ABSTRACT
Terrestrial Planet Finder (TPF) is a mission to locate and study extrasolar Earthlike planets. The TPF Coronagraph (TPF-C), planned for launch in the latter half of the next decade, will use a coronagraphic mask and other optics to suppress the light of the nearby star in order to collect visible light from such planets. The required contrast ratio of 5 x 10^-11 can only be achieved by maintaining pointing accuracy to 4 milli-arcseconds, and limiting optics jitter to below 5 microns. Numerous mechanical disturbances act to induce jitter. This paper concentrates on passive isolation techniques to minimize the optical degradation introduced by disturbance sources. A passive isolation system, using compliant mounts placed at an energy bottleneck to reduce energy transmission above a certain frequency, is a low risk, flight proven design approach. However, the attenuation is limited, compared to an active system, so the feasibility of the design must be demonstrated by analysis. The paper presents the jitter analysis for the baseline TPF design, using a passive isolation system. The analysis model representing the dynamics of the spacecraft and telescope is described, with emphasis on passive isolator modeling. Pointing and deformation metrics, consistent with the TPF-C error budget, are derived. Jitter prediction methodology and results are presented. Then an analysis of the critical design parameters that drive the TPF-C jitter response is performed.

Keywords: Coronagraph, jitter, reaction wheels, attitude control system, pointing control system, image control.

1. INTRODUCTION
The Terrestrial Planet Finder (TPF) is one of the proposed missions under NASA’s Origins Program, aimed to search for habitable extra-solar planets and life beyond Earth. Currently there are two promising architectures viable for extra-solar planet detection: visible-light coronagraph, and infrared interferometer. The studies described in this paper focus on the Coronagraph architecture that meets the minimum science requirement. For this mission, the system must suppress the bright light generated from the planet’s star, allowing the fainter, reflected light from the planet to be observed. To provide the requisite contrast ratio, the dynamic stability of the system must be maintained in the sub-milliarcsecond/sub-micrometer level, despite the presence of structural vibration and perturbations caused by internal mechanisms and external disturbances.

The design effort is currently carrying two design options for suppression of induced jitter: passive isolation and active isolation. Both concepts are designed to limit energy transmission from a dynamically noisy host structure (the support module) to a quiet payload carrying all of the optics. The passive isolation design uses soft flexures to reduce the transmission of energy from the disturbances to the optics. The active design actively decouples the payload from the disturbances. In this paper, we focus on the Flight Baseline Cycle 1 (FBC1) passively isolated pointing control system (PCS) for TPF Coronagraph. The goals of the analysis are to compare the predicted jitter with allocated jitter; to hand off RMS optical jitter to the optical modeling team for contrast simulation; and to generate engineering requirements for actuator stroke, bandwidth, and resolution, control system sample rates and gains, and sensor noise and bandwidth.

The paper first presents the requirements on jitter suppression, and outlines the passive isolation design. Once the PCS is defined, an integrated model can be formed by incorporating dynamic models from various disciplines, including structures, optics, and controls. Such a model allows us to perform end-to-end analyses and to predict the behavior of rigid body motion, image motion, and wave front error (WFE) from different disturbance sources. The focus of this paper is on flowing the disturbances through a frequency domain model of the system to structural, optical, and contrast responses.

In Section 2, the overall PCS design and related engineering requirements are presented. Following the general description of the system, a brief summary of the component models used in the integrated model is given in Section 3.
After obtaining a suitable integrated model, the attention turns to evaluating the performance of the integrated system. The equations that flow optical responses to contrast are summarized in Section 4 and the results from the linear model jitter analysis is presented in Section 5. Finally, summary of our analysis results and future work are provided in Section 6.

2. POINTING CONTROL SYSTEM DESIGN

The following subsections present the top level PCS requirements and the FB1 passive isolation design.

2.1. Requirements

The top level jitter requirements are formulated in terms of contrast. The contrast has contributions from the following sources:

- Line of sight (centration) error: motion of the centroid on the occulting mask. The FB1 model uses a linear mask aligned with the long axis of the Primary Mirror, so that only the centroid motion in the X axis influences the contrast.
- Beam walk: motion of the chief ray along each of the optical elements.
- Aberrations: distortion of the wavefront at the mask, caused by relative motion of the optical elements ("structural deformation") and bending of the optical elements ("optical deformation"). For the Flight Baseline Cycle 1, only deformation of the Primary is considered.
- Mask error: due to wavefront error at the mask.

The error budget defines requirements on physical motion of the telescope in terms of rigid body pointing (RBP) of the telescope, 6-DOF rigid-optics motion of the 21 optical elements, and deformation of the first 4 mirrors in terms of RMS-normalized Zernike amplitudes. Physical motions are then flowed to optical metrics. The optical metrics are then flowed to contrast contributions. The error budget assumes that optical motions are independent. The requirements on each of the contrast sources are given in Table 2-1. Contrast is defined as the ratio of light intensities, so is unitless.

2.2. TPF-C system overview

The TPF-C Flight Baseline 1 (FB1) design consists of an optical payload supported by a host spacecraft termed the "support module" (Figure 2-1). The support module provides power, communications, coarse attitude control, and passive thermal control. Dynamically significant components of the support module entail solar arrays, reaction wheels and a solar sail, and a sunshield, respectively. The payload encompasses an optics train consisting, in the FB1 design, of 21 optics running from an 8m by 3.5m elliptical primary, to a Secondary Mirror (SM) mounted at the tip of a 12m tower, through the remaining optics to the occulting mask. The payload and support module are connected by cables for power and data, as well as the isolation system (either passive or active). This paper will concentrate on the passive design alternative.

<table>
<thead>
<tr>
<th>Contribution</th>
<th>Requirement</th>
</tr>
</thead>
<tbody>
<tr>
<td>Beam walk</td>
<td>1.9e-012</td>
</tr>
<tr>
<td>LOS jitter</td>
<td>9.0e-014</td>
</tr>
<tr>
<td>LOS mask error</td>
<td>5.5e-013</td>
</tr>
<tr>
<td>Structural Deformation aber.</td>
<td>2.8e-017</td>
</tr>
<tr>
<td>SD aber. maskerror</td>
<td>1.7e-017</td>
</tr>
<tr>
<td>Optical deformation aber.</td>
<td>8.5e-013</td>
</tr>
<tr>
<td>OD aber. maskerror</td>
<td>5.2e-015</td>
</tr>
<tr>
<td>Total</td>
<td>3.4e-012</td>
</tr>
</tbody>
</table>
2.3. Staged pointing control
The PCS must maintain the physical motions of the optical elements, and the position of the centroid on the mask, to
within the requirements. The design approach is to locate intrinsically noisy components, such as reaction wheels, on a
noisy platform, and then limit the energy transmission into the optical payload. An image control system is then used to
actively control residual pointing error.

2.4. Passive isolation
Passive isolation is used to attenuate disturbance energy transmission from the reaction wheels to the telescope. The
passive isolation design effort focused on the need to apply realistic constraints to the performance of a passive isolator,
while not introducing excessive conservatism. The approach was to identify the limits to passive isolator performance,
model each effect (or demonstrate that the effect could be designed around), and tie the design to published
specifications of existing designs.

2.4.1. Limits to passive isolator performance
The general response of a passive isolator is that of a low-pass filter. Simple models of passive isolators show a
40dB/decade attenuation above the break frequency. Physical isolators exhibit an “isolation floor” where the
transmissibility rolls from 40dB/decade to (approximately) flat. There are four effects that drive isolator performance
away from the 40dB/decade attenuation of the simplified isolator model:

- “lockup” of the isolator damper: a pure damper acts as a rate feedback that transmits force with a
  +20dB/decade gain compared to a pure spring.
- non-ideal response of the payload and spacecraft structures: the simple damper model applies when the
  payload and structure roll off at 40dB/decade. A structure will roll off between 10 and 30 dB/decade above its
first mode. If the payload and spacecraft roll off at an average 20dB/decade each, the transmissibility from 
disturbances, through both structures and the isolator, to the sensitive location, will be flat.

- geometry: the hexapod arrangement of a typical isolator leads to coupling between the isolators that leads to a 
floor at high frequency
- cross-axis modes of the isolator: these modes can couple into the axial response, leading to localized high 
frequency amplification.

The TPF-C passive isolation design deals with these effects in the following manner. Damper lockup can be controlled 
by introducing a spring in series with the damper, that effectively filters high frequency energy transmission. The latter 
three effects are captured in the TPF-C analysis through the use of a physical isolator model that couples the payload 
and spacecraft, and that includes the cross-axial modes of the isolator.

The TPF-C isolator stages are placed between the Reaction Wheel Assembly (RWA) and the spacecraft, and between 
the payload and the spacecraft. An alternative design would place individual isolators on each reaction wheel, in place 
of the RWA isolator. The advantages of the RWA isolator are that it increases the suspended mass, enabling a lower 
break frequency, and that it requires fewer isolators, which should lower the cost.

2.4.2. Reaction wheel assembly isolation

The RWA isolator is a hexapod design using struts based on Honeywell D-struts\(^4\). The RWA mass is 61.4 kg, and the 
target frequency is 1.5 Hz. Each strut is modeled in NASTRAN with 3 nodes, two CBAR elements, two CONM2 
elements, and 12 CELAS2 lumped stiffnesses. A 4,2000 N/m flexure is assumed. The strut has a first bending (cross-
axis) mode of 102 Hz.

2.4.3. Payload isolation

For the FB1 design, the payload isolator is modeled as a set of 3-axis springs at each of the spacecraft/support module 
attachment locations. The springs are 30,000 N/m each.

2.5. Image stabilization

The image stabilization system uses several nested active control loops to remove residual LOS error, due to 
disturbances that propagate through the isolators.

2.5.1. Active control architecture

The active control system uses a Fine Guidance Sensor (FGS) that senses light reflected from the mask to measure 
centroid position. Since most of the light from the target star is reflected, the FGS readout rate can be relatively high, 
between 100 and 500 Hz. The FB1 design uses the Secondary Mirror, in addition to the Steering Mirror, as a LOS 
control actuator for the following reason. The 8th order mask significantly reduces sensitivity to wavefront error, so that 
the largest contrast contributor is beam walk along the optics. Beam walk is defined by the chief ray, which by 
definition goes through the center of the Deformable Mirror. If the Secondary Mirror is then used to center the spot on 
the occulting mask in the presence of a rigid body pointing angle, the chief ray will have zero beam walk on all optics 
downstream of the SM. Since 

The bandwidth of the SM is limited by the structural response of the tower, a Fine 
Guidance Mirror is required 
to control high frequency 
LOS errors. The FGM is 
small and light enough that it 
does not interact significantly 
with structural modes, and 
therefore the bandwidth can 
approach the sample-rate- 
constrained limit of 10-50 
Hz. The SM and FGM only 
control relative motion 
within the telescope, so 
reaction wheels are required 
to reject external disturbance

<table>
<thead>
<tr>
<th>Control loop</th>
<th>Parameter</th>
<th>Value</th>
<th>Sample Freq.</th>
<th>Margins</th>
<th>Bandwidth</th>
</tr>
</thead>
<tbody>
<tr>
<td>FGM</td>
<td>Break freq.</td>
<td>1 Hz</td>
<td>500 Hz</td>
<td>7.01dB</td>
<td>25.1 Hz</td>
</tr>
<tr>
<td></td>
<td>Lead</td>
<td>45°</td>
<td></td>
<td>25.6°</td>
<td></td>
</tr>
<tr>
<td>SM</td>
<td>Break freq.</td>
<td>0.001 Hz</td>
<td>1000 Hz</td>
<td>49.11 dB</td>
<td>0.1 Hz</td>
</tr>
<tr>
<td></td>
<td>Lead</td>
<td>45°</td>
<td></td>
<td>45.7°</td>
<td></td>
</tr>
<tr>
<td>ACS</td>
<td>Crossover</td>
<td>0.016 Hz</td>
<td>2 Hz</td>
<td>9.3 dB</td>
<td>0.043 Hz</td>
</tr>
<tr>
<td></td>
<td>Integral T.C. ratio</td>
<td>0.075</td>
<td></td>
<td>34.8°</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Estimator freq.</td>
<td>10 Hz</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Elliptical order</td>
<td>3</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Elliptical ripple</td>
<td>1 dB</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Elliptical atten.</td>
<td>30 dB</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Elliptical freq.</td>
<td>0.56 Hz</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>RW speed</td>
<td>Bandwidth</td>
<td>1 Hz</td>
<td>100 Hz</td>
<td>1 Hz</td>
<td></td>
</tr>
<tr>
<td>control</td>
<td>Lead</td>
<td>60°</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 2-2 Control system parameters.
torques and offload the FGM and SM at low frequency.

2.5.2. Control modes

The PCS must operate in several modes during acquisition and imaging. In the coarse (slewing) mode, when the telescope is retargeted to a new star, the attitude sensors consist of Star Trackers for attitude and gyros for rate. In the acquisition mode, the telescope uses Payload Star Acquisition Cameras to center the star in the FGS field of view. In the fine (imaging) mode, the staged image stabilization control system described above is operational.

2.5.3. Fine Guidance Mirror control

The FGM control consists of a second order low pass filter with a lead compensator. The bandwidth is 25 Hz for the FB1 design, in order to control LOS errors introduced by a pair of 10 Hz modes. The filter break frequency is 1 Hz, and the damping ratio is 0.707.

2.5.4. Secondary Mirror control

The SM controller also consists of a second order low pass filter with lead. The break frequency was set to 0.001 Hz in order to suppress thermally induced SM-PM relative motion. The bandwidth was initially set to 1 Hz to offload the FGM, however the laser truss sensor noise (which was amplified by the SM control loop in the 1-5 Hz range) excited the isolator modes in the 1-4 Hz range. The SM bandwidth was dropped to 0.1 Hz.

2.5.5. Attitude control

The attitude control system is a Proportional-Integral-Derivative (PID) design that was developed for the Next Generation Space Telescope Yardstick design. It uses structural filters to suppress the first flexible modes of the structure. The bandwidth is 0.016 Hz.

![Figure 2-2 TPF-C integrated model configured for passive isolation.](image-url)
3. INTEGRATED MODEL DESCRIPTION

The integrated model is a fully coupled mathematical model of the dynamics of the FB1 design. The integrated model describes structural, optical, and contrast responses in the presence of dynamic disturbances. This section presents the components of the model.

3.1. Integrated model overview

The integrated model is shown in Figure 2-2. It consists of a structural plant model, optics, controllers, and additional component models.

3.2. Structure model

The structure model is a Finite Element model generated by JPL and GSFC. It is provided in the form of Normal Modes frequencies and modeshapes. The Normal Modes model is converted to a state space model that maps physical inputs to nodal responses. Damping is modeled using modal damping on a component level, and allocated to the structural modes using a Strain Energy Fraction approach:

$$\zeta_i = \sum_j F_{ij} \zeta_j$$

where \(\zeta_i\) is the modal damping for mode \(i\), \(F_{ij}\) is the element strain energy fraction in mode \(i\) for component \(j\), and \(\zeta_j\) is the modal damping ratio for component \(j\). Damping values are based on a best estimate with a knockdown factor, and are tabulated in Table 3-1. The knockdown factors are lower when there is published data for a similar component, and higher in the absence of data.

The full order model has 7218 modes from 0 to 300 Hz. Two reduced order models were used. A 1000 mode model was used for design, and a 2000 mode model for analysis. Reduction was accomplished using tools in the DOCS Toolbox.

3.3. Optics model

The optics model is provided in the form of linear sensitivity matrices that map motions of the optical nodes of the FEM to optical responses: LOS, beam walk, and wavefront error (aberration). The LOS optical model gives motion of the centroid on the occulting mask, which is converted to an angle on the sky using the system focal length. The beam walk sensitivities give the motions of the chief ray on each of the 21 optics, as a function of rigid-optic motion of each of the optics. The Structural Deformation and Optical Deformation sensitivities give the wavefront error aberration, in Zernike amplitude normalized to unity RMS, from, respectively, rigid motion of the optical elements, and distortion of the Primary Mirror. Distortion of the downstream mirrors is budgeted but was not analyzed in the FB1 cycle.

3.4. Component models

The integrated model also includes several components that are modeled separately in order to allow for parametric sweeps, and to model various sensing and computational processes.

3.4.1. Secondary mirror and fine guidance mirror

The SM and FGM are represented as position-controlled dynamic systems. For example, a piezoelectric steering mirror would transform a voltage command into an angular position change. The motion of the mirror would also generate a reaction force back into the structure. The devices also generate a constant position noise (and accompanying reaction force) as a result of electrical noise in the drive electronics.

3.4.2. Metrology

The laser truss metrology system measures the relative motion of the SM and PM by sending laser legs through retroreflectors on the SM and PM. The length change of the legs is transformed into relative motion. The measurement should be possible at very high frequency (>1kHz) so a static gain matrix is used to relate corner cube motions to SM-PM motion.

3.4.3. Reaction wheel speed control

The reaction wheel speed controllers are used to reduce the effects of spin-axis disturbances, most significantly torque noise. The wheel speed controllers use a tachometer to drive the wheels at a commanded spin rate, which reduces spin-axis disturbances below the controller bandwidth, at the cost of amplification above the bandwidth, and of tachometer noise.

Table 3-1 Nominal component damping values.

<table>
<thead>
<tr>
<th>Component</th>
<th>Best estimate</th>
<th>Knock down</th>
<th>Nominal value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Payload isolator</td>
<td>5%</td>
<td>2.0</td>
<td>2.5%</td>
</tr>
<tr>
<td>RWA isolator</td>
<td>5%</td>
<td>1.2</td>
<td>4.17%</td>
</tr>
<tr>
<td>Sunshield</td>
<td>1%</td>
<td>3.0</td>
<td>0.33%</td>
</tr>
<tr>
<td>Bus</td>
<td>0.5%</td>
<td>5.0</td>
<td>0.1%</td>
</tr>
<tr>
<td>OTA</td>
<td>0.5%</td>
<td>5.0</td>
<td>0.1%</td>
</tr>
</tbody>
</table>
which contaminates the wheel command. The speed controller is implemented as an integral filter with a lead controller, with a bandwidth of 1 Hz and 60 degrees of lead. The tachometer is sampled at 100 Hz.

### 3.4.4. Estimator

The estimator provides the measured attitude signal to the ACS control, with the measurement derived from the appropriate sensor for the control mode. Selection of the control mode also feeds the correct sensor noise source into the estimator. The estimator is realized as a static gain matrix.

### 3.4.5. FGM, SM, and ACS controllers

The controllers are represented as state space systems that map sensor signals to control signals. All controllers include Padé approximations of the sample delay.

### 3.5. Disturbance Models

The disturbances acting on TPF-C are generally random processes that can be modeled as colored noise. The exceptions are the reaction wheel spin-rate-dependent forces, which are modeled using discrete tonal forces.

#### 3.5.1. Reaction wheel spin-rate-dependent forces

The RW imbalance forces are modeled as a sum of sinusoidal disturbances at harmonics of the wheel speed:

$$d(t) = \sum_{i=1}^{N_h} C_i f_{rw}^i \sin(2\pi h_i f_{rw} t + \phi_i)$$

where $C_i$ is the amplitude coefficient, $f_{rw}$ is the reaction wheel speed, $h_i$ is the $i$th harmonic, and $\phi_i$ is the phase associated with the $i$th harmonic.

#### 3.5.2. Sensor noise

The various sensor noises are modeled as sampled continuous time white noise. The sampling process is approximated by a 1-pole continuous time low pass filter. The filter matches the DC magnitude of the noise, so it over-predicts the noise.

#### Table 3-2 Actuator noise parameters.

<table>
<thead>
<tr>
<th>Noise source</th>
<th>Noise level</th>
<th>Bandwidth</th>
</tr>
</thead>
<tbody>
<tr>
<td>SM position error</td>
<td>0.02 nm RMS</td>
<td>0-50 Hz</td>
</tr>
<tr>
<td></td>
<td>0.02 nrad RMS</td>
<td></td>
</tr>
<tr>
<td>FGM position error</td>
<td>10 masec RMS</td>
<td>0-250 Hz</td>
</tr>
<tr>
<td>Torque noise</td>
<td>6e-4 N-m/Hz$^{1/2}$</td>
<td>0.1-1 Hz</td>
</tr>
</tbody>
</table>

#### Table 3-3 Sensor noise parameters.

<table>
<thead>
<tr>
<th>Noise source</th>
<th>RMS noise level</th>
<th>Bandwidth</th>
</tr>
</thead>
<tbody>
<tr>
<td>FGS</td>
<td>0.005 masec (X-axis)</td>
<td>500 Hz</td>
</tr>
<tr>
<td>Laser dθ/f</td>
<td>1e-9 Hz/Hz</td>
<td>1 kHz</td>
</tr>
<tr>
<td>Laser dL</td>
<td>25 nm</td>
<td></td>
</tr>
<tr>
<td>Kalman filter</td>
<td>0.120 masec</td>
<td>2 Hz</td>
</tr>
<tr>
<td>Star Tracker</td>
<td>1.35 asec</td>
<td>2 Hz</td>
</tr>
<tr>
<td>Gyro</td>
<td>6.8e-5 asec/sec$^{1/2}$</td>
<td>2 Hz</td>
</tr>
<tr>
<td></td>
<td>0.01 asec/sec$^{1/2}$</td>
<td></td>
</tr>
<tr>
<td>PSAC</td>
<td>0.135 asec</td>
<td>2 Hz</td>
</tr>
<tr>
<td>Tachometer</td>
<td>1e-3 rad/sec</td>
<td>100 Hz</td>
</tr>
</tbody>
</table>

Figure 3-1 Left, RMS SM position noise, translation (solid) and rotation (dotted). Right, FGM position error.
RMS noise by 25%. Sensor noises are assumed on the Fine Guidance Sensor, laser truss for SM position measurement (due to measurement error and frequency error), Star Tracker and gyro, PSAC, and RW tachometer. In coarse mode, the Star Tracker and gyro are combined using a Kalman Filter that lowers the noise level. The sensor noise values are given in Table 3-3.

3.5.3. Actuator noise
The feedback actuators are all subject to various non-idealities that inject noise into the plant. The reaction wheels have a number of characteristics that create spin-axis forces. The TPF-C Minimum Mission analysis showed that one of the strongest drivers was torque noise.

The two mirrors that are actively controlled are also subject to position noise. The amplifiers that provide the high voltage signals are subject to electronic noise, that feeds through the actuators to generate a position noise. The noise bandwidth is set by the resonance of the device. Figure 3-1 plots the assumed position noise spectra for (left) the secondary mirror actuators, and (right) the Fine Guidance Mirror. The actuator noise values are tabulated in Table 3-2.

3.6. Analysis tools
The structural model is developed in NASTRAN. The optical sensitivity matrices are created in MACOS. The model is integrated and analyzed in MATLAB® using the DOCS® Toolbox.

4. PERFORMANCE MODELING

4.1. Structural and optical responses
The RW analysis is conducted using a discrete wheel speed analysis. The disturbances are represented in the frequency domain and applied to the frequency response function (FRF) of the structure to predict the complex-valued optical performance:

\[ d(j\omega_i) = C_i f_{RW}^2 \delta(j\omega_i) e^{j\omega_i} \]

\[ z(j\omega) = \frac{1}{\sqrt{2}} \sum_{i=1}^{N_h} G_{zd}(j\omega_i) d(j\omega_i) \]

where \( \omega_i = 2\pi f_{RW} h_i \), \( \delta(\cdot) \) is the dirac-delta function, \( N_h \) is the total number of harmonics used, and \( G_{zd} \) is the frequency response function from wheel disturbance \( d \) to optical performance \( z \). The sensor noise analysis is conducted using a continuous PSD analysis:

\[ S_z(j\omega) = G_{zd}(j\omega) S_{zd}(j\omega) \]

\[ \Sigma_z = \frac{1}{2\pi} \int S_z(j\omega) d\omega \]

where \( S_z \) is the disturbance PSD, \( G_{zd} \) is the frequency response function from the disturbance to the optical performance, and \( \Sigma_z \) is the covariance of the optical response.

4.2. Model uncertainty
The predicted structural and optical responses were multiplied by a frequency dependent Model Uncertainty Factor that reflects the potential model error in the different components of the system. The low frequency (0-20 Hz) value was 3, above 40 Hz the value was 10, with a linear transition 20-40 Hz. The MUF levels were chosen on a component level, based on the maturity of the component (high for the RWA isolator, low for the telescope) and RSSed.

4.3. Contrast computations
The contrast degradation from the predicted optical response is generated using the following equations, taken from the TPF-C error budget.

4.3.1. LOS
The contrast degradation produced by image jitter, \( \sigma \), and offset \( \Omega \), is given by

\[ C_{LOS} = c_1 \sigma^4 \Omega^4 + c_2 \sigma^6 \Omega^2 + c_3 \sigma^2 \Omega^6 + c_4 \sigma^8 + c_5 \Omega^8 \]

This equation was developed using Monte Carlo simulation and a curve fit.
4.3.2. Beam walk

The beam walk contrast degradation for a particular optic is given by

\[ C_{BW,j} = A \frac{\sigma_x^2 + \sigma_y^2 + \sigma_z^2}{\Delta \sigma_x^2} \]  

(6)

where the \( A \) constant is derived from an area integral of surface roughness, \( \sigma_x, \sigma_y, \sigma_z \) are the RMS motions across the optic in the X, Y, and Z axes respectively, and \( \Delta \sigma_x \) is a normalizing wavelength. The beam walk contrasts are computed individually for each of the 21 optics, and summed to produce a total contrast.

4.3.3. Aberrations

Contrast due to Structural Deformation and Optical Deformation aberrations are both computed using a polynomial fit:

\[ C_j = 10^a \left( \frac{Z_{rms,j}}{\lambda \cdot 10^{10}} \right)^{p_j} \]  

(7)

where \( Z_{rms,j} \) is the RMS amplitude of Zernike mode \( j \) in Angstroms, \( \lambda \) is the wavelength in meters, and \( a_j \) and \( p_j \) are the polynomial coefficients.

4.3.4. Mask errors

The mask error contrast is a polynomial in the Zernike amplitude, given by:

\[ C_{ME,j} = \left( \frac{Z_{rms,j}}{\lambda \cdot 10^{10}} \right)^{4 a_j \Delta M} \]  

(8)

where \( Z_{rms,j} \) is the RMS amplitude of Zernike mode \( j \) in Angstroms, \( \lambda \) is the wavelength in meters, \( a_j \) and \( p_j \) are the polynomial coefficients, and \( \Delta M = 1e-3 \). The mask error contrast due to LOS can be computed using the same equation, using a scale factor, 1.9582, from radians to Zernike RMS amplitude in tip/tilt.

5. JITTER ANALYSIS

The following sections present the predicted contrast due to jitter for the FB1 design.

5.1. Optical element jitter

The rigid body pointing (RBP) versus wheel speed of the closed loop system is shown in Figure 5-1, for the body X (solid), body Y (dashed), and body Z (dotted). The maximum response above the minimum wheel speed of 3 RPS is 0.7 masec for the X-axis rotation. The peak RBP allocation depends on the authority of the secondary mirror control loop, and ranges from 4 masec at low frequency (where the SM is active) to 0.04 masec when the SM is effectively uncontrolled.

The peak RMS motions of the optical elements under the RW disturbance are plotted in Figure 5-2. The upper left plot shows the RMS translations in nanometers, while the upper right plot shows the RMS rotations in nano-radians. The legend calls out the peak response frequency. The motions are defined relative to the PM, so the PM response is 0. The requirements on the SM are 5 nm or lower in 3 axes of translation, and 5 nrad or lower in 3 axes of rotation. The responses are significantly higher, 57.6 nm at the 1st Y tower bending mode, and 71.5 nm at the 1st X tower bending mode. The rotation ranges from 4.8 to 7.1 nrad depending on the axis. The downstream optics are below the requirement of 10 nrad per axis in rotation, and 100 nm per axis in translation. The net effect will depend on the resulting contrast, which is driven primarily by the beam walk term.
Figure 5-2 Jitter predictions under RW disturbance. Upper left, RMS translations of the optics. Upper right, RMS rotations. Lower left, RMS SD Zernike amplitudes. Lower right, RMS PM Zernike amplitudes.

The lower two plots show the Zernike amplitudes from structural deformation (left) and PM deformation (right). The dashed lines plot the requirements. The structural deformation aberrations are above the requirement by about a decade. The primary mirror deformation exceeds the requirement at the higher Zernike modes. The exceedances are not as problematic as the SM motion since the aberration contributions to contrast are about two orders of magnitude below the beam walk.

5.2. Jitter induced contrast
The peak jitter induced contrast is summarized in Table 5-1. The columns indicate the disturbance source, and the rows indicate the contrast contribution. The last column gives the requirement for each contribution, and for the total contrast.

The largest contrast contributions are the beam walk, and the primary mirror deformation. The largest contributor by disturbance source is the RW imbalance. Next largest is the RW torque noise, followed by the secondary mirror position error. The next section looks at design alternatives that would reduce reaction wheel imbalance induced contrast.

5.3. Jitter sensitivities
The baseline passive PCS design was perturbed in order to assess the performance sensitivity. The parameters were chosen based on a combination of anticipated influence on the cost, and ease of modification. Four parameters were chosen:
Table 5-1 FB1 jitter induced contrast.

<table>
<thead>
<tr>
<th></th>
<th>PSAC noise</th>
<th>FGS noise</th>
<th>Tach noise</th>
<th>FGM posn</th>
<th>SM posn</th>
<th>Laser truss</th>
<th>RW torque noise</th>
<th>RW imb.</th>
<th>Total</th>
<th>Req</th>
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<tr>
<td>Beam walk</td>
<td>0.00</td>
<td>9.5e-17</td>
<td>5.3e-14</td>
<td>2.1e-13</td>
<td>3.0e-14</td>
<td>2.9e-15</td>
<td>1.0e-12</td>
<td>7.7e-12</td>
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<tr>
<td>LOS</td>
<td>1.2e-20</td>
<td>1.2e-20</td>
<td>1.2e-20</td>
<td>2.2e-15</td>
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<td>8.1e-17</td>
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<td>6.4e-14</td>
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<td>5.5e-13</td>
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<tr>
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<td>2.0e-18</td>
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<tr>
<td>PM deform</td>
<td>0.00</td>
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<td>2.0e-17</td>
<td>2.6e-16</td>
<td>1.7e-12</td>
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<tr>
<td>PM maskerr</td>
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<td>8.3e-20</td>
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<td>1.1e-12</td>
<td>8.0e-12</td>
<td>1.2e-11</td>
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</tr>
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</table>

1. FGM reacuation: an equivalent inertia can be driven 180° out of phase with the FGM, partially canceling the reaction force on the structure. This is commonly required for high performance optical systems, since the FGM acts as a high frequency disturbance source on the quiet side of the isolator.

2. SM reacuation: the secondary mirror assembly (SMA) for the baseline design is significantly over its mass budget, necessitating a redesign, so the effect on dynamic performance is an important question.

3. 20 Hz SM bandwidth: this will reduce the beam walk contribution from the tower modes at 5Hz. In order to maintain loop stability, the SM must be decoupled from the tower modes using SM reacuation.

4. 2% damping in the tower 1st and 2nd modes at 5 and 10 Hz: a passive damping treatment can reduce the dynamic amplification in these regions.

The sensitivity study looked only at the RW imbalance disturbance, since this is the largest contrast contributor. The sensitivity study was performed on a reduced order (250 mode) model, so the results are slightly different for the nominal.

The contrast predictions for the nominal design and four perturbed designs is given in Table 6-1. The columns give the design case, and rows give the contrast contribution. The last column gives the contrast requirement. The FGM reacuation does not change the contrast prediction at all. This is an indication that the FGM inertia is so low that the reaction forces are negligible. The next perturbation, SM reacuation, actually increases several of the contrast contributions. This results from a shift in a critical mode frequency, that causes it to couple more strongly to an adjacent mode and therefore to increase in magnitude. The conclusion is that lightweighting the SMA, while desirable from the standpoint of increasing the tower mode frequencies, will not change the induced vibration significantly, because of the low bandwidth of the SM loop. This conclusion could change if the SM loop bandwidth were increased. The 20Hz SM loop does reduce the beam walk contrast. However, the PM deformation contribution is unaffected (it increases due to the SM reacuation), so the total contrast is not reduced enough to meet requirements. The tower damping case significantly reduces the contrast. Under this scenario, the total contrast would drop to 3.85e-12.

6. CONCLUSIONS AND FUTURE WORK

The paper has presented a snapshot of the FBI passive jitter design activities. The results show that the current system does not meet requirements, but a number of promising design modifications might lead to a feasible design. They include:

- Passive damping treatments. In addition to reducing the nominal contrast, this would represent a significant risk buydown, by augmenting the highly uncertain inherent structural damping with a linear damping mechanism that could be well characterized prior to flight.
- Noise filtering. The large contribution from the SM position noise could be reduced by filtering the drive amplifier output above the SM control bandwidth.

In addition, a number of additional sensitivity studies are planned to examine:
• damping assumptions
• control system optimization (of the loop shaping designs as well as a modern optimal control system)
• parameter uncertainty, including variability in critical structural stiffnesses
These sensitivity studies will address system optimization for cost and risk.

ACKNOWLEDGEMENTS
The authors would like to thank Andy Kissil at JPL and Sandra Irish at GSFC for support with the structural modeling, Philip Dumont at JPL for assistance with the optical modeling, and Stuart Shaklin at JPL with support for the error budgeting.

REFERENCE


Table 6-1 RW jitter sensitivities.

<table>
<thead>
<tr>
<th>Design case</th>
<th>Nominal</th>
<th>Reactuated FGM</th>
<th>Reactuated SM</th>
<th>20 Hz SM</th>
<th>2% Twr Damping</th>
<th>Req</th>
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<td>Beam walk</td>
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<td>7.77e-12</td>
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