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Cyclic Axial-Torsional Deformation Behavior of a Cobalt-Base Superalloy

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SUMMARY

Multiaxial loading, especially at elevated temperature, can cause the inelastic response of a material to differ significantly from that predicted by simple flow rules, i.e., von Mises or Tresca. To quantify some of these differences, the cyclic high-temperature, deformation behavior of a wrought cobalt-base superalloy, Haynes 188, is investigated under combined axial and torsional loads. Haynes 188 is currently used in many aerospace gas turbine and rocket engine applications, e.g., the combustor liner for the T800 turboshaft engine for the RAH-66 Comanche helicopter and the liquid oxygen posts in the main injector of the space shuttle main engine. The deformation behavior of this material is assessed through the examination of hysteresis loops generated from a biaxial fatigue test program. A high-temperature axial, torsional, and combined axial-torsional fatigue data base has been generated on Haynes 188 at 760 °C. Cyclic loading tests have been conducted on uniform gauge section tubular specimens in a servohydraulic axial-torsional test rig. Test control and data acquisition were accomplished with a minicomputer. The fatigue behavior of Haynes 188 at 760°C under axial, torsional, and combined axial-torsional loads, and the monotonic and cyclic deformation behaviors under axial and torsional loads, have been previously reported. In this paper, the cyclic hardening characteristics and typical hysteresis loops in the axial stress versus axial strain, shear stress versus engineering shear strain, axial strain versus engineering shear strain, and axial stress versus shear stress spaces are presented for cyclic, in-phase and out-of-phase, axial-torsional tests. For in-phase tests three different values of the proportionality constant, λ (ratio of engineering shear strain amplitude to axial strain amplitude, γ_a/ϵ_a), are examined, viz., 0.86, 1.73, and 3.46. In the out-of-phase tests, three different values of the phase angle, ϕ (between the axial and engineering shear strain waveforms), are studied, viz., 30°, 60°, and 90° with $\lambda = 1.73$. The cyclic hardening behaviors of all the tests conducted on Haynes 188 at 760 °C are evaluated using the von Mises equivalent stress-strain and the maximum shear stress-maximum engineering shear strain (Tresca) curves. Comparisons are also made between the hardening behaviors of cyclic axial, torsional, and combined in-phase ($\lambda = 1.73$ and $\phi = 0^\circ$) and out-of-phase ($\lambda = 1.73$ and $\phi = 90^\circ$) axial-torsional fatigue tests. These comparisons are accomplished through simple Ramberg-Osgood type stress-strain functions for cyclic, axial stress-strain and shear stress-engineering shear strain curves.

INTRODUCTION

The imperatives of higher efficiency and improved performance in gas turbines require that the rotating speeds, power extraction per turbine stage, and operating temperatures all be increased beyond the

current levels. This may mean that the materials used in the hot section are being pushed up to, and beyond, their recommended usage limits. It is important that the deformation behavior of these materials be understood at temperatures and loading conditions that approximate the service conditions of the component. Design decisions for these materials are currently being made with material properties and data bases that have been extrapolated from lower-temperature, uniaxial fatigue and deformation data. These extrapolated data may imply a behavior that is significantly different from the material's actual response under service conditions.

The cyclic deformation behavior of polycrystalline metallic materials, under combined axial-torsional loading conditions, has been the subject of several investigations (refs. 1 to 9). These studies were conducted on tubular specimens of low-alloy steels (refs. 1, 3, and 7), stainless steels (refs. 1, 2, and 4 to 8), and a superalloy (ref. 9) at both room (refs. 1 to 7 and 9) and elevated (refs. 1 and 8) temperatures. Different types of waveforms, including sinusoidal (refs. 2 to 9), triangular (refs. 1, 4, and 6), and trapezoidal (refs. 4 to 7) were employed as command inputs for the axial and engineering shear strains. In this study, the cyclic deformation behavior of a wrought cobalt-base superalloy, Haynes 188, has been investigated under axial-torsional loading conditions at 760 °C. Haynes 188 is currently used in many aerospace gas turbine and rocket engine applications, e.g., the combustor liner for the T800 turboshaft engine for the RAH-66 Comanche helicopter and the liquid oxygen posts in the main injector of the space shuttle main engine.

The objective of this paper is to disseminate the cyclic deformation data collected in the course of performing high-temperature, axial-torsional, fatigue tests on Haynes 188, and to relay some observations about the collected data. Various independent, as well as simultaneous, combinations of axial and torsional loads were imposed on 36 specimens in the test program. The following axial-torsional deformation results are discussed: (1) the effect of the ratio of the engineering shear strain amplitude to the axial strain amplitude (proportionality constant, λ) on the in-phase (proportional) deformation behavior, and (2) the effect of phase angle (ϕ) between the axial and engineering shear strains (out-of-phase or nonproportional) on the cyclic and stabilized stress response. The cyclic hardening under different axial-torsional loading conditions is presented through plots of hysteresis loops at several cyclic increments, and plots of stress range versus number of cycles. In addition, the presentation format consists of normalized plots of stable (near half-life) axial and torsional hysteresis loops as well as normalized plots of the axial strain versus engineering shear strain and the axial stress versus shear stress for the near half-life conditions. Also, results of regressed fits to the Ramberg-Osgood equation with the stabilized cyclic deformation data under various axial-torsional loading conditions are reported. The stabilized deformation behaviors of the in- and out-of-phase axial-torsional experiments are compared.

All tests described in this paper were conducted in air, at 760 °C. This temperature was chosen because Haynes 188 displays a marked drop in ductility at this temperature (ref. 10). This ductility minimum is most likely due to complex interactions between mobile solute atoms and dislocations. Understanding the deformation behavior at this temperature will advance our ability to assess this material's usefulness in advanced gas turbine applications.

NOMENCLATURE

E,G	Young's and shear moduli
K'	cyclic axial strength coefficient
K' _t	cyclic torsional strength coefficient
N	cycle number

N_f	cyclic life
n'	cyclic axial strain hardening exponent
n'_t	cyclic torsional strain hardening exponent
γ, ϵ	engineering shear and axial strains
γ_a, ϵ_a	engineering shear and axial strain amplitudes
γ_{\max}	maximum engineering shear strain (Tresca)
Δ	denotes range of the variable
ϵ_e, ϵ_p	axial elastic and plastic strains
ϵ_{eq}	von Mises equivalent strain
λ	proportionality constant, γ_a/ϵ_a
ν_e, ν_p	elastic and plastic Poisson's ratios
ν_{eff}	effective Poisson's ratio
σ, τ	axial and shear stresses
σ_a, τ_a	axial and shear stress amplitudes
τ_{\max}	maximum shear stress (Tresca)
ϕ	phase angle between axial and engineering shear strain waveforms

EXPERIMENTAL PROGRAM

The cobalt-base superalloy, Haynes 188, was supplied by a commercial vendor in the form of hot rolled, solution-annealed, round bars with a nominal diameter of 50.8 mm (manufactured to Aerospace Material Specification 5772A). The chemical composition of the superalloy in weight percent is as follows: <0.002 S; 0.002 B; 0.012 P; 0.1 C; 0.4 Si; 0.034 La; 0.75 Mn; 1.24 Fe; 13.95 W; 21.84 Cr; and 22.43 Ni; with cobalt making up the balance. The grains in the supplied material were equiaxed and ranged in size from 45 to 65 μm . The specifications for machining the specimens were explicitly designed to minimize surface work hardening. No post-machining heat treatment was performed on the tubular specimens.

Thin-walled tubular specimens with a nominal outer diameter of 26 mm, a nominal inner diameter of 22 mm, and a nominal gauge length of 25 mm (fig. 1) were used in all experiments. The tubular specimens in the axial-torsional test program were heated to the test temperature of 760 °C using a 10 kHz, 10 kW, induction heating system with a three coil (each of the coils is independently moveable) fixture. In all tests, the temperature in the gauge section was maintained to within ± 7 °C of the control temperature. A servohydraulic axial-torsional load frame capable of ± 223 kN of axial load and ± 2.26 kN-m of torque was used in all experiments. A commercial, water-cooled, axial-torsional extensometer was employed for strain measurement. Further detail on the testing equipment can be found in references 11 to 13.

Data acquisition and test control were accomplished with a minicomputer and associated electronic hardware. Detailed information on the data acquisition and control hardware and software for the cyclic axial-torsional experiments can be found in reference 13. Data were acquired at 500 points per loading cycle to ensure that significant, high-rate, deformation phenomenon, and the peak stresses and strains, were accurately acquired.

Constant strain-rate (triangular) axial and/or engineering shear strain waveforms were imposed on all specimens. The frequency of both of the command waveforms was 0.1 Hz for all tests, therefore the strain rate from test to test varied depending on the amplitudes of the strain waveforms. The difference in the strain rates between the smallest and the largest amplitude tests was, at most, a factor of 7. Because the differences in strain rates were relatively small, little or no strain rate effect on the deformation behavior is expected in the tests performed. The engineering shear strain at the mean radius of the tubular specimen was controlled in all the experiments that had an imposed engineering shear strain. In calculating the shear stress at the mean radius of the specimen, the shear stress was assumed to be uniformly distributed through the thickness of the tubular specimen. In all experiments, the test control software incorporated a graduated five cycle load up. This allowed for better test control at the onset of serrated yielding behavior that is often displayed by Haynes 188 when large plastic strains are present. In almost every case this five-cycle loadup resulted in some initial plastic deformation in the specimens, therefore, some initial hardening was introduced before the first cycle data were collected.

The test matrix of the axial-torsional test program is shown in table I. Five different values of the proportionality constant, λ , and four phase angles, ϕ , have been investigated in the axial-torsional experiments. The number of tests conducted for each test condition, which is given by a set of λ and ϕ values, is shown in table I. In figure 2, a simple schematic is presented of the imposed strains during an in-phase and an out-of-phase axial-torsional fatigue test.

RESULTS

The effect of strain cycling on the shapes of the hysteresis loops is illustrated in figures 3 to 6. Axial and torsional loops at 1, 10, 100, and 1000 cycles are plotted for cyclic axial-torsional experiments performed with phase angles, ϕ , of 0°, 30°, 60°, and 90°. In all cases, Haynes 188 exhibited cyclic strain hardening, which is characterized by an increase in the stress range and an associated reduction in the width of the hysteresis loop.

To facilitate direct comparison of the axial and shear cyclic hardening rates of specimens that were subjected to in-phase (proportional) strain paths with different ratios of engineering shear to axial strain amplitudes, the stress ranges were normalized by the first cycle's (after the five cycle loadup) stress range. Plots of the normalized axial component of the in-phase cyclic stresses versus the number of cycles and the normalized shear component of the in-phase cyclic stresses versus the number of cycles are shown in figures 7 and 8. For the axial component of stress, all the in-phase axial-torsional tests exhibited similar cyclic hardening rate, which was lower than that observed in the axial test. For the shear component of stress, all the in-phase tests exhibited a cyclic hardening rate that was similar to the torsional test.

The cyclic hardening rates of specimens subjected to the same nominal axial and engineering shear strain amplitudes, with phase angles between the axial and torsional command waveforms of 0°, 30°, 60°, and 90°, are compared in figures 9 and 10. In these figures the axial and shear stress ranges are plotted against the number of cycles. Both the axial and shear stress components clearly indicate higher first cycle hardening as the phase angle, ϕ , increases from 0° to 90°. This pattern of increased hardening with phase angle is maintained throughout the life of the out-of-phase tests. In plotting the near half-life hysteresis loops from the out-of-phase tests, the stress and strain components were normalized with half the range (amplitude) of the corresponding variable, so that the shapes of the hysteresis loops for different ϕ values could be compared. By normalizing the variables, the isotropic hardening effects are concealed so that the kinematic effects can be compared directly. The maximum and minimum values of the strains and stresses in the near half-life axial and torsional loops are listed in table II. Figures 11 to 14

are the near half-life, normalized, axial (σ/σ_a) versus ϵ/ϵ_a) and torsional (τ/τ_a versus γ/γ_a) hysteresis loops from four specimens, which were subjected to the same nominal axial and engineering shear strain amplitudes but with four different phase angles (ϕ) between the strain waveforms. Also displayed in each figure are the normalized plots of the axial strain (ϵ/ϵ_a) versus the engineering shear strain (γ/γ_a) and the axial stress (σ/σ_a) versus the shear stress (τ/τ_a). The normalized axial strain—engineering shear strain plots display the strain path imposed on the specimen. The labels A, B, C, and D in figure 2 illustrate where each of the strain reversals occur. The labels are repeated at the corresponding points in the normalized figures (figs. 11 to 14). The small discontinuities seen in the normalized axial strain versus engineering shear strain and the normalized axial stress versus shear stress plots are due to a seal friction problem in the axial actuator of the test rig, which resisted all attempts of compensation.

For each axial-torsional test conducted, the von Mises equivalent stress, von Mises equivalent strain, the maximum shear stress and the maximum engineering shear strain (Tresca stress and strain) were computed from the near half-life hysteresis loop data. For each of these quantities, the calculation was performed at each of the 500 collected data points around the cycle to determine the maximum and minimum values. Performing the equivalent and maximum shear calculations in this way was not specifically necessary for the case of the in-phase tests, but it was required for the out-of-phase experiments because the maximum values of the equivalent or maximum shear stress and strain may not coincide with peak axial or torsional stresses and strains in the out-of-phase experiments.

An effective Poisson's ratio (ν_{eff}) was computed based on the measured axial stresses and strains. At each point around the hysteresis loop, ν_{eff} was computed with the following equation:

$$\nu_{\text{eff}} = \left[\frac{\epsilon_e \nu_e + \epsilon_p \nu_p}{\epsilon} \right] \quad (1)$$

where $\epsilon_e = \sigma/E$ and $\epsilon_p = \epsilon - \epsilon_e$. Values of $E = 170.2$ GPa, $G = 64.4$ GPa, and $\nu_e = 0.321$, determined from the averages of all measured values of Young's and shear moduli were used in computing ν_{eff} . A value of 0.5 was assumed for ν_p . For the seven tests performed with $\lambda = \infty$ (torsional loading only), a value of 0.5 was assumed for ν_{eff} . For axial-torsional loading, the von Mises equivalent stresses and strains were determined by:

$$\epsilon_{\text{eq}} = \sqrt{\epsilon^2 + \frac{3}{4} \frac{\gamma^2}{(1 + \nu_{\text{eff}})^2}} \quad (2)$$

$$\sigma_{\text{eq}} = \sqrt{\sigma^2 + 3\tau^2} \quad (3)$$

The maximum shear stress and maximum engineering shear strain (Tresca stresses and strains) within a given cycle of loading for the axial-torsional tests were determined according to:

$$\gamma_{\text{max}} = \sqrt{(1 + \nu_{\text{eff}})^2 \epsilon^2 + \gamma^2} \quad (4)$$

$$\tau_{\max} = \frac{1}{2} \sqrt{\sigma^2 + 4\tau^2} \quad (5)$$

The maximum and minimum of these calculated values were stored and used to calculate the range and amplitude of each variable (this was done to prevent any bias due to mean stresses or strains). The sign (positive or negative) of each of the calculated values was determined by the sign of quantity that had the larger absolute magnitude. The results of these computations for the in-phase experiments are shown in figures 15 (von Mises) and 16 (Tresca). Out-of-phase test results are shown in figures 17 (von Mises) and 18 (Tresca). In the von Mises equivalent stress-strain figures, a curve representing the Ramberg-Osgood equation fit to the cyclic axial data ($\lambda = 0$) is also plotted. In the maximum shear stress versus maximum engineering shear strain figures, a curve representing the Ramberg-Osgood equation fit to the cyclic torsional data ($\lambda = \infty$) is shown. In all four plots both the cyclic axial ($\lambda = 0$) and cyclic torsional ($\lambda = \infty$) data are also displayed. Some axial strain ratchetting¹ was observed in the torsional experiments ($\lambda = \infty$) but it was not used to compute the von Mises or Tresca strains.

The Ramberg-Osgood stress-strain curve obtained from the cyclic axial data seems to represent the in-phase axial-torsional data better than the maximum shear stress—maximum engineering shear strain curve obtained from the cyclic torsional data. Both the von Mises equivalent stress-strain curve and the maximum shear stress—maximum engineering shear strain curve under estimate the cyclic hardening in the out-of-phase axial-torsional tests where $\phi = 90^\circ$. Two out-of-phase axial-torsional tests with $\phi = 90^\circ$ were conducted with sinusoidal waveforms also at a frequency of 0.1 Hz. The cyclic hardening in these tests was similar to the cyclic hardening in tests conducted with triangular waveforms (figs. 17 and 18), indicating that the effect of waveform (or small differences in strain rate) is not significant for Haynes 188 at 760 °C.

Table III contains constants for a Ramberg-Osgood type of cyclic stress-strain relation for the various loading conditions. The forms of these relations are:

$$\epsilon = \frac{\sigma}{E} + \left[\frac{\sigma}{K'} \right]^{1/n'} \quad \text{for the axial stress-strain relation}$$

or

$$\gamma = \frac{\tau}{G} + \left[\frac{\tau}{K_t'} \right]^{1/n_t'} \quad \text{for the shear stress-strain relation} \quad (6)$$

These constants were determined in a previous study (ref. 18) by performing linear least-squares fits to the logarithms of the near half-life stress amplitudes versus the logarithms of the near half-life inelastic strain amplitudes for each of the loading conditions listed in table III. The axial and shear stresses corresponding to the axial and engineering shear strains of 0.5 percent are also listed in table III. In both

¹Similar axial strain ratchetting has been observed under torsional loading by several researchers (refs. 14 to 17). In the majority of the torsional tests ($\lambda = \infty$) on Haynes 188 at 760 °C, the mean axial ratchetting strain was positive and increased in magnitude with the number of cycles. However, for all the torsional experiments, the magnitude of the mean axial ratchetting strain near half-life was relatively small compared to the amplitude of the imposed engineering shear strain. Therefore, the axial ratchetting strain was not used in computing the von Mises and Tresca strains for the torsional experiments.

the axial and shear cases, cyclic stresses are lower under in-phase loading ($\lambda = 1.73$, $\phi = 0^\circ$), and higher under out-of-phase loading ($\lambda = 1.73$, $\phi = 90^\circ$) than the stresses corresponding to the individual axial ($\lambda = 0$) or torsional ($\lambda = \infty$) loading cases.

DISCUSSION

The cycle dependent hardening rate, as indicated by the normalized stress values for the in-phase tests (figs. 7 and 8), seems to be independent of any nonzero proportionality constant, λ . However the normalized stress range in the axial ($\lambda = 0$) test exhibited a slightly higher cycle dependent hardening rate than the three in-phase tests. Similar behavior was not observed in the normalized shear stress ranges. The reason for this difference in the axial and torsional hardening rates of the in-phase tests is not apparent at present. In the out-of-phase tests, both the axial and shear stress ranges exhibited similar cycle dependent hardening patterns.

It can be seen in figures 11 to 14 that the phase angle, ϕ , between the axial and engineering shear strain command waveforms has a substantial effect on the near half-life kinematic hardening behavior. The widths of both the axial and torsional hysteresis loops decrease markedly with each 30° increment of phase angle. This can also be observed in figures 3 to 6, 9, and 10 which show the decrease in the widths of the hysteresis loops and the corresponding increase in the axial and shear stress ranges as the phase angle increases from 0° to 90° . Other researchers have reported similar behavior under out-of-phase axial-torsional loading (refs. 2, 4, 7, and 9). The additional hardening that occurs in the out-of-phase axial-torsional loading is attributable to crystallographic slip in multiple directions, which is caused by the rotation of the principal axes that occurs in out-of-phase loading (refs. 2, 9, and 19).

The von Mises criterion is a good estimator of the cyclic in-phase deformation behavior of Haynes 188 at 760°C . As can be seen in figure 15, all of the in-phase data fall on or just above the Ramberg-Osgood fit to the cyclic axial data ($\lambda = 0$). The torsional ($\lambda = \infty$) von Mises equivalent data show the largest deviation from the Ramberg-Osgood fit with as much as a 10 percent higher stress amplitude at the same equivalent strain amplitude. The maximum shear stress-strain, or Tresca approach, however, almost always over estimates the amount of cyclic hardening in the in-phase and axial experiments (fig. 16). In the worst instance, the axial maximum shear stress amplitude is over estimated by 18 percent.

Both the von Mises and the Tresca approaches fail to adequately account for the extra hardening observed in the out-of-phase axial-torsional experiments, especially those with a phase angle of 90° (figs. 17 and 18). The 90° out-of-phase experiments exhibit as much as 20 percent more hardening than the Ramberg-Osgood fit to the cyclic axial data and as much as 15 percent more hardening than that estimated by the maximum shear stress-strain or Tresca approach. Kanazawa et al. (ref. 2) accounted for the additional hardening in the sinusoidal waveform, out-of-phase, axial-torsional experiments on 1 percent Cr-Mo-V steel by using a rotation factor, which is a ratio of the shear strain range at 45° from the maximum shear plane to the maximum shear strain range. This factor was an attempt to account for the movement of dislocations within and across multiple crystallographic slip systems in the material. They were able to correlate both the in- and out-of-phase cyclic deformation data to within the same scatter band by using the rotation factor in conjunction with the maximum shear stress-strain (Tresca) approach. For Haynes 188 at 760°C , the von Mises equivalent stress-strain curve, at least for the in-phase data, appears to represent the cyclic deformation data better than the maximum shear stress-strain method. Therefore, a method based on the von Mises approach, with appropriate flow and hardening rules to account for the phase angle dependent hardening, might be able to estimate the additional hardening observed in the out-of-phase tests.

CONCLUSIONS

The cyclic deformation behavior of a wrought cobalt-base superalloy, Haynes 188, has been investigated at 760 °C under various axial-torsional loading conditions. The following conclusions were drawn from the study of hysteresis loops and cyclic hardening behaviors under different loading conditions.

1. Under in-phase (proportional) loading, the ratio of the imposed engineering shear to axial strain amplitudes had little or no effect on the relative amounts of cycle dependent hardening in either the axial or shear directions.
2. In out-of-phase (nonproportional) loading, for a given ratio of engineering shear to axial strain amplitudes and phase angles ranging from 0° to 90°, similar cycle dependent hardening trends were observed for the axial and shear stress ranges. However, on an absolute basis, the largest stresses were observed when the phase angle was 90° and the smallest stresses were observed when the phase angle was 0°.
3. The amount of hardening exhibited by Haynes 188 at 760 °C and the shapes of the axial and torsional hysteresis loops under out-of-phase axial-torsional loading were directly dependent on the phase angle between the axial and engineering shear strain waveforms.
4. The equivalent stress-strain curve (von Mises) estimated the cyclic stress response of Haynes 188 at 760 °C to within 10 percent under in-phase (proportional) axial-torsional loading. However, the von Mises equivalent stress-strain criterion underestimated the out-of-phase (nonproportional) cyclic stress response by as much as 20 percent.
5. The maximum shear stress-strain (Tresca) criteria for Haynes 188 at 760 °C overestimated the cyclic in-phase axial-torsional stress response by as much as 18 percent and underestimated the cyclic out-of-phase axial-torsional stress response by as much as 15 percent.
6. When multiaxial loading conditions exist in a structure, the use of either the von Mises or the Tresca criterion to estimate the cyclic deformation behavior does not always yield the actual cyclic deformation behavior of the material, especially under out-of-phase loading.

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TABLE I.—AXIAL-TORSIONAL TEST MATRIX FOR
HAYNES 188 AT 760 °C

		λ				
		0	0.86	1.73	3.46	∞
ϕ	0°	7	2	6	2	7
	30°	-	-	1	-	-
	60°	-	-	2	-	-
	90°	-	-	9 ^a	-	-

^aTwo tests were performed with sinusoidal strain command waveforms.

TABLE II.—MAXIMUM AND MINIMUM STRAINS AND STRESSES IN THE NEAR HALF-LIFE AXIAL AND TORSIONAL
HYSTERESIS LOOPS

[$\lambda = 1.73$.]

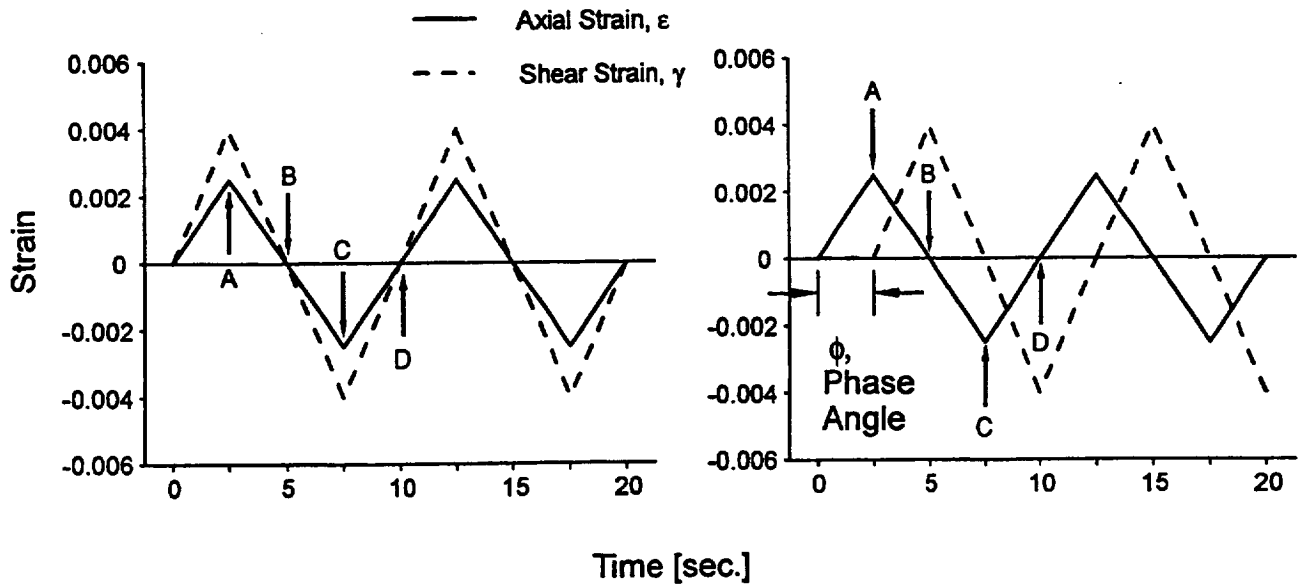
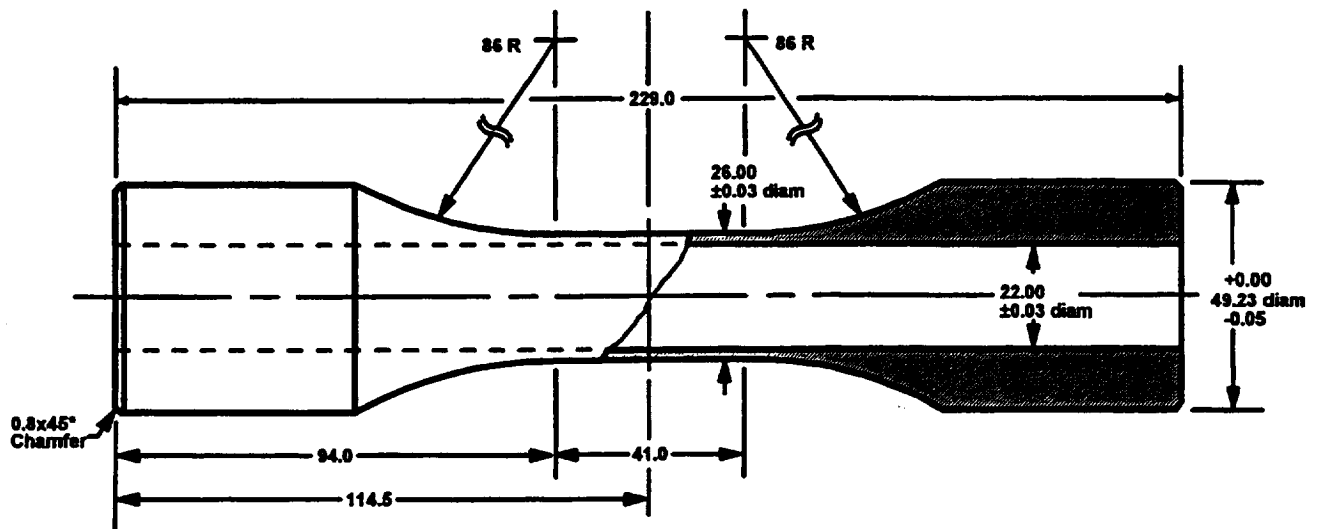
ϕ	N	N_f	Axial strain, ϵ , percent		Axial stress, σ , MPa		Engineering shear strain, γ , percent		Shear stress, τ , MPa	
			Maximum	Minimum	Maximum	Minimum	Maximum	Minimum	Maximum	Minimum
0°	3000	6261	0.21	-0.20	287	-279	0.35	-0.34	163	-168
30°	6000	12136	0.19	-0.20	277	-309	0.35	-0.35	186	-171
60°	6000	11564	0.19	-0.19	313	-310	0.35	-0.35	188	-187
90°	8000	16003	0.19	-0.20	345	-329	0.34	-0.34	211	-204

TABLE III.—RAMBERG-OSGOOD CONSTANTS FOR AXIAL AND SHEAR CYCLIC
STRESS-STRAIN CURVES UNDER VARIOUS LOADING CONDITIONS

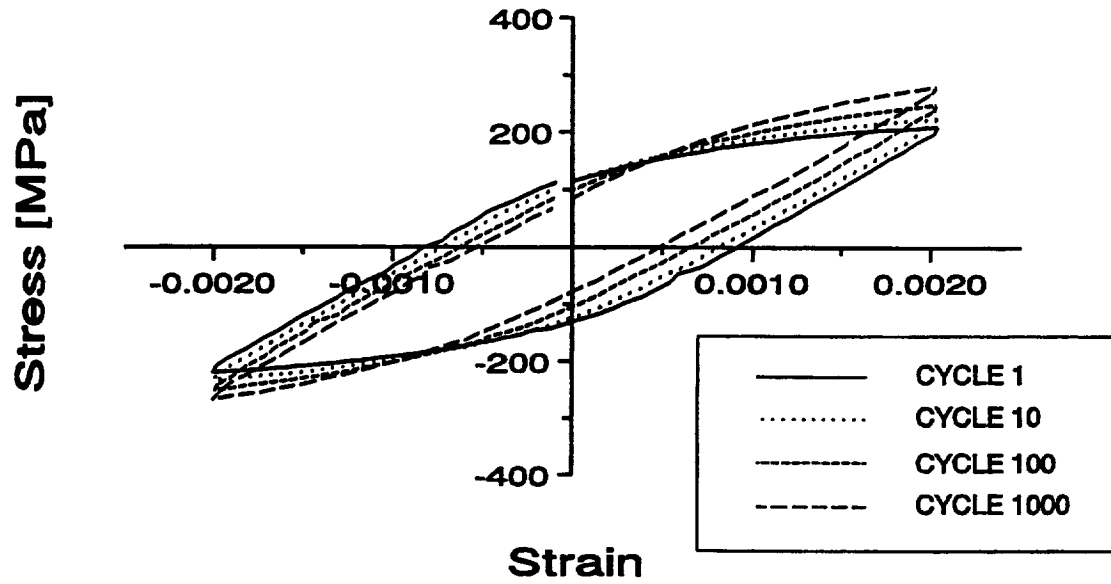
MATERIAL: HAYNES 188 AT 760 °C

Loading parameters		Ramberg-Osgood constants ^a				Stress at 0.5 percent strain	
ϕ	λ	K' , MPa	n'	K'_t , MPa	n'_t	σ , MPa	τ , MPa
0°	0	891	0.113	-----	-----	450	-----
0°	∞	-----	-----	589	0.142	-----	232
0°	1.73	1272	0.259	604	0.262	290	131
90°	1.73	2571	0.238	1247	0.230	563	256

^aFrom reference 18.



Axial Hysteresis Loop



Torsional Hysteresis Loop

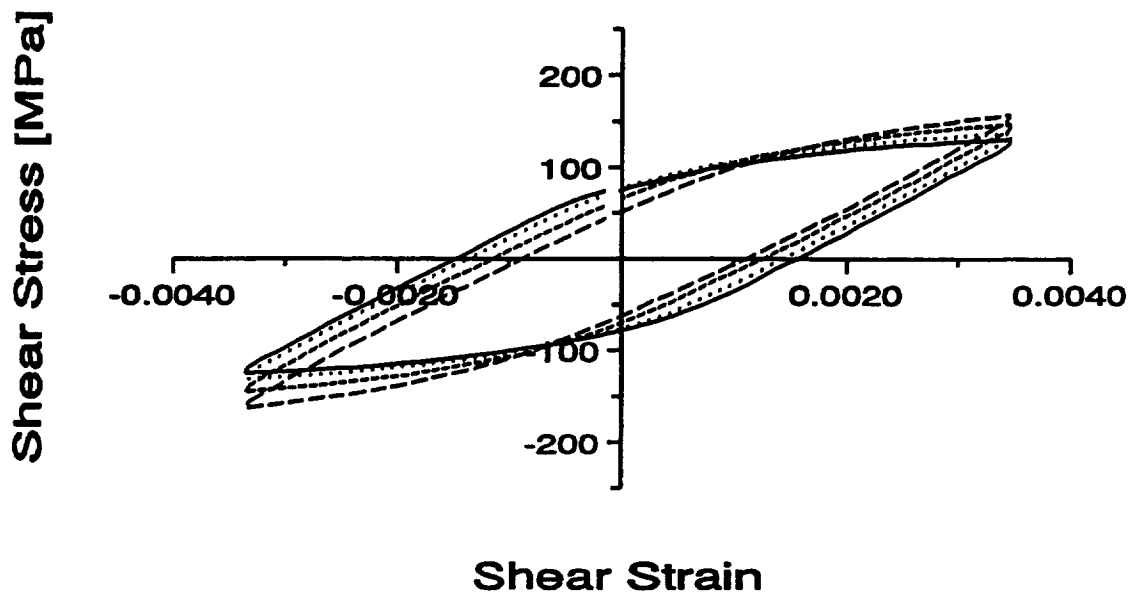


Figure 3.—Evolution of axial and torsional hysteresis loops, $\lambda = 1.73$, $\theta = 0^\circ$.

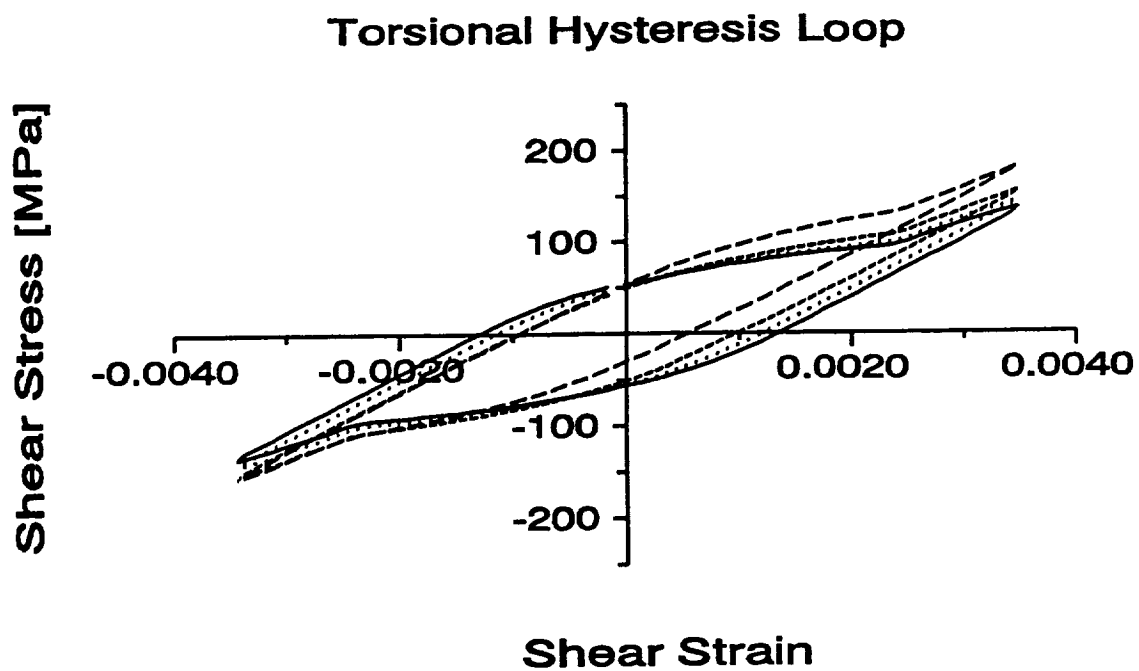
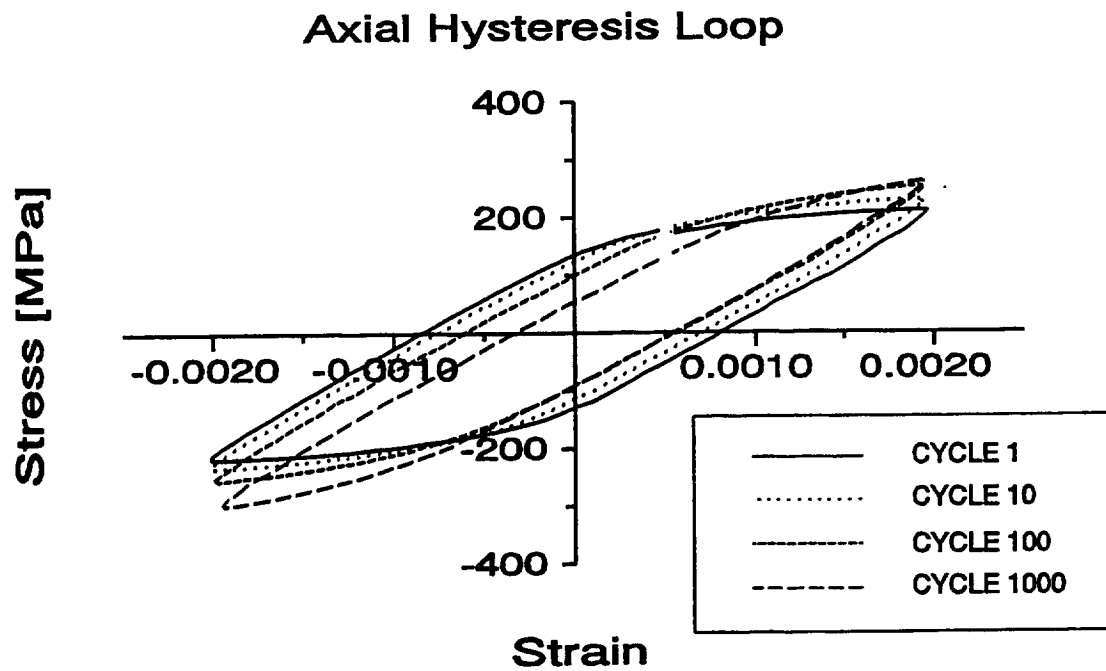
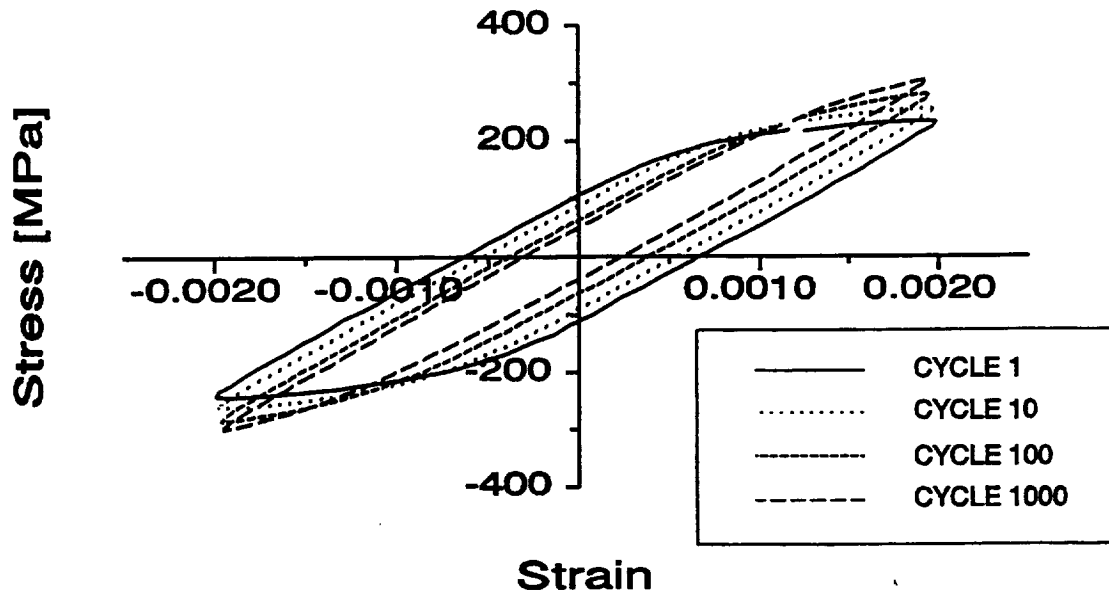


Figure 4.—Evdution of axial and torsional hysteresis loops, $\lambda = 1.73$, $\theta = 30^\circ$.

Axial Hysteresis Loop



Torsional Hysteresis Loop

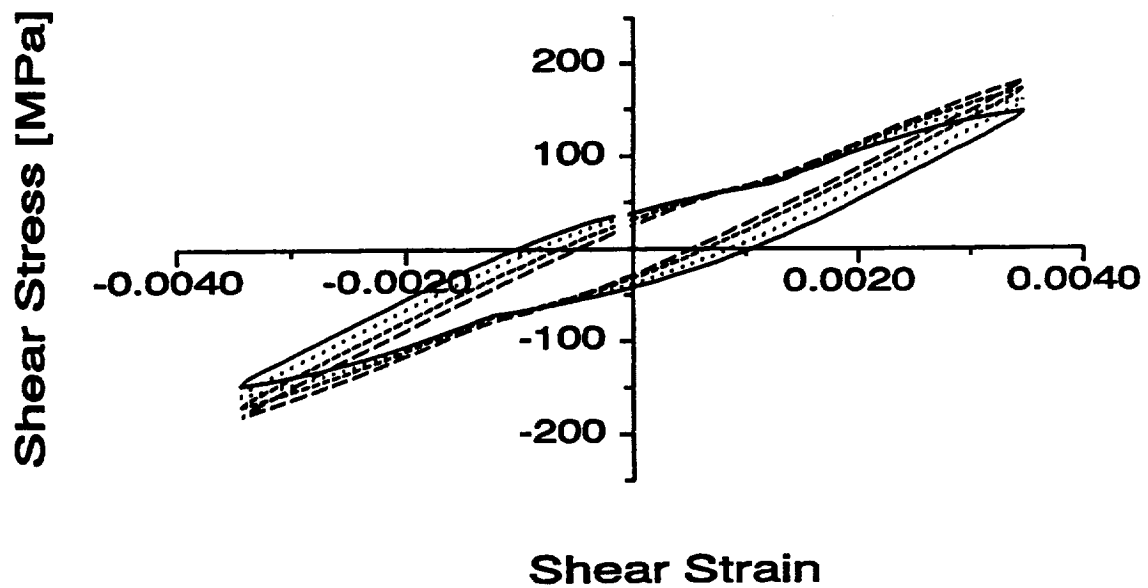
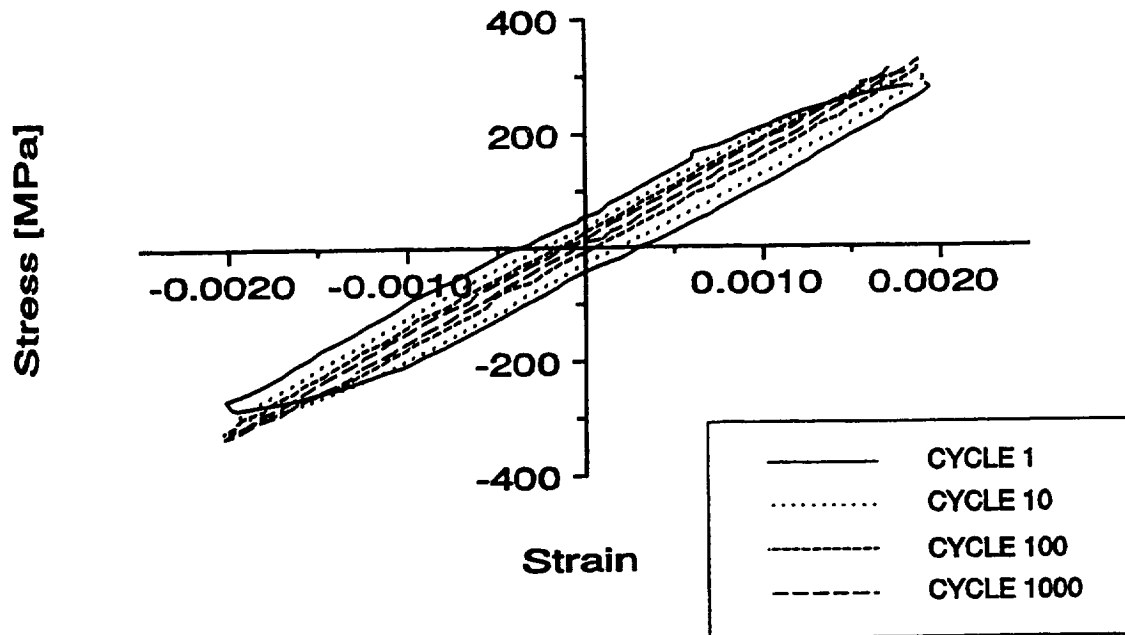


Figure 5.—Evolution of axial and torsional hysteresis loops, $\lambda = 1.73$, $\theta = 60^\circ$.

Axial Hysteresis Loop



Torsional Hysteresis Loop

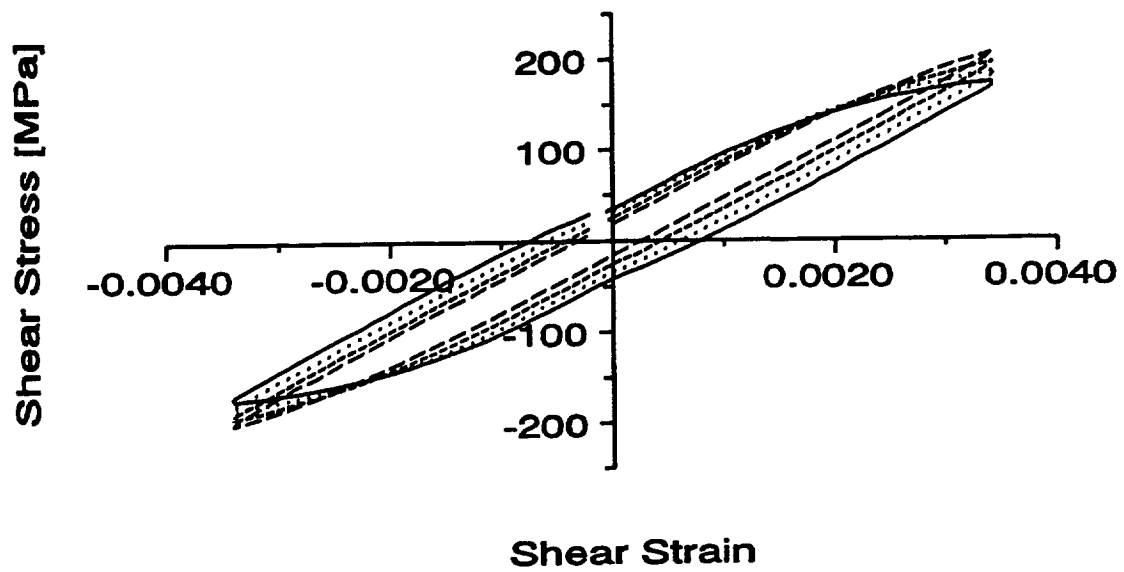


Figure 6.—Evolution of axial and torsional hysteresis loops, $\lambda = 1.73$, $\theta = 90^\circ$.

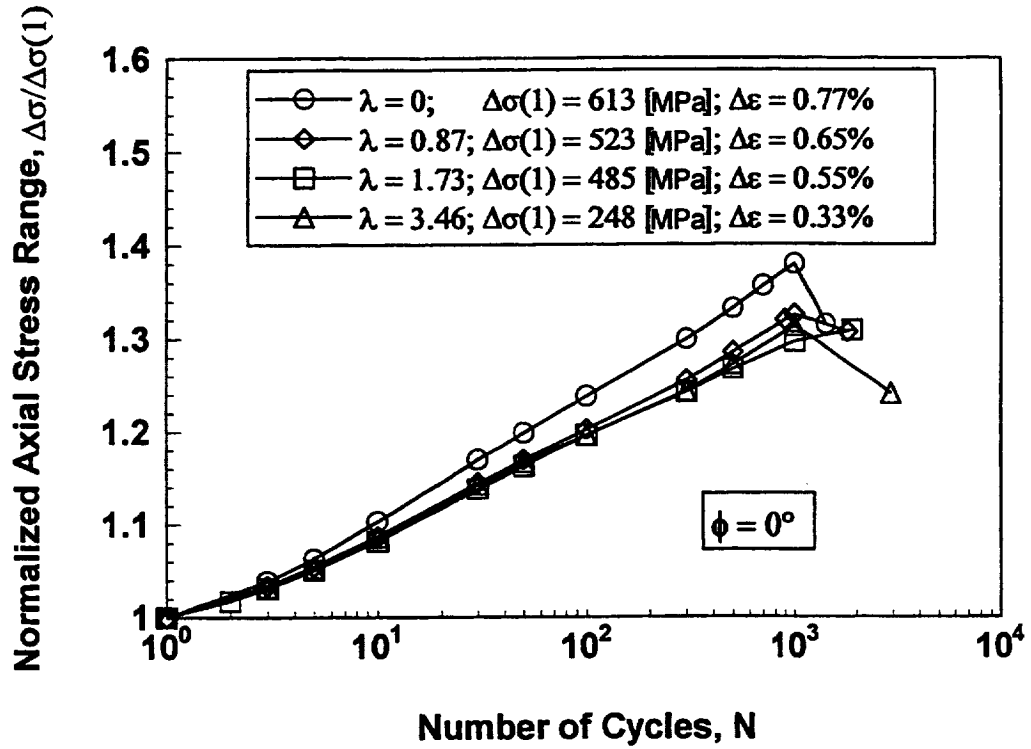


Figure 7.—Cyclic variation of the normalized (to first cycle axial stress range) axial stress range of in-phase experiments.

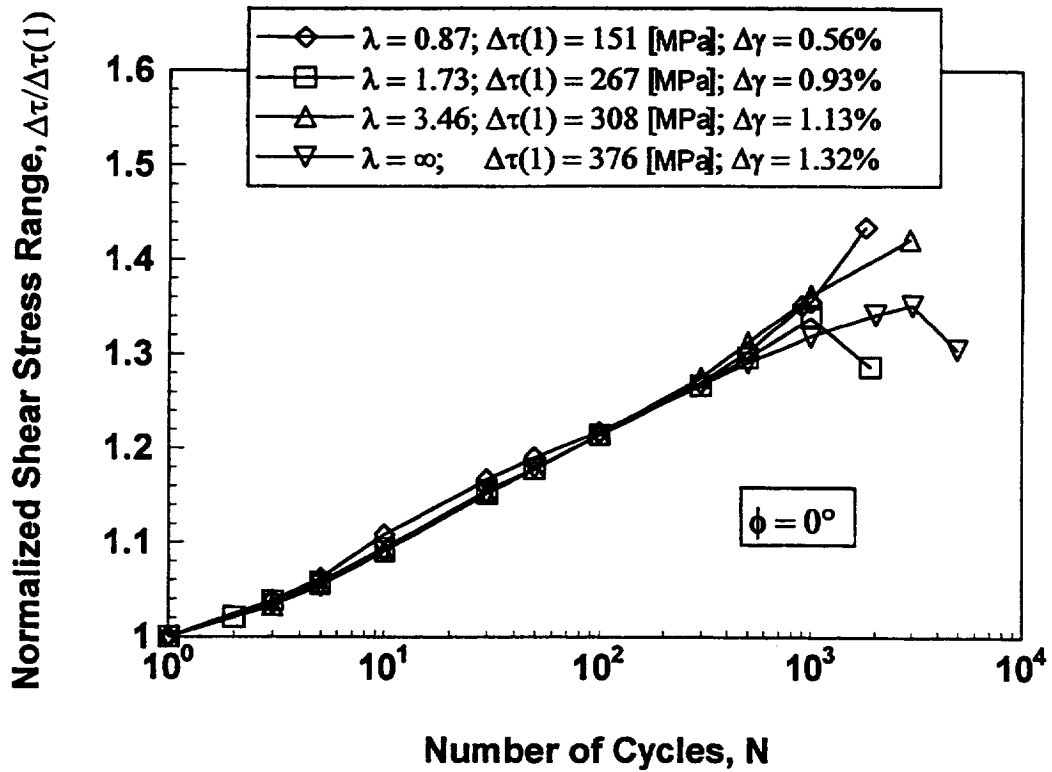


Figure 8.—Cyclic variation of the normalized (to first cycle shear stress range) shear stress range of in-phase experiments.

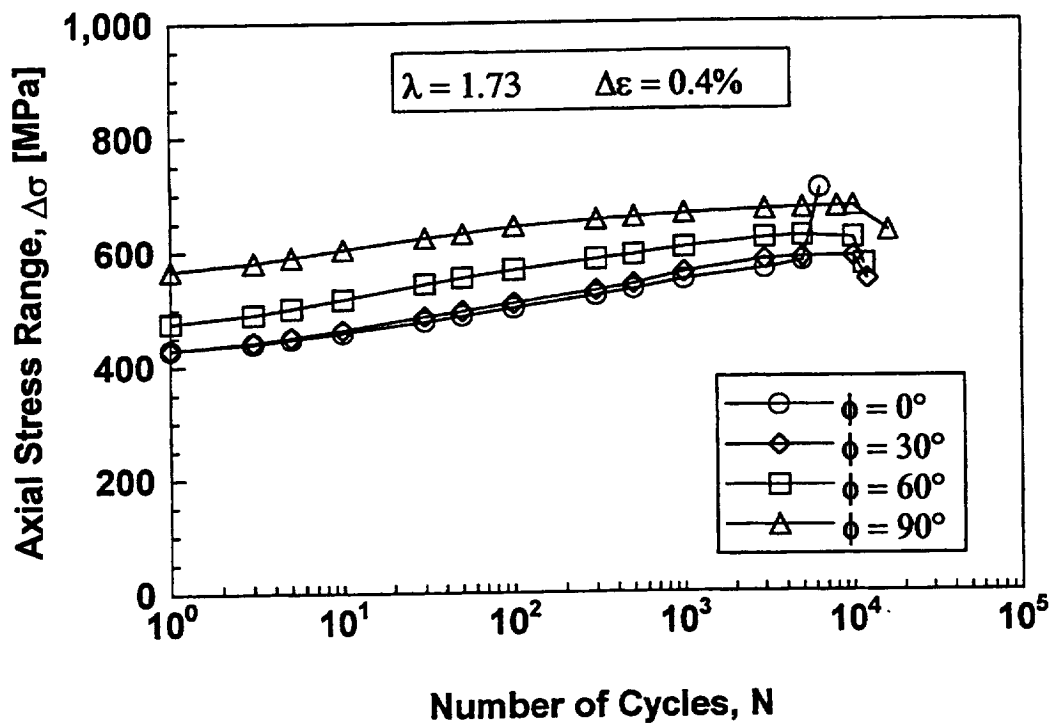


Figure 9.—Cyclic variation of axial stress range for out-of-phase experiments.

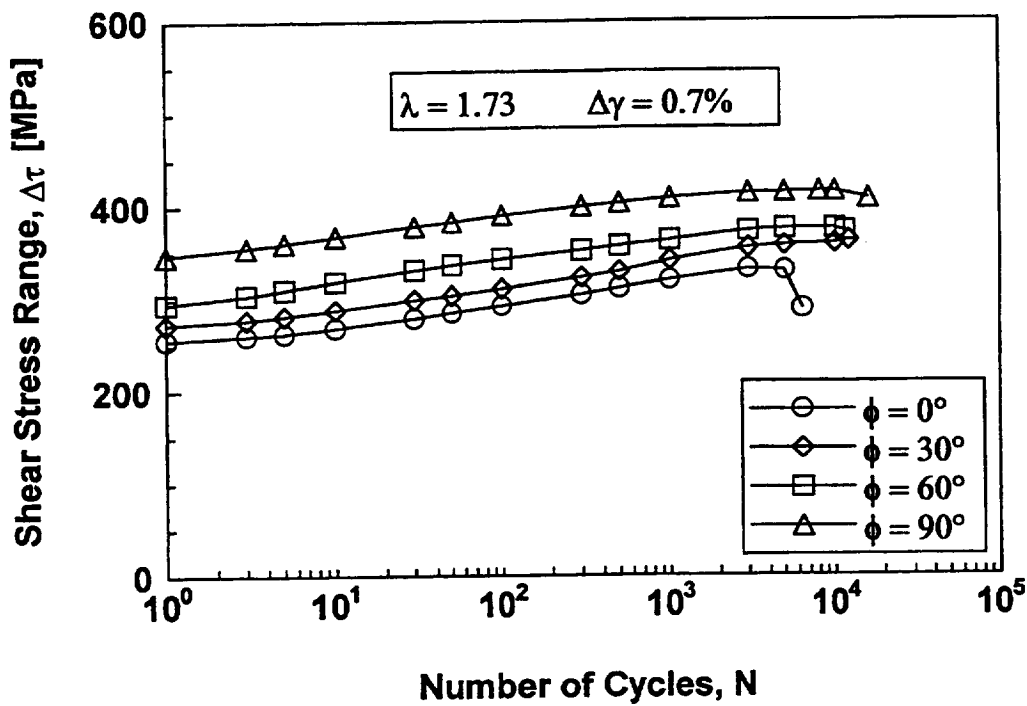


Figure 10.—Cyclic variation of shear stress range for out-of-phase experiments.

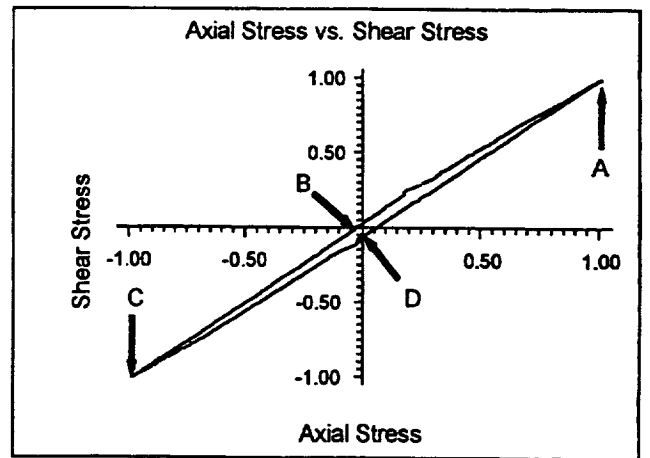
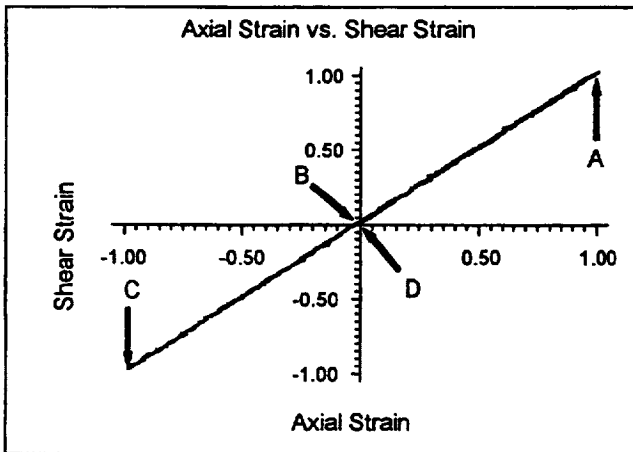
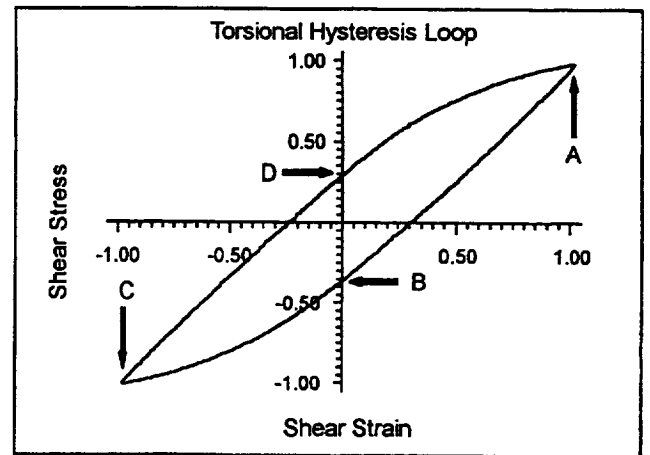
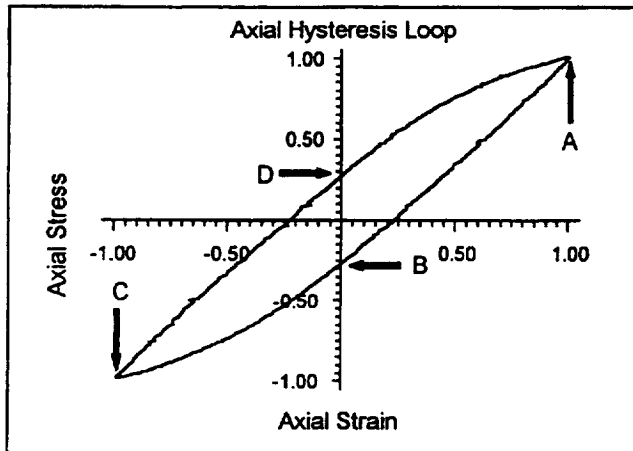


Figure 11.—Normalized loops, $\lambda = 1.73$, $\theta = 0^\circ$; axial hysteresis loop, torsional hysteresis loop, axial strain versus engineering shear strain, and axial stress versus shear stress.

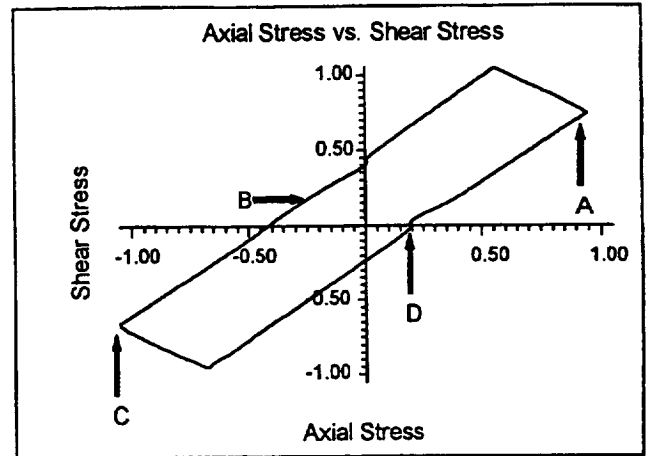
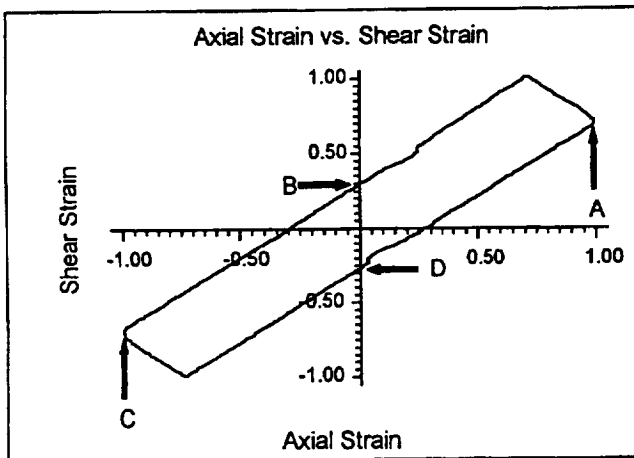
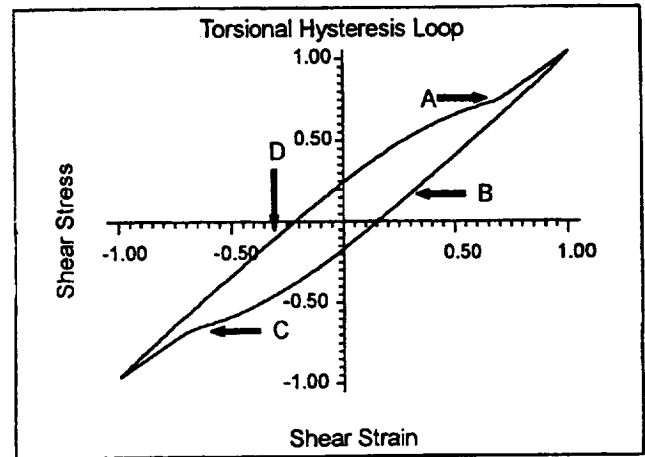
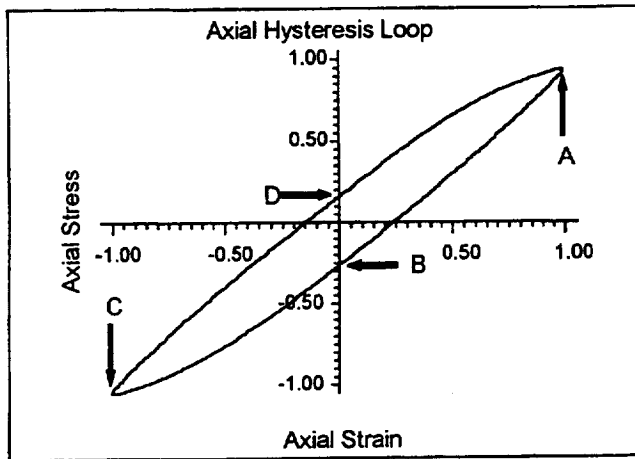


Figure 12.—Normalized loops, $\lambda = 1.73$, $\theta = 30^\circ$; axial hysteresis loop, torsional hysteresis loop, axial strain versus engineering shear strain, and axial stress versus shear stress.

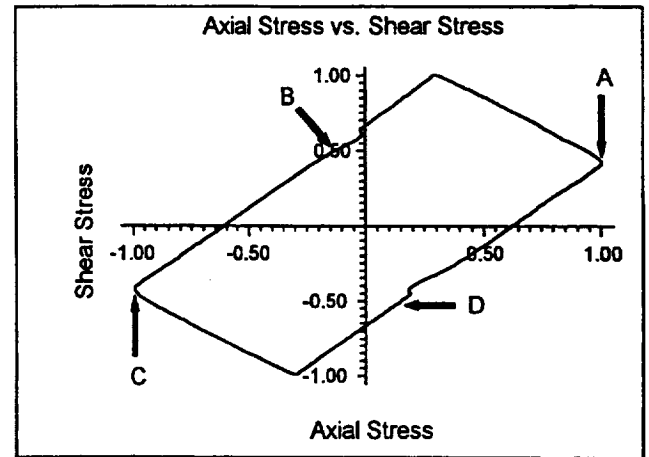
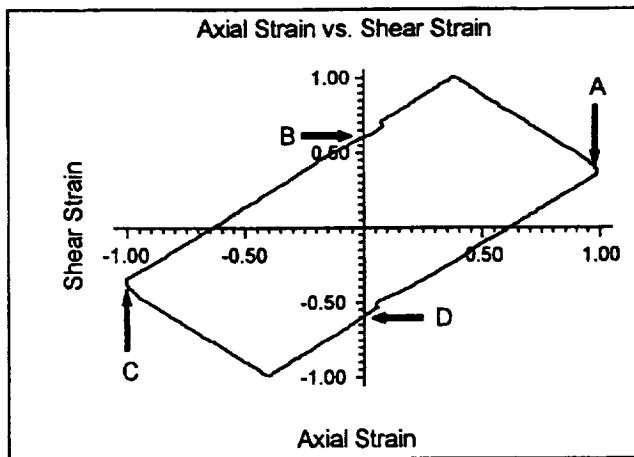
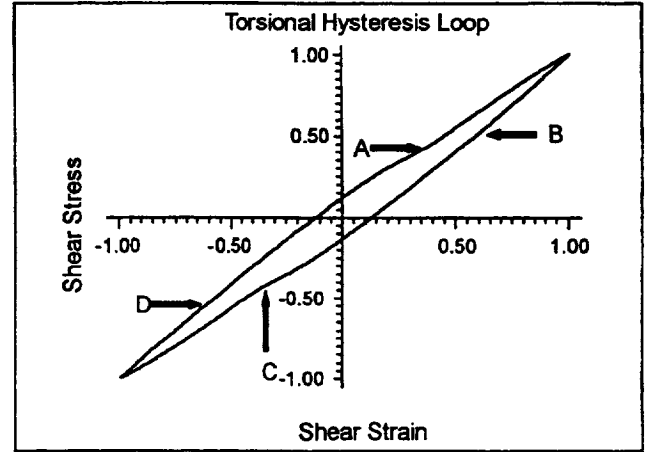
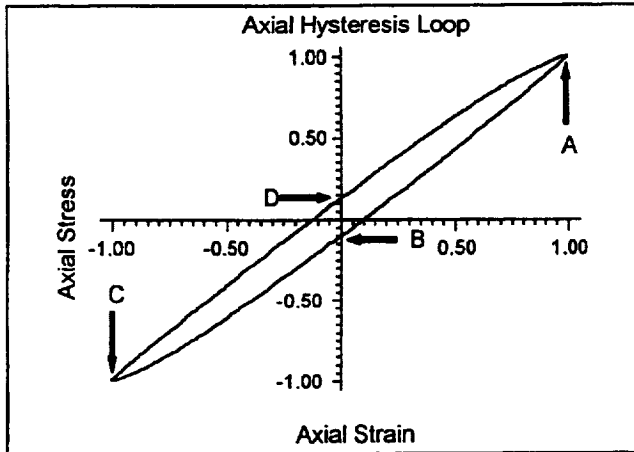


Figure 13.—Normalized loops, $\lambda = 1.73$, $\theta = 60^\circ$; axial hysteresis loop, torsional hysteresis loop, axial strain versus engineering shear strain, and axial stress versus shear stress.

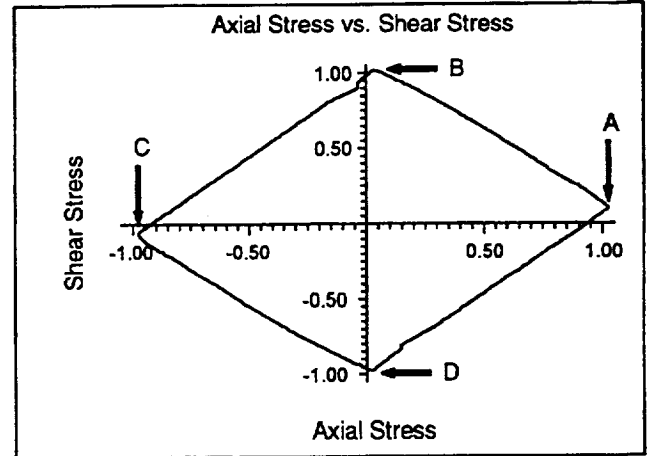
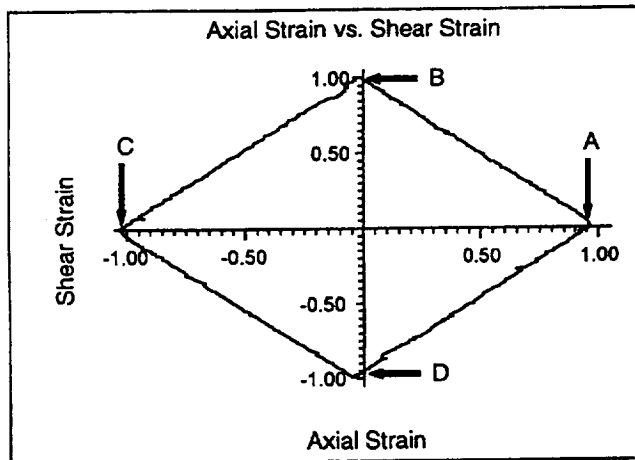
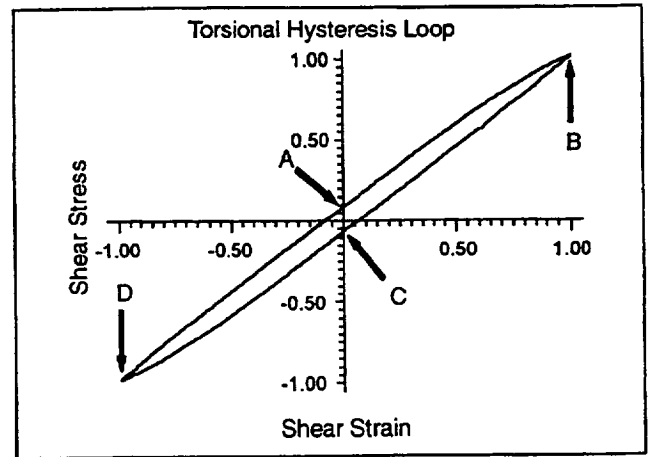
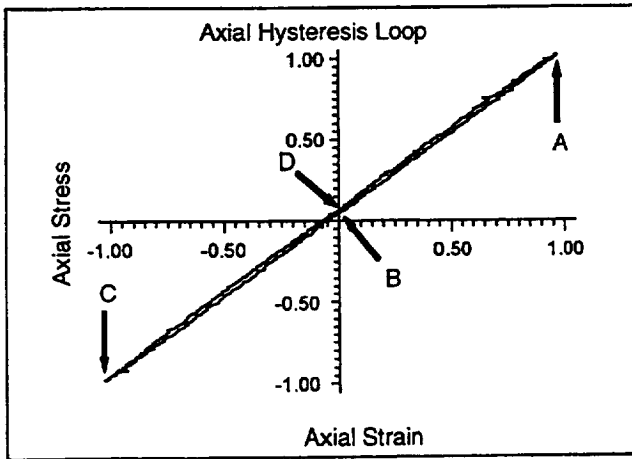


Figure 14.—Normalized loops, $\lambda = 1.73$, $\theta = 90^\circ$; axial hysteresis loop, torsional hysteresis loop, axial strain versus engineering shear strain, and axial stress versus shear stress.

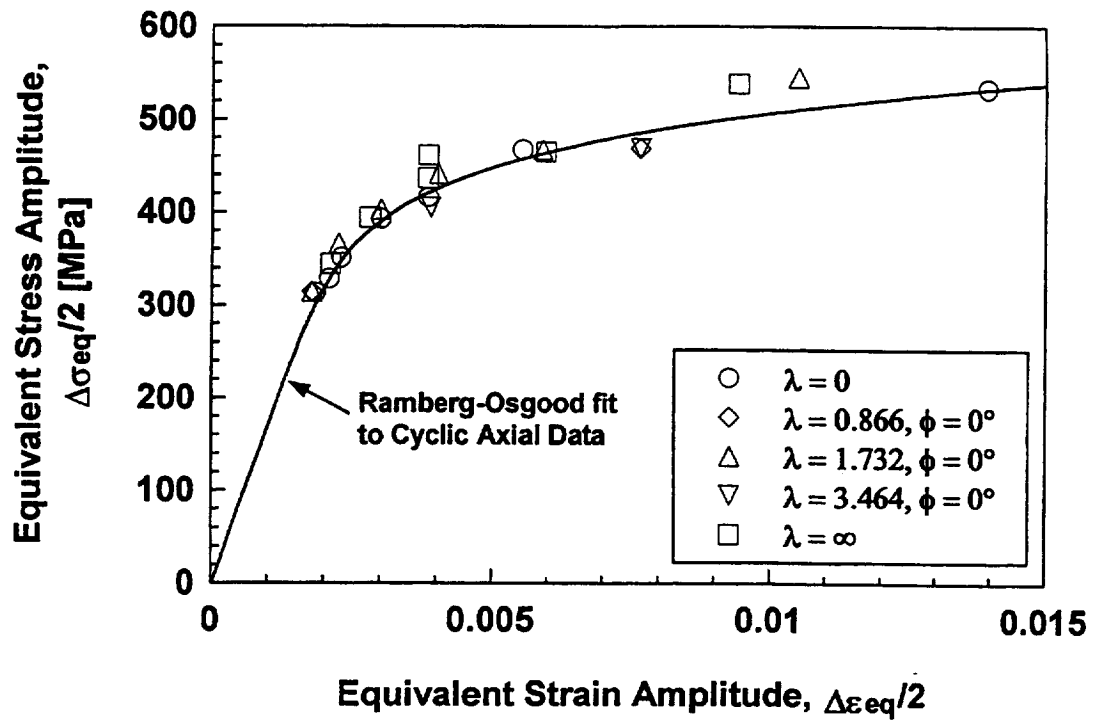


Figure 15.—Equivalent stress-strain (von Mises) data: In-phase experiments.

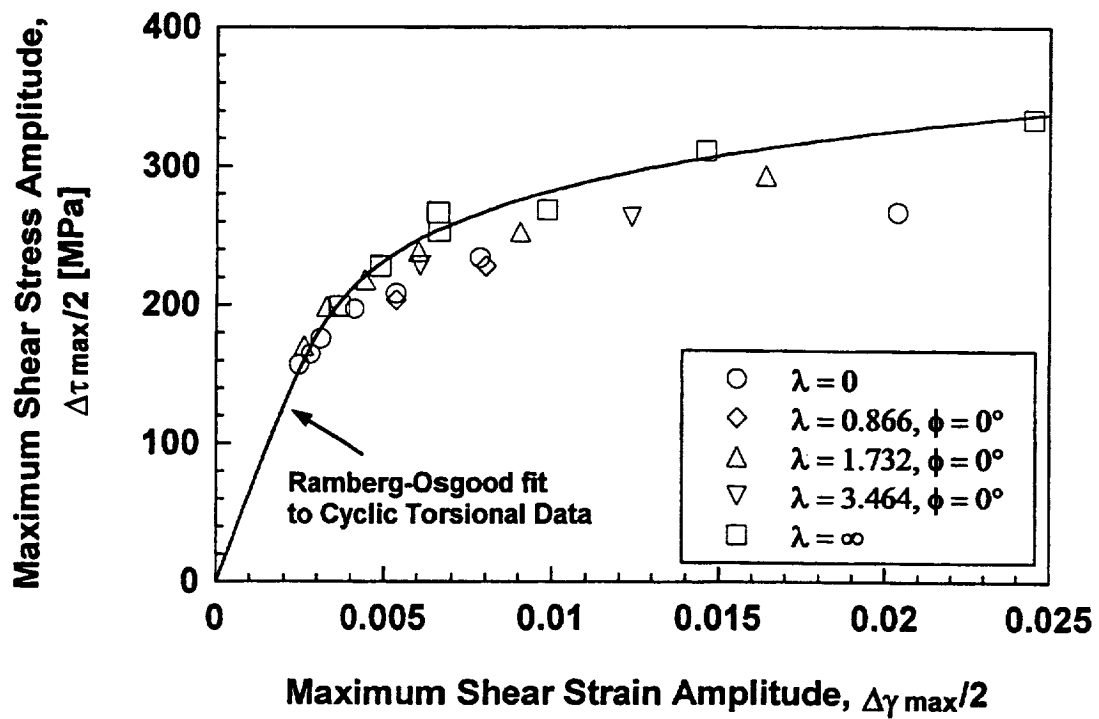


Figure 16.—Maximum shear stress strain (Tresca) data: In-phase experiments.

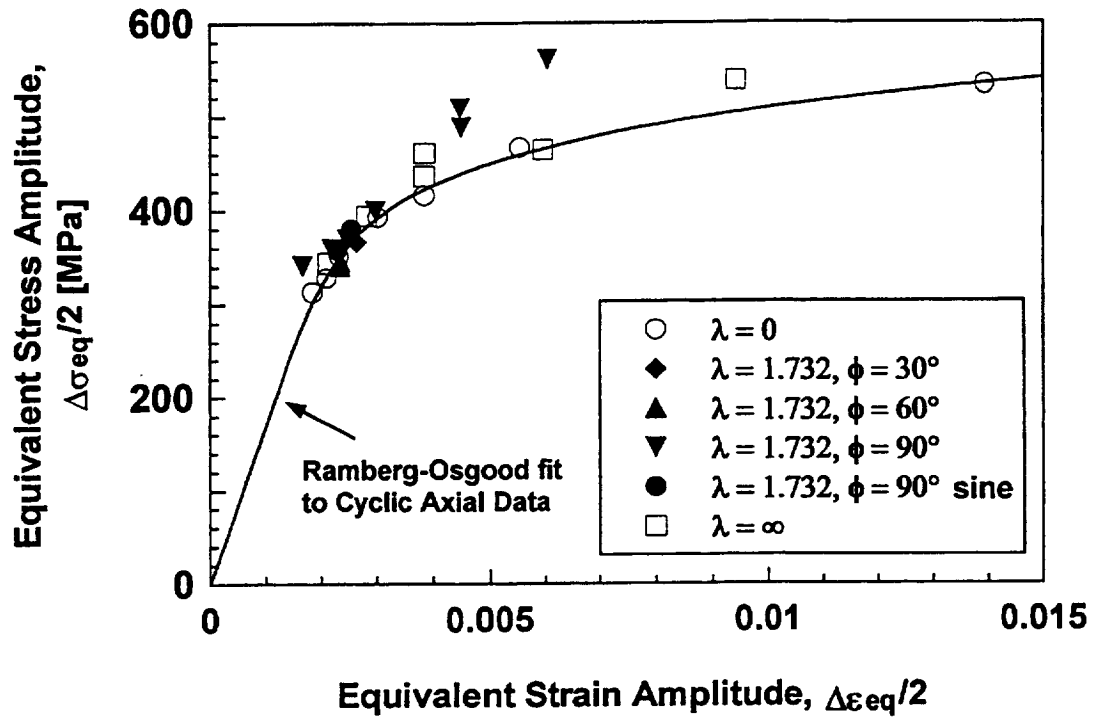


Figure 17.—Equivalent stress-strain (von Mises) data: Out-of-phase experiments.

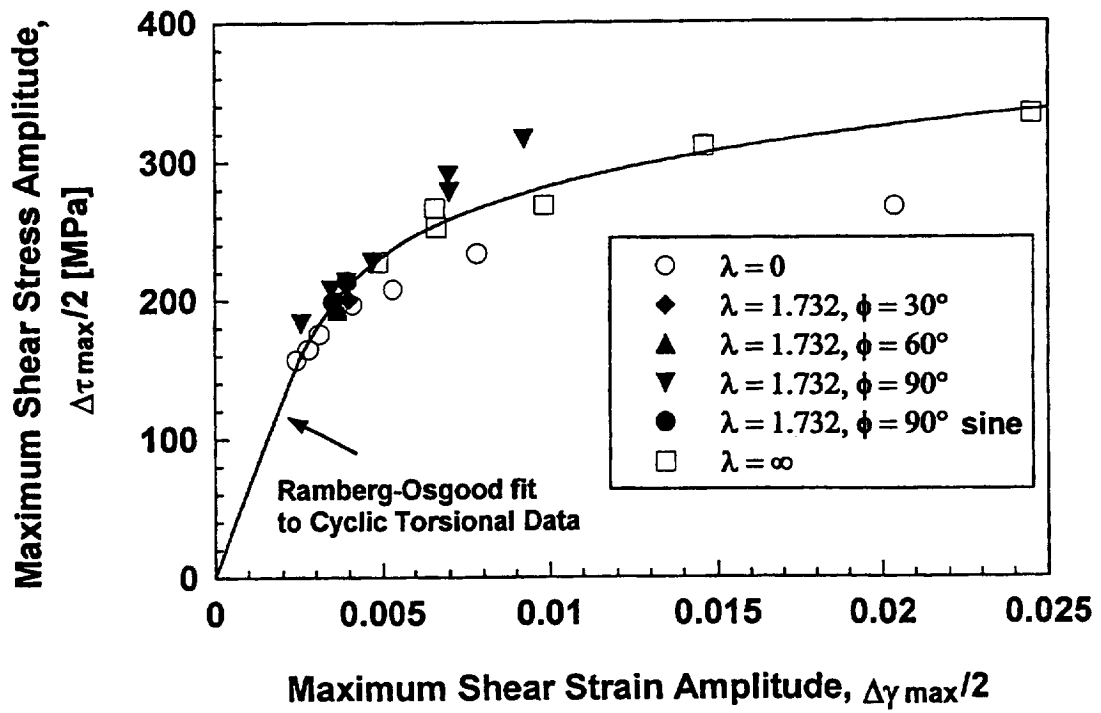


Figure 18.—Maximum shear stress strain (Tresca) data: Out-of-phase experiments.

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13. ABSTRACT (Maximum 200 words) Multiaxial loading, especially at elevated temperature, can cause the inelastic response of a material to differ significantly from that predicted by simple flow rules, i.e., von Mises or Tresca. To quantify some of these differences, the cyclic, high-temperature, deformation behavior of a wrought cobalt-base superalloy, Haynes 188, is investigated under combined axial and torsional loads. Haynes 188 is currently used in many aerospace gas turbine and rocket engine applications, e.g., the combustor liner for the T800 turboshaft engine for the RAH-66 Comanche helicopter and the liquid oxygen posts in the main injector of the space shuttle main engine. The deformation behavior of this material is assessed through the examination of hysteresis loops generated from a biaxial fatigue test program. A high-temperature axial, torsional, and combined axial-torsional fatigue data base has been generated on Haynes 188 at 760 °C. Cyclic loading tests have been conducted on uniform gauge section tubular specimens in a servohydraulic axial-torsional test rig. Test control and data acquisition were accomplished with a minicomputer. The fatigue behavior of Haynes 188 at 760 °C under axial, torsional, and combined axial-torsional loads, and the monotonic and cyclic deformation behaviors under axial and torsional loads, have been previously reported. In this paper, the cyclic hardening characteristics and typical hysteresis loops in the axial stress versus axial strain, shear stress versus engineering shear strain, axial strain versus engineering shear strain, and axial stress versus shear stress spaces are presented for cyclic, in-phase and out-of-phase, axial-torsional tests. For in-phase tests three different values of the proportionality constant, λ (ratio of engineering shear strain amplitude to axial strain amplitude, γ_a/ϵ_a), are examined, viz., 0.86, 1.73, and 3.46. In the out-of-phase tests, three different values of the phase angle, ϕ (between the axial and engineering shear strain waveforms), are studied, viz., 30°, 60°, and 90° with $\lambda = 1.73$. The cyclic hardening behaviors of all the tests conducted on Haynes 188 at 760 °C are evaluated using the von Mises equivalent stress-strain and the maximum shear stress-maximum engineering shear strain (Tresca) curves. Comparisons are also made between the hardening behaviors of cyclic axial, torsional, and combined in-phase ($\lambda = 1.73$ and $\phi = 0^\circ$) and out-of-phase ($\lambda = 1.73$ and $\phi = 90^\circ$) axial-torsional fatigue tests. These comparisons are accomplished through simple Ramberg-Osgood type stress-strain functions for cyclic, axial stress-strain and shear stress-engineering shear strain curves.				
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