Nitric Oxide PLIF Measurements in the Hypersonic Materials Environmental Test System (HYMETS)

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A nonintrusive laser-based measurement system has been applied for the first time in the HYMETS (Hypersonic Materials Environmental Test System) 400 kW arc-heated wind tunnel at NASA Langley Research Center. Planar laser-induced fluorescence of naturally occurring nitric oxide (NO) has been used to obtain instantaneous flow visualization images, and to make both radial and axial velocity measurements. Results are presented at selected facility run conditions, including some in simulated Earth atmosphere (75% nitrogen, 20% oxygen, 5% argon) and others in simulated Martian atmosphere (71% carbon dioxide, 24% nitrogen, 5% argon), for bulk enthalpies ranging from 6.5 MJ/kg to 18.4 MJ/kg. Flow visualization images reveal the presence of large scale unsteady flow structures, and indicate nitric oxide fluorescence signal over more than 70% of the core flow for bulk enthalpies below about 11 MJ/kg, but over less than 10% of the core flow for bulk enthalpies above about 16 MJ/kg. Axial velocimetry was performed using molecular tagging velocimetry (MTV). Axial velocities of about 3 km/s were measured along the centerline. Radial velocimetry was performed by scanning the wavelength of the narrowband laser and analyzing the resulting Doppler shift. Radial velocities of ±0.5 km/s were measured.

I. Introduction

Arcjet facilities are a vital tool in the testing and characterization of materials intended for hypersonic vehicles, including those designed for planetary entry. Arcjets are capable of producing flows of a higher enthalpy than traditional wind tunnels, and are thus better suited for evaluating and characterizing candidate materials for thermal protection systems. Like other types of hypersonic facilities, arcjets cannot perfectly simulate all the flow conditions relevant to hypersonic flight. For example, significant dissociation of freestream gases typically occurs. Determining how to interpret arcjet test results and then extrapolate those results to flight conditions can therefore be complicated. To that end, measurements of the flow conditions of an arcjet facility are needed to validate computational tools, to allow for reliable comparisons between simulations and test results, and ultimately to make possible reliable computational predictions of aerodynamic parameters and material response in flight environments that cannot be adequately simulated in ground test facilities. Currently, the flow parameters that can be measured (or calculated from measured quantities) in the Hypersonic Material Environmental Test System (HYMETS) facility at NASA Langley include stagnation pressure; heat flux (semi-catalytic hot-wall, fully-catalytic cold-wall, and/or non-catalytic cold-wall); gas mass flow rates; sonic, stagnation, and bulk specific enthalpy; and arc current, voltage, and power.1 Nonintrusive measurements of additional flow parameters are therefore desired. An arcjet flow presents a challenging environment for making measurements as the flow is typically a high-enthalpy, low pressure, chemically reacting, nonequilibrium environment. Several techniques have been applied by others to arcjet flows. Diode laser absorption has been demonstrated for making simultaneous velocity and temperature measurements of...
an argon arcjet plume.\textsuperscript{2} Oxygen (O)-atom and nitrogen (N)-atom laser-induced fluorescence (LIF) have been used to provide temperature, velocity and species concentration (number density) measurements at a single point or along a line.\textsuperscript{3,4,5} Nitric oxide (NO) planar LIF (PLIF) and O-atom LIF has previously been used in arcjets to measure translational temperature of O and rotational temperature of NO.\textsuperscript{6,7} References 8 and 9 give additional descriptions of techniques that have been used to make nonintrusive measurements in arcjets.

Researchers in charge of operations in HYMETS have set a goal of implementing nonintrusive diagnostics to obtain 1) flow visualization information, including measurements of shock standoff distance and flow uniformity assessments, 2) axial and radial velocity measurements in the freestream and near the test sample, 3) species detection and concentration measurements, including both species produced by the arcjet itself and gaseous species resulting from the ablation of test samples, and 4) measurements of rotational, vibrational, and electronic temperature. This paper presents results of the first application of NO PLIF in HYMETS and progress to varying degrees towards all four of these goals. Using NO PLIF, we have demonstrated that flow visualization, and radial and axial velocimetry can be performed over the full flowfield downstream of the nozzle exit for certain ranges of facility test conditions. The measurements will ultimately provide an improved understanding of the operation of the arc-heated facility and will also provide facility-to-facility and facility-to-flight scalings for materials tests occurring in the facility.

II. Experimental Methods

A. HYMETS Arcjet Facility

Tests were conducted at NASA Langley Research Center in the Hypersonic Materials Environmental Test System (HYMETS) facility, an arcjet wind tunnel with a 400 kW power supply. When compared to other, larger arc-heated wind tunnel facilities, significant advantages of HYMETS include the relatively small workforce required to operate the facility (typically one technician), long run times (up to several hours), short down-time between runs and sample changes (less than one hour), and relatively low operating costs. Also, numerous optical ports offer a variety of views of the flow and test specimens. Figure 1 shows an overhead schematic view of the arc plasma generator, nozzle, and test chamber. Note that the schematic shows the retracted position of two flow probes, with dashed lines indicating the injected position of one of the probes. (The facility has four such probes, described in more detail below. When looking down the flow axis from nozzle toward the diffuser, the probes are located at the 45°, 135°, 225°, and 315° positions with respect to the horizontal.) This schematic depicts the position of the seven access ports, each of which can be fitted with a 51 mm (2 inch) diameter UV-grade fused silica (quartz) window to provide optical access at wavelengths down to about 180 nm in the ultraviolet. Six ports are in the horizontal plane, one is below the centerline injected-probe position, and two are above the horizontal plane. Of the six ports in the horizontal plane, four are angled at approximately 45° to the flow axis and two are angled at 90° to the flow axis, just downstream of the leading edge of an injected probe.

A segmented-constrictor direct-current electric arc-heater serves as an arc plasma generator. The slightly diverging flow issues from a convergent-divergent 8 degree half-angle Mach 5 conical copper nozzle with a 12.7 mm (0.5 inch) diameter throat and a 63.5 mm (2.5 inch) diameter exit. Process gases consist of nitrogen (N\(_2\)), oxygen (O\(_2\)), carbon dioxide (CO\(_2\)), and argon (Ar). Test gasses are injected tangentially into the bore of the arc plasma generator at six discrete locations, where they are heated by a high-voltage electric-arc maintained between the cathode and anode to create a high temperature ionized plasma flow. The electric-arc is spin-stabilized in the arc plasma generator by the vortex motion of the injected test gasses. The test gasses used in the arc plasma generator are supplied by several compressed gas cylinders and can be custom mixed to any desired atmosphere. Adjustable volume percentages of N\(_2\) and Ar are used as shield gasses near the cathode and anode, respectively, to protect the electrodes from rapid oxidation.

The plasma flow from the arc plasma generator is accelerated through the nozzle and exhausted into a 0.6 m (2 ft) diameter by 0.9 m (3 ft) long vacuum test chamber where it stagnates on one of four water-cooled specimen/instrumentation injection stings arranged symmetrically around the inside circumference of the test chamber. The flow is then captured by a collector cone with a 0.2 m (8 inch) diameter inlet plane, a 0.15 m (6 inch) diameter constant cross-section diffuser, and a coiled-copper tubing heat exchanger to decelerate and cool the flow. A two-stage, continuous-flow, high-mass-capacity, mechanical pumping system, is used to evacuate the plasma flow from the facility. The whole facility is cooled by a re-circulating chiller with associated booster pumps and heat exchangers.

Four probes can alternately be hydraulically injected into the flow 51 mm (2 inches) downstream of the nozzle exit. Three of these probes typically consist of a pitot tube to measure stagnation pressure, a Gardon gauge and a
copper slug calorimeter to measure fully-catalytic cold-wall heat flux. The fourth probe is usually configured as either a Teflon® slug calorimeter to measure non-catalytic cold-wall heat flux, a silicon carbide (SiC) probe to measure semi-catalytic cold-wall heat flux, or a test specimen. For the results presented herein in which a probe was inserted into the flow, the probe used was a 25 mm diameter SiC probe.

A more thorough description of the facility, including detailed explanations of the gas injection system, the instrumentation available in the facility, schematics and photographs, comparisons with other similar facilities, and measured free stream quantities across a wide range of flow conditions can be found in Ref 1.

Figure 1. Schematic of the HYMETS test section. Laser sheet (shown in purple) enters test chamber through one of the viewing ports. A periscope (two mirrors, indicated by thick black lines) inside the test chamber then directs the laser sheet to the flow. Dashed lines indicate the position of one of the probes when injected into the flow.

B. Test Conditions

Two different gas mixtures were used for the present study. The first is used to simulate atmospheric entry conditions on Earth and consisted of a 75% nitrogen (N₂), 20% oxygen (O₂), 5% argon (Ar) mixture by volume. The second is used to simulate atmospheric entry conditions on Mars and consisted of a 71% carbon dioxide (CO₂), 24% N₂, 5% Ar mixture by volume. The total mass flow rate was varied from 76 slpm (standard liters per minute) to 404 slpm. The arc current was varied between 100 A and 200 A. These run conditions resulted in an arc plenum pressure (upstream of the nozzle) of between 31 kPa and 130 kPa, and a specific bulk enthalpy between 6.5 MJ/kg (2,790 BTU/lbm) and 18.4 MJ/kg (7,910 BTU/lbm). (Note that the units of enthalpy are units of energy—e.g. J or BTU—but that the “enthalpies” referred to herein are specific enthalpies, meaning that they are actually enthalpies per unit mass.) Hereafter, the conditions of a given run will be referenced by the specific bulk enthalpy and by the test gas mixture (“Earth” or “Mars” for short). We estimate an upper bound on the average free stream static translational temperature to be ~1,300 K (~1,900°F) for the 6.5 MJ/kg Earth condition and ~1,600 K (~2,400 °F) for the 10.8 MJ/kg Mars condition. See section III.C.4. for an explanation of how this estimate was obtained. Table 1 contains additional flow parameters for selected runs corresponding to cases for which specific results are shown in this paper.
Table 1. Test conditions of runs described in this paper. Asterisks indicate estimated or interpolated values based on measured data from similar runs.

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C. NO PLIF Flow Visualization

The PLIF laser system includes a tunable Nd:YAG-pumped dye laser with a Rhodamine dye mixture followed by a mixing crystal. Optics formed the beam into a laser sheet ~50 mm wide by ~0.2 mm thick (FWHM) in the measurement region. The laser sheet was oriented in the horizontal plane relative to the laboratory frame of reference and perpendicular to the axis of the primary flow. Fluorescence was imaged through the optical access port on the bottom of the test chamber, onto a gated, intensified CCD at a viewing angle approximately normal to the laser sheet. Images were acquired at 10 Hz with a 1μs camera gate.

The laser was tuned to the N=13 line of the Q1 branch near 225.7053 nm. (In this notation, “N” is the rotational quantum number of the state probed by the laser and “Q” indicates a set of transitions for which the change in rotational quantum number between the probed state and the laser-excited state is zero. The subscript 1 indicates that the parity of both the upper and lower states is positive, meaning that in both states, the electronic spin is aligned with the total angular momentum of the molecule.) While the fluorescence signal levels were comparable for the more commonly used N=1-3 lines, N=13 is a well-isolated line, which is desirable for obtaining a good Doppler-shift velocity measurement.

For most arc jet conditions, we acquired 100 single shots with the sample injected. If arc jet conditions permitted, we also acquired some images without the sample in order to look at the core flow of the arc jet. If the sample is left out of the flow for too long the cooling lines in the diffuser are damaged, so obtaining images of the core flow with no sample was not possible at some conditions.

Difficulties with the placement of optics (in particular, two mirrors which form a periscope inside the test section, shown in Fig. 1) resulted in a laser sheet which did not quite reach to the nozzle exit on the upstream edge of the laser sheet (although diffuse scatter off the nozzle is visible in the images, if the contrast is adjusted). This is
an area for improvement in later tests, and in fact was improved for the quantitative velocity measurements shown below. The downstream edge of the laser sheet skimmed the face of the sample. Vertically, the horizontally-oriented laser sheet was aligned with the center of the flow. The laser sheet was fairly uniform in intensity, although a few striations are noticeable in the images.

The camera (a Princeton Instruments PIMAX-II intensified 512x512 pixel CCD camera) is effectively looking up through a round window port in the bottom of the test section. Since this port is directly below the sample and since the desired field of view is upstream of the sample, the camera is looking back toward the nozzle at an angle. The intensifier gate width was set to 1 microsecond with a constant gain of 250.

D. Molecular Tagging Velocimetry (MTV) for Axial Velocity Measurements

The NO PLIF MTV method involves writing a pattern of lines into the flowfield and observing these lines at two different times. The displacement of the lines is used determine the flow velocity perpendicular to the lines. To form a laser sheet, the collimated 226 nm beam was passed through a cylindrical lens, which focused and then diverged the beam, expanding it in one direction while leaving it collimated in the other. A spherical lens then collimated the diverging axis of the beam and focused the other axis into a thin sheet approximately 60 mm wide by 0.5-mm thick. To tag multiple lines of NO in the test section for a velocimetry measurement, a 50 mm long, LaserOptik GmbH diffusion welded lens array of 25, 1 m focal length cylindrical lenses focused the laser sheet into 25 lines, running parallel to the model surface in the spanwise direction. The spacing of the lines was approximately 2 mm.

To image the tagged lines, a Cooke DiCAM-PRO camera, with an intensified 1280x1024 pixel array interline progressive scan CCD, was used. A 100 mm focal length, F/2.0 B. Halle Nachfl. lens was used. When used in double shutter mode, the camera is capable of acquiring an image pair with a minimum 500 ns delay between the end of the first gate and the beginning of the second. Each gate has a minimum duration of 20 ns, with delay settings and durations set in increments of 20 ns. A detailed discussion of the timing sequence methodology used in the NO PLIF experiments is provided in Ref. 10. The magnification of the images (pixels/mm) factors directly into the measurement of the velocity, and into the error analysis. To determine the magnification accurately, images were acquired of a planar surface imprinted with a regular pattern of dots that was placed in the same plane as the laser sheet. Use of this so-called dotcard allowed perspective distortions to be corrected as well.10

E. Doppler Velocimetry for Radial Velocity Measurements

Doppler-shift-based PLIF velocimetry is an established measurement technique and has been demonstrated on various supersonic and hypersonic flow applications.11-15 The Doppler effect shifts the location of the spectral line center relative to the static vacuum center if the flow has a velocity component in the direction of the laser. This Doppler shift, and thus the flow velocity, can be determined from NO PLIF imaging in a variety of ways, including both fixed- and tunable-frequency methods. Fix-laser-frequency measurement schemes can measure velocity instantaneously and so are preferred when time-resolved velocity measurements are required. The process of scanning the laser frequency limits this method to measuring time-averaged velocity. Tuned-frequency schemes, however, are less susceptible to systematic error16 and the dynamic range of the technique is not limited by the finite width of the spectral line or laser line as is with fixed-frequency schemes.17 In the current study, Doppler-shift based velocimetry was used to obtain quantitative distributions of radial velocity for two flow conditions simulating a 10.8 MJ/kg Mars atmosphere (Run 114) and 6.5 MJ/kg Earth atmosphere (Run 85). By scanning the laser over a small wavelength range, the excitation spectrum of the relatively well-isolated Q1(13) transition of NO was captured on a series of images using the Princeton Instruments PIMAX-2 intensified CCD camera with 512 x 512 pixel resolution. Specifically, the scan ranges were 3.5 pm (λd = 225.7075—225.7040 nm) with a scan step size of 0.05 pm and 10 images per wavelength for the 10.8 MJ/kg Mars case (a total of 720 images acquired over 72 seconds); and 4.4 pm (λd = 225.7079—225.7038 nm) with a scan step size of 0.1 pm and 10 images per wavelength for the 6.5 MJ/kg Earth case (a total of 450 images acquired over 45 seconds). Post-analysis of these images revealed a shift in the excitation spectra, which was information used to determine absolute magnitudes of radial velocity.

III. Analysis and Results

A. Flow Visualization Results

1. Single-Shot Images

Figures 2, 3 and 4 show flow visualization results for selected enthalpy conditions for Earth and Mars, respectively. For each condition, three false-color single-shot images are shown. The flow is from left to right. The
nozzle exit is clearly visible on the left side of Fig. 2, and the face of the 1-inch diameter silicon carbide sample is clearly visible on the right side of the images.

![Image of laser sheet and nozzle](image)

**Figure 2. Location of laser sheet relative to nozzle exit and SiC probe.** The intensity in this averaged image has been adjusted so that reflected light from the nozzle can be seen relative to the luminosity of the sample.

The instantaneous NO PLIF images in Figs. 3 and 4 show highly non-uniform flow containing large-scale flow structures. These highly irregular structures appear mushroom-shaped in some images. NO fluorescence was observed over a large percentage of the core jet flow for lower enthalpy conditions. NO fluorescence was observed only on the edges of the jet flow for the highest enthalpy conditions. Background (non-LIF) luminosity was also observed on the face of the sample at all conditions, although the intensity of this luminosity varied significantly from shot to shot.

The bow shock on the sample probe was clearly visible in many of the single-shot images, and can be seen in a few of the selected sample images shown in Fig. 3. The shock is evidenced by a sudden decrease in fluorescence in front of the sample probe. As described above, images of dotcards were acquired which allow for the determination of absolute scale in the images. Using an average of 100 single shots from a low-enthalpy air run where the bow shock in front of the stagnation probe was clearly visible (6.5 MJ/kg Earth, Run 36), the shock standoff distance was measured to be $9.5 \pm 1.1$ mm.
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<th>Image</th>
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Figure 3. Single-shot NO PLIF images in false color for Earth atmosphere simulations, at various enthalpies.
2. Variation in Fluorescence Signal Intensity with Enthalpy

One approximate indication of the concentration of NO in the flow is the magnitude of the fluorescence signal; while fluorescence intensity depends on many factors (including temperature, pressure, density, species mole fractions/quenching), in general, more fluorescence correlates with a higher concentration of NO. Figure 5 shows measurements of the mean signal intensity in the core region of the flow over a range of enthalpies. In order to calculate the mean signal intensity, averaged images were cropped to exclude all but the core of the flow. The boundaries defining this region of interest are depicted by a white dashed rectangle in Fig. 6. For the Earth runs, the SiC probe was retracted briefly to allow images to be acquired of the unperturbed free stream arcjet flow. For Mars conditions, the probe was not retracted, and so the images used to calculate signal fraction were of flows with the SiC probe injected.

Enthalpies below about 14 MJ/kg produced detectable signal levels, whereas the images obtained at higher enthalpies were relatively noisy. For all conditions examined, the shot-to-shot standard deviation in the mean intensity level was of the same order as the mean intensity. First, the mean intensity value was calculated for each pixel in the measurement region. Then, the standard deviation in the intensity at each pixel in the measurement region was calculated. Finally, the mean value of this standard deviation was calculated for all pixels in the measurement region. The standard deviation relative to the mean signal may provide a qualitative indication of the level of unsteadiness or turbulence in the flow. Note that the signal levels were lower for Mars cases than for Earth cases at the same specific bulk enthalpy. One possible reason could be that the chemical pathways leading to the creation of NO are different for the two gas mixtures, and so the amount of NO produced with the Mars mixture is less than the amount produced with the Earth mixture at an equivalent enthalpy. All of the flow conditions which we examined in this series of tests exhibited non-uniform behavior.
3. Fraction of Core Flow with Fluorescence Signal vs. Enthalpy

In addition to overall intensity, another metric for the usefulness of NO PLIF as a diagnostic technique in this facility is the percentage of the flow where fluorescence signal is observed. In order to calculate this quantity—hereafter called signal fraction—single shot images were cropped in the same manner as above, with the boundaries of the measurement region shown in Fig. 6. As in the measurement of mean signal intensity in the previous section, the SiC probe was retracted for Earth runs but not retracted for Mars runs. After cropping, a uniform background intensity value was subtracted from all the images from a given run. A threshold level of 500 counts (about 3% of the maximum signal intensity obtained) was then applied and the percentage of pixels with an intensity about 500 counts was calculated.

Figure 5. Measured NO fluorescence intensity versus specific bulk enthalpy. Curve is fitted to Mean Intensity (Air) data only.

Figure 6. Indication of relative location and size of measurement region for Figures 7 and 8.
Figure 7. **Signal fraction measurements for Earth stimulant at various enthalpies.** Percentages indicate the mean proportion of the core flow for each condition with nitric oxide fluorescence signal.

Figure 7 depicts false-color and black and white cropped single-shot images for a range of enthalpies for Earth runs, and Fig. 8 depicts similar images for Mars runs. The false-color images show a representative single-shot for the given run condition (i.e. the signal fraction in the selected single-shot images is very close to the mean signal fraction for all images in that run). The corresponding black and white images show the effect of background subtraction and threshold application, with white pixels representing those with an intensity of greater than the threshold level of 500 counts.
Figure 8. Signal fraction measurements for Mars stimulant at various enthalpies. Percentages indicate the mean proportion of the core flow for each condition with NO LIF signal.

Figure 9 shows a graph of the mean signal fraction as a function of enthalpy. The error bars indicate the standard deviation in the signal fraction for all of the single shot images used to calculate the mean signal fraction for each run. The exponential fitted line was fit to the Earth data; however, the Mars data appears to follow the same trend. Enthalpies below 10 MJ/kg had signal over almost the entire flow, but over about 12 MJ/kg, less than half of the flow had signal. This provides a guideline for the flow conditions where NO PLIF velocimetry measurements should be feasible, as well as those for which low signal fractions make single-shot molecular tagging velocity measurements unfeasible. This finding was in good agreement with the results of Mizuno et al. who reported that “total enthalpy of under 10 MJ/kg is suitable” for NO LIF in JAXA’s (the Japanese Aerospace Exploration Agency’s) 750kW arc heated wind tunnel. One additional observation is that for two runs at identical conditions (the two points with an enthalpy of 12.8 MJ/kg), two different mean signal fraction values were obtained. The reasons for this are not entirely clear. The difference could be an indication of real variations in the arcjet flow, or could perhaps be a byproduct of variations in the probe laser intensity. Future measurements should include simultaneous measurements of laser intensity.
4. **Upstream Influence of Stagnation Probe**

An unexpected finding of the flow visualization images was the effect that the presence of a stagnation probe had on the flow upstream of the probe. Figure 10 shows three false-color images from an 8.0 MJ/kg Earth run. Note that in all three images, the contrast has been enhanced over the left and right side of the images to show the positioning of the nozzle exit and the SiC probe (if present). The red image on the left is an average of 42 single shots without a probe in the flow; the green image on the right is an average of 54 single shots from the same run where a SiC probe is injected into the flow. The center image shows the composite of the two, highlighting the differences between the flow with and without the probe. With the probe in place, the NO PLIF signal extends to the top and bottom of the image. With the probe removed, the NO PLIF is localized closer to the core. In a purely supersonic flow, pressure disturbances cannot propagate upstream. However, in this wind tunnel flow, the subsonic boundary layer and the nearly stagnant flow outside the core of the open jet flow provide mechanisms for pressure disturbances to propagate upstream. Because HYMETS has a diverging conical nozzle, the flow is expected to be slightly diverging as it exits the nozzle. This can be seen in both the averaged image of the unperturbed core flow (i.e., without a probe inserted into the flow) and in the averaged image of the flow with the probe injected. Additionally, there appears to be relatively little NO outside the core flow in the no-probe case, but a significant amount of NO fluorescence can be seen in this region in the probe-in case. In the images with the probe inserted into the flow, the angle of divergence appears to be somewhat greater than in the no-probe case. This interpretation is likely misleading because the differences in the images are probably due to different amounts of NO and/or different quenching environments in the shear layer between the core flow and the nearly stagnant flow for the two different conditions. (Quenching is a process by which fluorescence intensity is reduced due to collisional energy transfer from excited NO molecules to other molecules. Oxygen is particularly effective at quenching NO fluorescence, so the additional NO present in the stagnant region in the probe-in case may displace ambient oxygen, thereby reducing the amount of quenching in the shear layer.)
B. Axial Velocity Analysis and Results

1. Axial Velocity Uncertainty Analysis:

The method used to process both single-shot and average velocities and associated uncertainties is similar to the approach outlined in Refs. 10 and 18. However, to investigate the potentially unsteady nature of the core flowfield, the previous method of determining the spatial uncertainty has been modified.

In the previous estimates of single-shot spatial uncertainty, which has been documented in Ref. 10, the flow is assumed to remain essentially laminar in nature. This assumption led to a formulation of single-shot uncertainty based upon the standard deviation in the measured single-shot tagged profile shifts, which had been defined as:

\[ u_{\Delta x} = \frac{\partial u}{\partial (\Delta x)} \cdot \sigma_{\Delta x} \]

In the above equations, \( C \) is the correction factor, \( \sigma_{\Delta x} \) is the standard deviation of the observed tagged profile shift in pixels, \( t_{n-1,95\%} \) is the student t-statistic at 95 percent confidence, \( \Delta \) is the time separation between sequential frames, and \( N \) being the total number of data points at a particular pixel location used to obtain \( \sigma_{\Delta x} \). For this paper the calculation of correction factor, which has a dependence on the ratio of peak signal intensities between the initial and delayed frames, can be described by the following relation:

\[ C = a + b \left( \frac{s_{1,max}}{s_{2,max}} \right)^{1/2} + e \ln \left( \frac{s_{1,max}}{s_{2,max}} \right) \]

with the coefficients \( a, b, \) and \( e \) being 0.988, 8,993(10^{-5}), and -2.783(10^{-3}), respectively, for an effective first gate of, \( t_{g1} \), of 5 ns.

In this paper, we have obtained single-shot spatial measurement uncertainty estimates based on signal-to-noise considerations alone, since the signal-to-noise ratio is the largest contributor to the measurement uncertainty in single-shot measurements. In order to make this estimate, measurements of displacement along several tagged profiles were made in regions well outside of the core nozzle flowfield where the mean axial velocity was measured to be essentially zero for a set of 143 sequential image pairs. Additionally, over the duration of these measurements, the laser was tuned over the Q1(12) + Q2(20) transition from 226.025 nm to 226.020 nm. Tuning the laser away from the absorption peak decreased the PLIF intensity significantly, so a dependence of spatial precision uncertainty on fluorescence intensity could be established. By grouping together points with intensities in the first gate within bins, starting with points with peak intensities between 20 and 30 counts and incremented by 10-count bins up to a maximum of 410 counts, the standard deviation of the measured shifts corresponding to the mean peak intensity within each 10-count bin is obtained. Using these standard deviation values, the spatial uncertainty is calculated and plotted against the average intensity values for each 10-count bin, as shown in Figure 11. As the signal intensity in the first peak decreases, the measurement uncertainty (and the standard deviation) increases. Based upon these measurements, empirical curve fits of the single-shot standard deviation and uncertainty as functions of peak signal intensity in the first gate are obtained:
\[ \sigma_{\Delta x(S_{1,\text{max}})} = \left[ \alpha_2 + \frac{\beta_2}{(S_{1,\text{max}})^{T_S}} \right]^{1/2} \]  

(3)

\[ u_{\Delta x} = t_{N - 1.95\%} \cdot \sigma_{\Delta x(S_{1,\text{max}})} = \left[ \alpha_1 + \frac{\beta_1}{(S_{1,\text{max}})^{T_S}} \right]^{1/2} \]  

(4)

with \( \alpha_1 \) and \( \beta_1 \) being 1.222 and 4739.613, respectively, and \( \alpha_2 \) and \( \beta_2 \) being 0.299 and 1238.136, respectively.

Figure 11. Determination of spatial uncertainty as a function of signal-to-noise ratio.

To obtain an estimate of the magnitude of fluctuating axial velocity component, \( V'_x \), a relation for the dependence of the standard deviation of the mean velocity, \( \sigma_{\bar{V}_X} \), must be made that separates out the signal-to-noise dependency identified in Fig. 11. Using the relation for standard deviation of the profile shift precision for single-shot measurements as a function of signal intensity put forth in Eq. (3), the standard deviation of the mean profile shift precision as a function of mean signal intensity, \( \sigma_{\Delta x(S_{1,\text{max}})} \), is:

\[ \sigma_{\Delta x(S_{1,\text{max}})} = \sigma_{\Delta x(S_{1,\text{max}})} + \left| \frac{\partial}{\partial S_{1,\text{max}}} \sigma_{\Delta x(S_{1,\text{max}})} \right| \cdot \sigma_{S_{1,\text{max}}} \]  

(5)

This relation provides an upper-bound estimate of the standard deviation in the measured shift with respect to the mean signal at a particular pixel location. Dividing this through by the corrected time separation between the undelayed and delayed frames, \( C \cdot \Delta t_{\text{ND}} \), and squaring the result provides the variance in the measured mean velocity due to random fluctuations in the mean signal intensity at the measurement location. Based upon observations of single-shot velocity distributions throughout each image and the corresponding signal intensities, no apparent correlation between the signal and measured mean velocity magnitude exists. Therefore, the variance in measured mean velocity due to random fluctuations in signal intensity is assumed to be independent of the variance.
in the measured mean velocity magnitude due to random turbulent fluid mechanical fluctuations. The sum of these two independent variance values results in the total variance (or covariance) in the measured mean axial velocity.

Using the signal-dependent velocity variance relation based upon Eq. (5) and the total variance in the measured mean axial velocity, the fluid mechanical fluctuation in the axial velocity component is:

\[
V_x' = \sqrt{\left(\sigma_{V_x}\right)^2 - \left(\frac{\Delta x \cdot \delta_{y,\text{max}}}{C \cdot \Delta N_D}\right)^2}
\]  
(6)

2. Image Pre-Processing:

The spatial resolution for the axial and velocity experiments was measured by acquiring an image of a matrix of square marks separated at equal spatial intervals, known as a dotcard, mentioned above and detailed in Ref. 19. To correct for optical and perspective distortion of the images in these experiments, the image of the dotcard in the test section was acquired with the cameras and a corresponding undistorted image of the same dotcard was created with Adobe Acrobat software. An image registration algorithm, UnwarpJ, was then used to correct for distortion.\(^{20}\) This software is a plug-in created for the image processing software, ImageJ, a freeware image processing program available from National Institutes of Health.\(^{21}\) For the axial velocity measurements, once the undistorted axial velocity images were obtained, an undistorted background image, acquired in the absence of any fluorescence, was subtracted from the set.

To improve the signal-to-noise ratio, MATLAB\(^\circledR\) was used to apply a 4-pixel radius average disk filter to the undelayed and delayed images. The images were then binned by 4 pixels in the spanwise direction. These two steps improved the signal-to-noise by smoothing camera noise and consolidating the signal in regions tagged by the laser. However, the spatial resolution of the measurement was degraded by a factor of 4 because of this processing.

3. Axial Velocity Processing:

The processing of velocity data is similar to that outlined in Ref. 10. A 1-dimensional cross-correlation method was used to calculate both averaged and instantaneous velocity values. In this paper, no estimations of spanwise uncertainty have been made. However, due to the reduced spatial resolution of this experiment, the tagged profiles appear more closely spaced, 25 pixels peak-to-peak, than in previous analyses (Refs. 10 and 18). Additionally, the axial velocity magnitudes encountered in the current test are about three times larger than in prior work, resulting in relatively large observed shifts in the profiles between the initial and delayed frames. This presents a difficulty in automating the cross-correlation-based velocity measurement algorithm: a correlation window fixed about the tagged profile, with the same width as the peak-to-peak profile separation in the initial gate, will occasionally result in erroneous correlations with neighboring profiles.

To correct for this error, a 75-pixel-wide by 1-pixel-high window, centered about and along each tagged profile, was used to provide an initial estimate of profile shift. This selection of this window size ensured that 3 separate profiles would be encompassed, with the exception of the first and last profiles, within the initial correlation. Using this initial shift estimate, a reduced correlation window of 25 pixels wide was placed about the center of the initial profile in the undelayed frame, with an additional correlation window of the same dimension offset by the initial shift estimate in the delayed frame. If the peak signal intensity of the profile of initial frame was below 20 counts, the data was rejected. The threshold of 20 counts was imposed to neglect regions which would otherwise return poor correlations and potentially skew uncertainty and fluid mechanic velocity fluctuation estimates. Signal counts below 20 were typically too low to produce good correlations between initial and delayed frame.

4. Axial Velocity Results:

Figures 12(a) and 12(b) show averaged undelayed and delayed images, respectively. These images were obtained by averaging the 143 pre-processed individual sequential image pairs used to compute both single-shot and mean axial velocities for a 400 slpm flow with a 100 amp arc current applied (6.5 MJ/kg Earth). The approximated time separation between the two images is 550 ns. Each line is approximately 13 pixels wide, and average displacements along the centerline are approximately 20 to 21 pixels.

Figure 13(a) shows the mean axial velocities measured along the 2nd, 11th, and 20th tagged line. The center of the black data points correspond to the measured mean velocities and the width of these points to the associated uncertainty of the mean. The portions of these profiles lying outside of the core flowfield have noticeably smaller (near zero) mean velocities with uncertainties, relative to the core flow region downstream of the nozzle. Along the 11th profile located 1.97-cm downstream of the exit plane of the nozzle, the mean velocity in this region is approximately 6 m/s with an uncertainty of 26 m/s. This relatively low uncertainty is attributed to the increased
signal-to-noise levels, persistence of signal throughout all of the sequential image pairs, and negligible fluid mechanic unsteadiness relative to the core nozzle flow. Within the core of the nozzle flow, both increased mean velocities and uncertainties are observed. For this same profile, located 1.97-cm downstream of the nozzle exit plane, the mean velocity and uncertainty interval within a 1-cm region centered about the axis of symmetry are 3,073 m/s and 182 m/s, respectively. Figure 3a also provides the fluctuating velocity component, $V'_x$, computed from Equation (6), and represented by the red data points. For this same 1-cm region about the centerline along the 11th profile, the mean value of the standard deviation, $V'_x$, is 207 m/s. This represents a fluctuating velocity that is approximately 6.8% of the mean velocity.

Figure 12. Pre-processed average image from (a) undelayed and (b) delayed frame obtained during axial velocity measurements. The sample is seen to the right side of the image.

Figure 13b provides a set of single-shot velocity measurement data along the same profile regions shown in Fig. 13(a). For a 2-cm region encompassing the centerline and located 1.97-cm downstream of the nozzle exit plane, the measured mean single-shot velocity and uncertainty are 2,928 m/s and 760 m/s, respectively. The absence of continuous measurement points along the profiles displayed in Fig. 13b, and in general for the set of single-shot sequential images, is due to reduced signal levels within the core of the nozzle flow and intermittent presence of NO within this flow region. Typically within this region, only 30 to 50 percent of the total image pairs at a particular pixel location yield a measurable shift. Outside of the core of the nozzle flow, the approximate yield increases to between 90 and 100 percent.
Figure 13. Axial (a) average and (b) single-shot velocity profiles. The width of the black velocity points in (a) and (b) correspond to two times the measured uncertainty. Red data points in (a) correspond to estimated fluctuating velocity component.
Figure 14 shows the axial velocity flowfield, interpolated over the entire region encompassing the measurements obtained along each tagged profile shown in Fig. 12(a). The flow propagating down the centerline of the flow appears to have a nearly constant velocity, despite the fact that the nozzle is conical so the flow is diverging and continuing to expand.

5. Radial Velocity Analysis and Results

1. Analysis Method

Using post processing software, ImageJ, a temporal distribution of the fluorescence signal was extracted from the image sequence at each spatial location. Since the laser scanning rate was synchronized to the camera system, a spectrum of the fluorescence signal versus wavelength could be obtained from the image data: each pixel in the flow resulting in an NO PLIF excitation spectrum. As stated in the Experimental Methods section, acquiring the data for a full wavelength scan at a given condition took approximately one minute (Typical spectra obtained from three 4x4 binned regions located 4 cm downstream of the nozzle exit ($P_1$ is a region outside the core flow; $P_2$ is a region of large positive radial velocity, and $P_3$ is a region of large negative radial velocity) are shown in Fig.15. (See Fig. 18(a) for the location of these three regions relative to the overall flowfield.)
Figure 15. Three typical spectra obtained from various locations in the flow. Scatter points = experiment, solid line = Gaussian curve fit. Locations from which spectra are extracted are depicted as points in Fig. 18(a): P1 (x = 4 cm, y = 4.4 cm), P2 (x = 4 cm, y = 2.8 cm), P3 (x = 4 cm, y = -2.8 cm). 4x4 binning is used in images.

The equation for the Gaussian curve fit shown in Fig. 15 is defined as:

\[ N_p = Ae^{-\frac{4\ln(2)(\lambda - \lambda_L)^2}{\Delta\lambda_D}} \]  

(7)

where \( A \), \( \lambda_L \), and \( \lambda_D \) are the signal level, transition center wavelength, and the apparent transition linewidth. The error between the experimental data, \( N_{p,\text{exp}} \), and \( N_p \) is defined as:

\[ E = \sum \left( N_{p,\text{exp}} - N_p \right)^2 \]  

(8)

By differentiating Eq. (8) with respect to \( A \), \( \lambda_L \), and \( \lambda_D \) it was possible to minimize the total error using the iterative Newton-Raphson method:

\[ A_{i+1} = A_i - \frac{\partial E}{\partial A} \frac{\partial A}{\partial E} \]  

(9)

\[ \lambda_{L,i+1} = \lambda_{L,i} - \frac{\partial E}{\partial \lambda_{L}} \frac{\partial \lambda_{L}}{\partial E} \]  

(10)

\[ \Delta\lambda_{D,i+1} = \Delta\lambda_{D,i} - \frac{\partial E}{\partial \Delta\lambda_{D}} \frac{\partial \Delta\lambda_{D}}{\partial E} \]  

(11)

To verify that each fit variable was properly optimized, the algorithm monitored the residual error between old and corrected values. If the calculated error for each fit parameter was less than the specified tolerance of \( 10^{-10} \), the optimization process would stop and the algorithm would proceed to the next spatial location. If the error exceeded the specified tolerance, the total number of iterations would double and an updated residual error would subsequently be calculated. For most regions of the flow, the optimization process would complete after 500 iterations. In regions of low signal-to-noise, the algorithm would require substantially more iterations to complete the process. If an upper limit of 1,000,000 iterations was reached at a single location, the algorithm would discard that portion of the experimental data. The discarding of measurements usually occurred in regions of very low signal-to-noise.
signal-to-noise ratio or regions outside of the laser sheet interrogation volume (shadow regions or at the sample). By filtering out regions with low signal-to-noise (i.e. \( A < 25 \)) prior to optimization, faster processing was achieved.

After obtaining the values of \( \lambda_L \) and \( \lambda_D \) it is possible to calculate quantitative values of radial velocity. Since the laser sheet was projected normal to the axial hypersonic flow produced by the facility, any radial component of velocity will cause an apparent shift in the transition center frequency, \( \nu_c \), relative to the laser center frequency, \( \nu_L \). This shift is termed the Doppler shift and is defined as:

\[
\Delta \nu_D = \nu_c - \nu_L
\]  

(12)

The wavelength, \( \lambda \), and Doppler shift in wavelength, \( \lambda_D \), are related to wavenumber, \( \nu \), and Doppler shift in wavenumber, \( \nu_D \), through the following equations:

\[
\nu \ [\text{cm}^{-1}] = \frac{10^7 \ [\text{cm}^{-1}\text{nm}]}{\lambda \ [\text{nm}]}
\]  

(13)

\[
\Delta \nu \ [\text{cm}^{-1}] = -10^7 \ [\text{cm}^{-1}\text{nm}] \frac{\Delta \lambda \ [\text{nm}]}{\lambda^2 \ [\text{nm}^2]}
\]  

(14)

The Doppler shift is related to the component of radial velocity, \( V_r \), and the speed of light, \( c \), by:

\[
V_r = \frac{c \Delta \nu_D}{\nu_L}
\]  

(15)

The measured shift in the excitation spectra were assumed to be due entirely to the Doppler shift, thereby ignoring the collisional shift (also known as pressure shift), which is significant at higher pressures. Errors resulting from this assumption are considered below. Also, in the analysis, symmetry was invoked only to determine where the centerline frequency reference was for stationary molecules. By symmetry we assumed that the radial flow velocity in the outermost regions of the flow were equal in magnitude but opposite in sign. However, the Doppler shift was observed to be equal in these two regions. Thus the velocity in both of these regions must be zero, providing a convenient reference for zero Doppler shift.

2. Uncertainty Analysis

The main sources of random error are due to randomness in the data and low signal-to-noise ratio. As the tolerance in the optimization algorithm was set to \( 10^{-10} \), the corresponding uncertainty in the velocity is approximately \( \pm 10^{-5} \text{ m/s} \), which is negligible. The uncertainty due to low signal-to-noise is demonstrated by looking at the effect of binning (Fig. 16). The effect of binning is to increase the total signal-to-noise ratio, but also to decrease the spatial resolution of the velocity measurement.

![Figure 16. Effect of binning on the radial distribution of radial velocity (10.8 MJ/kg Mars, Run 114).](image)
It was determined that a 4X4 binning provided adequate spatial resolution to capture any small scale structures independent of the measurement technique, but also provided sufficient integration of the signal to reduce random noise observed in the unbinned data of Fig. 16. Regions in the flow at the centerline and near the top and bottom wall surfaces have a near zero radial velocity component. By analyzing the fluctuation in velocity in those regions, an estimate for the uncertainty due to random noise and flow fluctuations could be determined. Near the top and bottom wall surfaces the uncertainty was ±16.8 m/s (95% confidence). A more conservative estimate of the error due to random noise and flow fluctuations could be determined from analyzing the variation in radial velocity near the flow centerline. This uncertainty was ±26 m/s.

Sources of systematic error in the measurement include laser beam attenuation, wavelength linearity of laser, and collisional shift. Due to Beer’s law of absorption, the laser intensity decreases approximately exponentially as the laser passes through the flow. The black curve in Fig. 17a shows the measured radial distribution of signal level (A) at a streamwise position of 4 cm downstream of the nozzle exit. By assuming that the absorption coefficient is constant along the path of the light and by imposing symmetry on the fluorescence intensity profile (in the absence of laser absorption), it is possible to calculate a radial profile of laser intensity (green curve in Fig. 17a). Correcting the black curve by the attenuated laser beam recovers a nearly symmetric red fluorescence profile (red curve in Fig. 17a). The attenuation in laser intensity will be more significant near the center of the absorption transition. Doppler shifted spectra near the bottom of the image will therefore have a different laser intensity that varies depending on the Doppler shift (and resulting absorption) of the gas above. This error is simulated in Fig 17b. After applying a simulated laser intensity profile to the experimental data and re-fitting the shifted spectra (shown as dashed lines in Fig 17b), a systematic error in $\lambda_c$ can be calculated (see red and blue curves in Fig. 17b). Laser beam attenuation acts to artificially amplify $v_D$ in regions of high absorption and large radial velocity, which results in an over prediction in the magnitude of radial velocity. The maximum uncertainty due to laser beam attenuation was measured to be ±56 m/s.

![Figure 17. Effect of laser beam attenuation on the measurement of Doppler shift.](image)

There is also an uncertainty in the radial velocity measurement due to non-linearity in the laser scanning drive. Such an error would be caused by the laser’s drive software not indicating the actual change in wavelength (absolute wavelength inaccuracy does not lead to an error in the current measurement). Based on the scan linearity measurements obtained from the manufacturer, a worst case error of approximately ±0.0045 cm$^{-1}$ in $v_D$ per wave number scanned was measured. This is equivalent to a systematic error in radial velocity of approximately ±0.009($v_r$). Thus, the maximum error in velocity due to non-linearity of the laser scanning is ±4.5 m/s.

The collisional shift also contributes to a systematic error in radial velocity measurements. Though this is a chemically reacting flow for which a perfect gas analysis does not strictly apply, such an analysis can be useful for estimating static conditions in the jet for the purposes of this uncertainty analysis. For an isentropically expanded Mach 5 jet having a stagnation pressure (arc pressure) of 1.1 atm, the pressure shift at the nozzle exit is approximately 0.0006 cm$^{-1}$, which corresponds to systematic error of just 1 m/s. This error was partially mitigated by the method of which the center wavelength, $\lambda_c$, was calculated. Since $\lambda_c$ is calculated from regions in the flow...
without a radial velocity component, any pressure shift resulting from a large uniform pressure field would be accounted for.

In summary, the total uncertainty in the flow depends somewhat on the spatial location. The maximum uncertainty measured in the flow is \( \pm 62 \text{ m/s} \), which includes both random and systematic errors. This error is dominated by the laser beam attenuation. Table 2 shows the contribution of errors at three representative locations in the flow. In future experiments, weaker NO transitions could be probed to minimize the error caused by absorption.

Table 2  Contribution of random and systematic errors at three positions (P1-P3 located at x = 4 cm)

<table>
<thead>
<tr>
<th>Uncertainty Type</th>
<th>P1 (y = 4.4 cm)</th>
<th>P2 (y = 2.8 cm)</th>
<th>P3 (y = -2.8 cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Random Noise (m/s)</td>
<td>25.9</td>
<td>25.9</td>
<td>25.9</td>
</tr>
<tr>
<td>Laser Beam Attenuation (m/s)</td>
<td>0.1</td>
<td>14.6</td>
<td>55.9</td>
</tr>
<tr>
<td>Laser Non-Linearity (m/s)</td>
<td>0.0</td>
<td>3.0</td>
<td>4.5</td>
</tr>
<tr>
<td>Collisional Shift (m/s)</td>
<td>1.1</td>
<td>1.1</td>
<td>1.1</td>
</tr>
<tr>
<td>Total Uncertainty (m/s)</td>
<td>25.9</td>
<td>29.9</td>
<td>61.8</td>
</tr>
</tbody>
</table>

3. Radial Velocity Results

Fig. 18(a) shows a vector plot for the 6.5 MJ/kg Earth condition (Run 114) overlaid with contours of radial velocity. The streamwise component of velocity was determined from the MTV technique (Run 157). Fig. 18(b) shows radial distributions of radial velocity at four different streamwise locations labeled L1-L4. The position of lines L1-L4 is shown as white dashed lines in Fig. 18(a). The white points, labeled P1-P3 are the positions where the spectra shown in Fig. 15 were obtained. Due to a varying systematic error, the magnitude of the error bars in Fig. 18(b) also vary with radial and streamwise position. Due to the systematic nature of these errors, the error bars are also positioned asymmetrically to reflect the direction that laser beam attenuation and laser wavelength non-linearity affect radial velocity. The regions of Fig. 18(a) not containing measurements correspond to regions of the flow where the optimization algorithm discarded data due to low signal.

![Figure 18](image-url)
Figure 19 shows a comparison between the velocity field measured from the 6.5 MJ/kg Earth condition (black vectors) to a theoretical velocity field (red vectors) assuming a perfectly expanded jet with a nozzle half-angle of 8 degrees. To construct the field, a point source was located upstream of the nozzle, the location of which was determined by projecting the nozzle walls back to a single point. In the theoretical velocity field, the total velocity magnitude was considered constant downstream of the nozzle at a value of 2994 m/s, which corresponds to the average centerline streamwise velocity in the experimental data. Although qualitative, there is close agreement between the two cases, which confirms the point-source nature of the flow produced by the facility and gives overall confidence to both the Doppler-shift based velocimetry and MTV techniques.

![Figure 19](image)

Figure 19. Comparison of experimental velocity field (black vectors) to an ideal velocity field assuming a perfectly diverging field of constant velocity magnitude with a unique point source (white vectors). Experimental data correspond to the 6.5 MJ/kg Earth condition (Run 114 and Run 157).

Figure 20 shows a comparison of maps of measured radial velocity for facility runs corresponding to the 6.5 MJ/kg Earth condition (Run 114) and the 10.8 MJ/kg Mars condition (Run 85). Although the overall magnitudes in radial velocity are similar in the top portion of the image, the magnitude of radial velocity measured for the 6.5 MJ/kg Earth condition is typically higher than for the 10.8 MJ/kg Mars condition.
MJ/kg Earth condition is 25% larger in the lower portion of the image. For the 10.8 MJ/kg Mars condition, the magnitudes in radial velocity are similar for both the top and bottom portions of the image. This may indicate that the systematic error in radial velocity due to laser beam attenuation is larger for the 6.5 MJ/kg Earth condition compared to the 10.8 MJ/kg Mars condition.

![Image of radial velocity distribution](image_url)

**Figure 20.** Comparison of radial distribution of velocity shown as a contour plot for the 6.5 MJ/kg Earth condition (Run 114) and 10.8 MJ/kg Earth condition (Run 85).

### 4. Free Stream Static Temperature Estimation

From measurements of the spectral width, Δν₉, of the Doppler-broadened Gaussian distribution such as shown in Fig. 15, it is possible to extract the translational temperature, T, through the following relationship:

\[
\Delta v_D = v_L \sqrt{\frac{8k (\ln(2)) N_A T}{(MW_{NO}) c^2}}
\]

where \(k\), \(N_A\), \(MW_{NO}\) are the Boltzmann constant, Avogadro’s number, and the molecular weight of NO, respectively. The average translational temperature in the core of the jet at the nozzle exit was measured to be ~1,300 K (~1,900 °F) for the 6.5 MJ/kg Earth condition and 1,600 K (2,400 °F) for the 10.8 MJ/kg Mars condition. When determining Δν₉ in the fitting process, collisional broadening was neglected. Additionally, we assumed that the laser’s linewidth of 0.07 cm⁻¹ added in quadrature with Δν₉ to fit the measured linewidth. The effect of laser beam absorption and saturation are systematic errors that both artificially broaden the transition. Therefore, the actual translational temperature is likely cooler than measured here if saturation and absorption are significant. Thus, the above reported temperature is an estimation of the upper limit of the average free stream static translational temperature.

### IV. Conclusion

NO PLIF has been successfully applied to the HYMETS facility at NASA Langley Research Center for the first time. Flow visualization and velocity measurements have helped to characterize previously uncertain flow parameters by providing both qualitative and quantitative temporally and spatially resolved information about the arcjet flow. We believe that these are the first NO PLIF based axial and radial velocity measurements in an arc-heated facility. The techniques demonstrated in this paper are expected to be applicable in arc-jet flows having enthalpies of less than 10 MJ/kg, where most images exhibit strong fluorescence. At higher enthalpies, O-atom and N-atom LIF can be used to determine flow properties, although these are point measurements as opposed to planar measurements.
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References


