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## Computational simulation of damage progression of composite thin shells subjected to mechanical loads

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# THEORETICAL AND APPLIED FRACTURE MECHANICS

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## Computational simulation of damage progression of composite thin shells subjected to mechanical loads

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### Abstract

Defect-free and defected composite thin shells with ply orientation  $(90/0/\pm 75)$  made of graphite/epoxy are simulated for damage progression and fracture due to internal pressure and axial loading. The thin shells have a cylindrical geometry with one end fixed and the other free. The applied load consists of an internal pressure in conjunction with an axial load at the free end, the cure temperature was 177°C (350°F) and the operational temperature was 21°C (70°F). The residual stresses due to the processing are taken into account. Shells with defect and without defects were examined by using CODSTRAN an integrated computer code that couples composite mechanics, finite element and account for all possible failure modes inherent in composites. CODSTRAN traces damage initiation, growth, accumulation, damage propagation and the final fracture of the structure. The results show that damage initiation started with matrix failure while damage/fracture progression occurred due to additional matrix failure and fiber fracture. The burst pressure of the  $(90/0/\pm 75)$  defected shell was 0.092% of that of the free defect. Finally the results of the damage progression of the  $(90/0/\pm 75)$ , defective composite shell was compared with the  $(90/0/\pm \theta)$ , where  $\theta = 45$  and 60, layup configurations. It was shown that the examined laminate  $(90/0/\pm 75)$  has the least damage tolerant of the two compared defective shells with the  $(90/0/\pm \theta)$ ,  $\theta = 45$  and 60 laminates.

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### 1. Introduction

Aircraft, marine and automotive vehicle industries use composite shells because of their low weight and high stiffness and stability features. Design considerations with regard to the durability of composite shells require a priori evaluation of damage initiation and propagation mechanisms under expected service loads. Concerns for safety and survivability of critical components require quantification of the composite structural damage tolerance during overloads.

Characteristic flexibilities in the tailoring of composite structures make them more versatile for fulfilling structural design requirements. However, these same design flexibilities render the assessment of composite structural response and durability more complex, prolonging the design and certification process and adding to the cost of the final product. It is difficult to evaluate composite structures because of the complexities in predicting their overall congruity and performance, especially when structural degradation and damage propagation take place. The predictions of damage initiation, damage growth, and propagation to fracture are important in evaluating the load carrying capacity, damage tolerance, safety, and reliability of composite structures. The most effective

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way to obtain this quantification is through integrated computer codes that couple composite mechanics with structural analysis and damage progression models. The COmposite Durability STRuctural ANalysis (CODSTRAN) computer code has been developed for this purpose by integrating and coupling the following disciplines: (i) mechanics of composites, (ii) structural analysis (FEM) and (iii) damage progression tracking. CODSTRAN computer code was used to simulate the damage progression in a variety of fiber composite structures such as: progressive fracture of fiber composite thin shell structures [1–3], fiber composite stiffshed panels [4], Stiflened adhesively bonded composite structures [5], dynamic damage progression of a containment structure hit by an escaping blade [6], damage progression in adhesively bonded fiber composite thin shell structures [7] and [8], damage progression in bolted composite structures [9] and simulation of the Iosipescu shear testing [10].

The objective of the present paper is to demonstrate what can be accomplished by integrating composite mechanics, finite element structural analysis, and tracking of composite failure modes into a stand-alone computer code. The computer code in our case is CODSTRAN. Reference to CODSTRAN throughout this report should not be construed neither as NASA endorsement nor as an advertisement of that computer code.

## 2. Progressive fracture methodology in codstran

CODSTRAN is an integrated computer code which was developed by coupling three modules: composite mechanics (ICAN [11]), finite element analysis (MHOST [12]) and a damage progression modelling algorithm:

(1) ICAN is a composite mechanics computer code [11] that provides the constituent (fiber and matrix) material properties using an available data bank, and computes the ply properties and the composite properties (effective properties) of the laminate in a hygrothermal environment. The theory of the code is based on the micromechanics of composites and the laminate theory. ICAN has the ability to compute the ply stresses by knowing the stress resultants (force per laminate thickness, where force can

### PLY FAILURE CRITERIA

#### ♦ MAXIMUM STRESS FAILURE CRITERION.

THE SIX PLY STRESS COMPONENTS ARE ALONG THE MATERIAL AXES.

$$S_{L11C} < \sigma_{L11} < S_{L11T}$$

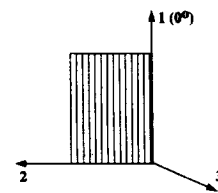
$$S_{L22C} < \sigma_{L22} < S_{L22T}$$

$$S_{L33C} < \sigma_{L33} < S_{L33T}$$

$$S_{L12(-)} < \tau_{L12} < S_{L12(+)}$$

$$S_{L23(-)} < \tau_{L23} < S_{L23(+)}$$

$$S_{L13(-)} < \tau_{L13} < S_{L13(+)}$$



#### ♦ MDE COMBINED STRESS FAILURE CRITERION.

$$F = 1 - [(\sigma_{L11a}/S_{L11a})^2 + (\sigma_{L22b}/S_{L22b})^2 - K_{L12ab}(\sigma_{L11a}/S_{L11a})(\sigma_{L22b}/S_{L22b}) + (\tau_{L12s}/S_{L12s})^2]^{1/2}$$

Fig. 1. Ply failure criteria.

be a concentrated load, a bending or a twisting load). In ICAN failure criteria were established (Fig. 1), for the detection of the ply failures as follows: (a) the maximum stress criterion, in which failure occurs when the individual ply stress  $\sigma_{Lij}$  for  $i, j = 1, 2, 3$ , exceeds the respective ply strength  $S_{Lij}$  for  $i, j = 1, 2, 3$ ; and (b) the modified distortion energy criterion, in which the combination of the ply stresses is taken into account. In Fig. 1, a and b are referred to the tensile and compressive stresses, respectively. In both criteria the ply stresses are referred to the material axes 1, 2, 3, and the direction of the  $0^\circ$  fibers are along the direction of the material 1-axis. For example a laminate with configuration  $(90/0/\pm 75)$  and ply stresses at the top ply ( $90^\circ$ ) are shown in Fig. 2. In ICAN, the described failure modes of the plies are: failure due to the fiber

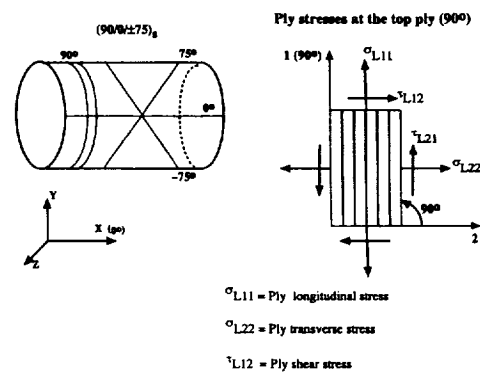


Fig. 2. A typical laminate configuration  $(90/0/\pm 75)$  and the ply stresses at the top ply ( $90^\circ$ ).

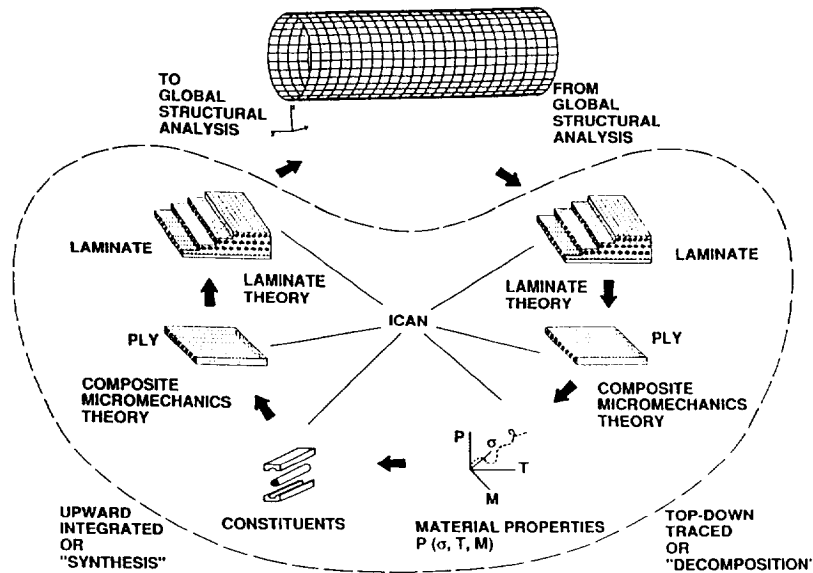


Fig. 3. CODSTRAN progressive fracture simulation cycle.

fracture in tension or in compression; damage due to the matrix fracture in tension or in compression; and damage due to intralaminar and interlaminar shear fracture.

(2) MHOST is a finite element computer code [12] for the solution of structural analysis problems. The code has the capability to perform linear or nonlinear static and dynamic analysis. MHOST has a library with a variety of elements and for the present work the four node shell element was used. By supplying the boundary conditions, the desire type of analysis, the applied loads and the laminate properties (using ICAN) MHOST performs the structural analysis. In addition MHOST provides the computed stress resultants to the ICAN code; and then ICAN computes the developed ply stresses for each ply and checks for ply failure.

(3) A module that keeps track the failure modes and communicate these modes to ICAN in order to degrade the properties associated with the respected failure modes.

An integrated schematic of the CODSTRAN simulation cycle is shown in Fig. 3. In this figure, from the left side along the clockwise direction the material properties of the constituents (fiber and matrix) are provided by ICAN's data bank, next the ply properties are computed by using the micromechan-

ics theory, and the laminate properties are computed using the laminate theory. These properties in conjunction with the finite element mesh, the loads and the boundary conditions are incorporated into MHOST. MHOST performs the structural analysis and provides the computed stress resultants in ICAN (in the right side of Fig. 3), where ICAN proceeds to compute the ply stresses using the laminate theory and checks for ply failure.

The nonlinear structural analysis in MHOST code is performed in conjunction with an incremental load algorithm. The load is increased in small increments

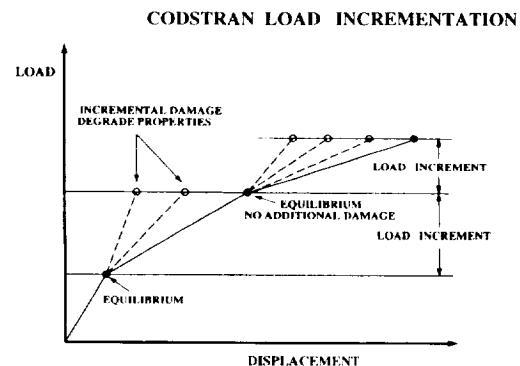


Fig. 4. CODSTRAN load increment.

(equilibrium positions). Within each equilibrium position a number of iterations are performed for damage growth and accompanying internal structural response to sustain the applied load, Fig. 4. In each iteration, the structure is checked for ply failure. If damages are detected in the structure, the model is automatically updated with a new finite element mesh and new laminate properties, and a new finite element analysis is performed; the above iterations continue until no further damage occurs (equilibrium position). After that, the load is increased, and the above procedure is repeated until the final failure of the structure. Following the above procedure, the damage progression, fracture and collapse of the structure is monitored.

### 3. Geometry, loads, materials and the FE model of the thin shell

The geometry of the fiber composite shell is a thin cylinder. The thin cylinder has inner diameter of 305 mm (12 in.) and length of 760 mm (30 in.). The boundary conditions are one end fixed supported and the other free. The corresponding graphite fibers (AS-4) and epoxy matrix (HMES) properties of the fiber composite thin shell were obtained from a data

Table 1  
AS-4 graphite fiber properties

Number of fibers per end = 10000
Fiber diameter = 0.00762 mm (0.3E-3 in)
Fiber density = $4.04 \times E - 7 \text{ kg/m}^3$ (0.063 lb/in. <sup>3</sup> )
Longitudinal normal modulus = 227 GPa ( $32.9 \times E + 6$ psi)
Transverse normal modulus = 13.7 GPa ( $1.99 \times E + 6$ psi)
Poisson's ratio ( $\nu_{12}$ ) = 0.2
Poisson's ratio ( $\nu_{23}$ ) = 0.25
Shear modulus ( $G_{12}$ ) = 13.8 GPa ( $2 \times E + 6$ psi)
Shear modulus ( $G_{23}$ ) = 6.9 GPa ( $1 \times E + 6$ psi)
Longitudinal thermal expansion coefficient = $1 \times E - 6/^{\circ}\text{C}$ ( $-0.55 \times E - 6/^{\circ}\text{F}$ )
Transverse thermal expansion coefficient = $1 \times E - 6/^{\circ}\text{C}$ ( $-0.56 \times E - 6/^{\circ}\text{F}$ )
Longitudinal heat conductivity = $43.4 \text{ J m/h/m}^2/^{\circ}\text{C}$ (580 BTU-in/h/in. <sup>2</sup> /°F)
Transverse heat conductivity = $4.34 \text{ J m/h/m}^2/^{\circ}\text{C}$ (58 BTU-in/h/in. <sup>2</sup> /°F)
Heat capacity = 712 J/kg/°C (0.17 BTU/lb/°F)
Tensile strength = 3723 MPa (540 psi)
Compressive strength = 3351 MPa (486 psi)

Table 2  
HMES epoxy matrix properties

Matrix density = $3.4 \times E - 7 \text{ kg/m}^3$ (0.0457 lb/in. <sup>3</sup> )
Normal modulus = 4.27 GPa (629 psi)
Poisson's ratio = 0.34
Coefficient of thermal expansion = $0.72/^{\circ}\text{C}$ ( $0.4 \times E - 4/^{\circ}\text{F}$ )
Heat conductivity = $1.25 \text{ BTU-in./h/in.}^2/^{\circ}\text{F}$
Heat capacity = 0.25 BTU/lb/°F
Tensile strength = 84.8 MPa (12.3 psi)
Compressive strength = 423 MPa (61.3 psi)
Shear strength = 148 MPa (21.4 psi)
Allowable tensile strain = 0.02
Allowable compressive strain = 0.05
Allowable shear strain = 0.04
Allowable torsional strain = 0.04
Void conductivity = $16.8 \text{ J m/h/m}^2/^{\circ}\text{C}$ (0.225 BTU-in./h/in. <sup>2</sup> /°F)
Glass transition temperature = 216°C (420 °F)

bank of composite constituent material properties resident in CODSTRAN and are given in Tables 1 and 2, respectively. The AS4/HMES ply strengths computed by ICAN code are given in Table 3. The fiber composite thin shell consists of eight 0.136 mm (0.00535 in.) plies resulting in a composite shell thickness of 1,088 mm (0.0428 in.). The laminate configuration is (90/0/±75), with the 90° plies in the hoop (or circumferential) direction and the 0° plies in the axial direction. Fiber orientations in the ±75° is shown in Fig. 2. The fiber volume ratio is 60% and the void volume ratio is 2% of the total volume of the structure. The residual stresses is been taken into account due to the processing. The cure temperature was 177°C (350°F) and the pressurization/use temperature is 21°C (70°F). The moisture content was zero. The closed-end cylindrical pressure vessel is simulated by applying a uniformly

Table 3  
AS-4/RMHS ply strengths

$S_{L11T}$ = 1930.30 MPa (280 psi)
$S_{L11C}$ = 1475.85 MPa (210 psi)
$S_{L22T}$ = 91.38 Mpa (13 psi)
$S_{L22C}$ = 228.27 MPa (33 psi)
$S_{L12}$ = 65.57 MPa (9.5 psi)
$S_{L23}$ = 59.98 MPa (8.7 psi)

Where 1, 2, 3 are the material axes of the ply. The direction of the fibers are parallel to 1-axis. T is for tension and C is for compression.

## FIBER COMPOSITE THIN CYLINDRICAL STRUCTURE

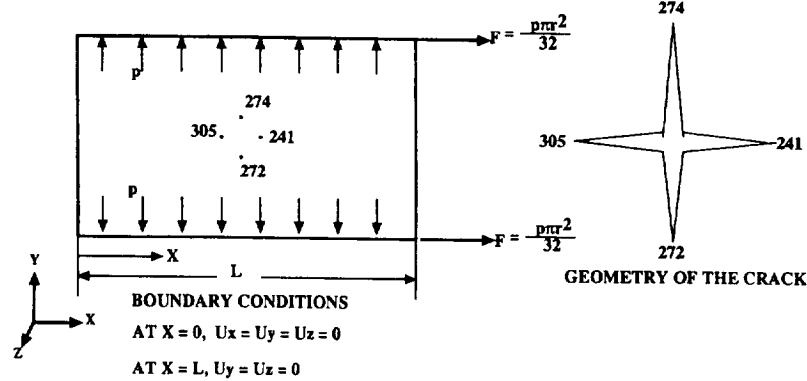
CYLINDER LENGTH,  $L = 76.2$  cm (30 in.)INNER RADIUS,  $r = 15.24$  cm (6 in.)LAMINATE THICKNESS,  $t = 0.11$  cm (0.043 in.)GRAPHITE/EPOXY, (90/0/±75)<sub>s</sub>, FIBER VOLUME FRACTION = 60 %

Fig. 5. Applied loads and boundary conditions of the thin shell structures.

distributed axial tension such that the generalized axial stresses in the shell wall were half of those developed in the hoop direction, Fig. 5. The shell is subjected to a monotonically increasing internal pressure until it burst. Shells with defect and defect free are examined. The defective shell has a through-the-thickness defect at a node located at the half length of the shell. After the load is applied in the

defective shell, a crack is formed at the location of the defective node as shown in Fig. 5. The geometry of the formed crack consists of a 95 mm (3.75 in.) long thin axial slit that is superimposed on a 60 mm (2.36 in.) long circumferential slit. Each finite element model contained 544 nodes and 512 uniformly sized rectangular elements, Fig. 6. Damage initiation, growth, fracture progression, and global structural

DAMAGE INITIATION, AT INTERNAL PRESSURE 25 PSI.

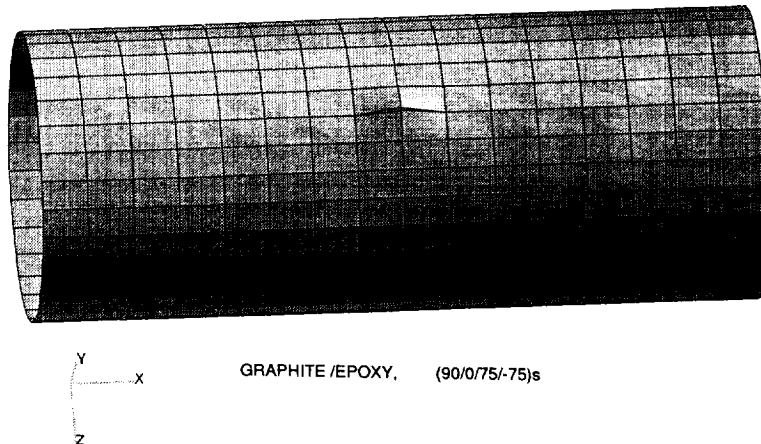


Fig. 6. Finite element mesh.

fracture stages were investigated. Computed results are presented up to global fracture for defect-free shells and shells with through-the-thickness defects.

#### 4. Results and discussion

(1) Fiber composite (90/0/±75), free defects thin shells. The damage of the thin shell structure is plotted versus the internal pressure in Fig. 7.1. Damage is defined as the ratio of the volume of the damaged plies divided by the total volume of the

plies. The depicted points of Fig. 7.1 are equilibrium points that were discussed in the previous chapter in CODSTRAN Methodology. Damage initiation occurred at pressure of 1.06 MPa (153 psi) with matrix cracking at the outermost ply 2 (0°). The damage progressed with shear failure at the ply 3 (75°) and matrix cracking at the plies 7 (0°) and 8 (90°). Further, the damage progressed and matrix cracking occurred at the outermost ply 1 (90°), and at the 5 (–75°) and 6 (75°). After the initial matrix degradation stage the pressure was increased without activating additional damage modes. The thin shell burst

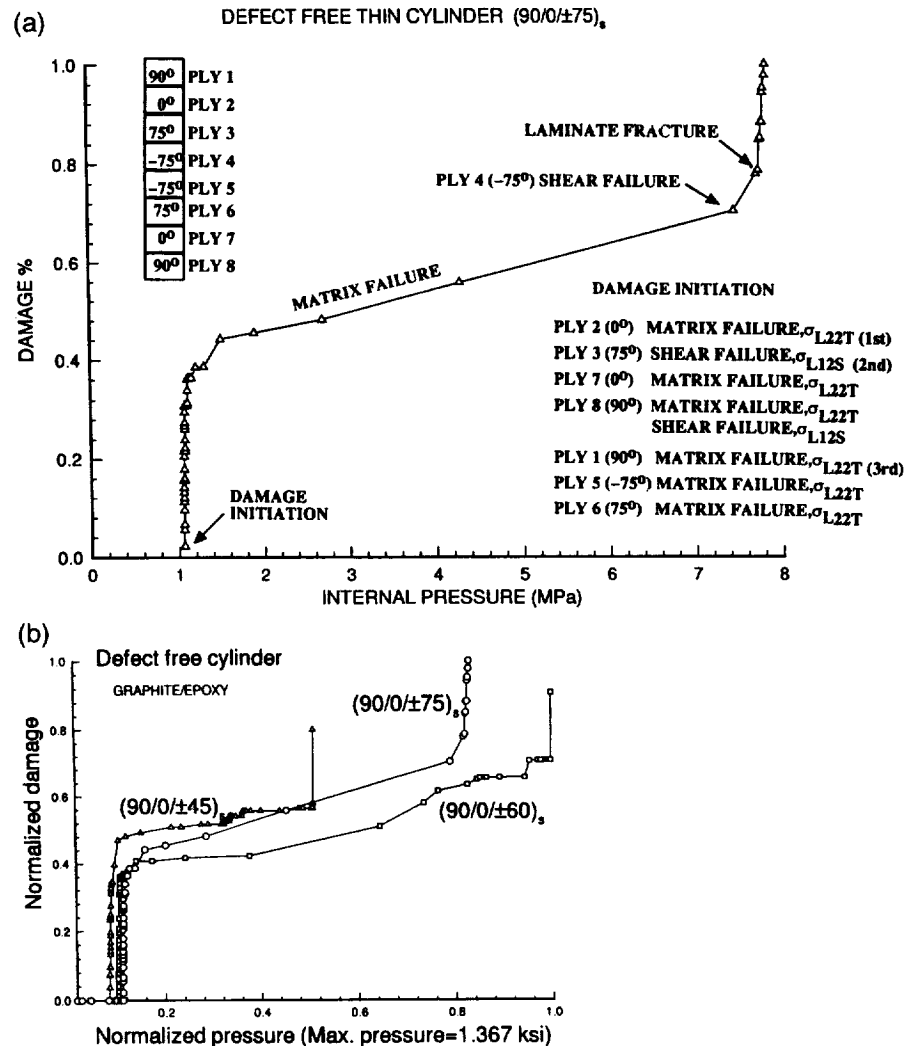


Fig. 7. (1) Damage versus pressure in defect-free thin shell. (2) effect of the laminate configuration, on the damage of the defect-free thin shells.



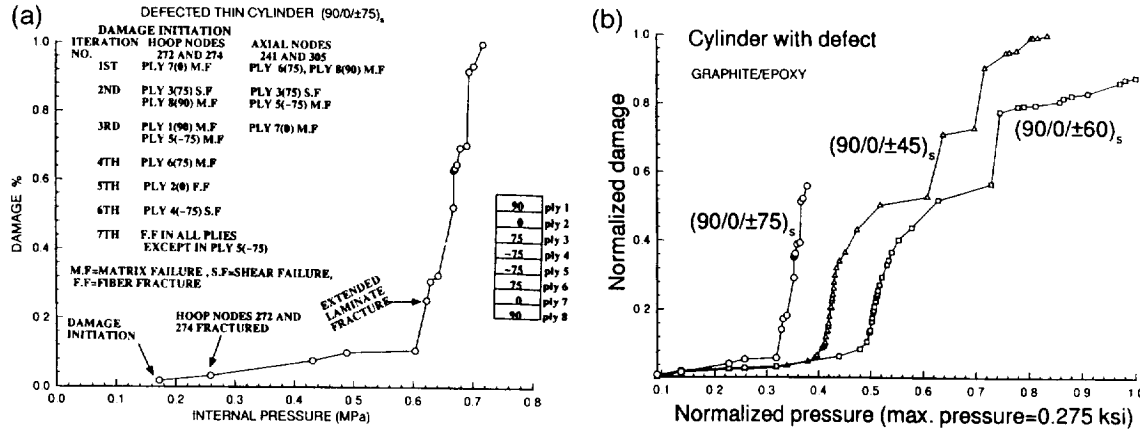


Fig. 8. (1) Damage versus pressure in defective thin shell. (2) Effect of the laminate configuration, on the damage of the defective thin shells.

when ply 2, the outermost 0° axial ply experienced fiber fractures that caused rapid damage propagation to the other plies and structural fracture. The structural fracture was initiated by the tensile failure of axial fibers. The simulated burst pressure was 7.83 MPa (1.14 psi).

The damage progression of the (90/0/±75) laminate compared with the (90/0/±45), and (90/0/±60), layup configurations in Fig. 7.2. In the case of the (90/0/±45), laminate, damage initiation occurred at 0.8 MPa (116 psi) with matrix cracking in the first ply (0°) followed by the 45° ply immediately adjacent to it, then the innermost (0°)

ply and the 90° ply on the interior surface. After damage initiation, all plies gradually sustained matrix cracking as the pressure was increased to 0.84 MPa (121 psi). After this damage accumulation stage the pressure was significantly increased without activating additional damage modes. The thin shell burst when the 90 hoop plies experience fiber fractures at 4.8 MPa (696 psi). In the case of the (90/0/±60), laminate, initial damage occurred at 0.97 MPa (140 psi) with matrix cracking at the 2nd ply (0) followed by the 3rd ply (60) then by the 7th ply (0) and finally by the 8th ply (90). After damage initiation, all plies gradually sustained matrix cracking as the pressure

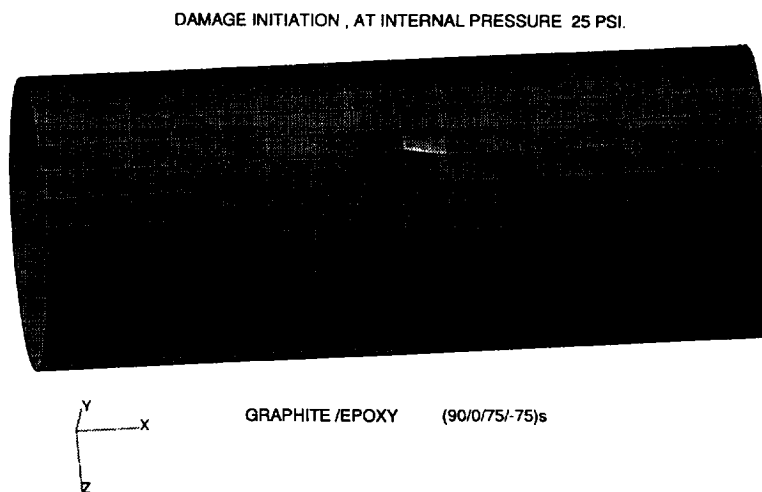


Fig. 9. Damage initiation at 0.17 MPa (25 psi).

## DAMAGE PROPAGATION, AT INTERNAL PRESSURE 37.5 PSI

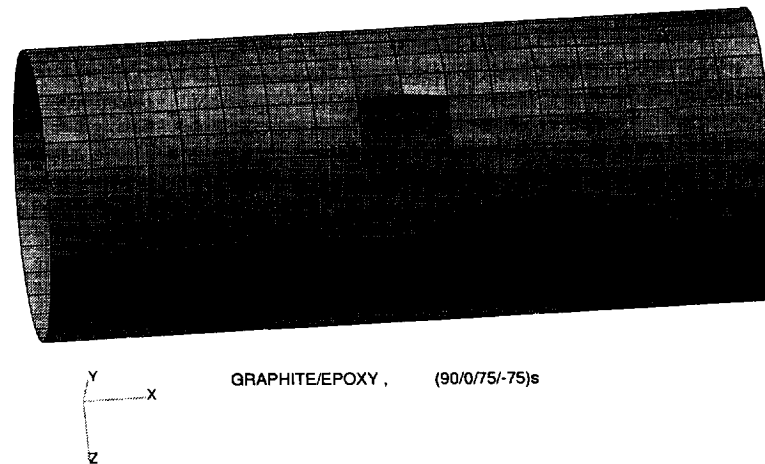


Fig. 10. Damage progression at 0.26 MPa (37.5 psi).

was retained virtually constant. After this damage accumulation stage, the pressure was significantly increased without activating additional damage modes. The thin shell burst when the outermost  $90^\circ$  hoop plies experienced fiber fractures at 9.42 MPa (1366 psi).

(2)  $(90/0/\pm 75)$ , fiber composite defective thin shells. The damage versus the internal pressure is shown in Fig. 8.1. The damage initiated at internal pressure of 0.172 MPa (25 psi.) with matrix fracture

along the hoop direction nodes 272 and 274 in the 7th ( $0^\circ$ ) ply and along the axial direction nodes 241 and 305 in the 6th ( $75^\circ$ ) and 8th ( $90^\circ$ ) plies. The damage progressed continuously with shear failure at the 3rd ( $75^\circ$ ) ply in both hoop and axial nodes, and with matrix failure at the 8th ( $90^\circ$ ) ply at the hoop and at the 5th ( $-75^\circ$ ) ply, at the axial node. The damage of the plies continued with relatively small increases in pressure in the hoop direction until fiber fracture occurred at all plies except of the 5th ( $-75^\circ$ ).

## DAMAGE PROPAGATION, AT INTERNAL PRESSURE 62.5 PSI

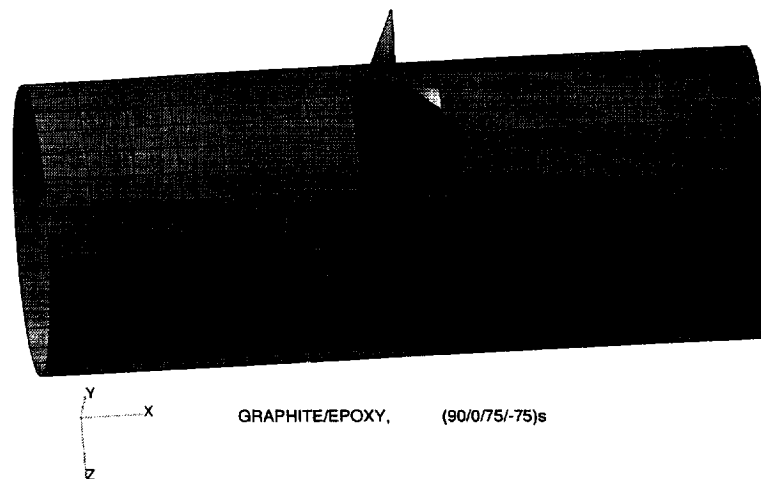


Fig. 11. Damage progression at 0.43 MPa (62.5 psi).

## DAMAGE PROPAGATION, AT INTERNAL PRESSURE 70.8 PSI

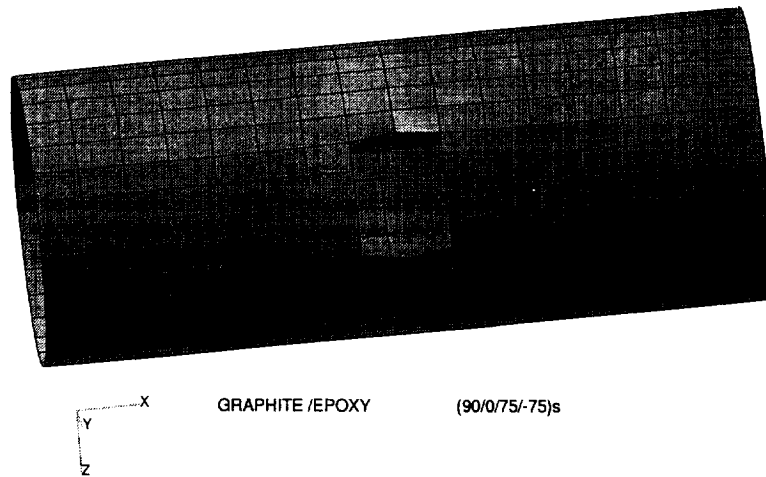


Fig. 12. Damage progression at 0.49 MPa (70.8 psi).

Increasing the load further, the damage of the shell progressed steadily until it reached the value of 0.62 MPa (90 psi) where the fracture growth became unstable, increased rapidly, and structural fracture occurred at burst pressure equal to 0.717 MPa (104 psi).

The damage progression of the  $(90/0/\pm 75)$  laminate compared with the  $(90/0/\pm 45)$  and  $(90/0/\pm 60)$  layup configurations as shown in Fig. 8.2. In the case of  $(90/0/\pm 45)$  laminate, the dam-

age initiation started at pressure 0.175 MPa (25 psi). The damage growth localized adjacent to the defect until a 0.74 MPa (108 psi) pressure reached. Damage propagation by fiber fractures concentrated near the defect. The thin shell burst at pressure equal to 1.58 MPa (230 psi). In the case of  $(90/0/\pm 60)$  laminate, damage initiation started at pressure 0.17 MPa (25 psi) by matrix cracking adjacent to the defect at the 8th ply ( $90^\circ$ ) at the circumferential slit tips and by the 7th ply ( $0^\circ$ ) at the axial slit tips. Damage

## DAMAGE PROPAGATION, AT INTERNAL PRESSURE 90. PSI

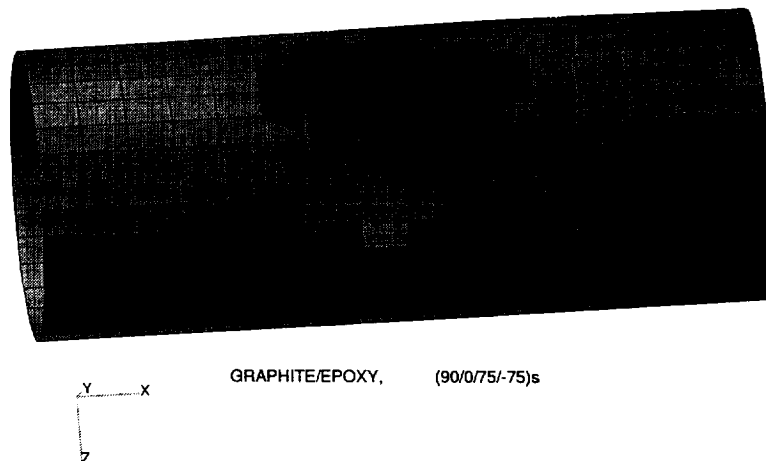


Fig. 13. Damage progression at 0.62 MPa (90.0 psi).

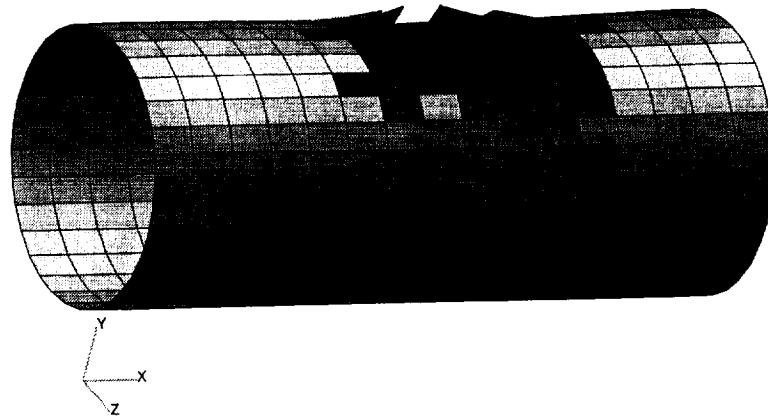


Fig. 14. Collapse of the defective shell at 0.71 MPa (104 psi).

growth remained localized adjacent to the defect as the pressure was increased to 0.91 MPa (132 psi). The thin shell burst at 1.9 MPa (275 psi).

Regarding the comparison of the direction of the damage progression: the damage growth of the (90/0/±45) laminate was mainly in the axial direc-

tion of the shell. The damage growth of the (90/0/±75) laminate was mainly in the circumferential direction of the shell. Finally, the direction for the damage growth for the (90/0/±60) laminate was both in the circumferential as well as in the axial direction.

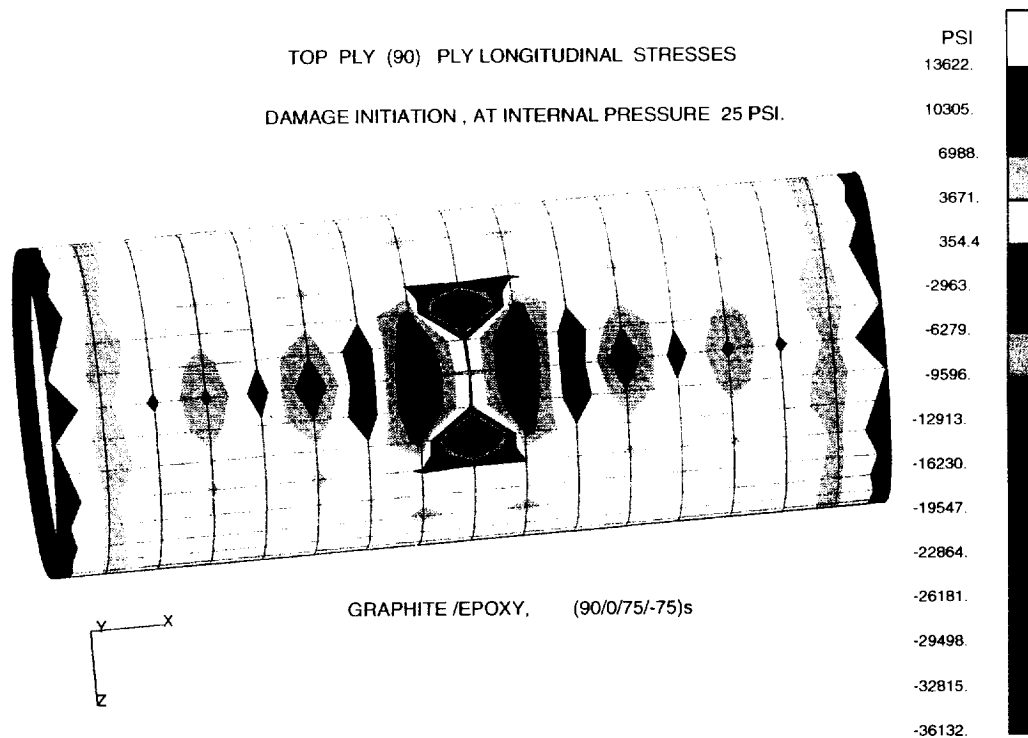


Fig. 15. At the top ply (90°), ply longitudinal stresses at 0.17 MPa (25 psi).

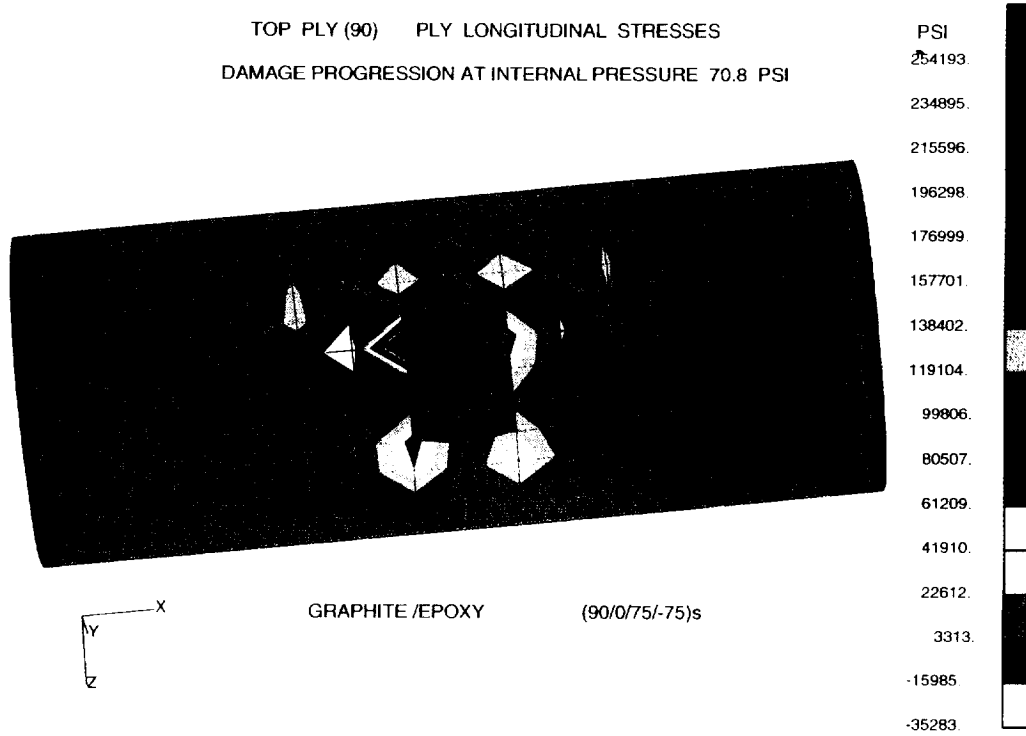


Fig. 16. At the top ply (90°), ply longitudinal stresses at 0.49 MPa (70.8 psi).

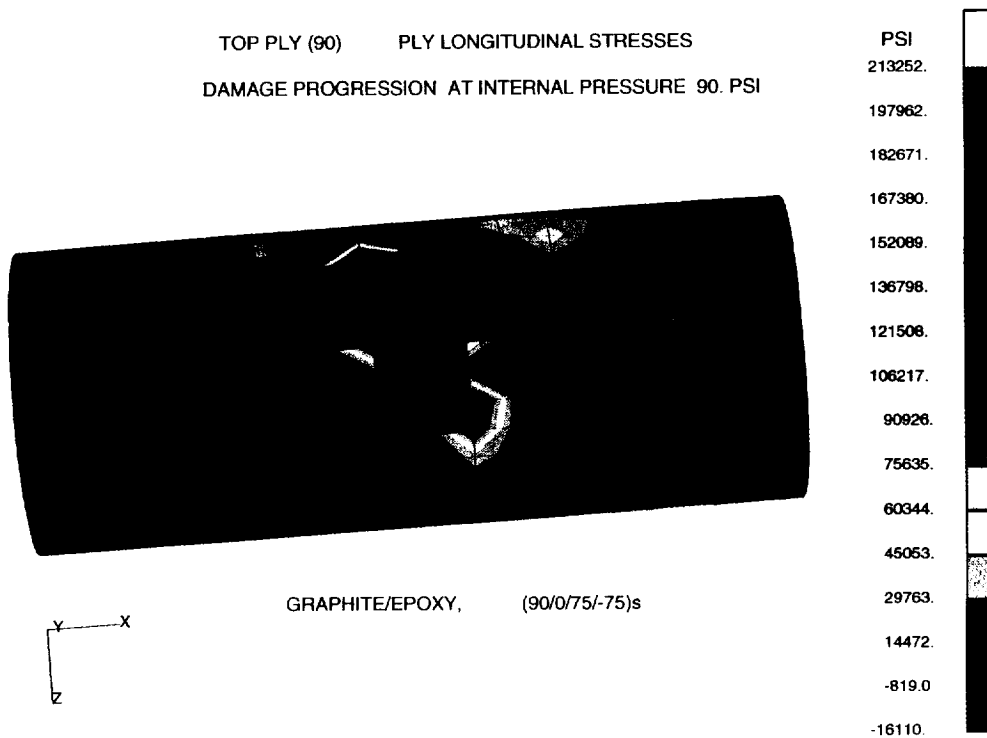


Fig. 17. At the top ply (90°), ply longitudinal stresses at 0.62 MPa (90 psi).

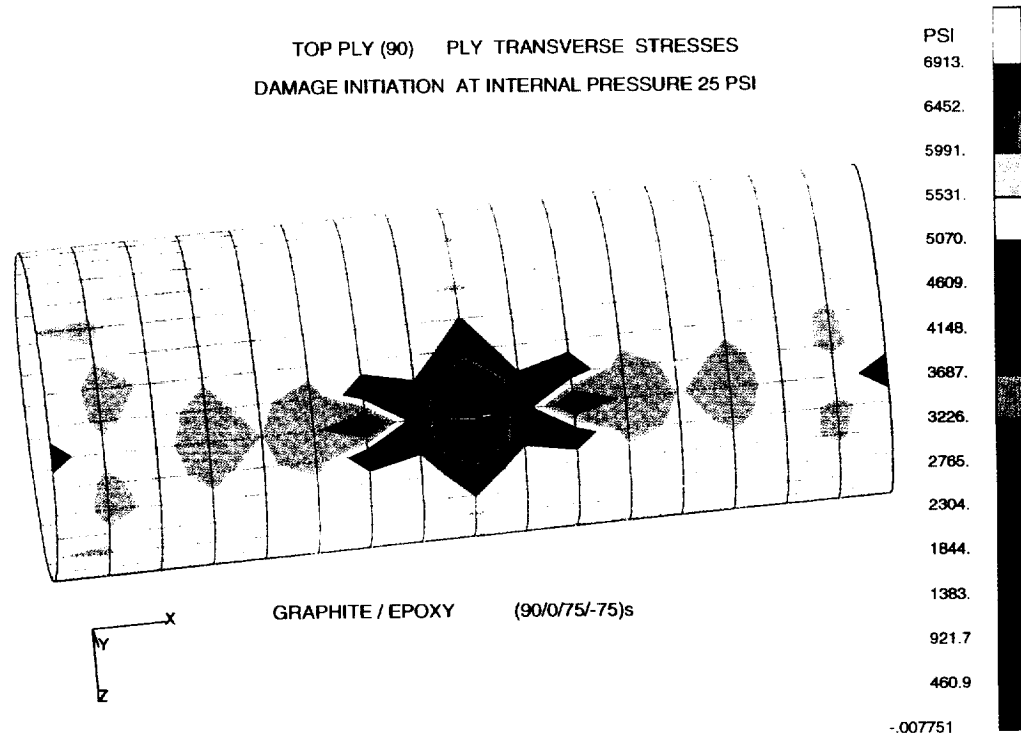


Fig. 18. At the top ply (90°), ply transverse stresses at 0.17 MPa (25 psi).

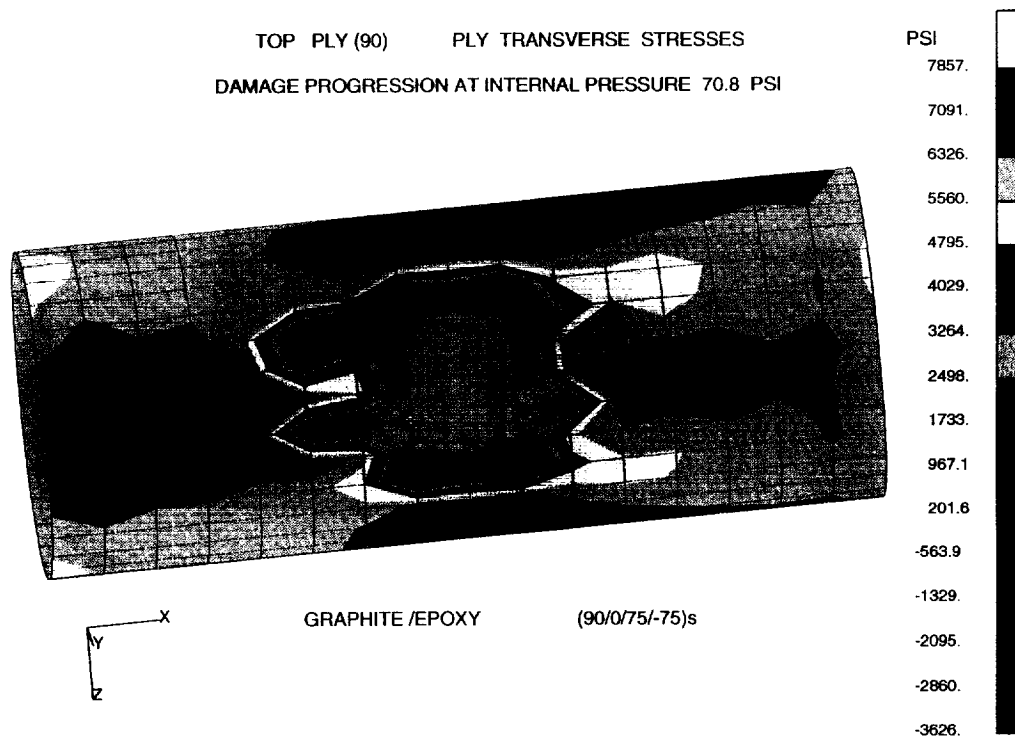


Fig. 19. At the top ply (90°), ply transverse stresses at 0.49 MPa (70.8 psi).

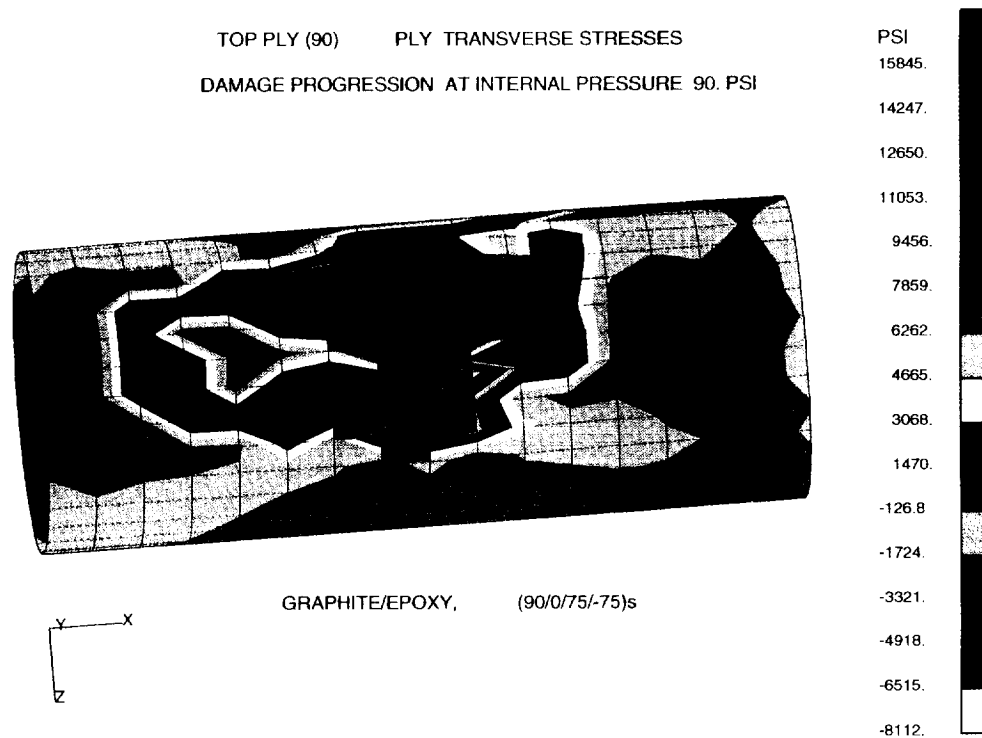


Fig. 20. At the top ply (90°), ply transverse stresses at 0.62 MPa (90 psi).

The fracture progression of the (90/0/±75) thin shell structure is depicted in Figs. 9–14, for different load increments. At the top ply (90°), the ply longitudinal stresses (in the hoop direction) are plotted in Figs. 15–17; and the ply transverse stresses (in the axial direction) are plotted in Figs. 18–20 for different load increments. At the damage initiation stage high ply stresses were developed at the edges of the crack, and when the fracture progressed the distribution of the ply stresses around the fractured area changed and decreased.

## 5. Summary

In this investigation, the simulation of the structural and damage progression response of a (90/0/±75), composite thin shell structure was examined. The damage progression of the (90/0/±75) laminate was compared with the (90/0/±θ), (for θ = 45 and 60) layup configurations. The significant results are as follows:

(1) For the case of the defect free (90/0/±75) thin shell structure damage initiation started at internal pressure 0.14% of the burst pressure 7.83 MPa (1.1 psi) with matrix cracking at the outermost ply 2 (0°) and followed by the same type of failure at the plies 3 (75°), 7 (0°) and 8 (90°). The damage progressed and when fiber fracture occurred at the outermost ply 2 (0°) rapid fracture initiated and collapse of the structure occurred at 0.717 MPa (0.104 psi).

(2) For the case of the defected (90/0/±75) thin shell structure, the damage initiation started at internal pressure of 0.24% of the burst pressure 0.717 MPa (0.104 psi), with matrix cracking at the plies near the nodes of the crack tips (hoop and the axial directions nodes). Increasing the applied pressure, the fiber fracture progressed in the hoop direction at a faster rate than in the axial direction, until the collapse of the structure.

(3) Comparing the defected with the defect free thin shell structure, it was observed that damage initiation started at 0.16% of the defect free thin shell

pressure 1.06 MPa (0.153 psi), while burst pressure occurred at 0.991% of the defect free thin shell pressure 7.83 MPa (1.13 psi).

(4) The direction of damage growth for the (90/0/±75) laminate was mainly in the circumferential direction of the defected shell. This laminate was the least damage tolerant of the two compared defective shells with (90/0/±45) and (90/0/±60) layup configurations.

(5) The direction of damage growth for the (90/0/±45) laminate was mainly in the axial direction of the defective shell, had significant damage tolerance and sustained the maximum amount of damage prior to bursting.

(6) The direction of damage growth for the (90/0/±60) laminate was both in the circumferential as well as in the axial direction of the defected shell. This laminate was able to sustain the highest burst pressure. However, the amount of damage sustained was lower than that corresponding to the (90/0/±45) laminate.

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