

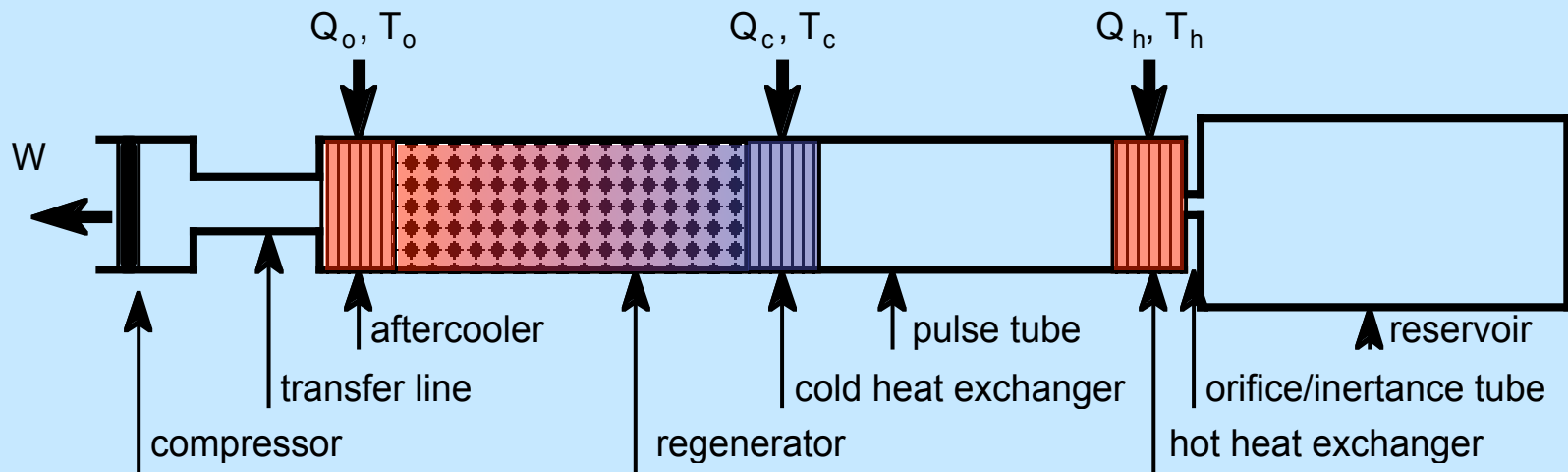
# Ultimate Temperature of Pulse Tube Cryocoolers

Peter Kittel  
Consultant

This work was funded through University Affiliated Research Center (UARC)  
Subcontract S0181769. UARC is managed by the University of California, Santa Cruz  
under NASA Ames Research Center Contract NAS2-03144

# Introduction

- ◆ Ideal pulse tube cooler with real gas
  - No losses (entropy generation) except in orifice / inertance tube
- ◆  $T_{min}$ ; result of real gas properties



# Regenerator Thermodynamics

Constraint:  $dT = 0$

**General expression**

$$ds = c_p dT/T - R dP/P$$

$$dh = c_p dT + [1 - T \beta] V dP$$

**Ideal gas**

$$ds = (V/T) dP$$

$$dh = 0$$

**Real gas**

$$ds = - V \beta dP$$

$$dh = [1 - T \beta] V dP$$

Volume expansivity:  $\beta = 1/V dV/dT|_P$

Ideal gas:  $T \beta = 1$

# Pulse Tube Thermodynamics

Constraint:  $ds = 0$

∴

**General expression**

$$ds = c_p dT/T - R dP/P$$

$$dh = c_p dT + [1 - T \beta] V dP$$

**Ideal gas**

$$ds = 0$$

$$dT/dP = V/c_p$$

$$dh = V dP$$

**Real gas**

$$ds = 0$$

$$dT/dP = T \beta V/c_p$$

$$dh = V dP$$

Volume expansivity:  $\beta = 1/V dV/dT|_P$

Ideal gas:  $T \beta = 1$

# Cooling Power

Change in Enthalpy flow at cold heat exchanger

∴

**General expression**

$$dq = \Delta dh$$

minimum  $T$

**Ideal gas**

$$dq = V dP$$

$$T_{min} = 0$$

**Real gas**

$$dq = T \beta V dP$$

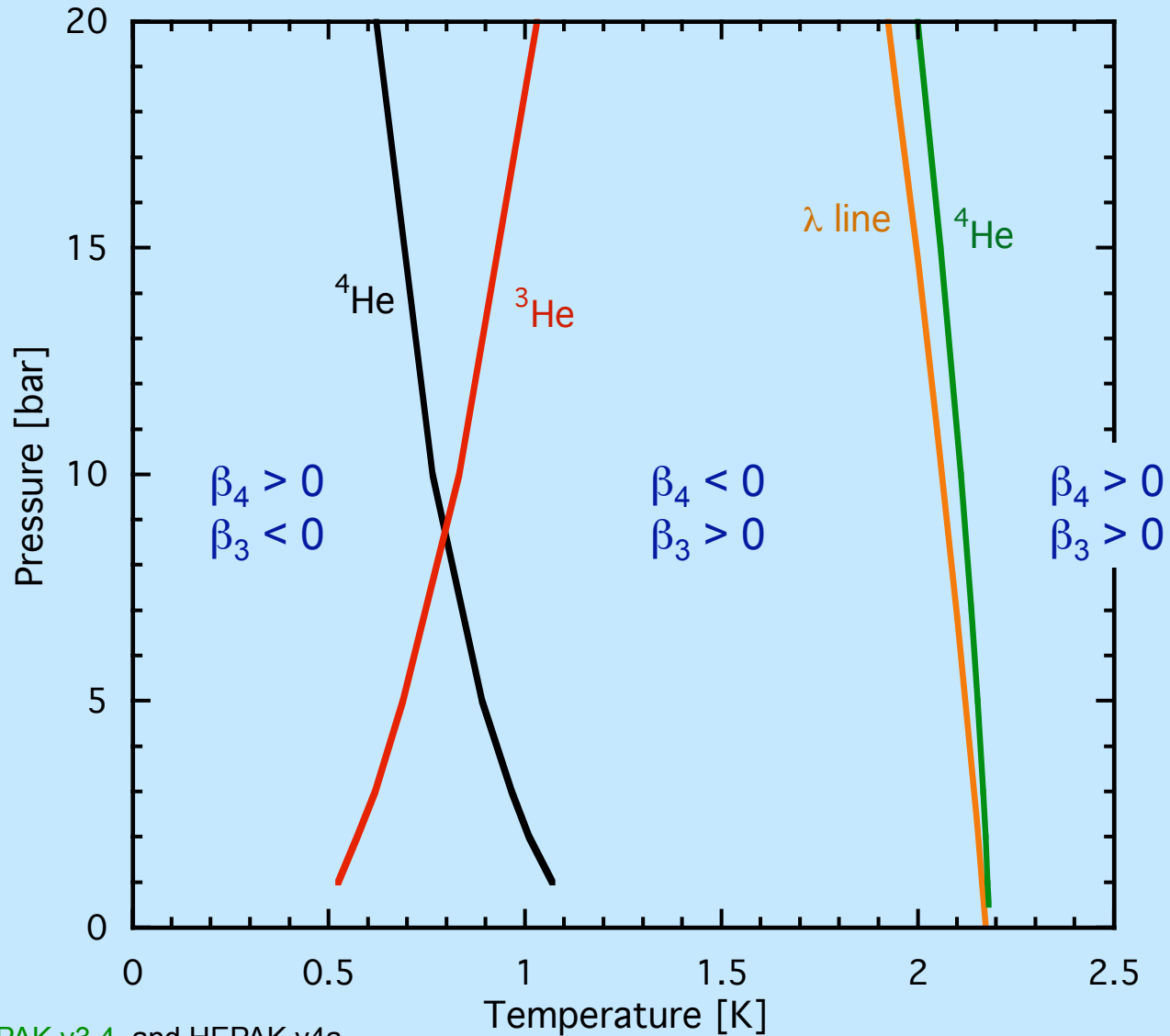
when  $\beta = 0$

$$(dV/dT|_P = 0)$$

Volume expansivity:  $\beta = 1/V dV/dT|_P$

Ideal gas:  $T \beta = 1$

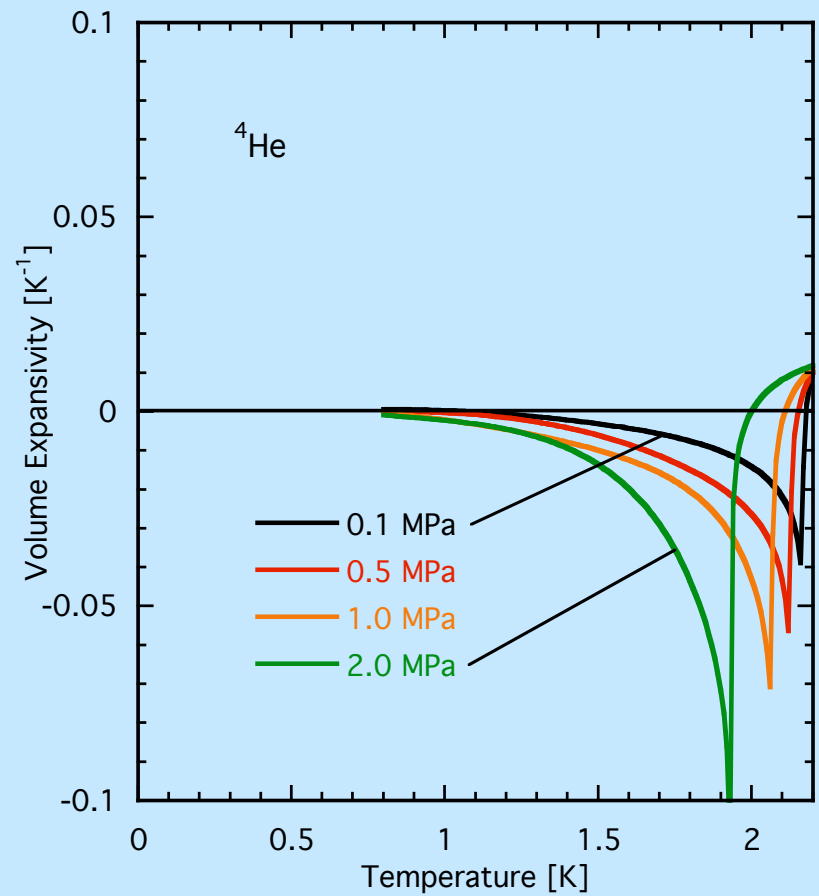
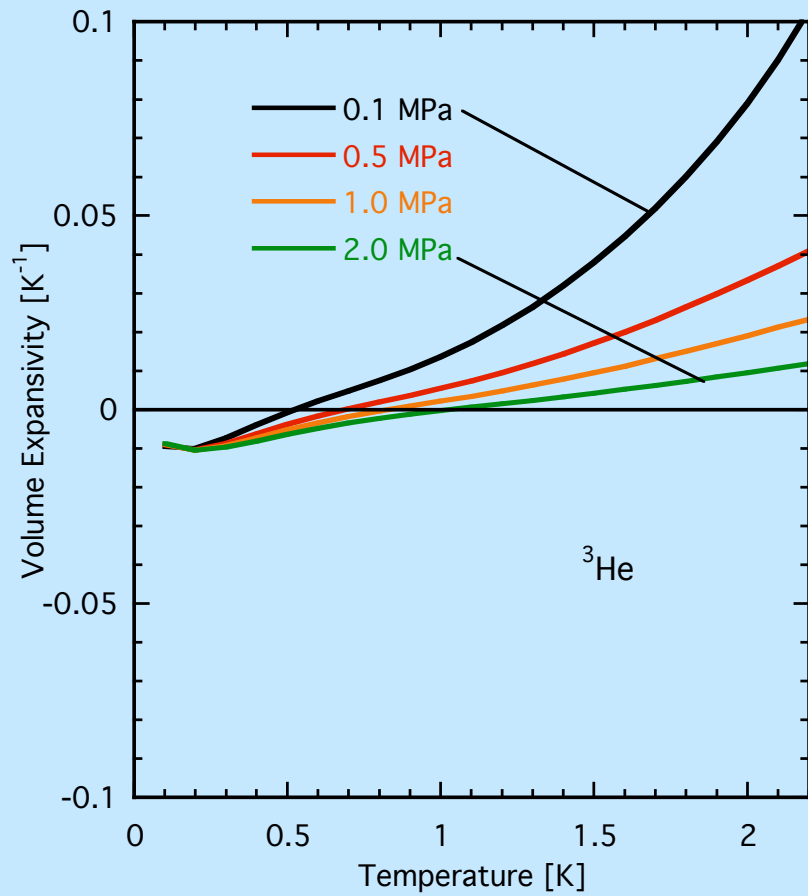
# Calculated Loci of $\beta = 0$



# ? Meaning of $\beta \neq 0$ ?

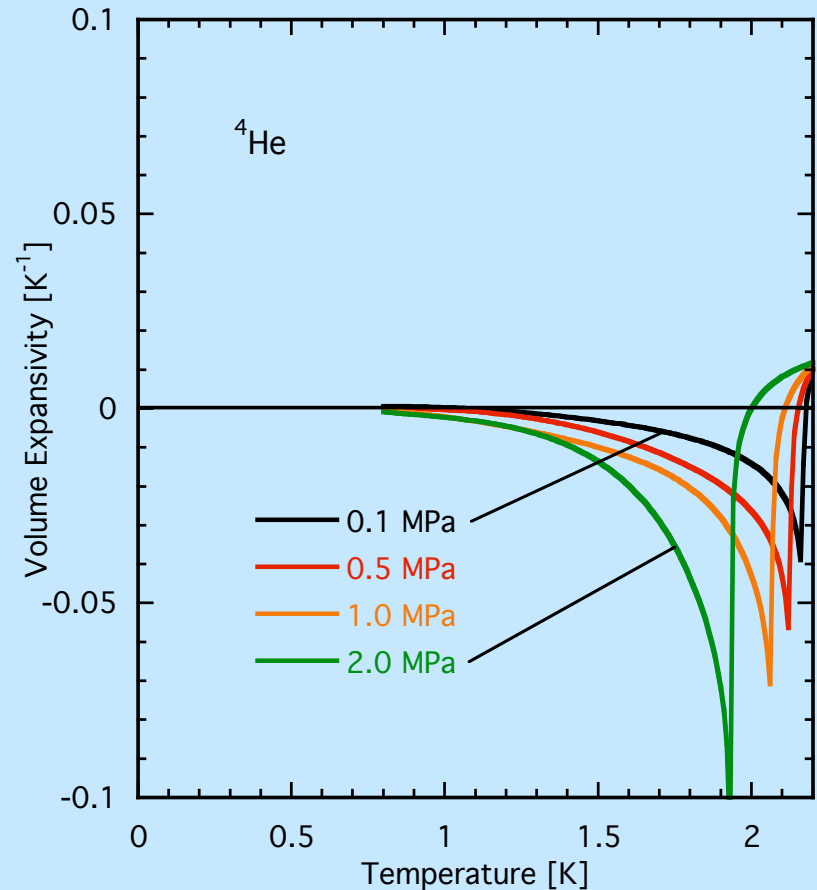
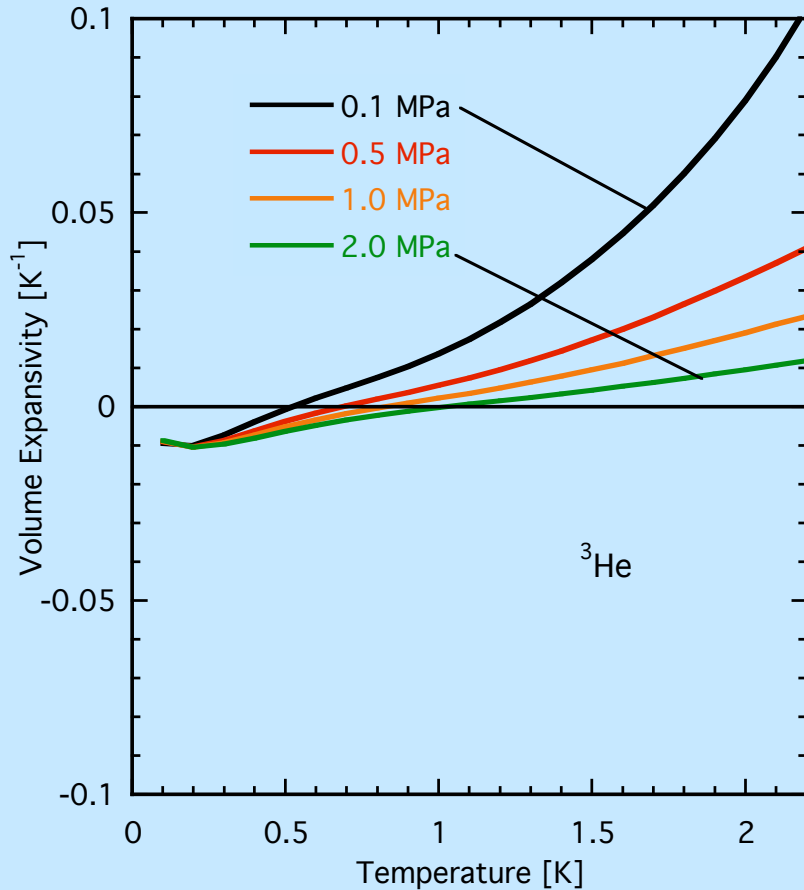
- ◆  $\beta > 0 \rightarrow$  Conventional PT
  - Can PT operate below 0.5 K ?
- ◆  $\beta < 0 \rightarrow$  What does this mean ?
- ◆ Effect of mixing  $^3\text{He}$  and  $^4\text{He}$  ?

# $\beta$ of $^3\text{He}$ and $^4\text{He}$





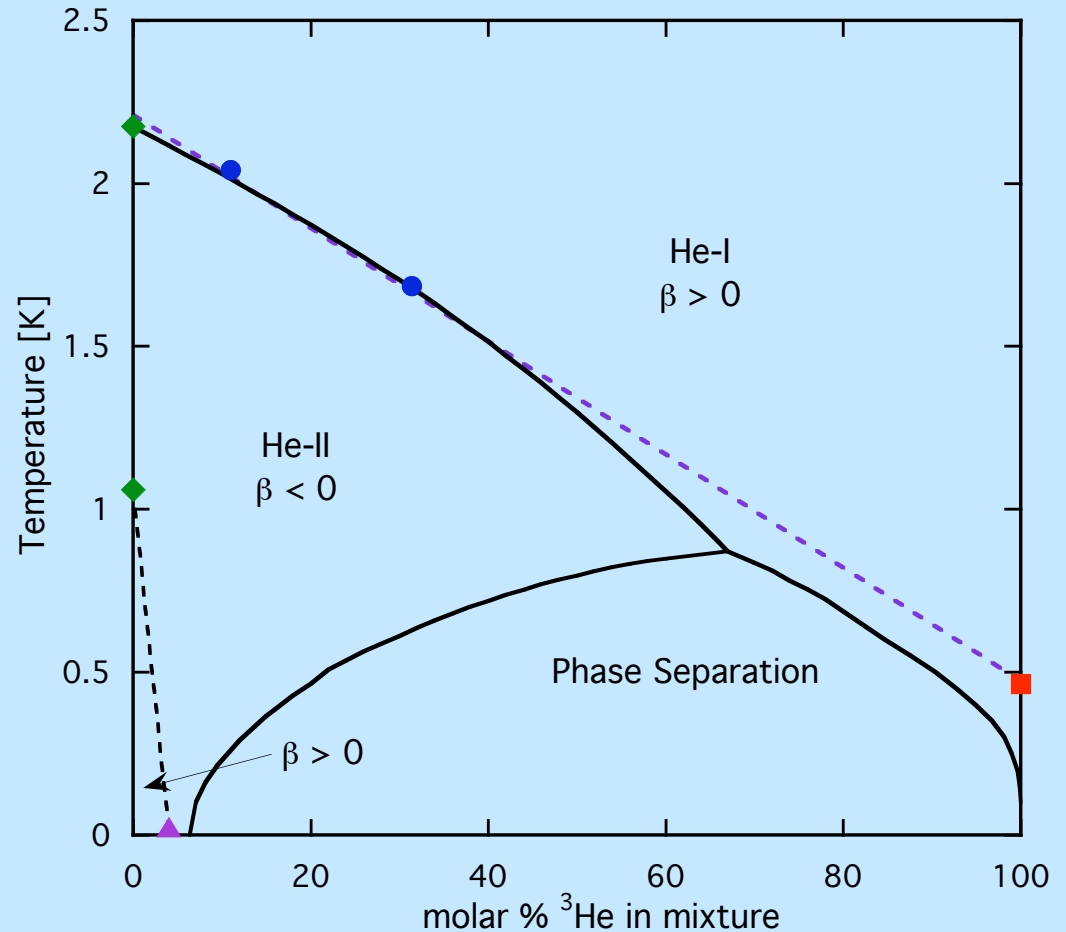
# $\beta$ of $^3\text{He}$ and $^4\text{He}$



- ◆  $\beta < 0$ : reverse enthalpy flow or  $\Delta\Phi$  between  $\dot{m}$  and  $P$  by  $\sim 180^\circ$
  - ◆  $\beta_3 < 0$ ,  $T < 1$  K:  $\beta$  is small
  - ◆  $\beta_4 > 0$ ,  $T < 1$  K:  $\beta$  is very small
- } to small to be useful

# $\beta = 0$ ; Mixed $^3\text{He} / ^4\text{He}$

- ◆ all data at SVP
- ◆ limited data in He-I region  $\approx$  straight line fit
- ◆ more data in He-II region
- ◆ lower  $\beta > 0$  region over estimated



Esel'son, B.N., et al.,  
*Solutions of  $\text{He}^3 - \text{He}^4$  Quantum Liquids*,  
Nauka, Moscow, 1973 (in Russian) p. 424.

Ebner, C. and Edwards, D.O.,  
"The Low Temperature Thermodynamic Properties of Superfluid Solutions of  $^3\text{He}$  in  $^4\text{He}$ ,"  
*Physics Reports* **2**, pp. 77-154 (1971)

# Los Alamos superfluid pulse tube

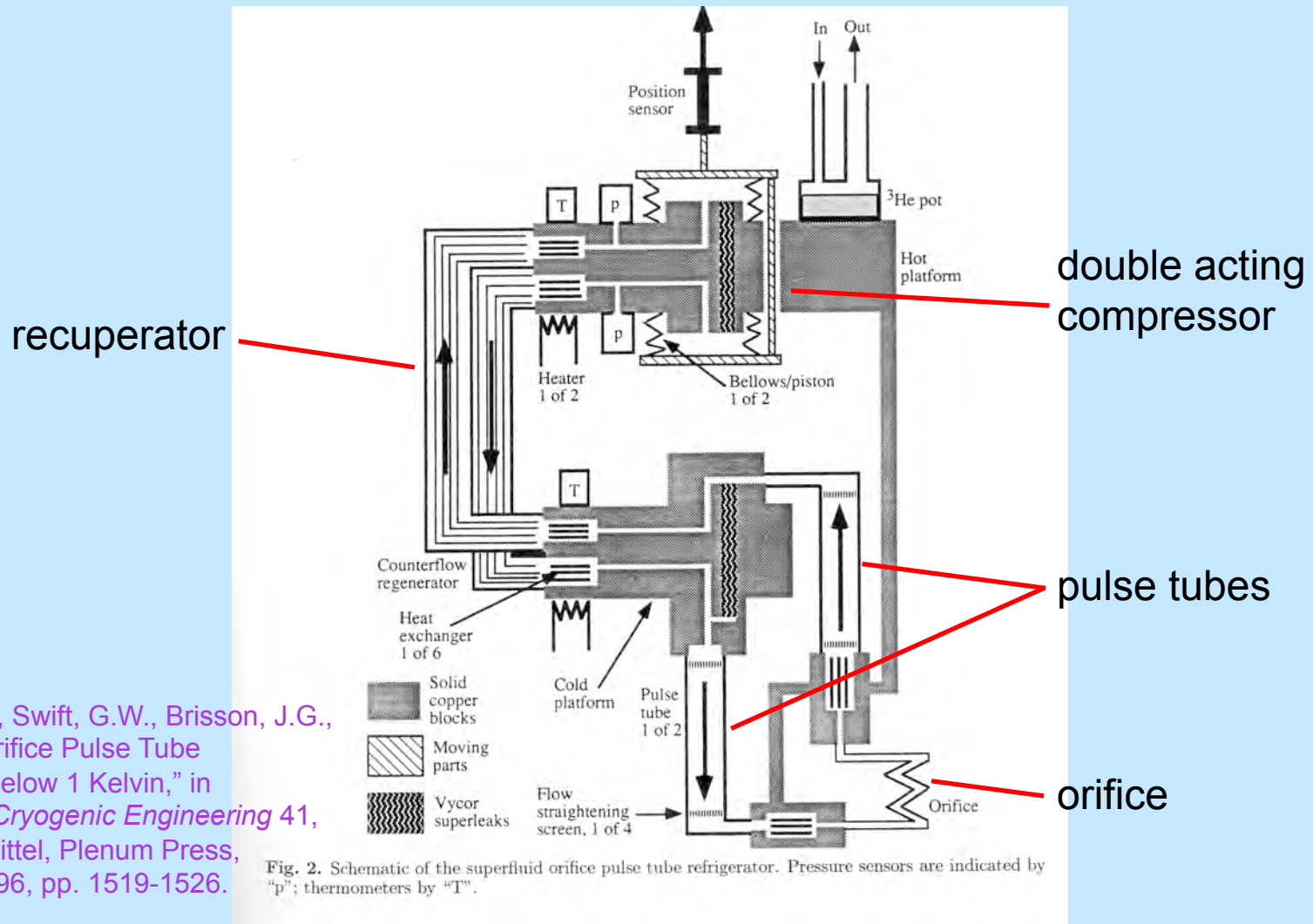


Fig. 2. Schematic of the superfluid orifice pulse tube refrigerator. Pressure sensors are indicated by "p"; thermometers by "T".

Watanabe, A., Swift, G.W., Brisson, J.G., "Superfluid Orifice Pulse Tube Refrigerator below 1 Kelvin," in *Advances in Cryogenic Engineering 41*, edited by P. Kittel, Plenum Press, New York, 1996, pp. 1519-1526.

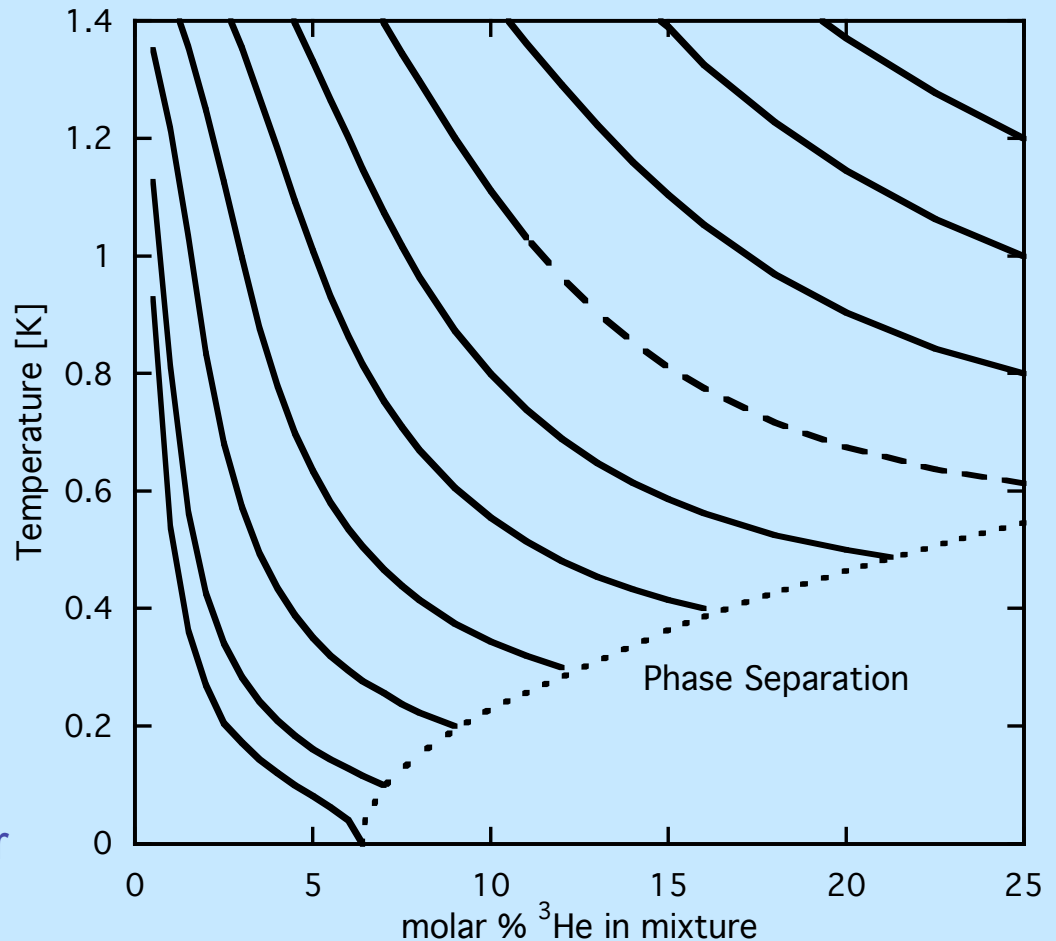
# $^3\text{He}$ in Superfluid $^4\text{He}$

## ◆ 2-fluid behavior

- $T < 1$  K:  $^3\text{He}$  low-density gas moving in fixed  $^4\text{He}$  background
- Los Alamos pulse tube cooler
  - filled with 17%  $^3\text{He}$  and operated between 1 K and 0.6 K
- Compressor does not cause pressure oscillations
  - causes the  $^3\text{He}$  concentration,  $x_3$ , and the osmotic pressure,  $\Pi_3$ , to oscillate.
  - in regenerator, heat exchangers, and orifices
    - $\nabla P$  replaced by  $\nabla \Pi_3$
  - In the pulse tube
    - constraint that  $\nabla P = 0$  is replaced by  $\nabla \mu_4 = 0$   
 $\mu_4$  is the chemical potential of the  $^4\text{He}$ .

# Loci of Constant $\mu_4$

- ◆ Dashed line:  
approx operation of  
Los Alamos cooler
- ◆  $T_{min}$  = phase separation
- ◆ Lowest  $T \Rightarrow$   
 $x_3 < 6.4\%$  @ cold hx  
 $x_3 < 1\%$  @ 0.6 K
  - Low density of  $^3\text{He}$   
limits the mass flow and  
cooling in practical cooler



# Summary

- ◆ Below  $\approx 1$  K,  $^3\text{He}$  concentration driven pulse tube
  - possible with no known ultimate limiting temperature
  - lack of thermodynamic data at very low  $T$
- ◆ Limit of conventional pulse tube cryocoolers:  $\beta = 0$ 
  - $^4\text{He}$  limit  $T > \approx 2.2$  K
  - $^3\text{He}$  limit  $T > \approx 1$  K.
  - mixture of  $^4\text{He}$  and  $^3\text{He}$ :
    - limit adjustable
  - mixing ratio not constant throughout the cooler
    - because  $\mu_4(T, P)$
  - $T_{min}$  depends on the mixing ratio at the cold hx

