

Improved Regression Analysis of Temperature–Dependent Strain–Gage Balance Calibration Data

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An improved approach is discussed that may be used to directly include first and second order temperature effects in the load prediction algorithm of a wind tunnel strain–gage balance. The improved approach was designed for the Iterative Method that fits strain–gage outputs as a function of calibration loads and uses a load iteration scheme during the wind tunnel test to predict loads from measured gage outputs. The improved approach assumes that the strain–gage balance is at a constant uniform temperature when it is calibrated and used. First, the method introduces a new independent variable for the regression analysis of the balance calibration data. The new variable is defined as the difference between the uniform temperature of the balance and a global reference temperature. This reference temperature should be the primary calibration temperature of the balance so that, if needed, a tare load iteration can be performed. Then, two temperature–dependent terms are included in the regression models of the gage outputs. They are the temperature difference itself and the square of the temperature difference. Simulated temperature–dependent data obtained from Triumph Aerospace’s 2013 calibration of NASA’s ARC–30K five–component semi–span balance is used to illustrate the application of the improved approach.

Nomenclature

AF	= axial force in the balance axis system
$\mathbf{C}_1, \mathbf{C}_2$	= matrices needed for AIAA’s load iteration equation (see Ref. [1], p.19, Eq. (3.3.7))
dT	= temperature difference used as “dependent” variable
dTi	= temperature difference used as “independent” variable (always equals dT)
F	= balance load symbol (force or moment)
\mathbf{F}_ξ	= vector of predicted balance loads for load iteration step ξ
\mathbf{H}	= load dependent matrix that is used in the load iteration equation
k	= gage index
n	= total number of balance load components (equals the total number of balance gages)
NF	= normal force in the balance axis system
PM	= pitching moment in the balance axis system
R	= electrical output of a strain–gage
R'	= part of the electrical output that is caused by the balance loads
R''	= part of the electrical output that is caused by the temperature difference
RM	= rolling moment in the balance axis system
rAF	= dimensionless electrical output of the axial force gage, $microV/V$
rNF	= dimensionless electrical output of the normal force gage, $microV/V$
rPM	= dimensionless electrical output of the pitching moment gage, $microV/V$
rRM	= dimensionless electrical output of the rolling moment gage, $microV/V$
rYM	= dimensionless electrical output of the yawing moment gage, $microV/V$

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T	= measured uniform temperature of the balance
T_o	= global reference temperature of the balance
YM	= yawing moment in the balance axis system
c_0, c_1, \dots	= regression coefficients of the fitted strain-gage outputs
$\Delta \mathbf{R}$	= vector of gage outputs and temperature difference that is an input for the load calculation
μ	= total number of coefficients that are exclusively associated with balance loads
ξ	= load iteration step index

I. Introduction

Different techniques are used in the aerospace testing community to predict strain-gage balance loads from gage outputs during a wind tunnel test. The load prediction is usually based on the result of a multivariate regression analysis of strain-gage balance calibration data. The *Iterative Method*, for example, first fits strain-gage outputs of a balance as a function of loads that were applied during the calibration. Then, resulting regression coefficients are converted to data reduction matrix coefficients so that loads can be predicted from measured gage outputs during a wind tunnel test using a load iteration scheme (see Refs. [1] to [4] for detailed discussions of the *Iterative Method*).

By design, the *Iterative Method* makes the assumption that the number of “independent” variables, i.e., balance loads, equals the number of “dependent” variables, i.e., strain-gage outputs. This implicit requirement made it difficult in the past to include a separate term in the regression model of a strain-gage output that describes temperature effects. Therefore, some researchers completely avoided the use of temperature-dependent regressors in the equations of the *Iterative Method* by simply assuming that the regression coefficients associated with the balance loads are a function of temperature. This approach has two disadvantages: (i) it requires a separate least squares fit for each calibration temperature of the balance, and, (ii) additional post-calibration data processing is needed to characterize the temperature-dependency of the regression coefficients of the balance loads for use during the wind tunnel test.

In 2011, the present author developed an alternative to the data processing approach that is described in the previous paragraph. He showed that it is possible to use “temperature-dependent” regressors side-by-side with “load-dependent” regressors in math models of gage outputs as long as the temperature is used as both an “independent” and “dependent” variable in the equations that the *Iterative Method* applies (for more detail see Refs. [5], [6]). The author already described in a previous paper how temperature sensitivities of strain-gage outputs could potentially be combined with the *Iterative Method* so that temperature dependencies are included to a certain degree in the prediction of balance loads (see Ref. [6]). In 2014 he developed a refinement of his original approach that uses a more general description of temperature effects for the regression analysis of strain-gage balance calibration data. Basic ideas of the refined approach will be discussed in the next section of the paper. Afterwards, simulated temperature-dependent calibration data of a five-component semi-span balance is used to illustrate the application of the new approach.

II. Extended Regression Model of the Gage Outputs

In principle, the author’s improved approach for the inclusion of temperature effects in regression models of the gage outputs applies the *Principle of Superposition*. It is simply assumed that temperature effects cause an “offset” in the electrical outputs that is a function of the difference between the uniform balance temperature and a global reference temperature. This temperature difference becomes the new “independent” variable in the regression models of the gage outputs. It has to be used as both an “independent” and “dependent” variable in the equations of the *Iterative Method* so that the load iteration scheme defined in Ref. [1] can still be applied (see also the detailed discussion of this topic in Ref. [5]). The temperature difference can be expressed as follows

$$dT = T - T_o \quad (1)$$

where T is the uniform balance temperature and T_o is the chosen global reference temperature. This reference temperature should be the primary calibration temperature of the balance so that, if needed, a tare load iteration can be performed to estimate loads caused by the calibration hardware and the metric part of the

balance (see, e.g., Ref. [1], p. 17 and pp. 25–40, for a discussion of the tare load iteration process). Ideally, the reference temperature should be located within the range of all uniform temperatures that the balance is expected to experience during the wind tunnel test.

Now, after assuming that (i) temperature effects influencing the gage outputs can be described by both a linear and a quadratic term and that (ii) no justification for the use of a temperature–dependent cross–product term exists, the following two new regressors are introduced in the regression model of each strain–gage output:

$$\underline{\text{one new independent variable}} : dT \quad \Longrightarrow \quad \underline{\text{two new regressors}} : dT, (dT)^2$$

Then, assuming that the balance has a total number of n gages and a total number of n load components, the “expanded” regression model of a gage output with index k becomes:

$$R(k) = R'(k) + R''(k) \quad ; \quad 1 \leq k \leq n \quad (2a)$$

where

$$R'(k) = c_0(k) + c_1(k) \cdot F(1) + c_2(k) \cdot F(2) + \cdots + c_\mu(k) \cdot |F^3(n)| \quad (2b)$$

$$R''(k) = c_{\mu+1}(k) \cdot dT + c_{\mu+2}(k) \cdot (dT)^2 \quad (2c)$$

The symbol $R(k)$ in Eq. (2a) above describes the total electrical output of the chosen gage output. $R'(k)$ is the part of the total output that is associated with balance loads (see load symbols $F(1), \dots, F(n)$). It is identical with the regression model of the gage outputs that AIAA recommends as an upper bound for use with the *Iterative Method* (see, e.g., Ref. [1], Eq. (3.1.2) or Eq. (3.1.3)). $R''(k)$ is the part of the total output that is associated with the temperature difference (see symbol dT). The symbols $c_0(k), c_1(k), \dots, c_{\mu+2}(k)$ are the final regression coefficients of the total electrical output of the gage. For clarity, Eq. (2a) can be expressed in slightly different form. We can write for $1 \leq k \leq n$:

$$R(k) = \underbrace{c_0(k) + c_1(k) \cdot F(1) + \cdots + c_\mu(k) \cdot |F^3(n)|}_{\text{terms associated with calibration loads}} + \underbrace{c_{\mu+1}(k) \cdot dT + c_{\mu+2}(k) \cdot (dT)^2}_{\text{terms associated with temperature}} \quad (3a)$$

In addition, the regression model of the new “dependent” variable dT can be expressed as follows:

$$\underbrace{dT}_{\text{dep.}} = 0 + 0 \cdot F(1) + 0 \cdot F(2) + \cdots + 0 \cdot |F^3(n)| + 1.0 \cdot \underbrace{dT}_{\text{indep.}} + 0 \cdot (dT)^2 \quad (3b)$$

Equations (3a) and (3b) describe the set of $n + 1$ linear equations that define the least squares problem of the temperature–dependent balance calibration data set. Fortunately, the regression coefficients of the “dependent” variable dT defined in Eq. (3b) are implicitly known as dT is used as both a “dependent” and “independent” variable. Consequently, coefficient $c_{\mu+1}(n + 1)$ is “1” and $c_\rho(n + 1)$ is “0” for $\rho \neq \mu + 1$. At this point, the extended set of “independent” variables, “dependent” variables, and regression coefficients defined in Eq. (3a) can be summarized as follows:

$$\begin{aligned} \text{extended set of } \underline{\text{independent}} \text{ variables} &\Longrightarrow \underbrace{F(1), F(2), \dots, F(n), dT}_{(n+1) \text{ variables}} \\ \text{extended set of } \underline{\text{dependent}} \text{ variables} &\Longrightarrow \underbrace{R(1), R(2), \dots, R(n), dT}_{(n+1) \text{ variables}} \\ \text{extended set of regression coefficients} &\Longrightarrow \underbrace{c_0(k), c_1(k), \dots, c_{\mu+2}(k)}_{1 \leq k \leq n} \end{aligned}$$

The extended variable and coefficient sets above can be used to construct a least squares fit that defines a data reduction matrix for the temperature–dependent balance calibration data set. This matrix supplies the coefficients for the load iteration equation that the *Iterative Method* uses for the prediction of balance

loads (see again Ref. [5] for more details). The load iteration equation has the following general format (from Ref. [1], p. 19, Eq. (3.3.7)):

$$\mathbf{F}_\xi = \underbrace{\begin{bmatrix} \mathbf{C}_1^{-1} \end{bmatrix}}_{\text{matrix}} \cdot \Delta \mathbf{R} - \underbrace{\begin{bmatrix} \mathbf{C}_1^{-1} \mathbf{C}_2 \end{bmatrix}}_{\text{matrix}} \cdot \mathbf{H}(\mathbf{F}_{\xi-1}) \quad (4)$$

where vector \mathbf{F} of the “independent” variable set is defined as

$$\mathbf{F}_{(n+1) \times 1} = \begin{bmatrix} F(1) \\ F(2) \\ \vdots \\ F(n) \\ dT \end{bmatrix} \quad (5a)$$

and vector $\Delta \mathbf{R}$ of the “dependent” variable set is defined as

$$\Delta \mathbf{R}_{(n+1) \times 1} = \begin{bmatrix} R(1) - c_0(1) \\ R(2) - c_0(2) \\ \vdots \\ R(n) - c_0(n) \\ dT \end{bmatrix} \quad (5b)$$

and matrices \mathbf{C}_1^{-1} and $\mathbf{C}_1^{-1} \mathbf{C}_2$ have the coefficients of the data reduction matrix that results from the fit of the balance calibration data. The symbol $\mathbf{H}(\mathbf{F}_{\xi-1})$ represents a rectangular matrix that only depends on load estimates of the previous iteration step (see Ref. [1], p. 18, for a detailed definition of the matrix).

A simulation of a temperature-dependent calibration data set of a five-component semi-span balance is used in the next section of the paper to illustrate the improved approach to include temperature effects in the prediction of loads of a strain-gage balance.

III. Discussion of Example

Recent calibration data of NASA’s ARC-30K five-component semi-span balance was selected to illustrate the improved approach to include temperature effects in the load prediction equations used by the *Iterative Method*. The ARC-30K balance was calibrated at Triumph Aerospace (Force Measurement Systems) in 2013 and commissioned for use in the wind tunnel in the fall of 2014 (see Ref. [7] for additional details associated with the calibration of the ARC-30K). Figures 1a and 1b show the balance during manufacturing and after installation in the test section floor of the Ames 11ft Transonic Wind Tunnel. Table 1 below summarizes important features of the balance and the calibration data set that was used for the present study.

Table 1: Balance and calibration data set characteristics of the ARC-30K balance.

CHARACTERISTIC	DESCRIPTION
BALANCE TYPE	5-component semi-span balance
DIMENSIONS	diameter = 15.0 inches (metric flange) ; height = 18 inches
CALIBRATION DATE AND PLACE	June/July 2013 at Triumph Aerospace
CALIBRATION HARDWARE	Triumph Aerospace’s Large Load Rig (LLR)
NUMBER OF ORIGINAL DATA POINTS	1459
CALIBRATION TEMPERATURE	70 degF

The ARC-30K balance was sized so that it is suitable for semi-span model testing of a commercial transport aircraft in the Ames 11ft Transonic Wind Tunnel. Table 2 below lists load capacities of the balance:

Table 2: Load capacities of the ARC-30K balance.

	NF, lbs	PM, in-lbs	YM, in-lbs	RM, in-lbs	AF, lbs
CAPACITY	30,000	300,000	150,000	1,300,000	3000

The balance was originally calibrated using Triumph’s Large Load Rig (LLR). The LLR is capable of loading the balance to capacity. In addition, the LLR can also apply complex load combinations that a semi-span model is expected to experience during a wind tunnel test.

During the calibration of the ARC-30K a total of 1459 data points were recorded at a single constant temperature of approximately 70 *degF*. In other words – no data was collected that could be used to model temperature effects on the gage outputs. Therefore, an assumed temperature dependency of the gage outputs had to be simulated using the original calibration data so that elements of the improved approach of including temperature effects in regression models of gage outputs could be tested. Table 3 below summarizes hypothetical relationships that were chosen to model the temperature-dependency of the five balance gages.

Table 3: Assumed temperature-dependency of the ARC-30K’s gage outputs.

GAGE OUTPUT	ASSUMED TEMPERATURE DEPENDENCY ($T_o = 70 \text{ degF}$)
$rNF, \text{ microV/V}$	$rNF(T) = rNF(T_o) + 1.0 \cdot (T - T_o) + 0.010 \cdot (T - T_o)^2$
$rPM, \text{ microV/V}$	$rPM(T) = rPM(T_o) + 1.1 \cdot (T - T_o) + 0.009 \cdot (T - T_o)^2$
$rYM, \text{ microV/V}$	$rYM(T) = rYM(T_o) + 0.9 \cdot (T - T_o) + 0.012 \cdot (T - T_o)^2$
$rRM, \text{ microV/V}$	$rRM(T) = rRM(T_o) + 0.8 \cdot (T - T_o) + 0.009 \cdot (T - T_o)^2$
$rAF, \text{ microV/V}$	$rAF(T) = rAF(T_o) + 0.7 \cdot (T - T_o) + 0.009 \cdot (T - T_o)^2$

The symbols rNF , rPM , rYM , rRM and rAF represent the electrical outputs of the five balance gages. The symbol T identifies the assumed uniform temperature of the balance. The symbol T_o represents the original calibration temperature of 70 *degF*. It is also used as the global reference temperature for the data analysis.

In theory, any temperature set different from the reference temperature of 70 *degF* could be used to illustrate the new approach of including temperature-dependent data in the *Iterative Method*. For simplicity, it was decided to simulate gage outputs at 50 *degF* and 90 *degF* by using the original calibration data at 70 *degF* as a baseline. The resulting total calibration data set, i.e., the set consisting of original plus simulated data, would be capable of supporting both first and second order temperature-dependent terms in the regression models of the gage outputs. Therefore, the total calibration data set consisted of 4377 data points, i.e., 1459 original data points plus 2918 simulated data points. Figure 2 shows parts of the contents of a calibration data input file that has both the original and simulated calibration data.

An analysis of the 4377-point calibration data set was performed using NASA’s BALFIT regression analysis tool (see Refs. [8] and [9] for details about BALFIT). The *Iterative Method* was chosen for both regression analysis and load prediction. The corresponding extended set of “dependent” variables, “independent” variables, and regression coefficients can be summarized as follows:

$$\text{extended set of six } \underline{\text{dependent}} \text{ variables} \implies rNF, rPM, rRM, rYM, rAF, dT$$

$$\text{extended set of six } \underline{\text{independent}} \text{ variables} \implies NF, PM, RM, YM, AF, dTi$$

where

$$dT = dTi = T - T_o ; T_o = 70 \text{ degF} \quad (6)$$

The ARC-30K is a highly linear single-piece balance design. Therefore, no absolute value terms of the load components were included in the regression models of the five gage outputs. BALFIT’s regression model search process was applied to the data in order to prevent “over-fitting” of the gage outputs. The resulting “optimized” regression models of the five gage outputs are depicted in column format in Fig. 3 (individual regression model terms are identified at the beginning of each row; all chosen regression model terms are marked using black rectangles).

It can clearly be seen in Fig. 3 that the temperature difference is being used as both a “dependent” and “independent” variable as the regression model of the “dependent” variable dT only uses the single term dTi (the symbol dTi indicates the use of dT as an “independent” variable). In addition, BALFIT’s automated regression model term selection process correctly deduced from the temperature-dependent calibration data that both dTi and $(dT_i)^2$ are “significant” for all five gages. This result is expected as the assumed temperature dependencies defined in Table 3 are “hidden” in the simulated gage outputs of the calibration data.

Figure 4 lists all regression coefficients that were computed as a result of the least squares fit of the simulated calibration data. The fitted coefficients of terms dTi and $(dT_i)^2$ are marked using red boxes. Table 4 below compares “fitted” coefficients of the terms dTi and $(dT_i)^2$ with corresponding “exact” values.

Table 4: Comparison of the regression coefficients of dTi and $(dT_i)^2$.

TERM	FITTED/EXACT	r_{NF}	r_{PM}	r_{YM}	r_{RM}	r_{AF}
dTi	exact (from Table 3)	1.00000	1.10000	0.90000	0.80000	0.70000
	fitted (from Fig. 4)	1.00000	1.10000	0.90000	0.80000	0.70000
$(dT_i)^2$	exact (from Table 3)	0.01000	0.00900	0.01200	0.00900	0.00900
	fitted (from Fig. 4)	0.00999	0.00879	0.01205	0.00903	0.00894

The comparison of the fitted and exact coefficient values of the term dTi is perfect. In addition, the comparison of the fitted and exact coefficient values of the term $(dT_i)^2$ is very good. These results indicate that the improved approach of modeling temperature effects on gage outputs of a balance with a uniform temperature distribution is working as intended. The reader has to keep in mind that the simulated data set was obtained from “real-world” calibration data of the balance. Consequently, larger differences between “fitted” and “exact” values of the coefficients of $(dT_i)^2$ can be explained by the fact that the regression models of the gage outputs have picked up data imperfections that are, by design, contained in the simulated data.

Figure 5 shows the final data reduction matrix of the temperature-dependent calibration data. This matrix can be used in combination with the load iteration scheme of the *Iterative Method* (Eq. (4)), the gage outputs, and the temperature difference for the prediction of the balance loads in the wind tunnel.

Figure 6 shows the final load residuals of the total calibration data set that consists of 4377 original and simulated data points. Overall, the performance of the balance is very good considering the fact that the balance calibration data set consisted of a large number of complex combined loadings.

IV. Summary and Conclusions

An improved approach was presented in the paper that may be used to include temperature effects in regression models of strain-gage outputs of a wind tunnel balance. The improved approach introduces the difference between the measured uniform balance temperature and a global reference temperature as a new independent variable for the calibration of the balance. Two new regressors are defined that are exclusively a function of this temperature difference. They are included in an extended regression model of the gage outputs that the *Iterative Method* needs for the prediction of balance loads from measured gage outputs during a wind tunnel test. Simulated temperature-dependent calibration data obtained from Triumph Aerospace’s 2013 calibration of the ARC-30K five-component semi-span balance was successfully used to illustrate key elements of the improved approach.

The improved approach has one key advantage when compared with alternate load prediction approaches that use the *Iterative Method*. It allows for the direct application of the *Iterative Method* by simply introducing

the temperature difference as both an “independent” and “dependent” variable during both calibration data analysis and balance load prediction. Consequently, no “customized” processing equations have to be implemented in the data system of a wind tunnel as a temperature-dependent data reduction matrix can simply be treated like the matrix of a balance that has one additional independent/dependent variable.

V. Acknowledgements

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VI. References

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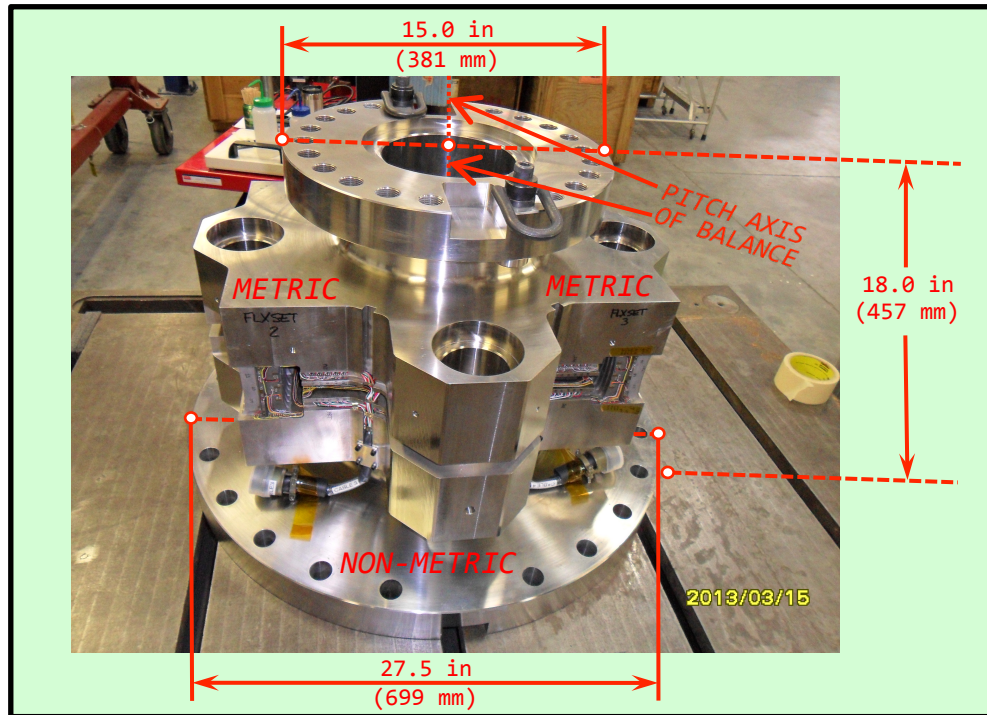


Fig. 1a NASA's ARC-30K 5-component semi-span balance.

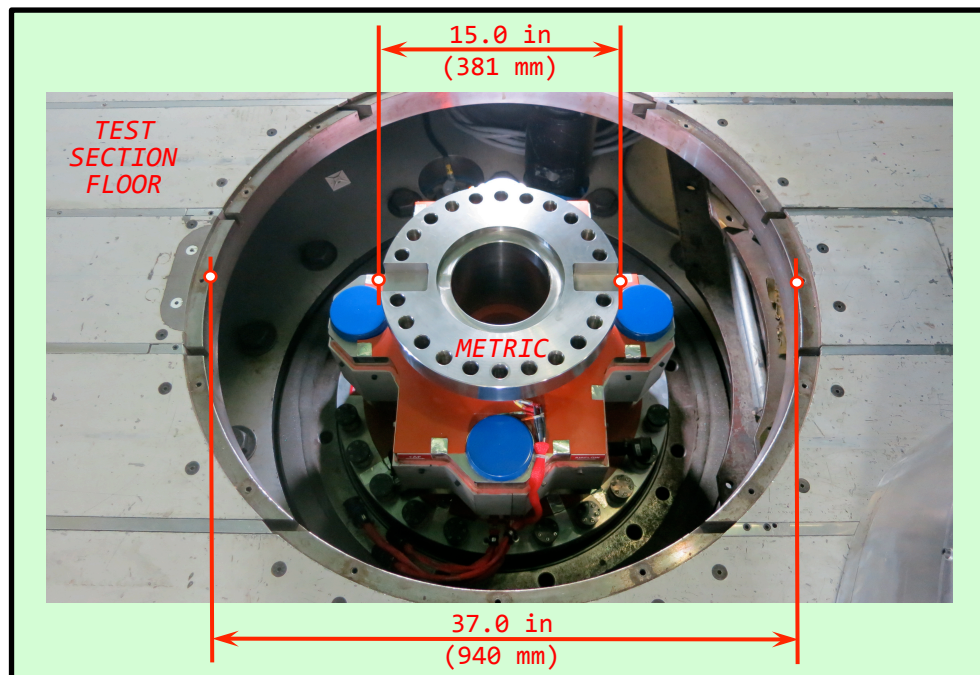


Fig. 1b Installation of the ARC-30K balance in the floor of the Ames 11ft Transonic Wind Tunnel.

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
1																		
2																		
3																		
4																		
5																		
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Fig. 2 Original and simulated calibration data of the ARC-30K balance.

NUMBER OF TERMS = 11, 14, 13, 13, 12, 1

HIERARCHICAL: rNF, rPM, rYM, rRM, rAF, dT

(HIERARCHY ANALYSIS USES $|F*G|=|F|*|G|$, $|F*F*F|=|F|*|F|*|F|$, $|F|*|F|=F*F$)

	rNF	rPM	rYM	rRM	rAF	dT		rNF	rPM	rYM	rRM	rAF	dT
INTERCEPT	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	YM*AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
NF	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	YM*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
PM	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	RM*AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
YM	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	RM*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
RM	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	AF*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
AF	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	NF* PM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
dTi	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	NF* YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
INF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	NF* RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
IPM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	NF* AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
IYM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	NF* dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
IRM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	PM* YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
IAF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	PM* RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
IdTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	PM* AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
NF*NF	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	PM* dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
PM*PM	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	YM* RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
YM*YM	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	YM* AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
RM*RM	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	YM* dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
AF*AF	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	RM* AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
dTi*dTi	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	RM* dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
NF* NF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	AF* dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
PM* PM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	INF *PM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
YM* YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	INF *YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
RM* RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	INF *RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
AF* AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	INF *AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
dTi* dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	INF *dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
NF*PM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IPM *YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
NF*YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IPM *RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
NF*RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IPM *AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
NF*AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IPM *dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
NF*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IYM *RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
PM*YM	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IYM *AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
PM*RM	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	IYM *dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
PM*AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IRM *AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
PM*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IRM *dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
YM*RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IAF *dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
YM*AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	NF*NF*NF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
YM*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	PM*PM*PM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
RM*AF	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	YM*YM*YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
RM*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	RM*RM*RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
AF*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	AF*AF*AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
INF*PM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	dTi*dTi*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
INF*YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	INF*NF*NF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
INF*RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IPM*PM*PM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
INF*AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IYM*YM*YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
INF*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IRM*RM*RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
IPM*YM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IAF*AF*AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
IPM*RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	IdTi*dTi*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
IPM*AF	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>							
IPM*dTi	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>							
IYM*RM	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>							

Fig. 3 Optimized regression models of the gage outputs of the ARC-30K balance.

INDEX	TERM	rNF	rPM	rYM	rRM	rAF	dT
1	INTERCEPT	-9.012208e+01	-1.123363e+02	-6.386578e+01	-4.050774e+01	+3.452281e+01	0
2	NF	+4.040841e-02	+8.873827e-05	+8.466777e-05	-1.923540e-03	-3.674487e-04	0
3	PM	-1.062855e-04	+5.551059e-03	+3.998764e-06	+6.922002e-06	-2.459394e-05	0
4	YM	-5.327869e-06	+2.860829e-06	+3.069503e-03	-1.524219e-06	-1.219140e-05	0
5	RM	+2.372123e-05	-4.395771e-06	+3.671878e-06	+1.058854e-03	-2.666958e-06	0
6	AF	-1.864776e-03	+3.432262e-04	-8.136127e-04	+1.992452e-04	+3.963488e-01	0
7	dTi	+1.000000e+00	+1.100000e+00	+9.000000e-01	+8.000000e-01	+7.000000e-01	+1.000000e+00
8	INF	0	0	0	0	0	0
9	IPM	0	0	0	0	0	0
10	IYM	0	0	0	0	0	0
11	IRM	0	0	0	0	0	0
12	IAF	0	0	0	0	0	0
13	IdTi	0	0	0	0	0	0
14	NF*NF	0	-4.826970e-09	+1.636763e-09	+4.321590e-10	-1.195511e-09	0
15	PM*PM	0	-1.002329e-11	-2.856620e-12	0	+9.197795e-12	0
16	YM*YM	0	-4.679570e-11	0	0	0	0
17	RM*RM	+9.972107e-13	0	-4.587186e-13	+2.488519e-13	0	0
18	AF*AF	0	+8.041729e-08	0	0	0	0
19	dTi*dTi	+9.994229e-03	+8.791125e-03	+1.204632e-02	+9.032056e-03	+8.940470e-03	0
20	NF*INF	0	0	0	0	0	0
21	PM*IPM	0	0	0	0	0	0
22	YM*IYM	0	0	0	0	0	0
23	RM*IRM	0	0	0	0	0	0
24	AF*IAF	0	0	0	0	0	0
25	dTi*IdTi	0	0	0	0	0	0
26	NF*PM	0	0	0	0	0	0
27	NF*YM	0	0	0	0	0	0
28	NF*RM	0	0	0	0	0	0
29	NF*AF	0	0	0	0	0	0
30	NF*dTi	0	0	0	0	0	0
31	PM*YM	+2.035398e-11	0	0	+5.196233e-12	0	0
32	PM*RM	0	+1.670685e-12	+4.786468e-12	+1.122090e-12	+5.630559e-10	0
33	PM*AF	0	0	0	0	0	0
34	PM*dTi	0	0	0	0	0	0
35	YM*RM	0	0	0	0	0	0
36	YM*AF	0	0	0	0	0	0
37	YM*dTi	0	0	0	0	0	0
38	RM*AF	+9.028544e-10	+8.563216e-10	-1.694094e-10	-5.355663e-11	+1.789840e-10	0
39	RM*dTi	0	0	0	0	0	0
40	AF*dTi	0	0	0	0	0	0

Fig. 4 Computed regression coefficients of the gage outputs of the ARC-30K balance.

INDEX	TERM	NF	PM	YM	RM	AF	dTi
1	INTERCEPT	-9.012208e+01	-1.123363e+02	-6.386578e+01	-4.050774e+01	+3.452281e+01	0
----- MATRIX D0 [TRANPOSE(C1INV)] -----							
-	rNF	+2.472099e+01	-3.606828e-01	-7.289978e-01	+4.490572e+01	+2.317580e-02	0
-	rPM	+4.745023e-01	+1.801374e+02	-2.443032e-01	-3.181481e-01	+1.160800e-02	0
-	rYM	+4.265486e-02	-1.687709e-01	+3.257867e+02	+5.456691e-01	+1.005371e-02	0
-	rRM	-5.517033e-01	+7.560966e-01	-1.112764e+00	+9.434077e+02	+5.849231e-03	0
-	rAF	+1.162634e-01	-1.584171e-01	+6.661061e-01	-2.615806e-01	+2.523147e+00	0
-	dTi	-2.492135e+01	-1.981325e+02	-2.917864e+02	-7.995899e+02	-1.815875e+00	+1.000000e+00
----- MATRIX D1 [MATRIX IS NOT USED] -----							
2	NF	0	0	0	0	0	0
3	PM	0	0	0	0	0	0
4	YM	0	0	0	0	0	0
5	RM	0	0	0	0	0	0
6	AF	0	0	0	0	0	0
7	dTi	0	0	0	0	0	0
----- MATRIX D2 [TRANPOSE(C1INVC2)] -----							
8	INF	0	0	0	0	0	0
9	IPM	0	0	0	0	0	0
10	IYM	0	0	0	0	0	0
11	IRM	0	0	0	0	0	0
12	IAF	0	0	0	0	0	0
13	IdTi	0	0	0	0	0	0
14	NF*NF	-2.598010e-09	-8.692779e-07	+5.331378e-07	+4.104436e-07	-3.053497e-09	0
15	PM*PM	-3.808554e-12	-1.806544e-09	-9.220733e-10	-7.758450e-13	+2.306232e-11	0
16	YM*YM	-2.220467e-11	-8.429656e-09	+1.143234e-11	+1.488796e-11	-5.432044e-13	0
17	RM*RM	+2.449517e-11	-9.410233e-14	-1.504483e-10	+2.792989e-10	+1.995492e-14	0
18	AF*AF	+3.815819e-08	+1.448616e-05	-1.964620e-08	-2.558460e-08	+9.334837e-10	0
19	dTi*dTi	+2.478089e-01	+1.583385e+00	+3.911004e+00	+8.971147e+00	+2.306573e-02	0
20	NF*INF	0	0	0	0	0	0
21	PM*IPM	0	0	0	0	0	0
22	YM*IYM	0	0	0	0	0	0
23	RM*IRM	0	0	0	0	0	0
24	AF*IAF	0	0	0	0	0	0
25	dTi*IdTi	0	0	0	0	0	0
26	NF*PM	0	0	0	0	0	0
27	NF*YM	0	0	0	0	0	0
28	NF*RM	0	0	0	0	0	0
29	NF*AF	0	0	0	0	0	0
30	NF*dTi	0	0	0	0	0	0
31	PM*YM	+5.003037e-10	-3.412476e-12	-2.062019e-11	+5.816177e-09	+5.021137e-13	0
32	PM*RM	+6.584066e-11	+2.117957e-10	+1.932766e-09	+9.133842e-10	+1.420747e-09	0
33	PM*AF	0	0	0	0	0	0
34	PM*dTi	0	0	0	0	0	0
35	YM*RM	0	0	0	0	0	0
36	YM*AF	0	0	0	0	0	0
37	YM*dTi	0	0	0	0	0	0
38	RM*AF	+2.276891e-08	+1.538896e-07	-5.587988e-08	-1.039411e-08	+4.804510e-10	0
39	RM*dTi	0	0	0	0	0	0
40	AF*dTi	0	0	0	0	0	0

Fig. 5 Data reduction matrix for the iterative prediction of loads that act on the ARC-30K balance.

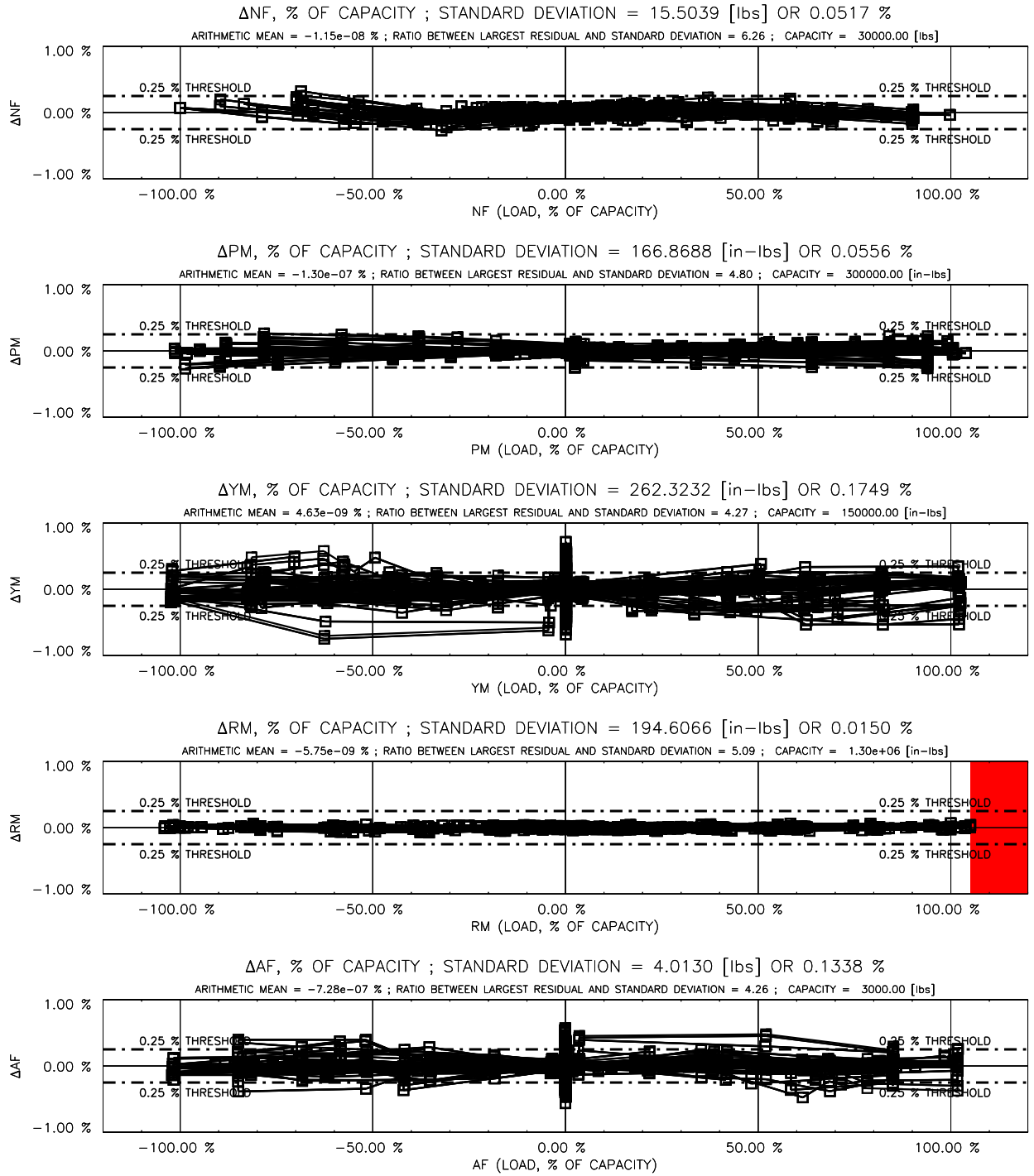


Fig. 6 Load residuals for the simulated temperature-dependent balance calibration data.