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RESEARCH MEMORANDUM

SUPERSONIC FREE-FLIGHT MEASUREMENT OF HEAT TRANSFER

AND TRANSITION ON A 10° CONE HAVING A

LOW TEMPERATURE RATIO

By Charles F. Merlet and Charles B. Rumsey

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NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

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SUMMARY

Heat-transfer coefficients in the form of Stanton number and boundary-layer transition data were obtained from a free-flight test of a 100-inch-long 10° total-angle cone with a 1/16-inch tip radius which penetrated deep into the region of infinite stability of laminar boundary layer over a range of wall-to-local-stream temperature ratios and for local Mach numbers from 1.8 to 3.5. Experimental heat-transfer coefficients, obtained at Reynolds numbers up to 160×10^6 , were in general somewhat higher than theoretical values. A maximum Reynolds number of transition of only 33 × 106 was obtained. Contrary to theoretical and some other experimental investigations, the transition Reynolds number initially increased while the wall temperature ratio increased at relatively constant Mach number. Further increases in wall temperature ratio were accompanied by a decrease in transition Reynolds number. Increasing transition Reynolds number with increasing Mach number was also indicated at a relatively constant wall temperature ratio.

INTRODUCTION

The Pilotless Aircraft Research Division of the Langley Aeronautical Laboratory is currently conducting a program to measure the aerodynamic heating and Reynolds number for boundary-layer transition on bodies in free flight at high Mach numbers. Data of this type are reported in reference 1 for a 10° total-angle cone, 40 inches in length, over a Mach number range from 1.15 to 3.7. The present test was also conducted with a 10° total-angle cone, and was planned to extend the results of reference 1 by obtaining test conditions deeper within the region of two-dimensional infinite laminar-boundary-layer stability defined by reference 2. In order to obtain low wall-to-stream temperature ratios, the

model skin was made of thick copper, selected because of its high heat capacity and thermal diffusivity. In order to measure large transition Reynolds numbers in the event they should occur, the nose cone was made 100 inches long, providing test Reynolds numbers up to 160×10^6 .

Although test conditions were obtained well into the region of two-dimensional stability, turbulent heating at all measurement stations during the early part of the test resulted in higher than anticipated wall-to-stream temperature ratios and the test conditions were only slightly deeper within the stability region than those of reference 1.

The measurements of transition Reynolds number and local heattransfer coefficient are presented for a Mach number range of 1.8 to 3.5 and for a range of Reynolds numbers from 5×10^6 to 164×10^6 based on nose length to a measurement station. The flight test was performed at the Langley Pilotless Aircraft Research Station at Wallops Island, Va.

SYMBOLS

A	area, sq ft
c _f	local skin-friction coefficient
cp	specific heat of air at constant pressure, $Btu/lb-^{O}F$
CW	specific heat of wall material, Btu/lb- ^O F
g	acceleration due to gravity, 32.2 ft/sec ²
h	local aerodynamic heat-transfer coefficient, Btu/sec-ft ² - ^o F
k	thermal conductivity of air, Btu-ft/sec- ^o F-ft ²
kw	thermal conductivity of wall material, Btu-ft/sec- ^o F-ft ²
М	Mach number
Mpr	Prandtl number, $gc_p\mu/k$
N _{St}	Stanton number, $\frac{h}{g \rho_v c_{p_v} V_v}$

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Q	quantity of heat, Btu
R	Reynolds number, pVx/µ
Т	absolute temperature, ^O R
t	time, sec
V	velocity, ft/sec
x	axial distance, ft
E	emissivity
μ	absolute viscosity of air, slugs/ft-sec
ρ	density of air, slugs/cu ft
Pw	density of wall material, lb/cu ft
σ	Stefan-Boltzman constant, 0.4806 × 10 ⁻¹² , Btu/ft ² -sec-(°R) ⁴
т	skin thickness, ft
Subscri	pts:
aw	adiabatic wall
S	stagnation
tr	at transition point
v	local condition just outside boundary layer
W	at wall
00	free stream

MODEL, INSTRUMENTATION, AND TESTS

Model

The model was a 100-inch long cone having a total angle of 10°, mounted on an M5 Jato rocket motor as shown in figures 1 and 2. The complete configuration was stabilized by four fins. Except for the

tip. the cone was constructed from two conic sections joined by a circumferential weld at station 58.5 (that is, 58.5 inches from the nose tip). These sections were formed from two copper sheets of which the thicknesses were 0.077 and 0.080 ± 0.002 inch. The thinner sheet formed the skin ahead of station 58.5. The weld was done with a copper rod of the same composition as the sheet. The model tip, made of steel, was welded to the first conic section at station 6. The sharp point was blunted with a small radius (approximately 1/16 inch) to prevent excessive heating. After construction was completed, the exterior surface of the cone was polished. Random sample measurements of the surface roughness as determined by a Physicists Research Company Profilometer varied from 10 to 16 microinches rms. However, subsequent to the flight test, sample roughness measurements made with the Profilometer were checked optically with a fringe-type interference microscope. The average roughness measured optically was about 8 to 10 times the root-mean-square value read on the Profilometer for a copper sample. Also, discrete scratches were observed optically which apparently did not influence the profilometer measurements. It appears that the average surface roughness of the model skin may have been of the order of 100 to 150 microinches.

Instrumentation

The model was equipped with 12 thermocouples located in line axially along the cone from station 12 to 88 as indicated in figure 1. The thermocouples, made from no. 30 chromel-alumel wire, were installed by drilling separate holes for each wire approximately 1/4 inch apart and soldering the wires in place with high-temperature silver solder. The external surface was then polished.

The 12 thermocouple outputs were commutated and transmitted on two telemeter channels. Each channel transmitted six thermocouple outputs and three standard voltages at a rate of 14 times per second and 7 times per second, respectively. The standard voltages chosen were equivalent to the lowest, middle, and highest temperatures expected and served as an in-flight calibration of the telemeter throughout the flight.

Test

The model was launched at an elevation angle of 70° (fig. 2) and propelled to a maximum flight Mach number of 3.6 by a single M5 Jato booster rocket motor. Data were obtained during the accelerating portion of the flight and the decelerating portion subsequent to rocket-motor burnout. Flight velocity was determined from CW Doppler radar. Altitude and flight-path data were obtained from measurements made by an NACA modified SCR-584 tracking radar. Ambient air conditions as well as winds aloft were measured with a radiosonde used in conjunction with an AN/CMD-1A rawin set.

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Figure 3 shows the time histories of flight Mach number, altitude, and free-stream Reynolds number per foot.

DATA REDUCTION

The time rate of change of heat within the skin at a given location on the conical nose can be written as follows:

$$\frac{\mathrm{d}Q}{\mathrm{d}t} = \rho_{\mathrm{w}} c_{\mathrm{w}} \tau A \frac{\mathrm{d}T_{\mathrm{w}}}{\mathrm{d}t} = hA \left(T_{\mathrm{aw}} - T_{\mathrm{w}} \right) - A\sigma \epsilon T_{\mathrm{w}}^{4} + Ak_{\mathrm{w}} \tau \left(\frac{\partial^{2} T_{\mathrm{w}}}{\partial x^{2}} + \frac{1}{x} \frac{\partial T_{\mathrm{w}}}{\partial x} \right)$$
(1)

The three terms on the right-hand side of equation (1) account for the aerodynamic heat transfer to the skin, the radiation of heat from the skin externally, and the rate of heat conduction along the skin, respectively. This equation neglects the heat absorbed by the skin from solar radiation and heat radiated inward from the skin, which are compensating and estimated to be negligible.

In the data presented herein, the effects of conduction along the skin have been neglected since calculations indicated that the largest conduction effects were less than 2 percent of the aerodynamic heat transfer. Radiation effects have not been included because the value of emissivity for copper varies greatly with surface conditions, and the effects on the surface condition of flight test conditions of temperature and velocity are unknown. Radiation effects were checked, however, using an emissivity of 0.70, which is for heavily oxided copper, and the highest value reported. The radiation effects thus calculated in general amounted to 10 percent or less of the aerodynamic heating from 10 seconds on. At earlier times, radiation in general was less than 5 percent of the aerodynamic heating. In no case, however, could the radiation effects alter the heat-transfer data sufficiently to influence the determination of the location of boundary-layer transition.

The adiabatic wall temperature T_{aw} was calculated from local stream conditions outside the boundary layer as determined from reference 3, using a recovery factor of $N_{Pr}^{1/2}$ and $N_{Pr}^{1/3}$ based on local temperature for laminar and turbulent boundary layer, respectively. Stanton number was then computed as follows:

$$N_{\rm St} = \frac{h}{g \rho_{\rm V} c_{\rm p_{\rm V}} V_{\rm V}}$$

RESULTS AND DISCUSSION

Skin Temperatures

The measured skin temperatures for each station are presented in table I for each time for which data have been reduced. The table also presents the corresponding local Mach number and Reynolds number per foot, and the corresponding values of $\frac{1}{A} \frac{dQ}{dt}$, the time rate of change of heat within a square foot of skin.

The temperature-time curves of the first five stations are plotted in figure 4, along with local Mach number just outside the boundary layer, as a function of time. The curves for the remaining stations are not plotted inasmuch as they would vary only slightly (see values for temperatures given in table I) from those shown for stations 27 and 35.

The abrupt decrease in slope of the temperature-time curves for stations 17 and 22 at time 3.5 and 4.0 seconds, respectively, and the earlier, more gradual reduction in slope for station 12 indicate transition from turbulent to laminar or transitional flow. However, the character of the boundary layer and the location of transition can be determined more readily from the heat-transfer coefficients, and will be discussed later.

Heat-Transfer Coefficient

The heat-transfer coefficients in the form of Stanton numbers are presented in figure 5 as a function of axial distance along the body. The wall temperature ratios are also shown, as well as the theoretical values of N_{St} . The theoretical Stanton numbers for conical laminar flow were obtained by multiplying the flat-plate values of reference 4 by $\sqrt{3}$. The theoretical turbulent values of N_{St} were obtained from c_f values by the conversion of reference 5 (that is, $N_{St} = 0.6c_f$). The values of c_f were obtained from charts of Van Driests flat-plate theory presented in reference 6 and converted to conical flow by the method of reference 7.

In general, the experimental turbulent values are in fair agreement with theory. From 3.0 seconds on, the experimental values tend to be somewhat higher than the theoretical predictions for both laminar and turbulent values. The data at 7.0 and 10.0 seconds, which exhibited the most scatter, occurred near the peak of the temperature-time curves (see fig. 4) and therefore have low forcing functions $(T_{aw} - T_w)$ and are least accurate. The remaining data, however, are unaccountably higher than theory.

Boundary-Layer Transition

The disagreement between theory and experiment is not enough to preclude the determination of transition, and the variation of transition along the cone as the flight time progressed is apparent. The experimental Stanton numbers of figure 5 indicate that prior to 3.0 seconds fully turbulent flow occurred at least as far forward as station 12, the first measuring station. Transition occurred first at the forward measuring station, then moved rearward with time until, at 4.5 seconds, station 22 showed laminar flow with a local Reynolds number of 33×10^6 . Transition then moved forward again until at 14 seconds the flow was again fully turbulent at station 12 and rearward.

The transition data determined from the data presented in figure 5 include a variation of both Mach number and wall temperature ratio. The variation of wall temperature ratio with local Mach number for the transition points (taken as the last station with a laminar heat-transfer coefficient) is shown in figure 6. The corresponding Reynolds number based on local conditions is indicated for each point in the figure. The broken curve shows for comparison the conditions of M_v and T_w/T_v of the test of reference 1. Also presented in the figure is the curve bounding the region of theoretical infinite laminar stability for twodimensional disturbances as determined by Van Driest in reference 2. It was this region that the model was designed to explore, and it can be seen that the data penetrated well into it. A more recent paper by Dunn and Lin (ref. 8), however, indicates that an infinite stability region cannot be found for three-dimensional disturbances. However, Dunn and Lin conclude that sufficient cooling can stabilize the boundary layer to very large Reynolds numbers.

The present data are somewhat at variance with this trend, as can be seen in figure 7, where transition Reynolds number is plotted against wall temperature parameter $\frac{T_w - T_{aw}}{T_s}$. The usual trend, as indicated by

the stability theory, is illustrated by the data from reference 9 which show an increase in transition Reynolds number as the wall is cooled. The data of the present test for a relatively constant Mach number (from 3.5 to 3.2), on the other hand, show an increase in Reynolds number of transition as the wall temperature increased from a temperature parameter of -0.50 to -0.31, corresponding to a wall temperature ratio change from 1.2 to 1.65. With a further decrease in temperature parameter as Mach number continued to decrease from 3.2 to 2.8, the transition Reynolds number decreased rather sharply. Although the reason for this behavior of transition Reynolds number with cooling is not known, data reported in reference 10 show that for certain degrees of roughness, cooling produces similar trends in transition Reynolds number, apparently by causing an excessive thinning of the boundary layer in comparison to the roughness. As previously mentioned (see section entitled "Model"), the average roughness of the present copper skin may have been 100 to 150 microinches in comparison with computed boundary-layer displacement thickness at the transition station of 0.0048 inch for the coolest wall condition $(R_{\rm tr} = 22.1 \times 10^6)$ and 0.0086 inch at maximum transition Reynolds number of 33.1 × 10⁶.

The data of reference 1, also shown in figure 7, indicate a similar trend, in that cooling beyond a certain point showed no further increase in transition Reynolds number. The average roughness of the model of reference 1, however, is estimated to be only 10 to 20 microinches, whereas computed boundary-layer displacement thicknesses are of the same order as those of the present test. (The estimated roughness of the model in ref. 1 is based on a comparison of the roughness of an Inconel sample determined from optical and profilometer measurements which indicated the average roughness may have been 3 to 4 times the profilometer measurements of 3 to 5 microinches rms reported in ref. 1.)

The measured transition Reynolds numbers of the present test were considerably higher than those reported in reference 1 despite the larger roughness of the present model. However, since the tip of the present model was blunted to a 1/16-inch radius while the tip of reference 1 model was sharp, the difference in magnitude of transition Reynolds numbers may be due, in part at least, to the beneficial effects of tip bluntness described in reference 11. Reference 11 points out that the detached shock wave associated with the blunt tip results in a "low Mach number region" of air flowing over the body. When the body boundary layer is enveloped by this low energy air, large increases in transition Reynolds number will result. In the present case, tip bluntness of the model was not large enough to envelope completely the laminar boundary layer in the low Mach number region defined in reference 11; however, comparison of the computed boundary-layer thickness with the inviscid Mach number profiles presented in reference 11 indicated the bluntness was enough so that the inviscid Mach number at the edge of the boundary layer at transition stations was markedly reduced below theoretical cone values.

Thus it appears that the difference in magnitude of transition Reynolds number in these two tests may be due, in part at least, to the bluntness of the tip of the present model. The similarity of trend of transition Reynolds number with increased cooling, however, is still not explained completely. Apparently some factor besides roughness influenced the trend of transition Reynolds number with cooling in these tests.

The transition Reynolds numbers for the latter part of the flight are shown in figure 8 as a function of Mach number for wall temperature

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ratios T_W/T_V from approximately 1.5 to 1.9. The data indicate a distinct increase in transition Reynolds number with Mach number for this model. A similar trend was noted in reference 1 for skin temperature ratios of about 1.2 to 1.3, although the Reynolds number increase was not as pronounced in reference 1. It is believed that this increased slope of transition Reynolds number with Mach number in the present test can be attributed to the effect on local Reynolds number of the tip bluntness employed on the present model. As indicated in reference 11, the effect of bluntness on local Reynolds number is greater as Mach number increases.

CONCLUDING REMARKS

Heat-transfer coefficients in the form of Stanton number and boundary-layer transition data were obtained from a free-flight test of a 10° total-angle conical nose with a 1/16-inch tip radius over a Mach number range from 1.8 to 3.5 and a range of wall-to-local-stream temperature ratios. In general, experimental heat-transfer coefficients were somewhat higher than theoretical predictions for turbulent values for Reynolds numbers up to 160×10^{6} . A maximum Reynolds number of transition of 33×10^{6} was obtained. Contrary to theoretical and some other experimental investigations, the Reynolds number of transition initially increased while the wall temperature ratio increased at relatively constant Mach number. Further increases in wall temperature ratio were accompanied by a decrease in transition Reynolds number. A favorable effect of increasing Mach number on transition Reynolds number was also indicated at a relatively constant wall temperature ratio.

Langley Aeronautical Laboratory,

National Advisory Committee for Aeronautics, Langley Field, Va., November 23, 1956.

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TABLE I.- SUMMARY OF DATA

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	M _v	R _v /ft	T _v , °R	Stat	Station 12		tion 17	Station 22		Station 27		Station 35		Station 43		Station 51		Station 59		Station 67		Station 75		Station 83		Station 88	
Time, sec				Τ _w , °R	$\frac{1}{A} \frac{dQ}{dt},$ Btu	T _w ,	$\frac{1}{A} \frac{dQ}{dt},$ Btu	T _w ,	$\frac{1}{A} \frac{dQ}{dt},$ Btu	Tw,	$\frac{1}{A} \frac{dQ}{dt}$,	I _w ,	$\frac{1}{A} \frac{dQ}{dt},$ Btu	T _w ,	$\frac{1}{A} \frac{dQ}{dt}$,	Tw,	$\frac{1}{A} \frac{dQ}{dt}$,	T _w ,	$\frac{1}{A} \frac{dQ}{dt}$ Btu op	$\frac{1}{A} \frac{dQ}{dt}$,	Tw,	$\frac{1}{A} \frac{dQ}{dt}$,	T _w ,	$\frac{1}{A} \frac{dQ}{dt}$,	Tw,	$\frac{1}{A} \frac{dQ}{dt}$	
					ft ² -sec	- K	ft ² -sec	R	ft ² -sec	A	ft ² -sec	-K	ft ² -sec	-11	ft ² -sec	-11	ft ² -sec	-11	ft ² -sec	-11	ft ² -sec	-11	ft ² -sec	-11	ft ² -sec	-A	ft ² -sec
2.0	1.96	13.6 × 10 ⁻⁶	538	563	20.0	563	20.9	563	17.0	565	17.3	562	15.2	563	18.3	560	13.5	563	18.2	560	14.5	563	18.9	561	13.5	563	18.9
2.5	2.64	18.2	542	607	35.9	607	33.1	604	34.4	601	37.6	594	34.8	595	29.4	590	31.1	596	34.2	592	28.8	596	29.5	592	29.9	595	29.5
3.0	3.28	22.1	550	650	24.9	670	51.4	667	56.3	676	60.8	666	59.1	663	62.3	658	55.3	666	61.4	651	58.8	660	60.0	649	56.9	656	59.2
3.5	3.48	22.4	547	684	20.3	788	31.2	772	49.9	770	61.1	757	62.1	755	58.3	745	57.5	760	63.0	736	57.6	745	56.8	736	56.2	739	54.4
4.0	3.31	20.2	536	711	17.3	812	9.6	852	28.3	851	48.6	837	42.0	829	44.6	820	39.9	836	43.5	810	42.8	813	37.4	803	37.7	807	38.2
4.5	3.15	18.1	527	732	11.6	824	7.4	875	8.0	903	26.0	889	26.2	877	25.9	865	25.6	885	27.0	856	26.2	853	27.2	845	26.2	850	26.7
5.0	3.01	16.3	521	747	10.8	833	5.5	888	10.3	934	18.8	922	19.8	908	19.4	896	20.1	917	18.8	885	19.0	890	18.0	877	18.6	881	17.9
6.0	2.78	13.5	508	775	7.2	848	5.2	914	7.3	967	5.4	957	8.5	950	9.4	936	9.1	954	8.5	923	9.8	924	9.3	914	9.3	916	8.8
7.0	2.58	11.3	498	791	4.5	863	5.2	931	3.3	975	2.1	972	1.7	966	4.5	953	4.0	966	2.8	941	3.6	940	3.9	932	4.5	935	5.0
10.0	2.17	7.6	462	816	1.6	885	-0.5	929	-2.3	960	-2.9	965	-3.2	959	-1.8	950	-2.4	959	-2.7	939	-2.5	940	-2.7	935	-2.0	935	-2.3
12.0	1.96	6.1	440	818	-0.3	872	-2.4	909	-3.7	935	-5.9	943	4.2	941	-4.5	930	-3.5	937	-4.6	922	-3.3	924	-3.3	917	-3.2	919	-3.0
14.0	1.79	5.0	421	813	-2.6	854	-3.8	887	4.2	910	4.5	918	4.2	916	-4.2	910	-3.5	912	-3.6	903	-3.6	903	-2.9	901	-3.3	901	-3.1



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Figure 2.- Model on the launcher. L-89648.1



Figure 3.- Time histories of free-stream Mach number, Reynolds number per foot, and altitude.







(b) 2.5 sec; $M_v = 2.64$; $R_v/ft = 18.2 \times 10^6$.

Figure 5.- The variation of Stanton number and wall temperature ratio with axial distance along body.



(d) 3.5 sec; $M_V = 3.48$; $R_V/ft = 22.4 \times 10^6$.

Figure 5.- Continued.



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Figure 5. - Continued.





Figure 5. - Continued.



Figure 5.- Continued.

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Figure 5.- Concluded.

Figure 6.- Mach number and wall-temperature-ratio transition stations.

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Figure 7.- Variation of transition Reynolds number with wall temperature parameter.

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Figure 8.- Variation of transition Reynolds number with local Mach number.

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