

UNIVERSIDAD POLITÉCNICA DE MADRID
E.T.S. de Ingenieros Aeronáuticos

**GLOBAL INSTABILITY
OF LAMINAR SEPARATION BUBBLES**



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PM: Douglas Smith
AFOSR Grant: FA8655-06-1-3066

POLITÉCNICA

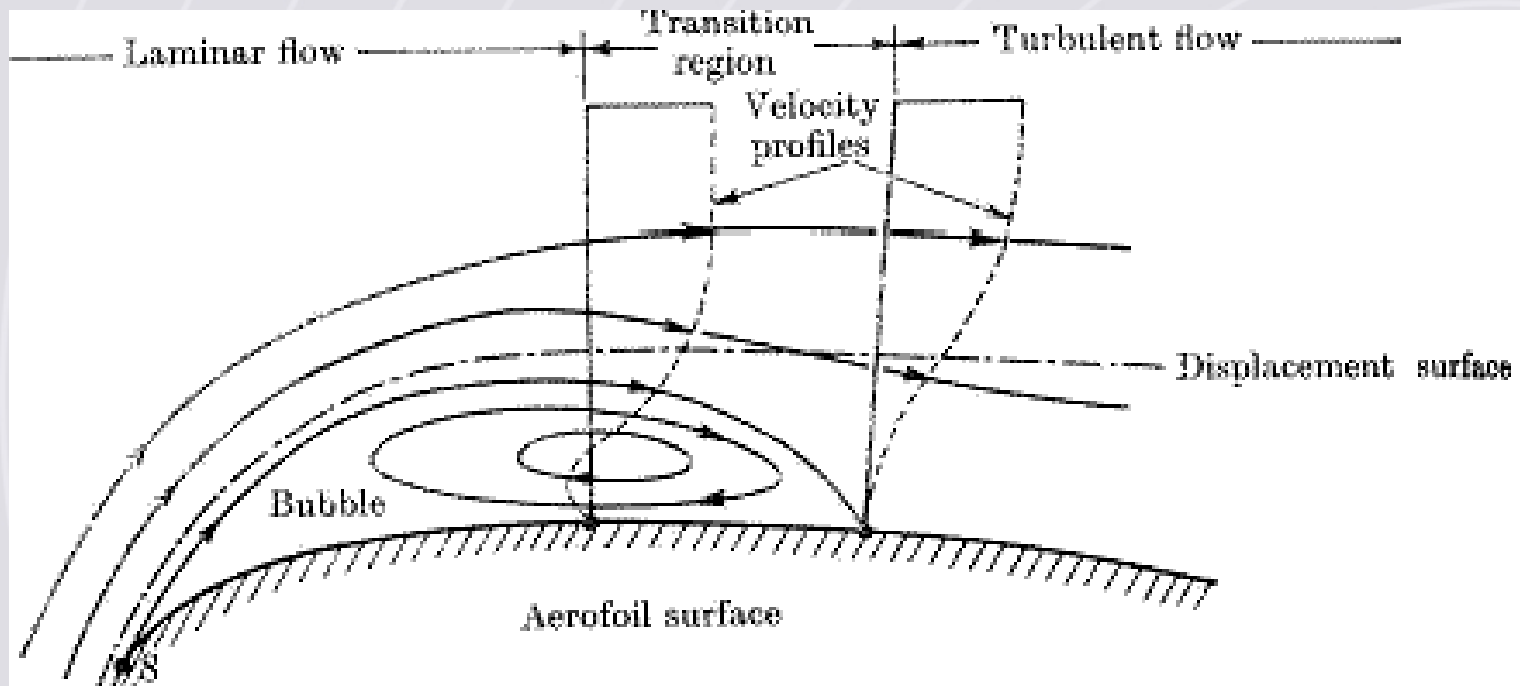


Introduction and Background



COMMON WISDOM ON LSB

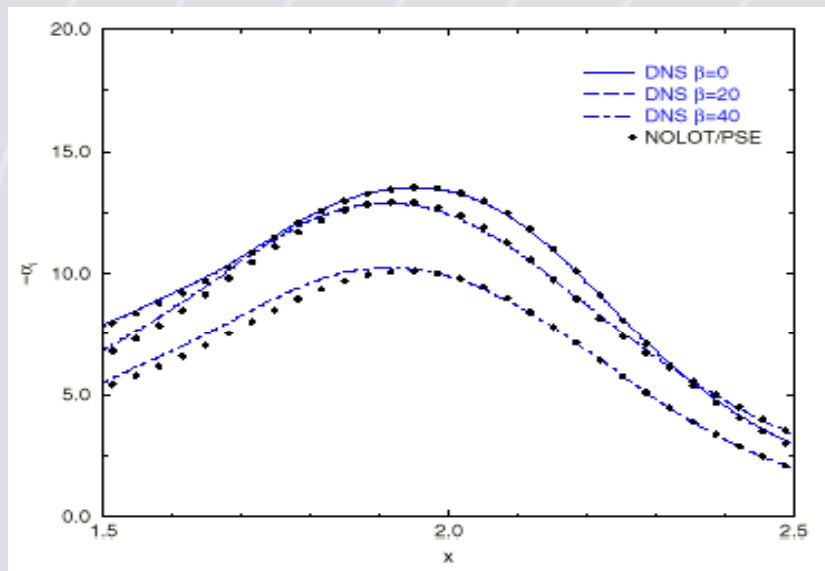
- Separation under adverse pressure gradient
- Reversed flow region enclosed → Shear layer
- Kelvin-Helmholtz instability → transition to turbulence
- Turbulent strong mixing forces re-attachment



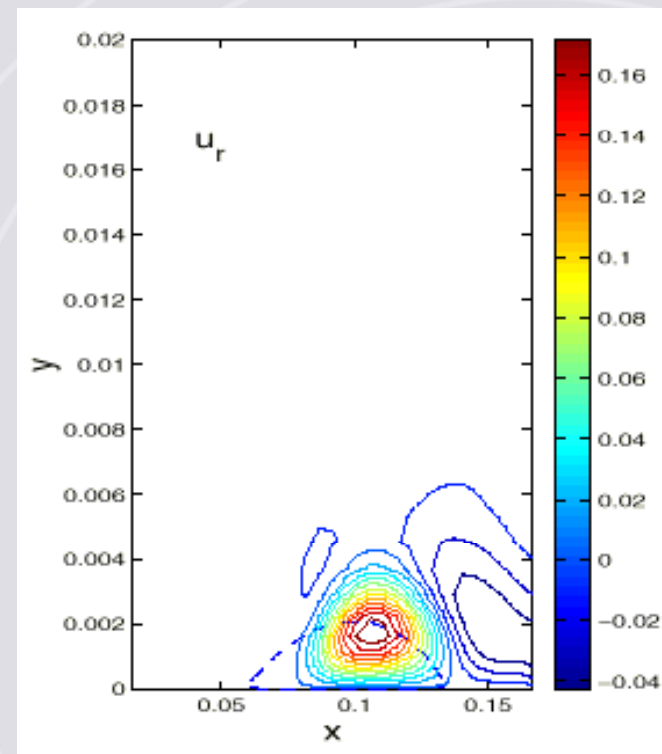


A MORE RECENT VIEW

- **Two different classes of eigenmodes:**
Shear-layer/KH



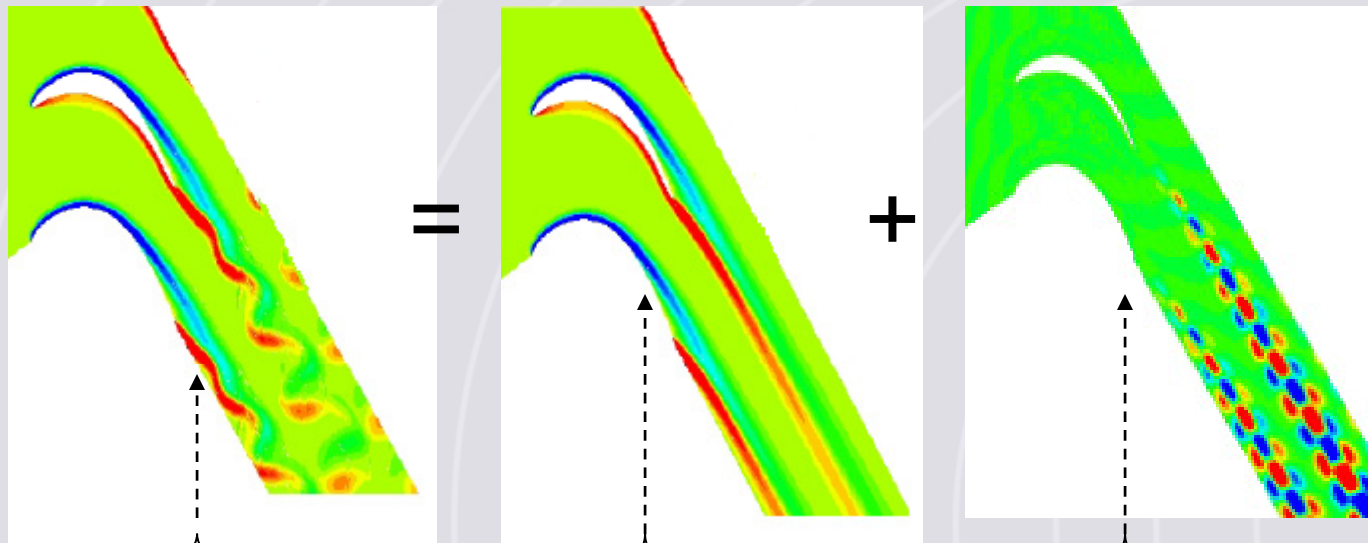
- Global mode





LPT FLOWS – THE (SL) WAKE MODE

- Amplification of the **wake mode** gives rise to the 2D time-periodic basic state

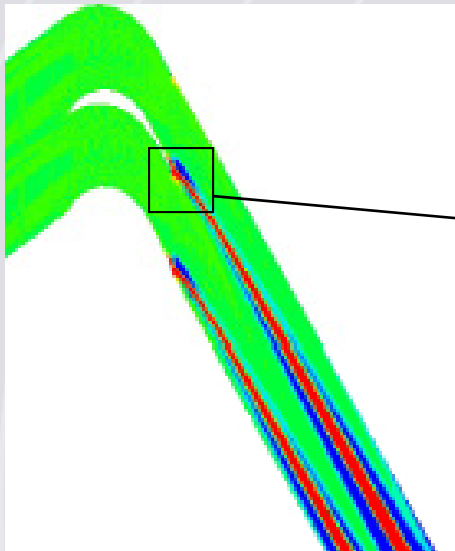


$$\mathbf{q}(x, y, t) = \bar{\mathbf{q}}(x, y) + \varepsilon \hat{\mathbf{q}}(x, y) \exp \Theta$$

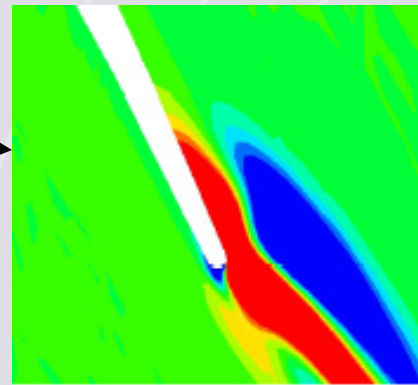


LPT FLOWS – THE BUBBLE MODE

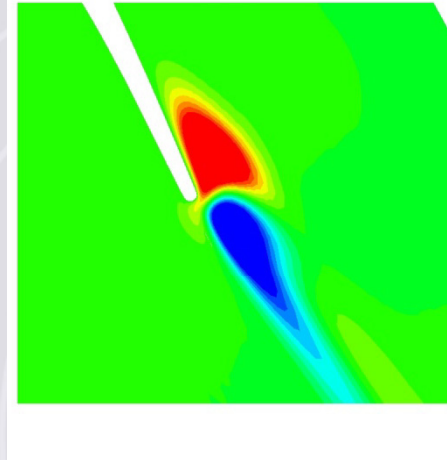
The **bubble mode** is stronger damped than the wake mode is



disturbance vorticity



spanwise velocity

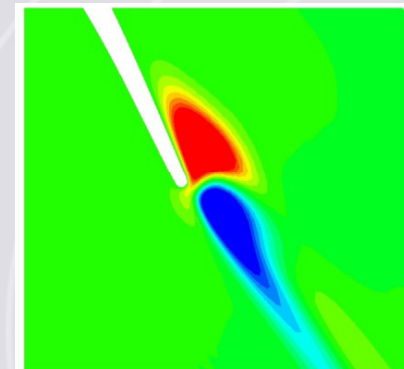
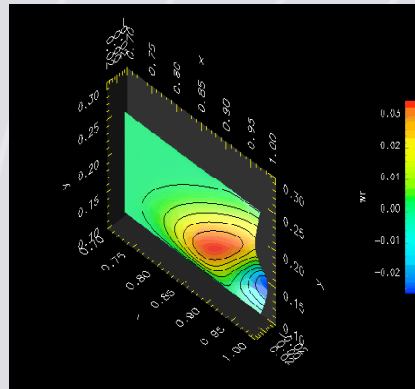
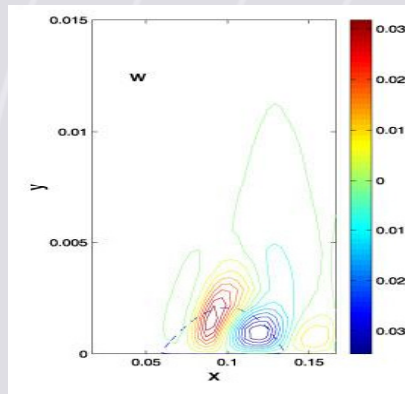




A UNIFYING PERSPECTIVE

THE GLOBAL MODE OF LSB

- The structure of the amplitude functions of the **minimally damped** global eigenmode of the LPT blade... spanwise $w(x,y)$



...is analogous to that on the flat-plate and the NACA 0012 aerofoil



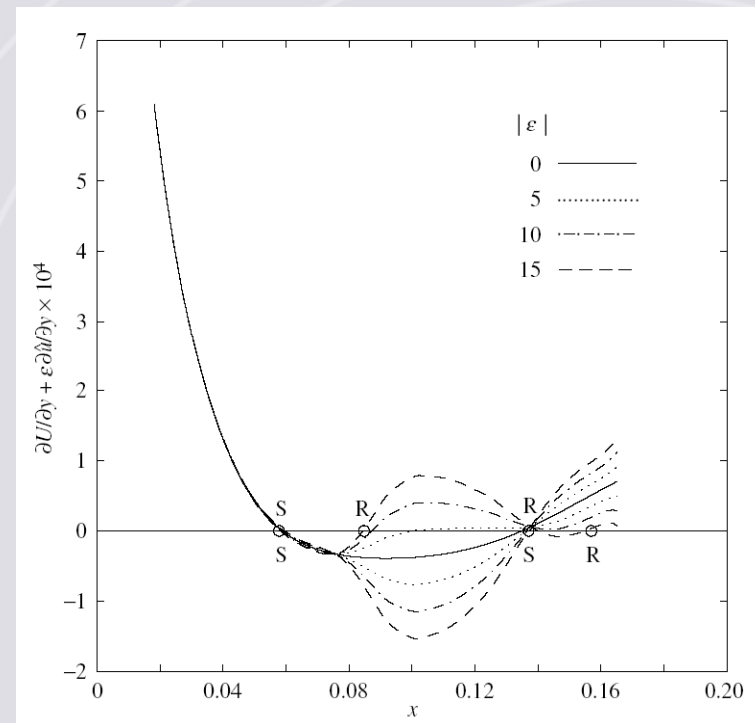
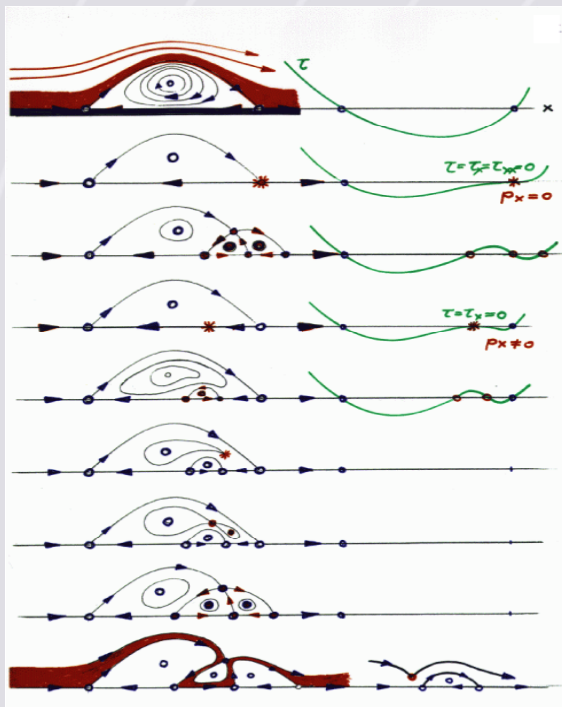
GLOBAL INSTABILITY OF LSB

Configuration	Authors	Methodology
Airfoils	Gaster (1964)	-
APG flat plate BL	Hammond & Redekopp (1998)	Absolute/Convective instability analysis
-//-	Theofilis (1998, 1999) Theofilis, Hein & Dallmann (2000)	BiGlobal instability analysis
Backward- and forward-facing steps	Barkley, Gomes, Henderson (2001) Marquet et al. (2006) Marino & Luchini (2009)	BiGlobal instability analysis, DNS
Low Pressure Turbine blades	Abdessemed, Sherwin & Theofilis (2004; 2006; 2009)	BiGlobal analysis, DNS
Shock / Boundary-Layer Interaction	Boin, Robinet (2004; 2007)	BiGlobal instability analysis, DNS
NACA Airfoils at AoA	Theofilis, Barkley & Sherwin (2002) Crouch et al. (2007; 2009)	BiGlobal instability analysis, DNS
Rounded open cavity, S-shaped duct	Hoepffner et al. (2007), Akervik et al. (2007), Marquet et al. (2008)	BiGlobal instability analysis, DNS
Bump-induced separation	Ehrenstein et al. (2007)	BiGlobal instability analysis, DNS
Low Pressure Turbine Cascade	Breiar & Hodson (2004)	Experiment
Iced Airfoil	Jacobs & Bragg (2006)	Experiment



GLOBAL INSTABILITY & FLOW TOPOLOGY – 1998

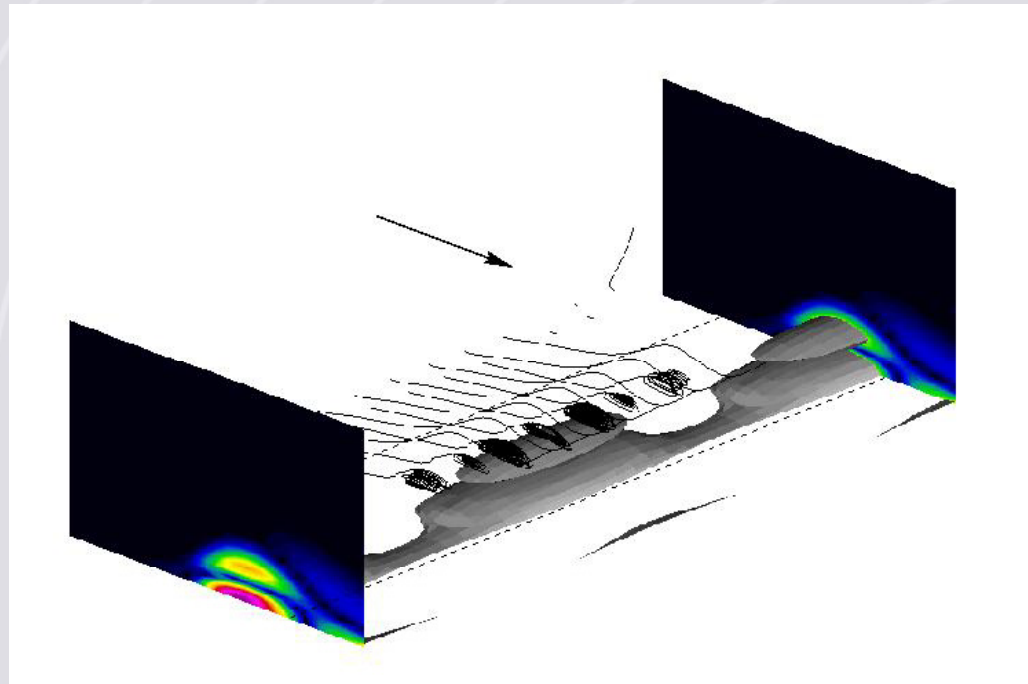
- **Dallmann's conjecture on the topological flowfield changes due to the global mode**





GLOBAL INSTABILITY & FLOW TOPOLOGY – 1999

- Amplification of the global mode leads to three-dimensionalization of the primary reattachment line in 3d...



...while it leaves the primary separation line unaffected



The present contributions



OUTLINE

Incompressible Flow

- Some numerics on the direct/adjoint EVP
- U-separation on a flat-plate
- Stall cells on a NACA0015 airfoil
- Receptivity and Sensitivity of LSB on a flat plate

Compressible Flow

- The Howarth/Briley bubble in subsonic flow
- Shock/Boundary-Layer Interaction (SBLI) on a semi-infinite plate at Mach 2
- SBLI on a 45° wedge

Focus on the (stationary, self-excited) global mode alone



Numerical considerations



MASSIVELY PARALLEL SOLUTION OF THE EVP

- **Ten years later...**
 - **Incoming TS waves at the inflow boundary**
(besides the homogeneous Dirichlet BCs used in THD)
 - **400x100 points per spatial direction used to resolve the amplitude function of the eigenmodes**
(as opposed to 60x40 in THD)
 - **25k CPU hrs (= 25 hrs x 1000 procs) per wavenumber**
(as opposed to 24 CPU hrs serial computing time on a single processor in THD)
- ...permit solving substantially larger **(but not all)** problems,
- **on Mare Nostrum at BSC and (the **Petaflop**) Blue-Gene/P at FZJ**
(but Jürgen Seidel finally got access to DoD HPC machines)

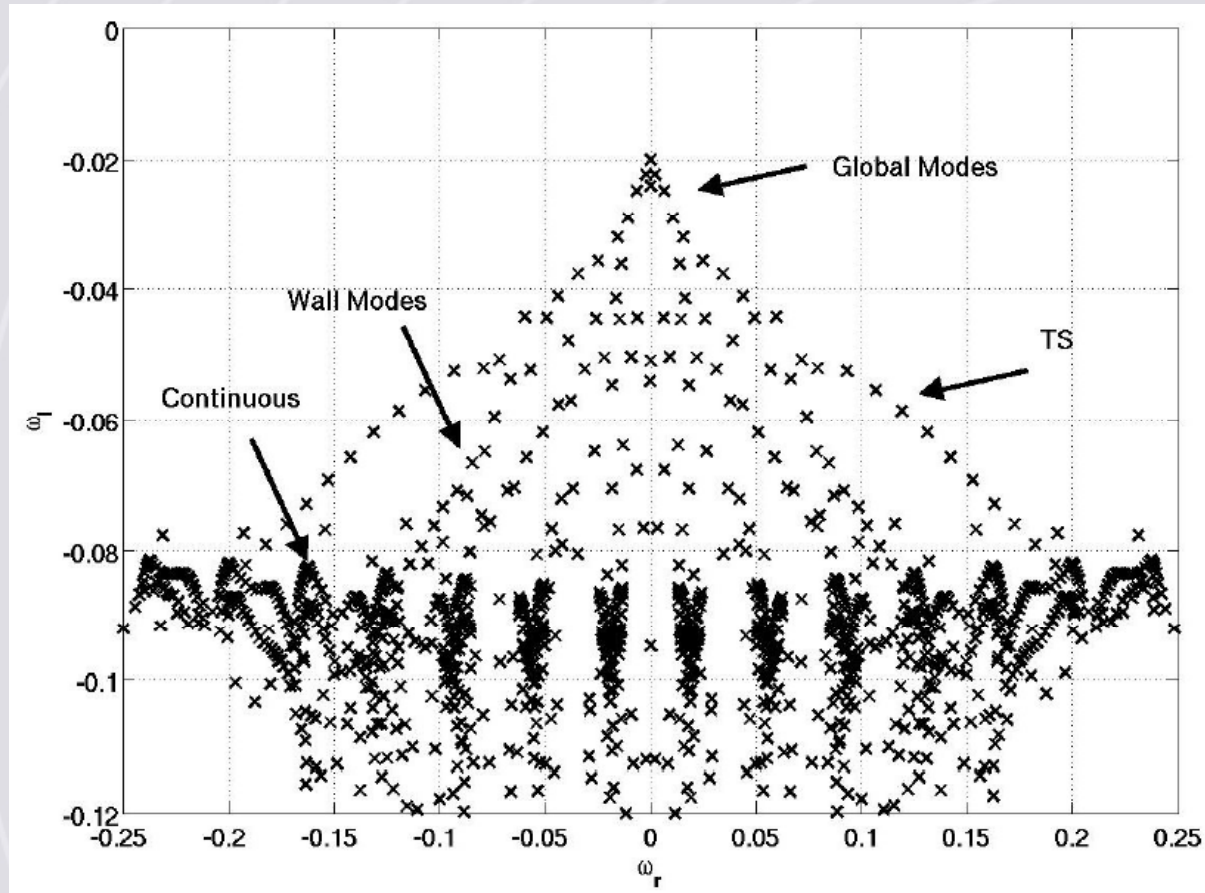


Classification of global modes of LSB flow



GLOBAL MODES IN LSB FLOW ON A FLAT PLATE

Case: $Re_{\delta^*}=500$ at inflow, $Re_{\delta^*}=700$ at outflow, **Separation Bubble**
Boundary conditions: **Dirichlet** at inflow & Extrapolation at outflow

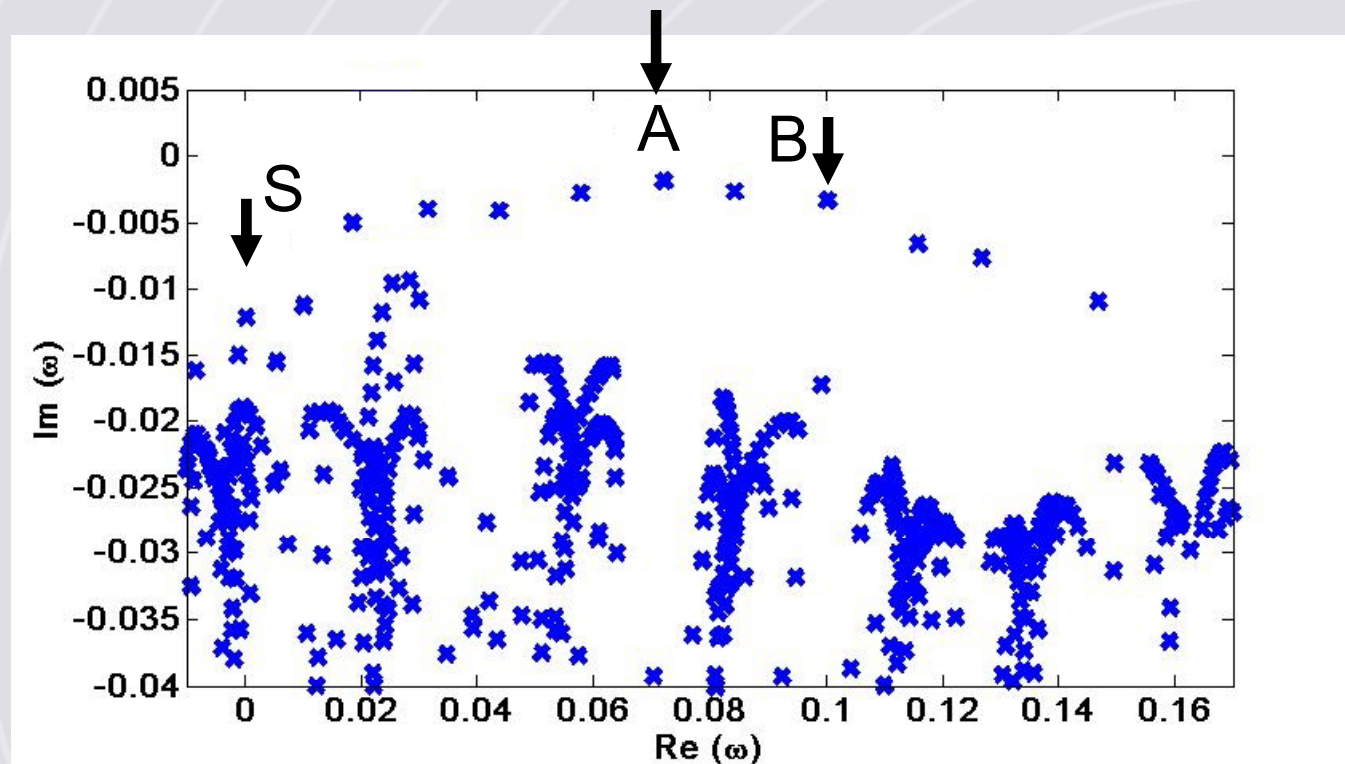


$$\beta = 1$$



TYPICAL FLAT-PLATE GLOBAL EIGENSPECTRUM

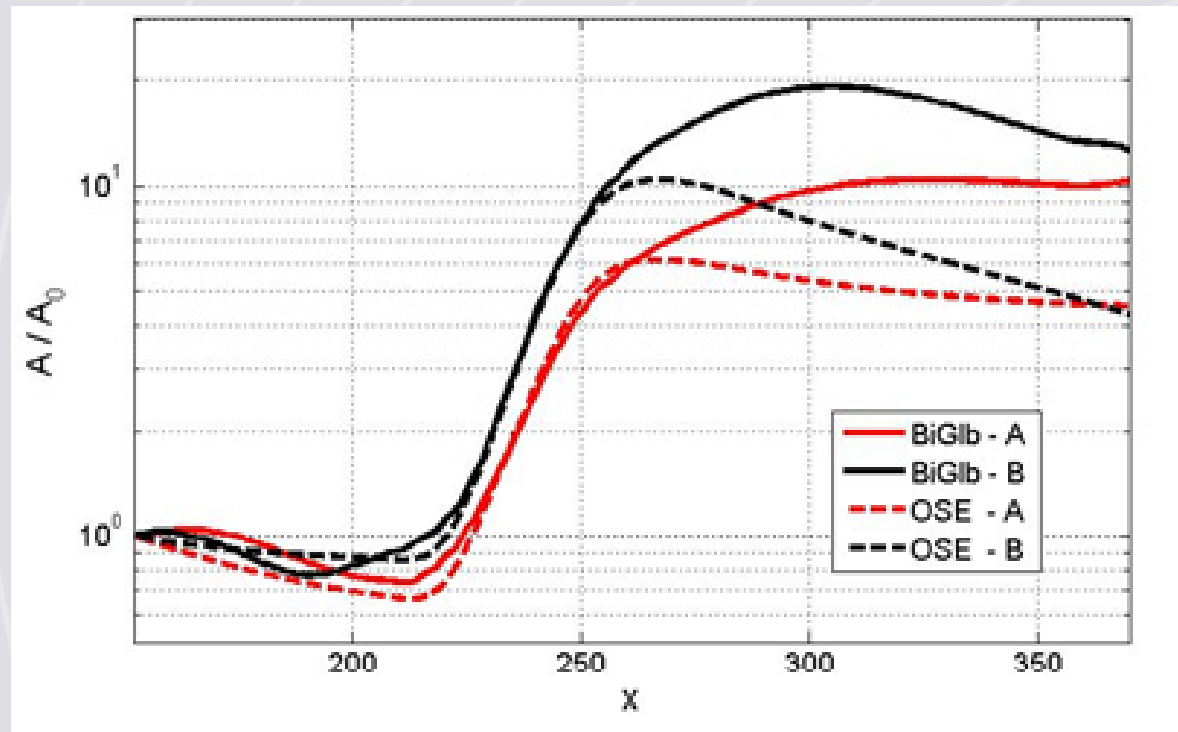
- Composed of discrete and continuous branches
- Focus discussion on two traveling (~~and the leading stationary~~) global eigenmodes





Comparison of traveling modes with OSE

- Extract “spatial amplification” from successive peaks of the (2d) global eigenfunction;
- Run a spatial OSE at successive downstream locations;
- Compare





Extracting physics out of eigenspectra:

- **U-separation** on a flat plate



U-SEPARATION

Fluid Mechanics Group -- M&ME - Windows Internet Explorer

http://www.mame.mu.oz.au/fluids/

Convert Select

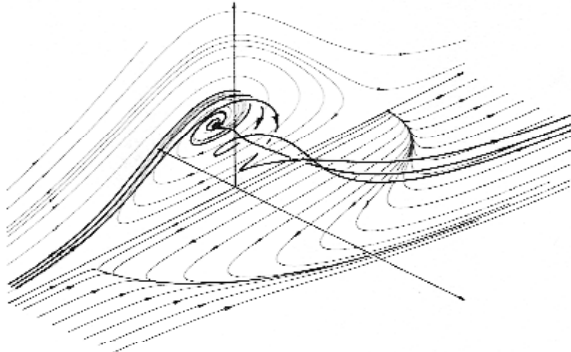
Fluid Mechanics Group -- M&ME

Herramientas

Fluid Mechanics Group

Walter Bassett Aerodynamics Laboratory

Department of Mechanical Engineering, University of Melbourne, Australia



The above diagram represents a local Taylor series expansion solution of the Navier-Stokes equation for a simple U-separation.

(From A.E. Perry & M.S. Chong, Annual Review of Fluid Mechanics, 1987, Vol. 19, pp.125-55).

[Academic Staff](#)

[Research Staff](#)



“U-SHAPED SEPARATION” – 1984

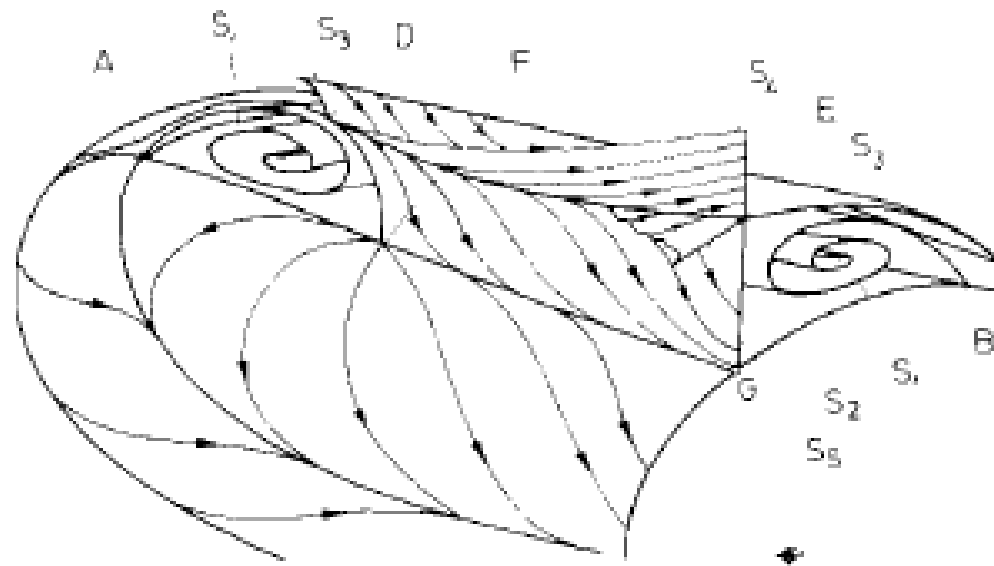
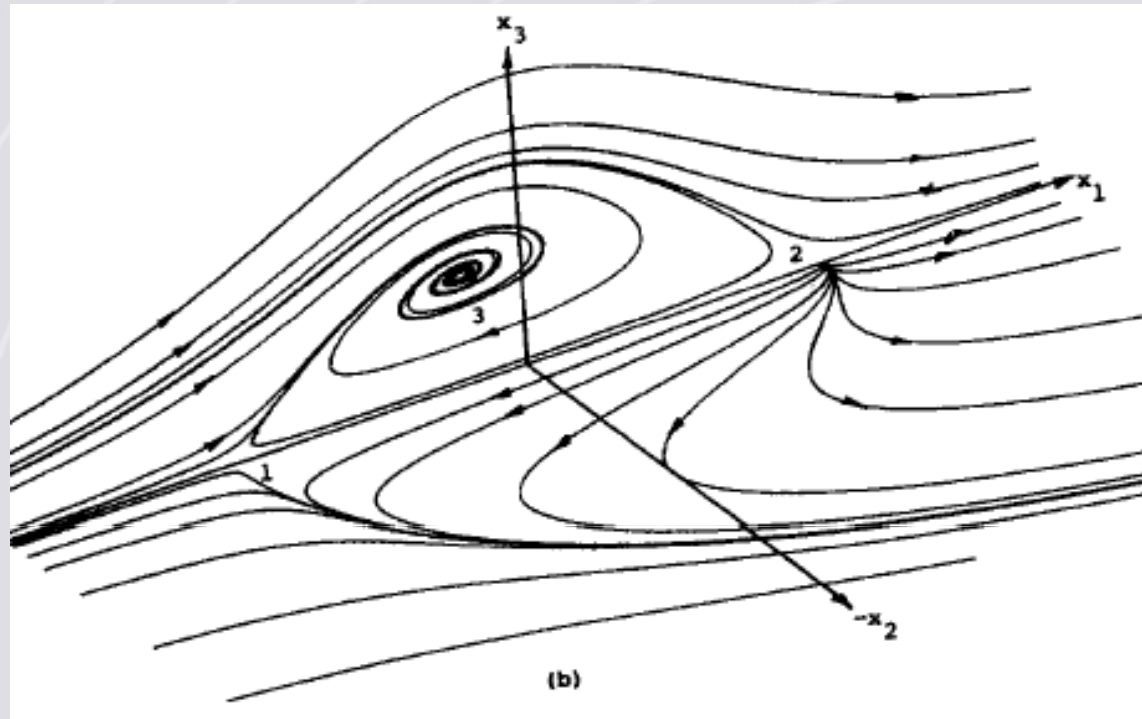


FIG. 17: Perspective view of the free stream surface sheets and wall streamlines of simple U-shaped separation



U-SEPARATION

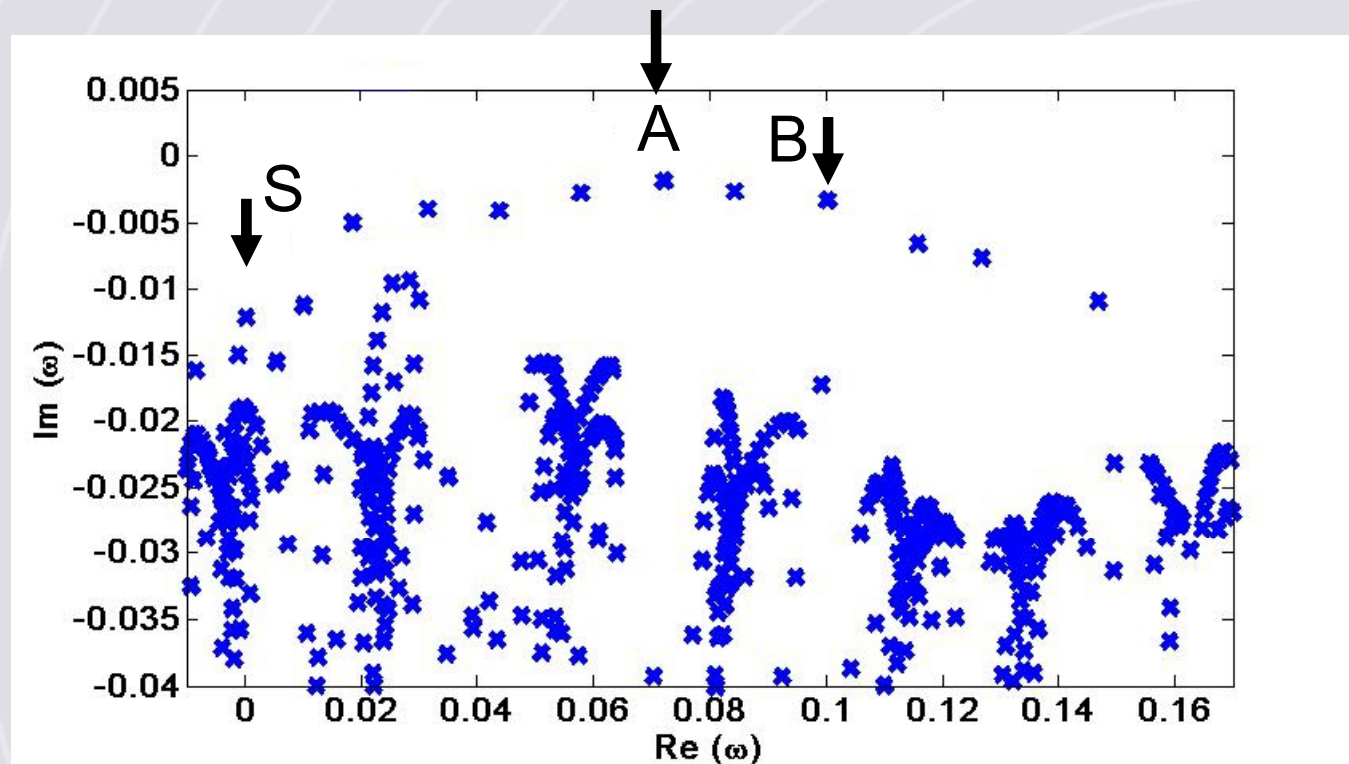


For example, Fig. 6 shows a three-dimensional separation pattern that has been classified as a U separation (Perry and Hornung¹⁷). The flow field has been obtained by solving the Navier-Stokes equations locally (see Perry and Chong¹⁸) using a third-order Taylor series expansion, and assuming that the flow pattern is symmetrical (i.e., \dot{x}_1 and \dot{x}_3 are as-



TYPICAL FLAT-PLATE GLOBAL EIGENSPECTRUM

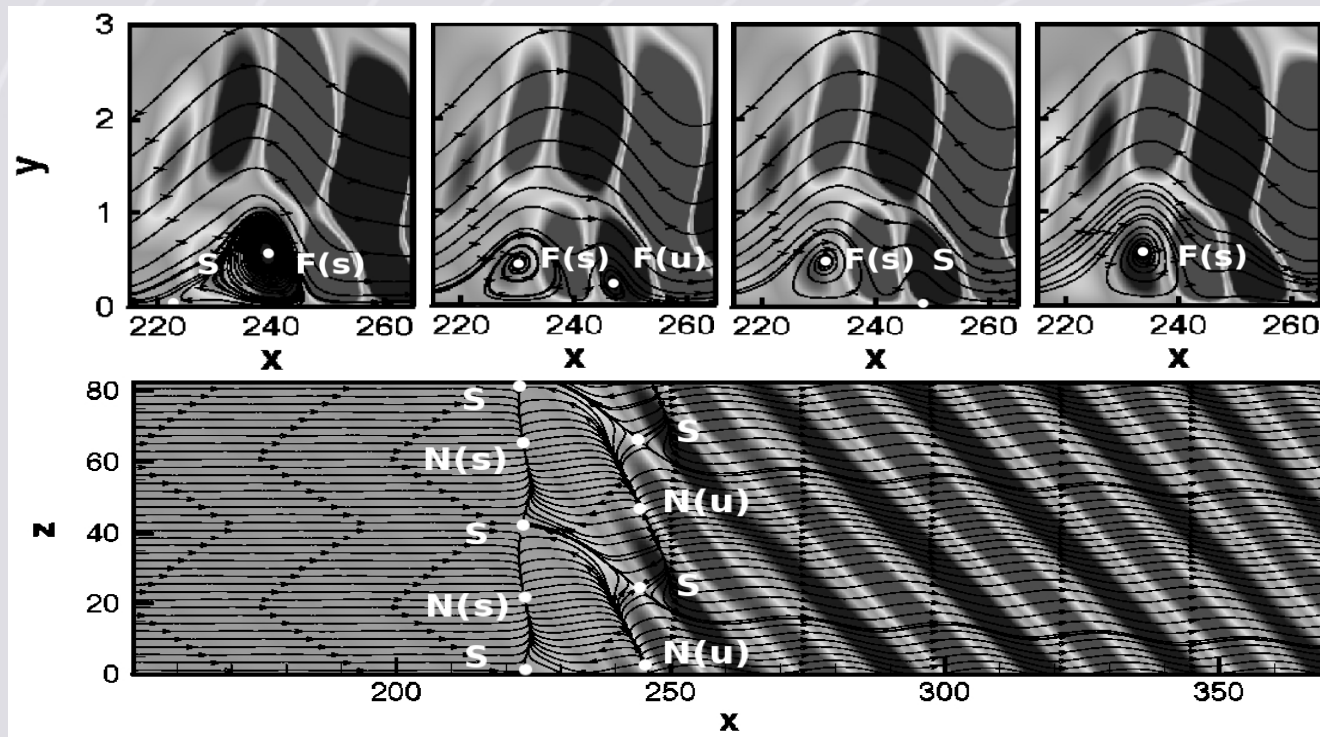
- Composed of discrete and continuous branches
- Focus on ~~(two traveling and)~~ the leading stationary global eigenmode





Critical Points of $(BF + \varepsilon A)$

- Reconstruct a composite flowfield, using the steady basic state and the leading global eigenmode
- Identify critical points and their nature



S: Saddle N: Node F: Focus C: Center
 (s): stable (u): unstable

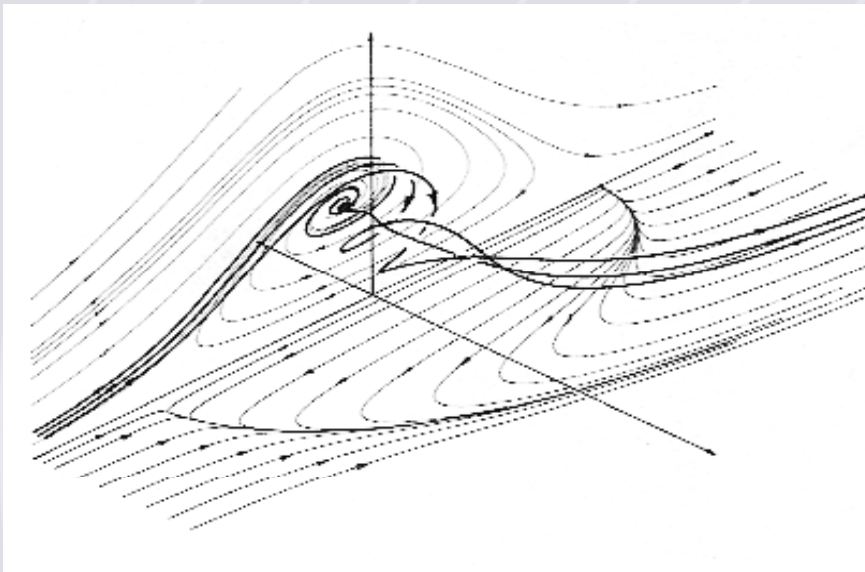


Critical Points of ($BF + \varepsilon S$)

- **Critical point analysis of composite flow**

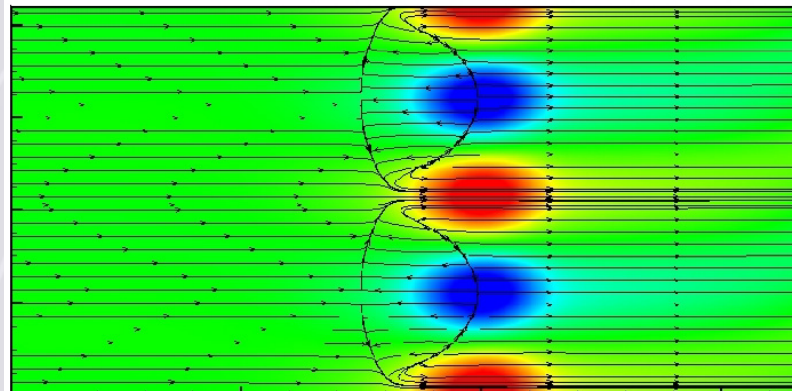
Eigenvalue spectrum

$BF + \varepsilon$ (Global Mode)

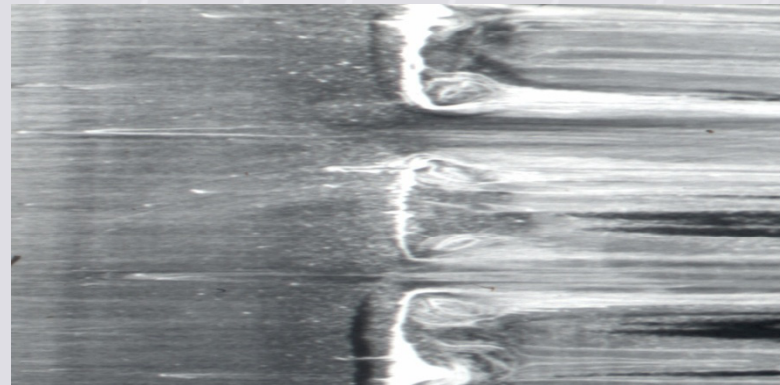




U – SEPARATION



Present computations



Bippes (198?)

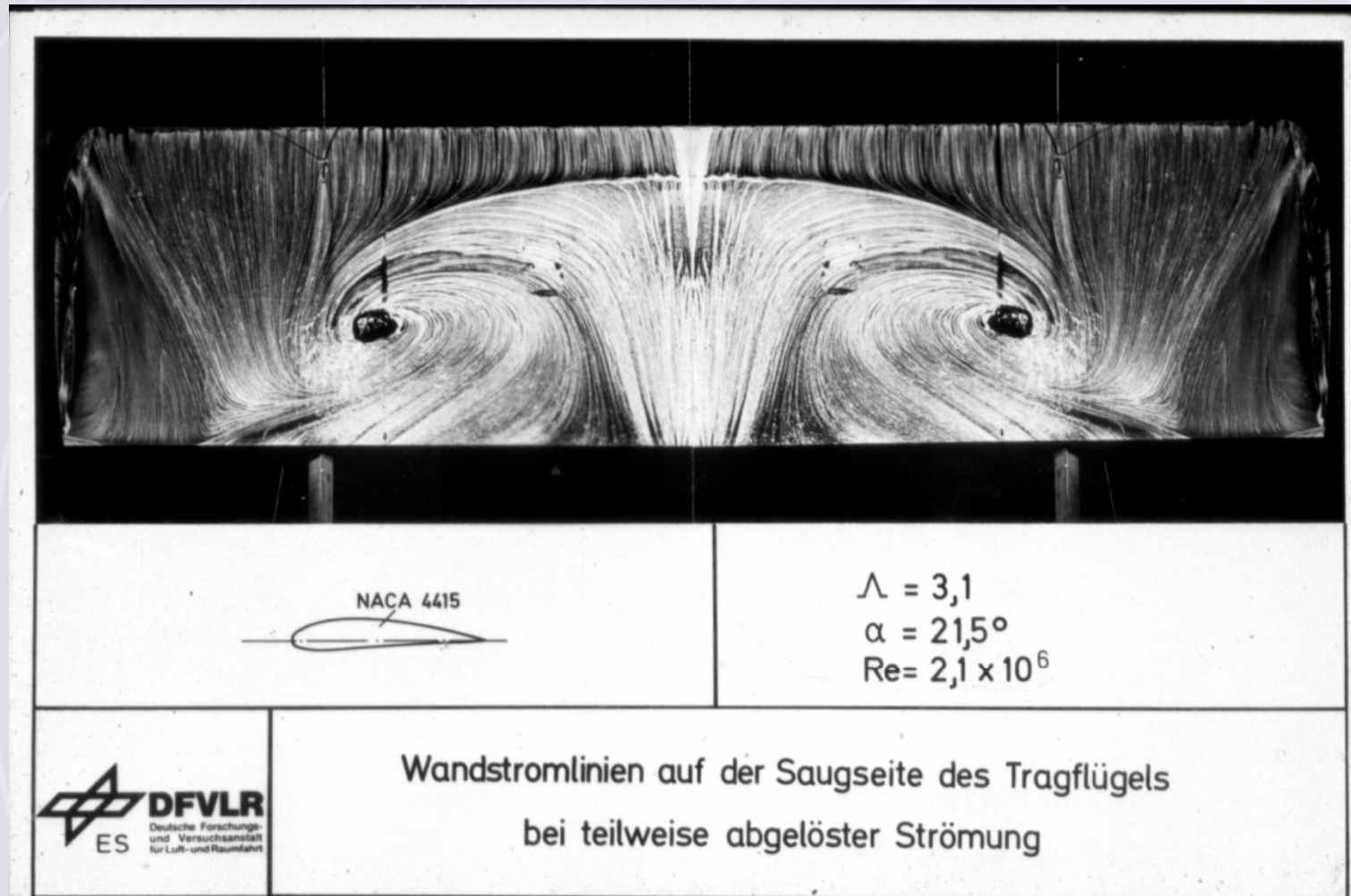


Extracting physics out of eigenspectra:

- **Stall Cells** on an Airfoil



STALL CELLS ON AIRFOILS

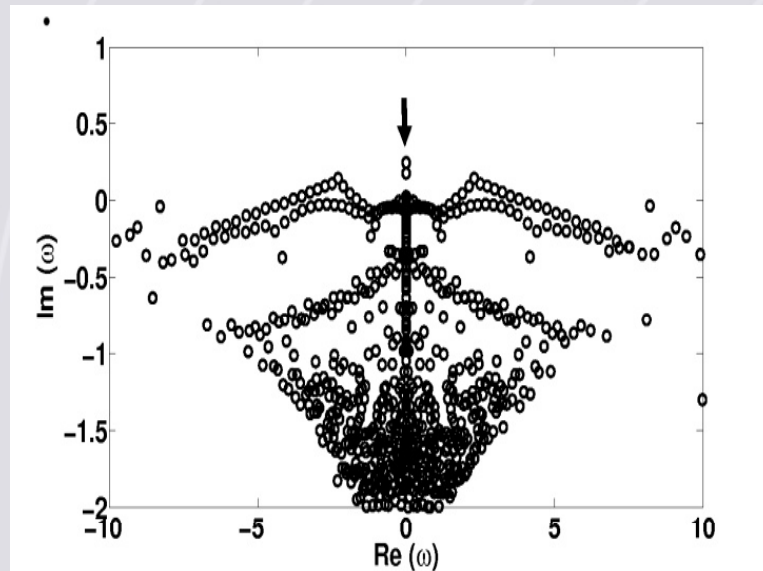




TYPICAL RESULTS ON A STALLED AIRFOIL

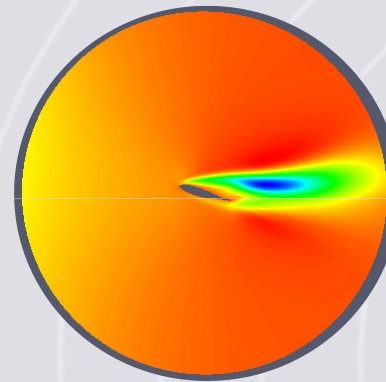
- **Critical point analysis of composite flow**

Eigenvalue spectrum

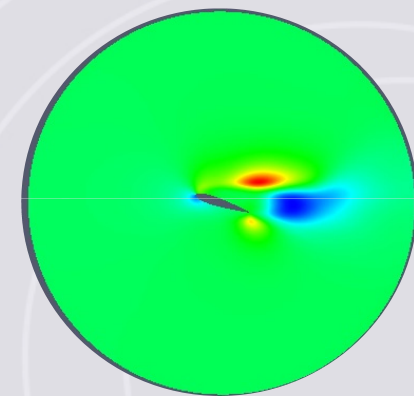


Leading stationary eigenmode

u-perturbation



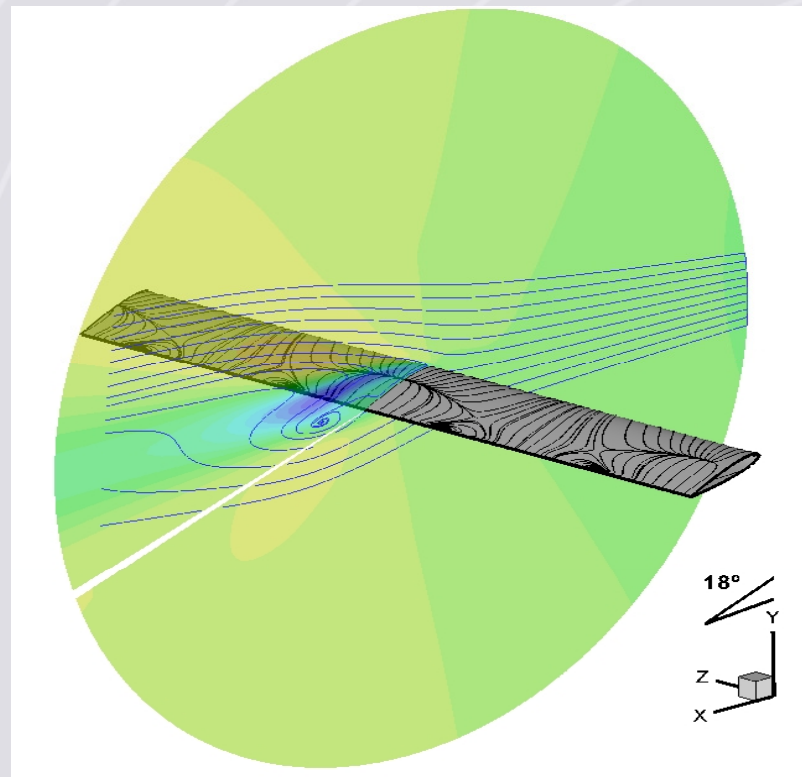
pressure perturbation





Critical Points of ($BF + \varepsilon$ GlobalMode)

- **Stall-cells appear on the airfoil, as result of linear modal amplification of the leading stationary global mode**





Flow Control of LSB

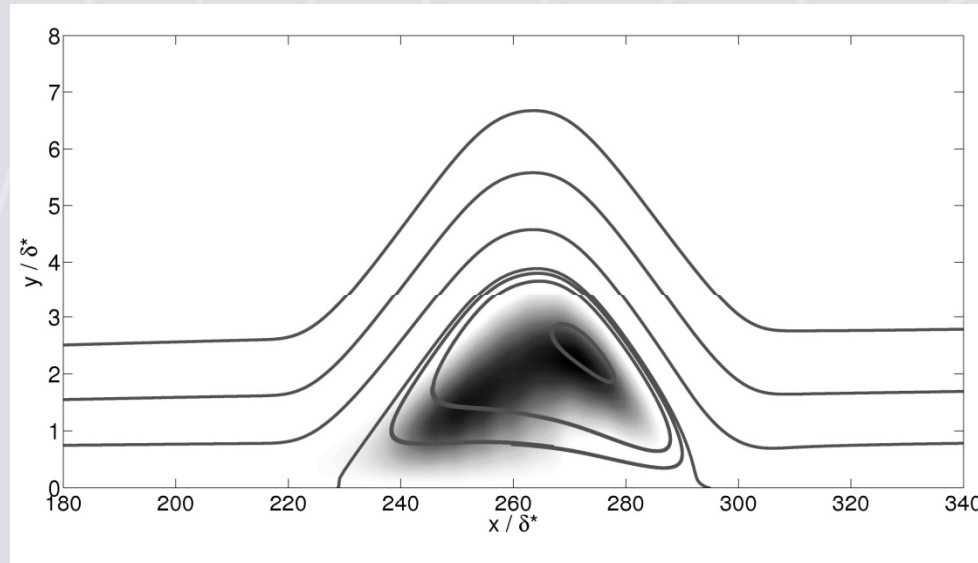
NASA/CP—2010-216112

235



SENSITIVITY OF LSB

- The kernel of the direct/adjoint coupling (Luchini 2003) permits identifying the region of **maximal feedback region**...

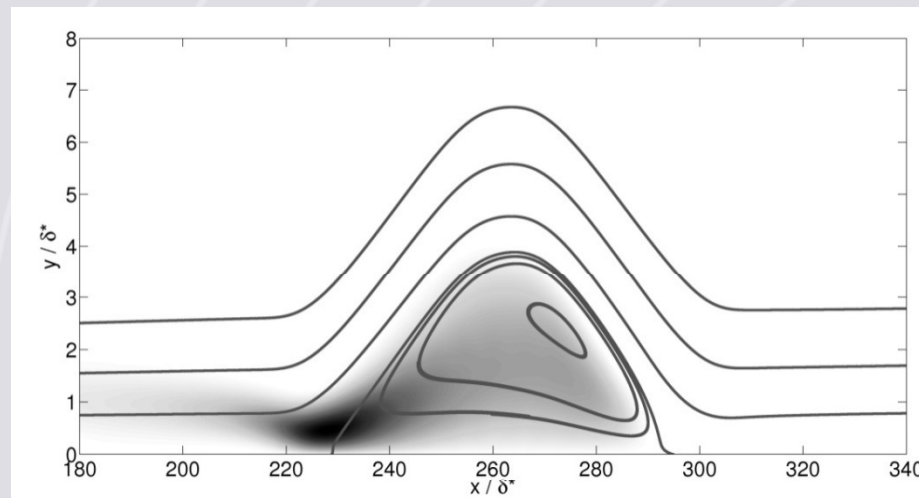


- ... it coincides with the **primary recirculation center**
- (a result not unexpected, really)



RECEPTIVITY OF LSB ON A FLAT-PLATE

- Solution of the adjoint eigenvalue problem permits identifying the **maximally receptive region** (dominant streamwise velocity perturbation)

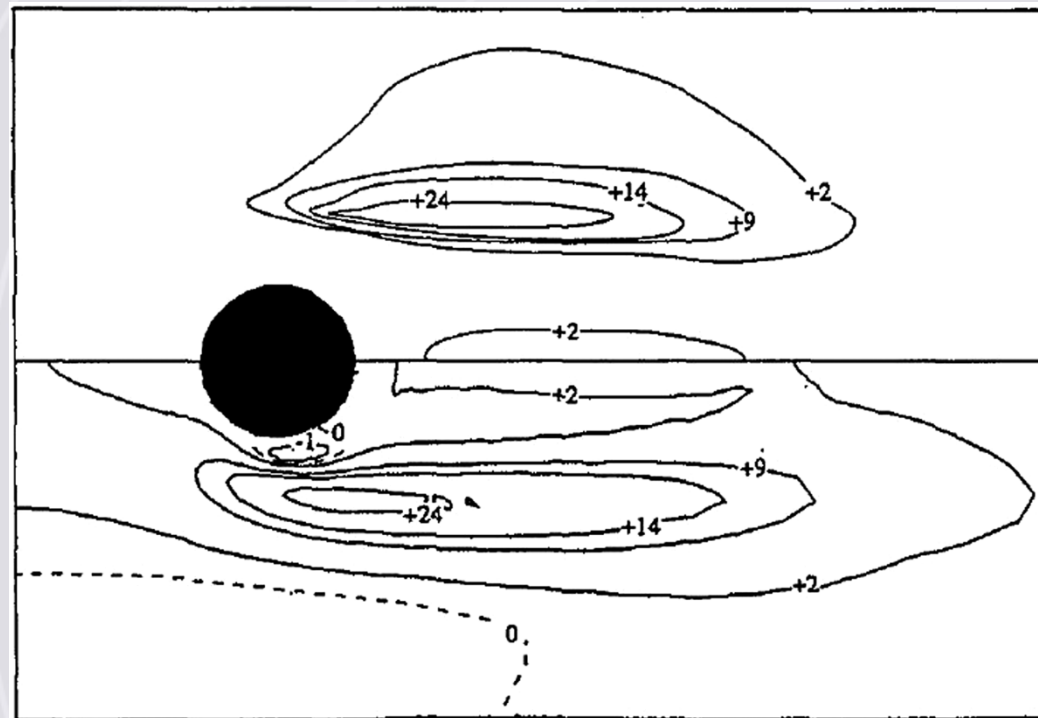


- ... it coincides with **the primary separation line**
- NB. Analysis is meaningful due to homogeneous Dirichlet BCs imposed upstream (direct) / downstream (adjoint) EVP



WHAT CAN THIS KNOWLEDGE DO FOR US?

- Predict the actuator placement without prior knowledge (or ad-hoc assumptions)



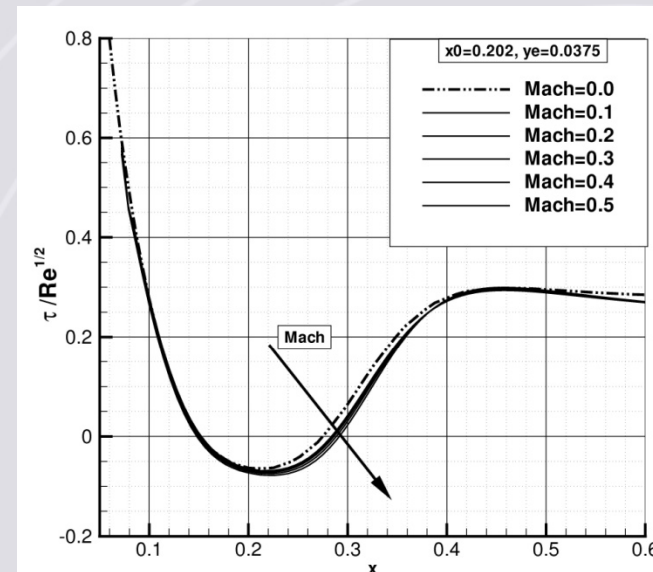
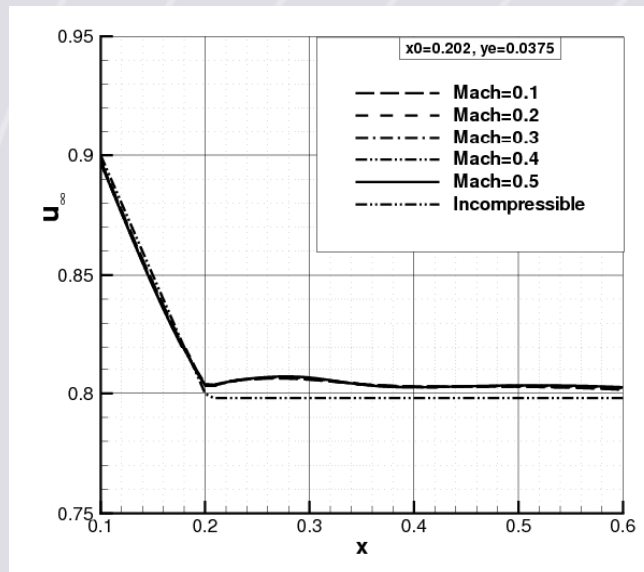


Compressibility effects – subsonic flow



MACH # EFFECT ON HOWARTH/BRILEY LSB

- Linear pressure increase (compressible) v linear deceleration (incompressible) in the free-stream



- No major differences in integral quantities have been found, ie.
- **Quantitative** but **no qualitative differences** of instability results
- Work in progress, in collaboration with Stanford U.

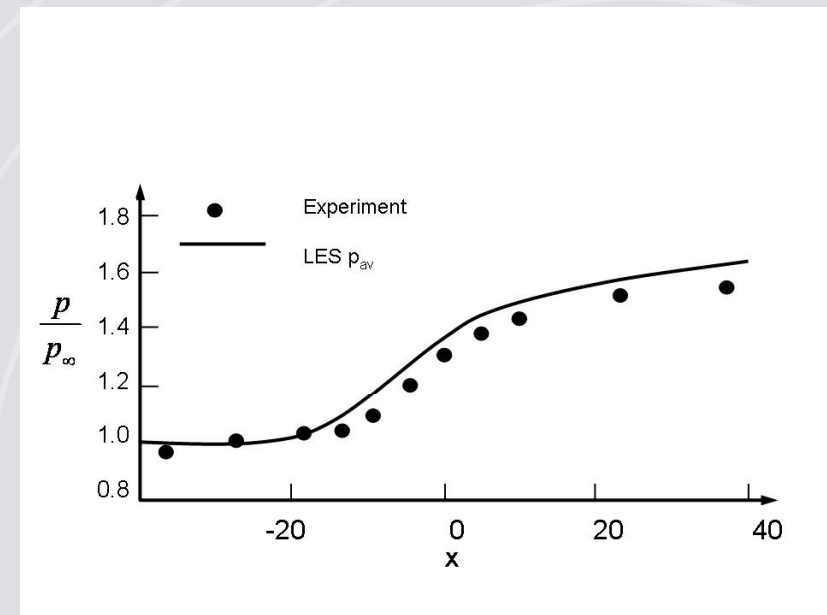
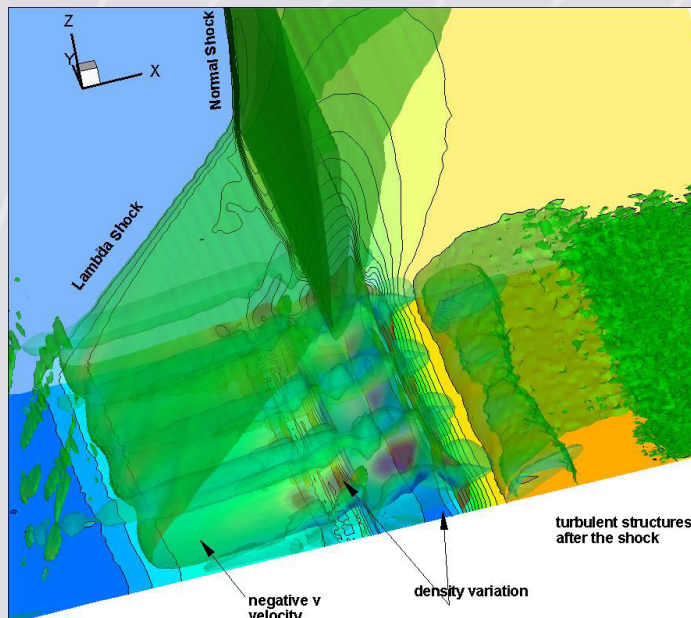


Compressibility effects – supersonic flow



SHOCK / BOUNDARY-LAYER INTERACTION

- Typical LES result at $Re_\delta = 10k$

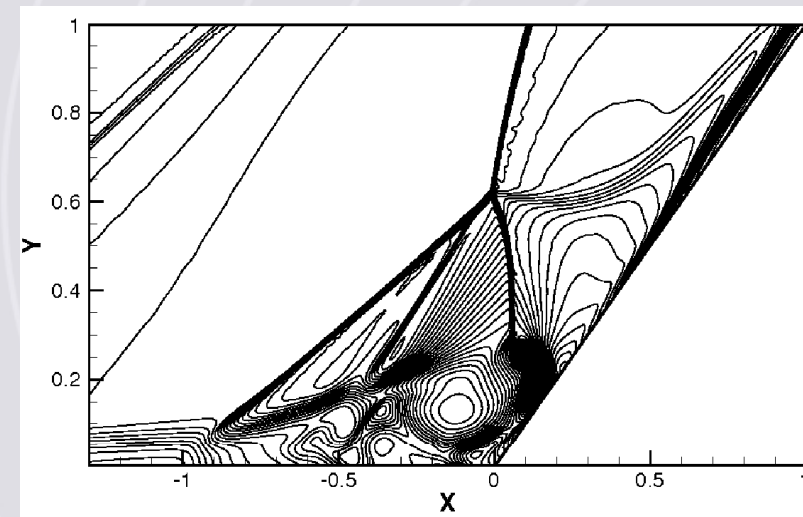
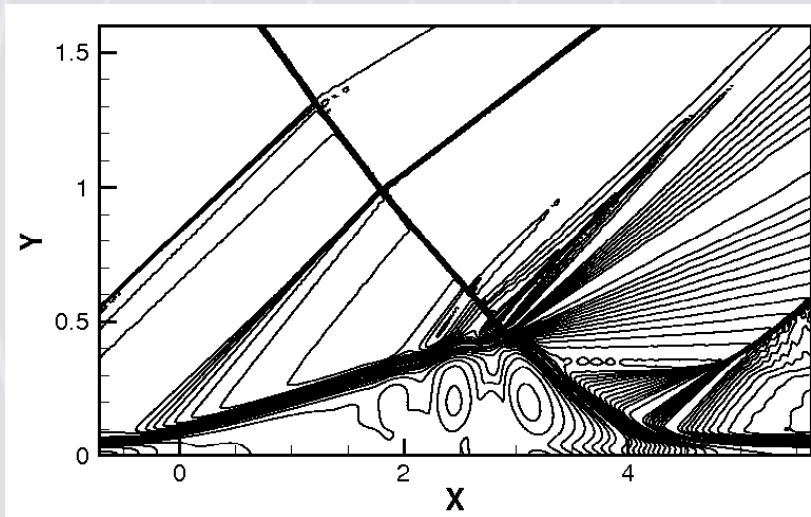


- Origin of **unsteadiness?**
- Origin of **spanwise periodic structures ?**



SBLI & 45° COMPRESSION CORNER – BF_s

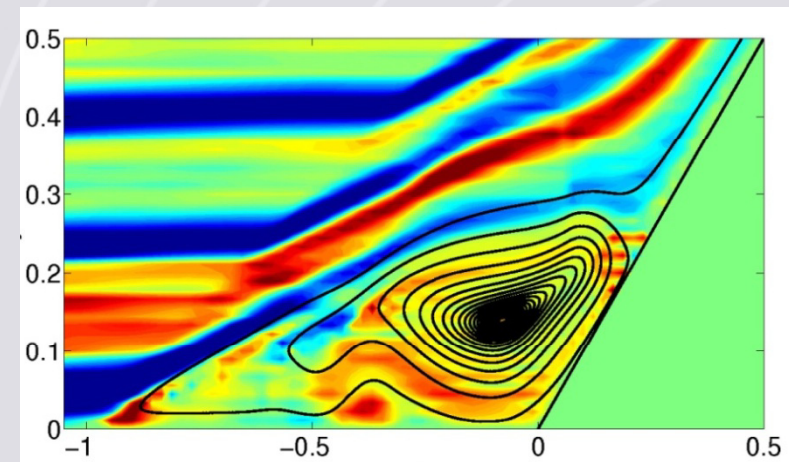
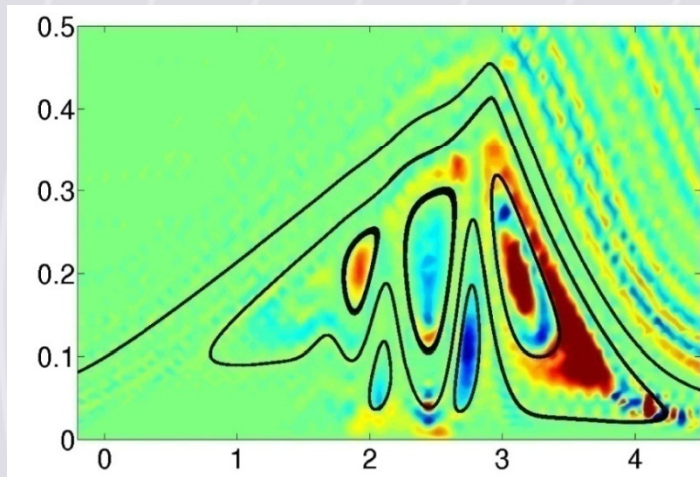
- Basic states obtained by high-order accurate, low-diffusion WENO schemes (Ekaterinaris)
- Flat plate leading edge included at upstream end of both domains
- Finite-angle wedge in compression corner (no triple-deck)
- Both flows at $5000 < Re_l < 20000$, $Ma = 2$ and 2.5
- Unsteadiness identified by DNS at $Re_l \approx 25k$





GLOBAL “MODES”

- Compressible BiGlobal EVP solved at $5000 < Re_L < 20000$ by
 - Spectral collocation (SBLI on flat plate)
 - Immersed boundary (45° compression corner)
- Entire BF domain considered – shocks not treated (≠ Crouch)
- Qualitatively reasonable results,...



- ...but spectra are **not converged** (despite very large resolutions)
- Work in progress, in collaboration with Patras U.



SUMMARY (I / II)

- **In the last 3 years, global linear instability of LSB has been revisited, using state-of-the-art hardware and algorithms**
- **Eigenspectra of LSB flows have been understood and classified in branches of known and newly-discovered eigenmodes**
- **Major achievements:**
 - **World-largest numerical solutions of global eigenvalue problems are routinely performed**
 - **Key aerodynamic phenomena have been explained via critical point theory, applied to our global mode results**
- **Theoretical foundation for control of LSB flows has been laid**



SUMMARY (II / II)

- **Global mode of LSB at the origin of observable phenomena**
 - U-separation on semi-infinite plate
 - Stall cells on (stalled) airfoil
- **Receptivity/Sensitivity/AFC feasible (practical?) via**
 - Adjoint EVP solution
 - Direct/adjoint coupling (the Crete connection)
- **Minor effect of compressibility on global instability in the subsonic compressible regime**
- **Global instability analysis of LSB in realistic supersonic flows apparently quite some way **down the horizon****

(Saric joke # 431: “**an imaginary, ever-receding line**”)



FUTURE CHALLENGES AND WORK DIRECTIONS

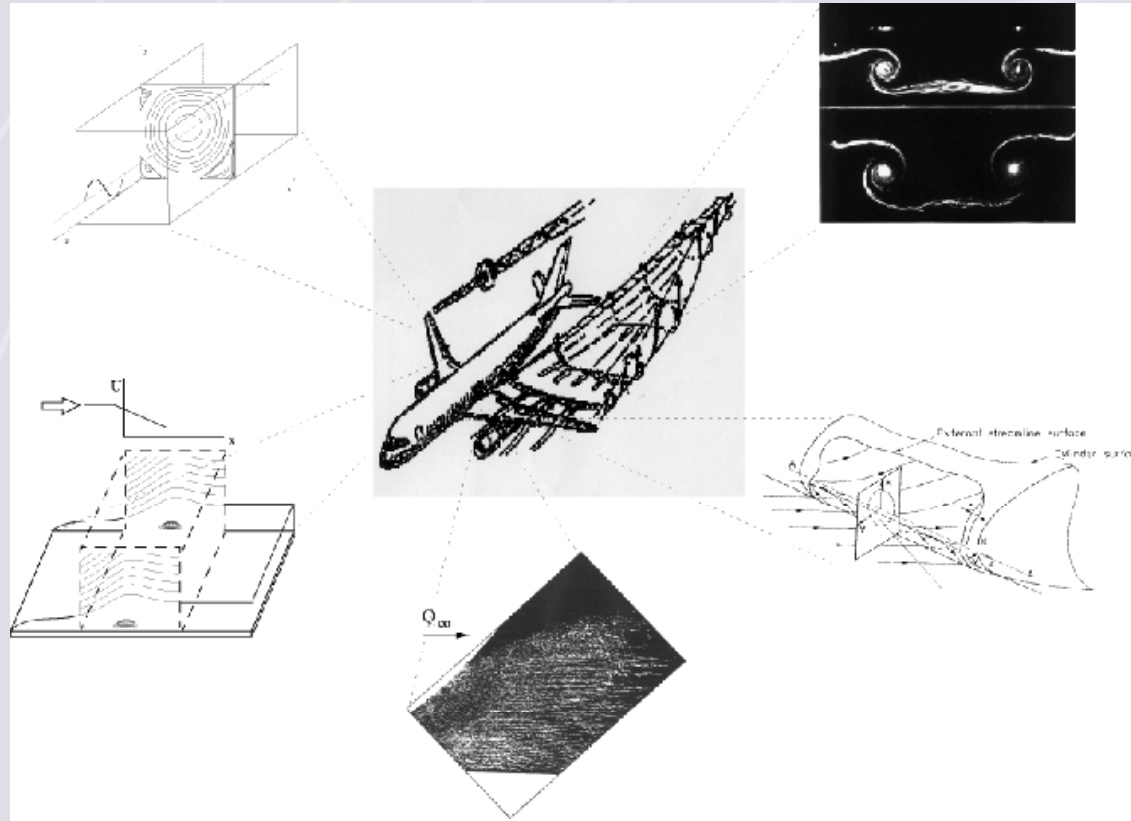
- From a **physical (and theoretical)** point of view
 - Continue with the analysis of EVP results
 - Instability analysis of turbulent flows (obtain EVP spectra of 2.5D flows)
 - Embed instability analysis into (AFC) flow control concepts (for 2.5D flows)
 - Extend global instability tools in 3D flows
- From a **numerical** point of view
 - Devise new algorithms for the efficient parallel solution of (massive) eigenvalue problems



Thank You



GLOBAL FLOW INSTABILITY AND CONTROL IV



Crete, Greece, Sept 28 – Oct 2, 2009



ADDITIONAL MATERIAL



BASIC LSB FLOW ON A FLAT PLATE

Boundary Layer transformation:

$$\xi = \frac{x}{L}$$

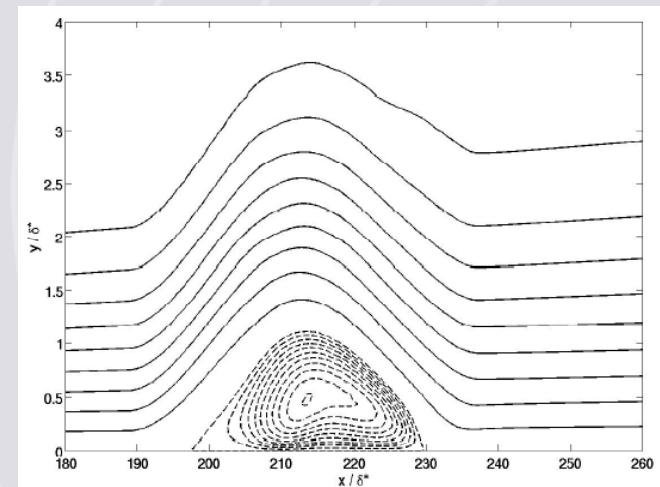
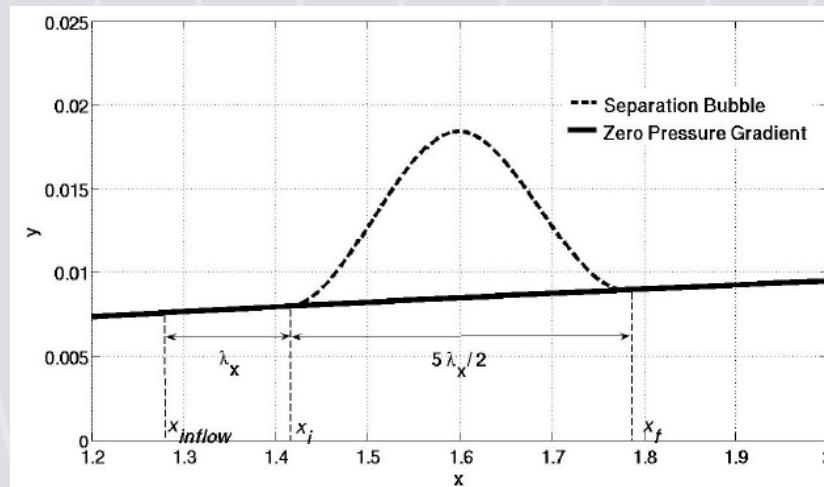
$$\eta = y \sqrt{\frac{U_e}{\nu x}}$$



$$\Psi = \sqrt{U_e \nu x} f(\xi, \eta)$$

Separated states recovery:

- Reyhner and Flügge-Lotz approximation
- Displacement thickness imposed





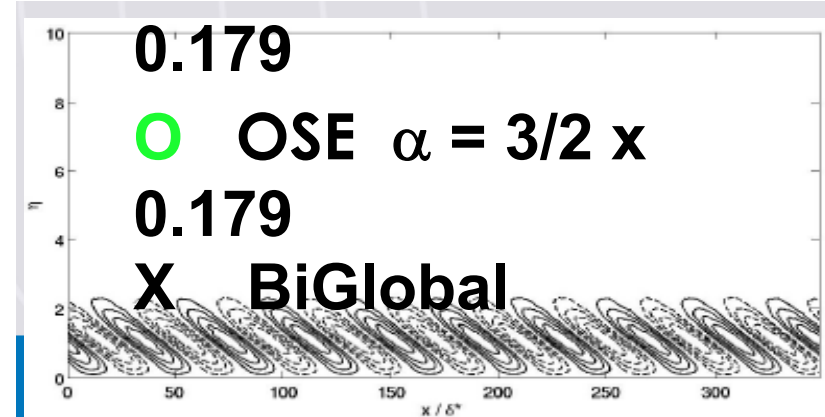
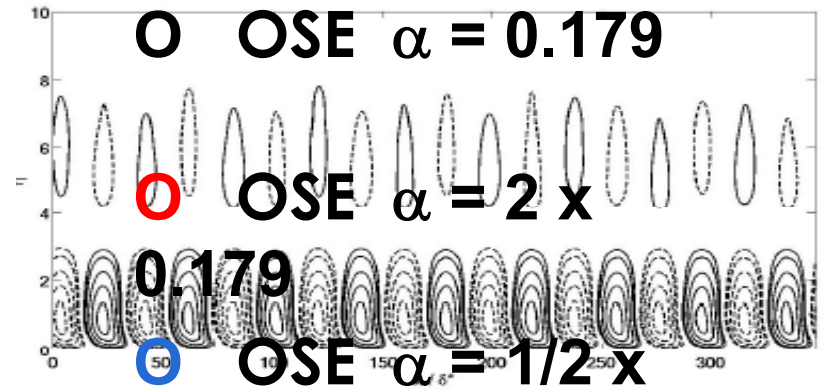
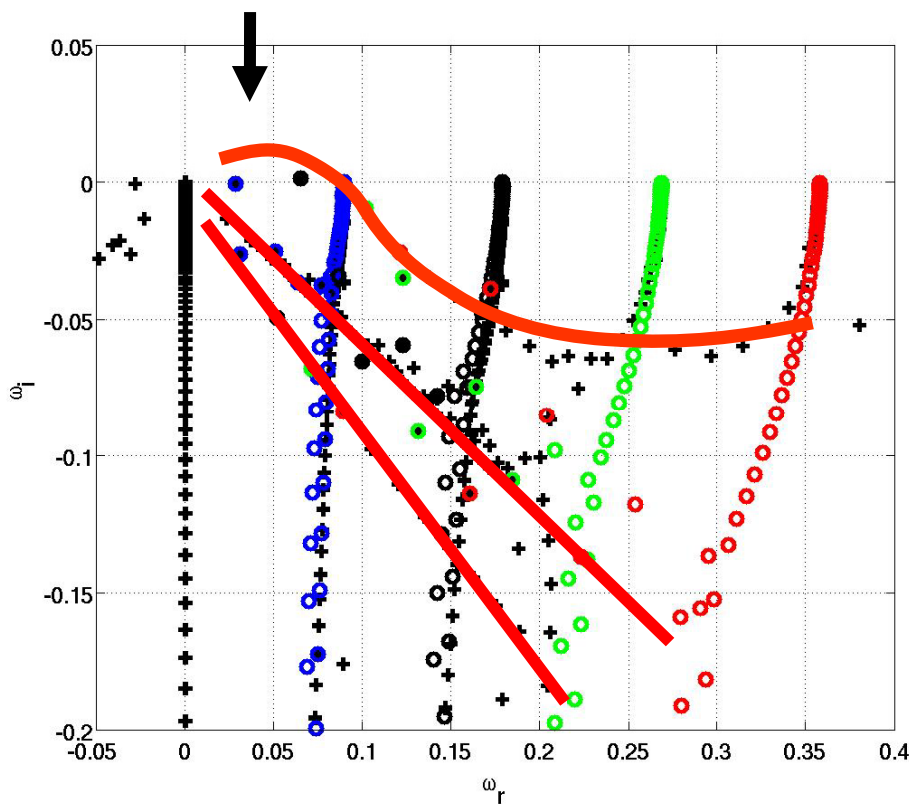
COMPARISON WITH TEMPORAL OSE

Basic Flow: Artificial parallel Blasius

Mack's Case: $Re = 580, \alpha = 0.179$ (Mack JFM 1976)

Streamwise extension: $L = 10 \times 2\pi / \alpha$

Periodic boundary conditions



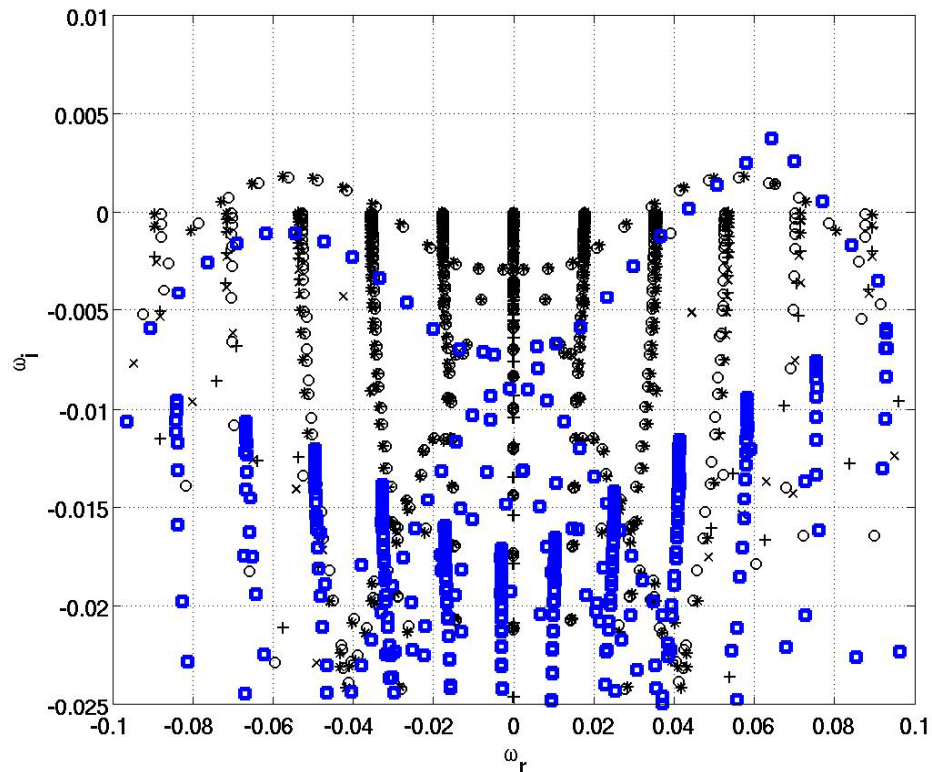


FURTHER COMPARISONS WITH TEMPORAL OSE

Basic Flow: Artificial parallel Blasius

Mack's Case: $Re = 580$, $\alpha = 0.179$ (Mack JFM 1976)

Streamwise extension: $L = 10 \times 2\pi / \alpha$



Boundary conditions:

- x** Periodicity - Fourier
- +** Periodicity - Chebyshev
- o** Robin inflow & outflow
- Robin inflow & Extrapolation outflow



COMPARISONS WITH SPATIAL OSE

Case: $Re_{\delta^*}=500$ at inflow, $Re_{\delta^*}=700$ at outflow

Analysis 1:

- **Basic Flow:** Artificial parallel Blasius
- **Boundary conditions:** Robin* at inflow & outflow

Analysis 2:

- **Basic Flow:** Artificial parallel Blasius
- **Boundary conditions:** Robin* at inflow & extrapolation at outflow

Analysis 3:

- **Basic Flow:** Real Blasius boundary layer
- **Boundary conditions:** Robin* at inflow & extrapolation at outflow

* **Robin boundary condition of Ehrenstein & Gallaire JFM 2005:**

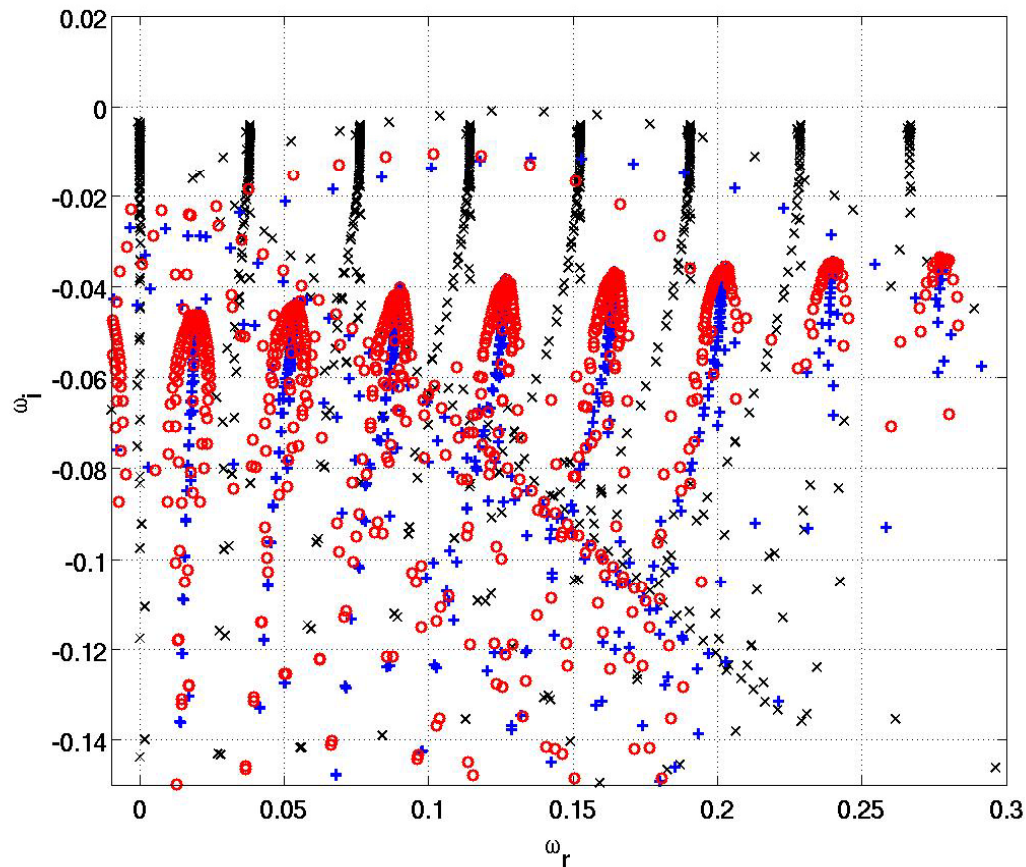
$$\frac{\partial \hat{\mathbf{q}}}{\partial x} = i \left(\alpha_{r,0} + \frac{\partial \alpha_r}{\partial \omega_r}(\omega_0) \cdot (\omega - \omega_0) \right) \hat{\mathbf{q}}$$



FURTHER COMPARISONS WITH SPATIAL OSE

Case: $Re_{\delta^*}=500$ at inflow, $Re_{\delta^*}=700$ at outflow

Robin boundary condition evaluated at: $\omega_0 = 0.13$



Analysis:

- 1 **X** Parallel Blasius,
Robin + Robin
- 2 **+** Parallel Blasius,
Robin + Extrapolation
- 3 **O** Real Blasius,
Robin + Extrapolation



PUBLICATIONS

Journals

- [J-4] Rodríguez, D., Theofilis, V. 2009 Massively Parallel Numerical Solution of the Bi-Global Linear Instability Eigenvalue Problem Using Dense Linear Algebra *AIAA Journal*, accepted for publication, DOI: 10.2514/1.42714
- [J-3] Kitsios, V., Rodríguez, D., Theofilis, V., Ooi, A., Soria, J. 2009 BiGlobal stability analysis in curvilinear coordinates of massively separated lifting bodies. *Journal of Computational Physics*, accepted for publication, DOI: 10.1016/j.jcp.2009.06.011
- [J-2] Rodríguez, D., Theofilis, V. 2009 On the birth of stall-cells on airfoils. *Theoretical and Computational Fluid Dynamics* (accepted for publication).
- [J-1] Rodríguez, D., Theofilis, V. 2009 Structural changes induced by global linear instability of laminar separation bubbles. *Journal of Fluid Mechanics* (submitted for publication).

Book Chapters

- [B-2] Theofilis, V. 2009 Role of instability theory in flow control. In *Fundamentals and Applications of Modern Flow Control* (Joslin RD, Miller D, eds.) ISBN 978-1-56347-938-0, AIAA Progress in Astronautics and Aeronautics, vol. 231, pp. 73-114.
- [B-1] de Vicente, J., Rodríguez, D., González, L. Theofilis, V. 2008. High-order numerical methods for BiGlobal flow instability analysis and control. In *Associação Brasileira de Ciências Mecânicas, Volume 6 tomo 2: Turbulência. 6ª Escola de Primavera em Transição e Turbulência*, Univ. São Paulo, Sao Carlos, 22- 26 Sept. 2008, (M. Teixeira Mendonça, M. Faraco de Medeiros, eds.), pp. 1-123.

Conferences

- [C-8] Rodríguez, D., Ekaterinaris, J., Valero, E., Theofilis, V. 2009 On receptivity and modal linear instability of laminar separation bubbles at all speeds. Seventh IUTAM Symposium on Laminar-Turbulent Transition, Stockholm, Sweden, June 23-26, 2009. Springer (to appear).
- [C-7] Theofilis, V. Rodríguez, D. 2009 Global Linear Instability on Laminar Separation Bubbles – revisited: U-separation and the Birth of Stall Cells on Airfoils. CEAS/KATnet II Conference on Key Aerodynamic Technologies, Bremen, Germany, May 12-14, 2009. 12pp. ISBN 978-3-00-027782-5.
- [C-6] Kitsios, V., Rodríguez, D., Theofilis, V., Ooi, A., Soria, J. 2008. BiGlobal instability analysis of turbulent flow over an airfoil at an angle of attack layer. AIAA 38th Fluid Dynamics Conference And Exhibit, Seattle, June 23-26, 2008. AIAA Paper 2008-4384.
- [C-5] Rodríguez, D., Theofilis, V. 2008 On instability and structural sensitivity of incompressible laminar separation bubbles in a flat-plate boundary layer. AIAA 38th Fluid Dynamics Conference And Exhibit, Seattle, June 23-26, 2008 AIAA Paper 2008-4148
- [C-4] Valero, E., Theofilis, V. 2008 Compressibility Effects in Howarth's Separation Bubble on a Flat Plate. AIAA 46th AIAA Aerospace Sciences Meeting and Exhibit, Reno, Nevada, Jan. 7-10, 2008, AIAA Paper 2008-0593.
- [C-3] Rodríguez, D., Theofilis, V. 2008 Massively Parallel Numerical Solution of the BiGlobal Linear Instability Eigenvalue Problem. AIAA 46th AIAA Aerospace Sciences Meeting and Exhibit, Reno, Nevada, Jan. 7-10, 2008. AIAA Paper 2008-0594.
- [C-2] Theofilis, V. 2007 On instability properties of incompressible laminar separation bubbles on a flat plate prior to shedding. AIAA 45th Aerospace Sciences Meeting, Reno, NV, Jan 8-11, 2007. AIAA Paper 2007-0540.
- [C-1] Theofilis, V. 2007 Global instability and control of laminar separation bubbles: Theoretical background, basic ow documentation, algorithmic developments and validation. IUTAM Symposium on Unsteady Separated Flows and their Control. Corfu, Greece, June 18-22, 2007. Springer (to appear). ISBN: 978-1-4020-9897-0.



TECHNICAL EXCHANGES

- **U of Arizona**
 - Theofilis Visiting/Adjunct Professor since 08
 - Rodríguez visited in 08, will return in 09 (one month)
 - Joint publications in preparation with
 - Tumin (on characterization of eigenspectra)
 - Fasel (on global instability of 3d bubble flows)
- **Stanford U**
 - Joint publication in preparation with
 - Marxen (on laminar separation bubbles)
- **U of Patras**
 - Provision of 2d shock-induced laminar separated basic flows
 - Joint publication (IUTAM 2009) with
 - Ekaterinaris (on preliminary global instability analyses)