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A Presentation on Robust Flutter Margin Analysis and a Flutterometer

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ABSTRACT

This paper documents an invited presentation given to The Boeing Company, Seattle, Washington on September 9, 1997. The audience consisted of structural dynamic and flight test engineers from the Boeing Commercial Airplane Group who were interested in discussing research which may be applied to future flight flutter test programs. A method to compute robust flutter margins is described which is a significant departure from traditional methods. This method uses the structured singular value, μ , to compute a flutter margin which directly accounts for modeling errors such that a worst-case flutter margin is computed with respect to those errors. This method may be applied in several ways. A post-flight application uses data sets from multiple test points to compute sflutter margins at each test point to track the flutter margins during a flight test. This on-line implementation is the basis for a flutterometer flight test tool that displays the distance to flutter at a given test point. Such a tool was not previously possible using traditional flutter flight test analysis methods. The F/A-18 System Research Aircraft was used to demonstrate these applications using flight data recorded from test points throughout the flight envelope.

NOMENCLATURE

С	damping matrix
Κ	stiffness matrix
М	mass matrix
Р	plant transfer function
\mathcal{P}	set of plant transfer functions
$ar{q}$	dynamic pressure
Q	unsteady aerodynamic force matrix
<i>S</i>	Laplace variable
β	pole in Padé approximation to a lag
$\delta_{ar{q}}$	perturbation to dynamic pressure
Δ	uncertainty operators
Δ	set of uncertainty operators
$\Delta_{m eta}$	uncertainty in β
η	state vector
μ	structured singular value
#	set of stable, linear time-invariant transfer functions
\mathcal{L}_{2}	set of finite square-integrable measurements



The structural dynamics group at NASA Dryden Flight Research Center has been actively involved in this research project for some years. The diversity of the team enables significant research issues to be addressed by engineers with specialization in that area.



There are several refereed publications which discuss aspects of the method for robust flutter margin analysis. The NASA Technical Paper, which is expected to appear in early 1998, is the most detailed and complete reference document.



This presentation has essentially three large sections. Some initial comments are given to briefly discuss flutter analysis issues and provide the motivation for this research. The main section introduces the method for flutter analysis, called the μ method, which produces robust flutter margins. This portion of the presentation details the issues of robustness and demonstrates their applicability to flutter analysis. The other large sections describe implementations of the μ method and demonstrate these implementations on the F/A-18 Systems Research Aircraft. The first implementation is a post-flight analysis which computes worst-case flutter margins to define a flight envelope. The second implementation is the on-line tracking of robust flutter margins via the flutterometer concept.



The procedures for flight flutter testing to clear a flight envelope are fairly standard throughout NASA and the flight test community, although implementation details vary widely between organizations. Response data is recorded from the aircraft at a stabilized test point and telemetered to the control room. The data is analyzed using strip chart monitoring and several computational algorithms in both the time and frequency domains. Estimates of the modal damping ratios and trends for those ratios as the envelope is expanded are used to determine the next suitable test point which does not incur an excessive level of risk.



NASA Dryden Flight Research Center is researching methods to improve flight test efficiency. Increasing efficiency implies reducing time and cost along with maintaining a high level of safety for the aircraft and crew. The entire scope of flight flutter testing is being investigated. The first step in the process investigates better signals and mechanisms to excite the aircraft and improve the dynamics observed with response data. An RBNB concept is being implemented to distribute this data to a variety of analysis facilities. Improved signal processing algorithms such as wavelet filtering are being utilized to accurately process transient response data. The last step in the process is to analyze this data to produce a confident flutter margin rather than the damping estimate which is currently computed. This last step is the focus of this presentation and is addressed by a parameter called μ .



These research areas are all steps towards the concept of a flutterometer which was envisioned in the 1980's at NASA Dryden Flight Research Center. This flutterometer is a flight test tool that indicates some measure of distance to a flutter condition. The center box in the dial present the altitude at which flutter occurs. The values along the dial present the difference between that altitude and the current altitude at which the aircraft is flying.

The type of measure, such as altitude or dynamic pressure or airspeed, can be selected to match units desired by the pilot or engineer. The main point is this tool provides a quantitative value of the flight conditions at which flutter occurs. This tool can drastically increase flight test efficiency since test points can be safely chosen with greater rate of expansion of the flight envelope.



This flutterometer concept can not be effectively implemented using any current flutter analysis method. One explanation for this is seen by dividing all current methods into two basic categories called Analytical Prediction methods and On-Line Estimation methods. The Analytical Prediction methods, of which the *p-k* method is the most common, utilize a computational model with no direct consideration of flight data. The On-Line Estimation methods, of which tracking damping estimates is the most common, utilize the flight data alone. Each of these methods has strengths and weaknesses that are directly related. The drawbacks to the Analytical Prediction methods are eliminated by the On-Line Estimate methods; however, the On-Line Estimate methods introduce their own drawbacks which are not problematic for Analytical Prediction methods.



The most common methods of flutter analysis, namely the analytical p-k method and the on-line estimation of damping, have been recognized as deficient for many years. Several new methods are being investigated by various researchers to replace these traditional methods. These new methods still fall into the two basic categories and thus have the same strengths and drawbacks. These are additional limitations that should also be considered for these new methods.



NASA Dryden Flight Research Center is developing a novel method for flutter analysis that combines the strengths of both categories of traditional flutter analysis. This method is essentially model based so it has the desired predictive nature of an Analytical Prediction method; however, this method, unlike traditional Analytical Prediction methods, can also utilize the flight data to obtain the desired accuracy of the On-Line Estimate methods. This method, referred to as the μ method, introduces a new category of analysis called Flight Test Prediction methods.



The μ method is able to make strong claims about robustness by utilizing a well developed mathematical framework. The underlying concepts are derived from functional analysis and introduce abstractions such as \mathcal{H}_{∞} operators and \mathcal{L}_2 signals. These abstractions are readily interpreted as standard systems concepts such as transfer functions and data measurements. The Linear Fractional Transformation is used to represent series and feedback operators in a single unified framework. The concept of a set of plants, denoted $F_u(P,\Delta)$, will be used extensively throughout this presentation and refers to the block diagram in the Figure.



The concept of robustness is frequently used in engineering terminology to loosely refer to stability and performance of a system despite some concept of perturbations. The μ framework utilizes a formal definition of robustness and associated perturbations. The perturbations are represented by a set of norm bounded operators, Δ , which affect the plant, P, through a feedback relationship using the LFT framework. This uncertainty can be parametric uncertainty which affect specific elements of a system or general dynamic uncertainty which affects groups of signals.



The formalized concept of robustness ensures the plant will be stable for any perturbation operator Δ contained within the set Δ . This concept is directly related to the concept of a stability margin. The structured singular value, μ , is defined as a necessary and sufficient condition to exactly compute the robustness of a plant operator. μ can be interpreted as a multivariable gain and phase margin but perhaps the most straightforward interpretation is that of the smallest destabilizing perturbation. The plant is usually weighted such that the set of uncertainty operators has a unity norm bound and the desired robustness condition is μ =1.



A difficulty in using μ to compute robust stability lies in choosing a set of meaningful uncertainty operators. Model validation algorithms are formulated to address this issue by comparing measured data to the set of plants generated by $F_u(P,\Delta)$. The model validation criterion determines there exists some Δ in the set Δ such that the plant $F_u(P,\Delta)$ could have generated the measured data. This criterion actually ensures the model is not invalidated since a model can never by truly validated by a finite set of data; however, even this restricted condition is useful to ensure the uncertainty set is reasonable.



A approach to model validation in the μ framework is developed using frequency domain transfer function data. The basic concept considers upper and lower bounds for the set of plant models with uncertainty and determines if the measured transfer function lies within those bounds. This approach uses a simple test at each frequency point without requiring estimates of specific system and modal parameters.



 μ was originally developed for control design and analysis and is a well-known concept in that field of engineering. NASA Dryden Flight Research Center is developing applications of μ for aeroelasticity research and has found several interpretations for this field. μ can be formulated to compute a flutter margin which is similar to that generated by traditional analysis methods such as the *p*-*k* method. μ can also represent a robust flutter margin that considers the worst-case flutter margin with respect to modeling errors and perturbations represented by the set Δ .

 μ can be especially valuable for flutter analysis. The confidence in the computed flutter margins are high due to the inclusion of flight data which describes the true aircraft. The formalized derivation of μ lends some mathematical guarantees that the computed robust margins are worst-case with respect to a set of perturbations. Also, μ is continuous and smooth with flight condition variation so replaces the poorly behaved nonlinear damping trend parameter to track during a flight test.



The first step in developing the μ method is to generate flutter margins which are equivalent to traditional margins generated by the *p*-*k* method. These margins do not account for any uncertainty and are denoted as nominal margins in the μ vernacular. μ is formulated as a flutter margin by considering the smallest destabilizing perturbation to a flight condition.



The equations of motions for an aeroelastic system utilize a structural model and an unsteady aerodynamic force model. The unsteady aerodynamic forces can be represented as a finite-dimensional state-space model using several standard algorithms.



The dynamic pressure effects the equations of motion in a linear manner so perturbations to this flight condition parameter may be easily represented with a feedback operator. The basic procedure is to isolate the perturbation from the known nominal dynamics and replace this perturbation with a norm bounded operator.



\$\mu\$ computes a flutter margin for the nominal system by considering the smallest perturbation to dynamic pressure which causes an instability. Considering all perturbations to dynamic pressure allows μ to extrapolate to the flutter boundary from a particular stable flight condition. The nominal margins computed with the μ and *p*-*k* methods should be similar since both methods utilize the same theoretical aeroelastic model with no accounting for modeling errors.



The μ method truly becomes a unique valuable tool for flutter analysis by accounting for modeling uncertainty. This uncertainty is essential since the nominal model is never exactly accurate so the flutter margins computed with that nominal model may be arbitrarily different than the margins of the true aircraft. The basic procedure for including uncertainty is to introduce feedback operators to appropriate elements of the system and utilize the LFT framework to express an uncertain plant model comprised of a nominal plant model and a single structured uncertainty set. A process iterating between adjustments to norm bounds on the uncertainty and computations of μ can be used to compute a flutter margin associated with the desired μ =1 condition.



An example of modeling uncertainty arises when considering aerodynamic lag from a Pade approximation. These lag terms may have slight errors so a perturbation can be introduced to account for the errors. The perturbation can be separated from the nominal dynamics and extracted as an uncertainty operator introduced in a feedback manner.



All the individual uncertainty operators, such as the lag uncertainty, are combined into a single structured uncertainty operator using the LFT framework. The nominal flutter margins are computed by considering the smallest destabilizing perturbation to dynamic pressure that causes an instability in the nominal plant P. The robust flutter margins are computed by considering the smallest destabilizing perturbation to dynamic pressure that causes an instability in the nominal plant P. The robust flutter margins are computed by considering the smallest destabilizing perturbation to dynamic pressure that causes an instability in the set of plants $F_u(P,\Delta)$.



The robust flutter margin concept seems a significant departure from traditional flutter margins; however, the robust flutter margin can be interpreted in terms of nominal flutter margins. A unique plant model is obtained for each uncertainty operator in the set and a nominal flutter margin can be computed for each of these unique plant models. The robust flutter margin is simply the smallest margin of these individual margins. The operator theory and functional analysis concepts are introduced to ensure the robust flutter margin analysis considers all uncertainty operators in the set.



Flight data provides the only true indication of the aircraft properties and should be included in the flutter margin analysis. The optimal approach would use this data to directly identify parameters in the model and an associated uncertainty set but this is extremely difficult. Approaches to utilize the data to identify a plant model are valuable but problematic since they are unreliable with poor quality data. The approach investigated at NASA Dryden Flight Research Center is to utilize the flight data to identify the errors and uncertainty in a theoretical plant model.



There are several advantages to using flight data to compute the uncertainty description as compared to identifying plant model parameters. One main advantage is the ability to utilize data with varying levels of noise. Another advantage, which will be utilized for the on-line implementation, is the ability to account for time-varying dynamics of the airplane.



An uncertainty description must be chosen that is a reasonable indication of modeling errors. This implies a tradeoff must be met between choosing Δ large enough to account for all errors but choosing Δ small enough to reduce conservatism in the robust margins.



The μ method can be formulated using a theoretical plant model and measured flight data. The theoretical plant model is assumed to be the best estimate of the aircraft dynamics so this model is not changed throughout the analysis. The flight data is incorporated entirely through the uncertainty operators. μ computes a flutter margin for the theoretical plant that is worst-case with respect to the uncertainty and thus is worst-case with respect to the observed flight data.



There are many sources of uncertainty in a plant model. The obvious sources are errors in the theoretical plant dynamics arising from inaccuracies in the structural and aerodynamic models. Utilizing flight data to validate the model introduces additional uncertainty since the data measurement and processing may not be accurate. Also, the aircraft may display behaviors for which the measured excitation signal does not account.



There are several desirable properties of μ that make this parameter an advantageous flutter margin as compared to damping. μ presents more information than damping since the conservatism between the robust and nominal margins is an indication of modeling sensitivity. Most importantly, μ is a stability predictor and extrapolates to an unstable flight condition whereas damping is merely a stability indicator and is only truly informative at the point of instability.



The μ method is a powerful tool for flutter margin analysis but it is only useful when its limitations and difficulties are understood. This method is limited to applications of analyzing stability of aircraft with a plant model comprised of linear operators. The main difficulty lies in choosing the uncertainty description. μ is directly related to this uncertainty description so the robust flutter margin may be meaningless if the uncertainty description is meaningless.



The μ method, despite its limitations and difficulties, can be effectively applied to many aircraft applications. This method is ideal for considering several variations and configurations of an aircraft that only slightly perturb the nominal model. This method is also ideal for analyzing aeroservoelastic stability since it is a trivial extension to include a controller in the formulation and consider the closed-loop dynamics.



The μ method can be utilized for post flight data analysis to compute worst-case flutter margins and determine a worst-case flight envelope. The conservatism between the robust and nominal margins demonstrates the sensitivity of the model and may indicates areas of the flight envelope for which more data should be generated due to dramatic differences between the theoretical nominal and flight derived robust margins.



There are several approaches that may be used for deriving an uncertainty description from multiple sets of flight data. This uncertainty description is formulated as a function of Mach number to associate with each plant model describing the dynamics at each Mach number. A robust flutter margin is computed for the associated plant and uncertainty models at each of these Mach numbers and the worst-case flight envelope is computed with respect to both dynamic pressure and Mach flight conditions.



The choice of which data sets to analyze affects the uncertainty description. A local approach generates an uncertainty description for the plant at a particular Mach number by only considering flight data measured at that Mach number. A global approach considers all sets of flight data and generates a single uncertainty description that is worst-case with respect to variations observed throughout the flight envelope. A hybrid approach can be used to group sets of flight data together by assuming certain Mach numbers at certain test points, such as subsonic flight conditions, are strongly related to each other but not to other flight regions.



Post flight analysis is used to compute worst-case flutter margins for the F/A-18 Systems Research Aircraft (SRA). This aircraft is an excellent application for this method since a well-developed theoretical model is available along with a complete set of nominal p-k flutter margins.



The F/A-18 SRA is also an excellent application since a large database of flight data has been recorded in response to a set of wingtip exciters. The test points for these response measurements cover a large range of flight conditions throughout the flight envelope.



The state-space model for this system includes 34 modes from the structural model and 84 states accounting for the unsteady aerodynamic forces. There are 5 accelerometers measurements on each wingtip of the aircraft with a measurement of excitation force on each wingtip.



Areas of modeling uncertainty can be seen by visually inspecting some flight data sets. The top plot demonstrates two flight data transfer functions taken at identical flight conditions. These transfer functions show a small variation of approximately .4 Hz in the modal natural frequency of the Wing 1st Bending mode. The bottom plots demonstrate the concept of nonrepeatibility that affects flight flutter testing. These two plots show transfer functions generated by response data at identical flight conditions for which the modal frequencies and levels displayed are clearly different.



An uncertainty description is chosen for the F/A-18 SRA based on the observed flight data variations. A parametric modal uncertainty operator is chosen to introduce 5% uncertainty in natural frequencies, 15% uncertainty in damping ratios and 15% uncertainty in aerodynamic lags. A complex dynamic input multiplicative uncertainty is included to introduce 10% uncertainty at low frequencies and increasing to demonstrate the model is poor at high frequencies. Sensor noise is included along with the perturbation to dynamic pressure that allows μ to extrapolate to the flutter margin.



The initial calculation of flutter margins considers only the nominal plant dynamics with no consideration of the uncertainty description. This plot shows the *p-k* margins as solid lines and the nominal μ margins as circles. These values are quite similar to indicate the μ method can accurately compute flutter margins. The frequencies of each unstable flutter mode are not given on this plot but are shown in the published reference documents to match closely.



Robust flutter margins are computed for the symmetric modes using μ with respect to the uncertainty description. The dashed line indicates these worst-case margins which are more conservative and closer to the flight envelope than the nominal margins. The robust flutter margins at transonic flight conditions are particularly conservative.



Robust flutter margins are also computed for the antisymmetric modes and are shown by the dashed line in this plot. These margins show a similarity to the symmetric mode margins in that the transonic flight condition is especially sensitive to modeling uncertainty.



The entire set of robust flutter margins can be considered by evaluating the margins for the symmetric and antisymmetric modes. These margins, despite the conservatism associated with including uncertainty, are more than 15% in airspeed from the flight envelope of the F/A-18 SRA.



The μ method for flutter analysis is extended to an on-line implementation by considering a test point approach. Flight data is gathered at each test point and immediately used to generate an uncertainty description and an associated robust flutter margin. The robust flutter margin information at each test point is displayed via the flutterometer tool which indicates the distance to flutter for that test point. This approach allows the flutterometer to track time-varying dynamics of the airplane since the uncertainty description is continually updated as flight data is measured and the μ margin accounts for the time-varying dynamics through this time-varying uncertainty.



The μ method can be implemented in a manner similar to computing damping estimates. The flight data can be simultaneously analyzed by traditional methods and the μ method on separate computers. The flight conditions for the next test point can be determined using the combination of information from the traditional damping estimate and the new μ method.



The choice of flight data to utilize at each test point allows flutter margins to be computed which are worst-case with respect to different uncertainty operators. A local approach uses only data from the current test point while a global approach uses all data from previous test points. A hybrid approach uses a forgetting factor and only uses data from recent test points.



The flutterometer based on the μ method can be easily implemented using current flight flutter test procedures. The only change is an additional analysis operation using the recorded flight data that computes a robust flutter margin. The resulting decision on future test points is considered confident since the damping estimates are accurate indicators of the current stability properties and the μ method provides significant additional information about the distance to a flutter instability.



A simulated flight flutter test of the F/A-18 SRA demonstrates the flutterometer concept. The aircraft is undergoing a constant Mach dive at M=1.2 to expand the envelope. Test points are chosen at every 100 units of dynamic pressure to illustrate the on-line computations with some detail. The time spent at each of these test points is determined entirely by the amount of computation time required to compute an uncertainty description and an associated robust flutter margin with μ . This plot shows the value of dynamic pressure throughout the simulation with the length of the horizontal lines indicating the time spent at a test point for which the flight condition did not change while μ is being computed.



A time-varying theoretical plant model of the F/A-18 SRA is used as the true plant model while a variation of this model is used as the nominal dynamical model. The nominal model has an error in structural damping and does not account for the time-varying mass of the true aircraft. The plot shows the increase in modal damping uncertainty that is required throughout the simulation to ensure the flight data recorded at each test point does not invalidate the uncertain model.



The top plot shows the true and computed flutter margins for each test point. The dashed line is the flutter margin of the true aircraft and decreases with time due to the time-varying mass of the aircraft. The solid line displays the robust flutter margin and also demonstrates a time-varying behavior due to the calculation of an uncertainty description and μ at each test point. This robust flutter margin utilizes uncertainty to account for the time-varying mass and remains conservative to the true flutter margin throughout the simulation. The dotted line near the top of the plot is the nominal flutter margin which does not account for any uncertainty in the nominal model.

The bottom plot shows the modal damping ratio at each test point for the mode that goes unstable at the M=1.2 flight condition. The damping remains fairly constant until minute 17 when it decreases sharply to indicate the oncoming instability.



These plots demonstrate the information displayed in the control room at the minute 17 test point. The flutterometer on the left indicates the aircraft can drop 7500 feet before a flutter condition is encountered. The damping trend on the right indicates an instability may be near but the flight conditions associated with that instability can be not accurately determined from this trend. These plots clearly show the usefulness of a valid flutterometer tool for flight flutter testing.



This simulation uses standard hardware and software often available in a flight data analysis facility. The computational time required at each test point is reasonable and does not introduce an excessive burden on a flight test program. The plot uses a star symbol to indicate the CPU time required at any test was not greater than 180 seconds.



The flutterometer tool is based on the μ method and has the same limitations and advantages as the μ method with several additional considerations. This tool is only directly applicable for flight programs using stabilized test points that can vary dynamic pressure while keeping Mach constant. The flutterometer can be extremely useful if these limitations are not problematic since the time-varying flutter margins can be tracked and μ is a much better behaved stability parameter than damping.



The μ method is a significant improvement to traditional flutter margin analysis methods since it directly accounts for modeling uncertainty by including flight data. This method can be used in several ways including an on-line implementation to develop a flutterometer flight test tool. This flutterometer can improve flight test efficiency by providing a confident measure of the distance to flutter so test points can be chosen that quickly and safely expand the flight envelope.



There are several research extensions to the μ method that are under investigation. The computation of aeroservoelastic stability margins is performed for an F/A-18 aircraft and results will be published in the 1998 AIAA SDM conference. Methods of reducing the conservatism in the robust margins are being considered using techniques such as wavelet filtering and model updating. The μ method is being extended to account for nonlinear limit cycle oscillations by including nonlinear operators in the LFT framework. Also, the μ method is being applied to several flight test programs to validate and improve the implementation issues.



The μ method is being applied to several small order testbed systems. These systems can be flown at the flutter boundary to ensure the flutterometer predicts the unstable flight conditions.



The μ method is also being considered for several aircraft flight flutter test programs. The cost of these programs could be dramatically reduced with even a small increase in flight test efficiency using the flutterometer.



μ Method : Discussion Topics (Boeing)

• Control room issues

NASA

- Hardware and software requirements
- Interaction with other Boeing tools and procedures
 - Work level of the user during a flight test
- Utilizing flutterometer
 - Availability of algorithms
 - Cost and effort to develop and implement
 - External funding possibilities and interests

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