Icing alters the shape and surface characteristics of aircraft components, which results in altered aerodynamic forces and moments caused by airflow over those iced components. The typical effects of icing are increased drag, reduced stall angle of attack, and reduced maximum lift. In addition to the performance changes, icing can also affect control surface effectiveness, hinge moments, and damping. These effects result in altered aircraft stability and control and flying qualities. Over the past 80 years, methods have been developed to understand how icing affects performance, stability, and control. Emphasis has been on wind-tunnel testing of two-dimensional subscale airfoils with various ice shapes to understand their effect on the flowfield and ultimately the aerodynamics. This research has led to wind-tunnel testing of subscale complete aircraft models to identify the integrated effects of icing on the aircraft system in terms of performance, stability, and control. Data sets of this nature enable pilot-in-the-loop simulations to be performed for pilot training or engineering evaluation of system failure impacts or control system design.

**Nomenclature**

- $b$: wing span
- $C_{d}$, $C_{D}$: drag coefficient
- $C_{h,AA}$: aileron hinge moment
- $C_{L,AA}$: aileron control effectiveness
- $C_{l}$, $C_{L}$: lift coefficient
- $C_{m}$: pitching moment coefficient
- $C_{m}^{a}$: pitching moment coefficient derivative with AoA, longitudinal stability
- $C_{N}$: normal force coefficient
- $c$: chord length
- $k/c$: ratio of protuberance height to chord length
- $Re$: Reynolds number
- $\sigma$, AoA: angle of attack, deg
- $\beta$: angle of sideslip, deg
- $\delta_{a}$, $\delta_{e}$, $\delta_{r}$, $\delta_{f}$: control surface deflection: aileron, elevator, rudder, flap, deg

**I. Introduction**

Airframe icing has been a threat to aviation safety for nearly 80 years. Over that time, significant progress has been made to reduce the hazard through the design and implementation of ice protection systems, improvement of certification procedures, and improved pilot training. The foundation of these advancements has been research to better understand the icing environment, the physics of the ice accretion process, and the degrading aerodynamic effects caused by ice. However, even with these advancements, icing-induced loss of control incidents and accidents have occurred and continue to occur on all classes of aircraft, from general aviation airplanes [1,2] and business jets [3,4] to transport category aircraft [5–11]. These events typically result from a combination of causal factors, but they usually precipitate from the altered aerodynamics caused by icing.

The continuing problem of icing has been recognized by many organizations including the National Transportation Safety Board (NTSB), the Commercial Aviation Safety Team (CAST), the Federal Aviation Administration (FAA), and the National Aeronautics and Space Administration (NASA). The NTSB has made numerous safety recommendations after icing related incidence and accidents and has ranked icing among its “MOST WANTED Aviation Transportation Safety Improvements” since 1997. CAST, a consortium of industry and government organizations working to improve aviation safety, has developed interventions specific to icing. They have also specified that the implicit icing effects on flight envelope protection and high-fidelity simulators for upset recovery training are among their highest ranked intervention needs [12]. The FAA and the NASA Aeronautics Research Mission Directorate have invested significant resources to support these safety recommendations, develop interventions, and to advance the state of knowledge on the icing atmosphere, the ice accretion process, and aerodynamic effects of icing.

The purpose of this paper is to review the methods currently available to model and simulate icing effects on performance, stability, and control. The primary method to model icing effects uses wind-tunnel testing of 2-D and 3-D models to develop mathematical expressions or databases of aerodynamic forces and moments. Icing effects simulation uses these mathematical models or databases in conjunction with the equations of motion to explore the inter-relationship of various parameters and the modified flight envelope imposed by the iced aerodynamics. Icing effects modeling and simulation methods have varied maturity levels and limitations in terms of verification and validation. Recommendations are made to continue research in flight simulation modeling and real-time modeling to continue advancing the state of the art.
II. Airframe Icing: How it Forms

To model and simulate the degraded aerodynamics that results from ice, one should understand the ice accretion process and the resulting ice characteristics because they drive the aerodynamic effects.

Ice forms on an airplane as it flies through clouds consisting of supercooled liquid droplets (i.e., liquid water drops that are below 0°C). The liquid droplets impinge on the leading edge surfaces, exchange heat with the environment and aircraft surface, and change phase from liquid to ice. Initially, the ice forms as a thin, rough layer. Over time, the ice thickness increases and reshapes the leading edges of all frontal surfaces. The rough, reshaped leading edges, in turn, degrade the aerodynamics of the airframe.

The ice accretion characteristics (size, shape, extent, roughness, and translucency) are related to the atmospheric environment parameters, the flight condition, the geometry of the aircraft component being iced, and the time in icing conditions. The icing cloud atmosphere has been defined using three primary parameters.

1) Liquid Water Content (LWC): a measure of the amount of liquid water in a unit volume of space.

2) Median Volumetric Diameter (MVD): a representative size of the water droplet spectrum. MVD is a value for a given spectrum such that half the volume of water is in drops with diameters smaller than the MVD and half the volume of water is in drops with diameters greater than the MVD.

3) Static Temperature (Ts): the ambient air temperature.

The flight conditions consist of true airspeed, angle of attack, and altitude. Geometric parameters consist of the size of the leading edge radius, the chord length (c), single or multi-element wing, and straight or swept wing or tail. Each of the preceding parameters influences the ice accretion development. The result is a multitude of possible ice shapes.

To illustrate the resulting geometry change due to icing conditions, two ice shapes are shown in Fig. 1. They were accreted on a NACA 23012 airfoil model in the NASA Icing Research Tunnel [13]. Figure 1a shows an example of a horn ice shape that forms at temperatures near freezing, where impinging water droplets can flow before freezing. Figure 1b shows an example of a streamwise ice shape. This type of ice forms at temperatures well below freezing where all of the impinging droplets freeze immediately on contact with the airfoil. Because these shapes are so different, they have very different effects on the aircraft aerodynamics.

To reduce the aerodynamic penalty of icing, ice protection systems (IPS) [14] are typically incorporated into airplanes to prevent or remove ice from critical flight components such as the wing and tail, engine nacelles and air intakes, propellers, and others. Ice protection systems that prevent ice from forming are typically called anti-icing systems, whereas those that remove ice are called de-icing systems. Anti-icing systems typically use heat from engine bleed-air or electrothermal heaters to evaporate water drops that impinge on the leading edge surfaces or to prevent the water drops from freezing on the heated areas. De-icing systems debond ice that has already formed on the leading edge through a mechanical deformation of the surface (e.g., pneumatic de-icing boots) or through intermittently heating the surface (e.g., electrothermal heaters near the propeller root). The design of an IPS on any given airplane may use a combination of anti-icing and de-icing equipment. Some airplanes have bleed-air thermal anti-icing on the wings and engine nacelle leading edges only, leaving the tail surface completely unprotected. Others have pneumatic de-icing boots on the wing, and on the horizontal and vertical tails while having electrothermal de-icing on propellers. Some have a combination of bleed-air thermal anti-icing on the wing and engine nacelle leading edges, pneumatic de-icing boots on the horizontal tail, and no-ice protection on the vertical tail.

There are other IPS designs as well, so the list could go on. In the end, the airframe manufacture determines the locations in which ice protection is needed and what type of IPS is required to enable safe flight operations in icing conditions and meet certification requirements.

Airframe icing is a highly complex dynamic phenomenon. The ice that forms on an airplane is the result of a combination of icing cloud atmospheric parameters, flight conditions, airframe geometry, location and type of ice-protection systems, and the time flown in icing conditions. Icing atmospheric conditions are not static but change spatially and temporally. Similarly, flight conditions and airplane geometry change as the phase of flight changes from climb, cruise, descent, to approach and landing. Some ice-protection systems do not remove all ice, but leave residual ice on the protected surface. Some thermal IPS may not fully evaporate the impinging water and allow water to run back aft of the protected areas where it freezes to form frozen rivulets, an ice ridge, or other shapes. The amount of time in icing conditions also plays a significant role as ice builds up on the unprotected surfaces such as unprotected tail, struts, radome, engine pylons, and flap hinge fairings.

Clearly, the inputs to icing formation are multidimensional and result in a wide range of potential ice shapes and ice characteristics. This presents a large challenge to accurately predict the entire range of possible effects on aircraft performance, stability and control, and handling. Over the past 80 years, many efforts have been undertaken to advance the understanding of ice accretion and the impact on aerodynamics. The next section briefly discusses some of these advances.

III. Modeling Icing Effects: Wind-Tunnel Results From Two-Dimensional Wing Models

The typical aerodynamic effects of ice on airfoils are increased drag, a reduced stall angle of attack, and a reduced maximum lift. In addition to these primary parameters, icing affects the pitching moment and, if equipped with a control surface, the control effectiveness and hinge moment.

To understand and model these effects, research organizations have conducted numerous wind-tunnel tests on a number of 2-D airfoil models and some 3-D wing and tail models. Recent iced aerodynamics simulation studies provide a significant body of knowledge examining the effects of ice accretion (size, shape, roughness, 3-Dity) on drag increase, lift loss, and stall characteristics of a NACA 23012 airfoil at full-scale and subscale geometry and Reynolds numbers [13]. Figure 2 illustrates the change in performance characteristics with different ice shapes at $Re = 1.8 \times 10^6$. Increase in drag is observed at the initial onset of icing (roughness),
and drag continues to increase as the ice takes shape and continues to grow in size. Drag increase is observable at all angles of attack. Ice affects lift mostly at higher angles of attack in which early stall occurs. For roughness, this is due to early flow separation caused by loss of boundary-layer momentum. For larger ice shapes, early stall occurs because the separation bubble that forms aft of the ice shape cannot reattach to the airfoil. Before this new stall point, there are shifts in the lift curve slope and the stall break, and post-stall behavior is clearly affected by the ice. The pitching moment is also affected due to the altered pressure distribution over the airfoil, and a pitch up tendency occurs at significantly lower angles of attack compared with the clean (no-ice) baseline.

Ice accretions have also degraded control surface effectiveness and increased the hinge moment loads on 2-D airfoil models. Figure 3 shows the effect of a simulated ice shape on aileron effectiveness ($C_{h,AA}$) and hinge moment ($C_{h,AA}$). This data are for a forward facing quarter round, $k/c = 0.0136$ at various chordwise locations at $Re = \frac{1.8 \times 10^6}{15}$. The first plot shows the rate of change in lift coefficient with change in aileron deflection, and the second plot shows the rate of change in hinge moment with change in aileron deflection. On the clean airfoil, the $C_{h,AA}$ value remained relatively constant from $AoA = -5$ deg to 5 deg. As the angle of attack was increased from this point, there was a gradual, almost linear, reduction in aileron effectiveness to $AoA = 14$ deg where the airfoil stalled. At stall, there was a sudden reduction in aileron effectiveness, where $C_{h,AA}$ became negative, meaning that deflecting the aileron trailing edge down at this angle of attack decreased lift. All three ice-shape locations ($x/c = 0.02, 0.10, \text{and } 0.20$) showed reduced aileron effectiveness at $AoA = 0$ deg, when compared with the clean airfoil. However, the reductions were greater when the ice shape was located at $x/c = 0.10$ and 0.20 than when it was located at $x/c = 0.02$. For all three iced cases, the aileron effectiveness started to decrease at lower angle of attack than the clean model. However, the rate at which it decreased varied with ice-shape location. The hinge moment data did not show any noticeable trend in the rate of change in hinge moment with aileron deflection. The $C_{h,AA}$ values did not appear to vary significantly with change in angle of attack. Also, the presence of ice shapes did not appear to have altered the $C_{h,AA}$ values significantly either.

Experimental efforts such as these have enabled a comprehensive understanding of the basic flow physics associated with various ice accretions and helped identify the major aerodynamic penalties associated with the particular ice accretion studied. Bragg et al. [16] provided an in-depth analysis of flowfields caused by ice geometries categorized as roughness, horn ice, streamwise ice, and spanwise ridge ice. Studies such as these are critical in developing and validating computational fluid dynamics (CFD) tools to predict iced airfoil and eventually iced airplane, aerodynamic characteristics. These studies are also beneficial in defining ice-shapes characteristics that are critical to specific aerodynamic parameters. However, to understand the interaction of iced wings and tails for various ice shapes on airplane flight dynamics, a different approach and test methods need to be employed.

IV. Modeling Icing Effects: Wind-Tunnel Results

From Subscale, Complete Airplane Models

When considering the aerodynamic effects of ice on an airplane configuration, the effects found on 2-D airfoils apply, but are expanded upon. In this case, the effects of drag on the airfoils are not isolated, but couple into the pitching moment of the airplane. The lift degradation on the horizontal tail also couples into the airplane pitching moment in a static sense but also a dynamic sense by reducing pitch damping. Lift degradation on the wing can affect longitudinal stability and roll damping. Adding the consequence of reduced control surface effectiveness can lead to an aircraft with substantially degraded stability and control and handling qualities.

These coupling effects are dependent on the airplane design, and airplane manufacturers are required to demonstrate safe flying characteristics with potential ice accretions that may occur in both normal operation and failure of the ice-protection system. To manage the wide range of possible ice shapes as described in Sec. II, the ice shapes tested are divided into three scenarios, but the onus is on the manufacturer to define the most critical ice shape for the given scenario. The work that has been and continues to be performed in aerodynamic studies such as [16] helps identify the critical ice-shape features and verify applicability of data from subscale testing. In practice, the ice shapes now commonly tested are 1) ice roughness,
(simulating delayed IPS activation or residual/intercycle ice), 2) runback ice (ice that forms aft of thermal IPS), 3) failure ice (ice that forms on the IPS after a failure, typically large horn ice), and 4) holding ice (ice that forms on unprotected surfaces during a 45 min hold, typically large horn ice).

Two test methods have been used to collect data on subscale, complete airplane models with ice shapes. These are static testing and static and dynamic testing. Each of these will be discussed in the following subsections.

A. Static Testing of Subscale, Complete Airplane Models

Static testing produces databases of airplane force and moment coefficients for static conditions ($\alpha$, $\beta$, $\delta_{\text{control surface}}$, ice case). These databases provide valuable insights into the effects that ice has on the airplane stability and control. Two examples of this type of modeling are provided to demonstrate this.

Prompted by icing related incidents, C. L. ’Kelly’ Johnson investigated the effects of ice on performance, stability, and control on the Lockheed Electra [17]. He found through wind-tunnel tests using artificial ice shapes with a scaled model (Fig. 4) that maximum lift was reduced by 32%, drag was increased by 47%, stall angle of attack was reduced by 4°, and aileron control effectiveness was reduced by 36%. Figure 5 shows the effect of icing on roll control. The results were obtained at $Re = 1.6 \times 10^{6}$. These data clearly show the dramatic reduction in stability and control when the Electra was iced up.

More recently, NASA conducted a static wind-tunnel test on a twin-engine short-haul transport to measure icing effects on performance and stability [18] at the NASA Langley Research Center (LaRC) 14 by 22 ft wind tunnel. These tests were conducted on a 1/8-scale model (Fig. 6) at $Re = 1.7 \times 10^{6}$. Representative results from this test are shown in Fig. 7. In this case, the ice shapes on the wings reduced stall angle of attack by about 5 deg and lowered maximum lift coefficient ($C_{L,\text{max}}$) by approximately 16% compared with the clean data at the test Reynolds number. The difference between the iced configuration and the no-ice configuration at flight Reynolds number is expected to be greater due to increase in $C_{L,\text{max}}$ for the no-ice configuration. A positive shift in the pitching moment occurred with the ice cases, but longitudinal stability ($C_{\alpha}$) was approximately the same as the no-ice case until the AoA reached about 8 deg where stall occurred and the aircraft became longitudinally unstable. No data were acquired with control surface deflections other than flaps in this wind-tunnel test, so that control effectiveness with the ice shapes could not be evaluated.

B. Static and Dynamic Testing of Subscale, Complete Airplane Models

Although static testing provides insights into the effect ice has on stability and control, it does not address the effects on dynamic motion. To better understand and model the full range of an iced aircraft flight dynamics, data from forced oscillation and rotary balance tests need to be gathered.

To that end, static and dynamic wind-tunnel tests were conducted under various projects on scaled DeHavilland DHC-6 Twin Otter, Cessna business jet [19], and Lockheed S-3B Viking models at the Bührle Applied Research Large Amplitude Multi-Purpose (LAMP) facility in Neuburg, Germany (Fig. 8). The scale of the models were 6.5, 8.3, and 6.5% and they were tested at $Re = 0.13, 0.15$, and $0.20 \times 10^{6}$, respectively.

The primary purpose of these research efforts was to understand the effect of airframe icing on flight dynamics. This was accomplished through the creation of flight simulation models that used the aerodynamic databases derived from wind-tunnel test results. This process was used to explore the utility of iced flight simulation in pilot training applications using the Twin Otter aircraft. Simulation models were developed for the no-ice (clean) and two IPS failure ice-shape configurations. The successful implementation of this approach led to a similar effort using a Cessna business jet. In this case, four configurations were considered: no-ice (clean), ice roughness, wing IPS failure ice, and wing runback ice. Lastly, since NASA John H. Glenn Research Center at Lewis Field is modifying a Lockheed S-3B Viking for icing flight research, there is a need to understand the impact of potential ice accretions on its flight dynamics. In this case, data were acquired for the no-ice baseline configuration and icing configurations consisting of large horn ice shapes on the wing and tail leading edges to represent a hold in icing conditions, and spanwise ridge shapes aft of the thermal IPS on the wing and horizontal tail to represent runback ice.

1. Challenges Associated With Subscale, Complete Airplane Model Testing

The geometric scale of these models and the associated Reynolds numbers required the development of methods to account for 1) the premature stalling characteristics typical of low $Re$ and 2) ice
accretion scaling to represent full-scale iced aerodynamics. To develop flight simulation models that are representative of full-scale flight characteristics from the low-Re wind-tunnel data, the clean non-ice wind-tunnel data are projected out along a trend line to the angle of attack in which stall is anticipated at flight Reynolds numbers. This angle of attack can be determined from other sources such as high Reynolds number wind-tunnel data and flight tests. This method of data extension is shown in Fig. 9 for the Twin Otter and Fig. 10 for the Cessna business jet. Another challenge with this type of wind-tunnel data is the reduced effectiveness of flaps for high lift (Fig. 9). As flap angle increased, the change in lift associated with that flap deflection was not as great as seen in flight. In this case, corrections were made based on flight data.

The small geometric scale of the complete airplane test articles required methods for defining the size and position of artificial ice shapes to represent full-scale aerodynamics. Although research on subscale 2-D airfoils with large ice shapes has shown iced aerodynamics to be relatively insensitive to Re effects [16], these complete aircraft model tests were conducted at much lower Re, and further research was warranted. To that end, a series of wind-tunnel tests on full-scale, mid-scale, and small-scale test articles were conducted. The small-scale test articles were representative of the subscale complete aircraft models. For the Twin Otter, this consisted of testing a full-scale, a 42%-scale and a 7%-scale horizontal tail (Fig. 11) to identify the size and position of the artificial ice for the 6.5%-scale Twin Otter model [20]. The full-scale ice shape for the wing and horizontal and vertical tail are shown in Fig. 12.

For the Cessna business jet, these tests used a full-scale, a 41.7%-scale and an 8.3%-scale wing panel model (Fig. 13) to identify the artificial ice for the 8.3%-scale business jet model [21]. The full-scale ice shapes that were tested are shown in Fig. 14.

These tests provided valuable insight into the aerodynamic scaling relationships for artificial ice shapes. For example, the failure IPS ice shapes could be geometrically scaled to obtain representative aerodynamics with the subscale model at low Re conditions. The roughness and runback ice cases for the Cessna business jet proved to be greater challenges. For these ice shapes, geometric simulation did not produce acceptable results because the full-scale $C_{L_{\text{max}}}$ with ice shapes were greater than the subscale no-ice baseline $C_{L_{\text{max}}}$. This led to determining the size and position of artificial ice on the subscale model that had similar offsets to those observed in the full-scale tests. Those results were then projected to the flight Re condition similar to the no-ice baseline simulation models.

2. Aerodynamic Model Results

The aerodynamic scaling tests provided confidence that the measurements made in the LAMP facility could be used for
modeling full-scale flight dynamics. The data acquired at the LAMP consisted of forces and moments along all three axes for static conditions \((\alpha, \beta, \delta_e, \delta_r, \delta_f)\); forced oscillations in roll, pitch, and yaw axes; and steady rotation about the wind vector. These data were acquired for the no-ice baseline and for the iced configurations. The no-ice baseline data were shifted to a full-scale \(Re\) stall AoA as described earlier. To illustrate key effects that ice had on the aerodynamic characteristics, select aerodynamic model results from the Twin Otter effort \([22,23]\) are presented.

C. Normal Force

The normal force coefficients were measured over a wide range of angles of attack, sideslip angles, elevator deflections, rotational velocities, and pitch rates during forced oscillations. Data from these measurements were analyzed to determine the model structural dependencies and to insure the preservation of all nonlinear effects. The initial definition of the basic force model \(C_{N\text{BASE}}\) was built from the most significant functional dependencies. For the Twin Otter these were angle of attack, angle of sideslip, and flap deflection. Incremental coefficient data tables were then generated to provide the effects of control deflections, dynamic damping, and power effects. The normal force coefficient can be represented by Eq. (1). The \(C_{N\text{BASE}}\) lookup table is based on static inputs of \(\alpha, \beta, \delta_r\); the \(\Delta C_{N\text{ROT}}\) lookup table of increments of \(C_N\) is based on inputs of \(\alpha, \Omega b/2V \times \text{SGN}(\beta), |\beta|, \delta_f\). The \(\Delta C_{N\text{DE}}\) lookup table of increments of \(C_N\) is based on static inputs \(\alpha, \delta_e, \delta_r\). Lastly, the \(\Delta C_{N_{\text{f}}}\) lookup table of increments of \(C_N\) is based on inputs \(\alpha, q\vec{c}/2V, \delta_f\). The result from each of these lookup tables is added to arrive at the total normal force coefficient.

1. Normal Force Coefficient Model for No-Ice Baseline

\[
C_{N_{\text{TOTAL,BASIC}}} = C_{N\text{BASE}}(\alpha, \beta, \delta_r) + \Delta C_{N\text{ROT}}(\alpha, \Omega b/2V \times \text{SGN}(\beta), |\beta|, \delta_f) + \Delta C_{N\text{DE}}(\alpha, \delta_e, \delta_r)
\]

(1)

where \(\text{SGN}(\beta) = \pm 1\) depending on the sign \((\pm)\) of \(\beta\). The differences in the no-ice and ICE02 (IPS failure ice on wing, horizontal and vertical tail) data sets drove the modeling effort to create separate databases for each configuration. Equation (2) shows that the model structure for ICE02 is the same as the no ice, but the values within the tables are different.

2. Normal Force Coefficient Model for All-Iced (ICE02)

\[
C_{N_{\text{TOTAL,ICE02}}} = C_{N\text{BASE,ICE02}}(\alpha, \beta, \delta_r) + \Delta C_{N\text{ROT,ICE02}}(\alpha, \Omega b/2V \times \text{SGN}(\beta), |\beta|, \delta_f) + \Delta C_{N\text{DE,ICE02}}(\alpha, \delta_e, \delta_r)
\]

(2)

As an example of the \(C_{N\text{BASE}}\) lookup tables, the normal force coefficient data for the Twin Otter with flaps at 0, 20, and 40 deg are presented in Fig. 15 for the no-ice baseline and the ICE02 configurations. Comparing these results, the effect of ice on the normal force is observed mostly at the angle of attack near stall, where there is a reduction in the maximum normal force for all flap settings. This effect is most pronounced with the flaps setting of \(\delta_f = 20\). The reduced normal force is similar to findings with 2-D airfoil research, but note that the stall break and post-stall character is similar to the no-ice baseline. This small change is due to the rather benign stall characteristics of the Twin Otter wing and the size and shape of the wing ice tested.

D. Pitching Moment

As with the normal force, the pitching moment coefficient data were measured over a wide range of angles of attack, sideslip angles, elevator deflections, rotational velocities, and pitch rates during forced oscillations. Data from these measurements were tabulated into five databases so that the pitching moment coefficient can be represented by Eq. (3). Similar to the \(C_N\) equations, there is a corollary equation and set of lookup tables for the ICE02 configuration. There is an additional term in the \(C_m\) equation for the thrust effects: \(\Delta C_{m\text{THR}}\). This database was developed using existing NASA Twin Otter flight data.
1. Pitching Moment Coefficient Model for No-Ice Baseline

\[ C_{\text{m TOTAL CLEAN}} = C_{\text{m BASIC}}(\alpha, \beta, \delta_f) + \Delta C_{\text{m ICE}}(\alpha, \Omega b / 2V) \times \text{SGN}(\delta_f) \cdot |\beta| \cdot \delta_f + \Delta C_{\text{m}e}(\alpha, \delta_e, \delta_f) \]

\[ + \Delta C_{\text{m}q}(\alpha, q\delta_e / 2V, \delta_f) + \Delta C_{\text{m}C_T}(\alpha, C_T, \delta_f) \]  

As an example of the \( C_{\text{m BASIC}} \) databases, the pitching moment coefficient data for the Twin Otter with flaps at 0, 20, and 40 deg are presented in Fig. 16 for the no-ice baseline and the ICE02 configurations. The effect that ice has is influenced by the flap deflection \( \delta_f \). With \( \delta_f = 0 \) deg, there is a general positive shift in \( C_m \) for \( \text{AoA} > -7 \) deg, indicating the download from the horizontal tail is reduced for the given elevator deflection. Also, the static longitudinal stability \( (C_{\text{m}e}) \) is reduced significantly for \( \text{AoA} < -7 \) deg, indicating longitudinal instability at this range. With \( \delta_f = 20 \) and 40 deg, the differences caused by the ice are insignificant in the linear range, but reduced static longitudinal stability occurs for \( \text{AoA} > 8 \) deg and for \( \text{AoA} < -4 \) deg. The wing ice causes the reduced \( C_{\text{m}e} \) at positive AoA, whereas the ice on the horizontal tail reduced the \( C_{\text{m}e} \) at the negative AoA.

To illustrate the data in the \( \Delta C_{\text{m ICE}} \) lookup tables, Fig. 17 is provided. Overall, the elevator is effective in creating proper pitching moments throughout the AoA range with or without ice. However, the ice does reduce the amount of pitching moment affected by the elevator in the \(-10 < \text{AoA} < 10 \) deg range. This means that larger elevator deflections are required to trim the iced aircraft. One thing to note is this effect is more pronounced with greater flap deflections. As flaps are deflected, the inflow angles at the horizontal tail increase causing separation bubbles to extend and reducing the effectiveness of the elevator. As seen in Fig. 18, the effect of the ice is greater in the \( \delta_f = 40 \) case and extends to lower angles of attack than when the flaps are not deflected.

E. Model Equations for Remaining Force and Moments

For completeness, the remaining force and moment equation models for the no-ice baseline Twin Otter are shown below in Eqs. (4–7). Like the normal force and pitching moments, each of these equations has identical model structure for the iced case but different values within the lookup tables.

1. Axial Force Coefficient Model for No-Ice Baseline

\[ C_{\text{A TOTAL CLEAN}} = C_{\text{A BASIC}}(\alpha, \beta, \delta_f) + \Delta C_{\text{A}q}(\alpha, \delta_e, \delta_f) \]

\[ + \Delta C_{\text{A}C_T}(\alpha, q\delta_e / 2V, \delta_f) + \Delta C_{\text{A}C_T}(\alpha, C_T, \delta_f) \]  

Fig. 12 Full-scale ice-shape profiles for Twin Otter wing, horizontal tail and vertical tail.

Fig. 13 Full-scale, 41.7%-scale, and 8.3%-scale business jet wing panel models.
PC-based simulation environment that fully supported both the Twin Otter and Cessna business jet simulation models development, as well as the analysis and validation activities.

One key objective of these research efforts was to enable real-time, pilot-in-the-loop simulations to demonstrate icing effects on flight dynamics to pilots and engineers. D-Six provided the simulation environment to accomplish this because it permits the dynamic linking of other object modules that can control everything from the simulation integration scheme to external graphics and network communications with no requirement to edit the source code. Pilot-in-the-loop simulations will be further discussed in the Using Flight Simulation Models V. Subsection.

B. Validating Flight Simulation Models

New flight test data were required to validate the flight simulation models. For the Twin Otter, a flight test program was conducted with the no-ice baseline, artificial ice on the horizontal tail only (ICE01 configuration), and artificial ice on the wing, horizontal tail and vertical tail (ICE02 configuration) [24]. Flight test maneuvers included control doublets, idle-power stalls, steady-heading sideslips, thrust transitions, throttle sweep, wind up turns, and simulated approach and missed approach.

Flight data from these maneuvers were then imported into D-Six for analysis and validation of the simulation models. A validation tool called Overdrive enabled the validation of the simulation aerodynamic database against flight-extracted data using the process illustrated in Fig. 19. At each time slice, Overdrive extracts aerodynamic moment coefficients from the flight-recorded time histories, as shown on the right side of Fig. 19. Angular rates are numerically differentiated to obtain the angular acceleration of the vehicle. After the removal of the inertial effects, the remainder is nondimensionalized to generate the aerodynamic force and moment coefficients experienced during flight.

![Fig. 15 Twin Otter normal force coefficient for various flap settings with no-ice baseline and ICE02 configurations.](image)

![Fig. 16 Twin Otter pitching moment coefficient for various flap settings with no-ice baseline and ICE02 configurations.](image)
At each time step, flight-recorded states, such as angle of attack, angle of sideslip, control surface positions, etc., are used to exercise the aerodynamic model in accordance with the aerodynamic model specification discussed previously. Each aerodynamic model element (i.e., pitching moment due to elevator, etc.) is stored and summed as prescribed in the aerodynamic model. By over-plotting the model predicted coefficients with the flight-extracted total coefficients (Fig. 20), differences can be easily identified. Correlating the discrepancies with the excitation of the individual elements and parameters from the flight time history aids in isolating potential weaknesses in the aerodynamic model.

Overdrive was used with the Twin Otter flight data to validate the models. The validation effort was reported on [25] but is currently not published.

C. Using Flight Simulation Models

One key objective of these research efforts was to enable real-time, pilot-in-the-loop simulations to demonstrate icing effects on flight dynamics to pilots and engineers. Although the simulation models could be run on a laptop or desktop PC, a portable flight training device called the Ice Contamination Effects Flight Training Device (ICEFTD) (Fig. 21) was developed to be a more effective tool [26].

The ICEFTD consists of a raised platform and framework that supports a pilot seat, a control yoke, rudder pedals, a twin turbo-prop throttle quadrant, a flap selector, three flat-panel monitors for out-the-window graphics, and two additional flat-panel monitors for instrument panel graphics. The control column is connected to a programmable loader for longitudinal force feedback, whereas the yoke (lateral) and rudder pedals force gradients are provided by spring resistance. Two PCs using D-Six host the simulation models and control the graphics. A third PC, the control loading computer (CLC), controls the electromechanical loader to simulate representative column forces. These PCs are mounted under the floor of the device, and the control loader device is mounted to the frame forward of the pilot’s feet. A curtain surrounds the ICEFTD to isolate the pilot from external visual distractions. The design is well suited for mobility and usability at various settings, from labs or offices to class rooms or hangars.

Both the Twin Otter and Cessna business jet flight models have been implemented on the ICEFTD and were used for pilot education and training, as well as pilot evaluations of the simulation models. The ICEFTD has been used to demonstrate icing effects on Twin Otter flight dynamics to over 150 pilots at seminars and short courses held by the University of Tennessee Space Institute, National Test Pilot School, Flight Safety International, and several conference exhibits [27]. The ICEFTD was also used in conjunction with the

![Fig. 17 Twin Otter pitching moment coefficient increment for no-ice baseline and ICE02 due to elevator deflection (δe = 0).](image)

![Fig. 18 Twin Otter pitching moment coefficient increment for no-ice baseline and ICE02 due to elevator deflection (δe = 40).](image)

![Fig. 19 Overdrive process diagram.](image)
flight model validation flight tests of the Cessna business jet [28]. Simulator sessions were conducted before the flight tests to identify anomalous flight characteristics that were predicted by the simulator. After the flight tests and flight model updates based on the new flight records, Cessna flight test pilots reevaluated the simulation models on the ICEFTD. For both airplane types, pilots could readily see the changes in performance, stall characteristics, and the increased workload to recover from the stall with the iced airplane.

VI. Future Directions

As described earlier, there is a large assortment of ice shapes possible for any aircraft, each having a range of effects on the aerodynamics of individual wings, fuselage, empennage, and other surfaces. More important, these ice shapes have a wide range of effects on the aerodynamics of the aircraft as an integrated machine–human system. The research with iced 2-D airfoils has helped reduce the scope of ice shapes that need to be considered by identifying key ice-shape features and the resulting flowfields. Similar research efforts are needed with 3-D wings and tails with control surfaces to determine if 3-D ice features such as scallops need to be considered as part of the so-called critical ice shapes.

Regarding icing effects on flight dynamics, the research efforts with the Twin Otter and business jet simulation models are an excellent start in that they have provided a method to develop and validate icing effects simulation models. These flight simulation models and the flight training device are valuable resources for additional research into icing effects on flight dynamics, pilot education, and future flight training simulator requirements. But the knowledge gained through the efforts with the Twin Otter and business jet cannot be applied across the entire spectrum of aircraft. Further efforts are needed to identify icing effects on other classes of aircraft, such as regional jets, large transports, and future designs such as blended wing body.

Understanding these needs, NASA is currently using the Twin Otter flight simulation models to develop and test new methods for identifying icing effects in real time to provide envelope protection to avoid loss of control. This effort is being conducted through a NASA Research Announcement (NRA) with the University of Tennessee Space Institute and Bihrle Applied Research, Inc. NASA is also initiating a new icing effects simulation activity using the NASA Langley Research Center Generic Transport Model (GTM). A significant database has already been developed using a generic twin-engine large transport model configuration to develop recovery strategies from loss of control events. To date, the emphasis of the effort has been on damaged aircraft or failure conditions, such as a rudder hardover. The new icing effects effort will provide another scenario under which loss of control can occur. Flight simulation models will be developed from this database and used in conjunction with adaptive control methods development and testing.

VII. Conclusions

The general effects of icing on aerodynamics are increased drag, reduced stall angle of attack and maximum lift, and altered pressure distribution over the airfoil surface. In addition, the stall break and post-stall characteristics can be dramatically different in the iced
cases when compared with the no-ice baseline. These aerodynamic effects have been studied using 2-D airfoil sections and much has been learned regarding ice-shape features and the associated flowfields that result in these performance degradations.

To understand the integrated effects of icing on aircraft performance, stability, and control research has been conducted using subscale complete aircraft models. From this research, flight simulation models were developed that incorporate the nonlinear nature of icing effects on the forces and moments along all three axes. These flight models can be implemented into piloted flight simulators for pilot evaluation and loss of control recovery strategies.

Significant progress has been made in this area of icing flight dynamics research, but the knowledge gained with the limited number of models may not be applicable to other airplane configurations. Additional research efforts using other airplane models are needed to extend our current understanding of icing flight dynamics.

References