# Towers for Earth Launch 

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# Fifteen kilometer tower 

(9.3 miles)

Size a 15 km tower to support launch weight of space-shuttle ( 2000 t ):

Structural material:
Graphite epoxy: Lc=107.5 km No taper needed
tower mass 280 tons

Cast steel: $\mathrm{Lc}=15.4 \mathrm{~km}$ taper required tower mass 5300 tons (taper ratio 2.6)
alternative: a 10 km tower on a 5km mountaintop

# Why launch from a fifteen kilometer tower? 

Single stage to orbit means that mass ratio is very sensitive to small changes in performance

much of the improvement is due to lower air pressure:
15 km gets you above $83 \%$ of the atmosphere

## Advantages of high-altitude launch:

## (1) Start at a fraction of the altitude needed to get to orbit

a. Initial potential energy
b. Gravity losses for first part of launch not
incurred

## (2) Start at a lower atmospheric pressure.

a. Reduced atmospheric drag loss
b. Vehicle can be designed with less attention to aerodynamics.
c. More optimum trajectory curves toward horizontal faster
d. Max-Q occurs at a much lower pressure;
lower aerodynamic stress
e. Aerodynamic vibrations lower; allows less
robust (lighter) payload
f. Wind loads on vehicle in flight much lower
g. Acoustic loads much lower
h. Cryogenic storage easier (lower conduction and convective heating)
i. Shroud jettison can occur earlier
(3) Lower pressure means rocket operation is closer to vacuum
a. Higher performance out of the rocket nozzle at launch
b. Higher expansion ratio possible; less design compromise needed

## (4) Start at a lower gravity

a. Lower gravity losses due to lower gravity and higher thrust/weight ratio
(5) Above the weather means no compromises needed for weather
a. Fewer delays for weather
b. Above lightning hazard
c. less robust design needed

## Advantages of high-altitude launch

Examine in detail 4 of these advantages:
1a. initial potential energy
5a. gravity loss
2a. atmospheric drag
3a. rocket engine performance
Comparison: launch from a $15-\mathrm{km}$ tower compared to sea-level

Single stage to orbit means that mass ratio is very sensitive to small changes in performance

## Baseline SSTO for calculation:

$\Delta V$ to orbit $=9 \mathrm{~km} / \mathrm{sec}$ (includes drag, gravity, and trajectory losses)
$\mathrm{H}_{2}-\mathrm{O}_{2}$ propulsion, $\mathrm{I}_{\mathrm{sp}}=425 \mathrm{sec} .[\mathrm{V}=4.16$ $\mathrm{km} / \mathrm{sec}$ ]

Theoretical mass ratio:
$\mathrm{Mf} / \mathrm{Mi}=\exp [-\Delta \mathrm{V} / \mathrm{glsp}]=\exp [-$

Vehicle mass (structure, engines, avionics, payload)
$=11.5 \%$ of gross lift-off mass
Payload $=2 \%$ of gross lift-off mass

Potential energy:<br>15 km tower gives a potential energy velocity of $\mathrm{mgh}=225 \mathrm{~kJ} / \mathrm{kg}$<br>Required launch energy is $40.5 \mathrm{MJ} / \mathrm{kg}$<br>Tower provides $0.56 \%$ of orbital energy<br>This is equivalent to:<br>$\Delta V=11 \mathrm{~m} / \mathrm{sec}$<br>negligible

## Gravity Loss

Shuttle: gravity loss $800 \mathrm{~m} / \mathrm{sec}$. Titan IV: gravity loss $750 \mathrm{~m} / \mathrm{sec}$.
Gravity for a 15 km tower is $99.4 \%$ as strong as gravity on the ground; this gives us a $0.45 \%$ decrease in gravity loss, and another 0.45\% decrease due to higher thrust/weight
$\Delta V=7 \mathrm{~m} / \mathrm{sec}$
negligible.

## Drag

atmospheric density $\exp [-15 / 8.4]=16.8 \%$ of baseline
Drag loss $=\mathrm{Kd} \mathrm{CdA}$ Wo,
For $\beta$ (burnout) $=30^{\circ}, \mathrm{Cd}=0.5, \mathrm{~A}=75 \mathrm{~m}^{2}$, Wo
(GLOW) $=950,000 \mathrm{~kg}$ and $\mathrm{I}_{\mathrm{sp}}(\mathrm{vac})=450 \mathrm{sec}, \mathrm{drag}$ loss $=230 \mathrm{~m} / \mathrm{sec}$ drag loss
A 15 km tower will multiply this loss by a factor of 0.168 . Improvement:
$\Delta V=191 \mathrm{~m} / \mathrm{sec}$

## Improved Engine Performance

$$
\mathrm{lsp} / \mathrm{lsp}(\mathrm{vac})=1-\varepsilon \mathrm{Po} /[\mathrm{PcCf}(\mathrm{vac})]
$$

or, in terms of practical parameters:

$$
\begin{aligned}
& \text { Isp/lsp(vac) }=1-\mathrm{AePo} / \mathrm{F} \\
& \mathrm{Ae}=\text { exit area } \\
& \mathrm{Po}=\text { atmospheric pressure } \\
& \mathrm{F}=\text { thrust }
\end{aligned}
$$

(Does not include additional gains possible by increasing expansion ratio)

Specific impulse at sea-level (SL) and in vacuum (vac)

Atias:
Rocketdyne MA-5 sustainer: 309 sec vac, 220 sec SL [V/SL $=140.5 \%$ ]
Rocketdyne MA-5A booster: 295 sec vac, 263 sec. SL [V/SL = 112.2\%]
Delta:
RS-27A: 302 sec vac, 255 sec SL [V/SL= 118.5\%] Shuttle:
SSME at 100\%: 2091 kN vac, 1668 kN SL [V/SL
thrust $=125.4 \%$ ]
Soyuz:
RD-107: $314 \mathrm{sec} \mathrm{vac}, 257 \mathrm{sec}$ SL [V/SL $=122.2 \%$ ]
RD-108: $315 \mathrm{sec} \mathrm{vac}, 248 \mathrm{sec}$ SL [V/SL $=127.0 \%$ ]
Energia/Zenit
RD-170/171: 336 sec vac, 308 sec SL [V/SL = 109.1\%]

Tripropellant
RD-701 (mode 1): 415 sec vac, 330 sec SL [V/SL = 125.8\%]

Total gain in effectove $\Delta \mathbf{V}$ : 405 meters per second

## The bottom line for payload:

## Baseline SSTO:

Payload+vehicle fraction $=\exp [-9 / 4.161]=11.5 \%$ of which $2 \%$ is payload and $9.5 \%$ vehicle

## Tower Launched SSTO:

Payload+vehicle fraction $=\exp [-(8.595) /(4.161)]=$ 12.7\%
of which $3.2 \%$ is payload, and $9.5 \%$ vehicle

Tower launch increases payload to orbit by 60\%

## The bottom line for payload:

## Detailed calculation of example SSTO:

Empty vehicle mass $10 \%$ of Gross lift-off weight
Payload mass 2.45\% of Gross lift-off weight

## Tower Launched SSTO:

| Tower <br> height <br> km | Payload (\% <br> of GLOW) | Fractional <br> increase |
| :--- | :---: | :---: |
| 0 | 2.45 | - |
| 5 km | 3.08 | $+26 \%$ |
| 10 km | 3.65 | $+49 \%$ |
| 15 km | 4.13 | $+69 \%$ |
| 20 km | 4.54 | $+85 \%$ |
| 25 km | 4.90 | $+100 \%$ |

Tower launch increases payload to orbit by $60 \%$

A convenient measure of a material's strength to weight ratio is the characteristic length Lc. This is the ultimate strength $\sigma$ divided by the density $\rho$ times the acceleration of gravity at the Earth's surface.

## $L c=\sigma / \rho g$

The physical meaning of $L_{c}$ is the length at which a length of constant cross section will fail under its own load, under a uniform force of one gravity.

| Material Strength | Density | Le | Le* |
| :---: | :---: | :---: | :---: |
| (* with safety factor) (GPa) |  | (km) | (km) |
| Grey Iron 1.2 | 7446 | 16.5 | 13.2 |
| Cast Steel 1.2 | 7800 | 15.4 | 12.3 |
| TiC 2.76 | 4000 | 70.3 | 35.2 |
| Graphite/Epoxy1.7 | 1610 | 107.5 | 53.8 |
| Quartz fabric 0.46 | 1716 | 27.2 | 13.6 |
| S-Glass 0.66 | 1909.9 | 35.2 | 17.6 |
| Boron/Epoxy 2.43 | 2020.6 | 122.5 | 66.3 |
| Glass polyimid 0.55 | 2214.2 | 25.3 | 12.7 |
| WC Carbide 4.48 | 15500 | 29.4 | 14.7 |
| $\mathrm{B}_{4} \mathrm{C} \quad 2.85$ | 2500 | 116.1 | 58.1 |
| SiC/Epoxy 2.33 | 2248 | 98.5 | 49.8 |

References: Handbook of Tables for Applied
Engineering; Handbook of Composites, George Lubin

