Quasi-Steady Acceleration Direction Indicator in Three Dimensions

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IN THREE DIMENSIONS

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ABSTRACT

Many materials processing and fluids physics experiments conducted in a microgravity environment require knowledge of the orientation of the low-frequency acceleration vector. This need becomes especially acute for space experiments such as directional solidification of a molten semiconductor, which is extremely sensitive to orientation and may involve tens of hours of operations of a materials furnace. These low-frequency acceleration data have been measured for many Shuttle missions with the Orbital Acceleration Research Experiment. Previous attempts at using fluid chambers for acceleration measurements have met with limited success due to pointing and vehicle attitude complications. An acceleration direction indicator is described, which is comprised of two orthogonal short cylinders of fluid, each with a small bubble. The motion and the position of the bubble within the chamber will indicate the direction of the acceleration experienced at the sensor location. The direction of the acceleration vector may then be calculated from these data. The frequency response of such an instrument may be tailored for particular experiments with the proper selection of fluid and gas parameters, surface type, and geometry. A three-dimensional system for sensing and displaying the low-frequency acceleration direction via an innovative technique described in this paper has advantages in terms of size, mass, and power compared with electronic instrumentation systems.

Glossary of Terms

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>D</td>
<td>characteristic length</td>
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<tr>
<td>g</td>
<td>acceleration magnitude</td>
</tr>
<tr>
<td>R_c</td>
<td>chamber radius</td>
</tr>
<tr>
<td>R_b</td>
<td>bubble radius</td>
</tr>
<tr>
<td>r</td>
<td>radial position of bubble</td>
</tr>
<tr>
<td>R_e</td>
<td>Reynolds number</td>
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<tr>
<td>R'</td>
<td>radial position of bubble center at wall, ( R' = R_c - R_b )</td>
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<tr>
<td>U</td>
<td>characteristic velocity</td>
</tr>
<tr>
<td>V_b</td>
<td>bubble velocity</td>
</tr>
<tr>
<td>V_{bt}</td>
<td>bubble terminal velocity</td>
</tr>
<tr>
<td>\nu_f</td>
<td>kinematic viscosity of liquid</td>
</tr>
<tr>
<td>\alpha</td>
<td>acceleration angular direction change, ( \alpha =</td>
</tr>
<tr>
<td>\beta</td>
<td>angle at which freely moving bubble is constrained by the chamber wall</td>
</tr>
<tr>
<td>\theta_b</td>
<td>angular position of bubble</td>
</tr>
<tr>
<td>\theta_i</td>
<td>initial position of bubble</td>
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<tr>
<td>\theta_f</td>
<td>equilibrium position of bubble</td>
</tr>
<tr>
<td>\mu_f</td>
<td>dynamic viscosity of liquid</td>
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<tr>
<td>\rho_b</td>
<td>density of bubble</td>
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<tr>
<td>\rho_f</td>
<td>density of liquid</td>
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INTRODUCTION

The microgravity acceleration environment can be captured in its full richness and complexity using a variety of acceleration instruments. But while microgravity acceleration data are essential to virtually every space experiment, each individual experiment may only require a subset of that complete data set, such as detailed acceleration magnitude data in particular frequency bands. For problems such as directional solidification of a semiconductor, the orientation of the net acceleration vector relative to the sample is critical. Off-axis orientation of the acceleration can give rise to substantial convective flow due to the large density gradients in the melt. For this problem in a space laboratory under normal operating conditions, knowledge of the orientation of the acceleration with respect to time may be of more importance than the magnitude.

The proposed Quasi-steady Acceleration Direction Indicator device will provide such data in real time with low power requirements, low mass, small volume, and low cost.
PREVIOUS SYSTEMS

The Passive Accelerometer System\(^1\) flown on USML-I used a spherical ball in a fluid-filled long cylinder to measure the acceleration magnitude based on the ball’s speed through the chamber. Limitations of restricted vehicle attitude and constrained instrument pointing have made this device difficult to use for long periods of time. Since this instrument was pointed manually by the crew, the vehicle attitude stability was important. If the vehicle attitude changed, the device had to be re-aligned manually by the crew.

For some materials processing experiments\(^2\), the axial to normal acceleration ratio was used as a measure of the quality of the microgravity environment for the experiment.\(^3\) The axial to normal acceleration ratio is the ratio of the component of the acceleration vector aligned with the long axis of the sample (the axial component) to the component of the acceleration vector acting perpendicular to the sample’s long axis (the normal component). The goal during experiment operations was to maximize the axial to normal ratio, which is to say that the quasi-steady acceleration is more aligned with the sample. On several Shuttle microgravity missions, Principal Investigators requested that the attitude of the Shuttle be established in such a way as to maximize this ratio during experiment operations.

INSTRUMENT DESIGN

The Quasi-steady Acceleration Direction Indicator is comprised of two short, orthogonal, right-cylindrical chambers filled with a fluid, figure 1. Inside the liquid is a small bubble with a volume of approximately 5%, relative to the chamber volume. When exposed to the microgravity environment, the bubble’s position within the chamber is controlled by the quasi-steady acceleration and fluid wall effect forces.

The frequency response of the bubble motion is dependent on the fluid viscosity, relative bubble size, and the chamber depth vs. width ratio.

ANALYSIS OF BUBBLE MOTION IN MICROGRAVITY

To investigate the response of the Quasi-steady Acceleration Direction Indicator, a step change in the orientation of acceleration is considered. With such a change, there are three modes of motion of the bubble from an initial location to a final, stable location. The first path is a constrained motion along a curved wall, figure 2. The second path is illustrated by path 1 of figure 3 as a free motion through the liquid without being constrained by the walls. The third is a combination of constrained and free motion, paths 1 and 2 of figure 3.

Several assumptions made for a numeric model of the Quasi-steady Acceleration Direction Indicator are:

1) the Reynolds number remains much less than one, \( R e \ll 1 \), where \( R e = (UD)/v_f \).
2) the bubble remains spherical,
3) the magnitude of the acceleration remains roughly constant, and
4) the effects of liquid flow driven by the chamber walls and any surface tension effects at the wall are ignored.

Performing a force balance for the bubble leads to an expression for the acceleration of the bubble when exposed to an acceleration, \( g \).

\[
\frac{dV_b}{dt} = g - \frac{1}{\rho_b R_b^2} \frac{3 \mu_f V_b}{\rho_f} \frac{\Delta t}{V_b} \quad (1)
\]

At the terminal velocity, \( V_{bt} \), acceleration and drag forces balance, so that

\[
\frac{dV_b}{dt} = 0.
\]

The terminal velocity is then

\[
V_{bt} = \left( \frac{R_b^2 g}{\rho_f} \right) \cdot (2)
\]

For this configuration and velocity,

\( Re = 10^{-4} \ll 1 \).

Therefore, in a step-wise calculation with \( n \) denoting an iteration number, the velocity is given by

\[
v_b^n + \Delta t = \min(v_b^n + \frac{dV_b^n}{dt} \Delta t, V_{bt}) \quad (3)
\]

We have based our calculations on an off-the-shelf fluid level sensor. The chamber, of radius \( R_c = 1.3 \text{ cm} \), is filled with water and an air bubble with a radius \( R_b \) of approximately 3.5 mm. The system is subjected to an acceleration of 1 \( \mu g \) with various step changes in orientation. For a bubble which is free within the fluid, the bubble achieves 99% \( V_{bt} \) at about 0.02 sec. after having traveled 0.00007 cm. The time step chosen for the calculations presented below was 0.1 milliseconds. A free bubble in the chamber may travel as far as \( 2R' = 1.9 \text{ cm} \), which requires 468 seconds. In many
typical scenarios, the freely moving bubble will be moving through the fluid at terminal velocity.

**Constrained bubble motion**

When motion of the bubble is constrained by the wall, the position of the bubble is shown in figures 2 and 4 and defined by:

\[ r = R' = R_c - R_b \]  
and  
\[ |\alpha| = |\theta_f - \theta_i| \leq \frac{\pi}{2}. \]

Only the tangential acceleration component drives the bubble motion, so that the \( g \) in equations (1) and (2) is reduced to the tangential component, \( g \cdot \sin(\theta_f - \theta_b) \).

The new bubble position after a small time increment, \( \Delta t \), is:

\[ r_b^{n+1} = R' \]  
\[ \theta_b^{n+1} = \theta_b + \frac{v_{b}^{n+1} \Delta t}{R} . \]

In cartesian coordinates, the position is given by:

\[ x_b = (R' \cos \theta_b^{n+1} - R' \sin \theta_b^{n+1}), \]  
\[ y_b = \frac{v_b^{n+1} \Delta t}{R}. \]

The effect of the wall is clearly evident in figure 5 for \( \theta_f - \theta_i = \pi/2 \), which shows the azimuthal position of the bubble as a function of time. The tangential acceleration component decreases towards zero as the bubble approaches its equilibrium position, resulting in an asymptotic approach to \( \theta_f \). The bubble reaches 99% \( \theta_f \) in about 1648 seconds. We expect that, on the International Space Station, the change in quasi-steady acceleration over an orbit of approximately 5400 seconds will be no more than 54 degrees and most likely significantly smaller. Moreover, the quasi-steady acceleration variation is much more gentle than the case considered here. For \( \theta_f - \theta_i = 54 \) degrees, the bubble reaches 99% of its equilibrium position at 1489 seconds (which may be a needlessly conservative estimate). For step changes on the order of 10 degrees, the response time is reduced to 1078 seconds.

**Free bubble motion**

For a bubble away from the chamber wall, the bubble motion direction is determined by the acceleration vector direction.

For a bubble against the chamber wall at the initiation of an acceleration step change with \( \pi / 2 < |\alpha| \leq \pi \), the bubble moves away from the wall and continues freely through the liquid until contacting the wall again. Free motion through the liquid means that one of the following is true:

\[ r < R' = R_c - R_b \]

or

\[ \frac{\pi}{2} < |\alpha| < \pi . \]

The distance travelled by the bubble over a time step, \( \Delta t \) is:

\[ d(n+1) = v_b^n \Delta t. \]

The coordinates for the new bubble position are given by:

\[ x_b^{n+1} = x_b^n + d \cos(\theta_f - \theta_b^n), \]  
\[ y_b^{n+1} = y_b^n + d \sin(\theta_f - \theta_b^n), \]
\[ n + 1 = \sqrt{(x_b^n)^2 + (y_b^n)^2} , \]  
\[ \theta_b^{n+1} = \arctan \left( \frac{y_b^n + 1}{x_b^n} \right) . \]

The bubble reaches the wall at an angle of

\[ \beta = 2(\alpha - \frac{\pi}{2}). \]

At this point, the bubble is constrained by the wall, and the calculation of bubble position with time proceeds using the analysis for a confined bubble above.

Although it is unlikely that a severe step change of the sort described here will be realized on the International Space Station, we have also examined many of these scenarios. An example is shown in figure 6, documenting the azimuthal position history for \( \theta_f - \theta_i = 160^\circ \). The bubble lifts off from its resting position at \( \theta_i = 0 \) in the direction of \( \theta_f \). The bubble meets the chamber wall at \( \theta_i = 140 \) degrees. Note that there is a significant period during which the bubble travels relatively speedily at terminal velocity. Its motion slows down, as expected, once it is confined by the wall. It reaches 99% \( \theta_f \) at 1682 seconds.

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The choice of chamber and bubble geometry and the fluids used can decrease the response time, as deemed necessary.

**Prototype**

An initial prototype, figure 1, was fabricated for use in the NASA Glenn Research Center 2.2 second drop tower. The prototype contained two commercial bubble levels in an orthogonal orientation with a mirror at 45°. This arrangement allowed both bubble levels to be observed simultaneously with a single camera.

The 2.2 second drop tower utilizes an experiment carrier within a drag shield enclosure to minimize aerodynamic drag accelerations on the experiment carrier. Under normal operations, the experiment carrier, inside the top of the drag shield, is released so the experiment carrier falls clear of the drag shield until the landing at the bottom. The drag shield enclosure is decelerated due to the aerodynamic drag and so the experiment carrier inside gradually falls to the bottom of the drag shield.

The prototype was dropped initially with the experiment carrier attached to the drag shield so as to experience a slight acceleration level due to the aerodynamic drag. During the test, the drag shield and the experiment carrier experienced an increasing acceleration due to the increasing velocity through the air. Initially, the bubble in the vertical plane was at the top of the chamber due to gravity. As soon as the carrier was released to fall, the bubble was observed to move toward the center of the indicator but remained above the outer ring of the indicator, figure 7a. This captive test was repeated four times with similar results each time.

The prototype was dropped in the free fall condition with the experiment carrier separate from the drag shield to minimize the aerodynamic drag on the experiment carrier. Initially, the bubble on the vertical two-dimensional indicator chamber was at the top of the chamber due to gravity. As soon as the carrier was released to fall, the bubble was observed to move toward the center of the indicator and crossed the outer ring of the indicator, figure 7b. The bubble on the horizontal surface remained in the same approximate position during the drop. This free fall test was repeated three times with similar results each time.

When the payload is released in the drop tower, the system undergoes a marked step change in its acceleration magnitude, although the primary component of the acceleration is still vertically down. Some off-axis jitter is present and may be appreciable.

The delicate balance of the bubble weight and buoyancy of the bubble, the fluid inertia, and the surface tension force due to bubble distortion and the available area for wetting is severely disrupted. We would expect that the higher-density preferentially wetting water may result in significant fluid flows as a result of the impulsive variation in acceleration and the variation in density between the two fluids. The precise quantification of the forces involved can not be captured in a simple numerical analysis such as is presented here. The front-to-back separation at the edge of the chamber, which is less than the bubble diameter, causes the bubble to form a resting oblate shape at 1g, as depicted in Figure 8. As the bubble moves downward after the drop, the front-to-back separation in the chamber relaxes, allowing the surface tension forces to create a spherically shaped bubble. We expect that as the hydrostatic and dynamic pressures equilibrate in the chamber, the bubble would move back up to the top of the chamber. If the bubble moves below 0.40 R₂, buoyant forces would require about 187 seconds to bring the bubble back up to its equilibrium position at the top of the chamber, much longer than is allowed in the experiment.

This centering action provided by the tapered chamber thickness at the edges is not desired for a microgravity device. The chamber would be fabricated with parallel front and back surfaces and a separation distance greater than the bubble diameter.

**IMPLEMENTATION**

**Data acquisition and analysis**

Data acquisition may be accomplished by video captured at a prescribed rate, depending on the desired frequency response. For low-frequency response, the frame rate would be quite slow relative to standard video and therefore could conceivably be sent to a ground station by interleaving in other video data streams.

The bubble position can be determined frame-by-frame by a computer image processing algorithm which would detect the bubble edges and calculate the bubble centroid location. To evaluate this concept, these data will be compared with data measured with a low-frequency accelerometer.

**Enhancements and options**

The basic concepts of the Quasi-steady Acceleration Direction Indicator may be applied in several different ways which will be explored in the future. Using transparent containers, these cylindrical chambers may be stacked so that more than one chamber/bubble combination may be observed simultaneously. This
would allow two (or more) chambers with different response characteristics to be observed simultaneously.

Alternately, a bubble with specific gravity less than the fluid and a particle with a specific gravity greater than the fluid could be combined in one chamber.

**ISS MICROGRAVITY ENVIRONMENT**

**Requirements for environment**

The requirements imposed on the ISS vehicle during microgravity mode operations include constraints on the amount of acceleration to which the science experiments are exposed. These requirements are documented in the System Specification for Space Station 5 and include quasi-steady ($f \leq 0.01$ Hz), vibratory ($0.01 < f < 300$ Hz), and transient acceleration constraints. These requirements apply to 50 percent of the internal payload locations. The constraints at the centers of those internal payload locations are stated such that the quasi-steady acceleration:

1) magnitude is less than or equal to 1 $\mu$g, and
2) the component perpendicular to the orbital average acceleration vector is less than or equal to 0.2 $\mu$g.

This defines a cylinder of radius 0.2 $\mu$g and of length 2 $\mu$g, within which the instantaneous acceleration vector must lie. This means that while the acceleration magnitude is constrained, the angle variation measured relative to the orbital average vector is unconstrained.

**Predicted environment**

The ISS Program prepares analytical predictions of the ISS microgravity environment in their Design Analysis Cycles (DAC). Analytical results show that the maximum angle deviation from the orbital average is approximately 27 degrees for racks in the ceiling of the U.S. Laboratory module after the ISS assembly is complete. More stable results are predicted for the port and starboard racks which should have a maximum deviation of only 7 degrees. The ceiling rack location results imply a worst case deviation of +/-27 degrees over one orbit, which must be adequately measured by the Quasi-steady Acceleration Direction Indicator.

Once a stable position has been attained by a Quasi-steady Acceleration Direction Indicator, the maximum deviation (54 degrees) for one orbit should keep the bubble constrained against the chamber wall.

**FUTURE WORK**

The theoretical analysis presented above did not account for the flows generated in the chamber by the motion of the bubble itself or by an impulsive change in acceleration magnitude. We expect to incorporate these features into our understanding of the problem by numerical simulation using the latest version of FIDAP (v. 8.5.2).

We also intend to investigate the impact of the chamber geometry, the bubble size, and the thermophysical properties of the fluids involved to optimize the sensor design. Conditions of oscillatory and transient accelerations will be investigated also.

**CONCLUSIONS**

The Quasi-steady Acceleration Direction Indicator appears to be a reasonable approach for acquiring low-frequency acceleration direction information for microgravity experiments on the International Space Station.

**REFERENCES**


Figure 1: Prototype Quasi-steady Acceleration Direction Indicator for drop tower tests.

Figure 2: Bubble path for acceleration direction step changes between 0° and 90°.

Figure 3: Bubble path for acceleration direction step changes between 90° and 180°.

Figure 4: Acceleration levels applied while bubble is constrained by wall.
Figure 5: History of bubble's azimuthal position for $\theta_f - \theta_i = 90^\circ$.

Figure 6: History of bubble's azimuthal position for $\theta_f - \theta_i = 160^\circ$.

Figure 7: Bubble position in front (vertical plane) bubble level during (a) captive and (b) free-fall drops in the 2.2 second drop tower.

Figure 8: Bubble position in front (vertical plane) bubble level before drops in the 2.2 second drop tower at NASA Glenn Research Center.
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**Subject Terms:**
Microgravity; Acceleration; Instrumentation