## (12) United States Patent <br> Sims, III

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(54) POWER DIVIDER FOR HARMONICALLY RICH WAVEFORMS
(75) Inventor: William Herbert Sims, III, Decatur, AL (US)
(73)

Assignee: The United States of America as represented by the Administrator of the National Aeronautics and Space Administration, Washington, DC (US)
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333/127: 333/136
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Primary Examiner-Robert Pascal
Assistant Examiner-Kimberly E Glenn
(74) Attomey: Agent, or Firm-James J. McGroary

ABSTRACT
A power divider divides an RF signal into two output signals having a phase difference of $180^{\circ}$ or a multiple thereof. When the RF signal is a square wave or another harmonically rich signal, the phases of the fundamental and the harmonics have the proper relationship. The divider can be implemented in the form of microstrips on a board, with one of the output microstrips having several bends to provide a different electrical length from the other.

20 Claims, 8 Drawing Sheets




FIG. 2


FIG. 3

FIG. 4




FIG. 8



FIG. 11



FIG. 13




FIG. 15


FIG. 16
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| Port | Harmonic 5 | VSWR | Coupling (dB) | Phasel |
| :---: | :---: | :---: | :---: | :---: |
| 502 | 1 | 1.0003 | $\mathrm{~N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ |
| 502 | 3 | 1.0003 | $\mathrm{~N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ |
| 502 | 5 | 1.0003 | $\mathrm{~N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ |
| 502 | 7 | 1.0003 | $\mathrm{~N} / \mathrm{A}$ | N |
| 508 | 1 | 1.0003 | -3.0002 | 0.0003 |
| 508 | 3 | 1.0003 | -3.0002 | 0.0003 |
| 508 | 5 | 1.0003 | -3.0002 | 0.003 |
| 508 | 7 | 1.0003 | -3.0002 | 0.0003 |
| 510 | 1 | 1.0003 | -3.0002 | 180.0 |
| 510 | 3 | 1.0003 | -3.0002 | 180.0 |
| 510 | 5 | 1.0003 | -3.0002 | 180.0 |
| 510 | 7 | 1.0003 | -3.0002 | 180.0 |

The phase differences closely match those desired. Thus. this simulation theoretically validates the basic concepts of the divider according to the present invention.

However, since the simulation described above was carried out under the assumption of perfect transmission lines, another simulation was carried out with striplines or microstrips. Again, jOmega was used for the simulation. The configuration of FIG. 6 was modified to result in the configuration of FIG. 7. In this configuration, a signal input to input port 702 travels through input line 703 and T-connector 712 to output lines 704 and 706 and thence to output ports 708 and 710 . Each of lines 704 and 706 includes bend portions 714. The output lines have total electric lengths differing by $180^{\circ}$. Tapered portions 716 at both output ports are provided only to allow the easy connection of SMA connectors to the printed circuit board. These connectors allow the circuit board to be connected to a network analyzer for simulation verification, as will be described below. The circuit board is formed of Rogers RT/Duroid 5880.15 mils thick, and 2-ounce copper. Rogers RT/Duroid 5880 has a dielectric constant $\epsilon_{r}=2.2 \pm 0.02$ and is designed for use beyond 18 Ghz . The output waveforms are shown in FIG. 8 and described in the table below.

| Pon | Harmonic ${ }^{\text {¢ }}$ | VSWR | Coupling (dB) | Phase |
| :---: | :---: | :---: | :---: | :---: |
| 702 | 1 | 1.6128 | N/A | N/A |
| 702 | 3 | 1.5632 | N/A | N/A |
| 702 702 | 5 | 1.6730 | N/A | N/A |
| 702 | 7 | 1.5642 | N/A | N/A |
| 708 | 3 | 1.6075 1.493 | -3.5224 -3779 | 2.0773 |
| 708 | 5 | 1.6821 | -3.8862 | 4.6293 3.9123 |
| 708 | 7 | 1.6220 | -4.2626 | ${ }_{0} \mathbf{3} .712152$ |
| 710 |  | 1.5923 | -3.3620 | 177.8 |
| 710 | 3 | 1.5886 | -3.3485 | 177.2 |
| 710 | 5 | 1.5919 | -3.7424 | 175.3 |
| 710 | 7 | 1.4633 | -3.5616 | 177.5 |

As can be seen from FIG. 8 and the table above, the modified simulation setup of FIG. 7 still produces excellent results.
After these simulations, a working model of the divider was built. The microstrip lines followed the layout of FIG. 7. The resulting layout shown in FIG. 9, had final size measurements of 2.0 inches in length and 1.0 inches in width. As shown in FIG. 9, layout 900 has input port 902 leading to input stripline 903. At T-point 905, stripline $\mathbf{9 0 3}$ branches into output striplines 904 and 906 , each of which has tapered portion 916 . The output striplines end in output ports 908 and 910 . The trace widths and lengths are given in the table below.

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| Pont | Width | Length |
| :---: | :---: | :---: |
| 902 | 71 | 290 |
| 908 | 27 | 3045 |
| 910 | 27 | 1124 |

The length to each port is measured from T-point 905 . The 0 dimensions are in mils.

The divider assembled with layout 900 is shown in FIG. 10. Divider 1000 has microstrip layout 900 on board 1018. Coaxial connectors 1002, 1008, and 1010 are connected to ports 902,908 . and 910 . Divider 1000 was assembled using a T-Tech milling machine and associated hardware, although any other suitable technique can be used.
As can be seen in FIG. 10, divider 1000 is very compact. Testing was done using a HewletuPackard network analyzer, model 8719 C . capable of operations only to 13.5 GHz . To discount the phasing effects of the SMA connectors on the test board, a delay factor of 20.67 mm (or 68.936 pS ) was added to the overall network analyzer calibration. The experimental results are set forth below.

| Port | Harmonic 5 | VSWR | Coupling (dB) | Phase |
| :---: | :---: | :---: | :---: | :---: |
| 902 | 1 | $(2 \mathrm{GHz})$ | 1.73 | $\mathrm{~N} / \mathrm{A}$ |
| 902 | 3 | $(6 \mathrm{GHz})$ | 1.17 | $\mathrm{~N} / \mathrm{A}$ |
| 902 | $5(10 \mathrm{GHz})$ | 1.50 | $\mathrm{~N} / \mathrm{A}$ |  |
| 902 | $7(14 \mathrm{GHz})$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ |
| 908 | 1 | 2.37 | -2.74 | $\mathrm{~N} / \mathrm{A}$ |
| 908 | 3 | 2.04 | -3.39 | -174.3 |
| 908 | 5 | 1.61 | -3.10 | -174.5 |
| 908 | 7 | $\mathrm{~N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ |
| 910 | 1 | 2.60 | -3.31 | 12.2 |
| 910 | 3 | 1.95 | -3.52 | 18.6 |
| 910 | 5 | 1.63 | -3.21 | 0.0 |
| 910 | 7 | $\mathrm{~N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ | $\mathrm{N} / \mathrm{A}$ |

One interesting note should be made concerning the VSWR for the output ports. During all the simulations of the divider, both ports were fed waveforms that were 180 degrees out of phase and of equal amplitudes. However, since the network analyzer is a two-port measurement device, one of the divider ports is not fed a signal source. Therefore, to equalize the measurements of simulation, another simulation was initiated. This simulation merely terminated one of the divider ports into $50 \mathrm{k} \Omega$. The new VSWR calculations are shown in the table below, compared with the experimental results set forth above.

| Port | Harmonic $\xi$ | Predicted VSWR | Actual VSWR | $\%$ <br> difference |
| :---: | :---: | :---: | :---: | :---: |
| 702 or 902 | 1 | 1.6093 | 1.73 | 7.5 |
| 702 or 902 | 3 | 1.5762 | 1.17 | 25.8 |
| 702 or 902 | 5 | 1.6530 | 1.50 | 9.3 |
| 702 or 902 | 7 | 1.6067 | N/A | N/A |
| 708 or 908 | 1 | 2.4428 | 2.37 | N/ 2.9 |
| 708 or 908 | 3 | 2.3442 | 2.04 | 2.9 12.9 |
| 708 or 908 | 5 | 2.2660 | 1.61 | 29.0 |
| 708 or 908 710 or 910 | 7 | 2.3106 | N/A | N/A |
| 710 or 910 | 1 | 2.4795 | 2.60 | N/A 4.6 |
| 710 or 910 | 3 | 2.2677 | 1.95 | 14.0 |
| 710 or 910 | 5 | 2.5711 | 1.63 | 36.6 |
| 710 or 910 | 7 | 2.3002 | N/A | N/A |

As can be seen from the table set forth above, all of the actual measurements were better than predicted for the

VSWR. With the actual circuit matching the simulation circuit. the concepts of the present invention have been experimentally validated.

A second area of concern deals with the signal source being modulated, thus increasing the signal from a constant continuous wave (CW) to a bandwidth limited signal. This bandwidth limited signal would impose frequency shifts to the center frequency. This frequency shifts would in turn cause the phase delay of each component of the square wave to change and thus destroy the phase relationship of the harmonic components. For instance, if the fundamental frequency phase delay were shifted by $5^{\circ}$, the seventh harmonic would be shifted $35^{\circ}$. How much this would affect the waveform will be shown. Simulations were run to evaluate and determine a usable bandwidth for this type of coupler.

This first type of simulation evaluated the VSWR across a $50 \%$ percent bandwidth relative to the 2 GHz center frequency. These results are shown in FIGS. 11-13. FIG. 10 shows the VSWR for the input port (port 702 in the simulation or 902 in the constructed device) of the divider. As can be seen in this figure, the input VSWR is below 2:1 across this entire frequency range. FIGS. 12 and 13 show the VSWR for ports 708 (or 908 ) and 710 (or 910 ) respectively.

Another simulation was run to determine phase characteristics in the same bandwidth. The results are shown for the input-to-output phase between ports 702 and 708 in FIG. 14 and between ports 702 and 710 in FIG. 15. The simulation was run again with a $5 \%$ bandwidth, and the results are shown between ports 702 and 708 in FIG. 16 and between ports 702 and 710 in FIG. 17.

With the $5 \%$ bandwidth, the third harmonic has approximately $8^{\circ}$ of difference relative to the fundamental. The next item of interest is to determine how much of a phase delay for each harmonic is allowed relative to the fundamental without detrimental effect to the fidelity of the square wave.

Using four signal sources, one for each harmonic of interest, the following procedure is used. If, for example. the third harmonic is $15^{\circ}$ out of phase with the fundamental, the fifth. seventh. and ninth harmonics are $25^{\circ}, 35^{\circ}$. and $45^{\circ}$ out of phase. FIG. 18 shows the waveform representative of the $8 \%$ phase error. The resulting waveform still resembles a square wave, albeit of poor fidelity. The waveform will be considered to have approximately a $5 \%$ bandwidth. The bandwidth can be increased. but the resulting efficiency of the power amplifier is adversely affected.

As can be seen, all of the actual measurements are better than predicted for the VSWR. With the actual circuit matching the simulation circuit, the divider topology according to the present invention has become a proven design.

While a preferred embodiment of the invention has been set forth above, those skilled in the art who have reviewed this disclosure will readily appreciate that many other embodiments can be realized within the scope of the invention. For example, any suitable transmission line can be used. Also, while the phase difference has been disclosed as being caused by a difference between the electrical lengths of the two output transmission lines, the phase delay can be introduced in any other way. Furthermore, the phase difference between the output ports can be $180^{\circ}$ or any multiple thereof. The phase differences between the output ports and the input ports can be offset by any amount; for example, the differences can be $180^{\circ}$ and $360^{\circ}, 90^{\circ}$ and $270^{\circ}$, or any other set of values having a difference which is a non-zero integer multiple of $180^{\circ}$.

What is claimed is:

1. A power divider for dividing a harmonically rich input signal into a first output signal and a second output signal, the power divider comprising:
2. A power divider as in claim 9, wherein the input transmission line, the first output transmission line, and the
an input transmission line for transmitting the input signal to a T-point at which the input signal is split into a first portion and a second portion:
a first output transmission line having a length which is a first non-zero integer multiple of approximately $\lambda \Omega$ of a wavelength of a fundamental frequency of the input signal, the first output transmission line receiving the first portion of the input signal at the T-point for transmitting the first portion while imparting a first phase delay to the first portion of the input signal to form the first output signal: and
a second output transmission line having a length which is a second non-zero integer multiple that is at least twice the value of the first non-zero integer multiple of the first transmission line, the second output transmission line receiving the second portion of the input signal at the T-point for transmitting the second portion while imparting a second phase delay to the second portion of the input signal to form the second output signal:
wherein the first phase delay and the second phase delay have a difference which is a non-zero integer multiple of $180^{\circ}$, and
the ratio of lengths of said first and second output transmission lines provide that harmonic frequencies output from each of the output transmission lines are in phase with each other.
3. A power divider as in claim 1 , wherein the difference is $180^{\circ}$.
4. A power divider as in claim 1, wherein each of the input transmission line, the first output transmission line. and the second output transmission line is an electrically conductive transmission line; and
the harmonically rich input signal is a square wave: and
an amplitude of the first output signal is approximately
equal to an amplitude of the second output signal.
5. A power divider as in claim 3. wherein each of the input transmission line, the first output transmission line, and the second output transmission line is a coaxial transmission line.
6. A power divider as in claim 3. wherein each of the input transmission line, the first output transmission line, and the second output transmission line is a microstrip line.
7. A power divider as in claim 5 , wherein:
the first output transmission line has a first number of bends: and
the second output transmission line has a second number of bends which is different from the first number of bends.
8. A power divider as in claim 3, wherein the length of the first transmission line is approximately $\lambda / 2$ of the fundamental frequency of the input signal. and the length of the second transmission line is approximately equal to the wavelength of the fundamental frequency of the input signal.
9. A power divider as in claim 7, wherein the input transmission line, the first output transmission line, and the second output transmission line are formed as part of a stripline assembly.
10. A power divider as in claim 1, wherein the length of the first transmission line is approximately $\lambda / 2$ of the fundamental frequency of the input signal. and the length of the second transmission line is approximately equal to the wavelength of the fundamental frequency of the input signal.
second output transmission line are formed as part of a stripline assembly.
11. A power divider as in claim 1, wherein the input transmission line, the first output transmission line, and the second output transmission line are formed as part of a stripline assembly.
12. A method of dividing a harmonically rich input signal into a first output signal and a second output signal, the method comprising:
(a) splitting the input signal into a first portion and a 1 second portion;
(b) imparting a first phase delay to the first portion of the input signal by providing a first transmission line having a length which is a non-zero integer multiple approximately $\lambda / 2$ of a wavelength of a fundamental frequency of the input signal to form the first output signal:
(c) imparting a second phase delay to the second portion of the input signal by providing a second transmission line having a length which is a non-zero integer multiple of at least twice the value of the non-zero integer multiple of the first transmission line to form the second output signal;
wherein the first phase delay and the second phase delay have a difference which is a non-zero integer multiple of $180^{\circ}$, and
the ratio of lengths of said first and second output transmission lines provide that harmonic frequencies output from each of the output transmission lines are in phase with each other.
13. A method as in claim 12. wherein the difference is $180^{\circ}$.
14. A method according to claim 12, wherein an amplitude of the first output signal provided in step (b) and an amplitude of the second output signal provided in step (c) are approximately equal; and
a frequency of the first output signal and the second output
signal are approximately equal. mission line.
15. A method as in claim 14, wherein all of the electrically conductive transmission lines are formed as one of a microstrip line and a stripline assembly.
16. A method according to claim 12, wherein the length of the first transmission line provided in step (b) is approximately $\lambda / 2$ of the fundamental frequency of the input signal; and
the length of the second transmission line provided in step
(c) is approximately equal to the wavelength of the fundamental frequency.
17. A method according to claim 17, wherein an amplitude of the first output signal provided in step (b) and an amplitude of the second output signal provided in step (c) are approximately equal.
18. A method as in claim 17, wherein the input transmission line, the first transmission line, and the second output transmission line are all formed as one of a microstrip line assembly and a stripline assembly.
19. A method as in claim 12. wherein steps (a)-(c) are performed in electrically conductive transmission lines.
20. A method as in claim 14, wherein each of the electrically conductive transmission lines is a coaxial trans-
