Numerical Roll Reversal
Predictor-Corrector
Aerocapture and Precision Landing
Guidance Algorithms for the
Mars Surveyor Program 2001 Missions

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This paper describes guidance algorithms that use numerical predictor-corrector techniques to guide the spacecraft to the proper objectives. The precision landing objective is to deploy a parachute within 10 km of the target, and the aerocapture objective is to use a single atmospheric pass instead of an orbit insertion burn, with the requirement of being within 0.1° of the desired inclination and needing less than 130 m/sec velocity increment (ΔV) to achieve the final orbit. For the precision landing mission, this paper will describe the algorithm, discuss the performance for the nominal mission and describe trade studies designed to evaluate the robustness of the algorithm. For the aerocapture mission, only results for the nominal mission are discussed.

Nomenclature

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
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<tbody>
<tr>
<td>AFE</td>
<td>Aeroassist Flight Experiment</td>
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<td>AFT</td>
<td>Atmospheric Flight Team</td>
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<tr>
<td>Cₐ</td>
<td>axial force coefficient</td>
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<td>Cₜ</td>
<td>normal force coefficient</td>
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<td>J₂</td>
<td>gravity harmonic term</td>
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<td>L/D</td>
<td>lift to drag ratio</td>
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<td>MCI</td>
<td>Mars centered inertial</td>
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<td>MCMF</td>
<td>Mars centered Mars fixed</td>
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<td>MSP</td>
<td>Mars Surveyor Program</td>
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<tr>
<td>NAV</td>
<td>Navigation derived (estimated) quantities</td>
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<tr>
<td>RRPC</td>
<td>Roll Reversal Predictor Corrector</td>
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<tr>
<td>3DOF</td>
<td>Three Degrees-of-Freedom</td>
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<tr>
<td>6DOF</td>
<td>Six Degrees-of-Freedom</td>
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<tr>
<td>ΔV</td>
<td>velocity increment, m/s</td>
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Overview

The specific objectives defined by the MSP project office for the guidance algorithms depend on the spacecraft and mission. The MSP '01 Lander must meet the parachute deployment conditions (Mach number between 1.6 and 2.3 and dynamic pressure between 400 and 1175 N/m²) while arriving within 10 km of its target point. For the MSP '01 Orbiter, a final inclination of 92.92° ± 0.10°, an orbital periapsis altitude (above a reference sphere) higher than −150 km, and a total ΔV less than 130 m/s for circularization into a 400 km orbit are required.
The AFT developed algorithm testbed has been used for the development and testing of these algorithms. This testbed consists of four simulations. Each mission has a high fidelity six degree-of-freedom (6DOF) and a less computationally intensive three degree-of-freedom (3DOF) simulation. Details about the aerodynamics, atmosphere, control system, mass properties, gravity, inertial measurement unit, and planet models for these simulations are given in reference 1.

Monte Carlo type analyses of the guidance algorithms are also conducted using these simulations. These assessments involve uncertainty in mass properties, aerodynamic coefficients, atmospheric conditions, control system thrusters, inertial measurement unit errors, state delivery and knowledge errors, as well as initial altitude and attitude rates. These uncertainty levels are given in Tables 3 and 4 of reference 1; further discussion of those uncertainties is also included in that reference. The MSP '01 established a success criteria of 99% of the simulations generated during the Monte Carlo process (i.e. 1980 successes of the 2000 total cases). This success criteria will be referred to as the 99-Centile for the remainder of the paper.

The guidance algorithm used to generate results for this paper can be described as a roll reversal numerical predictor-corrector (RRPC). Predictor-corrector algorithms integrate the equations of motion, evaluate errors between the integrated trajectory and the requirements, modify the command vector used in the initial trajectory propagation to remove these errors, and then iterate until the integrated trajectory meets the requirements. The command vector for the RRPC algorithm is composed of a roll angle magnitude and times from atmospheric interface to execute roll reversals (switch from roll right (positive roll) to roll left (negative roll) or vice versa). The total guidance algorithm is composed of an inner and outer loop. The outer loop controls the guidance process and is called at the simulation nominal guidance update cycle time - currently 0.1 sec. It provides all the guidance commands to the control system. It calls the inner loop, where the predictor-corrector logic resides, at specified intervals. The inner loop, which is composed of the integration and iterating routines determines a nominal roll angle magnitude, and the times to perform roll reversals. This information is passed back to the outer loop. The outer loop uses the inner-loop prediction to calculate the commanded roll angle which is provided to the control algorithm. The outer loop can modify the magnitude of the roll angle based on current state information (position, velocity, and accelerations), but cannot vary the roll reversal times calculated by the inner loop.

The major advantage of a numerical predictor-corrector algorithm over an analytic algorithm is that the equations of motion are actually integrated. Thus the vehicle can be modeled in as much detail as data is available. In addition, as the models or constraints change, they can be easily be incorporated into the guidance algorithm. The algorithms described in this paper integrate 3DOF (translational only) equations of motion. Since only the translational equations are integrated, the vehicle orientation strategy must be specified. As the guidance algorithm is developed, this requirement is used to define the orientation which maximizes the robustness of the algorithm. Another advantage of the predictor-corrector algorithm is that the inner-loop guidance algorithm can be called rather infrequently. This last advantage is mitigated by the increased computational time required to both integrate the equations of motion and then iterate to a solution. Another disadvantage of the predictor-corrector algorithm is that the total number of lines of code is greater than that required for typical analytical guidance algorithms.

Predictor-corrector techniques have been studied for the past several years. Reference 6 describes candidate predictor-corrector algorithms designed for the Aeroassist Flight Experiment (AFE). The AFE was designed to be deployed from the Space Shuttle, be accelerated to a velocity simulating return from geosynchronous orbit, enter the Earth's atmosphere (where it would decelerate), and exit the Earth’s atmosphere to be captured by the Space Shuttle. Reference 7 describes work by the JPL-led Mars Atmospheric Knowledge Working Group. This working group was charged with determining the level of knowledge of the Martian atmosphere that is required to insure that human missions could employ aerocapture. Two of the algorithms used by that working group were predictor-corrector routines. (See Refs. 8 and 9). Predictor-corrector algorithms have also been demonstrated for entry and landing missions. Reference 10 describes a predictor-corrector scheme for a Space Station resupply/rescue vehicle.

**Description of Algorithms**

The predictor-corrector algorithms for the precision landing and aerocapture missions share many common features. The algorithms receive state conditions (position and velocity) from the onboard navigation system. This information is provided in both the Mars-centered inertial (MC1) frame, and the Mars-centered Mars-fixed (MCMF) relative frame. In addition, the current roll angle and sensed body-axis accelerations are provided. The algorithm integrates the 3DOF translational equations of motion using a fourth-order Runge Kutta
Integration scheme. The algorithm has the following internal models:

1) Planet Model – oblate spheroid described by equatorial and polar radius;
2) Gravitation model – simple harmonic model using J2;
3) Aerodynamics – \( C_A \) and \( C_N \) as a linear function of velocity (table lookup);
4) Body attitude – angle of attack as a linear function of velocity (table lookup);
5) Mass properties – nominal values of mass, aerodynamic reference lengths and areas;
6) Atmosphere – density as a bivariant function of altitude and geodetic latitude. This relationship was derived using mean MarsGRAM (Ref. 11) values converted to a simple table lookup. Note that MarsGRAM is not explicitly included as a model. The internal model also assumes no winds.

The inner loop of the algorithm produces a command vector that is composed of roll angle magnitude and reversal times (i.e., times to switch the current sign of the roll angle). In addition, the algorithm produces a state history (for precision landing – range to target, energy and time rate of change in energy, for aerocapture – orbital energy, time rate of change in orbital energy, periapsis and apoapsis altitudes). Since the inner loop of the predictor-corrector is called at relatively long intervals (5 seconds for precision lander and 10 seconds for aerocapture), this state information is used to modify the roll angle magnitude between updates. This alteration is done in the outer loop by comparing the actual state conditions with the predicted state conditions and then modifying the roll angle appropriately. The 5-second and 10-second update times were chosen at the beginning of the study, and no trade study to determine sensitivity to update time has been performed.

Two methods were investigated to determine the appropriate roll angle and roll reversal time required to achieve the guidance objectives. The first is a gradient method. This method generally results in tighter convergence, but requires the numerical determination of a Jacobian (first derivative) matrix. In addition, the preliminary study found that some pathological cases resulted in no solution being reached by the algorithm. The second method is a half-interval search routine. This method has the advantages of not requiring a Jacobian matrix, and in general, the error decreases as the solution progresses. The half-interval search method was used for all the results presented in this paper.

The sensed acceleration data is used to update the internally stored atmospheric density profiles and aerodynamics. This is done by calculating the ratios of the normal and axial sensed acceleration values to those values predicted by the guidance algorithms. In addition, the guidance routines are used to calculate a local density scale height. By knowing both the aerodynamic acceleration ratios, and the local density scale height, scalar multipliers to the guidance predicted aerodynamics, and an altitude bias to the guidance atmospheric model can be calculated. These scalar multipliers and altitude bias quantities are averaged over 10 second intervals, and these averages are used within the inner loop.

Both the precision landing and aerocapture algorithms share the above features, but each required individual tailoring. The precision landing algorithm remains in the outer guidance loop until the Lander’s altitude drops below 80 km. During this initial phase, the only guidance correction is to reduce the heading error by changing the roll angle command. The algorithm compares the heading required to reach the target with the current heading and modulates the roll angle command to reduce the error. Once at an altitude of 80 km, the use of the inner-loop predictor-corrector algorithm is initiated. Once the predictor-corrector is invoked, the vehicle guidance strategy is a combination of roll angle magnitude and roll reversals. The general strategy is to iterate the roll angle magnitude until the predicted miss distance is within a pre-selected tolerance. Roll reversals are commanded if the heading error exceeds a preset limit. The roll angle magnitude and reversal times are then passed to the outer loop for execution.

Two different strategies are used to calculate the roll angle magnitude. The first is to iterate only the roll angle magnitude until the first roll reversal and then command the roll angle magnitude to be 90°. This strategy maintains as much performance margin as possible to be used in the later stages of the entry to improve targeting. The inner loop continues in this mode until the outer loop commands the first reversal. Once the first roll reversal is commanded by the outer loop, the inner-loop strategy changes to determine the roll angle magnitude to be maintained for the remainder of the trajectory.

The Orbiter aerocapture algorithm uses the outer loop until the spacecraft’s altitude drops below 80 km. Until then the roll angle is commanded to be 0°. Once 80 km is reached, the inner-loop algorithm is activated. The strategy is similar to the precision-landing algorithm in that roll angle magnitude and roll reversal times are calculated in the inner loop and passed to the outer loop. The roll reversals are commanded when inclination is
outside the upper or lower limits. These inclination limits are determined as follows. Since the Orbiter is commanded to fly a 0° sideslip angle to the atmospheric relative velocity vector, it will produce a force that is not in the plane of the inertial velocity vector. For the MSP '01 orbiter, this means the inclination will naturally decrease during the atmospheric maneuver. This natural decrease is reflected in the determination of the upper and lower inclination bounds. These limits are selected so that a nominal mission will require three roll reversals. It was found that the strategy of three reversals for the nominal mission provided adequate inclination control for the off-nominal cases.

As was the case for precision landing, two different inner-loop strategies are used in the aerocapture algorithm. The first is used until apoapsis is below 12000 km. For this strategy, the inner loop simulation modulates the roll angle magnitude until apoapsis is reduced to 8000 km, after which roll angle is commanded to 90°. Once the outer loop senses that apoapsis is less than 12000 km, the roll angle magnitude determined by the inner loop is maintained for the remainder of the trajectory. This two-part strategy is designed to maximize the performance margin available to correct off-nominal conditions during the latter part of the atmospheric pass. As for the Lander, the inner loop passes the required roll angle magnitude and roll reversal times to the outer loop.

**Precision Landing Simulation Results**

**Nominal Mission**

Figure 1 shows angle of attack, roll angle and altitude versus velocity for a nominal 6DOF entry. This nominal profile requires two roll reversals. The target miss distance is less than 0.5 km. The first guidance strategy is used until velocity decreases to 4500 m/s, at which point the second strategy is used. Note that the roll angle magnitude profile is rather benign until the velocity is reduced to 1800 m/s. The activity noted when the velocity drops below 1800 m/s is because more spacecraft maneuvering is required to correct errors as the Lander gets closer to the target.

**Monte Carlo Results**

Two thousand 3DOF and 6DOF Lander Monte Carlo cases using dispersions described by reference 1 were completed for this guidance algorithm. The 3DOF landing footprint for the estimated (NAV) and actual (simulation generated) states are shown in Figs. 2 and 3, respectively. The NAV states are estimated by the control
The results of these Monte Carlo runs are also contained in Table 1. This table shows the amount of the 99-Centile cases that fell within 50 km, 10 km, 5 km, and 2 km of the target parachute deploy point. The 99-Centile cases were generated using a cost function of NAV range, Mach number, and dynamic pressure. The 99-Centile cases represent the 1980 cases out of 2000 that best meet the defined cost function. Table 1 also indicates the discrepancy in the NAV and actual states, which has propagated from the start of the trajectory. As shown in the table, over half of the cases were within 2 km of the target using NAV states, and over 99 percent were within 5 km. These numbers fall off sharply when using the actual states, but again, the guidance algorithm is only provided the NAV states and has no knowledge of or ability to measure the error with respect to actual states.

As noted in Table 1, the 6DOF 99-Centile results strongly reflect those from the 3DOF runs. Almost two-thirds of the cases had range from target based on NAV states within 2 km, while over 98 percent were within 5 km. Once again, all of the cases were well within the 10-km requirement.

Figure 6 indicates that all the 99-Centile cases comply with the dynamic pressure (400 to 1175 N/m²) and Mach number (1.6 to 2.3) limits on parachute deploy. Although this figure is only for the 6DOF simulation, the 3DOF results also meet these limits. These values are determined using the actual states at the parachute deployment. This result shows that although the guidance algorithm is unable to predict actual states, 99% of the Monte Carlo-generated results still fall within acceptable limits.
deployment conditions. Since the guidance algorithm only has knowledge of the NAV states, the remaining Lander guidance algorithm results in this paper will only present quantities derived from these estimated states.

**MSP '01 Lander Trade Studies**

Several trade studies were conducted to assess the robustness of this predictor-corrector guidance algorithm developed for the MSP '01 Lander missions. These studies evaluated the effect of winds, lift-to-drag ratio, and parachute deploy target point on algorithm performance. The first study removed the winds provided by the MarsGRAM subroutines from the simulation. The next analysis compared the current MSP '01 Lander (with an L/D = 0.12) to two other options (L/D = 0.18 and 0.06). The last study evaluated changing the target parachute deploy point to ±60 km long and to ±30 km short of the nominal target point.

For the provided entry conditions (arrival date and states), the MarsGRAM predicted winds are predominately from the southwest as the parachute deploy point is approached. This data is verified by Fig. 7, which shows the NAV landing footprint for the 6DOF Monte Carlo without winds. By comparing Figs. 7 and 4, a tight grouping around the target point is seen. However, the target for the cases without winds had to be shifted to the southwest by ±6 km compared to the cases with winds. As seen in Table 1, the 6DOF cases without winds had slightly better performance than the cases including winds. This result indicates that the L/D = 0.12 vehicle is able to compensate for the simulated winds. The caveat is that this MarsGRAM model (version 3.7) does not have a wind perturbation model, thus all the entries
have basically the same wind profile. This feature makes the required target offset determination simple for these Monte Carlo simulations.

While this paper has discussed L/D as if the Lander has a constant value during entry, this is not the case. The control system is designed to maintain the Lander at the trim angle of attack. This trim angle of attack is determined by the off-axis (lateral) center of gravity position and the aerodynamics. Since the Lander entry covers the flow regimes ranging from free molecular to continuum and hypersonic to supersonic, there is some variation in both trim angle of attack and L/D. Figure 8 shows how the L/D varies with relative velocity for the three options studied. Figure 9 indicates the parachute deploy footprint for the L/D = 0.06 6DOF cases without winds and Fig. 10 has the footprint of the L/D = 0.18 Lander. From these figures, the 0.06 vehicle does not quite meet the 10 km requirement for 99-Centile of the cases, whereas the L/D = 0.18 Lander is able to get all of the 99-Centile cases below 5 km. Another benefit of this increased L/D of 0.18 is that over 90 percent of the spacecraft entries were within 2 km of the target location. For comparison, the L/D of 0.12 vehicle was able to get 81 percent of the entries within 2 km of the target deploy point.

A side point related to the wind/no wind trade reported above involves the ability of the L/D = 0.18 vehicle to handle the winds. Figure 11 shows the 6DOF footprint for this higher L/D vehicle when winds are included in the simulation and the no-wind target point is used. When compared with Fig. 4, the grouping is tighter.
for the higher L/D spacecraft and the target point would only need a 3 km eastward shift from the no wind target, as compared to a 6 km shift to the northeast for the L/D = 0.12 vehicle.

Another analysis was conducted to assess the sensitivity of the algorithm to target point selection. Two new targets were selected and the only change made to the algorithm was the internal target point. One target was ±60 km down range from the original target. The other target was ±30 km up range from the original.

The 6DOF Monte Carlo results for the new target point cases without winds are shown in Figs. 12 and 13. Note that the original target point is indicated as a box in these plots. Both the short target point and long target point cases were well within the 10-km requirement. In fact, these figures indicate a similar result regardless of which target point is selected. This result coupled with the minimal effort to change the algorithm for these new target points indicates an algorithm fairly robust to landing site changes.

**Aerocapture Simulation Results**

**Nominal Mission**

Figure 14 shows angle of attack, roll angle and altitude versus Mars relative velocity for a nominal 3DOF aerocapture. This nominal profile requires three roll reversals, as designed. It exits at an apoapsis of 423 km with an inclination of 93.00°, and ΔV of 108.8 m/s required for circularization into a 400 km orbit.

**Monte Carlo Results**

Two thousand 3DOF Orbiter Monte Carlo cases using dispersions described by reference 1 were completed for this guidance algorithm. Fig. 15 shows the 99-Centile inclination versus the ΔV required for 400 km circular orbit. This figure shows that 96.7% of the 99-Centile cases meet this criterion. Note that the dashed box indicates the inclination and ΔV requirements for aerocapture exit. This success level should be improved by further tuning of the algorithm. Aerocapture has been eliminated from the MSP '01 mission; thus only a small effort was devoted to guidance algorithm design for the aerocapture mission.
Conclusions

A numerical roll reversal predictor-corrector guidance algorithm was developed for the MSP '01 precision landing and aerocapture missions. These were evaluated using Monte Carlo analysis with both 3DOF and 6DOF analyses. For the precision lander, the baseline vehicle reaches the desired parachute deployment point within the acceptable range of dynamic pressures and Mach numbers. Trades were conducted that showed the impact of increased/decreased lift-to-drag ratio (L/D). Increasing the L/D by 50% noticeably decreased the sensitivity to winds, while decreasing the L/D to 50% of the baseline value reduced the percentage within the desired target range to 94%. Thus even this large reduction in L/D still provided a large degree of precision landing capability. A second trade determined the sensitivity to landing site selection. The trade study showed that moving the target towards either end of the landing ellipse does not significantly reduce the percentage of success.

For the Orbiter, the success of meeting the desired exit conditions after aerocapture was 96.7% of the 99-Centile cases as compared to the MSP ‘01 project office requirement of 100%. The algorithm has many tunable elements that could be used to increase this success rate. Since aerocapture was dropped from the MSP ‘01, the major effort was placed on precision landing instead of aerocapture.

References


