

HZETRN: Description of a Free-Space Ion and Nucleon Transport and Shielding Computer Program

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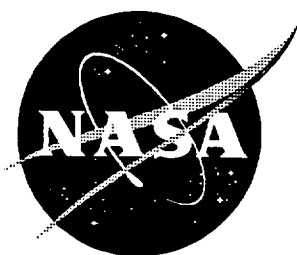
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Abstract

The high-charge-and-energy (HZE) transport computer program HZETRN is developed to address the problems of free-space radiation transport and shielding. The HZETRN program is intended specifically for the design engineer who is interested in obtaining fast and accurate dosimetric information for the design and construction of space modules and devices. The program is based on a one-dimensional space-marching formulation of the Boltzmann transport equation with a straight-ahead approximation. The effect of the long-range Coulomb force and electron interaction is treated as a continuous slowing-down process. Atomic (electronic) stopping power coefficients with energies above a few A MeV are calculated by using Bethe's theory including Bragg's rule, Ziegler's shell corrections, and effective charge. Nuclear absorption cross sections are obtained from fits to quantum calculations and total cross sections are obtained with a Ramsauer formalism. Nuclear fragmentation cross sections are calculated with a semiempirical abrasion-ablation fragmentation model. The relation of the final computer code to the Boltzmann equation is discussed in the context of simplifying assumptions. A detailed description of the flow of the computer code, input requirements, sample output, and compatibility requirements for non-VAX platforms are provided.

1. Introduction

During the last 40 years, propagation of galactic ions through extended matter and determination of the origin of these ions have been the subject of many studies. Peters (ref. 1) used the one-dimensional equilibrium solution, without including ionization energy loss and radioactive decay, to show that the light ions have their origin in the breakup of heavy particles. Davis (ref. 2) showed that one-dimensional propagation is simplistic and that leakage at the galactic boundary must be taken into account. Ginzburg and Syrovatskii (ref. 3) argued that the leakage can be approximated as a superposition of nonequilibrium one-dimensional solutions. The solution to the steady-state equations was given as a Volterra equation by Gloeckler and Jokipii (ref. 4), which was solved to the first order in the fragmentation cross sections by ignoring energy loss. This provided an approximation of the first-order solution that included ionization energy loss and was only valid at relativistic energies. Lezniak (ref. 5) gave an overview of the cosmic ray propagation and derived a Volterra equation that included the ionization energy loss and evaluated only the unperturbed term. The previous discussion indicates, that for a long time, the main interest of cosmic ray physicists was to achieve first-order solutions in the fragmentation cross sections where path lengths in the interstellar space are on the order of 3 to 4 g/cm². Clearly, higher order terms cannot be ignored in accelerator or space shielding transport problems. (See refs. 6–9.) Besides this simplification, previous cosmic ray models have neglected the complicated three-dimensional nature of the fragmentation process.

Several approaches to the solution of high-energy heavy ion propagation that include ionization energy loss have been developed (refs. 6–19) during the last 20 years. All but one (ref. 6) have assumed the straight-ahead approximation and velocity-conserving fragmentation interactions. Only two (refs. 6 and 9) have incorporated energy-dependent cross sections. The approach by Curtis, Doherty, and Wilkinson (ref. 14) for a primary ion beam represented the first-generation secondary fragments as a quadrature over the collision density of the primary beam. Allkofer and Heinrich (ref. 15) used an energy multigroup method in which an energy-independent fragmentation transport approximation was applied within each energy group after which the energy group boundaries were moved according to continuous slowing-down theory. Chatterjee, Tobias, and Lyman (ref. 16) solved

the energy-independent fragment transport equation with primary collision density as a source and neglected higher order fragmentation. The primary source term extended only to the primary ion range from the boundary and the energy-independent transport solution was modified to account for the finite range of the secondary fragment ions.

Wilson (ref. 7) derived an expression for the ion transport problem to the first-order (i.e., first-collision) term and gave an analytical solution for the depth-dose relationship. The more common approximations used in solving the heavy ion transport problem were examined further by Wilson. (See ref. 6.) The effect of conservation of velocity on fragmentation and on the straight-ahead approximation was found to be negligible for cosmic ray applications. Solution methods for representation of the energy-dependent nuclear cross sections were derived. (See ref. 6.) Letaw, Tsao, and Silberberg (ref. 17) approximated the energy loss term and the ion spectra by simple forms for which energy derivatives were evaluated explicitly. The resulting ordinary differential equations in terms of position were solved analytically. This approximation results in the decoupling of motion in space and a change in energy. In Letaw's formalism, the energy shifts were replaced by an effective attenuation factor. Wilson (ref. 8) added the next higher order (i.e., second-collision) term. This term was found to be very important in describing ^{20}Ne beams at 670A MeV. The three-term expansion was modified to include the effect of energy variation of the nuclear cross sections. (See ref. 9.) The integral form of the transport equation was also used to derive a numerical marching procedure to solve the cosmic ray transport problem. (See refs. 6 and 12.) This method could accommodate the energy-dependent nuclear cross sections within the numerical procedure. Comparison of the numerical procedure with an analytical solution of a simplified problem (refs. 12 and 13) validated the solution technique to approximately 1-percent accuracy. Several solution techniques and analytical methods have also been developed for testing future numerical solutions of the transport equation. (See refs. 18 and 19.) More recently, an analytical solution for the laboratory ion beam transport problem has been derived with a straight-ahead approximation, velocity conservation at the interaction site, and energy-dependent nuclear cross sections. (See ref. 10.)

From an overview of these past developments, the applications are divided into two categories: a single-ion species with a single energy at the boundary and a broad host of elemental types with a broad continuous energy spectrum. Techniques, which will represent the spectrum over an array of energy values, require vast computer storage and computation speed to maintain sufficient energy resolution for the laboratory beam problem. In contrast, analytical methods (ref. 6), which are applied as a marching procedure (ref. 12) have similar energy resolution problems. This is a serious limitation because a final (i.e., production) high-charge-and-energy (HZE) computer code for cosmic ray shielding must be thoroughly validated by laboratory experiments; some hope exists of having a single code which can be validated in the laboratory. (See refs. 9, 10, 20, and 21.) More recently, a Green's function has been derived which has promise for a code which can be tested in the laboratory and used on space radiation protection applications. (See ref. 22.)

In this paper, the starting point is the derivation of the general Boltzmann equation. By using standard assumptions to derive the straight-ahead equation in the continuous slowing-down approximation and the assumption that heavy projectile breakup conserves velocity, the Boltzmann equation is simplified. A numerical procedure is derived with the coupling of heavy ions to the nucleon fields. Numerical stability and error propagation are discussed. The environmental model required as input to the HZE transport computer program HZETRN is briefly discussed. Atomic and nuclear models used to obtain the transport coefficients are discussed. Monte Carlo results are compared with the numerical procedures and database. Sample results for solar minimum and maximum periods are provided. Detailed descriptions of the flow of the computer code, input requirements, sample output, and compatibility requirements for non-VAX platforms are provided. This program, which is designated LAR-15225, is available through NASA's software technology transfer center COSMIC (Computer Software Management and Information Center) at 382 E. Broad Street, University of Georgia, Athens, GA 30602.

2. Derivation of Boltzmann Equation

Because the volume of any material is mostly electrons, the interaction of energetic ions passing through any material is primarily with these electrons. The cross section for the interactions of electrons is $\sigma^{at} \approx 10^{-16} \text{ cm}^2$. The long range of the nuclear Coulomb field also presents a sizable cross section of $\sigma^c \approx 10^{-19} \text{ cm}^2$ to the passing ion. Ion collisions are dominated by these two processes, but individual collisions have little effect on the passing ions.

Although most collisions in the material are Coulomb collisions with orbital electrons and nuclei, the rare nuclear reactions are of importance because of the significant energy transferred in the reaction and the generation of new energetic particles. The transfer of kinetic energy into new secondary radiations occurs through several processes such as direct knockout of nuclear constituents, resonant excitation followed by particle emission, pair production, and possible coherent effects within the nucleus. Through these processes, a single particle incident on a shield may attenuate through energy transfer to electrons of the media or generate a multitude of secondaries which cause an increase in exposure. The process that dominates depends on energy, particle type, and material composition.

The relevant transport equations are derived on the basis of conservation principles by considering a region of space filled with matter described by appropriate atomic and nuclear cross sections. In figure 1, a small portion of such a region enclosed by a sphere of radius δ is shown. The number of particles of type j leaving a surface element $\delta^2 d\vec{\Omega}$ is given as $\phi_j(\vec{x} + \delta\vec{\Omega}, \vec{\Omega}, E) \delta^2 d\vec{\Omega}$, where $\phi_j(\vec{x}, \vec{\Omega}, E)$ is the particle flux density, \vec{x} is a vector to the center of the sphere, $\vec{\Omega}$ is normal to the surface element, and E is the particle energy. The projection of the surface element through the sphere center to the opposite side of the sphere defines a flux tube through which pass a number of particles of type j given as $\phi_j(\vec{x} - \delta\vec{\Omega}, \vec{\Omega}, E) \delta^2 d\vec{\Omega}$, which would equal the number leaving the opposite face if the tube defined by the projection were a vacuum. The two numbers of particles differ by the gains and losses created by atomic and nuclear collisions as follows:

$$\begin{aligned} \phi_j(\vec{x} + \delta\vec{\Omega}, \vec{\Omega}, E) \delta^2 d\vec{\Omega} &= \phi_j(\vec{x} - \delta\vec{\Omega}, \vec{\Omega}, E) \delta^2 d\vec{\Omega} \\ &+ \delta^2 d\vec{\Omega} \int_{-\delta}^{\delta} dl \sum_k \int \sigma_{jk}(\vec{\Omega}, \vec{\Omega}', E, E') \phi_k(\vec{x} + l\vec{\Omega}, \vec{\Omega}', E') d\vec{\Omega}' dE' \\ &- \delta^2 d\vec{\Omega} \int_{-\delta}^{\delta} dl \sigma_j(E) \phi_j(\vec{x} + l\vec{\Omega}, \vec{\Omega}, E) \end{aligned} \quad (2.1)$$

where $\sigma_j(E)$ and $\sigma_{jk}(\vec{\Omega}, \vec{\Omega}', E, E')$ are the media macroscopic cross sections. The cross section $\sigma_{jk}(\vec{\Omega}, \vec{\Omega}', E, E')$ represents all those processes by which type k particles moving in direction $\vec{\Omega}'$ with energy E' produce a type j particle in direction $\vec{\Omega}$ with energy E . Note that there may be several reactions that could produce this result, and the appropriate cross sections of equation (2.1) are the inclusive ones. The second term on the right side of equation (2.1) is the source of secondary particles integrated over the total volume $2\delta(\delta^2 d\vec{\Omega})$, and the third term is the loss through nuclear reaction integrated over the same volume. The expansion of the terms of each side and retention of the terms to order δ^3 explicitly result in

$$\begin{aligned} \delta^2 d\vec{\Omega} [\phi_j(\vec{x}, \vec{\Omega}, E) + \delta \vec{\Omega} \cdot \nabla \phi_j(\vec{x}, \vec{\Omega}, E)] &= \delta^2 d\vec{\Omega} [\phi_j(\vec{x}, \vec{\Omega}, E) - \delta \vec{\Omega} \cdot \nabla \phi_j(\vec{x}, \vec{\Omega}, E) \\ &\quad + 2\delta \sum_k \int \sigma_{jk}(\vec{\Omega}, \vec{\Omega}', E, E') \phi_k(\vec{x}, \vec{\Omega}', E') d\vec{\Omega}' dE' \\ &\quad - 2\delta \sigma_j(E) \phi_j(\vec{x}, \vec{\Omega}, E)] + O(\delta^4) \end{aligned} \quad (2.2)$$

which can be divided by the cylindrical volume $2\delta(d\vec{\Omega})$ and written as

$$\vec{\Omega} \cdot \nabla \phi_j(\vec{x}, \vec{\Omega}, E) = \sum_k \int \sigma_{jk}(\vec{\Omega}, \vec{\Omega}', E, E') \phi_k(\vec{x}, \vec{\Omega}', E') d\vec{\Omega}' dE' - \sigma_j(E) \phi_j(\vec{x}, \vec{\Omega}, E) + O(\delta) \quad (2.3)$$

for which the last term $O(\delta)$ approaches zero in the limit as $\delta \rightarrow 0$. Equation (2.3) is recognized as the time-independent form of the Boltzmann equation for a dual-species tenuous gas. Atomic collisions preserve the identity of the particle, and both terms on the right side of equation (2.3) contribute. The differential cross sections for the atomic processes have the approximate form

$$\sigma_{jk}^{\text{at}}(\vec{\Omega}, \vec{\Omega}', E, E') = \sum_n \sigma_{jn}^{\text{at}}(E') \delta(\vec{\Omega} \cdot \vec{\Omega}' - 1) \delta_{jk} \delta(E + \epsilon_n - E') \quad (2.4)$$

where n labels the electronic excitation levels and ϵ_n represents the corresponding excitation energies, which are small (1 to 100 eV) compared with the particle energy E . The atomic terms can then be written as

$$\begin{aligned} \sum_k \int \sigma_{jk}^{\text{at}}(\vec{\Omega}, \vec{\Omega}', E, E') \phi_k(\vec{x}, \vec{\Omega}', E') d\vec{\Omega}' dE' - \sigma_j^{\text{at}}(E) \phi_j(\vec{x}, \vec{\Omega}, E) \\ = \sum_n \sigma_{jn}^{\text{at}}(E + \epsilon_n) \phi_j(\vec{x}, \vec{\Omega}, E + \epsilon_n) - \sigma_j^{\text{at}}(E) \phi_j(\vec{x}, \vec{\Omega}, E) \\ \approx \sum_n \sigma_j^{\text{at}}(E) \phi_j(\vec{x}, \vec{\Omega}, E) + \sum_n \epsilon_n \frac{\partial}{\partial E} [\sigma_{jn}^{\text{at}}(E) \phi_j(\vec{x}, \vec{\Omega}, E)] - \sigma_j^{\text{at}}(E) \phi_j(\vec{x}, \vec{\Omega}, E) \\ = \frac{\partial}{\partial E} [S_j(E) \phi_j(\vec{x}, \vec{\Omega}, E)] \end{aligned} \quad (2.5)$$

because the stopping power is

$$S_j(E) = \sum_n \sigma_{jn}^{\text{at}}(E) \epsilon_n \quad (2.6)$$

and the atomic cross section is

$$\sigma_j^{\text{at}}(E) = \sum_n \sigma_{jn}^{\text{at}}(E) \quad (2.7)$$

Equations (2.5)–(2.7) permit the rewriting of equation (2.3) in the usual continuous slowing-down approximation as

$$\begin{aligned} \vec{\Omega} \cdot \nabla \phi_j(\vec{x}, \vec{\Omega}, E) - \frac{\partial}{\partial E} [S_j(E) \phi_j(\vec{x}, \vec{\Omega}, E)] + \sigma_j(E) \phi_j(\vec{x}, \vec{\Omega}, E) \\ = \int \sum_k \sigma_{jk}(\vec{\Omega}, \vec{\Omega}', E, E') \phi_k(\vec{x}, \vec{\Omega}', E') d\vec{\Omega}' dE' \end{aligned} \quad (2.8)$$

where the cross section of equation (2.8) now contains only the nuclear contributions.

3. Transport Formalism

The Boltzmann equation (2.8), as derived in section 2, can be rewritten as

$$\left[\vec{\Omega} \cdot \nabla - \frac{1}{A_j} \frac{\partial}{\partial E} S_j(E) + \sigma_j(E) \right] \phi_j(\vec{x}, \vec{\Omega}, E) = \sum_k \int dE' d\vec{\Omega}' \sigma_{jk}(E, E', \vec{\Omega}, \vec{\Omega}') \phi_k(\vec{x}, \vec{\Omega}', E') \quad (3.1)$$

where $\phi_j(\vec{x}, \vec{\Omega}, E)$ is the flux of ions of type j with atomic mass A_j at \vec{x} with motion along $\vec{\Omega}$ and energy E in units of A MeV, $\sigma_j(E)$ is the corresponding macroscopic cross section, $S_j(E)$ is the linear energy transfer (LET), and $\sigma_{jk}(E, E', \vec{\Omega}, \vec{\Omega}')$ is the production cross section for type j particles with energy E and direction $\vec{\Omega}$ by collision of a type k particle of energy E' and direction $\vec{\Omega}'$. The term that contains $S_j(E)$ on the left side of equation (3.1) is the result of the continuous slowing-down approximation. The solutions of equation (3.1) are unique in any convex region for which the inbound flux of each particle type is specified everywhere on the boundary surface. If the boundary is given as the loci of a two-parameter vector function $\gamma(s, t)$ for which a generic point on the boundary is given by $\vec{\Gamma}$, then the boundary condition is specified by requiring the solution of equation (3.1) to meet

$$\phi_j(\vec{\Gamma}, \vec{\Omega}, E) = \psi_j(\vec{\Gamma}, \vec{\Omega}, E) \quad (3.2)$$

for each value of $\vec{\Omega}$ such that

$$\vec{\Omega} \cdot \vec{n}(\vec{\Gamma}) < 0 \quad (3.3)$$

where $\vec{n}(\vec{\Gamma})$ is the outwardly directed unit normal vector at the boundary surface at point $\vec{\Gamma}$, and ψ_j is the specified boundary condition.

The fragmentation of the projectile and target nuclei is represented by the quantity $\sigma_{jk}(E, E', \vec{\Omega}, \vec{\Omega}')$, which is composed of three functions

$$\sigma_{jk}(E, E', \vec{\Omega}, \vec{\Omega}') = \sigma_k(E') m_{jk}(E') f_{jk}(E, E', \vec{\Omega}, \vec{\Omega}') \quad (3.4)$$

where $m_{jk}(E')$ is the multiplicity (i.e., average number) of type j particles being produced by a collision of type k of energy E' , and $f_{jk}(E, E', \vec{\Omega}, \vec{\Omega}')$ is the probability density distribution for producing particles of type j of energy E in the direction $\vec{\Omega}$ from the collision of a type k particle with energy E' moving in the direction $\vec{\Omega}'$. For an unpolarized source of projectiles and targets, the energy angle distribution of reaction products can be a function of energies and cosine of the production angle relative to the incident projectile direction. The secondary multiplicities $m_{jk}(E)$ and secondary energy angle distributions are the major unknowns in ion transport theory.

Information on the multiplicity $m_{jk}(E)$ was obtained in the past through experiments with galactic cosmic rays (GCR) as an ion source, and the fragmentation of the ions on target nuclei was observed in nuclear emulsion. (See ref. 23.) Such data are mainly limited by not knowing precisely the identity of the initial or secondary ions and by relatively low-counting rates of each ion type. The heavy ion acceleration by machine reduces the uncertainty because high-counting rates can be obtained with known ion

types. In addition, accelerator experiments provide information, which was not previously available, for the spectral distribution $f_{jk}(E, E', \vec{\Omega}, \vec{\Omega}')$. (See ref. 24.)

The spectral distribution function consists of two terms that describe the fragmentation of the projectile and the fragmentation of the struck nucleus as follows (refs. 25 and 26):

$$\sigma_{jk}(E, E', \vec{\Omega}, \vec{\Omega}') = \sigma_k(E') \left[v_{jk}^P(E') f_{jk}^P(E, E', \vec{\Omega}, \vec{\Omega}') + v_{jk}^T(E') f_{jk}^T(E, E', \vec{\Omega}, \vec{\Omega}') \right] \quad (3.5)$$

where v_{jk}^P and f_{jk}^P depend only weakly on the target and v_{jk}^T and f_{jk}^T depend only weakly on the projectile. Although the average secondary velocities associated with f^P are nearly equal to the projectile velocity, the average velocities associated with f^T are near zero. Experimentally,

$$\begin{aligned} f_{jk}^P(E, E', \vec{\Omega}, \vec{\Omega}') &\approx \left[\frac{m}{2\pi(\sigma_{jk}^P)^2} \right]^{3/2} \sqrt{2E} \exp \left[-\frac{(\vec{p} - \vec{p}')^2}{2(\sigma_{jk}^P)^2} \right] \\ &\approx \left[\frac{m}{2\pi(\sigma_{jk}^P)^2} \right]^{3/2} \sqrt{2E} \exp \left[-\frac{(\vec{\Omega} \sqrt{2mE} - \vec{\Omega}' \sqrt{2mE'})^2}{2(\sigma_{jk}^P)^2} \right] \end{aligned} \quad (3.6)$$

where \vec{p} and \vec{p}' are the momenta per unit mass of j and k ions, respectively, and

$$f_{jk}^T(E, E', \vec{\Omega}, \vec{\Omega}') \approx \left[\frac{m}{2\pi(\sigma_{jk}^T)^2} \right]^{3/2} \sqrt{2E} \exp \left[-\frac{\vec{p}^2}{2(\sigma_{jk}^T)^2} \right] \quad (3.7)$$

where σ_{jk}^P and σ_{jk}^T are related to the rms momentum spread of secondary products. These parameters depend only on the fragmenting nucleus. Feshbach and Huang (ref. 27) suggested that the parameters σ_{jk}^P and σ_{jk}^T depend on the average square momentum of the nuclear fragments as described by Fermi motion. A precise formulation of these ideas in terms of a statistical model was obtained by Goldhaber. (See ref. 28.)

4. Approximation Procedures

4.1. Neglect of Target Fragmentation

The use of equations (3.5)–(3.7) in the evaluation of the source term $\zeta_j(\vec{x}, \vec{\Omega}, E)$ of equation (3.1) results in

$$\begin{aligned} \zeta_j(\vec{x}, \vec{\Omega}, E) &= \sum_k \int dE' d\vec{\Omega}' \sigma_k(E') \phi_k(\vec{x}, \vec{\Omega}', E') \left[v_{jk}^P(E') f_{jk}^P(E, E', \vec{\Omega}, \vec{\Omega}') + v_{jk}^T f_{jk}^T(E, E', \vec{\Omega}, \vec{\Omega}') \right] \\ &\equiv \zeta_j^P(\vec{x}, \vec{\Omega}, E) + \zeta_j^T(\vec{x}, \vec{\Omega}, E) \end{aligned} \quad (4.1)$$

where as before, the superscripts P and T refer to the fragmentation of the projectile and the target, respectively. The target term is

$$\zeta_j^T(\vec{x}, \vec{\Omega}, E) = \sum_k \left[\frac{m}{2\pi(\sigma_{jk}^T)^2} \right]^{3/2} \sqrt{2E} \exp \left[-\frac{mE}{(\sigma_{jk}^T)^2} \right] \int d\vec{\Omega}' \int_E^\infty dE' v_{jk}^T(E') \sigma_k(E') \phi_k(\vec{x}, \vec{\Omega}', E') \quad (4.2)$$

which is negligibly small for

$$E \gg \frac{(\sigma_{jk}^T)^2}{m} \quad (4.3)$$

Thus, for calculating the flux at high energy,

$$\zeta_j(\vec{x}, \vec{\Omega}, E) \approx \zeta_j^P(\vec{x}, \vec{\Omega}, E) \quad (4.4)$$

4.2. Space Radiations

Space radiations have the convenient property of being nearly isotropic. This fact, coupled with the forward-peaked spectral distribution, leads to a substantial simplification in the source term as follows:

$$\zeta_j^P(\vec{x}, \vec{\Omega}, E) \approx \sum_k \int dE' d\vec{\Omega}' \sigma_k(E') v_{jk}^P(E') \left[\frac{m}{2\pi(\sigma_{jk}^P)^2} \right]^{3/2} \sqrt{2E'} \exp \left[-\frac{(\vec{\Omega} \cdot \sqrt{2mE} - \vec{\Omega}' \cdot \sqrt{2mE'})^2}{2(\sigma_{jk}^P)^2} \right] \phi_k(\vec{x}, \vec{\Omega}', E') \quad (4.5)$$

If $\phi_k(\vec{x}, \vec{\Omega}', E')$ is assumed to be a slowly varying function of $\vec{\Omega}'$, an expansion about the sharply peaked maximum of the exponential function is possible. Such an expansion is made by letting

$$\vec{\Omega}' = \vec{\Omega} + (\cos \theta - 1) \vec{\Omega} + \vec{e}_\phi \sin \theta \quad (4.6)$$

where

$$\cos \theta = \vec{\Omega} \cdot \vec{\Omega}' \quad (4.7)$$

and

$$\vec{e}_\phi = \frac{\vec{\Omega} \times \vec{\Omega}'}{|\vec{\Omega} \times \vec{\Omega}'|} \quad (4.8)$$

The flux may be expanded as

$$\phi_k(\vec{x}, \vec{\Omega}', E') = \phi_k(\vec{x}, \vec{\Omega}, E') + \left[\frac{\partial}{\partial \vec{\Omega}} \phi_k(\vec{x}, \vec{\Omega}, E') \right] \cdot [(\cos \theta - 1) \vec{\Omega} + \vec{e}_\phi \sin \theta] + \dots \quad (4.9)$$

Substitution of equation (4.9) into equation (4.5) and simplification result in

$$\begin{aligned} \zeta_j^P(\vec{x}, \vec{\Omega}, E) \approx & \sum_k \int dE' \sigma_k(E') v_{jk}^P(E') \left[\frac{m}{2\pi(\sigma_{jk}^P)^2} \right]^{3/2} \frac{\sqrt{2}}{\sqrt{E'}} \exp \left[-\frac{(\sqrt{2mE} - \sqrt{2mE'})^2}{2(\sigma_{jk}^P)^2} \right] \\ & \times \left\{ \phi_k(\vec{x}, \vec{\Omega}, E') - \left[\vec{\Omega} \cdot \frac{\partial}{\partial \vec{\Omega}} \phi_k(\vec{x}, \vec{\Omega}, E') \right] \left[\frac{(\sigma_{jk}^P)^2}{2m\sqrt{EE'}} \right] + \dots \right\} \end{aligned} \quad (4.10)$$

The leading term of equation (4.10) is clearly a good approximation of the source term whenever

$$\frac{2mE}{(\sigma_{jk}^P)^2} \gg \frac{\vec{\Omega} \cdot \frac{\partial}{\partial \vec{\Omega}} \phi_k(\vec{x}, \vec{\Omega}, E')}{\phi_k(\vec{x}, \vec{\Omega}, E')} \quad (4.11)$$

The leading term is equivalent to assuming that secondary ions are produced only in the direction of motion of the primary ions. For space radiations, which are nearly isotropic, equation (4.11) is easily met, and neglect of higher order terms in equation (4.10) results in the usual straight-ahead approximation. If radiations are highly anisotropic, then equation (4.11) is not likely to apply. Validity of straight-ahead approximation was studied empirically by Alsmiller et al. (refs. 29 and 30) for proton transport.

4.3. Velocity-Conserving Interactions

Customarily, in cosmic ion transport studies (ref. 31), fragment velocities are assumed to be equal to the fragmenting ion velocity before collision. The order of approximation resulting from such an assumption is derived with the assumption that the projectile energy E' is equal to the secondary energy plus a positive quantity ϵ ,

$$E' = E + \epsilon \quad (4.12)$$

where ϵ is assumed to contribute to equation (4.10) only across a small range above zero energy. Substitution of equation (4.12) into equation (4.10) and expansion of the integrand result in

$$\begin{aligned} \zeta_j^P(\vec{x}, \vec{\Omega}, E) = \sum_k \sigma_k(E) v_{jk}^P(E) \left\{ \phi_k(\vec{x}, \vec{\Omega}, E) \left[1 - \sqrt{\frac{(\sigma_{jk}^P)^2}{\pi m E}} \right] \right. \\ \left. + \left[E \frac{\partial}{\partial E} \phi_k(\vec{x}, \vec{\Omega}, E) \right] \sqrt{\frac{(\sigma_{jk}^P)^2}{\pi m E}} - \left[\vec{\Omega} \cdot \frac{\partial}{\partial \vec{\Omega}} \phi_k(\vec{x}, \vec{\Omega}, E) \right] \frac{(\sigma_{jk}^P)^2}{2mE} + \dots \right\} \quad (4.13) \end{aligned}$$

Because $\sqrt{(\sigma_{jk}^P)^2 / mE} \ll 1$, the assumption of velocity conservation at those energies for which most nuclear reactions occur is inferior to the straight-ahead approximation but may be adequate for space radiations where variation of $\phi_k(\vec{x}, \vec{\Omega}, E)$ with energy is sufficiently smooth. That is

$$E \frac{\partial}{\partial E} \phi_k(\vec{x}, \vec{\Omega}, E) \approx \phi_k(\vec{x}, \vec{\Omega}, E)$$

4.4. Decoupling Target and Projectile Flux

Equation (3.1) can be rewritten with equation (4.1) as

$$B_j \phi_j(\vec{x}, \vec{\Omega}, E) = \sum_k F_{jk}^T \phi_k(\vec{x}, \vec{\Omega}, E) + \sum_k F_{jk}^P \phi_k(\vec{x}, \vec{\Omega}, E) \quad (4.14)$$

where the differential operator is given by

$$B_j = \left[\vec{\Omega} \cdot \nabla - \frac{1}{A_j} \frac{\partial}{\partial E} S_j(E) + \sigma_j(E) \right] \quad (4.15)$$

and the integral operator $F_{jk} = F_{jk}^T + F_{jk}^P$ is given by

$$F_{jk}\phi_k(\vec{x}, \vec{\Omega}, E) = \int dE' d\vec{\Omega}' \sigma_{jk}(E, E', \vec{\Omega}, \vec{\Omega}') \phi_k(\vec{x}, \vec{\Omega}', E') \quad (4.16)$$

By defining the flux as the sum of two terms,

$$\phi_j(\vec{x}, \vec{\Omega}, E) = \phi_j^T(\vec{x}, \vec{\Omega}, E) + \phi_j^P(\vec{x}, \vec{\Omega}, E) \quad (4.17)$$

which permits the following separation:

$$B_j \phi_j^P(\vec{x}, \vec{\Omega}, E) = \sum_k F_{jk}^P \phi_k^P(\vec{x}, \vec{\Omega}, E) + \sum_k F_{jk}^P \phi_k^T(\vec{x}, \vec{\Omega}, E) \quad (4.18)$$

$$B_j \phi_j^T(\vec{x}, \vec{\Omega}, E) = \sum_k F_{jk}^T \phi_k^P(\vec{x}, \vec{\Omega}, E) + \sum_k F_{jk}^T \phi_k^T(\vec{x}, \vec{\Omega}, E) \quad (4.19)$$

As noted in connection with equations (4.1)–(4.4), the source term on the right side of equation (4.19) is small at high energies. Assume that

$$\phi_j^T(\vec{x}, \vec{\Omega}, E) \approx 0 \quad (4.20)$$

for $E \gg (\sigma_{jk}^T)^2/m$. As a result of equation (4.20) and the fact that the ion range is small compared with its mean free path at low energy,

$$B_j \phi_j^P(\vec{x}, \vec{\Omega}, E) \approx \sum_k F_{jk}^P \phi_k^P(\vec{x}, \vec{\Omega}, E) \quad (4.21)$$

$$B_j \phi_j^T(\vec{x}, \vec{\Omega}, E) \approx \sum_k F_{jk}^T \phi_k^P(\vec{x}, \vec{\Omega}, E) \quad (4.22)$$

The advantage of this separation is that, once equation (4.21) is solved, equation (4.22) can be solved in closed form. The solution of equation (4.22) is accomplished by noting that the inwardly directed flux ϕ_j^T must vanish on the boundary so that

$$\begin{aligned} \phi_j^T(\vec{x}, \vec{\Omega}, E) &\approx \sum_k \int_E^{E_\gamma} dE' \frac{A_j P_j(E')}{P_j(E) S_j(E)} \int dE'' d\vec{\Omega}' \sigma_{jk}^T(E', E'', \vec{\Omega}, \vec{\Omega}') \\ &\quad \times \phi_k^P\{\vec{x} + [R_j(E) - R_j(E')] \vec{\Omega}, \vec{\Omega}', E''\} \end{aligned} \quad (4.23)$$

where $E_\gamma = R_j^{-1}[d + R_j(E)]$ with d being the projected distance to the boundary.

The use of equations (3.5) and (3.7) in equation (4.23) yields

$$\begin{aligned} \phi_j^T(\vec{x}, \vec{\Omega}, E) &\approx \int_E^{E_\gamma} dE' \frac{A_j P_j(E')}{P_j(E) S_j(E)} \left[\frac{m}{2\pi (\sigma_{jk}^T)^2} \right]^{3/2} \sqrt{2E'} \exp \left[-\frac{mE'}{(\sigma_{jk}^T)^2} \right] \\ &\quad \times \zeta_j^T\{\vec{x} + [R_j(E) - R_j(E')] \vec{\Omega}\} \end{aligned} \quad (4.24)$$

where

$$\zeta_j^T(\vec{x}) = \sum_k \int dE' d\vec{\Omega}' \sigma_k(E') \mathbf{v}_{jk}^T(E') \phi_k^P(\vec{x}, \vec{\Omega}', E') \quad (4.25)$$

and σ_{jk}^T has been assumed to be a slowly varying function of projectile type k and projectile energy E . If the range of secondary type j ions is small compared with their mean-free-path lengths and the mean free paths of the fragmenting parent ions l_k , then

$$R_j \left[\frac{(\sigma_{jk}^T)^2}{m} \right] \ll l_k \quad (4.26)$$

and the integral of equation (4.24) may be simplified as

$$\phi_j^T(\vec{x}, \vec{\Omega}, E) \approx \frac{A_j}{S_j(E)} \zeta_j^T(\vec{x}) \int_E^{E'} \left[\frac{m}{2\pi(\sigma_{jk}^T)^2} \right]^{3/2} \sqrt{2E'} \exp \left[-\frac{mE'}{(\sigma_{jk}^T)^2} \right] dE' \quad (4.27)$$

which can be reduced into terms of known functions. Thus,

$$\phi_j^T(\vec{x}, \vec{\Omega}, E) \approx \frac{A_j}{S_j(E)} \zeta_j^T(\vec{x}) \frac{1}{2\pi\sqrt{\pi}} \left\{ \tilde{\Gamma} \left[\frac{3}{2} \frac{mE}{(\sigma_{jk}^T)^2} \right] - \tilde{\Gamma} \left[\frac{3}{2} \frac{mE_\gamma}{(\sigma_{jk}^T)^2} \right] \right\} \quad (4.28)$$

in terms of the incomplete gamma function. Equation (4.28) can be shown to be equivalent to

$$\begin{aligned} \phi_j^T(\vec{x}, \vec{\Omega}, E) \approx \frac{A_j}{S_j(E)} \zeta_j^T(\vec{x}) \frac{1}{2\pi} \left\{ \frac{1}{2} \operatorname{erfc} \left[\sqrt{\frac{mE}{(\sigma_{jk}^T)^2}} \right] - \frac{1}{2} \operatorname{erfc} \left[\sqrt{\frac{mE_\gamma}{(\sigma_{jk}^T)^2}} \right] \right. \\ \left. + \sqrt{\frac{mE}{\pi(\sigma_{jk}^T)^2}} \exp \left[-\frac{mE}{(\sigma_{jk}^T)^2} \right] - \sqrt{\frac{mE_\gamma}{\pi(\sigma_{jk}^T)^2}} \exp \left[-\frac{mE_\gamma}{(\sigma_{jk}^T)^2} \right] \right\} \end{aligned} \quad (4.29)$$

At points sufficiently far from the boundary such that

$$R_j^{-1}(d) \gg \frac{(\sigma_{jk}^T)^2}{m} \quad (4.30)$$

equation (4.28) may be reduced to

$$\phi_j^T(\vec{x}, \vec{\Omega}, E) \approx \frac{A_j}{S_j(E)} \zeta_j^T(\vec{x}) \frac{1}{2\pi} \left\{ \frac{1}{2} \operatorname{erfc} \left[\sqrt{\frac{mE}{(\sigma_{jk}^T)^2}} \right] + \sqrt{\frac{mE}{\pi(\sigma_{jk}^T)^2}} \exp \left[-\frac{mE}{(\sigma_{jk}^T)^2} \right] \right\} \quad (4.31)$$

which is the equilibrium solution because the target fragment spectrum is the difference between the collision source and collision losses. The solution of equation (4.21) is examined in section 4.5.

4.5. Back Substitution and Perturbation Theory

One approach to the solution of equation (4.21) results from the fact that the multiple charged ions tend to be destroyed in nuclear reactions. Thus,

$$F_{jk}^P \equiv 0 \quad (j \geq k) \quad (4.32)$$

This means that there is a maximum j such that

$$B_j \phi_j^P(\vec{x}, \vec{\Omega}, E) = 0 \quad (4.33)$$

where J is the maximum j . Furthermore,

$$B_{J-1}\phi_{J-1}^P(\vec{x}, \vec{\Omega}, E) = F_{J-1,J}^P\phi_J^P(\vec{x}, \vec{\Omega}, E) \quad (4.34)$$

and in general,

$$B_{J-N}\phi_{J-N}^P(\vec{x}, \vec{\Omega}, E) = \sum_{k=1}^{N-1} F_{J-N,J-k}^P\phi_{J-k}^P(\vec{x}, \vec{\Omega}, E) \quad (N < J-1) \quad (4.35)$$

Note that equations (4.34) and (4.35) constitute solvable problems. The singly and doubly charged ions satisfy

$$B_1\phi_1^P(\vec{x}, \vec{\Omega}, E) = F_{1,1}^P\phi_1^P(\vec{x}, \vec{\Omega}, E) + \sum_{k=2}^J F_{1,k}^P\phi_k^P(\vec{x}, \vec{\Omega}, E) \quad (4.36)$$

Equation (4.36), unlike equations (4.33)–(4.35), is an integral-differential equation that is difficult to solve directly. Equation (4.35) is solvable by perturbation theory, and the resultant series is known to converge rapidly for intermediate and low energies. (See refs. 10 and 32–34.) Note that equations (4.33) and (4.35) are also obtained from perturbation theory as applied to equation (4.21) at the outset. Thus, the perturbation series is expected to converge after the first J plus a few terms.

5. Galactic Ion Transport

5.1. Derivation of GCR Heavy Ion Transport Equation

In this section, the methods of previous nucleon transport studies (ref. 32) are expanded by combining analytical and numerical tools. The galactic cosmic ray ion transport problem is transformed to an integral along the characteristic curve of that particular ion, and the perturbation series (ref. 32) is replaced by a simple numerical procedure. The resulting method reduces the difficulty associated with the low-energy discretization and the restriction to a definite form for the stopping power. The resulting numerical procedure is simple and is not computationally intensive.

Here, the straight-ahead approximation is used, and the target secondary fragments are neglected. (See refs. 6 and 8.) For multiple charged ions, the transport equation can be written as

$$\left[\frac{\partial}{\partial x} - \frac{\partial}{\partial E} \tilde{S}_j(E) + \sigma_j \right] \phi_j(x, E) = \sum_{k>j} m_{jk} \sigma_k \phi_k(x, E) \quad (5.1)$$

where $\phi_j(x, E)$ is the flux of ions of type j with atomic mass A_j at x moving along the X -axis at energy E in units of A MeV, σ_j is the corresponding macroscopic nuclear absorption cross section, $\tilde{S}_j(E)$ is the change in E per unit distance, and m_{jk} is the multiplicity of ion j produced by ion k in a collision. The corresponding transport equation for the light ions is

$$\left[\frac{\partial}{\partial x} - \frac{\partial}{\partial E} \tilde{S}_j(E) + \sigma_j(E) \right] \phi_j(x, E) = \sum_k \int_E^\infty \sigma_{jk}(E, E') \phi_k(x, E') dE' \quad (5.2)$$

The quantities m_{jk} and σ_j are assumed to be energy independent in equation (5.1) but are fully energy dependent in equation (5.2).

The range of the ion is given as

$$R_j(E) = \int_0^E \frac{dE'}{\tilde{S}_j(E')} \quad (5.3)$$

The solution to equation (5.1) is found subject to the boundary specification at $x = 0$ and arbitrary E as

$$\phi_j(0, E) = F_j(E) \quad (5.4)$$

Usually, $F_j(E)$ is called the incident beam spectrum.

From Bethe's theory,

$$\tilde{S}_j(E) = \frac{A_p Z_j^2}{A_j Z_p^2} \tilde{S}_p(E) \quad (5.5)$$

which holds for all energies greater than $\approx 100A$ keV, provided that the ion effective charge is used, and leads to

$$\frac{Z_j^2}{A_j} R_j(E) = \frac{Z_p^2}{A_p} R_p(E) \quad (5.6)$$

The subscript p refers to proton. Equation (5.6) is accurate at high energy and only approximately true at low energy because of electron capture by the ion (which effectively reduces its charge), higher order Born corrections to Bethe's theory, and nuclear stopping at the lowest energies. Herein, the parameter v_j is defined as

$$v_j R_j(E) = v_k R_k(E) \quad (5.7)$$

so that

$$v_j = \frac{Z_j^2}{A_j} \quad (5.8)$$

Equations (5.6)–(5.8) are used in the subsequent development, and the energy variation in v_j is neglected. The inverse function of $R_j(E)$ is defined as

$$E = R_j^{-1} [R_j(E)] \quad (5.9)$$

For the purpose of solving equation (5.1), the following coordinates are used:

$$\eta_j \equiv x - R_j(E) \quad (5.10)$$

$$\xi_j \equiv x + R_j(E) \quad (5.11)$$

where η_j varies along the particle path, and ξ_j is constant along the particle trajectory. The new fluence functions are defined as

$$\chi_j(\eta_j, \xi_j) \equiv \tilde{S}_j(E) \phi_j(x, E) = \psi_j(x, r_j) \quad (5.12)$$

$$\bar{\chi}_k(\eta_j, \xi_j) \equiv \chi_k(\eta_k, \xi_k) \quad (5.13)$$

where

$$\xi_j + \eta_j = \xi_k + \eta_k \quad (5.14)$$

$$\eta_j - \xi_j = \frac{v_k}{v_j} (\eta_k - \xi_k) \quad (5.15)$$

and $r_j = R_j(E)$. By this coordinate mapping, equation (5.1) becomes

$$\left(2 \frac{\partial}{\partial \eta_j} + \sigma_j\right) \chi_j(\eta_j, \xi_j) = \sum_k m_{jk} \sigma_k \frac{v_j}{v_k} \chi_k(\eta_j, \xi_j) \quad (5.16)$$

where σ_j is assumed to be energy independent for simplicity of formalism. There is a small variation in σ_j (≈ 20 percent) that is accounted for in the code. (See ref. 35.) Equation (5.16) is solved by using line integration with an integrating factor (ref. 12), which results in

$$\mu_j(\eta_j, \xi_j) = \exp\left[\frac{1}{2}\sigma_j(\xi_j + \eta_j)\right] \quad (5.17)$$

Then,

$$\begin{aligned} \chi_j(\eta_j, \xi_j) = & \exp\left[-\frac{1}{2}\sigma_j(\xi_j + \eta_j)\right] \chi_j(-\xi_j, \xi_j) \\ & + \frac{1}{2} \int_{-\xi_j}^{\eta_j} \exp\left[\frac{1}{2}\sigma_j(\eta' - \eta_j)\right] \sum_k m_{jk} \sigma_k \frac{v_j}{v_k} \chi_k(\eta', \xi_k) d\eta' \end{aligned} \quad (5.18)$$

where

$$\begin{aligned} \eta'_k &= \frac{v_k + v_j}{2v_k} \eta' + \frac{v_k - v_j}{2v_k} \xi_j \\ \xi'_k &= \frac{v_k - v_j}{2v_k} \eta' + \frac{v_k + v_j}{2v_k} \xi_j \end{aligned}$$

By defining

$$\psi_j(x, r_j) = \chi_j(\eta_j, \xi_j) \quad (5.19)$$

then

$$\psi_j(x, r_j) = \exp(-\sigma_j x) \psi_j(0, r_j + x) + \int_0^x dz \exp(-\sigma_j z) \sum_k m_{jk} \sigma_k \frac{v_j}{v_k} \psi_k\left(x - z, r_k + \frac{v_j}{v_k} z\right) \quad (5.20)$$

Furthermore,

$$\begin{aligned} \psi_j(x + h, r_j) = & \exp(-\sigma_j h) \psi_j(x, r_j + h) \\ & + \int_0^h dz \exp(-\sigma_j z) \sum_k m_{jk} \sigma_k \frac{v_j}{v_k} \psi_k\left(x + h - z, r_k + \frac{v_j}{v_k} z\right) \end{aligned} \quad (5.21)$$

Equation (5.20) clearly shows that

$$\psi_k(x + h - z, r_k) = \exp[-\sigma_k(h - z)] \psi_k(x, r_k + h) + O(h - z) \quad (5.22)$$

which, after substitution into equation (5.21), yields

$$\begin{aligned} \psi_j(x + h, r_j) = & \exp(-\sigma_j h) \psi_j(x, r_j + h) \\ & + \int_0^h dz \exp(-\sigma_j z) \sum_k m_{jk} \sigma_k \frac{v_j}{v_k} \exp[-\sigma_k(h - z)] \psi_k\left(x, r_k + \frac{v_j}{v_k} z + h - z\right) \end{aligned} \quad (5.23)$$

which is correct to order h^2 . This expression can be further approximated by

$$\begin{aligned} \psi_j(x+h, r_j) &= \exp(-\sigma_j h) \psi_j(x, r_j+h) \\ &+ \sum_k m_{jk} \sigma_k \frac{v_j}{v_k} \left[\frac{\exp(-\sigma_j h) - \exp(-\sigma_k h)}{\sigma_k - \sigma_j} \right] \psi_k \left(x, r_k + \frac{v_j}{v_k} h \right) \end{aligned} \quad (5.24)$$

which is accurate to $O[(v_k - v_j)h]$. Equation (5.24) is the basis of the GCR transport computer code GCRTN. (See refs. 12, 13, and 36.) The nucleon transport equation (5.2) is solved by adding the heavy ion collision source of nucleons to the BRYNTRN computer code (ref. 33) to create HZETRN, which effectively solves equation (5.2) by adding a heavy ion collision source of nucleons to the right side of the equation. Equation (5.24) provides the propagation algorithm for the heavy ions. The corresponding propagation procedure for the light ions (refs. 33, 37, and 38) is

$$\psi(x+h, r) \approx e^{-\sigma h} \psi(x, r+h) + e^{-\sigma h} \int_0^h dz \int_r^\infty dr' f(r+z, r'+z) \psi(x, r'+h) \quad (5.25)$$

with the order of h^2 .

The following quantities are of interest:

1. The integral fluence is

$$\Phi_j(x, > E) = \int_{R_j(E)}^\infty \psi_j(x, r) dr \quad (5.26)$$

2. The energy absorbed per gram is

$$D_j(x, > E) = \int_E^\infty A_j \psi_j[x, R_j(E)] dE \quad (5.27)$$

3. The dose equivalent is

$$H_j(x, > E) = A_j \int_E^\infty Q_F \psi_j[x, R_j(E)] dE \quad (5.28)$$

where Q_F is the quality factor. These quantities are not recommended for use in shield design for protection from GCR but give some relative measure of their biological importance.

5.2. Numerical Procedure

The secondary particle production term of the propagation algorithm for the nucleons in equation (5.25) has been further reduced to a form that can be numerically integrated with ease. Details of the form and its validity are discussed in reference 33. For the heavy ions, the secondary production term (i.e., the second term on the right side of equation (5.24)) does not involve any integration; however, the interpolation of the transformed fluence function is based on the independent variable r_k , which is different from the range of ions r_j of type j given on the left side of the equation. To circumvent the problem, the equation is further modified by using the definition of $\tilde{S}_j(E)$, with E given in units of A MeV; then

$$\tilde{S}_j(E) = \tilde{S}_j(E_j/A_j) = -\frac{\Delta(E_j/A_j)}{\Delta x} = \frac{1}{A_j} \frac{\Delta E_j}{\Delta x} = \frac{1}{A_j} S_j(E_j) \quad (5.29)$$

with

$$S_j(E_j) = Z_j^2 S_p(E_j/A_j) \quad (5.30)$$

where S_p is the proton stopping power, and E_j is the energy in MeV of the ions of type j . Then

$$\tilde{S}_j(E) = \frac{1}{A_j} Z_j^2 S_p(E_j/A_j) \equiv v_j S_p(E_p) \quad (5.31)$$

where

$$E_p = E_j/A_j \quad (5.32)$$

By rewriting equation (5.19) as

$$\psi_j(x, r_j) \equiv \tilde{S}_j(E) \phi_j(x, E) = v_j S_p(E) \phi_j(x, E) \quad (5.33)$$

the new fluence function can be defined as

$$\psi'_j(x, r) \equiv v_j S_p(E) \phi(x, E) \equiv \psi_j(x, r_j) \quad (5.34)$$

with $r = r_p = v_j r_j$, where

$$r_p = \int_0^E \frac{dE'}{S_p(E')} \quad (5.35)$$

Equation (5.24) becomes

$$\psi'_j(x+h, r) = e^{-\sigma_j h} \psi'_j(x, r+v_j h) + \sum_k m_{jk} \sigma_k \left(\frac{e^{-\sigma_j h} - e^{-\sigma_k h}}{\sigma_k - \sigma_j} \right) \frac{v_k}{v_j} \psi'_k(x, r+v_j h) \quad (5.36)$$

so that there is now only one definition of range that is related to energy. The equation can be solved by setting up the proton range grid r and marching the solution from $x = 0$ by steps of h to the desired thickness.

5.3. Error Propagation

When considering how errors are propagated in the use of equation (5.36), the error is introduced locally by calculating $\psi'_j(x, r+v_j h)$ across the energy range grid. By limiting the analysis to the first term of equation (5.36), the error is defined at each range grid r_i such that

$$\psi'_j(x+h, r_i) = e^{-\sigma_j h} \psi'_j(x, r_i+v_j h) \quad (5.37)$$

The truncation error ϵ_i is introduced in the interpolation procedure for the value $\psi'_{j, \text{int}}$ and

$$\psi'_j(x, r_i+v_j h) = \psi'_{j, \text{int}}(x, r_i+v_j h) + \epsilon_i(h) \quad (5.38)$$

After the m th step from the boundary, the numerical solution is

$$\psi'_j(mh, r_i) = e^{-\sigma_j h} \psi'_{j, \text{int}}[(m-1)h, r_i+v_j h] + \sum_{l=0}^{m-1} e^{-\sigma_j(m-l)h} \epsilon_l(h) \quad (5.39)$$

Suppose $0 \leq \epsilon_l(h) \leq \epsilon(h)$ for all l ; then the propagated error is bounded by

$$\epsilon_{\text{prp}}(m) = \sum_{l=0}^{m-1} e^{-\sigma_j(m-l)h} \epsilon_l(h) \leq \epsilon(h) \sum_{l=0}^{m-1} e^{-\sigma_j(m-l)h} \quad (5.40)$$

Note that

$$\sum_{l=0}^{m-1} e^{-\sigma_j m h} e^{\sigma_j h l} \approx \frac{1}{h \sigma_j} \left(1 - e^{-\sigma_j m h} \right) \quad (5.41)$$

because $h \sigma_j \ll 1$. Clearly, the propagated error on the m th step is bounded by

$$\varepsilon_{\text{prp}}(h) < \frac{\varepsilon(h)}{h \sigma_j} \left(1 - e^{-\sigma_j m h} \right) \quad (5.42)$$

where $\varepsilon(h)$ is the maximum error per step. With the increasing value of m , the propagated error grows with each step to a maximum value of $\varepsilon(h)/h \sigma_j$. Because the increase in the value of h is limited by the perturbation theory, the reduction of the local truncation error is the only viable approach left for reducing the propagated error to a desired level. The same consideration can be applied to the second term of equation (5.36) as the terms are similar in nature. The issue of error propagation in HZETRN is further studied by Shinn and Wilson. (See ref. 39.)

5.4. Numerical Algorithms

The error analysis of section 5.3 results in the conclusion that, to effectively reduce the level of propagated error, the local truncated error must be reduced. Three numerical algorithms are involved in solving equations (5.25)–(5.28) and (5.36): interpolation, integration, and grid generation. The choice of grid distribution that is interrelated to the interpolation and integration methods can increase the efficiency of the code if the number of grids can be reduced.

The interpolation method in HZETRN is the third-order Lagrange's method, which was used successfully in improving BRYNTRN. (See ref. 37.) With the four neighboring interpolation grids (data points) placed on both sides of the interpolated point, the error will tend to be the smallest in the middle interval of all the data points if the grid distribution is rather uniform. (See ref. 40.) The choice of a much higher order Lagrange's method will substantially decrease the efficiency of the computer code because there are more than 10 interpolation calls for each energy point at each step. Other interpolation methods such as a cubic spline were considered but discarded. In general, the splines are more accurate; however, their characteristically large oscillations can result in erroneous solutions.

The procedure for numerical integration that was used in the improved BRYNTRN (ref. 37) is also used here in HZETRN. The procedure is based on the compound quadrature formulation summing over all the subintervals between the grids with the midpoint evaluated by making use of the improved interpolation procedure mentioned previously. A simple numerical method such as Simpson's rule is used to integrate for the subintervals.

Three considerations dictate how the grids should be distributed. The first is the shape of the input spectrum. Because the GCR fluences are several orders of magnitude greater at the lower energies (refs. 41–43), a logarithmic scale is used for the energy or range coordinate as was done in reference 37. The second is the choice of the interpolation method, which requires that the four neighboring grids be as uniformly spaced on a logarithmic scale as possible so that the interpolation error can be minimized. Because the interpolation is performed on the range grid rather than on the energy grid, a uniform grid distribution on a logarithm of range r is desired. The third is the code efficiency, which increased almost quadratically with the decrease in the number of grid points. With the uniform grid points on a logarithmic scale r as the basic structure, the distribution can be modified further to reduce the number of points in the region in which the data are not propagating through the steps. For BRYNTRN, this region occurred below $r_{\min} + h$ (i.e., $\approx 1 \text{ g/cm}^2$) because $r_{\min} \ll 1$ and h is assumed to equal 1 g/cm^2 . (See ref. 37.) This also applies to HZETRN, although the interpolation is now at $r_{\min} + v_j h$, where v_j is always equal to or much greater than 1; because in propagating a distance h , all ions with energy below $r_{\min} + h$ are slowed to energies below the first energy grid point.

6. Stopping Power

In passing through a material, an ion loses the greater fraction of its energy to electronic excitation of the material. Although a satisfactory theory of high-energy ion-electron interaction is available in the form of Bethe's theory utilizing the Born approximation, an equally satisfactory theory for low energies is not available. Bethe's high-energy approximation of the energy loss per unit length (i.e., stopping power) is given by

$$S_e = \frac{4\pi N Z_p^2 Z_t e^4}{m v^2} \left\{ \ln \left[\frac{2m v^2}{(1 - \beta^2) I_t} \right] - \beta^2 - \frac{C}{Z_t} \right\} \quad (6.1)$$

where Z_p is the projectile charge, N is the number of target molecules per unit volume, Z_t is the number of electrons per target molecule, m is the electron mass, v is the projectile velocity, $\beta = v/c$, c is the velocity of light, C is the velocity-dependent shell correction term (ref. 44), and I_t is the mean excitation energy given by

$$Z_t \ln(I_t) = \sum_n f_n \ln(E_n) \quad (6.2)$$

where f_n are the electric dipole oscillator strengths of the target, and E_n are the corresponding excitation energies. The sum in equation (6.2) includes discrete and continuum levels. Molecular stopping power is reasonably approximated by the sum of the corresponding empirically derived *atomic* stopping powers for which equations (6.1) and (6.2) imply that

$$Z \ln(I) = \sum_j n_j Z_j \ln(I_j) \quad (6.3)$$

where Z and I pertain to the molecule, Z_j and I_j are the corresponding atomic values, and n_j are the stoichiometric coefficients. This additive rule (eq. (6.3)) is usually called Bragg's rule. (See ref. 45.)

As an input to HZETRN, the high-energy cutoff for the incident GCR spectrum is usually taken to be far beyond the minimum stopping power of $\approx 2A$ GeV, where Bethe's theory starts to overestimate and worsens as the energy increases. This overestimation can be corrected by considering that the field of the incoming ion projectile is perturbed by the neighboring polarized atoms. In HZETRN the approximate correction for the polarization effect (i.e., density effect) is based on the work of Sternheimer. (See ref. 46.) In reference 46, the polarization effect corrections for various elements and compounds were evaluated and fitted by the expressions

$$\delta = 0 \quad (x < x_0) \quad (6.4a)$$

$$\delta = \ln \eta^2 + C + a(x_1 - x)^m \quad (x_0 < x < x_1) \quad (6.4b)$$

$$\delta = \ln \eta^2 + C \quad (x > x_1) \quad (6.4c)$$

where δ is the density effect correction used in the stopping-power formula, $\eta = p/m_o c$, p is the momentum, m_o is the rest mass of the charged particle, c is the velocity of light, and

$$x = (\log_{10} e) \ln \eta = 0.43429 \ln \eta$$

The quantities a , m , x_0 , and x_1 are constants that must be evaluated for each material; C is given by

$$C = -2 \ln(I/hv_p - 1) \quad (6.5)$$

where I is the mean ionization potential; the plasma energy $h\nu_p$ of the material is

$$h\nu_p = h \left(ne^2 / nm_e \right)^{1/2} \quad (6.6)$$

where n is the electron density in electrons/cm³, m_e is the rest mass, and e is the charge of an electron. For compounds and mixtures, the effective mean ionization potential can be determined by

$$\ln I = \frac{1}{n} \sum_i n_i \ln I_i \quad (6.7)$$

where n_i is the electron density for the i th element, and I_i is the corresponding atomic ionization potential.

Reference 46 suggests that, for some practical applications, the use of only the asymptotic density effect correction (eq. (6.4c)) may be adequate for all charged particle energies. In reference 47 Armstrong and Alsmiller compared the stopping-power differences between correct expressions and an asymptotic formula for several elements and compounds. The results indicated an overestimation of at most 6 percent when using the asymptotic formula. Therefore, only the asymptotic formula is used in HZETRN. Equation (6.1) with polarization effect modification becomes

$$S_e = \frac{4\pi N Z_p^2 Z_t e^4}{mv^2} \left\{ \ln \left[\frac{2mv^2}{(1-\beta^2)I} \right] - \beta^2 - \frac{C}{Z_t} - \frac{\delta}{2} \right\} \quad (6.8)$$

The use of equation (6.8) in conjunction with the asymptotic formula of equation (6.4c) does not involve any evaluation of the constants a , m , x_0 , and x_1 for the material considered. A comparison of equations (6.1) and (6.8) for different materials is discussed by Shinn et al. (See ref. 48.)

The electronic stopping power for protons is adequately described by equation (6.8) for energies >500 keV for which the shell correction C makes an important contribution up to 10 MeV. (See ref. 49.) For proton energies <500 keV, charge exchange reactions alter the proton charge over much of its path so that equation (6.8) is understood to be an average over the proton charge states. Normally, an average over the charge states is introduced into equation (6.8) so that the effective charge is the rms ion charge and not the average ion charge. At any ion energy, charge equilibrium is established very quickly in all materials. By utilizing the effective charge in equation (6.8), only modest improvement results at energies <500 keV, which presumably indicates the failure of this theory based on the Born approximation. (See refs. 49 and 50.)

The electronic stopping power for alpha particles requires terms in equation (6.8) of higher order in projectile charge Z_p because of corrections to the Born approximation. The alpha stopping power can not be related to the proton stopping power through their effective charges. Parametric fits to experimental data are given by Ziegler in reference 51 for all elements in both gaseous and condensed phases.

The electronic stopping powers for heavier ions are related to the alpha stopping power through their corresponding effective charges. HZETRN uses the effective charges suggested by Barkas (ref. 52) of

$$Z^* = Z_p \left[1 - \exp \left(-125\beta / Z_p^{2/3} \right) \right] \quad (6.9)$$

where Z_p in equation (6.9) is the atomic number of the ion.

At sufficiently low energies, the energy lost by an ion in a nuclear collision becomes important. The nuclear stopping-power theory used in HZETRN is a modification of the theory of Lindhard, Scharff, and Schiott. (See ref. 53.) The reduced energy is given as

$$\epsilon = \frac{32.53 A_p A_t E}{Z_p Z_t (A_p + A_t) \left(Z_p^{2/3} + Z_t^{2/3} \right)^{1/2}} \quad (6.10)$$

where E is in units of A keV, and A_p and A_t are the atomic masses of the projectile and the target, respectively. The nuclear stopping power in reduced units (ref. 51) is

$$S_n = \begin{cases} 1.59\epsilon^{1/2} & (\epsilon < 0.01) \\ \frac{1.7\epsilon^{1/2} \ln(\epsilon + e^1)}{1 + 6.8\epsilon + 3.4\epsilon^{3/2}} & (0.01 < \epsilon < 10) \\ \frac{\ln(0.47\epsilon)}{2\epsilon} & (10 < \epsilon) \end{cases} \quad (6.11)$$

and the conversion factor to units of (eV-atoms/cm²)/10¹⁵ is

$$f = \frac{8.426 Z_p A_t A_p}{(A_p + A_t) \left(Z_p^{2/3} + Z_t^{2/3} \right)^{1/2}}$$

The total stopping power S_j is obtained by summing the electronic and nuclear contributions. Other processes of energy transfer such as Bremsstrahlung and pair production for stopping massive ions are unimportant.

For energies greater than a few A MeV, Bethe's equation is adequate if the appropriate corrections to Bragg's rule (refs. 54–56), shell corrections (refs. 44, 49, and 50), and an effective charge are included. Electronic stopping power for protons is calculated from the parametric formulas of Andersen and Ziegler (ref. 49) with some modifications. (See ref. 9.)

Because alpha stopping power is not derivable from the formula for proton stopping power by using the effective charge at low energy, the parametric fits to empirical alpha stopping powers given by Ziegler (ref. 51) are used. Physical state and molecular binding effects are most important for hydrogen (ref. 54); water stopping power was approximated by using the condensed phase parameters for hydrogen and the gas phase experimentally derived parameters for oxygen. Electronic stopping powers for ions with a charge greater than 2 are related to the alpha stopping power by the effective charge of equation (6.9). Figures 2(a), 2(b), and 2(c) show the transport coefficient ranges and stopping powers for five different charge values Z , as calculated by HZETRN for aluminum, water, and liquid hydrogen targets, respectively.

7. Nuclear Database

The nuclear cross sections for neutron and proton interactions are described extensively in references 10 and 33. The heavy ion absorption cross sections σ_{abs} are currently derived from

$$\sigma_{\text{abs}} = \pi r_0^2 \left\{ A_p^{1/3} + A_t^{1/3} - \left[0.200 + A_p^{-1} + A_t^{-1} - 0.292 \exp\left(-\frac{E}{792}\right) \cos(0.229E^{0.453}) \right]^2 (1 + 5E^{-1}) \right\} \quad (7.1)$$

which for $r_0 = 1.26$ fm were fit to the quantum mechanical nuclear cross sections calculated in reference 57.

In this section, the heavy ion fragmentation mechanism is described by abrasion-ablation formalism. In the abrasion-ablation fragmentation model, the high-energy projectile nuclei collide with

stationary target nuclei. In the abrasion step, those portions of the nuclear volumes that overlap are sheared away by the collision. The remaining projectile piece, called "a prefragment," continues its trajectory with essentially its precollision velocity. As a result of the dynamics of the abrasion process, the prefragment is highly excited and subsequently decays by the emission of nuclear particles. This step is the ablation stage. Final deexcitation is through gamma emission. The resultant isotope is the nuclear fragment whose cross section is measured. The abrasion process can be analyzed with classical geometric arguments (refs. 11, 36, and 58) or methods obtained from formal quantum scattering theory. (See refs. 59 and 60.) The ablation stage can be analyzed with geometric arguments (ref. 11) or more sophisticated methods based on Monte Carlo or intranuclear cascade techniques. (See refs. 61–64.) Predictions of fragmentation cross sections on hydrogen targets are made with the approximate semiempirical parameterization formulas of references 65 and 66. The fragmentation cross sections for other heavier targets are generated by the NUCFRG series of semiempirical fragmentation codes, in particular, the second version NUCFRG2 as described in reference 67.

The amount of nuclear material stripped away in the collision of two nuclei of radius R_P and R_T is taken as the volume of the overlap region times an average attenuation factor. (See refs. 36 and 67.) The relevant formula for the constituents in the overlap volume in the projectile is given by

$$\Delta_{\text{abr}} = FA_P [1 - \exp(-C_T/\lambda)] \quad (7.2)$$

where C_T is the chord length at maximum overlap density of the intersecting volume of the projectile and the target λ is the nuclear mean free path, and the expression for F depends on the nature of the collision (i.e., peripheral versus central) and the relative sizes of the colliding nuclei.

From reference 61, for $R_T > R_P$,

$$P = 0.125 (\mu v)^{1/2} \left(\frac{1}{\mu} - 2 \right) \left(\frac{1-\beta}{v} \right)^2 - 0.125 \left[0.5 (\mu v)^{1/2} \left(\frac{1}{\mu} - 2 \right) + 1 \right] \left(\frac{1-\beta}{v} \right)^3 \quad (7.3)$$

and

$$F = 0.75 (1-v)^{1/2} \left(\frac{1-\beta}{v} \right)^2 - 0.125 [3(1-v)^{1/2} - 1] \left(\frac{1-\beta}{v} \right)^3 \quad (7.4)$$

with

$$v = \frac{R_P}{R_P + R_T} \quad (7.5)$$

$$\beta = \frac{b}{R_P + R_T} \quad (7.6)$$

and

$$\mu = \frac{1}{v} - 1 = \frac{R_T}{R_P} \quad (7.7)$$

Equations (7.3) and (7.4) are valid when the collision is peripheral (the two nuclear volumes do not completely overlap). In this case, the impact parameter b is restricted such that

$$R_T - R_P \leq b \leq R_T + R_P \quad (7.8)$$

If the collision is central, then the projectile nucleus volume completely overlaps the target nucleus volume ($b < R_T - R_P$), and all the projectile nucleons are abraded. In this case, equations (7.3) and (7.4) are replaced by

$$P = -1 \quad (7.9)$$

and

$$F = 1 \quad (7.10)$$

and there is no ablation of the projectile because it was destroyed by the abrasion.

For a peripheral collision with $R_P > R_T$, equations (7.3) and (7.4) (ref. 63) become

$$P = 0.125 (\mu v)^{1/2} \left(\frac{1}{\mu} - 2 \right) \left(\frac{1-\beta}{v} \right)^2 - 0.125 \left\{ 0.5 \left(\frac{v}{\mu} \right)^{1/2} \left(\frac{1}{\mu} - 2 \right) \frac{[1(1/v)(1-\mu^2)^{1/2}-1][1(2-\mu)\mu]^{1/2}}{\mu^3} \right\} \left(\frac{1-\beta}{v} \right)^3 \quad (7.11)$$

and

$$F = 0.75 (1-v)^{1/2} \left(\frac{1-\beta}{v} \right)^2 - 0.125 \left\{ \frac{3(1-v)^{1/2}}{\mu} - \frac{[1-(1-\mu^2)^{3/2}][1-(1-\mu)^2]^{1/2}}{\mu^3} \right\} \left(\frac{1-\beta}{v} \right)^3 \quad (7.12)$$

where the impact parameter is restricted such that

$$R_P - R_T \leq b \leq R_P + R_T \quad (7.13)$$

For a central collision ($b < R_P - R_T$) with $R_P > R_T$, equations (7.11) and (7.12) become

$$P = \left[\frac{1}{v} (1-\mu^2)^{1/2} - 1 \right] \left[1 - \left(\frac{\beta}{v} \right)^2 \right]^{1/2} \quad (7.14)$$

and

$$F = [1 - (1-\mu^2)^{3/2}] \left[1 - \left(\frac{\beta}{v} \right)^2 \right]^{1/2} \quad (7.15)$$

The charge ratio of the nuclear matter removed by the collision is assumed to be that of the parent nucleus. The spectators in the overlap region are assumed loosely bound to the remaining prefragment and are lost in a pre-equilibrium emission process. (See ref. 67.)

The surface distortion excitation energy of the projectile prefragment following abrasion of the m nucleons is calculated from the clean-cut abrasion formalism of reference 58. For this model, the colliding nuclei are assumed to be uniform spheres with radii R_i ($i = P, T$). In collision, the overlapping volumes shear off so that the resultant projectile prefragment is a sphere with a cylindrical hole gouged out of it. The excitation energy is then determined by calculating the difference in surface area between the distorted sphere and a perfect sphere of equal volume. This excess surface area ΔS is given in reference 61 as

$$\Delta S = 4\pi R_P^2 [1 + P - (1 - F)^{2/3}] \quad (7.16)$$

where the expressions for P and F differ and depend upon the nature of the collision (i.e., peripheral versus central) and the relative sizes of the colliding nuclei, which were given in previous equations.

The excitation energy associated with surface energy is known to be 0.95 MeV/fm² for near-equilibrium nuclei so that

$$E'_s = 0.95 \Delta S \quad (7.17)$$

for small surface distortions. When large numbers of nucleons are removed in the abrasion process, equation (7.17) is expected to be an underestimate of the actual excitation. This requires the introduction of an excess excitation factor (refs. 11 and 36) in terms of the number of abraded nucleons Δ_{abr} as

$$f = 1 + \frac{5\Delta_{abr}}{A_p} + [1500 - 320(A_p - 12)] \frac{\Delta_{abr}^3}{A_p^3} \quad (7.18)$$

which approaches 1 when the impact parameter is large but increases the excess excitation when many nucleons are removed and grossly distorted nuclei are formed by the collisions. (See ref. 11.) The quantity in the brackets accounts for light nuclei having greater excitation energy than heavier nuclei for the same fraction of mass removed (ref. 67) and is limited to values between 0 and 1500. The total excitation energy is then

$$E_s = E'_s f \quad (7.19)$$

which reduces to equation (7.17) for small Δ_{abr} . Also, the assumption is that 100 percent of the fragments with a mass of 5 are unbound, 90 percent of the fragments with a mass of 8 are unbound, and 50 percent of the fragments with a mass of 9 (^9B) are unbound. (See ref. 11.)

A secondary contribution to the excitation energy is the transfer of kinetic energy of relative motion across the intersecting boundary of the two ions. The rate of energy loss of a nucleon when it passes through nuclear matter (ref. 68) is taken as 13 MeV/fm, and the energy deposit is assumed to be symmetrically dispersed about the azimuth so that 6.5 (MeV/fm)/nucleon at the interface is the average rate of energy transfer into excitation energy. (See ref. 36.) This energy is transferred in single-particle collision processes, and the energy is transferred to excitation energy of the projectile for half of the events and leaves the projectile excitation energy unchanged for the remaining half of the events. (See ref. 11.) The first estimate of this contribution uses the length of the longest chord C_1 in the projectile surface interface. This chord length is the maximum distance traveled by any target constituent through the projectile interior. The number of other target constituents in the interior region can be found by estimating the maximum chord C_t transverse to the projectile velocity, which spans the projectile surface interface. (See ref. 36.) The total excitation energy from excess surface and spectator interaction is then

$$E'_x = 13C_1 \left[1 + \frac{1}{3}(C_t - 1.5) \right] \quad (7.20)$$

where the second term contributes only if $C_t > 1.5$ fm. Also, the effective longitudinal chord length for these remaining nucleons is assumed to be one third of the maximum chord length.

The decay of highly excited nuclear states is dominated by heavy particle emission. In the present model, a nucleon is assumed to be removed for every 10 MeV of excitation energy. The number of ablated nucleons is

$$\Delta_{abl} = \frac{E_s + E_x}{10} \quad (7.21)$$

In accordance with the previously discussed directionality of the energy transfer, E_x has two values

$$E_x = \begin{cases} E'_x & \text{for } P_x = \frac{1}{2} \\ 0 & \text{for } P_{\bar{x}} = \frac{1}{2} \end{cases} \quad (7.22)$$

where P_x and $P_{\bar{x}}$ are the corresponding probabilities of occurrence of each value in collisions.

The number ΔA of nucleons removed through the abrasion-ablation process is given as a function of the impact parameter as

$$\Delta A = \Delta_{\text{abr}}(b) + \Delta_{\text{abl}}(b) \quad (7.23)$$

The cross section for the removal of ΔA nucleons is estimated as

$$\sigma(\Delta A) = \pi(b_2^2 - b_1^2) \quad (7.24)$$

where b_2 is the impact parameter for which the volume of the intersection of the projectile contains Δ_{abr} nucleons and the resulting excitation energies release an additional Δ_{abl} nucleons at the rate of 1 nucleon for every 10 MeV of excitation such that

$$\Delta_{\text{abr}}(b_2) + \Delta_{\text{abl}}(b_2) = \Delta A - \frac{1}{2} \quad (7.25)$$

similarly, for b_1

$$\Delta_{\text{abr}}(b_1) + \Delta_{\text{abl}}(b_1) = \Delta A + \frac{1}{2} \quad (7.26)$$

In the previous discussion, the assumption of straight-line trajectories makes the impact parameter b the distance of closest approach. This assumption makes the abrasion-ablation model a high-energy heavy ion fragmentation model; thus, Coulomb corrections due to low-energy trajectories must be added to the standard abrasion-ablation model. Equations (7.24)–(7.26) can be combined and rewritten (ref. 58) as

$$\sigma(\Delta A) = \pi \left[b \left(\Delta A - \frac{1}{2} \right)^2 - b \left(\Delta A + \frac{1}{2} \right)^2 \right] \quad (7.27)$$

Equation (7.27) is retained in NUCFRG2 as written. However, b is no longer taken to be the distance of closest approach as used in equation (7.27) but is redefined in the following discussion.

The equations of motion in the nuclear Coulomb field are given by energy conservation as

$$E_{\text{tot}} = \frac{1}{2} \mu \dot{r}^2 + \frac{l^2}{2\mu r^2} + \frac{Z_P Z_T e^2}{r} \quad (7.28)$$

where E_{tot} is the total kinetic energy in the center-of-mass system at great relative distances, r is the relative distance between the charge centers with time derivative \dot{r} , μ is the reduced mass, l is the angular momentum, Z_P and Z_T are the atomic numbers of the projectile and target nucleus, respectively, and e is the electronic charge. The angular momentum is given as

$$l^2 = 2\mu E_{\text{tot}} b^2 \quad (7.29)$$

With the use of equation (7.29) and $\dot{r} = 0$, equation (7.28) becomes

$$E_{\text{tot}} = \frac{E_{\text{tot}} b^2}{r^2} + \frac{Z_P Z_T e^2}{r} \quad (7.30)$$

which can be written as

$$b^2 = r(r - r_m) \quad (7.31)$$

where

$$r_m = \frac{Z_P Z_T e^2}{E_{\text{tot}}} \quad (7.32)$$

Note that r_m is the distance of closest approach for the zero impact parameter. For a given ΔA , equation (7.32) is used in NUCFRG2 to calculate the distance of closest approach and equation (7.31) is used to calculate the impact parameter, which permits extrapolation backward in time along the Coulomb trajectory to the initial impact parameter. (See ref. 69.) This calculated value of b is used in equation (7.27) to evaluate the cross section. Note that the effect of the Coulomb trajectory is to move the separation at impact r to smaller impact parameters b and thus reduce the cross sections, especially at low energy.

A second correction to the trajectory calculation comes from the transfer of kinetic energy into binding energy in the release of particles from the projectile. The total kinetic energy in passing through the reaction zone is reduced from the initial energy E_i to the final energy E_f

$$E_f = E_i - 10\Delta A \quad (7.33)$$

by assuming that 10 MeV is the average binding energy. The kinetic energy used in the closest approach calculation is the average

$$E_{\text{tot}} = \frac{1}{2} (E_i + E_f) = E_i - \frac{1}{2} (10\Delta A) \quad (7.34)$$

As given by equation (7.34), E_{tot} is obviously very crude and equation (7.34) can be refined further.

The distribution of charge Z_F of final projectile fragments of mass A_F are strongly affected by nuclear stability. The charge distribution for a given $\sigma(\Delta A)$ as described by Rudstam (ref. 70) is

$$\sigma(A_F, Z_F) = F_1 \exp\left(-R|Z_F - SA_F + TA_F^2|^{3/2}\right) \sigma(\Delta A) \quad (7.35)$$

where $R = 11.8/A_F^D$, $D = 0.45$, $S = 0.486$, $T = 3.8 \times 10^{-4}$, and F_1 is a normalizing factor such that

$$\sum_{Z_F} \sigma(A_F, Z_F) = \sigma(\Delta A) \quad (7.36)$$

The Rudstam formula for $\sigma(\Delta A)$ was not used because the ΔA dependence is too simple and breaks down for heavy targets (refs. 11, 36, 71, and 72) and was replaced by equation (7.27) in the abrasion-ablation fragmentation model.

The charge of the removed nucleons ΔZ is calculated according to charge conservation

$$Z_P = Z_F + \Delta Z \quad (7.37)$$

and is divided between the nucleons and hydrogen and helium isotopes according to the following four rules:

1. The abraded nucleons are those removed from that portion of the projectile in the region of overlap with the target. (See ref. 67.) Therefore, the abraded nucleon charge is assumed to be proportional to the charge fraction of the projectile nucleus as

$$Z_{\text{abr}} = Z_P \Delta_{\text{abr}} / A_P \quad (7.38)$$

This, of course, ignores the charge separation caused by the giant dipole resonance model of reference 63. The charge release in the ablation stage is then

$$Z_{abl} = \Delta Z - Z_{abr} \quad (7.39)$$

which simply conserves the remaining charge.

2. The alpha particle is known to be unusually tightly bound in comparison with other nucleon arrangements. Because of this unusually tight binding of the alpha particles, the helium production is maximized in the ablation process. (See refs. 11 and 36.) The number of alpha particles is

$$N_{\alpha} = [\text{Int}(Z_{abl}/2), \text{Int}(A_{abl}/4)]_{\min} \quad (7.40)$$

where $\text{Int}(x)$ denotes the integer part of x . The remaining isotopes are likewise maximized from the remaining ablated mass and charge in the order of decreasing binding energy. (See ref. 69.) The number of protons N_p produced is given by charge conservation as

$$N_p = Z_{abl} - \sum_i Z_i N_i \quad (7.41)$$

where i ranges over all ablated particles of mass 2, 3, and 4. Similarly, mass conservation requires the number of neutrons N_n produced to be

$$N_n = A_{abl} - N_p - \sum_i A_i N_i \quad (7.42)$$

3. The calculation is performed for $\Delta A = 1$ to $\Delta A = A_p - 1$, for which the cross section associated with $\Delta A > A_p - 0.5$ is omitted. These are, of course, the central collisions for which the projectile is assumed to disintegrate into single nucleons if $r_p < r_T$. Then

$$N_p = Z_p \quad (7.43)$$

$$N_n = A_p - Z_p \quad (7.44)$$

Other collision products such as the energetic target fragments and mesonic components are ignored. The peripheral collisions with $\Delta A < 0.5$ are also ignored. Most important in these near collisions is the Coulomb dissociation process. (See ref. 73.)

4. The description of the nuclear radius is given by

$$R = 1.29 \left(R_{\text{rms}}^2 - R_p^2 \right) \quad (7.45)$$

where R_{rms} is the rms radius of the nucleus charge distribution and R_p is the radius of the proton charge distribution. The improvements to the abrasion-ablation model as implemented in NUCFRG2 and comparison with experiments are further described in references 74 and 75.

Finally, the electromagnetic (EM) dissociation cross-section contributions to the nuclear database as implemented in NUCFRG2 must be considered. In electromagnetic dissociation, the virtual photon field of the target nucleus interacts electromagnetically with the constituents of the projectile to cause excitation and eventual breakup. The electromagnetic dissociation model implemented in NUCFRG2 is limited to single nucleon (proton or neutron) removal processes.

The total electromagnetic cross section for one nucleon removal resulting from electric dipole (E1) and electric quadrupole (E2) interactions is written

$$\begin{aligned}\sigma_{\text{em}} &= \sigma_{E1} + \sigma_{E2} \\ &= \int [N_{E1}(E) \sigma_{E1}(E) + N_{E2}(E) \sigma_{E2}(E)] dE\end{aligned}\quad (7.46)$$

where the virtual photon spectra of energy E produced by the target nucleus (ref. 76) are given for the dipole field by

$$N_{E1}(E) = \frac{1}{2} \frac{Z^2}{E\pi} \alpha \frac{1}{\beta^2} \left[\xi K_0 K_1 - \frac{1}{2} \xi^2 \beta^2 (K_1^2 - K_0^2) \right] \quad (7.47)$$

and for the quadrupole field by

$$N_{E2}(E) = \frac{1}{2} \frac{Z^2}{E\pi} \alpha \frac{1}{\beta^4} \left[2(1 - \beta^2) K_1^2 + \xi(2 - \beta^2)^2 K_0 K_1 - \frac{1}{2} \xi^2 \beta^4 (K_1^2 - K_0^2) \right] \quad (7.48)$$

The terms $\sigma_{E1}(E)$ and $\sigma_{E2}(E)$ are the corresponding photonuclear reaction cross sections for the fragmenting projectile nuclei. The terms K_0 and K_1 in the expression for N_{E1} and N_{E2} are modified Bessel functions of the second kind and are also functions of the parameter ξ . The latter is

$$\xi = \frac{2\pi E b_{\min}}{\gamma \beta h c} \quad (7.49)$$

where E is the virtual photon energy, b_{\min} is the minimum impact parameter below which the collision dynamics are dominated by nuclear interactions rather than by EM interactions, β is the speed of the target measured from the projectile rest frame as a fraction of the speed of light c , h is Planck's constant, and γ is the usual Lorentz's factor from special relativity $\gamma = (1 - \beta^2)^{-1/2}$. The minimum impact parameter is

$$b_{\min} = (1 + x_d) b_c + \frac{\pi a_0}{2\pi} \quad (7.50)$$

where $x_d = 0.25$ and

$$a_0 = \frac{Z_P Z_T e^2}{m_0 v^2} \quad (7.51)$$

allows for trajectory deviation from a straight line. (See ref. 77.) The critical impact parameter for single-nucleon removal is

$$b_c = 1.34 [A_P^{1/3} + A_T^{1/3} - 0.75 (A_P^{-1/3} + A_T^{-1/3})] \quad (7.52)$$

with A_P and A_T being the projectile and target nucleon numbers, respectively.

The photonuclear cross sections $\sigma_{E1}(E)$ and $\sigma_{E2}(E)$ are Lorentzian shaped and somewhat sharply peaked in energy. Therefore, photon spectral functions can be taken outside of the integral of equation (7.46) to yield the approximate form (ref. 76) of

$$\sigma_{\text{em}} \approx N_{E1}(E_{\text{GDR}}) \int \sigma_{E1}(E) dE + N_{E2}(E_{\text{GQR}}) E_{\text{GQR}}^2 \int \sigma_{E2}(E) \frac{dE}{E^2} \quad (7.53)$$

where E_{GDR} and E_{GQR} are the energies at the peaks of the $E1$ and $E2$ photonuclear cross sections, respectively. These integrals of photonuclear cross sections, integrated over energy, are evaluated with the following sum rules (ref. 76):

$$\int \sigma_{E1}(E) dE = 60 \frac{N_p Z_p}{A_p} \quad (7.54)$$

and

$$\int \sigma_{E2}(E) \frac{dE}{E^2} = 0.22 f Z_p A_p^{2/3} \quad (7.55)$$

In equations (7.54) and (7.55), N_p is the number of neutrons, Z_p is the number of protons, and A_p is the mass number of the projectile nucleus. The fractional exhaustion of the energy-weighted sum rule in equation (7.55) (ref. 68) is

$$f = \begin{cases} 0.9 & (A_p > 100) \\ 0.6 & (40 < A_p \leq 100) \\ 0.3 & (40 \leq A_p) \end{cases} \quad (7.56)$$

In equation (7.53), E_{GDR} and E_{GQR} are the energies at the peaks of the $E1$ and $E2$ photonuclear cross sections, respectively. For the dipole term (ref. 68),

$$E_{\text{GDR}} = \frac{hc}{2\pi} \left[\frac{m^* c^2 R_0^2}{8J} \left(1 + u - \frac{1 + \epsilon + 3u}{1 + \epsilon + u} \epsilon \right) \right]^{-1/2} \quad (7.57)$$

with

$$u = \frac{3J}{Q} A_p^{-1/3} \quad (7.58)$$

and

$$R_0 = r_0 A_p^{1/3} \quad (7.59)$$

where $\epsilon = 0.0768$, $Q' = 17$ MeV, $J = 36.8$ MeV, $r_0 = 1.18$ fm, and m^* is 0.70 of the nucleon mass. For the quadrupole term,

$$E_{\text{GQR}} = \frac{63}{A_p^{1/3}} \quad (7.60)$$

Finally, the single-proton or single-neutron removal cross sections are obtained from σ_{em} (eq. (7.53)) by using proton- and neutron-branching ratios g_i ($i = p, n$). Then

$$\sigma(i) = g_i \sigma_{\text{em}} \quad (i = p \text{ or } n) \quad (7.61)$$

The proton-branching ratio has been parameterized by Westfall et al. (ref. 68) as

$$g_p = \min \left[\frac{Z_p}{A_p}, 1.95 \exp(-0.075 Z_p) \right] \quad (7.62)$$

where Z_p is the number of protons, and the minimum value of the two quantities in brackets is to be taken. This parameterization is satisfactory for heavier nuclei ($Z_p > 14$); however, for light nuclei, the following branching ratios are used instead:

$$g_p = \begin{cases} 0.5 & (Z_p < 6) \\ 0.6 & (6 \leq Z_p \leq 8) \\ 0.7 & (8 < Z_p < 14) \end{cases} \quad (7.63)$$

For neutrons, the branching ratio is

$$g_n = 1 - g_p \quad (7.64)$$

Figure 3 shows the absorption cross section as a function of energy for six different projectile charge numbers Z_p , as calculated by HZETRN for aluminum, water, and liquid hydrogen targets. The importance of the target size on the systematic variation of the absorption cross section with projectile mass is clearly seen. Small target nuclei preferentially fragmentize heavy ions, which is important to shield performance. (See ref. 78.)

Among the best known fragmentation cross sections are those for carbon ion beams on carbon targets. Measurements have been made at four energies (250A MeV in ref. 79, 600A MeV in ref. 80, and 1.05A and 2.1A GeV in ref. 81) and are compared in figure 4 with the results from NUCFRG2 cross-section calculation. The effects of the Coulomb trajectory are clearly apparent on the lighter mass fragments of lithium and beryllium which exhibit a change in slope below 100A MeV. Such Coulomb effects will be even more important for projectile and fragments of greater charge. Figure 5 shows the results of very-low-energy (11.7A MeV) oxygen projectiles onto a molybdenum target (ref. 82) where Coulomb effects are very important. The resulting charge removal cross sections seem well represented by NUCFRG2 calculation even at low energies. The process whereby a nucleon is exchanged between the oxygen projectile and the target nucleus is referred to as "exchange poles." As shown in figure 5, the addition of exchange poles to the model will bring charge removal cross sections into agreement as can be judged by the proton exchange pole (neutron removal) contribution for proton exchange.

Figure 6 shows three projectile-target combinations for which two groups of experimenters have taken measurements at nearly the same energy (1.55A GeV in ref. 83 and 1.88A GeV in ref. 84). On the basis of NUCFRG2 calculations, very small cross-section differences are expected to exist at these high energies. (See fig. 4.) Cross sections NUCFRG2 tend to favor the data of Westfall et al. (ref. 84) and lie 10 to 50 percent above that of Cummings et al. (See ref. 83.) Perhaps the most encouraging result of the comparison with the data of Cummings et al. is that trends in NUCFRG2 below aluminum measurements ($Z_F = 13$) of Westfall et al. appear in reasonable agreement with the results of Cummings et al. down to neon fragments ($Z_F = 10$). The NUCFRG2 fragmentation cross sections below neon remains untested.

To better quantify the comparison of results shown in figure 6, χ^2 analysis is used. The test data of the fragmentation model in NUCFRG2 are compared with the experimental data of Cummings et al. (ref. 83) and Westfall et al. (ref. 84) and shown in table I for iron projectiles on three targets. Shown in table I are the total χ^2 values and the average χ^2 contributions per degree of freedom n . Clearly, the data for producing aluminum fragments in the experiments of Westfall et al. show large systematic errors, which are nearly the sole contribution to the χ^2 values. The elimination of the aluminum data from the experiments of Westfall et al. is shown in the table as the values in parentheses. By excluding the aluminum data, the model then shows good agreement with the data of Westfall et al. for carbon and copper targets. The greater discrepancy for the lead targets surely results from the simplified nuclear matter distribution; the use of a diffusive surface model rather than the uniform sphere model is recommended. When comparing the model with the data of Cummings et al., similar trends are shown with

target mass, but the overall agreement with the data of Cummings et al. is inferior to the agreement with the data of Westfall et al. as was previously noted in the discussion of figure 6.

Table I. χ^2 Analysis of Iron Fragmentation Model

Shield + target	NUCFRG2-Westfall ^a		NUCFRG2-Cummings	
	χ^2	χ^2/n	χ^2	χ^2/n
Fe + C	50.2 (16.0)	5 (1.8)	48.3	3.7
Fe + Cu	200.6 (22.9)	20 (2.5)	78.1	6.0
Fe + Pb	177.4 (56.2)	18 (6.2)	83.1	6.7

^aAll values in parentheses exclude Westfall's aluminum cross section.

The χ^2 analysis has been used to compare how well the results of one experimental group compare with the results of another. Such a comparison is shown in table II. Again, the values in parentheses eliminate the aluminum data contribution of Westfall et al. What is clear from table II is that the model represents the two sets of experimental data better than either experimental data set represents the other. This is the best that can be hoped for within the present experimental uncertainty.

Table II. χ^2 Analysis of Iron Fragmentation Experiments

Shield + target	Westfall ^a -Cummings		Cummings-Westfall ^a	
	χ^2	χ^2/n	χ^2	χ^2/n
Fe + C	85.6 (43.3)	8.6 (4.8)	54.6 (33.6)	5.5 (3.7)
Fe + Cu	424.4 (108.4)	42.4 (12.0)	160.3 (69.4)	16.0 (7.7)
Fe + Pb	348.8 (79.5)	34.9 (8.8)	143.4 (55.8)	14.3 (6.2)

^aAll values in parentheses exclude Westfall's aluminum cross section.

Figures 7(a), 7(b), and 7(c) show the fragmentation cross sections as calculated by NUCFRG2 as a function of projectile and fragment mass numbers at four different projectile energies for aluminum, water, and liquid hydrogen targets, respectively. It is difficult to interpret the data directly in terms of shield performance. However, the ion fragmentation at lower energies is clearly most effective for complex target nuclei as can be seen by comparing the aluminum cross sections at 25A MeV in figure 7(a) with those of liquid hydrogen in figure 7(c). In contrast at high energies, the hydrogen target distributes the mass of the fragments more broadly than the aluminum targets as seen by comparing the results at 2400A MeV in figures 7(a) and 7(c). The water target displays both of these characteristics simultaneously.

8. Environmental Model

Calculations and measurements show that HZE ions in GCR particle fluxes vary inversely with solar activity. This dependency indicates that, at maximum solar activity, the GCR particle flux is at a minimum, and at minimum solar activity, the GCR particle flux reaches a maximum. This process of flux variation results from the shielding of the inner part of the solar system by the magnetic fields that are being carried away from the solar surface by the solar wind and varies periodically during an 11- to 13-year cycle. This shielding process is particularly effective in low-energy GCR particles. Calculations have shown that, for energies of 100A MeV or less, the GCR particle flux variation between solar minimum and solar maximum is a factor of 10 or more. At GCR particle energies above a few hundred A MeV, the effect of solar modulation on GCR particle flux gradually decreases and above approximately 10A GeV becomes negligible.

A numerical description of the previous solar modulation must be supplied as an input to the environmental model of any space radiation transport computer code including HZETRN. The environmental model of Badhwar and O'Neill is used in HZETRN. (See ref. 42.) This model is based on fitting measured differential energy spectra of 1954–1989 to stationary Fokker-Planck equation solutions to estimate the diffusion coefficient or the equivalent deceleration parameter Φ in units of MV. Reference 42 shows that, independent of energy, this approach fits the available data within an error of ± 10 percent rms. By using the calculated diffusion coefficient, the GCR spectra of hydrogen, helium, carbon, oxygen, silicon, and iron are estimated. The spectra of the remaining elements were scaled to the previous elements by following reference 43. The environmental model data (i.e., solar maxima-minima) available in HZETRN are for the years 1958–1959, 1970–1971, 1981–1982, and 1989 solar maxima and 1965, 1977, and 1986–1987 solar minima.

Based on the model of reference 42 used in HZETRN, figure 8 shows the predicted fluxes of 1977 solar minimum and 1981 solar maximum as a function of energy for five different charge groups. Figure 9 shows the flux ratio of the 1981 solar maximum compared with the 1977 solar minimum for five different charge groups in the energy range of 0.1 to 10^6 MeV. As discussed previously, the two spectra are essentially identical at energies above 50A GeV, while at lower energies, the ratio can be 1:10 or less depending on the ion type.

Solar flare occurrence is correlated with solar activity and the most important events seem to occur during the ascending or descending phase of the solar cycle. The four solar particle events (SPE) of February 1956, November 1960, August 1972, and October 1989 are widely used to estimate flare-shielding requirements. Fitted fluence energy spectra of these four events (refs. 85–88), King's-fitted spectrum of 1972, and Webber's fit (ref. 89) are as follows:

1. February 1956

$$\phi_p(>E) = 1.5 \times 10^9 \exp\left(-\frac{E-10}{25}\right) + 3 \times 10^8 \exp\left(-\frac{E-100}{320}\right)$$

2. November 1960

$$\phi_p(>E) = 7.6 \times 10^9 \exp\left(-\frac{E-10}{12}\right) + 3.9 \times 10^8 \exp\left(-\frac{E-100}{80}\right)$$

3. August 1972

$$\phi_p(>E) = 6.6 \times 10^8 \exp\left(-\frac{E-100}{30}\right)$$

4. October 1989

$$\phi_p(>E) = 8.65 \times 10^{10} \exp\left[-\frac{P(E)}{59.261}\right]$$

5. August 1972 (King spectrum)

$$\phi_p(>E) = 7.9 \times 10^9 \exp\left(-\frac{E-30}{26.5}\right)$$

6. Webber spectrum with 100 MV rigidity

$$\phi_p(>E) = 1.0 \times 10^9 \exp\left[\frac{239.1 - P(E)}{100}\right]$$

where E is the energy in MeV, $P(E) = \sqrt{E(E+1876)}$ is the rigidity, and $\phi_p(>E)$ is the proton integral fluence in protons/cm². Figure 10 shows the fitted spectra. The flare of October 1989 produced

the greatest number of protons less than 4 MeV, and the flare of August 1972 produced the greatest number of protons between 4 and 150 MeV. The February 1956 flare produced approximately one tenth as many protons greater than 10 MeV as the 1972 and 1989 flares, but it delivered far more protons of 200 MeV or greater than the three other flares. The November 1960 flare exhibited intermediate characteristics.

9. HZETRN Benchmarking

In this section, the subject of HZETRN validation is addressed. Ideally, validation should be accomplished with detailed transport data obtained from carefully planned and controlled experiments; unfortunately, such data are scarce. Although useful for comparative purposes, the atmospheric propagation measurements (ref. 36) used previously are clearly not definitive because they consist of integral fluences of as many as 10 different nuclear species combined into a single datum. Although limited quantities of HZE dosimetry measurements from manned space missions (e.g., Skylab) are available (ref. 90), numerous assumptions about the relationship between the dosimeter location and spacecraft shield thickness and geometry must be made to estimate astronaut dose with GCR codes. Because many of these assumptions may involve inherently great uncertainties (i.e., factors of 2 or greater), differences in results are difficult to attribute to the particular assumptions or approximations that may have been used in the analysis. Without definitive GCR transport measurements with which to compare code predictions, other methods of validation must be considered. One such method is to compare HZETRN with limited available proton transport Monte Carlo results. (See ref. 87.)

In reference 87 comparisons of the results obtained for a hypothetical problem with four different proton transport codes are presented. The hypothetical problem was to determine the dose, as a function of depth in water, resulting from a typical solar flare proton spectrum normally incident on a semi-infinite slab shield which is followed by the slab of water. The water was assumed to be 30 g/cm² thick. The solar proton spectrum was taken to be exponential in rigidity (Webber spectrum of section 8) with a characteristic rigidity of 100 MV and was normalized to 10⁹ protons/cm² with energy >30 MeV. The Nucleon Transport Code (NTC) (ref. 91) is used here and compared with HZETRN.

Figures 11(a) and 11(b) show the total dose in gray (Gy) and total dose equivalent in sievert (Sv) for 20 g/cm² shields of aluminum and iron, respectively, followed by 30 g/cm² of water. For both shields, the code correlation is good. At water depths >20 g/cm², HZETRN predictions are slightly greater than NTC because of the 400-MeV cutoff in the NTC calculation. (See ref. 37.)

Figures 12(a) and 12(b) show the secondary neutron dose in gray (Gy) and secondary neutron dose equivalent in sievert (Sv) for 20 g/cm² shields of aluminum and iron, respectively, followed by 30 g/cm² of water. For both shields, the code correlation is only fair, which results partly from the grid coarseness of the Monte Carlo secondary neutron prediction runs and current limitations in the neutron transport database and elastic scattering propagation. (See ref. 33.)

Other comparisons of HZETRN with analytic functions are reported in references 35, 39, and 75.

10. HZETRN Computational Results

In this section results from applying HZETRN to different targets and environmental periods (i.e., solar minimum or maximum) are presented to provide a sufficiently broad database for code testing. The emphasis is on information that can be extracted directly from a typical execution of HZETRN. Therefore, environmental periods of the 1977 solar minimum and 1981 solar maximum and target materials of aluminum, water, and liquid hydrogen are used. Although HZETRN-calculated dose equivalent results are based on the International Commission on Radiological Protection ICRP-26 and ICRP-60 (refs. 92 and 93) quality factor recommendations, only the dose equivalent results for ICRP-60 are shown here. The calculations include the following results for skin dose and blood-forming organ (BFO) dose:

1. Flux contributions from carbon, oxygen, calcium, and iron ions at different energies
2. Total and individual ions, dose and dose equivalent contributions for skin (0-cm surface dose), and BFO (5-cm-depth dose) at different depths
3. Flux contributions, total dose and dose equivalent contributions for skin (0 cm), and BFO (5 cm) at different linear energy transfers (LET)

Major shortcomings of the HZETRN calculations are as follows:

1. All secondary particles from HZE interactions are presently assumed to be produced with a velocity equal to that of the incident particle; this is conservative for neutrons produced in HZE particle fragmentations
2. Meson contributions to the propagating radiation fields are neglected
3. Target fragments in HZE reactions are neglected
4. Angular dependence, especially in neutron propagation is neglected

These data are not all conservative and probably account for the 15- to 30-percent underestimation of the exposure. As discussed in references 94 and 95, the main sources of uncertainty are the input nuclear fragmentation model and the incident GCR spectrum. Taken together, they could easily impose an uncertainty factor of 2 or more in the astronaut risk estimate. This is especially true for track structure dependent biological models. (See refs. 78 and 96.)

Figures 13–16 show the flux of carbon, oxygen, calcium, and iron ions in aluminum targets for the 1977 and 1981 solar periods at depths of 0, 10, 20, and 30 g/cm² in the energy range of 10⁻²A to 10⁵A MeV. Similarly, figures 17–24 show the flux for water and liquid hydrogen targets. In all figures the effect of solar minimum and solar maximum periods are demonstrated through a reduction in the magnitude of the particular ion flux during solar maximum. Figures 13–24 demonstrate that lighter target materials such as liquid hydrogen have better attenuation characteristics than heavier target materials such as aluminum for all target depths.

Figure 25 shows skin dose, Gy and dose equivalent, Sv, when using ICRP-60 quality factors in aluminum, water, and liquid hydrogen targets for the 1977 and 1981, 1982 solar periods at depths of 0 to 30 g/cm². Only a modest gain in protection is displayed by aluminum shielding. A water shield shows substantially better attenuation characteristics. Liquid hydrogen has excellent shielding characteristics. These results are demonstrated more clearly in figure 26, which shows skin dose, Gy, and dose equivalent, Sv, when using ICRP-60 quality factors in aluminum, water, and liquid hydrogen targets for the 1977 and 1981 solar periods at depths of 0 to 30 g/cm². In figure 26, the effect of the atomic and nuclear properties of the target is demonstrated by increases in skin doses for larger target nuclei.

Figures 27–29 show skin dose, Gy, and figures 30–32 show dose equivalent, Sv, when using ICRP-60 quality factors for six different charge groups in aluminum, water, and liquid hydrogen targets for the 1977 and 1981 solar periods at depths of 0 to 30 g/cm². The better attenuation properties of the liquid hydrogen target versus aluminum target at all target depths are shown for the given charge groups for both solar epochs.

Figures 33–40 show the attenuation behavior of GCR in aluminum, water, and liquid hydrogen at the 5-cm-BFO depth. The dosimetric characteristics of different target materials as a function of target depth are similar to those in figures 13–32, except here an additional attenuation exists in all data because of an additional 5 g/cm² of water.

Figures 41–49 show skin flux and dosimetric characteristics of GCR components in aluminum, water, and liquid hydrogen targets for the 1977 and 1981 solar periods for the LET range of 1 to 10⁵ MeV/cm of water at depths of 0, 10, 20, and 30 g/cm². The presence of the primary components of

GCR from proton to iron is clearly demonstrated as inflections in all figures. The attenuation characteristics of lighter targets such as liquid hydrogen versus heavier targets such as aluminum are shown at all depths and LET ranges.

Figures 50–58 show 5-cm-BFO flux and dosimetric characteristics of GCR components in aluminum, water, and liquid hydrogen targets for the 1977 and 1981 solar periods for the LET range of 1 to 10^5 MeV/cm of water at depths of 0, 10, 20, and 30 g/cm². As before, the dosimetric characteristics of different target materials as a function of target depth are similar to those in figures 41–49, except here an additional attenuation exists in all figures because of an additional 5 g/cm² of water. As in figures 41–49, the presence of the primary components of GCR from proton to iron is clearly demonstrated as inflections, and the attenuation characteristics of lighter targets such as liquid hydrogen versus heavier targets such as aluminum are shown at all depths and LET ranges.

The use of the HZETRN code and the control of the options to generate a typical output are discussed in appendix A. A complete sample output with the options of appendix A is provided in appendix B.

11. Concluding Remarks

The study of free-space radiations is essential for estimation of the risk factors for long-duration manned space flights. The estimates of galactic cosmic ray (GCR) ion flux inside a space module can be made by calculating quantities such as energy and linear energy transfer (LET) spectra. The estimation of doses and LET spectra by numerical predictive techniques, such as HZETRN, is essential for any long-duration manned space mission.

This paper reports the progress in computer code development for space radiation studies and shield design for future NASA space programs; the HZETRN code is a state-of-the-art fast computational tool available for a design engineer to obtain answers to some of the radiation questions that arise in planning any mission. However, major uncertainties in nuclear cross sections, environmental models, and astronaut risk affect the overall accuracy of the predictions of any analytical-computational technique. These uncertainties have a major impact on the proposed shield design for any mission and the subsequent mission cost. Much work remains to accurately resolve the problems with nuclear cross-section calculations, environmental model development, and risk estimate methods.

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Appendix A

HZETRN Description

A1. Program Structure

The main program and each subroutine or function module begins with a brief description of its purpose. The program has 8358 lines, is written in FORTRAN 77, and was developed on a VAX 4000 scaler minicomputer under the VMS operating system; in its current version, the program requires 463 blocks (237056 bytes) of storage space. However, the program is essentially platform and operating system independent. The complete computer code consists of a main program HZETRN, 63 subroutines, and 37 function modules. Table AI provides a list of the subroutines and function modules in the order in which they appear in the program. The overall structure of HZETRN is shown in figure A1, which includes input requirements and output options.

Table AI. HZETRN Program Modules

No.	Program module	Type ^a	No.	Program module	Type ^a	No.	Program module	Type ^a
1	MATTER	S	35	DENSEFF	F	69	FB	F
2	DMETRIC	S	36	ATOPA	S	70	SLOPE	F
3	PRPGT	S	37	ACOEf	F	71	ELSEC	F
4	OD	F	38	CCOEf	F	72	XTOT	F
5	TS	F	39	ATOPN	S	73	XTOTLM	F
6	F2	S	40	BUILD	F	74	XSEC	F
7	FRAG	F	41	SNF	F	75	ABSEC	F
8	XSECFRG	F	42	TEXP	F	76	LZEVAP	S
9	YIELDX	S	43	TSQR	F	77	ASIGM	S
10	YIELDN	S	44	RMAT	F	78	XTEST	S
11	YIELDA	S	45	SIONA	F	79	SPLCN	S
12	YIELDT	S	46	ZEFF	F	80	SPLIN	S
13	PXN	S	47	RTIS	F	81	PRPLI	S
14	YIELD1	S	48	MGAUSS	S	82	FD	S
15	YIELD2	S	49	IUNI	S*	83	LITEST	S
16	YIELD3	S	50	IBI	S*	84	TBARLI	S
17	YIELD4	S	51	QXZ114	F*	85	LIFRAG	S
18	NAND	F	52	QXZ115	S*	86	RADIUS	F
19	YIELDH	S	53	QXZ116	S*	87	XLISEC	F
20	YIELDLI	S	54	QXZ117	S*	88	LKOSPC	S
21	YIELDEM	F	55	SUTPAR	S*	89	E3MAX	F
22	BESSEL	F	56	QXZ060	S*	90	WDKO	S
23	GEODA	S	57	QXZ061	S*	91	LQESPC	S
24	BSEACH	S	58	QXZ062	S*	92	WQE	F
25	DELTA	S	59	QXZ063	F*	93	DERF	F
26	FPOFB	S	60	QXZ111	S*	94	GCRFLUX	S
27	LIMIT	S	61	QXZ112	S*	95	FBERT	S
28	GEOFR	S	62	QXZ119	S*	96	BERTINI	S
29	RADLI	F	63	PHTOINT	S	97	RANFT	S
30	EOFS	S	64	PHI	F	98	FDNP	S
31	CROSS0	S	65	PHTOD	S	99	Q60	F
32	QOFS	F	66	ELSPEC	S	100	SFBERT	S
33	ATOE	S	67	XPP	F			
34	ATOPP	S	68	XNP	F			

^a S—subroutine module.

F—function module.

S*—subroutine module taken from LaRC-NASA mathematical library (N2-3D).

F*—function module taken from LaRC-NASA mathematical library (N2-3D).

A2. HZETRN Input Requirements

The complete program is composed of the HZETRN source code (HZEALH2O.FOR in the COSMIC library) and three input data files. In the current version, HZEALH2O.FOR requires the following input files:

1. ATOMIC.DAT
2. NUCLEAR.DAT
3. JSCCOSMC.DAT

The following is a brief description of each file and how to set up the input flags if any are required.

1. FORTRAN code HZEALH2O.FOR is set up to transport galactic cosmic ray (GCR) particles in free space (geomagnetic cutoffs are ignored) through a given thickness of the aluminum shield followed by a given depth of water. Besides the setting of array dimensions for the energy grid points and isotope fragment number, which are defined in the PARAMETER statement throughout the code as $II=45$ and $IJ=59$, respectively, the only changes to the code required for any run are in the MAIN module and subroutine MATTER. In addition the user has the option of changing the isotope table that is used to represent the transported particle fields of the GCR particles in the shield or target material in function TS.

a. In the MAIN module, the following two integer variables must be defined:

- (1) IPRGCR, which specifies the extent (1, 2, or 3) of printed information, with 2 being a good choice for most calculations
- (2) IYEAR, which specifies the year in the solar cycle to be used (solar maxima for the years 1958, 1970, 1981, and 1989 and solar minima for the years 1965, 1977, and 1986)

b. In subroutine MATTER, the following arrays and variables must be defined:

- (1) Dimension of array XAL, which specifies the depth in the aluminum shield where dosimetric quantities are to be calculated and printed. The depth within the aluminum shield is determined by summing the elements of array XAL. For example, if XAL has a dimension of 3 and is defined in the data statement as DATA XAL/5,5,10/, the transport calculation results will be printed for the following depths of the shield material:

(a) Depth 1: $XAL(1) = 5 \text{ g/cm}^2$

(b) Depth 2: $XAL(1) + XAL(2) = 5 + 5 = 10 \text{ g/cm}^2$

(c) Depth 3: $XAL(1) + XAL(2) + XAL(3) = 5 + 5 + 10 = 20 \text{ g/cm}^2$

- (2) Dimension of array XWAT. The discussion in paragraph 1.b.(1) also applies to the array XWAT for water.

Note that for the shield and target material the particle fields are transported and calculated by default in steps of $H=1 \text{ g/cm}^2$ throughout the program, and the discussion in paragraphs 1.b.(1) and 1.b.(2) refers only to the depths for which data are to be printed.

- (3) Variables NTOT1 and NTOT2 must be equal to the dimensions of XAL and XWAT arrays, respectively. For example, if XAL has dimension 3 and XWAT has dimension 5, then NTOT1 and NTOT2 are defined by

```
DATA NTOT1,NTOT2/3,5/
```

- (4) The following physical properties of the shield and target material are included: NAT is the number of elements in the shield or target—NAT=1 for aluminum, NAT=2 for water, DN is the overall density of the shield or target in g/cm³, ATRG is the atomic mass number of each element of the shield or target, ZTRG is the atomic charge number of each element of the shield or target, and DENSTRG is the number of atoms/g of each element of the shield or target. DENSTRG is calculated from

$$\text{DENSTRG}(I) = [N0 * R(I)] / \text{SUM}[R(I) * \text{ATRG}(I)]$$

where N0 is the Avogadro number taken as 6.023E23 atoms/gram-atom, R(I) is the number of atoms/molecule, and ATRG(I) is the mass in gram/gram-atom of the Ith element in the shield or target. For a simple material like aluminum, DENSTRG becomes

$$\text{DENSTRG}(1) = (6.023\text{E}23 * 1) / (1 * 27.0) = 2.23\text{E}22 \text{ (for Al)}$$

For a compound material like water, DENSTRG becomes

$$\text{DENSTRG}(1) = (6.023\text{E}23 * 2) / (2 * 1.008 + 1 * 16.0) = 6.68\text{E}22 \text{ (for H)}$$

$$\text{DENSTRG}(2) = (6.023\text{E}23 * 1) / (2 * 1.008 + 1 * 16.0) = 3.34\text{E}22 \text{ (for O)}$$

Note that only 3 significant figures are retained for compatibility with the generated data files. Also, note that arrays ATRG, ZTRG, and DENSTRG currently have a dimensional limit of 5. For a more complex material with NAT>5, the dimensions of ATRG, ZTRG, and DENSTRG must be adjusted appropriately.

- (5) The transport of chosen particles in the shield or target is represented by a user-provided isotope table that is defined in function TS. The arrays APRO and ZPRO in common block PROJ contain the mass and charge numbers of transported isotopes. The isotope table can be changed by choosing a different table or, if more or less than 59 isotopes are needed, by adjusting variable IJ=59 in the PARAMETER statement throughout the codes to reflect a larger or smaller isotope table.

2. ATOMIC.DAT is the energy, range, and stopping-power database for water and aluminum. For any other material, the source code will automatically generate a file called NEWRMAT.DAT during execution. This file should be appended to the ATOMIC.DAT master data file for future transport runs. Note that DENSTRG format is E12.3, which permits only three significant figures.

3. NUCLEAR.DAT is the absorption and fragmentation cross-section database for water and aluminum. For any other material, the source code will automatically generate a file called NEWNUC59.DAT during execution. This file should be appended to the NUCLEAR.DAT master data file for future transport runs. Note that DENSTRG format is E12.3, which permits only three significant figures.

4. JSCCOSMC.DAT is the environmental model database taken from references 42 and 43 for the solar maxima for the years 1958, 1970, 1981, and 1989 and solar minima for the years 1965, 1977, and 1986.

A3. Compiler Dependencies

Besides the usual compiler-dependent OPEN and REAL*8 statements, which must be checked by the HZEALH2O.FOR code user, the source code has one compiler-dependent feature in subroutine QXZ061, which must be modified if this code is to be run on a non-VAX platform. In QXZ061,

variables `THIRD` and `SIXTH` are defined in OCTAL format and must be modified to conform with a non-VAX compiler octal number format. Besides these trivial changes, the rest of the source code should run on any platform with a FORTRAN compiler.

A4. Program Execution

To provide the users of `HZEALH2O.FOR` with a detailed description of a typical run, the following input conditions are used to generate the sample output given in appendix B:

1. `IPRGCR=2`
2. `IYEAR=4` (1977 solar minimum)
3. `XAL(3)=5, 5, 10` (aluminum depths of 5, 10, and 20 g/cm²)
4. `XWAT(5)=1, 1, 1, 1, 1` (water depths of 1, 2, 3, 4, and 5 g/cm²)

The sample output is divided into 36 blocks (`A, . . . , Z` and `AA, . . . , JJ`). Each block includes a brief description of the flow of the program and how to interpret the output.

Block A prints the values of the physical properties (mass, charge, density, etc.) of the target material, which in almost all cases is water. These quantities are used in the function `RTIS`. In `RTIS` the input data file `ATOMIC.DAT` is accessed to see if it contains the energy, range, and stopping power of the chosen target material. This is accomplished by comparing the supplied physical properties of the target with those available in `ATOMIC.DAT`. If the physical properties are the same, then the energy, range, and stopping-power arrays are loaded from `ATOMIC.DAT`. If `ATOMIC.DAT` does not have the information for the target of interest, then a host of other subroutines and functions are called to generate the appropriate energy, range, and stopping-power arrays. This new information is written into the file `NEWRTIS.DAT`. The user has the responsibility to append `NEWRTIS.DAT` to `ATOMIC.DAT` after the program execution for future use. The user is then informed that all appropriate arrays in `RTIS` are initialized, and the message `RTIS IS INITIALIZED` is printed.

Next, the user is informed that the 1977 solar minimum is chosen as the environmental model. The program searches the input data file `JSCCOSMC.DAT` to load and scale the flux arrays in `HZEALH2O.FOR` for later transport calculations.

Then, the program reads the physical properties (same quantities as previously read in `RTIS`) of the shield material from subroutine `MATTER`. The subroutine `MATTER`, as discussed previously, is the only module that the user has to modify to accommodate new shield and target materials. Once the shield material information is read from `MATTER`, the information concerning the transported particle field absorption and fragmentation cross sections for the shield material is read from the input data file `NUCLEAR.DAT`. This is accomplished by calling function `TS`. In `TS`, as in `RTIS`, the physical properties of the aluminum shield material are compared with those available in `NUCLEAR.DAT`. If the physical properties are the same, then the absorption and fragmentation cross-section arrays are loaded from `NUCLEAR.DAT`. If `NUCLEAR.DAT` does not have the information for the shield material of interest, then a host of other subroutines and functions are called to generate the appropriate cross-section arrays. This information is written into the file `NEWNUC59.DAT`. As in `RTIS`, the user has the responsibility to append `NEWNUC59.DAT` to `NUCLEAR.DAT` for future runs. The user is then informed that all appropriate cross-section arrays are initialized and the message `MATERIAL FOR TS 1 FOUND ON NUCLEAR.DAT FILE` is printed.

The physical properties of the shield material are used in function `RMAT` to load energy, range, and stopping-power arrays for the shield material from input data file `ATOMIC.DAT`. `RMAT` is identical to `RTIS`, except that it is designed to calculate or load the energy, range, and stopping-power arrays for shield material rather than for target material. As in `RTIS`, if the `ATOMIC.DAT` does not have the information for the shield material, a new file called `NEWRMAT.DAT` is generated which will have to be

appended to ATOMIC.DAT for future runs. Finally, when all appropriate arrays in RMAT are initialized, the message RMAT IS INITIALIZED is printed.

Block B contains the depth values of the shield material in g/cm^2 at which transported quantities are printed. The first depth value corresponds to the free-space boundary or $X=0 \text{ g/cm}^2$. The quantities for the transported particles are atomic mass, atomic charge, integral flux for a given isotope in particles/ $\text{cm}^2\text{-yr}$, dose in cGy, and dose equivalent in cSv according to the International Commission on Radiological Protection ICRP-26 and ICRP-60 guidelines are printed for charge $Z=0$ to $Z=28$. Note that dose and dose equivalent can be easily converted to engineering units by the following:

$$1 \text{ rad} = 1 \text{ centiGray (cGy)} = 0.01 \text{ Gy}$$

$$1 \text{ rem} = 1 \text{ centiSievert (cSv)} = 0.01 \text{ Sv}$$

Then, the minimum and maximum energy, $A \text{ MeV}$, and range, g/cm^2 , that were used to calculate the previous flux quantities are printed.

Block C prints the cumulative integral flux and dosimetric values at the depths of the shield material that correspond to the same depths as block B. The cumulative transported quantities are grouped into six charge groups of $Z=0$, $Z=1$, $Z=2$, $3 \leq Z \leq 10$, $11 \leq Z \leq 20$, and $21 \leq Z \leq 28$. The units for integral flux, dose, and dose equivalents are the same as for block B.

Then, the total cumulative integral flux and dosimetric values for all six charge groups are printed.

Block D contains the depth values of shield material at which transport quantities are calculated and stored. The depth increment is set by default to $H=1 \text{ g/cm}^2$. The printing of depth values stops when the first depth of the shield material as defined in subroutine MATTER is reached.

Blocks E, H, and K are similar to block B.

Blocks F, I, and L are similar to block C.

Blocks G and J are similar to block D. At this stage, calculations for the aluminum shield material are complete and the program begins to read information for the target material.

Block M prints the values of the physical properties (mass, charge, density, etc.) of the target material, as defined in subroutine MATTER. These quantities are used in function RMAT. As described in the second half of block A, these physical properties are compared with those available in the input data file ATOMIC.DAT, and the appropriate arrays for energy, range, and stopping power are either loaded from ATOMIC.DAT or calculated and stored in NEWRMAT.DAT. As in block A, the user has the responsibility to append NEWRMAT.DAT to ATOMIC.DAT after the program execution for future use.

Blocks N, Q, S, U, W, and Y are similar to block B.

Blocks O, R, T, V, X, and Z are similar to block C.

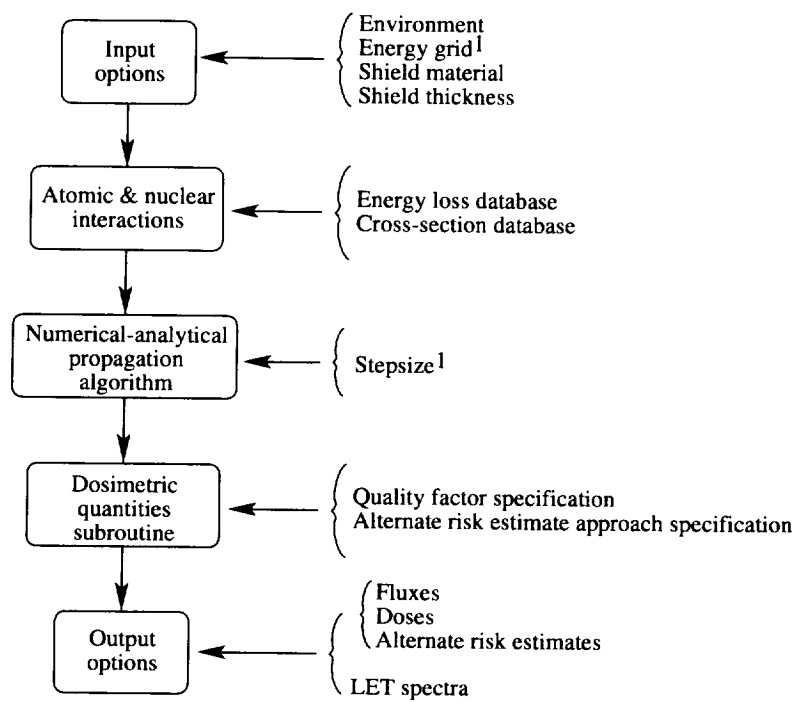
Block P is similar to block D. At this stage, calculations for the water target material are complete and the program begins the stopping-power calculations for the shield and target materials.

Block AA is the start of the printed transported quantities as a function of stopping power $S=\text{LET}$. It contains the depth values of the shield material in g/cm^2 , at which the transported quantities are calculated. The first depth value corresponds to the free-space boundary at $X=0 \text{ g/cm}^2$. The printed quantities for the transported particles are LET in $\text{MeV}/(\text{g/cm}^2)$, integral flux at a given LET in particles/ $\text{cm}^2 \text{ yr}$, dose in cGy, and dose equivalent in cSv to ICRP-26 and ICRP-60 guidelines.

Blocks BB, CC, and DD are similar to block AA. The printed quantities in blocks AA, . . . , DD are LET-related quantities in the shield material.

Block EE prints the transported quantities as a function of LET for the target material at a target depth of $X=0 \text{ g/cm}^2$.

Blocks FF, GG, HH, II, and JJ are similar to block EE.



¹Designates semiflexible inputs.

Figure A1. Computational structure of HZETRN.

Appendix B

HZETRN Computer Code Sample Output

```

<-----
1.000      2
1.000    16.000      0.000      0.000      0.000
1.0      8.0      0.0      0.0      0.0
0.668E+23  0.334E+23  0.000E+00  0.000E+00  0.000E+00

RTIS FOUND      2 ELEMENTS OF CHARGE      1.000000      8.000000
MATERIAL FOR RTIS      2 FOUND ON ATOMIC.DAT FILE
THERE ARE      2 ELEMENTS OF CHARGES      1.000000      8.000000
RTIS IS INITIALIZED

1977      SOLAR MINIMUM IS CHOSEN

TS FOUND      2 ELEMENTS OF CHARGE      1.000000      8.000000
TS FOUND      1 ELEMENTS OF CHARGE      13.000000

MATERIAL FOR TS      1 FOUND ON NUCLEAR.DAT FILE
THERE ARE      1 ELEMENTS OF CHARGES      13.000000

1.000      2
1.000    16.000      0.000      0.000      0.000
1.0      8.0      0.0      0.0      0.0
0.668E+23  0.334E+23  0.000E+00  0.000E+00  0.000E+00

RMAT FOUND      2 ELEMENTS OF CHARGE      1.000000      8.000000

2.700      1
27.000      0.000      0.000      0.000      0.000
13.0      0.0      0.0      0.0      0.0
0.223E+23  0.000E+00  0.000E+00  0.000E+00  0.000E+00

RMAT FOUND      1 ELEMENTS OF CHARGE      13.000000
MATERIAL FOR RMAT      1 FOUND ON ATOMIC.DAT FILE
THERE ARE      1 ELEMENTS OF CHARGES      13.000000
RMAT IS INITIALIZED

X=  0.000 IN NLAY=      1 XLAY=  5.000 XTOT=  0.000

      A      Z      FLUX      DOSE      DOSE EQ.(26)      DOSE EQ.(60)
1.00      0.00      0.00000E+00  0.00000E+00  0.00000E+00  0.00000E+00
1.00      1.00      0.17841E+09  0.77503E+01  0.93698E+01  0.93457E+01
2.00      1.00      0.50007E-13  0.19301E-20  0.26842E-20  0.27186E-20

```

3.00	1.00	0.50007E-13	0.19374E-20	0.28056E-20	0.28400E-20
3.00	2.00	0.50007E-13	0.76025E-20	0.94841E-20	0.96518E-20
4.00	2.00	0.16392E+08	0.34543E+01	0.43032E+01	0.41057E+01
6.00	3.00	0.17324E-12	0.57729E-19	0.61718E-19	0.61620E-19
7.00	3.00	0.10894E+06	0.52334E-01	0.84889E-01	0.76320E-01
8.00	4.00	0.12993E-12	0.76862E-19	0.84780E-19	0.80875E-19
9.00	4.00	0.58104E+05	0.49576E-01	0.11394E+00	0.98781E-01
10.00	5.00	0.10394E-12	0.96006E-19	0.15775E-18	0.10093E-18
11.00	5.00	0.15847E+06	0.21116E+00	0.69319E+00	0.59601E+00
12.00	6.00	0.51917E+06	0.10098E+01	0.44333E+01	0.40285E+01
13.00	6.00	0.93838E-13	0.12476E-18	0.28551E-18	0.13239E-18
14.00	7.00	0.13295E+06	0.33513E+00	0.17810E+01	0.17296E+01
15.00	7.00	0.79549E-13	0.14391E-18	0.43393E-18	0.21232E-18
16.00	8.00	0.47594E+06	0.16389E+01	0.10900E+02	0.11914E+02
17.00	8.00	0.69025E-13	0.16307E-18	0.62119E-18	0.42139E-18
18.00	9.00	0.57746E-13	0.17263E-18	0.80397E-18	0.66289E-18
19.00	9.00	0.99335E+04	0.42220E-01	0.32371E+00	0.37562E+00
20.00	10.00	0.75894E+05	0.39821E+00	0.34977E+01	0.42672E+01
21.00	10.00	0.54570E-13	0.20138E-18	0.11170E-17	0.10557E-17
22.00	10.00	0.57169E-13	0.21098E-18	0.11702E-17	0.11061E-17
23.00	11.00	0.16720E+05	0.10614E+00	0.10478E+01	0.13265E+01
24.00	12.00	0.99764E+05	0.75113E+00	0.81832E+01	0.10647E+02
25.00	12.00	0.45114E-13	0.23971E-18	0.17755E-17	0.20335E-17
26.00	12.00	0.46919E-13	0.24930E-18	0.18466E-17	0.21149E-17
27.00	13.00	0.17539E+05	0.15551E+00	0.18551E+01	0.24642E+01
28.00	14.00	0.72668E+05	0.75723E+00	0.98219E+01	0.13339E+02
29.00	15.00	0.38357E+04	0.45275E-01	0.62425E+00	0.84808E+00
30.00	16.00	0.30452E-13	0.28760E-18	0.32319E-17	0.48006E-17
31.00	16.00	0.31467E-13	0.29719E-18	0.33396E-17	0.49606E-17
32.00	16.00	0.15412E+05	0.20627E+00	0.30125E+01	0.41096E+01
33.00	17.00	0.29672E-13	0.31635E-18	0.38552E-17	0.60421E-17
34.00	18.00	0.27269E-13	0.32593E-18	0.42778E-17	0.70550E-17
35.00	17.00	0.30908E+04	0.46838E-01	0.72232E+00	0.99548E+00
36.00	18.00	0.28873E-13	0.34510E-18	0.45295E-17	0.74700E-17
37.00	19.00	0.26634E-13	0.35468E-18	0.49836E-17	0.86293E-17
38.00	18.00	0.57401E+04	0.97518E-01	0.15759E+01	0.21556E+01
39.00	19.00	0.39739E+04	0.75221E-01	0.12664E+01	0.17111E+01
40.00	20.00	0.83798E+04	0.16763E+00	0.26833E+01	0.39329E+01
41.00	20.00	0.26636E-13	0.39302E-18	0.58606E-17	0.10670E-16
42.00	20.00	0.27285E-13	0.40261E-18	0.60240E-17	0.10930E-16
43.00	21.00	0.18545E+04	0.42882E-01	0.77172E+00	0.99891E+00
44.00	22.00	0.23624E-13	0.42177E-18	0.70593E-17	0.11969E-16
45.00	22.00	0.24160E-13	0.43135E-18	0.72197E-17	0.12241E-16
46.00	22.00	0.24697E-13	0.44094E-18	0.73802E-17	0.12513E-16
47.00	22.00	0.64907E+04	0.16472E+00	0.30444E+01	0.37885E+01

0.23579E-13	0.46011E-18	0.80973E-17	0.12489E-16
0.30908E+04	0.85730E-01	0.16210E+01	0.18861E+01
0.22557E-13	0.47927E-18	0.88389E-17	0.12467E-16
0.23008E-13	0.48886E-18	0.90157E-17	0.12717E-16
0.61817E+04	0.18669E+00	0.35982E+01	0.39361E+01
0.22036E-13	0.50803E-18	0.97881E-17	0.12687E-16
0.44155E+04	0.14470E+00	0.28327E+01	0.29287E+01
0.21142E-13	0.52719E-18	0.10455E-16	0.12659E-16
0.39904E+05	0.13506E+01	0.26719E+02	0.26959E+02
0.13567E+03	0.49521E-02	0.98950E-01	0.95185E-01
0.19952E+04	0.78319E-01	0.15664E+01	0.14516E+01

```
EMIN,EMAX= 0.1000E-01 0.5000E+05
RMIN,RMAX= 0.29827E-04 0.21716E+05
```

RELEVANT QUANTITIES AT X= 0.000 FOLLOW

```

FOR Z=0 FNU1,DNU1,HNUT(26),HNUT(60)= 0.000E+00 0.000E+00 0.000E+00 0.000E+00
FOR Z=1 FPDT,DPDT,HPDT(26),HPDT(60)= 0.178E+09 0.775E+01 0.937E+01 0.935E+01
FOR Z=2 FALP,DALP,HALP(26),HALP(60)= 0.164E+08 0.345E+01 0.430E+01 0.411E+01
FOR 3<=Z<=10 FLIT,DLIT,HLIT(26),HLIT(60)= 0.154E+07 0.374E+01 0.218E+02 0.231E+02
FOR 11<=Z<=20 FMED,DMED,HMED(26),HMED(60)= 0.247E+06 0.241E+01 0.310E+02 0.415E+02
FOR 21<=Z<=28 FHVY,DHVY,HHVY(26),HHVY(60)= 0.641E+05 0.206E+01 0.403E+02 0.420E+02

```

TOTALS FLUX, DOSE, HD0SE(26), HD0SE(60) = 0.197E+09 0.194E+02 0.107E+03 0.120E+03 <

1
CALCULATE TRANSPORT COEFFICIENT OF LAYER= 1
1 BEGIN TRANSPORT IN NLAY= 1 FROM X= 0.000 TO XTOT= 5.000
WITH XLAY= 5.000 IN STEPS OF H= 1.000

X=	1.000	IN	NLAY=	1	XLAY=	5.000	XTOT=	5.000
X=	2.000	IN	NLAY=	1	XLAY=	5.000	XTOT=	5.000
X=	3.000	IN	NLAY=	1	XLAY=	5.000	XTOT=	5.000
X=	4.000	IN	NLAY=	1	XLAY=	5.000	XTOT=	5.000
X=	5.000	IN	NLAY=	1	XLAY=	5.000	XTOT=	5.000

A	Z	FLUX	DOSE.	DOSE EQ. (26)	DOSE EQ. (60)
1.00	0.00	0.41116E+08	0.30709E-01	0.61807E+00	0.61807E+00
1.00	1.00	0.19038E+09	0.11071E+02	0.15369E+02	0.15251E+02
1.00	1.00	0.49064E+06	0.36974E+00	0.13705E+01	0.14163E+01
1.00	1.00	0.21916E+06	0.10003E+00	0.44412E+00	0.49481E+00
2.00	2.00	0.56899E+05	0.49823E-01	0.39996E+00	0.50464E+00
2.00	2.00	0.14818E+08	0.34186E+01	0.79783E+01	0.89723E+01
3.00	3.00	0.59425E+04	0.28866E-02	0.50940E-02	0.47353E-02
3.00	3.00	0.98992E+05	0.47732E-01	0.83630E-01	0.77754E-01

8.00	0.18952E+04	0.16337E-02	0.40377E-02	0.36209E-02
9.00	0.53319E+05	0.45492E-01	0.11092E+00	0.99410E-01
10.00	0.79655E+04	0.10724E-01	0.37178E-01	0.32613E-01
11.00	0.13859E+06	0.18375E+00	0.62522E+00	0.54569E+00
12.00	0.42961E+06	0.82968E+00	0.37329E+01	0.33843E+01
13.00	0.53138E+04	0.10155E-01	0.45383E-01	0.41083E-01
14.00	0.11312E+06	0.28043E+00	0.14750E+01	0.13886E+01
15.00	0.46715E+04	0.12113E-01	0.67187E-01	0.65371E-01
16.00	0.37717E+06	0.12791E+01	0.85122E+01	0.90763E+01
17.00	0.21494E+04	0.71096E-02	0.46323E-01	0.48873E-01
18.00	0.14429E+04	0.60168E-02	0.45645E-01	0.51476E-01
19.00	0.98591E+04	0.40940E-01	0.30933E+00	0.34830E+00
20.00	0.59208E+05	0.30146E+00	0.25875E+01	0.30636E+01
21.00	0.13691E+04	0.70375E-02	0.60937E-01	0.72362E-01
22.00	0.87815E+03	0.45116E-02	0.39035E-01	0.46343E-01
23.00	0.15207E+05	0.93593E-01	0.90139E+00	0.11118E+01
24.00	0.74832E+05	0.54242E+00	0.57332E+01	0.72969E+01
25.00	0.79455E+03	0.58929E-02	0.63379E-01	0.80982E-01
26.00	0.72141E+03	0.53316E-02	0.57165E-01	0.73059E-01
27.00	0.14144E+05	0.12059E+00	0.13962E+01	0.18256E+01
28.00	0.52918E+05	0.53396E+00	0.67749E+01	0.90637E+01
29.00	0.31299E+04	0.35101E-01	0.46795E+00	0.63527E+00
30.00	0.12347E+01	0.15700E-04	0.22231E-03	0.30567E-03
31.00	0.94977E+02	0.12073E-02	0.17095E-01	0.23477E-01
32.00	0.11492E+05	0.14599E+00	0.20663E+01	0.28389E+01
33.00	0.50711E+02	0.73053E-03	0.10957E-01	0.15186E-01
34.00	0.51582E+01	0.82466E-04	0.12936E-02	0.18010E-02
35.00	0.27960E+04	0.40735E-01	0.61443E+00	0.84909E+00
36.00	0.16276E+03	0.26086E-02	0.40966E-01	0.56988E-01
37.00	0.42494E+02	0.76021E-03	0.12488E-01	0.17298E-01
38.00	0.43081E+04	0.70444E-01	0.11163E+01	0.15414E+01
39.00	0.30711E+04	0.55663E-01	0.91921E+00	0.12652E+01
40.00	0.57759E+04	0.11118E+00	0.18793E+01	0.26246E+01
41.00	0.52740E+02	0.10371E-02	0.17665E-01	0.24341E-01
42.00	0.42168E+03	0.82959E-02	0.14133E+00	0.19466E+00
43.00	0.16036E+04	0.35268E-01	0.62477E+00	0.83747E+00
44.00	0.81960E+01	0.19449E-03	0.35343E-02	0.46314E-02
45.00	0.32542E+02	0.77315E-03	0.14054E-01	0.18398E-01
46.00	0.26371E+03	0.62601E-02	0.11377E+00	0.14905E+00
47.00	0.45567E+04	0.11027E+00	0.20137E+01	0.25972E+01
48.00	0.12798E+03	0.33020E-02	0.61565E-01	0.75441E-01
49.00	0.23772E+04	0.62586E-01	0.11717E+01	0.14138E+01
50.00	0.95773E+02	0.26879E-02	0.51280E-01	0.58878E-01
51.00	0.20058E+03	0.56081E-02	0.10694E+00	0.12313E+00
52.00	0.42138E+04	0.12083E+00	0.23127E+01	0.26155E+01

53.00	25.00	0.24588E+03	0.74221E-02	0.14428E+00	0.15688E+00	
54.00	25.00	0.31977E+04	0.98915E-01	0.19273E+01	0.20624E+01	
55.00	26.00	0.30733E+03	0.97452E-02	0.19227E+00	0.20151E+00	
56.00	26.00	0.25601E+05	0.82459E+00	0.16281E+02	0.16892E+02	
57.00	27.00	0.98891E+02	0.34226E-02	0.68376E-01	0.67660E-01	
58.00	28.00	0.12613E+04	0.46802E-01	0.93602E+00	0.89380E+00	
EMIN,EMAX= 0.10000E-01 0.50000E+05						
RMIN,RMAX= 0.29827E-04 0.21716E+05						
RELEVANT QUANTITIES AT X= 5.000 FOLLOW						
FOR Z=0 FNUT,DNUT,HNUT(26),HNUT(60)= 0.411E+08 0.307E-01 0.618E+00 0.618E+00						
FOR Z=1 FPD,DPDT,HPDT(26),HPDT(60)= 0.191E+09 0.115E+02 0.172E+02 0.172E+02						
FOR Z=2 FALP,DALP,HALP(26),HALP(60)= 0.149E+08 0.347E+01 0.838E+01 0.948E+01						
FOR 3<=Z<=10 FLIT,DLIT,HLIT(26),HLIT(60)= 0.131E+07 0.307E+01 0.178E+02 0.184E+02						
FOR 11<=Z<=20 FMED,DMED,HMED(26),HMED(60)= 0.190E+06 0.178E+01 0.222E+02 0.295E+02						
FOR 21<=Z<=28 FHVY,DHVY,HHVY(26),HHVY(60)= 0.442E+05 0.134E+01 0.260E+02 0.282E+02						
TOTALS FLUX,DOSE,HD0SE(26),HD0SE(60)= 0.249E+09 0.212E+02 0.922E+02 0.103E+03						
X= 6.000 IN NLAY= 1 XLAY= 5.000 XTOT= 10.000						
X= 7.000 IN NLAY= 1 XLAY= 5.000 XTOT= 10.000						
X= 8.000 IN NLAY= 1 XLAY= 5.000 XTOT= 10.000						
X= 9.000 IN NLAY= 1 XLAY= 5.000 XTOT= 10.000						
X= 10.000 IN NLAY= 1 XLAY= 5.000 XTOT= 10.000						
A Z FLUX DOSE DOSE EQ.(26) DOSE EQ.(60)						
1.00	0.00	0.78412E+08	0.58211E-01	0.11702E+01	0.11702E+01	
1.00	1.00	0.19580E+09	0.12347E+02	0.17116E+02	0.16959E+02	
2.00	1.00	0.65564E+06	0.38928E+00	0.14446E+01	0.15030E+01	
3.00	1.00	0.35456E+06	0.11622E+00	0.48846E+00	0.54669E+00	
3.00	2.00	0.92769E+05	0.62425E-01	0.43951E+00	0.54996E+00	
4.00	2.00	0.13352E+08	0.31034E+01	0.78035E+01	0.88879E+01	
6.00	3.00	0.10178E+05	0.48514E-02	0.83571E-02	0.77807E-02	
7.00	3.00	0.89633E+05	0.42696E-01	0.73687E-01	0.68604E-01	
8.00	4.00	0.32062E+04	0.27017E-02	0.64501E-02	0.57644E-02	
9.00	4.00	0.48683E+05	0.40886E-01	0.97205E-01	0.86882E-01	
10.00	5.00	0.13238E+05	0.17397E-01	0.58267E-01	0.50424E-01	
11.00	5.00	0.12122E+06	0.15764E+00	0.52102E+00	0.44933E+00	
12.00	6.00	0.35702E+06	0.67461E+00	0.29517E+01	0.26341E+01	
13.00	6.00	0.87086E+04	0.16204E-01	0.69878E-01	0.61965E-01	
14.00	7.00	0.96645E+05	0.23512E+00	0.12061E+01	0.11168E+01	
15.00	7.00	0.75277E+04	0.18966E-01	0.10157E+00	0.96727E-01	
16.00	8.00	0.30154E+06	0.99511E+00	0.64261E+01	0.67528E+01	

17.00	0.34483E+04	0.11029E-01	0.69068E-01	0.71433E-01
18.00	0.22972E+04	0.92492E-02	0.67525E-01	0.74983E-01
19.00	0.94594E+04	0.38067E-01	0.27779E+00	0.30843E+00
20.00	0.46950E+05	0.23124E+00	0.19184E+01	0.22472E+01
21.00	0.21356E+04	0.10578E-01	0.88245E-01	0.10355E+00
22.00	0.13710E+04	0.67941E-02	0.56687E-01	0.66533E-01
23.00	0.13687E+05	0.81412E-01	0.75931E+00	0.92985E+00
24.00	0.57385E+05	0.40104E+00	0.41062E+01	0.52042E+01
25.00	0.12064E+04	0.86020E-02	0.89519E-01	0.11388E+00
26.00	0.10929E+04	0.77756E-02	0.80760E-01	0.10273E+00
27.00	0.11567E+05	0.95204E-01	0.10705E+01	0.13993E+01
28.00	0.39456E+05	0.38300E+00	0.47313E+01	0.63444E+01
29.00	0.26089E+04	0.28054E-01	0.36374E+00	0.49761E+00
30.00	0.23964E+01	0.29193E-04	0.40292E-03	0.56056E-03
31.00	0.14193E+03	0.17287E-02	0.23860E-01	0.33174E-01
32.00	0.86631E+04	0.10796E+00	0.14901E+01	0.20725E+01
33.00	0.77772E+02	0.10738E-02	0.15747E-01	0.22180E-01
34.00	0.84890E+01	0.12997E-03	0.19973E-02	0.28406E-02
35.00	0.24838E+04	0.34618E-01	0.51025E+00	0.71697E+00
36.00	0.23744E+03	0.36472E-02	0.56139E-01	0.79740E-01
37.00	0.62781E+02	0.10751E-02	0.17348E-01	0.24660E-01
38.00	0.33222E+04	0.52021E-01	0.80822E+00	0.11397E+01
39.00	0.24380E+04	0.42219E-01	0.68458E+00	0.96787E+00
40.00	0.41128E+04	0.76071E-01	0.12674E+01	0.18203E+01
41.00	0.77932E+02	0.14659E-02	0.24582E-01	0.34932E-01
42.00	0.60063E+03	0.11304E-01	0.18961E+00	0.26933E+00
43.00	0.13811E+04	0.28957E-01	0.50597E+00	0.70381E+00
44.00	0.11794E+02	0.26731E-03	0.48051E-02	0.65410E-02
45.00	0.47198E+02	0.10710E-02	0.19259E-01	0.26189E-01
46.00	0.37050E+03	0.84086E-02	0.15121E+00	0.20560E+00
47.00	0.33317E+04	0.76971E-01	0.13908E+01	0.18631E+01
48.00	0.18000E+03	0.44381E-02	0.82067E-01	0.10416E+00
49.00	0.18760E+04	0.47060E-01	0.87347E+00	0.10937E+01
50.00	0.13322E+03	0.35694E-02	0.67691E-01	0.80369E-01
51.00	0.27565E+03	0.73665E-02	0.13964E+00	0.16612E+00
52.00	0.30071E+04	0.82210E-01	0.15642E+01	0.18302E+01
53.00	0.33618E+03	0.96968E-02	0.18779E+00	0.21056E+00
54.00	0.24038E+04	0.70721E-01	0.13725E+01	0.15187E+01
55.00	0.41674E+03	0.12688E-01	0.24992E+00	0.26878E+00
56.00	0.17165E+05	0.52970E+00	0.10441E+02	0.11131E+02
57.00	0.74467E+02	0.24659E-02	0.49257E-01	0.50045E-01
58.00	0.84061E+03	0.29831E-01	0.59662E+00	0.58502E+00

EMIN,EMAX= 0.10000E-01 0.50000E+05
 RMIN,RMAX= 0.29827E-04 0.21716E+05

RELEVANT QUANTITIES AT X= 10.000 FOLLOW									
<----->									
FOR Z=0 FNUT,DNUT,HNUT(26),HNUT(60)= 0.784E+08 0.582E-01 0.117E+01 0.117E+01 0.117E+01									
FOR Z=1 FPD,DPDT,HPDT(26),HPDT(60)= 0.197E+09 0.129E+02 0.190E+02 0.190E+02 0.190E+02									
FOR Z=2 FALP,DALP,HALP(26),HALP(60)= 0.134E+08 0.317E+01 0.824E+01 0.824E+01 0.944E+01									
FOR 3<=Z<=10 FLIT,DLIT,HLIT(26),HLIT(60)= 0.112E+07 0.251E+01 0.140E+02 0.142E+02 0.142E+02									
FOR 11<=Z<=20 FMED,DMED,HMED(26),HMED(60)= 0.149E+06 0.134E+01 0.163E+02 0.218E+02 0.218E+02									
FOR 21<=Z<=28 FHVY,DHVY,HHVY(26),HHVY(60)= 0.319E+05 0.915E+00 0.177E+02 0.198E+02 0.198E+02									
TOTALS FLUX,D0SE,HD0SE(26),HD0SE(60)= 0.290E+09 0.208E+02 0.764E+02 0.854E+02 0.854E+02									
<----->									
X= 11.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
X= 12.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
X= 13.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
X= 14.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
X= 15.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
X= 16.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
X= 17.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
X= 18.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
X= 19.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
X= 20.000 IN NLAY= 1 XLAY= 10.000 XTOT= 20.000									
<----->									
A Z FLUX D0SE D0SE EQ. (26) D0SE EQ. (60)									
1.00	0.00	0.14270E+09	0.10464E+00	0.20983E+01	0.20983E+01	0.20983E+01	0.20983E+01	0.20983E+01	0.20983E+01
1.00	1.00	0.19925E+09	0.13663E+02	0.18893E+02	0.18893E+02	0.18701E+02	0.18701E+02	0.18701E+02	0.18701E+02
2.00	1.00	0.89981E+06	0.41553E+00	0.15481E+01	0.15481E+01	0.16265E+01	0.16265E+01	0.16265E+01	0.16265E+01
3.00	1.00	0.53087E+06	0.13649E+00	0.54970E+00	0.54970E+00	0.61991E+00	0.61991E+00	0.61991E+00	0.61991E+00
3.00	2.00	0.13411E+06	0.75539E-01	0.48601E+00	0.48601E+00	0.60598E+00	0.60598E+00	0.60598E+00	0.60598E+00
4.00	2.00	0.10845E+08	0.25661E+01	0.74485E+01	0.74485E+01	0.86701E+01	0.86701E+01	0.86701E+01	0.86701E+01
6.00	3.00	0.15120E+05	0.69903E-02	0.11611E-01	0.11611E-01	0.10836E-01	0.10836E-01	0.10836E-01	0.10836E-01
7.00	3.00	0.73237E+05	0.34131E-01	0.57242E-01	0.57242E-01	0.53384E-01	0.53384E-01	0.53384E-01	0.53384E-01
8.00	4.00	0.46586E+04	0.37935E-02	0.85914E-02	0.85914E-02	0.76480E-02	0.76480E-02	0.76480E-02	0.76480E-02
9.00	4.00	0.40321E+05	0.32982E-01	0.75130E-01	0.75130E-01	0.66866E-01	0.66866E-01	0.66866E-01	0.66866E-01
10.00	5.00	0.18590E+05	0.23560E-01	0.74914E-01	0.74914E-01	0.63589E-01	0.63589E-01	0.63589E-01	0.63589E-01
11.00	5.00	0.93161E+05	0.11757E+00	0.37130E+00	0.37130E+00	0.31443E+00	0.31443E+00	0.31443E+00	0.31443E+00
12.00	6.00	0.25020E+06	0.45665E+00	0.19107E+01	0.19107E+01	0.16617E+01	0.16617E+01	0.16617E+01	0.16617E+01
13.00	6.00	0.11933E+05	0.21347E-01	0.87304E-01	0.87304E-01	0.75022E-01	0.75022E-01	0.75022E-01	0.75022E-01
14.00	7.00	0.71085E+05	0.16807E+00	0.83046E+00	0.83046E+00	0.74930E+00	0.74930E+00	0.74930E+00	0.74930E+00
15.00	7.00	0.10008E+05	0.24168E-01	0.12278E+00	0.12278E+00	0.11295E+00	0.11295E+00	0.11295E+00	0.11295E+00
16.00	8.00	0.19720E+06	0.62410E+00	0.38438E+01	0.38438E+01	0.39414E+01	0.39414E+01	0.39414E+01	0.39414E+01
17.00	8.00	0.45758E+04	0.13980E-01	0.82811E-01	0.82811E-01	0.83089E-01	0.83089E-01	0.83089E-01	0.83089E-01
18.00	9.00	0.30115E+04	0.11566E-01	0.80055E-01	0.80055E-01	0.86812E-01	0.86812E-01	0.86812E-01	0.86812E-01
19.00	9.00	0.82418E+04	0.31717E-01	0.22003E+00	0.22003E+00	0.23888E+00	0.23888E+00	0.23888E+00	0.23888E+00
20.00	10.00	0.30461E+05	0.14344E+00	0.11351E+01	0.11351E+01	0.13071E+01	0.13071E+01	0.13071E+01	0.13071E+01

21.00	10.00	0.26987E+04	0.12720E-01	0.10073E+00	0.11601E+00
22.00	10.00	0.17327E+04	0.81777E-02	0.64848E-01	0.74735E-01
23.00	11.00	0.10857E+05	0.61613E-01	0.54899E+00	0.66390E+00
24.00	12.00	0.35070E+05	0.23362E+00	0.22901E+01	0.28787E+01
25.00	12.00	0.14555E+04	0.98419E-02	0.97740E-01	0.12327E+00
26.00	12.00	0.13110E+04	0.88525E-02	0.87802E-01	0.11072E+00
27.00	13.00	0.79600E+04	0.62283E-01	0.67251E+00	0.87619E+00
28.00	14.00	0.23042E+05	0.21170E+00	0.25113E+01	0.33729E+01
29.00	15.00	0.18598E+04	0.18979E-01	0.23716E+00	0.32669E+00
30.00	16.00	0.41030E+01	0.47411E-04	0.63264E-03	0.89097E-03
31.00	16.00	0.16744E+03	0.19350E-02	0.25822E-01	0.36361E-01
32.00	16.00	0.55503E+04	0.64191E-01	0.85706E+00	0.12071E+01
33.00	17.00	0.96391E+02	0.12631E-02	0.17981E-01	0.25779E-01
34.00	18.00	0.11756E+02	0.17099E-03	0.25593E-02	0.37251E-02
35.00	17.00	0.19063E+04	0.25137E-01	0.35916E+00	0.51418E+00
36.00	18.00	0.26856E+03	0.39182E-02	0.58751E-01	0.85412E-01
37.00	19.00	0.72959E+02	0.11850E-02	0.18675E-01	0.27352E-01
38.00	18.00	0.20779E+04	0.30802E-01	0.46573E+00	0.67322E+00
39.00	19.00	0.16048E+04	0.26277E-01	0.41571E+00	0.60650E+00
40.00	20.00	0.22089E+04	0.38955E-01	0.63680E+00	0.94522E+00
41.00	20.00	0.90465E+02	0.16149E-02	0.26535E-01	0.39081E-01
42.00	20.00	0.65081E+03	0.11628E-01	0.19112E+00	0.28132E+00
43.00	21.00	0.10098E+04	0.20009E-01	0.34328E+00	0.49925E+00
44.00	22.00	0.13113E+02	0.28179E-03	0.49929E-02	0.71152E-02
45.00	22.00	0.53055E+02	0.11415E-02	0.20234E-01	0.28804E-01
46.00	22.00	0.39188E+03	0.84398E-02	0.14964E+00	0.21285E+00
47.00	22.00	0.19045E+04	0.41622E-01	0.74123E+00	0.10409E+01
48.00	23.00	0.19096E+03	0.44680E-02	0.81703E-01	0.10816E+00
49.00	23.00	0.12049E+04	0.28556E-01	0.52380E+00	0.68617E+00
50.00	24.00	0.13859E+03	0.35218E-02	0.66242E-01	0.81816E-01
51.00	24.00	0.27952E+03	0.70909E-02	0.13333E+00	0.16491E+00
52.00	24.00	0.16443E+04	0.42505E-01	0.80197E+00	0.97790E+00
53.00	25.00	0.33772E+03	0.92490E-02	0.17819E+00	0.20710E+00
54.00	25.00	0.14211E+04	0.39464E-01	0.76159E+00	0.87666E+00
55.00	26.00	0.40911E+03	0.11887E-01	0.23362E+00	0.25889E+00
56.00	26.00	0.82651E+04	0.24288E+00	0.47766E+01	0.52538E+01
57.00	27.00	0.43889E+02	0.13824E-02	0.27608E-01	0.28899E-01
58.00	28.00	0.40316E+03	0.13611E-01	0.27222E+00	0.27492E+00

EMIN,EMAX= 0.10000E-01 0.50000E+05
RMIN,RMAX= 0.29827E-04 0.21716E+05

RELEVANT QUANTITIES AT X= 20.000 FOLLOW

FOR Z=0 FNUT,DNUT,HNUT(26),HNUT(60)= 0.143E+09 0.105E+00 0.210E+01 0.210E+01

FOR Z=1 FPD,DPDT,HPDT(26),HPDT(60)= 0.201E+09 0.142E+02 0.210E+02 0.209E+02
 FOR Z=2 FALP,DALP,HALP(26),HALP(60)= 0.110E+08 0.264E+01 0.793E+01 0.928E+01
 FOR 3<Z<=10 FLIT,DLIT,HLIT(26),HLIT(60)= 0.835E+06 0.173E+01 0.908E+01 0.896E+01
 FOR 11<Z<=20 FMED,DMED(26),HMD(60)= 0.963E+05 0.814E+00 0.952E+01 0.128E+02
 FOR 21<Z<=28 FHVY,DHVV,HHVY(26),HHVY(60)= 0.177E+05 0.476E+00 0.912E+01 0.107E+02

TOTALS FLUX,DOSE,HD0SE(26),HD0SE(60)= 0.355E+09 0.200E+02 0.587E+02 0.648E+02
 TS FOUND 2 ELEMENTS OF CHARGE 1.000000 8.000000

MATERIAL FOR TS 2 FOUND ON NUCLEAR.DAT FILE
 THERE ARE 2 ELEMENTS OF CHARGES 1.000000 8.000000

1.000 2
 1.000 16.000 0.000 0.000 0.000
 1.0 8.0 0.0 0.0 0.0
 0.668E+23 0.334E+23 0.000E+00 0.000E+00 0.000E+00

RMAT FOUND 2 ELEMENTS OF CHARGE 1.000000 8.000000
 MATERIAL FOR RMAT 2 FOUND ON ATOMIC.DAT FILE
 THERE ARE 2 ELEMENTS OF CHARGES 1.000000 8.000000
 RMAT IS INITIALIZED

X= 0.000 IN NLAY= 2 XLAY= 1.000 XTOT= 0.000

A	Z	FLUX	DOSE	DOSE EQ. (26)	DOSE EQ. (60)
1.00	0.00	0.14270E+09	0.10464E+00	0.20983E+01	0.20983E+01
1.00	1.00	0.19925E+09	0.13663E+02	0.18893E+02	0.18701E+02
2.00	1.00	0.89981E+06	0.41553E+00	0.15481E+01	0.16265E+01
3.00	1.00	0.53087E+06	0.13649E+00	0.54970E+00	0.61991E+00
3.00	2.00	0.13411E+06	0.75539E-01	0.48601E+00	0.60598E+00
4.00	2.00	0.10845E+08	0.25661E+01	0.74485E+01	0.86701E+01
6.00	3.00	0.15120E+05	0.69903E-02	0.11611E-01	0.10836E-01
7.00	3.00	0.73237E+05	0.34131E-01	0.57242E-01	0.53384E-01
8.00	4.00	0.46586E+04	0.37935E-02	0.85914E-02	0.76480E-02
9.00	4.00	0.40321E+05	0.32982E-01	0.75130E-01	0.66866E-01
10.00	5.00	0.18590E+05	0.23560E-01	0.74914E-01	0.63589E-01
11.00	5.00	0.93161E+05	0.11757E+00	0.37130E+00	0.31443E+00
12.00	6.00	0.25020E+06	0.45665E+00	0.19107E+01	0.16617E+01
13.00	6.00	0.11933E+05	0.21347E-01	0.87304E-01	0.75022E-01
14.00	7.00	0.71085E+05	0.16807E+00	0.83046E+00	0.74930E+00
15.00	7.00	0.10008E+05	0.24168E-01	0.12278E+00	0.11295E+00
16.00	8.00	0.19720E+06	0.62410E+00	0.38438E+01	0.39414E+01
17.00	8.00	0.45758E+04	0.13980E-01	0.82811E-01	0.83089E-01
18.00	9.00	0.30115E+04	0.11566E-01	0.80055E-01	0.86812E-01
19.00	9.00	0.82418E+04	0.31717E-01	0.22003E+00	0.23888E+00

20.00	10.00	0.30461E+05	0.14344E+00	0.11351E+01	0.13071E+01
21.00	10.00	0.26987E+04	0.12720E-01	0.10073E+00	0.11601E+00
22.00	10.00	0.17327E+04	0.81777E-02	0.64848E-01	0.74735E-01
23.00	11.00	0.10857E+05	0.61613E-01	0.54899E+00	0.66390E+00
24.00	12.00	0.35070E+05	0.23362E+00	0.22901E+01	0.28787E+01
25.00	12.00	0.14555E+04	0.98419E-02	0.97740E-01	0.12327E+00
26.00	12.00	0.13110E+04	0.88525E-02	0.87802E-01	0.11072E+00
27.00	13.00	0.79600E+04	0.62283E-01	0.67251E+00	0.87619E+00
28.00	14.00	0.23042E+05	0.21170E+00	0.25113E+01	0.33729E+01
29.00	15.00	0.18598E+04	0.18979E-01	0.23716E+00	0.32669E+00
30.00	16.00	0.41030E+01	0.47411E-04	0.63264E-03	0.89097E-03
31.00	16.00	0.16744E+03	0.19350E-02	0.25822E-01	0.36361E-01
32.00	16.00	0.55503E+04	0.64191E-01	0.85706E+00	0.12071E+01
33.00	17.00	0.96391E+02	0.12631E-02	0.17981E-01	0.25779E-01
34.00	18.00	0.11758E+02	0.17099E-03	0.25593E-02	0.37251E-02
35.00	17.00	0.19063E+04	0.25137E-01	0.35916E+00	0.51418E+00
36.00	18.00	0.26856E+03	0.39182E-02	0.58751E-01	0.85412E-01
37.00	19.00	0.72959E+02	0.11850E-02	0.18675E-01	0.27352E-01
38.00	18.00	0.20779E+04	0.30802E-01	0.46573E+00	0.67322E+00
39.00	19.00	0.16048E+04	0.26277E-01	0.41571E+00	0.60650E+00
40.00	20.00	0.22089E+04	0.38955E-01	0.63680E+00	0.94522E+00
41.00	20.00	0.90465E+02	0.16149E-02	0.26535E-01	0.39081E-01
42.00	20.00	0.65081E+03	0.11628E-01	0.19112E+00	0.28132E+00
43.00	21.00	0.10098E+04	0.20009E-01	0.34328E+00	0.49925E+00
44.00	22.00	0.13113E+02	0.28179E-03	0.49929E-02	0.71152E-02
45.00	22.00	0.53055E+02	0.11415E-02	0.20234E-01	0.28804E-01
46.00	22.00	0.39188E+03	0.64398E-02	0.14964E+00	0.21285E+00
47.00	22.00	0.19045E+04	0.41622E-01	0.74123E+00	0.10409E+01
48.00	23.00	0.19096E+03	0.44680E-02	0.81703E-01	0.10816E+00
49.00	23.00	0.12049E+04	0.28556E-01	0.52380E+00	0.68617E+00
50.00	24.00	0.13859E+03	0.35218E-02	0.66242E-01	0.81816E-01
51.00	24.00	0.27952E+03	0.70909E-02	0.13333E+00	0.16491E+00
52.00	24.00	0.16443E+04	0.42505E-01	0.80197E+00	0.97790E+00
53.00	25.00	0.33772E+03	0.92490E-02	0.17819E+00	0.20710E+00
54.00	25.00	0.14211E+04	0.39464E-01	0.76159E+00	0.87666E+00
55.00	26.00	0.40911E+03	0.11887E-01	0.23362E+00	0.25889E+00
56.00	26.00	0.82651E+04	0.24288E+00	0.47766E+01	0.52538E+01
57.00	27.00	0.43889E+02	0.13624E-02	0.27608E-01	0.28899E-01
58.00	28.00	0.40316E+03	0.13611E-01	0.27222E+00	0.27492E+00

EMIN,EMAX= 0.10000E-01 0.50000E+05
 RMIN,RMAX= 0.29827E-04 0.21716E+05

RELEVANT QUANTITIES AT X= 0.000 FOLLOW

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FOR Z=0 FNUT,DNUT,HNUT(26),HNUT(60)= 0.143E+09 0.105E+00 0.210E+01 0.210E+01
FOR Z=1 FPD,DPDT,HPDT(26),HPDT(60)= 0.201E+09 0.142E+02 0.210E+02 0.209E+02
FOR Z=2 FALP,DALP,HALP(26),HALP(60)= 0.110E+08 0.264E+01 0.793E+01 0.928E+01
FOR 3<=Z<=10 FLIT,DLIT,HLIT(26),HLIT(60)= 0.836E+06 0.173E+01 0.908E+01 0.896E+01
FOR 11<=Z<=20 FMED,DMED,HMED(26),HMED(60)= 0.963E+05 0.814E+00 0.952E+01 0.128E+02
FOR 21<=Z<=28 FHVY,DHVY,HHVY(26),HHVY(60)= 0.177E+05 0.476E+00 0.912E+01 0.107E+02
TOTALS FLUX,DOSE,HD0SE(26),HD0SE(60)= 0.355E+09 0.200E+02 0.587E+02 0.648E+02 <---

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CALCULATE TRANSPORT COEFFICIENT OF LAYER= 2
BEGIN TRANSPORT IN NLAY= 2 FROM X= 0.000 TO XTOT= 1.000
WITH XLAY= 1.000 IN STEPS OF H= 1.000

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X= 1.000 IN NLAY= 2 XLAY= 1.000 XTOT= 1.000

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A	Z	FLUX	DOSE	DOSE EQ. (26)	DOSE EQ. (60)
1.00	0.00	0.13788E+09	0.98517E-01	0.19622E+01	0.19622E+01
1.00	1.00	0.19806E+09	0.13224E+02	0.17391E+02	0.17016E+02
2.00	1.00	0.80392E+06	0.23694E+00	0.78395E+00	0.78304E+00
3.00	1.00	0.53184E+06	0.75888E-01	0.22983E+00	0.25433E+00
3.00	2.00	0.14146E+06	0.56130E-01	0.22057E+00	0.26551E+00
4.00	2.00	0.10511E+08	0.24427E+01	0.65329E+01	0.76491E+01
6.00	3.00	0.16380E+05	0.75125E-02	0.12196E-01	0.11346E-01
7.00	3.00	0.71273E+05	0.33008E-01	0.54159E-01	0.50345E-01
8.00	4.00	0.62919E+04	0.50618E-02	0.11094E-01	0.98029E-02
9.00	4.00	0.39213E+05	0.31864E-01	0.71007E-01	0.62889E-01
10.00	5.00	0.20154E+05	0.25397E-01	0.79363E-01	0.66928E-01
11.00	5.00	0.89751E+05	0.11248E+00	0.34856E+00	0.29312E+00
12.00	6.00	0.23753E+06	0.43051E+00	0.17730E+01	0.15324E+01
13.00	6.00	0.12391E+05	0.21980E-01	0.88239E-01	0.75190E-01
14.00	7.00	0.68018E+05	0.16005E+00	0.78238E+00	0.70369E+00
15.00	7.00	0.10504E+05	0.25111E-01	0.12535E+00	0.11447E+00
16.00	8.00	0.18432E+06	0.57871E+00	0.35178E+01	0.35986E+01
17.00	8.00	0.47133E+04	0.14272E-01	0.83246E-01	0.83172E-01
18.00	9.00	0.31748E+04	0.12107E-01	0.82889E-01	0.89858E-01
19.00	9.00	0.80499E+04	0.30712E-01	0.21033E+00	0.22800E+00
20.00	10.00	0.28431E+05	0.13285E+00	0.10405E+01	0.11988E+01
21.00	10.00	0.27854E+04	0.13035E-01	0.10220E+00	0.11783E+00
22.00	10.00	0.17592E+04	0.82175E-02	0.64296E-01	0.74064E-01
23.00	11.00	0.10506E+05	0.59184E-01	0.52285E+00	0.63337E+00
24.00	12.00	0.32338E+05	0.21376E+00	0.20785E+01	0.26188E+01
25.00	12.00	0.15042E+04	0.10113E-01	0.99834E-01	0.12628E+00
26.00	12.00	0.13205E+04	0.88230E-02	0.86582E-01	0.10942E+00
27.00	13.00	0.75100E+04	0.58309E-01	0.62520E+00	0.81694E+00
28.00	14.00	0.21087E+05	0.19198E+00	0.22611E+01	0.30489E+01

29.00	15.00	0.17831E+04	0.18026E-01	0.22373E+00	0.30959E+00
30.00	16.00	0.52981E+01	0.59872E-04	0.78730E-03	0.11155E-02
31.00	16.00	0.17572E+03	0.20285E-02	0.27065E-01	0.38129E-01
32.00	16.00	0.51552E+04	0.59075E-01	0.78418E+00	0.11102E+01
33.00	17.00	0.10591E+03	0.13797E-02	0.19584E-01	0.28184E-01
34.00	18.00	0.14213E+02	0.20805E-03	0.31255E-02	0.45293E-02
35.00	17.00	0.18394E+04	0.23998E-01	0.34094E+00	0.49114E+00
36.00	18.00	0.28850E+03	0.42011E-02	0.62975E-01	0.91726E-01
37.00	19.00	0.83506E+02	0.13720E-02	0.21730E-01	0.31601E-01
38.00	18.00	0.19374E+04	0.28388E-01	0.42690E+00	0.62161E+00
39.00	19.00	0.15181E+04	0.24576E-01	0.38702E+00	0.56917E+00
40.00	20.00	0.19764E+04	0.34596E-01	0.56408E+00	0.84239E+00
41.00	20.00	0.96476E+02	0.17090E-02	0.28010E-01	0.41508E-01
42.00	20.00	0.67794E+03	0.11968E-01	0.19591E+00	0.29116E+00
43.00	21.00	0.98409E+03	0.19307E-01	0.33033E+00	0.48457E+00
44.00	22.00	0.14759E+02	0.31629E-03	0.56033E-02	0.80094E-02
45.00	22.00	0.57253E+02	0.12281E-02	0.21761E-01	0.31075E-01
46.00	22.00	0.40402E+03	0.86295E-02	0.15273E+00	0.21888E+00
47.00	22.00	0.17544E+04	0.37990E-01	0.67522E+00	0.95598E+00
48.00	23.00	0.19864E+03	0.46279E-02	0.84585E-01	0.11242E+00
49.00	23.00	0.11335E+04	0.26668E-01	0.48865E+00	0.64413E+00
50.00	24.00	0.14986E+03	0.38211E-02	0.71943E-01	0.88713E-01
51.00	24.00	0.28907E+03	0.73555E-02	0.13841E+00	0.17091E+00
52.00	24.00	0.15004E+04	0.38589E-01	0.72772E+00	0.89115E+00
53.00	25.00	0.35378E+03	0.97628E-02	0.18824E+00	0.21781E+00
54.00	25.00	0.13043E+04	0.35962E-01	0.69362E+00	0.80278E+00
55.00	26.00	0.42335E+03	0.12432E-01	0.24441E+00	0.26903E+00
56.00	26.00	0.71921E+04	0.20969E+00	0.41226E+01	0.45599E+01
57.00	27.00	0.40497E+02	0.12685E-02	0.25334E-01	0.26621E-01
58.00	28.00	0.35137E+03	0.11774E-01	0.23548E+00	0.23902E+00

EMIN,EMAX= 0.10000E-01 0.50000E+05
RMIN,RMAX= 0.29827E-04 0.21716E+05

RELEVANT QUANTITIES AT X= 1.000 FOLLOW

FOR Z=0	FNUT, DNUT, HNUT(26), HNUT(60)=	0.138E+09	0.985E-01	0.196E+01	0.196E+01
FOR Z=1	FPDT, DPDT, HPDT(26), HPDT(60)=	0.199E+09	0.135E+02	0.184E+02	0.181E+02
FOR Z=2	FALP, DALP, HALP(26), HALP(60)=	0.107E+08	0.250E+01	0.675E+01	0.791E+01
FOR 3<=Z<=10	FLIT, DLIT, HLIT(26), HLIT(60)=	0.805E+06	0.164E+01	0.845E+01	0.831E+01
FOR 11<=Z<=20	FMED, DMED, HMED(26), HMED(60)=	0.899E+05	0.754E+00	0.876E+01	0.118E+02
FOR 21<=Z<=28	FHVV, DHVV, HHVV(26), HHVV(60)=	0.162E+05	0.429E+00	0.821E+01	0.972E+01
TOTALS FLUX, DOSE, HD0SE(26), HD0SE(60)= 0.349E+09 0.190E+02 0.525E+02 0.578E+02 <---					

X= 2.000 IN NLAY= 2 XLAY= 1.000 XTOT= 2.000

A	Z	FLUX	D0SE	D0SE EQ. (26)	D0SE EQ. (60)
1.00	0.00	0.13481E+09	0.94303E-01	0.18675E+01	0.18675E+01
1.00	1.00	0.19728E+09	0.13144E+02	0.17249E+02	0.16885E+02
2.00	1.00	0.83251E+06	0.23038E+00	0.76363E+00	0.76465E+00
3.00	1.00	0.56251E+06	0.77192E-01	0.22951E+00	0.25410E+00
3.00	2.00	0.15077E+06	0.58840E-01	0.22436E+00	0.26900E+00
4.00	2.00	0.10191E+08	0.23710E+01	0.64310E+01	0.75507E+01
5.00	3.00	0.17520E+05	0.79934E-02	0.12885E-01	0.11984E-01
7.00	3.00	0.69369E+05	0.31997E-01	0.52135E-01	0.48448E-01
8.00	4.00	0.77730E+04	0.62156E-02	0.13469E-01	0.11877E-01
9.00	4.00	0.38137E+05	0.30862E-01	0.68195E-01	0.60285E-01
10.00	5.00	0.21517E+05	0.27037E-01	0.84060E-01	0.70719E-01
11.00	5.00	0.86485E+05	0.10791E+00	0.33177E+00	0.27788E+00
12.00	6.00	0.22562E+06	0.40731E+00	0.16672E+01	0.14353E+01
13.00	6.00	0.12767E+05	0.22530E-01	0.89695E-01	0.76009E-01
14.00	7.00	0.65088E+05	0.15280E+00	0.74432E+00	0.66782E+00
15.00	7.00	0.10905E+05	0.25896E-01	0.12807E+00	0.11618E+00
16.00	8.00	0.17241E+06	0.53882E+00	0.32561E+01	0.33206E+01
17.00	8.00	0.48201E+04	0.14518E-01	0.84054E-01	0.83630E-01
18.00	9.00	0.33065E+04	0.12561E-01	0.85621E-01	0.92631E-01
19.00	9.00	0.78536E+04	0.29807E-01	0.20279E+00	0.21918E+00
20.00	10.00	0.26559E+05	0.12356E+00	0.96284E+00	0.11074E+01
21.00	10.00	0.28479E+04	0.13278E-01	0.10366E+00	0.11934E+00
22.00	10.00	0.17751E+04	0.82392E-02	0.63995E-01	0.73522E-01
23.00	11.00	0.10154E+05	0.56966E-01	0.50109E+00	0.60632E+00
24.00	12.00	0.29846E+05	0.19642E+00	0.19017E+01	0.23946E+01
25.00	12.00	0.15371E+04	0.10302E-01	0.10142E+00	0.12824E+00
26.00	12.00	0.13215E+04	0.87730E-02	0.85559E-01	0.10802E+00
27.00	13.00	0.70870E+04	0.54777E-01	0.58499E+00	0.76429E+00
28.00	14.00	0.19322E+05	0.17498E+00	0.20521E+01	0.27685E+01
29.00	15.00	0.17094E+04	0.17187E-01	0.21246E+00	0.29426E+00
30.00	16.00	0.63682E+01	0.71205E-04	0.92941E-03	0.13182E-02
31.00	16.00	0.18137E+03	0.20909E-02	0.27870E-01	0.39236E-01
32.00	16.00	0.47949E+04	0.54664E-01	0.72314E+00	0.10252E+01
33.00	17.00	0.11359E+03	0.14760E-02	0.20919E-01	0.30106E-01
34.00	18.00	0.16316E+02	0.23950E-03	0.36022E-02	0.52042E-02
35.00	17.00	0.17723E+04	0.22987E-01	0.32546E+00	0.46969E+00
36.00	18.00	0.30284E+03	0.44118E-02	0.66137E-01	0.96181E-01
37.00	19.00	0.91487E+02	0.15075E-02	0.23908E-01	0.34631E-01
38.00	18.00	0.18086E+04	0.26322E-01	0.39442E+00	0.57602E+00
39.00	19.00	0.14366E+04	0.23114E-01	0.36292E+00	0.53550E+00
40.00	20.00	0.17706E+04	0.30875E-01	0.50260E+00	0.75254E+00
41.00	20.00	0.10104E+03	0.17858E-02	0.29232E-01	0.43363E-01

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42.00 20.00 0.69473E+03 0.12213E-01 0.19952E+00 0.29730E+00
43.00 21.00 0.95519E+03 0.18667E-01 0.31889E+00 0.46923E+00
44.00 22.00 0.16012E+02 0.34421E-03 0.60999E-02 0.86966E-02
45.00 22.00 0.60264E+02 0.12950E-02 0.22946E-01 0.32720E-01
46.00 22.00 0.41000E+03 0.87360E-02 0.15448E+00 0.22167E+00
47.00 22.00 0.16169E+04 0.34885E-01 0.61934E+00 0.87972E+00
48.00 23.00 0.20289E+03 0.47336E-02 0.86519E-01 0.11486E+00
49.00 23.00 0.10642E+04 0.24997E-01 0.45778E+00 0.60426E+00
50.00 24.00 0.15691E+03 0.40323E-02 0.75984E-01 0.93136E-01
51.00 24.00 0.29238E+03 0.74827E-02 0.14089E+00 0.17321E+00
52.00 24.00 0.13677E+04 0.35165E-01 0.66298E+00 0.81211E+00
53.00 25.00 0.36023E+03 0.10002E-01 0.19292E+00 0.22224E+00
54.00 25.00 0.11951E+04 0.32835E-01 0.63305E+00 0.73445E+00
55.00 26.00 0.42626E+03 0.12558E-01 0.24690E+00 0.27117E+00
56.00 26.00 0.62664E+04 0.18200E+00 0.35774E+01 0.39668E+01
57.00 27.00 0.37276E+02 0.11646E-02 0.23258E-01 0.24476E-01
58.00 28.00 0.30661E+03 0.10237E-01 0.20474E+00 0.20826E+00

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EMIN,EMAX= 0.10000E-01 0.50000E+05
RMIN,RMAX= 0.29827E-04 0.21716E+05

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RELEVANT QUANTITIES AT X= 2.000 FOLLOW

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FOR Z=0 FNUT,DNUT,HNUT(26),HNUT(60)= 0.135E+09 0.943E-01 0.187E+01 0.187E+01
FOR Z=1 FPDT,DPDT,HPDT(26),HPDT(60)= 0.199E+09 0.135E+02 0.182E+02 0.179E+02
FOR Z=2 FALP,DALP,HALP(26),HALP(60)= 0.103E+08 0.243E+01 0.666E+01 0.782E+01
FOR 3<=Z<=10 FLIT,DLIT,HLIT(26),HLIT(60)= 0.775E+06 0.156E+01 0.795E+01 0.779E+01
FOR 11<=Z<=20 FMED,DMED,HMED(26),HMED(60)= 0.841E+05 0.701E+00 0.812E+01 0.110E+02
FOR 21<=Z<=28 FHVY,DHVV,HHVY(26),HHVY(60)= 0.147E+05 0.389E+00 0.742E+01 0.884E+01

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TOTALS FLUX,DOSE,HD0SE(26),HD0SE(60)= 0.345E+09 0.186E+02 0.503E+02 0.552E+02

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X= 3.000 IN NLAY= 2 XLAY= 1.000 XTOT= 3.000

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A      Z      FLUX      DOSE      DOSE EQ. (26)      DOSE EQ. (60)
1.00  0.00  0.13283E+09 0.91266E-01 0.17985E+01 0.17985E+01
1.00  1.00  0.19658E+09 0.13106E+02 0.17184E+02 0.16823E+02
2.00  1.00  0.86714E+06 0.23042E+00 0.76028E+00 0.76168E+00
3.00  1.00  0.59116E+06 0.79013E-01 0.23130E+00 0.25583E+00
3.00  2.00  0.15907E+06 0.61180E-01 0.22751E+00 0.27190E+00
4.00  2.00  0.98605E+07 0.23022E+01 0.63349E+01 0.74580E+01
6.00  3.00  0.18544E+05 0.84243E-02 0.13510E-01 0.12568E-01
7.00  3.00  0.67514E+05 0.31032E-01 0.50277E-01 0.46717E-01
8.00  4.00  0.91118E+04 0.72557E-02 0.15620E-01 0.13771E-01
9.00  4.00  0.37088E+05 0.29905E-01 0.65637E-01 0.57959E-01

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10.00	5.00	0.22693E+05	0.28442E-01	0.88116E-01	0.74043E-01
11.00	5.00	0.83339E+05	0.10360E+00	0.31651E+00	0.26434E+00
12.00	6.00	0.21436E+06	0.38565E+00	0.15709E+01	0.13482E+01
13.00	6.00	0.13066E+05	0.22956E-01	0.90801E-01	0.76619E-01
14.00	7.00	0.62275E+05	0.14589E+00	0.70858E+00	0.63437E+00
15.00	7.00	0.11220E+05	0.26485E-01	0.12992E+00	0.11715E+00
16.00	8.00	0.16133E+06	0.50210E+00	0.30184E+01	0.30694E+01
17.00	8.00	0.48983E+04	0.14687E-01	0.84507E-01	0.83773E-01
18.00	9.00	0.34092E+04	0.12905E-01	0.87595E-01	0.94579E-01
19.00	9.00	0.76519E+04	0.28907E-01	0.19555E+00	0.21079E+00
20.00	10.00	0.24821E+05	0.11503E+00	0.89246E+00	0.10249E+01
21.00	10.00	0.28885E+04	0.13423E-01	0.10440E+00	0.12003E+00
22.00	10.00	0.17811E+04	0.82224E-02	0.63467E-01	0.72749E-01
23.00	11.00	0.98001E+04	0.54777E-01	0.47999E+00	0.58019E+00
24.00	12.00	0.27559E+05	0.18068E+00	0.17430E+01	0.21932E+01
25.00	12.00	0.15560E+04	0.10398E-01	0.10209E+00	0.12901E+00
26.00	12.00	0.13149E+04	0.86811E-02	0.84220E-01	0.10622E+00
27.00	13.00	0.66870E+04	0.51481E-01	0.54789E+00	0.71555E+00
28.00	14.00	0.17720E+05	0.15973E+00	0.18666E+01	0.25183E+01
29.00	15.00	0.16378E+04	0.16393E-01	0.20196E+00	0.27983E+00
30.00	16.00	0.73159E+01	0.81202E-04	0.10544E-02	0.14971E-02
31.00	16.00	0.18489E+03	0.21248E-02	0.28265E-01	0.39812E-01
32.00	16.00	0.44634E+04	0.50667E-01	0.66831E+00	0.94824E+00
33.00	17.00	0.11963E+03	0.15497E-02	0.21924E-01	0.31569E-01
34.00	18.00	0.18107E+02	0.26547E-03	0.39902E-02	0.57659E-02
35.00	17.00	0.17044E+04	0.21997E-01	0.31050E+00	0.44864E+00
36.00	18.00	0.31241E+03	0.45433E-02	0.68040E-01	0.98953E-01
37.00	19.00	0.97202E+02	0.15988E-02	0.25336E-01	0.36728E-01
38.00	18.00	0.16892E+04	0.24443E-01	0.36513E+00	0.53442E+00
39.00	19.00	0.13589E+04	0.21748E-01	0.34059E+00	0.50390E+00
40.00	20.00	0.15872E+04	0.27585E-01	0.44838E+00	0.67287E+00
41.00	20.00	0.10427E+03	0.18378E-02	0.30040E-01	0.44636E-01
42.00	20.00	0.70224E+03	0.12298E-01	0.20054E+00	0.29953E+00
43.00	21.00	0.92313E+03	0.17974E-01	0.30659E+00	0.45246E+00
44.00	22.00	0.16924E+02	0.36374E-03	0.64443E-02	0.91890E-02
45.00	22.00	0.62243E+02	0.13366E-02	0.23674E-01	0.33779E-01
46.00	22.00	0.41064E+03	0.87265E-02	0.15417E+00	0.22195E+00
47.00	22.00	0.14896E+04	0.32030E-01	0.56804E+00	0.80925E+00
48.00	23.00	0.20416E+03	0.47617E-02	0.87012E-01	0.11554E+00
49.00	23.00	0.99647E+03	0.23359E-01	0.42754E+00	0.56528E+00
50.00	24.00	0.16045E+03	0.41344E-02	0.77928E-01	0.95318E-01
51.00	24.00	0.29074E+03	0.74533E-02	0.14035E+00	0.17232E+00
52.00	24.00	0.12451E+04	0.31967E-01	0.60250E+00	0.73877E+00
53.00	25.00	0.35967E+03	0.99989E-02	0.19287E+00	0.22197E+00
54.00	25.00	0.10930E+04	0.29925E-01	0.57670E+00	0.67074E+00

55.00 26.00 0.42133E+03 0.12410E-01 0.24399E+00 0.26801E+00
 56.00 26.00 0.54629E+04 0.15810E+00 0.31072E+01 0.34531E+01
 57.00 27.00 0.34233E+02 0.10666E-02 0.21301E-01 0.22453E-01
 58.00 28.00 0.26770E+03 0.89072E-02 0.17814E+00 0.18157E+00

EMIN,EMAX= 0.10000E-01 0.50000E+05
 RMIN,RMAX= 0.29827E-04 0.21716E+05

RELEVANT QUANTITIES AT X= 3.000 FOLLOW

FOR Z=0 FNUT,DNUT,HNUT(26),HNUT(60)= 0.133E+09 0.913E-01 0.180E+01 0.180E+01
 FOR Z=1 FPDT,DPDT,HPDT(26),HPDT(60)= 0.198E+09 0.134E+02 0.182E+02 0.178E+02
 FOR Z=2 FALP,DALP,HALP(26),HALP(60)= 0.100E+08 0.236E+01 0.656E+01 0.773E+01
 FOR 3<=Z<=10 FLIT,DLIT,HLIT(26),HLIT(60)= 0.746E+05 0.148E+01 0.750E+01 0.732E+01
 FOR 11<=Z<=20 FMED,DMED,HMED(26),HMED(60)= 0.786E+05 0.653E+00 0.754E+01 0.102E+02
 FOR 21<=Z<=28 FHVY,DHVV,HVY(26),HVY(60)= 0.134E+05 0.353E+00 0.671E+01 0.803E+01

TOTALS FLUX,DOSE,HD0SE(26),HD0SE(60)= 0.342E+09 0.184E+02 0.483E+02 0.529E+02

X= 4.000 IN NLAY= 2 XLAY= 1.000 XTOT= 4.000

A	Z	FLUX	DOSE	DOSE EQ. (26)	DOSE EQ. (60)
1.00	0.00	0.13157E+09	0.89015E-01	0.17466E+01	0.17466E+01
1.00	1.00	0.19591E+09	0.13082E+02	0.17142E+02	0.16783E+02
2.00	1.00	0.90115E+06	0.23152E+00	0.75961E+00	0.76115E+00
3.00	1.00	0.61735E+06	0.80710E-01	0.23308E+00	0.25755E+00
3.00	2.00	0.16646E+06	0.63194E-01	0.23007E+00	0.27426E+00
4.00	2.00	0.95804E+07	0.22362E+01	0.62434E+01	0.73696E+01
6.00	3.00	0.19461E+05	0.88071E-02	0.14066E-01	0.13090E-01
7.00	3.00	0.65705E+05	0.30103E-01	0.48540E-01	0.45107E-01
8.00	4.00	0.10318E+05	0.81877E-02	0.17535E-01	0.15460E-01
9.00	4.00	0.36062E+05	0.28982E-01	0.63245E-01	0.55809E-01
10.00	5.00	0.23697E+05	0.29621E-01	0.91424E-01	0.76718E-01
11.00	5.00	0.80305E+05	0.99480E-01	0.30221E+00	0.25177E+00
12.00	6.00	0.20370E+06	0.36527E+00	0.14809E+01	0.12672E+01
13.00	6.00	0.13295E+05	0.23264E-01	0.91472E-01	0.76880E-01
14.00	7.00	0.59574E+05	0.13929E+00	0.67462E+00	0.60273E+00
15.00	7.00	0.11457E+05	0.26900E-01	0.13094E+00	0.11741E+00
16.00	8.00	0.15102E+06	0.46822E+00	0.28017E+01	0.28417E+01
17.00	8.00	0.49507E+04	0.14785E-01	0.84623E-01	0.83626E-01
18.00	9.00	0.34862E+04	0.13152E-01	0.88934E-01	0.95846E-01
19.00	9.00	0.74458E+04	0.28014E-01	0.18857E+00	0.20279E+00
20.00	10.00	0.23206E+05	0.10718E+00	0.82839E+00	0.94989E+00
21.00	10.00	0.29101E+04	0.13482E-01	0.10452E+00	0.12001E+00
22.00	10.00	0.17786E+04	0.81720E-02	0.62746E-01	0.71771E-01

23.00	11.00	0.94468E+04	0.52622E-01	0.45950E+00	0.55481E+00
24.00	12.00	0.25458E+05	0.16632E+00	0.15992E+01	0.20106E+01
25.00	12.00	0.15631E+04	0.10413E-01	0.10196E+00	0.12875E+00
26.00	12.00	0.13018E+04	0.85528E-02	0.82594E-01	0.10406E+00
27.00	13.00	0.63083E+04	0.48386E-01	0.51329E+00	0.67006E+00
28.00	14.00	0.16260E+05	0.14594E+00	0.16998E+01	0.22933E+01
29.00	15.00	0.15681E+04	0.15630E-01	0.19196E+00	0.26605E+00
30.00	16.00	0.81470E+01	0.89951E-04	0.11637E-02	0.16535E-02
31.00	16.00	0.18664E+03	0.21375E-02	0.26368E-01	0.39986E-01
32.00	16.00	0.41573E+04	0.47004E-01	0.61829E+00	0.87789E+00
33.00	17.00	0.12423E+03	0.16042E-02	0.22651E-01	0.32636E-01
34.00	18.00	0.19615E+02	0.28696E-03	0.43086E-02	0.62306E-02
35.00	17.00	0.16360E+04	0.21015E-01	0.29580E+00	0.42790E+00
36.00	18.00	0.31803E+03	0.46122E-02	0.68965E-01	0.10038E+00
37.00	19.00	0.10117E+03	0.16587E-02	0.26249E-01	0.38117E-01
38.00	18.00	0.15781E+04	0.22712E-01	0.33827E+00	0.49614E+00
39.00	19.00	0.12848E+04	0.20458E-01	0.31960E+00	0.47407E+00
40.00	20.00	0.14237E+04	0.24663E-01	0.40033E+00	0.60206E+00
41.00	20.00	0.10636E+03	0.18685E-02	0.30497E-01	0.45411E-01
42.00	20.00	0.70210E+03	0.12247E-01	0.19935E+00	0.29854E+00
43.00	21.00	0.88876E+03	0.17239E-01	0.29365E+00	0.43466E+00
44.00	22.00	0.17550E+02	0.37655E-03	0.66674E-02	0.95208E-02
45.00	22.00	0.63364E+02	0.13580E-02	0.24038E-01	0.34356E-01
46.00	22.00	0.40699E+03	0.86232E-02	0.15220E+00	0.21969E+00
47.00	22.00	0.13717E+04	0.29393E-01	0.52071E+00	0.74410E+00
48.00	23.00	0.20306E+03	0.47286E-02	0.86369E-01	0.11483E+00
49.00	23.00	0.93097E+03	0.21769E-01	0.39818E+00	0.52754E+00
50.00	24.00	0.16128E+03	0.41550E-02	0.78310E-01	0.95792E-01
51.00	24.00	0.28543E+03	0.73126E-02	0.13769E+00	0.16911E+00
52.00	24.00	0.11322E+04	0.29008E-01	0.54651E+00	0.67117E+00
53.00	25.00	0.35393E+03	0.98323E-02	0.18964E+00	0.21835E+00
54.00	25.00	0.99818E+03	0.27234E-01	0.52463E+00	0.61163E+00
55.00	26.00	0.41076E+03	0.12079E-01	0.23747E+00	0.26111E+00
56.00	26.00	0.47649E+04	0.13745E+00	0.27007E+01	0.30078E+01
57.00	27.00	0.31376E+02	0.97502E-03	0.19472E-01	0.20557E-01
58.00	28.00	0.23385E+03	0.77560E-02	0.15512E+00	0.15840E+00

EMIN,EMAX= 0.10000E-01 0.50000E+05
 RMIN,RMAX= 0.29827E-04 0.21716E+05

RELEVANT QUANTITIES AT X= 4.000 FOLLOW

FOR Z=0 FNUT,DNUT,HNUT(26),HNUT(60)= 0.132E+09 0.890E-01 0.175E+01 0.175E+01
 FOR Z=1 FPDT,DPDT,HPDT(26),HPDT(60)= 0.197E+09 0.134E+02 0.181E+02 0.178E+02
 FOR Z=2 FALP,DALP,HALP(26),HALP(60)= 0.975E+07 0.230E+01 0.647E+01 0.764E+01

FOR 3<Z<=10 FLIT,DLIT,HLIT(26),HLIT(60)= 0.718E+06 0.141E+01 0.707E+01 0.689E+01
 FOR 11<Z<=20 FMED,DMED,HMED(26),HMED(60)= 0.736E+05 0.608E+00 0.700E+01 0.947E+01
 FOR 21<Z<=28 FHVY,DHVV,HHVY(26),HHVY(60)= 0.123E+05 0.319E+00 0.607E+01 0.730E+01

TOTALS FLUX,DOSE,HD0SE(26),HD0SE(60)= 0.340E+09 0.181E+02 0.465E+02 0.508E+02 <-----

X= 5.000 IN NLAY= 2 XLAY= 1.000 XTOT= 5.000

A	Z	FLUX	DOSE	DOSE EQ.(26)	DOSE EQ.(60)
1.00	0.00	0.13082E+09	0.87319E-01	0.17067E+01	0.17067E+01
1.00	1.00	0.19524E+09	0.13065E+02	0.17112E+02	0.16755E+02
2.00	1.00	0.93341E+06	0.23277E+00	0.75946E+00	0.76109E+00
3.00	1.00	0.64119E+06	0.82237E-01	0.23469E+00	0.25912E+00
3.00	2.00	0.17302E+06	0.64924E-01	0.23212E+00	0.27616E+00
4.00	2.00	0.92898E+07	0.21726E+01	0.61563E+01	0.72856E+01
6.00	3.00	0.20276E+05	0.91444E-02	0.14550E-01	0.13547E-01
7.00	3.00	0.63940E+05	0.29207E-01	0.46898E-01	0.43590E-01
8.00	4.00	0.11401E+05	0.90192E-02	0.19224E-01	0.16948E-01
9.00	4.00	0.35060E+05	0.28089E-01	0.60968E-01	0.53769E-01
10.00	5.00	0.24544E+05	0.30598E-01	0.94062E-01	0.78809E-01
11.00	5.00	0.77377E+05	0.95536E-01	0.28866E+00	0.23990E+00
12.00	6.00	0.19361E+06	0.34611E+00	0.13973E+01	0.11925E+01
13.00	6.00	0.13462E+05	0.23468E-01	0.91774E-01	0.76860E-01
14.00	7.00	0.56981E+05	0.13298E+00	0.64248E+00	0.57299E+00
15.00	7.00	0.11626E+05	0.27166E-01	0.13133E+00	0.11714E+00
16.00	8.00	0.14141E+06	0.43687E+00	0.26030E+01	0.26339E+01
17.00	8.00	0.49802E+04	0.14820E-01	0.84434E-01	0.83205E-01
18.00	9.00	0.35404E+04	0.13313E-01	0.89692E-01	0.96480E-01
19.00	9.00	0.72365E+04	0.27124E-01	0.18176E+00	0.19502E+00
20.00	10.00	0.21702E+05	0.99908E-01	0.76944E+00	0.88098E+00
21.00	10.00	0.29151E+04	0.13465E-01	0.10405E+00	0.11932E+00
22.00	10.00	0.17685E+04	0.80911E-02	0.61829E-01	0.70581E-01
23.00	11.00	0.90952E+04	0.50496E-01	0.43947E+00	0.53002E+00
24.00	12.00	0.23525E+05	0.15318E+00	0.14681E+01	0.18443E+01
25.00	12.00	0.15602E+04	0.10361E-01	0.10115E+00	0.12763E+00
26.00	12.00	0.12833E+04	0.83931E-02	0.80705E-01	0.10157E+00
27.00	13.00	0.59499E+04	0.45474E-01	0.48090E+00	0.62749E+00
28.00	14.00	0.14929E+05	0.13346E+00	0.15494E+01	0.20904E+01
29.00	15.00	0.15004E+04	0.14897E-01	0.18242E+00	0.25289E+00
30.00	16.00	0.88675E+01	0.97508E-04	0.12578E-02	0.17884E-02
31.00	16.00	0.18692E+03	0.21331E-02	0.28240E-01	0.39838E-01
32.00	16.00	0.38744E+04	0.43639E-01	0.57255E+00	0.81346E+00
33.00	17.00	0.12756E+03	0.16419E-02	0.23139E-01	0.33362E-01
34.00	18.00	0.20863E+02	0.30440E-03	0.45642E-02	0.66071E-02
35.00	17.00	0.15677E+04	0.20048E-01	0.28143E+00	0.40756E+00

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36.00	18.00	0.32038E+03	0.46309E-02	0.69119E-01	0.10074E+00	
37.00	19.00	0.10368E+03	0.16935E-02	0.26753E-01	0.38932E-01	
38.00	18.00	0.14745E+04	0.21114E-01	0.31359E+00	0.46087E+00	
39.00	19.00	0.12140E+04	0.19240E-01	0.29987E+00	0.44592E+00	
40.00	20.00	0.12778E+04	0.22068E-01	0.35773E+00	0.53909E+00	
41.00	20.00	0.10747E+03	0.18815E-02	0.30664E-01	0.45765E-01	
42.00	20.00	0.69576E+03	0.12089E-01	0.19645E+00	0.29498E+00	
43.00	21.00	0.85287E+03	0.16482E-01	0.28036E+00	0.41623E+00	
44.00	22.00	0.17935E+02	0.38390E-03	0.67930E-02	0.97202E-02	
45.00	22.00	0.63778E+02	0.13633E-02	0.24115E-01	0.34543E-01	
46.00	22.00	0.39998E+03	0.84485E-02	0.14898E+00	0.21563E+00	
47.00	22.00	0.12627E+04	0.26964E-01	0.47717E+00	0.68397E+00	
48.00	23.00	0.20009E+03	0.46493E-02	0.84879E-01	0.11305E+00	
49.00	23.00	0.86808E+03	0.20243E-01	0.37004E+00	0.49134E+00	
50.00	24.00	0.16002E+03	0.41160E-02	0.77557E-01	0.94977E-01	
51.00	24.00	0.27746E+03	0.70955E-02	0.13356E+00	0.16426E+00	
52.00	24.00	0.10288E+04	0.26292E-01	0.49511E+00	0.60919E+00	
53.00	25.00	0.34441E+03	0.95506E-02	0.18417E+00	0.21231E+00	
54.00	25.00	0.91026E+03	0.24753E-01	0.47665E+00	0.55698E+00	
55.00	26.00	0.39617E+03	0.11623E-01	0.22848E+00	0.25160E+00	
56.00	26.00	0.41580E+04	0.11957E+00	0.23489E+01	0.26213E+01	
57.00	27.00	0.28707E+02	0.88978E-03	0.17770E-01	0.18788E-01	
58.00	28.00	0.20439E+03	0.67579E-02	0.13516E+00	0.13827E+00	
EMIN,EMAX= 0.10000E-01 0.50000E+05						
RMIN,RMAX= 0.29827E-04 0.21716E+05						
RELEVANT QUANTITIES AT X= 5.000 FOLLOW						
FOR Z=0 FNUT,DNUT,HNUT(26),HNUT(60)= 0.131E+09 0.873E-01 0.171E+01 0.171E+01						
FOR Z=1 FPDT,DPDT,HPDT(26),HPDT(60)= 0.197E+09 0.134E+02 0.181E+02 0.178E+02						
FOR Z=2 FALP,DALP,HALP(26),HALP(60)= 0.946E+07 0.224E+01 0.639E+01 0.756E+01						
FOR 3<=Z<=10 FLIT,DLIT,HLIT(26),HLIT(60)= 0.692E+06 0.134E+01 0.668E+01 0.649E+01						
FOR 11<=Z<=20 FMED,DNED,HMED(26),HMED(60)= 0.688E+05 0.567E+00 0.651E+01 0.880E+01						
FOR 21<=Z<=28 FHVY,DHVY,HHVY(26),HHVY(60)= 0.112E+05 0.289E+00 0.549E+01 0.663E+01						
TOTALS FLUX,DOSE,HDOSE(26),HDOSE(60)= 0.338E+09 0.179E+02 0.449E+02 0.490E+02						
LET SPECTRUM						
X= 0.00						
LET (MEV/CM)						
1.235000	FLUX	DOSE	DOSE EQ.(26)	DOSE EQ.(60)		
1.525225	1.9665483E+08	19.40947	106.7463	120.1109		
	1.9665483E+08	19.40947	106.7463	120.1109		

1.883653	1.9665483E+08	19.40947	106.7463	120.1109
2.326311	8.5867032E+07	15.54402	101.8223	115.1869
2.872995	5.2124576E+07	14.15150	100.1645	113.5290
3.548148	3.6814416E+07	13.36868	99.27546	112.6400
4.381963	2.8633458E+07	12.85308	98.70613	112.0707
5.411725	2.4143282E+07	12.50431	98.32808	111.6926
6.683480	2.1643074E+07	12.26377	98.07031	111.4349
8.254098	1.8274530E+07	11.63393	97.59650	110.9611
10.19381	1.0269397E+07	10.68077	96.32190	109.6864
12.58936	7184351.	10.12135	95.72423	109.0888
15.54786	5223367.	9.683538	95.26331	108.6279
19.20160	3931311.	9.326126	94.89050	108.2551
23.71398	3096545.	9.041931	94.59603	107.9606
29.28676	2575231.	8.822865	94.37014	107.7347
36.16915	2226893.	8.641833	94.18350	107.5484
44.66890	2014140.	8.504918	94.02551	107.4078
55.16610	1827718.	8.354546	93.80959	107.2535
68.13013	1709448.	8.238809	93.61201	107.1352
84.14071	1423319.	7.885621	92.86658	106.7750
103.9138	1234956.	7.600614	92.13807	106.4777
128.3335	1092779.	7.340090	91.35043	106.0928
158.4919	776685.4	6.627639	88.77053	104.4470
195.7375	632989.7	6.224379	87.00059	103.0633
241.7358	503009.4	5.775250	84.64703	100.9304
298.5437	400981.0	5.325092	81.78353	97.95136
368.7015	311081.4	4.852000	78.30517	93.97840
455.3463	230346.2	4.316658	73.65116	88.07861
562.3527	175996.8	3.874913	69.19182	81.86836
694.5056	138718.5	3.502138	64.84644	75.22351
857.7144	110197.2	3.152392	60.14720	67.29071
1059.277	89094.38	2.830073	55.21940	58.24710
1308.208	71371.18	2.493410	49.38514	48.94845
1615.636	38802.93	1.734875	34.69980	30.07641
1995.311	23543.40	1.298017	25.96015	20.26027
2464.209	14434.61	0.9771570	19.54303	13.78303
3043.298	8757.669	0.7290645	14.58121	9.278485
3758.473	5271.602	0.5406055	10.81207	6.202319
4641.714	3138.308	0.3976641	7.953224	4.106205
5732.517	1845.654	0.2901950	5.803854	2.693263
7079.659	1070.730	0.2093815	4.187608	1.742806
8743.378	608.7352	0.1488544	2.977073	1.108556
10798.07	337.7346	0.1039986	2.079980	0.6903607
13335.62	180.9302	7.0786193E-02	1.415735	0.4169019

X= 5.00

LET (MEV/CM)	FLUX	DOSE	DOSE EQ. (26)	DOSE EQ. (60)
1.235000	2.0750747E+08	21.19472	91.60429	102.6974
1.525225	2.0750747E+08	21.19472	91.60429	102.6974
1.883653	2.0750747E+08	21.19472	91.60429	102.6974
2.326311	1.0020835E+08	17.45156	86.83646	97.92957
2.872995	6.6422324E+07	16.05615	85.17535	96.26846
3.548148	5.0124976E+07	15.22170	84.22771	95.32082
4.381963	4.0359732E+07	14.60460	83.54633	94.63944
5.411725	3.3971044E+07	14.10655	83.00650	94.09962
6.683480	2.9512580E+07	13.67587	82.54498	93.63809
8.254098	2.4479334E+07	13.05043	81.86434	92.95745
10.19381	1.5517026E+07	11.75316	80.44151	91.53462
12.58936	1.1300499E+07	10.98869	79.62735	90.72047
15.54786	8372984.	10.33392	78.93744	90.03056
19.20160	6319398.	9.765270	78.34222	89.43535
23.71398	4871017.	9.271760	77.82832	88.92145
29.28676	3856887.	8.845343	77.38629	88.47937
36.16915	3116442.	8.460476	76.98797	88.08174
44.66890	2599806.	8.126672	76.60034	87.73817
55.16610	2180473.	7.790356	76.12176	87.39304
68.13013	1884750.	7.501533	75.62727	87.09787
84.14071	1493883.	7.022734	74.62245	86.61235
103.9138	1231010.	6.627378	73.61726	86.19628
128.3335	1039691.	6.275746	72.55260	85.67158
158.4919	725789.0	5.569050	69.99041	84.03518
195.7375	575275.8	5.143203	68.12064	82.57938
241.7358	445810.3	4.698043	65.78872	80.46758
298.5437	348127.2	4.265248	63.04241	77.61410
368.7015	263597.0	3.820159	59.77280	73.88205
455.3463	191284.7	3.341811	55.61729	68.61665
562.3527	142743.1	2.948154	51.64085	63.07357
694.5056	109339.7	2.614297	47.76218	57.16362
857.7144	83820.09	2.299230	43.51883	49.96938
1059.277	64225.67	1.997406	38.88366	41.49617
1308.208	49748.64	1.718177	34.01421	33.85430
1615.636	25470.03	1.146814	22.93986	19.70009
1995.311	14472.71	0.8220770	16.44231	12.54873
2464.209	8614.668	0.6117616	12.23517	8.345682
3043.298	5249.258	0.4646466	9.292865	5.675462
3758.473	3212.393	0.3541763	7.083489	3.875062
4641.714	1960.020	0.2698541	5.397024	2.642288
5732.517	1189.575	0.2049696	4.099346	1.794562
7079.659	714.2457	0.1543779	3.087536	1.206523
8743.378	419.9864	0.1144070	2.286123	0.7967451

BB

10798.07
13335.62

242.6695
135.5334

8.3730273E-02
5.9762012E-02

0.5180907
0.3275247

X= 10.00

LET (MEV/CM)

FLUX

DOSE

DOSE EQ. (26)

DOSE EQ. (60)

1.235000
1.525225
1.883653
2.326311
2.872995
3.548148
4.381963
5.411725
6.683480
8.254098
10.19381
12.58936
15.54786
19.20160
23.71398
29.28676
36.16915
44.66890
55.16610
68.13013
84.14071
103.9138
128.3335
158.4919
195.7375
241.7358
298.5437
368.7015
455.3463
562.3527
694.5056
857.7144
1059.277
1308.208
1615.636
1995.311
2464.209
3043.298
3758.473

2.1155706E+08
2.1155706E+08
2.1155706E+08
1.0773261E+08
7.4053880E+07
5.7002712E+07
4.6006664E+07
3.8189712E+07
3.2342060E+07
2.6254556E+07
1.6929704E+07
1.2204586E+07
8892354.
6586730.
4973347.
3848809.
3034078.
2468334.
2019863.
1704666.
1323917.
1070315.
887628.3
610590.6
477023.4
364740.0
280726.3
209225.8
149909.5
110500.2
83594.70
62605.27
46584.69
35117.03
17054.66
9233.386
5360.414
3232.254
1964.676

20.78543
20.78543
20.78543
17.16402
15.77209
14.89818
14.20225
13.59195
13.02655
12.27822
10.92531
10.06884
9.328007
8.689834
8.140068
7.667271
7.244134
6.878710
6.518841
6.211108
5.746011
5.363910
5.028190
4.404976
4.027387
3.641298
3.270702
2.894531
2.501690
2.181288
1.910146
1.653680
1.403704
1.181595
0.7559865
0.5204192
0.3782375
0.2852169
0.2164031

84.27078
84.27078
84.27078
79.65842
78.00159
77.00912
76.24075
75.57926
74.97337
74.16318
72.68559
71.77454
70.99374
70.32514
69.75206
69.26147
68.82413
68.44796
68.07869
67.76424
67.29318
66.89041
66.38873
64.94560
63.65689
61.82653
59.38600
56.23429
51.91201
47.39824
42.61026
36.74058
29.71858
23.66071
13.13679
8.002539
5.179007
3.490730
2.369821

CC

4641.714	1192.799	0.1643194	3.286348	1.609151
5732.517	720.0665	0.1243768	2.487490	1.088374
7079.659	429.3130	9.3261868E-02	1.865214	0.7281018
8743.378	251.3218	6.8647705E-02	1.372946	0.4773583
10798.07	143.8673	4.9886577E-02	0.997745	0.3081247
13335.62	79.58363	3.5302449E-02	0.7060526	0.1931151
<----->				
X=	20.00	<----->		
LET (MEV/CM)	FLUX	DOSE	DOSE EQ. (26)	DOSE EQ. (60)
1.235000	2.1261362E+08	19.88201	56.64134	62.69411
1.525225	2.1261362E+08	19.88201	56.64134	62.69411
1.883653	2.1261362E+08	19.88201	56.64134	62.69411
2.326311	1.1563305E+08	16.50031	52.33493	58.38769
2.872995	8.2522216E+07	15.13034	50.70450	56.75727
3.548148	6.4512104E+07	14.20600	49.65477	55.70754
4.381963	5.1841208E+07	13.40281	48.76797	54.82075
5.411725	4.2121804E+07	12.64321	47.94466	53.99744
6.683480	3.4512640E+07	11.90708	47.15578	53.20856
8.254098	2.7246888E+07	11.02317	46.20353	52.25631
10.19381	1.7870250E+07	9.658879	44.72131	50.77409
12.58936	1.2731265E+07	8.727863	43.73220	49.78498
15.54786	9107912.	7.917469	42.87786	48.93064
19.20160	6605202.	7.224811	42.15152	48.20431
23.71398	4872218.	6.634452	41.53547	47.58825
29.28676	3670715.	6.129496	41.01111	47.06383
36.16915	2808396.	5.681208	40.54670	46.60024
44.66890	2209255.	5.294860	40.09784	46.20248
55.16610	1744991.	4.922479	39.56911	45.82039
68.13013	1419446.	4.604591	39.02491	45.49562
84.14071	1069384.	4.178347	38.13317	45.06471
103.9138	837677.7	3.829479	37.24780	44.69604
128.3335	672873.3	3.527337	36.33308	44.24338
158.4919	455769.3	3.037095	34.55518	43.10758
195.7375	348252.7	2.732767	33.21904	42.07157
241.7358	261227.9	2.432993	31.64991	40.65175
298.5437	197842.5	2.151659	29.86906	38.80419
368.7015	143871.8	1.872147	27.81826	36.46521
455.3463	101692.6	1.594260	25.40600	33.41034
562.3527	73697.00	1.366779	23.10688	30.20229
694.5056	55327.57	1.171448	20.84519	26.76979
857.7144	38997.62	0.9849204	18.32677	22.48337
1059.277	27278.99	0.7967587	15.42410	17.19313
1308.208	19517.59	0.6452311	12.76134	13.09081
1615.636	9012.698	0.3945958	7.894961	6.931796

DD

1995.311	4512.546	0.2511063	5.023024	3.888988	
2464.209	2476.218	0.1741660	3.483300	2.389457	
3043.298	1482.855	0.1307051	2.614072	1.600919	
3758.473	897.2331	9.8829582E-02	1.976581	1.082273	
4641.714	542.1210	7.4805327E-02	1.496083	0.7320482	
5732.517	324.8218	5.6376945E-02	1.127517	0.4926534	
7079.659	192.3851	4.1995119E-02	0.8398918	0.3271987	
8743.378	110.9534	3.0584957E-02	0.6116936	0.2121500	
10798.07	62.91464	2.1981493E-02	0.4396288	0.1353616	
13335.62	34.41126	1.5346996E-02	0.3069398	8.3705693E-02	<-----
X=	0.00				<-----
LET (MEV/CM)	FLUX	DOSE	DOSE EQ. (26)	DOSE EQ. (60)	
1.235000	2.1261362E+08	19.88201	56.64134	62.69411	
1.525225	2.1261362E+08	19.88201	56.64134	62.69411	
1.883653	2.1261362E+08	19.88201	56.64134	62.69411	
2.326311	1.1563305E+08	16.50031	52.33493	58.38769	
2.872995	8.2522216E+07	15.13034	50.70450	56.75727	
3.548148	6.4512104E+07	14.20600	49.65477	55.70754	
4.381963	5.1841208E+07	13.40281	48.76797	54.82075	
5.411725	4.2121804E+07	12.64321	47.94466	53.99744	
6.683480	3.4512640E+07	11.90708	47.15578	53.20856	
8.254098	2.7246888E+07	11.02317	46.20353	52.25631	
10.19381	1.7870250E+07	9.658879	44.72131	50.77409	
12.58936	1.2731265E+07	8.727863	43.73220	49.78498	
15.54786	9107912.	7.917469	42.87786	48.93064	
19.20160	6605202.	7.224811	42.15152	48.20431	
23.71398	4872218.	6.634452	41.53547	47.58825	
29.28676	3670715.	6.129496	41.01111	47.06383	
36.16915	2808396.	5.681208	40.54670	46.60024	
44.66890	2209255.	5.294880	40.09784	46.20248	
55.16610	1744991.	4.922479	39.56911	45.82039	
68.13013	1419446.	4.604591	39.02491	45.49562	
84.14071	1069384.	4.178347	38.13317	45.06471	EE
103.9138	837677.7	3.829479	37.24780	44.69604	
128.3335	672873.3	3.527337	36.33308	44.24338	
158.4919	455769.3	3.037095	34.55518	43.10758	
195.7375	348252.7	2.732767	33.21904	42.07157	
241.7358	261227.9	2.432993	31.64991	40.65175	
298.5437	197842.5	2.151659	29.86906	38.80419	
368.7015	143871.8	1.872147	27.81826	36.46521	
455.3463	101692.6	1.594260	25.40600	33.41034	
562.3527	73697.00	1.366779	23.10688	30.20229	
694.5056	55327.57	1.171448	20.84519	26.76979	

857.7144	38997.62	0.9849204	18.32677	22.48337	
1059.277	27278.99	0.7967587	15.42410	17.19313	
1308.208	19517.59	0.6452311	12.76134	13.09081	
1615.636	9012.698	0.3945958	7.894961	6.931796	
1995.311	4512.546	0.2511063	5.023024	3.888988	
2464.209	2476.218	0.1741660	3.483300	2.389457	
3043.298	1482.855	0.1307051	2.614072	1.600919	
3758.473	897.2331	9.8829582E-02	1.976581	1.082273	
4641.714	542.1210	7.4805327E-02	1.496083	0.7320482	
5732.517	324.8218	5.6376945E-02	1.127517	0.4926534	
7079.659	192.3851	4.1995119E-02	0.8398918	0.3271987	
8743.378	110.9534	3.0584957E-02	0.6116936	0.2121500	
10798.07	62.91464	2.1981493E-02	0.4396288	0.1353616	
13335.62	34.41126	1.5346996E-02	0.3069398	8.3705693E-02	<-----
X=	1.00				<-----
LET (MEV/CM)	FLUX	DOSE	DOSE EQ. (26)	DOSE EQ. (60)	
1.235000	2.1095694E+08	18.86146	50.57154	55.82568	
1.525225	2.1095694E+08	18.86146	50.57154	55.82568	
1.883653	2.1095694E+08	18.86146	50.57154	55.82568	
2.326311	1.1483788E+08	15.51001	46.30378	51.55794	
2.872995	8.1765688E+07	14.14146	44.67506	49.92921	
3.548148	6.3661080E+07	13.21219	43.61970	48.87385	
4.381963	5.0876776E+07	12.40179	42.72491	47.97908	
5.411725	4.1065844E+07	11.63502	41.89381	47.14797	
6.683480	3.3406258E+07	10.89414	41.09983	46.35398	
8.254098	2.6167518E+07	10.01397	40.15187	45.40602	
10.19381	1.6951048E+07	8.672909	38.69529	43.94945	
12.58936	1.1902359E+07	7.758419	37.72378	42.97794	
15.54786	8364700.	6.967151	36.88959	42.14375	
19.20160	5951859.	6.299755	36.18977	41.44393	
23.71398	4309064.	5.740067	35.60577	40.85993	
29.28676	3193542.	5.271591	35.11938	40.37348	
36.16915	2410885.	4.865095	34.69840	39.95323	
44.66890	1884389.	4.525332	34.30394	39.60351	
55.16610	1485014.	4.204842	33.84893	39.27478	
68.13013	1212869.	3.939621	33.39519	39.00389	
84.14071	911276.9	3.572144	32.62628	38.63198	
103.9138	716693.1	3.279251	31.88215	38.32305	
128.3335	581162.8	3.029071	31.12525	37.94962	
158.4919	389893.2	2.599650	29.56940	36.95670	
195.7375	299538.6	2.343234	28.44374	36.08291	
241.7358	225123.1	2.086713	27.10119	34.86764	
298.5437	169843.2	1.843413	25.55955	33.26811	FF

368.7015	123454.2	1.601172	23.78100	31.23804
455.3463	86766.59	1.359707	21.68569	28.58538
562.3527	62203.51	1.164106	19.71010	25.82971
694.5056	46259.47	0.9968666	17.76635	22.86811
857.7144	33526.18	0.8403746	15.65140	19.27649
1059.277	24024.76	0.6892716	13.31925	15.03027
1308.208	17003.00	0.5526497	10.92371	11.31724
1615.636	7685.229	0.3323972	6.650510	5.883673
1995.311	3927.238	0.2149646	4.299601	3.358049
2464.209	2179.576	0.1504154	3.008291	2.090215
3043.298	1295.718	0.1117362	2.234703	1.388374
3758.473	776.6027	8.3491512E-02	1.669822	0.9286222
4641.714	463.3249	6.2338755E-02	1.246757	0.6200082
5732.517	273.8837	4.6281740E-02	0.9256178	0.4110640
7079.659	159.9249	3.3969540E-02	0.6793836	0.2689418
8743.378	91.01273	2.4438839E-02	0.4887750	0.1722464
10798.07	50.85242	1.7350622E-02	0.3470109	0.1085810
13335.62	27.57073	1.1999684E-02	0.2399922	6.6524014E-02

X= 2.00

LET (MEV/CM)

1.235000	2.0988915E+08	18.53352	48.39278	53.32382
1.525225	2.0988915E+08	18.53352	48.39278	53.32382
1.883653	2.0988915E+08	18.53352	48.39278	53.32382
2.326311	1.1462917E+08	15.21226	44.16356	49.09461
2.872995	8.1602944E+07	13.84542	42.53689	47.46793
3.548148	6.3411280E+07	12.91160	41.47634	46.40738
4.381963	5.0520528E+07	12.09442	40.57405	45.50509
5.411725	4.0621208E+07	11.32079	39.73550	44.66653
6.683480	3.2911230E+07	10.57505	38.93630	43.86734
8.254098	2.5691214E+07	9.697756	37.99169	42.92272
10.19381	1.6617299E+07	8.377227	36.55785	41.48888
12.58936	1.1637552E+07	7.475306	35.59974	40.53078
15.54786	8156536.	6.696687	34.77888	39.70992
19.20160	5787167.	6.041181	34.09150	39.02254
23.71398	4177535.	5.493175	33.51968	38.45073
29.28676	3090221.	5.036471	33.04551	37.97649
36.16915	2328636.	4.640903	32.63583	37.56753
44.66890	1817387.	4.310833	32.25265	37.22780
55.16610	1427954.	3.999069	31.80998	36.90803
68.13013	1164153.	3.741143	31.36872	36.64460
84.14071	872201.6	3.385628	30.62492	36.28482
103.9138	684283.3	3.102265	29.90495	35.98590
126.3335	552235.7	2.860237	29.17274	35.62460

GG

68.13013	1124294.	3.569231	29.57164	34.53825
84.14071	839257.1	3.222492	28.84630	34.18742
103.9138	655978.8	2.946106	28.14410	33.89579
128.3335	527814.9	2.710203	27.43043	33.54355
158.4919	353618.7	2.318295	26.01039	32.63723
195.7375	269884.6	2.081818	24.97232	31.83175
241.7358	201913.8	1.847221	23.74456	30.72045
298.5437	152190.6	1.625714	22.34200	29.26592
368.7015	110074.4	1.406697	20.73393	27.43037
455.3463	77312.16	1.191556	18.86760	25.06808
562.3527	55100.21	1.015953	17.09407	22.59392
694.5056	41091.17	0.8642662	15.33107	19.90818
857.7144	28731.74	0.7221183	13.40912	16.64305
1059.277	20417.83	0.5841442	11.27781	12.76532
1308.208	14109.12	0.4616110	9.126889	9.440195
1615.636	6422.284	0.2781587	5.565844	4.923498
1995.311	3206.866	0.1771479	3.543234	2.767067
2464.209	1778.358	0.1228274	2.456535	1.705864
3043.298	1057.842	9.1318563E-02	1.826350	1.134215
3758.473	634.3615	6.8252586E-02	1.365043	0.7588736
4641.714	378.4091	5.0952878E-02	1.019040	0.5065923
5732.517	223.4822	3.7803135E-02	0.7560457	0.3356222
7079.659	129.9881	2.7711166E-02	0.5542149	0.2192946
8743.378	74.05918	1.9894633E-02	0.3978911	0.1401494
10798.07	41.42682	1.4092857E-02	0.2818552	8.8145494E-02
13335.62	22.29413	9.7217383E-03	0.1944350	5.3861424E-02

X= 4.00

LET (MEV/CM)	FLUX	DOSE	DOSE EQ. (26)	DOSE EQ. (60)
1.235000	2.0797494E+08	18.03352	44.75592	49.10080
1.525225	2.0797494E+08	18.03352	44.75592	49.10080
1.883653	2.0797494E+08	18.03352	44.75592	49.10080
2.326311	1.1442622E+08	14.77233	40.60344	44.94831
2.872995	8.1510912E+07	13.40975	38.98186	43.32674
3.548148	6.3166308E+07	12.46793	37.91217	42.25705
4.381963	5.0081788E+07	11.63841	36.99622	41.34109
5.411725	4.0020332E+07	10.85209	36.14387	40.48875
6.683480	3.2209086E+07	10.09663	35.33423	39.67912
8.254098	2.5013722E+07	9.223474	34.39460	38.73949
10.19381	1.6190098E+07	7.938952	33.00081	37.34570
12.58936	1.1313985E+07	7.055773	32.06274	36.40762
15.54786	7909888.	6.294426	31.26005	35.60495
19.20160	5593288.	5.653740	30.58817	34.93306
23.71398	4024228.	5.119218	30.03035	34.37524

29.28676	2965122.	4.674531	29.56860	33.91344
36.16915	2222474.	4.289024	29.16932	33.51485
44.66890	1724571.	3.967360	28.79588	33.18376
55.16610	1345059.	3.663431	28.36433	32.87202
68.13013	1087877.	3.412041	27.93427	32.61528
84.14071	809384.1	3.073127	27.22542	32.27242
103.9138	630150.5	2.802982	26.53913	31.98731
128.3335	504934.7	2.572608	25.84218	31.64324
158.4919	337990.0	2.197001	24.48113	30.77451
195.7375	257254.1	1.968964	23.48008	29.99794
241.7358	191976.5	1.743840	22.30193	28.93156
298.5437	144401.5	1.531859	20.96021	27.54048
368.7015	104215.4	1.323013	19.42683	25.79015
455.3463	73197.16	1.119338	17.66019	23.55428
562.3527	52418.35	0.9523972	15.97418	21.20207
694.5056	38562.18	0.8074518	14.28967	18.63623
857.7144	26791.49	0.6715284	12.45148	15.51279
1059.277	18882.61	0.5392824	10.40775	11.79575
1308.208	12929.38	0.4231711	8.368335	8.647358
1615.636	5898.551	0.2553363	5.109169	4.519594
1995.311	2928.331	0.1611889	3.224039	2.517788
2464.209	1608.643	0.1111642	2.223270	1.543372
3043.298	957.0494	8.2680568E-02	1.653592	1.026651
3758.473	573.8574	6.1805658E-02	1.236105	0.6870285
4641.714	342.1400	4.6137404E-02	0.9227301	0.4585985
5732.517	201.9632	3.4218587E-02	0.6843567	0.3037106
7079.659	117.6305	2.5065603E-02	0.5013045	0.1982964
8743.378	66.77499	1.7973442E-02	0.3594653	0.1265736
10798.07	37.14429	1.2714426E-02	0.2542867	7.9493254E-02
13335.62	20.13804	8.7564401E-03	0.1751292	4.8494667E-02
X= 5.00				
LET (MEV/CM)	FLUX	DOSE	DOSE EQ. (26)	DOSE EQ. (60)
1.235000	2.0705118E+08	17.81856	43.17377	47.25764
1.525225	2.0705118E+08	17.81856	43.17377	47.25764
1.883653	2.0705118E+08	17.81856	43.17377	47.25764
2.326311	1.1435334E+08	14.58724	39.05944	43.14332
2.872995	8.1503464E+07	13.22718	37.44088	41.52476
3.548148	6.3092650E+07	12.28189	36.36723	40.45110
4.381963	4.9919792E+07	11.44678	35.44507	39.52895
5.411725	3.9783784E+07	10.65461	34.58638	38.67026
6.683480	3.1923306E+07	9.894417	33.77166	37.85554
8.254098	2.4736374E+07	9.022814	32.83395	36.91783
10.19381	1.6026879E+07	7.754657	31.45841	35.54229

12.58936
15.54786
19.20160
23.71398
29.28676
36.16915
44.66890
55.16610
68.13013
84.14071
103.9138
128.3335
158.4919
195.7375
241.7358
298.5437
368.7015
455.3463
562.3527
694.5056
857.7144
1059.277
1308.208
1615.636
1995.311
2464.209
3043.298
3758.473
4641.714
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7079.659
8743.378
10798.07
13335.62

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5519376.
3963731.
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1684699.
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1054332.
781423.4
606057.6
483668.6
323165.8
245621.5
182539.7
136988.9
98226.08
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49931.12
36451.30
26186.74
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5.5989150E-02
4.1790400E-02
3.0982036E-02
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1.6237872E-02
1.1469165E-02
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0.1576874

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14.48525
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7.1679145E-02
4.3644756E-02

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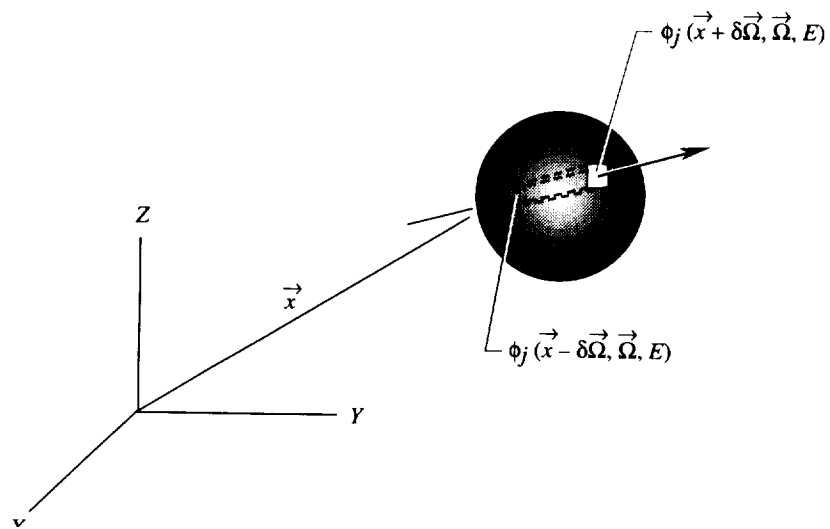
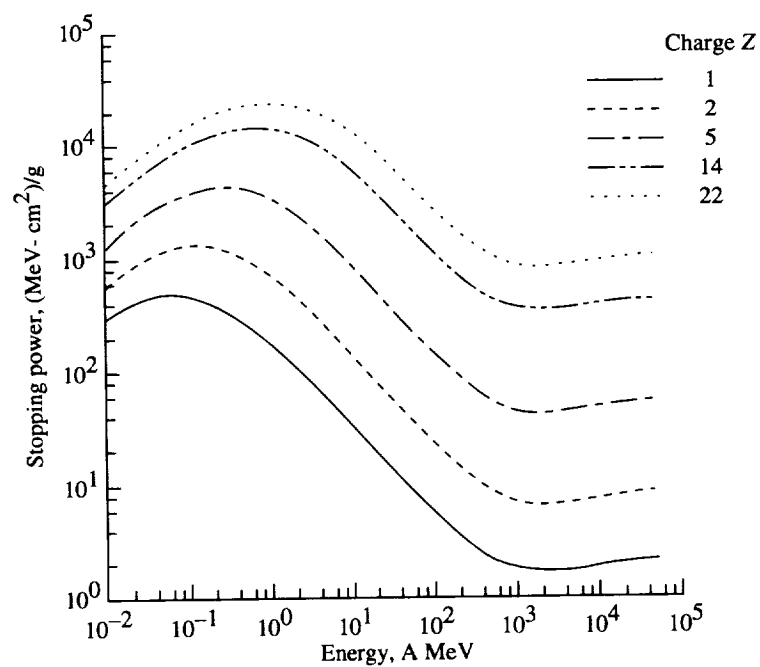
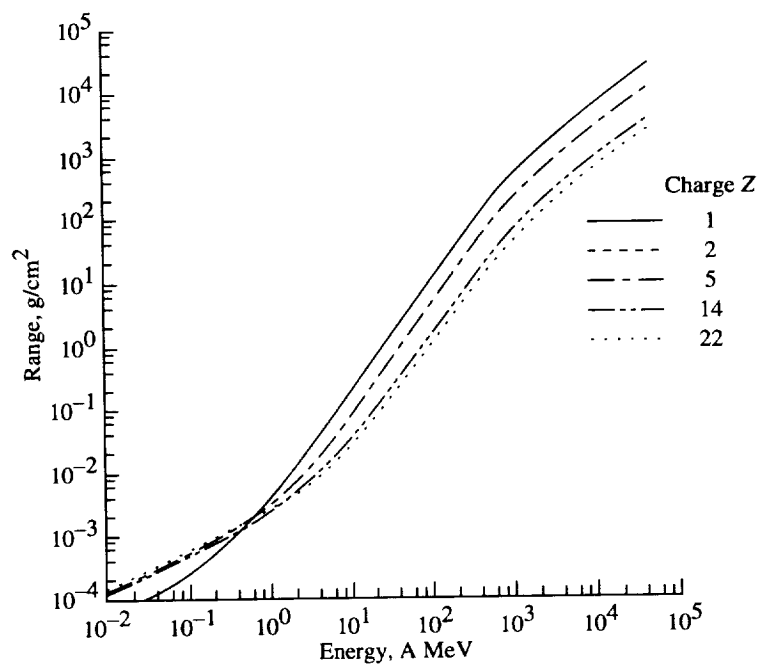
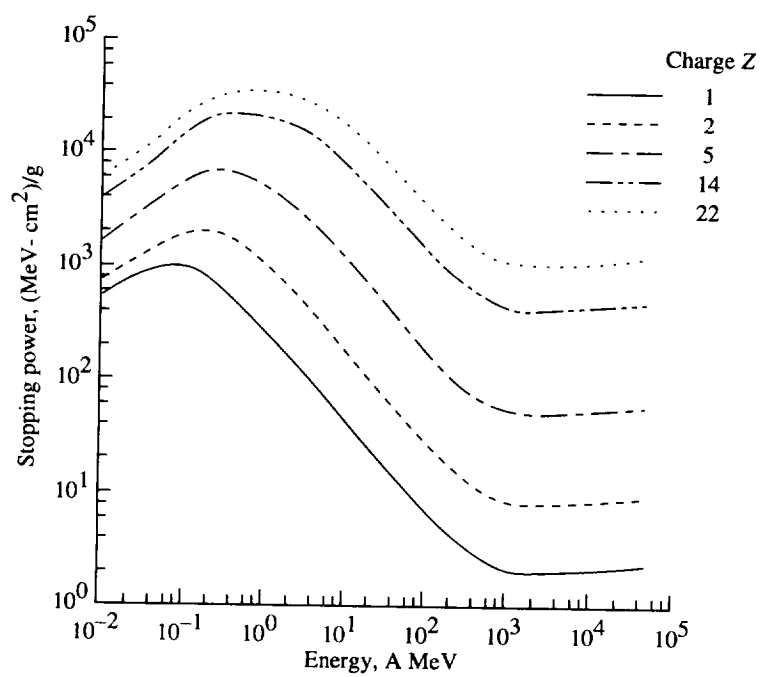
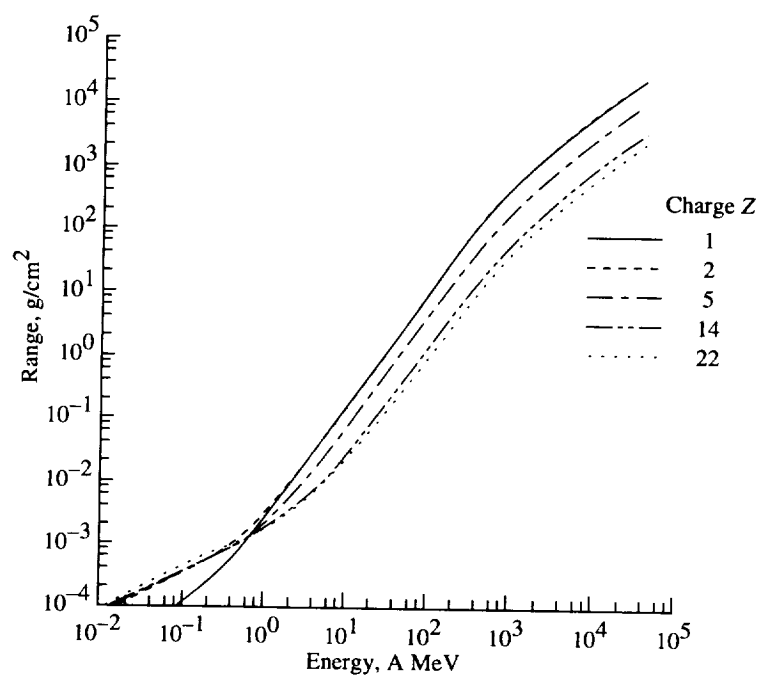


Figure 1. Transport of particles through spherical region.



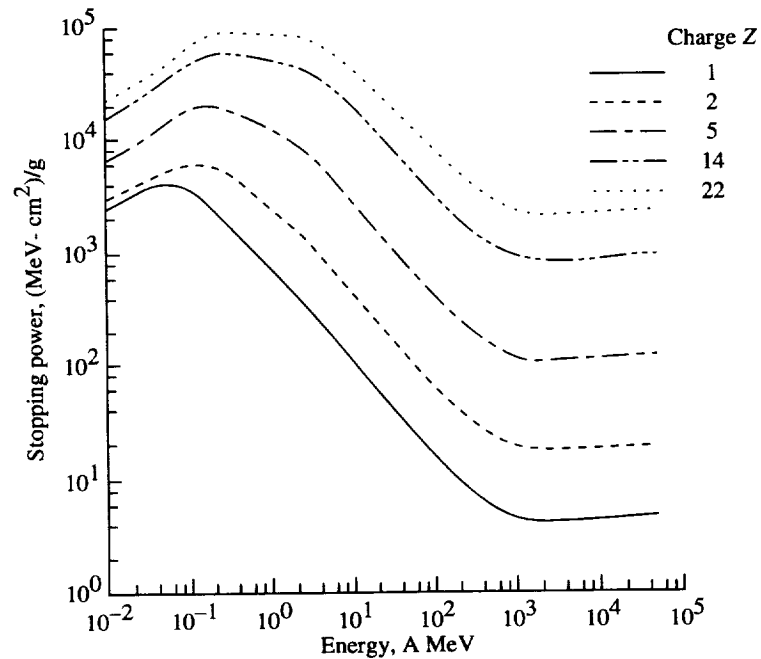
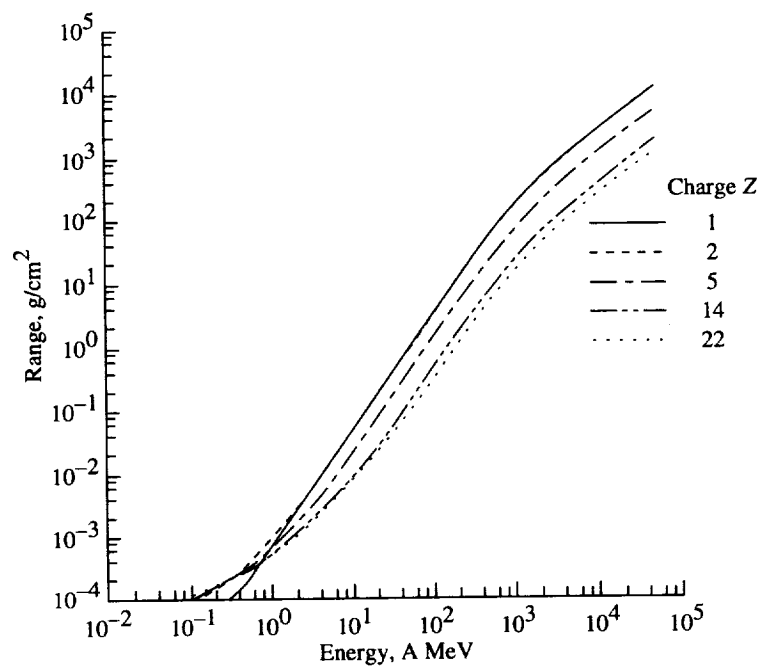
(a) Range and stopping power in aluminum.

Figure 2. Linear energy transfer (LET).



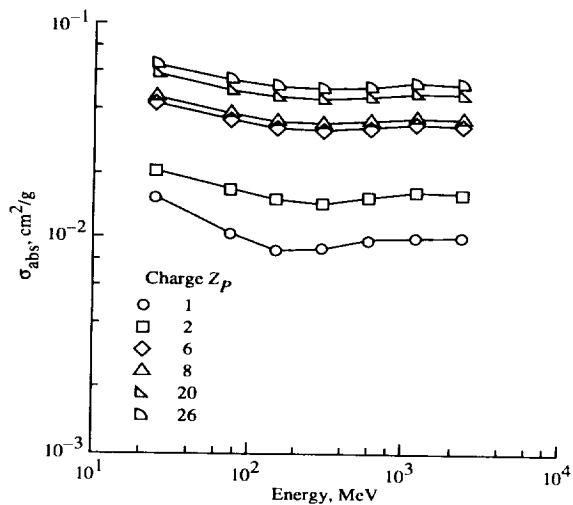
(b) Range and stopping power in water.

Figure 2. Continued.

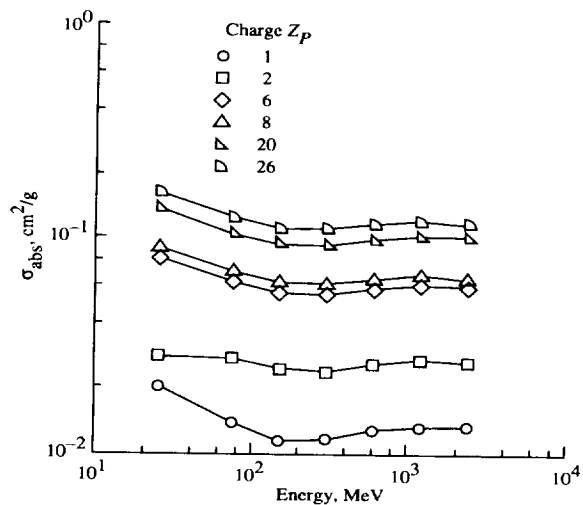


(c) Range and stopping power in liquid hydrogen.

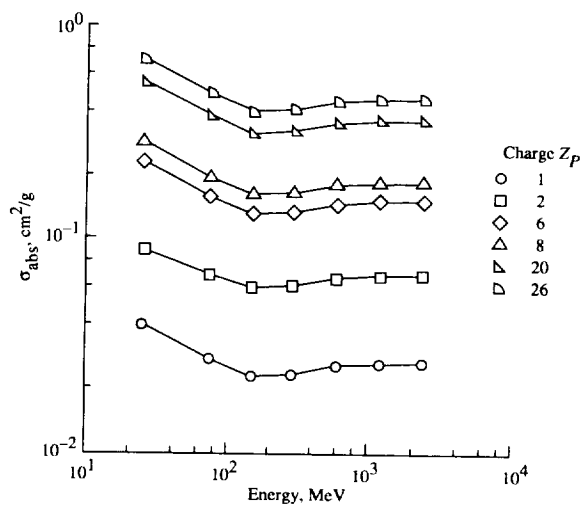
Figure 2. Concluded.



(a) Aluminum target.



(b) Water target.



(c) Liquid hydrogen target.

Figure 3. Absorption cross section σ_{abs} .

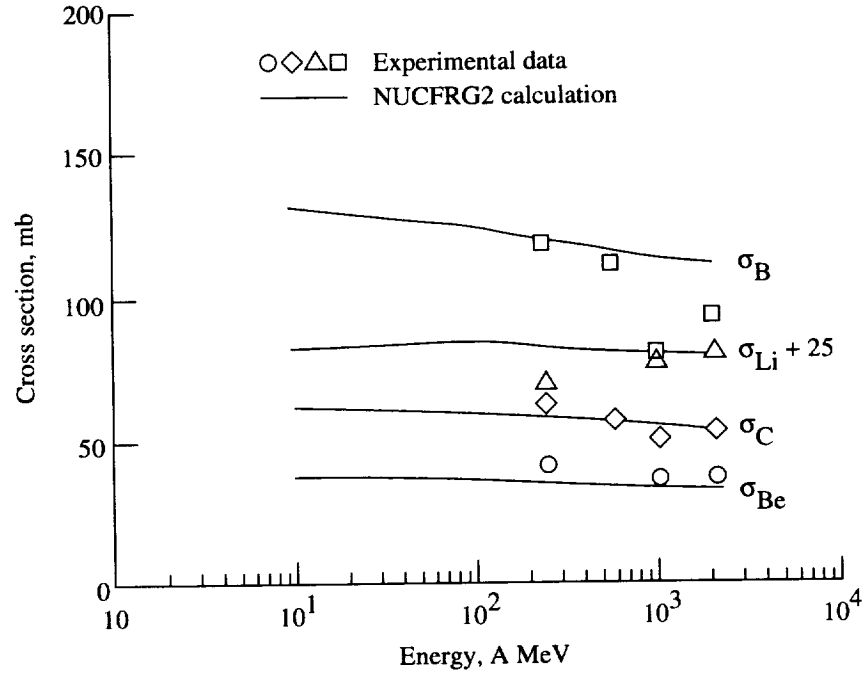


Figure 4. Charge-removal cross sections for carbon on carbon.

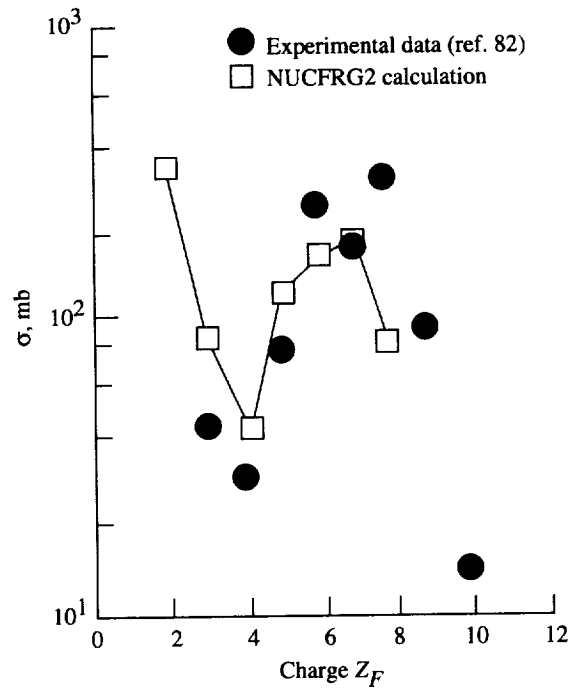
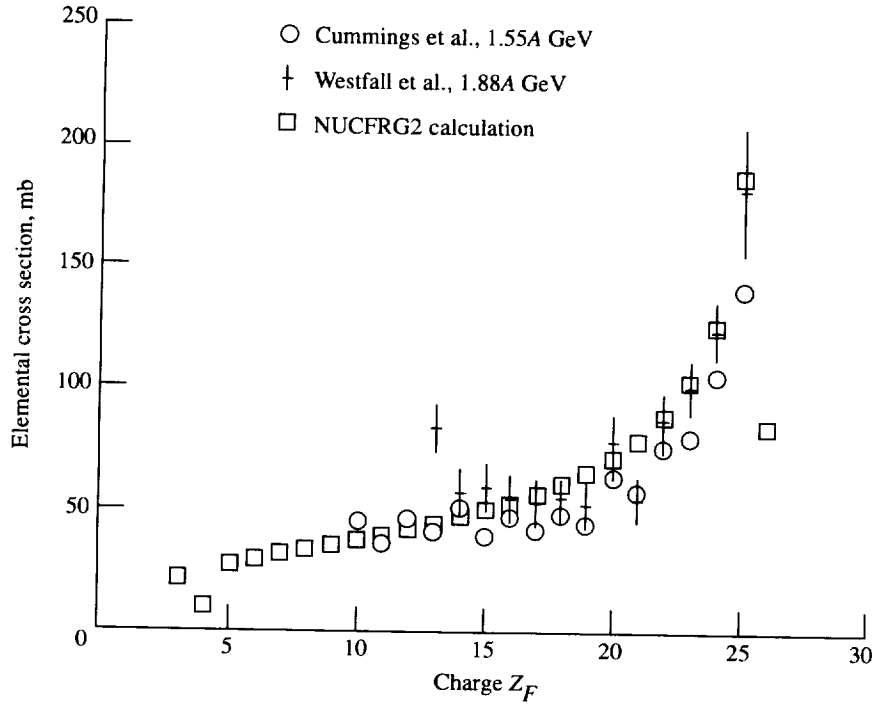
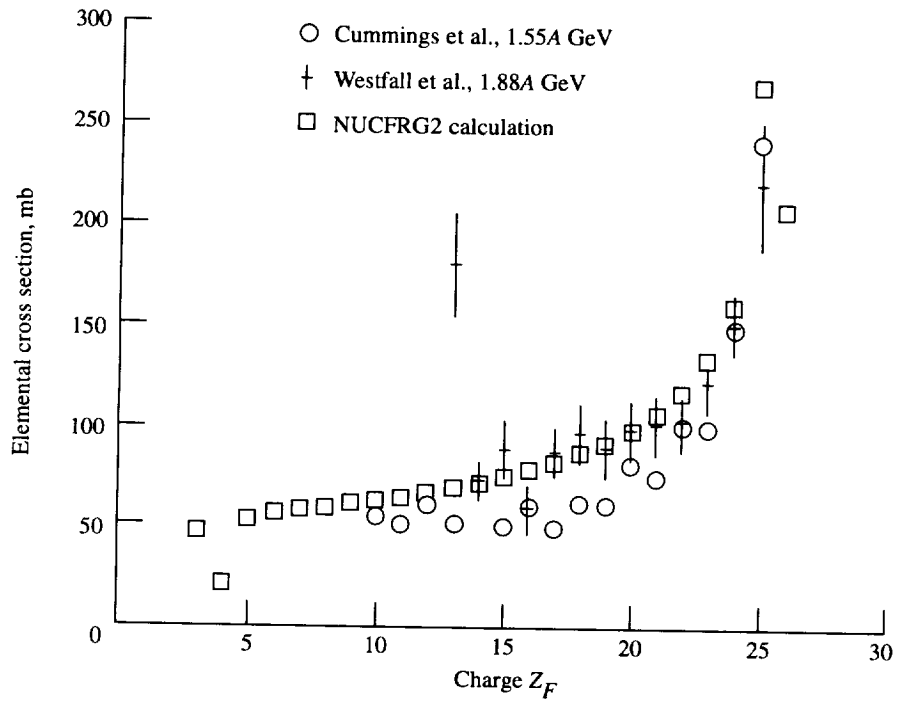


Figure 5. Charge-removal cross sections for 11.7A-MeV oxygen projectile on molybdenum target.

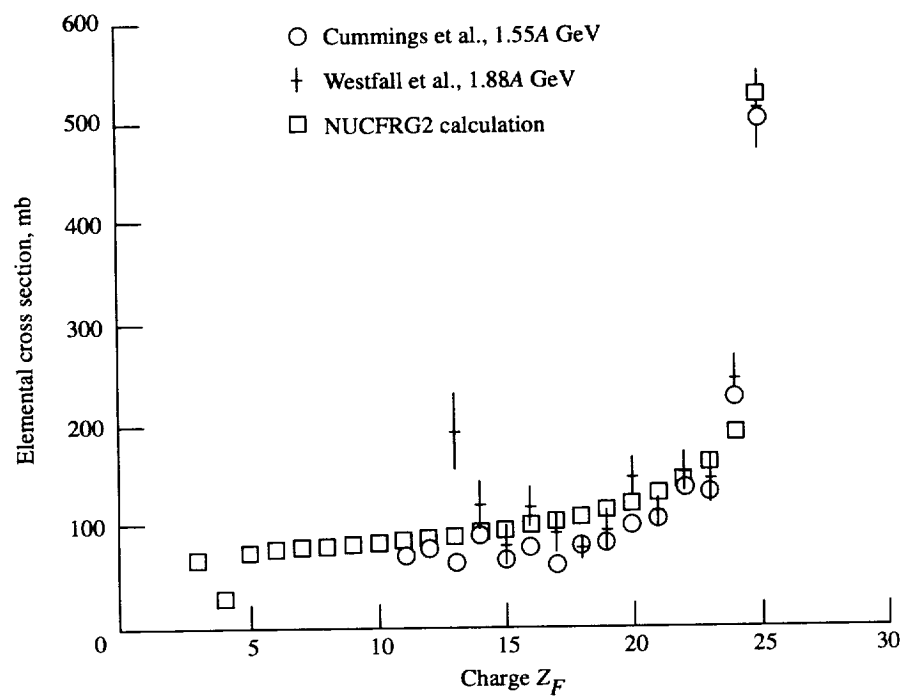


(a) Carbon target.



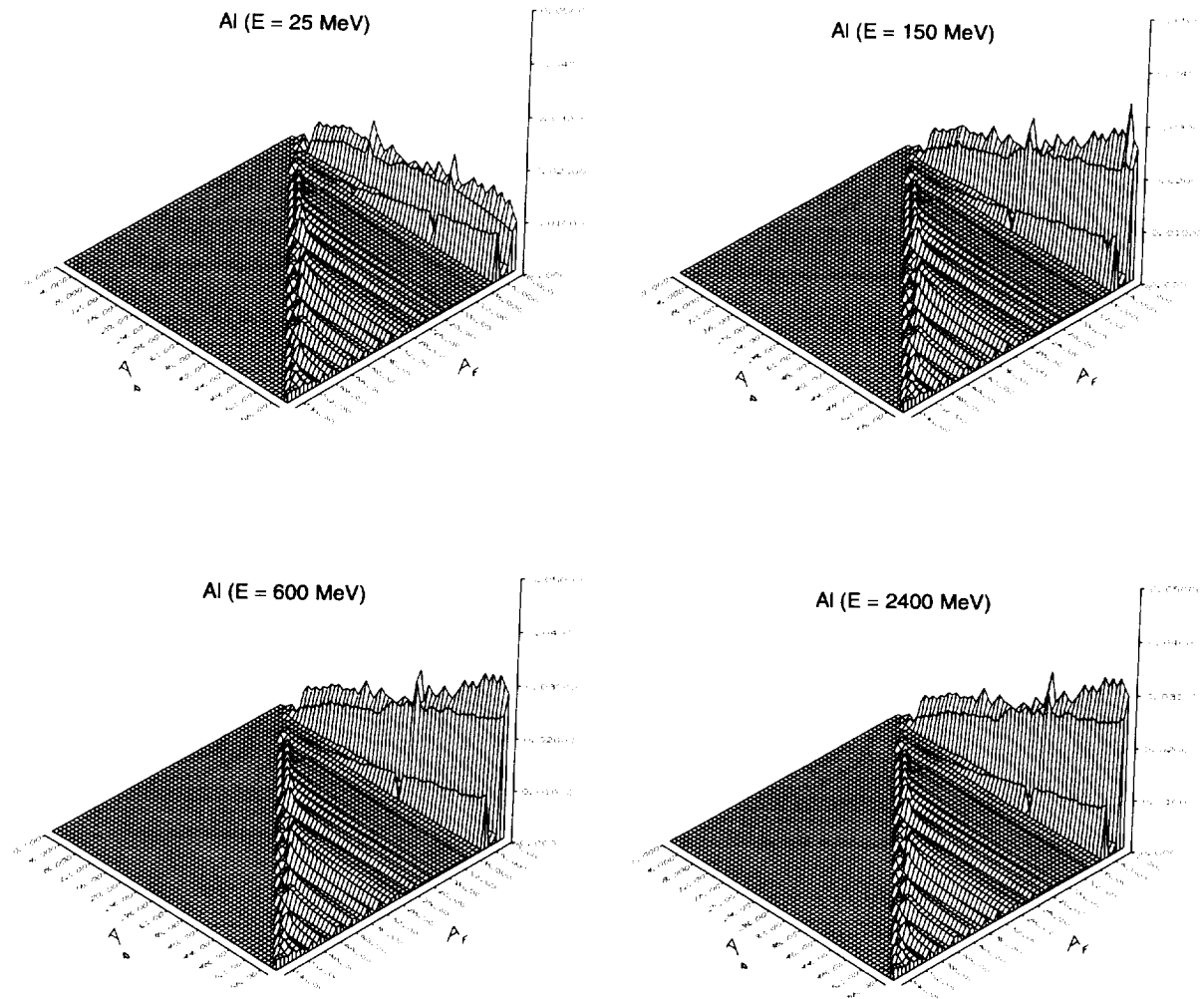
(b) Copper target.

Figure 6. Charge-removal cross sections for 1.88A-GeV iron projectile.



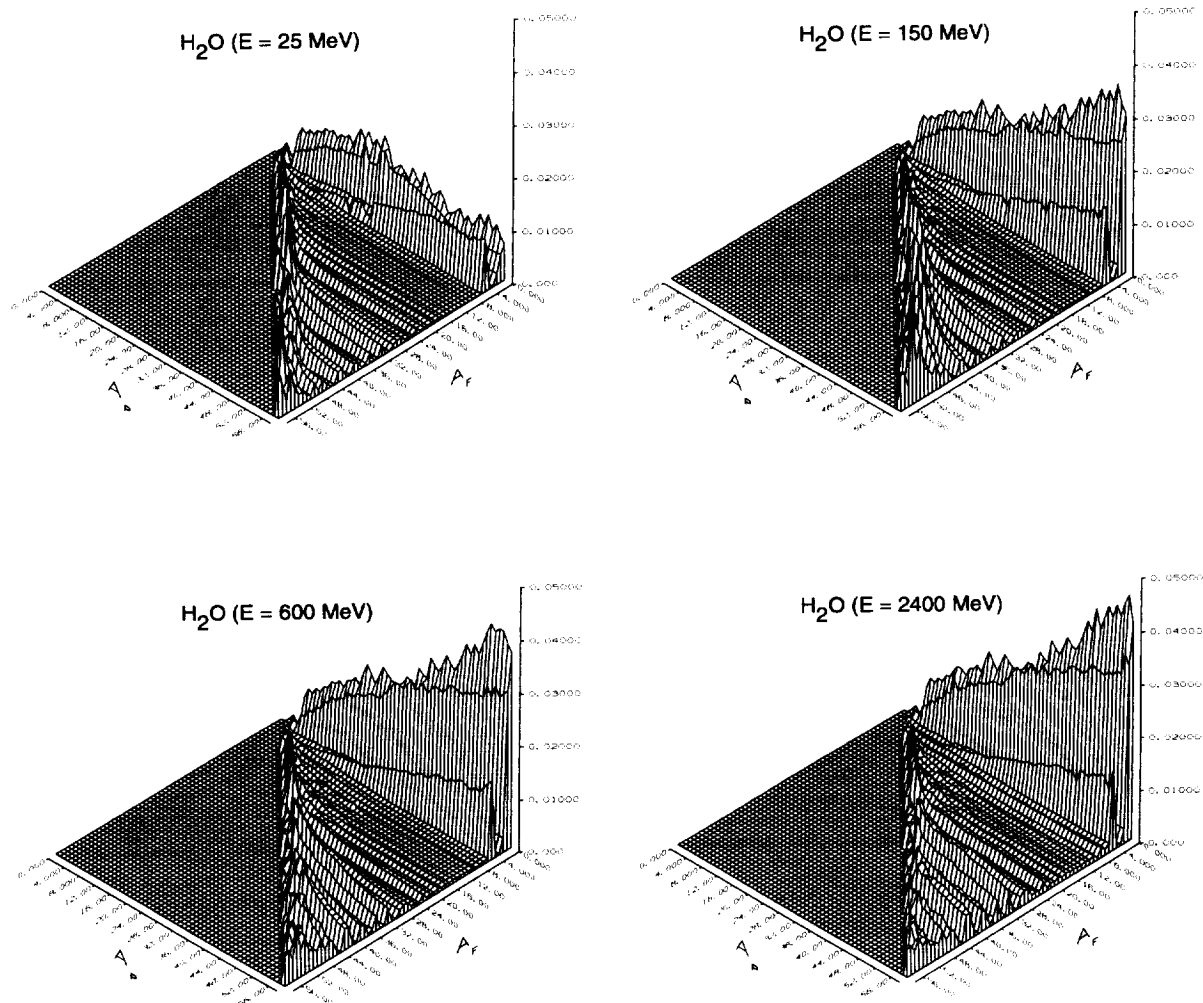
(c) Lead target.

Figure 6. Concluded.



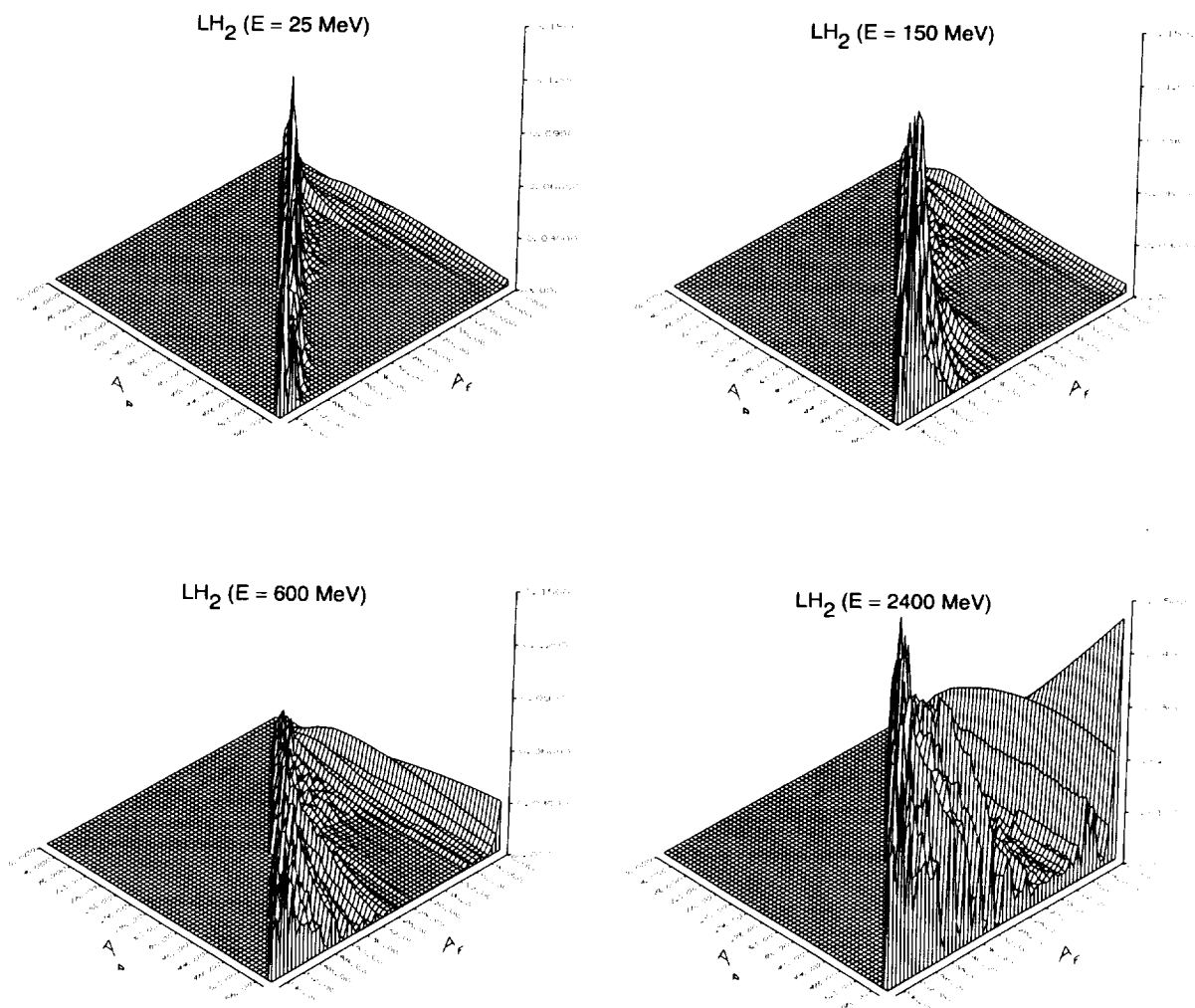
(a) Four energy levels in aluminum.

Figure 7. Fragmentation cross sections.



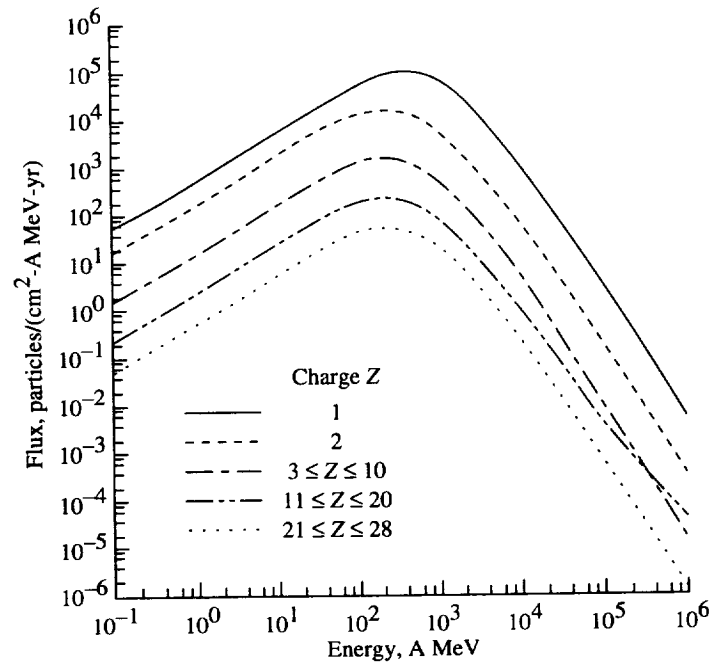
(b) Four energy levels in water.

Figure 7. Continued.

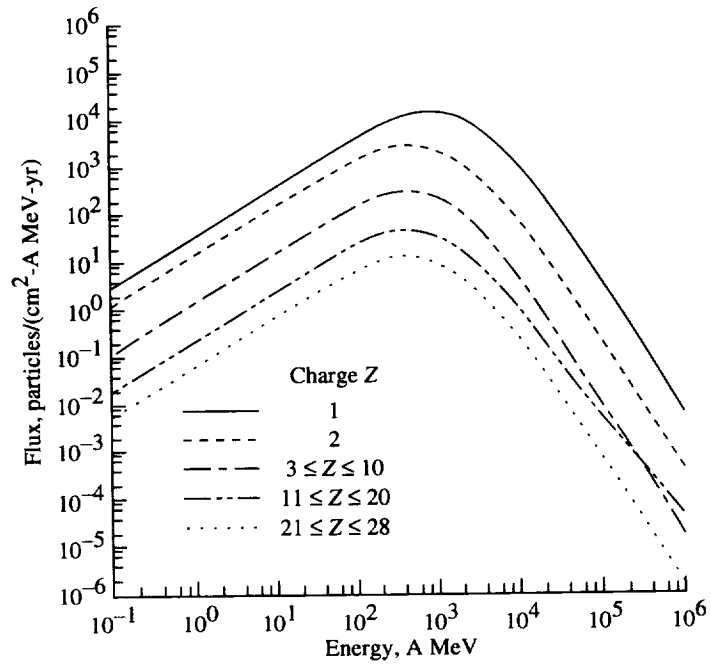


(c) Four energy levels in liquid hydrogen.

Figure 7. Concluded.



(a) GCR ion flux for 1977 solar minimum.



(b) GCR ion flux for 1981 solar maximum.

Figure 8. Differential fluence spectra.

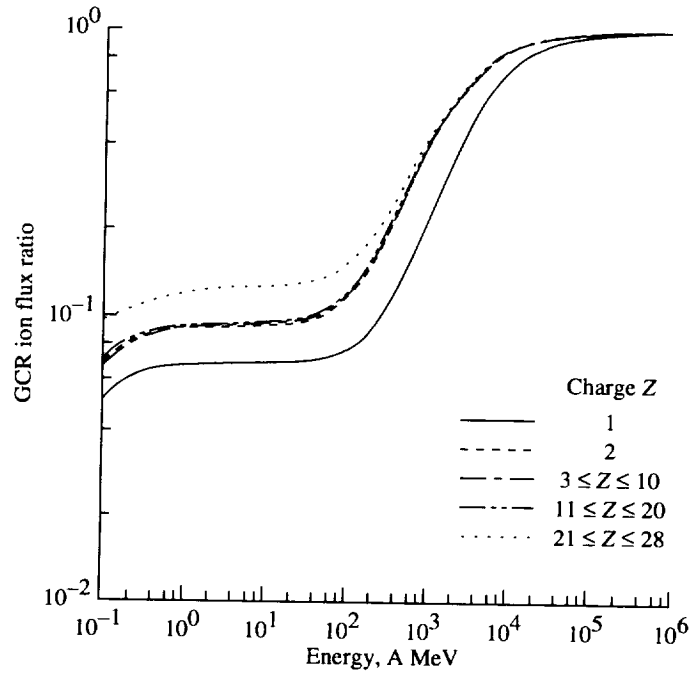


Figure 9. GCR ion flux ratio of 1981 solar maximum to 1977 solar minimum.

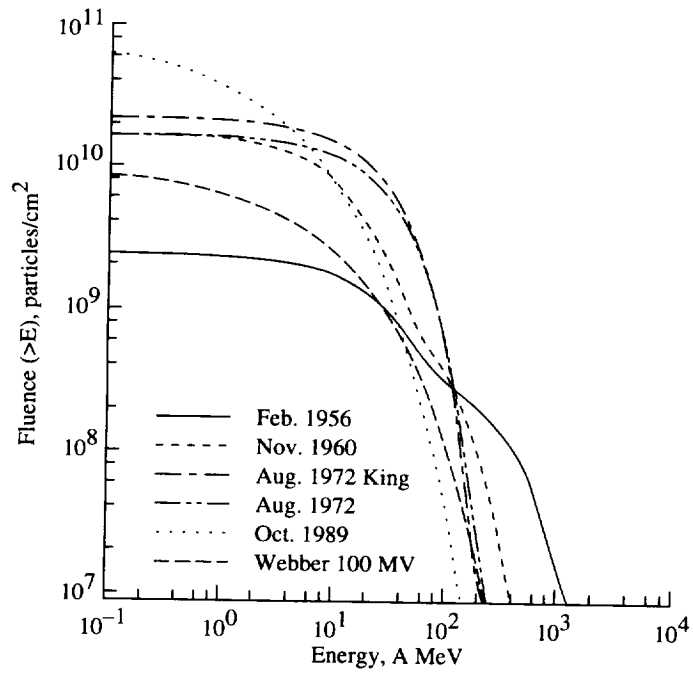
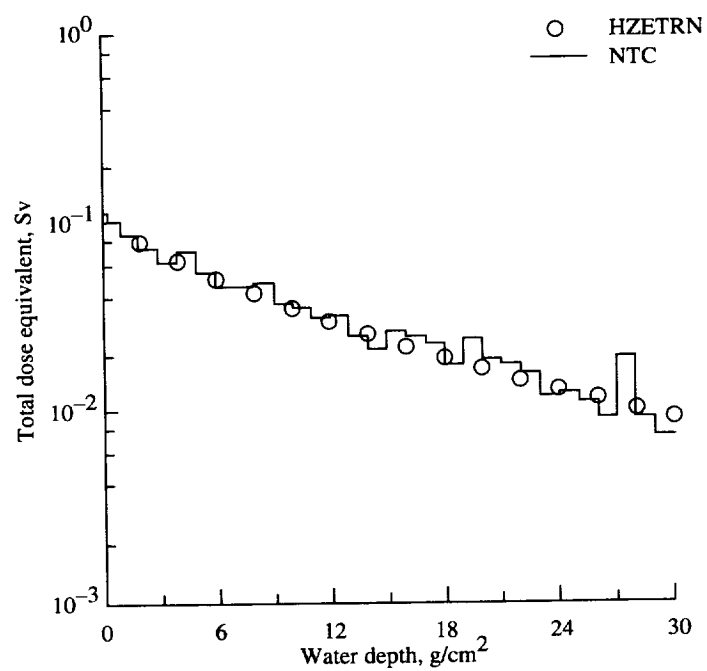
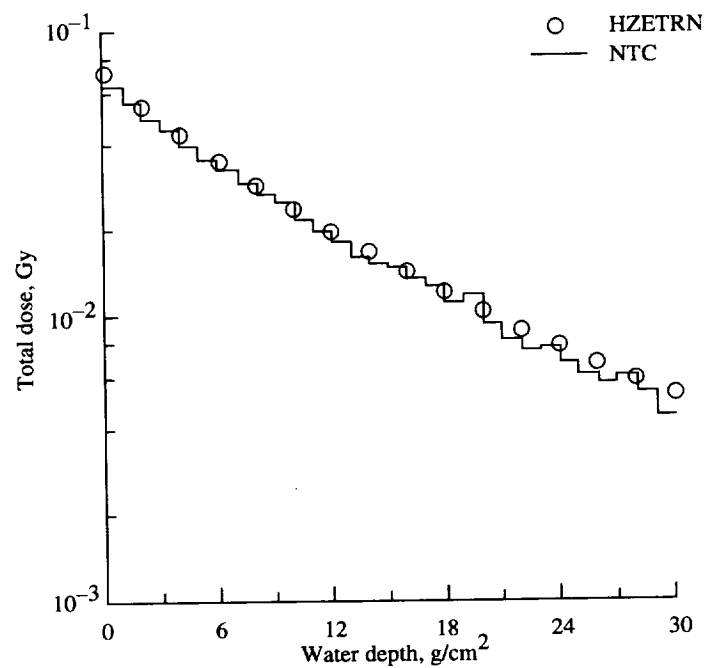
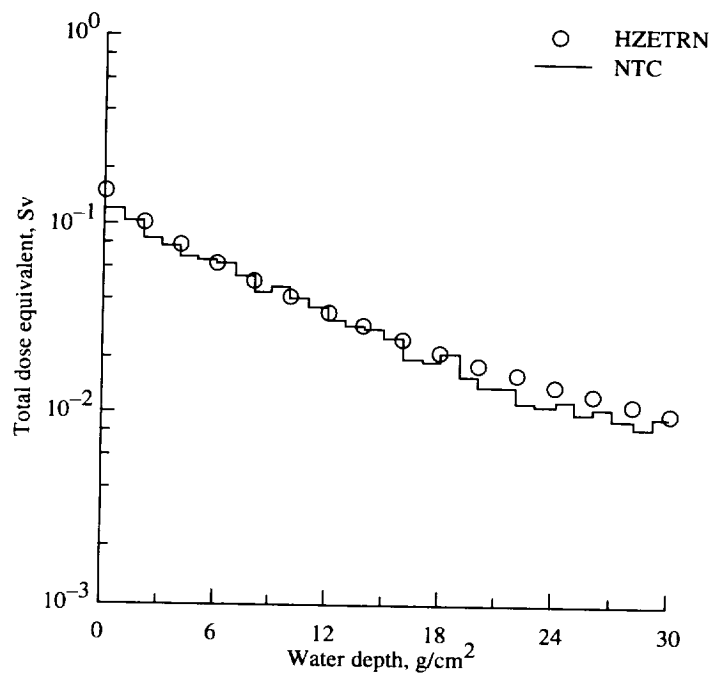
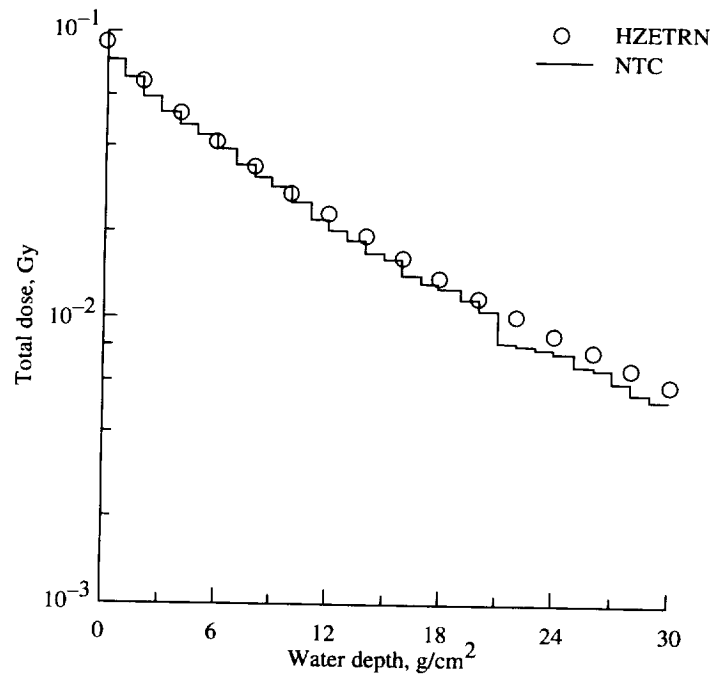


Figure 10. Integral fluence spectra of important solar particle events.



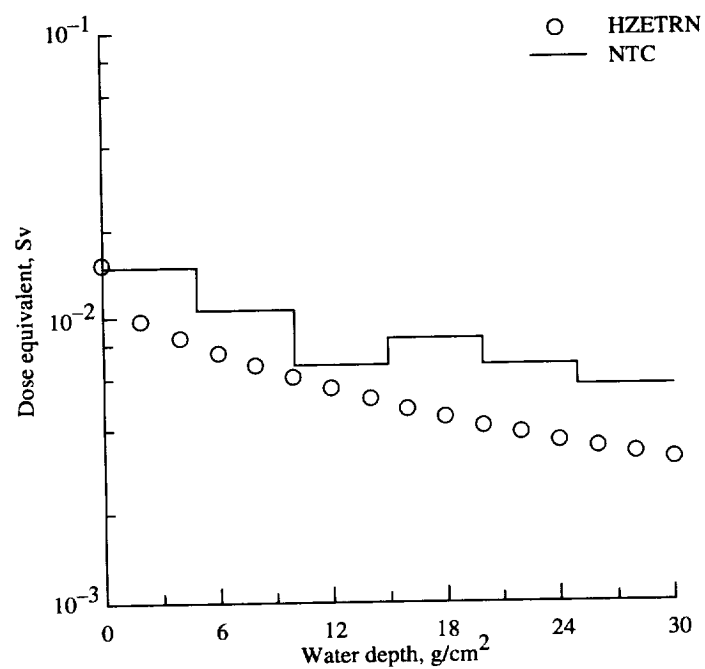
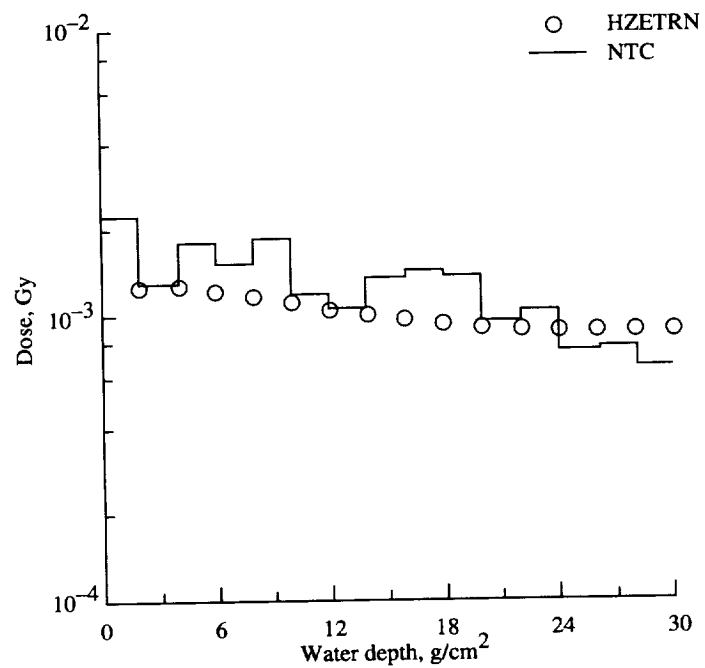
(a) Aluminum shield on water. 20 g/cm² Al; 30 g/cm² water.

Figure 11. Total dose and total dose equivalent.



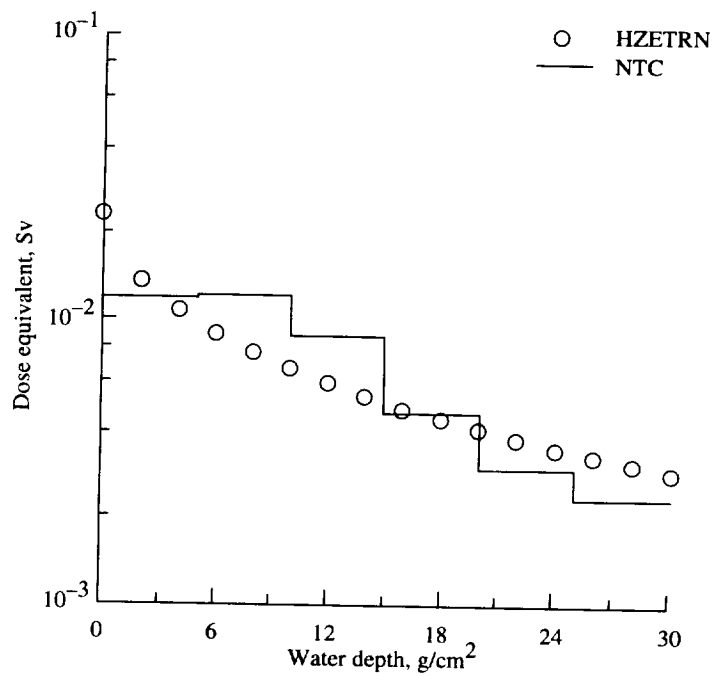
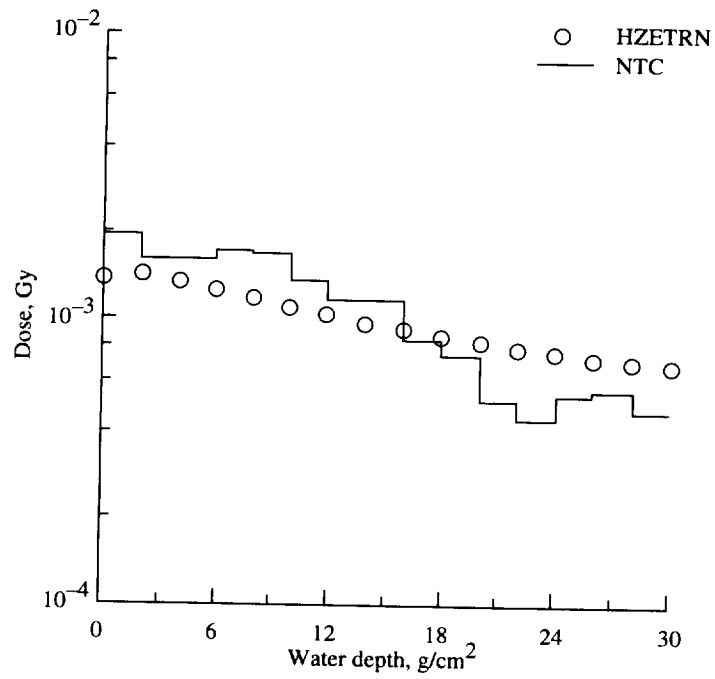
(b) Iron shield on water. 20 g/cm² Fe; 30 g/cm² water.

Figure 11. Concluded.



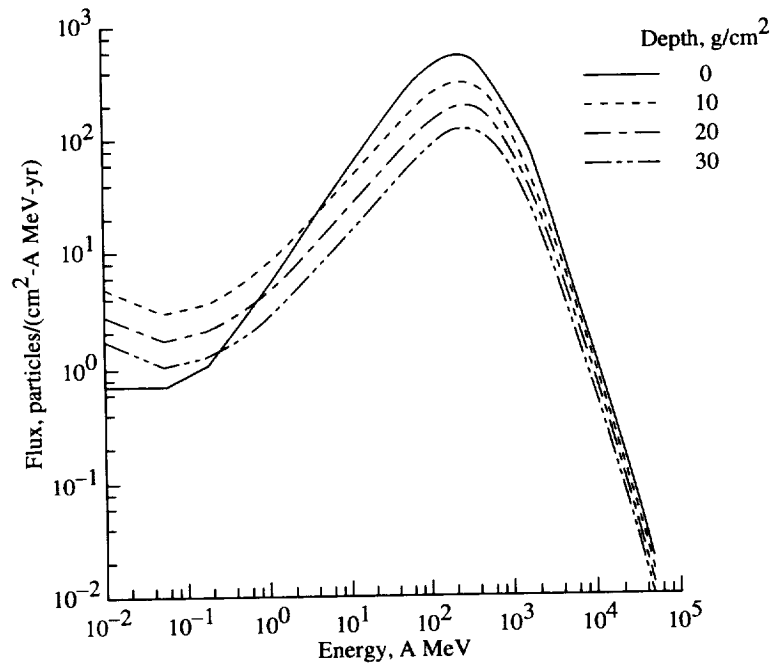
(a) Aluminum shield on water. 20 g/cm² Al; 30 g/cm² water.

Figure 12. Secondary neutron dose and dose equivalent.

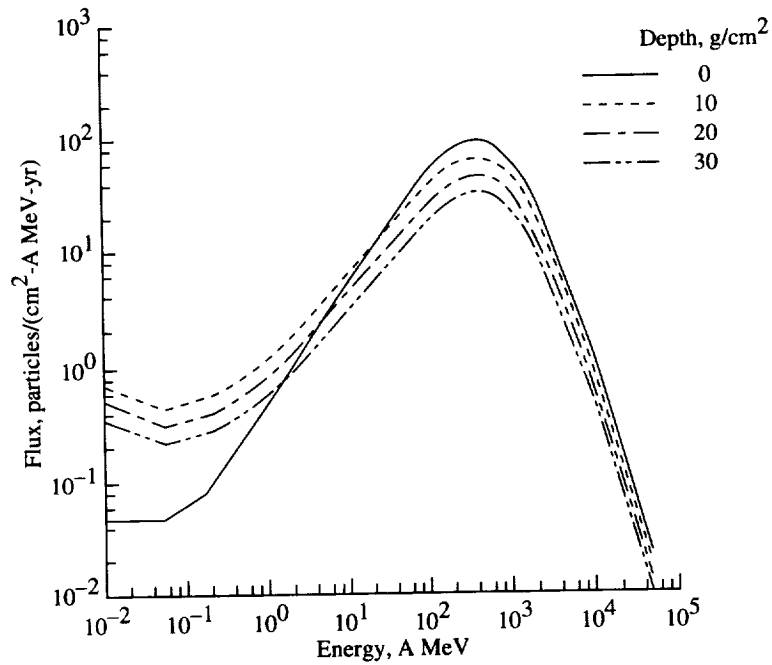


(b) Iron shield on water. 20 g/cm² Fe; 30 g/cm² water.

Figure 12. Concluded.

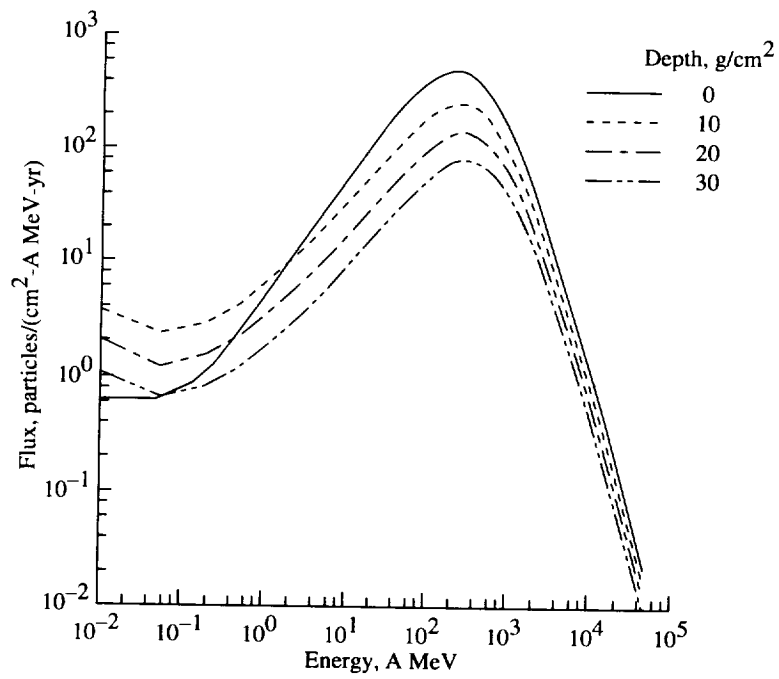


(a) 1977 solar minimum.

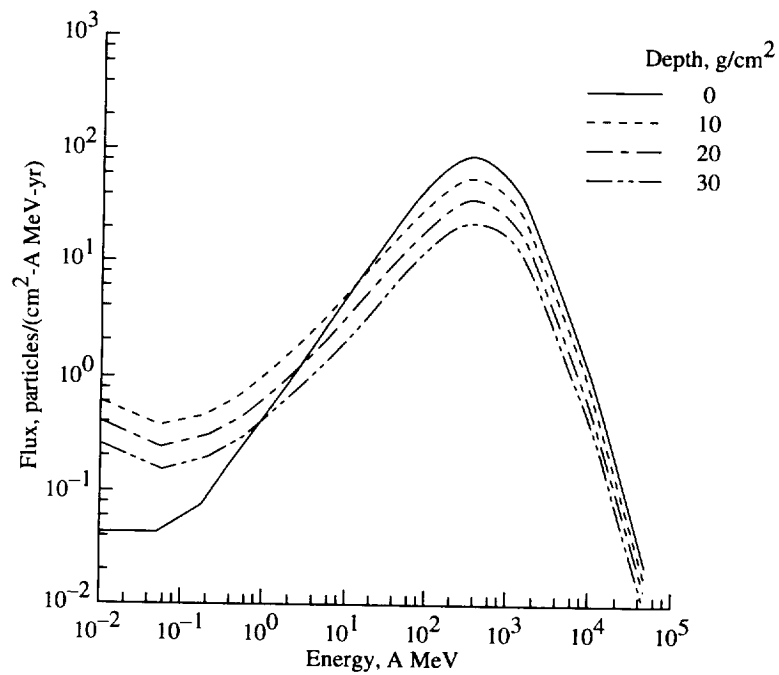


(b) 1981 solar maximum.

Figure 13. GCR energy flux for carbon ion in aluminum.

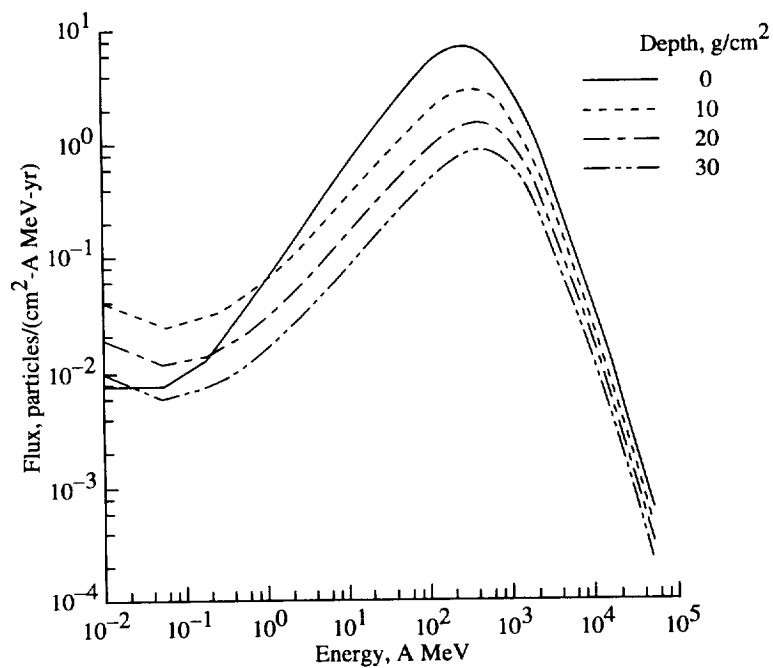


(a) 1977 solar minimum.

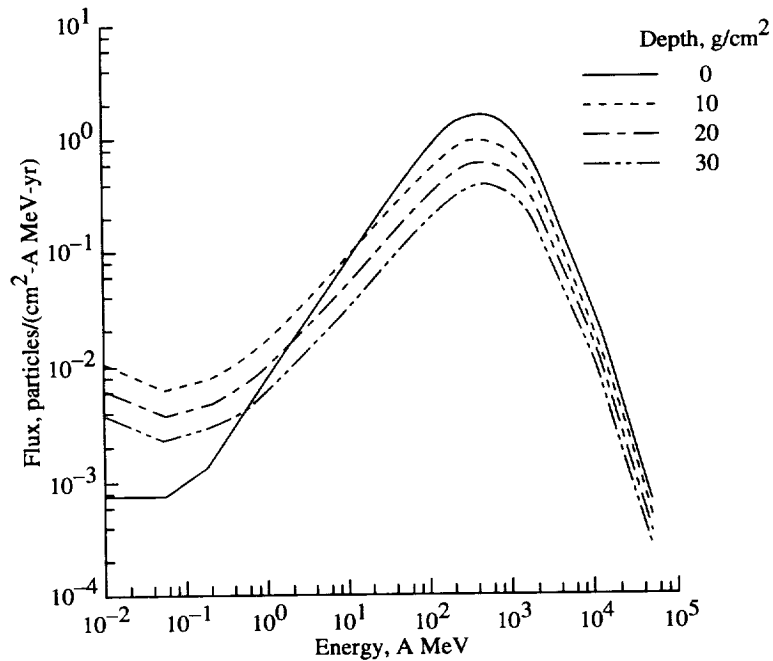


(b) 1981 solar maximum.

Figure 14. GCR energy flux for oxygen ion in aluminum.

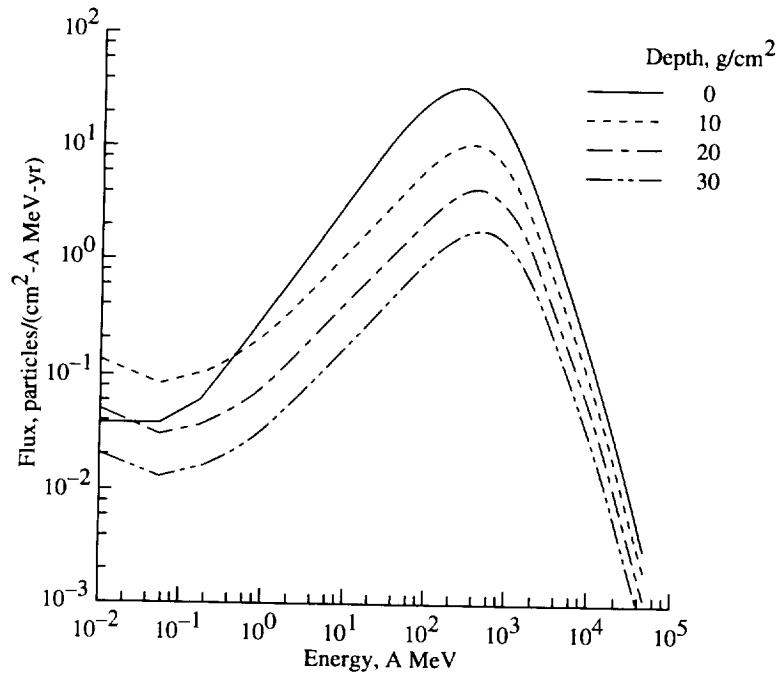


(a) 1977 solar minimum.

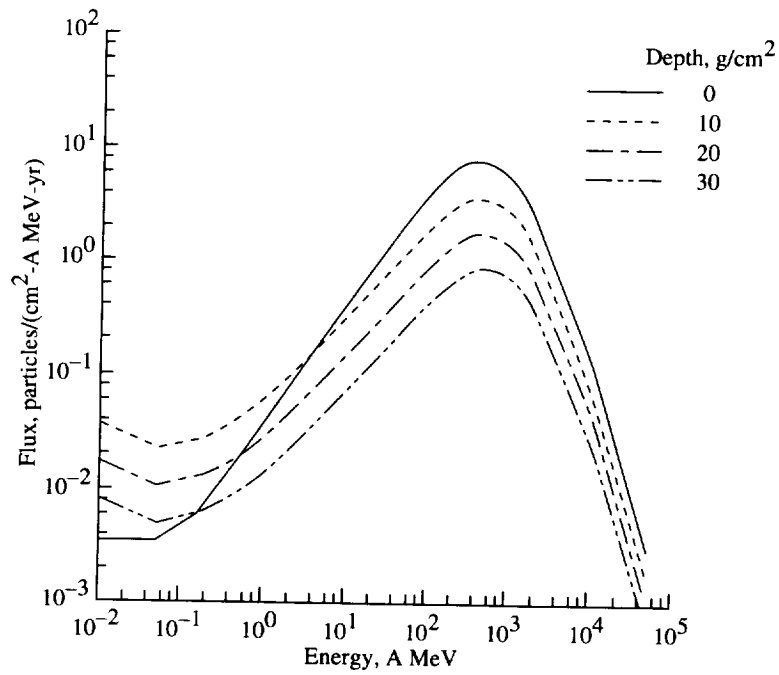


(b) 1981 solar maximum.

Figure 15. GCR energy flux for calcium ion in aluminum.

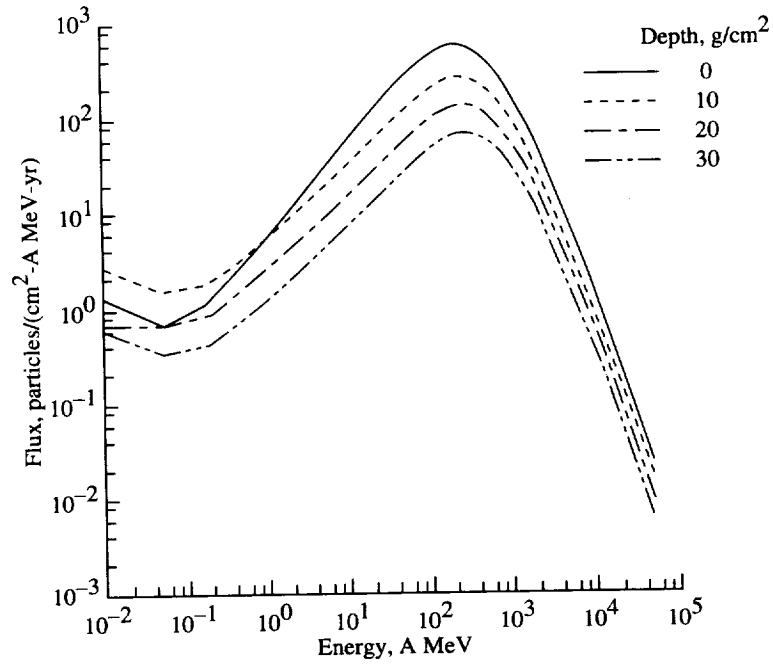


(a) 1977 solar minimum.

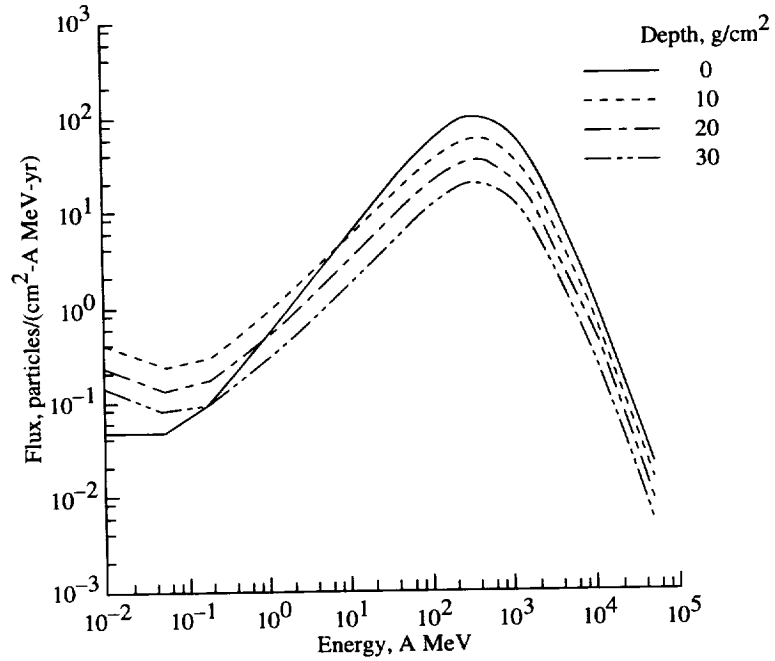


(b) 1981 solar maximum.

Figure 16. GCR energy flux for iron ion in aluminum.

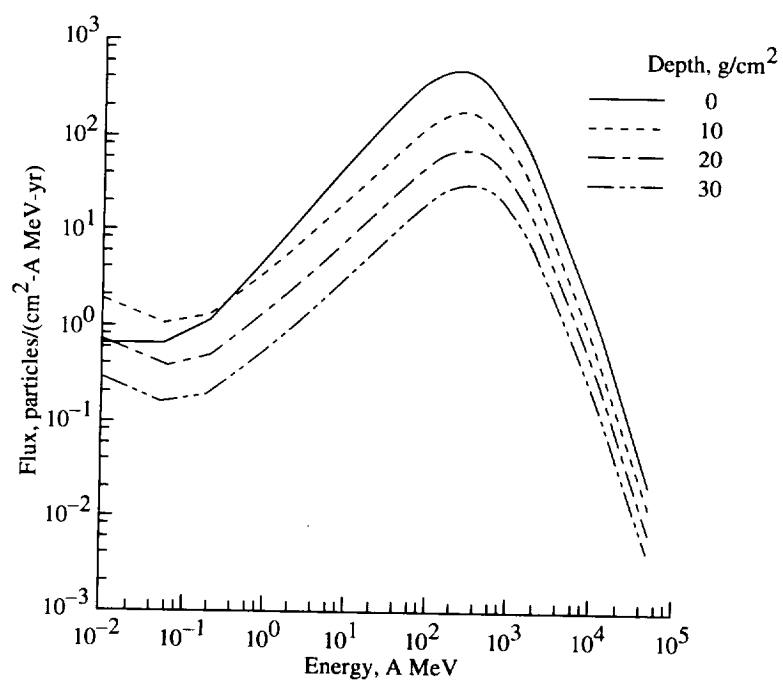


(a) 1977 solar minimum.

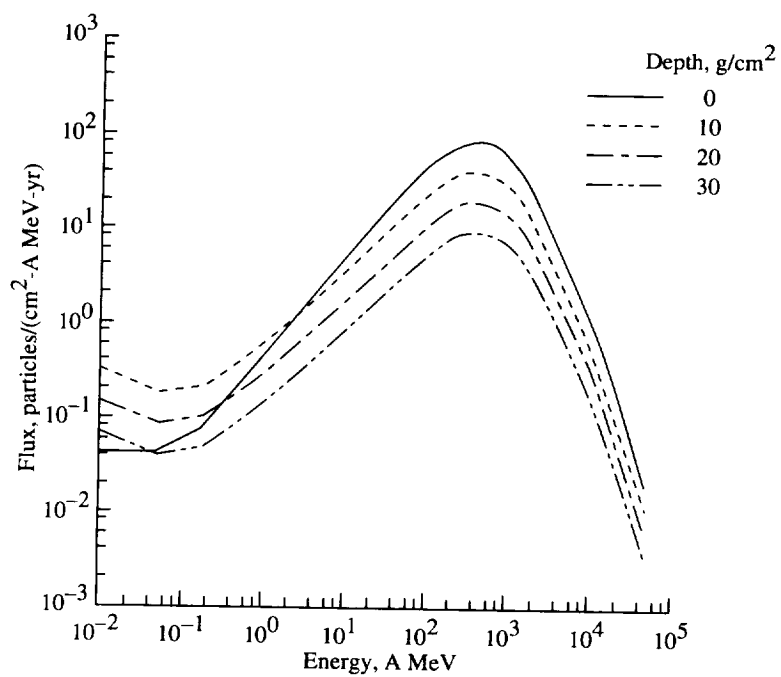


(b) 1981 solar maximum.

Figure 17. GCR energy flux for carbon ion in water.

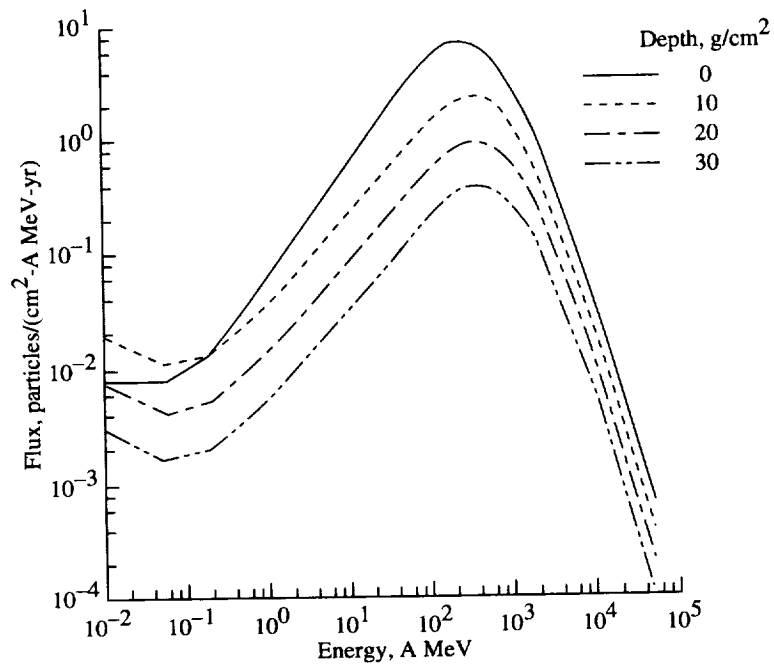


(a) 1977 solar minimum.

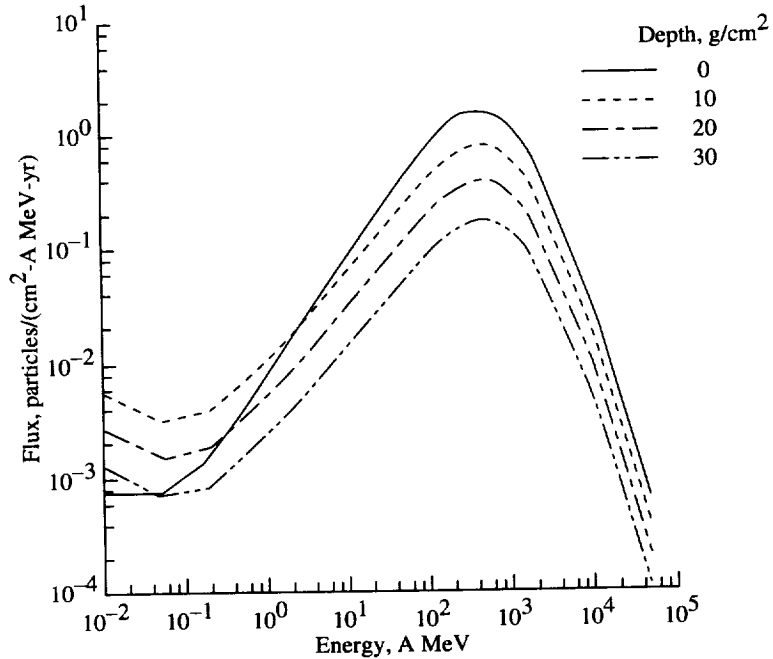


(b) 1981 solar maximum.

Figure 18. GCR energy flux for oxygen ion in water.

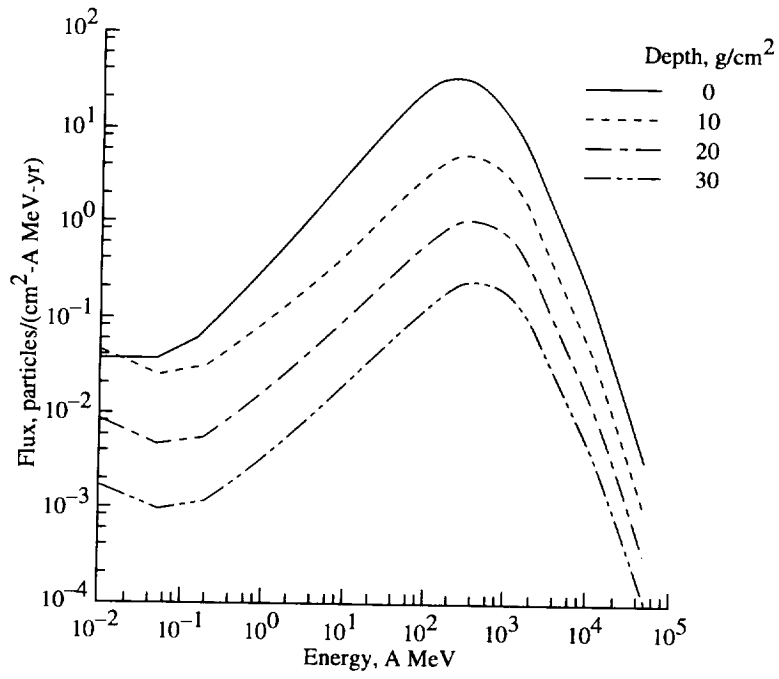


(a) 1977 solar minimum.

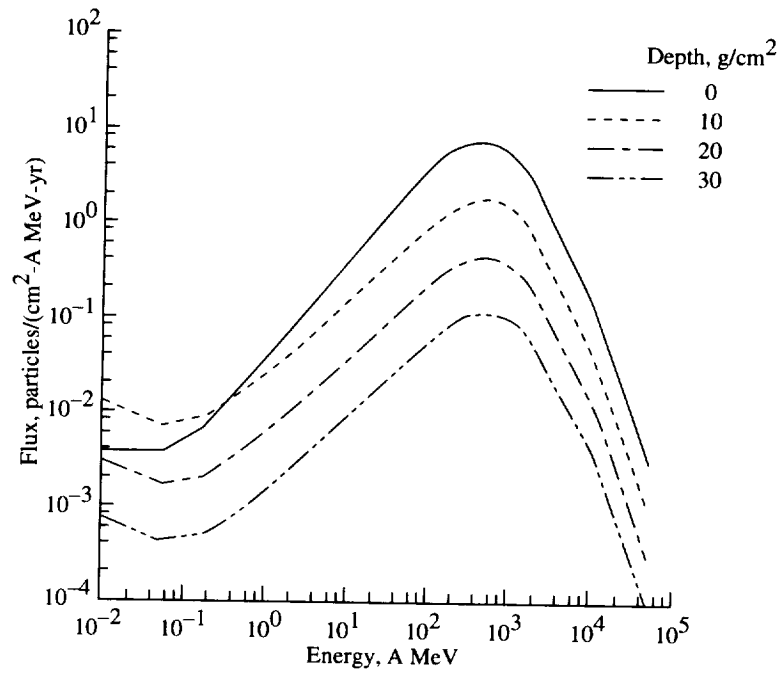


(b) 1981 solar maximum.

Figure 19. GCR energy flux for calcium ion in water.

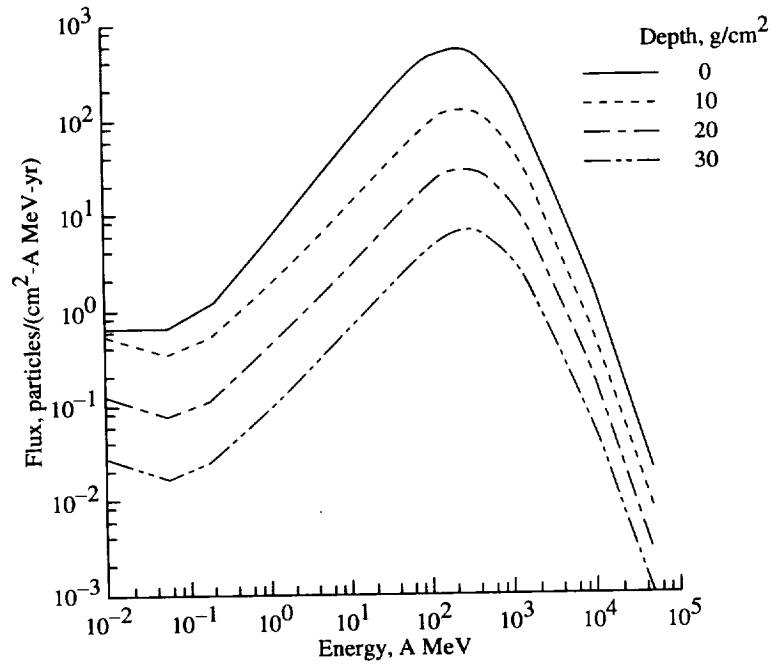


(a) 1977 solar minimum.

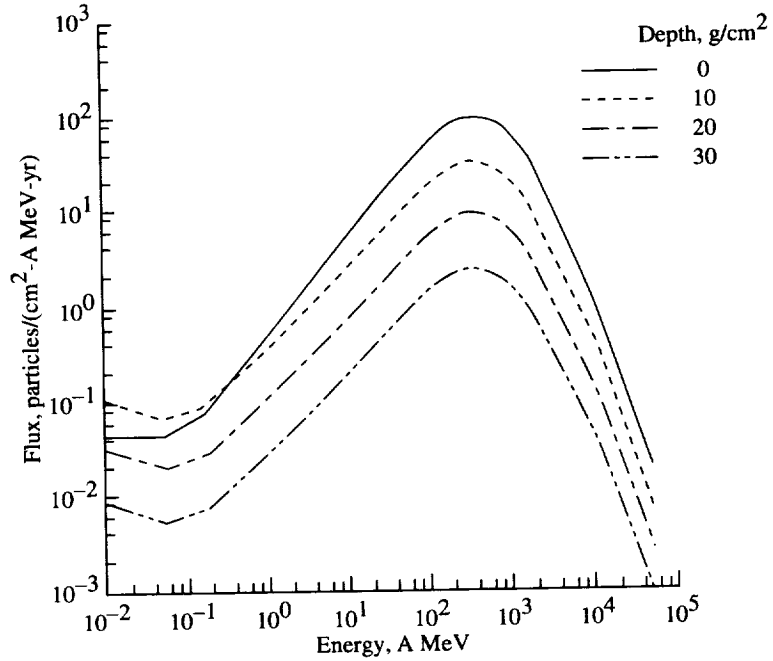


(b) 1981 solar maximum.

Figure 20. GCR energy flux for iron ion in water.

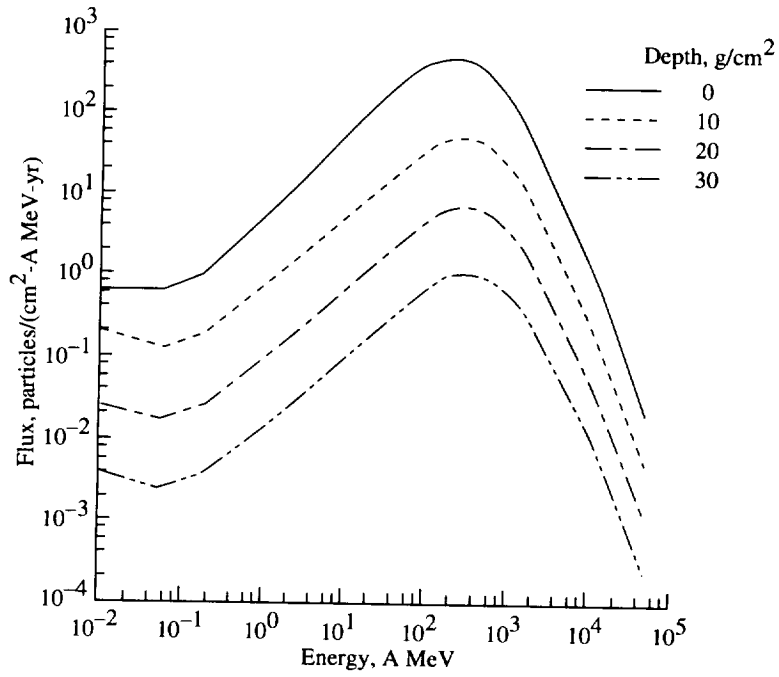


(a) 1977 solar minimum.

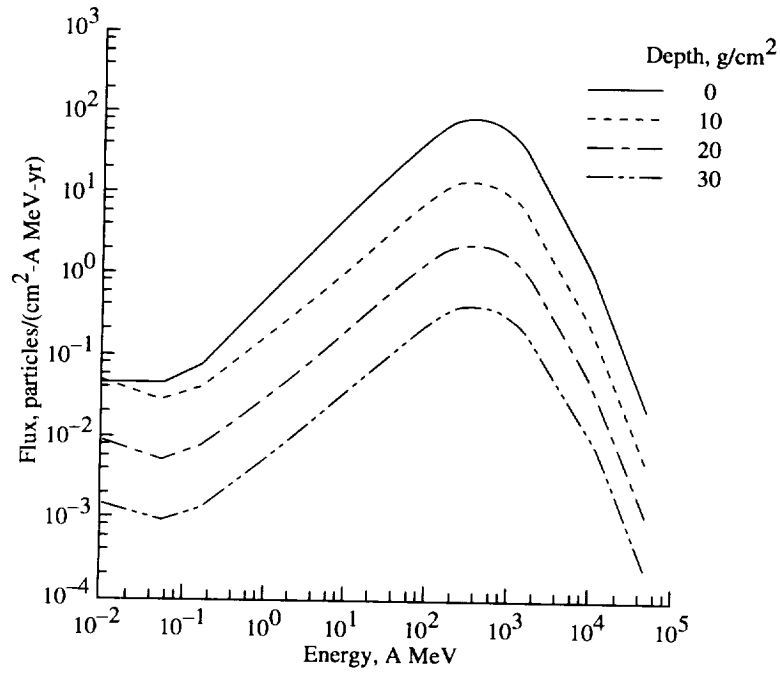


(b) 1981 solar maximum.

Figure 21. GCR energy flux for carbon ion in liquid hydrogen.

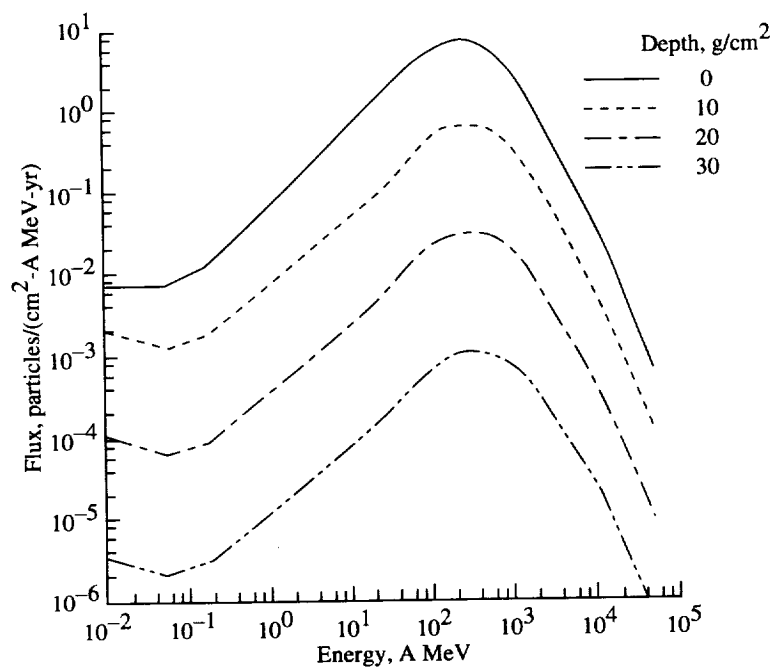


(a) 1977 solar minimum.

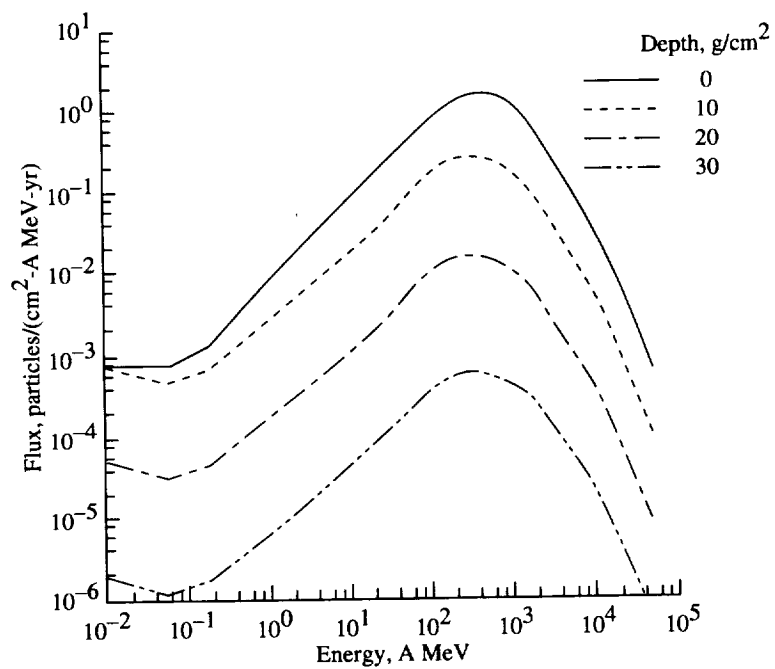


(b) 1981 solar maximum.

Figure 22. GCR energy flux for oxygen ion in liquid hydrogen.

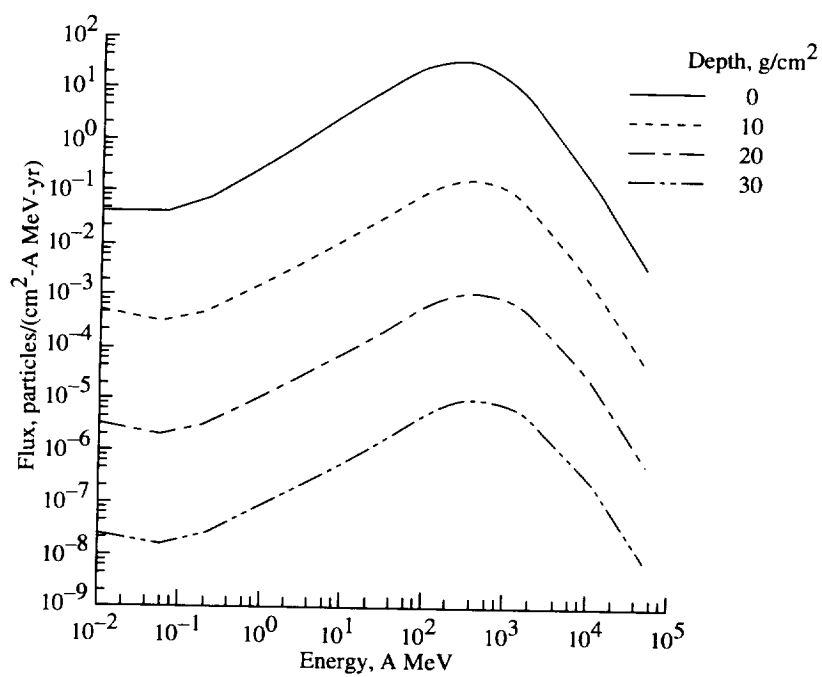


(a) 1977 solar minimum.

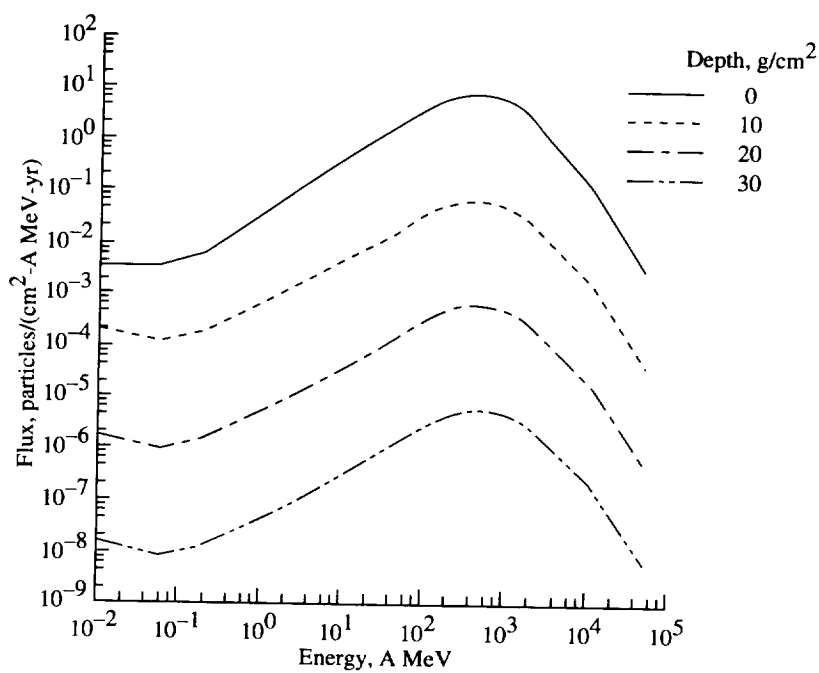


(b) 1981 solar maximum.

Figure 23. GCR energy flux for calcium ion in liquid hydrogen.

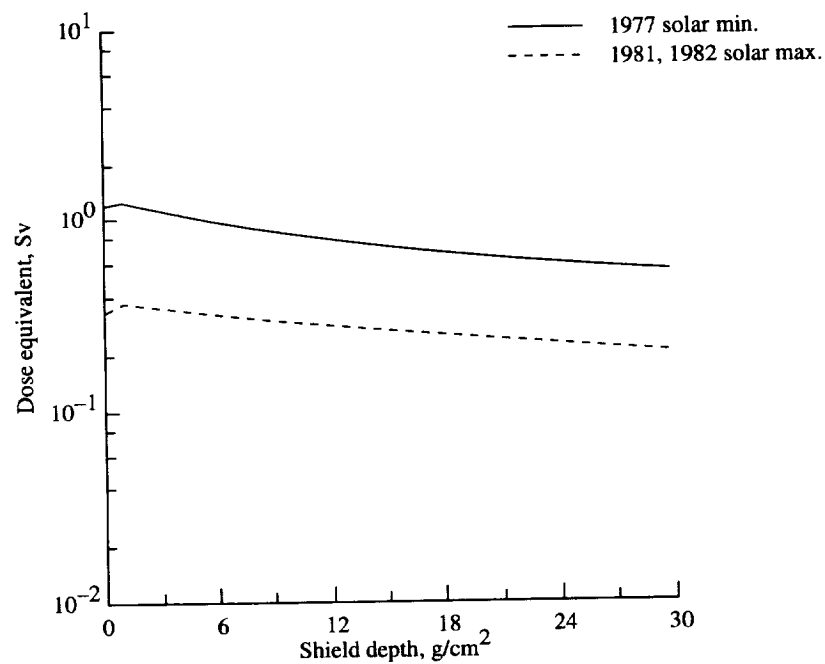
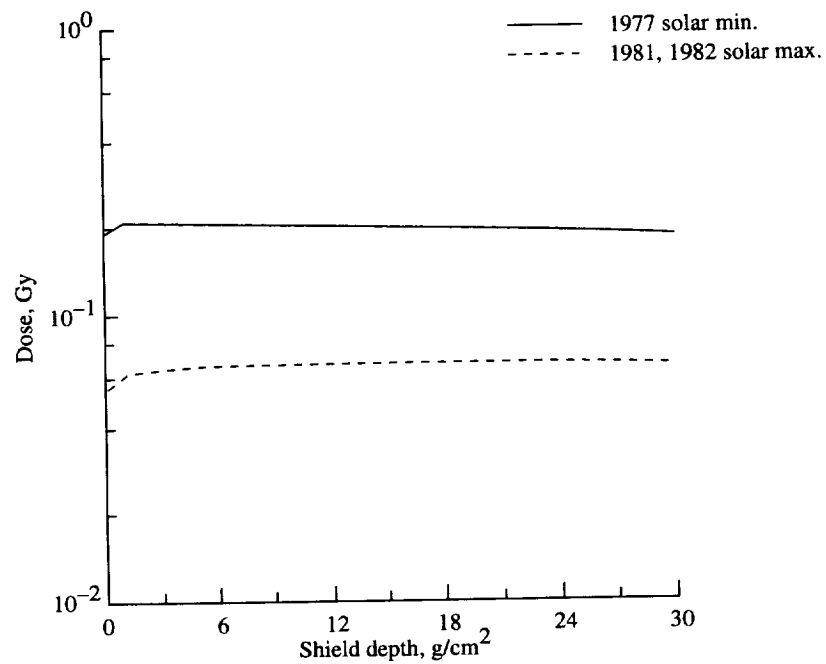


(a) 1977 solar minimum.



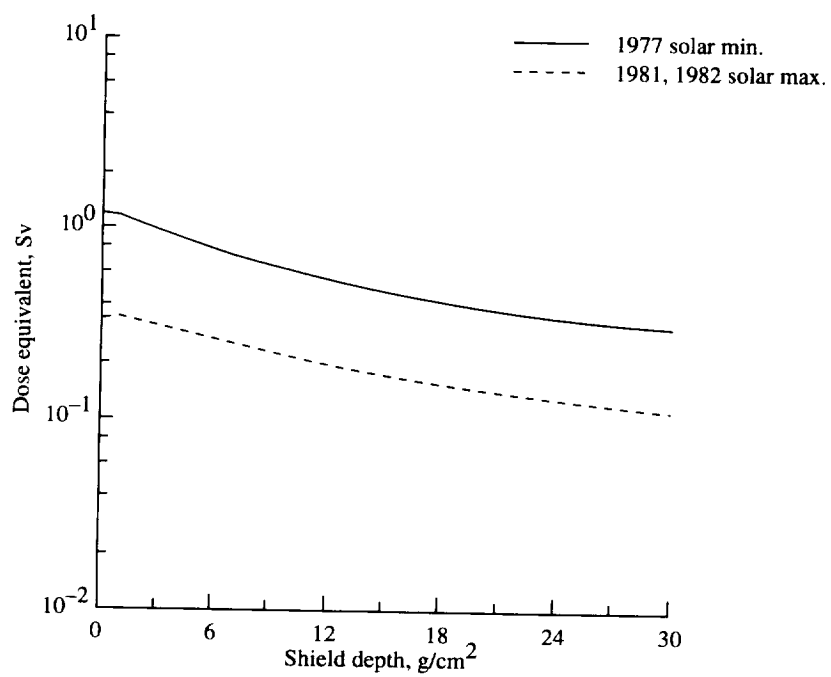
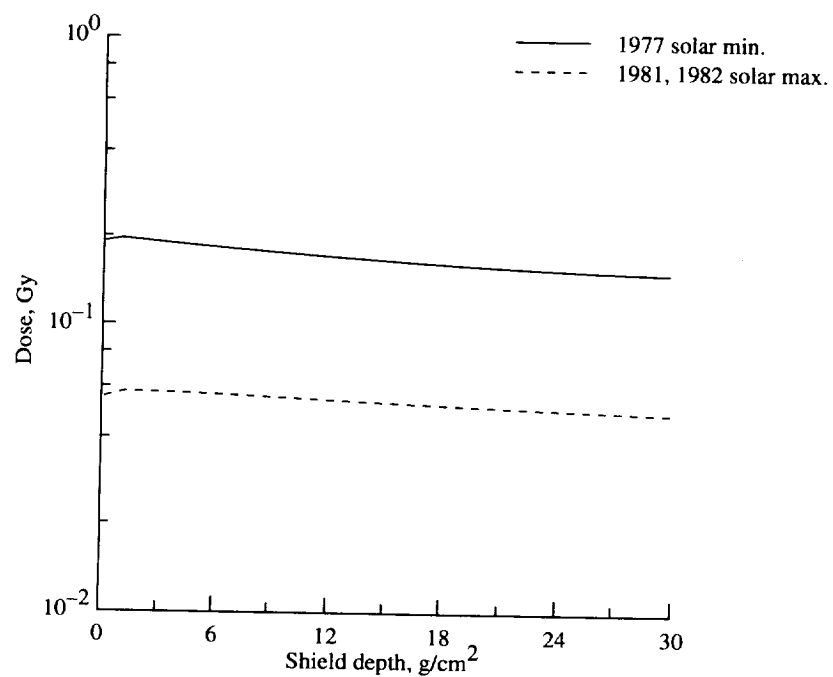
(b) 1981 solar maximum.

Figure 24. GCR energy flux for iron ion in liquid hydrogen.



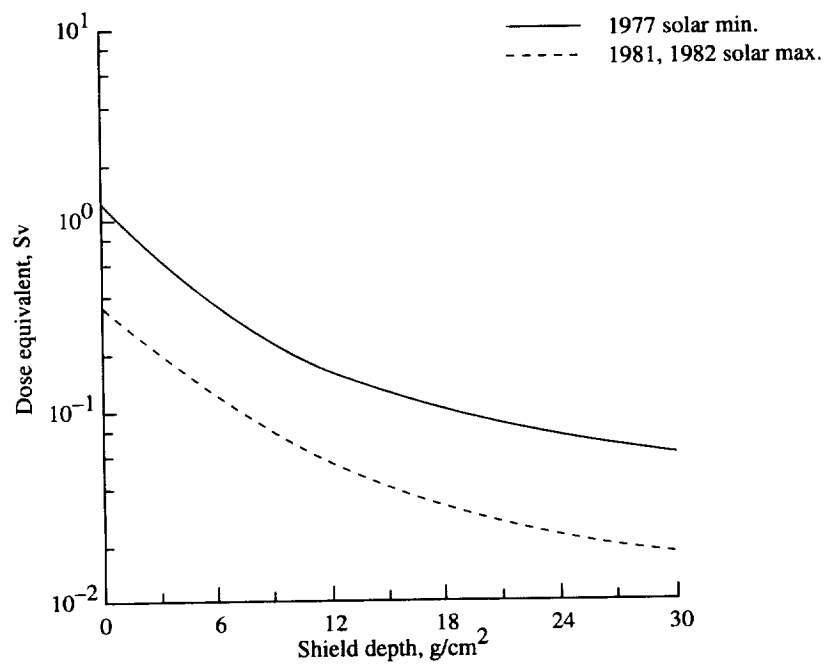
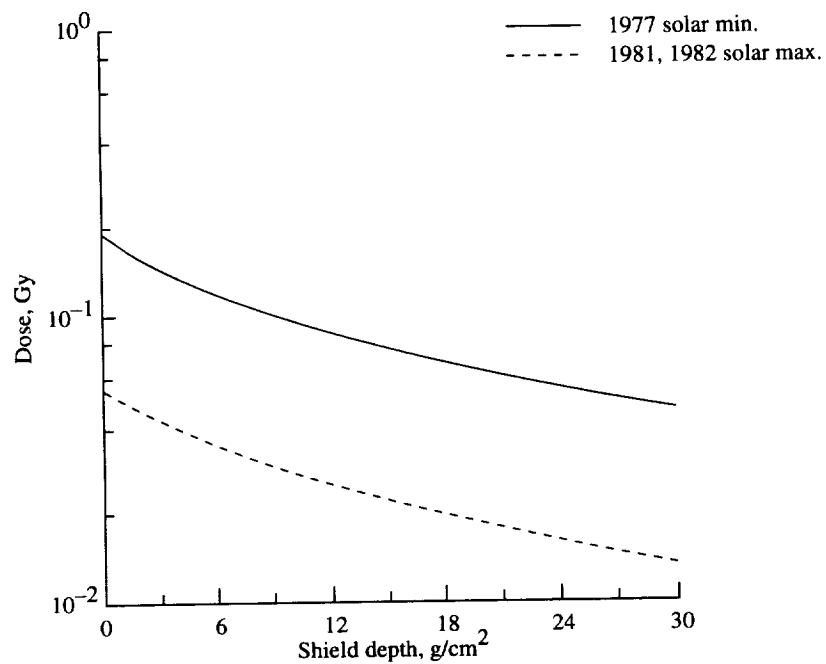
(a) In aluminum.

Figure 25. GCR skin dose and dose equivalent.



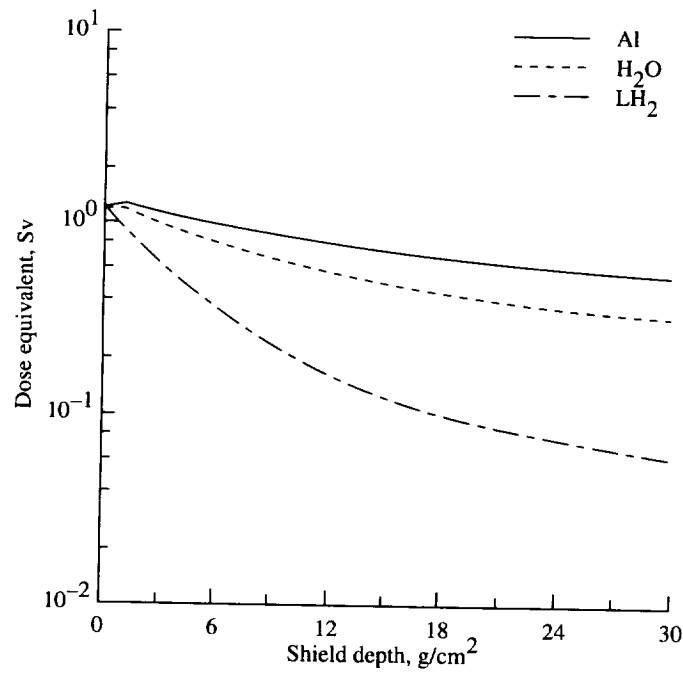
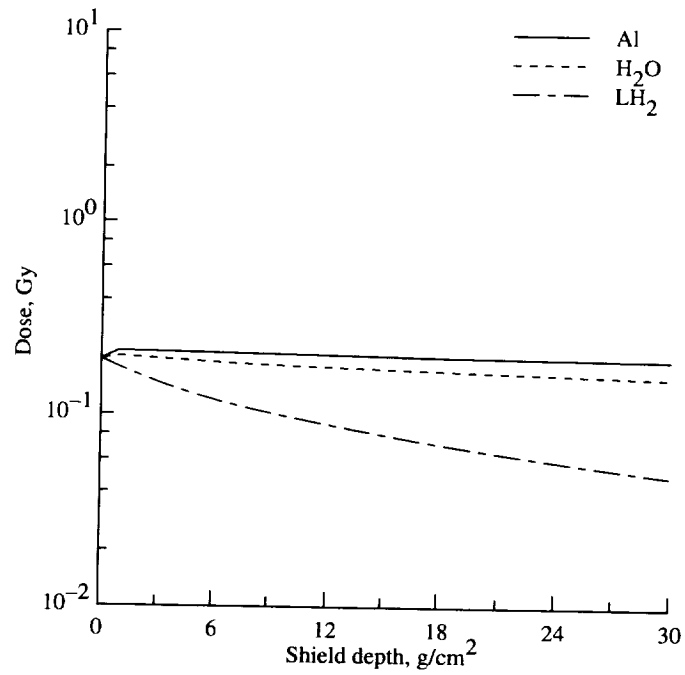
(b) In water.

Figure 25. Continued.



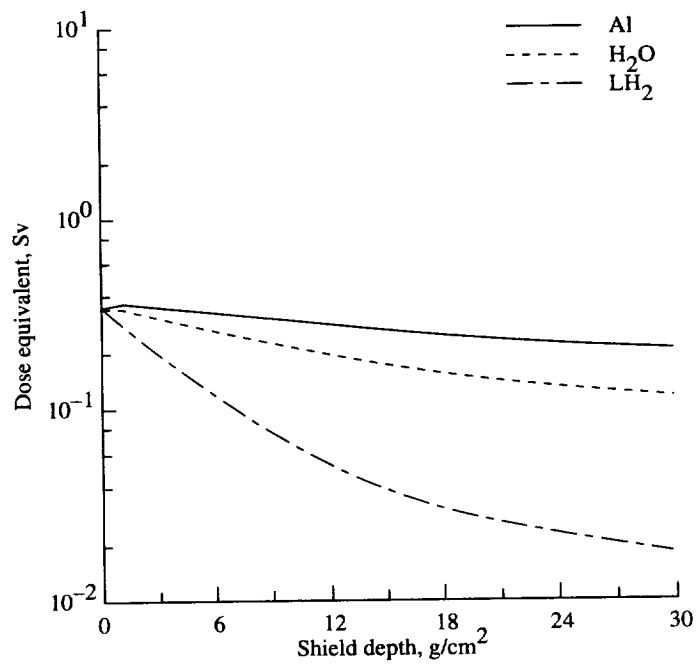
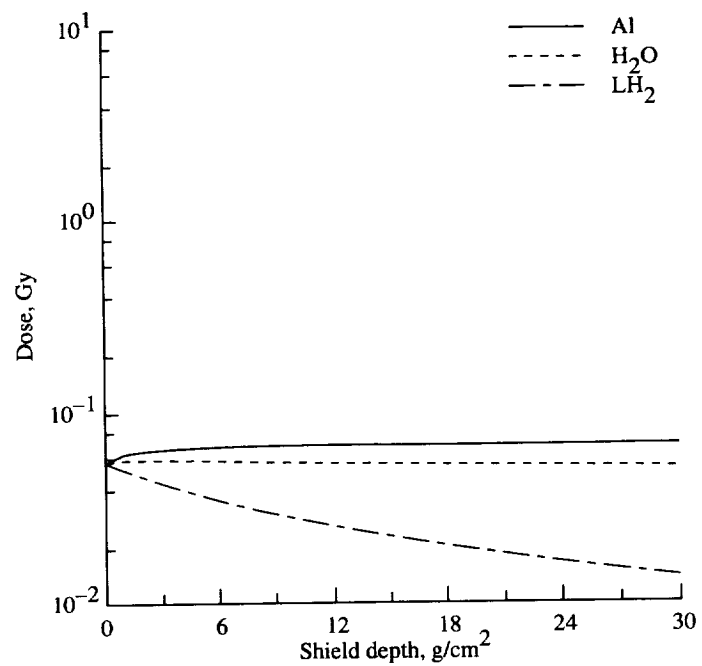
(c) In liquid hydrogen.

Figure 25. Concluded.



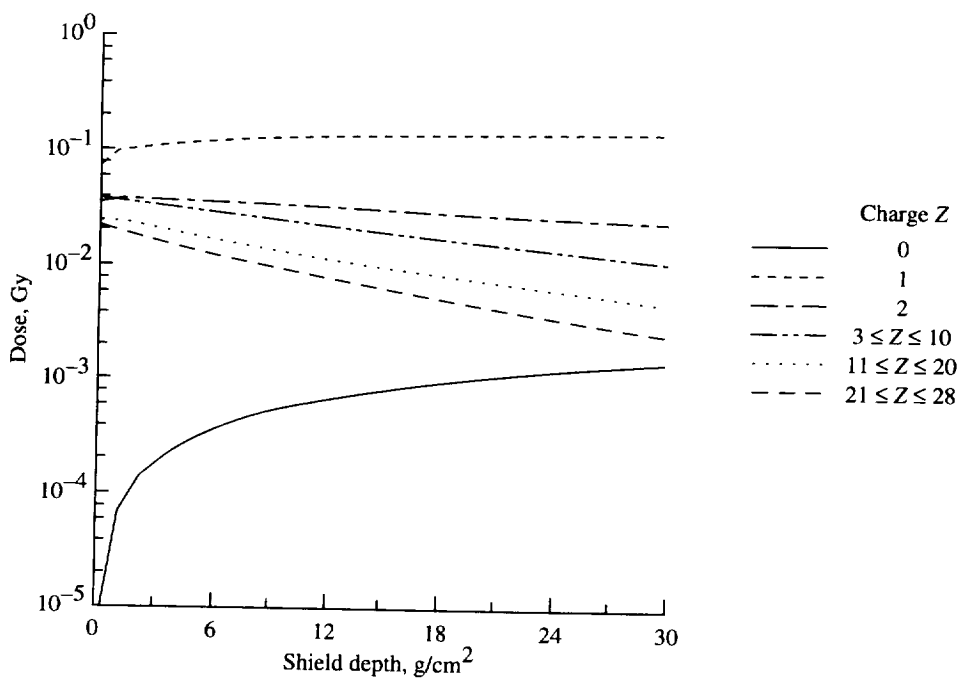
(a) 1977 solar minimum.

Figure 26. GCR skin dose and dose equivalent in aluminum, water, and liquid hydrogen.

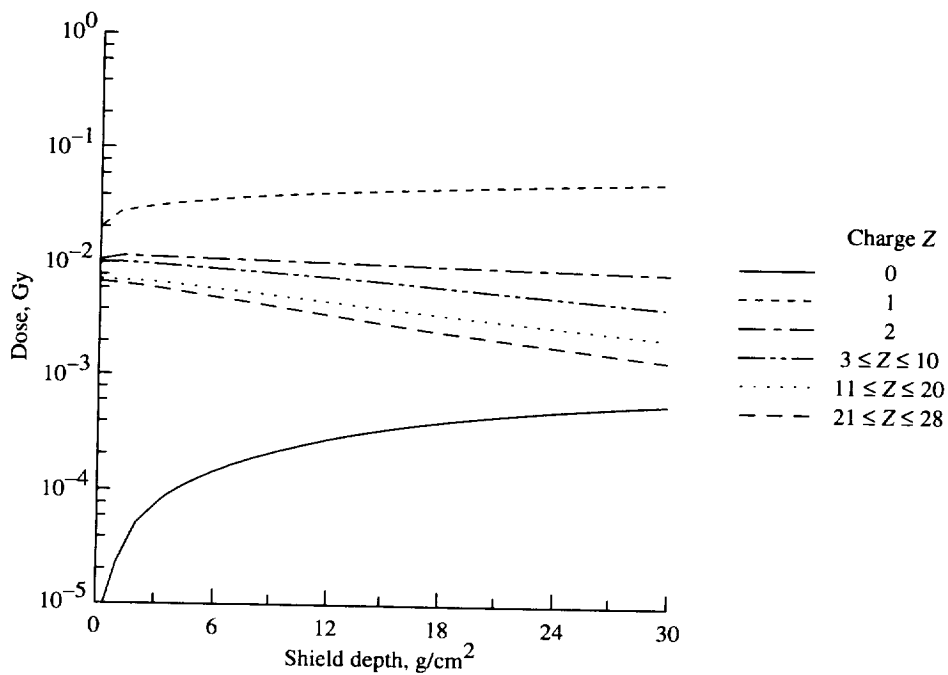


(b) 1981 solar maximum.

Figure 26. Concluded.

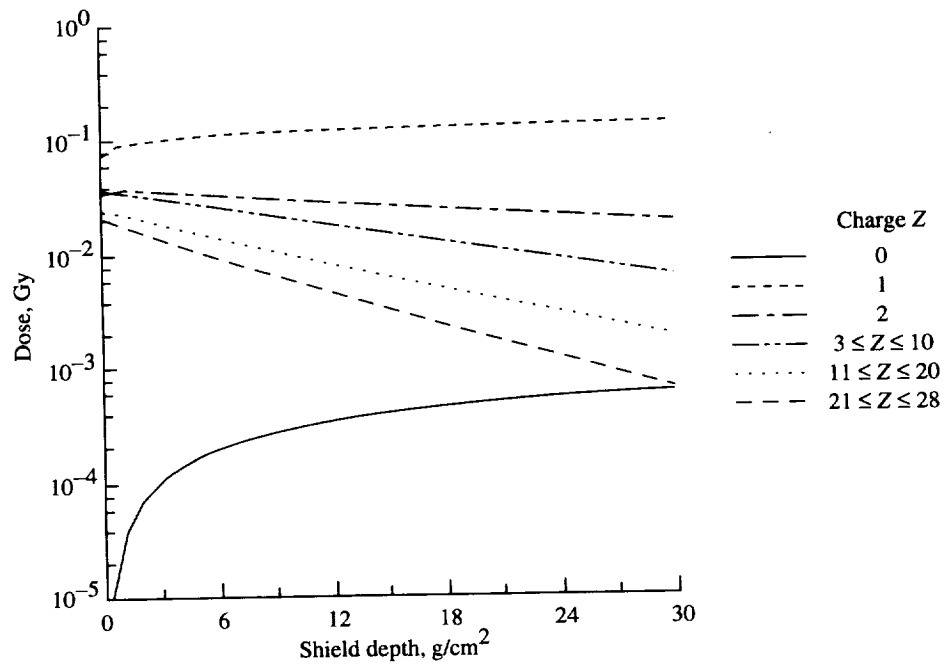


(a) 1977 solar minimum.

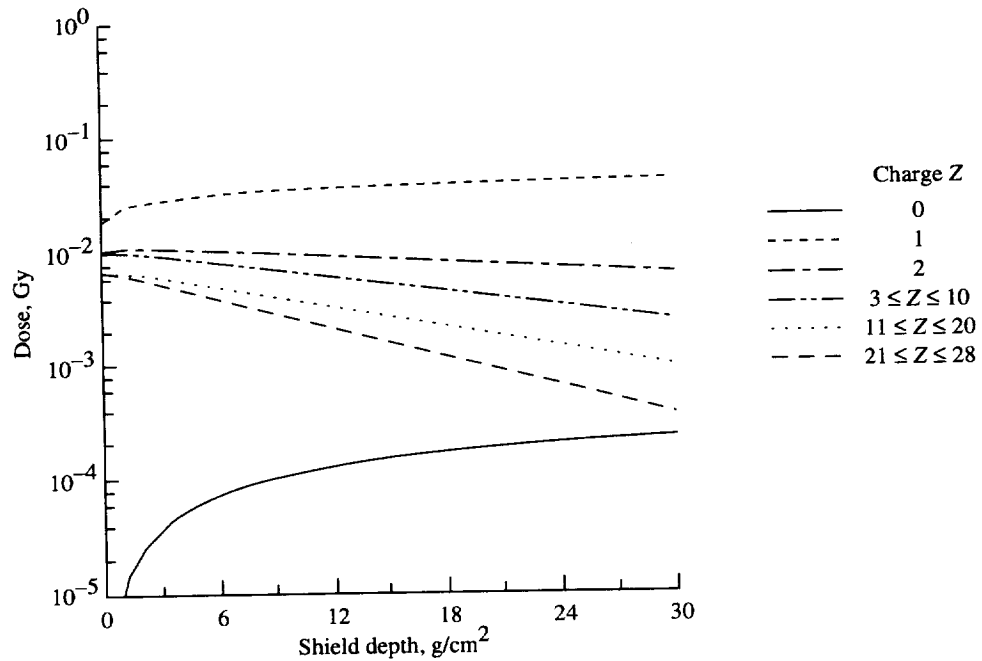


(b) 1981 solar maximum.

Figure 27. GCR skin dose for six charge Z groups in aluminum.

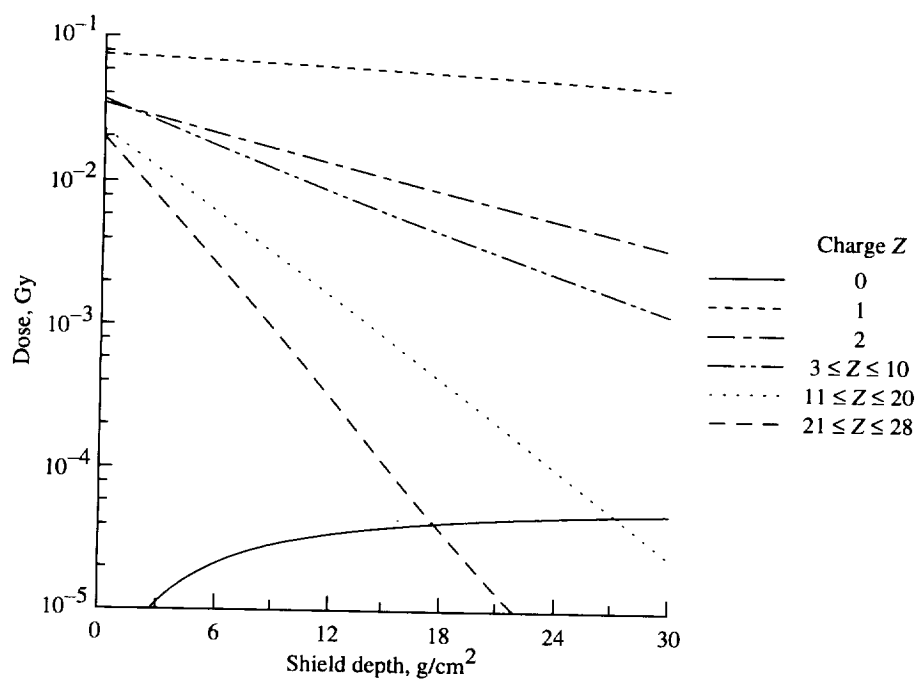


(a) 1977 solar minimum.

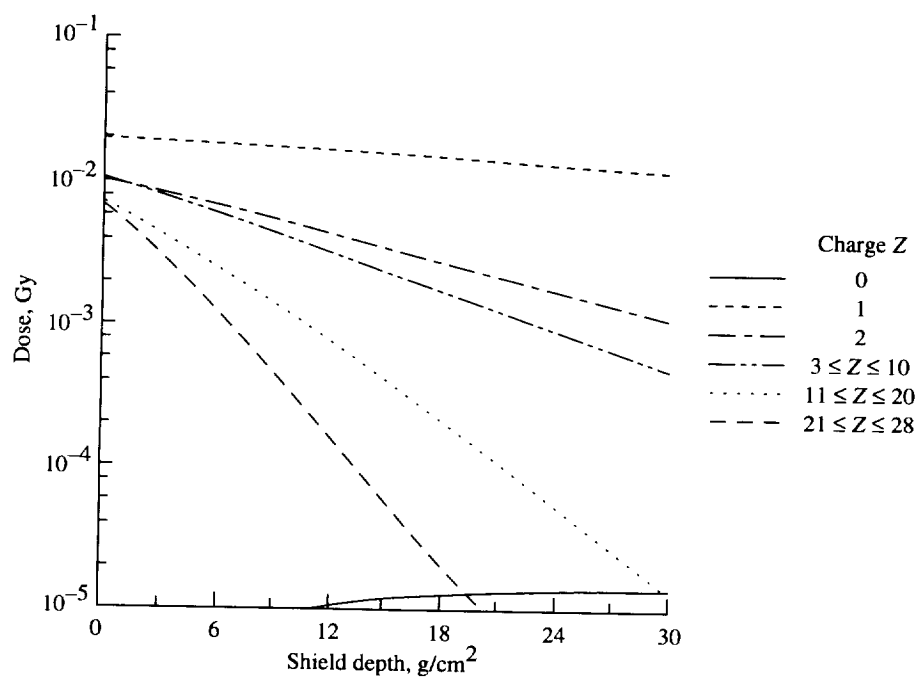


(b) 1981 solar maximum.

Figure 28. GCR skin dose for six charge Z groups in water.

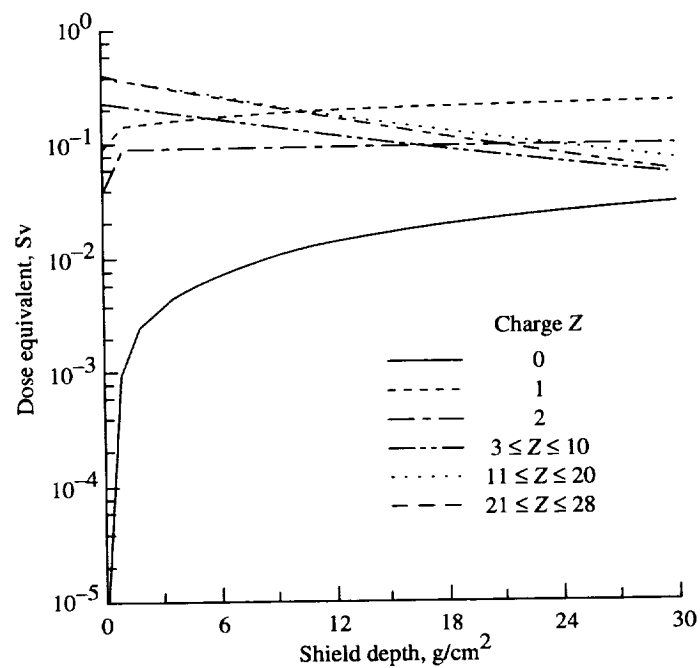


(a) 1977 solar minimum.

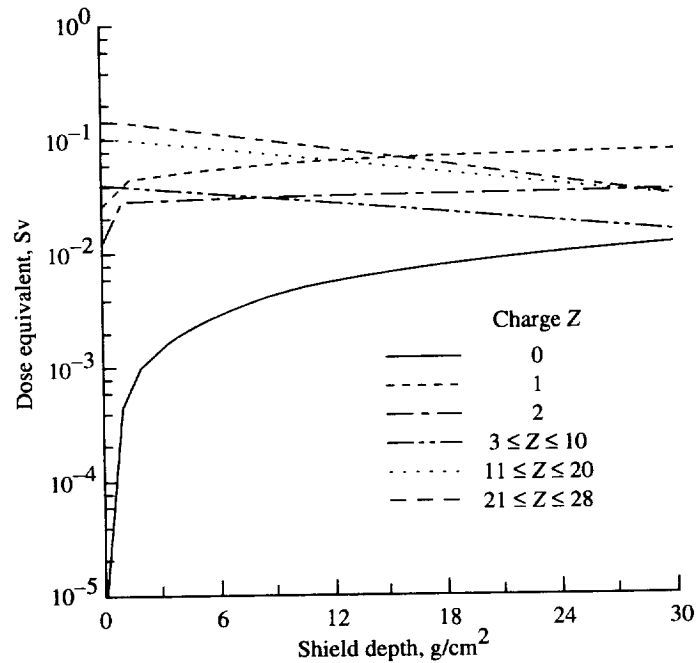


(b) 1981 solar maximum.

Figure 29. GCR skin dose for six charge Z groups in liquid hydrogen.

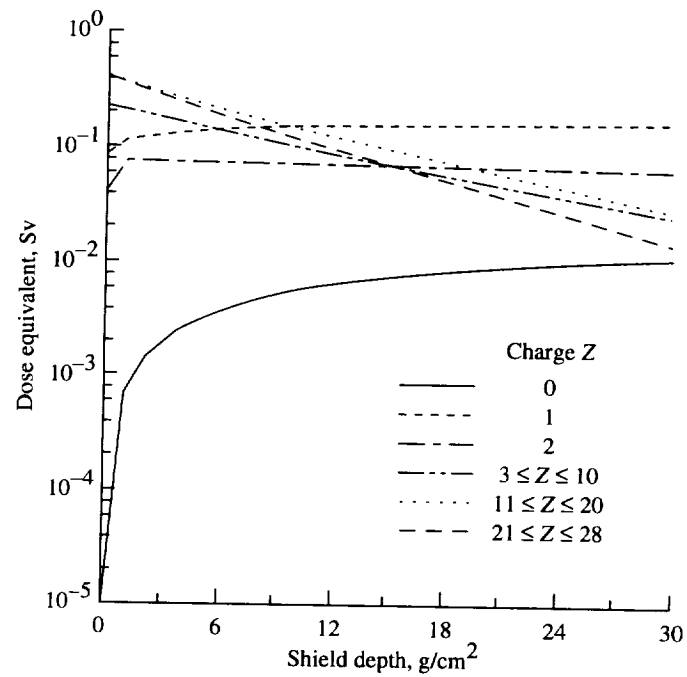


(a) 1977 solar minimum.

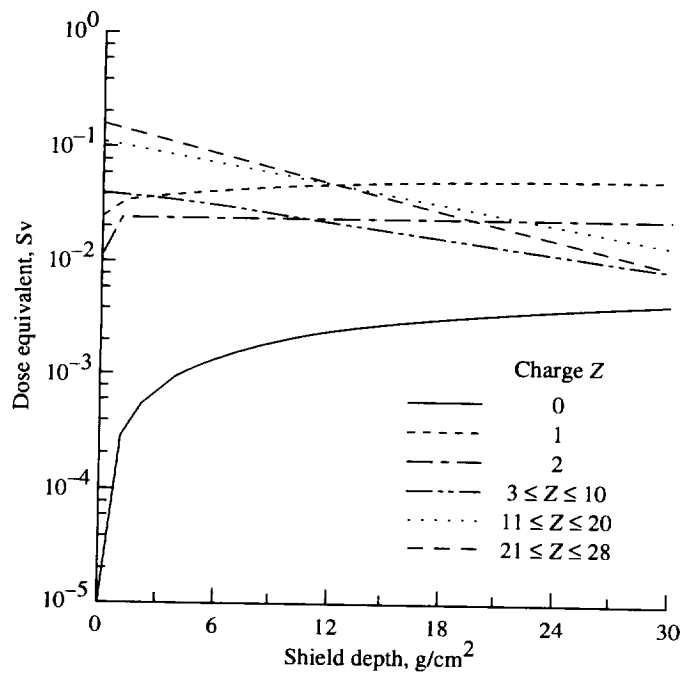


(b) 1981 solar maximum.

Figure 30. GCR skin dose equivalent for six charge Z groups in aluminum.

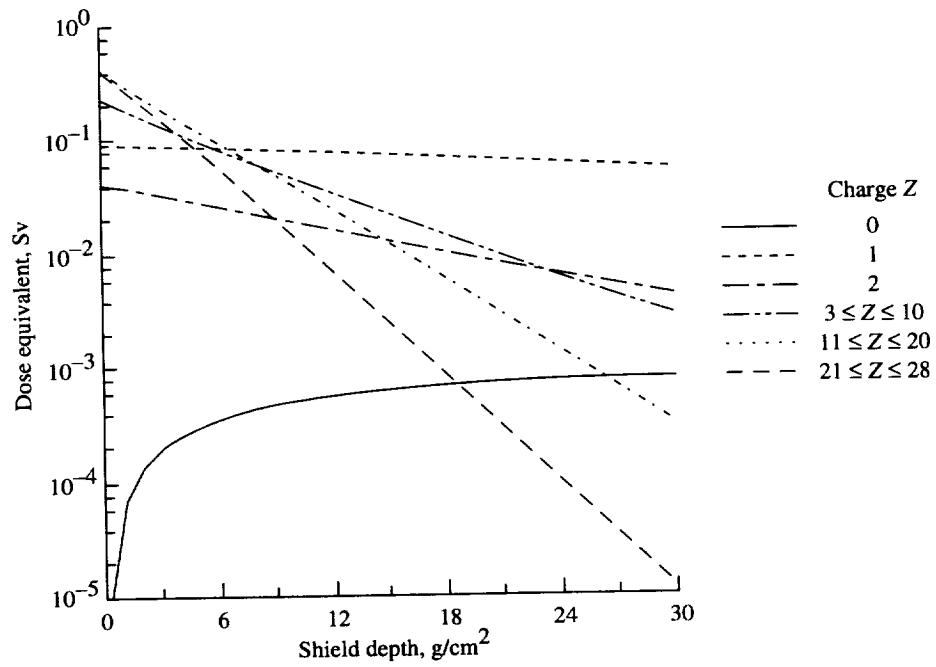


(a) 1977 solar minimum.

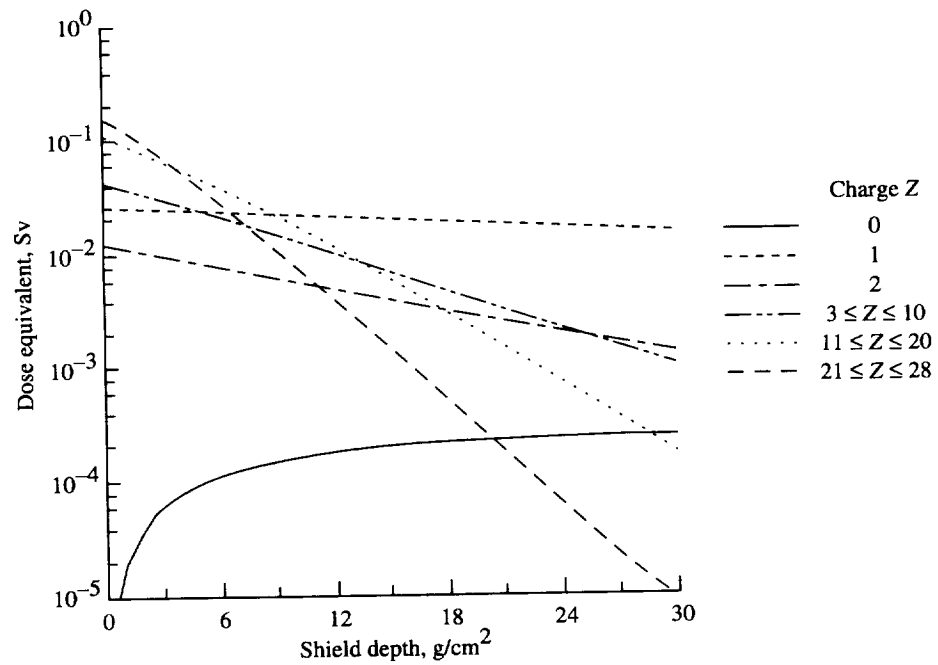


(b) 1981 solar maximum.

Figure 31. GCR skin dose equivalent for six charge Z groups in water.

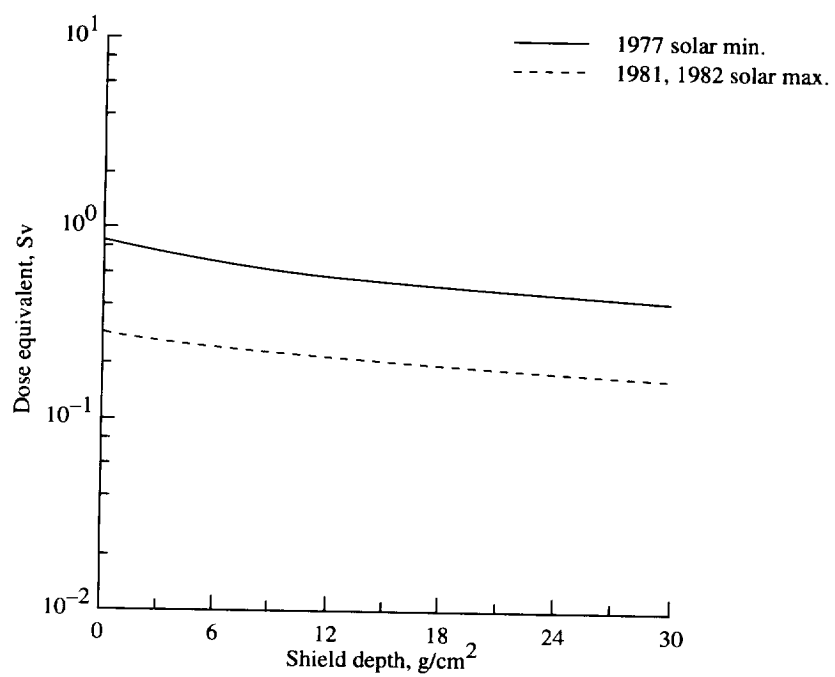
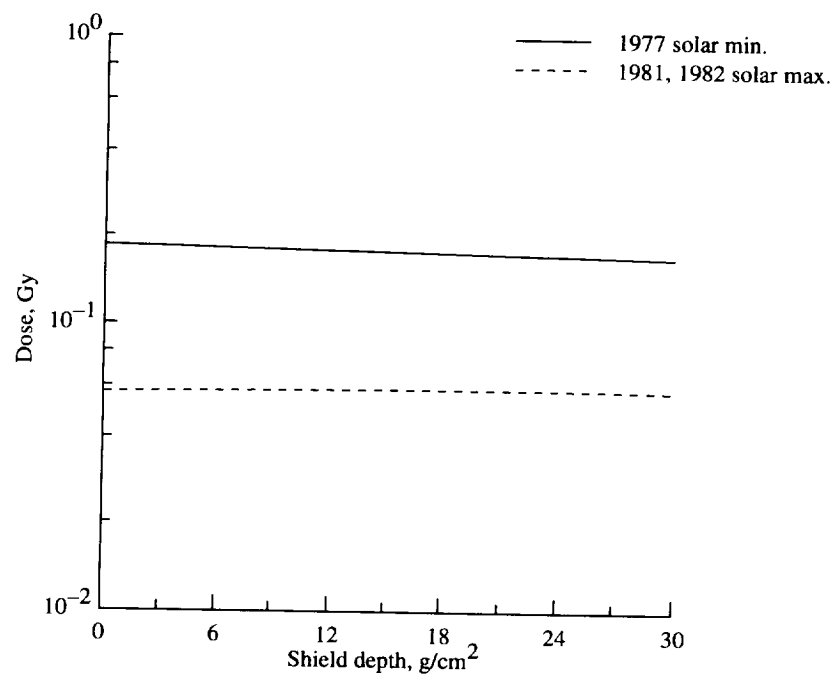


(a) 1977 solar minimum.



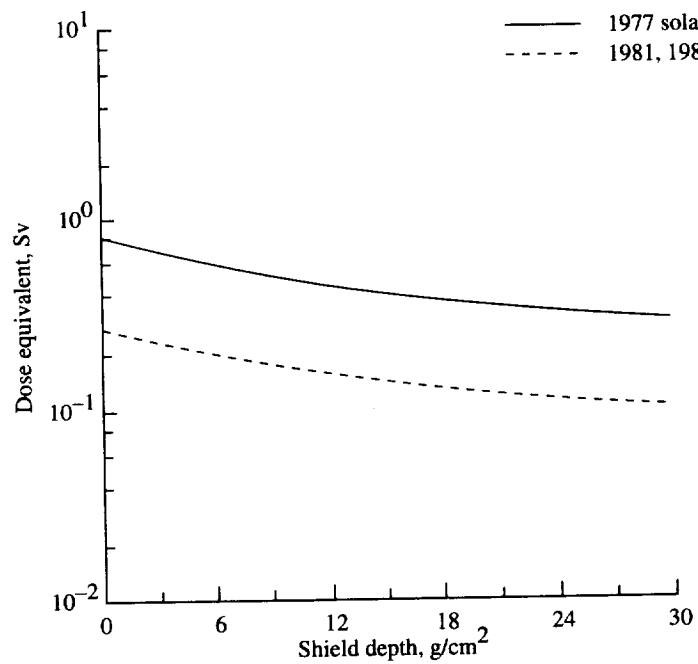
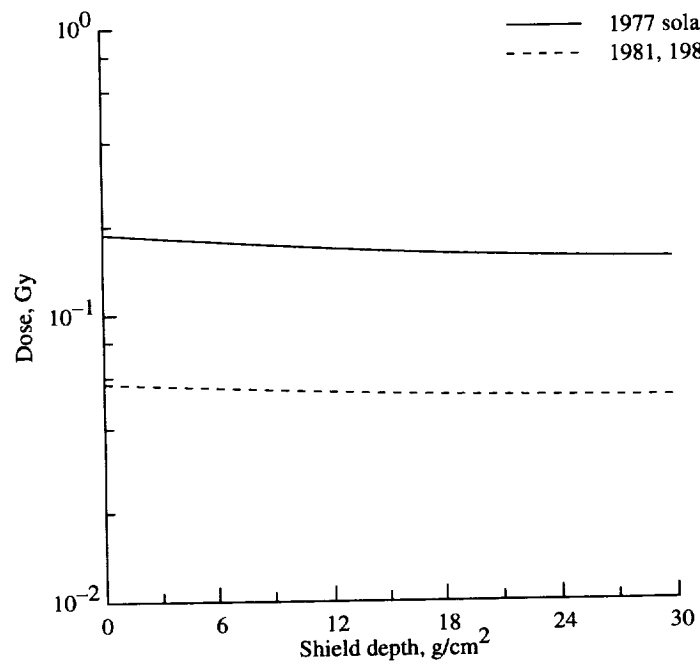
(b) 1981 solar maximum.

Figure 32. GCR skin dose equivalent for six charge Z groups in liquid hydrogen.



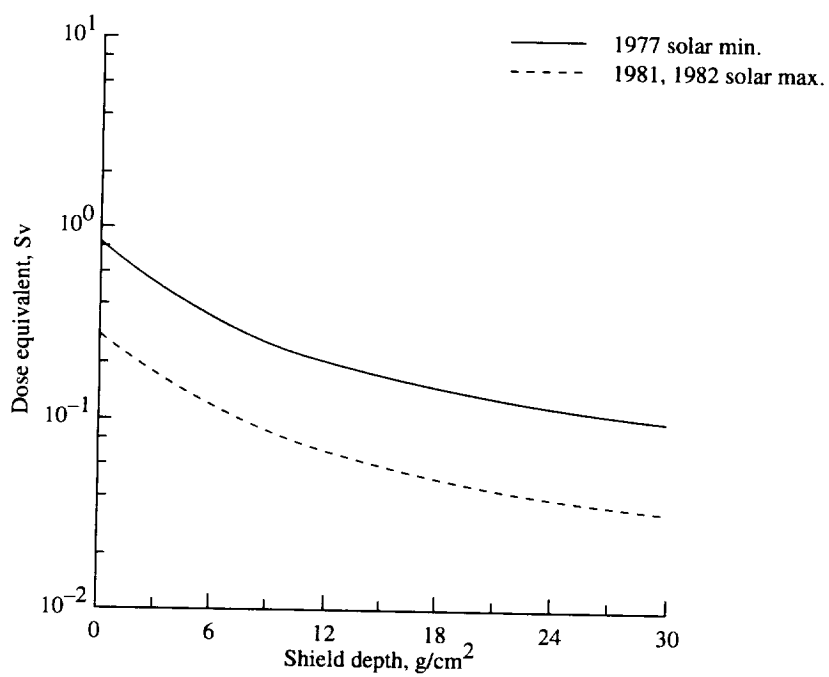
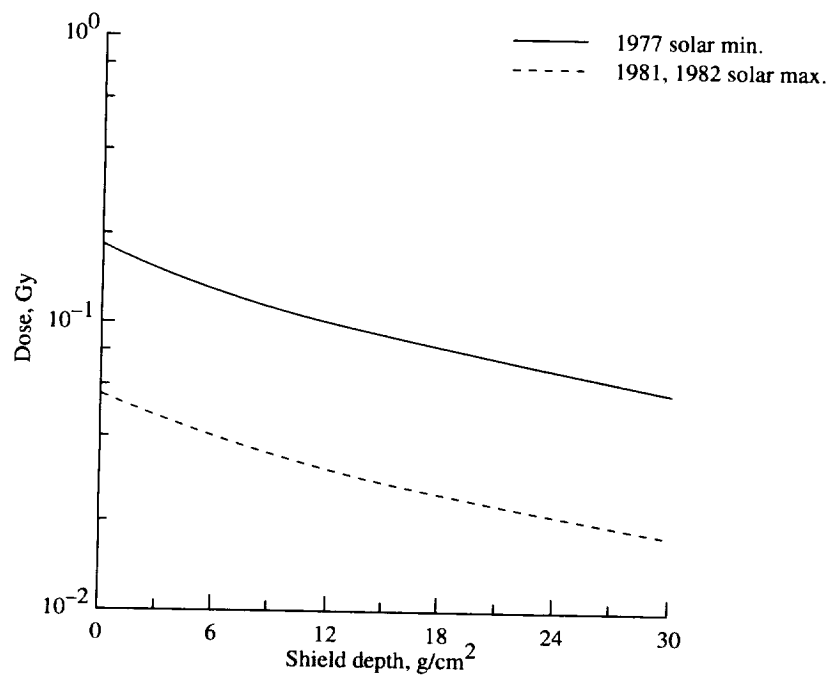
(a) In aluminum.

Figure 33. GCR 5-cm-BFO dose and dose equivalent.



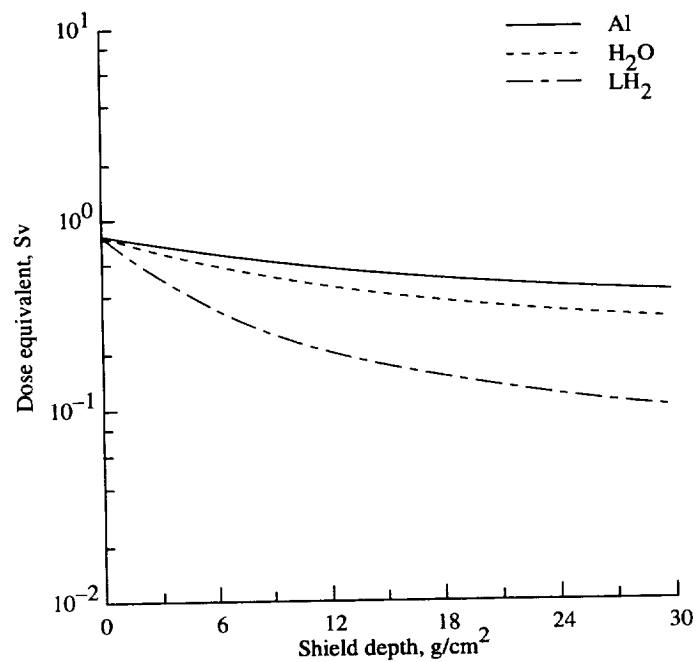
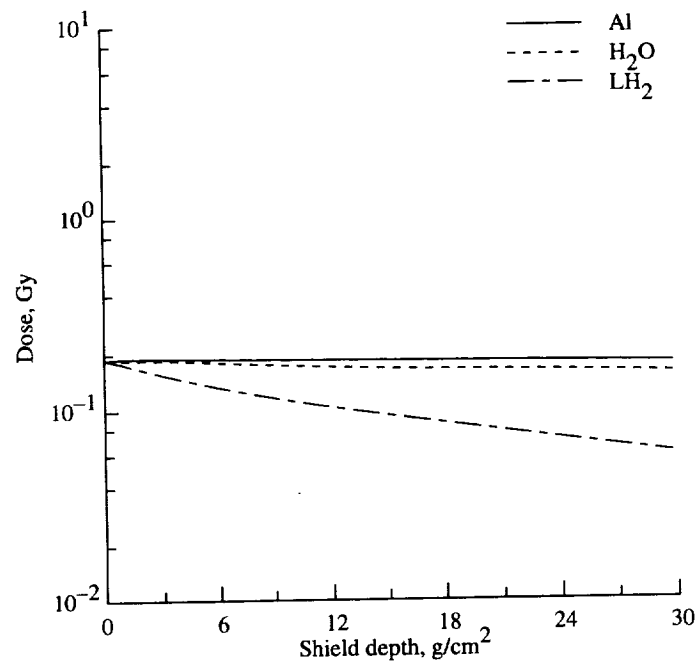
(b) In water.

Figure 33. Continued.



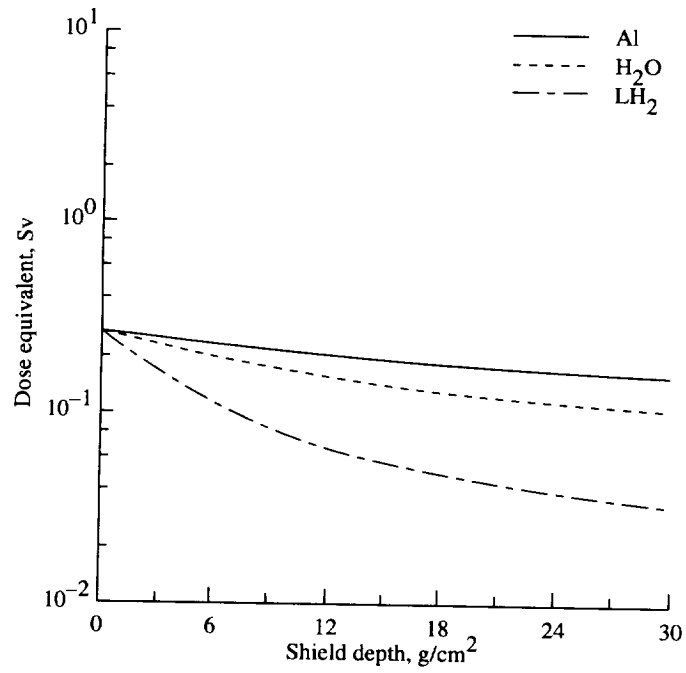
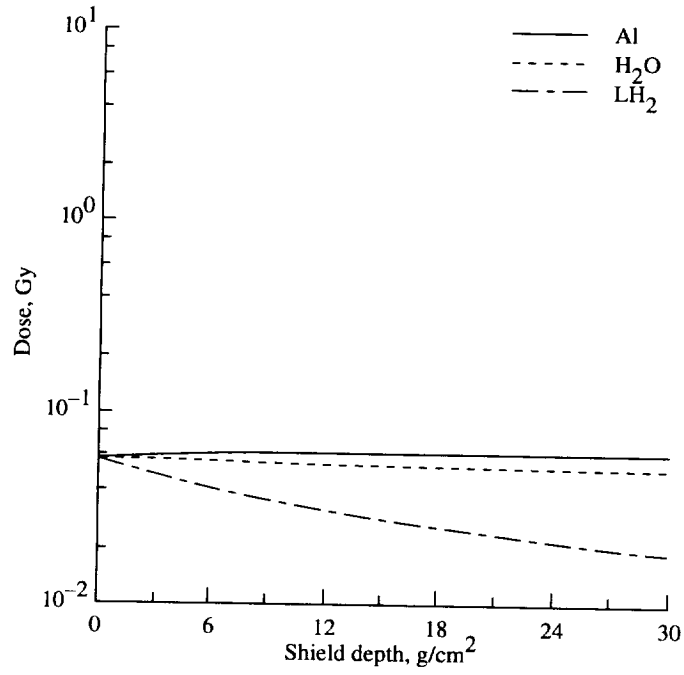
(c) In liquid hydrogen.

Figure 33. Concluded.



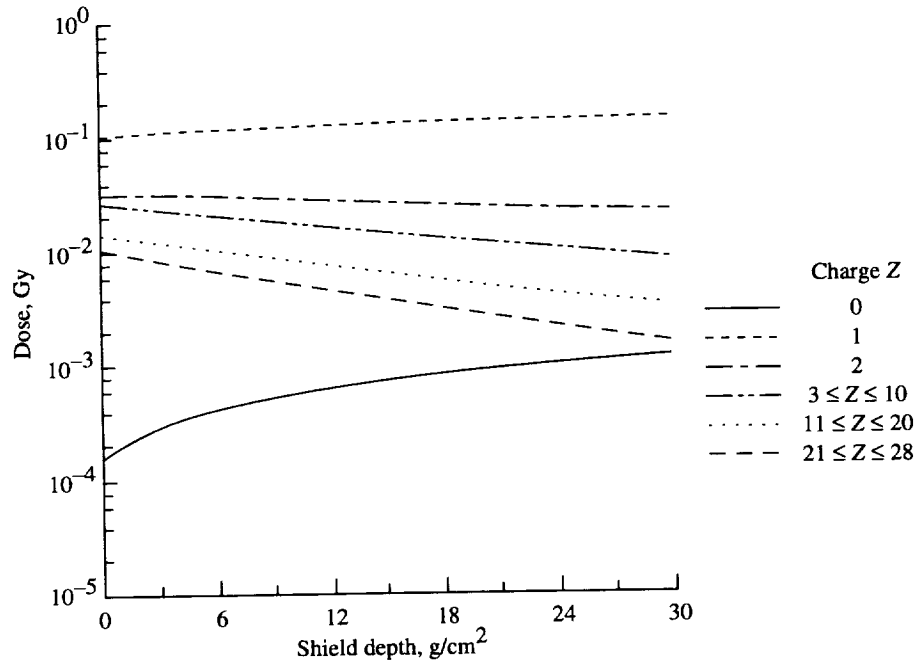
(a) 1977 solar minimum.

Figure 34. GCR 5-cm-BFO dose and dose equivalent in aluminum, water, and liquid hydrogen.

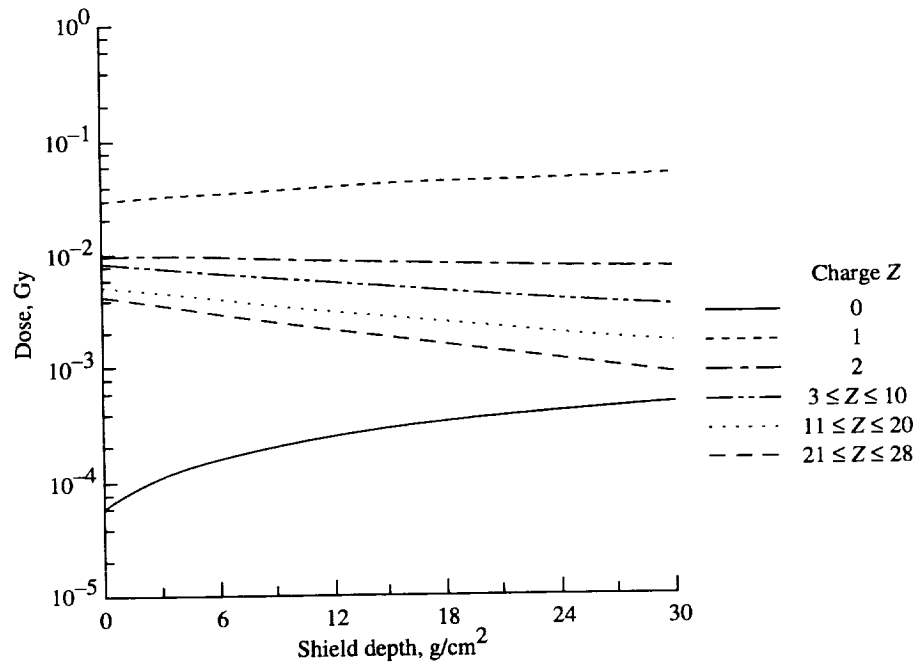


(b) 1981 solar maximum.

Figure 34. Concluded.

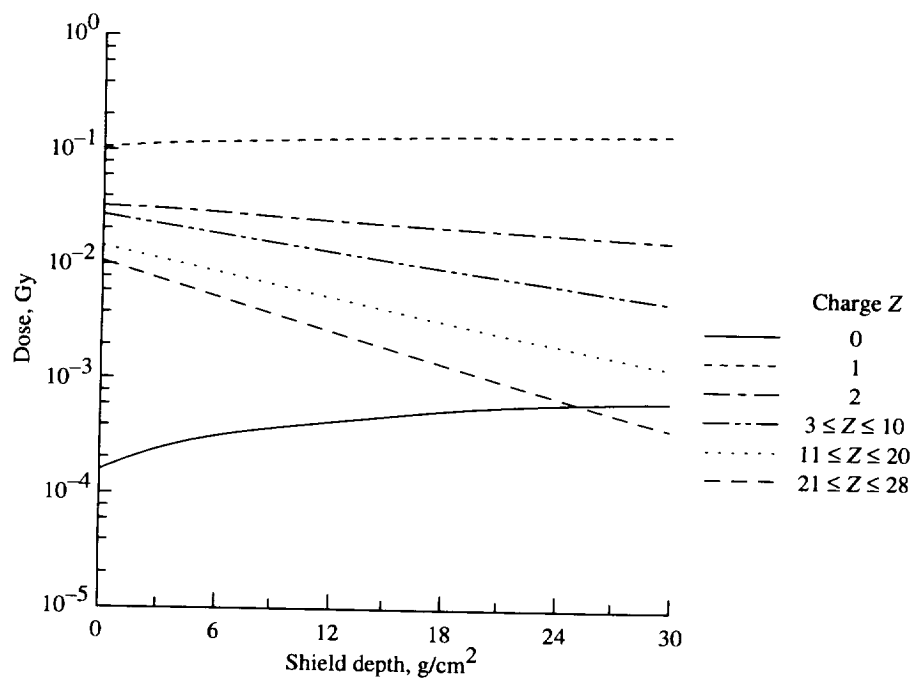


(a) 1977 solar minimum.

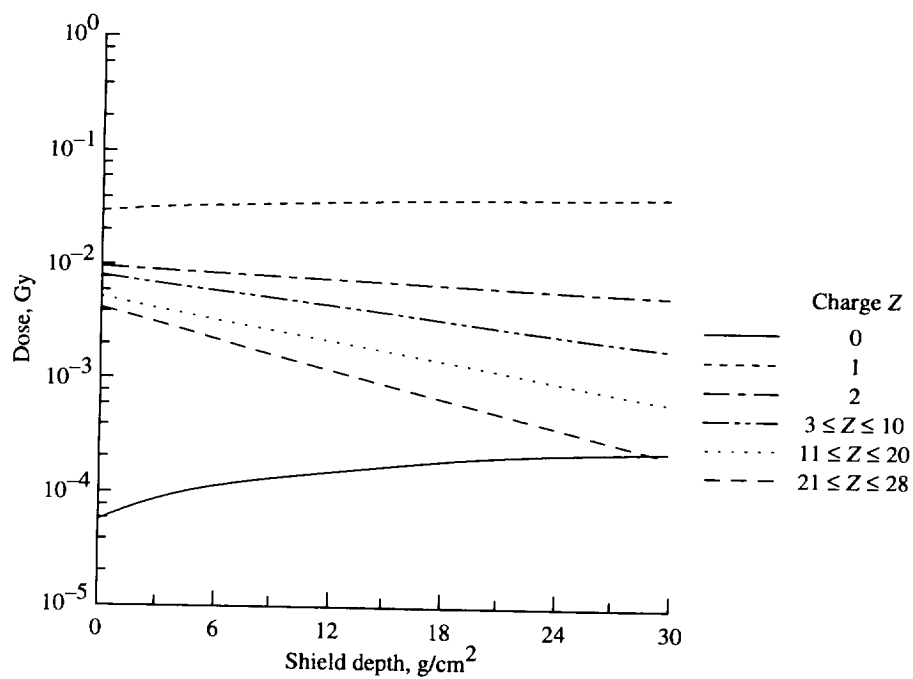


(b) 1981 solar maximum.

Figure 35. GCR 5-cm-BFO dose for six charge Z groups in aluminum.

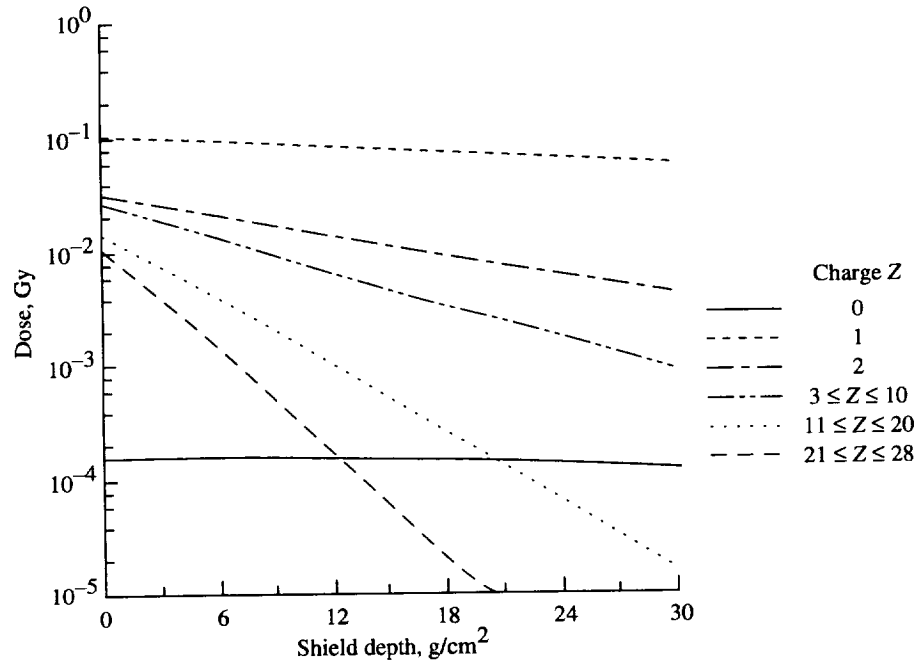


(a) 1977 solar minimum.

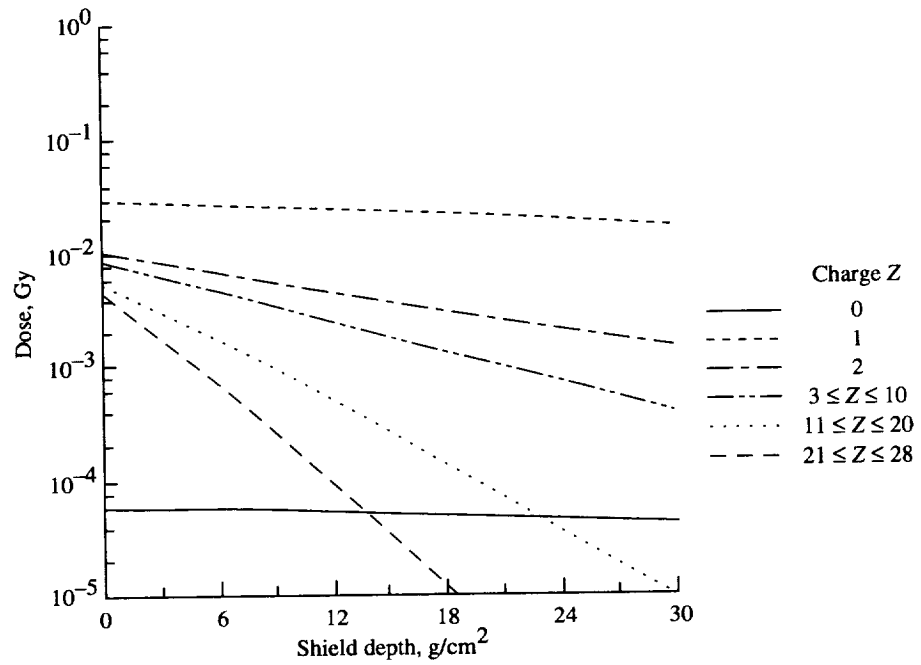


(b) 1981 solar maximum.

Figure 36. GCR 5-cm-BFO dose for six charge Z groups in water.

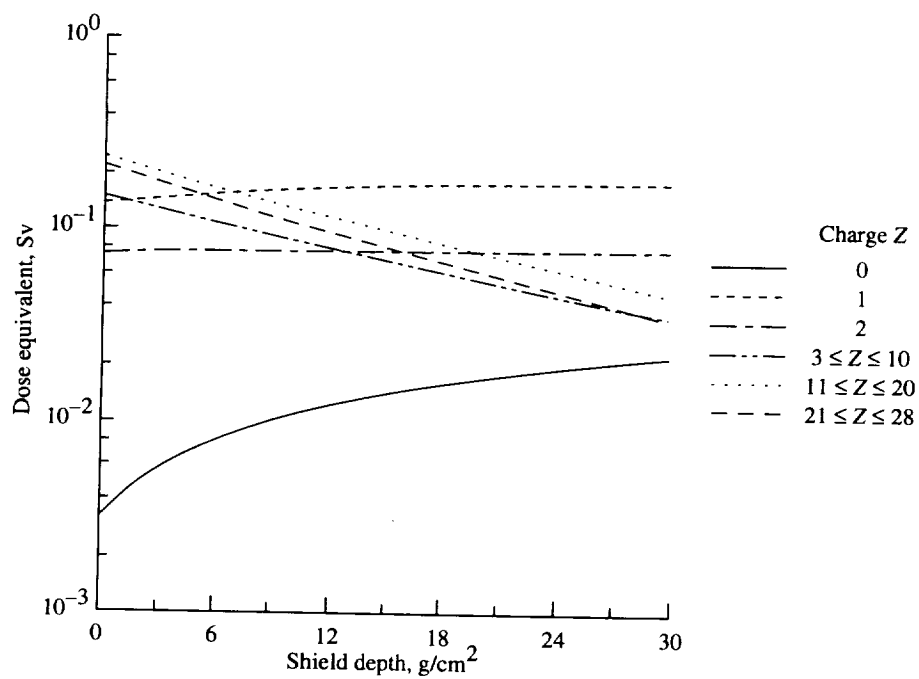


(a) 1977 solar minimum.

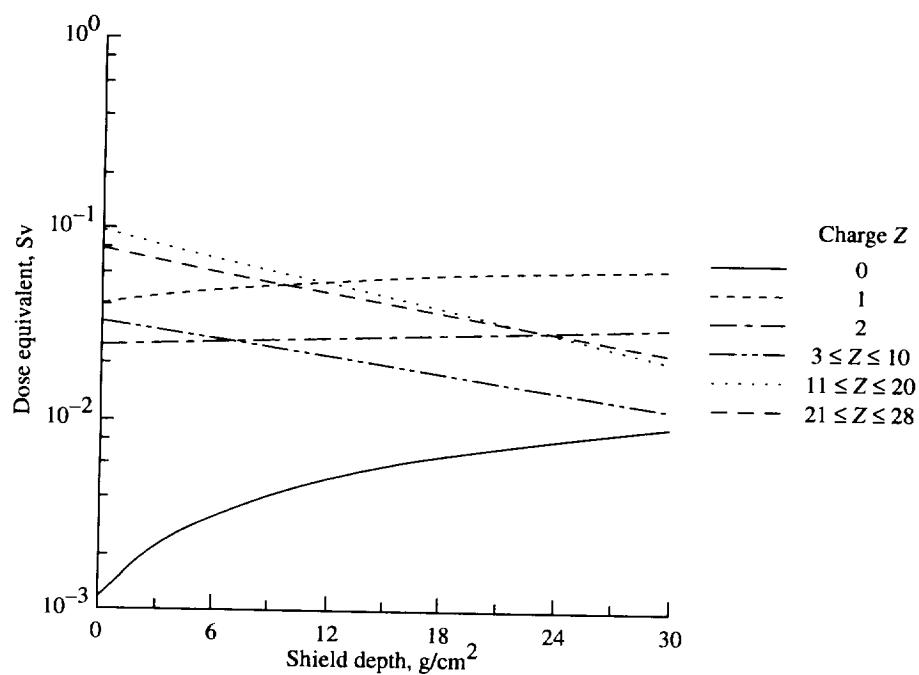


(b) 1981 solar maximum.

Figure 37. GCR 5-cm-BFO dose for six charge Z groups in liquid hydrogen.

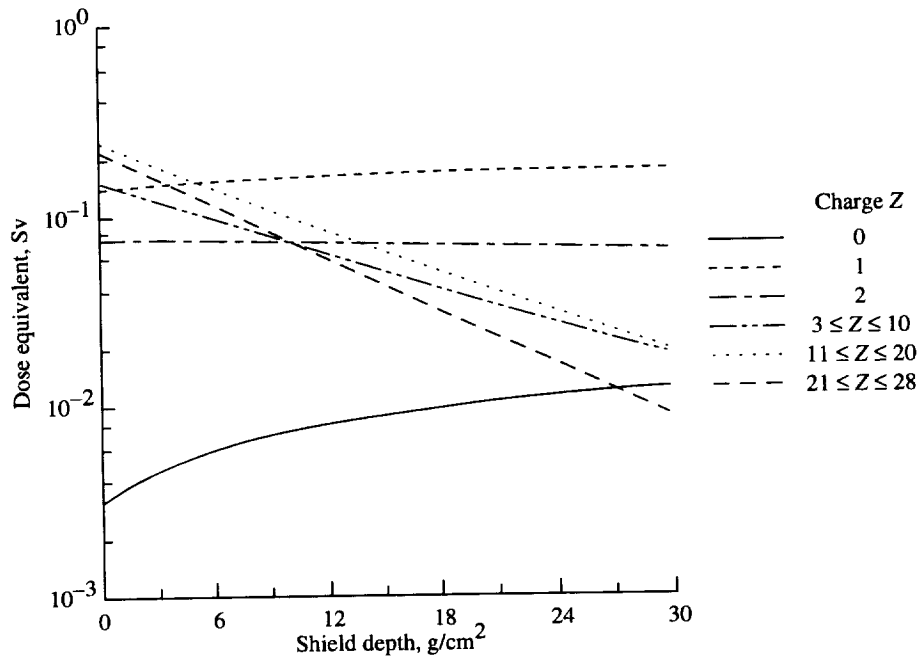


(a) 1977 solar minimum.

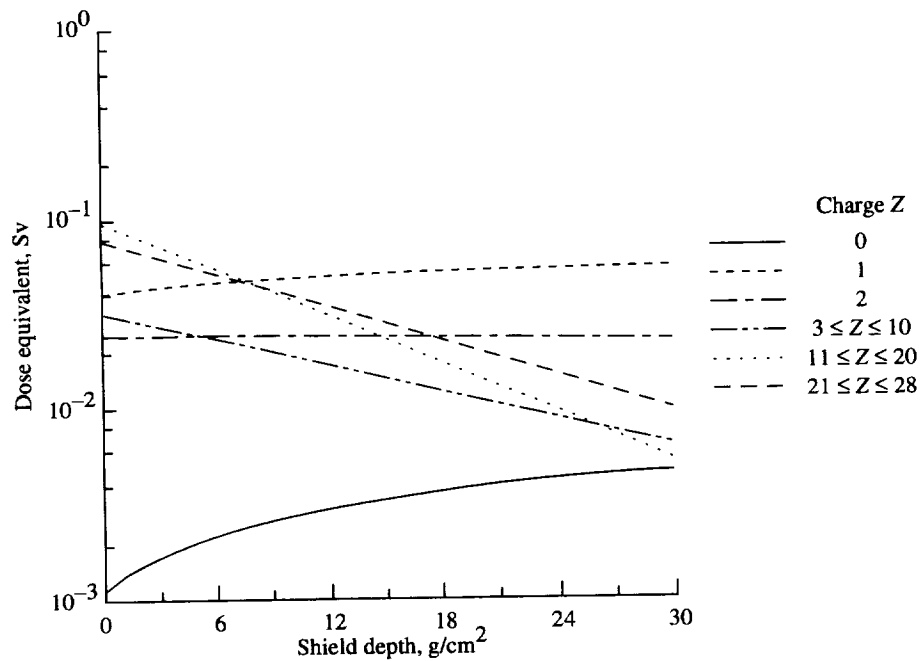


(b) 1981 solar maximum.

Figure 38. GCR 5-cm-BFO dose equivalent for six charge Z groups in aluminum.

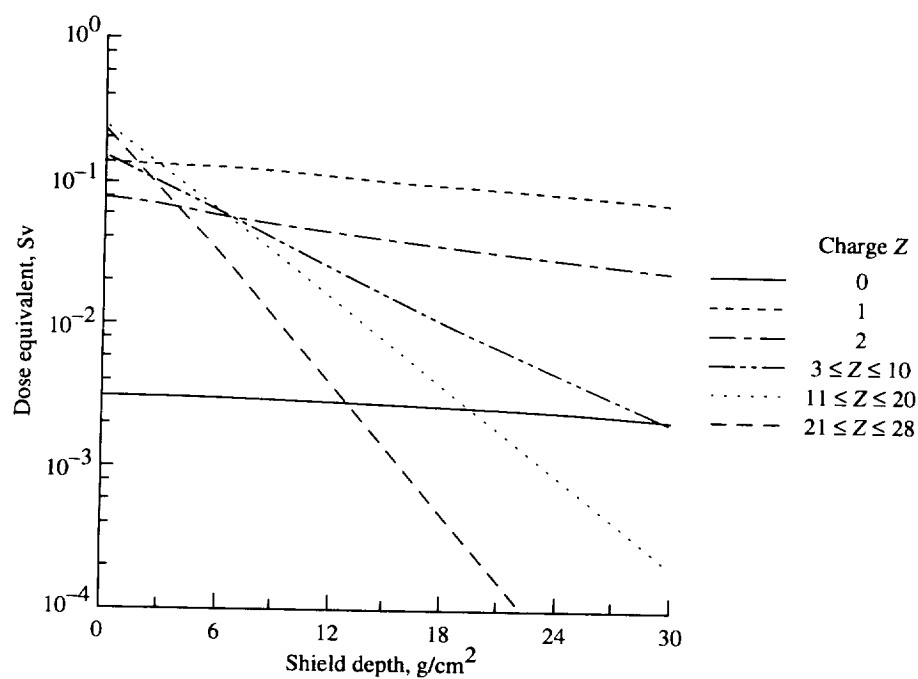


(a) 1977 solar minimum.

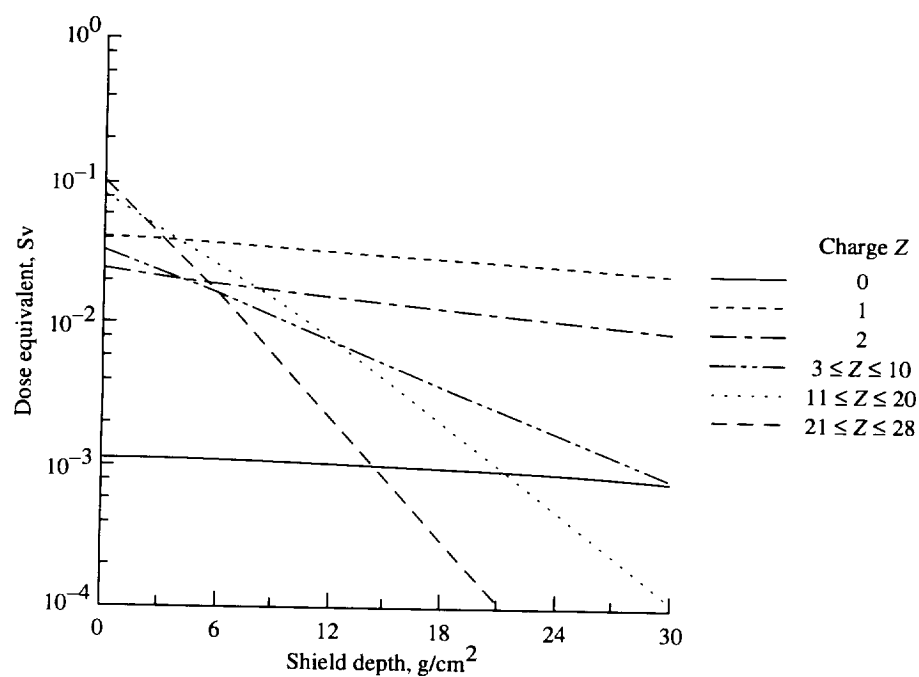


(b) 1981 solar maximum.

Figure 39. GCR 5-cm-BFO dose equivalent for six charge Z groups in water.

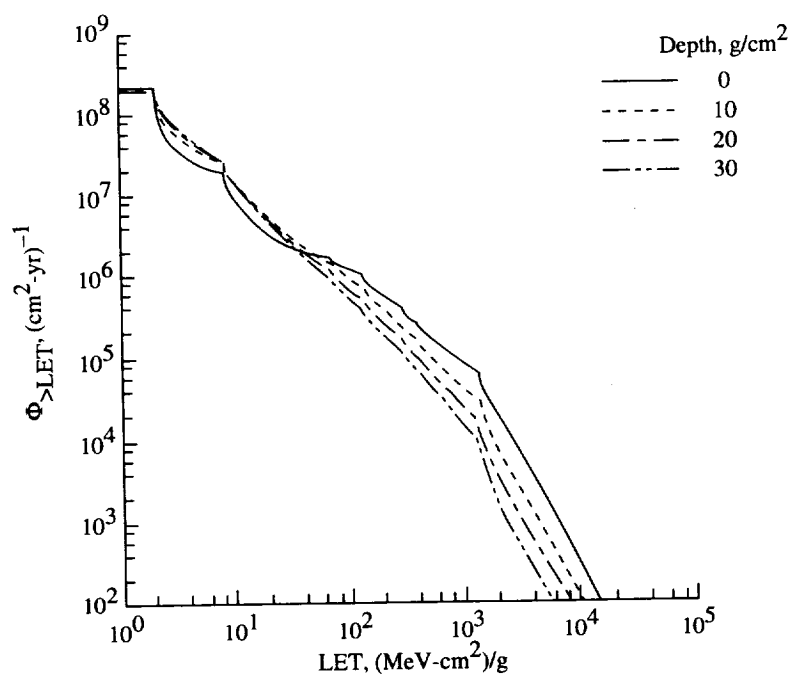


(a) 1977 solar minimum.

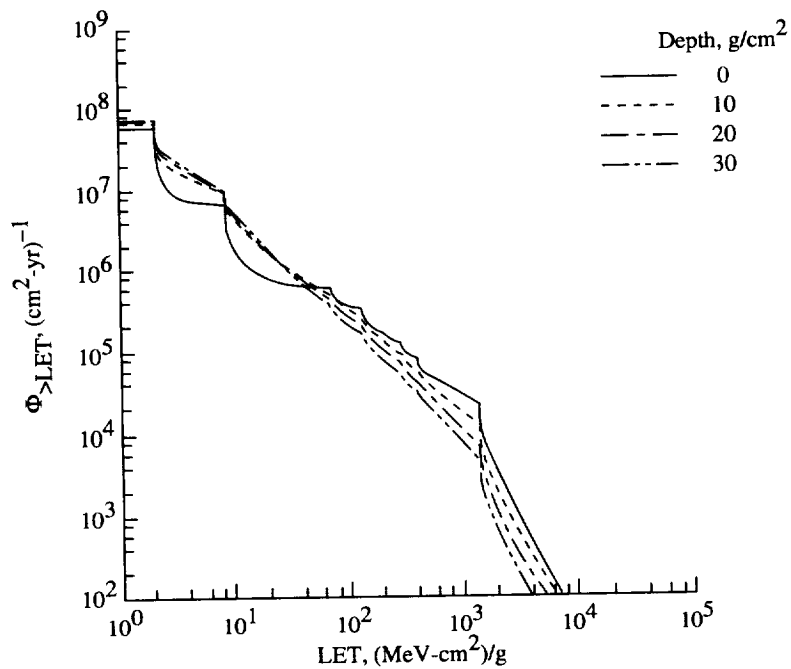


(b) 1981 solar maximum.

Figure 40. GCR 5-cm-BFO dose equivalent for six charge Z groups in liquid hydrogen.

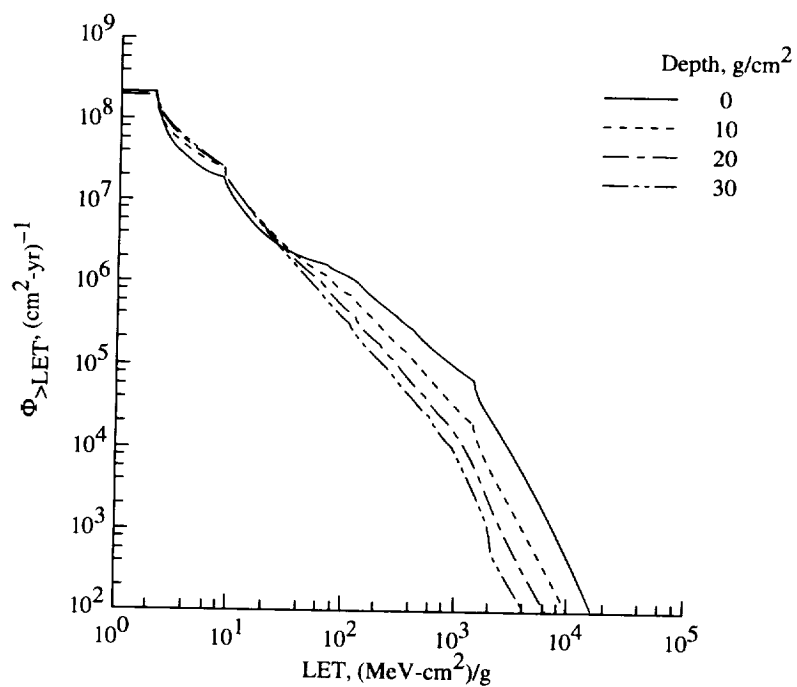


(a) 1977 solar minimum.

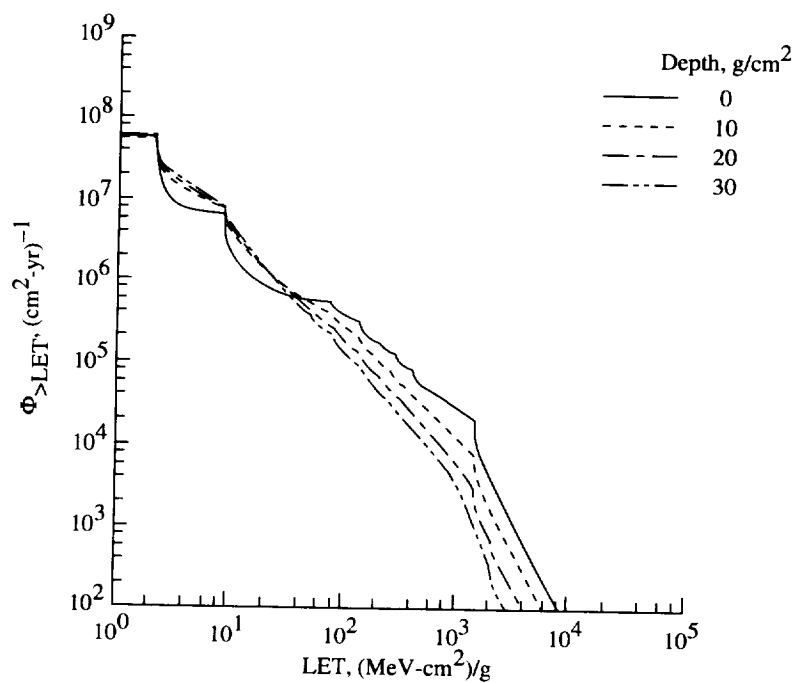


(b) 1981 solar maximum.

Figure 41. GCR skin integral flux LET spectra in aluminum.

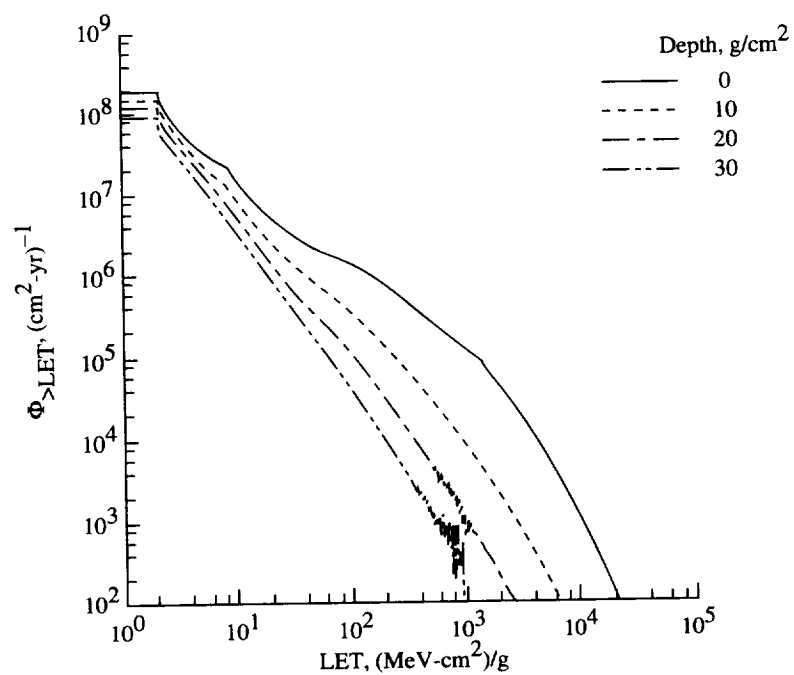


(a) 1977 solar minimum.

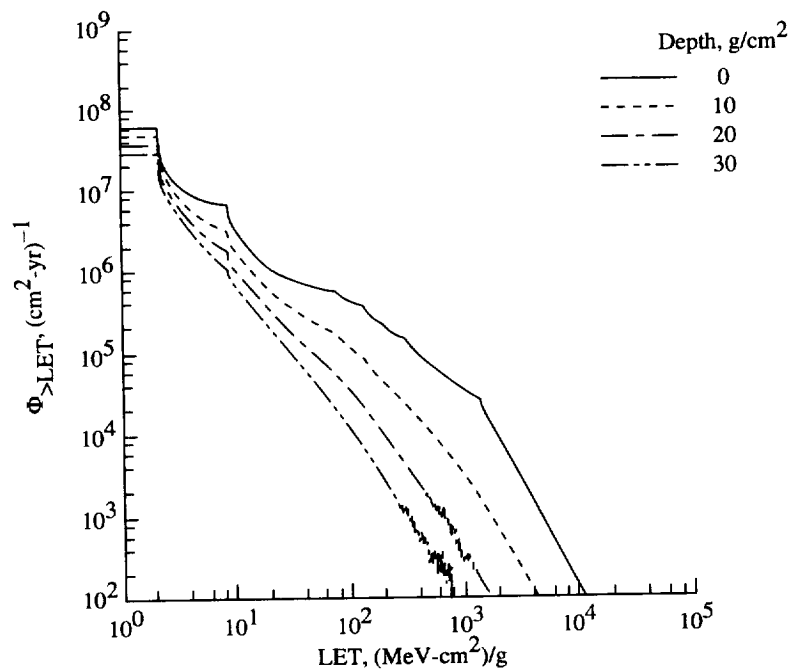


(b) 1981 solar maximum.

Figure 42. GCR skin integral flux LET spectra in water.

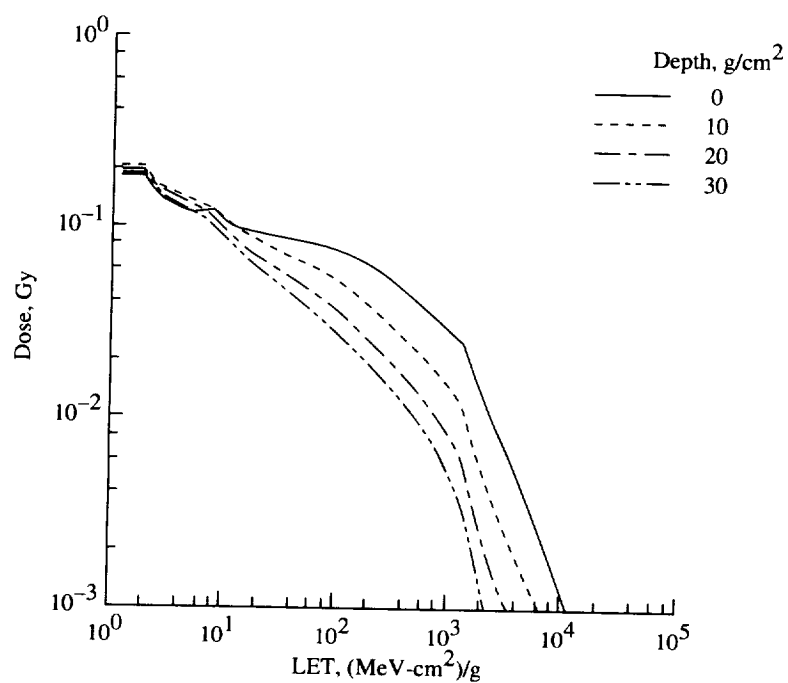


(a) 1977 solar minimum.

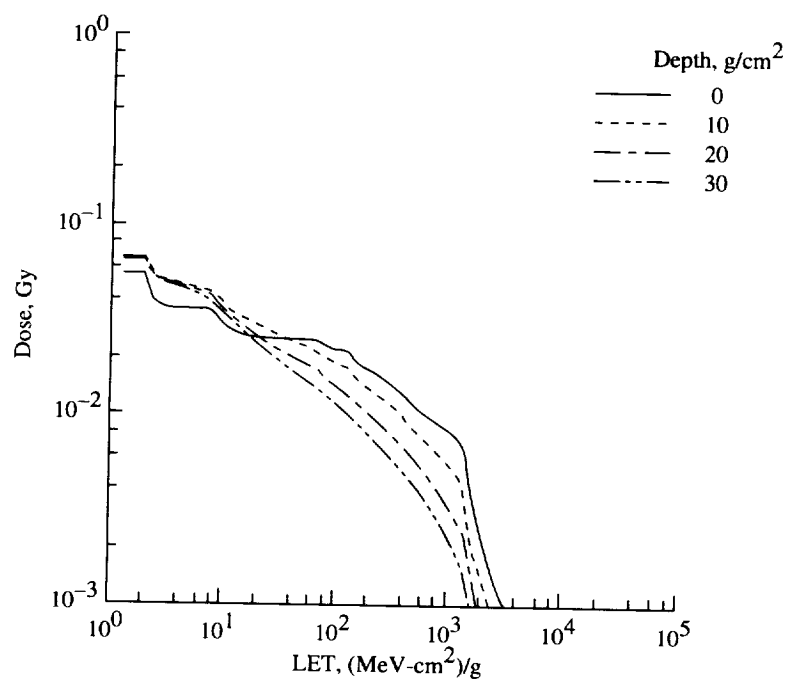


(b) 1981 solar maximum.

Figure 43. GCR skin integral flux LET spectra in liquid hydrogen.

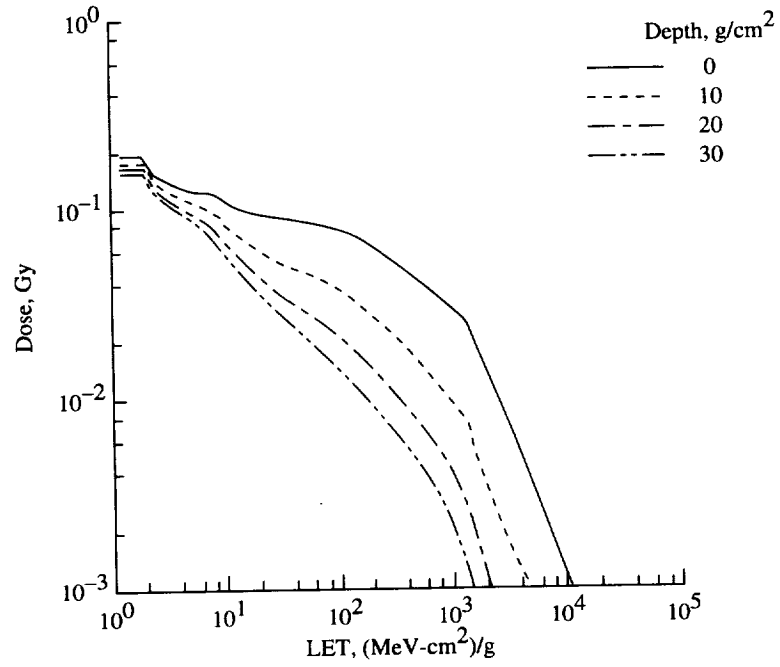


(a) 1977 solar minimum.

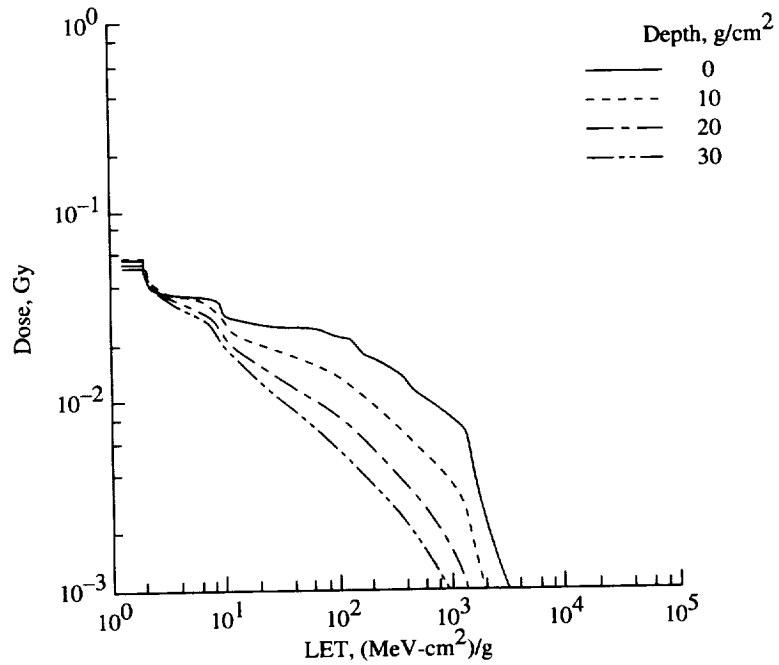


(b) 1981 solar maximum.

Figure 44. GCR skin dose LET spectra in aluminum.

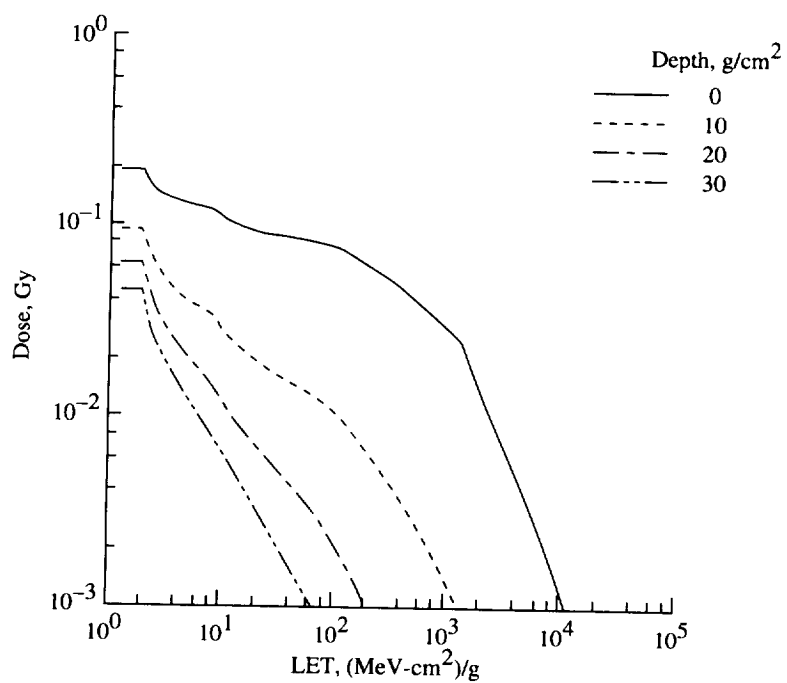


(a) 1977 solar minimum.

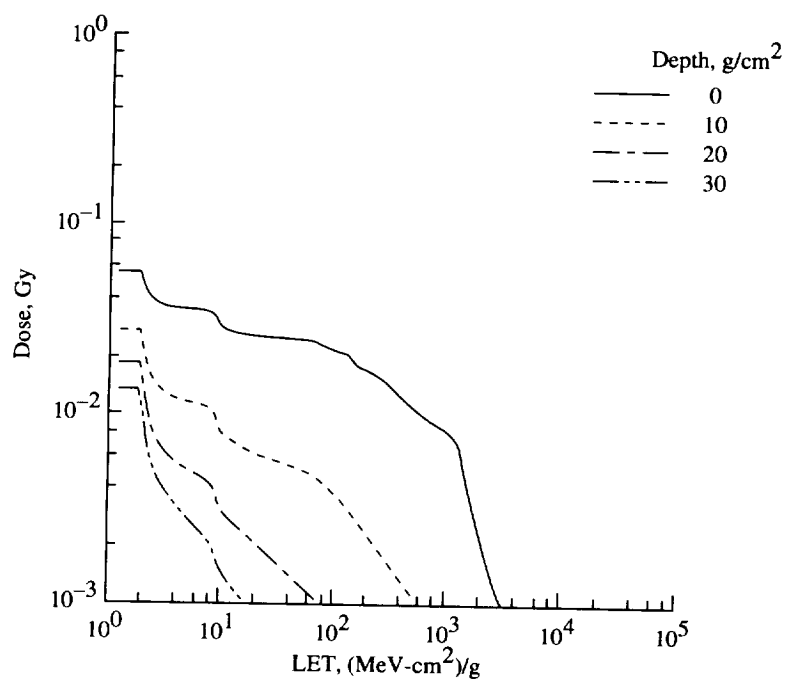


(b) 1981 solar maximum.

Figure 45. GCR skin dose LET spectra in water.

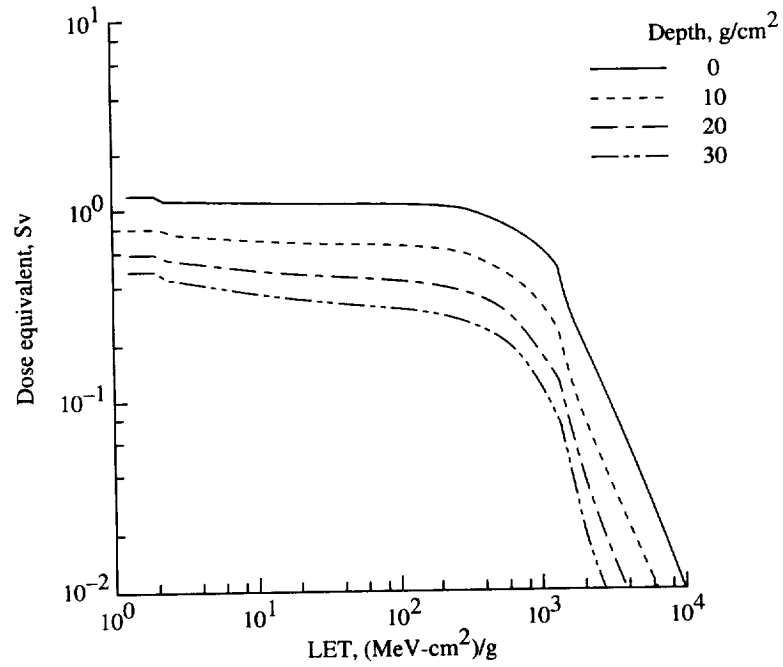


(a) 1977 solar minimum.

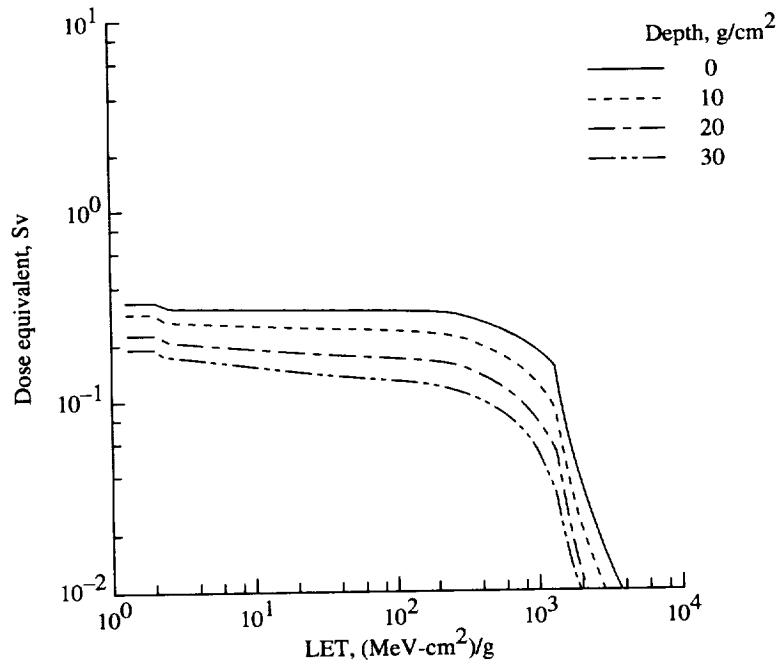


(b) 1981 solar maximum.

Figure 46. GCR skin dose LET spectra in liquid hydrogen.

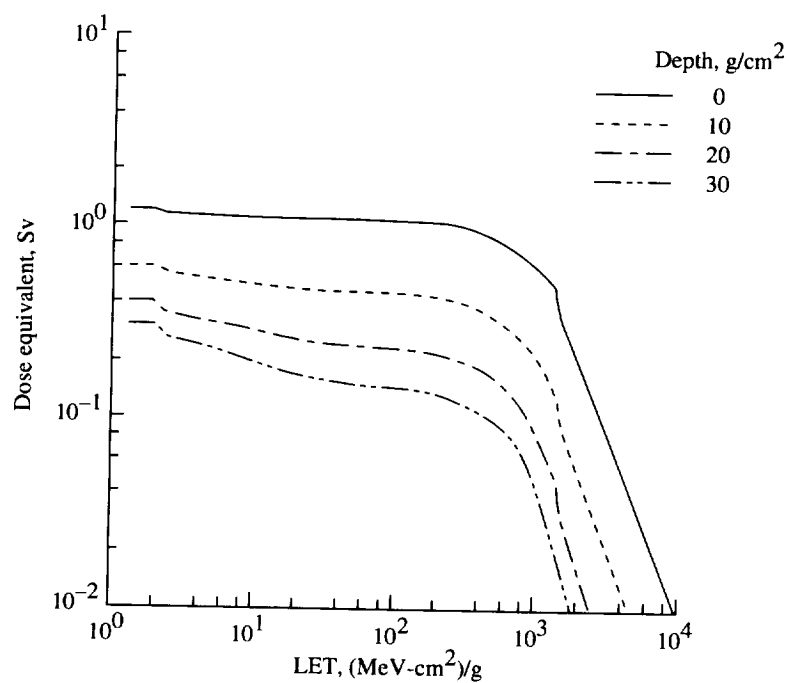


(a) 1977 solar minimum.

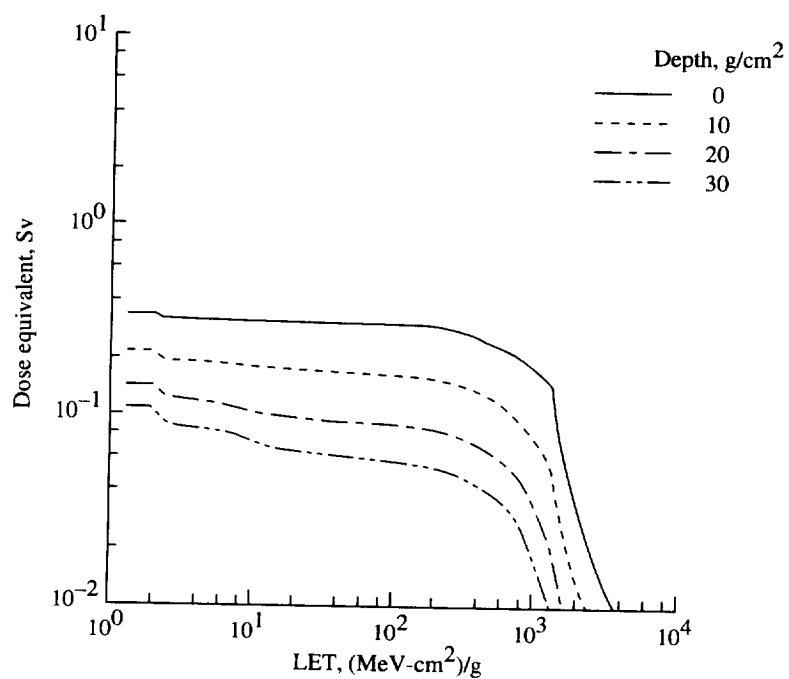


(b) 1981 solar maximum.

Figure 47. GCR skin dose equivalent LET spectra in aluminum.

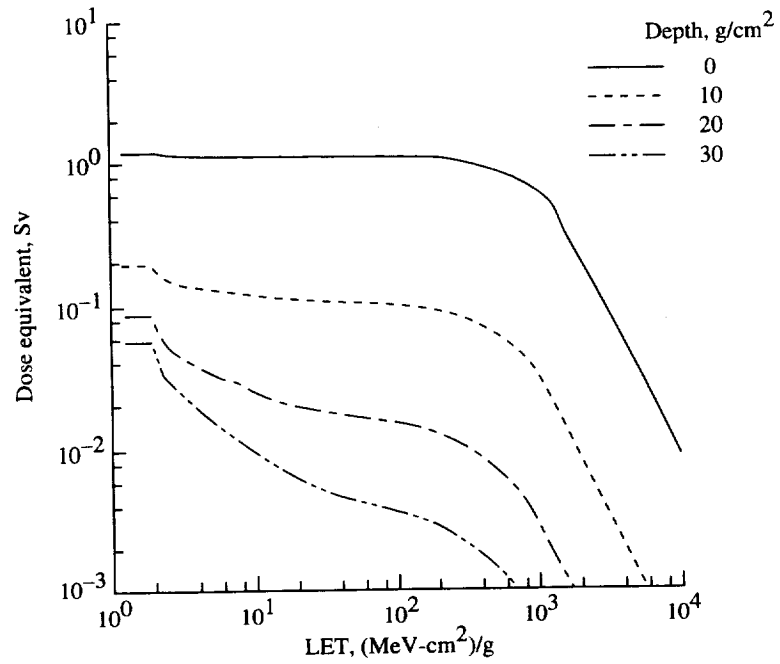


(a) 1977 solar minimum.

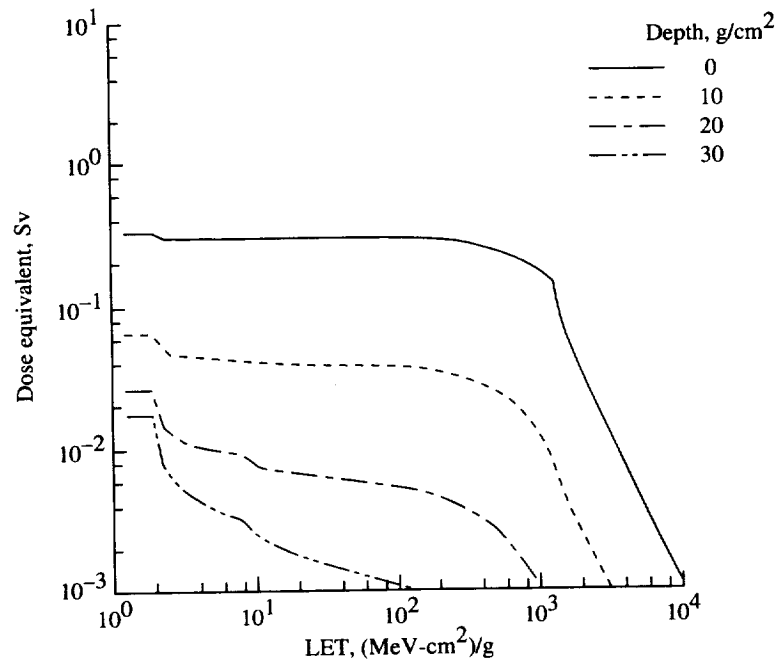


(b) 1981 solar maximum.

Figure 48. GCR skin dose equivalent LET spectra in water.

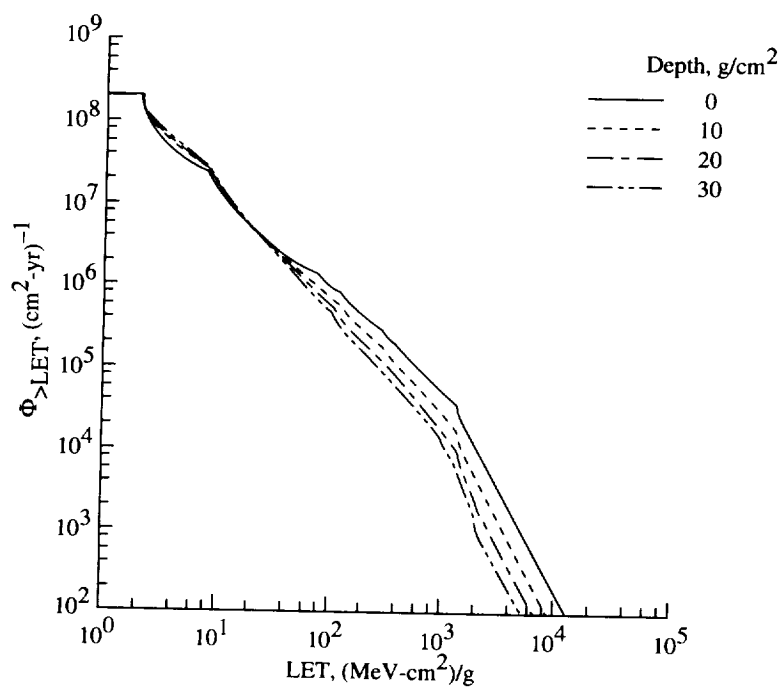


(a) 1977 solar minimum.

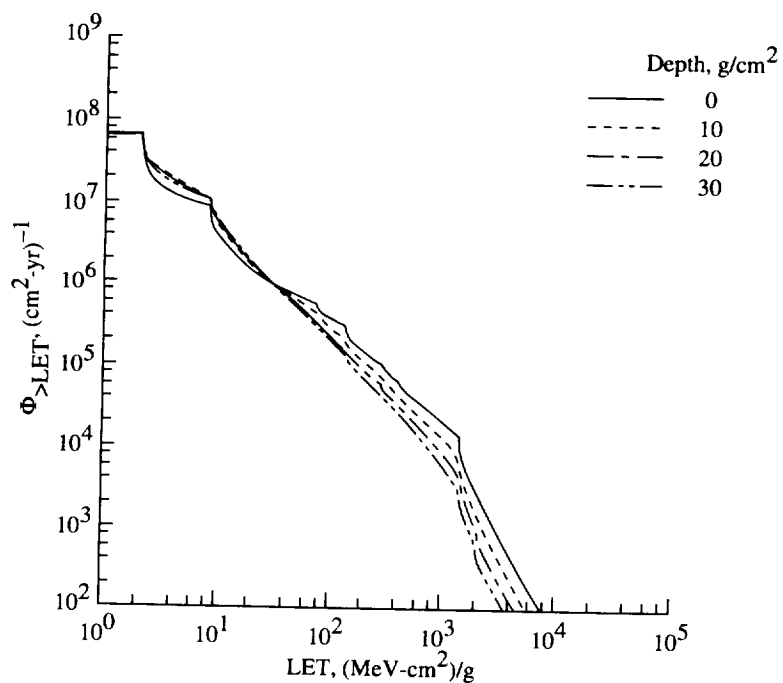


(b) 1981 solar maximum.

Figure 49. GCR skin dose equivalent LET spectra in liquid hydrogen.

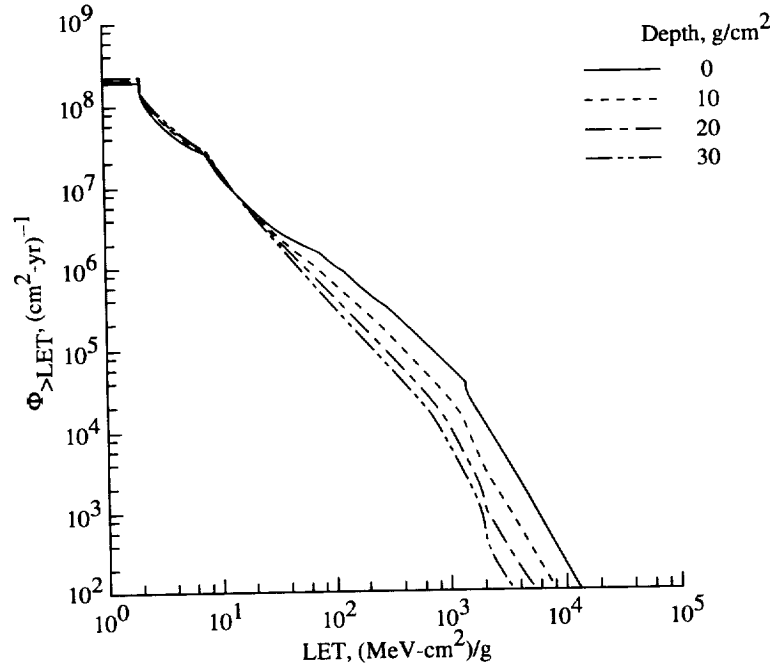


(a) 1977 solar minimum.

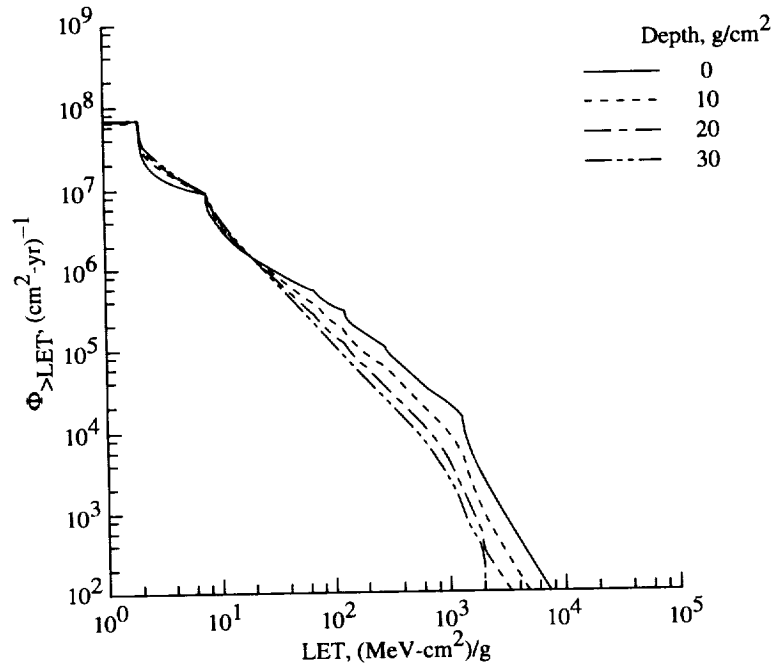


(b) 1981 solar maximum.

Figure 50. GCR 5-cm-BFO integral flux LET spectra in aluminum.

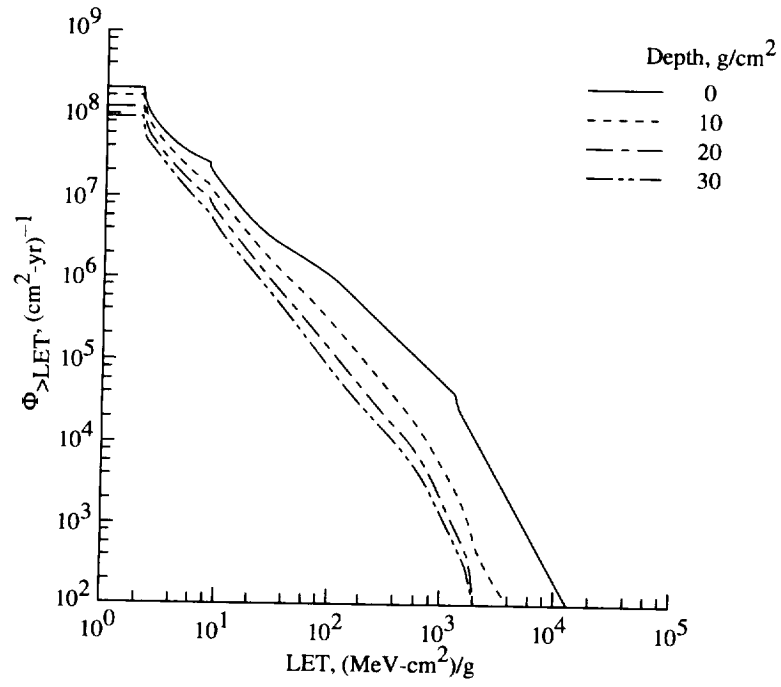


(a) 1977 solar minimum.

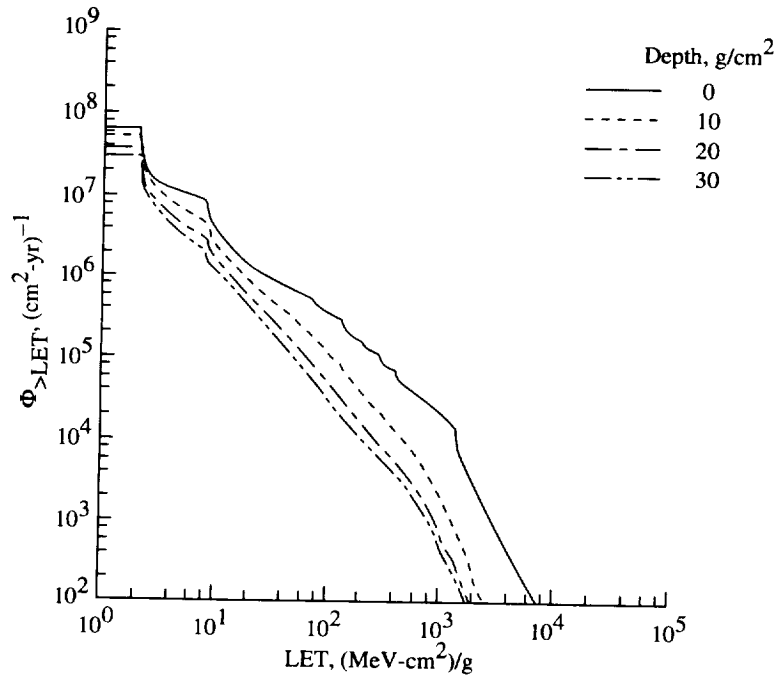


(b) 1981 solar maximum.

Figure 51. GCR 5-cm-BFO integral flux LET spectra in water.

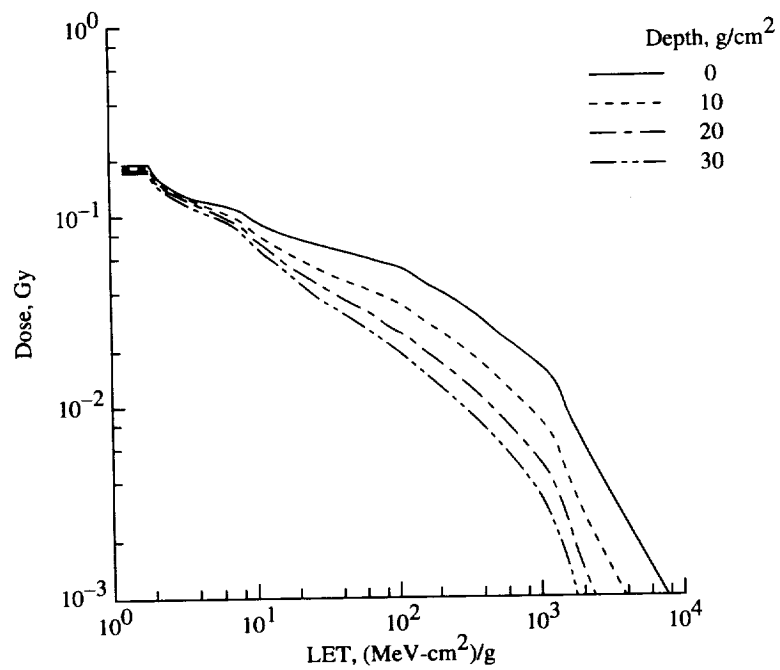


(a) 1977 solar minimum.

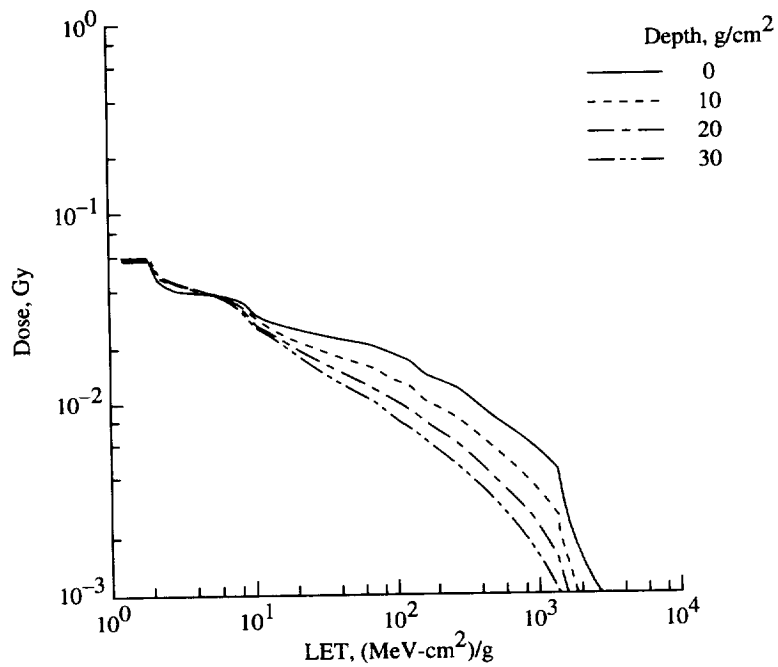


(b) 1981 solar maximum.

Figure 52. GCR 5-cm-BFO integral flux LET spectra in liquid hydrogen.

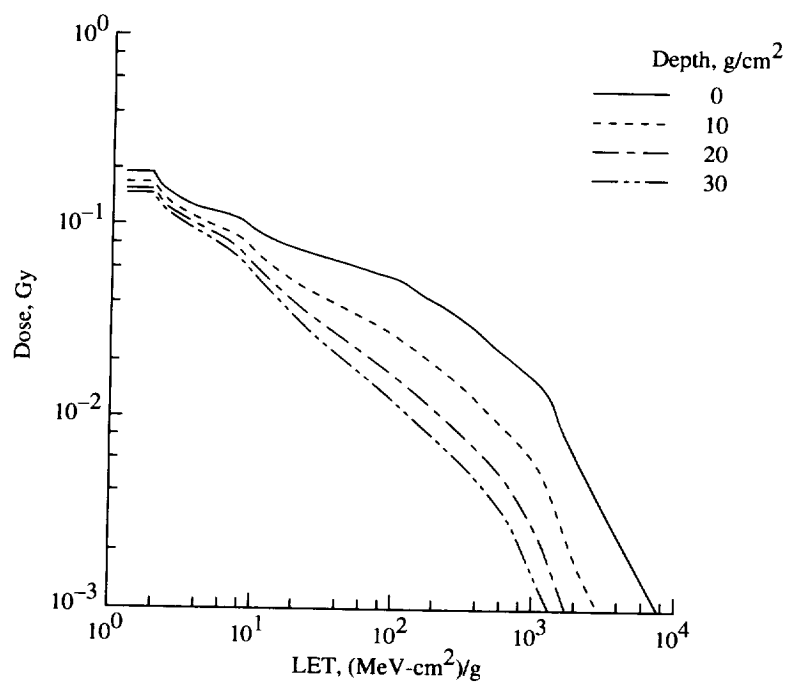


(a) 1977 solar minimum.

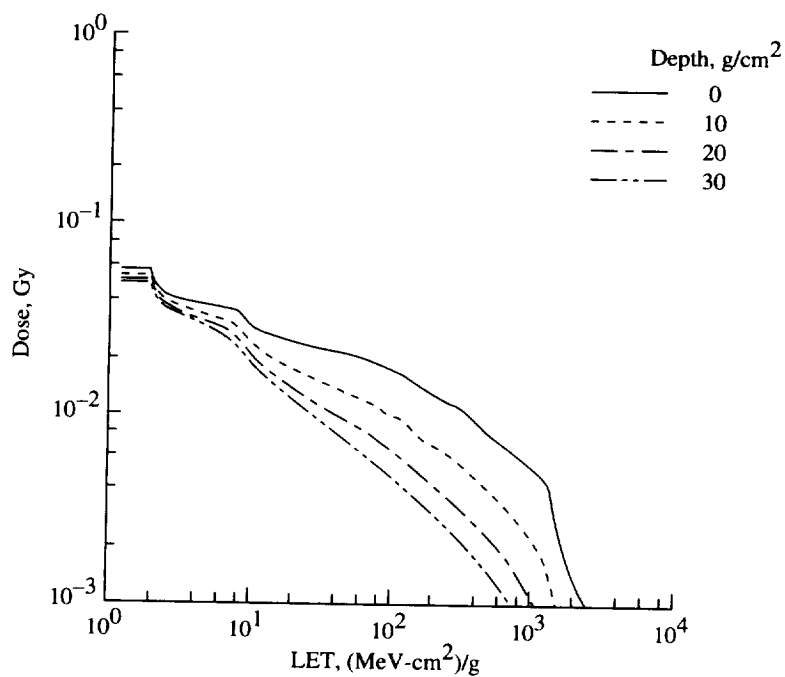


(b) 1981 solar maximum.

Figure 53. GCR 5-cm-BFO dose LET spectra in aluminum.

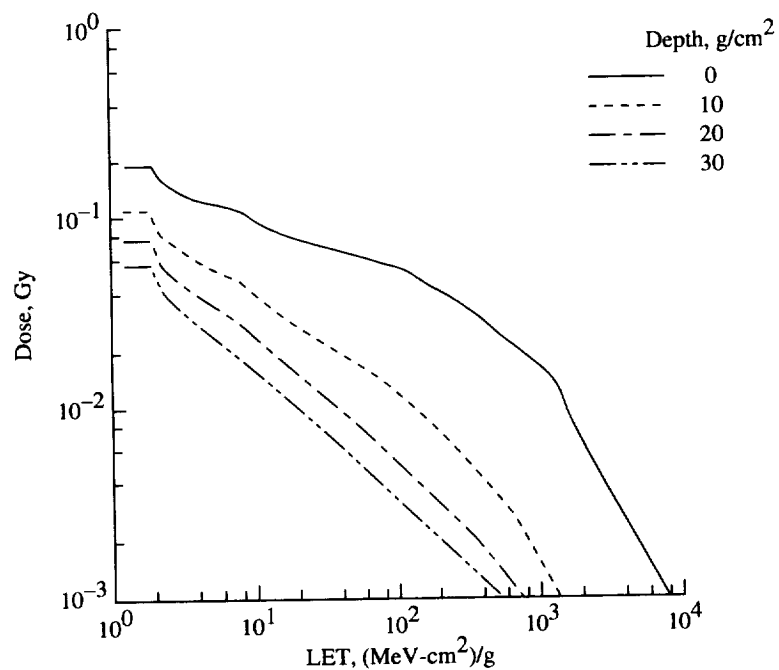


(a) 1977 solar minimum.

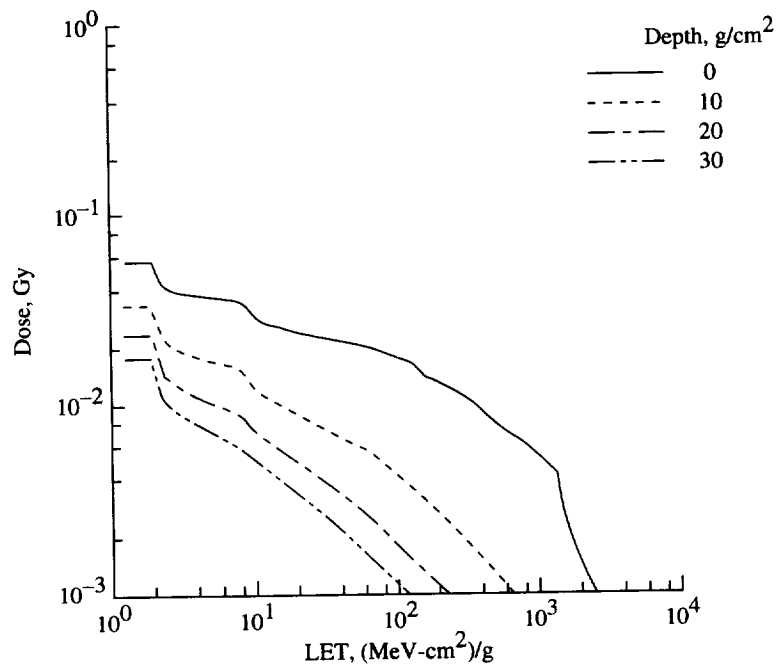


(b) 1981 solar maximum.

Figure 54. GCR 5-cm-BFO dose LET spectra in water.

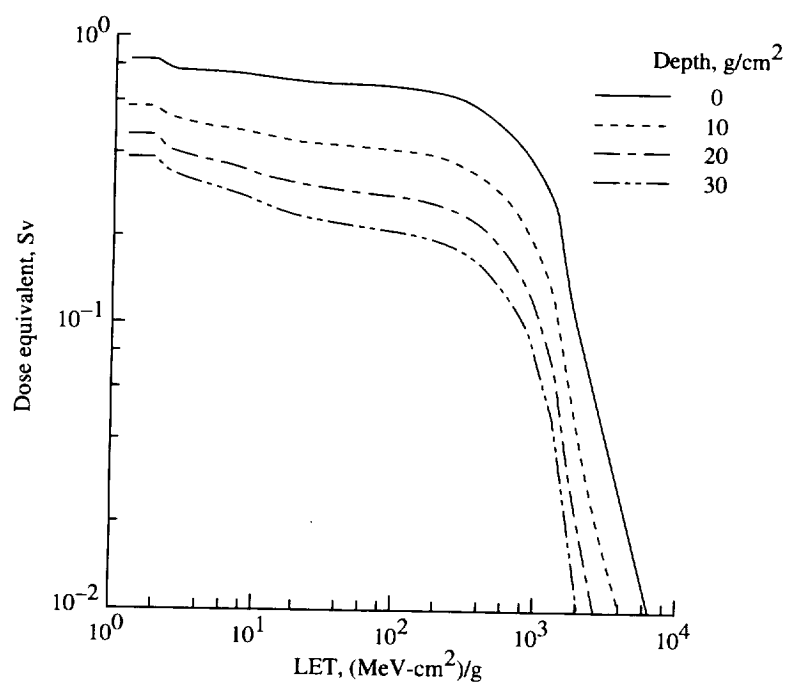


(a) 1977 solar minimum.

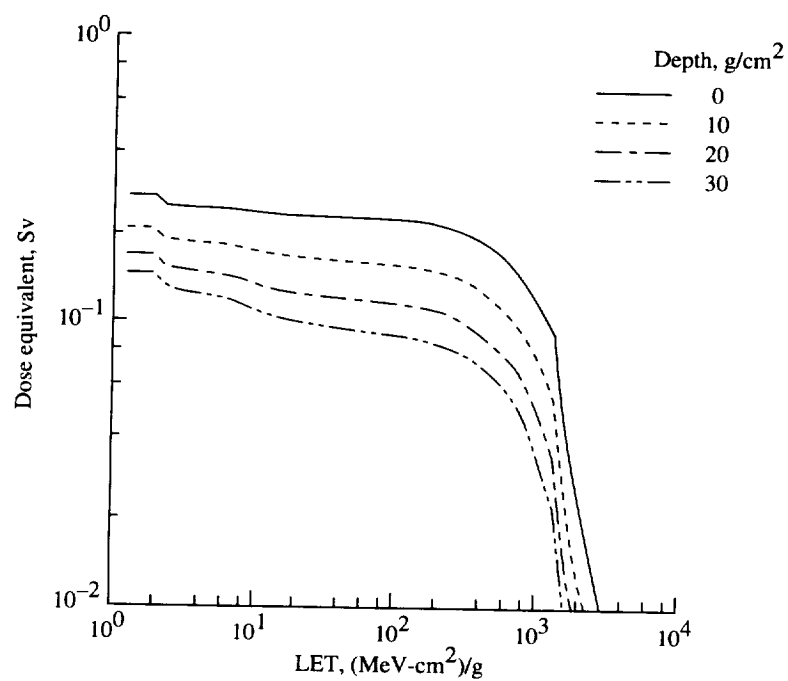


(b) 1981 solar maximum.

Figure 55. GCR 5-cm-BFO dose LET spectra in liquid hydrogen.

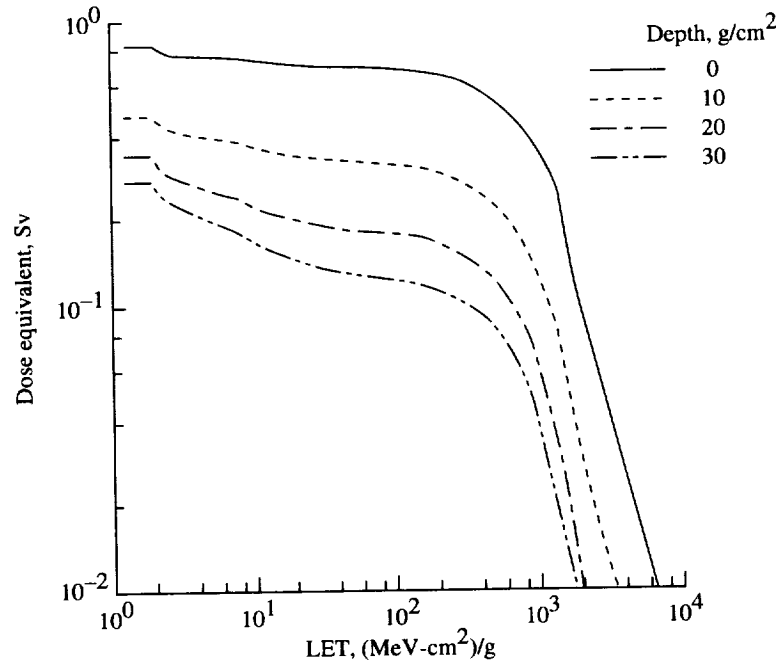


(a) 1977 solar minimum.

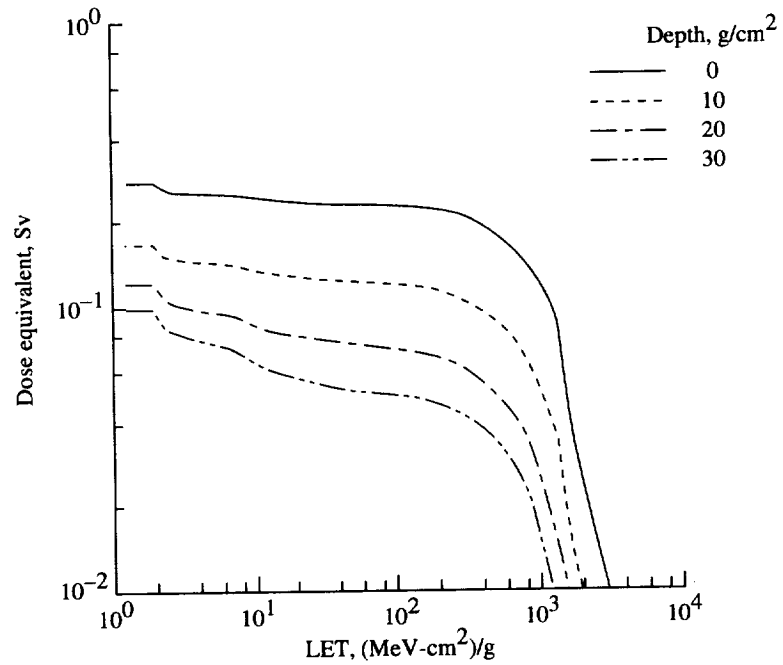


(b) 1981 solar maximum.

Figure 56. GCR 5-cm-BFO dose equivalent LET spectra in aluminum.

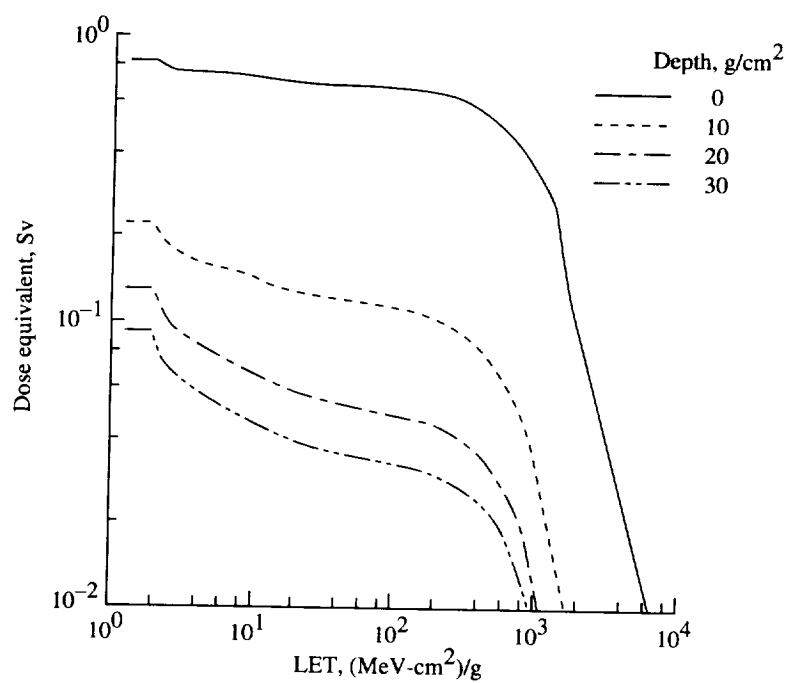


(a) 1977 solar minimum.

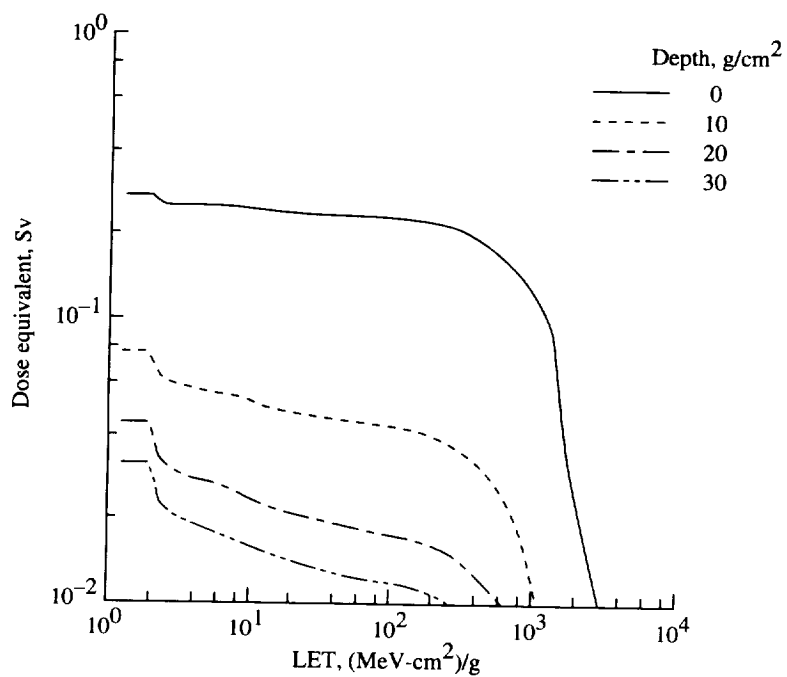


(b) 1981 solar maximum.

Figure 57. GCR 5-cm-BFO dose equivalent LET spectra in water.



(a) 1977 solar minimum.



(b) 1981 solar maximum.

Figure 58. GCR 5-cm-BFO dose equivalent LET spectra in liquid hydrogen.

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13. ABSTRACT (Maximum 200 words) The high-charge-and-energy (HZE) transport computer program HZETRN is developed to address the problems of free-space radiation transport and shielding. The HZETRN program is intended specifically for the design engineer who is interested in obtaining fast and accurate dosimetric information for the design and construction of space modules and devices. The program is based on a one-dimensional space-marching formulation of the Boltzmann transport equation with a straight-ahead approximation. The effect of the long-range Coulomb force and electron interaction is treated as a continuous slowing-down process. Atomic (electronic) stopping power coefficients with energies above a few A MeV are calculated by using Bethe's theory including Bragg's rule, Ziegler's shell corrections, and effective charge. Nuclear absorption cross sections are obtained from fits to quantum calculations and total cross sections are obtained with a Ramsauer formalism. Nuclear fragmentation cross sections are calculated with a semiempirical abrasion-ablation fragmentation model. The relation of the final computer code to the Boltzmann equation is discussed in the context of simplifying assumptions. A detailed description of the flow of the computer code, input requirements, sample output, and compatibility requirements for non-VAX platforms are provided.				
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