

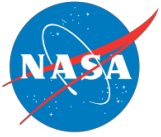
# **Large Scale Flutter Data for Design of Rotating Blades using Navier-Stokes Equations**

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## Acknowledgements

**Pieter Buning (LaRc) : Overset grid methods**

**Doug Boyd (LaRc) : Deforming grid in overset grid topology**

**Dennis Jespersen (ARC) : MPI for flow solver**

**Johnny Chang (ARC) : MPlexec based PBS script**

**David Barker (ARC) : MPlexec/MPI based PBS script**

**Project Support : Subsonic Rotary Wing (SRW)  
High End Computing (HEC)**



# Objective

- **Demonstrate a procedure to compute flutter data for rotating blades**
  - **Frequency domain approach**
  - **Large scale computations**
  - **Focusing on bending-torsion flutter**
  - **Navier-Stokes (NS) equations based Computational Fluids Dynamics (CFD) as a tool**



# Background

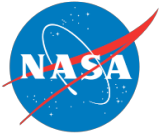
- **Bending-torsion flutter for rotating blade can occur**
  - while retreating (center of pressure moves back)
  - when flow is transonic (center of pressure moves back)
  - for high advance ratios
  - during stall
- **Large number of cases are needed for design**
- **Current fast procedures for solving flows use linear theory (LT)**
- **Higher fidelity equations are needed for accuracy**
- **Efficient use of supercluster is needed for large scale NS based computations**



## **Background (continued) Bending-Torsion Flutter in Flight**

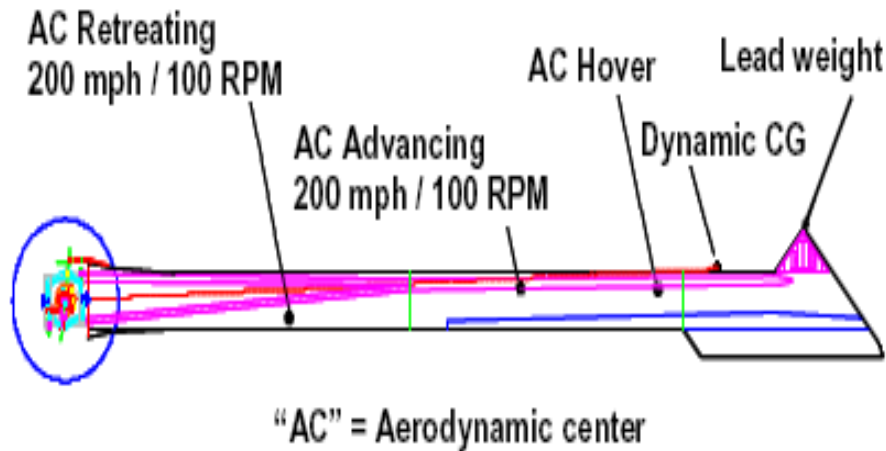


Camera following the blade



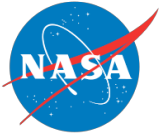
# Background (continued)

## High Advance Ratio ( $\mu \sim 1$ ) Configuration (Courtesy of Carter Aviation Technologies)



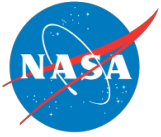
**Bending-torsion flutter  
is an issue during design**





# Approach

- **Flow equations are solved using the OVERFLOW (2.1c & 2.2c) code**
  - Reynolds averaged Navier-Stokes (RANS) equations
  - Pulliam-Chausse diagonal form of central difference solver
  - Spalart-Allmaras turbulence model
  - Structured overset grids with 2<sup>nd</sup> order spatial/temporal accuracy
  - Well validated for unsteady flow calculations
  - 1-D prescribed modal motion interface (AIAA 2012-4789)
- **Lagrange's structural equations of motion solved using FLUMOD**
  - Modal form
  - Frequency domain
- **Initial validation using**
  - Kernel Function and Doublet-Lattice based linear aero methods
  - Experiments for fixed blades
  - Comparison with fixed blade flutter
- **Use CFD grids previously validated for steady flows**  
(Doug Boyd, AHS 56 May 2009, Guruswamy J of Aircraft, May 2010)



## **U-g method (Velocity-damping)**

- **Assumes linear-superposition of modes similar to that in reduced-order modeling (ROM) methods**
- **Predicts on-set of flutter**
- **Built-in procedure in NASTRAN using doublet-lattice and Mach box linear aerodynamic theories**
  - **Routinely used by aerospace industry**
- **Extensively applied for fixed wings using NS equations**



# Frequency Domain Formulation

- With  $[\Phi]$  as modal matrix, displacements are expressed as

$$\{d\} = [\Phi] \{h\}$$

- Generalized displacements at flutter are  $\{h\} = \{\bar{h}\} e^{\omega(1+ig)t}$

$\omega$  = circular frequency,  $g$  = structural damping;  $t$  = time

- Complex Eigenvalue Eqn for bending  $\bar{h}_1$  and torsion  $\bar{h}_2$

$$\eta k_r^2 [[M] - [A]] \{\bar{h}\} = \lambda [K] \{\bar{h}\}$$

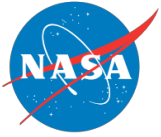
**Air-Mass Ratio**  $\eta = M_{11}/(\pi\rho R c^2)$     **Reduced Freq**  $k_r = 4\omega c / 3\Omega R$

**Eigen-Value**  $\lambda = \eta(1+ig)\omega_f^2 c^2 / 4S^2$  ;    **Flutter Speed**  $S = 2U/c\omega_2$

$\Omega$  = rotation speed;  $\omega_1, \omega_2, \omega_f$  = bending, torsion, flutter freq

$[M]$  = mass;  $[K]$  = stiffness.;  $c$  = chord;  $U$  = velocity;  $R$  = radius

- $[A]$  = aerodynamic matrix computed using RANS solver



# Aerodynamic Coefficients from RANS Solver

$$A_{11} = \int_0^R C_{l\delta} \Phi_1^2 \delta r \quad A_{12} = \int_0^R C_{l\alpha} \Phi_1 \Phi_2 \delta r$$
$$A_{21} = \int_0^R C_{m\delta} \Phi_2 \Phi_1 \delta r \quad A_{22} = \int_0^R C_{m\alpha} \Phi_2^2 \delta r$$

$\Phi_1$  and  $\Phi_2$  are bending and torsion modes, respectively

$C_{l\delta}(r) =$  Lift due to bending mode

$C_{l\alpha}(r) =$  Lift due to torsion mode

$C_{m\delta}(r) =$  Moment due to bending mode

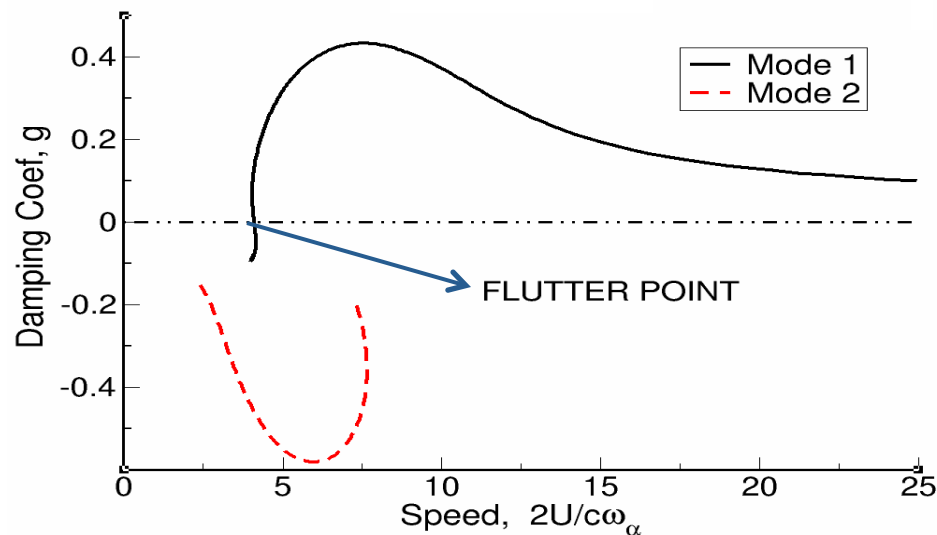
$C_{m\alpha}(r) =$  Moment due to torsion mode



# Flutter Solution Procedure

- Compute force responses for 2 modes and various frequencies at a given rotating speed ( $\Omega$ )
- Compute real/imaginary values of forces from Fourier analysis
- Solve Eigen-Value equation by varying the frequency and tracking  $g$
- Extract flutter point when  $g$  changes sign

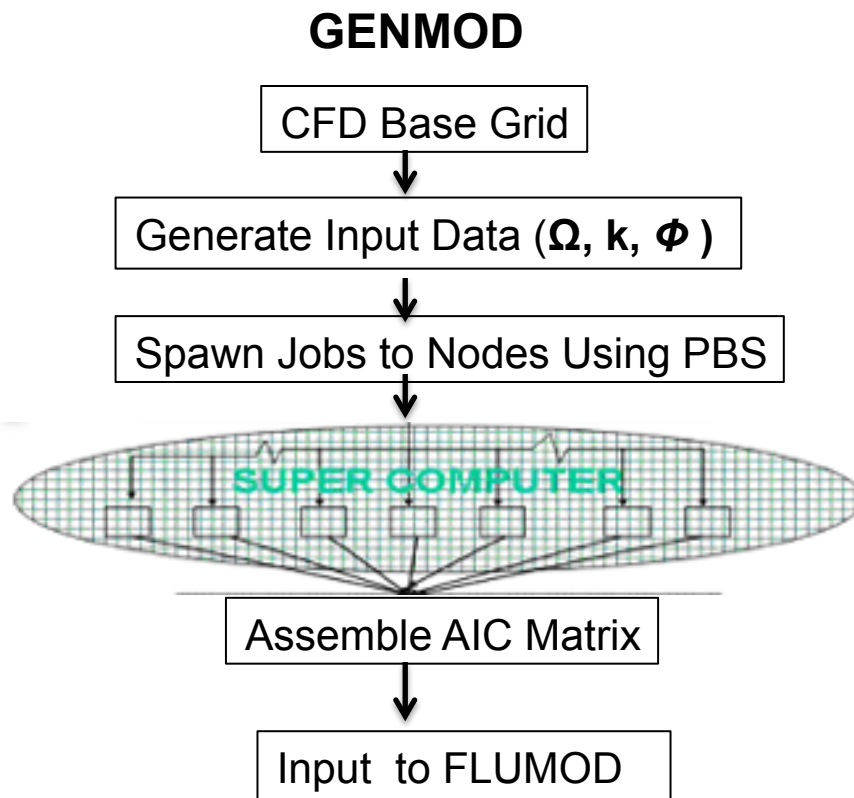
Typical U-g plot





# Parallel Computational Procedure

- Massively parallel computations
- Single job submission script to run all cases at same time using portable batch system (PBS)

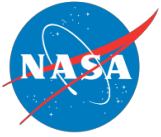


## Typical Timings

- 25 wall-clock hrs  
to run up to 1000  
responses for  
flexible wing



# VALIDATION AND DEMONSTRATIONS

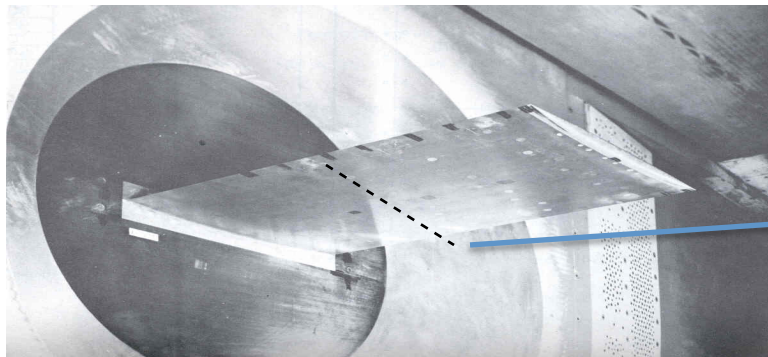


# Validation of Unsteady Pressures

Non-Rotating blade,  $M_\infty = 0.90$ , Reduced Freq. = 0.26,  $Re = 2.1 \times 10^6$

## Computations

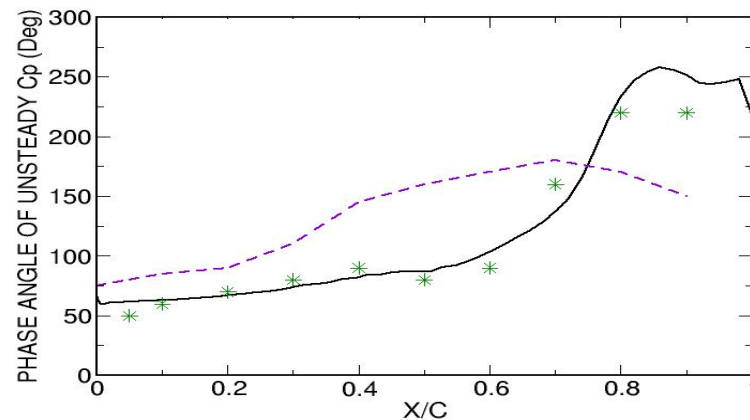
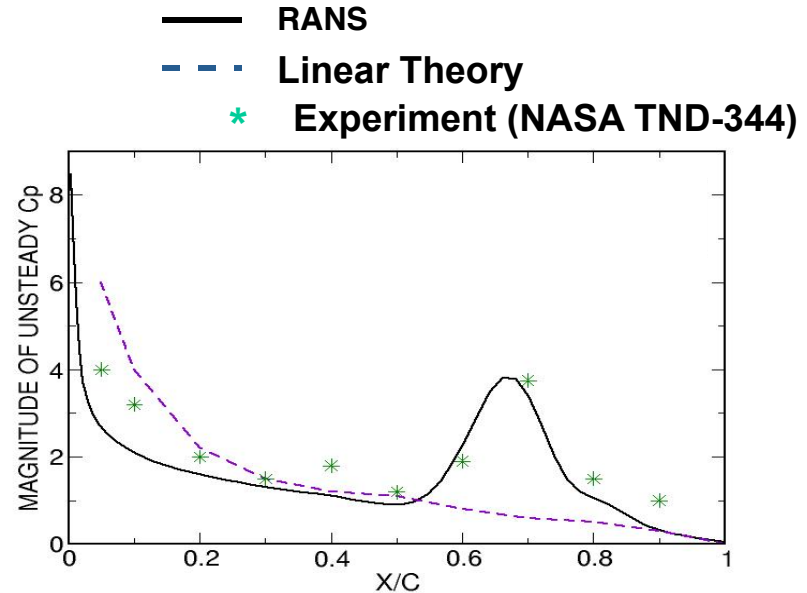
- C-H grid, 253K (151x35x48)
- 2400 time steps per cycle
- results at 4th cycle
- data taken at 50% with no wall viscous effects



NASA TND-344 (1960,ARC)

6% thick parabolic arc, Aspect Ratio = 5  
Blade oscillating in first flapping mode

## Unsteady $C_p$ at 50% Semispan





# Validation of Flutter Boundary

Non-rotating aeroelastic rectangular wing,  $Re = 4.5 \times 10^6$   
NASA TMX -79 (1959, LaRc), 6% Parabolic Arc, Aspect Ratio = 5

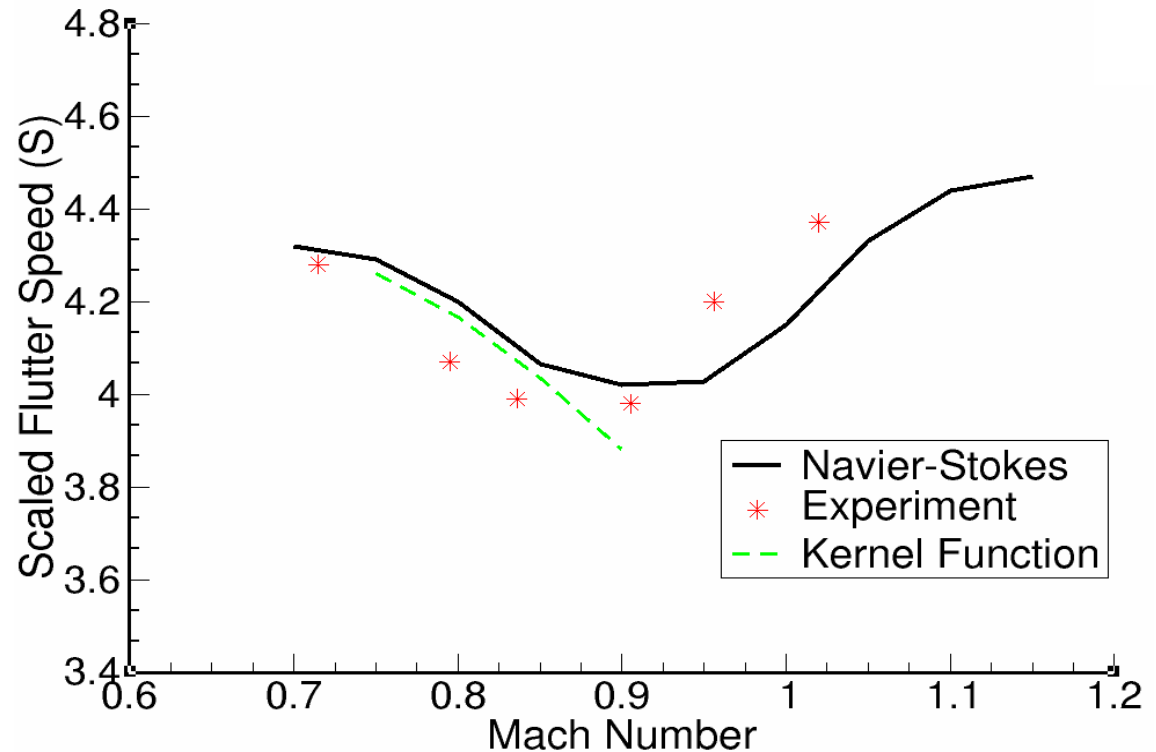
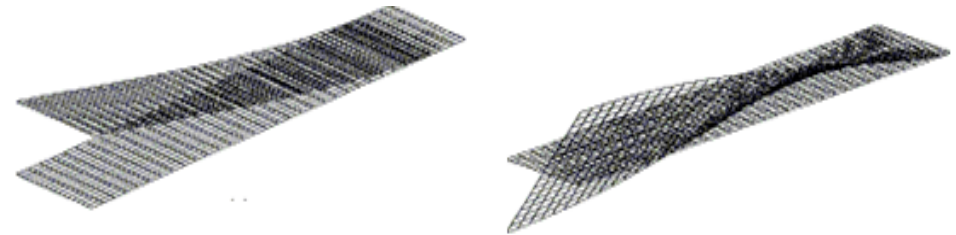
## Computations

- C-H grid, 253K points (151x35x48)
- 2400 steps per cycle
- 4 oscillations
- 2 modes, 5 frequencies, 10 Mach numbers

## Kernel Function

- NASA TP-2292 (1984)

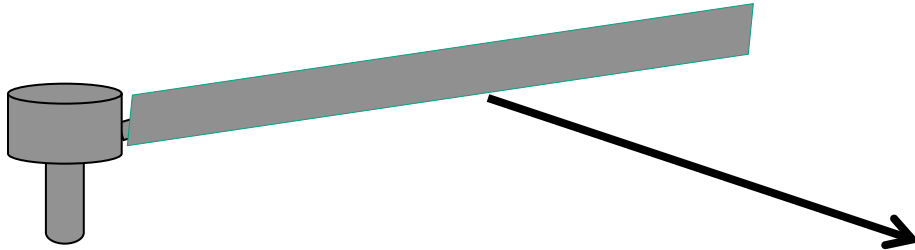
## Modes





# Demonstration for Single Rotating Blade

Hover,  $\theta_c = 10$  deg, Aspect ratio =16, NACA23012,  $Re = 15 \times 10^6$



## Grid

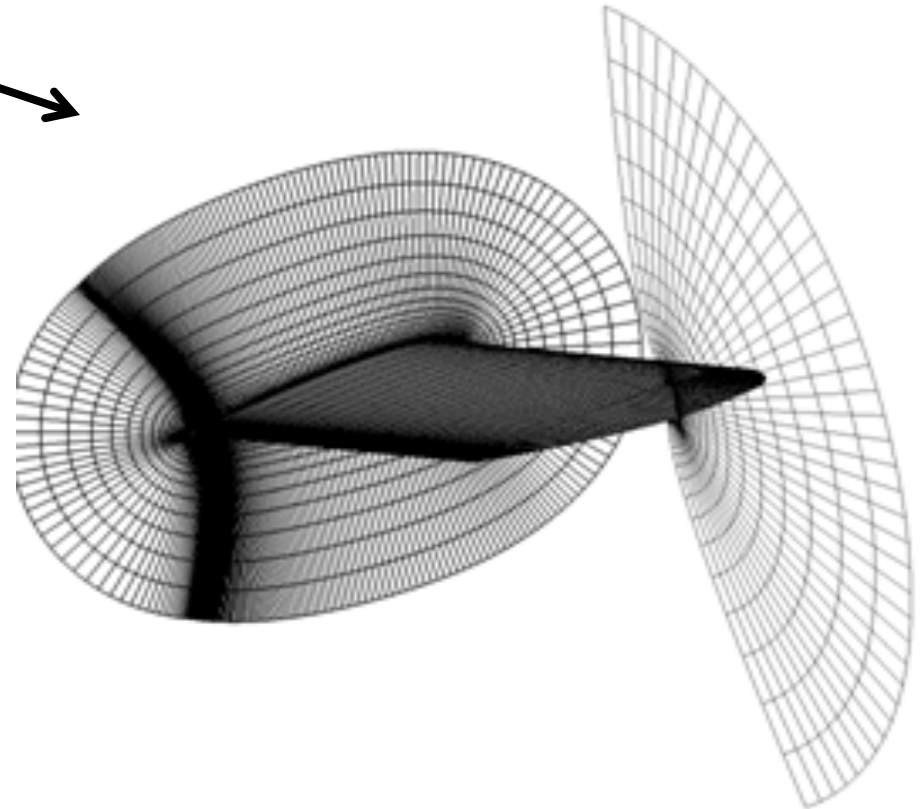
- Doug Boyd, 56<sup>th</sup> AHS, 2009
- $1.8 \times 10^6$ , 3 near body blocks
- outer boundaries  $\sim 10$  chords

## Structural Properties

$$\omega_1 / \omega_2 = 0.30$$

mass center = 45% chord

elastic axis = 25% chord

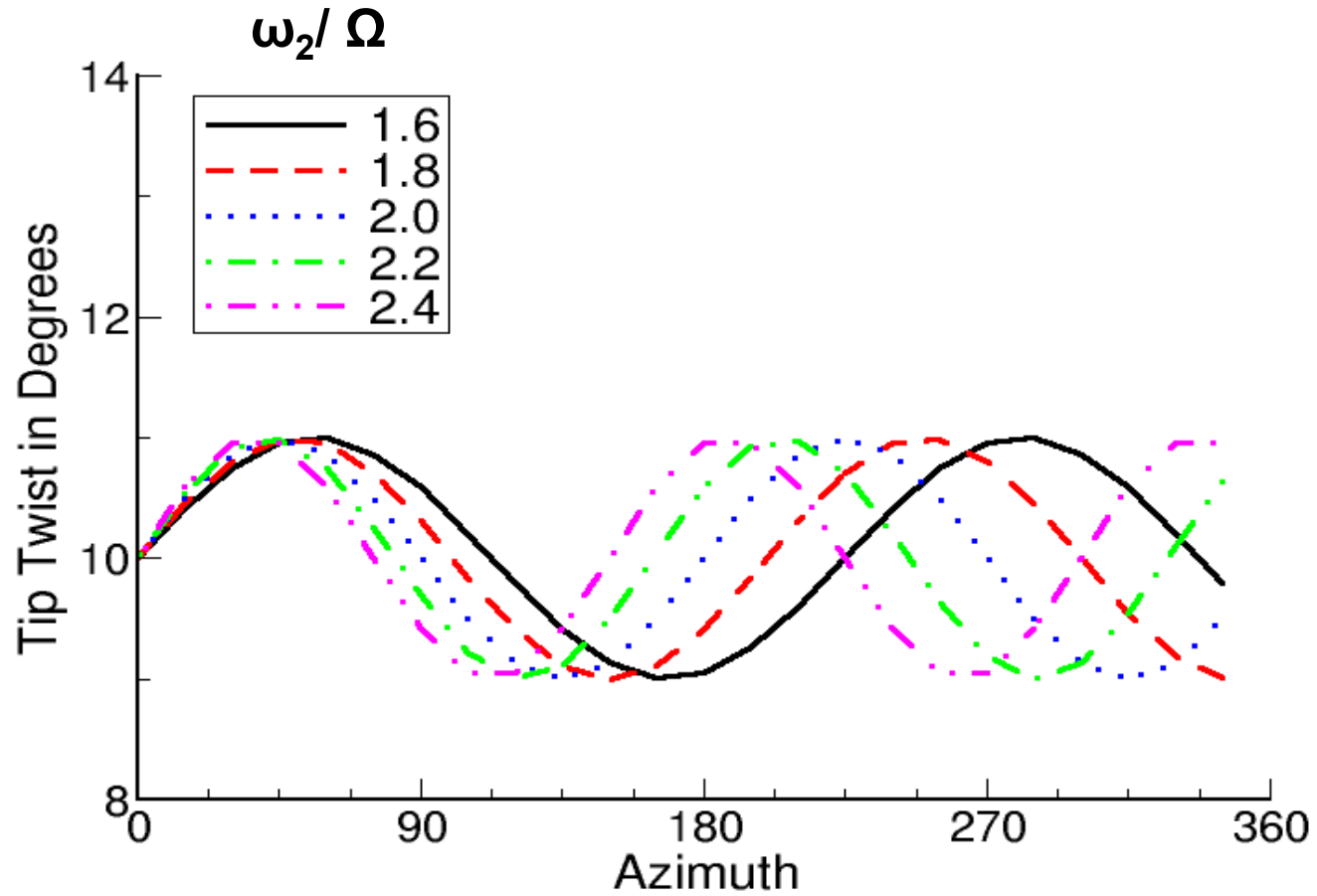


## Cases - 100

- 10 rotating speeds
- 2 modes
- 5 frequencies



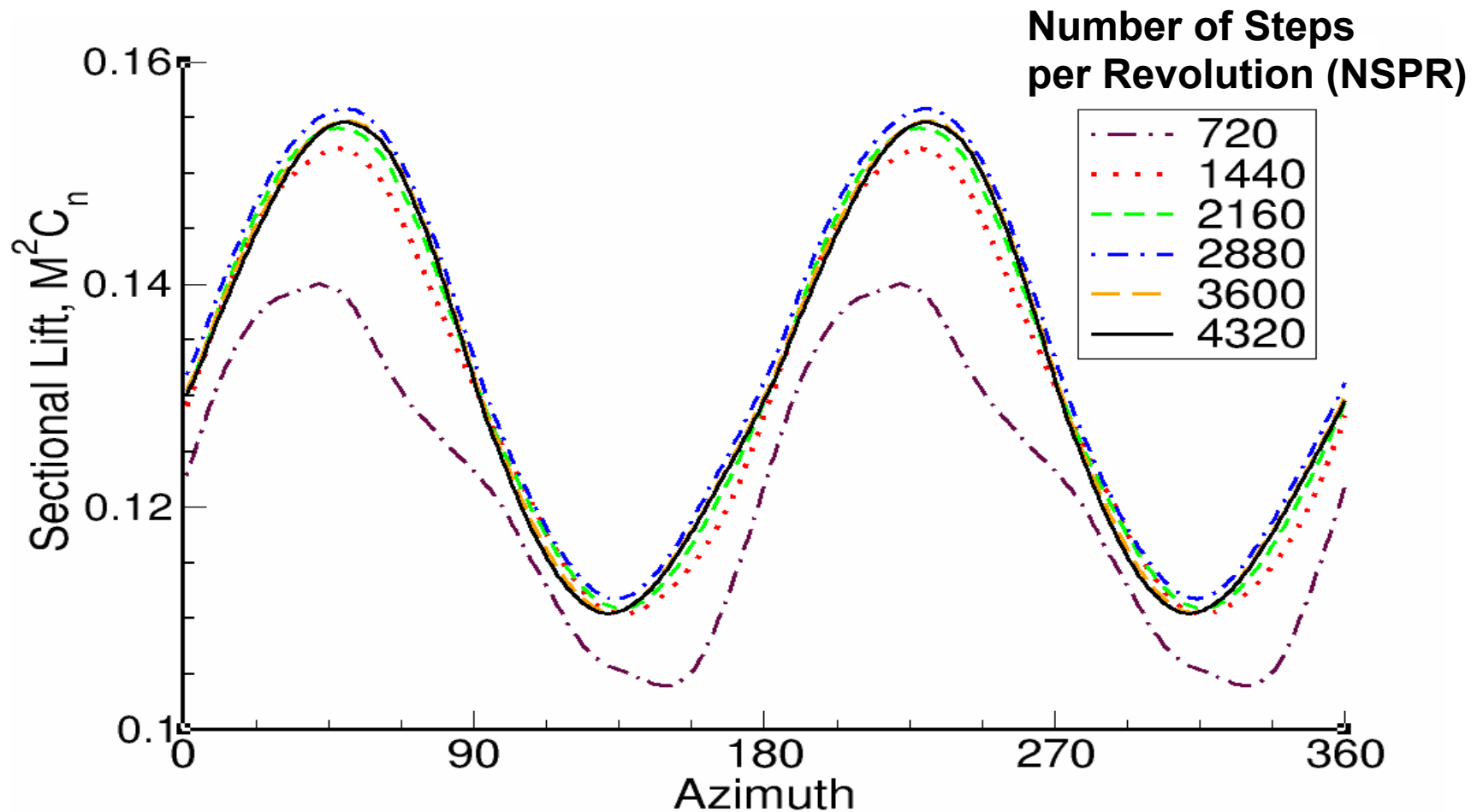
# Twist Modes





# Time Step Convergence of Sectional Lift

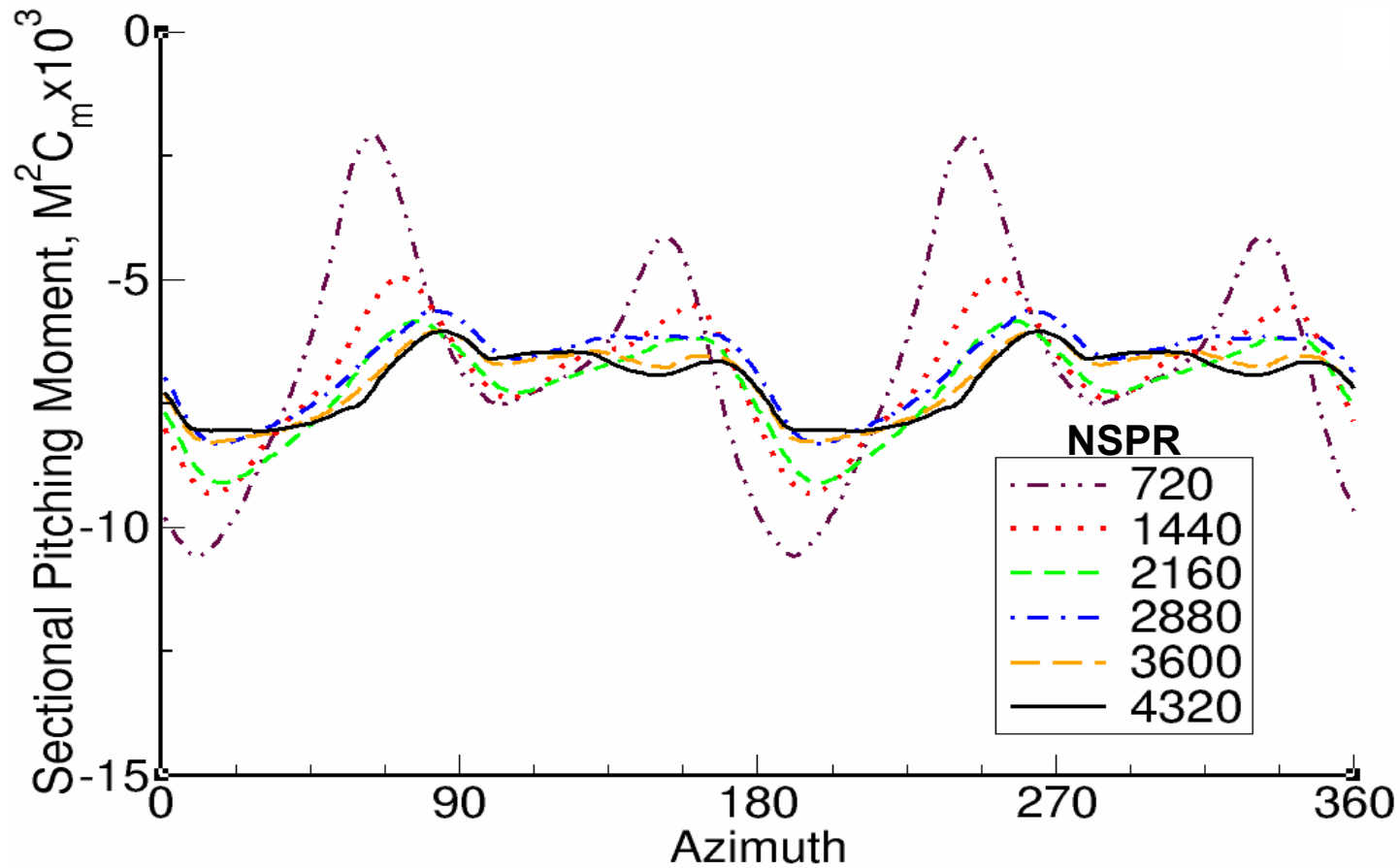
$\omega_2/\Omega = 2.0$ , 4<sup>th</sup> Revolution, 85% radial station





# Time Step Convergence of Pitching Moment

$\omega_2/\Omega = 2.0$ , 4<sup>th</sup> Revolution, 85% radial station

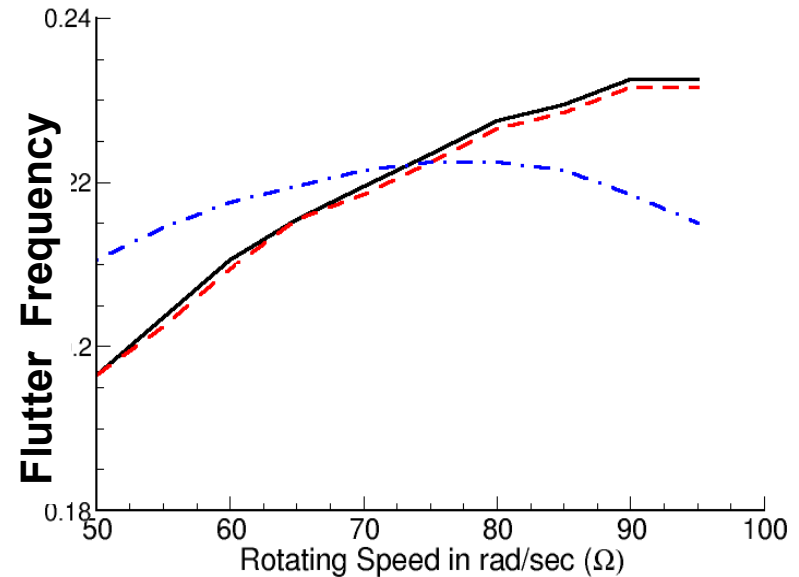
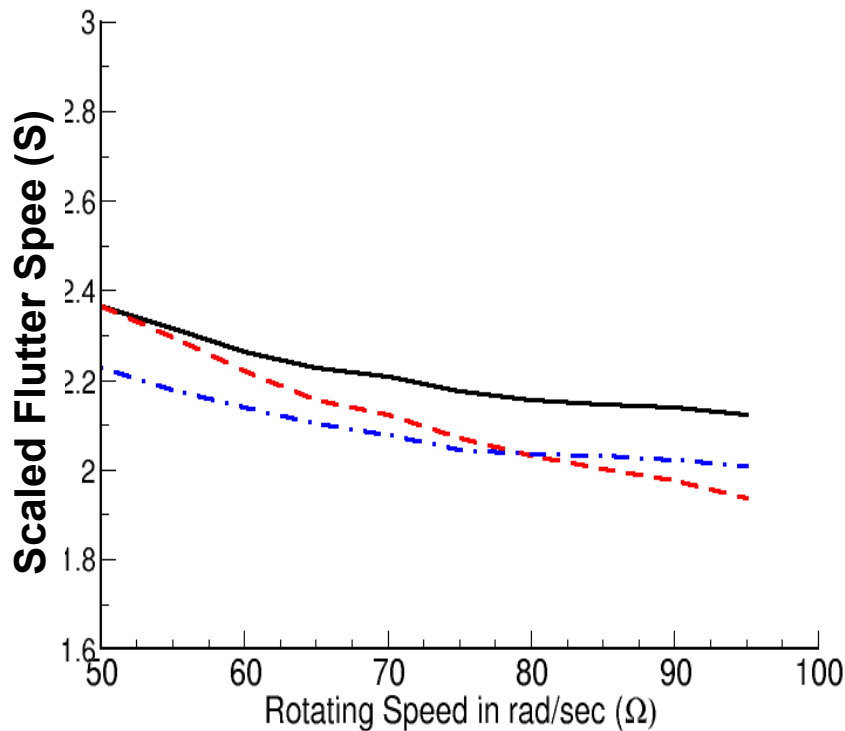


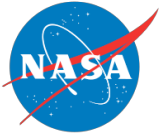


# Flutter Boundary for a Rotating Blade

- 100 responses with 4 revolutions using NSPR = 3600
  - Each case is assigned to one core, 24 hr wall clock time

— Rotating    - - - Rotating (Constant Stiffness)    . . . Non-Rotating





## Summary

- **A procedure to compute flutter boundaries of rotating blades is presented**
  - **Navier-Stokes equations**
  - **Frequency domain method compatible with industry practice**
- **Procedure is initially validated**
  - **Unsteady loads with flapping wing experiment**
  - **Flutter boundary with fixed wing experiment**
- **Large scale flutter computation is demonstrated for rotating blade**
  - **Single job submission script**
  - **Flutter boundary in 24 hour wall clock time with 100 cores**
  - **Linearly scalable with number of cores. Tested with 1000 cores that produced data in 25 hrs for 10 flutter boundaries.**
- **Further wall-clock speed-up is possible by performing parallel computations within each case**
  - **work in progress**