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Reexamination of Ball-Race Conformity Effects on Ball Bearing Life

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Abstract

G. Lundberg and A. Palmgren in 1947 established the primary relation between rolling-element bearing geometry and bearing life. Their analysis of ball and roller bearings did not consider the life of the bearing's set of rolling elements independent of race life. The analysis in this report considers the life of the ball set as well as the respective lives of the races to reassess the effect of ball-race conformity on ball bearing life. The related changes in ball bearing life are incorporated in life factors that can be used to modify the bearing predicted life using the Lundberg-Palmgren equations and the ANSI/ABMA and ISO Standards. Two simple algebraic relationships were established to calculate life factors LF_c to determine the effect of inner- and outer-race conformity combinations on bearing L_{10} life for deep-groove and angular-contact ball bearings, respectively. Depending on the bearing type and series as well as conformity combinations, the calculated life for deep-groove ball bearings can be over 40 percent less than that calculated by the Lundberg-Palmgren equations. For angular-contact ball bearings, the life can vary between +16 and -39 percent from that calculated by the Lundberg-Palmgren equations. Comparing the two ball bearing types, the life factors LF_c for the deep-groove bearings can be as much as 40 percent lower than that for angular-contact ball bearings. The use of a fatigue limit from either the program ASMELIFE or the proposed ISO 281:2006 standard can significantly overpredict bearing life over a range of normal operating Hertz stresses, which can result in the selection of undersized bearings for a particular application.

Nomenclature

- *a* semimajor axis of contact ellipse, m (in.)
- **B** total curvature, m (in.)
- **b** semi-minor axis of contact ellipse, m (in.)
- *C_D* dynamic load capacity, N (lbf)
- *c* stress-life exponent
- **D** distance between centers of curvature of inner and outer races, m (in.)
- D_{ir} raceway diameter at ball-race contact of inner race, m (in.)
- **D**_{or} raceway diameter at ball-race contact of outer race, m (in.)
- *d* ball diameter, m (in.)
- d_e pitch diameter, m (in.)
- *e* Weibull slope

conformity, percent or fractional percent
bearing geometry and geometry coefficient
exponent
number of rows of balls
geometry-load constant
life, number of stress cycles or hr
10-percent life or life at which 90 percent of a population survives, number of stress cycles or hr
characteristic life or life at which 63.2 percent of population fails, number of stress cycles or hr
life factor
race track length, circumference of ring at ball contact, m (in.)
life, number of stress cycles
Hertz stress-life exponent
diametral clearance, m (in.)
equivalent radial load, N (lbf)
normal load of maximum loaded ball in deep-groove ball bearing, N (lbf)
normal load on ball in angular-contact ball bearing, N (lbf)
normal load, N (lbf)
load-life exponent
race-groove radius, m (in.)
probability of survival, fraction or percent
maximum Hertz stress, GPa (ksi)
stressed volume, m ³ (in. ³)
load-life exponent, $w = pe$
ratio of outer-race life to inner-race life, L_{or}/L_{ir}
number of balls in bearing
depth to the maximum orthogonal shearing stress, m (in.)
free contact angle
transcendental function from Hertz theory
transcendental function from Hertz theory
critical shearing stress, GPa (ksi)
fatigue limit, GPa (ksi)
orthogonal shearing stress, GPa (ksi)
ipts:
conformity

- i i^{th} component
- *ir* inner race
- *m* modified based on race conformity
- or outer race
- *re* rolling element (ball)

Introduction

By the close of the 19th Century, the bearing industry began to focus on sizing of bearings for specific applications and determining bearing life and reliability. In 1896, R. Stribeck (ref. 1) in Germany began fatigue testing full-scale bearings. J. Goodman (ref. 2) in 1912 in Great Britain published formulae based on fatigue data that would compute safe loads on ball and cylindrical roller bearings. In 1914, the "American Machinists Handbook and Dictionary of Shop Terms" (ref. 3), devoted 6 pages to rolling-element bearings that discussed bearing sizes and dimensions and recommended (maximum) loading at specified speeds. However, the publication (ref. 3) did not address the issue of bearing life. During this time, it would appear that rolling-element bearing fatigue testing was the only way to determine or predict the minimum or average life of ball and roller bearings.

In 1924, A. Palmgren (ref. 4) in Sweden published a paper in German outlining his approach to bearing life prediction and an empirical formula based upon the concept of an L_{10} life or the time that 90 percent of a bearing population would equal or exceed without failure. During the next 20 years he empirically refined his approach to bearing life prediction and matched his predictions to test data (ref. 5). However, his formula lacked a theoretical basis or an analytical proof.

In 1939, W. Weibull (refs. 6 and 7) in Sweden published his theory of failure. Weibull was a contemporary of Palmgren and shared the results of his work with him. Palmgren in concert with G. Lundberg, also of Sweden, in 1947 incorporated his previous work along with that of Weibull and what appears to be the work of V. Thomas and H. Hoersch (ref. 8) into what has become known as the Lundberg-Palmgren theory (refs. 9 and 10). (In 1930, V. Thomas and H. Hoersch (ref. 8) at the University of Illinois, Urbana, developed an analysis for determining subsurface principal stresses under Hertzian contact (ref. 11). Lundberg and Palmgren (refs. 9 and 10) do not reference the work of V. Thomas and H. Hoersch (ref. 8 in their papers.)

Lundberg and Palmgren (refs. 9 and 10) established the primary relation between bearing geometry and bearing life. For ball bearings they related bearing life to five variables. These are ball diameter, pitch diameter, inner- and outer-race conformities, number of balls, and contact angle. Except for bearing contact angle, the relation between these parameters remains the same regardless of whether the bearing is a deep-groove ball bearing or an angular-contact ball bearing. These relations have been incorporated into both the International Organization for Standardization (ISO) and the American National Standards Institute (ANSI)/American Bearing Manufactures Association (ABMA) standards (ABMA was formerly AFBMA, Anti-Friction Bearing Manufactures Association) for the load ratings and life of rollingelement bearings (refs. 12 to 14) as well as in current bearing codes to predict life.

The Lundberg-Palmgren equations only relate to the lives of the inner and outer races and incorporate ball life into their analysis by inference (ref. 9). It has since been recognized (ref. 15) that the life of the ball set in relation to the races is different for a deep-groove ball bearing and an angular-contact ball bearing as well as being dependent on the relative contact (Hertz) stresses at the inner and outer races. It is the objectives of the work reported herein to (a) consider the life of the ball set as well as the lives of the respective races to reassess the effect of ball-race conformities on ball bearing life and (b) incorporate the related changes in ball bearing life to life factors that can be used to modify the bearing predicted life using the Lundberg-Palmgren equations and the ANSI/ABMA and the ISO Standards.

Ball Bearing Geometry and Stresses

Bearing Geometry

While there are several types of ball bearings, there are two common basic types. These are the deepgroove ball bearing (figs. 1 and 2(a)) that is designed to handle primarily radial loads and the angularcontact ball bearing (fig. 2(b)) designed to handle primarily thrust loads. These bearings comprise a plurality of balls interspersed between an inner and outer race and separated and positioned by a cage or separator.



Figure 1.—Deep-groove ball bearing. (a) Schematic. (b) Cross section without cage.





The operating characteristics of a ball bearing are dependent its internal fitup measured by the diametral clearance (P_D) illustrated in the cross section schematic of figure 1(b) where

$$\boldsymbol{P}_{\boldsymbol{D}} = \boldsymbol{D}_{\boldsymbol{or}} - \boldsymbol{D}_{\boldsymbol{ir}} - 2\boldsymbol{d} \tag{1}$$

where D_{or} and D_{ir} are the raceway diameters at the ball-race contact of the outer and inner races, respectively, and d is the ball diameter. While diametral clearance is generally used in conjunction with single row deep-groove ball bearings, it is applicable to angular-contact ball bearings where there is a relation between diametral clearance P_D , race curvatures r_{ir} and r_{or} , and free contact angle β (ref. 16) (fig. 2(b)).

Where $P_D = 0$, the bearing pitch diameter is

$$d_e = \frac{D_{or} + D_{ir}}{2} \tag{2}$$

Referring to figure 2, the race conformity f is the ratio of the race-groove radius, or curvature, r to the ball diameter d in a plane passing through the bearing axis and transverse to the raceway and expressed as a percent or fractional percent (ref. 16) where

$$f = \frac{r}{d}$$
(3a)

The race-groove radius, or curvature, can be expressed as

$$\boldsymbol{r} = \boldsymbol{f}\boldsymbol{d} \tag{3b}$$

The distance between the centers of curvatures of two races in line contact with a ball is indicated by D in figure 2(a). It is a fixed quantity depending on race radii and ball diameter where

$$\boldsymbol{D} = (\boldsymbol{f}_{or} + \boldsymbol{f}_{ir} - 1)\boldsymbol{d} \tag{4a}$$

$$\boldsymbol{B} = (\boldsymbol{f}_{or} + \boldsymbol{f}_{ir} - 1) \tag{4b}$$

Then

$$\boldsymbol{D} = \boldsymbol{B}\boldsymbol{d} \tag{4c}$$

The quantity B is referred to as the "total curvature" and is a measure of the conformity of the inner and outer races (ref. 16). The computation of deflection in ball bearings under load is dependent on the value of the total curvature B (ref. 16).

Figure 2(b) is a schematic of a cross section of a ball in an angular-contact ball bearing showing a free contact angle β . The free contact angle is the contact angle of the bearing without load being applied. It is defined as "the angle made by a line passing through the points of contact of the ball and both raceways with a plane perpendicular to the axis of the bearing when both races are centered to each other and one race is axially displaced with respect to the other without the application of measurable force (ref. 16)." The free contact angle is determined by the diametral clearance, P_D , and the total curvature B, where

$$\cos\beta = \frac{2Bd - P_D}{2Bd}$$
(5a)

$$\boldsymbol{P}_{\boldsymbol{D}} = 2\boldsymbol{B}\boldsymbol{d} \left(1 - \cos \boldsymbol{\beta}\right) \tag{5b}$$

or

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Contact (Hertz) Stress

The contact (Hertz) stresses at the respective races of a bearing are a function of the bearing geometry, the normal load at the contact and the elastic properties of the bearing materials. Jones (ref. 16) relates the Hertz contact theory for the stresses of nonconforming bodies in contact for both ball and roller bearings. From Jones (ref. 16), the following relations for the maximum Hertz stresses S_{max} at the inner and outer races of ball bearings can be derived:

For deep-groove ball bearings with a radial load only,

$$S_{\max_{or}} = \frac{K \left[-\frac{2}{D_{or}} + \frac{4}{d} - \frac{1}{f_{or}d} \right]^{2/3} P_{\max}^{1/3}}{\mu v}$$
(6a)

for the outer race, and

$$S_{\max_{ir}} = \frac{K \left[\frac{2}{D_{ir}} + \frac{4}{d} - \frac{1}{f_{ir}d}\right]^{2/3} P_{\max}^{1/3}}{\mu v}$$
(6b)

for the inner race.

For angular-contact ball bearings with a thrust load only,

$$S_{\max_{or}} = \frac{K \left[-\frac{2\cos\beta}{d_e + d\cos\beta} + \frac{4}{d} - \frac{1}{f_{or}d} \right]^{2/3} P_N^{1/3}}{\mu\nu}$$
(7a)

for the outer race and

$$S_{\max_{ir}} = \frac{K \left[\frac{2\cos\beta}{d_e - d\cos\beta} + \frac{4}{d} - \frac{1}{f_{ir}d}\right]^{\frac{2}{3}} P_N^{\frac{1}{3}}}{\mu\nu}$$
(7b)

~ /

for the inner race.

For bearing steel on bearing steel, $K = 1.58 \times 10^{-3}$ for S_{max} in GPa and K = 23.58 for S_{max} in ksi. The values for the transcendental functions, μ and \mathbf{v} , vary with conformity f and can be found in reference 16.

From the above equations, the conformities at the inner and outer races affect the resultant Hertz stresses and the lives of their respective raceways. The determination of life factors LF_{ir} and LF_{or} based on conformities for the inner and outer races, respectively, can be calculated by normalizing the equations for Hertz stress for the inner and outer races to a conformity of 0.52 (the value of 0.52 was chosen as a typical reference value). The change in stress for the same race diameter but varying the conformity is determined as a function of conformity. The accepted relation between life L and S_{max} is

$$\boldsymbol{L} \sim \left(\frac{1}{\boldsymbol{S}_{\max}}\right)^{\boldsymbol{n}}$$
(8a)

Where n is normally accepted as being 9 (ref. 9). From equation (8a) for the same normal load P_o , the ratio of the stress at a 0.52 conformity to that of the ball-race conformity gives the appropriate life factor where

$$LF = \left(\frac{S_{\max_{0.52}}}{S_{\max}}\right)^9 \tag{8b}$$

Representative values of these life factors for conformities ranging from 0.505 to 0.57 are given for inner and outer races, respectively, in table I. It was found, subject to round-off error, that the life factors based upon conformities for the respective inner and outer races were independent of bearing size and series. However, they were different at the inner and outer races for each respective conformity.

TABLE I.—REPRESENTATIVE LIFE FACTORS FOR INNER AND OUTER RACE BASED ON BALL-RACE CONFORMITY

	Ball-race conformity,												
						į	f						
0.505	0.51	0.515	0.52	0.525	0.53	0.535	0.54	0.545	0.55	0.556	0.56	0.565	0.57
	Inner-race life factors,												
						L	F _{ir}						
4.5	2.04	1.22	1	0.62	0.49	0.40	0.33	0.29	0.25	0.22	0.19	0.17	0.16
	Outer-race life factors,												
LF _{or}													
5.4	2.5	1.3	1	0.75	0.61	0.47	0.38	0.32	0.28	0.24	0.21	0.19	0.17

Bearing Life Analysis

In probabilistic life models the bearing physical characteristics, applied load, operating profile, and environment determine the probability of failure, assuming that the life is represented by a known probability function. Weibull (refs. 6 and 7) was the first to suggest a reasonable way to estimate material fracture strength with such a probability function. Based upon the work of Weibull, G. Lundberg and A. Palmgren (ref. 9) in 1947 showed that the probability of survival S could be expressed as a power function of the orthogonal shearing stress τ_o , life N, depth to the maximum orthogonal shear stress Z_o , and stressed volume V of the race. That is

$$\ln\frac{1}{S} \sim \tau_o^c \frac{N^e}{Z_o^h} V \tag{9}$$

From equation (1) and for a given value of S, the life L is

$$\boldsymbol{L} = \boldsymbol{N} \sim \left(\frac{1}{\tau_o}\right)^{c_e} \left(\frac{1}{V}\right)^{1/e} \left(\boldsymbol{Z}_o\right)^{h/e}$$
(10)

where for ball bearings the stressed volume of the race

$$V = al_L Z_o \tag{11}$$



Figure 3.—Schematic of contact profile of ball on raceway.

where a is the semimajor axis of the contact ellipse and l_L is the race track length or circumference of the ring at ball contact. The resultant variables in equations (9) and (11) are also shown in figure 3.

Lundberg and Palmgren (ref. 9) incorporated into their analysis a method and distribution function developed by Weibull (refs. 6 and 7) for statistically describing the fatigue life of materials, referred to as the two-parameter Weibull distribution function:

$$\ln \ln \frac{1}{S} = e \ln \left(\frac{L}{L_{\beta}} \right) \text{ where } 0 < L < \infty \text{ and } 0 < S < 1$$
(12)

From equation (12), Lundberg and Palmgren (ref. 9) first derived the relationship between individual component life and system life. A bearing is a system of multiple components, each with a different life. As a result, the life of the system is different from the life of an individual component in the system. The L_{10} bearing system life, where 90 percent of the population survives, can be expressed as

$$\frac{1}{L_{10}^{e}} = \frac{1}{L_{10ir}^{e}} + \frac{1}{L_{10or}^{e}}$$
(13)

where the life of the rolling elements, by inference, is incorporated into the life of each raceway tacitly assuming that all components have the same Weibull slope *e*. In properly designed and operated rollingelement bearings, fatigue of the cage or separator should not occur and, therefore, is not considered in determining bearing life and reliability. From equations (12) and (13), Lundberg and Palmgren (ref. 9) derived the following relation:

$$\boldsymbol{L}_{10} = \left(\frac{\boldsymbol{C}_{\boldsymbol{D}}}{\boldsymbol{P}_{\boldsymbol{eq}}}\right)^{\boldsymbol{p}} \tag{14}$$

From Lundberg-Palmgren (ref. 9), the *load-life* exponent *p* equals 3 for ball bearings.

Formulas for the basic load capacity for ball bearings that derived from Lundberg and Palmgren (ref. 9) and incorporated into the ANSI/ABMA Standards (refs. 13 and 14) and the ISO Standards (ref. 12) are as follows:

For ball bearings with $d \le 25$ mm and $\beta \le 45^\circ$,

$$C_{D} = f_{cm} (i \cos \beta)^{0.7} Z^{\frac{2}{3}} d^{1.8}$$
(15a)

For ball bearings with d > 25 mm and $\beta \le 45^\circ$,

$$C_{D} = f_{cm} (i \cos \beta)^{0.7} Z^{\frac{2}{3}} d^{1.4}$$
(15b)

where f_{cm} is the bearing geometry and material coefficient. Prior to 1990, the coefficient f_{cm} was designated as f_c (ref. 15). The bearing geometry including the race conformities is incorporated into this coefficient.

While Lundberg and Palmgren allow for calculating the effect of ball bearing race conformities into their life calculation, the standards and the bearing manufacturers' catalogs generally normalize their values of f_{cm} to conformities on the inner and outer races of 0.52 (52 percent). Representative values of f_{cm} as a function of the year introduced by ANSI/ABMA are given in table II for representative bearing sizes, indicated by values of $\frac{d\cos\beta}{d_e}$. For values of $\frac{d\cos\beta}{d_e}$ not shown in table II, values of f_{cm} are obtained by

interpolating between the respective values shown. These coefficients apply to both deep-groove and angular-contact ball bearings without distinction. Their relative sizes and relative dynamic load capacities C_D are illustrated in figure 4 for the five series of 40-mm-bore deep-groove ball bearings.

In ANSI/ABMA standards 12.1 and 12.2 (refs. 17 and 18) for instrument bearings, the bearing geometry and material coefficient f_{cm} contain the representative combinations of inner- and outer-race conformities. The values of the coefficient f_{cm} are summarized in table III. Again, the standards do not distinguish between deep-groove (radially-loaded) and angular-contact (thrust-loaded) ball bearings nor do they separate the effect of ball life from that of the raceway.

Inner- and outer-race conformities are equal to 0.52.									
Bearing size,		Bearing geometry and material coefficient, ^a							
$d \cos \beta$		f_{cm}							
d_e	1960	1972	1978	1990	1985				
					(standards 12.1 and 12.2)				
0.05	46.75	59.52	46.75	60.70	60.70				
0.05	(3550)	(4520)	(3550)	(4610)	(4620)				
10	55.57	73.34	55.57	72.16	72.69				
.10	(4220)	(5570)	(4220)	(5480)	(5520)				
16	59.65	84.41	59.65	77.56	77.56				
.10	(4530)	(6410)	(4530)	(5890)	(5890)				
22	59.65	92.96	59.65	77.56	79.14				
.22	(4530)	(7060)	(4350)	(5890)	(6010)				
28	57.15	100.08	57.15	74.27	74.40				
.20	(4340)	(7600)	(4340)	(5640)	(5650)				
24	53.33	106	53.33	69.26	69.26				
.34	(4050)	(8050)	(4050)	(5260)	(5260)				
40			75.94	62.94					
.40			(3670)	(4780)					

TABLE II.—REPRESENTATIVE VALUES OF ROLLING-ELEMENT BEARING GEOMETRY AND MATERIAL COEFFICIENT *f_{cm}* IN ANSI/ABMA STANDARD 9 (REFS. 13 AND 14) FOR REPRESENTATIVE BALL BEARING SIZES BY YEAR INTRODUCED

^aValues of f_{cm} are for use with SI units; those in parentheses are for use with English units. ^bPrior to 1990, f_{cm} was designated as f_c .



Figure 4.—Relative sizes and dynamic capacities, CD, of 40-mm-bore deep-groove ball bearings.

TABLE III.—REPRESENTATIVE VALUES FOR ROLLING-ELEMENT BEARING GEOMETRY AND MATERIAL COEFFICIENT f_{cm} IN ANSI/ABMA STANDARD 12.1 AND 12.2 (REFS. 17 AND 18) FOR COMBINATIONS OF INNER- AND OUTER-RACE CONFORMITIES

		0.		and octai	i la lo b				
$d \cos \beta$			Bea	aring geome	try and mate	rial coefficie	nt, ^a		
d.	f_{cm}								
				Inner	-race confor	mity,			
			-		f _{ir}				-
	0.515	0.52	0.52	0.52	0.53	0.54	0.54	0.54	0.57
				Outer	r-race confor	mity,			
			-		for				-
	0.515	0.52	0.53	0.54	0.54	0.54	0.56	0.60	0.57
0.05	68.21	60.84	56.62	53.33	49.51	46.48	43.45	38.98	37.79
0.05	(5180)	(4620)	(4300)	(4050)	(3760)	(3530)	(3300)	(2960)	(2870)
10	81.11	72.63	68.74	65.58	59.65	55.30	52.67	48.59	44.90
.10	(6160)	(5520)	(5220)	(4980)	(4530)	(4200)	(4000)	(3690)	(3410)
16	86.91	77.56	75.32	73.08	64.92	59.39	57.67	55.57	48.19
.10	(6600)	(5890)	(5720)	(5550)	(4930)	(4510)	(4380)	(4220)	(3660)
22	86.91	79.14	76.37	75.06	65.58	59.39	58.47	56.62	48.19
.22	(6600)	(6010)	(5800)	(5700)	(4980)	(4510)	(4440)	(4300)	(3660)
28	83.52	74.40	73.74	73.21	63.21	56.88	56.49	55.57	42.22
.20	(6330)	(5650)	(5600)	(5560)	(4800)	(4320)	(4290)	(4220)	(3510)
34	77.69	69.26	69.00	68.74	58.99	52.93	52.54	52.41	43.06
.54	(5900)	(5260)	(5240)	(5220)	(4480)	(4020)	(3990)	(3980)	(3270)

^aValues of f_{cm} are for use with SI units; those in parentheses are for use with English units. ^bPrior to 1990, f_{cm} was designated as f_c .

Results and Discussion

G. Lundberg and A. Palmgren in 1947 (ref. 9) established the primary relation between bearing geometry and bearing life. For ball bearings they related bearing life to five variables. These are ball diameter, pitch diameter, inner- and outer-race conformities, number of balls, and contact angle. Except for bearing contact angle, the relation between these parameters remains the same regardless of whether the bearing is a deep-groove ball bearing or an angular-contact ball bearing. These relations have been incorporated into both the ANSI/ABMA and the ISO Standards to predict bearing life as well as current life prediction bearing codes (refs. 12, 13, 17, and 18). The Lundberg-Palmgren equation (ref. 9) only

relates to the lives of the inner and outer races and incorporate ball life into their analysis by inference. It has since been recognized that the life of the ball set in relation to the races is different for a deep-groove ball bearing and an angular-contact ball bearing as well as being dependent on the relative contact (Hertz) stresses at the inner and outer races (ref. 15).

Ball Set Life

Lundberg and Palmgren (ref. 9) do not directly calculate the life of the rolling-element (ball or roller) set of the bearing. However, through benchmarking of the equations with bearing life data by use of a material-geometry factor f_{cm} , the life of the rolling-element set is implicitly included in the life calculation of equations (15a) and (15b).

The rationale for not including the rolling-element set in equation (13) appears in the 1945 edition of A. Palmgren's book (ref. 5) wherein he states that, "...the fatigue phenomenon which determines the life (of the bearing) usually develops on the raceway of one ring or the other. Thus, the rolling elements are not the weakest parts of the bearing ...". The database that Palmgren used to benchmark his and later the Lundberg-Palmgren equations were obtained under radially loaded conditions. Under these conditions, the life of the rolling elements as a system (set) will be equal to or greater than that of the outer race. As a result, failure of the rolling elements in determining bearing life was not initially considered by Palmgren. Had it been, equation (13) would have been written as follows:

$$\left(\frac{1}{L_{10}}\right)^{\boldsymbol{e}} = \left(\frac{1}{L_{\boldsymbol{i}\boldsymbol{r}}}\right)^{\boldsymbol{e}} + \left(\frac{1}{L_{\boldsymbol{r}\boldsymbol{e}}}\right)^{\boldsymbol{e}} + \left(\frac{1}{L_{\boldsymbol{o}\boldsymbol{r}}}\right)^{\boldsymbol{e}}$$
(16)

where the Weibull slope *e* is the same for each of the components as well as for the bearing as a system.

Comparing equation (16) with equation (13), the value of the L_{10} bearing life will be the same. However, the values of the L_{ir} and L_{or} between the two equations will not be the same, but the ratio of L_{or}/L_{ir} will remain unchanged.

The fraction of failures due to the failure of a bearing component is expressed by Johnson (ref. 19) as

Fraction of inner-race failures
$$= \left[\frac{L_{sys}}{L_{ir}}\right]^e$$
 (17a)

Fraction of rolling-element failures
$$= \left[\frac{L_{sys}}{L_{re}}\right]^e$$
 (17b)

Fraction of outer-race failures
$$= \left[\frac{L_{sys}}{L_{or}}\right]^e$$
 (17c)

From equations (17a) to (17c), if the life of the bearing and the fractions of the total failures represented by the inner race, the outer race and the rolling element set are known, the life of each of these components can be calculated. Hence, by observation, it is possible to determine the life of each of the bearing components with respect to the life of the bearing.

Equations (17a) to (17c) were verified using radially loaded and thrust-loaded 50-mm-bore ball bearings. Three hundred forty (340) virtual bearing sets totaling 31,400 bearings were randomly assembled and tested by Monte Carlo (random) number generation (ref. 20). From the Monte Carlo

TABLE IV.—COMPARISON OF BEARING FAILURE DISTRIBUTIONS BASED UPON WEIBULL-
BASED MONTE CARLO METHOD AND THOSE CALCULATED FROM EQUATIONS (17a) TO (17c)
FOR 50-MM-BORE DEEP-GROOVE AND ANGULAR-CONTACT BALL BEARINGS (REF. 20)

TOK JU-WIWI-BC	FOR 50-MINI-BORE DEEL-GROOVE AND ANOULAR-CONTACT DALL DEARINGS (REF. 20)								
Ball-bearing type	Component	Percer	ent failure						
		Weibull-based Monte	Results from						
		Carlo results	equations (17a) to (17c)						
Deen groote	Inner race	70.1	69.9						
Deep-groove	Rolling element	14.8	15.0						
	Outer race	15.1	15.0						
	Inner race	45.4	45.1						
Angular-contact	Rolling element	45.2	45.1						
	Outer race	9.4	9.7						



Figure 5.—Rolling element fatigue lives of AISI 52100 204-size angular-contact ball bearings. Contact angle is 10°; outer-race temperature, 79 °C (175 °F); thrust load, 1108 N (249 lb); inner-ring speed, 10 000 rpm; lubricant, MiL-L-7808; *L*₁₀ life, 20.5×10⁶ inner-ring revolutions (34.2 hr); and failure index, 7 out of 12 (ref. 21).

simulation the percentage of each component failed was determined and compared to those predicted from equations (17a) to (17c). These results are shown in table IV. There is excellent agreement between these techniques (ref. 20).

Figure 5 summarizes rolling-element fatigue life data for ABEC 7 204-size angular-contact ball bearings made from AISI 52100 steel (ref. 21). The bearings had a free contact angle of 10°. Operating conditions were an inner-ring speed of 10 000 rpm, an outer-ring temperature of 79 °C (175 °F), and a thrust load of 1108 N (249 lb). The thrust load produced maximum Hertz stresses of 3172 MPa (460 ksi) on the inner race and 2613 MPa (379 ksi) on the outer race. From a Weibull analysis of the data, the bearing L_{10} life was 20.5 million inner-race revolutions or approximately 34.2 hr of operation (ref. 21).

Seven of the twelve bearings failed from rolling-element fatigue. Two of the failed bearings had fatigue spalls on a ball and an inner race. Two bearings had inner-race fatigue spalls. Two bearings had

fatigue spalls on a ball, and one bearing had an outer-race fatigue spall. Counting each component that failed as an individual failure independent of the bearing, there were four inner-race failures, four ball failures, and one outer-race failure for a total of nine failed components. Inner race failures were responsible for 44.4 percent of the failures; ball failures, 44.4 percent; and outer-race failures, 11.2 percent. Using each of these percentages in equations 17(a) to 17(c) together with the experimental L_{10} life, the lives of the inner and outer races and the ball set were calculated. For purposes of the calculation, the Weibull slope *e* was assumed to be 1.11, the same as Lundberg and Palmgren (ref. 9). The resultant component L_{10} lives were 53 million inner-race revolutions (88.3 hr) for both the inner race and ball set and 183.3 million inner-race revolutions (305.5 hr) for the outer race.

For nearly all rolling-element bearings the number of inner-race failures is greater than those of the outer race. Accordingly, from equations (17a) and (17c), the life of the outer race will be greater than that of the inner race. Zaretsky (ref. 15) noted that for radially loaded bearings (ball or roller), the percent of failures of the rolling-element set was generally equal to and/or less than the outer race. For thrust-loaded ball or roller bearings, Zaretsky (ref. 15) further noted that the percent of the rolling-element set was equal to or less than the inner race but more than the outer race. In order to account for material and processing variations, Zaretsky developed what is now referred to as *Zaretsky's Rule* (ref. 15) as follows:

For radially loaded ball and roller bearings, the life of the rolling element set is equal to or greater than the life of the outer race. Let the life of the rolling element set (as a system) be equal to that of the outer race.

From equation (16)

$$\left(\frac{1}{L_{10}}\right)^{e} = \left(\frac{1}{L_{ir}}\right)^{e} + 2\left(\frac{1}{L_{or}}\right)^{e}$$
(18)

where

 $L_{re} = L_{or}$

For thrust loaded ball and roller bearings, the life of the rolling element set is equal to or greater than the life of the inner race but less than that of the outer race. Let the life of the rolling-element set (as a system) be equal to that of the inner race.

From equation (16)

$$\left(\frac{1}{L_{10}}\right)^{e} = 2\left(\frac{1}{L_{ir}}\right)^{e} + \left(\frac{1}{L_{or}}\right)^{e}$$
(19)

where

 $L_{re} = L_{ir}$

Examples of using equations (18) and (19) are given in reference 15. As previously stated, the resulting values for L_{ir} and L_{or} from these equations are not the same as those from equation (13). They will be higher.

H. Takata (ref. 22), using a modified approach to the Lundberg-Palmgren theory (ref. 9), derived the basic dynamic load capacity of the rolling-element bearing set in addition to those for the inner and outer races for radial and thrust-loaded ball and roller bearings. For radially loaded ball bearings, Takata (ref. 22) assumes random ball rotation. For thrust-loaded ball bearings, he assumes a single or fixed

running track on each ball. According to Takata (ref. 22), the basic dynamic load capacity C_D of a bearing system can be expressed as

$$C_{D} = \left(C_{ir}^{-w} + C_{re}^{-w} + C_{or}^{-w} \right)^{-1/w}$$
(20)

where C_{p} is calculated from equations (15a) and (15b) (from Lundberg-Palmgren (ref. 9)), and exponent w is equal to 10/3 for ball bearings. Takata provides equations for calculating the dynamic load capacity of the rolling-element (ball) set, C_{re} . The resulting values for C_{ir} and C_{or} will be higher than those from the Lundberg-Palmgren equations (ref. 9).

Takata (ref. 22) performed a single ball-set life calculation within his paper for a 30-mm-bore deepgroove ball bearing. From this calculation he concluded that for this bearing

$$C_{ir} < C_{re} < C_{or} \tag{21a}$$

This would imply that

$$\boldsymbol{L_{ir}} < \boldsymbol{L_{re}} < \boldsymbol{L_{or}} \tag{21b}$$

However, he did not validate his example or his equations to determine ball-set or roller-set life with a bearing life data base.

Harris (ref. 23), citing Takata (ref. 22), compared the rolling-element fatigue life of 28.575-mm-(1.125-in.-) diameter AISI 52100 and AISI M–50 steel balls in a Pratt & Whitney one-ball fatigue tester. He ran nine test series, each comprising 12 to 48 balls. The test balls had fixed double running tracks. The maximum Hertz stress ranged from 3980 to 4160 MPa (577.2 to 603.3 ksi) with most tests run at 4000 MPa (580.1 ksi). The number of rolling-element fatigue failures for each test series varied from 3 to 36. He compared the test results to the Lundberg-Palmgren theory (ref. 9) and to a modified Lundberg-Palmgren theory (ref. 23) incorporating a "fatigue limit." The fatigue limit that he used for his calculations for both the AISI 52100 and AISI M–50 steels was 175 MPa (25.4 ksi). He concluded that the application of a fatigue limit to the modified Lundberg-Palmgren theory predicted ball lives in the one-ball fatigue tester that correlated well with the measured ball lives. He further concluded that the Lundberg-Palmgren life prediction method modified using currently accepted material-life and lubrication-life factors did not yield a satisfactory correlation.

Zaretsky, Anderson, and Parker (ref. 21) using the NASA five-ball fatigue tester and the Pratt & Whitney one-ball fatigue tester reported similar work to that of Harris (ref. 23). They also compared their experimental results to the Lundberg-Palmgren dynamic load capacity equations derived for these two test rigs. These comparisons are shown in figure 6. Unlike Harris (ref. 23), it was concluded from these data that, for contact angles up to 30°, the Lundberg-Palmgren capacity equations very nearly predict the thrust capacity for the two test systems. Further, unlike Harris, these results would justify—although not verify—the ball life prediction approach reported by Takata (ref. 22).

In a discussion of Harris's work (ref. 23), S. Pinel and F. Rehman attempted to verify Harris's calculations for the Lundberg-Palmgren life predictions (ref. 23). The ratio of Pinel and Rehman's predicted L_{10} life based on Lundberg-Palmgren to the actual experimental life was 0.70 (ref. 23). This compares to a ratio of 16.3 from Harris's Lundberg-Palmgren calculations (ref. 23), suggesting an error in the Harris analysis.



Figure 6.—Comparison of normalized dynamic load capacities of NASA five-ball fatigue tester and Pratt-Whitney one-ball fatigue tester determined experimentally to those predicted from Lundberg-Palmgren equation (ref. 21).

Bearing Life Factors Based on Conformity

From the above, the life of the bearing can be related to the life of the inner race where the ratio X between the outer- and inner-race lives is known or can be calculated where

$$X = \frac{L_{or}}{L_{ir}}$$
(22a)

and

$$\boldsymbol{L_{or}} = \boldsymbol{X} \boldsymbol{L_{ir}} \tag{22b}$$

The value X can be approximated from equation (22a) and Lundberg and Palmgren (ref. 9) as follows:

$$X = \frac{L_{or}}{L_{ir}} = 1.12 \left(\frac{1 + \frac{d\cos\beta}{d_e}}{1 - \frac{d\cos\beta}{d_e}} \right)^{5.16}$$
(23)

Deep-Groove Ball Bearings—Applying equation (22b) to (18) for radially loaded deep-groove ball bearings, equation (18) becomes

$$\boldsymbol{L}_{10} = \left(\frac{\boldsymbol{X}^{\boldsymbol{e}} \boldsymbol{L}_{\boldsymbol{ir}}^{\boldsymbol{e}}}{\boldsymbol{X}^{\boldsymbol{e}} + 2}\right)^{1/\boldsymbol{e}}$$
(24)

Applying life factors based on the effect of conformity on the respective lives of the inner and outer races, equation (24) becomes

$$L_{10_{m}} = \left[\frac{(LF_{ir})^{e}(LF_{or})^{e} XL_{ir}^{e}}{(LF_{or})^{e} X^{e} + 2(LF_{ir})^{e}}\right]^{\frac{1}{e}}$$
(25)

Dividing equation (25) by equation (24) provides the bearing life factor for the radially loaded deepgroove bearing based on conformity LF_c :

$$LF_{c} = \left[\frac{(LF_{ir})^{e}(LF_{or})^{e}(X^{e}+2)}{(LF_{or})^{e}X^{e}+2(LF_{ir})^{e}}\right]^{\frac{1}{e}}$$
(26)

Angular-Contact Ball Bearings—Applying equation (22b) to equation (19) for deep-groove ball bearings, equation (19) becomes

$$L_{10} = \left\{ \frac{X^{e} L_{ir}^{e}}{2X^{e} + 1} \right\}^{\frac{1}{e}}$$
(27)

Applying life factors based on the effect of conformity on the respective lives of the inner and outer races, equation (27) becomes

$$L_{10_{m}} = \left\{ \frac{\left[(LF_{ir})(LF_{o})XL_{ir} \right]^{e}}{2(LF_{or})^{e} X^{e} + (LF_{ir})^{e}} \right\}^{\frac{1}{e}}$$
(28)

Dividing equation (28) by equation (27) provides the bearing life factor LF_c for the thrust-loaded angular-contact ball bearing based on conformity:

Bearing type ^a	$d \cos \beta$	Life ratio, ^b
	d_e	L_{or}/L_{ir}
Extremely light	0.15	4.4
Extra light	.18	5.9
Light	.23	9.6
Medium	.25	13.0
Heavy	.28	17.7

TABLE V.—REPRESENTATIVE RATIOS OF OUTER- TO INNER-RACE LIFE, L_o/L_i , FOR REPRESENTATIVE BALL BEARING TYPES.

^aSee fig. 4.

^bFrom equation (23).

$$LF_{c} = \left[\frac{(LF_{ir})^{e} (LF_{or})^{e} (2X^{e} + 1)}{2(LF_{or})^{e} X^{e} + (LF_{ir})^{e}}\right]^{\frac{1}{e}}$$
(29)

Representative life factors LF_{ir} and LF_{or} for ball bearing sizes shown in figure 4 are summarized in table V.

Application to Lundberg-Palmgren Equations

In order to calculate a life factor (LF_c) based on the conformity of a ball in a nonconforming race groove, it is necessary to obtain from the bearing manufacturer's catalog the bearing outside diameter (OD), inside diameter (ID), free contact angle β and ball diameter *d*. Knowing the bearing OD and ID, calculate the pitch diameter *d_e* from equation (2). From these values, the ratio of the outer to inner race lives *X* can be calculated either from equation (20) or from an appropriate bearing computer program where the inner-and outer-race conformities are the same.

From table I, life factors (*LF*) based on individual race conformities are obtained for both the inner and outer races. These LF values are normalized to a ball-race conformity (*f*) of 0.52. Depending on whether the bearing is a deep-groove or angular-contact ball bearing, these values together with that for the race-life ratio *X* are used in equations (26) or (29), respectively, to calculate bearing life factor *LF_c* based on the combined inner- and outer-race conformities. These values of *LF_c* can then be applied against the bearing catalog life or the values calculated from equations (14), (15a), and (15b).

For the bearing series shown in figure 4 and summarized in table V, representative life factors were calculated for deep-groove and angular-contact ball bearings using equations (26) and (29), respectively, with race conformities ranging from 0.505 to 0.57. The conformity of one race was fixed at 0.52 and the other race was allowed to vary and vice versa. The results were normalized for the conformity combination of 0.52 inner and 0.52 outer, where the resultant bearing life factor for conformity LF_c is equal to 1. These results were compared to those generated from the Lundberg-Palmgren equations from reference (ref. 9). The Lundberg-Palmgren equations are the same for deep-groove and angular-contact ball bearings except for the inclusion of the cosine of the contact angle β . Where $\cos \beta = 1$, the results for the two types of ball bearings are identical.

Table VI shows a comparison of these life factors for extreme combinations of conformities for extremely light and heavy series ball bearings. The results for both bearing types are different from that calculated from the Lundberg-Palmgren equations. Depending on the bearing type and series as well as conformity combinations, the calculated life for deep-groove ball bearings can be over 40 percent less than that calculated by the Lundberg-Palmgren equations. For angular-contact ball bearings, the life can vary from 22 to -39 percent from that calculated by the Lundberg-Palmgren equations.

	NORWALIZED TO INNER' AND OUTER-INTEL CONTORUNTILS OF 0.52								
Ball bearing	Ball-race	conformity		Bearing life factor for conformity,					
series					LF_c				
(see table V	Inner race	Outer race	Lundberg-	Deep-groove	e ball bearing	Angular-contact ball bearing			
and fig. 4)			Palmgren	From	Change from	From	Change from		
			results for	equation (26)	Lundberg-	equation (29)	Lundberg-		
			deep-groove		Palmgren,		Palmgren,		
			and angular-		percent		percent		
			contact						
			bearing						
			(ref. 9)						
Extremely	0.505	0.52	3.02	2.22	-27	3.37	12		
light	.57	.52	.27	.16	-41	.17	-37		
	.52	.505	1.14	1.13	-1	1.07	-6		
	.52	.57	.65	.41	-37	.68	5		
Heavy	.505	.52	3.60	3.49	-3	4.17	16		
	.57	.52	.26	.17	-39	.16	-39		
	.52	.505	1.09	1.06	-3	1.02	-6		
	.52	.57	.74	.71	-4	.90	22		

TABLE VI.—COMPARISON OF LIFE FACTORS BASED ON COMBINATIONS OF BALL-RACE CONFORMITIES NORMALIZED TO INNER- AND OUTER-RACE CONFORMITIES OF 0.52

While the trend between bearing life factors are qualitatively similar, they are quantitatively different between the angular-contact ball bearings and the deep-groove ball bearings. Comparing the two bearing types, the life factors LF_c for the deep-groove bearings can be as much as 34 percent lower than that for angular-contact ball bearings.

Other Bearing Life Methods

From equation (10), Lundberg-Palmgren (ref. 9) have bearing life inversely proportional to the orthogonal shearing stress τ_o raised to the c/e power where

$$\boldsymbol{L} \sim 1/(\boldsymbol{\tau}_{\boldsymbol{o}})^{c/e} \tag{30a}$$

From Lundberg and Palmgren (ref. 9) the value of c/e for ball bearings is 9.3. Lundberg and Palmgren (ref. 9) assumed that the orthogonal shearing stress τ_o is the critical stress related to and affecting rollingelement fatigue. However, other shearing stresses designated τ that are proportional to the maximum Hertz stress, such as maximum shearing stress, octahedral shearing stress, and von Mises equivalent stress, are also related to and affect rolling-element fatigue. As a result, equation (30a) can be written as

$$\boldsymbol{L} \sim 1/(\boldsymbol{\tau})^{c/e} \tag{30b}$$

Incorporating a fatigue limit τ_{ℓ} in equation (30b),

$$\boldsymbol{L} \sim 1/(\boldsymbol{\tau} - \boldsymbol{\tau}_{\boldsymbol{\ell}})^{c/e} \tag{30c}$$

Background

In recent years there has been a movement to incorporate the concept of a "fatigue limit" in the Lundberg-Palmgren equations (ref. 9). The fatigue limit as applied to ball and roller bearings is a shearing stress below which no rolling-element fatigue should occur. The concept of a fatigue limit for rolling-element bearings was proposed by Palmgren in 1924 (ref. 4). It was apparently abandoned by him first in 1945 (ref. 5) and then again with Lundberg in 1947 (ref. 9). In 1985, Ioannides and Harris (ref. 24) applied Palmgren's concept of a fatigue limit to the Lundberg-Palmgren equations in the form shown in

equation (31). The ostensible reason Ioannides and Harris used the fatigue limit was to replace the material and processing life factors (ref. 15) that are used as life modifiers in conjunction with the bearing lives calculated from the Lundberg-Palmgren equations (ref. 15).

There are two problems associated with the use of a fatigue limit for rolling-element bearings. The first problem is that the form of equation (30c) may not reflect the presence of a fatigue limit but the presence of a compressive residual stress (ref. 15). The second problem is that there are no data in the open literature that would justify the use of a fatigue limit for through-hardened bearing steels such as AISI 52100 and AISI M–50. In fact, a paper presented by Tosha et al. (ref. 25), reporting the results of rotating beam fatigue experiments for through-hardened AISI 52100 steel at very low stress levels, shows conclusively that a fatigue limit does not exist for this bearing steel.

Recent publications by the ASME (ref. 26) and the ISO (refs. 27 and 28) for calculating the life of rolling-element bearings include a fatigue limit and the effects of ball-race conformity on bearing fatigue life. These methods do not, however, include the effect of ball failure on bearing life. The ISO method is based on the work reported by Ioannides, Bergling, and Gabelli (ref. 29). The ASME method as contained in their proposed ASMELIFE software (ref. 26) uses the von Mises stress as the critical stress with a fatigue limit value of 684 MPa (99,180 psi). This corresponds to a Hertz surface contact stress of 1140 MPa (165,300 psi). The ISO 281:2006 (ref. 28) method uses a fatigue limit stress of 900 MPa (130,500 psi), which corresponds to a Hertz contact stress of 1500 MPa (217,500 psi).

The concept of a fatigue limit load (bearing load under which the fatigue stress limit is just reached in the most heavily loaded raceway contact) introduced in the proposed (revised) ISO rating methods is proportional to the fatigue limit stress raised to the 3rd power for ball bearings (point contact). These differing values of stress would result in a 128 percent higher load using ISO 281:2006 (ref. 28) than ASMELIFE (ref. 26) below which no fatigue failure would be expected to occur.

The effect of using different values of fatigue limit or no fatigue limit on rolling-element fatigue life prediction is shown in table VII. This table summarizes the qualitative results obtained for maximum Hertz stresses of 1379, 1724, and 2068 MPa (200, 250, and 300 ksi) for point contact using equation (30) for Lundberg-Palmgren without a fatigue limit and equation (30c) for fatigue limits of 684 MPa (99,180 psi) (from ASMELIFE) and 900 MPa (130,500 psi) (from ISO 281:2006). The results are normalized to a maximum Hertz stress of 1379 MPa (200 ksi) with no fatigue limit where the quotient of equation (30c) divided by equation (30b) is taken to the *c/e* power of 9.3 (taken from Lundberg and Palmgren). The effect of stressed volume was also factored into these calculations.

Fatigue limit. ^a	Relative life ^{b,c}						
т.	Maximum Hertz stress,						
		MPa (ksi)					
MPa (ksi)	1379 (200)	1724 (250)	2068 (300)				
0 (0), Lundberg-Palmgren (ref. 9)	1	0.134	0.026				
684 (99.2), ASMELIFE (ref. 26)	11.9×10^{6}	3152	44.6				
900 (130.5), ISO281-2006 (ref. 28)	œ	23.3×10^{6}	4258				

TABLE VII.—EFFECT OF FATIGUE LIMIT τ on Rolling-element fatigue life

^avon Mises stress.

^bIncludes effect of stressed volume.

^cNormalized to life at maximum Hertz stress of 1379 MPa (200 ksi) with no fatigue limit.

Comparison of Results

Figures 7 and 8 show the comparison of ball set life and race conformity on bearing life for radially loaded vacuum-arc-remelted (VAR) AISI 52100 steel, 60-mm-bore, ball bearings under pure radial and thrust loads. Bearing geometry, operating parameters, and life factors used for these calculations are summarized in table VIII.



Figure 7.—Effect of ball set life and race conformity on calculated bearing life using ASMELIFE, Lundberg-Palmgren equations, and Zaretsky's Rule. Bearing type, 60-mm-bore ball bearing; contact angle, 0°; radial load, 2224 N (500 lb); speed, 3600 rpm; and material, VAR AISI 52100 steel. (a) ASMELIFE with fatigue limit (ISO 281/2 (ref. 27)) and without ball set life. (b) Lundberg-Palmgren (ref. 9) and ISO 281:1990(E) (ref. 12) with life factors (ref. 15) and without ball set life. (c) Lundberg-Palmgren (ref. 9) and ISO 281:1990(E) (ref. 12) modified by ball set life (Eq. (26)) and with life factors (15).



Figure 8.—Effect of ball set life and race conformity on calculated bearing life using ASMELIFE, Lundberg-Palmgren equations, and Zaretsky's Rule. Bearing type, 60-mm bore ball bearing; contact angle, 25°; thrust load, 4448 N (1000 lb); speed, 3600 rpm; and material, VAR AISI 52100 steel. (a) ASMELIFE with fatigue limit (ISO 281/2 (ref. 27)) and without ball set life. (b) Lundberg-Palmgren (ref. 9) and ISO 281:1990(E) (ref. 12) with life factors (ref. 15) and without ball set life. (c) Lundberg-Palmgren (ref. 9) and ISO 281:1990(E) (ref. 12) modified by ball set life (Eq. (ref. 29)) and with life factors (15).

Bearing information	Radially loaded	Thrust-loaded
	bearing	bearing
Ball bearing geometry:		
Bore, mm (in.)	60 (2.362)	60 (2.362)
Outside diameter, mm (in.)	110 (4.331)	110 (4.331)
Width, mm (in.)	22 (0.866)	22 (0.866)
Ball diameter, mm (in.)	16 (0.625)	16 (0.625)
Number of balls	10	10
Surface finish, µm (µin.), AA: ^a		
Races	0.1 (4)	0.1 (4)
Balls	0.025(1)	0.025 (1)
Surface composite finish, µm (µin.), AA ^a	0.103 (4.123)	0.103 (4.123)
Free contact angle, degrees	0	25
Material ^b	VAR AISI 52100	VAR AISI 52100
Operating parameters:		
Speed, rpm	3600	3600
Load, N (lb)	2224 (500)	4448 (1000)
Inner-race stress at 52 percent conformity, MPa (ksi)	1544 (224)	1544 (244)
Outer-race stress at 52 percent conformity, MPa (ksi)	1324 (192)	1324 (192)
Dynamic load capacity, C_p at 52 percent inner- and outer-race	40 343 (9070)	37 279 (8381)
conformities, N (lb)		
Ratio of outer-race life to inner-race life at 52 percent inner-	5.843	5.576
and outer-race conformities		
Life factors (<i>LF</i>) for Lundberg-Palmgren life analysis:		
Material and processing, a_2 :		
Material, AISI 52100	3	3
Processing, VAR ^b	3	3
Operating conditions, a_3 :		
EHD ^c film thickness/surface composite finish, Λ ratio = 7	3	3
Oil filtration, 3 µm	1.4	1.4
$\boldsymbol{LF} = \boldsymbol{a}_2 \times \boldsymbol{a}_3 = 3 \times 3 \times 3 \times 1.4 = 37.8$	37.8	37.8
Life factors (<i>LF</i>) for ASMELIFE:		
Fatigue limit, MPa (ksi) von Mises	684 (99.2)	684 (99.2)
Operation conditions, a_3 :	_	
EHD' film thickness/ surface composite finish, Λ ratio = 7	3	3
Oil contamination factor	0.7863	0.7863
$LF = 3 \times 0.7863 = 2.36$	2.36	2.36

TABLE VIIIBALL BEARING GEOMETRY,	, OPERATING PARAMETERS, AND
LIFE FACTORS FOR BEARING	LIFE CALCULATIONS

^aAA is arithmetic average.

^bVAR is vacuum arc remelting.

^aEHD is elastohydrodynamic.

For each figure set of figures 7 and 8, there are two curves. One curve represents the conformity of the outer race constant at 0.52 (52 percent) and the inner-race conformity varied from 0.51 to 0.57 (51 to 57 percent). This will be referred to as "constant outer-race conformity." For the second curve, the inner-race conformity was held constant at 52 percent and the outer-race conformity was varied from 51 to 57 percent. This will be referred to as "constant inner-race conformity."

Figures 7(a) and 8(a) show the results for the ASMELIFE (ref. 26) calculation for the radially loaded and thrust-loaded bearings, respectively. For the radially loaded bearing with constant outer-race conformity, life decreased by 93 percent when the inner-race conformity was varied from 52 to 57 percent (fig. 7(a)). For constant inner-race conformity, the calculated life decreased by 99 percent (fig. 7(a)). Contrary to what would be intuitively expected, the lives obtained for constant outer-race conformity exceeded those lives calculated for constant inner-race conformity. The opposite result should have occurred, suggesting an error in the ASMELIFE computer program.

For the thrust-loaded bearing (fig. 8(a)), the lives obtained for constant inner-race conformity exceeded those lives calculated for constant outer-race conformity. For constant outer-race conformity, life decreased by 93 percent when the inner-race conformity was varied from 52 to 57 percent. For constant inner-race conformity, the calculated life decreased by 82 percent.

Figures 7(b) and 8(b) show the calculated life results from classical Lundberg-Palmgren theory (ref. 9) and ISO 281 (ref. 12) with life factors but without ball set life for the radially and thrust-loaded bearings, respectively. For the radially loaded bearing with constant outer-race conformity (fig. 7(b)), life decreased by 74 percent when the inner-race conformity was varied from 52 to 57 percent. For constant inner-race conformity, the calculated life decreased by 28 percent when the outer-race conformity was varied from 52 to 57 percent. For the thrust-loaded bearing with constant outer-race conformity (fig. (8(b)), life decreased by 77 percent when the inner-race conformity was varied from 52 to 57 percent. For constant inner-race conformity, the calculated bearing with constant outer-race conformity (fig. (8(b)), life decreased by 77 percent when the inner-race conformity was varied from 52 to 57 percent. For constant inner-race conformity, the calculated life decreased by 39 percent when the outer-race conformity was varied from 52 to 57 percent. For constant inner-race conformity, the calculated life decreased by 39 percent when the outer-race conformity was varied from 52 to 57 percent.

Figures 7(c) and 8(c) show the life results from classical Lundberg-Palmgren theory (ref. 9) factoring in ball set life using equations (26) and (29) with life factors. For the radially loaded bearing with constant outer-race conformity (fig. 7(c)), life decreased by 81 percent when the inner-race conformity was varied from 52 to 57 percent. For constant inner-race conformity, the calculated life decreased by 55 percent when the outer-race conformity (fig. (8(c)), life decreased by 83 percent when the inner-race conformity was varied from 52 to 57 percent. For the thrust-loaded bearing with constant outer-race conformity (fig. (8(c)), life decreased by 83 percent when the inner-race conformity was varied from 52 to 57 percent. For constant inner-race conformity, the calculated life decreased by 27 percent. For constant inner-race conformity was varied from 52 to 57 percent.

Comparing the results from classical Lundberg-Palmgren theory (ref. 9) and ISO 281 (ref. 12) to those from ASMELIFE (ref. 26), for a radially loaded bearing at inner- and outer-race conformities of 52 percent, ASMELIFE calculated a life 17,175 percent greater than that obtained from Lundberg-Palmgren and ISO 281 with life factors. For a thrust-loaded bearing with inner- and outer-race conformities of 52 percent, ASMELIFE calculated a life 385 percent greater than that obtained from Lundberg-Palmgren and ISO 281 with life factors.

At inner-race conformity of 57 percent and outer-race conformity of 52 percent for a radially-loaded bearing, ASMELIFE calculated a life 4,235 percent greater than that obtained from Lundberg-Palmgren and ISO 281 with life factors. For a thrust-loaded bearing, this amount was 49 percent. At inner-race conformity of 52 percent and outer-race conformity of 57 percent for the radially loaded bearing, ASMELIFE calculated a life 188 percent greater than that obtained from Lundberg-Palmgren and ISO 281 with life factors. For the thrust-loaded bearing, this amount was 42 percent.

When comparing results calculated from the Lundberg-Palmgren theory (ref. 9) incorporating ball set life (figs. (7(c) and 8(c)) to those that did not (figs. 7(b) and 8(b)), the lives at inner- and outer-race conformities of 52 percent are assumed to be equal for the specified operating condition. As the conformity is increased, differences in life emerge as a result of ball set life. At conformities greater than 52 percent, including the life of the ball set results in a lower life prediction than that obtained from the Lundberg-Palmgren equations (figs. 7(b) and (c)). At an inner-race conformity of 52 percent and outer-race conformity of 57 percent for the radially loaded bearing (fig. 7), the life of the ball set life. At an outer-race conformity of 52 percent and inner-race conformity of 57 percent for a radially loaded bearing (fig. 7), the life of the aradially loaded bearing (fig. 7), the life of the aradially loaded bearing (fig. 7), the life of the aradially loaded bearing (fig. 7), the life of the bearing with ball set life is 25 percent for a radially loaded bearing (fig. 7), the life of the bearing with ball set life is 25 percent less than that calculated from the Lundberg-Palmgren equations without ball set life is 26 percent for a radially loaded bearing (fig. 7), the life of the bearing with ball set life is 25 percent for a radially loaded bearing (fig. 7), the life of the bearing with ball set life is 25 percent less than that calculated from the Lundberg-Palmgren equations without ball set life.

For the thrust-loaded bearing (figs. 8(b) and (c)) at inner-race conformity of 52 percent and outer-race conformity of 57 percent, the calculated life of the bearing factoring in ball set life (fig. 8(c)) is 19 percent less than calculated from the Lundberg-Palmgren equations without ball set life (fig. 8(b)). At outer-race conformity of 52 percent and inner-race conformity of 57 percent, the life of the bearing factoring in ball set life (fig. 8(c)) is 27 percent less than calculated from the Lundberg-Palmgren equations without ball set life (fig. 8(c)) is 27 percent less than calculated from the Lundberg-Palmgren equations without ball set life (fig. 8(b)).

Under the range of stresses examined, the use of a fatigue limit would suggest that (for most operating conditions under which a ball bearing will operate) the bearing will not fail from classical rolling-element fatigue. Realistically, this does not occur. The use of a fatigue limit from either ASMELIFE (ref. 26) or ISO 281:2006 (ref. 28) will significantly over predict bearing life over a range of normal operating Hertz stresses. (The use of ISO 281:2006 in these calculations would result in a bearing life approaching infinity.) Since the predicted lives of rolling-element bearings are high, the problem can become one of undersizing a bearing for a particular application.

Summary of Results

G. Lundberg and A. Palmgren in 1947 established the primary relation between bearing geometry and bearing life. These relations have been incorporated into both the ANSI/ABMA and the ISO Standards to predict bearing life as well as current life prediction bearing codes. The Lundberg-Palmgren equations only relate to the lives of the inner and outer races and incorporate ball life into their analysis by inference. It has since been recognized that the life of the ball set in relation to the races is different for a deep-groove ball bearing and an angular-contact ball bearing as well as being dependent on the relative contact (Hertz) stresses at the inner and outer races. The analysis reported herein considers the life of the ball set as well as the respective lives of the races and to reassess the effect of ball-race conformity on ball bearing life. The related changes in ball bearing life are incorporated in life factors that can be used to modify the bearing predicted life using the Lundberg-Palmgren equations and the ANSI/ABMA and ISO Standards. The following results were obtained:

- 1. Two simple algebraic relationships that incorporated ball set life were established to calculate life factors (LF_c) incorporating ball set life to determine the effect inner- and outer-race conformity combinations have on bearing L_{10} life for deep-groove and angular-contact ball bearings, respectively.
- 2. Depending on the bearing type and series as well as conformity combinations, the calculated life for deep-groove ball bearings can be over 40 percent less than that calculated by the Lundberg-Palmgren equations. For an angular-contact ball bearing, the life can vary from 16 to -39 percent from that calculated by the Lundberg-Palmgren equations.
- 3. The trend between bearing life factors are qualitatively similar but quantitatively different between angular-contact and the deep-groove ball bearings. Comparing the two bearing types, the life factors LF_c for the deep-groove bearings can be as much as 40 percent lower than that for angular-contact ball bearings.
- 4. The use of a fatigue limit from either ASMELIFE or ISO 281:2006 can significantly overpredict bearing life over a range of normal operating Hertz stresses, which can result in the selection of undersized bearings for a particular application.

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