

# Allowable Trajectory Variations for Space Shuttle Orbiter Entry-Aeroheating CFD

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Reynolds-number criteria are developed for acceptable variations in Space Shuttle Orbiter entry trajectories for use in computational aeroheating analyses. The criteria determine if an existing computational fluid dynamics solution for a particular trajectory can be extrapolated to a different trajectory. The criteria development considers twelve types of computational aeroheating data, such as boundary layer thickness. For each type of datum, the allowable uncertainty contribution due to trajectory variation has been set by the Entry Aeroheating Subsystem team. Then Reynolds-number relations between trajectory variation and output uncertainty are determined. From these relations the criteria are established for the maximum allowable trajectory variations. The most restrictive criterion allows a 25% variation in Reynolds number at constant Mach number between trajectories.

## I. Nomenclature

The subject matter in the present report considers relative changes in fluid dynamic properties. Therefore dimensional units for the symbols are not pertinent to the results.

### *Symbols*

$C_P$	Pressure coefficient
$D$	Cavity depth
$H$	Total enthalpy
$M$	Mach number
$P$	Pressure
$q$	Heat transfer rate
$Re$	Reynolds number
$T$	Temperature
$V$	Velocity magnitude
$\delta$	Boundary layer thickness
$\delta^*$	Displacement thickness
$\mu$	Viscosity
$\rho$	Density
$\theta$	Momentum thickness

### *Subscripts*

$e$	Boundary layer edge
$k$	Protuberance height

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$w$	Wall
$\infty$	Free stream

### *Operators*

$\Delta$	Difference: $\Delta x = x_2 - x_1$
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### *Acronyms*

BF	Bump factor
BLT	Boundary layer transition
CFD	Computational fluid dynamics
DPLR	Data-parallel line relaxation CFD code
LAURA	Langley aerothermodynamic upwind relaxation algorithm CFD code
OML	Outer mold line
RCC	Reinforced carbon-carbon

## II. Introduction

The Space Shuttle Orbiter Entry Aeroheating Subsystem team has pre-computed computational fluid dynamics (CFD) solutions of Orbiter flow fields for nominal entry trajectories.<sup>1</sup> During missions, these solutions may be used to predict aerothermodynamic properties in the course of assessing Orbiter damage and repairs.<sup>2</sup> But, the mission-specific entry trajectory will not match the nominal trajectory, because of differences such as the Orbiter weight or atmospheric conditions. These differences in trajectories can be expressed as differences in Reynolds numbers at given Mach numbers. This report develops Reynolds-number criteria to characterize how close in trajectory space a particular trajectory must be to a nominal trajectory so that the nominal CFD solutions are sufficient for damage assessment purposes. The most restrictive criterion is then used to define the allowable trajectory variations for reuse of the nominal CFD solutions during a mission.

The criteria are developed under several assumptions: a spot-check at one Mach number applies for all Mach numbers (the Mach numbers of most interest are greater than 15); uncertainties are symmetric and can be expressed as  $\pm$  quantities; uncertainty trends extrapolate linearly in Reynolds number; and, angle of attack variations are negligible (the angles of attack are within  $40 \pm 2^\circ$ ).

The development of the criteria begins by identifying twelve types of aerothermodynamic data, such as surface temperature and boundary layer thickness, that are available in the CFD solution set and are relevant to Orbiter damage or repair assessments. For each datum type, accuracy requirements at approximately 1:20 odds have been set by the Entry Aeroheating Subsystem team. Reynolds number scalings are then developed to relate trajectory variations to variations in the CFD results. Finally, the allowable trajectory Reynolds number variations are determined by inverting the scaling relations.

The Reynolds number criteria are summarized as a tabulation in section IV-M.

An expanded treatment of the present material, along with similar analyses for an additional five more types of aerothermodynamic data, is available in a NASA Technical Memorandum.<sup>3</sup>

## III. Nominal Orbiter CFD solutions

Aeroheating CFD solutions of entry flow fields about the Orbiter vehicle<sup>a</sup> exist for several points along a few nominal trajectories. The CFD codes, the solution processes, the verification techniques, the validation data, and the solutions themselves have been accepted for use during Space Shuttle missions by the Orbiter Configuration Control Board.<sup>1</sup> Previous Orbiter solutions of a similar nature and application, using the same CFD codes, have been reported<sup>4</sup> in the context of the *Columbia* accident investigation.

These solutions typically require about a week each to obtain, although with exclusive access to a super-computer in a round-the-clock staffing mode solutions have been obtained in a day or two. It is desired to

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<sup>a</sup>The CFD Orbiter model used by the Entry Aeroheating Subsystem team is truncated in the vicinity of the body-flap hinge line, 1280 inches from the nose.

Priority	Parameter
1	Idealized cavity heating bump factors
2	Smooth OML surface temperatures
3	Smooth OML heating rates
4	Boundary layer thickness
5	$\frac{Re_\theta}{M_e} \cdot \frac{1}{\delta} \cdot \left(\frac{H_e}{H_w}\right)^{0.3}$ — BLT correlation parameter
6	$Re_k^{0.6} \left(Re_\theta \cdot \frac{\mu_e}{\mu_k}\right)^{0.4}$ — BLT correlation parameter
7	$\frac{Re_\theta}{M_e} \cdot \frac{1}{\delta} \cdot \left(\frac{T_e}{T_w}\right)^{0.51}$ — BLT correlation parameter
8	$\frac{Re_\theta}{M_e} \cdot \frac{1}{\delta} \cdot \left(\frac{T_e}{T_w}\right)^{0.67}$ — BLT correlation parameter
9	Boundary layer $C_p$ , shock relations
10	Boundary layer $C_p$ , stream-tube relations
11	Displacement thickness
12	$\frac{H_w}{H_e}$

**Table 1. CFD aeroheating products, ordered by perceived importance.**

avoid this cost of creating new entry Orbiter solutions; thus the present report’s topic of how much these existing solutions can be reused for different trajectories.

#### A. CFD codes

Two CFD codes are normally employed by the Entry Aeroheating Subsystem team, and the present analyses utilize the solutions from both codes interchangeably. The two codes provide a measure of verification when used redundantly, and pragmatically allows the team members to choose their most proficient analysis tool. The two codes are the Data Parallel Line-Relaxation (DPLR) software<sup>5</sup> and the Langley Aerothermodynamic Upwind Relaxation Algorithm (LAURA).<sup>6,7</sup>

Both DPLR and LAURA are finite-volume upwind-flux schemes for solving the Navier-Stokes<sup>8,9</sup> equations with non-equilibrium chemistry. All the CFD results considered here have laminar boundary layers, a five-species air model, and assume a radiative-equilibrium surface temperature using reaction-cured glass properties.

#### B. Solution repository

There are currently 20 full-vehicle Orbiter solutions covering parts of three nominal trajectories. The solutions are stored on a data repository at the NASA Advanced Supercomputing facility. The CFD data for the present report was all obtained from this solution repository. The solutions span the Mach number range 6–25. The trajectories correspond to STS-107 (*Columbia’s* last flight), STS-115 (a typical entry from the International Space Station), and ISSHVFW (a severe entry from the International Space Station).

### IV. Trajectory variation criteria

Twelve CFD aeroheating products are considered. The products are listed in table 1 as prioritized by the Entry Aeroheating Subsystem team, based on the perceived importance for mission-support assessments. The products are considered by this report only on the wind side of the Orbiter.

For each product, the following sections define the product, explain its application for mission support, and present an accuracy requirement for the CFD prediction from the Entry Aeroheating Subsystem team. The Reynolds number is used to parameterize the degree a trajectory is off-nominal, and criteria are developed that relate trajectory Reynolds number variation to the allowable error in the aeroheating product due to trajectory variation from nominal. The criteria limits are set in the context of approximately 1:20 odds. These criteria are developed subject to several assumptions. Usually, spot-checks are only performed at one Mach number, with the criteria assumed to apply for all Mach numbers; the Mach numbers of most interest

are 15–25. Variations are most often only considered in one direction, and the rates of change are assumed to be the same in both the positive and negative sides. The product variations are assumed to extrapolate linearly with Reynolds number. The effects of angle of attack variations are assumed to be negligible; the angles of attack are within  $40 \pm 2^\circ$ .

The trajectory criteria are summarized in table 3 in section IV-M.

### A. Cavity heating bump factors

The cavity heating bump factors are surface heat transfer rates that have been normalized to a reference nominal heating rate on the smooth OML. The cavities are simplified models of actual damage geometries, such as hexahedrons, and solutions are obtained as local perturbations within the global Orbiter flow field. In the terminology of the Entry Aeroheating Subsystem team, these geometry models are called idealized cavities. Examples of the cavity modeling and analysis process have been published by Pulsonetti and Wood.<sup>10</sup> CFD cavity heating bump factors can be used during missions to assess and supplement the predictions from the Cavity Heating Tool,<sup>11</sup> which is the standard cavity heating engineering tool used by the Entry Aeroheating Subsystem team. Of primary interest is the predicted bump factors on the floor of a cavity. The Entry Aeroheating Subsystem team has set the allowable error in bump factors due to trajectory variations at  $\pm 25\%$ .

The trajectory criteria for cavity bump factors is developed using the Cavity Heating Tool correlations, which are based upon cavity wind tunnel data. In particular, two of the Cavity Heating Tool correlations show a sensitivity to free stream conditions: the fore-85% floor of Everhart (short) cavities and the aft-10% floor of long cavities. See Hyatt et al.<sup>11</sup> for a full description of the Cavity Heating Tool nomenclature.

The Everhart cavity fore-85% floor bump factor varies with boundary layer thickness as

$$BF = \frac{5}{4} - \frac{5}{2} \frac{D}{\delta}, \quad 0.1 < \frac{D}{\delta} < 0.3 \quad (1)$$

The difference in bump factor for the same cavity at two different boundary layer thicknesses can be expressed in absolute and relative terms as

$$\Delta BF = BF_2 - BF_1 \quad (2)$$

$$\Delta BF = -\frac{5}{2} \frac{D}{\delta_1} \left( \frac{\delta_1}{\delta_2} - 1 \right) \quad (3)$$

$$\frac{\Delta BF}{BF_1} = \frac{\frac{\delta_1}{\delta_2} - 1}{1 - \frac{1}{2(D/\delta_1)}} \quad (4)$$

Similarly, the long cavity aft-10% floor bump factor varies with boundary layer thickness as

$$BF = \frac{14}{3} \frac{D}{\delta} - \frac{3}{5}, \quad 0.3 < \frac{D}{\delta} < 1.2 \quad (5)$$

The absolute and relative changes in bump factor as functions of boundary layer thickness are

$$\Delta BF = \frac{14}{3} \frac{D}{\delta_1} \left( \frac{\delta_1}{\delta_2} - 1 \right) \quad (6)$$

$$\frac{\Delta BF}{BF_1} = \frac{\frac{\delta_1}{\delta_2} - 1}{1 - \frac{9}{70(D/\delta_1)}} \quad (7)$$

Variations in boundary layer thickness can be related to variations in Reynolds number, because the boundary layer thickness varies approximately linearly with the reciprocal of the square root of the Reynolds number, as demonstrated in section D. This relationship is expressed as

$$\delta \propto \frac{1}{\sqrt{Re}} \quad (8)$$

$$\frac{\delta_1}{\delta_2} = \sqrt{\frac{Re_2}{Re_1}} \quad (9)$$

Now, the change in bump factors can be expressed in terms of Reynolds number variations, and so can the inverse relations for Reynolds number change be expressed in terms of bump factor variations. For the Everhart-cavity fore-85% floor bump factor

$$\Delta BF = -\frac{5}{2} \frac{D}{\delta_1} \left( \sqrt{\frac{Re_2}{Re_1}} - 1 \right) \quad (10)$$

$$\frac{Re_2}{Re_1} = \left( 1 - \frac{2 \Delta BF}{5(D/\delta_1)} \right)^2 \quad (11)$$

$$\frac{\Delta BF}{BF_1} = \frac{\sqrt{\frac{Re_2}{Re_1}} - 1}{1 - \frac{1}{2(D/\delta_1)}} \quad (12)$$

$$\frac{Re_2}{Re_1} = \left[ 1 + \left( 1 - \frac{1}{2(D/\delta_1)} \right) \frac{\Delta BF}{BF_1} \right]^2 \quad (13)$$

For the long-cavity aft-10% floor bump factor

$$\Delta BF = \frac{14}{3} \frac{D}{\delta_1} \left( \sqrt{\frac{Re_2}{Re_1}} - 1 \right) \quad (14)$$

$$\frac{Re_2}{Re_1} = \left( 1 + \frac{3 \Delta BF}{14(D/\delta_1)} \right)^2 \quad (15)$$

$$\frac{\Delta BF}{BF_1} = \frac{\sqrt{\frac{Re_2}{Re_1}} - 1}{1 - \frac{9}{70(D/\delta_1)}} \quad (16)$$

$$\frac{Re_2}{Re_1} = \left[ 1 + \left( 1 - \frac{9}{70(D/\delta_1)} \right) \frac{\Delta BF}{BF_1} \right]^2 \quad (17)$$

Because equations 11, 13, 15, and 17 are monotonic in  $\delta_1$ , a positive-definite quantity, the extreme value theorem states that the maximum variation will occur at an endpoint of the  $\delta$  ranges listed in equations 1 and 5.

By equation 1,  $BF(D/\delta = 0.1) = 1$ . Using either equation 11 or 13, it can be determined that a 300% increase in Reynolds number is needed to reduce the bump factor by 25% to 0.75.

By equation 1,  $BF(D/\delta = 0.3) = 0.5$ . Using either equation 11 or 13, it can be determined that a 31% decrease in Reynolds number is needed to increase the bump factor by 25% to 0.625.

By equation 5,  $BF(D/\delta = 0.3) = 0.8$ . Using either equation 15 or 17, it can be determined that a 31% increase in Reynolds number is needed to increase the bump factor by 25% to 1.0.

By equation 5,  $BF(D/\delta = 1.2) = 5$ . Using either equation 15 or 17, it can be determined that a 40% decrease in Reynolds number is needed to decrease the bump factor by 25% to 3.75.

Coincidentally, the limiting allowable variation in Reynolds number to produce a 25% variation in bump factor is the same for both the Everhart and long cavities—31%. Thus the cavity heating bump factor criteria for allowable trajectory variation is a  $\pm 31\%$  variation in Reynolds number.

## B. Surface temperature

The CFD surface temperatures are radiative equilibrium values assuming reaction-cured glass properties for the entire Orbiter. Of primary interest is the wind-side tile acreage of the vehicle. The CFD surface temperatures may be used during a mission to assess the predicted values from the standard entry aeroheating tools. The Entry Aeroheating Subsystem team has set the allowable change in surface temperature predictions due to trajectory variations at  $\pm 3\%$ .

The variation in surface temperature with free stream conditions has been approximately scaled by  $(\rho_\infty V_\infty^2)^{1/8}$  for an Orbiter boundary layer probe tool.<sup>12</sup> But the present analysis is considering variations in Reynolds number at a fixed Mach number. For the Orbiter entry trajectories, because the temperature does not vary much in the mesosphere, the possible velocity variation at a fixed Mach number is small. Thus,

the Reynolds number variations are caused primarily due to density variations at different altitudes, and the surface temperature changes can be related to Reynolds number variations scaled to the  $1/8$  power.

The Mach-18 STS-115 trajectory point has a 21.1% lower Reynolds number than the Mach-18 STS-107 trajectory point. Multiplying the Mach-18 STS-107 nominal surface temperatures by the Reynolds number ratio to the  $1/8$  power,  $0.789^{(1/8)} = 0.971$ , produces an estimate of the STS-115 surface temperatures. The error in this estimate relative to the nominal STS-115 solution, for the wind side of the Orbiter, is shown in figure 1. The errors are within  $\pm 2\%$  over at least 95% of the surface.

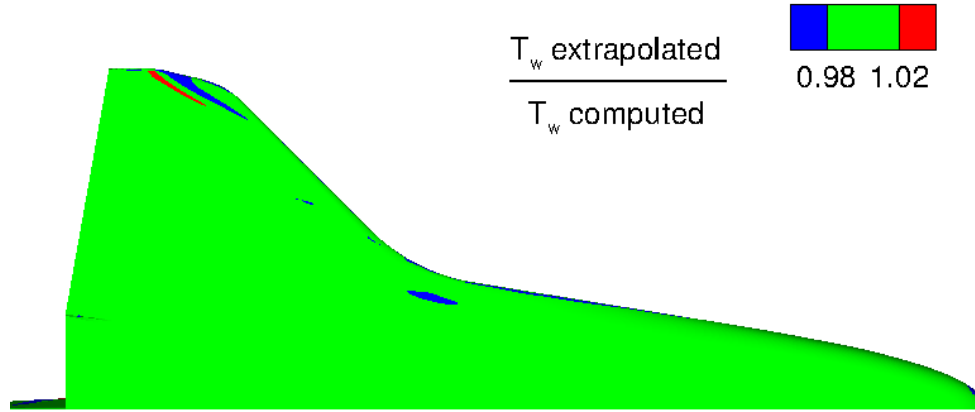


Figure 1. Extrapolation error in surface temperature for Mach-18 check case.

Using a  $\pm 2\%$  bound on the error, the Reynolds number criterion for allowable trajectory variation of surface temperatures is

$$\left( \frac{3\% \text{ allowable}}{2\% \text{ observed}} \right) 21.1\% = 31.7\% \simeq \pm 32\% \quad (18)$$

### C. Smooth OML heating

The CFD surface heat transfer rates are based upon reaction-cured glass properties for the entire Orbiter. Of primary interest is the wind-side tile acreage of the vehicle. The CFD smooth-OML heating rates may be used during a mission to assess the predicted values from the standard entry aeroheating tools. The Entry Aeroheating Subsystem team has set the allowable change in heat transfer rate predictions due to trajectory variations at  $\pm 10\%$ .

In section B, the surface temperatures are shown to scale with  $Re^{(1/8)}$ . For radiative equilibrium the relation between surface temperature and heating rates is  $q \propto T^4$ . The assumed variation in heating due to Reynolds number changes is then  $q \propto \sqrt{Re}$ .

The Mach-18 STS-115 trajectory point has a 21.1% lower Reynolds number than the Mach-18 STS-107 trajectory point. Multiplying the Mach-18 STS-107 nominal surface heating rates by  $\sqrt{0.789} = 0.888$  produces an estimate of the STS-115 heating rates. The error in this estimate relative to the nominal STS-115 solution, for the wind side of the Orbiter, is shown in figure 2. The errors are within  $\pm 7\%$  over about 95% of the surface.

Using a  $\pm 7\%$  bound on the error, the Reynolds number criterion for allowable trajectory variation of smooth-OML surface heating rates is

$$\left( \frac{10}{7} \right) 21.1\% = 30.1\% \simeq \pm 30\% \quad (19)$$

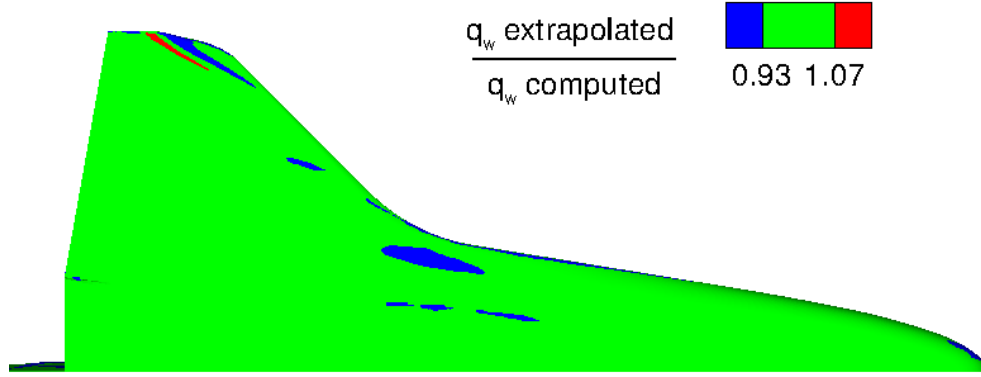


Figure 2. Extrapolation error in heating rates for Mach-18 check case.

#### D. Boundary layer thickness

The CFD boundary layer thickness has been defined by the Entry Aeroheating Subsystem team for the Orbiter flow fields as a variation on the traditional 99.5%  $H/H_\infty$  definition. See references<sup>1,12,13</sup> for details of the boundary layer thickness definition. The boundary layer thickness may be used as a correlating parameter when creating engineering models of Orbiter damage during a mission. The Entry Aeroheating Subsystem team has set the allowable change in boundary layer thickness predictions due to trajectory variations at  $\pm 11\%$ .

Classic incompressible boundary layer theory<sup>14</sup> scales boundary layer thickness inversely with  $\sqrt{Re}$ . A  $1/\sqrt{Re}$  scaling was used to extrapolate boundary layer thicknesses at three locations on the Orbiter—at the nose landing gear door, at the external tank door, and at the RCC-9 carrier panel—from the STS-107 trajectory to the STS-115 trajectory for six trajectory points spanning Mach 17.9–24.9. The scaling factors are listed in table 2.

$M_\infty$	$\frac{Re_{115}-Re_{107}}{Re_{107}}$	$\sqrt{\frac{Re_{107}}{Re_{115}}}$
24.9	19.6%	0.91
24.2	6.2	0.97
22.9	- 9.4	1.05
20.3	- 7.1	1.04
19.4	-16.7	1.10
17.9	-21.1	1.13

Table 2. Boundary layer thickness scaling factors from STS-107 to STS-115 trajectories.

Figure 3 plots the absolute value of the extrapolation error, relative to CFD solutions for the STS-115 free-stream conditions, for each of the eighteen check points versus the absolute value of the percentage variation in Reynolds number between the STS-107 and STS-115 trajectories. No simple correlation is evident, but the errors are bounded by about 5.5%, with a maximum 21% variation in Reynolds number.

The Reynolds number criterion for allowable trajectory variation of boundary layer thicknesses is

$$\left(\frac{11}{5.5}\right) \times 21.1\% = 42.2\% \simeq \pm 40\% \quad (20)$$

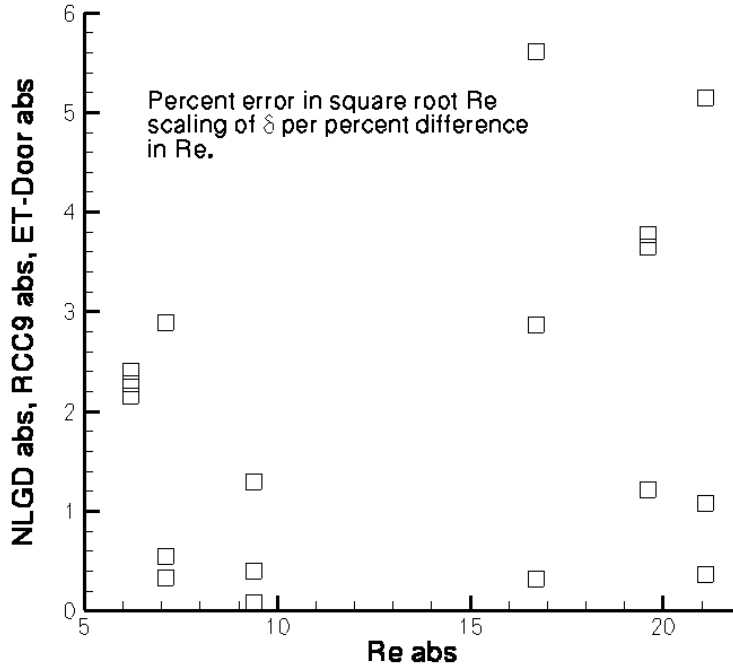


Figure 3. Extrapolation errors for boundary layer thickness test points.

### E. Protuberance boundary layer trip parameter

As part of the primary correlation for predicting boundary layer transition induced by a protuberance, the Entry Aeroheating Subsystem team uses the parameter

$$\frac{Re_{\theta}}{M_e} \cdot \frac{1}{\delta} \cdot \left( \frac{H_e}{H_w} \right)^{0.3} \quad (21)$$

All of the variables in parameter (21) are obtained from CFD solutions of the smooth-OML Orbiter. The scaling of this parameter leads to the most restrictive Reynolds number trajectory criterion. The Entry Aeroheating Subsystem team has set the allowable error contribution due to trajectory variations at  $\pm 10\%$ .

The boundary layer scalings from the Boundary Layer Transition Tool documentation<sup>12</sup> are used to obtain a scaling for parameter (21):  $M_e$  is not scaled with  $Re$ ,  $Re_{\theta}$  is scaled with  $\sqrt{Re}$ , and  $\delta$  is scaled with  $1/\sqrt{Re}$ .  $(H_e/H_w)^{0.3}$  is shown in reference<sup>12</sup> to scale with  $Re/10$ , and is neglected— meaning it is unscaled in the present analysis— because the variation is an order of magnitude less than the variation of  $Re_{\theta}/\delta$ . Thus the parameter (21) is scaled with  $Re$ .

The linear scaling with Reynolds number is tested at Mach 19.4, by extrapolating the STS-107 parameter to the STS-115 conditions, a 16.7% reduction in Reynolds number. Absolute values of the percentage differences between the computed and the extrapolated STS-115 parameter-(21) values that exceed 6.5% are shown as red in figure 4. Approximately 95% of the windside surface has extrapolation errors less than 6.5%.

The Reynolds number criterion for the allowable trajectory variation of the protuberance boundary layer trip parameter is

$$\left( \frac{10}{6.5} \right) \times 16.7\% = 25.7\% \simeq \pm 25\% \quad (22)$$



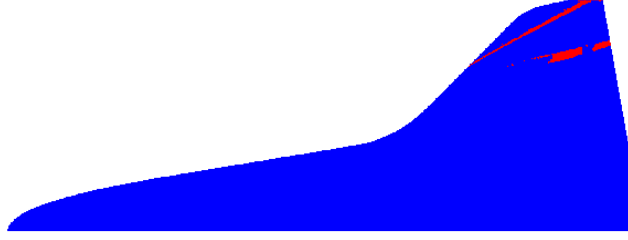


Figure 4. Absolute values of percentage extrapolation errors for protuberance boundary layer transition parameter (21). Red is more than 6.5%. Blue is less than 6.5%.



Figure 5. Absolute values of percentage extrapolation errors for  $Re_k$  boundary layer transition parameter (23). Red is more than 4.5%. Blue is less than 4.5%.

## F. $Re_k$ boundary layer transition parameter

As part of the secondary correlation for predicting boundary layer transition induced by a protuberance, the Entry Aeroheating Subsystem team uses the parameter

$$Re_k^{0.6} \left( Re_\theta \cdot \frac{\mu_e}{\mu_k} \right)^{0.4} \quad (23)$$

All of the variables in parameter (23) are obtained from CFD solutions of the smooth-OML Orbiter. The Entry Aeroheating Subsystem team has set the allowable error contribution due to trajectory variations at  $\pm 10\%$ .

Assuming  $k \simeq \delta$ , then both  $Re_k$  and  $Re_\theta$  can be scaled with  $\sqrt{Re}$ . Viscosity scales approximately with the square root of temperature, and so  $(\mu_e/\mu_k)^{0.4}$  scales like  $(T_e/T_k)^{0.2}$ , and is neglected. Substitution into the expression (23) leads to the entire parameter being scaled with  $\sqrt{Re}$ .

The  $\sqrt{Re}$  scaling is tested at Mach 19.4, by extrapolating the STS-107 parameter (23) to the STS-115 conditions, a 16.7% reduction in Reynolds number. Absolute values of the percentage differences between the computed and the extrapolated STS-115 parameter-(23) values that exceed 4.5% are shown as red in figure 5. Approximately 95% of the windside surface has extrapolation errors less than 4.5%.

The Reynolds number criterion for the allowable trajectory variation of the  $Re_k$  boundary layer trip parameter is

$$\left( \frac{10}{4.5} \right) \times 16.7\% = 37.1\% \simeq \pm 37\% \quad (24)$$

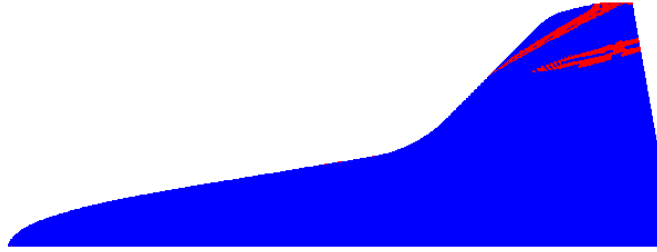


Figure 6. Absolute values of percentage extrapolation errors for cavity-volume boundary layer transition parameter (25). Red is more than 4%. Blue is less than 4%.

### G. Cavity-volume boundary layer transition parameter

As part of the volume-based correlation for predicting boundary layer transition induced by a cavity, the Entry Aeroheating Subsystem team uses the parameter

$$\frac{Re_\theta}{M_e} \cdot \frac{1}{\delta} \cdot \left( \frac{T_e}{T_w} \right)^{0.51} \quad (25)$$

All of the variables in parameter (25) are obtained from CFD solutions of the smooth-OML Orbiter. The Entry Aeroheating Subsystem team has set the allowable error contribution due to trajectory variations at  $\pm 10\%$ .

$Re_\theta$  is scaled with  $\sqrt{Re}$ ,  $\delta$  is scaled inversely with  $\sqrt{Re}$ , and  $M_e$  is unscaled. The temperature ratio scaling is neglected, because  $T_e/T_w$  is shown to scale with  $Re^{0.18}$  in reference,<sup>12</sup> and when  $T_e/T_w$  is raised to the 0.51 power the scaling becomes less than  $Re^{0.1}$ . The entire parameter (25) is thus scaled linearly with Reynolds number.

The linear scaling with Reynolds number is tested at Mach 19.4, by extrapolating the STS-107 parameter to the STS-115 conditions, a 16.7% reduction in Reynolds number. Absolute values of the percentage differences between the computed and the extrapolated STS-115 parameter-(25) values that exceed 4% are shown as red in figure 6. Approximately 95% of the windside surface has extrapolation errors less than 4%.

The Reynolds number criterion for the allowable trajectory variation of the cavity-volume boundary layer trip parameter is

$$\left( \frac{10}{4} \right) \times 16.7\% = 41.8\% \simeq \pm 40\% \quad (26)$$

### H. Cavity-area boundary layer transition parameter

As part of the area-based correlation for predicting boundary layer transition induced by a cavity, the Entry Aeroheating Subsystem team uses the parameter

$$\frac{Re_\theta}{M_e} \cdot \frac{1}{\delta} \cdot \left( \frac{T_e}{T_w} \right)^{0.67} \quad (27)$$

All of the variables in parameter (27) are obtained from CFD solutions of the smooth-OML Orbiter. The Entry Aeroheating Subsystem team has set the allowable error contribution due to trajectory variations at  $\pm 10\%$ .

$Re_\theta$  is scaled with  $\sqrt{Re}$ ,  $\delta$  is scaled inversely with  $\sqrt{Re}$ , and  $M_e$  is unscaled. The temperature ratio scaling is neglected because  $T_e/T_w$  is shown to scale with  $Re^{0.18}$  in reference,<sup>12</sup> and when  $T_e/T_w$  is raised to the 0.67 power the scaling becomes approximately  $Re^{0.1}$ . The entire parameter (27) is thus scaled linearly with Reynolds number.

The linear scaling with Reynolds number is tested at Mach 19.4, by extrapolating the STS-107 parameter to the STS-115 conditions, a 16.7% reduction in Reynolds number. Absolute values of the percentage



Figure 7. Absolute values of percentage extrapolation errors for cavity-area boundary layer transition parameter (27). Red is more than 4%. Blue is less than 4%.



Figure 8. Absolute values of percentage errors for post normal-shock stagnation pressure coefficients. Black is more than 3%.

differences between the computed and the extrapolated STS-115 parameter-(27) values that exceed 4% are shown as red in figure 7. Approximately 95% of the windside surface has extrapolation errors less than 4%.

The Reynolds number criterion for the allowable trajectory variation of the cavity-area boundary layer trip parameter is

$$\left(\frac{10}{4}\right) \times 16.7\% = 41.8\% \simeq \pm 40\% \quad (28)$$

## I. Boundary layer $C_p$ , shock relations

One of the techniques used by the Entry Aeroheating Subsystem team to estimate protuberance bending loads utilizes boundary-layer profile pressure coefficients that assume normal-shock stagnation pressures. These pressure coefficients are obtained from the smooth-OML CFD baseline solutions. The Entry Aeroheating Subsystem team has set the allowable error contribution due to trajectory variations at  $\pm 12\%$ .

To test the boundary layer pressure coefficient scaling, post normal-shock pressure coefficients are computed at the boundary layer edge for Mach-19.4 trajectory points on both the STS-107 and STS-115 trajectories. These two trajectory points differ by 16.7% in Reynolds number.

The absolute values of the percentage differences between the wind-side STS-115 and STS-107 pressure coefficients are shown in figure 8. Black regions have differences greater than 3%. Approximately 95% of the wind-side surface has differences less than 3%.

The Reynolds number criterion for the allowable trajectory variation of the normal-shock boundary layer pressure coefficients is

$$\left(\frac{12}{3}\right) \times 16.7\% = 66.8\% \simeq \pm 67\% \quad (29)$$



Figure 9. Absolute values of percentage errors for total-pressure coefficients. Black is more than 3%.

### J. Boundary layer $C_p$ , stream-tube

One of the techniques used by the Entry Aeroheating Subsystem team to estimate protuberance bending loads utilizes boundary-layer profile pressure coefficients that assume stream-tube theory total pressures,  $P + \frac{1}{2}\rho V^2$ . These pressure coefficients are obtained from the smooth-OML CFD baseline solutions. The Entry Aeroheating Subsystem team has set the allowable error contribution due to trajectory variations at  $\pm 12\%$ .

To test the boundary layer pressure coefficient scaling, total-pressure coefficients are computed at the boundary layer edge for Mach-19.4 trajectory points on both the STS-107 and STS-115 trajectories. These two trajectory points differ by 16.7% in Reynolds number.

The absolute values of the percentage differences between the wind-side STS-115 and STS-107 pressure coefficients are shown in figure 9. Black regions have differences greater than 3%. Approximately 95% of the wind-side surface has differences less than 3%.

The Reynolds number criterion for the allowable trajectory variation of the stream-tube boundary layer pressure coefficients is

$$\left(\frac{12}{3}\right) \times 16.7\% = 66.8\% \simeq \pm 67\% \quad (30)$$

### K. Displacement thickness

The Entry Aeroheating Subsystem team has developed a tool, named Endigestion, for estimating breach flows. During operation, the Endigestion tool integrates mass flux through the boundary layer. The flow properties used by Endigestion are obtained from the smooth-OML CFD baseline solutions. The Entry Aeroheating Subsystem team has set the allowable error contribution due to trajectory variations at  $\pm 50\%$ .

The displacement thickness is used to estimate the trajectory error scaling of the Endigestion mass flux. The displacement thickness scales with  $1/\sqrt{Re}$ .

The STS-107  $\delta^*$  at  $M_\infty = 19.4$  are scaled to the STS-115 trajectory, a 16.7%  $Re$  difference. The absolute values of the percentage scaling errors are shown in figure 10, where the red indicates errors greater than  $\pm 5\%$ . Approximately 95% of the wind-side surface has scaling errors less than 5%.

The Reynolds number criterion for the allowable trajectory variation of the displacement thickness is

$$\left(\frac{50}{5}\right) \times 16.7\% = 167\% \simeq \pm 165\% \quad (31)$$

### L. Total enthalpy ratio

The Entry Aeroheating Subsystem team has developed a tool, named Endigestion, for estimating breach flows. The Endigestion tool estimates the fraction of free stream total enthalpy that is ingested into the breach. The flow properties used by Endigestion are obtained from the smooth-OML CFD baseline solutions. The Entry Aeroheating Subsystem team has set the allowable error contribution due to trajectory variations at  $\pm 50\%$ .

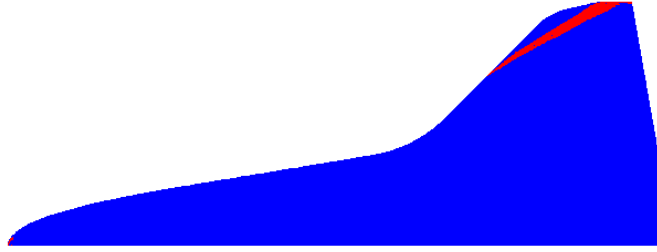


Figure 10. Absolute values of percentage errors for  $\delta^*$  scaling. Red is more than 5%. Blue is less than 5%.

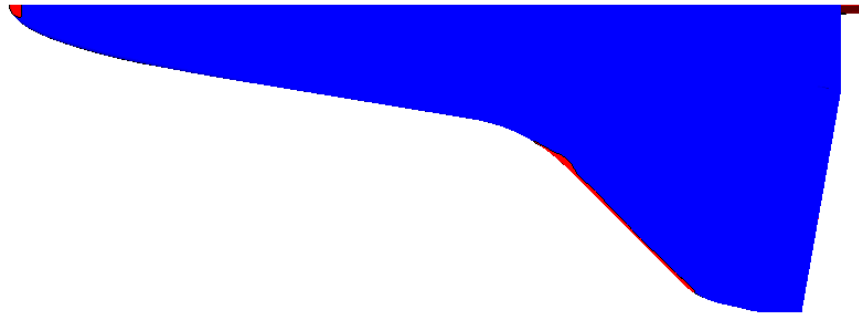


Figure 11. Absolute values of percentage errors from scaling the percentage changes in  $H_w/H_e$  by  $-0.4$  times the percentage change in Reynolds number. Red is more than 3%. Blue is less than 3%.

The scaling of the total enthalpy ratio  $H_w/H_e$  is used here to estimate the trajectory scaling error for the Endigestion total enthalpy ratio. As part of the BLT (version 2) documentation,<sup>12</sup> the percentage change in the ratio  $H_w/H_e$  is shown to scale as  $-0.4$  times the percentage change in Reynolds number for  $M_\infty \geq 20$ . In reference,<sup>12</sup> this scaling has been normalized for a 10% change in Reynolds number. Figure 11 re-plots the scaled data from reference,<sup>12</sup> this time showing a threshold of  $\pm 3\%$  error in the scaling, marked red in the figure. Over 95% of the wind side surface is seen to have a scaling error less than 3%.

The Reynolds number criterion for the allowable trajectory variation of the total enthalpy ratio is

$$\left(\frac{50}{3}\right) \times 10\% = 167\% \simeq \pm 165\% \quad (32)$$

## M. Tabulation

Table 3 lists the allowable error contributions due to trajectory variations for each of the twelve CFD products discussed in the present report. The last column of table 3 lists the resulting allowable trajectory variation, expressed in terms of trajectory Reynolds number. The most restrictive criterion, for the primary protuberance-induced boundary layer transition parameter, allows a  $\pm 25\%$  variation in trajectory Reynolds number.

## V. Summary of results

Criteria were established for reusing the computational fluid dynamics (CFD) solutions of the Space Shuttle Orbiter at specific entry trajectory points for new entry trajectories. These criteria were developed for twelve particular types of aeroheating data that the Entry Aeroheating Subsystem team might need during

Priority	Parameter	allowable trajectory error contribution, %	trajectory $Re$ criterion, %
1	Idealized cavity heating bump factors	25	31
2	Smooth OML surface temperatures	3	32
3	Smooth OML heating rates	10	30
4	Boundary layer thickness	11	40
5	$\frac{Re_\theta}{M_e} \cdot \frac{1}{\delta} \cdot \left(\frac{H_e}{H_w}\right)^{0.3}$	10	25
6	$Re_k^{0.6} \left(Re_\theta \cdot \frac{\mu_e}{\mu_k}\right)^{0.4}$	10	37
7	$\frac{Re_\theta}{M_e} \cdot \frac{1}{\delta} \cdot \left(\frac{T_e}{T_w}\right)^{0.51}$	10	40
8	$\frac{Re_\theta}{M_e} \cdot \frac{1}{\delta} \cdot \left(\frac{T_e}{T_w}\right)^{0.67}$	10	40
9	Boundary layer $C_p$ , shock relations	12	67
10	Boundary layer $C_p$ , stream-tube relations	12	67
11	Displacement thickness	50	165
12	$\frac{H_w}{H_e}$	50	165

**Table 3. Summary of allowable error contributions due to trajectory variations for CFD products and the resulting trajectory variation limits expressed as Reynolds number thresholds.**

a Space Shuttle mission to assess thermal protection damage to the Orbiter. The criteria are expressed in terms of Reynolds number variations for fixed Mach numbers.

The development of the trajectory variation criteria began by defining the allowable error contribution due to trajectory variations as set by the Entry Aeroheating Subsystem team for each of the twelve CFD aeroheating datum types. Scaling relations were applied to cast the datum uncertainty in terms of the trajectory Reynolds number variations. Spot checks of the scalings were performed against CFD solutions for different trajectories, and the allowable trajectory variation criteria were obtained to approximately 95%-confidence levels.

The criteria were developed under several assumptions: a spot-check at one Mach number applied for all Mach numbers (the Mach numbers of most interest were greater than 15); uncertainties were the same for the positive and negative sides; uncertainty trends extrapolated linearly in Reynolds number; and, angle of attack variations were negligible (the angles of attack were within  $40 \pm 2^\circ$ ).

The most restrictive trajectory variation criteria, for a protuberance-induced boundary layer transition correlation parameter, allows for a 25% variation in Reynolds number. The criteria for all the eight highest-priority datum types allow 40% or less variations in Reynolds number. In light of the noted development assumptions, for future Space Shuttle missions the Entry Aeroheating Subsystem team has decided to use a criteria of 15–20% variation in Reynolds number, when assessing the need for trajectory-specific CFD solutions.

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