

All-particle cosmic ray energy spectrum measured with 26 IceTop stations



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ABSTRACT

We report on a measurement of the cosmic ray energy spectrum with the IceTop air shower array, the surface component of the IceCube Neutrino Observatory at the South Pole. The data used in this analysis were taken between June and October, 2007, with 26 surface stations operational at that time, corresponding to about one third of the final array. The fiducial area used in this analysis was 0.122 km². The analysis investigated the energy spectrum from 1 to 100 PeV measured for three different zenith angle ranges between 0° and 46°. Because of the isotropy of cosmic rays in this energy range the spectra from all zenith angle intervals have to agree. The cosmic-ray energy spectrum was determined under different assumptions on the primary mass composition. Good agreement of spectra in the three zenith angle ranges was found for the assumption of pure proton and a simple two-component model. For zenith angles $\theta < 30^\circ$, where the mass dependence is smallest, the knee in the cosmic ray energy spectrum was observed at about 4 PeV, with a spectral index above the knee of about -3.1 . Moreover, an indication of a flattening of the spectrum above 22 PeV was observed.

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1. Introduction

100 years after the discovery of cosmic rays, their sources and acceleration mechanisms still remain mostly unknown. The energy spectrum of cosmic rays as measured by various experiments follows a relatively smooth power law with spectral index $\gamma \approx -2.7$

up to about 4 PeV, where it steepens to $\gamma \approx -3.1$ [1]. While this feature in the spectrum called “knee” is well established, its origin remains controversial [2]. Most models to explain the knee involve a change in chemical composition of cosmic rays in the energy region above the knee. Such a change has been observed by various experiments [3] but systematic uncertainties are too large to discriminate individual descriptions. Features in the all-particle cosmic ray energy spectrum and their chemical composition bear important information on the acceleration and propagation of cosmic rays. The measurement of the cosmic ray energy spectrum and composition is the main goal of the IceTop air shower array.

IceTop is the surface component of the IceCube Neutrino Observatory at the geographic South Pole [4]. Installation of IceCube and IceTop was completed at the end of 2010, with 86 IceCube strings and 81 IceTop stations deployed covering an area of about 1 km²

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and a volume of about 1 km^3 . IceTop was designed to measure the energy spectrum and the primary mass composition of cosmic ray air showers in the energy range between $5 \cdot 10^{14} \text{ eV}$ and 10^{18} eV .

The average atmospheric depth at the South Pole is about 680 g/cm^2 . IceTop is therefore located close to the shower maximum for showers in the PeV range (for vertical protons about 550 g/cm^2 at 1 PeV to 720 g/cm^2 at 1 EeV). This has the advantage that local shower density fluctuations are smaller than at later stages of shower development.

In this paper, we present the first analysis of IceTop data on high-energy cosmic rays and a measurement of the cosmic ray energy spectrum. This analysis is based on air shower data taken with the IceTop surface stations. The data were taken between June and October 2007 with 26 IceTop stations operating, which comprise about 1/3 of the complete detector.

Section 2 of this paper gives an overview over the IceTop array, and the processing and calibration of tank signals, which are the basis for reconstructing air showers. Section 3 describes the dataset and run selection criteria. Section 4 introduces event reconstruction, and in Section 5, simulation of air showers and of the IceTop tank response are presented. In Section 6 the final event selection and detector performance are discussed. Section 7 describes the determination of the primary energy, whereas systematic uncertainties are discussed in Section 8. In Section 9 the results are presented and discussed.

2. The detector

2.1. IceTop

The IceTop air shower array is the surface component of IceCube, covering an area of about 1 km^2 with 81 detector stations above the 86 IceCube strings [4]. The stations are mostly located next to IceCube strings with a average spacing of 125 m, except for three stations placed as an infill with a smaller spacing in the central part of the detector, in order to lower the energy threshold of the detector to about 300 TeV. By 2007, 22 IceCube strings and 26 IceTop stations had been deployed. These stations are

highlighted in Fig. 1, which shows the layout of the IceTop air shower array in its final configuration.

Each station consists of two ice-filled tanks separated from each other by 10 m. The two tanks of each station are embedded in snow with their tops aligned with the surface in order to minimize the accumulation of drifting snow (see Section 2.5) and to protect the ice from temperature variations.

The tanks are cylindrical with an inner diameter of 1.82 m, and are filled with transparent ice to a depth of 90 cm (see Fig. 2). The inner tank walls are covered with a diffusely reflective coating. The first four stations deployed in 2005 have a liner with a higher reflectivity. This difference affects amplitude and pulse width of detected tank signals, since the higher reflectivity reduces Cherenkov photon absorption, leading to longer pulses. The ice is covered with perlite as thermal and optical insulation. The perlite also offers proper diffuse reflectivity at the ice surface.

Each tank is equipped with two ‘Digital Optical Modules’ (DOMs) [5] to record Cherenkov light generated by charged particles passing through the tank. The DOMs are identical to those used in other IceCube components and consist of a $10''$ photomultiplier tube (PMT) [6], plus electronic circuitry for signal digitization, readout, triggering, calibration, data transfer and various control functions. The two DOMs in each tank were operated at different PMT gains, $5 \cdot 10^6$ (high-gain DOM) and $5 \cdot 10^5$ (low-gain DOM), to enhance the dynamic range. This resulted in a linear dynamic range from 1 to more than 10^5 photoelectrons (PE). During the data taking period used in this analysis all 104 DOMs in the 26 IceTop stations were fully operational.

2.2. Trigger and data acquisition

A DOM records PMT signals autonomously. A signal is recorded if it surpasses a certain discriminator threshold, which in the case of IceTop was set to 22 mV for the high-gain DOMs (corresponding to about 20 pe) and 12 mV for the low-gain DOMs (corresponding to about 180 pe). The exact charge threshold depends on the shape of the IceTop multi-photoelectron pulses, which is determined by the arrival times of photoelectrons. After triggering, the delayed

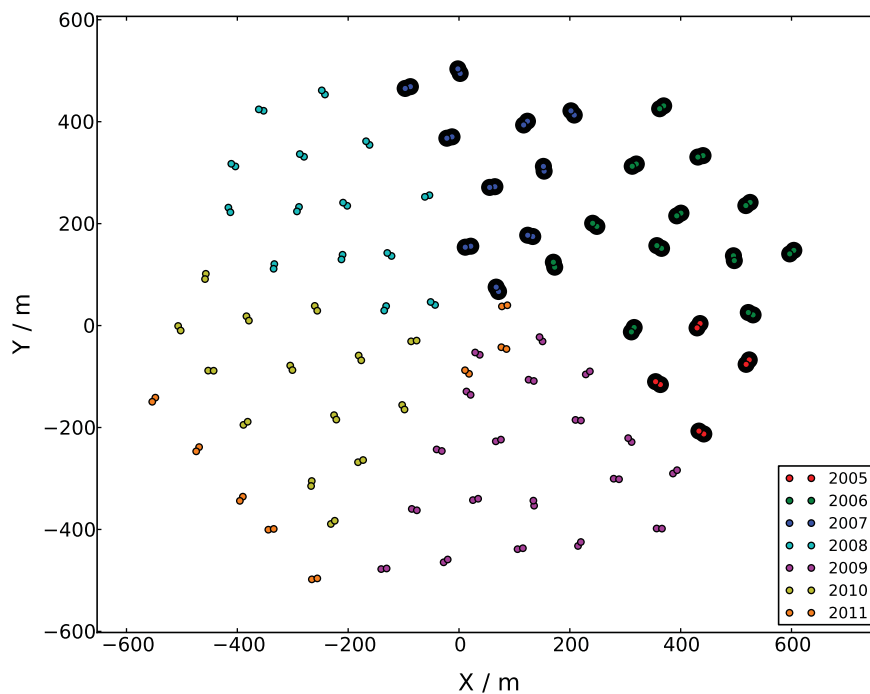


Fig. 1. Layout of the IceTop air shower array. Colors indicate the year of deployment and the 26 stations installed in 2007 are highlighted.

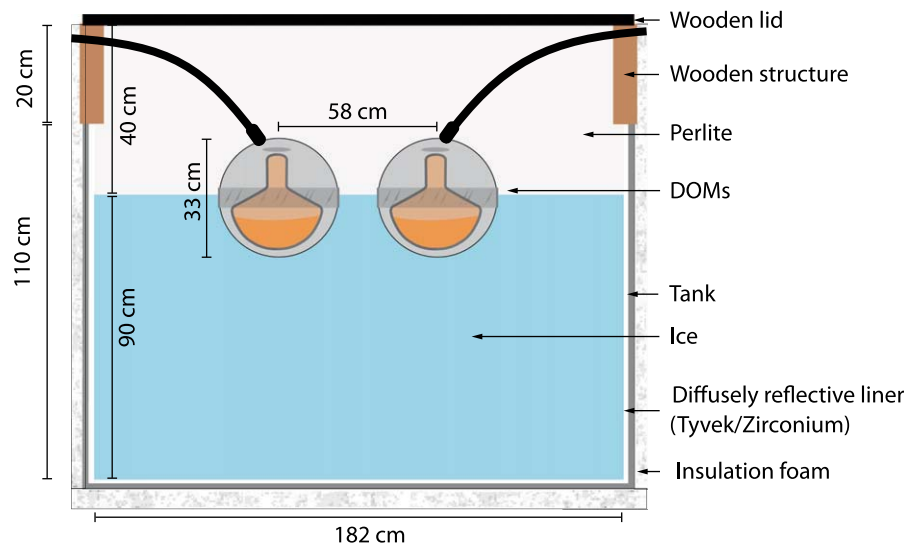


Fig. 2. Cross section of a tank showing the tank geometry with insulation and position of the DOMs. The center of the ice surface between the two DOMs is used as tank position by reconstruction algorithms.

PMT pulse is sampled by ‘Analog Transient Waveform Digitizers’ (ATWDs) with three different gain channels (nominal gains are 0.25, 2, and 16) in 128 bins with a width of 3.3 ns, corresponding to a total sampling time of about 422 ns. The analog samples are then digitized to 10 bit accuracy.

Up to this point, signal recording happens independently in each DOM. To reduce the high trigger rates in high-gain DOMs (~ 2 kHz), which are mostly from low-energy showers, a hardware ‘local coincidence’ with a coincidence time window of $\pm 1 \mu\text{s}$ between the high-gain DOMs in the two tanks of a station is required to initiate the readout and transmission of DOM data to the counting house (IceCube Lab).

In the counting house an event is built if the IceTop software trigger condition is satisfied requiring six or more DOMs to report a (local coincident) signal within a time window of $5 \mu\text{s}$. The event will contain waveforms from all IceTop and IceCube DOMs, which fulfilled the local coincidence condition between $10 \mu\text{s}$ before the first until $10 \mu\text{s}$ after the last of the six DOMs that triggered the event building. The requirement of 6 DOMs means that at least two stations had to trigger. For the 26 station configuration, the total IceTop trigger rate was about 14 Hz.

2.3. Charge extraction and calibration

Fig. 3 shows a typical waveform measured in IceTop. While waveforms are recorded in three ATWD channels, this analysis used only the highest gain unsaturated (less than 1022 ADC counts) channel. In this analysis only the integrated charge (i.e. the integral over the whole 422 ns waveform) and the signal time were used. Before a waveform was integrated, its baseline was subtracted by determining the average value in bins 83 to 123 highlighted in the figure. The undershoot is caused by droop introduced by the transformer used to couple the photomultiplier tube to the DOM’s front-end electronics. The signal time (‘leading edge time’) was defined by extrapolating the steepest rise of the waveform before the maximum down to the baseline. The absolute time scale of a DOM is calibrated with respect to all other DOMs to an accuracy of about 3 ns [7].

The charge produced by a single photoelectron, the amplifier gains and the digitizers are calibrated in a procedure common to all IceCube DOMs [7]. However, the signal response to a particle

of a given type and energy traversing the tank, expressed in photoelectrons, differs from tank to tank, due to differences in ice quality and reflectivity of the tank walls. Therefore, the signal of each tank is converted to a common unit called ‘Vertical Equivalent Muon’ (VEM). Calibration was done by recording charge spectra of DOMs in dedicated calibration runs with all DOMs operated at a gain of $5 \cdot 10^6$ and without requiring local coincidence (for an example see Fig. 3, right). These charge spectra show a clear peak due to penetrating muons above a background of electrons and photons. The spectra are fitted by the sum of a function describing the muon peak and an exponentially falling background term. Measurements with a portable scintillator telescope mounted on top of tanks, restricting muons to nearly vertical angles of incidence, indicated that the peak for vertical muons lies about 5% lower than for the full angular range. Simulation studies confirmed that restricting the angles of incidence of muons shifts the peak position by about 5% [8]. The scaled peak is referred to as ‘VEM peak’. For a given DOM the VEM unit can be expressed in terms of number of photoelectrons. These values average 120 and 200 photoelectrons for the low and high reflectivity tanks (see above), respectively.

For the 5-month run, 15 calibration runs were used. Between two consecutive calibration runs, the charge calibration was assumed to be stable (see also the discussion in Section 8.4).

2.4. Atmospheric conditions

Variations of the atmosphere influence the development of air showers and thus the signals measured in IceTop. Since IceTop is below the shower maximum for all energies of interest in this analysis and for all primary masses, an increase of the atmospheric overburden leads to an attenuation of shower sizes. Vertical atmospheric overburden is related to ground pressure p as $X_v = p/g$, where $g = 9.87 \text{ m/s}^2$ is the gravitational acceleration at the South Pole. While there is some annual variation of the ground pressure, it mostly varies on shorter time scales on the order of days.

Besides ground pressure, the altitude profile of the atmosphere, $dX_v(h)/dh$, also influences the development of air showers. This altitude profile has a pronounced annual cycle because the cold atmosphere during the winter months is much denser than the warmer atmosphere of the summer months. The data used in this analysis were mostly taken during the winter months.

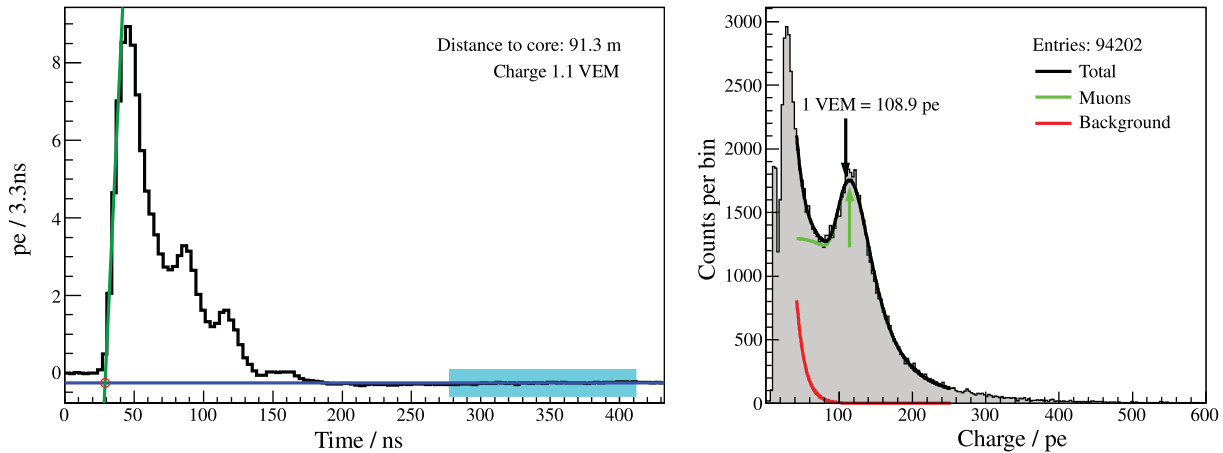


Fig. 3. *Left:* A typical IceTop waveform. The blue horizontal line marks the baseline and the near vertical green line indicates the extrapolation of the leading edge yielding the signal time marked by the red circle. The baseline is below 0 (dashed line) due to droop. *Right:* A typical charge spectrum recorded for the VEM calibration. The spectra are fitted with an empirical formula to determine the peak position. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

In the simulations used to interpret the air shower data a model of the South Pole atmosphere is used, which should represent the average atmosphere during the data taking period. Nevertheless, variations of the atmosphere around the average lead to an additional uncertainty on the measured energy spectrum. These systematic uncertainties will be discussed in Section 8.2.

2.5. Snow

During installation, IceTop tanks are embedded in snow up to the upper surface of the tanks. Depending on location, surrounding surface and structures, each tank is covered by accumulated layers of snow of varying thickness. Each year the amount of snow on the IceTop tanks grows on average by 20 cm.

As shown in Fig. 4, the snow height for the analyzed data varied mostly between 0 and 30 cm, except for four stations close to a building, which are covered by 60 to 90 cm of snow. The average snow height was 20.5 cm in January, 2007.

The snow has an average density of 0.38 g/cm^3 , depending on snow height and location. The snow on top of and around the tanks influences the response to air shower particles penetrating the

tanks and needs to be taken into account in simulations and for the determination of the shower energy.

3. Data set and data selection

Event filtering and data transmission. The data used in this analysis were taken between June 1st and October 31st, 2007. The analysis was performed using a data sample which was transferred with limited bandwidth via satellite to the IceCube data center at UW Madison. Due to these bandwidth constraints, events with less than 16 participating DOMs were prescaled by a factor of 5. Events with 16 or more DOMs were transmitted at a rate of 0.9 Hz and the small events at a rate of 2.5 Hz. Due to the high event rate, the pre-scale does not cause any statistical problems in the low-energy region.

Run selection. In order to ensure detector stability and data quality, the following criteria were applied to runs which were used in this analysis:

- The run was longer than 30 min. A normal detector run lasted 8 h, and nearly all runs that were aborted after a short time encountered some sort of problem.
- All DOMs were running stably.
- After correction for atmospheric pressure variations the trigger and filter rates were stable and within $\pm 5\%$ agreement with the previous good run. Pressure correction was done by fitting the relation between ground pressure p and rate R with an exponential function, $R(p) \sim \exp(-bp)$, yielding a barometric coefficient $b = 0.0077/\text{mbar}$ [9]. Then, the rates were corrected to the average South Pole ground pressure of 680 mbar:

$$R_{\text{corrected}} = R \exp(b(p - 680 \text{ mbar})). \quad (1)$$

These cuts reduced the livetime by about 10%.

Event cleaning. Before starting the reconstruction, events were cleaned based on a few simple timing criteria. When both DOMs of a tank triggered, the tank signal was rejected if the time difference between the two signals was greater than 40 ns. The analysis used only one signal per tank. For each high-gain DOM a saturation threshold was determined from a comparison of signals that triggered both DOMs in a tank. Signals with less charge were taken from the high-gain DOM. If the charge exceeded the saturation threshold, the charge measured by the low-gain DOM was used and the time was determined from the high-gain signal.

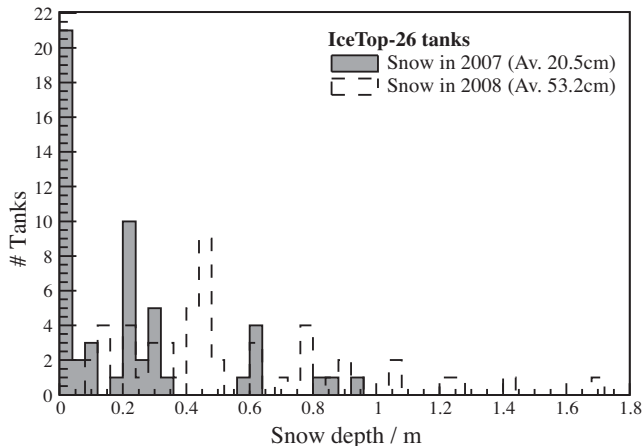


Fig. 4. Snow heights on top of IceTop tanks measured in January 2007. All 20 newly deployed tanks had no snow on top, the average snow height was 20.5 cm. The dashed histogram is the snow height distribution on top of the same tanks measured one year later.

Furthermore, a tank signal was also rejected if only the low-gain DOM triggered and the high-gain DOM was missing.

Then, a maximum time difference of

$$|t_A - t_B| < \frac{|\mathbf{x}_A - \mathbf{x}_B|}{c} + 200 \text{ ns} \quad (2)$$

between signals in tanks A and B of the same station was required. Here, t_A and t_B are the signal times in the two tanks and \mathbf{x}_A and \mathbf{x}_B are the tank locations. The tolerance of 200 ns was introduced in order to account for shower fluctuations. Finally, stations were grouped in clusters, such that any pair of stations i and j in the cluster fulfilled the condition

$$|t_i - t_j| < \frac{|\mathbf{x}_i - \mathbf{x}_j|}{c} + 200 \text{ ns}. \quad (3)$$

The station position \mathbf{x}_i is the center of the line connecting its two tanks, and t_i is the average time of the tank signals. In each event, only the largest cluster of stations was kept.

Only about 10% of events were affected by this event cleaning, and about 2.5% of events dropped below the threshold of 5 stations required for reconstruction. On average 2.3 tanks were removed.

Charge-based retriggering. In order to reduce uncertainties due to the description of the detector threshold in the simulation, all events were retriggered to a common threshold based on total registered charge. All pulses with a charge below $S_{\text{thr}} = 0.3$ VEM were removed, and afterwards the local coincidence conditions (see Section 2.2) were re-evaluated discarding all pulses that no longer fulfilled this condition. This procedure was applied to both experimental and simulated data.

Event selection. For further processing, a total of $N_{\text{tot}} = 8,895,205$ events were selected where at least five stations had triggered. These five stations do not have to be neighbors. Events which fulfilled this condition, but had less than 16 DOMs read out (before event cleaning), were reweighted in the analysis with the prescale factor of 5 (see above).

The effective livetime was calculated by fitting the distribution of time differences between events, Δt , with an exponential function,

$$N(\Delta t) = N_0 \exp(-\Delta t/\tau). \quad (4)$$

This was done individually for each data taking run. The selected runs have a total effective livetime of $T = \sum_{\text{runsi}} (N_i \cdot \tau_i) = (3274.0 \pm 1.9)$ h, which corresponds to 89.4% of the selected 153 days period. The uncertainty on the livetime was included in the statistical error.

4. Air shower reconstruction

The energy of the primary particle cannot be measured directly, but has to be determined from the properties of the observed air shower. From the measured charges and times of the tank signals the shower core position, the shower direction, and the shower size are reconstructed. The latter is a measure of primary energy and was defined here as the signal S_{125} measured at a distance $R = 125$ m from the shower axis. Details of the reconstruction procedure are described in [4,10]. In the following we summarize the essential steps.

Air shower reconstruction required at least 5 triggered stations. The logarithm of the signal, $\log S(R)$, of a tank at distance R from the shower axis was fitted by a lateral distribution function which is a second order polynomial in $\log R$ [11]:

$$\log S(R) = \log S_{125} - \beta \log \left(\frac{R}{125 \text{ m}} \right) - \kappa \log^2 \left(\frac{R}{125 \text{ m}} \right). \quad (5)$$

The free parameters of the function, in addition to the shower size, S_{125} , are the slope β and the curvature κ . The latter parameter was

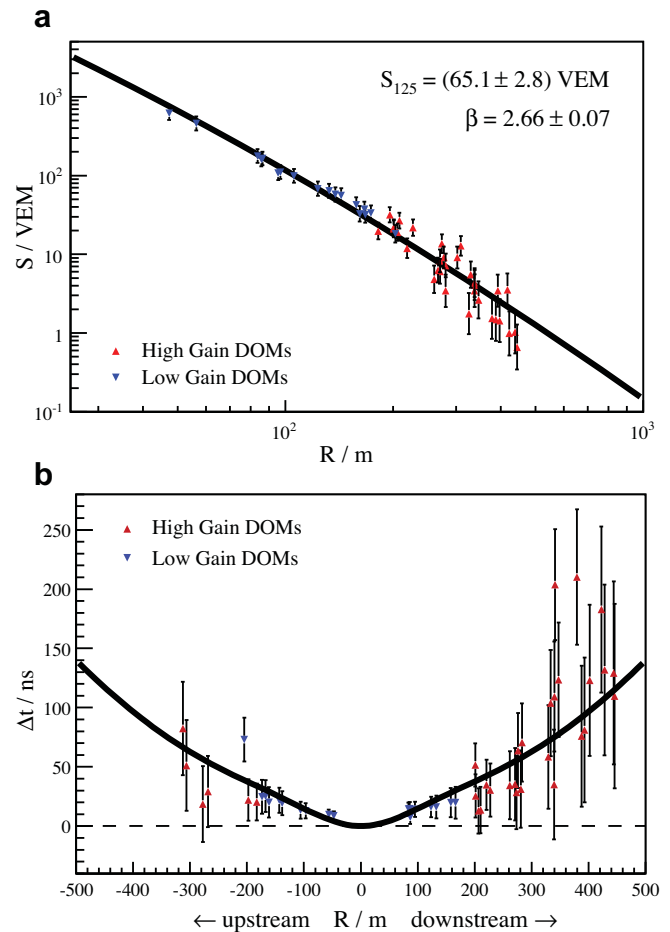


Fig. 5. Left: Example of an IceTop lateral fit. The shower triggered 25 stations and the reconstructed shower size is $S_{125} = (65.1 \pm 2.8)$ VEM. Right: Time residuals with respect to a plane perpendicular to the shower direction fitted by the sum of a parabola and a Gaussian function. “Upstream” and “downstream” refer to tanks being hit before and after the shower core reaches the ground.

fixed to $\kappa = 0.303$, the average value found in simulation studies. Implicitly the function (5) depends on four more parameters since R depends on the shower core position (x_c, y_c) and direction (θ, ϕ) . Since the function (5) behaves unphysically at small distances to the shower axis ($R \lesssim 1$ m) all signals within 11 m of the core are excluded from the fit. Fig. 5 left shows an example of the lateral distribution function fit of a shower with 25 triggered stations.

The arrival times of the signals map out the shower front which was described by the sum of a parabola and a Gaussian function, both symmetric around the shower axis (Fig. 5 right).

The lateral distribution function and the function describing the shower front curvature the charge and time of air shower signals were fitted to the measured signal charges and times using the maximum likelihood method. In addition to terms for the signal charges and times, the likelihood function also takes into account stations that did not trigger.

5. Simulation of air showers and the IceTop detector

The relation between the measured signals and the energy of the primary particle, as well as detection efficiency and energy resolution were obtained from CORSIKA [12] air shower simulations and simulations of the IceTop detector.

5.1. Air shower simulation

We simulate the development of air showers in the atmosphere using the simulation code CORSIKA [12]. Inside CORSIKA, the hadronic component of the air showers was simulated using the models SIBYLL2.1 [13,14] and FLUKA 2008.3 [15,16] for the high and low energy interactions, respectively. The electromagnetic component was simulated using the EGS4 code [17] and no ‘thinning’ (reduction of the number of traced particles) was applied. To study systematic effects of the hadronic interaction model, small samples of showers were simulated using the QGSJET-II [18,19] and EPOS 1.99 [20] high energy interaction models. Two different parameterizations of the South Pole atmosphere from two days in 1997 based on the MSIS-90-E model [21] were used: July 1st and October 1st (CORSIKA atmospheres 12 and 13). The July atmosphere has a total overburden of 692.9 g/cm², while the October atmosphere has an overburden of 704.4 g/cm². The July atmosphere was used in the data analysis, because its total overburden is close to the average measured overburden of 695.5 g/cm² and its profile corresponds to that of a South Pole winter atmosphere. The October atmosphere model was used to study systematic uncertainties due to the atmospheric profile used in the simulation.

5.2. Detector simulation

The output of the CORSIKA program, i.e. the shower particle types, positions and momenta at the observation level of 2835 m, were injected into the IceTop detector simulation. The simulation determines the amount of light produced by the shower particles in the tanks followed by the simulation of the PMT, the DOM electronics and the trigger chain.

The Cherenkov emission inside the tanks is simulated using Geant4 [22,23]. All structures of the tank, the surrounding snow, including individual snow heights on top of each tank, as well as the air above the snow are modeled realistically [4]. The snow heights used in the simulation corresponded to those measured in January 2007 (see Fig. 4). In order to save computing time, Cherenkov photons are not tracked; only the number of photons emitted in the wavelength interval 300 nm to 650 nm is recorded. Using Geant4 simulations, that include Cherenkov photon tracking until photons reach the PMT, it was shown that the number of detected photons scales linearly with the number of emitted photons, independent of incident particle type and energy. The propagation of Cherenkov photons is modeled by distributing the arrival times according to an exponential distribution, which is tuned such that simulated waveform decay times match those observed in experimental data (26.5 ns for all tanks commissioned after 2005 and 42.0 ns for tanks commissioned in 2005).

The number of photoelectrons corresponding to 1 VEM was taken from the VEM calibration of the real tanks and used as an input for the simulation. The simulated tanks were then calibrated by generating muon spectra as in experimental data using air shower simulations with primary energies between 3 GeV and 30 TeV and zenith angles up to 65°. Thus, the ratio between the number of emitted Cherenkov photons and observed photoelectrons was determined by the VEM calibration of simulated tanks.

In the next step the generated photoelectrons are injected into a detailed simulation of the PMT followed by the analog and digital electronics of the DOM. To simulate the photomultipliers, Gaussian single photoelectron waveforms with a random charge according to the average single photoelectron spectrum are superimposed [6]. Afterwards, a saturation function is applied to the resulting waveforms. In the DOM simulation, the pulse shaping due to the analog front end electronics is applied to the output of the PMT simulation. This includes the individual shaping of the signal paths to the ATWD and the discriminators, as well as the simulation of

the droop effect induced by the toroid that couples the high voltage circuits of the PMT to the readout electronics. Then, the discriminators are simulated and the local coincidence conditions are evaluated. Finally, the waveform digitization and the array trigger are simulated.

Simulated data are of the same format as the experimental data and were reconstructed in the same way, as described in the previous section.

5.3. Simulation datasets

In this analysis we describe the cosmic ray composition just with the two extreme nuclei proton and iron. The justification comes from the fact that the final result is not very sensitive to details of the composition assumption but mostly to the mean logarithmic mass.

In total $2 \cdot 10^5$ showers of proton and iron primaries in the energy range between 100 TeV and 100 PeV were generated in 30 logarithmic energy bins according to an E^{-1} distribution. For the analysis, the events are reweighted to an E^{-3} flux, which is closer to the results of previous experiments and thus reduces systematic biases (see also Section 8.10). In addition to pure proton and iron simulations we also combined the datasets using a parametrization of Glasstetter’s two-component model [24] (see Fig. 6). We transformed the proton flux to the form

$$\frac{dI}{dE} = I_0 \left(\frac{E}{1 \text{ PeV}} \right)^{\gamma_1+1} \left(1 + \left(\frac{E}{E_{\text{knee}}} \right)^\varepsilon \right)^{-(\gamma_2-\gamma_1)/\varepsilon}, \quad (6)$$

as suggested in [25], with $I_0 = 3.89 \cdot 10^{-6} \text{ m}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$, $\gamma_1 = -2.67$, $\gamma_2 = -3.39$, $E_{\text{knee}} = 4.1 \text{ PeV}$, and $\varepsilon = 2.1$. The iron flux was used as specified in Ref. [24]:

$$\frac{dI}{dE} = 1.95 \cdot 10^{-6} \text{ m}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \cdot \left(\frac{E}{1 \text{ PeV}} \right)^{-1.69}. \quad (7)$$

The total flux was then normalized to the same E^{-3} spectrum as in case of the single component Monte Carlo.

Since shower generation is CPU intensive the same showers were sampled several times inside a circle with a radius of

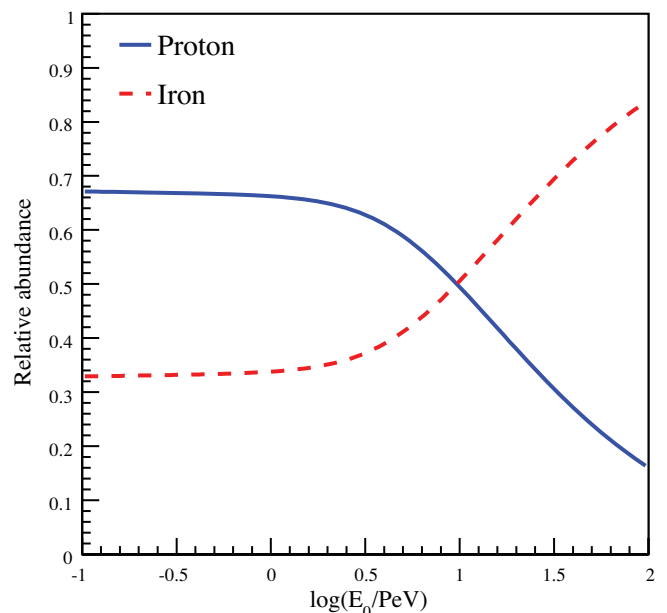


Fig. 6. Relative abundance of proton and iron in our parametrization of Glasstetter’s two-component model as a function of primary energy. Above about 10 PeV the spectrum is dominated by iron.

1200 m around the center of the 26 station IceTop array. The number of samples was chosen for different energy bins such that every shower would remain on average only once in the final sample after applying the cuts described in the next section. This ensures a good balance between an effective use of the generated showers and the artificial fluctuations introduced by oversampling.

6. Event selection and reconstruction performance

Quality cuts. Based on the reconstruction results the following quality criteria were required for each event entering the final event sample, for both simulated and experimental data:

- Containment cut: The reconstructed core and the first-guess core position had to be at least 50 m inside the boundary of the array. The array boundary is defined by the polygon with vertices at the centers of stations at the periphery of the array and edges connecting these stations. This cut defines a fiducial area of $A_{\text{cut}} = 0.122 \text{ km}^2$. Furthermore, it was required that the station containing the largest signal is not on the border of the array.
- Only events with zenith angles $\theta < 46^\circ$ were considered.
- The reconstruction uncertainty on the core position had to fulfill $\sigma_{\text{core}} = \sqrt{\sigma_x^2 + \sigma_y^2} < 20 \text{ m}$, which is the fit uncertainty of the position parameters calculated from the width of the likelihood function around the minimum.
- The slope parameter β had to be in the range $2.0 \leq \beta < 4.5$ because most events with β values outside this range were badly reconstructed and because β was limited in the fit. The eliminated events predominantly had low primary energies, $E_0 \lesssim 1 \text{ PeV}$.

In the experimental dataset 3,096,334 events passed the quality cuts. Passing rates for the individual cuts are shown in Table 1 for events with $S_{125} > 1\text{VEM}$. Differences between data and two-component Monte Carlo are discussed later in Section 8.7.

Reconstruction performance. Core position and angular resolution, shown in Fig. 7, are key criteria for the performance of air shower reconstruction. The 1σ core resolution is defined as the 68% quantile of the cumulative distribution of the distances between true and reconstructed shower cores; correspondingly the angular resolution is defined as the angle between true and reconstructed shower direction. The numbers shown are for showers with zenith angle $\theta \leq 30^\circ$, obtained from the two-component Monte Carlo after applying the quality cuts listed in the previous paragraph. At the highest energies, a core resolution of 7 m and an angular resolution of 0.4° were achieved. In the most inclined zenith angle range considered in this analysis, $40^\circ \leq \theta < 46^\circ$, the core resolution is between 10 and 30% worse and the angular resolution between 10 and 25% worse, depending on energy and primary mass.

Table 1

Passing rates of the quality cuts described in the text for events with $S_{125} > 1 \text{ VEM}$. Statistical errors on experimental data are negligible.

Cut	Experimental data		Monte Carlo	
	Passing rate (%)	Cumulative (%)	Passing rate (%)	Cumulative (%)
$N_{\text{station}} > 5$ and $S_{125} > 1 \text{ VEM}$	100		100	
Largest signal contained	42.5	42.5	(39.4 ± 0.5)	(39.4 ± 0.5)
First guess core contained	95.8	40.7	(95.4 ± 0.4)	(37.6 ± 0.5)
Core contained	78.9	32.1	(81.1 ± 0.5)	(30.5 ± 0.6)
Zenith $\theta < 46^\circ$	96.3	30.9	(96.4 ± 0.5)	(29.4 ± 0.6)
$\sigma_{\text{core}} < 20 \text{ m}$	99.7	30.8	100	(29.4 ± 0.6)
$2.0 \leq \beta < 4.5$	98.1	30.2	(99.7 ± 0.1)	(29.3 ± 0.6)

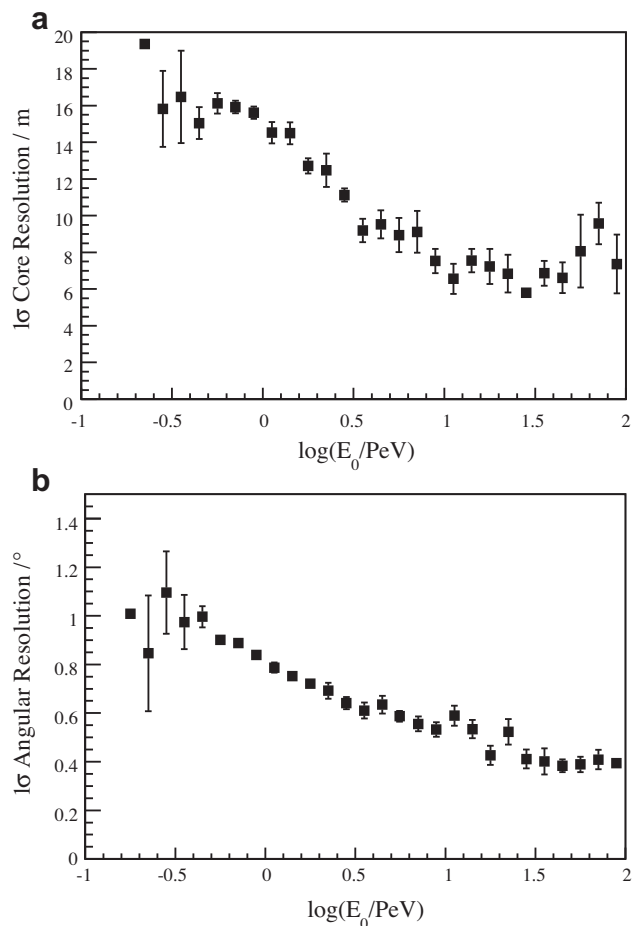


Fig. 7. Core position and angular resolution for showers with $\theta \leq 30^\circ$, obtained from the two-component Monte Carlo. At high energies, the distance between true and reconstructed core position of 68% of showers is 7 m or less. The angle between true and reconstructed directions of 68% of showers at 1 PeV is smaller than 0.8° and this value decreases to 0.4° at 100 PeV.

In the most inclined zenith angle range considered in this analysis, $40^\circ \leq \theta < 46^\circ$, a core resolution of 10 m and an angular resolution of 0.5° was achieved.

The intrinsic spread of the shower size distribution due to the detector was studied using such simulated proton air showers, which remained more than once in the final sample after resampling, detector simulation, and reconstruction. While the value of S_{125} cannot be predicted or calculated analytically for a given air shower, the distribution of reconstructed shower sizes for a given air shower (at different locations inside the detector), is a measure of the intrinsic resolution of the apparatus and the measurement. As shown in Fig. 8, the RMS of $\log_{10}(S_{125}/\text{VEM})$ improves from about 0.08 at 1 PeV primary energy to better than 0.04 above primary energies of 10 PeV, almost independent of zenith angle. A comparison of this intrinsic resolution with the spread of reconstructed energies discussed in Section 7.2 shows that for the most vertical zenith angle range ($\theta < 30^\circ$) the intrinsic resolution is dominant, whereas the energy resolution of more inclined showers is dominated by fluctuations of the shower development. Reconstructed shower core distribution. The distribution of reconstructed shower core locations is shown in Fig. 9. While this distribution is not entirely flat, it is reasonably well reproduced by simulation, and the structures are understood as described below. Therefore, we do not expect a significant systematic error introduced by the containment criteria.

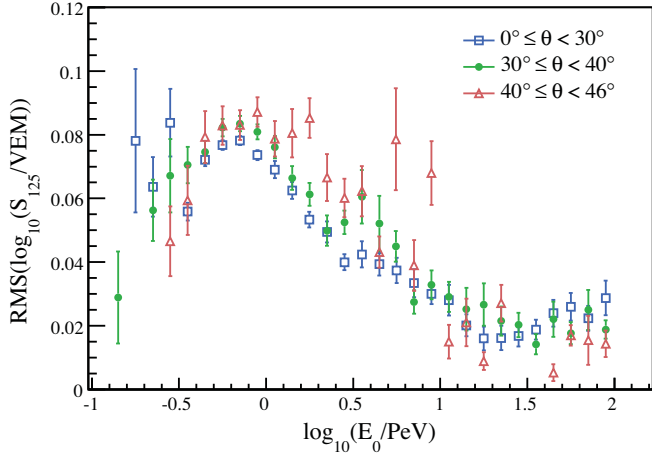


Fig. 8. RMS spread of the S_{125} distribution due to the apparatus and the shower reconstruction plotted against the primary energy.

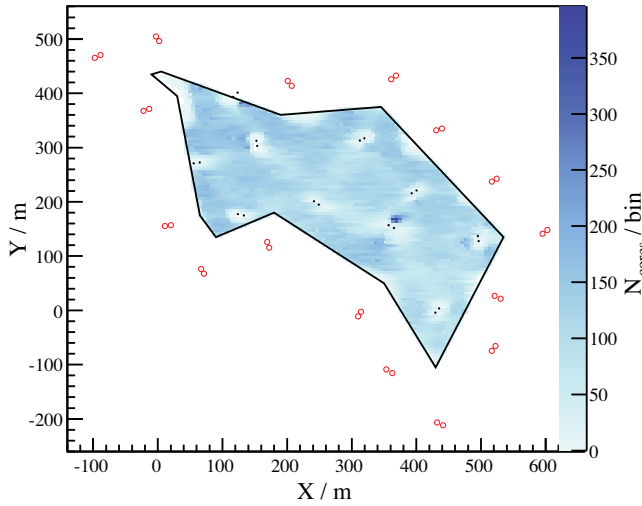


Fig. 9. Distribution of reconstructed core positions in IceTop for showers with $S_{125} \geq 2$ VEM. The black line represents the containment region. The dots are the IceTop tanks, red open circles being those that are considered on the border of the array for the containment cut. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

The right half of the array ($x > 200$ m) has been deployed in 2005/06 and the left half has been deployed in 2007. Consequently, the right half of the array is covered by a thicker layer of snow. This increases the energy threshold in this part of the array, leading to a lower rate for cores with $x > 200$ m.

There are regions along the border of the containment region (black line), where the closest station is one that is not considered contained (red dots in the figure). Due to the requirement that the station with the largest signal should be contained, shower cores reconstructed in this area are less likely to pass the containment cut. It should be noted that these stations still contribute to the lateral fits of all events.

Finally, there are some structures in the vicinity of stations, which are an artifact of the removal of tanks closer than 11 m to the core during the reconstruction. This requirement slightly decreases the efficiency of the array close to tanks and at the same time favors core positions further away from the stations. The large peak in the center of the array is probably due to this effect combined with the fact that the nearest station in that direction is particularly close.

7. Determination of energy spectra

Using the reconstruction methods and quality cuts described in Sections 4 and 6, the shower size spectra shown in Fig. 10 were obtained. In this analysis, the data were split into three zenith angle ranges roughly equidistant in $\sec \theta$, defined as:

$$\Omega_1 = [0^\circ, 30^\circ], \quad \Omega_2 = [30^\circ, 40^\circ], \quad \Omega_3 = [40^\circ, 46^\circ]. \quad (8)$$

A steepening of the spectral slope is visible at $\log(S_{125}/\text{VEM}) = 0.5$ and a possible flattening at about $\log(S_{125}/\text{VEM}) = 1.4$. To determine the energy spectrum from measured data, these S_{125} spectra were unfolded. Unfolding was performed for each zenith angle range independently.

7.1. General method

For the unfolding procedure the response of the detector to a primary particle of mass M , energy E_0 , zenith angle θ , azimuth ϕ , and core position (x_c, y_c) has to be determined from simulation. In this analysis we consider only an unfolding of energies. Within each zenith angle range, we average over the dependencies on zenith, azimuth, and core position. The response of the detector is the probability of measuring a shower size S_{125} given a primary energy E_0 and mass M in a certain zenith range Ω_k .

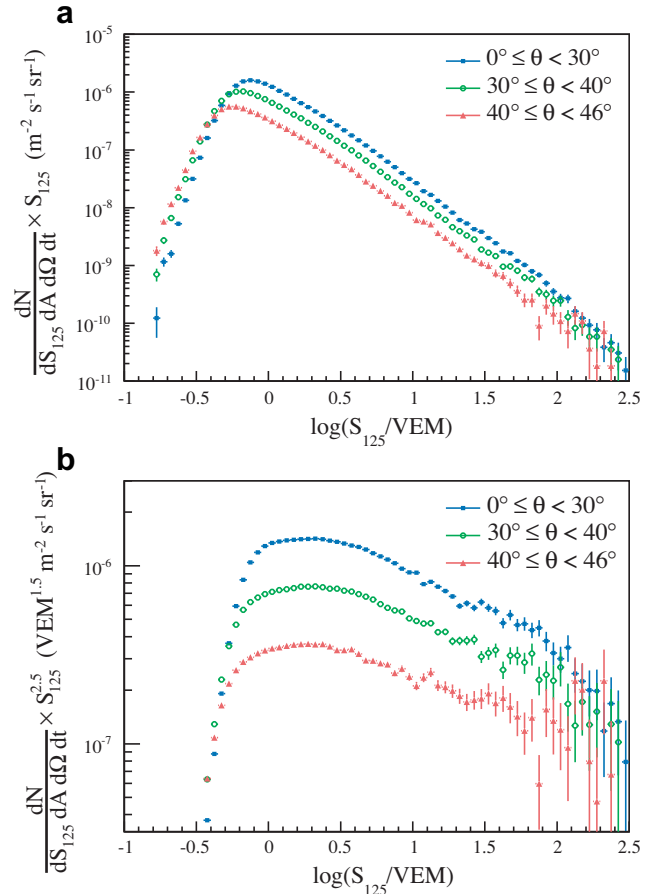


Fig. 10. Left: Reconstructed shower size spectra in three zenith angle bins. The energy spectrum was derived from these spectra using an unfolding method as described in Section 7. On the right, the same spectra are shown, weighted by $S_{125}^{1.5}$. In this representation the knee can be seen at $\log S_{125} \approx 0.5$ and there are indications of a flattening above $\log S_{125} \approx 1.4$.

In a discrete formulation we define a response matrix \mathbf{R} which relates the bin contents $N_i^s (i = 1, \dots, m)$ of a measured S_{125} spectrum with the bin contents $N_j^e (j = 1, \dots, n)$ of a primary energy spectrum for a fixed zenith range Ω_k :

$$N_i^s = R_{ij}^{(k)} N_j^e. \quad (9)$$

The response matrix elements $R_{ij}^{(k)}$ are defined as acceptance integrals

$$R_{ij}^{(k)} = \frac{\sum_M \int_{\Delta E_0^i} dE_0 \int d\Omega \int dA_{\perp} \Phi_M(E_0) p_M^{(k)}(S_{125}^i | E_0)}{\sum_M \int_{\Delta E_0^j} dE_0 \int_{\Omega_k} d\Omega \int_{A_{\text{cut}}} dA_{\perp} \Phi_M(E_0)}. \quad (10)$$

The model flux $\Phi_M(E_0)$ of nuclei with mass M weighted by their acceptance function

$$p_M^{(k)}(S_{125}^i | E_0) = p(S_{125}, \Omega_k | E_0, x_c, y_c, \theta, \phi; M) \quad (11)$$

is integrated over primary energy bin E_0^j , the angles θ and ϕ , and area A_{\perp} projected on a plane perpendicular to the particle direction. It is summed over all mass components M that contribute to the assumed composition model. $R_{ij}^{(k)}$ is normalized to the flux integrated over bin j in E_0 , solid angle Ω_k , and fiducial area A_{cut} . The function p_M is the probability of an event with mass M and kinematical variables $(E_0, x_c, y_c, \theta, \phi)$ to be reconstructed with shower size S_{125} in bin i and zenith angle θ in the range Ω_k , and to pass all cuts listed in Section 6. Thus, $R_{ij}^{(k)}$ for a given primary energy bin j , is the ratio between number of events measured in S_{125} bin i and zenith bin k , that pass all cuts, and the true number of events in that energy bin j and zenith bin k inside the fiducial area. Since the E_0 bins of $R_{ij}^{(k)}$ are independent, the total flux model only affects weighting of events within one bin, but not neighboring bins. The flux normalization in $R_{ij}^{(k)}$ cancels out, and the dependence on the spectral index of the flux model is small (see also Section 8.10). The integrals in Eq. (10) were determined numerically using the Monte Carlo method.

With the normalisation to the full flux integral the response matrix has the following normalisation properties (we drop the superscript k for zenith range):

$$\sum_i R_{ij} = \varepsilon_j, \quad \sum_j R_{ij} = 1. \quad (12)$$

That means, for a given energy bin j the sum of the probabilities to be detected in any signal bin is the efficiency ε_j ; for a given S_{125} bin i the probability to belong to any energy E_0 is unity. The efficiency depends on the energies, the core position (x_c, y_c) and the angles. However, in the analysis we will integrate over core positions and azimuth angle. The determination of ε_j is described in Eq. (14).

To obtain the primary energy spectrum from the measured signals the matrix Eq. (9) would have to be inverted:

$$N_j^e = (R^{-1})_{ji} N_i^s. \quad (13)$$

In order to avoid explicit inversion of the badly conditioned matrix R , an iterative unfolding method according to Ref. [26] was used.

7.2. Evaluation of response matrices, efficiencies and resolutions

Fig. 11 shows the response matrix for simulated proton and iron primaries in the interval Ω_1 of smallest zenith angles based on an E^{-3} spectrum. In each bin the colour code represents the probability that an event with energy E_0 yields a signal S_{125} . The binning uses a logarithmic scale.

For computational purposes and to smooth fluctuations in the simulated response matrix, the $\log S_{125}$ projections of each $\log E_0$ bin j were fitted by a normal distribution function yielding the mean value $\langle \log S_{125} \rangle_j$ and standard deviation $\sigma_{\log S_{125} j}$. The χ^2 probability distribution of these fits is almost flat, with a peak at 0

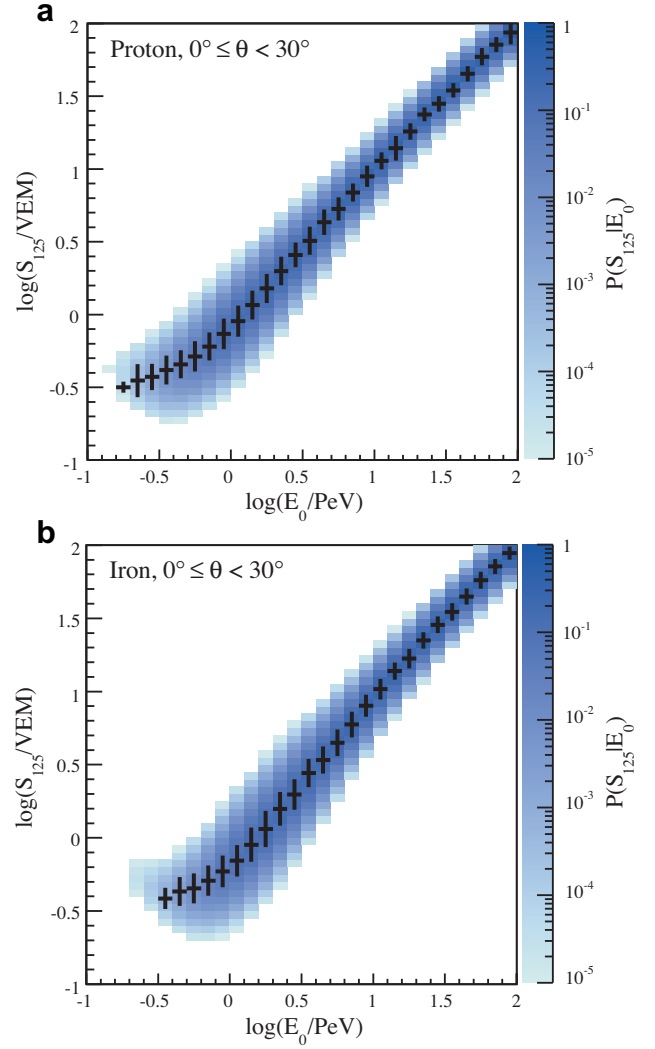


Fig. 11. Response matrix: shower size S_{125} distribution as a function of primary energy for proton (left) and iron (right) showers with zenith angles up to 30° simulated using the hadronic interaction model SIBYLL. The crosses give the mean value and spread (RMS) of the distribution in each energy bin. The matrices have been smoothed as described in Section 7.2 and Appendix A.

caused by cut-off distributions in the threshold region (see also discussion of the energy resolution below). The normalisation ε_j was calculated as the ratio between the sum of Monte Carlo event weights in the final sample and the sum of weights of events generated inside the fiducial area defined in Section 6:

$$\varepsilon_j = \frac{\sum_{i=1}^{N_{\text{rec}}} W_i}{\sum_{i=1}^{N_{\text{gen}}} W_i}. \quad (14)$$

Due to migration of shower cores from outside the fiducial area, this quantity can become larger than unity. The energy dependence of the parameters $\langle \log S_{125} \rangle$, $\sigma_{\log S_{125}}$, and ε was then fitted by empirical functions (see A). These functions were used to smooth statistical fluctuations in the response matrix and to extrapolate the range of simulations to higher energies in order to avoid potential artifacts that might be introduced by cutting the spectra off at 100 PeV.

The mean values and standard deviations are indicated in Fig. 11 by the points with vertical bars. The average shower sizes $\langle \log S_{125}(E_0) \rangle$ of proton showers for the three different zenith angular intervals Ω_k are shown in Fig. 12(a). Since the shower maximum lies above the detector throughout the covered energy range, showers from larger zenith angles are more strongly attenuated

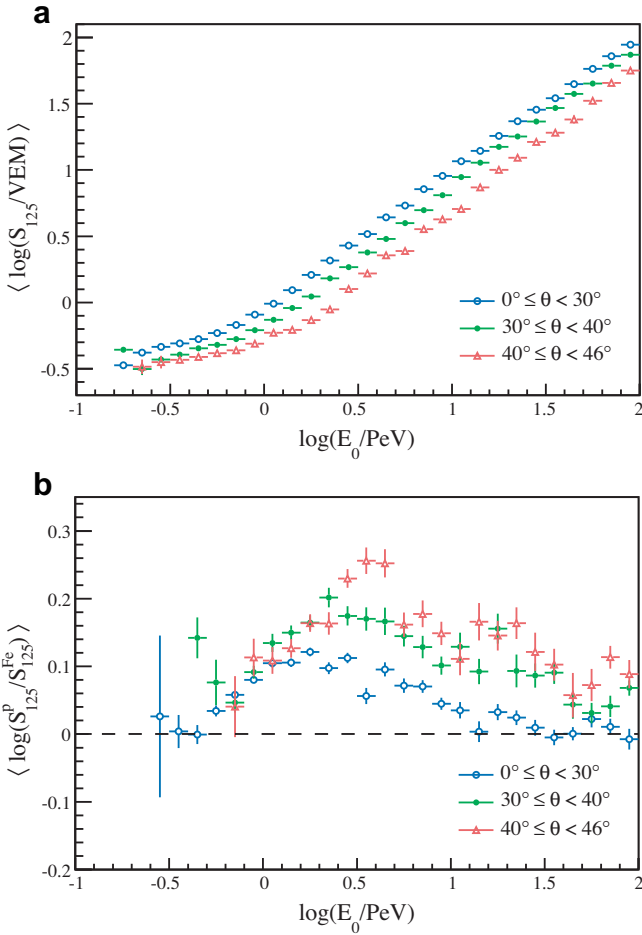


Fig. 12. (a) Mean shower size as a function of energy for proton showers of various zenith angles. (b) Shower size ratio between proton and iron showers. The ratio increases for larger zenith angles because the attenuation of iron showers is stronger than for proton showers. Both figures are based on an E^{-3} flux.

by the atmosphere and thus have a smaller shower size. In Fig. 12(b), these points are compared to the mean values for iron. The response matrices for proton and iron are very different: on average, iron showers have their first interaction at larger height leading to a larger shower age than for protons. Iron showers yield a smaller average signal than proton showers with the same primary energy. The difference between proton and iron increases at larger zenith angles. This zenith angle dependence has been exploited to test the consistency of our data with models for the mass composition, as will be discussed in Section 9. It also means that the systematic error due to primary composition will be larger for more inclined showers. Therefore, we restricted the final results to events with $\theta < 30^\circ$.

Fig. 13 shows the efficiencies ε obtained in the $\log E_0$ bins, which are the normalisations of the normal distributions of $\log S_{125}$ belonging to this bin, for protons and iron nuclei comparing all zenith angle intervals. The lines are fits to Eq. (A.3). Due to the requirement that the station with the largest signal is not on the border of the array (see Section 6), peak efficiencies were significantly below 100%. The maximum efficiencies in the three zenith angle ranges Ω_k correspond to the following effective areas:

$$\Omega_1 : A_{\text{eff}} = (1.051 \pm 0.013) \cdot 10^5 \text{ m}^2$$

$$\Omega_2 : A_{\text{eff}} = (0.900 \pm 0.019) \cdot 10^5 \text{ m}^2$$

$$\Omega_3 : A_{\text{eff}} = (0.803 \pm 0.012) \cdot 10^5 \text{ m}^2.$$

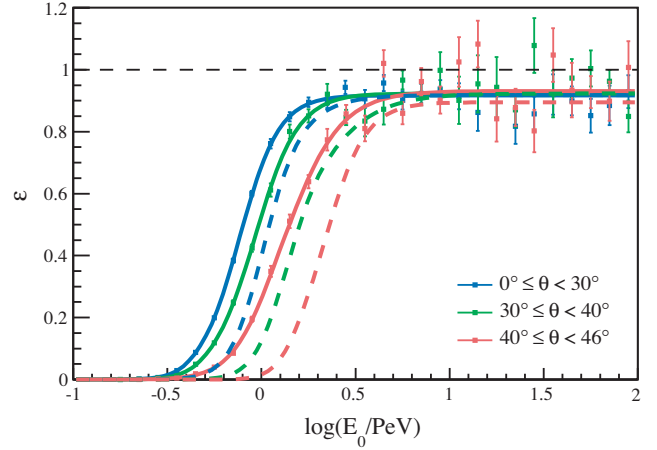


Fig. 13. Total efficiency for proton showers in different zenith angle ranges as a function of energy. The solid lines are fits of function (A.3), and the dashed lines are the results of the corresponding fits for pure iron.

The decrease of the effective area is a geometrical effect as the projection of the fiducial area on the shower plane scales with $\cos \theta$. Within statistical uncertainties the same values were obtained for iron primaries.

The spread of reconstructed energies (see Fig. 14) has been determined by transforming the $\log S_{125}$ distribution for a given E_0 back onto the $\log E_0$ axis. Above the threshold (between 1 and 3 PeV depending on zenith angle and primary mass assumption) this spread is a measure of the energy resolution. It improves with increasing energy, reaching values between 0.04 and 0.12 in $\log(E_0)$ at 100 PeV, corresponding to a resolution $\sigma_{E/E}$ between 9% and 23%. The drop below the energy threshold is an artifact of the procedure: In the threshold region the trigger condition biases toward upward fluctuating showers. This is one reason why this region is excluded from the final spectrum. This resolution only covers the statistical fluctuations, systematic uncertainties are discussed later in Section 8.

The response matrices obtained by this method depend on the primary composition assumption, as well as the hadronic interaction models and the parametrization of the South Pole atmosphere assumed in the simulation. Response matrices were generated for

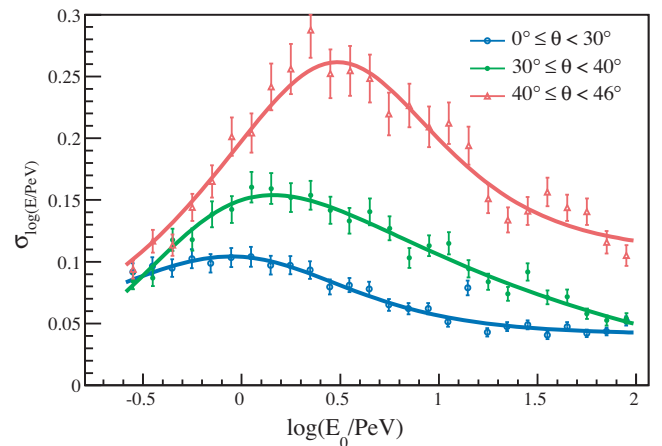


Fig. 14. Spread of reconstructed energies as a function of primary energy determined as described in the text for proton showers in different zenith angle ranges. The lines are fits according to Eq. (A.2) in order to guide the eye.

pure proton, pure iron, and for the two-component model described in Section 5.3.

7.3. Unfolding

Eq. (9) was solved using an iterative unfolding method based on Bayes' theorem described in Ref. [26], which takes into account the total efficiency ε and migration due to the fluctuations $\sigma_{\log(S)}$. Simply inverting the response matrix \mathbf{R} would lead to unnatural fluctuations in the result.

Starting from a prior distribution $P^{(k)}(E_{0j})$ ($j = 1, \dots, n$) in the k th iteration, the inverse of the response matrix \mathbf{R}^{-1} is constructed by inverting $P(S_{125,i}|E_{0,j}) = R_{ij}$ using Bayes' theorem:

$$P^{(k)}(E_{0j}|S_{125,i}) = \frac{P(S_{125,i}|E_{0,j})P^{(k)}(E_{0,j})}{\sum_{\ell} P(S_{125,i}|E_{0,\ell})P^{(k)}(E_{0,\ell})}. \quad (15)$$

Then, an estimate of the energy spectrum $\widehat{N}_j^{e(k)}$, $j = 1, \dots, n$, is obtained from the shower size spectrum N_i^s , $i = 1, \dots, n$:

$$\widehat{N}_j^{e(k)} = \frac{1}{\varepsilon_j} \sum_i N_i^s P^{(k)}(E_{0j}|S_{125,i}). \quad (16)$$

In the last step of the iteration, $P^{(k)}(E_{0j})$ is replaced by

$$P^{(k+1)}(E_{0j}) = \frac{\widehat{N}_j^{e(k)}}{\sum_{\ell} \widehat{N}_{\ell}^{e(k)}}. \quad (17)$$

As initial prior, $P^{(0)}(E_{0j}) \sim E_0^{-3}$ was chosen.

After each iteration, the unfolded spectrum was folded with the response matrix, $\widehat{N}_i^{s(k)} = \sum_j R_{ij} N_j^{e(k)}$, and compared to the measured shower size spectrum. A convergence criterion was then defined using the change in χ^2 between $\widehat{N}_i^{s(k)}$ and the measured shower size spectrum N^s between two iterations k and $k+1$, as in [27]:

$$\Delta\chi^2(k, k+1) = \chi^2(\widehat{N}^{s(k)}, N^s) - \chi^2(\widehat{N}^{s(k+1)}, N^s). \quad (18)$$

This quantity decreases monotonically during the iteration process. However, at $\Delta\chi^2(k, k+1) = 0$ the unfolding would be equivalent to simply inverting $R_{ij}^{(k)}$ and the unfolded spectrum would fluctuate unnaturally. To avoid this, the iteration was terminated once $\Delta\chi^2(k, k+1)$ fell below a certain value $\Delta\chi_{\text{term}}^2$. The value of this limit was determined beforehand using a simple toy simulation in which a known spectrum was folded with the response matrix and then, after adding statistical fluctuations, unfolded again. In every iteration step of this unfolding procedure, the unfolded spectrum was compared to the known true spectrum. Finally, $\Delta\chi_{\text{term}}^2 = 1.1$ was chosen where the agreement with the true spectrum was best on average.

The error bars on the unfolded spectrum were determined by varying the shower size spectra within their statistical errors and repeating the unfolding. This was repeated $n = 3000$ times and the statistical errors in bin j were determined by comparing each unfolding result $N^{e(k)}$ to the average result $\langle N^e \rangle$:

$$\langle \sigma_j^e \rangle^2 = \frac{1}{n-1} \sum_{k=1}^n (N_j^{e(k)} - \langle N^e \rangle_j)^2. \quad (19)$$

Similarly, bin-to-bin correlations were obtained:

$$\text{cov}(i, j) = \frac{1}{n} \sum_{k=1}^n (N_i^{e(k)} - \langle N^e \rangle_i) (N_j^{e(k)} - \langle N^e \rangle_j). \quad (20)$$

It was verified with a simple toy model that this algorithm correctly reproduces a true input spectrum, which was folded with the detector response and that the error determination is correct [10].

7.4. Correction for snow

Snow can accumulate at any time on top of the IceTop tanks, but a manual measurement of the snow height is only possible during the austral summer and therefore is done only once every year. The detector simulation took the snow depths measured in January, 2007, into account. Data, on the other hand, were taken between June and October, 2007, when more snow had accumulated. In order to estimate the effect of this difference, the detector response to proton showers with primary energies of 1 PeV, 10 PeV and 30 PeV and zenith angles 0° , 30° and 40° was simulated assuming once the snow heights measured in January 2007 and once those measured in January 2008. In January 2007 the average snow depth on top of IceTop tanks was 20.5 cm, while in January 2008 the average height on top of the same tanks was 53.2 cm. Assuming constant increase in snow depth and proportionality between $\Delta \log S_{125}$ and snow depth, shower sizes in August, 2007, were estimated. This leads to the following zenith angle dependent energy corrections relative to the simulations based on the January 2007 snow height measurement, which were applied to all unfolded energy spectra. Within the statistical uncertainties, no energy dependence could be observed:

$$\begin{aligned} \Omega_1 : \Delta \log(E/\text{PeV}) &= 0.0368 \pm 0.0009, \\ \Omega_2 : \Delta \log(E/\text{PeV}) &= 0.0440 \pm 0.0013, \\ \Omega_3 : \Delta \log(E/\text{PeV}) &= 0.0513 \pm 0.0008. \end{aligned} \quad (21)$$

8. Systematic uncertainties

All systematic errors are summarized in Table 2. In the following, details about the determination of the uncertainties of the energy determination and the flux measurement will be given.

8.1. Snow height

To estimate the systematic error due to the energy correction for snow described in Section 7.4, snow accumulation was assumed proportional to wind speed. The numbers obtained in this way were compared to those assuming constant growth of the snow depth (see above). The result of this comparison was used as an estimate of the systematic error on energy determination due to snow height.

8.2. Variations of the atmosphere

As discussed in Section 2.4, variations of the atmosphere affect the observed shower sizes. The influence of two parameters of the atmosphere has been studied in a data driven way: the total overburden X_0 , and the altitude profile $dX_v(h)/dh$.

First, the days of data taking were ordered according to the total atmospheric overburden X_0 . Then the 50 days with the highest and the 50 days with the lowest overburden were selected from the total of 153 days. The average overburdens during these periods were $X_{\text{low}} = 679 \text{ g/cm}^2$ and $X_{\text{high}} = 700 \text{ g/cm}^2$, yielding a difference of $\Delta X = 21 \text{ g/cm}^2$. From the data taken during these days shower size spectra were created for each zenith range Ω_k .

By comparing the shower size spectra obtained in the two periods, the dependence of S_{125} with atmospheric overburden was derived. The RMS variation of the total atmospheric overburden between June 1 and October 31, 2007, of $\sigma_{X_v} = 9.86 \text{ g/cm}^2$ was used to estimate the systematic error on the energy determination due to atmospheric overburden variations. With the given statistical precision, an energy dependence of this variation could not be observed.

Table 2

Summary of systematic uncertainties of the energy and flux determination in the three zenith angle intervals Ω_1 , Ω_2 , and Ω_3 . The individual points are explained in the text. All numbers are given for the full energy range, unless otherwise stated. The main source of systematic uncertainty, the unknown primary composition, will be treated separately in the next section.

Uncertainty	$0^\circ \leq \theta < 30^\circ$		$30^\circ \leq \theta < 40^\circ$		$40^\circ \leq \theta < 46^\circ$	
	Energy (%)	Flux (%)	Energy (%)	Flux (%)	Energy (%)	Flux (%)
Snow height	0.4		0.4		0.4	
Overburden variation	0.26		1.9		3.0	
Atmosphere profile variation	2.5		1.8		1.1	
Atmosphere model	0.9		1.1		0.6	
MC Calibration	1.5		1.5		1.5	
PMT saturation, $E_0 \leq 10$ PeV	0.5		0.5		0.5	
PMT saturation, $E_0 > 10$ PeV	<2.5		<2.5		<2.5	
Droop	1.5		1.5		1.5	
Calibration stability	3.0		3.0		3.0	
Interaction model, $E_0 \leq 10$ PeV	2.1		4.3		2.0	
Interaction model, $E_0 > 10$ PeV	3.3		5.5		4.1	
Shower attenuation	3.0		3.0		3.0	
Flux model	0.7		1.0		1.0	
$\langle \log S \rangle$ and $\sigma_{\log S_{125}}$	0.7		1.2		0.8	
Cut passing rates		3.0		3.0		3.0
Efficiency		0.9		1.6		1.2
Unfolding procedure		1.6		3.4		5.2
Total: $E_0 \leq 10$ PeV (%)	6.0	3.5	7.2	4.8	6.3	6.1
$E_0 > 10$ PeV (%)	6.9	3.5	8.3	4.8	7.6	6.1

In contrast to total overburden the altitude profile of the atmosphere at South Pole undergoes a clear annual cycle. To study the effect of varying the atmospheric profile on air shower measurements the data taking period was divided into a period of very dense atmosphere (July 25th to October 10th) and one when the atmosphere was less dense (remaining days between June 1st and July 24th and between October 11th and October 31st). Shower size spectra were extracted from the data taken in these two periods and by comparing those spectra, an additional systematic error due to the atmospheric profile variation was derived.

8.3. Atmosphere model in simulation

The CORSIKA simulations used a model of the South Pole atmosphere. A systematic uncertainty arises from the choice of model since it does not exactly match the average atmosphere during the data taking period. To estimate this error on the energy scale simulations two different atmosphere parametrizations were compared. CORSIKA atmosphere model 12 (July 1, 1997), which was used in the unfolding procedure, has a total overburden of 692.9 g/cm² and atmosphere model 13 (October 1, 1997) has a total overburden of 704.4 g/cm². Averaging the difference in $\log S_{125}$ for proton showers between the two simulations above $E_0 = 1$ PeV the systematic error due to the difference of the simulated overburden and the average overburden in data was determined.

8.4. Calibration

Systematic uncertainties due to calibration can arise for two reasons: variations of the calibration constants between calibration runs, and a discrepancy between the calibration of the experiment and the detector simulation.

The first point was addressed by studying the variation of the number of photoelectrons corresponding to 1 VEM between calibration runs. From this variation the systematic uncertainty on the energy reconstruction due to the tank calibration was estimated to be 3.0%.

The simulated tanks were calibrated using the same procedure as for the real tanks, as described in Section 5.2. The conversion factor between Cherenkov photons and photo electrons resulting from this calibration has a statistical uncertainty of 1.5%, which was included as a systematic error on the energy.

8.5. Droop

The toroid used to decouple the PMT from the signal capture electronics introduces a significant droop effect (see Section 2.3), which was not corrected for in the analysis. Not correcting for droop is not a source of systematic uncertainty in itself if it is done consistently in data and simulation. However, discrepancies in the way the droop effect is simulated in the detector Monte Carlo, may lead to undesired systematic effects. In order to quantify these effects, the effect of a droop correction algorithm on the recorded charges was compared between data and simulation. From this comparison a systematic error on the energy determination of 1.5% was derived.

8.6. PMT saturation

Inaccuracies in the simulated saturation behaviour of the PMT could introduce systematic uncertainties on the energy determination mostly at high energies. In simulation, saturation sets in at higher charges than in the experiment. In order to estimate the effect of this discrepancy on the energy spectrum, an artificial, charge-based saturation function was applied to the simulated charges to bring the simulated charge spectrum into agreement with experimental data. Then, the simulated showers were reprocessed, and the change in $\log(S_{125}/\text{VEM})$ was used to estimate the systematic error on the energy. For primary energies below 10 PeV, the systematic error due to the difference in saturation behaviour is less than 0.5%. Above 10 PeV it increases exponentially to a value of 2.5% at 100 PeV.

8.7. Cut efficiencies

Differences in the effects of quality cuts described in Section 6 when applied to experimental and simulated data lead to a systematic uncertainty on the efficiency and consequently on the flux normalization. Passing rates of all cuts for data and Monte Carlo events above threshold are listed in Table 1. There is a relative difference of 3.0% between data and two-component Monte Carlo in the total cumulative passing rate, which is included in the systematic uncertainty on the flux. No significant zenith dependence on the difference between data and simulation was found.

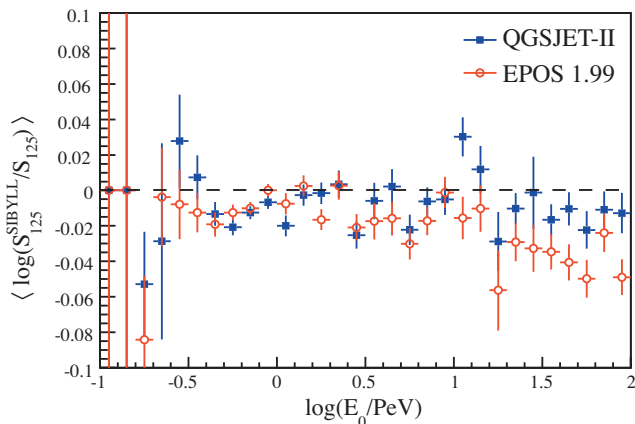


Fig. 15. Shower size ratio for the two-component assumption between SIBYLL and QGSJET and EPOS based Monte Carlo simulations for the two component primary assumption and showers with zenith angles up to 30° .

8.8. Interaction model

Small simulation datasets of proton and iron showers created using the high energy hadronic interaction models QGSJET-II and EPOS 1.99 in addition to SIBYLL were used to estimate the systematic uncertainty due to the modeling of hadronic interactions. Fig. 15 shows the shower size ratio between SIBYLL and the alternative simulations as a function of primary energy for the two-component primary composition assumption and zenith angles up to 30° . Simulations with SIBYLL seem to yield systematically smaller shower sizes, and the same observation was made for more inclined showers.

The systematic error derived in this way is purely based on a comparison of the three interaction models. All of these models have different known strengths and weaknesses in their description of the underlying physics. Additionally, they all include extrapolations of cross-sections and multiplicity distributions to energy ranges not accessible by current collider experiments which are relevant in the first few cosmic ray interactions. Thus, there is an unknown systematic error in case the range of hadronization models does not cover the true behavior.

8.9. Shower attenuation

Since this analysis relies on shower attenuation to extract information about the primary mass composition, we want to ensure that the observed attenuation of the measured shower sizes is compatible with simulation lying between proton and iron attenuation. The method of constant intensity cuts [28,29] was used to determine shower attenuation. Spectra of $N(> S_{125})$ in three zenith angle ranges were created by integrating the spectra in Fig. 10 left for both experimental and simulated data. Assuming an isotropic flux of cosmic rays, shower sizes S_{125} at different zenith angles that result in an equal number of events $N(> S_{125})$ correspond to the same primary energy for any constant mass composition. Shower attenuation, i.e. the zenith dependence of S_{125} for a given primary energy, was measured by determining the values of S_{125} in the three zenith angle ranges that correspond to six different values of $N(> S_{125})$. These six constant intensity cuts correspond to six different primary energies. In simulation, intensity levels were chosen such that the shower size of proton in the most vertical zenith range was the same as in experimental data and for iron cuts were made at the same primary energy as for protons. This way no assumption on the absolute normalization of the spectrum nor an absolute energy scale in experimental data are needed. Fig. 16 shows the difference between sizes of inclined showers and those in the most vertical zenith range. Attenuation in experimental data is between the values of proton and iron or consistent with proton. As discussed in Section 7.2, iron showers are more strongly attenuated than proton showers. Thus, considering the primary mass dependence of shower attenuation the description of attenuation in the simulation is consistent with experimental data at the reconstruction level.

However, the predicted shower attenuation differs between hadronic interaction models. This leads to a zenith dependent systematic uncertainty on the change of observed flux for a given primary energy with mass. Mass dependence of shower attenuation shown in Fig. 12(b) for the SIBYLL hadronic interaction model was compared to corresponding results obtained with the hadronic interaction model EPOS. From the observed zenith dependences of the differences between both models a systematic error of the shower attenuation of 3% was estimated. Since data from only three zenith ranges is available a zenith dependence of this error

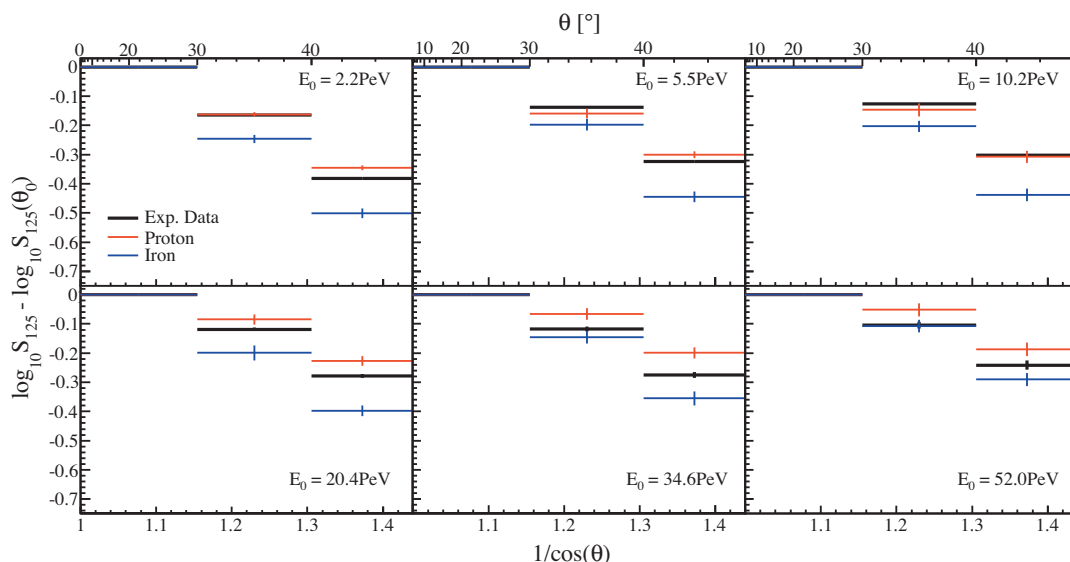


Fig. 16. Shower attenuation obtained from six constant intensity cuts applied to experimental and simulated shower size spectra as described in Section 8.9. The corresponding primary energies in simulation are given in each panel.

could not be observed. Note, that this uncertainty may already be partially included in the discussion of the systematic error absolute energy scale in the previous subsection.

8.10. Response matrix

Limited Monte Carlo statistics introduce uncertainties into the response matrix. Assuming the efficiency is constant above the threshold, the flux error induced by uncertainties of the detector response can be estimated by the fit error on c_0 in Eq. (A.3). The uncertainties on the parameters a_0 and b_0 in Eqs. (A.1) and (A.2) translate to an uncertainty on the energy in the unfolding process. These statistical uncertainties on the response matrix were also included in the systematic error of the final result.

Additionally, the flux model used in the simulation also influences the response matrix. A harder spectrum leads to larger average shower sizes in an energy bin than a softer one. Simulations based on an E^{-2} flux and an E^{-4} flux were compared with the standard simulation which assumes a power law of E^{-3} . Above the threshold the resulting difference in shower size appears to be independent of primary energy. The differences in shower size between the two extreme spectral indices were used as an estimate of the systematic error on energy scale due to the assumed flux model. The resulting systematic uncertainty on the energy spectrum is less than 1%.

8.11. Unfolding procedure

Two parameters besides the response matrix influence the result of the unfolding: the termination criterion $\Delta\chi^2_{\max}$ and the prior distribution P_0 . Varying the termination criterion, lead to a variation of the total flux, which was included as a systematic error.

In addition, varying the spectral index of the initial prior P_0 between -2.5 and -3.5 , a variation of the total flux of about 2% was observed. Below the knee region around 3 to 4 PeV, the spectral index seems to depend on the prior (in the most inclined zenith interval even up to 10 PeV. Varying the prior lead to a variation of the spectral index below the knee in the most vertical zenith band by ± 0.01 , and in the most inclined zenith range by ± 0.025 . At higher energies variations appear to be purely statistical.

8.12. Summary of systematic errors

Systematic uncertainties are summarized in Table 2. The total systematic uncertainty was determined by quadratically adding the individual contributions. The error on the determination of the primary energy in the most vertical zenith angle range is 6.0% below $E_0 = 10$ PeV, and 6.9% above. Main contributions are the calibration stability (3.0%), atmosphere (2.7% in total), and the hadronic interaction model (2.1%/3.3%). Furthermore, a flux uncertainty of 3.5% is caused by differences in cut efficiencies between data and Monte Carlo, the efficiency calculation in Monte Carlo, and the termination criterion and seed in the unfolding procedure. However, the main source of systematic error is the unknown primary composition, which will be discussed in detail in the next section.

9. Energy spectrum

Fig. 17 shows energy spectra for three zenith angular intervals unfolded under three assumptions on the mass composition: all-proton, all-iron and the two-component model [24] explained in Section 5.3. The lower end of the energy range of each spectrum was selected where the efficiency according to Eq. (A.3) reached 90% of the maximum value. The threshold was determined

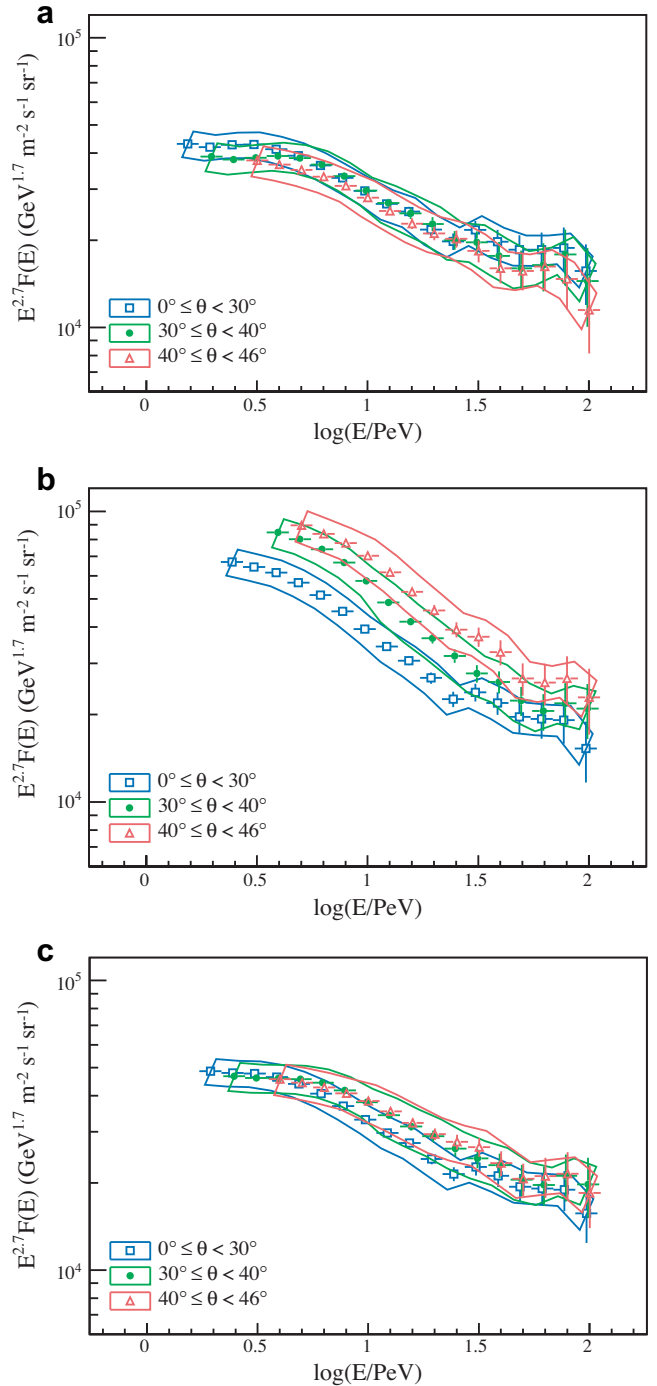


Fig. 17. Resulting flux measured with IceTop, weighted with $E^{2.7}$. The reconstruction was done using three different composition assumptions as described in the text: (a) pure proton, (b) pure iron, and (c) Glasstetter's two-component model. In each case, the data were divided into three different zenith angle bands equidistant in $\sec(\theta)$. Based on the assumption of an isotropic flux, the three individual spectra should agree. The boxes indicate the systematic errors.

individually for each zenith interval and primary composition assumption. That way the threshold region is excluded and the efficiency can be assumed almost constant. Based on the energy resolution, a binning of 10 bins per decade was chosen.

The systematic error bands were constructed from the numbers in Table 2 by defining error boxes around each data point as follows: The quadratic sum of flux error and the energy error weighted with $E^{2.7}$ was used as a vertical error bar. The horizontal error bar is given by the error on energy determination. The error

bands were then constructed by connecting the edges of these boxes.

In Fig. 12(b) it was shown that the difference in shower size between simulated proton and iron showers increases with zenith angle due to the increasing slant depth in the atmosphere, which has a different effect for the different masses: iron showers are attenuated more strongly with increasing slant depth than proton showers. Since the cosmic-ray flux is isotropic to a few per thousand [30,31] the flux measured in different zenith angular intervals has to be the same.

In case of the pure proton assumption (Fig. 17(a)) a good agreement between the three spectra is observed. Assuming pure iron (Fig. 17(b)), the individual spectra for the three different zenith bands clearly disagree at low energies while they start to converge towards higher energies. Agreement of the three spectra in case of the two-component model (Fig. 17(c)) is good at low and high energies. In the intermediate energy range there is some deviation between the spectrum obtained from steepest zenith angle range

and the other two spectra. However, they are still consistent when considering systematic uncertainties.

Using a χ^2 comparison of fluxes in each bin of the spectra from the three zenith angle ranges, pure iron could be excluded at a >99% confidence level below 24 PeV. This comparison took into account both statistical and systematic errors. The latter were treated in a conservative way by assuming no correlations between them for the different zenith angle intervals. Using the same comparison and various mixtures of proton and iron, up to 70% of iron cannot be excluded at any energy. A mixture of protons with 70% iron correspond to a mean logarithmic mass of $\ln(A) \approx 2.8$. These results are in agreement with previous measurements of the composition of cosmic rays, which have established a light composition around 1 PeV and an increasing mass above the knee [32].

In Fig. 18, the results obtained in the steepest zenith angle range Ω_1 with three primary composition assumptions are compared: pure proton, the two-component model, and 70% iron. Only the most vertical zenith angle range was chosen, because the difference in size for showers initiated by different primaries is smallest in this zenith interval, as seen in Fig. 12(b), and because systematic uncertainties are smallest in this range. Because the difference in shower size between proton and iron decreases toward higher energies, the spectrum obtained under the 70% iron assumption is softer than the proton-based result. While the composition model has a sizable influence on the measured all-particle flux below 10 PeV, the difference between the two extreme assumptions of pure proton and 70% iron almost disappears above 30 PeV.

As the final result the cosmic ray spectrum is given for the two-component model, which represents a realistic mixture of proton and iron and is in good agreement with data. Fig. 19 shows the result, without the systematic error bands, in comparison to a selection of other experiments [33–47]. Within systematic errors, our results are in good agreement with these previous measurements. An analysis of coincident events in IceTop and IceCube [48] using a different dataset acquired with a different experimental configuration resulted in a somewhat lower total flux. However, the results are compatible within systematic errors.

Table 3 lists the measured fluxes including statistical and systematic errors. The systematic errors on the flux have been calculated by transforming the systematic error on energy into a flux error based on the local spectral index γ : $\Delta F/F = \gamma \Delta E/E$. This was

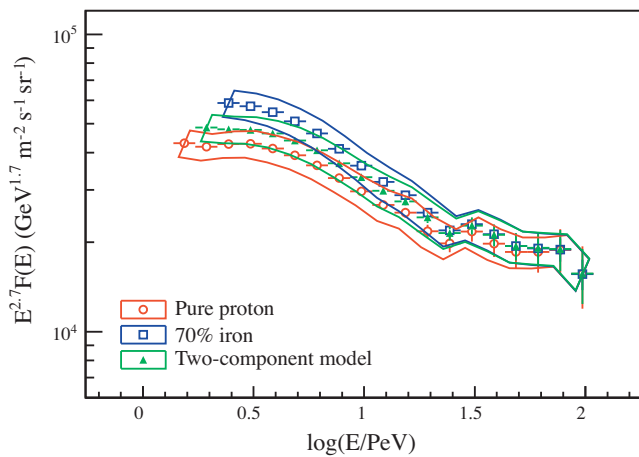


Fig. 18. All particle spectra obtained with IceTop from air showers with zenith angles up to 30° under three different composition assumptions: pure proton, the two-component model, and a mixture of 30% proton and 70% iron.

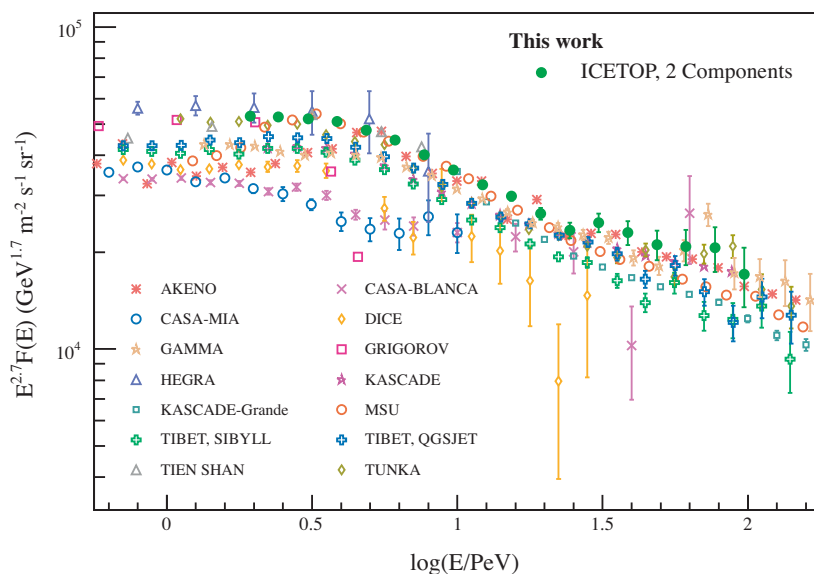


Fig. 19. The all-particle cosmic ray energy spectrum obtained from the analysis of IceTop data of events with zenith angles up to 30° compared to a selection of other experimental results [33–47].

Table 3

All-particle cosmic ray energy spectra measured by the IceTop air shower array for the two-component primary composition assumptions using the hadronic interaction model SIBYLL2.1. Systematic errors from Table 2 and due to composition are listed separately.

Energy (10^6 GeV)	$dF/dE \pm \text{stat} \pm \text{syst} \pm \text{comp}$ ($\text{GeV}^{-1} \text{m}^{-2} \text{s}^{-1} \text{sr}^{-1}$) Two-component assumption
1.94	$(5.612 \pm 0.018 \pm 1.2^{+1.3}_{-0.8}) \times 10^{-13}$
2.44	$(2.974 \pm 0.012 \pm 0.6^{+0.7}_{-0.3}) \times 10^{-13}$
3.07	$(1.589 \pm 0.008 \pm 0.4^{+0.3}_{-0.17}) \times 10^{-13}$
3.86	$(8.30 \pm 0.06 \pm 1.8^{+1.5}_{-1.0}) \times 10^{-14}$
4.86	$(4.22 \pm 0.04 \pm 1.0^{+0.7}_{-0.21}) \times 10^{-14}$
6.12	$(2.098 \pm 0.023 \pm 0.5^{+0.3}_{-0.23}) \times 10^{-14}$
7.71	$(1.021 \pm 0.015 \pm 0.24^{+0.13}_{-0.12}) \times 10^{-14}$
9.70	$(4.92 \pm 0.10 \pm 1.2 \pm 0.5) \times 10^{-15}$
12.21	$(2.38 \pm 0.06 \pm 0.6^{+0.17}_{-0.25}) \times 10^{-15}$
15.38	$(1.18 \pm 0.04 \pm 0.29^{+0.06}_{-0.1}) \times 10^{-15}$
19.36	$(5.58 \pm 0.23 \pm 1.4^{+0.21}_{-0.6}) \times 10^{-16}$
24.37	$(2.66 \pm 0.15 \pm 0.6^{+0.95}_{-0.21}) \times 10^{-16}$
30.68	$(1.51 \pm 0.10 \pm 0.4^{+0.015}_{-0.07}) \times 10^{-16}$
38.62	$(7.5 \pm 0.7 \pm 1.9^{+0.10}_{-0.5}) \times 10^{-17}$
48.62	$(3.72 \pm 0.4 \pm 0.9^{+0.010}_{-0.12}) \times 10^{-17}$
61.21	$(1.97 \pm 0.25 \pm 0.5^{+0.010}_{-0.06}) \times 10^{-17}$
77.06	$(1.05 \pm 0.17 \pm 0.27^{+0.07}_{-0.01}) \times 10^{-17}$
97.01	$(4.7 \pm 1.0 \pm 1.4 \pm 0.1) \times 10^{-18}$

added quadratically to the systematic error on the flux. The error due to the unknown composition is given by the difference between the two-component result and the 70% iron and pure proton spectra, respectively.

The spectrum has been fitted with function (6) transformed such that the intensity I_{knee} at energy E_{knee} is used as a reference. In the fit, statistical errors and bin-to-bin correlations according to Eqs. (19) and (20) were used. The results are listed in Table 4.

The systematic uncertainty of the knee energy E_{knee} is the systematic error on energy determination at that primary energy as given in Section 8. The systematic error of I_{knee} has been obtained by quadratically adding the systematic error on the flux determination and the systematic energy error transformed into a flux uncertainty based on the local spectral index. In order to determine systematic errors on γ_1 and γ_2 , the fit was repeated using the systematic errors of the data points as statistical errors. The errors due to primary composition were determined by the range of parameter values obtained when fitting the pure proton and the 70% iron results in the same way. The sharpness parameter ε of the knee was included to obtain an unbiased fit, but is not very well constrained by the data. Its value indicates a relatively sharp knee, and in fact we cannot distinguish between a smooth and an infinitely sharp knee ($\varepsilon \rightarrow \infty$). Fixing ε to very large values resulted in a χ^2 that is not significantly worse.

Above about 22 PeV a possible flattening of the spectrum can be observed independent of primary composition assumption. This

Table 4

Fit parameters of the cosmic-ray energy spectrum according to function (6). Systematic errors and uncertainties due to primary composition (“comp”) were derived as described in the text.

Parameter	Best fit
$I_{\text{knee}}/10^{-7} \text{m}^{-2} \text{s}^{-1} \text{sr}^{-1}$	2.38 $\pm 0.23(\text{stat}) \pm 0.5(\text{syst})$ $^{+1.42}_{-0.97}(\text{comp})$
$E_{\text{knee}}/\text{PeV}$	4.32 $\pm 0.22(\text{stat}) \pm 0.26(\text{syst})$ $^{+0.38}_{-1.1}(\text{comp})$
γ_1	-2.759 $\pm 0.015(\text{stat}) \pm 0.5(\text{syst})$ $^{+0.26}_{-0.011}(\text{comp})$
γ_2	-3.107 $\pm 0.016(\text{stat}) \pm 0.4(\text{syst})$ $^{+0.03}_{-0.08}(\text{comp})$
ε	9 $\pm 3(\text{stat})$
χ^2/N_{df}	19.4/13

Table 5

Parameters of the flattening of the spectrum at high energy. The errors given are only statistical.

$E_{\text{break}}/\text{PeV}$	23	± 5
γ_3	-2.87	± 0.09
χ^2/N_{df}	7.1/11	

feature is also visible in the measured shower size spectra (see Fig. 10). The position of this flattening does not significantly depend on the primary composition assumption because proton and iron showers with $\theta < 30^\circ$ have almost the same shower size in this energy range (see Fig. 12(b)). In order to test its statistical significance, the spectra were fitted with function (6) plus an additional hard break at E_{break} with spectral index γ_3 . The goodness of fit improves to $\chi^2/N_{\text{df}} = 7.1/11$, which corresponds to a significance of 3.2 standard deviations. This, however, does not include systematic errors. The parameters of the flattening are listed in Table 5.

While a pure power law above the knee cannot be excluded, a flattening of the spectrum is preferred by the data. Such a behavior has recently been reported by KASCADE-Grande [49]. In addition, they observed a steepening of the spectrum just below 10^{17} eV, which could not be seen in this analysis due to the limited energy range. Several models of the cosmic ray energy spectrum predict features above the knee similar to the one observed [2]. For instance, assuming a pure rigidity dependence of the knee there can be “gaps” or “concavities” between the knees of two primaries if intermediate nuclei are insufficiently abundant to fill in this range. Alternatively, a second component of galactic cosmic rays could also create the observed behavior.

10. Summary

We have derived the all-particle cosmic ray energy spectrum in the energy range between 1 PeV and 100 PeV from data taken between June and October 2007 with the 26-station configuration of the IceTop air shower array at South Pole.

Using the air shower simulation package CORSIKA with the high-energy hadronic interaction model SIBYLL2.1 the relation between shower size S_{125} and primary energy, as well as the detection efficiency and energy resolution were determined. Three different assumption on the primary mass composition were used as input: pure proton, pure iron and a simple two-component model [24]. Based on these results, the shower size spectra obtained in three zenith angle ranges were unfolded with a Bayesian unfolding algorithm to obtain energy spectra.

In case of pure proton and the two-component model, it was found that the spectra obtained in the different zenith angle ranges were in good agreement. In the pure iron case, on the other hand, a strong disagreement between the three spectra was observed at low energies. Since one can safely assume that cosmic rays are isotropic in the given energy range, the spectra in all three zenith angle ranges should be the same. With this assumption, we concluded that pure iron primaries can be excluded below energies of 24 PeV.

We showed that the attenuation of air showers with increasing zenith angle bears exploitable information about the chemical composition of cosmic rays. Nevertheless, the main source of systematic error in the reconstruction of the energy spectrum still remains the primary mass composition. The systematic error due to the choice of a hadronic interaction model is relatively small in this analysis because most air shower signals are dominated by the electromagnetic component of an air shower, which is relatively well understood. For the final result, only the spectra obtained from the most vertical zenith angle range, $0^\circ \leq \theta < 30^\circ$, were considered because in this range the dependence on composition and systematic errors are smallest.

By fitting the energy spectrum with function (6), the knee position was determined at 4.3 PeV with spectral indices of -2.76 below and -3.11 above. Around an energy of 22 PeV an indication of a flattening of the cosmic ray spectrum to an index of about -2.85 was observed at the 3σ level.

Since the completion of IceTop and IceCube in 2011, the array is three times larger than the configuration used in this analysis. With this larger array, statistics and containment of high-energy showers will be much better, allowing to extend the analysis to higher energies. The main strength of IceTop, however, is the possibility to measure air showers at the surface in coincidence with high-energy muons penetrating deep enough into the ice to trigger IceCube. The ratio between the two measurements is highly sensitive to the mass of the primary particle.

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Appendix A. Parametrization of the response matrix

In order to mitigate the effects of statistical fluctuations in the unfolding procedure, the response matrices described in Section 7.2 were separated into mean logarithmic shower size ($\langle \log S_{125} \rangle$), resolution $\sigma_{\log S}$, and efficiency ε . There dependences on $x = \log E_p$ were then fitted by empirical functions:

$$\langle \log S_{125} \rangle(x) = a_0 + x + \ln \left(\frac{\exp(a_1 x) + \exp(a_2 + a_3 x + a_4 x^2)}{1 + \exp(a_2)} \right), \quad (\text{A.1})$$

$$\sigma_{\log S}(x) = \frac{b_0(1 + \exp(b_3 b_4)) + \exp(-b_1)(\exp(-b_2 x) - 1)}{1 + \exp(-b_3(x - b_4))} \quad (\text{A.2})$$

and

$$\varepsilon(x) = \begin{cases} \frac{c_0}{1 + \exp(-c_1(x - c_2) + c_3(x - c_4)^2)} & x < c_4 \\ \frac{c_0}{1 + \exp(-c_1(x - c_2))} & x \geq c_4 \end{cases}. \quad (\text{A.3})$$

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