



Spatial Sound Mapping via Constrained Spectral Conditioning and CLEAN-SC

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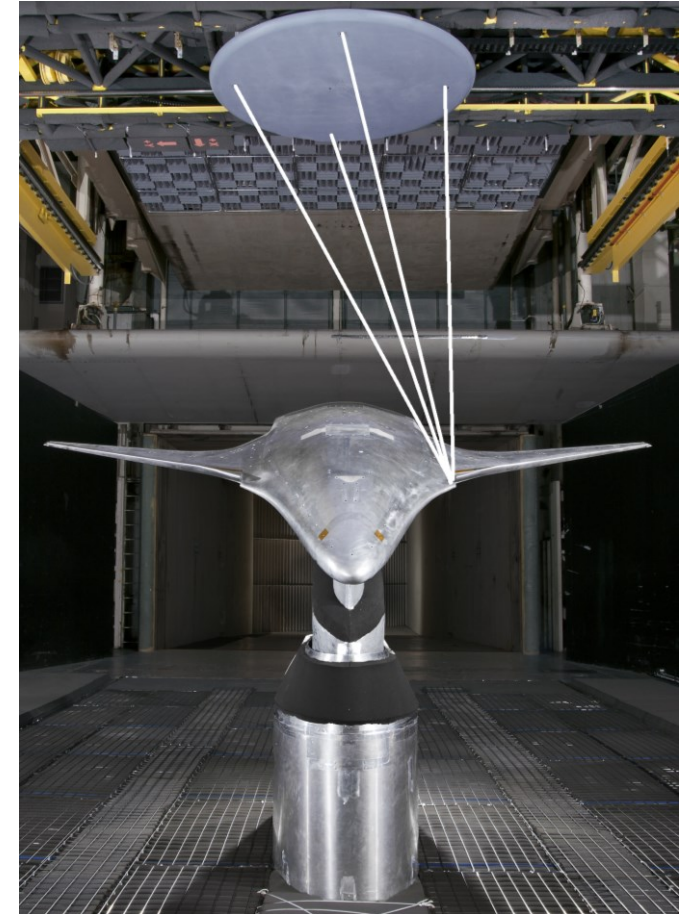
Spring 2015 Acoustics Technical Working Group Meeting

Wednesday, April 22, 2015

NASA LaRC, Hampton, VA

Problem Statement

- Spatially map sound with qualitative/quantitative accuracy
- Microphone arrays allow for spatial separation of distinct sources
- Many existing processing methods



Downstream view of Hybrid Wing Body model inverted on test stand with phased microphone array overhead



Existing Spatial Sound Mapping Methods in Aeroacoustics

- Cross-spectral
 - Beamforming
 - CLEAN-PSF [*Högbom 1974*]
 - Spectral Estimation Method [*Blacodon & Élias 2003*]
 - DAMAS and DAMAS-C [*Brooks & Humphreys 2004, 2006*]
 - CLEAN-SC [*Sijtsma 2007*]
 - Functional Beamforming [*Dougherty 2014*]
- Eigenspace
 - Generalized Inverse [*Suzuki 2008*]
 - Orthogonal Beamforming [*Sarradj 2010*]
- Wavespace
 - Wavespace Deconvolution [*Bahr & Cattafesta 2012*]



Research Objectives

- Use:
 - Single-channel filtering based on user-defined spatial constraints

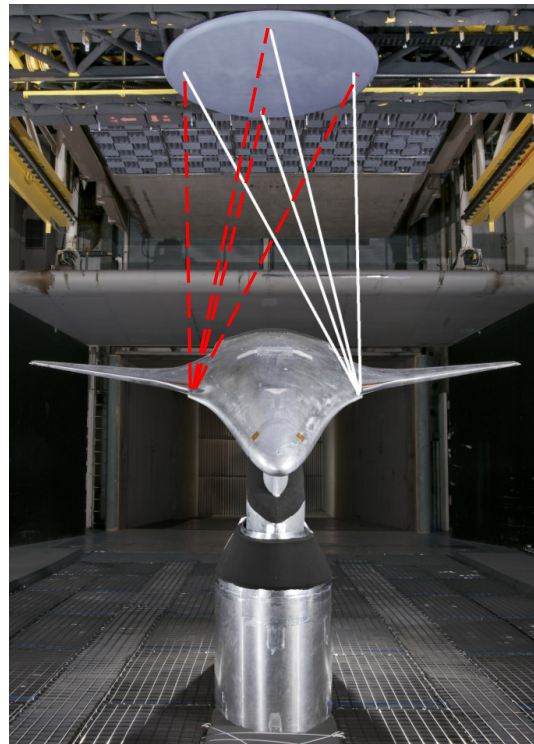
- As:
 - Building-block for existing spatial mapping techniques

- For:
 - Qualitative/quantitative improvement in accuracy

Microphone Array Filtering

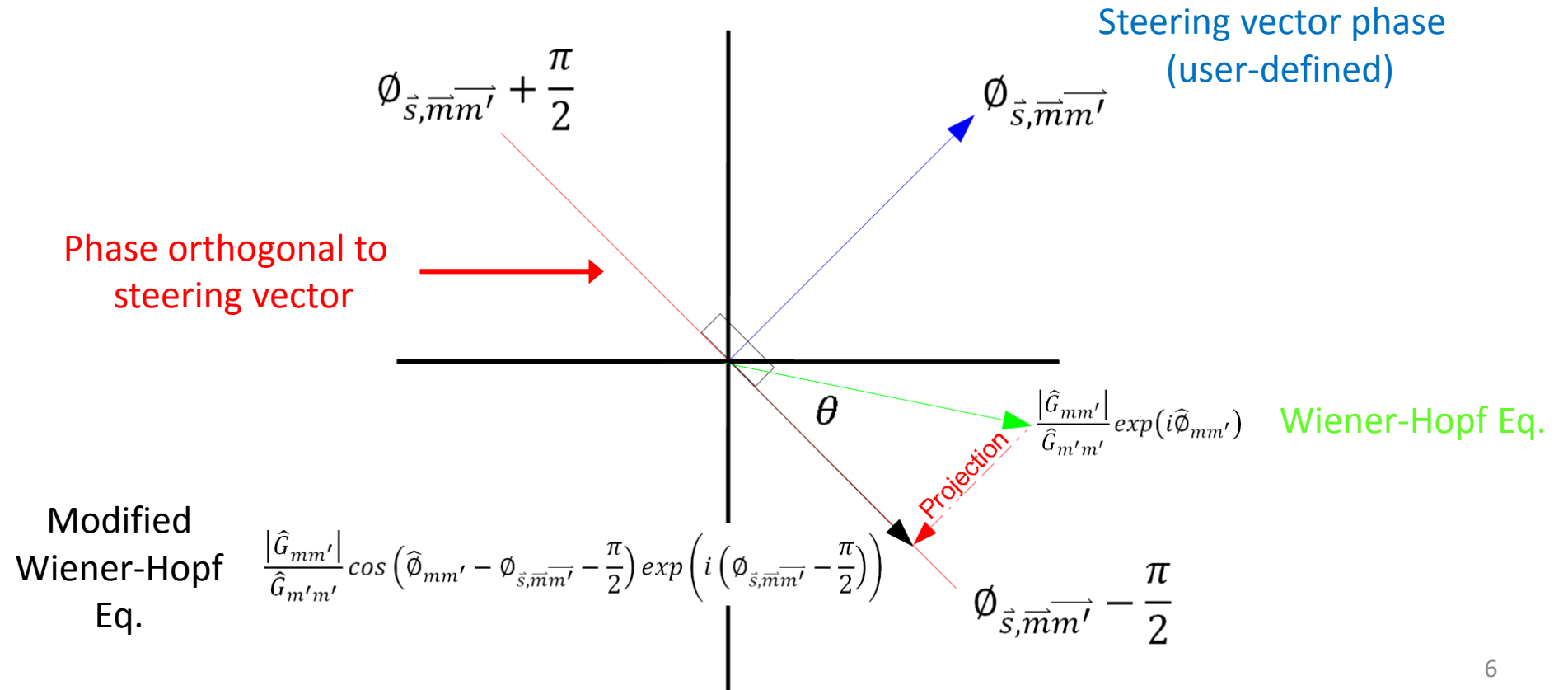
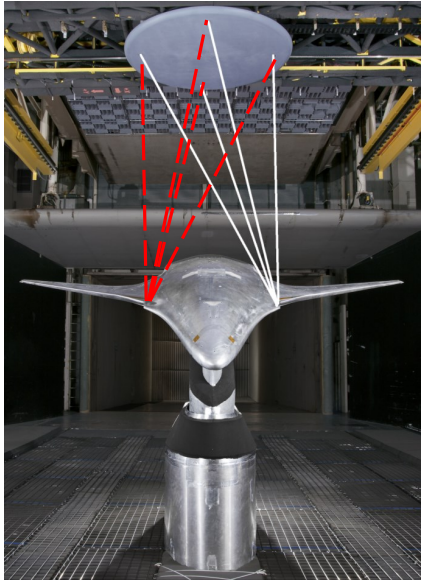
- Goal: Filter channel data for more accurate spatial sound estimation

**Filter dashed-red to
better estimate solid-white**



Modified Wiener-Hopf Eq. for Spatial Filtering

- Combine: Optimal, least-squares filtering of Wiener-Hopf Eq. + Spatial filtering
- Only constraint = User-defined phase
- Modified weight vector → Filters + Prevents targeted signal cancellation



Constrained Spectral Conditioning (CSC)

- Conditioned Spectral Analysis¹ with modified Wiener-Hopf Eq. (WB) becomes CSC²
- Optimal, spatially-constrained, least-squares filtering for Fourier Transforms of microphone outputs

Wiener-Hopf Eq.

$$W = \frac{|\hat{G}_{mm'}|}{\hat{G}_{m'm'}} \exp(i\hat{\Phi}_{mm'})$$

↓

Modified Wiener-Hopf
Eq. via Orthogonal
Projection

$$WB = \frac{|\hat{G}_{mm'}|}{\hat{G}_{m'm'}} \cos\left(\hat{\Phi}_{mm'} - \phi_{\bar{s}, \bar{m}m'} - \frac{\pi}{2}\right) \exp\left(i\left(\phi_{\bar{s}, \bar{m}m'} - \frac{\pi}{2}\right)\right)$$

↓

Constrained
Spectral
Conditioning

$$CH_{m,m'_{removed}} = CH_m - WB[CH_{m'}]$$

Basic Spatial Sound Mapping

Frequency-Domain
Beamforming (FDBF)
(a.k.a. Delay-and-Sum (DAS))

Steering
Vector

$$e_{\vec{s},\vec{m}} = A_{\vec{s},\vec{m}} \exp(i\phi_{\vec{s},\vec{m}})$$

Steering
Vector Matrix

$$e_{\vec{s}} = [e_{\vec{s},1} \quad e_{\vec{s},2} \quad \cdots \quad e_{\vec{s},M}]$$

Cross-Spectral
Matrix (CSM)

$$\hat{G} = \begin{bmatrix} \hat{G}_{11} & \hat{G}_{12} & \cdots & \hat{G}_{1M} \\ \hat{G}_{21} & \ddots & & \vdots \\ \vdots & & \ddots & \vdots \\ \hat{G}_{M1} & \cdots & \cdots & \hat{G}_{MM} \end{bmatrix}$$

FDBF

$$Y_{\vec{s}} = \left(\frac{1}{M^2}\right) e_{\vec{s}}^T \hat{G} e_{\vec{s}}$$

**CSM formed
from CSC
outputs =
"CSC-CSM"**

FDBF via
CSC

FDBF via CSC

$$e_{\vec{s},\vec{m}} = A_{\vec{s},\vec{m}} \exp(i\phi_{\vec{s},\vec{m}})$$

$$e_{\vec{s}} = [e_{\vec{s},1} \quad e_{\vec{s},2} \quad \cdots \quad e_{\vec{s},M}]$$

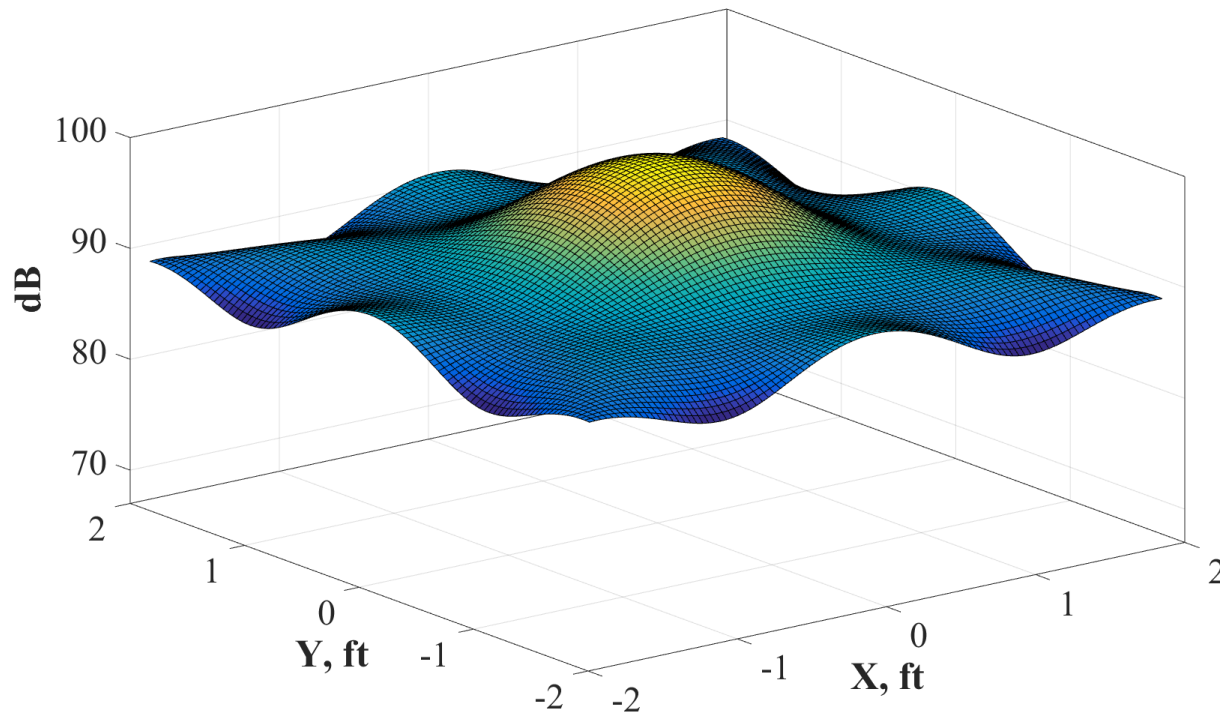
$$\hat{G}_{\vec{s},CSC} = \begin{bmatrix} \hat{G}_{\vec{s},11} & \hat{G}_{\vec{s},12} & \cdots & \hat{G}_{\vec{s},1M} \\ \hat{G}_{\vec{s},21} & \ddots & & \vdots \\ \vdots & & \ddots & \vdots \\ \hat{G}_{\vec{s},M1} & \cdots & \cdots & \hat{G}_{\vec{s},MM} \end{bmatrix}$$

$$Y_{\vec{s},CSC} = \left(\frac{1}{M^2}\right) e_{\vec{s}}^T \hat{G}_{\vec{s},CSC} e_{\vec{s}}$$

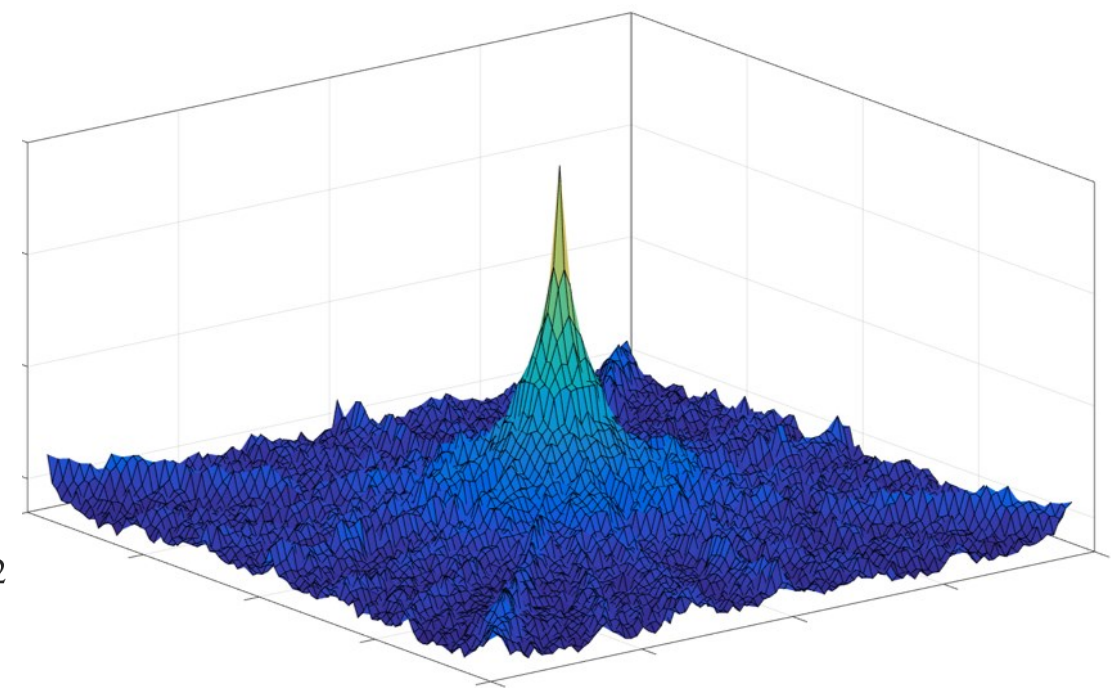
FDBF Beamwidth and Sidelobes: Simulated Point Source

- Point source “measured” with SADA¹: 60” from array face, $f = 10$ kHz, SNR = 20 dB

FDBF via Initial CSM

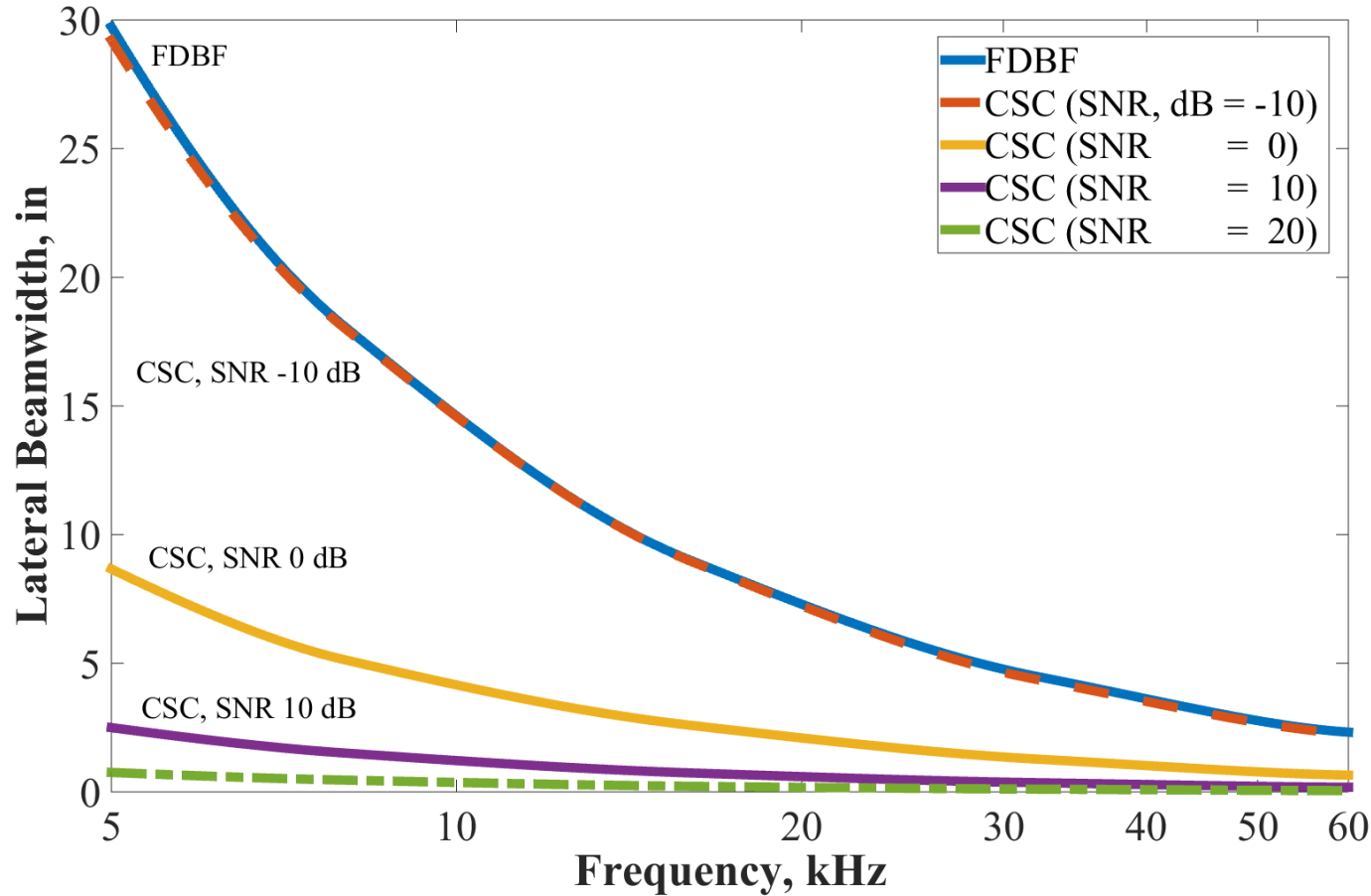


FDBF via CSC-CSM



FDBF Beamwidth & Highest Sidelobe Level vs. Frequency

- CSC performance dependent on SNR & frequency



| SNR, dB | Highest Sidelobe of FDBF via CSC-CSM relative to highest sidelobe of FDBF via initial CSM, dB |
|---------|---|
| -10 | 0 |
| 0 | -5.5 |
| 10 | -12.3 |
| 20 | -19.6 |



CSC Observations

- Constrained Spectral Conditioning (CSC)
 - Single-channel processing → **Building-block for existing algorithms** as it processes the Fourier Transforms of microphone outputs
 - Uses only relative phase differences as constraints
- CSC success dependent on:
 - Frequency
 - Source field
 - Solid angle
 - Microphone layout
 - Signal-to-Noise Ratio (SNR)



CSC Observations, cont.

- CSC output datasets (“CSC-CSMs”) are estimates
- FDBF using CSC-CSMs
 - Non-integratable (due to inaccuracies)
 - Non-linear → Cannot be deconvolved “easily”

➤ ***Modified approach needed for accurate spatial sound mapping***

Advanced Spatial Sound Mapping via CSM Decomposition

- CLEAN-PSF¹

Iterate

$$Y_{\vec{s}}^i = \left(\frac{1}{M^2}\right) e_{\vec{s}}^T \widehat{G}^i e_{\vec{s}}, \quad \vec{s} \in \vec{S}$$

$$\widehat{G}^{i+1} = \widehat{G}^i - \varphi Y_{\vec{s}_{max}}^i \begin{matrix} \text{PSF} \\ \left[e_{\vec{s}_{max}} \ e_{\vec{s}_{max}}^T \right] \end{matrix}$$

Stop if: $\sum |\widehat{G}^i| \geq \sum |\widehat{G}^{i-1}|$

$$Y_{\text{CLEAN-PSF}} = \varphi \sum_{i=1}^I Y_{\vec{s}_{max}}^i$$

FDBF to locate
max location
on map

Subtract CSM
estimate

Iteration stop
criterion

Output
source
map

- Pros
 - Takes advantage of “uncovered” information
- Cons
 - No sidelobe discrimination
 - Relies on the PSF for source propagation model

Advanced Spatial Sound Mapping via CSM Decomposition, cont.

- CLEAN-CSC¹

Iterate

$$Y_{\vec{s}}^i = \left(\frac{1}{M^2}\right) e_{\vec{s}}^T \widehat{G}^i e_{\vec{s}}, \quad \vec{s} \in \vec{S}$$

FDBF to locate max location on map

$$\widehat{G}^{i+1} = \widehat{G}^i - \varphi Y_{\vec{s}_{max,CSC}} \overset{\text{CSC-CSM}}{\boxed{\widehat{G}_{\vec{s}_{max,CSC}}}}$$

Subtract CSM estimate

Stop if: $\sum |\widehat{G}^i| \geq \sum |\widehat{G}^{i-1}|$

Iteration stop criterion

$$Y_{CLEAN-CSC} = \varphi \sum_{i=1}^I Y_{\vec{s}_{max,CSC}}^i$$

Output source map

- Pros

- Higher location/level accuracy than FDBF
- Sidelobe discrimination
- Does not use PSF magnitudes

- Cons

- CSC-CSMs have inaccuracies
- PSF phase still used
- Cannot take advantage of “uncovered” information

Advanced Spatial Sound Mapping via CSM Decomposition, cont.

- CLEAN-SC¹

Iterate

$$Y_{\vec{s}}^i = \left(\frac{1}{M^2}\right) e_{\vec{s}}^T \widehat{G}^i e_{\vec{s}}, \quad \vec{s} \in \vec{S}$$

FDBF to locate max location on map

$$h_{\vec{s}_{max}}^i = \left(\frac{1}{\sqrt{1 + w_{\vec{s}_{max}}^T H^i w_{\vec{s}_{max}}}} \right) \frac{\widehat{G}^i w_{\vec{s}_{max}}}{Y_{\vec{s}_{max}}^i}$$

Form CSM estimate

CLEAN-SC-CSM

$$\widehat{G}^{i+1} = \widehat{G}^i - \varphi Y_{\vec{s}_{max}}^i \begin{bmatrix} h_{\vec{s}_{max}}^i & h_{\vec{s}_{max}}^{iT} \end{bmatrix}$$

Subtract CSM estimate

Iteration stop criterion

$$\text{Stop if: } \sum |\widehat{G}^i| \geq \sum |\widehat{G}^{i-1}|$$

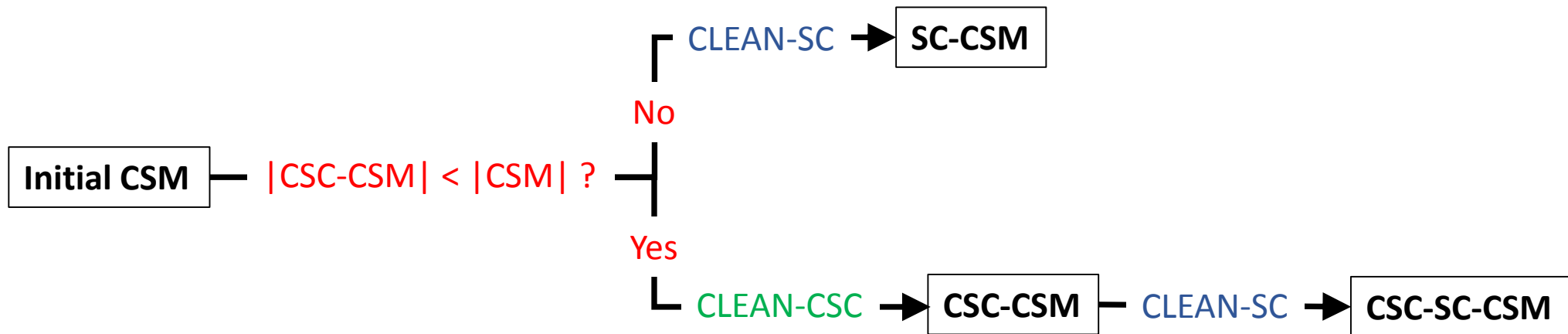
Output source map

$$Y_{CLEAN-SC} = \varphi \sum_{i=1}^I Y_{\vec{s}_{max}}^i$$

- Pros
 - Adaptively defines CSM estimate magnitudes/phases
 - Takes advantage of “uncovered” information
- Cons
 - No sidelobe discrimination
 - Multiple/distributed sources bias CSM estimate
 - Stronger sources bias weaker sources
 - Inaccurate for coherent sources

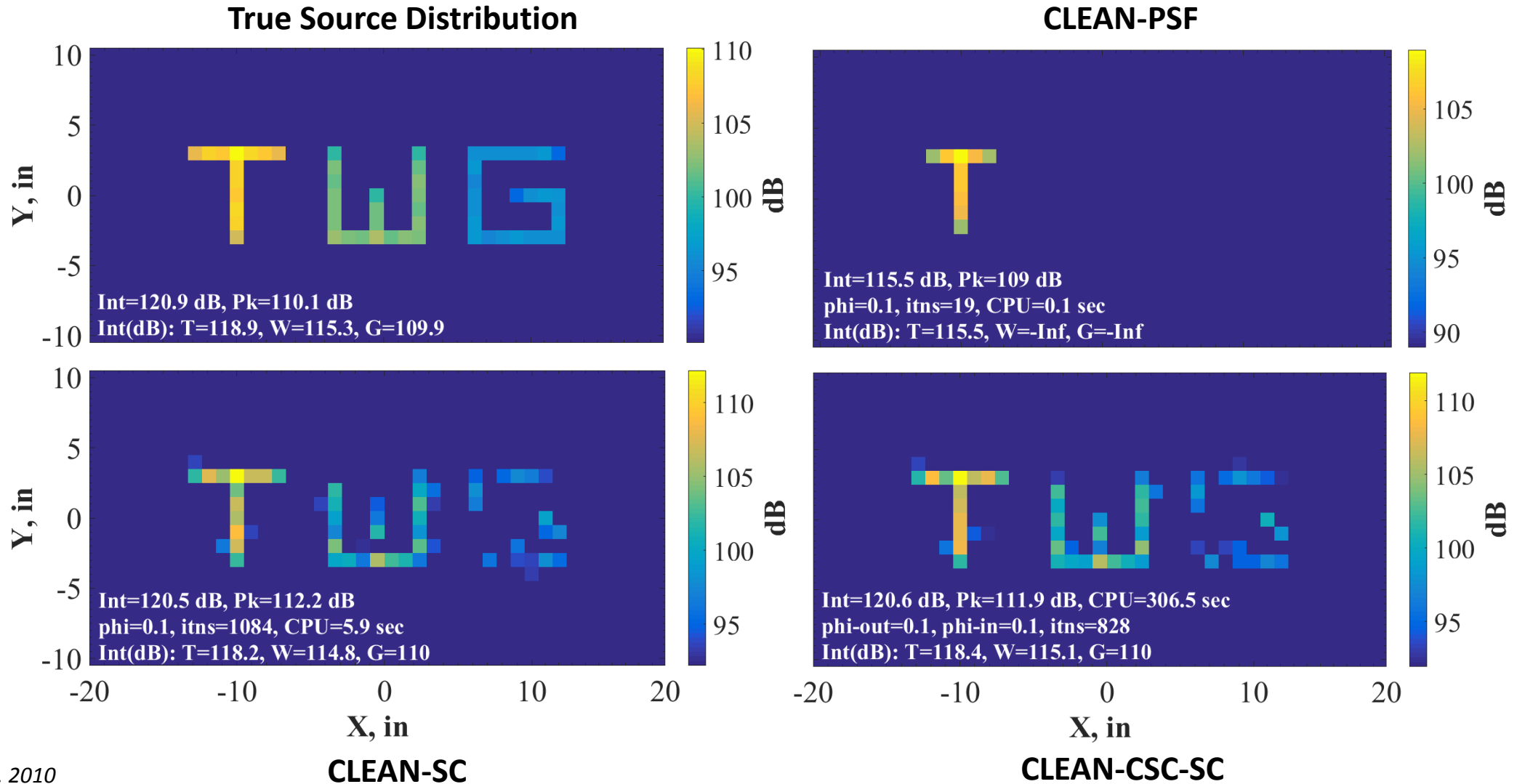
CLEAN-CSC + CLEAN-SC \rightarrow CLEAN-CSC-SC¹

- CSC \rightarrow FDBF and CSM at max locations
- CLEAN-SC \rightarrow Further decompose CSC-CSM \rightarrow CSC-SC-CSM
 - Improves CSC-CSM magnitude estimates
 - Corrects deviations in initial phase definitions
- CLEAN-SC only used once original CSM is sufficiently decomposed
 - Improves dynamic range



Simulation: Modified PSF, Incoherent Sources

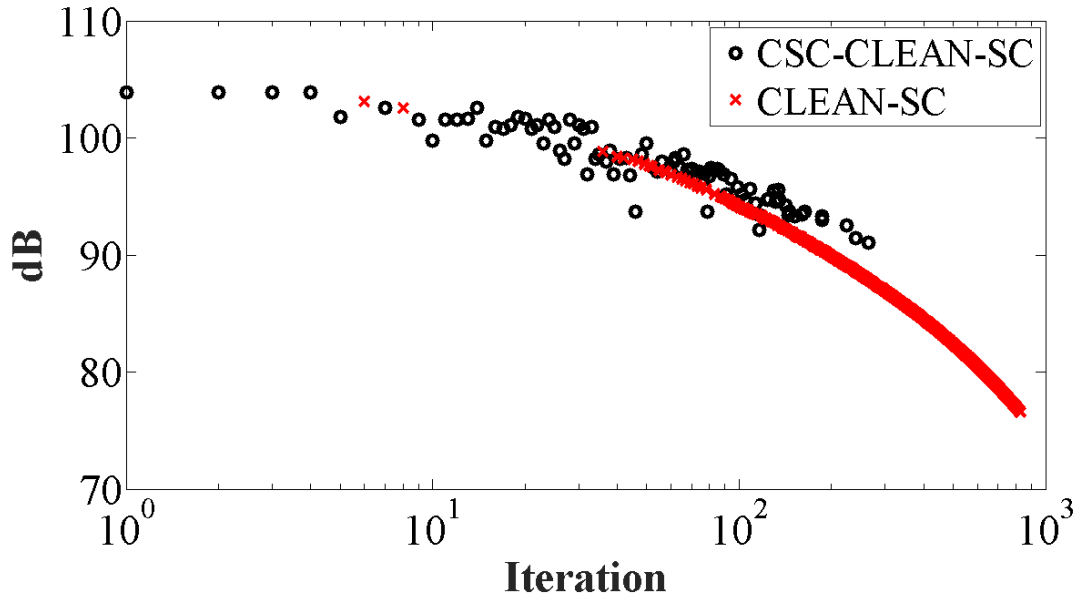
- 467 point sources “measured” with JEDA¹: 72” from array face, $f = 15$ kHz, SNR = 20 dB



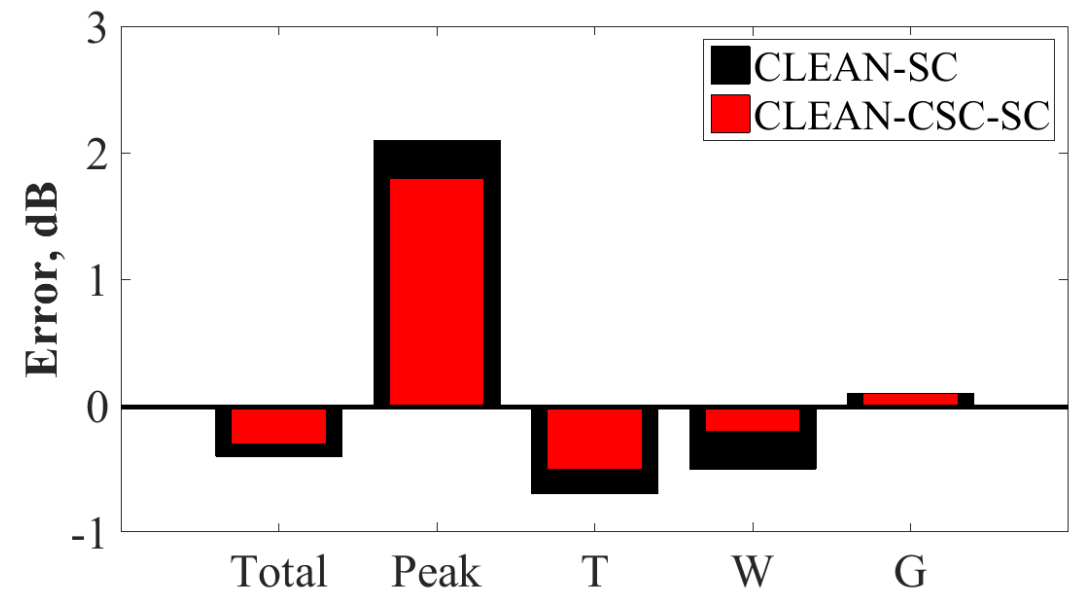
¹Brooks et al. 2010

Simulation: Modified PSF, Incoherent Sources, cont.

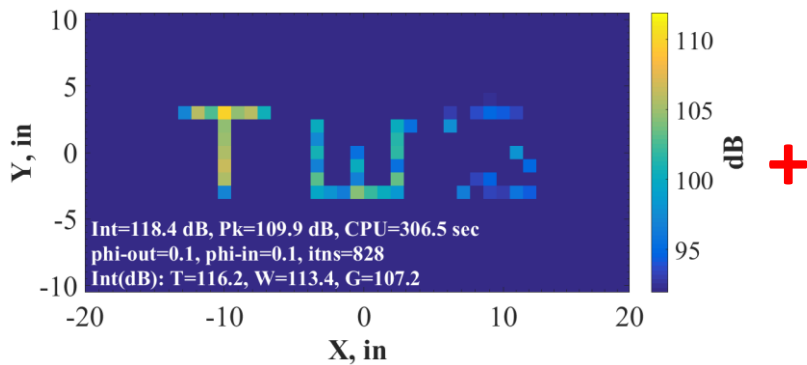
CSM usage during decomposition



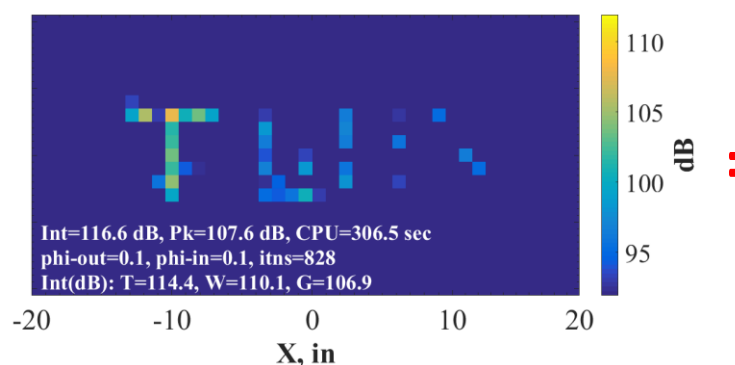
CLEAN-SC vs. CLEAN-CSC-SC



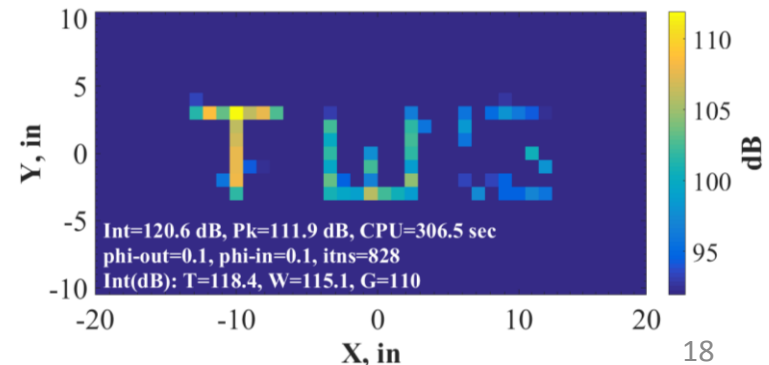
CSM via CSC-CLEAN-SC



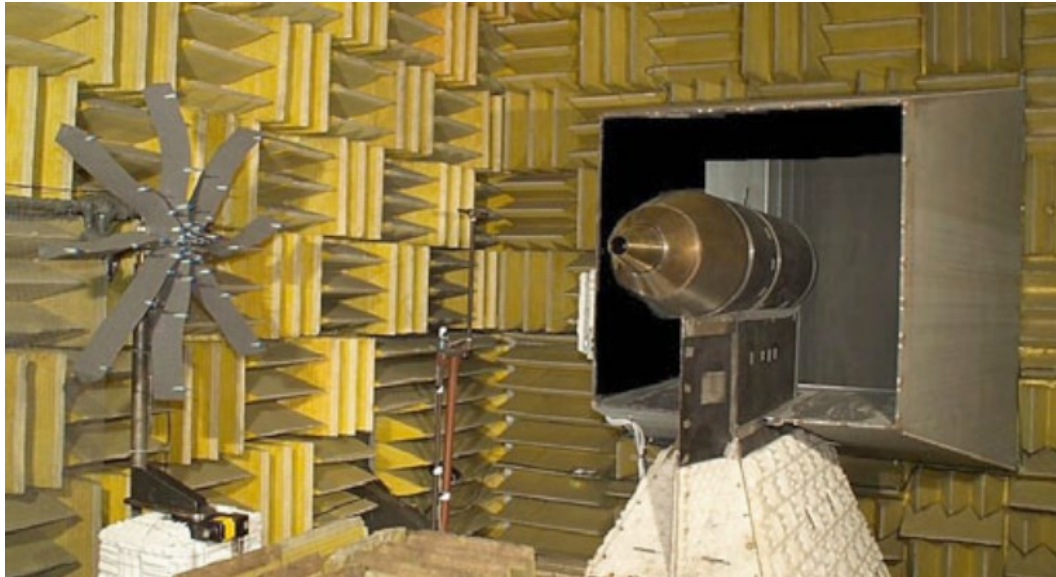
CSM via CLEAN-SC



CLEAN-CSC-SC



Preliminary Jet Noise Results

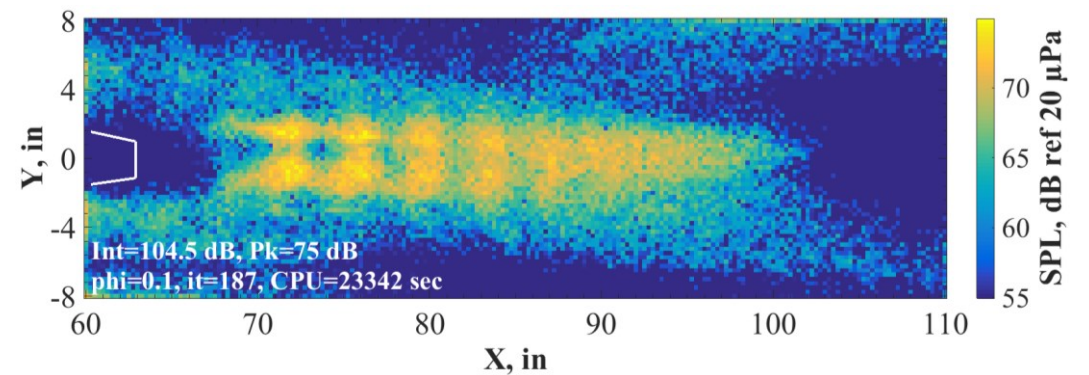
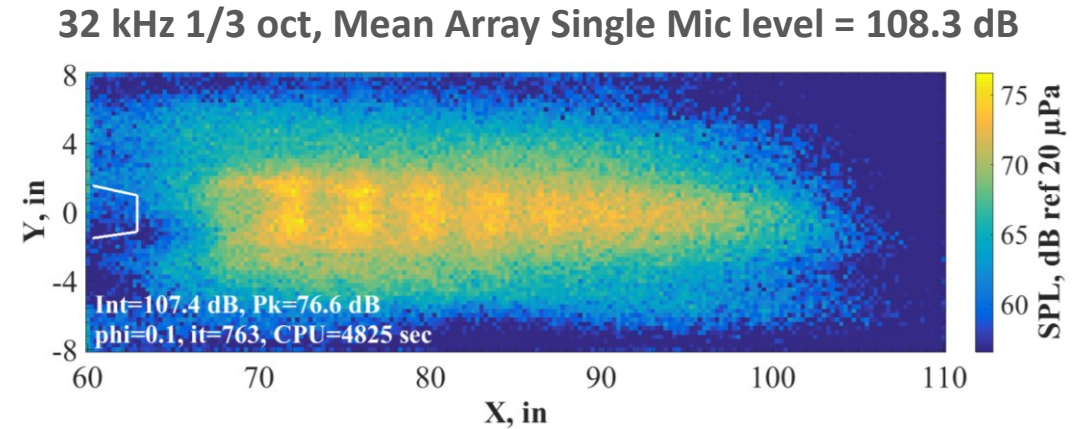
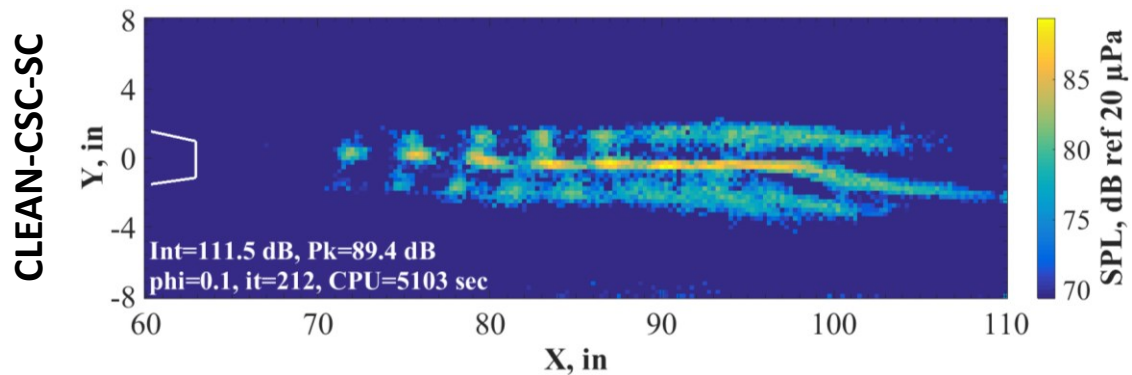
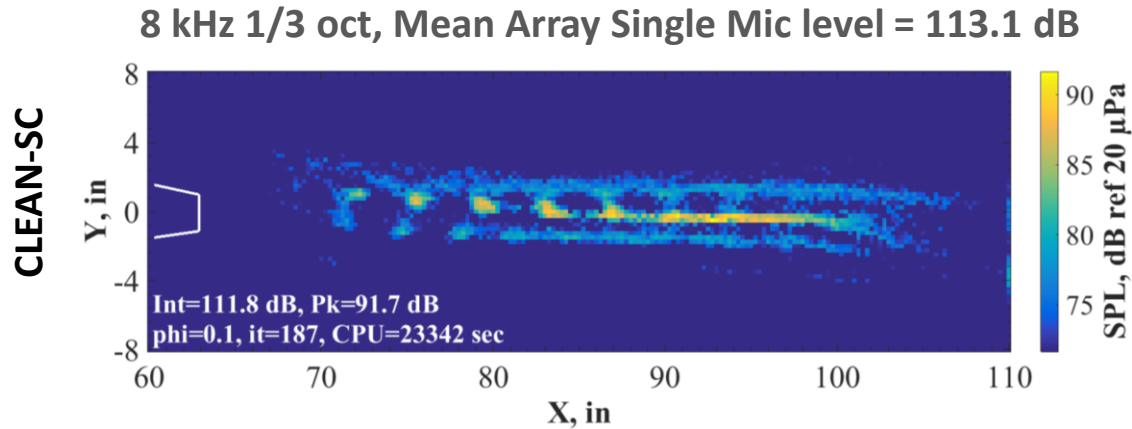


JEDA (left) positioned at 90° with respect to the jet exit plane in the JNL.

- Single-stream, convergent nozzle
- Exit diameter 2.67"
- Supersonic, cold jet at Mach 1.48
- Wind tunnel co-flow at Mach 0.1
- Array ("JEDA") 6 ft from jet centerline

Preliminary Jet Noise Results, cont.

- No CSM Diagonal Removal, No CSM Weighting





CSC Conclusions

- Building block for existing algorithms
- Improves result accuracy under incoherent source conditions
- Not “plug-and-play” for advanced spatial mapping algorithms



CLEAN-CSC-SC Conclusions

- More qualitatively/quantitatively accurate than CLEAN-SC for incoherent sources
- More analysis needed when source coherence exists



Acknowledgements

- This work was funded under:
 - NASA Project # NNLO8AA00B
 - NASA Pathways Program

- This work would not have been possible without the support of:
 - Dr. Chris Fuller
 - Dr. Tom Brooks
 - Dr. Charlotte Whitfield
 - LaRC Aeroacoustics Branch
 - National Institute of Aerospace

Backup Slides



CLEAN-CSC-SC¹

- Spatial sound mapping via decomposition of the initial CSM using CSC² and CLEAN-SC³

$$Y_{\vec{s}}^i = \left(\frac{1}{M^2} \right) e_{\vec{s}}^T \hat{G}^i e_{\vec{s}}, \quad \vec{s} \in \bar{S}$$

$$Y_{\vec{s}_{max}, CSC} = \left(\frac{1}{M^2} \right) e_{\vec{s}_{max}}^T \hat{G}_{\vec{s}_{max}, CSC} e_{\vec{s}_{max}}$$

$$h_{\vec{s}_{max}, CSC-SC} = \left(\frac{1}{\sqrt{1 + w_{\vec{s}_{max}}^T H w_{\vec{s}_{max}}}} \right) \frac{\hat{G}_{\vec{s}_{max}, CSC} w_{\vec{s}_{max}}}{Y_{\vec{s}_{max}, CSC}}$$

$$\hat{G}_{\vec{s}_{max}, CSC-SC} = Y_{\vec{s}_{max}, CSC} [(h_{\vec{s}_{max}, CSC-SC})(h_{\vec{s}_{max}, CSC-SC}^T)]$$

if $|\hat{G}_{\vec{s}_{max}, CSC}| < |\hat{G}^i|$

$$\hat{G}^{i+1} = \hat{G}^i - \varphi \hat{G}_{\vec{s}_{max}, CSC-SC}$$

else

$$\hat{G}^{i+1} = \hat{G}^i - \varphi Y_{\vec{s}_{max}}^i [(h_{\vec{s}_{max}, SC})(h_{\vec{s}_{max}, SC}^T)]$$

Stop if: $\sum |\hat{G}^i| \geq \sum |\hat{G}^{i-1}|$

1. Beamform to locate max grid location
2. Calculate CSC beamform estimate at max location using a CSC-CSM
3. Form normalized steering vectors from CSC beamform and CSC-CSM using CLEAN-SC
4. Calculate CSC-SC-CSM at max location using normalized steering vectors
5. Lower CSM energy is deemed more accurate
6. Update decomposed CSM accordingly
7. Stop if CSM energy increases or remains unchanged

¹Spalt et al. 2015

²Spalt 2014

³Sijtsma 2007



Outline

1. Introduction
2. Research Methodology
3. Simulated Data Analysis
4. Experimental Data Results
5. Contributions
6. Future Work



CSC Extension to Full Array

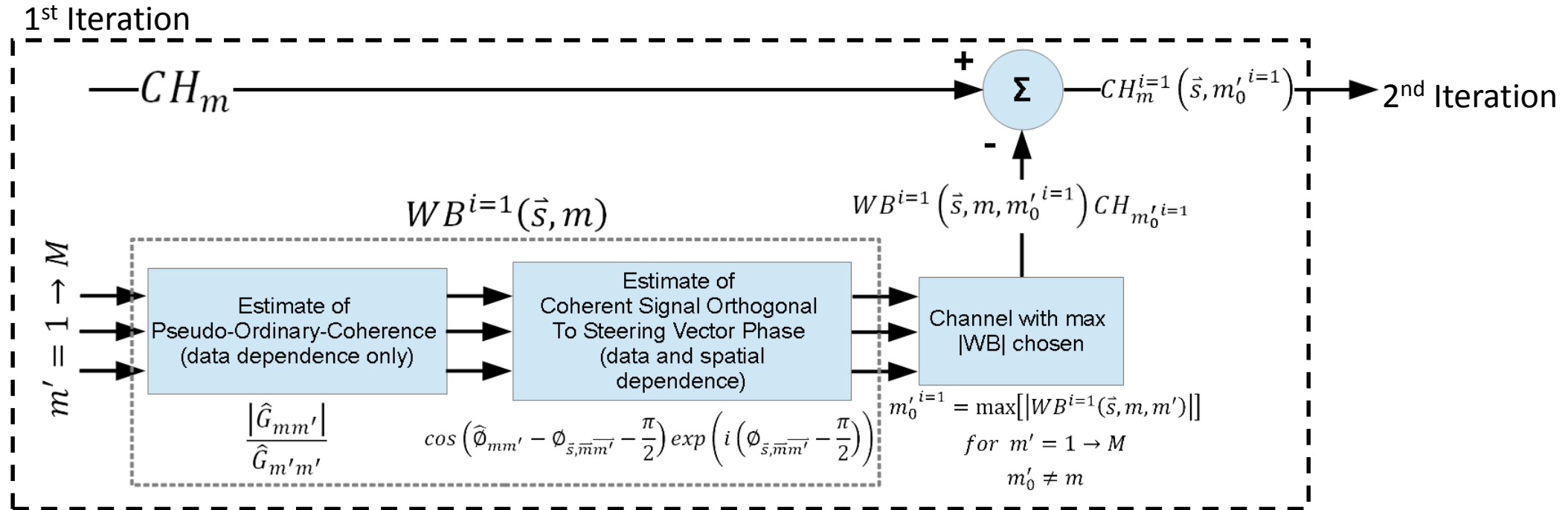
- *Optimum reference channel for use in arrays*:
 1. Maximize undesired signal cancellation
 2. Prevent amplification of noise

$$m'_0(m, \vec{s}) = \underline{\max} |WB| \leq 1$$

$$m' = 1 \rightarrow M$$

$$m' \neq m$$

CSC Iterative Processing Algorithm

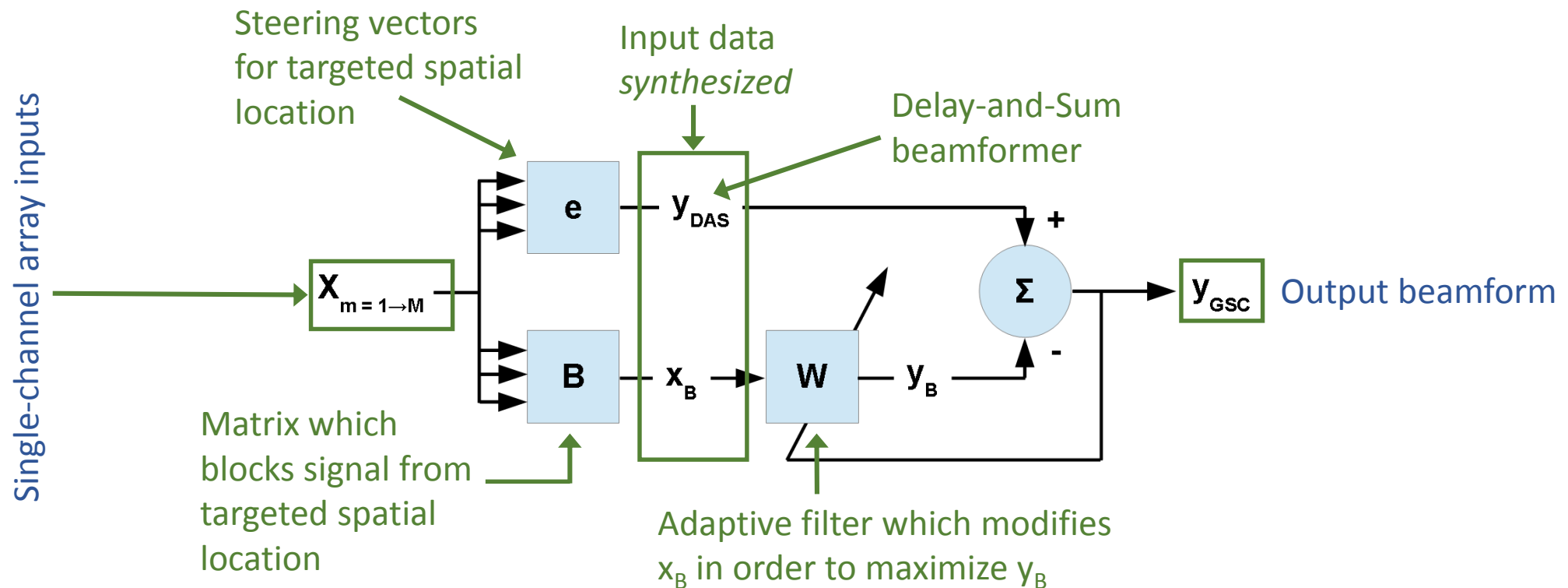


- *Stop if*:

1. Processed channel's magnitude > channel's initial magnitude
2. Coherent signal between channels \leq noise floor between channels

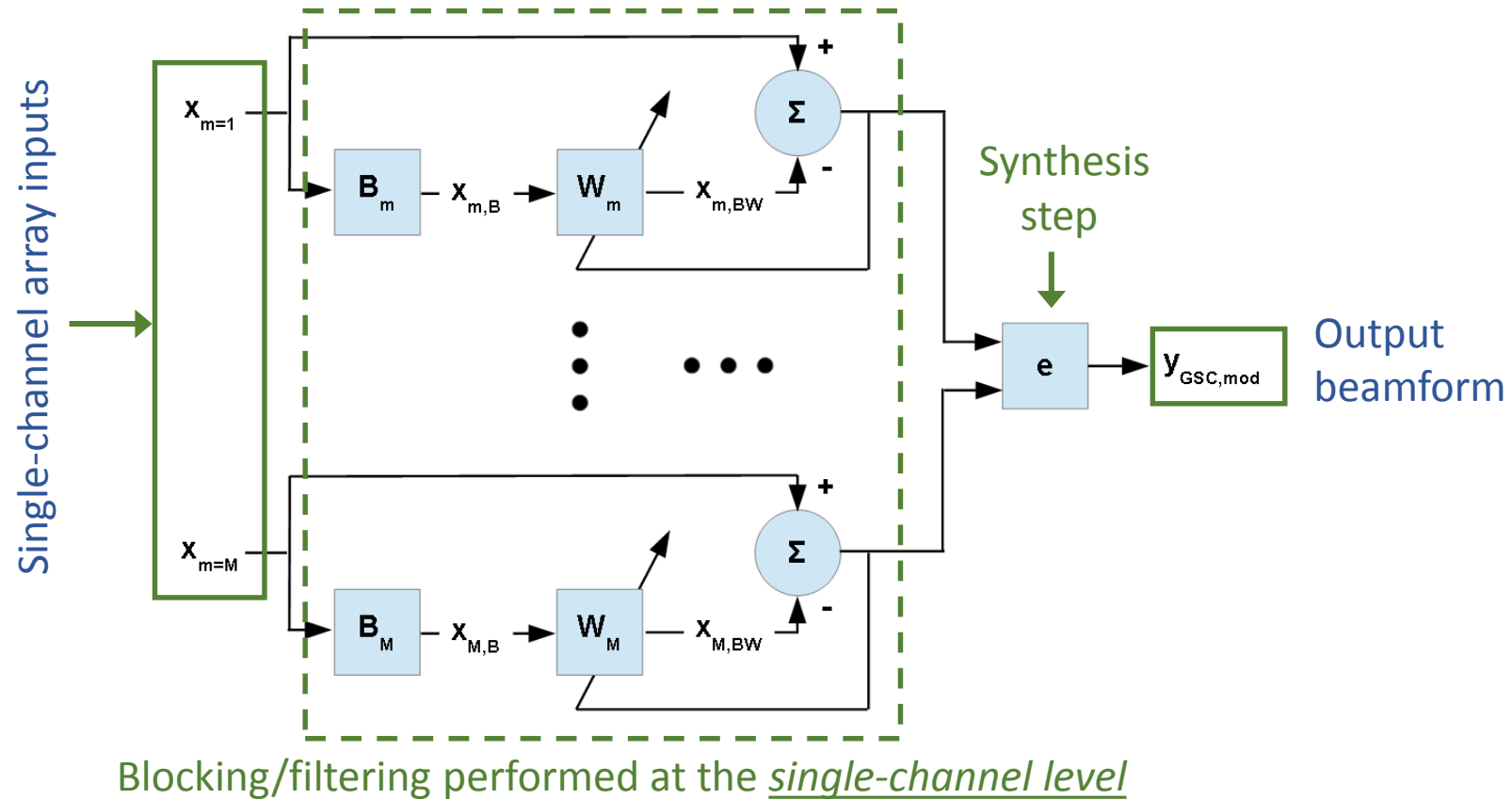
Undesired Signal Cancellation via Spatial Filtering

- Generalized Sidelobe Canceller (GSC)^{1,2}
 - Filtering method designed to attenuate all signal except that from a user-defined point in space/direction
 - Filtering performed on the synthesized array data



Undesired Signal Cancellation via Spatial Filtering, cont.

- Modified GSC¹



¹Liu & Van Veen 1991

“Background Subtraction” for CSC

$$\hat{G}_{mm,background\ sub} = \hat{G}_{mm,source+flow} - \hat{G}_{mm,flow}$$

$$m = 1 \rightarrow M$$

if $\hat{G}_{mm,background\ sub} < 0$

$$\hat{G}_{mm,background\ sub} = \overline{\hat{G}_{mm,source+flow}} \left[\frac{1}{M'} \sum_{m=1}^{M'} (\hat{G}_{mm,background\ sub} > 0) \right]$$

where $\overline{\hat{G}_{mm,source+flow}} = \frac{\hat{G}_{mm,source+flow}}{\frac{1}{M} \sum_{m=1}^M \hat{G}_{mm,source+flow}}$

$$CH_m \rightarrow CH_m \sqrt{\frac{\hat{G}_{mm,background\ sub}}{\hat{G}_{mm,source+flow}}}$$