

DEPARTMENT OF MECHANICAL ENGINEERING & MECHANICS  
COLLEGE OF ENGINEERING & TECHNOLOGY  
OLD DOMINION UNIVERSITY  
NORFOLK, VIRGINIA 23529

**RADIATIVE INTERACTIONS IN MOLECULAR GASES  
UNDER LOCAL AND NONLOCAL THERMODYNAMIC  
EQUILIBRIUM CONDITIONS**

By

S. N. Tiwari, Principal Investigator

and

M. K. Jha, Graduate Research Assistant

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Progress Report

For the period ended April 30, 1993

Prepared for  
National Aeronautics and Space Administration  
Langley Research Center  
Hampton, Virginia 23681-0001

Under  
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Dr. Ajay Kumar, Technical Monitor  
FLDMD-Theoretical Flow Physics Branch

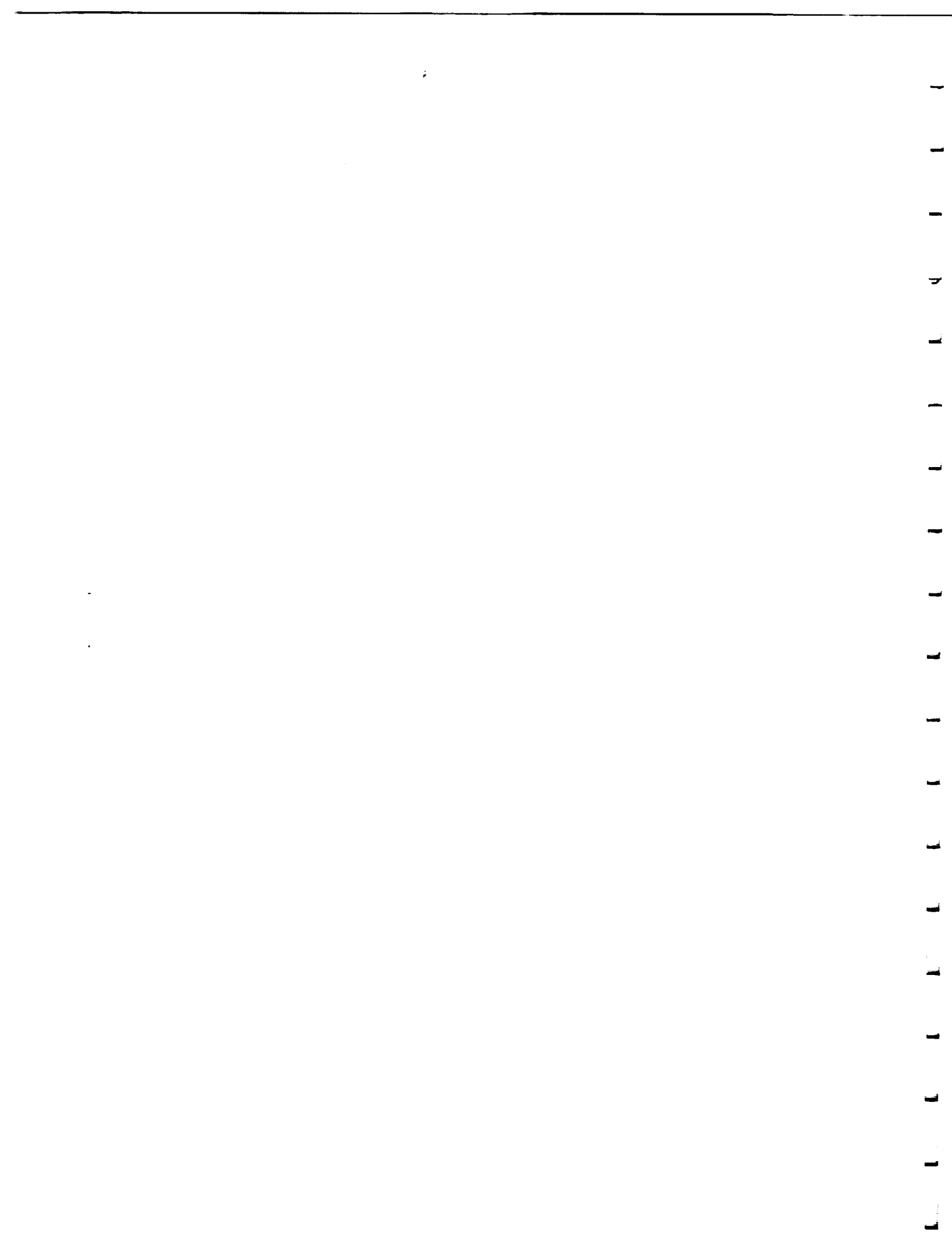
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## FOREWORD

This is a progress report on the research project, "Analysis and Computation of Internal Flow Field in a Scramjet Engine," for the period ended April 30, 1993. Special attention during this period was directed to "Radiative Interactions in Molecular Gases under Local and Nonlocal Thermodynamic Equilibrium Conditions".

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# **RADIATIVE INTERACTIONS IN MOLECULAR GASES UNDER LOCAL AND NONLOCAL THERMODYNAMIC EQUILIBRIUM CONDITIONS**

**By**

**M. K. Jha† and S. N. Tiwari‡**

**Department of Mechanical Engineering and Mechanics**

**Old Dominion University, May 1993**

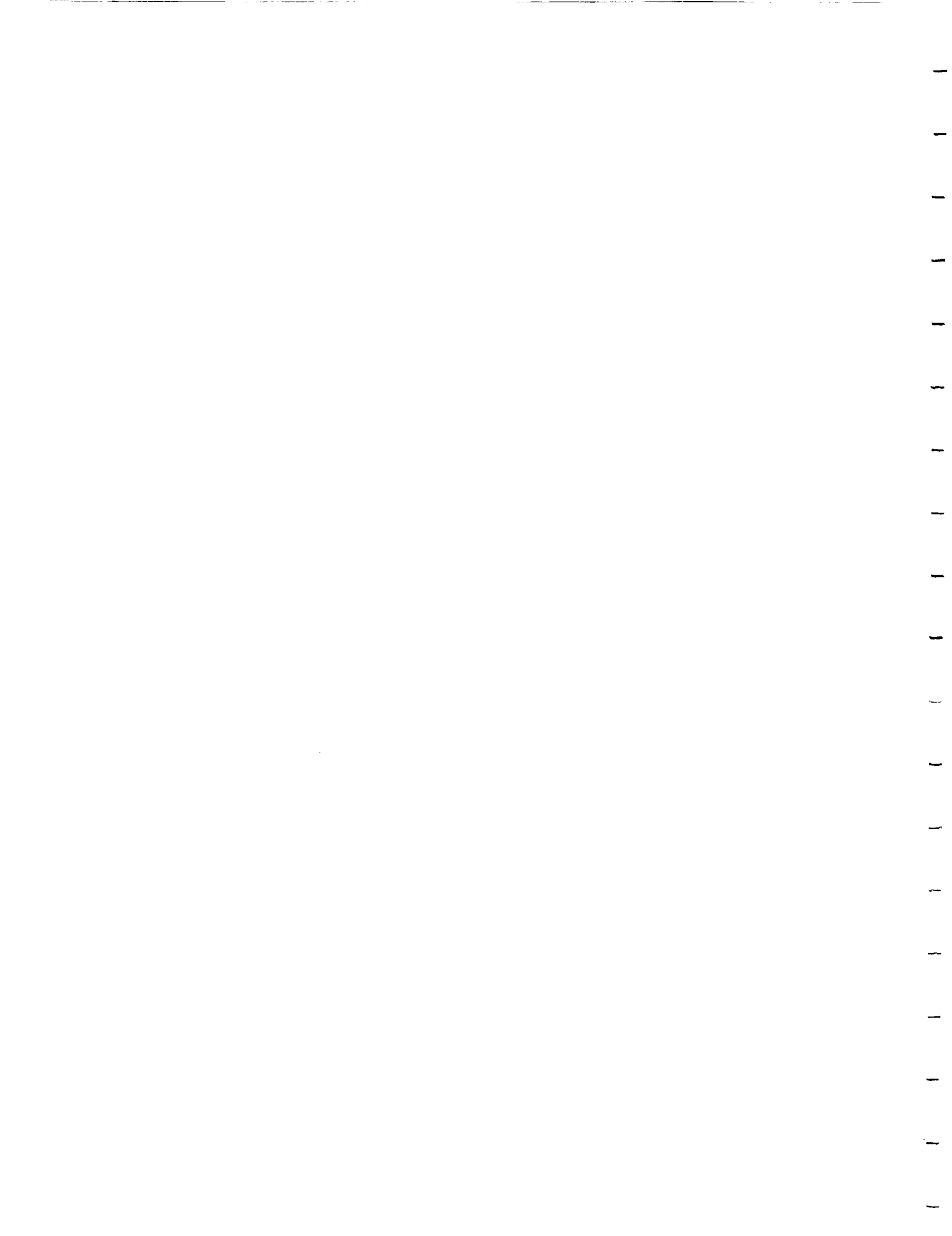
## **ABSTRACT**

Basic formulations, analyses, and numerical procedures are presented to investigate radiative heat interactions in diatomic and polyatomic gases under local and nonlocal thermodynamic equilibrium conditions. Essential governing equations are presented for both gray and nongray gases. Information is provided on absorption models, relaxation times, and transfer equations. Radiative flux equations are developed which are applicable under local and nonlocal thermodynamic equilibrium conditions.

The problem is solved for fully developed laminar incompressible flows between two parallel plates under the boundary condition of a uniform surface heat flux. For specific applications, three diatomic and three polyatomic gases are considered. The results are obtained numerically by employing the method of variation of parameters. The results are compared under local and nonlocal thermodynamic equilibrium conditions at different temperature and pressure conditions. Both gray and nongray studies are conducted extensively for all molecular gases considered. The particular gases selected for this investigation are, CO, NO, OH, CO<sub>2</sub>, H<sub>2</sub>O, and CH<sub>4</sub>. The temperature and pressure range considered are 300–2000 K and 0.1–10 atmosphere, respectively. In general, results demonstrate that the

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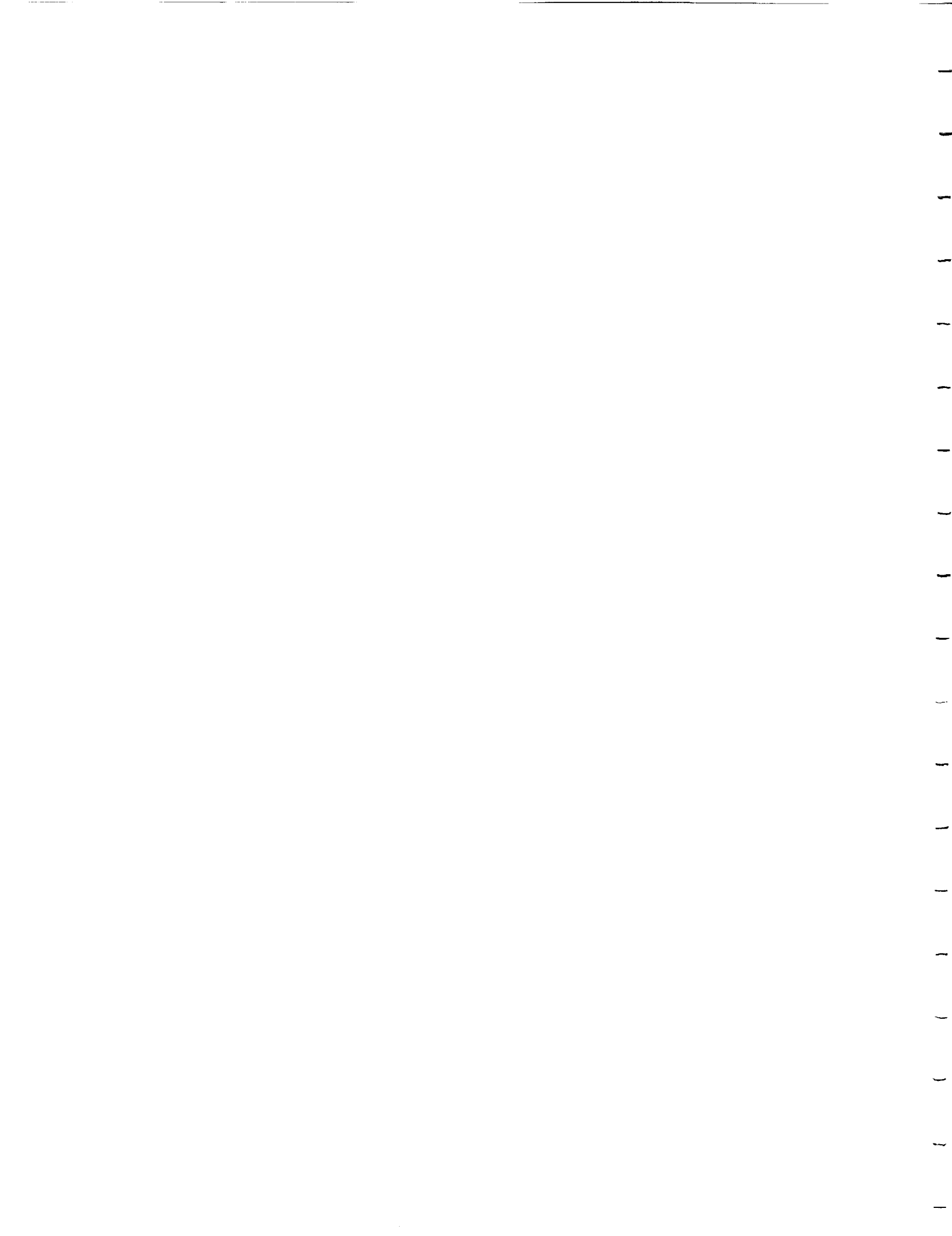


gray gas approximation overestimates the effect of radiative interaction for all conditions. The conditions of NLTE, however, result in underestimation of radiative interactions. The method developed for this study can be extended to solve complex problems of radiative heat transfer involving nonequilibrium phenomena.

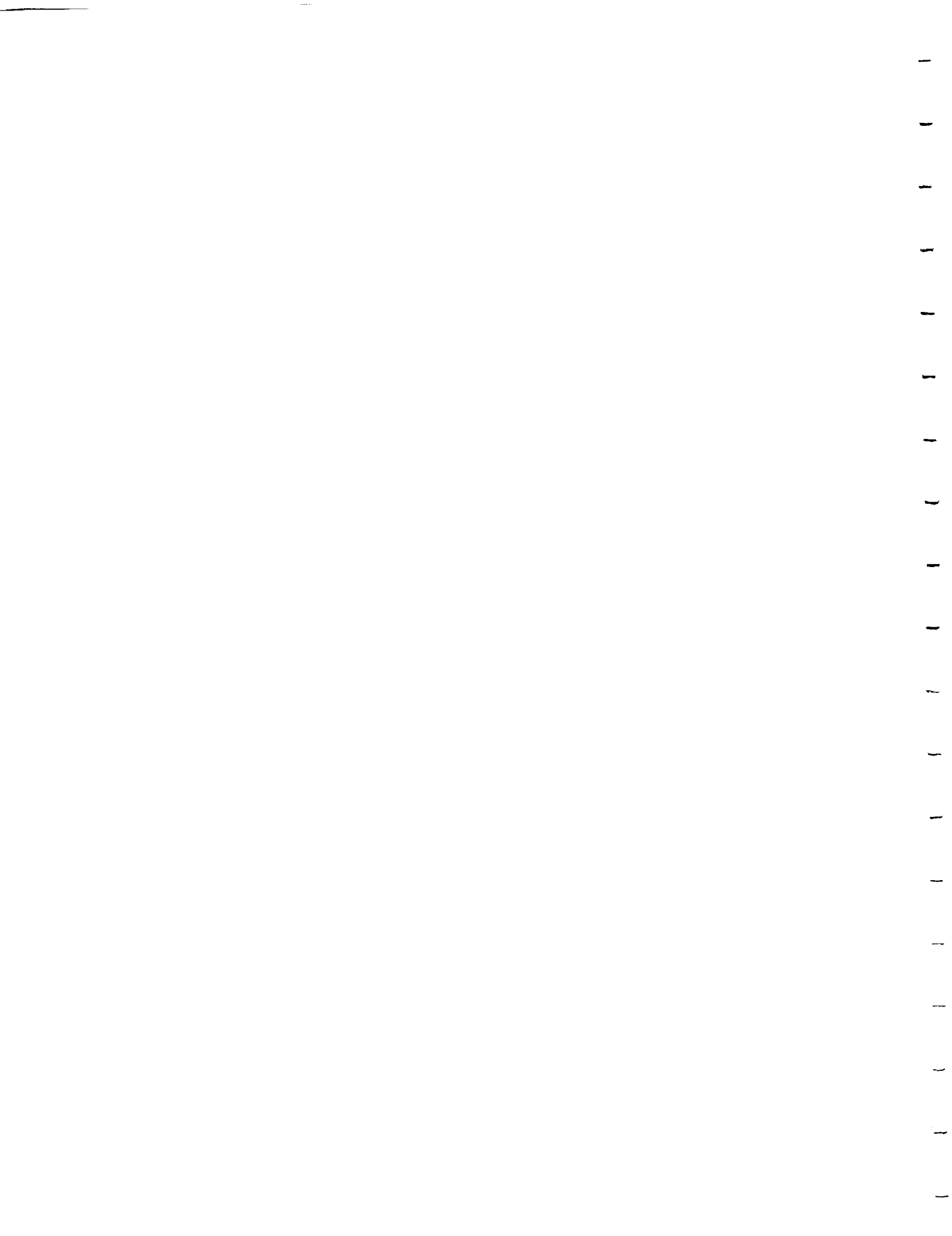


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## LIST OF SYMBOLS

### Latin Symbols

$A, A_i$	Total band absorptance, $\text{cm}^{-1}$
$A_{0i}$	Correlation quantity, $\text{cm}^{-1}$
$\bar{A}, \bar{A}_i$	Dimensionless band absorptance
$B^2, B_i^2$	Correlation quantity
$B_e, B_{ei}$	Rotational constant, $\text{cm}^{-1}$
$B_\nu$	Black body intensity of frequency $\nu$ and at local temperature
$B_\omega(T_1), B_\omega(T_w)$	Spectral surface radiosity, $(\text{watts}/\text{cm}^2)\text{cm}^{-1}$
$c$	Speed of light
$C_0^2, C_{0i}^2$	Correlation quantity
$E_n(t)$	Exponential integral
$E_r$	Rotational Energy
$E_v$	Vibrational energy
$E_v^*$	Equilibrium vibrational energy
$e$	Total black body emissive power
$e_\omega$	Planck's function, $(\text{watts}/\text{cm}^2)/\text{cm}^{-1}$
$e_{1\omega}, e_{1\omega i}$	Planck's function evaluated at temperature $T_1$
$h$	Planck's constant
$I_\nu$	Intensity of a beam of radiation of frequency $\nu$
$J_\nu, J_{\nu c}$	Radiative source function
$k$	Boltzmann constant



P	Gas pressure, atm
$q_w$	Wall heat flux, watts/cm <sup>2</sup>
$q_R$	Total radiative heat flux, watts/cm <sup>2</sup>
$q_{Ri}$	Radiation heat flux for ith band, watts/cm <sup>2</sup>
$q_{R\omega}, q_{R\omega i}$	Spectral radiative flux, (watts/cm <sup>2</sup> )/cm <sup>-1</sup>
$S(T)$	Total band intensity, atm <sup>-1</sup> cm <sup>-2</sup>
$S_v$	Nonequilibrium source function
$S_v^*$	Equilibrium source function
T	Temperature, K
$T_0$	Reference temperature (equilibrium)
$T_1, T_2, T_w$	Wall temperature
$T_b$	Bulk temperature, K
$u, u_i$	Dimensionless coordinate, $C_0^2 P y$
$u_0, u_{0i}$	Dimensionless path length, $C_0^2 P L$
$v_x$	Velocity, cm/sec
$v_m$	Mean velocity, cm/sec
y	Physical coordinate, cm
Greek Symbols	
$\alpha$	Thermal diffusivity, cm <sup>2</sup> /sec
$\beta, \beta_i$	Line structure parameter, $B^2 P e$
$\gamma_1$	Nondimensional quantity, $3 \tau_0^2 / \bar{N}$
$\epsilon, \epsilon_i$	Surface emittance
$\eta_c$	Vibrational relaxation time, sec
$\eta_r$	Radiative life time of vibrational state, sec
$\theta_p$	Dimensionless temperature, $(T-T_1)/(q_w L/\kappa)$
$\theta_{bp}$	Dimensionless bulk temperature, $(T_b-T_1)/(q_w L/\kappa)$





$\kappa, \kappa$	Thermal conductivity, watts/cm <sup>2</sup> /K
$\kappa_\nu$	Absorption coefficient of frequency $\nu$
$\kappa_\nu^*$	Equilibrium absorption coefficient at frequency $\nu$
$\kappa_\omega$	Equilibrium spectral absorption coefficient, cm <sup>-1</sup>
$\kappa_m$	Modified Planck mean coefficient, cm <sup>-1</sup>
$\kappa_p$	Planck mean coefficient, cm <sup>-1</sup>
$\nu$	Frequency
$\nu_c, \nu_0, \nu_i$	Frequency corresponding to band center
$\xi$	Dimensionless coordinate, $y/L$
$\rho, \rho$	Density
$\sigma$	Stefan–Boltzmann constant
$\Omega$	Solid angle
$\omega$	Wave number, cm <sup>-1</sup>
$\omega_c, \omega_i$	Band center, cm <sup>-1</sup>



# Chapter 1

## INTRODUCTION

Radiation is an important mode of energy transfer in systems involving high temperature variations. In past several years, radiative energy transfer has been the subject of research in many heat transfer problems. This is because of the specific applicability of radiative heat transfer analyses in certain important areas. Some of the popular areas of application are, remote sensing, earth's radiation budget studies and climate modelling, fire and combustion research, entry and reentry phenomena, hypersonic propulsion, and defense oriented research. Until the sixties and early seventies, attentions were directed mainly on one dimensional treatment of radiative transfer problems. Multidimensional analyses became popular only in the mid-to-late seventies. Today, there are several books [1-11]\*, review articles, and research papers available which deal with radiative heat transfer analyses in a variety of systems.

To understand the radiative energy transfer, it is important to understand the basic transfer processes ( mass, momentum, and energy ) in various systems. Essential formulations for such processes are available in standard references [12-19]. It is necessary to assume a suitable model for vibration-rotation bands, and to obtain relevant spectroscopic information

\* Numbers in brackets represent references

for the gases under consideration. One should be thoroughly conversant with different numerical and computational procedures.

There are a number of analyses involving duct flows of absorbing–emitting gases in literature. Usiskin and Sparrow [20] studied thermal radiation between parallel plates separated by an absorbing–emitting, nonisothermal gas. Viskanta and Grosh [21] studied heat transfer in an absorbing and scattering medium. Lick [22] studied the effect of energy transfer by combined radiation and conduction. Viskanta [23] studied the interaction of conduction, laminar convection, and radiation in a plane layer of radiating fluid. Cess and Tiwari [24] investigated heat transfer to laminar flow of an absorbing–emitting gas between parallel plates. Tiwari [25] studied radiative interaction in transient energy transfer in gaseous systems. Tiwari and Singh [26] extended Tiwari’s work to fully developed laminar flows. The studies involving nonlocal thermodynamic equilibrium (NLTE) phenomena are discussed in [27–31]. The studies presented in [32–35] have reviewed other available literature on gray as well as nongray radiative transfer between planar geometries.

Most of the radiative heat transfer treatment have been done under local thermodynamic equilibrium (LTE) conditions. The goal of this research is to treat the radiative heat transfer problems under NLTE conditions. The gases under consideration are, CO, NO, OH, CO<sub>2</sub>, H<sub>2</sub>O, and CH<sub>4</sub>. Both gray and nongray analyses have been conducted for these gases. The analyses have been presented for laminar flow between black parallel plates. However, the same analyses can be extended to circular, triangular, or other complex geometries with proper modifications. The LTE and NLTE results are compared at different pressures and temperatures. The range of pressure, temperature, and plate spacing is chosen in such a way that maximum radiative effect is observed. The pressure ranges from 0.1 to 10 atmosphere,

and the temperature ranges from 300 to 2000 K. The spacing between the plates is taken from 0.1 to 100 centimeters.

The basic theoretical formulation is provided in Chap. 2. Chapter 3 presents radiative transfer models which include absorption models, rate equations and equations for relaxation times, the equation of radiative transfer, and radiative flux equations. Chapter 4 deals with gray gas analyses under LTE and NLTE conditions. Chapter 5 provides nongray radiative transfer formulations under LTE and NLTE conditions. Results and discussion for all the cases are presented in Chap. 6.



## Chapter 2

### BASIC THEORETICAL FORMULATION

As stated in the introduction, the basic governing equations for fluid mechanics and heat transfer are available in standard references [12–19]. These equations are used in different forms depending upon the nature of the problem being solved. These are presented here without providing detailed derivations.

The equation for conservation of mass which is known as continuity equation, is given as

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0 \quad (2.1a)$$

For an incompressible fluid, this reduces to

$$\nabla \cdot \mathbf{u} = 0 \quad (2.1b)$$

The equation for conservation of momentum, in most general form, is given as

$$\rho \frac{D\mathbf{u}}{Dt} = \rho \mathbf{f} - \nabla P + \frac{\partial}{\partial x_j} \left[ \rho u \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} \delta_{ij} \mu \frac{\partial u_k}{\partial x_k} \right] \quad (2.2a)$$

where  $\delta_{ij}$  is known as the Kronecker delta and  $i, j, k = 1, 2, 3$ . In deriving Eq. (2.2a), the coefficient of bulk viscosity is assumed to be zero. Assuming incompressible fluid and viscosity  $\mu$  to be constant, Eq. (2.2a) reduces to





$$\frac{Du}{Dt} = f - \frac{\nabla P}{\rho} + \nu \nabla^2 u \quad (2.2b)$$

The energy equation is expressed in several forms which are available in [12,15,16]. The proper form which is convenient for this study is given as

$$\rho C_p \left( \frac{DT}{Dt} \right) = \frac{\partial Q}{\partial t} + \nabla \cdot (\kappa \nabla T) - \nabla \cdot q_R + \beta T \left( \frac{Dp}{Dt} \right) + \phi \quad (2.3)$$

where

$$\begin{aligned} \phi = \mu [ & 2 \left( \frac{\partial u}{\partial x} \right)^2 + 2 \left( \frac{\partial v}{\partial y} \right)^2 + 2 \left( \frac{\partial w}{\partial z} \right)^2 + \left( \frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} \right)^2 + \left( \frac{\partial w}{\partial y} + \frac{\partial v}{\partial z} \right)^2 \\ & + \left( \frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} \right)^2 - \frac{2}{3} \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} \right)^2 ] \end{aligned}$$

In Eq. (2.3), the quantity Q represents the heat generated (or lost) by external agencies, and  $\beta$  is the coefficient of thermal expansion of the fluid. Other quantities are defined in cited references.

Equations (2.1)–(2.3), in general, are called Navier–Stokes equations. For computational conveniences, these equations are expressed in a compact vector form as [19]

$$\frac{\partial U}{\partial t} + \frac{\partial E}{\partial x} + \frac{\partial F}{\partial y} + \frac{\partial G}{\partial z} = 0 \quad (2.4)$$

where it is assumed that there is no external heat addition and no body forces. The quantities U, E, F, and G are vectors and are defined as

$$U = \begin{bmatrix} \rho \\ \rho u \\ \rho v \\ \rho w \\ Et \end{bmatrix}$$

$$E = \begin{bmatrix} \rho u \\ \rho u^2 + P - \tau_{xx} \\ \rho uv - \tau_{xy} \\ \rho uw - \tau_{xz} \\ (E_t + P) u - u\tau_{xx} - v\tau_{xy} - w\tau_{xz} + q_{cx} + q_{Rx} \end{bmatrix}$$

$$F = \begin{bmatrix} \rho v \\ \rho uv - \tau_{xy} \\ \rho v^2 + P - \tau_{yy} \\ \rho vw - \tau_{yz} \\ (E_t + P) v - u\tau_{xy} - v\tau_{yy} - w\tau_{yz} + q_{cy} + q_{Ry} \end{bmatrix}$$

$$G = \begin{bmatrix} \rho w \\ \rho uw - \tau_{xz} \\ \rho vw - \tau_{yz} \\ \rho w^2 + P - \tau_{zz} \\ (E_t + P) w - u\tau_{xz} - v\tau_{yz} - w\tau_{zz} + q_{cz} + q_{Rz} \end{bmatrix}$$

where

$$E_t = \rho \left( e + \frac{V^2}{2} \right); \quad V^2 = u^2 + v^2 + w^2$$

$$\tau_{xx} = \frac{2}{3} \mu \left( 2 \frac{\partial u}{\partial x} - \frac{\partial v}{\partial y} - \frac{\partial w}{\partial z} \right)$$

$$\tau_{yy} = \frac{2}{3} \mu \left( 2 \frac{\partial v}{\partial y} - \frac{\partial u}{\partial x} - \frac{\partial w}{\partial z} \right)$$

$$\tau_{zz} = \frac{2}{3} \mu \left( 2 \frac{\partial w}{\partial z} - \frac{\partial u}{\partial x} - \frac{\partial v}{\partial y} \right)$$

$$\tau_{xy} = \mu \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) = \tau_{yx}$$

$$\tau_{xz} = \mu \left( \frac{\partial w}{\partial x} + \frac{\partial u}{\partial z} \right) = \tau_{zx}$$

$$\tau_{yz} = \mu \left( \frac{\partial v}{\partial z} + \frac{\partial w}{\partial y} \right) = \tau_{zy}$$

In Eq. (2.4), first row represents the continuity equation, second, third, and fourth rows represent the three momentum equations, and the last row represents the energy equation.

For two-dimensional laminar flow in channels, the energy equation given by Eq. (2.3) reduces to [6]

$$\rho C_p \left( \frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} \right) = \frac{\partial}{\partial y} \left( \kappa \frac{\partial T}{\partial y} \right) + \beta T u \frac{dP}{dx} + \mu \left( \frac{\partial u}{\partial y} \right)^2 - \text{div } q_R \quad (2.5)$$

The energy equation given in this form can be applied to radiatively induced nonequilibrium flows by replacing the divergence of the radiative flux by its nonequilibrium counterpart.

In deriving Eq. (2.5), it has been assumed that the conduction heat transfer in the x-direction is negligible compared to that in the y-direction. This represents the physical condition of a large value of the Peclet number. Similar reasoning can be applied to show that the radiative heat transfer in the x-direction is negligible in comparison to that in the y-direction.

Within the confines of the foregoing assumptions, for small values of the Eckert number, Eq. (2.5) reduces to

$$\frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = \alpha \frac{\partial^2 T}{\partial y^2} - \frac{1}{\rho C_p} \frac{\partial q_R}{\partial y} \quad (2.6)$$

where  $\alpha = \kappa / \rho C_p$  is the thermal diffusivity of the fluid and fluid properties has been assumed to be constant locally.

In order to apply energy equation to problems involving radiation participating medium, it is necessary to have an appropriate formulation for the radiative flux,  $q_R$ . As stated earlier, in dealing with problems involving nonequilibrium phenomena, one should use the nonequilibrium counterpart of the radiative flux equation. Different forms of radiative flux equation as well as other relevant topics are covered in the next chapter.

## **Chapter 3**

# **RADIATIVE TRANSPORT MODELS**

As stated in Chap. 2, one should consider an appropriate radiative transport model while applying the energy equation to problems involving radiation participating medium. This section presents discussion on absorption models, rate equations and relaxation times, transfer equations, and radiative flux equations.

### **3.1 Absorption Models**

To study the radiative effects in nonhomogeneous medium, it is essential to know the absorption, emission, and scattering characteristics of the gases under consideration. An accurate model for the spectral absorption coefficient is required to formulate radiative flux equations. In addition, one needs to identify the major bands of the gas under consideration, and to evaluate the line parameters ( line intensity, line half-width, and line spacing ) of these bands. The line parameters depend on temperature, pressure, and concentration of the absorbing molecules. Considerable efforts have been made to obtain the line parameters and absorption coefficient of some important atomic and molecular species.

The quantity of primary interest which is applied with respect to the band approximation, is the integrated band intensity,  $S$ . This is also called integrated band absorption or band intensity, and is defined as

$$S(T) = \int_{\Delta\omega} \frac{\kappa_{\omega}}{P} d\omega \quad (3.1)$$

where  $\kappa_{\omega}$  represents the spectral absorption coefficient. This quantity is independent of pressure because the total area of the individual rotational line is independent of pressure.

The temperature variation of the integrated band intensity is given by [33–35]

$$T S(T) = T_0 S(T_0) F(T) \quad (3.2)$$

where  $T_0$  is the reference temperature ( usually 300 K) and  $F(T)=1$  for fundamental and pure rotation bands, but it differs from unity for overtone and combination bands. For combination and overtone bands of important molecules, relations for  $F(T)$  exists in literature [35]. Band intensities for some important gases are presented in Appendix A.

For gray gas analyses, the total band absorption coefficient is expressed in terms of either the Planck mean absorption coefficient  $\kappa_p$  or the modified Planck mean absorption coefficient  $\kappa_m$ . For a single-band gas, these are defined as [6]

$$\kappa_p(T) = \frac{\int_{\Delta\omega} \kappa_{\omega}(T) e_{\omega}(T) d\omega}{e(T)} \quad (3.3)$$

$$\kappa_m(T, T_1) = \int_{\Delta\omega} \frac{\kappa_{\omega}(T) e_{\omega}(T_1) d\omega}{\sigma T_1^4} \quad (3.4)$$

where  $e_\omega$  is Planck function. Assuming the Planck function  $e_\omega(T)$  to be independent of the wave number within the band, and using Eqs. (3.1) and (3.2), Eqs. (3.3) and (3.4) can be written as

$$\frac{\kappa_p(T)}{P} = \frac{e_{\omega c}(T)}{\sigma T^4} S(T) \quad (3.5)$$

$$\frac{\kappa_m(T, T_1)}{P} = \frac{e_{\omega c}(T_1)}{\sigma T_1^4} S(T) = \frac{\kappa_p(T_1) T_1}{P T} \quad (3.6)$$

The definition of  $\kappa_p$  and  $\kappa_m$  can be extended to multiband gases, and by combining Eqs. (3.2), (3.3), and (3.4), a general expression can be obtained as

$$\frac{T \kappa_m(T, T_1)}{T_1 \kappa_p(T_1)} = \frac{\sum_{i=1}^n e_{\omega_i}(T_1) S_i(T_0) F_i(T)}{\sum_{i=1}^n e_{\omega_i}(T_1) S_i(T_0) F_i(T_1)} \quad (3.7)$$

where  $n$  is the number of bands. By including the contributions from overtone and combination bands, calculations performed for CO, CO<sub>2</sub>, and H<sub>2</sub>O [31] show that the right hand side of Eq. (3.7) is approximately equal to unity, and therefore Eq. (3.6) is an excellent approximation for Eq. (3.7).

In a similar manner, the general expression for Eq. (3.5) for multiband gases can be given as

$$\kappa_p(T) = \frac{P \sum_{i=1}^n [ e_b(\omega_{ci}, T) S_i(T) ]}{\sigma T^4} \quad (3.8)$$

For a mixture of gases, Eq. (3.8) can be written as

$$\kappa_p(T) = \frac{\sum_j P_j \left\{ \sum_{i=1}^n [ e_b(\omega_{ci}, T) S_i(T) ] \right\}}{\sigma T^4} \quad (3.9)$$

where  $j$  is the number of species and  $P_j$  is the partial pressure of the  $j$ th species.

For an accurate evaluation of the absorptance of a molecular band, a convenient line model is used to represent the variation of the spectral absorption coefficient. The commonly used line models are Lorentz, Doppler, and Voigt line models. A detailed discussion of these line models is presented in [31]. In a particular band consisting of many lines, the absorption coefficient varies very rapidly with frequency. Thus, it is very difficult to evaluate the total band absorptance over the actual band contour by employing the line model. To overcome this difficulty, several band models (narrow as well as wide) have been proposed which represent absorption from an actual band with reasonable accuracy [33–35]. There are several continuous correlations for the total band absorptance which are available in literature. The detailed discussion of the various band models are given in cited references.

### 3.2 Rate Equations and Relaxation Times

In this section, discussion on rate equations and equations for relaxation times are presented briefly. For any radiative heat exchange process, it is important to know the rate of change of vibrational energy [31]. The rate of change of vibrational energy of a system of oscillator can be given as



$$\frac{dE_v}{dt} = \left( \frac{dE_v}{dt} \right)_{coll} + \left( \frac{dE_v}{dt} \right)_{rad} \quad (3.10)$$

where first and second terms on the right hand side represent vibrational energy due to collisional and radiative processes respectively. The radiative field exchanges energy with rotational as well as vibrational degree of freedom. The relation for radiative flux in terms of rate of change of vibrational as well as rotational energy is given by

$$- \operatorname{div} q_R = \left( \frac{dE_v}{dt} \right)_{rad} + \left( \frac{dE_r}{dt} \right)_{rad} \quad (3.11)$$

where  $E_v$  and  $E_r$  are vibrational and rotational energy per unit volume. The second term on the right of Eq. (3.11) can be neglected because of small separation of rotational levels.

The divergence of radiative flux is related to specific intensity  $I_\nu$ , and for one-dimensional case, it is given as

$$\operatorname{div} q_R = \frac{dq_R}{dy} = \int_0^\infty \frac{dq_{R\nu}}{dy} d\nu = \int_0^\infty \int_0^{4\pi} \frac{dI_\nu}{ds} d\Omega d\nu \quad (3.12)$$

Combining Eqs. (3.10) – (3.12), one obtains

$$\frac{dE_v}{dt} = \left( \frac{dE_v}{dt} \right)_{coll} - \int_0^\infty \int_0^{4\pi} \frac{dI_\nu}{ds} d\Omega d\nu \quad (3.13)$$

The first part of Eq. (3.13), i.e. the rate of change of vibrational energy of a system undergoing a collisional relaxation process is given by the Bethe–Teller relation [31]

$$\frac{dE_v}{dt} = \frac{E_v^* - E_v}{\eta_c} \quad (3.14)$$

where  $E_v^*$  is the equilibrium value of the vibrational energy and  $\eta_c$  is vibrational relaxation time. The relaxation time is defined as the average time required to transfer energy from one mode to another by collision. Therefore, it is also termed as collisional relaxation time.

By assuming  $E_{v0}$  to be the initial amount of vibrational energy, integration of Eq. (3.14) yields

$$E_v - E_v^* = (E_{v0} - E_v^*) \exp\left(-\frac{t}{\eta_c}\right) \quad (3.15)$$

In order to use Eq. (3.15), an explicit relation for  $\eta_c = \eta_c(T,P)$  is required. There are several expressions available in literature to calculate  $\eta_c$ . Some of them are briefly discussed here. An explicit relation for  $\eta_c$  is given by the Landau–Teller relation [31]

$$\eta_c = K_1 P^{-1} \exp(K_2 T^{-1/3}) \quad (3.16)$$

where  $K_1$  and  $K_2$  are positive constants and depend on the physical properties of the molecule. For diatomic gases, an empirical relation for  $\eta_c$  is given by [36, 37]

$$P \eta_c = \exp [ A ( T^{-1/3} - 0.015 \mu^{1/4} ) - 18.42 ] \quad (3.17)$$

where  $A$  is a constant and is related to the molecular constants of the colliding species and  $\mu$  is the reduced mass of the colliding pairs. Values of  $A$  and  $\mu$  for some gases are available in the references. For  $\text{CO}_2$ , the relation for  $\eta_c$  is given by [31]

$$\eta_c = \frac{1}{P} [ \exp ( AT^{-1/3} - B ) \times 10^{-6} ] \quad (3.18)$$

For CH<sub>4</sub>,  $\eta_c$  is given by [31]

$$\eta_c = \frac{1}{P} [ - 5 . 4 + 40 T^{-1/3} ] \times 10^{-6} \quad (3.19)$$

For cases where specific relation for  $\eta_c$  do not exist, one can use the general expression given by Millikan and White [36, 37]

$$P \eta_c = \exp [ ( 1 . 16 \times 10^{-3} ) \mu^{1/2} \theta^{4/3} ( T^{-1/2} - 0 . 15\mu^{1/4} ) - 18 . 42 ] \quad (3.20)$$

where  $\theta$  is the characteristic temperature (K) and is given as  $\theta = hc/k\lambda$ , and  $h$  is the Planck's constant,  $c$  is the speed of light,  $k$  is the Boltzmann constant, and  $\lambda$  is the wavelength.

In all the expressions for  $\eta_c$ ,  $P$  is the total pressure in atmosphere,  $\eta_c$  is in seconds, and  $T$  is the temperature in degrees Kelvin. Although these relations show a strong dependency of  $\eta_c$  on pressure, in reality it has a larger temperature variation. This is because collisional frequencies are higher at higher temperatures and consequently it takes relatively less time to deactivate the excited states. Further discussions on collisional relaxation time are provided by Tiwari and Manian [30].

### 3.3 Transfer Equations

By transfer equations, we mean equations for radiative energy transfer over a specifically defined volume. These equations are usually represented in terms of intensity of radiation  $I_\nu$ . In this section, we will derive several forms of radiative transfer equations and discuss their physical meaning. The transfer equations are derived for a simple harmonic oscillator based on the assumption that the rotational and vibrational levels are populated according

to the Boltzmann distribution. The rotational energy is characterized by equilibrium temperature  $T$  whereas the vibrational energy is characterized by the nonequilibrium temperature  $T_v$ . Two level transitions between the vibrational states are considered in such a way that a single independent vibration-rotation band is obtained corresponding to the fundamental frequency of vibration. Therefore, the nonequilibrium transfer equation which is described next, is applicable to only fundamental bands of diatomic and polyatomic gases.

For a two level system, let  $n(v-1)$  and  $n(v)$  represent the number density of molecules in the lower and upper vibrational levels respectively. In each vibrational level, molecules are assumed to be distributed over rotational levels according to Boltzmann distribution function  $f(j)$  such that  $\sum f(j) = 1$ . The quantity  $v$  is called the vibrational quantum number and  $j$  is a set of rotational quantum numbers corresponding to the lower vibrational level. Thus, number density in the state  $(v-1, j)$  is given as  $n(v-1) f(j)$ . Number of molecules that actually make a transition from state  $(v-1, j)$  to  $(v, j')$  are governed by the Einstein coefficients such that number of molecules undergoing spontaneous emission, induced or stimulated emission, and absorption are given by  $a(j', j) A(v, v-1)$ ,  $b(j', j) B(v, v-1)$ , and  $b(j, j') B(v-1, v)$  respectively. If rotational and vibrational wave functions are assumed to be separable,  $j$  coefficients can be assumed such that the following relation is satisfied

$$\sum_j a(j', j) = \sum_j b(j, j') = \sum_j b(j, j') = 1$$

Based on the above assumption for a two level transition of molecules contained in a volume  $dS$  (cross section is assumed to be unity), the change in radiative energy within the solid angle  $d\Omega$ , can be written as

$$\frac{dI_v}{ds} d\Omega = n(v) f(j') a(j', j) A(v, v-1) \left( \frac{d\Omega}{4\pi} \right)$$

$$\begin{aligned}
& - [n(v - 1)f(j)b(j, j')B(v - 1, v) - n(v)f \\
& - n(v)f(j')b(j', j)B(v, v - 1)] \frac{I_\nu}{c} d\Omega
\end{aligned} \tag{3.21}$$

where first, second, and third terms on the right represent contribution due to spontaneous emission, absorption, and induced emission respectively, and  $c$  is the speed of light.

If one applies the principle of detailed balance, following relations are obtained

$$a(j', j) A(v, v - 1) = \delta_\nu b(j', j) B(v, v - 1) \tag{3.22a}$$

$$b(j', j) B(v, v - 1) = \frac{g(j)}{g(j')} b(j, j') B(v - 1, v) \tag{3.22b}$$

where  $\delta_\nu = 8\pi \nu^2/c^3$  and  $g(j)$  is the statistical weight of  $j$  th rotational level. The following relation is obtained for a simple harmonic oscillator from quantum mechanics

$$B(v, v - 1) = \nu B(0, 1) \tag{3.23}$$

Since each pair of vibrational levels of a simple harmonic oscillator absorb and emit equal quanta, a summation over all the vibrational level is possible. As a result, the following relation can be obtained

$$E_\nu = \sum_{v=1}^{\infty} \nu n(v) \tag{3.24}$$

where  $E_\nu$  is written in the normalized form, and

$$E_\nu^* = n \left[ \exp\left(\frac{h\nu_0}{kT}\right) - 1 \right]^{-1} \tag{3.25a}$$

such that [31]

$$\frac{E_\nu}{E_\nu^*} = \frac{\left[ \exp\left(\frac{h\nu_0}{kT}\right) - 1 \right]}{\left[ \exp\left(\frac{h\nu_0}{kT_\nu}\right) - 1 \right]} \tag{3.25b}$$

where  $T_\nu$  is the nonequilibrium temperature.

By using Eqs. (3.22) through (3.25) in Eq. (3.21), the transfer equation can be written in the form

$$\frac{dI_\nu}{ds} = \frac{n B(0,1) b(j,j') f(j)}{c[1 - \exp(-\frac{h\nu_0}{\kappa T_\nu})]} \left\{ \frac{2h\nu^3}{c^2} \exp[-\frac{h}{\kappa}(\frac{\nu_0}{T_\nu} + \frac{\nu - \nu_0}{T})] - I_\nu + I_\nu \exp[-\frac{h}{\kappa}(\frac{\nu_0}{T_\nu} + \frac{\nu - \nu_0}{T})] \right\} \quad (3.26)$$

where  $n$  is the total number of molecules.

Equation (3.26) is written in an alternative form as

$$\frac{dI_\nu}{ds} = \kappa_\nu (S_\nu - I_\nu) \quad (3.27)$$

where  $\kappa_\nu$  and  $S_\nu$  are net absorption coefficient and source function respectively, and are given as

$$\kappa_\nu (n, T, T_\nu) = \frac{n B(0,1) b(j,j') f(j)}{c [1 - \exp(-\frac{h\nu_0}{\kappa T_\nu})]} \left\{ 1 - \exp[-\frac{h}{\kappa}(\frac{\nu_0}{T_\nu} + \frac{\nu - \nu_0}{T})] \right\} \quad (3.27a)$$

$$S_\nu (T, T_\nu) = \left( \frac{2h\nu^3}{c^2} \right) \left\{ \exp \left[ \frac{h}{\kappa} \left( \frac{\nu_0}{T_\nu} + \frac{\nu - \nu_0}{T} \right) \right] - 1 \right\} \quad (3.27b)$$

For the case of LTE,  $T_\nu = T$  and Eqs. (3.27a) and (3.27b) can be written as

$$\kappa_\nu^* (n, T) = \frac{n B(0,1)}{c} b(j,j') f(j) \left\{ \frac{1 - \exp(-\frac{h\nu}{\kappa T})}{1 - \exp(-\frac{h\nu_0}{\kappa T})} \right\} \quad (3.28a)$$

$$S_\nu^* = B_\nu (T) = \frac{\left( \frac{2h\nu^3}{c^2} \right)}{\left[ \exp \left( \frac{h\nu}{\kappa T} \right) - 1 \right]} \quad (3.28b)$$

where  $B_\nu$  is black body intensity of frequency  $\nu$  at local temperature.

Using Eqs. (3.25) through (3.28), radiation transfer equation can be given as

$$\frac{dI_{\nu}}{ds} = \kappa_{\nu} \left( \frac{\kappa_{\nu}^*}{\kappa_{\nu}} B_{\nu} \frac{E_{\nu}}{E_{\nu}^*} - I_{\nu} \right) = \kappa_{\nu}^* \left( B_{\nu} \frac{E_{\nu}}{E_{\nu}^*} - \frac{\kappa_{\nu}}{\kappa_{\nu}^*} I_{\nu} \right) \quad (3.29)$$

Comparing Eq. (3.29) with Eq. (3.27), it is seen that the quantity  $\frac{\kappa_{\nu}^*}{\kappa_{\nu}} B_{\nu} \frac{E_{\nu}}{E_{\nu}^*}$  is the source function  $S(T, T_{\nu})$ . Equation (3.29) can be regarded as the nonequilibrium radiative transfer equation and is identical to that obtained by Goody [ 4 ].

Under steady state conditions, for each fundamental band, a combination of Eqs. (3.13), (3.14), and (3.29) results in

$$\left( \frac{E_{\nu}}{E_{\nu}^*} \right) \left[ \left( \frac{E_{\nu}^*}{\eta_c} \right) + \int d\Omega \int \kappa_{\nu} B_{\nu} d\nu \right] = \left( \frac{E_{\nu}^*}{\eta_c} \right) + \int d\Omega \int \kappa_{\nu} I_{\nu} d\nu \quad (3.30)$$

where integration is taken over the frequency range of an individual band and over the solid angle from 0 to  $4\pi$ . If one introduces a time constant  $\eta_r$  as

$$\eta_r = \frac{E_{\nu}^*}{\int d\Omega \int \kappa_{\nu} B_{\nu} d\nu} \quad (3.31)$$

then combining Eqs. (3.29) and (3.30), one can write the radiative transfer equation as

$$\frac{dI_{\nu}}{ds} = \kappa_{\nu} (J_{\nu} - I_{\nu}) \quad (3.32a)$$

where

$$J_{\nu} = B_{\nu} \frac{(\eta_r + \eta_c X)}{(\eta_r + \eta_c)} \quad (3.32b)$$

and

$$X = \frac{\int d\Omega \int \kappa_\nu I_\nu d\nu}{\int d\Omega \int \kappa_\nu B_\nu d\nu} \quad (3.32c)$$

The quantity  $\eta_r$  is called the radiative life time of vibrational states. It can be shown that [33]  $\eta_r = 1/A(1,0)$ , where  $A(1,0)$  is the Einstein coefficient for spontaneous emission from the first vibrational level.

A combination of Eqs. (3.12) and (3.32) yields an alternative expression for  $J_\nu$

$$J_\nu = \frac{B_\nu}{\eta_r + \eta_c} \frac{\{ \eta_r + \eta_c [ (\bar{h} + \int d\Omega \int \kappa_\nu J_\nu d\nu) ] \}}{\int d\Omega \int \kappa_\nu B_\nu d\nu} \quad (3.33a)$$

where

$$\bar{h} = - \int \frac{dq_{R\nu}}{dy} d\nu \quad (3.33b)$$

By noting that  $B_\nu$  and  $J_\nu$  are isotropic,  $J_\nu$  can be expressed as

$$J_{\nu c} = B_{\nu c} + \frac{1}{2} \left( \frac{\eta_c}{\eta_r} \right) \bar{H} \quad (3.34a)$$

where

$$H = \frac{\bar{h}}{2\pi \int \kappa_\nu d\nu} \quad (3.34b)$$



and  $J_{\nu c}$  and  $B_{\nu c}$  are the values evaluated at the band center. This is because  $J_{\nu}$  and  $B_{\nu}$  are slowly varying functions of  $\nu$  and for narrow bands, they can be assumed to be independent of  $\nu$ . In Eqs. (3.32) and (3.33),  $B_{\nu}$  is called blackbody intensity of radiation and is related to the Planck function of radiation  $e_{b\nu}$  by  $e_{b\nu} = \pi B_{\nu}$ . This relation is true for isotropic radiation.

For very low pressures, the collisional relaxation time  $\eta_c$  is large compared to  $\eta_r$  [31]. Therefore, the right hand side of Eq. (3.32b) reduces to  $B_{\nu} X$ . On the other hand, for high pressures,  $\eta_c$  approaches zero and the right hand side of Eq. (3.32b) becomes  $B_{\nu}$  which is equivalent to the Planck function. This is the situation of LTE usually assumed in most radiation transfer analyses.

The NLTE effect is characterized by the nonequilibrium parameter  $\eta$  which is expressed as  $\eta = \eta_c / \eta_r$ . When  $\eta$  is unity or greater than unity, NLTE effect usually prevails; whereas for  $\eta$  being less than unity, LTE effect usually prevails.

A combination of Eqs. (3.25a), (3.28b), and (3.31) results in an expression for  $\eta_r$  [31]

$$\eta_r^{-1} = 8\pi \left( \frac{\nu_0}{c} \right)^2 \int \left( \frac{\kappa_{\nu}}{n} \right) d\nu = 8\pi c \omega_c^2 \left( \frac{P}{n} \right) \int \left( \frac{\kappa_{\omega}}{P} \right) d\omega \quad (3.35)$$

where  $n$  is the number density of the molecules, and  $\omega_c = (\nu_0 / c)$  is the wave number corresponding to  $\nu_0$ . In the derivation of Eq. (3.35), it has been assumed that  $B_{\nu}$  is independent of frequency. An alternative form of Eq. (3.35) is given as

$$\eta_r^{-1} = (8\pi \omega_c^2) (4.08 \times 10^{-12}) T_0 S(T_0) \quad (3.36)$$

where  $S$  is the integrated band intensity as defined in the earlier section and  $T_0$  is the reference temperature. The radiative life time  $\eta_r$  has the units of seconds, and for fundamental bands of some important molecules values of  $\eta_r$  are tabulated in Appendix A.

### 3.4 Radiative Flux Equations

For this study, the physical model consists of an absorbing-emitting gas bounded by two infinite parallel plates ( Fig. 3.1 ). The plate surfaces are assumed to emit and reflect in a diffused manner. For the physical model considered, the integration of the transfer equation, Eq. (3.32a), gives

$$q_{R\omega} = 2 B_{1\omega} E_3(\tau_\omega) - 2 B_{2\omega} E_3(\tau_{0\omega} - \tau_\omega) + 2\pi \left[ \int_0^{\tau_\omega} J_\omega(t) E_2(\tau_\omega - t) dt - \int_{\tau_\omega}^{\tau_{0\omega}} J_\omega(t) E_2(t - \tau_\omega) dt \right] \quad (3.37)$$

where

$$\tau_\omega = \kappa_\omega y, \quad \tau_{0\omega} = \kappa_\omega L \quad (3.38a)$$

$$J_\omega(t) = \frac{e_\omega(t)}{\pi} + \frac{1}{2}\eta \bar{H}(t), \quad \eta = \frac{\eta_c}{\eta_r} \quad (3.38b)$$

$$\bar{H}(y) = \frac{-\text{div } q_R(y)}{2\pi P S(T)} = \frac{-\int_0^\infty \left( \frac{dq_{R\omega}}{dy} \right) d\omega}{2\pi P S(T)} \quad (3.38c)$$

In Eq. (3.37),  $\tau_{0\omega}$  is the optical path length and  $t$  is a dummy variable for  $\tau_{0\omega}$ . The quantities  $B_{1\omega}$  and  $B_{2\omega}$  are surface radiosities, and  $E_n(t)$  are exponential integral functions. It has been assumed that the spectral absorption coefficient  $\kappa_{\omega}$  is independent of temperature. The detailed explanation of the derivation of Eq. (3.37) is given in [ 31 ]. The expressions for surface radiosity can be given as [ 6 ]

$$B_{1\omega} = \varepsilon_{1\omega} e_{1\omega} + 2 (1 - \varepsilon_{1\omega}) [ B_{2\omega} E_3(\tau_{0\omega}) + \pi \int_0^{\tau_{0\omega}} J_{\omega}(t) E_2(t) dt ] \quad (3.39a)$$

$$B_{2\omega} = \varepsilon_{2\omega} e_{2\omega} + 2 (1 - \varepsilon_{2\omega}) [ B_{1\omega} E_3(\tau_{0\omega}) + \pi \int_0^{\tau_{0\omega}} J_{\omega}(t) E_2(\tau_{0\omega} - t) dt ] \quad (3.39b)$$

For black surfaces,  $B_{1\omega} = e_{1\omega}$  and  $B_{2\omega} = e_{2\omega}$ . This is obvious from Eq. (3.39) because in that case  $\varepsilon_{1\omega} = \varepsilon_{2\omega} = 1$ . Under the assumptions of LTE,

$$J_{\omega}(t) = \frac{e_{\omega}(t)}{\pi}$$

The total radiative flux is given by

$$q_R = \int_0^{\infty} q_{R\omega} d\omega \quad (3.40)$$

Under LTE assumptions, Eq. (3.37) may be expressed for black bounding surfaces as

$$q_{R\omega}(\tau_{\omega}) = e_{1\omega} - e_{2\omega} + 2 \left[ \int_0^{\tau_{\omega}} F_{1\omega}(t) E_2(\tau_{\omega} - t) dt - \int_{\tau_{\omega}}^{\tau_{0\omega}} F_2(t) E_2(t - \tau_{\omega}) dt \right] \quad (3.41)$$

where

$$F_{1\omega}(t) = e_{\omega}(t) - e_{1\omega} ; F_{2\omega}(t) = e_{\omega}(t) - e_{2\omega}$$

A direct differentiation of Eq. (3.41) gives

$$-\frac{dq_{R\omega}}{d\tau_{\omega}} = -2 [ F_{1\omega}(\tau_{\omega}) + F_{2\omega}(\tau_{\omega}) ] + 2 \left[ \int_0^{\tau_{\omega}} F_{1\omega}(t) E_1(\tau_{\omega} - t) dt \right. \\ \left. + \int_{\tau_{\omega}}^{\tau_{0\omega}} F_{2\omega}(t) E_1(t - \tau_{\omega}) dt \right] \quad (3.42)$$

Equations (3.41) and (3.42) are the LTE radiative flux equations for the physical model described in Figs. (3.1) and (3.2).

Equation (3.37) can be written in a different form by replacing the exponential integral  $E_n(t)$  by an exponential function. The exponential integrals  $E_2(t)$  and  $E_3(t)$  in Eq. (3.37) are approximated as follows

$$E_2(t) \approx \frac{3}{4} \exp\left(-\frac{3}{2}t\right) ; E_3(t) = - \int E_2(t) dt \approx \frac{1}{2} \exp\left(-\frac{3}{2}t\right) \quad (3.43)$$

The detailed discussion of this approximation is available in [6]. Substituting Eq. (3.43) in Eq. (3.37), one obtains

$$q_{R\omega} = B_{1\omega} \exp\left[-\frac{3}{2} \kappa_{\omega} y\right] - B_{2\omega} \exp\left[-\frac{3}{2} \kappa_{\omega} (L - y)\right]$$

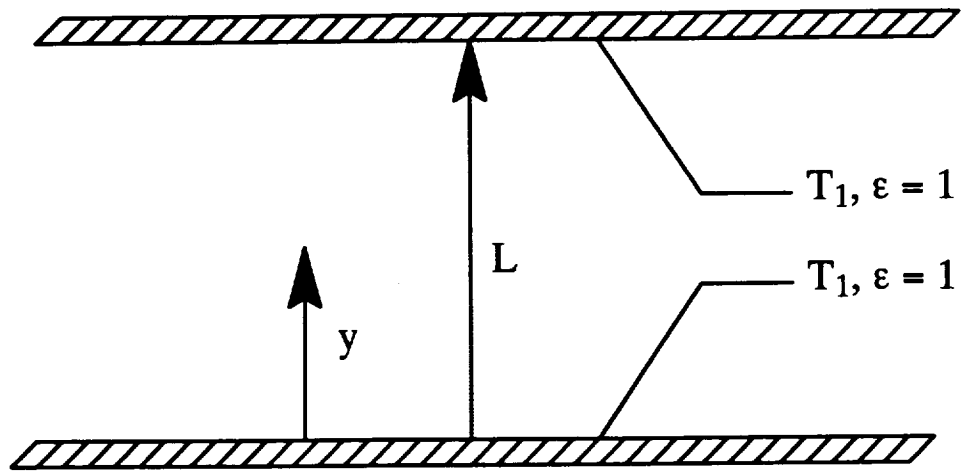


Fig. 3.1 Physical model for radiative interaction

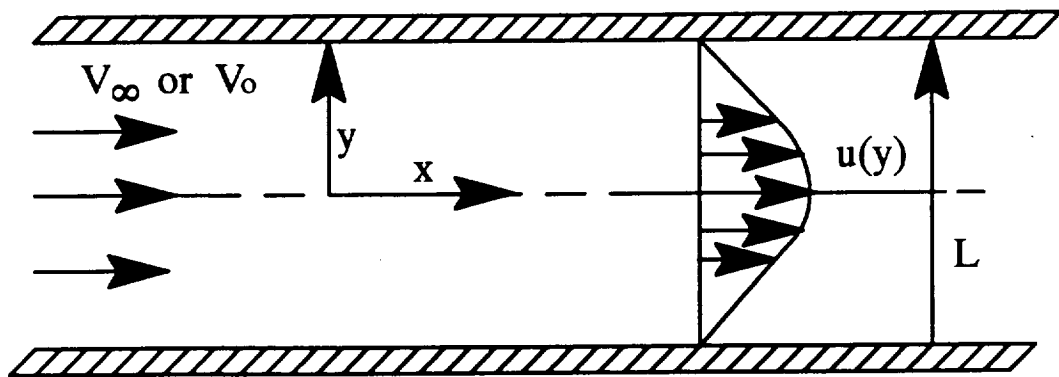


Fig. 3.2 Incompressible laminar flow between two parallel plates

$$+ \frac{3\pi}{2} \left\{ \int_0^y J_{\omega}(z) \kappa_{\omega} \exp\left[-\frac{3}{2} \kappa_{\omega}(y-z)\right] dz - \int_y^L J_{\omega}(z) \kappa_{\omega} \exp\left[-\frac{3}{2} \kappa_{\omega}(z-y)\right] dz \right\} \quad (3.44)$$

For black bounding surfaces, the radiosities appearing in Eq. (3.44) should be replaced by appropriate expressions of the Planck function.

### 3.4.1 Nongray Formulation

A combination of Eqs. (3.40) and (3.44) gives the following expression for radiative flux for nongray gases

$$q_R = e_1 - e_2 + \frac{3}{2} \int_0^y \left[ \pi J_{\omega c}(z) - e_{1\omega c} \right] \int_{\Delta\omega} \kappa_{\omega} \exp\left[-\frac{3}{2} \kappa_{\omega}(y-z)\right] d\omega dz - \frac{3}{2} \int_y^L \left[ \pi J_{\omega c}(z) - e_{2\omega c} \right] \int_{\Delta\omega} \kappa_{\omega} \exp\left[-\frac{3}{2} \kappa_{\omega}(z-y)\right] d\omega dz \quad (3.45)$$

Equation (3.45) is valid for black bounding surfaces and it has been assumed that  $J_{\omega}(y)$  is independent of wave number within the band.

By defining the following nondimensional independent variables

$$\xi = \frac{y}{L} = \frac{\tau_{\omega}}{\tau_{0\omega}} = \frac{u}{u_0} ; \quad \xi' = \frac{u'}{u_0} = \frac{z}{L} \quad (3.46)$$

where  $u$  is the dimensionless path length and  $u_0 = (S/A_0) PL$ , the radiative flux equation is expressed in it's final form as

$$\begin{aligned}
 q_R(\xi) = & e_1 - e_2 \\
 & + \frac{3}{2} A_0 u_0 \left\{ \int_0^{\xi} F_{1\omega c} \bar{A}' \left[ \frac{3}{2} u_0 (\xi - \xi') d\xi' \right] - \int_{\xi}^1 F_{2\omega c} \bar{A}' \left[ \frac{3}{2} u_0 (\xi' - \xi) d\xi' \right] \right\} \\
 & - \frac{3}{8} \eta \left\{ \int_0^{\xi} \left( \frac{dq_R}{d\xi'} \right) \bar{A}' \left[ \frac{3}{2} u_0 (\xi - \xi') d\xi' \right] - \int_{\xi}^1 \left( \frac{dq_R}{d\xi'} \right) \bar{A}' \left[ \frac{3}{2} u_0 (\xi' - \xi) d\xi' \right] \right\} \quad (3.47)
 \end{aligned}$$

where  $\bar{A}'(u)$  is the derivative of the dimensionless band absorptance  $\bar{A}(u)$  with respect to  $u$ . The detailed derivation of Eq. (3.47) is provided in [31].

Equation (3.47) is applicable to gases which have only one fundamental band contributing to the radiative process. For a multiband system, Eq. (3.47) can be written in the form

$$\begin{aligned}
 q_R(\xi) = & e_1 - e_2 \\
 & + \frac{3}{2} \sum_{i=1}^n A_{0i} u_{0i} \left\{ \int_0^{\xi} F_{1\omega i} \bar{A}'_i \left[ \frac{3}{2} u_{0i} (\xi - \xi') d\xi' \right] - \int_{\xi}^1 F_{2\omega i} \bar{A}'_i \left[ \frac{3}{2} u_{0i} (\xi' - \xi) d\xi' \right] \right\} \\
 & - \frac{3}{8} \sum_{i=1}^n \eta_i \left\{ \int_0^{\xi} \left( \frac{dq_R}{d\xi'} \right) \bar{A}'_i \left[ \frac{3}{2} u_{0i} (\xi - \xi') d\xi' \right] - \int_{\xi}^1 \left( \frac{dq_R}{d\xi'} \right) \bar{A}'_i \left[ \frac{3}{2} u_{0i} (\xi' - \xi) d\xi' \right] \right\} \quad (3.48)
 \end{aligned}$$

where  $n$  denotes the number of bands.

Equation (3.48) can be regarded as a general expression for radiative flux equation. For LTE case, the last two terms, i.e., the terms involving  $\eta$ , vanish, and for NLTE case, Eq. (3.48) could be regarded as the radiative flux equation in nongray gases.

### 3.4.2 Gray Consideration under LTE Assumption

Under LTE assumption, a combination of Eq. (3.40) and (3.44) results in the following radiative flux equation

$$q_{RL}(\tau) = F(\tau) + \Gamma \left\{ \int_0^{\tau} T^4(t) \exp[-b(\tau - t)] dt - \int_{\tau}^{\tau_0} T^4(t) \exp[-b(t - \tau)] dt \right\} \quad (3.49a)$$

where

$$F(\tau) = \sigma T_1^4 \exp(-b\tau) - \sigma T_2^4 \exp[-b(\tau_0 - \tau)] \quad (3.49b)$$

$$b = \frac{3}{2}; \quad \Gamma = b\sigma \quad (3.49c)$$

Differentiating Eq. (3.49a) twice by using the Leibnitz formula, one obtains

$$\frac{d^2 q_{RL}}{d\tau^2} = \frac{d^2 F}{d\tau^2} + 2\Gamma \frac{dT^4}{d\tau} + \Gamma b^2 \left\{ \int_0^{\tau} T^4(t) \exp[-b(\tau - t)] dt - \int_{\tau}^{\tau_0} T^4(t) \exp[-b(t - \tau)] dt \right\} \quad (3.50)$$

Elimination of integrals between Eqs. (3.49a) and (3.50) results in

$$\frac{d^2 q_{RL}}{d\tau^2} - b^2 q_{RL}(\tau) = 2\Gamma \frac{dT^4}{d\tau} + \frac{d^2 F}{d\tau^2} - b^2 F(\tau) \quad (3.51)$$



Equation (3.51) is the general differential equation for radiative flux for gray gases under LTE assumption. For the specific relation of  $F(\tau)$  as defined in Eq. (3.49b), there is obtained

$$\frac{d^2 F}{d\tau^2} - b^2 F(\tau) = 0$$

Consequently, Eq. (3.51) reduces to

$$\frac{d^2 q_{RL}}{d\tau^2} - \frac{9}{4} q_R = 3\sigma \frac{dT^4}{d\tau} \quad (3.52)$$

This is the appropriate relation for radiative flux for gray gas analyses under LTE assumption of the present physical problem.

### 3.4.3 Gray Consideration under NLTE Assumption

The radiative flux equation for gray gas analyses under NLTE assumption can be obtained by adding the NLTE part of the radiative flux equation in Eq. (3.50). The NLTE part of the radiative flux equation can be given by

$$q_{RN} = -KS \left\{ \int_0^\tau \frac{dq_R}{dt} \exp[-b(\tau - t)] dt - \int_\tau^{\tau_0} \frac{dq_R}{dt} \exp[-b(t - \tau)] dt \right\} \quad (3.53a)$$

where

$$KS = \frac{3}{8} \frac{\eta}{PS(T)} \quad (3.53b)$$

Differentiating Eq. (3.53a) twice by using Leibnitz formula, one obtains

$$\frac{d^2 q_{RN}}{d\tau^2} = -2KS \frac{d^2 q_R}{d\tau^2} - KSb^2 \left\{ \int_0^\tau \frac{dq_R}{dt} \exp[-b(\tau - t)] dt - \int_\tau^{\tau_0} \frac{dq_R}{dt} \exp[-b(t - \tau)] dt \right\} \quad (3.54)$$

Equation (3.50) is the radiative flux equation under LTE assumption. The flux equation under NLTE assumption is given by combining Eqs. (3.50) and (3.54).

$$M_2 \frac{d^2 q_R}{d\tau^2} - \frac{9}{4} q_R = 3\sigma \frac{dT^4}{d\tau} \quad (3.55a)$$

where

$$M_2 = (1 + 2KS) \quad (3.55b)$$

Equation (3.55a) can be regarded as the radiative flux equation for gray gas analyses under NLTE assumption. The complete derivation of Eq. (3.55a) is provided in Appendix B.

## **Chapter 4**

# **GRAY RADIATIVE TRANSFER IN LAMINAR FLOW**

Gray medium assumption is probably the greatest approximation for the real gases. This assumption replaces the wave number dependent absorption coefficient by a wave number averaged quantity. The following sections deal with the general formulation and the resulting equations under LTE and NLTE conditions for gray gas assumption.

### **4.1 General Formulation**

The physical model considered is assumed to be the same as discussed in the previous chapter ( Figs. 3.1 and 3.2 ). The boundary condition along each of the plate surfaces is taken to be that of a uniform heat flux, and thus the temperature of the plates  $T$  varies in the axial direction only. Only fully developed flow and heat transfer are considered. Attention is additionally restricted to small temperature differences, such that constant properties and linearized radiation may be assumed.

Since the wall temperature varies in the axial direction, there will exist radiative transfer between wall elements located at different axial positions, and in general this would preclude the possibility of achieving fully developed heat transfer. For linearized radiation, however,

it is easily shown that fully developed heat transfer can be obtained with the subsequent result that there will be no net radiative transfer between the wall elements.

Within the confines of the foregoing assumptions, the energy equation for the present problem can be obtained from Eq. (2.6) as

$$v_x \frac{\partial T}{\partial x} = \alpha \frac{\partial^2 T}{\partial y^2} - \frac{1}{\rho C_p} \frac{\partial q_R}{\partial y} \quad (4.1)$$

where the parabolic velocity profile is given by

$$v_x = 6v_m \left[ \frac{y}{L} - \left( \frac{y}{L} \right)^2 \right] \quad (4.2a)$$

The mean velocity is given by the expression

$$v_m = \frac{1}{A_c} \int_{A_c} v_x dA_c \quad (4.2b)$$

where  $A_c$  represents the cross sectional area normal to the direction of flow. For uniform wall heat flux and fully developed heat transfer,  $\partial T / \partial x$  is a constant and is given by the expression

$$\frac{\partial T}{\partial x} = \frac{2\alpha q_w}{v_m L \kappa} \quad (4.2c)$$

Employing these quantities, Eq. (4.1) can be written in dimensionless form as

$$12(\xi - \xi^2) = \frac{d^2 \theta_p}{d\xi^2} - \frac{1}{q_w} \frac{dq_R}{d\xi} \quad (4.3a)$$

where

$$\xi = \frac{y}{L} ; \quad \theta_p = \frac{(T - T_1)}{\left( \frac{q_w L}{\kappa} \right)} \quad (4.3b)$$

Upon integrating this equation once, and by noting that  $d\theta_p/d\xi = 0$  and  $q_R = 0$  at  $\xi = 1/2$ , one finds

$$\frac{d\theta_p}{d\xi} - 2(3\xi^2 - 2\xi^3) + 1 = \frac{q_R}{q_w} \quad (4.4)$$

Equation (4.4) can be treated as the general governing equation for both gray and nongray analyses. The only difference will be shown by the radiative flux equation on the right hand side of Eq. (4.4). Proper form of the radiative flux equation should be used in Eq. (4.4) to get the final solution for the dimensionless temperature,  $\theta_p$ .

## 4.2 LTE Assumption

As mentioned earlier, gray medium approximation replaces the wave number dependent absorption coefficient by a wave number averaged quantity. For lack of more rational choice, this average coefficient will be taken to be  $\kappa_p(T_1)$ . For convenience, attention will be directed only to black bounding surfaces. Replacing  $\kappa_\omega$  by  $\kappa_p$  in Eq. (3.44), integrating over the wave number, and utilizing the linearized expression  $T^4 - T_1^4 = 4T^3(T - T_1)$ , following expression is obtained for the present problem

$$q_R = 6\sigma\kappa_p T_1^3 \left\{ \int_0^y [T(z) - T_1] \exp\left[-\frac{3}{2}\kappa_p(y-z)\right] dz - \int_y^L [T(z) - T_1] \exp\left[-\frac{3}{2}\kappa_p(z-y)\right] dz \right\} \quad (4.5)$$

Upon differentiating this equation twice, the integrals repeat themselves and may be eliminated, and the resulting equation can be expressed as

$$\frac{d^2 q_R}{d\xi^2} - \frac{9}{4} \tau^2 q_R = \gamma_1 q_w \frac{d\theta_p}{d\xi} \quad (4.6a)$$

where

$$\gamma_1 = \frac{3\tau_0^2}{\bar{N}} ; \bar{N} = \frac{\kappa \kappa_p}{4\sigma T_1^3} ; \tau_0 = \kappa_p L \quad (4.6b)$$

The boundary conditions for this equation are

$$q_R\left(\frac{1}{2}\right) = 0 ; \frac{3}{2} q_R(0) = \frac{1}{\tau_0} \left( \frac{dq_R}{d\xi} \right)_{\xi=0} \quad (4.6c)$$

Note that Eq. (4.6a) is analogous to Eq. (3.52) which was the radiative flux equation for gray gases under LTE assumption. The simultaneous solution of Eqs. (4.4) and (4.6) is straightforward and the final expression for the dimensionless bulk temperature,  $\theta_{bp}$ , is expressed as [31]

$$\theta_{bp} = C_1 [24 - 12M_1 + M_1^3 + (M_1^3 - 12M_1 - 24) \exp(-M_1)] - \frac{12}{5} \frac{\gamma_1}{M_1^4} + \frac{17}{70} \frac{\gamma_1}{M_1^2} - \frac{17}{70} \quad (4.7a)$$

where

$$C_1 = \frac{\gamma_1}{M_1^8} \left[ \frac{48 - 3\tau_0 M_1^2 + 36\tau_0}{3\tau_0(1 - e^{-M_1}) + 2M_1(1 + e^{-M_1})} \right] \quad (4.7b)$$

$$M_1^2 = 3 \tau_0^2 \left( \frac{3}{4} + \frac{1}{\bar{N}} \right) \quad (4.7c)$$

The governing parameters for this equation are  $\bar{N}$  and  $\tau_0$ . Note that  $\bar{N}$  characterizes the relative importance of radiation versus conduction for gray gases.

### 4.3 NLTE Consideration

Under NLTE consideration, a combination of Eqs. (3.55) and (4.4) gives

$$\frac{d^2 q_R}{d\xi^2} - \overline{M}_1^2 q_R = \overline{\gamma}_1 q_w (6\xi^2 - 4\xi^4 + 1) \quad (4.8a)$$

where

$$\overline{M}_1 = \frac{M_1}{\sqrt{M_2}}; \quad \overline{\gamma}_1 = \frac{\gamma_1}{M_2}; \quad M_2 = 1 + \frac{3}{4} \frac{\eta}{PS(T)} \quad (4.8b)$$

The quantities  $M_1$  and  $\gamma_1$  are defined in the same way as discussed in the preceding section.

The solution of Eq. (4.8) is given as

$$\theta_{bp} = C_1 [24 - 12\overline{M}_1 + \overline{M}_1^3 + (\overline{M}_1^3 - 12\overline{M}_1 - 24)e^{-\overline{M}_1}] - \frac{12}{5} \frac{\overline{\gamma}_1}{\overline{M}_1^4} + \frac{17}{70} \frac{\overline{\gamma}_1}{\overline{M}_1^2} - \frac{17}{70} \quad (4.9a)$$

where

$$C_1 = \frac{\overline{\gamma}_1}{\overline{M}_1^8} \left[ \frac{48 - 3\tau_0 \overline{M}_1^2 + 36\tau_0}{3\tau_0(1 - e^{-\overline{M}_1}) + 2\overline{M}_1(1 + e^{-\overline{M}_1})} \right] \quad (4.9b)$$

Thus it is obvious that  $\eta$  is the driving force for NLTE. For  $\eta = 0$ ,  $M_2 = 1$ , and the solution for  $\theta_{bp}$  reduces to that under LTE.





## Chapter 5

# NONGRAY RADIATIVE TRANSFER IN LAMINAR FLOW

In this chapter, the radiative heat transfer is discussed for nongray gases. General formulation of the problem is the same as discussed in the previous chapter. The solutions under LTE and NLTE conditions are presented in next sections.

### 5.1 LTE Assumption

The nongray radiative flux equation under LTE assumption is given by dropping the NLTE part of Eq. (3.48)

$$\begin{aligned}
 q_R(\xi) = e_1 - e_2 \\
 + \frac{3}{2} \sum_{i=1}^n A_{0i} U_{0i} \left\{ \int_0^{\xi} F_{1\omega_i} \bar{A}_i' \left[ \frac{3}{2} u_{0i}(\xi - \xi') d\xi' \right] - \int_{\xi}^0 F_{2\omega_i} \bar{A}_i' \left[ \frac{3}{2} u_{0i}(\xi' - \xi) d\xi' \right] \right\}
 \end{aligned}
 \tag{5.1}$$



Using the following relations

$$F_{1\omega i} = e_{\omega i}(\xi') - e_{1\omega i} = \left( \frac{de_{\omega i}}{dT} \right)_{T_1} (T - T_1) \quad (5.2a)$$

$$F_{2\omega i} = e_{\omega i}(\xi') - e_{2\omega i} = \left( \frac{de_{\omega i}}{dT} \right)_{T_2} (T - T_2) \quad (5.2b)$$

$$H_{1i} = A_{0i}(T) \left( \frac{de_{\omega i}}{dT} \right)_{T_1} \quad (5.2c)$$

$$H_{2i} = A_{0i}(T) \left( \frac{de_{\omega i}}{dT} \right)_{T_2} \quad (5.2d)$$

$$\theta_{1p}(\xi) = \frac{(T - T_1)}{\left( \frac{q_w L}{\kappa} \right)} \quad (5.2e)$$

$$\theta_{2p}(\xi) = \frac{(T - T_2)}{\left( \frac{q_w L}{\kappa} \right)} \quad (5.2f)$$

Equation (5.1) can be expressed in an alternative form as

$$\frac{q_R(\xi)}{q_w} = e_1 - e_2 + \frac{3L}{2\kappa} \sum_{i=1}^n u_{0i} \left\{ H_{1i} \int_0^{\xi} \theta_{1p}(\xi') \bar{A}'(I) d\xi' - H_{2i} \int_{\xi}^1 \theta_{2p}(\xi') \bar{A}'(II) d\xi' \right\} \quad (5.3a)$$

where

$$\bar{A}'(I) = \bar{A}' \left[ \frac{3}{2} u_{0i} (\xi - \xi') \right] ; \quad \bar{A}'(II) = \bar{A}' \left[ \frac{3}{2} u_{0i} (\xi' - \xi) \right] \quad (5.3b)$$

If, at any x-location, the two plates have the same temperature, then  $T_1 = T_2$  and  $e_1 = e_2$ , and

Eq. (5.3a) becomes

$$\frac{q_R(\xi)}{q_w} = \frac{3L}{2\kappa} \sum_{i=1}^n H_i u_{0i} \left\{ \int_0^{\xi} \theta_p(\xi') \bar{A}'(I) d\xi' - \int_{\xi}^1 \theta_p(\xi') \bar{A}'(II) d\xi' \right\} \quad (5.4)$$

Combining Eqs. (4.4) and (5.4), one obtains

$$\frac{d\theta_p}{d\xi} - 2(3\xi^2 - 2\xi^3) + 1 = \frac{q_R(\xi)}{q_w} = \frac{3L}{2\kappa} \sum_{i=1}^n H_i \mu_{0i} \left\{ \int_0^{\xi} \theta_p(\xi') \bar{A}'(I) d\xi' - \int_{\xi}^1 \theta_p(\xi') \bar{A}'(II) d\xi' \right\} \quad (5.5)$$

The temperature profile within the gas,  $\theta_p(\xi)$ , is thus described by Eq. (5.5). The boundary condition for this equation follows to be  $\theta_p(0) = 0$ .

For flow problems, the quantity of primary interest is the bulk temperature of the gas, which is the mean temperature at any location  $x$  in the flow direction. It is the temperature which fluid would assume if it was instantaneously and adiabatically mixed after leaving the cross section under consideration. Mathematically, the bulk temperature is defined as

$$T_b = \frac{1}{u_m A_c} \int_{A_c} u T dA \quad (5.6)$$

The bulk temperature can be expressed in dimensionless form as

$$\theta_{bp} = \frac{T_b - T_1}{\left(\frac{q_w L}{\kappa}\right)} = 6 \int_0^1 \theta_p(\xi) (\xi - \xi^2) d\xi \quad (5.7)$$

The heat transfer  $q_w$  is given by the expression  $q_w = h_c (T_1 - T_b)$ , where  $h_c$  is the equivalent heat transfer coefficient in Watts / m<sup>2</sup>-K. The heat transfer results are expressed usually in terms of the Nusselt number,  $N_u$ , defined in terms of the hydraulic diameter  $D_h$ . For the present geometry,  $D_h = 2L$ . Eliminating the effective heat transfer coefficient  $h_c$  from the expression for  $q_w$  and  $N_u$ , a relation between the Nusselt number and the bulk temperature is obtained as

$$N_u = \frac{2L q_w}{\kappa(T_1 - T_b)} = \frac{-2}{\theta_{bp}} \quad (5.8)$$

The numerical solution of Eq. (5.5) is obtained by employing the method of undetermined parameters. For this case, a polynomial solution for  $\theta_p(\xi)$  is assumed as

$$\theta_p(\xi) = a_0 + a_1\xi + a_2\xi^2 + a_3\xi^3 + a_4\xi^4 \quad (5.9)$$

After employing the conditions  $\theta_p(0) = 0$ ,  $\theta_p'(1/2) = 0$ , and  $\theta_p'(0) = -\theta_p'(1)$ , Eq. (5.9) becomes

$$\theta_p(\xi) = a_1(\xi - 2\xi^3 + \xi^4) + a_2(\xi^2 - 2\xi^3 + \xi^4) \quad (5.10)$$

The constants  $a_1$  and  $a_2$  are obtained by satisfying the governing integro-differential equation at two convenient locations  $\xi = 0$ , and  $\xi = 1/4$ . A combination of Eq. (5.7) and (5.10) results in

$$\theta_{bp} = \frac{1}{70}(17a_1 + 3a_2) \quad (5.11)$$

Thus, with  $a_1$  and  $a_2$  known, the bulk temperature (or the Nusselt number) is obtained from Eq. (5.11). The procedure for evaluating the constants  $a_1$  and  $a_2$  is described in detail in [32].

## 5.2 NLTE Consideration

The radiative flux equation under NLTE consideration is given by Eq. (3.48). By employing definitions given in Eqs. (5.2) and (5.3b), Eq. (3.48) can be expressed in an alternative form as

$$q_R(\xi) = e_1 - e_2 + \frac{3}{2} \sum_{i=1}^n \left\{ H_{1i} \int_0^{\xi} (T - T_1) \overline{A}_i'(I) d\xi' - H_{2i} \int_{\xi}^1 (T - T_1) \overline{A}_i'(II) d\xi' \right\} \\ - \frac{3}{8} \sum_{i=1}^n \eta_i \left\{ \int_0^{\xi} \frac{dq_R}{d\xi'} \overline{A}_i'(I) d\xi' - \int_{\xi}^1 \frac{dq_R}{d\xi'} \overline{A}_i'(II) d\xi' \right\} \quad (5.12)$$

For black plates with  $T_1 = T_2$ ,  $e_1 = e_2$ , and Eq. (5.12) becomes

$$q_R(\xi) = \frac{3}{2} \sum_{i=1}^n \mu_{0i} H_i \left\{ \int_0^{\xi} (T - T_1) \overline{A}_i'(I) d\xi' - \int_{\xi}^1 (T - T_1) \overline{A}_i'(II) d\xi' \right\} \\ - \frac{3}{8} \sum_{i=1}^n \eta_i \left\{ \int_0^{\xi} \frac{dq_R}{d\xi'} \overline{A}_i'(I) d\xi' - \int_{\xi}^1 \frac{dq_R}{d\xi'} \overline{A}_i'(II) d\xi' \right\} \quad (5.13)$$

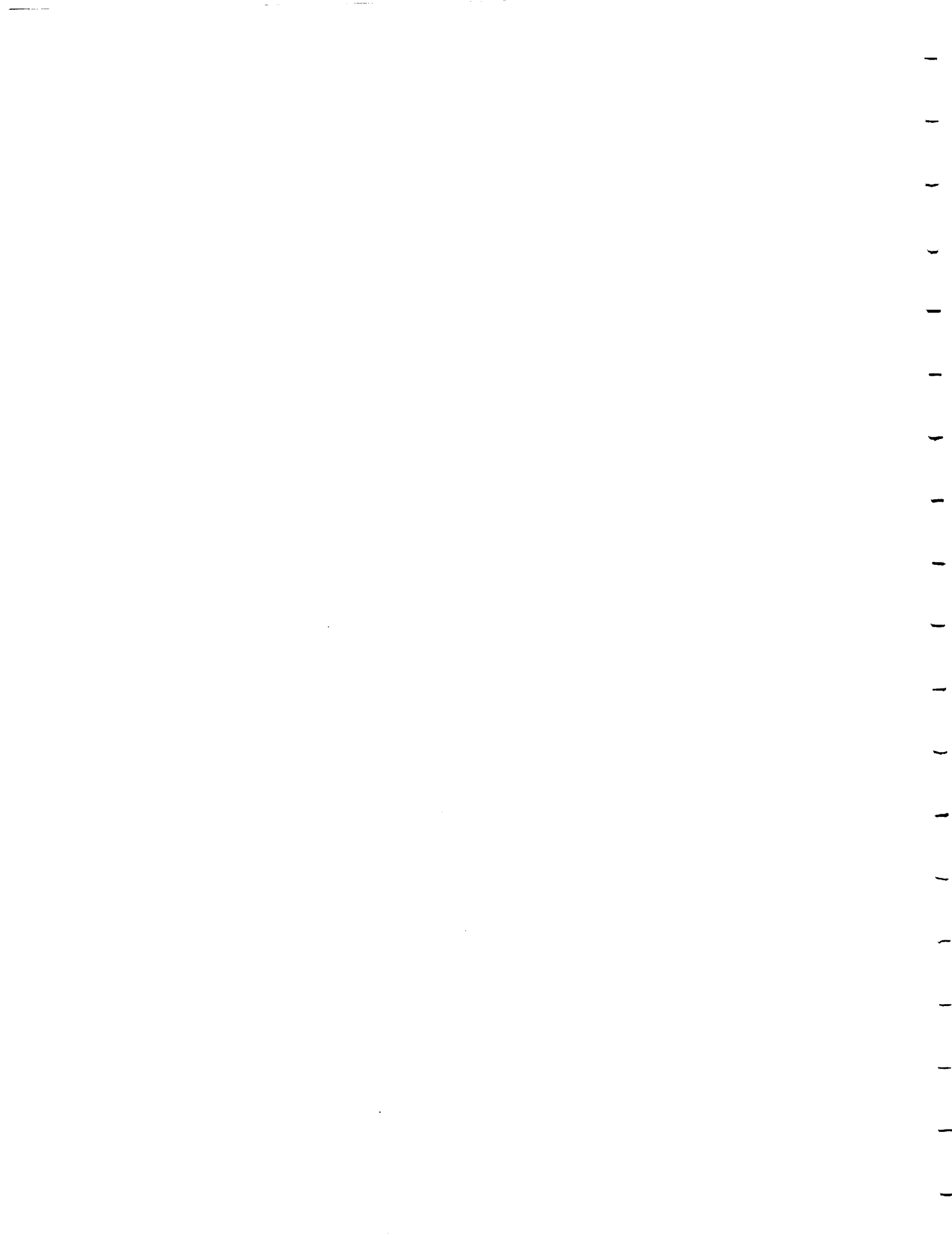
The energy equation is given by Eq. (4.3a) which is rewritten as

$$\frac{dq_R}{d\xi} = q_w \left[ \frac{d^2\theta_p}{d\xi^2} - 12(\xi - \xi^2) \right] \quad (5.14)$$

Combining Eqs. (4.4), (5.7), (5.13), and (5.14), one obtains

$$\frac{d\theta_p}{d\xi} - 2(3\xi^2 - 2\xi^3) + 1 = \\ \frac{3L}{2\kappa} \sum_{i=1}^n H_i \mu_{0i} \left\{ \int_0^{\xi} \theta(\xi') \overline{A}_i'(I) d\xi' - \int_{\xi}^1 \theta(\xi') \overline{A}_i'(II) d\xi' \right\} \\ - \frac{3}{8} \sum_{i=1}^n \eta_i \left\{ \int_0^{\xi} \left[ \frac{d^2\theta}{d\xi'^2} - 12(\xi' - \xi'^2) \right] \overline{A}_i'(I) d\xi' - \int_{\xi}^1 \left[ \frac{d^2\theta}{d\xi'^2} - 12(\xi' - \xi'^2) \right] \overline{A}_i'(II) d\xi' \right\} \quad (5.15)$$

The numerical solution of Eq. (5.15) is obtained by the same way as discussed in the previous section. Thus,  $\theta_{bp}$  is given by Eq. (5.11). Note that the constants  $a_1$  and  $a_2$  in this case are different. The entire procedure of evaluating the constants  $a_1$  and  $a_2$  is described in Appendix C.





# **Chapter 6**

## **RESULTS AND DISCUSSION**

Extensive results were obtained after solving the equations described in earlier chapters. The results are presented in terms of bulk temperature as a function of temperature, pressure, and spacing between the plates. The results were obtained for six different gases. These are CO, NO, OH, CO<sub>2</sub>, H<sub>2</sub>O, and CH<sub>4</sub>. LTE and NLTE results for these gases were compared at different temperature and pressure conditions. The results obtained for both gray and non-gray analyses are presented in the following sections.

### **6.1 Gray Results**

In this section, results are presented for the six gases under consideration under gray gas assumption. Both LTE and NLTE results have been obtained for all the gases considered. The results are compared at pressures ranging from 0.1 to 10 atm. and at temperatures ranging from 300 K to 2000 K. The spacing between the plates is varied from 0.1 to 100 centimeters.

The LTE and NLTE results for CO are presented in Fig. 6.1. In Fig. 6.1(a), pressure is kept constant at one atmosphere and LTE results are compared at four different temperatures



(300 K, 500 K, 1000 K, and 2000 K). The results show that as one goes from higher temperature to lower temperature, the bulk temperature decreases for any particular plate spacing. At any given temperature, the bulk temperature is seen to vary significantly in the intermediate range of plate spacings. A lower value of bulk temperature means higher capacity of the gas to exchange radiation. For lower spacings, there is almost negligible radiative contribution. Radiative interaction increases with increasing plate spacing. Figure 6.1(b) illustrates the results at a fixed temperature of 500 K and for  $P = 0.1, 1, \text{ and } 10 \text{ atm}$ . The variation between the results at different pressures show that as we decrease the pressure, the radiative heat transfer effect decreases. Thus Figs. 6.1(a) and 6.1(b) show that under LTE assumption, the radiative heat exchange capacity of CO is higher at higher temperatures and pressures.

In Figs. 6.1(c) and 6.1(d), LTE and NLTE results are compared for CO. In Fig. 6.1(c), pressure is kept constant at one atmosphere and temperature is varied from 300 to 2000 K. The results show that the variation between LTE and NLTE results is maximum at lower temperatures. The LTE and NLTE results show maximum differences at moderate pressures (Fig. 6.1(d)). This implies that NLTE effect is pronounced at lower temperatures and moderate pressures. Thus NLTE effect must be considered when the temperature and pressures are relatively low. It should be noted that the effect of NLTE is to lower the ability of the gas for radiative interaction.

Figures 6.2 present results for NO. In Figs. 6.2(a) and 6.2(b), LTE results are compared at different temperatures and pressures, and in Figs. 6.2(c) and 6.2(d), LTE and NLTE results are compared at different temperatures and pressures. The result shows the same behavior as in the case of CO. In a similar manner, Figs. 6.3 show the results for OH. There appears to be no NLTE effect for OH. Figure 6.4 is a comparison of LTE and NLTE results for CO, NO, and OH at a temperature of 500 K and one atmospheric pressure. The results show that

OH has the lowest radiative ability while CO shows the highest radiative ability at the particular temperature and pressure considered. Further, The variation between the LTE and NLTE is maximum for CO and minimum for OH. This implies that CO has a higher tendency to show radiative effect as well as it is more sensitive to nonequilibrium phenomena.

The LTE and NLTE results for polyatomic gases are presented in Figs. 6.5 through 6.8. Figure 6.5 presents results for CO<sub>2</sub>. The LTE results are compared for temperatures ranging from 300 K to 2000 K and one atmospheric pressure. The results illustrate that bulk temperature decreases with increasing temperature. In Fig. 5(b), LTE results are shown at different pressures between 0.1 and 10 atm. and at a temperature of 500 K. It is seen that bulk temperature decreases, in general, with increasing pressure. At higher pressures, bulk temperature decreases smoothly for low plate spacings, but at higher plate spacings, it becomes uniform. The reasons for this behavior of CO<sub>2</sub> are given in [ 31, 32 ]. Figure 6.5(c) is a comparison of LTE and NLTE results at various temperatures and 1 atmospheric pressure. It is seen that there is almost no difference between LTE and NLTE results at any temperature. In Fig. 6.5(d), LTE and NLTE results are compared at various pressures and a temperature of 500 K. At a pressure of 0.1 atm, there are some differences between LTE and NLTE results. The differences are negligible at higher pressures.

The results for H<sub>2</sub>O are presented in Figs. 6.6. The trend of the results are more or less the same as observed in the case of CO<sub>2</sub>. The LTE results are compared at different temperatures and one atmospheric pressure in Fig. 6.6(a). The results show that bulk temperature decreases with increasing temperature which implies higher capacity for radiative exchange. Figure 6.6(b) illustrates results at different pressures and 500 K temperature. In general, the bulk temperature is seen to decrease with pressure. It becomes uniform at higher pressures and at higher plate spacings. However, bulk temperature becomes uniform at higher plate

spacings compared to CO<sub>2</sub>. Figures 6.6(c) and 6.6(d) show a comparison of LTE and NLTE results at different temperatures and pressures. There is almost no variation between LTE and NLTE results except at 500 K and 0.1 atm. The variation is more than that observed for CO<sub>2</sub>.

The results for CH<sub>4</sub> are presented in Figs. 6.7. In Figs. 6.7(a) and 6.7(b), LTE results are presented at different pressures and temperatures. The trend of results is similar to that exhibited by CO<sub>2</sub> and H<sub>2</sub>O. Figures 6.7(c) and 6.7(d) show comparison of LTE and NLTE results at different temperatures and pressures. There is absolutely no difference between LTE and NLTE results at any temperature and pressure. This implies that NLTE consideration is not important for CH<sub>4</sub>.

Figure 6.8 shows a comparison of NLTE results for all the gases under consideration at 500 K and one atmospheric pressure. It is seen that bulk temperature is highest for OH and lowest for CO<sub>2</sub>. This implies that OH is the least radiating gas whereas CO<sub>2</sub> has the highest ability for radiative exchange under the given conditions.

The overall conclusion is that the NLTE results for polyatomic gases do not show much variation from LTE results. On the other hand, the NLTE results for diatomic gases show significant variations from LTE results at lower temperatures and moderate pressures. This implies that NLTE has significant influence on diatomic gases at relatively low temperatures and pressures.

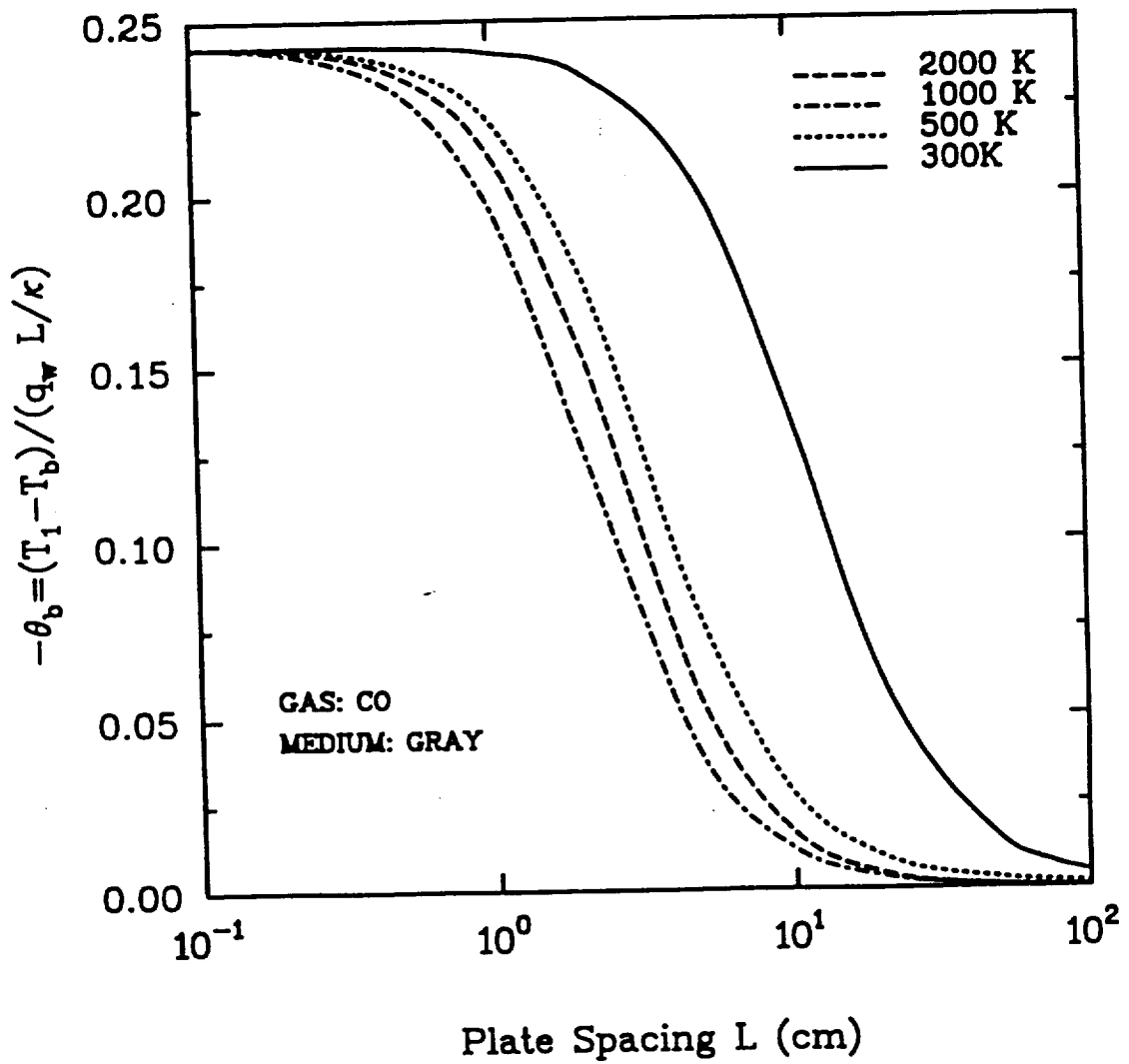


Fig. 6.1(a): LTE results for CO,  $P=1$  atm,  $T_w=300-2000$  K

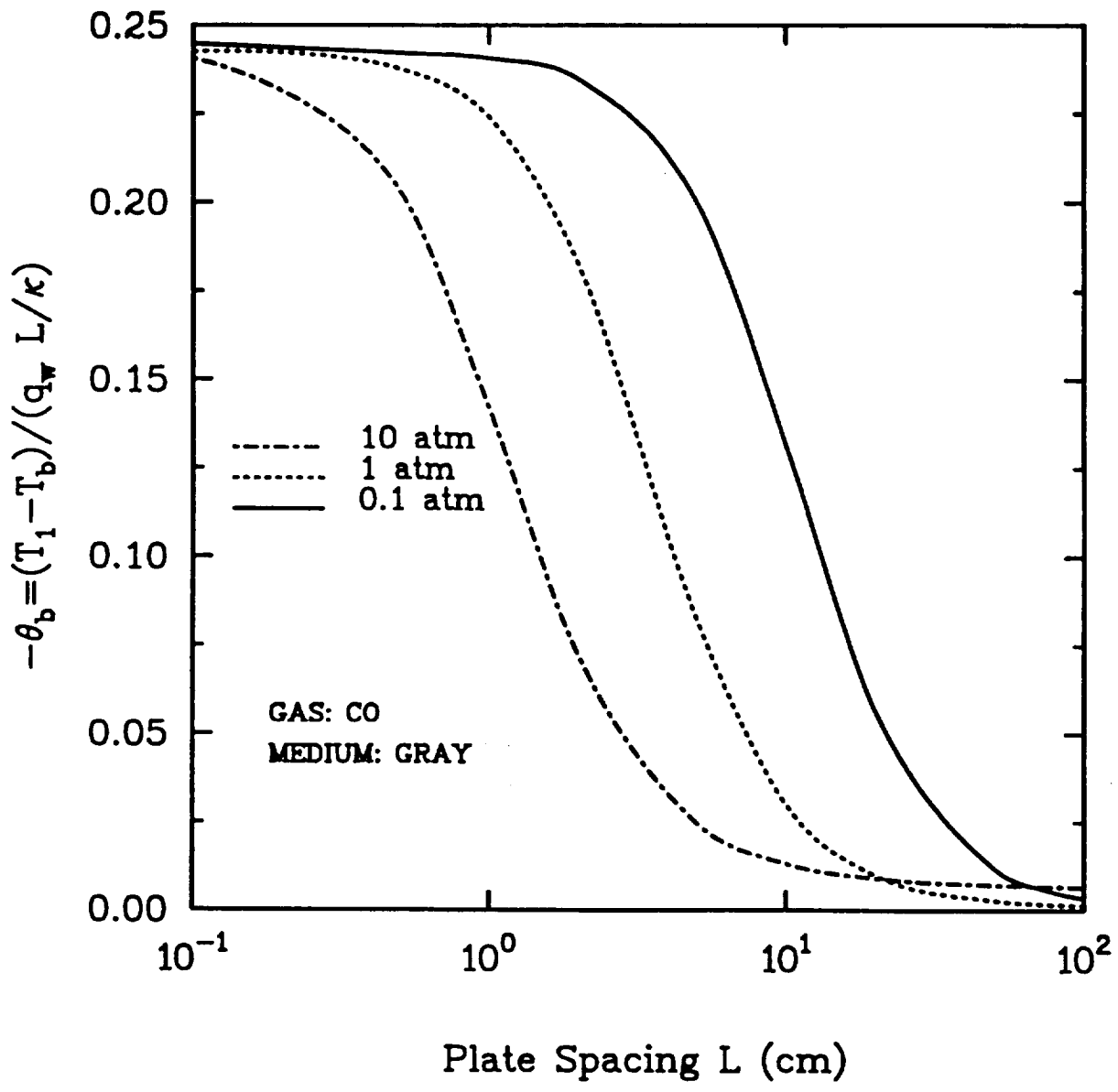


Fig. 6.1(b): LTE results for CO,  $T_w=500$  K,  $P=0.1-10$  atm

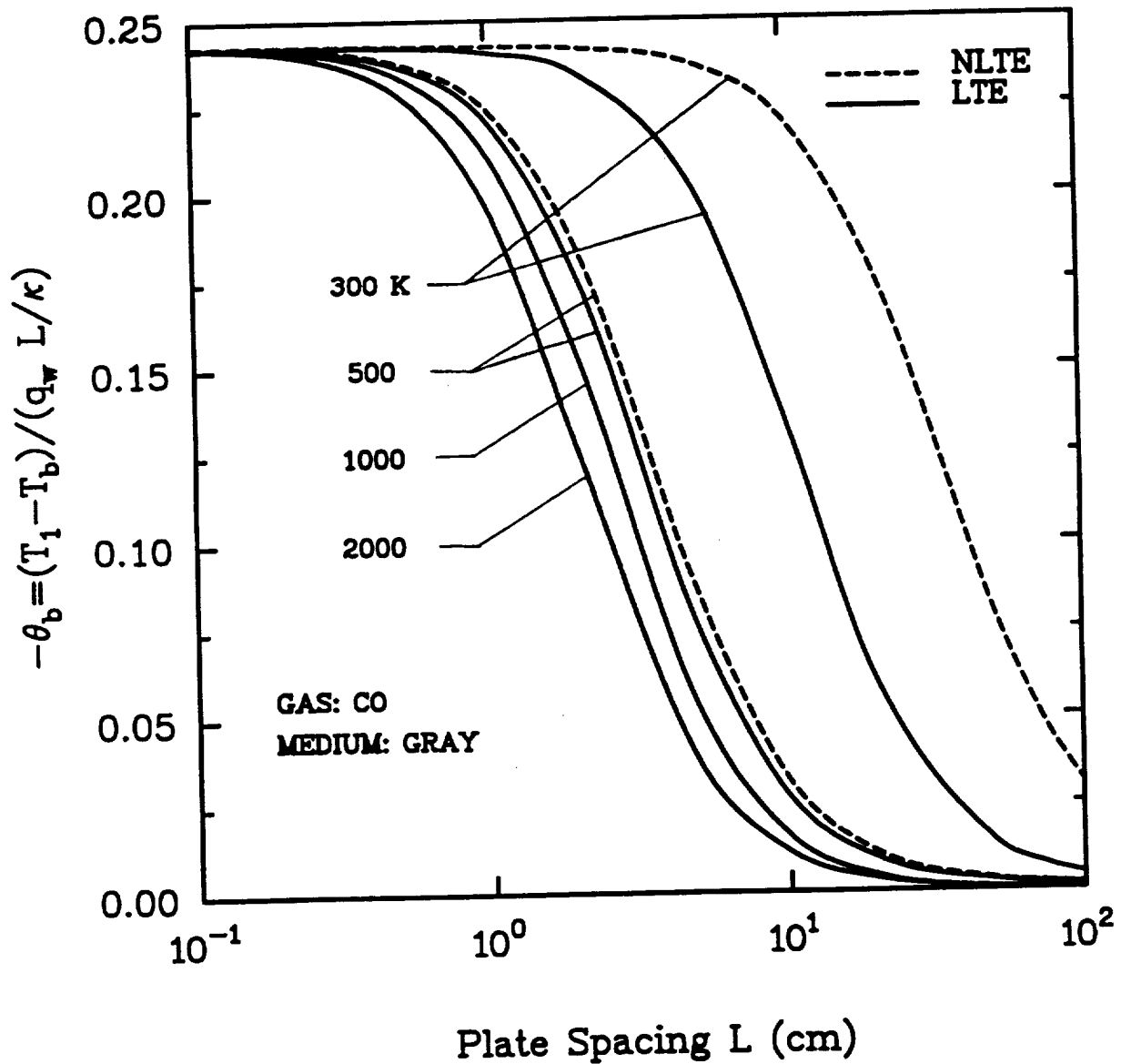


Fig. 6.1(c): LTE and NLTE results for CO,  $P=1$  atm,  $T_w=300-2000$  K



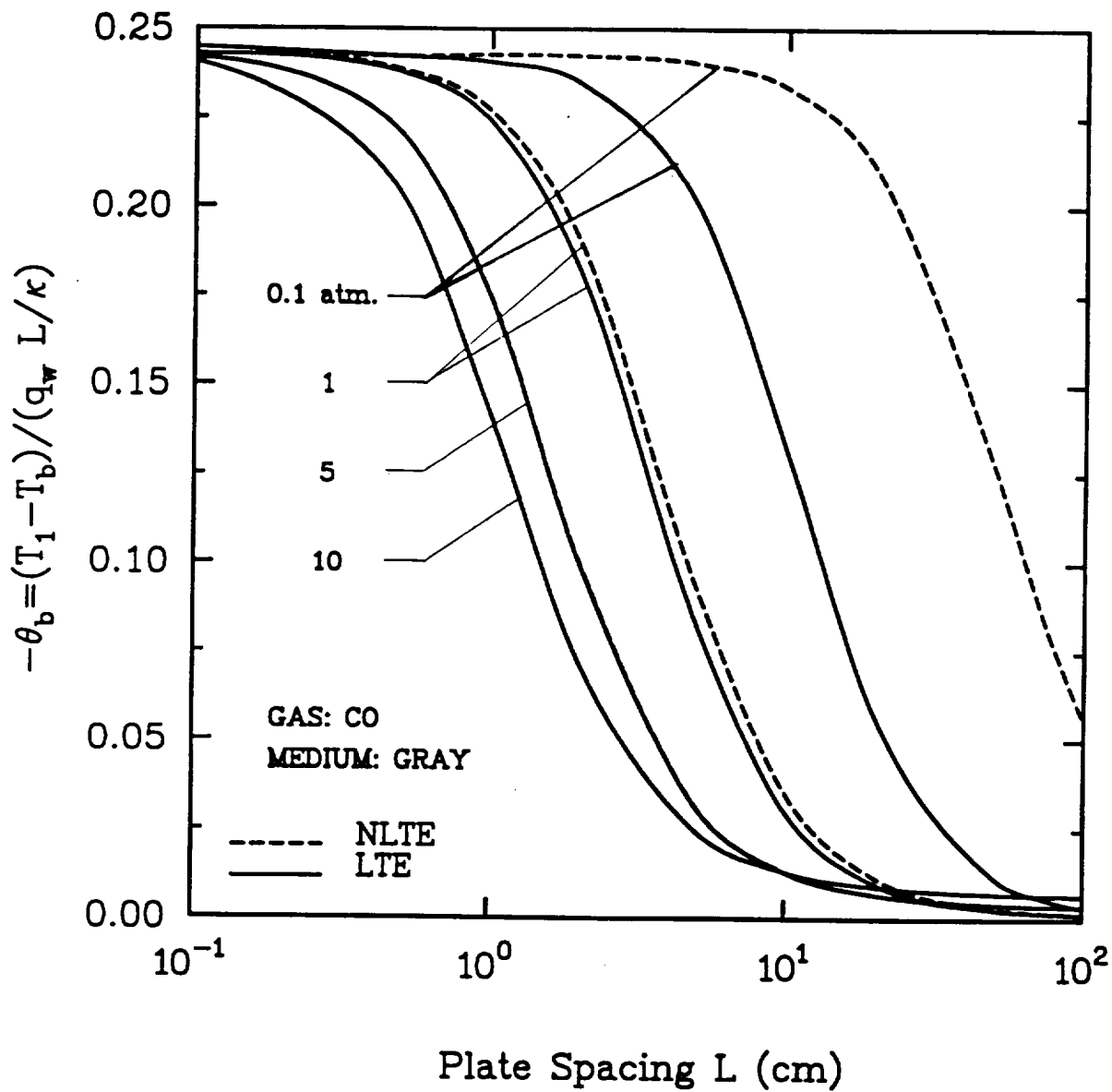


Fig. 6.1(d): LTE and NLTE results for CO,  $T_w=500$  K,  $P=0.1-10$  atm

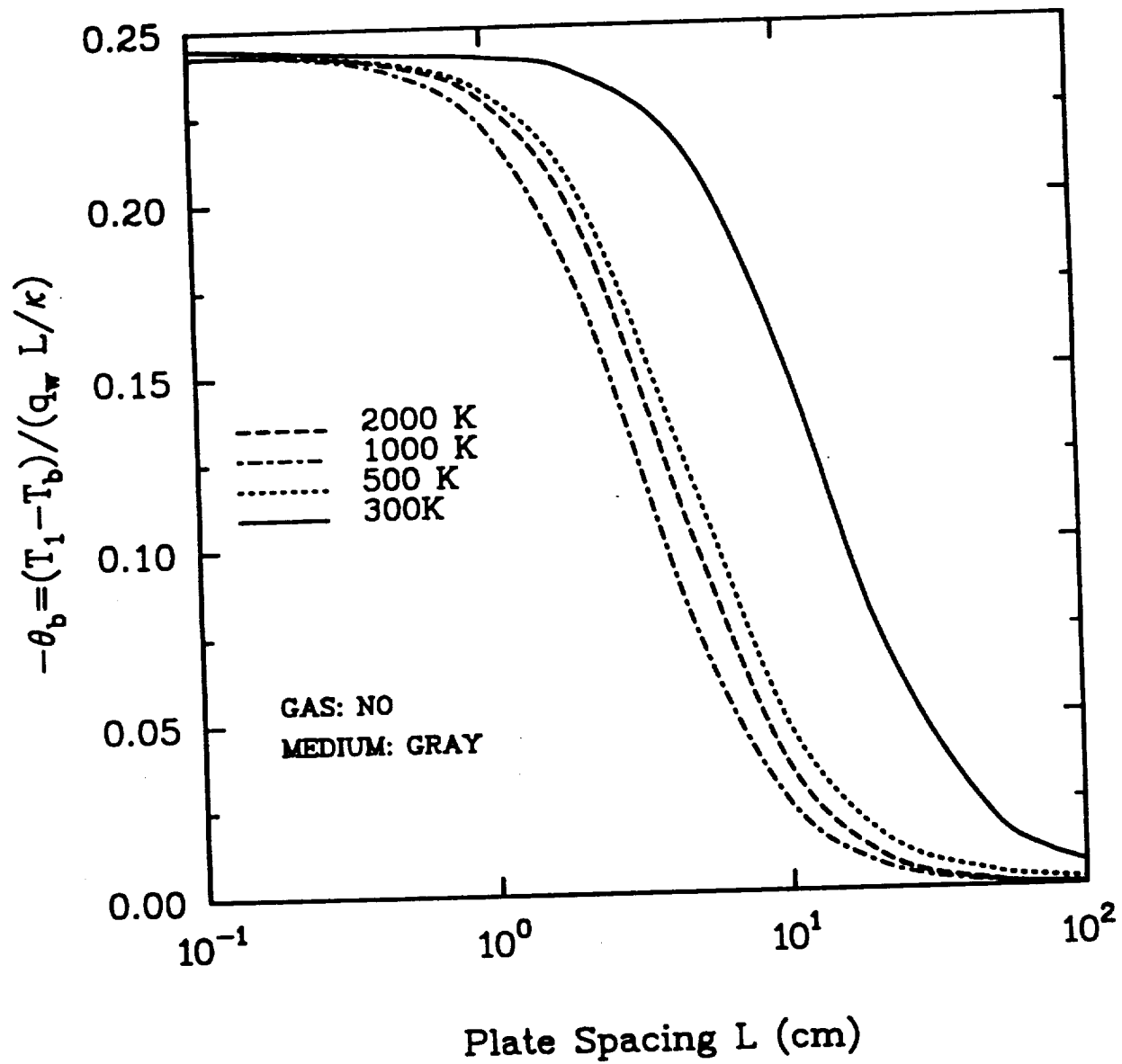


Fig. 6.2(a): LTE results for NO, P=1 atm,  $T_w=300-2000$  K

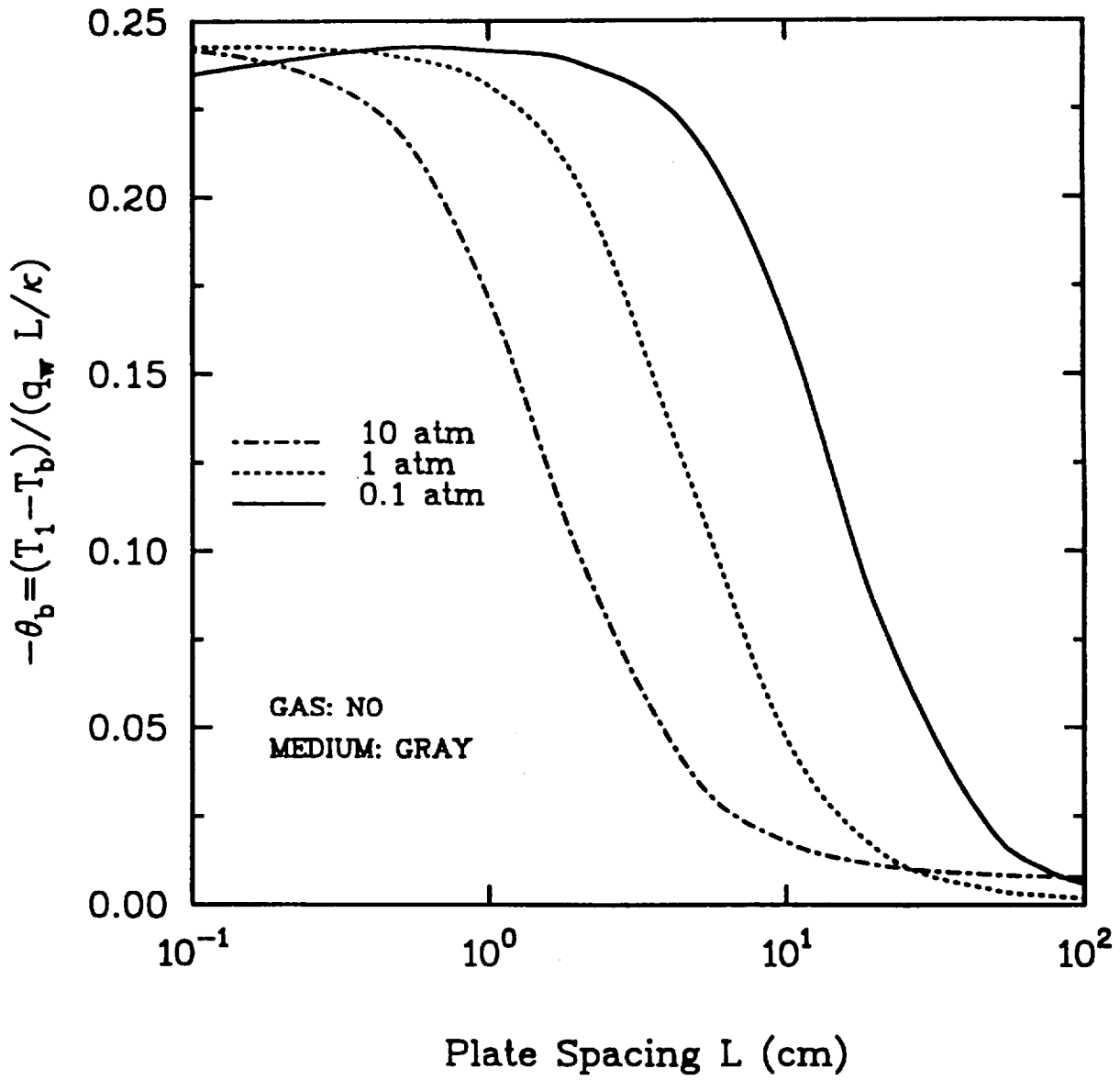


Fig. 6.2(b): LTE results for NO,  $T_w=500$  K,  $P=0.1-10$  atm

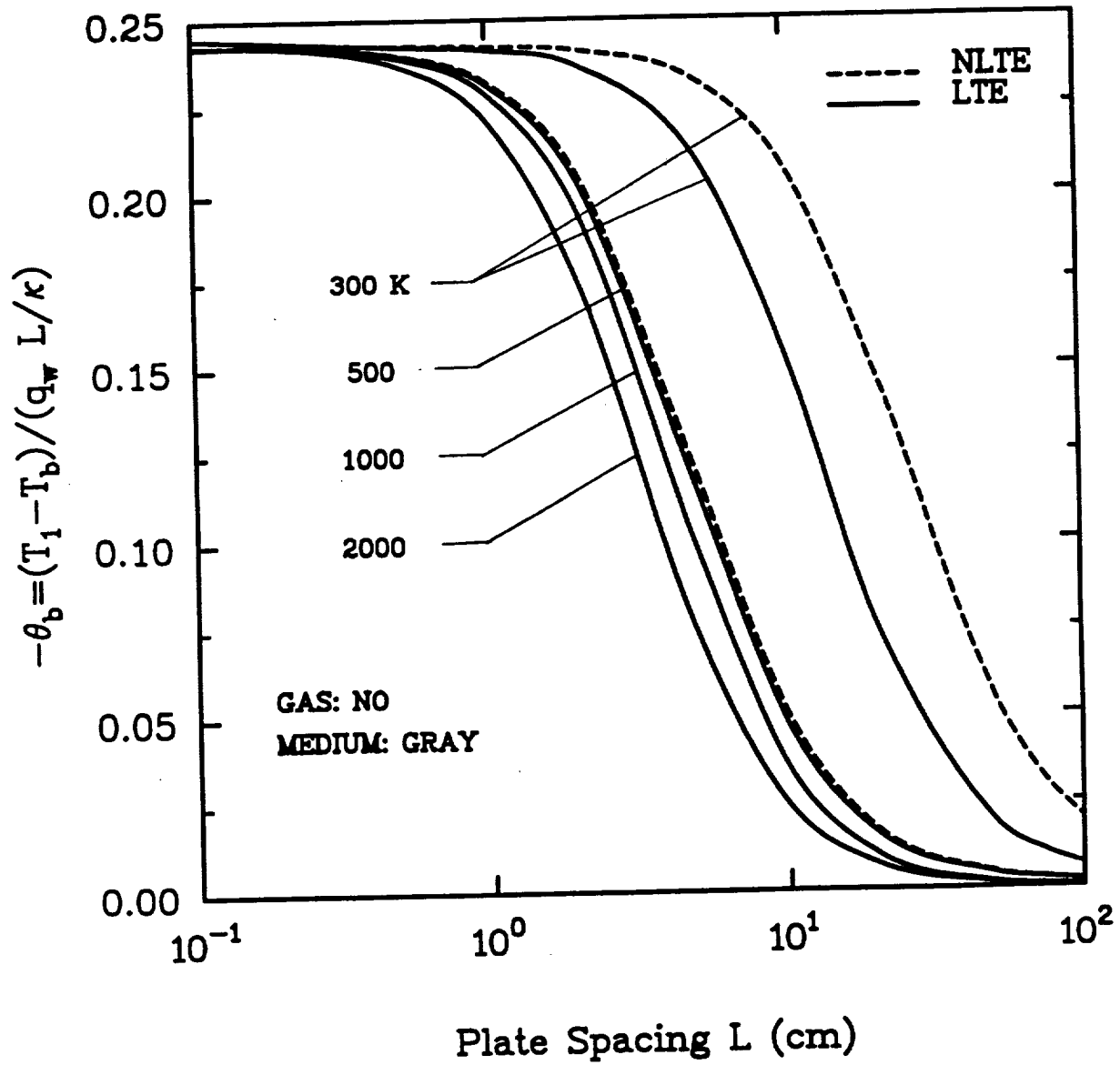


Fig. 6.2(c): LTE and NLTE results for NO,  $P=1$  atm,  $T_w=300-2000$  K

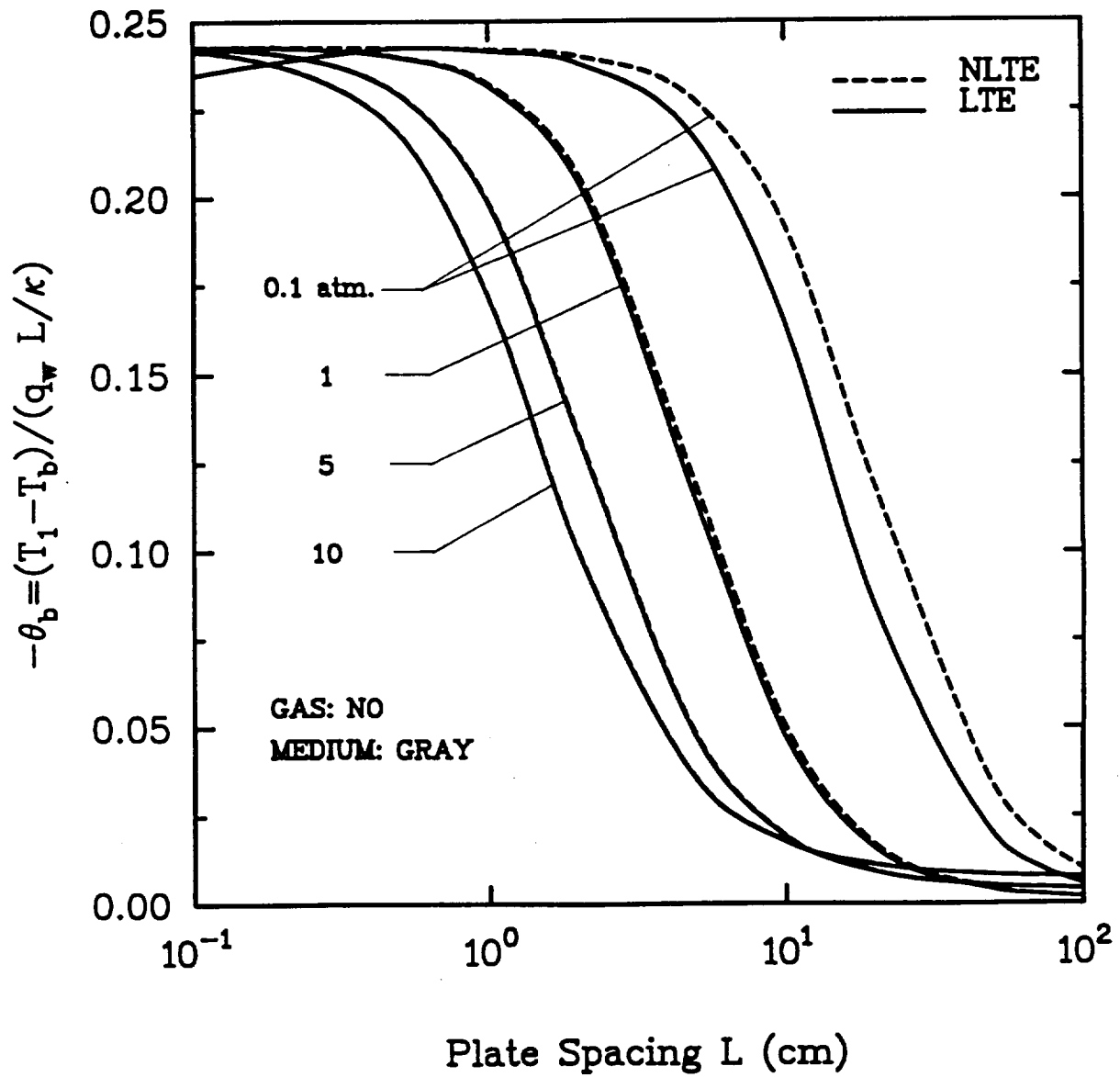


Fig. 6.2(d): LTE and NLTE results for NO,  $T_w=500$  K,  $P=0.1-10$  atm

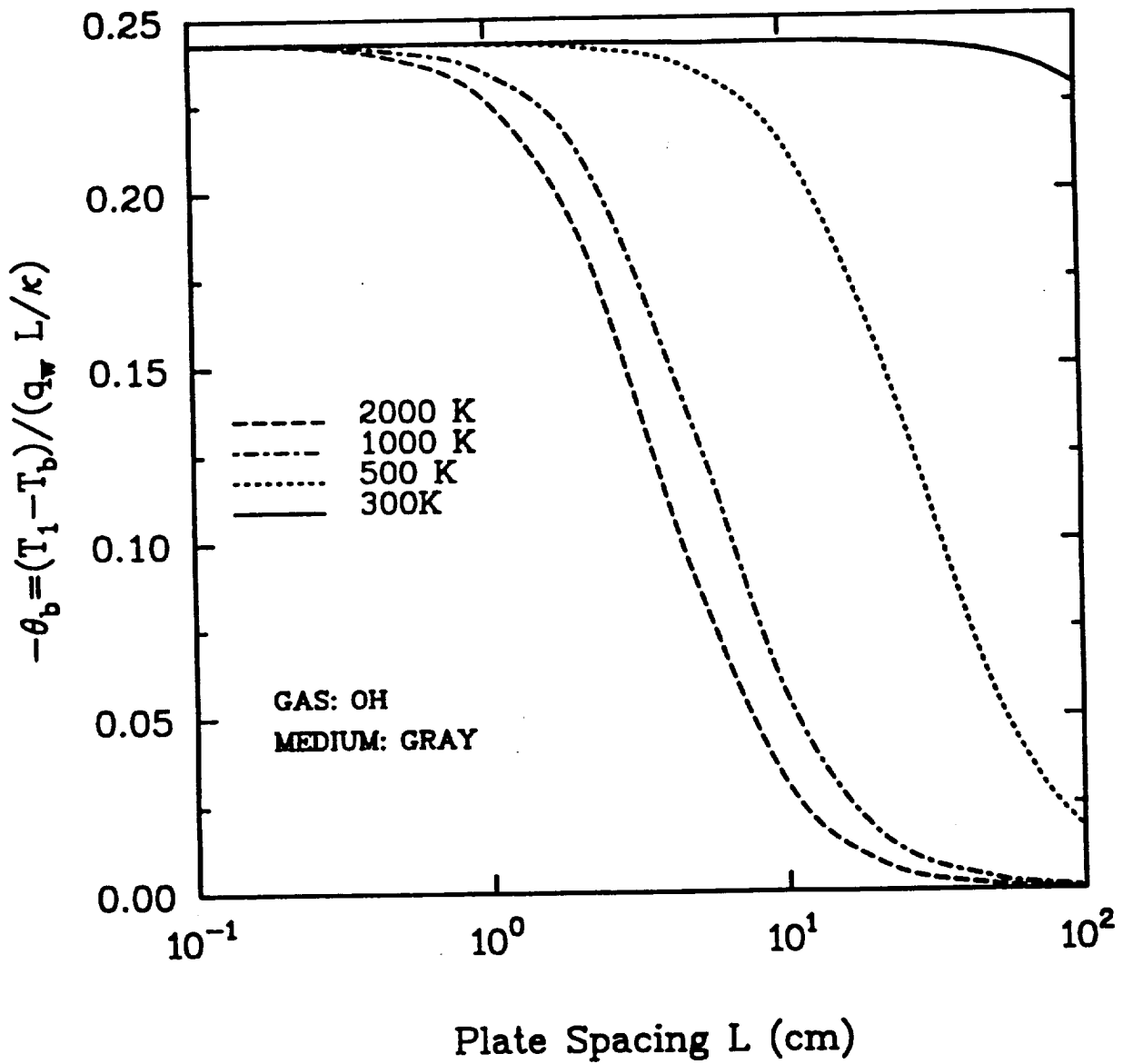


Fig. 6.3(a): LTE results for OH, P=1 atm,  $T_w=300-2000$  K

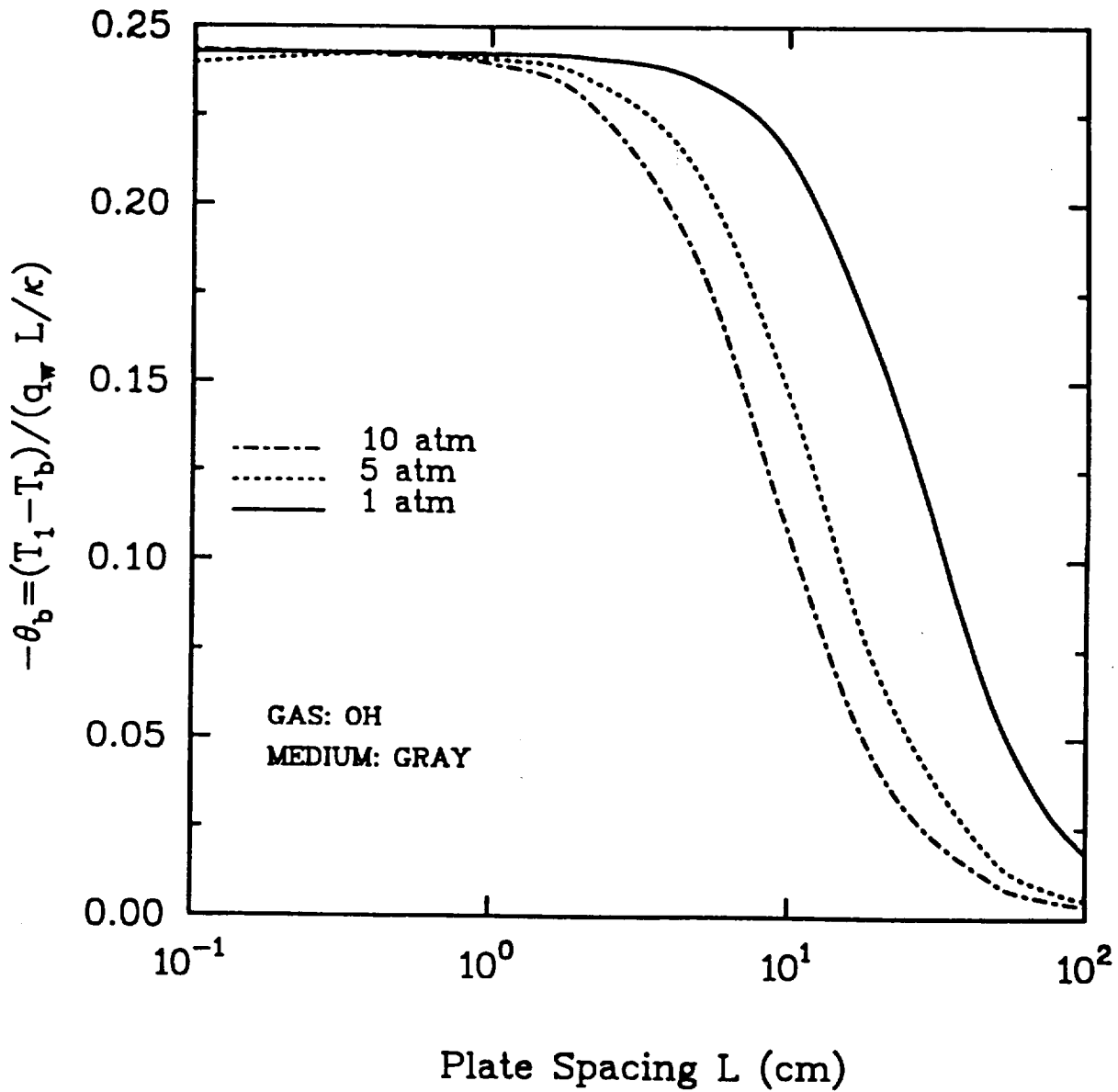


Fig. 6.3(b): LTE results for OH,  $T_w=500$  K,  $P=1-10$  atm

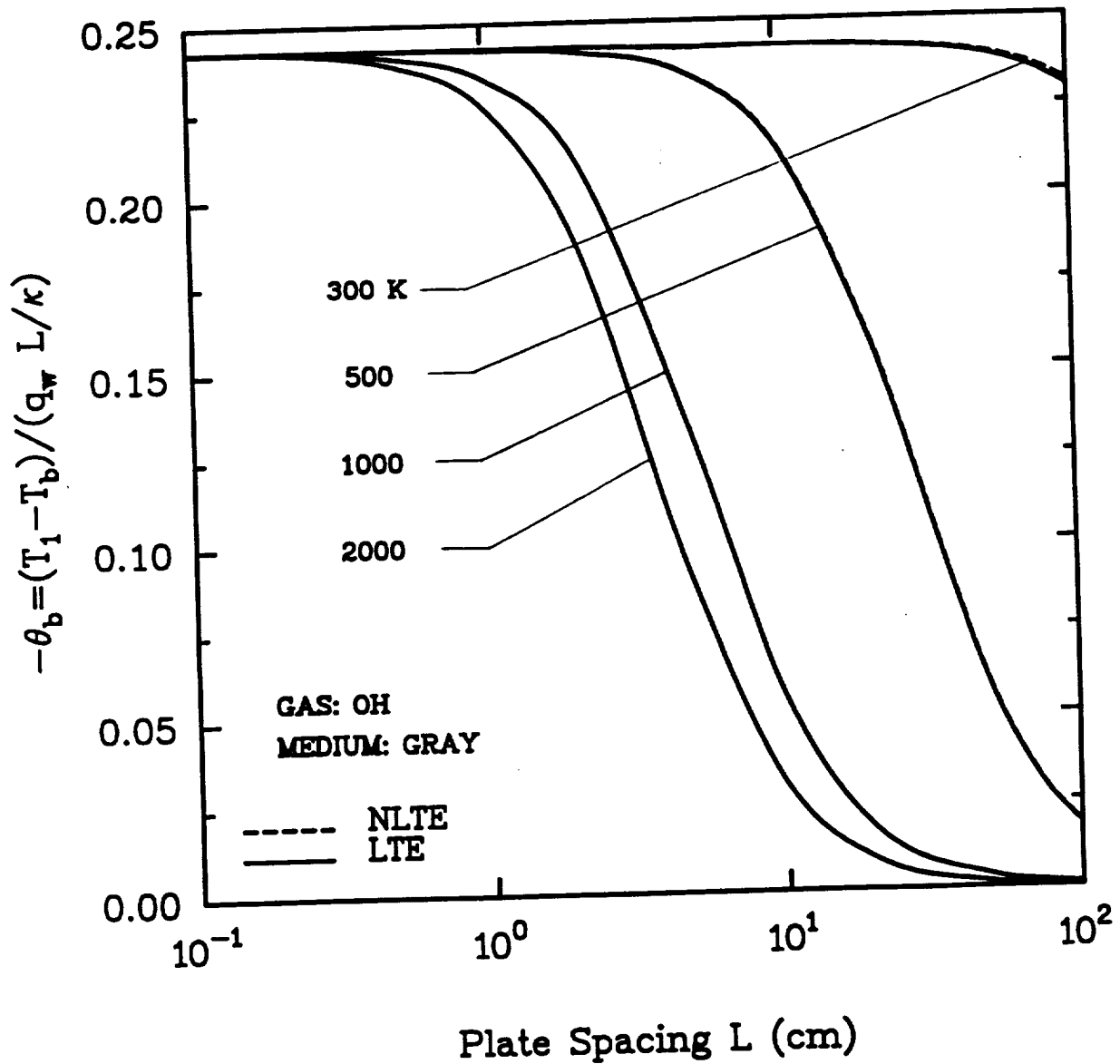


Fig. 6.3(c): LTE and NLTE results for OH,  $P=1$  atm,  $T_w=300-2000$  K



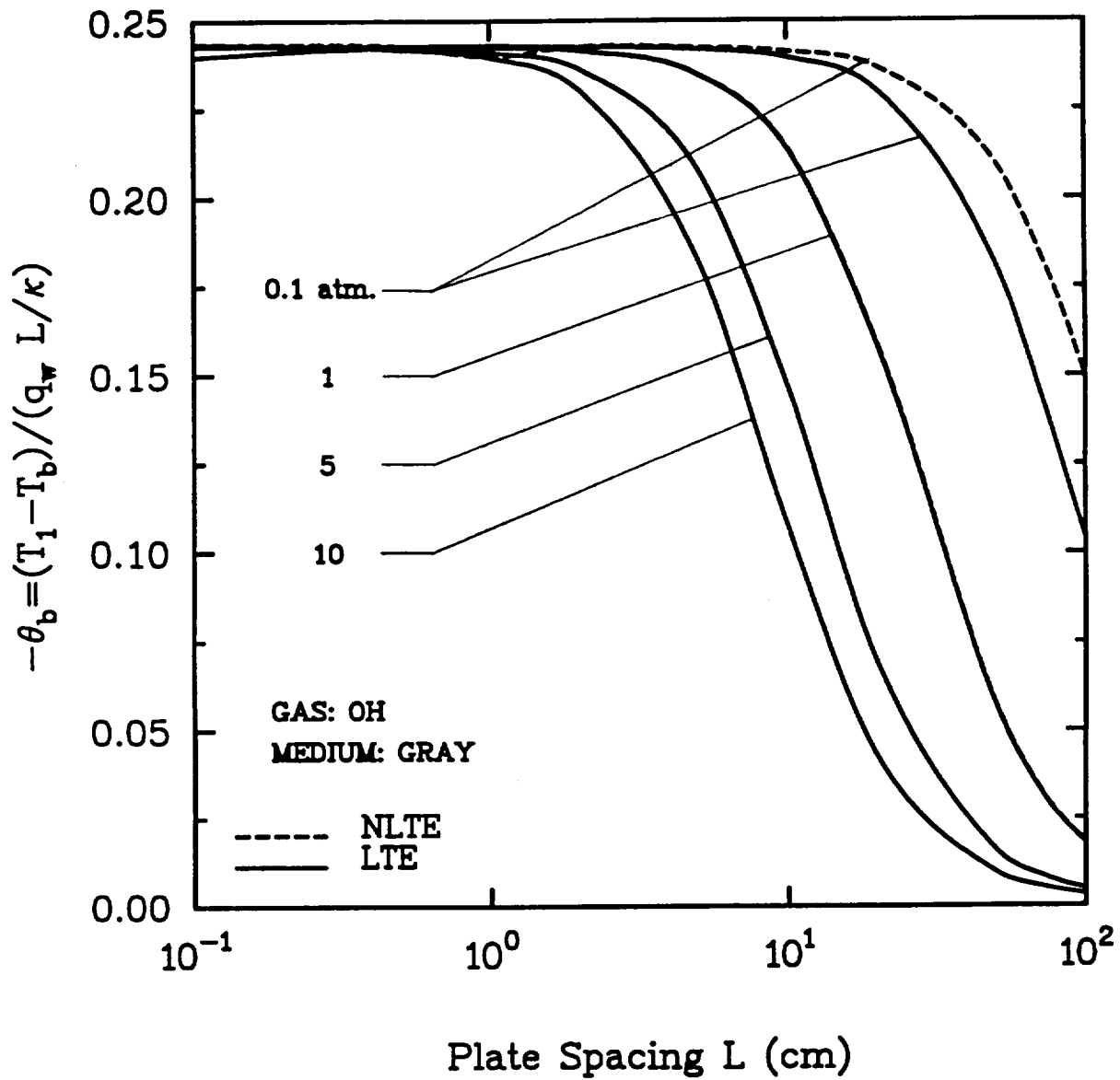


Fig. 6.3(d): LTE and NLTE results for OH,  $T_w=500$  K,  $P=0.1-10$  atm

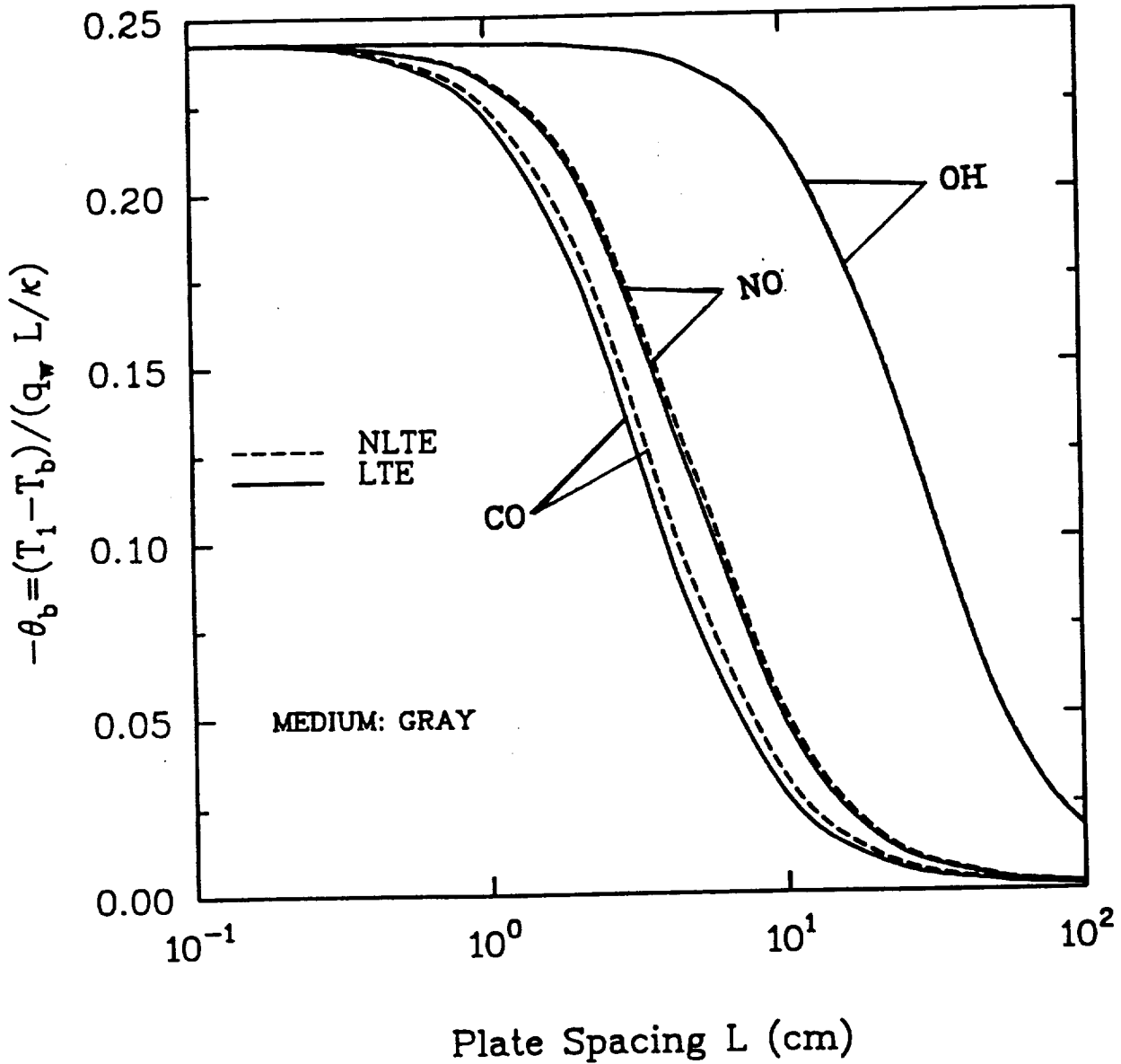


Fig. 6.4: Comparison of LTE and NLTE results for diatomic Gases at 500 K and 1 Atm.

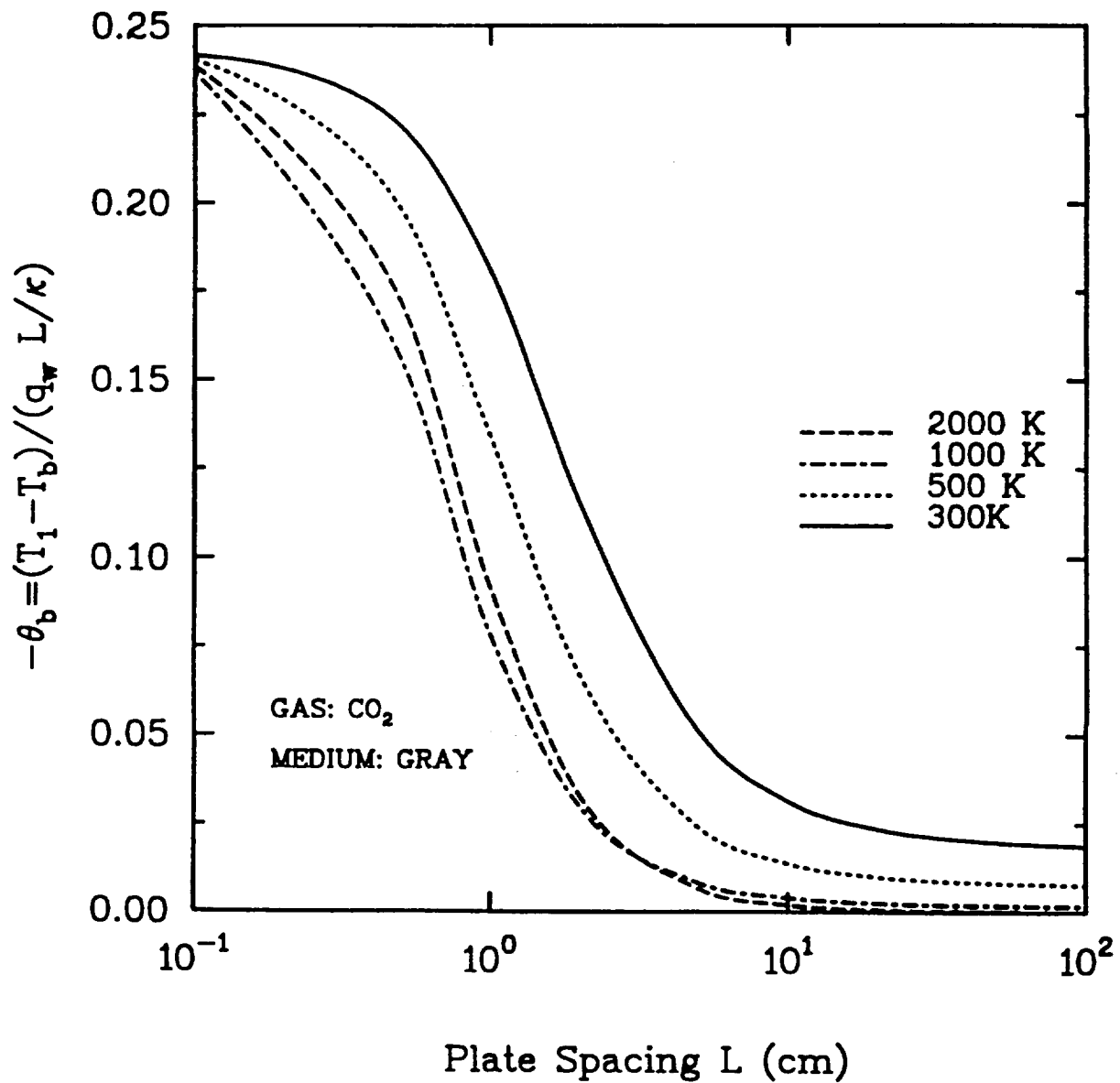


Fig. 6.5(a): LTE results for CO<sub>2</sub>, P=1 atm, T<sub>w</sub>=300–2000 K

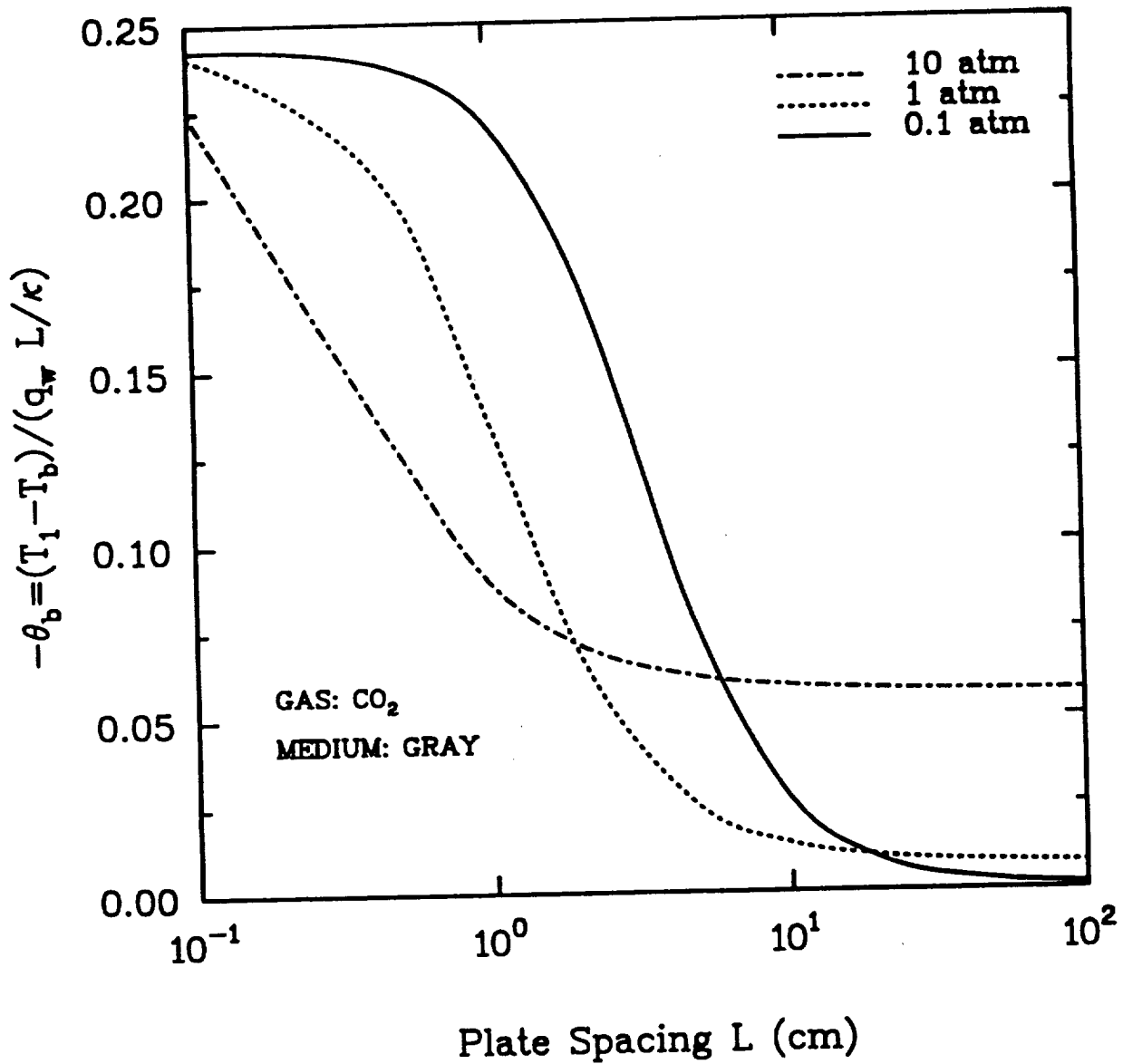


Fig. 6.5(b): LTE results for CO<sub>2</sub>, T<sub>w</sub>=500 K, P=0.1–10 atm

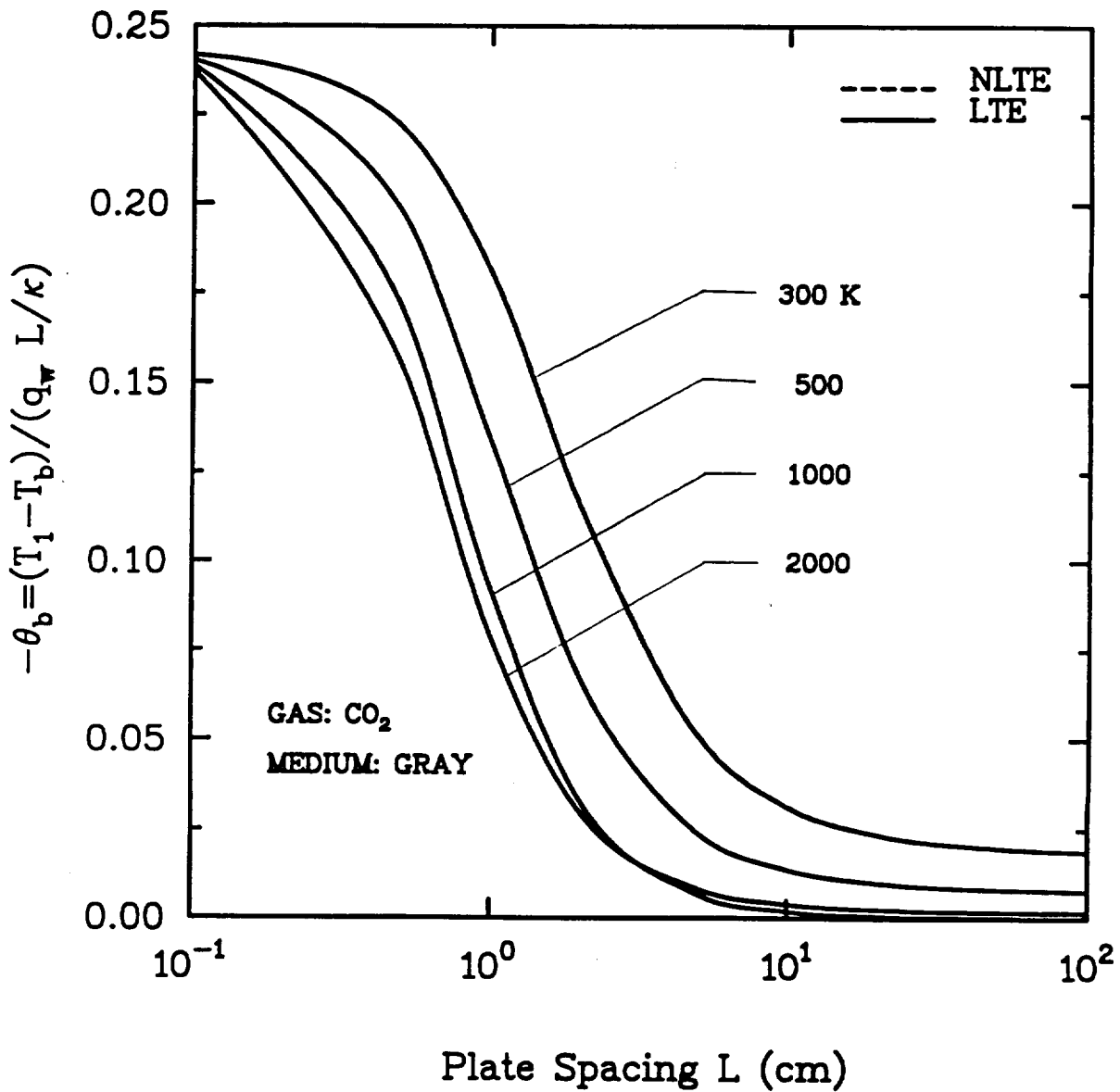


Fig. 6.5(c): LTE and NLTE results for CO<sub>2</sub>, P=1 atm, T<sub>w</sub>=300–2000 K

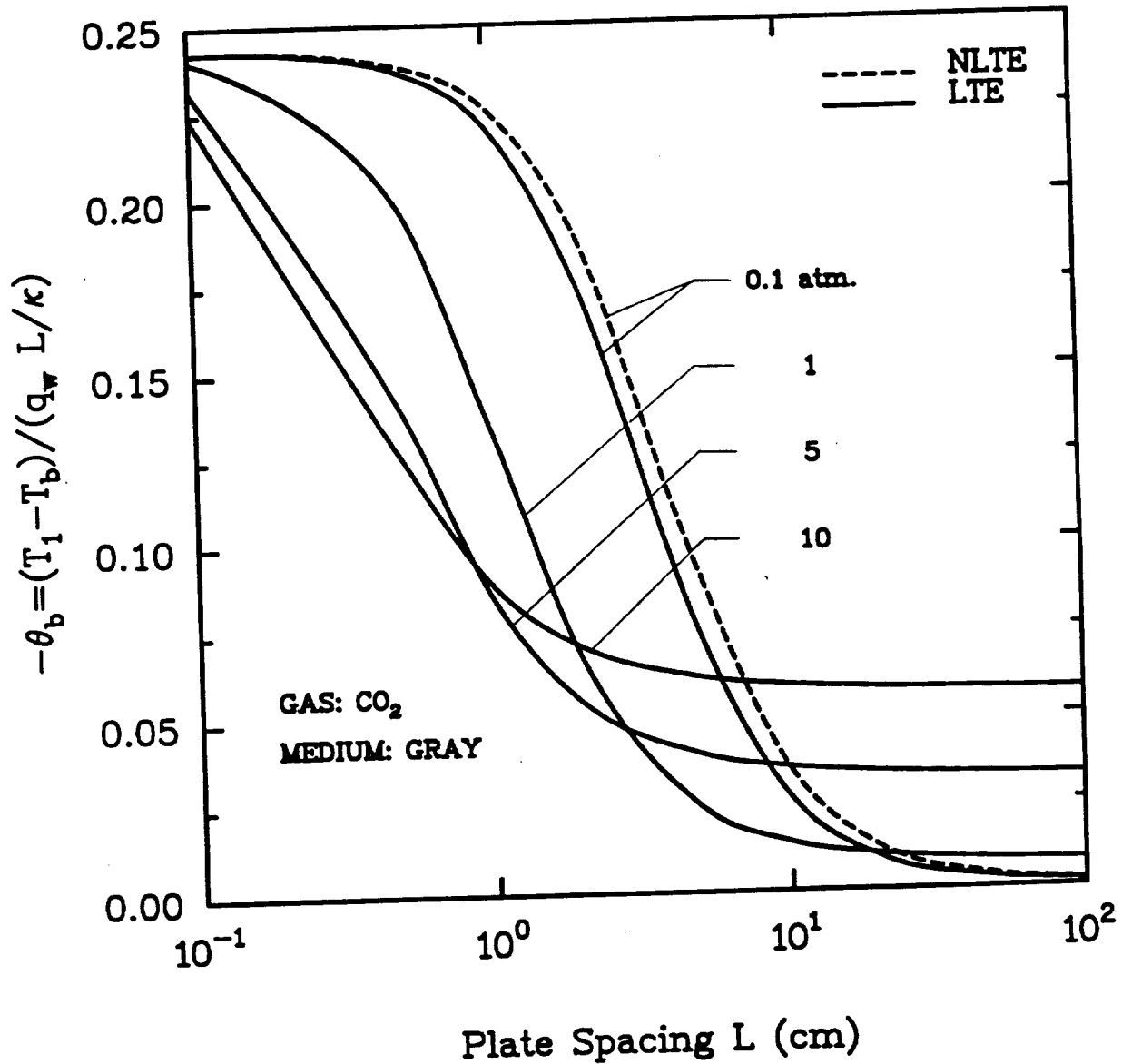


Fig. 6.5(d): LTE and NLTE results for CO<sub>2</sub>, T<sub>w</sub>=500 K, P=0.1-10 atm

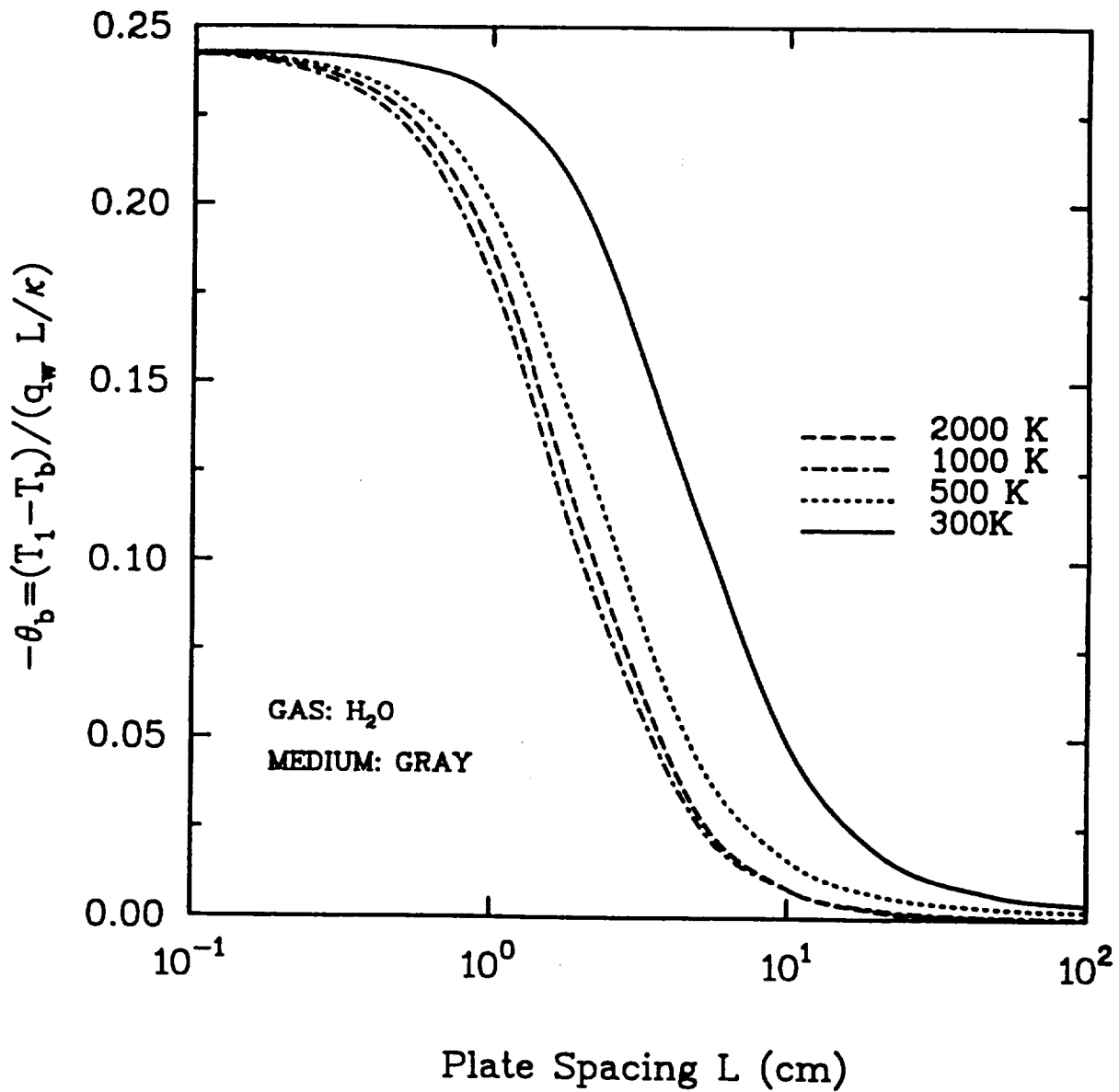


Fig. 6.6(a): LTE results for H<sub>2</sub>O, P=1 atm, T<sub>w</sub>=300–2000 K

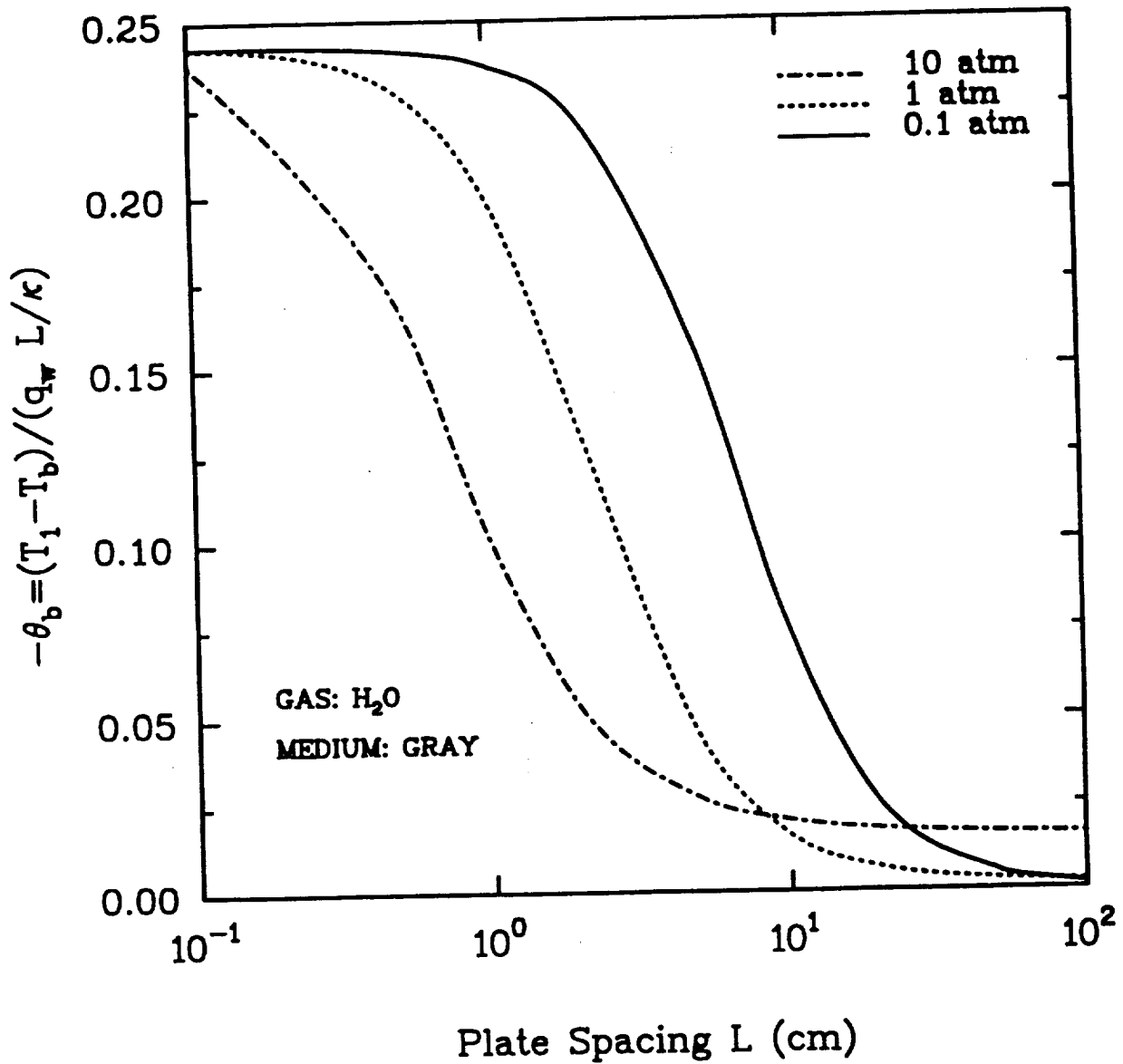


Fig. 6.6(b): LTE results for H<sub>2</sub>O, T<sub>w</sub>=500 K, P=0.1-10 atm



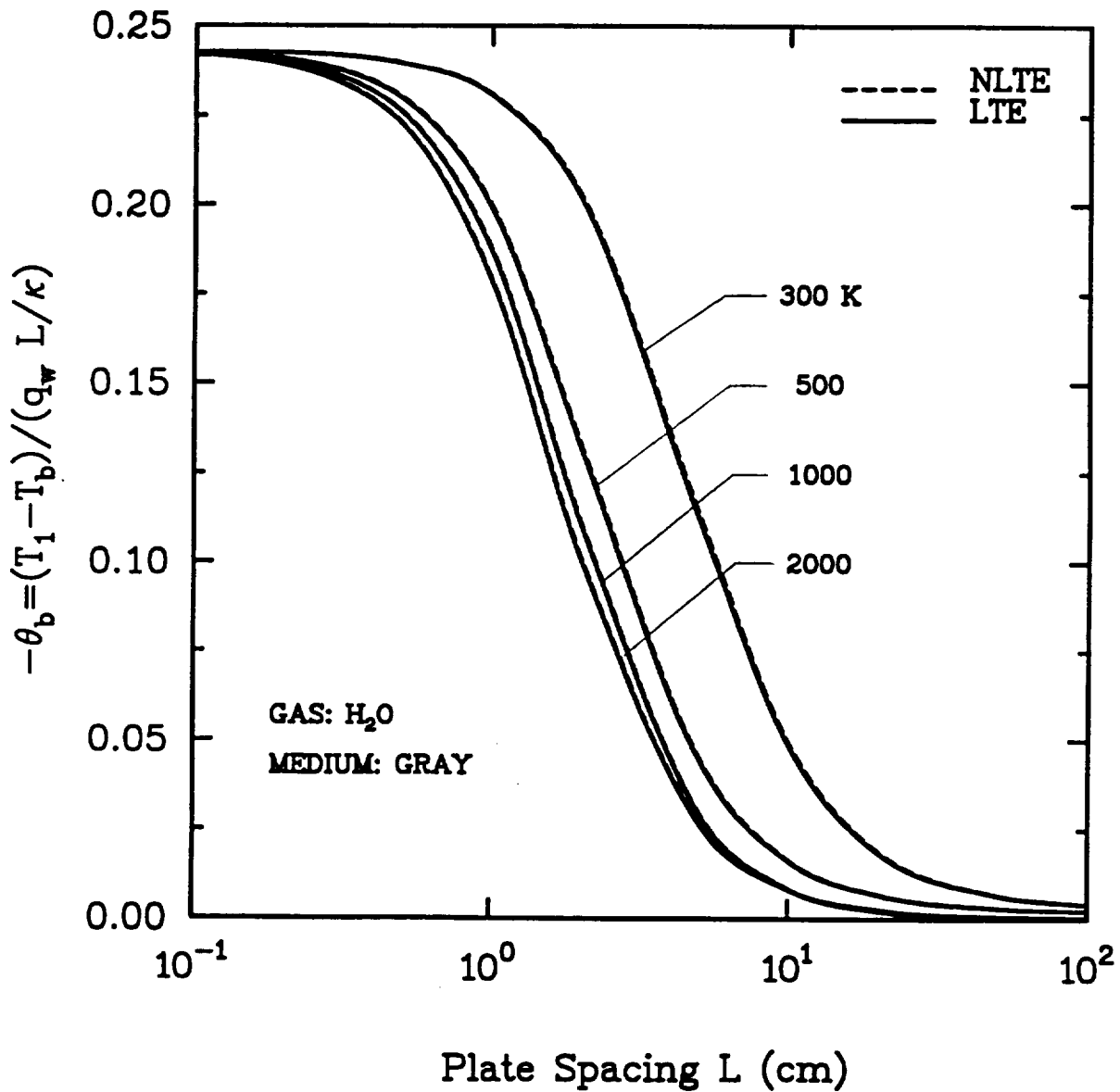


Fig. 6.6(c): LTE and NLTE results for  $H_2O$ ,  $P=1$  atm,  $T_w=300-2000$  K

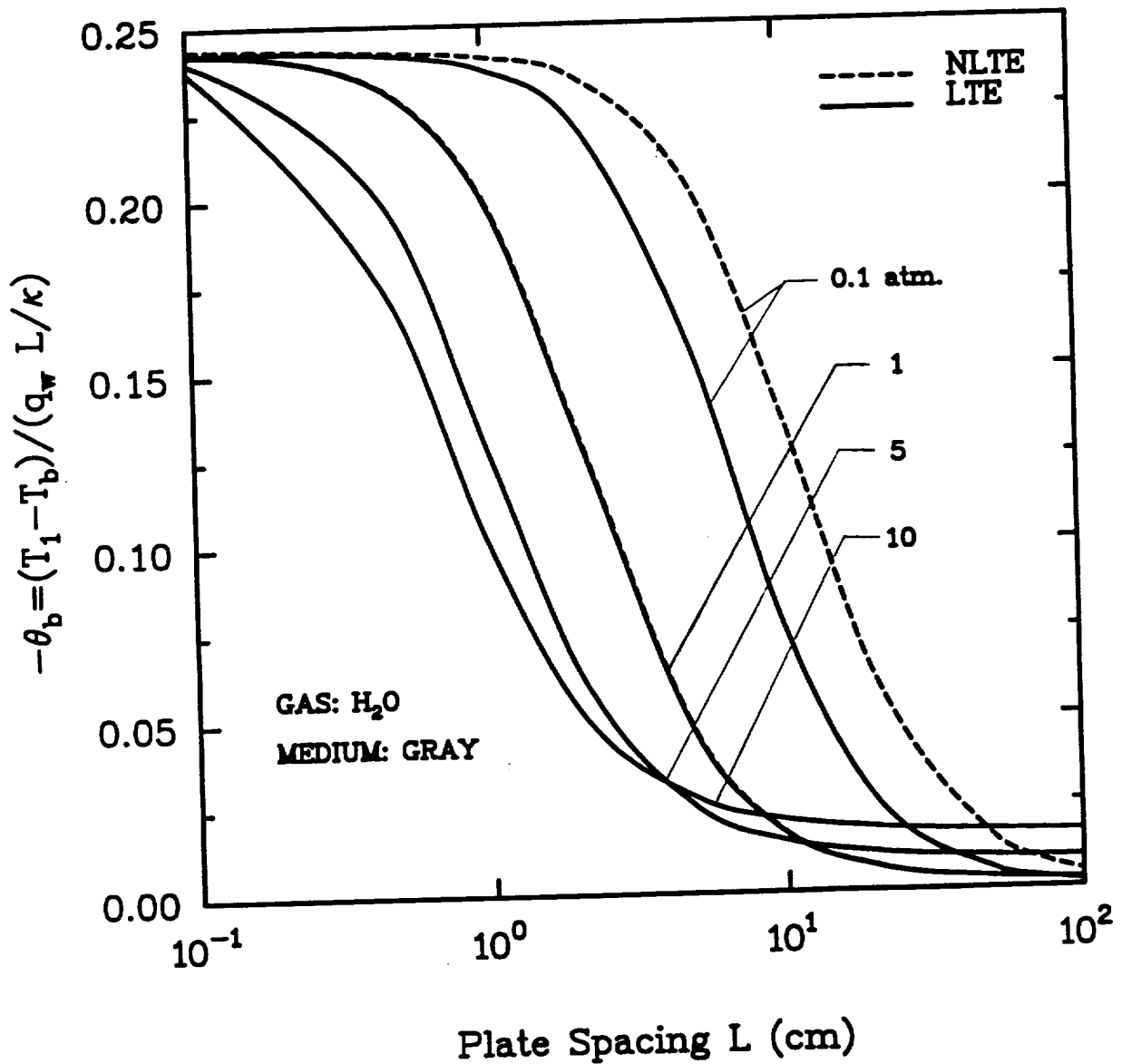


Fig. 6.6(d): LTE and NLTE results for  $H_2O$ ,  $T_w=500$  K,  $P=0.1-10$  atm

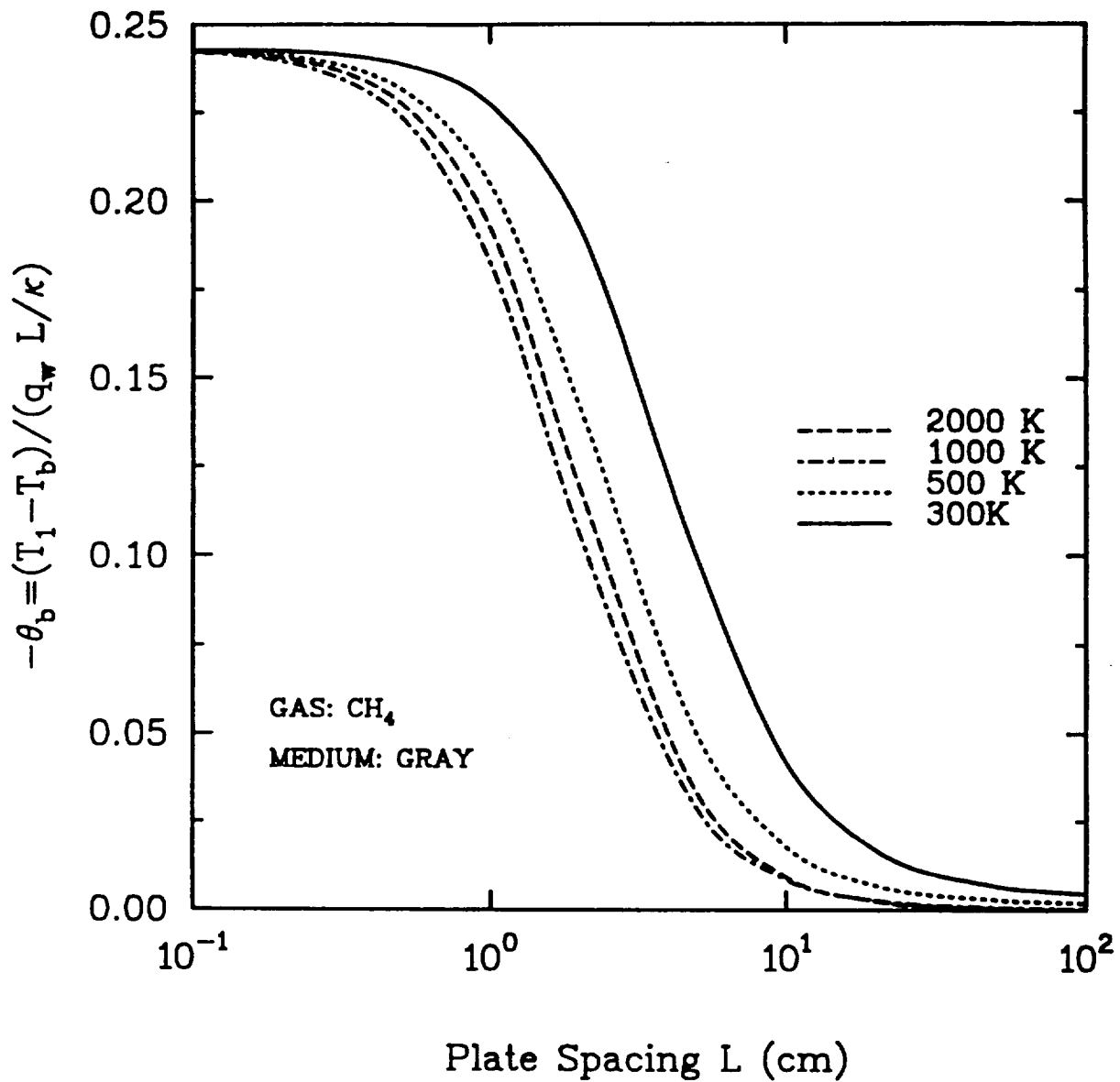


Fig. 6.7(a): LTE results for CH<sub>4</sub>, P=1 atm, T<sub>w</sub>=300–2000 K

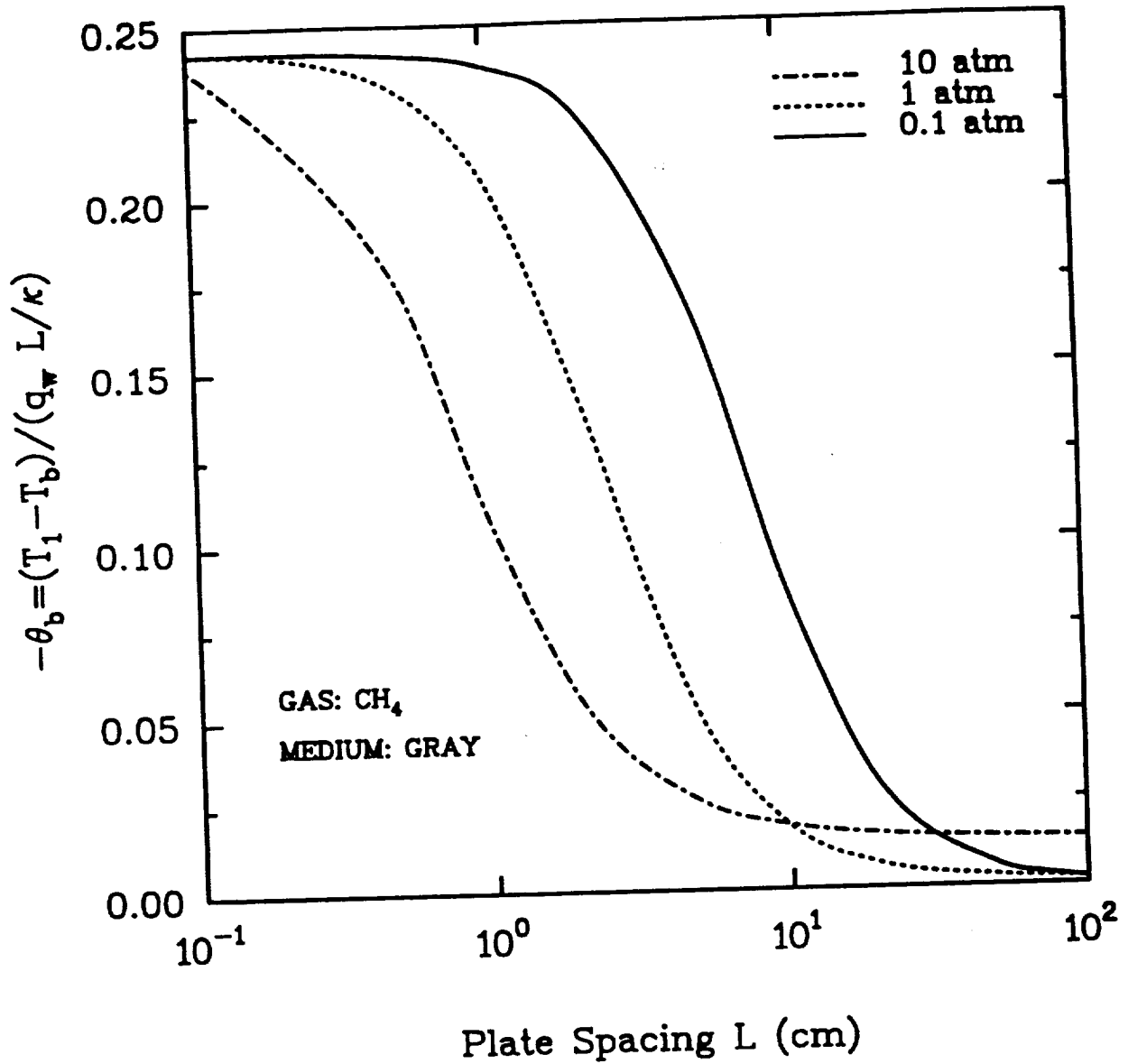


Fig. 6.7(b): LTE results for CH<sub>4</sub>, T<sub>w</sub>=500 K, P=0.1-10 atm

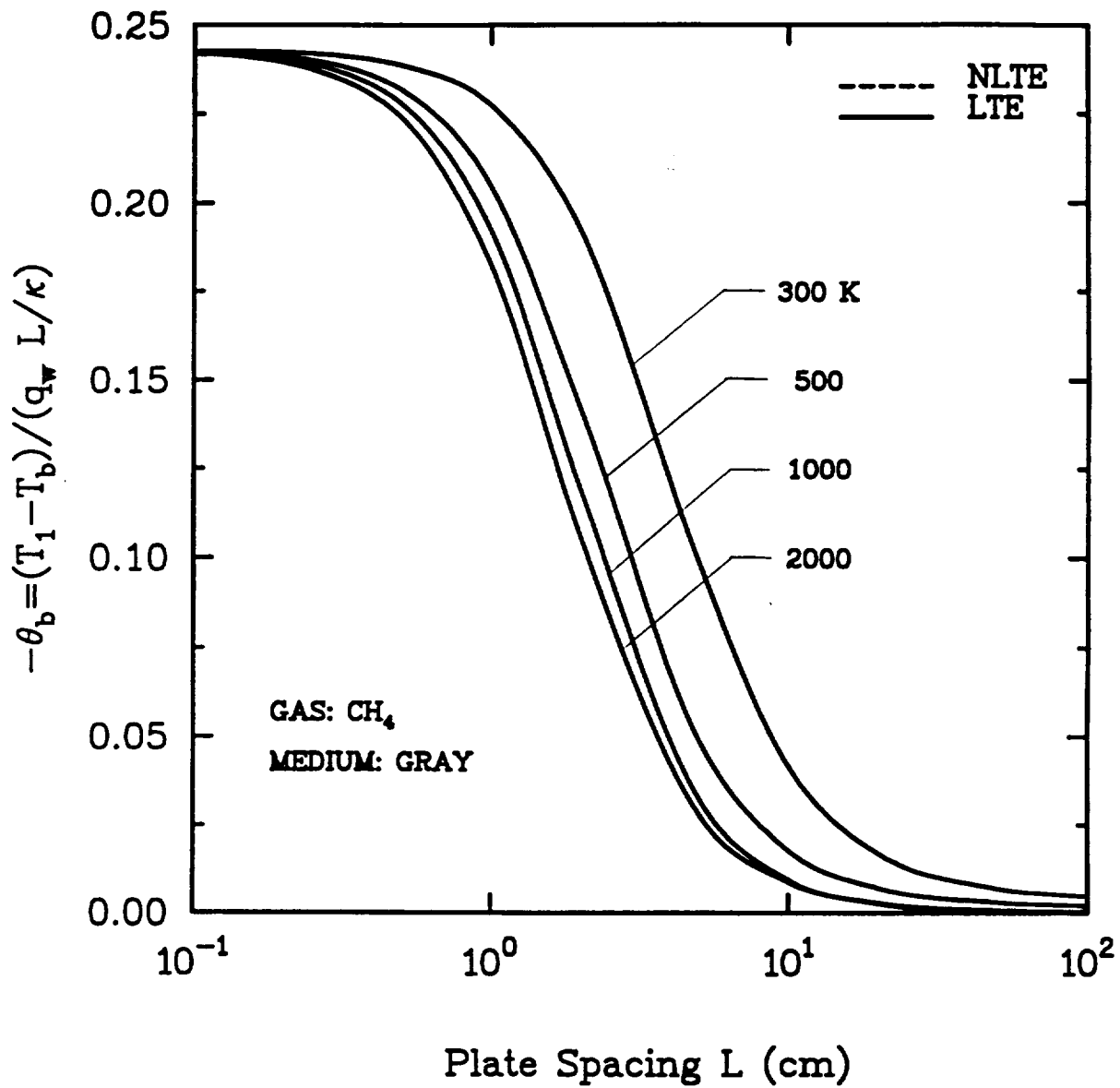


Fig. 6.7(c): LTE and NLTE results for  $\text{CH}_4$ ,  $P=1$  atm,  $T_w=300-2000$  K

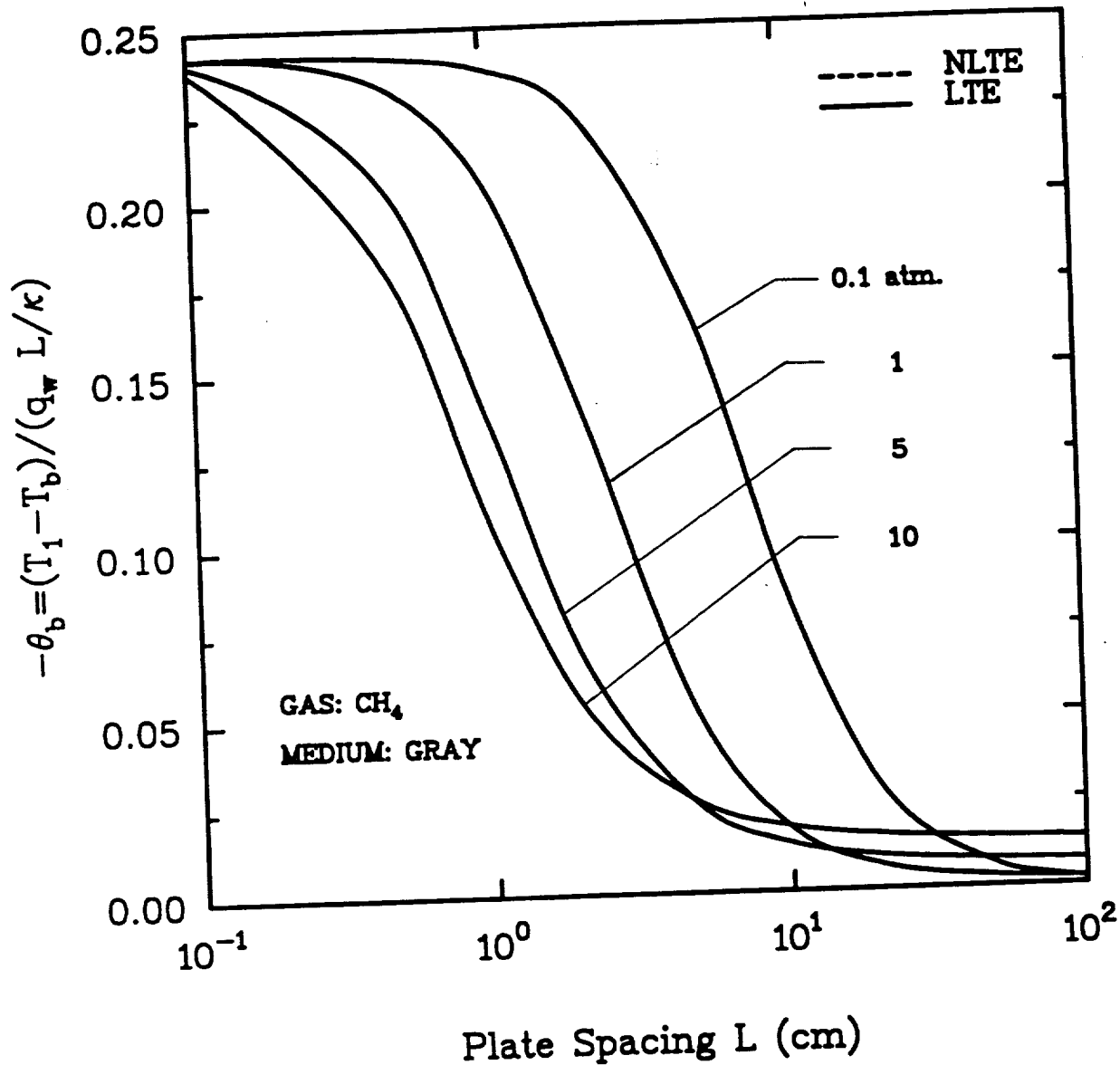


Fig. 6.7(d): LTE and NLTE results for CH<sub>4</sub>, T<sub>w</sub>=500 K, P=0.1-10 atm

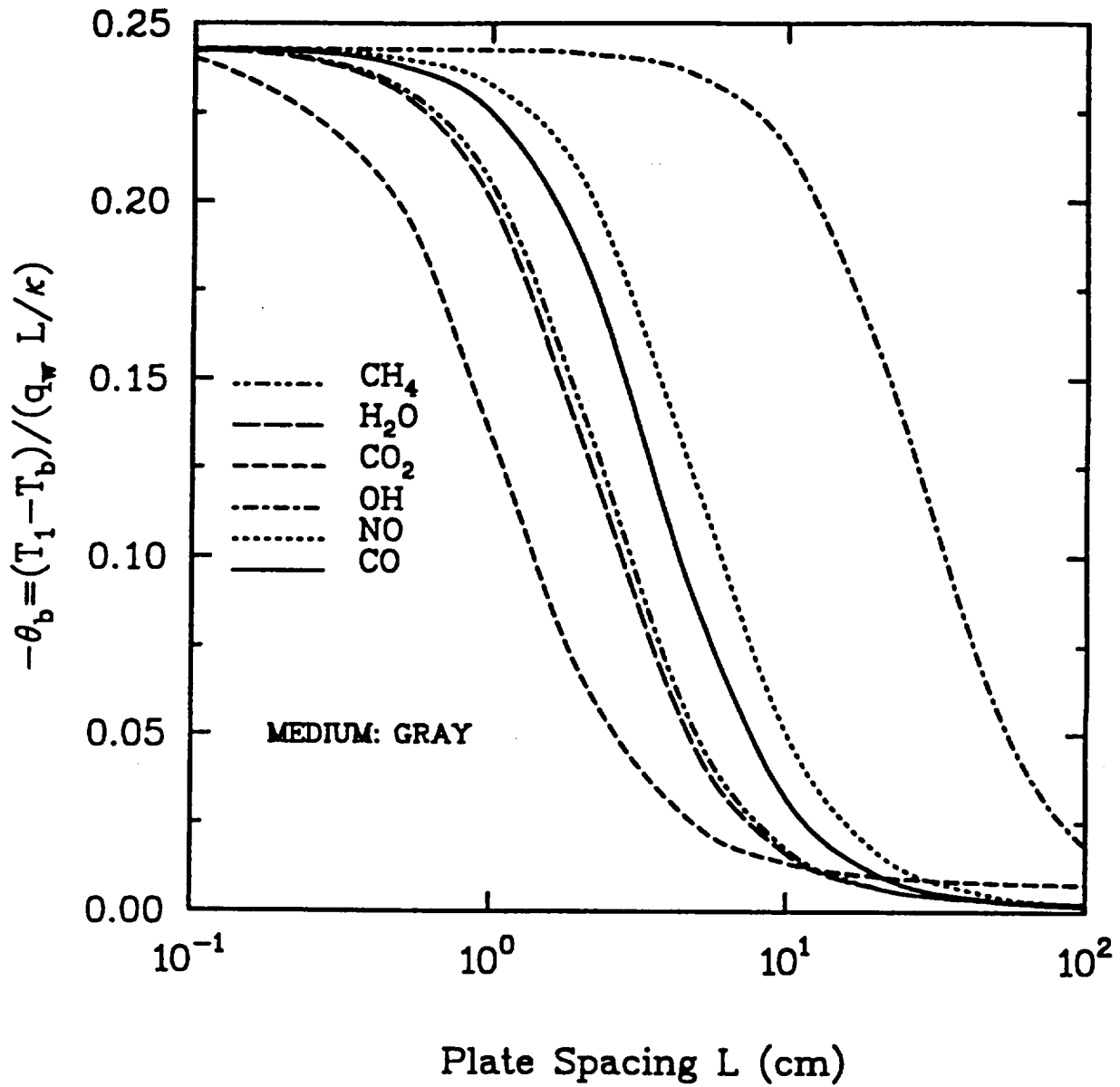


Fig. 6.8: Comparison of NLTE results for different Gases at 500 K and 1 Atm.

## 6.2 Nongray Results

In this section, nongray results are presented for different gases under LTE and NLTE conditions. The temperature and pressure ranges are same as for gray gas analyses. The plate spacing is kept between 0.01 to 100 centimeters. Figures 6.9 through 6.14 present results for CO, NO, OH, CO<sub>2</sub>, H<sub>2</sub>O, and CH<sub>4</sub>, respectively.

Figure 6.9(a) presents LTE result for CO at temperatures ranging from 300 to 2000 K and for one atmospheric pressure. The results show that the bulk temperature decreases from lower to higher values of wall temperatures. In Fig. 6.9(b), temperature is kept fixed at 500 K and results are compared at 0.1, 1, 5, and 10 atm. It is seen that the bulk temperature decreases with increasing pressure. One interesting observation is that the variation is seen only at higher plate spacings. At lower plate spacings, the results are almost identical for any temperatures and pressures. This is due to optically thin radiative interaction in this region. Figure 6.9(c) is a comparison of LTE and NLTE results at one atmospheric pressure and temperatures in the range of 300 to 2000 K. The study reveals that LTE and NLTE results differ only at lower temperatures. Results presented in Fig. 6.9(d) demonstrate that NLTE effects are important only at low pressures.

Results for NO are presented in Fig. 6.10. Figures 6.10(a) and 6.10(b) are comparison of LTE results at different pressures and temperatures. The trend of the results are similar to that observed for CO. Figures 6.10(c) and 6.10(d) show LTE and NLTE comparisons at different pressures and temperatures. The results follow the same pattern as for CO. Figures 6.11 illustrate results for OH. A study of Fig. 6.11(a) shows that OH has very little radiative



interaction at a temperature of 300 K and one atmospheric pressure. However, it shows some effect at higher temperatures and pressures (Figs. 6.11(a) and 6.11(b)). In Figs. 6.11(c) and 6.11(d), LTE and NLTE results are compared. It is seen that there is no difference between LTE and NLTE results at any temperature and pressure. This implies that NLTE does not have significant effect on OH at any temperature and pressure. However, it does have some effect at low temperatures and pressures (Figs. 6.11(c) and 6.11(d)).

Figures 6.12 present results for CO<sub>2</sub>. Figures 6.12(a) and 6.12(b) present LTE results at different temperatures and pressures, respectively. It is seen that bulk temperature decreases with increasing pressure and temperature. Figures 6.12(c) and 6.12(d) are comparison of LTE and NLTE results at different temperatures and pressures, respectively. There appears to be no difference between LTE and NLTE results at these conditions. Figure 6.12(d) suggests that there is little difference between LTE and NLTE results at 0.1 atm. and 500 K. Figures 6.13(a) and 6.13(b) are comparison of LTE results for H<sub>2</sub>O at different pressures and temperatures. The trend is almost similar to that observed for CO<sub>2</sub>. Figures 6.13(c) and 6.13(d) are comparisons of LTE and NLTE results. There is no difference between LTE and NLTE results except at low temperatures and pressures. The difference is quite significant at 0.1 atm. and 500 K. The difference in this case is more than that observed for CO<sub>2</sub>. Figures 6.14(a) and 6.14(b) present LTE results for CH<sub>4</sub> at various temperatures and pressures, respectively. Again, the bulk temperature is seen to decrease with increasing temperature. Figures 6.14(c) and 6.14(d) are comparison of LTE and NLTE results for CH<sub>4</sub> at various temperatures and pressures, respectively. The results do not show any difference between LTE and NLTE at any temperature and pressure conditions. Thus, NLTE consideration is not important for CH<sub>4</sub>. Figure 6.15 is a comparison of NLTE results for all the gases under consideration at 500 K and one atmospheric pressure. The results show that the gases in the descending order of bulk temperature are OH, CO, NO, CO<sub>2</sub>, CH<sub>4</sub>, and H<sub>2</sub>O. This implies that among

the gases  $\text{H}_2\text{O}$  is highest radiating gas whereas  $\text{OH}$  is the least radiating gas.

By studying the results under nongray assumption, it becomes obvious that bulk temperature usually decreases with an increase in temperature and pressure. This implies that the radiating capacity of the gases increases with an increase in temperature and pressure. Second important observation is that polyatomic gases do not contribute significantly in NLTE process. However,  $\text{OH}$  being a diatomic radical, shows least variation from LTE conditions among the diatomic gases under consideration. Further,  $\text{CH}_4$  shows absolutely no effect of NLTE at any temperature and pressure; whereas NLTE results for other polyatomic gases show little variation from LTE results at moderate pressures and temperatures.

### **6.3 Comparative Results for Gray and Nongray Analyses**

In this section, gray and nongray results are compared at different temperatures and pressures. Figures 6.16 through 6.21 present these comparative results

Figure 6.16(a) presents gray and nongray NLTE results for  $\text{CO}$  at temperatures ranging from 300 to 2000 K and one atmospheric pressure. The results show that there is significant difference between gray and nongray results at lower temperatures. At higher temperatures, the difference is relatively lower. However, the rate of decrease of the difference between gray and nongray results is less as temperature is increased. Thus, even at 2000 K, significant difference between gray and nongray results is observed. Figure 6.16(b) is a comparison of gray and nongray results at 500 K and 0.1, 1, and 10 atm. The variation between gray and nongray results is quite significant and it increases with increasing pressure.

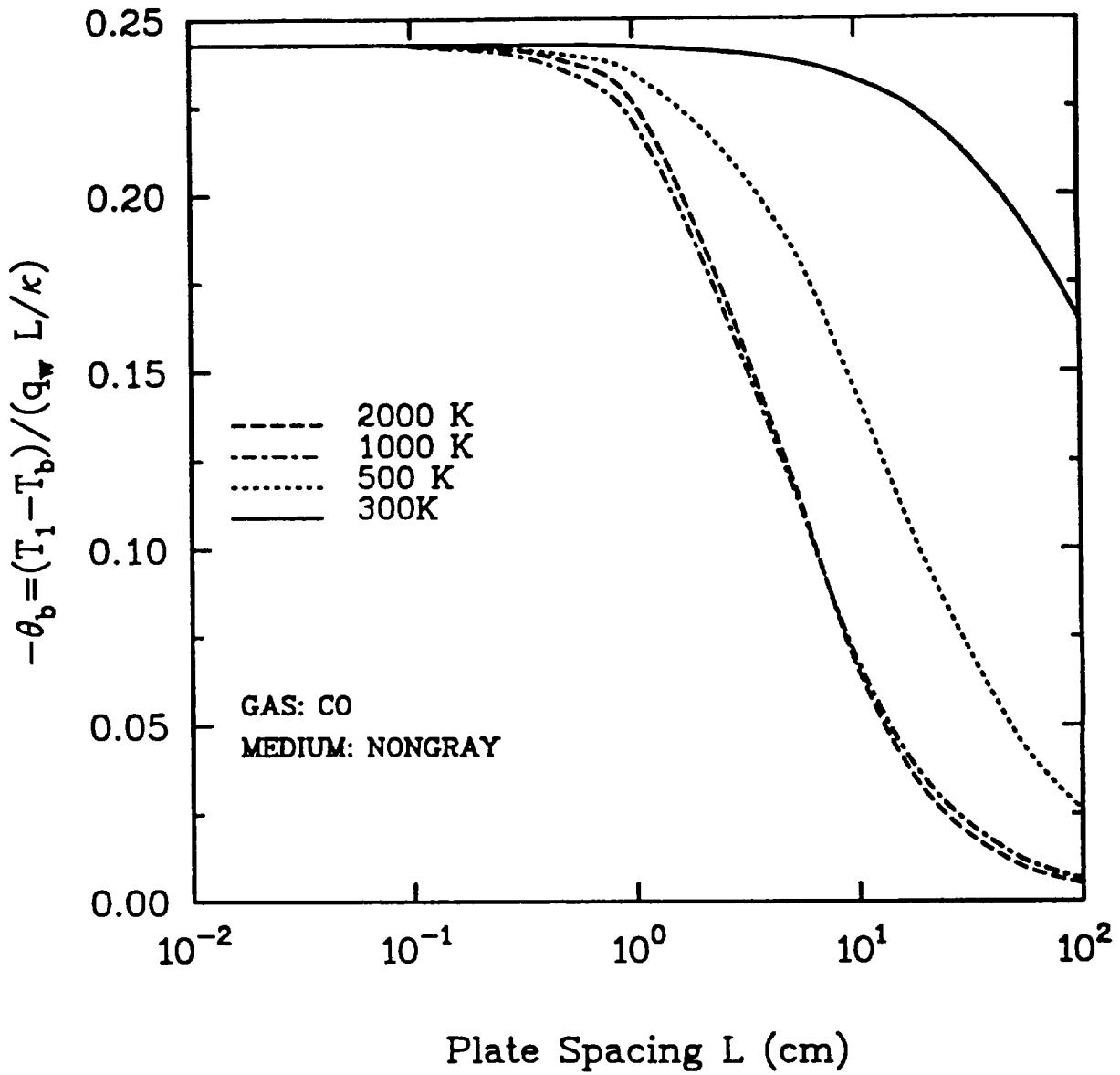


Fig. 6.9(a): LTE results for CO, P=1 atm,  $T_w=300-2000$  K

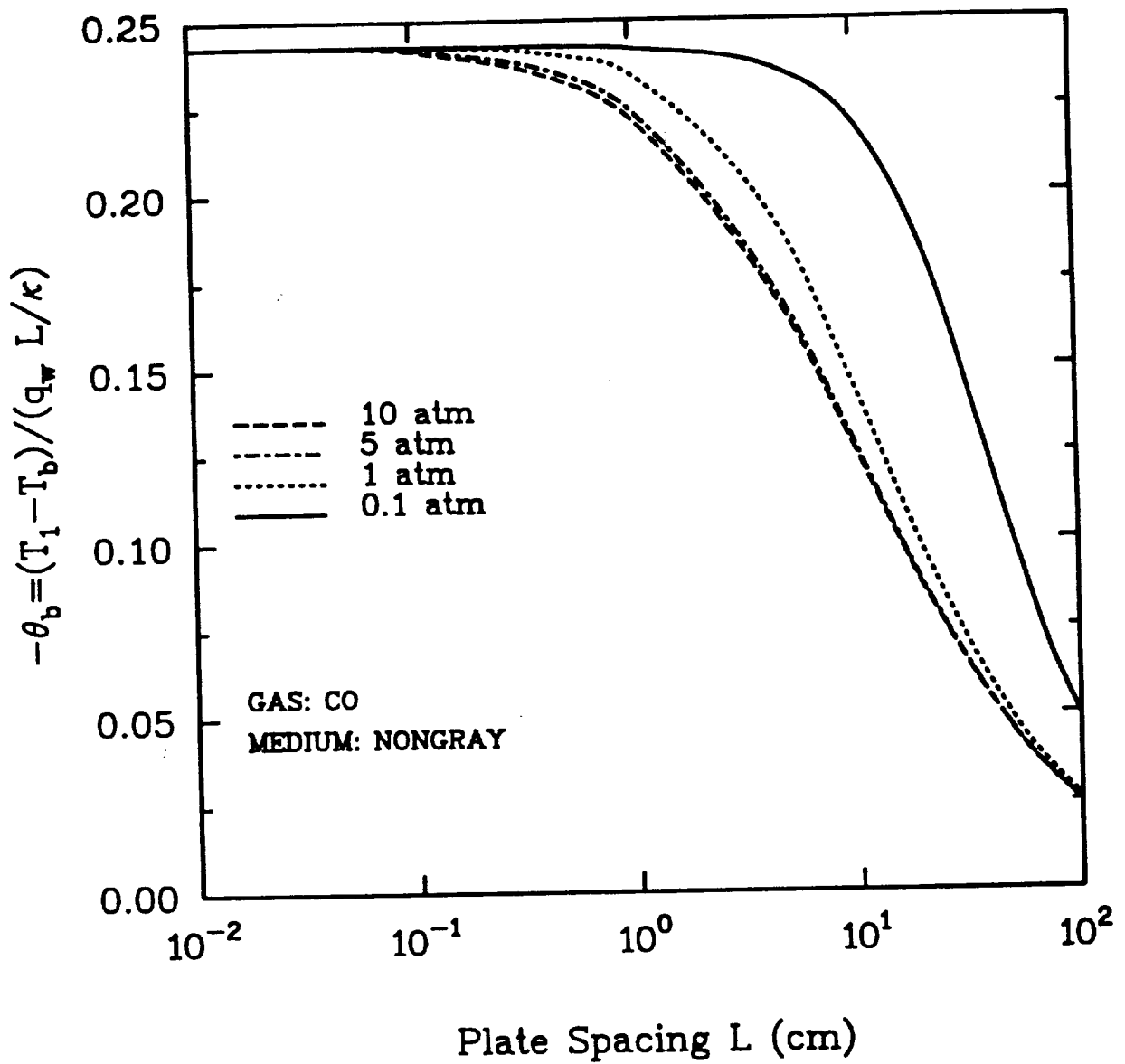


Fig. 6.9(b): LTE results for CO,  $T_w=500$  K,  $P=0.1-10$  atm

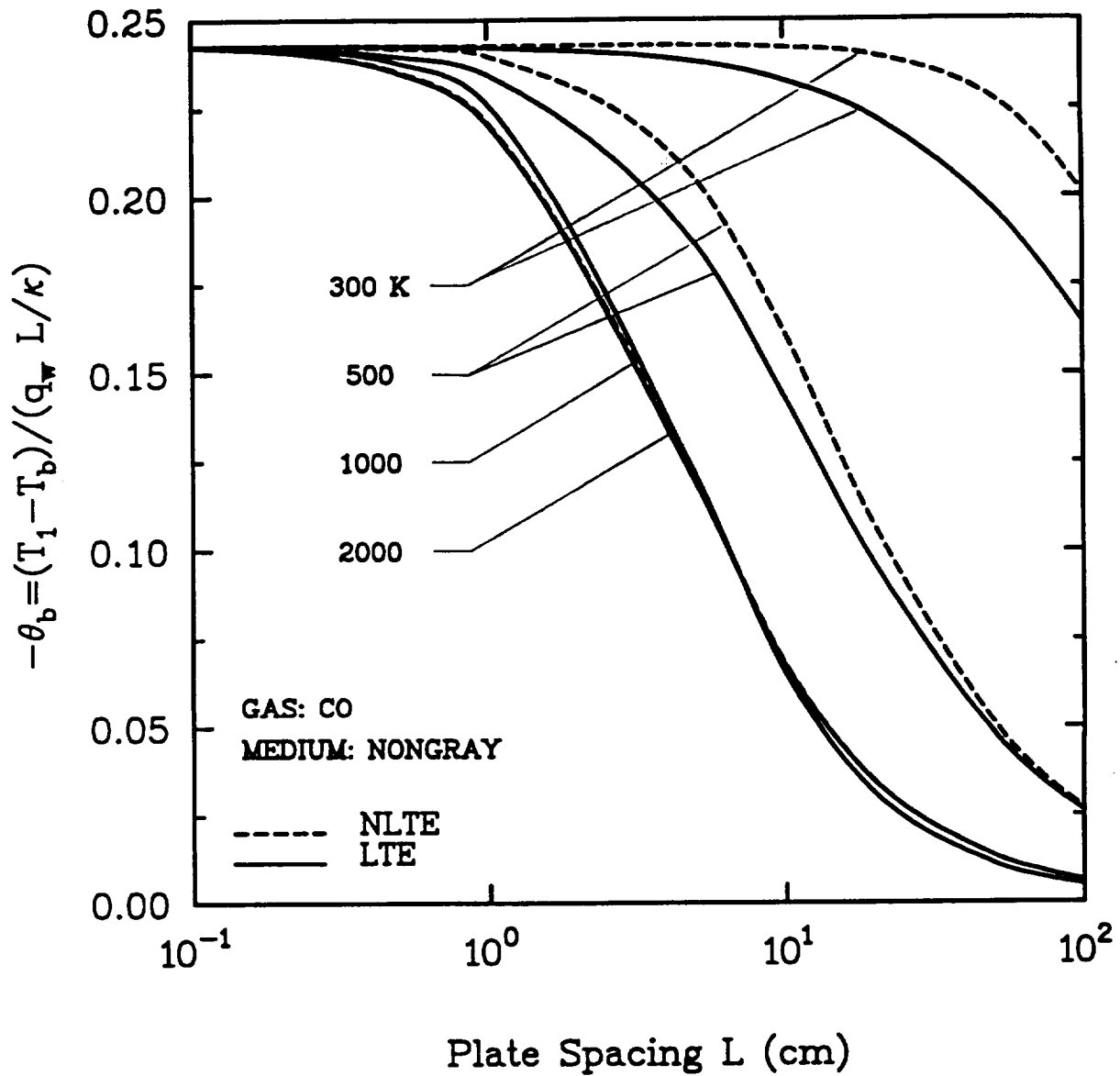


Fig. 6.9(c): LTE and NLTE results for CO, P=1 atm,  $T_w=300-2000$  K

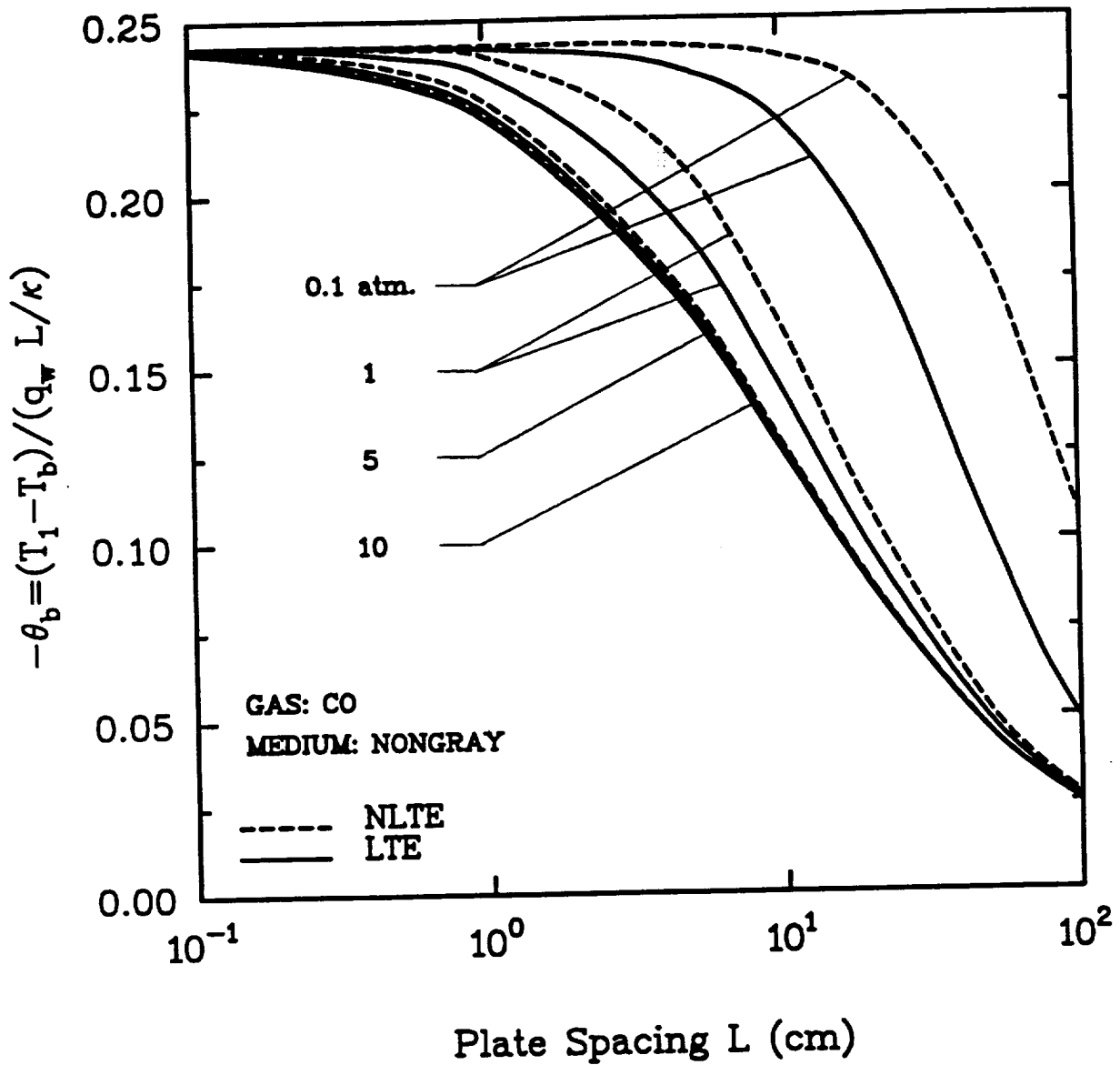


Fig. 6.9(d): LTE and NLTE results for CO,  $T_w=500$  K,  $P=0.1-10$  atm

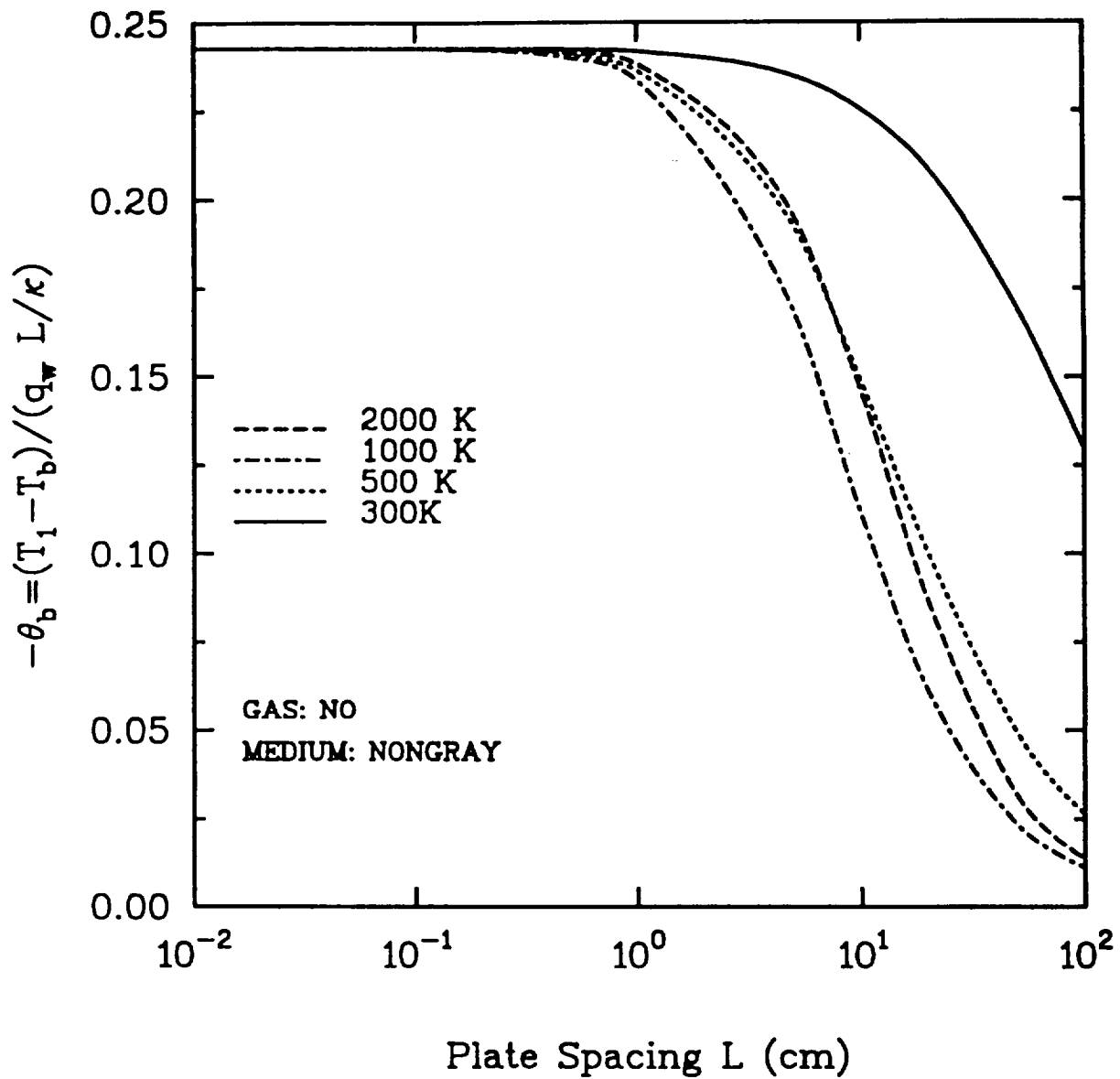
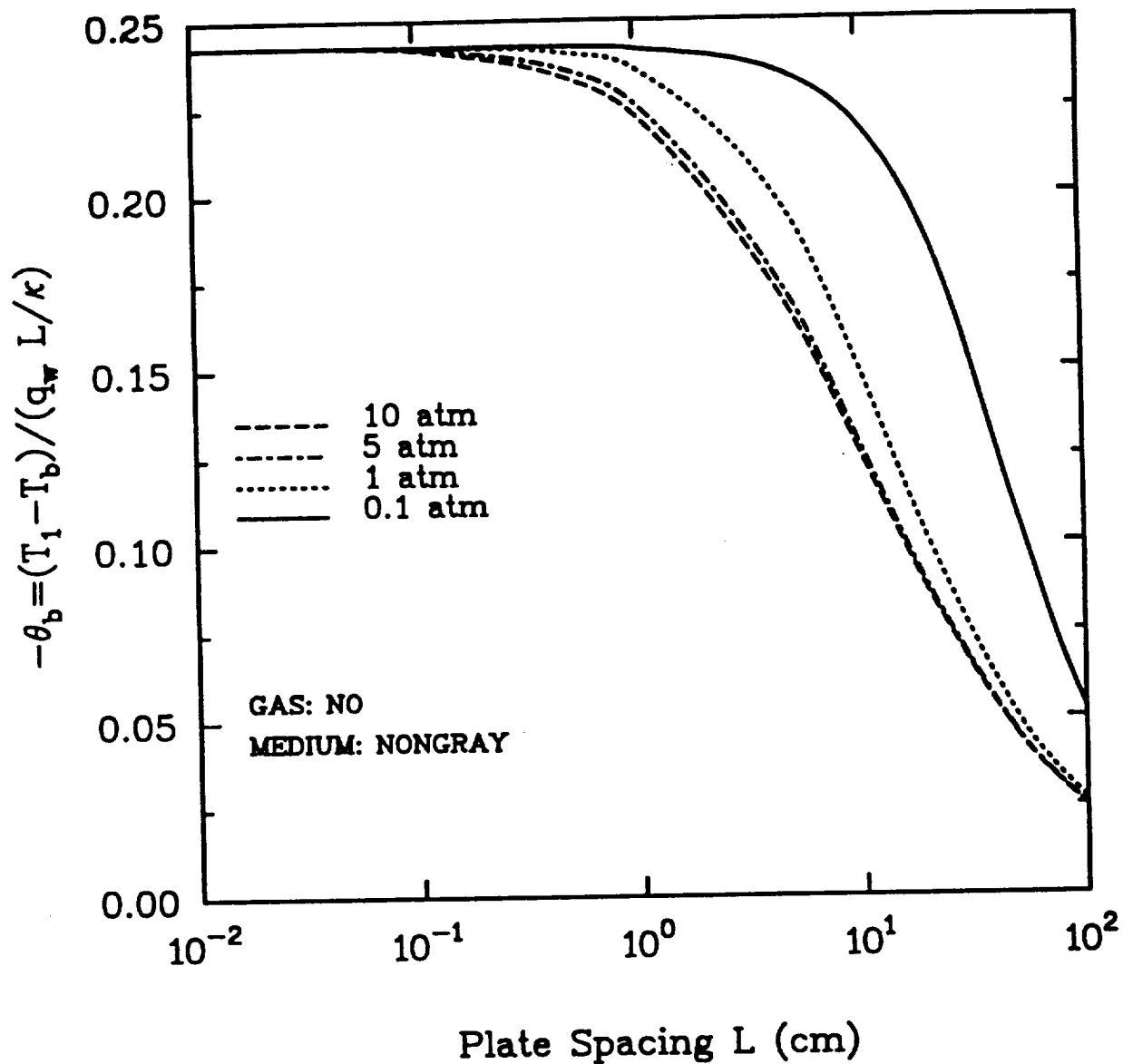


Fig. 6.10(a): LTE results for NO, P=1 atm,  $T_w=300-2000$  K





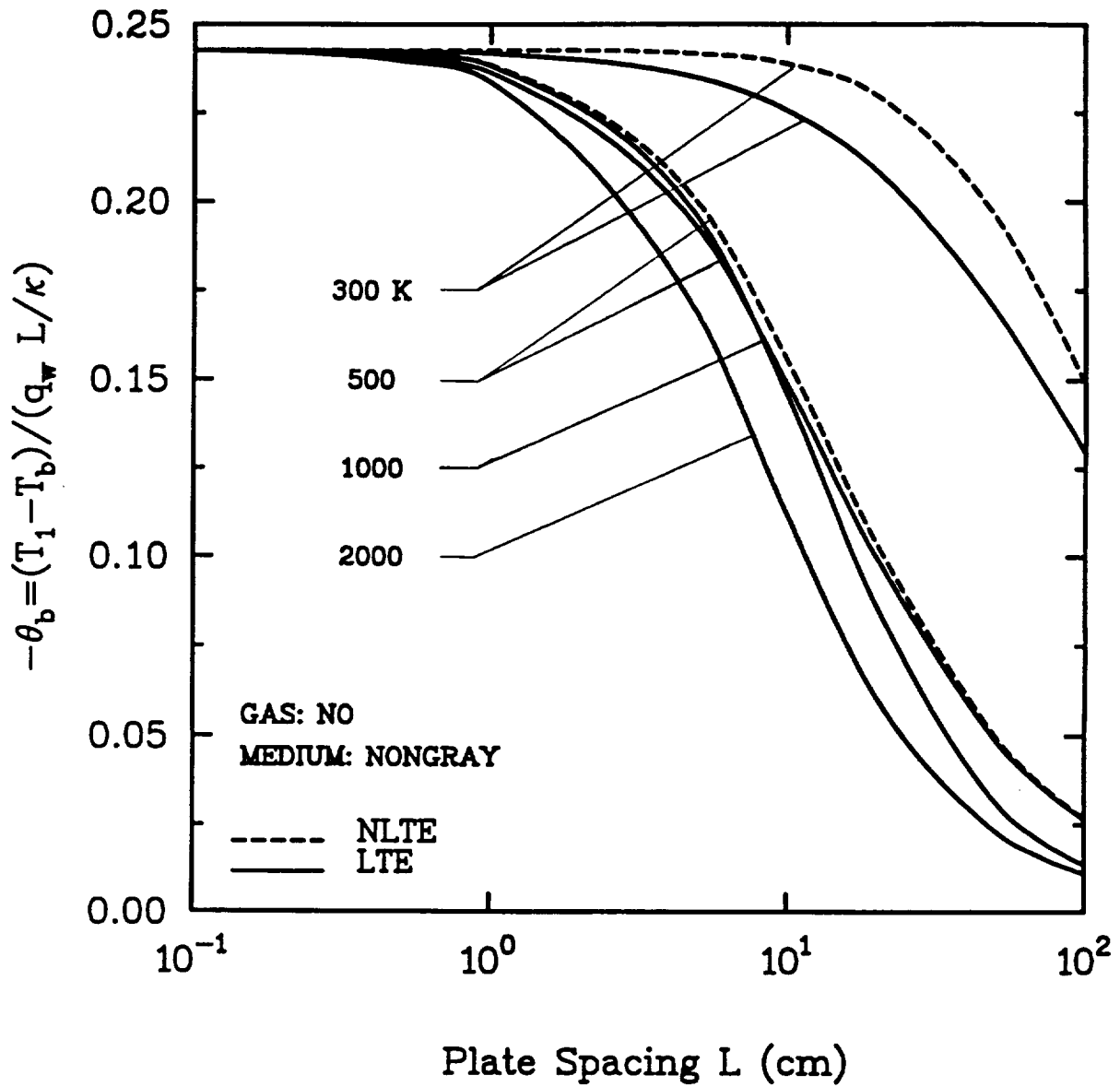


Fig. 6.10(c): LTE and NLTE results for NO, P=1 atm,  $T_w=300-2000$  K

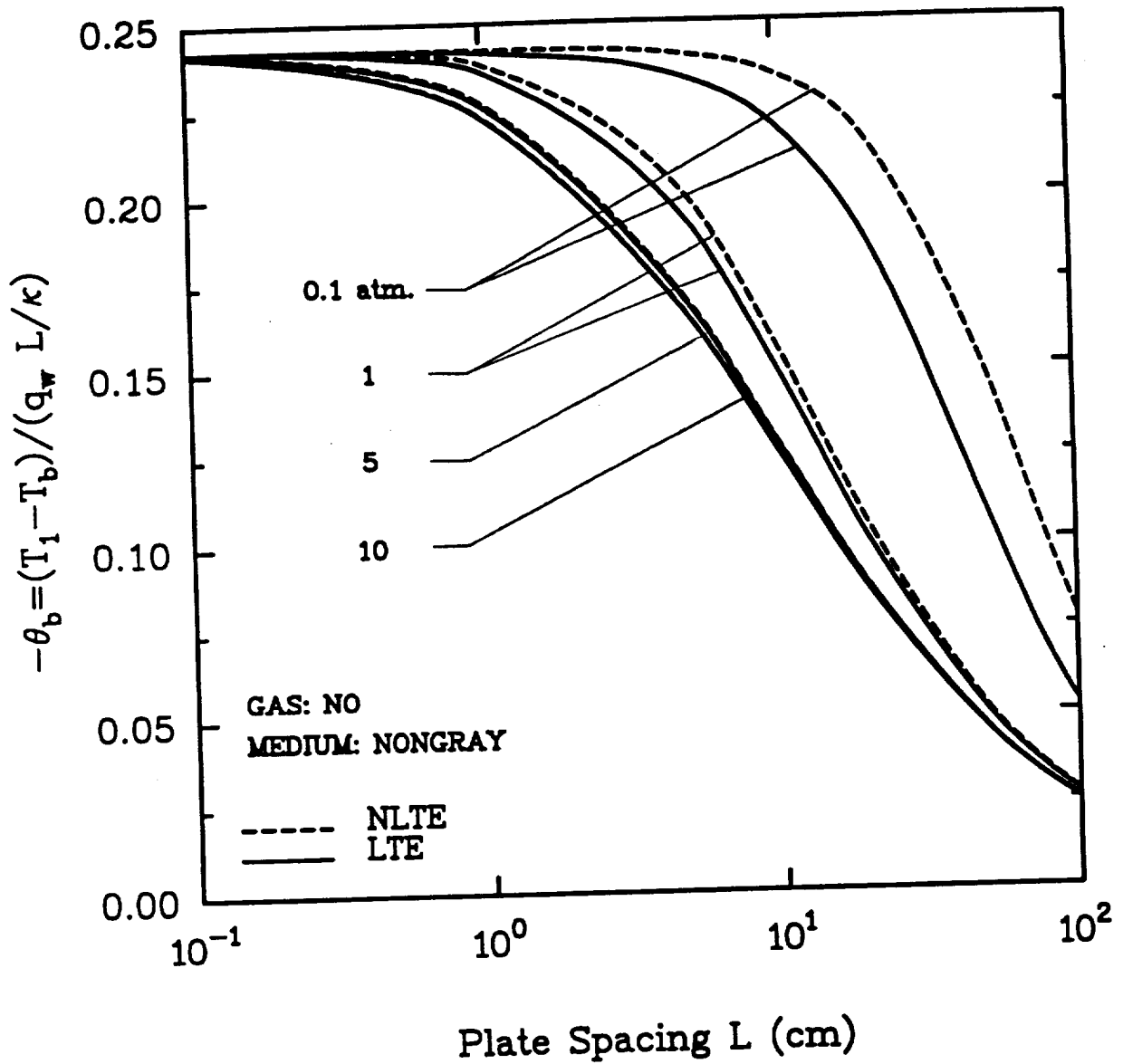


Fig. 6.10(d): LTE and NLTE results for NO,  $T_w=500$  K,  $P=0.1-10$  atm

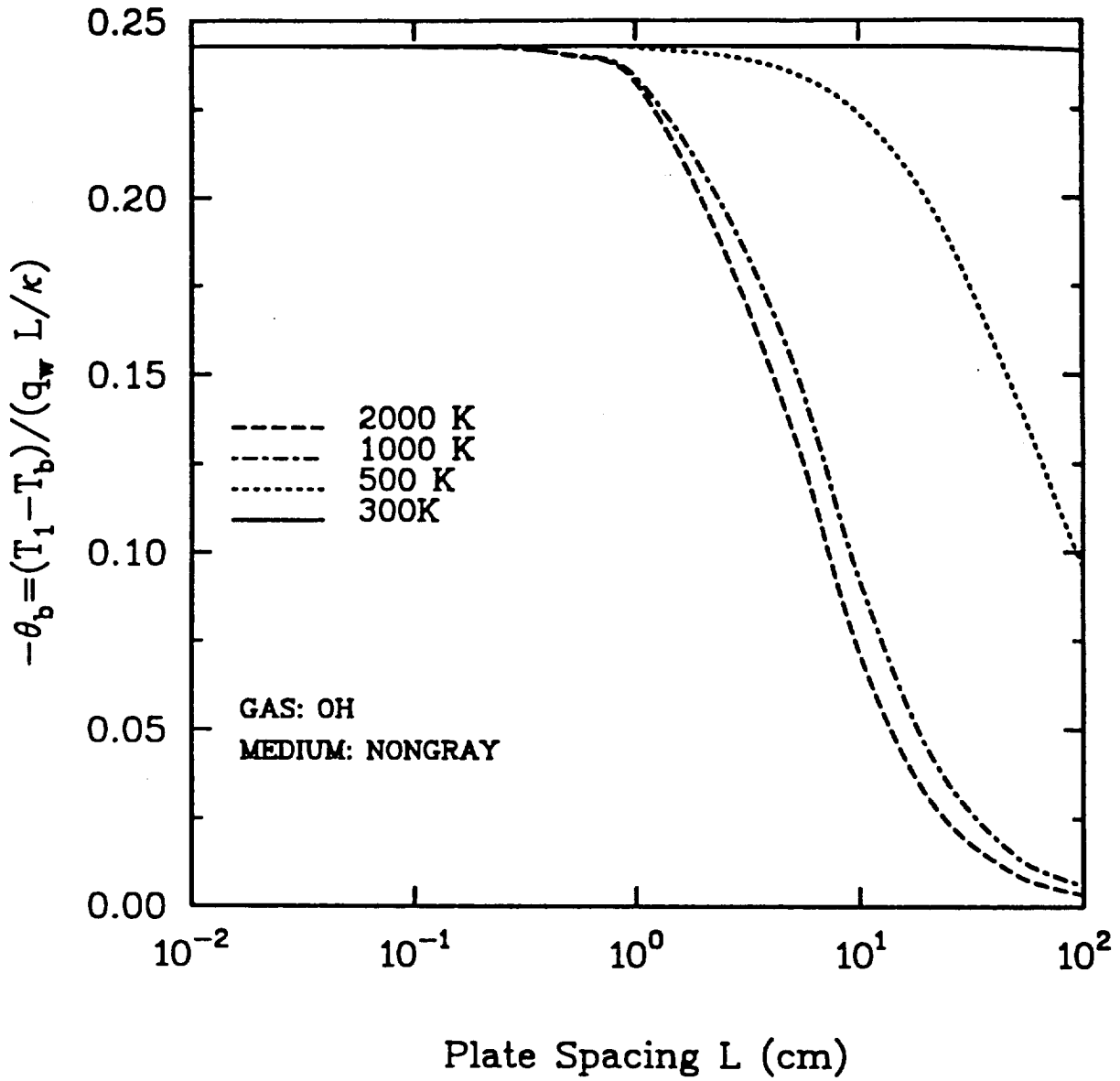


Fig. 6.11(a): LTE results for OH, P=1 atm, T<sub>w</sub>=300–2000 K

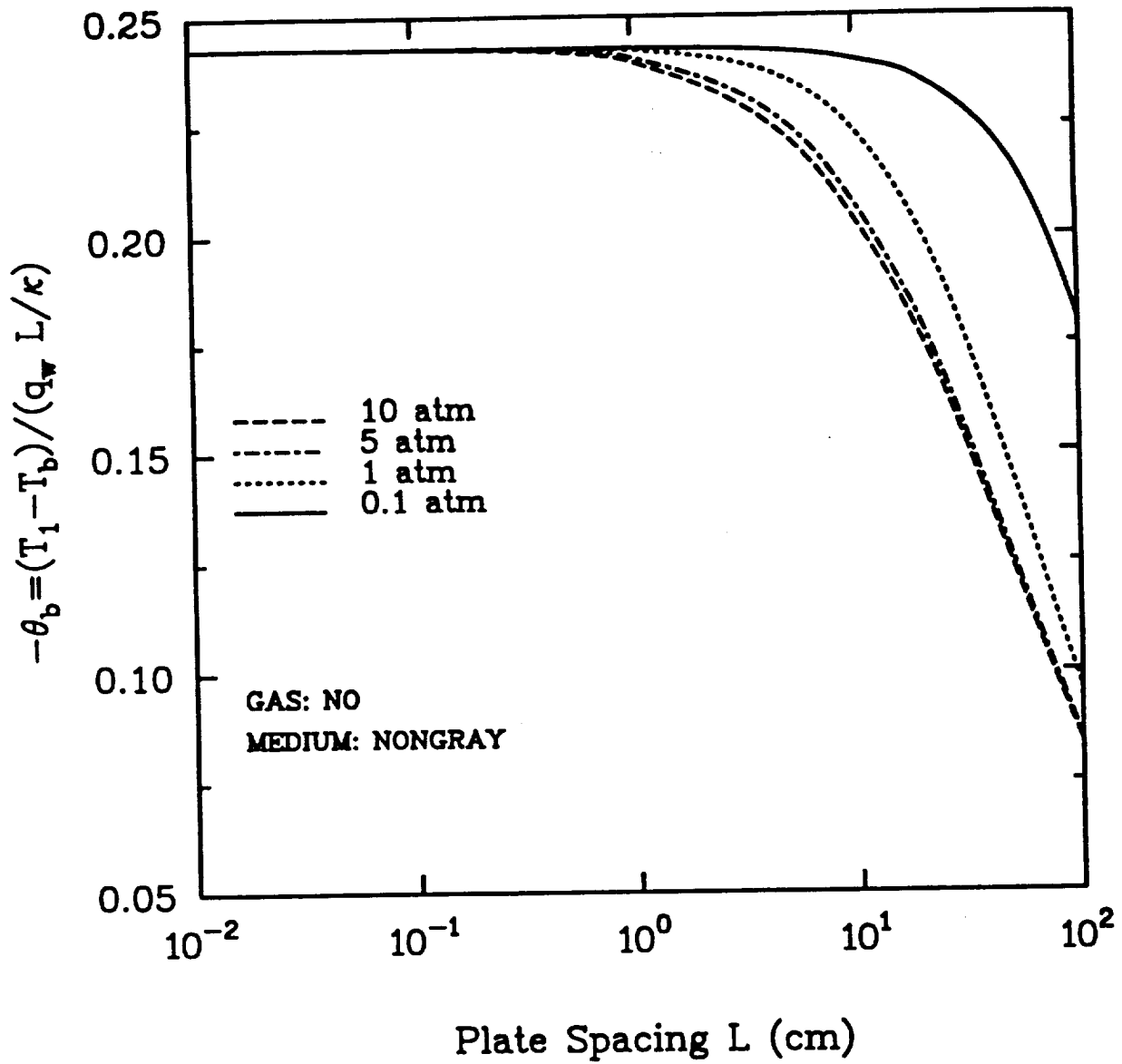
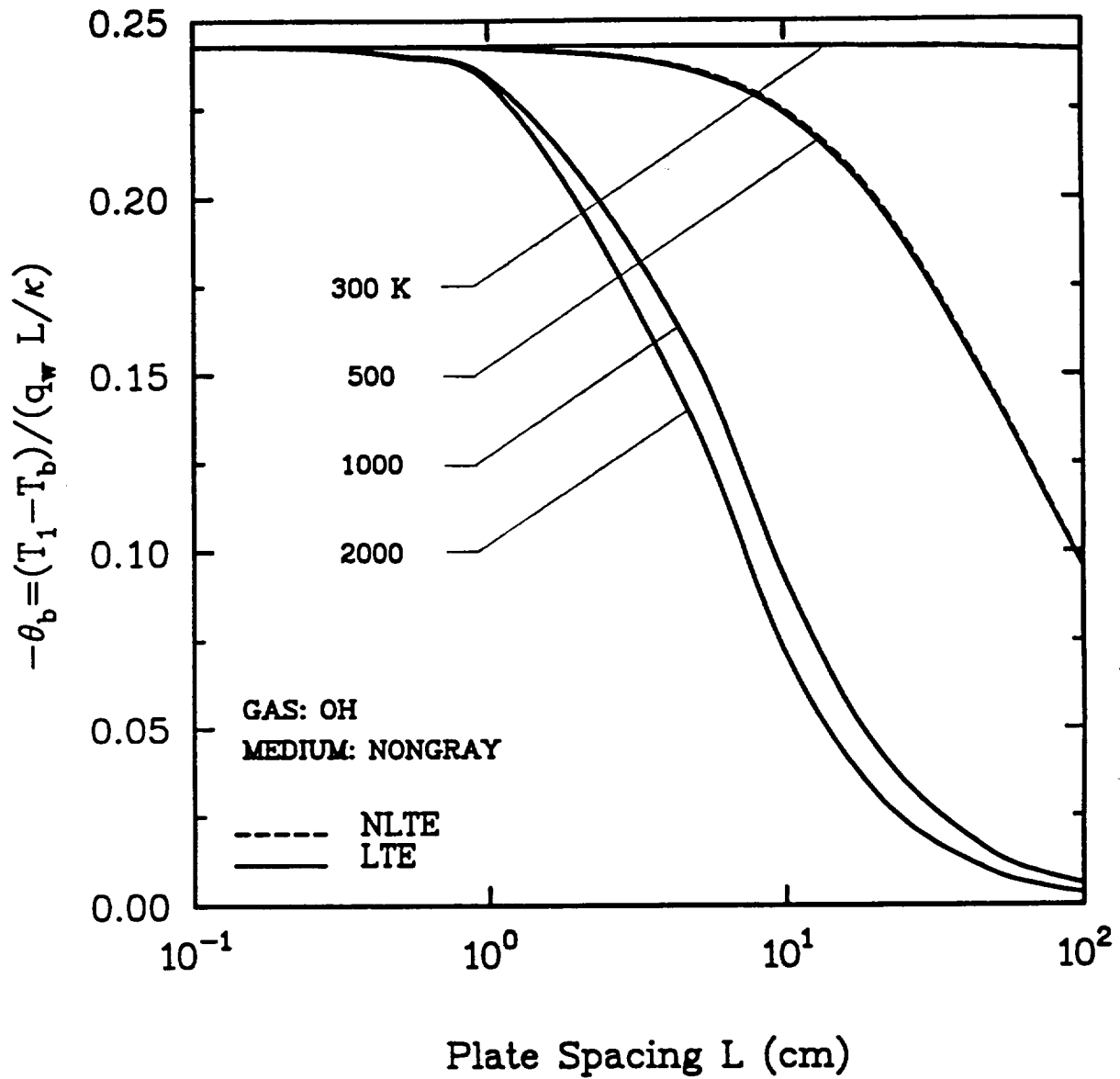


Fig. 6.11(b): LTE results for OH,  $T_w=500$  K,  $P=0.1-10$  atm



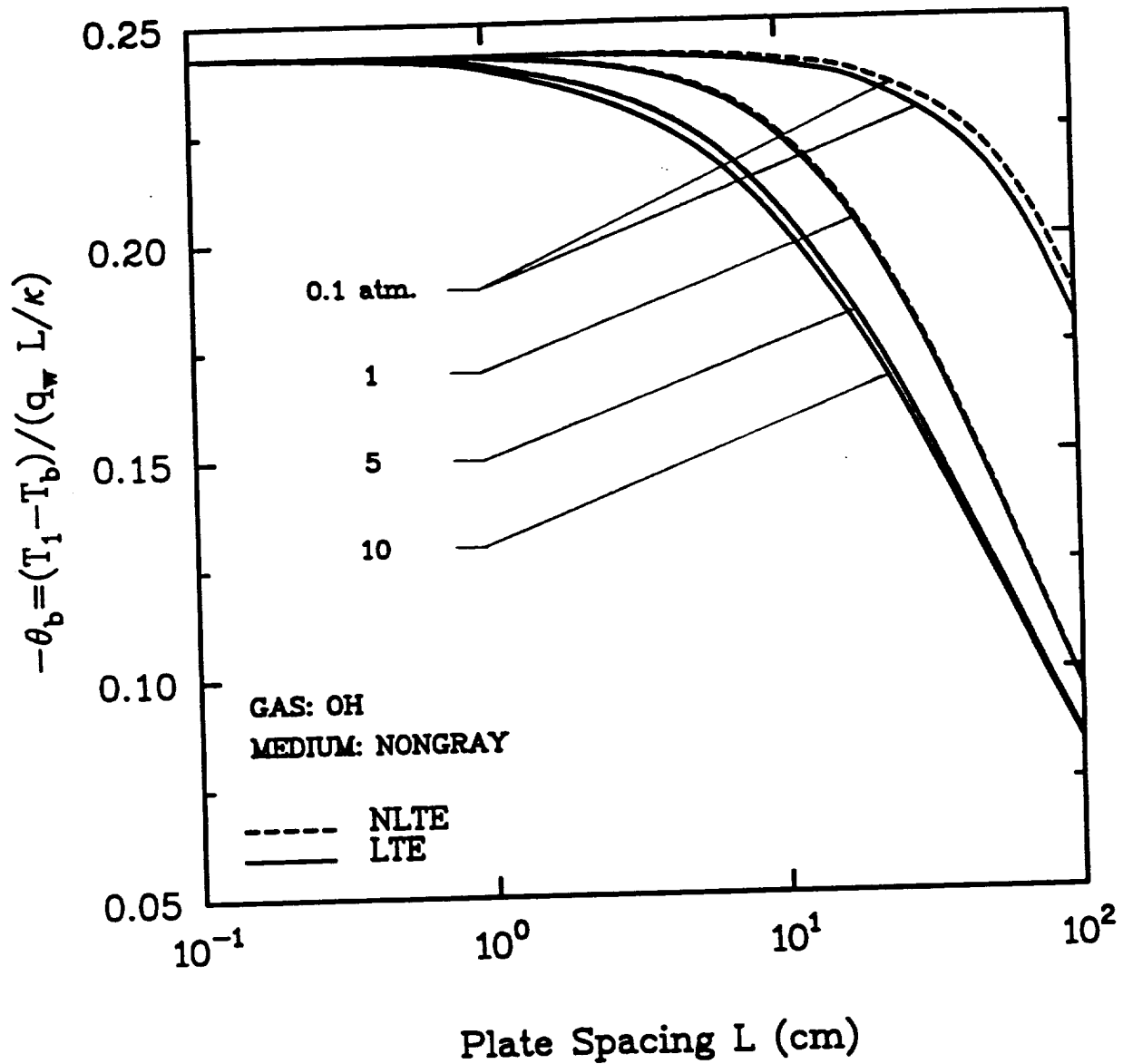


Fig. 6.11(d): LTE and NLTE results for OH,  $T_w=500$  K,  $P=0.1-10$  atm

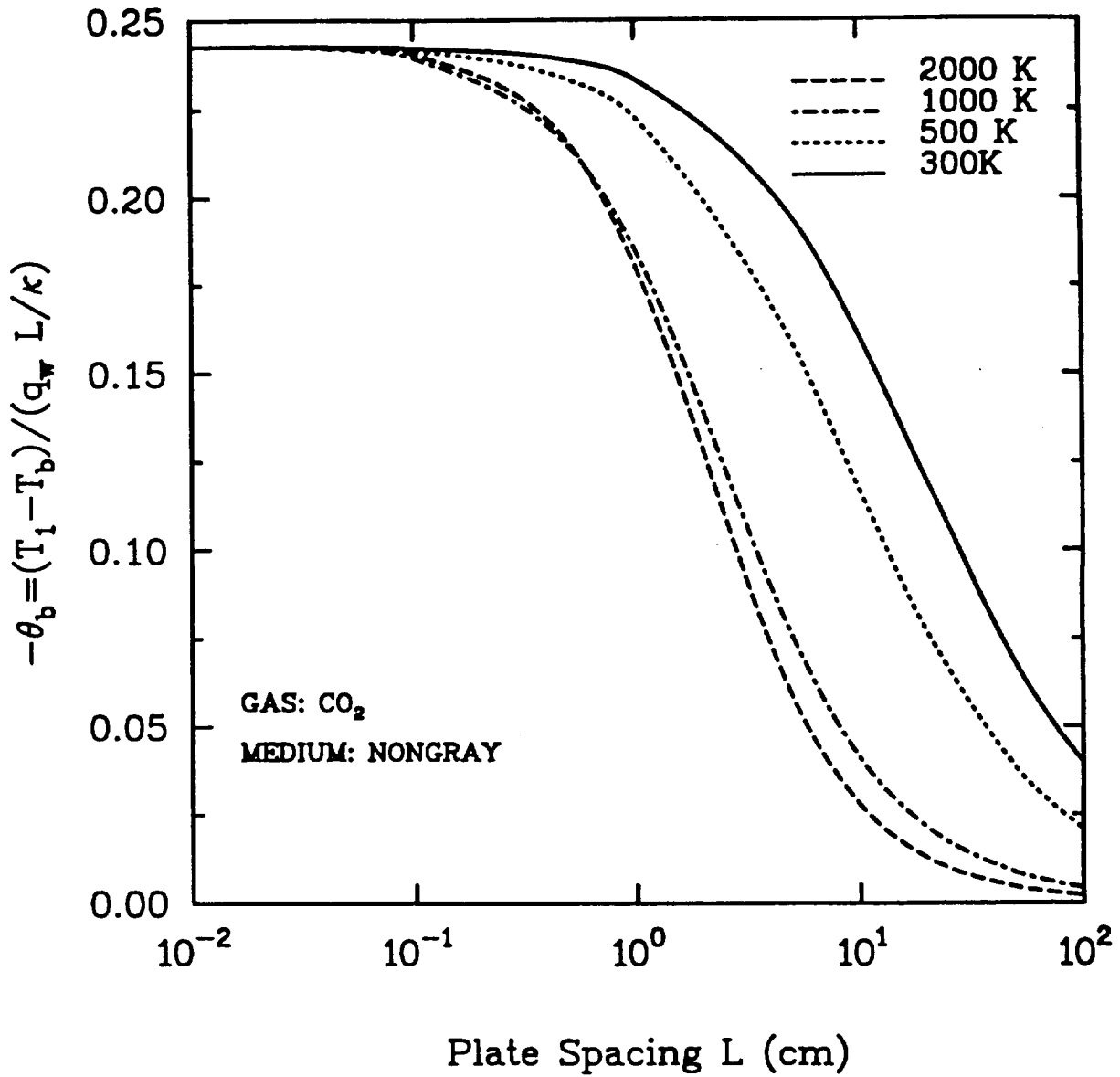


Fig. 6.12(a): LTE results for CO<sub>2</sub>, P=1 atm, T<sub>w</sub>=300–2000 K

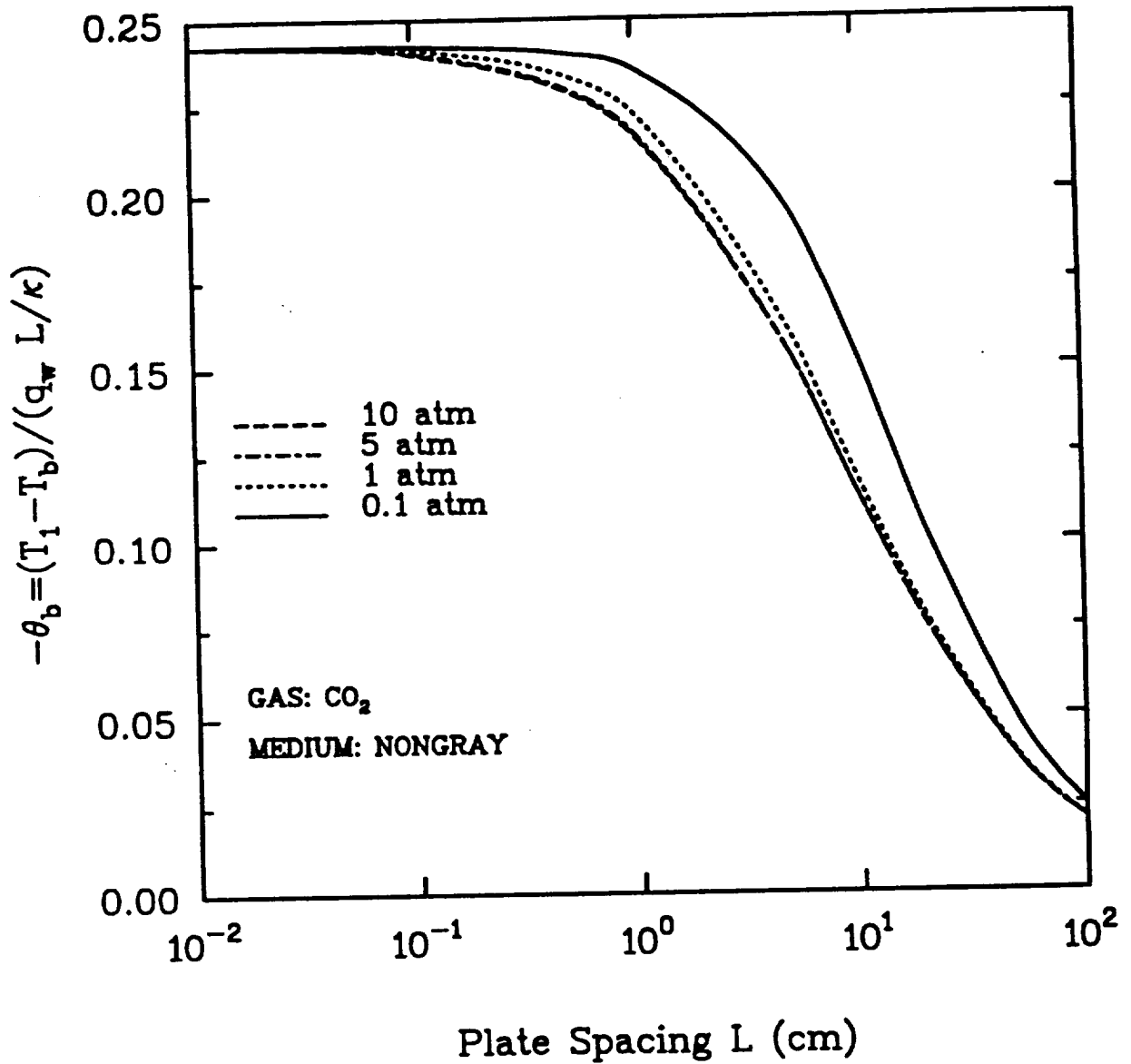


Fig. 6.12(b): LTE results for CO<sub>2</sub>, T<sub>w</sub>=500 K, P=0.1-10 atm



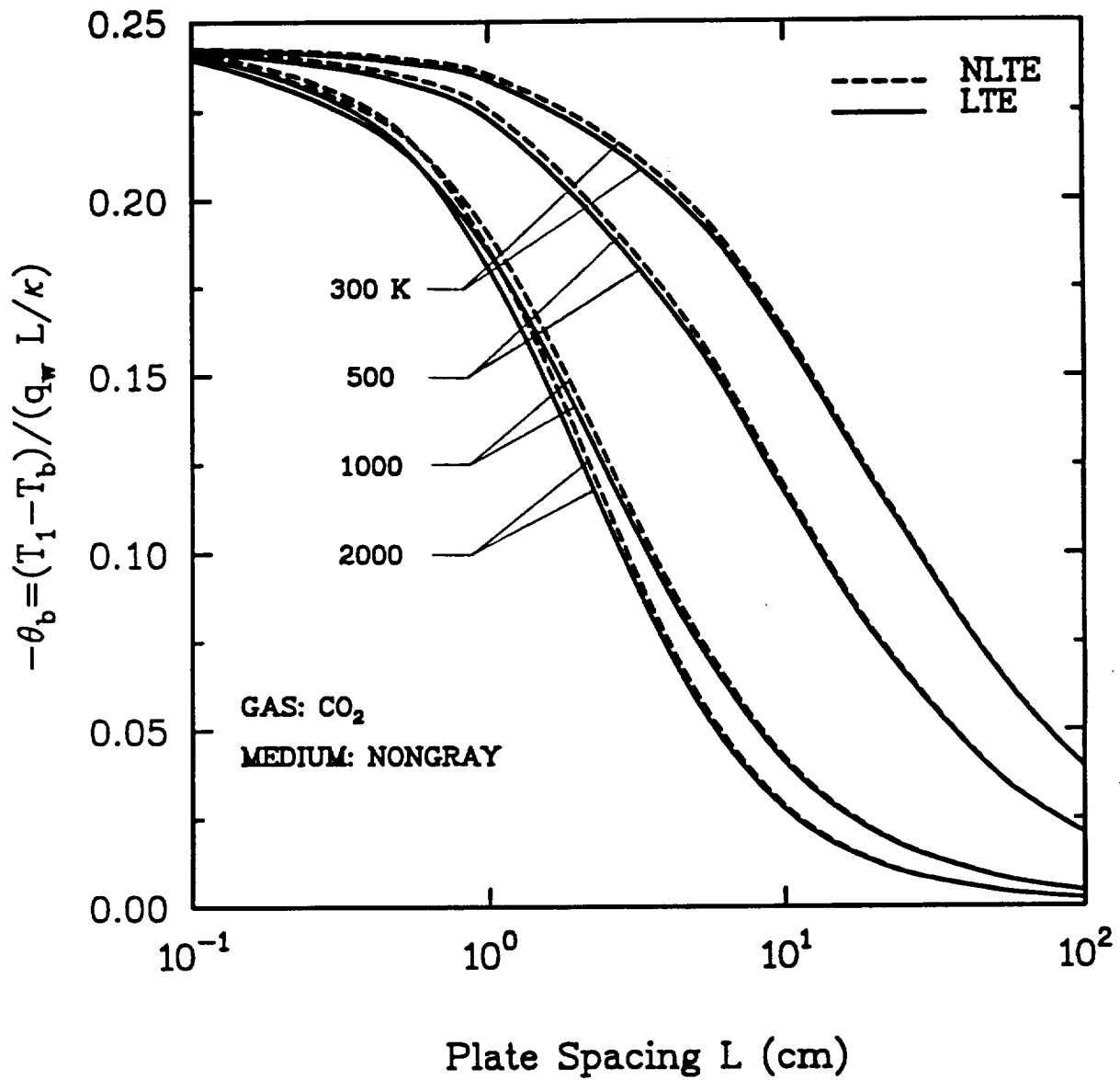


Fig. 6.12(c): LTE and NLTE results for  $\text{CO}_2$ ,  $P=1$  atm,  $T_w=300-2000$  K

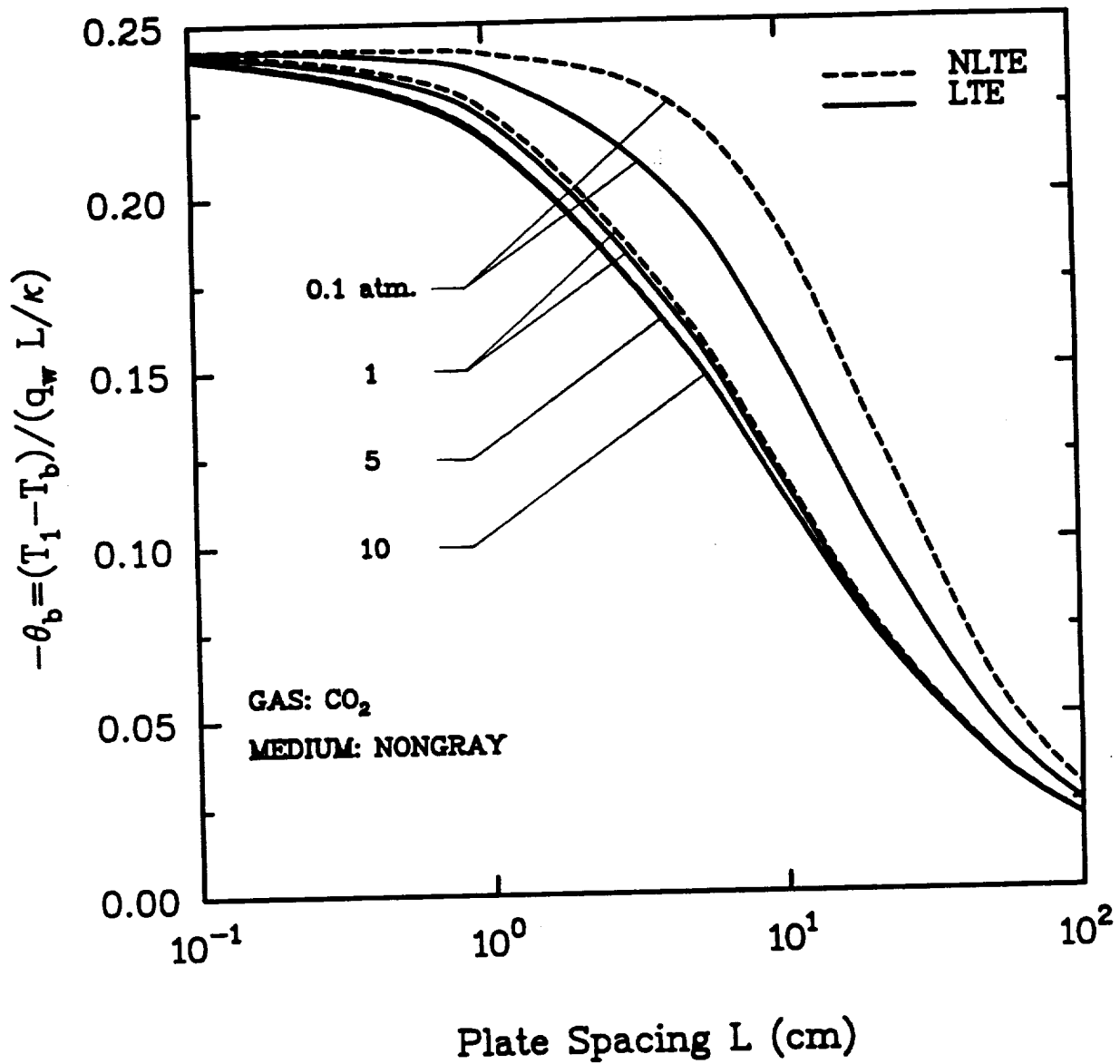


Fig. 6.12(d): LTE and NLTE results for CO<sub>2</sub>, T<sub>w</sub>=500 K, P=0.1–10 atm

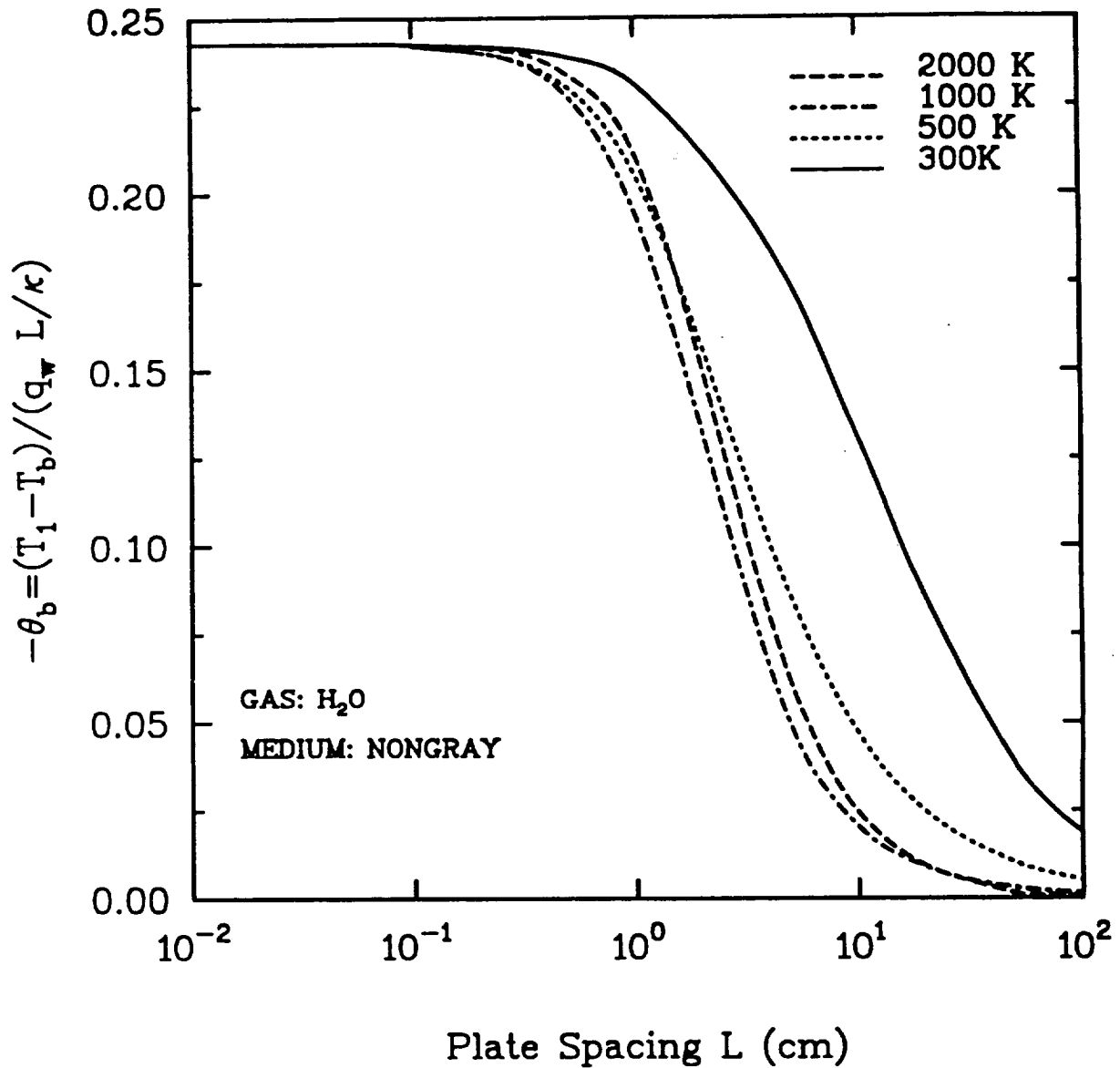


Fig. 6.13(a): LTE results for H<sub>2</sub>O, P=1 atm, T<sub>w</sub>=300–2000 K

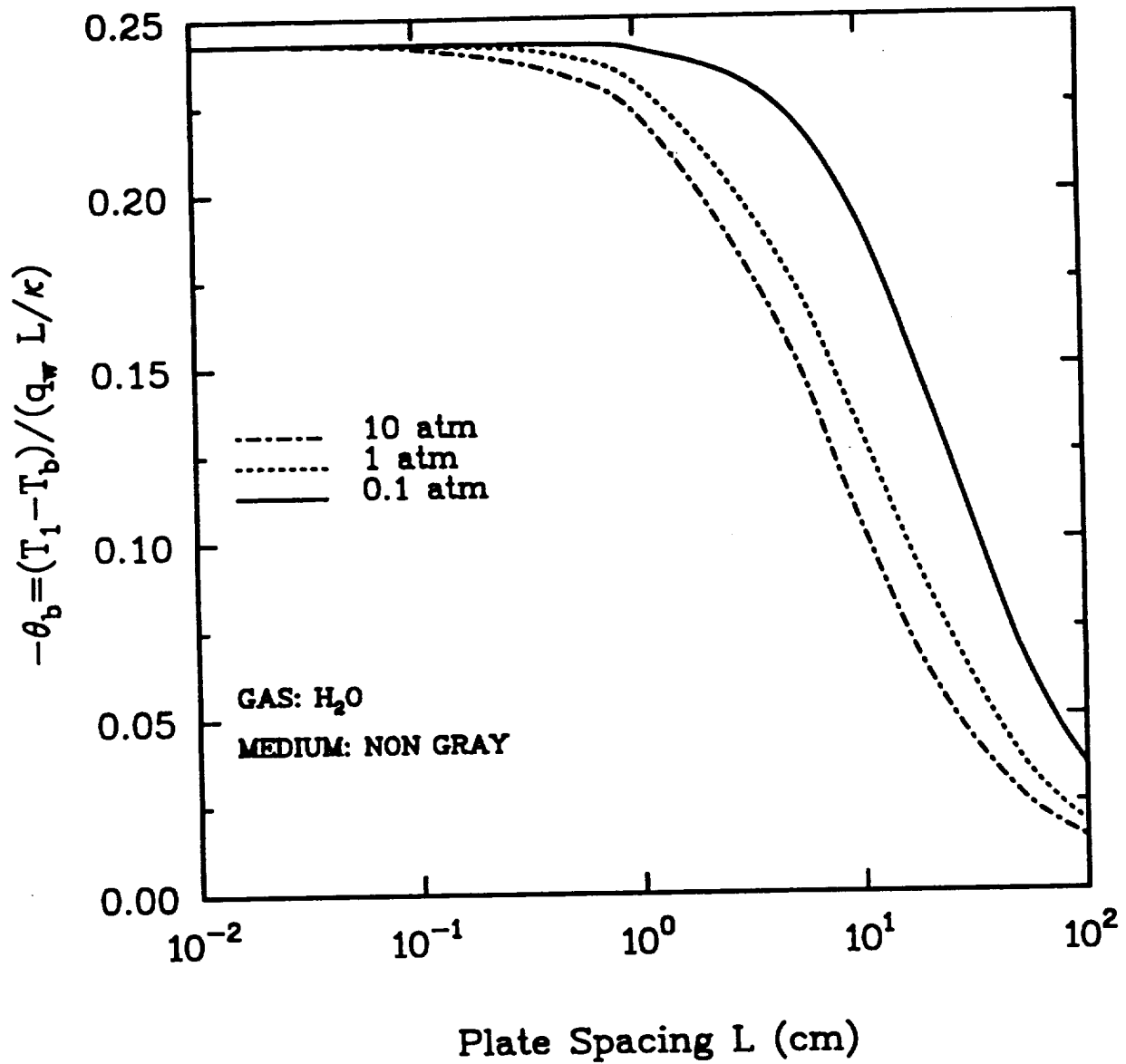


Fig.613(b): LTE results for H<sub>2</sub>O, T<sub>w</sub>=300 K, P=0.1-10 atm

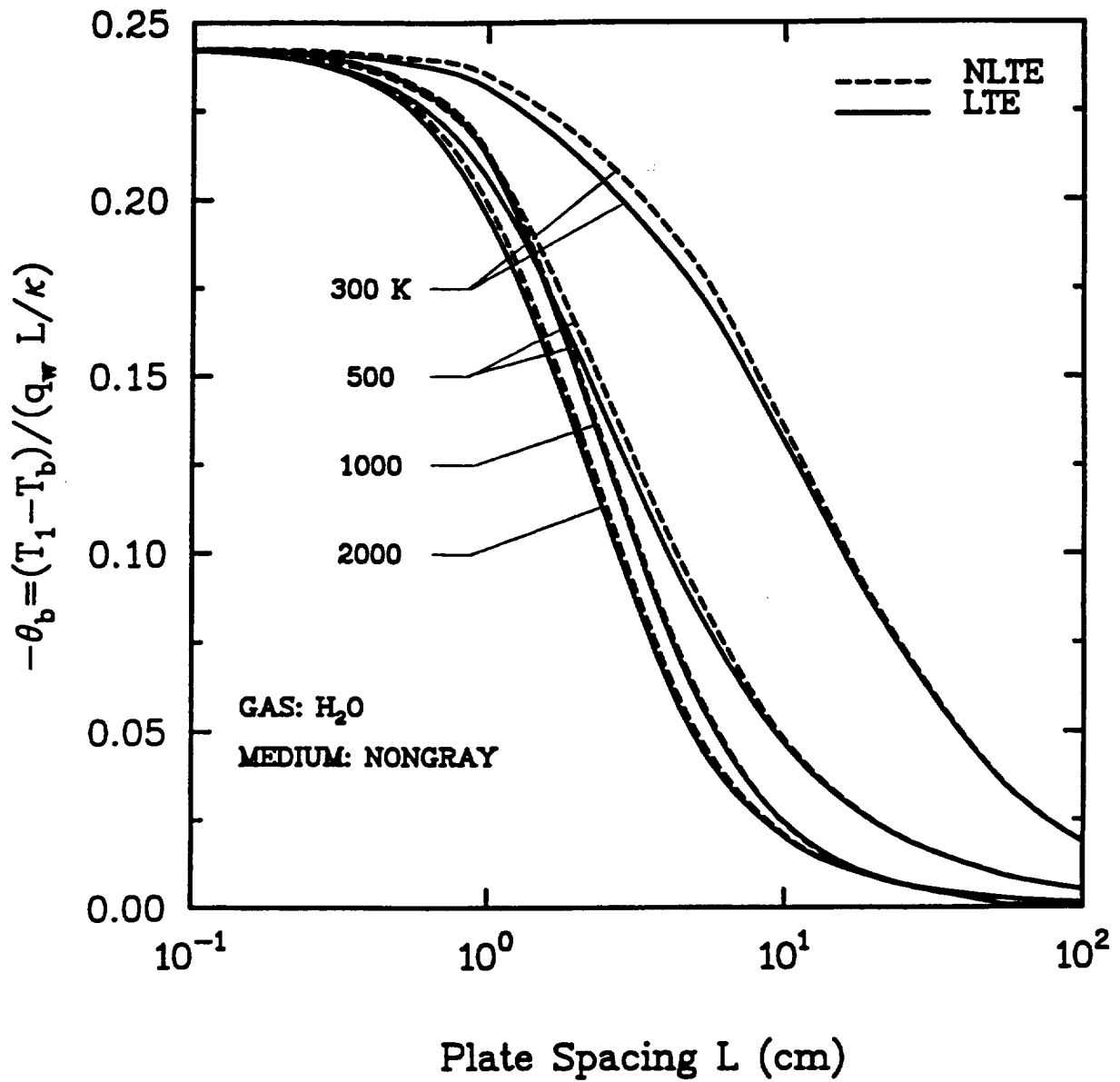


Fig. 6.13(c): LTE and NLTE results for H<sub>2</sub>O, P=1 atm, T<sub>w</sub>=300–2000 K

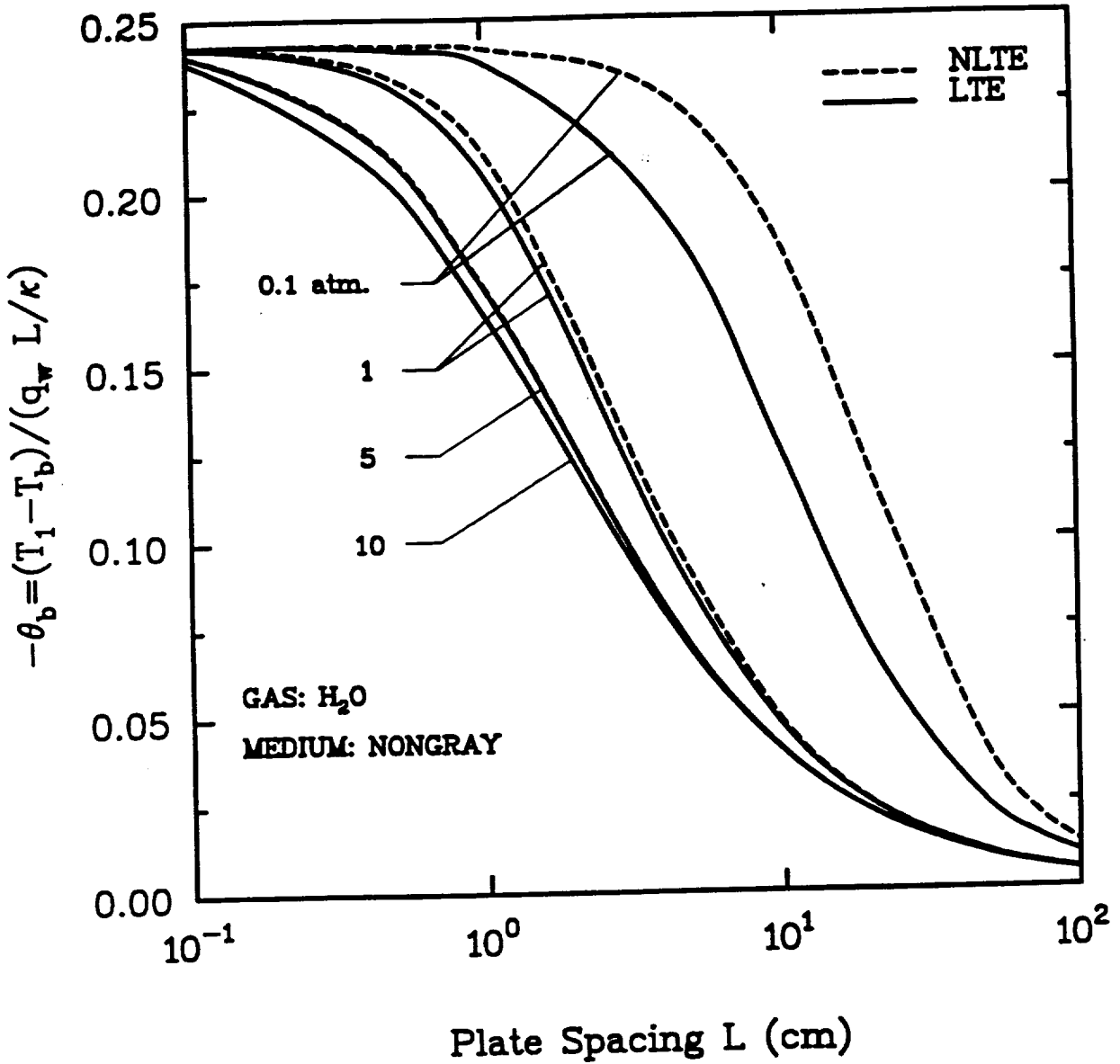


Fig. 6.13(d): LTE and NLTE results for  $H_2O$ ,  $T_w=500$  K,  $P=0.1-10$  atm

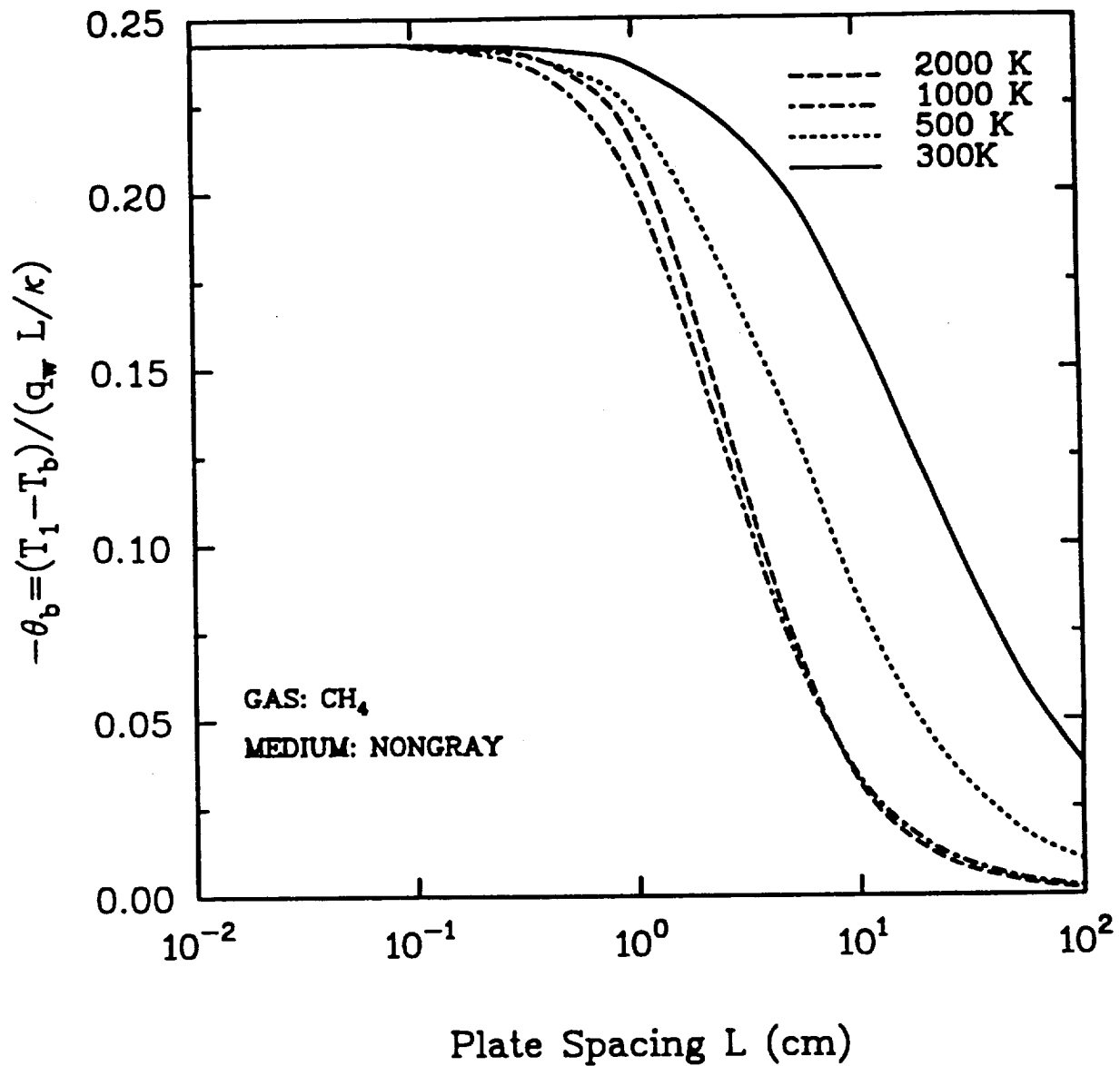


Fig. 6.14(a): LTE results for CH<sub>4</sub>, P=1 atm, T<sub>w</sub>=300–2000 K

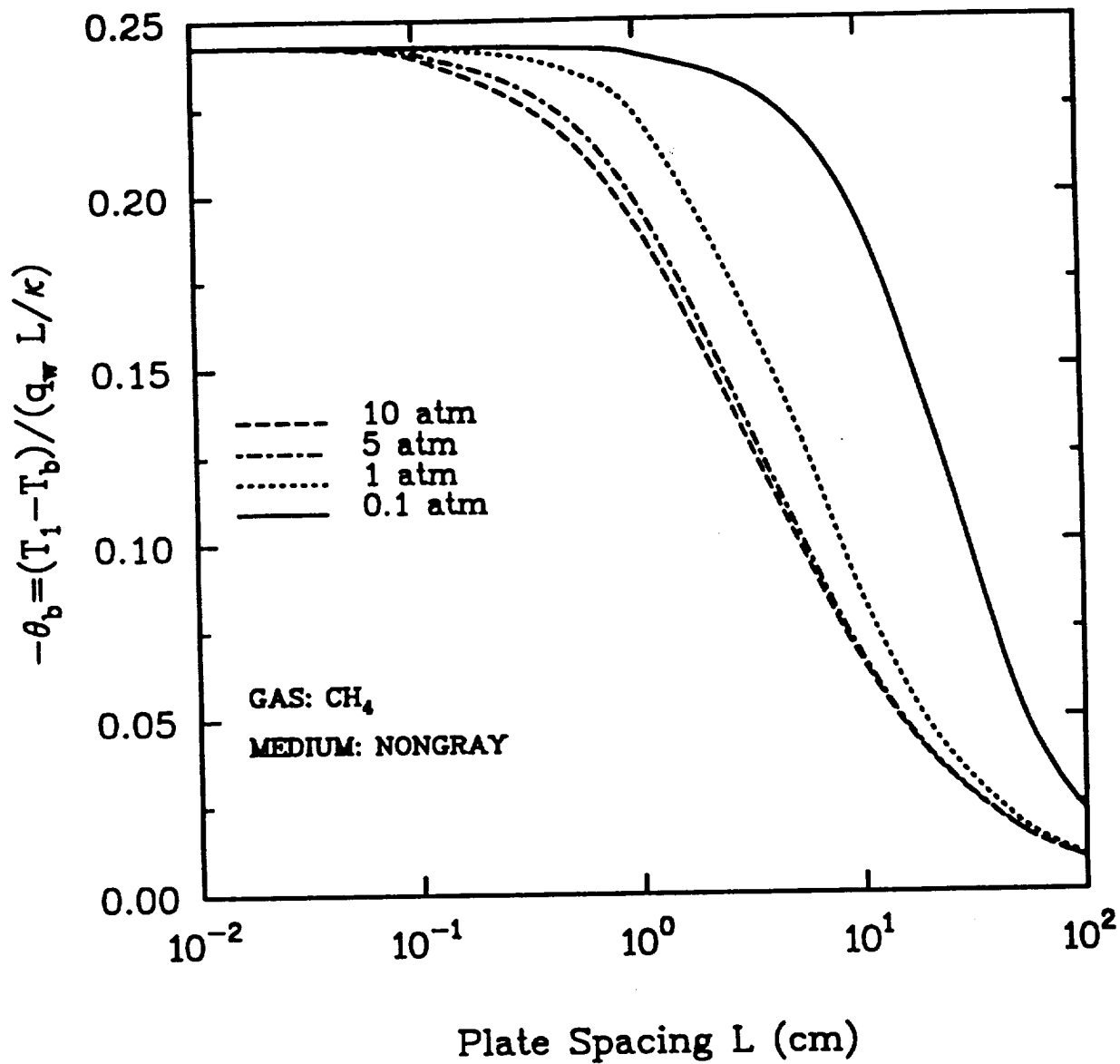


Fig. 6.14(b): LTE results for CH<sub>4</sub>, T<sub>w</sub>=500 K, P=0.1–10 atm



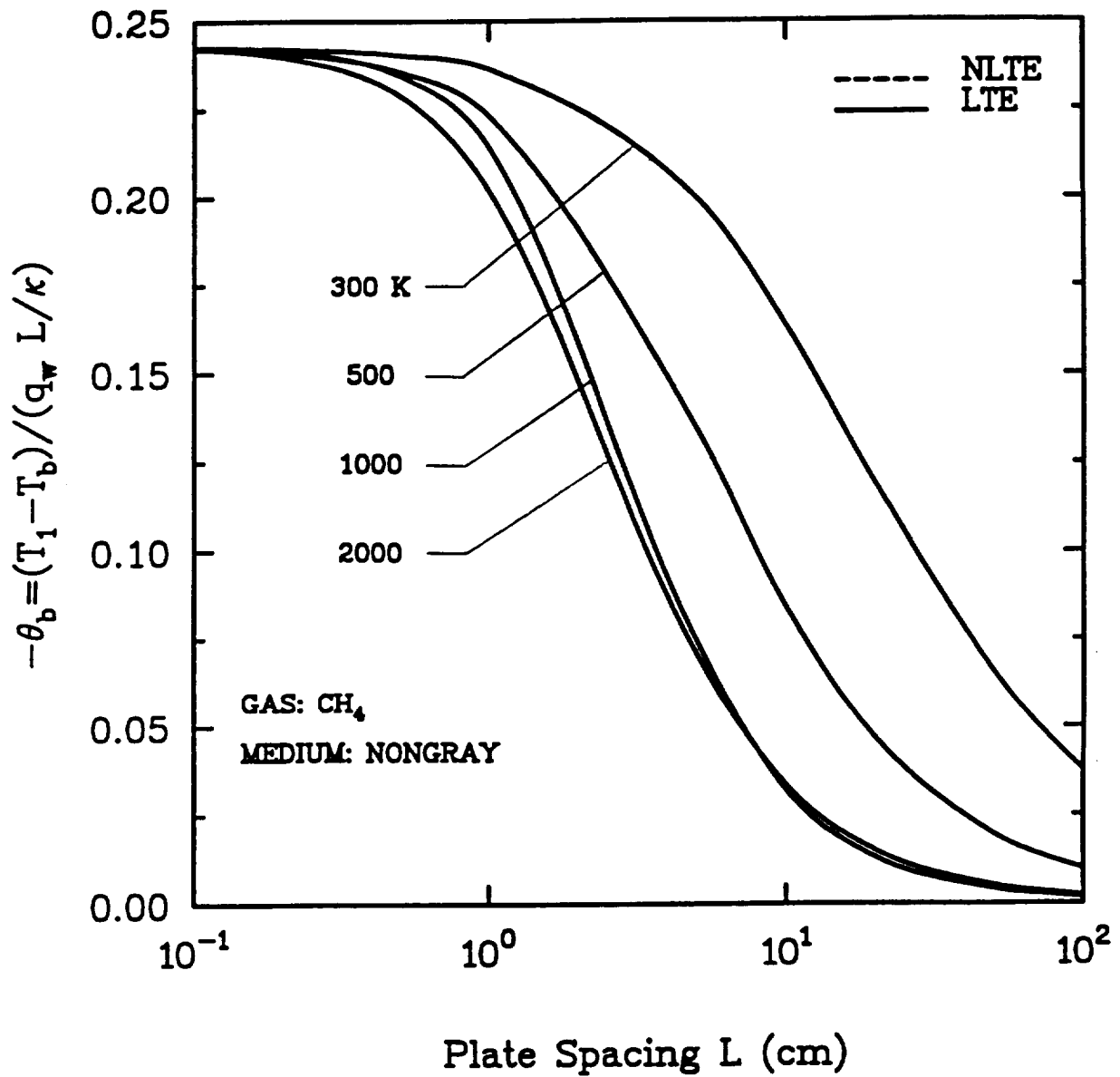


Fig. 6.14(c): LTE and NLTE results for  $\text{CH}_4$ ,  $P=1$  atm,  $T_w=300-2000$  K

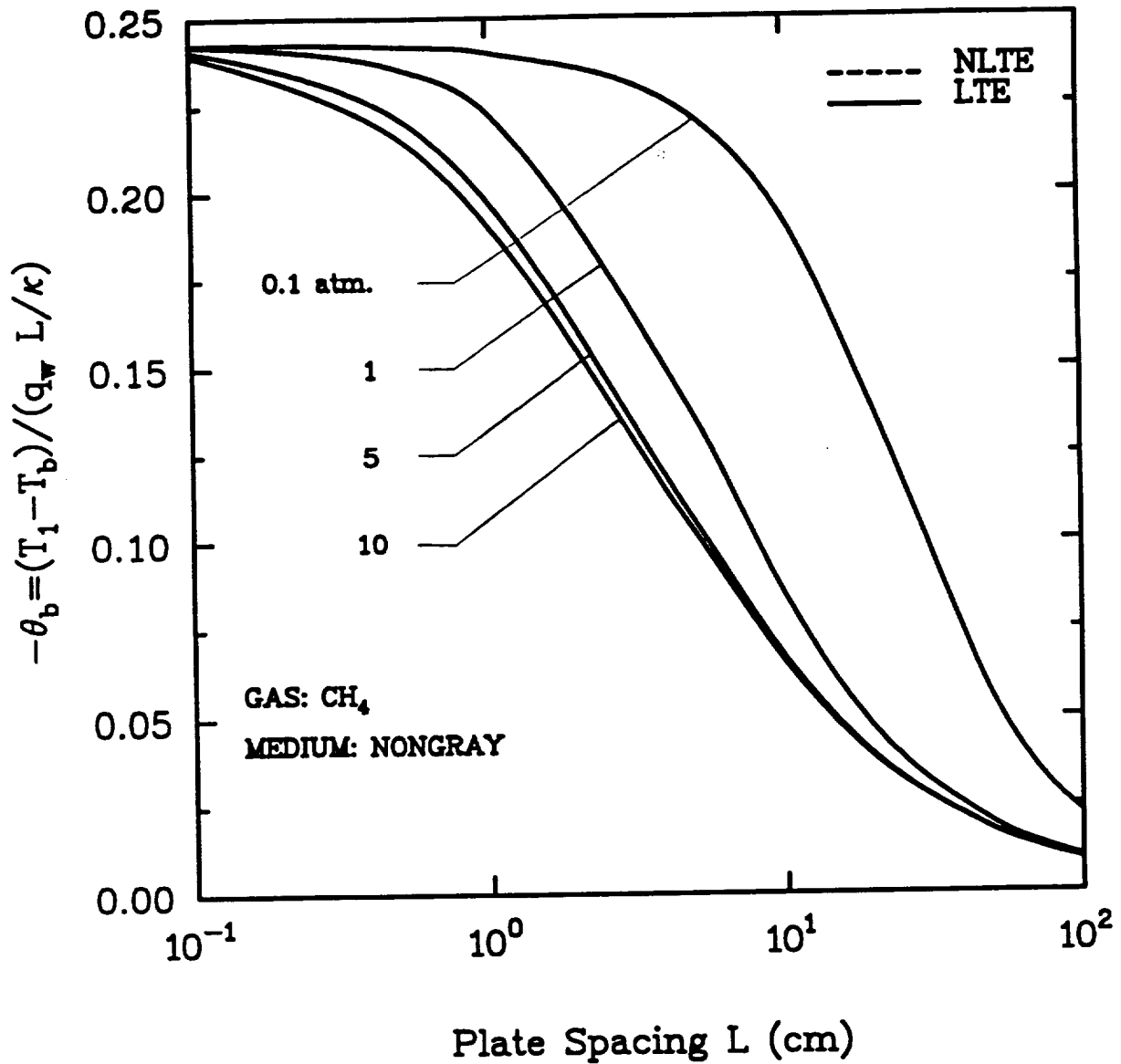


Fig. 6.14(d): LTE and NLTE results for CH<sub>4</sub>, T<sub>w</sub>=500 K, P=0.1-10 atm

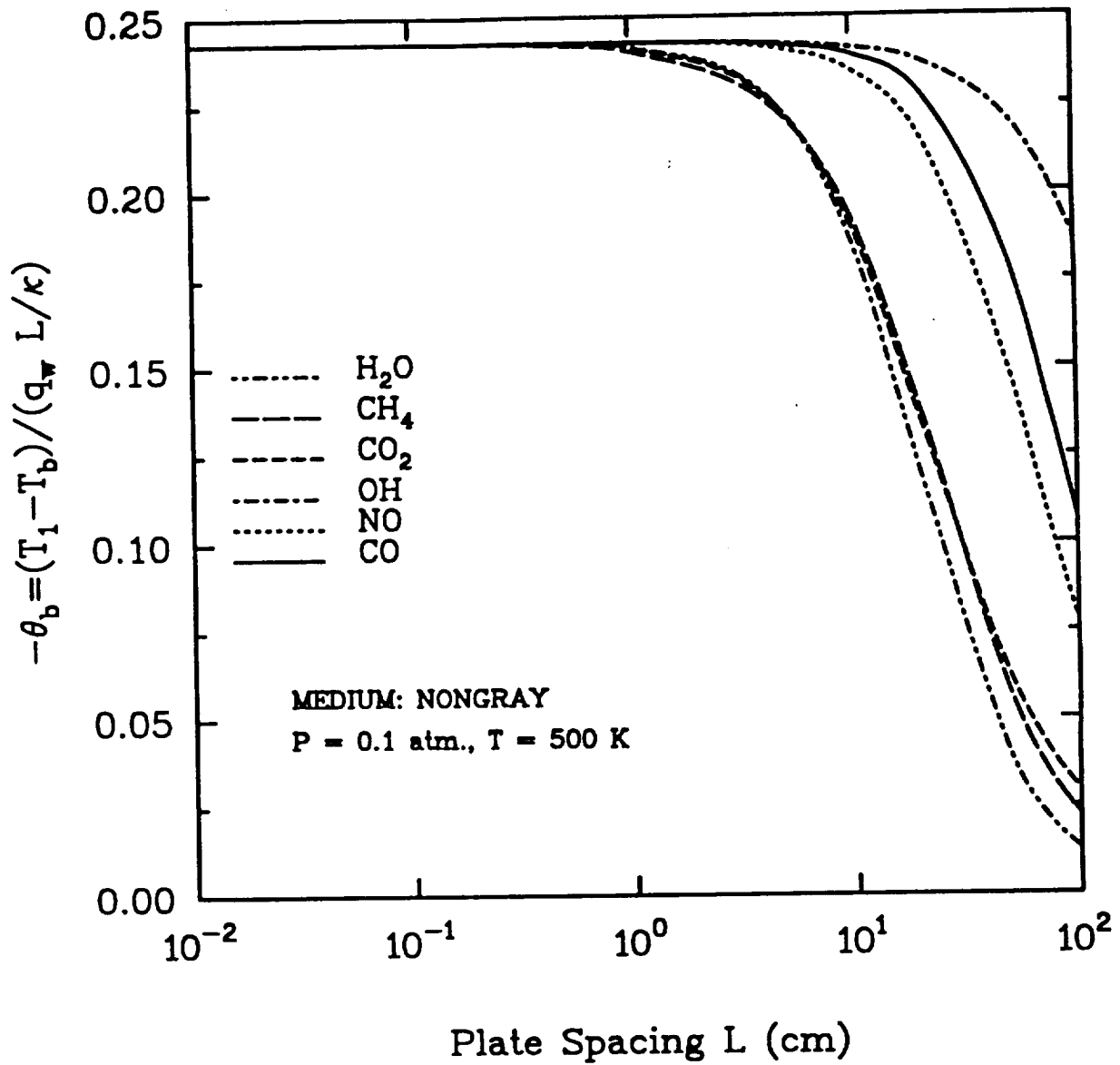


Fig. 6.15: Comparison of NLTE results for different gases

Figure 6.17(a) illustrates comparative results for gray and nongray for NO at four temperatures in the range of 300 to 2000 K and one atmospheric pressure. As seen in the case of CO, the difference between the two results is appreciable and decreases slowly with increasing temperature. Figure 6.17(b) provides the comparison at 500 K and 0.1, 1, and 10 atm. It is seen that the difference between gray and nongray results increases with increasing pressure.

Figures 6.18 through 6.21 present results for OH, CO<sub>2</sub>, H<sub>2</sub>O, and CH<sub>4</sub>, respectively. The results show the same behavior as shown by CO and NO. Thus, it is obvious that the difference between gray and nongray results is very significant at any temperature and pressure. The difference decreases slowly with increasing temperature and increases with increasing pressure. Another interesting observation is that the bulk temperature, under gray gas assumption at any pressure and temperature condition, is lower than that under nongray gas assumption. This means that radiating effect of the species under gray gas assumption is higher than that under nongray assumption, i.e., the gray gas approximation overpredicts the ability of a gas for radiative interaction.

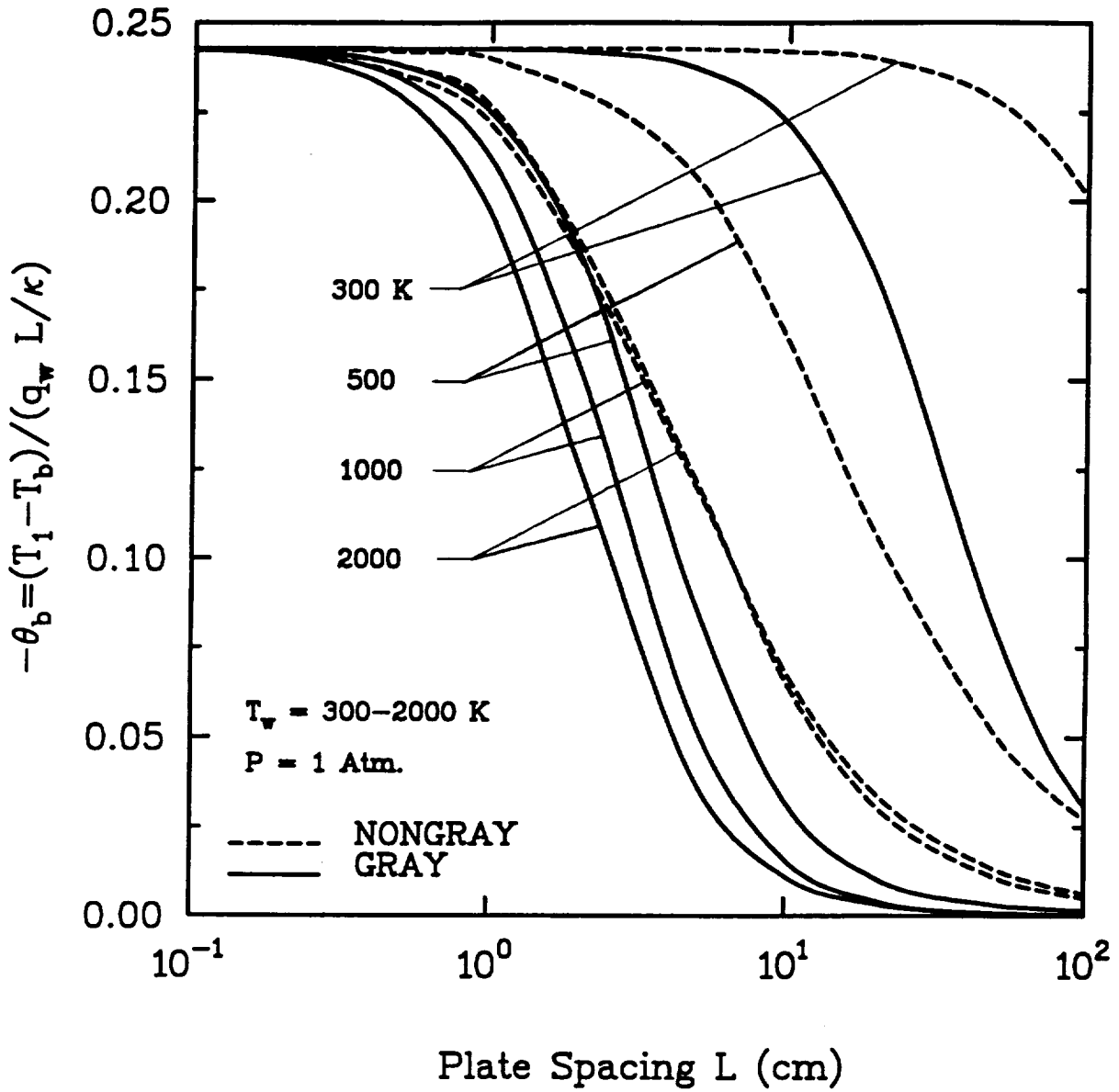


Fig. 6.16(a): Comparison of Gray and Nongray(NLTE) results for CO

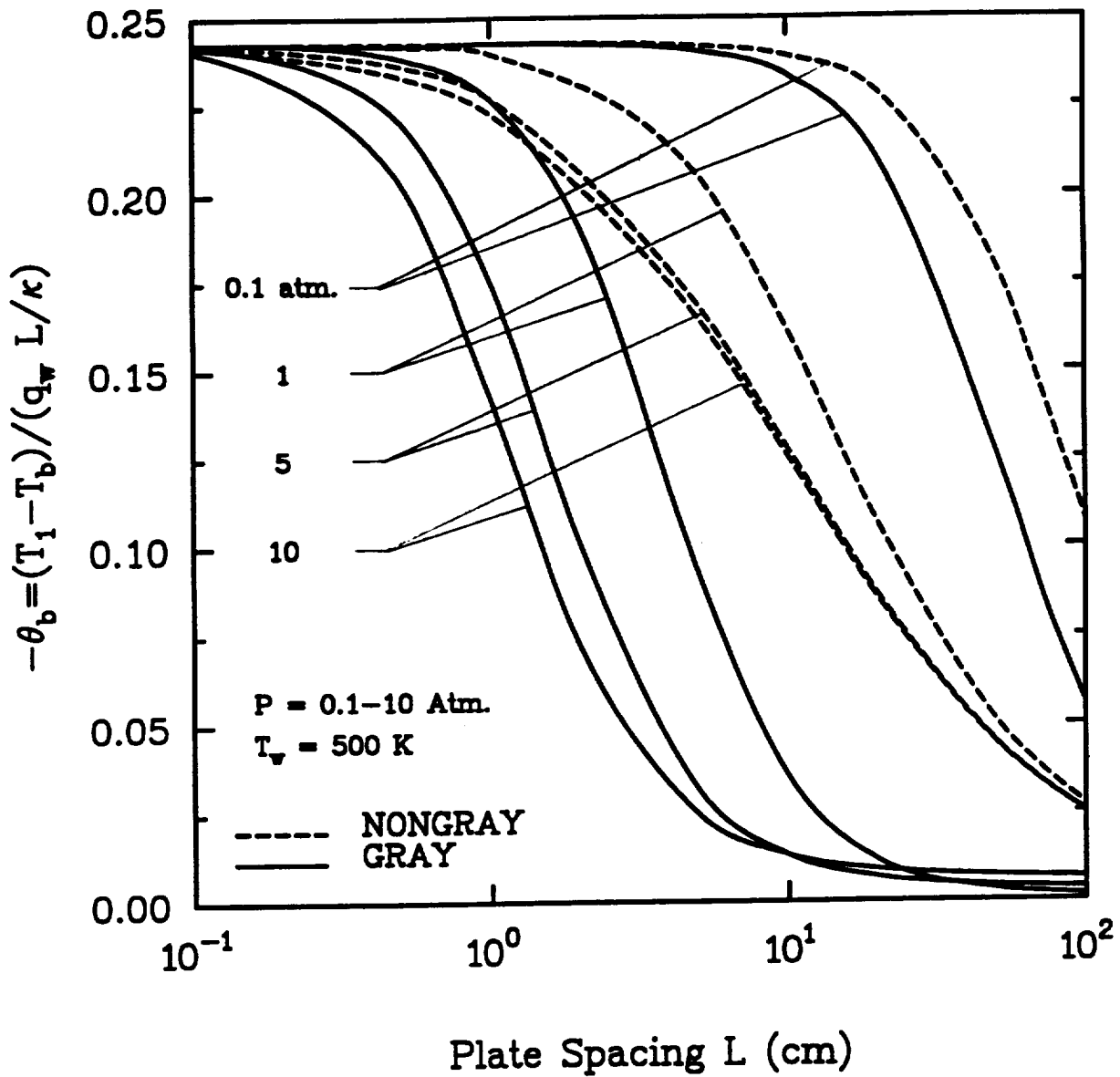


Fig. 6.16(b): Comparison of Gray and Nongray(NLTE) results for CO

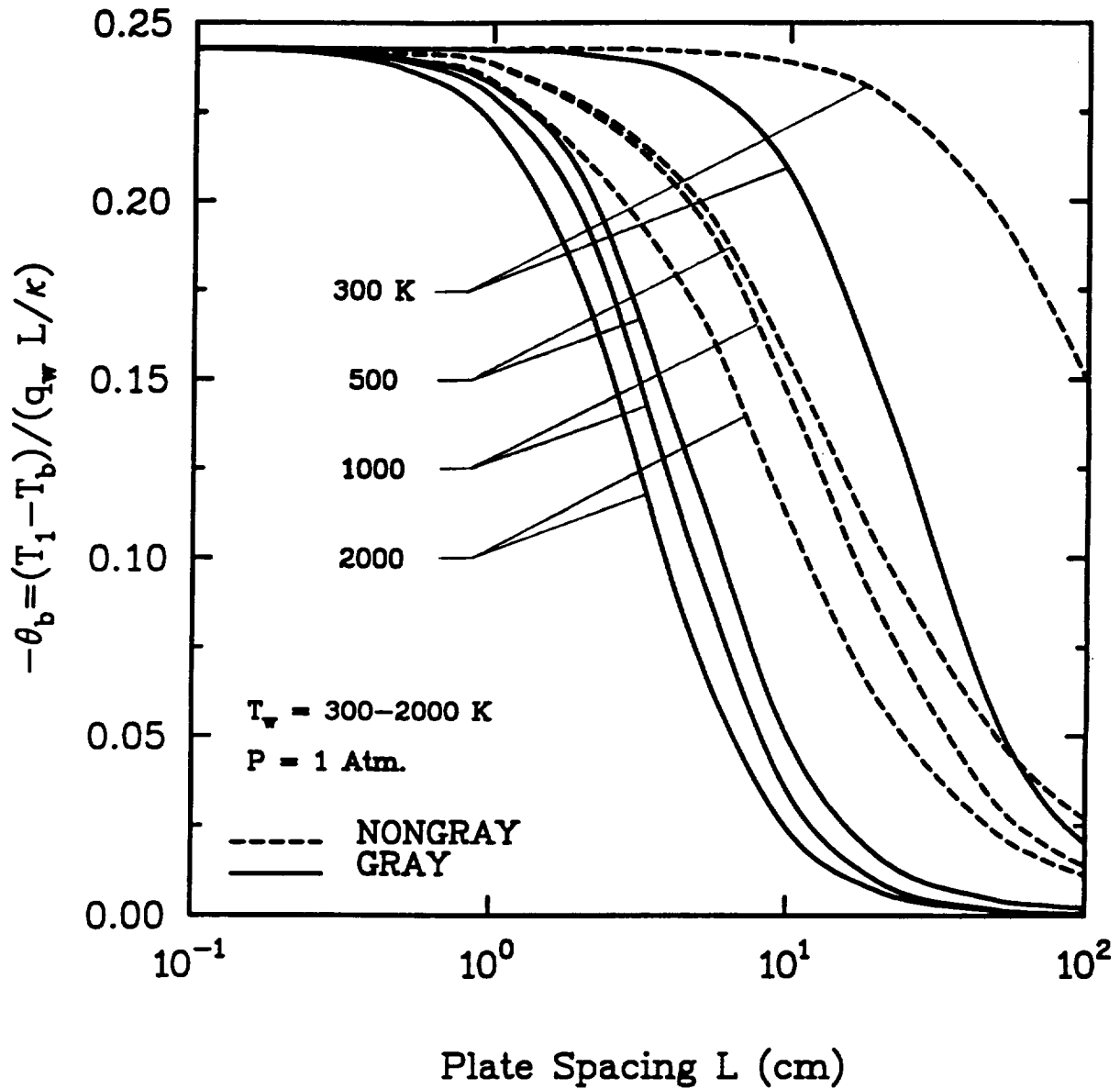


Fig. 6.17(a): Comparison of Gray and Nongray(NLTE) results for NO

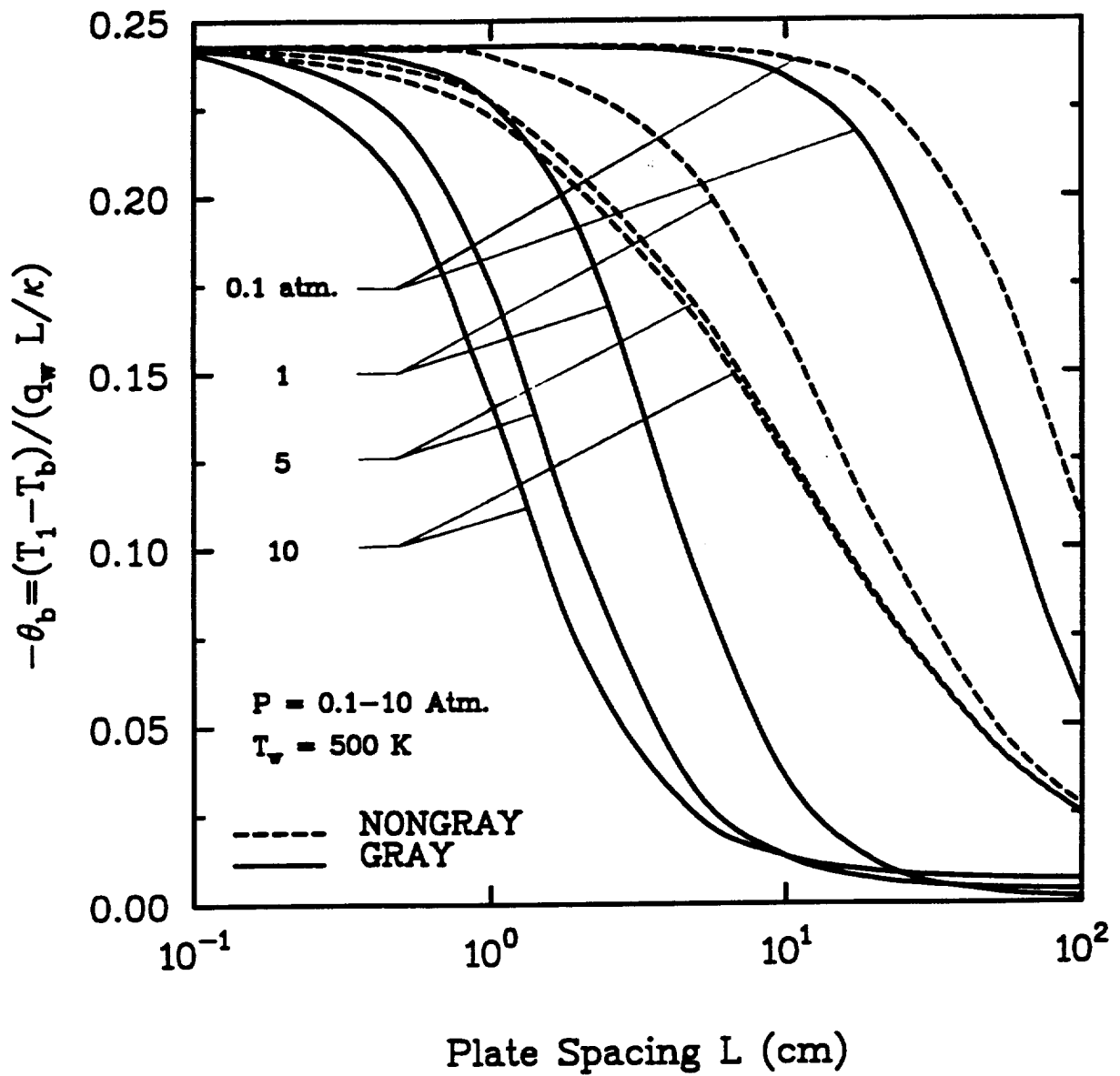


Fig. 6.17(b): Comparison of Gray and Nongray(NLTE) results for NO



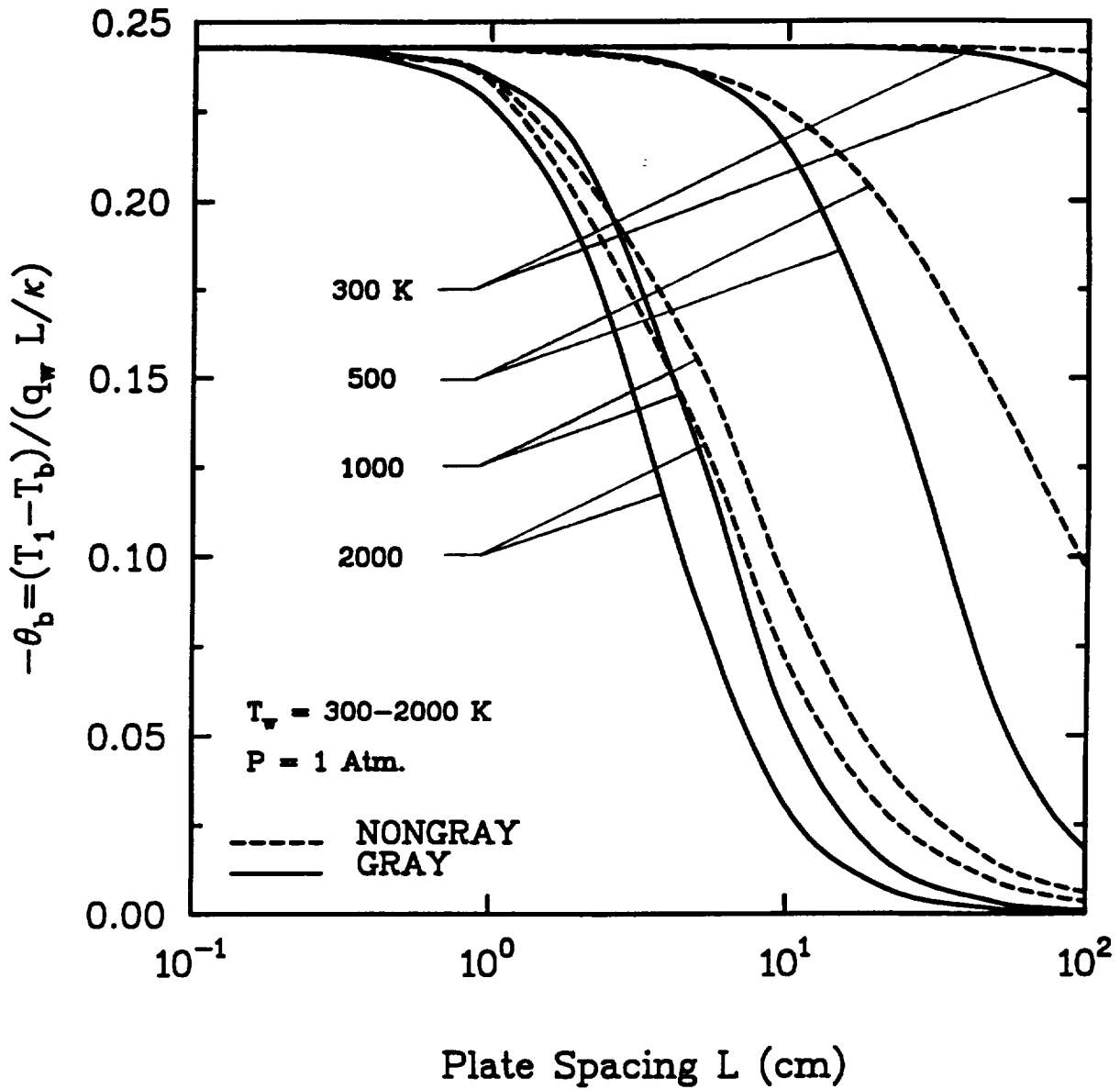


Fig. 6.18(a): Comparison of Gray and Nongray(NLTE) results for OH

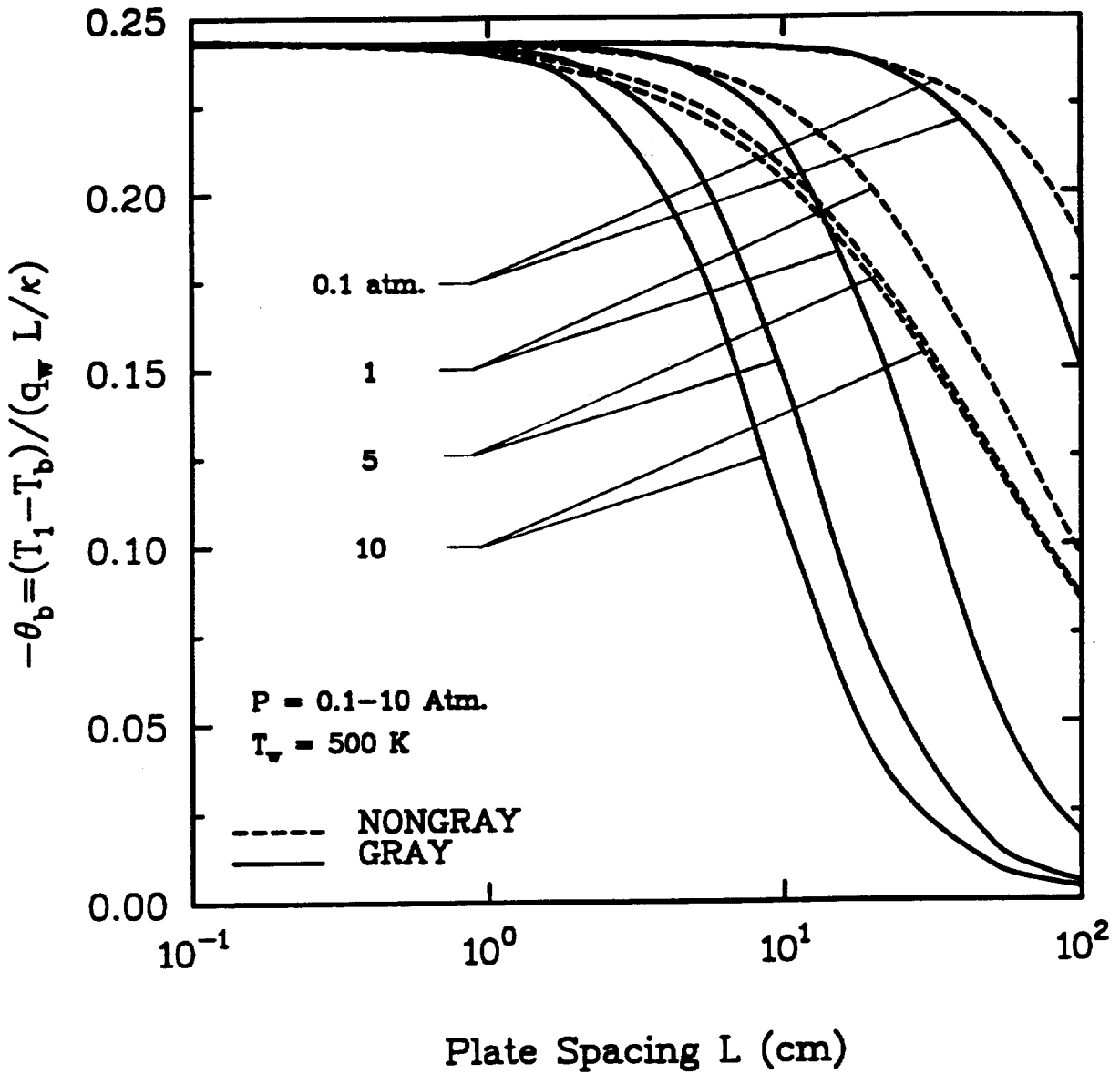


Fig. 6.18(b): Comparison of Gray and Nongray(NLTE) results for OH

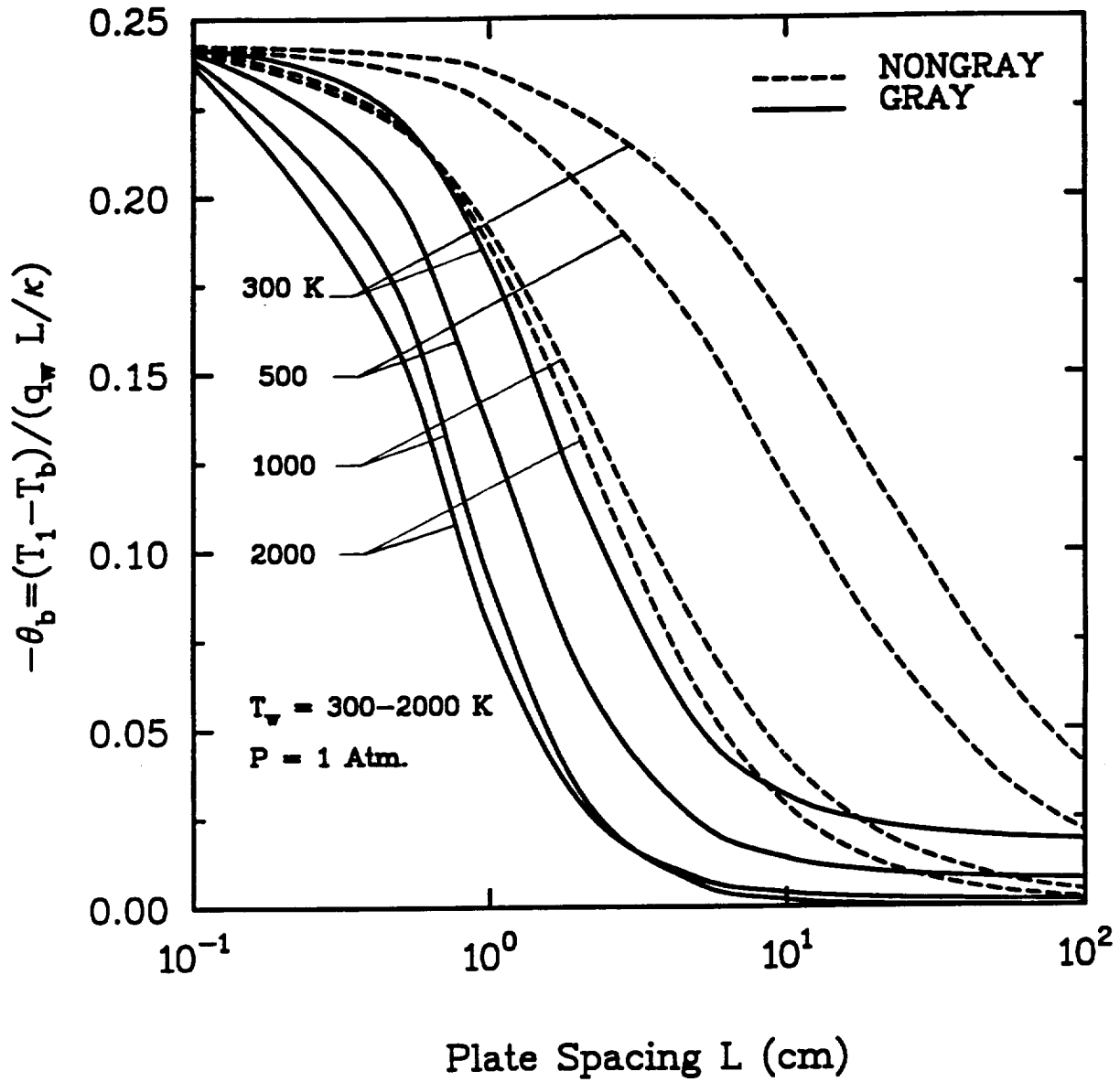


Fig. 6.19(a): Comparison of Gray and Nongray(NLTE) results for CO<sub>2</sub>

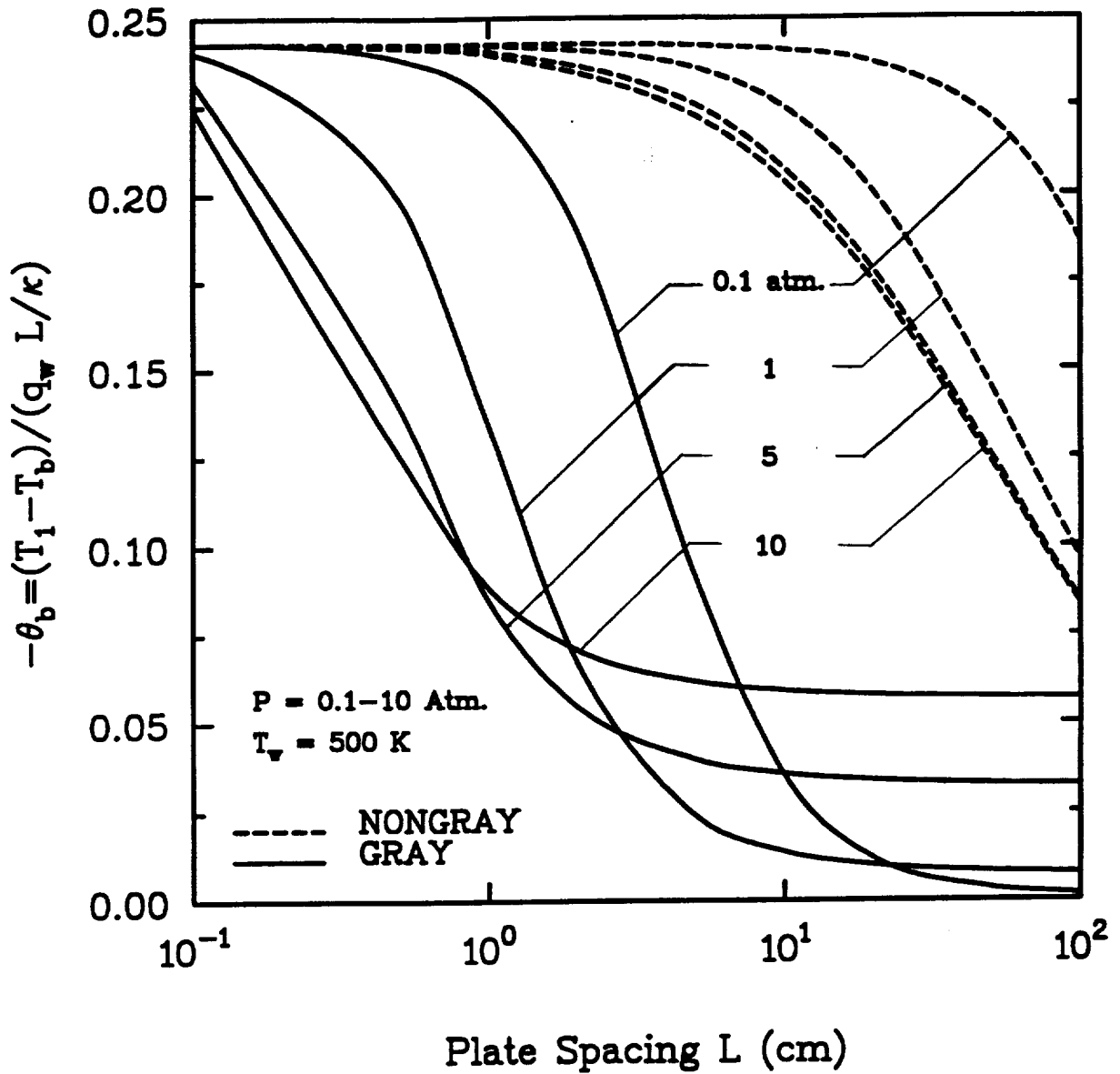


Fig. 6.19(b): Comparison of Gray and Nongray(NLTE) results for CO<sub>2</sub>

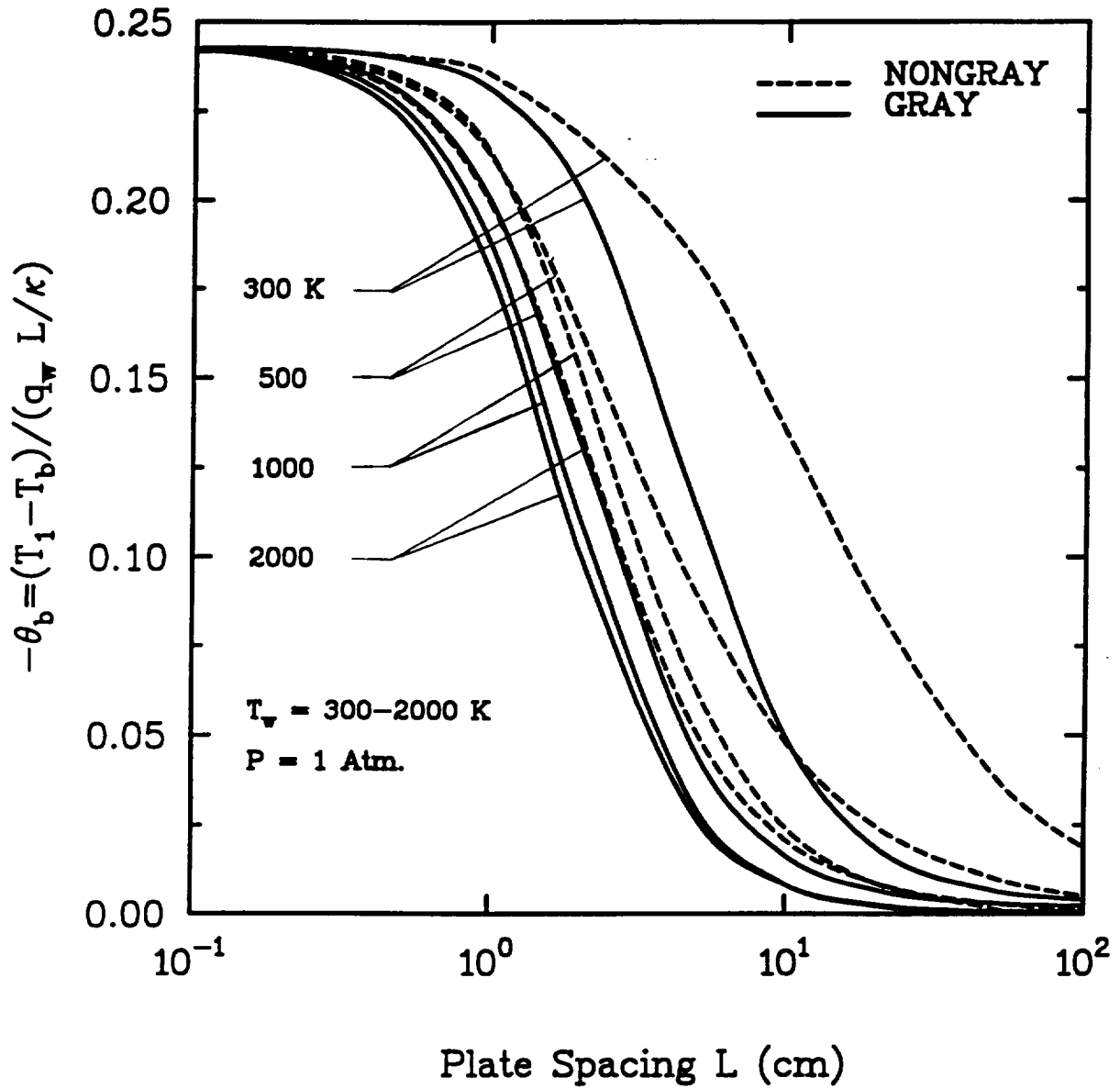


Fig. 6.20(a): Comparison of Gray and Nongray(NLTE) results for H<sub>2</sub>O

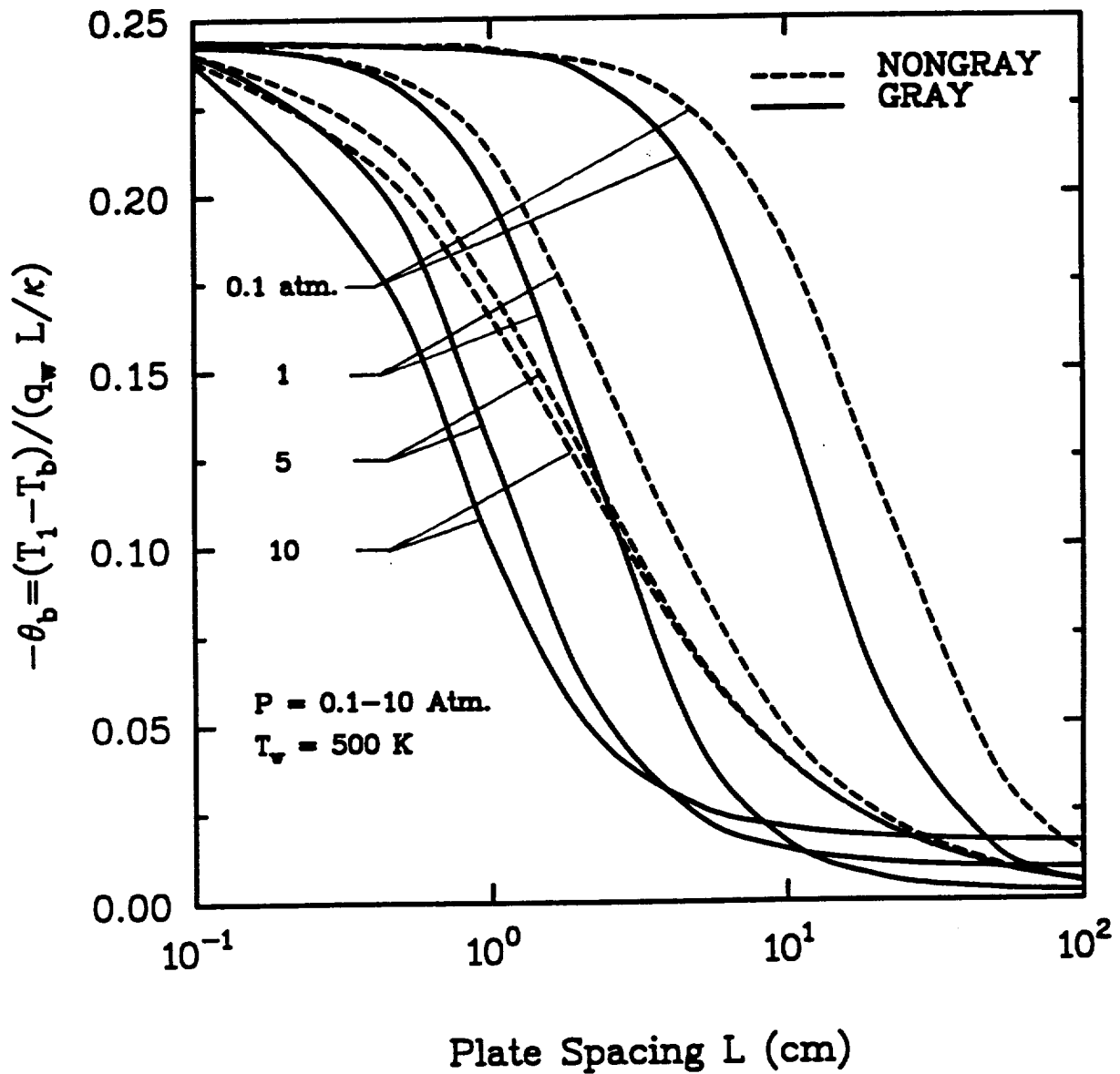


Fig. 6.20(b): Comparison of Gray and Nongray(NLTE) results for H<sub>2</sub>O

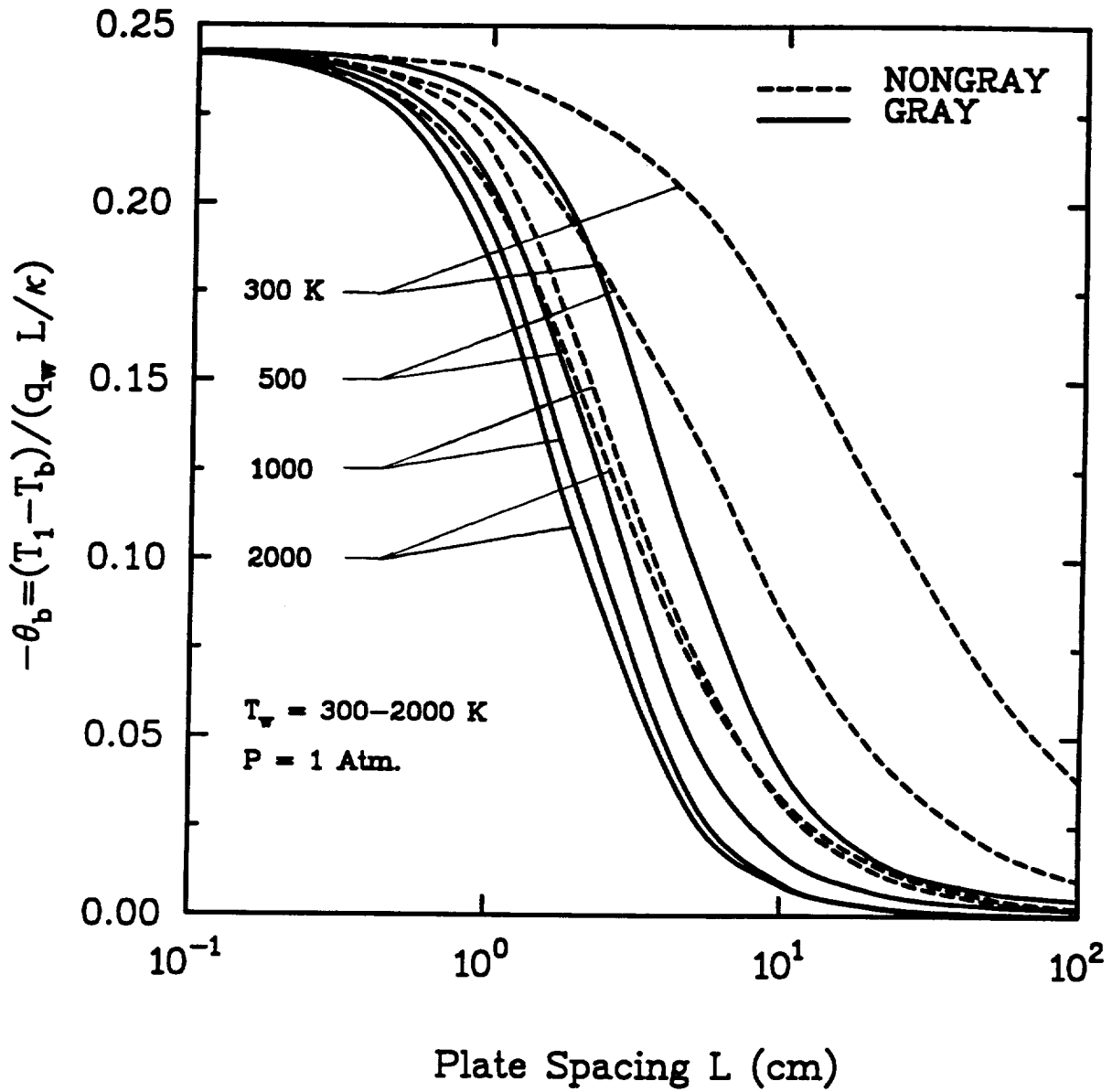


Fig. 6.21(a): Comparison of Gray and Nongray(NLTE) results for CH<sub>4</sub>

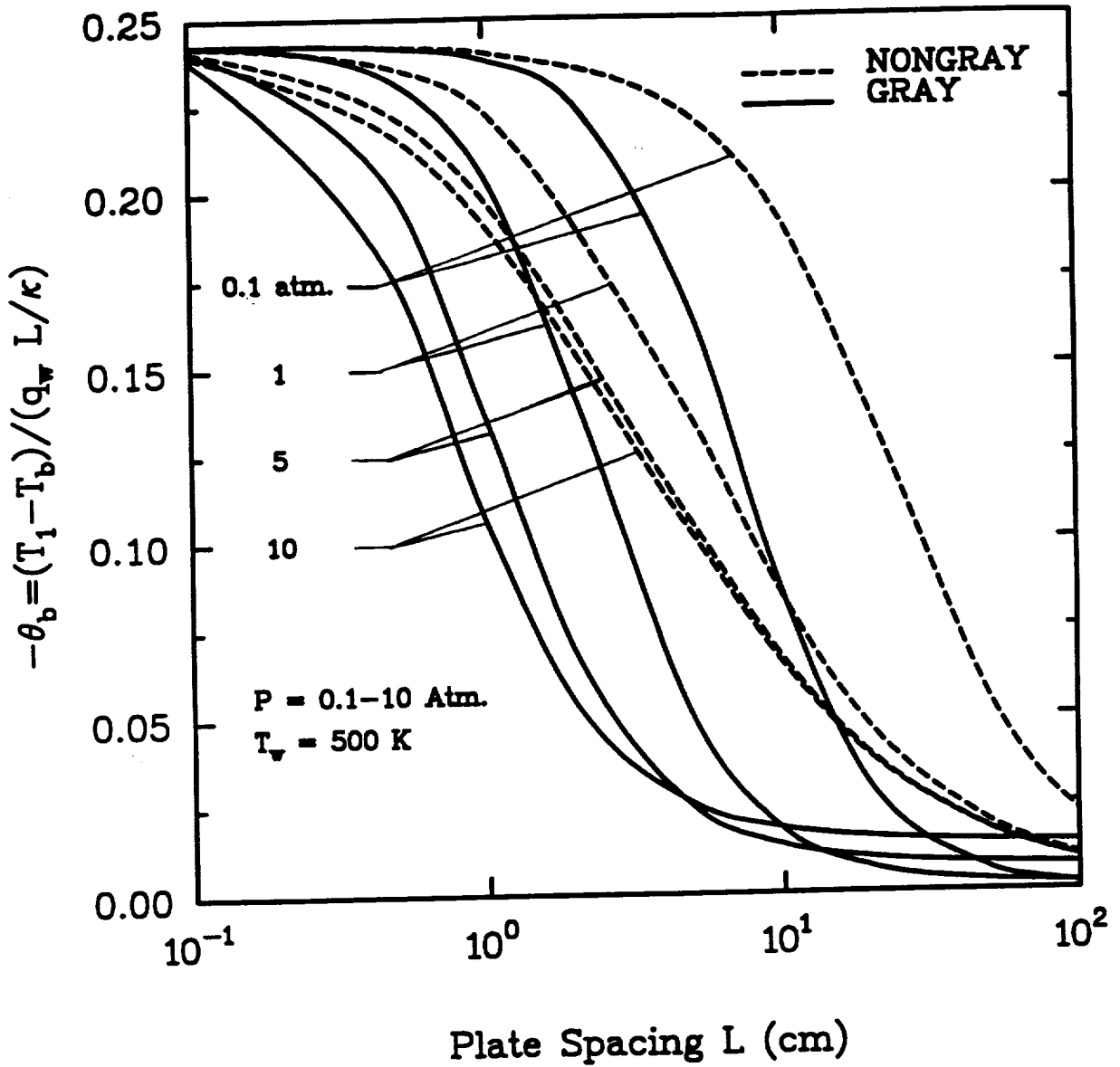


Fig. 6.21(b): Comparison of Gray and Nongray(NLTE) results for CH<sub>4</sub>



## Chapter 7

# CONCLUDING REMARKS

Analytical and numerical procedures have been developed to treat a physical problem when local and nonlocal thermodynamic equilibrium conditions prevail. The NLTE effects have been investigated for some diatomic and polyatomic gases under gray and nongray gas assumptions. The NLTE results under gray and nongray assumption are compared at different temperatures and pressures. The NLTE condition is governed by the NLTE parameter  $\eta$ . For  $\eta = O(1)$ , NLTE prevails and for  $\eta = 0$ , LTE prevails. The bulk temperature is expressed as a function of plate spacing at various temperatures and pressures. The limiting value of bulk temperature is 0.243 which corresponds to negligible radiation.

The results show that, in general, bulk temperature decreases with increasing temperatures, pressures, and plate spacings. This implies that the radiative ability of the gases increases with increasing temperatures, pressures, and plate spacings. The consideration of NLTE effect is important while dealing with diatomic gases. The NLTE effect becomes significant at lower temperatures and pressures. Therefore, it is necessary to take NLTE into account when working temperatures and pressures are moderate. Among the gases, OH shows least radiative effect and H<sub>2</sub>O shows highest radiative effect under both gray and nongray assumption. Polyatomic gases, however, do not show much variation from LTE at any temperature

and pressure. Therefore, NLTE consideration is not important for polyatomic gases. The gray gas approximation overpredicts the ability of a gas for radiative interaction. The method developed can be applied to investigate NLTE effects in other diatomic and polyatomic gases, mixture of gases, and multidimensional problems using sophisticated spectral models for radiation absorption.

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## **APPENDICES**

## APPENDIX A

# INFORMATION ON SPECTROSCOPIC PROPERTIES

To formulate radiative heat transfer problems, it is essential to know the various spectroscopic properties of the gases under consideration. Some relevant information for the gases into consideration is provided here. For a detailed understanding and information, one should refer to [31].

A correlation for the exponential wide band absorptance based on a set of mathematical properties of the total band absorptance was introduced by Tien and Lowder [33], and this is expressed as

$$A = A_0 \ln \left\{ u f(t) \left[ \frac{u + 2}{u + 2f(t)} \right] + 1 \right\} \quad (A.1a)$$

$$u = C_0^2 P Y ; \quad t = \left[ \frac{C_2^2}{4 C_1 C_3} \right] P_e = B^2 P_e \quad (A.1b)$$

$$f(t) = 2.94 [1 - \exp(-2.60t)] \quad (A.1c)$$

The quantities  $u$ ,  $t$ ,  $B^2$ , and  $P_e$  are all dimensionless. The band width parameter  $A_0 = C_3$ , and it is a function of temperature only. The correlation quantity  $C_0^2$  is proportional to  $(C_1/C_3)$ . It can be shown [33] that



$$A_0 C_0^2 = S(T) \quad (A.2)$$

The quantity  $t$  is the line structure parameter, and  $P_e$  is the equivalent ( effective ) broadening pressure and is given by

$$P_e = \left[ \frac{(P_B + bP_A)}{P_0} \right]^n, \quad P_0 = 1 \text{ atm} \quad (A.3)$$

where  $P_A$  is the partial pressure of the absorbing gas,  $P_B$  is the partial pressure of the broadening gas, and  $b$  is the self-broadening power of the molecule  $A$  with respect to molecule  $B$  ( $N_2$  in all cases here ). The pressure parameter,  $n$ , which is always less than or equal to unity, accounts for the partial overlapping of bands with different lower states [35]. The quantities  $b$  and  $n$  are obtained experimentally by using various gas compositions.

By using the information on  $C_1$ ,  $C_2$ , and  $C_3$ , the quantities  $A_0$ ,  $C_0^2$ , and  $B^2$  were evaluated and expressed in the units employed here. These are given in Table A.1. The procedure for converting the correlation constants  $C_1$ ,  $C_2$ , and  $C_3$  from the data of Edwards et al. [35] into the relations and units of quantities  $A_0$ ,  $C_0^2$ , and  $B^2$  is discussed in [31].

**Table A.1 Exponential Band Model Correlation Quantities \***

Molecule	Band $\mu$	Band Center $\text{cm}^{-1}$ $\omega_c$	Pressure Parameters		$A_0(T)$ $\text{cm}^{-1}$	$C_0^2(T)$ $\text{atm}^{-1} \text{cm}^{-1}$	$B^2(T)$ dimensionless
			b	n			
CO	4.7	2143	1.1	0.8	$38.1 k_1(T)$	$6.24 k_2(T)$	$0.314 \delta_1(T)$
	2.35	4260	1.0	0.8	$38.1 k_1(T)$	$0.024 k_2(T)$	$0.300 \delta_1(T)$
NO	5.3	1876	1.0	0.65	$36.0 k_1(T)$	**	**
	2.7	3724	1.0	0.65	$36.0 k_1(T)$		
OH	2.8	3570	**	**	$117 k_1(T)$	**	**
	1.4	6974			$117 k_1(T)$		
CO <sub>2</sub>	15	667	1.3	0.7	$22.3 k_1(T)$	$15.2 k_2(T)$	$0.084 k_1(T)$
	4.3	2350	1.3	0.8	$19.9 k_1(T)$	$98.7 k_2(T)$	$0.329 k_1(T)$
	2.7	3715	1.3	0.65	$41.6 k_1(T)$	$1.72 k_2(T)$ $\phi_2(T)$	$0.111 \delta_2(T)$
H <sub>2</sub> O	I.R	500	5.0	1.0	$49.4 k_1(T)$	$771 k_2(T)$ $\phi_7(T)$	$0.073/k_1(T)$
	6.3	1600	5.0	1.0	$90.1 k_1(T)$	$3.35 k_2(T)$	$0.130/k_1(T)$
	2.7	3750	5.0	1.0	$112.6 k_1(T)$	$1.52 k_2(T)$	$0.145/k_1(T)$
	1.87	5350	5.0	1.0	$79.7 k_1(T)$	$0.276 k_2(T)$ $\phi_{011}(T)$	$0.118/k_1(T)$
	1.38	7250	5.0	1.0	$79.7 k_1(T)$	$0.230 k_2(T)$ $\phi_{101}(T)$	$0.201/k_1(T)$
CH <sub>4</sub>	7.6	1310	1.3	0.8	$39.8 k_1(T)$	$4.58 k_2(T)$	$0.067 k_1(T)$
	3.3	3020	1.3	0.8	$95.3 k_1(T)$	$3.15 k_2(T)$	$0.036 k_1(T)$

\* Notes on table A.1:

1. Notations:  $k_1(T) = (T/300)^{1/2}$ ,  $k_2(T) = (300/T)^{1/2}$ ,  $\delta_1 = [ \phi_1^2(T)/k_1(T) ] \times 10^{-3}$ ,

$$\delta_2 = \phi_3^2(T) / [ \phi_2(T) k_1(T) ]$$

$$h = 6.625 \times 10^{-27} \text{ erg-sec}, c = 2.998 \times 10^{10} \text{ cm/sec}, \kappa = 1.380 \times 10^{-16} \text{ erg/K},$$

$$hc/\kappa = 1.44 \text{ cm-K}$$

2. For CO:  $\omega = 2143 \text{ cm}^{-1}$ ,  $\phi_1(T) = [ 15.15 + 0.22 (T/T_0)^{3/2} ] [ 1 - \exp(-hc\omega/\kappa T) ]$ ,

$$T_0 = 100 \text{ K}, S(T_{01}) = 289 \pm 30 \text{ cm}^{-2}\text{-atm}^{-1}, T_{01} = 300 \text{ K}, \eta_r = 0.0297 \text{ seconds.}$$

3. For NO:  $\omega = 1876 \text{ cm}^{-1}$ ,  $S(T_{01}) = 132 \text{ cm}^{-2}\text{-atm}^{-1}$ ,  $T_{01} = 300 \text{ K}$ ,  $\eta_r = 0.07 \text{ secs.}$

4. For OH:  $\omega = 3570 \text{ cm}^{-1}$ ,  $S(T_{01}) = 110 \text{ cm}^{-2}\text{-atm}^{-1}$ ,  $T_{01} = 300 \text{ K}$ ,  $\eta_r = 0.0232 \text{ secs.}$

5. For CO<sub>2</sub>:  $\omega_1 = 1351 \text{ cm}^{-1}$ ,  $\omega_2 = 667 \text{ cm}^{-1}$ ,  $\omega_3 = 2396 \text{ cm}^{-1}$

$$\phi_2(T) = \{ 1 - \exp [ (-hc/\kappa T) (\omega_1 + \omega_3) ] \} \times \{ [ 1 - \exp(-hc\omega_1/\kappa T) ] [ 1 - \exp(-hc\omega_3/\kappa T) ] \}^{-1},$$

$$\phi_3(T) = 1 + 0.053 (T/300)^{3/2}, S_1(T_{01}) = 362 \pm 90, S_2(T_{01}) = 2970, S_3(T_{01}) = 67 \text{ cm}^{-2}\text{-atm}^{-1},$$

$$T_{01} = 300 \text{ K}, \eta_{1r} = 0.215 \text{ secs.}, \eta_{2r} = 0.0022 \text{ secs.}, \eta_{3r} = 0.0846 \text{ secs.}$$

6. For H<sub>2</sub>O:  $\omega_1 = 3652 \text{ cm}^{-1}$ ,  $\omega_2 = 1595 \text{ cm}^{-1}$ ,  $\omega_3 = 3756 \text{ cm}^{-1}$ ,  $\phi_{v_1v_2v_3}(T) = \{ 1 - \exp [ -hc(v_1\omega_1 + v_2\omega_2 + v_3\omega_3)/\kappa T ] \} \times \{ [ 1 - \exp(-hc\omega_2/\kappa T) ] [ 1 - \exp(-hc\omega_3/\kappa T) ] \}^{-1}$ ,

$$\phi_7(T) = \exp [ -17.6 (T/100)^{-1/2} ], S_1(T_{01}) = 1840, S_2(T_{01}) = 300 \pm 60, S_3(T_{01}) = 200 \pm 20 \text{ cm}^{-2}\text{-atm}^{-1},$$

$$T_{01} = 300 \text{ K}, \eta_{2r} = 0.0468 \text{ secs.}, \eta_{3r} = 0.0127 \text{ secs.}$$

6. For CH<sub>4</sub>:  $\omega_1 = 1310 \text{ cm}^{-1}$ ,  $\omega_2 = 3020 \text{ cm}^{-1}$ ,  $S_1(T_{01}) = 185, S_2(T_{01}) = 320, \text{ cm}^{-2}\text{-atm}^{-1},$   
 $T_{01} = 300 \text{ K}, \eta_{1r} = 0.113 \text{ secs.}, \eta_{2r} = 0.0122 \text{ secs.}$

\*\* The information is not available in literature, and therefore suitable assumptions were made to calculate those quantities.

- For additional informations, one should refer to [31].

## APPENDIX B

### SOLUTION PROCEDURE FOR GRAY NLTE FORMULATION

In this appendix, solution procedure for gray gas analysis under NLTE assumption is provided.

The radiative flux equation for the present study is given by Eq. (3.44). Using the following relations

$$\int_0^{\infty} B_{1\omega} d\omega = B_1 = e_1 = \sigma T_1^4 \quad (B.1)$$

$$\int_0^{\infty} B_{2\omega} d\omega = B_2 = e_2 = \sigma T_2^4 \quad (B.2)$$

$$\int_0^{\infty} J_{\omega}(z) d\omega = J(z) = \frac{e(z)}{\pi} + \frac{1}{2} \eta \bar{H}(z) \quad (B.3)$$

where

$$H(z) = \frac{-\frac{dq_R}{dz}}{2\pi PS(T)} \quad (B.4)$$

and substituting Eq. (3.40) in Eq. (3.44), one obtains

$$q_R = \sigma T_1^4 \exp(-b\tau) - \sigma T_2^4 \exp[(-b\tau_0 - \tau)]$$

$$\begin{aligned}
& + \frac{3}{2} \left\{ \int_0^{\tau} e(t) \exp[-b(\tau - t)] dt - \int_{\tau}^{\tau_0} e(t) \exp[-b(t - \tau)] dt \right\} \\
& - \frac{3}{8} \eta \left\{ \int_0^{\tau} \frac{dq_R}{dt} \exp[-b(\tau - t)] dt - \int_{\tau}^{\tau_0} \frac{dq_R}{dt} \exp[-b(t - \tau)] dt \right\} \times \frac{1}{PS(T)} \quad (B.5)
\end{aligned}$$

Equation (B.5) can be rewritten as

$$q_R(\tau) = q_{RL}(\tau) + q_{RN}(\tau) \quad (B.6)$$

where  $q_{RL}(\tau)$  and  $q_{RN}(\tau)$  are defined as in Eqs. (3.49a) and (3.53a) respectively. Differentiating Eq. (B.6) twice using Leibnitz formula, one obtains

$$\frac{d^2 q_R}{d\tau^2} = \frac{d^2 F}{d\tau^2} + 2\Gamma \frac{d\Gamma^4}{d\tau} + \Gamma b^2(I) - 2KS \frac{d^2 q_R}{d\tau^2} - KS b^2(II) \quad (B.7a)$$

where 
$$I = \int_0^{\tau} T^4(t) \exp[-b(\tau - t)] dt - \int_{\tau}^{\tau_0} T^4(t) \exp[-b(t - \tau)] dt \quad (B.7b)$$

$$II = \int_0^{\tau} \frac{dq_R}{dt} \exp[-b(\tau - t)] dt - \int_{\tau}^{\tau_0} \frac{dq_R}{dt} \exp[-b(t - \tau)] dt \quad (B.7c)$$

and  $F(\tau)$ ,  $b$ ,  $\Gamma$ , and  $KS$  are defined as in Eqs. (3.49b), (3.49c), and (3.53b) respectively. the quantity  $I$  can be obtained from Eq. (3.49a) as

$$I = \frac{q_{RL}(\tau) - F(\tau)}{\Gamma} \quad (B.8a)$$

Similarly, the quantity  $II$  can be obtained from Eq. (3.53a) as

$$II = -\frac{q_{RN}}{KS} \quad (B.8b)$$

Substituting Eqs. (B.8a) and (B.8b) in Eq. (B.7a), there is obtained

$$M_2 \frac{d^2 q_R}{dt^2} - \frac{9}{4} q_R = 3\sigma \frac{dT^4}{dt} \quad (B.9)$$

which is Eq. (3.55a), and  $M_2$  is defined as in Eq. (3.55b).

## APPENDIX C

### SOLUTION PROCEDURE FOR NONGRAY NLTE FORMULATION

In this appendix, some important steps to solve the nongray NLTE equation, Eq. (5.13), are given.

Substituting Eq. (5.10) in 5.(13), one obtains

$$\begin{aligned}
 & a_1(1 - 6\xi^2 + 4\xi^3) + a_2(2\xi - 6\xi^2 + 4\xi^3) - 2(3\xi^2 - 2\xi^2 - 2\xi^3) + 1 = \\
 & \frac{3}{2} \left( \frac{L}{\kappa} \right) H u_0 \left[ \int_0^\xi \theta(\xi') \bar{A}'(I) d\xi' - \int_\xi^1 \theta(\xi') \bar{A}'(II) d\xi' \right] \\
 & - \frac{3}{8} \eta \left[ \int_0^\xi \left( 1 + \frac{d^2\theta}{d\xi'^2} \right) \bar{A}'(I) d\xi' - \int_\xi^1 \left( 1 + \frac{d^2\theta}{d\xi'^2} \right) \bar{A}'(II) d\xi' \right] \quad (C1)
 \end{aligned}$$

where  $\bar{A}'(I)$  and  $\bar{A}'(II)$  are defined as Eq. (5.3b).

Solving Eq. (B1) at  $\xi = 0$ , and assuming a multiband species, there is obtained

$$a_1 a_1 + a_2 a_2 = a_0 \quad (C2)$$

where

$$a_0 = \left(\frac{3}{8}\eta c R_0 - 1\right) \quad (C3)$$

$$a_1 = 1 + \left[\left(\frac{L}{\kappa}\right)H_1(cR_1 - 2c^3R_3 + c^4R_4)\right] - \left[\left(\frac{9}{2}\right)\eta(c^3R_2 - c^2R_1)\right] \quad (C4)$$

$$a_2 = \left[\left(\frac{L}{\kappa}\right)H_1(c^2R_2 - 2c^3R_3 + c^4R_4)\right] - \left[\left(\frac{3}{4}\right)\eta(cR_0 - 6c^2R_1 + 6c^3R_2)\right] \quad (C5)$$

where  $c = 2/(3 u_0)$ ,  $b = 1/u$ , and  $R_i$ 's are integral functions defined as

$$R_0 = \int_0^b \bar{A}'(u) du \quad (C6)$$

$$R_1 = \int_0^b u \bar{A}'(u) du \quad (C7)$$

$$R_2 = \int_0^b u^2 \bar{A}'(u) du \quad (C8)$$

$$R_3 = \int_0^b u^3 \bar{A}'(u) du \quad (C9)$$

$$R_4 = \int_0^b u^4 \bar{A}'(u) du \quad (C10)$$

In a similar manner, solving at  $\xi = 1/4$ , one obtains

$$a_1 a_3 + a_2 a_4 = a_5 \quad (C11)$$

where

$$a_3 = \left\{ \left(\frac{L}{\kappa}\right)H_1 \left[ \left(\frac{57}{256}\right)S_1 + \left(\frac{11}{16}\right)c(S_2 + S_3) - \left(\frac{9}{8}\right)c^2S_4 - c^3(S_5 + S_6) + c^4S_7 \right] \right\} +$$



$$\left\{ \left(\frac{3}{8}\right)\eta\left[\left(\frac{9}{4}\right)cS_1 + 6c^2(S_2 + S_3) - 12c^3S_4\right] \right\} + \frac{11}{16} \quad (C12)$$

$$\alpha_4 = \left\{ \left(\frac{L}{\kappa}\right)H_1\left[\left(\frac{9}{256}\right)S_1 + \left(\frac{3}{16}\right)c(S_2 + S_3) - \left(\frac{1}{8}\right)c^2S_4 - c^3(S_5 + S_6) + c^4S_7\right] \right\} + \left\{ \left(\frac{3}{8}\right)\eta\left[\left(\frac{1}{4}\right)cS_1 + 6c^2(S_2 + S_3) - 12c^3S_4\right] \right\} + \frac{3}{16} \quad (C13)$$

$$\alpha_5 = \left\{ \left(\frac{3}{8}\right)\eta c \right\} S_1 - \frac{11}{16} \quad (C14)$$

and  $S_i$ 's are integral functions defined as

$$S_1 = \int_{b/4}^{3b/4} \bar{A}'(u) du \quad (C15)$$

$$S_2 = \int_0^{b/4} u \bar{A}'(u) du \quad (C16)$$

$$S_3 = \int_0^{3b/4} u \bar{A}'(u) du \quad (C17)$$

$$S_4 = \int_{b/4}^{3b/4} u^3 \bar{A}'(u) du \quad (C18)$$

$$S_5 = \int_0^{b/4} u^3 \bar{A}'(u) du \quad (C19)$$

$$S_6 = \int_0^{3b/4} u^3 \bar{A}'(u) du \quad (C20)$$

$$S_7 = \int_{b/4}^{3b/4} u^4 \bar{A}'(u) du \quad (C21)$$

Thus, the constants  $a_1$  and  $a_2$  can be evaluated by solving Eqs. (C2) and (C11)

$$a_1 = \frac{\alpha_0 \alpha_4 - \alpha_2 \alpha_5}{DEN} \quad (C22a)$$

$$a_2 = \frac{\alpha_0 \alpha_3 - \alpha_2 \alpha_5}{-DEN} \quad (C22b)$$

where  $DEN = \alpha_4 \alpha_1 - \alpha_2 \alpha_3$  (C22c)

Once  $a_1$  and  $a_2$  are evaluated, the solution for bulk temperature,  $\theta_{bp}$  is given by Eq. (5.11).

For additional information, one should refer to [32].

**APPENDIX D**

**SELECTED COMPUTER PROGRAMS  
AND RESULTS**

In this appendix, computer programs for all the gases are presented which were used to obtain the results. Two general programs are provided which can solve LTE and NLTE problems under gray as well as nongray assumption. After every program, results are presented in tabulated form. The programs can be used to obtain results for other gases simply by changing the spectroscopic properties.

c program to calculate LTE and NLTE bulk temp. under gray

c gas assumption for CO

implicit double precision (a-h,o-z)

real l,kfb

dimension u(10),press(4),Temp(4)

data u/0.1,0.5,1.0,2.0,5.0,10.0,20.0,50.0,75.,100.0/

data press/0.1,1.,5.,10./

data temp/300.,500.,1000.0,2000.0/

open(unit=21, file='nlp')

open(unit=22, file='lp')

open(unit=23, file='out23.dat')

write(23,230)

write(21,13)

write(21,\*) 10,1

13 format('3',/, 'x',/, 't',/, 't1',/,i4,x,'1')

write(22,14)

write(22,\*) 10,1

14 format('2',/, 'x',/, 't',/,/,i4,x,'1')

do 101 it=1,4

tw=temp(it)

do 202 kk=1,4

p=press(kk)

do 303 i=1,10

l=u(i)

---

c Calculation of Plank's Function and it's derivative

c wnb Band Center

c hck Constant

c ccc c1\*c2 (erg\_k\_cm\*\*3/sec)

c pfdbi Plank's Function's derivative for ith band

---

tk1=tw\*\*2

tk2=tw\*\*0.5

tk3=tw/273.0

hck=1.439257246

ts=300.0/tw

---

c Spectroscopic Properties of CO

c Two Bands of CO are considered(4.7 and 2.35 microns)

c wnb1 Band Center (1/cm)

---

wnb1=2143.

wnb2=4260.

c2b1=hck\*wnb1

c2b2=hck\*wnb2

ccc=0.000053847734

ccb1=ccc\*(wnb1\*\*4.)

ccb2=ccc\*(wnb2\*\*4.)

fb1=c2b1/tw

```

tb2=c2b2/tw
teb1= exp(tb1)
teb2= exp(tb2)
c1b1=ccb1/c2b1
c1b2=ccb2/c2b2
pfb1=c1b1/(teb1-1.0)
pfb2=c1b2/(teb2-1.0)
dev1=tk1*((teb1-1.0)**2.0)
dev2=tk1*((teb2-1.0)**2.0)
pfdb1=(ccb1*teb1)/dev1
pfdb2=(ccb2*teb2)/dev2

```

---

c Band Model Correlations(Tien & Lowder Wide Band Model)

```

c azi aoi (1/cm)
c czsi coi**2 (1/atm-cm)
c bsi b**2 (Nondimensional)
c omegi Wave Number (1/cm)
c si Integrated Band Intensity (1/atm cm**2)

```

---

```

ak1=(tw/300.)**0.5
ak2=(300./tw)**1.5
az1=38.1*ak1
az2=az1

```

---

c dkf Thermal Conductivity (Erg/cm-sec-k)

---

```

kfb=(1488.365171)*(tk3**1.23)
omeg1=2143.
tx=-(hck/tw)
tx1=tx*omeg1
etx1= exp(tx1)
c1=1.0-etx1
c01=6.24*ak2
c02=0.042*ak2
s1=az1*c01
s2=az2*c02
ETC1=(14.)**(1./4.)
ETC2=0.015*ETC1
ETC3=TW**(-1./3.)
ETC4=ETC3-ETC2
ETC5=175.*ETC4
ETC6=(ETC5-18.42)
ETC7=EXP(ETC6)
ETAC=ETC7/P
etar11=8.*3.14*((wnb1**2.))*4.08*(1.e-12)*tw*s1
ETAR1=1/ETAR11
etar22=8.*3.14*((wnb2**2.))*4.08*(1.e-12)*tw*s2
etar2=1/etar22
ETA11=ETAC/ETAR1

```

```

cta12=ctac/ctar2
aap1=cta11/s1
aap2=cta12/s2
aapx1=(3./4.)*(aap1)/p
aapx2=(3./4.)*(aap2)/p
am2=1.+(aapx1+aapx2)
if(am2.le.0.)then
am2=.79
endif
tin=p*1**2/kfb*(s1*pfdb1+s2*pfdb2)
tn=exp(-3.*tin)**0.5)
ala=0.00005668
akp=p/(ala*tw**4.)*(s1*pfb1+s2*pfb2)
tao=akp*1
anba=kfb*akp/(4.*ala*tw**3.)
r=3.*tao**2./anba
a1m=3.*tao**2.*((0.75)+(1./anba))
am=sqrt(a1m)
em=exp(-am)
ad=3.*tao*(1.-em)+2.*am*(1.+em)
ac=(r/(am**8.))*(48.-3.*tao*am**2.+36.*tao)/ad
pa1=24.-12.*am+am**3.+(am**3.-12.*am-24.)*em
pa2=-12.*r/(5.*am**4.)+17.*r/(70.*am**2.)
ambar=sqrt(a1m/am2)
write(*,*) a1m,am2
rbar=r/am2
embar=exp(-ambar)
adbar=3.0*tao*(1.0-embar)+2.0*ambar*(1.0+embar)
acbar=(rbar/(ambar**8.))*(48.-3.*tao*(ambar**
* 2.0)+36.0*tao)/adbar
pa1bar=24.0-12.0*ambar+ambar**3.0
* +(ambar**3.0-12.0*ambar-24.0)*embar
pa2bar=-12.0*rbar/(5.0*ambar**4.0)+
* 17.0*rbar/(70.0*ambar**2.0)
tbulk=ac*pa1+pa2-17./70.
tbulkn=acbar*pa1bar+pa2bar-17.0/70.0
write(21,109) l,-tbulk,-tbulkn
write(22,100) l,-tbulkn
write(23,1000)tw, p, l, -tbulk, -tbulkn
100 format(1x,f9.2,3x,e10.4)
109 format(1x,f9.2,2(3x,e10.4))
303 continue
202 continue
101 continue
1000 format(1x,f7.2, 3x,f6.2, 3x,f6.2, 3x,e10.4, 3x,e10.4)
230 format(4x,'tw',8x,'p',6x,'l',9x,'tbulk',9x,'tbulkn')
stop
end

```

## GRAY GAS RESULTS FOR CO

tw	p	l	tbulk (LTE)	tbulkn (NLTE)
300.00	0.10	0.10	0.1649E+02	0.2468E+08
300.00	0.10	0.50	0.2430E+00	-.9185E+06
300.00	0.10	1.00	0.2427E+00	0.8417E+04
300.00	0.10	2.00	0.2422E+00	-.8730E+02
300.00	0.10	5.00	0.2385E+00	0.1610E+00
300.00	0.10	10.00	0.2264E+00	0.2435E+00
300.00	0.10	20.00	0.1885E+00	0.2428E+00
300.00	0.10	50.00	0.8728E-01	0.2423E+00
300.00	0.10	75.00	0.4887E-01	0.2416E+00
300.00	0.10	100.00	0.3041E-01	0.2406E+00
300.00	1.00	0.10	0.2450E+00	0.6133E+01
300.00	1.00	0.50	0.2424E+00	0.2428E+00
300.00	1.00	1.00	0.2411E+00	0.2426E+00
300.00	1.00	2.00	0.2360E+00	0.2420E+00
300.00	1.00	5.00	0.2061E+00	0.2378E+00
300.00	1.00	10.00	0.1429E+00	0.2241E+00
300.00	1.00	20.00	0.6587E-01	0.1837E+00
300.00	1.00	50.00	0.1530E-01	0.8624E-01
300.00	1.00	75.00	0.7767E-02	0.5082E-01
300.00	1.00	100.00	0.4886E-02	0.3353E-01
300.00	5.00	0.10	0.2428E+00	0.2428E+00
300.00	5.00	0.50	0.2407E+00	0.2412E+00
300.00	5.00	1.00	0.2345E+00	0.2363E+00
300.00	5.00	2.00	0.2131E+00	0.2192E+00
300.00	5.00	5.00	0.1332E+00	0.1484E+00
300.00	5.00	10.00	0.6092E-01	0.7320E-01
300.00	5.00	20.00	0.2244E-01	0.2788E-01
300.00	5.00	50.00	0.6654E-02	0.8075E-02
300.00	5.00	75.00	0.4423E-02	0.5221E-02
300.00	5.00	100.00	0.3510E-02	0.4049E-02
300.00	10.00	0.10	0.2427E+00	0.2427E+00
300.00	10.00	0.50	0.2386E+00	0.2389E+00
300.00	10.00	1.00	0.2270E+00	0.2280E+00
300.00	10.00	2.00	0.1914E+00	0.1942E+00
300.00	10.00	5.00	0.9734E-01	0.1014E+00
300.00	10.00	10.00	0.4095E-01	0.4325E-01
300.00	10.00	20.00	0.1661E-01	0.1753E-01
300.00	10.00	50.00	0.6857E-02	0.7114E-02
300.00	10.00	75.00	0.5365E-02	0.5517E-02
300.00	10.00	100.00	0.4721E-02	0.4828E-02
500.00	0.10	0.10	0.2449E+00	-.5491E+02
500.00	0.10	0.50	0.2423E+00	0.2423E+00
500.00	0.10	1.00	0.2408E+00	0.2428E+00
500.00	0.10	2.00	0.2349E+00	0.2425E+00

500.00	0.10	5.00	0.2004E+00	0.2405E+00
500.00	0.10	10.00	0.1320E+00	0.2337E+00
500.00	0.10	20.00	0.5657E-01	0.2106E+00
500.00	0.10	50.00	0.1190E-01	0.1272E+00
500.00	0.10	75.00	0.5701E-02	0.8200E-01
500.00	0.10	100.00	0.3400E-02	0.5580E-01
500.00	1.00	0.10	0.2427E+00	0.2427E+00
500.00	1.00	0.50	0.2378E+00	0.2387E+00
500.00	1.00	1.00	0.2241E+00	0.2270E+00
500.00	1.00	2.00	0.1827E+00	0.1907E+00
500.00	1.00	5.00	0.8245E-01	0.9284E-01
500.00	1.00	10.00	0.3007E-01	0.3523E-01
500.00	1.00	20.00	0.9946E-02	0.1176E-01
500.00	1.00	50.00	0.2786E-02	0.3220E-02
500.00	1.00	75.00	0.1821E-02	0.2061E-02
500.00	1.00	100.00	0.1429E-02	0.1591E-02
500.00	5.00	0.10	0.2418E+00	0.2418E+00
500.00	5.00	0.50	0.2204E+00	0.2205E+00
500.00	5.00	1.00	0.1748E+00	0.1752E+00
500.00	5.00	2.00	0.1004E+00	0.1009E+00
500.00	5.00	5.00	0.3138E-01	0.3158E-01
500.00	5.00	10.00	0.1311E-01	0.1318E-01
500.00	5.00	20.00	0.6858E-02	0.6888E-02
500.00	5.00	50.00	0.4280E-02	0.4290E-02
500.00	5.00	75.00	0.3836E-02	0.3842E-02
500.00	5.00	100.00	0.3632E-02	0.3636E-02
500.00	10.00	0.10	0.2408E+00	0.2408E+00
500.00	10.00	0.50	0.2033E+00	0.2033E+00
500.00	10.00	1.00	0.1420E+00	0.1421E+00
500.00	10.00	2.00	0.7209E-01	0.7219E-01
500.00	10.00	5.00	0.2466E-01	0.2469E-01
500.00	10.00	10.00	0.1320E-01	0.1321E-01
500.00	10.00	20.00	0.9033E-02	0.9039E-02
500.00	10.00	50.00	0.7122E-02	0.7124E-02
500.00	10.00	75.00	0.6760E-02	0.6762E-02
500.00	10.00	100.00	0.6588E-02	0.6589E-02
1000.00	0.10	0.10	0.2428E+00	0.2429E+00
1000.00	0.10	0.50	0.2416E+00	0.2420E+00
1000.00	0.10	1.00	0.2379E+00	0.2394E+00
1000.00	0.10	2.00	0.2242E+00	0.2295E+00
1000.00	0.10	5.00	0.1599E+00	0.1784E+00
1000.00	0.10	10.00	0.7937E-01	0.9969E-01
1000.00	0.10	20.00	0.2662E-01	0.3644E-01
1000.00	0.10	50.00	0.4890E-02	0.6945E-02
1000.00	0.10	75.00	0.2275E-02	0.3244E-02
1000.00	0.10	100.00	0.1331E-02	0.1898E-02
1000.00	1.00	0.10	0.2424E+00	0.2424E+00
1000.00	1.00	0.50	0.2309E+00	0.2309E+00
1000.00	1.00	1.00	0.2014E+00	0.2015E+00



1000.00	1.00	2.00	0.1340E+00	0.1342E+00
1000.00	1.00	5.00	0.4134E-01	0.4148E-01
1000.00	1.00	10.00	0.1265E-01	0.1271E-01
1000.00	1.00	20.00	0.3774E-02	0.3790E-02
1000.00	1.00	50.00	0.9107E-03	0.9141E-03
1000.00	1.00	75.00	0.5485E-03	0.5503E-03
1000.00	1.00	100.00	0.4057E-03	0.4069E-03
1000.00	5.00	0.10	0.2404E+00	0.2404E+00
1000.00	5.00	0.50	0.1939E+00	0.1939E+00
1000.00	5.00	1.00	0.1229E+00	0.1229E+00
1000.00	5.00	2.00	0.5226E-01	0.5226E-01
1000.00	5.00	5.00	0.1240E-01	0.1240E-01
1000.00	5.00	10.00	0.4449E-02	0.4449E-02
1000.00	5.00	20.00	0.1995E-02	0.1995E-02
1000.00	5.00	50.00	0.1055E-02	0.1055E-02
1000.00	5.00	75.00	0.9011E-03	0.9012E-03
1000.00	5.00	100.00	0.8321E-03	0.8321E-03
1000.00	10.00	0.10	0.2380E+00	0.2380E+00
1000.00	10.00	0.50	0.1632E+00	0.1632E+00
1000.00	10.00	1.00	0.8596E-01	0.8597E-01
1000.00	10.00	2.00	0.3290E-01	0.3290E-01
1000.00	10.00	5.00	0.8690E-02	0.8691E-02
1000.00	10.00	10.00	0.3931E-02	0.3931E-02
1000.00	10.00	20.00	0.2340E-02	0.2340E-02
1000.00	10.00	50.00	0.1653E-02	0.1653E-02
1000.00	10.00	75.00	0.1528E-02	0.1528E-02
1000.00	10.00	100.00	0.1469E-02	0.1469E-02
2000.00	0.10	0.10	0.2434E+00	0.2423E+00
2000.00	0.10	0.50	0.2421E+00	0.2421E+00
2000.00	0.10	1.00	0.2398E+00	0.2399E+00
2000.00	0.10	2.00	0.2311E+00	0.2314E+00
2000.00	0.10	5.00	0.1843E+00	0.1853E+00
2000.00	0.10	10.00	0.1070E+00	0.1084E+00
2000.00	0.10	20.00	0.4007E-01	0.4085E-01
2000.00	0.10	50.00	0.7500E-02	0.7670E-02
2000.00	0.10	75.00	0.3413E-02	0.3492E-02
2000.00	0.10	100.00	0.1944E-02	0.1989E-02
2000.00	1.00	0.10	0.2425E+00	0.2425E+00
2000.00	1.00	0.50	0.2354E+00	0.2354E+00
2000.00	1.00	1.00	0.2155E+00	0.2155E+00
2000.00	1.00	2.00	0.1612E+00	0.1612E+00
2000.00	1.00	5.00	0.5865E-01	0.5866E-01
2000.00	1.00	10.00	0.1812E-01	0.1812E-01
2000.00	1.00	20.00	0.4918E-02	0.4920E-02
2000.00	1.00	50.00	0.8629E-03	0.8631E-03
2000.00	1.00	75.00	0.4090E-03	0.4091E-03
2000.00	1.00	100.00	0.2451E-03	0.2451E-03
2000.00	5.00	0.10	0.2413E+00	0.2413E+00
2000.00	5.00	0.50	0.2097E+00	0.2097E+00

2000.00	5.00	1.00	0.1492E+00	0.1492E+00
2000.00	5.00	2.00	0.6974E-01	0.6974E-01
2000.00	5.00	5.00	0.1523E-01	0.1523E-01
2000.00	5.00	10.00	0.4250E-02	0.4250E-02
2000.00	5.00	20.00	0.1219E-02	0.1219E-02
2000.00	5.00	50.00	0.2810E-03	0.2810E-03
2000.00	5.00	75.00	0.1649E-03	0.1649E-03
2000.00	5.00	100.00	0.1196E-03	0.1196E-03
2000.00	10.00	0.10	0.2398E+00	0.2398E+00
2000.00	10.00	0.50	0.1848E+00	0.1848E+00
2000.00	10.00	1.00	0.1084E+00	0.1084E+00
2000.00	10.00	2.00	0.4156E-01	0.4156E-01
2000.00	10.00	5.00	0.8347E-02	0.8347E-02
2000.00	10.00	10.00	0.2423E-02	0.2423E-02
2000.00	10.00	20.00	0.7780E-03	0.7780E-03
2000.00	10.00	50.00	0.2386E-03	0.2386E-03
2000.00	10.00	75.00	0.1651E-03	0.1651E-03
2000.00	10.00	100.00	0.1346E-03	0.1346E-03

C Program to calculate LTE and NLTE bulk temp. under gray  
c gas assumption for NO

```
IMPLICIT DOUBLE PRECISION (A-H,O-Z)
REAL L,KFB
DIMENSION U(10),PRES(4),TEMP(4)
OPEN (1,FILE='out1a')
OPEN (2,FILE='nlp')
OPEN (3,FILE='lp')
DATA U/0.1,0.5,1.,2.,5.,10.,20.,50.,75.,100./
DATA PRES/0.1,1.,5.,10./
DATA TEMP/300.,500.,1000.,2000./
WRITE (1,11)
write(2,13)
write(2,*) 10,1
13 format('3', 'x', 't', 't1', /, i4, x, '1')
write(3,14)
write(3,*) 10,1
14 format('2', 'x', 't', /, /, i4, x, '1')
DO 4 IT=1,4
TW=TEMP(IT)
DO 5 KK=1,4
P=PRES(KK)
DO 6 I=1,10
L=U(I)
TK1=TW**2.
TK2=TW**0.5
TK3=TW/273.
HCK=1.439257246
TS=300./TW
WNB1=1876.
wnb2=3724.
C2B1=HCK*WNB1
c2b2=hck*wnb2
CCC=0.000053847734
CCB1=CCC*(WNB1**4.)
ccb2=ccc*(wnb2**4.)
TB1=C2B1/TW
tb2=c2b2/tw
TEB1=EXP(TB1)
teb2=exp(tb2)
C1B1=CCB1/C2B1
c1b2=ccb2/c2b2
PFB1=C1B1/(TEB1-1.)
pfb2=c1b2/(teb2-1.)
DEV1=TK1*((TEB1-1.)**2.)
dev2=tk1*((teb2-1.)**2.)
PFDB1=(CCB1*TEB1)/DEV1
pfd2=(ccb2*teb2)/dev2
AK1=(TW/300.)**0.5
```

```

AK2=(300./TW)**1.5
AZ1=36.*AK1
az2=36.*ak1
KFB=(TW/179.16)*0.01378*(1.E+8)*(1./(36.*23.889))
OMEG=1876.
S1=132.*TS
s2=2.2*ts
ETC1=1.16*1.E-3*((15)**0.5)*(2700.**4./3.)
ETC2=TW**(-1./3.)-0.015*((15.)**0.25)
ETC3=ETC1*ETC2-18.42
ETC4=EXP(ETC3)
ETAC=ETC4/P
c ETC1=(14.)**(1./4.)
c ETC2=0.015*ETC1
c ETC3=TW**(-1./3.)
c ETC4=ETC3-ETC2
c ETC5=175.*ETC4
c ETC6=(ETC5-18.42)
c ETC7=EXP(ETC6)
c ETAC=ETC7/P
ETAR1=8*3.14*(1876.**2)*4.08*(1.E-12)*300.*132.
ETAR2=8*3.14*(3724.**2)*4.08*(1.E-12)*300.*2.2
ETAR11=1/ETAR1
ctar12=1/ctar2
ETA1=ETAC/ETAR11
cta2=ctac/ctar12
aap1=cta1/s1
aap2=cta2/s2
aapx=(3./4.)*(aap1+aap2)
am2=1.+(aapx)
write(*,*)am2
tin=p*1**2.0/kfb*(s1*pfdb1+s2*pfdb2)
tn=exp(-(3.0*tin)**0.5)
anexp=(1.0-tn)/(1.0+tn)
tcm=1/kfb*(pfdb1*az1+pfdb2*az2)
ala=0.00005668
akp=p/(ala*tw**4.0)*(s1*pfb1+s2*pfb2)
tao=akp*1
anba=kfb*akp/(4.0*ala*tw**3.0)
r=3.0*tao**2.0/anba
aim=3.0*tao**2.0*(0.75+1.0/anba)
am=sqrt(aim)
em=exp(-am)
ad=3.0*tao*(1.0-em)+2.0*am*(1.0+em)
ac=r/am**8.0*(48.0-3.0*tao*am**2.0+36.0*tao)/ad
pa1=24.0-12.0*am+am**3.0+(am**3.0-12.0*am-24.0)*em
pa2=-12.0*r/(5.0*am**4.0)+17.0*r/(70.0*am**2.0)
ambar=am/(sqrt(am2))
rbar=r/am2

```

```

cbar=exp(-ambar)
adbar=3.0*tao*(1.0-cbar)+2.0*ambar*(1.0+cbar)
acbar=(rbar/(ambar**8.))*(48.-3.*tao*(ambar**
* 2.0)+36.0*tao)/adbar
pa1bar=24.0-12.0*ambar+ambar**3.0
* +(ambar**3.0-12.0*ambar-24.0)*cbar
pa2bar=-12.0*rbar/(5.0*ambar**4.0)+
* 17.0*rbar/(70.0*ambar**2.0)
tbulk=ac*pa1+pa2-17.0/70.0
tbulkn=acbar*pa1bar+pa2bar-17.0/70.0
WRITE (1,19) TW,P,L,-TBULK,-TBULKN
WRITE (2,20) L,-TBULK,-tbulkn
WRITE (3,21) L, -TBULKN
6 CONTINUE
5 CONTINUE
4 CONTINUE
19 FORMAT (1X,F7.2,2(3X,F6.2),2(3X,E10.4))
20 FORMAT (3X,F6.2,2(3X,E10.4))
21 FORMAT (3X,F6.2,3X,E10.4)
11 FORMAT (4X, 'TW',8X, 'P',6X, 'L',9X, 'TBULK',9X, 'TBULKN')
STOP
END

```

## GRAY GAS RESULTS FOR NO

TW	P	L	TBULK (LTE)	TBULKN (NLTE)
300.00	0.10	0.10	0.5314E+01	0.1035E+07
300.00	0.10	0.50	0.2430E+00	-3009E+01
300.00	0.10	1.00	0.2427E+00	0.7631E-01
300.00	0.10	2.00	0.2423E+00	0.2418E+00
300.00	0.10	5.00	0.2392E+00	0.2427E+00
300.00	0.10	10.00	0.2290E+00	0.2423E+00
300.00	0.10	20.00	0.1958E+00	0.2406E+00
300.00	0.10	50.00	0.9796E-01	0.2297E+00
300.00	0.10	75.00	0.5670E-01	0.2155E+00
300.00	0.10	100.00	0.3594E-01	0.1986E+00
300.00	1.00	0.10	0.2451E+00	0.8474E+00
300.00	1.00	0.50	0.2425E+00	0.2428E+00
300.00	1.00	1.00	0.2414E+00	0.2424E+00
300.00	1.00	2.00	0.2372E+00	0.2412E+00
300.00	1.00	5.00	0.2116E+00	0.2330E+00
300.00	1.00	10.00	0.1541E+00	0.2084E+00
300.00	1.00	20.00	0.7624E-01	0.1490E+00
300.00	1.00	50.00	0.1922E-01	0.5481E-01
300.00	1.00	75.00	0.1015E-01	0.3056E-01
300.00	1.00	100.00	0.6604E-02	0.1994E-01
300.00	5.00	0.10	0.2427E+00	0.2427E+00
300.00	5.00	0.50	0.2411E+00	0.2416E+00
300.00	5.00	1.00	0.2359E+00	0.2382E+00
300.00	5.00	2.00	0.2178E+00	0.2255E+00
300.00	5.00	5.00	0.1458E+00	0.1680E+00
300.00	5.00	10.00	0.7275E-01	0.9412E-01
300.00	5.00	20.00	0.2946E-01	0.4030E-01
300.00	5.00	50.00	0.1021E-01	0.1335E-01
300.00	5.00	75.00	0.7327E-02	0.9140E-02
300.00	5.00	100.00	0.6112E-02	0.7360E-02
300.00	10.00	0.10	0.2427E+00	0.2427E+00
300.00	10.00	0.50	0.2393E+00	0.2400E+00
300.00	10.00	1.00	0.2296E+00	0.2321E+00
300.00	10.00	2.00	0.1993E+00	0.2066E+00
300.00	10.00	5.00	0.1119E+00	0.1249E+00
300.00	10.00	10.00	0.5233E-01	0.6099E-01
300.00	10.00	20.00	0.2402E-01	0.2782E-01
300.00	10.00	50.00	0.1180E-01	0.1295E-01
300.00	10.00	75.00	0.9820E-02	0.1052E-01
300.00	10.00	100.00	0.8945E-02	0.9440E-02
500.00	0.10	0.10	0.2349E+00	0.7721E-01
500.00	0.10	0.50	0.2426E+00	0.2427E+00
500.00	0.10	1.00	0.2417E+00	0.2422E+00
500.00	0.10	2.00	0.2383E+00	0.2403E+00

500.00	0.10	5.00	0.2169E+00	0.2277E+00
500.00	0.10	10.00	0.1646E+00	0.1921E+00
500.00	0.10	20.00	0.8453E-01	0.1189E+00
500.00	0.10	50.00	0.1996E-01	0.3362E-01
500.00	0.10	75.00	0.9652E-02	0.1676E-01
500.00	0.10	100.00	0.5741E-02	0.1007E-01
500.00	1.00	0.10	0.2427E+00	0.2428E+00
500.00	1.00	0.50	0.2400E+00	0.2402E+00
500.00	1.00	1.00	0.2318E+00	0.2326E+00
500.00	1.00	2.00	0.2045E+00	0.2069E+00
500.00	1.00	5.00	0.1146E+00	0.1193E+00
500.00	1.00	10.00	0.4719E-01	0.5014E-01
500.00	1.00	20.00	0.1594E-01	0.1707E-01
500.00	1.00	50.00	0.4164E-02	0.4432E-02
500.00	1.00	75.00	0.2588E-02	0.2734E-02
500.00	1.00	100.00	0.1958E-02	0.2055E-02
500.00	5.00	0.10	0.2423E+00	0.2423E+00
500.00	5.00	0.50	0.2295E+00	0.2297E+00
500.00	5.00	1.00	0.1984E+00	0.1990E+00
500.00	5.00	2.00	0.1327E+00	0.1336E+00
500.00	5.00	5.00	0.4708E-01	0.4765E-01
500.00	5.00	10.00	0.1920E-01	0.1943E-01
500.00	5.00	20.00	0.9308E-02	0.9395E-02
500.00	5.00	50.00	0.5302E-02	0.5329E-02
500.00	5.00	75.00	0.4633E-02	0.4650E-02
500.00	5.00	100.00	0.4330E-02	0.4342E-02
500.00	10.00	0.10	0.2417E+00	0.2417E+00
500.00	10.00	0.50	0.2184E+00	0.2186E+00
500.00	10.00	1.00	0.1716E+00	0.1720E+00
500.00	10.00	2.00	0.9975E-01	0.1002E+00
500.00	10.00	5.00	0.3534E-01	0.3553E-01
500.00	10.00	10.00	0.1773E-01	0.1781E-01
500.00	10.00	20.00	0.1132E-01	0.1135E-01
500.00	10.00	50.00	0.8457E-02	0.8468E-02
500.00	10.00	75.00	0.7929E-02	0.7936E-02
500.00	10.00	100.00	0.7681E-02	0.7686E-02
1000.00	0.10	0.10	0.2414E+00	0.2433E+00
1000.00	0.10	0.50	0.2423E+00	0.2423E+00
1000.00	0.10	1.00	0.2405E+00	0.2406E+00
1000.00	0.10	2.00	0.2338E+00	0.2340E+00
1000.00	0.10	5.00	0.1958E+00	0.1965E+00
1000.00	0.10	10.00	0.1240E+00	0.1252E+00
1000.00	0.10	20.00	0.5055E-01	0.5134E-01
1000.00	0.10	50.00	0.1003E-01	0.1022E-01
1000.00	0.10	75.00	0.4652E-02	0.4742E-02
1000.00	0.10	100.00	0.2691E-02	0.2743E-02
1000.00	1.00	0.10	0.2426E+00	0.2426E+00
1000.00	1.00	0.50	0.2372E+00	0.2372E+00
1000.00	1.00	1.00	0.2216E+00	0.2216E+00

1000.00	1.00	2.00	0.1759E+00	0.1760E+00
1000.00	1.00	5.00	0.7306E-01	0.7316E-01
1000.00	1.00	10.00	0.2443E-01	0.2447E-01
1000.00	1.00	20.00	0.7130E-02	0.7143E-02
1000.00	1.00	50.00	0.1475E-02	0.1478E-02
1000.00	1.00	75.00	0.7930E-03	0.7944E-03
1000.00	1.00	100.00	0.5342E-03	0.5350E-03
1000.00	5.00	0.10	0.2417E+00	0.2417E+00
1000.00	5.00	0.50	0.2171E+00	0.2171E+00
1000.00	5.00	1.00	0.1658E+00	0.1658E+00
1000.00	5.00	2.00	0.8704E-01	0.8706E-01
1000.00	5.00	5.00	0.2214E-01	0.2215E-01
1000.00	5.00	10.00	0.7161E-02	0.7163E-02
1000.00	5.00	20.00	0.2628E-02	0.2628E-02
1000.00	5.00	50.00	0.1026E-02	0.1026E-02
1000.00	5.00	75.00	0.7898E-03	0.7899E-03
1000.00	5.00	100.00	0.6881E-03	0.6882E-03
1000.00	10.00	0.10	0.2406E+00	0.2406E+00
1000.00	10.00	0.50	0.1970E+00	0.1971E+00
1000.00	10.00	1.00	0.1281E+00	0.1281E+00
1000.00	10.00	2.00	0.5623E-01	0.5624E-01
1000.00	10.00	5.00	0.1387E-01	0.1387E-01
1000.00	10.00	10.00	0.5173E-02	0.5173E-02
1000.00	10.00	20.00	0.2438E-02	0.2438E-02
1000.00	10.00	50.00	0.1366E-02	0.1366E-02
1000.00	10.00	75.00	0.1188E-02	0.1188E-02
1000.00	10.00	100.00	0.1107E-02	0.1107E-02
2000.00	0.10	0.10	0.2326E+00	0.2513E+00
2000.00	0.10	0.50	0.2425E+00	0.2425E+00
2000.00	0.10	1.00	0.2414E+00	0.2414E+00
2000.00	0.10	2.00	0.2372E+00	0.2372E+00
2000.00	0.10	5.00	0.2113E+00	0.2113E+00
2000.00	0.10	10.00	0.1521E+00	0.1522E+00
2000.00	0.10	20.00	0.7176E-01	0.7182E-01
2000.00	0.10	50.00	0.1533E-01	0.1535E-01
2000.00	0.10	75.00	0.7084E-02	0.7092E-02
2000.00	0.10	100.00	0.4049E-02	0.4053E-02
2000.00	1.00	0.10	0.2427E+00	0.2427E+00
2000.00	1.00	0.50	0.2393E+00	0.2393E+00
2000.00	1.00	1.00	0.2292E+00	0.2292E+00
2000.00	1.00	2.00	0.1961E+00	0.1961E+00
2000.00	1.00	5.00	0.9773E-01	0.9774E-01
2000.00	1.00	10.00	0.3518E-01	0.3519E-01
2000.00	1.00	20.00	0.9987E-02	0.9988E-02
2000.00	1.00	50.00	0.1717E-02	0.1717E-02
2000.00	1.00	75.00	0.7896E-03	0.7897E-03
2000.00	1.00	100.00	0.4586E-03	0.4586E-03
2000.00	5.00	0.10	0.2421E+00	0.2421E+00
2000.00	5.00	0.50	0.2260E+00	0.2260E+00



2000.00	5.00	1.00	0.1872E+00	0.1872E+00
2000.00	5.00	2.00	0.1114E+00	0.1114E+00
2000.00	5.00	5.00	0.2945E-01	0.2945E-01
2000.00	5.00	10.00	0.8342E-02	0.8342E-02
2000.00	5.00	20.00	0.2274E-02	0.2274E-02
2000.00	5.00	50.00	0.4399E-03	0.4399E-03
2000.00	5.00	75.00	0.2271E-03	0.2271E-03
2000.00	5.00	100.00	0.1476E-03	0.1476E-03
2000.00	10.00	0.10	0.2414E+00	0.2414E+00
2000.00	10.00	0.50	0.2115E+00	0.2115E+00
2000.00	10.00	1.00	0.1527E+00	0.1527E+00
2000.00	10.00	2.00	0.7285E-01	0.7285E-01
2000.00	10.00	5.00	0.1612E-01	0.1612E-01
2000.00	10.00	10.00	0.4504E-02	0.4504E-02
2000.00	10.00	20.00	0.1289E-02	0.1289E-02
2000.00	10.00	50.00	0.2947E-03	0.2947E-03
2000.00	10.00	75.00	0.1720E-03	0.1720E-03
2000.00	10.00	100.00	0.1242E-03	0.1242E-03

c Program to calculate LTE and NLTE bulk temp. under gray  
 c gas assumption for OH

```

IMPLICIT DOUBLE PRECISION (A-H,O-Z)
REAL L,KFB
dimension u(10),pres(4),temp(4)
OPEN (1,FILE='out11a')
OPEN (2,FILE='nlp')
OPEN (3,FILE='lp')
DATA U/0.1,0.5,1.,2.,5.,10.,20.,50.,75.,100./
DATA PRES/0.1,1.,5.,10./
DATA TEMP/300.,500.,1000.,2000./
WRITE (1,11)
write(2,13)
write(2,*) 10,1
13 format('3',/,'x',/,'t',/,'t1',/,'i4,x','1')
   write(3,14)
   write(3,*) 10,1
14 format('2',/,'x',/,'t',/,'/,'i4,x','1')
DO 4 IT=1,4
  TW=TEMP(IT)
DO 5 KK=1,4
  P=PRES(KK)
DO 6 I=1,10
  L=U(I)
  TK1=TW**2.
  TK2=TW**0.5
  TK3=TW/273.
  HCK=1.439257246
  TS=300./TW
  WNB1=3570.
  wnb2=6974.
  C2B1=HCK*WNB1
  c2b2=hck*wnb2
  CCC=0.000053847734
  CCB1=CCC*(WNB1**4.)
  ccb2=ccc*(wnb2**4.)
  TB1=C2B1/TW
  tb2=c2b2/tw
  TEB1=EXP(TB1)
  teb2=exp(tb2)
  C1B1=CCB1/C2B1
  c1b2=ccb2/c2b2
  PFB1=C1B1/(TEB1-1.)
  pfb2=c1b2/(teb2-1.)
  DEV1=TK1*((TEB1-1.)**2.)
  dev2=tk1*((teb2-1.)**2.)
  PFDB1=(CCB1*TEB1)/DEV1
  pfdb2=(ccb2*teb2)/dev2

```

```

AK1=(TW/300.)**0.5
AK2=(300./TW)**1.5
AZ1=117.*AK1
az2=117.*ak1
IF (TW.EQ.300.) THEN
KFB=4879.71
ELSEIF (TW.EQ.500.) THEN
KFB=6993.13
ELSEIF (TW.EQ.1000.) THEN
KFB=11504.56
ELSEIF (TW.EQ.2000.) THEN
KFB=20276.33
ENDIF
OMEG=3570.
S1=110.*TS
s2=4.4*ts
ETC1=1.16*1.E-3*((9.)**0.5)*(2700.**(.4/.3.))
ETC2=TW**(-1./3.)-0.015*((9.)**0.25)
ETC3=ETC1*ETC2-18.42
ETC4=EXP(ETC3)
ETAC=ETC4/P
c ETC1=(8.5)**(1./4.)
c ETC2=0.015*ETC1
c ETC3=TW**(-1./3.)
c ETC4=ETC3-ETC2
c ETC5=175.*ETC4
c ETC6=(ETC5-18.42)
c ETC7=EXP(ETC6)
c ETAC=ETC7/P
ETAR1=8.*3.14*(3570.**(.2.))*4.08*(1.E-12)*s1*tw
ETAR11=1./ETAR1
ETAR2=8.*3.14*(6974.**(.2.))*4.08*(1.E-12)*s2*tw
etar12=1./etar2
ETA1=ETAC/ETAR11
eta2=etac/etar12
aap1=eta1/s1
aap2=eta2/s2
aapx=(3./4.)*(aap1+aap2)/p
am2=1.+aapx
write(*,*)am2
if(am2.le.0.)then
am2=.97
endif
tin=p*1**2.0/kfb*(s1*pfdb1+s2*pfdb2)
tn=exp(-(3.0*tin)**0.5)
anexp=(1.0-tn)/(1.0+tn)
ala=0.00005668
akp=p/(ala*tw**4.0)*(s1*pfb1+s2*pfb2)
tao=akp*1

```

```

anba=kfb*akp/(4.0*ala*tw**3.0)
r=3.0*tao**2.0/anba
aim=3.0*tao**2.0*(0.75+1.0/anba)
am=sqrt(aim)
cm=exp(-am)
ad=3.0*tao*(1.0-cm)+2.0*am*(1.0+cm)
ac=r/am**8.0*(48.0-3.0*tao*am**2.0+36.0*tao)/ad
pa1=24.0-12.0*am+am**3.0+(am**3.0-12.0*am-24.0)*cm
pa2=-12.0*r/(5.0*am**4.0)+17.0*r/(70.0*am**2.0)
ambar=am/(sqrt(am2))
rbar=r/am2
cmlbar=exp(-ambar)
adbar=3.0*tao*(1.0-cmlbar)+2.0*ambar*(1.0+cmlbar)
acbar=(rbar/(ambar**8.0))*(48.-3.*tao*(ambar**
* 2.0)+36.0*tao)/adbar
pa1bar=24.0-12.0*ambar+ambar**3.0
* +(ambar**3.0-12.0*ambar-24.0)*cmlbar
pa2bar=-12.0*rbar/(5.0*ambar**4.0)+
* 17.0*rbar/(70.0*ambar**2.0)
tbulkn=ac*pa1+pa2-17.0/70.0
tbulkn=acbar*pa1bar+pa2bar-17.0/70.0
WRITE (1,19) TW,P,L,-TBULK,-TBULKN
WRITE (2,20) L,-TBULK,-tbulkn
WRITE (3,21) L,- TBULKN
6 CONTINUE
5 CONTINUE
4 CONTINUE
write(*,*) etac,etar,eta
19 FORMAT (1X,F7.2,2(3X,F6.2),2(3X,E10.4))
20 FORMAT (3X,F6.2,2(3X,E10.4))
21 FORMAT (3X,F6.2,3X,E10.4)
11 FORMAT (4X, 'TW',8X,'P',6X,'L',9X,'TBULK',9X,'TBULKN')
STOP
END

```

## GRAY GAS RESULTS FOR OH

TW	P	L	TBULK (LTE)		TBULKN (NLTE)	
300.00	0.10	0.10	-.1029E+13	0.6671E+09		
300.00	0.10	0.50	0.1716E+07	0.2668E+08		
300.00	0.10	1.00	0.1699E+05	0.6671E+07		
300.00	0.10	2.00	0.9029E+03	-.1026E+08		
300.00	0.10	5.00	0.1639E+01	0.1247E+05		
300.00	0.10	10.00	0.2493E+00	-.3966E+02		
300.00	0.10	20.00	0.2427E+00	0.1703E+00		
300.00	0.10	50.00	0.2425E+00	0.2442E+00		
300.00	0.10	75.00	0.2421E+00	0.2427E+00		
300.00	0.10	100.00	0.2415E+00	0.2428E+00		
300.00	1.00	0.10	0.4289E+07	-.5186E+09		
300.00	1.00	0.50	0.5466E+03	0.1937E+04		
300.00	1.00	1.00	-.8436E+01	-.2078E+02		
300.00	1.00	2.00	0.1698E+00	-.2315E+00		
300.00	1.00	5.00	0.2425E+00	0.2423E+00		
300.00	1.00	10.00	0.2427E+00	0.2427E+00		
300.00	1.00	20.00	0.2423E+00	0.2424E+00		
300.00	1.00	50.00	0.2395E+00	0.2399E+00		
300.00	1.00	75.00	0.2354E+00	0.2363E+00		
300.00	1.00	100.00	0.2298E+00	0.2314E+00		
300.00	5.00	0.10	-.3067E+06	-.1514E+07		
300.00	5.00	0.50	0.3094E+01	0.2776E+01		
300.00	5.00	1.00	0.2549E+00	0.1936E+00		
300.00	5.00	2.00	0.2427E+00	0.2430E+00		
300.00	5.00	5.00	0.2427E+00	0.2427E+00		
300.00	5.00	10.00	0.2422E+00	0.2422E+00		
300.00	5.00	20.00	0.2401E+00	0.2402E+00		
300.00	5.00	50.00	0.2268E+00	0.2269E+00		
300.00	5.00	75.00	0.2096E+00	0.2097E+00		
300.00	5.00	100.00	0.1894E+00	0.1897E+00		
300.00	10.00	0.10	0.1707E+05	0.1560E+05		
300.00	10.00	0.50	0.1120E+00	-.1176E+01		
300.00	10.00	1.00	0.2437E+00	0.2398E+00		
300.00	10.00	2.00	0.2427E+00	0.2428E+00		
300.00	10.00	5.00	0.2425E+00	0.2425E+00		
300.00	10.00	10.00	0.2415E+00	0.2415E+00		
300.00	10.00	20.00	0.2375E+00	0.2375E+00		
300.00	10.00	50.00	0.2128E+00	0.2129E+00		
300.00	10.00	75.00	0.1844E+00	0.1845E+00		
300.00	10.00	100.00	0.1555E+00	0.1556E+00		
500.00	0.10	0.10	0.5585E+04	-.4203E+05		
500.00	0.10	0.50	0.1946E+00	0.9841E+00		
500.00	0.10	1.00	0.2431E+00	0.2345E+00		
500.00	0.10	2.00	0.2427E+00	0.2428E+00		

500.00	0.10	5.00	0.2420E+00	0.2425E+00
500.00	0.10	10.00	0.2396E+00	0.2413E+00
500.00	0.10	20.00	0.2305E+00	0.2369E+00
500.00	0.10	50.00	0.1819E+00	0.2099E+00
500.00	0.10	75.00	0.1385E+00	0.1796E+00
500.00	0.10	100.00	0.1040E+00	0.1494E+00
500.00	1.00	0.10	-.9847E+00	-.8765E+00
500.00	1.00	0.50	0.2428E+00	0.2428E+00
500.00	1.00	1.00	0.2425E+00	0.2425E+00
500.00	1.00	2.00	0.2416E+00	0.2416E+00
500.00	1.00	5.00	0.2350E+00	0.2351E+00
500.00	1.00	10.00	0.2142E+00	0.2145E+00
500.00	1.00	20.00	0.1586E+00	0.1592E+00
500.00	1.00	50.00	0.5712E-01	0.5761E-01
500.00	1.00	75.00	0.2964E-01	0.2994E-01
500.00	1.00	100.00	0.1790E-01	0.1808E-01
500.00	5.00	0.10	0.2399E+00	0.2429E+00
500.00	5.00	0.50	0.2425E+00	0.2425E+00
500.00	5.00	1.00	0.2412E+00	0.2412E+00
500.00	5.00	2.00	0.2365E+00	0.2365E+00
500.00	5.00	5.00	0.2084E+00	0.2084E+00
500.00	5.00	10.00	0.1471E+00	0.1472E+00
500.00	5.00	20.00	0.6905E-01	0.6908E-01
500.00	5.00	50.00	0.1596E-01	0.1597E-01
500.00	5.00	75.00	0.7992E-02	0.7996E-02
500.00	5.00	100.00	0.4953E-02	0.4955E-02
500.00	10.00	0.10	0.2434E+00	0.2437E+00
500.00	10.00	0.50	0.2420E+00	0.2420E+00
500.00	10.00	1.00	0.2397E+00	0.2397E+00
500.00	10.00	2.00	0.2306E+00	0.2306E+00
500.00	10.00	5.00	0.1832E+00	0.1832E+00
500.00	10.00	10.00	0.1075E+00	0.1075E+00
500.00	10.00	20.00	0.4253E-01	0.4253E-01
500.00	10.00	50.00	0.9684E-02	0.9685E-02
500.00	10.00	75.00	0.5169E-02	0.5170E-02
500.00	10.00	100.00	0.3433E-02	0.3433E-02
1000.00	0.10	0.10	0.1860E+00	0.3166E+00
1000.00	0.10	0.50	0.2426E+00	0.2427E+00
1000.00	0.10	1.00	0.2420E+00	0.2421E+00
1000.00	0.10	2.00	0.2395E+00	0.2397E+00
1000.00	0.10	5.00	0.2233E+00	0.2246E+00
1000.00	0.10	10.00	0.1799E+00	0.1833E+00
1000.00	0.10	20.00	0.1014E+00	0.1058E+00
1000.00	0.10	50.00	0.2525E-01	0.2695E-01
1000.00	0.10	75.00	0.1202E-01	0.1288E-01
1000.00	0.10	100.00	0.6972E-02	0.7484E-02
1000.00	1.00	0.10	0.2428E+00	0.2428E+00
1000.00	1.00	0.50	0.2407E+00	0.2407E+00
1000.00	1.00	1.00	0.2346E+00	0.2347E+00

1000.00	1.00	2.00	0.2131E+00	0.2132E+00
1000.00	1.00	5.00	0.1304E+00	0.1305E+00
1000.00	1.00	10.00	0.5536E-01	0.5539E-01
1000.00	1.00	20.00	0.1727E-01	0.1729E-01
1000.00	1.00	50.00	0.3278E-02	0.3280E-02
1000.00	1.00	75.00	0.1607E-02	0.1609E-02
1000.00	1.00	100.00	0.9924E-03	0.9931E-03
1000.00	5.00	0.10	0.2424E+00	0.2424E+00
1000.00	5.00	0.50	0.2327E+00	0.2327E+00
1000.00	5.00	1.00	0.2071E+00	0.2071E+00
1000.00	5.00	2.00	0.1448E+00	0.1448E+00
1000.00	5.00	5.00	0.4844E-01	0.4844E-01
1000.00	5.00	10.00	0.1551E-01	0.1551E-01
1000.00	5.00	20.00	0.4862E-02	0.4862E-02
1000.00	5.00	50.00	0.1309E-02	0.1309E-02
1000.00	5.00	75.00	0.8419E-03	0.8419E-03
1000.00	5.00	100.00	0.6534E-03	0.6534E-03
1000.00	10.00	0.10	0.2420E+00	0.2420E+00
1000.00	10.00	0.50	0.2236E+00	0.2236E+00
1000.00	10.00	1.00	0.1814E+00	0.1814E+00
1000.00	10.00	2.00	0.1052E+00	0.1052E+00
1000.00	10.00	5.00	0.2911E-01	0.2911E-01
1000.00	10.00	10.00	0.9507E-02	0.9507E-02
1000.00	10.00	20.00	0.3438E-02	0.3438E-02
1000.00	10.00	50.00	0.1297E-02	0.1297E-02
1000.00	10.00	75.00	0.9844E-03	0.9844E-03
1000.00	10.00	100.00	0.8507E-03	0.8507E-03
2000.00	0.10	0.10	0.2411E+00	0.2444E+00
2000.00	0.10	0.50	0.2424E+00	0.2424E+00
2000.00	0.10	1.00	0.2411E+00	0.2411E+00
2000.00	0.10	2.00	0.2361E+00	0.2362E+00
2000.00	0.10	5.00	0.2060E+00	0.2064E+00
2000.00	0.10	10.00	0.1417E+00	0.1423E+00
2000.00	0.10	20.00	0.6306E-01	0.6354E-01
2000.00	0.10	50.00	0.1297E-01	0.1310E-01
2000.00	0.10	75.00	0.5966E-02	0.6025E-02
2000.00	0.10	100.00	0.3406E-02	0.3441E-02
2000.00	1.00	0.10	0.2427E+00	0.2427E+00
2000.00	1.00	0.50	0.2386E+00	0.2386E+00
2000.00	1.00	1.00	0.2267E+00	0.2267E+00
2000.00	1.00	2.00	0.1890E+00	0.1890E+00
2000.00	1.00	5.00	0.8756E-01	0.8757E-01
2000.00	1.00	10.00	0.3023E-01	0.3023E-01
2000.00	1.00	20.00	0.8471E-02	0.8472E-02
2000.00	1.00	50.00	0.1467E-02	0.1467E-02
2000.00	1.00	75.00	0.6819E-03	0.6819E-03
2000.00	1.00	100.00	0.4002E-03	0.4003E-03
2000.00	5.00	0.10	0.2420E+00	0.2420E+00
2000.00	5.00	0.50	0.2230E+00	0.2230E+00

2000.00	5.00	1.00	0.1793E+00	0.1793E+00
2000.00	5.00	2.00	0.1009E+00	0.1009E+00
2000.00	5.00	5.00	0.2535E-01	0.2535E-01
2000.00	5.00	10.00	0.7157E-02	0.7157E-02
2000.00	5.00	20.00	0.1986E-02	0.1986E-02
2000.00	5.00	50.00	0.4087E-03	0.4087E-03
2000.00	5.00	75.00	0.2212E-03	0.2212E-03
2000.00	5.00	100.00	0.1500E-03	0.1500E-03
2000.00	10.00	0.10	0.2411E+00	0.2411E+00
2000.00	10.00	0.50	0.2063E+00	0.2063E+00
2000.00	10.00	1.00	0.1425E+00	0.1425E+00
2000.00	10.00	2.00	0.6442E-01	0.6442E-01
2000.00	10.00	5.00	0.1390E-01	0.1390E-01
2000.00	10.00	10.00	0.3937E-02	0.3937E-02
2000.00	10.00	20.00	0.1173E-02	0.1173E-02
2000.00	10.00	50.00	0.2994E-03	0.2994E-03
2000.00	10.00	75.00	0.1873E-03	0.1873E-03
2000.00	10.00	100.00	0.1426E-03	0.1426E-03



```

c   This program solves for bulk temperature for CO_2
c   under gray gas assumption. The program calculates bulk
c   temperature under both LTE and NLTE condition.
c *****
  implicit double precision (a-h,o-z)
  real l,kfb
  dimension u(10),press(4),temp(4)
  data u/0.1,0.5,1.0,2.0,5.0,10.0,20.0,50.0,75.,100.0/
  data press/0.1,1.,5.,10.0/
  data temp/300.,500.,1000.0,2000.0/
  open(unit=12,file='out12.dat')
  open(unit=11,file='nlp')
  open(10,file='lp')
  write(11,13)
write(11,*) 10,1
13 format('3',/, 'x',/, 't',/, 't1',/, i4,x, '1')
  write(12,111)
  write(10,14)
  write(10,*) 10,1
14 format('2',/, 'x',/, 't',/,/, i4,x, '1')
  do 10 it=1,4
    Tw=temp(it)
  do 20 kk=1,4
    P=press(kk)
  do 30 i=1,10
    L=u(i)
c *****
c   Calculation of Plank's function and it's derivative
c   wnb Band Center
c   hck Constant
c   ccc=c1*c2
c   pfb1 Plank's Function for the ith band
c   pfd1 Derivative of Plank's Function for ith band
c *****
  tk1=tw**2
  tk2=tw**0.5
  tk3=tw/273.0
  hck=1.439257246
  ts=300.0/tw
c *****
c   Now we will consider the spectroscopic properties of co2
c   We have considered only three bands(15,4.3&2.7 microns)
c *****
  wnb1=667.0
  wnb2=2347.0
  wnb3=3716.0
  c2b1=hck*wnb1
  c2b2=hck*wnb2
  c2b3=hck*wnb3

```

```

ccc=0.000053847734
ccb1=ccc*(wnb1**4)
ccb2=ccc*(wnb2**4)
ccb3=ccc*(wnb3**4)
tb1=c2b1/tw
tb2=c2b2/tw
tb3=c2b3/tw
teb1=exp(tb1)
teb2=exp(tb2)
teb3=exp(tb3)
c1b1=ccb1/c2b1
c1b2=ccb2/c2b2
c1b3=ccb3/c2b3
pfb1=c1b1/(teb1-1.0)
pfb2=c1b2/(teb2-1.0)
pfb3=c1b3/(teb3-1.0)
dev1=tk1*((teb1-1.0)**2.0)
dev2=tk1*((teb2-1.0)**2.0)
dev3=tk1*((teb3-1.0)**2.0)
pfdb1=(ccb1*teb1)/dev1
pfdb2=(ccb2*teb2)/dev2
pfdb3=(ccb3*teb3)/dev3

```

```

c*****
c Band Model Correlations(Tien & Lowder wide band model)
c azi aoi is band width parameter
c czsi=coi**2 coi is correlation parameter
c bsi=b**2 is non dimensional quantity
c omegi is wave number
c si is integrated band intensity
c*****

```

```

ak1=(tw/300.0)**0.5
ak2=(300.0/tw)**1.5
az1=1.29*tk2
az2=1.15*tk2
az3=2.4*tk2
kfb=(1488.365171)*(tk3**1.23)
omeg1=1351.0
omeg2=667.0
omeg3=2396.0
tx=-(hck/tw)
tx1=tx*omeg1
tx2=tx*omeg2
tx3=tx*omeg3
ctx1=exp(tx1)
ctx2=exp(tx2)
ctx3=exp(tx3)
c1=1.0-ctx1
c2=1.0-ctx2

```

```

c3=1.0-ctc3
brkt=tx*(omeg1+omeg3)
phi2=(1.0-exp(brkt))/(c1*c3)
ts=300.0/tw
s1=339.685*ts
s2=2702.7*ts
s3=71.497*ts*phi2
ETC1=((36.5*(TW**(-1/3.)))+3.9)
ETC2=EXP(ETC1)*(1.E-6)
ETAC=ETC2/P
ETR11=8.*3.14*(667.**2.))*4.08*(1.E-12)*300.*339.685
ETAR1=1./ETR11
ETR12=8.*3.14*(2347.**2.))*4.08*(1.E-12)*300.*2702.7
ETAR2=1./ETR12
ETR13=8.*3.14*(3716.**2.))*4.08*(1.E-12)*300.*71.497*PHI2
ETAR3=1./ETR13
ETA11=ETAC/ETAR1
ETA12=ETAC/ETAR2
ETA13=ETAC/ETAR3
aap1=eta11/s1
aap2=eta12/s2
aap3=eta13/s3
aapx1=(3./4.)*(aap1)/p
aapx2=(3./4.)*(aap2)/p
aapx3=(3./4.)*(aap3)/p
am2=1.+(aapx1+aapx2+aapx3)
tin=p*1**2.0/kfb*(s1*pfdb1+s2*pfdb2+s3*pfdb3)
tn=exp(-(3.0*tin)**0.5)
anexp=(1.0-tn)/(1.0+tn)
tcm=1/kfb*(pfdb1*az1+pfdb2*az2+pfdb3*az3)
ala=0.00005668
akp=p/(ala*tw**4.0)*(s1*pfb1+s2*pfb2+s3*pfb3)
tao=akp*1
anba=kfb*akp/(4.0*ala*tw**3.0)
r=3.0*tao**2.0/anba
aim=3.0*tao**2.0*(0.75+1.0/anba)
am=sqrt(aim)
cm=exp(-am)
ad=3.0*tao*(1.0-cm)+2.0*am*(1.0+cm)
ac=r/am**8.0*(48.0-3.0*tao*am**2.0+36.0*tao)/ad
pa1=24.0-12.0*am+am**3.0+(am**3.0-12.0*am-24.0)*cm
pa2=-12.0*r/(5.0*am**4.0)+17.0*r/(70.0*am**2.0)
ambar=am/(sqrt(am2))
rbar=r/am2
embar=exp(-ambar)
adbar=3.0*tao*(1.0-embar)+2.0*ambar*(1.0+embar)
acbar=(rbar/(ambar**8.))*(48.-3.*tao*(ambar**
* 2.0)+36.0*tao)/adbar
pa1bar=24.0-12.0*ambar+ambar**3.0

```

```

* +(ambar**3.0-12.0*ambar-24.0)*embar
pa2bar=-12.0*rbar/(5.0*ambar**4.0)+
* 17.0*rbar/(70.0*ambar**2.0)
tbulk=c*pa1+pa2-17.0/70.0
tbulkn=acbar*pa1bar+pa2bar-17.0/70.0
write(12,200)tw,p,l,-tbulk,-tbulkn
write(11,202)l,-tbulk,-tbulkn
write(10,203)l,-tbulkn
111 format(4x,'tw',8x,'p',6x,'l',9x,'tbulk',9x,'tbulkn')
30 continue
20 continue
10 continue
202 format(1x,f9.2,2(3x,e10.4))
203 format(1x,f9.2,3x,e10.4)
200 format(8x,f7.2,3x,f6.2,3x,f6.2,3x,e10.4,3x,e10.4)
stop
end

```

## GRAY GAS RESULTS FOR CO<sub>2</sub>

tw	p	l	tbulk (LTE)	tbulkn (NLTE)
300.00	0.10	0.10	0.2428E+00	0.2428E+00
300.00	0.10	0.50	0.2403E+00	0.2412E+00
300.00	0.10	1.00	0.2331E+00	0.2364E+00
300.00	0.10	2.00	0.2087E+00	0.2193E+00
300.00	0.10	5.00	0.1242E+00	0.1492E+00
300.00	0.10	10.00	0.5514E-01	0.7461E-01
300.00	0.10	20.00	0.2053E-01	0.2913E-01
300.00	0.10	50.00	0.6530E-02	0.8836E-02
300.00	0.10	75.00	0.4521E-02	0.5834E-02
300.00	0.10	100.00	0.3687E-02	0.4583E-02
300.00	1.00	0.10	0.2418E+00	0.2418E+00
300.00	1.00	0.50	0.2217E+00	0.2218E+00
300.00	1.00	1.00	0.1810E+00	0.1813E+00
300.00	1.00	2.00	0.1158E+00	0.1161E+00
300.00	1.00	5.00	0.5112E-01	0.5127E-01
300.00	1.00	10.00	0.3134E-01	0.3140E-01
300.00	1.00	20.00	0.2355E-01	0.2357E-01
300.00	1.00	50.00	0.1982E-01	0.1983E-01
300.00	1.00	75.00	0.1910E-01	0.1910E-01
300.00	1.00	100.00	0.1875E-01	0.1876E-01
300.00	5.00	0.10	0.2383E+00	0.2383E+00
300.00	5.00	0.50	0.1854E+00	0.1855E+00
300.00	5.00	1.00	0.1376E+00	0.1377E+00
300.00	5.00	2.00	0.1014E+00	0.1015E+00
300.00	5.00	5.00	0.7995E-01	0.7995E-01
300.00	5.00	10.00	0.7389E-01	0.7389E-01
300.00	5.00	20.00	0.7119E-01	0.7120E-01
300.00	5.00	50.00	0.6970E-01	0.6970E-01
300.00	5.00	75.00	0.6939E-01	0.6939E-01
300.00	5.00	100.00	0.6923E-01	0.6923E-01
300.00	10.00	0.10	0.2348E+00	0.2348E+00
300.00	10.00	0.50	0.1755E+00	0.1755E+00
300.00	10.00	1.00	0.1426E+00	0.1426E+00
300.00	10.00	2.00	0.1234E+00	0.1234E+00
300.00	10.00	5.00	0.1129E+00	0.1129E+00
300.00	10.00	10.00	0.1099E+00	0.1099E+00
300.00	10.00	20.00	0.1085E+00	0.1085E+00
300.00	10.00	50.00	0.1077E+00	0.1077E+00
300.00	10.00	75.00	0.1075E+00	0.1075E+00
300.00	10.00	100.00	0.1074E+00	0.1074E+00
500.00	0.10	0.10	0.2426E+00	0.2427E+00
500.00	0.10	0.50	0.2369E+00	0.2385E+00
500.00	0.10	1.00	0.2210E+00	0.2265E+00
500.00	0.10	2.00	0.1751E+00	0.1894E+00

500.00	0.10	5.00	0.7442E-01	0.9157E-01
500.00	0.10	10.00	0.2671E-01	0.3500E-01
500.00	0.10	20.00	0.9026E-02	0.1195E-01
500.00	0.10	50.00	0.2722E-02	0.3442E-02
500.00	0.10	75.00	0.1854E-02	0.2260E-02
500.00	0.10	100.00	0.1497E-02	0.1773E-02
500.00	1.00	0.10	0.2405E+00	0.2405E+00
500.00	1.00	0.50	0.1980E+00	0.1981E+00
500.00	1.00	1.00	0.1340E+00	0.1342E+00
500.00	1.00	2.00	0.6695E-01	0.6711E-01
500.00	1.00	5.00	0.2407E-01	0.2413E-01
500.00	1.00	10.00	0.1378E-01	0.1380E-01
500.00	1.00	20.00	0.9968E-02	0.9978E-02
500.00	1.00	50.00	0.8174E-02	0.8178E-02
500.00	1.00	75.00	0.7828E-02	0.7831E-02
500.00	1.00	100.00	0.7663E-02	0.7665E-02
500.00	5.00	0.10	0.2323E+00	0.2323E+00
500.00	5.00	0.50	0.1391E+00	0.1391E+00
500.00	5.00	1.00	0.8487E-01	0.8487E-01
500.00	5.00	2.00	0.5473E-01	0.5474E-01
500.00	5.00	5.00	0.3961E-01	0.3961E-01
500.00	5.00	10.00	0.3557E-01	0.3557E-01
500.00	5.00	20.00	0.3378E-01	0.3378E-01
500.00	5.00	50.00	0.3279E-01	0.3279E-01
500.00	5.00	75.00	0.3258E-01	0.3258E-01
500.00	5.00	100.00	0.3248E-01	0.3248E-01
500.00	10.00	0.10	0.2246E+00	0.2246E+00
500.00	10.00	0.50	0.1254E+00	0.1254E+00
500.00	10.00	1.00	0.8858E-01	0.8858E-01
500.00	10.00	2.00	0.7075E-01	0.7075E-01
500.00	10.00	5.00	0.6172E-01	0.6172E-01
500.00	10.00	10.00	0.5914E-01	0.5914E-01
500.00	10.00	20.00	0.5794E-01	0.5794E-01
500.00	10.00	50.00	0.5726E-01	0.5726E-01
500.00	10.00	75.00	0.5711E-01	0.5711E-01
500.00	10.00	100.00	0.5703E-01	0.5703E-01
1000.00	0.10	0.10	0.2423E+00	0.2424E+00
1000.00	0.10	0.50	0.2290E+00	0.2319E+00
1000.00	0.10	1.00	0.1957E+00	0.2046E+00
1000.00	0.10	2.00	0.1247E+00	0.1399E+00
1000.00	0.10	5.00	0.3655E-01	0.4510E-01
1000.00	0.10	10.00	0.1113E-01	0.1411E-01
1000.00	0.10	20.00	0.3381E-02	0.4294E-02
1000.00	0.10	50.00	0.8649E-03	0.1068E-02
1000.00	0.10	75.00	0.5404E-03	0.6509E-03
1000.00	0.10	100.00	0.4109E-03	0.4844E-03
1000.00	1.00	0.10	0.2371E+00	0.2372E+00
1000.00	1.00	0.50	0.1552E+00	0.1553E+00
1000.00	1.00	1.00	0.7859E-01	0.7874E-01

1000.00	1.00	2.00	0.2981E-01	0.2988E-01
1000.00	1.00	5.00	0.8251E-02	0.8270E-02
1000.00	1.00	10.00	0.3977E-02	0.3984E-02
1000.00	1.00	20.00	0.2516E-02	0.2518E-02
1000.00	1.00	50.00	0.1867E-02	0.1868E-02
1000.00	1.00	75.00	0.1746E-02	0.1747E-02
1000.00	1.00	100.00	0.1689E-02	0.1690E-02
1000.00	5.00	0.10	0.2182E+00	0.2182E+00
1000.00	5.00	0.50	0.7878E-01	0.7879E-01
1000.00	5.00	1.00	0.3574E-01	0.3575E-01
1000.00	5.00	2.00	0.1824E-01	0.1824E-01
1000.00	5.00	5.00	0.1078E-01	0.1078E-01
1000.00	5.00	10.00	0.8946E-02	0.8946E-02
1000.00	5.00	20.00	0.8161E-02	0.8161E-02
1000.00	5.00	50.00	0.7733E-02	0.7733E-02
1000.00	5.00	75.00	0.7643E-02	0.7643E-02
1000.00	5.00	100.00	0.7598E-02	0.7598E-02
1000.00	10.00	0.10	0.2008E+00	0.2008E+00
1000.00	10.00	0.50	0.6196E-01	0.6196E-01
1000.00	10.00	1.00	0.3354E-01	0.3354E-01
1000.00	10.00	2.00	0.2230E-01	0.2230E-01
1000.00	10.00	5.00	0.1713E-01	0.1713E-01
1000.00	10.00	10.00	0.1573E-01	0.1573E-01
1000.00	10.00	20.00	0.1509E-01	0.1509E-01
1000.00	10.00	50.00	0.1472E-01	0.1472E-01
1000.00	10.00	75.00	0.1464E-01	0.1464E-01
1000.00	10.00	100.00	0.1460E-01	0.1460E-01
2000.00	0.10	0.10	0.2424E+00	0.2425E+00
2000.00	0.10	0.50	0.2330E+00	0.2350E+00
2000.00	0.10	1.00	0.2077E+00	0.2144E+00
2000.00	0.10	2.00	0.1450E+00	0.1587E+00
2000.00	0.10	5.00	0.4695E-01	0.5673E-01
2000.00	0.10	10.00	0.1395E-01	0.1747E-01
2000.00	0.10	20.00	0.3767E-02	0.4768E-02
2000.00	0.10	50.00	0.6748E-03	0.8551E-03
2000.00	0.10	75.00	0.3264E-03	0.4125E-03
2000.00	0.10	100.00	0.1995E-03	0.2512E-03
2000.00	1.00	0.10	0.2388E+00	0.2388E+00
2000.00	1.00	0.50	0.1713E+00	0.1715E+00
2000.00	1.00	1.00	0.9190E-01	0.9205E-01
2000.00	1.00	2.00	0.3301E-01	0.3308E-01
2000.00	1.00	5.00	0.6569E-02	0.6586E-02
2000.00	1.00	10.00	0.1974E-02	0.1980E-02
2000.00	1.00	20.00	0.6813E-03	0.6829E-03
2000.00	1.00	50.00	0.2422E-03	0.2426E-03
2000.00	1.00	75.00	0.1794E-03	0.1796E-03
2000.00	1.00	100.00	0.1527E-03	0.1529E-03
2000.00	5.00	0.10	0.2241E+00	0.2241E+00
2000.00	5.00	0.50	0.8214E-01	0.8215E-01

2000.00	5.00	1.00	0.2956E-01	0.2957E-01
2000.00	5.00	2.00	0.9516E-02	0.9516E-02
2000.00	5.00	5.00	0.2492E-02	0.2493E-02
2000.00	5.00	10.00	0.1196E-02	0.1196E-02
2000.00	5.00	20.00	0.7565E-03	0.7566E-03
2000.00	5.00	50.00	0.5606E-03	0.5606E-03
2000.00	5.00	75.00	0.5241E-03	0.5241E-03
2000.00	5.00	100.00	0.5067E-03	0.5067E-03
2000.00	10.00	0.10	0.2086E+00	0.2086E+00
2000.00	10.00	0.50	0.5266E-01	0.5266E-01
2000.00	10.00	1.00	0.1826E-01	0.1826E-01
2000.00	10.00	2.00	0.6567E-02	0.6567E-02
2000.00	10.00	5.00	0.2366E-02	0.2367E-02
2000.00	10.00	10.00	0.1501E-02	0.1501E-02
2000.00	10.00	20.00	0.1173E-02	0.1173E-02
2000.00	10.00	50.00	0.1010E-02	0.1010E-02
2000.00	10.00	75.00	0.9770E-03	0.9770E-03
2000.00	10.00	100.00	0.9611E-03	0.9611E-03



C Program to calculate LTE and NLTE bulk temp. under gray

c gas assumption for H<sub>2</sub>O

implicit double precision (a-h,o-z)

real l,kfb

dimension u(10),press(4),Temp(4)

data u/0.1,0.5,1.0,2.0,5.0,10.0,20.0,50.0,75.,100.0/

data press/0.1,1.0,5.,10.0/

data temp/300.,500.,1000.0,2000.0/

open(unit=25, file='nlp')

open(unit=26, file='lp')

open(unit=27, file='out27.dat')

write(27,230)

write(25,13)

write(25,\*) 10,1

13 format('3',/, 'x',/, 't',/, 't1',/,i4,x,'1')

write(26,14)

write(26,\*) 10,1

14 format('2',/, 'x',/, 't',/,/,i4,x,'1')

do 101 it=1,4

tw=temp(it)

do 202 kk=1,4

p=press(kk)

do 303 i=1,10

l=u(i)

c

c Calculation of Plank's Function and it's derivative

c wnb Band Center

c hck Constant

c ccc c1\*c2 (erg\_k\_cm\*\*3/sec)

c pfdbi Plank's Function's derivative for ith band

c

tk1=tw\*\*2

tk2=tw\*\*0.5

tk3=tw/273.0

hck=1.439257246

ts=300.0/tw

c

c Spectroscopic Properties of H<sub>2</sub>O

c Five Bands of H<sub>2</sub>O are considered(I.R,6.3,2.7,1.87,1.38 microns)

c wnb<sub>i</sub> Band Center (1/cm)

c

wnb1=500.

wnb2=1600.

wnb3=3750.

wnb4=5350.

wnb5=7250.

c2b1=hck\*wnb1

c2b2=hck\*wnb2

c2b3=hck\*wnb3

```

c2b4=hck*wnb4
c2b5=hck*wnb5
ccc=0.000053847734
ccb1=ccc*(wnb1**4)
ccb2=ccc*(wnb2**4)
ccb3=ccc*(wnb3**4)
ccb4=ccc*(wnb4**4)
ccb5=ccc*(wnb5**4)
tb1=c2b1/tw
tb2=c2b2/tw
tb3=c2b3/tw
tb4=c2b4/tw
tb5=c2b5/tw
teb1=exp(tb1)
teb2=exp(tb2)
teb3=exp(tb3)
teb4=exp(tb4)
teb5=exp(tb5)
c1b1=ccb1/c2b1
c1b2=ccb2/c2b2
c1b3=ccb3/c2b3
c1b4=ccb4/c2b4
c1b5=ccb5/c2b5
pfb1=c1b1/(teb1-1.0)
pfb2=c1b2/(teb2-1.0)
pfb3=c1b3/(teb3-1.0)
pfb4=c1b4/(teb4-1.0)
pfb5=c1b5/(teb5-1.0)
dev1=tk1*((teb1-1.0)**2.0)
dev2=tk1*((teb2-1.0)**2.0)
dev3=tk1*((teb3-1.0)**2.0)
dev4=tk1*((teb4-1.0)**2.0)
dev5=tk1*((teb5-1.0)**2.0)
pfdb1=(ccb1*teb1)/dev1
pfdb2=(ccb2*teb2)/dev2
pfdb3=(ccb3*teb3)/dev3
pfdb4=(ccb4*teb4)/dev4
pfdb5=(ccb5*teb5)/dev5

```

---

c Band Model Correlations (Tien & Lowder Wide Band Model)

```

c azi aoi (1/cm)
c czsi coi**2 (1/atm-cm)
c bsi b**2 (Nondimensional)
c omegi Wave Number (1/cm)
c si Integrated Band Intensity (1/atm cm**2)

```

---

```

ak1=(tw/300.)**0.5
ak2=(300./tw)**1.5
az1=49.4*ak1

```

az2=90.1\*ak1  
az3=112.6\*ak1  
az4=79.7\*ak1  
az5=79.7\*ak1

---

c dkf Thermal Conductivity (Erg/cm-sec-k)

---

kfb=(1488.365171)\*(tk3\*\*1.23)  
omeg1=3652.  
omeg2=1595.  
omeg3=3756.  
tx=-(hck/tw)  
tx1=tx\*omeg1  
tx2=tx\*omeg2  
tx3=tx\*omeg3  
etx1=exp(tx1)  
etx2=exp(tx2)  
etx3=exp(tx3)  
c1=1.0-etx1  
c2=1.0-etx2  
c3=1.0-etx3  
brkt=tx\*(omeg1+omeg3)  
ph101=(1.0-exp(brkt))/c1\*c2\*c3  
ts1=(tw/100.)\*\*(-0.5)  
phi7=exp(-17.6\*ts1)  
co1=771.\*ak2\*phi7  
co2=3.35\*ak2  
co3=1.52\*ak2  
co4=0.276\*ak2\*ph101  
co5=0.230\*ak2\*ph101  
s1=az1\*co1  
s2=az2\*co2  
s3=az3\*co3  
s4=az4\*co4  
s5=az5\*co5  
ETC1=((36.5\*(TW\*\*(-1/3.)))+3.9)  
ETC2=EXP(ETC1)\*(1.E-6)  
ETAC=ETC2/P  
ETR11=8.\*3.14\*(500.\*\*2)\*\*4.08\*(1.E-12)\*s1\*tw  
ETAR1=1./ETR11  
ETR12=8.\*3.14\*(1600.\*\*2)\*\*4.08\*(1.E-12)\*s2\*tw  
ETAR2=1./ETR12  
ETR13=8.\*3.14\*(3750.\*\*2)\*\*4.08\*(1.E-12)\*s3\*tw  
ETAR3=1./ETR13  
ETR14=8.\*3.14\*(5350.\*\*2)\*\*4.08\*(1.E-12)\*s4\*tw  
ETAR4=1./ETR14  
ETR15=8.\*3.14\*(7250.\*\*2)\*\*4.08\*(1.E-12)\*s5\*tw  
ETAR5=1./ETR15  
ETA11=ETAC/ETAR1

```

ETA12=ETAC/ETAR2
ETA13=ETAC/ETAR3
ETA14=ETAC/ETAR4
ETA15=ETAC/ETAR5
aap1=eta11/s1
aap2=eta12/s2
aap3=eta13/s3
aap4=eta14/s4
aap5=eta15/s5
aap6=eta16/s6
aapx1=(3./4.)*(aap1)/p
aapx2=(3./4.)*(aap2)/p
aapx3=(3./4.)*(aap3)/p
aapx4=(3./4.)*(aap4)/p
aapx5=(3./4.)*(aap5)/p
am2=1.+(aapx1+aapx2+aapx3+aapx4+aapx5)
tin=p*1**2./kfb*(s1*pfdb1+s2*pfdb2+s3*pfdb3+s4*pfdb4+s5*pfdb5)
tn=exp(-(3.*tin)**0.5)
ala=0.00005668
akp=p/(ala*tw**4.)*(s1*pfb1+s2*pfb2+s3*pfb3+s4*pfb4+s5*pfb5)
tao=akp*I
anba=kfb*akp/(4.*ala*tw**3.)
r=3.*tao**2./anba
a1m=3.*tao**2.*(0.75+1./anba)
am=sqrt(a1m)
em=exp(-am)
ad=3.*tao*(1.-em)+2.*am*(1.+em)
ac=r/am**8.*(48.-3.*tao*am**2.+36.*tao)/ad
pa1=24.-12.*am+am**3.+(am**3.-12.*am-24.)*em
pa2=-12.*r/(5.*am**4.)+17.*r/(70.*am**2.)
ambar=am/(sqrt(am2))
rbar=r/am2
embar=exp(-ambar)
adbar=3.0*tao*(1.0-embar)+2.0*ambar*(1.0+embar)
acbar=(rbar/(ambar**8.))*(48.-3.*tao*(ambar**
* 2.0)+36.0*tao)/adbar
pa1bar=24.0-12.0*ambar+ambar**3.0
* +(ambar**3.0-12.0*ambar-24.0)*embar
pa2bar=-12.0*rbar/(5.0*ambar**4.0)+
* 17.0*rbar/(70.0*ambar**2.0)
tbulk=ac*pa1+pa2-17./70.
tbulkn=acbar*pa1bar+pa2bar-17.0/70.0
write(25,100)l,-tbulk,-tbulkn
write(26,104)l,-tbulkn
write(27,1000)tw,p,l,-tbulk,-tbulkn
100 format(1x,f9.2,2(3x,e10.4))
104 format(1x,f9.2,3x,e10.4)
303 continue
202 continue

```

```
101 continue
1000 format (1x,f7.2, 3x,f6.2, 3x,f6.2, 3x,e10.4, 3x,e10.4)
230 format (4x,'tw',8x,'p',6x,'l',9x,'bulk',9x,'bulkn')
  stop
  end
```

## GRAY GAS RESULTS FOR H<sub>2</sub>O

tw	p	l	tbulk (LTE)	tbulkn (NLTE)
300.00	0.10	0.10	0.2411E+00	-.6838E+00
300.00	0.10	0.50	0.2425E+00	0.2428E+00
300.00	0.10	1.00	0.2416E+00	0.2425E+00
300.00	0.10	2.00	0.2378E+00	0.2414E+00
300.00	0.10	5.00	0.2145E+00	0.2343E+00
300.00	0.10	10.00	0.1596E+00	0.2122E+00
300.00	0.10	20.00	0.8027E-01	0.1554E+00
300.00	0.10	50.00	0.1931E-01	0.5723E-01
300.00	0.10	75.00	0.9650E-02	0.3096E-01
300.00	0.10	100.00	0.5941E-02	0.1953E-01
300.00	1.00	0.10	0.2427E+00	0.2427E+00
300.00	1.00	0.50	0.2397E+00	0.2398E+00
300.00	1.00	1.00	0.2308E+00	0.2311E+00
300.00	1.00	2.00	0.2019E+00	0.2028E+00
300.00	1.00	5.00	0.1124E+00	0.1139E+00
300.00	1.00	10.00	0.4836E-01	0.4932E-01
300.00	1.00	20.00	0.1849E-01	0.1888E-01
300.00	1.00	50.00	0.6534E-02	0.6638E-02
300.00	1.00	75.00	0.4775E-02	0.4835E-02
300.00	1.00	100.00	0.4032E-02	0.4074E-02
300.00	5.00	0.10	0.2422E+00	0.2422E+00
300.00	5.00	0.50	0.2286E+00	0.2286E+00
300.00	5.00	1.00	0.1971E+00	0.1971E+00
300.00	5.00	2.00	0.1344E+00	0.1344E+00
300.00	5.00	5.00	0.5559E-01	0.5563E-01
300.00	5.00	10.00	0.2880E-01	0.2882E-01
300.00	5.00	20.00	0.1846E-01	0.1847E-01
300.00	5.00	50.00	0.1379E-01	0.1380E-01
300.00	5.00	75.00	0.1294E-01	0.1294E-01
300.00	5.00	100.00	0.1254E-01	0.1254E-01
300.00	10.00	0.10	0.2416E+00	0.2416E+00
300.00	10.00	0.50	0.2176E+00	0.2176E+00
300.00	10.00	1.00	0.1730E+00	0.1730E+00
300.00	10.00	2.00	0.1087E+00	0.1087E+00
300.00	10.00	5.00	0.5097E-01	0.5097E-01
300.00	10.00	10.00	0.3390E-01	0.3390E-01
300.00	10.00	20.00	0.2708E-01	0.2708E-01
300.00	10.00	50.00	0.2373E-01	0.2373E-01
300.00	10.00	75.00	0.2307E-01	0.2307E-01
300.00	10.00	100.00	0.2275E-01	0.2275E-01
500.00	0.10	0.10	0.2428E+00	0.2440E+00
500.00	0.10	0.50	0.2415E+00	0.2424E+00
500.00	0.10	1.00	0.2374E+00	0.2409E+00
500.00	0.10	2.00	0.2225E+00	0.2353E+00

500.00	0.10	5.00	0.1555E+00	0.2029E+00
500.00	0.10	10.00	0.7613E-01	0.1373E+00
500.00	0.10	20.00	0.2607E-01	0.6176E-01
500.00	0.10	50.00	0.5344E-02	0.1431E-01
500.00	0.10	75.00	0.2731E-02	0.7301E-02
500.00	0.10	100.00	0.1750E-02	0.4598E-02
500.00	1.00	0.10	0.2423E+00	0.2423E+00
500.00	1.00	0.50	0.2299E+00	0.2302E+00
500.00	1.00	1.00	0.1992E+00	0.1999E+00
500.00	1.00	2.00	0.1325E+00	0.1336E+00
500.00	1.00	5.00	0.4434E-01	0.4499E-01
500.00	1.00	10.00	0.1623E-01	0.1648E-01
500.00	1.00	20.00	0.6705E-02	0.6794E-02
500.00	1.00	50.00	0.3095E-02	0.3120E-02
500.00	1.00	75.00	0.2531E-02	0.2547E-02
500.00	1.00	100.00	0.2284E-02	0.2294E-02
500.00	5.00	0.10	0.2402E+00	0.2402E+00
500.00	5.00	0.50	0.1937E+00	0.1937E+00
500.00	5.00	1.00	0.1279E+00	0.1280E+00
500.00	5.00	2.00	0.6349E-01	0.6352E-01
500.00	5.00	5.00	0.2389E-01	0.2390E-01
500.00	5.00	10.00	0.1439E-01	0.1440E-01
500.00	5.00	20.00	0.1082E-01	0.1082E-01
500.00	5.00	50.00	0.9109E-02	0.9110E-02
500.00	5.00	75.00	0.8775E-02	0.8776E-02
500.00	5.00	100.00	0.8615E-02	0.8615E-02
500.00	10.00	0.10	0.2377E+00	0.2377E+00
500.00	10.00	0.50	0.1676E+00	0.1676E+00
500.00	10.00	1.00	0.1005E+00	0.1005E+00
500.00	10.00	2.00	0.5236E-01	0.5236E-01
500.00	10.00	5.00	0.2684E-01	0.2684E-01
500.00	10.00	10.00	0.2052E-01	0.2052E-01
500.00	10.00	20.00	0.1794E-01	0.1794E-01
500.00	10.00	50.00	0.1659E-01	0.1659E-01
500.00	10.00	75.00	0.1632E-01	0.1632E-01
500.00	10.00	100.00	0.1618E-01	0.1618E-01
1000.00	0.10	0.10	0.2428E+00	0.2432E+00
1000.00	0.10	0.50	0.2407E+00	0.2419E+00
1000.00	0.10	1.00	0.2343E+00	0.2393E+00
1000.00	0.10	2.00	0.2120E+00	0.2291E+00
1000.00	0.10	5.00	0.1275E+00	0.1770E+00
1000.00	0.10	10.00	0.5309E-01	0.9832E-01
1000.00	0.10	20.00	0.1624E-01	0.3602E-01
1000.00	0.10	50.00	0.2962E-02	0.7045E-02
1000.00	0.10	75.00	0.1409E-02	0.3364E-02
1000.00	0.10	100.00	0.8444E-03	0.2009E-02
1000.00	1.00	0.10	0.2420E+00	0.2420E+00
1000.00	1.00	0.50	0.2227E+00	0.2230E+00
1000.00	1.00	1.00	0.1789E+00	0.1796E+00

1000.00	1.00	2.00	0.1013E+00	0.1022E+00
1000.00	1.00	5.00	0.2663E-01	0.2696E-01
1000.00	1.00	10.00	0.8157E-02	0.8266E-02
1000.00	1.00	20.00	0.2648E-02	0.2682E-02
1000.00	1.00	50.00	0.8082E-03	0.8164E-03
1000.00	1.00	75.00	0.5571E-03	0.5618E-03
1000.00	1.00	100.00	0.4535E-03	0.4566E-03
1000.00	5.00	0.10	0.2385E+00	0.2385E+00
1000.00	5.00	0.50	0.1697E+00	0.1697E+00
1000.00	5.00	1.00	0.9245E-01	0.9248E-01
1000.00	5.00	2.00	0.3581E-01	0.3582E-01
1000.00	5.00	5.00	0.9158E-02	0.9162E-02
1000.00	5.00	10.00	0.3939E-02	0.3941E-02
1000.00	5.00	20.00	0.2225E-02	0.2225E-02
1000.00	5.00	50.00	0.1501E-02	0.1501E-02
1000.00	5.00	75.00	0.1371E-02	0.1371E-02
1000.00	5.00	100.00	0.1311E-02	0.1311E-02
1000.00	10.00	0.10	0.2345E+00	0.2345E+00
1000.00	10.00	0.50	0.1339E+00	0.1339E+00
1000.00	10.00	1.00	0.6233E-01	0.6233E-01
1000.00	10.00	2.00	0.2382E-01	0.2382E-01
1000.00	10.00	5.00	0.7691E-02	0.7692E-02
1000.00	10.00	10.00	0.4375E-02	0.4375E-02
1000.00	10.00	20.00	0.3171E-02	0.3171E-02
1000.00	10.00	50.00	0.2600E-02	0.2600E-02
1000.00	10.00	75.00	0.2489E-02	0.2489E-02
1000.00	10.00	100.00	0.2436E-02	0.2436E-02
2000.00	0.10	0.10	0.2428E+00	0.2434E+00
2000.00	0.10	0.50	0.2411E+00	0.2421E+00
2000.00	0.10	1.00	0.2358E+00	0.2398E+00
2000.00	0.10	2.00	0.2169E+00	0.2311E+00
2000.00	0.10	5.00	0.1390E+00	0.1843E+00
2000.00	0.10	10.00	0.6106E-01	0.1071E+00
2000.00	0.10	20.00	0.1892E-01	0.4021E-01
2000.00	0.10	50.00	0.3297E-02	0.7603E-02
2000.00	0.10	75.00	0.1498E-02	0.3488E-02
2000.00	0.10	100.00	0.8576E-03	0.2003E-02
2000.00	1.00	0.10	0.2421E+00	0.2421E+00
2000.00	1.00	0.50	0.2260E+00	0.2262E+00
2000.00	1.00	1.00	0.1871E+00	0.1877E+00
2000.00	1.00	2.00	0.1112E+00	0.1120E+00
2000.00	1.00	5.00	0.2936E-01	0.2970E-01
2000.00	1.00	10.00	0.8305E-02	0.8413E-02
2000.00	1.00	20.00	0.2259E-02	0.2289E-02
2000.00	1.00	50.00	0.4344E-03	0.4400E-03
2000.00	1.00	75.00	0.2232E-03	0.2259E-03
2000.00	1.00	100.00	0.1444E-03	0.1462E-03
2000.00	5.00	0.10	0.2393E+00	0.2393E+00
2000.00	5.00	0.50	0.1774E+00	0.1774E+00



2000.00	5.00	1.00	0.9891E-01	0.9894E-01
2000.00	5.00	2.00	0.3650E-01	0.3651E-01
2000.00	5.00	5.00	0.7279E-02	0.7283E-02
2000.00	5.00	10.00	0.2152E-02	0.2153E-02
2000.00	5.00	20.00	0.7182E-03	0.7185E-03
2000.00	5.00	50.00	0.2391E-03	0.2392E-03
2000.00	5.00	75.00	0.1721E-03	0.1721E-03
2000.00	5.00	100.00	0.1439E-03	0.1439E-03
2000.00	10.00	0.10	0.2358E+00	0.2358E+00
2000.00	10.00	0.50	0.1406E+00	0.1406E+00
2000.00	10.00	1.00	0.6344E-01	0.6344E-01
2000.00	10.00	2.00	0.2080E-01	0.2081E-01
2000.00	10.00	5.00	0.4259E-02	0.4259E-02
2000.00	10.00	10.00	0.1429E-02	0.1429E-02
2000.00	10.00	20.00	0.5954E-03	0.5954E-03
2000.00	10.00	50.00	0.2870E-03	0.2870E-03
2000.00	10.00	75.00	0.2381E-03	0.2381E-03
2000.00	10.00	100.00	0.2164E-03	0.2164E-03

c Program to calculate LTE and NLTE bulk temp. under gray

c gas assumption for CH<sub>4</sub>

implicit double precision (a-h,o-z)

real l,kfb

dimension u(10),press(4),Temp(4)

data u/0.1,0.5,1.0,2.0,5.0,10.0,20.0,50.0,75.,100.0/

data press/0.1,1.,5.,10.0/

data temp/300.,500.,1000.0,2000.0/

open(unit=29, file='nlp')

open(unit=30, file='lp')

open(unit=31, file='out31.dat')

write(31,230)

write(29,13)

write(29,\*) 10,1

13 format('3','x','t','t1',/i4,x,'1')

write(30,14)

write(30,\*) 10,1

14 format('2','x','t',/i4,x,'1')

do 101 it=1,4

tw=temp(it)

do 202 kk=1,4

p=press(kk)

do 303 i=1,10

l=u(i)

---

c Calculation of Plank's Function and it's derivative

c wnb Band Center

c hck Constant

c ccc  $c_1 \cdot c_2$  (erg\_k\_cm\*\*3/sec)

c pfdbi Plank's Function's derivative for ith band

---

c

tk1=tw\*\*2

tk2=tw\*\*0.5

tk3=tw/273.0

hck=1.439257246

ts=300.0/tw

---

c

c Spectroscopic Properties of CH<sub>4</sub>

c Two Bands of CH<sub>4</sub> are considered(7.6 and 3.3 microns)

c wnb<sub>i</sub> Band Center (1/cm)

---

c

wnb1=1310.

wnb2=3020.

c2b1=hck\*wnb1

c2b2=hck\*wnb2

ccc=0.000053847734

ccb1=ccc\*(wnb1\*\*4)

ccb2=ccc\*(wnb2\*\*4)

tb1=c2b1/tw

```

tb2=c2b2/tw
teb1= exp(tb1)
teb2= exp(tb2)
c1b1=ccb1/c2b1
c1b2=ccb2/c2b2
pfb1=c1b1/(teb1-1.0)
pfb2=c1b2/(teb2-1.0)
dev1=tk1*((teb1-1.0)**2.0)
dev2=tk1*((teb2-1.0)**2.0)
pfdb1=(ccb1*teb1)/dev1
pfdb2=(ccb2*teb2)/dev2

```

---

Band Model Correlations (Tien & Lowder wide band model)

```

c azi aoi (1/cm)
c czsi coi**2 (1/atm-cm)
c bsi b**2 (Nondimensional)
c omegi Wave Number (1/cm)
c si Integrated Band Intensity (1/atm cm**2)

```

---

```

ak1=(tw/300.)**0.5
ak2=(300./tw)**1.5
az1=39.8*ak1
az2=95.3*ak1

```

---

c dkf Thermal Conductivity (Erg/cm-sec-k)

---

```

kfb=(1488.365171)*(tk3**1.23)
c01=4.58*ak2
c02=3.15*ak2
s1=az1*c01
s2=az2*c02
ETC1=((40.*(TW**(-1/3.)))-5.4)
ETC2=EXP(ETC1)*(1.E-6)
ETAC=ETC2/P
ETR11=8.*3.14*(1310.**2)**4.08*(1.E-12)*s1*tw
ETAR1=1./ETR11
ETR12=8.*3.14*(3020.**2)**4.08*(1.E-12)*s2*tw
ETAR2=1./ETR12
ETA11=ETAC/ETAR1
ETA12=ETAC/ETAR2
aap1=eta11/s1
aap2=eta12/s2
aapx1=(3./4.)*(aap1)/p
aapx2=(3./4.)*(aap2)/p
am2=1.+(aapx1+aapx2)
tin=p**2./kfb*(s1*pfdb1+s2*pfdb2)
tn= exp(-(3.*tin)**0.5)
anexp=(1.-tn)/(1.+tn)
tcm=l/kfb*(pfdb1*az1+pfdb2*az2)

```

```

ala=0.00005668
akp=p/(ala*tw**4.)*(s1*pfb1+s2*pfb2)
tao=akp*l
anba=kfb*akp/(4.*ala*tw**3.)
r=3.*tao**2./anba
alm=3.*tao**2.*(0.75+1./anba)
am= sqrt(alm)
cm= exp(-am)
ad=3.*tao*(1.-cm)+2.*am*(1.+cm)
ac=r/am**8.*(48.-3.*tao*am**2.+36.*tao)/ad
pa1=24.-12.*am+am**3.+(am**3.-12.*am-24.)*cm
pa2=-12.*r/(5.*am**4.)+17.*r/(70.*am**2.)
ambar=am/(sqrt(am2))
rbar=r/am2
cmbar=exp(-ambar)
adbar=3.0*tao*(1.0-cmbar)+2.0*ambar*(1.0+cmbar)
acbar=(rbar/(ambar**8.))*(48.-3.*tao*(ambar**
* 2.0)+36.0*tao)/adbar
pa1bar=24.0-12.0*ambar+ambar**3.0
* +(ambar**3.0-12.0*ambar-24.0)*cmbar
pa2bar=-12.0*rbar/(5.0*ambar**4.0)+
* 17.0*rbar/(70.0*ambar**2.0)
tbulk=ac*pa1+pa2-17./70.
tbulkn=acbar*pa1bar+pa2bar-17.0/70.0
write(29,104) l,-tbulk,-tbulkn
write(30,100) l,-tbulkn
write(31,1000)tw, p, l, -tbulk, -tbulkn
100 format(1x,f9.2,3x,e10.4)
104 format(1x,f9.2,2(3x,e10.4))
303 continue
202 continue
101 continue
1000 format(1x,f7.2, 3x,f6.2, 3x,f6.2, 3x,e10.4, 3x,e10.4)
230 format(4x,'tw',8x,'p',6x,'l',9x,'tbulk',9x,'tbulkn')
stop
end

```

## GRAY GAS RESULTS FOR CH<sub>4</sub>

tw	p	l	tbulk (LTE)	tbulkn (NLTE)
300.00	0.10	0.10	0.2490E+00	0.2392E+00
300.00	0.10	0.50	0.2424E+00	0.2424E+00
300.00	0.10	1.00	0.2412E+00	0.2412E+00
300.00	0.10	2.00	0.2363E+00	0.2363E+00
300.00	0.10	5.00	0.2074E+00	0.2074E+00
300.00	0.10	10.00	0.1452E+00	0.1453E+00
300.00	0.10	20.00	0.6771E-01	0.6771E-01
300.00	0.10	50.00	0.1578E-01	0.1578E-01
300.00	0.10	75.00	0.7989E-02	0.7989E-02
300.00	0.10	100.00	0.5008E-02	0.5008E-02
300.00	1.00	0.10	0.2427E+00	0.2427E+00
300.00	1.00	0.50	0.2388E+00	0.2388E+00
300.00	1.00	1.00	0.2276E+00	0.2276E+00
300.00	1.00	2.00	0.1929E+00	0.1929E+00
300.00	1.00	5.00	0.9929E-01	0.9929E-01
300.00	1.00	10.00	0.4184E-01	0.4184E-01
300.00	1.00	20.00	0.1681E-01	0.1681E-01
300.00	1.00	50.00	0.6791E-02	0.6791E-02
300.00	1.00	75.00	0.5267E-02	0.5267E-02
300.00	1.00	100.00	0.4611E-02	0.4611E-02
300.00	5.00	0.10	0.2420E+00	0.2420E+00
300.00	5.00	0.50	0.2250E+00	0.2250E+00
300.00	5.00	1.00	0.1883E+00	0.1883E+00
300.00	5.00	2.00	0.1235E+00	0.1235E+00
300.00	5.00	5.00	0.5240E-01	0.5240E-01
300.00	5.00	10.00	0.2976E-01	0.2976E-01
300.00	5.00	20.00	0.2095E-01	0.2095E-01
300.00	5.00	50.00	0.1683E-01	0.1683E-01
300.00	5.00	75.00	0.1605E-01	0.1605E-01
300.00	5.00	100.00	0.1568E-01	0.1568E-01
300.00	10.00	0.10	0.2412E+00	0.2412E+00
300.00	10.00	0.50	0.2121E+00	0.2121E+00
300.00	10.00	1.00	0.1637E+00	0.1637E+00
300.00	10.00	2.00	0.1022E+00	0.1022E+00
300.00	10.00	5.00	0.5243E-01	0.5243E-01
300.00	10.00	10.00	0.3813E-01	0.3813E-01
300.00	10.00	20.00	0.3230E-01	0.3230E-01
300.00	10.00	50.00	0.2935E-01	0.2935E-01
300.00	10.00	75.00	0.2876E-01	0.2876E-01
300.00	10.00	100.00	0.2847E-01	0.2847E-01
500.00	0.10	0.10	0.2426E+00	0.2427E+00
500.00	0.10	0.50	0.2417E+00	0.2417E+00
500.00	0.10	1.00	0.2383E+00	0.2383E+00
500.00	0.10	2.00	0.2256E+00	0.2256E+00

500.00	0.10	5.00	0.1651E+00	0.1651E+00
500.00	0.10	10.00	0.8540E-01	0.8540E-01
500.00	0.10	20.00	0.3012E-01	0.3012E-01
500.00	0.10	50.00	0.6114E-02	0.6114E-02
500.00	0.10	75.00	0.3067E-02	0.3067E-02
500.00	0.10	100.00	0.1929E-02	0.1929E-02
500.00	1.00	0.10	0.2424E+00	0.2424E+00
500.00	1.00	0.50	0.2319E+00	0.2319E+00
500.00	1.00	1.00	0.2050E+00	0.2050E+00
500.00	1.00	2.00	0.1422E+00	0.1422E+00
500.00	1.00	5.00	0.4962E-01	0.4962E-01
500.00	1.00	10.00	0.1782E-01	0.1782E-01
500.00	1.00	20.00	0.6949E-02	0.6949E-02
500.00	1.00	50.00	0.2911E-02	0.2911E-02
500.00	1.00	75.00	0.2299E-02	0.2299E-02
500.00	1.00	100.00	0.2034E-02	0.2034E-02
500.00	5.00	0.10	0.2406E+00	0.2406E+00
500.00	5.00	0.50	0.1996E+00	0.1996E+00
500.00	5.00	1.00	0.1364E+00	0.1364E+00
500.00	5.00	2.00	0.6842E-01	0.6842E-01
500.00	5.00	5.00	0.2421E-01	0.2421E-01
500.00	5.00	10.00	0.1358E-01	0.1358E-01
500.00	5.00	20.00	0.9666E-02	0.9666E-02
500.00	5.00	50.00	0.7838E-02	0.7838E-02
500.00	5.00	75.00	0.7488E-02	0.7488E-02
500.00	5.00	100.00	0.7321E-02	0.7321E-02
500.00	10.00	0.10	0.2385E+00	0.2385E+00
500.00	10.00	0.50	0.1746E+00	0.1746E+00
500.00	10.00	1.00	0.1066E+00	0.1066E+00
500.00	10.00	2.00	0.5407E-01	0.5407E-01
500.00	10.00	5.00	0.2541E-01	0.2541E-01
500.00	10.00	10.00	0.1840E-01	0.1840E-01
500.00	10.00	20.00	0.1560E-01	0.1560E-01
500.00	10.00	50.00	0.1417E-01	0.1417E-01
500.00	10.00	75.00	0.1388E-01	0.1388E-01
500.00	10.00	100.00	0.1374E-01	0.1374E-01
1000.00	0.10	0.10	0.2428E+00	0.2428E+00
1000.00	0.10	0.50	0.2408E+00	0.2408E+00
1000.00	0.10	1.00	0.2349E+00	0.2349E+00
1000.00	0.10	2.00	0.2141E+00	0.2141E+00
1000.00	0.10	5.00	0.1324E+00	0.1324E+00
1000.00	0.10	10.00	0.5646E-01	0.5646E-01
1000.00	0.10	20.00	0.1746E-01	0.1746E-01
1000.00	0.10	50.00	0.3180E-02	0.3180E-02
1000.00	0.10	75.00	0.1506E-02	0.1506E-02
1000.00	0.10	100.00	0.8987E-03	0.8987E-03
1000.00	1.00	0.10	0.2420E+00	0.2420E+00
1000.00	1.00	0.50	0.2241E+00	0.2241E+00
1000.00	1.00	1.00	0.1826E+00	0.1826E+00

1000.00	1.00	2.00	0.1059E+00	0.1059E+00
1000.00	1.00	5.00	0.2839E-01	0.2839E-01
1000.00	1.00	10.00	0.8666E-02	0.8666E-02
1000.00	1.00	20.00	0.2769E-02	0.2769E-02
1000.00	1.00	50.00	0.8130E-03	0.8130E-03
1000.00	1.00	75.00	0.5494E-03	0.5494E-03
1000.00	1.00	100.00	0.4413E-03	0.4413E-03
1000.00	5.00	0.10	0.2389E+00	0.2389E+00
1000.00	5.00	0.50	0.1735E+00	0.1735E+00
1000.00	5.00	1.00	0.9662E-01	0.9662E-01
1000.00	5.00	2.00	0.3778E-01	0.3778E-01
1000.00	5.00	5.00	0.9497E-02	0.9497E-02
1000.00	5.00	10.00	0.3964E-02	0.3964E-02
1000.00	5.00	20.00	0.2166E-02	0.2166E-02
1000.00	5.00	50.00	0.1417E-02	0.1417E-02
1000.00	5.00	75.00	0.1284E-02	0.1284E-02
1000.00	5.00	100.00	0.1223E-02	0.1223E-02
1000.00	10.00	0.10	0.2351E+00	0.2351E+00
1000.00	10.00	0.50	0.1382E+00	0.1382E+00
1000.00	10.00	1.00	0.6531E-01	0.6531E-01
1000.00	10.00	2.00	0.2483E-01	0.2483E-01
1000.00	10.00	5.00	0.7742E-02	0.7742E-02
1000.00	10.00	10.00	0.4260E-02	0.4260E-02
1000.00	10.00	20.00	0.3011E-02	0.3011E-02
1000.00	10.00	50.00	0.2427E-02	0.2427E-02
1000.00	10.00	75.00	0.2314E-02	0.2314E-02
1000.00	10.00	100.00	0.2260E-02	0.2260E-02
2000.00	0.10	0.10	0.2428E+00	0.2428E+00
2000.00	0.10	0.50	0.2413E+00	0.2413E+00
2000.00	0.10	1.00	0.2367E+00	0.2367E+00
2000.00	0.10	2.00	0.2199E+00	0.2199E+00
2000.00	0.10	5.00	0.1469E+00	0.1469E+00
2000.00	0.10	10.00	0.6737E-01	0.6737E-01
2000.00	0.10	20.00	0.2137E-01	0.2137E-01
2000.00	0.10	50.00	0.3750E-02	0.3750E-02
2000.00	0.10	75.00	0.1703E-02	0.1703E-02
2000.00	0.10	100.00	0.9733E-03	0.9733E-03
2000.00	1.00	0.10	0.2422E+00	0.2422E+00
2000.00	1.00	0.50	0.2280E+00	0.2280E+00
2000.00	1.00	1.00	0.1927E+00	0.1927E+00
2000.00	1.00	2.00	0.1192E+00	0.1192E+00
2000.00	1.00	5.00	0.3290E-01	0.3290E-01
2000.00	1.00	10.00	0.9387E-02	0.9387E-02
2000.00	1.00	20.00	0.2544E-02	0.2544E-02
2000.00	1.00	50.00	0.4789E-03	0.4789E-03
2000.00	1.00	75.00	0.2419E-03	0.2419E-03
2000.00	1.00	100.00	0.1541E-03	0.1541E-03
2000.00	5.00	0.10	0.2397E+00	0.2397E+00
2000.00	5.00	0.50	0.1835E+00	0.1835E+00

2000.00	5.00	1.00	0.1067E+00	0.1067E+00
2000.00	5.00	2.00	0.4062E-01	0.4062E-01
2000.00	5.00	5.00	0.8145E-02	0.8145E-02
2000.00	5.00	10.00	0.2371E-02	0.2371E-02
2000.00	5.00	20.00	0.7664E-03	0.7664E-03
2000.00	5.00	50.00	0.2384E-03	0.2384E-03
2000.00	5.00	75.00	0.1661E-03	0.1661E-03
2000.00	5.00	100.00	0.1361E-03	0.1361E-03
2000.00	10.00	0.10	0.2367E+00	0.2367E+00
2000.00	10.00	0.50	0.1482E+00	0.1482E+00
2000.00	10.00	1.00	0.6958E-01	0.6958E-01
2000.00	10.00	2.00	0.2320E-01	0.2320E-01
2000.00	10.00	5.00	0.4690E-02	0.4690E-02
2000.00	10.00	10.00	0.1525E-02	0.1525E-02
2000.00	10.00	20.00	0.6045E-03	0.6045E-03
2000.00	10.00	50.00	0.2714E-03	0.2714E-03
2000.00	10.00	75.00	0.2200E-03	0.2200E-03
2000.00	10.00	100.00	0.1973E-03	0.1973E-03



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PROGRAM NLTE
C THIS PROGRAM INVESTIGATES LTE and NLTE EFFECT IN CO (NONGRAY CASE)
C THIS PROGRAM IS WRITTEN BY MANOJ K. JHA IN AUGUST 1992
C
C IMPLICIT DOUBLE PRECISION (A-H,O-Z)
DOUBLE PRECISION IERR
REAL L,KFB
EXTERNAL F10,F11,F12,F13,F14
DIMENSION U(9),PRES(4),TEMP(4),EPS(2)
COMMON F
OPEN (1,FILE='out111a')
OPEN (2,FILE='nlp')
OPEN (3,FILE='lp')
DATA U/0.1,0.5,1.,5.,10.,20.,50.,75.,100./
DATA PRES/0.1,1.,5.,10./
DATA TEMP/300.,500.,1000.,2000./
WRITE (1,11)
write(2,13)
write(2,*) 9,1
13 format('3',/, 'x',/, 't',/, 't1',/,i4,x,'1')
write(3,14)
write(3,*) 9,1
14 format('2',/, 'x',/, 't',/,/,i4,x,'1')
DO 4 IT=1,4
TW=TEMP(IT)
DO 5 KK=1,4
P=PRES(KK)
DO 6 I=1,9
L=U(I)
TK1=TW**2.
TK2=TW**0.5
TK3=TW/273.
HCK=1.439257246
TS=300./TW
WNB=2143.
C2B=HCK*WNB
CCC=0.000053847734
CCB=CCC*(WNB**4.)
TB=C2B/TW
TEB=EXP(TB)
C1B=CCB/C2B
PFB=C1B/(TEB-1.)
DEV=TK1*((TEB-1.)**2.)
PFDB=(CCB*TEB)/DEV
AK1=(TW/300.)**0.5
AK2=(300./TW)**1.5
AZ=38.1*AK1
KFB=2325.570579*(TK3**0.8)
OMEG=2143.

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TX=-(HCK/TW)
TX1=TX*OMEG
ETX1=EXP(TX1)
C1=1.-ETX1
PHI1=(15.15+(0.22*((TW/100.)**1.5)))*C1
CZ=6.24*AK2
S=AZ*CZ
PL=P*L
UZ=CZ*PL
DEL1=((PHI1**2.)/AK1)*0.001
BS=0.314*DEL1
PE=(1.1*P)**0.8
BETA=BS*PE
F=2.94*(1.-EXP(-(2.6*BETA)))
EPS(2)=1.E-03
EPS(1)=1.E-03
X1=0.
X2=(3./8.)*UZ
Y1=1.5*UZ
Y2=3.*X2
CALL QDAGS (F10,X1,Y1,EPS(2),EPS(1),R0,IERR)
CALL QDAGS (F11,X1,Y1,EPS(2),EPS(1),R1,IERR)
CALL QDAGS (F12,X1,Y1,EPS(2),EPS(1),R2,IERR)
CALL QDAGS (F13,X1,Y1,EPS(2),EPS(1),R3,IERR)
CALL QDAGS (F14,X1,Y1,EPS(2),EPS(1),R4,IERR)
CALL QDAGS (F10,X2,Y2,EPS(2),EPS(1),S1,IERR)
CALL QDAGS (F11,X1,X2,EPS(2),EPS(1),S2,IERR)
CALL QDAGS (F11,X1,Y2,EPS(2),EPS(1),S3,IERR)
CALL QDAGS (F12,X2,Y2,EPS(2),EPS(1),S4,IERR)
CALL QDAGS (F13,X1,X2,EPS(2),EPS(1),S5,IERR)
CALL QDAGS (F13,X1,Y2,EPS(2),EPS(1),S6,IERR)
CALL QDAGS (F14,X2,Y2,EPS(2),EPS(1),S7,IERR)
H=AZ*PFDB
AM=(H*L)/KFB
CU=2./(3.*UZ)
BU=1./CU
BR1A=(CU*R1)-(2.*(CU**3.)*R3)+((CU**4.)*R4)
BR1B=((CU**2.)*R2)-(CU*R1)
ETC1=(14.)*(1./4.)
ETC2=0.015*ETC1
ETC3=TW**(-1./3.)
ETC4=ETC3-ETC2
ETC5=175.*ETC4
ETC6=(ETC5-18.42)
ETC7=EXP(ETC6)
ETAC=ETC7/P
ETAR=0.0297
ETA=ETAC/ETAR
SUMA=H*BR1A

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AL1L=1.+(L/KFB)\*SUMA)  
ALPH1=AL1L-(9./2.)\*ETA\*CU\*BR1B)  
BR2A=((CU\*\*2.)\*R2)-(2.\*(CU\*\*3.)\*R3)+((CU\*\*4.)\*R4)  
BR2B=R0-(6.\*CU\*R1)+(6.\*(CU\*\*2.)\*R2)  
SUMB=H\*BR2A  
AL2L=(L/KFB)\*SUMB  
ALPH2=AL2L-(3./4.)\*ETA\*CU\*BR2B)  
ALPH0 = (9./2.)\*ETA\*(CU\*\*2.)\*(CU\*R2-R1)-1.  
BR3A=((57./256.)\*S1)+((11./16.)\*CU\*(S2+S3))  
\*-(9./8.)\*(CU\*\*2.)\*S4)-((CU\*\*3.)\*(S5+S6))+((CU\*\*4.)\*S7)  
BR3B=((9./4.)\*CU\*S1)+(6.\*(CU\*\*2.)\*(S2+S3))  
\*-(12\*(CU\*\*3.)\*S4)  
SUMC=H\*BR3A  
AL3L=((L/KFB)\*SUMC)+(11./16.)  
ALPH3 =AL3L+((3./8.)\*ETA\*BR3B)  
BR4A=((9./256.)\*S1)+((3./16.)\*CU\*(S2+S3))  
\*-(1./8.)\*(CU\*\*2.)\*S4)-((CU\*\*3.)\*(S5+S6))+((CU\*\*4.)\*S7)  
BR4B=((1./4.)\*CU\*S1)+(6.\*(CU\*\*2.)\*(S2+S3))-12.\*(CU\*\*3.)\*S4  
SUMD=H\*BR4A  
AL4L=((L/KFB)\*SUMD)+(3./16.)  
ALPH4 =AL4L+((3./8.)\*ETA\*BR4B)  
BRK5=(3./16.)\*(CU\*S1)+(1./2.)\*(CU\*\*2.)\*(S2+S3)-(CU\*\*3.)\*S4  
ALPH5 = -(9./2.)\*ETA\*BRK5+(11./16.))  
DENA = (ALPH1\*ALPH4)-(ALPH2\*ALPH3)  
A1=((ALPH0\*ALPH4)-(ALPH2\*ALPH5))/DENA  
A2=((ALPH1\*ALPH5)-(ALPH0\*ALPH3))/DENA  
TBULK = (1./70.)\*((17.\*A1)+(3.\*A2))  
CONST=1./16.\*(AL1L\*AL4L-AL2L\*AL3L))  
a1l=(11.\*a12l-16.\*a14l)\*CONST  
A2L=(16.\*AL3L-11.\*AL1L)\*CONST  
TBULKL=(1/70.)\*(17.\*A1L+3.\*A2L)  
BET0=-(3./8.)\*(ETA\*CU)\*(LOG((BU+EPS(1))/EPS(1)))  
BET1=1+AM\*(7./12.)+(9./4.)\*ETA\*CU)  
BET2=(AM/12.)-(3./4.)\*ETA\*CU\*(LOG((BU+EPS(1))/EPS(1))-3.)  
BET3=AM\*((57./256.)\*LOG(3.)+(65./192.))+11./16.)  
\*+(3./8.)\*ETA\*CU\*((9./4.)\*LOG(3.)+3.)  
BET4=AM\*((9./256.)\*LOG(3.)+(17./192.))+3./16.)  
\*+(3./8.)\*ETA\*CU\*((LOG(3.)/4.)+3.)  
BET5=((3./8.)\*ETA\*CU\*LOG(3.))-11./16.)  
DENB=BET1\*BET4-BET2\*BET3  
B1=-(BET4+(BET0\*BET4)+(BET2\*BET5))/DENB  
B2=(BET3+(BET0\*BET3)+(BET1\*BET5))/DENB  
TTHIC=(1./70.)\*(17.\*B1+3.\*B2)  
AN=PL\*CZ\*H  
ANBA=AN/(1.+(3./4.)\*ETA)  
ANBA1=SQRT(3.\*ANBA)  
BRKT=(1.-EXP(-ANBA1))/(1.+EXP(-ANBA1))  
BRKT1=576.\*BRKT/ANBA1  
BRKT2=BRKT1-(21.6\*(ANBA\*\*2.))+(72.\*ANBA)-288.

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TTHIN=BRKT2/((3.*ANBA)**3.)
WRITE (1,19) TW,P,L,-TBULK,-TBULKL
WRITE (2,20) L,-TBULKL,-TBULK
WRITE (3,21) L,- TBULK
6 CONTINUE
5 CONTINUE
4 CONTINUE
  write(*,*) ctac,ctar,cta
19 FORMAT (1X,F7.2,2(3X,F6.2),2(3X,E10.4))
20 FORMAT (3X,F6.2,2(3X,E10.4))
21 FORMAT (3X,F6.2,3X,E10.4)
11 FORMAT (4X, 'TW',8X, 'P',6X, 'L',9X, 'TBULK',9X, 'TBULKL')
STOP
END

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C

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FUNCTION F10(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F10=AUD
RETURN
END
FUNCTION F11(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F11=AUD*U
RETURN
END
FUNCTION F12(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F12=AUD*(U**2.)
RETURN
END
FUNCTION F13(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F13=AUD*(U**3.)
RETURN
END
FUNCTION F14(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F14=AUD*(U**4.)

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RETURN  
END

## NONGRAY RESULTS FOR CO

TW	P	L	TBULK (NLTE)	TBULKL (LTE)
300.00	0.10	0.10	0.2429E+00	0.2429E+00
300.00	0.10	0.50	0.2429E+00	0.2428E+00
300.00	0.10	1.00	0.2429E+00	0.2428E+00
300.00	0.10	5.00	0.2429E+00	0.2421E+00
300.00	0.10	10.00	0.2428E+00	0.2406E+00
300.00	0.10	20.00	0.2428E+00	0.2361E+00
300.00	0.10	50.00	0.2426E+00	0.2176E+00
300.00	0.10	75.00	0.2424E+00	0.2016E+00
300.00	0.10	100.00	0.2420E+00	0.1868E+00
300.00	1.00	0.10	0.2429E+00	0.2428E+00
300.00	1.00	0.50	0.2429E+00	0.2426E+00
300.00	1.00	1.00	0.2428E+00	0.2422E+00
300.00	1.00	5.00	0.2427E+00	0.2383E+00
300.00	1.00	10.00	0.2421E+00	0.2330E+00
300.00	1.00	20.00	0.2399E+00	0.2228E+00
300.00	1.00	50.00	0.2280E+00	0.1966E+00
300.00	1.00	75.00	0.2149E+00	0.1791E+00
300.00	1.00	100.00	0.2010E+00	0.1644E+00
300.00	5.00	0.10	0.2429E+00	0.2428E+00
300.00	5.00	0.50	0.2428E+00	0.2423E+00
300.00	5.00	1.00	0.2427E+00	0.2417E+00
300.00	5.00	5.00	0.2400E+00	0.2370E+00
300.00	5.00	10.00	0.2352E+00	0.2314E+00
300.00	5.00	20.00	0.2250E+00	0.2209E+00
300.00	5.00	50.00	0.1979E+00	0.1948E+00
300.00	5.00	75.00	0.1798E+00	0.1774E+00
300.00	5.00	100.00	0.1648E+00	0.1629E+00
300.00	10.00	0.10	0.2428E+00	0.2428E+00
300.00	10.00	0.50	0.2427E+00	0.2422E+00
300.00	10.00	1.00	0.2423E+00	0.2416E+00
300.00	10.00	5.00	0.2381E+00	0.2369E+00
300.00	10.00	10.00	0.2324E+00	0.2312E+00
300.00	10.00	20.00	0.2218E+00	0.2208E+00
300.00	10.00	50.00	0.1953E+00	0.1947E+00
300.00	10.00	75.00	0.1778E+00	0.1773E+00
300.00	10.00	100.00	0.1632E+00	0.1629E+00
500.00	0.10	0.10	0.2429E+00	0.2428E+00
500.00	0.10	0.50	0.2428E+00	0.2425E+00
500.00	0.10	1.00	0.2428E+00	0.2419E+00
500.00	0.10	5.00	0.2419E+00	0.2347E+00
500.00	0.10	10.00	0.2391E+00	0.2208E+00
500.00	0.10	20.00	0.2290E+00	0.1851E+00
500.00	0.10	50.00	0.1799E+00	0.1013E+00
500.00	0.10	75.00	0.1389E+00	0.6731E-01

500.00	0.10	100.00	0.1069E+00	0.4877E-01
500.00	1.00	0.10	0.2428E+00	0.2427E+00
500.00	1.00	0.50	0.2420E+00	0.2399E+00
500.00	1.00	1.00	0.2400E+00	0.2348E+00
500.00	1.00	5.00	0.2056E+00	0.1869E+00
500.00	1.00	10.00	0.1614E+00	0.1433E+00
500.00	1.00	20.00	0.1068E+00	0.9607E-01
500.00	1.00	50.00	0.5095E-01	0.4798E-01
500.00	1.00	75.00	0.3537E-01	0.3388E-01
500.00	1.00	100.00	0.2709E-01	0.2619E-01
500.00	5.00	0.10	0.2424E+00	0.2420E+00
500.00	5.00	0.50	0.2365E+00	0.2345E+00
500.00	5.00	1.00	0.2272E+00	0.2245E+00
500.00	5.00	5.00	0.1688E+00	0.1668E+00
500.00	5.00	10.00	0.1279E+00	0.1269E+00
500.00	5.00	20.00	0.8678E-01	0.8636E-01
500.00	5.00	50.00	0.4480E-01	0.4470E-01
500.00	5.00	75.00	0.3208E-01	0.3203E-01
500.00	5.00	100.00	0.2502E-01	0.2499E-01
500.00	10.00	0.10	0.2418E+00	0.2415E+00
500.00	10.00	0.50	0.2335E+00	0.2325E+00
500.00	10.00	1.00	0.2229E+00	0.2220E+00
500.00	10.00	5.00	0.1651E+00	0.1646E+00
500.00	10.00	10.00	0.1256E+00	0.1254E+00
500.00	10.00	20.00	0.8572E-01	0.8563E-01
500.00	10.00	50.00	0.4450E-01	0.4448E-01
500.00	10.00	75.00	0.3193E-01	0.3191E-01
500.00	10.00	100.00	0.2493E-01	0.2492E-01
1000.00	0.10	0.10	0.2428E+00	0.2428E+00
1000.00	0.10	0.50	0.2423E+00	0.2420E+00
1000.00	0.10	1.00	0.2409E+00	0.2401E+00
1000.00	0.10	5.00	0.2206E+00	0.2173E+00
1000.00	0.10	10.00	0.1913E+00	0.1873E+00
1000.00	0.10	20.00	0.1383E+00	0.1344E+00
1000.00	0.10	50.00	0.5584E-01	0.5395E-01
1000.00	0.10	75.00	0.3210E-01	0.3104E-01
1000.00	0.10	100.00	0.2110E-01	0.2044E-01
1000.00	1.00	0.10	0.2425E+00	0.2424E+00
1000.00	1.00	0.50	0.2357E+00	0.2354E+00
1000.00	1.00	1.00	0.2217E+00	0.2211E+00
1000.00	1.00	5.00	0.1197E+00	0.1188E+00
1000.00	1.00	10.00	0.6795E-01	0.6753E-01
1000.00	1.00	20.00	0.3450E-01	0.3436E-01
1000.00	1.00	50.00	0.1329E-01	0.1327E-01
1000.00	1.00	75.00	0.8684E-02	0.8671E-02
1000.00	1.00	100.00	0.6425E-02	0.6417E-02
1000.00	5.00	0.10	0.2410E+00	0.2410E+00
1000.00	5.00	0.50	0.2175E+00	0.2173E+00
1000.00	5.00	1.00	0.1853E+00	0.1851E+00

1000.00	5.00	5.00	0.7958E-01	0.7952E-01
1000.00	5.00	10.00	0.4681E-01	0.4679E-01
1000.00	5.00	20.00	0.2591E-01	0.2590E-01
1000.00	5.00	50.00	0.1116E-01	0.1116E-01
1000.00	5.00	75.00	0.7580E-02	0.7579E-02
1000.00	5.00	100.00	0.5740E-02	0.5740E-02
1000.00	10.00	0.10	0.2395E+00	0.2394E+00
1000.00	10.00	0.50	0.2076E+00	0.2075E+00
1000.00	10.00	1.00	0.1728E+00	0.1727E+00
1000.00	10.00	5.00	0.7488E-01	0.7487E-01
1000.00	10.00	10.00	0.4486E-01	0.4486E-01
1000.00	10.00	20.00	0.2521E-01	0.2521E-01
1000.00	10.00	50.00	0.1100E-01	0.1100E-01
1000.00	10.00	75.00	0.7502E-02	0.7502E-02
1000.00	10.00	100.00	0.5694E-02	0.5694E-02
2000.00	0.10	0.10	0.2428E+00	0.2428E+00
2000.00	0.10	0.50	0.2423E+00	0.2423E+00
2000.00	0.10	1.00	0.2410E+00	0.2410E+00
2000.00	0.10	5.00	0.2168E+00	0.2166E+00
2000.00	0.10	10.00	0.1826E+00	0.1824E+00
2000.00	0.10	20.00	0.1316E+00	0.1314E+00
2000.00	0.10	50.00	0.6003E-01	0.5993E-01
2000.00	0.10	75.00	0.3659E-01	0.3653E-01
2000.00	0.10	100.00	0.2459E-01	0.2456E-01
2000.00	1.00	0.10	0.2426E+00	0.2426E+00
2000.00	1.00	0.50	0.2381E+00	0.2381E+00
2000.00	1.00	1.00	0.2267E+00	0.2267E+00
2000.00	1.00	5.00	0.1214E+00	0.1213E+00
2000.00	1.00	10.00	0.6542E-01	0.6540E-01
2000.00	1.00	20.00	0.3108E-01	0.3108E-01
2000.00	1.00	50.00	0.1102E-01	0.1102E-01
2000.00	1.00	75.00	0.6983E-02	0.6983E-02
2000.00	1.00	100.00	0.5070E-02	0.5070E-02
2000.00	5.00	0.10	0.2418E+00	0.2418E+00
2000.00	5.00	0.50	0.2232E+00	0.2232E+00
2000.00	5.00	1.00	0.1898E+00	0.1898E+00
2000.00	5.00	5.00	0.6823E-01	0.6823E-01
2000.00	5.00	10.00	0.3700E-01	0.3700E-01
2000.00	5.00	20.00	0.1946E-01	0.1946E-01
2000.00	5.00	50.00	0.8102E-02	0.8102E-02
2000.00	5.00	75.00	0.5463E-02	0.5463E-02
2000.00	5.00	100.00	0.4124E-02	0.4124E-02
2000.00	10.00	0.10	0.2408E+00	0.2408E+00
2000.00	10.00	0.50	0.2115E+00	0.2115E+00
2000.00	10.00	1.00	0.1705E+00	0.1705E+00
2000.00	10.00	5.00	0.6040E-01	0.6040E-01
2000.00	10.00	10.00	0.3399E-01	0.3399E-01
2000.00	10.00	20.00	0.1844E-01	0.1844E-01
2000.00	10.00	50.00	0.7886E-02	0.7886E-02



2000.00	10.00	75.00	0.5358E-02	0.5358E-02
2000.00	10.00	100.00	0.4061E-02	0.4061E-02

PROGRAM NLTE  
 C THIS PROGRAM INVESTIGATES LTE and NLTE EFFECT IN NO (NONGRAY CASE)  
 C THIS PROGRAM IS WRITTEN BY MANOJ K. JHA IN SEPTEMBER 1992  
 C

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C IMPLICIT DOUBLE PRECISION (A-H,O-Z)  
 DOUBLE PRECISION IERR  
 REAL L,KFB  
 EXTERNAL F10,F11,F12,F13,F14  
 DIMENSION U(9),PRES(4),TEMP(4),EPS(2)  
 COMMON F  
 OPEN (1,FILE='out11ba')  
 OPEN (2,FILE='nlp')  
 OPEN (3,FILE='lp')  
 DATA U/0.1,0.5,1.,5.,10.,20.,50.,75.,100./  
 DATA PRES/0.1,1.,5.,10./  
 DATA TEMP/300.,500.,1000.,2000./  
 WRITE (1,11)  
 write(2,13)  
 write(2,\*) 9,1  
 13 format('3',/, 'x',/, 't',/, 't1',/,i4,x,'1')  
 write(3,14)  
 write(3,\*) 9,1  
 14 format('2',/, 'x',/, 't',/,/,i4,x,'1')  
 DO 4 IT=1,4  
 TW=TEMP(IT)  
 DO 5 KK=1,4  
 P=PRES(KK)  
 DO 6 I=1,9  
 L=U(I)  
 TK1=TW\*\*2.  
 TK2=TW\*\*0.5  
 TK3=TW/273.  
 HCK=1.439257246  
 TS=300./TW  
 WNB=1876.  
 C2B=HCK\*WNB  
 CCC=0.000053847734  
 CCB=CCC\*(WNB\*\*4.)  
 TB=C2B/TW  
 TEB=EXP(TB)  
 C1B=CCB/C2B  
 PFB=C1B/(TEB-1.)  
 DEV=TK1\*((TEB-1.)\*\*2.)  
 PFDB=(CCB\*TEB)/DEV  
 AK1=(TW/300.)\*\*0.5  
 AK2=(300./TW)\*\*1.5  
 AZ=36.\*AK1  
 KFB=(TW/179.16)\*0.01378\*(1.E+8)\*(1./(36.\*23.889))  
 OMEG=1876.

```

TX=-(HCK/TW)
TX1=TX*OMEG
ETX1=EXP(TX1)
C1=1.-ETX1
S=132.*TS
CZ=S/AZ
PL=P*L
UZ=CZ*PL
PE=P**.65
BS=0.1042117/ak1
BETA=BS*PE
F=2.94*(1.-EXP(-(2.6*BETA)))
EPS(2)=1.E-03
EPS(1)=1.E-03
X1=0.
X2=(3./8.)*UZ
Y1=1.5*UZ
Y2=3.*X2
CALL QDAGS (F10,X1,Y1,EPS(2),EPS(1),R0,IERR)
CALL QDAGS (F11,X1,Y1,EPS(2),EPS(1),R1,IERR)
CALL QDAGS (F12,X1,Y1,EPS(2),EPS(1),R2,IERR)
CALL QDAGS (F13,X1,Y1,EPS(2),EPS(1),R3,IERR)
CALL QDAGS (F14,X1,Y1,EPS(2),EPS(1),R4,IERR)
CALL QDAGS (F10,X2,Y2,EPS(2),EPS(1),S1,IERR)
CALL QDAGS (F11,X1,X2,EPS(2),EPS(1),S2,IERR)
CALL QDAGS (F11,X1,Y2,EPS(2),EPS(1),S3,IERR)
CALL QDAGS (F12,X2,Y2,EPS(2),EPS(1),S4,IERR)
CALL QDAGS (F13,X1,X2,EPS(2),EPS(1),S5,IERR)
CALL QDAGS (F13,X1,Y2,EPS(2),EPS(1),S6,IERR)
CALL QDAGS (F14,X2,Y2,EPS(2),EPS(1),S7,IERR)
H=AZ*PFDB
AM=(H*L)/KFB
CU=2./(3.*UZ)
BU=1./CU
BR1A=(CU*R1)-(2.*(CU**3.)*R3)+((CU**4.)*R4)
BR1B=((CU**2.)*R2)-(CU*R1)
ETC1=1.16*1.E-3*((15)**0.5)*(2700.** (4./3.))
ETC2=TW**(-1./3.)-0.015*((15. )**0.25)
ETC3=ETC1*ETC2-18.42
ETC4=EXP(ETC3)
ETAC=ETC4/P
ETAR1=8*3.14*(1876.** (2.))*4.08*(1.E-12)*300*132
ETAR=1/ETAR1
ETA=ETAC/ETAR
SUMA=H*BR1A
AL1L=1.+((L/KFB)*SUMA)
ALPH1=AL1L-(9./2.)*ETA*CU*BR1B)
BR2A=((CU**2.)*R2)-(2.*(CU**3.)*R3)+((CU**4.)*R4)
BR2B=R0-(6.*CU*R1)+(6.*(CU**2.)*R2)

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SUMB=H*BR2A
AL2L=(L/KFB)*SUMB
ALPH2=AL2L-((3./4.)*ETA*CU*BR2B)
ALPH0=(9./2.)*ETA*(CU**2.)*(CU*R2-R1)-1.
BR3A=((57./256.)*S1)+((11./16.)*CU*(S2+S3))
*-(9./8.)*(CU**2.)*S4)-((CU**3.)*(S5+S6))+((CU**4.)*S7)
BR3B=((9./4.)*CU*S1)+(6.*(CU**2.)*(S2+S3))
*-(12*(CU**3.)*S4)
SUMC=H*BR3A
AL3L=((L/KFB)*SUMC)+(11./16.)
ALPH3=AL3L+((3./8.)*ETA*BR3B)
BR4A=((9./256.)*S1)+((3./16.)*CU*(S2+S3))
*-(1./8.)*(CU**2.)*S4)-((CU**3.)*(S5+S6))+((CU**4.)*S7)
BR4B=((1./4.)*CU*S1)+(6.*(CU**2.)*(S2+S3))-12*(CU**3.)*S4)
SUMD=H*BR4A
AL4L=((L/KFB)*SUMD)+(3./16.)
ALPH4=AL4L+((3./8.)*ETA*BR4B)
BRK5=(3./16.)*(CU*S1)+(1./2.)*(CU**2.)*(S2+S3)-(CU**3.)*S4
ALPH5=-((9./2.)*ETA*BRK5+(11./16.))
DENA=(ALPH1*ALPH4)-(ALPH2*ALPH3)
A1=((ALPH0*ALPH4)-(ALPH2*ALPH5))/DENA
A2=((ALPH1*ALPH5)-(ALPH0*ALPH3))/DENA
TBULK=(1./70.)*((17.*A1)+(3.*A2))
CONST=1./16.*(AL1L*AL4L-AL2L*AL3L)
a1l=(11.*a12l-16.*a14l)*CONST
A2L=(16.*AL3L-11.*AL1L)*CONST
TBULKL=(1/70.)*(17.*A1L+3.*A2L)
WRITE (1,19) TW,P,L,-TBULK,-TBULKL
WRITE (2,20) L,-TBULKL,-TBULK
WRITE (3,21) L,-TBULK
6 CONTINUE
5 CONTINUE
4 CONTINUE
write(*,*) etac,ctar,cta
19 FORMAT (1X,F7.2,2(3X,F6.2),2(3X,E10.4))
20 FORMAT (3X,F6.2,2(3X,E10.4))
21 FORMAT (3X,F6.2,3X,E10.4)
11 FORMAT (4X, 'TW',8X, 'P',6X, 'L',9X, 'TBULK',9X, 'TBULKL')
STOP
END

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C
FUNCTION F10(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F10=AUD
RETURN
END
FUNCTION F11(U)

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COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F11=AUD*U
RETURN
END
FUNCTION F12(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F12=AUD*(U**2.)
RETURN
END
FUNCTION F13(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F13=AUD*(U**3.)
RETURN
END
FUNCTION F14(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F14=AUD*(U**4.)
RETURN
END

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## NONGRAY RESULTS FOR NO

TW	P	L	TBULK (NLTE)	TBULKL (NLTE)
300.00	0.10	0.10	0.2429E+00	0.2429E+00
300.00	0.10	0.50	0.2429E+00	0.2428E+00
300.00	0.10	1.00	0.2429E+00	0.2427E+00
300.00	0.10	5.00	0.2428E+00	0.2413E+00
300.00	0.10	10.00	0.2428E+00	0.2386E+00
300.00	0.10	20.00	0.2427E+00	0.2307E+00
300.00	0.10	50.00	0.2416E+00	0.2010E+00
300.00	0.10	75.00	0.2401E+00	0.1776E+00
300.00	0.10	100.00	0.2381E+00	0.1576E+00
300.00	1.00	0.10	0.2429E+00	0.2428E+00
300.00	1.00	0.50	0.2428E+00	0.2425E+00
300.00	1.00	1.00	0.2428E+00	0.2419E+00
300.00	1.00	5.00	0.2418E+00	0.2350E+00
300.00	1.00	10.00	0.2390E+00	0.2258E+00
300.00	1.00	20.00	0.2301E+00	0.2089E+00
300.00	1.00	50.00	0.1961E+00	0.1698E+00
300.00	1.00	75.00	0.1703E+00	0.1469E+00
300.00	1.00	100.00	0.1491E+00	0.1295E+00
300.00	5.00	0.10	0.2428E+00	0.2428E+00
300.00	5.00	0.50	0.2426E+00	0.2420E+00
300.00	5.00	1.00	0.2421E+00	0.2409E+00
300.00	5.00	5.00	0.2349E+00	0.2323E+00
300.00	5.00	10.00	0.2251E+00	0.2224E+00
300.00	5.00	20.00	0.2074E+00	0.2051E+00
300.00	5.00	50.00	0.1679E+00	0.1666E+00
300.00	5.00	75.00	0.1451E+00	0.1442E+00
300.00	5.00	100.00	0.1279E+00	0.1273E+00
300.00	10.00	0.10	0.2428E+00	0.2427E+00
300.00	10.00	0.50	0.2423E+00	0.2418E+00
300.00	10.00	1.00	0.2413E+00	0.2406E+00
300.00	10.00	5.00	0.2327E+00	0.2319E+00
300.00	10.00	10.00	0.2228E+00	0.2221E+00
300.00	10.00	20.00	0.2053E+00	0.2048E+00
300.00	10.00	50.00	0.1666E+00	0.1663E+00
300.00	10.00	75.00	0.1442E+00	0.1440E+00
300.00	10.00	100.00	0.1273E+00	0.1272E+00
500.00	0.10	0.10	0.2429E+00	0.2428E+00
500.00	0.10	0.50	0.2428E+00	0.2426E+00
500.00	0.10	1.00	0.2427E+00	0.2419E+00
500.00	0.10	5.00	0.2405E+00	0.2339E+00
500.00	0.10	10.00	0.2348E+00	0.2203E+00
500.00	0.10	20.00	0.2166E+00	0.1877E+00
500.00	0.10	50.00	0.1483E+00	0.1074E+00
500.00	0.10	75.00	0.1054E+00	0.7215E-01

500.00	0.10	100.00	0.7741E-01	0.5235E-01
500.00	1.00	0.10	0.2428E+00	0.2427E+00
500.00	1.00	0.50	0.2416E+00	0.2407E+00
500.00	1.00	1.00	0.2387E+00	0.2365E+00
500.00	1.00	5.00	0.1999E+00	0.1927E+00
500.00	1.00	10.00	0.1558E+00	0.1490E+00
500.00	1.00	20.00	0.1037E+00	0.9970E-01
500.00	1.00	50.00	0.5015E-01	0.4905E-01
500.00	1.00	75.00	0.3494E-01	0.3439E-01
500.00	1.00	100.00	0.2680E-01	0.2647E-01
500.00	5.00	0.10	0.2424E+00	0.2423E+00
500.00	5.00	0.50	0.2366E+00	0.2360E+00
500.00	5.00	1.00	0.2276E+00	0.2267E+00
500.00	5.00	5.00	0.1694E+00	0.1686E+00
500.00	5.00	10.00	0.1281E+00	0.1277E+00
500.00	5.00	20.00	0.8663E-01	0.8647E-01
500.00	5.00	50.00	0.4450E-01	0.4446E-01
500.00	5.00	75.00	0.3181E-01	0.3179E-01
500.00	5.00	100.00	0.2478E-01	0.2477E-01
500.00	10.00	0.10	0.2420E+00	0.2419E+00
500.00	10.00	0.50	0.2340E+00	0.2337E+00
500.00	10.00	1.00	0.2236E+00	0.2233E+00
500.00	10.00	5.00	0.1652E+00	0.1650E+00
500.00	10.00	10.00	0.1253E+00	0.1252E+00
500.00	10.00	20.00	0.8520E-01	0.8516E-01
500.00	10.00	50.00	0.4406E-01	0.4406E-01
500.00	10.00	75.00	0.3157E-01	0.3157E-01
500.00	10.00	100.00	0.2463E-01	0.2463E-01
1000.00	0.10	0.10	0.2428E+00	0.2428E+00
1000.00	0.10	0.50	0.2425E+00	0.2425E+00
1000.00	0.10	1.00	0.2418E+00	0.2416E+00
1000.00	0.10	5.00	0.2297E+00	0.2290E+00
1000.00	0.10	10.00	0.2118E+00	0.2108E+00
1000.00	0.10	20.00	0.1762E+00	0.1751E+00
1000.00	0.10	50.00	0.9652E-01	0.9572E-01
1000.00	0.10	75.00	0.6162E-01	0.6108E-01
1000.00	0.10	100.00	0.4234E-01	0.4196E-01
1000.00	1.00	0.10	0.2427E+00	0.2427E+00
1000.00	1.00	0.50	0.2399E+00	0.2399E+00
1000.00	1.00	1.00	0.2338E+00	0.2338E+00
1000.00	1.00	5.00	0.1686E+00	0.1684E+00
1000.00	1.00	10.00	0.1116E+00	0.1114E+00
1000.00	1.00	20.00	0.6075E-01	0.6067E-01
1000.00	1.00	50.00	0.2337E-01	0.2335E-01
1000.00	1.00	75.00	0.1508E-01	0.1507E-01
1000.00	1.00	100.00	0.1105E-01	0.1104E-01
1000.00	5.00	0.10	0.2421E+00	0.2421E+00
1000.00	5.00	0.50	0.2317E+00	0.2317E+00
1000.00	5.00	1.00	0.2136E+00	0.2136E+00

1000.00	5.00	5.00	0.1163E+00	0.1162E+00
1000.00	5.00	10.00	0.7215E-01	0.7214E-01
1000.00	5.00	20.00	0.4096E-01	0.4095E-01
1000.00	5.00	50.00	0.1786E-01	0.1786E-01
1000.00	5.00	75.00	0.1215E-01	0.1215E-01
1000.00	5.00	100.00	0.9207E-02	0.9206E-02
1000.00	10.00	0.10	0.2415E+00	0.2415E+00
1000.00	10.00	0.50	0.2255E+00	0.2255E+00
1000.00	10.00	1.00	0.2026E+00	0.2025E+00
1000.00	10.00	5.00	0.1062E+00	0.1062E+00
1000.00	10.00	10.00	0.6688E-01	0.6687E-01
1000.00	10.00	20.00	0.3876E-01	0.3875E-01
1000.00	10.00	50.00	0.1730E-01	0.1730E-01
1000.00	10.00	75.00	0.1186E-01	0.1186E-01
1000.00	10.00	100.00	0.9024E-02	0.9024E-02
2000.00	0.10	0.10	0.2429E+00	0.2429E+00
2000.00	0.10	0.50	0.2427E+00	0.2427E+00
2000.00	0.10	1.00	0.2423E+00	0.2423E+00
2000.00	0.10	5.00	0.2349E+00	0.2349E+00
2000.00	0.10	10.00	0.2228E+00	0.2228E+00
2000.00	0.10	20.00	0.1993E+00	0.1992E+00
2000.00	0.10	50.00	0.1420E+00	0.1419E+00
2000.00	0.10	75.00	0.1070E+00	0.1070E+00
2000.00	0.10	100.00	0.8165E-01	0.8163E-01
2000.00	1.00	0.10	0.2428E+00	0.2428E+00
2000.00	1.00	0.50	0.2415E+00	0.2415E+00
2000.00	1.00	1.00	0.2384E+00	0.2384E+00
2000.00	1.00	5.00	0.1958E+00	0.1958E+00
2000.00	1.00	10.00	0.1460E+00	0.1460E+00
2000.00	1.00	20.00	0.8603E-01	0.8602E-01
2000.00	1.00	50.00	0.3156E-01	0.3156E-01
2000.00	1.00	75.00	0.1932E-01	0.1932E-01
2000.00	1.00	100.00	0.1362E-01	0.1362E-01
2000.00	5.00	0.10	0.2426E+00	0.2426E+00
2000.00	5.00	0.50	0.2372E+00	0.2372E+00
2000.00	5.00	1.00	0.2256E+00	0.2256E+00
2000.00	5.00	5.00	0.1337E+00	0.1337E+00
2000.00	5.00	10.00	0.8147E-01	0.8146E-01
2000.00	5.00	20.00	0.4419E-01	0.4419E-01
2000.00	5.00	50.00	0.1815E-01	0.1815E-01
2000.00	5.00	75.00	0.1209E-01	0.1209E-01
2000.00	5.00	100.00	0.9046E-02	0.9046E-02
2000.00	10.00	0.10	0.2423E+00	0.2423E+00
2000.00	10.00	0.50	0.2329E+00	0.2329E+00
2000.00	10.00	1.00	0.2150E+00	0.2150E+00
2000.00	10.00	5.00	0.1141E+00	0.1141E+00
2000.00	10.00	10.00	0.6943E-01	0.6943E-01
2000.00	10.00	20.00	0.3881E-01	0.3881E-01
2000.00	10.00	50.00	0.1671E-01	0.1671E-01



2000.00	10.00	75.00	0.1133E-01	0.1133E-01
2000.00	10.00	100.00	0.8569E-02	0.8569E-02

PROGRAM NLTE

C THIS PROGRAM INVESTIGATES LTE and NLTE EFFECT IN OH (NONGRAY CASE)  
C THIS PROGRAM IS WRITTEN BY MANOJ K. JHA IN OCTOBER 1992

C IMPLICIT DOUBLE PRECISION (A-H,O-Z)

DOUBLE PRECISION IERR

REAL L,KFB

EXTERNAL F10,F11,F12,F13,F14

DIMENSION U(9),PRES(4),TEMP(4),EPS(2)

COMMON F

OPEN (1,FILE='out11ca')

OPEN (2,FILE='nlp')

OPEN (3,FILE='lp')

DATA U/0.1,0.5,1.,5.,10.,20.,50.,75.,100./

DATA PRES/0.1,1.,5.,10./

DATA TEMP/300.,500.,1000.,2000./

WRITE (1,11)

write(2,13)

write(2,\*) 9,1

13 format('3',/, 'x',/, 't',/, 't1',/,i4,x,'1')

write(3,14)

write(3,\*) 9,1

14 format('2',/, 'x',/, 't',/,/,i4,x,'1')

DO 4 IT=1,4

TW=TEMP(IT)

DO 5 KK=1,4

P=PRES(KK)

DO 6 I=1,9

L=U(I)

TK1=TW\*\*2.

TK2=TW\*\*0.5

TK3=TW/273.

HCK=1.439257246

TS=300./TW

WNB=3570.

C2B=HCK\*WNB

CCC=0.000053847734

CCB=CCC\*(WNB\*\*4.)

TB=C2B/TW

TEB=EXP(TB)

C1B=CCB/C2B

PFB=C1B/(TEB-1.)

DEV=TK1\*((TEB-1.)\*\*2.)

PFDB=(CCB\*TEB)/DEV

AK1=(TW/300.)\*\*0.5

AK2=(300./TW)\*\*1.5

AZ=117.\*AK1

IF (TW.EQ.300.) THEN

KFB=4879.71

```

ELSEIF (TW.EQ.500.) THEN
KFB=6993.13
ELSEIF (TW.EQ.1000.) THEN
KFB=11504.56
ELSEIF (TW.EQ.2000.) THEN
KFB=20276.33
ENDIF
AMB=H/KFB
OMEG=3570.
TX=-(HCK/TW)
TX1=TX*OMEG
ETX1=EXP(TX1)
C1=1.-ETX1
S=110.*TS
CZ=S/AZ
PL=P*L
UZ=CZ*PL

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C

C We assume BS and PE as defined for NO

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C

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c PHI1=(15.15+(0.22*((TW/100.)**1.5)))*C1
c DEL1=((PHI1**2.)/AK1)*0.001
c BS=0.314*DEL1
c PE=(1.1*P)**0.8
PE=P**0.65
BS=0.1042117/ak1
BETA=BS*PE
F=2.94*(1.-EXP(-(2.6*BETA)))
EPS(2)=1.E-04
EPS(1)=1.E-04
X1=0.
X2=(3./8.)*UZ
Y1=1.5*UZ
Y2=3.*X2
CALL QDAGS (F10,X1,Y1,EPS(2),EPS(1),R0,IERR)
CALL QDAGS (F11,X1,Y1,EPS(2),EPS(1),R1,IERR)
CALL QDAGS (F12,X1,Y1,EPS(2),EPS(1),R2,IERR)
CALL QDAGS (F13,X1,Y1,EPS(2),EPS(1),R3,IERR)
CALL QDAGS (F14,X1,Y1,EPS(2),EPS(1),R4,IERR)
CALL QDAGS (F10,X2,Y2,EPS(2),EPS(1),S1,IERR)
CALL QDAGS (F11,X1,X2,EPS(2),EPS(1),S2,IERR)
CALL QDAGS (F11,X1,Y2,EPS(2),EPS(1),S3,IERR)
CALL QDAGS (F12,X2,Y2,EPS(2),EPS(1),S4,IERR)
CALL QDAGS (F13,X1,X2,EPS(2),EPS(1),S5,IERR)
CALL QDAGS (F13,X1,Y2,EPS(2),EPS(1),S6,IERR)
CALL QDAGS (F14,X2,Y2,EPS(2),EPS(1),S7,IERR)
H=AZ*PFDB
AM=(H*L)/KFB
CU=2./(3.*UZ)

```

BU=1./CU  
 BR1A=(CU\*R1)-(2.\*(CU\*\*3)\*R3)+((CU\*\*4)\*R4)  
 BR1B=((CU\*\*2)\*R2)-(CU\*R1)  
 ETC1=1.16\*1.E-3\*((9.)\*\*0.5)\*(2700.\*\*4./3.)  
 ETC2=TW\*\*(-1./3.)-0.015\*((9.)\*\*0.25)  
 ETC3=ETC1\*ETC2-18.42  
 ETC4=EXP(ETC3)  
 ETAC=ETC4/P  
 c ETC1=(8.5)\*\*(1./4.)  
 c ETC2=0.015\*ETC1  
 c ETC3=TW\*\*(-1./3.)  
 c ETC4=ETC3-ETC2  
 c ETC5=175.\*ETC4  
 c ETC6=(ETC5-18.42)  
 c ETC7=EXP(ETC6)  
 c ETAC=ETC7/P  
 ETAR1=8.\*3.14\*(3570.\*\*2.))\*\*4.08\*(1.E-12)\*s\*tw  
 ETAR=1./ETAR1  
 ETA=ETAC/ETAR  
 SUMA=H\*BR1A  
 AL1L=1.+(L/KFB)\*SUMA  
 ALPH1=AL1L-((9./2.)\*ETA\*CU\*BR1B)  
 BR2A=((CU\*\*2)\*R2)-(2.\*(CU\*\*3)\*R3)+((CU\*\*4)\*R4)  
 BR2B=R0-(6.\*CU\*R1)+(6.\*(CU\*\*2)\*R2)  
 SUMB=H\*BR2A  
 AL2L=(L/KFB)\*SUMB  
 ALPH2=AL2L-((3./4.)\*ETA\*CU\*BR2B)  
 ALPH0 = (9./2.)\*ETA\*(CU\*\*2.)\*(CU\*R2-R1)-1.  
 BR3A=((57./256.)\*S1)+((11./16.)\*CU\*(S2+S3))  
 \*-(9./8.)\*(CU\*\*2.)\*S4-((CU\*\*3.)\*(S5+S6))+((CU\*\*4.)\*S7)  
 BR3B=((9./4.)\*CU\*S1)+(6.\*(CU\*\*2.)\*(S2+S3))  
 \*-(12\*(CU\*\*3.)\*S4)  
 SUMC=H\*BR3A  
 AL3L=((L/KFB)\*SUMC)+(11./16.)  
 ALPH3 =AL3L+((3./8.)\*ETA\*BR3B)  
 BR4A=((9./256.)\*S1)+((3./16.)\*CU\*(S2+S3))  
 \*-(1./8.)\*(CU\*\*2.)\*S4-((CU\*\*3.)\*(S5+S6))+((CU\*\*4.)\*S7)  
 BR4B=((1./4.)\*CU\*S1)+(6.\*(CU\*\*2.)\*(S2+S3))-12\*(CU\*\*3.)\*S4  
 SUMD=H\*BR4A  
 AL4L=((L/KFB)\*SUMD)+(3./16.)  
 ALPH4 =AL4L+((3./8.)\*ETA\*BR4B)  
 BRK5=(3./16.)\*(CU\*S1)+(1./2.)\*(CU\*\*2.)\*(S2+S3)-(CU\*\*3.)\*S4  
 ALPH5 = -(9./2.)\*ETA\*BRK5+(11./16.)  
 DENA = (ALPH1\*ALPH4)-(ALPH2\*ALPH3)  
 A1=((ALPH0\*ALPH4)-(ALPH2\*ALPH5))/DENA  
 A2=((ALPH1\*ALPH5)-(ALPH0\*ALPH3))/DENA  
 TBULK = (1./70.)\*((17.\*A1)+(3.\*A2))  
 CONST=1./16.\*(AL1L\*AL4L-AL2L\*AL3L))  
 a1L=(11.\*aL2L-16.\*aL4L)\*CONST

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A2L=(16.*AL3L-11.*AL1L)*CONST
TBULKL=(1/70.)*(17.*A1L+3.*A2L)
WRITE (1,19) TW,P,L,-TBULK,-TBULKL
WRITE (2,20) L,-TBULKL,-TBULK
WRITE (3,21) L,- TBULK
6 CONTINUE
5 CONTINUE
4 CONTINUE
write(*,*) etac,etar,eta
19 FORMAT (1X,F7.2,2(3X,F6.2),2(3X,E10.4))
20 FORMAT (3X,F6.2,2(3X,E10.4))
21 FORMAT (3X,F6.2,3X,E10.4)
11 FORMAT (4X, 'TW',8X, 'P',6X, 'L',9X, 'TBULK',9X, 'TBULKL')
STOP
END

```

C

```

FUNCTION F10(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F10=AUD
RETURN
END
FUNCTION F11(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F11=AUD*U
RETURN
END
FUNCTION F12(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F12=AUD*(U**2.)
RETURN
END
FUNCTION F13(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F13=AUD*(U**3.)
RETURN
END
FUNCTION F14(U)
COMMON F
DEN=(F*((U**2.)+(2.*U)+2.)+U)*(U+(2.*F))
AUD=(F*((U**2.)+(4.*U*F)+(4.*F)))/DEN
F14=AUD*(U**4.)

```

RETURN  
END

## NONGRAY RESULTS FOR OH

TW	P	L	TBULK (NLTE)	TBULK (LTE)	TBULK (LTE)
300.00	0.10	0.10	0.2429E+00	0.2429E+00	0.2429E+00
300.00	0.10	0.50	0.2429E+00	0.2429E+00	0.2429E+00
300.00	0.10	1.00	0.2429E+00	0.2429E+00	0.2429E+00
300.00	0.10	5.00	0.2429E+00	0.2429E+00	0.2429E+00
300.00	0.10	10.00	0.2429E+00	0.2428E+00	0.2428E+00
300.00	0.10	20.00	0.2429E+00	0.2428E+00	0.2428E+00
300.00	0.10	50.00	0.2428E+00	0.2427E+00	0.2427E+00
300.00	0.10	75.00	0.2428E+00	0.2425E+00	0.2425E+00
300.00	0.10	100.00	0.2427E+00	0.2424E+00	0.2424E+00
300.00	1.00	0.10	0.2429E+00	0.2429E+00	0.2429E+00
300.00	1.00	0.50	0.2429E+00	0.2429E+00	0.2429E+00
300.00	1.00	1.00	0.2429E+00	0.2429E+00	0.2429E+00
300.00	1.00	5.00	0.2428E+00	0.2428E+00	0.2428E+00
300.00	1.00	10.00	0.2428E+00	0.2428E+00	0.2428E+00
300.00	1.00	20.00	0.2427E+00	0.2426E+00	0.2426E+00
300.00	1.00	50.00	0.2423E+00	0.2422E+00	0.2422E+00
300.00	1.00	75.00	0.2419E+00	0.2418E+00	0.2418E+00
300.00	1.00	100.00	0.2416E+00	0.2415E+00	0.2415E+00
300.00	5.00	0.10	0.2429E+00	0.2429E+00	0.2429E+00
300.00	5.00	0.50	0.2429E+00	0.2429E+00	0.2429E+00
300.00	5.00	1.00	0.2428E+00	0.2428E+00	0.2428E+00
300.00	5.00	5.00	0.2428E+00	0.2428E+00	0.2428E+00
300.00	5.00	10.00	0.2427E+00	0.2427E+00	0.2427E+00
300.00	5.00	20.00	0.2426E+00	0.2426E+00	0.2426E+00
300.00	5.00	50.00	0.2421E+00	0.2421E+00	0.2421E+00
300.00	5.00	75.00	0.2417E+00	0.2417E+00	0.2417E+00
300.00	5.00	100.00	0.2413E+00	0.2413E+00	0.2413E+00
300.00	10.00	0.10	0.2429E+00	0.2429E+00	0.2429E+00
300.00	10.00	0.50	0.2429E+00	0.2429E+00	0.2429E+00
300.00	10.00	1.00	0.2428E+00	0.2428E+00	0.2428E+00
300.00	10.00	5.00	0.2428E+00	0.2428E+00	0.2428E+00
300.00	10.00	10.00	0.2427E+00	0.2427E+00	0.2427E+00
300.00	10.00	20.00	0.2425E+00	0.2425E+00	0.2425E+00
300.00	10.00	50.00	0.2421E+00	0.2421E+00	0.2421E+00
300.00	10.00	75.00	0.2417E+00	0.2417E+00	0.2417E+00
300.00	10.00	100.00	0.2413E+00	0.2413E+00	0.2413E+00
500.00	0.10	0.10	0.2429E+00	0.2429E+00	0.2429E+00
500.00	0.10	0.50	0.2428E+00	0.2428E+00	0.2428E+00
500.00	0.10	1.00	0.2428E+00	0.2428E+00	0.2428E+00
500.00	0.10	5.00	0.2423E+00	0.2418E+00	0.2418E+00
500.00	0.10	10.00	0.2410E+00	0.2399E+00	0.2399E+00
500.00	0.10	20.00	0.2373E+00	0.2353E+00	0.2353E+00
500.00	0.10	50.00	0.2212E+00	0.2170E+00	0.2170E+00
500.00	0.10	75.00	0.2043E+00	0.1987E+00	0.1987E+00

500.00	0.10	100.00	0.1864E+00	0.1799E+00
500.00	1.00	0.10	0.2429E+00	0.2428E+00
500.00	1.00	0.50	0.2427E+00	0.2427E+00
500.00	1.00	1.00	0.2423E+00	0.2423E+00
500.00	1.00	5.00	0.2359E+00	0.2355E+00
500.00	1.00	10.00	0.2246E+00	0.2239E+00
500.00	1.00	20.00	0.2006E+00	0.1997E+00
500.00	1.00	50.00	0.1448E+00	0.1441E+00
500.00	1.00	75.00	0.1158E+00	0.1153E+00
500.00	1.00	100.00	0.9615E-01	0.9576E-01
500.00	5.00	0.10	0.2428E+00	0.2428E+00
500.00	5.00	0.50	0.2422E+00	0.2422E+00
500.00	5.00	1.00	0.2408E+00	0.2407E+00
500.00	5.00	5.00	0.2255E+00	0.2254E+00
500.00	5.00	10.00	0.2073E+00	0.2072E+00
500.00	5.00	20.00	0.1782E+00	0.1781E+00
500.00	5.00	50.00	0.1256E+00	0.1255E+00
500.00	5.00	75.00	0.1010E+00	0.1010E+00
500.00	5.00	100.00	0.8468E-01	0.8466E-01
500.00	10.00	0.10	0.2428E+00	0.2428E+00
500.00	10.00	0.50	0.2417E+00	0.2417E+00
500.00	10.00	1.00	0.2397E+00	0.2397E+00
500.00	10.00	5.00	0.2223E+00	0.2223E+00
500.00	10.00	10.00	0.2037E+00	0.2036E+00
500.00	10.00	20.00	0.1748E+00	0.1748E+00
500.00	10.00	50.00	0.1235E+00	0.1235E+00
500.00	10.00	75.00	0.9959E-01	0.9959E-01
500.00	10.00	100.00	0.8361E-01	0.8360E-01
1000.00	0.10	0.10	0.2428E+00	0.2428E+00
1000.00	0.10	0.50	0.2426E+00	0.2426E+00
1000.00	0.10	1.00	0.2419E+00	0.2419E+00
1000.00	0.10	5.00	0.2262E+00	0.2256E+00
1000.00	0.10	10.00	0.1985E+00	0.1975E+00
1000.00	0.10	20.00	0.1512E+00	0.1501E+00
1000.00	0.10	50.00	0.7990E-01	0.7940E-01
1000.00	0.10	75.00	0.5358E-01	0.5329E-01
1000.00	0.10	100.00	0.3841E-01	0.3821E-01
1000.00	1.00	0.10	0.2427E+00	0.2427E+00
1000.00	1.00	0.50	0.2404E+00	0.2404E+00
1000.00	1.00	1.00	0.2342E+00	0.2342E+00
1000.00	1.00	5.00	0.1547E+00	0.1545E+00
1000.00	1.00	10.00	0.9228E-01	0.9217E-01
1000.00	1.00	20.00	0.4460E-01	0.4455E-01
1000.00	1.00	50.00	0.1441E-01	0.1440E-01
1000.00	1.00	75.00	0.8609E-02	0.8605E-02
1000.00	1.00	100.00	0.5995E-02	0.5992E-02
1000.00	5.00	0.10	0.2423E+00	0.2423E+00
1000.00	5.00	0.50	0.2321E+00	0.2321E+00
1000.00	5.00	1.00	0.2096E+00	0.2096E+00



1000.00	5.00	5.00	0.8363E-01	0.8361E-01
1000.00	5.00	10.00	0.4284E-01	0.4283E-01
1000.00	5.00	20.00	0.2094E-01	0.2093E-01
1000.00	5.00	50.00	0.8028E-02	0.8028E-02
1000.00	5.00	75.00	0.5265E-02	0.5264E-02
1000.00	5.00	100.00	0.3908E-02	0.3908E-02
1000.00	10.00	0.10	0.2418E+00	0.2418E+00
1000.00	10.00	0.50	0.2237E+00	0.2237E+00
1000.00	10.00	1.00	0.1905E+00	0.1905E+00
1000.00	10.00	5.00	0.6669E-01	0.6668E-01
1000.00	10.00	10.00	0.3526E-01	0.3526E-01
1000.00	10.00	20.00	0.1810E-01	0.1810E-01
1000.00	10.00	50.00	0.7351E-02	0.7351E-02
1000.00	10.00	75.00	0.4917E-02	0.4917E-02
1000.00	10.00	100.00	0.3694E-02	0.3694E-02
2000.00	0.10	0.10	0.2428E+00	0.2428E+00
2000.00	0.10	0.50	0.2426E+00	0.2426E+00
2000.00	0.10	1.00	0.2417E+00	0.2417E+00
2000.00	0.10	5.00	0.2212E+00	0.2212E+00
2000.00	0.10	10.00	0.1832E+00	0.1831E+00
2000.00	0.10	20.00	0.1232E+00	0.1231E+00
2000.00	0.10	50.00	0.5555E-01	0.5551E-01
2000.00	0.10	75.00	0.3701E-01	0.3698E-01
2000.00	0.10	100.00	0.2721E-01	0.2720E-01
2000.00	1.00	0.10	0.2427E+00	0.2427E+00
2000.00	1.00	0.50	0.2401E+00	0.2401E+00
2000.00	1.00	1.00	0.2327E+00	0.2327E+00
2000.00	1.00	5.00	0.1353E+00	0.1353E+00
2000.00	1.00	10.00	0.7122E-01	0.7122E-01
2000.00	1.00	20.00	0.3131E-01	0.3131E-01
2000.00	1.00	50.00	0.9162E-02	0.9162E-02
2000.00	1.00	75.00	0.5161E-02	0.5161E-02
2000.00	1.00	100.00	0.3423E-02	0.3423E-02
2000.00	5.00	0.10	0.2423E+00	0.2423E+00
2000.00	5.00	0.50	0.2302E+00	0.2302E+00
2000.00	5.00	1.00	0.2021E+00	0.2021E+00
2000.00	5.00	5.00	0.5888E-01	0.5888E-01
2000.00	5.00	10.00	0.2506E-01	0.2506E-01
2000.00	5.00	20.00	0.1043E-01	0.1043E-01
2000.00	5.00	50.00	0.3394E-02	0.3394E-02
2000.00	5.00	75.00	0.2108E-02	0.2108E-02
2000.00	5.00	100.00	0.1515E-02	0.1515E-02
2000.00	10.00	0.10	0.2417E+00	0.2417E+00
2000.00	10.00	0.50	0.2195E+00	0.2195E+00
2000.00	10.00	1.00	0.1762E+00	0.1762E+00
2000.00	10.00	5.00	0.3993E-01	0.3993E-01
2000.00	10.00	10.00	0.1742E-01	0.1742E-01
2000.00	10.00	20.00	0.7739E-02	0.7739E-02
2000.00	10.00	50.00	0.2778E-02	0.2778E-02

2000.00	10.00	75.00	0.1793E-02	0.1793E-02
2000.00	10.00	100.00	0.1320E-02	0.1320E-02

C THIS PROGRAM SOLVES FOR BULK TEMPERATURE FOR CO\_2  
 C UNDER NONGRAY ASSUMPTION. THE PROGRAM CAN CALCULATE BULK  
 C TEMPERATURE UNDER BOTH LTE AND NLTE CONDITIONS.  
 c IMPLICIT DOUBLE PRECISION (A-H,O-Z)

DOUBLE PRECISION IERR

REAL L,KFB

EXTERNAL F101,F102,F103,F111,F112,F113,F121,F122,F123,F131,F132,  
 \*F133,F141,F142,F143

DIMENSION U(9),PRES(4),TEMP(4),EPS(3)

COMMON F1,F2,F3

OPEN(6,file='output1')

open(7,file='nlp')

open(8,file='lp')

DATA U/0.1,0.5,1.0,5.0,10.0,20.0,50.0,75.,100.0/

DATA PRES/0.1,1.,5.,10.0/

DATA TEMP/300.,500.,1000.0,2000.0/

WRITE(6,111)

write(7,13)

write(7,\*) 9,1

13 format('3',/, 'x',/, 't',/, 't1',/,i4,x,'1')

write(8,14)

write(8,\*) 9,1

14 format('2',/, 'x',/, 't',/,/,i4,x,'1')

DO 44 IT = 1,4

TW = TEMP(IT)

DO 55 KK = 1,4

P = PRES(KK)

DO 66 I = 1, 9

L= U(I)

C

C CALCULATION OF PLANK'S FUNCTION IT'S DERIVATIVES

C

C WNB BAND CENTER (1/CM)

C HCK CONSTANT (K CM)

C CCC C1\*C2 (ERG-K-CM\*\*3?SEC)

C PFDBI PLANCK FUNCTION DERIVATIVE FOR I BAND

C

CESS = TW\*\*2

STU = TW\*\*0.5

SNT = TW/273.

HCK = 1.439257246

AK1 = (TW/300.)\*\*0.5

TS = 300./TW

C

C SPECTROSCOPIC PROPERTIES OF CO2

C HERE WE HAVE CONSIDERED ONLY THREE BANDS(15,4.3 & 2.7 MICRONS)

C WNBI BAND CENTER (1/CM)

C

WNB1 = 667.

WNB2 = 2347.  
 WNB3 = 3716.  
 C2B1 = HCK\*WNB1  
 C2B2 = HCK\*WNB2  
 C2B3 = HCK\*WNB3  
 CCC = 0.000053847734  
 CCB1 = CCC\*(WNB1\*\*4)  
 CCB2 = CCC\*(WNB2\*\*4)  
 CCB3 = CCC\*(WNB3\*\*4)  
 TB1 = C2B1/TW  
 TB2 = C2B2/TW  
 TB3 = C2B3/TW  
 TEB1 = EXP(TB1)  
 TEB2 = EXP(TB2)  
 TEB3 = EXP(TB3)  
 SNTB1 = CESS\*((TEB1-1.)\*\*2.)  
 SNTB2 = CESS\*((TEB2-1.)\*\*2.)  
 SNTB3 = CESS\*((TEB3-1.)\*\*2.)  
 PFDB1 = (CCB1\*TEB1)/SNTB1  
 PFDB2 = (CCB2\*TEB2)/SNTB2  
 PFDB3 = (CCB3\*TEB3)/SNTB3

---

C  
 C BAND MODEL CORRELATIONS (TIEN & LOWDER WIDE BAND MODEL)  
 C AZI AOI (1/CM)  
 C CZSI COI\*\*2 (1/(ATM-CM))  
 C BSI B\*\*2 (NON DIMENSIONAL)  
 C OMGI WAVE NUMBER (1/CM)  
 C SI INTEGRATED BAND INTENSITY (1/(ATM CM\*\*2))  
 C

---

AK1 = (TW/300.)\*\*0.5  
 AK2 = (300./TW)\*\*1.5  
 AZ1 = 1.29\*STU  
 AZ2 = 1.15\*STU  
 AZ3 = 2.4\*STU

---

C  
 C DKF THERMAL CONDUCTIVITY (ERG/CM-SEC-K)  
 C

---

KFB = (1488.365171)\*(SNT\*\*1.23)  
 AMB = H/KFB  
 OMG1 = 1351.0  
 OMG2 = 667.0  
 OMG3 = 2396.0  
 TX = -(HCK/TW)  
 TX1 = TX\*OMG1  
 TX2 = TX\*OMG2  
 TX3 = TX\*OMG3  
 ETX1 = EXP(TX1)  
 ETX2 = EXP(TX2)  
 ETX3 = EXP(TX3)

```

C1 = 1.0-ETX1
C2 = 1.0-ETX2
C3 = 1.0-ETX3
BRKT = TX*(OMG1+OMG3)
PHI2 = (1.0- EXP(BRKT))/(C1*C3)
TS = 300.0/TW
S1 = 339.685*TS
S2 = 2702.7*TS
S3 = 71.497*TS*PHI2
CZS1 = S1/AZ1
CZS2 = S2/AZ2
CZS3 = S3/AZ3
C-----
C  PL PRESSURE PATH LENGTH (ATM-CM)
C-----
PL = P* L
UZ1 = CZS1*PL
UZ2 = CZS2*PL
UZ3 = CZS3*PL
BS1 = 0.0841*AK1
BS2 = 0.32895*AK1
PHI3 = 1.0+0.053*((TW/100.0)**1.5)
DEL2 = (PHI3**2.0)/(PHI2 *AK1)
BS3 = 0.1112*DEL2
C-----
C  PEI EFFECTIVE PRESSURE FOR EACH BAND (NON DIMENSIONAL)
C-----
PE1 = (1.3*P)**0.7
PE2 = (1.3*P)**0.8
PE3 = (1.3*P)**0.65
C-----
C  BETAI LINE STRUCTURE PARAMETR
C-----
BETA1 = BS1*PE1
BETA2 = BS2*PE2
BETA3 = BS3*PE3
C-----
C  CORRELATION FOR EACH BAND
C-----
F1 = 2.94*(1.0- EXP(-(2.6*BETA1)))
F2 = 2.94*(1.0- EXP(-(2.6*BETA2)))
F3 = 2.94*(1.0- EXP(-(2.6*BETA3)))
C-----
C  NUMERICAL INTEGRATION
C-----
EPS(2) = 1E-04
EPS(1) = 1E-04
EP = 1.E-5
X1 = 0.0

```

```

X21 = (3./8.)*UZ1
X22 = (3./8.)*UZ2
X23 = (3./8.)*UZ3
Y11 = 1.5*UZ1
Y12 = 1.5*UZ2
Y13 = 1.5*UZ3
Y21 = 3.0*X21
Y22 = 3.0*X22
Y23 = 3.0*X23
CALL QDAGS (F101,X1,Y11,EPS(2),EPS(1),R01,IERR)
CALL QDAGS (F102,X1,Y12,EPS(2),EPS(1),R02,IERR)
CALL QDAGS (F103,X1,Y13,EPS(2),EPS(1),R03,IERR)
CALL QDAGS(F111,X1,Y11,EPS(2),EPS(1),R11,IERR)
CALL QDAGS(F112,X1,Y12,EPS(2),EPS(1),R12,IERR)
CALL QDAGS(F113,X1,Y13,EPS(2),EPS(1),R13,IERR)
CALL QDAGS(F121,X1,Y11,EPS(2),EPS(1),R21,IERR)
CALL QDAGS(F122,X1,Y12,EPS(2),EPS(1),R22,IERR)
CALL QDAGS(F123,X1,Y13,EPS(2),EPS(1),R23,IERR)
CALL QDAGS(F131,X1,Y11,EPS(2),EPS(1),R31,IERR)
CALL QDAGS(F132,X1,Y12,EPS(2),EPS(1),R32,IERR)
CALL QDAGS(F133,X1,Y13,EPS(2),EPS(1),R33,IERR)
CALL QDAGS(F141,X1,Y11,EPS(2),EPS(1),R41,IERR)
CALL QDAGS(F142,X1,Y12,EPS(2),EPS(1),R42,IERR)
CALL QDAGS(F143,X1,Y13,EPS(2),EPS(1),R43,IERR)
CALL QDAGS(F101,X21,Y21,EPS(2),EPS(1),S11,IERR)
CALL QDAGS(F102,X22,Y22,EPS(2),EPS(1),S12,IERR)
CALL QDAGS(F103,X23,Y23,EPS(2),EPS(1),S13,IERR)
CALL QDAGS(F111,X1,X21,EPS(2),EPS(1),S21,IERR)
CALL QDAGS(F112,X1,X22,EPS(2),EPS(1),S22,IERR)
CALL QDAGS(F113,X1,X23,EPS(2),EPS(1),S23,IERR)
CALL QDAGS(F111,X1,Y21,EPS(2),EPS(1),S31,IERR)
CALL QDAGS(F112,X1,Y22,EPS(2),EPS(1),S32,IERR)
CALL QDAGS(F113,X1,Y23,EPS(2),EPS(1),S33,IERR)
CALL QDAGS(F121,X21,Y21,EPS(2),EPS(1),S41,IERR)
CALL QDAGS(F122,X22,Y22,EPS(2),EPS(1),S42,IERR)
CALL QDAGS(F123,X23,Y23,EPS(2),EPS(1),S43,IERR)
CALL QDAGS(F131,X1,X21,EPS(2),EPS(1),S51,IERR)
CALL QDAGS(F132,X1,X22,EPS(2),EPS(1),S52,IERR)
CALL QDAGS(F133,X1,X23,EPS(2),EPS(1),S53,IERR)
CALL QDAGS(F131,X1,Y21,EPS(2),EPS(1),S61,IERR)
CALL QDAGS(F132,X1,Y22,EPS(2),EPS(1),S62,IERR)
CALL QDAGS(F133,X1,Y23,EPS(2),EPS(1),S63,IERR)
CALL QDAGS(F141,X21,Y21,EPS(2),EPS(1),S71,IERR)
CALL QDAGS(F142,X22,Y22,EPS(2),EPS(1),S72,IERR)
CALL QDAGS(F143,X23,Y23,EPS(2),EPS(1),S73,IERR)
H1=AZ1*PFDB1
H2=AZ2*PFDB2
H3=AZ3*PFDB3
H=H1+H2+H3

```

$AM = (H \cdot L) / KFB$   
 $CU1 = 2. / (3. \cdot UZ1)$   
 $CU2 = 2. / (3. \cdot UZ2)$   
 $CU3 = 2. / (3. \cdot UZ3)$   
 $BR1A1 = (CU1 \cdot R11) - 2. \cdot (CU1^{**3.}) \cdot R31 + (CU1^{**4.}) \cdot R41$   
 $BR1A2 = (CU2 \cdot R12) - 2. \cdot (CU2^{**3.}) \cdot R32 + (CU2^{**4.}) \cdot R42$   
 $BR1A3 = (CU3 \cdot R13) - 2. \cdot (CU3^{**3.}) \cdot R33 + (CU3^{**4.}) \cdot R43$   
 $BR1B1 = ((CU1^{**2.}) \cdot R21) - (CU1 \cdot R11)$   
 $BR1B2 = ((CU2^{**2.}) \cdot R22) - (CU2 \cdot R12)$   
 $BR1B3 = ((CU3^{**2.}) \cdot R23) - (CU3 \cdot R13)$   
 $ETC1 = ((36.5 \cdot (TW^{**(-1/3.))}) + 3.9)$   
 $ETC2 = EXP(ETC1) \cdot (1.E-6)$   
 $ETAC = ETC2 / P$   
 $ETR11 = 8. \cdot 3.14 \cdot (667. \cdot (2.)) \cdot 4.08 \cdot (1.E-12) \cdot 300. \cdot 339.685$   
 $ETAR1 = 1. / ETR11$   
 $ETR12 = 8. \cdot 3.14 \cdot (2347. \cdot (2.)) \cdot 4.08 \cdot (1.E-12) \cdot 300. \cdot 2702.7$   
 $ETAR2 = 1. / ETR12$   
 $ETR13 = 8. \cdot 3.14 \cdot (3716. \cdot (2.)) \cdot 4.08 \cdot (1.E-12) \cdot 300. \cdot 71.497 \cdot PHI2$   
 $ETAR3 = 1. / ETR13$   
 $ETA11 = ETAC / ETAR1$   
 $ETA12 = ETAC / ETAR2$   
 $ETA13 = ETAC / ETAR3$   
 $SUMA1 = H1 \cdot BR1A1$   
 $SUMA2 = H2 \cdot BR1A2$   
 $SUMA3 = H3 \cdot BR1A3$   
 $SUMAL = SUMA1 + SUMA2 + SUMA3$   
 $AL1L = 1. + (L / KFB) \cdot SUMAL$   
 $SUMAN1 = ETA11 \cdot CU1 \cdot BR1B1$   
 $SUMAN2 = ETA12 \cdot CU2 \cdot BR1B2$   
 $SUMAN3 = ETA13 \cdot CU3 \cdot BR1B3$   
 $SUMAN = (9. / 2.) \cdot (SUMAN1 + SUMAN2 + SUMAN3)$   
 $ALPH1 = AL1L - SUMAN$   
 $BR2A1 = (CU1^{**2.}) \cdot R21 - 2. \cdot (CU1^{**3.}) \cdot R31 + (CU1^{**4.}) \cdot R41$   
 $BR2A2 = (CU2^{**2.}) \cdot R22 - 2. \cdot (CU2^{**3.}) \cdot R32 + (CU2^{**4.}) \cdot R42$   
 $BR2A3 = (CU3^{**2.}) \cdot R23 - 2. \cdot (CU3^{**3.}) \cdot R33 + (CU3^{**4.}) \cdot R43$   
 $BR2B1 = R01 - (6. \cdot CU1 \cdot R11) + (6. \cdot (CU1^{**2.}) \cdot R21)$   
 $BR2B2 = R02 - (6. \cdot CU2 \cdot R12) + (6. \cdot (CU2^{**2.}) \cdot R22)$   
 $BR2B3 = R03 - (6. \cdot CU3 \cdot R13) + (6. \cdot (CU3^{**2.}) \cdot R23)$   
 $SUMB1 = H1 \cdot BR2A1$   
 $SUMB2 = H2 \cdot BR2A2$   
 $SUMB3 = H3 \cdot BR2A3$   
 $SUMBL = SUMB1 + SUMB2 + SUMB3$   
 $SUMBN1 = ETA11 \cdot CU1 \cdot BR2B1$   
 $SUMBN2 = ETA12 \cdot CU2 \cdot BR2B2$   
 $SUMBN3 = ETA13 \cdot CU3 \cdot BR2B3$   
 $SUMBN = (3. / 4.) \cdot (SUMBN1 + SUMBN2 + SUMBN3)$   
 $AL2L = (L / KFB) \cdot SUMBL$   
 $ALPH2 = AL2L - SUMBN$   
 $ALPH01 = ETA11 \cdot (CU1^{**2.}) \cdot (CU1 \cdot R21 - R11)$

ALPH02=ETA12\*(CU2\*\*2)\*(CU2\*R22-R12)  
 ALPH03=ETA13\*(CU3\*\*2)\*(CU3\*R23-R13)  
 ALPH0=(9./2.)\*(ALPH01+ALPH02+ALPH03)-1.  
 BR3A1 = (57./256.)\*S11+(11./16.)\*CU1\*(S21+S31)  
 \*-(9./8.)\*(CU1\*\*2)\*S41-(CU1\*\*3.)\*(S51+S61)+(CU1\*\*4.)\*S71  
 BR3A2 = (57./256.)\*S12+(11./16.)\*CU2\*(S22+S32)  
 \*-(9./8.)\*(CU2\*\*2)\*S42-(CU2\*\*3.)\*(S52+S62)+(CU2\*\*4.)\*S72  
 BR3A3 = (57./256.)\*S13+(11./16.)\*CU3\*(S23+S33)  
 \*-(9./8.)\*(CU3\*\*2)\*S43-(CU3\*\*3.)\*(S53+S63)+(CU3\*\*4.)\*S73  
 BR3B1=((9./4.)\*CU1\*S11)+(6.\*(CU1\*\*2.)\*(S21+S31))  
 \*-(12\*(CU1\*\*3.)\*S41)  
 BR3B2=((9./4.)\*CU2\*S12)+(6.\*(CU2\*\*2.)\*(S22+S32))  
 \*-(12\*(CU2\*\*3.)\*S42)  
 BR3B3=((9./4.)\*CU3\*S13)+(6.\*(CU3\*\*2.)\*(S23+S33))  
 \*-(12\*(CU3\*\*3.)\*S43)  
 SUMC1 = H1\*BR3A1  
 SUMC2 = H2\*BR3A2  
 SUMC3 = H3\*BR3A3  
 SUMCL=SUMC1+SUMC2+SUMC3  
 SUMCN1=ETA11\*BR3B1  
 SUMCN2=ETA12\*BR3B2  
 SUMCN3=ETA13\*BR3B3  
 SUMCN=(3./8.)\*(SUMCN1+SUMCN2+SUMCN3)  
 AL3L = (11./16.)+(L/KFB)\*SUMCL  
 ALPH3=AL3L+SUMCN  
 BR4A1 = (9.0/256.)\*S11+(3.0/16.)\*CU1\*(S21+S31)  
 \*-(1./8.)\*(CU1\*\*2)\*S41-(CU1\*\*3.)\*(S51+S61)+(CU1\*\*4.)\*S71  
 BR4A2 = (9.0/256.)\*S12+(3.0/16.)\*CU2\*(S22+S32)  
 \*-(1./8.)\*(CU2\*\*2)\*S42-(CU2\*\*3.)\*(S52+S62)+(CU2\*\*4.)\*S72  
 BR4A3 = (9.0/256.)\*S13+(3.0/16.)\*CU3\*(S23+S33)  
 \*-(1./8.)\*(CU3\*\*2)\*S43-(CU3\*\*3.)\*(S53+S63)+(CU3\*\*4.)\*S73  
 BR4B1=((1./4.)\*CU1\*S11)+(6.\*(CU1\*\*2.)\*(S21+S31))-  
 \*(12.\*(CU1\*\*3.)\*S41)  
 BR4B2=((1./4.)\*CU2\*S12)+(6.\*(CU2\*\*2.)\*(S22+S32))-  
 \*(12.\*(CU2\*\*3.)\*S42)  
 BR4B3=((1./4.)\*CU3\*S13)+(6.\*(CU3\*\*2.)\*(S23+S33))-  
 \*(12.\*(CU3\*\*3.)\*S43)  
 SUMD1 = H1\*BR4A1  
 SUMD2 = H2\*BR4A2  
 SUMD3 = H3\*BR4A3  
 SUMDL=SUMD1+SUMD2+SUMD3  
 SUMDN1=ETA11\*BR4B1  
 SUMDN2=ETA12\*BR4B2  
 SUMDN3=ETA13\*BR4B3  
 SUMDN=(3./8.)\*(SUMDN1+SUMDN2+SUMDN3)  
 AL4L = (3.0/16.)+(L/KFB)\*SUMDL  
 ALPH4=AL4L+SUMDN  
 BR5B1=(3./16.)\*(CU1\*S11)+(1./2.)\*(CU1\*\*2.)\*(S21+S31)-(CU1\*\*3.)\*S41  
 BR5B2=(3./16.)\*(CU2\*S12)+(1./2.)\*(CU2\*\*2.)\*(S22+S32)-(CU2\*\*3.)\*S42



```

BR5B3=(3./16.)*(CU3*S13)+(1./2.)*(CU3**2.)*(S23+S33)-(CU3**3.)*S43
SUMEN1=ETA11*BR5B1
SUMEN2=ETA12*BR5B2
SUMEN3=ETA13*BR5B3
SUMEN=SUMEN1+SUMEN2+SUMEN3
ALPH5=-((9./2.)*SUMEN+(11./16.))
DENA = (ALPH1*ALPH4)-(ALPH2*ALPH3)
A1=((ALPH0*ALPH4)-(ALPH2*ALPH5))/DENA
A2=((ALPH1*ALPH5)-(ALPH0*ALPH3))/DENA
TBULK = (1./70.)*((17.*A1)+(3.*A2))
CONST=1./(16.*(AL1L*AL4L-AL2L*AL3L))
a1l=(11.*a12l-16.*a14l)*CONST
A2L=(16.*AL3L-11.*AL1L)*CONST
TBULKL=(1/70.)*(17.*A1L+3.*A2L)
WRITE(6,200) TW,P,L,-TBULK,-TBULKL
write(7,202)l,-tbulkl,-tbulk
write(8,201)l,-tbulk
66 CONTINUE
55 CONTINUE
44 CONTINUE
200 FORMAT(8X,F7.2, 3X,F6.2, 3X,F6.2, 2(3X,E10.4))
111 FORMAT(8X,'TW',8X,'P',6X,'L',9X,'TBULK',7X,'TBULKL')
201 format (1x,f9.2,3x,e10.4)
202 format (1x,f9.2,2(3x,e10.4))
STOP
END

```

C

```

FUNCTION F101(U1)
COMMON F1,F2,F3
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1))/DEN1
F101 = AUD1
RETURN
END
FUNCTION F102(U2)
COMMON F1,F2,F3
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = F2*((U2**2.)+(4.*U2*F2)+(4.*F2))/DEN2
F102 = AUD2
RETURN
END
FUNCTION F103(U3)
COMMON F1,F2,F3
DEN3 =((F3*((U3**2.)+2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 = (F3*((U3**2.)+(4.*U3*F3)+(4.*F3))/DEN3
F103 = AUD3
RETURN
END
FUNCTION F111(U1)

```

```

COMMON F1,F2,F3
DEN1 = (F1*((U1**2)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2)+(4.*U1*F1)+(4.*F1)))/DEN1
F111 = AUD1*U1
RETURN
END
FUNCTION F112(U2)
COMMON F1,F2,F3
DEN2 = (F2*((U2*U2)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2*U2)+(4.*U2*F2)+(4.*F2)))/DEN2
F112 = AUD2*U2
RETURN
END
FUNCTION F113(U3)
COMMON F1,F2,F3
DEN3 = (F3*((U3**2)+(2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 = (F3*((U3**2)+(4.*U3*F3)+(4.*F3)))/DEN3
F113 = AUD3*U3
RETURN
END
FUNCTION F121(U1)
COMMON F1,F2,F3
DEN1 = (F1*((U1**2)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2)+(4.*U1*F1)+(4.*F1)))/DEN1
F121 = AUD1*U1*U1
RETURN
END
FUNCTION F122(U2)
COMMON F1,F2,F3
DEN2 = (F2*((U2**2)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2)+(4.*U2*F2)+(4.*F2)))/DEN2
F122 = AUD2*U2**2.
RETURN
END
FUNCTION F123(U3)
COMMON F1,F2,F3
DEN3 = (F3*((U3**2)+(2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 = (F3*((U3**2)+(4.*U3*F3)+(4.*F3)))/DEN3
F123 = AUD3*U3*U3
RETURN
END
FUNCTION F131(U1)
COMMON F1,F2,F3
DEN1 = (F1*((U1**2)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2)+(4.*U1*F1)+(4.*F1)))/DEN1
F131 = AUD1*U1**3.
RETURN
END
FUNCTION F132(U2)

```

```

COMMON F1,F2,F3
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2.)+(4.*U2*F2)+(4.*F2)))/DEN2
F132 = AUD2*U2**3.
RETURN
END
FUNCTION F133(U3)
COMMON F1,F2,F3
DEN3 = (F3*((U3**2.)+(2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 = (F3*((U3**2.)+(4.*U3*F3)+(4.*F3)))/DEN3
F133 = AUD3*U3**3.
RETURN
END
FUNCTION F141(U1)
COMMON F1,F2,F3
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F141 = AUD1*U1**4.
RETURN
END
FUNCTION F142(U2)
COMMON F1,F2,F3
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2.)+(4.*U2*F2)+(4.*F2)))/DEN2
F142 = AUD2*U2*U2*U2*U2
RETURN
END
FUNCTION F143(U3)
COMMON F1,F2,F3
DEN3 = (F3*((U3**2.)+(2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 = (F3*((U3**2.)+(4.*U3*F3)+(4.*F3)))/DEN3
F143 = AUD3*U3**4.
RETURN
END

```

## NONGRAY RESULTS FOR CO<sub>2</sub>

TW	P	L	TBULK (NLTE)	TBULK (LTE)
300.00	0.10	0.10	0.2429E+00	0.2428E+00
300.00	0.10	0.50	0.2428E+00	0.2422E+00
300.00	0.10	1.00	0.2426E+00	0.2411E+00
300.00	0.10	5.00	0.2372E+00	0.2250E+00
300.00	0.10	10.00	0.2226E+00	0.1985E+00
300.00	0.10	20.00	0.1847E+00	0.1525E+00
300.00	0.10	50.00	0.1044E+00	0.8367E-01
300.00	0.10	75.00	0.7297E-01	0.5980E-01
300.00	0.10	100.00	0.5527E-01	0.4636E-01
300.00	1.00	0.10	0.2426E+00	0.2424E+00
300.00	1.00	0.50	0.2400E+00	0.2390E+00
300.00	1.00	1.00	0.2355E+00	0.2338E+00
300.00	1.00	5.00	0.1979E+00	0.1954E+00
300.00	1.00	10.00	0.1631E+00	0.1612E+00
300.00	1.00	20.00	0.1205E+00	0.1194E+00
300.00	1.00	50.00	0.6807E-01	0.6774E-01
300.00	1.00	75.00	0.5018E-01	0.5000E-01
300.00	1.00	100.00	0.3980E-01	0.3970E-01
300.00	5.00	0.10	0.2419E+00	0.2418E+00
300.00	5.00	0.50	0.2367E+00	0.2366E+00
300.00	5.00	1.00	0.2305E+00	0.2303E+00
300.00	5.00	5.00	0.1908E+00	0.1907E+00
300.00	5.00	10.00	0.1574E+00	0.1573E+00
300.00	5.00	20.00	0.1170E+00	0.1169E+00
300.00	5.00	50.00	0.6680E-01	0.6679E-01
300.00	5.00	75.00	0.4945E-01	0.4945E-01
300.00	5.00	100.00	0.3933E-01	0.3933E-01
300.00	10.00	0.10	0.2416E+00	0.2416E+00
300.00	10.00	0.50	0.2362E+00	0.2362E+00
300.00	10.00	1.00	0.2300E+00	0.2299E+00
300.00	10.00	5.00	0.1904E+00	0.1903E+00
300.00	10.00	10.00	0.1570E+00	0.1570E+00
300.00	10.00	20.00	0.1168E+00	0.1168E+00
300.00	10.00	50.00	0.6674E-01	0.6674E-01
300.00	10.00	75.00	0.4942E-01	0.4942E-01
300.00	10.00	100.00	0.3931E-01	0.3931E-01
500.00	0.10	0.10	0.2428E+00	0.2426E+00
500.00	0.10	0.50	0.2425E+00	0.2402E+00
500.00	0.10	1.00	0.2415E+00	0.2359E+00
500.00	0.10	5.00	0.2227E+00	0.1949E+00
500.00	0.10	10.00	0.1899E+00	0.1528E+00
500.00	0.10	20.00	0.1338E+00	0.1020E+00
500.00	0.10	50.00	0.6055E-01	0.4815E-01
500.00	0.10	75.00	0.3971E-01	0.3290E-01

500.00	0.10	100.00	0.2915E-01	0.2486E-01
500.00	1.00	0.10	0.2421E+00	0.2417E+00
500.00	1.00	0.50	0.2355E+00	0.2337E+00
500.00	1.00	1.00	0.2258E+00	0.2232E+00
500.00	1.00	5.00	0.1625E+00	0.1596E+00
500.00	1.00	10.00	0.1189E+00	0.1171E+00
500.00	1.00	20.00	0.7753E-01	0.7672E-01
500.00	1.00	50.00	0.3832E-01	0.3813E-01
500.00	1.00	75.00	0.2705E-01	0.2696E-01
500.00	1.00	100.00	0.2092E-01	0.2087E-01
500.00	5.00	0.10	0.2408E+00	0.2407E+00
500.00	5.00	0.50	0.2302E+00	0.2299E+00
500.00	5.00	1.00	0.2178E+00	0.2176E+00
500.00	5.00	5.00	0.1535E+00	0.1533E+00
500.00	5.00	10.00	0.1131E+00	0.1130E+00
500.00	5.00	20.00	0.7470E-01	0.7467E-01
500.00	5.00	50.00	0.3752E-01	0.3751E-01
500.00	5.00	75.00	0.2662E-01	0.2662E-01
500.00	5.00	100.00	0.2065E-01	0.2065E-01
500.00	10.00	0.10	0.2404E+00	0.2403E+00
500.00	10.00	0.50	0.2293E+00	0.2292E+00
500.00	10.00	1.00	0.2168E+00	0.2168E+00
500.00	10.00	5.00	0.1532E+00	0.1531E+00
500.00	10.00	10.00	0.1130E+00	0.1130E+00
500.00	10.00	20.00	0.7474E-01	0.7473E-01
500.00	10.00	50.00	0.3754E-01	0.3754E-01
500.00	10.00	75.00	0.2664E-01	0.2664E-01
500.00	10.00	100.00	0.2066E-01	0.2066E-01
1000.00	0.10	0.10	0.2428E+00	0.2424E+00
1000.00	0.10	0.50	0.2414E+00	0.2357E+00
1000.00	0.10	1.00	0.2378E+00	0.2226E+00
1000.00	0.10	5.00	0.1782E+00	0.1296E+00
1000.00	0.10	10.00	0.1151E+00	0.7718E-01
1000.00	0.10	20.00	0.5783E-01	0.3942E-01
1000.00	0.10	50.00	0.1878E-01	0.1430E-01
1000.00	0.10	75.00	0.1121E-01	0.9001E-02
1000.00	0.10	100.00	0.7800E-02	0.6491E-02
1000.00	1.00	0.10	0.2407E+00	0.2397E+00
1000.00	1.00	0.50	0.2194E+00	0.2151E+00
1000.00	1.00	1.00	0.1907E+00	0.1854E+00
1000.00	1.00	5.00	0.7829E-01	0.7591E-01
1000.00	1.00	10.00	0.4208E-01	0.4112E-01
1000.00	1.00	20.00	0.2148E-01	0.2117E-01
1000.00	1.00	50.00	0.8727E-02	0.8667E-02
1000.00	1.00	75.00	0.5866E-02	0.5839E-02
1000.00	1.00	100.00	0.4428E-02	0.4412E-02
1000.00	5.00	0.10	0.2366E+00	0.2363E+00
1000.00	5.00	0.50	0.2018E+00	0.2012E+00
1000.00	5.00	1.00	0.1647E+00	0.1642E+00

1000.00	5.00	5.00	0.6204E-01	0.6190E-01
1000.00	5.00	10.00	0.3539E-01	0.3535E-01
1000.00	5.00	20.00	0.1943E-01	0.1942E-01
1000.00	5.00	50.00	0.8438E-02	0.8436E-02
1000.00	5.00	75.00	0.5767E-02	0.5766E-02
1000.00	5.00	100.00	0.4387E-02	0.4387E-02
1000.00	10.00	0.10	0.2351E+00	0.2350E+00
1000.00	10.00	0.50	0.1957E+00	0.1955E+00
1000.00	10.00	1.00	0.1571E+00	0.1569E+00
1000.00	10.00	5.00	0.6082E-01	0.6078E-01
1000.00	10.00	10.00	0.3551E-01	0.3550E-01
1000.00	10.00	20.00	0.1973E-01	0.1972E-01
1000.00	10.00	50.00	0.8580E-02	0.8579E-02
1000.00	10.00	75.00	0.5853E-02	0.5853E-02
1000.00	10.00	100.00	0.4446E-02	0.4445E-02
2000.00	0.10	0.10	0.2428E+00	0.2426E+00
2000.00	0.10	0.50	0.2417E+00	0.2384E+00
2000.00	0.10	1.00	0.2385E+00	0.2279E+00
2000.00	0.10	5.00	0.1783E+00	0.1286E+00
2000.00	0.10	10.00	0.1098E+00	0.7039E-01
2000.00	0.10	20.00	0.4990E-01	0.3214E-01
2000.00	0.10	50.00	0.1373E-01	0.9842E-02
2000.00	0.10	75.00	0.7604E-02	0.5750E-02
2000.00	0.10	100.00	0.5028E-02	0.3948E-02
2000.00	1.00	0.10	0.2414E+00	0.2409E+00
2000.00	1.00	0.50	0.2202E+00	0.2162E+00
2000.00	1.00	1.00	0.1864E+00	0.1807E+00
2000.00	1.00	5.00	0.6093E-01	0.5875E-01
2000.00	1.00	10.00	0.2865E-01	0.2786E-01
2000.00	1.00	20.00	0.1292E-01	0.1267E-01
2000.00	1.00	50.00	0.4667E-02	0.4623E-02
2000.00	1.00	75.00	0.3050E-02	0.3030E-02
2000.00	1.00	100.00	0.2275E-02	0.2264E-02
2000.00	5.00	0.10	0.2371E+00	0.2369E+00
2000.00	5.00	0.50	0.1939E+00	0.1932E+00
2000.00	5.00	1.00	0.1471E+00	0.1465E+00
2000.00	5.00	5.00	0.4069E-01	0.4057E-01
2000.00	5.00	10.00	0.2075E-01	0.2072E-01
2000.00	5.00	20.00	0.1063E-01	0.1062E-01
2000.00	5.00	50.00	0.4458E-02	0.4457E-02
2000.00	5.00	75.00	0.3040E-02	0.3039E-02
2000.00	5.00	100.00	0.2315E-02	0.2314E-02
2000.00	10.00	0.10	0.2346E+00	0.2345E+00
2000.00	10.00	0.50	0.1828E+00	0.1826E+00
2000.00	10.00	1.00	0.1334E+00	0.1332E+00
2000.00	10.00	5.00	0.3777E-01	0.3774E-01
2000.00	10.00	10.00	0.2022E-01	0.2021E-01
2000.00	10.00	20.00	0.1073E-01	0.1073E-01
2000.00	10.00	50.00	0.4581E-02	0.4580E-02

2000.00	10.00	75.00	0.3124E-02	0.3124E-02
2000.00	10.00	100.00	0.2375E-02	0.2375E-02

c This program calculates LTE and NLTE bulk temp. under nongray.  
c gas assumption for H<sub>2</sub>O

c IMPLICIT DOUBLE PRECISION (A-H,O-Z)

REAL L,KFB

EXTERNAL F101,F102,F103,F104,F105,F111,F112,F113,

\* F114,F115,F121,F122,F123,F124,F125,F131,F132,

\*F133,F134,F135,F141,F142,F143,F144,F145

DIMENSION U(9),PRES(4),TEMP(4)

COMMON F1,F2,F3,F4,F5

OPEN(4,file='output4')

open(5,file='nlp')

open(6,file='lp')

DATA U/0.1,0.5,1.0,5.0,10.0,20.0,50.0,75.,100.0/

DATA PRES/0.1,1.,5.,10.0/

DATA TEMP/300.,500.,1000.0,2000.0/

WRITE(4,111)

write(5,13)

write(5,\*) 11,1

13 format('3',/, 'x',/, 't',/, 't1',/,i4,x,'1')

write(6,14)

write(6,\*) 11,1

14 format('2',/, 'x',/, 't',/,/,i4,x,'1')

DO 44 IT = 1,4

TW = TEMP(IT)

DO 55 KK = 1,4

P = PRES(KK)

DO 66 I = 1,9

L= U(I)

---

C  
C CALCULATION OF PLANK'S FUNCTION IT'S DERIVATIVES

C  
C WNB BAND CENTER (1/CM)  
C HCK CONSTANT (K CM)  
C CCC C1\*C2 (ERG-K-CM\*\*3?SEC)  
C PFDBI PLANCK FUNCTION DERIVATIVE FOR I BAND

---

CESS = TW\*\*2

STU = TW\*\*0.5

SNT = TW/273.

HCK = 1.439257246

AK1 = (TW/300.)\*\*0.5

TS = 300./TW

---

C  
C SPECTROSCOPIC PROPERTIES OF H<sub>2</sub>O  
C HERE WE HAVE CONSIDERED FIVE BANDS(I.R.,6.3,2.7,1.87,1.38 MICRONS)  
C WNB1 BAND CENTER (1/CM)

---

WNB1 = 500.

WNB2 = 1600.



WNB3 = 3750.  
 WNB4 = 5350.  
 WNB5 = 7250.  
 C2B1 = HCK\*WNB1  
 C2B2 = HCK\*WNB2  
 C2B3 = HCK\*WNB3  
 C2B4 = HCK\*WNB4  
 C2B5 = HCK\*WNB5  
 CCC = 0.000053847734  
 CCB1 = CCC\*(WNB1\*\*4)  
 CCB2 = CCC\*(WNB2\*\*4)  
 CCB3 = CCC\*(WNB3\*\*4)  
 CCB4 = CCC\*(WNB4\*\*4)  
 CCB5 = CCC\*(WNB5\*\*4)  
 TB1 = C2B1/TW  
 TB2 = C2B2/TW  
 TB3 = C2B3/TW  
 TB4 = C2B4/TW  
 TB5 = C2B5/TW  
 TEB1 = EXP(TB1)  
 TEB2 = EXP(TB2)  
 TEB3 = EXP(TB3)  
 TEB4 = EXP(TB4)  
 TEB5 = EXP(TB5)  
 SNTB1 = CESS\*((TEB1-1.)\*\*2.)  
 SNTB2 = CESS\*((TEB2-1.)\*\*2.)  
 SNTB3 = CESS\*((TEB3-1.)\*\*2.)  
 SNTB4 = CESS\*((TEB4-1.)\*\*2.)  
 SNTB5 = CESS\*((TEB5-1.)\*\*2.)  
 PFDB1 = (CCB1\*TEB1)/SNTB1  
 PFDB2 = (CCB2\*TEB2)/SNTB2  
 PFDB3 = (CCB3\*TEB3)/SNTB3  
 PFDB4 = (CCB4\*TEB4)/SNTB4  
 PFDB5 = (CCB5\*TEB5)/SNTB5

---

C  
 C BAND MODEL CORRELATIONS (TIEN & LOWDER WIDE BAND MODEL)  
 C AZI AOI (1/CM)  
 C CZSI COI\*\*2 (1/(ATM-CM))  
 C BSI B\*\*2 (NON DIMENSIONAL)  
 C OMGI WAVE NUMBER (1/CM)  
 C SI INTEGRATED BAND INTENSITY (1/(ATM CM\*\*2))

---

AK1 = (TW/300.)\*\*0.5  
 AK2 = (300./TW)\*\*1.5  
 AZ1 = 49.4\*AK1  
 AZ2 = 90.1\*AK1  
 AZ3 = 112.6\*AK1  
 AZ4 = 79.7\*AK1  
 AZ5 = 79.7\*AK1

C  
C DKF THERMAL CONDUCTIVITY (ERG/CM-SEC-K)  
C

KFB = (1488.365171)\*(SNT\*\*1.23)  
AMB = H/KFB  
OMG1 = 3652.0  
OMG2 = 1595.0  
OMG3 = 3756.0  
TX = -(HCK/TW)  
TX1 = TX\*OMG1  
TX2 = TX\*OMG2  
TX3 = TX\*OMG3  
ETX1 = EXP(TX1)  
ETX2 = EXP(TX2)  
ETX3 = EXP(TX3)  
C1 = 1.0-ETX1  
C2 = 1.0-ETX2  
C3 = 1.0-ETX3  
BRKT1 = TX\*(OMG1+OMG3)  
BRKT2 = TX\*(OMG2+OMG3)  
PH101 = (1.-EXP(BRKT1))/C1\*C2\*C3  
PH011 = (1.-EXP(BRKT2))/C1\*C2\*C3  
TS11 = (TW/100.)\*\*(-0.5)  
PHI7 = EXP(-17.6\*TS11)  
CZS1 = 771.\*AK2\*PHI7  
CZS2 = 3.35\*AK2  
CZS3 = 1.52\*AK2  
CZS4 = 0.276\*AK2\*PH011  
CZS5 = 0.230\*AK2\*PH101  
S1 = AZ1\*CZS1  
S2 = AZ2\*CZS2  
S3 = AZ3\*CZS3  
S4 = AZ4\*CZS4  
S5 = AZ5\*CZS5

C  
C PL PRESSURE PATH LENGTH (ATM-CM)  
C

PL = P\*L  
UZ1 = CZS1\*PL  
UZ2 = CZS2\*PL  
UZ3 = CZS3\*PL  
UZ4 = CZS4\*PL  
UZ5 = CZS5\*PL  
BS1 = 0.073/AK1  
BS2 = 0.130/AK1  
BS3 = 0.145/AK1  
BS4 = 0.118/AK1  
BS5 = 0.201/AK1

C PEI EFFECTIVE PRESSURE FOR EACH BAND (NON DIMENSIONAL)

C

$$PE = 5.0 * P$$

C

C BETA1 LINE STRUCTURE PARAMETR

C

$$BETA1 = BS1 * PE$$

$$BETA2 = BS2 * PE$$

$$BETA3 = BS3 * PE$$

$$BETA4 = BS4 * PE$$

$$BETA5 = BS5 * PE$$

C

C CORRELATION FOR EACH BAND

C

$$F1 = 2.94 * (1.0 - \text{EXP}(-2.6 * BETA1))$$

$$F2 = 2.94 * (1.0 - \text{EXP}(-2.6 * BETA2))$$

$$F3 = 2.94 * (1.0 - \text{EXP}(-2.6 * BETA3))$$

$$F4 = 2.94 * (1.0 - \text{EXP}(-2.6 * BETA4))$$

$$F5 = 2.94 * (1.0 - \text{EXP}(-2.6 * BETA5))$$

$$H1 = AZ1 * PFDB1$$

$$H2 = AZ2 * PFDB2$$

$$H3 = AZ3 * PFDB3$$

$$H4 = AZ4 * PFDB4$$

$$H5 = AZ5 * PFDB5$$

$$H = H1 + H2 + H3 + H4 + H5$$

$$AM = H * L / KFB$$

C

C NUMERICAL INTEGRATION

C

$$EP = 1.E-3$$

$$X1 = 0.0$$

$$X21 = (3./8.) * UZ1$$

$$X22 = (3./8.) * UZ2$$

$$X23 = (3./8.) * UZ3$$

$$X24 = (3./8.) * UZ4$$

$$X25 = (3./8.) * UZ5$$

$$Y11 = 1.5 * UZ1$$

$$Y12 = 1.5 * UZ2$$

$$Y13 = 1.5 * UZ3$$

$$Y14 = 1.5 * UZ4$$

$$Y15 = 1.5 * UZ5$$

$$Y21 = 3.0 * X21$$

$$Y22 = 3.0 * X22$$

$$Y23 = 3.0 * X23$$

$$Y24 = 3.0 * X24$$

$$Y25 = 3.0 * X25$$

CALL RHBINT(F101,X1,Y11,R01,100,5,EP,KE)

CALL RHBINT(F102,X1,Y12,R02,100,5,EP,KE)

CALL RHBINT(F103,X1,Y13,R03,100,5,EP,KE)

CALL RHBINT(F104,X1,Y14,R04,100,5,EP,KE)  
CALL RHBINT(F105,X1,Y15,R05,100,5,EP,KE)  
CALL RHBINT(F111,X1,Y11,R11,100,5,EP,KE)  
CALL RHBINT(F112,X1,Y12,R12,100,5,EP,KE)  
CALL RHBINT(F113,X1,Y13,R13,100,5,EP,KE)  
CALL RHBINT(F114,X1,Y14,R14,100,5,EP,KE)  
CALL RHBINT(F115,X1,Y15,R15,100,5,EP,KE)  
CALL RHBINT(F121,X1,Y11,R21,100,5,EP,KE)  
CALL RHBINT(F122,X1,Y12,R22,100,5,EP,KE)  
CALL RHBINT(F123,X1,Y13,R23,100,5,EP,KE)  
CALL RHBINT(F124,X1,Y14,R24,100,5,EP,KE)  
CALL RHBINT(F125,X1,Y15,R25,100,5,EP,KE)  
CALL RHBINT(F131,X1,Y11,R31,100,5,EP,KE)  
CALL RHBINT(F132,X1,Y12,R32,100,5,EP,KE)  
CALL RHBINT(F133,X1,Y13,R33,100,5,EP,KE)  
CALL RHBINT(F134,X1,Y14,R34,100,5,EP,KE)  
CALL RHBINT(F135,X1,Y15,R35,100,5,EP,KE)  
CALL RHBINT(F141,X1,Y11,R41,100,5,EP,KE)  
CALL RHBINT(F142,X1,Y12,R42,100,5,EP,KE)  
CALL RHBINT(F143,X1,Y13,R43,100,5,EP,KE)  
CALL RHBINT(F144,X1,Y14,R44,100,5,EP,KE)  
CALL RHBINT(F145,X1,Y15,R45,100,5,EP,KE)  
CALL RHBINT(F101,X21,Y21,S11,100,5,EP,KE)  
CALL RHBINT(F102,X22,Y22,S12,100,5,EP,KE)  
CALL RHBINT(F103,X23,Y23,S13,100,5,EP,KE)  
CALL RHBINT(F104,X24,Y24,S14,100,5,EP,KE)  
CALL RHBINT(F105,X25,Y25,S15,100,5,EP,KE)  
CALL RHBINT(F111,X1,X21,S21,100,5,EP,KE)  
CALL RHBINT(F112,X1,X22,S22,100,5,EP,KE)  
CALL RHBINT(F113,X1,X23,S23,100,5,EP,KE)  
CALL RHBINT(F114,X1,X24,S24,100,5,EP,KE)  
CALL RHBINT(F115,X1,X25,S25,100,5,EP,KE)  
CALL RHBINT(F111,X1,Y21,S31,100,5,EP,KE)  
CALL RHBINT(F112,X1,Y22,S32,100,5,EP,KE)  
CALL RHBINT(F113,X1,Y23,S33,100,5,EP,KE)  
CALL RHBINT(F114,X1,Y24,S34,100,5,EP,KE)  
CALL RHBINT(F115,X1,Y25,S35,100,5,EP,KE)  
CALL RHBINT(F121,X21,Y21,S41,100,5,EP,KE)  
CALL RHBINT(F122,X22,Y22,S42,100,5,EP,KE)  
CALL RHBINT(F123,X23,Y23,S43,100,5,EP,KE)  
CALL RHBINT(F124,X24,Y24,S44,100,5,EP,KE)  
CALL RHBINT(F125,X25,Y25,S45,100,5,EP,KE)  
CALL RHBINT(F131,X1,X21,S51,100,5,EP,KE)  
CALL RHBINT(F132,X1,X22,S52,100,5,EP,KE)  
CALL RHBINT(F133,X1,X23,S53,100,5,EP,KE)  
CALL RHBINT(F134,X1,X24,S54,100,5,EP,KE)  
CALL RHBINT(F135,X1,X25,S55,100,5,EP,KE)  
CALL RHBINT(F131,X1,Y21,S61,100,5,EP,KE)  
CALL RHBINT(F132,X1,Y22,S62,100,5,EP,KE)

CALL RHBINT(F133,X1,Y23,S63,100,5,EP,KE)  
 CALL RHBINT(F134,X1,Y24,S64,100,5,EP,KE)  
 CALL RHBINT(F135,X1,Y25,S65,100,5,EP,KE)  
 CALL RHBINT(F141,X21,Y21,S71,100,5,EP,KE)  
 CALL RHBINT(F142,X22,Y22,S72,100,5,EP,KE)  
 CALL RHBINT(F143,X23,Y23,S73,100,5,EP,KE)  
 CALL RHBINT(F144,X24,Y24,S74,100,5,EP,KE)  
 CALL RHBINT(F145,X25,Y25,S75,100,5,EP,KE)  
 CU1 = 2./(3.\*UZ1)  
 CU2 = 2./(3.\*UZ2)  
 CU3 = 2./(3.\*UZ3)  
 CU4 = 2./(3.\*UZ4)  
 CU5 = 2./(3.\*UZ5)  
 BR1A1 = (CU1\*R11)-2.\*(CU1\*\*3.)\*R31+(CU1\*\*4.)\*R41  
 BR1A2 = (CU2\*R12)-2.\*(CU2\*\*3.)\*R32+(CU2\*\*4.)\*R42  
 BR1A3 = (CU3\*R13)-2.\*(CU3\*\*3.)\*R33+(CU3\*\*4.)\*R43  
 BR1A4 = (CU4\*R14)-2.\*(CU4\*\*3.)\*R34+(CU4\*\*4.)\*R44  
 BR1A5 = (CU5\*R15)-2.\*(CU5\*\*3.)\*R35+(CU5\*\*4.)\*R45  
 BR1B1=((CU1\*\*2.)\*R21)-(CU1\*R11)  
 BR1B2=((CU2\*\*2.)\*R22)-(CU2\*R12)  
 BR1B3=((CU3\*\*2.)\*R23)-(CU3\*R13)  
 BR1B4=((CU4\*\*2.)\*R24)-(CU4\*R14)  
 BR1B5=((CU5\*\*2.)\*R25)-(CU5\*R15)  
 ETC1=((36.5\*(TW\*\*(-1/3.)))+3.9)  
 ETC2=EXP(ETC1)\*(1.E-6)  
 ETAC=ETC2/P  
 ETR11=8.\*3.14\*(500.\*\*(2.))\*4.08\*(1.E-12)\*s1\*tw  
 ETAR1=1./ETR11  
 ETR12=8.\*3.14\*(1600.\*\*(2.))\*4.08\*(1.E-12)\*s2\*tw  
 ETAR2=1./ETR12  
 ETR13=8.\*3.14\*(3750.\*\*(2.))\*4.08\*(1.E-12)\*s3\*tw  
 ETAR3=1./ETR13  
 ETR14=8.\*3.14\*(5350.\*\*(2.))\*4.08\*(1.E-12)\*s4\*tw  
 ETAR4=1./ETR14  
 ETR15=8.\*3.14\*(7250.\*\*(2.))\*4.08\*(1.E-12)\*s5\*tw  
 ETAR5=1./ETR15  
 ETA11=ETAC/ETAR1  
 ETA12=ETAC/ETAR2  
 ETA13=ETAC/ETAR3  
 ETA14=ETAC/ETAR4  
 ETA15=ETAC/ETAR5  
 SUMA1 = H1\*BR1A1  
 SUMA2 = H2\*BR1A2  
 SUMA3 = H3\*BR1A3  
 SUMA4 = H4\*BR1A4  
 SUMA5 = H5\*BR1A5  
 AL1L = 1.+(L/KFB)\*(SUMA1+SUMA2+SUMA3+SUMA4+SUMA5)  
 SUMAN1=ETA11\*CU1\*BR1B1  
 SUMAN2=ETA12\*CU2\*BR1B2

SUMAN3=ETA13\*CU3\*BR1B3  
 SUMAN4=ETA14\*CU4\*BR1B4  
 SUMAN5=ETA15\*CU5\*BR1B5  
 SUMAN=(9./2.)\*(SUMAN1+SUMAN2+SUMAN3+SUMAN4+SUMAN5)  
 ALPH1=AL1L~SUMAN  
 BR2A1 = (CU1\*\*2.)\*R21-2.\*(CU1\*\*3.)\*R31+(CU1\*\*4.)\*R41  
 BR2A2 = (CU2\*\*2.)\*R22-2.\*(CU2\*\*3.)\*R32+(CU2\*\*4.)\*R42  
 BR2A3 = (CU3\*\*2.)\*R23-2.\*(CU3\*\*3.)\*R33+(CU3\*\*4.)\*R43  
 BR2A4 = (CU4\*\*2.)\*R24-2.\*(CU4\*\*3.)\*R34+(CU4\*\*4.)\*R44  
 BR2A5 = (CU5\*\*2.)\*R25-2.\*(CU5\*\*3.)\*R35+(CU5\*\*4.)\*R45  
 BR2B1=R01-(6.\*CU1\*R11)+(6.\*(CU1\*\*2.)\*R21)  
 BR2B2=R02-(6.\*CU2\*R12)+(6.\*(CU2\*\*2.)\*R22)  
 BR2B3=R03-(6.\*CU3\*R13)+(6.\*(CU3\*\*2.)\*R23)  
 BR2B3=R04-(6.\*CU4\*R14)+(6.\*(CU4\*\*2.)\*R24)  
 BR2B3=R03-(6.\*CU5\*R15)+(6.\*(CU5\*\*2.)\*R25)  
 SUMB1 = H1\*BR2A1  
 SUMB2 = H2\*BR2A2  
 SUMB3 = H3\*BR2A3  
 SUMB4 = H4\*BR2A4  
 SUMB5 = H5\*BR2A5  
 SUMBL=SUMB1+SUMB2+SUMB3+SUMB4+SUMB5  
 SUMBN1=ETA11\*CU1\*BR2B1  
 SUMBN2=ETA12\*CU2\*BR2B2  
 SUMBN3=ETA13\*CU3\*BR2B3  
 SUMBN4=ETA14\*CU4\*BR2B4  
 SUMBN5=ETA15\*CU5\*BR2B5  
 SUMBN=(3./4.)\*(SUMBN1+SUMBN2+SUMBN3+SUMBN4+SUMBN5)  
 AL2L = (L/KFB)\*SUMBL  
 ALPH2=AL2L~SUMBN  
 ALPH01=ETA11\*(CU1\*\*2.)\*(CU1\*R21-R11)  
 ALPH02=ETA12\*(CU2\*\*2.)\*(CU2\*R22-R12)  
 ALPH03=ETA13\*(CU3\*\*2.)\*(CU3\*R23-R13)  
 ALPH04=ETA14\*(CU4\*\*2.)\*(CU4\*R24-R14)  
 ALPH05=ETA15\*(CU5\*\*2.)\*(CU5\*R25-R15)  
 ALPH0=(9./2.)\*(ALPH01+ALPH02+ALPH03+ALPH04+ALPH05)-1.  
 BR3A1 = (57./256.)\*S11+(11./16.)\*CU1\*(S21+S31)  
 \*-(9./8.)\*(CU1\*\*2.)\*S41-(CU1\*\*3.)\*(S51+S61)+(CU1\*\*4.)\*S71  
 BR3A2 = (57./256.)\*S12+(11./16.)\*CU2\*(S22+S32)  
 \*-(9./8.)\*(CU2\*\*2.)\*S42-(CU2\*\*3.)\*(S52+S62)+(CU2\*\*4.)\*S72  
 BR3A3 = (57./256.)\*S13+(11./16.)\*CU3\*(S23+S33)  
 \*-(9./8.)\*(CU3\*\*2.)\*S43-(CU3\*\*3.)\*(S53+S63)+(CU3\*\*4.)\*S73  
 BR3A4 = (57./256.)\*S14+(11./16.)\*CU4\*(S24+S34)  
 \*-(9./8.)\*(CU4\*\*2.)\*S44-(CU4\*\*3.)\*(S54+S64)+(CU4\*\*4.)\*S74  
 BR3A5 = (57./256.)\*S15+(11./16.)\*CU5\*(S25+S35)  
 \*-(9./8.)\*(CU5\*\*2.)\*S45-(CU5\*\*3.)\*(S55+S65)+(CU5\*\*4.)\*S75  
 BR3B1=((9./4.)\*CU1\*S11)+(6.\*(CU1\*\*2.)\*(S21+S31))  
 \*-(12\*(CU1\*\*3.)\*S41)  
 BR3B2=((9./4.)\*CU2\*S12)+(6.\*(CU2\*\*2.)\*(S22+S32))  
 \*-(12\*(CU2\*\*3.)\*S42)

$$\begin{aligned}
&BR3B3 = ((9./4.) * CU3 * S13) + (6. * (CU3 ** 2.) * (S23 + S33)) \\
&\quad * -(12. * (CU3 ** 3.) * S43) \\
&BR3B4 = ((9./4.) * CU4 * S14) + (6. * (CU4 ** 2.) * (S24 + S34)) \\
&\quad * -(12. * (CU4 ** 3.) * S44) \\
&BR3B5 = ((9./4.) * CU5 * S15) + (6. * (CU5 ** 2.) * (S25 + S35)) \\
&\quad * -(12. * (CU5 ** 3.) * S45) \\
&SUMC1 = H1 * BR3A1 \\
&SUMC2 = H2 * BR3A2 \\
&SUMC3 = H3 * BR3A3 \\
&SUMC4 = H4 * BR3A4 \\
&SUMC5 = H5 * BR3A5 \\
&SUMCL = SUMC1 + SUMC2 + SUMC3 + SUMC4 + SUMC5 \\
&SUMCN1 = ETA11 * BR3B1 \\
&SUMCN2 = ETA12 * BR3B2 \\
&SUMCN3 = ETA13 * BR3B3 \\
&SUMCN4 = ETA14 * BR3B4 \\
&SUMCN5 = ETA15 * BR3B5 \\
&SUMCN = (3./8.) * (SUMCN1 + SUMCN2 + SUMCN3 + SUMCN4 + SUMCN5) \\
&AL3L = (11./16.) + (L/KFB) * SUMCL \\
&ALPH3 = AL3L + SUMCN \\
&BR4A1 = (9.0/256.) * S11 + (3.0/16.) * CU1 * (S21 + S31) \\
&\quad * -(1./8.) * (CU1 ** 2.) * S41 - (CU1 ** 3.) * (S51 + S61) + (CU1 ** 4.) * S71 \\
&BR4A2 = (9.0/256.) * S12 + (3.0/16.) * CU2 * (S22 + S32) \\
&\quad * -(1./8.) * (CU2 ** 2.) * S42 - (CU2 ** 3.) * (S52 + S62) + (CU2 ** 4.) * S72 \\
&BR4A3 = (9.0/256.) * S13 + (3.0/16.) * CU3 * (S23 + S33) \\
&\quad * -(1./8.) * (CU3 ** 2.) * S43 - (CU3 ** 3.) * (S53 + S63) + (CU3 ** 4.) * S73 \\
&BR4A4 = (9.0/256.) * S14 + (3.0/16.) * CU4 * (S24 + S34) \\
&\quad * -(1./8.) * (CU4 ** 2.) * S44 - (CU4 ** 3.) * (S54 + S64) + (CU4 ** 4.) * S74 \\
&BR4A5 = (9.0/256.) * S15 + (3.0/16.) * CU5 * (S25 + S35) \\
&\quad * -(1./8.) * (CU5 ** 2.) * S45 - (CU5 ** 3.) * (S55 + S65) + (CU5 ** 4.) * S75 \\
&BR4B1 = ((1./4.) * CU1 * S11) + (6. * (CU1 ** 2.) * (S21 + S31)) - \\
&\quad * (12. * (CU1 ** 3.) * S41) \\
&BR4B2 = ((1./4.) * CU2 * S12) + (6. * (CU2 ** 2.) * (S22 + S32)) - \\
&\quad * (12. * (CU2 ** 3.) * S42) \\
&BR4B3 = ((1./4.) * CU3 * S13) + (6. * (CU3 ** 2.) * (S23 + S33)) - \\
&\quad * (12. * (CU3 ** 3.) * S43) \\
&BR4B4 = ((1./4.) * CU4 * S14) + (6. * (CU4 ** 2.) * (S24 + S34)) - \\
&\quad * (12. * (CU4 ** 3.) * S44) \\
&BR4B5 = ((1./4.) * CU5 * S15) + (6. * (CU5 ** 2.) * (S25 + S35)) - \\
&\quad * (12. * (CU5 ** 3.) * S45) \\
&SUMD1 = H1 * BR4A1 \\
&SUMD2 = H2 * BR4A2 \\
&SUMD3 = H3 * BR4A3 \\
&SUMD4 = H4 * BR4A4 \\
&SUMD5 = H5 * BR4A5 \\
&SUMDL = SUMD1 + SUMD2 + SUMD3 + SUMD4 + SUMD5 \\
&SUMDN1 = ETA11 * BR4B1 \\
&SUMDN2 = ETA12 * BR4B2 \\
&SUMDN3 = ETA13 * BR4B3
\end{aligned}$$

```

SUMDN4=ETA14*BR4B4
SUMDN5=ETA15*BR4B5
SUMDN=(3./8.)*(SUMDN1+SUMDN2+SUMDN3+SUMDN4+SUMDN5)
AL4L = (3.0/16.)+(L/KFB)*SUMDL
ALPH4=AL4L+SUMDN
BR5B1=(3./16.)*(CU1*S11)+(1./2.)*(CU1**2.)*(S21+S31)-(CU1**3.)*S41
BR5B2=(3./16.)*(CU2*S12)+(1./2.)*(CU2**2.)*(S22+S32)-(CU2**3.)*S42
BR5B3=(3./16.)*(CU3*S13)+(1./2.)*(CU3**2.)*(S23+S33)-(CU3**3.)*S43
BR5B4=(3./16.)*(CU4*S14)+(1./2.)*(CU4**2.)*(S24+S34)-(CU4**3.)*S44
BR5B5=(3./16.)*(CU5*S15)+(1./2.)*(CU5**2.)*(S25+S35)-(CU5**3.)*S45
SUMEN1=ETA11*BR5B1
SUMEN2=ETA12*BR5B2
SUMEN3=ETA13*BR5B3
SUMEN4=ETA14*BR5B4
SUMEN5=ETA15*BR5B5
SUMEN=SUMEN1+SUMEN2+SUMEN3+SUMEN4+SUMEN5
ALPH5=-((9./2.)*SUMEN+(11./16.))
DENA = (ALPH1*ALPH4)-(ALPH2*ALPH3)
A1=((ALPH0*ALPH4)-(ALPH2*ALPH5))/DENA
A2=((ALPH1*ALPH5)-(ALPH0*ALPH3))/DENA
TBULK = (1./70.)*((17.*A1)+(3.*A2))
CONST=1./(16.*(AL1L*AL4L-AL2L*AL3L))
a1l=(11.*a12l-16.*a14l)*CONST
A2L=(16.*AL3L-11.*AL1L)*CONST
TBULKL=(1/70.)*(17.*A1L+3.*A2L)
WRITE(4,200) TW,P,L,-TBULK,-TBULKL
write(5,202)l,-tbulkl,-tbulk
write(6,201)l,-tbulk
66 CONTINUE
55 CONTINUE
44 CONTINUE
200 FORMAT(1X,F7.2, 3X,F6.2, 3X,F6.2, 2(3X,E10.4))
111 FORMAT(4X,'TW',8X,'P',6X,'L',9X,'TBULK',7X,'TBULKL')
201 format (1x,f9.2,3x,e10.4)
202 format (1x,f9.2,2(3x,e10.4))
STOP
END

```

C

```

subroutine rhbint(fct,a,b,romb,nsd,ko,ep,ke)
dimension t(20)
ke=0.
xnsd=nsd
dlx=(b-a)/xnsd
romb=0.
xul=a
templ=fct(xul)
do 4 i=1,nsd
xll=xul
xul=xul+dlx

```



```

tempu=fct(xul)
t(1)=(templ+tempu)/2
n=1
xn=1.
do 3 nh=1,ko
n2m=2*n-1
u=0.
cm=dlx/(2.*xn)
txn=-1.
do 1 j=1,n2m,2
txn=txn+2.
u=u+fct(xl1+txn*cm)
1 continue
7 nh1=nh+1
t(nh1)=(u/xn+t(nh))/2.
9 ef=1.
do 2 j=1,nh
8 ef=4.*ef
jm=nh1-j
12 temp=t(jm+1)+(t(jm+1)-t(jm))/(ef-1.)
if (abs ((t(jm)-t(jm+1))/amax1(t(jm),t(jm+1)))-ep)10,10,2
2 t(jm)=temp
xn=xn+xn
n=n+n
3 continue
ke=ke+1
go to 11
10 t(1)=temp
11 romb=romb+t(1)
templ=tempu
4 continue
5 romb=romb*dlx
6 return
end

```

---

```

FUNCTION F101(U1)
COMMON F1,F2,F3,F4,F5
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F101 = AUD1
RETURN
END
FUNCTION F102(U2)
COMMON F1,F2,F3,F4,F5
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = F2*((U2**2.)+(4.*U2*F2)+(4.*F2))/DEN2
F102 = AUD2
RETURN
END

```

```

FUNCTION F103(U3)
COMMON F1,F2,F3,F4,F5
DEN3 =(F3*((U3**2.)+(2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 =(F3*((U3**2.)+(4.*U3*F3)+(4.*F3)))/DEN3
F103 = AUD3
RETURN
END
FUNCTION F104(U4)
COMMON F1,F2,F3,F4,F5
DEN4 =(F4*((U4**2.)+(2.*U4)+2.)+U4)*(U4+(2.*F4))
AUD4 =(F4*((U4**2.)+(4.*U4*F4)+(4.*F4)))/DEN4
F104 =AUD4
RETURN
END
FUNCTION F105(U5)
COMMON F1,F2,F3,F4,F5
DEN5 =(F5*((U5**2.)+(2.*U5)+2.)+U5)*(U5+(2.*F5))
AUD5 =(F5*((U5**2.)+(4.*U5*F5)+(4.*F5)))/DEN5
F105 = AUD5
RETURN
END
FUNCTION F111(U1)
COMMON F1,F2,F3,F4,F5
DEN1 =(F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 =(F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F111 = AUD1*U1
RETURN
END
FUNCTION F112(U2)
COMMON F1,F2,F3,F4,F5
DEN2 =(F2*((U2*U2)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 =(F2*((U2*U2)+(4.*U2*F2)+(4.*F2)))/DEN2
F112 = AUD2*U2
RETURN
END
FUNCTION F113(U3)
COMMON F1,F2,F3,F4,F5
DEN3 =(F3*((U3**2.)+(2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 =(F3*((U3**2.)+(4.*U3*F3)+(4.*F3)))/DEN3
F113 = AUD3*U3
RETURN
END
FUNCTION F114(U4)
COMMON F1,F2,F3,F4,F5
DEN4 =(F4*((U4**2.)+(2.*U4)+2.)+U4)*(U4+(2.*F4))
AUD4 =(F4*((U4**2.)+(4.*U4*F4)+(4.*F4)))/DEN4
F114 = AUD4*U4
RETURN
END

```

```

FUNCTION F115(U5)
COMMON F1,F2,F3,F4,F5
DEN5 = (F5*((U5**2.)+(2.*U5)+2.)+U5)*(U5+(2.*F5))
AUD5 = (F5*((U5**2.)+(4.*U5*F5)+(4.*F5)))/DEN5
F115 = AUD*U5
RETURN
END
FUNCTION F121(U1)
COMMON F1,F2,F3,F4,F5
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F121 = AUD1*U1*U1
RETURN
END
FUNCTION F122(U2)
COMMON F1,F2,F3,F4,F5
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2.)+(4.*U2*F2)+(4.*F2)))/DEN2
F122 = AUD2*U2*U2
RETURN
END
FUNCTION F123(U3)
COMMON F1,F2,F3,F4,F5
DEN3 = (F3*((U3**2.)+(2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 = (F3*((U3**2.)+(4.*U3*F3)+(4.*F3)))/DEN3
F123 = AUD3*U3*U3
RETURN
END
FUNCTION F124(U4)
COMMON F1,F2,F3,F4,F5
DEN4 = (F4*((U4**2.)+(2.*U4)+2.)+U4)*(U4+(2.*F4))
AUD4 = (F4*((U4**2.)+(4.*U4*F4)+(4.*F4)))/DEN4
F124 = AUD4*U4*U4
RETURN
END
FUNCTION F125(U5)
COMMON F1,F2,F3,F4,F5
DEN5 = (F5*((U5**2.)+(2.*U5)+2.)+U5)*(U5+(2.*F5))
AUD5 = (F5*((U5**2.)+(4.*U5*F5)+(4.*F5)))/DEN5
F125 = AUD5*U5*U5
RETURN
END
FUNCTION F131(U1)
COMMON F1,F2,F3,F4,F5
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F131 = AUD1*U1**3.
RETURN
END

```

```

FUNCTION F132(U2)
COMMON F1,F2,F3,F4,F5
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2.)+(4.*U2*F2)+(4.*F2)))/DEN2
F132 = AUD2*U2**3.
RETURN
END
FUNCTION F133(U3)
COMMON F1,F2,F3,F4,F5
DEN3 = (F3*((U3**2.)+(2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 = (F3*((U3**2.)+(4.*U3*F3)+(4.*F3)))/DEN3
F133 = AUD3*U3**3.
RETURN
END
FUNCTION F134(U4)
COMMON F1,F2,F3,F4,F5
DEN4 = (F4*((U4**2.)+(2.*U4)+2.)+U4)*(U4+(2.*F4))
AUD4 = (F4*((U4**2.)+(4.*U4*F4)+(4.*F4)))/DEN4
F134 = AUD4*U4**3
RETURN
END
FUNCTION F135(U5)
COMMON F1,F2,F3,F4,F5
DEN5 = (F5*((U5**2.)+(2.*U5)+2.)+U5)*(U5+(2.*F5))
AUD5 = (F5*((U5**2.)+(4.*U5*F5)+(4.*F5)))/DEN5
F135 = AUD5*U5**3
RETURN
END
FUNCTION F141(U1)
COMMON F1,F2,F3,F4,F5
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F141 = AUD1*U1**4.
RETURN
END
FUNCTION F142(U2)
COMMON F1,F2,F3,F4,F5
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2.)+(4.*U2*F2)+(4.*F2)))/DEN2
F142 = AUD2*U2*U2*U2*U2
RETURN
END
FUNCTION F143(U3)
COMMON F1,F2,F3,F4,F5
DEN3 = (F3*((U3**2.)+(2.*U3)+2.)+U3)*(U3+(2.*F3))
AUD3 = (F3*((U3**2.)+(4.*U3*F3)+(4.*F3)))/DEN3
F143 = AUD3*U3**4.
RETURN
END

```

```

FUNCTION F144(U4)
COMMON F1,F2,F3,F4,F5
DEN4 = (F4*((U4**2.)+(2.*U4)+2.)+U4)*(U4+(2.*F4))
AUD4 = (F4*((U4**2.)+(4.*U4*F4)+(4.*F4)))/DEN4
F144 = AUD4*U4**4.
RETURN
END
FUNCTION F145(U5)
COMMON F1,F2,F3,F4,F5
DEN5 = (F5*((U5**2.)+(2.*U5)+2.)+U5)*(U5+(2.*F5))
AUD5 = (F5*((U5**2.)+(4.*U5*F5)+(4.*F5)))/DEN5
F145 = AUD5*U5**4.
RETURN
END

```

## NONGRAY RESULTS FOR H<sub>2</sub>O

TW	P	L	TBULK (NLTE)	TBULK (LTE)
300.00	0.10	0.10	0.2429E+00	0.2428E+00
300.00	0.10	0.50	0.2428E+00	0.2423E+00
300.00	0.10	1.00	0.2427E+00	0.2411E+00
300.00	0.10	5.00	0.2393E+00	0.2215E+00
300.00	0.10	10.00	0.2309E+00	0.1916E+00
300.00	0.10	20.00	0.2062E+00	0.1414E+00
300.00	0.10	50.00	0.1263E+00	0.7024E-01
300.00	0.10	75.00	0.8345E-01	0.4758E-01
300.00	0.10	100.00	0.5821E-01	0.3550E-01
300.00	1.00	0.10	0.2427E+00	0.2426E+00
300.00	1.00	0.50	0.2404E+00	0.2389E+00
300.00	1.00	1.00	0.2352E+00	0.2315E+00
300.00	1.00	5.00	0.1819E+00	0.1749E+00
300.00	1.00	10.00	0.1352E+00	0.1312E+00
300.00	1.00	20.00	0.8646E-01	0.8498E-01
300.00	1.00	50.00	0.3852E-01	0.3821E-01
300.00	1.00	75.00	0.2545E-01	0.2530E-01
300.00	1.00	100.00	0.1876E-01	0.1866E-01
300.00	5.00	0.10	0.2421E+00	0.2420E+00
300.00	5.00	0.50	0.2348E+00	0.2345E+00
300.00	5.00	1.00	0.2247E+00	0.2245E+00
300.00	5.00	5.00	0.1611E+00	0.1610E+00
300.00	5.00	10.00	0.1130E+00	0.1129E+00
300.00	5.00	20.00	0.6707E-01	0.6703E-01
300.00	5.00	50.00	0.2890E-01	0.2889E-01
300.00	5.00	75.00	0.1953E-01	0.1953E-01
300.00	5.00	100.00	0.1476E-01	0.1476E-01
300.00	10.00	0.10	0.2417E+00	0.2416E+00
300.00	10.00	0.50	0.2334E+00	0.2333E+00
300.00	10.00	1.00	0.2229E+00	0.2229E+00
300.00	10.00	5.00	0.1537E+00	0.1537E+00
300.00	10.00	10.00	0.1043E+00	0.1043E+00
300.00	10.00	20.00	0.6151E-01	0.6150E-01
300.00	10.00	50.00	0.2745E-01	0.2745E-01
300.00	10.00	75.00	0.1889E-01	0.1889E-01
300.00	10.00	100.00	0.1445E-01	0.1445E-01
500.00	0.10	0.10	0.2428E+00	0.2428E+00
500.00	0.10	0.50	0.2426E+00	0.2414E+00
500.00	0.10	1.00	0.2417E+00	0.2377E+00
500.00	0.10	5.00	0.2226E+00	0.1833E+00
500.00	0.10	10.00	0.1855E+00	0.1257E+00
500.00	0.10	20.00	0.1187E+00	0.6809E-01
500.00	0.10	50.00	0.3785E-01	0.2349E-01
500.00	0.10	75.00	0.2009E-01	0.1415E-01

500.00	0.10	100.00	0.1280E-01	0.9859E-02
500.00	1.00	0.10	0.2424E+00	0.2422E+00
500.00	1.00	0.50	0.2332E+00	0.2304E+00
500.00	1.00	1.00	0.2125E+00	0.2059E+00
500.00	1.00	5.00	0.8986E-01	0.8524E-01
500.00	1.00	10.00	0.4797E-01	0.4674E-01
500.00	1.00	20.00	0.2471E-01	0.2446E-01
500.00	1.00	50.00	0.1012E-01	0.1006E-01
500.00	1.00	75.00	0.6790E-02	0.6752E-02
500.00	1.00	100.00	0.5109E-02	0.5083E-02
500.00	5.00	0.10	0.2403E+00	0.2402E+00
500.00	5.00	0.50	0.2104E+00	0.2097E+00
500.00	5.00	1.00	0.1735E+00	0.1729E+00
500.00	5.00	5.00	0.6908E-01	0.6907E-01
500.00	5.00	10.00	0.3999E-01	0.3997E-01
500.00	5.00	20.00	0.2200E-01	0.2199E-01
500.00	5.00	50.00	0.9510E-02	0.9506E-02
500.00	5.00	75.00	0.6484E-02	0.6481E-02
500.00	5.00	100.00	0.4925E-02	0.4923E-02
500.00	10.00	0.10	0.2384E+00	0.2384E+00
500.00	10.00	0.50	0.2020E+00	0.2019E+00
500.00	10.00	1.00	0.1653E+00	0.1652E+00
500.00	10.00	5.00	0.6768E-01	0.6768E-01
500.00	10.00	10.00	0.3973E-01	0.3972E-01
500.00	10.00	20.00	0.2207E-01	0.2206E-01
500.00	10.00	50.00	0.9587E-02	0.9585E-02
500.00	10.00	75.00	0.6537E-02	0.6536E-02
500.00	10.00	100.00	0.4964E-02	0.4963E-02
1000.00	0.10	0.10	0.2428E+00	0.2428E+00
1000.00	0.10	0.50	0.2422E+00	0.2412E+00
1000.00	0.10	1.00	0.2403E+00	0.2368E+00
1000.00	0.10	5.00	0.1975E+00	0.1635E+00
1000.00	0.10	10.00	0.1341E+00	0.9611E-01
1000.00	0.10	20.00	0.6480E-01	0.4469E-01
1000.00	0.10	50.00	0.1700E-01	0.1350E-01
1000.00	0.10	75.00	0.8955E-02	0.7653E-02
1000.00	0.10	100.00	0.5706E-02	0.5078E-02
1000.00	1.00	0.10	0.2423E+00	0.2422E+00
1000.00	1.00	0.50	0.2294E+00	0.2279E+00
1000.00	1.00	1.00	0.1989E+00	0.1950E+00
1000.00	1.00	5.00	0.5104E-01	0.4876E-01
1000.00	1.00	10.00	0.2090E-01	0.2032E-01
1000.00	1.00	20.00	0.8783E-02	0.8667E-02
1000.00	1.00	50.00	0.3025E-02	0.3012E-02
1000.00	1.00	75.00	0.1934E-02	0.1929E-02
1000.00	1.00	100.00	0.1418E-02	0.1415E-02
1000.00	5.00	0.10	0.2397E+00	0.2396E+00
1000.00	5.00	0.50	0.1911E+00	0.1904E+00
1000.00	5.00	1.00	0.1295E+00	0.1288E+00

1000.00	5.00	5.00	0.2636E-01	0.2632E-01
1000.00	5.00	10.00	0.1272E-01	0.1272E-01
1000.00	5.00	20.00	0.6249E-02	0.6246E-02
1000.00	5.00	50.00	0.2492E-02	0.2491E-02
1000.00	5.00	75.00	0.1668E-02	0.1667E-02
1000.00	5.00	100.00	0.1255E-02	0.1255E-02
1000.00	10.00	0.10	0.2369E+00	0.2368E+00
1000.00	10.00	0.50	0.1684E+00	0.1681E+00
1000.00	10.00	1.00	0.1070E+00	0.1068E+00
1000.00	10.00	5.00	0.2373E-01	0.2373E-01
1000.00	10.00	10.00	0.1202E-01	0.1202E-01
1000.00	10.00	20.00	0.6095E-02	0.6094E-02
1000.00	10.00	50.00	0.2488E-02	0.2488E-02
1000.00	10.00	75.00	0.1674E-02	0.1674E-02
1000.00	10.00	100.00	0.1263E-02	0.1263E-02
2000.00	0.10	0.10	0.2428E+00	0.2428E+00
2000.00	0.10	0.50	0.2423E+00	0.2419E+00
2000.00	0.10	1.00	0.2407E+00	0.2393E+00
2000.00	0.10	5.00	0.2015E+00	0.1845E+00
2000.00	0.10	10.00	0.1385E+00	0.1160E+00
2000.00	0.10	20.00	0.6686E-01	0.5490E-01
2000.00	0.10	50.00	0.1909E-01	-.1867E-01
2000.00	0.10	75.00	0.7382E-02	0.5546E-02
2000.00	0.10	100.00	0.5626E-02	0.4192E-02
2000.00	1.00	0.10	0.2425E+00	0.2425E+00
2000.00	1.00	0.50	0.2345E+00	0.2340E+00
2000.00	1.00	1.00	0.2133E+00	0.2118E+00
2000.00	1.00	5.00	0.6285E-01	0.6126E-01
2000.00	1.00	10.00	0.2424E-01	0.2444E-01
2000.00	1.00	20.00	-.9451E-03	0.7439E-03
2000.00	1.00	50.00	0.1477E-02	0.1416E-02
2000.00	1.00	75.00	0.8948E-03	0.8675E-03
2000.00	1.00	100.00	0.6293E-03	0.6142E-03
2000.00	5.00	0.10	0.2410E+00	0.2410E+00
2000.00	5.00	0.50	0.2064E+00	0.2061E+00
2000.00	5.00	1.00	0.1473E+00	0.1469E+00
2000.00	5.00	5.00	0.2678E-01	0.2708E-01
2000.00	5.00	10.00	0.3265E-02	0.3264E-02
2000.00	5.00	20.00	0.2381E-02	0.2365E-02
2000.00	5.00	50.00	0.8647E-03	0.8621E-03
2000.00	5.00	75.00	0.5466E-03	0.5455E-03
2000.00	5.00	100.00	0.3947E-03	0.3941E-03
2000.00	10.00	0.10	0.2392E+00	0.2392E+00
2000.00	10.00	0.50	0.1830E+00	0.1828E+00
2000.00	10.00	1.00	0.1143E+00	0.1141E+00
2000.00	10.00	5.00	-.4760E+00	-.2229E+00
2000.00	10.00	10.00	0.4333E-02	0.4318E-02
2000.00	10.00	20.00	0.2160E-02	0.2157E-02
2000.00	10.00	50.00	0.7773E-03	0.7767E-03



2000.00	10.00	75.00	0.4927E-03	0.4924E-03
2000.00	10.00	100.00	0.3569E-03	0.3567E-03

```

c Computer Code to calculate Radiative Heat Interaction between two
c Parallel Plates(Flow is assumed to be fully developed)
c CH4 is the participating gas and two bands of CH4 are considered
c This program is written on the basis of NonGray Gas approximation and can
c calculate both LTE and NLTE bulk temp.
c This program is written by Manoj K. Jha in September 1991
*****

```

```

c
c  implicit double precision (a-h,o-z)
real l,kfb
EXTERNAL F101,F102,F111,F112,F121,F122,F131,F132,
*F141,F142
dimension u(9),pres(4),Temp(4),eps(3)
data u/0.1,0.5,1.0,5.0,10.0,20.0,50.0,75.,100.0/
DATA PRES/0.1,1.,5.,10.0/
DATA TEMP/300.,500.,1000.0,2000.0/
COMMON F1,F2
OPEN(6,file='output5')
open(7,file='nlp')
open(8,file='lp')
WRITE(6,111)
write(7,13)
write(7,*) 11,1
13 format('3',/, 'x',/, 't',/, 't1',/,i4,x,'1')
write(8,14)
write(8,*) 11,1
14 format('2',/, 'x',/, 't',/,/,i4,x,'1')
do 101 it=1,4
tw=temp(it)
do 202 kk=1,4
p=pres(kk)
do 303 i=1,9
l=u(i)

```

---

```

c
c Calculation of Plank's Function and it's derivative
c wnb Band Center
c hck Constant
c ccc c1*c2 (erg_k_cm**3/sec)
c pfdbi Plank's Function's derivative for ith band
c

```

```

tk1=tw**2
tk2=tw**0.5
tk3=tw/273.0
hck=1.439257246
ts=300.0/tw

```

---

```

c Spectroscopic Properties of CH4
c Two Bands of CH4 are considered(7.6 and 3.3 microns)
c wnbi Band Center (1/cm)

```

---

```

wnb1=1310.
wnb2=3020.
c2b1=hck*wnb1
c2b2=hck*wnb2
ccc=0.000053847734
ccb1=ccc*(wnb1**4)
ccb2=ccc*(wnb2**4)
tb1=c2b1/tw
tb2=c2b2/tw
teb1= exp(tb1)
teb2= exp(tb2)
c1b1=ccb1/c2b1
c1b2=ccb2/c2b2
pfb1=c1b1/(teb1-1.0)
pfb2=c1b2/(teb2-1.0)
dev1=tk1*((teb1-1.0)**2.0)
dev2=tk1*((teb2-1.0)**2.0)
pfdb1=(ccb1*teb1)/dev1
pfdb2=(ccb2*teb2)/dev2

```

---

c Band Model Correlations (Tien & Lowder wide band model)

```

c azi aoi (1/cm)
c czsi coi**2 (1/atm-cm)
c bsi b**2 (Nondimensional)
c omegi Wave Number (1/cm)
c si Integrated Band Intensity (1/atm cm**2)

```

---

```

ak1=(tw/300.)**0.5
ak2=(300./tw)**1.5
az1=39.8*ak1
az2=95.3*ak1

```

---

c dkf Thermal Conductivity (Erg/cm-sec-k)

```

kfb=(1488.365171)*(tk3**1.23)
czs1=4.58*ak2
czs2=3.15*ak2
s1=az1*cz1
s2=az2*cz2

```

---

C PL PRESSURE PATH LENGTH (ATM-CM)

```

PL = P* L
UZ1 = CZS1*PL
UZ2 = CZS2*PL
bs1 = 0.067*ak1
BS2 = 0.036*AK1

```

---

C PEI EFFECTIVE PRESSURE FOR EACH BAND (NON DIMENSIONAL)

C

$$PE1 = (1.3*P)**0.8$$

$$PE2 = (1.3*P)**0.8$$

C

C BETAI LINE STRUCTURE PARAMETR

C

$$BETA1 = BS1*PE1$$

$$BETA2 = BS2*PE2$$

C

C CORRELATION FOR EACH BAND

C

$$F1 = 2.94*(1.0 - EXP(-(2.6*BETA1)))$$

$$F2 = 2.94*(1.0 - EXP(-(2.6*BETA2)))$$

C

C NUMERICAL INTEGRATION

C

$$EPS(2) = 1E-04$$

$$EPS(1) = 1E-04$$

$$EP = 1.E-5$$

$$X1 = 0.0$$

$$X21 = (3./8.)*UZ1$$

$$X22 = (3./8.)*UZ2$$

$$Y11 = 1.5*UZ1$$

$$Y12 = 1.5*UZ2$$

$$Y21 = 3.0*X21$$

$$Y22 = 3.0*X22$$

CALL QDAGS(F101,X1,Y11,EPS(2),EPS(1),R01,IERR)

CALL QDAGS(F102,X1,Y12,EPS(2),EPS(1),R02,IERR)

CALL QDAGS(F111,X1,Y11,EPS(2),EPS(1),R11,IERR)

CALL QDAGS(F112,X1,Y12,EPS(2),EPS(1),R12,IERR)

CALL QDAGS(F121,X1,Y11,EPS(2),EPS(1),R21,IERR)

CALL QDAGS(F122,X1,Y12,EPS(2),EPS(1),R22,IERR)

CALL QDAGS(F131,X1,Y11,EPS(2),EPS(1),R31,IERR)

CALL QDAGS(F132,X1,Y12,EPS(2),EPS(1),R32,IERR)

CALL QDAGS(F141,X1,Y11,EPS(2),EPS(1),R41,IERR)

CALL QDAGS(F142,X1,Y12,EPS(2),EPS(1),R42,IERR)

CALL QDAGS(F101,X21,Y21,EPS(2),EPS(1),S11,IERR)

CALL QDAGS(F102,X22,Y22,EPS(2),EPS(1),S12,IERR)

CALL QDAGS(F111,X1,X21,EPS(2),EPS(1),S21,IERR)

CALL QDAGS(F112,X1,X22,EPS(2),EPS(1),S22,IERR)

CALL QDAGS(F111,X1,Y21,EPS(2),EPS(1),S31,IERR)

CALL QDAGS(F112,X1,Y22,EPS(2),EPS(1),S32,IERR)

CALL QDAGS(F121,X21,Y21,EPS(2),EPS(1),S41,IERR)

CALL QDAGS(F122,X22,Y22,EPS(2),EPS(1),S42,IERR)

CALL QDAGS(F131,X1,X21,EPS(2),EPS(1),S51,IERR)

CALL QDAGS(F132,X1,X22,EPS(2),EPS(1),S52,IERR)

CALL QDAGS(F131,X1,Y21,EPS(2),EPS(1),S61,IERR)

CALL QDAGS(F132,X1,Y22,EPS(2),EPS(1),S62,IERR)

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CALL QDAGS(F141,X21,Y21,EPS(2),EPS(1),S71,IERR)
CALL QDAGS(F142,X22,Y22,EPS(2),EPS(1),S72,IERR)
H1=AZ1*PFDB1
H2=AZ2*PFDB2
H=H1+H2+H3
AM=(H*L)/KFB
CU1 = 2./(3.*UZ1)
CU2 = 2./(3.*UZ2)
BR1A1 = (CU1*R11)-2.*(CU1**3)*R31+(CU1**4)*R41
BR1A2 = (CU2*R12)-2.*(CU2**3)*R32+(CU2**4)*R42
BR1B1=((CU1**2)*R21)-(CU1*R11)
BR1B2=((CU2**2)*R22)-(CU2*R12)
ETC1=((40.*(TW**(-1/3.)))-5.4)
ETC2=EXP(ETC1)*(1.E-6)
ETAC=ETC2/P
ETR11=8.*3.14*(1310.**2.)*4.08*(1.E-12)*s1*tw
ETAR1=1./ETR11
ETR12=8.*3.14*(3020.**2.)*4.08*(1.E-12)*s2*tw
ETAR2=1./ETR12
ETA11=ETAC/ETAR1
ETA12=ETAC/ETAR2
SUMA1 = H1*BR1A1
SUMA2 = H2*BR1A2
SUMAL=SUMA1+SUMA2
AL1L = 1.+(L/KFB)*SUMAL
SUMAN1=ETA11*CU1*BR1B1
SUMAN2=ETA12*CU2*BR1B2
SUMAN=(9./2.)*(SUMAN1+SUMAN2)
ALPH1=AL1L-SUMAN
BR2A1 = (CU1**2)*R21-2.*(CU1**3)*R31+(CU1**4)*R41
BR2A2 = (CU2**2)*R22-2.*(CU2**3)*R32+(CU2**4)*R42
BR2B1=R01-(6.*CU1*R11)+(6.*(CU1**2)*R21)
BR2B2=R02-(6.*CU2*R12)+(6.*(CU2**2)*R22)
SUMB1 = H1*BR2A1
SUMB2 = H2*BR2A2
SUMBL=SUMB1+SUMB2
SUMBN1=ETA11*CU1*BR2B1
SUMBN2=ETA12*CU2*BR2B2
SUMBN=(3./4.)*(SUMBN1+SUMBN2)
AL2L = (L/KFB)*SUMBL
ALPH2=AL2L-SUMBN
ALPH01=ETA11*(CU1**2)*(CU1*R21-R11)
ALPH02=ETA12*(CU2**2)*(CU2*R22-R12)
ALPH0=(9./2.)*(ALPH01+ALPH02)-1.
BR3A1 = (57./256.)*S11+(11./16.)*CU1*(S21+S31)
*-(9./8.)*(CU1**2)*S41-(CU1**3.)*(S51+S61)+(CU1**4.)*S71
BR3A2 = (57./256.)*S12+(11./16.)*CU2*(S22+S32)
*-(9./8.)*(CU2**2)*S42-(CU2**3.)*(S52+S62)+(CU2**4.)*S72
BR3B1=((9./4.)*CU1*S11)+(6.*(CU1**2.)*(S21+S31))

```

```

*-(12*(CU1**3.)*S41)
BR3B2=((9./4.)*CU2*S12)+(6.*(CU2**2.)*(S22+S32))
*-(12*(CU2**3.)*S42)
SUMC1 = H1*BR3A1
SUMC2 = H2*BR3A2
SUMCL=SUMC1+SUMC2
SUMCN1=ETA11*BR3B1
SUMCN2=ETA12*BR3B2
SUMCN=(3./8.)*(SUMCN1+SUMCN2)
AL3L =(11./16.)+(L/KFB)*SUMCL
ALPH3=AL3L+SUMCN
BR4A1 = (9.0/256.)*S11+(3.0/16.)*CU1*(S21+S31)
*-(1./8.)*(CU1**2.)*S41-(CU1**3.)*(S51+S61)+(CU1**4.)*S71
BR4A2 = (9.0/256.)*S12+(3.0/16.)*CU2*(S22+S32)
*-(1./8.)*(CU2**2.)*S42-(CU2**3.)*(S52+S62)+(CU2**4.)*S72
BR4B1=((1./4.)*CU1*S11)+(6.*(CU1**2.)*(S21+S31))-
*(12.*(CU1**3.)*S41)
BR4B2=((1./4.)*CU2*S12)+(6.*(CU2**2.)*(S22+S32))-
*(12.*(CU2**3.)*S42)
SUMD1 = H1*BR4A1
SUMD2 = H2*BR4A2
SUMDL=SUMD1+SUMD2
SUMDN1=ETA11*BR4B1
SUMDN2=ETA12*BR4B2
SUMDN=(3./8.)*(SUMDN1+SUMDN2)
AL4L = (3.0/16.)+(L/KFB)*SUMDL
ALPH4=AL4L+SUMDN
BR5B1=(3./16.)*(CU1*S11)+(1./2.)*(CU1**2.)*(S21+S31)-(CU1**3.)*S41
BR5B2=(3./16.)*(CU2*S12)+(1./2.)*(CU2**2.)*(S22+S32)-(CU2**3.)*S42
SUMEN1=ETA11*BR5B1
SUMEN2=ETA12*BR5B2
SUMEN=SUMEN1+SUMEN2
ALPH5=-((9./2.)*SUMEN+(11./16.))
DENA = (ALPH1*ALPH4)-(ALPH2*ALPH3)
A1=((ALPH0*ALPH4)-(ALPH2*ALPH5))/DENA
A2=((ALPH1*ALPH5)-(ALPH0*ALPH3))/DENA
TBULK = (1./70.)*((17.*A1)+(3.*A2))
CONST=1./16.*(AL1L*AL4L-AL2L*AL3L))
a11=(11.*a12-16.*a14)*CONST
A2L=(16.*AL3L-11.*AL1L)*CONST
TBULKL=(1/70.)*(17.*A1L+3.*A2L)
WRITE(6,200) TW,P,L,-TBULK,-TBULKL
write(7,203)l,-tbulk,-tbulk
write(8,201)l,-tbulk
303 CONTINUE
202 CONTINUE
101 CONTINUE
200 FORMAT(1X,F7.2, 3X,F6.2, 3X,F6.2, 2(3X,E10.4))
111 FORMAT(4X,'TW',8X,'P',6X,'L',9X,'TBULK',7X,'TBULKL')

```

```

201 format (1x,f9.2,3x,e10.4)
203 format (1x,f9.2,2(3x,e10.4))
STOP
END

```

C

```

FUNCTION F101(U1)
COMMON F1,F2
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F101 = AUD1
RETURN
END

```

```

FUNCTION F102(U2)
COMMON F1,F2
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2.)+(4.*U2*F2)+(4.*F2)))/DEN2
F102 = AUD2
RETURN
END

```

```

FUNCTION F111(U1)
COMMON F1,F2
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F111 = AUD1*U1
RETURN
END

```

```

FUNCTION F112(U2)
COMMON F1,F2
DEN2 = (F2*((U2*U2)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2*U2)+(4.*U2*F2)+(4.*F2)))/DEN2
F112 = AUD2*U2
RETURN
END

```

```

FUNCTION F121(U1)
COMMON F1,F2
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F121 = AUD1*U1*U1
RETURN
END

```

```

FUNCTION F122(U2)
COMMON F1,F2
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2.)+(4.*U2*F2)+(4.*F2)))/DEN2
F122 = AUD2*U2**2.
RETURN
END

```

```

FUNCTION F131(U1)
COMMON F1,F2

```

```

DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F131 = AUD1*U1**3.
RETURN
END
FUNCTION F132(U2)
COMMON F1,F2
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2.)+(4.*U2*F2)+(4.*F2)))/DEN2
F132 = AUD2*U2**3.
RETURN
END
FUNCTION F141(U1)
COMMON F1,F2
DEN1 = (F1*((U1**2.)+(2.*U1)+2.)+U1)*(U1+(2.*F1))
AUD1 = (F1*((U1**2.)+(4.*U1*F1)+(4.*F1)))/DEN1
F141 = AUD1*U1**4.
RETURN
END
FUNCTION F142(U2)
COMMON F1,F2
DEN2 = (F2*((U2**2.)+(2.*U2)+2.)+U2)*(U2+(2.*F2))
AUD2 = (F2*((U2**2.)+(4.*U2*F2)+(4.*F2)))/DEN2
F142 = AUD2*U2*U2*U2*U2
RETURN
END

```



## NONGRAY RESULTS FOR CH<sub>4</sub>

TW	P	L	TBULK (NLTE)	TBULKL (LTE)
300.00	0.10	0.10	0.2428E+00	0.2428E+00
300.00	0.10	0.50	0.2426E+00	0.2426E+00
300.00	0.10	1.00	0.2421E+00	0.2421E+00
300.00	0.10	5.00	0.2362E+00	0.2362E+00
300.00	0.10	10.00	0.2236E+00	0.2236E+00
300.00	0.10	20.00	0.1909E+00	0.1909E+00
300.00	0.10	50.00	0.1126E+00	0.1126E+00
300.00	0.10	75.00	0.7865E-01	0.7865E-01
300.00	0.10	100.00	0.5912E-01	0.5912E-01
300.00	1.00	0.10	0.2427E+00	0.2427E+00
300.00	1.00	0.50	0.2405E+00	0.2405E+00
300.00	1.00	1.00	0.2366E+00	0.2366E+00
300.00	1.00	5.00	0.2000E+00	0.2000E+00
300.00	1.00	10.00	0.1638E+00	0.1638E+00
300.00	1.00	20.00	0.1192E+00	0.1192E+00
300.00	1.00	50.00	0.6551E-01	0.6551E-01
300.00	1.00	75.00	0.4776E-01	0.4776E-01
300.00	1.00	100.00	0.3762E-01	0.3762E-01
300.00	5.00	0.10	0.2421E+00	0.2421E+00
300.00	5.00	0.50	0.2369E+00	0.2369E+00
300.00	5.00	1.00	0.2301E+00	0.2301E+00
300.00	5.00	5.00	0.1873E+00	0.1873E+00
300.00	5.00	10.00	0.1524E+00	0.1524E+00
300.00	5.00	20.00	0.1116E+00	0.1116E+00
300.00	5.00	50.00	0.6256E-01	0.6256E-01
300.00	5.00	75.00	0.4603E-01	0.4603E-01
300.00	5.00	100.00	0.3647E-01	0.3647E-01
300.00	10.00	0.10	0.2418E+00	0.2418E+00
300.00	10.00	0.50	0.2358E+00	0.2358E+00
300.00	10.00	1.00	0.2288E+00	0.2288E+00
300.00	10.00	5.00	0.1860E+00	0.1860E+00
300.00	10.00	10.00	0.1515E+00	0.1515E+00
300.00	10.00	20.00	0.1110E+00	0.1110E+00
300.00	10.00	50.00	0.6237E-01	0.6237E-01
300.00	10.00	75.00	0.4592E-01	0.4592E-01
300.00	10.00	100.00	0.3640E-01	0.3640E-01
500.00	0.10	0.10	0.2428E+00	0.2428E+00
500.00	0.10	0.50	0.2420E+00	0.2420E+00
500.00	0.10	1.00	0.2403E+00	0.2403E+00
500.00	0.10	5.00	0.2214E+00	0.2214E+00
500.00	0.10	10.00	0.1925E+00	0.1925E+00
500.00	0.10	20.00	0.1370E+00	0.1370E+00
500.00	0.10	50.00	0.5533E-01	0.5533E-01
500.00	0.10	75.00	0.3292E-01	0.3292E-01

500.00	0.10	100.00	0.2243E-01	0.2243E-01
500.00	1.00	0.10	0.2424E+00	0.2424E+00
500.00	1.00	0.50	0.2358E+00	0.2358E+00
500.00	1.00	1.00	0.2235E+00	0.2235E+00
500.00	1.00	5.00	0.1348E+00	0.1348E+00
500.00	1.00	10.00	0.8414E-01	0.8414E-01
500.00	1.00	20.00	0.4670E-01	0.4670E-01
500.00	1.00	50.00	0.1961E-01	0.1961E-01
500.00	1.00	75.00	0.1315E-01	0.1315E-01
500.00	1.00	100.00	0.9874E-02	0.9874E-02
500.00	5.00	0.10	0.2410E+00	0.2410E+00
500.00	5.00	0.50	0.2220E+00	0.2220E+00
500.00	5.00	1.00	0.1981E+00	0.1981E+00
500.00	5.00	5.00	0.1049E+00	0.1049E+00
500.00	5.00	10.00	0.6676E-01	0.6676E-01
500.00	5.00	20.00	0.3906E-01	0.3906E-01
500.00	5.00	50.00	0.1758E-01	0.1758E-01
500.00	5.00	75.00	0.1208E-01	0.1208E-01
500.00	5.00	100.00	0.9208E-02	0.9208E-02
500.00	10.00	0.10	0.2397E+00	0.2397E+00
500.00	10.00	0.50	0.2163E+00	0.2163E+00
500.00	10.00	1.00	0.1912E+00	0.1912E+00
500.00	10.00	5.00	0.1016E+00	0.1016E+00
500.00	10.00	10.00	0.6527E-01	0.6527E-01
500.00	10.00	20.00	0.3849E-01	0.3849E-01
500.00	10.00	50.00	0.1745E-01	0.1745E-01
500.00	10.00	75.00	0.1201E-01	0.1201E-01
500.00	10.00	100.00	0.9167E-02	0.9167E-02
1000.00	0.10	0.10	0.2428E+00	0.2428E+00
1000.00	0.10	0.50	0.2413E+00	0.2413E+00
1000.00	0.10	1.00	0.2374E+00	0.2374E+00
1000.00	0.10	5.00	0.1870E+00	0.1870E+00
1000.00	0.10	10.00	0.1370E+00	0.1370E+00
1000.00	0.10	20.00	0.8174E-01	0.8174E-01
1000.00	0.10	50.00	0.2821E-01	0.2821E-01
1000.00	0.10	75.00	0.1570E-01	0.1570E-01
1000.00	0.10	100.00	0.1013E-01	0.1013E-01
1000.00	1.00	0.10	0.2422E+00	0.2422E+00
1000.00	1.00	0.50	0.2292E+00	0.2292E+00
1000.00	1.00	1.00	0.2023E+00	0.2023E+00
1000.00	1.00	5.00	0.7068E-01	0.7068E-01
1000.00	1.00	10.00	0.3343E-01	0.3343E-01
1000.00	1.00	20.00	0.1501E-01	0.1501E-01
1000.00	1.00	50.00	0.5215E-02	0.5215E-02
1000.00	1.00	75.00	0.3305E-02	0.3305E-02
1000.00	1.00	100.00	0.2403E-02	0.2403E-02
1000.00	5.00	0.10	0.2396E+00	0.2396E+00
1000.00	5.00	0.50	0.1955E+00	0.1955E+00
1000.00	5.00	1.00	0.1418E+00	0.1418E+00

1000.00	5.00	5.00	0.3756E-01	0.3756E-01
1000.00	5.00	10.00	0.1943E-01	0.1943E-01
1000.00	5.00	20.00	0.9923E-02	0.9923E-02
1000.00	5.00	50.00	0.4036E-02	0.4036E-02
1000.00	5.00	75.00	0.2704E-02	0.2704E-02
1000.00	5.00	100.00	0.2033E-02	0.2033E-02
1000.00	10.00	0.10	0.2368E+00	0.2368E+00
1000.00	10.00	0.50	0.1755E+00	0.1755E+00
1000.00	10.00	1.00	0.1211E+00	0.1211E+00
1000.00	10.00	5.00	0.3371E-01	0.3371E-01
1000.00	10.00	10.00	0.1809E-01	0.1809E-01
1000.00	10.00	20.00	0.9493E-02	0.9493E-02
1000.00	10.00	50.00	0.3948E-02	0.3948E-02
1000.00	10.00	75.00	0.2661E-02	0.2661E-02
1000.00	10.00	100.00	0.2008E-02	0.2008E-02
2000.00	0.10	0.10	0.2428E+00	0.2428E+00
2000.00	0.10	0.50	0.2420E+00	0.2420E+00
2000.00	0.10	1.00	0.2395E+00	0.2395E+00
2000.00	0.10	5.00	0.1915E+00	0.1915E+00
2000.00	0.10	10.00	0.1320E+00	0.1320E+00
2000.00	0.10	20.00	0.7231E-01	0.7231E-01
2000.00	0.10	50.00	0.2597E-01	0.2597E-01
2000.00	0.10	75.00	0.1540E-01	0.1540E-01
2000.00	0.10	100.00	0.1035E-01	0.1035E-01
2000.00	1.00	0.10	0.2425E+00	0.2425E+00
2000.00	1.00	0.50	0.2347E+00	0.2347E+00
2000.00	1.00	1.00	0.2147E+00	0.2147E+00
2000.00	1.00	5.00	0.7459E-01	0.7459E-01
2000.00	1.00	10.00	0.3195E-01	0.3195E-01
2000.00	1.00	20.00	0.1307E-01	0.1307E-01
2000.00	1.00	50.00	0.4140E-02	0.4140E-02
2000.00	1.00	75.00	0.2542E-02	0.2542E-02
2000.00	1.00	100.00	0.1813E-02	0.1813E-02
2000.00	5.00	0.10	0.2411E+00	0.2411E+00
2000.00	5.00	0.50	0.2091E+00	0.2091E+00
2000.00	5.00	1.00	0.1553E+00	0.1553E+00
2000.00	5.00	5.00	0.3194E-01	0.3194E-01
2000.00	5.00	10.00	0.1475E-01	0.1475E-01
2000.00	5.00	20.00	0.7026E-02	0.7026E-02
2000.00	5.00	50.00	0.2743E-02	0.2743E-02
2000.00	5.00	75.00	0.1825E-02	0.1825E-02
2000.00	5.00	100.00	0.1369E-02	0.1369E-02
2000.00	10.00	0.10	0.2395E+00	0.2395E+00
2000.00	10.00	0.50	0.1880E+00	0.1880E+00
2000.00	10.00	1.00	0.1255E+00	0.1255E+00
2000.00	10.00	5.00	0.2607E-01	0.2607E-01
2000.00	10.00	10.00	0.1288E-01	0.1288E-01
2000.00	10.00	20.00	0.6470E-02	0.6470E-02
2000.00	10.00	50.00	0.2640E-02	0.2640E-02

2000.00	10.00	75.00	0.1778E-02	0.1778E-02
2000.00	10.00	100.00	0.1342E-02	0.1342E-02