# Variable-Speed Power-Turbine for the Large Civil Tilt Rotor 

Mark Suchezky and G. Scott Cruzen

Williams International Co. LLC

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Prepared under Contract NNC10BA15B

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This report contains preliminary findings, subject to revision as analysis proceeds.

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### 1.0 Introduction

The Large Civil Tilt-Rotor (LCTR) is part of NASA’s Heavy Lift Systems Investigation. This proposed 90 passenger aircraft would offload short to medium range air traffic from large airports and/or runways. Due to its vertical takeoff and landing capability, only a helipad would be needed within existing airport infrastructure (Figure 1.1).

The proposed vehicle has four turbo-shaft engines powering two rotors. Each engine is to develop $7,500 \mathrm{hp}$ for a total 30,000 hp. The mission would require high rotor rpm at sea level take off ( $650 \mathrm{ft} / \mathrm{s}$ tip speed) and significantly lower rpm at cruise ( $350 \mathrm{ft} / \mathrm{s}$ tip speed) (Ref. 1). That is, the cruise rpm of the main rotors is 54 percent of the SLTO rpm. This requirement comes from the fact that the main rotors are more efficient at low rpm during the altitude cruise but require high rpm during sea level take-off (SLTO). The turboshaft engines will drive the main rotors through a gearbox enabling the high rpm power turbines (PT) to spin the low rpm (103 to 191 rpm ) main rotors. Each main rotor is driven by two engines. There are two possible methods for achieving the required rpm sweep.

1. Two (or higher) gear-ratio transmission: with the power turbine operating at near constant rpm.
2. Fixed gear-ratio transmission: with the power turbine experiencing the full 54 to 100 percent speed range.

For method 1, the complexity of designing a flight weight, $15,000 \mathrm{hp}$ transmission (two engines X $7,500 \mathrm{hp}$ each), while obtaining high life and reliability is a formidable task. The method for changing gears (ex. torque converter, clutch, etc.) would also need to be addressed. This method is not within the scope of this study and will not be further considered.


Figure 1.1—NASA LCTR Concept

## Nomenclature

| $\mathrm{AN}^{2}$ | See Appendix B |
| :--- | :--- |
| $\mathrm{Cm} / \mathrm{U}$ | Flow Coefficient |
| $\mathrm{Cx} / \mathrm{U}$ | Flow Coefficient |
| $\Delta \mathrm{h}_{0} / \mathrm{U}^{2}$ | Work Coefficient |
| FOM | Figure of Merit |
| $\mathrm{h}_{0}$ | Total Enthalpy |
| LCTR | Large Civil Tilt-Rotor |
| LE | Leading Edge |
| $\eta$ | Efficiency (see Appendix G) |
| NPSS | Numerical Propulsion System Simulator |
| PT | Power Turbine |
| SLTO | Sea Level Take Off |
| TE | Trailing Edge |
| U | Wheel Speed (usually associated with midspan) |
| VSPT | Variable Speed Power Turbine |

### 2.0 VSPT Concept Development

### 2.1 Figure of Merit

In this study various techniques are investigated to improve efficiency and off-design characteristics of a power turbine operating in the LCTR mission. The relative performance of each design modification needs to be assessed using some form of figure of merit (FOM). The FOM chosen for this study is overall fuel burn during the mission. The overall mission profile is not well established at this time so a fictitious but representative mission needs to be assumed. Based on the work of Snyder and Thurman (Ref. 1), a study engine simulation was generated using the Numerical Propulsion System Simulator (NPSS). This simulation software has the ability to predict engine performance throughout the flight envelope based on performance maps of the individual engine components. Four output points were generated from this model and made available for this study. These four flight conditions are:

Point 1
SLTO; 100\% PT Speed, 100ft, 0.0 Mach, Std. Day
Point 2
Climb; 100\% PT Speed, 2,000ft 0.0 Mach $+45^{\circ} \mathrm{F}$
Point 3
Start Cruise; $100 \%$ PT Speed $\quad 28,000 \mathrm{ft} \quad 0.51$ Mach $\quad$ Std. Day
Point 4
Cruise; $\quad 54 \%$ PT Speed $\quad 28,000 \mathrm{ft} \quad 0.51$ Mach $\quad$ Std. Day

A detailed output from the NPSS cycle model is included in Appendix A. These four points are the only points currently available from the model and therefore a mission made up of only these four points was assumed. The actual mission will deviate significantly from this mission, but this mission is used as a starting point (Table 2.1).

This mission was made to mimic the mission shown in Figure 2.1, provided by C. Sndyer of NASA at contract start.

TABLE 2.1-LCTR MISSION SEGMENTS

| Point | Description | $\Delta$ time | Cycle PT | Power | Wf | PT | Fuel Burned |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Minutes | ETA | hp | Ibm/hr | Speed | Ibm |  |
| 1 | SLTO;100\% PT Speed,100ft,0.0 Mach, Std. Day | 2 | 0.85 | 7500 | 2581.28 | 100.0\% | 86.0 |  |
| 2 | Climb;100\% PT Speed, $2,000 \mathrm{ft0} 0.0 \mathrm{Mach}+45^{\circ} \mathrm{F}$ | 2 | 0.8266 | 4639.6 | 1761.6 | 100.0\% | 58.7 |  |
| 3 | Start Cruise;100\% PT Speed 28,000ft 0.51Mach Std. Day | 30 | 0.8485 | 2651.5 | 836.01 | 100.0\% | 418.0 |  |
| 4 | Cruise;54\% PT Speed 28,000ft 0.51 Mach Std. Day | 180 | 0.7859 | 2345.4 | 805.23 | 54.0\% | 2415.7 |  |
| 3 | Start Cruise;100\% PT Speed 28,000ft 0.51Mach Std. Day | 30 | 0.8485 | 2651.5 | 836.01 | 100.0\% | 418.0 |  |
| 2 | Climb;100\% PT Speed, $2,000 \mathrm{ft0} 0.0 \mathrm{Mach}+45^{\circ} \mathrm{F}$ | 2 | 0.8266 | 4639.6 | 1761.6 | 100.0\% | 58.7 |  |
|  | TOTALS | $\begin{aligned} & 246 \\ & \text {-or- } \end{aligned}$ | Minutes |  |  |  | 3455.2 | lbm |
|  |  | $\begin{aligned} & 4 \\ & 6 \\ & \hline \end{aligned}$ | hours minutes |  |  |  |  |  |

## LCTR Mission Profile ("similar" to Regional aircraft)



Engines and transmission were sized for the most demanding of Category A OEI takeoff or landing segments at 5,000 feet pressure altitude, ISA $\mathbf{+ 2 0 ^ { \circ }} \mathrm{C}$ or 2,000 feet, ISA $+25^{\circ} \mathrm{C}$.

## Mission fuel is cruise-dominated. <br> Propulsion system weight and overall fuel efficiency are critical.

| LCTR Mission and Engine Analysis, Sept 2010 | Subsoric Rotary Wing Project | www.nasa.gov |
| :--- | :--- | :--- |

Figure 2.1.—LCTR Mission Profile
Unfortunately, cycle points such as idle and taxi were not available to use in this cycle so there is some error introduced. The mission used in this study (Table 2.1) includes a long cruise segment of 3 hr with $1 / 2 \mathrm{hr}$ of climb condition before and after. There is also some high power SLTO time at the beginning and end of the mission to simulate vertical takeoff and landing.

Given the cycle predicted fuel burns at each condition and the assumed duration of each segment, the fuel burned can be integrated. (Eq. (1))

$$
\begin{equation*}
\mathrm{W}_{\text {fuel }}=\sum_{\text {seg }=1}^{\text {nseg }} \dot{\mathrm{W}}_{\text {fuel }} \times \Delta \text { Time } \tag{1}
\end{equation*}
$$

Table 2.1 shows that the predicted fuel burn would be 3455.2 lbm of fuel per engine over the 4 hr and 6 min flight. Because all of the power to drive the main rotors comes from the power turbine, the fuel burn at any condition will be proportional to PT efficiency. Therefore we can evaluate the impact of predicted PT efficiencies ( $\eta_{\text {PT }}$ ) throughout the mission by scaling the fuel flows by the ratio of predicted $\eta_{\text {PT }}$ to cycle $\eta_{\text {PT. }}$.

$$
\begin{equation*}
\mathrm{W}_{\text {fuel }}=\sum_{\text {seg }=1}^{\text {nseg }} \frac{\eta_{\text {predicted }}}{\eta_{\text {cycle }}} \dot{\mathrm{W}}_{\text {fuel }} \times \Delta \text { Time } \tag{2}
\end{equation*}
$$

Using this technique, a prediction for $\eta_{\text {PT }}$ can be input into Equation (2) for each of the four cycle points and an overall mission fuel burn can be calculated. Comparing the new predicted fuel burn back to the cycle prediction ( 3455.2 lbm ) yields the FOM used in this study.

### 2.2 Efficiency Prediction Technique

Efficiency predictions are made by the use of a 'meanline' analysis. The meanline used is proprietary to Williams International and is referred to as 'MeanTurb'. MeanTurb is a row by row analysis tool that tracks the mean particle through each airfoil row. All three components of velocity are modeled which makes the tool very general and can be used for axial, mixed flow, or radial turbines. The velocity triangles are solved with the loss system, cooling flows (if applicable), gas properties, and seal leakages all converged simultaneously. The solution technique is to solve each blade row independently and then use small-change effects (Jacobian matrix) and Newton's Method to close on continuity, angular momentum, and energy. The loss system used in this study is a combination of various public domain loss systems (Kacker and Okapuu (Ref. 4) and Moustapha, Kacker and Tremblay (Ref. 5)) with modifications based on Williams International experience.

The technique used to predict turbine efficiency is two parts. The first part is referred to as 'design mode'. In this phase a simpler design-mode meanline called "Falcon" is used. This meanline is different from MeanTurb in that you specify mass-flow, power, pressure reaction and airfoil loading coefficient (Zweifel). The velocity triangles are calculated using nearly the same loss system as MeanTurb with several simplifying assumptions. Falcon is wrapped with a graphical user interface which allows for intuitive design as well as optimization functionality. Figure 2.2 is a screen shot of the interface.


Figure 2.2—Falcon Meanline Code Interface

The second part of the efficiency prediction process begins after a satisfactory design has been produced in Falcon. Falcon writes out an off-design input file for MeanTurb. At this point the geometry is assumed fixed and parameters such as power, work split, reaction, mass-flow and efficiency are outputs of MeanTurb. One important point in this study is that the LE metal angles are assumed fixed so the impact of off-incidence design is captured in the MeanTurb calculations.

### 2.3 Structural Constraints

The 100 percent speed condition must be structurally viable. This study used aggressive $\mathrm{AN}^{2}$ and Rim Speed limits of $60 . \mathrm{E} 9 \mathrm{in}^{2} \cdot \mathrm{rpm}^{2}$ and $1200 \mathrm{ft} / \mathrm{s}$ respectively as upper limits. (See Appendix B for definitions.) The most challenging structural design will be the last stage blade which will have the largest span and highest pull stress. Fortunately it is also the coolest airfoil which aids in creep rupture life. Although challenging, these limits should be achievable for a long life application. After designing several flowpaths to this criterion, a sanity check calculation was performed. A meanline analysis was run for Point 1 (the hottest and fastest of the four performance conditions used) with the inlet temperature raised by $100^{\circ} \mathrm{F}$ to simulate deterioration and hot day operation. The average blade pull-stress was estimated at 68 ksi and metal temperature at $1190{ }^{\circ} \mathrm{F}$. Based on proprietary material databases, there are several commercially available alloys capable of $>20,000 \mathrm{hr}$ of useful life at these conditions. Over-speed protection in the event of a gearbox or coupling failure has not been addressed. It is possible that failure analysis may require more structural conservatism.

### 2.4 Exhaust Constraint

Choosing the exit annulus area determines the exit Mach number from the turbine (last blade, absolute frame of reference). The four cycle points given have nozzle (tail pipe) exit Mach numbers of about 0.27 . This very low exit Mach number corresponds to a design philosophy of extracting as much energy out of the power turbine as possible and achieving nearly no thrust from the nozzle. Achieving such low exit Mach numbers at the exit of a gas turbine is difficult and results in large, heavy turbines operating at low rpm. It is more advantageous to design to an exit Mach number of .4 to .55 and diffuse through the exhaust system. For the purposes of this study, Mach numbers in this range will be used. In a more formal detailed design, a trade study between nozzle exit Mach number, turbine weight, exhaust system weight and fuel burn should be performed to find the best overall system trade.

It can be shown that the combination of the structural and exhaust constraints sets the turbine rpm and the last stage flowpath. That is: picking a Mach number exiting the turbine sets the turbine exit annulus area because of continuity (although swirl angle and boundary layer blockage play a role). Then, with $\mathrm{AN}^{2}$ already chosen, the rpm falls out. (See Appendix B for more information)

$$
\begin{align*}
& \text { A = function(PT, TT, Mdot, Mach, Swirl) }  \tag{3}\\
& \qquad \operatorname{rpm}=\sqrt{\frac{\mathrm{AN}^{2}}{\mathrm{~A}}} \tag{4}
\end{align*}
$$

The Rim Speed can be used to calculate the last blade trailing edge hub radius:

$$
\begin{equation*}
\operatorname{Rim}_{\text {Speed(ft/s) }}=\text { Radius }_{\text {Hub }}(\mathrm{in} .) / 12 . * \text { rpm } * \pi / 30 . \tag{5}
\end{equation*}
$$

Then the trailing edge tip radius can be determined by the annulus area.

$$
\begin{equation*}
\text { Radius }_{\text {Tip }}=\sqrt{\frac{\mathrm{A}}{\pi}+\text { Radius }_{\text {Hub }}^{2}} \tag{6}
\end{equation*}
$$

From the above relations it is clear that selecting structural criteria and an exit Mach number uniquely defines the exit of the turbine and the rpm. In a more detailed engine design exercise, the front of the power turbine would need to mate to the exit of the previous turbine which would further define the
flowpath. In this work, no special attention is given to the proceeding turbine. Detailed design of the overall turbine section is out of scope.

### 2.5 List of Analytical Studies

Several analytical studies have been performed to gain confidence and reduce risk in designing a power turbine capable of nearly a 2 X speed variation while maintaining acceptable efficiency levels.

1. Flow Path Selection
a. CX/U
b. Work Coefficient
c. Number of Stages
2. Loss System Validation via CFD
3. Incidence Tolerant Design
a. LE Shape
b. Airfoil Thickness

### 2.6 Flow Path Selection: Cx/U

Turbine Flow Coefficient, commonly referred to as $\mathrm{Cx} / \mathrm{U}$, is the ratio of through-flow velocity to mean wheel speed. Often $\mathrm{Cx} / \mathrm{U}$ is referred to as axial velocity over wheel speed but in this study the radial velocity is taken into account. The meridional velocity is used instead and defined as:

$$
\begin{equation*}
\mathrm{V}_{\text {meridional }} \equiv \sqrt{\mathrm{V}_{\mathrm{axial}}^{2}+\mathrm{V}_{\text {radial }}^{2}} \tag{7}
\end{equation*}
$$

For the purposes of this study, $\mathrm{Cx} / \mathrm{U}$ and $\mathrm{Cm} / \mathrm{U}$ will be used synonymously and is defined as:

$$
\begin{equation*}
\mathrm{Cm} / \mathrm{U}=\mathrm{Cx} / \mathrm{U} \equiv \frac{\sqrt{V_{\text {axial }}^{2}+V_{\text {radial }}^{2}}}{\omega \overline{\mathrm{r}}} \tag{8}
\end{equation*}
$$

where:
all values are calculated at the TE plane of the turbine blade
$\bar{r}$ equals the average of the hub and tip radius of the blade TE
The Flow Coefficient, $\mathrm{Cx} / \mathrm{U}$ is a good indicator of the velocity triangles. Low $\mathrm{Cx} / \mathrm{U}$ designs are characterized by high turning and relatively low velocity whereas high $\mathrm{Cx} / \mathrm{U}$ designs tend towards low turning (camber) and higher velocities. The airfoil shapes can be dramatically different as shown in Figure 2.3.

The off-incidence loss generated at the LE of an airfoil is a function of two factors: 1) Loss Coefficient and 2) Inlet dynamic head. Low CX/U designs have lower LE Mach number but higher swings in incidence. High CX/U designs have lower excursions in incidence but always operate at higher inlet Mach number. Therefore it is reasonable to assume that there is an optimum CX/U for off incidence performance. Figure 2.4 and Figure 2.5 show a simplified example of velocity triangle for Low versus High CX/U designs.

For the VSPT, the corrected speed variation is from 54 to 100 percent. This implies that the wheel speed (U) varies from 54 to 100 percent but velocity triangle analysis shows that the Cx is nearly constant. Therefore, CX/U is approximately inversely proportional to speed.

Two flowpaths were generated to look at the impact of CX/U on mission fuel burn. The design philosophy was to follow the structural and exhaust constraints as given in the previous section and build turbine flowpaths that have good cruise velocity triangles and airfoil loadings. Once the flowpaths are established, MeanTurb is run to investigate the off design characteristics. Very good cruise performance ( $>90$ percent) is achieved with four stage turbines. See Figure 2.6.


Figure 2.3.—Airfoil Shapes


Figure 2.4.—Low CXIU Design Velocity Triangles


Figure 2.5—High CXIU Design Velocity Triangles


Figure 2.6.-Comparison of High and Low CX/U Flowpaths

If the turbines in Figure 2.6 were designed for the low speed cruise condition ( 54 percent speed), they would have predicted efficiencies of 91.4 and 90.2 percent respectively when operating at that design point. Unfortunately, each of these turbines is predicted to have an efficiency of 69.3 percent when operating at the high speed cruise condition ( 100 percent speed). Likewise, if the two turbines were designed for the 100 percent speed condition, the efficiencies would be 92.8 and 91.4 percent respectively. These turbines both would have very low efficiencies (<58 percent) when operating at the 54 percent speed conditions. Of course, these off-design efficiency predictions are highly dependent on the empirical loss system used in the meanline prediction system. Nonetheless, a compromised design point somewhere between 54 and 100 percent would most likely be a good compromise. A method for determining the optimal design point was developed. Four design speeds were chosen: 54, 69, 85 and 100 percent speed. A preliminary design was produced for each of these turbines at each of these speeds. This preliminary design process sets the LE metal angles and blade counts for the velocity triangles corresponding to that speed. Each of these designs was then run off-design using MeanTurb to the four different mission points in order to predict the efficiency. The resulting efficiencies are available in Table 2.2. For each of these designs, the resulting efficiencies for points $1,2,3$, and 4 were used in Equation (2) (via spread sheet) and the overall impact to mission fuel burn was calculated, the results of which are also included in Table 2.2.

The results of Table 2.2 are plotted in Figure 2.7. From this plot, the best design practice is to pick a design point that is compromised between the low speed and high speed cruise but favoring the low speed cruise condition. An unexpected outcome of this study is the fact that both the High CX/U design and the Low CX/U design optimize at about the same speed and result in about the same overall fuel burn. Neither design philosophy appears to have an advantage. There is no compelling evidence from this study that CX/U (in of itself) is a determining factor in the design of this type of turbine.

TABLE 2.2.-FUEL BURN COMPARISON FOR HIGH AND LOW CX/U DESIGNS High CXIU

| \% Speed | Design RPM | Fuel Burn\% | ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 53.8 | 8045 | -3.29 | 73.34 | 68.62 | 69.34 | 91.39 |
| 69.2 | 10343 | -7.88 | 88.33 | 84.71 | 84.12 | 88.62 |
| 84.6 | 12642 | 1.41 | 92.95 | 90.84 | 90.63 | 74.87 |
| 100.0 | 14941 | 23.20 | 91.25 | 91.58 | 92.80 | 57.42 |

Low CXIU

| \% Speed | Design RPM | Fuel Burn\% | ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 53.8 | 8045 | -2.22 | 69.98 | 66.62 | 69.30 | 90.20 |
| 69.2 | 10343 | -7.80 | 87.58 | 83.60 | 82.85 | 89.14 |
| 84.6 | 12642 | -1.84 | 92.00 | 89.60 | 89.44 | 78.75 |
| 100.0 | 14941 | 24.30 | 89.29 | 89.78 | 91.43 | 57.00 |



Figure 2.7.—Design Speed Selection for High and Low CX/U Designs

### 2.7 Work Coefficient

The Work Coefficient $\left(\Delta \mathrm{h}_{0} / \mathrm{U}^{2}\right)$ is a dimensionless parameter relating the turbine work to the mean wheel speed of the turbine. The use of Work Coefficient (Wcoeff) combined with Flow Coefficient ( $\mathrm{Cx} / \mathrm{U}$ ) was popularized by Smith (Ref. 6) with his correlation of turbine efficiency using both parameters. Smith showed that there was an optimum relationship between the two parameters. There is no indication that Smith's 1965 correlation considered turbines operating far off-design so it is not obvious whether his correlation is helpful in determining optimum velocity triangles for the LCTR power turbine application when operating at its full range of speeds. The Smith correlation was presented (Ref. 6) as a plot and Figure 2.8 is a reproduction produced by digitizing the figure in his paper.

Assuming the LCTR power turbine is designed at the 54 percent cruise condition, then as the turbine transitions from 54 to 100 percent speed, the Flow Coefficient $(\mathrm{Cx} / \mathrm{U})$ and Work Coefficient $\left(\Delta \mathrm{h}_{0} / \mathrm{U}^{2}\right)$ change considerably. MeanLine and cycle analysis confirm that $\Delta \mathrm{h}_{0} / \mathrm{U}^{2}$ is nearly proportional to $1 / \mathrm{rpm}^{2}$ and $C x / U$ is nearly proportional to $1 / \mathrm{rpm}$. Therefore the Wcoeff increases by $1 / .54^{2}$ or 3.4 times when the rotor speed drops from 100 to 54 percent rpm. Likewise the $\mathrm{Cx} / \mathrm{U}$ increases by a corresponding factor of $1 / .54$ or 1.85. If Smith's correlation indicates optimum relationships between these two parameters, it is reasonable to assume that it may provide some guidance in designing a turbine that transitions over a large swing in these parameters. The two turbines in the $\mathrm{Cx} / \mathrm{U}$ study were placed on the Smith correlation in Figure 2.9.

## Smith Correlation



Figure 2.8.-Work Coefficient Versus Flow Coefficient


Figure 2.9.-Work Coefficient Versus Flow Coefficient


Figure 2.10.-Comparison of Three Stage and Four Stage Turbine Flowpaths
From this plot, the high $\mathrm{Cx} / \mathrm{U}$ flowpath is shown to transition through the heart of the efficiency islands while the low $\mathrm{Cx} / \mathrm{U}$ is in a non-optimum part of the correlation.

Both flowpaths developed in the $\mathrm{Cx} / \mathrm{U}$ study have similar Work Coefficients which drop to very low levels when the rotor rpm is at 100 percent. These low levels are outside of normal gas turbine design experience. Another study was conducted to investigate the impact of running to higher Work coefficients in order to assure operation within the traditional design space. A new flowpath was generated by removing the first stage but holding the same rpm and about the same overall radius of the last three stages. This Three Stage turbine has the same power and speed as the two four stage turbines already analyzed but the average work per stage is higher (by the ratio of $4 / 3$ ). Figure 2.10 compares the Three Stage turbine with the High $\mathrm{Cx} / \mathrm{U}$ four stage design from the previous study.

The same process of picking four design speeds, calculating efficiency at each of the four mission points, and integrating the fuel burn across the mission was performed with the Three Stage design. Table 2.3 documents the results and Figure 2.11 plots the Three Stage turbine results against the results of the Four Stage $\mathrm{Cx} / \mathrm{U}$ study.

The Three Stage does not show a predicted improvement in overall fuel burn relative to the lower work four stage designs, but it does show a significantly different trend. Figure 2.11 shows that the Three stage turbine is more forgiving than any of the Four Stage designs in choosing the design speed. It also indicates that the optimal design speed is closer to the SLTO rpm which is different than the previous two designs and is not the expected result. In Figure 2.12, the Three Stage turbine is shown on the Smith Correlation compared to the two Four Stage designs. The Three Stage falls between the two Four Stage designs. If the Smith Correlation were a good indicator of off-design capability, then it could be expected that the Three Stage design would have off-design performance characteristics between the two Four Stage designs: which it clearly does not.

The large difference in character between the Three Stage and Four Stage designs begs the question as to what makes the Three Stage so different. The difference in Work Coefficient appears to have played
a significant role. At 54 percent speed, the Work coefficient of the Three Stage turbine is about 2.1 which is well within design experience. Designing to higher Work Coefficient may further improve performance. Higher Work Coefficients are generally more challenging to design because they result in higher airfoil turnings and Mach numbers. The practical limit is approximately 3.0, above which the design becomes very challenging. To assess whether higher Work Coefficient is better for overall mission fuel burn, a High Work Four Stage turbine was designed (Figure 2.13). The Work Coefficient at the 54 percent cruise speed was set at 2.83 and the Flow Coefficient was set to 1.0 in an attempt to stay in the center of the Smith Correlation. After the same process of picking four design speeds, calculating efficiencies, and integrating mission fuel burn, this design proved to be the best out of a total of 8 flowpaths that were examined (Table 2.4). The flowpath is reduced in radius relative to the designs presented so far, making it smaller and lighter, which is an added benefit. (Figure 2.14)

The fuel burn calculation versus speed plot for this turbine is shown in Figure 2.14.
The corresponding Smith Curve correlation is shown in Figure 2.15.

TABLE 2.3.-Three-STAGE TURBINE RESULTS
3 Stage

\% Speed
\% Design RPM
53.8
69.2


Figure 2.11.-Turbine Design Speed Selection


Figure 2.12.-Smith Correlation for Three Turbines


Figure 2.13.-Four-Stage Turbine Flowpath


Figure 2.14.—Design Speed Versus Segment Fuel Burn
TABLE 2.4.-FOUR-STAGE TURBINE SEGMENT FUEL BURN
4 Stg Hi Loading (1)

| \% Speed | Design RPM | Fuel Burn\% | ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 53.8 | 8045 | -0.84 | 78.77 | 71.42 | 69.10 | 87.45 |
| 69.2 | 10343 | -7.98 | 90.15 | 87.28 | 87.13 | 87.37 |
| 84.6 | 12642 | -8.31 | 93.67 | 92.32 | 92.37 | 85.64 |
| 100.0 | 14941 | -3.68 | 93.96 | 93.59 | 94.26 | 79.31 |



Figure 2.15.—Smith Correlation for Four Study Turbines

A complete description of the 8 flowpaths examined in this study is provided in Appendix C.
This flowpath (Four Stage: High Loading 1) emerges from the flowpath study as having the best potential to minimize mission fuel burn. This conclusion is based on the assumption that the meanline loss model and, more specifically, the off-design loss model adequately predict the efficiency characteristics through a significant range in incidence and loading. Presumably, the design is centered in the design space such that the turbine will not rapidly lose performance as speed and loading change throughout the flight envelope. In order to gain confidence in this conclusion, a 3-D design was executed at 75 percent speed ( 11174 rpm ) and investigated in various CFD simulations. Appendix D contains both the $3-\mathrm{D}$ and $1-\mathrm{D}$ analysis summaries for the design conditions. An additional summary of the meanline predictions for 54 and 100 percent design speed is presented in Appendix E. This is provided to illustrate the large impact of the full speed variation and its implication to the design velocity triangles.

### 2.8 3-D Design Execution

Airfoils were designed consistent with the chosen flowpath (Four Stage: High Loading 1). The design was executed at 75 percent speed, i.e., 11174 rpm. The basic methodology for executing the 3-D design was as follows:

- Each of the 8 airfoils is designed by stacking three 2-D design sections, i.e., a hub section, a mean section and a tip section. (Figure 2.16)
- Each 2-D section is manually designed in an interactive design tool called "FoilGen". (Figure 2.17) FoilGen has a variety of tools that allow for simple structural analysis, $2-\mathrm{D}$ aerodynamics, 3-D stacking and airfoil internal core validation if applicable.
- Design iterations are passed through an in-house 3-D solver called VORTEX. VORTEX has an inviscid mode with an empirical loss model which aids in establishing the correct velocity triangles in the absence of viscous effect. This solver runs fast enough to execute several design iterations per day.
- Designs are validated via viscous simulation. VORTEX can be run with the full Navier Stokes equations turned on. The turbulence model is the $\kappa-\omega$ model with integration to the walls (no wall functions). A steady state mixing plane assumption was used at the interface between stators and rotors.

The full Four Stage design was executed at 75 percent speed which is consistent with Figure 2.14. This places the design point approximately half way between the cruise ( 54 percent speed) and the SLTO (100 percent speed) conditions. The airfoil geometry was not refined to a final status for all 8 airfoils, but only to a satisfactory level for further study. The third Stage was chosen as a representative stage for more in-depth analysis. The third Stage design was pulled out and further refined (Figure 2.18). Calculations were performed using boundary conditions from the full Four stage calculation. A detailed review of the full four stage 3-D CFD run is documented in Appendix D.


Figure 2.16.—Airfoil Stacking


Figure 2.17.—FoilGen Output


Figure 2.18.—Third Stage extracted from full simulation to investigate off-design performance

### 2.9 Loss System Validation via CFD

The optimum flowpath selected for this turbine and the choice of design speed relies on the off-design predictive capability of the meanline analysis. In order to assess the validity of this model, various CFD models were exercised. The third stage vane and blade were chosen as a representative set of airfoils. Two separate studies were performed. The first study addresses the incidence tolerance of the third blade and the other adds the vane and assesses the third stage together. The blade study was performed with two different blade thicknesses.

### 2.10 Turbine Blade Incidence Study

The third stage vane and blade were run together through a series of CFD runs. All CFD runs are based on steady state assumptions using mixing planes to account for time averaging between stationary and rotating frames. The inlet conditions (Total Pressure, Total Temperature, and gas angles) to the third vane were held fixed and the exit static pressure from the third blade was also fixed. The CFD was then run over a sweep of rpm. This analysis will simulate the incidence and loading sweeps that the blade would undergo throughout the operating envelope while the vane remains fixed at design point. The meanline was run exactly the same way to predict the efficiency changes as the speed changes. Both the meanline and the CFD assume no leakage flows, cooling flows or tip clearance. The meanline has a real gas model while the CFD runs assume ideal gas. The CFD confirms the large incidence swing and loading changes that are expected as the rpm is varied. Four different CFD simulations were performed; each one was swept through the speed range. All four simulations predict better incidence tolerance than the meanline correlation. This result is particularly satisfying because the meanline prediction was better
than the cycle simulation. If actual incidence tolerance is better than the meanline characteristic, than overall engine performance should surpass the NPSS simulation.

The four CFD simulations used are:

1. VORTEX (Williams International proprietary solver). $\kappa-\omega$ turbulence model, integrated through boundary layers to the wall.
2. FLUENT (ANSYS, Inc.) $\kappa-\varepsilon$ realizable, using wall functions
3. FLUENT $\kappa-\omega$ turbulence model, transitional flow model
4. FLUENT $\kappa-\omega$ turbulence model, SST

All FLUENT calculations used a density based, implicit solver while VORTEX used a density based explicit solver. FLUENT version 6.3 was used.

Figure 2.19 compares the meanline prediction and the four CFD runs. Inside of the design speed range, all four CFD simulations predict flatter efficiency trends than the meanline. There is considerable variability in the predicted level of efficiency among the FLUENT turbulence models. VORTEX and the Std, $\kappa-\omega$ SST model are very similar and close to the meanline level. The transitional flow model for $\kappa-\omega$ predicts unrealistically low efficiency even at the design point. VORTEX was run to a more broad speed range to search for an incidence cliff. It did reveal a very rapid fall off in efficiency at 40 percent speed when the loading was high enough to cause suction side separations. At that condition, the efficiency fall off was more rapid than predicted by the meanline.


Figure 2.19.—Efficiency Comparisons for Four Turbine Designs

Figure 2.19 is good testimony to the fact that CFD is still paced by the lack of fidelity in turbulence modeling. The level of efficiency predicted by various turbulence models is significant. However, all four models predict a very similar efficiency trend with speed. The results give some confidence that the design may meet its incidence tolerance goals but is not adequate to completely mitigate risk. If it were necessary to chose between a fixed speed turbine and a variable speed turbine, a turbine rig test would still be recommended to determine if this design can truly meet the incidence tolerance goals. Another observation from Figure 2.19 is that the turbine blade is more tolerant to negative incidence than positive. This would lead us to move the design speed lower (higher camber airfoils) and allow the turbine to run off-design further on the negative side than the positive.

### 2.11 Thin Turbine Blade Incidence Study

Traditional airfoil design philosophy would indicate that larger leading edge diameters are more incidence tolerant than smaller diameters. While this is well established for airfoils in a free-stream, it is not nearly so obvious for airfoil cascades where the internal flow between the airfoils is more like channel flow than external flow. When a cascade airfoil has a larger LE diameter, the entire airfoil must be thicker. Thicker airfoils have higher through flow velocities and therefore (by intuition) generate more viscous scrubbing losses. Although this statement seems straight forward and logical, the high camber inherent in gas turbine blades complicates the situation.

Consider the airfoil shown in Figure 2.20. The throat of the airfoil cascade spans from the TE of one airfoil to the suction side of an adjacent airfoil. The passage between the two airfoils is bounded by the suction side of one airfoil and the pressure side of the adjacent. This passage controls the through-flow Mach numbers of the gas as it passes through the airfoils. It is desirous for this passage to be separation free and as low loss as possible. In this figure, the design philosophy is to produce a smooth, converging passage through the airfoil to the throat. To illustrate this passage convergence, a line of the same dimension as the throat is shown in orange. It is swept forward in the direction of the green line perpendicular to the suction side resulting in the orange trace. This gives a visual cue to the convergence through the passage as well as how the airfoil pressure side can impact the channel convergence.

Now consider the airfoil shown in Figure 2.21. This cascade has the same suction side as Figure 2.22 but a pressure side that results in a thinner airfoil. The airfoil passage now has a non-smooth area distribution through the channel. After the leading edge of the airfoil, the pressure side diffuses and then converges to the airfoil throat. Experience with this type of cascade would predict pressure side separation and reattachment as sketched in light grey. If the resulting separation bubble is large enough, the resulting blockage may result in through-flow Mach numbers similar to the airfoil in Figure 2.20. Separation bubbles that occur at relatively low velocities and are followed by strong acceleration generally do not generate high pressure loss. However, in the case of a rotating blade, the low momentum fluid trapped in a separation bubble can be centrifugally pumped outward due to the high rotational acceleration field. This can cause much higher loss than in the case of a stationary airfoil.

A study was executed to determine if a thin blade could potentially improve overall fuel burn by lowering through-flow velocity or would a separation bubble out-weigh any perceived benefit. Again the third stage was used as a representative stage. The blade was redesigned to be thinner but still maintain the same suction side as the nominal blade.

Figure 2.22 shows visually the change made to the blade. The brown line in the background indicates the nominal blade pressure side.


Figure 2.20.—A Simple Turbine Blade Cascade


Figure 2.21.—A sample thin blade cascade


Figure 2.22.—Blade Profile Modifications


Figure 2.23.-Thin turbine blade geometry compared to nominal
The thin blade should be more susceptible to pressure side separation at high negative incidence (high speed). At positive incidence (low speed), the air impinges on the airfoil in a more favorable way for the pressure side and may not separate. We would therefore expect a thin blade to be similar or better at low speed but potentially worse at high speed. The airfoil in Figure 2.22 was run through FLUENT in a consistent manor with Figure 2.19. The results are shown in Figure 2.23. The dash lines indicate the results of the thin airfoil and are color consistent with the nominal blade run to the same turbulence model. The results are very similar with the thin blade overall slightly higher in loss. All three analyzes hint that low speed performance trends better than high speed performance. Based on this study there is no compelling evidence to depart from normal design philosophy (i.e., smooth channel convergence).

### 2.12 Third Stage Combined Incidence Study

The third Stage combined study was conducted in similar fashion as the third blade only study. The simulation was composed of the second blade, the third vane and the third blade. (Figure 2.24) The inlet conditions into the second blade were held fixed in the absolute frame of reference simulating the exit conditions of the second vane. The exit condition of the third blade was a free vortex boundary with the average static pressure iterated to match the proper exit corrected flow. In order to assess the third stage performance, the efficiency of the second blade was ignored and the third stage was calculated based on its inlet and exit conditions in the converged solution. The meanline analysis was performed in exactly the same manor so that the CFD and meanline results may be compared directly. The speed was varied in a similar way as was done in the blade only study. There was no tip clearance, leakage or cooling modeled. In this calculation both the third vane and third blade experience the incidence swing associated with the speed change, therefore the efficiency impact with speed is higher than the previous study. Figure 2.25 compares the resulting meanline efficiency to the CFD prediction. The conclusions are generally the same
as the blade only calculations. The CFD prediction is more incidence tolerant than the meanline prediction and also indicates that negative incidence (high speed) is more forgiving than positive incidence.

The third vane total pressure loss was extracted from the CFD and compared to the meanline prediction as well (Figure 2.26).

The vane exhibits a similar trend as the blade in that it is more incidence tolerant at high speed (negative incidence) rather than low speed. The vane is exceptionally tolerant at negative incidence because the pressure side separation bubble is: 1) very small (less than $1 / 2$ the thickness of the airfoil), and 2) completely reattached at relatively low Mach number before the airfoil throat (Figure 2.27). Unlike the blade, the vane is not subject to the high centrifugal acceleration field and therefore the low momentum fluid trapped in the separation bubble is not transported radially.


Figure 2.24.-Third Stage Speed Study composed of Three airfoils


Figure 2.25.—Third Stage Performance


Figure 2.26.—Third Vane Pressure Loss


Figure 2.27.—Vane Velocity Vectors

All the CFD work performed suggests that mission fuel burn is improved by designing for relatively low corrected speed. In this present work, the design speed chosen was 75 percent speed, or approximately half way between low speed cruise ( 54 percent) and high speed take-off ( 100 percent) based on meanline predictions. The CFD suggests that the turbine is: 1) more forgiving than the meanline predictions and 2 ) able to tolerate higher negative incidence. A lower design speed may further improve overall mission fuel burn. Figure 2.14 would suggest a design speed of 70 percent as a logical compromise or next design iteration. Designing for lower speed also results in airfoils with higher camber. This is an added benefit because higher camber airfoils are generally stiffer and more resilient to high cycle fatigue.

### 2.13 Airfoil Leading Edge Geometry

The aviation industry routinely designs wings for variation in loading and incidence. From the largest commercial aircraft to the private general aviation airplane, variable geometry (flaps and/or LE slats) are employed to increase loading coefficient and wing area during take-off and landing. Zenith Aircraft Company uses a fixed LE slat (Figure 2.28) to make their STOL CH 701 stall resistant to very high angles of attack. The completely passive nature of their design is very attractive from a cost and complexity standpoint. Similarly, in this VSPT design, it would be very desirable to include features that improve tolerance while being completely passive. Turbine airfoils are relatively small and made from investment castings. It would be impractical to attempt to cast them with such intricate details. It would however be very advantageous to design turbine airfoils with a LE shape that was inherently incidence tolerant. One concept investigated in this study is to attempt to smooth the LE curvature distribution as much as possible in order to allow the air to smoothly transition from the LE to the airfoil pressure and suction sides.

Turbine airfoils are typically designed with an elliptical LE connected to a curved pressure and suction side. See Figure 2.29. Although the intersection of the ellipse and airfoil curves is designed to match point and slope, it does not typically match curvature and can in fact be discontinuous. In order to assess the impact of this discontinuity, a smoothing algorithm was developed and applied to the third blade from the previous studies. The algorithm calculates the curvature as a function of surface length (Sdistance) and calculates a local correction factor based on the gradient in curvature from one point to the next. Each point is moved normal to the surface in the direction to smooth the gradient by a small amount. The process was iterated 200 times until a smooth curvature distribution was obtained. See Figure 2.30. The actual change in the surface profile required to smooth the curvature distribution is well within any reasonable casting profile tolerance. As shown in Figure 2.30(b) it is nearly within the thickness of a line when plotted at a reasonable viewing size. Figure 2.30(c) clearly shows the discontinuity in curvature at the tangency points and the result of running the smoothing algorithm. Nonetheless, it is still desirable to establish the best possible design shape and apply manufacturing tolerance about that nominal shape rather than a less optimal design. In order to determine if the smooth shape is in fact better, the smoothed third blade was run through the same set of CFD calculations as in the blade incidence study.


Figure 2.28.-Fixed geometry LE slats. Used with permission from Zenith Aircraft Company, Mexico, Missouri, 65265-0650.


Figure 2.29.—Typical Turbine Airfoil Leading Edge Profile


Figure 2.30.-Third Blade Mean, surface curvature smoothed

The changes to the geometry and CFD mesh were basically imperceivable to the eye. The global CFD results (i.e., efficiency and flow) for the third Blade at design speed ( 75 percent) were virtually unchanged relative to the non-smoothed blade. Figure 2.31 gives the mid-span surface static pressure loading also showing nearly identical results. Despite this disappointing result, the CFD was run at high and low speed to investigate off-incidence tolerance. The resulting efficiency trend with variation in speed was surprising. See Figure 2.32. Shown in green, the smoothed LE contour maintained better incidence tolerance at low speed relative the non-smoothed baseline configuration shown in pink. In order to understand this, a detailed investigation into the flow field was performed. At the design speed, no significant flow field changes were evident. This was also true at negative incidence (high speed), but at low speed, the smoothed LE resulted in an improved flow field. At approximately 80 percent span, the airfoil suction side loading is highest. As the airfoil loading is increased, this is the most likely location for the airfoil to separate.


Tue Jan 11 13:33:37 2011
Figure 2.31.—Third Blade mid span static pressure distribution


Figure 2.32.—Smoothed third Blade Efficiency Trend with Speed
Combing through the velocity vectors did reveal a separation in this location for the baseline (unsmoothed) blade. The easiest way to visualize this is to capture the separation bubble with a constant Mach number surface.

In Figure 2.33, the non-smoothed blade is compared to the smoothed blade. An iso-Mach number surface was generated for each calculation. The yellow-green surfaces shown are surfaces of Mach number equal to 0.15 . Since the through-flow Mach numbers are all much higher than 0.15 , all of the flow beneath the surfaces shown are boundary layers or separations. The non-smoothed blade has a separation bubble near the tip that is nearly completely removed after the blade is smoothed. The separation bubble is visually interacting with the secondary flow field near the shroud line.

This result is based on a single solver and turbulence model. No further CFD modeling was performed within this study. It is not know how transition from laminar to turbulent flow may be impacted by curvature smoothing. Likewise, the impact of the unsteady flow field is not known.

This work reinforces the importance of maintaining boundary layer health upstream of diffusing flowpaths. These results are encouraging: they suggest careful design of LE geometry can improve airfoil incidence tolerance. Additional, this completely passive design does not change the design point methodology. The design point analysis was completely unaffected by the incorporation of the smoothing algorithm. Addition research in this area may result in airfoil shapes that are inherently more incidence capable.


Figure 2.33.-Separation bubble visualization

### 3.0 VSPT LCTR Mission Performance Modeling

A thermodynamic cycle model was developed to study the performance impact of various power turbine designs. The basis of this study was the TS2-NPSS model provided by the NASA Glenn Research Center. The model was originally created March 5, 2010, and has description: "two-spool turboshaft about equal work for LPC/HPC, HPC is PR=1.3 axial + centrifugal - includes update for turbine cooling (best guess for number turbine stages)". The model was updated from NPSSv1.6.5 to NPSSv2.3 and the output of the model was enhanced. A copy of the updated model was provided to NASA to assist in adopting the latest version of NPSS consistent with NASA's overall goals. The only performance feature of the cycle model that was modified was the Power Turbine maps.

Three turbine designs were evaluated at the three critical mission points defined in the LCTR "Design" Mission Profile. These mission points define the design conditions for the overall cycle and present some challenges for the turbine design because of the wide range of shaft speeds. Table 3.1 summarizes the flight conditions and shaft speeds.

TABLE 3.1.-CRITICAL MISSION POINTS

| Mission Segment | Takeoff hot | Climb | Cruise |
| :--- | :---: | :---: | :---: |
| Time, hr | 0.07 | 1.00 | 3.00 |
| Power, hp | 7859 | 2646 | 2351 |
| N3, rpm | 15000 | 15000 | 8077 |
| Ambient |  |  |  |
| Mach Number | 0 | 0.51 | 0.51 |
| Altitude, ft | 0 | 28000 | 28000 |
| Delta T from standard conditions, F | 45 | 0 | 0 |
| VTAS, knot | 0 | 303 | 303 |



Figure 3.1.—VSPT Total Mission Fuel Burn for Three Williams International Designs
The Takeoff hot condition requires the maximum power at high rotor speed, but the amount of time at that condition is limited to 3 min for takeoff and 3 min for landing with an additional minute for taxi. The climb is represented by the top of climb condition at high rotor speed and represents 30 min to climb plus an additional 30 min to fly to an alternate destination. The cruise condition is represented by the same flight condition as the climb point, but at shaft rpm that is 54 percent of the full throttle condition and also at high power output for 3 hr .

The power turbine map provided with the NASA model was run at the three flight conditions and the power output was used as the requirement for each flight condition. Three power turbines were designed to provide performance at the cruise condition and to meet the maximum shaft speed requirement. The turbine design points were set at 65,75 and 85 percent corrected speed and are labeled accordingly. Figure 3.1 shows the total mission fuel burn for the three designs.

The three proposed designs have significantly reduced mission fuel burn compared to the baseline power turbine design. The 75 percent design has the lowest mission fuel burn and is the best design on this basis. The 75 percent design uses 1.6 percent less fuel than the 65 percent design and 0.6 percent less fuel than the 85 percent design. The 75 percent design uses 12.1 percent less fuel than the baseline design and is the best overall design based on this preliminary design study. For each of the three turbine designs, the NPSS output for the three critical mission points is given in Appendix H.

In the cycle detailed output, there are 6 points presented for each turbine design. The takeoff point (T/O) is the cycle design point at takeoff power on a standard day at $15,000 \mathrm{rpm}$ power turbine speed. The second point is takeoff on a hot day. The third point is at the climb condition, $15,000 \mathrm{rpm}$ at the same power setting as the NASA design climb condition; however the power setting condition logic does not result in the same power output for different turbine designs. The fourth point is at the climb condition at the same power output as the NASA design to allow fuel flow comparisons. The fifth point is at the Cruise condition at reduced shaft speed of $8,077 \mathrm{rpm}$ at the NASA power setting. The sixth point is at the Cruise condition at the NASA power level and is used for the fuel flow comparison.

### 4.0 Development of a Cost-Effective Approach to an LCTR-Relevant VSPT Component Experiment

Testing of a power turbine presents unique challenges in that it is not self-supporting. In order to test a power turbine, inlet compressed air is required that requires heating to at least several hundred degrees F to avoid ice formation on exhaust structures and instrumentation. A power sink is also required that has excellent control characteristics in order to set rpm and avoid overspeeds. Ideally, the power turbine should be tested at full scale to minimize Reynolds effects and so that key inter-stage instrumentation can be inserted without unduly affecting the flow conditions in the local area. Since the VSPT for the LCTR will be relatively large, full scale testing will require a test facility that can provide continuous flow of large volumes of heated inlet air with substantial power absorption capability. Use of an existing engine as a gas generator testbed for testing the VSPT was considered as an option, but ruled out because the engine operating line would severely limit the range of power turbine entrance conditions that could be achieved during test. The optimum approach appears to be to develop a dedicated VSPT rig to mate to the single-spool turbine test facility at NASA GRC. The capabilities and limits of the single-spool turbine facility, listed in Table 4.1, provide more than sufficient capability to produce the entrance and exit conditions needed to evaluate the LCTR VSPT design concept at full scale.

There are two basic engine configurations that can provide power to the rotor system, and both have been used successfully in large numbers of turboshaft and turboprop systems. The gas generator can be mounted with the compressor facing in the direction of flight, or opposite to the direction of flight. The aft-facing compressor configuration, similar to that used by the Pratt \& Whitney PT-6 turboprop, provides a very large advantage in that the power turbine shaft can be very short and large in diameter since the power turbine module is adjacent to the reduction drive gearbox, compared to the long, thin shaft needed by the forward-compressor configuration, which needs to pass the turbine shaft through the center of the gas generator shafts. This greatly reduces or eliminates the rotordynamics and torque limitations issues associated with the long, thin shaft. The disadvantage of this configuration is that the airflow must be turned $180^{\circ}$ prior to entering the inlet, and once again in the exhaust duct. This is necessary to avoid having the inlets face the ground during VTOL operation. An advantage is that it provides a simple method for rejecting ice, birds, or other foreign matter before it can enter the gas generator. The forwardfacing compressor configuration requires an S-duct inlet and can use an axial exhaust, which have lower aerodynamic losses. The aft-facing compressor design also provides a much easier approach to an inertial separator design for ejecting ice and solid objects, another distinct advantage. Mostly because of the reduced rotordynamics concerns, the compressor-aft configuration is recommended for the LCTR application. Figure 4.1 is a schematic of this configuration for a twin-pack LCTR design. The spacing between the power turbine exhaust and the reduction drive gearbox is the minimum required to provide a low-loss turn in the exhaust duct.

TABLE 4.1.-NASA GRC SINGLE-SPOOL TURBINE TEST FACILITY CAPABILITIES

|  | Maximum Turbine Inlet Pressure | 50 psia |
| :---: | :---: | :---: |
|  | Minimum Exhaust Pressure | 2 psia |
|  | Maximum Inlet Air Temperature (from in-line vitiated natural gas combustors) | $940^{\circ} \mathrm{F}$ |
|  | Maximum Primary Air Flow Rate | 27 pps |
| - Secondary Air (150 psig supply):$\begin{aligned} & >2 \text { Legs }-1.5 \text { pps each up to } 555^{\circ} \mathrm{F} \\ & \gg 4 \text { Legs }-0.08 \text { to } 1.19 \text { pps each up to } 250^{\circ} \mathrm{F} \\ & \gg 6 \text { Legs }- \text { at } 70^{\circ} \mathrm{F} \end{aligned}$ |  |  |
|  | Maximum Turbine Rotational Speed (with maximum Gear Ratio, G.R., of 7.87) | 14,000 rpm |
|  | aximum Turbine Torque | $36,217 \mathrm{ft} \cdot \mathrm{lb} / \mathrm{f} . \mathrm{R}$. |
|  | Minimum Gear Ratio, G.R. $=1.51$ <br> $\left(N_{\text {max }}=2,718\right.$ rpm; orrque $_{\text {max }}=24,000$ ft $\left.\cdot \mathrm{b}_{\mathrm{F}}\right)$ |  |
|  | Maximum Test Article Diameter | 52 inch |



Figure 4.1.-Schematic of Recommended Engine Configuration for LCTR
Rotordynamics of turboshaft machinery such as tilt rotors are generally divided up into two categories, lateral and torsional. Each has its own set of typical challenges.

Lateral challenges typically involve long flexible drive shafts that operate above the first flexible critical mode, i.e., supercritical rotors. Inadequate damping at the bearings results in damaging vibrations when traversing the lateral critical modes of drive shaft. Controlling run-out and wall thickness variation of long hollow flexible shafts at reasonable cost is often challenging. Misalignment of drive shaft between gearbox and power-turbine adds further complexity that must be addressed. Last and perhaps most important the large overhung tilt rotor makes the system sensitive to rotating unbalance.

Torsional challenges typically involve shock from start up and elevated transient loading through the drive shaft. Unloading of gear teeth during surge events, back lash, gear run out, random vibration due to gear inaccuracies and rolling element defects, and closed loop control system instabilities have all been known to lead to torsional failure modes. All of these issues need to be addressed as part of the full engine and test article designs.

Figure 4.2 shows a layout of the proposed full scale VSPT test article mated to the NASA GRC single spool turbine test facility dynamometer drive frame. Locations are indicated for multi-element instrumentation rakes at the inlet and exit of the VSPT, and for cylindrical radially-translating flow angle sensors at each of the three interstage locations. The rig inner and outer flowpaths are a combination of formed sheet metal and machined details, with the inner flowpath and bearing support structures supported by an exit guide vane row set well behind the last stage rotor. The four-stage turbine is overhung on the front of the shaft, supported by an aft roller bearing and forward ball bearing to react thrust loads. As shown, the thrust loads are intended to be reacted through the front bearing and out into the outer frame structure through the exit guide vane row. The bearing cartridge in the SSTTF has sufficient load capacity to support the VSPT test article as an entirely overhung mass, so an alternative approach would be to eliminate the VSPT bearings altogether and hang the VSPT off the front of the drive spindle. If feasible, this arrangement would simplify the system and eliminate the bearing lubrication requirements, as well as reducing the cost of the design and hardware. It will be necessary to analyze the shaft system to ensure that critical speeds are not an issue and displacements do not drive excessive tip clearances in the test article. The preliminary aero and structural design tasks in the experimental program will determine if it will also be necessary to include one or more balance pistons to offset some of the thrust load.


Figure 4.2.—VSPT Test Article Mated to NASA-GC Single Spool Turbine Test Facility

The four-stage rotor is shown as a clamped assembly with the clamp loads applied at the hub through curvic couplings. This was done in order to make it possible to use the cylindrical wake angle sensors. This type of sensor has performed very well in past tests and has the advantage of being much smaller in diameter than traditional cobra probe sensors because it is supported at both ends of the flowpath rather than cantilevered from the outer wall. This greatly minimizes blockage but imposes some limitations on the design of the test component. Since the sensing position on the probe has to transit the entire span from the outer to the inner wall, provisions must be made for the probe body to penetrate an equal distance beneath the inner flowpath when the inlet holes are at the innermost radial position. This makes it impossible to use with a drum rotor configuration. A detailed rotordynamic analysis of the rotor/shaft system will be a key part of the experimental program and its results will determine whether this approach is feasible or if a drum rotor configuration with conventional probes is required to achieve sufficient speed and frequency margins relative to the operating speed range. The spacing between stages and between vane and blade rows shown in the figure is notional and would be optimized during the test article design process to provide access and routing for all of the planned instrumentation.

### 4.1 Experimental Test Plan and Instrumentation List

The proposed operating conditions of the VSPT vary from 54 to 100 percent speed. Therefore, it would be beneficial to develop a turbine map that fully describes the turbine efficiency within this range. The proposed test plan to characterize this turbine would include a pressure ratio sweep from 3.0 to 7.0 and a speed sweep of 40 to 120 percent (Table 4.2). Generally speaking, it is easier to change speed than PR in a test facility so the order of operations would be to set PR and then increment through the speed range to develop lines of constant PR.

TABLE 4.2.—PROPOSED MAP/TEST PLAN

|  | PR |  |  |  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Speed\% | 3 | 3.5 | 4 | 4.5 | 5 | 5.5 | 6 | 6.5 | 7 |
| 40 |  |  |  |  |  |  |  |  |  |
| 50 |  |  |  |  |  |  |  |  |  |
| 60 |  |  |  |  |  |  |  |  |  |
| 70 |  |  |  |  |  |  |  |  |  |
| 80 |  |  |  |  |  |  |  |  |  |
| 90 |  |  |  |  |  |  |  |  |  |
| 100 |  |  |  |  |  |  |  |  |  |
| 110 |  |  |  |  |  |  |  |  |  |
| 120 |  |  |  |  |  |  |  |  |  |

The turbine map should be developed at both high and low Reynolds number where "high" is equivalent to a SLTO condition and "low" is equivalent to the cruise condition.

Low Reynolds number cruise at highest corrected speed is most challenging condition, and requires vacuum. For similitude in Reynolds number, PR, Corrected Flow and Corrected speed, the following table defines the 100 percent speed conditions for the turbine:

|  | Engine | Proposed Rig |
| :--- | :--- | :--- |
| Inlet PT | 31.01 psia | 20.6 psia |
| Inlet TT | $1749.1^{\circ} \mathrm{R}$ | $1260 .^{\circ} \mathrm{R}\left(800^{\circ} \mathrm{F}\right)$ |
| Inlet Mass Flow | $12.04 \mathrm{lbm} / \mathrm{s}$ | $9.425 \mathrm{lbm} / \mathrm{s}$ |
| Power | 2740 hp | 1525 hp |
| Exit PT | 5.35 psia | 3.55 psia |
| rpm | 14898 | 12645 |
|  |  |  |
| First Vane Reynolds Number | 178,000 | 172,000 |
| Last Blade Reynolds Number | 61,000 | 61,000 |

The SLTO (high Reynolds Number) condition requires the following parameters:

|  | Engine | Proposed Rig |
| :--- | :--- | :--- |
| Inlet PT | 88.49 psia | 45 psia |
| Inlet TT | $2166.3^{\circ} \mathrm{R}$ | $1260^{\circ} \mathrm{R}\left(800^{\circ} \mathrm{F}\right)$ |
| Inlet Mass Flow | $9.41 \mathrm{lbm} / \mathrm{s}$ | $20.6 \mathrm{lbm} / \mathrm{s}$ |
| Power | 7500 hp | 3350 hp |
| Exit PT | 15.43 psia | 7.76 psia |
| rpm | 14898 | 12645 |
|  |  |  |
| First Vane Reynolds Number | 395,000 | 377,000 |
| Last Blade Reynolds Number | 130,000 | 134,000 |

These rig conditions are within the advertised capability of the New Single Spool Turbine Facility proposed by NASA to replace W-6A Warm Core Turbine Facility.

In order to simplify the rig as much as possible, the rig would be uncooled. The proposed warm inlet temperature of $800^{\circ} \mathrm{F}$ should allow for nearly no cooling flow. This allows for simple turbine efficiency calculations based only on measured inlet and exit total pressure and total temperatures. The Turbine efficiency can be calculated as follows:

$$
\eta=\frac{\Delta \mathrm{T}}{\mathrm{~T}_{\text {in }}\left(1.0-\mathrm{PR}^{\frac{1.0-\gamma}{\gamma}}\right)}
$$

where $\gamma$ is the ratio of specific heats calculated at the average of the inlet and exit temperatures.
The corrected speed is calculated as:

$$
\operatorname{rpm}_{\text {corr }}=\operatorname{rpm} \sqrt{\frac{518.67}{\mathrm{~T}_{\mathrm{in}}}}
$$

where 100 percent is defined as $\mathrm{rpm}_{\text {corr }}=8113$.
Of great interest is the turbines performance at the two design conditions (54 and 100 percent) speed. At these conditions, inter stage gas swirl angle and total pressure profiles will be measured and compared back to predictions. The use of a cylindrical probe between the stages is proposed to measure gas angles behind rotors with minimal blockage. It is significantly more difficult to measure the gas angles behind stators because the circumferential variation in angle and pressure complicates the measurement and therefore it is not recommended.

Table 4.3 comprises an initial recommendation for instrumentation required to collect the desired test data.

TABLE 4.3.-PROPOSED INSTRUMENTATION LIST FOR VSPT COMPONENT EXPERIMENT

| Sensor type | Objective | Location | Quantity | Required accuracy |
| :---: | :---: | :---: | :---: | :---: |
| Radially translating cylindrical gas angle sensor | Measure flow angles exiting each turbine stage | Nozzle vane Leading Edge | 1 per stage, 3 total | $\pm 1^{\circ}$ |
| Six-element total pressure rake | Measure total pressure at entrance and exit of VSPT | Inlet and exit | 6 | $\pm 0.5 \%$ |
| Static pressure taps | Determine pressure distribution around vanes | Outer and inner wall, at root of nozzle vane | $20 \text { OD, } 20 \text { ID, } 3$ <br> locations, 120 total | $\pm 0.5 \%$ |
| Six-element total temperature rake | Determine stage temperature drop | Inlet and exit | 6 | $\pm 1^{\circ} \mathrm{F}$ |
| Bearing Thermocouple, type K | Monitor bearing health | Outer race | 2 per bearing, 4 total | $\pm 10^{\circ} \mathrm{F}$ |
| NSMS or capacitance probe | Actively monitor tip clearance | At tip of each blade row | 4 | $\pm 0.001$ in. |
| Rub Pins | Verify min tip clearance | At tip of each blade row | 2 per row, 8 total | $\pm 0.001 \mathrm{in}$. |
| Triax accelerometer | Monitor vibes for rig health | On fwd and aft bearing housing | 2 | $\pm 1 \mathrm{~g}$ |
| Real Time Spectrum Analyzer | Monitor vibes and frequencies for rig health | Accelerometer output | 1 | N/A |
| Oil sump thermocouple, type K | Monitor oil temperature | Oil sump | 1 | $\pm 10^{\circ} \mathrm{F}$ |
| Strain gage thrust ring | Monitor bearing thrust load | Fwd bearing | 2 | $\pm 10 \mathrm{lbf}$ |
| Facility Speed pickup | Monitor speed | facility | 2 | $\pm 10 \mathrm{rpm}$ |

### 4.2 VSPT Component Experiment Program Plan, Schedule, and ROM Cost

A program to provide experimental validation of the proposed LCTR VSPT using the NASA GRC Single Spool Turbine Facility can be accomplished in 36 months, of which 33 months are required for the technical effort and 3 months for reporting. Figure 4.3 shows a notional program schedule to accomplish this effort. During the preliminary design task, the concept for the VSPT will be refined to the point where all key aspects of the component and rig designs have been defined in sufficient detail to ensure that no key risk items are likely to force substantive design changes during detailed design. This requires that a comprehensive layout be produced, from which a bill of materials and parts list can be generated. Preliminary aerodynamics will be defined for each blade and vane row, from which structural models will be prepared. The aerodynamic, structural, and dynamic design of the blades, vanes, and other flowpath elements needs to take into consideration the actual operating conditions the VSPT would see in operation behind the gas generator, not just the relatively cold rig operating conditions, since it would do no good to test a component design which has no chance of surviving the actual operating conditions in the real engine. Rotordynamic analyses will be required as a part of the preliminary design in order to ensure that sufficient speed and frequency margins can be obtained with the proposed configuration. For a power turbine module that interfaces with the reduction gearbox directly rather than by extending a shaft through


Figure 4.3.—Proposed Schedule for VSPT Experiment
the gas generator (e.g., PT-6 configuration) there is substantial freedom in the design and opportunity to vary shaft characteristics and bearing spacing to achieve sufficient margins, so the risk of not achieving acceptable margins is fairly low. To reduce risk, a Design Failure Modes and Effects Analysis (DFMEA) will be conducted during preliminary design. This will help identify any potential failure modes and define mitigation approaches early enough in the program so they can be incorporated into the design and test plan.

The rig configuration will be driven by the requirements to obtain the key data for validating the design, and by the interfaces with NASA's single spool turbine facility. At the outset of the preliminary design task, Substantial coordination with the NASA technical team will be required to define the rig/facility interface requirements, as well as routing for instrumentation and secondary systems plumbing and rig and facility safety requirements.

The lubrication and secondary air systems will also be defined in the preliminary design. For the rig, a conventional jetted recirculating oil lubrication system will be used. Facility pumps will provide motive flow and scavenge and these will be sized according to the predicted requirements of the rig across its operating range of speed and power output. Purge air flow and pressure requirements for bearing compartments and to prevent flowpath air ingestion will also be defined. The preliminary design effort is expected to require 7 months to complete. At the conclusion of the preliminary design efforts, a preliminary design review with the NASA technical team is planned.

Since all of the key characteristics of the VSPT component and rig design will have been defined in Preliminary Design, the detailed design efforts will focus on substantiating the preliminary design configuration via detailed modeling and analysis. The instrumentation and test plan will be finalized and will be provided to NASA along with a 3-D external model of the test rig and all its secondary systems and plumbing. Component aerodynamics will be finalized via detailed CFD, structural, and dynamics
analyses, including transient analyses to define final operating and build tip clearances. If necessary due to design changes, the rotordynamics model will be updated and exercised to finalize the design of the rotary group and bearing system. Design release packages will be produced, comprising all the design and manufacturing information needed to produce or procure the component and rig hardware. At the completion of the detailed design task, a detailed design review will be held with the NASA technical team. The DDR will include a review of the updated DFMEA based on the completed state of the design.

Once the DDR is approved, long lead hardware will be ordered and hardware fabrication will begin. Since the rig and component hardware is primarily to be made of steel and aluminum, it is likely the only long lead hardware may be the bearings. As a risk reduction approach, the rig can be designed around bearings that are already in hand and available, or are known to be available on short lead. Fabrication of rig and component hardware, as well as facility adaptive hardware, can be completed in 8 months, at which time instrumentation and assembly of the rig will begin. The milestone for delivery of the completed instrumented rig to the NASA test facility occurs at month 24.

A detailed test readiness and safety review will be conducted once the rig is installed at the test facility. This review will address all aspects of rig operation and data collection, including a review of the DFMEA.

Testing will begin at month 28 and will follow the approved test plan. Ideally, two sets of hardware with slightly different aerodynamics will be tested back-to-back to bracket the design and provide data for a sensitivity analysis. At completion of the test program, the rig and component hardware will be torn down and assessed to determine if any conditions exist that may have affected the test data, such as tip rubs or damage to any of the hardware or instrumentation. The test data will be reduced and analyzed and compared to pre-test predicted maps. The maps used in the cycle model will be updated to reflect actual performance and the mission analysis will be re-run to determine the effects of the status updates on the overall mission performance.

The program schedule shows milestones for major reviews and on-site meetings at the test facility. A final report will be compiled and submitted at month 36 .

A ROM cost estimate for the proposed 36-month VSPT experiment program shown in Figure 4.3 is $\$ 4.5 \mathrm{M}$, broken down as follows:

- Preliminary Design: $\$ 800,000$
- Detailed Design: $\$ 1,400,000$
- Component and rig hardware: $\$ 1,200,000$
- Testing: \$300,000
- Program management: $\$ 800,000$

This ROM represents an estimate of contractor cost to perform the design, build the hardware, conduct testing, and manage the effort. It does not include an estimate of costs for use of the test facility and support from NASA and government service contractors. If it is determined that the VSPT test components can be overhung directly from the facility bearing cartridge, eliminating the need for the dedicated component bearings and lube system, the cost to design and build the components would be reduced, and the total cost of the program could potentially be lower by as much as $\$ 200,000$.

### 5.0 Conclusions

In this study, a variable speed power turbine design was executed for a proposed Large Civil Tiltrotor. This application is unique in that it requires a turbine with far greater off-design capability than traditional propulsion related gas turbines. Airfoil incidence can change as much as $60^{\circ}$ between the high speed and low speed rotor settings. These large changes in incidence cause airfoil separations and large loading changes resulting in reduced efficiency. In order to address these large loading swings, a study was performed in which a methodical multiple design-point process was used to arrive at a flowpath that
is fundamentally speed insensitive. This is in direct contrast to other techniques such as variable geometry or a variable gear ratio transmission. The figure of merit used in this study was to minimize the fuel burn throughout the mission by weighting various performance conditions in such a way as to mimic a typical flight. Various designs were analyzed and traded against each other with a turbine meanline code and CFD calculations were used to validate the results. CFD consistently showed better negative incidence tolerance (high speed) than the 1-D meanline loss systems. This finding would suggest moving the design point selection to lower speed than the 1-D prediction. Any further research would require testing.

A component experiment program plan was proposed that can be accomplished within a 36 -month period. This program would design and fabricate a stand-alone rig to mate to the NASA GRC Single Spool Turbine Test Facility and take advantage of its capabilities to run the testing at full scale for the proposed LCTR application in an economical manner. A notional component test article design was proposed that emulates the configuration recommended for the LCTR engine, and which greatly minimizes rotordynamic issues that would be major concerns for alternative configurations.

The design methodology and technology investigated in this study can provide benefits to other systems beyond the LCTR. Any system that can benefit from improved off-design performance, whether turbofan, turboshaft, or turboprop, may be able to take advantage of the proposed approach to avoid the complexity and cost associated with traditionally variable geometry approaches. This includes not only aviation engines, but also ground power and automotive engines.
TABLE A．1．－SEA LEVEL STATIC（MRP） 100 PERCENT NPT


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| TABLE A.1.-Concluded. |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ----DUCTS---- | dPnorm | mN | Aphy | C_L | Uncharg | B1) | 0.0563 | 1.0000 | 1.0000 | 1.6163 | 1248.88 | 173.74 | 294.057 |
| Duct1 | 0.0000 | 0.4000 | 132.95 | $\mathrm{C}^{-}$ | Charg | B1> | 0.0916 | 1.0000 | 1.0000 | 2.4239 | 1661.69 | 282.22 | 294.057 |
| ICduct | 0.0020 | 0.4000 | 14.19 | $\mathrm{C}_{-}$ | Uncharg |  | 0.1751 | 1.0000 | 1.0000 | 4.6347 | 1661.69 | 282.22 | 610.864 |
| Duct6 | 0.0000 | 0.2500 | 5.85 |  |  |  |  |  |  |  |  |  |  |
| Duct43 | 0.0000 | 0.3000 | 19.55 |  |  |  |  |  |  |  |  |  |  |
| ITduct | 0.0000 | 0.2000 | 89.22 |  |  |  |  |  |  |  |  |  |  |
| Duct12 | 0.0000 | 0.3000 | 292.50 |  |  |  |  |  |  |  |  |  |  |
| ---SHAFTS---- | Nmech | trq in | pwr in |  |  |  |  |  |  |  |  |  |  |
| HP_Shaft | 14800.0 | 1613.4 | 4546.4 |  |  |  |  |  |  |  |  |  |  |
| IP_Shaft | 12000.0 | 2984.7 | 6819.3 |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{LP}_{-}^{-}$Shaft | 15000.0 | 2626.1 | 7500.0 |  |  |  |  |  |  |  |  |  |  |
| ---BURNERS--- | TtOut | eff | dPnorm | Wfuel | FAR |  | EINOX | ppm |  |  |  |  |  |
| Burner | 3660.00 | 1.0000 | 0.0200 | 0.71702 | 0.03695 |  |  |  |  |  |  |  |  |
| ---NOZZLES--- | PR | Cfg | CdTh | Cv | Ath |  | MNth | Vact | Pg |  |  |  |  |
| Nozzle | 1.050 | 0.9900 | 1.0000 | 0.9900 | 320.24 |  | 0.271 | 500.5 | 457.5 |  |  |  |  |

TABLE A.2.-2,000 ALTITUDE, $+45^{\circ} \mathrm{F}$ DAY, HOVER (NOT AT MAXIMUM POWER) 100 PERCENT NPR


| TURBOMACHINERY |  | perpornance | data |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Wc | PR | eff | Ne | TR | efPoly | pwr | sma | SNW |  |  |  |  |
| LPC | 23.54 | 11.521 | 0.8564 | 11309.372 | 2.1462 | 0.8953 | -4691.4 | 21.06 | 21.55 |  |  |  |  |
| HPC axi | 3.00 | 1.135 | 0.8893 | 9597.988 | 1.0388 | 0.8912 | -354.2 | 19.71 | 11.97 |  |  |  |  |
| HPC cens | 2.48 | 2.517 | 0.8579 | 9416.842 | 1.3185 | 0.8736 | -2858.1 | 22.75 | 21.37 |  |  |  |  |
| HPT | 1.29 | 2.077 | 0.8502 | 245.635 | 1.1376 | 0.8209 | 3212.4 |  |  |  |  |  |  |
| LPT | 3.17 | 3.200 | 0.8516 | 225.094 | 1.2476 | 0.8285 | 4691.4 |  |  |  |  |  |  |
| PowerT | 9.64 | 4.612 | 0.8266 | 327.916 | 1.3431 | 0.7964 | 4639.6 |  |  |  |  |  |  |
| TURBOMACHINERY MAP DATA |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | WcMap | PRmap | effinap | NcMap | R/Parm | = WcDea | a PRdea | a_effD | an |  |  |  |  |
| LPC | 24.61 | 7.278 | 0.8637 | 94.245 | 1.8331 | 0.956433 | $\overline{1} .6759$ | -0.9916 |  |  |  |  |  |
| HPC axi | 29.63 | 1.200 | 0.8542 | 0.987 | 1.9397 | 0.100682 | 0.6728 | 1.03 |  |  |  |  |  |
| HPC cens | 29.62 | 3.086 | 0.8515 | 0.987 | 2.0262 | 0.083407 | 0.7273 | 1.00 |  |  |  |  |  |
| HPT | 30.15 | 5.998 | 0.9290 | 100.408 | 5.9980 | 0.042649 | 4.6409 | 0.915 |  |  |  |  |  |
| LPT | 149.98 | 5.735 | 0.9294 | 99.582 | 5.7349 | 0.021123 | 2.1523 | 0.91 |  |  |  |  |  |
| PowerT | 172.96 | 1.763 | 0.8861 | 101.749 | 1.7630 | 0.055750 | 0.2112 | - 0.93 |  |  |  |  |  |
| ---INLETS---- |  | elam | Afs | Fram |  |  |  |  |  |  |  |  |  |
| Inlet | 1.0000 |  |  | 0.1 | C_LPTCharg Bly |  | $\begin{aligned} & \text { Wb/Win } \\ & 0.0214 \end{aligned}$ | $\begin{aligned} & \text { hacale } \\ & 1.0000 \end{aligned}$ | $\begin{aligned} & \text { Pacale } \\ & 1.0000 \end{aligned}$ | $\begin{array}{r} \text { W } \\ 0.4525 \end{array}$ | $\begin{array}{r} \mathrm{Tt} \\ 1240.86 \end{array}$ | $\begin{array}{r} \mathrm{ht} \\ 171.69 \end{array}$ | $\begin{gathered} \mathrm{Pt} \\ 66.179 \end{gathered}$ |


TABLE A．3．－CRUISE MISSION $1,303.4 \mathrm{kn}, 28,000$ ALTITUDE，$+0^{\circ} \mathrm{F}$ DAY，INITIAL CRUISE POWER LEVEL， 100 PERCENT NPR rpm／650 ROTOR TIP SPEED








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$\begin{array}{lrr} & \text { Wc } & \text { PR } \\ \text { LPC } & 27.88 & 14.061 \\ \text { HPC＿axi } & 3.02 & 1.135 \\ \text { HPC＿cen＞} & 2.50 & 2.566 \\ \text { HPT } & 1.29 & 2.093 \\ \text { LPT } & 3.17 & 3.365 \\ \text { PowerT } & 10.06 & 6.499\end{array}$
$\begin{array}{lcc} & \\ \text { TURBOMACHINERY MAP } & \text { DATA } \\ & \text { WcMap } & \text { PRmap } \\ \text { LPC } & 29.15 & \text { B．793 } \\ \text { HPC＿axi } & 29.90 & 1.201 \\ \text { HPC＿cens } & 29.90 & 3.153 \\ \text { HPT } & 30.16 & 6.027 \\ \text { LPT } & 149.97 & 6.091 \\ \text { PowerT } & 180.41 & 2.162\end{array}$

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TABLE A．4．－CRUISE MISSION $1,303.4 \mathrm{kn}, 28,000$ ALTITUDE，$+0^{\circ} \mathrm{F}$ DAY，INITIAL CRUISE POWER LEVEL


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| TABLE A.4.-Concluded. |  |  |
| :--- | :--- | :--- |
| C_LPTUncharg B1s | 0.0563 | 1.0000 |
| C-HPTCharg | B1s | 0.0916 |
| C_HPTUncharg B1s | 0.1751 | 1.00000 |
| C_HP |  |  |



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## Appendix B.-Definitions

$\mathrm{AN}^{2}$ is an indicator of blade pull stress. This stems from the fact that the pull stress of a spinning radial cylinder is proportional to $\mathrm{AN}^{2}$. A good rule of thumb is that blade stress will be proportional to $\mathrm{AN}^{2}$ at the rate of 10 ksi per $10 \mathrm{E} 9 \mathrm{AN}^{2}$. For example, a well designed turbine blade with nickel based alloys operating at $50 \mathrm{E} 9 \mathrm{AN}^{2}$ will have an average pull stress of about 50 ksi .

$$
\mathrm{AN}^{2} \equiv\left(\text { Flowpath Annulus area in. }{ }^{2}\right) \mathrm{X}\left(\mathrm{rpm}^{2}\right)
$$

Rim speed combined with $\mathrm{AN}^{2}$ is an indicator of disk loading. Rim speed is calculated using the TE hub radius.

$$
\operatorname{Rim}_{\text {Speed }}(\mathrm{ft} / \mathrm{s})=\text { Radius }_{\text {Hub }}(\mathrm{in} .) / 12 . * \text { rpm } * \pi / 30 .
$$



Figure B.1.-Turbine $\mathrm{AN}_{2}$ and Rim Speed Definitions

## Appendix C.-FlowPath Details



High CXIU

| \% Speed | Design RPM | Fuel Burn\% | ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 53.8 | 8045 | -3.29 | 73.34 | 68.62 | 69.34 | 91.39 |
| 69.2 | 10343 | -7.88 | 88.33 | 84.71 | 84.12 | 88.62 |
| 84.6 | 12642 | 1.41 | 92.95 | 90.84 | 90.63 | 74.87 |
| 100.0 | 14941 | 23.20 | 91.25 | 91.58 | 92.80 | 57.42 |

\%Speed Work Coeff. Flow Coeff.

| 54 | 1.68 | 0.813 |
| ---: | ---: | ---: |
| 100 | 0.5 | 0.448 |

Figure C.1.-High Cx/U Four Stage


## Low CXIU

| \% Speed | Design RPM | Fuel Burn\% | ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 53.8 | 8045 | -2.22 | 69.98 | 66.62 | 69.30 | 90.20 |
| 69.2 | 10343 | -7.80 | 87.58 | 83.60 | 82.85 | 89.14 |
| 84.6 | 12642 | -1.84 | 92.00 | 89.60 | 89.44 | 78.75 |
| 100.0 | 14941 | 24.30 | 89.29 | 89.78 | 91.43 | 57.00 |


| \%Speed | Work Coeff. | Flow Coeff. |
| ---: | ---: | ---: |
| 54 | 1.66 | 0.532 |
| 100 | 0.49 | 0.3 |

Figure C.2.-Low Cx/U Four Stage


## 3 Stg

| \% Speed | Design RPM | Fuel Burn\% | ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 53.8 | 8045 | -1.11 | 70.57 | 66.14 | 67.52 | 89.72 |
| 69.2 | 10343 | -4.51 | 78.24 | 74.89 | 74.04 | 89.63 |
| 84.6 | 12642 | -7.19 | 93.53 | 91.76 | 91.60 | 84.44 |
| 100.0 | 14941 | -6.36 | 92.35 | 92.49 | 93.53 | 66.26 |

\%Speed Work Coeff. Flow Coeff.

| 54 | 2.11 | 0.722 |
| ---: | :--- | :--- |
| 100 | 0.63 | 0.368 |

Figure C.3.-Three Stage


## 4 Stg Hi Loading (1)

\% Speed Design RPM Fuel Burn\%

| 53.8 | 8045 | -0.84 |
| ---: | ---: | ---: |
| 69.2 | 10343 | -7.98 |
| 84.6 | 12642 | -8.31 |
| 100.0 | 14941 | -3.68 |


| ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: |
| 78.77 | 71.42 | 69.10 | 87.45 |
| 90.15 | 87.28 | 87.13 | 87.37 |
| 93.67 | 92.32 | 92.37 | 85.64 |
| 93.96 | 93.59 | 94.26 | 79.31 |


| \%Speed | Work Coeff. | Flow Coeff. |
| ---: | ---: | ---: |
| 54 | 2.826 | 1.008 |
| 100 | 0.828 | 0.467 |

Figure C.4.-Four Stage High Loading (1)


## 4 Stg Hi Loading (2)

| \% Speed | Design RPM | Fuel Burn\% | ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 54.0 | 7000 | 3.62 | 76.30 | 65.58 | 63.81 | 85.34 |
| 69.3 | 8988 | -6.27 | 89.07 | 85.79 | 86.38 | 85.44 |
| 84.7 | 10975 | -8.11 | 92.90 | 91.62 | 92.32 | 85.12 |
| 100.0 | 12963 | -7.29 | 93.67 | 93.29 | 94.31 | 83.67 |

\%Speed Work Coef

| 54 | 3.116 | 0.832 |
| ---: | ---: | ---: |
| 100 | 0.919 | 0.377 |

Figure C.5.-Four Stage High Loading (2)


## 6 Stage A

| \% Speed | Design RPM | Fuel Burn\% | ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 54.0 | 7000 | 1.01 | 69.66 | 63.25 | 64.03 | 89.39 |
| 69.3 | 8988 | -6.27 | 87.12 | 83.61 | 82.71 | 87.05 |
| 84.7 | 10975 | 0.50 | 92.74 | 90.47 | 90.61 | 75.84 |
| 100.0 | 12963 | 20.42 | 92.19 | 92.22 | 93.34 | 59.02 |

\%Speed Work Coeff. Flow Coeff.
$54 \quad 2.031 \quad 1.037$
$100 \quad 0.611 \quad 0.541$

Figure C.6.-SixStage High Cx/U


## 3 Stage B

| \% Speed | Design RPM | Fuel Burn\% | ETA 1 | ETA 2 | ETA 3 | ETA 4 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 54.0 | 6790 | 4.91 | 65.66 | 61.47 | 62.07 | 85.80 |
| 69.3 | 8718 | -5.68 | 87.75 | 83.89 | 83.69 | 85.81 |
| 84.7 | 10646 | -8.02 | 92.48 | 91.06 | 91.67 | 85.58 |
| 100.0 | 12574 | -7.45 | 93.23 | 92.82 | 93.98 | 84.00 |


| \%Speed | Work Coeff. | Flow Coeff. |
| ---: | ---: | ---: |
| 54 | 2.991 | 0.8423 |
| 100 | 0.966 | 0.4147 |

Figure C.7.—Three Stage B


## 4 Stage C

\% Speed Design RPM Fuel Burn\%

| 54.0 | 6200 | 4.41 |
| ---: | ---: | ---: |
| 69.3 | 7960 | -5.8 |
| 84.7 | 9721 | -6.21 |
| 100.0 | 11482 | 0.60 |
|  |  |  |
| eed Work Coeff. | Flow Coeff. |  |
| $\mathbf{5 4}$ | $\mathbf{2 . 9 2 5}$ | $\mathbf{1 . 0 9 0 2 5}$ |
| $\mathbf{1 0 0}$ | $\mathbf{0 . 8 6 4}$ | $\mathbf{0 . 5 0 7}$ |

\%Speed Work Coeff. Flow Coeff.

ETA 1 ETA 2 ETA 3 ETA 4
4.41 5.84
6.21
0.60
68.91
87.2
92.48
93.00
60.48
83.39
90.80
92.65
62.16 83.22 91.14
93.82
86.31
86.26
83.40 74.85

Figure C.8.-Four Stage C


Figure C.9.—Smith Curve of All Turbines


Figure C.10.—Design Speed Comparison: All Turbines

## Appendix D.-Four Stage CFD Analysis

The Four Stage power turbine presented in this study was analyzed using a Williams International proprietary CFD code called VORTEX. VORTEX is a 3-D, finite volume, explicit time marching flow solver. The solution assumes steady-state, time averaged flow. Each blade row is analyzed in the relative frame using mixing planes to jump from rotating to stationary blade rows. The mixing planes assure conservation of mass, momentum and energy. The performance used to analyze the turbine was based on the mission point 4 (see Table 2.1 and Table A.4) with small modifications. Point 4 corresponds to a 54 percent speed cruise condition. The CFD uses a fictitious design point. To execute the design, point 4 is used for the thermodynamics, but the speed is increased to 75 percent. The pressure ratio was also modified. The NPSS model had an efficiency at point 4 of 78.6 percent and an efficiency at point 3 ( 100 percent speed) of 84.9 percent. The predicted efficiency of this four stage is 86.54 and 90.74 percent respectively which requires less PR in order to meet the power requirement. This would be a significant rematch to the engine and would require additional cycle work, possible including a reduction in engine core size. Below is a summary of the parameters used in the CFD as well as the cycle targets. The inlet temperature and pressures shown are mass averaged values taken from the converged solution and differ slightly from the targets. Typically the inlet profiles can be adjusted as the simulation/design matures to hone in on the target values. The inlet mass flow is approximately 2.7 percent high which would require closing airfoil throat areas to assure proper engine matching.

|  | Cycle | CFD |
| :---: | :---: | :---: |
| - PT | 31.0 psia | 30.93 psia |
| TT | $1749{ }^{\circ} \mathrm{R}$ | $1696{ }^{\circ} \mathrm{R}$ |
| Mdot | $12.04 \mathrm{lbm} / \mathrm{s}$ | $12.37 \mathrm{lbm} / \mathrm{s}$ |
| - rpm |  | 11174 (75 percent speed) |
| - PR | 6.18 | 5.6 |
| ETA | 78.6-84.9 percent | 92.9 percent ${ }^{1}$ |
| No leakage, cooling or tip clearance: MeanLine prediction $=93.55$ percent @ PR $=5.78$ |  |  |

The geometry used in the CFD did not have fillets between the airfoil and endwall intersection. The following are surface static pressure loading plots of each stage. The vane and blade are plotted together: Hub, Mean and Tip.

## D. 1 Stage 1

50\% Span


10\% Span


90\% Span

D. 2 Stage 2

10\% Span


50\% Span


90\% Span


## D. 3 Stage 3



50\% Span


90\% Span

D. 4 Stage 4

10\% Span




## Meanline Analysis of Design Point

 75\% Speed ( 11174 rpm)| Flow Parm. (Inlet) | 16.240 |  |
| :---: | :---: | :---: |
| Mass Flow | 12.040 |  |
| Efficiency | 92.8662\% |  |
| Flow Parm. (Exit) | 76.472 |  |
| Power (hp) | 2684.958 |  |
| Pressure Ratio (Total/Total) | 5.769 |  |
| Pressure Ratio (Total/Static) | 6.330 |  |
| Inlet Temp. (degrees R / F) | 1749.080 / | 1289.410 |
| TRIT (degrees R / F) | 1749.080 / | 1289.410 |
| Exit TT (degrees R / F) | 1165.389 / | 705.719 |
| Enthalpy Drop (BTU/lbm) | 39.608 |  |
| Ratio Specific Heats (Gamma) | 1.340 |  |
| Gas Constant (ft-lbf/degR/lbm) | 53.374 |  |
| Avg. Work Coefficient | 1.459 |  |
| Core Flow (lbm/s) | 12.040 |  |
| Nozzle Cooling | 0.000\% |  |
| Rotor Cooling | 0.000\% |  |


| Rotor Summary: |  |  |  |  |  |  |
| :--- | :--- | :--- | :---: | ---: | ---: | ---: |
| Title |  | Reaction | WorkCoef | Cm/U | AN^2 | RimSpeed |
| ROTOR: STAGE | 1 | $48.000 \%$ | 1.470 | 0.726 | 11.390 | 689.720 |
| ROTOR: STAGE | 2 | $47.000 \%$ | 1.490 | 0.563 | 18.720 | 671.266 |
| ROTOR: STAGE | 3 | $45.000 \%$ | 1.496 | 0.551 | 27.121 | 617.638 |
| ROTOR: STAGE | 4 | $40.000 \%$ | 1.384 | 0.702 | 32.240 | 567.395 |


(based on TRIT \& 1st rpm found)

|  | Vane | Blade |
| :---: | :---: | :---: |
| Turning | 58.1564 | 78.4812 |
|  | 85.9121 | 90.6473 |
|  | 92.4592 | 93.8363 |
|  | 88.4801 | 81.7638 |
| RVR | 2.0792 | 1.9532 |
|  | 2.0969 | 2.2366 |
|  | 2.4743 | 2.4077 |
|  | 2.4598 | 2.0300 |
| Convergence Ratio | 1.8046 | 1.6902 |
|  | 1.7790 | 1.8930 |
|  | 2.0383 | 1.9791 |
|  | 1.9660 | 1.6718 |
| Reynolds \#, SS/1000. | 179.2235 | 152.0635 |
|  | 145.1666 | 126.1129 |
|  | 118.1032 | 93.2357 |
|  | 80.7626 | 59.2618 |
| LE Mach \# (relative) | 0.2733 | 0.2985 |
|  | 0.2872 | 0.2673 |
|  | 0.2553 | 0.2647 |
|  | 0.2783 | 0.3262 |
| TE Mach \# (relative) | 0.5824 | 0.5983 |
|  | 0.6181 | 0.6148 |
|  | 0.6509 | 0.6579 |
|  | 0.7092 | 0.6836 |
| LE Swirl (relative) | 0.0000 | 17.9747 |
|  | -22.1197 | 24.7990 |
|  | -25.4011 | 27.7528 |
|  | -24.2202 | 23.9420 |
| TE Swirl (relative) | 58.1564 | -60.3947 |
|  | 63.7159 | -65.7272 |


|  | 66.9995 | -65.9808 |
| :---: | :---: | :---: |
|  | 64.2247 | -57.7576 |
| Total Loss \% | 1.4064 | 1.9212 |
|  | 2.0358 | 2.1632 |
|  | 2.1774 | 2.3416 |
|  | 2.1681 | 2.2357 |
| Zweifel | 1.0569 | 1.0284 |
|  | 1.0437 | 1.0370 |
|  | 1.0391 | 1.0437 |
|  | 1.0225 | 1.0499 |
| Throat Area | 37.6309 | -42.5160 |
|  | 49.0312 | -59.0217 |
|  | 69.3542 | -85.1203 |
|  | 102.2492 | -131.8714 |
| Number of Airfoils | 52 | 65 |
|  | 62 | 62 |
|  | 59 | 65 |
|  | 67 | 76 |
| Exit Mach/Swirl (Absolute) | 0.3718 | -9.3783 |

# Appendix E.-Meanline Results for Four Stage: High Loading 1 

Rotor Summary at Design Speed of 54 percent:

| Title | Reaction | WorkCoef | $\mathrm{Cm} / \mathrm{U}$ | $\mathrm{AN}^{2}$ | RimSpeed |
| :--- | :---: | :---: | :---: | ---: | ---: |
| ROTOR: STAGE 1 | $48.000 \%$ | 2.826 | 1.072 | 5.902 | 496.707 |
| ROTOR: STAGE 2 | $45.000 \%$ | 2.840 | 0.857 | 9.700 | 483.381 |
| ROTOR: STAGE 3 | $45.000 \%$ | 2.863 | 0.880 | 14.081 | 444.190 |
| ROTOR: STAGE 4 | $39.992 \%$ | 2.774 | 1.224 | 16.650 | 410.626 |
| Overall Efficiency $=87.5 \%$ |  |  |  |  |  |

Rotor Summary @ Design Speed 100\%:

| Title | Reaction | WorkCoef | $\mathrm{Cm} / \mathrm{U}$ | $\mathrm{AN}^{2}$ | RimSpeed |
| :--- | :---: | :---: | :---: | :---: | :---: |
| ROTOR: STAGE 1 | $48.000 \%$ | 0.834 | 0.539 | 20.240 | 919.819 |
| ROTOR: STAGE 2 | $45.000 \%$ | 0.848 | 0.416 | 33.265 | 895.143 |
| ROTOR: STAGE 3 | $45.000 \%$ | 0.851 | 0.402 | 48.287 | 822.569 |
| ROTOR: STAGE 4 | $40.000 \%$ | 0.778 | 0.512 | 57.098 | 760.413 |
| Overall Efficiency $=94 \%$ |  |  |  |  |  |

## Airfoil Summary

|  | 54\% Speed |  | 100\% Speed |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Vane | Blade | Vane | Blade |
| Turning | 59.3261 | 101.7896 | 57.7106 | 51.4604 |
|  | 110.8252 | 114.7838 | 58.0856 | 58.7734 |
|  | 115.4375 | 116.0826 | 53.8484 | 56.6190 |
|  | 110.8802 | 100.6000 | 52.2701 | 50.9701 |
| Vexit/Vinlet | 2.2231 | 1.7296 | 2.0611 | 2.0179 |
|  | 1.6517 | 1.6362 | 2.2851 | 2.4019 |
|  | 1.8324 | 1.7477 | 2.6784 | 2.6977 |
|  | 1.7983 | 1.5571 | 2.6875 | 2.2304 |
| Reynolds \#, SS/1000. | 192.2316 | 162.2900 | 176.8202 | 166.8413 |
|  | 147.8500 | 121.7398 | 160.8162 | 137.0289 |
|  | 112.3183 | 87.5698 | 136.1440 | 106.9008 |
|  | 73.1437 | 53.5719 | 94.8810 | 66.7247 |
| LE Mach \# (relative) | 0.2730 | 0.3809 | 0.2730 | 0.2876 |
|  | 0.4105 | 0.4037 | 0.2644 | 0.2426 |
|  | 0.3843 | 0.4147 | 0.2332 | 0.2325 |
|  | 0.4390 | 0.5105 | 0.2532 | 0.2931 |
|  | 54\% Spee |  | 100\% Speed |  |


|  | Vane | Blade | Vane | Blade |
| :---: | :---: | :---: | :---: | :---: |
| TE Mach \# (relative) | 0.6244 | 0.6770 | 0.5764 | 0.5956 |
|  | 0.6956 | 0.6769 | 0.6213 | 0.5993 |
|  | 0.7258 | 0.7479 | 0.6439 | 0.6480 |
|  | 0.8204 | 0.8226 | 0.7056 | 0.6759 |
| LE Swirl (relative) | 0.0000 | 39.4746 | 0.0000 | -9.0460 |
|  | -46.1872 | 48.9328 | 5.9468 | -6.6781 |
|  | -48.6347 | 50.4989 | 13.3548 | -9.6122 |
|  | -47.9455 | 44.9543 | 12.4835 | -7.2519 |
| TE Swirl (relative) | 59.3261 | -62.1228 | 57.7106 | -60.5652 |
|  | 64.5339 | -65.7028 | 64.0554 | -65.4882 |
|  | 66.7344 | -65.4703 | 67.2378 | -66.2728 |
|  | 62.8947 | -55.5671 | 64.7740 | -58.2441 |
| Total Loss \% | 1.6196 | 3.4411 | 1.3734 | 1.4617 |
|  | 3.8016 | 3.8811 | 1.5134 | 1.5536 |
|  | 3.8187 | 4.4511 | 1.6540 | 1.6506 |
|  | 4.1192 | 5.0666 | 1.6129 | 1.5247 |
| Zweifel | 1.0550 | 1.0259 | 1.0649 | 1.0237 |
|  | 1.0657 | 1.0499 | 1.0140 | 1.0355 |
|  | 1.0641 | 1.0576 | 1.0127 | 1.0284 |
|  | 1.0377 | 1.0356 | 1.0124 | 1.0190 |
| Number of Airfoils | 51 | 76 | 52 | 50 |
|  | 74 | 77 | 50 | 49 |
|  | 72 | 82 | 45 | 49 |
|  | 88 | 105 | 49 | 56 |
| Exit Mach/Swirl (Absolute) | 0.5549 | -32.7647 | 0.3768 | 18.4055 |

## Appendix F.-Disk Sizing

A 2-D disk sizing tool was used to approximate disk mass and structural feasibility. Below is a screen shot of disks that were designed based on achieving 25 percent over speed capability with typical disk alloys. The resulting weight and mass moment of inertia of each disk plus the blades is shown.


Figure F.1.-Approximate Disk Size

## Appendix G.-Efficiency and Reaction Definitions

The scope of this work is concentrated on understanding speed variations and the impact to turbine efficiency. In order to simplify this understanding, the analysis presented in this report does not consider cooling flows. This simplifies the efficiency definition. The efficiency numbers presented in this report are calculated assuming ideal gas as follows.

$$
\eta \equiv \frac{\text { ActualPower }}{\text { IdealPower }}=\frac{\Delta \mathrm{Tt}}{\operatorname{Tin} *\left(1-\operatorname{Pr} \frac{1-\gamma}{\gamma}\right)}
$$

where:
$\mathrm{Pr}=$ Total Pressure at inlet / Total Pressure at outlet
$\Delta \mathrm{Tt}=$ Total Temperature at inlet - Total Temperature at outlet
Tin = Total temperature at inlet
$\gamma$ is the ratio of specific heats taken at the average of the inlet and exit Total Temperatures.
In this work, stage reaction refers to pressure reaction defined as the static pressure drop across the rotor normalized by the static pressure drop across the whole stage.

$$
\text { Re action } \equiv\left(\frac{\mathrm{Ps}_{\text {RotorLE }}-\mathrm{Ps}_{\text {RotorTE }}}{\mathrm{Ps}_{\text {NozzleLE }}-\mathrm{Ps}_{\text {RotorTE }}}\right)
$$

## Appendix H.-NPSS Output for Critical Mission Point

TABLE H.1.-65 PERCENT DESIGN SPEED TAKE OFF


[^1]TABLE H.2.-65 PERCENT DESIGN SPEED CLIMB




TABLE H.4.-75 PERCENT DESIGN SPEED TAKE OFF


TABLE H.5.-75 PERCENT DESIGN SPEED CLIMB


TABLE H.6.-75 PERCENT DESIGN SPEED CRUISE


TABLE H.7.-85 PERCENT DESIGN SPEED TAKE OFF

TABLE H.8.-85 PERCENT DESIGN SPEED CLIMB


TABLE H.9.- 85 PERCENT DESIGN SPEED CRUISE


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    岑水
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    | :--- | :---: | :---: | :---: | :---: |
    | TURBOMACHINERY MAP | DATA |  |  |  |
    |  | WcMap | PRmap | effMap |  |
    | LPC | 29.33 | B．975 | 0.8538 |  |
    | HPC＿axi | 29.53 | 1.201 | 0.8552 |  |
    | HPC＿cens | 29.52 | 3.058 | 0.8516 |  |
    | HPT | 30.15 | 5.993 | 0.9286 |  |
    | LPT | 149.61 | 6.446 | 0.9246 |  |
    | PowerT | 187.94 | 2.094 | 0.8424 |  |
    |  |  |  |  |  |
    | －－INLETS－－－－ | eRam | Afa |  |  |
    | Inlet | 1.0000 | 107.98 |  |  |

[^1]:    

