0500		.860 .870	0040	0264
.360	.0499	0499		.880	0063	0267
.370	.0498	0498		.890	0087 0111	0271 0277
.380	.0497	0496		.900	0136	0285
.390	.0495	0494		.910	0161	0295
.400	.0493	0492		.920	0187	0307
.410	.0491 .0488	0489		.930	0214	0321
.420	.0488	0486		.940	0241	0337
.440	.0485	0483		.950	0269	0355
.450	.0478	0476		.970	0298 0327	0375 0398
.460	.0474	0472		.980	0327	0423
.470	.0470	0468		.990	0388	0451
.480	.0465	0464		1.000	0420	0481
.490	.0460	0459				

Table XIV. Coordinates of 10-Percent-Thick Supercritical Airfoil SC(2)-1010 Designed for 1.0 Lift Coefficient

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r			1			[ <b></b> ]
x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	0.00000	0.00000		.500	.05808	05808
.002	.00912	00912		.510	.05772	05772
.005	.01392	01392		.520	.05736	05736
.010	.01860	01860		.530	.05688	05688
.020	.02484	02484		.540	.05640	05640
.030	.02916	02916		.550	.05580 .05520	05580
.040	.03240	03240		.560 .570	.05460	05520 05460
.050	.03504	03504		.570	.05388	05388
.060	.03732	03732 03939		.590	.05316	05316
.080	.03939 .04119	04119		.600	.05232	05232
.090	.04282	04282		.610	.05136	05136
.100	.04428	04428		.620	.05040	05040
.110	.04560	04560		.630	.04932	04932
.120	.04680	04680		.640	.04824	04824
.130	.04800	04800		.650	.04704	04704
.140	.04908	04908		.660	.04584	04584
.150	.05004	05004		.670	.04458	04458
.160	.05100	05100		.680	.04332	04332
.170	.05184	05184		.690	.04206	04206
.180	.05268	05268		.700	.04080 .03954	04080
.190	.05340	05340		.710 .720	.03954	03954
.200	.05412	05412		.720	.03702	03828 03702
.210	.05472	05472		.740	.03576	03576
.220	.05532	05532 05592		.750	.03450	03450
.240	.05592	05640		.760	.03324	03324
.250	.05688	05688		.770	.03198	03198
.260	.05736	05736		.780	.03072	03072
.270	.05772	05772		.790	.02946	02946
.280	.05808	05808		.800	.02820	02820
.290	.05844	05844		.810	.02694	02694
.300	.05880	05880		.820	.02568	02568
.310	.05904	05904		.830	.02442	02442
.320	.05928	05928		.840	.02316 .02190	02316
.330	.05952	05952		.860	.02190	02190 02064
.340	.05964 .05976	05964 05976		.870	.01938	01938
.360	.05976	05988		.880	.01812	01812
.370	.06000	06000		.890	.01686	01686
.380	.06000	06000		.900	.01560	01560
.390	.06000	06000		.910	.01434	01434
.400	.06000	06000		.920	.01308	01308
.410	.06000	06000	1	.930	.01182	01182
.420	.05988	05988		.940	.01056	01056
.430	.05976	05976		.950	.00930	00930
.440	.05964	05964		.960	.00804	00804
.450	.05952	05952	1	.970	.00552	00678 00552
.460	.05928	05928	l	.990	.00426	00552
.470	.05904	05904	L	1.000	.00300	00300
.490	.05880	05844				
	L .03044		1	[		1

Table XV. Coordinates of 12-Percent-Thick Symmetrical Supercritical Airfoil SC(2)-0012

F

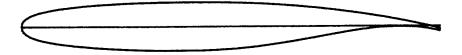
,

x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>	x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000 .002 .005 .010 .020 .030 .040 .050 .060 .070 .080 .090 .100 .110 .120 .130 .140 .150 .160 .170 .180 .190 .200 .210 .220 .240 .220 .240 .250 .240 .240 .250 .240 .240 .250 .240 .240 .250 .240 .240 .250 .240 .240 .240 .240 .240 .240 .240 .24	0.0000 .0092 .0141 .0190 .0253 .0297 .0330 .0357 .0380 .0400 .0418 .0434 .0434 .0434 .0434 .0473 .0484 .0473 .0484 .0473 .0484 .0473 .0484 .0473 .0594 .0504 .0513 .0522 .0530 .0556 .0556 .0556 .0556 .0556 .0557 .0579 .0583 .0595 .0597 .0598 .0599 .0598 .0597 .0598 .0597 .0598 .0597 .0598 .0597 .0598 .0597 .0598 .0597 .0598 .0597 .0598 .0597 .0598 .0597 .0598 .0597 .0598 .0597 .0595 .0593 .0595 .0593 .0591	$\begin{array}{c} (y/6)_1 \\ \hline 0.0000 \\ \hline .0092 \\ \hline .0141 \\ \hline .0190 \\ \hline .0253 \\ \hline .0296 \\ \hline .0329 \\ \hline .0356 \\ \hline .0379 \\ \hline .0400 \\ \hline .0418 \\ \hline .0434 \\ \hline .0449 \\ \hline .0463 \\ \hline .0476 \\ \hline .0488 \\ \hline .0499 \\ \hline .0509 \\ \hline .0518 \\ \hline .0527 \\ \hline .0518 \\ \hline .0527 \\ \hline .0555 \\ \hline .0518 \\ \hline .0527 \\ \hline .0555 \\ \hline .0561 \\ \hline .0581 \\ \hline .0585 \\ \hline .0581 \\ \hline .0585 \\ \hline .0581 \\ \hline .0585 \\ \hline .0581 \\ \hline .0591 \\ \hline .0593 \\ \hline .0593 \\ \hline .0593 \\ \hline .0597 \\ \hline .0598 \\ \hline .0599 \\ \hline .0598 \\ \hline .0599 \\ \hline .0598 \\ \hline .0599 \\ \hline .0598 \\ \hline .0598 \\ \hline .0596 \\ \hline .0592 \\ \hline .0588 \\ \hline .0588 \\ \hline .0596 \\ \hline .0592 \\ \hline .0588 \\ \hline .0586 \\ \hline .0582 \\ \hline .0573 \\ \hline .0568 \\ \hline .0562 \\ \end{array}$	x/c .500 .510 .520 .530 .540 .550 .550 .550 .570 .580 .600 .610 .620 .630 .620 .630 .620 .630 .640 .650 .640 .650 .640 .670 .710 .720 .710 .720 .740 .720 .740 .720 .740 .750 .800 .810 .820 .840 .820 .840 .850 .840 .850 .800 .840 .850 .800 .800 .810 .800 .900	$(y/c)_u$ . 0588 . 0585 . 0582 . 0578 . 0574 . 0570 . 0565 . 0565 . 0560 . 0555 . 0549 . 0543 . 0536 . 0529 . 0522 . 0514 . 0506 . 0497 . 0488 . 0479 . 0469 . 0449 . 0459 . 0449 . 0459 . 04417 . 0406 . 0394 . 0358 . 0370 . 0358 . 0345 . 0332 . 0319 . 0306 . 0292 . 0278 . 0264 . 0250 . 0205 . 0190 . 0174 . 0158 . 0142 . 0125 . 0108 . 0090 . 0072 . 0053 . 0033	$(y/c)_1$ 0555 0547 0539 0530 0520 0509 0498 0486 0473 0459 0444 0429 0413 0397 0380 0362 0344 0326 0307 0288 0269 0250 0212 0193 0174 0155 0137 0119 0122 0085 0068 0052 0037 0023 0009 .0023 .0014 .0024 .0032 .0045 .0022 .0010

 Table XVI. Coordinates of 12-Percent-Thick Supercritical Airfoil SC(2)-0412

 Designed for 0.4 Lift Coefficient

Table XVII. Coordinates of 12-Percent-Thick Supercritical Airfoil SC(2)-0612 Designed for 0.6 Lift Coefficient



				i		
x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>
Ó.000	0.0000	0.0000		.500	.0586	0554
.002	.0092	0092		.510	.0583	0546
.005	.0141	0141		.520	.0580	0538
.010	.0190	0190		.530	.0576	0529
.020	.0252	0252		.540	.0572	0519
.030	.0296	0296		.550	.0568	0509
.040	.0329	0329		.560	.0563	0497
.050	.0355	0355		.570	.0558	0485
.060	.0378	0378		.580	.0553	0472
.070	.0398	0398		.590	.0547	0458
.080	.0416	0416		.600	.0541	0444
.090	.0432	0432		.610	.0534	0429
.100	.0447	0447		.620	.0527	0414
.110	.0460	0460		.630	.0520	0398
.120	.0472	0473		.640	.0512	0382
.130	.0484	0485		.650	.0504	0365
.140	.0495	0496		.660	.0495	0348
.150	.0505	0506		.670	.0486	0330
.160	.0514	0515		.680	.0476	0312
.170	.0523	0524		.690	.0466	0294
.180	.0531	0532		.700	.0456	0276 0258
.190	.0538	0540		.710 .720	.0445 .0434	0258
.200	.0545	0547 0554		.720	.0434	0222
.210	.0551 .0557	0560		.740	.0422	0204
.220	.0563	0565		.750	.0397	0186
.240	.0568	0570		.760	.0384	0168
.250	.0573	0575		.770	.0371	0150
.260	.0577	0579		.780	.0357	0133
.200	.0581	0583		.790	.0343	0117
.280	.0585	0586		.800	.0328	0102
.290	.0588	0589		.810	.0313	0087
.300	.0591	0592		.820	.0297	0073
.310	.0593	0594		.830	.0281	0060
.320	.0595	0595		.840	.0265	0048
.330	.0597	0596		.850	.0248	0037
.340	.0599	0597		.860	.0231	0028
.350	.0600	0598		.870	.0213	0021
.360	.0601	0598		.880	.0195	0016
.370	.0602	0598		.890	.0176	0012
.380	.0602	0598	L	.900	.0157	0010
.390	.0602	0597		.910	.0137	0010
.400	.0602	0596	1	.920	.0117 .0096	0013 0018
.410	.0602	0594 0592		.930	.0098	0018
.420	.0601	0592	1	.940	.0053	0035
.430	.0600	0586	1	.960	.0031	0048
.440	.0599	0582	1	.970	.0008	0063
.450	.0598	0578	1	.980	0016	0081
.400	.0594	0573	1	.990	0041	0102
.480	.0592	0567	1	1.000	0067	0125
.490	.0589	0561	1			
L			1	L		1

Table XVIII. Coordinates of 12-Percent-Thick Supercritical Airfoil SC(2)-0712Designed for 0.7 Lift Coefficient

$\sim$							
			-				
x/c	(y/c) <sub>11</sub>	(y/c) <sub>1</sub>		x/c	(y/c) <sub>11</sub>	(y/c) <sub>1</sub>	
	ŭ				<u> </u>	±	
0.000	0.0000	0.0000		.500	.0584	0554	
.002	.0092	0092		.510	.0581	0546	
.005	.0141	0141		.520	.0577	0537	
.010	.0190	0190		.530	.0573	0528	
.020	.0252	0252		.540	.0569	0518	
.030	.0294	0294		.550	.0564	0508	
.040	.0327	0327		.560	.0559	0496	
.050	.0354	0353		.570	.0554	0484	
.060	.0377	0376		.580	.0549	0471	
.070	.0397	0396		.590	.0543	0457	
.080	.0415	0414		.600	.0537	0443	
.090	.0431	0430		.610	.0530	0429	
.100	.0446	0445		.620	.0523	0414	
.110	.0459	0459		.630	.0516	0398	
.120	.0471	0472		.640	.0508	0382	
.130	.0483	0484		.650	.0500	0366	
.140	.0494	0495		.660	.0491	0349	
.150	.0504	0505		.670	.0482	0332	
160	.0513	0514		.680	.0472	0315	
.170	.0522	0523		.690	.0462	0298	
.180	.0530	0531		.700	.0451	0280	
.190	.0537	0539		.710	.0440	0262	
.200	.0544	0546		.720	.0428	0244	
.210	.0551	0553		.730	.0416	0226	
.220	.0557	0559		.740	.0403	0208	
.230	.0562	0564		.750	.0390	0191	
.240	.0567	0569		.760	.0376	0174	
.250	.0572	0574		.770	.0362	0157	
.260	.0576	0578		.780	.0347	0141	
.270	.0580 .0584	0582 0585		.790	.0332	0125	
.280	.0584	0585		.800	.0316	0110	
.290	.0590	0588		.810 .820	.0300	0095	
.300	.0590	0593		.820	.0283	0082	
.310 .320	.0594	0595		.830	.0248	0070 0059	
.320	.0596	0596		.840	.0248	0059	
.340	.0598	0597		.860	.0230	0043	
.340	.0599	0598		.870	.0192	0038	
.360	.0600	0598		.880	.0172	0035	
.370	.0601	0598		.890	.0152	0033	
.380	.0601	0598		.900	.0131	0034	
.390	.0601	0597		.910	.0110	0036	
.400	.0601	0596		.920	.0088	0041	
.410	.0601	0594		.930	.0065	0049	
.420	.0600	0592		.940	.0042	0059	
.430	.0599	0589		.950	.0018	0072	
.440	.0598	0586		.960	0007	0087	
.450	.0596	0582		.970	0033	0105	
.460	.0594	0578		.980	0060	0126	
.470	.0592	0573		.990	0088	0150	
.480	.0590	0567		1.000	0117	0177	
.490	.0587	0561					
			L				

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Table XIX. Coordinates of 14-Percent-Thick Supercritical Airfoil SC(2)-0414Designed for 0.4 Lift Coefficient



r	r				1	
x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	0.0000	0.0000		.500	.0684	0642
.002	.0108	0108		.510	.0680	0633
.005	.0166	0166		.520	.0676	0623
.010	.0225	0225		.530	.0672	0612
.020	.0299	0299		.540	.0667	0600
.030	.0350	0350		.550	.0662	0587
.040	.0389	0389		.560	.0656	0573
.050	.0421	0421		.570	.0650	0558
.060	.0448	0448		.580	.0643	0543
.070	.0471	0472		.590	.0636	0527
.080	.0491	0493		.600	.0628	0510
.090	.0510	0512		.610	.0620	0492
.100	.0527	0529		.620	.0611	0474
.110	.0542	0545		.630	.0602	0455
.120	.0556	0560		.640	.0593	0435
.130	.0569	0573		.650	.0583	0415
.140	.0581	0585		.660	.0573	0394
.150	.0592	0597		.670	.0562	0373
.160	.0602	0608		.680	.0551	0352
.170	.0612	0618		.690	.0540	0330
.180	.0621	0627		.700	.0528	0308
.190	.0629	0636		.710	.0516	0286
.200	.0637	0644		.720	.0503	0264
.210	.0644	0651		.730	.0490	0242
.220	.0651	0658		.740	.0477	0220
.230	.0657	0664		.750	.0464	0198
.240	.0663	0670		.760	.0450	0177
.250	.0668	0675		.770	.0436	0156
.260	.0673	0680		.780	.0422	0136
.270	.0677	0684		.790	.0407	0116
.280	.0681	0688		.800	.0392	0097
.290	.0685	0691		.810	.0377	0078
.300	.0688	0694		.820	.0362	0060
.310	.0691	0696		.830	.0346	0043
.320	.0693	0698		.840	.0330	0027
.330 .340	.0695 .0697	0699		.850	.0314	0012
.340	.0699	0700 0700		.860 .870	.0298 .0281	.0001
.360	.0700	0700		.870	.0281	.0013 .0023
.370	.0701	0699		.890	.0247	.0032
.380	.0702	0698		.900	.0229	.0032
.390	.0702	0697		.910	.0229	.0044
.400	.0702	0695		.920	.0193	.0044
.410	.0702	0693		.930	.0175	.0046
.420	.0701	0690		.940	.0156	.0043
.430	.0700	0686	- 1	.950	.0137	.0038
.440	.0699	0682		.960	.0117	.0031
.450	.0697	0677		.970	.0097	.0021
.460	.0695	0672		.980	.0076	.0008
.470	.0693	0666		.990	.0055	0008
.480	.0690	0659		1.000	.0033	0027
.490	.0687	0651				
			Ľ			

 $\mathbf{34}$ 

x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>		x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>
0.000	0.0000	0.0000 0108		.500	.0681	0642 0632
.005	.0166	0166		.520	.0673	0622
.010	.0225	0225		.530	.0669	0611
.030	.0349	0298 0349		.540	.0664	0599 0586
.040	.0387	0388		.560	.0653	0572
.050	.0418	0419		.570	.0647	0557
.060	.0445	0446 0469		.580 .590	.0640	0541
.080	.0489	0490		.600	.0633	0525 0508
.090	.0508	0509		.610	.0618	0491
.100	.0525	0526		.620	.0610	0473
.120	.0541 .0555	0542 0557		.630	.0601	0455
.130	.0568	0570		.650	.0591	0436 0417
.140	.0580	0582		.660	.0570	0397
.150 .160	.0591	0594		.670	.0559	0377
.170	.0602 .0612	0605 0615		.690	.0547	0356 0336
.180	.0621	0624		.700	.0522	0315
.190	.0629	0633		.710	.0509	0294
.200	.0637 .0644	0641 0648		.720 .730	.0495	0274
.220	.0651	0655		.740	.0481	0253 0233
.230	.0657	0661		.750	.0451	0213
.240	.0663	0667		.760	.0436	0193
.250	.0668 .0673	0672 0677		.770 .780	.0420	0174
.270	.0678	0681		.790	.0404	0155 0137
.280	.0682	0685		.800	.0370	0119
.290	.0686	0688		.810	.0352	0102
.300	.0689 .0692	0691 0693		.820 .830	.0334 .0316	0086
.320	.0694	0695		.840	.0297	0072 0059
.330	.0696	0697		.850	.0278	0047
.340	.0698	0698 0699		.860 .870	.0258	0037
.360	.0700	0699		.870	.0238 .0218	0029
.370	.0701	0698		.890	.0197	0023 0019
.380	.0701	0697		.900	.0176	0017
.390	.0701 .0701	0696 0694		.910 .920	.0154	0017
.410	.0700	0692		.920	.0132 .0109	0019 0024
.420	.0699	0689		.940	.0086	0024
.430	.0698	0686		.950	.0062	0041
.440	.0696 .0694	0682 0677		.960 .970	.0038 .0013	0054
.460	.0692	0672		.980	0013	0069 0087
.470	.0690	0666		.990	0039	0108
.480	.0687	0659		1.000	0066	0132
.490	.0684	0651	L			

Table XX. Coordinates of 14-Percent-Thick Supercritical Airfoil SC(2)-0614 Designed for 0.6 Lift Coefficient

Table XXI. Coordinates of 14-Percent-Thick Supercritical Airfoil SC(2)-0714Designed for 0.7 Lift Coefficient

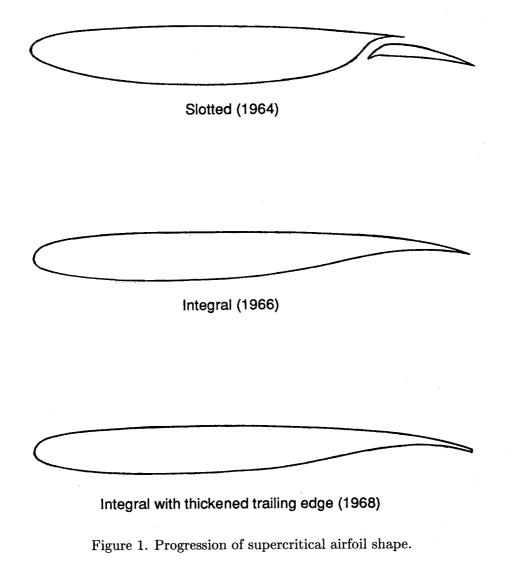
<u>,</u>			r	r	
x/c	(y/c) <sub>u</sub>	(y/c) <sub>l</sub>	x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	0.00000	0.00000	.500	.06800	06460
.002	.01077	01077	.510	.06760	05370
.005	.01658	01658	.520	.06720	06270
.010	.02240	02240	.530	.06680	06160
.020	.02960	02960	.540	.06630	06040
.030	.03460	03450	.550	.06580	05910
.040	.03830	03820	.560	.06530	05770
.050	.04140	04130	.570	.06470	05620
.060	.04400	04390	.580	.06410	05460
.070	.04630	04620	.590	.06350	05290
.080	.04840	04830	.600	.06280	05110
.090	.05020	05010	.610	.06210	04920
.100	.05190	05180	.620	.06130	04730
.110	.05350	05340	.630	.06050	04530
.120	.05490	05490	.640	.05970	04330
.130	.05620	05620	.650	.05880	04120
.140	.05740	05740	.660	.05790	03910
.150	.05860	05860	.670	.05690	03700
.160	.05970	05970	.680	.05590	03480
.170	.06070	06070	.690	.05480	03260
.180	.06160	06160	.700	.05370	03040
.190	.06250	06250	.710	.05250	02820
.200	.06330	06330 06410	.720 .730	.05130	02600
.210	.06410	06410	.730	.05000	02380
.220	.06480	06550	.740	.04870	02160
.230	.06540	06610	.760	.04730	01940
.240	.06600	06670	.770	.04580	01730
.260	.06700	06720	.780	.04430	01520 01320
.270	.06750	06770	.790	.04270	01130
.280	.06790	06810	.800	.03940	00950
.290	.06830	06850	.810	.03760	00790
.300	.06860	06880	.820	.03580	00640
.310	.06890	06910	.830	.03390	00500
.320	.06920	06930	.840	.03190	00380
.330	.06940	06950	.850	.02990	00280
.340	.06960	06960	.860	.02780	00200
.350	.06970	06970	.870	.02560	00140
.360	.06980	06970	.880	.02340	00100
.370	.06990	06970	.890	.02110	00080
.380	.06990	06960	.900	.01870	00090
.390	.06990	06950	.910	.01620	00120
.400	.06990	06930	.920	.01370	00170
.410	.06980	06910	.930	.01110	00250
.420	.06970	06880	.940	.00840	00360
.430	.06960	06850	.950	.00560	00500
.440	.06950	06810	.960	.00270	00670
.450	.06930	06770	.970	00020	00870
.460	.06910	06720 06670	.980	00320	01100
.470	.06890 .06860	06610	.990	00630	01360
.480	.06860	06540	1.000	00950	01650
.490	.00030				

Table XXII. Coordinates of 18-Percent-Thick Supercritical Airfoil SC(2)-0518Designed for 0.5 Lift Coefficient



	r	·····	<b></b>		
x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>	x/c	(y/c) <sub>u</sub>	(y/c) <sub>1</sub>
0.000	0.0000	0.0000	.500	.0867	0806
.002	.0139	0139	.510	.0860	0792
.005	.0213	0213	.520	.0853	0777
.010	.0291	0291	.530	.0845	0761
.020	.0389	0389	.540	.0837	0744
.030	.0456	0457	.550	.0828	0726
.040	.0508	0509	.560	.0819	0707
.050	.0550	0550	.570	.0809	0688
.060	.0585	0585	.580	.0798	0668
.070	.0615	0615	.590	.0787	0647
.080	.0642	0642	.600	.0775	0626
.090	.0666	0666	.610	.0763	0604
.100	.0687	0687	.620	.0750	0582
.110	.0707	0707	.630	.0737	0560
.120	.0725	0725	.640	.0724	0537
.130	.0742	0742	.650	.0710	0514
.140	.0757	0758	.660	.0696	0491
.150	.0771	0773	.670	.0681	0468
.160	.0784 .0796	0787	.680	.0666	0444
.170 .180	.0798	0799.	.690	.0650	0420
	.0818	0811	.700	.0634	0396
.190 .200	.0828	0822	.710	.0618	0372
.200	.0828	0832	.720	.0601	0348
.210	.0845	0841	.730	.0584	0324
.220	.0845	0849	.740	.0566	0300
.240	.0860	0857	.750	.0548	0276
.250	.0866	0864 0870	.760	.0530	0252
.260	.0872	0875	.780	.0492	0229 0206
.270	.0877	0880	.790	.0492	0183
.280	.0882	0884	.800	.0453	0161
.290	.0886	0888	.810	.0433	0139
.300	.0890	0891	.820	.0413	0118
.310	.0893	0893	.830	.0392	0098
.320	.0896	0895	.840	.0371	0079
.330	.0898	0896	.850	.0350	0061
.340	.0900	0897	.860	.0328	0044
.350	.0901	0897	.870	.0306	0029
.360	.0902	0896	.880	.0284	0016
.370	.0903	0895	.890	.0262	0005
.380	.0903	0893	.900	.0239	.0003
.390	.0903	0890	.910	.0216	.0009
.400	.0902	0887	.920	.0193	.0012
.410	.0901	0883	.930	.0169	.0012
.420	.0899	0878	.940	.0145	.0009
.430	.0897 .0894	0872	.950	.0120	.0003
.440	.0894	0865	.960	.0094	0007
.450 .460	.0891	0858	.970	.0068	0020
.400	.0883	0850	.980	.0041	0037
.470	.0878	0841	.990	.0014	0058
.480	.0873	0831	1.000	0014	0083
• 4 9 0	.0075	0819			

 $\mathbf{37}$ 



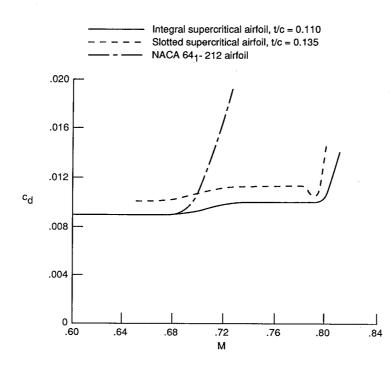


Figure 2. Variation of section drag coefficient with Mach number for section normal-force coefficient of 0.65.

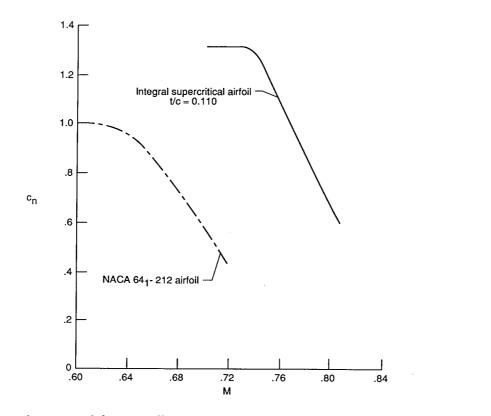


Figure 3. Variation of section normal-force coefficient with Mach number for onset of upper-surface boundarylayer separation.

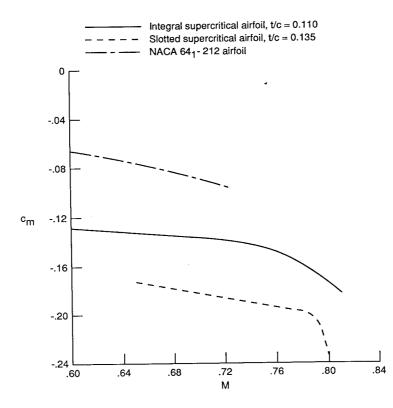


Figure 4. Variation of section pitching-moment coefficient with Mach number for section normal-force coefficient of 0.65.

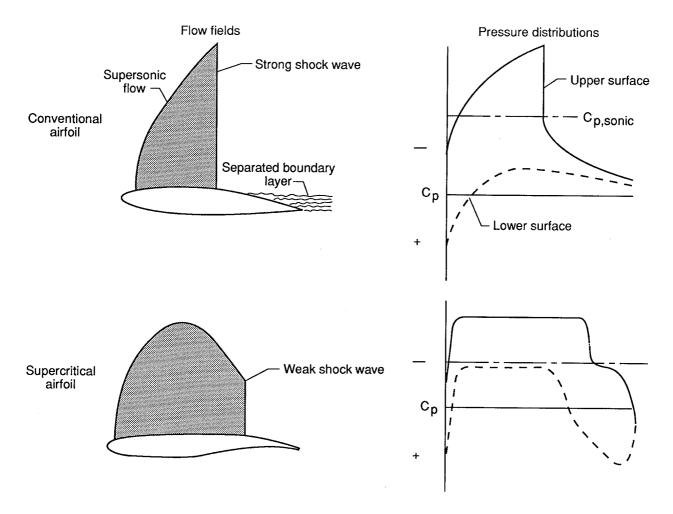


Figure 5. Flow fields around supercritical and conventional airfoils.

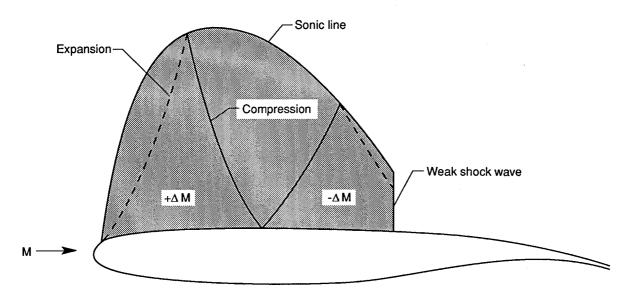
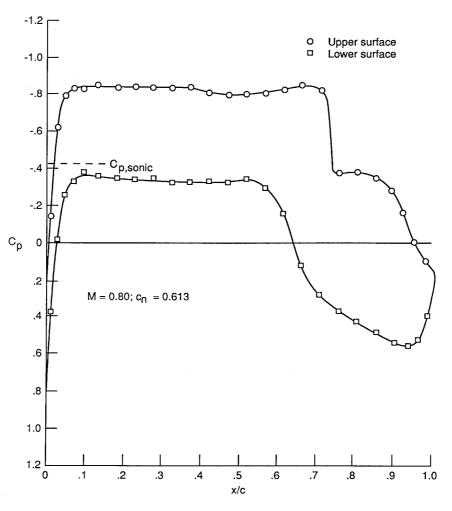


Figure 6. Schematic flow field of supercritical airfoil.



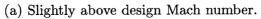
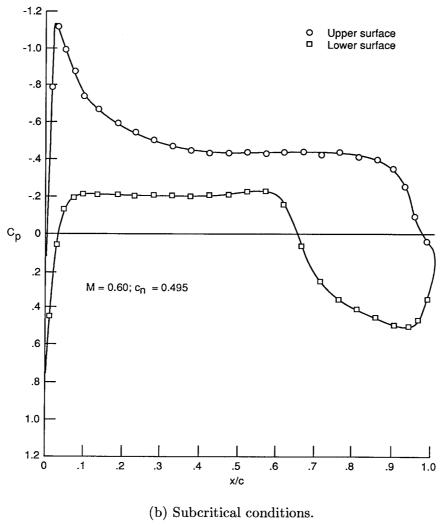
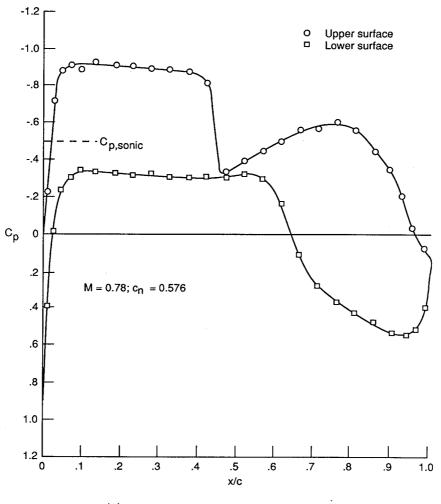


Figure 7. Chordwise pressure distributions on 11-percent-thick integral supercritical airfoil.







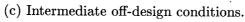
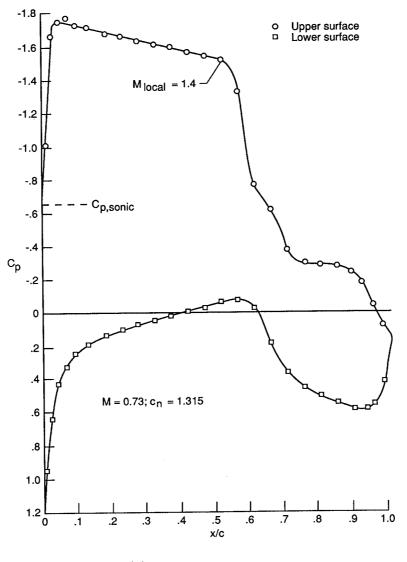
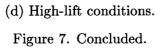


Figure 7. Continued.





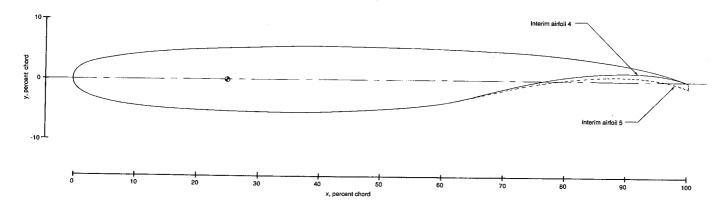


Figure 8. Sketches of 11-percent-thick interim supercritical airfoils showing sharp and blunt trailing edges.

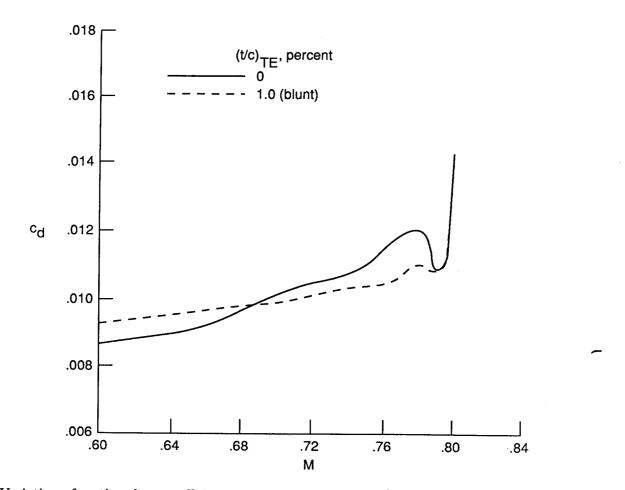
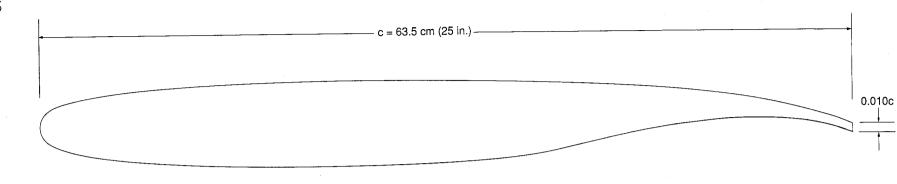
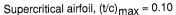


Figure 9. Variation of section drag coefficient with Mach number at a normal-force coefficient of 0.7 for the 11-percent-thick interim supercritical airfoils with sharp and blunt trailing edges.





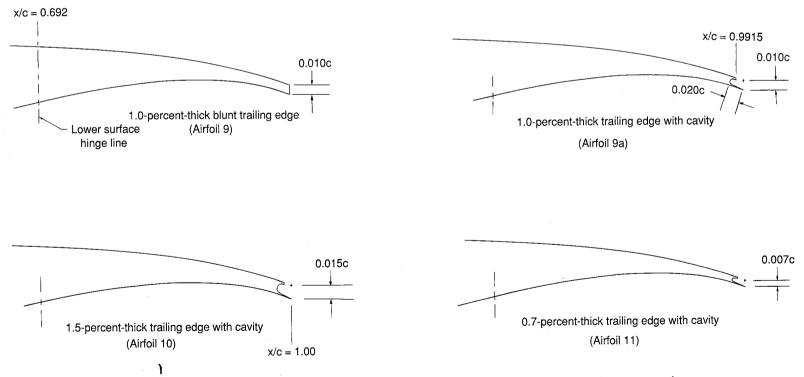


Figure 10. Sketches of refined supercritical airfoil with various trailing-edge geometries.

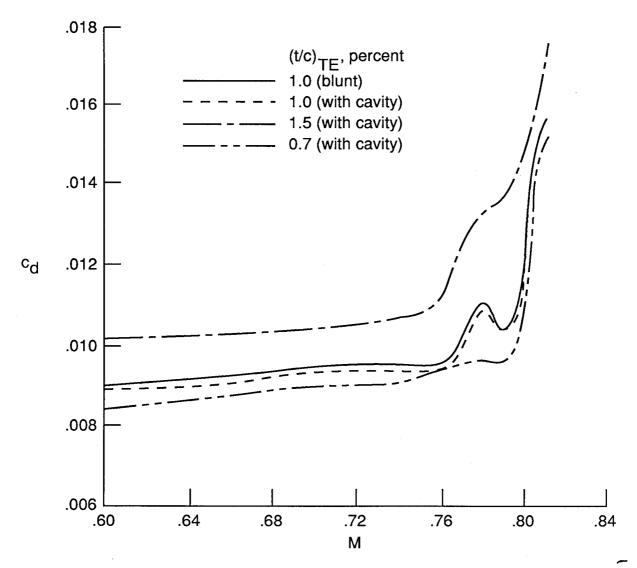


Figure 11. Effect of trailing-edge geometry on variation of section drag coefficient with Mach number at a normal-force coefficient of 0.7 for the 10-percent-thick refined supercritical airfoil.

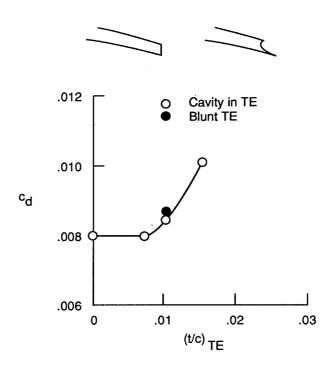


Figure 12. Effect of trailing-edge thickness on subcritical drag coefficient for 10-percent-thick refined supercritical airfoil. M = 0.60,  $c_n = 0.60$ .

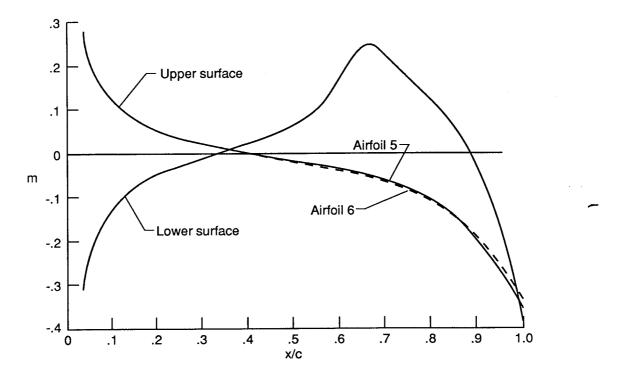
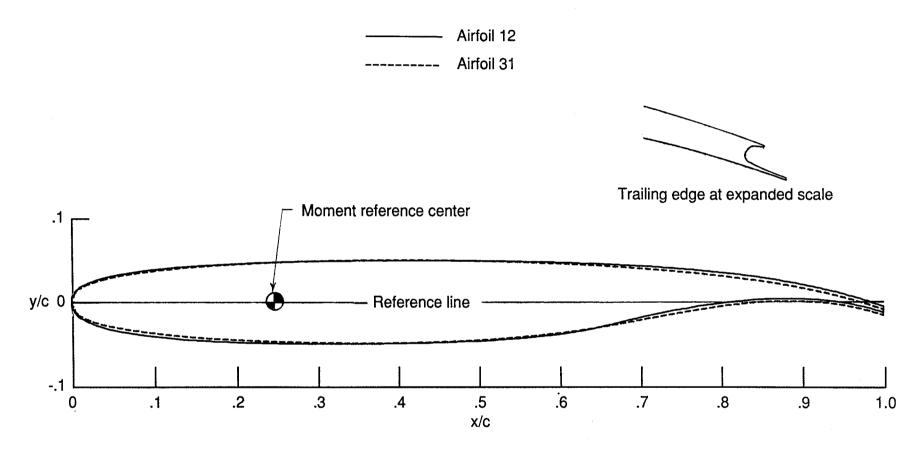


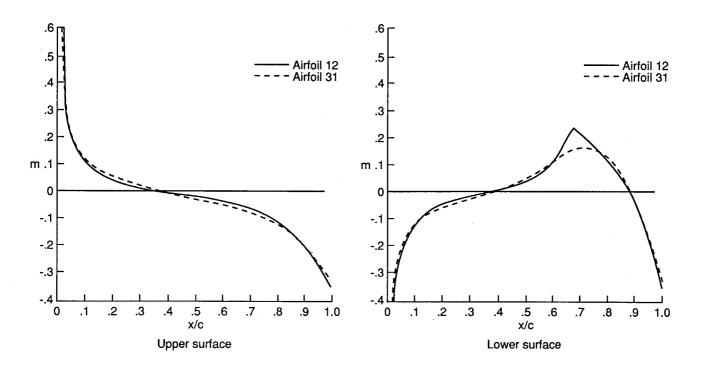
Figure 13. Chordwise distribution of slopes.



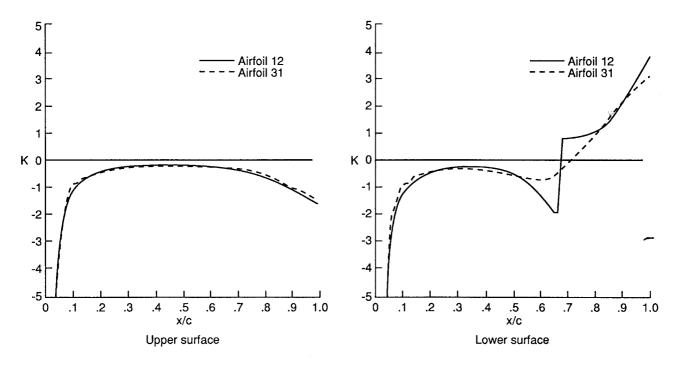
(a) Airfoil sketches.

Figure 14. Geometric characteristics of supercritical airfoils 12 and 31.

51



(b) Chordwise distribution of airfoil surface slopes.



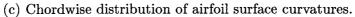


Figure 14. Concluded.

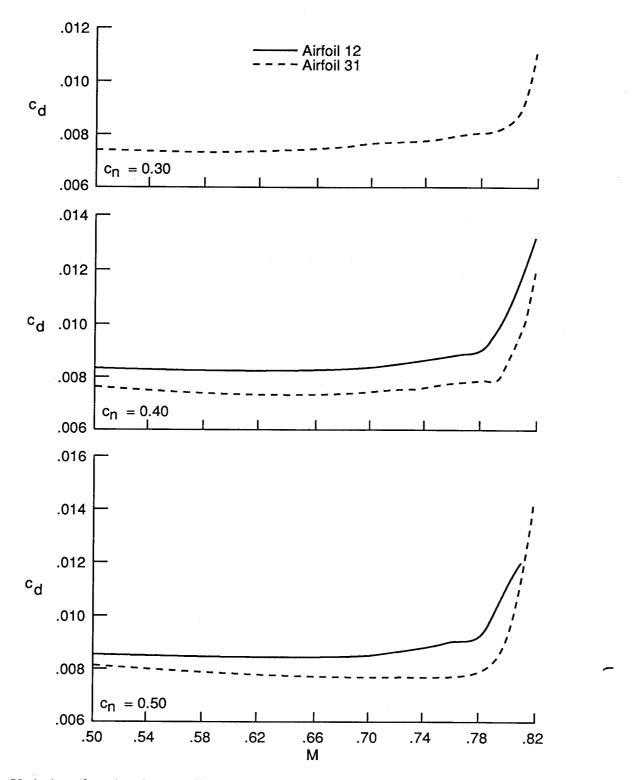


Figure 15. Variation of section drag coefficient with Mach number of supercritical airfoils 12 and 31 at various normal-force coefficients.

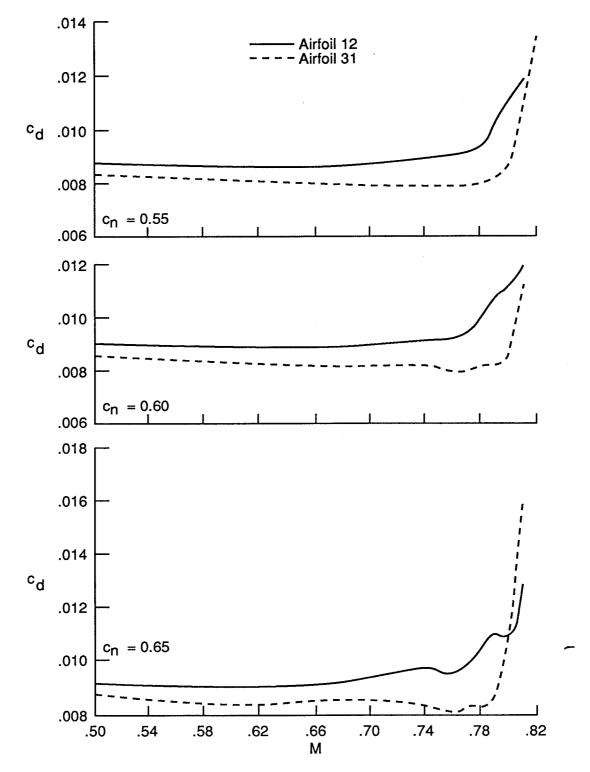


Figure 15. Continued.

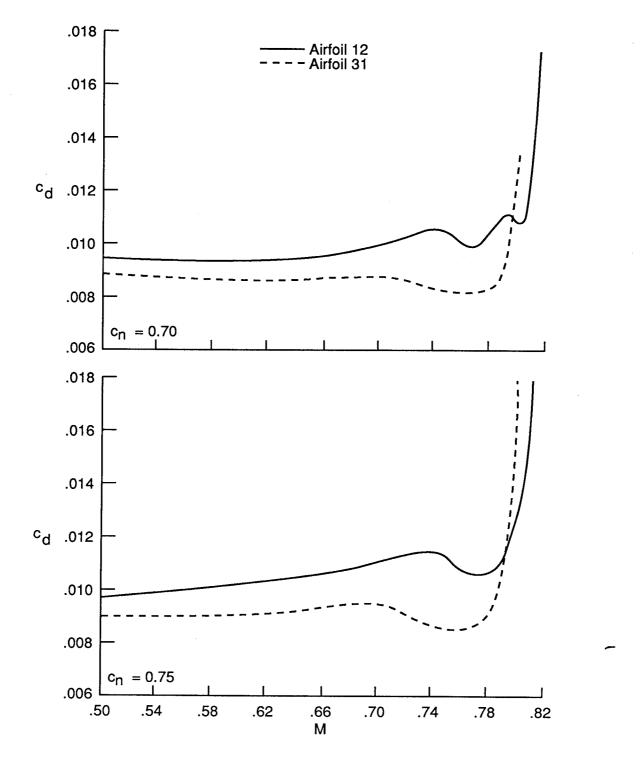


Figure 15. Continued.

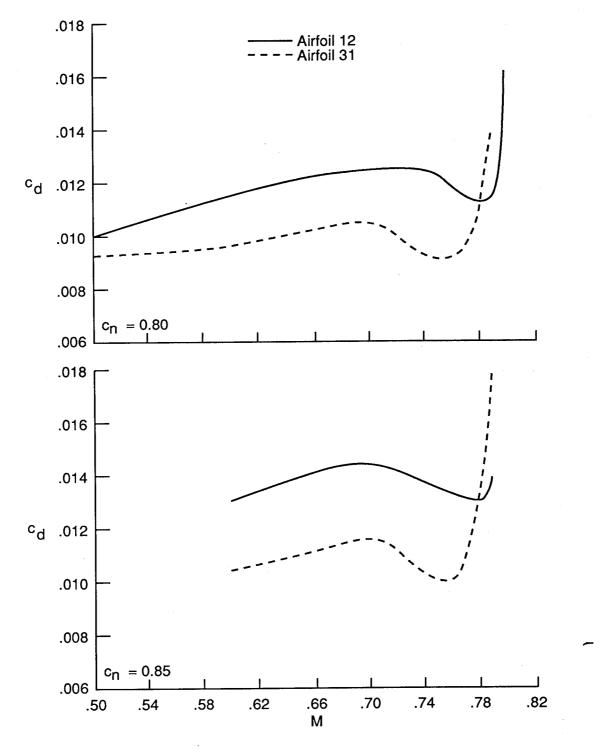


Figure 15. Continued.

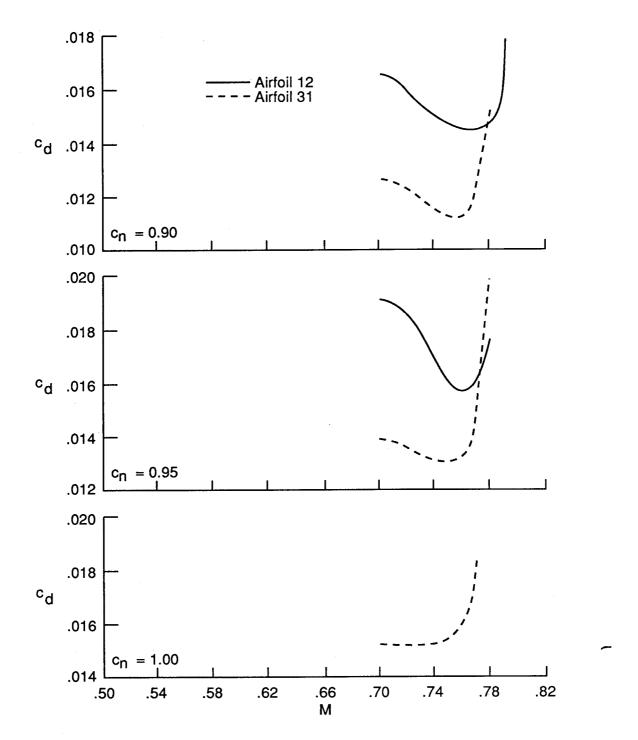


Figure 15. Concluded.

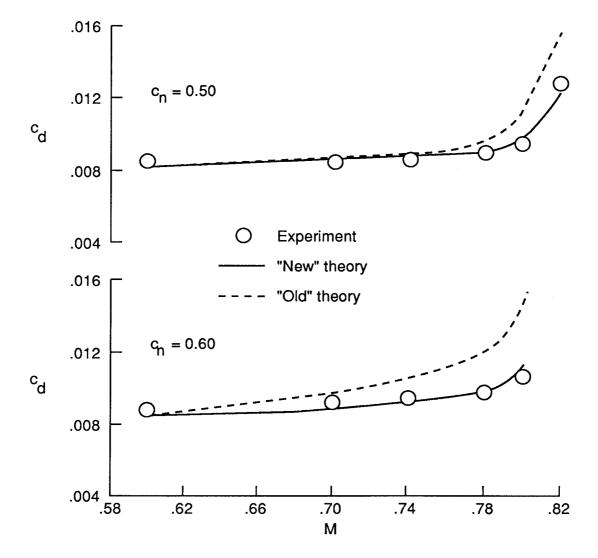


Figure 16. Comparison of experimental and analytical drag characteristics for supercritical aiffoil 27.  $R_c = 11 \times 10^6$ .

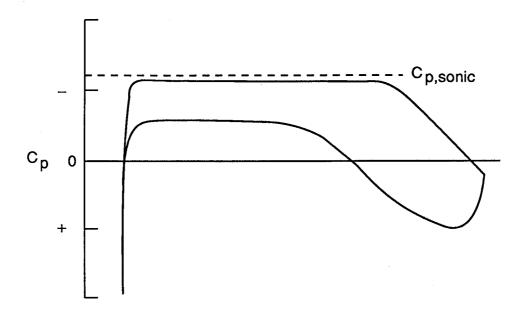


Figure 17. Generalized sonic-plateau pressure distribution.

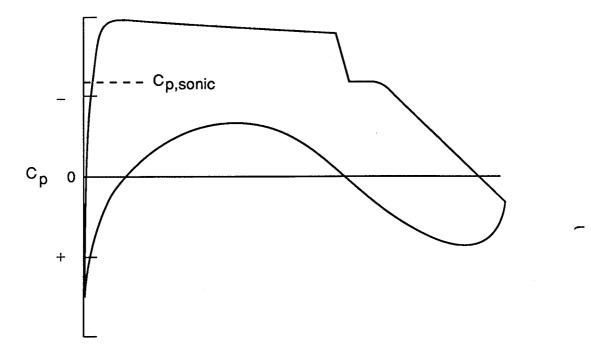


Figure 18. Generalized design pressure distribution.

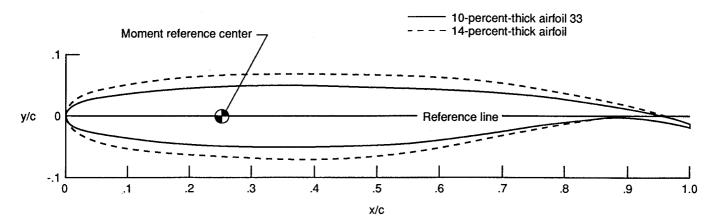


Figure 19. Comparison of 14-percent-thick airfoil with 10-percent-thick airfoil 33.

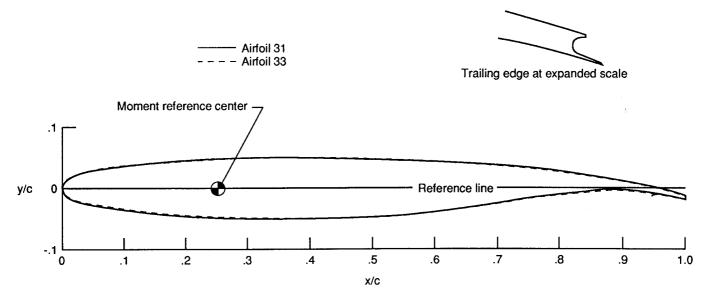


Figure 20. Sketches of 10-percent-thick supercritical airfoils 31 and 33.

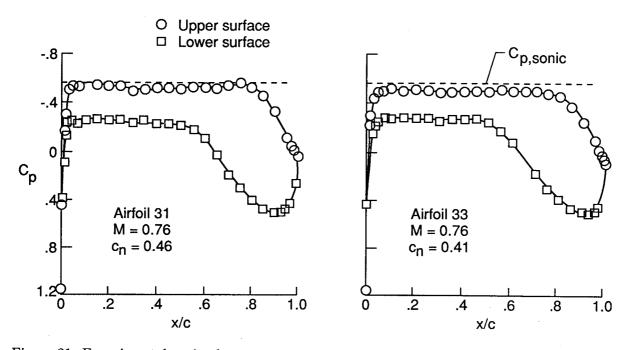


Figure 21. Experimental sonic-plateau pressure distributions for supercritical airfoils 31 and 33.

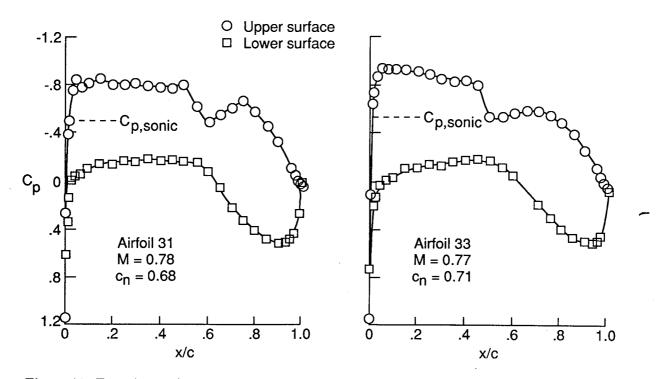


Figure 22. Experimental near-design pressure distributions for supercritical airfoils 31 and 33.

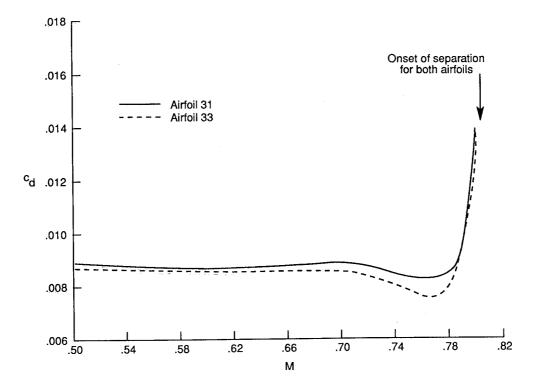


Figure 23. Experimental drag characteristics for supercritical airfoils 31 and 33.

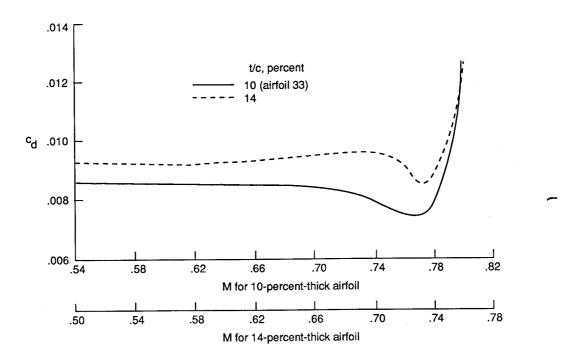
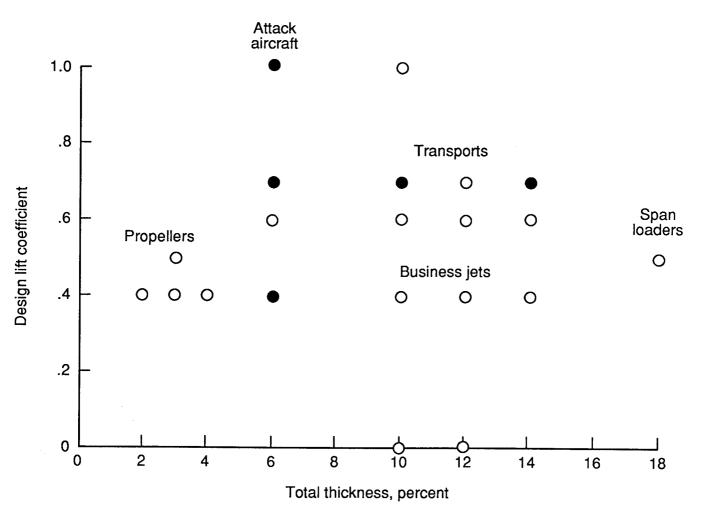
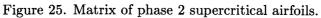


Figure 24. Experimental drag characteristics for 10-percent-thick supercritical airfoil 33 and 14-percent-thick supercritical airfoil.  $c_n = 0.70$ .





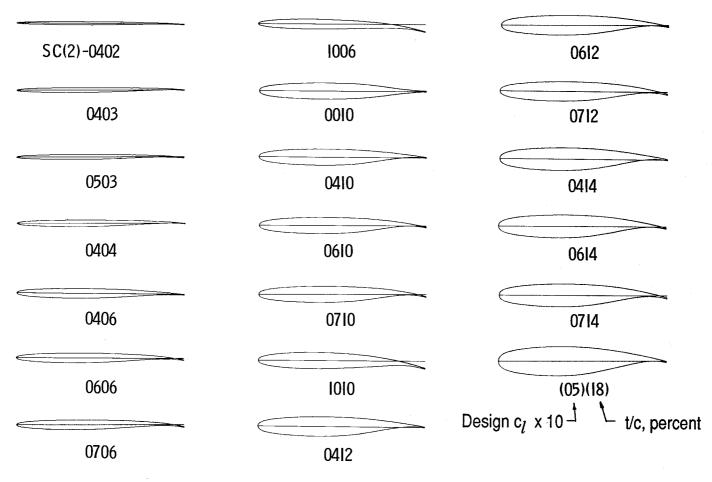


Figure 26. Sketches of airfoils in phase 2 supercritical airfoil matrix.

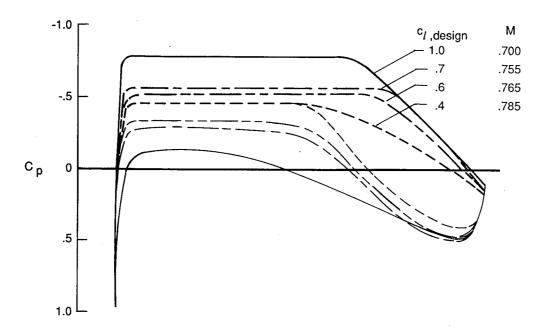
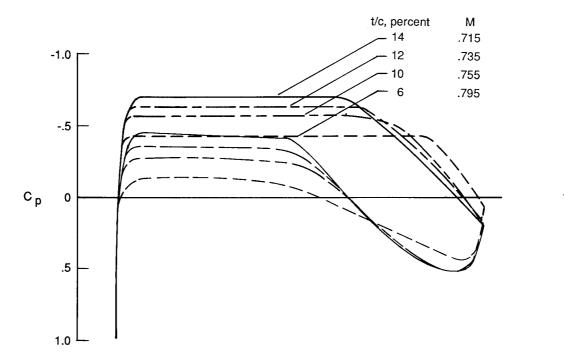
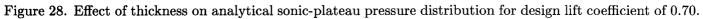


Figure 27. Effect of design lift coefficient on analytical sonic-plateau pressure distribution for 10-percent-thick supercritical airfoils.





65

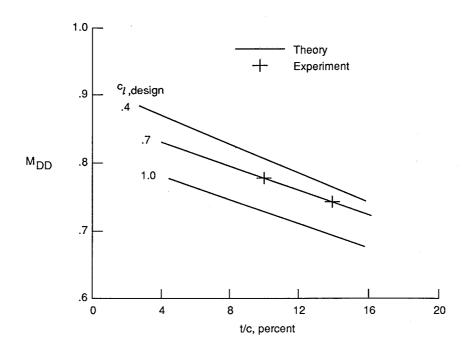


Figure 29. Analytical drag divergence Mach numbers for phase 2 supercritical airfoils.

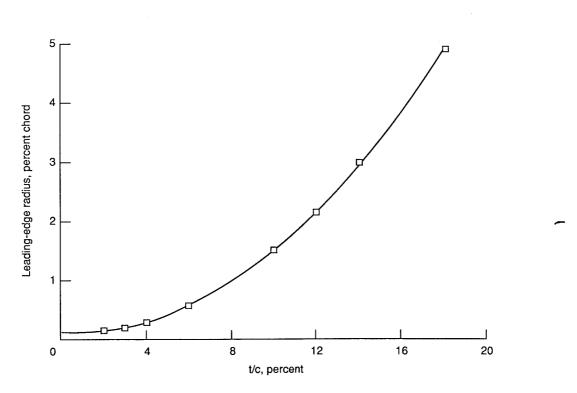


Figure 30. Variation of leading-edge radius with maximum thickness for phase 2 supercritical airfoils.



Figure 31. Sketches of 12-percent-thick supercritical airfoil with and without forward lower-surface undercutting.

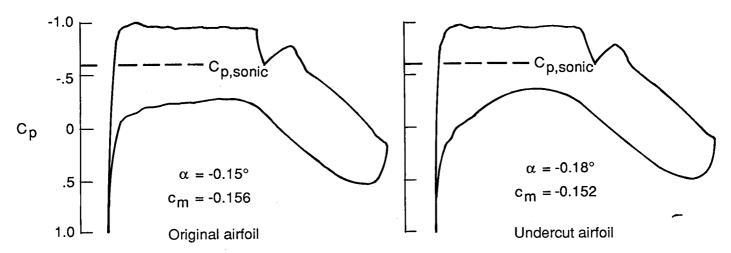
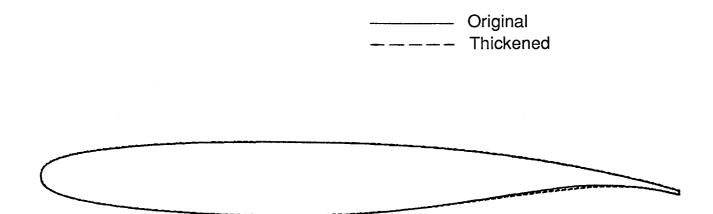
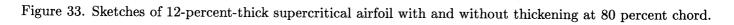


Figure 32. Effect on analytical design pressure distribution of undercutting forward lower surface on 12-percentthick supercritical airfoil. M = 0.75,  $c_l = 0.70$ ;  $R_c = 30 \times 10^6$ .





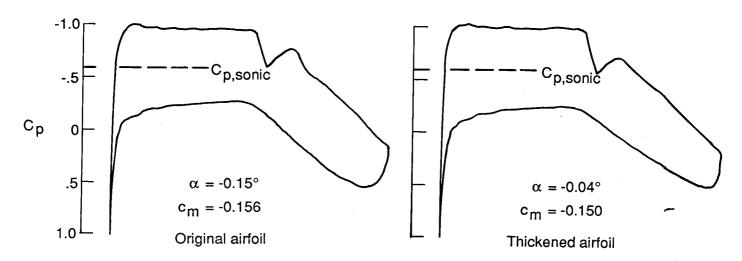


Figure 34. Effect on analytical design pressure distribution of thickening 12-percent-thick supercritical airfoil at 80 percent chord. M = 0.75;  $c_l = 0.70$ ;  $R_c = 30 \times 10^6$ .

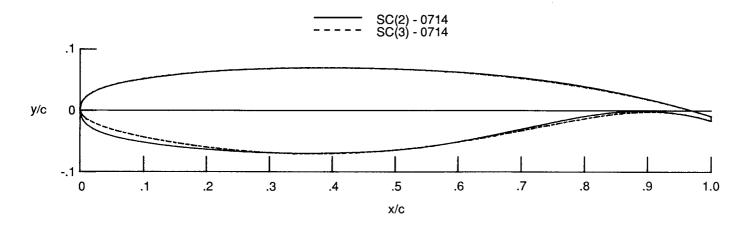


Figure 35. Sketches of 14-percent-thick phase 2 and phase 3 supercritical airfoils.

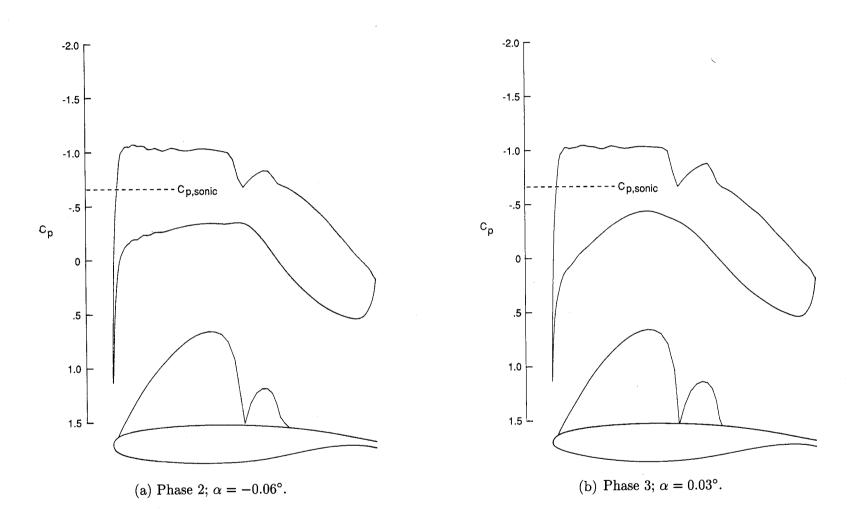


Figure 36. Analytical design pressure distributions for 14-percent-thick phase 2 and phase 3 supercritical airfoils. M = 0.730;  $c_l = 0.70$ ;  $R_c = 30 \times 10^6$ .

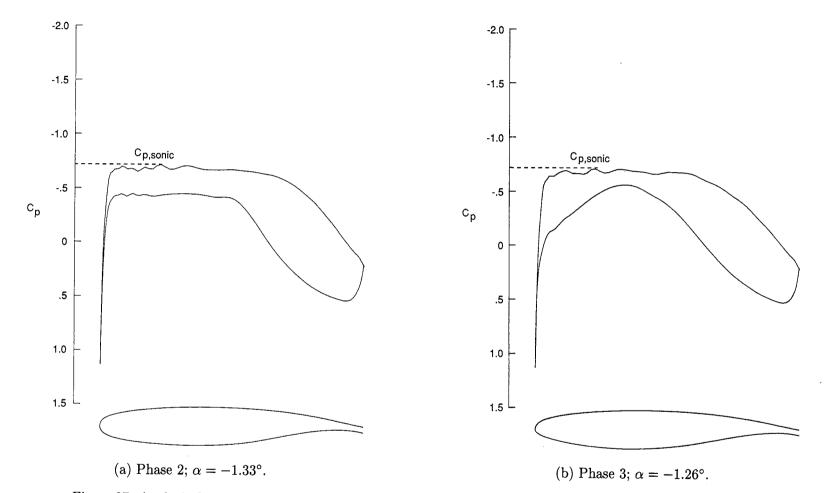


Figure 37. Analytical sonic-plateau pressure distributions for 14-percent-thick phase 2 and phase 3 supercritical airfoils. M = 0.715;  $c_l = 0.42$ ;  $R_c = 30 \times 10^6$ .

National Aeronaulics and Space Administration	Report Docum	entation Page		
1. Report No. NASA TP-2969	2. Government Accession	n No.	3. Recipient's Cat	alog No.
4. Title and Subtitle NASA Supercritical Airfoils A Matrix of Family-Related A	irfoils		<ol> <li>5. Report Date March 1990</li> <li>6. Performing Org</li> </ol>	
7. Author(s) Charles D. Harris			L-16625	ganization Report No.
9. Performing Organization Name and Add NASA Langley Research Cent Hampton, VA 23665-5225			<ol> <li>10. Work Unit No 505-61-21-0</li> <li>11. Contract or G</li> </ol>	)3
12. Sponsoring Agency Name and Address National Aeronautics and Spa Washington, DC 20546-0001			<ol> <li>Type of Report Technical I</li> <li>Sponsoring Ag</li> </ol>	_
15. Supplementary Notes				
16. Abstract				
This report summarizes the N fashion, discusses some of the family-related supercritical air from 0 to 1.0.	e airfoil design guidel	ines, and presen	its coordinates	of a matrix of
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17. Key Words (Suggested by Authors(s)) Airfoil Supercritical aerodynamics Transonic aerodynamics	ì	18. Distribution Sta Unclassified	atement —Unlimited	
		Su	bject Category	y 02
19. Security Classif. (of this report) Unclassified NASA FORM 1626 OCT 86	20. Security Classif. (of Unclassified	this page)	21. No. of Pages 72	22. Price A04 NASA-Langley, 199

For sale by the National Technical Information Service, Springfield, Virginia 22161-2171