



Minnowbrook VI, August 2009

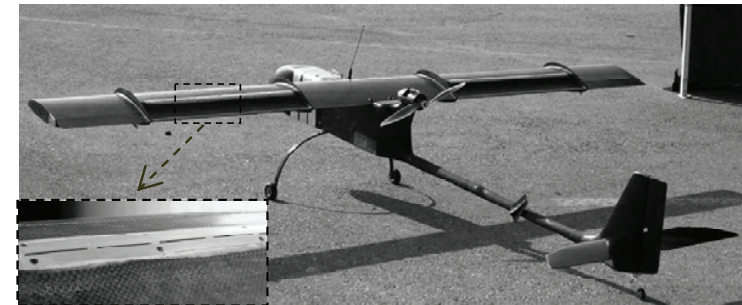
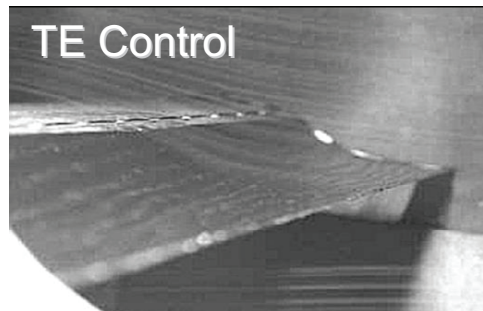
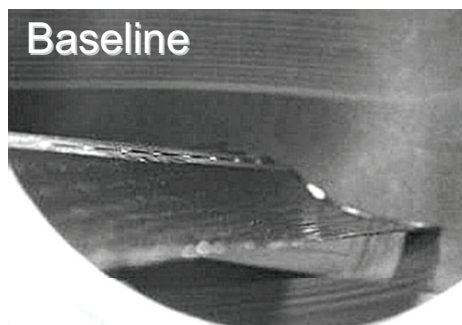


Amplitude Scaling of Active Separation Control

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Acknowledgment:

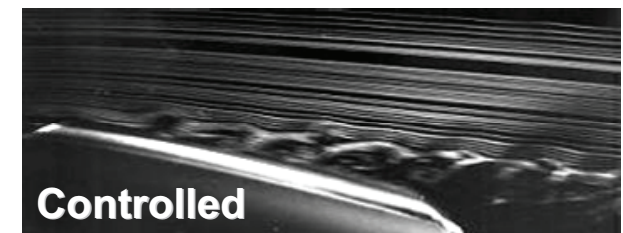
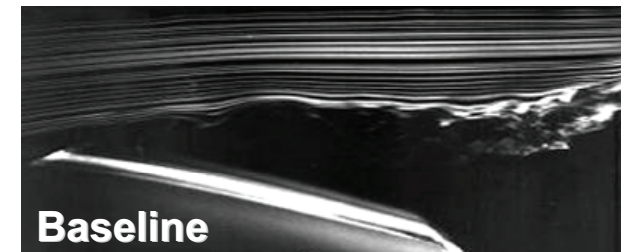
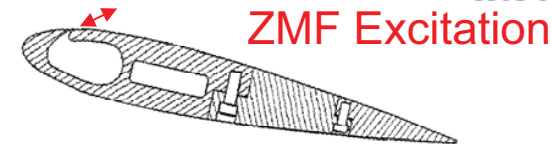
I. Fono, G. Arwatz, T. Yehoshua, E. Ben-Hamou, I. Dayan
S. Pasteur, E. Nevo, Kronish, Blas, Meadow Aero Lab members



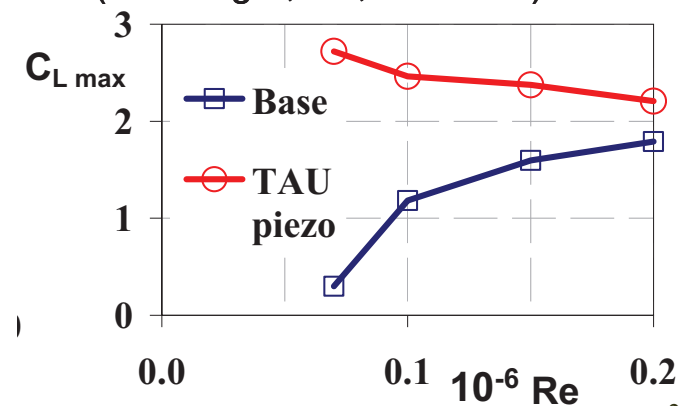
Motivation



- Active control of boundary layer separation leads to many benefits
- Frequency parameter: Strouhal (F^+)
- Length scale under controversy
- Amplitude scaling?
- We use C_μ – historically, steady blowing
- But does it scale the data?
- Are there other parameters we should consider?
- We revisit here known and define 2 new amplitude scaling parameters
- Check their validity using low Re data ($Re < 1 \times 10^6$)



(Neuburger, '89, $Re < 100k$)





Amplitude scaling - 1



- **Velocity Ratio**

$$VR \equiv \frac{U_p}{U_e} \approx \frac{U_p}{U_\infty}$$

- U_p - peak excitation velocity
- U_e - local external velocity
- U_∞ - free-stream velocity
- Actuator Mach number over free-stream Mach number
- Implies linearity



(Yehoshua)



Amplitude scaling - 2



- **Momentum coefficient**

$$C_{\mu} \equiv \frac{h}{c} \left(\frac{U_p}{U_{\infty}} \right)^2 = \frac{h}{c} (VR)^2$$

- **Ratio between (incomp., isoth.)**

- Excitation momentum (h =slot width)

$$hU_p^2$$

- Free stream momentum (c =chord)

$$cU_{\infty}^2$$

- U_p - peak excitation velocity

- U_{∞} - free-stream velocity

- h – slot width, c – airfoil chord

- Follows steady-blowing concept

(Yehoshua)





Amplitude scaling - 3



- **Reynolds # corrected momentum coefficient**

- **Ratio between**

- Excitation momentum

$$\approx h U_p^2$$

- BL momentum deficit

$$\approx \theta U_\infty^2$$

- **Laminar momentum thickness**

$$\frac{\theta_{Lam}}{c} \approx Re^{-0.5}$$

- **Turbulent momentum thickness**

$$\frac{\theta_{Turb}}{c} \approx Re^{-0.2} \Rightarrow \theta_{Turb} \approx c Re^{-0.2}$$

$$C_{\mu, Re} \equiv \frac{h}{\theta} \frac{U_p^2}{U_\infty^2} \approx \frac{h (VR)^2}{c Re^m} = \frac{h}{c} (VR)^2 Re^{-m}$$



(Yehoshua)



Vorticity-flux / Circulation - 4



- **Actuator's vorticity flux (blowing, half slot width)**

$$VF \approx \int_0^{T/2} \int_0^{h/2} \omega_z(y, t) U_p(y, t) dy dt$$

$$VF \approx \int_0^{h/2} \int_0^{T/2} U_p(y, t) \frac{dU_p(y, t)}{dy} dt dy$$

$$VF \approx \frac{U_p^2}{h} \frac{hT}{4} \approx \frac{U_p^2 T}{4} \approx \frac{U_p^2}{4f}$$

- **Kutta-Zhukovsky**

$$C_L = \frac{\rho_\infty U_\infty \Gamma}{1/2 \rho_\infty U_\infty^2 c}$$

- **Circulation**

$$\Gamma = c C_L U_\infty$$

- **Vorticity-flux coefficient**

$$C_\Gamma \equiv \frac{\text{Slot_Vorticity_Flux}}{\text{Baseline_Circulation}} \approx \frac{U_p^2 T}{4 \Gamma_{\text{Baseline}}}$$

$$C_\Gamma \approx \frac{U_p^2 T}{4 c C_L U_\infty} = \frac{1}{4 C_L} \left(\frac{U_p}{U_\infty} \right)^2 \frac{1}{S_t} = \frac{(VR)^2}{4 C_L S_t}$$



Frequency corrected VR - 5



- Nagib et al (2006)
- Proposed to scale AFC effect on lift using
- Velocity ratio
- Strouhal number
- For large separated regions
- Low frequencies
- Problematic at $f \rightarrow 0 \dots$

$$H \equiv \frac{U_p / U_\infty}{\sqrt{fc / U_\infty}} = \frac{VR}{\sqrt{S_t}}$$



(Yehoshua)



Amplitude Scaling Options



- **Velocity ratio (VR)**

$$VR \equiv \frac{U_p}{U_e} \approx \frac{U_p}{U_\infty}$$

- **Strouhal weighted VR (Nagib et al, 2006)**

$$H \equiv \frac{VR}{\sqrt{S_t}}$$

- **Momentum coefficient**

$$C_\mu \equiv \frac{h}{c} (VR)^2$$

- **Reynolds corrected C_μ**
 - $m=0.2$ (Turb.), $m=0.5$ (Lam.)

$$C_{\mu, \text{Re}} \equiv \frac{h}{c} (VR)^2 \text{Re}^m$$

- **Vorticity flux coefficient**

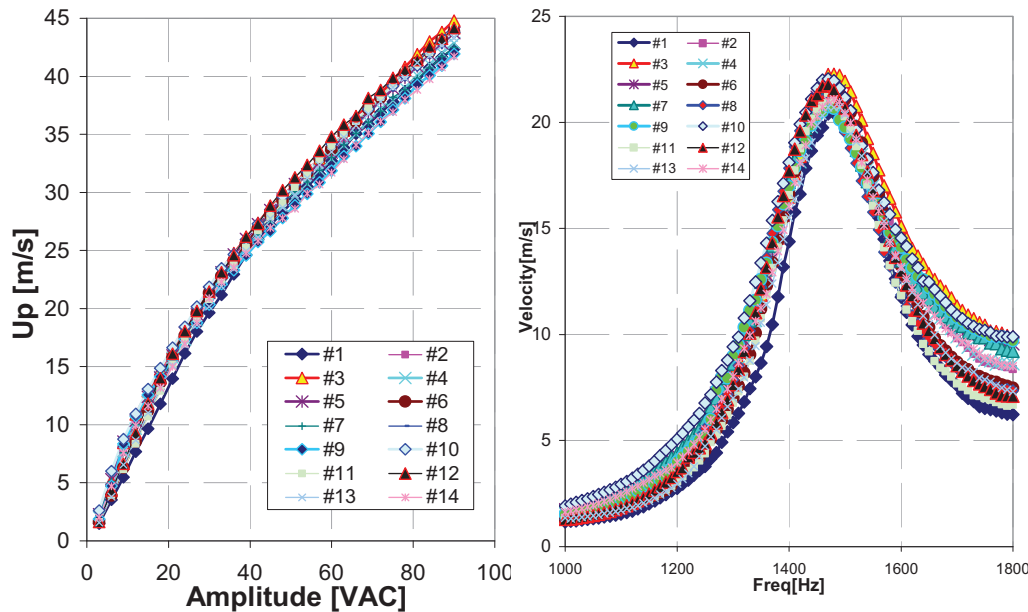
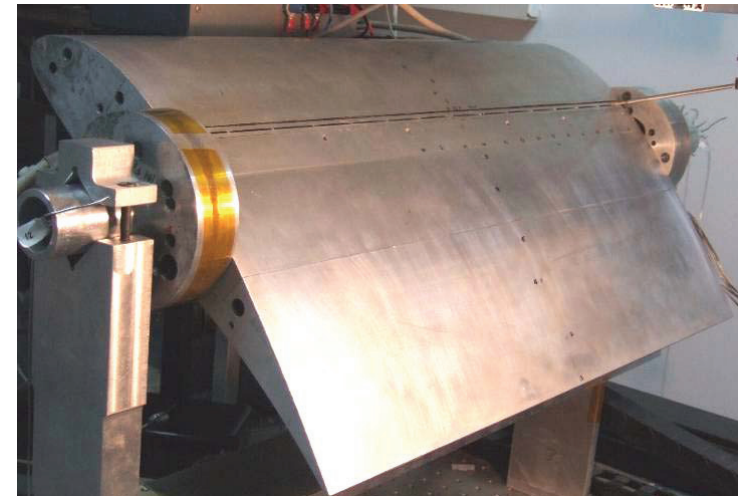
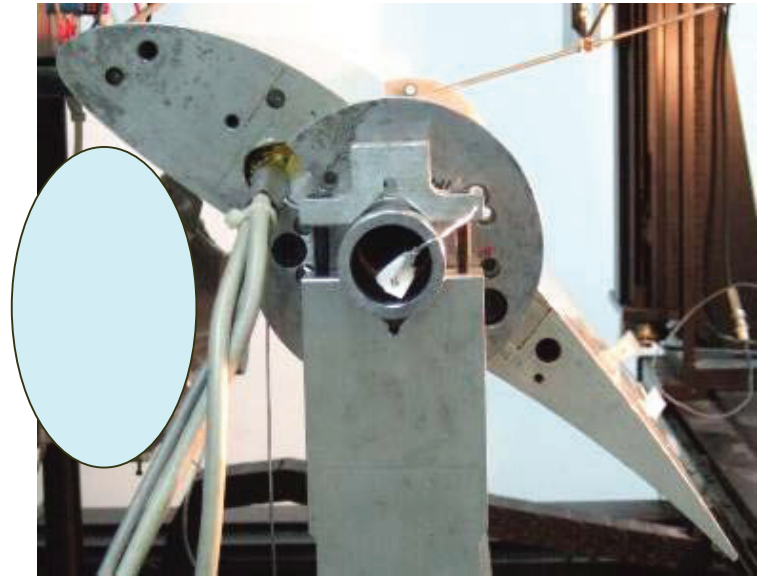
$$C_\Gamma \equiv \frac{(VR)^2}{C_L S_t}$$



IAI-Pr8-40 Airfoil AFC Testing



- Chord 360mm, span 609mm
- Actuator at $x/c=0.38$
- Shallow angle, downstream excitation
- 14 segmented, individually controlled
- Piezo actuators ($f_{\text{Helmholtz}}=1460\text{Hz}$)
- Slots: 0.9mm by 40mm
- Power: 1.7w per actuator at 100vac

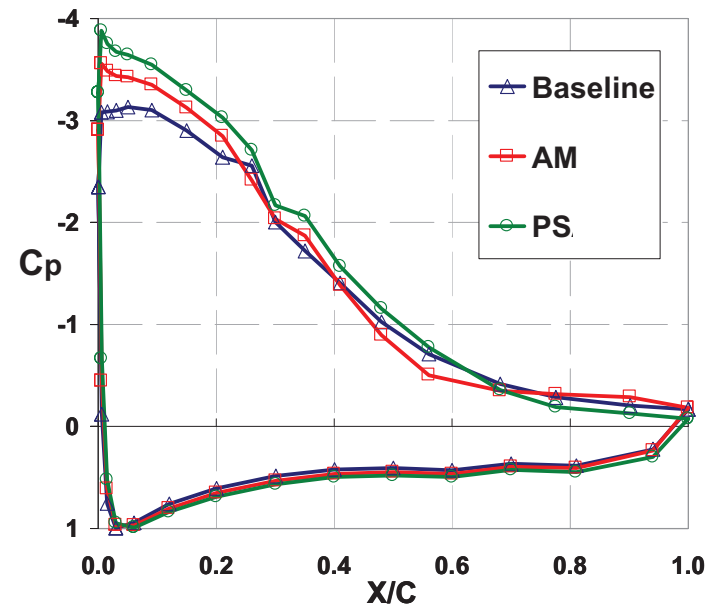
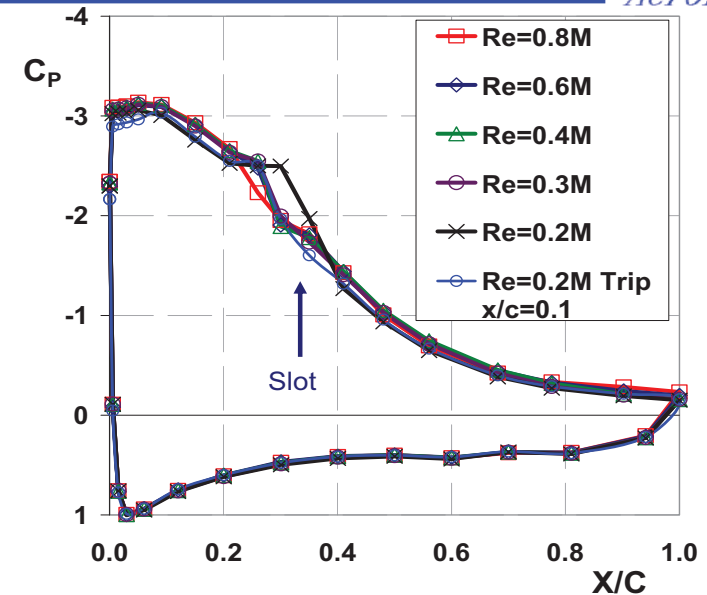
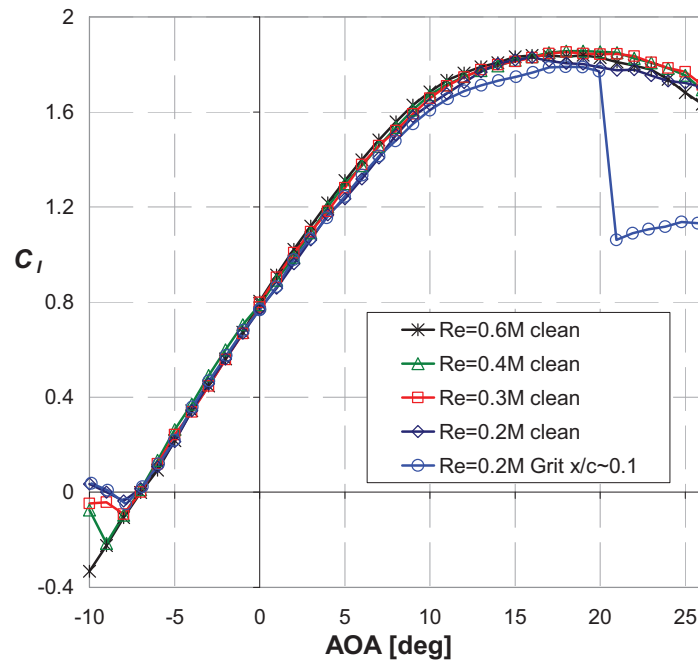




IAI-Pr8-40 Baseline



- Thick, Efficient, Low Re airfoil
- Mild, trailing edge stall
- Chord 360mm, span 609mm
- Actuator at $x/c=0.38$
- Shallow angle, downstream excitation
- 14 segmented, individually controlled
- Piezo actuators ($f_{\text{Helmholtz}}=1460\text{Hz}$)
- Slots: 0.9mm by 40mm

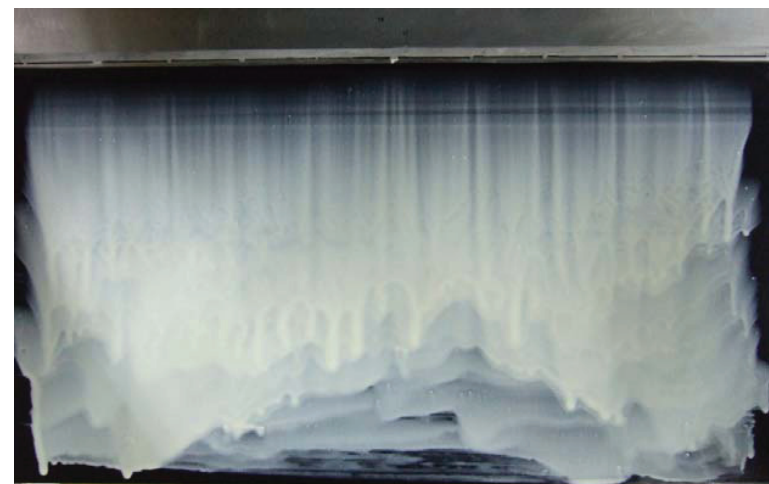
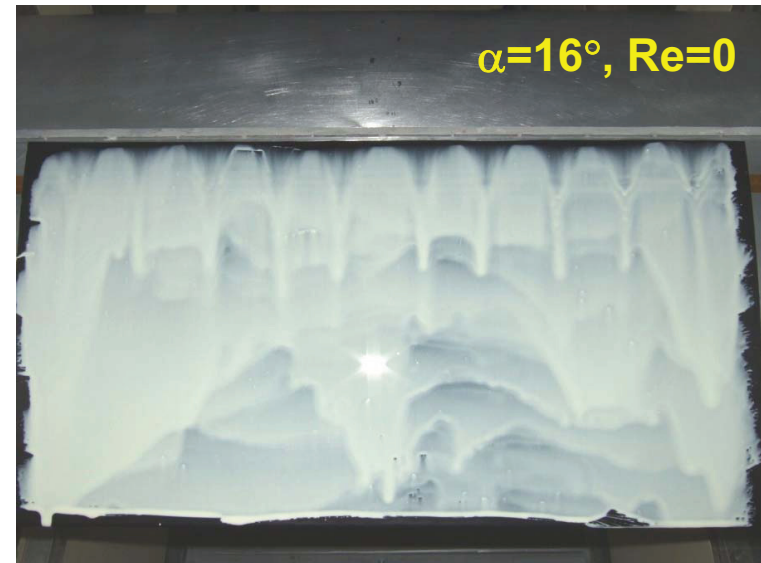
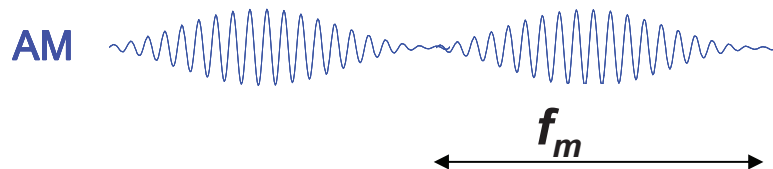




IAI-Pr8-40 Controlled



- Actuator at $x/c=0.38$
- Shallow angle, downstream excitation
- 14 segmented, individually controlled
- Piezo actuators ($f_{\text{Helmholtz}}=1460\text{Hz}$)
- Slots: 0.9mm by 40mm
- Two modes of operation:
 - Pure sine, Anti-phase, $F^+ > 10$
 - AM, In-phase, $F^+ \sim 1$
- Control of TBL separation
- Conducted amplitude scans at otherwise fixed conditions
- Scale lift increment vs amplitude



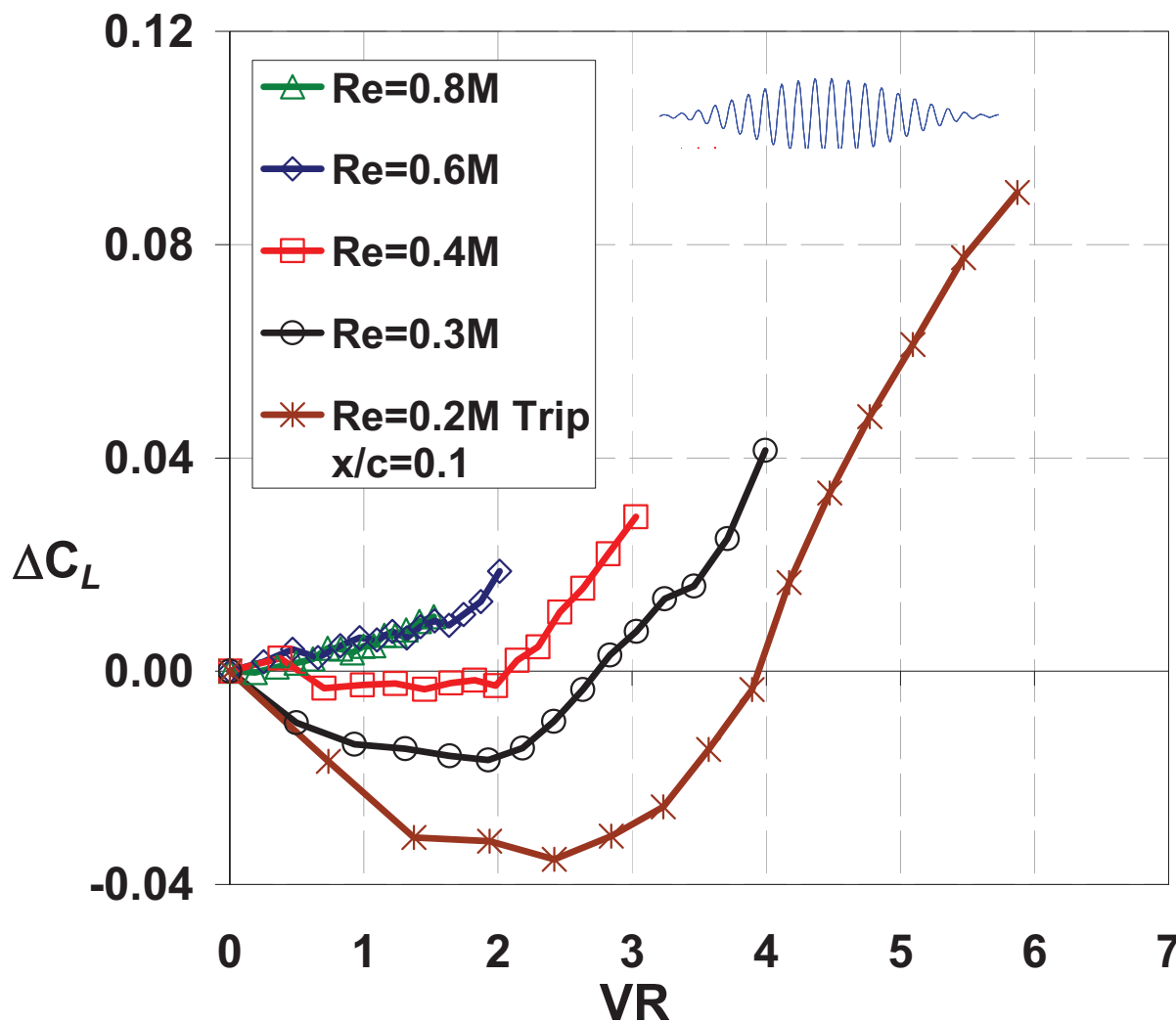


Low Frequency Amp Scaling



- Velocity ratio (VR)

$\alpha=16^\circ$, AM, $F^+=1$



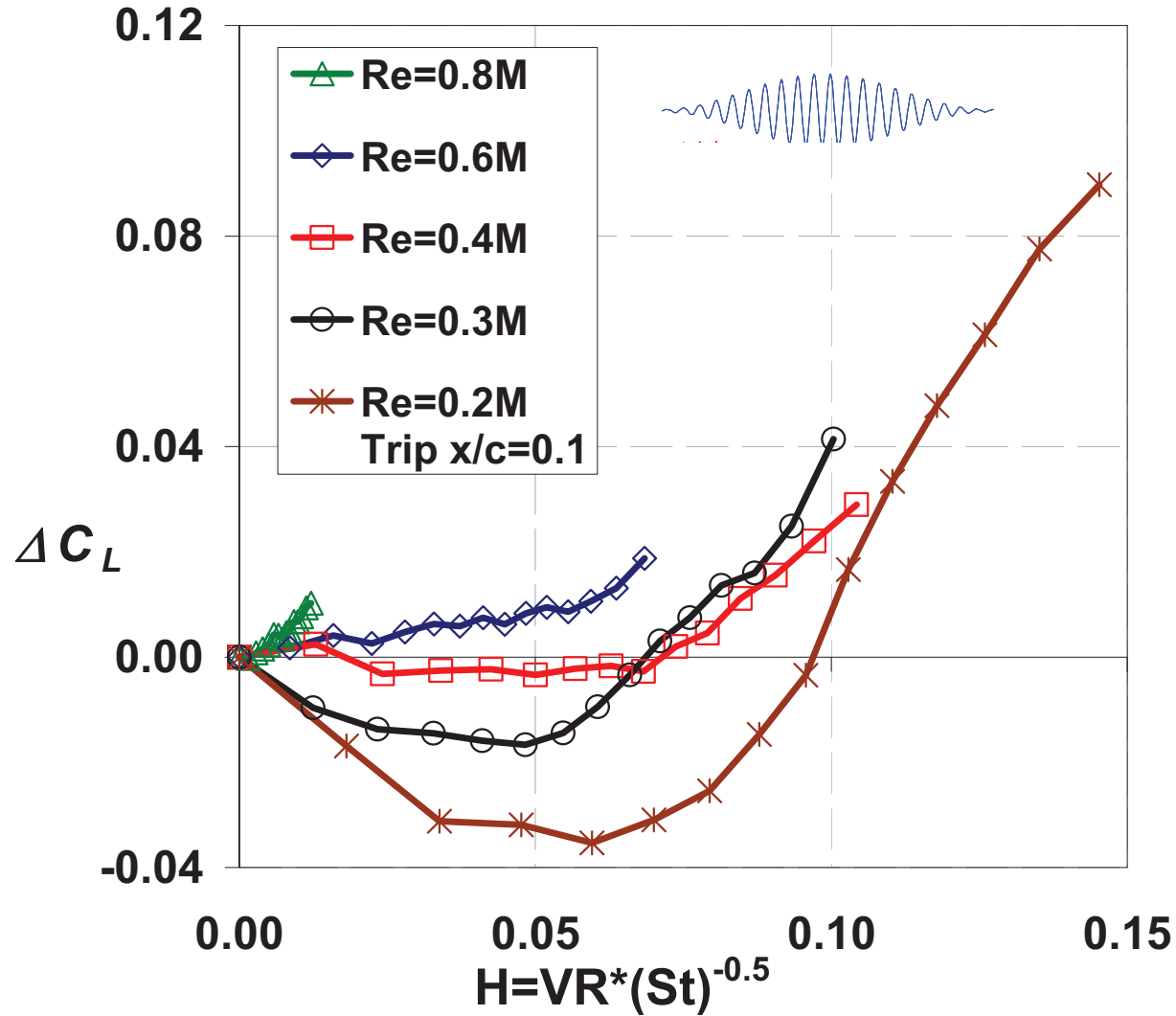


Low Frequency Amp Scaling



- St corrected VR

$\alpha=16^\circ$, AM, $F^+=1$



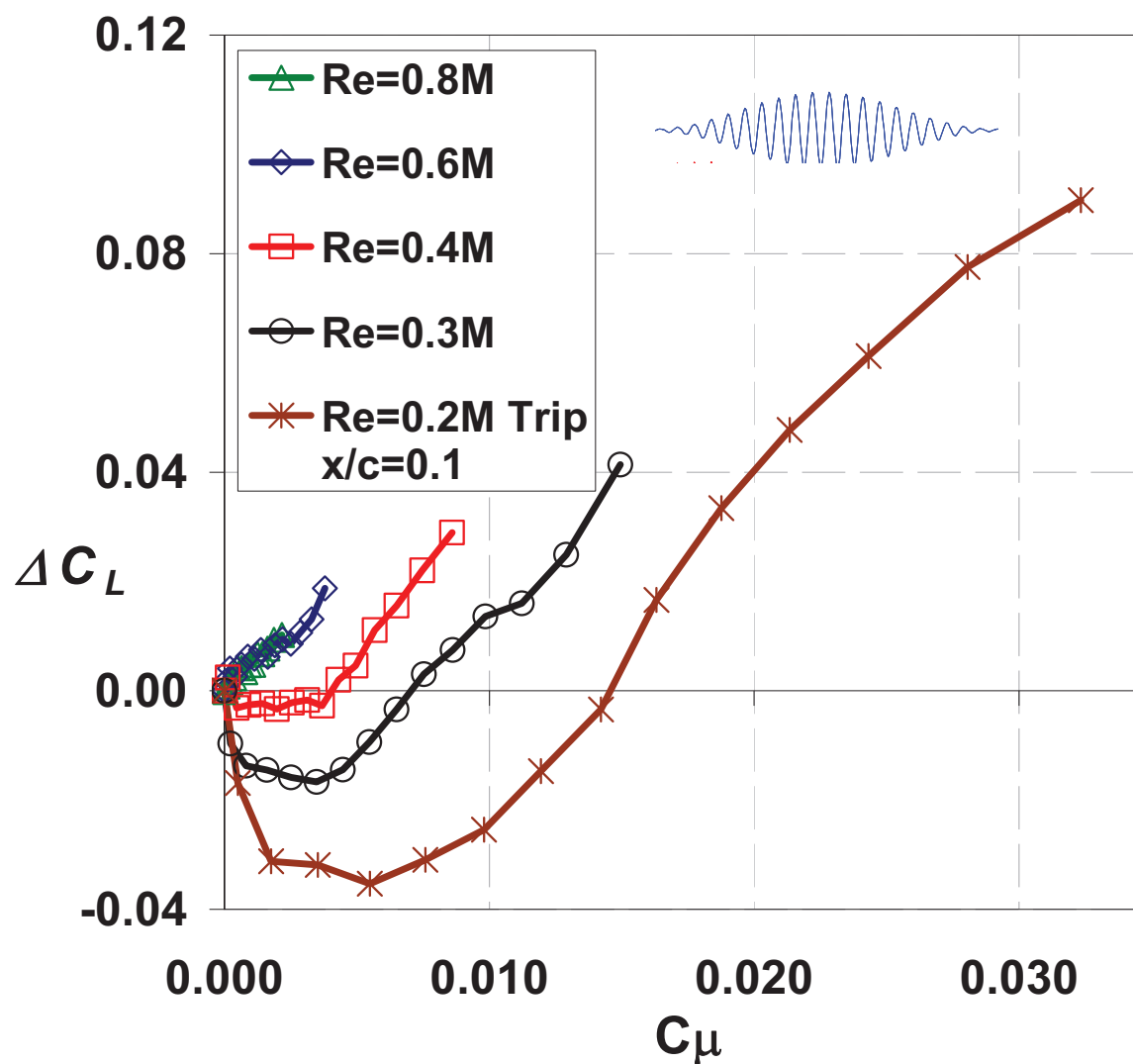


Low Frequency Amp Scaling



- Momentum Coefficient

$\alpha=16^\circ$, AM, $F+=1$



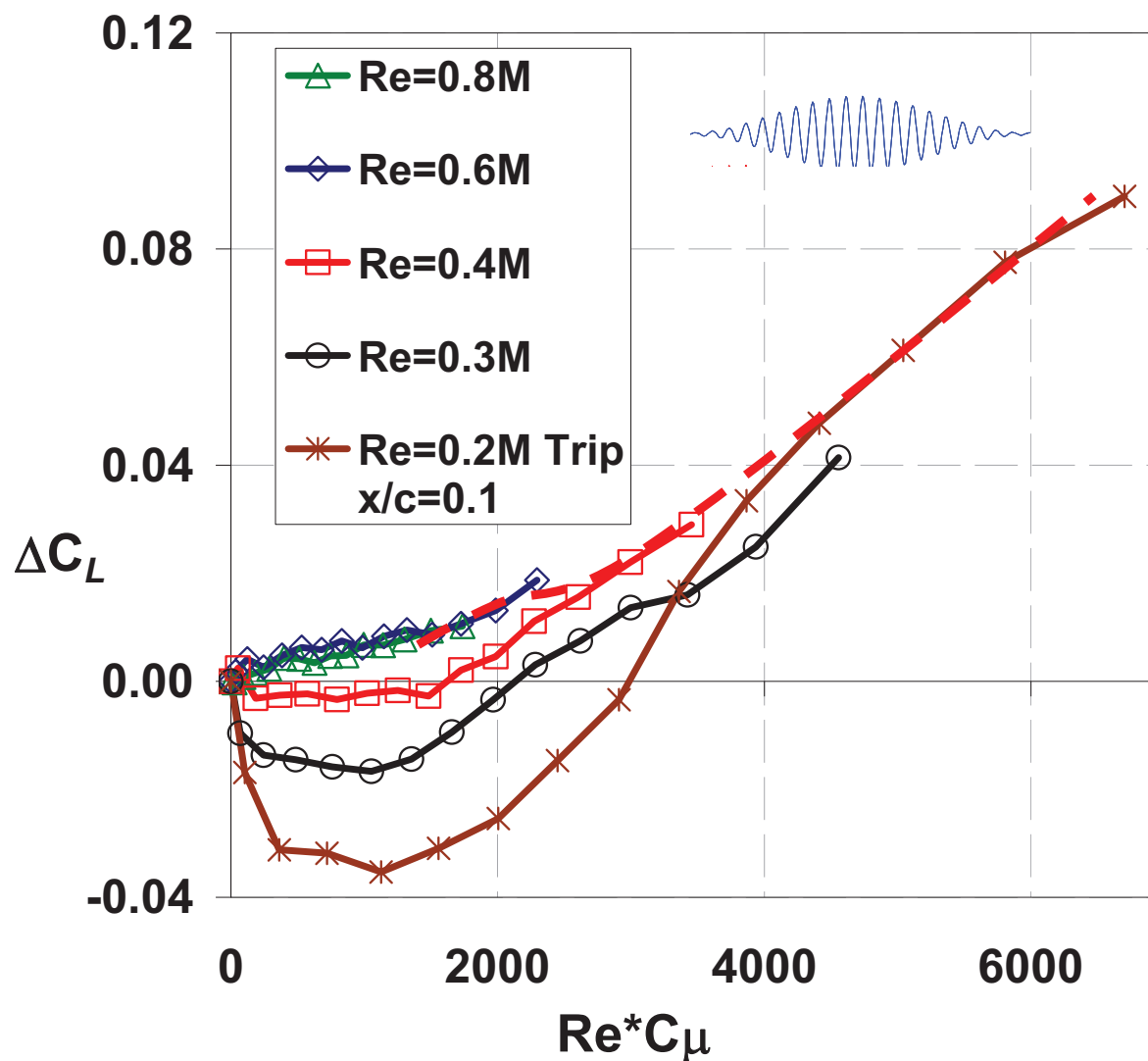


Low Frequency Amp Scaling



- Reynolds corrected Momentum Coefficient

$\alpha=16^\circ$, AM, $F+=1$

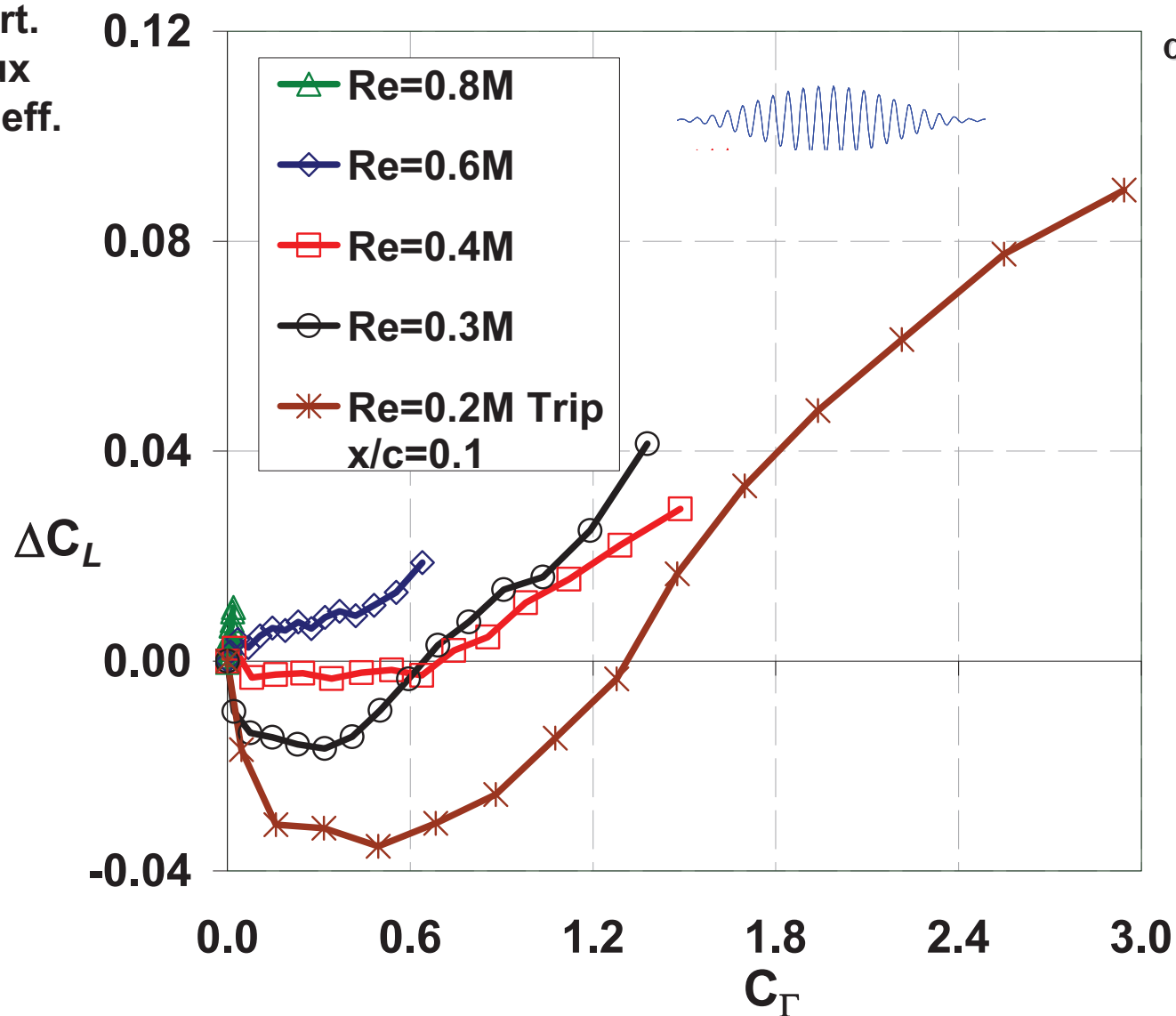




Low Frequency Amp Scaling



- Vort. Flux Coeff.

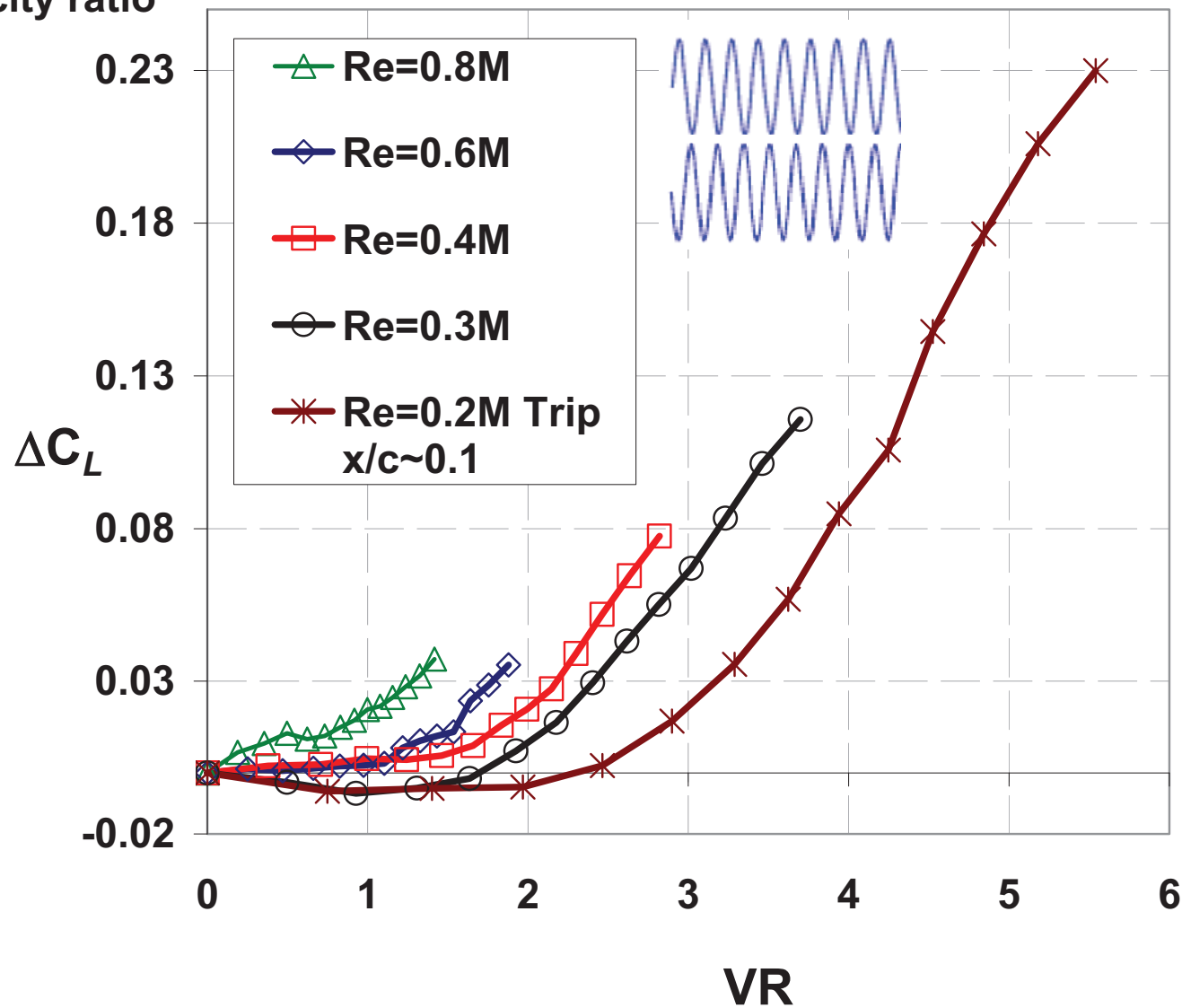




High Frequency Amp Scaling



- Velocity ratio

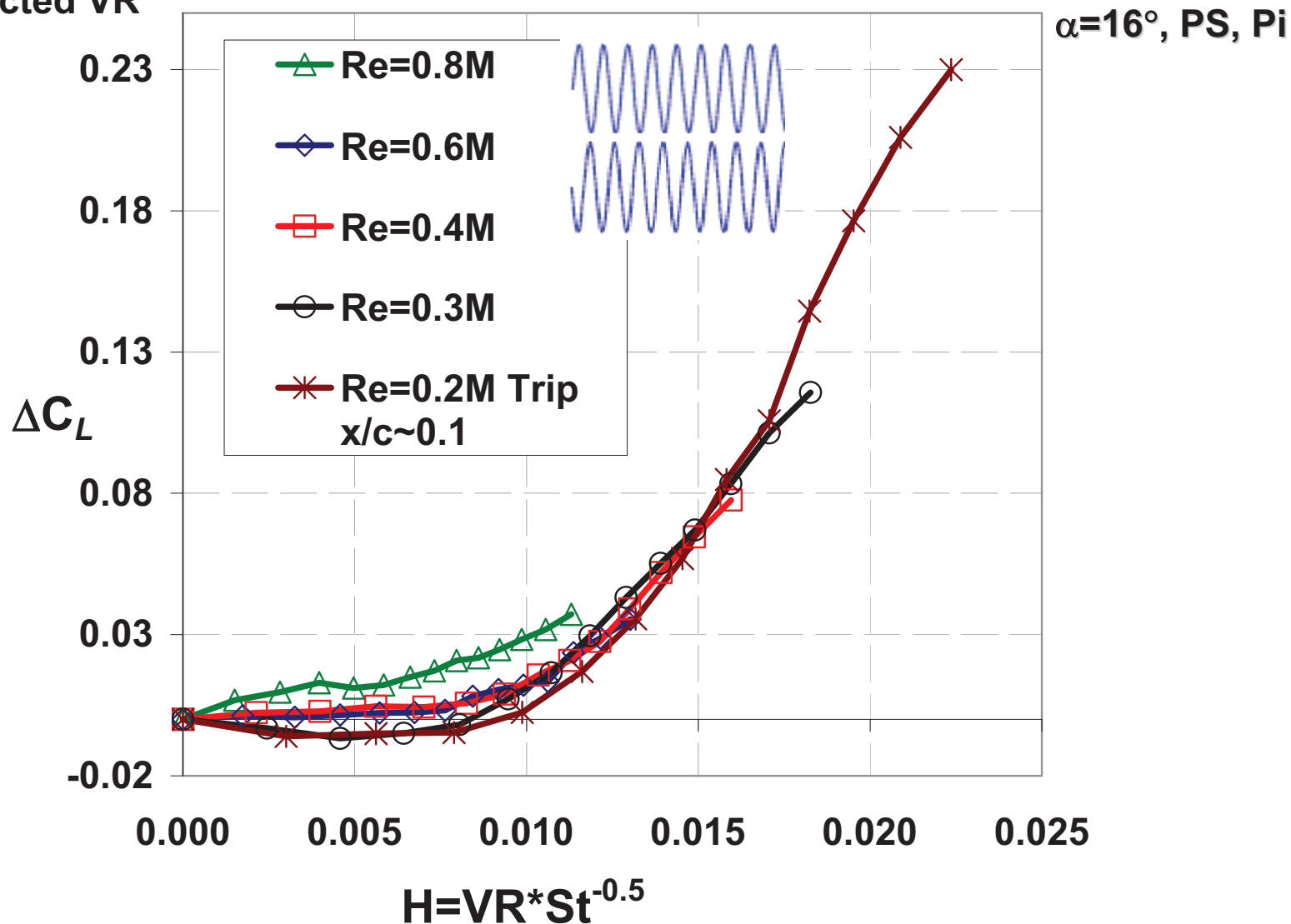




High Frequency Amp Scaling



- St corrected VR

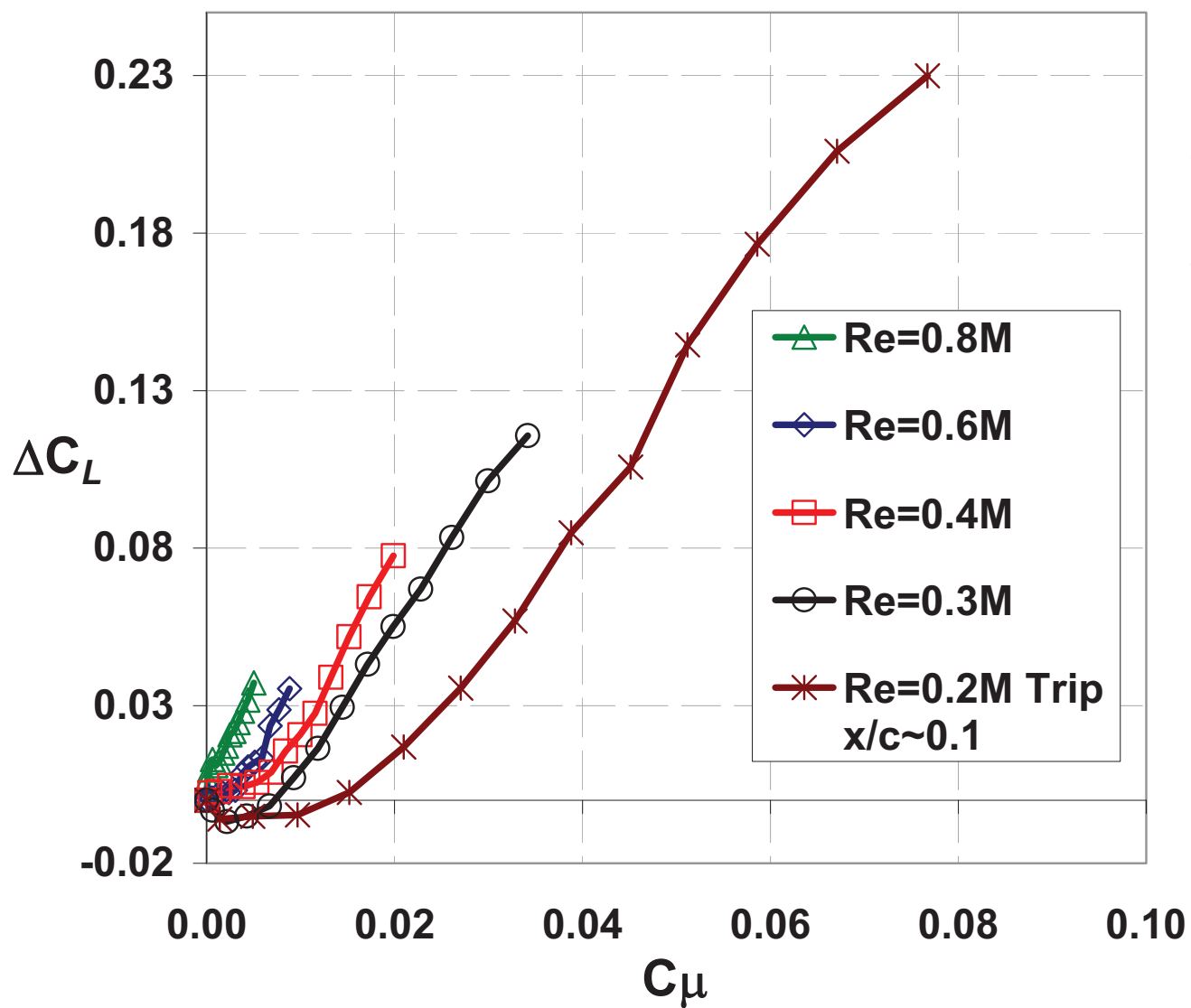




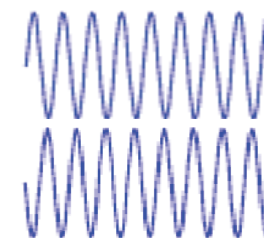
High Frequency Amp Scaling



• C_μ



$\alpha=16^\circ$, PS, Pi

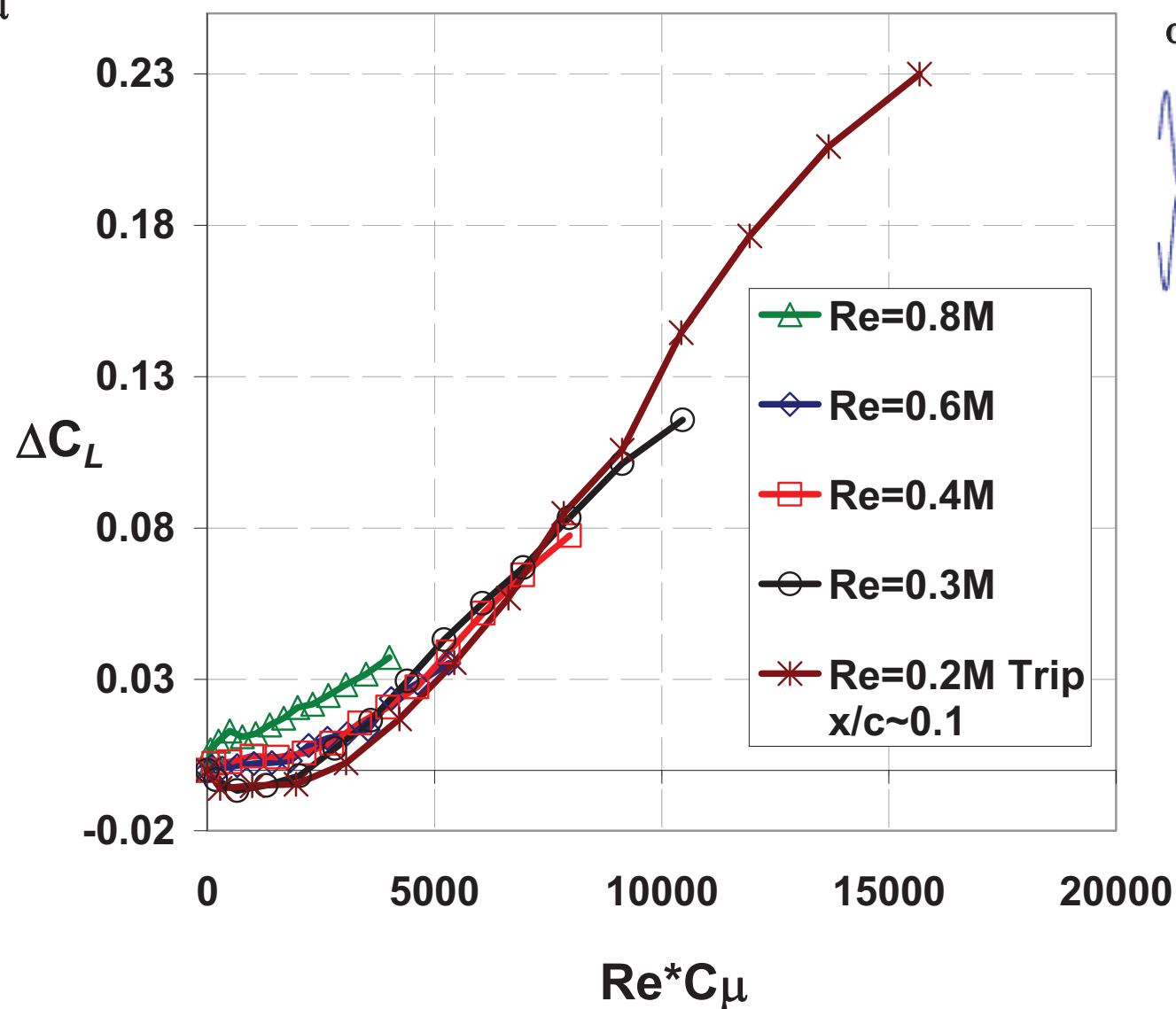




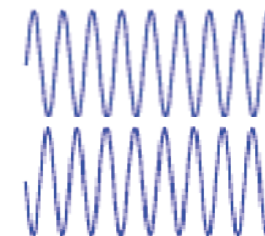
High Frequency Amp Scaling



- $Re \cdot C_\mu$



$\alpha=16^\circ$, PS, Pi

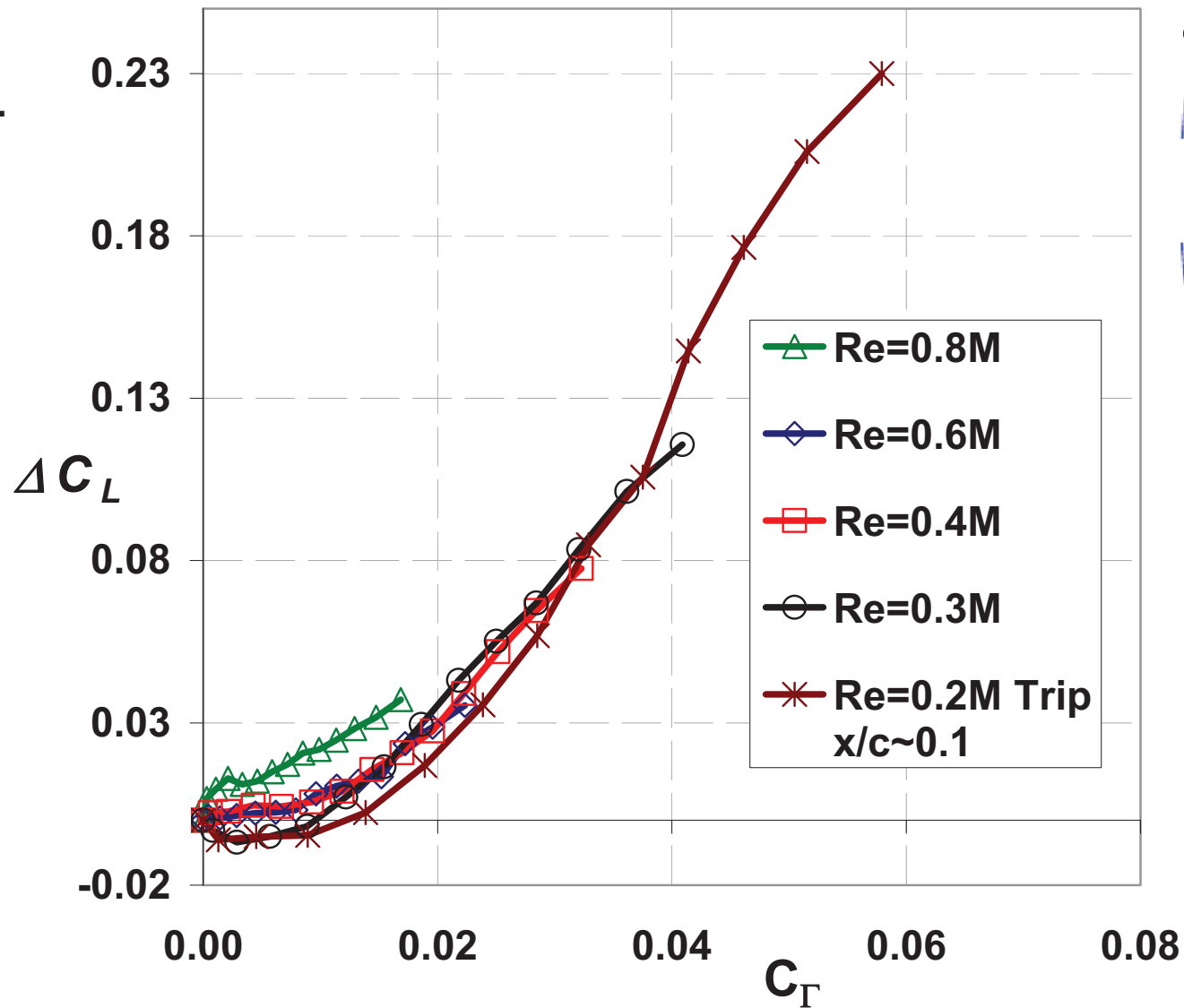




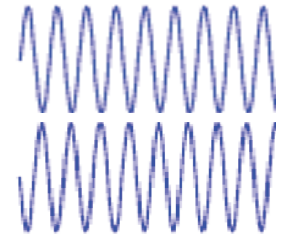
High Frequency Amp Scaling



- Vort. Flux Coeff.



$\alpha=16^\circ$, PS, Pi





Amplitude Scaling Summary



F⁺=1 **F⁺>10**

- **Velocity ratio (VR)**

$$VR \equiv \frac{U_p}{U_e} \approx \frac{U_p}{U_\infty}$$

X

X

- **Strouhal weighted VR (Nagib et al, 2006)**

$$H \equiv \frac{VR}{\sqrt{S_t}}$$

X

✓

- **Momentum coefficient**

$$C_\mu \equiv \frac{h}{c} (VR)^2$$

X

X

- **Reynolds corrected C_μ**
 - $m=0.2$ (Turb.), $m=0.5$ (Lam.)
 - used $m=1...$

$$C_{\mu, Re} \equiv \frac{h}{c} (VR)^2 Re^m$$

~ ✓

✓

- **Vorticity flux coeff.**

$$C_\Gamma \equiv \frac{(VR)^2}{C_L S_t}$$

X

✓



Conclusions



- Three existing and two new excitation magnitude scaling options for active separation control at Reynolds numbers below one Million.
- The physical background for the scaling options was discussed and their relevance was evaluated using two different sets of experimental data.
- For $F^+ \sim 1$, 2D excitation:
 - The traditional VR and C_μ - do not scale the data
 - Only the $Re \cdot C_\mu$ is valid
- This conclusion is also limited for positive lift increment.
- For $F^+ > 10$, 3D excitation, the Re corrected C_μ , the St corrected velocity ratio and the vorticity flux coefficient, *all* scale the amplitudes equally well.
- Therefore, the Reynolds weighted C_μ is the preferred choice, relevant to both excitation modes.
- Incidence also considered, using U_e from local C_p



Vorticity flux ratio - 4



- **Actuators also generate vorticity flux and alter circulation**

$$C_{VF} \equiv \frac{\left[U_p(t, y) \frac{dU_p(t, y)}{dy} \right]_{\max}}{\left[U_{BL}(y) \frac{dU_{BL}(y)}{dy} \right]_{\max}} \approx \frac{U_p^2}{h/2} \frac{\theta}{U_e^2} = \frac{2\theta}{h} \left(\frac{U_p}{U_e} \right)^2 \approx \frac{0.01c}{h} \left(\frac{U_p}{U_e} \right)^2$$

- **While the momentum coefficient**
- **For** $h/c = 0.005$ (and $\theta/c = 0.005$)

$$C_\mu \equiv \frac{2h}{c} \left(\frac{U_p}{U_e} \right)^2$$

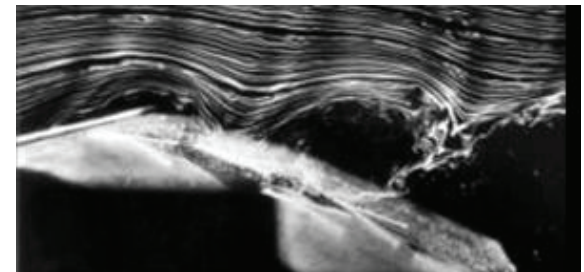
- **So the ratio** $C_{VF}/C_\mu \equiv \frac{0.01c}{h} \bigg/ \frac{2h}{c} = \frac{0.005c^2}{h^2} \approx \frac{5 \times 10^{-3}}{2.5 \times 10^{-5}} = 200$
- **Is very large; define *Vorticity Flux Coefficient***



AFC Open Forum: **Actuators Comparison Criteria**

Avraham “Avi” Seifert

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Acknowledgment:

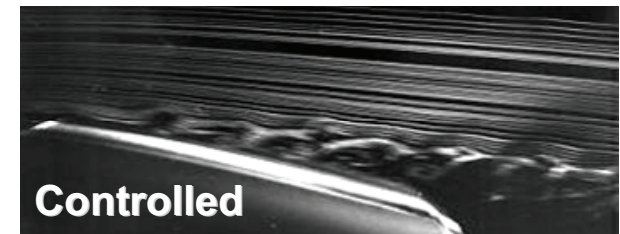
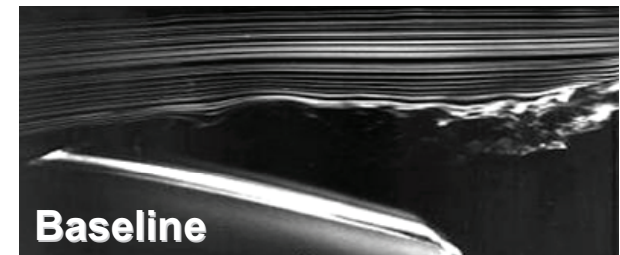
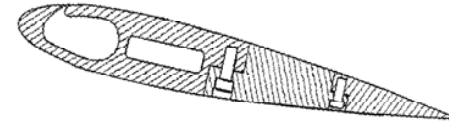
**I. Fono, G. Arwatz, T. Yehoshua, O. Stalnov, E. Ben-Hamou
I. Dayan, S. Paster, E. Nevo, Meadow Aero Lab members**



Motivation



- **Active control of boundary layer separation**
- **Actuation: key enabling technology**
- **Many actuator types exist**
- **No accepted criteria for actuator comparison**
- **Rare to find:**
 - **Energy, efficiency, weight, cost data**



(Neuburger, '89, $Re < 100k$)



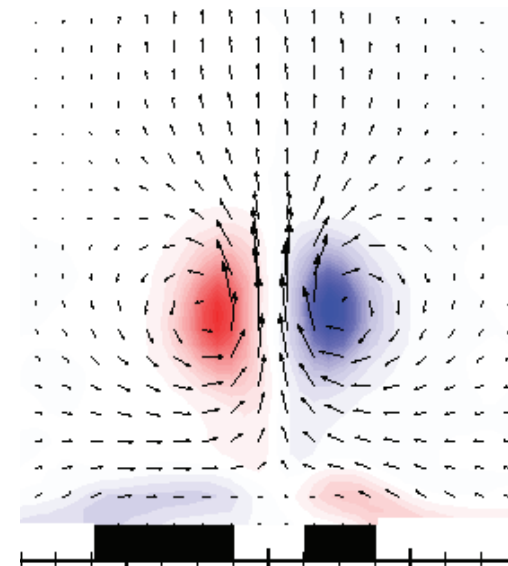
Comparison criteria: OFM



- **Overall Figure of Merit**
- **Actuator operates in still air**
- F_a – force generated
- When not/can not be measured could be estimated by
- With C from 0.25 to 0.5 (blowing only, velocity profile)
- U_p - peak generated velocity
- W_a – actuator weight
- P – actuator energy consumption
 - Electric, fluidic, combined

$$OFM \equiv \frac{F_a^2 U_p}{W_a P}$$

$$F_a \approx C \rho A_a U_p^2$$



(Yehoshua) 27



Comparison criteria: AFM-1



- **Aerodynamic Figure of Merit (1)**

$$AFM1 \equiv \frac{U_{\infty} L_c / (U_{\infty} D_c + P)}{(L/D)_{baseline}}$$

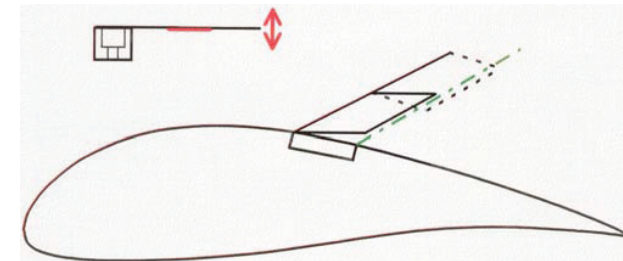
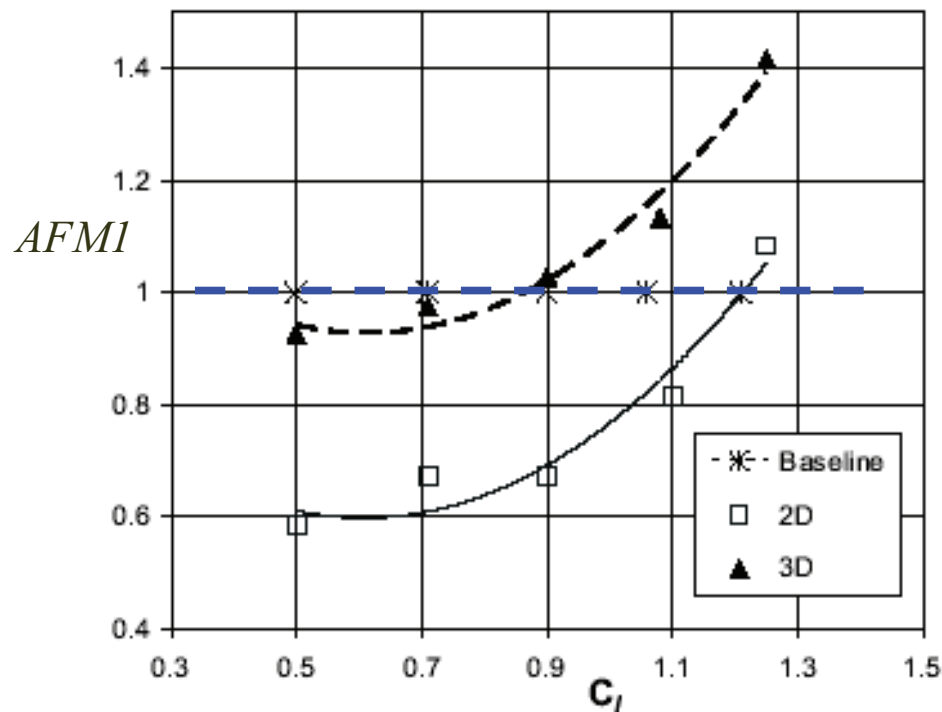
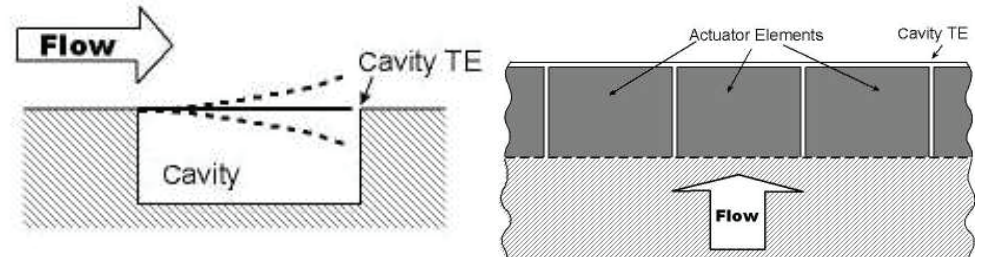
- Application, actuators and flow condition dependent
- U_{∞} – Free-stream velocity
- L – lift (baseline or controlled)
- D – Drag (baseline or controlled)
- P – actuator energy consumption
- Situation: Have system and actuators
- **Question:** Direct energy into power-plant or actuators?
- **Answer:** Only when $AFM1 > 1$ operate actuators



AFM-1 Example: 3D PZE



- Low Re Control of separation
- TAU Developed piezo-benders
- Considered energy efficiency
- Found that 3D excitation more effective than 2D



$$AFM1 \equiv \frac{U_{\infty} L_c / (U_{\infty} D_c + P_a)}{\left(\frac{L}{D} \right)_{baseline}}$$

(Seifert et al, '99)



Comparison criteria: AFM-2



- Aerodynamic Figure of Merit (2)**

$$AFM2 \equiv \frac{U_{\infty} (L_c - W_a) / (U_{\infty} D_c + P)}{\left(\frac{L}{D} \right)_{baseline}}$$

- Application, actuators and flow condition dependent
- U_{∞} – Free-stream velocity
- L – lift (baseline or controlled)
- D – Drag (baseline or controlled)
- W_a – weight of actuation system (incl. drivers, cables...)
- P – actuation SYSTEM energy consumption
- **Situation:** Scaled $AFM1 > 1$ and actuation system weight known (or predicted)
- **Question:** Should we include actuation in system?
- **Answer:** only when $AFM2 > 1$ (probably 1.1 minimum)



Actuation Methods



(Not a tutorial nor a comprehensive review)

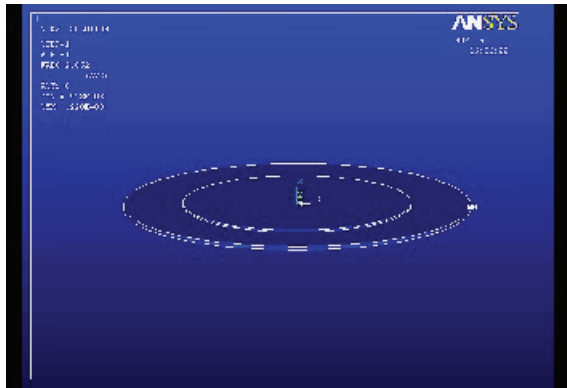
- **External**
 - Speakers on tunnel walls
 - Speakers in cavities
 - Mechanical rotary
 - Mechanical – pneumatic
 - Ribbons + shakers
- **Internal...**



ZNMF Piezo Actuator Operation

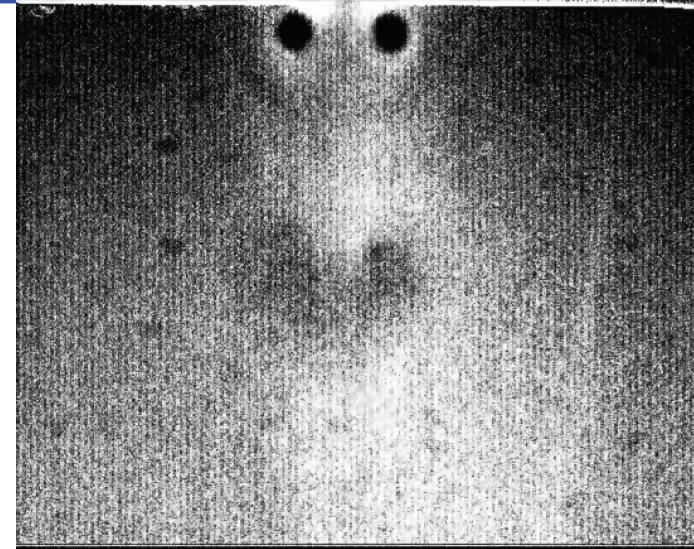


1St mode - Membrane

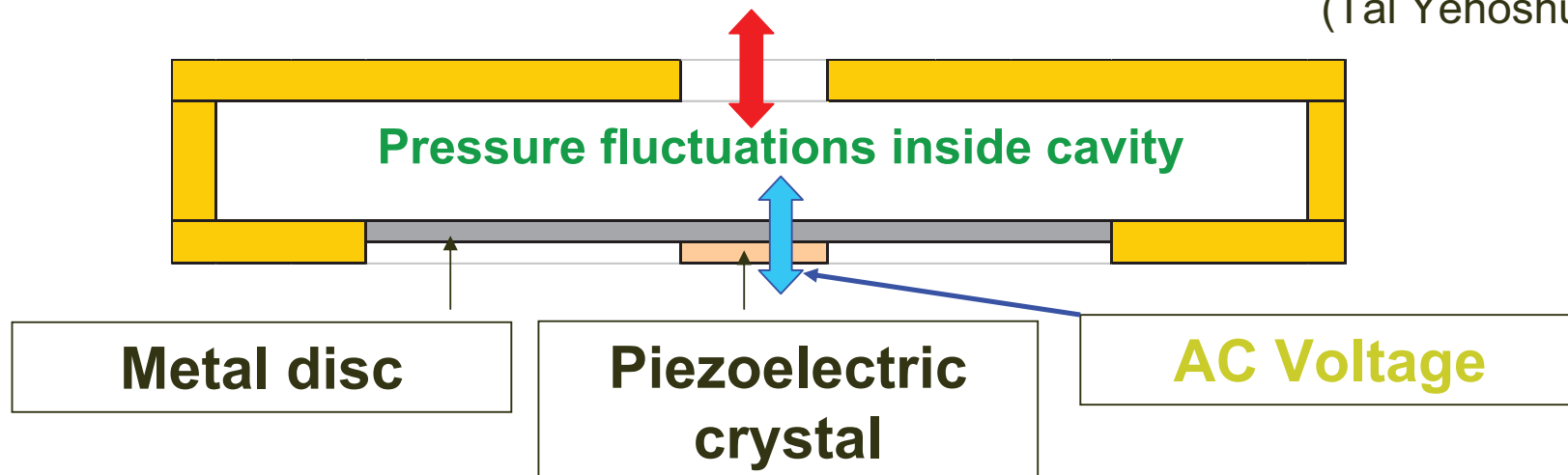


(Assaf Nahum)

**Zero
Net
Mass
Flux**



(Tal Yehoshua)

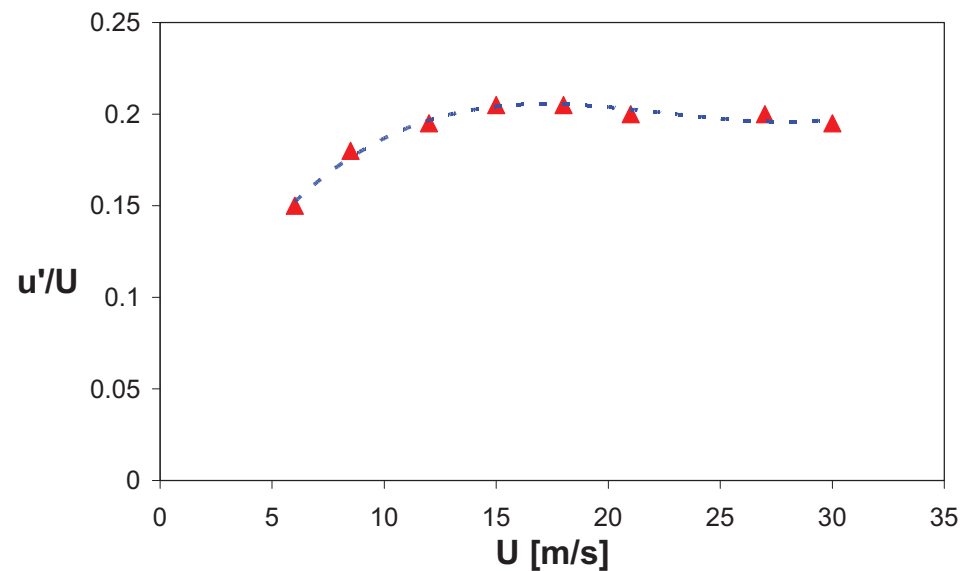
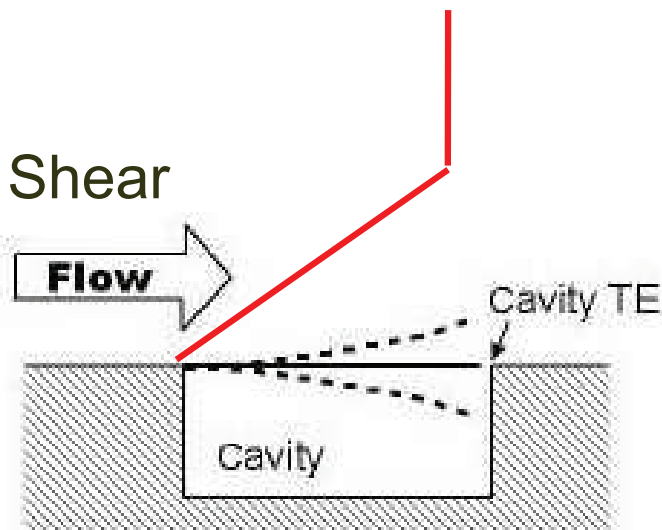




Surface Mechanical Actuators



- Requirement: Sufficient control authority (...any type)
- Type (affecting method and feasibility of characterization)
- Mechanical: Amplitude, Mode shape...
- Micro balloons, micro flaps...



(Seifert et al., 1998, *AIAA J.*, V. 36, N. 8.)



Combustion actuator

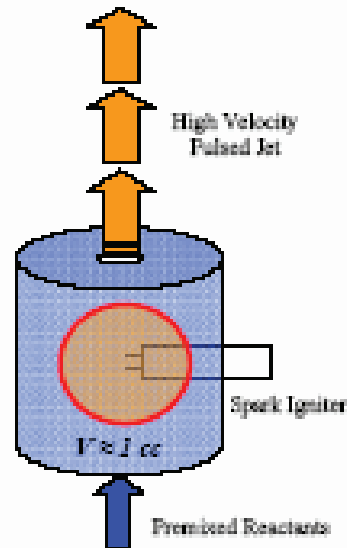
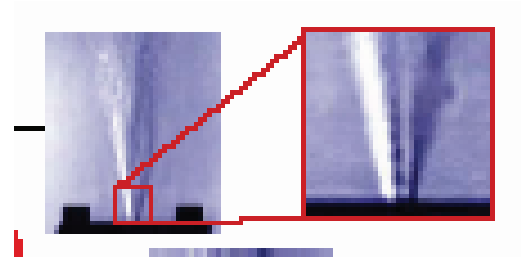


Figure 1. Schematic illustration of combustion-driven jet actuator



Microfabricated, Combustion-Driven Jet Actuators for Flow Control Applications

T. Crittenden and A. Glezer

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Surface Plasma actuator

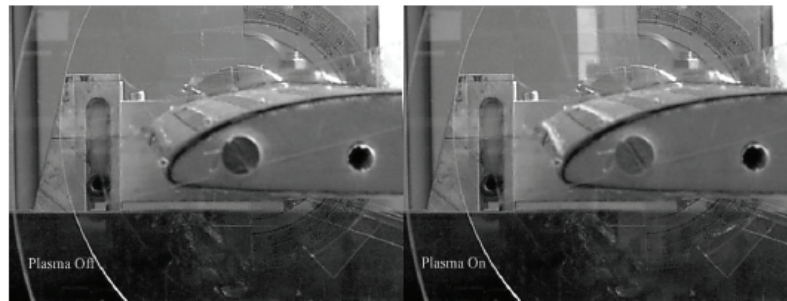
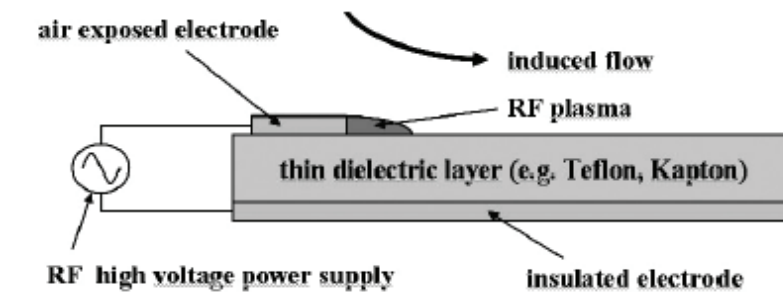


Figure 4 Two activated plasma actuators with 180° phase shift on the leading edge

Actu power – 17W/m

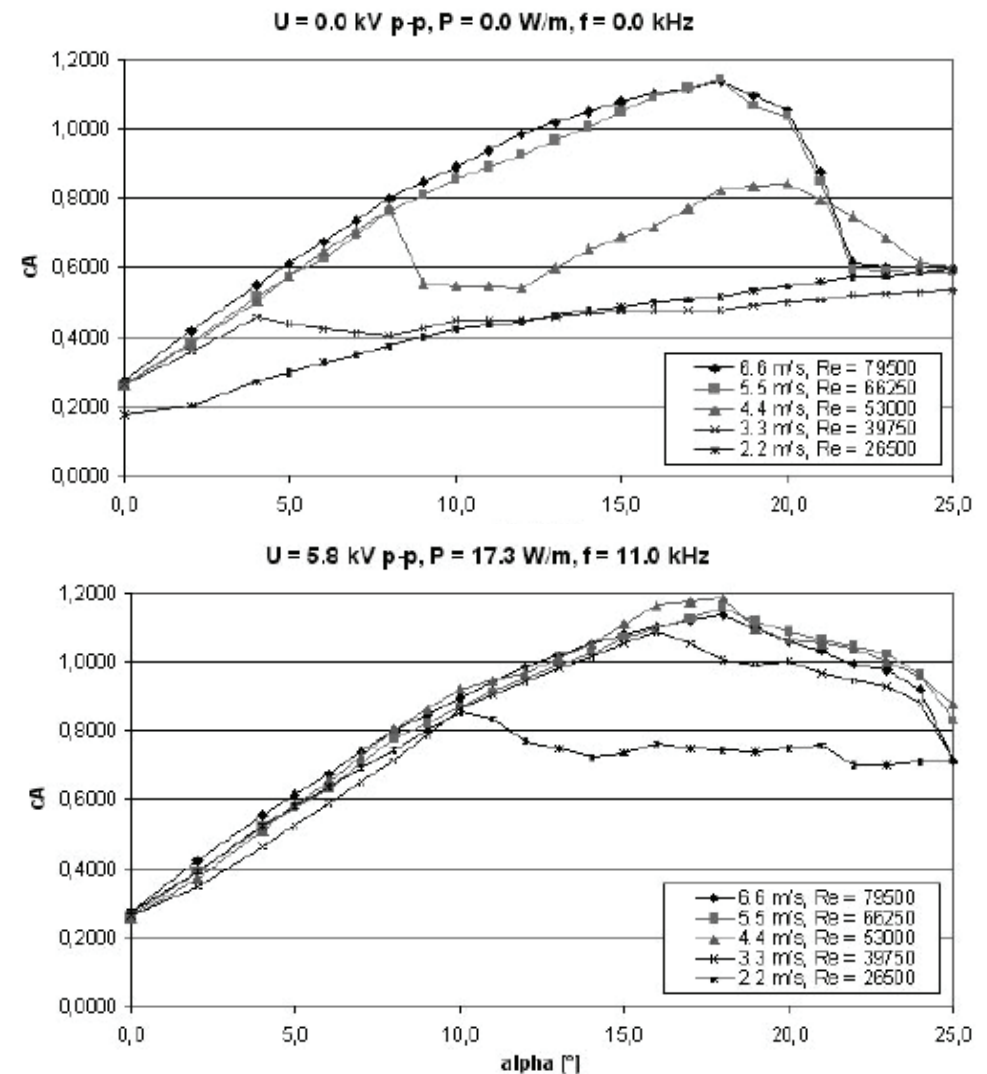
$U_{inf}=2-6\text{m/s}$

Plasma $U_p=2-4\text{m/s}$

Lift recovery for $Re \leq 50k$

No drag data

$1/2 \rho U^3 = 4.4\text{Watt}$

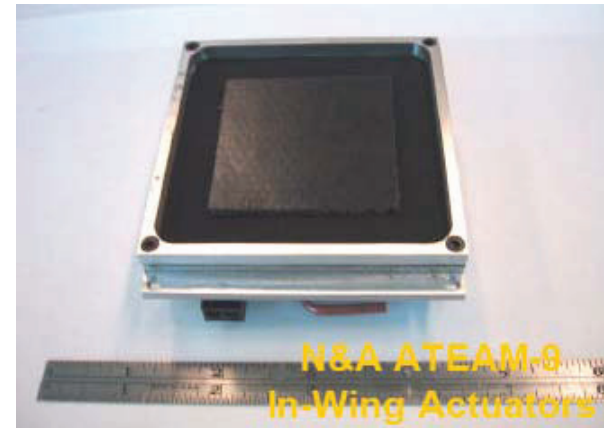


Active Flow Control by Surface Smooth Plasma Actuators

B. GÖKSEL, I. RECHENBERG, TUB



Electro Magnetic actuator (XV-15)



Actu power – 1000W/m
Up=80m/s
Wa>3kg

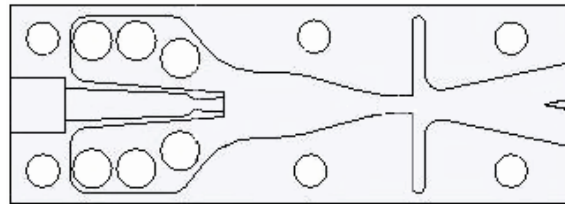


http://fdrc.iit.edu/research/docs/MAFC_XV_15_Briefing_Final.pdf



TAU

Suction and Oscillatory Blowing (SaOB) Actuator

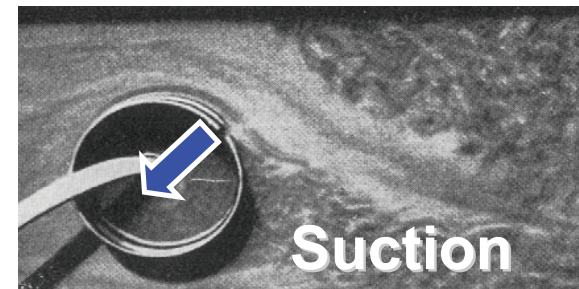
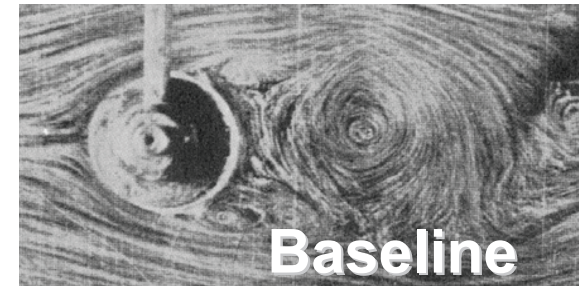




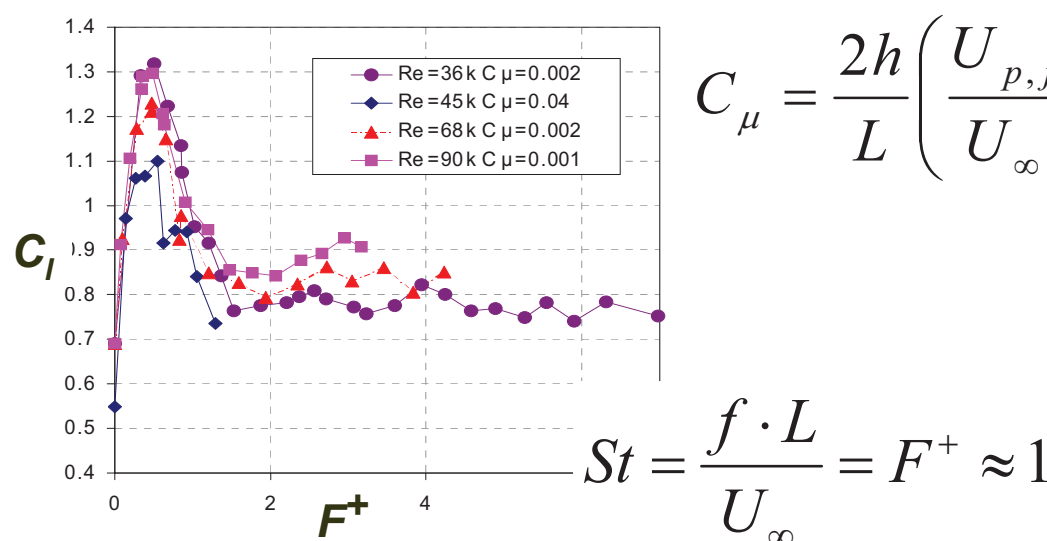
Background



- Boundary layer separation control by steady suction (note date...)
- Steady, wall tangential blowing
- Oscillatory blowing (directed ZMF)
- The importance of flow instability for efficient AFC

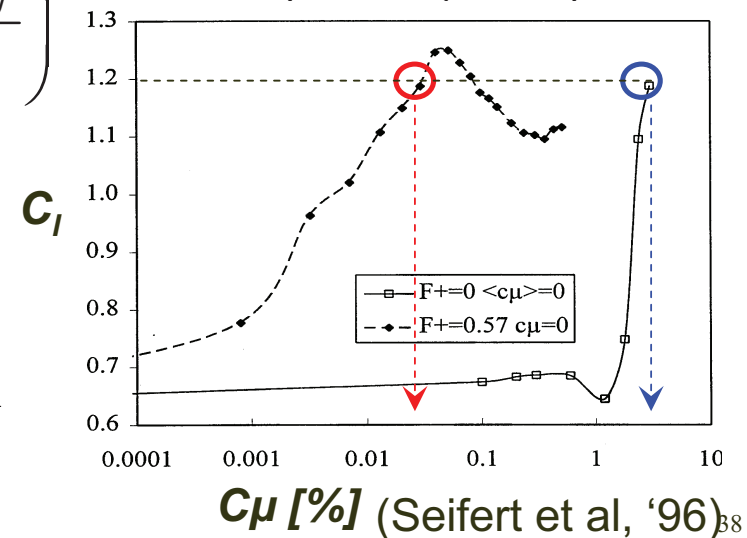


(Prandtl, 1904)



(Yom-Tov & Seifert, '05)

$$C_\mu = \frac{2h}{L} \left(\frac{U_{p,j}}{U_\infty} \right)^2$$



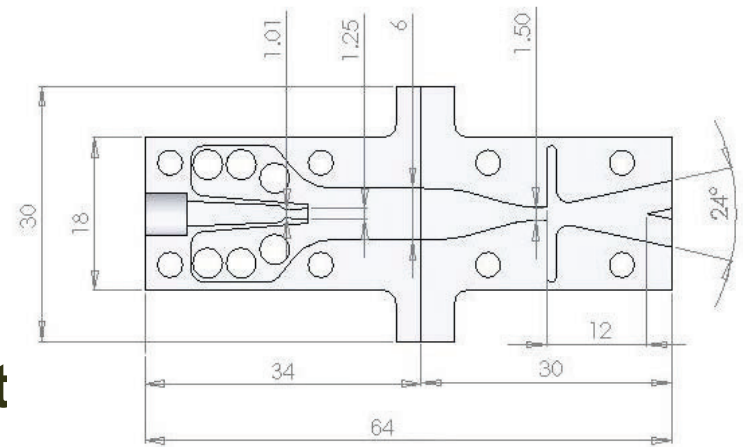
C_μ [%] (Seifert et al, '96)₈₈



The SaOB actuator concept



- G. Arwatz (MSc), I. Fono, London MEMS IUTAM, Sep '06
- Available ZNMF devices limited to $M=0.3$
- Suction and oscillatory blowing – high potential for efficient AFC
- **Combination of *steady suction and oscillatory blowing in one device***
- High velocity, near sonic, output
- Wide range of output frequencies
- Enables 3D excitation
- Frequency proportional to flow rate
- No moving parts
- Low power consumption



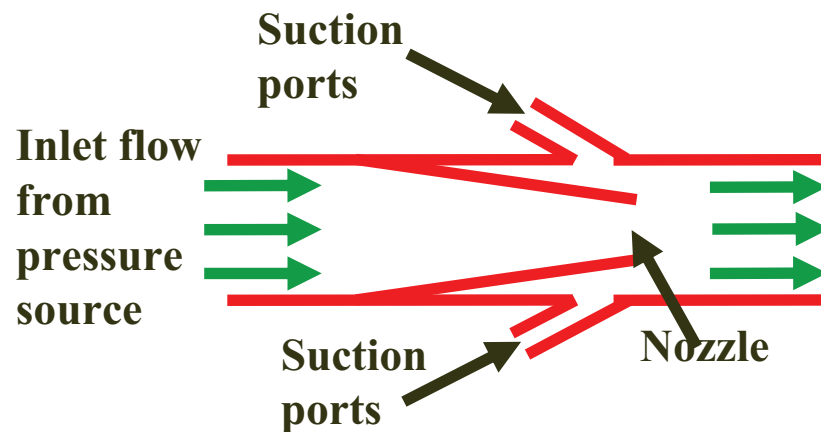


The SaOB actuator concept

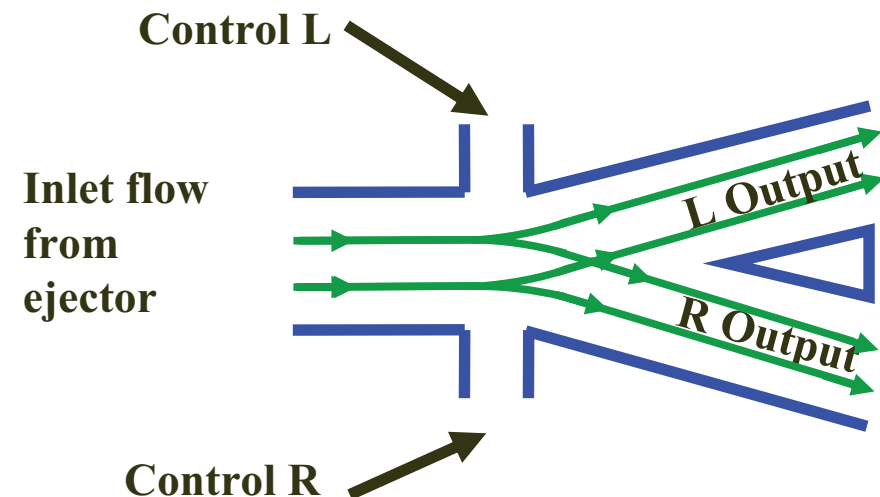


- Combination of ejector and switching valve

Ejector (steady suction)



Bi-stable fluidic amplifier (oscillatory blowing)

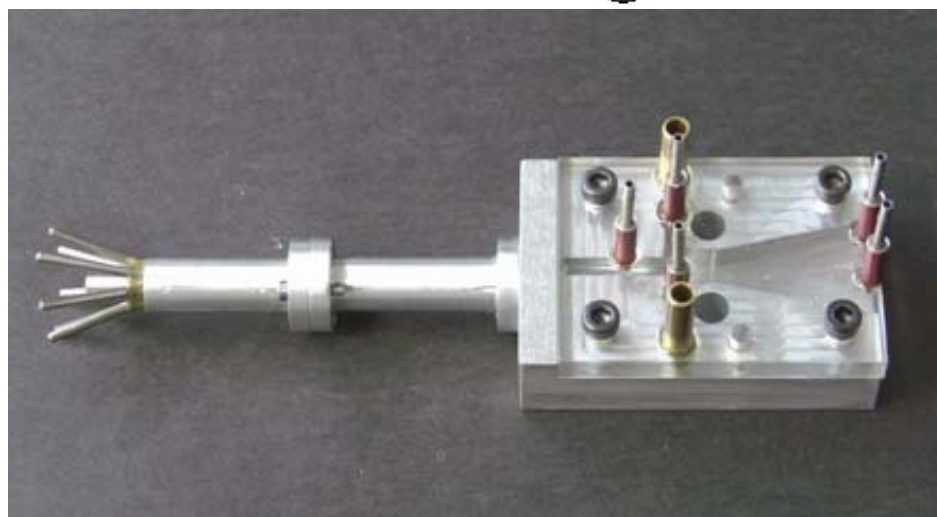
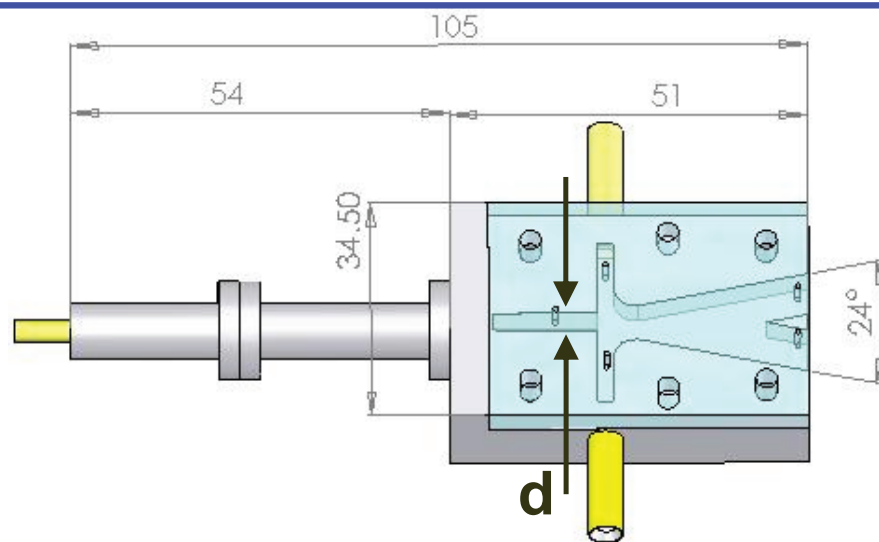




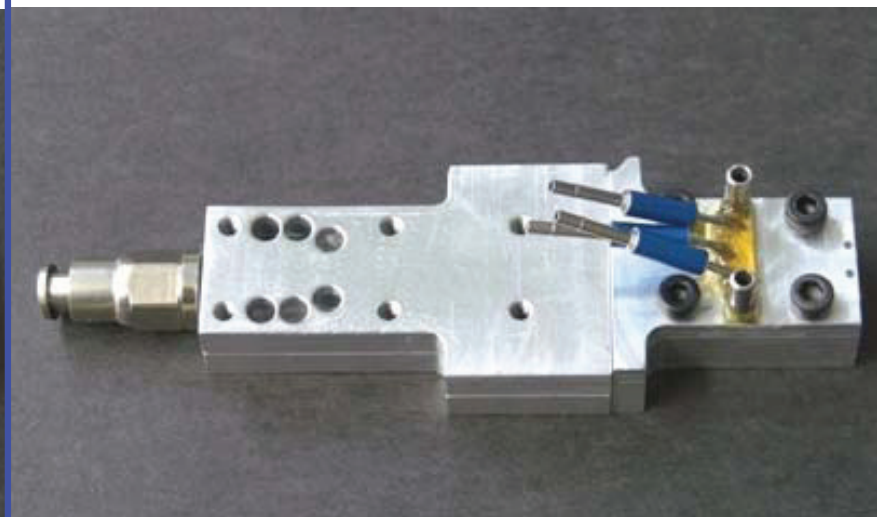
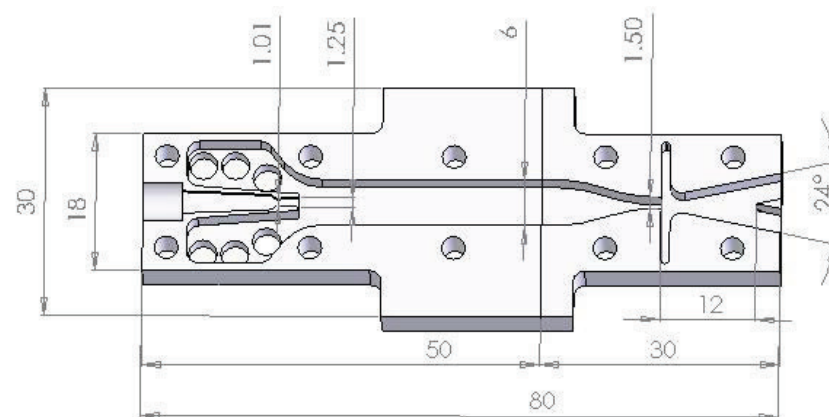
Valve generations, 2nd & 3rd



Medium scale $d=3\text{mm}$



Small scale $d=1.5\text{mm}$





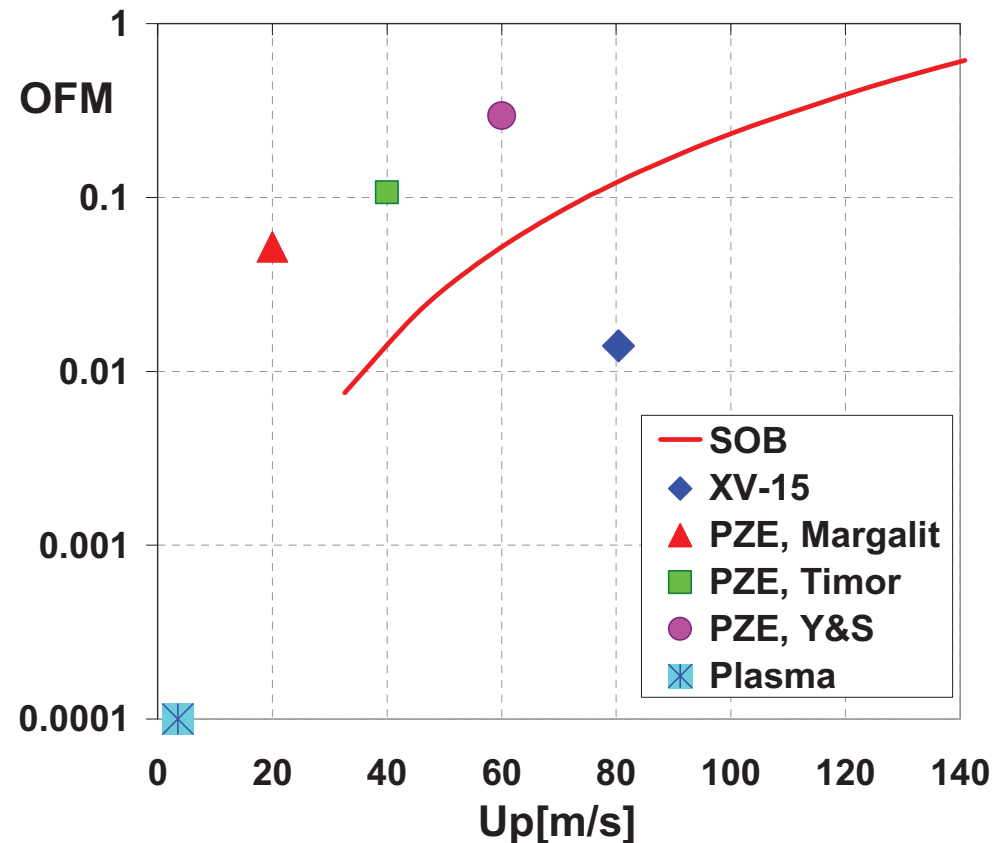
Actuators' Efficiency



- Overall Figure of Merit

$$OFM = \frac{F_a^2 U_p}{W_a P_a}$$

- Still air operation
- SaOB weight - 15 gm
- Thrust-suction+blowing
- Note: OFM Log scale





Summary (Actuators)



- **Actuator comparison criteria suggested**
- **Overall and Aerodynamic figures of merit**
- **New actuator for steady suction and oscillatory blowing was developed, modeled and characterized**
- **OFM for ZNMF, Plasma and SaOB actuators compared**
- **Rare to find data for AFM (Need: Weight, power, Up, L, D)**
- **Please measure and publish**